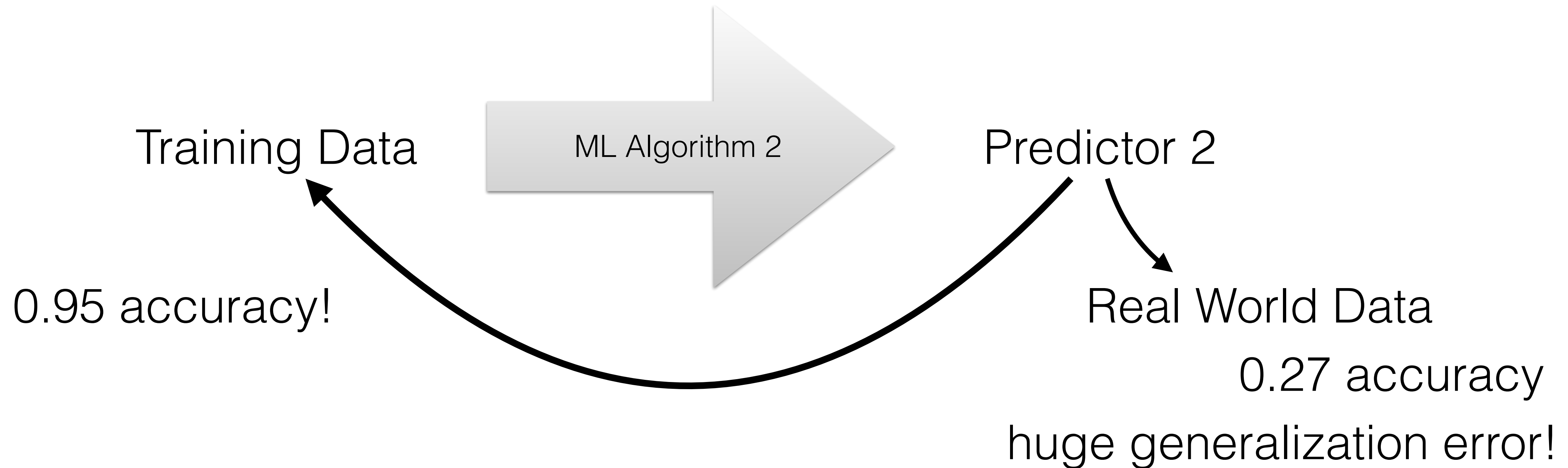
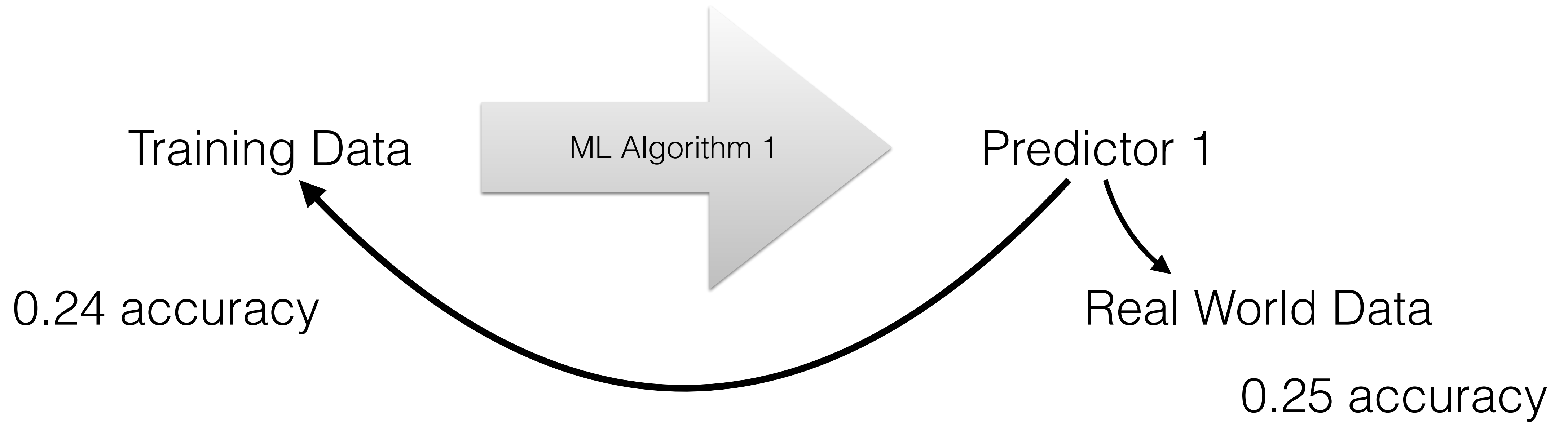


