RESEARCH ON PARAMETERS OF MMC FRACTURE CRITERION FOR ADVANCED HIGH STRENGTH DUAL-PHASE STEEL SHEETS

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1. Introduction

Advanced high-strength steels (AHSS), especially advanced high strength dual-phase (DP) steels, have the advantages of a low yield ratio and high collision performance. It is an important material to achieve a lightweight body, so it has been widely used in the automotive industry in recent years. However, various issues have arisen during manufacturing processes of AHSS. A typical problem occurs during stamping is a ductile fracture termed the shear fracture which has no obvious necking phenomenon and almost no thinning at the fracture (Gotoh et al., 1997; Sriram et al., 2003; Walp et al., 2006; Shih and Shi, 2008; Levy and Van Tyne, 2009; Shih et al., 2008; Shih, 2009). Due to the incompetence of the forming limit diagram (FLD) for industrial applications, it cannot predict this type of shear fracture for the dual-phase steel.

A lot of study on shear fracture of a dual-phase steel sheet have launched and appeared phenomenological models that are most suitable for industrial applications. The phenomenological ductile fracture model called the “Modified Mohr-Coulomb” (MMC) model is currently more widely used (Bai and Wierzbicki, 2010) to predict shear fracture damage of a dual-phase steel sheet. Wierzbicki et al. (2005) compared several widely used failure criteria through experiments on aluminum alloy materials, and summarized the change law of stress triaxiality for most of the failure criteria. The calculations of Xue (2007) and Xue and Wierzbicki (2009) show that the key factors determining the shear fracture are the third invariant of the stress state and softening due to damage. The MMC criterion proposed by Bai-Wierzbicki was based on aluminum alloy materials. Later research was extended to a DP steel. The study by Li (2010) et al. found that the MMC criterion can be applied to stress triaxiality between −2 and 1. Lou and Huh (2013) also adopted the MMC criterion to study the failure behavior of an advanced high-strength steel under different stress triaxial degrees. Lian et al. (2013, 2015) also used the MMC criterion...
considering the stress triaxiality and the lode angle to study the influence of stress triaxiality on the plastic behavior and fracture phenomena by designing different three-point bending experiments. Ji et al. (2020) conducted tensile tests on aluminum alloy samples with different stress triaxial degrees and Rod angles, different loading directions, different strain rates, and developed an improved MMC-based fracture model to describe the relevant fracture characteristics. They combined a test and simulation to verify the reliability of the criterion. Qian et al. (2020) proved the superiority of the MMC fracture criterion by designing five fracture tests of advanced high-strength steel TRIP780 from the shear stress state to tensile stress state and employing scanning electron microscopy of the fracture. Granum et al. (2021) presented a novel calibration procedure of the modified Mohr-Coulomb (MMC) fracture model by localization analysis and applied it for AA6016 aluminum alloy, and reduced the number of mechanical tests required to calibrate the MMC fracture model in a certain extent.

To our knowledge, the fracture criterion used for numerical simulation is relatively complete. However, the applicability of the MMC fracture criterion to DP980 and DP1180 needs further study due to the complexity of deformation of the sheet metal. On the other hand, validating three parameters of the MMC fracture criterion requires multiple sets of test data as a basis, and the solution process is cumbersome. Due to three parameters of the MMC fracture criterion are relevant to material properties, if we can develop a relationship formula between three parameters of the MMC fracture criterion and material properties for an advanced high-strength dual-phase steels sheet, it is very helpful to validate these MMC parameters.

In this paper, uniaxial tensile and shear tests were performed on DP590, DP780, DP980, and DP1180, and the Hill orthotropic elasto-plastic model and the MMC fracture criterion were used to comprehensively characterize the plastic behavior and ductile fracture properties of the plates. A numerical program employing the user material subprogram of Abaqus Explicit was performed to compare the simulation with the test results. Finally, a series of parametric studies were carried out to discuss the changes of MMC parameters under different steel sheets performance parameters, and a relationship between three parameters of the MMC fracture criterion and material properties for advanced high-strength dual-phase steels sheet was developed to help validation of the three parameters of the MMC criterion.

