Anomalous capillary filling and wettability reversal in nanochannels

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This work revisits capillary filling dynamics in the regime of nanometric to subnanometric channels. Using molecular dynamics simulations of water in carbon nanotubes, we show that for tube radii below one nanometer, both the filling velocity and the Jurin rise vary non-monotonically with the tube radius. Strikingly, with fixed chemical surface properties, this leads to confinement-induced reversal of the tube wettability from hydrophilic to hydrophobic for specific values of the radius. By comparing with a model liquid metal, we show that these effects are not specific to water. Using complementary data from slit channels, we then show that they can be described using the disjoining pressure associated with the liquid structuring in confinement. This breakdown of the standard continuum framework is of main importance in the context of capillary effects in nanoporous media, with potential interests ranging from membrane selectivity to mechanical energy storage.

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I. INTRODUCTION

Capillary rise is a standard phenomenon of fluid transport, coupling capillarity to hydrodynamics [1–3]. In view of its importance for many applications, this phenomenon has been thoroughly investigated for more than an century [4–6]. Yet it still raises many questions, as a growing number of situations of interest now concern capillary effects arising in nanometric to subnanometric channels [3, 7–14]. This is associated with the fast development of nanofluidics [15] and the renewed activities around membranes and nanoporous media arising from water resources or energy problems. At such scales new behaviors are expected [15–17], which jeopardize the standard treatment of capillary filling dynamics. This might be due to a breakdown of continuum hydrodynamics when approaching the liquid molecular scale [18, 19], the onset of dominant slip effects [20], or increasingly important deviations in interfacial properties [21–26] arising from the molecular structuring of ultra-confined liquids [27].

In order to unveil some specificities of molecular scale capillary effects, we revisit in this contribution the classic problem of capillary filling in nanometric to subnanometric channels. Using molecular dynamics (MD) simulations, we focus on carbon nanotubes (CNTs) as a model confining system and on water as a representative liquid. Overall, we observe significant deviations from standard continuum predictions for tubes with diameters as large as 3 nm. In particular, for specific radii the fluid is expelled from the pore, in contrast with standard predictions. These remarkable behaviors are attributed to liquid structuring effects, which are able to reverse the effective wettability of the channel for a given system chemistry. Additional simulations with a model liquid metal show that the anomalous capillary filling and the wettability reversal are not specific to water, which behaves as a simple liquid in that particular situation. Complementing these results with slit-geometries simulations, we then show that these deviations from the standard continuum framework can be captured by the disjoining pressure, usually introduced to account for fluid structuring in the context of homogeneous films. Finally we discuss the consequences of this work for applications involving nanoporous media.

II. STANDARD CONTINUUM DESCRIPTION

We consider the capillary filling of a CNT (radius $a$, length $H$) with water (density $\rho$, viscosity $\eta$), see Fig. 1. The liquid surface tension is denoted $\gamma$, the contact...
angle of the liquid on the solid $\theta$, and the length of the liquid column inside the tube $L$. The driving force for capillary filling is the Laplace pressure jump through the liquid/vapor meniscus at the extremity of the liquid column, which writes:

$$\Delta p_{\text{men}} = p_0 - p_L = \frac{2 \Delta \gamma}{a}, \quad (1)$$

where $\Delta \gamma = \gamma \cos \theta$. The filling dynamics can then be limited by viscous friction inside the tube and at the tube entrance, or by inertia. At the macroscale, the tube inner friction generally dominates, leading to the standard Lucas-Washburn law [32, 33]. However, experimental and numerical work has shown that water flows with an ultralow friction in CNTs, due to giant liquid/solid slip [29]. This results in a plug-flow regime with a flat velocity profile inside the tubes, and a negligible inner viscous dissipation as compared to entrance dissipation [30]. Moreover, inertial effects can be neglected compared to viscous ones in the considered situation [31]. Therefore the filling dynamics is only limited by entrance dissipation, inducing a pressure drop $\Delta p_{\text{ent}}$ related to the flow rate $Q$ according to Sampson equation:

$$\Delta p_{\text{ent}} = \frac{C \eta}{2a^3} \times Q, \quad (2)$$

with $C$ a numerical prefactor depending on the entrance geometry and hydrodynamic boundary condition [32, 33]. Using that $Q = \pi a^2 v_c$ in the plug-flow regime, and writing that $\Delta p_{\text{men}} = \Delta p_{\text{ent}}$, one finds that the liquid fills the tube with a constant velocity $v_c$ (capillary velocity) given by:

$$v_c = \frac{4 \Delta \gamma}{\pi C \eta}. \quad (3)$$

At first sight, the capillary velocity seems independent of the tube radius. At the nanoscale however, the spherical shape of carbon atoms effectively chamfers the tube entrance, leading to a radius-dependent decrease of the Sampson coefficient $C$. This effect is well described by continuum hydrodynamics down to single-file flows [34], and $C(a_c)$ can be computed using finite element calculations, see the Appendix.

