The MOSDEF Survey: The Variation of the Dust Attenuation Curve with Metallicity

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Abstract

We derive a UV-optical stellar dust attenuation curve of galaxies at $z = 1.4$–2.6 as a function of gas-phase metallicity. We use a sample of 218 star-forming galaxies, excluding those with very young or heavily obscured star formation, from the MOSFIRE Deep Evolution Field survey with Hβ, Hδ, and [NⅡ]λ 6585 spectroscopic measurements. We constrain the shape of the attenuation curve by comparing the average flux densities of galaxies sorted into bins of dust obscuration using Balmer decrements, i.e., Hβ-to-Hδ luminosities. The average attenuation curve for the high-metallicity sample ($12 + \log(O/H) > 8.5$, corresponding to $M_\odot \gtrsim 10^{10.4} M_\odot$) has a shallow slope, identical to that of the Calzetti local starburst curve, and a significant UV 2175 Å extinction bump that is $\sim 0.5 \times$ the strength of the Milky Way bump. On the other hand, the average attenuation curve of the low-metallicity sample ($12 + \log(O/H) \approx 8.2$ – 8.5) has a steeper slope similar to that of the SMC curve, only consistent with the Calzetti slope at the 3σ level. The UV bump is not detected in the low-metallicity curve, indicating the relative lack of the small dust grains causing the bump at low metallicities. Furthermore, we find that on average the nebular reddening ($E(B-V)$) is a factor of 2 times larger than that of the stellar continuum for galaxies with low metallicities, while the nebular and stellar reddening are similar for galaxies with higher metallicities. The latter is likely due to a high surface density of dusty clouds embedding the star-forming regions but also reddening the continuum in the high-metallicity galaxies.

Unified Astronomy Thesaurus concepts: Galaxy evolution (594); Interstellar dust extinction (837); High-redshift galaxies (734); Galaxy abundances (574); Chemical abundances (224); Galaxy properties (615); Galaxies (573); Interstellar dust (836); Interstellar abundances (832)

1. Introduction

What kind of dust attenuation curve should be used to correct the stellar continuum emission of galaxies? This question has a long history in galaxy evolution studies. In spite of the profound differences observed in the extinction curves of the Milky Way (MW; Cardelli et al. 1989; Fitzpatrick 1999) and a few well-studied local galaxies (e.g., Gordon et al. 2003; Fitzpatrick & Massa 2007; Clayton et al. 2015), at high redshifts a single UV-optical curve can be typically adopted to correct the rest-frame UV-optical light. The most common attenuation curves used at high redshift are the empirical starburst curve of (Calzetti et al. 2000, hereafter the C00 curve) and the two-component dust model of Charlot & Fall (2000). However, a variety of other curves are also found in the literature, as discussed below.

Extinction and attenuation curves are different by definition. An extinction curve is measured by observing stars with a screen of dust along the line of sight, which is influenced by the properties of dust grains (i.e., composition, size distribution). An attenuation curve refers to the average impact of dust absorption and scattering on a collection of stars, which includes the effects of the geometrical distribution of dust and stars in addition to the dust grain properties (i.e., for the extinction). The main differences observed in the shapes of the attenuation/extinction curves are the strengths of a broad extinction feature at 2175 Å, called the UV extinction bump, and the steepness (slope) of the UV curve (see the review by Salim & Narayanan 2020). The bump strength and the UV slope can be affected by both the radiative transfer effects (including dust-star geometry) in the attenuation curve, and by the underlying dust grain properties of the extinction curve.

A variety of behaviors are observed in the attenuation/extinction curves in the local universe and over cosmic time. The UV bump is observed along many sightlines within the MW, and to the LMC (Gordon et al. 2003; Fitzpatrick & Massa 2007), and M31 (Bianchi et al. 1996), but is weak or absent in the SMC. The bump is also absent in the C00 and the Charlot & Fall (2000) attenuation curves. The SMC extinction curve has a steep UV rise, while the C00 attenuation curve and the MW extinction curve have shallower slopes.

There are several studies of the attenuation curve of local galaxies that reach a variety of conclusions. In a series of papers, Battisti and collaborators examined variations in the shape of the attenuation curve for a large sample of local...
(z < 0.1) galaxies, using the methodology of Calzetti et al. (1994). Accordingly, these authors compared the average spectral energy distributions (SEDs) of galaxies with similar stellar populations but different dust reddening inferred from Balmer decrements, based on the flux ratio of Hα to Hβ (Battisti et al. 2016, 2017a, 2017b). They did not find any trend between the slope of the curve and stellar mass, specific star formation rate (sSFR), or metallicity. However, they found that galaxies with the highest inclination have a weak UV extinction bump and concluded that overall the effective attenuation ($\langle k_V - R_V \rangle$) in the UV is lower than that derived from the C00 curve. Wild et al. (2011a) compared the SEDs of pairs of galaxies matched to have similar intrinsic SEDs but different amounts of dust. They found that the UV slope of the curve and the UV bump strength vary strongly with inclination, but not with sSFR or optical depth. They observed the UV bump in all of their samples (except possibly the high sSFR sample). In another study at low redshifts ($z = 0.01–0.05$), Conroy et al. (2010) speculated that the UV bump may be responsible for their observed trends in the UV and optical colors. The bump has been also detected in the nearby sample of Burgarella et al. (2005), who suggested an average attenuation curve with the characteristics of the LMC curve. Using energy-balance SED fitting codes and UV-to-IR data for samples of local galaxies, Leja et al. (2017) and Salim et al. (2018) found a range of attenuation curve slopes, and a correlation between the slope and optical attenuation ($A_V$). Salim et al. (2018) reported slopes that are on average steep (SMC-like) and a variety of UV bump amplitudes, with an average of $\sim 1/3$ the strength of the MW bump. They also found that the local analogs of high-redshift galaxies have UV attenuation curves even steeper than the SMC curve.

At higher redshifts, $z \sim 1–3$, different methods are used to determine the shape of the attenuation curve, again with a range of results. Noll et al. (2009) set direct observational constraints on the strength of the bump by using high-quality rest-frame UV spectra at $z = 1.0–2.5$. They concluded that a significant bump is present in at least 30% of their sample, particularly those with higher reddening. Reddy et al. (2015) used Balmer decrements to empirically derive the attenuation curve at $z \sim 1.5–2.5$. They found marginal evidence for the UV bump and a UV curve slope identical to that of the C00 curve, but with a lower normalization ($R_V$). In multiple studies, flexible SED fitting techniques that allow the attenuation curve to be a free parameter have been used to infer the shape of the curve. For a sample of $z \sim 1.5$ galaxies with high average optical attenuation ($\langle A_V \rangle \sim 0.9$), Buat et al. (2011) found a shallow curve with a UV bump of $\sim 0.5$ the strength of the MW bump. In a later study, Buat et al. (2012) used a UV-selected sample with $\langle A_V \rangle \sim 0.5$ and found an average attenuation slope steeper than that of the C00 curve slope and a UV bump with amplitude similar to the LMC super-shell. Investigating the composite SEDs of galaxies at $z = 0.5–2.0$ with $A_V \gtrsim 0.5$, Kriek & Conroy (2013) derived an average curve with a shallow slope similar to the C00 slope. They also found that steeper curves show stronger UV bumps, and that the bump strength and curve slope vary with sSFR. Zeimann et al. (2015) defined an intrinsic SED using the average properties of their sample, and also found a varying UV slope with stellar mass, and no UV bump. Salmon et al. (2016) used a Bayesian formalism and incorporated IR luminosities along with UV-optical photometry, and found a variety of slopes. These authors showed that galaxies with higher color excesses ($E(B - V)$) have shallower curves. Tress et al. (2018) found a wide range of UV bump strengths at $z = 1.5–3$ with a correlation between the bump amplitude and color excess. Scoville et al. (2015) also observed a weak UV bump and a C00-like curve slope in their sample of young galaxies with $\langle A_V \rangle \sim 0.6$ (identified by strong CIV 1540 absorption features) at $z = 2.0–6.5$. Battisti et al. (2020) showed that a UV bump of $\sim 1/3$ the strength of the MW bump is required to achieve better SED fits to galaxies at $z \sim 0.1–3.0$, and that the slope of the curve strongly anti-correlates with star formation rate (SFR) and $A_V$.

The UV extinction bump has also been detected in the afterglow spectrum of gamma-ray bursts (GRBs) at $z \sim 2$ (Elíasdóttir et al. 2009; Perley et al. 2011; Zafar et al. 2018a). In another study of seven GRB hosts, Corre et al. (2018) found a great variety in the slopes and UV bump strengths. Multiple other GRB afterglow studies at $z \sim 1–3$ and higher ($z > 3$), found steep and bump-free extinction curves consistent with the SMC curve (Japelj et al. 2015; Zafar et al. 2018b).

In summary, the attenuation curves reported in the literature show a large degree of variation. However, in most cases, the variations can be attributed to sample selection effects—specifically to differences in the average optical attenuation, $A_V$, of the samples (Salim & Narayanan 2020). Theoretical work based on radiative transfer modeling has shown that the attenuation curve slope and the bump strength correlate with total dust column density, such that galaxies with larger optical depths (or $A_V$) have shallower slopes and suppressed bumps (Witt & Gordon 2000; Pierini et al. 2004; Inoue 2005; Chevallard et al. 2013). These relationships are also recovered in cosmological simulations (Narayanan et al. 2018; Shen et al. 2020; Trayford et al. 2020).

In addition, the attenuation curve is also affected by dust grain properties. The origin of the UV bump is most commonly attributed to small carbonaceous grains in the form of graphite or polycyclic aromatic hydrocarbon (PAHs; Stecher & Donn 1965; Li & Draine 2001; Weingartner & Draine 2001a; Draine 2003), and the steep UV rise of the extinction curve is speculated to be a result of a higher fraction of small dust grains (Gordon et al. 1997; Hou et al. 2017) and/or a lower fraction of small carbonaceous to small silicate grains (Weingartner & Draine 2001a). Therefore, the bump and the steep UV slope will be more prominent in environments that are amenable to the carriers of the bump and the steep UV rise, respectively. A proxy to probe the small dust grains in the ISM is gas-phase metallicity, owing to dust depletion of interstellar elements (Dwek 1998; Jenkins 2009).

In this study, we aim to investigate the variation of the attenuation curve with gas-phase metallicity by fixing the distribution of dust optical depths in our samples to control for the radiative transfer effects and eliminate the selection biases due to different optical depth distributions. We adopt the empirical Balmer decrement method that was first developed by Kinney et al. (1994) and Calzetti et al. (1994, 2000), and later exploited by Battisti et al. (2016, 2017a, 2017b) for local samples of galaxies and by Reddy et al. (2015) for high-redshift galaxies. In this method, the Balmer decrement is used as an independent indicator of dust reddening to sort galaxies into bins of obscuration, allowing comparison of the average wavelength-dependent flux densities of more obscured galaxies to those of galaxies that are less obscured. Such a method...
requires a large spectroscopic sample with measurements of at least two Balmer lines, which is achievable at high redshifts using multi-object near-IR spectrometers.

The MOSFIRE Deep Evolution Field (MOSDEF) survey (Kriek et al. 2015) is one of the largest rest-frame optical spectroscopic surveys of galaxies at z ~ 1.5–3.5, with Keck/MOSFIRE spectra of ~1500 galaxies, covering Hα and Hβ for those at z ~ 1.5–2.5. Using the first 2 (out of 4) yr of the MOSDEF survey data set, Reddy et al. (2015) derived the z ~ 2 attenuation curve adopting the Balmer decrement method. In this study, we build on this previous work by dividing the full MOSDEF sample into two metallicity bins with matched distributions in Balmer optical depth (τ_{Hα} – τ_{Hβ}) and sSFR. The former avoids biases due to different dust column densities, and the latter ensures similar intrinsic stellar populations among the metallicity bins. Moreover, this study has the advantage of better sampling the rest-frame UV SED compared to similar photometric studies at z ~ 0 (usually limited to the Galaxy Evolution Explorer near-UV (NUV) and far-UV (FUV) bands at 1771–2831 Å and 1344–1786 Å, respectively), as the rest-frame UV at z ~ 2 is redshifted to wavelengths accessible to optical instruments.

