Spin waves near the edge of halogen substitution induced magnetic order in Ni(Cl$_{1-x}$Br$_x$)$_2$·4SC(NH$_2$)$_2$

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We report an inelastic neutron scattering study of magnetic excitations in a quantum paramagnet driven into a magnetically ordered state by chemical substitution, namely Ni(Cl$_{1-x}$Br$_x$)$_2$·4SC(NH$_2$)$_2$ with $x = 0.21(2)$. The measured spectrum is well accounted for by the generalized spin wave theory (GSWT) approach [M. Matsumoto and M. Koga, J. Phys. Soc. Jap. 76, 073709 (2007)]. This analysis allows us to determine the effective Hamiltonian parameters for a direct comparison with those in the previously studied parent compound and “underdoped” system. The issue of magnon lifetimes due to structural disorder is also addressed.

I. INTRODUCTION

Long range magnetic order can in some cases be induced in disordered quantum spin systems by a continuous tuning of exchange constants [1]. In such quantum phase transitions (QPTs) a quantum paramagnet transforms to a semiclassical Néel state via a softening of the spin gap. The best known examples in real materials are driven by applying hydrostatic pressure. Pressure induced ordering has been extensively studied the the dimer systems TiCuCl$_4$ [2,3] and PHCC [5,7], as well as in the single ion singlet compound CsFeCl$_3$ [8,9]. These transitions differ from the better known magnetic field induced “Bose–Einstein condensation of magnons” [10,11] in the same species [12,14]. The crucial distinction is that the excitation spectrum remains parabolic at BEC, and thus the dynamical exponent $z = 2$. In contrast, at the pressure-induced QPT the spectrum is linear, implying $z = 1$.

Pressure is not the only potential “handle” on the exchange constants. Chemical substitution on non-magnetic sites presents an alternative. It directly affects exchange and anisotropy parameters or produces an effect of “chemical pressure” [15–17]. Recently, we have demonstrated that chemical modification can indeed drive a $z = 1$ QPT, namely in the anisotropic $S = 1$ quantum paramagnet NiCl$_2$·4SC(NH$_2$)$_2$ known as DTNX [18]. Upon Br substitution for Cl in Ni(Cl$_{1-x}$Br$_x$)$_2$·4SC(NH$_2$)$_2$ [this modification is abbreviated as DTNX], the spin gap decreases. At around $x_c \approx 0.15$ the spin-singlet ground state is replaced by spontaneous Néel order. In particular, at $x = 0.21(2) > x_c$, the material undergoes long-range ordering at $T_N = 0.64$ K, albeit with a much reduced ordered moment $\langle S \rangle \approx 0.3 \mu_B$ at low temperatures [18]. In the present work we continue the investigation of this weakly ordered system, focusing on spin excitations. We find that the measured spectrum is remarkably well described by the so-called generalized spin wave theory (GSWT) [19,21]. This allows us to determine the Hamiltonian parameters and discuss the placement of this compound of the theoretical phase diagram. The effect of disorder on the magnetic excitations is found to be minor.

II. MATERIAL AND EXPERIMENT

A. DTNX: a short introduction

The physics of the parent compound NiCl$_2$·4SC(NH$_2$)$_2$ is rather well understood [22,24]. The $S = 1$ ions of Ni$^{2+}$ are bridged by two Cl ions into linear chains, which run along the high-symmetry axis of the tetragonal structure ($a = 9.56$ Å and $c = 8.98$ Å, see Fig. 1). Due to the body-centered I4 space group there are two such tetragonal “sublattices”, effectively decoupled from each other magnetically.

A model magnetic Hamiltonian can be written as:

$$\hat{H} = \sum_\text{Site} D(\hat{S}_r^z)^2 + \sum_\text{Chain} J_c(\hat{S}_r \cdot \hat{S}_{r+c}) + \sum_\text{Plane} J_a(\hat{S}_r \cdot \hat{S}_{r+a_1})$$

(1)

Here $a_{1,2}$ and $c$ are lattice translations as in Fig. 1. The vector $r$ runs through all Ni$^{2+}$ sites. The strongest contribution to Hamiltonian (1) is the easy-plane single ion anisotropy $D = 0.7$ meV. Intrachain Heisenberg exchange is $J_c = 0.15$ meV is significantly stronger than inter-chain interactions $J_a \approx 0.1 J_c$. The planar anisotropy term dominates and drives the system into a trivial quantum disordered state with $S^z = 0$ for each ion.

