DEEP INFRARED ZAMS FITS TO BENCHMARK OPEN CLUSTERS
HOSTING δ SCUTI STARS

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ABSTRACT

This research aims to secure precise distances for cluster δ Scutis in order to investigate their properties via a $VI$ Wesenheit framework. Deep $JHK_s$ colour–colour and ZAMS relations derived from $\approx 700$ unreddened stars featuring 2MASS photometry and precise Hipparcos parallaxes ($d \lesssim 25$ pc) are applied to establish distances to several benchmark open clusters that host δ Scutis: Hyades, Pleiades, Praesepe, α Persei, and M67 ($d = 47 \pm 2, 138 \pm 6, 183 \pm 8, 171 \pm 8, 815 \pm 40$ pc). That analysis provided constraints on the δ Sct sample’s absolute Wesenheit magnitudes ($W_{VI,0}$), evolutionary status, and pulsation modes (order, $n$). The reliability of $JHK_s$ established cluster parameters is demonstrated via a comparison with van Leeuwen (2009) revised Hipparcos results. Distances for 7 of 9 nearby ($d \leq 250$ pc) clusters agree, and the discrepant cases (Pleiades & Blanco 1) are unrelated to (insignificant) $T_K - (J - K_s)$ variations with cluster age or iron abundance. $JHK_s$ photometry is tabulated for $\approx 3 \times 10^3$ probable cluster members on the basis of proper motions (NOMAD). The deep $JHK_s$ photometry extends into the low mass regime ($\approx 0.4M_\odot$) and ensures precise ($\lesssim 5\%$) ZAMS fits. Pulsation modes inferred for the cluster δ Scutis from $VI$ Wesenheit and independent analyses are comparable ($\pm n$), and the methods are consistent in identifying higher order pulsators. Most small-amplitude cluster δ Scutis lie on $VI$ Wesenheit loci characterizing $n \geq 1$ pulsators. A distance established to NGC 1817 from δ Scutis ($d \approx 1.7$ kpc) via a universal $VI$ Wesenheit template agrees with estimates in the literature, assuming the variables delineate the $n \geq 1$ boundary. Small statistics in tandem with other factors presently encumber the use of mmag δ Scutis as viable distance indicators to intermediate-age open clusters, yet a $VI$ Wesenheit approach is a pertinent means for studying δ Scutis in harmony with other methods.

Subject headings: δ Scuti variables — Hertzsprung-Russell and colour-magnitude diagrams — infrared: stars — open clusters and associations: general.

1. INTRODUCTION

δ Scutis are unique among standard candles of the classical instability strip for permitting the determination of distances to population I and II environments from a single $VI$ Wesenheit calibration. SX Phe and other metal-poor population II δ Scutis lie toward the short-period extension of the Wesenheit ridge characterizing population I δ Scutis (Fig. 3 in Majaess et al. 2010, see also Petersen & Høg 1998). That presents an opportunity to bridge and strengthen the distance scales tied to globular clusters, open clusters, nearby galaxies, and the Galactic center where such variables are observed (McNamara et al. 2000, 2007; Poleski et al. 2010; Majaess et al. 2010). To that end the present research examines δ Sct calibrators associated with benchmark open clusters via a $VI$ Wesenheit framework, an analysis which relies on the establishment of precise cluster distances and multiband photometry ($VIJHK_s$).

In this study, infrared colour–colour and ZAMS relations are constructed from unreddened stars in close proximity to the Sun with precise Hipparcos parallaxes (22). The relations are subsequently employed to establish parameters for five benchmark open clusters which host δ Scutis, namely the Hyades, Pleiades, Praesepe, α Persei, and M67 (22). Cluster membership provides constraints on the absolute Wesenheit magnitudes ($W_{VI,0}$), evolutionary status, and pulsation modes (order, $n$) for the δ Scutis (33). An independent determination of the cluster parameters is pursued since the objects form the foundation of the open cluster scale and yet their distances are uncertain. Most notably the Hipparcos distance to stars in the Pleiades is $d = 120.2 \pm 1.9$ pc (van Leeuwen 2009a), whereas HST observations imply $d = 134.6 \pm 3.1$ pc (Soderblom et al. 2005). Likewise, four Hipparcos-based distances cited in the literature for α Persei disagree (Table 1). In [33] a Wesenheit analysis...
(VI) is shown to be a viable means for investigating δ Scutis. Lastly, the distance to NGC 1817 is evaluated via a universal Wesenheit template using new VI photometry acquired from the Abbey Ridge Observatory (ARO, Lane 2007; Turner et al. 2009a) for the cluster’s numerous δ Scutis (§).

