Effect of Inclination of Rectangular Reinforced Concrete Short Columns on the Confinement

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HIGHLIGHTS

- The inclination effect on the concrete column decrease confinement.
- There are certain angles that we can adopt in the design of inclined columns to avoid reducing confinement.
- The use of high strength concrete contributes greatly to avoiding the reduction of confinement in the inclined columns.

ABSTRACT

The main objective of this paper is to study the confinement of the rectangular reinforced concrete short inclined columns. This paper was based on theoretical analysis using the MATLAB program according to Universal Codes, and variables that were carefully selected to be the most influential factor. The angle of the inclination (α) was taken as a major variable in the paper, in addition other variables which in turn affect directly on the behavior of inclined columns such as the percentage of reinforcing steel in the concrete section of the column (ρ), the compressive strength of the concrete (f’c), yield strength of steel bars (fy) and effective depth ratio (γ). The results show that best ratio of reinforcing steel that improves the value of the confinement ranges from 0.4 - 0.6 which leads to an increase in the confinement of (60 – 100)%, and these rates increase with increasing α, and the increase in f’c leads to a significant increase in the confinement, especially when HSC is used. On the other hand, decreasing fy leads to increase in confinement, and the value of the γ had a considerable effect on the confinement that was decreased by about 11% when γ equals 0.9, compared with the corresponding γ equals 0.6.

1. Introduction

Transverse reinforcements in columns in the form of hoops, cross-ties, or spirals act a significant task in protection the columns, chiefly when they are exposed to intense seismic activity or side loads. They are necessary in any column whether they are roles of a moment resistant frame or the gravity technique for them to twist horizontally and supply the necessary ductility. Purpose of crosswise reinforcement is definite in design codes for beams and columns to support the following four purposes:

Avoid buckling of longitudinal reinforcing bars, withstand shear forces and to prevent shear failure, confine the concrete core to supply enough deformability (ductility), fasten together lap splices-after splitting cracks form corresponding to the splices, ties or spirals confine slipup between the joined bars. [1]

Confinement plays an important role in raising the strength of compressive strength compared with the unconfined concrete. Bearing in mind none of these purposes are influenceable till the concrete cracks or spall. The chief factor in the confinement is to enclose the concrete with hoops so that it acts like a belt, and that there are factors that plays a role in raising this confinement such as the distance between the hoops and the shape of the hoops and their number. The strain at top confined strength εcc is assumed as a function of the strain at top unconfined strength of concrete εc depending on the formula of Richart et al [2].

\[
\varepsilon_{cc} = \varepsilon_{c0} \left[1 + 5 \left(\frac{f_{cc}}{f_{c0}} - 1\right)\right]
\]  

[1]
Richart et al [2] proposed the following relationship for strength applied to both spirally reinforced and hydraulically confined columns[2].

\[ f_{cc} = f_{co} + 4.1f_l \]  

(2)

Popovic in [3], Utilizes the model of the equation primarily established to exemplify the stress-strain rejoinder of unconfined concrete. A constant confining pressure \( f_l \) founded by this model. The axial stress of the confined concrete \( f_c \) for any given strain \( \varepsilon_c \) is correlated to the top confined strength \( f_{cc} \) as shown in eq (3) and (4):

\[ f_c = f_{cc} \times x \frac{r}{r - 1 + \frac{r}{x}} \]  

(3)

\[ x = \frac{\varepsilon_c}{\varepsilon_{cc}} \]  

(4)

Where \( \varepsilon_{cc} \), the strain at the top strength \( f_{cc} \)

\[ r = \frac{E_c}{E_{sec}} \]  

(5)

Where \( E_c \) is the tangent elastic modulus of unconfined concrete and can be predestined as \( 5000\sqrt{f_{cc}} \) (MPa). \( E_{sec} \) is the secant modulus of confined concrete and can be predestined as \( f_{co}/\varepsilon_{cc} \). Murray [4] developed the top confined strength \( f_{cc} \) is a function of the unconfined strength \( f_c \) and the constant pressure of confining \( f_l \), a nonlinear correlation is suggested depending on the greatest strength surface.