The paper is structured as follows. Section 2 presents the methodology for deriving the attenuation curve. In Section 3, we describe the data, sample, and measurements. We present the derivation of the attenuation curve in bins of metallicity in Section 4. In Section 5, we discuss the physical interpretation of our metallicity-dependent attenuation curves, and review the implications of using these curves for calculating dust-corrected SFRs, UV continuum slopes, and stellar color excesses (E(B – V)). Section 6 summarizes the main results. Throughout this paper, line wavelengths are presented in vacuum. We assume a Chabrier (2003) initial mass function (IMF) and adopt a cosmology with H_0 = 70 km s^{-1} Mpc^{-1}, Ω_m = 0.7, and ΩΛ = 0.3.

2. Methodology

We follow the methodology that was used initially in Calzetti et al. (1994), and later in Calzetti et al. (2000), Reddy et al. (2015), and Battisti et al. (2016), to derive the selective attenuation curve, k_{λ} – R_{λ}, where k_{λ} is the total attenuation curve as a function of wavelength and R_{λ} is the normalization. The normalization is conventionally taken at 5500 Å, the effective wavelength of the V band (i.e., k_{V} = R_{V}). Later in Section 4.3, we combine our results on the selective attenuation curve with those of Reddy et al. (2015) to obtain the total attenuation curve, k_{λ}. Total attenuation at a given wavelength is then A_{λ} = E(B – V)k_{λ}, where E(B – V) is the stellar color excess, or reddening. Assuming a geometry of a screen of dust in front of the emitters, the intrinsic stellar emission (F_{λ, int}) can be recovered using the standard formulation of F_{λ, int} = F_{λ, obs} × 10^{-0.4 E(B-V)k_{λ}} (Calzetti et al. 1994, 2000), where F_{λ, obs} is the observed flux density.

The difference in optical depth between Hα and Hβ is the Balmer optical depth, τ_{H} (Calzetti et al. 1994), defined as

\[ \tau_{H} = \tau_{Hα} - \tau_{Hβ} = \ln \left( \frac{F(Hα)}{F(Hβ)} \right) \]

where F(Hα) and F(Hβ) are the Hα and Hβ line fluxes and 2.86 is the theoretical value for the ratio in Case B recombination with T_e = 10^4 K and n_e = 100 cm^{-3} (Osterbrock & Ferland 2006).

The Balmer optical depth indicates the nebular dust reddening, which correlates with stellar dust reddening, as shown in multiple previous studies (e.g., Calzetti et al. 1994; Reddy et al. 2015; Battisti et al. 2016; Theios et al. 2019). We show the correlation in our sample later in Section 3.4.1 and Figure 2.

We sort the galaxies into bins of τ_{H}. The lowest τ_{H} bin is consistent with (τ_{H}) ~ 0, and its average flux densities are taken as the intrinsic (dust-free) SED of the sample. The flux densities of each target are normalized at rest frame 5500 Å, using the individual best-fit SEDs (Section 3.3), and are shifted to the rest frame. We use the moving median (as a smoothing technique) of flux densities in each τ_{H} bin at λ = 1250–7000 Å to construct empirical SEDs. By dividing the empirical SED in each τ_{H} bin by that of the lowest τ_{H} bin ((τ_{H}) ~ 0), and normalizing to the difference in Balmer optical depths, we calculate the selective attenuation curve as

\[ Q_{i} = -\frac{\ln \left( \frac{F_{i,λ}}{F_{0,λ}} \right)}{τ_{H,i} - τ_{H,0}}, \]

where τ_{H,0} and F_{λ,0} are the average Balmer optical depth and flux density of the lowest τ_{H} bin, respectively (τ_{H,0} is consistent with 0), and the quantities with i indices denote those of the ith τ_{H} bins. We adopt three τ_{H} bins (two Q_{i}s), as our sample size does not allow for higher number of bins without each bin getting dominated by the statistical noise (read about the sample in Section 3.4). The average selective curve, or the “effective” attenuation (Q_{eff}) is the average of all the selective attenuation curves (Q_{i}s).

To derive robust uncertainties we performed a Monte Carlo simulation by (a) randomly perturbing the flux densities assuming a Gaussian distribution centered at the measured value with a standard deviation equal to the photometric error, (b) randomly perturbing the boundaries of the τ_{H} bins assuming Gaussian distributions centered at the boundaries shown in the right panel of Figure 1, with a standard deviation of 0.1, which is about the typical error in τ_{H} measurements, and (c) performing a jackknife resampling (Quenouille 1949; Tukey 1958) by randomly removing an object from the sample without a replacement. The realizations are measured at least 1000 times. The final effective curve and its uncertainty are determined based on the average and standard deviation of the 1000 realizations.

To find the functional form of the attenuation curve, we fit Q_{eff} versus 1/λ with a second-order polynomial, and where applicable, a Drude function is added to account for the UV extinction bump using the Fitzpatrick & Massa (2007) formalization:

\[ Q_{eff}(x) = a_1 x^2 + a_2 x + a_3 + D(x, E_b), \]

\[ D(x, E_b) = E_b \frac{x^2}{(x^2 - q_0^2)^2 + x^2 \gamma^2}, \]

where x = 1/λ in μm^{-1} and D(x, E_b) is the Drude function. We fix the central wavelength (q_{0}) and width (\gamma) of the UV extinction bump to the MW values of 4.59 and 0.922 μm^{-1}, adopted from Fitzpatrick & Massa (2007), and leave the amplitude of the Drude function (E_b) as a free parameter. The fits are performed at λ = 1250–3000 Å and 4000–7000 Å. Wavelengths of λ < 1250 Å and λ = 3000–4000 Å are excluded to avoid variations in Lyα equivalent width and the
strength of the Balmer/4000 Å break, respectively. Our second-order polynomial fit is supported over a linear fit according to the Akaike information criterion (AIC; Akaike 1973) and the reduced \( \chi^2 \) of the fits. A linear fit to \( Q_{\text{eff}} \) versus 1/\( \lambda \) always results in a curve with a steep UV slope, as the fit is highly influenced by the longer wavelength data (>4000 Å) and does not have the flexibility to simultaneously fit the UV data points.

The \( Q_{\text{eff}} \) curve can be related to the total attenuation through

\[
k_{\lambda} = f \, Q_{\text{eff}}(\lambda) + R_V.
\]

Calculating \( R_V \), which in this formalization is the vertical offset at 5500 Å, requires extrapolation to rest-frame near-IR wavelengths, where the attenuation is considered to be negligible (Calzetti 1997; Gordon et al. 2003; Reddy et al. 2015; Battisti et al. 2017b), or alternatively, requires an energy-balance calculation between the IR dust emission and UV-optical attenuation (Calzetti et al. 2000). Constraining the \( R_V \) for our curves is beyond the scope of this work and will be discussed in a future paper. Here, we focus on the shape of the attenuation curve at rest-frame UV and optical wavelengths. The factor \( f \) in the equation above constrains the slope of the curve at \( \lambda = 4400-5500 \) Å and is conventionally defined such that \( k_B - k_V = 1 \):

\[
f = \frac{1}{Q_{\text{eff}}(B) - Q_{\text{eff}}(V)},
\]

where the \( B \) and \( V \) bands correspond to \( \lambda = 4400 \) and 5500 Å, respectively. Note that in the formalization presented here, by definition, \( Q_{\text{eff}}(V) \) is zero.

3. Data and Sample

3.1. The MOSDEF Survey

MOSDEF is a near-IR spectroscopic survey of ~1500 galaxies at \( z = 1.4-3.8 \) with the Keck/MOSFIRE spectrograph (McLean et al. 2010, 2012), carried out over 48.5 nights of observation from 2012–2016. The parent sample is selected in three redshift bins of \( z = 1.37-1.70, 2.09-2.61, \) and 2.95–3.80, down to \( H \)-band AB magnitudes of \( H = 24.0, 24.5, \) and 25.0 respectively, corresponding to \( M_{\star} \sim 10^9 \, M_{\odot} \) for star-forming galaxies, using the photometric and spectroscopic catalogs from the 3D-HST survey (Skelton et al. 2014; Momcheva et al. 2016). The three redshift intervals ensure coverage of the strongest rest-optical nebular emission lines, including \([\text{O} \, \text{II}], \ H\beta, \ [\text{O} \, \text{III}], \) and \( \text{H} \alpha \). As the \( \text{H} \alpha \) line is not accessible for the highest redshift bin, only the first two redshift bins (\( z = 1.37–2.61 \)) are used in this analysis. The targets for MOSFIRE observations are further selected based on prior redshift measurements (external spectroscopic or 3D-HST grism redshifts and/or photometric redshifts) that place them in the aforementioned redshift ranges. We refer readers to Kriek et al. (2015) for more details on the survey strategy, observations, and data reduction.

MOSDEF targets lie in the deep extragalactic Cosmic Assembly Near-infrared Deep Extragalactic Legacy Survey (CANDELS) fields: AEGIS, COSMOS, GOODS-N, GOODS-S, and UDS (Grogin et al. 2011; Koekemoer et al. 2011), and hence covered by a wealth of ancillary data. In this work, the UV-to-near-IR photometric catalogs of the 3D-HST survey (Skelton et al. 2014) are used for SED fitting and deriving rest-frame UV SFRs and UV slopes (Section 3.3).

3.2. Optical Line Measurements

Emission-line fluxes are determined by fitting Gaussian functions on top of a linear continuum to MOSFIRE 1D spectra (Kriek et al. 2015; Reddy et al. 2015; Freeman et al. 2019), and the uncertainties are derived by perturbing the spectrum of each object according to its error spectrum and measuring the standard deviation of the distribution of perturbed line fluxes. A triple Gaussian function was used to fit the \( \text{H} \alpha + [\text{N} \, \text{II}] \lambda 6550, 6585 \) complex. Slit-loss corrections are applied by normalizing the spectrum of a “slit star” placed on each observing mask to match the 3D-HST total photometric flux. Additionally, the HST images of the resolved targets were used to estimate and correct for differential flux loss relative to that of the star described above (Reddy et al. 2015). Details on line flux measurement and slit-loss correction are provided in Kriek et al. (2015) and Reddy et al. (2015).

The \( \text{H} \alpha \) and \( \text{H} \beta \) fluxes are further corrected for underlying stellar Balmer absorption, estimated from the best-fit SED models to the photometry (Kriek et al. 2015; Reddy et al. 2015). The \( \text{H} \beta \) absorption fluxes are on average ~15% of the \( \text{H} \beta \) observed emission fluxes. The uncertainty in the absorbed fluxes is ~2% (Reddy et al. 2015), which is negligible compared to the typical uncertainty of our emission-line fluxes (~15%).
3.3. SED Fitting and SFR Measurements

Throughout this work, the photometry is corrected for contamination from nebular emission lines measured from the MOSDEF rest-frame optical spectra (R. Sanders et al., in preparation). Corrections are considered for any filter in the 3D-HST catalog that overlaps with the MOSFIRE $Y-J-H-K$ bands, which includes $z$, $Y$, $J$, $H$, $K$, $K_s$, $F125W$, $F140W$, $F160W$, and $F850LP$ filters, whenever available. To determine the emission-line correction factor, we create a model spectrum composed of the best-fit Gaussian profile of the emission lines (Section 3.2) and convolve it with the filter transmission curves. The value of the correction factor depends on the width of the contaminated filter and the emission-line equivalent width. In cases where the difference between the original photometry and the emission-line corrected photometry is more than $1\sigma$ (where $\sigma$ is the photometric error on the observed point), the corrected photometry is adopted.