2. JHK_s INTRINSIC RELATIONS

Intrinsic colour-colour and ZAMS relations are derived from JHK_s photometry for A, F, G, K, and M-type stars that feature precise parallaxes (d \( \lesssim \) 25 pc). The infrared photometry and parallaxes are provided via the 2MASS and Hipparcos surveys (Perryman & ESA 1997; Cutri et al. 2003; Skrutskie et al., 2006). 2MASS photometry may be saturated for nearby stars, yet reliable data are available for fainter stars of late spectral type. The photometric uncertainties thus increase for brighter early-type stars (Fig. 1), which are already undersampled owing to the nature of the initial mass function. Spurious data deviating from the evident intrinsic functions were excluded.

\[ \frac{M_J}{(J - H)_0} \text{ and } \frac{M_J}{(J – K_s)_0} \] colour-magnitude diagrams for the calibration are presented in Fig. 1 (red dots). The latter passband combination exhibits smaller uncertainties. \( (J – H)_0/(H – K_s)_0 \) and \( (J – K_s)_0/(H – K_s)_0 \) colour-colour diagrams are likewise shown in Fig. 1 (red dots). Infrared relations offer advantages over those founded on \( UBV \) photometry owing to the mitigated impact of chemical composition (§2.1, Fig. 3), differential reddening, and total extinction.

Colour-magnitude and colour-colour diagrams were assembled for the target clusters by obtaining 2MASS photometry for members on the basis of proper motions (Figs. 1). The Naval Observatory Merged Astrometric Dataset (NOMAD, Zacharias et al. 2004) features proper motion data for the fields inspected. JHK_s photometry for \( \sim \) 3 \( \times \) 10^6 probable clusters members were tabulated, and the list includes previously unidentified members. That sample shall be made available online via the Centre de Données astronomiques de Strasbourg. Photometry for the brighter stars may be saturated, as noted earlier, while lower mass members are catalogued despite being near the faint-limit of the 2MASS survey. High-precision multi-epoch JHK_s data for M67 is available from Nikolaev et al. (2001); see also Sarajedini et al. (2009).

Reddenings for the target clusters were secured by shifting the intrinsic colour-colour relations to the observed data (Fig. 1). JHK_s extinction laws were adopted from Bonatto et al. (2008) and references therein. The distance to a cluster follows by matching the ZAMS to the observed data for the reddening established by the intrinsic colour-colour relations. Precise results were obtained because the trends for late-type stars in JHK_s colour-magnitude and colour-colour diagrams provide excellent anchor points for fitting ZAMS and intrinsic relations (Figs. 1, 2). \( J - K_s \) and \( J - H \) were observed to remain nearly constant and become bluer with increasing magnitude \( M_J \gtrsim 6 \) for low mass main-sequence stars beginning near spectral type M (Figs. 1, 2 see also Sarajedini et al. 2009 and references therein), and a sizable separation exists between main-sequence and evolved M-type stars in the JHK_s colour-colour diagram (see also Straizys & Laugalys 2009). Turner (2010b) developed intrinsic JHK_s functions to describe early-type stars (\( \lesssim K0 \)) via an alternate approach.

Distances obtained for the benchmark clusters examined are summarized in Table I.

2.1. AGE AND METALLICITY DEPENDENCIES

The JHK_s distances agree with van Leeuwen (2009a) Hipparcos results for 7 of 9 star clusters within 250 pc (Table I). The distance determined here to the Pleiadesfavours the HST estimate rather than that established by Hipparcos (Table I, § Soderblom et al. (2005) (& others) argue that the Hipparcos distance to the Pleiades is erroneous. Conversely, the reliability of the ZAMS dis-

\[ \text{Fig. 1.— Deep 2MASS } JHK_s \text{ colour-magnitude and colour-colour diagrams for the calibration (red dots) and Praesepe star cluster (black dots). Likely members of the Praesepe were selected on the basis of proper motions (NOMAD). The resulting parameters are } E(J – K_s) = 0.025 \pm 0.015 \text{ and } d = 183 \pm 8 \text{ pc.} \]
to the Pleiades has been questioned owing to the possible neglect of colour-$T_e$ variations with stellar age and chemical composition. The matter is now investigated.

An age-luminosity effect has been proposed as a possible source for the disagreement between the ZAMS and Hipparcos distance to the Pleiades. That hypothesis is not supported by the infrared distances established here. The Hyades, Praesepe, and α Persei clusters bracket the discrepant cases of the Pleiades and Blanco 1 in age (Table 1). $JHK_s$ and van Leeuwen (2009a) Hipparcos distances to the former clusters are in broad agreement (Table 1). The comparatively nearby ($d \leq 250$ pc) open clusters IC 2602, NGC 2451, IC 2391, and Coma Ber were investigated to bolster the case, but proved more difficult to assess. The Hipparcos distance to the Pleiades implies that the cluster’s ZAMS is a sizable $\pm 0.4$ below the faintest calibration stars (Fig. 1) where the photometric uncertainties are minimized, $M_J/(J-K_s)_0$. The Hipparcos zero-point for the Pleiades is inconsistent with a $M_J/(J-K_s)_0$ ZAMS calibration (Fig. 1) which features stars of differing age, chemical composition, and peculiarities.

