Abstract

The MACHO Project has catalogued \( \sim 8000 \) RR Lyrae stars in the Large Magellanic Cloud, \( \sim 1800 \) in the Galactic bulge, and \( \sim 50 \) in the Sgr dwarf galaxy. These variables are excellent distance indicators, and are used as tools to study the structure of the Large Magellanic Cloud and the bulge. The large datasets also probe uncommon pulsation modes. A number of double-mode RR Lyrae stars (RR\( d \)) are found in the Large Magellanic Cloud sample. These stars provide important clues for understanding the formation and evolution of the inner Galaxy, the Large Magellanic Cloud and the Sgr dwarf galaxy. A large number of second overtone pulsators (RR\( e \)) are found in the LMC and bulge. Finally, the RR Lyrae belonging to the Sgr dwarf yield an accurate distance to this galaxy. Their presence also alerts us of the very interesting possibility of distant sources for bulge microlensing events.

1 Introduction

Even though all pulsating variables are interesting probes of the internal constitution and evolution of stars [17], a subset of them, the RR Lyrae stars, are particularly good for astronomers for a variety of other reasons.
We use RR Lyr to measure distances within the Local Group. Having a narrow range of colors and luminosities, they are easy to identify from their characteristic variability.

We also use RR Lyr to date the Universe, and to study the formation of the Milky Way (MW), since they are among the oldest stars known.

The MACHO project discovered large numbers of RR Lyr in the MW, the Large Magellanic Cloud (LMC), and the Sgr dwarf galaxy (Sgr). Here we will discuss a few astronomical applications of our ongoing study of this sample, starting with a brief description of the selection of RR Lyr among various other periodic variable stars (Section 2).

RR Lyr are excellent tools to study pulsational physics, and therefore to determine fundamental stellar parameters. They can be used to determine masses, the distance to the LMC, and the ages of the oldest stellar populations, and to compare the old stellar populations of the LMC and the MW bulge (Section 3). RR Lyr are primary distance indicators. They can be used to study the structure of the inner MW (Section 4), and to determine the distance and dynamical evolution of Sgr, thereby aiding in the interpretation of the microlensing optical depth (Section 5).

2 Selection of the Sample

The MACHO database contains so far about 40000 periodic variable stars in the LMC and a similar number in the MW bulge. A description of the variable star database has been published elsewhere [13]. Among these stars, we have selected about 8000 RR Lyr in the LMC, about 1800 RR Lyr in the MW bulge, and about 50 RR Lyr in Sgr. The selection process in the LMC is straightforward [2], and here we will briefly describe the selection of the bulge sample. The bulge RR Lyr were selected using the period-amplitude and amplitude-amplitude diagrams. Here we analyze the data from 1993, covering over 100 days. The selection of RR Lyrae in this database is complicated by aliases. Some of the stars with periods $P = 1/n$ days maybe badly phased because the MACHO observations are done roughly every 24 hours. However, almost all aliases are discarded by demanding that

$$P^V = P^R,$$

which stresses the importance of having continuous coverage in two passbands. The selection of RR Lyrae is also complicated by the presence of other variable stars with overlapping periods: eclipsing binaries, $\delta$ Scu stars, etc. Fortunately again, we have good quality light curves in two passbands. The amplitude ratios can be used to discriminate the pulsating variable stars from the eclipsing variables (Figure 1).

The final RR Lyr sample is then selected from the period-amplitude diagram, including all stars with $0.2^d < P < 1.1^d$, and $0.1 < AV < 2$ (Figure 2). The light curves of these objects were inspected to identify a few surviving binary stars. As a final check, the light curves are fitted by a series of Fourier sine functions [35]. The resulting Fourier coefficients (e.g. the $R_{31}$ vs $\phi_{31}$ or the $\phi_{21}$ vs $\phi_{31}$ planes) were used to discriminate among RR Lyr pulsating in the fundamental mode (RRab), in the first-overtone (RRc), or in the second-overtone (RRe).

This final sample is representative of the whole RR Lyr population in the bulge, but it is not complete. Independent estimates of the completeness of our RR Lyr sample are obtained by comparison with other surveys ([1], [40], [7]). Note that the number of bonafide RR Lyr in the MW bulge sample will increase as the data from the following years is analyzed.

The photometric calibration of such a large database using non-standard filters is challenging. We have used the latest calibrations [5], and have made a series of external comparisons with other photometry [43], [40], [41], [14].

