Extremely High Thermal Conductivity of Aligned Carbon Nanotube-Polyethylene Composites

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The ultra-low thermal conductivity of bulk polymers may be enhanced by combining them with high thermal conductivity materials such as carbon nanotubes. Different from random doping, we find that the aligned carbon nanotube-polyethylene composites has a high thermal conductivity by non-equilibrium molecular dynamics simulations. The analyses indicate that the aligned composite not only take advantage of the high thermal conduction of carbon nanotubes, but enhance thermal conduction of polyethylene chains.

Polymers have been widely utilized in all walks of life due to their outstanding physical properties, such as high toughness, low density, and corrosion resistance. However, its poor heat transfer ability limits its applications\textsuperscript{1,2}. The ultra-low thermal conductivities ($\kappa$), on the order of 0.1 Wm$^{-1}$K$^{-1}$ at room temperature\textsuperscript{3}, comes from the structures of random and twisting chains which cause a lot of phonon scatterings and leads to a short phonon mean free path.

Recently, it is reported that a suspended polymer chain and oriented polymer chains have remarkable thermal conductivities\textsuperscript{4–9}. Chen's group predicted that the thermal conductivity of a suspended polyethylene chain (SPEC), $\kappa_{\text{SPEC}}$, achieved as high as 350 Wm$^{-1}$K$^{-1}$ at room temperature by molecular dynamics (MD) simulation\textsuperscript{4,5}. Moreover, they measured the thermal conductivity of ultra-drawn polyethylene (PE) nanofibers, $\kappa_{\text{PE}}$, as 104 Wm$^{-1}$K$^{-1}$ using the cantilever method\textsuperscript{6}. Besides, Virendra et al. measured the $\kappa$ of amorphous polythiophene nanofibers as 4.4 Wm$^{-1}$K$^{-1}$ at room-temperature and calculated $\kappa$ as 43.3 Wm$^{-1}$K$^{-1}$ by MD for a suspended polythiophene chain\textsuperscript{7}. Moreover, Zhang et al. demonstrated that a high thermal conductivity and good stability could be achieved in polymers with rigid backbones\textsuperscript{8}. However, it is quite difficult to take advantage of a single polymer chain in bulk structures.

Another way to enhance thermal property of polymer structure is to produce polymer/carbon nanotube composites. The carbon nanotube (CNT) has been well studied since its discovery in 1991\textsuperscript{10,11}. It is found that CNT has a super-high thermal conductivity on the order of 1000 Wm$^{-1}$K$^{-1}$ at room temperature\textsuperscript{12}. Some efforts have been made in fabricating polymer/CNT composites which have both a better thermal transport properties than bulk polymer\textsuperscript{13–25}. However, the interfacial thermal resistance between CNT and polymer obstructs a further enhancement in thermal transport\textsuperscript{23,26,27}. It was suggested that a strong coupling between CNTs and polymers could reduce phonon scatterings at interfaces and effectively improve the thermal transport in composites\textsuperscript{26,27}.

In order to further enhance thermal properties of PE composites, we investigated numerically the thermal conductivity of aligned carbon nanotube-polyethylene composites (ACPCs) in this paper.
(structure shown in Fig. 1(a)). Here, the well-studied (10, 10) single-walled carbon nanotube (SWCNT) and PE chains are chosen. The ACPC structure is based on a SWCNT array system, and PE chains are aligned with SWCNTs, which will avoid both disordered and interfacial phonon scatterings existed in amorphous PE composites. In the following, we show firstly a description of the model and simulation procedures. Secondly, we discuss simulation results and analyze mechanism. The results show that the non-bonded interactions between the parallel-aligned SWCNT and PE chains could enhance significantly the thermal conductivity of PE chains. Our study may inspire productions and measurements of aligned carbon nanotube and polymer-based composites.

Results and Discussions

The main results are shown in Fig. 2 which includes the thermal conductivities of a suspended SWCNT, a SPEC, and several ACPCs with different structures. The value of $\kappa_{\text{SWCNT}}$ reaches 155 Wm$^{-1}$ K$^{-1}$ when the length of the SWCNT is 160 nm. Obviously, the $\kappa$ of (10, 10) SWCNT is not converged and will keep diverging as its length increases. Our result is slightly smaller than previous reported simulation results, due to the difference of empirical potential. The simplified Morse potential neglects some interactions within the SWCNT, such as dihedral and van der Waals interactions. That is, our result is conservative and undervalue the $\kappa_{\text{SWCNT}}$ a little.

