Estimation of Short Circuit Duration for the Assessment of Dynamic Effects in Distribution Substations with Flexible Conductors

Piotr Piechocki 1, Ryszard Frackowiak 2, Grzegorz Dombek 2,* and Irena Chmielewska 3

1 PSE S.A, Marcelinska 71, 60-354 Poznan, Poland; piotr.piechocki@pse.pl
2 Institute of Electric Power Engineering, Poznan University of Technology, Piotrowo 3A, 60-965 Poznan, Poland; ryszard.frackowiak@put.poznan.pl
3 Power Engineering Department, Higher School of Managerial Staff, Zagorowska 3a, 62-500 Konin, Poland; rektorat@wskmkonin.edu.pl
* Correspondence: grzegorz.dombek@put.poznan.pl; Tel.: +48-61-665-2192

Received: 13 November 2019; Accepted: 18 February 2020; Published: 21 February 2020

Abstract: The paper focuses on finding short circuit duration for computing the dynamic effects in Extra High Voltage (EHV) distribution substations with flexible conductors with the use of probabilistic method. To find fault duration for selected substation points, a risk criterion was involved, namely the expected annual frequency of exceeding the calculated values of dynamic forces. A dedicated simulation model based on the Monte Carlo method was used to analyze the dynamic effects of short circuit current flow in the substation during faults within it and in its vicinity. The short circuit duration model is the key part of the simulation model. Due to the discussion of how the selected factors affect the estimated short circuit duration, indications helpful to find the values of the latter were formulated and some examples for the 220 kV distribution substation were given.

Keywords: EHV distribution substation; dynamic effects; short circuit duration; Monte Carlo simulation

1. Introduction

Analysis of the dynamic effects in power distribution substations is an important issue in designing new facilities and modernizing the existing ones. Research centers around the world have already been interested in studying the phenomenon of electrodynamic interactions for short overhead spans in switching stations. Calculation of the dynamic effects in power distribution substations with flexible conductors has been discussed by many authors [1–7]. In the nineties, the issue was also addressed by CIGRÉ. The effect of the team’s work as part of CIGRÉ included the brochure [8] and standard [9]. In CIGRÉ Brochure No. 105, [8] provided information about mechanical effects of short circuit currents in High Voltage (HV) and Extra High Voltage (EHV) open air conventional substations. The standard [9] provides procedures for calculating the effects of short circuit currents in alternating current networks with rated voltages up to and including 420 kV. The effects of electromagnetic impact on rigid and flexible conductors, as well as thermal effects in bare conductors are included. Although these methods are easy to implement, both of them have some limitations.

In [4], Awad et al. presented methods to design a strain bus for new 230 and 500 kV power distribution substations and to uprate the existing substations. In addition, the authors discussed mechanical, electrical, and arc-thermal effects of short circuit currents on strain-bus systems. In turn, in [5] Hermann et al. presented studies of tensile forces, stresses, and conductor displacements for short circuit currents in arrangements representing strained conductors of typical 123 and 420 kV power distribution substations. Based on the obtained results, they developed a calculation method taking into account short circuit duration, which leads to reduced forces and displacements in the case...
of brief current flows. In reference [6], Stein et al. conducted extensive short circuit tests on substation bus bars of stranded conductors with and without droppers. These tests included 100 and 400 kV systems. When calculating the dynamic effects in substations with flexible conductors the authors found that the Finite-Element Method (FEM) showed a remarkable comparative accuracy. In [1], the authors measured the dynamic effects by conducting short circuit tests on a typical 138 kV disconnect switch stand. The authors performed dynamic finite element analyses on the tested structure, which were validated with the test data. The authors’ results confirmed the reduced dynamic response of the structure. In 2010, the Institute of Electrical and Electronic Engineers published a guide [7] providing information on different bus arrangements used in power distribution substations and specifying the advantages and disadvantages of each of them. The guide also gives information on calculation tools for each bus type. Based on these calculations, specification of forces acting on the bus structure is also possible. The IEEE 605 guide assumed straight long parallel conductors in two-dimensional (2D) force calculations while ignoring any bends and 3D placement of conductors. Referring to [7] and [8] Bosworth et al. in [2] proposed two extensions to IEEE 605 and CIGRE 105 for calculating short circuit current reaction forces. The authors presented a closed-form equation defining the simplified 2D short circuit force time history during a fault and a computationally inexpensive numerical 3D force calculation technique. In reference [3] Stein et al. presented the results of studies showing a simplified approach to short circuit strength assessment. The authors presented the results of short circuit tests and compared them with the FEM calculations for four representative 100 kV conductor arrangements. Based on the obtained results, very good compatibility of calculations and test results was stated, which indicates the usefulness of FEM technology for this type of analysis.

Correct and effective operation of an electric power system necessitates constant conduct of various observations and considerations, for both regular and fault conditions [10,11]. Adjusting device parameters to short circuit conditions is one of the most important tasks at the stage of designing and modernizing power networks. The constant development of global economies, involving the growing demand for power, forces the development of power infrastructure. In addition, a constantly growing number of generating units and transformers significantly affects the maximum value of short circuit currents in the power system. This forces the necessity to assess the adaptation of existing substation components to new short circuit powers. However, the data and assumptions, as well as models adopted by power system operators to make the analyses create various types of uncertainty. It is not uncommon that decisions based on defined values do not always allow a comprehensive risk assessment of making too many errors. It should be borne in mind that assessment of the adopted assumptions, models, and data from the point of view of reliability and costs of proposed solutions is important [12,13]. For example, the increase in short circuit power in an electric power system entails the need to adapt the power distribution substation to new short circuit conditions. Therefore, calculations of dynamic effects in power distribution substations are an important element of short circuit analyses [1–3].