Equation (3) accounts for specific nanoscale effects (liquid/solid slip and atomic chamfering of the tube entrance) but it ignores the discrete nature of the liquid and its possible structuring in confinement. We will therefore refer to Eq. (3) as the standard continuum prediction [35].

III. MOLECULAR DYNAMICS SIMULATIONS

We now test the robustness of the standard continuum prediction at the molecular scale using MD simulations.

A. Systems

We considered an initially empty CNT bounded by pierced graphene sheets, in contact with a water reservoir (left end) and an empty reservoir (right end); Fig. 1 shows the water reservoir and the left tube entrance. The CNT length was 10 nm, with radii $a_c$ varying between 3.9 Å and 24 Å. Note that $a_c$ refers to the position of carbon atoms. We showed in previous work that the effective radius $a$ seen by water molecules is smaller: $a_c - a \approx 2.5$ Å [34]. Periodic boundary conditions were imposed in all directions and a third graphene sheet (the left one in Fig. 1) was used as a piston. This piston prevented evaporation from one reservoir to the other through periodic boundaries. We also used it to stop the filling process in order to measure the meniscus pressure jump in static conditions, see below.

The simulations were performed with LAMMPS [36]. We used the TIP4P/2005 model for water [37] and the AMBER96 force field for the carbon-oxygen interactions, i.e. a Lennard-Jones potential with parameters $\epsilon_{\text{C-CO}} = 0.114$ kcal/mol and $\sigma_{\text{C-CO}} = 0.328$ nm [38]. Long-range Coulombic interactions were computed using the particle-particle particle-mesh (PPPM) method. Water molecules were held rigid using the SHAKE algorithm. The equations of motion were solved using the velocity Verlet algorithm with a timestep of 2 fs.

The positions of the carbon atoms (wall+CNT) were fixed [39]. Water molecules located more than 5 Å away from the membrane enclosing the tube entrance inside the left reservoir were kept at a temperature of 300 K using a Berendsen thermostat [40]. The cut-off value $r_c$ for the Lennard-Jones potential was taken equal to 12 Å, which is slightly larger than the usual 10 Å [37, 38]. Indeed, the capillary velocity was found to depend on the value of $r_c$, converging only for $r_c \geq 12$ Å. Moreover, the box size along the $x$ and $y$ directions was taken sufficiently large to ensure that interactions between image CNTs did not affect the velocity measurements, typically twice the tube diameter [41]. Finally we made sure that the reservoir was larger than 10 times $a_c$ along the tube axis. Finite element calculations indicated that, in that configuration, the error on the entrance pressure drop due to finite size effects is lower than 0.25 % [34].

B. Data acquisition

The protocol of data acquisition has been divided in four stages in order to extract the two quantities of interest, which are the capillary velocity (dynamic regime) and the meniscus pressure jump (static regime). Before each measurement stage, equilibration stages were performed. Let us now describe those different stages as well as the corresponding measured quantities. Water molecules are initially placed on a simple cubic lattice with equilibrium density. The system is equilibrated during 0.4 ns, with a plug at the tube entrance to prevent
water from entering. The plug is then removed and the evolution of the number of molecules inside the tube $N$ is recorded as a function of time. This constitutes the dynamic regime of measurement. For a given tube radius, $N$ increased linearly with time during the simulation, corresponding to a constant filling velocity (capillary velocity), as expected from the standard continuum prediction (see Sec. II). The capillary velocity, $v_c$, could thus be defined as

$$v_c = \frac{dN}{dt} \frac{1}{\lambda},$$

where $dN/dt$ is the temporal derivative of the number of molecules inside the tube $N$ fitted during the dynamic stage and $\lambda$ is the linear density of fluid inside the tube, measured once the tube is filled. The dynamic regime lasts until the tube is partially filled (typically 1 or 2 ns, depending on the tube radius). At that moment, the piston is frozen, which prevents water molecules to continue filling the tube. After another equilibration stage of 0.4 ns, the pressure inside the liquid (measured by recording the total force on the piston, divided by its surface) is recorded during 2.5 ns: this constitutes the static measurement regime. In the absence of flow, this piston pressure corresponds to the pressure on the liquid side of the meniscus, and can be used to compute the static meniscus pressure jump. An example for a tube radius $a_c = 5.1$ Å is plotted in Fig. 2. For each set of numerical parameters, the simulations have been performed 5 times with different initial conditions; the resulting velocity and pressure values have been averaged and standard deviations have been calculated.