The clusters in Table 1 exhibiting discrepant distances are not correlated with iron abundance. That supports Alonso et al. (1990) and Percival et al. (2005) assertion that $J - K_s$ is relatively insensitive to metallicity over the baseline examined. Percival et al. (2005) suggested that $J - K_s$ may exhibit a marginal dependence on metallicity, but cautioned that the errors are sizable and the correlation coefficient is consistent with zero. The impact of a marginal $T_e - [\text{Fe/}\text{H}] - (J-K_s)$ dependence appears insignificant since stars belonging to the clusters examined display near solar iron abundances (Mermilliod et al. 1997, van Leeuwen 1999, their Table 1). 270 calibration stars (Fig. 1) featured in Soubiran et al. (2010) PASTEL catalogue of stellar atmospheric parameters exhibit a peak distribution near $[\text{Fe/}\text{H}] \simeq -0.05$, which is analogous to or inappreciably less than members of the Pleiades ($[\text{Fe/}\text{H}] = -0.039 \pm 0.014, +0.03 \pm 0.05, +0.06 \pm 0.01$, Taylor 2008, Soderblom et al. 2009, Paunzen et al. 2010). Colours for calibrating stars (Fig. 1) in PASTEL were plotted as a function of effective temperature and metallicity (Fig. 3) with $j$ and $[\text{Fe/}\text{H}]$ are model dependent).

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### Table 1: Distances to Benchmark Open Clusters

| Cluster   | HIP (M97) | HIP (R99) | HIP (V99) | HIP (V09) | $JHK_s$ | HST |
|-----------|-----------|-----------|-----------|-----------|---------|-----|
| M67       | ⋯         | ⋯         | ⋯         | ⋯         | $815 \pm 40$ pc | ⋯   |
| Hyades    | ⋯         | ⋯         | ⋯         | ⋯         | $46.45 \pm 0.50$ pc | $47 \pm 2$ pc | $48.3 \pm 2.0$ pc |
| Praesepe  | $177.0 \pm 10.3$ pc | $180.5 \pm 10.7$ pc | $180$ pc | $181.6 \pm 6.0$ pc | $183 \pm 8$ pc | ⋯ |
| Pleiades  | $116.3 \pm 3.3$ pc | $118.2 \pm 3.2$ pc | $125$ pc | $120.2 \pm 1.9$ pc | $138 \pm 6$ pc | $134.6 \pm 3.1$ pc |
| α Persei  | $184.2 \pm 7.8$ pc | $190.5 \pm 7.2$ pc | $170$ pc | $172.4 \pm 2.7$ pc | $171 \pm 8$ pc | ⋯ |
| Coma Ber* | $88.2 \pm 1.7$ pc | $87.0 \pm 1.6$ pc | $86$ pc | $86.7 \pm 0.9$ pc | $85 \pm 6$ pc | ⋯ |
| Blanco 1  | $252.5 \pm 31.1$ pc | $263 \pm 31$ pc | $190$ pc | $207 \pm 12$ pc | $240 \pm 10$ pc | ⋯ |
| IC 2391*  | $147.5 \pm 5.4$ pc | $146.0 \pm 4.7$ pc | $140$ pc | $144.9 \pm 2.5$ pc | $134 \pm 13$ pc | ⋯ |
| IC 2602*  | $146.8 \pm 4.7$ pc | $152 \pm 3.7$ pc | $155$ pc | $148.6 \pm 2.0$ pc | $147 \pm 14$ pc | ⋯ |
| NGC 2451* | ⋯         | $188.7 \pm 6.8$ pc | $220$ pc | $183.5 \pm 3.7$ pc | $189 \pm 15$ pc | ⋯ |

Notes: Hipparcos (HIP) distances from Mermilliod et al. (1997, M97), Robichon et al. (1999a, R99), van Leeuwen (1999, V99), and van Leeuwen (2009a, V09). HST distances to the Hyades and Pleiades from van Altena et al. (1997) and Soderblom et al. (2009). $JHK_s$ results from this study. Clusters highlighted by an asterisk were more difficult to assess ($JHK_s$). Iron abundances and age estimates for the clusters are tabulated in Mermilliod et al. (1997) and van Leeuwen (1999).
Fig. 2.— Deep 2MASS $JHK_s$ colour-magnitude diagrams for M67, Hyades, Praesepe, Pleiades, and α Persei star clusters. The clusters feature a common ZAMS morphology in the infrared. The δ Scutis examined in §3 (red dots) may be evolved (Hyades/Praesepe), blue stragglers (M67), or occupy the binary / rapid rotator sequence (Pleiades).

forthcoming VVV survey [Artigau et al. 2009, 2010; Minniti et al. 2010], whereas brighter stars could be observed as part of the AAVSO’s IR photometry program (Henden 2002; Templeton 2009).

