MPR 1.0: a stand-alone multiscale parameter regionalization tool for improved parameter estimation of land surface models

Robert Schweppe1,2, Stephan Thober1, Sebastian Müller1, Matthias Kelbling1, Rohini Kumar1, Sabine Attinger1,2, and Luis Samaniego1

1Helmholtz-Centre for Environmental Research – UFZ, Permoserstraße 15, 04315 Leipzig, Germany
2Institute of Earth and Environmental Science, University of Potsdam, Karl-Liebknecht-Str. 24–25, 14476 Potsdam-Golm, Germany

Correspondence: Stephan Thober (stephan.thober@ufz.de)

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Abstract. Distributed environmental models such as land surface models (LSMs) require model parameters in each spatial modeling unit (e.g., grid cell), thereby leading to a high-dimensional parameter space. One approach to decrease the dimensionality of the parameter space in these models is to use regularization techniques. One such highly efficient technique is the multiscale parameter regionalization (MPR) framework that translates high-resolution predictor variables (e.g., soil textural properties) into model parameters (e.g., porosity) via transfer functions (TFs) and upscaling operators that are suitable for every modeled process. This framework yields seamless model parameters at multiple scales and locations in an effective manner. However, integration of MPR into existing modeling workflows has been hindered thus far by hard-coded configurations and non-modular software designs. For these reasons, we redesigned MPR as a model-agnostic, stand-alone tool. It is a useful software for creating graphs of NetCDF variables, wherein each node is a variable and the links consist of TFs and/or upscaling operators. In this study, we present and verify our tool against a previous version, which was implemented in the mesoscale hydrologic model (mHM; https://www.ufz.de/mhm, last access: 16 January 2022). By using this tool for the generation of continental-scale soil hydraulic parameters applicable to different models (Noah-MP and HTESSEL), we showcase its general functionality and flexibility. Further, using model parameters estimated by the MPR tool leads to significant changes in long-term estimates of evapotranspiration, as compared to their default parameterizations. For example, a change of up to 25 % in long-term evapotranspiration flux is observed in Noah-MP and HTESSEL in the Mississippi River basin. We postulate that use of the stand-alone MPR tool will considerably increase the transparency and reproducibility of the parameter estimation process in distributed (environmental) models. It will also allow a rigorous uncertainty estimation related to the errors of the predictors (e.g., soil texture fields), transfer function and its parameters, and remapping (or upscaling) algorithms.

1 Introduction

Distributed environmental models simulate key fluxes and states of the atmosphere, land surface, and subsurface for a given spatial domain and time period (e.g., CLM, Andre et al., 2020, JULES, Best et al., 2011, or ORCHIDEE, Krinner et al., 2005). The underlying physical processes are simplified with parameterizations that are manifested as computer algorithms. Parameterizations are idealized representations of reality, and as such there is inherent uncertainty in their formulation. They require additional variables and model parameters in order to perform simulations. The latter could be constant, or it could be spatially and temporally variable over the simulation domain (i.e., the so-called distributed model parameters). Constant model parameters do not allow accurate characterization of environmental processes over a range of climatic regimes and geophysical properties (Samaniego et al., 2010; Beck et al., 2016). The number of distributed model parameters tend to scale linearly with the number of spatiotemporal units, which is defined...
by the coordinates along each dimension of the parameterized process. Model parameters are often fine-tuned to match observed fluxes and states of physical processes in various fields, such as hydrology (Zink et al., 2017; Pagliero et al., 2019), Earth system sciences (Troy et al., 2008), and hydraulics (Shoarinezhad et al., 2020). Currently, there exists a plethora of methods for parameter estimation (Samaniego et al., 2017), which is the process of estimating a set of model parameters over the whole domain and their respective distribution functions. Such methods include classification linked through lookup tables (for example, ECMWF, 2019; Andre et al., 2020), direct calibration (for example, Li et al., 2018; Arheimer et al., 2020), calibration and regionalization (for example, Carrera et al., 2005; Oudin et al., 2008; Samaniego et al., 2010; Rojas-Serna et al., 2016; Hundecha et al., 2016), and probabilistic methods (for example, González-García et al., 1998; Thiemann et al., 2001). Optimization issues related to parameter estimation through calibration tasks are often solved by the application of optimization algorithms (for example, Duan et al., 1993; Tolson and Shoemaker, 2007).

Distributed models have a parameter space with a very large dimensionality (Schaaake, 2003). Even if high-performance computing (HPC) is available, it is not only numerically infeasible to estimate parameters for every individual grid cell but also an ill-posed problem in lieu of limited availability of reference datasets (Kirchner, 2006). Samaniego et al. (2017), for example, indicated the presence of large differences in parameter estimation methods and the derived distributed parameter fields for many state-of-the-art global hydrological models (GHMs) and land surface models (LSMs). Regionalization techniques, such as multiscale parameter regionalization (MPR) (Samaniego et al., 2010), provide an approach for reduction of dimensionality of parameter space through efficient use of regularization functions to estimate spatially explicit model parameters (Pokhrel and Gupta, 2010; Gupta et al., 2014).

The MPR framework operates on a two-step procedure. In the first step, it employs transfer functions (TFs) to translate high-resolution geophysical properties into high-resolution model parameters. It can easily meet the requirements posed by Van Looy et al. (2017) to couple information from different datasets (e.g., soil, vegetation, and topography) or establish time-varying parameters depending on changes in land use or climate (Vereecken et al., 2019). In the second step, high-resolution parameters are upscaled using upscaling operators to the spatial resolution and topology of the selected spatial units at which the model is to be applied. The resulting quasi-scale-independent parameters explicitly consider sub-grid variability and predictor uncertainty if multiple sources are used (Samaniego et al., 2010; Kumar et al., 2013b; Rakovec et al., 2016; Dembélé et al., 2020). Optimization approaches therefore should adjust the (globally applied) parameters of the TFs and the parameters of the upscaling operator.

Currently, MPR is implemented as part of the source code of the mesoscale hydrologic model (mHM) (Samaniego et al., 2010; Kumar et al., 2013b) and cannot be easily adapted for other models. Furthermore, this mHM-bound version is restricted to rectangular grids and uses a hard-coded set of TFs for model parameters required by the mHM specifically. Mizukami et al. (2017) proposed a flexible version of MPR (MPR-flex) to estimate parameters for the hydrological models VIC (Liang et al., 1994; Hamman et al., 2018) and SAC (Burnash, 1995). This tool is also limited to a set of model-specific parameters: namely, TFs and the two targeted models. In recent years, there have been numerous applications of MPR as a parameter estimation technique for other models (for example, Samaniego et al., 2017; Mizukami et al., 2017; Imhoff et al., 2020); however, no generic software currently exists. In addition, existing applications are more targeted toward hydrologic applications; nevertheless, challenges persist with regards to accurate estimation of the seamless fields of model parameters across a variety of spatial resolutions in different compartments of Earth system science models.

