Article

Reversible Diels–Alder Addition to Fullerenes: A Study of Dimethylanthracene with H$_2$@C$_{60}$

Mahboob Subhani 1,†, Jinrong Zhou 1,†, Yuguang Sui 1, Huijing Zou 2, Michael Frunzi 3, James Cross 3,*, Martin Saunders 3, Cijun Shuai 4,*, Wenjie Liang 1,*, and Hai Xu 1,5,*

1 College of Chemistry and Chemical Engineering, Central South University, South Lushan Road, Changsha 410083, China; mehboobsuhhani814@gmail.com (M.S.); 18171099526@163.com (J.Z.); sui_yg@csu.edu.cn (Y.S.)
2 Department of Biology, College of Arts and Science, New York University, New York, NY 10012, USA; hz2750@nyu.edu
3 Department of Chemistry, Yale University, New Haven, CT 06520, USA; micheal.frunzi@gmail.com (M.F.); james.cross@yale.edu (J.C.); ms@gaus90.chem.yale.edu (M.S.)
4 College of Mechanical and Electrical Engineering, Central South University, South Lushan Road, Changsha 410083, China
5 Shenzhen Research Institute, Central South University, High-Tech Industrial Park, Yuehai Street, Shenzhen 518057, China
* Correspondence: shuai@csu.edu.cn (C.S.); liang_wenjie@163.com (W.L.); xhisaac@csu.edu.cn (H.X.)
† These authors contributed equally to this work.

Abstract: The study of isolated atoms or molecules inside a fullerene cavity provides a unique environment. It is likely to control the outer carbon cage and study the isolated species when molecules or atoms are trapped inside a fullerene. We report the Diels–Alder addition reaction of 9,10-dimethyl anthracene (DMA) to H$_2$@C$_{60}$ while $^1$H NMR spectroscopy is utilized to characterize the Diels–Alder reaction of the DMA with the fullerene. Through $^1$H NMR spectroscopy, a series of isomeric adducts are identified. The obtained peaks are sharp, precise, and straightforward. Moreover, in this paper, H$_2$@C$_{60}$ and its isomers are described for the first time.

Keywords: $^1$H NMR spectroscopy; Diels–Alder reaction; 9,10-dimethylanthracene; fullerene; H$_2$@C$_{60}$

1. Introduction

A fullerene molecule is an allotrope of carbon. Investigating this newly discovered class of form has become a particularly striking and dynamic research area [1,2]. In the 1990s, the formation of an orifice on fullerene C$_{60}$ attracted immense attention for targeting endohedral fullerenes in organic syntheses, such as molecular containers [3–8], and investigating their ability as electron acceptors in solar cells. Inside the cavity, endofullerene contains small atoms or molecules, including helium, hydrogen, and water, as well as endohedral metal-fullerenes, such as Li, Th, and Sc$_3$N [9–14]. Inserting small molecules or atoms into a big closed fullerene cage is an intriguing yet demanding research area for scientists. Moreover, the encased molecule performs like a confined quantum rotor, with a sophisticated energy level structure [15] that could be investigated via neutron scattering, infrared (IR), as well as nuclear magnetic resonance (NMR) spectroscopy [15–21]. The steadiness and homogeneity of endofullerenes like H$_2$@C$_{60}$, HF@C$_{60}$, and H$_2$O@C$_{60}$ make it possible to examine crucial physical phenomena like nuclear spin isomer transformation with ease and precision [18,22–25]. Fullerene’s exterior chemical functionalities are heavily influenced by their bond reactivity.

The Diels–Alder addition reaction is a valuable research area in fullerene chemistry. To functionalize fullerenes, the Diels–Alder reaction is used [26]. When small molecules or atoms are encapsulated in the fullerene, they not only enhance the stability but also increase the Diels–Alder cycloaddition reactivity of the fullerene [27–29]. On the one hand,
it has been demonstrated that the Diels–Alder reaction of 9,10-dimethylanthracene with 
C_{60} is reversible at ambient temperature. This phenomenon also happens with C_{70} \cite{30}. On 
the other hand, a reduction in the exothermicity of the reaction may cause a reversible 
reaction because two methyl groups can increase steric hindrance. Hirsch has employed 
the reaction to manipulate the position of several malonate additions by adding removable 
templates to C_{60} (see Figure 1) \cite{30–32}. In an early publication, we successfully employed 
heavier spectroscopy to explain the reactions of C_{60} and C_{70} with DMA and studied the 
equilibria of the reaction \cite{33}. When helium is inserted inside an endohedral fullerene 
cage, and its NMR chemical shift is matched with the chemical shift of $^3$He outside, the 
magnetic field shielded by the fullerene can be measured directly \cite{27,34–41}. This is caused 
by diamagnetism and is linked to the ring currents in the molecular orbitals of fullerene. 
Higher fullerenes, He@C_n, have previously been demonstrated to have helium NMR 
chemical shifts that fall between two extremes, namely low-field C_{60} and high-field C_{70}, 
indicating that they have an “intermediate” aromatic nature \cite{37,39}. The $^3$He NMR is vital 
for fullerene chemistry \cite{42,43}. Still, there are some limitations to helium NMR, i.e., the 
measurement at low temperature demands high sensitivity, low noise, and high pressure. 
Even if the NMR signal itself is visible, changes in the signals are negligible at the lowest 
temperature. Besides that, $^3$He can be studied in a specially designed and constructed 
cryostat. Helium NMR spectra use potassium cyanide, or KCN, which is highly toxic, as 
well as special $^3$He isotopes, which are very costly. While $^1$H NMR is inexpensive, simple, 
and easy to operate, the spectra for each adduct give a simple and sharp peak.