Performing an analysis of dynamic effects in power distribution substations involves the knowledge of quantities characterizing the short circuit current. Assuming the appropriate value of short circuit duration (short circuit current flow time \( T_k \)) in calculations is particularly important [9,14]. The maximum values of forces related to conductor movement caused by interfacial interaction in HV and EHV switchgears usually occur during short circuits lasting longer than 300 ms (this time depends on: The value of short circuit current, span length and phase conductor spacing, type of force). Usually, short circuits occurring in high voltage switchgears and in their vicinity are switched off in about 100 ms. Adopting such a time value significantly reduces the determined force values in relation to the maximum possible value. Higher values of short circuit duration are also possible in the event of, for example, failure of protections or switches. However, the probability of such a short circuit is relatively low. In the case of switchgear modernization associated with matching it with higher levels of short circuit currents, appropriate determination of the short circuit duration value has an economic dimension. For example, it affects decisions regarding the supporting structures: Whether to leave the existing ones for
further operation, strengthen them, or replace with new ones. Adoption of excessive values of short circuit duration may be associated with oversizing switchgear components and it may even enforce an uneconomical decision to rebuild the entire switchgear. On the other hand, adoption of an excessively small value of short circuit duration may lead to losses related to damage to or even destruction of devices.

Few papers dealing with statistical studies on short circuit duration in the HV grid provide a view on the type of distribution of this value [1,9]. However, due to the relatively low number of available samples, the credibility of the obtained distributions of this random variable is low and does not permit the assessment of short circuit duration value $T_k$ based on the probability of its occurrence. Moreover, such $T_k$ values and their probability distribution depend on different factors including types of implemented circuit-breakers and protections, their settings, and operating reliability. To some extent, the choice of the short circuit duration value for finding the risk caused by fault disturbances can be supported by simulation examinations. The issue of using probabilistic analyses for the dimensioning of power distribution substation elements was the focus of interest of many authors [15–18]. Although the problem is not new, it is still valid. For economic reasons, High Voltage (HV) and Extra High Voltage (EHV) substations operating in Poland will be overhead substations for several or several dozen years going forward. This means that a significant proportion of them must be adapted to new, higher levels of short circuit current. As the available literature shows, there are no studies on the criteria for the selection of short circuit duration values in analyzing dynamic forces in power distribution substations. The issue of short circuit duration impact on the values of dynamic pulls in substations discussed in the literature is a focus of the deterministic approach. There are basically no works devoted to other criteria for determining the value of short circuit duration when calculating dynamic effects in high-voltage switchgears with flexible conductors. Therefore, the goal adopted by the authors of this paper was to consider the possibility of using a probabilistic approach to develop principles helpful in determining the value of time $T_k$ when analyzing dynamic effects in substations. The use of the risk criterion, i.e., the allowable annual frequency of exceedances of the calculated force, was proposed to determine the value of short circuit duration for dynamic force calculations. This value can be determined, for example, against an economic account [19]. Monte Carlo simulation was used to solve the task, using the developed simulation model of switchgear and its surroundings. It includes models of the place and type of short circuit for individual power network elements, as well as the duration model of short circuit associated with the work mapping for Power System Protection and switchgear in the EHV network (location, configuration, and reliability of these devices and protection zones). In a simulation study, current flowing through a selected bay is calculated for a specific location and type of short circuit and current flow time is determined. Taking into account the random nature of these two short circuit quantities, the annual frequency of exceeding individual values of the calculated dynamic force is determined. During the simulation, the values of dynamic forces were calculated using the method described in DIN EN 60865-1. The subject matter of the study was not the very method contained in the aforementioned standard. The designer performs calculations of the dynamic force value for the maximum current value during a short circuit on bus-bars and for a specified value of short circuit duration. When assuming time values which are smaller than the value at which the maximum force value appears, the designer must take into account a certain risk of exceeding the determined force value caused by the possibility of more adverse conditions (maximum current and short circuit duration greater than originally assumed). The study carried out tests of this type of risk as a function of short circuit duration assumed during the calculation of dynamic forces. It was proposed that in choosing the value of short circuit duration, one should be guided by the value of the risk of exceedances considered as acceptable (e.g., determined on the basis of economic impact calculations). For the acceptable risk values adopted from the available literature, examples are given of short circuit duration values which should be used in calculations of forces for the selected protection system configurations. Currently, no described method is available for determining the duration of a short circuit taking into account the economic criterion. Therefore, the proposed approach can support the deterministic analysis of dynamic forces in power distribution
substations. The authors’ intention was not to replace the deterministic method with the probabilistic method, but to apply a probabilistic approach to determining the value of short circuit duration.

