Measurement of indirect $CP$ asymmetries in $D^0 \rightarrow K^- K^+$ and $D^0 \rightarrow \pi^- \pi^+$ decays using semileptonic $B$ decays

LHCb Collaboration; Aaij, R; Adeva, B; Adinolfi, M; Anderson, J; Bernet, R; Bowen, E; Bursche, A; Chiapolini, N; Chrzaszcz, M; Dey, B; Elsasser, C; Graverini, E; Lionetto, F; Lowdon, P; Mauri, A; Müller, K; Serra, N; Steinkamp, O; Storaci, B; Straumann, U; Tresch, M; Vollhardt, A; et al

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$$A_{\Gamma}(K^- K^+) = (-0.134 \pm 0.077 ^{+0.026}_{-0.034})\%,$$
$$A_{\Gamma}(\pi^- \pi^+) = (-0.092 \pm 0.145 ^{+0.025}_{-0.033})\%,$$

where the first uncertainties are statistical and the second systematic. This result is in agreement with previous measurements and with the hypothesis of no indirect $CP$ violation in $D^0$ decays.

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†Authors are listed at the end of this paper.
1 Introduction

In neutral meson systems, mixing may occur between the particle and anti-particle states. This mixing is very small in the charm-meson ($D^0$) system. Experimentally, a small, non-zero $D^0$–$\bar{D}^0$ mixing is now firmly established by several experiments [1–6], where the average of these measurements excludes zero mixing at more than 11 standard deviations [7]. This opens up the possibility to search for a breaking of the charge-parity ($CP$) symmetry occurring in the $D^0$–$\bar{D}^0$ mixing alone or in the interference between the mixing and decay amplitudes. This is called indirect $CP$ violation and the corresponding asymmetry is predicted to be $O(10^{-4})$ [8, 9], but can be enhanced in theories beyond the Standard Model [10]. Indirect $CP$ violation can be measured in decays to $CP$ eigenstates such as the singly Cabibbo-suppressed decays $D^0 \to K^- K^+$ and $D^0 \to \pi^- \pi^+$ (the inclusion of charge-conjugate processes is implied hereafter) from the asymmetry between the effective $D^0$ and $\bar{D}^0$ lifetimes, $A_T$. The effective lifetime is the lifetime obtained from a single exponential fit to the decay-time distribution. Several measurements of $A_T$ exist [1,11,12]. The most precise determination was made by LHCb with data corresponding to 1.0 fb$^{-1}$ of integrated luminosity, resulting in $A_T(K^- K^+) = (-0.035 \pm 0.062 \pm 0.012)\%$, and $A_T(\pi^- \pi^+) = (0.033 \pm 0.106 \pm 0.014)\%$ [11]. When indirect $CP$ violation is assumed to be the same in the two modes, the world average becomes $A_T = (-0.014 \pm 0.052)\%$ [7].

In all previous measurements of $A_T$, the initial flavour of the neutral charm meson (i.e., whether it was a $D^0$ or $\bar{D}^0$ state) was determined (tagged) by the charge of the pion in a $D^* \to D^0 \pi$ decay. In this paper, the time-dependent $CP$ asymmetry is measured in $D^0$ decays originating from semileptonic $b$-hadron decays, where the charge of the accompanying muon is used to tag the flavour of the $D^0$ meson. These samples are dominated by $B^- \to D^0 \mu^- \bar{\nu}_\mu X$ and $\bar{B}^0 \to D^0 \mu^- \bar{\nu}_\mu X$ decays, where $X$ denotes other particle(s) possibly produced in the decay. The same data samples as for the measurement of time-integrated $CP$ asymmetries [13] are used.

2 Formalism and method

The time-dependent $CP$ asymmetry for a neutral $D$ meson decaying to a $CP$ eigenstate, $f$, is defined as

$$A_{CP}(t) \equiv \frac{\Gamma(D^0 \to f; t) - \Gamma(\bar{D}^0 \to f; t)}{\Gamma(D^0 \to f; t) + \Gamma(\bar{D}^0 \to f; t)},$$

(1)

where $\Gamma(D^0 \to f; t)$ and $\Gamma(\bar{D}^0 \to f; t)$ are the time-dependent partial widths of initial $D^0$ and $\bar{D}^0$ mesons to final state $f$. The $CP$ asymmetry can be approximated as [14]

$$A_{CP}(t) \approx A_{CP}^{dir} - A_T \frac{t}{\tau},$$

(2)
where $A^{\text{dir}}_{CP}$ is the direct $CP$ asymmetry and $\tau$ is the $D^0$ lifetime. The linear decay-time dependence is determined by $A_{\Gamma}$, which is formally defined as

$$A_{\Gamma} \equiv \frac{\hat{\Gamma}_{D^0} - \hat{\Gamma}_{\bar{D}^0}}{\Gamma_{D^0} + \Gamma_{\bar{D}^0}} ,$$

