Measurements of the BK$_{Ca}$ Channel’s High-Affinity Ca$^{2+}$ Binding Constants: Effects of Membrane Voltage

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It has been established that the large conductance Ca$^{2+}$-activated K$^+$ channel contains two types of high-affinity Ca$^{2+}$ binding sites, termed the Ca$^{2+}$ bowl and the RCK1 site. The affinities of these sites, and how they change as the channel opens, is still a subject of some debate. Previous estimates of these affinities have relied on fitting a series of conductance–voltage relations determined over a series of Ca$^{2+}$ concentrations with models of channel gating that include both voltage sensing and Ca$^{2+}$ binding. This approach requires that some model of voltage sensing be chosen, and differences in the choice of voltage-sensing model may underlie the different estimates that have been produced. Here, to better determine these affinities we have measured Ca$^{2+}$ dose–response curves of channel activity at constant voltage for the wild-type mSlo channel (minus its low-affinity Ca$^{2+}$ binding site) and for channels that have had one or the other Ca$^{2+}$ binding site disabled via mutation. To accurately determine these dose–response curves we have used a series of 22 Ca$^{2+}$ concentrations, and we have used unitary current recordings, coupled with changes in channel expression level, to measure open probability over five orders of magnitude. Our results indicate that at −80 mV the Ca$^{2+}$ bowl has higher affinity for Ca$^{2+}$ than does the RCK1 site in both the opened and closed conformations of the channel, and that the binding of Ca$^{2+}$ to the RCK1 site is voltage dependent, whereas at the Ca$^{2+}$ bowl it is not.

INTRODUCTION

Large-conductance Ca$^{2+}$-activated potassium (BK$_{Ca}$) channels are important for the modulation of many physiological processes, such as neuronal firing, smooth muscle contraction, and neurotransmitter release (Storm, 1987; Roberts et al., 1990; Sah and McLachlan, 1992; Robitaille et al., 1993; Nelson and Quayle, 1995; Brenner et al., 2000; Hu et al., 2001; Wang et al., 2001; Semenov et al., 2006). They are uniquely suited to regulate these processes because they are sensitive to both intracellular Ca$^{2+}$ and membrane voltage. This is seen as a leftward shift in the BK$_{Ca}$ channel’s conductance–voltage (G-V) relation as the internal Ca$^{2+}$ concentration is increased. Biophysical studies have shed considerable light on the mechanisms by which voltage influences channel opening (Cui et al., 1997; Stefani et al., 1997; Diaz et al., 1998; Horrigan and Aldrich, 1999, 2002; Horrigan et al., 1999; Rothberg and Magleby, 2000; Bao and Cox, 2005); however, the mechanisms by which Ca$^{2+}$ influences channel opening remain less well understood.

Unlike K$^+$ channels gated solely by voltage, the BK$_{Ca}$ channel’s pore-forming subunit (four per functional channel) contains a large intracellular domain that confers Ca$^{2+}$ sensitivity on a voltage-gated structure (Wei et al., 1994; Schreiber and Salkoff, 1997; Schreiber et al., 1999). The structure of this domain remains a matter of debate; however, it is generally agreed that within this domain there are three distinct Ca$^{2+}$ binding sites, one of low affinity (millimolar dissociation constants) and two of high affinity (micromolar dissociation constants) (Bao et al., 2002; Shi et al., 2002; Xia et al., 2002; Magleby, 2003). Mutations at these sites together eliminate the BK$_{Ca}$ channel’s characteristic Ca$^{2+}$-dependent G-V shift (Xia et al., 2002). The first of these sites to be identified, the Ca$^{2+}$ bowl, is an aspartate-rich region near the carboxy terminus (Schreiber and Salkoff, 1997). Considered high affinity, this site contributes to the channel’s Ca$^{2+}$ sensitivity in the micromolar range (Bao et al., 2002; Xia et al., 2002). Mutations within the Ca$^{2+}$ bowl such as D897-901N (referred to as D5N5) or D898A/D900A (referred to here as D2A2) can eliminate the contribution of this site to the channel’s Ca$^{2+}$ sensitivity (Bian et al., 2001; Bao et al., 2004). The second high-affinity site, termed here the RCK1 site, resides in a domain thought to be similar in structure to the ligand binding RCK domains of bacterial potassium channels and transporters (Schreiber and Salkoff, 1997; Jiang et al., 2001; Bao et al., 2002; Jiang et al., 2002; Xia et al., 2002;
Zeng et al., 2005). Although the residues that coordinate Ca\(^{2+}\) at this site have yet to be determined, the mutation D367A has been shown to eliminate the contribution of this high-affinity site to Ca\(^{2+}\) sensing (Xia et al., 2002). The BK\(_{Ca}\) channel’s low-affinity Ca\(^{2+}\) binding site is also thought to reside in the channel’s RCK1 domain, and its influence can be eliminated by the mutation E399N (Shi et al., 2002; Xia et al., 2002).

The binding properties of the BK\(_{Ca}\) channel’s two high-affinity Ca\(^{2+}\) binding sites are uncertain. Bao et al. (2002) estimated the Ca\(^{2+}\) bowl’s Ca\(^{2+}\) dissociation constant to be 3.5 \(\mu M\) when the channel is closed (\(K_C\)) and 0.8 \(\mu M\) when it is open (\(K_O\)) (Bao et al., 2002), whereas Xia et al. (2002) estimated \(K_C\) to be 4.5 \(\mu M\) and \(K_O\) to be 2.0 \(\mu M\) (Xia et al., 2002). These numbers may seem similar, but according to allosteric theory the ratio \(K_C / K_O\) is equivalent to the factor by which Ca\(^{2+}\) binding at a given site alters the equilibrium constant for channel opening. The estimates of Bao et al. (2002) yield a \(K_C / K_O\) value of 4.4, whereas those of Xia et al. (2002) yield a \(K_C / K_O\) value of 2.2. Thus, for a single binding event the two groups predict effects of Ca\(^{2+}\) on the equilibrium constant for channel opening that differ by a factor of two, and if there are four Ca\(^{2+}\) bowl-related sites—as there appears to be (Niu and Magleby, 2002)—then when all four sites are occupied, the difference is 14-fold. Further, there are larger differences between the two groups’ estimates of \(K_C\) and \(K_O\) for the channel’s other type of high-affinity Ca\(^{2+}\) binding site, the RCK1 site. The estimates of Bao et al. (2002) are considerably smaller than those of Xia et al. (2002) and more like those of the Ca\(^{2+}\) bowl (Bao et al. [2002]: \(K_C = 3.8\) \(\mu M\) and \(K_O = 0.9\) \(\mu M\); Xia et al. [2002]: \(K_C = 17.2\) \(\mu M\) and \(K_O = 4.6\) \(\mu M\)).

One likely reason for these discrepancies is that both groups made their estimates by fitting gating models to a series of G-V relations determined for a series of [Ca\(^{2+}\)], and to make these estimates they necessarily had to assume some model of the voltage-sensing mechanism of the channel. The two groups used different voltage-sensing models. More generally, however, a better way to estimate the affinity constants of the channel’s Ca\(^{2+}\) binding sites would be to study the effect of Ca\(^{2+}\) on channel opening at many [Ca\(^{2+}\)] but at a single voltage, such that the effect of voltage on channel opening can be treated as a constant.

Here, we have taken this approach. We have used mutations at each type of Ca\(^{2+}\) binding site and high-resolution Ca\(^{2+}\) dose-response curves to characterize the binding properties of each of the BK\(_{Ca}\) channel’s high-affinity Ca\(^{2+}\) binding sites at both -80 and 0 mV. Our results indicate that the two sites have substantially different affinities, as suggested by Xia et al. (2002), at both these potentials, and that Ca\(^{2+}\) binding at the RCK1 site is voltage-dependent, whereas at the Ca\(^{2+}\) bowl it is not.