In sum, neither variations in iron abundance or stellar age readily explain the discrepancies between the $JHK_s$ ZAMS and Hipparcos distances (Table 1). It is emphasized that the problematic cases (the Pleiades & Blanco 1) constitute the minority (Table 1). Note that the four published Hipparcos distances to Blanco 1 exhibit a sizable 20% spread (Table 1, see also α Persei). Further research is needed, and the reader should likewise consider the interpretations of Mermilliod et al. (1997), Robichon et al. (1999b), Soderblom et al. (2005), and van Leeuwen (2009a,b).

3. CLUSTER δ SCUTIS

3.1. VI PHOTOMETRY

The cluster δ Scutis examined are summarized in Table 2, along with references for their VI photometry. Certain sources feature I-band photometry not standardized to the Cousins system (e.g., Mendoza 1967). Additional observations for the δ Scutis were obtained via the AAVSO’s Bright Star Monitor (BSM 2) and the Naval Observatory’s Flagstaff Station (NOFS) (Table 2). The BSM features an SBIG ST8XME CCD (fov: 127′ × 84′) mounted upon a 6-cm wide-field telescope located at the AstroKolhkoz telescope facility near Cloudcroft, New Mexico. The AAVSO observations are tied to Landolt (1983, 1992) photometric standards according to precepts outlined in Henden & Kaitchuck (1990) (see also Henden & Munari 2008).

VI photometry is used since LMC and Galactic δ Scutis follow VI Wesenheit relations which vary as a function of the pulsation order $n$ (Fig. 4; Poleski et al. 2010; Majaess et al. 2010), thereby enabling constraints on that parameter for target δ Scutis at common or known distances (see §3.2). Furthermore, the author has advocated that RR Lyrae variables and Cepheids—which partly form the basis for the calibration used in §3.2—obey VI Wesenheit and period-colour relations which are comparatively insensitive to metallicity (Majaess et al. 2008, 2009a; Majaess 2009, 2010a,b, see also Bono & Marconi 1999; Udalski et al. 2001; Bono 2003; Pietrzyński et al. 2004; Bono et al. 2008). For example, Majaess (2010a) reaffirmed that the slope of the VI Wesenheit function for Milky Way Classical Cepheids (Benedict et al. 2007; Turner 2010a) characterizes classical Cepheids in the LMC, NGC 6822, SMC, and IC 1613 (see Fig. 2 in Majaess 2010a). Classical Cepheids in the aforementioned galaxies exhibit precise ground-based photometry, span a sizable abundance baseline, and adhere to a common VI Wesenheit slope to within the uncertainties ($α = -3.34 ± 0.08(2σ)$, $Δ[Fe/H] ≃ 1$). More importantly, Majaess (2010a) noted that a negligible distance offset exists between OGLE classical Cepheids and RR Lyrae variables in the LMC, SMC, and IC 1613 as established via a VI Wesenheit function, thereby precluding a dependence on metallicity. Admittedly, the impact of a reputed metallicity effect is actively debated in the literature (Smith 2004; Romaniello et al. 2008; Catelan 2009, and references therein). By contrast there appears to be a consensus that relations which rely on BV photometry are sensitive to variations in chemical abundance, and a significant break in the period-magnitude relation is apparent (Majaess et al. 2008, 2009a,b and references therein).

2http://www.aavso.org/aavsonet
3.2. WESENHEIT MAGNITUDES

A Wesenheit diagram segregates variables into their distinct classes (Fig. 4). Wesenheit magnitudes for the cluster δ Scutis were computed as follows:

\[ W_{VI,0} = \langle V \rangle - R_{VI}(\langle V \rangle - \langle I \rangle) - \mu_0 \]  

(1)

\( \mu_0 \) is the distance modulus from Table 1 and \( R_{VI} = 2.55 \) is the canonical extinction law, although there are concerns with adopting a colour-independent extinction law. VI Wesenheit magnitudes are reddening-free and comparatively insensitive to chemical composition and the width of the instability strip. The Wesenheit function is defined and discussed in the following references: Madore (1982), Freedman (1983, 1999), Madore & Freedman (1991, 2009), Kovács & Jurcsik (1997), Kovács & Walker (2001), Di Criscienzo et al. (2004, 2007), and Turner (2010a).