The paper was organized in the following way: Analysis of short circuit quantities in highest voltage networks from the point of view of dynamic effects in a substation with flexible bus-bars was carried out using the developed model based on the Monte Carlo simulation method presented in Section 2. The principle of determining the duration of short circuit and the structure of the developed model are also described in Section 2. In turn, Section 3 presents the developed time distributions of protection operation occurring in the examined network. Section 4 presents short circuit current distributions for the two points of the 220 kV substation under test. Section 5 contains the results of short circuit duration and dynamic force analysis for the four selected PSPA configurations. Section 6 presents the authors’ method of determining the value of short circuit duration for the purposes of calculating dynamic forces. A method based on the risk criterion (expected annual frequency of exceedances of the determined force) was proposed. Based on the presented method, the impact of selected factors on the estimated short circuit duration was also examined. The obtained results allowed the authors to formulate guidelines helpful in determining the value of fault duration during the analysis of dynamic short circuit effects in the substation. Section 7 contains a summary and the final conclusions. Example values of short circuit duration are given for a risk of $10^{-3}$/1/a depending on the PSPA configuration.

2. Scheme of Finding the Dynamic Forces Distribution by the Monte Carlo Simulation Method

The method described in standard IEC 60865-1 [9] was used to determine the value of dynamic forces acting from flexible conductors on the supporting structures of the substations.

Figure 1a shows an example of phase conductor movement due to short circuit current. The phase conductor suspension points are at the axis intersection at point 4. In turn, Figure 1b presents the time of occurrence of the characteristic dynamic forces acting at the phase conductor suspension points. At the beginning of the short circuit current flow, as a result of the conductors approaching in the harness, force $F_{pi}$ occurs (point 1). Due to interaction between conductors of adjacent phases, the conductors move and the maximum force caused by this interaction (force $F_i$) is observed at point 2. After switching off the short circuit current, the conductor continues its upward movement and then falls. At this moment, a force is caused by the falling conductor $F_f$ (point 3).

![Movement of suspended wires between support structures](image)

**Figure 1.** Movement of suspended wires between support structures: (a) Phase conductor motion due to phase current flow; (b) time of occurrence of characteristic dynamic forces acting at conductor suspension points; 1—sticking of conductors in the harness, 2—interphase interaction, 3—conductors’ droop, 4—suspension of conductors (Adapted from [20]).

The time of occurrence of force $F_{pi}$ has very small values, lower than the actual values of short circuit duration in the electric power system [19]. However, the values of forces $F_i$ and $F_f$ depend on the flow time and the value of short circuit current (periodic component) [14].
Calculations of the values and probability distributions of dynamic forces occurring in a given span of the substation are made using the Monte Carlo method (Figure 2). During simulation calculations, short circuits on the substation bus-bars, in its bays and surroundings are taken into account. The values of dynamic forces in the span are specified on the basis of the determined value of current in the conductors and the duration of short circuit for a random place and type of short circuit. Random number generators were used for the draw. After an assumed number of simulations have been done, the annual frequency of occurrence of these forces is calculated [14]. On that basis, also the expected annual frequency of exceeding individual force values is calculated.

A computer program for dynamic force analysis using a simulation method was created in Delphi. Its basic elements are simulation models of short circuit current [19,21] and short circuit duration.

The PLANS (Plans Ltd., Warsaw, Poland) program was used to calculate the short circuit current in the power grid [22]. The program allows modeling various types of short circuit. PLANS makes it possible to calculate the value of short circuit current in a selected node, as well as its spread.

The value of short circuit duration (short circuit current flow) for a specific place and type of short circuit is specified for randomly determined values of protection times and switches participating in interference elimination. It can be considered that short circuit current and short circuit duration are, to some extent, dependent variables. Their values depend on the short circuit location and type. Determining the fault duration value in subsequent simulated faults takes place in the stages shown in Figure 3.

Types, arrangement, operation, and range of zones used in the simulation model of PSPA elements protecting substation bus bars, devices in its substation bays, lines, and transformers are presented.
in [23]. The model takes into account the requirements contained in the Instruction of Transmission System Operation and Maintenance [24]. The general scheme for calculating short circuit duration is shown in Figure 4. Detailed algorithms for determining the value of short circuit duration during short circuits occurring on elements of the power network are presented in [23].

![Figure 3](image-url). Stages of determining the value of short circuit duration using the Monte Carlo simulation method.

![Figure 4](image-url). General algorithm for simulation-based finding of short circuit duration (Adapted with permission from [14], Piechocki, P. Frackowiak, R., Eksploatacja i Niezawodność—Maintenance and Reliability, Polish Maintenance Society, 2017).
3. Operation Time of Protections

Distributions of operation times for chosen protections and circuit breakers found on the basis of analysis of true fault recordings are presented in [25]. To find the distributions of the protection’s operation times for simulation purposes, the results of periodic inspections carried out in the years 2003–2009 were used. Protections in the distribution bays of the 400, 220, and 110 kV substations belonging to Polskie Sieci Elektroenergetyczne S.A., Poland, and located in the area managed by Polskie Sieci Elektroenergetyczne S.A. Poznan, Poland, were investigated.

Investigations of the protections are carried out in the distribution bays at the place of their installation. The protections are separated from the protected elements and connected to the dedicated circuit. Protection operation time is measured with a timer from the excitation time until the pulse is sent to the circuit-breaker.

For protections located in the section of interest of the 220 kV substation, the histograms were found and the adequate theoretical distribution was chosen (positive contingency test results). The Statistica (Tibco Software Inc., Palo Alto, CA, USA) software was implemented. For investigated protections, the probability density of the normal and log-normal distributions was found, and the latter is more suitable for the variable’s description.

