Active Galactic Nuclei In Cosmological Simulations - I.
Formation of black holes and spheroids through mergers

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4 August 2021

ABSTRACT

This is the first paper of a series on the methods and results of the Active Galactic Nuclei In Cosmological Simulations (AGNICS) project, which incorporates the physics of AGN into GalICS, a galaxy formation model that combines large cosmological N-body simulations of dark matter hierarchical clustering and a semi-analytic approach to the physics of the baryons. The project explores the quasar-galaxy link in a cosmological perspective, in response to growing observational evidence for a close relation between supermassive black holes (SMBHs) and spheroids. The key problems are the quasar fuelling mechanism, the origin of the BH to bulge mass relation, the causal and chronological link between BH growth and galaxy formation, the properties of quasar hosts and the role of AGN feedback in galaxy formation.

This first paper has two goals. The first is to describe the general structure and assumptions that provide the framework for the AGNICS series. The second is to apply AGNICS to studying the joint formation of SMBHs and spheroids in galaxy mergers. We investigate under what conditions this scenario can reproduce the local distribution of SMBHs in nearby galaxies and the evolution of the quasar population.

AGNICS contains two star formation modes: a quiescent mode in discs and a starburst mode in proto-spheroids, the latter triggered by mergers and disc instabilities. Here we assume that BH growth is linked to the starburst mode. The simplest version of this scenario, in which the black hole accretion rate \( \dot{M}_* \) and the star formation rate in the starburst component \( \dot{M}_{\text{burst}} \) are simply related by a constant of proportionality, does not to reproduce the cosmic evolution of the quasar population. A model in which \( \dot{M}_* \propto \rho_{\text{burst}} \dot{M}_{\text{burst}} \), where \( \rho_{\text{burst}} \) is the density of the gas in the starburst and \( \zeta \approx 0.5 \), can explain the evolution of the quasar luminosity function in B-band and X-rays (taking into account the presence of obscured AGN inferred from X-ray studies). The scatter and the tilt that this model introduces in the BH-to-bulge mass relation are within the observational constraints. The model predicts that the quasar contribution increases with the total bolometric luminosity and that, for a given bulge mass, the most massive black holes are in the bulges with the oldest stars.

Key words: galaxies: formation, active – quasars: general

1 INTRODUCTION

1.1 The connection between quasars and galaxies:
observational evidence and open problems

Several observational and theoretical arguments suggest a direct link between quasars and galaxy formation.
vational fact. The relation between the black hole mass and the mass, luminosity and velocity dispersion of the host spheroid (Muzzin et al. 1998; Ferrarese & Merritt 2000; Gebhardt et al. 2000; Merritt & Ferrarese 2001; Tremaine et al. 2002; Marconi & Hunt 2003; Haring & Rix 2004) together with the chronological agreement between the quasar epoch (z ~ 2 – 3) and the stellar ages of early-type galaxies (Cattaneo & Bernardi 2003) prove that black hole growth mechanisms are directly related to the origin of the bulge component.

This relation opens two kinds of questions. The first one concerns the triggering mechanism that activates black hole growth (what starts the accretion). The second concerns the mechanism that determines the final black hole mass (e.g. what terminates the accretion).

The first attempts to explain the link between quasars and galaxy formation were in the context of the monolithic collapse model (Eggen et al. 1962). Matter with low angular momentum falls to the centre first forming the galactic nucleus and the bulge, while matter with high angular momentum slowly settles into a disc.

Toomre & Toomre (1972) were the pioneers of computer simulations of galaxy interactions. They argued that galaxy mergers can drive a sudden supply of gas into the nuclear region while producing a morphological transformation of spiral galaxies into ellipticals. Smoothed-particle-hydrodynamics simulations of galaxy mergers confirmed their intuition (Barnes & Hernquist 1993, 1996; Mihos & Hernquist 1994, 1996; Springel 2000). The impressive results of hydrodynamic simulations together with the widespread and successful use of the merger model in semi-analytic models of hierarchical galaxy formation (see below) contributed to a paradigm shift from the monolithic to the merger scenario.

From the point of view of AGN fuelling, the fundamental points of the merging scenario are that AGN are fuelled with cold gas from the discs of the merging galaxies and that black hole growth is conditional to a triggering process. A process with a trigger and a short intrinsic duration is consistent with the episodic nature of AGN (in the monolithic collapse model, the brief life time of quasars was attributed to the rapid consumption of low angular momentum gas).

In relation to the mechanism that determines the black hole mass, two scenarios are possible. The first is that black hole growth is determined by fuel availability. In this case, the quasar switches off when stars have consumed all the gas (e.g. Kauffmann & Hachnelt 2000). In the second scenario, black hole growth is self-regulated through mechanical (jets or winds, Omma et al. 2004 and references therein) or radiative (Compton heating, Ciotti & Ostriker 1997, 2001) feedback. In this second case, supermassive black holes may be an essential ingredient of galaxy formation and not just a mere by-product (Silk & Rees 1998; Granato et al. 2004; Di Matteo et al. 2003).

1.2 Cosmological models of the formation of quasars and galaxies

The fuelling mechanism, the timing of the active phase in relation to the host galaxy evolution and the mechanism that limits the accretion are the three main open problems in relation to the link between quasars and galaxies.

There are two ways of approaching these problems. The first is to observe and model in great detail a small sample of individual objects. The second is to test if specific assumptions can reproduce the population properties of quasars and galaxies in a cosmological volume. Semi-analytic models are a powerful tool for this second type of study.

White & Rees (1978) and Efstathiou & Rees (1988) were the pioneer of galaxy formation and quasar formation in a cosmological scenario, in which structures form through gravitational instability and hierarchical clustering of primordial density fluctuation. Semi-analytic models of galaxy formation have given a substantial contribution towards a more detailed comprehension of galaxy formation in a cosmological scenario. The field is now so vast that it is no longer possible to cite all authors who contributed to its development. The most advanced models are those of the research groups in Durham (e.g. Cole et al. 2000 and references therein), Munich (Kauffmann et al. 1999 and references therein), Kauffmann & Hachnelt (2000), Paris (Hatton et al. 2003) and Santa Cruz (Somerville & Primack 1999; Somerville et al. 2003). Conceptually, a semi-analytic model is structured into two steps. In the first one, Press-Schechter theory (Press & Schechter 1974) or N-body simulations (i.e. Kauffmann et al. 1999) are used to follow gravitational clustering in the dark matter component. The aim of this first step is to construct merger trees for a sample of dark matter haloes, which are thought to represent the Universe. The second step is to use semi-analytic prescriptions to follow the physics of the baryons (cooling, star formation, stellar evolution, feedback, chemical enrichment, reprocessing of light by dust, mergers, bar instabilities, etc.) in the merger trees. Models in which merger trees are built by using N-body simulations, such as the GAlICs (Galaxies In Cosmological Simulations) model by Hatton et al. (2003), are sometimes called hybrid models to distinguish them from pure semi-analytic models, in which merger trees are constructed from Press-Schechter theory.

Quasar modellers have followed a similar path (Carlberg 1990; Hachnelt & Rees 1993; Katz et al. 1994; Mulderoen et al. 1994; Bi & Fang 1997; Haiman & Loeb 1998; Cattaneo et al. 1999; Nitta 1999; Menou & Haiman 1999; Percival & Miller 1999; Haiman & Menou 2000; Monaco et al. 2000; Valageas & Schaeffer 2000; Cattaneo 2001; 2002; Haiman & Hui 2004; Hatziminaoglou et al. 2001; Martini & Weinberg 2004; Nath & Rovey 2004; Volonteri et al. 2003a,b; Hatziminaoglou et al. 2003). The assumptions in these papers are different, but most of them follow the common strategy of modelling the quasar luminosity function from the Press-Schechter (1974) mass function of dark matter haloes in combination with various assumptions for the probability that a halo of mass $M_{halo}$ at redshift $z$ contains a quasar with luminosity $L_{QSO}$. These studies do not treat the complicated physics of galaxy formation and AGN fuelling, but show the fundamental scaling relations that a physical model has to satisfy.

The next logical development is the merging of the two research programmes achieved by including quasars into semi-analytic models of galaxy formation (Kauffmann & Hachnelt 2000, 2002; Hachnelt & Kauffmann 2000, 2002; Enoki et al. 2003; Di Matteo et al. 2003). From an AGN perspective, this development allows a more physical modelling and thus a
more physical understanding, while it reduces the number of arbitrary assumptions that the modeller can make. E.g., merging rates cannot be changed without changing galaxy morphologies, colours, luminosity function, etc. Of course, that means that more hypotheses and parameters go into the model, but the current data allow to constrain them. From a galaxy formation perspective, AGN may provide an answer to two long standing problems: the overcooling problem in massive haloes (cD galaxies are too many, too massive and too blue; e.g. Hatton et al. 2003 and references therein) and the difficulty of reproducing sub-millimetre counts without ending up with galaxies that are too bright at the present cosmic epoch (e.g. Devriendt & Guiderdoni 2003).