where $\hat{\Gamma}$ is the effective partial decay rate of an initial $D^0$ or $\bar{D}^0$ state to the $CP$ eigenstate. Furthermore, $A_{\Gamma}$ can be approximated in terms of the $D^0$-$\bar{D}^0$ mixing parameters, $x$ and $y$, as

$$A_{\Gamma} \approx \left( A^{\text{mix}}_{CP}/2 - A^{\text{dir}}_{CP} \right) y \cos \phi - x \sin \phi ,$$

where $A^{\text{mix}}_{CP} = |q/p|^2 - 1$ describes $CP$ violation in $D^0$-$\bar{D}^0$ mixing, with $q$ and $p$ the coefficients of the transformation from the flavour basis to the mass basis, $|D_{1,2}⟩ = p|D^0⟩ ± q|\bar{D}^0⟩$. The weak phase $\phi$ describes $CP$ violation in the interference between mixing and decay, and is specific to the decay mode. Finally, $A_{\Gamma}$ receives a contribution from direct $CP$ violation as well.

The raw asymmetry is affected by the different detection efficiencies for positive and negative muons, and the different production rates of $D^0$ and $\bar{D}^0$ mesons. These effects introduce a shift to the constant term in Eq. (2), but have a negligible effect on the measurement of $A_{\Gamma}$ (see Sect. 6). The decay $D^0 \to K^-\pi^+$, also flavour-tagged by the muon from a semileptonic $b$-hadron decay, is used as a control channel. Since this is a Cabibbo-favoured decay mode, direct $CP$ violation is expected to be negligible. More importantly, any indirect $CP$ violation is heavily suppressed as the contribution from doubly Cabibbo-suppressed $D^0 \to K^+\pi^-$ decays is small.

## 3 Detector and simulation

The LHCb detector [17,18] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing $b$ or $c$ quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the $pp$ interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes placed downstream of the magnet. The polarity of the magnetic field is regularly reversed during data taking. The tracking system provides a measurement of momentum, $p$, with a relative uncertainty that varies from 0.5% at low momentum to 1.0% at 200 GeV/$c$. The minimum distance of a track to a primary vertex, the impact parameter, is measured with a resolution of $(15 + 29/p_{T}) \mu$m, where $p_{T}$ is the component of the momentum transverse to the beam, in GeV/$c$. Different types of charged hadrons are distinguished using information from two ring-imaging Cherenkov detectors. Photon, electron and hadron candidates are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter and a hadronic calorimeter. Muons are identified by a system composed of alternating layers
of iron and multiwire proportional chambers, situated behind the hadronic calorimeter. The trigger \cite{19} consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full event reconstruction.

In the simulation, $pp$ collisions are generated using \textsc{Pythia} \cite{20} with a specific LHCb configuration \cite{21}. Decays of hadronic particles are described by \textsc{EvtGen} \cite{22}, in which final-state radiation is generated using \textsc{Photos} \cite{23}. The interaction of the generated particles with the detector, and its response, are implemented using the \textsc{Geant4} toolkit \cite{24} as described in Ref. \cite{25}.

4 Data set and selection

This analysis uses a data set corresponding to an integrated luminosity of 3.0 fb$^{-1}$. The data were taken at two different $pp$ centre-of-mass energies: 7 TeV in 2011 (1.0 fb$^{-1}$) and 8 TeV in 2012 (2.0 fb$^{-1}$). The data sets recorded with each dipole magnet polarity are roughly equal in size.

At the hardware trigger stage, the events are triggered by the presence of the muon candidate in the muon system. This requires the muon $p_T$ to be greater than 1.64 GeV/c (1.76 GeV/c) for the 2011 (2012) data. At the software trigger stage, one of the final-state particles is required to have enough momentum and be significantly displaced from any primary $pp$ vertex. In addition, the candidates must be selected by a single-muon trigger or by a topological trigger that requires the muon and one or two of the $D^0$ daughters to be consistent with the topology of $b$-hadron decays \cite{19}.