In the continuation of our previous work \cite{44}, we used the T-Jump Method to the 
Diels–Alder addition of 9,10-dimethylanthracene to C_{60}. It was essential to ensure that 
the equilibrium data of $^3$He@C_{60} was applied to H_{2}@C_{60}. Herein, we extended H_{2}@C_{60} 
to investigate the Diels–Alder addition reaction of 9,10-dimethylanthracene and fullerene. 
Through $^1$H NMR characterization and analysis, we found 1 mono-, 6 bis-, 11 tris-, and 10 
tetrakis-adducts.

**Figure 1.** Gauss view of mono-adduct of DMA and C_{60}.

2. Experimental Section

**Preparation of Fullerene** H$_2$@C$_{60}$ was prepared by following the previously described method [45,46]. NMR tubes were used to prepare all of the $^1$H NMR samples. A total of 3.6 mg of H$_2$@C$_{60}$ was kept in the nuclear magnetic tube. Subsequently, 1 mL of mixed solvent CS$_2$: CDCl$_3$ = 4:1 was added to dissolve H$_2$@C$_{60}$ completely, and then a $^1$H NMR test was performed to find the corresponding spectrum. Firstly, 0.51 mg of DMA (0.5 equiv) was placed in the NMR tube. The reaction mixture (3.6 mg of C$_{60}$ and 1.03 mg of DMA (1 equiv)) were mixed in 1 mL of CS$_2$: CDCl$_3$. $^1$H NMR was used to characterize the reaction of C$_{60}$ and DMA. It was found that almost no free DMA could be found by $^1$H NMR (~30 min after the mixing) was allowed to stand overnight, and then the corresponding $^1$H NMR test was conducted to reach equilibrium. After that, a weighted amount of dimethyl anthracene was added to the mixture to obtain another sample. To reach a saturated solution, this procedure could be repeated. Increase the mass of DMA in increments of 1.03 mg (1 equiv), 1.54 mg (1.5 equiv), 2.04 mg (2 equiv), 2.57 mg (2.5 equiv), 4.12 mg (4 equiv), 6.19 mg (6 equiv), 10.31 mg (10 equiv), 15.41 mg (15 equiv), and 20.63 mg (20 equiv) until the saturation solution is reached.

**Proton NMR Spectroscopy** A 500 MHz Bruker Avance spectrometer obtained $^1$H NMR spectra. A solvent-gating pulse sequence was adopted to remove a substantial signal from the ring protons on the non-deuterated solvent molecules. Bulky solvent signals diminish the instrument’s automatic gain setting, decreasing sensitivity for smaller ones. A total of 256 scans were acquired for the competitive reaction with a 3-second acquisition time, a 2-second recycling delay, and a 5 Hz line broadening.

3. Results and Discussion

When the DMA concentration is increased at room temperature, the Diels–Alder addition of DMA to C$_{60}$ becomes reversible and yields mono-, bis-, tris-, and tetrakis-adducts, respectively. Greater levels of the higher adducts accumulate as more DMA is taken. A series of mixtures of DMA and H$_2$@C$_{60}$ were prepared in 4:1 CS$_2$: CDCl$_3$. After the establishment of equilibrium, the $^1$H NMR spectra were recorded. When C$_{60}$ reacts with DMA, a new peak in the DMA product peak appears at $\delta = 8.3$, 7.4 ppm, and near $\delta = 2.3$–2.6 ppm in the $^1$H NMR spectrum, although the spectral peaks are complicated and the integral area is relatively small. This is mainly because the addition product of C$_{60}$ and DMA lowers C$_{60}$’s symmetry, and the addition product is an isomer with the same symmetrical features as C$_{60}$, and its distinctive peaks cannot be created in $^1$H NMR. As a result, corresponding to the new spectral peaks one by one using $^1$H NMR is difficult, as illustrated in Figure 2.