There are two inequivalent halogen sites in the structure. In Ni(Cl$_{1-x}$Br$_x$)$_2$·4SC(NH$_2$)$_2$ the Br substitute tends to occupy a particular one of them [18]. This distorts the environment of Ni$^{2+}$ and strongly affects the covalency of the Ni-halogen bonds. In turn, interactions are strongly modified, especially $J_c$ for which the two-halide bond is the primary superexchange mediator [17]. Recent NMR [25] and theoretical [26] studies suggest that...
tering intensities as a function of momentum and energy given in Fig. 2. It shows a false color plot of neutron scattering data were recorded with a position-sensitive detector array for a sequence of 140 frames with 1◦ detector rotation steps. All data were analyzed using the Horace software [30].

Scattering data were performed at a base temperature of about 70 mK on the IN5 spectrometer at Institute Laue–Langevin [29]. A sample consisting of two co-aligned samples of Ni(Cl1−Br2)2-4SC(NH2)2. These were grown from aqueous solution using the temperature gradient method as described in [27, 28]. The Br concentration in as-grown crystals was verified by means of single-crystals x-ray diffraction on an APEX-II Bruker diffractometer and determined to be x = 0.21(2).

Time-of-flight inelastic neutron measurements were performed on the IN5 spectrometer at Institute Laue–Langevin [29]. A sample consisting of two co-aligned crystals with total mass of about 0.2 g was installed onto the cold finger of a 3He-4He dilution refrigerator. The scattering plane was (1, −1, 0) as defined by its normal. This provided access to the momentum transfers of Q = (h, h, l) = h(a1+2a2*c) type. The measurements were performed at a base temperature of about 70 mK using neutrons with incident energies Ei = 2.26 meV. Scattering data were recorded with a position-sensitive detector array for a sequence of 140 frames with 1◦ sample rotation steps. All data were analyzed using HORACE software [30].

III. RESULTS AND DATA ANALYSIS

A. Overview of the excitation spectrum

An overview of the measured excitation spectrum is given in Fig. 2. It shows a false color plot of neutron scattering intensities as a function of momentum and energy transfer. As indicated in the inset, the momentum transfer follows a sequence of high symmetry directions in the (h, h, l) plane. The spectrum is clearly dominated by a single excitation branch, which remains underdamped in the entire zone. Overall, its dispersion is not dissimilar to that previously measured in the parent compound x = 0 [22] and for x = 0.06 [17] (dotted and dashed lines in Fig. 2). The key difference is that in the present compound there is no excitation gap. This is consistent with notably different thermodynamics, as compared to x < xc (“underdoped”) materials [18].

B. Theoretical approach

As mentioned, the ordered moment in the present x = 0.21(2) material is significantly reduced compared to the classical expectation of 2µB per Ni2+. Under these circumstances, the standard spin wave theory reaches its applicability limit. To quantitatively analyze the data we instead employed the so-called GSWT approach [20, 21]. We follow the particular formulation for a DTN-like Hamiltonian [1] developed by Matsumoto and Koga [19]. This method utilizes a basis of local states and is similar to “bond operator theory” [31, 32] used for treating dimerized spin systems. In the quantum paramagnetic phase the GSWT spectrum features two degenerate bosonic modes with dispersion relations identical to those obtained in the random phase approximation (RPA) [33]. The ordered state is then treated as the quantum mechanical condensate of such excitations. Here there are three new types of quasiparticles: two transverse spin wave modes (yy) and (zz) (see schematic in Fig. 1), and one amplitude mode (xx). The transverse modes are gapless. Their dispersions are related by a translation by a single excitation branch, which remains underdamped in the entire zone. Overall, its dispersion is not dissimilar to that previously measured in the parent compound x = 0 [22] and for x = 0.06 [17] (dotted and dashed lines in Fig. 2). The key difference is that in the present compound there is no excitation gap. This is consistent with notably different thermodynamics, as compared to x < xc (“underdoped”) materials [18].

C. Data analysis

In order to quantify the dispersion, intrinsic width and intensity of the observed excitations, we analyzed individual constant-Q cuts of the data for a grid of wave vectors with a step of δQ = 0.05 r.l.u. in both h and l directions. At each wave vector the fitting function was a Voigt profile. Its Gaussian component was the calculated energy-dependent energy resolution of the spectrometer [34]. The Lorentzian component represented the intrinsic excitation width and was one of the fit pa-
FIG. 2. False color map of neutron scattering intensity measured in the $x = 0.21(2)$ DTNX sample at $T \approx 70$ mK. The momentum transfer $Q$ follow a specific trajectory between high symmetry points of the Brillouin zone (inset). The reference dispersion curves for $x = 0$ and $x = 0.06$ materials [17, 22] are shown as dotted and dashed lines. The solid line is a dispersion fit to the present data, as described in the text. Hatching marks the region dominated by parasitic quasielastic scattering.