To further suppress background, the $D^0$ daughters are required to have $p_T > 300$ MeV/c. All final-state particles are required to have a large impact parameter and be well identified by the particle identification systems. The impact parameter requirement on the muon reduces the contribution from $D^0$ mesons produced directly in the $pp$ interaction to below 2%. The scalar $p_T$ sum of the $D^0$ daughters should be larger than 1.4 GeV/c, and the $p_T$ of the $D^0$ candidate should be larger than 0.5 GeV/c. The two tracks from the $D^0$ candidate and the $D^0\mu$ combination are required to form good vertices and the latter vertex should be closer to the primary vertex than the $D^0$ vertex. The $D^0$ decay time is determined from the distance between these two vertices, and the reconstructed $D^0$ momentum. The invariant mass of the $D^0\mu$ combination is required to be between 2.5 and 5.0 GeV/c$^2$, where the upper bound suppresses hadronic $b$-hadron decays into three-body final states. Backgrounds from inclusive $b$-hadron decays into charmonium are suppressed by vetoing candidates where the invariant mass of the muon and the oppositely charged $D^0$ daughter, misidentified as a muon, is consistent with the $J/\psi$ or $\psi(2S)$ mass. Additionally, the invariant mass of the muon and same-charge $D^0$ daughter, under the muon mass hypothesis, is required to be larger than 240 MeV/c$^2$ to remove events where a single charged particle is reconstructed as two separate tracks. For most selection requirements, the efficiency is roughly independent of the $D^0$ decay time, giving efficiency variations of $O(1\%)$. The largest dependence on the decay time comes from the topological trigger, which introduces an efficiency profile that decreases with $D^0$ decay time, resulting in about
20% relative efficiency loss at large decay times.

\section{Determination of $A_\Gamma$}

The mass distributions for the selected $D^0 \to K^- K^+$, $D^0 \to \pi^- \pi^+$ and $D^0 \to K^- \pi^+$ candidates are shown in Fig. 1. The numbers of signal candidates are determined from unbinned extended maximum-likelihood fits in the range 1810 to 1920 MeV/c^2. The signal for all three decay modes is modelled by a sum of three Gaussian functions. The first two have the same mean, but independent widths; the third is used to describe a small radiative tail, and has a lower mean and larger width. The effective width of the signal ranges from 7.1 MeV/c^2 for $D^0 \to K^- K^+$ candidates to 9.3 MeV/c^2 for $D^0 \to \pi^- \pi^+$ candidates. As the final states $K^- K^+$ and $\pi^- \pi^+$ are charge symmetric, the shape parameters for the signal are the same for both $D^0$ and $\bar{D}^0$ candidates. The combinatorial background is modelled by an exponential function. In the $\pi^- \pi^+$ invariant mass distribution, a reflection from $D^0 \to K^- \pi^+$ decays is visible in the region below 1820 MeV/c^2. This background component is modelled by a single Gaussian function and the fit range is extended from 1795 to 1930 MeV/c^2. The shape parameters and overall normalisation of the background components are allowed to differ between $D^0$ and $\bar{D}^0$ candidates. The numbers of signal candidates obtained from these global fits are $2.33 \times 10^6$ for $D^0 \to K^- K^+$, $0.79 \times 10^6$ for $D^0 \to \pi^- \pi^+$ and $11.31 \times 10^6$ for $D^0 \to K^- \pi^+$ decays. The latter number corresponds to only half of the available $D^0 \to K^- \pi^+$ candidates, randomly selected, to reduce the sample size.

The raw $CP$ asymmetry is determined from fits to the mass distributions in 50 bins of the $D^0$ decay time. The fits are performed simultaneously for $D^0$ and $\bar{D}^0$ candidates and the asymmetry is determined for each decay-time bin. The shape parameters and relative normalisation for the third Gaussian function and for the $D^0 \to K^- \pi^+$ reflection background are fixed from the global fit. All other parameters are allowed to vary in these fits. In particular, since both the amount and the composition of background depend on the decay time, the background parameters are free to vary in each decay-time bin. For decay times larger than 1 ps the relative contribution from combinatorial background increases. This is due to the exponential decrease of the signal and a less steep dependence of the combinatorial background on the decay time. The mass distribution in each decay-time bin is well described by the model.

Events at large $D^0$ decay times have a larger sensitivity to $A_\Gamma$ compared to events at small decay times, which is balanced by the fewer signal candidates at large decay times. The binning in $D^0$ decay time is chosen such that every bin gives roughly the same statistical contribution to $A_\Gamma$. The value of $A_\Gamma$ is determined from a $\chi^2$ fit to the time-dependent asymmetry of Eq. (2). The value of $A_\Gamma$ and the offset in the asymmetry are allowed to vary in the fit, while the $D^0$ lifetime is fixed to $\tau = 410.1$ fs \cite{26}. Due to the exponential decay-time distribution, the average time in each bin is not in the centre of the bin. Therefore, the background-subtracted \cite{27} average decay time is determined in each bin and used in the fit. This fit procedure gives unbiased results and correct uncertainties,
as is verified by simulating many experiments with large samples.