Model Selection

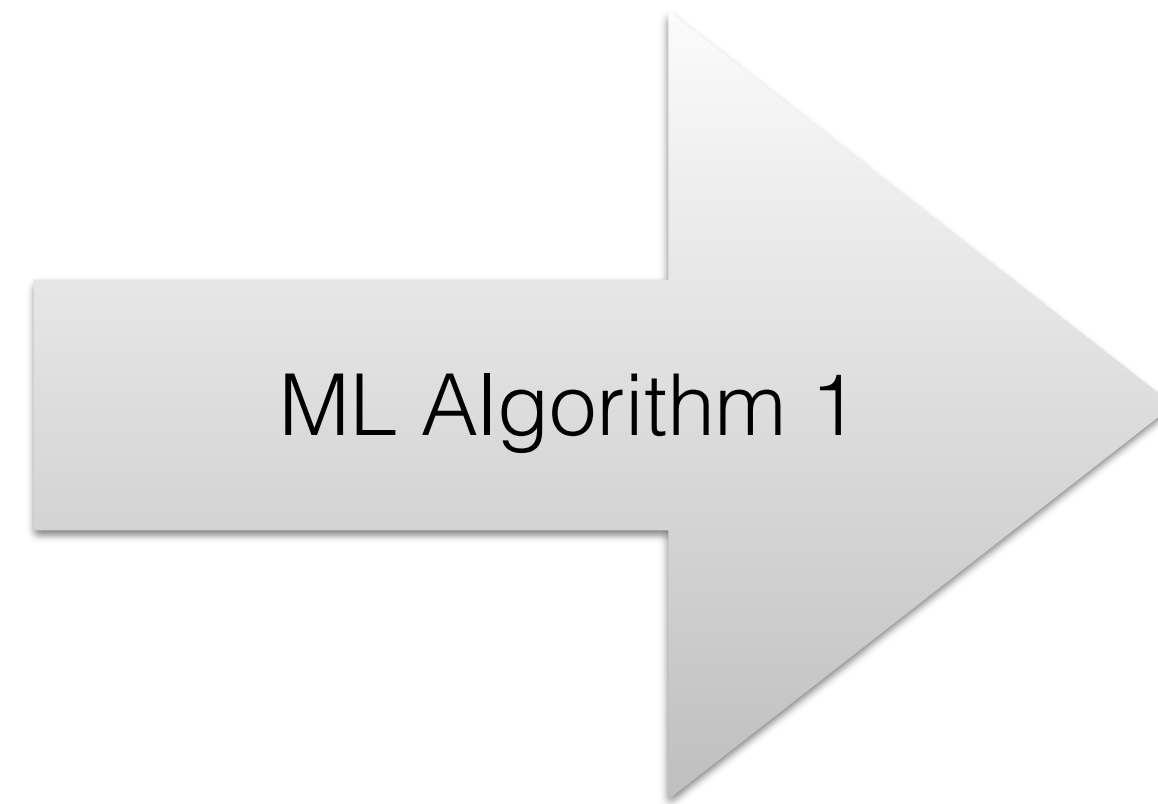
Machine Learning
CSx824/ECEx242
Bert Huang
Virginia Tech

Model Complexity

- Overfitting and underfitting
- Generalization error
- Validation for model selection

