INTRODUCTION

Optimization of operating parameters is a vital step in machining, particularly for operating Computer Numerical Control (CNC) machine tools. Many researchers have investigated machining optimization problems. In this research effective optimization techniques approach response surface methodology is utilized for finding the optimal cutting conditions for best minimum temperature rise and also developed second order mathematical model for process parameters and analysis of variance measured for process parameters to ensure the significant effects.

Experiments are conducted as per the Design of Experiments (DoE) of Response Surface Methodology (RSM) to predict the temperature rise by varying the cutting parameters such as cutting speed, feed rate and depth of cut. In the present study, the experiment was conducted on Aluminium Al 6061 by coated carbide tool. A second order mathematical model in terms of machining parameters was developed for temperature rise prediction using RSM. This model gives the factor effects of the individual process parameters. Values of Prob> F less than 0.05 indicate model terms are significant. The cutting speed is the most important parameter that cause the temperature of the turning process compared to the other factors such as feed rate and depth of cut. Validation results show good agreement between the actual process output and the predicted temperature rise.

The response surface methodology (RSM) is a traditional technique for experimental process optimization. For the RSM, an experimental design was chosen and tests were performed in order to generate the proper models. Results indicate that both methods are capable of locating optimum conditions, with a relatively small number of experiments (Davi Sampaio Correia et al., 2005). The parameters that influence the quality of laser transmission joining were optimized using response methodology for achieving good joint strength and minimal joint width. The central composite second-order Rotational Design (CCRD) has been utilized to plan the experiments and response surface methodology (RSM) is employed to develop mathematical relationships between joining parameters and desired responses. The experimental values nearly agree with the predicted values from mathematical models, indicate that the models can predict the responses adequately and optimize the key process parameters quickly (Xiao Wang et al., 2012).

Response surface methodology (RSM) with the help of Design Expert Version 7.1.6 (STAT-EASE Inc., USA) was used for optimization of the extraction process and evaluation of interaction effects of different operating parameters (Keka Sinha et al., 2012). This study intends to determine the optimal cutting parameters required to minimize the cutting time while maintaining an acceptable quality level. This equation can be determined by studying the output cutting times vs. input cutting parameters through CATIA software, with assistance from the statistical method, response surface Methodology (RSM) (Angus Jeang, 2011).

A predictive model for laser turning process parameters is created using a feed-forward artificial neural network (ANN) technique utilized the experimental observation data based on response surface methodology (RSM) (Dhupal et al., 2009). ANOVA was employed to identify the level of importance of the machining...
Response surface methodology (RSM) is used for modeling whereas multi-objective optimization is performed using hybrid approach of TM and grey relational analysis (GRA) coupled with entropy measurement methodology. The results indicate that the hybrid approaches applied for modeling and optimization of the LBC process are reasonable (Amit Sharma et al., 2012)

The used parameters such as helix angle of cutter, spindle speed, feed rate, axial and radial depth of cut on temperature rise in end milling (Sivasakthivel et al., 2013). The development and utilization of an optimization system, which determines optimum machining parameters for milling operations (Baskar et al., 2005). In this work a mathematical model has been developed based on both the material behavior and the machine dynamics to determine cutting force for milling operations (Palanisamy, et al., 2007). The experimentation work to determine the effects of cutting conditions and tool geometry on the surface roughness in the finish hard turning of the bearing steel (AISI 52100) (Dilbag Singh et al., 2007)

Most published studies on metal cutting regard the cutting speed as having the greatest influence on tool wear and, thus, tool life, while other parameters and characteristics of the cutting process have not attracted as much attention in this respect (Viktor P. Astakhov, 2007)

The design variables used in this research such as depth of cut, cutting speed and the feed rate in each pass. Bounds on depth of cut, cutting speed, feed; surface finishing, cutting force, cutting power and tool life were considered as technological constraints (Conceicao Antonio et al., 2009). The second-order mathematical models, in terms of the machining parameters for each of these five roughness parameters prediction using response surface method on the basis of experimental results (Routara et al., 2009).

The literature indicated above reveals that not much work has been reported on prediction and optimization of temperature rise in turning operation. The main objective of this research is to develop a model based on response surface methodology to the cutting temperature rise in terms of machining parameters such as cutting speed, feed rate, and depth of cut. During turning process, the cutting temperature rise is measured using pyrometer. The second order mathematical model helped us to study the direct and interaction effect of each parameter to ensure the significant effects.