For illustration, the distributions of operation time of the LZ-32 distance protection (an old-type electromechanical protections still in operation) is shown in Figures 5 and 6; the operation duration probability distributions of the protection found for 187 measurements and instantaneous setting is shown in Figure 5 whilst those found for 65 results and 500 ms setting are shown in Figure 6.

![Figure 5. Histogram and the normal and log-normal operating time distributions for LZ-32 protection with instantaneous setting.](image1)

![Figure 6. Histogram and the normal and log-normal operating time distributions for LZ-32 protection with 500 ms setting.](image2)
Similar distributions were found for the 7SA protection which is the increasingly applied new-generation digital distance protection superseding the older ones. It is characterized by a slightly lower operating time dispersion. For instantaneous setting (Figure 7), the 7SA protection’s operating time values are clustered around 25 ms; thus, its operating time is much shorter than that of LZ-32. For 500 ms setting, the measured time values fall between 460 and 520 ms (Figure 8). The 7SA protection’s operating reliability is much higher than that of the older electromechanical ones.

4. Distribution Substation’s Model and Short Circuit Current Distribution

For the purposes of dynamic effects analysis, a 220 kV two-system substation with 16 bay sections was chosen. Six overhead 220 kV lines, two transformers, and one transversal coupler bay used for connecting bus bars and covering two bay sections, are connected to the ten bays in use.

In Figure 9, the 220 kV substation is shown, and the points of division of the bus system into the wire sections are indicated. The width of a bay section is 14 m. A single-wire section of the bus system covers four bay sections and is 56 m long. The entire sixteen-bay substation comprises four guy-wire sections forming a single bus bar system. Within the section, a bundle of two AFL 8-525 conductors per phase was applied.

Moreover, two points A and B are indicated on the bus bar system at which the fault conditions and dynamical strengths were analyzed.
In the first case (system II, point A), the line (bay No. 16) with a very low contribution to the bus fault current is located on one side of the inspection point. The fault in this substation’s area results in the flow of fault current nearly reaching the maximum value.

![Figure 9. Layout of substation with bus bar system guy-wire sections](image)

In the second case, two bays with the transformer (bay No. 14) and the line (bay No. 15) connected are on one side of the investigation point, whilst the other branches considered in the scheme are on the other side. To assess the substation’s capability to deal with higher fault currents, an algorithm allowing for the appropriate rescaling of the short circuit current flow was developed. The scaling is carried out with respect to the maximum value of fault current on the substation bus (for instance, 40 or 50 kA).

PSPA systems included in the simulation tests are presented in [14].

Referring to statistical data, the failure rate of protections, Circuit Breakers (CB) and Breaker Failure Protection (BFP) was assumed as 0.03, 0.03, and 0.01, respectively. Parameters describing the intensity of faults on the individual elements of the substation, as well as on those of the connected lines and transformers were also assumed [19].

In Figure 10, the results of analysis of the expected annual frequency of exceeding (risk) individual values of the short circuit current at the lookout points A and B during the faults in the considered system section are reported; the unit is 1/a. The maximum assumed value of the short circuit current on the bus bar was 40 kA.

![Figure 10. Expected annual frequency of exceeding actual values of short circuit current at inspection points A and B on substation bus bar.](image)
The maximum currents expected at points A and B of the substation during three-phase short circuits are close to 40 and 27 kA, respectively.

5. Results of the Short Circuit Duration and Dynamic Force Analyses

The annual frequency of exceeding actual values of short circuit duration was discussed for four different PSPA configurations in the 220 kV substation. The main distance protections are assumed to be the new 7SA release. The PSPA configurations in substations are described in detail in Table 1. In the simulations, system sections in which the short circuit current values (important in dynamic effect analysis) flow through the lookout points are considered.

| Equipment                                      | Configuration No. 1 | Configuration No. 2 | Configuration No. 3 | Configuration No. 4 |
|------------------------------------------------|----------------------|----------------------|----------------------|----------------------|
| Automatic reclosing equipment and               | yes                  | no                   | yes                  | yes                  |
| duplicated operation of protections            |                      |                      |                      |                      |
| Circuit-breaker back-up system                 | yes                  | yes                  | yes                  | yes                  |
| Disconnecting protection in bus coupler bay    | yes                  | yes                  | no                   | yes                  |
| Bus bar protection                             | yes                  | yes                  | yes                  | no                   |

The plots presenting the found frequency of exceeding the short circuit duration at lookout point A for the considered four different PSPA configurations are shown in Figure 11. In calculations, faults on the second bus bar system section in line bay No. 16 and on the line connected to the bay (on the right of the lookout point) were taken into account.

Figure 11. Expected annual frequency of exceeding actual values of short circuit duration at inspection point A on substation bus bar.

If only one 220 kV line is on the right of the lookout point, the Automatic Reclosing (AR) equipment, as well as duplication of protections on the line affect mostly the investigated frequency. When the exceeding frequency is $10^{-1}$ 1/a or $10^{-2}$ 1/a, the lack of AR equipment significantly overstates the short circuit duration values that are found.

The curves in Figure 11 for configuration No. 1, No. 3, and No. 4 are comparable. When exceeding frequency is $10^{-3}$ 1/a or lower, there is no noticeable impact of the PSPA configuration on the results obtained.

