Has a \( \pi pK^- \) Signal in \( p+p \) Reactions been Observed Yet?

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Our answer to the question posed in the title is: probably no. In this work we show that it is rather unlikely that the structure \( X(2265) \) reported by the DISTO collaboration corresponds to a kaonic nuclear bound state. The main argumentation is based on the repetition of the DISTO analysis on the HADES data sample, containing \( p+p \) reactions at 3.5 GeV. We further discuss many aspects in connection with the \( pK^+\Lambda \) final state and the \( \Lambda(1405) \)-resonance. The results evidence possible problematic in the interpretation of the DISTO data.

I. THE \( pK^+\Lambda \) FINAL STATE IN \( p+p \) REACTIONS

Since the first measurement of open strangeness production via the reaction

\[ p + p \to p + K^+ + \Lambda \]  

(1)

has been reported\(^1\), many experiments have exclusively measured this final state. Three issues were mainly investigated thereby: the production of \( N^* \) resonances and their subsequent decay into \( K^+\Lambda \)\(^2\),\(^3\),\(^4\), the \( p\Lambda \) final state interaction\(^5\),\(^6\)\(^7\),\(^8\),\(^9\),\(^10\), and the cusp structure appearing at 2.13 GeV in the \( p\Lambda \) invariant mass distribution\(^11\),\(^12\). A fourth aspect was recently added to this list with the investigation of the kaonic nuclear bound state \( \bar{K}NN \) by the DISTO collaboration\(^17\),\(^18\). In this analysis the following scenario has been investigated

\[ p + p \to \pi pK^- + K^+ \]  

(2)

Here, a kaonic nuclear bound state \( \bar{K}NN \), also called \( \pi pK^- \), is produced in \( p+p \) reactions together with a \( K^+ \), and its non-mesonic decay in a \( p\Lambda \) pair has been considered. The aim of this work is to cross-check the claim that the observed structure (named \( X(2265) \)), \( M=2267 \text{ MeV}/c^2 \) and \( \Gamma=118 \text{ MeV} \) in a so-called deviation spectrum of Refs.\(^17\),\(^18\) corresponds to the signature of an intermediate \( \bar{K}NN \) cluster to the final state\(^11\).

In the following, we will explain what a deviation spectrum is, what difficulties arise from this method and why the absence of \( X(2265) \) at lower beam energies is not linked to the absence of \( \Lambda(1405) \) production - which is considered as a doorway for the formation of a \( \bar{K}NN \) state. We will further discuss whether a \( \bar{K}NN \) production strength of 17\% of the total \( pK^+\Lambda \) production cross section at 2.85 GeV, as reported in Ref.\(^2\),\(^3\), is a realistic scenario, given the upper limits for \( X(2265) \) from Ref.\(^2\) and this work. The discussion is completed by summarizing all \( p\Lambda \) mass spectra published so far where no clear signature of \( X(2265) \) or any other kind of \( \pi pK^- \) signal is visible.

II. THE 2.5 GEV AND 2.85 GEV DISCREPANCY

After the publication of the DISTO results on the formation of a \( \pi pK^- \) in \( p+p \) reactions at a beam kinetic energy of 2.85 GeV\(^17\),\(^18\), the same authors have analyzed also a data set measured by DISTO at a beam kinetic energy of 2.5 GeV\(^21\). Despite the expectation, that as much as 33\% of the observed yield of the structure \( X(2265) \) at 2.85 GeV should be visible also at the lower beam energy of 2.5 GeV, no signal appeared in the data. Therefore, an upper limit of 0.2\% of the \( pK^+\Lambda \) production cross section was estimated\(^21\).

