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Published in:
Physical Review C

DOI:
10.1103/PhysRevC.100.014311

Published: 16/07/2019

Document Version
Publisher's PDF, also known as Version of record

Link to publication on the UWS Academic Portal

Citation for published version (APA):
Spagnoletti, P., Simpson, G., Kisyov, S., Bucurescu, D., Regis, J-M., Saed-Samii, N., Blanc, A., Jentschel, M., Koster, U., Mutti, P., Soldner, T., de France, G., Ur, C. A., Urban, W., Bruce, A. M., Bernards, C., Drouet, F., Fraile, L. M., Gaffney, L. P., ... Zielinska, M. (2019). Lifetimes and shape-coexisting states of 99Zr. Physical Review C, 100(1), [014311]. https://doi.org/10.1103/PhysRevC.100.014311

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Lifetimes and shape-coexisting states of $^{99}$Zr

P. Spagnoletti,1 G. Simpson,2 S. Kisyov,3 D. Bucurescu,3 J.-M. Régis,4 N. Saed-Samii,4 A. Blanc,5 M. Jentschel,5 U. Köster,5 P. Mutti,5 T. Soldner,5 G. de France,6 C. A. Ur,7 W. Urban,8 A. M. Bruce,9 C. Bernards,10 F. Drouet,2 L. M. Fraile,11 L. P. Gaffney,12 D. G. Ghită,3 S. Ilieva,13 J. Jolie,14 T. Kröll,13 S. Lalkovski,15 C. Larijarni,16,17 R. Lică,3 H. Mach,11,18 N. Márginean,3 V. Pazić,11 Zs. Podolyák,16 P. H. Regan,16,17 M. Scheck,1 J. F. Smith,1 G. Thiamova,5 C. Townsley,16 A. Vancraeyenest,2 V. Vedia,11 N. Warr,4 V. Werner,10,13 and M. Zielnińska14

1School of Engineering, University of the West of Scotland, Paisley PA1 2BE, United Kingdom
2LPSC, Université Grenoble Alpes, CNRS/IN2P3, Institut National Polytechnique de Grenoble, 38026 Grenoble Cedex, France
3Horia Hulubei National Institute of Physics and Nuclear Engineering (IFIN-HH), 077125 Bucharest, Romania
4Institut für Kernphysik der Universität zu Köln, Zülpicher Straße 77, 50937 Köln, Germany
5Institut Laue-Langevin, 71 avenue des Martyrs, 38042 Grenoble Cedex 9, France
6Grand Accélérateur National d’Ions Lourds, CEA/DRF-CNRS/IN2P3, Boulevard Henri Becquerel, 14076 Caen, France
7INFN, via Marzolo 8, 35131 Padova, Italy
8Faculty of Physics University of Warsaw, ulica Pasteura 5, 02-093 Warsaw, Poland
9SCM, University of Brighton, Lewes Road, Brighton BN2 4GJ, United Kingdom
10WNSL, Yale University, P.O. Box 208120, New Haven, Connecticut 06520-8120, USA
11Grupo de Física Nuclear & IPARCOS, Universidad Complutense de Madrid, CEI Moncloa, 28040 Madrid, SPAIN
12EP Department, ISOLDE, CERN, Geneva, Switzerland
13Institut für Kernphysik, TU Darmstadt, Schlossgartenstraße 9, 64289 Darmstadt, Germany
14CEA de Saclay, IRFU, 91191 Gif-sur-Yvette, France
15Faculty of Physics, University of Sofia, 1164 Sofia, Bulgaria
16Department of Physics, University of Surrey, Guildford GU2 7XH, United Kingdom
17National Physical Laboratory, Teddington, Middlesex TW11 0LW, United Kingdom
18National Centre for Nuclear Research, ulica Hoża 69, Warsaw, Poland

(Received 14 January 2019; revised manuscript received 18 April 2019; published 16 July 2019)

Lifetimes of intermediate-spin states in two rotational bands of $^{99}$Zr have been measured. These states were populated following the neutron-induced fission of $^{235}$U at the PF1B beamline of the Institut Laue-Langevin, Grenoble, during the EXILL-FATIMA campaign. The nucleus $^{99}$Zr exhibits shape coexistence and lies precisely on the border of an abrupt change in ground-state deformation when going from $N = 58$ to $N = 60$, making its study interesting for understanding the mechanisms involved in the rapid onset of deformation here. The $B(E2)$ values extracted for decays in the $v3/2[541]$ band allow quadrupole deformations of $\beta_2 = 0.34(1)$ and $0.26(3)$ to be determined for the 821.6- and 1236.6-keV members, whereas $\beta_2 = 0.32(3)$ was found for the 850.5-keV member of the $v3/2[411]$ band. Some of the excited states known in $^{99}$Zr have been reasonably described with interacting boson-fermion model (IBFM) calculations. Type-II shell evolution is proposed to play a major role in modifying single-particle energies in $^{99}$Zr.