Response Surface Methodology (RSM)

Response surface method (RSM) is the combination of experimental and statistical techniques which are useful for the modeling and analysis of problems in which a response of interest is influenced by several variables. RSM saves cost and time by reducing the number of experiments required for investigation. In this RSM technique, the main objective is to optimize the response i.e temperature rise which is influenced by cutting parameters using design expert software. A second order regression equation is developed. The (Fig.1) flow chart has given to understand the methodology used to study the effect of important parameters:

![Figure 1: Methodology of optimization](image)

**MATERIALS AND METHODS**

**Experimental Designs**

Response surface methodology is the most effective method to analyze the results obtained from factorial experiments. It is an effective tool for modeling and analyzing the engineering problems. It provides more information with less number of experimentation. In most of the RSM problems, the form of the relationship between the response and the independent variables is unknown (Routara et al., 2009)

The limit of the process parameters has to be defined in response surface methodology and the initial experimentation was done to identify the machining parameters that affect the temperature rise and to explore the range of the selected machining parameters (Sivasakthivel et al., 2013). In the present work, cutting speed, feed rate, depths of cut have been considered as the machining parameters. The response temperature rise T can be expressed as a function of process parameters cutting speed (X1), feed rate (X2), and depth of cut (X3).
Zeelan Basha et al.,

Temperature Rise = ϕ(X₁, X₂, X₃) + eₙₜ

Where ϕ is the response surface, eₙₜ is the residual, and u is the number of observations in the factorial experiment and ui represents level of uᵢ in the rᵗʰ factor. When the mathematical form of ϕ is unknown, this function can be approximated satisfactorily within the experimental region by polynomials in terms of the process parameter variable.

In statistics, Box–Behnken designs are experimental designs for response surface methodology, devised by George E.P. Box and Donald Behnken in 1960. Each factor, or independent variable, is placed at one of three equally spaced values, usually coded as -1, 0, +1. In each block, a certain number of factors are put through all combinations for the factorial design, while the other factors are kept at the central values. It has three factors—three levels Box–Behnken rotatable design consisting of 17 sets of actual conditions (Table 1). The design of experiment with response as shown in (Table 2).

Table 1: Process Parameters and their Levels

| No | Cutting parameters (X₁) | unit | -1  | 0  | 1  |
|----|-------------------------|------|-----|----|----|
| 1  | Cutting speed (X₁)      | m/min| 90  | 110| 120|
| 2  | Feed rate (X₂)          | mm/rev| 0.18| 0.27| 0.36|
| 3  | Depth of cut (X₃)       | mm  | 0.2 | 0.4 | 0.6|

Experimental Procedure

The (figure2) experiments were conducted based on the design of experiments using XLTURN-CNC lathe. The specification of the XLTURN-cnc lathe has been given below.

Specification: Control system-fanuc emulated
Spindle power-1Hp
Spindle speed-100 to 3000 rpm
Max. Turning dia-32mm
Rapid traverse rate-1.2m/min

The figure 3 suitable tool insert has been selected from the tool selection guide. The model tool AK10 Carbide Inserts turning Ground and Polished for Aluminium Uni-tip was used for turning process.

The work piece material used for the turning process is aluminium 6061 and the material hardness has been tested, found to be 43 HRC. The chemical composition of aluminium 6061(Table 3).

The temperature was measured by using pyrometer and the observations are tabulated to obtain the mathematical model (Table 2).
Development of Mathematical Model

In statistics, regression analysis is a statistical process for estimating the relationships among variables. It includes many techniques for modeling and analyzing several variables, when the focus is on the relationship between a dependent variable and one or more independent variables. The general form of a quadratic polynomial which gives the relation between response surface \( y \) and the process variable \( x \) under investigation is given by

\[
Y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_1 x_1^2 + \beta_2 x_2^2 + \beta_{12} x_1 x_2, \quad \text{equ. 1}
\]

Where \( \beta_0 \) is a constant, \( \beta_1, \beta_2, \beta_{12} \) is the quadratic term coefficient and \( \beta_{12} \) is the interaction term coefficient (Sivasakthivel et al., 2013).

Regression equations (equ.2) were formed using values of the coefficients of the polynomials. A statistical software design expert 8.0 was used to calculate the values of these coefficients. The second order mathematical model is developed using the experimental values and responses by neglecting the insignificant coefficients to predict the temperature rise (T).

Temperature rise (T) = 407.17500 - 7.10200 * \( X_1 \) - 77.72222 * \( X_2 \) - 0.031756 * \( X_1^2 \) + 12.37500 * \( X_2^2 \) - 68.51852 * \( X_1 \) * \( X_2 \) = 2.104852 * \( X_1^3 \) + 12.37500 * \( X_2^3 \),

Where

\[
X_1 = \text{cutting speed m/min}
\]

\[
X_2 = \text{feed rate mm/rev}
\]

\[
X_3 = \text{depth of cut mm}
\]

Statistical Analysis

The effects of cutting speed, feed rate, and depth of cut on temperature rise were experimentally investigated and calculated with a statistical analysis of variance (ANOVA) were performed. The ANOVAs (Table 4) shows that the parameter experimented have been significant effect and it is sufficient.