In addition, while using H$_2$@C$_{60}$ with DMA, the addition product’s $^1$H NMR peak appeared in the high field at $\delta = -1.39$ ppm, which is easier to examine since the corresponding spectral peak is far away from the spectral peak of other functional groups. Adducts with more DMA molecules correspond to the faster-increasing peak if this ratio varies with DMA concentration. Due to the high symmetry of C$_{60}$, there is only one mono-adduct between C$_{60}$ and DMA. When 0.5 equiv DMA reacts with C$_{60}$, its presence can be found by analyzing the $^1$H NMR spectra (as shown in Figure S1 Supplementary Materials. Since C$_{60}$ is excessive at this time, the Diels–Alder addition reaction between DMA and C$_{60}$ is dominated by mono-adducts, and mono-adducts account for the majority. Therefore, we speculate that the peak at $\delta = -4.979$ ppm corresponds to the peak of the mono-adduct. The Diels–Alder addition reaction with C$_{60}$ cannot generate the tris- and tetrakis-adducts due to the small amount of DMA, or the concentration of the tris- and tetrakis-adducts is too low to detect. Therefore, we speculate that the peaks at $\delta = -4.591$ ppm and $\delta = -5.896$ ppm are due to a small number of bis-adducts. When the amount of DMA was increased to 1 equiv and 1.5 equiv (as shown in Figures S2 and S3 Supplementary Materials), the analysis of the $^1$H NMR spectra showed that at this time, the proportion of H$_2$@C$_{60}$ was relatively low, that is, the unreacted H$_2$@C$_{60}$ continued to react with the newly added DMA, and the intensity of the spectral peak at $\delta = -4.979$ ppm was relatively increased, that is, the
proportion of the mono-addition products gradually increased. Meanwhile, 4 new spectral peaks appeared at \( \delta = -5.941, -6.779, -8.276, -8.329 \) ppm, respectively, which we assumed were bis-adduct peaks because the amount of DMA at this time was only 1 equiv or 1.5 equiv, and it was difficult to generate tris- and tetrakis-adducts in the Diels–Alder addition reaction with \( \text{C}_{60} \), or the concentration of tris- and tetrakis-adducts was too low to be detected. When the amount of DMA was increased to 2 equiv, the analysis of the \(^1\text{H}\) NMR spectra showed (as shown in Figure S4 Supplementary Materials) that the amount of unreacted \( \text{H}_2@\text{C}_{60} \) continued to decrease and the amount of unreacted and bis-adduct continued to increase. In the meantime, a new spectral peak appeared at \( \delta = -11.733 \) ppm. The concentration of the tris-adduct should be detected, and we presumed that the new spectral peak is the tris-adduct based on the chemical shift of the bis-adduct and its change trend and that the tris- and tetrakis-adducts are analyzed by this method. A comparative analysis of the spectra of 15 equiv DMA and 20 equiv DMA showed that no new spectral peak appeared except for the increase in the proportion of the tetrakis-adducts (as shown in Figures S5 and S6 Supplementary Materials) and the relative decrease in the tris-adduct. Therefore, we speculated that the Diels–Alder addition reaction between DMA and \( \text{H}_2@\text{C}_{60} \) took place without the pentakis- or hextakis-adducts. Or the concentration of the resulting pentakis- or hextakis-adducts may be too low to detect.

![Figure 2](image)

**Figure 2.** \(^1\text{H}\) NMR spectra of (a) DMA, (b) 1.0 equivalent DMA + \( \text{C}_{60} \).

As a result, we can estimate the number of DMA addition products based on the \(^1\text{H}\) NMR spectrum peak because the peak intensity ratio of the two peaks is not dependent on DMA concentration. Then they will resemble an equal number of DMA molecules [33], and \( \text{H}_2@\text{C}_{60} \) will correspond to the adduct utilizing a similar quantity. But when the ratio varies with DMA concentration, faster-rising peaks could be linked to an adduct containing extra DMA molecules. The use simplifies the study of the Diels–Alder addition reaction between \( \text{C}_{60} \) and DMA. The 29 new \(^1\text{H}\) NMR peaks are evaluated one by one, the fraction of the NMR intensity for each isomer at 298 K, as shown in Figure 3a,c, (a partial enlargement of Figure 3c is shown in Figure S7 Supplementary Materials) and the chemical shifts, as well as the \(^1\text{H}\) NMR peaks, are described accordingly.
Figure 3. (a) $^1$H NMR spectra of $H_2@C_{60}$ with 2.5 equiv of DMA, (b) $^3$He NMR spectra of $^3$He@C$_{60}$ with 2.5 equiv DMA; (c) $^1$H NMR spectra of $H_2@C_{60}$ with 10 equiv of DMA; (d) $^3$He NMR spectra of $^3$He@C$_{60}$ with 10 equiv DMA at room temperature. The numbers 1, 2, 3, 4 stand for the isomers of mono-, bis-, tris-, and tetrakis-adducts, respectively. Chemical shift in ppm relative to TMS (for (a,c)) and dissolved $^3$He gas (for (b,d) ([J. Am. Chem. Soc. 2001, 123, 256–259]).

As shown in Table 1, we found 1 mono-, 6 bis-, 11 tris-, 10 tetrakis-adducts, and an unreacted embedded hydrogen fullerene from the Diels–Alder addition reaction between DMA and C$_{60}$. There were no spectral lines shown with an increasing concentration of DMA. As a result, we did not find any indication of pentakis- and hexakis-adducts in the
DMA-C$_{60}$ Diels–Alder addition reaction. Such a conclusion is used by Wang Guanwu et al. at 295.4 K [33] for $^3$He@C$_{60}$, and the obtained peak patterns are very similar, except for the overall shift of the NMR spectrum (as shown in Figure 3b,d). Furthermore, with the increase in DMA concentration, the mono-adduct gradually decreases, and correspondingly, the multi-addition products gradually increase.

Table 1. Chemical shifts of addition products of C$_{60}$ and DMA.

|          | $\delta$ (ppm) | $f$ | $\delta$ (ppm) | $f$ |
|----------|----------------|-----|----------------|-----|
| Mono     |                |     |                |     |
| 1        | -4.954         | 1.000 | -6.667         | 0.008 |
| Bis      | -4.591         | 0.012 | -8.092         | 0.009 |
| 2        | -5.896         | 0.073 | -9.397         | 0.031 |
| 3        | -5.941         | 0.008 | -10.041        | 0.047 |
| 4        | -6.779         | 0.092 | -9.351         | 0.003 |
| 5        | -8.276         | 0.435 | -10.321        | 0.282 |
| 6        | -8.329         | 0.380 | -10.482        | 0.042 |
| Tris     |                | 10   | -11.145        | 0.166 |
| 1        | -6.073         | 0.005 |
| 2        | -7.076         | 0.008 |
| 3        | -7.120         | 0.024 |
| 4        | -7.198         | 0.042 |
| 5        | -8.618         | 0.053 |
| 6        | -9.142         | 0.009 |
| 7        | -9.182         | 0.162 |
| 8        | -9.249         | 0.018 |
| 9        | -9.881         | 0.217 |
| 10       | -11.142        | 0.054 |
| 11       | -11.733        | 0.408 |

$^a$ Chemical shift in ppm relative to TMS; $^b$ Fraction in each isomer of the total NMR signal for all isomers with a given number of DMA addends.