Therefore, a new MPR tool that provides a tailored framework for distributed parameter estimation is urgently needed (Van Looy et al., 2017; Vereecken et al., 2019). With this aim in mind, we propose an MPR framework that can be used as a preprocessor for both large-scale applications of land surface models and global or regional hydrologic models. It needs to be a flexible, model-agnostic, lightweight, and high-performance tool with few external dependencies. Another key goal is to allow the MPR tool to be embedded in optimization workflows such that TFs and remapping techniques can be easily modified (Van Looy et al., 2017). Thus, the configuration overhead should be kept minimal. Although targeted towards and originating from the LSM community, the development of MPR is aimed at supporting parameter estimation for distributed models in any scientific field.

One key challenge is establishing a proper linkage between model parameters and suitable predictor variables (Clark et al., 2016; Blöschl et al., 2019). Most currently used TFs are derived from commonly observed or measured predictors and parameters (Van Looy et al., 2017). Mathematical frameworks (e.g., linear regression models, artificial neural networks, and random forests) are applied to training datasets in order to develop functional relationships. However, TFs can also be inferred through inverse methods. Emerging methods for the development of TFs do exist (Kloet et al., 2017; Feigl et al., 2020; Merz et al., 2020). MPR provides the interface to link these tools to distributed environmental models.

Providing a library of remapping schemes is crucial, as the parameterizations in environmental models are not applied on the scales at which they were derived. For example, the Richardson and Richards’ equation (Richardson, 1922; Richards, 1931) describing unsaturated water flow through
porous media at the representative elemental volume scale is often used at the landscape scale (say 10^2 km). The inherent uncertainty of the physical parameters describing this phenomenon needs to be adequately considered by the choice of transfer functions and upscaling operators (Montzka et al., 2017; Vereecken et al., 2019). More generally, flow rates such as saturated hydraulic conductivity are common parameters in environmental models, and their scaling behavior should be considered (Zhu and Mohanty, 2002; Kumar et al., 2013b). Additionally, their anisotropic properties necessitate a dimension-dependent selection of upscaling operators (e.g., harmonic and arithmetic mean).

In this paper, we first present a working example to illustrate current challenges in the estimation of distributed parameter fields in environmental models. We would like to provide hands-on information to environmental modellers from the Earth system science communities in Sects. 2, 3.5, 4, and 5.

Section 2 outlines different ways to estimate distributed parameters and deduces feature requirements for the MPR tool. Section 3.5 highlights those features and the resulting applicability. In Sect. 4, we demonstrate the versatility of the MPR tool by reproducing an open-source dataset (EU-SoilHydroGrids Tóth et al., 2017) containing soil hydraulic properties derived from a set of TFs. We demonstrate its tight coupling to the hydrologic model mHM and its capabilities with regard to the reproduction of the original mHM model behavior. The effects on long-term evapotranspiration from the coupling of MPR to state-of-the-art land surface models (Noah-MP and HTESSEL) are also shown. This is achieved by an effective TF application and parameter regridding that is applicable to any model that requires distributed parameters (e.g., LSM or environmental models). Section 5 concludes our work on the parameter estimation tool MPR.

Section 3.1 to 3.4 contain details of the technical implementation of MPR that are interesting for software engineers and model developers that would like to integrate MPR in their software. We show how the new generic and agnostic MPR tool is designed and configured to meet the required features. Section 3.2 elucidates the configuration of MPR and is followed by a detailed description of how to interface MPR through a stand-alone executable, as well as through its API (application programming interface), in Sect. 3.4.

2 A minimal working example in environmental modeling

2.1 Objective

For demonstration purposes we define an objective that is commonly encountered in environmental modeling. For a hypothetical intercomparison project, the influence of different parameter estimation schemes for soil parameters is investigated for a given domain along with two different resolutions and three different model-specific grid types.

A common parameter present in many environmental models is soil porosity (θs), which denotes the pore volume fraction of the total soil volume in the vadose zone. The SoilGrids (SG) dataset (Hengl et al., 2017) provides soil physical properties at a high resolution (1/480°). From the extensive literature on pedotransfer functions (TFs for soil parameters) (Patil and Singh, 2016), we selected a TF for estimating θs based on bulk density, organic matter, clay, and sand content (Weynants et al., 2009). The southeastern United States, which includes the state of Florida, was chosen as the domain of interest due to high heterogeneity in the physical properties of the soil in this region. We selected different grid layouts that are often used in different modeling disciplines. These are regular rectangular grids generally used in distributed environmental modeling (Ma et al., 2017; Zink et al., 2017), icosahedral grids representing the group of geodesic grids increasingly used in the earth system science community (Zängl et al., 2015; Skamarock et al., 2012), and polygons or hydrologic response units (HRUs) often used in hydrology or the soil sciences (Wellen et al., 2015).
The exemplary workflow depicted in Fig. 1 shows the high-resolution predictor variables (shown in the lower-left corner) that are passed to the transfer function (TF) to derive the resulting porosity (lower-right corner) at the predictor resolution. It exhibits considerable heterogeneity in various gradients between the southeast and northwest regions of the domain, coastal and inland areas, riverbeds, and mountainous areas. The target variable is then upscaled to six different spatial grids at different resolutions. Regular rectangular grids with resolutions of 1/8 and 1° are shown in the left column of the top panel of Fig. 1. The lower grid is the same as the one used for the North American Land Data Assimilation System 2 forcing dataset (Mitchell et al., 2004). The latter dataset covers the domain of the conterminous United States (CONUS) and has been used for different LSMs (Xia et al., 2012). The two icosahedral grids specified by the identifiers R02B04 and R02B05 (Fig. 1 the center column in the top panel Zängl et al., 2015) can be used for the configuration of LSM JSBACH (Mauritsen et al., 2019). Finally, polygons denoting the WBDHU4 and WBDHU6 domains (Fig. 1, right column in the top panel) and the realizations of the National Watershed Boundaries Dataset (Service Center Agencies, 2019) can be used for HRU-based (Flügel, 1995) models such as SWAT (Gassman et al., 2007) or PRMS (Markstrom et al., 2015). The figure demonstrates how different grids represent compromises between conservation of sub-grid heterogeneity and reduction of spatial complexity. Although the parameter gradients in the valleys in South Carolina in the parameter fields of the 1/8° rectangular grid are still visible, they are not visible in the other grids. The reduced number of grid cells allows for a lower computational load during model run times (simulations).