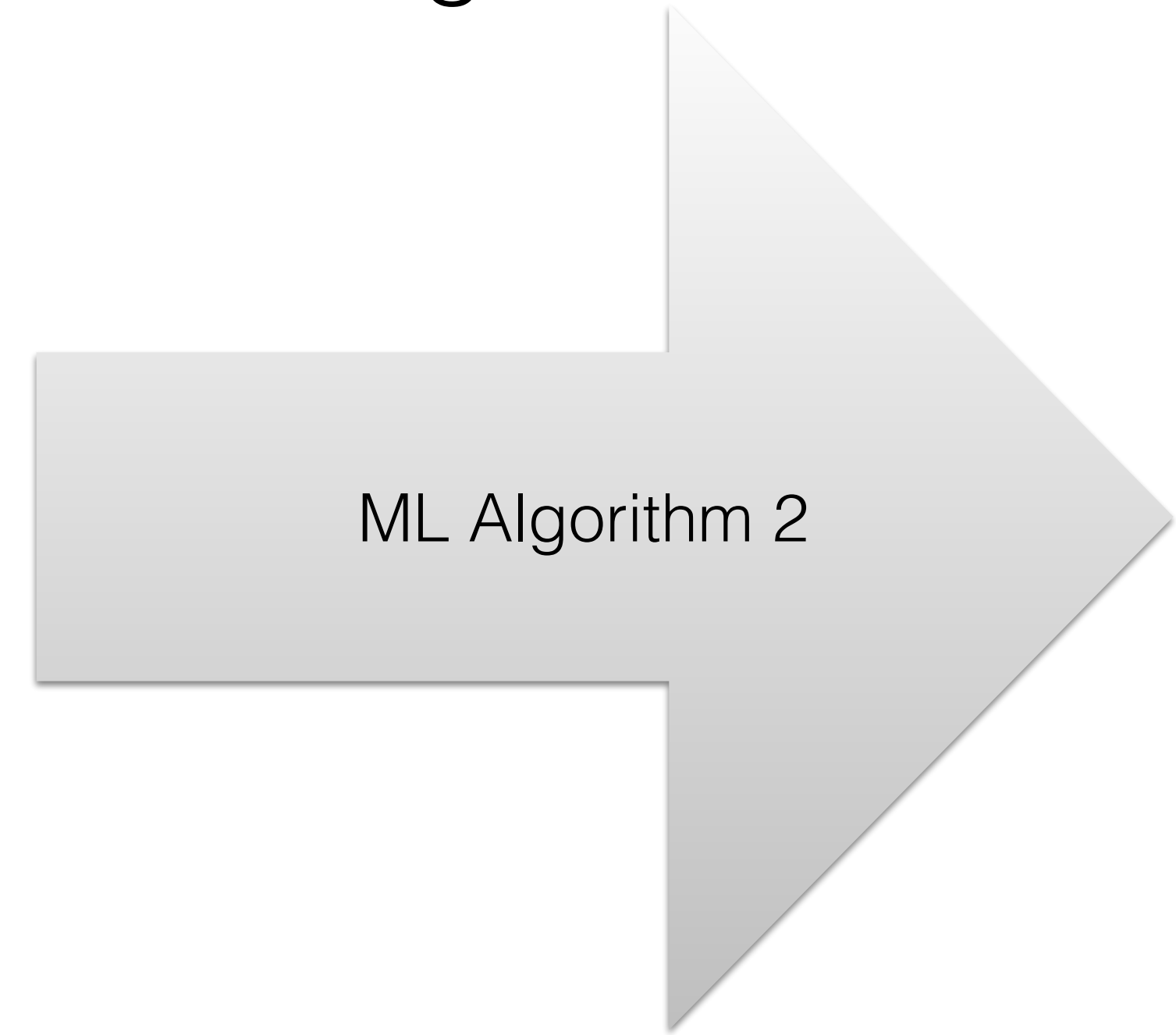


Underfitting

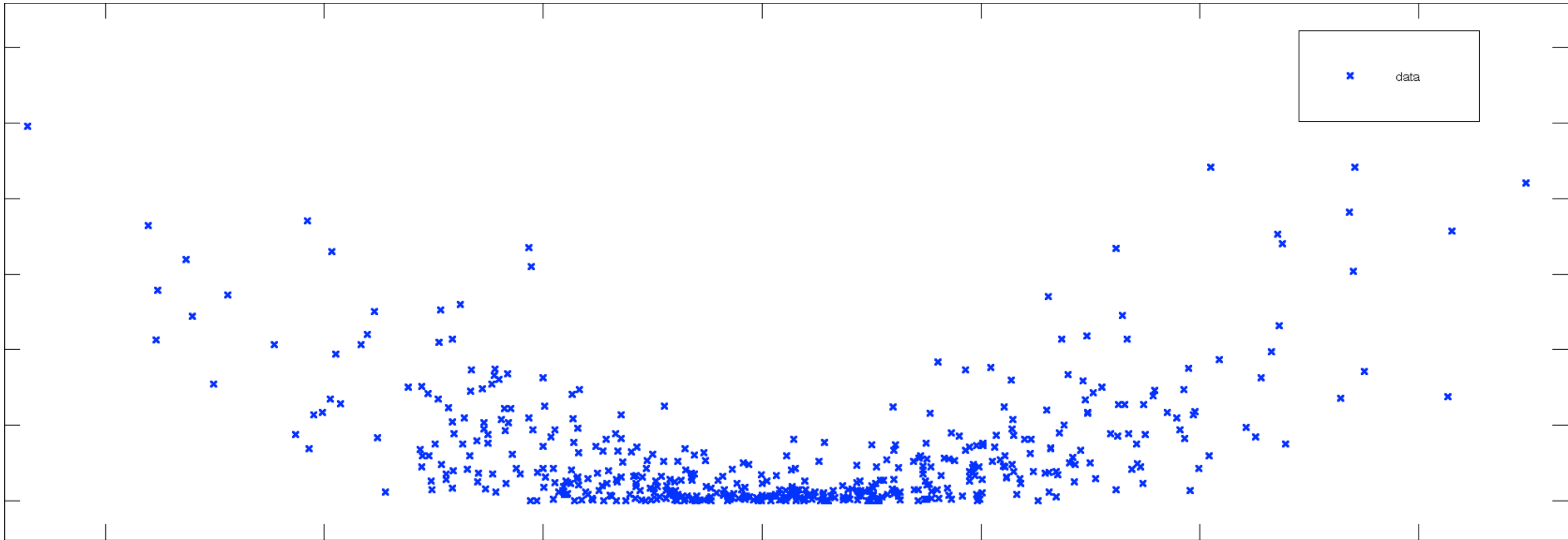


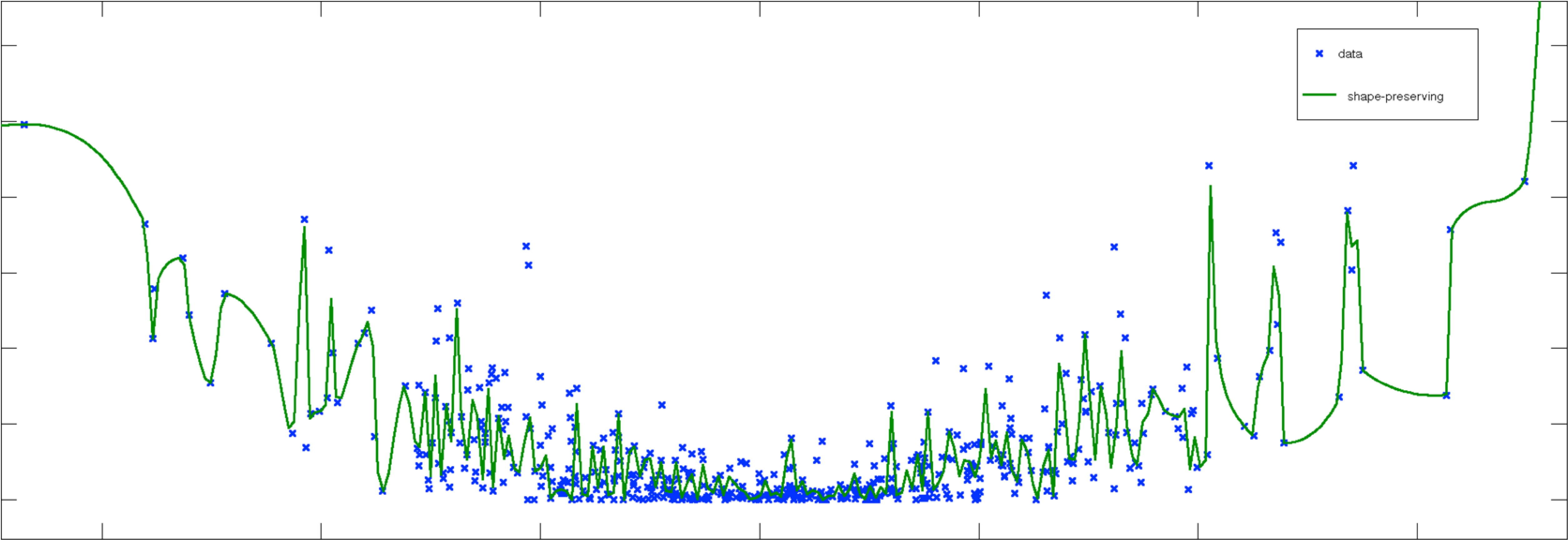
- Low dimensional
- Heavily regularized
- Bad modeling assumptions