A. The depletion of the \( \Lambda(1405) \) yield

The missing signature of \( X(2265) \) at 2.5 GeV was explained by the lower abundance of the \( \Lambda(1405) \)-resonance at this energy which is, according to Refs.\(^14\),\(^20\), a doorway for the formation of the \( \bar{K}NN \) in \( p+p \) reactions\(^22\). The abundance of the \( \Lambda(1405) \)-resonance was, however, only roughly estimated on the base of the missing mass distribution to the proton and \( K^+ \) (\( MM_{pK^+} \)) at 2.85 GeV and 2.5 GeV. In this approach the high mass region of the \( MM_{pK^+} \) spectra, which includes among others the contributions by the \( \Lambda(1405) \) and \( \Sigma(1385) \)\(^0\), was considered and the \( \Lambda(1405) \) production at 2.5 GeV was estimated to be maximally 10\% as for the data set at 2.85 GeV\(^21\). This estimation assumed that first, the statistic in the resonance region of the \( MM_{pK^+} \) spectra measured by DISTO. The second, that the \( \Sigma(1385) \)\(^0 \) to \( \Lambda(1405) \) production ratio is the same for the two energies. The first assumption was disproven by the investigation of the \( \Lambda(1405) \) resonance at a beam energy of 3.5 GeV\(^23\). Indeed in the latter work the individual contributions to the \( MM_{pK^+} \) spectrum were determined and it was found that a substantial contribution stems from the production of the \( \Lambda(1520) pK^+ \), \( \Sigma^+\pi^- pK^+ \), and \( \Delta^{++}(1232) \bar{K}^- K^+ \) final states. While the \( \Lambda(1520) \) production is below threshold at 2.5 GeV (\( E_{kin}(\text{Threshold}) = 2.77 \text{ GeV} \)) and probably small at 2.85 GeV, the other two final states will definitely contribute to the observed yield in the high mass region of the \( MM_{pK^+} \), spectra measured by DISTO. The sec-
The long dashed curve shows the parametrisation scaled down to fit to the two $pK^+\Lambda$ data points and the dotted curve is a free fit of the Fäldt-Wilkin parametrisation to the two points $[23, 25]$. The vertical lines show the scaled curve and 0.3 for the curve based on the free assumption about a constant $\Sigma(1385)^0$ to $\Lambda(1405)$ production ratio is also questionable as the analysis in Ref. $[24]$ showed that at 3.5 GeV this ratio is reduced by about 15% in comparison to the ratio measured by the ANKE collaboration at $E_{kin}=2.83$ GeV $[24]$. Both values have, however, large uncertainties so that it is difficult to extrapolate to lower energies.

We suggest an alternative ansatz to compare the $\Lambda(1405)$ production cross section at the two DISTO energies. In Ref. $[23]$ the energy dependence of the production cross section of the $pK^+\Lambda(1405)$ final state was determined on the base of the values measured in $p+p$ collisions $[23, 25]$. Figure 1 shows a compilation of measured cross sections from the $pK^+\Lambda$ and $pK^+\Lambda^*$ final states versus the excess energy. The two vertical dashed lines mark the excess energy for the $\Lambda(1405)$ production for the two data sets, measured by DISTO (48.8 MeV and 161.2 MeV). The $pK^+\Lambda$ data are well described by a Fäldt and Wilkin parametrisation as done in Refs. $[3, 20]$. By assuming a similar behavior of the two channels close to threshold, we have scaled the $pK^+\Lambda$ curve down so that it fits the data points of the $pK^+\Lambda^*$ final state (long-dashed curve). We did also perform a free fit of the mentioned parametrisation from Refs. $[3, 20]$ to the two data points which also describes them well (dotted curve). With help of the two curves the ratio of the $\Lambda^*$ production cross section between the two DISTO energies was determined to be $\sigma_{pK^+\Lambda(1405)}(2.5\text{GeV})/\sigma_{pK^+\Lambda(1405)}(2.85\text{GeV})=0.23$, for the scaled curve and 0.3 for the curve based on the free fit to the data. The ratios show that the cross section of $\Lambda(1405)$ production at the 2.5 GeV data set is in any case a sizable fraction of that at 2.85 GeV. Following the assumption that the $KNN$ production in $p+p$ collision should proceed through the intermediate formation of a $\Lambda(1405)$, at least 23% of the observed $X(2265)$ yield at 2.85 GeV should be expected at the lower energy.

In fact, the fraction of events affected by the $\Lambda(1405)p$ final state interaction should be even higher at lower energies due to phase space considerations $[11]$. Provided that the hypothesis of the $\Lambda(1405)$ being a doorway for the creation of "$ppK^+\Lambda$" is valid, that would result in an increased number of $KNN$ per $\Lambda(1405)$.

We, thus, argue that the reasoning in Ref. $[21]$ regarding the absence of a $X(2265)$ signal at the 2.5 GeV DISTO data is not convincing as the $\Lambda(1405)$ yield at lower energies is larger than estimated by the authors.

B. The problematic of deviation spectra

To provide a further cross check of the reported results by the DISTO collaboration, we have repeated the analysis of Refs. $[17, 18, 21]$ and produced so-called deviation spectra. The original idea behind this approach was that any measured event distribution in a given observable which deviates from a purely phase space driven production process hints to the presence of a new signal. The deviation spectrum is obtained by dividing the experimental event distribution of an observable by the same simulated distribution obtained by employing phase space simulations of the final state.