This parameter estimation routine, which is followed by simulations of the distributed model, might then be used iteratively by a calibration routine in order to optimize TF parameters. These are global parameters of the TF whose application to the predictors is used to derive the effective distributed model parameters. Next, a workflow to derive these parameters in an efficient and consistent manner is presented.

2.2 Options for parameter estimation workflow

There exists a range of different options for the workflow described in the previous section, which we briefly describe here. A few existing software tools and general circulation model (GCM) couplers can be used to perform the two key steps of applying a TF and remapping a multi-dimensional grid onto another.

1. In climate sciences, the command line data-processing tools cdo (Schulzweida, 2019), nco (Zender, 2008) or TempestRemap (Ullrich and Taylor, 2015) are commonly used. cdo and nco can perform both application of TFs (ncap2 operator) and remapping (ncremap operator). TempestRemap, however, serves solely as a regridding library.

To perform parameter estimations using one of these tools, we need to establish a stack of calls to the expr operator and remap. This can be achieved either directly or from a scripting language, for which wrapper libraries are provided. To improve the usability of the approach, the setup would need a wrapper library on its own to manage file input/output (I/O), parameters, coordinates, transfer functions, and upscale operations. One advantage of the developed MPR tool is that the entire workflow is described in a single configuration file.

2. Numerous couplers of Earth system models (ESMs) contain routines for the remapping of variables, e.g., ESMF (Collins et al., 2005) with RegridWeightGen, Atlas (Deconinck et al., 2017), and OASIS (Craig et al., 2017). For example, parts of the ESMF library can be compiled to the ESMF RegridWeightGen application, which readily interfaces with multiple NetCDF-based grid formats and performs a number of different remapping algorithms. In addition, LFRic (Adams et al., 2019) and Atlas also provide a data model explicitly designed to support HPC applications. All of the aforementioned software tools and couplers expose their API and are publicly available and actively maintained by their respective communities.

Coupling libraries perform a multitude of tasks and thus have a code base of considerable size. The installation procedure requires multiple dependencies on third-party software and is extremely demanding. Apart from RegridWeightGen, access to the correct sections of the API for remapping and function evaluation is not easily attainable. Accurate imitation of MPR functionality would require a setup similar to that of cdo, as well as establishment of a wrapper that effectively executes a set of commands or directly accesses the backend routines.

3. The processing of polygon-based data from shapefiles or geodatabases is often conducted using Geographic Information Systems (GIS) such as QGIS (QGIS development team, 2020) or ArcGIS (ESRI, 2020). The support of NetCDF-based data has been introduced in recent versions of QGIS by the MDAL library (MDAL contributors, 2020). GIS possesses a large inventory for handling spatial data and associated visualizations.

After launching the target program, for example QGIS, the predictor dataset needs to be loaded and the TF must be applied on the variable through the field calculator. A new layer is created through application of the appropriate spatial interpolation plugin. The exporting of workflow steps to Python is available for automatization.
2.3 Motivation for a new software tool

To the best of our knowledge, none of the aforementioned GCM couplers and GIS support out-of-the-box TF and upscaling applications. Although cdo and nco support dynamic evaluation of algebraic expressions, their implementation is cumbersome, bound to heavy disk I/O, and has a long run time because of the dynamic evaluation of the transfer function. Additionally, not every tool supports remapping between polygons (e.g., basin boundaries or hydrological response units). cdo poses further restrictions on variable dimensions (conventionally, it supports only specific \( x, y, z \) and \( t \) axes). The support of dimension-dependent upscaling operators is not available for remapping tools (e.g., vertical dimensions must be handled differently than horizontal dimensions in aggregation of soil horizon specific parameters).

Previous software implementations of the MPR framework (Samaniego et al., 2010; Mizukami et al., 2017) have limited applicability as a result of hard-coded parameters, TFs, and upscaling operators.

The aforementioned restrictions inspired the motivation to rewrite MPR from scratch. The new tool has some key advantages:

- It can use multiple, high-resolution datasets on different grids for parameter estimation.
- It allows for applying the MPR technique for any distributed model, namely calculating model parameters at the highest resolution possible before aggregating to a model resolution.
- It can incorporate an arbitrary number of predictor variables, TFs, and upscaling operators.
- It has a low run time because of it is implemented in Fortran.
- The reproducibility of the parameter estimation workflow is increased.

The example runs of MPR producing the parameter fields for the regular \( 1/8^\circ \) and WBDHU6 polygons in Fig. 1 from predictor variables at \( 1/480^\circ \) resolution consumed a maximum of 29 and 24 GB memory with a total run time of 5 min and 1 s and 16 min and 33 s, respectively. Those values were estimated by the Valgrind tool and for an executable compiled by the gFortran compiler on a computing cluster.

Some of its advantages also have a respective trade-off. As such, the tool depends on Fortran compilers and the NetCDF library, which can be cumbersome to install. In addition, the MPR technique poses a high memory requirement. In its current development state, MPR was designed to be coupled with specific LSMs that require the NetCDF input format for its distributed parameters. Usage of MPR therefore is only possible for models that support the setting of (distributed) parameters in the NetCDF format.

3 Salient configurations of the developed MPR tool

3.1 Nomenclature, conventions, and general design

The API is closely built around the NetCDF file format (version \( > 4.4.1 \)) (Unidata UCAR, 2020). The resemblance of the NetCDF format is motivated by its widespread use in environmental modeling and its paradigm of being scalable, portable, and self-describing. A file typically contains numerous multidimensional variables. Each dimension of each variable is an array of monotonically ordered integers and can be shared among multiple variables. Each variable and dimension has a name, and the referencing of dimensions is done using these names. The CF (Climate and Forecast) convention (Eaton et al., 2017) further defines a coordinate variable as a one-dimensional variable sharing the same name as its associated dimension. Its values are ordered monotonically and missing values are prohibited. Auxiliary coordinate variables also contain coordinate information, but their names differ from their dimensions. Attributes containing meta-information can be added to various objects such as variables, dimensions, and the file itself.