**MATERIALS AND METHODS**

Heterologous Expression of BK\(_{Ca}\) Channels in TSA 201 Cells

TSA201 cells (modified human embryonic kidney cells) were transiently transfected with expression vectors (pDNA 3; Invitrogen) encoding the subunit of the BK\(_{Ca}\) channel from mouse (mSlo- mbr5) (Butler et al., 1993), enhanced green fluorescent protein (eGFP-N1; BD Biosciences), and the empty pcDNA 3.1+ vector (Invitrogen) to control for total amount of transfected DNA. Cells were transiently transfected using the Lipofectamine 2000 reagent (Invitrogen). The enhanced green fluorescent protein was used to monitor successfully transfected cells. For transfection, cells at 80–90% confluence in 35-mm falcon dishes were incubated with a mixture of the plasmids (total of 4 \(\mu g\) DNA) Lipofectamine and OptiMem (Invitrogen) according to the manufacturer’s instructions. In brief, the mixture was left on the cells 4–8 h after which the cells were replated into recording Falcon 3004 dishes in standard tissue culture media: DMEM with 1% fetal bovine serum, 1% t-glutamine, and 1% penicillin-streptomycin solution (all from Invitrogen). The cells were patch-clamped 1–3 d after transfection.

**Electrophysiology**

All recordings were performed in the inside-out patch-clamp configuration (Hamill et al., 1981). Patch pipettes were made of borosilicate glass (VWR micropipettes) with 0.8–5 M\(\Omega\) resistances that were varied for different recording purposes. The tips of the patch pipettes were coated with sticky wax (KerrLab) and fire polished. Data were acquired using an Axopatch 200B patch clamp amplifier and a Macintosh-based computer system equipped with an ITC-16 hardware interface (InstruTECH) and Pulse acquisition software (HEKA electronik). For macroscopic current recordings, data were sampled at 50 kHz and filtered at 10 kHz. In most macroscopic current recordings, capacity and leak current were subtracted using a P/5 subtraction protocol with a holding potential of -120 mV and leak pulses in opposite polarity to the test pulse, but with BK\(_{Ca}\) currents recorded with >100 \(\mu M\) Ca\(^{2+}\), no leak subtraction was performed.

Unitary current recordings acquired at -80 mV were sampled at 100 kHz and filtered at 10 kHz. Unitary current recordings acquired at 0 mV were sampled at 100 kHz and filtered at 2 kHz. All experiments were performed at room temperature, 22–24°C.

**Solutions**

The pipette solution for macroscopic current recordings contained the following: 118 mM KMeSO\(_3\), 20 mM N-methyl-glucamine-MeSO\(_4\), 2 mM KCl, 2 mM MgCl\(_2\), 2 mM HEPES, pH 7.20. The pipette solution for current recordings at 0 mV contained the following: 3 mM KMeSO\(_3\), 135 mM N-methyl-glucamine-MeSO\(_4\), 2 mM KCl, 2 mM MgCl\(_2\), 2 mM HEPES, pH 7.20. 10 \(\mu M\) GdCl\(_3\) was added to both pipette solutions to block endogenous stretch-activated channels. GdCl\(_3\) did not block BK\(_{Ca}\) currents (not depicted) (Yang and Sachs, 1989; Qian and Magleby, 2003). The bath solution for all recordings contained the following: 118 mM KMeSO\(_3\), 20 mM N-methyl-glucamine-MeSO\(_4\), 2 mM KCl, 2 mM HEPES, pH 7.20. 1 mM EGTA (Fluka) was used as the Ca\(^{2+}\) buffer for solutions containing 3–500 nM free [Ca\(^{2+}\)], 1 mM HEDTA (Sigma-Aldrich) was used as the Ca\(^{2+}\) buffer for solutions containing 0.8–20 \(\mu M\) free [Ca\(^{2+}\)], and no Ca\(^{2+}\) chelator was used in solutions containing between 20 \(\mu M\) and 2.5 mM free Ca\(^{2+}\), 50 \(\mu M\) (+)-18-crown-6-tetracarboxylic acid (18C6TA) was added to all internal solutions to prevent contaminant Ba\(^{2+}\) block at high voltages. Both internal and external solutions were brought to pH 7.20.
The appropriate amount of total Ca\textsuperscript{2+} (100 mM CaCl\textsubscript{2} standard solution; Orion Research, Inc.) to add to the buffered solutions to yield the desired approximate free Ca\textsuperscript{2+} concentrations of 3 nM to 2.5 mM was calculated using the program MaxChelator (see Online Supplemental Material), and the solutions were prepared as described previously (Bao et al., 2002). The Ca\textsuperscript{2+} concentrations reported are averages of three independent measurements determined with an Orion Ca\textsuperscript{2+}-sensitive electrode. The solutions bathing the intracellular side of the patch were changed by means of a DAD valve-controlled pressurized superfusion system (ALA Scientific Instruments).

Data Analysis
All data analysis was performed with Igor Pro graphing and curve-fitting software (WaveMetrics Inc.), and the Levenberg-Marquardt algorithm was used to perform nonlinear least-square curve-fitting. Values in the text are given ± SEM.

G-V Curves
G-V relations were determined from the amplitude of tail currents measured 200 μs after repolarizations to −80 mV following voltage steps to the test voltage. Each G-V relation was fitted with a Boltzmann function,

\[
G = \frac{G_{\text{max}}}{1 + e^{\frac{V - V_{1/2}}{k}}} 
\]

and normalized to the maximum of the fit.

Single-Channel Analysis
Under conditions where the open probability (Popen) is small (<10\textsuperscript{−4}), single-channel openings were observed in patches containing hundreds of channels and I\textsubscript{K} was measured from steady-state recordings 30 s in duration. NPopen was determined from all-points histograms by measuring the fraction of time spent (SPopen) at each open level (k) using a half-amplitude criteria and summing their contributions, NPopen = Σ kPopen, where N is the number of channels in the patch.

Popen Versus Ca\textsuperscript{2+} Curves
The effect of Ca\textsuperscript{2+} on Popen was determined from the ratio of NPopen at a given Ca\textsuperscript{2+} to NPopen at 5.3 μM Ca\textsuperscript{2+} for all Ca\textsuperscript{2+} concentrations tested on a given patch. The (NPopen/NPopen\textsubscript{5.3 μM}) versus [Ca\textsuperscript{2+}] relation from each patch was then plotted and averaged across many patches. The mean (NPopen/NPopen\textsubscript{5.3 μM}) versus [Ca\textsuperscript{2+}] relation was then adjusted such that at 3 nM Ca\textsuperscript{2+} log (NPopen/NPopen\textsubscript{max}) = 0. In some cases Popen, rather than being normalized (NPopen/NPopen\textsubscript{max}), was reported as a function of [Ca\textsuperscript{2+}]. This was done by determining Popen for each channel type at a single [Ca\textsuperscript{2+}] in separate experiments, and then adjusting the average log (NPopen/NPopen\textsubscript{max}) versus log [Ca\textsuperscript{2+}] curve vertically, such that Popen was correct at the [Ca\textsuperscript{2+}] at which Popen was known. At 0 mV, the calibrated Popen was determined at 2.5 mM from patches whose channel content was apparent (n = 1–4). At −80 mV, the calibrating Popen was determined at 5.3 μM [Ca\textsuperscript{2+}] from unitary current measurements of NPopen from a series of patches in which N was calculated from the maximal current measured at +80 mV and separate Popen measurements taken at +80 mV for single channels.

Online Supplemental Material
The amount of Ca\textsuperscript{2+} to add to internal solutions to yield the desired free Ca\textsuperscript{2+} concentrations was calculated using the program MaxChelator, which was downloaded from http://www.stanford.edu/~cpatton/maxc.html and is included as executable files here. The online supplemental material is available at http://www.jgp.org/cgi/content/full/jgp.200810094/DC1.

RESULTS

The Effect of Ca\textsuperscript{2+} with Both Sites Intact
The BK\textsubscript{Ca} channel is both Ca\textsuperscript{2+} and voltage sensitive, and the effects of these stimuli are often displayed as a series of G-V relations determined at several Ca\textsuperscript{2+} concentrations (Barrett et al., 1982). Such a series, determined from BK\textsubscript{Ca} channels exogenously expressed in TSA-201 cells, is shown in Fig. 1 B. The data are from excised inside-out macropatches (Fig. 1 A). Increasing intracellular Ca\textsuperscript{2+} shifts the channel’s G-V curve leftward, an effect that is known under wild-type conditions to be due to three types of Ca\textsuperscript{2+} binding sites, two of high affinity and one of low affinity. The channels in the patches of Fig. 1, however, contained the mutation E399N, which eliminates low-affinity Ca\textsuperscript{2+} sensing (Shi et al., 2002; Xia et al., 2002) and thereby allows one to examine high-affinity Ca\textsuperscript{2+} sensing in isolation. We refer to the mouse Slo (mSlo) channel carrying this mutation as ΔE. Increasing Ca\textsuperscript{2+} from 3 nM to 2.5 mM shifts the ΔE G-V relation ∼−200 mV.