DOI: 10.1103/PhysRevC.100.014311

I. INTRODUCTION

Nuclei of the neutron-rich $A \approx 100$ region possess a wide variety of shape phenomena. A rapid change in ground-state deformation between the spherical $^{96}$Zr, weakly deformed $^{98}$Zr [1], and strongly deformed $^{100}$Zr [2] is well known. This discovery was surprising as the properties of the atomic nucleus generally evolve smoothly as a function of neutron or proton number. The $Z = 38$ ($\pi p_{3/2}$) and 40 ($\pi p_{1/2}$) and the $N = 50$ ($\nu g_{9/2}$), 56 ($\nu d_{5/2}$), and 58 ($\nu s_{1/2}$) spherical subshell closures, combined with a weak integrated residual proton-neutron interaction, mean that from $N = 50$ to 58 the low energy structure of the Sr and Zr isotopes resembles that of a semimagic nucleus. At $N = 60$ a strongly (prolate) deformed ground-state rotational band develops and forms the first few states. This shape change is more gradual across $N = 58$–60 for the higher-Z Mo–Pd nuclei of the region, which exhibit triaxiality [3–6]. At lower $Z$ values the $N \geq 60$ nuclei $^{96,98,100}$Kr have recently been shown to possess considerably less collectivity, due to reduced $\pi g_{9/2}$ occupation and prolate-oblate shape coexistence [7,8]. The rapid nature of this ground-state deformation change has made this region a challenge to study theoretically. Furthermore, these neutron-rich

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nuclei are often far from stability and difficult to access experimentally.

A variety of theoretical explanations exist to explain this shape change including the crossing of two different mean-field configurations; one governed by spherical shell effects and the other a deformed intruder containing multiple particle-hole excitations, dominated by the integrated residual proton-neutron interaction [9–11]. Experimental evidence for coexisting spherical and deformed configurations exists for 96–98Sr [11–12], 96–102Y [13–15], and 98–100Zr [10,16–19]. A strong interaction between occupied πg9/2–νg7/2 spin-orbit partners has been proposed to play a major role in obliterating the N = 56, 58 and Z = 38, 40 spherical subshell closures, leading to collective motion [20–22]. Occupation of high- j, low-Ω deformation driving νh11/2 orbitals [21], along with the presence of deformed shell gaps at Z = 38, N = 60 [4,13], has also been shown to help stabilize deformation here. The rapid onset of the ground-state deformation is an example of quantum shape phase transition [23]. Recently type-II shell evolution [24] has been proposed to explain the onset of collectivity in this region [25]. In this mechanism specific particle-hole excitations for excited levels modify the underlying shell-structure due to the changed occupation probabilities altering the strength of the tensor force.

For the Zr isotopes the latter mechanism occurs once the νd5/2 subshell approaches full occupation and neutrons can then first occupy the νg7/2 and νh11/2 orbitals. Proton particle-hole excitations provide initial πg9/2 subshell occupation. These then interact strongly and attractively with neutrons situated in both the νg7/2 spin-orbit partner and νh11/2 orbitals. The tensor and central forces act coherently on the νg7/2 orbit, lowering its monopole energy, which in turn results in higher occupancy. Although the tensor and central forces act incoherently for the πg9/2–νh11/2 coupling, the net interaction is still attractive. The energy of the πg9/2–πp1/2 subshell gap is then reduced, further increasing its filling. Higher occupancy of the πg9/2 orbit leads to the creation of more holes in the πpf shell, further increasing collectivity. Evidence for this feedback mechanism presents itself beyond N = 56, once the νd5/2 subshell approaches full occupation and neutrons can first enter the νg7/2 and νh11/2 orbitals. Quasirotational bands appear at 1581.6 and 854.0 keV in 96,98Zr, which drop further in energy and increase in collectivity in 100Zr, to become the ground-state rotational band.

It is of particular interest to study the properties of shape-coexisting structures at the spherical-deformed border (N = 59), which may allow additional insights into the underlying mechanisms driving the shape change. To date no coherent theoretical explanation exists describing all shape coexisting features found in this region, even though it contains some of the best known cases in the whole nuclear landscape [26]. In 99Zr low-lying spherical states coexist with well-deformed rigid rotational bands situated at 0.6–1.0 MeV [10,17,18,27]. An absence of reliable and pertinent experimental data on the rotational bands of 99Zr has so far hampered any theoretical interpretations. Different quadrupole moments have been reported for the νh9/2[2404] and νh5/2[541] bands of 99Zr [17,18], implying that the rigidity of its core is sensitive to the occupation of specific orbitals. Furthermore, there is, to date, no evidence for oblate shapes expected to exist and play a significant role in the rapid onset of ground-state deformation here. For this reason we have chosen to study the shapes of the rotational bands in 99Zr.