Some of the MACHO bulge fields have significant overlap. The internal comparisons of 44 bulge RR Lyr in overlap regions yield the following errors in the magnitudes $\sigma V_M = 0.120$, $\sigma R_M = 0.114$, in the positions $\sigma \alpha = 0.58''$, $\sigma \delta = 0.37''$, in the periods $\sigma_P = 0.000054^d$, and in the amplitudes $\sigma AV_M = 0.12$, $\sigma AR_M = 0.06$. 


Figure 1: Red vs blue amplitudes for all the variable stars with $0.25^d < P < 0.4^d$ in the MACHO database. For binary stars $A_V \approx A_R$. Note the clear separation from the RRc, which follow the relation $A_R \approx 0.7A_V$. This is very useful in order to discriminate different variables, and it is possible in the MACHO data because we have excellent coverage of the light curves in both passbands.

Figure 2: Separation between eclipsing (lower panels) and pulsating (upper panels) variable stars with $0.1 < P < 100$ days in the MACHO 93 data. From left to right we show the color-magnitude diagram (using the reddening independent magnitudes $W_V$), the amplitude-magnitude diagram, and the amplitude-period diagram. In order of increasing periods, there are contact and detached binaries, and spotted or RS CVn-type stars in the lower panels. The upper panels show in order of increasing periods δ Scu, RRe, RRc, RRab, pulsating yellow variable, and long-period variable stars.
Figure 3: Period distribution for RR Lyr stars in the LMC (right panel), and the Galactic bulge (left panel). The peaks correspond, from right to left, to RRab, RRc, and RRe, respectively. Note that the overall distribution of bulge RR Lyr is shifted towards shorter periods. This is a metallicity effect, with the bulge RRab being about 0.5 dex more metal-rich in the mean than the RRab in the LMC.

3 Comparison Between RR Lyrae in the LMC and in the Bulge

The RR Lyr in the MW bulge have mean $[Fe/H] = -1.1$, based on spectroscopic determinations of 54 RR Lyr in Baade’s window [43]. This is significantly more metal-poor than the bulk of the bulge population, which have mean $[Fe/H] = -0.2$ to $-0.6$, as measured from spectroscopy of K giants in different bulge fields [25], [27]. This is not surprising, however, since we know from globular clusters that metal-rich populations do not produce as many RR Lyr [39], [21].

The transition periods (defined based on the longest period RRc star) in the bulge and LMC are $P_{tr} = 0.432^d$, and $P_{tr} = 0.457^d$, respectively. The RR Lyr population in the LMC is Oosterhoff type I, while in the bulge it is extreme Oosterhoff type I.

In particular, the mean periods of the RR Lyr pulsating in the different modes are longer in the LMC than in the MW bulge, as listed in Table 1. Also shown in Table 1 are the mean reddening independent magnitudes $W_V$ for bulge RR Lyr pulsating in the fundamental, 1st overtone, and 2nd overtone, respectively.

The large sample sizes allow us to identify uncommon pulsation modes, such as double-mode RR Lyr or RRd. While the bulge database has not been searched yet, we have identified more than 70

| Type | Puls. Mode | $P_{LMC}$ | $P_{MWB}$ | $W_V_{MWB}$ |
|------|------------|-----------|-----------|-------------|
| RRab | Fundamental | 0.55$^d$  | 0.53$^d$  | 14.05       |
| RRc  | 1st Overtone| 0.34$^d$  | 0.32$^d$  | 14.29       |
| RRe  | 2nd Overtone| 0.28$^d$  | 0.27$^d$  | 14.39       |
| RRd  | Double     | 0.48$^d$  |           |             |

Alcock et al. [2] studied the RR Lyr in the LMC, here we compare that sample with the RR Lyr in the MW bulge. The RR Lyr in the LMC and in the bulge have very different metallicity distributions (Figure 4). Their mean metallicities differ by $\Delta[Fe/H] = 0.5$ dex, with the LMC ones being more metal-poor. This has to be one of the major parameters driving the different distribution of RR Lyr in the Bailey diagram [2], and in their different period distribution, as shown in Figure 3.
Figure 4: Metallicity distribution of RR Lyr in Baade’s Window from Walker & Terndrup (1992), and for the LMC from Alcock et al. (1995). The histograms have been arbitrarily normalized to the same total number of counts.

