Dynamic Equivalent Circuit Model to Estimate State-of-Health of Lithium-Ion Batteries

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ABSTRACT Lithium-ion (Li-ion) batteries have increasingly been used in diverse applications. Accurate estimation of the state of health (SOH) of the Li-ion batteries is vital for all stakeholders and critical in various applications such as electric vehicles (EVs). The electrical equivalent circuit (EEC) 2-RC model is often used to model the battery operation but has not been used to capture the degradation of battery cells over time. This paper uses the 2-RC model to capture the degradation of the Li-ion battery. The proposed model is not only time-dependent but also captures the effect of temperature on battery degradation. The proposed approach estimates the SOH accurately and is also considerably flexible for diverse cells of different chemistry. We further generalize an N-RC model approach to evaluate the SOH of the battery. We compare the proposed model (2-RC) with the 1-RC model, and through numerical results, we show that the 2-RC model outperforms 1-RC and reduces the computational cost significantly. Similarly, the 2-RC model outperforms 3-RC and higher-order circuits. We also show that the proposed approach can capture the battery dynamics better for specific smaller orders of the polynomial (associated with Arrhenius equation) when compared with the 1-RC approach with considerably reduced (up to 60%) root mean square error (RMSE). Lastly, the average testing RMSE for 2-RC is 52.4%.

INDEX TERMS Lithium-ion battery, state-of-health, equivalent circuit model, open circuit voltage.

I. INTRODUCTION

Batteries are ubiquitous in 21st century; from personal computers to residential storage units, from storage for renewable energy sources to high power electric vehicles (EVs), batteries are used as sources of energy and storage. They power medical devices, home appliances and store energy in grids. Use of batteries in EVs is getting popular as the world is facing a high rate of depletion in fossil fuels than its formation. Moreover, with the gain in popularity of EVs, smart grid technology is incorporating EVs in their models for better energy management systems [1], [2]. Therefore, to reduce failure scenarios and the need for better battery monitoring systems is rising and the need to study the degradation of battery is crucial.

Lithium-ion (Li-ion) batteries are gradually becoming the most commonly used type of battery because of their low maintenance, long lifetime, lightweight, high energy density, considerable depth of discharge, wide temperature range, low self-discharge rate, and fast charging capabilities [3]–[5]. Li-ion batteries have diverse applications and are manufactured with various storage capacities and chemistries. Some common chemistries include Lithium Cobalt Oxide (LCO), Lithium Iron Phosphate (LFP), Lithium Manganese Oxide (LMO), Lithium Nickel Cobalt Aluminum Oxide (NCA), and Lithium Nickel Manganese Cobalt Oxide (NMC). These batteries differ in their energy storage capabilities, such as energy density and power density for different applications. Li-ion technology is also entering the realm of backup power system storage because of its long cycle-life at high temperatures, high energy efficiency, and high energy utilization, even at high discharge current rates [6].

Li-ion batteries undergo a continuous degradation process [7]. The irreversible electrochemical changes, such as solid electrolyte interface (SEI) growth during repeated charging and discharging, occur in the battery [8]. Loss of
lithium inventory (LLI) generally results as a product of SEI growth [9]. Ageing can further be due to other reactions such as loss of active material on anode and cathode [9]. The degradation leads to reduced storage capacity and performance, and so using these batteries beyond the end of life (EOL) can lead to catastrophic results, especially in critical applications such as EVs or biomedical applications [10]. Battery management system (BMS) that monitor the health of the battery under safe operating conditions require accurate knowledge of the state of health (SOH) of battery. In order to have an accurate knowledge of the battery’s degradation state, BMS execute SOH estimation algorithms [11].