1.3 The AGNICS project

The Active Galactic Nuclei In Cosmological Simulations (AGNICS) project started as an extension of the GalICS (Galaxies In Cosmological Simulations) hybrid galaxy formation model (Hatton et al. 2003). AGNICS was developed to investigate some aspects of the link between quasars and galaxy formation in a broad and coherent context. Combined models of quasars and galaxy formation are in a qualitative agreement with the cosmic evolution of the quasar population (Kauffmann & Haehnelt 2000), but do not reproduce the quantitative decrease of the number of bright quasars at low redshift. Secondly, most of the AGN population is optically unseen (Ueda et al. 2003; Sazonov et al. 2004), but the impact of obscured AGN on models of the evolution of the quasar luminosity function has not been explored yet. Moreover, an interesting by-product of the AGNICS project is the possibility to use AGNICS as a tool for generating a virtual sky of quasars and galaxies, which may assist the planning of forthcoming observations. The virtual sky may be used to train automatic recognition algorithms and test sources of bias or incompleteness in observational studies.

The structure of this first paper is as follows. In Section 2 we recall the main assumptions and features of the GalICS galaxy formation model used to develop the AGNICS model while we refer to Hatton et al. (2003) for a more detailed presentation. We give particular importance to the origin of galaxy morphologies because a correct modelling of spheroids is essential to derive meaningful results for black holes and AGN. In Section 3 we describe the method that AGNICS uses to model black hole growth and AGN. Thereafter, we distinguish between two main models: the simplest possible model, in which the black hole accretion rate and the starburst rate are simply related by a constant of proportionality (we call this the basic model), and the reference model (the model which allows us to find the best agreement with the data). In Section 4 we show that the basic model does not reproduce the low redshift decrease of the comoving density of bright quasars, but we also show that we can modify the basic model by changing the expression for the black hole accretion rate and introducing a factor proportional to a power of starburst density \( \dot{M}_\bullet \propto \rho_{\text{burst}}^{\zeta} M_{\text{burst}} \), where \( \dot{M}_\bullet \) is the black hole accretion rate, \( M_{\text{burst}} \) is the star formation rate in the starburst component and \( \rho_{\text{burst}} \) is the density of the gas in the starburst). For \( \zeta \approx 0.5 \), the modified model (the reference model) satisfies the observational constraints deriving from optical (Wolf et al. 2003) and X-ray (Ueda et al. 2003) observations of AGN and from the scatter in the black hole-to-bulge mass relation (Marconi & Hunt 2003; Haring & Rix 2004).

In the Conclusion (Section 5), we discuss what we can learn from the work presented in this article and which questions that are still open. The study of quasar hosts is postponed to a future publication of the AGNICS series.

2 THE GALICS GALAXY FORMATION MODEL

GalICS is a model of hierarchical galaxy formation which combines high resolution cosmological simulations to describe the dark matter content of the Universe with semi-analytic prescriptions to follow the physics of the baryonic component. The modules that enter the GalICS model are the cosmology (to generate the merger trees), the cooling model (to follow cooling of hot gas in dark matter haloes), the model for the galaxy internal structure and dynamics, the merger model (merging rates and effect of mergers on galactic morphologies), the star formation and stellar evolution model (including feedback and metal enrichment) and the spectral evolution model (stellar spectra, extinction and dust thermal emission). We begin this Section by describing the N-body simulation used to generate the merger trees. Then we progress into explaining the main physical assumptions that enter each functional unit.

2.1 The dark matter simulation

2.1.1 Simulation parameters

The cosmological N-body simulation used to construct the merger trees was carried out by using the parallel tree-code developed by Ninin (1999). This simulation was run for a flat cold dark matter model with a cosmological constant of \( \Omega = 0.667 \). The simulated volume is a cube of side \( L_{\text{box}} = 100 h^{-1} \) Mpc, with \( h_{100} \equiv h_0/100 \) km s\(^{-1}\) = 0.667, containing 256\(^3\) particles of mass \( 8.3 \times 10^9 M_\odot \) (\( H_0 \) is the Hubble constant). The smoothing length is of 29.29 kpc. The cold dark matter power spectrum was normalised in agreement with the present day abundance of rich clusters (\( \sigma_8 = 0.88 \)). The simulation produced 100 snapshots spaced logarithmically in the expansion factor \((1 + z)^{-1}\) from \( z = 35.59 \) to \( z = 0 \).

2.1.2 Halo identification

On each snapshot a friend-of-friend algorithm was run to identify virialised groups of more than 20 particles. The minimum mass of a dark matter halo is therefore \( 1.66 \times 10^{11} M_\odot \). For each halo we compute a set of properties, which include the position and the velocity of the centre of mass, the kinetic and the potential energy, the spin parameter and the tensor of inertia.

We fit a triaxial ellipsoid to each dark matter halo identified in the snapshot. The semi-axes of the ellipsoid are in a ratio determined by the ratio between the three different components of the inertia tensor. We shrink the ellipsoid until the inner region satisfies the virial theorem. The matter within this virial volume determines the virial mass. The
virial radius is the radius of a sphere whose volume is equal to the virial volume and the virial density is equal to the virial mass divided by the virial volume.

When passing from N-body to semi-analytic simulations, we idealise dark matter haloes as singular isothermal spheres truncated at the virial radius. The information about each individual halo passed to the semi-analytic model is therefore contained in three parameters. They are the virial mass, the virial density (the mean density within the virial radius) and the spin parameter.

2.1.3 Merger trees

The merger trees are computed by linking the haloes identified in each snapshot with their progenitors at the previous time-step. All predecessors from which a halo has inherited one or more particles are counted as progenitors, but only one is the main progenitor, the one that has given the largest particle contribution. In the same way one can identify a main descendant for each dark matter halo. The merging histories that we obtain are thus far more complex than those constructed from Press-Schechter theory as they include the processes of evaporation and fragmentation of dark matter haloes. In such situations we assume that all baryons remain in the most massive remnant.

2.2 From haloes to discs

2.2.1 Gas cooling and infall

Newly identified haloes are given a mass of hot gas by using a universal baryonic fraction of Ω_b/Ω_m = 0.135. Hot gas is assumed to be shocked heated to the virial temperature of the halo and in hydrostatic equilibrium with the dark matter potential. The density profile of the hot gas is that of a singular isothermal sphere truncated at the virial radius. The cooling time is calculated from the hot gas density distribution with the Sutherland & Dopita (1993) cooling function. The gas that can cool in a time Δ t is the gas whose cooling time and free-fall time are both lower than Δ t. GalICS assumes that gas cooling is accompanied by a simultaneous gas inflow in order to maintain the same hot gas density profile at all times. The disc radius is r_d = λ r_{vir} / √2, where r_{vir} is the virial radius and λ is the angular momentum parameter of the halo. Cooling is inhibited in haloes with λ > 0.5.

We also prevent cooling in haloes that contain a total mass of bulge stars > 10^{11} M_☉ not to exceed the observational constraints on the number of massive galaxies. The theoretical argument behind this solution is that the bulge mass is proportional to the black hole mass and therefore to the total energy budget of AGN over the life of the halo. We assume that AGN deposit energy in the intergalactic medium mechanically (through jets or winds) and radiatively (through hard X-ray photons) and that this input is proportional to the black hole accretion rate. In reality, the long term outcome of the interaction between the black hole and the intergalactic medium is poorly understood. In particular, there is no strong physical reason why feedback should become important above a critical black hole mass (but see Cattaneo 2002, Dunlop et al. 2003). The cut-off at a bulge mass of > 10^{11} M_☉ introduced by Hatton et al. (2003) and used for the work presented in this article is a temporary measure, whose justification is in its capacity of reproducing the data. In fact, all groups working on semi-analytic models of galaxy formation were forced to make arbitrary assumptions to fit the bright part of the galaxy luminosity function. Meanwhile, we are looking for a motivated self-consistent approach, which will appear in another paper of the AGNICS series.

2.2.2 Star formation and stellar evolution

The star formation rate in the disc is

\[ \dot{M}_* = \frac{M_{\text{cold}}}{\beta \tau_{\text{dyn}}} \]

Here \( M_{\text{cold}} \) is the mass of the gas in the disc (all the gas in the disc is cold and all the gas in the halo is hot) and \( \tau_{\text{dyn}} \) is the dynamical time (the time to complete a half rotation at the disc half mass radius). The parameter \( \beta_* \), which determines the efficiency of star formation has a fiducial value of \( \beta_* = 50 \). The mass of newly formed stars is distributed according to the initial mass function. Stars are evolved between time-steps using a sub-stepping of at most 1 Myr. During each sub-step, stars release mass and energy into the interstellar medium. Most of the mass comes from the red giant and the asymptotic giant branch of stellar evolution, while most of the energy comes from shocks due to supernova explosions. In GalICS, the enriched material released in the late stages of stellar evolution is mixed to the cold phase, while the energy released from supernovae is used to reheat the cold gas and return it to the hot phase in halo. The reheated gas can also be ejected from the halo if the potential is shallow enough. The rate of mass loss in the supernova-driven wind that flows out of the disc is directly proportional to the supernova rate. The details of the model and their justification are found in Hatton et al. (2003).