The supposed reversible reactions of $^3$H@C$_{60}$ and DMA have been described in the following Equations (1)–(4):

$$
H_2@C_{60} + DMA \rightleftharpoons H_2@C_{60}(DMA)
$$

Equation (1)

$$
H_2@C_{60}(DMA) + DMA \rightleftharpoons H_2@C_{60}(DMA)_{2}
$$

Equation (2)

$$
H_2@C_{60}(DMA)_{2} + DMA \rightleftharpoons H_2@C_{60}(DMA)_{3}
$$

Equation (3)

$$
H_2@C_{60}(DMA)_{3} + DMA \rightleftharpoons H_2@C_{60}(DMA)_{4}
$$

Equation (4)

The calculations of mono-, bis-, tris-, and tetrakis-adducts are measured in these equations. Though the $^3$H spectrum can be used to determine the sums of C$_{60}$ and the mono-, bis-, tris-, and tetrakis-adducts, it cannot determine the quantity of free DMA. As a result, a computer program was written that simulates the experimental results using the concentration of free DMA. A number of values for concentrations of free C$_{60}$ and DMA were obtained for any presumed values of $K_1$, $K_2$, $K_3$, and $K_4$. The preceding formula was applied to calculate the total concentrations of the various types of adducts based on these values. When these quantities are added together, the overall concentration of C$_{60}$ is calculated. Similarly, the total volume of DMA was calculated by summing up the number of DMA molecules in each adduct. The experimental results were compared with estimated values. To meet the experimental facts, $K_1$, $K_2$, $K_3$, and $K_4$ were modified. The theoretical concentration curves presented in Figure 4 were created using values of 3,608,505.76, 38.89,
and 2.42 M\(^{-1}\), which best fit the experimental results. As shown, all of the experimental values for C\(_{60}\) and C\(_{60}\)(DMA)\(_n\) fractions at different DMA/C\(_{60}\) ratios are very close to the estimated curves. With the addition of DMA, the concentration of free C\(_{60}\) declines until it is close to 0 at 2.5 equiv of DMA, whereas the concentrations of mono-adducts, bis-adducts, and tris-adducts initially increase, reach a maximum value, and then decrease. The concentration of tris-adduct peaks reached the maximum at 6.3 equiv of DMA and then gradually fell. Tetrakis-adduct concentrations continue in an upward direction.

The initial concentrations of H\(_2\)@C\(_{60}\) and DMA are 5 mM and 4.74 mM, respectively. From the NMR peak strengths of H\(_2\)@C\(_{60}\) and DMA, we can infer the concentrations of each single addition product and multi-addition product. In contrast, the concentration of unreacted DMA can be calculated by subtracting the reacted part from the initial concentration of DMA. According to the spectrum analysis, when the DMA concentration is increased to 2 equiv, the mono-adduct concentration reaches its maximum, and essentially no bis-adduct is formed. As a result, the following formula can be used to derive the corresponding equilibrium constant K\(_1\):

\[
K_1 = \frac{[Mono]}{[DMA][H2@C60]}
\]

The concentrations of the three after the reaction can be calculated using the NMR peak intensities of H\(_2\)@C\(_{60}\) and DMA, which are [Mono] = 2.15 mM, [DMA] = 0.1453 mM, and [H\(_2\)@C\(_{60}\)] = 4.1 mM, respectively.

\[
K_1 = \frac{2.15}{0.1456 \times 4.1} = 3608 \text{ M}^{-1}
\]

When the concentration of DMA is increased to 4 equiv, the concentration of unreacted H\(_2\)@C\(_{60}\) tends to zero, the concentration of mono- and bis-adducts increases and gradually decreases after reaching the maximum value, and the corresponding equilibrium constant K\(_2\) is derived.

\[
K_2 = \frac{[Bis]}{[Mono][DMA]}
\]
In the meantime, there are six bis-adducts, so $[\text{Bis}]_{\text{total}} = [\text{Bis}]_1 + [\text{Bis}]_2 + [\text{Bis}]_3 + [\text{Bis}]_4 + [\text{Bis}]_5 + [\text{Bis}]_6$, since the amounts of $[\text{Bis}]_1$ and $[\text{Bis}]_3$ are very small, so neglected. By analysing the nuclear magnetic peak strength in the spectra, it is obtained that $[\text{DMA}] = 0.000145 \text{ mM}$, $[\text{Bis}]_2 = 0.0108 \text{ mM}$, $[\text{Bis}]_4 = 0.0140 \text{ mM}$, $[\text{Bis}]_5 = 0.728 \text{ mM}$, $[\text{Bis}]_6 = 0.0605 \text{ mM}$, so $[\text{Bis}]_{\text{total}} = 0.158 \text{ mM}$, from which the equilibrium constant $K_2$ is calculated.

$$K_2 = \frac{0.158}{2.15 \times 0.000145} = 505.76 \text{ M}^{-1}$$

And so, $K_3 = 38.89 \text{ M}^{-1}$ and $K_4 = 2.42 \text{ M}^{-1}$.