IV. RESULTS

Figure 3 compares the measured capillary velocities $v_c$ with the standard continuum prediction, Eq. 3, for various tube radii $a_c$. In the prediction, we included the variation of the Sampson coefficient $C$ with the tube radius $a_c$, computed in previous work using the finite element method [24], see the Appendix. The standard continuum prediction should hold for the largest tubes [31, 42] and for $a_c > 15$ Å, MD results indeed agree with Eq. 3 when taking for the viscosity the tabulated value for TIP4P/2005 water and for $\Delta \gamma$ a value of 14 mN/m. Below 15 Å however, the results deviate from Eq. 3, represented as the solid line in Fig. 3. Such deviations are not unexpected, as interfacial properties are predicted to depart from their large-scale values at the nanoscale [24], as encompassed for instance in the Tolman length correction to the surface tension [21] or in line tension effects [40, 41]. However two striking features appear in Fig. 3 for radii $a_c < 7.5$ Å. First the decrease in capillary velocity is not monotonic with the tube radius, with local maxima of $v_c$ measured for $a_c$ around 5.1 Å and 3.9 Å. Second for radii $a_c = 4.3$ and 4.7 Å, the capillary velocity $v_c$ becomes negative [15] (reverse capillary flow).

The observed anomalous capillary filling could be caused by deviations of both hydrodynamics and capillarity from their standard continuum behavior. However, as discussed above, the continuum description of entrance hydrodynamics remains valid down to the single file regime. Moreover, hydrodynamics alone cannot explain the appearance of a reverse capillary flow, pointing to the crucial role of capillarity. To illustrate that scenario, we performed a Jurin-like numerical experiment, by comparing the final height of water within vertical nanotubes, under a gravity field $g$, Fig. 4. For illustrative purpose, we chose an unphysically large value of $1.7 \times 10^{13}$ m s$^{-2}$ so that the capillary rise remained nano-
to 7 Å radius range. As we will show in the following, we see that the dynamic and static approaches can be seen in the 5.5 Å radius case. Let us note that some discrepancy between standard continuum predictions for the driving pressure jump deviate from classical expectations arise due to a breakdown of molecular-scale inversion. This confirms that molecular scale deviations from local minima/maxima together with the wettability may be associated with changes in the fluid structuring under both conditions.

V. DISCUSSION

Overall, subnanometric tubes showed anomalous capillary imbibition departing from standard continuum expectations. These deviations, peaking at special radii \(a_c = 4.3-4.7\) Å for which a wettability reversal is observed, are controlled by changes in the driving pressure jump at the static meniscus. We now discuss the origin of this molecular-scale effect. We first note that other works suggest the existence of special radii for water in CNTs. For instance, water molecules must overcome a larger free energy barrier to enter a CNT with radius \(a_c = 4.6\) Å than to enter smaller and larger tubes \([47, 48]\). Similarly, water can be stabilized in CNTs by very different mechanisms depending on the tube radius \([49]\). To probe whether the observed capillary phenomenon was water-specific, we conducted complementary simulations of CNTs imbibition by a simpler liquid. We considered a model liquid metal, which lacks directional interactions and hydrogen-bonding effects. Compared to the even simpler Lennard-Jones liquids, liquid metals have the advantage of their large cohesion which allows the liquid to resist to the high negative pressures at play in (sub)nanometric capillary filling.

A. Capillary filling of CNTs by a liquid metal

FIG. 4. Top: Ascension under a gravity field (Jurin-like numerical experiment) inside subnanometric nanotubes. Tube radii from left to right: 3.9, 4.3, 5.5, and 8.2 Å. Bottom: Snapshot of water molecules inside CNTs of various radii, \(a_c = 3.9, 4.3, 4.7, 5.1, 5.5, 5.9, 6.2, 7.0,\) and 8.2 Å.

