Triple Diffusive Unsteady Flow of Eyring–Powell Nanofluid Over a Periodically Accelerated Surface With Variable Thermal Features

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This research communicates the triple diffusion perspective of Eyring–Powell nano-materials configured by a periodically moving configuration. The thermal consequences of variable natures are utilized as a novelty. Combined magnetic and porous medium effects are also involved, which result in a magneto-porosity parameter. The thermophoretic and Brownian motion aspects are reported by using Buongiorno’s nanofluid theory. The formulated flow equations in non-dimensional forms are tackled with the implementation of a homotopy analysis algorithm. A detailed physical investigation against derived parameters is presented graphically. Due to periodically accelerated surface, the oscillations in velocity and wall shear stress have been examined.

Keywords: eyring–powell nanofluid, triple diffusion, variable thermal conductivity, oscillatory stretching sheet, homotopy analysis method

INTRODUCTION

Recent advances in nanotechnology have discovered an advanced source of energy based on utilization nanoparticles. Nanofluids have been interacted for the impressive thermal properties that turn into enhancement of energy transportation. The enhancement of thermo-physical features of conventional base liquids with the addition of micro-sized metallic particles is a relatively new and interesting development in nanotechnology. Nanoparticles attain microscopic size, having a range between 1 and 100 nm. Recently, the investigations on nano-materials become a new class of intense engineering research due to inherent significances in biomedical, chemical, and mechanical industries, electronic field, nuclear reactors, power plants, cooling systems, diagnoses, diseases, etc. The primary investigation on this topic was reported by Choi [1], which was further worked out by several scientists, especially in the current century. The convective features for nano-materials based on thermophoresis and Brownian movement phenomenon were notified by Buongiorno [2]. This investigation revealed that the role of thermophoresis and Brownian motion factors was quite essential for convective slip mechanism. Khan and Pop [3] discussed the feature of nanofluid immersed in base material confined by moving configuration. Sheikholeslami et al. [4] reported the features of thermal radiation in magneto-nanoparticle flow between circular cylinders. The slip flow in nano-material due to porous surface has been reported by
Shahzadi et al. [5], Khan et al. [6] directed their investigation regarding stability prospective of nanoliquids in a curved geometry and successfully estimated a dual solution for the formulated problem. Turkylimazoglu [7] imposed zero mass flux constraints regarding asymmetric channels filled by nanoparticles. Vaidya et al. [8] enrolled the fundamental thermal characteristics in the three-dimensional (3D) flow of Maxwell nanofluid where analytical expressions were developed by using optimal homotopic procedure. Hayat et al. [9] focused on the thermal properties and developed the 3D flow of Oldroyd-B fluid featuring mixed convection effects. Some valuable closed-form expressions for a nanofluid flow problem in porous space have been computed by Turkylimazoglu [10]. Krishna and Chamkha [11] investigated the ion and hall slip effects in the rotating flow of nanofluid configured by a vertical porous plate. The enhancement of heat transfer by using hybrid nanofluids having variable thermal viscosity was reported by Manjunatha et al. [12]. Sardar et al. [13] used non-Fourier’s expressions for Carreau nanofluid and suggested some useful multiple numerical solutions successfully. Alwatban et al. [14] performed a numerical analysis to examine the rheological consequences in Eyring–Powell fluid subjected to the second-order slip along with activation energy. The stability analysis for bioconvection flow of nanofluid was reported by Zhao et al. [15]. Alkanhal et al. [16] involved thermal radiation and external heat source for nanofluid enclosed by a wavy shaped cavity. Kumar et al. [17] discussed the thermo-physical properties of hybrid ferrofluid in thin-film flow impacted by uniform magnetic field. Bhattacharyya et al. [18] evaluated the characteristics of different carbon nanotubes for coaxial movement of disks. Mekheimer and Ramdan [19] investigated the flow of Prandtl nanofluid in the presence of gyrotactic microorganisms over a stretching/shrinking surface.

