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Phonon quarticity induced by changes in phonon-tracked hybridization during lattice expansion, and its stabilization of rutile TiO$_2$

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Although the rutile structure of TiO$_2$ is stable at high temperatures, the conventional quasiharmonic approximation predicts that several acoustic phonons decrease anomalously to zero frequency with thermal expansion, incorrectly predicting a structural collapse at temperatures well below 1000 K. Inelastic neutron scattering was used to measure the temperature dependence of the phonon density of states (DOS) of rutile TiO$_2$ from 300 to 1373 K. Surprisingly, these anomalous acoustic phonons were found to increase in frequency with temperature. First-principles calculations showed that with lattice expansion, the potentials for the anomalous acoustic phonons transform from quadratic to quartic, stabilizing the rutile phase at high temperatures. In these modes, the vibrational displacements of adjacent Ti and O atoms cause variations in hybridization of 3$d$ electrons of Ti and 2$p$ electrons of O atoms. With thermal expansion, the energy variation in this “phonon-tracked hybridization” flattens the bottom of the interatomic potential well between Ti and O atoms, and induces a quarticity in the phonon potential.

I. INTRODUCTION

Titanium dioxide (TiO$_2$) is of longstanding interest in physics, chemistry, surface science and materials science. It has numerous technological applications including pigments, optical coatings, catalysis, solar cells and gas sensors. Rutile is the stable phase of TiO$_2$ at temperatures below 1800 K, and the two other naturally-occurring phases of TiO$_2$, anatase and brookite, both convert to rutile upon heating. The thermal properties of rutile TiO$_2$ are central for applications that involve heat generation, thermal transport and temperature-driven phase transitions. Nevertheless, even after numerous experimental and theoretical investigations, the stability of the rutile phase at high temperatures remains poorly understood.

The quasiharmonic approximation (QHA) is based on how phonon frequencies change with volume. In the QHA, all shifts of phonon frequencies from their low temperature values are the result of thermal expansion alone. For a lattice expansion of 0.5%, the energies of transverse phonons decrease by 10% to 50% in the QHA, giving Grüneisen parameters as large as 100 for rutile TiO$_2$. In the QHA, many transverse acoustic modes decrease to zero frequency at a lattice expansion of 0.75%, so the QHA predicts a collapse of the rutile structure at temperatures below 1000 K. The QHA does not account for all non-harmonic effects, however. Although the QHA accounts for some frequency shifts, the phonon modes are still assumed to be harmonic, non-interacting, and their energies depend only on the volume of the crystal.

In non-harmonic potentials, phonon-phonon interactions are responsible for pure anharmonicity that shortens phonon lifetimes and shifts phonon frequencies. Anharmonicity competes with quasiharmonicity to alter the stability of phases at high temperatures, as has been shown, for example, with experiments and frozen phonon calculations on bcc Zr.\textsuperscript{22} and the possible stabilization of bcc Fe-Ni alloys at conditions of the Earth’s core.\textsuperscript{23} For PbTe and ScF$_3$, there are recent reports of anharmonicity being so large that both the QHA and anharmonic perturbation theory fail dramatically.\textsuperscript{24,25} These cases are suitable for ab initio molecular dynamics (AIMD) simulations, however, which naturally includes all orders of anharmonicity.\textsuperscript{26-28} The AIMD method should be reliable when the electrons are near their ground states and the nuclear motions are classical.

In this work, we study phonons at high temperatures in rutile TiO$_2$ by neutron inelastic scattering, AIMD, and other methods. We report a remarkable quartic anharmonicity that develops because the hybridization between electron states at Ti and O atoms changes dynamically during atom vibrations, and these changes are highly sensitive to lattice expansion. This “phonon-tracked hybridization” induces the phonon quarticity that is essential for stabilizing the rutile phase at high temperatures, and affects properties such as ferroelectricity and thermal transport.