\[ f_{cc} = f_{co} \left( -1.254 + 2.254 \sqrt{1 + \frac{7.94f_l}{f_{co}} - 2 \left( \frac{f_l}{f_{co}} \right)} \right) \]  

(6)

Kent and Park [5], Sheikh and Uzumeri [6] and Mander, Priestley, and Park [7]. These researchers most famous deals with confinement, have suggested analytic models for the stress-strain curve of steel stirrups-confined concrete.

Sheikh and Khoury [8] proposed a performance-based confining reinforcement design procedure. The researchers employed curvature ductility, \( \mu_\beta \) as the performance parameter in their design equations. The seismic performance of a column was classified to be in one of the following three categories: (1) highly ductile columns \( (\mu_\beta \geq 16) \), (2) moderately ductile columns \( (16 > \mu_\beta \geq 8) \), and (3) columns displaying low levels of ductility \( (\mu_\beta < 8) \). The following equation was proposed and calibrated to relate the amount of lateral reinforcement in the potential plastic hinge regions of tied columns to axial load level and to curvature ductility.

\[ A_{sh} = \alpha \left[ 1 + 13 \left( \frac{P}{P_c} \right)^5 \frac{(\mu_\beta)^{1.15}}{29} A_{sh, ACI} \right] \]  

(7)

The constant \( \alpha \) was used to take the arrangement of lateral and longitudinal steel into account. According to Sheikh and Khoury [8], \( \alpha \) may be equal to one for tightly knit lateral reinforcement configurations in which effective lateral support to longitudinal bars is provided. In the presence of less efficient lateral reinforcement configurations and higher axial load levels, greater \( \alpha \) values are recommended. They concluded that the ACI 318-95 [9], requirements for confining reinforcement may not be sufficient even in columns with efficient lateral reinforcement configurations to meet the high curvature ductility demands under moderate-to-high levels of axial loads. They recommended that at low axial load levels \( (P < 0.4P_c) \) the code requirements may be relaxed. Bayrak and Sheikh [10] modified the equation (7) for high strength concrete columns with concrete strengths ranging from between 55 MPa and 115 MPa.

\[ A_{sh} = \alpha \left[ 1 + 13 \left( \frac{P}{P_c} \right)^5 \left( \frac{\mu_\beta}{8.12} \right)^{0.82} A_{sh, ACI} \right] \]  

(8)

P. Paulthe and F. Légeron [11] proposed new equations for the design of confinement reinforcement for conventional columns with a circular and rectangular cross section depending on performance determined in terms of curvature demand. These equations are derived from a parametric study of a very huge number of columns to get a sure level of sectional ductility and considered for the effect of concrete strength, axial load level, transverse reinforcement yield strength, and transverse confinement reinforcement especially distribution. The following parameters were chosen in the statistical study,“ (1) the longitudinal reinforcement ratio \( \rho_\ell = 0.5, 1.5 \) and 2.5 %, (2) the axial load level calculated as the ratio of axial load to compressive strength of gross concrete \( P/A_g f_c = 0.1, 0.2, 0.3, 0.4, 0.5 \) and 0.6, (3) the compressive strength of concrete cylinder \( f_c = 30, 45, 60, 80 \) and 100 MPa, with various cross section size.” Simplification of these equations, while retaining the main governing factors, leads to design equations for design codes. These equations are then confirmed with a huge set of experimental results. Their accomplishment in the Canadian Standard for Design of Concrete Structures is described.
Objectives
The main goal of this paper is to study the effect of inclination of the concrete column on the quantity of the confinement considering variables, angle of inclination, the ratio of steel bars, concrete compressive strength, yield strength of steel bars and the value of $\gamma$.