FIG. 3. Representative constant-$Q$ cuts of the measured neutron intensity (symbols). The data is truncated below $\hbar \omega = 0.1$ and above $\hbar \omega = 1.2$ meV, where instrument background dominates. Solid lines are fits to individual cuts, as described in the text.

rameters. Also fitted was the peak position, an intensity prefactor and a flat background. Representative examples of such fits for a few representative points are given in Fig. 3. For high-symmetry reciprocal space directions the fitted peak positions and intensities are plotted against wave vector transfer in Fig. 4.

To obtain the Hamiltonian parameters the dispersion relation determined on the entire wave vector grid was fit using the GSWT result. We attribute the observed scattering to the $yy$ excitation branch. The best fit is obtained with $D = 0.639(5)$ meV, $J_c = 0.241(2)$ meV, and $J_a = 0.013(1)$ meV. The dispersion relation along high symmetry directions calculated with these values is plotted in a solid line in Fig. 4 (top panel) to illustrate the excellent level of agreement.

A GSWT calculation with these parameters can reproduce the measured intensities as well. This defines the neutron polarization factor, as neutrons are only scattered by magnetization components that are transverse to the momentum transfer. Since a macroscopic sample
is bound to split into domains with different orientations of the ordered moment in the tetragonal plane, this effect needs to be averaged accordingly. In our analysis we thus multiplied the mode intensities calculated with GSWT by the polarization factor $P_{yy}(Q) = 1 - (2\pi ha/Q)^2$. An additional correction was the $\text{Ni}^{2+}$ magnetic form factor $|F(Q)|^2$ that we included in our calculation within the dipole approximation [35]. With just one additional fit parameter, namely a single overall scale factor, the GSWT model with exchange and anisotropy constants as obtained in dispersion fit gives an excellent agreement with the measurement (solid line in the bottom panel of Fig. 4).

Our data analysis also yields the intrinsic linewidth $\Gamma(Q)$ of excitations as a function of wave vector. For a direct comparison with previous studies, we choose to plot the energy dependence of the linewidth $\Gamma(\omega)$, averaged over the Brillouin zone. For our present sample this quantity is shown in Fig. 5 in filled circles. Previously published data for the “underdoped” $x = 0.06$ material are plotted in open squares. For reference, the energy resolution of the spectrometer (the same in both studies) is plotted in a dashed line.

IV. DISCUSSION

A. Other GSWT modes

The agreement of the GSWT predictions for the $yy$ mode with experiment is remarkable, but what about the other two excitation branches? In Fig. 6 we show the GSWT calculation for all three polarizations, based on the Hamiltonian parameters obtained in the fit above. The polarization factors for each mode and the magnetic form factor are accounted for as appropriate. All modes in this simulation have zero intrinsic line widths, as appropriate for GSWT. This simulation tells us that the out of plane transverse $zz$ mode could well be too weak to be observable in the present experiment. However, the longitudinal $xx$ mode would be strong enough to be seen, if only it were underdamped. It is well understood however that a sharp longitudinal excitation is an artifact of GSWT. In fact, longitudinal modes in antiferromagnets with gapless spin waves are known to be prone to decays into transverse modes [36, 37]. Being overdamped, they cannot be even associated with a peak feature in the spectrum. In the few materials [4, 38, 39] where longitudinal modes are observed, they are stabilized by Ising-like anisotropy effects absent in DTNX. We conclude that detecting only one of the excitation branches predicted by GSWT is actually not that surprising.

B. Hamiltonian parameters

As already mentioned, in the quantum paramagnetic phase GSWT is equivalent to the RPA. This allows a meaningful comparison of the Hamiltonian parameters that we obtain for the “overdoped” $x = 0.21(2) > x_c$ material to those previously determined for the parent compound [22] and for the “underdoped” $x = 0.06$ system [17].

This comparison is made in Table I. The left panel of Fig. 7 positions the three compounds on the phase diagram calculated with the Mean Field (MF) or GSWT approximations. The MF boundary between the gapped and ordered phases, i.e., the line of gap closure, corresponds to $D = 4J_c + 8J_a$. In this context, the $x = 0.21(2)$ material lands deep inside the ordered phase. The complication is that the RPA and GSWT exchange constants are known to be strongly renormalized compared to actual values. For the gapped compounds this renormalization can be accounted for by the self-consistent “Lagrange multiplier method” [20, 31]. The phase space of actual, rather than renormalized, Hamiltonian parameters is shown in the right panel of Fig. 7. This plot also shows the numerically computed phase boundaries for weakly-coupled $S = 1$ spin chains with planar anisotropy [40, 11]. Unfortunately, this procedure cannot be applied to determine the actual Hamiltonian parameters in our “overdoped” system, which is already in the ordered state.
FIG. 6. Simulated GSWT spectrum with the background $B(Q) = 2 \cdot 10^{-3}$, convoluted with $\sigma = 50 \mu\text{eV}$ Gaussian. Polarization factors and magnetic ion form factor are also taken into account.