Measurements of the electromagnetic transition rates between different states in the bands of odd-Z nuclei can give crucial information on collectivity, or help identify the unpaired orbital. The reduced E2 transition rate, B(E2), is directly related to quadrupole collectivity. This quantity can be derived from the measured lifetime of a stretched intraband E2 transition. Alternatively, the underlying single-particle structure of a band can be probed by measurements of intraband B(M1) values, which are often orbital dependent. In the present study the lifetimes of excited states in 99Zr have been measured. These nuclei were populated following the cold-neutron induced fission of 235U. Previously, the β decay of mass-separated 99Y ions was used to populate 99Zr for lifetime measurements [10]. The 5/2+ spin of the ground state of 99Y [15], originating from the occupation of a π5/2[422] Nilsson orbital, permitted only limited access to members of the rotational bands of 99Zr. The prompt-fission reaction produces nuclei, on average, with intermediate-spin states (6h–8h), allowing lifetime measurements of levels with higher spins than those fed following β decay.

II. EXPERIMENT

Lifetimes of excited states in 99Zr were measured via the fast-timing technique. This uses γ(E, t)–γ(E, t) coincidences for direct timing measurements and relies on the good time resolution (≈200 ps) of LaBr3(Ce) detectors to access the lifetimes of states in the 10 ps-to-ns time range. Cold-neutron induced fission of 235U produces secondary neutron-rich nuclei in the A ≈ 100 region with average spins of 6h–8h. It is therefore a suitable reaction to populate the excited states of interest in 99Zr, especially as this nucleus is situated at one peak of the fission-yield distribution. As some 100 fission fragments are reasonably well produced in this reaction, the modest energy resolution of the LaBr3(Ce) detectors is not sufficient to uniquely select a γ-ray cascade of interest. This requires additional γ-ray detection using Ge detectors with their superior energy resolution.

The experiment was performed at the PFIB cold-neutron guide [28] of the high-flux reactor of the Institut Laue-Langevin, Grenoble, within the framework of the EXILL-FATIMA campaign [29]. The collimated neutron beam, with a flux Φ ≈ 108 n/(cm² s), was ≈1 cm² in area [30] and induced fission in a 0.8-mg 235UO2 (0.675 mg 235U) target. The target was sandwiched between two 25-μm-thick Be backings, in order to stop the fission fragments in a time of just a few ps. This minimized the Doppler broadening of any emitted prompt γ rays. The target was placed at the center of the EXILL-FATIMA γ-ray detector array, which consisted of 8 EXOGAM clover Ge and 16 LaBr3(Ce) detectors [29]. The data were acquired during a two-week measurement period and sorted offline into γ(E)–γ(LaBr3)–γ(LaBr3) coincidence events, occurring within a 120-ns time window. Timing signals of the LaBr3(Ce) detectors were recorded in analog.
FIG. 1. Partial decay scheme of $^{99}$Zr. Transition and level energies are taken from Ref. [18]. Some known weak decay branches are not shown.

time-to-amplitude converters (TACs) with a 50 ns range. More details on the experiment can be found in Ref. [29].

III. RESULTS

A partial level scheme of $^{99}$Zr, containing the levels and decays of interest for the present work, is shown in Fig. 1. Here the level and transition energies are taken from Ref. [31].

The lifetime of the 121.7-keV level has been reported to be measured several times [31] and, therefore, constitutes a good test case. Furthermore several lifetimes measured from this data set have been reported previously [32–34]. The 192.6–536.0–121.7-keV cascade was used for this. The spectra presented in Fig. 2 were obtained by gating on the 192.6-keV transition (blue), using a background gate at 208 keV (red), with the Ge detectors, and by gating on the 536.0-keV transition with the LaBr$_3$(Ce) detectors. The corresponding time spectra (see Fig. 3) were produced with an additional gate using the LaBr(Ce) detectors on the 121-keV transition and shows that the background is not entirely prompt and therefore contributes to the slow component of the time spectrum. The background is subtracted and the slope is measured. This was performed for both the delayed and antidelayed time spectra and a weighted average is given. The delayed time spectrum corresponds to a time-to-amplitude converter (TAC) being started with a transition which feeds the level of interest and stopped by a transition decaying from the level of interest. The reverse is true for the antidelayed time spectrum. The value of $\tau$ = 1550(90) ps obtained in the present work agrees well with the value of $\tau$ = 1544(43) ps reported in the compilation of Ref. [31], while a value of $\tau$ = 1880(120) ps is obtained

FIG. 2. Energy spectra obtained when gating on the 536.0-keV transition with the LaBr$_3$(Ce) detectors and the 192.6-keV transition (blue) and a background energy of 208.0 keV with the Ge detectors, respectively.