The data for this analysis $[10, 27, 29]$ stem from the $p(E_{kin}=3.5\text{GeV})+p$ reaction measured by the high acceptance di-electron spectrometer (HADES) at the SIS18 synchrotron (GSI Helmholtzzentrum in Darmstadt, Germany). For details about the spectrometer and the experiment see Refs. $[10, 30]$. The in the following discussed deviation spectra were obtained by dividing the measured event distribution of the invariant mass distribution of $p-\Lambda$-pairs ($IM_{p\Lambda}$) by the according simulated spectrum. The simulations were performed under the assumption that the three particles in the final state ($\Lambda$, $p$, $p$) are produced via phase space only. The division is performed with measured spectra which means that the data are shown inside of the HADES acceptance and are filtered by the event selection procedure. As the $pK^+\Lambda$ statistic was obtained within two different regions of the spectrometer acceptance (HADES and WALL, see Ref. $[10]$ for details) we present two different deviation spectra in Figs. $[2, 3]$ respectively.

The two figures show several deviation spectra obtained under different data selections. While the red histograms show the deviation spectra for the full statistics as analysed in $[10]$, the long-dashed histogram represents the result after applying the very same cuts as done in the analysis by DISTO: $\cos\theta_p < 0.6$ and $-0.2 < \cos\theta_{K^+} < 0.4$ $[17, 18]$. To point out the impact of such subsequent
FIG. 2. (Color online) Different deviation spectra, obtained by dividing the reconstructed $pK^+\Lambda$ statistic by phase space simulations in the HADES acceptance.

FIG. 3. (Color online) Different deviation spectra, obtained by dividing the reconstructed $pK^+\Lambda$ statistic by phase space simulations in the WALL acceptance.

FIG. 4. (Color online) Different deviation spectra, obtained by dividing the reconstructed $pK^+\Lambda$ statistic by a partial wave analysis model in the HADES acceptance.
of the data by the PWA so that the applied cuts, therefore, act symmetrically on the data and the model.

Summarizing, we have shown that deviation spectra strongly depend on the model to which the data are compared to. If the simulation model is not fully adequate, the applied cuts may distort the deviation spectrum drastically and no reliable conclusions can be drawn. We thus consider this method as suboptimal to look for peak structures. From our perspective it is, thus, not astonishing that a certain structure at 2.85 GeV can not be retrieved at the 2.5 GeV DISTO data set.

III. DEVIATION SPECTRA REVISITED

We want to extend our discussion on deviation spectra to other energies. Indeed, the idea of comparing phase space simulation to experimental data for the Reaction dates back to Ref. There inclusive spectra of the missing mass to the kaon were divided by phase space distributions at different kaon angles and beam kinetic energies. The result of is shown in Figure The deviation spectrum differs from unity in the high missing mass region (the missing mass to the kaon (MMK+) corresponds to the mass of the residue X with which it is produced, e.g. X= pA or ΣNπ). The horizontal gray line indicates the signal range of X(2265). No deviation at $MMK_+ = 2267 \text{MeV}/c^2$ is visible in these data sets. Indeed, the authors of Ref. have investigated the deviations in Figure under the assumption of a di-baryon being produced together with the kaon. They have, however, also considered the fact that the presence of N* resonances in the data might cause the observed deviations from phase space, as was already suggested by an earlier work.

IV. ANY SIGNS OF A LARGE VISIBLE SIGNAL?

Since no X(2265) signal at the 2.5 GeV DISTO data has been found, an upper limit for its production strength of $0.2 \pm 2.1\%$ of the total $pK_+Λ$ production cross section has been estimated. An independent analysis of p+p data measured by HADES has also set an upper limit on the production of a $KNN$ in p+p reactions at $E_{kin}=3.5 \text{GeV}$ . The major difference between the DISTO and the HADES analysis is that in the former case visible bumps in the pΛ invariant mass spectrum were associated to a signal, while the latter analysis is done with help of a partial wave analysis (PWA). In the PWA the amplitude strength of a wave associated to the production of a kaonic nuclear bound state was determined and coherently added to all other contributing waves. These two different approaches prevent, however, a direct comparison of the signal strength and the upper limits. In the best case, a partial wave analysis would be performed on the three data sets simultaneously. For the time being, we have performed a simple incoherent analysis of the data to extract the upper limit of a visible signal strength, in order to be able to compare it consistently to the DISTO results. Such an extracted limit does not necessarily correspond to the real signal strength which is maximally compatible with the data, as interferences with other signals are neglected in this approach.

