Inhibited nonradiative decay at all exciton densities in monolayer semiconductors

Hyungjin Kim1,2,†, Sheik Zia Uddin1,2,†, Naoki Higashitamizu1,2, Eran Rabani2,3,4, Ali Javey1,2,†

Most optoelectronic devices operate at high photocarrier densities, where all semiconductors suffer from enhanced nonradiative recombination. Nonradiative processes proportionately reduce photoluminescence (PL) quantum yield (QY), a performance metric that directly dictates the maximum device efficiency. Although transition metal dichalcogenide (TMDC) monolayers exhibit near-unity PL QY at low exciton densities, nonradiative exciton-exciton annihilation (EEA) enhanced by van-Hove singularity (VHS) rapidly degrades their PL QY at high exciton densities and limits their utility in practical applications. Here, by applying small mechanical strain (less than 1%), we circumvented VHS resonance and markedly suppressed EEA in monolayer TMDCs, resulting in near-unity PL QY at all exciton densities despite the presence of a high native defect density. Our findings can enable light-emitting devices that retain high efficiency at all brightness levels.

In this work, we modulated these three factors simultaneously. Along with $V_g$ and pump power, we altered the electronic band structure by applying a uniaxial strain ($e$). With appropriate strain, all neutral excitons recombined radiatively even at high concentrations in monolayers of WS$_2$, WSe$_2$, and MoS$_2$, resulting in near-unity quantum yield (QY) at all measured $G$s. The density of states of electrons in a two-dimensional (2D) periodic crystal is topologically constrained to exhibit logarithmic van Hove singularities (VHs) arising from saddle points in the energy dispersion ($\gamma$). When the energy of a transition is near the VHS, weak interactions are often intensified by the enhanced density of states (DOS) ($\delta$). On the basis of the energy and momentum conservation, we found that as-exfoliated TMDC monolayers exhibited enhanced EEA because the final energy of this process coincided with inherent VHS. Strain drove the final energy away from the VHS resonance and substantially reduced EEA in both sulfur- and selenide-based TMDCs. We could uniformly suppress all nonradiative recombination in a centimeter-scale chemical vapor deposition (CVD)–grown WS$_2$ monolayer at all $G$s.

Monolayer field effect transistor devices were fabricated on plastic flexible substrate, enabling simultaneous modulation of carrier concentration and strain while performing quantitative photoluminescence (PL) QY measurements (device fabrication details are available in the supplementary materials). Figure 1A shows the schematic and optical micrograph of such a device using WS$_2$ monolayers. Mechanically exfoliated monolayers were transferred to a polyvinyl alcohol layer attached to polyethylene terephthalate (PET)–handling substrate, a combination selected for its superior strain transfer efficiency ($\gamma$). Exfoliated hexagonal boron nitride (70 to 100 nm in thickness) and graphene (2 to 5 nm in thickness) were transferred sequentially on the monolayer WS$_2$ to serve as a gate insulator and gate electrode, respectively. The WS$_2$ monolayer was electrically grounded and $V_g$ was applied to the top graphene. Bending the PET substrate with positive curvature applied tensile strain to the monolayer in the direction of bending (18). Applied strain was calculated from geometrical considerations. $G$ is the number of excitons created or the number of photons absorbed per unit area per unit time, which can be tuned by changing the laser intensity.

As-exfoliated monolayer WS$_2$ is known to be electron rich. Application of a negative $V_g$ ($-30$ V) electrostatically compensated for that unintentional electron doping and ensured that the recombination process was dominated by neutral excitons ($\gamma$). At this biasing condition, we compared PL spectra of an unstrained and strained WS$_2$ monolayer at a high $G$ of $6.5 \times 10^{19}$ cm$^{-2}$ s$^{-1}$ (Fig. 1B). We observed both a redshift of PL spectra and $\sim 15$ times enhancement in PL intensity with the application of $e = 0.4\%$ tensile strain at this high $G$. Note that $G$ is independent of strain because absorption at pump wavelength does not change with strain (fig. S1).

Calibrated PL measurements at room temperature were performed to quantitatively extract the QY as a function of $e$, $V_g$, and $G$ (Fig. 1C to F, and fig. S2), and Fig. 1C shows PL QY as a function of $V_g$ and $G$ when no strain is applied. At zero and positive gate voltages, the background electron concentration of monolayer WS$_2$ was large and led to the formation of negative trions that predominantly recombined nonradiatively, thus yielding a low PL QY. At negative $V_g$, the background electrons were removed, and recombination of neutral excitons dominated. At low $G$, neutral excitons recombined completely radiatively despite native defect density.

At high $G$, PL QY rolled off because of EEA. These same results were observed previously for other substrates such as poly(methyl methacrylate) and SiO$_2$, and are quantitatively the same as the results here ($\gamma$). With the application of 0.2% tensile strain, the PL QY drop-off at high exciton $G$ was notably reduced for negative $V_g$ (Fig. 1D). For a tensile strain of 0.4%, no PL QY drop-off at high $G$ was observed (Fig. 1E). Thus, all nonradiative recombination processes in as-exfoliated monolayer WS$_2$ were suppressed by applying tensile strain and $V_g$.