Short circuit duration values for both selected levels of frequency of exceeding and the considered PSPA configurations at the lookout point A are reported in Table 2.
Table 2. Short circuit duration values $T_k$ found at lookout point A for selected risk levels $R_a$ and four PSPA configurations.

| Risk levels $R_a$ (1/a) | Conf. No. 1 $T_k$ (ms) | Conf. No. 2 $T_k$ (ms) | Conf. No. 3 $T_k$ (ms) | Conf. No. 4 $T_k$ (ms) |
|-------------------------|------------------------|------------------------|------------------------|------------------------|
| $10^{-1}$               | 109.3                  | 535.4                  | 109.3                  | 116.0                  |
| $10^{-2}$               | 509.3                  | 608.1                  | 509.6                  | 511.3                  |
| $10^{-3}$               | 1040.4                 | 1040.8                 | 1040.5                 | 1040.4                 |
| $10^{-4}$               | 1052.2                 | 1052.9                 | 1052.0                 | 1052.6                 |

At lookout point B, the influence of PSPA configuration on the short circuit duration distribution is slightly different [5].

As an example, computations for a defined 56 m long 220 kV span were carried out. In Figure 12, the curves presenting the annual frequency of exceeding the value of force $F_t$ for four different PSPA configurations are shown. Table 3 presents the found values of the considered force $F_t$ for three risk levels.

Figure 12. Annual frequency of exceeding actual values of force $F_t$ at lookout point A for different PSPA configurations.

Table 3. Values of force $F_t$ for chosen risk levels and four different PSPA configurations at lookout point A.

| Risk Levels $R_a$ (1/a) | Configuration No. 1 $F_t$ (kN) | Configuration No. 2 $F_t$ (kN) | Configuration No. 3 $F_t$ (kN) | Configuration No. 4 $F_t$ (kN) |
|-------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| $10^{-2}$               | 24.1                            | 24.7                            | 24.1                            | 24.5                            |
| $10^{-3}$               | 27.0                            | 33.4                            | 27.0                            | 45.9                            |
| $10^{-4}$               | 45.9                            | 45.9                            | 45.9                            | 45.9                            |

The highest impact of the PSPA configuration is observed when the risk of exceedance is $10^{-3}$ 1/a. The value of $F_t$ found for configurations No. 1 and No. 3 is 27.0 kN. The highest value equal to the maximum one (i.e., 45.9 kN) occurs when there is no bus protection. When AR is missing, $F_t$ equals 33.4 kN.

The PSPA configuration affects the expected annual frequency of exceeding force $F_t$ in the similar way as it is for $F_f$. However, the probability that force $F_f$ occurs is much lower: $F_t$ occurs only for sufficiently high values of both the current and the short circuit duration.
6. Finding the Short Circuit Duration Value for Dynamic Force Assessment Purposes

6.1. Probabilistic Method

Using the expected annual frequency of exceedances of individual dynamic force values and the dependence of this force value on the duration of short circuit adopted for its calculation $T_{ko}$, it is possible to determine the relationship between this time and the risk of exceeding the calculated force. To illustrate, the method of determining the time value $T_{ko}$ for calculating force $F_t$ is assumed taking into account a risk of exceedance at $10^{-3}$ 1/a. The current value during a three-phase short circuit on the substation bus bars is 40 kA. For the first PSPA configuration, the assumed risk value corresponds to force $F_t$ equal to 27 kN (Table 3). This force value is obtained assuming a short circuit duration of 98.4 ms (Figure 13). In this way, the relationship between the risk of exceeding the calculated value of force $F_t$ and the value of time $T_{ko}$ can be determined (Figure 14). Based on this relationship, it is possible to estimate the value of time $T_{ko}$ which should be taken when calculating the dynamic force $F_t$ at different risk levels.

Similarly, values of $T_{ko}$ can be found to determine force $F_f$.

![Figure 13. Force $F_t$ versus short circuit duration for $I_k'' = 40$ kA.](image)

![Figure 14. Risk of exceeding force $F_t$ versus $T_{ko}$ (assumed for $F_t$ calculations) under short circuit conditions at point A for configuration No. 1.](image)

6.2. Influence of Power System Protection Automatics Configuration on Estimated Short Circuit Duration

Influence of PSPA configuration on estimated short circuit duration values has been presented under short circuit conditions at lookout point A in which much higher values of the short circuit current occur. A list of force $F_t$ values and the corresponding time $T_{ko}$ values for four considered PSPA configurations at selected risk levels are reported in Table 4.
Table 4. Values of force $F_t$ and time $T_{ko}$ for defined risk levels and different PSPA configurations under short circuit conditions at lookout point A.

| Risk Levels $R_a$ (1/a) | Conf. No. 1 | Conf. No. 2 | Conf. No. 3 | Conf. No. 4 |
|-------------------------|-------------|-------------|-------------|-------------|
|                         | $F_t$ (kN)  | $T_{ko}$ (ms) | $F_t$ (kN)  | $T_{ko}$ (ms) | $F_t$ (kN)  | $T_{ko}$ (ms) | $F_t$ (kN)  | $T_{ko}$ (ms) |
| $10^{-2}$               | 24.1        | 62.2        | 24.7        | 70.9        | 24.1        | 62.5        | 24.5        | 67.7        |
| $10^{-3}$               | 27.0        | 98.4        | 33.4        | 160.5       | 27.0        | 98.5        | 45.9        | 317.1       |
| $10^{-4}$               | 45.9        | 317.1       | 45.9        | 317.1       | 45.9        | 317.1       | 45.9        | 317.1       |

Found values of $T_{ko}$ at risk value equal to $10^{-3}$ 1/a are 100 ms (configuration No. 1 and No. 3). The lack of bus bar protection results in an important increase (approx. three times) in the time value found. For the considered risk level, the influence of the lack of both, AR and protections duplication, is evident ($T_{ko}$ of 160 ms).