The measured asymmetries in bins of decay time are shown in Fig. 2 including the result of the time-dependent fit. The results in the three decay channels are

\[
A_Γ(K^-K^+) = (-0.134 \pm 0.077)\% ,
\]

\[
A_Γ(\pi^-\pi^+) = (-0.092 \pm 0.145)\% ,
\]

\[
A_Γ(K^-\pi^+) = (0.009 \pm 0.032)\% ,
\]

where the uncertainties are statistical only. The values for \( A_Γ \) are compatible with the assumption of no indirect CP violation. The fits have good \( p \)-values of 54.3\% \( (D^0 \to K^-K^+) \), 30.8\% \( (D^0 \to \pi^-\pi^+) \) and 14.5\% \( (D^0 \to K^-\pi^+) \). The measured values for the raw time-integrated asymmetries, which are sensitive to direct CP violation, agree with those reported in Ref. [13].
Figure 2: Raw $CP$ asymmetry as function of $D^0$ decay time for (a) $D^0 \rightarrow K^- K^+$, (b) $D^0 \rightarrow \pi^- \pi^+$ and (c) $D^0 \rightarrow K^- \pi^+$ candidates. The results of the $\chi^2$ fits are shown as blue, solid lines with the $\pm 1$ standard-deviation ($\sigma$) bands indicated by the dashed lines. The green, dashed lines indicate one $D^0$ lifetime ($\tau = 410.1$ fs). Underneath each plot the pull in each time bin is shown.
Table 1: Contributions to the systematic uncertainty of $A_\Gamma(K^-K^+)$ and $A_\Gamma(\pi^-\pi^+)$. The constant and multiplicative scale uncertainties are given separately.

| Source of uncertainty                          | $D^0 \to K^-K^+$ constant | $D^0 \to K^-K^+$ scale | $D^0 \to \pi^-\pi^+$ constant | $D^0 \to \pi^-\pi^+$ scale |
|-----------------------------------------------|----------------------------|-------------------------|-------------------------------|----------------------------|
| Mistag probability                            | 0.006%                     | 0.05                    | 0.008%                       | 0.05                      |
| Mistag asymmetry                              | 0.016%                     | 0.016%                  |                               |                           |
| Time-dependent efficiency                     | 0.010%                     | 0.010%                  |                               |                           |
| Detection and production asymmetries          | 0.010%                     | 0.010%                  |                               |                           |
| $D^0$ mass fit model                          | 0.011%                     | 0.007%                  |                               |                           |
| $D^0$ decay-time resolution                   | 0.09                       | 0.07                    |                               |                           |
| $B^0 - \bar{B}^0$ mixing                      | 0.007%                     | 0.007%                  |                               |                           |
| Quadratic sum                                 | 0.026%                     | 0.10                    | 0.025%                       | 0.09                      |

6 Systematic uncertainties and consistency checks

The contributions to the systematic uncertainty on $A_\Gamma$ are listed in Table 1. The largest contribution is due to the background coming from random combinations of muons and $D^0$ mesons. When the muon has the wrong charge compared to the real $D^0$ flavour, this is called a mistag. The mistag probability ($\omega$) dilutes the observed asymmetry by a factor $(1 - 2\omega)$. This mistag probability is measured using $D^0 \to K^-\pi^+$ decays, exploiting the fact that the final state determines the flavour of the $D^0$ meson, except for an expected time-dependent wrong-sign fraction due to $D^0 - \bar{D}^0$ mixing and doubly Cabibbo-suppressed decays. The mistag probability before correcting for wrong-sign decays is shown in Fig. 3. After subtracting the (time-dependent) wrong-sign ratio $[3]$, the mistag probability as function of $D^0$ decay time is obtained. The mistag probability is small, with an average around 1%, but it is steeply increasing, reaching 5% at five $D^0$ lifetimes. This is due to the increase of the background fraction from real $D^0$ mesons from $b$-hadron decays combined with a muon from the opposite-side $b$-hadron decay. This random-muon background is reconstructed with an apparently longer lifetime. The time-dependent mistag probability is parameterised by an exponential function, which is used to determine the shift in $A_\Gamma$. The systematic uncertainty from this time-dependent mistag probability is 0.006% for the $D^0 \to K^-K^+$ and 0.008% for the $D^0 \to \pi^-\pi^+$ decay mode, with a supplementary, multiplicative scale uncertainty of 0.05 for both decay modes.

The mistag probabilities can potentially differ between positive and negative muons. Such a mistag asymmetry would give a direct contribution to the observed asymmetry. The slope of the mistag asymmetry is also obtained from $D^0 \to K^-\pi^+$ decays. This slope is consistent with no time dependence, and its statistical uncertainty (0.016%) is included in the systematic uncertainty on $A_\Gamma$.

The selection of signal candidates, in particular the topological software trigger, is known to introduce a bias in the observed lifetime. Such a bias could be charge dependent,
Figure 3: Mistag probability, before subtracting the contribution from wrong-sign (WS) decays, determined with $D^0 \to K^-\pi^+$ candidates. The result of the fit to the data points with an exponential function is overlaid (solid, blue line). The red, dashed line indicates the expected mistag contribution from WS decays.

thus biasing the measurement of $A_\Gamma$. It is studied with the $D^0 \to K^-\pi^+$ sample and a sample of $D^- \to K^+\pi^-\pi^-$ decays from semileptonic $b$-hadron decays. No asymmetry of the topological triggers in single-muon-triggered events is found within an uncertainty of 0.010%. This number is propagated as a systematic uncertainty.