SOH is generally defined as the percentage of remaining maximum capacity at a particular time compared to the nominal rated capacity of the battery at the time of manufacturing. It is defined mathematically using equation 1,

$$\text{SOH(\%)} = \frac{Q_{\text{max}}}{Q_{\text{nom}}} \times 100\%$$  \hspace{1cm} (1)$$

where $Q_{\text{max}}$ is the maximum capacity of the given cycle, and $Q_{\text{nom}}$ is the rated nominal capacity of the battery. The nominal capacity is defined as the amount of charge delivered by a fully charged battery [12].

A. LITERATURE REVIEW

Numerous methods to estimate the battery’s SOH can be found in the literature. Traditionally, these methods can be divided into two categories: data-driven methods and model-based methods or a combination of both techniques.

In data-driven methods, understanding the electrochemical reactions and their modelling is not necessary and so these methods utilize only the degradation patterns present in the data using large data sets. Various methods such as Gaussian-process based Kalman filter [13]–[15], neural network (NN) [16], [17], fuzzy logic [18], [19], genetic algorithm (GA) [20], support vector machine (SVM) [21], and long short term memory (LSTM) [21], [22], and other data-driven techniques [23]–[25] have been employed for SOH estimation. These methods have high accuracy and are flexible to the changes in SOH. However, as data driven techniques are trained on particular data sets, these techniques are mostly not generalizable to unseen data [11].

The model-based approaches can be further divided into two categories; electrochemical models [26], [27], and equivalent circuit (EEC) models [28]–[30]. Fractional order models (FOM) are closely linked to electrochemical models. They represent the physical changes in the battery such as electrochemical reactions inside the battery [31], [32]. However, the FOM models are generally more complex compared to an integer-order model. Thus, they require more computational power and are generally slow [33]. The electrochemical model can capture the state of the electrode at a given instance. However, this approach has its drawbacks, such as requiring the computation of a large number of complex parameters and thus having a high computational cost and so would not be suitable for real-time applications such as in EVs.

Li-ion batteries are modelled as equivalent circuits comprising basic circuit elements like resistors and capacitors (RC) in the EEC model. Their time dependency can be used to model the parameters of the circuit. An EEC model based on the Thevenin equivalent circuit can be used to study the SOH of the battery as it degrades [34]. There has been extensive research on different EEC models. The two most common EEC models are the 1-RC model and the 2-RC model [11]. Bian et al. [29] proposed a 1-RC model lumped with an Arrhenius constant to factor in the temperature dependency of the battery degradation. The model reduced the number of parameters, but it did not factor in the battery’s dynamics, such as electrochemical polarization and their transients. A 2-RC model can capture the dynamics more effectively [29]. Several techniques are utilized to estimate model parameters such as least-squares fitting [11], [35], multi-objective genetic algorithm [36], and so on. The least-squares fitting is the most straightforward technique and produces a reasonable estimate of the model parameters. Furthermore, cell inconsistency analysis can be done using the Thevenin equivalent circuit [37]. To limit the scope of this article, we will not discuss cell consistency analysis, however, we will keep it as future work.

Transient response of the battery is the response when battery is triggered to a different state from its steady state. During the rest time, the SOH of the battery changes, and the transient response can be used to analyze the difference in the SOH of the battery after discharging [38]. However, as mentioned in [38] the accuracy achieved has an error of 3%. A model which can capture this degradation as well to enhance the accuracy of estimated SOH is a challenge.

Differential methodologies such as incremental capacity analysis (ICA) and differential voltage analysis (DVA) are used to study the degradation of the Li-ion battery [39]–[41]. These peaks shift in terms of amplitude and position with time in ICA peaks indicates degradation of the battery. The peak shifts occur due to battery ageing and failure mechanisms like loss of useful Li-ion [42], [43]. However, these approaches have a few drawbacks, such as requiring accurate charging and discharging over a broader range, and there are also challenges in extracting features from the IC curves [44]. With the help of the IC curve, we can find the range of values for a specific charging/discharging cycle which can help in estimating the SOH of the cycle using a small portion of the data provided [29].