FIG. 7. Ground state phase diagrams of Hamiltonian (1). Left panel: Phase diagram in the mean field approximation including quantum disordered (QD) and antiferromagnetically ordered (AF) phases [19]. The points, locating three different DTNX family members on this phase diagram are obtained from GSWT without taking the quantum corrections into account. Right panel: the exact phase diagram, obtained by Quantum Monte–Carlo (QMC) calculations. A new Haldane phase (H) appears in the decoupled Heisenberg chain limit. The experimental points for $x = 0$ and $x = 0.06$ materials of DTNX family now correspond to the estimated bare microscopic parameters [17, 22]. Dashed line shows the linear low bromine concentration trend in both figures.

V. SUMMARY

The three take-home messages of this study are: 1) Transverse spin excitations in the entire series of DTNX materials, both “underdoped” and “overdoped”, are remarkably well described by GSWT. 2) The underdamped longitudinal mode, a known artefact of GSWT, is absent in the DTNX. 3) The effect of chemical disorder is rather subtle and for the most part amounts to a moderate broadening of magnons.

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Appendix A: GSWT exact results

In this Appendix we recite the GSWT theoretical results for the DTN-like material obtained by Matsumoto and Koga [19]. We would like to start with the excitations in the ordered phase. First, the following auxiliary notation are introduced:

\[ u, v = \sqrt{\frac{1}{2} \left( 1 \pm \frac{D}{4J_c + 8J_a} \right)} \], \quad (A1)

\[ \gamma(Q) = 2J_c \cos(Q \cdot c) + 2J_a \left[ \cos(Q \cdot a_1) + \cos(Q \cdot a_2) \right] \]. \quad (A2)

Note, that within GSWT \[ 2\gamma(0) = 4J_c + 8J_a \] corresponds to the critical value of single-ion anisotropy \( D_c \) at which the antiferromagnetic order is suppressed.

Then, Eqs. (A1) and (A2) are plugged into the following four terms related to longitudinal (L) and transverse (T) excitation channels:

\[ \epsilon_L(Q) = (u^2 - v^2)D + 4u^2v^2(4J_c + 8J_a) \]
\[ + (u^2 - v^2)^2\gamma(Q), \]
\[ \delta_L(Q) = (u^2 - v^2)^2\gamma(Q), \quad (A3) \]
\[ \epsilon_T(Q) = u^2D + 2u^2v^2(4J_c + 8J_a) + (u^2 - v^2)^2\gamma(Q), \]
\[ \delta_T(Q) = \gamma(Q). \]

Finally, the terms (A3) are used to construct the dispersion relations and the corresponding equal-time structure factors (intensities) of the spin wave excitations:

\[ \hbar\omega_{xx}(Q) = \sqrt{\epsilon_L(Q)^2 - \delta_L(Q)^2}, \quad (A4) \]
\[ \hbar\omega_{yy}(Q) = \sqrt{\epsilon_T(Q)^2 - \delta_T(Q)^2}, \quad (A5) \]
\[ \hbar\omega_{zz}(Q) = \sqrt{\epsilon_L(Q + Q_0)^2 - \delta_L(Q + Q_0)^2}, \quad (A6) \]
\[ S_{xx}(Q) = A(u^2 - v^2)^2 \left[ \frac{\epsilon_L(Q) - \delta_L(Q)}{\epsilon_L(Q) + \delta_L(Q)} \right], \quad (A7) \]
\[ S_{yy}(Q) = A(u^2)^2 \left[ \frac{\epsilon_L(Q) - \delta_L(Q)}{\epsilon_L(Q) + \delta_L(Q)} \right], \quad (A8) \]
\[ S_{zz}(Q) = A(u^2)^2 \left[ \frac{\epsilon_L(Q + Q_0) - \delta_L(Q + Q_0)}{\epsilon_L(Q + Q_0) + \delta_L(Q + Q_0)} \right]. \quad (A9) \]

In the equations above \( A \) is the overall normalization parameter, used for direct comparison with the experimental neutron scattering intensities.

In case of quantum paramagnetic phase the \( zz \) excitation vanishes, while \( xx \) and \( yy \) excitations converge to a single doubly degenerate mode. Its dispersion is simply:

\[ \hbar\omega_{PM}(Q) = \sqrt{D^2 + 2D\gamma(Q)}. \quad (A10) \]

The corresponding intensity is given by:

\[ S_{PM}(Q) = A \frac{D}{\hbar\omega_{PM}(Q)^2} \quad (A11) \]

with \( A \) being the same as in Eqs. (A7) – (A9).

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