2. Theory and Method

2.1 Confinement Concept
In vertical columns, the hoops act as ties or spiral work to increase concrete resistance and avoid buckling in the longitudinal steel bar. In beams, hoops act as a stirrup work against the shear force generated by loads, while in columns inclined, the hoops act as a composite between the two types of hoops referred to above, their function changes with the change in inclination angle of the column. The basic idea is to find an equation for this change in terms of the angle of inclination and find the critical angle through which an inclined column can be created with acceptable efficiency.

Cross ties are used in columns, the load is carried by the vertical steel bars, while the ties are arranged to fix the bars in their wanted position with no developing disturbed while compacting the concrete by the vibration process, the ties are evenly spaced along with the all height of the column, from the other hand stirrups are worked to describe the transverse reinforcement arranged in beams where the essential form of load transmit through bending and shear, the stirrups are arranged to avoid cracks forming in the concrete beam due to shear, bending, and tension. The spacing of the stirrups is not constant throughout the length of the beam, they are spaced nearer close the supports and remoter apart in the middle portion.

2.2 Effecting of the inclination of RC column on the confinement
It is not possible to impose axial load to the concrete column greater than the axial load capacity multiplied by the reduction factor, so the maximum load can be applied ($\phi P_n$), and it may be less than that; depending on the level of loading, New Zealand code, representing (Ash/Sbc) as follows:

$$\frac{A_{sh}}{sb_c} = \left[\frac{1.3-\rho m A_g f' c}{3.3} \frac{p}{A_c f_{yt} 0.85 f' c A_g}\right] = 0.006$$ (9)

$$e = \frac{M_n}{P_n}$$ (10)

$$e = \cos \alpha l$$ (11)

$$P_n = \frac{M_n}{\cos \alpha l}$$ (12)

At maximum $\phi P_n = P_u = \frac{\phi M_n}{\cos \alpha l}$ (13)

At $\alpha = 90^\circ$ $P_u = \phi P_n$

$$\frac{A_{sh}}{sb_c} = \left[\frac{1.3-\rho m A_g f' c}{3.3} \frac{\phi M_n}{\cos \alpha l}\right]$$ (14)

$\lambda_{\alpha} = 1$ [Proposed]

$$f_1 = \frac{A_{sh}}{sb_c} f_{yt}$$ (15)

$$f_{ce} = f_{cp} + 4.1 f_i$$ (16)

(P) which represents the applied load in terms of the load capacity of the concrete column, which is the maximum value to be carried by the column in terms inclination angle of the concrete column with the added factor ($\lambda_{\alpha}$) represented the ratio of axially applied load to the axial load capacity of column, with keeping the minimum limit.

2.3 Equations of confinement
Main factors affecting the confinement of columns given by different codes of practice are listed in Table 1.
### Table 1: Equations of Main Factor, In Confinement Ash/Sbc, for Different Codes

| Code                        | Ash/sbc                                                                 |
|-----------------------------|-------------------------------------------------------------------------|
| IS 13920:1993[13]           | 0.18\(\frac{k_u}{f_{yt}}\left(\frac{A_g}{A_c} - 1.0\right)\)          |
| ACI 318-14[14]              | 0.3\(\frac{f_{ct}}{f_{yt}}\left(\frac{A_g}{A_c} - 1.0\right)\)        |
| NZS 3101-06[15]             | \[1.3 - \rho \frac{m A_g f_{ct}}{A_c f_{yt} 0.85f_{ct} A_g}\] - 0.006   |
|                            | Where \(m = \frac{0.85f_{ct}}{f_{ct}}\)                                |
|                            | 0.3 knkp \frac{f_{ct} f_{ys}}{A_c} where \(P\)                        |
|                            | \(k_n = \left(\frac{n}{n_{cr-2}}\right)\) and \(k_p = \frac{P}{f_{ps}} \geq 0.2\) |

### 2.4 Characteristics of the material

The main characteristics are compressive strength in concrete, yield strength in steel and modules of elasticity of steel, a wide range of columns have been studied with concrete strength ranging from 25 to 120 MPa confined with steel bars and having yield strength ranging from 250 to 800 MPa, the major reason for using these wide ranges for concrete strength to investigate the behavior of columns under different cases study.