II. EXPERIMENT

A. Inelastic neutron scattering

Samples were commercial TiO$_2$ powder (Alfa Aesar, Ward Hill, MA) with a rutile phase fraction of at least 99.9%. The sample powder was loaded into a niobium sachet for neutron scattering measurements at high temperatures. Measurements were performed with the ARCS spectrometer at the Oak Ridge National Laboratory, using incident neutron energies of 75 meV.
and 30 meV. A vacuum furnace with niobium radiation shields was used for measurements at 300, 673, 1073, and 1373 K. Furnace backgrounds were measured with empty sample containers at each temperature. Data reduction was performed with the software package DRCS.\textsuperscript{30} The raw data of individual neutron detection events were first binned into scattering angle and energy transfer, $E$, and normalized by the proton current on target. The data were corrected for furnace background and detector efficiency. The data were then rebinned into intensity, $S(Q, E)$, where $\hbar Q$ is the momentum transfer to the sample. This $S(Q, E)$ is averaged over all crystallographic directions, and is a reasonably well-balanced sampling of all phonons in the material.

**B. Results**

Surprisingly, temperature causes a global increase in energy of the entire TA branch. The lowest phonon dispersions formed by the TA branch at 14 meV at 300 K increase significantly in energy at 1373 K, as seen in the $S(Q, E)$ phonon spectra (Fig. 1). There are no dispersions that soften between 2 and 4 Å$^{-1}$, and there are no signs of phonons that collapse to zero frequency. This anomalous thermal stiffening is also apparent in the phonon DOS curves, which were obtained after corrections for multiphonon and multiple scattering using the getdos package.\textsuperscript{31} As shown in Fig. 2(a), peak 1 (centered at 14 meV) exhibits an unusual stiffening as large as 2.7 meV, and it remains sharp. The large stiffening of this DOS peak is even more apparent in measurements with higher energy resolution, using an incident energy of 30 meV (see Fig. 3(a)). On the other hand, as shown in Fig. 2(a) and Fig. 3(a), most other features of the phonon DOS above 20 meV undergo substantial softening and broadening with temperature, in good agreement with the individual phonons measured by Raman spectrometry at high temperatures.\textsuperscript{9,19} It is well-known that rutile TiO$_2$ has a ferroelectric soft mode $A_{2u}$ at the $\Gamma$-point that
stiffens with heating, but the global stiffening of the entire lower-lying TA branch is surprising.

Figure 3(b) presents the DOS calculated with the quasi-harmonic model at 1373 K, showing that contrary to the experimental trend in Fig. 3(a), the first peak in the phonon DOS undergoes a large softening with temperature. Consistent with previous results, our QHA calculations predict that modes in the TA branch soften through zero frequency with the thermal expansion of 1373 K, giving imaginary frequencies in the DOS (shown as negative in Fig. 3(b)) that would destabilize the rutile structure at high temperatures.

### III. CALCULATIONS

#### A. First principles molecular dynamics simulations and techniques for calculating the vibrational spectra

First-principles calculations using the local density approximation (LDA) of density functional theory (DFT) were performed with the VASP package. Projector augmented wave pseudopotentials and a plane wave basis set with an energy cutoff of 500 eV were used in all calculations. Previous work showed that for best accuracy, the Ti pseudopotential should treat the semicore 3s and 3p states as valence, and we took this approach with a similar LDA functional. Our calculated elastic properties, lattice dynamics, and dielectric properties derived from the optimized structure for 0 K, were in good agreement with results from experiment and from previous DFT calculations. Phonon dispersions and phonon DOS spectra were obtained in the quasiharmonic approximation by minimizing the vibrational free energy as a function of volume

\[
F(V,T) = E_0 + \int_{-\infty}^{+\infty} g(\omega) \left( \frac{\hbar \omega}{2} + k_B T \ln(1 - e^{-\hbar \omega/k_B T}) \right) d\omega, \tag{1}
\]

where \(E_0\) is the energy calculated for the relaxed structure at \(T = 0\) K.

First-principles Born-Oppenheimer AIMD simulations for a \(2 \times 2 \times 4\) supercell and a \(2 \times 2 \times 1\) \(k\)-point sampling were performed to thermally excite phonons to the target temperatures of 300 and 1373 K. For each temperature, the system was first equilibrated for 3 ps as an NVT ensemble with temperature control by a Nosé thermostat, then simulated as an NVE ensemble for 20 ps with time steps of 1 fs. Good relaxations with residual pressures below 0.5 GPa were achieved in each calculation that accounted for thermal expansion. The lattice parameters and thermal expansivities determined by the simulations are presented in Table I.