Suppression of EEA is further elucidated in Fig. 1F, where we show PL QY as a function of strain at $V_g = -30$ V and at a high $G$ of $6.5 \times 10^{19}$ cm$^{-2}$ s$^{-1}$. For no applied strain, PL QY was low at this $G$, but for a threshold strain of 0.3%, PL QY increased sharply and asymptotically approached unity. This PL QY enhancement by strain was also reversible and repeatable, because PL QY traces for increasing and decreasing strain fully overlapped (fig. S3). Such reversibility and repeatability indicate an

---

*Electrical Engineering and Computer Sciences, University of California, Berkeley, CA 94720, USA. 1Materials Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA. 2Department of Chemistry, University of California, Berkeley, CA 94720, USA. 3The Raymond and Beverly Sackler Center of Computational Molecular and Materials Science, Tel Aviv University, Tel Aviv 69978, Israel. 4Corresponding author. Email: ajavey@berkeley.edu

†These authors contributed equally to this work.
absence of slippage, so applied strain is equal to the actual strain transferred to the monolayer. High PL QY at all pump powers persisted even for a tensile strain of \( \varepsilon = 1.0\% \) (Fig. 1F and fig. S4). In addition to electrostatic counterdoping, high PL QY was achieved by applying tensile strain in monolayer WS\(_2\), chemically counterdoped by Nafion, a known hole dopant (fig. S5).

The PL QY for neutral excitons (\( V_G = -30 \) V) can be written as the ratio of radiative recombination rate to the total recombination rate as follows:

\[
QY = \frac{R_e}{R_e + R_{nr}}
\]

(1)

where \( R_e \) and \( R_{nr} \) are the exciton radiative and nonradiative recombination rates, respectively. Nonradiative recombination for neutral excitons is predominantly attained through the EEA process \((J)\). Therefore, \( R_{nr} = R_{EEA} \), where \( R_{EEA} \) is the nonradiative EEA rate. Even with the application of strain, the semiconductor remained strongly excitonic \((\delta)\), so strain did not change the PL QY versus \( G \) response at low \( G \) and \( R_e \) was independent of strain (Fig. 1D to F). However, because strain changed the QY at high pump powers, \( R_{EEA} \) must depend strongly on the strain. Using the experimentally measured PL QYs at a high \( G \) of \( 6.5 \times 10^{19} \) cm\(^{-2}\)s\(^{-1}\), we found that

\[
\frac{R_{EEA}(\varepsilon = 0.4\%)}{R_{EEA}(\varepsilon = 0.0\%)} \approx 7 \times 10^{-3}
\]

(2)

which would indicate a roughly two orders of magnitude decrease in EEA rate at the highest \( G \). Although the EEA rate was not rigorously zero, it was decreased by the application of strain such that \( R_e \approx R_{EEA} \) and the radiative relaxation dominated the total recombination.

The photophysics of these monolayer semiconductors as a function of \( V_G \) and \( G \) arises from the quasiparticle interaction and can be captured by a simple kinetic model described elsewhere \((J)\). The exciton-to-trion ratio can be tuned with \( V_G \), activating their respective recombination routes, whereas high densities of neutral excitons activate the EEA process. However, the mechanism by which strain suppresses EEA at high pump necessitated a closer look at the EEA process itself. EEA occurs when one exciton ionizes another exciton by nonradiatively transferring its energy (Fig. 2A) \((\delta)\). The initial state consists of two excitons, with center-of-mass momenta \( K_1 \) and \( K_2 \) and energies \( E_1 \) and \( E_2 \), respectively. The exciton energy and momentum are related by \((13)\) as follows:

\[
E_1 = E_G - E_h + \frac{\hbar^2|K_1|^2}{2M_X}
\]

(3)

\[
E_2 = E_G - E_h + \frac{\hbar^2|K_2|^2}{2M_X}
\]

(4)

In the above relations, \( E_G \) is the fundamental band gap, \( E_h \) is the exciton binding energy, and \( M_X \) is the exciton mass. The final state consists of a high-energy electron and hole, with crystal momenta \( K_e \) and \( K_h \) and energies \( E_e \) and \( E_h \), respectively.