Previous estimates of the affinities of the BK\textsubscript{Ca} channel’s high-affinity Ca\textsuperscript{2+} binding sites have been based on fitting gating models to data like that shown in Fig. 1 B. This necessarily requires that one assume some model of voltage-dependent gating, and the resulting Ca\textsuperscript{2+} binding parameters produced by the fits are then dependent on this choice (Bao et al., 2002; Xia et al., 2002). To circumvent this necessity, and thereby more directly determine the BK\textsubscript{Ca} channel’s high-affinity Ca\textsuperscript{2+} binding constants, here we have studied the effects of Ca\textsuperscript{2+} at constant voltage.

Fig. 2 A shows unitary ΔE currents recorded from a single membrane patch at −80 mV and four different [Ca\textsuperscript{2+}]. Corresponding amplitude histograms are shown in Fig. 2 B. Although the patch contained hundreds of channels, each channel’s open probability (Popen) is low in the absence of Ca\textsuperscript{2+}, such that activity is observed as the infrequent and brief opening of single channels. Application of Ca\textsuperscript{2+} then caused a large increase in Popen that resulted in multi-channel openings. From data like these we derived the ΔE channel’s Popen versus [Ca\textsuperscript{2+}] relation (Fig. 2 C). So that all parts of the curve could be well determined, Popen was measured over five orders of magnitude with 22 Ca\textsuperscript{2+} concentrations. To do this, many patches were used and normalized by their values of NPopen at 5.3 μM, where N is the number of channels in a given patch. The data were then averaged at each [Ca\textsuperscript{2+}], and the whole curve was adjusted vertically to match the BK\textsubscript{Ca} channel’s Popen at 5.3 μM and −80 mV, which was determined in separate experiments (see Materials and methods).

These data were then analyzed as follows. If one assumes that there are four of each type of Ca\textsuperscript{2+} binding site and that each site influences channel opening by altering the equilibrium constant of a single conformational
change between closed and open—as much evidence suggests (McManus and Magleby, 1991; Cox et al., 1997; Cui et al., 1997; Horrigan and Aldrich, 1999, 2002; Horrigan et al., 1999; Rothberg and Magleby, 1999, 2000; Cox and Aldrich, 2000)—and that there are no interactions between binding sites, then at constant voltage the channel’s open probability as a function of voltage can be written as:

\[
P_{\text{open}} = \frac{M(1 + [\text{Ca}]/K_{\text{O1}})^4(1 + [\text{Ca}]/K_{\text{O2}})^4}{(1 + [\text{Ca}]/K_{\text{C1}})^4(1 + [\text{Ca}]/K_{\text{C2}})^4 + M(1 + [\text{Ca}]/K_{\text{O1}})^4(1 + [\text{Ca}]/K_{\text{O2}})^4},
\]

where \( K_{\text{O1}} \) and \( K_{\text{O2}} \) represent the dissociation constants of binding sites 1 and 2 in the closed conformation, \( K_{\text{O1}} \) and \( K_{\text{O2}} \) represent the dissociation constants of binding sites 1 and 2 in the open conformation, and \( M \) represents the closed-to-open equilibrium constant when no Ca\(^{2+}\) is bound. As relates to the BK\(_{\text{Ca}}\) channel, \( M \) is voltage dependent and incorporates all effects of voltage on opening.

In the absence of Ca\(^{2+}\), Eq. 1 reduces to:

\[
P_{\text{open}} = \frac{M}{1 + M},
\]

which can be rearranged to:

\[
M = \frac{P_{\text{open}}}{1 - P_{\text{open}}}. \tag{3}
\]

Thus, \( M \) can be determined directly from \( P_{\text{open}} \) in the absence of Ca\(^{2+}\). From Fig. 2 C we can estimate \( M \) to be \(~2.5 \times 10^{-6}\) However, better still, when \( P_{\text{open}} \) is small over the entire Ca\(^{2+}\) dose-response curve, as is the case here, Eq. 1 reduces to Eq. 4 below (Horrigan and Aldrich, 2002):

\[
P_{\text{open}} = \frac{M(1 + [\text{Ca}]/K_{\text{O1}})^4(1 + [\text{Ca}]/K_{\text{O2}})^4}{(1 + [\text{Ca}]/K_{\text{C1}})^4(1 + [\text{Ca}]/K_{\text{C2}})^4 + M(1 + [\text{Ca}]/K_{\text{O1}})^4(1 + [\text{Ca}]/K_{\text{O2}})^4}, \tag{4}
\]

and then dividing through by \( P_{\text{open}} \) at 0 \([\text{Ca}^{2+}]\) yields:

\[
\frac{P_{\text{open}}(\text{Ca})}{P_{\text{open}}(0)} = \frac{(1 + [\text{Ca}]/K_{\text{O1}})^4(1 + [\text{Ca}]/K_{\text{O2}})^4}{(1 + [\text{Ca}]/K_{\text{C1}})^4(1 + [\text{Ca}]/K_{\text{C2}})^4}. \tag{5}
\]

This eliminates \( M \) and leaves a curve whose properties are determined solely by the channel’s Ca\(^{2+}\) binding constants (Horrigan and Aldrich, 2002). Thus, the curve in Fig. 2 C was normalized by its minimum value to yield a \( P_{\text{open}} \) (Ca\(^{2+}\))/\( P_{\text{open}} \) (0) versus [Ca\(^{2+}\)] curve (Fig. 3) and then fitted with Eq. 5. Properties of this curve of note are: (1) Ca\(^{2+}\) increases \( P_{\text{open}} \) by a factor of \(~2.8 \times 10^4\); (2) \( P_{\text{open}} \) saturates at high [Ca\(^{2+}\)], \(~100 \text{ mM}\); and (3) the curve has a shallow quality suggestive of multiple binding sites with differing affinities. Indeed the fit (solid line) yielded the following dissociation constants: SITE 1, \( K_{\text{C1}} = 3.7 \pm 2.1 \text{ mM}, K_{\text{O1}} = 0.7 \pm 0.14 \text{ mM}; \) SITE 2, \( K_{\text{C2}} = 51 \pm 42 \text{ mM}, K_{\text{O2}} = 21 \pm 24 \text{ mM}. \)

Further, when we forced both types of binding sites to have the same affinities, a substantially worse fit was obtained (dashed line, \( K_{\text{C}} = 6.1 \pm 0.4 \text{ mM}, K_{\text{O}} = 1.9 \pm 0.31 \text{ mM} \)). Thus, this analysis suggests that one of the BK\(_{\text{Ca}}\) channel’s high-affinity Ca\(^{2+}\) binding sites has substantially higher
affinity for Ca$^{2+}$ than the other, both in the open and closed conformations, although noise in the data introduces some uncertainty about the fitted values.

**Mutations That Eliminate Ca$^{2+}$ Sensing**

To measure the affinities of each type of high-affinity Ca$^{2+}$ binding site individually, we used mutations that selectively eliminate the effect of Ca$^{2+}$ at each type of site. D367A eliminates Ca$^{2+}$ sensing via RCK1 sites (Xia et al., 2002), and D897N/D898N/D899N/D900N/D901N (D5N5) or D898A/D900A (D2A2) eliminate Ca$^{2+}$ sensing via the Ca$^{2+}$ bowls (Schreiber and Salkoff, 1997; Bian et al., 2001; Bao et al., 2004). Before using these mutations, however, it was important to confirm that in conjunction with E399N they eliminate all Ca$^{2+}$ sensing. Shown in Fig. 4A are currents recorded at various [Ca$^{2+}$] from a patch expressing the triple mutant (E399N)(D367A)(D897N/D898N/D899N/D900N/D901N), which we refer to as $\text{H9004}_E \text{H9004}_R$ (D5N5). Corresponding amplitude histograms are superimposed in Fig. 4B, and in Fig. 4C the $\text{H9004}_E \text{H9004}_R$ channel’s Ca$^{2+}$ dose-response relation is plotted at $\text{H11002}80$ mV. As is evident, the triple mutant shows virtually no response to Ca$^{2+}$, which demonstrates that the three sites targeted by these mutations can together account for all of the channel’s Ca$^{2+}$ sensing.