MPR adopted this concept and nomenclature for its data structures while imposing a number of additional restrictions. MPR variables are called Data_Arrays, as variables is a very generic term. We drop the concept of dimensions in favor of coordinate variables. This is necessitated by the fact that each cell needs to be explicitly bounded along its dimensions to avoid ambiguities during upscaling. Coordinate variables are referred to as Coordinates. Data_Arrays need to point to instances of Coordinates defining their extent. We also assume that each one-dimensional coordinate variable, in principle, represents not a point but an interval (or cell) and that adjacent intervals are contiguous for one-dimensional coordinates. MPR supports the boundary variables as defined by Eaton et al. (2017) and is generally able to handle two-dimensional auxiliary coordinate variables as well. Thus, MPR accepts either one-dimensional or two-dimensional auxiliary coordinate variables. Users can set custom string attributes to coordinate variables for creating a self-describing output file.

3.2 Interfacing a standalone executable MPR

We show an example configuration in Fig. 2 to derive a target variable that is similar to what is shown in Fig. 1 (marked as medium non-rectangular grid).

The configuration is performed in a Fortran-native, hierarchically organized namelist format (comparable to .json, .yaml, .ini, etc.). MPR has three required sections and two optional sections. Users can enter the minimal required information in a flexible and intuitive manner. The required sections are Main, Data_Arrays, and Coordinates and the optional sections are Parameters and Upscalers.
designed as arrays of respective objects whose specific properties are set using the correct list index. The term Data_Arrays refers to any n-dimensional variable and serves as a generic term for predictors and target variables. In lines 1ff. in Fig. 2, there are four Data_Arrays specified: the first three are read directly from file, while the fourth is calculated from the former. The property from_data_arrays specifies the array of predictors to be used. They also appear in the TF equation that is supplied as a string in transfer_func. It follows the Fortran syntax for operators, brackets, and some elemental mathematical functions (see Appendix Table E1 for a list of possible operators). Users can use any parameter defined in Parameters in a TF. The TF string is not dynamically evaluated during execution because it leads to unnecessarily high computational run times. Additionally, the effort required to modify the Fortran source code each time a new function is used would substantially diminish the user-friendliness of the MPR tool. Instead, a Python preprocessor script is implemented that interprets and adds the transfer function from the namelist and modifies the source code accordingly. At run time, simple search and replacement routines translate the string into a unique function ID that is checked against all unique function IDs in the source code.

The target coordinates and associated upscaling operators are set with target_coord_names and upscale_ops. Upscaling operators are real numbers provided as strings. They specify the \( p \) parameter of the Hölder mean and geometric mean (Sykora, 2009) (when entered as a real number). Alternatively, the subgrid minimum, maximum, sum, variance, or the value with the largest area fraction can be used when entered as a string. A full list of all possible operators is provided in Appendix Table E2. A flag to_file can be set to signal the data array to be stored on the disk.

All parameters referred to from any TF can be specified by name and value in the Parameters section (1ff. in Fig. 2). The TF for the fourth data array requires multiple parameters (e.g., \( a5 \)). Accordingly, more parameters can be set and reused in multiple TFs, while users should avoid naming duplications with TF operators or data arrays.
parameters usually encompass constants and variable parameters subject to optimization, and as such the Parameters section can also be read from a separate file containing only the parameters subject to optimization. This file is optional, and its parameters replace previously read parameters in the case of duplicates.

The target coordinates are specified in the Coordinates section (l. 26 ff. in Fig. 2). The user explicitly specifies the boundaries of the soil layers by values in this example (coord_from_values). These refer to the stagger of each cell or horizon (coord_stagger). In this case, the first cell does not have a neighboring cell boundary, and as such the user must specify the coordinate boundary to provide a start value (coord_from_values_bound). A two-dimensional coordinate serving as the target grid is read from the file (coord_from_file). Its associated dimensions are specified through coord_sub_dims. Alternatively, coordinate values can be specified from a range if the user provides values for start, step, and count.

The Main section (l. 37 ff. in Fig. 2) configures general information. The link from the target coordinates to the respective source coordinates during upscaling is constructed through the coordinate_groups entries. During upscaling, each source coordinate needs to receive a target coordinate. If the source coordinate shares the same coordinate_group as one of the target coordinates, upscaling is performed for that coordinate pair. Users can enter an arbitrary number of groups, although a dimension system with \( x, y, z, \) and \( t \) is most commonly defined. Finally, the path to the output file is set.

A more exhaustive description of the aforementioned configuration can be found in https://chs.pages.ufz.de/MPR/index.html, last access: 16 January 2022.

3.3 Interdependence of parameters

MPR allows for constructing arbitrarily complex interdependence graphs between predictors and the temporary and final (output) data arrays. As such, it is for example possible to link soil related parameters not only to soil properties but also to land use or geological predictors or any of its derivative properties. However, a basic requirement is that the required dimensions for each Data_Array need to be present in the predictor Data_Arrays referenced by the Data_Array’s TF. Such an example configuration is shown in Fig. 3, for creation of NetCDF variable graphs, where each node is a Data_Array and the links consisting of TFs and/or upscaling operations. It visualizes the dependency graph for two of the parameters required for the mHM in its standard configuration. The blue ellipses denote the predictor variables used. While land_cover is a three-dimensional array with coordinates, year, latitude, longitude \((t_1, y, x)\), lai_class is a three-dimensional array with coordinates, month of year, latitude, and longitude \((t_2, y, x)\). The TF for the model parameter PET_LAI_corr_factor requires both leaf area index (LAI) and land cover information. Both predictors need to be broadcast to a four-dimensional array \((t_1, t_2, y, x)\), and thus temporary arrays are created. The TF for the model parameter Aerodyn_resist requires information on canopy and wind measurement height, while the wind measurement height is derived from the former alone. For the calculation of canopy_height, a max-normalized LAI is needed for each cell. The Data_Array contains this information, and its broadcast variant LAI_max_t2_4D will thus be the same shape as the other predictors of the TF responsible for producing canopy_height. The two model parameters highlighted by the red ellipses are finally upscaled to the target model resolution with coordinates modeling year, month of year, low-resolution latitude, and low-resolution longitude.