In 2009 [44], we found very similar results by analyzing the reaction rates and equilibrium constants of DMA and C$_{60}$ using H$_2$@C$_{60}$ and $^3$He@C$_{60}$. The chemical shifts of the spectral peaks for the mono-adduct of H$_2$@C$_{60}$ and $^3$He@C$_{60}$ are $\delta = -1.39 \text{ ppm}$, $\delta = -6.32 \text{ ppm}$, and $\delta = -4.95 \text{ ppm}$, $\delta = -9.86 \text{ ppm}$, respectively. Hence, the single mono-adduct shift differences are 3.56 ppm and 3.54 ppm, which are very close, indicating that the embedded H$_2$ and $^3$He have little effect on the C$_{60}$ shell reaction (as shown in Figure 5), while in $^{129}$Xe@C$_{60}$, the chemical shift between the mono-adduct and unreacted C$_{60}$ is $\delta = +10.9 \text{ ppm}$ [47]. In both scenarios, it is concluded that the endohedral molecule is bouncing around inside the C$_{60}$ cage without creating any substantial interference to the C$_{60}$’s electrons. The carbon cage of fullerene and the molecule inside have a weak van der Waals force, as well as a repulsive force when the molecule approaches the cage. The equilibrium constants of both endohedral fullerenes can then be safely assumed to be the same as those of empty C$_{60}$.

![Chemical Shift (ppm)](image)

**Figure 5.** (a) $^3$He NMR spectrum of $^3$He@C$_{60}$ and mono-adduct with DMA; (b) $^1$H NMR spectrum of H$_2$@C$_{60}$ and mono-adduct with DMA [44].

Nonetheless, the synthesis of H$_2$@C$_{60}$ is a complex process that takes eight steps to be complete [37,39,48]. H$_2$@C$_{60}$ is still preferred to $^3$He@C$_{60}$ for different reasons. (1) Because the matching peaks are far away from the peaks of other functional groups, $^1$H is an excellent NMR probe to analyze H$_2$@C$_{60}$ precisely. (2) We can make H$_2$@C$_{60}$ with a 100% incorporation ratio, whereas $^3$He@C$_{60}$ has approximately 1%. Since H$_2$@C$_{60}$ has two hydrogen atoms versus one helium atom in $^3$He@C$_{60}$, hence giving us a sensitivity
boost of more than two orders of magnitude. (3) In proton NMR, there is no issue of noise as compared to helium NMR, as shown in Figure 5. As the endohedral hydrogen resonances occur far up-field from the solvent, the peak separation is easy and well separated from the other remaining spectrum. Furthermore, the force between H$_2$ and C$_{60}$ in endohedral fullerenes is a van der Waals force. As a result, the H$_2$ atom has little effect on the basic chemical reactivities of C$_{60}$.

4. Conclusions

In summary, we have employed $^1$H NMR spectroscopy to explain the reaction between fullerene C$_{60}$ and DMA. Through obtaining several $^1$H NMR spectra of the reaction mixture of H$_2$@C$_{60}$ and DMA, we were able to identify a series of DMA molecules that reacted to the fullerene and the isomers that existed in the reaction mixture for each peak in the $^1$H NMR spectroscopy. We have successfully obtained 1 mono-adduct, 6 bis-adducts, 11 tris-adducts, and 10 tetrakis-adducts from C$_{60}$ and DMA. The findings suggest that changing the skeleton of fullerene can substantially impact the cage’s reactivity and that H$_2$@C$_{60}$ will be helpful in a number of complex fullerene reactions, such as the conversion of electrophile to nucleophile [49], and is expected to have numerous applications in materials science and technology [50], as well as H$_2$@C$_{60}$, paves the way to the pyrrolidinoendofullerene [51–53]. Further work is underway to investigate H$_2$@C$_{60}$ inside the fullerene cage and explore its chemical and physical properties.

Supplementary Materials: The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/nano12101667/s1, Figure S1: $^1$H NMR spectra of H$_2$@C$_{60}$ with 0.5 eq DMA; Figure S2: $^1$H NMR spectra of H$_2$@C$_{60}$ with 1 eq DMA; Figure S3: $^1$H NMR spectra of H$_2$@C$_{60}$ with 1.5 eq DMA; Figure S4: $^1$H NMR spectra of H$_2$@C$_{60}$ with 2 eq DMA; Figure S5: $^1$H NMR spectra of H$_2$@C$_{60}$ with 15 eq DMA; Figure S6: $^1$H NMR spectra of H$_2$@C$_{60}$ with 20 eq DMA; Figure S7: $^1$H NMR spectra of H$_2$@C$_{60}$ with 10 eq DMA.

Author Contributions: Data curation, Y.S.; Funding acquisition, W.L. and C.S.; Investigation, W.L.; Methodology, J.Z. and W.L.; Project administration, C.S. and H.X.; Supervision, J.C., M.S. (Martin Saunders) and H.X.; Validation, M.F., J.C. and C.S.; Visualization, M.S. (Martin Saunders); Writing—original draft, M.S. (Mahboob Subhani); Writing—review & editing, H.Z. and J.C. All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by the National Natural Science Foundation of China (No. 21975288), Hunan Reaserch Founding (No. 2020JJ4683), Changsha Research Founding No. 2014121, and Shenzhen Research Founding (No. JCYJ20190806144616528).

Acknowledgments: We are grateful to Jean-Pierre Sauvage (winner of the 2016 Nobel Prize in Chemistry) for sharing his expert insight and careful guidance during the research.

Conflicts of Interest: The authors declare no conflict of interest.