Cluster δ Scutis in Tables 3 and 4 are plotted on a universal VI Wesenheit template (Fig. 4, see also Majaess et al. 2010). 30 variables with distances measured by geometric means formed the calibration (Majaess et al. 2009a, their Table 1). The sample consisted of 8 SX Phe and δ Sct stars (HIP, van Leeuwen 2007), 4 RR Lyrae variables (HIP and HST, Benedict et al. 2002a, van Leeuwen 2007), 2 Type II Cepheids (HIP, van Leeuwen 2007), and 10 classical Cepheids (HST, Benedict et al. 2002a, 2007). That sample was supplemented by 6 Type II Cepheids detected by Macri et al. (2006) in their comprehensive survey of the galaxy M106 (Majaess et al. 2009a), which features a precise geometric-based distance estimate (VLBA, Herrnstein et al. 1999). Type II Cepheids within the inner region of M106 were not incorporated into the calibration because of the likelihood of photometric contamination via crowding and blending (Majaess et al. 2009a, 2010a; Majaess et al. 2010b; see also Stanek & Udalski 1999; Mochejska et al. 2001; Macri et al. 2006; Vilardeco et al. 2007; Smith et al. 2007). The stars employed were observed in the outer regions of M106 where the stellar density and surface brightness are diminished by comparison. Admittedly, it is perhaps ironic that stars 7.2 Mpc distant may be enlisted as calibrators owing to an absence of precise parallaxes for nearby objects. Additional observations of new variables in M106 are forthcoming (Macri & Riess 2009).

LMC variables catalogued by OGLE, including the latest sample of δ Scutis (Poleski et al. 2010), were added to the Wesenheit template (Fig. 4; OGLE data: Udalski et al. 1999, Soszyński et al. 2002, 2003, 2008, 2009; see also Udalski 2009). The LMC data were calibrated with a distance established via the geometric-anchored universal Wesenheit template (\( \mu_0 = 18.43 \pm 0.03(\sigma) \), Majaess et al. 2010). That distance agrees with a mean derived from 300+ results tabulated for the LMC at the NASA/IPAC Extragalactic Database

Table 2: New Photometry for Cluster δ Scutis

| Star     | Cluster | CMD position | V   | V–Ic |
|----------|---------|--------------|-----|------|
| EX Cnc   | M67     | BS           | 10.90 | 0.30 |
| EW Cnc   | M67     | BS           | 12.24 | 0.30 |
| HD 23156 | Pleiades | MS          | 8.23  | 0.28 |
| HD 23194 | Pleiades | MS          | 8.08  | 0.20 |
| HD 23567 | Pleiades | MS          | 8.29  | 0.41 |
| HD 23607 | Pleiades | MS          | 8.25  | 0.27 |
| HD 23628 | Pleiades | MS,BR       | 7.69  | 0.24 |
| HD 23643 | Pleiades | MS,BR       | 7.79  | 0.16 |

Notes: magnitudes are means of observations acquired from the AAVSO’s BSM, NOFS, TASS (Droege et al. 2006), and Mendoza (1967). The identifiers are as follows: stars occupying the blue straggler region (BS), binary / rapid rotator sequence (BR), and main-sequence (MS) of the colour-magnitude diagram (Fig. 2).

The results are consistent (in part) with the findings of 2.1 however, a direct comparison is not valid.
Fig. 4.— A calibrated universal \( V_I \) Wesenheit template constructed from data presented in Majaess et al. (2010) and the latest OGLEIII observations (e.g., Poleski et al. 2010). The cluster \( \delta \) Scutis are displayed as black dots. Wesenheit magnitudes were computed via Eqn. 1 using the \( JHK_s \) established cluster distances and \( V_I \) photometry highlighted in Tables 1 & 4 accordingly. First-order constraints on the inferred pulsation modes \( (n) \) are listed in Tables 3 & 4.

The universal Wesenheit template (Fig. 4) unifies variables of the instability strip to mitigate uncertainties tied to establishing a distance scale based on Cepheids, RR Lyrae, or \( \delta \) Sct variables individually. Anchoring the distance scale via the universal \( V_I \) Wesenheit calibration yields the same LMC distance with reduced uncertainties.

The universal Wesenheit template (Fig. 4) unifies variables of the instability strip to mitigate uncertainties tied to establishing a distance scale based on Cepheids, RR Lyrae, or \( \delta \) Sct variables individually. Anchoring the distance scale via the universal Wesenheit template (Fig. 4) mobilizes the statistical weight of the entire variable star demographic to ensure a precise distance determination. Moreover, the universal Wesenheit template may be calibrated directly via parallaxes and apparent magnitudes, mitigating the propagation of uncertainties tied to extinction corrections. F. Benedict and coauthors are presently acquiring HST parallaxes for additional population II variables which shall bolster the template (Feast 2008). Further calibration could likewise ensue via variables in clusters with distances secured by dynamical means or eclipsing binaries (Cluster AgeS Experiment, Pietrukowicz & Kaluzny 2004; Guinan & Engle 2006; Kaluzny et al. 2007), and variables in the Galactic bulge that are tied to a precise geometric-based distance (Kubiak & Udalski 2003; Eisenhauer et al. 2005; Reid et al. 2009, supported by observations from the upcoming VVV survey; Minniti et al. 2010).

