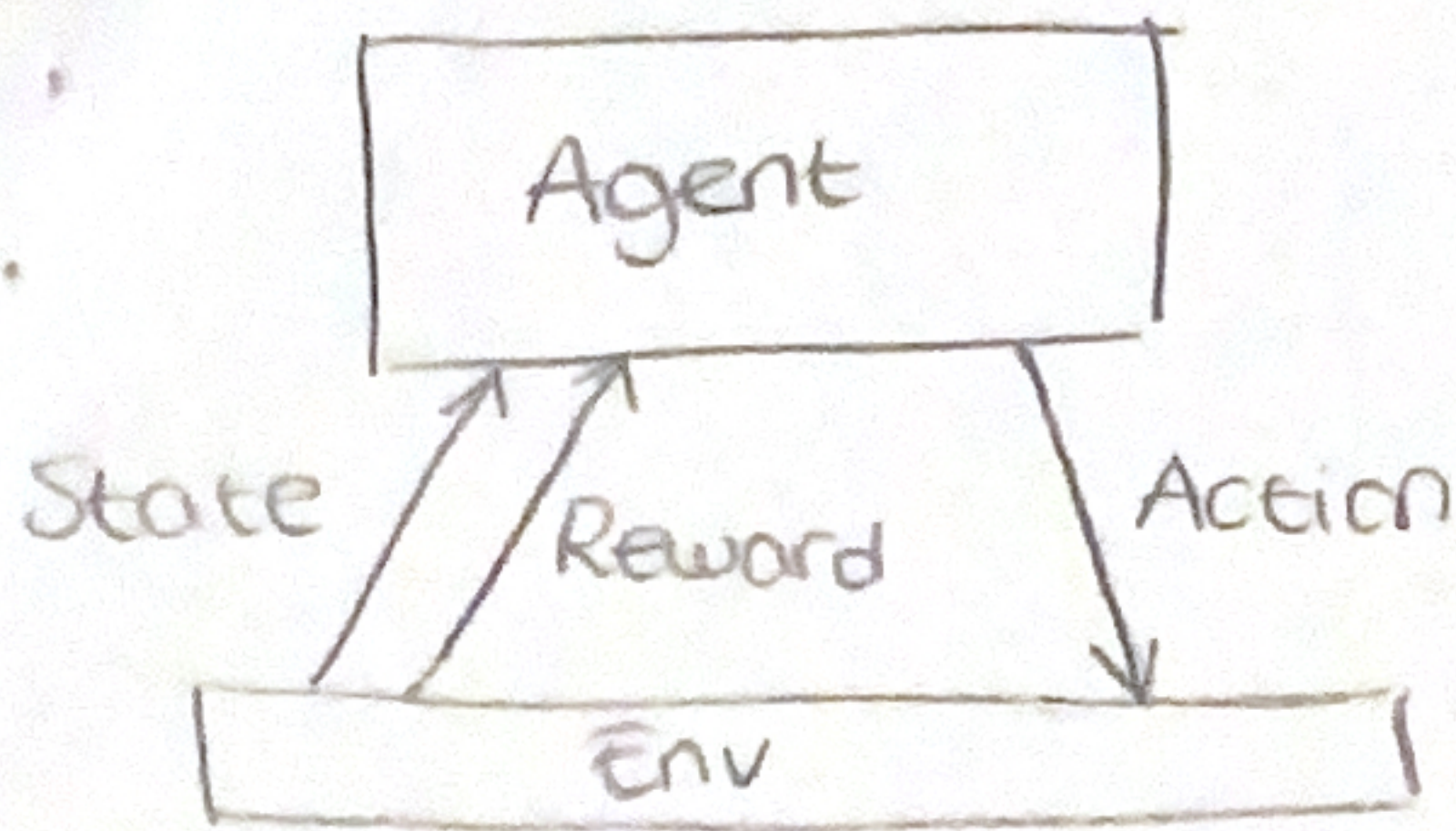


# Reinforcement Learning



$$s_0 \xrightarrow[r_0]{a_0} s_1 \xrightarrow[r_1]{a_1} \dots$$

Agent chooses action  $a_i$  in state  $s_i$  and gets reward  $r_i$ . But goal is to maximize:

$$r_0 + \gamma r_1 + \gamma^2 r_2 + \dots \quad 0 \leq \gamma < 1$$

Reward on the long term

$\gamma$ : discount factor  
(a parameter on how much we care about immediate & future rewards)

- Learn a control policy

$$\pi: S \rightarrow A$$

set of states

set of actions

- Take  $a$  from  $A$  given current state  $s$  from  $S$

## Problems

- Delayed Reward & Temporal Credit Assignment  
Determine which of the actions in its sequence are to be credited for eventual rewards.
- Exploration vs Exploitation  
Trade-off in choosing exploration of unknown states & actions (more info) or exploitation of states & actions that are known to yield reward.

## The Learning Task

### Markov Decision Process

$S \rightarrow$  set of states  
 $A \rightarrow$  set of actions

At each  $t$ , in  $s_t$ , perform  $a_t$ , get  $r(s_t, a_t)$ , produce  $s_{t+1} = \delta(s_t, a_t)$

$$\pi: S \rightarrow A$$

learn this

$$V^\pi(s_t) = r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \dots$$

$$\downarrow$$

$$\text{cumulative reward} = \sum_{i=0}^{\infty} \gamma^i r_{t+i}$$

$0 \leq \gamma < 1$

- When  $\gamma = 0 \rightarrow$  only immediate reward is considered
- When  $\gamma \approx 1 \rightarrow$  future rewards are more important

These only depend on current state.

Optimal policy is:

$$\pi \in \arg \max V^\pi(s)$$

$\downarrow$   
pick the policy with the most value