Irrespective of the details of the interaction potential, two quantities are conserved in the EEA process: total momentum and energy \((13, 19, 20)\). The condition for conservation of crystal momentum yields \((13)\) is

\[
K_e + K_h = K_1 + K_2
\]

(5)

Because \( K_1 \) and \( K_2 \) are determined by the thermal motion of excitons, they are negligible compared with \( K_e \) and \( K_h \), implying that the electron and the hole momentum in the final state should be almost opposite to each other

\[
K_e = -K_h
\]

(6)

Therefore, momentum conservation dictates that the electron and hole from the ionized exciton have opposing crystal wavevectors (on top of each other in the energy dispersion, shown with the red dashed line in Fig. 2A). The condition for conservation of crystal momentum yields \((13)\) is

\[
E_e + E_h = E_1 + E_2
\]

(7)

Because the exciton center of mass wavevector is negligible, \( E_i = E_2 = E_G - E_h = E_X \), where \( E_X \) is the exciton transition energy. Therefore, energy conservation stipulates that the energy difference between the electron and hole must be \( 2E_X \)

\[
E_e + E_h = 2E_X
\]

(8)

If we denote the conduction and valence band of the semiconductor as \( E_C \) and \( E_V \), then combined momentum and energy conservation can be written as

\[
E_e + E_h = E_C(K_e) - E_V(-K_h) = E_C(K_e) - E_V(K_e) = 2E_X
\]

(9)

Therefore, any wavevector for which the energy difference between the conduction and
valence band is equal to twice the exciton transition energy. The JDOS at that energy determines the rate of EEA. (C and D) Energy difference between the conduction and valence bands for unstrained and 0.4% strained monolayer WS₂, respectively. Gray hexagon denotes the first Brillouin zone (each side is 19.946 nm), and red areas are the possible final wavevectors. Possible final wavevectors in unstrained monolayer WS₂ include the saddle points ("Q") where there are VHSs but strained samples do not. (E) Calculated JDOS for monolayer WS₂: JDOS \( \rho_{CV}(E) \) at \( E = E_C - E_V = 2E_X \) determines EEA rate. Dashed lines denote values of \( 2E_X \) at the corresponding strain.

Typically, the effective mass approximation is invoked to determine the energy of the ionized electron. However, the ionized electron and hole have high energy, so this is no longer a valid approximation. We first calculated the band structure of monolayer TMDC with an 11-band tight-binding theory based on Wannier transformation of ab initio density functional theory calculations [details of the band structure are in (21) and (22)]. We then calculated the energy difference between the conduction and valence band \( (E_C - E_V) \) for unstrained and strained monolayer WS₂, respectively. The first Brillouin zone is indicated by a grey hexagon in Fig. 2C and D; red areas are the possible final states of the electron from the ionized exciton where the conservation laws are satisfied.

Possible final wavevectors in unstrained monolayer WS₂ include the saddle points (indicated by "Q" in Fig. 2C), but in 0.4% strained WS₂, they do not include the saddle points (Fig. 2D). Saddle points in the band structure of a 2D semiconductor create VHS and result in a logarithmically diverging JDOS (15, 23, 24). The JDOS for monolayer WS₂ \( \rho_{CV}(E) \) at \( E = E_C - E_V = 2E_X \) determines the strength of EEA. Figure 2E shows the JDOS of 0.4% strained and unstrained WS₂. In unstrained samples, there was a VHS at twice the exciton transition energy, resulting in an expedited EEA due to strain. Strain shifted the exciton transition energy \( E_X \) such that \( 2E_X \) did not overlap VHS resonance and reduced EEA.

We also show the JDOS of a 0.4% compressively strained WS₂ monolayer in Fig. 2E. We note that compressive strain also drove the EEA process off VHS resonance by changing the exciton transition energy, for both uniaxial strain applied in any direction and biaxial strain (figs. S6 to S8). The choice of tensile versus compressive strain to suppress all nonradiative recombination should ensure that the system remains direct gap bandgap with the application of strain to avoid nonradiative recombination through momentum-dark indirect excitons (25). Compressive strain can make some TMDC monolayers such as WS₂ indirect.

Strain has also been used to reduce traditional Auger recombination in conventional 3D semiconductors, but the mechanism is different (26). In 3D semiconductors, bandgap renormalization and effective mass equalization by applied strain can lead to one order of magnitude reduction of the conventional Auger rate (27). However, in the case of 2D TMDCs, EEA is inhibited by shifting the exciton transition energy \( E_X \) such that \( 2E_X \) did not overlap VHS resonance. Because of the existence of saddle points, logarithmic VHSs always characteristically appeared in 2D semiconductors and were not found in 3D, leading to a much stronger response to strain in monolayer TMDCs (15).

These principles applied equally to other TMDC semiconductors. Like WS₂, exfoliated monolayer WSe₂ also exhibited near-unity PL QY at all Gs when it was made intrinsically by electrostatic counterdoping and tensile strain was being applied (Fig. 3A and fig. S9). As-exfoliated monolayer MoS₂ has a PL QY in the range of 0.1 to 1.0%, which markedly increased at low pump after chemical counterdoping by Nafion (Fig. 3B). Unlike WS₂ and WSe₂, monolayer MoS₂ became an indirect-gap material when tensile strain was applied and remained...
Fig. 3. General nature of EEA suppression. Near-unity PL QY at all generation rates (Gs) in electrostatically counterdoped WSe$_2$ (A) and chemically counterdoped MoS$_2$ (B) by tensile and compressive strain, respectively, demonstrates the universality of the conditions that suppress nonradiative recombination.