B. CONTRIBUTIONS

This paper proposes a dynamic EEC model that adapts and captures the SOH dynamics over time and can reliably predict degradation in the battery’s health. The model is based on the 2-RC EEC model that uses open-circuit voltage (OCV), which is the function of the state of charge (SOC). The model uses non-linear least squares curve fitting to approximate the parameter of the model which can then be used to estimate
the SOH for a given cycle. To validate the model, numerical tests are performed on the Center for Advanced Life Cycle Engineering (CALCE) dataset provided by the University of Maryland (UMD) College Park and the publicly available National Aeronautics and Space Administration (NASA) Ames Research Center dataset [45].

The paper’s organization is as follows; in Section II, we discuss the modeling of the Li-ion battery using resistors and capacitors. In Section III, we discuss the algorithm’s development and validation to test the model. In Section IV, we evaluate the model using error metrics and compare it with the 1-RC approach. In Section IV-C we discuss a generalized N-RC model-based approach. And in Section IV-A, we discuss the voltage window and ICA peaks. In Section V, we summarize the key advantages, findings, conclusions, and future work.

II. 2-RC EQUIVALENT CIRCUIT MODEL

To model the battery and capture its dynamics, we used an EEC 2-RC model as shown in Figure 1 [46]. As the battery degrades, the rate at which the voltage drops increases. To model this trend against battery capacity, we use our 2-RC model. State of Charge (SOC) of a battery is defined as the quantity of charge stored at a given instant relative to the maximum quantity of charge that can be stored in a particular cycle. Mathematically, this can be written as

\[ \text{SOC} = \frac{Q}{Q_{\text{max}}}, \]  

(2)

where \(Q_{\text{max}}\) is the maximum charge that can be stored which changes as the battery degrades, and \(Q\) is the charge stored at the given instant of that cycle.

A more robust way to define SOC is

\[ \text{SOC} = \text{SOC}_0 + \frac{Q}{Q_{\text{max}}}, \]  

(3)

here we take into account the initial approximate of SOC of the cycle as \(\text{SOC}_0\).

The battery dynamics can be expressed using basic circuit components. The Thevenin based EEC model consists of a self-discharging resistor \(R_0\), RC parallel networks. \(R_p, R_q\) are polarization resistances where \(R_p\) captures electrochemical polarizations and \(R_q\) captures concentration polarization and \(C_p, C_q\) are polarization capacitors to capture the transients [47]. \(R_0\) represents the electrolytic and connection resistance of the Li-ion battery as well [48]. The terminal voltage is \(V\) whereas the current \(I\) is assumed to be positive during the charging phase and negative during the discharging phase of the battery. \(\tau_1\) and \(\tau_2\) are the time constant of the cell.

The OCV is a function of a given SOC and temperature. Equations (4), (5), (6), and (7) are written by applying Kirchhoff’s voltage law (KVL) on Fig 1.

\[ \text{OCV}(	ext{SOC}, T) = V - V_p - V_q - V_o \]  

(4)

\[ V_o = IR_0 \]  

(5)

\[ V_p = V_{p,0} e^{-\frac{t_1}{\tau_1}} + IR_p(1 - e^{-\frac{t_1}{\tau_1}}) \]  

(6)

\[ V_q = V_{q,0} e^{-\frac{t_2}{\tau_2}} + IR_q(1 - e^{-\frac{t_2}{\tau_2}}) \]  

(7)

In equation (4), \(V_p\) and \(V_q\) are the electrochemical polarization voltages. \(V_o\) is the voltage drop across the ohmic resistance. By substituting equations (5), (6), and (7) into equation (4), we get

\[ \text{OCV}(	ext{SOC}, T) = V + (IR_p - V_{p,0}) e^{-\frac{t_1}{\tau_1}} \]  

\[ + (IR_q - V_{q,0}) e^{-\frac{t_2}{\tau_2}} - I(R_o + R_p + R_q) \]  

(8)

The battery’s capacity and performance degrade with temperature \(T\) [49]. The Arrhenius equation for the temperature’s model is represented as \([29], [33]\)

\[ \text{OCV}(	ext{SOC}, T) = e^{k(T_{\text{ref}} - T)} \sum_{k=0}^{m} a_k \text{SOC}^k \]  

(9)

where \(a_k\) are polynomial coefficients, \(E\) is the activation energy, \(T_{\text{ref}}\) is temperature constant and \(R\) is the energy gas constant.

