Refined Force Field for Liquid Sulfolane with Particular Emphasis to Its Transport Characteristics

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ABSTRACT: An all‐atom force field dedicated to capturing the properties of multifunctional sulfolane is necessary. In addition to being an excellent solvent and extractor, sulfolane is also a frequently investigated component for battery electrolytes in recent times. Given this, theoretically capturing its transport properties is essential. However, given the rather high shear viscosity of liquid sulfolane and its polar aprotic nature, formulating an appropriate non‐polarizable force field for this compound remains a challenge. Starting from a generic force field, we report a refined force field for sulfolane which quantitatively captures its bulk properties, resulting in significantly improved estimates for self‐diffusion constant and shear viscosity of sulfolane in comparison to force fields reported hitherto. Density, self‐diffusion constant, and shear viscosity were determined between temperatures (303 and 398) K and at 1 bar pressure. All properties determined from the refined force field are in good agreement with experiments. The refined model employs atomic site charges obtained from the density‐derived electrostatic and chemical (DDEC6) method for liquid sulfolane modeled using quantum density functional theory. Lennard‐Jones parameters were refined using quantum potential energy scans. Despite possessing a large dipole moment, the large molecular size of sulfolane partially disrupts intermolecular dipolar ordering in liquid sulfolane. Molecular dipoles of near neighbor sulfolane, however, retain a partial preference for antiparallel orientation even at the highest temperatures investigated here.
The broad applicability of sulfolane partially finds its footing in its "two-in-one" structure, a predominantly carbon atom-composed ring and a SO₂ crown. Although aprotic, the SO₂ group of sulfolane is the source of its significant dipole moment (5.65 debye from MP2 level calculations carried out in this work). The massive dipole moment contributes to its high relative permittivity of 43.3, when compared to other dipolar aprotic solvents. Sulfolane's ring of carbon atoms and its large dielectric constant come with a twin benefit. Sulfolane is miscible in several polar organic compounds, and at the same time, as a solvent, it solvates many inorganic compounds. Examining its SO₂ group more closely, the vibrational spectrum of SO₂ in sulfolane is very typical of most sulfones.

Earlier work on sulfolane by providing molecular level insights into its nature and exploring the full utility of this promising molecule of sulfolane calculated from the model is just 3.9 debye when compared to the value calculated from MP2 level quantum calculations of 5.65 debye (vide infra). Thus, our continued search for a more physicochemically meaningful and quantitatively reliable force field for sulfolane is not out of place.

While general, all-purpose force fields capture relatively simpler physical properties such as the density of such solvents, quantitatively accurate force fields for transport properties of sulfolane are required, which can enable molecular simulations to provide insights and directions to experimental research on a near-equal footing. The current manuscript is aimed in that direction.

In this study, we aim to arrive at effective force field parameters for sulfolane with particular emphasis on selecting appropriate non-bonded descriptors such as site charges and Lennard-Jones (LJ) parameters, for use in molecular simulations. The atomic-site charges in a liquid can, in principle, be considerably different from those obtained through quantum gas-phase calculations. To derive liquid-phase atomic-site charges for our MD simulations of bulk sulfolane, quantum density functional theory (DFT) optimizations of independent snapshots obtained from the liquid phase of sulfolane were carried out. These snapshots were selected from MD simulations using a generic force field and gas-phase DDEC6 charges (see computational methods).

In the past, molecular simulations, molecular dynamics (MD) simulations, and configurational-bias Monte Carlo simulations have used general and refined force fields to accurately capture several, if not all, experimentally reported thermophysical and thermochemical properties of substances. However, a force field that accurately captures the transport properties of sulfolane and whose potential energy surface (PES) is in good agreement with the quantum mechanical PES is currently absent. The availability of such a force field is of paramount importance to realize the utility of sulfolane-based battery electrolytes. The simulations of Aparicio and co-workers in ref 24 on sulfolane reproduce the density, heat of vaporization, and self-diffusion constant in fair comparison with experiments; however, the shear viscosity predicted by the model is half that of the experimental value, which is somewhat surprising as the self-diffusion coefficient predicted by the model too is 23% lesser than the experimental value. Furthermore, the electric dipole moment of a single molecule of sulfolane calculated from the model is just 3.9 debye when compared to the value calculated from MP2 level quantum calculations of 5.65 debye (vide infra). Thus, our continued search for a more physicochemically meaningful and quantitatively reliable force field for sulfolane is not out of place.