#### 1. Fourier transformed velocity autocorrelation method

Velocity trajectories were extracted from the MD simulation at each temperature, and were then transformed to the corresponding vibrational energy and/or momentum domain. Because the FTVC method does not assume a form for the Hamiltonian, it is a robust tool for obtaining vibrational spectra from MD simulations, even with strong anharmonicity. The phonon DOS is given by

\[
g(\omega) = \sum_{n,b} \int e^{-i\omega t} \langle \vec{v}_{n,b}(t) \cdot \vec{v}_{0,d}(0) \rangle \, dt, \tag{2}
\]

where \(\langle \rangle\) is an ensemble average, and \(\vec{v}_{n,b}(t)\) is the velocity of the atom \(b\) in the unit cell \(n\) at time \(t\). Further
FIG. 4. Diffuse curves are TDEP phonon dispersions below 25 meV at (a) 300 K, and (b) 1373 K, compared with the results from the FTVAC method (red circles). The white curves are phonon dispersions for the quasiharmonicity plus quartic anharmonicity calculated with all $\psi_{ijk}$ set to zero in Eq. 3. In (b), the dispersions are compared to the quasiharmonic dispersions (orange dashed curve) and the single quartic oscillator model (orange triangles). (c) Frozen phonon potential (black) of TA mode at R point with $q = (0.5, 0, 0.5)$ at 1373 K, showing the harmonic component (red) and quartic component (blue). The low temperature potential surface is also shown (dashed black).

TABLE II. Frequencies (meV) of the transverse acoustic modes of rutile at ambient and high temperature, from experiment and from calculations with QHA, MD and TDEP methods

|       | $X$     | $X(0.5, 0.25)$ | $R$     | $Z$     | $Z(0, 0.25)$ | $\Gamma$ | $M$     | $M(0.5, 0.25)$ | $\Lambda$ |
|-------|---------|----------------|---------|---------|--------------|----------|---------|----------------|-----------|
| $T = 300$ K |         |                |         |         |              |          |         |                |           |
| Exp $^a$ | 12.77  | 12.15          | 0       | 12.15  |
| QHA $^b$ | 11.04  | 17.30          | 10.42   | 10.42  | 7.15         | 0        | 9.55    | 5.65           | 9.92      |
| QHA $^c$ | 13.52  | 13.02          | 12.90   | 8.33   | 0            | 9.05     | 12.03   |
| QHA $^d$ | 11.68  | 17.67          | 12.30   | 12.60  | 8.33         | 0        | 9.15    | 7.09           | 12.09     |
| MD $^e$  | 13.60  | 19.88          | 13.49   | 15.36  | 10.36        | 0        | 10.95   | 9.90           | 13.07     |
| TDEP $^f$ | 13.60  | 22.27          | 8.51    | 16.26  | 10.40        | 0        | 11.01   | 6.01           | 9.20      |
| $T = 1373$ K |         |                |         |         |              |          |         |                |           |
| QHA $^d$ | 5.81   | 12.85          | 4.09    | 7.61   | 3.06 $i$     | (>7) $i$| 4.28    | 5.75$i$        | 8.63      |
| QHA $^c$ | 3.13   | 12.59          | 2.02    | 9.07   | 3.78 $i$     | 9.83 $i$| 3.50    | 5.82$i$        | 9.83      |
| MD $^e$  | 15.41  | 19.81          | 16.93   | 18.04  | 13.34        | 0        | 12.27   | 13.78          | 14.28     |
| TDEP $^f$ | 16.91  | 21.12          | 13.53   | 19.63  | 13.35        | 0        | 11.07   | 11.48          | 11.57     |

$^a$ Experimental data from Ref. [8]
$^b$ First principles calculations from Ref. [18]
$^c$ First principles calculations from Ref. [16]
$^d$ First principles calculations from Ref. [16] with ambient temperature but 1% isotropic lattice expansion

projection of the phonon modes onto each $k$ point in the Brillouin zone was performed by computing the phonon power spectrum with the FTVAC method, with a resolution determined by the size of the supercell in the simulation.