2. Experiments

2.1. Material

A family of advanced high strength steels is comprised of a variety of steels, most of which are multiphase materials with tensile strength greater than 600 MPa, such as Dual-Phase steel (DP), Transformation Induced Plasticity steel (TRIP), etc. This paper selects DP590, DP780, DP980 and DP1180 steels produced by Shanghai Baosteel Company for research. The microstructure of DP steels mainly consists of two phases: ferrite and martensite.

2.2. Plasticity characterization

A complete plasticity model consists of the yield criterion, the flow rule and the hardening rule. In the literature, various yield criteria have been used to simulate AHSS: von Mises isotropic yield criterion (Yoshida et al., 2008; Durrenberger et al., 2008). Hill (1948) quadratic orthotropic yield criterion; non-quadratic anisotropic Barlat yield criterion (Barlat et al., 2003; Lee et al., 2005). In this paper, due to the anisotropy of the DP steel sheet, we make use of the Hill (1948) orthotropic yield criterion to build a simulation model of the DP steel sheet. The yield condition reads

\[
\sigma = \sqrt{F(\sigma_y - \sigma_z)^2 + G(\sigma_z - \sigma_x)^2 + H(\sigma_x - \sigma_y)^2 + 2L\sigma_{yz}^2 + 2M\sigma_{zx}^2 + 2N\sigma_{xy}^2} \quad (2.1)
\]
where $\bar{\sigma}$ is the Hill (1948) equivalent stress, $\sigma_i$ represents the component of the Cauchy stress tensor, the six constants $F-N$ are anisotropic parameters.

The hardening law defines the method of establishing the subsequent yield surface, and its form changes with different materials. In this paper, the swift hardening law is used to fit the stress-strain curve of the uniform extension of the DP steel

$$\sigma = K(\varepsilon_0 + \varepsilon_p)^n \quad (2.2)$$

where $K$ is the hardening coefficient, $\varepsilon_0$ represents the pre-strain, $n$ denotes the hardening index, and $\varepsilon_p$ is the plastic strain.

By simplifying Eq. (2.3) and transforming it into a linear formula, the $K$ and $n$ values are initially determined by obtaining the slope and intercept of the specimen curve from the yield point to the tensile strength point. The steel plant provided performance parameters of the DP steel and determined the anisotropy parameters as shown in Table 1.

**Table 1.** Hill’s constants of steel sheets

| Steel   | F   | G   | H   | L   | M   | N   |
|---------|-----|-----|-----|-----|-----|-----|
| DP590   | 0.84| 1.023| 0.98| 2.768| 2.768| 2.768|
| DP780   | 0.56| 0.56| 0.44| 1.5 | 1.5 | 1.5 |
| DP980   | 0.4907| 0.573| 0.427| 1.38| 1.38| 1.38|
| DP1180  | 0.46| 0.55| 0.45| 1.46| 1.46| 1.46|

**2.3. Uniaxial tensile test**

The WDW-20D material performance testing machine was used to conduct uniaxial tensile tests on DP590, DP780, DP980, and DP1180 in DP steel sheets. A single tensile test specimen was shown in Fig. 1. Engineering stress-strain curves for four types of DP steels are show in Fig. 2. Through the data processing of the elastic and plastic section of the test stress-strain curve, the performance parameters of each steel sheet are obtained. Material properties are listed in Table 2.