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Figure 1. (a) Molecular structure of sulfolane. (b) Atom types of sulfolane. (c) Chemical identifiers of compound sulfolane.
COMPUTATIONAL METHODS

The non-planar nature of a sulfolane molecule is illustrated in Figure 1 which also provides atom labels which will be later used in the manuscript.

Liquid sulfolane modeled at 303 K and 1 bar using the force field described in ref 2 yielded a reasonably accurate density of 1284 kg m⁻³. However, the self-diffusion coefficient of sulfolane using the force field of ref 2 (D_{ref,2} was calculated to be 6.0 × 10⁻¹⁰ m² s⁻¹) was more than two orders of magnitude lesser than the experimental value of D_{expt} extraplated = 14.72 × 10⁻¹¹ m² s⁻¹ obtained from extrapolation from experimental data in ref 2. As a consequence of the underestimated diffusivity, the viscosity of sulfolane was inestimable from molecular simulations even when calculated through a long MD trajectory of 25 ns duration.

To investigate the applicability of the OPLS force field of sulfolane, we first obtained its parameters from the LgPARGen server.26-28 Although we found that the OPLS force field with the 1.14Å CM1A-LBCC charges27 estimates many physical properties of liquid sulfolane well, the viscosity calculated using this force field was around twice the experimentally reported value of 10.284 mPa.s.29 Hence, a refined force field for sulfolane capturing its transport properties accurately remained a necessity.

We started the force field refinement of sulfolane using the parameters used in ref 2 as our initial guess.

\[
U = \frac{1}{2} \sum_{\text{bonds}} k_b (r - r_0)^2 + \frac{1}{2} \sum_{\text{angles}} k_{\theta} (\theta - \theta_0)^2 + \sum_{\text{dihedrals}} \sum_{n=1} \kappa_n (1 + \cos(n\phi - \phi_n)) + \sum_i \sum_{j \neq i} 4\epsilon_{ij} \sigma_{ij} \left[ \left( \frac{r_{ij}}{\sigma_{ij}} \right)^{12} - 2 \left( \frac{r_{ij}}{\sigma_{ij}} \right)^{6} \right] + \frac{1}{4\epsilon_{ij}} \sum_i \sum_{j \neq i} \frac{q_i q_j}{r_{ij}}
\]

The total potential energy of the system is a sum total of energies from non-bonded contributions such as the Coulombic and the LJ interactions and those from the bonded contributions of bond, angle, and dihedral-angle excitations (eq 1). We refine the Coulombic and LJ interactions and bond and angle equilibrium values to arrive at the refined set of parameters reported here. r₀ is equilibrium bond length, k_b is bond force constant, θ₀ is equilibrium bond angle, k_θ is angle force constant, and φ₀, k_φ, and φ₀ are dihedral parameters. σ_{ij} and ϵ_{ij} are LJ parameters, and r_{ij} is the distance between the centers of the i-th and j-th atoms. ε_{ij} is the permittivity of free space, and q_i is the atomic site charge of the i-th atom.

**Non-bonded Parameters. Deriving Atomic-Site Charges.** The method of refining atomic site charges (DDEC) used here has earlier been employed to refine parameters for imidazolium cation-based ionic liquids. Refined for the imidazolium cation—PF₆⁻ anion pair, these parameters were found to be transferable across a family of imidazolium-based ionic liquids.21,30,31 The fact that this procedure, when systematically applied to two very different kinds of liquids, has yielded reliable parameters (property predictions are comparable to experimentally measured values) prompts us to believe that this procedure can now be used to refine force field parameters for many different classes of liquids. It is also possible that the refined force field for sulfolane reported here is extendable with minor modifications to the entire class of sulfone compounds.