2. Temperature-dependent effective potential method

In general, the cubic phonon anharmonicity contributes to both the phonon energy shift and the lifetime broadening, whereas the quartic anharmonicity contributes only to the phonon energy shift.$^{36,37}$ To distinguish the roles of cubic and quartic anharmonicity, the temperature-dependent effective potential (TDEP) method$^{38,39}$ was used. In the TDEP method, an effective model Hamiltonian is used to sample the potential energy surface, not at the equilibrium positions of atoms, but at the most probable positions for a given tempera-
ture in an MD simulation\(^\text{38}\)
\[
H = U_0 + \frac{1}{2} \sum_i m p_i^2 + \frac{1}{2} \sum_{ij \beta} \phi_{ij}^\beta u_i^\beta u_j^\beta + \frac{1}{3!} \sum_{ijk\alpha} \psi_{ijk}^{\alpha} u_i^{\alpha} u_j^{\beta} u_k^{\gamma}
\]
where \(\phi_{ij}\) and \(\psi_{ijk}\) are second- and third-order force constants, \(p\) is momentum, and \(u_i^\alpha\) is the Cartesian component of the displacement of atom \(i\). In the fitting, the “effective” harmonic force constants \(\phi_{ij}\) are renormalized by the quartic anharmonicity. The cubic anharmonicity, however, is largely accounted for by the third-order force constants \(\psi_{ijk}\), and can be understood in terms of the third-order phonon self-energy that causes linewidth broadening.\(^\text{36,40}\)

The resulting Hamiltonian was used to obtain the renormalized phonon dispersions (TDEP spectra) accounting for both the anharmonic shifts \(\Delta\), and broadenings \(\Gamma\), of the mode \(\tilde{q}j\). These are derived from the real and imaginary parts of the cubic self-energies \(\Sigma^{(3)}\), respectively.\(^\text{36}\)

\[
\Delta(\tilde{q}j; \Omega) = \frac{18\pi}{h^2} \sum_{\tilde{q}_1, \tilde{q}_2} |V(\tilde{q}j; \tilde{q}_1, \tilde{q}_2)|^2 \Delta(\tilde{q}_1 + \tilde{q}_2 - \tilde{q}) \\
\times \left[ \frac{1}{n_1 + n_2 + 1} \frac{1}{\Omega - \omega_1 - \omega_2} - \frac{n_1 + n_2 + 1}{\Omega + \omega_1 + \omega_2} - \frac{n_1 + n_2}{\Omega + n_1 - n_2} \right]
\]

\[
\Gamma(\tilde{q}j; \Omega) = \frac{18\pi}{h^2} \sum_{\tilde{q}_1, \tilde{q}_2} |V(\tilde{q}j; \tilde{q}_1, \tilde{q}_2)|^2 \Delta(\tilde{q}_1 + \tilde{q}_2 - \tilde{q}) \\
\times \left[ \frac{(n_1 + n_2 + 1) \delta(\Omega - \omega_1 - \omega_2)}{\Omega + n_1 - n_2} + 2(n_1 - n_2) \delta(\Omega + \omega_1 - \omega_2) \right]
\]

where \(\Omega\) is the renormalized phonon frequency and \(\varphi\) denotes the Cauchy principal part. The \(V(\cdot)\)'s are elements of the Fourier transformed third order force constants \(\psi_{ijk}\) obtained in the TDEP method. The \(\Delta(\tilde{q}_1 + \tilde{q}_2 - \tilde{q})\) ensures conservation of momentum.

### B. Crystal orbital Hamilton population method

The Crystal Orbital Hamilton Population Method (COHP) projects plane waves to local orbital basis functions and is used to partition the band-structure energy into the bonding, nonbonding and antibonding interactions between two atoms. COHP provides a semiquantitative interpretation of the net bonding characteristics.

In this work, COHP spectra were calculated with the package Local-Orbital Basis Suite Towards Electronic-Structure Reconstruction (LOBSTER).\(^\text{41,42}\) The phonon displacement patterns were generated in a \(2 \times 2 \times 4\) supercell with a \(8 \times 8 \times 4\) \(k\)-point sampling according to the eigenvectors of the mode. Self-consistent wavefunctions were then computed and projected onto a local basis of Slater type orbitals with proper orthonormalization, giving the COHP spectra of the system. Since negative values of the COHP suggest bonding contributions, –COHP spectra are presented, following convention.