To derive stellar masses, and later to normalize the photometry of individual sources to a common base (at rest frame 5500 Å, Section 2), we use best-fit SED models. The SED fitting is done using the FAST code (Kriek et al. 2009), the stellar population model library of Conroy et al. (2009) for solar stellar metallicity, a Chabrier (2003) IMF, delayed exponentially declining star formation history (SFH; SFR $\sim t \exp(-t/\tau)$), where $t$ is the age and $\tau$ is the exponential timescale), and the Calzetti et al. (2000) attenuation curve. The choice of attenuation curve has a statistically insignificant impact on the inferred stellar masses and the normalization at 5500 Å.

The SFR used to derive sSFR in the following sections is the dust attenuation-corrected H$\alpha$ SFR ($\text{SFR}_{\text{H} \alpha, \text{att}}$). We correct H$\alpha$ luminosity for attenuation using the Balmer decrement and the Cardelli et al. (1989) MW extinction curve (see Reddy et al. 2015; Shivaei et al. 2015a, 2016). Assuming that the H II regions follow a foreground dust screen model, the MW curve is preferable for the extinction correction of nebular lines, as it is derived based on the line-of-sight measurements of H II regions (Calzetti et al. 1994; Wild et al. 2011b; Liu et al. 2013; Salim & Narayan 2020) and is shown to be an accurate representation of nebular attenuation curve at $z \sim 2$ (N. Reddy et al., in preparation). Multiple studies have also shown a good agreement between dust-corrected SFR($\text{H} \alpha$) using the MW curve and IR-inferred SFRs (e.g., Flores et al. 2004; Shivaei et al. 2016). The dust-corrected H$\alpha$ luminosities are converted to SFR based on the Hao et al. (2011) conversion, modified for a Chabrier IMF.

3.4. Sample

We start with a sample of 271 galaxies from the MOSDEF survey with H$\alpha$, H$\beta$, and [N II] detections. To determine the attenuation curve, we must ensure that the intrinsic (i.e., dust-free) SEDs of the galaxies have similar shapes. Therefore, avoiding galaxies that are optically thick in the UV or in optical nebular lines, and those with very young ages whose intrinsic UV slope is a strong function of stellar population age, is necessary. We impose the following criteria on the parent MOSDEF sample to obtain a clean sample for our analysis:

1. Robust ($>3\sigma$) detection of H$\alpha$ and H$\beta$ emission lines;
2. Removal of targets with active galactic nucleus (AGN) contamination based on X-ray emission, IRAC colors, and/or [N II]/H$\alpha$ ratios (for details on MOSDEF AGN identification see Coil et al. 2015; Azadi et al. 2017, 2018; Leung et al. 2019);
3. Removal of ultraluminous infrared galaxies (ULIRGs) ($L(\text{IR}) > 10^{12} L_\odot$) to ensure the sample is clean of heavily dust-obscured objects. We use Spitzer/MIPS 24 μm flux densities and the redshift-dependent conversion of Rujopakarn et al. (2013), to estimate total IR luminosities of individual objects;
4. Removal of targets with [O III] and H$\alpha$ line equivalent widths greater than 630 and 1600 Å, respectively, to avoid targets with ages younger than 100 Myr (the limits are determined based on the results of Reddy et al. 2018b);
5. Removal of quiescent targets using $UVJ$ criteria (Zick et al. 2018) and those with low sSFRs (log(sSFR/yr$^{-1}$) < −9.6);
6. Removal of targets with Balmer optical depth of $\tau_{\text{H} \alpha} > 1$ (Equation (1) below) to avoid optically thick objects.

Shivaei et al. (2016) have shown that SFR$_{\text{H} \alpha,\text{H} \beta}$ agrees well with the bolometric UV-to-IR SFR up to $\sim 100 M_\odot$ yr$^{-1}$ in IR-detected galaxies. This SFR limit corresponds to $\tau_{\text{H} \alpha} \sim 1$, based on a linear regression fit to SFR$_{\text{H} \alpha,\text{H} \beta}$ versus $\tau_{\text{H} \alpha}$ in our current sample;
7. Robust ($>3\sigma$) detection of [N II] $\lambda$6585 for metallicity measurements, see below, as the main goal of this work is to evaluate the change in the attenuation curve as a function of metallicity.

These criteria result in a sample of 218 galaxies at $z = 1.4-2.6$.

3.4.1. Sample with Metallicity Measurements

The [N II] and H$\alpha$ lines are used to estimate the gas-phase metallicity (oxygen abundances, $12 + \log(O/H)$), assuming the Pettini & Pagel (2004) empirical calibration (Sanders et al. 2015; Shapley et al. 2015). The [N II]/H$\alpha$ ratio is shown to be a good tracer of metallicity in the local universe for the range of metallicities that we trace ($12 + \log(O/H) \sim 8.0-8.8$; Pettini & Pagel 2004; Marino et al. 2013), but at high redshifts, the ratio has uncertainties as a diagnostic of oxygen abundance due to N/O variations and other uncertainties regarding the physical conditions in H II regions (e.g., Shapley et al. 2015; Strom et al. 2017; Bian et al. 2018). Therefore, the absolute metallicity values should be taken with caution. However, using [N II]/H$\alpha$ to sort galaxies by metallicity, as in this study, is robust, as the ratio correlates well with other metallicity indicators that use oxygen lines (e.g., Steidel et al. 2014; Sanders et al. 2015).

We divide the sample into two metallicity bins at $12 + \log(O/H) = 8.5$, hereafter low- and high-metallicity bins. The oxygen abundance of 12 + log(O/H) = 8.5 is the [N II]/H$\alpha$ metallicity limit below which the mid-IR aromatic band (PAH) intensity at rest frame 7.7 μm (defined as the ratio of 7.7 μm luminosity to total SFR) decreases significantly in the MOSDEF sample, as shown in Shivaei et al. (2017). As PAHs are suggested as one of the main carriers of the UV extinction bump (Stecher & Donn 1965; Li & Draine 2001; Weingartner & Draine 2001a; Draine 2003), we divide the sample at this metallicity limit to look for variations in the bump strength. There are 83 and 135 galaxies in the low- and high-metallicity bins.

We further impose three additional criteria to avoid biases due to different optical depths and intrinsic SEDs in the two metallicity subsamples and within each metallicity subsample.
when divided into bins of Balmer optical depth ($\tau_b \equiv \tau_{H\alpha} - \tau_{H\beta}$), see Section 2):

1. In the absence of short-term star formation variations, large differences in the SFR may indicate differences in the shape of the SED. Therefore, we limit the sSFRs to $-8.5 < \log(\text{sSFR}/\text{yr}^{-1}) < -9.4$ to avoid large variations in the SFR of galaxies as a function of $\tau_b$ in each metallicity subsample (see the discussion in the Appendix). This criterion helps with having similar intrinsic stellar populations within the $\tau_b$ bins and mitigating the uncertainties associated with the change of intrinsic SED as a function of $\tau_b$ (Chevallard et al. 2013). We estimate the systematic uncertainty within our sample associated with the SFR stochasticity and variations in the average sSFRs in Section 4.1.1 and the Appendix, showing they do not affect our results. The right panel of Figure 1 shows sSFR versus $\tau_b$ in the two metallicity subsamples;

2. To control for the variations of the intrinsic stellar populations between the two metallicity subsamples, we match the two subsamples in their SFR distribution, as follows. For each high-metallicity galaxy with a given sSFR, a galaxy from the low-metallicity sample with an sSFR within 0.2 dex of that of the high-metallicity galaxy is selected (see Section 2). The K–S statistic of the two sSFR distributions is 0.14 with a $p$-value of 0.72, consistent with the hypothesis that the sSFR distributions of the two samples are the same. The distributions are shown in the middle panel of Figure 1;

3. In the same way as matching the SFR distributions, the $\tau_b$ distributions of the two metallicity subsamples are also matched within $\Delta \tau_b = 0.2$ (K–S statistic of 0.14 with a high $p$-value of 0.71, consistent with the hypothesis that the $\tau_b$ distributions of the two samples are the same), to control for the effect of different optical depth distributions in the low- and high-metallicity attenuation curves, as it is known that the shape of the attenuation curve varies with the optical depth (Chevallard et al. 2013; Salmon et al. 2016; Salim et al. 2018). The distributions are shown on the left panel of Figure 1.

The final sample has 48 objects in each metallicity bin.

The UV continuum slope ($\beta$ in $f_{\lambda} \propto \lambda^\beta$ at $\lambda = 1260\text{2600}\text{Å}$) is an indication of the stellar reddening for typical star-forming galaxies (Meurer et al. 1999). The relation between $\tau_b$ and $\beta$ in the two metallicity samples is shown in Figure 2, where $\beta$ is calculated by fitting a power-law function to the best-fit SED models (Section 3.3), $f_{\lambda} \propto \lambda^\beta$, at $\lambda \sim 1260\text{–}2600\text{ Å}$. The good correlation between $\beta$ and $\tau_b$ (Pearson correlation coefficient of $\sim0.6$ with $p$-value of $\lesssim10^{-3}$) and similar trends with the original Calzetti et al. (2000) and Battisti et al. (2016) local samples show the validity of the adopted methodology to derive the stellar attenuation curve, as discussed in Section 2.

4. Results

It is expected that the physical properties of dust grains (e.g., dust grain composition), and as a result the shape of the attenuation curve, vary with ISM gas abundances. Shivaei et al. (2017) have shown that the emission intensity of the PAH dust grains in the mid-IR, suggested as the origin of the UV extinction bump (Stecher & Donn 1965; Li & Draine 2001; Weingartner & Draine 2001a; Draine 2003), strongly depends on the gas metallicity at $z \sim 2$ (consistent with similar studies at lower redshifts, e.g., Engelbracht et al. 2005; Draine et al. 2007; Smith et al. 2007; Marble et al. 2010). Motivated by such studies, we explore the variations of the shape of the curve (UV rise and the UV extinction bump) with metallicity in this section. We use the methodology described in Section 2 to derive the attenuation curves ($Q_{\text{eff}} \equiv k_b - R_0$) in two metallicity bins, separated at $12 + \log(\text{O/H}) = 8.5$, as defined in Section 3.4.

4.1. Variations in the Curve Slope

The left and middle panels in Figure 3 show the attenuation curves in the two metallicity bins, fit with a second-order polynomial without a Drude profile (Equation (3); the UV extinction bump will be investigated in the next section). The shaded regions show the 68, 95, and 99.7 percentile bounds from our Monte Carlo analysis (Section 2).

The low-metallicity curve shows a steep UV rise, similar to that of the SMC curve from Gordon et al. (2003). Nonetheless, the curve is consistent with the C00 and the Reddy et al. (2015) (hereafter, R15) curves at 3$\sigma$. On the other hand, the high-metallicity curve is identical to the C00 and R15 curves.\footnote{As we use a quadratic function to fit the curves, the high-metallicity fit had a turnover to low attenuation curve values at $\lambda \lesssim 2000\text{ Å}$, which is not physically motivated, and hence corrected for by linearly extrapolating the quadratic curve to short wavelengths (Figure 3-middle).} Our result of a steeper attenuation curve at low metallicities is also applicable to galaxies with low masses, given the correlation between stellar mass and gas-phase metallicity. This result is in
agreement with previous studies showing that steeper attenuation curves are favored in low-mass galaxies at high redshifts (Reddy et al. 2018a; Álvarez-Márquez et al. 2019).

We note that the R15 curve was derived using a sample that partially overlaps with ours, separated into two sSFR bins. Using the same sample as in R15, we find the exact same results, except for a stronger indication of the UV bump as discussed below. It is when the samples are divided into metallicity bins that the low-metallicity curve starts to deviate in the UV (bluewards of 2500 Å) from the shallower curve of the high-metallicity bin and the R15 curve.