The detection and production asymmetries introduce a constant offset in the raw time-dependent asymmetries. Since these asymmetries depend on the muon or $b$-hadron momentum, they can also introduce a time dependence in case the momentum spectrum varies between decay-time bins. This effect is tested by fitting the time-dependent asymmetry after weighting the events so that all decay-time bins have the same $D^0$ or muon momentum distribution. The observed shifts in $A_\Gamma$ are within the statistical variations. The shift (0.010\%) observed in the larger $D^0 \to K^-\pi^+$ sample, which has the same production asymmetry and larger detection asymmetry, is taken as a measure of the systematic uncertainty.

An inaccurate model of the mass distribution can introduce a bias in $A_\Gamma$. The effect on the observed asymmetries is studied by applying different models in the fits to the invariant mass distributions. For the signal, a sum of two Gaussian functions with and without an exponential tail, and for the background a first and a second-order polynomial are tested. The maximum variation from the default fit for each decay mode (0.011\% for $D^0 \to K^-K^+$; 0.007\% for $D^0 \to \pi^-\pi^+$) is taken as a systematic uncertainty on $A_\Gamma$.

The $D^0$ decay-time resolution affects the observed time scale, and therefore changes the measured value of $A_\Gamma$. For each decay mode, the resolution function is obtained from the simulation, which shows that for the majority of the signal (90\%) the decay time is measured with an RMS of about 103 fs. The remaining candidates (10\%) are measured with an RMS of about 312 fs. The theoretical decay rates are convolved with the resolution
functions in a large number of simulated experiments. The effect of the time resolution scales linearly with the size of $A_Γ$. The corresponding scale uncertainty on $A_Γ$ is 0.09 for the $D^0 \rightarrow K^- K^+$ decay mode and 0.07 for the $D^0 \rightarrow \pi^- \pi^+$ decay mode. Decays where the muon gives the correct tag but the decay time is biased, e.g., when the muon originates from a $τ$ lepton in the semileptonic $b$-hadron decay, are studied and found to be negligible.

About 40% of the muon-tagged $D^0$ decays originate from neutral $B$ mesons [28]. Due to $B^0$–$B^0$ mixing the observed production asymmetry depends on the $B^0$ decay time [29]. A correlation between the $B^0$ and $D^0$ decay times may result in a shift in the measured value of $A_Γ$. The effect of this correlation, determined from simulation, together with a 1% $B^0$ production asymmetry [29,30], is estimated to be a shift of 0.007% in the observed value of $A_Γ$. This is taken as systematic uncertainty.

Possible shifts in $A_Γ$ coming from the 1.5 fs uncertainty on the world-average $D^0$ lifetime [26], from the uncertainty on the momentum scale and detector length scale [31,32] and from potential biases in the fit method are negligible.

The scale uncertainty (cf. Table 1) gives a small contribution to the overall systematic uncertainty, which depends on the true value of $A_Γ$. In order to present a single systematic uncertainty, the effect of the scale uncertainty is evaluated with a Neyman construction [33]. For each true value of $A_Γ$, the absolute size of the scale uncertainty is known and added in quadrature to the constant uncertainty. In this way, a confidence belt of observed values versus true values is constructed. This procedure gives a slightly asymmetric systematic uncertainty, which is $^{+0.026}_{-0.034}$% for the $D^0 \rightarrow K^- K^+$ decay channel and $^{+0.025}_{-0.033}$% for the $D^0 \rightarrow \pi^- \pi^+$ decay channel. Except for the contribution from the mass fit model, all contributions to the systematic uncertainty are fully correlated, resulting in an overall correlation coefficient of 89% between the systematic uncertainties of $A_Γ(K^- K^+)$ and $A_Γ(\pi^- \pi^+)$. Additional checks have been performed to determine potential sensitivity of the measurements on the data-taking conditions, detector configuration, and analysis procedure. Changing to a finer decay-time binning yields compatible results. Potential effects on the measurement of $A_Γ$ coming from detection asymmetries are expected to appear when dividing the data set by magnet polarity and data-taking period. Detection asymmetries originating from a left-right asymmetric detector change sign when reversing the magnet polarity. Similarly, during the two data-taking periods, detection asymmetries and production asymmetries might have changed due to different running conditions. As shown in Fig. 4 there is no significant variation of $A_Γ$ across various configurations. Also splitting the data set according to the number of primary vertices or in bins of the $B$ decay time does not show any deviation in the measured values of $A_Γ$.