FIG. 3. Delayed time spectra obtained when gating on the 536.0- and 121.7-keV transitions with the LaBr$_3$(Ce) detectors and additional gates on the 192.6-keV transition (blue) and a background energy of 208.0 keV (red).
TABLE I. Gates set on Ge and LaBr$_3$(Ce) detectors for lifetime ($\tau$) measurements and the results obtained. The subscripts $ij$ and $ji$ correspond to the gate orders start/stop and stop/start, respectively. Lifetimes above 1 ns were determined using the slope (SL) method and lifetimes below 1 ns were determined using the centroid difference (CD) method.

| $E_i$ (keV) | $\gamma$-ray Gates (keV) | $\tau$ (ps) | Method |
|-------------|--------------------------|-------------|--------|
|              |              |             |        |
| Ge | LaBr$_{ij}$ | LaBr$_{ji}$ |
| 121.7 | 192.6 | 536.0 | 121.7 | 1550(90) | SL |
| 657.9 | 121.7 | 192.6 | 536.0 | 35(13) | CD |
| 821.6 | 566.0 | 415.0 | 143.0 | 3900(200) | SL |
| 850.5 | 121.7, 536.0 | 215.5 | 192.6 | 100(25) | CD |
| 1236.6 | 143.0 | 566.0 | 415.0 | 40(7) | CD |

without employing any background subtraction. This method was also employed to measure the lifetime of the $2_1^+$ state in $^{146}$Ba. A value of $\tau = 1260(40)$ ps is obtained, which agrees well with the value of $\tau = 1240(40)$ ps reported in the compilation of Ref. [35].

Measurements of the lifetimes of four other states of $^{99}$Zr were possible. The various gates used are listed in Table I, along with the lifetimes obtained. For the 850.5-keV state a quadruple Ge-Ge-LaBr$_3$-LaBr$_3$ coincidence was required to achieve the necessary selectivity. A summary of the results obtained is presented in Table I. With the exception of the value for the 121.7-keV level, all other lifetimes are reported for the first time.

Spectra obtained when gating on the 121.7- and 192.6-keV transitions in the Ge and LaBr$_3$(Ce) detectors are shown in Fig. 4. Here one can clearly see the 536.0-keV transition depopulating the 657.9-keV level in both the Ge and LaBr$_3$(Ce) detectors.

The lifetime of the 657.9-keV level was measured using the centroid difference technique. The lifetime is determined by the centroid difference in the delayed and antidelayed time spectra, which are shown in Fig. 5. When there is no background contribution the lifetime is related to the centroid difference by the equation

$$\Delta C_{\text{FEP}} = \Delta C_{\text{exp}} + 2\tau,$$

(1)

where FEP stands for full-energy peak and PRD is the prompt response difference. The PRD describes the combined $\gamma-\gamma$ time walk of the setup [36].

In the case where the background contribution to the time spectra are not negligible, the centroid difference between the full-energy peaks, $C_{\text{FEP}}$, is related the the experimental centroid difference, $C_{\text{exp}}$, by the relation

$$\Delta C_{\text{FEP}} = \Delta C_{\text{exp}} + \frac{1}{2}[t_{\text{corr}}(\text{feeder}) + t_{\text{corr}}(\text{decay})],$$

(2)

where

$$t_{\text{corr}}(\text{feeder}) = \left[\frac{\Delta C_{\text{exp}} - \Delta C_{\text{bg}}}{P/B}\right]_{\text{feeder}},$$

and

$$t_{\text{corr}}(\text{decay}) = \left[\frac{\Delta C_{\text{exp}} - \Delta C_{\text{bg}}}{P/B}\right]_{\text{decay}}.$$

(3)

The term $\Delta C_{\text{bg}}$ is the centroid difference of the background and is determined analytically for both transitions. The analytical corrections for both the feeding and decaying transitions are shown in Figs. 6 and 7, respectively. The term $P/B$ is the peak-to-background ratio. A thorough description of this method is presented in Refs. [33,34].