**Ca$^{2+}$ Binding at the Ca$^{2+}$ Bowl**

We then used the mutant (E399N)(D367A), which we refer to as $\Delta \text{E} \Delta \text{AR}$, to examine Ca$^{2+}$ sensing via the Ca$^{2+}$ bowl. Fig. 5A compares BK$_{Ca}$ currents at various [Ca$^{2+}$] recorded from a single $\Delta \text{E} \Delta \text{AR}$ patch at $\text{H80}$ mV. The corresponding amplitude histograms are shown in Fig. 5B. As with $\Delta \text{E}$, $\text{Popen}$ is low in the absence of Ca$^{2+}$, and activity is observed as the infrequent and brief opening of single channels. Application of Ca$^{2+}$ then increases $\text{Popen}$, but the increase is not as great ($\sim 10^2$-fold) as it is with the $\text{H9004}_E$ channel ($\sim 10^4$-fold), presumably because the $\text{H9004}_E$R channel has lost half of its high-affinity binding sites. A Ca$^{2+}$ dose–response relation for the $\Delta \text{E} \Delta \text{AR}$ channel at $\text{H80}$ mV is shown in Fig. 5C. The affinities of

**Figure 2.** The Ca$^{2+}$ dependence of $\text{Popen}$ for mutant $\Delta \text{E}$. (A) Inward potassium currents recorded at $\text{H80}$ mV and filtered at 10 kHz from a macropatch exposed to the indicated [Ca$^{2+}$] demonstrate that $\text{Popen}$ increases in a Ca$^{2+}$-dependent manner when voltage is constant. The corresponding all-points amplitude histograms are plotted in B on a semi-log scale and were constructed from 30-s recordings at each [Ca$^{2+}$]. The dose–response relation for the effect of Ca$^{2+}$ on $\text{Popen}$ at negative voltage ($\text{H80}$ mV) is shown in C. For determination of $\text{Popen}$ see Materials and methods. Each point represents the average of between 7 and 17 patches at each Ca$^{2+}$ concentration tested. Error bars represent SEM.

**Figure 3.** The Ca$^{2+}$ binding affinity of mutant $\Delta \text{E}$ at $\text{H80}$ mV. The mean log ratio of $\text{NPopen}$ in the presence and absence of Ca$^{2+}$ determined from the data shown in Fig. 2. Log ($\text{NPopen}$ / $\text{NPopen}_{\text{min}}$) spans the entire [Ca$^{2+}$] range and is fit (solid line) by Eq. 5 yielding values of $K_{O1} = 0.7$ μM, $K_{C1} = 3.7$ μM, $K_{O2} = 21$ μM, and $K_{C2} = 51$ μM. Also shown is the fit (dashed line) assuming both types of binding sites have the same affinity for Ca$^{2+}$ ($K_o = 1.9$ μM and $K_c = 6.4$ μM). Error bars represent SEM.
Figure 4. Mutation of all three types of Ca\textsuperscript{2+} binding sites eliminates the Ca\textsuperscript{2+} dependence of Popen. (A) Inward K\textsuperscript{+} currents recorded for mutant ΔEFARΔB\textsubscript{(DNS)} at \(-80\) mV and filtered at 10 kHz from a macropatch in the indicated [Ca\textsuperscript{2+}] demonstrate that Popen does not increase in a Ca\textsuperscript{2+}-dependent manner when voltage is constant. The corresponding all-points amplitude histograms are plotted in B on a semi-log scale and were constructed from 30-s recordings. (C) Dose–response relations for the effect of Ca\textsuperscript{2+} on Popen at negative voltage (\(-80\) mV) obtained by plotting the mean log ratio of N\textsubscript{Popen} in the presence and absence of Ca\textsuperscript{2+}. For both mutant ΔEFARΔB\textsubscript{(DNS)} (filled circles) and mutant ΔEFARΔB\textsubscript{(DNS)}, log (N\textsubscript{Popen}/N\textsubscript{Popen\textsubscript{min}}) spans the entire [Ca\textsuperscript{2+}] range but cannot be fitted because Popen does not vary with [Ca\textsuperscript{2+}]. Each point represents the average of between 6 and 8 patches at each [Ca\textsuperscript{2+}] tested. Error bars represent SEM.

Figure 5. The Ca\textsuperscript{2+} binding affinities of the Ca\textsuperscript{2+} bowl site at \(-80\) mV. (A) Inward K\textsuperscript{+} currents recorded from mutant ΔEFAR at \(-80\) mV and filtered at 10 kHz from a macropatch exposed to the indicated [Ca\textsuperscript{2+}] demonstrate that Popen increases in a Ca\textsuperscript{2+}-dependent manner when voltage is constant. The corresponding all-point amplitude histograms are plotted in B on a semi-log scale and were constructed from 30-s recordings as in Fig. 2. The dose–response relation for the effect of [Ca\textsuperscript{2+}] on Popen (left axis) and N\textsubscript{Popen}/N\textsubscript{Popen\textsubscript{min}} (right axis) at negative voltage (\(-80\) mV) is shown in C. Each point represents the average of between 6 and 11 patches at each [Ca\textsuperscript{2+}] tested. Log (N\textsubscript{Popen}/N\textsubscript{Popen\textsubscript{min}}) spans the entire [Ca\textsuperscript{2+}] range but is fit (solid line) by Eq. 6 yielding values of K\textsubscript{C} = 0.88 \(\mu\)M and K\textsubscript{C} = 3.13 \(\mu\)M. Error bars represent SEM.
the intact Ca\textsuperscript{2+} bowl site were then determined from a fit (solid line) with Eq. 6 below, which is analogous to Eq. 5, but represents the case where there is only one type of Ca\textsuperscript{2+} binding site (Horrigan and Aldrich, 2002).

\[
\frac{P_{\text{open}}(Ca)}{P_{\text{open}}(0)} = \frac{(K_C)^4}{(K_O)^4} = C^4,
\]

Of importance here, Eq. 6 contains only the channel’s open- and closed-state Ca\textsuperscript{2+} dissociation constants as free parameters, and in the limit of high [Ca\textsuperscript{2+}], Eq. 6 becomes:

\[
\log \frac{P_{\text{open}}(Ca)}{P_{\text{open}}(0)} = \log \frac{K_C^4}{K_O^4} = 4 \log C.
\]

Thus, the change in log \((P_{\text{open}})\) from 0 to saturating [Ca\textsuperscript{2+}], which is the distance along the vertical axis spanned by the data in Fig. 5 C, depends only on the ratio of the open and closed conformation Ca\textsuperscript{2+} dissociation constants. This means that measuring \(P_{\text{open}}\) precisely at both the top and the bottom of the curve—as we have done here with unitary current recordings—places an important constraint on the fitting. Indeed, because the amplitude of the curve is determined by \(C\), this leaves only one parameter free to determine the shape of the curve, either \(K_C\) or \(K_O\). Thus, in fitting with Eq. 6, the fit is highly constrained, and it is therefore remarkable how well Eq. 6 fits the data (solid line). The fit yields the following Ca\textsuperscript{2+} dissociation constants for the Ca\textsuperscript{2+} bowl (\(K_O = 0.88 \pm 0.06 \mu M; K_C = 3.13 \pm 0.22 \mu M; C = 3.55\)) (see also Table I), and it is of note that they are similar to the \(K_C\) and \(K_O\) values estimated from the \(\Delta E\) data in Fig. 3.