A. An incoherent upper limit for the $KNN$ production at 3.5 GeV

To carry out this analysis, we have used the acceptance corrected $pΛ$ invariant mass spectrum. The PWA solution from Ref. delivers a model that describes the experimental spectrum well without the inclusion of
a $KNN$ cluster signal. Although the PWA analysis was performed within the detector acceptance, an extrapolation of the solution to the full solid angle is possible. This way, with help of the $4\pi$-model also the measured data can be corrected to the full solid angle. Figure 6 shows the reconstructed experimental data in $4\pi$ overlayed with the PWA solution. To extract an upper limit we have added a Breit-Wigner signal with varying mass, width, and amplitude to the PWA solution (signal hypothesis) and compared the new spectra to the data. We have considered the model compatible with the data, if the confidence level of the signal strength ($CL_s$) was smaller than 95%. Since there are small uncertainties from the acceptance correction (gray error bars in Fig. 6), the upper limit was determined four times. Each time the signal hypothesis was compared to the experimental data which were corrected with one of the four best PWA models of Ref. 10. The resulting upper limit, as a function of the mass of the bound state, is shown in Figure 7 for four different signal widths (30, 50, 70 and 90 MeV/$c^2$). The width of the curves is due to the different upper limits obtained with the four different PWA models. The upper limit of about 0.7 $\mu$b (in the relevant mass range) is below the coherent upper limit of the PWA of Ref. 10 which is consequential, as the interferences included in the PWA may hide the signal which makes it possible to include more signal strength while the spectra stay smooth.

We have also determined an upper limit specifically for the $X(2265)$ properties ($M=2267$ MeV/$c^2$, $\Gamma=118$ MeV/$c^2$) which is 0.3-1 $\mu$b depending on the PWA solution to which the signal is added.

Figure 8 summarizes the observed yield at the DISTO energy of 2.85 GeV, the coherent upper limit from Ref. 10 at 3.5 GeV, the upper limit from the 2.5 GeV DISTO measurement, the here extracted upper limit from the 3.5 GeV HADES data set and the calculated prediction of a production cross section for the $KNN$ cluster of Ref. 37. While the upper limits for a visible signal strength at 2.5 and 3.5 GeV lie apparently below the predictions of Ref. 37 the DISTO value does exceed it by a factor of 4. No clear explanation for the excess with respect to the prediction at this specific energies was made available so far. This means in conclusion that ei-

![Image](https://via.placeholder.com/150)
ther the cross sections for the production of $X(2265)$ has a very strong energy dependence or the observed structure $X(2265)$ is a non-physical signal.

B. Qualitative Observations at Different \(p+p\) Beam Kinetic Energies

Besides the quantitative information discussed in the previous section there are several \(p\Lambda\) invariant mass spectra that have been published in the last years. Figures 9 and 10 contain a compilation of these spectra at various beam kinetic energies. For the production of a state with mass $M=2265\text{MeV}/c^2$ the threshold beam kinetic energy is $E_{K_{in}}=2.18\text{GeV}$. Given the large width of the signal it could also be produced at an energy of $E_{K_{in}}=2.16\text{GeV}$. If the hypothesis is true that a kaonic nuclear cluster is predominantly produced via the $\Lambda(1405)$-doorway scenario [19, 20], the threshold for the production of a $\overline{K}NN$ is $E_{K_{in}}=2.35\text{GeV}$ (respecting the low mass of the $\Lambda(1405)$) in $p+p$ collisions [23].

The here collected spectra give only a qualitative impression of a potentially visible signal, but a strong deviation of the data from the according models in the region of the $X(2265)$-signal (green box) is nevertheless not evident. It seems as if there is no hint for a strong visible signal of $X(2265)$ in any of the available data sets which means that if a signal is present its cross section can only be a small fraction of the total $pK^+\Lambda$ final state.