Transition branching ratios from [31] and corrections for internal conversion [37] were used to convert the measured level lifetimes into partial stretched $E2$ lifetimes ($\tau_{E2}$). Reduced transition rates were then calculated using the formula

$$B(E2) = \frac{450\hbar}{24\pi e^2 b^2 \tau_{E2}} \left(\frac{\hbar c}{E_\gamma}\right)^5.$$  

(4)

From the $B(E2)$ values transition quadrupole moments, $Q_t$, can be derived in the rigid-rotor framework using the formula

$$Q_t^2 = \frac{16\pi}{5} \frac{B(E2)}{\langle J_f K 20 | J_i K \rangle^2}.$$  

(5)
The present work adopts the \( ^2\gamma \) ray (LaBr \(_3\)).

where \( J_i \) is the initial spin, \( J_f \) is the final spin, and \( K \) is the projection of the aligned angular momentum on the symmetry axis. Deformation parameters, \( \beta_2 \), can be determined using

\[
\beta_2 = \frac{91.7 Q_0}{2 A^{2/3}},
\]

with \( Q_1 = Q_0 \).

For \( \Delta J = 1 \) transitions the experimental partial \( M1 \) lifetime (\( \tau_M \)) is related to the reduced transition rate by

\[
B(M1) = \frac{9h}{16\pi \mu_N^2 \tau_M} \left( \frac{\hbar e}{E_{\gamma}} \right)^3.
\]

In the case of the (3/2\(^+\)) band built on either the 575.7-keV [18] or 657.9-keV [27] states, conflicting spin assignments exist. The present work adopts the \( J^\pi \) assignments from Ref. [18] and provides experimental evidence to support this choice in Sec. IV. A rigid-rotor analysis of the \( \Delta J = 1 \) branching ratios allows the mixing ratio \( \delta \) to be estimated for intraband transitions. For either scenario the \( E2 \) contribution to a \( \Delta J = 1 \) transition was calculated to be at most 23-\% and more typically \( \approx 5\% \). These estimations agree with the experimentally measured \( \delta \) values for transitions in the \( \nu 3/2[411] \) band of the neighboring \(^{97}\)Zr [38,39]. Therefore \( \Delta J = 1 \) transitions in the (3/2\(^+\)) band were considered to be pure \( M1 \) in nature in the analysis. Values of \( B(M1) = 0.032(10) \) and \( B(M1) = 0.042(21) \) W.u. were found for the 192.6- and 82.2-keV transitions, respectively, in the \( \gamma \) cascade of the 850.5–657.9–575.7-keV levels. A summary of the reduced transition probabilities measured in this work is given in Table II. Calculations of deformation parameters for members of the \( \nu 3/2[541] \) and \( \nu 3/2[411] \) bands are presented in Table III.

### IV. DISCUSSION

#### A. 575.7–657.9–850.5-keV levels

The exact nature of the 575.7- and 657.9-keV levels is uncertain. A positive parity was assigned to these states based on measured \( \log ft \) values from the \( \beta \) decay of \(^{99}\)Y [10,40]. In [17] these two levels were presented as the bandheads of two separate \( K = 3/2^+ \) and \( 5/2^+ \) decoupled bands. This was then revised to them being the \( (3/2^+) \) and \( (5/2^+) \) members of the same \( K = 3/2^+ \) band [18]. This interpretation is supported by an observed transition between the \( K = 9/2^+ \) isomer at 1038.5 keV and the 657.9-keV level with energy 381 keV. However, Lhersonneau et al. later noted that the 82.2-keV \( K + 1 \rightarrow K \) transition connecting them appeared to be too weak to be an intraband transition [40]. In a separate work the 657.9-keV state was proposed to be a 3/2\(^+\) bandhead, with mixed \( \nu 3/2[411] \) and \( \nu 3/2[422] \) parentage [27], though the

### Table II. Level energies \( E_i \), transition energies \( E_{\gamma} \), level lifetimes, and reduced transition rates \( B(\sigma L) \) determined for states of \(^{99}\)Zr in the present work. All \( \Delta J = 0, \pm 1 \) transitions are assumed to be pure \( M1 \).

| \( E_i \) (keV) | \( E_{\gamma} \) (keV) | \( J_i \rightarrow J_f \) | \( \sigma L \) | \( B(\sigma L) \) (W.u.) |
|---|---|---|---|---|
| 121.7 | 121.7 | 3/2\(^+\) \rightarrow 1/2\(^+\) | \( M1 \) | 0.010(7) |
| 657.9 | 82.2 | 5/2\(^+\) \rightarrow 3/2\(^+\) | \( M1 \) | 0.042(21) |
| 536.0 | 5/2\(^+\) \rightarrow 3/2\(^+\) | \( M1 \) | 0.0047(20) |
| 821.6 | 143.0 | 11/2\(^+\) \rightarrow 7/2\(^-\) | \( E2 \) | 99(6) |
| 850.5 | 192.6 | 7/2\(^+\) \rightarrow 5/2\(^+\) | \( M1 \) | 0.032(10) |
| 274.5 | 7/2\(^+\) \rightarrow 3/2\(^+\) | \( E2 \) | 46(12) |
| 1236.6 | 415.0 | 15/2\(^-\) \rightarrow 11/2\(^-\) | \( E2 \) | 60(11) |