Fig. 4. High PL QY on large-area CVD-grown WS$_2$. (A) Schematic (top) and photograph (bottom) of the flexible substrate used to strain CVD grown, centimeter-scale WS$_2$. (B) Normalized PL spectra of a typical spot at different strains. (C and D) Spatial mapping of PL QY of a 2-mm × 2-cm area of WS$_2$ grown at a low $G$ of 10$^{16}$ cm$^{-2}$ s$^{-1}$ and a high $G$ of 10$^{20}$ cm$^{-2}$ s$^{-1}$, respectively, shows that high PL QY is uniformly achieved by strain at the highest $G$ while maintaining high PL QY at low pump.

da direct-gap material when compressive strain was applied (17).

We found that, rather than creating compressive strain, downward bending of flexible substrate with negative curvature resulted in buckling of monolayer TMDC. Instead, we used the thermal coefficient of expansion mismatch between the glycol-modified PET substrate and MoS$_2$ to apply compressive strain. A chemically counterdoped, 0.5% compressively strained monolayer MoS$_2$ also exhibited roll-off free PL QY at all Gs. The optoelectronic quality of large-area 2D TMDCs must be improved for their use as next-generation devices. The principles of suppressing all nonradiative recombination can also be applied to achieve high PL QY on centimeter-scale WS$_2$ monolayer grown by CVD. We first transferred a large-area CVD-grown WS$_2$ (28) onto a flexible substrate and spin-coated it with Nafion (Fig. 4A). The normalized PL spectra redshifted with applied tensile strain (Fig. 4B). Nafion counterdoping led to a strain-independent PL QY of 70 ± 10% (mean ± SD) at low pump powers, as can be seen in a spatial map of the PL QY of a 2-mm × 2-cm area taken at a $G$ of 10$^{16}$ cm$^{-2}$ s$^{-1}$ (Fig. 4C).

ACKNOWLEDGMENTS

We thank J. Cho for providing large-area CVD-grown WS$_2$ samples.

Funding: This work was funded by the U.S. Department of Energy, Office of Science, Office of Basic Energy Sciences, Materials Sciences and Engineering Division under contract no. DE-AC02-05-CH11231 (EMAT program KC1201). E.R. acknowledges support from the U.S.

REFERENCES AND NOTES

1. D.-H. Lien et al., Science 364, 468–471 (2019).
2. J. S. Ross et al., Nat. Commun. 4, 1474 (2013).
3. F. Withers et al., Nat. Mater. 14, 303–306 (2015).
4. M. Amani et al., Science 350, 1065–1068 (2015).
5. Y. Yu et al., Phys. Rev. B 93, 201111 (2016).
6. F. Wang, Y. Wu, S. H. Hwang, T. F. Heinz, Phys. Rev. B Condens. Matter Mater. Phys. 73, 245424 (2006).
7. S. Z. Uddin, E. Rabani, A. Javey, Nano Lett. 21, 424–429 (2021).
8. C. Murawski, K. Leo, M. C. Gather, Adv. Mater. 25, 6831–6827 (2013).
9. W. Zou et al., Nat. Commun. 9, 608 (2018).
10. W. K. Bae et al., Nat. Commun. 4, 2661 (2013).
11. J. Iveland, L. Martini, J. Peretti, J. S. Speck, C. Weisbuch, Phys. Rev. Lett. 110, 174706 (2013).
12. M. A. Green, IEEE Trans. Electron Dev. 31, 671–678 (1984).
13. G. M. Kavoulakis, G. Baym, Phys. Rev. B Condens. Matter 54, 16525–16536 (1996).
14. O. B. Aslan, M. Deng, T. F. Heinz, Phys. Rev. B 98, 115308 (2018).
15. L. Van Hove, Phys. Rev. 89, 1189–1193 (1953).
16. J. E. Hirsch, D. J. Scalapino, Phys. Rev. Lett. 56, 2732–2735 (1986).
17. Z. Li et al., Nat. Commun. 11, 1151 (2020).
18. S. B. Desai et al., Nano Lett. 14, 4592–4597 (2014).
19. P. Landsberg, Recombination in Semiconductors (Cambridge Univ. Press, 2003).
20. V. N. Abakumov, V. I. Perel, I. N. Yassievich, Nonradiative Recombination in Semiconductors (Elsevier, 1991).
21. S. Fang, S. Carr, M. A. Cazalilla, E. Kaviris, Phys. Rev. B 98, 075106 (2018).
22. S. Fang et al., Phys. Rev. B Condens. Matter Mater. Phys. 92, 205308 (2015).
23. F. Basan, G. P. Parravicini, R. A. Ballinger, J. L. Birman, Phys. Today 23, 58–59 (1976).
24. M. Cardona, P. Y. Yu, Fundamentals of Semiconductors (Springer, Heidelberg, ed. 3, 2005).
25. J. Madelung et al., Science 370, 1299–1304 (2020).
26. M. Silver, E. P. O’Reilly, A. R. Adams, IEEE J. Quantum Electron. 33, 1557–1566 (1997).
27. A. Haug, J. Phys. C Solid State Phys. 16, 4159–4172 (1983).
28. J. Cho et al., Adv. Funct. Mater. 30, 1907941 (2020).
H.K. and S.Z.U. performed optical measurements. H.K., S.Z.U., and N.H. fabricated devices. H.K., S.Z.U., and A.J. analyzed the data. S.Z.U. and E.R. performed analytical modeling. S.Z.U., H.K., N.H., and A.J. wrote the manuscript. All authors discussed the results and commented on the manuscript. **Competing interests:** The authors declare no competing interests. **Data and materials availability:** All data needed to evaluate the conclusions in this study are present in the main text or the supplementary materials. Materials that support the findings of this study are available from the corresponding author upon reasonable and well-intentioned request.