Lastly, Majaess et al. (2010) plotted the universal Wesenheit template (Fig. 4) as a function of the fundamentalized period to highlight the first-order \( V_I \) period-magnitude continuity between RR Lyrae and Type II Cepheid variables (Matsunaga et al. 2006; Majaess 2009, see also Marconi & Di Criscienzo 2007 and references therein). The Wesenheit template presented here as Fig. 4 is plotted as a function of the dominant period, so pulsation modes may be inferred directly from the diagram.

3.3. PULSATION MODE

Wesenheit ridges in Fig. 4 that define \( \delta \) Scutis pulsating in the fundamental, first, second, and third overtone
Table 3: A Comparison of δ Sct Pulsation Modes

| Star     | Cluster | n(W_V,I) | n | Source |
|----------|---------|----------|---|--------|
| EX Cnc   | M67     | >3       | 3 | Z05    |
| EW Cnc   | M67     | 1 or 0   | 0 | Z05    |
| HD 23156 | Pleiades| 1        | 0 | F06    |
| HD 23194 | Pleiades| >3       | 4 | F06    |
| HD 23567 | Pleiades| 1 or 2   | 0 | F06    |
| HD 23607 | Pleiades| 1        | 0 | F06    |
| HD 23628 | Pleiades| 1        | 0 | F06    |
| HD 23643 | Pleiades| 1 or 0   | 0 | F06    |
| HD 73175 | Praesepe| >3       | 3 | P98    |
| HD 73450 | Praesepe| 1        | 1 | P98    |
| HD 73575 | Praesepe| ≥3       | 3/?| P98   |
| HD 73576 | Praesepe| ≥3       | 3 | P98    |
| HD 73763 | Praesepe| >3       | 3/?| P98   |
| HD 74028 | Praesepe| ≥3       | 3 | P98    |

Notes: pulsation modes (primary signal, order n) inferred for M67, Pleiades, and Praesepe δ Sctis from the Wesenheit template (Fig. 4 n(W_V,I)) and sources in the literature (n). Sources are Zhang et al.(2005, Z05), Fox Machado et al. (2006, F06), and Pena et al. (1998, P98).

were constructed from data presented in Poleski et al. (2010, LMC) and Majaess et al. (2010, Galactic). LMC and Galactic δ Sctis pulsating in the overtone exhibit brighter V I Wesenheit magnitudes (W_V,I) than their fundamental mode counterparts at a given period (Fig. 4 or bottom panel of Fig. 4 in Poleski et al. 2010). However, a clear separation was less evident in Garg et al. (2010) shorter-wavelength (V R) observations of LMC δ Sctis (their Fig. 3), thereby motivating those authors to favor an alternate conclusion. The present research relies on V I observations of δ Sctis.

Estimates of the pulsation modes (order, n) for the cluster δ Sctis were inferred from the Wesenheit template (Fig. 4) and are summarized in Table 4. Pulsation modes established from Wesenheit and seismological analyses for δ Sctis in the Pleiades, Praesepe, and M67 are comparable within the mutually expected (albeit large) uncertainties (±n) (Table 4). The methods identify high and low order pulsators in consistent fashion (e.g., HD23194 and HD73450, Table 3). Most small-amplitude cluster δ Sctis lie on Wesenheit loci characterizing n ≥ 1 pulsators (non-fundamental mode, Fig. 4 and Table 4), and a sizable fraction are associated with n = 1 (Table 4). The results are consistent with Poleski et al. (2010) findings and past predictions (Breger 2000, McNamara et al. 2007, and references therein).

A primary source of uncertainty associated with the analysis rests with the pulsation periods adopted. Periods for the cluster δ Sctis were taken from Rodríguez et al. (2000), the GCVS (Samms et al. 2009a), and the AAVSO’s VSX archive (Watson, Henden & Price 2010). In several instances discrepant periods are cited and newer estimates were favored (SAO 38754, L9 2003). Efforts to extract the primary pulsation period (high SNR) for mmag δ Sctis in α Persei from ARO observations were unsuccessful, likely owing to increased humidity tied to summertime observations in Nova Scotia. That underscores the challenge such mmag pulsators present to low-altitude observatories near sea-level. An additional source of uncertainty arises from a companion’s influence on the observed Wesenheit magnitudes. The pulsation mode assigned to HD 28052, which is a spectroscopic binary and bright X-ray source, should therefore be interpreted cautiously (Table 4). A star’s non-radial and multi-mode pulsation, and rotation/inclination along the line of sight likewise complicate a determination of n solely from the pulsation period and Wesenheit magnitude. Constraints established by Wesenheit analyses are admittedly limited by comparison to those inferred from uninterrupted space-based mmag time-series photometry (MOST, COROT, Kepler), yet the Wesenheit approach is a viable first-order tool that can be applied promptly to δ Sctis in any field and concurrently with other methods.