### Table III. Level energies \( E_i \), transition energies \( E_{\gamma} \), reduced transition rates \( B(E2) \), and deformation parameters determined for states of \(^{99}\)Zr in the present work.

| \( E_i \) (keV) | \( E_{\gamma} \) (keV) | \( B(E2) \) (W.u.) | \( Q_\beta \) (eb) | \( \beta_2 \) | Band |
|---|---|---|---|---|---|
| 821.6 | 143.0 | 99(6) | 3.3(1) | 0.34(1) | \( \nu 3/2[451] \) |
| 1236.6 | 415.0 | 66(5) | 2.4(3) | 0.26(3) | \( \nu 3/2[451] \) |
| 850.5 | 274.5 | 46(12) | 2.9(3) | 0.32(3) | \( \nu 3/2[411] \) |
The 381-keV transition was rejected in the evaluation by [31] as it is inconsistent with the adopted $J^\pi = 3/2^+$ assigned to the 657.9-keV level. Figure 8 shows a coincident $\gamma$-ray spectrum. This figure corresponds to a gate on the 218-keV transition, which feeds the $K = 9/2^+$ isomer, and gates on the 536.0- and 121.7-keV transitions, which correspond to the cascade of decays from the 657.9-keV level. The 381-keV transition is clearly present along with the 251-keV transition that feeds the $J^\pi = 11/2^+$ above the $K = 9/2^+$ isomer. Therefore a $J^\pi = 3/2^+$ assignment for the 657.9-keV level is rejected and the $J^\pi = 5/2^+$ assignment as suggested in Ref. [18] is proposed to be correct. The disparity in intensity between the 192.6- and 188.5-keV transitions is due to the 215.5-keV transition which, populating the 850.5-keV level, has an energy similar to the 218-keV coincidence gate.

The reduced $M1$ transition rates obtained in the present work, $B(M1) = 0.032(10)$ and 0.042(21) W.u. for the 192.6- and 82.2-keV transitions, respectively, are the same, within errors. This implies the 850.5-, 657.9-, and 575.7-keV levels have a similar structure, or are all members of the same band, in agreement with [18]. The low intensity of the 82.2-keV intraband transition is therefore a consequence of other strong decay paths out of the 657.9-keV level. Its energy is likely perturbed by interactions with other nearby ($3/2^+$) states, or the $3/2^+_1$ level.

The band containing the 575.7-, 657.9-, and 850.5-keV levels has been proposed to have a $v^3/2[411]$ configuration, which has a significant $v_{g7/2}$ component [18]. The log $ft$ values derived for $\beta$ feeding to these levels are 6.3, 6.7, and 6.6, respectively [40]. These values are much higher than those of an allowed Gamow-Teller transition, likely due to the strong spherical $v_{d3/2}$ single-particle component and quasihole nature of the $v^3/2[411]$ orbital. The collectivity present in the band will also fragment the $v_{g7/2}$ strength across several levels, resulting in higher log $ft$ values. The shape coexistence present in $^{99}$Zr and mixed configurations means that it is unclear if asymptotic Nilsson orbital labels are applicable. Nevertheless, a $v^3/2[411]$ label is kept in the article for consistency with the existing literature.

B. $v^3/2[541]$ band

The lifetimes of the three lowest lying members of the $v^3/2[541]$ band, based on the 614.1-keV level were previously measured [40]. These levels were populated following the $\beta$ decay of $^{99}$Y parent nuclei, though only one $B(E2)$ value was obtained, $B(E2; 7/2^+ \rightarrow 3/2^+) = 210(70)$ W.u.

The values of $\beta_2 = 0.34(1)$ and 0.26(3) derived for the $(11/2^-)$ and $(15/2^-)$ members of the same $v^3/2[541]$ band of $^{99}$Zr in the present work are inconsistent. The latter $\beta_2$ value, however, agrees with $\beta_2 = 0.28(1)$ measured for this band’s $(19/2^-)$ and $(23/2^-)$ members [17]. It is also close to $\beta_2 = 0.32(2)$ determined for the same band in the isotope $^{97}$Sr [17]. The change in quadrupole moment across the 821.6-keV state, with spin $(11/2^-)$, may indicate a crossing with a Nilsson orbital of the same spin. A deformation of $\beta_2 = 0.356(8)$ has been reported for the $(21/2^-)$ state of $^{100}$Zr [41], showing that the collectivities of members of the $v^3/2[541]$ band are close to that of the deformed even-even ground-state core. Simplistically this band can be thought of as a $v^3/2[541]$ hole coupled to a $^{100}$Zr core, with the hole acting to reduce the quadrupole moment.