**SUPPLEMENTARY MATERIALS**

science.sciencemag.org/content/373/6553/448/suppl/DC1

Materials and Methods

Figs. S1 to S10

References (29, 30)

MDAR Reproducibility Checklist

8 April 2021; accepted 21 June 2021

10.1126/science.abi9193
Inhibited nonradiative decay at all exciton densities in monolayer semiconductors
Hyungjin Kim, Shiekh Zia Uddin, Naoki Higashitarumizu, Eran Rabani and Ali Javey

Science 373 (6553), 448-452.
DOI: 10.1126/science.abi9193

Straining for high photoluminescence
The photoluminescence quantum yield in monolayer transition metal dichalcogenides generally drops at high emission intensities because the excitons undergo nonradiative annihilation. Kim et al. show that this process is resonantly amplified in these materials by van Hove singularities in their joint density of states. However, application of small mechanical strains (~0.5%) shifted the van Hove singularities and suppressed the nonradiative processes. Near-unity photoluminescence quantum yield at high exciton densities was seen in exfoliated monolayers of molybdenum sulfide, tungsten sulfide, and tungsten selenide, as well as centimeter-scale tungsten sulfide monolayers grown by chemical vapor deposition.

Science, abi9193, this issue p. 448
Supplementary Materials for

Inhibited nonradiative decay at all exciton densities in monolayer semiconductors

Hyungjin Kim†, Shiekh Zia Uddin†, Naoki Higashitarumizu, Eran Rabani, Ali Javey*

†These authors contributed equally to this work.
*Corresponding author. Email: ajavey@berkeley.edu

Published 23 July 2021, Science 373, 448 (2021)
DOI: 10.1126/science.abi9193

This PDF file includes:

Materials and Methods
Figs. S1 to S10
References
MATERIALS AND METHODS

Device Fabrication

TMDC monolayers (WS\textsubscript{2} and WSe\textsubscript{2} from HQ Graphene, MoS\textsubscript{2} from SPI supplies) were mechanically exfoliated on top of 50 nm SiO\textsubscript{2}/Si p++ substrates and were identified by optical contrast. 10 wt\% polyvinyl alcohol (PVA, Alfa Aesar, 98–99\% hydrolyzed, molecular weight 130,000 g/mol) solution were spin-coated at 1000 rpm for 40 seconds on the substrate with TMDC monolayer, and baked at 70 °C for 3 minutes to remove water solvent. Subsequently, a polyethylene terephthalate (PET, 125 μm thick) film is attached on top of the PVA film using adhesive (Super glue, Gorilla Glue Company) for ease of handling. Next, the entire flexible substrate (PVA/adhesive/PET) with the encapsulated monolayer TMDC is slowly peeled off from SiO\textsubscript{2} substrate using tweezer and resized so that the monolayer is at the center. Hexagonal boron-nitride (hBN, HQ Graphene) is mechanically exfoliated onto a 1×1 cm polydimethylsiloxane (PDMS) substrate. The flexible substrate is put on a sample stage under a modified optical microscope (bh2, Olympus) at room temperature and the hBN-exfoliated PDMS stamp was positioned upside down and aligned with the monolayer on the flexible substrate. The stamp was slowly brought into contact with the monolayer and peeled off rapidly, leading to transferred hBN on top of TMDC monolayer forming the insulator. In a similar fashion, Graphene (Graphenium, NGS Naturgraphit) is subsequently stamp-transferred on top of the TMDC monolayer/hBN stack to from source and top gate. Contacts are formed to the source and gate by applying silver conductive paste (EMS #12640, Electron Microscopy Sciences) to the graphene with a sharpened wooden tip under a Nikon stereomicroscope. Lastly, the device is encapsulated with poly(methyl
methacrylate) (PMMA; 950 A11, Microchem) prior to measurement by dropcasting and subsequent soft-baking at 70 °C for 5 minutes.