4.1.1. Slope Uncertainties

The uncertainty intervals shown in Figure 3 encompass measurement uncertainties, and uncertainties associated with sample selection and \( \tau_b \) bin variations (see Section 2). The \( 1\sigma \) relative uncertainties, \( \Delta \Omega_{\text{eff}}/\Omega_{\text{eff}} \), at \( \lambda = 1500 \) Å of the low- and high-metallicity curves are \(+48\%\), \(-23\%\) and \(+9\%\), \(-7\%\), respectively. The measurement uncertainties associated with the flux measurement errors are \(+20\%\), \(-15\%\) and \(+7\%\), \(-5\%\) for the low- and high-metallicity curves, respectively. As is evident, the uncertainty in the high-metallicity curve is dominated by the measurement uncertainties. On the other hand, the uncertainty of the low-metallicity curve is much larger than the measurement uncertainties, which suggests a larger intrinsic scatter in the attenuation curves of low-metallicity galaxies compared to those of the high-metallicity galaxies.

The other source of uncertainty in the Balmer optical depth method used here is associated with the variations in the intrinsic SEDs of galaxies used to derive the attenuation curve. Calzetti et al. (1994) pioneered determination of the attenuation curve using Balmer optical depths by appealing to the similarity of galaxy SEDs in the 1200–2600 Å range, assuming a constant rate of star formation. They pointed out that even a young, instantaneous star formation burst has a spectral slope in this range deviating by only 13%, within the errors of their study. Our study depends on a similar assumption about the UV SEDs; in the Appendix, we test its validity given the current understanding of the MOSDEF galaxies. There we demonstrate that the average slopes used in our analysis are not influenced by SED variations significantly compared with the other errors in the results. Furthermore, limits we place on the sSFR in Section 3.4.1 make the sSFR distribution between the two metallicity samples similar. Therefore, any potential uncertainty would affect the two metallicity curves similarly, and would not affect the results in terms of comparing the attenuation curve of the low- and high-metallicity samples.

In summary, the average attenuation curve for our low-metallicity sample agrees well with the prototypical curve for low-metallicity galaxies from the SMC. Based on the errors induced by measurement uncertainties alone, it is unlikely that the Calzetti/high-metallicity curve applies to the low-metallicity sample on average. The formal significance of this result of \( \sim 3\sigma \) is probably understated, because it is likely that the derived uncertainty is amplified by intrinsic scatter in the curve among the low-metallicity galaxies.

4.2. Variations in the UV Extinction Bump

In this section, we fix the shape of the attenuation curve to those derived in the previous section (Section 4.1) and investigate the presence of a UV extinction bump in the data. We refit the effective attenuation curves, this time by adding a Drude function to the best-fit polynomials from the previous section (Equation (4)).

In Figure 4, we show the fit residuals (data–best-fit model) with and without a UV bump for the two metallicity bins. The high-metallicity curve is significantly improved when a UV bump is added, given that the residuals of the fit including a bump are consistent with zero within \( 2\sigma \). On the other hand, a bump with similar strength as the high-metallicity bump is ruled out by \( \sim 3\sigma \) in the low-metallicity curve. The low-metallicity fit without a bump shows residuals consistent with zero within \( 1\sigma \).

To constrain the strength of the UV bump in the high-metallicity bin, we fit the effective attenuation curve of all galaxies with \( 12 + \log(O/H) > 8.5 \) in our sample with the C00 effective curve \( (k_{\lambda}-R_{\lambda}) \) and a Drude profile, leaving the amplitude of the bump as a free parameter. For this part, we remove the previous restrictions on the sSFR and \( \tau_b \) to be matched to the low-metallicity distributions. The total sample consists of 83 galaxies. We find that the bump amplitude for the high-metallicity sample is \( E_0 = 1.53^{+0.33}_{-0.37} \) shown in the right panel of Figure 3. For comparison, the MW bump amplitude is \( E_0 = 3.3 \) (Fitzpatrick 1999). The relative strength found here agrees with that reported by Buat et al. (2011) and is not significantly different from the reports by Noll et al. (2009), Kriek & Conroy (2013), Salim et al. (2018), and Battisti et al. (2020).

4.3. Total Attenuation Curves

The effective attenuation curves \( (k_{\lambda}-R_{\lambda}) \) derived in this work can be approximated by the SMC curve for the low-metallicity
The residual of the best-fit effective attenuation curve ($f_{\text{Drude}}$-model) with (orange) and without (blue) a Drude profile UV bump for the low- and high-metallicity samples in the left and right panels, respectively. The shaded regions reflect the error in the fit given the measurement uncertainties of the input flux densities. The black horizontal line shows zero residual. The high-metallicity sample is best fit with a UV bump, while no bump is indicated for the low-metallicity sample by $\sigma > 3\sigma$.

The total attenuation curves for the two metallicity subsamples, separated at $12 + \log(O/H) = 8.5$, corresponding to $M_* \sim 10^{10.4} M_\odot$. The high-metallicity curve (violet) is estimated as the Calzetti et al. (2000) effective curve with a UV bump with $E_b = 1.53$ (Equation (4)) at $\lambda < 6000$Å and the Reddy et al. (2015) curve at $\lambda > 6000$Å. The low-metallicity curve is estimated as the Gordon et al. (2003) curve without a UV bump at $\lambda < 6000$Å and the Reddy et al. (2015) curve at $\lambda > 6000$Å. The Gordon et al. (2003) SMC curve lies largely underneath our low-metallicity curve. In both the high- and low-metallicity curves, $R_V = 2.505$.

To compare our curves to the total attenuation curves ($k_\lambda$) from other studies, we need to assume an $R_V$ value and a functional form for the long-wavelength ($\lambda > 0.60$ μm) part of the curve. The long-wavelength shape of the curve is dominated by diffuse dust in the ISM and less affected by the dust grain properties and dust-star geometry effects around massive stars. Similarly, in the absence of IR data, the best way of determining $R_V$ is by extrapolating the curve to long wavelengths.13 As the sample used in this study and that of R15 are from the same MOSDEF parent sample and overlap with each other to a large extent, we take the shape of the long-wavelength ($\lambda > 0.60$ μm) curve and $R_V = 2.505$ of the R15 curve to calculate the total attenuation curve. The $R_V$ is determined by setting a limit condition of $k_\lambda = 0$ at $\lambda = 2.85$ μm. Extrapolating the curve to $k_\lambda \to \infty$ results in $R_V = 2.672$, and extrapolating it to $\lambda = \infty$ with a functional form of $1/\lambda$ results in $R_V = 2.942$ (Reddy et al. 2015). The inconsistency among different values reflects the uncertainty in determining $R_V$ by extrapolating the attenuation curve to near-IR wavelengths, as the curve is not constrained at $\lambda > 2$ μm. For the rest of this work, we adopt $R_V = 2.505$, because it requires the least amount of extrapolation. The total attenuation curves, shown in Figure 5, are

\[
k(\lambda) = -2.659(−2.156 + 1.509 x − 0.198 x^2 + 0.011 x^3) + 1.53 \frac{x^2}{(x^2 - x_0^2)^2 + x^2 x_0^2} + 2.505,
\]

where $x = 1/\lambda$ in μm$^{-1}$, and the central wavelength ($x_0$) and width ($\gamma$) of the UV extinction bump are the MW values of 4.59 and 0.922 μm$^{-1}$, adopted from Fitzpatrick & Massa (2007).

Owing to the mass–metallicity relation (e.g., Tremonti et al. 2004), we may attribute our low- and high-metallicity curves to low- and high-mass galaxies, respectively. The variation of the attenuation curve with mass has been a controversial topic in the literature. While Salmon et al. (2016) did not find any correlation between stellar mass and the slope of the curve or the strength of the UV bump, Zeimann et al. (2015) concluded that the UV slope of the attenuation curve increases with increasing mass (but did not find a correlation with the UV bump strength), and attributed the trend to dust-star geometry. The slopes found in Zeimann et al. (2015), over the mass range of $\log(M_*/M_\odot) = 7.2–10.2$, were consistently lower than the C00 slope (and the slopes found in this study). On the other hand, Reddy et al. (2018a) found that the slope of the curve increases with decreasing mass. In this work, extrapolating from the mass–metallicity relation, we see a similar trend to that of Reddy et al. (2018a), such that the high-mass galaxies have shallower attenuation curves (and stronger UV bumps) compared to low-mass galaxies. We mainly attribute this trend

13 The most direct way of determining $R_V$ is by using IR data and implementing energy balance between the absorbed and re-emitted light (Calzetti et al. 2000). However, given the large uncertainties in current IR measurements of high-redshift galaxies (using Spitzer and Herschel), inferring $R_V$ is still a challenging task and beyond the scope of this paper.
to the differences in dust grain properties of low- and high-metallicity galaxies (discussion in Section 5.1).

The metallicity division of our two samples, $12 + \log(O/H) = 8.5$, corresponds to a stellar mass of $M_*/M_\odot \sim 10^{10.4}$, according to the MOSDEF mass–metallicity relation for the same [N II]/Hα metallicity indicator from Table 1 of Sanders et al. (2018). However, we note that the cut in metallicity does not correspond to a clean cut in stellar mass, owing to the large scatter in the mass–metallicity relation (see Figure 2 in Sanders et al. 2018).

5. Discussion and Implications

In this section, we review some of the implications of the attenuation curves derived in this study. First, in Section 5.1, we discuss how different dust grain properties and dust-star geometry may explain the observed variations in the UV attenuation curve as a function of metallicity. We compare the SFRs calculated using our metallicity-dependent curves with the SFR(Hα/Hβ) in Section 5.2. Section 5.3 shows how a UV extinction bump may affect the photometry of high-redshift galaxies, and hence the measurements of the UV continuum slope. Lastly, in Section 5.4, we present the comparison of stellar reddening ($E(B-V)$), derived from the UV slope and assuming our new attenuation curves, with gas reddening, derived from Balmer nebular lines.

5.1. Dust Grains and Geometry

The UV slope of the curve—A steep rise in the UV extinction can be produced by varying the dust grain size distribution and/or grain composition. Small grains are shown to produce steep extinction curves (Hou et al. 2017), hence an environment with shocks or intense radiation that shatters dust grains and produces small grains can result in a steep UV rise (Gordon et al. 1997). The other possibility is a lower fraction of small carbonaceous to small silicate grains (Weingartner & Draine 2001a), which may result from delayed carbon enrichment from AGB stars (Zhukovska & Henning 2013) or more efficient destruction of small carbonaceous grains relative to small silicate grains by supernovae (Hou et al. 2016). Such environments may be more common in the turbulent ISM of actively star-forming galaxies at $z \sim 2$ and in lower metallicity galaxies that have preferentially younger ages and also more intense radiation (Sanders et al. 2016; Strom et al. 2018). Also, the molecular fraction (ratio of molecular to total gas mass) is a function of metallicity, such that the low-metallicity galaxies have fewer molecular clouds (e.g., Krumholz et al. 2009; Fumagalli et al. 2010). Therefore, the decreased gas and dust shielding from UV radiation in low-metallicity galaxies can provide a more favorable environment for shattering large grains and hence, a steeper UV attenuation curve.

Radiative transfer effects, such as a higher dust column density, turbulent or clumpy ISM (instead of homogeneous), and a geometry with a mixture of stars and dust (as opposed to a screen-shell of dust), generally result in flatter attenuation curves and weaker bump strengths (Witt & Gordon 2000; Seon & Draine 2016; Popping et al. 2017). However, an age-dependent attenuation, in which young stars are embedded in their more-than-average dusty birth clouds and are more attenuated than older stars, can explain a steep UV attenuation curve (Inoue 2005; Panuzzo et al. 2007; Tress et al. 2018, 2019). An age-dependent attenuation model suggests that older stars, dominating the emission at long wavelengths, are subject to less attenuation compared to younger stars that dominate the emission at short wavelengths, resulting in a steep attenuation curve. Similar trends have also been seen at $z \sim 2$, where young galaxies show a lower IR-to-UV luminosity at a given UV continuum slope, suggesting a steeper attenuation curve (Reddy et al. 2010, 2012a, 2018a) or the stacks of young galaxies indicate a better agreement with IR+UV SFRs if a steeper than C00 curve is used to correct the observed UV SFRs (Shivaei et al. 2015b). Inoue (2005) also attributed a steep attenuation curve slope to a decreased optical thickness in galaxies with lower dust-to-gas mass ratios. Therefore, we expect that given our low-metallicity galaxies are younger14 (Gallazzi et al. 2005) and expected to have lower dust-to-gas ratios compared to higher metallicity galaxies (Rémy-Ruyer et al. 2014), they would show a steeper UV attenuation curve. In this study, we cannot robustly distinguish the effect of different grain properties from that of age-dependent geometries on the slope of the curve.