2.3 Galaxy morphologies

2.3.1 Galaxy internal structure

GalICS models the baryonic part of a galaxy as the sum of three components: the disc, the bulge and the starburst. These three components are not always present at the same time. The fundamental assumption is that all galaxies are born as discs at the centre of a dark matter halo. The transformation of disc stars into bulge stars and of disc gas into starbursting gas is due to bar instabilities and mergers. Gas is never added to bulges directly and the only gas in bulges is that coming from stellar mass loss. The starbursting gas forms a young stellar population that forms part of the bulge stellar population when the stars have reached an age of 100 Myr. We do not readjust the bulge radius when this happens. The disc has an exponential profile, while the bulge and the starburst are described by a Hernquist (1990) density distribution. The starburst scale is \( r_{\text{starburst}} = k r_{\text{bulge}} \) with \( k = 0.1 \). This model cannot take into account the presence of more complex morphologies, which are particularly relevant to the case of starburst galaxies, but has a justification that comes from smoothed particle hydrodynamics simulations of galaxy mergers. The star formation law (Eq. 1) has the same form and uses the same efficiency parameter.
\( \beta \), for all three components when we redefine \( M_{\text{cold}} \) as the mass of the gas in the component and \( t_{\text{dyn}} \) as the dynamical time of the component. For the components described by a Hernquist profile, the dynamical time is \( t_{\text{dyn}} = r_{0.5}/\sigma \), where \( r_{0.5} \) is the half mass radius and \( \sigma \) is the velocity dispersion at the half mass radius.

### 2.3.2 Disc instabilities

The formation of a bulge from a disc instability is modelled as follows. A disc is globally stable if \( v_{d} < 0.7v_{\text{tot}} \) (e.g. van den Bosch 1998). Here \( v_{\text{tot}} \) is the circular velocity at the disc half mass radius, computed from the total gravitational potential of the disc, the bulge, the starburst and the halo, while \( v_{d} \) is the circular velocity computed from the gravitational potential of the disc only. The bar instability transfers gas from the disc to the starburst and stars from the disc to the bulge until the stability criterion is fulfilled.

### 2.3.3 Merging rate

Mergers are the second path to form spheroids. The model for galaxy mergers is articulated into two parts: the computation of the merging rate and the model for predicting the outcome of mergers when they occur. Let us begin with the first one. In the beginning there is one galaxy at the centre of each halo. When two haloes merge, the central galaxies of the two haloes will sink towards the common centre of mass owing to dynamical friction. That will take some time, so that the halo may temporarily be without a central galaxy. The common centre of mass will be closer to the centre of mass of the more massive halo, so that the central galaxy of the more massive halo will reach the centre of the new halo more rapidly, not only because it is more massive and is therefore subject to stronger dynamical friction (computed from the standard differential equation in Binney & Tremaine 1987), but also because it starts from a lower radial coordinate. Galaxy groups and clusters form because above a certain mass the dynamical friction timescale for galaxy mergers becomes longer than the timescale on which dark matter haloes merge. When groups or clusters merge, the radial coordinates of satellite galaxies in the new halo are determined according to a prescription such that, if the satellites come from the main progenitor and this is almost as massive as the final halo, their radial coordinates are nearly unperturbed. On the other, if the satellites come from a much less massive halo, their final radial coordinates are close to the virial radius of the new halo. GalICS considers not only mergers at the centre of the halo due to dynamical friction, but also mergers due to encounters of galaxies at a non zero radial coordinate (collisions between satellite galaxies), but these events are a small correction to the predominant merging activity with the central galaxy.

### 2.3.4 Effect of mergers

We now come to the second part of the merging model: how mergers transform galactic morphologies. Bulge material remains bulge material and starburst material remains starburst material, while some of the disc material is removed from the disc. As in the case of the bar instability, gas is transferred to the starburst and stars are transferred to the bulge. The fraction of the disc mass transferred to the spheroidal component (the bulge and the starburst) depends on the mass ratio of the merging galaxies. The exact formula for this fraction is in Hatton et al. (2003), but the idea is that when one of the two galaxies is much less massive than the other one (minor merger), most of the disc mass stays in the disc. On the contrary, if the two galaxies have comparable masses (major merger), most of the disc mass is transferred to the spheroidal component. The separation between a minor and a major merger is for a mass ratio of 1:3.

Devriendt et al. (in preparation) have used GaICS to investigate the relative importance of bars, minor mergers and major mergers in the formation of spheroids. Elliptical galaxies acquire most of their mass through mergers, although disc instabilities are predominant in forming the bulges of spiral and lenticular galaxies. Minor mergers predominate over major mergers in all galaxy types.

### 2.3.5 Tests of the model

In Fig. 1, the predictions of the GalICS model for the mass function and the stellar ages of local spheroids are shown as solid lines. These predictions are compared with a variety of data (shown as points with error bars, dashed and dotted lines).

The mass function of spheroids is a key test of the model. We have tried to make the comparison as robust as possible by using data derived with completely different methods. The first is to start from the galaxy luminosity function decomposed by morphological type, to assume a bulge fraction for each morphological type and finally to use a bulge mass-to-light ratio to convert the spheroid luminosity function into a mass function. We have applied this method to the 2Mass \( K \) band data of Kochanek et al. (2001) and to the Sloan Digital Sky Survey \( r^* \) band data of Nakamura et al. (2002), both with an aperture correction of -0.2 mag (see Shankar et al. 2004, from where we have taken the bulge-to-total mass ratios for early-type and late-type galaxies, and the \( K \) band and \( R \) band mass-to-light ratios). With these data, we have found the mass functions shown by the open diamonds (Kochanek et al. 2001) and the dotted line (Nakamura et al. 2002) in Fig. 1. The second way to compute the spheroid mass function is to perform a bulge to disc decomposition on a complete galaxy sample, to determine a bulge mass function and then to use a bulge mass-to-light ratio. The open triangles show the result of this method with the \( I \) band spheroid luminosity function of Benson et al. (2002). The third method does not pass through galaxy luminosities at all. Instead, it uses the relation of bulge mass and velocity dispersion to convert the Sloan early-type galaxies velocity dispersion distribution (e.g. Cattaneo & Bernard 2003) into a spheroid mass function. The spheroid mass function computed through this method is shown by the dashed line (which misses the bulges of spirals because it is derived from a sample of early-type galaxies). The luminosity functions by Kochanek et al. (2001) and Nakamura et al. (2002) give very similar results. The mass functions obtained from Benson et al. (2002) and Cattaneo & Bernard (2003) resemble each other very closely, too, while there is difference...
Figure 1. The properties of spheroids in the GaIICS model and in the data. The left panel compares the spheroid mass function predicted by GaIICS (solid line) with those inferred from the 2Mass K luminosity function of Kochanek et al. (2001) (diamonds with error bars), the Sloan Digital Sky Survey r* band luminosity function of Nakamura et al. (2004) (dotted line), the I band luminosity function of Benson et al. (2002) (triangles with error bars) and the Sloan Digital Sky Survey velocity dispersion distribution in Cattaneo & Bernardi (2003) (dashed line). The right panel shows the mass - stellar age relation in GaIICS (small points; the solid line shows the mean value) and in the Sloan Digital Sky Survey (Cattaneo & Bernardi 2003, points with error bars).

between the first and the second group. However, the overall impression is that there is good agreement between the model and the data. In this comparison, we should have in mind that the dark matter simulation cannot resolve haloes less massive than $1.6 \times 10^{11} M_\odot$. (haloes that contain less than $2 \times 10^{10} M_\odot$ in baryons). Therefore, a galaxy less massive than $2 \times 10^{10} M_\odot$ is formally below the resolution limit.

In the case of Fig. 1, the importance of resolution effects is reduced by the fact that the fraction of the baryonic mass in bulges is small in low mass haloes.