3.4. δ SCT DISTANCE TO NGC1817

A potential role for mmag δ Sctis as distance indicators for intermediate-age open clusters is now explored using the aforementioned framework. Arentoft et al. (2005) observations of NGC 1817 indicated that the open cluster hosts a statistically desirable sample of 11 δ Sctis. Balaguer-Núñez et al. (2004) proper motions implied that five of those stars are not cluster members (V1, V6, V8, V10, V12, see Arentoft et al. 2005). Yet Arentoft et al. (2003) concluded that 11 variables (V1→V12, excluding V10) exhibit positions in V vs. B − V and b − y colour-magnitude diagrams consistent with δ Sct pulsation and cluster membership. A preliminary V vs. V − I colour-magnitude diagram for NGC 1817 (Fig. 5) confirms that most variables display positions consistent with membership (except V10). The V I data were obtained from the ARO and processed using ARAF (Land 2007) and DAOPHOT (Stetson 1987). The ARO features an SBIG ST8XME CCD mounted upon a 35-cm telescope located near Stillwater Lake, Nova Scotia, Canada. The ARO is a remotely operated robotic observatory (Land 2007). A description of the ARO observations for NGC 7062, including an analysis using VaST (Sokolovsky & Lebedev 2005), shall be provided in a subsequent study.

The V I Wesenheit diagram compiled for the δ Sctis
(Fig. 5) implies that V10, V11, and V12 either exhibit spurious data, are not bona fide δ Scutis, or are not cluster members. V10 is too faint, as corroborated by its position in the colour-magnitude diagram (Fig. 5). The variability detected in V11 is marred by low signal to noise and other complications (Arentoft et al. 2005). V12 is likewise too faint (\(W_{VI}\)) and features a period beyond that typically expected for δ Sct variables (Percy 2007). An advantage to applying the Wesenheit technique is that high and low-order pulsators may be identified. V1, V2, and V6 are likely pulsating at higher orders if the stars are members (Fig. 5). V3, V4, V7, V8, and V9 are tightly clustered and may define the \(n \geq 1\) boundary (Fig. 5, see §3.3). The resulting distance to NGC 1817 is \(d \simeq 1.7\) kpc, assuming the aforementioned mode distribution. The δ Sct distance to NGC 1817 agrees with estimates established for the cluster by other means (Arentoft et al. 2005, see references therein). However, employing \(mmag\) δ Sct as distance indicators for open clusters is complicated by the need for independently confirmed periods, and \textit{a priori} knowledge of the pulsation modes or the adoption of a mode distribution \((n \geq 1)\) given sizable statistics (see §3.3). Establishing the distance to NGC 1817 or the Praesepe under the latter caveat may yield a pertinent result, yet the ensuing distance to \(\alpha\) Persei would be in error owing to small statistics. \(\alpha\) Persei certainly features more than 3 δ Scutis, however a detection bias emerges since nearby clusters exhibit large angular diameters which exceed the field of view of most CCDs. Continued research is needed.

### 4. SUMMARY AND FUTURE RESEARCH

This research aimed to outline and evaluate a \(VI\) Wesenheit framework for investigating cluster δ Scutis, an analysis which relied on securing absolute Wesenheit magnitudes from precise open cluster distances. \(JHK_s\) ZAMS and colour-colour relations were derived from unreddened stars near the Sun with precise Hipparcos parallaxes and were applied to infer parameters for several benchmark star clusters which host δ Scutis (Fig. 1, Table 1). That analysis yielded constraints on the absolute Wesenheit magnitudes (\(W_{VI,0}\)), evolutionary status, and pulsation modes (order, \(n\)) for the cluster δ Scutis (Figs. 3, 4 Tables 2, 3). \(VI\) photometry for the variables were tabulated to facilitate further research (Table 4), and include new data acquired via the AAVSO’s robotic telescopes (Table 2).

The \(JHK_s\) established cluster distances are bolstered by the relative insensitivity of \(J - K_s\) photometry to variations in [Fe/H] and age over the baseline examined (Table 1, Fig. 3). The deep \(JHK_s\) photometry extends into the low mass regime (\(\simeq 0.4M_\odot\)) and indicates that the clusters feature a common ZAMS in the infrared, and that \(J - K_s\) remains constant with increasing magnitude (\(M_J \simeq 6\)) for low mass M-type dwarfs whereas \(J - H\) exhibits an inversion (\(\simeq 5\%\)) \(JHK_s\) ZAMS fits by providing distinct anchor points in colour-magnitude and colour-colour diagrams (Figs. 1, 2). The trends ensure precise (\(\leq 5\%\)) \(JHK_s\) ZAMS fits for 7 of 9 clusters within 250 pc agree with van Leeuwen (2009a) revised Hipparcos estimates (Table 1). However, the \(JHK_s\) distance to the Pleiades supports the HST estimate rather than that derived from Hipparcos data (Table 1). van Leeuwen (2009a) argues in favour of the revised Hipparcos distances to open clusters and
the reader is referred to that comprehensive study. Yet the distance scale can (presently) rely on a suite of clusters that are independent of the Pleiades. Models should be calibrated and evaluated using those nearby clusters where consensus exists regarding the distances (Table 1).