3.4 Interfacing MPR library

While the previous section introduced the use of MPR as a standalone wrapper, we anticipate a tight coupling of the MPR code to the main modeling code. We intend to impose maximum reusability of the MPR API and ease its implementation into other libraries. Top-level objects such as Data_Arrays or Coordinates can be reused multiple times and can also be written to and read from the disk as requested. The Fortran API is used here for this purpose, which is based on the object-oriented programming paradigm and exposes four main objects (derived type in Fortran), which are also present in the namelist configuration (see previous section): Coordinate, Parameter, Data_Array, and CoordUpscaler. After initialization, these types are stored in global arrays that allow for cross-referencing with other types. They are briefly described in this section, and additional detail can be found at the following URL: https://chs.pages.ufz.de/MPR/index.html, last access: 16 January 2022.

3.4.1 Coordinate type

One central derived type in MPR is the Coordinate. First and foremost, it stores the boundaries of its \( n \) cells. In the case of a (one-dimensional) coordinate variable, each cell has two boundaries \((v = 2)\), and as cells are contiguous, the boundaries do not need to be stored in a \((v, n)\)-shaped array but in an \((n + 1)\) array. This property is termed boundaries1d. In the case of a two-dimensional auxiliary coordinate variable, the number of boundaries and edges can vary. To obtain a general formulation, we stored the boundaries of both dimensions in an \((v, n)\)-shaped array. These properties are termed boundaries2dDim1 and boundaries2dDim2. Additionally, the cell centers are stored in centers2dDim1 and centers2dDim2.

3.4.2 Parameter type

Parameters are objects with names and numerical values assigned to them.

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3.4.3 Data_Array type

The main derived type is the Data_Array, which can be read directly from an existing NetCDF file (blue circle in Fig. 3) or computed from other Data_Arrays and/or Parameters using TF and upscaling operators (red and black circle in Fig. 3). It stores multidimensional data, which must be passed to multiple other routines. In order to have a common sparse data container, non-masked cells are stored in a one-dimensional array data with type real, regardless of the number of underlying dimensions. A Boolean mask of the data is stored in a flattened, one-dimensional array, reshapedMask. A one-dimensional array pointing to its associated Coordinates is set as coords. This holds the shape information of the original uncompressed data. These core properties, reshapedMask, data, and coords, are pointed at from within the wrapper type InputFieldContainer. It is used for referencing the core properties of the Data_Array and are usually passed...
as an argument for the TransferHelper type, which is described in the next section.

### 3.4.4 Application of transfer functions

The type TransferHelper is intended to be used for the initialization of Data_Array, which originates from either a file or from other Data_Arrays via TFs (e.g., see canopy_height in Fig. 3). During its initialization, it performs checks on the passed InputFieldContainer, checks their Coordinates, optionally concatenates Data_Arrays, and optionally adapts their masks. After these checks, the TF is applied. TFs are designed as a subroutine accepting an arbitrarily sized list of InputFieldContainer (its data property is accessed only) and Parameters. An abstract interface for TFs thus allows for a variable number of predictor arrays and parameters. A one-dimensional array is returned. We provide a template for a subroutine containing a TF so that users can modify the source code and implement their own TFs (see Appendix Fig. D1). This enables the integration of more complex mathematical formulations such as artificial neural networks or support vector machines. Based on the majority of TFs used in existing LSMs (Van Looy et al., 2017), we anticipate users primarily using TFs that employ common mathematical operators such as multiplication and division. Such equations can be automatically parsed from configuration files and inserted into the Fortran source code using a Python preprocessor, which is described next.

Each TF string occurring in a namelist is translated into a unique identifier. For example, string \( \exp (a5 + c5 \times \text{sand} + d5 \times \text{bd} + e5 \times \text{om}) / \text{unit_conversion} \) (Fig. 2) can be set in the configuration file and will then be analyzed and processed by a parser routine. MPR replaces all parameters (a5, c5, d5, e5, unit_conversion) and variable names (sand, bd, om) by identifiers, translating the resulting string \( \exp (p1 + p2 \times x1 + p3 \times x2 + p4 \times x3) / p5 \) into a unique function identifier \( \exp_{bs\_pl\_pl\_p2\_ti\_x1\_pl\_p3\_ti\_x2\_pl\_p4\_ti\_x3\_be\_di\_p5} \). This identifier represents the exact mathematical function that can be used for multiple applications with different Data_Arrays and Parameters. The number of TFs contained in the source code is thereby reduced, and duplications of TFs are avoided. TFs support multiple operators such as scalar numeric expressions (e.g., \(*\), \(/\), \(+\), \(\log\), \(\ldots\)), trigonometric functions, relational operators (\(>\), \(=\), \(==\), \(\ldots\)), logical expressions, and constructs using if and where expressions (see Appendix Table E1). The resulting identifier is checked against existing identifiers in the source code.

#### 3.4.5 API for upscaling

For the upscaling step, two Coordinates sharing the same dimensions are compared. In Fig. 3, this step is for example performed when comparing each coordinate of PET_LAI_corr_factor with its predictors. There, dimensions \(x\), \(y\), and \(t\) all need to be scaled from a high to a low resolution. For each cell of the target grid, the underlying \(n\) source cells (subcells) are stored in an ids array, and their relative contributing area is stored in a weights array. These properties are contained in the type CoordUpscaler. They can be initialized from existing remapping weights stored in the NetCDF file format following the SCRIP convention (Jones, 2010). By default, first-order conservative remapping is used for weight calculation, and thus the integral of the values is preserved in the presence of missing values. Two-dimensional auxiliary coordinate variables are mapped using a simple algorithm that only checks that the cell center of the source cell is within the target cell boundaries and assigns equal weights to each source cell. In the future, more sophisticated remapping schemes for two-dimensional coordinate variables will be implemented.

The upscaling of a Data_Array is conducted through the wrapper type UpscaleHelper, which is also a property of the Data_Array type. It consists of a one-dimensional array pointing to the source coordinates sourceCoords and target coordinates targetCoords, as well as the upscale operator names for each target coordinate upscaleOperatorNames. The Upscaler type performs multiple checks on the source and target coordinates of Data_Array. If applicable, it transposes or broadcasts the Data_Array if the order of source and target coordinates does not match. Multiple CoordUpscaler instances can be combined with an aggregated CoordUpscaler object, effectively combining the weights and subcell IDs when the user specifies the same upscaling operator for multiple coordinates of the target grid. The upscaling operation is then executed separately for each group of target dimensions using the same upscaling operator. Again, the upscaling for the example Data_Array PET_LAI_corr_factor in Fig. 3 is conducted for dimensions \(x\), \(y\), and \(t\) consecutively and governed by the wrapper type UpscaleHelper. There are a number of standard upscaling operators, such as the minimum, maximum, or weighted generalized mean function, which employ the power parameter (see Appendix Table E2). Users can easily add another upscaling function to the source code as long as it effectively aggregates the variability of the subcells into one value (see Appendix Fig. D2).