**Table 2.** Material properties

| Steel   | $E$  | $u$  | $K$  | $n$ |
|---------|------|------|------|-----|
| DP590   | 201000| 0.28| 950-1000| 0.175|
| DP780   | 215000| 0.29| 1000-1050| 0.11|
| DP980   | 216000| 0.29| 1150-1180| 0.08|
| DP1180  | 218000| 0.29| 1250-1360| 0.06|

**2.4. Shear test**

In order to study a series of shear fracture phenomena of AHSS, a series of shear specimens (Fig. 2) were designed to conduct shear tests with angles under different steel sheets through a testing machine. Figure 3 shows shear load-displacement curves of DP590, DP780, DP980 and DP1180 steel sheets at different shear angles.
3. Fracture modeling

3.1. MMC ductile fracture model

As mentioned in Section 1, Bai and Wierzbicki (2010) derived a novel functional form of the MMC fracture envelope by transforming the classical stress-based Mohr-Coulomb failure criterion into the space of stress triaxiality, Lode angle parameter and equivalent plastic strain

$$
\varepsilon = \left\{ \frac{K}{c_2} \left[ c_3 + \frac{\sqrt{3}}{2} (1 - c_3) \left( \sec \left( \frac{\theta \pi}{6} \right) - 1 \right) \right] \left[ \sqrt{\frac{1 + c_1^2}{3} \cos \frac{\theta \pi}{6}} + c_1 \left( \eta + \frac{1}{3} \sin \frac{\theta \pi}{6} \right) \right] \right\}^{-\frac{1}{n}}
$$

(3.1)

where the equivalent strain is a function based on the stress triaxiality $\eta$ and the Rod angle parameter $\theta$, $A$ and $n$ are Swift law hardening parameters, and $C_1$, $C_2$, $C_3$ are three material constants which should be calibrated through at least three sets of shear experiments and simulation calibration.
A unique relationship between the triaxiality and Lode angle has been obtained by Wierzbicki and Xue (2005).

\[-\frac{27}{2} \eta \left( \eta^2 - \frac{1}{3} \right) = \cos(2\theta) = \sin \left( \frac{\pi \overline{f}}{2} \right) \quad \eta = \frac{\sigma_m}{\overline{\sigma}} \]  

(3.2)

The stress triaxiality is a dimensionless parameter. The stress triaxiality is always negative in the compression state. Its value is 0 in the pure shear state, it is 1/3 in uniaxial tension, and its value is $-1/3$ in uniaxial compression. There are currently few calculation formulas that can accurately characterize the ultimate equivalent strain of the shear specimen. In this paper, shear simulation is used to obtain the stress triaxiality of the fracture specimen and the fracture strain obtained from the experiment (Fig. 3) to solve the MMC fracture criterion parameters.

3.2. Parameters calibration

With at least three different tests providing three unique combinations of the triaxiality $\eta$ and the Rod angle $\overline{f}$, various optimization approaches could be taken to fit the fracture envelope to the experimental points and thus to obtain $C_1$, $C_2$, and $C_3$.

All the numerical simulations of the present tests in Section 2 were performed in the environment of Abaqus Explicit with the Hill (1948) plasticity model. The stress state parameters $\eta$ and $\overline{f}$ for each test were obtained through detailed FE simulations, and the Hill (1948) equivalent strain to fracture for every test was determined by a hybrid method of DIC and FEA. A Matlab subroutine was written to minimize the Mean Squared Error (MSE) between the test results and fracture envelope and to optimize the values of $C_1$, $C_2$, and $C_3$. The calibrated MMC parameters are listed in Table 3. One can see a small MSE value for tests, which shows a strong data fitting ability of the MMC fracture envelope.
Table 3. Calibrated MMC parameters of DP steel and MSE for the calibration

| Material | $C_1$  | $C_2$ (MPa) | $C_3$  | MSE  |
|----------|--------|-------------|--------|------|
| DP590    | 0.1281 | 536         | 0.9115 | 6.1% |
| DP780    | 0.1535 | 720         | 0.9882 | 5.3% |
| DP980    | 0.1693 | 926         | 1.1574 | 5.8% |
| DP1180   | 0.1855 | 1110        | 1.2615 | 7.2% |

A user material subroutine (VUMAT) in the environment of Abaqus Explicit with both the Hill (1948) plasticity and MMC fracture model was implemented to simulate the present tests. The element deletion technique is used to model the fracture process and the added damage parameters caused the mesh to disappear to realize the specimen fracture. When the fracture parameter reaches 1, the specimen is damaged and fractured. Figure 4 shows fracture of the tensile test specimen at different angles, which is consistent with the test results. The comparison of the fracture curves of the $0^\circ$ specimen is shown in Fig. 5a.