Recently, researchers specified their attention toward the complex and interesting properties of non-Newtonian materials due to their miscellaneous application in many industries and technologies. The non-Newtonian materials due to convoluted features attracted special attention especially in the current century. The novel physical importance of such non-Newtonian liquids in various engineering and physical processes, biological sciences, physiology, and manufacturing industries is associated due to complex rheological features. Some useful applications associated with the non-Newtonian fluids include polymer solutions, certain oil, petroleum industries, blood, honey, lubricants, and many more. It is commonly observed that distinctive features of such non-Newtonian fluid cannot be pointed out via single relation. Therefore, different non-Newtonian fluid models are suggested by investigators according to their rheology. Among these, Eyring–Powell fluid is inferred from kinetic laws of gases instead of any empirical formulas. This model reduces the viscous fluid at both low and high shear rates (see Powell and Eyring [19]). Gholiania et al. [20] carried out the homogenous and heterogeneous impact in flow of Powell–Eyring liquid due to rotating. Khan et al. [21] focused on viscosity-dependent mixed convection flow of Eyring–Powell nanofluid encountered by inclined surface. Salawu and Ogunsaye [22] reported the entropy generation prospective in Eyring–Powell nanofluid featuring variable thermal consequences and electric field. Another useful continuation performed by Abegunrin et al. [23] examined the change in the boundary layer for the flow of Eyring–Powell fluid subjected by the catalytic surface reaction. Rahimi et al. [24] adopted a numerical technique to compute the numerical solution of a boundary value problem modeled due to the flow of Eyring–Powell fluid. Reddy et al. [25] involved some interesting thermal features, like activation energy, chemical reaction, and non-linear thermal radiation in the 3D flow of Eyring–Powell nanofluid induced via slandering surface. Hayat and Nadeem [26] examined the flow of Eyring–Powell fluid and suggested modification in energy and concentration expressions by using generalized Fourier’s law. Ghahidoklai et al. [27] reported the Joule heating and thermal radiation features inflow of Eyring–Powell non-Newtonian fluid in a stretching walls channel.

The double diffusion convection is a natural phenomenon that encountered multiple novel applications in area soil sciences, groundwater, oceanography, petroleum engineering, food processing, etc. The double-diffusive convection refers to the intermixing of components of two fluid having different diffuse rates. However, the situation becomes quite interesting when double-diffusive convection depends upon more than two components of fluids. Examples of such multiple diffusive phenomena include seawater, molten alloy solidification, and geothermally heated lakes. The triple diffusion flow appears in diverse engineering and scientific fields like geology, astrophysics, disposals of nuclear waste, deoxyribonucleic acid (DNA), chemical engineering, etc. [28–30].

After careful observation of the previously cited work, it is claimed that no efforts have been made to report the triple diffusion flow of Eyring–Powell nanofluid induced by an oscillatory stretching surface with variable thermal features. Although some investigations on flow that is due to periodical acceleration have been available in the literature, thermodiffusion features for Eyring–Powell nanofluid are not studied yet. Therefore, our prime objective of this contribution is to report the triple diffusion aspects of Eyring–Powell nanofluid flow by using variable thermal properties. The most interesting convergent technique homotopy analysis procedure is followed to simulate the solution [31–35]. The graphs are prepared to see the impact of different flow parameters with relevant physical consequence.

**FLOW PROBLEM**

To develop governing equations for unsteady flow of Eyring–Powell nanofluid, we have considered a periodically stretching surface where \( x \)-axis is assumed along with the stretched configuration, whereas \( y \)-axis is taken normally. The source of induced flow is based on the periodically moving surface where amplitude of oscillations are assumed to be small. Let velocity of the moving surface as \( u = u_0 = bx \sin \omega t \), \( b \) as stretching rate, \( \omega \) being angular frequency, whereas \( t \) represent time. The uniform features of the magnetic field are reported by implementing it vertically. Let \( T \) represent the temperature, \( C \) solutal concentration, whereas \( \Phi \) report the nanoparticle volume.
fraction. Furthermore, $T_\infty$, $C_\infty$, and $\Phi_\infty$ denote free stream nanoparticle temperature, free stream solutal concentration, and volume fraction of nanofluid, respectively. After using such assumptions, the flow problem is modeled through the following equations [22, 33]:

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0,$$

(1)

$$u \left( \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} \right) + \frac{\partial u}{\partial t} = \left( \frac{\partial^2 u}{\partial y^2} \right) - \frac{1}{\rho_f \beta_c C} \left( \frac{\partial u}{\partial y} \right)^2 - \left( \frac{\sigma B_0^2}{\rho_f} + \frac{v \theta}{K} \right),$$

(2)

$$\frac{\partial \theta}{\partial x} + \frac{\partial \theta}{\partial y} = \frac{1}{\rho_c \beta_f} \left( K(T) \frac{\partial T}{\partial y} \right) + \tau_T \left[ \frac{\partial \phi}{\partial y} + \frac{\partial T}{\partial y} \right] + D_{TC} \left( \frac{\partial^2 C}{\partial y^2} \right),$$

(3)

$$\frac{\partial \phi}{\partial x} + v \frac{\partial \phi}{\partial y} = \frac{\partial \phi}{\partial t} = D_s \left( \frac{\partial^2 \phi}{\partial y^2} \right) + D_{CT} \left( \frac{\partial^2 T}{\partial y^2} \right),$$

(4)

$$\frac{\partial \Phi}{\partial x} + v \frac{\partial \Phi}{\partial y} = \frac{\partial \Phi}{\partial t} = D_B \left( \frac{\partial^2 \Phi}{\partial y^2} \right) + D_{TC} \left( \frac{\partial^2 T}{\partial y^2} \right),$$

(5)

where $v$ is viscosity, $\rho_f$ fluid density, $(\beta_*, C)$ fluid parameters, $\theta$ permeability of porous medium, $\beta_f$ electrical conductivity, $\alpha_1$ thermal diffusivity, $D_{TC}$ Dufour diffusivity, $\tau_T = (\rho_c \beta_f)/(\rho_f \beta_c)$ ratio of heat capacity of nanoparticles to heat capacity of fluid, $D_B$ Brownian diffusion coefficients, $D_s$ solutal diffusivity, $D_T$ thermophoretic diffusion coefficient, whereas $D_{CT}$ Soret diffusivity.

Following boundary assumptions are articulated for current flow problem

$$u = u(x, t) = u_w \sin \omega t = bx \sin \omega t, \quad v = 0,$$

$$T = T_w, \quad C = C_w, \Phi = \Phi_w \text{ at } y = 0,$$

$$u \to 0, \quad v \to 0, \quad T \to T_\infty, \quad C \to C_\infty, \Phi \to \Phi_\infty \text{ at } y \to \infty.$$

(6)

(7)

In order to suggest modification in energy equation (3), we used the following relations for variable thermal conductivity [33, 34]

$$K(T) = K_\infty \left[ 1 + \epsilon \frac{(T - T_\infty)}{AT} \right],$$

(8)

where $K_\infty$ ambient fluid conductivity and $\epsilon$ thermal dependence conductivity constant. Now, before perfume analytical simulations, first, we reduce the number of independent variables in the governing equations by using the following variables:

$$\xi = \left( \frac{b}{v} \right)^{1/2}, \quad \tau = t \omega, \quad u = u_w f_\xi(\xi, \tau),$$

$$v = -\sqrt{v b f_\xi(\xi, \tau)},$$

$$\theta(\xi, \tau) = \frac{(T - T_\infty)}{(T_w - T_\infty)} \phi(\xi, \tau) = \frac{(C - C_\infty)}{C_w - C_\infty} \phi(\xi, \tau),$$

$$\phi(\xi, \tau) = \frac{(\Phi - \Phi_\infty)}{(\Phi_w - \Phi_\infty)},$$

(9)

(10)

The dimensionless set of equations in view of the previously mentioned transformations is

$$(1 + K) f_\xi \phi_\xi - \delta f_\xi - f_{\phi_\xi} + f f_{\phi_\xi} - \Gamma f_{\xi_\phi} f_{\xi_\xi} = 0,$$

(11)

$$(1 + \delta \theta) \phi_\xi + \delta (\theta T) + \theta T \left[ f \phi_\xi - S \phi_\tau + N b \phi_\xi + N t (\theta \phi)_T^2 \right] + (\nu_D) \phi_\xi \phi_\xi = 0,$$