In order to derive atomic site charges from DFT calculations of liquid sulfolane, seven independent snapshots were chosen from a NVT MD run. This MD run used the force field of ref 2 barring the atomic site charges. Atomic site charges used were obtained for a single sulfolane molecule from DDEC625 calculations (Table S1). This MD run contained 26 sulfolane molecules in the liquid phase at 303 K. The linear dimension of the NPT equilibrated box was 16.3 Å. These snapshots were then geometry optimized within quantum DFT using CP2K software (version 6.1)32 with the Perdew, Burke, and Ernzerhof (PBE) exchange–correlation functional33 and Grimme’s D3 empirical van der Waals corrections.34 A convergence criteria of 10⁻⁶ a.u. for the gradient of electronic wave functions and 5 × 10⁻³ a.u. for the force on the nuclei were employed. The core electrons and nuclei were accounted for using the Geodecker–Teter–Hutter pseudopotentials.35,36 All valence electrons were represented by triple-ζ double-polarized basis sets with an energy cutoff of 320 Ry. The coordinates obtained from this minimization were used to obtain valence electron density at the same level of theory. This density was stored in a cube file and was used to obtain DDEC6 liquid-phase atomic charges using Chargemol software (Version 3.5).37 The atomic site charge distributions over seven snapshots were fairly narrow (see Supporting Information Figure S1), and hence, their means were utilizable. More detailed discussions on the applicability of this procedure followed in deriving condensed-phase charges can be found in ref 30. Site charges were averaged over all the molecules of a snapshot as well as over all the seven snapshots to arrive at the final liquid-phase DDEC6 charges employed in the refined force field simulations. These charges are presented in Table 1. Charges from ref 2 and those from OPLS27 are also provided for the sake of completeness.

**Refinement of LJ Parameters.** The LJ parameters were obtained by conducting several trials to fit quantum chemical rigid PES scans of a pair of sulfolane molecules as a function of distance between them. The PES scans were performed using Gaussian 16 software.38 These scans were performed in the gas phase along two different directions of approach of the molecules (shown in Figure 2a,b). The two initial configurations for gas-phase calculations were created in GaussView software (version 5.0.9).39 Subsequently, the LJ parameters employed in ref 2 were suitably modified through several trials so that the total potential energy calculated with the force field matches the quantum chemical PES as closely as possible (shown in Figure 2c,d). Since the PES calculations were
carried out in the gas phase, the gas-phase DDEC6 site charges presented in Table S1 were used to arrive at the refined LJ parameters. The LJ parameters of ref 2, OPLS, and our refined force field (used henceforth in this work) are provided in Table 2. The PESs of both OPLS and of ref 2 are much shallower when compared to the MP2 result.

Table 2. LJ Parameters for all the Force Fields Studied—σ_{ii} (Å) and ε_{ii} (kJ·mol⁻¹) of Eq 1

| atom type | σ | ε |
|-----------|---|---|
| SFO       | 3.55 | 3.80 | 1.046 | 2.000 |
| OFO       | 2.96 | 2.90 | 0.879 | 0.711 |
| CS1       | 3.50 | 3.55 | 0.276 | 0.100 |
| CS2       | 3.50 | 3.50 | 0.276 | 0.100 |
| HC1       | 2.50 | 2.00 | 0.126 | 0.050 |
| HC2       | 2.50 | 2.50 | 0.126 | 0.067 |

Those of ref 2 and of OPLS are provided for the sake of completeness.

The bonded parameters (bond stretch and angle bending) used in the current manuscript are provided in the Supporting Information Tables S2 and S3. Sulfolane, being a cyclic molecule, was anticipated to have large dihedral energy barriers at equilibrium structures. Therefore, any refinement to dihedral parameters was anticipated to have a negligible effect on transport properties. Hence, dihedral parameters were adopted as such from ref 2 without any refinement.