3.3. Parameter correlation

Figure 5b shows the values of three MMC parameters under different steel sheets. As the yield strength of steel sheets increases, the three parameters of MMC show an upward trend, and the interval of each parameter is relatively fixed.
Research on parameters of MMC fracture criterion...

Fig. 5. (a) Comparison of load-displacement responses of simulations with $0^\circ$ shear specimen against experimental data. (b) MMC parameters curve

The currently used process of solving MMC fracture parameters is relatively cumbersome and requires at least three test results to solve the equations. Therefore, it is important to study the correlation between the obtained MMC parameters and the material properties of DP steel. It is found that the $C_1$ range is concentrated between 0.1-0.3, the $C_2$ parameter is about 90% of the tensile strength, and the $C_3$ fluctuates around 1. The correlation between the three fracture parameters and the material properties ($K, n$) of DP steel is built as shown in Eq (3.3), $R^2$ represents goodness of fit, which is the degree to which the regression line fits the observed value. The three parameters of $C_1$, $C_2$, $C_3$ are respectively fitted in a linear form, and the expressions were established by the work hardening index $n$. The preliminary fitting parameters $M_D$, $M_P$ and $R^2$ are shown in Table 4

$$C_{1,2,3} = M_Dn + M_P$$  \hspace{1cm} (3.3)

Table 4. MMC parameters table

| MMC parameters | $M_D$  | $M_P$  | $R^2$  |
|----------------|--------|--------|--------|
| $C_1$          | -0.338 | 0.19512| 0.9562 |
| $C_2$          | -2.48371K | 1.003K | 0.9991 |
| $C_3$          | -2.81245 | 1.40876| 0.9871 |

The approximate value of the three MMC free parameters of $C_1$, $C_2$, $C_3$ can be initially determined with Eq. (3.2). For a kind of dual-phase steel sheet, the three parameters of the MMC criterion can be fine-tuned after employing a test curve such as a uniaxial tensile test to obtain $K, n$. Equation (3.3) can reduce the difficulty of solving the three parameters of the MMC criterion.

4. MMC fracture model verification

In order to verify the fracture parameters of various steel sheets and their mutual relations and the accuracy of the MMC fracture model in different intervals when stress triaxiality is greater than zero, stretch-bending tests and numerical simulations were carried out. The stretch-bending test and Nakazima test specimens were designed. The Nakazima tests and the stretch-bending tests were carried out through a punching machine. The VUMAT fracture subroutine was embedded in Abaqus to simulate the MMC fracture under different fracture conditions.
4.1. Stretch-bending tests and simulation

4.1.1. Stretch-bending tests

The punching machine (Fig. 6a) has been used to perform stretch-bending tests on different steel samples with different rounded dies. Figure 6b shows the unbroken stretch-bending test to establish a basis for comparing the fracture simulation models. Figure 8 shows the fractured stretch-bending test. Figure 8a shows the stretch-bending specimens with tensile fracture. Figure 8b shows the change from shear fracture to tensile fracture with rounded corners and specimens. Figure 8c shows the shear fracture specimens with multiple steel sheets and multiple rounded corners.

![Fig. 6. (a) Punching machine mould. (b) Unbroken stretch-bending tests](image)

![Fig. 7. Unbroken stretch-bending simulation](image)

![Fig. 8. Fractured stretch-bending specimens](image)
4.1.2. Stretch-bending model verification

Establish a stretch-bending model in Abaqus and embed the VUMAT subroutine to perform a series of stretch bending simulations. As shown in Fig. 7, the stretch-bending simulation was carried out according to the blank holder force and depth in the stretch-bending test. The comparison with the test results proves that the simulation and test stretch-bending specimen results are quite good, which proves that the establishment of the MMC fractured model is relatively accurate.