The second panel of Fig. 1 shows the mean stellar ages of spheroids in GaIICS (solid line) and in the Sloan Digital Sky Survey (points with error bars). The small points show the scatter in GaIICS ages. The points with error bars come from Cattaneo & Bernardi (2003) using $M_{\text{bulge}} \sim 10^{11} (\sigma/200 \text{ km s}^{-1})^4$, where $\sigma$ is the stellar velocity dispersion of the spheroid. The stellar ages of spheroids that we are comparing are not exactly the same thing because the model outputs are mean values weighted by stellar mass, while the mean values inferred from the Sloan Digital Sky Survey are weighted by luminosity, but the difference should not be large for the $r$-band, especially for massive galaxies with old stellar populations. The agreement is acceptable but not so good as that found for the spheroid mass function. In the cosmology used for this paper the Universe is 13.7 Gyr old. Lookback times of 7, 10 and 11 Gyr correspond to redshifts of 1, 1.7 and 2.3, respectively. Low mass ellipticals are older in the model than in the data because at low mass disc galaxies contaminate the early-type sample, but the real problem is at large masses. GalICS shows that the typical redshift of formation of the stars in a galaxy with $M_{\text{bulge}} \sim 2.5 \times 10^{11} M_\odot$ is of $z \sim 1.1$ whereas the data suggest a value closer to $z = 1.7$. This discrepancy is a sign that the formation of spheroids in semi-analytic models of galaxy formation is an open problem and indicates the need of more work on this topic.

In Fig. 2 we show the cosmic evolution of the galaxy merging rate by plotting total masses (stars and cold gas) and gas masses for all mergers that have occurred in 4 time spans of 100 Myr each at redshifts of about 2, 1, 0.5 and 0. This figure contains more information than a plot of the merging rate as a function of redshift for galaxies above a mass threshold. The decrease of the merging rate as a function of redshift is not dramatic because the larger intergalactic distance at lower density of is compensated by a larger galaxy number, especially at high galaxy masses. On the other hand, low redshift mergers have a tendency to a lower gas fraction.

2.4 Galaxy luminosities

Stellar spectral energy distributions (SEDs) in the optical and near infrared are computed by convolving the star formation history of each component with the SEDs derived from the STARDUST (Devriendt et al. 1999) stellar population synthesis model. STARDUST calculates the SEDs associated with a single burst of star formation at time intervals that go from 10 Myr to 50 Gyr. These SEDs assume a Kennicutt stellar initial mass function and depend on the metallicity of the stellar population. Dust absorption is computed with an extinction law depending on the mean hydrogen column density and the gas metallicity. The column density depends on the mass and the geometry of the gas distribution. GaIICS uses two models: a spheroidal distribu-
Figure 2. Total masses (stars and cold gas, x-axis) and gas masses only (y-axis) for mergers that have occurred in four time intervals of 100 Myr each at redshifts of 2, 1, 0.5 and 0. The dashed lines correspond to the position on the plots of mergers in which the galaxies are 100% gas. Notice that the plotting range on the vertical axis is different in each plot.

3 THE STRUCTURE OF THE AGNICS MODEL

3.1 Black hole growth model

The most recent data suggest that most bulges contain a supermassive black hole (see the Introduction). We do not know how these black holes formed, although Rees (1984) identified a number of astrophysical paths that are likely to result in the formation of a supermassive black hole. The main problem is how gas concentrates from a scale of \( \sim 100 \) pc down to \( \sim 1 \) pc. We do not try to model the complicated physics of how gas flows from the galaxy into the accretion disc and then from the accretion disc into the supermassive black hole. Instead, we accept as a fact that whenever there is a bulge or a starburst, there is a supermassive black hole.

The model for black hole growth is based on three ingredients: the initial black hole mass, the model for black hole accretion and the model for black hole coalescence.

3.1.1 Seed mass

The initial black hole mass is important in models where the black hole mass determines the maximum accretion rate. If the accretion rate cannot exceed the Eddington limit (discussed in Section 3.2), then a larger initial mass allows the black hole to grow more rapidly. If we do not limit the accretion rate to the Eddington limit, then the value of the initial black hole mass is irrelevant (at least as long as the initial black hole mass is \( \lesssim 10^5 M_\odot \)).

3.1.2 Accretion rate

The model for black hole accretion is the fundamental element that distinguishes between different models in the literature and also between different implementation of the AGNICS model. There are two families of models: those in which black holes grow through the accretion of cold
gas (e.g. Cattaneo et al. 1999, Kauffmann & Haehnelt 2000, Enoki et al. 2003), in which case we expect a relation between black hole growth and star formation, and those in which black hole grow through spherical Bondi (1952) accretion of hot gas (e.g. Nulsen & Fabian 2000). In this paper we only fuel AGN with cold gas. We tried to develop models of the second type but we were not able to do it without over-predicting the number density of bright quasars at low redshift. The reason is that, at low redshift, potential wells are deeper and haloes are less dense, with the consequence that shock heating is more effective, the cooling time is longer and a higher baryonic fraction is in hot gas.

Within the family of models in which black hole accretion is fuelled with cold gas and triggered by mergers, we can identify different prescriptions for the gas mass accreted by the black hole. Cattaneo et al. (1999) assumed that at each major merger the black hole accretes a mass \( \Delta M_{\bullet} \propto (1 + z)^α \Delta M_{\text{burst}} \), where \( \Delta M_{\text{burst}} \) is the stellar mass formed by the merger (in practice the mass of the gas in the discs of the merging galaxies) and \( \eta \) is a free parameter determined to reproduce the cosmic growth of the comoving mass density in supermassive black holes (a reasonable agreement with the data required that \( \eta \sim 2 \)).

Kauffmann & Haehnelt (2000) assumed that on average, at each major merger, the black hole accretes a mass

\[
\Delta M_{\bullet} = \frac{f_{\text{BH}} M_{\text{cold}}}{1 + (280 \text{ km s}^{-1}/V_c)^2},
\]

where \( M_{\text{cold}} \) is the mass of cold gas in the merging galaxies, \( V_c \) is the host halo circular velocity and \( f_{\text{BH}} \) is a free parameter determined from the black hole-to-bulge mass relation. The accretion was distributed over time with the law:

\[
\dot{M}_{\bullet} = \Delta M_{\bullet} \exp \left(-\frac{t}{t_{\text{acc}}(z)}\right),
\]

where \( t_{\text{acc}}(z) \) is a free parameter determined by fitting the quasar luminosity function. Enoki et al. (2003) used a very similar model with

\[
\Delta M_{\bullet} = f_{\text{BH}} \Delta M_{\text{burst}} = \frac{f_{\text{BH}} M_{\text{cold}}}{0.75 + (280 \text{ km s}^{-1}/V_c)^2},
\]

where \( \Delta M_{\text{burst}} \) is the total mass of the stars formed in the starburst that accompanies the merger.

In AGNICS we integrate a differential equation for the black hole mass. In this paper we only consider models of the form:

\[
\dot{M}_{\bullet} = k M_{\text{burst}}.
\]

\( M_{\text{burst}} \) is the star formation rate in the starburst component. Black holes in starbursts are active while black holes in galaxies that do not contain a starburst are quiescent. The accretion efficiency \( k \) can depend on a large number of parameters (morphologies of the merging galaxies, gas fraction, structure of the intergalactic medium, effect of AGN and supernova feedback, impact parameter, inclination of the orbital plane with respect to the discs of the merging galaxies, corotation or counterrotation of the two discs, black hole spin, etc.). In practice, we only consider very simple cases. In this paper we discuss four of them (Table 1 summarizes all the models considered in this paper):

- \( k = \text{constant} \): there is a one-to-one relation between black hole growth and starbursts. This is what we called the basic model and corresponds to model A.
- \( k = \text{constant}, \ M_{\bullet} \leq M_{\text{Edd}} \) (model B).
- \( k \propto \rho_{\text{cold}} \) where \( \rho_{\text{cold}} \) is the density of the gas in the starburst component. This is the reference model, which gives the best fit to the data and corresponds to models C, D and E.
- \( k \propto \rho_{\text{cold}}/[1 + (280 \text{ km s}^{-1}/V_c)^2] \) to suppress black hole growth in small haloes (model F).

These recipes describe a mean accretion rate: the approach model oversimplifies the physics of individual objects, but can be expected to be meaningful in a statistical sense, when it is used to compute mean values in a cosmological volume. However, neglecting the dependence of \( k \) on other parameters will lead to underestimate the scatter in the properties of black holes and AGN. The scatter in the results of the simulations can only be meaningful as a lower limit to the scatter predicted by the model. Another remark: Eq. (3) implies that the AGN duty cycle coincides with the entire duration of the starburst. This is a simplification because black hole accretion is likely to be highly time-dependent, as it is shown by AGN variability.

3.1.3 Black hole coalescence

The third choice that one has to make to complete the black hole growth model is what happens when two galaxies with black holes merge. We assume that the black holes immediately coalesce prior to any gas accretion. This is not a good description of reality if the active phase starts before the black holes have merged (it is not difficult to find images of quasar hosts with double nuclei). It is also possible that a third black hole from a second merger reaches the centre before the two black holes from the first merger have had time to coalesce. In this case, the three-body interaction may result in the ejection of one black hole from the galaxy (Begelman et al. 1980, Hut & Rees 1992, Volonteri et al. 2003). Nevertheless, the simple assumption of instantaneous coalescence is the most natural within the assumption of instantaneous morphological transformation at the time of merging used in semi-analytic models.