Figure 5: Petersen diagram for RRd in the LMC taken from Alcock et al. (1996b). The ridge lines corresponding to different masses from the pulsation equation are shown. A wide range of masses is evident in the LMC RRd stars. Note that both $P_1$ and $P_0/P_1$ are very accurately measured. We strongly caution that the whole parameter space has not been fully exploited. In particular, there may be more RRd with shorter and longer periods that those shown here. The lower limit to the masses will be dictated by bare stellar cores, with $M \geq M_{WD}$. Conversely, because of mass loss during the RGB phase, the upper limit to the masses is constrained by the mass of turn off stars, $M \leq M_{TO}$. 
RRd in the LMC \cite{2}. These are double-mode pulsators, with typical light curves as shown in \cite{3}. We use the Petersen diagram \cite{31} to measure the masses of these stars (Figure 5). Knowing the masses, we can obtain their intrinsic luminosities from the pulsation equation \cite{10}, which in turn provides with a measure of the distance to the LMC. We can then solve the old problem of the different LMC distance scales produced by the Cepheids and RR Lyrae \cite{13}. The results of this revised LMC distance scale will be published elsewhere \cite{4}.

The existence of RR Lyrae pulsating in the second overtone or RRc have been difficult to prove \cite{35}, \cite{36}. Large numbers of RRc have been now identified in the LMC and the MW bulge. In the mean, bulge RRc candidate stars are about 0.1 mag fainter than RRc stars (Table 1). These are not to be confused with $\delta$ Scu stars in the bulge, which are more than a magnitude fainter in the mean. Further study will reveal more fundamental properties of these candidate RRc stars.

4 Spatial Distribution of Bulge RR Lyrae

There is a bar in the inner MW, seen from the integrated IR light \cite{8}, from tracers of metal-rich populations such as Miras \cite{17}, and from the kinematics of gas \cite{3}, and stars \cite{48}. This bar is well described by the density distribution $p_0 \propto r^2 \exp[1/2(\{(r \cos b \cos l - R_0)/1.49\}^2 + (r \cos b \sin l/0.58)^2 + (r \sin b/0.40)^4)^1/2$ modeled from the IR maps of COBE \cite{15}. Clump giants have also been used to study the spatial distribution of the MW bulge. The clump giants show a barred distribution seen in other sources, with the closer side of the bar located at positive longitudes \cite{37}, \cite{38}. There is a clear magnitude difference between the near and far sides of the bar, about 0.5 mag every 20 degrees. The RR Lyrae are excellent distance indicators, and should show the bar effect if this is present. We have computed the mean magnitudes of the bulge RR Lyrae in the different MACHO fields. Figure 6 shows the mean reddening-independent magnitudes of the RRab and RRc in each of the MACHO bulge fields. Each point comes from averaging 20-90 stars. RR Lyrae belonging to the foreground or to the Sgr dwarf have been discarded before computing these mean magnitudes. It is evident that the RR Lyrae do not follow the expected barred distribution indicated by the solid line. This result confirms previously unpublished results from the Palomar-Groningen field \cite{46}.

The morphology of the Bailey diagram (amplitude-period diagram) is determined in part by the metallicity of the population \cite{9}. This diagram allows us to obtain relative abundances, and to divide the RRab sample into three bins, containing metal-poor, intermediate metallicity, and metal-rich RRab stars. We have computed the mean $W_V$ magnitudes of these three RRab subsamples of different metallicities. These do not show a barred distribution, with the possible exception of the most metal-rich ones. For the metal-rich subsample, the bar cannot be ruled out within the errors. Note that a potentially more precise way to measure metallicities directly from their light curves requires the use of the Fourier coefficients \cite{20}.

Having established that the line of sight distribution of RR Lyrae is not barred, we will now examine the radial dependence of their surface density distribution. This is complicated by effects such as incompleteness, the line of sight depth of the bulge, the presence of a mixed population and of a metallicity gradient. On top of these, reddening is always a concern in bulge fields \cite{28}. We used reddening independent magnitudes, defined as $W = V - 3.97 (V - R)$. In order to evaluate the completeness, we will use the counts of bright W UMa systems in the bulge. Because of our magnitude limits, these systems belong to the disk, and their distribution should be uniform in the MACHO fields. W UMa stars are very numerous variable stars with similar periods and amplitudes as the bulge RR Lyrae, and therefore provide an excellent check on our efficiency to find RR Lyrae in the different bulge fields.

In the innermost bulge fields, where crowding is severe and incompleteness may be higher than 50%, the ratio of relative numbers $N_{RR}/N_{WUMa}$ would give a better indication of the real density profile of the RR Lyrae population. The price to pay here is that we add the Poisson noise of $N_{WUMa}$. While the relative count normalizations in different fields are obtained with the help of the W Umas, the absolute normalization is uncertain. We use the total number of MACHO RR Lyrae discovered in Baade’s Window, which is the most thoroughly studied bulge field, complemented with the searches
Figure 6: Mean magnitudes of RRab (top panel) and RRc (bottom panel) for the 24 MACHO bulge fields as function of Galactic longitude. The solid line shows the trend expected from a barred distribution. This figure shows that the RR Lyr do not follow the barred distribution seen in the clump giants and other tracers.

of [7], [40], and [41].