The UV extinction bump—Our data show an unambiguous signature of a UV bump in the attenuation curve of the high-metallicity sample and rule out a bump of similar strength in the low-metallicity curve by $\sim 3\sigma$. Theoretically, the strength of the bump in an attenuation curve (assuming the underlying extinction curve has a bump) correlates with the UV slope of the curve, such that the radiative transfer effects that suppress the bump (e.g., high optical depth or clumpy ISM) also make the curve flatter (Witt & Gordon 2000; Seon & Draine 2016). This effect has also been indicated in observations (Kriek & Conroy 2013; Salim et al. 2018). However, we see the opposite of this trend: the high-metallicity curve is shallower but has a stronger bump compared to the low-metallicity curve. This result suggests that the absence of a significant bump in the steep low-metallicity curve is a reflection of dust grain properties, rather than radiative transfer effects (which includes the dust-star geometry effects). Moreover, the bump strength observed in the high-metallicity curve is likely a lower limit on the intrinsic bump strength in the extinction curve of high-metallicity galaxies, owing to the same argument that the observed bump is likely suppressed due to geometrical effects.

A significant difference between the two metallicity samples is the change of the intensity of the mid-IR aromatic band at 7.7 $\mu$m, attributed to emission from PAH molecules. The 7.7 $\mu$m luminosity to total SFR ratio changes from $\sim 35 \pm 9$ (in units of $10^8 L_{\odot}/M_\odot$yr$^{-1}$) in the high-metallicity sample to $\sim 6 \pm 1$ in the low-metallicity sample (see Table 1 and Figure 3 of Shivaei et al. 2017). The decrease in the PAH intensity can be caused by either preferential destruction of PAHs by the harder ionizing radiation of low-metallicity environments or a delayed enrichment of PAHs in young (and low-metallicity) galaxies (e.g., Dwek 2005; Draine et al. 2007; Smith et al. 2007; Galliano et al. 2008). The trend between the UV bump strength and metallicity in this work combined with the trend of the PAH intensity with metallicity from Shivaei et al. (2017) may suggest a correlation between the strength of the UV extinction bump and the PAH emission intensity. PAHs have been suggested as the origin of the UV extinction bump in 14 Average ages of our low- and high-metallicity samples, derived from SED fitting (Section 3.3) are log(age/yr) = 8.67 ± 0.02 and 8.87 ± 0.03, respectively, with a large scatter of ~0.3 dex. We note that the ages inferred from SED fitting assuming rising star formation histories are ambiguous (e.g., Reddy et al. 2012b).
theoretical studies (Li & Draine 2001) and lab experiments (Joblin et al. 1992).

5.2. SFR Comparison

SFR is a key parameter to describe galaxies and their cosmic evolution. The most widely used SFR indicator at high redshifts is UV stellar continuum, as it redshifts to longer wavelengths that are easily accessible from the ground, and can be detected down to lower luminosities given the higher sensitivity of optical-near-IR instruments compared to that of the far-IR observatories. However, the UV is highly affected by dust attenuation and SFRs derived from fitting SED models to the photometry are sensitive to the assumed attenuation curve. In this section, we compare SED-inferred SFRs, assuming our metallicity-dependent curves and the SM and C00 curves, with independently derived SFRHα,Hβ.

The Hα nebular line is a robust indicator of recent star formation once accurately corrected for attenuation, even for highly star-forming galaxies at $z \sim 2$ (e.g., Muzzin et al. 2010; Reddy et al. 2010; Shivaei et al. 2015b, 2016). Our MOSDEF sample has 441 non-AGN targets with spectroscopic Hα and Hβ line measurements (signal-to-noise ratio $>3\sigma$) at $z = 1.4-2.6$. We correct Hα luminosity for attenuation using the Balmer decrement and assuming the Cardelli et al. (1989) MW curve (see Reddy et al. 2015; Shivaei et al. 2015a, 2016). The MW curve is preferable for the extinction correction of nebular lines, as it is derived based on the line-of-sight measurements of H II regions (Calzetti et al. 1994; Wild et al. 2011b; Salim & Narayan 2020) and shown to be an accurate representation of nebular attenuation curve at $z \sim 2$ (N. Reddy et al., in preparation).

We select galaxies that have metallicities from [N II], which results in a sample of 271 galaxies (the additional criteria that were imposed to derive the attenuation curve in Section 3.4 are not used here), and compare the SFRs for the two subsamples of low- and high-metallicity galaxies separated at $12 + \log(O/H) = 8.5$ (average $(12 + \log(O/H))$ of 8.4 and 8.6, respectively). To determine SFRs from dust-corrected Hα luminosities, we use $L(H\alpha)$-to-SFR conversions derived from BPASSv2.2 SPS models (Stanway & Eldridge 2018), assuming a Chabrier IMF with an upper mass cutoff of 100 $M_\odot$ and $Z_\odot = 0.02$ and 0.004 for the high- and low-metallicity samples, respectively (Theios et al. 2019). The solar metallicity ($Z_\odot = 0.02$) conversion is only different by 0.05 dex from the conversion factors of Hao et al. (2011) and Kennicutt & Evans (2012), once corrected for IMF differences (see Table 2 of Theios et al. 2019).

To synthesize the unattenuated UV continua, we use the FAST SED fitting code (Kriek et al. 2009), with the library of Bruzual & Charlot (2003) stellar population synthesis models, solar ($Z = 0.02$) and subsolar ($Z = 0.004$) stellar metallicities for the high- and low-metallicity samples, respectively, a Chabrier (2003) IMF, and delayed exponentially declining SFH (SFR \sim t exp(-t/\tau), where $t$ is the age and $\tau$ is the exponential timescale). The $A_V$ is allowed to vary between 0 and 4 in increments of 0.1. Using the BPASS binary models instead of the Bruzual & Charlot (2003) models would not significantly alter the SED-inferred SFRs, as the effect of binary evolution is much less significant on UV continuum compared to the nebular lines (e.g., Stanway et al. 2016; Shivaei et al. 2018; Theios et al. 2019). Figure 6 shows the results of the SED-inferred SFRs assuming various attenuation curves compared with the SFRHα,Hβ. The SFRs from the low- and high-metallicity curves agree well with the SFRHα,Hβ in both of the samples. The C00 curve tends to overestimate the SFR in the low-metallicity sample, but agrees well with the SFRHα,Hβ in the high-metallicity sample. The SMC curve with a solar metallicity stellar population underestimates the SFR in the high-metallicity sample. We do not show the results of the SMC curve with subsolar stellar metallicity for the low-metallicity sample, as the shape of the low-metallicity curve in the UV is identical to the SMC curve.

In conclusion, this study suggests that on average, a steep attenuation curve, similar to the SMC curve, is more applicable to the low-metallicity (and hence low-mass) high-redshift galaxies, while a shallower C00 curve is preferred for the higher metallicity/mass galaxies. The metallicity division we used in this study is at $12 + \log(O/H) = 8.5$ and corresponds to $M_\star \sim 10^{10.4} M_\odot$. We caution that the cut in metallicity should not be taken as a clear cut in stellar mass, due to the scatter in the mass–metallicity relation (Sanders et al. 2018). We note that SFR calculations are also affected by parameters other than the attenuation curve, such as stellar metallicity, stellar multiplicity, and the shape of the IMF. However, we showed in Shivaei et al. (2018) that the variations between the SFRHα,Hβ and UV-inferred SFRs (which is the same as our SED-inferred SFRs within the uncertainties) are on average dominated by the uncertainties in the adopted attenuation curve, compared to those associated with stellar metallicity, multiplicity, and IMF.

5.3. UV Continuum Slope

The UV continuum slope ($\beta$) is commonly used as a tracer of the attenuation of the stellar continuum, particularly at high redshifts as the rest-frame UV becomes accessible to optical/near-IR instruments. The importance of accurate $\beta$ measurements and the assumed attenuation curve in correcting the observed UV SFRs for dust attenuation has been demonstrated in many previous studies (e.g., Calzetti et al. 1994; Meurer et al. 1999; Reddy et al. 2006, 2015, 2018a; Boquien et al. 2012; Kriek & Conroy 2013; Shivaei et al. 2015a, 2018; Popping et al. 2017; Safarzadeh et al. 2017; Fudamoto et al. 2020). The UV slope is measured by fitting a linear function to $\log(f_\lambda)$ versus $\log(\lambda)$ at rest frame 1260–2600 Å, a range that includes the UV 2175 Å bump.

The presence of a UV bump affects medium-band photometry and the corresponding $\beta$ measurements. As an example, we look into the effect of the bump for $z \sim 2$ observations. At $z = 1.8$, for a set of G, V, R, and I photometric bands, the UV extinction bump falls into the R band, while the I band covers the continuum red-ward of the bump. Assuming a UV bump similar to that of our high-metallicity curve, the UV slope derived from G, V, and R bands would be underestimated compared to the UV slope derived from the photometry including the I band by $\Delta \beta = 0.2, 0.6$, and 0.8 for $A_V$ of 0.2, 0.5, and 0.7, respectively. With all four bands, it is possible to estimate both the UV slope and the strength of the bump. This is a similar effect to that demonstrated for James Webb Space Telescope (JWST)/NIRCam photometry of higher redshift galaxies in Figure 7, as explained below.

Although the high-metallicity galaxies (with metallicities of $\sim Z_\odot$) are rare at high redshifts, they still exist, for example in the case of high-redshift quasars (Jiang et al. 2007; Juarez et al. 2009).
or luminous dusty galaxies (Nagao et al. 2012; De Breuck et al. 2019). To illustrate this effect, we therefore show an example with the JWST NIRCam filters for galaxies at $z \sim 6–10$. Depending on the redshift and the available set of photometry, similar results can be obtained on lower redshift galaxies with shorter wavelength medium-band filters.

We model the intrinsic (dust-free) spectrum of a galaxy to be a power-law function of wavelength with a given intrinsic power ($\beta_0$). The exact choice of $\beta_0$ is irrelevant for our purpose, as we are only interested in the difference between the multiple $\beta$ estimates (hence, $\beta_0$ cancels out in the equations). The intrinsic $f_\lambda$ is attenuated assuming four $A_V$ values ($A_V = 0.1, 0.4, 0.7, 1.0$) and two attenuation curves: (1) the high-metallicity curve with a bump with $\sim 0.5$ the strength of the MW bump, and (2) the same curve without the bump, which is identical to the R15 curve. We calculate $\beta$ through the JWST/NIRCam wide (F115W, F150W, F200W, F277W) and medium-band filters (F140M, F162M, F182M, F210M, F250M) filters for targets at $z = 6.3–10.0$ with different $A_V$ values, assuming the two attenuation curves with and without a bump (Figure 7). Similar results are obtained when fitting the rest-frame UV photometry of lower redshift galaxies from HST and ground-based optical telescopes (e.g., Popping et al. 2017; Tress et al. 2018).

The upper panel of Figure 7 shows the difference in the measured and true $\beta$ as a function of redshift and $A_V$, where $\beta_{\text{measured}}$ is calculated from the high-metallicity curve with a bump and $\beta_{\text{true}}$ is calculated from the same curve but without the bump. The measured $\beta$ often underestimate the true $\beta$ (underestimates the true reddening) as the UV 2175 Å feature moves through the photometric filters. The UV slope calculated in the case of the curve with a bump becomes progressively bluer (smaller $\beta$) as the longest-wavelength filter used in the calculations moves into the UV 2175 Å feature. Once a filter red-ward of the bump is added, the $\beta$ from the curve with a bump gets closer to the true (no-bump) value (notice the jumps at $z \sim 7$ and 8.5 in Figure 7, top). This effect is also illustrated in the lower panel of Figure 7 qualitatively, where a linear function fit to the three photometric points, excluding the F210W filter, results in a bluer $\beta$ compared to the fit to four filters, which captures the continuum on both sides of the UV 2175 Å feature. A fit to only two bands, where one is affected by the UV 2175 Å feature, underestimates $\beta$.