(12)

$$\phi_\xi = \phi_\tau + L f \phi_\xi + L d \theta_\xi = 0,$$

(13)

$$f_{\xi_\phi} - S \phi_\tau + L n f \phi_\xi + \frac{N t}{N_b} \theta_\xi \phi_\xi = 0,$$

(14)

The boundary constraints in the non-dimensional form are

$$f_{\xi}(0, \tau) = \sin \tau, \quad f(0, \tau) = 0,$$

$$\theta(0, \tau) = 1, \phi(0, \tau) = 1, \phi(0, \tau) = 1,$$

$$f_{\phi}(\infty, \tau) \to 0, \theta(\infty, \tau) \to 0, \phi(\infty, \tau) \to 0, \phi(\infty, \tau) \to 0,$$

(15)

(16)

where $K = 1/\mu \beta_* C$ and $\Gamma = u_w^2 b / 2 v C^2$ denote the material parameters, $\Omega = \sigma B_0^2 / \rho_f b + v \theta / k b$ is magneto-porosity constant, $S = \sigma b /}\alpha_m$ oscillating frequency-to-stretching rate ratio, $N_r = (\rho c)_T D_T (T_w - T_\infty) / (\rho c)_f T_\infty$ thermophoresis parameter, $Pr = \nu / \alpha_m$ is Prandtl number, $N_b = (\rho c)_T D_B (C_w - C_\infty) / (\rho c)_f T_\infty$ Brownian motion constant, $N_d = D_{TC} (C_w - C_\infty) / \alpha_m (T_w - T_\infty)$ modified Dufour number, $L_d = D_{CT} (T_w - T_\infty) / \alpha_m (C_w - C_\infty)$ Dufour Lewis number, $Le = \nu / D_s$ regular Lewis number, whereas $L_n = \nu / D_B$ nano-Lewis number.

We define the following relations associated with the definitions of wall shear stress, local Nusselt number, Sherwood

![FIGURE 1](https://example.com/figure1.png)

$FIGURE 1$ Magnetic curves for $f_{\xi}(0, \pi/2), \phi_{\xi}(0, \pi/2), \phi(0, \pi/2)$, and $\phi(0, \pi/2)$ temperature, solutal concentration, and nanoparticle concentration.
number, and nano-Sherwood number:

\[ C_f = \frac{\tau_w \rho u_w}{\rho u_w}, \quad Nu_x = \frac{xq_j}{k (T_w - T_\infty)}, \quad Sh_x = \frac{xj_s}{D_B (C_w - C_\infty)}, \]

\[ Sh_{x\tau} = \frac{xq_m}{D_s (\phi_w - \phi_\infty)}, \]

where \( q_s \), \( j_s \), and \( g_s \) stand for surface heat flux, surface mass flux, and motile microorganisms flux, respectively. The dimensionless forms of the previously mentioned physical quantities are

\[
\begin{align*}
\text{Re}_x^{1/2} C_f &= (1 + K) f_{\xi \xi} - \frac{k}{3} \beta f_{\xi \xi} \bigg|_{\xi = 0}, \\
Nu_x \text{Re}_x^{-1/2} &= -\theta_{\xi} (0, \tau), \\
Sh_x \text{Re}_x^{-1/2} &= -\phi_{\xi} (0, \tau), \\
Sh_n \text{Re}_x^{-1/2} &= -\phi_{\xi} (0, \tau).
\end{align*}
\]

TABLE 1 | Comparison of \( f_{\xi \xi} (0, \tau) \) for \( \tau \) with Abbas et al. [35] when \( S = 1 \), \( \Omega = 12 \), \( \Gamma = 0 \), and \( K = 0 \).

| \( \tau \) | Abbas et al. [35] | Present results |
|---|---|---|
| \( \pi \) | 11.678656 | 11.6786560 |
| \( 5.5 \pi \) | 11.678707 | 11.678708 |
| \( 9.5 \pi \) | 11.678656 | 11.678656 |