Results of similar analysis carried out under short circuit conditions at lookout point B and reported in Table 5: $T_{ko}$ values seem to be much lower due to lower values of the short circuit current (Figure 11). In configurations 1, 2, and 3, at risk level of $10^{-2}$ 1/a, force $F_t$ does not occur for such current values as lookout point B. A list of force $F_t$ values and corresponding time values for four considered PSPA configurations and under short circuit conditions at lookout point A is shown in Table 6.

The impact of PSPA configuration on the results of force $F_t$ and time $T_{ko}$ analyses for short circuit conditions in point A is shown in Table 6. The risk of force $F_t$ occurrence for PSPA configuration No. 1 and No. 3 is less than $10^{-3}$ 1/a. For other configurations, time $T_{ko}$ values are 270 ms (for configuration No. 3) and 425 ms (for configuration No. 4).

Table 5. Values of force $F_t$ and time $T_{ko}$ for defined risk levels and different PSPA configurations under short circuit conditions at lookout point B.

| Risk Levels $R_a$ (1/a) | Conf. No. 1 | Conf. No. 2 | Conf. No. 3 | Conf. No. 4 |
|-------------------------|-------------|-------------|-------------|-------------|
|                         | $F_t$ (kN)  | $T_{ko}$ (ms) | $F_t$ (kN)  | $T_{ko}$ (ms) | $F_t$ (kN)  | $T_{ko}$ (ms) | $F_t$ (kN)  | $T_{ko}$ (ms) |
| $10^{-2}$               | -           | -           | -           | -           | 22.7        | 34.1         |
| $10^{-3}$               | 22.5        | 28.0        | 22.6        | 31.1        | 22.5        | 28.1         | 28.0        | 109.3        |
| $10^{-4}$               | 22.7        | 36.2        | 22.7        | 35.6        | 22.8        | 36.4         | 28.0        | 109.3        |

Table 6. Force $F_t$ and time $T_{ko}$ values for defined risk levels and different PSPA configurations under short circuit conditions at point A.

| Risk Levels $R_a$ (1/a) | Conf. No. 1 | Conf. No. 2 | Conf. No. 3 | Conf. No. 4 |
|-------------------------|-------------|-------------|-------------|-------------|
|                         | $F_t$ (kN)  | $T_{ko}$ (ms) | $F_t$ (kN)  | $T_{ko}$ (ms) | $F_t$ (kN)  | $T_{ko}$ (ms) | $F_t$ (kN)  | $T_{ko}$ (ms) |
| $10^{-3}$               | -           | -           | 53.0        | 269.9       | -           | -           | 62.8        | 424.6        |
| $10^{-4}$               | 61.0        | 391.2       | 64.0        | 451.2       | 65.2        | 481.9       | 65.7        | 495.9        |
| $10^{-5}$               | 65.2        | 482.3       | 66.3        | 516.2       | 65.9        | 500.6       | 66.0        | 505.0        |

6.3. Influence of Maximum Value of Short Circuit Current

In Figure 15, the annual frequency of exceeding force $F_t$ value for three current values during a three-phase fault in the bus is presented. In Figure 16, the risk of exceeding the found force versus time $T_{ko}$ assumed for its calculation is plotted at the same three current values. Calculations were carried out for short circuit conditions at point A with PSPA configuration No. 1.

For risk values of $10^{-2}$ 1/a and $10^{-3}$ 1/a, the short circuit current value strongly affects the maximum value of force $F_t$, and does not affect the found value of $T_{ko}$. However, for lower risk value ($10^{-4}$ 1/a), the found values of $T_{ko}$ differ significantly and equal 280 and 340 ms for currents of 50 and 32.5 kA, respectively.
For a full configuration of protections (configuration No. 1), the occurrence frequency of force $F_f$ is below $10^{-3}$ 1/a (Table 6). To keep the frequency of exceeding $F_f$ at $10^{-4}$ 1/a, time $T_{ko}$ taken for its calculation should be close to 380 ms for the three considered short circuit currents (32.5, 40, and 50 kA) in the bus.

6.4. Influence of Failure Rate of Protections and Circuit-Breakers

Results of simulation studies carried out for an assumed failure rate of protections and circuit-breakers equal to $N_{fZ} = N_{bwo} = N_{b} = 0.03$ were compared to those for failure rate two times lower and two times higher. A list of force $F_t$ values and corresponding $T_{ko}$ values for three different failure rate values is shown in Table 7.