7 Conclusions

The time-dependent $CP$ asymmetries in $D^0 \rightarrow K^- K^+$ and $D^0 \rightarrow \pi^- \pi^+$ decays are measured using muon-tagged $D^0$ mesons originating from semileptonic $b$-hadron decays in the 3.0 fb$^{-1}$ data set collected with the LHCb detector in 2011 and 2012. The asymmetries in the
Figure 4: Measured values of $A_\Gamma$ for different magnet polarities and data-taking periods for (a) $D^0 \to K^- K^+$, (b) $D^0 \to \pi^- \pi^+$ and (c) $D^0 \to K^- \pi^+$ decays. The vertical line and error band indicate the average $A_\Gamma$ obtained from the combined data set. The error bars indicate the statistical uncertainty only.

effective lifetimes are measured to be

$$A_\Gamma(K^- K^+) = (-0.134 \pm 0.077^{+0.026}_{-0.034})\%,$$
$$A_\Gamma(\pi^- \pi^+) = (-0.092 \pm 0.145^{+0.025}_{-0.033})\%,$$

where the first uncertainty is statistical and the second systematic. Assuming that indirect $CP$ violation in $D^0$ decays is universal \cite{10}, and accounting for the correlation in the systematic uncertainties, the average of the two measurements becomes $A_\Gamma = (-0.125 \pm 0.073)\%$. The results in this paper are uncorrelated with the time-integrated asymmetries reported in Ref. \cite{13}. The results are consistent with other $A_\Gamma$ measurements \cite{1,11,12}, and independent of the $A_\Gamma$ measurements \cite{11} from LHCb using $D^0$ mesons from $D^{*+} \to D^0 \pi^+$ decays. They are consistent with the hypothesis of no indirect $CP$ violation in $D^0 \to K^- K^+$ and $D^0 \to \pi^- \pi^+$ decays.