### Ca\textsuperscript{2+} Binding at the RCK1 Site

Similarly, to determine the affinities of the RCK1 site, we examined the effect of Ca\textsuperscript{2+} on the open probability of the mutant (E399N) (D898A/D900A), which we refer to as \(\Delta E\). The two D→A mutations render the Ca\textsuperscript{2+} bowl nonfunctional (Bao et al., 2004). Fig. 6 A shows unitary \(\Delta E\) currents recorded at −80 mV with various [Ca\textsuperscript{2+}] from a patch that contained hundreds of channels. Corresponding amplitude histograms are shown in Fig. 6 B, and the Ca\textsuperscript{2+} dose–response relation we acquired for the \(\Delta E\) channel at −80 mV is shown in Fig. 6 C (open squares). In fact, both \(\Delta E\) and another Ca\textsuperscript{2+} bowl mutation, (D897N/D898N/D900N/D901N) (\(\Delta E\)) (see Table I), were analyzed (Fig. 6 C, closed squares), and both mutations behave similarly. The affinity of the RCK1 site was then estimated by fitting Eq. 6 to the two datasets in Fig. 6 C. The fits yielded similar values (\(K_O = 4.9 \pm 0.6 \mu M; K_C = 23.2 \pm 2.6 \mu M; C = 4.75\)) for \(\Delta E\) and \(\Delta E\) and another Ca\textsuperscript{2+} bowl mutation, (D897N/D898N/D900N/D901N) (\(\Delta E\)) (see Table I). Thus, the RCK1 site binds Ca\textsuperscript{2+} more weakly than does the Ca\textsuperscript{2+} bowl site, both when the channel is open and when it is closed (Ca\textsuperscript{2+} bowl: \(K_O = 0.88 \pm 0.06 \mu M; K_C = 3.13 \pm 0.22 \mu M; C = 3.55\) from Fig. 5), but it has a 36% larger \(C\) value and thus a bigger effect on opening at saturating [Ca\textsuperscript{2+}]. This is illustrated graphically in Fig. 7, where the \(\Delta E\) (closed triangles) and \(\Delta E\) (closed squares) Ca\textsuperscript{2+} dose–response curves are overlaid.

With regard to Figs. 5 and 6, however, it is interesting to note that Eq. 6 fits the data from the \(\Delta E\) channel (Fig. 5) better than it does those from the \(\Delta E\) and \(\Delta E\) channels (Fig. 6 C). That is, the idea represented by Eq. 6 does not appear to be as good an approximation of reality for the RCK1 site as it does the Ca\textsuperscript{2+} bowl site. To try to improve the fit, we have added a cooperativity factor by which the binding at one site influences binding at sites on adjacent subunits. If we call this factor \(f\) and suppose for simplicity that \(f\) is the same for the opened and closed channel, then Eq. 9 below represents this idea (Cox et al., 1997, scheme III and discussion page 269).

\[
\frac{P_{\text{open}}(Ca)}{P_{\text{open}}(0)} = \frac{(1 + 4 K_C^2 (Ca)^2 + 4 K_O^2 f^2 [Ca]^2 + K_C^4 f^4 [Ca]^4)}{(1 + 4 K_C^2 (Ca)^2 + 4 K_O^2 f^2 [Ca]^2 + 4 K_C^4 f^4 [Ca]^4)}
\]

### Table I

**BK\textsubscript{Ca} Channel Ca\textsuperscript{2+} Binding Parameters**

| Binding Site          | Membrane Potential (mV) | \(K_C\) (μM) | \(K_O\) (μM) | \(M\) | \(f\) | \(C\) |
|-----------------------|-------------------------|--------------|--------------|-------|-------|------|
| Ca\textsuperscript{2+} Bowl |                        |              |              |       |       |      |
| \(\Delta E\Delta R\) | −80                     | 3.1 ± 0.2    | 0.88 ± 0.06  |       |       | 3.55 |
| \(\Delta E\Delta R\) | 0                       | 3.1          | 0.88         |       |       | 3.55 |
| RCK1                  |                          |              |              |       |       |      |
| \(\Delta E\Delta B\) | −80                     | 23.2 ± 2.6   | 4.9 ± 0.6    |       |       | 4.75 |
| \(\Delta E\Delta B\) | 0                       | 26.8 ± 3.8   | 5.6 ± 0.8    |       |       | 4.75 |
| \(\Delta E\Delta B\) | −80                     | 13.7 ± 2.3   | 2.8 ± 0.5    | 0.45  | ± 0.1 |      |
| \(\Delta E\Delta B\) | 0                       | 9.4 ± 1.8    | 1.8 ± 0.2    | 0.27  | ± 0.05 |      |
| \(\Delta E\Delta B\) | 0                       | 15.8 ± 3.1   | 2.10 ± 0.4   | 1.8 × 10\textsuperscript{2} | 7.52 |
where \( P \) represents the equilibrium constant for channel opening when the ring is relaxed. \( H \) represents the equilibrium constant for ring expansion when the channel is closed, and no \( \text{Ca}^{2+} \) is bound. \( Q \) represents the factor by which ring expansion favors channel opening, and \( \text{Ca}^{2+} \) binding favors ring expansion. Then, for \( \text{Popen} \) we have:

\[
\text{Popen} = \frac{P(1 + H \text{U}_{\text{Ca}}Q)}{1 + H \text{U}_{\text{Ca}} + P(1 + H \text{U}_{\text{Ca}}Q)},
\]
measured for each high-affinity Ca\(^{2+}\) binding site in Figs. 5 C and 6 C. In Fig. 7 this prediction (dark solid curve) is compared with the \(\Delta E\) data (filled circles). Of most interest, the predicted curve, although similar to the data, does not everywhere overlay the data, but rather it predicts a larger response to Ca\(^{2+}\) than is observed. We might consider two possible reasons for this outcome. The first is that one or the other of the mutations we have used is not completely selective. That is, in addition to eliminating Ca\(^{2+}\) sensing via one type of Ca\(^{2+}\) binding site, a given mutation may also affect Ca\(^{2+}\) binding at the other site. We do not favor this explanation, however, because in order for it to explain the data, the mutation would have to eliminate Ca\(^{2+}\) binding at one site while augmenting it at the other. Although this cannot be ruled out, it seems unlikely. The second potential explanation is that there is negative cooperativity between Ca\(^{2+}\) binding sites, such that their individual influences are naturally less than what is observed when they are combined. Pursuing this idea further we have calculated that a cooperativity factor between the RCK1 and Ca\(^{2+}\) bowl Ca\(^{2+}\) binding sites on the same subunit of 1, when the channel is open (negative cooperativity), and 0.75, when the channel is closed (no cooperativity), could explain this effect (Fig. 7, gray curve).

Do These Results Explain the G-V Shifts with \([Ca^{2+}]\)?
Another question of interest is do the binding affinities we have measured at a single voltage (-80 mV) explain the BK\(_{Ca}\) channel’s sensitivity to Ca\(^{2+}\) over a range of voltages? Fig. 8 A shows the mSlo G-V relation at a series of \([Ca^{2+}]\) fit simultaneously with the BK\(_{Ca}\)-gating model of Horrigan and Aldrich (2002) (the HA model) but modified to include two sets of Ca\(^{2+}\) binding sites, four per set. There were no free parameters in this fit, but rather gating parameters determined from these and previous experiments (Bao and Cox, 2005) were used. The parameters were as follows: \(K_{O1} = 0.88 \mu M; K_{C1} = 3.13 \mu M; K_{O2} = 4.88 \mu M; K_{C2} = 23.2 \mu M; I_{o} = 2e-06; z_{lit} = 0.41 e; V_{h} = 151 mV; V_{m} = 57 mV; Z_{j} = 0.58 e.\) The allosteric factors \(E_{1}\) and \(E_{2}\) were set to 1 to simulate no interaction between voltage-sensor movement and Ca\(^{2+}\) binding at either site. The fit is poor. The model responds to Ca\(^{2+}\) less than is required to move the model G-V

The Two Sites Are Less Than Additive
Can the affinities measured for each binding site in isolation, when combined, explain the effect of Ca\(^{2+}\) when both binding sites are intact? To answer this question we calculated the predicted \(Popen/Popen(0)\) versus \([Ca^{2+}]\) curve for the \(\Delta E\) channel based on the affinities measured for each high-affinity Ca\(^{2+}\) binding site in Figs. 5 C and 6 C. In Fig. 7 this prediction (dark solid curve) is compared with the \(\Delta E\) data (filled circles). Of most interest, the predicted curve, although similar to the data, does not everywhere overlay the data, but rather
relation along with the data. Interestingly, however, when we let $E_1$ and $E_2$ vary freely, that is, we allowed interactions between binding sites and voltage sensors, the fit markedly improved ($E_1 = 1.43; E_2 = 1.73$) (Fig. 8 B). This suggests that voltage-sensor movement may alter Ca\textsuperscript{2+} binding and vice versa.