References
1. Kroto, H. C$_{60}$: Buckminsterfullerene. Nature 1985, 318, 162–163. [CrossRef]
2. Krätschmer, W.; Lamb, L.D.; Fostiropoulos, K.; Huffman, D.R. Solid C$_{60}$: A new form of carbon. Nature 1990, 347, 354–358. [CrossRef]
3. Murata, M.; Murata, Y.; Komatsu, K. Surgery of fullerenes. Chem. Commun. 2008, 6083–6094. [CrossRef]
4. Vougioukalakis, G.C.; Roubelakis, M.M.; Orfanopoulos, M. Open-cage fullerenes: Towards the construction of nanosized molecular containers. Chem. Soc. Rev. 2010, 39, 817–844. [CrossRef]
5. Shi, L.; Gan, L. Open-cage fullerenes as tailor-made container for a single water molecule. J. Phys. Org. Chem. 2013, 26, 766–772. [CrossRef]
6. Chen, C.P.; Lin, Y.W.; Horng, J.C.; Chuang, S.C. Open-Cage Fullerenes as n-Type Materials in Organic Photovoltaics: Relevance of Frontier Energy Levels, Carrier Mobility and Morphology of Different Sizable Open-Cage Fullerenes with Power Conversion Efficiency in Devices. Adv. Energy Mater. 2011, 1, 776–780. [CrossRef]
7. Murata, M.; Morinaka, Y.; Murata, Y.; Yoshikawa, O.; Sagawa, T.; Yoshikawa, S. Modification of the π-framework of [60] fullerene for bulk-heterojunction solar cells. Chem. Commun. 2011, 47, 7335–7337. [CrossRef]
8. Castro, E.; Artigas, A.; Pla-Quintana, A.; Roglans, A.; Liu, F.; Perez, F.; Lledó, A.; Zhu, X.-Y.; Echegoyen, L. Enhanced open-circuit voltage in perovskite solar cells with open-cage [60] fullerenes as electron-transporting materials. *Materials* 2019, 12, 1314. [CrossRef]

9. Komatsu, K.; Murata, M.; Murata, Y. Encapsulation of Molecular Hydrogen in Fullene C_{60} by Organic Synthesis. *Science* 2005, 307, 238–240. [CrossRef]

10. Kurutobi, K.; Murata, Y. A Single Molecule of Water Encapsulated in Fullerene C_{60}. *Science* 2011, 333, 613–616. [CrossRef]

11. Aoyagi, S.; Nishibori, E.; Sawa, H.; Sugimoto, K.; Takata, M.; Miyata, Y.; Kitaura, R.; Shinhara, H.; Okada, H.; Sakai, T. A layered ionic crystal of polar Li@C_{60} superatoms. *Nat. Chem.* 2010, 2, 678–683. [CrossRef]

12. Nakawa, H.; Araki, Y.; Slanina, Z.; Tsuchiya, T.; Akasaka, T.; Wada, T.; Ito, O.; Dinse, K.-P.; Ata, M.; Kato, T. The effect of atomic nitrogen on the C_{60} cage. *Chem. Commun.* 2010, 46, 631–633. [CrossRef]

13. Liu, G.; Gimenez-Lopez, M.d.C.; Jovic, M.; Khlobystov, A.N.; Briggs, G.A.D.; Poryfyrikas, K. Alignment of N=C@60 Derivatives in a Liquid Crystal Matrix. *J. Phys. Chem. B* 2013, 117, 5925–5931. [CrossRef]

14. Krachmalnicoff, A.; Bounds, R.; Mamone, S.; Alom, S.; Concistrò, M.; Meier, B.; Kouřil, K.; Light, M.E.; Johnson, M.R.; Rols, S. The dipolar endofullereene hf@C_{60}. *Nat. Chem.* 2016, 8, 953–957. [CrossRef]

15. Levitt, M.H. Spectroscopy of light-molecule endofullerenes. *Philos. Trans. R. Soc. A Math. Phys. Eng. Sci.* 2013, 371, 20120429. [CrossRef]

16. Horsewill, A.; Goh, K.; Rols, S.; Ollivier, J.; Johnson, M.; Levitt, M.; Carravetta, M.; Mamone, S.; Murata, Y.; Chen, J.-C. Potential energy and dipole moment surfaces for HF@C_{60}: Prediction of spectral and electric response properties. *Philos. Trans. R. Soc. A Math. Phys. Eng. Sci.* 2013, 371, 20110627. [CrossRef]

17. Horsewill, A.; Panesar, K.; Rols, S.; Johnson, M.; Murata, Y.; Komatsu, K.; Mamone, S.; Danquigny, A.; Cuda, F.; Maltsev, S. Quantum translator-rotator: Inelastic neutron scattering of dihydrogen molecules trapped inside anisotropic fullerene cages. *Phys. Rev. Lett.* 2009, 102, 013001. [CrossRef]

18. Beduz, C.; Carravetta, M.; Chen, J.Y.-C.; Concistrò, M.; Denning, M.; Frunzi, M.; Horsewill, A.J.; Johannessen, O.G.; Lawler, R.; Lei, X. Quantum rotation of ortho and para-water encapsulated in a fullerene cage. *Proc. Natl. Acad. Sci. USA* 2012, 109, 12894–12898. [CrossRef]

19. Mamone, S.; Ge, M.; Hiuveno, D.; Nagel, U.; Danquigny, A.; Cuda, F.; Grossel, M.; Murata, Y.; Komatsu, K.; Levitt, M. Rotor in a cage: Infrared spectroscopy of an endohedral hydrogen-fullerene complex. *J. Chem. Phys.* 2009, 130, 081103. [CrossRef]