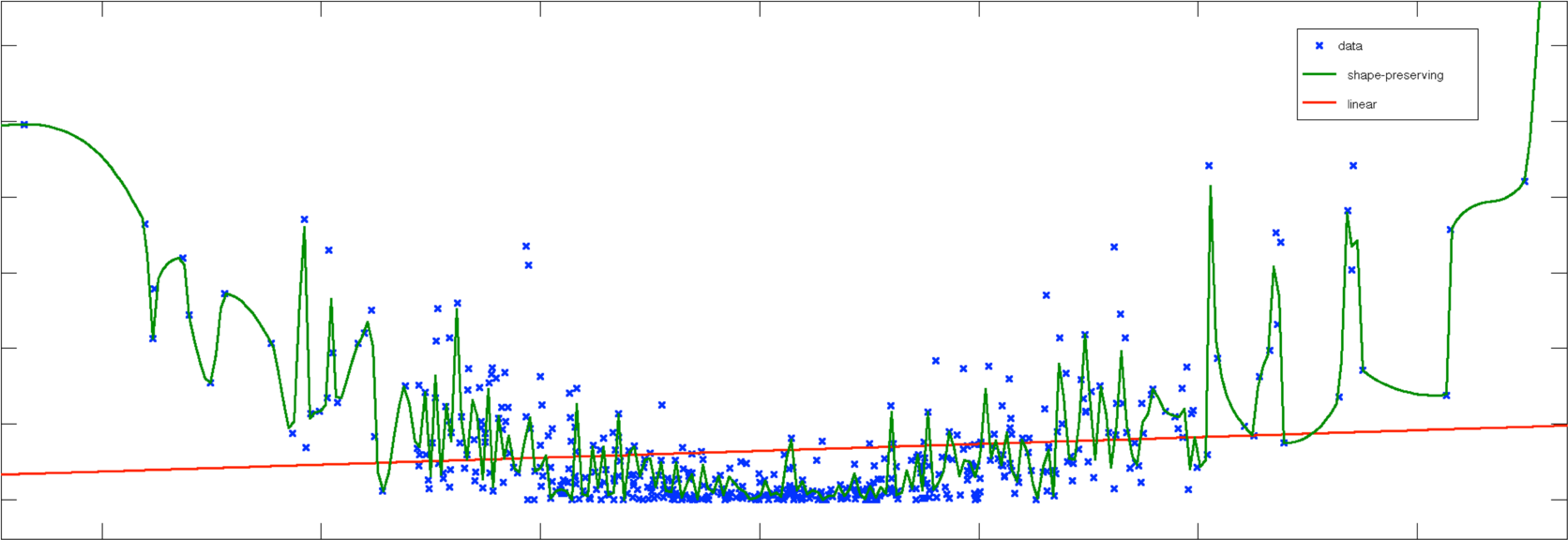
Overfitting

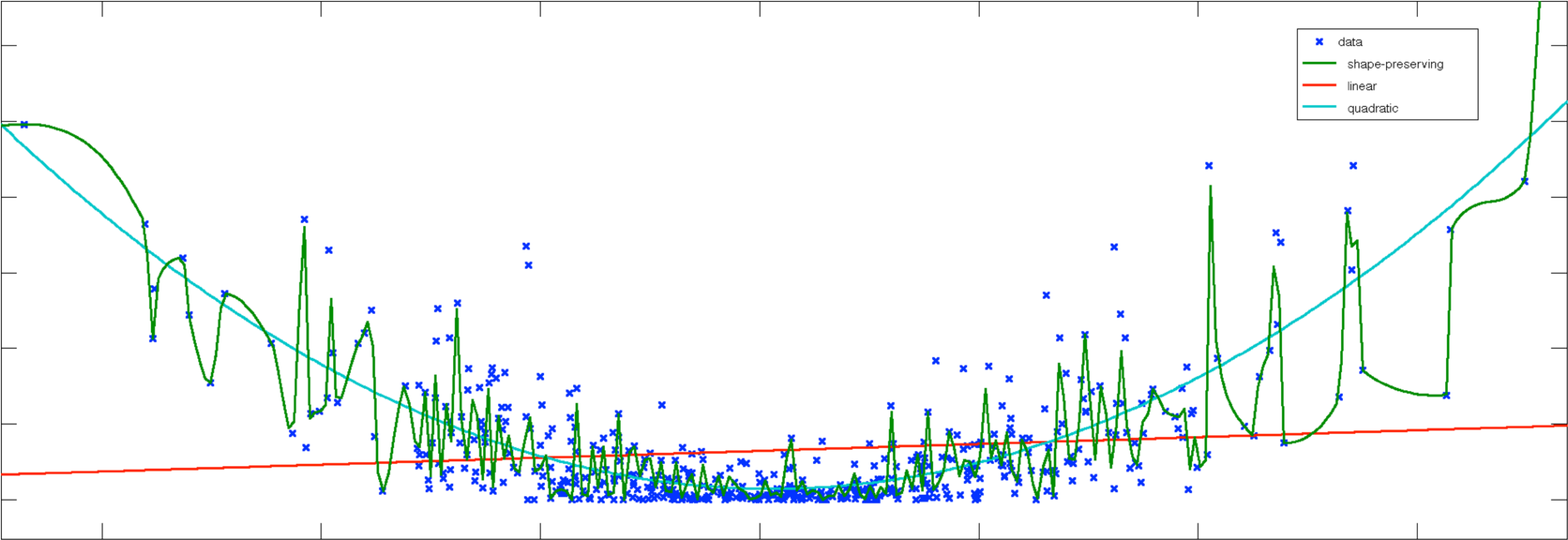


- High dimensional or non-parametric
- Weakly regularized
- Not enough modeling assumptions
- Not enough data
