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R. Aaij41, B. Adeva37, M. Adinolfi46, A. Affolder52, Z. Ajaltouni5, S. Aka6, J. Albrecht9, F. Alessio38, M. Alexander51, S. Ali41, G. Alkhazov30, P. Alvarez Cartelle53, A.A. Alves Jr.25,38, S. Amato2, S. Amerio22, Y. Amhis7, L. An3, L. Anderlini17,9, J. Anderson40, R. Andreassen57, M. Andreotti16,f, J.E. Andrews58, R.B. Appleby34, O. Aquines Gutierrez10, F. Archilli38, A. Artamonov35, M. Artuso59, E. Aslanides8, G. Auriemma25,n, M. Baalouch5, S. Bachmann11, J.J. Back48, A. Badalov36, C. Baess060, W. Baldini16, R.J. Barlow54, C. Barschel38, S. Barsuk7, W. Barter38, V. Batozskaya28, V. Battista39, A. Bay39, L. Beaucourt4, J. Beddow51, F. Bedeschi23, I. Bediaga1, S. Belogurov31, I. Belyaev31, E. Ben-Haim8, G. Bencivenni18, S. Benson38, L. Benton46, A. Berezhnoy32, R. Beron40, A. Bertolini22, M.-O. Bettler47, M. van Beuzekom41, A. Bien11, S. Bifani19, T. Bird54, A. Bizzeti17,3, T. Blake48, F. Blanc39, J. Blouw10, S. Blusk59, V. Bocci25, A. Bondar34, N. Bondas30,38, W. Bonivent015, S. Borgi43, A. Borgia59, M. Borsato7, T.J.V. Bowcock52, E. Bowen40, C. Bozzi16, D. Brett54, M. Britsch10, T. Britton59, J. Brodzicka54, N.H. Brook46, A. Bursche40, J. Buytaert38, S. Cadeddu15, R. Calabrese16,f, M. Calvi24,k, M. Calvo Gomez36,p, P. Campana16, D. Campora Perez58, L. Capriotti54, A. Carbone14,d, G. Carboni24,l, R. Cardinale19,38,j, A. Cardini55, P. Carniti20, L. Carson30, K. Carvalho Akiba138, RCM Casanova Mohr36, G. Casse52, L. Cassina20,k, L. Castillo Garcia38, M. Cattaneo38, Ch. Cauet9, G. Cavallero19, R. Cenci24,t, M. Charles8, Ph. Charpentier53, M. Chefdeville4, S. Chen54, S.-F. Cheung55, N. Chiapolini40, M. Chrzaszczy40,26, X. Cid Vidal38, G. Ciezarek41, P.E.L. Clarke50, M. Clemencie438, H.V. Cliff47, J. Closier38, V. Coco38, J. Cogan5, E. Cogneras3, V. Cogoni15, e, L. Cojocariu29, G. Collazuol22, P. Collins38, A. Comerma-Montells11, A. Contu15,38, A. Cook46, M. Coombes36, S. Coqueran8, G. Corti38, M. Corvo7, f, I. Counts56, B. Couturier38, G.A. Cowan50, D.C. Craik48, A.C. Crocombe48, M. Cruz Torres60, S. Cunliffe53, R. Currie53, C. D’Ambrosio38, J. Dalseno46, P. David8, P.N.Y. David41, A. Davis57, K. De Bruyn43, S. De Capua54, M. De Cian11, J.M. De Miranda1, L. De Paula2, W. De Silva57, P. De Simone18, C.-T. Dean51, D. Decamp4, M. Dechenhoff9, L. Del Buono8, N. Déleage4, D. Derkach55, O. Deschamps3, F. Dettori38, B. Dev40, A. Di Canto38, A Di Domenico25, F. Di Ruscio24, H. Dijkstra38, S. Donleavy52, F. Dordei11, M. Dorigo39, A. Dosil Suárez37, D. Dossett48, A. Dovbnya43, KD Dreimanis52, K. Dreimanis52, G. Dujany34, F. Dupertuis39, P. Durante6, R. Dzhelyadin35, A. Dziura26, A. Dzyuba30, S. Easo30, U. Egede53, V. Eggorichev34, S. Eidelman34, S. Eisenhardt50, U. Eitschberger9, R. Ekelhof6, L. Eklund34, I. El Rafai5, Ch. Elsasser40, S. Ely59, S. Enen14, H.M. Evans47, T. Evans55, A. Falabella14, C. Färber11, C. Farinelli41, N. Farley45, S. Farry52, R. Fay52, D. Ferguson50, V. Fernandez Albors37, F. Ferreira Rodrigues4, M. Ferro-Luzzi38, S. Filippov33, M. Fiore16,f, M. Fiorini16,f, M. Firlej27, C. Fitzpatrick39, T. Fiatowski27, P. Floyd53, M. Fontana16, F. Fontanelli19, R. Forte38, O. Francisco2, M. Frank38, C. Frei38, M. Froisini17, J. Fu21,38, E. Furfaro24,l, A. Gallas Torreira37, D. Galli14,d, S. Gallorini22,38, S. Gambetta19,j, M. Gandelman2, P. Gandini59, Y. Gao3, J. García Pardiñas37, J. Garofoli59, J. Garra Tico47, L. Garrido36, D. Gascon36, C. Gaspar38, U. Gastald16, R. Gaul55, L. Gavardi9, G. Gazzoni5, A. Gera1, E. Gersabeck11, M. Gersabeck54, T. Gershon48, Ph. Ghez4, A. Gianelle22, S. Giani39, V. Gibson47, L. Giubega29, V.V. Gligorov38, C. Gőbel56, D. Golubkov31, A. Golutvin34,31,38, A. Gomes3,a, C. Gotti20,8, M. Grabalosa Gándara5, R. Graciani Diaz36, L.A. Granado Cardoso38, E. Graugés36, E. Graverini40, G. Graziani17, A. Grecu29, E. Greening55, S. Gregson47, P. Griffith45, L. Grillo11, O. Grünberg63, B. Gui49, E. Gushchin33, Yu. Guz35,38, T. Gys38, C. Hadjivasiliiou59, G. Haefeli39, C. Haen38, S.C. Haines47, S. Hall53,
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D.M. Saunders\textsuperscript{46}, D. Savrina\textsuperscript{31,32}, M. Schiller\textsuperscript{38}, H. Schindler\textsuperscript{38}, M. Schlupp\textsuperscript{9}, M. Schmelling\textsuperscript{10},
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M. Straticiu\textsuperscript{29}, U. Straumann\textsuperscript{40}, R. Stroili\textsuperscript{22}, L. Sun\textsuperscript{57}, W. Sutcliffe\textsuperscript{53}, K. Swientek\textsuperscript{27},
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D. Tonelli\textsuperscript{38}, S. Topp-Joergensen\textsuperscript{55}, N. Torr\textsuperscript{55}, E. Tournefier\textsuperscript{4}, S. Tourneur\textsuperscript{39}, K Trabelsi\textsuperscript{39},
M.T. Tran\textsuperscript{39}, M. Tresch\textsuperscript{40}, A. Trisovic\textsuperscript{38}, A. Tsaregorodtsev\textsuperscript{6}, P. Tsypelas\textsuperscript{41}, N. Tuning\textsuperscript{41,38},
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G. Valenti\textsuperscript{14}, A. Vallier\textsuperscript{7}, R. Vazquez Gomez\textsuperscript{18}, P. Vazquez Regueiro\textsuperscript{37}, C. Vázquez Sierra\textsuperscript{37},
S. Vecchi\textsuperscript{16}, J.J. Velthuis\textsuperscript{46}, M. Velti\textsuperscript{17,h}, G. Veneziano\textsuperscript{39}, M. Vesterinen\textsuperscript{11},
J.V. Viana Barbosa\textsuperscript{38}, B. Vianu\textsuperscript{7}, D. Vieira\textsuperscript{2}, M. Vieites Diaz\textsuperscript{37}, X. Vilasis-Cardona\textsuperscript{36,p},
A. Vollhardt\textsuperscript{30}, D. Volynskyy\textsuperscript{10}, D. Voong\textsuperscript{46}, A. Vorobyev\textsuperscript{30}, V. Vorobyev\textsuperscript{34}, C. Voß\textsuperscript{53},
J.A. de Vries\textsuperscript{41}, R. Waldi\textsuperscript{63}, C. Wallace\textsuperscript{48}, R. Wallace\textsuperscript{12}, J. Walsh\textsuperscript{23}, S. Wandernoth\textsuperscript{11},
J. Wang\textsuperscript{59}, D.R. Ward\textsuperscript{47}, N.K. Watson\textsuperscript{45}, D. Websdale\textsuperscript{53}, M. Whitehead\textsuperscript{48}, D. Wieder\textsuperscript{11},
G. Wilkinson\textsuperscript{55,38}, M. Wilkinson\textsuperscript{59}, M.P. Williams\textsuperscript{45}, M. Williams\textsuperscript{56}, H.W. Wilschut\textsuperscript{67},
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S.A. Wotton\textsuperscript{47}, S. Wright\textsuperscript{47}, K. Wyllie\textsuperscript{38}, Y. Xie\textsuperscript{61}, Z. Xing\textsuperscript{59}, Z. Xu\textsuperscript{39}, Z. Yang\textsuperscript{3}, X. Yuan\textsuperscript{34},
O. Yushchenko\textsuperscript{35}, M. Zangoli\textsuperscript{14}, M. Zavertyaev\textsuperscript{10,b}, L. Zhang\textsuperscript{3}, W.C. Zhang\textsuperscript{12}, Y. Zhang\textsuperscript{3},
A. Zhelezov\textsuperscript{11}, A. Zhokhov\textsuperscript{31}, L. Zhong\textsuperscript{3}.