### 3.5 New features of current MPR release

The current set of features encompasses the functionality of the previous version of MPR as used in the mHM source code (Samaniego et al., 2019). This implementation lacks...
some key features that are highlighted by a comparison of Fig. 1 with Fig. 1 in Kumar et al. (2013a). First, the new MPR library is modularized and refactored, and thus it does not depend on mHM and its integrated optimization algorithms. Second, the original mHM implementation required grids to be rectangular, and the target resolution was a multiple of the source resolution. Finally, predictors, TFs, upscaling operators, and target grids can now be freely chosen and recombined in an MPR configuration file. This allows users to generate a set of parameter fields without any restrictions. Previously, parameter fields were bound to mHM requirements, and their properties could only be altered through changing the source code and were accessible only after a model run through its restart files.

Furthermore, it allows for a modular and flexible configuration of parameter estimation without common preprocessing steps of the input files (resorting coordinates, renaming variables, adding missing meta-information, applying unit conversion, etc.). Use of MPR is easy and intuitive, especially in the formulation of TFs, defining new coordinate variables, and assigning them to variables. The initialization of coordinate variables can be performed dynamically depending on existing coordinate variables (e.g., by using its bounds). The user can freely and flexibly enter simple regression-based TFs in a semi-automatic manner. More sophisticated functions, such as artificial neural networks or support vector machines, can be easily coupled to the code. The same holds true for upscaling operators. We allowed MPR to be easily integrated in workflows (e.g., auto-calibration) or have an API called from an external code.

Coordinate variables can be split and combined, which enables users to set coordinate-dependent parameter values (e.g., for certain horizons along a soil profile). The order of coordinate variables for individual variables can be changed. MPR supports up to five-dimensional variables without restrictions on their kind. Different upscaling operators can be chosen for each coordinate to be upscaled. Intermediate variables can be reused for the creation of other variables, allowing the creation of complex graphs of parameter interdependencies. Parameters can also be reused for multiple TFs.

4 Applications of MPR

4.1 Verification of MPR against previous version in mHM

The core objective of the new MPR tool was to reproduce the same model behavior as the original implementation of MPR in the mesoscale hydrological model (mHM) (Samaniego et al., 2019), which we refer to as mHM-MPR here. The model description, its code modifications, and the MPR configuration can be found in Appendices B1 and C1.

The comparison of the new MPR tool coupled to mHM with mHM-MPR shows that they yield the same simulation results within a tolerance of 0.1 %, which can be attributed to floating point precision deviations after the conversion of the input file format from text files to NetCDF. In a default model configuration of the Moselle River basin in Central Europe, the coupled version reproduced the same model parameter arrays. Consequently, this leads to differences in the hydrograph of the basin outlet within $10^{-5} \text{m}^3 \text{s}^{-1}$, as compared to the previous implementation.

4.2 Reproducing the EU-SoilHydroGrids dataset with MPR

We selected the EU-SoilHydroGrids (SHG) dataset (Tóth et al., 2017) as it is relevant to the Earth system modeling community and is publicly available. The same holds true for its predictors and the TFs used. We reproduced the aforementioned dataset and showed the salient seamless spatial scaling feature of the MPR tool. The dataset description and its configuration can be found in Appendices B2 and C2 and the MPR configuration in the Supplement.
Figure 4 shows the spatial distribution of $K_s$ (soil-saturated hydraulic conductivity) on a logarithmic scale for different resolutions and data sources at a depth of 15 cm, with values ranging across 3 orders of magnitude from $10^{-6}$ to $10^{-3}$ m s$^{-1}$. Each row of the plot shows grids with the same spatial resolution, and each column shows the data sources and processing schemes.

The values were estimated using a decision tree with 21 leaves (Tóth et al., 2015, Table S1, model 16). When we attempted to reproduce the SHG values (Fig. 4a) with the recommended procedure in Tóth et al. (2015) using an R-library (Fig. 4b), we obtained a bias of up to 10% in comparison to Fig. 4a. An investigation of the SoilGrids version 1 meta-information (https://www.isric.org/explore/soilgrids, last access: 16 March 2019) revealed that the SoilGrids (SG) dataset is subject to frequent updates depending on the arrival of new source soil profiles. We could not verify the exact version of SG used to create the SHG, but we assume that it was different than the one we used. The high bias observed is a result of the decision tree, as small deviations in predictor values might result in use of a different branch. An additional source for the observed bias could be the projected coordinate system used for the SHG, in contrast to SG being available in the geographical WGS84 coordinate system.

When using MPR to apply the TFs to the SG dataset (Fig. 4c), we obtained a mean relative bias below 0.06% compared to Fig. 4b, which was only due to rounding errors of the global parameters. SHG and SG are also available at a 1 km resolution, where variables are aggregated using the Geospatial Data Abstraction Library (GDAL/OGR contributors, 2019) average method (Fig. 4d and e).

In accordance with the MPR framework, we derived the 1 km $K_s$ field by averaging the high-resolution SG data at 250 m (Fig. 4c). Because the selected TF is based on a decision tree algorithm, there exist only some discrete values in Fig. 4d and e, whereas spatial averaging increases the variability of the derived parameter field. The capability of MPR in flexible aggregation of the data is shown in Fig. 4g). A resolution of 25 km was arbitrarily selected as the target resolution, as specific resolutions (e.g., 1 km) are typically not needed by users. By merely changing a single number in the configuration file, it is possible to scale the variable at interest to every user-defined resolution. This analysis highlights the capability of MPR in reproduction of environmental parameters and generation of outputs that meet specific user requirements.

4.3 Application with land surface model Noah-MP

We used the land surface model (LSM) Noah-MP (Niu et al., 2011) as an example to showcase the capability of MPR in coupling with state-of-the-art distributed environmental models. The model description and configuration can be found in Appendices B3 and C3 and the MPR configuration in the Supplement. We found that the inherent parameter uncertainty that occurs when choosing a TF and an upsampling operator for the soil parameters of the model eventually leads to differences in long-term mean annual evapotranspiration (ET) flux, up to 20% (Fig. 5) in relation to its default setup.