The general agreement between the $JHK_s$ distances derived here and van Leeuwen (2009a) Hipparcos estimates is noteworthy (Table 1). The $\sim 10 - 20\%$ offset in distance for the discrepant cases (Pleiades & Blanco 1) is not typical for studies of open clusters (Fig. 2 in Mermilliod & Netopil 2006, see also Dias et al. 2002). Several clusters feature distance estimates spanning nearly a factor of two, such as NGC 2453 (Majaess et al. 2007), their Table 4), ESO 096-SC04, Collinder 419, Shorlin 1, and Berkeley 44 (Turner 2010b,c). The universal $VI$ Wesenheit template could be applied to cluster $\delta$ Scuti so to isolate viable distance solutions, provided certain criteria are satisfied ($\gtrsim 3.4$, e.g., sizable statistics). A Wesenheit analysis ($VI$) is a viable means for establishing pertinent constraints on a target population of $\delta$ Scuti variables, particularly in tandem with other methods (Figs. 2, 4, 5, Tables 3, 4).

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Table 4: δ Scutis in Benchmark Open Clusters

| Star       | Cluster | CMD position | n(W_V) | VI Photometry |
|------------|---------|--------------|--------|---------------|
| SAO 38754 | α Perse | MS           | 1      | TASS, S85     |
| HD 20919  | α Perse | MS,BR:       | 2 or 3 | TASS          |
| HD 21553  | α Perse | MS           | 0      | TASS          |
| HD 23156  | Pleiades| MS           | 1      | Table2        |
| HD 23194  | Pleiades| MS           | >3     | Table2        |
| HD 23567  | Pleiades| MS           | 1 or 2 | Table2        |
| HD 23607  | Pleiades| MS           | 1      | Table2        |
| HD 23628  | Pleiades| MS,BR        | 1      | Table2        |
| HD 23643  | Pleiades| MS,BR        | 1 or 0 | Table2        |
| HD 27397  | Hyades  | EV           | 1 or 2 | T85           |
| HD 27459  | Hyades  | EV           | 1      | J06           |
| HD 27628  | Hyades  | sat./EV:     | 1      | J06           |
| HD 28052  | Hyades  | sat./EV:     | 1 or 0 | J06           |
| HD 28052  | Hyades  | sat./EV:     | 0      | J06           |
| HD 28319  | Hyades  | sat./EV:     | >3     | J06           |
| HD 30780  | Hyades  | sat.         | >3     | J06           |
| HD 73175  | Praesepe| MS/EV        | >3     | TASS, ME67    |
| HD 73345  | Praesepe| MS/EV        | >3     | TASS, ME67    |
| HD 73450  | Praesepe| MS           | 1      | TASS, ME67    |
| HD 73575  | Praesepe| EV           | ≥3     | TASS, ME67    |
| HD 73576  | Praesepe| MS/EV,BR     | ≥3     | TASS, ME67    |
| HD 73712  | Praesepe| EV           | 1 or 2 | TASS, ME67    |
| HD 73729  | Praesepe| MS/EV,BR     | 2 or 3 | TASS, ME67    |
| HD 73746  | Praesepe| MS           | 1      | TASS, ME67    |
| HD 73763  | Praesepe| MS/EV        | >3     | TASS, ME67    |
| HD 73798  | Praesepe| MS/EV        | 1      | TASS, ME67    |
| HD 73819  | Praesepe| EV           | 0      | TASS, ME67    |
| HD 73890  | Praesepe| MS/EV,BR     | >3     | TASS, ME67    |
| HD 74028  | Praesepe| MS/EV        | ≥3     | TASS, ME67    |
| HD 74050  | Praesepe| MS/EV        | 3      | TASS, ME67    |
| EX Cnc    | M67     | BS           | >3     | Table2        |
| EW Cnc    | M67     | BS           | 1 or 0 | Table2        |

Notes: δ Sc cluster list compiled primarily from Li & Michel (1999) and references therein. The identifiers are as follows: stars occupying the blue straggler region (BS), binary/rapid rotator sequence (BR), evolved region (EV), and main-sequence (MS) of the colour-magnitude diagram (Fig. 2). Pulsation modes (primary signal, order n) inferred for the δ Scutis from the VI Wesenheit template (Fig. 4). Hyades members may feature saturated (sat.) 2MASS photometry owing to their proximity (Table 1). There are concerns regarding the photometric zero-point for bright δ Scutis sampled in the all-sky surveys (Henden & Sallman 2007). References for the photometry are Mendoza (1967, ME67), Taylor & Joner (1985, T85), Stauffer et al. (1983, T85), and Joner et al. (2006, J06).