Similarly, the thermal conductivity of a SPEC also shows a strong length dependence. The $\kappa_{\text{SPEC}}$ achieves 57 Wm$^{-1}$ K$^{-1}$ with a length of 160 nm at room temperature. Compared with previous simulation results, our result is less than the Hu's, 104 Wm$^{-1}$ K$^{-1}$ at 160 nm length, and a little higher than the Zhang's, 49 Wm$^{-1}$ K$^{-1}$ with at 50 nm length. The discrepancy between them is chiefly derived from the different models used for the PE chain. Such as, a simplified model of a PE chain is applied in Hu's simulations, where methylene (CH$_2$) groups are regarded as united atoms. Moreover, in Zhang's work, a different potential (COMPASS) is used to model the PE chain. As a SPEC possesses a much higher thermal conductivity than that of an amorphous bulk PE, we will take advantage of this property in enhancing the $\kappa$ of PE-based materials.

The most significant finding is that the thermal conductivities of ACPCs are not only three orders higher than the bulk PE, but almost twice as large as a SPEC. That is, the $\kappa$ of PE composite is greatly enhanced by the SWCNT’s reinforcement. In our simulations, the maximum value of $\kappa_{\text{ACPC}}$ is 99.5 Wm$^{-1}$ K$^{-1}$ for an ACPC 3–8 with a length of 320 nm, which is comparable to that of measurements in ultra-drawn PE nanofibers, around 104 Wm$^{-1}$ K$^{-1}$. Moreover, the $\kappa_{\text{ACPC}}$ is just limited by the simulation cell's length and could reach a much more higher value with the increasing of length due to the divergence behavior of $\kappa$ in low dimensional structures. Furthermore, there are few reports on polymer composites with such a
high thermal conductivity and the $\kappa_{\text{ACPC}}$ is at least 30 times higher than the reported $\kappa$ of CNT-polymer composites. As mentioned in the introduction, in the work by Virendra et al. the measured $\kappa$ of chain-oriented amorphous polythiophene nanofibers is about one-tenth of the MD calculated $\kappa$ of a suspended polythiophene chain at room-temperature. Besides, in the work by Chen's group, the measured $\kappa$ of ultra-drawn PE nanofibers is about one-third of the MD calculated $\kappa$ of a SPEC. Thus, estimated by previous works, we would predict that the measured $\kappa$ of the ACPCs is in a scope from 10 to 33 Wm$^{-1}$K$^{-1}$ based on current fabricating technologies.

The high thermal conductivity of ACPC attributes to three mechanisms. Firstly, the SWCNTs possess a high thermal conductivity, which contributes a lot in enhancing the thermal conductivity of the PE-based composites. Secondly, instead of random doping, the SWCNTs are aligned with PE chains, which is the most important factor. The aligned structures not only take advantage of the divergent $\kappa$ of PE chains with length, but avoid the interface scattering issue between SWCNTs and PE chains in composites. Thirdly, it was found that the non-bonded interactions between the SWCNTs and PE chains also have a significantly positive effect on the thermal transport in ACPCs. The van der Waals forces between the SWCNTs and PE chains hinder vibrations, inducing a crystal-like structure in the PE chains. Hence, the thermal conductivity of the PE chains within an ACPC is improved by the SWCNT interactions to become even higher than that of a SPEC.

Besides the length dependence, the thermal conductivity of ACPC also depends on the number of chains inside SWCNTs, M (shown in Fig. 2). As the number M increases, the $\kappa_{\text{ACPC}}$ first increases and then decreases. A maximum value of thermal conductivity was observed when there are three PE chains inside SWCNTs. Due to the space limitation inside a SWCNT, the van der Waals interactions increase with an increasing number of PE chains within a SWCNT. The van der Waals interactions could take two competitive effects. When 3 or fewer chains are placed inside the SWCNT, there is a slight van der Waals interaction which can suppress the transversal bending of chains and enhance the heat transfer. However, when M is above 3, stronger interactions will bring more phonon scatterings which decrease the thermal conductivity.