Figure 5 shows the absolute values of the default model parameters $K_s$ [m s$^{-1}$] (log10-transformed) and $\theta_s$ [–] and the resulting long-term annual ET flux [mm yr$^{-1}$] in the first row (maps 1a–c). The following rows (2–4) show the relative differences (in %) of the field with respect to the default simulation in row 1. The relative differences observed when using the MPR approach with the same soil dataset, same TF, and subsequent spatial upsampling are shown in the second row (subplots 2a–c). Larger differences occur in regions with considerable subgrid heterogeneity in soil texture, where the hydraulic parameters associated with the mean textural information of the dominant class do not represent underlying variability. Absolute differences of more than 5% for both parameters occur in Florida, parts of Nebraska, and parts of the southwestern United States. The average difference is $-1.6\%$ and $-1.3\%$ for both parameter fields, and a greater variability can be found for $\theta_s$. The difference for the long-term ET flux is $-3\%$ on average, with pronounced low values of less than $-10\%$ in the aforementioned regions. The lower ET fluxes are due to the accumulated effects of lower porosity and lower hydraulic conductivity, which leads to decreased storage capacity and capability to meet evaporation water demands. It is important to keep in mind that these changes stem solely from using non-classified continuous soil textural information and aggregation of subgrid parameters, in contrast to using the dominant soil type. In other words, variation originates from different methods of handling sub-grid variability.

In the next step, we replaced the TF in MPR with another continuous TF based on the linear regression of the predictors of sand content, clay content, and organic matter (Saxton and Rawls, 2006) (maps 3a–c in Fig. 5). This TF is also available within Noah-MP version 4.0. This leads to $K_s$ values that are on average 4.7% higher than in the default setup. Application of the TF results in a decreased $\theta_s$ over the majority of the domain, with average values around $-8.6\%$. The ET fluxes exhibit a decrease for most of the CONUS in comparison to the default setup (on average $-4.0\%$ with maxima in the Appalachians of 18.4% and minima in Florida of $-27.3\%$).

Yet another spatial pattern of parameter values is produced by application of the TF of Vereecken et al. (1989) for $\theta_s$ and Vereecken et al. (1990) for $K_s$. TFs use the predictors of sand content, clay content, bulk density, and organic matter. While the overall relative differences in comparison to the default parameter distribution of $K_s$ are positive, there are negative differences of approximately $-25\%$ in the northwestern areas of the CONUS domain, in Florida, and along the US east coast between Louisiana and Virginia. An inverse signal can be observed for the parameter $\theta_s$. The overall decrease in ET that predominates in Texas, Florida, and the
northern Rocky Mountains highlights the nonlinear dependence of ET on the modified soil parameters as a new spatial pattern occurs. However, the results obtained must be assessed critically. Significant differences in parameter values in some areas indicate the limited applicability of the chosen TF. Indeed, high values of bulk density exist in parts of southern CONUS, and high organic matter contents are present in Oregon, Washington, and along the western coastline. The reported range of values (0.01 % to 6.6 % for organic matter content and 1.04 to 1.23 g cm$^{-3}$ for bulk density) upon which the regression for the TF was computed (Vereecken et al., 1989) is based on a small dataset of soil samples from Belgium. This does not cover the range of the values present in the chosen soil dataset (i.e., SG). The applicability of a given TF needs to be evaluated in the context of the utilized soil database (Wösten et al., 2001).

The model bias for a standard Noah-MP configuration in comparison to the reference product FLUXNET has been assessed in a previous study (Ma et al., 2017). They observed a spatial pattern in the long-term bias of ET in regards to prescribed leaf area index (LAI), which showed similarities to the spatial pattern in the long-term bias of ET in regards to prescribed leaf area index (LAI), which showed similarities to the pattern seen in Fig. 5 2c, 3c, and 4c. Although the setup of Noah-MP was not identical, MPR might serve as a valuable tool in addressing the problem of model bias through improved parameter estimation.

Cuntz et al. (2016) investigated parameter sensitivity in simulated fluxes by Noah-MP. They reported a strong sensitivity of ET on the soil parameters $\theta_s$ and $K_s$, which is in accordance to our findings shown in Fig. 5. One limitation in their results is that they directly investigated grid cell-specific parameters. As a result, the dimensionality of the parameter space linearly scales with the area of the model domain. Thus, only a few catchments using a spatially constant scale factor could be used. Using MPR, the number of TF parameters remains independent of the size of the model domain, which allowed us to conduct a more spatially comprehensive sensitivity analysis. At the same time, MPR requires TFs for every parameter, which indicates that the uncertainty due to the choice of TF cannot be neglected when conducting a sensitivity analysis. For example, MPR and Noah-MP can be executed subsequently by an optimization algorithm. The optimizers draw new parameter sets for MPR that result in updated soil parameter maps for Noah-MP. In turn, updated ET fields are calculated by Noah-MP.

4.4 Application with land surface model HITESSEL

We used the land surface model HITESSEL (Balsamo et al., 2009) as an example to showcase the capability of MPR in coupling with state-of-the-art distributed environmental models. HITESSEL is the land surface scheme used within the integrated forecasting system developed at the European Center for Medium-Range Weather Forecasts (ECMWF). The model description and its configuration can be found in Appendices B4 and C4 and the MPR configuration in the Supplement.

Similar to the application of Noah-MP (Fig. 5), we found differences in the long-term evapotranspiration (ET) flux of up to 15 % over the Mississippi River basin (Fig. 6) when using different transfer functions to compute soil hydraulic properties.

Figure 6 is organized in the same way as Fig. 5. In its default configuration based on SoilGrids (SG), there exist only five different soil classes over the entire domain. Through a lookup table, each class is assigned the values for the van Genuchten model (Genuchten, 1980) of the hydraulic conductivity curve (Eq. 1) and moisture retention curve (Eq. 2): $K_s$, $\theta_r$, $\theta_s$, $n$, $l$, $\alpha$, and $\theta_s$. It is worth mentioning that this lookup table was originally derived for the FAO 2003 soil map (CBL, 2007).

\[
\gamma = K_s \left[ \frac{(1 + (\alpha h)^n)^{1-1/n} - (\alpha h)^{n-1}}{(1 + (\alpha h)^n)^{1-1/n}(l+2)} \right],
\]  

\[
\theta(h) = \theta_r + \frac{\theta_s - \theta_r}{(1 + (\alpha h)^n)^{1-1/n}}.
\]  