To prepare compressively strained monolayer MoS\textsubscript{2}, first MoS\textsubscript{2} was exfoliated on PDMS and then stamp was slowly brought into contact with the center of a piece of glycol-modified Polyethylene terephthalate (PETG, 2.54 mm thick, 3 cm length) at 90° C and peeled off, followed by rapid quenching of the MoS\textsubscript{2}-transferred PETG down to room temperature. The coefficients of thermal expansion (CTEs) of PETG and monolayer MoS\textsubscript{2} over the range of 20-90 °C were experimentally measured to be 80.5 ± 2.5 ppm/°C and 7 ppm/°C, respectively (29). The biaxial compressive strain applied in the monolayer MoS\textsubscript{2} due to the CTE mismatch can thus be calculated as

\[
\varepsilon(T_{tr}) = \int_{20^\circ C}^{T_{tr}} \alpha_{\text{PETG}}(T) dT - \int_{20^\circ C}^{T_{tr}} \alpha_{\text{MoS}_2}(T) dT \tag{1}
\]

where \(T_{tr}\) is the transfer temperature of monolayer onto the PETG, \(\alpha_{\text{PETG}}\) is the CTE of the PETG substrate, and \(\alpha_{\text{MoS}_2}\) is the CTE of the monolayer MoS\textsubscript{2}. Since we are using the transfer temperature of 90 °C, the biaxial compressive strain in the monolayer MoS\textsubscript{2} resulting from this quenching process was 0.51 %.

After the transfer, 3% Nafion perfluorinated resin solution (5 wt % in lower aliphatic alcohols and water, contains 15–20% water, Sigma Aldrich) diluted by ethanol was spin coated at 4000 rpm on the prepared MoS\textsubscript{2} sample with biaxial compressive strain.

Electrical and Optical Characterization

2
Devices were charged from an Keithley 2410 Source Meter Unit connected to the gate electrode, while the graphene source contact was grounded. The PL QY was measured using a customized micro-PL instrument which was calibrated as following procedure. The PL QY measurement calibration is also described in detail in previous study (1, 4). The wavelength of spectrometer was verified with Ar lamps (Newport) and the wavelength-dependent instrument response function was measured by a virtual Lambertian blackbody source, which was created with a stabilized lamp (Thorlabs SLS201) and a spectralon reflection standard (Labsphere). The collection efficiency was then acquired by measuring the laser response which was focused on the spectralon reflection standard. Because the emission profile of the monolayer semiconductors has been known to be Lambertian, this gives the reasonable approximation of the source of PL emission from the monolayers. For calibration measurements taken from the spectralon reflection standard, the fraction of generated photons which escape from the sample was calculated using $1/4n^2$, where $n$ is the refractive index of the medium (30). Independent approach was also used to verify the system calibration using a sample which has been known to have QY $\sim$100% (rhodamine 6G in methanol).

Generation rate $G$ is the number of excitons created or the number of photons absorbed per-unit area per unit time.

\[
G = \frac{\alpha P}{A\hbar\omega}
\]

where, $\alpha$ is the monolayer absorption at pump wavelength, $P$ is the pump laser power in Watts, $A$ is the area of the laser spot in cm$^2$, and $\hbar\omega$ is the energy of a 514.5 nm single photon. The absorption at pump wavelength is independent of strain. We vary the generation rate by varying the incident pump laser power.
In order to ensure that there is no change in light outcoupling factors or collection efficiency, we measured the samples that have PL QY independent of strain, as shown in the fig. S10. All of the samples show no change in PL spectra with applied strains, indicating that substrate-bending does not affect the PL QY and the same calibration approach can be used due to no change in light outcoupling and collection efficiency of the system.

An Ar ion laser with a 514.5 nm line was used as the excitation source. All measurements reported in this paper are taken at room temperature, in an ambient lab conditions under nitrogen flow. The applied strain on the flexible substrate were calculated using the equation \( \varepsilon = t / R \), where \( 2t \) and \( R \) are the substrate thickness and curvature radius. The thickness \( 2t \) of the entire flexible substrate is measured through the cross-section optical image. The curvature radius \( R \) were measured through the side-view photograph. All theory calculations are carried out in MATLAB.
fig. S1. Absorption at excitation wavelength under applied strain. Absorption of monolayer WS$_2$ as a function of applied strain at laser wavelength ($\lambda = 514.5$ nm).
fig. S2. PL QY versus $G$ and $V_g$ in WS$_2$ at different strains. A color plot of PL QY in monolayer WS$_2$ as a function of gate voltages and generation rate with applied strains.
**fig. S3 PL peak position shift of monolayer WS$_2$.** (A), Normalized PL intensity of monolayer WS$_2$ at $V_g = -30 V$ as a function of applied strains. (B), PL peak position during multiple bending and release cycles.
fig. S4 Near-unity PL QY in WS$_2$ at all generation rates. PL QY of monolayer WS$_2$ as a function of gate voltage and generation rate at 1.0 % strain.
fig. S5. Near-unity PL QY in chemically counterdoped WS$_2$ under strain. PL QY of as-exfoliated and chemically counterdoped monolayer WS$_2$ as a function of strain.
fig. S6. Direction independence of EEA suppression. (A), Direction of uniaxial strain (B), Exciton transition energy as a function of strain direction (C), VHS is shifted from twice of exciton transition energy independent of tensile strain direction.
fig. S7. Direction independence of EEA suppression. (A), Direction of uniaxial strain (B), Exciton transition energy as a function of strain direction (C), VHS is shifted from twice of exciton transition energy independent of compressive strain direction.
**fig. S8. EEA Suppression with Biaxial Strain.** VHS is also shifted from twice of exciton transition energy with biaxial compressive strain.
**fig. S9. Near-unity PL QY in WSe$_2$ at all generation rates.** (A), (B), (C), PL QY of monolayer WSe$_2$ as a function of gate voltage, generation rate and strain.
fig. S10. Negligible change in PL by bending of substrates. PL spectra of (A) PDY-132, (B) Poly(p-phenylene vinylene) (PPV), (C) CdSe quantum dots on PVA-PET flexible substrates as a function of applied strains.
References and Notes