As the UV 2175 Å feature is very broad, if present, it would affect the NIRCam wide-band photometry as well (dotted lines in Figure 7). The disadvantage of using the wide-band filters is poorer sampling of the UV continuum window (only two or three filters at rest frame 1200–2600 Å), which makes it impractical to mask out the filters that are sensitive to the UV 2175 Å feature.

An underestimated (overestimated) $\beta$ at a given $L$(IR)/$L$(UV) would resemble a shallower (steeper) attenuation curve in the IRX–$\beta$ relation (relation between $L$(IR)/$L$(UV) and $\beta$) and results in incorrect estimates of dust attenuation. For example, a galaxy that follows the Meurer et al. (1999) IRX–$\beta$ relation has a $\beta = -1.0$ at IRX = 10. If the measured $\beta$ of this galaxy is underestimated by $\sim 0.5$ ($\beta_{\text{measured}} \sim -1.5$) due to the presence of a UV bump similar to the one found in the high-metallicity curve, the observed location of the galaxy will be shifted to the left of the Meurer et al. (1999) IRX–$\beta$ locus. As a result, this shift may be misinterpreted as bluer $\beta_0$ (for the same attenuation curve) or complex dust-star geometries (e.g., Popping et al. 2017; Reddy et al. 2018a).

The relationship between $\beta$ and stellar continuum color excess ($E(B-V)_{\text{stellar}}$) assuming the high-metallicity attenuation curve, excluding the bump, and an intrinsic $\beta$ of $\beta_0 = -2.44$ (corresponding to a stellar population with solar metallicity and constant star formation for longer than 100 Myr) is

$$\beta = -2.44 + 4.75 \times E(B-V)_{\text{stellar}}. $$

The $\beta = E(B-V)_{\text{stellar}}$ relationship for the steeper low-metallicity curve and a bluer intrinsic $\beta$ of $\beta_0 = -2.62$, which is shown to be more applicable to the low-mass/metallicity galaxies at these redshifts (Steidel et al. 2016; Reddy et al. 2018a), is

$$\beta = -2.62 + 11.47 \times E(B-V)_{\text{stellar}}. $$

Different assumptions for the intrinsic $\beta_0$, which depends on the stellar metallicity of the underlying stellar populations, would change the inferred $\beta$ values systematically. Our $\beta_0$
The effect of the presence of a bump in measuring $\beta$ for high-redshift galaxies with JWST/NIRCam filters. Top: difference in the measured and true UV slopes ($\beta$) in the presence of a bump similar to the high-metallicity curve bump, as a function of redshift (horizontal axis) and different $A_V$ lines (with shades of gray). $\beta$ is calculated by fitting to the JWST/NIRCam medium-band fluxes (circles and solid lines) and wide-band fluxes (dashed lines) at rest frame 1260–2600 Å as $\log(f_{\lambda}) \propto \beta \log(\lambda)$. In the case of the medium-band filters, the absence of photometric coverage of the continuum longward of the bump ($\lambda > 2400$ Å) affects the linear fit to $\log(f_{\lambda}) - \log(\lambda)$ and underestimates the UV slope (i.e., smaller $\beta_{\text{true}}$ compared to $\beta_{\text{measured}}$). The jumps at $z \sim 7$ and 8.5 in the medium-band filters occur when a filter is added redward of the UV bump. This effect is demonstrated in the lower panel. The situation with wide-band filters is similar, but note that the wide-band filters have a poorer sampling of the UV slope window, with only two filters at $z = 6.3$–6.7 and 8.3–9.7 and three filters in between. Bottom: difference in the slope ($\beta$) of the linear fit to $\log(f_{\lambda}) - \log(\lambda)$ in three cases where the continuum on the both sides of the bump is covered (orange line) or not (blue and green lines). The gray curve is the spectrum of a $z = 7.5$ galaxy with intrinsic flux of $f_{\lambda} \propto \lambda^{-2.4}$, attenuated assuming the high-metallicity curve and $A_V = 0.7$. The circles are the calculated photometry in JWST/NIRCam filters shown at the bottom. The lack of photometric coverage of the continuum biases the measured $\beta$ and in this case, resulting in a bluer (steeper) $\beta$. This effect is shown quantitatively in the upper panel. The lack of any coverage blue-ward of the bump would result in a redder (shallower) $\beta$.

assumptions here are motivated by previous $z \sim 2$ studies in the literature, as mentioned before.

### 5.4. Nebular versus Stellar Reddening

Color excess, or reddening, is the difference between the total attenuation at $B$ and $V$ bands, $E(B - V) \equiv A_B - A_V$. In a simple star-dust geometry of a screen of dust in front of the stars, $E(B - V)$ represents the thickness of the dust screen (i.e., the dust column density). The color excess measured from the continuum emission (e.g., using UV continuum slope $\beta$ or $\text{SED}$ fitting to the photometry) shows the reddening of the stellar continuum, while the color excess derived from the nebular emission lines indicates the nebular (gas) reddening. If all of the stars in a galaxy are subject to the same dust column densities, the stellar and nebular reddenings should be similar (Erb et al. 2006; Reddy et al. 2010; Pannella et al. 2015; Shivaei et al. 2015b; Puglisi et al. 2016). However, multiple studies have shown a higher nebular reddening compared to the stellar reddening in star-forming galaxies (Calzetti et al. 1994, 2000; Garn et al. 2010; Mancini et al. 2011; Wild et al. 2011a; Kashino et al. 2013; Price et al. 2014; Reddy et al. 2015; Battisti et al. 2016; Buat et al. 2018; Qin et al. 2019; Theios et al. 2019). We compile a number of these determinations in Table 1. The simplest physical interpretation of a differential attenuation is a two-component dust-star model, where all stars experience a modest attenuation due to the diffuse ISM dust, but the young and massive stars that give rise to the nebular lines are embedded in their dense and dusty birth clouds (e.g., Calzetti et al. 1994; Charlot & Fall 2000).

![Figure 7](image-url)

| $E(B-V)$ (Observed) | Redshift | Reference |
|---------------------|----------|-----------|
| $E(B-V)$ (Calculated) | $z$ = 7.5, $A_V = 0.7$ | 3 filters | $f_{\lambda}$ arbitrary units | $\log(\lambda_{\text{observed}}/\mu\text{m})$ | 2.0 | 2.7 | 3.4 | 4.1 | 4.8 | 5.5 | 6.2 | 6.9 | 7.6 | 8.3 | 9.0 | 9.7 | 10.4 | 11.1 | 11.8 | 12.5 | 13.2 | 13.9 | 14.6 | 15.3 | 16.0 | 16.7 | 17.4 | 18.1 |
| $f_{\lambda}$ (arbitrary units) | $\log(\lambda_{\text{observed}}/\mu\text{m})$ | 0.10 | 0.15 | 0.20 | 0.25 | 0.30 | 0.35 | 2.0 | 2.7 | 3.4 | 4.1 | 4.8 | 5.5 | 6.2 | 6.9 | 7.6 | 8.3 | 9.0 | 9.7 | 10.4 | 11.1 | 11.8 | 12.5 | 13.2 | 13.9 | 14.6 | 15.3 | 16.0 | 16.7 | 17.4 | 18.1 |

![Table 1](table-url)

| $E(B-V)$ (Observed) | Redshift | Reference |
|---------------------|----------|-----------|
| $E(B-V)$ (Calculated) | $z$ = 7.5, $A_V = 0.7$ | 3 filters | $f_{\lambda}$ arbitrary units | $\log(\lambda_{\text{observed}}/\mu\text{m})$ | 2.0 | 2.7 | 3.4 | 4.1 | 4.8 | 5.5 | 6.2 | 6.9 | 7.6 | 8.3 | 9.0 | 9.7 | 10.4 | 11.1 | 11.8 | 12.5 | 13.2 | 13.9 | 14.6 | 15.3 | 16.0 | 16.7 | 17.4 | 18.1 |

**Table 1**

| $E(B-V)$ (Observed) | Redshift | Reference |
|---------------------|----------|-----------|
| $E(B-V)$ (Calculated) | $z$ = 7.5, $A_V = 0.7$ | 3 filters | $f_{\lambda}$ arbitrary units | $\log(\lambda_{\text{observed}}/\mu\text{m})$ | 2.0 | 2.7 | 3.4 | 4.1 | 4.8 | 5.5 | 6.2 | 6.9 | 7.6 | 8.3 | 9.0 | 9.7 | 10.4 | 11.1 | 11.8 | 12.5 | 13.2 | 13.9 | 14.6 | 15.3 | 16.0 | 16.7 | 17.4 | 18.1 |

The stellar reddening derived from UV slope and Equations (8) and (9) closely follows the reddening derived from SED model fitting, using the same attenuation curves.
inferences, we do not set the negative $E(B-V)$’s to zero.\footnote{Our main results will be unaffected by setting the cases with $E(B-V) < 0$ to zero (as has been done in some studies). This condition will systematically increase the average $E(B-V)_{\text{neb}}$ values, as expected, but does not change any of the main conclusions, as the negative $E(B-V)_{\text{neb}}$ values are distributed over all metallicities and masses and are not systematically clustered at a certain metallicity or mass. By setting the negative nebular reddenings to zero, the average reddening ratios $\langle E(B-V)_{\text{neb}},E(B-V)_{\text{stellar}} \rangle$ for the low- and high-metallicity bins will be $2.81 \pm 0.17$ and $1.58 \pm 0.15$, respectively, and for the low- and high-mass bins will be $2.30 \pm 0.14$ and $2.52 \pm 0.31$, respectively.}

As seen in Figure 8(a), there are no corresponding negative values in the stellar reddenings, as in our sample the measured $\beta$ is always larger than the assumed intrinsic $\beta_0$ in Equations (8) and (9).

The Pearson correlation coefficient in Figure 8(a) indicates a correlation between the nebular and stellar reddening in our sample with $\rho = 0.2$ and a $p$-value of $\sim 10^{-4}$. The differential attenuation relation of $E(B-V)_{\text{neb}} = 2.27 \, E(B-V)_{\text{stellar}}$, suggested by Calzetti et al. (2000), and the unity relation are also shown in Figure 8(a). The large scatter in the relation (standard deviation of 2.43 from the mean) makes it difficult to favor one relation over the other; however, the majority of the galaxies show $E(B-V)_{\text{neb}} > E(B-V)_{\text{stellar}}$, with an average of $E(B-V)_{\text{neb}} = (2.11 \pm 0.15) E(B-V)_{\text{stellar}}$ for the full sample.

The derived nebular reddenings do not significantly change under a different assumption of the dust curve, as $E(B-V)_{\text{neb}}$ depends on the shape of the dust curve at H\textbeta and H\alpha wavelengths ($E(B-V)_{\text{neb}} = \frac{2.5}{\log(\text{H}\alpha/\text{H}\beta)} \log(\text{H}\alpha/\text{H}\beta)$) and the shapes of various curves, such as MW LMC, SMC, and C00, at these wavelengths are very similar to each other. The nebular reddening, as mentioned before, is more affected by measurement uncertainties and statistical noise. On the other hand, the derived stellar reddening depends strongly on the assumption of the attenuation curve and the intrinsic $\beta_0$, smaller stellar $E(B-V)$’s are obtained if an SMC curve is assumed for high-metallicity galaxies (e.g., as assumed in Figure 9 of Theios et al. 2019). In this study, we have found that a combination of two different attenuation curves is more applicable to galaxies over a wide range of metallicities, and hence, we use the Equations (8) and (9) to derive the stellar reddenings for $12 + \log(O/H) > 8.5$ and $<8.5$, respectively.