4.1.3. Stretch-bending simulation verification

MMC model fracture simulation of stretch-bending specimens was carried out in ABAQUS. To verify the accuracy of the fracture parameters of each steel sheet, based on the MMC parameters obtained in Section 3, the material properties of each steel sheet were imported into the stretch-bending model for fracture simulation. Figure 9 shows the two kinds of fracture simulation. Figure 9a shows the stretch-bending specimens with necking fracture, the stress triaxiality of necking fracture is 0.3-0.6. Figure 9b shows the stretch-bending specimens with shear fracture, the stress triaxiality ranges from 0 to 0.3. For the fractured specimens with the same fillet, compare the unbroken specimen with the unbroken simulation to verify the MMC fracture model, and verify the MMC parameters through the fractured specimen and simulation.

Fig. 9. Stretch-bending model fracture simulation
Compared with the test results, the fracture position of the simulation model is more consistent with the bending depth, which proves that the MMC criterion can accurately predict the necking fracture and shear fracture of DP steel sheets, and the MMC parameters are more accurate.

4.2. Nakazima tests and simulation

4.2.1. Nakazima test

In order to study the fracture condition of DP steel sheets under biaxial tension, Nakazima tests were carried out on four DP steel grades through the punching machine (Fig. 10). The circular grid was printed on the specimen through electrochemical corrosion, and the strain and fracture were determined by measuring the length of the long and short axes of the grid after fracture. The Nakazima test specimens are shown in Fig. 11.

4.2.2. Nakazima simulation verification

Establish a Nakazima model in Abaqus and embed the VUMAT subroutine to simulate the fracture under biaxial tension in a series of stretch bending simulations. The fracture condition of the MMC fracture model under biaxial tensile state was obtained by simulating the Nakazima specimens (Fig. 12), and compared with the Nakazima test, the accuracy of the MMC fracture model under the biaxial tensile state was verified. The value of stress triaxiality is 0.66. The comparison between the simulated result and the test specimen shows that the fracture location and strain are the same, which proves that the MMC fracture model can accurately predict the fracture in the biaxial tensile range, and the accuracy of MMC parameters is further verified.
5. Conclusions

In this paper, tensile, shear and stretch-bending tests of AHSS DP steel sheets of DP590, DP780, DP980, DP1180 were designed, the equivalent strains under different stress states were obtained using the DIC-3D strain gauge, and the MMC fracture model was established to predict the tensile and shearing properties. For shear fracture, the stress triaxiality and equivalent strain were solved through a combination of more than three sets of experiments and simulations. The equations were established to obtain the MMC fracture parameters of AHSS DP steel sheets, and the model simulation parameters relationships of different steel sheets were determined. Combining the performance parameters of different AHSS DP steel sheets, the expression for MMC fracture parameters was established. Finally, the accuracy of the MMC parameters was verified through stretch-bending, Nakazima tests and simulations. The main conclusions of this research are:

- By comparing the numerical results and experimental data of the AHSS (DP590, DP780, DP980, DP1180) tensile and shear tests, it proves that the MMC simulated fracture model can also accurately predict the ductile fracture of DP980 and DP1180. It is proved by fracture simulation that the MMC fracture criterion is applicable to a wide range of stress triaxiality for the ductile fracture of DP steel.

- Based on the property parameters of the four kinds of sheet materials, MMC fracture parameter curves of the AHSS DP steel sheets DP590, DP780, DP980, DP1180 were established by fitting the correlation curves of $C_1$, $C_2$ and $C_3$ with the material properties $K$ and $n$. For a kind of dual-phase steel sheets, the approximate values of $C_1$, $C_2$ and $C_3$ of the MMC criterion were preliminarily determined with material properties, and then the MMC criterion can be fine-tuned employing a test curve such as a uniaxial tensile test, which reduces the difficulty of solving the three parameters of the MMC criterion.

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