Nearest-Neighbor Classifiers

0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

classifier = {

-  : 0,
-  : 0,
-  : 0,
-  : 0,
-  : 0,
-  : 1,
-  : 1,

100% training accuracy!



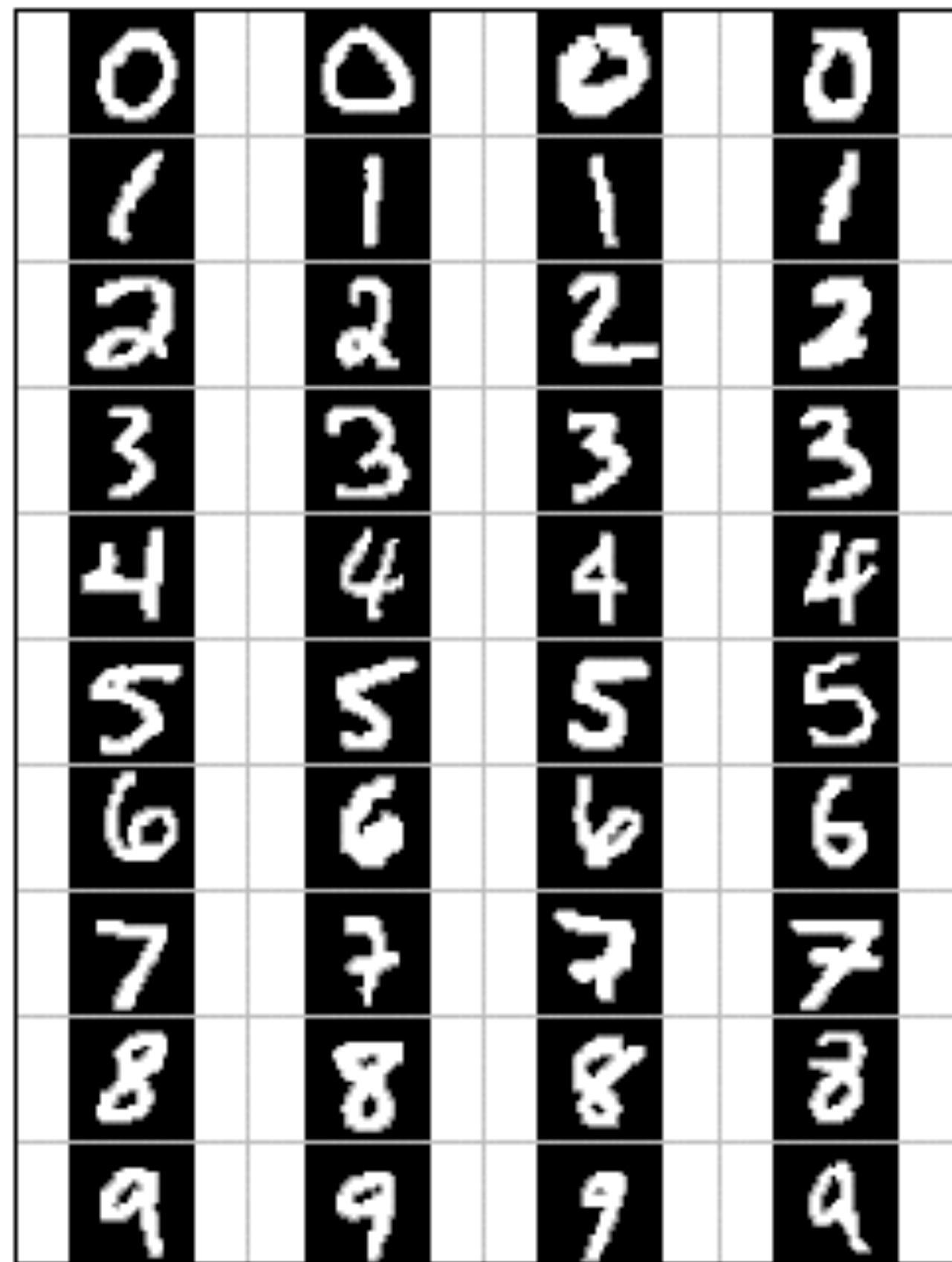
} ...