We further investigate the ratio of the nebular-to-stellar reddening (the reddening ratio) as a function of galaxy parameters in Figure 8. We calculate the average and standard deviations of the reddening ratio in different ranges of gas-phase metallicity, mass, and SFR, shown with horizontal lines and shaded regions. In gas-phase metallicity, we divide the sample at $12 + \log(O/H) = 8.5$, the same metallicity limit that was used in deriving the two attenuation curves. The stellar...
mass and SFR limits are calculated based on the MOSDEF mass–metallicity relation (Sanders et al. 2018) and MOSDEF SFR-mass relations for Hα and SED SFRs (Shivaei et al. 2015a) at the metallicity of $12 + \log(O/H) = 8.5$.

As shown in Figure 8(d), the reddening ratio correlates with SFR$_{H\alpha,H\beta}$ ($\rho = 0.6$, p-value <10$^{-5}$). However, the positive correlation may be due to the degeneracy between the two parameters, as $E(B-V)_{\text{neb}}$ is used to correct SFR$_{H\alpha,H\beta}$ for dust attenuation. The correlation disappears when SED SFR is used instead of SFR$_{H\alpha,H\beta}$ (panel (e)), and instead, the reddening ratio shows a large scatter at low SED SFRs. The SED SFR is also indirectly related to the reddening ratio, as the $E(B-V)_{\text{stellar}}$ correlates tightly with the SED-inferred $E(B-V)$, which determines the dust correction in SED SFR. The modest correlation between the reddening ratio and sSFR (SFR$_{H\alpha,H\beta}$ /$M_*$, panel (f)) may also be a consequence of the degeneracy between $E(B-V)_{\text{neb}}$ and SFR$_{H\alpha,H\beta}$. Due to the aforementioned degeneracies, and the inconsistent results based on Hα and SED SFRs, we do not draw robust conclusions regarding the correlation between the reddening ratio and SFR or sSFR. Disentangling the relation between the reddening ratio and SFR requires an independent SFR indicator, such as IR. The average reddening ratio, shown with the magenta line in panel (f), is $E(B-V)_{\text{neb}} = (2.11 \pm 0.15)E(B-V)_{\text{stellar}}$, with a large scatter shown with the magenta region (standard deviation of 2.43). The average of the reddening differences can also be expressed as $(E(B-V)_{\text{neb}} - E(B-V)_{\text{stellar}}) = 0.18 \pm 0.02$. Keeping this conversion in mind, our Figures 8 (a) and (d) agree well with Figures 16 and 17 of Reddy et al. (2015).

Mass and metallicity are derived independently from the two redenning ratios. Stellar mass is inferred from the best-fit SED model (Section 3.3), and is determined by the normalization of the SED model relative to the photometry. The gas-phase metallicity is derived from the ratio of [N II] to Hα. Although metallicity has the uncorrected Hα line luminosity in common with the nebular reddening, the two parameters are not strongly degenerate.

The trend of the reddening ratio with metallicity is interesting (Figure 8(b)). Objects with high metallicity tend to have a similar reddening for line and continuum photons, $E(B-V)_{\text{neb}}/E(B-V)_{\text{stellar}} = 1.38 \pm 0.19$\textsuperscript{17}, with a standard deviation of $\sigma = 1.91$. In comparison, the low-metallicity galaxies show an increase in the reddening ratio, $E(B-V)_{\text{neb}}/E(B-V)_{\text{stellar}} = 2.60 \pm 0.20$, and an increased scatter of $\sigma = 2.59$. This trend is consistent with the findings of Kashino et al. (2013), Pannella et al. (2015), and Puglisi et al. (2016), who found similar nebular and stellar redenning ratios, based on samples in which a considerable majority of galaxies have log($M_*/M_\odot$) > 10.4. As discussed in Section 4.3, these galaxies would fall within our high-metallicity bin. Most of the other studies cited earlier are extended to significantly lower masses (Garn et al. 2010; Mancini et al. 2011; Wild et al. 2011a; Price et al. 2014; Battisti et al. 2016; Qin et al. 2019), thus accounting for the larger values they obtain for $E(B-V)_{\text{neb}}/E(B-V)_{\text{stellar}}$ (∼1.9 – 2.9), consistent with our average high value of $E(B-V)_{\text{neb}}/E(B-V)_{\text{stellar}} = 2.11$ over the full range of metallicities ($12 + \log(O/H) \sim 8.0 – 8.8$).

\textsuperscript{17} This value results from using the appropriate attenuation curve, i.e., $C00$, for the high-metallicity sample; use of the SMC curve would raise this value to correspond more closely with the low-metallicity part of our sample.

We do not see significant correlation between the reddening ratio and stellar mass (Figure 8(c)), in agreement with Reddy et al. (2015), Figure 17. The average reddening ratio is 2.07 ± 0.17 and 2.44 ± 0.34 with a scatter of 2.48 and 2.01, respectively, for the masses below and above log($M_*/M_\odot$) = 10.4, corresponding to the dividing line between the low- and high-metallicity bins (Section 4.3). We suspect that the lack of correlation between the reddening ratio and mass, despite the correlation between the reddening ratio and metallicity, is due to (1) the relatively small number of galaxies in our sample with log($M_*/M_\odot$) > 10.4; and (2) the large scatter in the mass–metallicity relation, particularly when [N II] / Hα is adopted as the metallicity diagnostic (Sanders et al. 2018).

Further insight to the trend between reddening and metallicity is provided in Figure 9 in the left panel. A positive correlation between dust reddening and metal abundance is expected, due to the increase of dust-to-gas mass ratios, as well as the increase of molecular gas fractions, with oxygen abundances (Draine et al. 2007; Leroy et al. 2011). However, contrary to expectation, the correlation between the nebular reddening and metallicity in our sample is weak (Figure 9; Pearson $\rho = 0.08$ with a p-value of 0.17), while the stellar reddening shows a significantly stronger correlation with metallicity ($\rho = 0.68$, p-value <10$^{-5}$). Additionally, at $12 + \log(O/H) < 8.5$, the stellar reddening is lower with a very small scatter $(E(B-V)_{\text{stellar}} = 0.12$, $\sigma = 0.04$) compared to the nebular reddening $(E(B-V)_{\text{neb}} = 0.29$, $\sigma = 0.27$), while at higher metallicities the average and scatter of stellar reddening increase and approach those of the nebular reddening $(E(B-V)_{\text{stellar}} = 0.26$, $\sigma = 0.11$ and $E(B-V)_{\text{neb}} = 0.33$, $\sigma = 0.38$). The reduced scatter of the stellar reddening at low metallicities might be partly affected by the choice of a steeper attenuation curve, which tends to result in lower $\beta$-inferred color excesses (Equation (9)). However, we also see an increase in the scatter of the observed $\beta$ with metallicity in our sample. Further investigation on this correlation is beyond the focus of this paper and will be discussed elsewhere (A. Shapley et al., in preparation).

Pannella et al. (2015) suggested that the close to unity ratio of $E(B-V)_{\text{neb}}/E(B-V)_{\text{stellar}}$ in their high-redshift sample ($z \geq 1.5$, similar behavior seen in Erb et al. (2006), Reddy et al. (2010), and Shivaei et al. (2015b)) is a result of high SFR surface densities (higher SFRs and smaller sizes) of galaxies at $z > 1.5$ compared to local galaxies (e.g., Whitaker et al. 2012b; van der Wel et al. 2014; Rujopakarn et al. 2016; Elbaz et al. 2018). As mentioned before, the high-redshift sample of Pannella et al. (2015) has masses of $M_\alpha \geq 10^{10.5} M_\odot$, consistent with the masses of our high-metallicity sample. In such systems, the high star formation surface density and larger dust-to-gas ratios result in a dense ISM that evidently reddens the stellar continuum photons to a similar degree as the reddening of the nebular photons that emerge from the dense birth clouds of newly born stars. This results in divergence from the two-component dust-star model and hence, $E(B-V)_{\text{neb}} \sim E(B-V)_{\text{stellar}}$. Such an effect is weaker at lower metallicities, due to both the reduced dust-to-gas mass ratios (Rémy-Ruyer et al. 2014) and lower scattering and absorption coefficients of different dust grains that are present in low-metallicity galaxies compared to the high-metallicity ones (Weingartner & Draine 2001a). Hence, at low metallicities, the continuum photons are mainly reddened by the uniformly distributed diffuse dust in the ISM, which is nearly transparent in these galaxies and results in low stellar redenning. Meanwhile, the line photons, originating from the
H II regions, are still heavily obscured as high gas densities are still required for massive star formation, therefore resulting in $E(B - V)_{\text{neb}} > E(B - V)_{\text{stellar}}$ at low metallicities. This situation is illustrated by extinction maps of the SMC (Dobashi et al. 2009), which show a few localized spots of very high extinction in what is otherwise a very low level extinction across the galaxy. The two-component model is preserved in this case because of the finite lifetimes of these birth clouds (Charlot & Fall 2000) and the low ISM absorption once they dissipate.

In this physical picture, the low opacity of the ISM in low-metallicity galaxies outside a small number of actively star-forming regions is consistent with the larger scatter in the nebular-to-stellar reddening ratio at low metallicities ($\sigma = 2.59$) compared to that at high metallicities ($\sigma = 1.90$; shaded regions in Figure 8(b)). A similar trend of decreasing the scatter of the reddening ratio is seen with increasing stellar mass and SED SFR in Figure 8. The large intrinsic scatter in the attenuation curve at low metallicities discussed in Section 4.1.1 is also related to the large scatter at low metallicities in Figure 8(b), both suggesting large galaxy-to-galaxy variations in dust-star geometry at low metallicities with potentially younger ages (see also the discussion in Section 5.1).

A similar trend between the reddenings and metallicity was seen in the $z = 2.0$–2.6 sample of Theios et al. (2019). These authors attributed the trend to the line ratios, such as [N II]/H$\alpha$, being more sensitive to the stellar abundance of Fe, and not the gas-phase oxygen abundance (Steidel et al. 2014; Sanders et al. 2016; Strom et al. 2017). In that scenario, the tight correlation between the stellar reddening and the [N II]/H$\alpha$ ratio is explained by both quantities being closely tied to the spectral shape of the ionizing radiation field produced by the massive stars.

Nebular reddening has a tighter correlation with stellar mass compared to metallicity, with a Pearson $\rho = 0.37$ and a high significance ($p$-value $\sim 10^{-10}$). As a useful empirical relation (as shown in, e.g., Garn & Best 2010; Whitaker et al. 2017; McLure et al. 2018), we fit the reddening versus stellar mass data with a linear function:

$$E(B - V)_{\text{neb}} = 0.26 \log(M_*/M_\odot) - 2.31$$

(10)

$$E(B - V)_{\text{stellar}} = 0.10 \log(M_*/M_\odot) - 0.87$$

(11)

Caution should be taken when using these equations, given the large scatters. The scatter from the best-fit line in the nebular reddening-mass equation is 0.28 and the scatter in the stellar reddening fit is 0.09. The right panel of Figure 9 confirms that the reddening, and hence dust content of galaxies, increases with mass, for both the stellar continuum and the nebular emission. The ratio of the two fits (Equations 10 and 11), i.e., nebular-to-stellar reddening as a function of mass) is shown in Figure 8(c) (orange curve).

In summary, calculating the continuum reddening is highly sensitive to the assumed attenuation curve. We exploit our metallicity-dependent attenuation curves to derive the continuum reddening and compare it to the nebular reddening calculated from Balmer decrement. On average, we observe a differential attenuation, where the line photons are $\sim 2$ times more reddened than the continuum photons. However, the differential attenuation is less significant in the high-metallicity sample compared to low-metallicity galaxies, which is likely due to the higher surface density of very dusty regions that redden both the continuum and nebular photons in high-metallicity galaxies. At low metallicities, where galaxies are also preferentially younger, the enhanced differential attenuation suggests a two-component dust-star model with older stars reddened by the transparent ISM dust and younger stars are embedded in their dust cocoons. In any case, the reddening shows a large scatter at a given mass or metallicity, indicating a large galaxy-to-galaxy variation between the nebular and stellar reddenings.