Voltage Affects Ca\textsuperscript{2+} Binding

To test this hypothesis directly, we repeated the experiments so far described, but changed the voltage from −80 to 0 mV. We reasoned that at −80 mV few voltage sensors would be active (5% or less) (Stefani et al., 1997; Horrigan and Aldrich, 1999, 2002; Bao and Cox, 2005), and thus there would be very little influence of voltage-sensor movement on Ca\textsuperscript{2+} binding. But at 0 mV, where the channels' voltage sensors are active 35% of the time when the channels are open (Horrigan and Aldrich, 1999, 2002; Bao and Cox, 2005), if voltage-sensor movement affects Ca\textsuperscript{2+} binding, some influence of the change in voltage should be observed. Shown in Fig. 9 (A and C) are the $P_{open}(Ca\textsuperscript{2+})/P_{open}(0)$ versus [Ca\textsuperscript{2+}] curves derived from these experiments (open symbols) along with their counterparts determined at −80 mV (filled symbols). Examining first the $\Delta E\Delta R$ channel (Fig. 9 A), we see that its 0- and −80-mV $P_{open}(Ca\textsuperscript{2+})/P_{open}(0)$ versus [Ca\textsuperscript{2+}] curves superimpose. This indicates that voltage-sensor movement does not affect Ca\textsuperscript{2+} binding at the Ca\textsuperscript{2+} bowl, but rather a change in voltage simply slides the $P_{open}$ versus [Ca\textsuperscript{2+}] curve up the $P_{open}$ axis (see Fig. 9 B). Conversely, there is a substantial effect of voltage on Ca\textsuperscript{2+} binding at the RCK1 sites (Fig. 9, C and D). The maximal effect of Ca\textsuperscript{2+} on the open probability of the $\Delta E\Delta B_{(D2A2)}$ channel is ~10-fold larger at 0 mV than it is at −80 mV (Fig. 9 C), and fitting the 0 mV curve in Fig. 9 C with Eq. 6 yields Ca\textsuperscript{2+} dissociation constants of 15.6 ± 2.5 μM and 2.1 ± 0.3 μM ($C = 7.39$), as compared with 23.2 ± 2.6 μM and 4.9 ± 0.6 μM ($C = 4.75$) at −80 mV.

It is not rigorously correct, however, to fit the 0 mV $\Delta E\Delta B_{(D2A2)}$ data in Fig. 9 C with Eq. 6, as an assumption underlying this equation is that $P_{open}$ is never greater than $10^{-2}$. Although this is the case for the $\Delta E\Delta R$ and $\Delta E\Delta B$ channels at −80 mV, as shown in Fig. 9 D, it is not the case for the $\Delta E\Delta B_{(D2A2)}$ channel at 0 mV. Thus, to determine the dissociation constants of the RCK1 sites at 0 mV, we fit the $\Delta E\Delta B_{(D2A2)} P_{open}$ versus [Ca\textsuperscript{2+}] curve in Fig. 9 D with Eq. 14 below, which does not require this assumption.

$$P_{\text{open}} = \frac{M(1+[Ca]/K_C)^4}{(1+[Ca]/K_C)^4 + M(1+[Ca]/K_C)^4}$$ (14)

This yielded (Fig. 9 D, solid curve) $K_C = 15.8 ± 3.1$ μM, $K_O = 2.10 ± 0.4$ μM ($C = 752$), and $M = 1.8 × 10^{-3} ± 0.5 × 10^{-5}$ (see Table 1). Thus, changing the voltage from −80 mV to 0 mV decreases $K_C$ at the RCK1 Ca\textsuperscript{2+} binding site by a factor of 0.7 (23.2→15.8). It decreases $K_O$ by a factor of 0.4 (4.88→2.10), and it increases $C$ by a factor of 1.8. This increase in $C$ makes the efficacy of the RCK1 sites an order of magnitude larger than the efficacy of the Ca\textsuperscript{2+} bowl sites at 0 mV. This is highlighted in Fig. 10, where the 0 mV Ca\textsuperscript{2+} dose-response curves for the two sites are superimposed. Also evident, at 0 mV, as we saw at −80 mV, the $\Delta E$ channel's Ca\textsuperscript{2+} dose-response curve spans a smaller range of open probabilities than is predicted (Fig. 10, dark solid curve) by the combination of the fits to each individual dose-response curve. And again, we can explain this effect by supposing negative cooperativity between the RCK1 and the Ca\textsuperscript{2+} bowl sites in each subunit. A cooperativity factor of 1 when the channel is closed (no cooperativity) and 0.65 when the channel is open (negative cooperativity) produced the best fit (Fig. 10, gray curve).

![Figure 8](image-url) Voltage likely affects the affinity of the BK\textsubscript{Ca} channel for Ca\textsuperscript{2+}. Shown are a series of mSlo1 G-V relations determined at the following [Ca\textsuperscript{2+}]: 0.003, 0.070, 0.130, 0.360, 0.8, 10, and 100 μM and fitted simultaneously with the HA model modified to include two Ca\textsuperscript{2+} binding sites (Bao et al., 2002; Horrigan and Aldrich, 2002). Using values determined from this and previous experiments in our laboratory (Bao and Cox, 2005), the parameters were held as follows: $K_{O1} = 0.88$ μM, $K_{C1} = 3.18$ μM, $K_{O2} = 4.88$ μM, $K_{C2} = 23.2$ μM, $L_0 = 2.2 × 10^{-5}$, $z_O = 0.41$, $V_{01} = 151$ mV, $V_{02} = 27$ mV, and $z_L = 0.58$. In A, the values of allosteric factors $E_1$ and $E_2$ were held to a value of 1 for both Ca\textsuperscript{2+} binding sites A and B. In B, the values of $E_1$ and $E_2$ were allowed to vary. The best fit values of $E_1$ and $E_2$ were 1.43 and 1.73, respectively.
We could explain the effect of voltage on Ca\textsuperscript{2+} binding at the RCK1 site by supposing that as the channel’s voltage sensors move to their active conformation, they alter the affinity of the channel’s RCK1 sites by a factor $E$ (Horrigan and Aldrich, 2002). To estimate $E$, we fit the $P_{\text{open}}$ versus $[\text{Ca}^{2+}]$ curves at both $-80$ mV (open circles) or at $0$ mV (solid circles). Each point represents the average of between 6 and 13 patches at each $\text{Ca}^{2+}$ concentration tested. Shown is the fit (dashed curve) of $P_{\text{open}}/P_{\text{open}}_{\text{min}}$ based on Eq. 6 and previously shown in Fig. 5. The values determined from the fit are: $K_O = 0.88$ μM and $K_C = 3.13$ μM. (B) The mean $P_{\text{open}}$ versus $[\text{Ca}^{2+}]$ relation for mutant $\text{H9004E/H9004R}$ at both 0 and $-80$ mV are well fitted with the HA model using the $\text{Ca}^{2+}$ binding constants determined. The values for the parameters were held as follows: $K_O = 0.88$ μM, $K_C = 3.18$ μM, $L_O = 6.3 \times 10^{-6}$, $z_L = 0.41 e$, $V_{hc} = 151$ mV, $V_{ho} = 27$ mV, $z_J = 0.58 e$, and $E = 1$. (C) The $P_{\text{open}}/P_{\text{open}}_{\text{min}}$ versus $\text{[Ca}^{2+}]$ relation for mutant $\text{H9004E/H9004B}$ (D2A2) is shown for patches held at 0 mV (open circles) or at $-80$ mV (solid circles). Each point represents the average of between 6 and 14 patches at each $\text{Ca}^{2+}$ concentration tested. The $P_{\text{open}}/P_{\text{open}}_{\text{min}}$ versus $\text{Ca}^{2+}$ relations are fitted with Eq. 6. The values of the fit parameters are: $K_O = 2.1$ μM and $K_C = 15.6$ μM. (D) The mean $P_{\text{open}}$ versus $[\text{Ca}^{2+}]$ curves at both $-80$ and $0$ mV in Fig. 9 D simultaneously with the HA model. We held the voltage sensing parameters: $V_{hc}$, $V_{ho}$, $z_J$ to values previously determined for the mSlo channel (Bao and Cox, 2005).