1. D.-H. Lien, S. Z. Uddin, M. Yeh, M. Amani, H. Kim, J. W. Ager 3rd, E. Yablonovitch, A. Javey, Electrical suppression of all nonradiative recombination pathways in monolayer semiconductors. Science 364, 468–471 (2019). doi:10.1126/science.aaw8053 Medline

2. J. S. Ross, S. Wu, H. Yu, N. J. Ghimire, A. M. Jones, G. Aivazian, J. Yan, D. G. Mandrus, D. Xiao, W. Yao, X. Xu, Electrical control of neutral and charged excitons in a monolayer semiconductor. Nat. Commun. 4, 1474 (2013). doi:10.1038/ncomms2498 Medline

3. F. Withers, O. Del Pozo-Zamudio, A. Mishchenko, A. P. Rooney, A. Gholiniya, K. Watanabe, T. Taniguchi, S. J. Haigh, A. K. Geim, A. I. Tartakovskii, K. S. Novoselov, Light-emitting diodes by band-structure engineering in van der Waals heterostructures. Nat. Mater. 14, 301–306 (2015). doi:10.1038/nmat4205 Medline

4. M. Amani, D.-H. Lien, D. Kiriya, J. Xiao, A. Azcatl, J. Noh, S. R. Madhavapathy, R. Addou, S. Ke, M. Dubey, K. Cho, R. M. Wallace, S.-C. Lee, J.-H. He, J. W. Ager 3rd, X. Zhang, E. Yablonovitch, A. Javey, Near-unity photoluminescence quantum yield in MoS2. Science 350, 1065–1068 (2015). doi:10.1126/science.aad2114 Medline

5. Y. Yu, Y. Yu, C. Xu, A. Barrette, K. Gundogdu, L. Cao, Fundamental limits of exciton-exciton annihilation for light emission in transition metal dichalcogenide monolayers. Phys. Rev. B 93, 201111 (2016). doi:10.1103/PhysRevB.93.201111

6. F. Wang, Y. Wu, M. S. Hybertsen, T. F. Heinz, Auger recombination of excitons in onedimensional systems. Phys. Rev. B Condens. Matter Mater. Phys. 73, 245424 (2006). doi:10.1103/PhysRevB.73.245424

7. S. Z. Uddin, E. Rabani, A. Javey, Universal inverse scaling of exciton–exciton annihilation coefficient with exciton lifetime. Nano Lett. 21, 424–429 (2021). doi:10.1021/acs.nanolett.0c03820 Medline

8. C. Murawski, K. Leo, M. C. Gather, Efficiency roll-off in organic light-emitting diodes. Adv. Mater. 25, 6801–6827 (2013). doi:10.1002/adma.201301603 Medline

9. W. Zou, R. Li, S. Zhang, Y. Liu, N. Wang, Y. Cao, Y. Miao, M. Xu, Q. Guo, D. Di, L. Zhang, C. Yi, F. Gao, R. H. Friend, J. Wang, W. Huang, Minimising efficiency roll-off in high-brightness perovskite light-emitting diodes. Nat. Commun. 9, 608 (2018). doi:10.1038/s41467-018-03049-7 Medline

10. W. K. Bae, Y.-S. Park, J. Lim, D. Lee, L. A. Padilha, H. McDaniel, I. Robel, C. Lee, J. M. Pietryga, V. I. Klimov, Controlling the influence of Auger recombination on the performance of quantum-dot light-emitting diodes. Nat. Commun. 4, 2661 (2013). doi:10.1038/ncomms3661 Medline

11. J. Iveland, L. Martinelli, J. Peretti, J. S. Speck, C. Weisbuch, Direct measurement of Auger electrons emitted from a semiconductor light-emitting diode under electrical injection: Identification of the dominant mechanism for efficiency droop. Phys. Rev. Lett. 110, 177406 (2013). doi:10.1103/PhysRevLett.110.177406 Medline