53% testing accuracy...

Held-out Validation

0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

Held-out Validation



training data

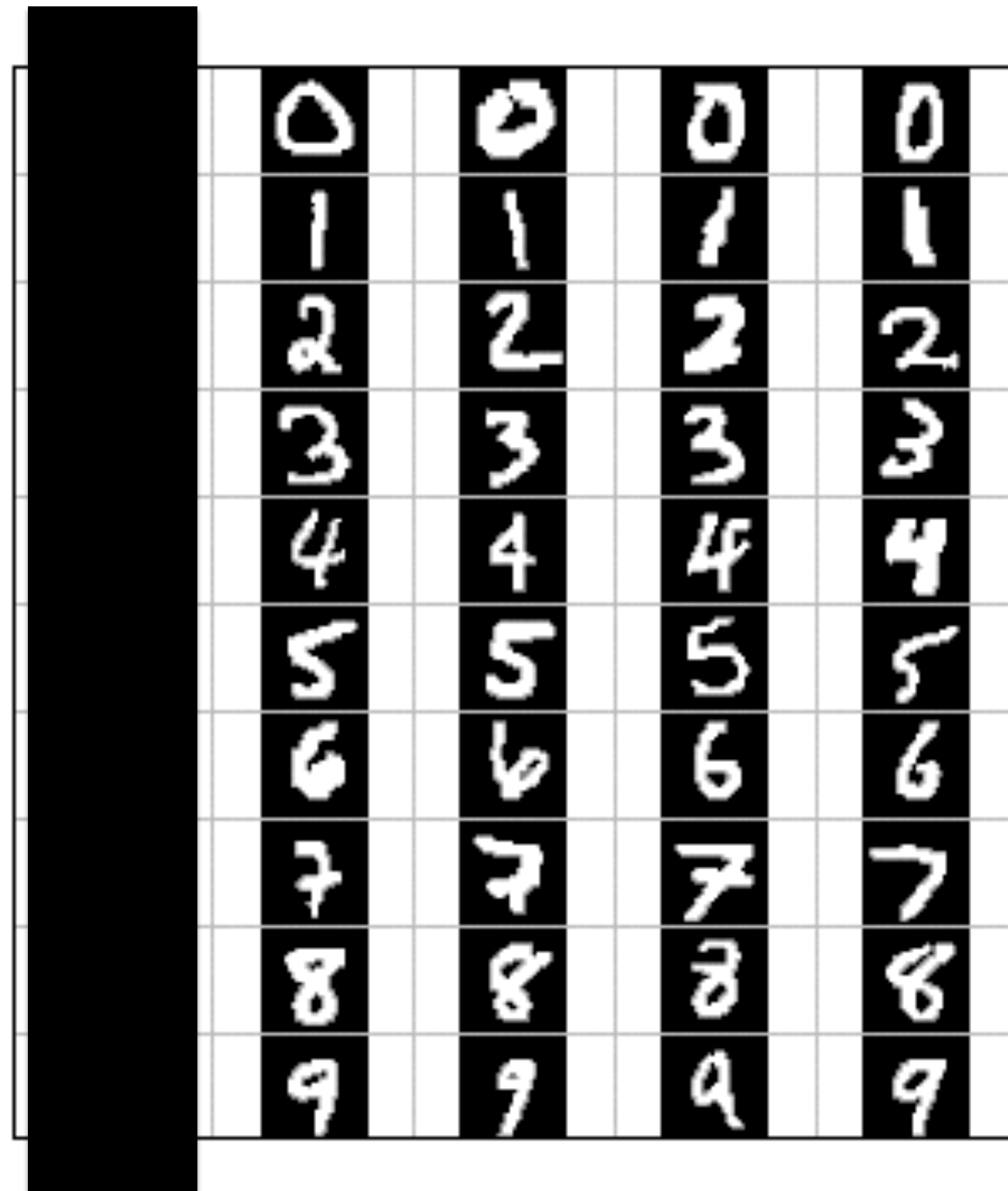
	Accuracy on training data	Accuracy on validation data
Simple	0.91	0.83
Medium	0.95	0.88
Complex	0.99	0.79
Super Complex	1.0	0.54



validation data

Cross Validation

Fold 1



0	0	0	0
1	1	1	1
2	2	2	2
3	3	3	3
4	4	4	4
5	5	5	5
6	6	6	6
7	7	7	7
8	8	8	8
9	9	9	9

training data



0
1
2
3
4
5
6
7
8
9

validation data

Cross Validation

Fold 2

0		0		0		0			
1		1		1		1			
2		2		2		2			
3		3		3		3			
4		4		4		4			
5		5		5		5			
6		6		6		6			
7		7		7		7			
8		8		8		8			
9		9		9		9			

training data

0
1
2
3
4
5
6
7
8
9

validation data

Cross Validation

Fold 3

0			0
1			1
2			2
3			3
4			4
5			5
6			6
7			7
8			8
9			9

training data

0
1
2
3
4
5
6
7
8
9

validation data

Cross Validation

Fold 4

0		0		0		0		0	
1		1		1		1		1	
2		2		2		2		2	
3		3		3		3		3	
4		4		4		4		4	
5		5		5		5		5	
6		6		6		6		6	
7		7		7		7		7	
8		8		8		8		8	
9		9		9		9		9	