Since the OCV of a battery depends on the SOC and temperature, we combine equations (8) and (9). The combined model of OCV is written as

\[ V = e^{k(T_{\text{ref}} - T)} \sum_{k=0}^{m} a_k \text{SOC}^k \]  

\[ - (IR_p - V_{p,0}) e^{-\frac{t_1}{\tau_1}} \]  

\[ - (IR_q - V_{q,0}) e^{-\frac{t_2}{\tau_2}} - I(R_o + R_p + R_q) \]  

(10)

Here \(\text{SOC}_0\) is the value of SOC at \(t = 0\). The simplified version of the final expression can be written as

\[ V = c_0 \sum_{k=1}^{m} a_k \text{SOC}^k + \frac{Q}{Q_{\text{max}}} + c_1 e^{p_1 \text{SOC}} + c_2 e^{p_2 \text{SOC}} + r, \]  

(11)

where \(p_1, p_2, c_0, c_1, c_2,\) and \(r\) are constants for a given cycle. The mapping of coefficients is shown in Table 1.

III. MODEL TRAINING METHODOLOGY

To obtain an estimate of SOH, we use equation (11) to compute \(Q_{\text{max}}\) which will then be substituted in equation (1). The algorithm to approximate SOH has been summarized in Fig 2. The model assumes that the coefficients \(c_0, c_1, c_2, p_1,\) and \(p_2\) are constant for constant current charge/discharge cycle as
we are using the V-Q profile of one cycle. The coefficients capture the trend and shape of the curve, which is why they are kept constant for one cycle. The parameters for $a_k, \text{ref}$ need to be computed once for the initial cycle. As these constants capture the general shape of the VQ profile. These parameters then remain constant for the remaining cycles. Afterward, only $c_0, c_1, c_2, p_1, p_2, \text{SOC},$ and $Q_{\text{max}}$ are required to compute the SOH. The last cycle is defined by the user as the cycle till which we want to estimate the SOH of battery.

In this type of modeling, a constraint has to be placed on $c_0$ such that $c_0 \in [0.5, 1.5]$ [29]. The results also validate this restriction on $c_0$, as model accuracy decreases outside this range. Likewise, $Q_{\text{max}} \in [Q_{\text{end}}, Q_0]$, where $Q_0$ is the maximum discharge capacity of the cycle, and $Q_{\text{end}}$ is the end capacity of the given charge/discharge cycle.

We train on the initial cycle to compute the value of $a_1, \text{ref}, \ldots, a_k, \text{ref}$. During the initial cycle, we do a 70-30 train-test split. We randomize the data for the initial cycle to avoid over-fitting. This creates a limitation, however, as the accuracy varies according to randomization. To overcome this limitation, we repeat the cycle for many iterations and average out the final value. Moreover, we utilize the ICA curve to check the fitting of the parameters. We compare the ICA curve we obtain from the estimated parameters with the original ICA curve. If the error between the two curves is low we conclude that the fitting for the first cycle is accurate and we can use the values of $a_1, \text{ref}, \ldots, a_k, \text{ref}$ obtained for the rest of the cycles. The evolution of $Q_{\text{max}}$ is computed for every cycle by fitting equation (11) to the V-Q profile for the given cycle. The value obtained is then used to compute SOH from equation (1).

The proposed 2-RC model is compared with the 1-RC model proposed in [29]. For the 1-RC model, equation (11) reduces to

$$V = c_0 \sum_{k=1}^{m} a_k, \text{ref} (SOC_0 + \frac{Q}{Q_{\text{nom}}})^k + c_1 e^{p1Q} + r.$$  (12)

The same algorithm is shown in Fig 2 is used for both the 1-RC model and the 2-RC model. The RMSE for both models are compared for different values of $m$ where $m$ is the polynomial degree.