**SOLUTION METHODOLOGY**

The structured set of non-linear partial differential equations (12–16) with boundary conditions (17–18) are simulated analytically via homotopy analysis technique. Due to efficient and convincing accuracy, various physical problems in recent years have been solved by following this procedure. The initial guesses for the present flow problem are

\[ f_0 (\xi, \tau) = \sin \tau (1 - e^{-\xi}), \quad \theta_0 (\xi) = e^{-\xi}, \quad \phi_0 (\xi) = e^{-\xi}, \quad \phi_0 (\xi) = e^{-\xi}, \]

Following auxiliary linear operators that are followed to precede the solution

\[ \xi f = \frac{\partial^3}{\partial \xi^3} - \frac{\partial}{\partial \xi}, \quad \xi \theta = \frac{\partial^2}{\partial \xi^2} - 1, \quad \xi \phi = \frac{\partial^2}{\partial \xi^2} - 1, \]

satisfying

\[ \xi f [a_1 + a_2 e^\xi + a_3 e^{-\xi}] = 0, \]

where \( \text{Re}_x = \frac{\mu_w \bar{u}}{v} \) is mentioned for local Reynolds number.

**FIGURE 2** | Impact of (A) \( K \) (B) \( S \) on skin friction coefficient.

**FIGURE 3** | Impact of (A) \( K \) (B) \( \Omega \) on velocity.
\[ \varepsilon_\theta \left[ a_4 e^{\xi} + a_5 e^{-\xi} \right] = 0, \quad (22) \]
\[ \varepsilon_\varphi \left[ a_6 e^{\xi} + a_7 e^{-\xi} \right] = 0, \quad (23) \]
\[ \varepsilon_\psi \left[ a_8 e^{\xi} + a_9 e^{-\xi} \right] = 0, \quad (24) \]

where \( a_1, \ldots, a_9 \) are arbitrary constants.

**CONVERGENT REGION**

The convergence procedure in homotopic solution is regulated with auxiliary parameters \( h_f, h_\theta, h_\varphi, \) and \( h_\psi \). On this end, we prepare \( h \)-curves to report the convincible range of such parameters. It is obvious from Figure 1 that the preferable range of these such parameters can be utilized from \(-2 \leq h_f \leq 0, -1.2 \leq h_\theta \leq -0.2, -1.4 \leq h_\varphi \leq 0\) and \(-1.2 \leq h_\psi \leq -0.2\).

**VALIDATION OF RESULTS**

Table 1 shows the comparison of present results with Abbas et al. [35] as a limiting case. An excellent accuracy of results is noted with these reported investigations.

**DISCUSSION**

This section aims to manifest the features of some interesting flow parameters that appeared in the dimensionless equations, where material parameter \( K \), magneto-porosity constant \( \Omega_1 \), oscillating frequency-to-rate of stretching ratio \( S \), Brownian motion \( Nb \), thermophoresis constant \( Nt \), variable thermal conductivity \( \delta \), Prandtl number \( Pr \), Dufour Lewis number \( Ld \), modified Dufour constant \( Nd \), regular Lewis number \( Le \), and nano-Lewis number \( Ln \). During variation of each flow parameter, we fixed some numerical values to remaining parameters, like \( K=0.2, \Omega = 0.4, S = 0.2, Nt = 0.3, Pr = 0.7, Nb = 0.4, Nd = 0.5, Ld = 0.3, Le = 0.2, \) and \( Ln = 0.3 \).

**Skin Friction Coefficient**

The impact of the skin friction coefficient against time \( \tau \) for diverse variation of \( K \) and \( S \) is evaluated in Figures 2A,B. An interesting periodic oscillation in the wall shear stress is evaluated by both figures. Furthermore, the growing values of both parameters increase the amplitude of oscillation sufficiently. Due to no-slip conditions at the surface, the fluid particles accelerated together with surface in same amplitude and phase. However, the occurrence of a phase shift in both curves is almost negligible.