training data

0
1
2
3
4
5
6
7
8
9

validation data

Cross Validation

Fold 5

0	0	0	0
1	1	1	1
2	2	2	2
3	3	3	3
4	4	4	4
5	5	5	5
6	6	6	6
7	7	7	7
8	8	8	8
9	9	9	9

training data

0
1
2
3
4
5
6
7
8
9

validation data

Leave-one-out Cross Validation

	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

training data



validation data

Leave-one-out Cross Validation

0			0		0		0
1			1		1		1
2			2		2		2
3			3		3		3
4			4		4		4
5			5		5		5
6			6		6		6
7			7		7		7
8			8		8		8
9			9		9		9

training data



validation data

Leave-one-out Cross Validation

0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

training data



validation data

Leave-one-out Cross Validation

0		0		0		0		0		0
1		1		1		1		1		1
2		2		2		2		2		2
3		3		3		3		3		3
4		4		4		4		4		4
5		5		5		5		5		5
6		6		6		6		6		6
7		7		7		7		7		7
8		8		8		8		8		8
9		9		9		9		9		9

training data



validation data

Leave-one-out Cross Validation

0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

training data



validation data

Leave-one-out Cross Validation

0		0		0		0		0
1		1		1		1		
2		2		2		2		2
3		3		3		3		3
4		4		4		4		4
5		5		5		5		5
6		6		6		6		6
7		7		7		7		7
8		8		8		8		8
9		9		9		9		9

training data



validation data

Leave-one-out Cross Validation

0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

training data



validation data

How Many Folds?

- What are the pros and cons of leave-one-out cross-validation?
- We usually train on $N-1$ folds and test on 1 fold. What are pros and cons of doing the inverse: train on 1 fold and test on $N-1$ folds?

0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

Training

0
1
2
3
4
5
6
7
8
9

Testing

How Many Folds?

- What are the pros and cons of leave-one-out cross-validation?
- We usually train on $N-1$ folds and test on 1 fold. What are pros and cons of doing the inverse: train on 1 fold and test on $N-1$ folds?

0
1
2
3
4
5
6
7
8
9

Training

0	0	0	0	0
1	1	1	1	1
2	2	2	2	2
3	3	3	3	3
4	4	4	4	4
5	5	5	5	5
6	6	6	6	6
7	7	7	7	7
8	8	8	8	8
9	9	9	9	9