\[ \Delta \Delta E_{\text{B(O2A2)}} = \text{is shown for patches held at 0 mV (open circles) or at } -80 \text{ mV (solid circles). Each point represents the average of between 6 and 14 patches at each } [\text{Ca}^{2+}] \text{ tested. The } P_{\text{open}}/P_{\text{open}}_{\text{min}} \text{ versus } \text{Ca}^{2+} \text{ relations are fitted with Eq. 6. The values of the fit parameters are: } \Delta \Delta E_{\text{B(O2A2)}} \text{ at } -80 \text{ mV, } K_O = 4.9 \text{ μM and } K_C = 23.2 \text{ μM; } \Delta \Delta E_{\text{B(O2A2)}} \text{ at } 0 \text{ mV, } K_O = 2.1 \text{ μM and } K_C = 15.6 \text{ μM. (D) The mean } P_{\text{open}} \text{ versus } [\text{Ca}^{2+}] \text{ relation for mutant } \text{H9004E/H9004B} \text{ is shown for patches held at 0 mV (open circles) or at } -80 \text{ mV (solid circles). Each point represents the average of between 6 and 14 patches at each } [\text{Ca}^{2+}] \text{ tested. Various fits of } \log (P_{\text{open}}/P_{\text{open}}_{\text{min}}) \text{ are superimposed on the data. The fit of } \text{H9004E/H9004R} \text{ (short dashed line) with Eq. 6 yielded values of } K_O = 0.63 \text{ μM and } K_C = 2.28 \text{ μM. The fit of } \Delta \Delta E_{\text{B(O2A2)}} \text{ (long dashed curve) yielded values of } K_O = 1.56 \text{ μM and } K_C = 12.7 \text{ μM. Using the same equation, we simulated the log } (P_{\text{open}}/P_{\text{open}}_{\text{min}}) \text{ versus } \text{Ca}^{2+} \text{ relation (dark solid line) predicted by the affinities determined for each site in isolation. The parameters of the fit were: } K_{O1} = 0.63 \text{ μM, } K_{C1} = 2.28 \text{ μM, } K_{O2} = 1.56 \text{ μM, } K_{C2} = 12.7 \text{ μM, } a = 1, \text{ and } b = 0.65. \text{ Error bars represent SEM.} \]
We held $K_C$ and $K_O$ to the values we determined in this study at $-80 \text{ mV}$. We set $I(0)$ to the value determined by the bottom of the $P_{open}$ versus $[\text{Ca}^{2+}]$ curve at $-80 \text{ mV}$, and we allowed only $E$ to vary. Remarkably, both RCK1 site $\text{Ca}^{2+}$ dose-response curves, $-80$ and $0 \text{ mV}$, could be fitted fairly well with the same parameters with $E$ equal to 6.03 (Fig. 9 D, dotted line).

The value of $E$ estimated in this way, however, is dependent on the voltage-sensing parameters of the model ($V_{ho}, V_{hc}, z_L$ and $z_J$), parameters that we have taken from previous experiments with wild-type mSlo channels. As here, however, we are using the mutant E399N as our background channel. It may be that this mutation alters one or more of these parameters and thereby renders this method inaccurate. Indeed, differences between the mSlo and E399N G-V curves in the absence of $\text{Ca}^{2+}$ (unpublished data) make us think this may be the case. Thus, another approach we have taken to determining $E$ for the wild-type mSlo channel’s RCK1 site is to fit the wild-type channel’s G-V relation as a function of $[\text{Ca}^{2+}]$ with a two-$\text{Ca}^{2+}$ binding site HA model that includes a voltage sensor–$\text{Ca}^{2+}$ binding site interaction factor $E$ for only one of the high-affinity binding sites, the one with lower affinities. That is:

$$P_{gen} = \frac{T_C}{T_C + T_O}$$

where

$$T_C = (1 + K_{C1} + K_{C2} + K_{C1}K_{C2} + J_C(1 + K_{C1} + K_{C2}E + K_{C1}K_{C2}E))^4$$

$$T_O = (1 + K_{O1} + K_{O2} + K_{O1}K_{O2} + J_O(1 + K_{O1} + K_{O2}E + K_{O1}K_{O2}E))^4$$

where

$$L = L(0)e^{\frac{z_F}{RT}V}$$

where

$$J_O = e^{\frac{z_F}{RT}V_{ho}}$$

$$J_C = e^{\frac{z_F}{RT}V_{hc}}$$

We held all parameters but $E$ to values that have been independently determined either here or previously (Bao and Cox, 2005) and allowed only $E$ to vary. The resulting best fit from this approach is shown in Fig. 11. It shows that even with these severe constraints, the two-site HA model with our newly determined $\text{Ca}^{2+}$ binding constants can approximate the shifting of the mSlo channel’s G-V relation as a function of $[\text{Ca}^{2+}]$, and remarkably the fit yields $E = 2.8$, a value that is very similar to the value of $E$ (2.4) estimated independently by Horrigan and Aldrich (2002) from measurements of the

![Figure 11. A modified HA model can explain the effect of $\text{Ca}^{2+}$ on the steady-state gating properties of the BK$_{Ca}$ channel. Shown are series of mSlo1uG G-V relations determined at the following $[\text{Ca}^{2+}]$: 0.005, 0.070, 0.130, 0.360, 0.8, 10, and 100 $\mu \text{M}$ and fit simultaneously with the modified model that includes two types of $\text{Ca}^{2+}$ binding sites, one type interacts with the voltage sensor, and the other type is independent. The data are the same as shown in Fig. 8. The parameters were held as follows: $K_{O1} = 0.88$ $\mu \text{M}$, $K_{C1} = 3.18$ $\mu \text{M}$, $K_{O2} = 4.88$ $\mu \text{M}$, $K_{C2} = 23.2$ $\mu \text{M}$, $L_O = 2.2 \times 10^{-6}$, $z_L = 0.41 e$, $V_{ho} = 151$ $\text{mV}$, $V_{hc} = 27$ $\text{mV}$, and $z_J = 0.58 e$. The value of $E$ coupling voltage sensor activation and $\text{Ca}^{2+}$ binding at one type of site was allowed to vary. Shown is the best fit obtained. The value of $E$ was calculated to be 2.84 ± 0.13.](image-url)
channel’s gating charge movement as a function of voltage at 0 and 70 μM [Ca^{2+}]. Thus, we currently favor this estimate.

**DISCUSSION**

Here, we have measured the Ca^{2+} binding constants of the BK_{ca} channel’s two types of high-affinity Ca^{2+} binding sites. To be as accurate as possible, we used unitary current recordings from patches containing from a few hundred to just a few channels. This allowed us to determine P_{open} over five orders of magnitude. To be as model-independent as possible, as pioneered by Horrigan and Aldrich (2002), we have made measurements at constant voltage and low P_{open}, such that the amplitudes and shapes of the resulting Ca^{2+} dose-response curves were dependent only on the channel’s Ca^{2+} binding parameters. Further, to prevent potential interactions between Ca^{2+} binding sites and voltage sensors from complicating our analysis, our initial experiments were done at −80 mV, where the BK_{ca} channel’s voltage sensors are very seldom active. The essential assumptions we made in fitting our data were as follows: (1) that there is a single conformational change between open and closed that can occur with any number of Ca^{2+} bound (this idea is consistent with a great many single-channel and macroscopic BK_{ca} channel studies and all current models) (McManus and Magleby, 1991; Cox et al., 1997; Cui et al., 1997; Horrigan and Aldrich, 1999, 2002; Horrigan et al., 1999; Rothenberg and Magleby, 1999, 2000; Cox and Aldrich, 2000); and (2) that there are four of each type of high-affinity site. This has been established for the Ca^{2+} bowl (Niu and Magleby, 2002), and given the fourfold symmetry of the channel, it seems likely to be the case for the RCK1 site as well.