3.2 Luminosity and spectral energy distribution of AGN

The bolometric luminosity of a quasar is

\[
L_{\text{bol}} = \frac{\epsilon_{\text{rad}}}{1 - \epsilon_{\text{rad}}} M_{\bullet} \dot{M},
\]

where \( \epsilon_{\text{rad}} \approx 0.1 \) is the radiative efficiency of black hole accretion. Bardeen (1993) explains the physics of this value.

The Eddington luminosity \( L_{\text{Edd}} \) is the critical luminosity above which the radiation pressure is stronger than the gravitational attraction. The justification for requiring \( L_{\text{bol}} \leq L_{\text{Edd}} \) is that, as soon as the Eddington luminosity is exceeded, radiation pressure pushes the gas outwards and brings the accretion rate back to sub-Eddington values. However, there are physical situations in which this limit can be exceeded, e.g. if the emission is beamed into a narrow cone or if photons are trapped into a radiatively inefficient, optically thick flow and advected into the event horizon (Begelman 1978). In the latter case it is possible to have \( M_{\bullet} > M_{\text{Edd}} \) without requiring that \( L_{\text{bol}} > L_{\text{Edd}} \).
(here $M_{\text{Edd}}$ is the black hole accretion rate for which Eq. 6 gives $L_{\text{bol}} = L_{\text{Edd}}$). Imposing the condition $M_\text{} \leq M_{\text{Edd}}$ introduces a characteristic time-scale for the growth of the black hole. This time-scale is linked to the Salpeter time $t_S = 4 \times 10^8$ yr, the time in which a black hole radiating at the Eddington limit releases its entire mass energy $M_\text{} c^2$. Since a black hole cannot radiate its entire mass energy, the accretion time-scale is limited to $t_{\text{accr}} = \epsilon_{\text{rad}} t_S$ and the black hole mass cannot grow faster than $\exp(-1/t_{\text{accr}})$.

Mirabel & Rodríguez (1999) have shown that some microquasars in the Milky Way are accreting well above the Eddington limit. In this paper we consider different models (see Table 1): the default assumption is that nothing stops black holes from accreting at super-Eddington rates, but the luminosity cannot exceed the Eddington limit. This is the same assumption of Kaufmann & Hachneld (2009).

The standard reference in the literature for the quasar SED is the Elvis et al. (1994) median SED inferred from radio, sub-millimetre, infrared, optical, ultraviolet and X-ray observations of a sample of optically selected quasars. With this template, the blue magnitude of an optical quasar is

$$M_R = -23.64 - 2.5 \log(L_{\text{bol}}/10^{46} \text{ erg s}^{-1})$$

and the colours are: $U - B = -0.911$, $B - V = 0.092$, $V - R = 0.320$ and $R - K = 3.287$. The Elvis et al. (1994) SED gives a bolometric correction of $\approx 32$ for the 2-10 keV X-ray band. Marconi et al. (2004) have shown that a luminosity-dependent bolometric correction provides a more adequate fit to the X-ray data and it is their model that we use to compute X-ray luminosities.

### 3.3 Obscured AGN

Obscured AGN are AGN where the optical/UV continuum and the broad line spectrum are not observable. Unified models state that unobscured and obscured AGN are intrinsically the same type of systems, made of a central black hole surrounded by its accretion disc and, more further out, by a dusty torus. In obscured (also called type 2) AGN, the system is observed from the equatorial plane of the torus and the optical/UV continuum is not observable because it is absorbed by dust on the line of sight. Obscured AGN can be detected in hard X-rays, at optical wavelengths (through scattered polarised light and strong narrow line emission), by using mid-infrared spectroscopy and with radio observations (see the review article by Risaliti & Elvis 2004). Ueda et al. (2003; Szokoly et al. 2004; Barger et al. 2005) used X-ray selected sample to estimate the fraction of obscured AGN and found that the result is strongly luminosity-dependent (Fig. 3). Most bright quasars are unobscured, while $> 75\%$ low luminosity AGN are obscured. These findings are consistent with those by Sazonov et al. (2004), who studied the combined cosmic infrared and X-ray background and inferred an obscured/unobscured ratio of a factor of three. Optical extinction is therefore an important effect and can shift the peak of the cosmic accretion history of supermassive black holes to lower redshifts (e.g. Cattaneo & Bernardi 2004; Steffen et al. 2003).

The Elvis et al. (1994) SED is a phenomenological template for unobscured (type 1) quasars. It contains three components: the big blue bump (due to thermal emission from the accretion disc), the infrared bump (due to thermal emission from the inner edge of the dusty torus) and the X-ray bump (due to Comptonization of accretion disc light). We cannot treat AGN extinction as we do with the absorption of stellar light by dust, where we assume a covering factor of $\sim 1$, because that grossly underpredicts the number of AGN by extinguishing the entire quasar population with $A_V \sim 5$. Instead, we assume that for a given bolometric luminosity there is an obscuration probability $f_{\text{obs}}(L_X)$, which is determined phenomenologically from the data in Fig. 3. This is the same as to assume that the torus has a luminosity-dependent opening angle. When an AGN is viewed from the equatorial plane of the torus we still see the infrared thermal emission from the torus and the X-ray emission from the central engine (assuming that we can neglect self-absorption at infrared wavelengths and that the torus is not Compton-thick).

The most delicate point is the choice of the function $f_{\text{obs}}$. Fig. 3 shows the two model functions used in this paper. The first one, shown by the dashed line, fits the data Ueda et al. (2003) and Szokoly et al. (2004), while the second one, shown by the solid line, is closer to the new data by Barger et al. (2005). The two lines cover only a small fraction of the luminosity range because AGN with $L_X \lesssim 3 \times 10^{46}$ erg s$^{-1}$ are too faint to contribute to the luminosity function of optical quasars and we do not want to extrapolate the curves beyond the range to which we are applying them as a phenomenological model for the extinction of quasars by dust.
Table 1. Models used to produce the figures of the paper. In the most general case, the black hole accretion efficiency $k$ (Eq. 5) depends on the mass of the gas in the starburst $M_{11}$ (in units of $10^{11} M_\odot$), on the starburst radius $r_{\text{burst}}$ (in kpc) and on the halo circular velocity $V_{280}$ (in units of 280 km s$^{-1}$). We have considered three models for the physics of the Eddington limit. In models A and E, the Eddington limit is completely ignored. In model B, black holes are constrained to accrete at sub-Eddington rates. In models C, D and F, black holes can grow at super-Eddington rates but their luminosities cannot exceed the Eddington limit. The radiative efficiency $\epsilon_{\text{rad}}$ is the one used in Eq. (6) to convert the black hole accretion rate into a bolometric luminosity. The extinction laws I and II refer to the solid line and the dash line in Fig. 3, respectively.

| Model     | $k$         | Eddington limit | $\epsilon_{\text{rad}}$ | Extinction |
|-----------|-------------|-----------------|-------------------------|------------|
| A (the basic model) | 0.0017 | $M_\bullet \leq M_{\text{Edd}}$ | 0.26 | II |
| B          | 0.0017 | $L_{\text{bol}} \leq L_{\text{Edd}}$ | 0.1 | II |
| C (the reference model) | 0.0012 | $M_\bullet \leq 10^{-7} M_{\odot}$ | 0.08 | II |
| D          | 0.0012 | $L_{\text{bol}} \leq L_{\text{Edd}}$ | 0.1 | I |
| E          | 0.0012 | $L_{\text{bol}} \leq L_{\text{Edd}}$ | 0.1 | I |
| F          | 0.0012 | $L_{\text{bol}} \leq L_{\text{Edd}}$ | 0.1 | I |

Figure 4. The simulated black hole mass - bulge mass relation in a model in which the black hole accretion rate is directly proportional to the star formation rate in the starburst component ($\dot{M}_\bullet = 0.0017 \dot{M}_{\text{burst}}$). The left and the right panel shows the model predictions respectively without and with the condition $\dot{M}_\bullet \leq \dot{M}_{\text{Edd}}$ (models A and B of Table 1). Model B is computed for a seed mass of $M_\bullet = 10^{-7} M_{\odot}$ where $M_{\odot}$ is the mass of the gas in the starburst component. The predictions made by AGNICS are shown as dots, blue for black holes in disc-dominated galaxies, red for black holes in bulge-dominated galaxies. The open squares are the mass estimates by Marconi & Hunt (2003) and the filled triangles those by Haring & Rix (2004). The dashed-dotted lines corresponds to a 1.12 slope (the best fit to the data of Haring & Rix 2004) and the dashed lines show a scatter of $\pm 0.3$ dex around this relation. The solid line is the Marconi & Hunt (2003) $M_\bullet = 0.002 M_{\odot}$ relation rescaled for $M_\bullet = 0.0017 M_{\odot}$. These lines and the data points are the same in both panels.