20. Ge, M.; Nagel, U.; Hiuveno, D.; Rööm, T.; Mamone, S.; Levitt, M.; Carravetta, M.; Murata, Y.; Komatsu, K.; Lei, X. Infrared spectroscopy of endohedral HD and D_{2} in C_{60}. *J. Chem. Phys.* 2011, 135, 114531. [CrossRef]

21. Rööm, T.; Peedu, L.; Ge, M.; Hiuveno, D.; Nagel, U.; Ye, S.; Xu, M.; Bačić, Z.; Mamone, S.; Levitt, M. Infrared spectroscopy of small-molecule endofullerenes. *Philos. Trans. R. Soc. A Math. Phys. Eng. Sci.* 2013, 371, 20110631. [CrossRef]

22. Vidal, S.; Izquierdo, M.; Alom, S.; García-Borràs, M.; Filipponi, S.; Osuna, S.; Solá, M.; Whitby, R.J.; Martin, N. Effect of incarcerated HF on the exohedral chemical reactivity of HF@C_{60}. *Chem. Commun.* 2017, 53, 10993–10996. [CrossRef]

23. Mamone, S.; Concistrò, M.; Carignani, E.; Meier, B.; Krachmalnicoff, A.; Johannessen, O.G.; Lei, X.; Denning, M.; Carravetta, M. Nuclear spin conversion of water inside fullerene cages detected by low-temperature nuclear magnetic resonance. *J. Chem. Phys.* 2014, 140, 194306. [CrossRef]

24. Frunzi, M.; Jockusch, S.; Chen, J.Y.-C.; Calderon, R.M.K.; Lei, X.; Murata, Y.; Komatsu, K.; Guldí, D.M.; Lawler, R.G.; Turro, N.J. A Photochemical On–Off Switch for Tuning the Equilibrium Mixture of H_{2} Nuclear Spin Isomers as a Function of Temperature. *J. Am. Chem. Soc.* 2011, 133, 14232–14235. [CrossRef]

25. Li, Y.; Lei, X.; Jockusch, S.; Chen, J.Y.-C.; Frunzi, M.; Johnson, J.A.; Lawler, R.G.; Murata, Y.; Murata, K.; Komatsu, K. A magnetic switch for spin-catalyzed interconversion of nuclear spin isomers. *J. Am. Chem. Soc.* 2010, 132, 4042–4043. [CrossRef]

26. Sato, S.; Maeda, Y.; Guo, J.-D.; Yamada, M.; Mizorogi, N.; Nagase, S.; Akasaka, T. Mechanistic Study of the Diels–Alder Reaction of Paramagnetic Endohedral Metallofullerene: Reaction of La@C_{82} with 1,2,3,4,5-Pentamethycyclopentadiene. *J. Am. Chem. Soc.* 2013, 135, 5582–5587. [CrossRef]

27. Cioslowski, J.; Fleischmann, E.D. Endohedral complexes: Atoms inside the C_{60} cage. *J. Chem. Phys.* 1991, 94, 3730–3734. [CrossRef]

28. García-Borràs, M.; Osuna, S.; Luis, J.M.; Swart, M.; Solà, M. A Complete Guide on the Influence of Metal Clusters in the Diels–Alder Regioselectivity of I_{h}-C_{60} Endohedral Metallofullerenes. *Chem.—A Eur. J.* 2013, 19, 14931–14940. [CrossRef]

29. Zhao, P.; Zhao, X.; Ehará, M. Regioselectivity of Sc_{2}C_{2}C_{38}(8)-C_{82}: Role of the Sumanene-Type Hexagon in Diels–Alder Reaction. *J. Org. Chem.* 2016, 81, 8169–8174. [CrossRef]

30. Lamparth, I.; Maichle–Mössmer, C.; Hirsch, A. Reversible Template-Directed Activation of Equatorial Double Bonds of the Fullerene Framework: Regioselective Direct Synthesis, Crystal Structure, and Aromatic Properties of T_{h}-C_{60}(COOEt)_{12}. *Angew. Chem. Int. Ed. Engl.* 1995, 34, 1607–1609. [CrossRef]

31. Hirsch, A.; Vostrowsky, O. C_{60} Hexakisadducts with an Octahedral Addition Pattern – A New Structure Motif in Organic Chemistry. *Eur. J. Org. Chem.* 2001, 2001, 829–848. [CrossRef]

32. Lamparth, I.; Herzog, A.; Hirsch, A. Synthesis of [60] fullerenes derivatives with an octahedral addition pattern. *Tetrahedron* 1996, 52, 5065–5075. [CrossRef]

33. Wang, G.-W.; Saunders, M.; Cross, R.J. Reversible Diels–Alder Addition to Fullerenes: A Study of Equilibria Using {³}He NMR Spectroscopy. *J. Am. Chem. Soc.* 2001, 123, 256–259. [CrossRef] [PubMed]
34. Buehl, M.; Thiel, W.; Jiao, H.; Schleyer, P.v.R.; Saunders, M.; Anet, F.A. Helium and lithium NMR chemical shifts of endohedral fullerene compounds: An ab initio study. J. Am. Chem. Soc. 1994, 116, 6005-6006. [CrossRef]

35. Elser, V.; Haddon, R. Icosahedral C60: An aromatic molecule with a vanishingly small ring current magnetic susceptibility. Nature 1987, 325, 792-794. [CrossRef]