Table 7. Force $F_t$ values and corresponding $T_{ko}$ values for defined risk levels and different values of protection and circuit-breaker failure rates; fault conditions at point A.

| Risk Levels $R_a$ (1/a) | $0.5 \cdot N_b$ | $N_b$ | $2 \cdot N_b$ |
|------------------------|----------------|-------|---------------|
| $F_t$ (kN) | $T_{ko}$ (ms) | $F_t$ (kN) | $T_{ko}$ (ms) | $F_t$ (kN) | $T_{ko}$ (ms) |
| $10^{-2}$ | 24.1 | 61.6 | 24.1 | 62.2 | 24.2 | 63.9 |
| $10^{-3}$ | 26.7 | 95.2 | 27.0 | 98.4 | 28.0 | 108.7 |
| $10^{-4}$ | 33.2 | 158.8 | 45.9 | 317.1 | 45.9 | 317.1 |
Thus, the influence of changes in protection and circuit-breaker failure rates within assumed limits on the found $T_{ko}$ values at the assumed risk equal to $10^{-2}$ 1/a is negligible. Influence is noticeable at risk equal to $10^{-3}$ 1/a, and evident at $10^{-4}$ 1/a.

6.5. Influence of Span Parameters

Calculations for four spans with parameters listed in Table 8 were carried out. In Figure 17, curves presenting the risk of exceeding force $F_t$ versus $T_{ko}$ values taken for calculation are shown for four considered spans.

| Span | Length $l$ (m) | Static Tension $F_{st}$ (kN/phase) | Additional Mass $m_{st}$ (kg) |
|------|----------------|-----------------------------------|-----------------------------|
| P1   | 56             | 20                                | 40                          |
| P2   | 56             | 10                                | 40                          |
| P3   | 56             | 20                                | 80                          |
| P4   | 28             | 20                                | 40                          |

Figure 17. Risk of exceeding force $F_t$ versus $T_{ko}$ values for short circuit current of 40 kA for four different spans.

For risk levels of $10^{-3}$ 1/a or higher, time $T_{ko}$ can be regarded as nearly constant in values (near 100 ms) and independent from the considered span parameters. However, at lower risk of exceeding the values, $T_{ko}$ values depend on span parameters, and are evidently lower for the shorter span P4.

To keep the frequency of exceeding the found force $F_f$ at $10^{-4}$ 1/a, time $T_{ko}$ for the full configuration of protections taken for its calculations should be 400 ms for spans P1, P2, P3. For the shorter span P4, force $F_f$ does not occur.

7. Conclusions

The paper presents the method of determining short circuit duration in HV and EHV networks for the purposes of dynamic forces analysis in electric distribution substations. Expected annual frequency of exceeding the determined force was proposed as a criterion for selecting $T_{ko}$ fault duration. Due to the performed investigations, the influence of PSPA equipment configuration, maximum short circuit current values on the buses, protection and circuit-breaker failure rates, and span parameters on the examined values of time $T_{ko}$ was established under defined fault conditions in the 220 kV substation.

In works approaching the problem of risk allowable in choosing devices for specific fault conditions, the values of $10^{-2}$ 1/a and $10^{-3}$ 1/a are indicated [19]. Our studies have shown that for risk values mentioned above, the short circuit duration value found to calculate force $F_t$ is mostly affected by...
PSPA configuration, whereas the influence of maximum short circuit current on the bus, failure rate of protections, and circuit-breakers, as well as span parameters is negligible.

When discussing dynamic forces $F_t$ for a 220 kV substation assuming the risk level at $10^{-3} \, \text{1/a}$, the following values of $T_{ko}$ are to be taken:

- 100 ms—full PSPA configuration in substation and no protection in the coupler bay,
- 160 ms—no AR working, no duplication of protections,
- 320 ms—no bus protection.

A lack of disconnecting protection in the bus connector bay does not affect the calculated short circuit duration value. Results of calculations carried out for risk levels lower than $10^{-3} \, \text{1/a}$ also show the influence of other factors on the estimated $T_{ko}$ values.

In EHV substations, force $F_f$ values are generally higher than those of force $F_t$. However, the probability that $F_f$ appears is low, i.e., less than $10^{-3} \, \text{1/a}$ at the full PSPA configuration in the substation. The $T_{ko}$ values found to calculate force $F_f$ under low risk conditions are higher than those used to calculate force $F_t$.

Due to the adopted assumptions, particularly the omission of short circuit current flow within a single span or constant temperature of conductors before the fault, the calculated expected risk value can be overestimated and true risk can be lower.

Further research will focus on analyses of higher short circuit currents and 400 kV substations. The studies will assess the usefulness of the relevant relationships and obtained results for the abovementioned conditions.

**Author Contributions:** Section 1 was prepared by R.F., G.D., and I.C. Section 2 was prepared by P.P., R.F., and G.D. Section 3 was prepared by P.P., R.F., and I.C. Section 4 was prepared by P.P. and R.F. Section 5 was prepared by all the authors. Section 6 was prepared by P.P. and R.F. Conclusions were prepared jointly by all the authors. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research was funded by the Ministry of Science and Higher Education, grant number 04/41/SBAD/4408.