### 2.5 Variables of the Parametric Study

The main variables of the investigate were angle of the inclination of the concrete column (ranging from 0 to 90), ratio of the reinforcing steel in the section (ranging from 0.01 to 0.09), compressive strength of the normal and high strength concrete (ranging from 20 to 120), yield strength of steel (ranging from 250 to 800) and gamma (ranging from 0.6 to 0.9).

### 3. Results and Discussion

#### 3.1 Effect of inclination on the confinement

Figure 3 Illustrated the relationship of the inclination angle and the main factor which is adopted globally in the confinement, and through the relationship below, we can clearly discover that the relationship is a clearly proportional directly, so the lower the angle of inclination less than 90 degrees (the universal vertical axis that represents the traditional column), this ratio is less, and this is due to the axial load capacity of the inclined concrete column with the inclination angle, and that most of the relationships of the international codes depend on this variable, except for the American Code. This may be the focus of criticism of the American code in this field.

#### 3.2 Effect of the percentage of steel bars (p) on the confinement

Figure 4 describes the effect of reinforcement ratio on the confinement with different inclination angle, there is a double effect of the ratio of reinforcing steel that it is proportional to a certain extent, and then the relationship is reflected due to the problem of steel congestion. Will arise; from the other hand Figure 5 illustrate the rate of change with different reinforcement steel ratio.

#### 3.3 Effect compressive strength of concrete (f’c) and yield strength of steel (fy) on the confinement

The confinement-inclination angle relationship with compressive strength of concrete and yield strength of steel for inclined column presented in Figure 6 to 9. It can be easily seen that the rise of compressive strength of concrete increased the confinement, from the other hand there is an inverse effect increased yield strength of steel decreased confinement, note that as the yield strength is raised, the amount of required confining reinforcement will be decreased, based on the hypothesis of how much strain will happen in transverse reinforcement.

#### 3.4 Effect of gamma (γ) on the confinement

Figure 11 exhibits the inclination angle of inclined column and confinement curves for the four value of \(\gamma\) 0.6, 0.7, 0.8 and 0.9 respectively, it can be noted that when the \(\gamma\) decrease the \((\text{Ash/Sbc})\) increase because the decrease of \(\gamma\) led to decline the value of \(A_c\) which increases the \((A_g/A_c)\) factor in the confinement equation, but that factor has limit in international codes therefore when \(\gamma\) equal 0.6 the \((\text{Ash/Sbc})\) drop.
Figure 1: Columns under compression axial load

Park and Kent [5]

Figure 2: Described model of confinement by Mander et al. [7]

Figure 3: Illustrated the relationship between the inclination angle and the confinement

Figure 4: Illustrated the effect of (ρ) on the confinement

Figure 5: Illustrated the effect of (ρ) on the rate of change in confinement

Figure 6: Illustrated the effect of ($f'$c) on the confinement
4. Conclusion

The best ratio of reinforcing steel that improves the value of the confinement ranges from 0.4 - 0.6 which leads to an increase in the confinement of (60 – 100) %, and that these rates increase with increasing $\alpha$. The increase in $f'c$ leads to a significant increase in the confinement, especially when used HSC, where the use of $f'c$ 28, 35 and 55 MPa, leads to an increase confinement 44%, 75%, and 175% respectively, on the other hand, decreased $f_y$ leads to increase of confinement, where using of $f_y$ 400, 550 and 800 MPa, leads to a decrease in confinement 38%, 55%, and 69% respectively. The value of the $\gamma$ had a considerable
influence on the confinement, the confinement was decreased by about 11% when \( \gamma \) equals 0.9, compared with the corresponding \( \gamma \) which to 0.6.

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All authors contributed equally to this work.

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**Data availability statement**
The data that support the findings of this study are available on request from the corresponding author.

**Conflicts of interest**
The authors declare that there is no conflict of interest.

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