In the following, we show a further analysis of the mechanism in the thermal conductivity enhancement of PE chains within an ACPC. As shown in superimposed images (inserts of Fig. 3), the PE chains within ACPC 3–12 have a clear crystalline structure compared with the SPEC. Accordingly, shown in Fig. 3, the radius density profile, g(r), of a SPEC appears amorphous, suggesting a large spread of atom vibrations and many segmental rotations of chain. In contrast, the g(r) of a PE chain within ACPC 3–12 has clear peaks and valleys, corresponding to a more ordered crystal lattice. That is, the van der Waals forces in ACPC make PE chains crystal-like and reduce disorder phonon scatterings survived in suspended chain.

We keep analyzing the details of the enhancement of thermal conductivity by ACPCs. In Fig. 4(a), it shows that the thermal conductivity of 20 nm ACPC 3-N changes a little on No. of PE chains outside the SWCNT (N). A maximum value of 63.7 Wm$^{-1}$K$^{-1}$ was obtained for the ACPC 3-N thermal conductivity when N is 8. Besides, we pick up the heat flux (J) of PE chains alone in ACPCs. The thermal conductance is defined as $\text{G} = \kappa A/L = -J/\Delta T$, where $\kappa$, A, and L are the thermal conductivity, cross-section area, and length, respectively. The thermal conductance of PE chains in ACPCs (the blue circles) is compared with that of a 20nm SPEC (blue dashed line) shown in Fig. 4(a). It shows that there is a significant enhancement in the thermal conductance of PE chains in the ACPCs. The $G_{\text{PE}}$ of ACPC 3–4 is around...
four times larger than G of SPEC, since the non-bonding interactions in ACPC make a more crystal-like PE structure. That is, the high $\kappa$ of ACPC comes from not only SWCNT but the PE chains.

Fig. 4(b) shows the thermal conductivity of ACPCs versus PE content for ACPC M-12 and 3-N structures. With increasing PE content, the thermal conductivity of ACPCs does not decrease monotonically, although $\kappa_{PE}$ is much smaller than $\kappa_{SWCNT}$. For example, the thermal conductivity of 20 nm ACPC 3-N is not sensitive to the increase of PE content. For the 20 nm and 40 nm ACPC M-12, an increase is observed when the PE content increase from 19.5% to 22%. Therefore, the PE chains in ACPCs do account for a significant contribution in thermal transport.
Moreover, Fig. 4(c) shows the contribution of PE chains and SWCNT to thermal conductance of ACPC 3–8 and ACPC 3–4 with 80 nm in length. It shows that the PE chains contribute a considerable percentage of the total thermal transport, 36.4% (27.8%) for ACPC 3–8 (3–4). Both the G values of SWCNTs in ACPC 3–4 (22.6 × 10^{-10} W K^{-1}) and ACPC 3–8 (23.86 × 10^{-10} W K^{-1}) are smaller than that of a suspended 80 nm SWCNT (26.32 × 10^{-10} W K^{-1}) due to the scattering from non-bonding interactions in ACPC. The values of thermal conductance per PE chain inside and outside the SWCNT in ACPC 3–8 and 3–4 are shown in Fig. 4(d). Compared with an 80 nm SPEC, the G value per PE chain is improved by as large as 38.5% for chains inside SWCNT in ACPC 3–8. That is, the non-bonded interactions in ACPCs enhance the thermal transport of the PE considerably, about 23% on average.

Conclusions
We propose a new composite model as aligned carbon nanotube-polyethylene composites, namely ACPCs. The thermal conductivity (κ) of ACPCs are studied by non-equilibrium molecular dynamics simulations. The most significant finding is that the thermal conductivities of ACPCs are not only three orders higher than the bulk PE, but almost twice as large as a suspended PE chain which is well known by its high κ. The κ_{ACPC} is also at least 30 times higher than the κ of other reported CNT-polymer composites. Besides, there is a large enhancement (~23%) of thermal conduction for PE chains in ACPCs even comparing with a suspended PE chain. So that, the PE chains have a considerable contribution (~30%) to the thermal transport in ACPCs.