**MD Simulations of Liquid Sulfolane.** Liquid sulfolane was modeled using these refined parameters. Classical MD simulations were performed using GROningen MACHine for Chemical Simulations, that is, GROMACS package (version 2018.3). The particle–particle–mesh Ewald solver was used to calculate the long-range electrostatic interactions. A precision of 10⁻⁵ was used for the same. The leap-frog algorithm, with a time step of 1 fs, was used to evolve the system in time. Atom coordinates were dumped at an interval of 1 ps. C–H covalent bonds were held constrained with the LINCS (Linear Constraint Solver) algorithm present in GROMACS. The Verlet algorithm used by GROMACS was employed for neighbor lists. Van der Waals and Coulomb cutoff distances were both taken to be 12 Å, with a neighbor list up to 14 Å. Interactions between different atom types were defined using the geometric mean, that is, \( \sigma_{ij} = \sqrt{\sigma_{ii} \sigma_{jj}} \) and \( \epsilon_{ij} = \left( \epsilon_{ii} \epsilon_{jj} \right)^{1/2} \). The same combining rules are used by OPLS and our calculations using the force field in ref 2. 1–2 and 1–3 pairs interact via bond stretch and bending interactions only. For the non-bonding interaction involving 1–4 pairs, a scale factor of 0.5 is applied to both the LJ and Coulomb interactions. For all remaining atom pairs, the scale factor for non-bonding interactions is 1.0. Long-range energy and pressure dispersion corrections were applied. The Nose–Hoover thermostat was employed with a coupling time constant of 0.5 ps. NVT production trajectories were used for a majority of the analyses. Berendsen47 and Parrinello–Rahman barostats were used for constant temperature and constant pressure NPT equilibration and NPT production runs, respectively. In either case, a coupling time constant of 2 ps was used. The barostat was coupled to the system every 10 steps when using the Berendsen barostat and every step with the Parrinello–Rahman barostat. All algorithms mentioned are as implemented by GROMACS. An initial configuration of 800 sulfolane molecules was generated using the packing optimization for the automated generation of starting configurations for MD simulation (Packmol-Version 18.002) software.50 Minimization using the steepest gradient method was followed by constant NPT equilibration of the system for 10 ns, following constant NPT production runs of 25 ns. After that, constant NVT equilibration for 10 ns was performed. In the OPLS force field framework and that of the refined force field reported here, the NVT productions runs at 303 K were of duration 50 ns each. Only in the case of the simulations carried out using the force field of ref 2 at 303 K, owing to its sluggishness, an NVT production of 1 μs was required to reach the diffusive regime.

Liquid sulfolane was simulated at several temperatures in the range 303–398 K using the refined force field. NVT production runs of 50 ns were conducted for simulations at...
303 K, 25 ns at 323 and 348 K, and over 12 ns at 373 and 398 K. Other details for these runs remain the same as those for the one performed at 303 K.

Periodic boundary conditions were applied along all three directions. The NPT equilibrated box lengths to accommodate 80 sulfolane molecules for various force fields studied here and for the various temperatures at which the refined force field was studied are given in the Supporting Information Table S4. Visualization was carried out in Visual MD (VMD) software.51

**RESULTS AND DISCUSSION**

All percentage deviations mentioned are calculated from the corresponding experimental value, unless stated otherwise. All expanded uncertainties (U) are those calculated on the average value of the property reported.

**Density.** The average density for each force field studied was calculated by considering 25 ns of the NPT production run (after NPT equilibration). The data was divided into five blocks of 5 ns duration each. The method of calculating the expanded uncertainty (U) on the mean is provided in the Supporting Information. The NPT equilibrated box lengths are provided in Table S4. As shown in Table 3, percentage errors in density (Δρ) with respect to the experimental density, defined as

$$\Delta \rho = \frac{(\rho_{\text{exp}} - \rho_{\text{sim}})}{\rho_{\text{exp}}} \times 100$$

for all force fields, are within 3%.

| force field | ρ_{\text{sim}} | Δρ (%) |
|-------------|---------------|--------|
| force field of ref 2 | 1297.15 ± 1.8 | 2.71 |
| OPLS | 1250.00 ± 0.3 | -1.02 |
| this work | 1292.28 ± 0.4 | 2.33 |
| literature | 1262.9,53 1262.956 1262.957 | |

“Experimental density at the same state point is ρ_{exp} = 1262.9 kg m^{-3} (ref 52).” The expanded uncertainty (U) is reported at 95% level of confidence.

**Molecular Dipole Moment and Intermolecular Dipole Correlations.** The dipole moment from each force field of a single sulfolane molecule was calculated using the geometry optimized structure obtained from the MP2 level of theory but with charges as prescribed by the respective force field. These values are tabulated in Table 5. The magnitude of the dipole moment from the OPLS force field and that from our force field are within 5% of the MP2 value, while that described in ref 2 is within 10% of the same.