### IV. VALIDATION AND EVALUATION

We evaluated our algorithm on the UMD CALCE dataset, and NASA Ames Research Center dataset. We performed our simulations in MATLAB using the optimization toolbox. The evaluation criteria and the results are discussed below.

#### A. EVALUATION METRICS

The SOH is computed utilizing the algorithm explained in Fig 2. The estimated SOH is compared with the ground truth provided in the dataset. We then calculate the RMSE defined as

$$\text{RMSE}_{\text{SOH}} = \sqrt{\frac{\sum_{i=1}^{N} (\hat{\text{SOH}} - \text{SOH})^2}{N}}.$$  (13)
where $\text{SOH}$ is the predicted value of SOH for the given cycle, $\text{SOH}_\text{ref}$ is the ground truth, and $N$ is the total number of cycles for a given test dataset. As explained in Section III, the V-Q data for the first cycle is randomized such that values of voltage measured are randomly indexed in the array. We compute the SOH for a different number of iterations and compute an average RMSE of SOH.

Moreover, to further prove the superiority we make use of bayesian information criterion (BIC). BIC is generally used to determine the best model given a certain dataset as it penalizes the model which has too many fitting parameters. BIC is defined as [50]

$$BIC = D \ln (\sigma^2) + (k + 1) \ln(D) \quad (14)$$

where $D$ is the size of the dataset, $k$ is the order of model defined as

$$k = n + m + 1 \quad (15)$$

$n$ is the integer order of RC pair (e.g. 1, 2, …) and $\sigma$ is defined as

$$\sigma^2 = \frac{1}{D-k-1} \sum_{i=1}^{D} (\text{SOH}_m - \text{SOH}_e)^2 \quad (16)$$

We set $D$ as the number of cycles present in the dataset that we are estimating on. A lower BIC score indicates that a certain model is superior.

**B. RESULTS**

In this section, we present the results with two different datasets: the UMD CALCE dataset and the NASA Ames dataset. The validation of the proposed scheme is done with two different datasets to show the generalizability of the proposed methodology.

1) CALCE DATASET

The CALCE dataset contains degradation data of different pouch cell batteries under 20+ test conditions with six different vendors. The cycling dataset has a constant current (CC) and constant voltage (CV) charging profile, and a CC discharging profile. Conditions such as temperature and C-rate were changed for different tests. There were two broad types of tests: cycling tests, and interval tests. In the cycling tests, only a 10 minutes rest period was used before starting the next cycle, whereas, in the interval testing, rest periods of 12 hours and 24 hours were used after each cycle. Table 2 summarizes the test conditions of the CALCE dataset.

To evaluate the proposed algorithm, we used vendor-4 test datasets. The batteries were exposed to different test conditions where discharging C-rate, rest time, and the temperate was varied. The discharging C-rate varied from 0.5C to 1.5C. The temperature varied from 25°C Celsius to 55°C Celsius, and rest time varied from 10 minutes to 24 hours. The cells were all charged until a cut-off voltage of 4.40 V, and the current at the CC stage was 2.25 A. During the discharging phase, the cut-off voltage of these cells was 3.0 V. Fig 3 shows the discharging V-Q curves for Test 1 (25°C Celsius and 0.5C discharge rate). In Fig. 3, it is clear that as the battery ages, the discharging profile changes. The proposed algorithm is applied to the dataset for different polynomial orders for both 1-RC and 2-RC. We compare the results for both EEC models. The result demonstrates that for certain smaller values of $m$, i.e. $m = 5, 6, 7, 8$ the 2-RC model outperforms the 1-RC model. Fig. 4 compares the RMSE for different values of $m$, and for $m = 6, 7, 8$ the 2-RC model can better estimate the SOH. After that, for a higher value of $m$, we see overfitting, and the RMSE increases. The overfitting occurs due to an increase in the order of polynomials which closely follows the trend of the initial cycle for $a_c, a_v$. However, these computed values then do not capture the trend in later cycles. Moreover, a lower value of $m$ saves computational power and time compared to higher-order polynomials.