In these inner MW fields we have to consider the contribution from all possible Galactic components, namely disk, bulge and halo. They have different radial density profiles, and we can try to relate the RR Lyr density distribution to one of these components.

The MW disk behaves as a double exponential, $\rho \propto e^{-r/h_r} e^{-z/h_z}$, with scalelength $h_r = 3.5$ kpc, and scaleheight $h_z = 0.3$ kpc [29]. The peaked magnitude distribution of the RR Lyr in the MACHO fields (Figure 1 of [3]), as well as their concentrated spatial distribution, rules out a significant contribution from disk RR Lyr. The W UMas, however, are useful tracers of the disk, as noted above. We will use these variables to study the structure of the inner disk in a future paper, following [33].

The MW bulge shows a very steep density distribution along the bulge minor axis, traced by K and M giants, IRAS sources, and integrated K-band light. This radial density distribution is represented by a power law, $\rho_b \propto r^{-m}$, with $m = 3.7 - 4.2$ [10]. Such a steep power law with $m = 3.7 - 4.2$ does not fit our observations.

The MW halo outside of the bulge region ($R > 3$ kpc), traced by halo globulars [19], RR Lyrae stars [34], field BHB stars [32], also shows a power law density distribution, $\rho_h \propto r^{-n}$, although shallower, with $n = 3.0 - 3.5$. The RR Lyr in the MACHO fields are more consistent with the extrapolation of such a power law with $n = 3.0 - 3.2$ for $0.3 < R < 1$ kpc, extending the results on the Palomar-Groningen field at $R = 1$ kpc [10].

Once again, the radial density profile of bulge RR Lyr is different from the bulk of the metal-rich bulge component represented by K and M giants. The most straightforward interpretation is that these represent different populations, tracing different components of the MW. The RR Lyr would belong to the inner extension of the halo, which is relatively metal-poor, while the dominant metal-rich component traced by the clump giants would represent the bar [24].
Figure 7: Galactic meridien de Paris, showing schematically the distances to the Sgr dwarf galaxy measured at different Galactic latitudes using RR Lyr stars (large circles). The sizes of the circles roughly scale with the errors in the distance determinations. From top to bottom, the MACHO distance, the DUO distance, and two OGLE distances. Paris is at (0,0), and the MW bulge is at (8,0).

5 RR Lyrae in the Sgr Dwarf

From the magnitude distribution of RR Lyr in the MACHO bulge database we found about 50 RR Lyr that are fainter than a typical bulge RR Lyr by ~ 2.2 mag. These belong to the Sgr dwarf [3], extending even more the known size of Sgr: its major axis would now cover ≥ 20° in the sky. These faint RR Lyr can be used to obtain an accurate distance of Sgr in the MACHO fields. This distance turns out to be smaller than that measured in other fields [23], [24], [1], as shown in Figure 7. This has allowed us to obtain the 3-dimensional shape of the Sgr dwarf.

The discovery of Sgr RR Lyr in the bulge fields is significant because the observed microlensing optical depth towards the bulge was larger than expected [13]. Most, if not all, of the large optical depth may be explained by the presence of a bar in the inner MW, pointing almost towards the Sun [30]. However, MACHO has detected 100 microlensing events towards the MW bulge as of June 1996. As the sample increases in size, it is tempting to consider that a small fraction of the events may have sources in the Sgr dwarf [12], [3]. Note that Sgr will provide a relatively small number of sources, but the number of bulge lenses is large. Because we know the geometry, as well as the relative velocities involved, this opens up the interesting possibility of directly measuring the mass of a lens for the configuration (source, lens) = (Sgr, bulge). A first, and relatively simple, step towards identifying possible Sgr sources would be to acquire accurate radial velocities for the observed events.

6 Summary

We are exploring the RR Lyr in the MACHO database. A comparison between the properties of the RR Lyr in the LMC, the MW bulge, and the Sgr dwarf yields several interesting results:

- The large number of RR Lyr in the LMC and the MW bulge allowed us to identify uncommon pulsation modes.
- LMC and MW bulge RR Lyr have different properties, mostly due to their different metallicities.
- The RR Lyr population in the MW bulge is not barred, in contrast with the clump giants.
- The Sgr dwarf is very extended, > 20° along its major axis.
• The number of microlensing events detected in the MW bulge is large enough (> 100) that the sample may already contain some due to sources in the Sgr dwarf.

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