**Conflicts of Interest:** The authors declare no conflict of interest.

**References**

1. Hodgson, I.; Sause, R.; Tahmasebi, E.; Birrell, D.; Villani, L.; Sagareli, S.; Hughes, M.; Bosworth, M.; Garber, L.; Zorn, A.V. Testing and analysis of dynamic response of a high-voltage substation structure to short-circuit current forces. *IEEE Trans. Power Deliv.* **2018**, *33*, 2097–2105. [CrossRef]
2. Bosworth, M.; Steurer, M.; Graber, L.; Hodgson, I.; Sause, R.; Tahmasebi, E.; Sagareli, S.; Villani, L.; Birrell, D.; Hughes, M.; et al. Modeling of reaction forces in high-voltage substation structures. *IEEE Trans. Power Deliv.* **2018**, *33*, 1510–1517. [CrossRef]
3. Stein, N.; Miri, A.M. High-voltage substations with rigid conductors—Full-scale short-circuit tests and comparative FEM studies on connections with so-called elbow bends. In Proceedings of the International Conference on Optimization of Electrical and Electronic Equipment, Brasov, Romania, 22–24 May 2008; pp. 1–6.
4. Awad, M.B.; Huestis, H.W. Influence of short-circuit currents on HV and EHV strain bus design. *IEEE Trans. Power Appar. Syst.* **1980**, *PAS-99*, 480–487. [CrossRef]
5. Hermann, B.; Stein, N.; Kiessling, G. Short-circuit effects in HV substations with strained conductors—Systematic full scale tests and a simple calculation method. *IEEE Trans. Power Deliv.* **1989**, *4*, 1021–1028. [CrossRef]
6. Stein, N.; Rieyer, W.; Miri, A.M. Tests and calculations of short-circuit forces and displacements in high-voltage substations with strained conductors and droppers. *Eur. Trans. Electr. Power* **2000**, *10*, 131–137. [CrossRef]
7. IEEE Power and Energy Society. *IEEE Guide for Bus Design in Air Insulated Substations*; The Institute of Electrical and Electronic Engineers (IEEE): New York, NY, USA, 2010.
8. Lilien, J.L.; Declerq, G.; El Adnani, M.; Ford, G.; Meyer, W.; Miri, A.M.; Nordin, R.; Polevoy, A.; Stein, N.; Tsanakas, D. The mechanical effects of short-circuit currents in open air substations (rigid and flexible bus-bar). In Cigré Technical Brochure 105; International Council on Large Electric System (CIGRE): Paris, France, 1996.
9. International Electrotechnical Commission (IEC). IEC 60865-1: Short-Circuit Currents—Calculation of Effects—Part 1: Definitions and Calculation Methods; International Electrotechnical Commission (IEC): Geneva, Switzerland, 1993.
10. Ciapessoni, E.; Cirio, D.; Massucco, S.; Morini, A.; Pitto, A.; Silvestro, F. Risk-based dynamic security assessment for power system operation and operational planning. Energies 2017, 10, 475. [CrossRef]
11. Xu, Y.; Dong, Z.Y.; Zhao, J.H.; Zhang, P.; Wong, K.P. A reliable intelligent system for real-time dynamic security assessment of power systems. IEEE Trans. Power Syst. 2012, 27, 1253–1263. [CrossRef]
12. Anders, C.J. Probability Concepts in Electrical Systems, 1st ed.; John Wiley and Sons: New York, NY, USA, 1990.
13. Li, J.; Feng, G.; Fan, K.; Chen, K.; Zhao, H.; Zhang, Z. Monitoring and controlling management system for transmission network operation and maintenance. In Proceedings of the International Conference on Electrical and Control Engineering, Yichang, China, 16–18 September 2011; pp. 249–253.
14. Piechocki, P.; Frackowiak, R. Assessment of dynamic effects in distribution substations with flexible conductors regarding short-circuit duration values. Eksploat. Niewiadom. Maint. Reliab. 2017, 19, 237–243. [CrossRef]
15. El-Kady, M.A. Probabilistic short-circuit analysis by Monte Carlo simulations. IEEE Trans. Power Appar. Syst. 1983, PAS-102, 1308–1316. [CrossRef]
16. Germani, M.D.; Vainberg, M.; Ford, G.L.; El-Kady, M.A.; Ganton, R. Probabilistic short-circuit uprating of station strain bus system—Overview, application and risk assessment. In Proceedings of the First International Symposium, Toronto, Canada, 11–13 July 1986; pp. 567–579.
17. Miroshnik, R. The probabilistic model of the dynamic of the cables under short-circuit current. Comput. Methods Appl. Mech. Eng. 2000, 187, 201–211. [CrossRef]
18. Mijailovic, V. Probabilistic method for planning of maintenance activities of substation components. Electr. Power Syst. Res. 2003, 64, 53–58. [CrossRef]
19. Frackowiak, R. Statistical and Probabilistic Approach to Electric Power Engineering Problems; Poznan University of Technology Publishing House: Poznan, Poland, 2013. (In Polish)
20. Landin, I. The mechanical effects of short-circuit currents in substations with flexible conductors. The stresses in the case of horizontally tensioned conductors. In Cigré Technical Brochure WG-02; International Council on Large Electric System (CIGRE): Paris, France, 1980.
21. Frackowiak, R.; Piechocki, P. Simulation-based estimation of short-circuit currents in 110, 220 and 400 kV substations. Prz. Elektrotech. 2010, 86, 237–240.
22. Plans. Available online: http://www.plans.com.pl (accessed on 20 September 2019).
23. Frackowiak, R.; Piechocki, P. Short-circuit duration values estimated by simulation for EHV distribution substations. Prz. Nauk. Metod. Eduk. Bezpieczenstwa 2016, 1, 1338–1352.
24. Transmission Network Code. Available online: http://www.pse.pl (accessed on 21 September 2019).
25. Frackowiak, R.; Paszyłk, R.; Zajac, J. Short-circuit duration was in 110 kV network. Autom. Elektroenerg. 2009, 1, 8–12.

© 2020 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).