The proposed methodology is validated over multiple tests with different test conditions on the CALCE vendor-4 dataset. Tests 1, 3, 4, 5, and 6 are used to generate these results. In Fig. 6 where the RMSE is computed for multiple tests (1, 3, 4, 5, and 6) and averaged out. In Table 2, note that the conditions are different for different tests; for tests 1 and 3, the temperature is 25°C Celsius, the discharge rates are 0.5C and 1.5C, respectively, and the rest time is 10 minutes. For tests 4, 5, and 6, the temperature is 35°C Celsius, the discharge rates are 0.5C, 1C, and 1.5C, respectively, and the rest time is 10 minutes. Again we see that $m = 7$ is optimal even when averaged over multiple tests of variable test conditions. To demonstrate how closely does the model fits the ground truth, Fig 7 shows the estimated and measured SOH using the optimal value of $m = 7$ for tests 1 and 4. It is evident that measured and estimated SOHs are in close conformity. The RMSE for test 1 is 0.0535 and for test 4 is 0.0722. For 1-RC, the optimal value of $m$ is 11 or higher, where the error is minimum. However, when we compare the time for the algorithm to run for 1-RC ($m = 11$) and 2-RC ($m = 7$), the 1-RC model requires approximately 6 seconds more in total, which get significant for large datasets.

To further validate we make use of BIC as defined in equation 14. We compute results up till 5-RC models to verify the superiority of our model and the result is shown

### TABLE 2. UMD CALCE dataset test conditions used in this paper.

| Vendor | Test No. | Temperature | C-rate | Rest Time |
|--------|----------|-------------|--------|-----------|
| 1      | 3        | 25          | 1.5    | 10 min    |
| 2      | 5        | 35          | 1.0    | 10 min    |
| 2      | 8        | 45          | 1.0    | 10 min    |
| 2      | 9        | 45          | 1.5    | 10 min    |
| 2      | 12       | 25          | 0.5    | 24 hr     |
| 2      | 15       | 45          | 0.5    | 12 hr     |
| 2      | 21       | 55          | 0.5    | 12 hr     |
| 4      | 1        | 25          | 0.5    | 10 min    |
| 4      | 3        | 25          | 1.5    | 10 min    |
| 4      | 4        | 35          | 1.0    | 10 min    |
| 4      | 5        | 35          | 1.5    | 10 min    |
| 4      | 6        | 35          | 1.5    | 10 min    |
in figure 5. The results verify our claim that the 2-RC model performs best at \( m = 7 \).

2) NASA AMES DATASET

To show the generalizability of the proposed methodology, we test our algorithm on a publicly available dataset from the NASA Ames Research Center [45]. The dataset is generated from NCA cells with a nominal capacity of 2 Ah. In this paper, we utilized cells numbered B0005, B0006, B0007, and B0018. The cycling dataset has a CC and CV charging profile and a CC discharging profile. The cells are all charged until a maximum cut-off voltage of 4.2 V, and the current at the CC stage is 1.5 A. During the CV stage, the cut-off current is 20 mA. However, during the discharging phase, the cut-off voltages of these cells are 2.7, 2.5, 2.2, and 2.5 V, respectively.