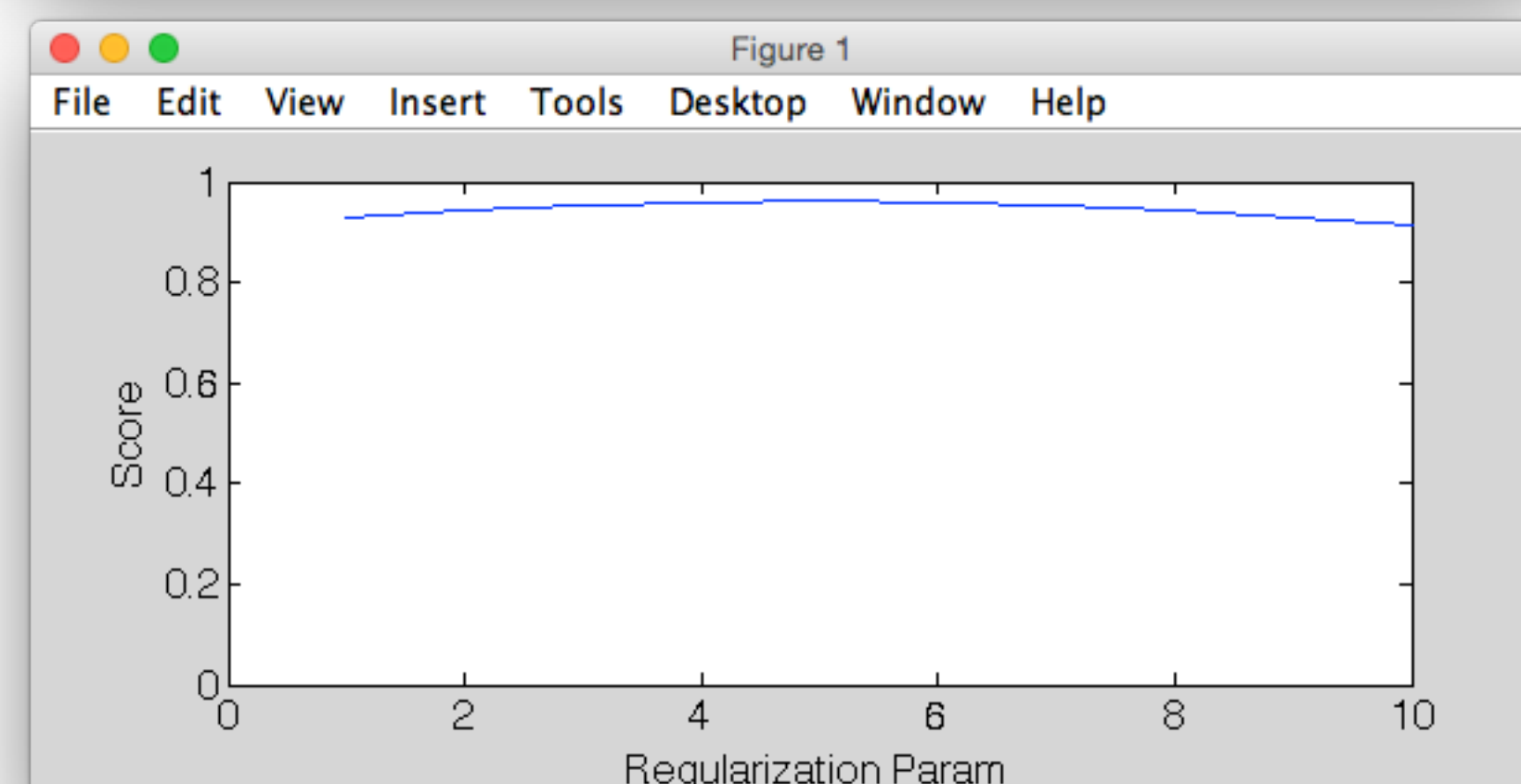
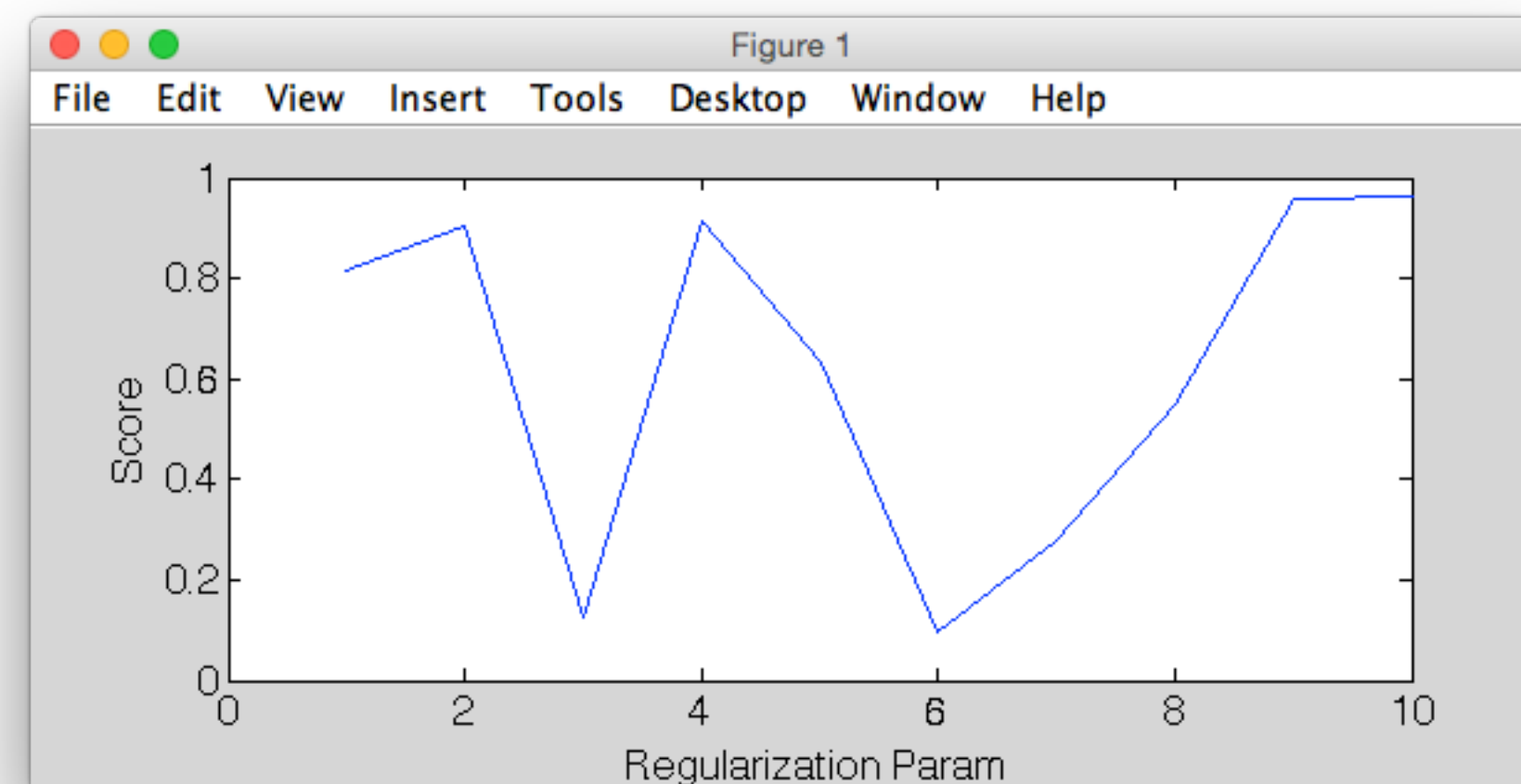
Testing

Testing versus Validation

- Best practice for experiments:
 - Hold out test set completely hidden from training
 - Use validation on training data for model (or parameter) selection
 - Evaluate on held-out test data

Scenarios

- Mystery ML algorithm with single complexity parameter
- Scenario 1: cross-validation scores are extremely erratic
- Scenario 2: cross-validation score is very uniform



Model Selection via Validation

- Measure performance on **held-out** training data
 - Simulate testing environment
- Rotate **folds** of held-out subsets
- Can even hold out one at a time: **leave-one-out** validation
- Use (cross) validation performance to tune extra parameters