36. Pasquarello, A.; Schlüter, M.; Haddon, R. Ring Currents in Icosahedral C60. J. Am. Chem. Soc. 1994, 116, 10831-10832. [CrossRef]

37. Saunders, M.; Jimenez-Vázquez, H.A.; Cross, R.J.; Mroczkowski, S.; Freedberg, D.I.; Anet, F.A. Probing the interior of fullerenes by 3He NMR spectroscopy of endohedral 3He@C60 and 3He@C70. Nature 1994, 367, 256-258. [CrossRef]

38. Smith, A.B., III; Strongin, R.M.; Brard, L.; Romanow, W.J.; Saunders, M.; Jimenez-Vázquez, H.A.; Cross, R.J. Synthesis and 3He NMR studies of C60 and C70 epoxide, cyclopropane, and annulene derivatives containing endohedral helium. J. Am. Chem. Soc. 1994, 116, 10831-10832. [CrossRef]

39. Saunders, M.; Cross, R.J.; Jimenez-Vázquez, H.A.; Shimshi, R.; Khong, A. Noble gas atoms inside fullerenes. Science 1996, 271, 1693-1697. [CrossRef]

40. Saunders, M.; Jimenez-Vazquez, H.A.; Bangerter, B.W.; Cross, R.J.; Mroczkowski, S.; Freedberg, D.I.; Anet, F.A. 3He NMR: A powerful new tool for following fullerene chemistry. J. Am. Chem. Soc. 1994, 116, 3621-3622. [CrossRef]

41. Saunders, M.; Jimenez-Vazquez, H.A.; Cross, R.J.; Billups, W.; Gesenberg, C.; Gonzalez, A.; Luo, W.; Haddon, R.; Diederich, F.; Herrmann, A. Analysis of isomers of the higher fullerenes by 3He NMR spectroscopy. J. Am. Chem. Soc. 1995, 117, 9305-9308. [CrossRef]

42. Zhao, S.; Zhao, P.; Cai, W.; Bao, L.; Chen, M.; Xie, Y.; Zhao, X.; Lu, X. Stabilization of Giant Fullerenes C2(41)-C80, D3(85)-C92, C1(132)-C94, C2(157)-C96, and C1(175)-C98 by Encapsulation of a Large La2C2 Cluster: The Importance of Cluster–Cage Matching. J. Am. Chem. Soc. 2017, 139, 4724-4728. [CrossRef] [PubMed]

43. Wei, T.; Wang, S.; Lu, X.; Tan, Y.; Huang, J.; Liu, F.; Li, Q.; Xie, S.; Yang, S. Entrapping a Group–VB Transition Metal, Vanadium, within an Endohedral Metallofullerene: V1Sc4-N@h5-C80 (x = 1, 2). J. Am. Chem. Soc. 2016, 138, 207-214. [CrossRef]

44. Frunzi, M.; Xu, H.; Cross, R.J.; Saunders, M. NMR Temperature-Jump Method for Measuring Reaction Rates: Reaction of Dimethylanthracene with H2@C60. J. Phys. Chem. A 2009, 113, 4996-4999. [CrossRef] [PubMed]

45. Komatsu, K. Classic Carbon Nanostructures. Philos. Trans. R. Soc. A Math. Phys. Eng. Sci. 2013, 371, 20110636. [CrossRef]

46. Krachmalnicoff, A.; Levitt, M.H.; Whitby, R.J. An optimised scalable synthesis of H2O@C60 and a new synthesis of H2@C60. Chem. Commun. 2014, 50, 13037-13040. [CrossRef]

47. Cross, R.; Khong, A.; Saunders, M. Using Cyanide To Put Noble Gases inside C60. J. Org. Chem. 2003, 68, 8281-8283. [CrossRef]

48. Rubin, Y.; Jarroson, T.; Wang, G.W.; Bartberger, M.D.; Houk, K.; Schick, G.; Saunders, M.; Cross, R.J. Insertion of helium and molecular hydrogen through the orifice of an open fullerene. Angew. Chem. Int. Ed. 2001, 40, 1543-1546. [CrossRef]

49. Yao, J.; Xiao, Z.; Zhang, J.; Yang, X.; Gan, L.; Zhang, W.-X. Switched role of fullerene in the Diels–Alder reaction: Facile addition of dienophiles to the conjugated fullerene diene moiety. Chem. Commun. 2008. [CrossRef]

50. Kadish, K.M.; Ruoff, R.S. Fullerenes: Chemistry, Physics, and Technology. John Wiley & Sons: New York, NY, USA, 2000.

51. Filipponne, S.; Maroto, E.E.; Martin-Domenech, A.; Suarez, M.; Martin, N. An efficient approach to chiral fullerene derivatives by catalytic enantioselective 1,3-dipolar cycloadditions. Nat. Chem. 2009, 1, 578-582. [CrossRef]

52. Maroto, E.E.; de Cózar, A.; Filipponne, S.; Martin-Domenech, A.; Suarez, M.; Cossio, F.P.; Martin, N. Hierarchical Selectivity in Fullerenes: Site-, Regio-, Diastereo-, and Enantiocontrol of the 1,3-Dipolar Cycloaddition to C70. Angew. Chem. Int. Ed. 2011, 50, 6060-6064. [CrossRef] [PubMed]

53. Maroto, E.E.; Filipponne, S.; Martin-Domenech, A.; Suarez, M.; Martin, N. Switching the stereoselectivity: (Fuller) pyrrolidines “a la carte”. J. Am. Chem. Soc. 2012, 134, 12936-12938. [CrossRef] [PubMed]