One can expect the significantly large electric dipole moment (Figure 4a) of sulfolane to influence the intermolecular structure and orientation in its liquid phase. As mentioned earlier, MP2 calculations of the single molecule yield a dipole moment value of 5.65 debye (Figure 5a). Despite the fact that sulfolane possesses a gas-phase dipole moment which is significantly higher than that of water (1.85 debye),58 its static dielectric constant is much lesser (43.35) than that of liquid water (76.55 at 303 K) and is comparable to that of dimethyl sulfoxide (DMSO) (4660 at 298 K). The molecular size (volume) of a sulfolane molecule is approximately 101.04 Å^3 per molecule from quantum calculations using Gaussian 16 software.58

![Figure 3. Comparison between densities predicted from this work with those from experiments in the temperature range T = 303−398 K and at pressure p = 1 bar.](https://dx.doi.org/10.1021/acsomega.0c04243)
Details for this calculation are provided in the Supporting Information.

This large molecular volume and hence large intermolecular distances even to the first solvation shell (see the COM−COM pair-correlation function in Figure 4a) limit the extent of intermolecular orientational preferences that can potentially arise from its large dipole moment; the large molecular volume of sulfolane results in smaller dielectric constant in comparison to DMSO1 and water. However, the large dipole moment of sulfolane may possibly be a part of the reason behind its higher dielectric constant in comparison to other polar aprotic solvents.1

Figure 5b shows the combined probability density function (PDF), \( P(r, \cos \theta) \), representing orientational preference and spatial distribution of dipoles of sulfolane molecules around a central sulfolane dipole. Here, \( r \) is the radial distance from the central sulfolane dipole, and \( \theta \) is the angle made between the central dipole and the dipole at \( r \). \( P(r, \cos \theta) \) is averaged over all sulfolane dipoles over a 5 ns trajectory. Figure 5b−d suggests that the orientational effect of a central dipole on its neighboring dipoles is limited; however, a certain degree of antiparallel or near-antiparallel alignment of near neighbor sulfolane molecules is seen. The PDF of dipole orientations for dipoles present between 4.5 and 5.5 Å from a central sulfolane molecule is shown in Figure 5e. Once again, a preference for antiparallel orientations is noticed. The increased intensity between 5.5 and 6 Å in Figure 5b (corresponding to Figure 5f) coincides with the first peak position of the COM−COM pair RDF between the following pairs of atoms at 303 K—(a) COM−COM, (b) SFO−SFO, and (c) OFO−HC1 (intermolecular). (d−f) coordination numbers corresponding to (a−c), respectively. Black—force field of ref 2, red—OPLS, and blue—this work.

**Table 5. Dipole Moment \( p \) (debye) of a Sulfolane Molecule in the Gas Phase Obtained By All Force Fields and Quantum Chemical Calculation**

| description               | \( p \) (debye) | \( \Delta p \) (%) |
|---------------------------|-----------------|-------------------|
| MP2/aug-cc-pvdz            | 5.646           |                   |
| force field of ref 2       | 6.178           | 9.42              |
| OPLS                      | 5.425           | −3.91             |
| this work                 | 5.922           | 4.89              |

“The dipole moment predicted from the refined force field (this work) uses the derived DDEC6 liquid phase charges reported under "This work" in Table 1. The experimentally determined gas-phase dipole moment is 4.69 debye.1 The deviation \( \Delta p \) has been calculated with respect to the MP2/aug-cc-pvdz value.

Figure 4. RDF between the following pairs of atoms at 303 K—(a) COM−COM, (b) SFO−SFO, and (c) OFO−HC1 (intermolecular). (d−f) coordination numbers corresponding to (a−c), respectively. Black—force field of ref 2, red—OPLS, and blue—this work.
correlation function presented in Figure 4a. A weak preference for a parallel orientation with the central sulfolane dipole is seen at these distances. This feature is due to a weak competition in the dipole–dipole interactions of molecules in this region with the central molecule and with molecules in the 4.5 to 5.5 Å region.

We also study \( P(r, \cos \theta) \) as a function of temperature (Figure 6). We find that temperature does not have a significant effect on \( P(r, \cos \theta) \) over the temperature range studied here. This, we speculate, is due to the large dipole moment of sulfolane. However, we see some decrease in the number of sulfolane molecules whose dipoles align antiparallel to the central sulfolane dipole. Also, the various regions of \( P(r, \cos \theta) \) shift marginally to larger distances as a result of the decrease in density with an increase in temperature.