4 BLACK HOLE MASSES AND THE REDSHIFT EVOLUTION OF THE QUASAR POPULATION

We want to determine if a model in which the black hole accretion rate is related to the star formation rate in the proto-spheroid (Eq. 5) can reproduce the masses of black holes in nearby galaxies and the cosmic evolution of the quasar population.

4.1 The basic model

The simplest scenario is that the black hole accretion rate is directly proportional to the star formation rate in the starburst component (models A and B of Table 1). This assumption gives a tight $M_\bullet - M_{\text{bulge}}$ relation consistent with a linear scaling. The left and the right panel in Fig. 4 present the case without and with the constraint $M_\bullet \leq M_{\text{Edd}}$, respectively. The blue and the red points are the results of the simulations for disc-dominated (late-type) and bulge-dominated (early-type) galaxies. The open squares are the mass estimates by Marconi & Hunt (2003) and the filled tri-
angles those by Haring & Rix (2004). The solid line shows the linear relation $M_{b, \text{bulge}} = 0.0017 M_{\text{bulge}}$. These lines and the data points are the same in both panels.

The tight $M_{\bullet} \propto M_{\text{bulge}}$ relation follows directly from our assumption. The $\sim 0.1$ dex scatter in the left panel (model A) is due to the presence of a stellar component in the discs of the merging galaxies. In a merger, the masses of the two bulges add together, and so do the masses of the two black holes. The gas in the discs of the merging galaxies contributes to the formation of bulge stars and to the growth of the black hole in a fixed proportion. However, the stars in the discs of the merging galaxies can only contribute to the growth of the bulge mass, and as the gas fraction is lower at high masses (Fig. 2), high mass mergers produce lower values of $M_{\bullet}/M_{\text{bulge}}$ and a shallower $M_{\bullet} - M_{\text{bulge}}$ relation at high masses. The model with $M_{\bullet} \leq M_{\text{Edd}}$ (model B) contains more scatter because the Eddington limit introduces a characteristic time-scale for the growth of the black hole. In some galaxies with a short star formation time-scale, the starburst may be over before the black hole has had time to grow significantly. Nevertheless, the similarity between the two panels of Fig. 4 indicates that the importance of this effect is limited.

The basic model cannot reproduce the observational scatter in any of the two versions. That is not surprising, because we expect that our approach underestimates the scatter, since it ignores many parameters that can affect the mass accreted by black holes (Section 3.1). The real problem comes from the quasar luminosity function (Fig. 5).

Once we have specified the black hole growth model, our only freedom to fit the quasar luminosity function is in the value of the radiative efficiency parameter $\epsilon_{\text{rad}}$ and in the choice of the extinction law (the fraction of type 2 AGN as a function of the X-ray luminosity, $f_{\text{obs}}(L_X)$). The luminosity functions corresponding to models A and B in Fig. 5 were computed for a radiative efficiency of $\epsilon_{\text{rad}} \approx 0.26$ by using the extinction law II in Fig. 3. Very likely, these assumptions overestimate the blue light that comes out of powerful AGN. Nevertheless, Fig. 5 shows that model A underpredicts the number of bright quasars at $z \sim 2$ (model B is even worse).

We can improve the fit to the luminosity function at $z \sim 2$ by pushing the radiative efficiency to an even higher value, by removing optical extinction completely and by increasing the normalisation of the $M_{\bullet} - M_{\text{bulge}}$ relation (the data allow an increase up to a maximum of 30%). However, that misses the physical point, besides the difficulty of justifying such assumptions. The problem exists because the basic model underestimates the scatter in the black hole mass distribution. If the black hole mass distribution is a Gaussian in $\log(M_{\bullet})$, then more scatter in $\log(M_{\bullet})$ with the same mean value of $\log(M_{\bullet})$ increases the comoving mass density of supermassive black holes, which automatically raises the total light output of the quasar population. Therefore, we can fix the lack of bright quasars at $z \sim 2$ just by introducing a scatter factor $\propto \chi^5$ in front of the right hand side of Eq. 4, where $\chi$ is a Gaussian random deviate.

However, that does not solve the second problem of model A: the simulated evolution of the quasar luminosity function between $z \sim 2$ and $z \sim 0.5$ is not so strong in the model as it is in the data (here we have made the comparison with the 2dF data by Croom et al. 2004, This finding is not surprising because the figures in Kauffmann & Haehnelt (2000) and Cattaneo (2001) had already shown this limitation of the simplest scenario. The Durham group too has encountered the same problem when they have started trying and incorporating AGN into their semi-analytic model of galaxy formation (R. Malbon, private communication).

4.2 The reference model

The method to obtain a model that by construction reproduces the strong evolution of the quasar population is to identify the parameters that are significantly different in high and low redshift AGN and to force a dependence of the black hole accretion rate on these parameters. We find that the main difference between $z \sim 2$ and $z \sim 0.5$ AGN is not in the gas fraction or in the potential well, but in the density of the gas in the central starburst that fuel the AGN. Therefore, we choose to explore a model in which the black hole accretion rate is

$$M_{\bullet} \propto \rho_{\text{burst}} M_{\text{burst}}.$$

Cattaneo, Haehnelt & Rees (1999) used a similar approach when they assumed that $\Delta M_{\bullet} \propto (1 + z)^{\eta} \Delta M_{\text{burst}}$ with $\eta = 2$ in order to obtain a reasonable agreement with the cosmic evolution of the comoving mass density of supermassive black holes. The difference is that here $z$ does not appear explicitly. We find a reasonable agreement with the local black hole masses and with the luminosity function of quasars for a dependence with a power of $\zeta = 0.5$, a radiative efficiency of $\epsilon_{\text{rad}} = 0.1$ and model II for the fraction of obscured AGN (Figs. 5-6, model C, called the reference model hereafter).

4.2.1 Black hole masses

The blue (late-type galaxies) and red (early-type galaxies) point clouds in Fig. 6 show the results of the reference model at different redshifts while the squares and the triangles with error bars are the mass estimates by Marconi & Hunt (2003) and Haring & Rix (2004), and are the same in all four panels. In fact, they are the same as in Fig. 4. The black hole mass distribution at $z = 2$ is bimodal because two processes fuel AGN: mergers (predominant in elliptical galaxies) and bar instabilities (predominant in spiral and lenticular galaxies). Low redshift starbursts are less dense and form objects with lower values of $M_{\bullet}/M_{\text{bulge}}$. This mechanism generates scatter in the $M_{\bullet} - M_{\text{bulge}}$ relation. At low redshift the scatter becomes so large that it erases any trace of the original bimodality and creates a continuity between the products of bars and those of mergers.

The $\rho_{\text{burst}}^{0.5}$ factor not only introduces scatter, but also increases the slope of the $\log(M_{\bullet}) - \log(M_{\text{bulge}})$ relation, since the densest starburst are also the most massive ones. Perhaps it is not coincidental the data contain a tilt in the same sense (the lines in Fig. 6 show the $M_{\bullet} \propto M_{\text{bulge}}$ relation found by Haring & Rix (2004).

Since Ferrarese & Merritt (2000) and Gebhardt et al. (2000), there has been considerable interest in the $M_{\bullet} - \sigma$ relation, where $\sigma$ is the velocity dispersion of the host bulge. This interest has been due to the discovery that the $M_{\bullet} - \sigma$ relation contains less scatter than the $M_{\bullet} - L_{\text{bulge}}$ relation, where $L_{\text{bulge}}$ is the optical luminosity of the host bulge. Nevertheless, Marconi & Hunt (2003) and Haring & Rix (2004)
Figure 5. The outputs of AGNICS (solid lines) for the six models listed in Table 1 compared with the 2dF quasar luminosity function of Croom et al. (2004) (points with error bars). The shaded areas show the error bars in the simulated luminosity functions.
Figure 6. The small points show the simulated black hole mass - bulge mass relation in a model in which $\dot{M}_\bullet = 0.0012(M_{\text{cold}}/10^{11}M_{\odot})^{0.5}(r_{\text{burst}}/\text{kpc})^{-1.5}M_{\text{burst}}$ (the reference model). Here $M_{\text{cold}}$, $r_{\text{burst}}$ and $M_{\text{burst}}$ are the gas mass, the Hernquist radius and the star formation rate of the starburst component. The blue points are for black holes and bulges of late-type galaxies. The red points are for black holes and bulges of early-type galaxies. The open squares are the mass estimates by Marconi & Hunt (2003) and the filled triangles those by Haring & Rix (2004). The dashed-dotted lines corresponds to a 1.12 slope (the best fit to the data by Haring & Rix 2004) and the dashed lines show a scatter of $\pm 0.3$ dex around this relation. These lines are the same in all four panels. They refer to data at $z = 0$ but they have also been shown in the diagrams at $z > 0$ to ease the comparison. The results of the AGNICS model are shown for four different redshifts. The formal resolution of the simulation is $2 \times 10^{10}M_{\odot}$ for the galaxy and $4 \times 10^{7}M_{\odot}$ for the black hole.