The high thermal conductivity of ACPCs attributes to the high thermal conductivity SWCNTs, the aligned SWCNTs with PE chains, and the non-bonded interactions between SWCNTs and PE chains. Our predictions may inspire manufacturing aligned polymer-based composites for a wide variety of applications.

Methods
Classical non-equilibrium molecular dynamics (NEMD) simulations are used to study the thermal conductivity of the SWCNT, the SPEC and the ACPC. All simulations are performed by the large-scale atomic/molecular massively parallel simulator (LAMMPS) package\(^4^4\). The temperatures of the heat source and heat sink are set at 310 K and 290 K, respectively. The fixed boundary condition is applied in the longitudinal direction and the periodic boundary conditions are applied in the two transversal directions. The cross-section of ACPC simulation cell after relaxation spreads from 400 to 500 Å\(^2\) which depends on the structure of ACPC.

The potential energy of the SWCNT is described by a Morse bond and a harmonic cosine angle for bonding interactions, which includes both the two-body and three-body potential terms\(^35^–37\). The atomic interactions of PE chains are described by an adaptive intermolecular reactive empirical bond order (AIREBO) potential\(^38\), which is developed from the second-generation Brenner potential\(^39\). In addition, the non-bonded interactions between the SWCNT and PE are described by the Lennard-Jones potential:

\[
V_{\text{LJ}}(r_{ij}) = 4\varepsilon \left[ \left( \frac{\sigma}{r_{ij}} \right)^{12} - \left( \frac{\sigma}{r_{ij}} \right)^{6} \right]
\]

where \(\varepsilon\) is the depth of the potential well, \(r_{ij}\) is the distance between atom i and j. The Lennard-Jones parameters are \(\sigma_{\text{SC-PC}} = 3\) Å, \(\varepsilon_{\text{SC-PC}} = 0.0028\) eV, \(\sigma_{\text{PC-PH}} = 3.025\) Å, and \(\varepsilon_{\text{PC-PH}} = 0.0021\) eV; the SC, PC, and PH subscripts represent the carbon atoms within the SWCNT, the carbon atoms within the PE chains, and the hydrogen atoms within the PE chains, respectively. Additionally, an 8.5 Å cutoff distance is used for the 12–6 Lennard-Jones interaction.

Fig. 1(a) shows the typically perspective view of initial positions of ACPC 3–8. The basic cell of the ACPC, which is based on a SWCNT array system, is chosen as the simulation domain to calculate the thermal conductivity for bulk materials by periodic boundary conditions. After the relaxation, the final structures of ACPC 1–12 and 3–12 are shown in Fig. 1(b,c), respectively. Moreover, several different ACPC structures are taken into consideration. We named ACPC M-N as the structure which have M PE chains inside the SWCNT and N chains outside the SWCNT. Fig. 1(d) shows a typical setup and the corresponding temperature profile. The simulation system is divided into 20 or 50 slabs according to the length\(^40\). The motion equations are integrated by the velocity Verlet algorithm with a time step of 0.2 fs.

In calculations of thermal conductivity, it is based on Fourier’s law, \(\kappa = -J/(A \cdot \nabla T)\), where J is heat flux, A is cross-section area, and T is temperature. The cross-section of (10, 10) SWCNT is defined as a ring with 3.4 Å in thick\(^41\). Besides, the cross-sectional area of a PE chain is taken as 18 Å\(^2\)\(^4\). The NEMD method has been detailed in the Ref. 42.

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Acknowledgements
This project was supported in part by the National Natural Science Foundation of China: 51376069 (Z.L.) and 51576076 (N.Y.), and the Major State Basic Research Development Program of China No. 2013CB228302 (Z.L.). The work was performed at the National Supercomputer Center in Tianjin and the calculations were performed on TianHe-1(A).

Author Contributions
Q.L. carried out the MD calculations. Z.L., W.L., and N.Y. supervised the research. All authors analyzed the calculation data and edited the manuscript.

Additional Information
Competing financial interests: The authors declare no competing financial interests.

How to cite this article: Liao, Q. et al. Extremely High Thermal Conductivity of Aligned Carbon Nanotube-Polyethylene Composites. Sci. Rep. 5, 16543; doi: 10.1038/srep16543 (2015).

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