C. Moments of inertia

Differences in the kinematic moment of inertia of the $v^3/2[411]$ band in $^{99}$Zr, compared to other bands of this nucleus have been noted by Wu et al. [27]. This quantity is plotted for the $v^3/2[411]$ bands of $^{99,101,103}$Zr and $^{97}$Sr in Fig. 9. The $v^3/2[411]$ bands of $^{101,103}$Zr and $^{97}$Sr have almost constant moments of inertia, indicating rigid rotation, whereas the slope for the $v^3/2[411]$ band of $^{99}$Zr indicates a degree of softness in the core. Figure 10 of Wu et al. [27] shows that the moments of inertia of the $3/2[541]$ bands of $^{97}$Sr and $^{99}$Zr are also consistent with rigid rotation, with values similar to

FIG. 8. Energy spectra obtained when gating on the 121.7-keV [Ge/LaBr$_3$(Ce)], 536.0-keV (Ge), and 218.0-keV [Ge/LaBr$_3$(Ce)] $\gamma$ rays.

FIG. 9. Kinematic moments of inertia of $v^3/2[411]$ bands in $^{99,101,103}$Zr and $^{97}$Sr.
odd nucleon, allowed to occupy single-particle shell-model orbitals, to an even-even core described by the interaction boson model 1 (IBM-1) [45,46]. The description of the known spectroscopic properties of the lowest-lying states allowed a fine tuning of the IBFM-1 parameters [42] (see also Table IV). Here we use the results of these calculations to investigate their ability to describe the properties of other excited states, including those determined in this experiment.

It should, however, be emphasized that the IBFM-1 description has strong limitations. Nuclei in this region of rapid shape transition, around $N = 60$, have been found to exhibit shape coexistence phenomena, which cannot be accounted for by this model. The fast structure evolution around $N = 60$ also makes it difficult to choose an appropriate even-even core nucleus for $^{99}$Zr as the ground-state deformation changes between the energies of its ground-state band members and the energy distribution of the low-lying states in $^{99}$Zr. The IBM-1 description employed for the core was taken from Ref [47]. The odd neutron coupled to the core was allowed to span the single-particle orbits of the $N = 50–82$ valence space ($s_1/2$, $d_3/2$, $d_5/2$, $g_{7/2}$, and $h_{11/2}$). The IBFM-1 calculations are similar to those performed in Ref. [48] for the isotonic nucleus $^{95}$Sr, which presents structure similarities with $^{99}$Zr. The main difference from the calculations in Ref. [48] is the inclusion of the $h_{11/2}$ orbital in the present calculations, and the use of the same IBFM-1 parameters for the description of both positive and negative parity states.

The single-particle energies for nuclei in this region are not known; they were adjusted to reasonably reproduce the low-energy part of the experimental level scheme. The values adopted for these calculations are given in Table IV, together with quasiparticle energies obtained from BCS calculations with a pairing parameter $\Delta = 1.5$ MeV. The values chosen for the boson-fermion interaction parameters [43,44] were $\Lambda_0 = 0.08$ MeV, $\Gamma_0 = 0.3$ MeV, $\Lambda_0 = 2.9$ MeV$^2$, and $\hbar\omega = 1.5$ MeV.

Electromagnetic $E2$ transition rates were calculated using a boson charge $e_B = 0.159$ $eb$ which describes the $B(E2)$ values in $^{100}$Zr [47] and a fermion charge $e_F$ with the same value. For the $M1$ transitions we used the simplest transfer operator, with gyromagnetic ratios $g_d = 0.4\mu_N$ for the $d$-boson $g$ factor, and $g_n = -2.68\mu_N$ for the fermion, which is 70% of the free neutron value to account for core polarization effects, and a value $g_I = 0$ (the odd nucleon is a neutron).
Figure 11 shows a comparison of the calculated level scheme with the experimental one. The theoretical levels (left side of the figure) are arranged according to the dominating quasiparticle component in their wave functions, with the observation that a general feature is the rather strong mixing between the positive parity orbitals, especially the $d_{5/2}$ and $g_{7/2}$ ones. The experimental level scheme (right side of the figure) highlights some differences between the ENSDF adopted level scheme [31] and the spin assignments of Ref. [18] (see also Fig. 1), showing two distinct bandlike structures: one based on the $576$-keV $3^+$ state, and the remaining part of the $\left( A, a \right)$ structure above the $1323$-keV $9^+$ state.