**Velocity Profile**

The results reported in Figures 3A,B show the change in velocity \( f_\xi \) verse time \( \tau \) and leading values of material constant \( K \), and magneto-porosity parameter \( \Omega \). Figure 3A characterized the influence of \( K \) on \( f_\xi \), which shows that an increment in \( K \) leads to higher velocity amplitude. The physical justification of such enhancing velocity distribution is attributed to the lower viscosity of fluid associated with the higher values of \( K \). However, reverse observations are predicated for \( \Omega \). In fact, magneto-porosity
constant is the combination of magnetic field and porous space. The existence of a magnetic force encountered the effects of Lorentz force, in which a declining oscillation behavior is noticed. Similarly, the permeability of a porous medium also retards the velocity amplitude due to the loss of fluid. Moreover, the utilization of magnetic force enhances the apparent viscosity of fluid up to a certain point of becoming an elastic solid, and subsequently, the fluid stress can be managed upon changing the magnetic force. These interesting observations can be used in various processes, like magnetohydrodynamic drive ion propulsion, magnetohydrodynamic drive power generators, electromagnetic material casting, etc.

**Temperature Distribution**

To visualize the alter profile of nanoparticle temperature $\theta$ due to $\delta$, $K$, and $Nd$. Figures 4A–C are prepared. Figure 4A reveals that temperature distribution $\theta$ increases with variable thermal conductivity constant $\delta$. Figure 4B is constituted to observe the change in $\theta$ due to material parameter $K$. A fall in $\theta$ is associated with leading variation of $K$. An increment in viscosity would yield for arising values of $K$ that increases the fluid velocity but a decline in the temperature of fluid. The change in $\theta$ with effect of modified Dufour number $Nd$ has been reported in Figure 4C. A slightly dominant variation in $\theta$ is seen with larger values of $Nd$.

**Solutal Concentration Profile**

Now, we observe the variation in solutal concentration profile $\varphi$ by varying regular Lewis number ($Le$), Dufour Lewis constant ($Ld$), and material constant ($K$). Figure 5A is designed to observe the impact of $Le$ on $\varphi$. A decreasing solutal concentration profile $\varphi$ is notified due to $Le$. Physical explanation of such declining variation of $\varphi$ can be justified on the fact that $Le$ captures reverse relation with species diffusion, which means that when $Le$ is maximum, species diffusion is lower, which leads to the decrement of the resulting solutal concentration. From Figure 5B, $\varphi$ increases with the growth of $Ld$. Physically, $Ld$ depends upon the Lewis number due to lower mass diffusivity. Figure 5C presents change in $\varphi$ due to material constant $K$. Again, an enhanced distribution of solutal concentration profile $\varphi$ has resulted for maximum values of $K$.

**Nanoparticle Concentration**

The physical consequences of $Ln$, $Nt$, and $Nb$ on concentration distribution $\varphi$ are deliberated in Figures 6A–C. Figure 6A specified the input of $Ln$ on $\varphi$. A declining concentration distribution $\varphi$ is examined in the peak values of $Ln$. This decreasing behavior of $\varphi$ is attributed to the fact that $Ln$ is associated with the Brownian diffusion coefficient because $Ln$ expresses the thermal diffusivity-to-mass diffusivity ratio. This parameter that is referred to the fluid flow in a
phenomenon of heat and mass transfer occurs due to convection. The consequences for another important parameter, namely thermophoresis constant $N_t$, are analyzed in Figure 6B. As expected, a larger concentration distribution $\phi$ is reported due to involvement of $N_t$. The larger variation of $N_t$ helps to improve the thermal conductivity of fluid. Physically, the thermophoretic process is based on collective migrated heat particles in the region of low temperature and plays a momentous role in many physical processes.