**Heat of Vaporization.** The heat of vaporization provides a good estimate of the strength of intermolecular interactions present in any liquid. Assuming ideality in the gas phase, it is defined as \( \Delta H_{vap} = E_{\text{gas}} - E_{\text{liq}} + RT \), where \( \Delta H_{vap} \) is the heat of vaporization, \( E_{\text{gas}} \) is the average total energy of a sulfolane molecule in the gas phase, \( E_{\text{liq}} \) is the average total energy per molecule in the liquid phase, \( R \) is the universal gas constant, and \( T \) is temperature. The mean heat of vaporization of liquid sulfolane at 303 K was calculated from three independent single-molecule gas phase NVT calculations \( (E_{\text{gas}}) \) \( (N_{\text{sample}} = 3) \) and from a common single realization of \( E_{\text{liq}} \) for each force field. Details are provided in the Supporting Information.

All the force fields yield heat of vaporization within 11% of the experiment (Table 6).

**Surface Tension.** Details of calculation of surface tension are provided in the Supporting Information. The surface tension data estimated from all the force fields, including the one presented here, are presented in Table 7. Surface tension data in the literature seems to vary greatly from one experimental report to another. Thus, we desisted from calculating it as a function of temperature and limited ourselves to ambient conditions.

**Shear Viscosity.** Another crucial transport property to validate the transport properties obtained through the force field is shear viscosity. We calculate it from the off-diagonal components of the pressure tensor from equilibrium MD simulations. The stress–stress time correlation function and the shear viscosity derived therefrom are calculated according to the Green–Kubo method in a manner similar to ref 65. The Green–Kubo expression used for viscosity calculation is provided in the Supporting Information eq S1. An example for the pressure tensor correlation function in time is shown in Figure S4. Further details of the calculation are provided in the Supporting Information.

The viscosity predicted by the current force field compares very well with the experimental value. The calculation of uncertainty \( U \) on the reported viscosity (Table 8 and Figure 7) obtained from block averaging was obtained in a manner very similar to that of density.

We have also calculated the shear viscosity of liquid sulfolane at different temperatures and found that the calculated

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**Table 6. Heat of Vaporization \( \Delta H \) (kJ·mol\(^{-1}\)) Obtained Using Force Fields at Temperature \( T = 303 \) K and Pressure \( p = 1 \) bar\(^{a}\)**

| force field       | \( \Delta H_{vap,exp} \) (kJ·mol\(^{-1}\)) | \( \Delta(\Delta H_{vap}) \) (%) |
|-------------------|--------------------------------------------|---------------------------------|
| force field of ref 2 | 67.05 ± 0.17                              | 0.48                            |
| OPLS              | 60.71 ± 0.24                               | -9.02                           |
| this work         | 59.43 ± 0.27                               | -10.94                          |

\(^{a}\) The experimental value using the Clapeyron and Cox equations is 66.73 kJ·mol\(^{-1}\). \(^{b}\) The expanded uncertainty \( (U) \) is reported at 95% level of confidence.

**Table 7. Surface Tension \( \gamma \) (mN·m\(^{-1}\)) of Liquid Sulfolane at Temperature \( T = 303 \) K and Pressure \( p = 1 \) bar Calculated Using Different Force Fields\(^{a}\)**

| force field       | \( \gamma \) (mN·m\(^{-1}\)) | \( \Delta(\gamma) \) (%) |
|-------------------|-------------------------------|--------------------------|
| force field of ref 2 | 53.43 ± 4.6                  | 50.51                    |
| OPLS              | 45.50 ± 1.6                   | 28.17                    |
| this work         | 34.62 ± 0.5                   | -2.48                    |
| literature        | 35.5±3.6                      | -35.6                     |

\(^{a}\) The expanded uncertainty \( (U) \) is reported at 95% level of confidence. https://m.chemicalbook.com/ChemicalProductProperty_DE_cb3852996.htm.
Table 8. Shear Viscosity \( \eta \) (mPa·s) Estimated by All Force Fields at Temperature \( T = 303 \) K, and Pressure \( p = 1 \) bar

| force field | \( \eta/\text{mPa} \cdot \text{s} \) | \( \Delta \eta \) (%) |
|-------------|----------------|----------------|
| force field of ref 2 | not estimable within 25 ns run | not estimable |
| OPLS | 20.47 ± 0.04 | 99.05 |
| this work | 11.43 ± 0.15 | 10.02 |
| literature | 10.228\textsuperscript{\text{a}}, \textsuperscript{\text{b}} | 10.05\textsuperscript{\text{b}} |
| | 10.30\textsuperscript{\text{c}}, \textsuperscript{\text{d}} | 10.74\textsuperscript{\text{c}} |
| | 10.40\textsuperscript{10\text{c}} |

\( \text{a} \)Experimentally determined value of shear viscosity is 10.284 mPa·s. \( \text{b} \)The expanded uncertainty (\( U \)) is reported at 95% level of confidence.