have shown that the $M_\bullet - M_{\text{bul}}$ is as tight as the $M_\bullet - \sigma$ relation. Therefore, there is no reason to believe that the latter is more fundamental than the former. However, we have chosen to show our simulated $M_{\text{bul}} - \sigma$ relation (Fig. 8). This appears to have a shallower slope than that inferred from the mass estimates of Ferrarese & Merritt (2000) and Tremaine et al. (2002), but the difference is entirely attributable to the slope in the $M_{\text{bul}} - \sigma$ relation, which is shallower in GalICS than in the data (see the dashed line in Fig. 8). The result is not so bad if we consider that GalICS calculate radii, and therefore velocity dispersions, of bulges assuming that mergers conserve the mass and the total energy, while neglecting the loss of mass and energy in tidal tails and ignoring any angular momentum consideration.
4.2.2 Evolution of the AGN population

The fiducial model assumes that \( M_\bullet \propto \rho_\text{burst}^{0.5} \rho_\text{burst}^{0.5} \). The scatter introduced by the \( \rho_\text{burst} \) factor is large enough that it allows to fit the luminosity function of quasars with \( \epsilon_{\text{rad}} = 0.1 \) (model C of Fig. 5) without violating the constraints on black hole masses (Fig. 6). In Fig. 7, we take exactly the same model and compare its predictions with the data from COMBO-17 (Wolf et al. 2003), which probe fainter AGN and higher redshifts (left panel). In the right panel, we show the predictions of our model for the comoving number density of AGN with \( 10^{44} \text{erg} \text{s}^{-1} < L_{\text{2-10 keV}} < 3 \times 10^{44} \text{erg} \text{s}^{-1} \) and \( 3 \times 10^{44} \text{erg} \text{s}^{-1} < L_{\text{2-10 keV}} < 10^{46} \text{erg} \text{s}^{-1} \). The solid lines and the dashed lines are the predictions derived with the bolometric corrections in Marconi et al. (2004) and Elvis et al. (1994), respectively. We compare these predictions with the data by Ueda et al. (2003) (points with error bars). The model that uses the bolometric corrections proposed by Marconi et al. (2004) is in better agreement with the data.

The fraction of obscured AGN in model C is computed with extinction law II, given by the dashed line in Fig. 3. We should clearly say that this law has been deliberately chosen to fit the blue luminosity function without obscuration and the optical data is due to extinction. The change in the extinction law at the magnitude separation of 2.44. The success of our model is not a mere consequence of the change in the extinction law at the magnitude separating high and low redshift data. Fig. 7 also shows that our model can reproduce a good agreement with the X-ray data. This agreement is independent of the obscuration model and supports the conclusion that the discrepancy between the blue luminosity function without obscuration and the optical data is due to extinction.

We introduced a steep increase in the type 2 fraction at low luminosities to suppress the number of AGN with \( M_B > -24 \) Kauffmann & Haehnelt (2000) and Enoki et al. (2003) dealt with the same problem by introducing a low circular velocity cut-off (Eqs. 4.1). Model F shows our results when we apply this solution in combination with the extinction law I derived from the data in Ueda et al. (2003). The fit to the data is good at \( z \simeq 2 \) and \( z \simeq 0.5 \). The discrepancy at \( z \simeq 1 \) occurs because all our AGN \( z \simeq 1 \) are in large galaxy groups, where the low circular velocity cut-off has limited consequences, but this may be an effect of small number statistics due to cosmic variance together with the finite size of the computational box. The model with the low circular velocity cut-off gives a steeper slope in the \( \log(M_\bullet) - \log(M_{\text{bulge}}) \) relation than the model without this cut-off.

Model E is an alternative version of model C in which we have dropped the \( L_{\text{bol}} \leq L_{\text{Edd}} \) condition. The excess of blue light from super-Eddington AGN is compensated by reducing the radiative efficiency from \( \epsilon_{\text{rad}} = 0.1 \) to \( \epsilon_{\text{rad}} = 0.000 \) RAS, MNRAS 000, 000–000
active black holes are objects of \( \sim \) M_
ogalaxies deriving from the size of the computational box. At baryons with respect to the dark matter, although Figs. 1 of galaxy formation or anti-hierarchical evolution of the (Monaco et al. 2000; Granato et al. 2001; Corbin & Vacca 2002). The continuous solid line is a fit to the data of Tremaine et al. (2002), and has a slope of 4.02. The dashed line has a slope of 2.4. It is not a fit and is only shown to guide the eye.

0.08. Model E fits the data even better that model C does, but we have chosen to present model C as our reference model because its assumptions are more standard.

4.2.3 AGN activity and black hole mass

Fig. 9 shows relation between the mass of the black hole and the luminosity of the AGN in model E (the reference model without the \( L_{\text{bol}} \leq L_{\text{Edd}} \) condition). This figure prompts two considerations. The first one is that, even when we remove the Eddington limit, it is very difficult to find quasars brighter than \( 3 \times 10^7 L_{\odot} \). The second one is the limited statistics deriving from the size of the computational box. At \( z = 2 \), there are 22 quasars with \( M_B < -24 \) and only 4 with \( M_B < -26 \).

Fig. 10 presents the cosmic evolution of the mass function of supermassive black holes and the fraction of black holes that are active at an \( M_B < -22 \) level as a function of black hole mass. These plots are identical for models C and E. The black hole mass function shows that black holes are still growing at \( 1 < z < 2 \), but the growth is small at \( z < 1 \). The evolution in the interval \( 1 < z < 2 \) is stronger at \( M_\bullet \sim 10^8 M_\odot \) than it is at \( M_\bullet > 10^9 M_\odot \). The fraction of active black holes decreases by almost two orders of magnitude between \( z \sim 2 \) and \( z \sim 0.5 \). The two panels combined suggest a picture in which the most massive black holes form earlier while less massive black holes continue growing to lower redshifts. This is consistent with the finding that the most massive galaxies form at higher redshifts (Monaco et al. 2000; Granato et al. 2001; Corbin & Vacca 2002; Cattaneo & Bernard 2003) also known as down-sizing of galaxy formation or anti-hierarchical evolution of the baryons with respect to the dark matter, although Figs. 1 and 10 show that hierarchical models of galaxy formation can in fact reproduce this behaviour.

5 DISCUSSION AND CONCLUSION

Observational and theoretical arguments (see the Introduction) suggest that the same physical mechanisms are responsible for the growth of bulges and supermassive black holes. The main questions are what are these mechanisms and if they work one-way only (from the galaxy to the black hole) or both ways (through AGN feedback).

Mergers and disc instabilities provide a path for transforming late-type galaxies into early-type galaxies while driving a sudden fuel supply into the galactic nucleus. The importance of this process is demonstrated by hydrodynamic simulations and observed in the real Universe. Semi-analytic models of galaxy formation have incorporated the merger model since the early 1990s and have achieved a substantial degree of success (e.g. Fig. 1), but some discrepancies (overcooling at the centre of massive haloes, late formation of massive galaxies, low SCUBA counts in relation to the blue light that comes out of local galaxies) remain. Critics of semi-analytic models have argued that the great complexity of the models and the inherent large number of free parameters allow for the possibility that incorrect assumptions may be reconciled with the data. After all, the Ptolemaic model allowed to compute the ephemerides with reasonable accuracy, but its basic assumptions were false. This is a real danger when models are developed to reproduce a small number of observational constraints. However, the increasing volume of astronomical data from sub-millimetre, infrared, optical and X-ray bands heavily outnumber the free parameters in the hand of the simulators. The presence of the same discrepancies in models developed independently and the difficulty that the modellers are encountering in solving these problems prove that the semi-analytic approach is robust (although some relevant physics are still missing).

In this paper, we have presented AGNICS (Active Galactic Nuclei In Cosmological Simulations), a hybrid approach that incorporates large cosmological N-body simulations, a semi-analytic model of galaxy formation and a scheme for the growth of supermassive black holes. We have used this model to investigate a scenario where mergers and disc instabilities drive massive gas inflows from galaxy discs into compact central starbursts, while a small fraction of this gas fuels the growth of a supermassive black hole. If \( M_\star \) and \( M_{\text{burst}} \) are simply related by a constant of proportionality, that leaves us with a tight \( M_\star \propto M_{\text{bulge}} \) relation with \( q \leq 1 \). In a standard semi-analytic model, this simple scenario is not consistent with the strong evolution of the quasar population at \( z \leq 2 \) observed in optical studies of the quasar luminosity function (e.g. Groom et al. 2003, and references therein).