Of primary interest, we found that the Ca^{2+} bowl’s dose-response curve at −80 mV could be well fitted by supposing that each Ca^{2+} bowl independently influences opening, and that each site has an affinity of 3.13 ± 0.22 μM when the channel is closed and 0.88 ± 0.06 μM when the channel is open. These values produce a C value of 3.55, which allows us to calculate that each bound Ca^{2+} at a Ca^{2+} bowl decreases the energy difference between open and closed by 3.1 KJ/mol. These numbers may be compared with the previous estimates of Xia et al. (2002), \( K_C = 17.2 ± 4.0 \) μM and \( K_O = 4.6 ± 1.0 \) μM, C = 3.74, which are similar to what we have found, and those of Bao et al. (2002), \( K_O = 3.8 ± 0.2 \) μM and \( K_C = 0.94 ± 0.06 \) μM, C = 4.0, which are higher affinity than what we have found (but see next paragraph). Interestingly, and of relevance here, we have found that Ca^{2+} binding at the RCK1 site is voltage dependent. The Ca^{2+} binding affinities in both the closed and open conformation increased as the voltage was depolarized. Moving the membrane voltage from −80 to 0 mV decreased \( K_C \) from 23.2 ± 2.6 μM to 15.8 ± 3.1 μM and \( K_O \) from 4.9 ± 0.6 μM to 2.1 ± 0.4 μM. This increased C from 4.75 to 7.52. Thus, as the voltage is depolarized, Ca^{2+} ions bind more tightly to the RCK1 site in both the closed and open conformations of the channel, and the factor by which each binding event increases the equilibrium constant for opening increases ∼1.5-fold.

In light of this result, one might suppose that the binding properties of the BK_{ca} channel’s two types of high-affinity Ca^{2+} binding sites will come closer together as the membrane voltage is further depolarized and the RCK1 sites’ Ca^{2+} dissociation constants become progressively smaller. Although we have not done experiments at membrane voltages more positive than 0 mV and therefore cannot here confirm this hypothesis, such an idea could explain why Qian et al. (2006), in experiments with hybrid channels containing differing numbers of functional RCK1 or Ca^{2+} bowl sites, found that channels with either just four Ca^{2+} bowl sites or just four RCK1 sites showed almost identical Ca^{2+} dose-response curves at +50 mV. Further, it may also account, at least in part, for the estimates of Bao et al. (2002) being higher affinity than what we have found here for the RCK1 site, as Bao et al.’s estimates were based on the behavior of the mutant channel’s full G-V relation as a function of Ca^{2+}, and therefore they necessarily took into account P_{open} measurements at high voltage.

We have also observed that the effects of Ca^{2+} binding at each site, when measured individually, sum to more than what is observed when both sites are intact. We are unsure of the cause of this lack of strict independence, but we can explain it by supposing negative cooperativity between the Ca^{2+} bowl and RCK1 sites within the

At the RCK1 site we found the ΔEΔB_{(D2A2)} dose-response curve at −80 mV could be fitted with a \( K_C \) of 23.2 ± 2.6 μM and a \( K_O \) of 4.9 ± 0.55 μM (C = 4.75), which yields a change in the energy difference between open and closed per bound Ca^{2+} of −3.8 KJ/mol. However, in this case the fit was improved by supposing some negative cooperativity between sites. The best fit was achieved with a cooperativity factor of 0.45 ± 0.1, now with \( K_C = 13.7 ± 2.3 \) μM and \( K_O = 2.8 ± 0.5 \) μM. With either method of fitting, however, the RCK1 site has a substantially lower affinity for Ca^{2+} than does the Ca^{2+} bowl in both the closed and in the open conformation. These differences may be compared with the previous estimates of Xia et al. (2002), \( K_C = 17.2 ± 4.0 \) μM and \( K_O = 4.6 ± 1.0 \) μM, C = 3.74, which are similar to what we have found, and those of Bao et al. (2002), \( K_O = 3.8 ± 0.2 \) μM and \( K_C = 0.94 ± 0.06 \) μM, C = 4.0, which are higher affinity than what we have found (but see next paragraph). Interestingly, and of relevance here, we have found that Ca^{2+} binding at the RCK1 site is voltage dependent. The Ca^{2+} binding affinities in both the closed and open conformation increased as the voltage was depolarized. Moving the membrane voltage from −80 to 0 mV decreased \( K_C \) from 23.2 ± 2.6 μM to 15.8 ± 3.1 μM and \( K_O \) from 4.9 ± 0.6 μM to 2.1 ± 0.4 μM. This increased C from 4.75 to 7.52. Thus, as the voltage is depolarized, Ca^{2+} ions bind more tightly to the RCK1 site in both the closed and open conformations of the channel, and the factor by which each binding event increases the equilibrium constant for opening increases ∼1.5-fold.

In light of this result, one might suppose that the binding properties of the BK_{ca} channel’s two types of high-affinity Ca^{2+} binding sites will come closer together as the membrane voltage is further depolarized and the RCK1 sites’ Ca^{2+} dissociation constants become progressively smaller. Although we have not done experiments at membrane voltages more positive than 0 mV and therefore cannot here confirm this hypothesis, such an idea could explain why Qian et al. (2006), in experiments with hybrid channels containing differing numbers of functional RCK1 or Ca^{2+} bowl sites, found that channels with either just four Ca^{2+} bowl sites or just four RCK1 sites showed almost identical Ca^{2+} dose-response curves at +50 mV. Further, it may also account, at least in part, for the estimates of Bao et al. (2002) being higher affinity than what we have found here for the RCK1 site, as Bao et al.’s estimates were based on the behavior of the mutant channel’s full G-V relation as a function of Ca^{2+}, and therefore they necessarily took into account P_{open} measurements at high voltage.

We have also observed that the effects of Ca^{2+} binding at each site, when measured individually, sum to more than what is observed when both sites are intact. We are unsure of the cause of this lack of strict independence, but we can explain it by supposing negative cooperativity between the Ca^{2+} bowl and RCK1 sites within the
same subunit. In fact, all that is required is weak negative cooperativity between sites when the channel is open (b = 0.75 [−80 mV] or b = 0.65 [0 mV]) and no cooperative interaction between sites when the channel is closed. Thus, perhaps as the BK Ca channel opens, a negative interaction between binding sites develops. In contrast to this result, however, in a study of single hybrid BK Ca channels that contained two RCK1 sites and two Ca2+ bowl sites either on the same or on different subunits, Qian et al. (2006) found that there was positive rather than negative cooperativity between binding sites in the same subunit. The reason for these differing conclusions is not clear to us; however, as their study was done at +50 mV and ours at lower voltages, this difference may be the most relevant factor. What we can say, however, is that the Ca2+ binding constants reported by Qian et al. (2006) at +50 mV are not compatible at either site with our Ca2+ dose-response curves recorded at −80 and 0 mV.

Finally, one might ask what is the physical mechanism by which a change in voltage influences Ca2+ binding at the RCK1 sites? And why does this not occur at the Ca2+ bowl sites? We do not yet know the answers to these questions, but our current hypothesis is that the RCK1 sites lie in close proximity to the channel’s voltage-sensing domains, and that as a given voltage sensor moves, it alters the structure of its nearby RCK1 Ca2+ binding site, while having no such interaction at the Ca2+ bowl. An allosteric interaction between the BK Ca channel’s low-affinity Ca2+ binding sites (those disabled by the E399N mutation) and its voltage sensors has already been firmly established (Hu et al., 2001; Cui et al., 1997, Yang and Sachs, 1989; Cui et al., 1997; Horrigan and Ma, 2008), and like the high-affinity RCK1 sites we have investigated here, these low-affinity sites are also thought to reside in the channel’s RCK1 domains. Alternatively, one might suppose that Ca2+ binding is voltage dependent because Ca2+ binds within the electric field of the membrane; however, the RCK1 domains of the channel are thought to be suspended below the channel and thus they are not likely within the membrane’s electric field.

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