To test our algorithm, we use the discharging V-Q profiles shown in Fig. 8 which are similar to the V-Q profiles of the CALCE dataset. We apply the same algorithm described in Section III. Again, we repeat our algorithm for different values of \( m \) and evaluate the results for the 1-RC and 2-RC models illustrated in Fig. 9. For 2-RC at \( m = 5 \), the RMSE is minimum. The RMSE stays low for a few higher values of \( m \) before it starts to increase again. In the 1-RC model, the RMSE continues to decrease for higher values of \( m \) and even performs better than the 2-RC model for \( m \geq 8 \), giving a better estimate of the SOH of the battery at the expense of higher computational cost. Just as observed in the CALCE dataset, the 1-RC model consumes more time than the 2-RC model (approximately 1.5 seconds). Although it looks minimal, that is due to fewer cycles (138/139) in the NASA Ames dataset. For any dataset with a higher number of cycles, the difference will become higher, an observation consistent with the fact that for the CALCE dataset, the difference was around 6 seconds for 1045 cycles. For the 2-RC model, Fig. 10 shows the SOH estimation as a function of cycles with an optimal value of \( m = 5 \) for the three batteries in the NASA Ames dataset. Again, the measured and the estimated SOH
are in solid agreement with each other. The RMSE for SOH estimated for B0005, B0006 and B0007 is 0.7960, 0.5884, and 0.8005, respectively.

C. 3-RC AND N-RC MODEL

During the rest time, the SOH of the battery changes, and transient response can be used to analyze the difference in the SOH of the battery after discharging [38]. It can be assumed that the transient response can be expressed better using an additional RC parallel network. It might be assumed that increasing the RC network in the model will increase the model’s accuracy. In this subsection, we introduce the Thevenin 3-RC EEC model. The addition of an RC parallel network adds a new exponential term and a constant term. Moreover, this approach can be extended to an N-RC model where N represents the number of parallel RC networks. Generalized N-RC equation can be written as

\[ V = A \sum_{k=0}^{m} a_{k, \text{ref}}(\text{SOC}_0 + \frac{Q}{Q_{\text{nom}}} \cdot k) + \sum_{n=1}^{N} c_n e^{P_n Q} + B, \quad (17) \]

where, \( A = e^{\frac{E_r}{T_{\text{ref}}} - \frac{1}{T}} \), \( c_n = -(IR_n - V_{n,0}) \), \( P_n = -\frac{1}{T_n} \), and \( B = I(\sum_{n=0}^{N} R_n) \).

We repeat the same procedure explained in Sections III and IV for \( N = 3 \) for NASA dataset and \( N = 5 \) for UMD dataset to estimate the SOH of the battery. The RMSE with different order of RC models is compared in Fig. 11 and Fig. 12. The RMSE is higher for the 3-RC model compared to both 1-RC and 2-RC as shown in 13. From \( m = 6 \) onwards the 3-RC model overfits.

The assumption that by adding an exponential term, the model will capture the transient response better than 2-RC [51] is not valid in this case. It looks like \( N > 2 \) overfits the data, and the RMSE increases. Moreover, the datasets (both CALCE and NASA) do not have a sampling interval short enough to capture higher-order transients. Therefore, going beyond \( N = 2 \) does not provide a good fit and increases the computational complexity. However, the N-RC model is flexible, and different values of \( N \) can be used depending on the dataset and its sampling intervals. Thus, for CALCE and NASA Ames datasets, the 2-RC model suffices to estimate the SOH of Li-ion batteries.

D. VALIDATION OF 2-RC MODEL

To further evaluate our model and test whether it can predict the SOH of a battery in general, we validate the model using the CALCE vendor-2 dataset. In the vendor-2 dataset, we have three samples for one test, and all are tested under similar conditions (see Table 2). We compute coefficients
This is represented in equation (12). Based on table 3 the average testing RMSE for 2-RC is 52.4%. Lastly, we believe that our model will work on the dynamic dataset. We plan to include analysis of dynamic dataset in our future work.

It is essential to determine the correct order of the polynomial to choose the right value of $m$. We show that higher values of $m$ overfits the data and the RMSE starts increasing. The generalizability of the proposed methodology is shown by validating the model over two different data sets having different types of batteries. The results show that the 2-RC model outperforms 1-RC and N-RC models for $N > 2$.

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