![Figure 6 | Impact of (A) $L_n$, (B) $N_t$, and (C) $N_b$.](image)

**TABLE 2 |** Numerical values of $-\theta_1 (0, \tau)$, $-\psi_1 (0, \tau)$, and $-\phi_2 (0, \tau)$, when $\tau = \pi/2$.

| $\Omega$ | $Pr$ | $N_t$ | $N_b$ | $\varepsilon$ | $K$ | $-\theta_1 (0, \tau)$ | $-\psi_1 (0, \tau)$ | $-\phi_2 (0, \tau)$ |
|----------|------|------|------|----------|-----|-----------------|-----------------|-----------------|
| 0.0      | 0.7  | 0.3  | 0.3  | 0.1      | 0.1 | 0.62231         | 0.55537         | 0.54652         |
| 0.5      | 0.60854 | 0.53876 | 0.51828 | 0.49632 |
| 1.0      | 0.59654 | 0.50535 | 0.49632 | 0.49632 |
| 0.2      | 0.2   | 0.48896 | 0.44689 | 0.42658 |
| 0.5      | 0.55658 | 0.47598 | 0.46485 | 0.46485 |
| 1.0      | 0.57875 | 0.49535 | 0.50280 | 0.50280 |
| 0.7      | 0.0   | 0.58029 | 0.60986 | 0.62384 |
| 0.4      | 0.53331 | 0.56154 | 0.57567 | 0.57567 |
| 0.5      | 0.51189 | 0.519856 | 0.53878 | 0.53878 |
| 0.2      | 0.3   | 0.49598 | 0.455454 | 0.43562 |
| 0.5      | 0.44357 | 0.44543 | 0.50635 | 0.50635 |
| 0.7      | 0.42637 | 0.43045 | 0.57420 | 0.57420 |
| 0.3      | 0.2   | 0.48351 | 0.44659 | 0.50015 |
| 0.4      | 0.46743 | 0.42798 | 0.48243 | 0.48243 |
| 0.6      | 0.44092 | 0.40659 | 0.44564 | 0.44564 |
| 0.3      | 0.0   | 0.49359 | 0.44659 | 0.52658 |
| 0.4      | 0.46787 | 0.42298 | 0.50256 | 0.50256 |
| 0.6      | 0.43395 | 0.41326 | 0.47559 | 0.47559 |
phomenons. The curve of \( \phi \) attained maximum level due to \( Nt \). However, a reduced concentration distribution \( \phi \) is associated with \( Nb \), as shown in Figure 6C. The Brownian movement is based on random pattern moving fluid particles in flow surface. It is further justified from Equation (16), which clearly shows that reverse relation is developed between \( Nb \) and \( \phi \). In fact, the specified numerical values of \( Nb \) are associated to the more prominent nanoparticle moments that are being pushed back from accelerated plate to quiescent, which resulted in a retarded concentration distribution.

Physical Quantities
To perform the numerical simulations for local Nusselt number \( -\theta_\xi (0, \tau) \), local Sherwood Number \( -\phi_\xi (0, \tau) \) and nanofluid Sherwood number \( -\phi_\xi (0, \tau) \), Table 2 is designed. It is observed that when \( \Omega \), \( s \), and \( K \) assigned larger numerical values, a decreasing trend in \( -\theta_\xi (0, \tau) \), \( -\phi_\xi (0, \tau) \), and \( -\phi_\xi (0, \tau) \) is reported. However, these physical quantities increase with the variation of \( Pr \).

CONCLUSIONS
We have focused on periodically accelerated unsteady flow of Eyring–Powell nanofluid with utilization of thermal diffusive features. The variable impact of thermal conductivity, porous medium, and magnetic field consequences are also utilized. The important observations from current flow problem are summarized as:

- The magneto-porosity parameter declined the periodic oscillation in the velocity, and subsequently, the magnitude of velocity declined.
- The wall shear stress oscillates periodically with time that increases by varying material parameter.
- The thermal conductivity with the variable nature is more effective in enhancing the nanoparticle temperature.
- The modified Dufour number increases the temperature distribution.
- It is noted that solutal concentration increases subject to Dufour Lewis number and material constant.
- An increasing change in nanoparticle concentration determined with nano-Lewis number and a material parameter.

The observation based on the reported results can be used to improve thermal extrusion processes, heat exchangers, solar technology, energy production, cooling processes, etc.

DATA AVAILABILITY STATEMENT
The original contributions presented in the study are included in the article/supplementary materials, further inquiries can be directed to the corresponding author/s.

AUTHOR CONTRIBUTIONS
All authors listed have made a substantial, direct and intellectual contribution to the work, and approved it for publication.

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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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