There are also other measurements at the same energy as the two DISTO data sets. Figure 11 shows the missing mass to the $K^-$ [39] (at $2.85\text{GeV}$, $\theta_{K^-}=17^\circ$) and [33] $(2.54\text{GeV}, \theta_{K^-}=20^\circ)$. The data exhibit no significant structure in the indicated $X(2265)$ signal range. One has to note, however, that these are inclusive spectra of the production of a residue $X_R$ together with a $K^-$. $X_R$ can, depending on the available energy, be composed out of $\Delta p$, $\Lambda N\pi$, $\Sigma N$, and $\Sigma N\pi$. While in an exclusive analysis, as done in the DISTO and HADES cases, $X_R$ is identified with the $p\Lambda$ system, in Fig. 11 all possible decay channels of the kaonic nuclear cluster ($YN$ and $YN\pi$) are summarized. This is on the one hand a disadvantage, as the background description for the sum of several channels is more difficult than in an exclusive analysis, on the other hand, however, this inclusive analysis would compensate for a small branching ratio of a $\overline{K}NN$ in the $p\Lambda$ channel and a signal would thus nevertheless appear in Fig. 11 if kaonic bound states were produced with a large cross section. Under the assumption of a smooth background underneath the signal this is obviously not the case for both data sets. So that also from this point of view it seems that a visible signal by a $\overline{K}NN$ cluster is not present in the data.

There is one last data set at $2.83\text{GeV}$, taken by the ANKE collaboration, which contains exclusive $pK^+\Lambda$ events. Although a proposal had been set up for the analysis of the data with respect to the $\overline{K}NN$ cluster [40], it has not been pursued so far. These are probably the only data whose analysis can quickly resolve the question whether $X(2265)$ is due to a physical origin or not.

V. CONCLUSIONS

We have summarized all available experimental measurements of $p+p$ collisions relevant for the search of the lightest kaonic nuclear bound state ”$ppK^-$” to cross check the hypothesis that the signal $X(2265)$, reported by the DISTO collaboration, can be associated to a kaonic nuclear bound state $\overline{K}NN$. The signal is missing at low ($E_{K_{in}}<2.85\text{GeV}$) and high ($E_{K_{in}}>2.85\text{GeV}$) beam kinetic energies. Its absence can not be explained by a depletion of the $\Lambda(1405)$ yield as was explained with help of Figure 11. The upper limits for the production cross section of $X(2265)$ set at $2.5$ and $3.5\text{GeV}$ suggest that its contribution to the total $pK^+\Lambda$ production cross section is only a few percent.

The strongest argument against the argued nature of $X(2265)$ comes from the method with which the signal was extracted. The deviation spectrum technique to search for a new signal is not applicable, if the employed model is not under firm control and if the applied cuts arbitrarily influence the outcome of the spectra.

We do, thus, think that the structure $X(2265)$ is very unlikely to be due to a kaonic nuclear bound state. On the other hand, the extracted upper limits are still rather sizable and in the order of the predicted yield in Ref. [37]. This calls for new and high statistic experiments to measure the $pK^+\Lambda$ final state, possibly also employing polarization, and their subsequent analysis with modern techniques such as a partial wave analysis [10]. The best data set so far for such an analysis is indeed the one measured by DISTO with $400,000$ $pK^+\Lambda$ events ($2.85\text{GeV}$). Given the fact that $N^*$ resonances do play a dominant role in the $pK^+\Lambda$ final state and given the fact that one data set is not enough to pursue a partial wave analysis with a unique solution as shown in Ref. [10], we call for a simultaneous analysis of all available $pK^+\Lambda$ data sets to finally pin down the issue of $\overline{K}NN$ production in $p+p$ collisions.

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In this view the Λ(1405), being partially a pK- bound state, forms together with a proton a KNN by final state interaction.
FIG. 9. The upper row shows measurements from the COSY-TOF Collaboration at two different beam kinetic energies [16]. The data are compared to phase space simulations indicated in yellow. The lower row shows also data from the COSY-TOF Collaboration at slightly higher beam kinetic energies [8]. The measured data are compared to a model that includes N*-resonances and final-state interaction. The green boxes mark the range of the $X(2265)$ signal $(M \pm \Gamma/2)$.

FIG. 10. The tree figures show data at a higher $E_{\text{Kin}}$ than used for the DISTO data sets. The left figure shows data measured by FOPI [38]. They are compared to solutions from a partial wave analysis. The middle figure shows data from the Brookhaven bubble chamber [2]. The data are compared to a model of phase space and one-pion exchange. The right figure shows data from the LRL bubble-chamber experiment where the data are compared to phase space simulations and kinematic reflections [3]. The green boxes mark the range of the $X(2265)$ signal $(M \pm \Gamma/2)$. 
FIG. 11. Two data sets of the missing mass to the $K^+$ at beam kinetic energies of 2.85 GeV, $\theta_{K^+} = 17^\circ$ (upper) and 2.54 GeV, $\theta_{K^+} = 20^\circ$ (lower) [14]. The green box marks the range of the $X(2265)$ signal ($M \pm \Gamma/2$).