To complement the results for water, we simulated the capillary filling of CNTs by a liquid metal. Again, the capillary velocity and the meniscus pressure jump have been recorded for various tube radii \((a_c = 3.5 \text{ to } 23\) Å). Liquid metals are commonly described by the embedded atom method (EAM) \([50]\). Here, we based our model liquid metal on the liquid gold EAM model developed by Grochola et al. \([51]\). The fluid temperature was set to 1200 K and we adjusted the so-called distance space parameter \(d_r = 0.6410^{-3}\) Å to reproduce water density, thus making comparisons easier. We measured both the liquid metal viscosity, \(\eta_m = 30\pm4\) mPa s, and surface tension, \(\gamma_m = 777 \pm 2\) mN/m. Finally the metal and carbon atoms interacted through a Lennard-Jones potential with an interaction parameter \(\epsilon_{MC} = 0.052\) kcal/mol, while keeping \(\sigma_{MC} = \sigma_{OC} = 3.28\) Å, where \(M\) refers to metal, \(C\) to carbon and \(O\) to oxygen.

The capillary velocity \(v_c\) and the meniscus pressure jump \(p_0 - p_L\), measured for various radii, are plotted in Fig. 5 and compared with standard continuum predictions, respectively \(4\Delta\gamma/\pi\eta C\) for the velocity and \(2\Delta\gamma/\alpha\) for the pressure. As for liquid water, both the capillary velocity and meniscus pressure jump deviate from standard continuum predictions for a tube radius below \(1\) nm. For example, for both liquids, negative velocities are found for tubes with radii \(a_c \sim 4.3-4.7\) Å, as well as positive velocities for \(a_c = 3.9\) Å and \(a_c \geq 5.1\) Å. Alto-
B. Structuring effects

Figure 5 shows snapshots of water structuring inside CNTs. From single-file ($a_c = 3.9 \text{ Å}$) to quasi-continuum state ($a_c = 8.2 \text{ Å}$), the geometrical patterns shown by water molecules can be correlated to the velocity measurements presented in Fig. 3. The three smallest tubes ($a_c = 3.9, 4.3$ and $4.7 \text{ Å}$) can be filled by single-file water, but only the one with $a_c = 3.9 \text{ Å}$ is hydrophilic, as seen in Fig. 3. This probably arises from the increasing amount of vacuum from $a_c = 3.9$ to $a_c = 4.7 \text{ Å}$, coming together with an energetically unfavorable increase of the water-gas contact surface. For the larger radii $a_c = 5.1$ and $5.5 \text{ Å}$, side-by-side molecules are allowed, and those tubes show an increase in capillary velocity, consistently with the apparent small amount of vacuum present in these tubes. For tube radii $a_c = 5.9$ and $6.2 \text{ Å}$, a ring structure is observed, and the curve $v_c$ versus $a_c$ shows a local minimum, which could be related to the cost of having vacuum in the center of the tube. Finally, for radii $a_c = 7.0 \text{ Å}$ and beyond, the fluid loses its structure, corresponding to a velocity that tends toward the standard continuum value ($\sim 7 \text{ m/s}$).

Formally, structuring effects can be described in terms of a disjoining pressure $\Pi_d$ that can be added to the Laplace pressure $\Delta p^{\text{Laplace}}$ [24]. The total pressure drop across the meniscus, previously defined as $\Delta p^{\text{men}} = p_0 - p_L$, writes now:

$$\Delta p^{\text{men}} = \Delta p^{\text{Laplace}} + \Pi_d.$$  \hspace{1cm} (5)

$\Pi_d$ is a function of the ratio between the fluid molecule diameter $\sigma$ and the tube radius $a$. While the expression of $\Pi_d$ as a function of the radius $a$ is not trivial for a cylinder, $\Pi_d$ can be expressed analytically for a fluid of hard spheres confined in a slit (2D) pore as [52]:

$$\Pi_d^{2D}(h) = -\rho_\infty k_B T \cos \left(2\pi h / \sigma \right) e^{-h / \sigma},$$  \hspace{1cm} (6)

with $\sigma$ the fluid particle diameter, $\rho_\infty$ the fluid bulk density, and $h$ the distance between the walls. To test the validity of Eq. (6) together with Eq. (5), we simulated water filling slit nanochannels. The system was identical to the previous one, except that the channel was made of two planar graphene sheets, separated by a distance $h_c$ varied from $7.2$ to $18 \text{ Å}$. As for CNTs, $h_c$ refers to the position of carbon atoms, and the effective height $h$ seen by water molecules is smaller: $h \approx h_c - 5 \text{ Å}$. The width $w$ of the system was larger than $10 \text{ nm}$ to avoid finite size effects in the lateral direction.