Figure 7. Running integral for shear viscosity of liquid sulfolane estimated from the OPLS force field and from the current work at temperature \( T = 303 \) K and pressure \( p = 1 \) bar. The dashed line is drawn at an experimental value of 10.284 mPa·s\( \text{a}\) for comparison.

Table 9. Comparison between the Shear Viscosity of Liquid Sulfolane Calculated Using the Force Field Reported Here, \( \eta_{\text{this work}} \) (mPa·s), with That Reported in Experiments \( \eta_{\text{exp}} \) (mPa·s) in the Temperature Range \( T = (303–398) \) K, and at Pressure \( p = 1 \) bar

| temperature/K | \( \eta_{\text{this work}} \) \( \pm \) \% | \( \eta_{\text{exp}} \) \( \pm \) \% | \( \Delta \eta \) (%) |
|---------------|----------------|----------------|----------------|
| 303 | 11.43 ± 0.15 | 10.284\textsuperscript{4} | 10.02 |
| 323 | 6.53 ± 0.03 | 6.312\textsuperscript{4} | 3.45 |
| 348 | 5.25 ± 0.03 | 3.846\textsuperscript{4} | 36.50 |
| 373 | 2.05 ± 0.02 | 2.57\textsuperscript{4} | −20.23 |
| 398 | 1.59 ± 0.04 | 1.835\textsuperscript{4} | −13.35 |

\( \Delta \eta \) is calculated with respect to the experimental value. \( \text{b} \)The expanded uncertainty (\( U \)) is reported at 95% level of confidence. The data follows the Vogel–Fulcher–Tammann (VFT) equation, \( \eta = \eta_0 e^{B/T−C} \), where \( \eta_0 = 0.0026 \) mPa·s, \( B = 2554.6092 \) K, and \( T_\text{VFT} = 0.0 \) K. Since, in the present case, the VFT equation reduces to the Arrhenius equation, the activation energy obtained from an Arrhenius fit is 21.24 kJ·mol\(^{-1}\).

Self-Diffusion Coefficient. The self-diffusion coefficient of sulfolane was calculated from the mean squared displacement (MSD). Reliable measurements of the experimental diffusion coefficient were not found in the literature. Thus, we estimated it by a linear extrapolation of the experimentally reported diffusivity of sulfolane in solutions of varying concentrations of LiBF\(_4\) to zero concentration of LiBF\(_4\) at 303 K. The diffusion constant obtained through this procedure is \( 14.72 \times 10\text{−11} \) m\(^2\)·s\(^{-1}\) and is herein considered as the experimental diffusion constant, against which values from different force fields are compared. Constant NVT simulations of duration 50 ns at the equilibrated density were used to calculate the MSD for the OPLS force field and for the refined force field (see Figure 9). The smallest time interval for which MSD was calculated was 1 ps. The diffusive regime was determined from the time point, and the exponent \( \beta(t) \) defined in the Supporting Information (see \( \text{Figure 8} \)) reaches unity (2 to 26 ns). Further details of the calculation are provided in the Supporting Information.

The diffusion coefficients (\( D \)) are calculated as shown in Figure 9. \( \beta(t) \) for sulfolane in each force field considered is shown in the Supporting Information (see Figure S6). The self-diffusion coefficients (\( D \)) are calculated in Table 10. The diffusion constant from the refined force field developed here is closest to the experimental value.

We also calculated the self-diffusion coefficient of sulfolane as a function of temperature. The results are provided in Table 11 and Figure 10. Experimental self-diffusion constants were not found in the literature for comparison.