### C. Results

As shown in Fig. 2(b), the neutron-weighted DOS spectra calculated with FTVCAC method reproduced the thermal shifts and broadenings observed in the experimental DOS of Fig. 2(a). In particular, upon heating to 1373 K, an anomalous softening of peak 1 by 2.1 meV was obtained.

Figure 4 shows the vibrational energies of the TA branch, calculated by the FTVCAC method with AIMD trajectories. From 300 to 1373 K, the TA branch increases in energy by an average of about 2.1 meV. Especially for this TA branch, Fig. 4(b) shows an enormous discrepancy of phonon energies between the MD calculation and the QHA (orange dashed line) at 1373 K. The unstable phonon modes predicted by the QHA are fully stable in the AIMD simulations at high temperatures, however.

Using the same MD trajectories as for the FTVCAC method, the calculated TDEP dispersions agree well with the FTVCAC results as shown in Fig. 4(a), and also in Table II. (The full TDEP dispersions are shown in the Supplemental Material.)\(^\text{43}\) The cubic anharmonicity of rutile TiO\(_2\) is strong for phonons at energies above 25 meV\(^\text{19}\) causing broadening of the phonon DOS of Fig. 2 and broadening of the dispersions.\(^\text{43}\) Nevertheless, at 1373 K the TA modes below 20 meV have only small linewidth broadenings. Furthermore, they are close in energy to those calculated if all \(\psi_{ijk}\) are set to zero in Eq. 3, showing the dominance of quartic anharmonicity and the small cubic anharmonicity of the TA modes.

### IV. DISCUSSION

#### A. Phonon quarticity of TA branch

For more details about the anomalous anharmonicity of the TA modes, the frozen phonon method was used to calculate potential energy surfaces for specific phonons, as in Fig. 4(c). At 300 K the potential energy of the TA mode at the \(R\)-point is nearly quadratic, with a small quartic part. With the lattice expansion characteristic of 1373 K, the potential energy curve transforms to being nearly quartic.

In fact, for all modes in the TA branch that were evaluated by the frozen phonon method, the potential energy surface develops a quartic form with lattice expansion (see Supplemental Material).\(^\text{43}\) Even more interesting behavior occurs along the directions of \(M\)–\(A\), \(\Gamma\)–\(Z\) and \(\Gamma\)–\(X\), where the potential energy surface develops a...
FIG. 5. (a) Displacements of atoms for the TA mode at the R-point in the (1-10) plane. Light blue spheres are Ti atoms, and O atoms are red. Arrows depict distortions of the structural units (dashed rhombuses). The rotational movements of structures, or the “ring” patterns, are indicated with circled arrows. (b) ELF isosurface of a “ring” shown in (a) with the value of 0.3. The ELF increase is apparent in the bond of shorter distance owing to the ring displacement. The ELF is the probability measure of finding an electron at a location given the existence of neighboring electrons. It ranges from 0 (no electron) to 1 (perfect localization). (c) COHP analysis of Ti–O bonds for equilibrium lattice parameter at \( T = 0 \text{K} \) (0%), and for linear expansions of 1% and 2%. Shown in color are –COHP results for the same structures with the phonon of panel (a) having 0.14 Å normal displacements of Ti atoms. Curves for 1% and 2% expansion are offset by 0.6 and 1.2.

Landau-type form, with negative curvature at zero displacement, but a positive quartic shape at large displacements. (The height of the energy barrier between the two minima is lower than \( k_B T \), however.) For a quantum quartic oscillator, the vibrational frequency stiffens with temperature owing to the increasing spread between the energy levels.\(^{25,44}\) We assessed a high temperature behavior by assigning Boltzmann factors to the different oscillator levels derived from frozen phonon potentials, giving the energies of the quartic TA modes at 1373 K. As shown in Fig. 4(b), they are reasonably close to the FTVAC and TDEP results.