In Fig. 11, correspondences between calculated and experimental levels are indicated. These are based not only on the excitation energy, but also on the description of the experimental $\gamma$-decay patterns of the states (branching ratios and, when known, reduced transition probabilities). The correspondence between calculated and experimental levels is indicated by the order number of the calculated states of each spin. Tentative associations are indicated by placing this order number within parentheses.

For positive parities, besides the lowest energy states, a one-to-one correspondence with calculated states could be established in this way for a number of states with spin $3/2$ and $5/2$ in the energy range $\approx 600$–$1000$ keV Also, for the higher-spin members of the $\left( A, a \right)$ structure, theoretical counterparts have been proposed. Some difficulties were encountered in the description of the decay patterns of the states at $850$, $1066$, and $1323$ keV, therefore their theoretical assignment is only tentative. Table V shows the comparison between calculated and experimental transition rates. While for the lower-energy states the agreement is good, for the $850$-keV $7^+$ state it is worse, especially its $E2$ branch towards the $576$-keV $3^+$ state is predicted less collective, with a $B(E2)$ value $3$–$4$ times smaller than the experimental value. The decay pattern of the $1323$-keV $9^+$ state towards the $850$-keV $7^+$ and $1066$-keV $9^+$ states [31] also could not be well reproduced (therefore, these states are only tentatively associated with calculated ones). It appears that the connection between the two level structures [band $\left( A, a \right)$] and the band based on the $576$-keV $3^+$ state cannot be well described by this simple model (in terms of these calculations, one would need a
not expected to generate the strong collectivity present towards the bottom of the $v_3/2[541]$ and $v_3/2[411]$ bands. Multi-quasiparticle bands are expected at an energy of $\sim 2\Delta$, much higher than the bandhead energies. Another mechanism must be present which significantly changes the nuclear structure, most likely type-II shell evolution. In particular, the poor agreement between the calculated and experimental members of the $v_3/2[541]$ band may be due to the monopole evolution of the $v_{h11/2}$ orbit, known to be shifted in energy by type-II shell evolution [25].

As observed above, with $N$ increasing from 51 ($^{91}$Zr) to 57 ($^{97}$Zr), the single-particle energies of the positive-parity orbitals evolve rather smoothly as the $v_{d5/2}$ and $v_{s1/2}$ orbits are filled, while the energy of the $v_{h11/2}$ orbit increases. The $v_{h11/2}$ orbit rises in energy with increasing $v_{d5/2}$ occupation due to the repulsive nature of the tensor force for two alike $l + s$ orbits. At $N = 59$ a drastic change in the single-particle energies occurs, with the overall separation of all orbits greatly reduced. This coincides with significant occupation of $\pi g_{9/2}$, $\nu g_{7/2}$, and $v_{h11/2}$ orbits, providing evidence that monopole evolution occurs in collective regions.

V. CONCLUSION

Lifetimes of states in the $v_3/2[541]$ and $v_3/2[411]$ rotational bands of the nucleus $^{99}$Zr have been measured using the fast-timing technique. The $^{99}$Zr nuclei were populated following the neutron-induced fission of a $^{235}$U target during the EXILL-FATIMA campaign. The $v_3/2[541]$ band was deduced to possess quadrupole deformations of $\beta_2 = 0.34(1)$ and $0.26(3)$ at spins of $(11/2^-)$ and $(15/2^-)$, whereas the $(7/2^+)$ member of the $3/2[411]$ band has $\beta_2 = 0.32(3)$. IBFM-1 calculations reasonably reproduce characteristics of many of the known levels of $^{99}$Zr. An exception are the energies of the "antialigned" levels (of spin lower that 11/2) of the negative parity band, which in these calculations has a pure $v_{h11/2}$ origin. Type-II shell evolution is proposed to play a major role in the creation of low-lying rotational bands of $^{99}$Zr.

ACKNOWLEDGMENTS

This work was supported by NuPNET and the German BMBF by Grants No. 05P12PKNUF, No. 05P15RDFN1 and No. 05P12DRNUP, the German Research Council (DFG) under Grant No. SFB 1245, the Spanish MINECO via Project No. FPA2015-65035-P, the UK STFC by Contract No. DNC7RP01/4, the US DOE under Grant No. DE-FG02-91ER40699, and the UK National Measurement Office. The EXILL-FATIMA campaign would not have been possible without the support of several services at the ILL and the LPSC. We are grateful to the EXOGAM Collaboration for the loan of the detectors, to GANIL for assistance during installation and dismantling, and to the FATIMA Collaboration for the provision of LaBr$_3$(Ce) detectors and analog electronics.
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