Table 10. Self Diffusion Coefficient \( D \) (m\(^2\)·s\(^{-1}\)) of Liquid Sulfolane Estimated From Simulations Using the Three Force Fields, at Temperature \( T = 303 \) K and Pressure \( p = 1 \) bar

| force field | \( D/10\text{−11} \text{m}^2\text{·s}^{-1} \) | \( \Delta D \) (%) |
|-------------|----------------|----------------|
| force field of ref 2 | 0.06 ± 0.001 | −99.59 |
| OPLS | 7.12 ± 0.08 | −51.63 |
| this work | 11.89 ± 0.4 | −19.16 |

\( \text{a} \)Experimentally determined value of diffusion constant obtained through extrapolation from data in ref 2 is \( 14.72 \times 10\text{−11} \) m\(^2\)·s\(^{-1}\). \( \text{b} \)The expanded uncertainty (\( U \)) is reported at 95% level of confidence.
Table 11. Self-Diffusion Coefficient of Liquid Sulfolane as a Function of Temperature as Predicted from This Work, $D$

| temperature/K | $D/10^{-11}$ m$^2$ s$^{-1/2}$ |
|---------------|-------------------------------|
| 303           | $11.89 \pm 0.4$               |
| 323           | $22.33 \pm 0.5$               |
| 348           | $40.83 \pm 0.7$               |
| 373           | $65.77 \pm 1.2$               |
| 398           | $103.38 \pm 1.3$              |

"The expanded uncertainty ($U$) is reported at 95% level of confidence. The data follows an exponential fit of the form: $D = A e^{-E_a/kT}$. Where activation energy $E_a = 22.60$ kJ mol$^{-1}$ and $A = 97372.59 \times 10^{-11}$ m$^2$ s$^{-1}$."

**Figure 10.** Self-diffusion coefficients of liquid sulfolane as a function of temperature in the range $T = (303–398)$ K.

### CONCLUSIONS

In this work, the need for a force field that quantitatively captures the transport properties of liquid sulfolane has been met. In order to achieve this, average atomic site charges were derived for the liquid phase of sulfolane using periodic DFT calculations and the DDEC6 method for partitioning the electronic density into atomic site charges. Narrow atomic site charge distributions in the liquid allowed for obtaining site charges through DFT geometry optimizations of independent snapshots chosen from a MD trajectory.

A modification of charges necessitates a refinement of LJ parameters as well. Thus, chemically different atom types were identified, and their LJ-parameters were tuned so that the total potential energy of a pair of sulfolane molecules as a function of their intermolecular distance calculated within the refined force field matches that obtained from reference quantum chemical calculations as closely as possible. Lastly, we also modified the equilibrium bond length and bond angles to those obtained from gas-phase quantum chemical optimization of a sulfolane molecule.

Although our force field is a non-polarizable one, the values predicted by our force field for several physical and chemical properties such as molecular dipole moment, liquid density, viscosity, self-diffusion coefficient, and surface tension quantitatively matching the experimental data to a fair extent with the benefit of having computed them with much lesser computational cost as compared to simulations using ab-initio MD methods or with polarizable force fields. In particular, we stress on the remarkable agreement of self-diffusion coefficient and shear viscosity of this refined force field with experiments since reproducing transport quantities from non-polarizable force fields has always posed a challenge.69 We notice that the match of density and heat of vaporization from the refined force field with experiments is not as good as that for transport properties and surface tension. However, among other force fields studied here, the refined force field parameters reported here yield the closest match to the quantum PES scans. Also, the rigorous method used for derivation of atomic site charges within the liquid phase of sulfolane reinforces our faith in the reliability of the refined force field, particularly for transport properties. A temperature-dependent study of several physical quantities yielded results in quantitative agreement with experiments. This increased the reliability of this refined force field. The near-neighbor structure in liquid sulfolane is characterized by antiparallel arrangement of molecular dipoles.

Several qualitative predictions regarding sulfolane-assisted reactions and its viability as an emerging battery electrolyte component can now be made with fair certainty. It is also interesting to note that the refined force field for sulfolane may be applicable to the entire class of sulfone compounds with minor modifications. To investigate along these various lines using this refined force field is our future objective.

### ASSOCIATED CONTENT

#### Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsomega.0c04243.

Determination of gas-phase DDEC6 charges; charge distribution obtained in liquid-phase DDEC6 charge calculation; bonded parameters; additional MD details; example of block average calculation: illustrated via density; additional RDF plots; details for single-molecule volume calculation; uncertainty calculation for heat of vaporization; calculation of surface tension; shear viscosity Green–Kubo relation; pressure tensor time correlation function; calculation of mean shear viscosity and uncertainty on the mean, defining the diffusive regime; calculation of the mean diffusion constant and uncertainty on the mean (PDF)

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**Notes**

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