**B. Phonon-tracked hybridization and its change with thermal expansion**

The patterns of atom displacements in the anomalous modes at \( \Gamma, R \), and along \( Z-\Gamma \), \( \Gamma-M \), and \( M-A \) were identified, and those for the R point in Fig. 5(a) are typical. In these anomalous modes, the O atoms were approximately stationary, and each O atom has a Ti neighbor that moves towards it and another Ti neighbor that moves away from it by approximately the same amount. These modes have “ring” patterns in which displacements of Ti atoms rotate a structural unit, and all the O atoms see approximately the same change in their Ti neighborhood. In the positive and negative displacements of these modes, the O atoms show an accumulation of charge in the Ti–O bond of shorter distance and a depletion in the bond of longer distance, as indicated by a much higher value of the electron localization function (ELF)\(^{45}\) for the short bond shown in Fig. 5(b).

We calculated the “bond-weighted” electron DOS by partitioning the band structure energy into bonding and no-bonding contributions and obtaining the crystal orbital Hamilton population (COHP) spectrum\(^{41,42}\) of rutile with different lattice parameters in a \( 2 \times 2 \times 4 \) supercell. Figure 5(c) shows the COHP spectrum of the bonds formed by the Ti 3\(d\) and O 2\(p\) orbitals between 5.5 and 3.5 eV below the Fermi energy. With lattice expansion (of 1% or 2%), these bonding states become less favorable, and their COHP spread narrows. Also shown in color in Fig. 5(b) is the COHP with a frozen phonon mode at the R-point having 0.14 Å displacements of Ti atoms. On the scale of thermal energies, the broadening effect from the phonon changes considerably with lattice expansion. For the equilibrium lattice parameter (labeled “0%”), bonding states at both the top and bottom of the Ti 3\(d\) – O 2\(p\) band are shifted upwards by the phonon. With larger lattice parameter, however, the changes take place mostly in the states at the bottom of the band, which broadens the COHP spectra and helps to lower the bonding energy. Additional bonding states also appear near \( -3 \text{ eV} \). The overall effect is that the potential energy is relatively insensitive to small displacements, and the phonon potential has a much flatter bottom with 1% lattice expansion as shown in Fig. 4(c). For a 2% linear expansion, a Landau-type phonon potential evolves, with local minima away from zero displacement owing to the spread of states to the lowest part of the band.

The effect can be understood by adapting a hard sphere model for the chain of -Ti-O-Ti-O- atoms along the direction “A” or around the “ring” units in the phonon displacement pattern in Fig. 5(a). With an increase in lattice parameter, the longer Ti–O bond makes a smaller contribution to the interatomic force during its vibrational cycle. The shorter Ti–O bond gives a stronger hybridization of Ti 3\(d\) – O 2\(p\) orbitals as the Ti atom moves.
The hybridization in the Ti–O bond is very sensitive to interatomic distance, much as has been noticed in the ferroelectric distortion of BaTiO$_3$. For rutile TiO$_2$, however, the hybridization follows the atom displacements in thermal phonons (instead of a displacive phase transition), and this “phonon-tracked hybridization” changes with lattice parameter. It provides a source of extreme phonon anharmonicity, but also provides thermodynamic stability for rutile TiO$_2$. It may occur in other transition metal oxides that show unusual changes of properties with lattice parameter or with structure, and such materials may be tunable with composition or pressure to control this effect. Besides altering thermodynamic phase stability, properties such as ferroelectricity and thermal transport will be affected directly.

V. CONCLUSION

Several inter-dependent methods proved useful for assessing the anharmonic phonon dynamics of rutile TiO$_2$. Ab initio methods of molecular dynamics, temperature-dependent effective potential, and frozen phonons gave accurate accounts of the thermal stiffening of the TA phonons that was measured by inelastic neutron scattering on rutile TiO$_2$. These methods avoided the structural instability predicted by the quasiharmonic approximation (QHA). With thermal expansion, many acoustic modes were unstable in the QHA, as observed previously. From AIMD simulations and frozen phonon calculations, it was found that when the rutile structure undergoes thermal expansion, a hybridization between Ti and O atoms gives low-energy electron states when the Ti and O atoms are in closest proximity during their vibrations. This phonon-tracked hybridization flattens the bottom of the potential of the anomalous phonon modes, giving quartic potentials that stabilize the rutile structure at high temperatures.

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