\textsuperscript{1}Centro Brasileiro de Pesquisas Físicas (CBPF), Rio de Janeiro, Brazil
\textsuperscript{2}Universidade Federal do Rio de Janeiro (UFRJ), Rio de Janeiro, Brazil
\textsuperscript{3}Center for High Energy Physics, Tsinghua University, Beijing, China
\textsuperscript{4}LAPP, Université de Savoie, CNRS/IN2P3, Annecy-Le-Vieux, France
\textsuperscript{5} Clermont Université, Université Blaise Pascal, CNRS/IN2P3, LPC, Clermont-Ferrand, France
\textsuperscript{6}CPPM, Aix-Marseille Université, CNRS/IN2P3, Marseille, France
\textsuperscript{7}LAL, Université Paris-Sud, CNRS/IN2P3, Orsay, France
\textsuperscript{8}LPNHE, Université Pierre et Marie Curie, Université Paris Diderot, CNRS/IN2P3, Paris, France
\textsuperscript{9}Fakultät Physik, Technische Universität Dortmund, Dortmund, Germany
\textsuperscript{10}Max-Planck-Institut für Kernphysik (MPIK), Heidelberg, Germany
\textsuperscript{11}Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany
\textsuperscript{12}School of Physics, University College Dublin, Dublin, Ireland
\textsuperscript{13}Sezione INFN di Bari, Bari, Italy
\textsuperscript{14}Sezione INFN di Bologna, Bologna, Italy
\textsuperscript{15}Sezione INFN di Cagliari, Cagliari, Italy
\textsuperscript{16}Sezione INFN di Ferrara, Ferrara, Italy
\textsuperscript{17}Sezione INFN di Firenze, Firenze, Italy
\textsuperscript{18}Laboratori Nazionali dell’INFN di Frascati, Frascati, Italy
\textsuperscript{19}Sezione INFN di Genova, Genova, Italy
\textsuperscript{16}
Universidade Federal do Triângulo Mineiro (UFTM), Uberaba-MG, Brazil
P.N. Lebedev Physical Institute, Russian Academy of Science (LPI RAS), Moscow, Russia
Università di Bari, Bari, Italy
Università di Bologna, Bologna, Italy
Università di Cagliari, Cagliari, Italy
Università di Ferrara, Ferrara, Italy
Università di Firenze, Firenze, Italy
Università di Urbino, Urbino, Italy
Università di Modena e Reggio Emilia, Modena, Italy
Università di Genova, Genova, Italy
Università di Milano Bicocca, Milano, Italy
Università di Roma Tor Vergata, Roma, Italy
Università di Roma La Sapienza, Roma, Italy
Università della Basilicata, Potenza, Italy
AGH - University of Science and Technology, Faculty of Computer Science, Electronics and Telecommunications, Kraków, Poland
LIFAELS, La Salle, Universitat Ramon Llull, Barcelona, Spain
Hanoi University of Science, Hanoi, Viet Nam
Università di Padova, Padova, Italy
Università di Pisa, Pisa, Italy
Scuola Normale Superiore, Pisa, Italy
Università degli Studi di Milano, Milano, Italy
Politecnico di Milano, Milano, Italy