Recently, Barger et al. (2005) have plotted the evolution with redshift of the rest-frame 2-8 keV comoving energy density production rate for AGN with \( L_{2-8\text{keV}} > 10^{42} \text{erg s}^{-1} \) and shown that this has a clear peak at \( z \sim 1 \). This result goes in the same sense of an earlier study by Cattaneo & Bernard (2003), where we assumed that supermassive black holes form at the same time as the stellar
Figure 9. The black hole mass - blue luminosity relation in model E (the reference model without the Eddington limit) at four different redshifts. Each diagram is divided in six intervals of black hole mass. The row of numbers in the lower part of each diagram gives the number of black holes in each mass interval for the \((150 \text{ Mpc})^3\) box with \(256^3\) particles in the dark matter simulation. The formal resolution for the black hole mass is \(\sim 4 \times 10^7 M_\odot\).

populations of their host galaxies and used this hypothesis to calculate the evolution with redshift of the total mass accreted by supermassive black holes per comoving volume and unit time. We found a peak at \(z \sim 1.6\), but this can be an overestimate if some stars have formed before the black hole.

The discrepancy between X-ray and optical data is attributed to the presence of an obscured AGN population (type 2 AGN), which predominates at low luminosities, attributed to the presence of an obscured AGN population (type 2 AGN), which predominates at low luminosities. Following the method of Soltan (1982) and Chokshi & Turner (1992), Yu & Tremaine (2002) estimated the mass per unit cosmic volume accreted by optical quasars over the life of the Universe, \(\rho_{\bullet B}\), by using the equation

\[
\rho_{\bullet B} = \frac{C_B}{\epsilon_{\text{rad}} c^2} \int dt \int L_B \phi(L_B, t) dL_B,
\]

where \(\phi(L_B, t) dL_B\) is the number density of quasars with...
blue luminosity between \( L_B \) and \( L_B + dL_B \) at a time \( t \) after the Big Bang and \( C_B \equiv L_{bol}/L_B \) (this equation uses Eq. 9 in the opposite direction). For \( \epsilon_{\text{rad}} = 0.1 \), \( C_B = 11.8 \) (as in Elvis et al. 1994) and the Boyle et al. (2000) model for the luminosity function of quasars, in which \( \phi(L_B, t) = \phi_n(t^a + t^b) \), where \( t \equiv L_B/L_B(t) \) and \( \phi_n, a \) and \( b \) are parameters determined from the data. Yu & Tremaine (2002) found \( \dot{\rho}_{\text{sys}} \simeq 2.1 \times 10^5 M_\odot \text{Mpc}^{-3} \). They compared this value to their estimate of the local mass density of supermassive black holes, \( \rho_\bullet \simeq (2.5 \pm 0.4) \times 10^7 M_\odot \text{Mpc}^{-3} \) and concluded that the need for non-luminous accretion is limited. There are two objections to this argument. The first one is that inserting \( \phi(L_B, t) = \phi_n(t^a + t^b) \) into Eq. 9 extrapolates the power law behaviour outside the measured magnitude range. Barger et al. (2003) argue that this leads to overestimating \( \rho_\bullet \) by a factor of \( \sim 1.8 \). Secondly, most other studies, including Salucci et al. (1999), Merritt & Ferrarese (2001), Marconi et al. (2004), favour values closer to \( \rho_\bullet \sim 4 \times 10^5 M_\odot \text{Mpc}^{-3} \). It seems plausible to conclude that 50–75% of black hole accretion is optically obscured. Sazonov et al. (2004) analysed the combined infra-red and X-ray background and reached a similar conclusion.

With these considerations in mind, we ask ourselves if obscuration, which is more effective on the low redshift luminosity function, can reconcile the simple model \( M_\bullet \propto M_{\text{burst}} \) with the data. The answer is that it cannot because model A in Fig. 5 does not fit the data even if it includes a large amount of obscuration (which may be an overestimate of the type 2 fraction at low luminosities).

There are two possible solutions. The first one is that this problem is related to the other shortcomings of semi-analytic models of galaxy formation. Overcooling in massive haloes, late formation of elliptical galaxies, low number of high redshift sub-millimetre sources, delayed quasar epoch, all point to a scenario in which the most massive baryonic structures form too late. In recent times, there has been great interest on mechanical (jets, winds) and radiative (Compton heating) AGN feedback as a possible answer to this physical problem (Tabor & Binney 1993; Binney & Tabor 1995; Tucker & David 1997; Ciotti & Ostriker 1997, 2001; Quilis et al. 2001; Reynolds et al. 2001a, 2001b; Quilis et al. 2001; Omma et al. 2004; Omma & Binney 2004). In this case, quasars and galaxy formation cease to exist as separate problems because we cannot solve one without solving the other. We plan to present and discuss such a model in a forthcoming publication of the AGNICS series.

The second possibility, which we have studied in this paper, is to introduce a second parameter that breaks the strict proportionality between black hole accretion and star formation. This solution introduces a scatter and a tilt in the \( M_\star - M_{\text{bulge}} \) relation.

A model in which the black hole accretion rate is enhanced by a factor proportional to the square root of the gas density can reproduce the evolution of the quasar population over the entire redshift range covered by 2dF (Croom et al. 2004) and Combo-17 (Wolf et al. 2003) data both at optical and X-ray (Ueda et al. 2003) wavelengths, without need to deviate from the standard radiative efficiency of \( \epsilon_{\text{rad}} \sim 0.1 \) and in a manner that is consistent with the observational constraints on the normalisation, the slope and the scatter of the \( M_\bullet - M_{\text{bulge}} \) relation. This model produces a final black hole mass density of \( \rho_\bullet \simeq 4.4 \times 10^5 M_\odot \text{Mpc}^{-3} \), very close to the most recent estimate of \( 4.5 \times 10^5 M_\odot \text{Mpc}^{-3} \) by Marconi et al. (2004) (see the discussion above). Black holes with \( M_\bullet \gtrsim 2 \times 10^8 M_\odot \) are in bulge dominated galaxies and have mostly grown through mergers. At \( M_\bullet < 10^8 M_\odot \) disc instabilities are an important growth path. The good
agreement with the X-ray data support the conclusion that
the high type 2 fraction that we need to invoke to fit the
optical data at low luminosities has a physical basis. Allowing
or preventing radiation at $L_{\text{bol}} > L_{\text{Edd}}$ does not any
significant difference, which cannot be compensated by a
small change of the value of the radiative efficiency $\epsilon_{\text{rad}}$. It
is difficult to say to which extent this model is physical and
to which extent the factor $\propto \rho_{\text{burst}}^{0.5}$ simply compensates the
shortcomings mentioned above. Up to a point, it certainly
does, but it would be a coincidence if the dependence that
compensates a shortcoming of the galaxy formation model
and gives the appropriate evolution of the quasar luminosity
function was also the dependence that introduces the right
scatter in the black hole mass distribution (and tilts the dis-
tribution of an amount that does not exceed the constraints
on the power of the $M_\bullet - M_{\text{bulge}}$ relation).

The solution proposed in this paper, which breaks the
exact proportionality between black accretion and star for-
formation in favour a higher accretion rate in dense high red-
shift starbursts, makes two observable predictions. The first
one is that the quasar contribution to the total bolometric
luminosity is stronger in the most powerful, denser star-
bursts (Fig. 11). This is a prediction that can be tested
by inspecting the SEDs of ultra-luminous infra-red galax-
ies (ULIRGs) for AGN features and by studying how the
presence and the strength of these features increase with
the total bolometric luminosity of these objects. Tran et al.
(2001) studied the mid-infrared spectra of 16 ULIRGs and
found a transition from mostly starburst-powered to mostly
AGN-powered objects at a luminosity of $\sim 2 - 3 \times 10^{12} L_\odot$
in reasonable agreement with the prediction of the reference
model (Fig. 11). The systematic discussion of the infra-red
and sub-millimetre properties of AGN is left to a future pub-
llication of the AGNICS series. We can anticipate that we
have checked the most fundamental constraints. E.g. even if
we make the extreme assumption that all the AGN power
in the Universe is absorbed and reemitted in the far infrared
by dust in the host galaxies, that could account for
$< 1/3$ of the number of SCUBA sources counted at a flux of $S_{250 \mu m} > 2 \text{mJy}$. The second prediction of our model is
that, for a given bulge mass, the most massive black holes are
found in the bulges with the oldest stellar populations.
Observations (Merrifield et al. 2000) seem to confirm this
second prediction, too, but it is important to have more data
to make this conclusion more secure. Moreover, low redshift
mergers have much lower gas fraction than high redshift
mergers. That can be another explanation why bulges with
younger stellar populations have a lower black hole mass
fraction. The first prediction is thus a cleaner test of our
assumption.

6 ACKNOWLEDGEMENTS

A. Cattaneo acknowledges financial support from the Euro-
pean Commission, through a Marie Curie Research Fellow-
ship, and from the Golda Meir Foundation. He also wishes to
thank A. Dekel, G. Mamon and L. Wisotzki for interesting
discussion.

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