Using data available at the time, Reddy et al. (2015) found an increasing difference in nebular and stellar reddening with increasing SFR and dust attenuation, similar to the trends we see in Figure 8 with SFR$_{\text{H}\alpha}$, SFR$_{\text{H}2}$ and SFR(SED). Our new analysis suggests that the ratio of the nebular and stellar reddening is smaller at higher gas-phase metallicities (and hence, higher dust
attenuation). This difference in interpretation stems mainly from a direct analysis of $E(B-V)_{\text{H}\beta}/E(B-V)_{\text{stellar}}$ versus gas-phase metallicity, and our use of a gas-phase-metallicity-dependent attenuation curve. Direct observations of dust obscuration, such as from the ratio of IR-to-UV luminosity, should help to clarify the how $E(B-V)_{\text{H}\beta}/E(B-V)_{\text{stellar}}$ is connected to dust content, gas-phase metallicity, stellar mass, and SFR.

We note that our conclusions, by definition, may not hold for IR-selected samples with heavily obscured objects, such as those in the majority of the Atacama Large Millimeter/submillimeter Array (ALMA) extragalactic surveys. Although for this part of the analysis we do not impose the criteria we used for the curve derivation (Section 3.4) and we include galaxies with $\tau_b > 1$, the sample is still selected based on the detection of optical emission lines and is biased against objects that are heavily obscured. In panel (b) of Figure 8 we show the reddening ratio of objects with undetected ($<3\sigma$) H$\beta$ lines (H$\alpha$ is detected) and the full sample of detected-H$\alpha$ galaxies (regardless of detection in H$\beta$) with empty and filled stars, respectively. To derive the Balmer decrement for these galaxies, we normalize the individual spectra to their H$\alpha$ luminosities, stack the normalized spectra, and measure the H$\beta$ luminosity by fitting a Gaussian function. The inverse of the normalized stacked H$\beta$ luminosity is taken as the average $<\text{H}\alpha/\text{H}\beta>$ ratio. For details of the stacking technique refer to Section 3.1 of Shivaei et al. (2018).\(^{18}\) The reddening ratio inferred from the stacked spectrum of the H$\beta$-undetected sample (empty star in Figure 8(b)) is larger than the average reddening ratio of the H$\beta$-detected sample (solid horizontal line in Figure 8(b)), indicating an increased nebular attenuation, but the trend with metallicity is not changed (Figure 8(b)). The average reden- ddenings of the full sample of H$\alpha$-detected galaxies (filled stars in Figure 8(b)) are 2.90 and 1.59 for the low- and high-metallicity bins, respectively, consistent with the averages of the H$\alpha$- and H$\beta$-detected sample (horizontal lines; 2.60 ±0.20 and 1.38±0.19 for the low and high metallicities, respectively). The majority of our H$\beta$-undetected galaxies have sky line contamination in their H$\beta$ lines, which may explain the low signal to noise. Further investigations of the reden- ddenings of galaxies with large optical depths require IR-selected samples.

6. Summary

In this work, we present constraints on the shape of the UV-optical stellar attenuation curve as a function of gas-phase metallicity at $z \sim 2$. Our sample consists of 218 star-forming galaxies at $z = 1.4-2.6$ with robust H$\alpha$, H$\beta$, and [NII] spectroscopic line measurements from the MOSDEF survey. The sample is carefully selected to exclude galaxies that show AGN activity, the quiescent populations, ULIRGs, and heavily obscured galaxies, and those with high emission-line equivalent widths and young stellar populations. Following the method of Calzetti et al. (2000) and Reddy et al. (2015), we derived the effective attenuation curve (i.e., $k_\lambda - R_V$) in two bins of gas-phase metallicity separated at $12 + \log(O/H) = 8.5$. We matched the Balmer optical depth ($\tau_b$) and SFR distributions of the two samples to control for the dust optical depth biases and different intrinsic stellar populations, respectively. We investigated the variation of the UV extinction bump at 2175 Å and the UV slope of the curve in the two metallicity samples. The main results are as follows:

1. The low-metallicity curve appears to show a steep UV rise similar to that of the SMC curve, along with some evidence for variations from galaxy to galaxy. The slope of the high-metallicity curve is identical to that of the C00 curve. This result can be explained by different dust grain properties in low- and high-metallicity environments, or different dust-star geometries in young (and low-metallicity) galaxies compared to older (more metal-rich) galaxies. In the latter scenario, the steep attenuation curve is a result of a higher fraction of young stars embedded in their birth clouds and subject to larger attenuation at short wavelengths. The former scenario suggests that the small dust grains that produce the UV rise are preferentially present in the low-metallicity environments, due to shattering of the large grains in the intense ionizing radiation and/or because of the low fraction of molecular clouds for dust grains to hide in (Sections 4.1 and 5.1).

2. The high-metallicity curve is best fitted with a UV bump at 2175 Å with $\sim 0.5$ the strength of the MW UV bump. This is a lower limit on the intrinsic strength of the extinction bump, as the bump can be easily suppressed by radiative transfer effects in a clumpy or dusty ISM. A bump of similar strength is ruled out for the low-metallicity curve at $>3\sigma$, showing that the dust grains that produce the bump are significantly less prevalent in the low-metallicity environment. At metallicities of $12 + \log(O/H) < 8.5$, Shivaei et al. (2017) showed a significant decrease in the intensity of the mid-IR PAH emission in our sample, which may suggest the PAHs as the main carriers of the bump (Sections 4.2 and 5.1).

3. We propose metallicity/mass dependent attenuation curves to be used for galaxies below and above $12 + \log(O/H) \sim 8.5$ and $M_s \sim 10^{10.4} M_\odot$ (note that our metallicity threshold is based on $[\text{NII}]/\text{H}\alpha$ strong line calibrations of Pettini & Pagel (2004)): at low metallicity/mass, the UV shape of the curve is set to the SMC curve from Gordon et al. (2003), and at high metallicity/mass the shape of the curve is set to the Calzetti et al. (2000) curve with a UV bump added. Adopting the long-wavelength shape and $R_V$ of the Reddy et al. (2015) curve, we propose metallicity-dependent total attenuation curves in Equation (7) (Section 4.3 and Figure 5).

4. The SFRs inferred from SED model fitting, assuming our two metallicity-dependent attenuation curves, agree well with the independently derived dust-corrected SFR$_{\text{H}\alpha/\text{H}\beta}$ (Section 5.2).

5. As the UV bump is a distinct and broad feature that may be significant at high masses, it is advisable to exclude the wavelength region of the bump ($\lambda = 1950-2400$ Å) in calculating the UV continuum slope $\beta$. The effect of a UV bump, similar to the bump we found in the high-metallicity curve, on the future JWST observations of high-redshift galaxies is presented in Section 5.3.

6. We find that the ionized gas reddening ($E(B-V)$) is, on average, $\sim 2$ times larger than the stellar continuum reddening at low metallicities, and is similar to the continuum reddening at high metallicities. There is not a strong correlation between the nebular-to-stellar reddening ratio and stellar mass, however the scatter in the reddening ratio increases at low masses, low metallicities, and low SFRs (based on UV diagnostics). These trends

\(^{18}\) Source code available at doi:10.5281/zenodo.3932386.
may be explained by a physical picture in which at high metallicities, the high surface density of optically thick dust clouds affects both the ionized gas and stellar continuum emission, while the larger scatter in the reddening ratio at lower metallicities, lower masses, and lower SFRs, indicates that the continuum and nebular emission are reddened by different dust components, i.e., the diffuse ISM dust and dusty birth clouds, respectively. Incorporating other direct tracers of dust attenuation, such as IRX (IR-to-UV luminosities), in the future, will cast more light on the nature of the difference in the stellar and nebular $E(B-V)$s (Section 5.4).

In the future, this study can be improved using larger spectroscopic samples that will allow for finer bins in metallicity. Also, resolved studies of dust and UV emission would shed light on differences in reddening between the lines and continuum (e.g., combining ALMA, UV, and Hα observations). JWST/NIRSpec and JWST/NIRCam observations can extend such studies to higher redshifts. JWST/NIRCam will be an important asset to constrain the UV extinction bump in massive high-redshift galaxies efficiently. Moreover, JWST/MIRI imaging will provide invaluable data to measure the mid-IR emission at z ~ 2 and set robust constraints on the total-to-selective attenuation, $R_V$, which will help to accurately compute dust-corrected SFRs and robust physical parameters.

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Appendix

To first order, the behavior of $z$ ~ 2 galaxies can be approximated by a smoothly varying rate of star formation (e.g., Reddy et al. 2012a; Shivaei et al. 2016). However, stochastic fluctuations of star formation are expected on top of this smooth behavior, as indicated both by observations (e.g., Shivaei et al. 2015a) and theory (e.g., Mitra et al. 2017; Sparre et al. 2017), with amplitudes of 0.2–0.4 dex rms in the star-forming SFR-$M_g$ relation. Timescales for fluctuations in the star formation on this scale appear to be of order ~100–200 Myr (Mitra et al. 2017; Zick et al. 2018).

To understand the effects of the SFH on the UV slope, we simulate galaxy stellar populations. Our simulations utilize the PopStar models (Mollá et al. 2009) for a Chabrier IMF, which we combine to provide SEDs for different SFHs. These models do not include massive binary stars, which would extend the duration of strong ionizing fluxes by a factor of ~1.5–2 (e.g., Stanway et al. 2016), but would not change our results in a significant way. For the purpose of this section, we measure the UV slope of the composite stellar populations between 1000 and 2500 Å. As a baseline model, we assume a constant star formation of 1 $M_\odot$ yr$^{-1}$ for 1 Gyr. By definition, this yields an sSFR of 10$^{-9}$ yr$^{-1}$, which is approximately the median sSFR of our sample. The details of the SFH between 200 Myr and 1 Gyr have very little effect on the UV slope, and they preserve the sSFR as long as the stellar mass formed prior to 200 Myr is preserved.

Over the age range of 0–400 Myr, we change the mass of the stellar populations by factors of 2 over 100 Myr intervals (including the youngest stellar populations, where these changes result in a change of the sSFR by 0.3 dex). In addition to the baseline constant SFH model, we also evaluate exponentially rising and declining SFH models with time constants of 200 Myr, starting at an age of 200 Myr, and changing the SFR at time zero by factors of 2 (i.e., changing the sSFR by 0.3 dex). We find that stars younger than 3 Myr have a significant effect on the slope, as well as stars between 50 and 200 Myr. Changes in the SFR in these age ranges by factors of order two could affect the slope by ~10–15%. For most other age ranges, the changes are of order $\lesssim$6%. For our subsamples of up to 100 galaxies, the changes in UV slope due to stochasticity in the SFR will tend to average out, and the associated net uncertainty in the average slope should be only a few percent.

Another measure of the influence of SED variations on our results can be obtained by ignoring the stochasticity of the SF and adopting the sSFR as a proxy for the shape of the intrinsic SED, assuming a smooth variation of star formation with time. In each metallicity sample, the average sSFR in the $\tau_1$ bins changes by at most ~0.24 dex (Figure 1, right). Assuming a constant SFH, we estimate the systematic error of the attenuation curve associated with the sSFR difference, as follows. We model two intrinsic (dust-free) SEDs using the Bruzual & Charlot (2003) models, with the mass and SFR of the average mass and SFR in the low and high $\tau_1$ bins in Figure 1, right. The “correction factor” that stems from the difference in the two intrinsic SEDs is calculated using Equation (2) (based on the error calculation in Section 3.6.4 of Reddy et al. 2015), and applied to the selective curves ($Q_s$). The “corrected” effective curves show ~5 and 20% systematic shift to shallower slopes compared to the original high- and low-metallicity curves, respectively, which are within the 1σ uncertainties shown in Figure 3.

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