Figure 6 presents the results of static measurements of $\Delta p^{\text{men}}$, realized in the same manner as for CNTs. MD results can be fitted quantitatively using $\Delta p^{\text{Laplace}} = \Delta \gamma / \eta$ and a modified expression of the disjoining pressure, with an added screening parameter in the exponential term and a larger value for $\rho_\infty$. These corrections account for the softer interactions between water molecules as compared to a hard sphere fluid [52], and for the large contact density of water near a graphitic solid surface [53]. Now turning to dynamics, the entrance pressure drop writes $\Delta p^{\text{ent}} = C^{2D} \eta v / (2h)$, with the 2D Sampson coefficient $C^{2D}$ evaluated from finite element calculations in the spirit of Ref. [54]. The capillary velocity should then write $v^{2D}_c = (\Delta \gamma + \Pi_d^{2D}) \times 2 / (C^{2D} \eta)$. Figure 6 shows...
a comparison between this prediction and MD simulations. As expected, the capillary velocity oscillates when varying the inter-plate distance $h_c$, and the qualitative agreement between theory and simulations is good. Note a quantitative difference for $h_c \sim 9-10 \text{ Å}$, reminiscent of a similar deviation observed in the case of the cylindrical geometry, see Fig. 3.

VI. CONCLUSION

To conclude, we have shown that in contrast with standard continuum expectations, the capillary velocity depends non-monotonically on the channel dimensions, specifically for tube radii below one nanometer, with the possibility of effectively reversing the wettability for special confinements. We then have shown that these effects are associated with the structuring of water inside the pore. Surprisingly, the anomalous capillary filling and wettability reversal are not specific to water – which behaves as a simple liquid for this particular problem, as confirmed by results obtained with a model liquid metal. The observed phenomena can therefore be described with generic continuum models accounting for fluid structure at the molecular scale such as density functional theory [22, 23, 25]. We have even shown that the deviations from the standard continuum framework could be described by the disjoining pressure, a continuum concept usually introduced in the context of homogeneous films. On this basis, it is accordingly possible to theoretically predict the capillary velocity down to the smallest confinement. Altogether this shows that the standard continuum framework for capillary imbibition could be described by the disjoining pressure, a continuum concept usually introduced in the context of homogeneous films. On this basis, it is accordingly possible to theoretically predict the capillary velocity down to the smallest confinement. Altogether this shows that the standard continuum framework for capillary imbibition cannot be used per se to account for the capillary driven flows in subnanometric channels, but that it can be refined with simple continuum tools accounting for liquid structuring.

The present results are of importance in the study of the filling of nanoporous media. Indeed, according to these results the hydrodynamic permeability of the medium should vary non-monotonically with the pore size distribution and the effect can be quite strong, particularly in the case of water filling nanoporous media with pore radii distributed around 3.9-5.1 Å. A similar effect was actually reported experimentally for the capillary imbibition of water in a carbon nanotube [54], without an explanation up to now. Furthermore, the imbibition of nanoporous media should be disturbed by the present effect, leading to an effective porosity lower than the expected one. Finally, the present results could help to explain the selectivity of membranes, with potential consequences for example in the understanding (and fabrication) of selective ion channels [55].

Appendix: Entrance viscous dissipation

From Ref. [34] the viscous dissipation for a liquid flowing through a carbon nanotube, including inner and entrance contributions, can be obtained. The overall dissipation is dominated by entrance effects, and entirely determined by the value of the numerical prefactor $C$, see Eq. (2). Values of $C$ for different tube radii are gathered in Fig. 7. First, note that the $C$ coefficient varies with the tube radius $a_c$. This variation comes from the chamfering of the entrance induced by the finite radius of carbon atoms, see Ref. [34]. Moreover, note that continuum predictions are in good agreement with molecular dynamics results for the description of the viscous entrance dissipation. Therefore, viscous entrance effects cannot be the main reason of the deviations to the standard continuum predictions observed in the present paper. In particular, viscous entrance effects cannot explain the reversal of the tube wettability. Note however that these results have been obtained with a different water model (TIP3P).

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