| Source            | Sum of Squares | df | Mean Square | F Value | P-value | Prob > F |
|-------------------|----------------|----|-------------|---------|---------|-----------|
| Model             | 346.37         | 9  | 38.49       | 4.62    | 0.0280  | significant |
| A-cutting speed   | 42.32          | 1  | 42.32       | 5.08    | 0.0588  |           |
| B-feed rate       | 61.61          | 1  | 61.61       | 7.40    | 0.0298  |           |
| C-depth of cut    | 0.13           | 1  | 0.13        | 0.015   | 0.9059  |           |
| AB                | 14.44          | 1  | 14.44       | 1.73    | 0.2293  |           |
| AC                | 9.61           | 1  | 9.61        | 1.15    | 0.3183  |           |
| BC                | 0.040          | 1  | 0.040       | 4.804E-003 | 0.9467  |           |
| A2                | 214.95         | 1  | 214.95      | 25.82   | 0.0014  |           |
| B2                | 1.30           | 1  | 1.30        | 0.16    | 0.7048  |           |
| C2                | 1.03           | 1  | 1.03        | 0.12    | 0.7352  |           |
| Residual          | 58.28          | 7  | 8.33        |         |         |           |
| Lack of Fit       | 53.43          | 3  | 17.81       | 14.68   | 0.0126  |           |
| Pure Error        | 4.85           | 4  | 1.21        |         |         |           |
| Cor Total         | 404.65         | 16 |            |         |         |           |
RESULTS AND DISCUSSION

Interaction Effect of Cutting Speed on Temperature Rise

From the (Figure 6) it is noticed that feed rate has the direct influence on temperature rise at lower cutting speed. This may be due to the fact that as the feed rate increases, the speed of cutting tool movement relative to the work piece also increases resulting in higher temperature rise. An increasing cutting speed results in increasing the cutting temperature rise to a point where atomic diffusion between the tool and work piece material takes place, which in turn propagates the tool wear. The temperature rise slightly increases with decreasing cutting speed from 96 to 90 m/min; this may be due to the adhesion of work material on the tool, which results in more friction. From the change of levels in the figure 2 observed that, which shows that the cutting speed resulted in a decrease in temperature rise from 96 to 104 m/min, increase in temperature from 114 to 120 m/min, and optimal in between 104 and 106 m/min.

Interaction Effect of Feed Rate on Temperature Rise

From (Figure 7) and (Figure 8) shows that the interaction effects of feed rate and depth of cut on temperature rise are less significant. It has been concluded from the interaction effect that increasing feed rate and depth of cut increases the temperature rise. This may be due to the fact that, when feed rate and depth of cut increases, the contact area between the tool and the work piece also increases resulting in the formation of more chips and thus increases the temperature rise. For reducing the temperature rise, it can be noticed from the results that the feed rate and depth of cut should be minimum in the range of 0.18 to 0.23 mm/rev and 0.20 to 0.30 mm.

Prediction Vs Actual

Figure 9 shows the significant error in normal line between the prediction and actual responses. The graph is obtained from the experimental and prediction responses using RSM.

Validation of the Model

The (Table 5) shows that a regression model developed using Box–Behnken by RSM of design of experiment were verified using confirmatory test. It shows the comparison of predicted vs experimental value of temperature rise for the cutting parameters. The percentage of error is found to be within ±3% which shows the validity of the model.
Zeelan Basha et al.,

Figure 9: Prediction Vs Experimental

Table 5: Validation of observed Vs predicted

| Trail | Cutting Parameters | Responses (temperature rise) | Error % |
|-------|--------------------|------------------------------|---------|
|       | X1:     | X2:     | X3:     | Observed | Predicted |         |
| 1     | 96      | 0.20    | 0.20    | 25.2     | 24.57     | 2.5     |
| 2     | 114     | 0.24    | 0.25    | 26.1     | 25.8      | 1.14    |
| 3     | 96      | 0.18    | 0.30    | 23.1     | 23.24     | -0.6    |

CONCLUSIONS

Based on the experimental investigation, application of RSM and Box–Behnken for modeling and optimization of temperature rise of turning process has been discussed. Mathematical model equations were derived for temperature rises by using mathematical software package DESIGN EXPERT 8.0. The confirmatory test shows the predicted values from the model equations were found to be good agreement with observed values and the percentage of error is found to be within ±3%. Considering the factors such as cutting speed, feed rate and depth of cut using design of experiments concept the following conclusions are drawn: The cutting speed, feed rate and depth of cut were the most important parameters to be considered for reducing the temperature rise of the turning process. For reducing the temperature rise, cutting speed should be between 96 and 114 m/min, Feed rate should be less than 0.23 mm/rev, depth of cut should be between 0.20 and 0.30 mm.

ACKNOWLEDGEMENTS

The authors are grateful to the Management, Department of Mechanical Engineering and Department of Production Engineering, Karunya University, Coimbatore, India.

REFERENCES

Amit Sharma., Vinod Yadava., (2012). Modelling and optimization of cut quality during pulsed Nd:YAG laser cutting of thin Al-alloy sheet for straight profile. Optics and Laser Technology 44: 159-168.

Angus. J., (2011). Robust cutting parameters optimization for production time via computer experiment. Applied Mathematical Modelling 35: 1354-1362.

Baskar, N., Asokan, P., Saravanan, R., Prabhaharan, G. (2005). Optimization of Machining Parameters for milling operations using non-conventional methods. International Journal of Advanced Manufacturing Technology 25: 1078-1088.