12. M. A. Green, Limits on the open-circuit voltage and efficiency of silicon solar cells imposed by intrinsic Auger processes. IEEE Trans. Electron Dev. 31, 671–678 (1984). doi:10.1109/T-ED.1984.21588
13. G. M. Kavoulakis, G. Baym, Auger decay of degenerate and Bose-condensed excitons in Cu$_2$O. Phys. Rev. B Condens. Matter 54, 16625–16636 (1996). doi:10.1103/PhysRevB.54.16625 Medline

14. O. B. Aslan, M. Deng, T. F. Heinz, Strain tuning of excitons in monolayer WSe$_2$. Phys. Rev. B 98, 115308 (2018). doi:10.1103/PhysRevB.98.115308

15. L. Van Hove, The occurrence of singularities in the elastic frequency distribution of a crystal. Phys. Rev. 89, 1189–1193 (1953). doi:10.1103/PhysRev.89.1189

16. J. E. Hirsch, D. J. Scalapino, Enhanced superconductivity in quasi-two-dimensional systems. Phys. Rev. Lett. 56, 2732–2735 (1986). doi:10.1103/PhysRevLett.56.2732 Medline

17. Z. Li, Y. Lv, L. Ren, J. Li, L. Kong, Y. Zeng, Q. Tao, R. Wu, H. Ma, B. Zhao, D. Wang, W. Dang, K. Chen, L. Liao, X. Duan, X. Duan, Y. Liu, Efficient strain modulation of 2D materials via polymer encapsulation. Nat. Commun. 11, 1151 (2020). doi:10.1038/s41467-020-15023-3 Medline

18. S. B. Desai, G. Seol, J. S. Kang, H. Fang, C. Battaglia, R. Kapadia, J. W. Ager, J. Guo, A. Javey, Strain-induced indirect to direct bandgap transition in multilayer WSe$_2$. Nano Lett. 14, 4592–4597 (2014). doi:10.1021/nl501638a Medline

19. P. Landsberg, Recombination in Semiconductors (Cambridge Univ. Press, 2003).

20. V. N. Abakumov, V. I. Perel, I. N. Yassievich, Nonradiative Recombination in Semiconductors (Elsevier, 1991).

21. S. Fang, S. Carr, M. A. Cazalilla, E. Kaxiras, Electronic structure theory of strained two-dimensional materials with hexagonal symmetry. Phys. Rev. B 98, 075106 (2018). doi:10.1103/PhysRevB.98.075106

22. S. Fang, R. Kuate Defo, S. N. Shirodkar, S. Lieu, G. A. Tritsaris, E. Kaxiras, Ab initio tight-binding Hamiltonian for transition metal dichalcogenides. Phys. Rev. B Condens. Matter Mater. Phys. 92, 205108 (2015). doi:10.1103/PhysRevB.92.205108

23. F. Bassani, G. P. Parravicini, R. A. Ballinger, J. L. Birman, Electronic states and optical transitions in solids. Phys. Today 29, 58–59 (1976). doi:10.1063/1.3023374

24. M. Cardona, P. Y. Yu, Fundamentals of Semiconductors (Springer, Heidelberg, ed. 3, 2005).

25. J. Madéo, M. K. L. Man, C. Sahoo, M. Campbell, V. Pareek, E. L. Wong, A. Al-Mahboob, N. S. Chan, A. Karmakar, B. M. K. Mariserla, X. Li, T. F. Heinz, T. Cao, K. M. Dani, Directly visualizing the momentum-forbidden dark excitons and their dynamics in atomically thin semiconductors. Science 370, 1199–1204 (2020). doi:10.1126/science.aba1029 Medline

26. M. Silver, E. P. O’Reilly, A. R. Adams, Determination of the wavelength dependence of Auger recombination in long-wavelength quantum-well semiconductor lasers using hydrostatic pressure. IEEE J. Quantum Electron. 33, 1557–1566 (1997). doi:10.1109/3.622637

27. A. Haug, Auger recombination in direct-gap semiconductors: Band-structure effects. J. Phys. C Solid State Phys. 16, 4159–4172 (1983). doi:10.1088/0022-3719/16/21/017
28. J. Cho, M. Amani, D.-H. Lien, H. Kim, M. Yeh, V. Wang, C. Tan, A. Javey, Centimeter-scale and visible wavelength monolayer light-emitting devices. *Adv. Funct. Mater.* **30**, 1907941 (2020). doi:10.1002/adfm.201907941

29. L. Zhang, Z. Lu, Y. Song, L. Zhao, B. Bhatia, K. R. Bagnall, E. N. Wang, Thermal expansion coefficient of monolayer molybdenum disulfide using micro-Raman spectroscopy. *Nano Lett.* **19**, 4745–4751 (2019). doi:10.1021/acs.nanolett.9b01829 Medline

30. E. Yablonovitch, G. D. Cody, Intensity enhancement in textured optical sheets for solar cells. *IEEE Trans. Electron Dev.* **29**, 300–305 (1982). doi:10.1109/T-ED.1982.20700