The most common values are 1.16e-6 m s$^{-1}$ and 0.439 % for $K_s$ and $\theta_s$, respectively. These values correspond to the medium soil texture class in the lookup table. High $K_s$ values (up to 4.6e-5 m s$^{-1}$) can be found in Missouri, Kansas, and the Nebraska Sandhills. Occurrences of high $\theta_s$ values of 0.52 (fine texture) can be found in Missouri and Kansas. Notably, both parameter maps show the distribution of only two out of the six soil hydraulic parameters. This parameter selection is a dominant part of all soil hydraulic properties that are relevant for simulated ET. However, it is not sufficient to show the highly nonlinear relationship between soil hydraulic properties (i.e., hydraulic conductivity curves and moisture retention curve) and simulated ET at every location. Long-term ET values increase from 250 to 1450 mm per year along a gradient from the northwest to the southeast of the domain (Fig. 61c). We selected two sets of TFs from the literature to calculate soil hydraulic properties (Zacharias and Wessolek, 2007; Wösten et al., 2001). These TFs are applied to SG and can easily be implemented in MPR. After application of TF 2 (Zacharias and Wessolek, 2007), the parameter values $\theta_s$ are reduced by about $-9.0$ % (Fig. 6.2b). The highest differences occur again in Missouri and Kansas (around $-30$ % to $-47$ % for $\theta_s$). This TF does not contain $K_s$ and the default $K_s$ values are thus used. The change in $\theta_s$ reduces long-term ET flux by about $-5.0$ % (Fig. 6.2c). This can be expected because soil moisture storage (i.e., porosity) is generally reduced (Fig. 6.2b). In turn, the amount of water available for plant transpiration is limited. The use of TF 3 (Wösten et al., 2001) for the estimation of $K_s$ and $\theta_s$ reduces parameter values by approximately $-6$ % for $K_s$ and $-7$ % for $\theta_s$ on average over the entire domain. Applying TF 3 reduces porosity (Fig. 6.3b) in a similar order of magnitude.
Figure 5. Grid plot showing maps of parameters and simulation results for Noah-MP. Columns denote the following parameters and variables: (a) soil parameter $K_s$ (saturated hydraulic conductivity) at the soil horizon between 0.1 and 0.3 m, (b) soil parameter $\theta_s$ (maximum soil moisture content) at the soil horizon between 0.1 and 0.3 m, and (c) mean annual evapotranspiration values of Noah-MP. Rows denote the following configurations: row (1) shows the standard Noah-MP setup using the dominant USDA soil class based on SoilGrids (Hengl et al., 2017) and a lookup table based on the TF from Cosby et al. (1984), and rows (2)–(4) show the relative differences ((MPR − default) / default) in percentage of parameters and simulation results using an MPR setup with a TF from Cosby et al. (1984), Saxton and Rawls (2006), and Vereecken et al. (1989, 1990), respectively.

compared to TF 2. Additionally, saturated hydraulic conductivity is reduced at most by 16% resulting in reduced ET in comparison to the default setup (Fig. 6.3c). This reduction is not as strong as that of TF 2 because the reduced $K_s$ values increase the water holding capacity of the soil.

By producing continuous fields of parameter values with MPR, increased (decreased) $K_s$ values are found in regions with low (high) default values. Similarly, the highest reductions of $\theta_s$ are found in regions with the highest default values. This highlights that the MPR-derived fields reduce the amplitude of the parameter values but substantially increase the spatial variability. MPR-derived fields make more use of the spatial information of the soil dataset and lead to more realistic spatial parameter fields. It is worth mentioning that the spatial patterns for changes in ET do not correspond to either changes in parameter fields or the spatial pattern of the default ET values. This indicates the complex interplay between ET and soil hydraulic properties and calls for a deeper analysis of all MPR-derived soil parameters (i.e., also $\alpha$, $n$, $l$, $\theta_r$, etc.).
Figure 6. Maps of parameters and simulation results for HETESSEL. Columns denote the following parameters and variables: (a) soil parameter $K_s$ (saturated hydraulic conductivity) at the soil horizon between 0.07 and 0.28 m, (b) soil parameter $\theta_s$ (maximum soil moisture content) at the soil horizon between 0.07 and 0.28 m, and (c) mean annual evapotranspiration (ET) values of HETESSEL. Rows denote the following configurations: row (1) shows the standard HETESSEL setup using the dominant soil classes based on the SoilGrids dataset (Hengl et al., 2017) and lookup table based on the TF from (Balsamo et al., 2009), and rows (2)–(3) show the relative differences ((MPR − default)/default) of parameters and simulation results using MPR based on SoilGrids (Hengl et al., 2017) with TFs from Zacharias and Wessolek (2007) (TF2) and Wösten et al. (2001) (TF3), respectively.

4.4.1 Differences between HETESSEL and Noah-MP over the Mississippi River basin

This section compares the effect of similar changes in soil parameters on long-term model outputs for both models presented in the previous sections. While it does not provide a rigorous model intercomparison, it puts the results into context and provides a template for future studies that can use MPR to systematically assess differences in parameters and parameterizations across models.

There are several differences between the simulations conducted with Noah-MP and HETESSEL that go beyond the fact that these two are based on different mathematical models. First, the default simulations compute different amounts of long-term ET (compare 1c in Figs. 5 and 6). Both maps exhibit a similar spatial pattern, but the long-term ET flux for HETESSEL is approximately 20\% higher than that of Noah-MP. This might be due to the use of different forcing datasets NLDAS2 (Xia and NCEP/EMC, 2009) and ERA5 (ECMWF, 2019) for Noah-MP and HETESSEL, respectively. Xu et al. (2019) and Saxe et al. (2020) suggest mean precipitation of ERA5 is higher than in NLDAS2 in the study domain.

Second, the default soil hydraulic parameters show a different spatial pattern (compare panels 1a and 1b in Figs. 5 and 6). The default setup uses a lookup table with a limited number of soil classes based on the TFs from Cosby et al. (1984) for Noah-MP and HYPRES (1997) for HETESSEL. The estimation of the effective soil class follows the dominant class approach, which leads to a limited spatial variability of soil hydraulic properties for both models. It is worth mentioning that both lookup tables were derived for other soil maps than the one used in this study (for example, CBL (2007) for HETESSEL). Here, we applied both default lookup tables to the same dataset (SG) to rule out differences coming from different soil maps. While a decreased spatial variability, especially for HETESSEL, with only five active soil texture classes is found, the Cosby TF leads to a more consistent spatial pattern for Noah-MP. In addition to the spatial pat-
tern, the parameter values themselves are also different for both models. $\theta_s$ for Noah-MP varies around 0.46, and HTESSEL again shows slightly lower values of approximately 0.44. $K_s$ is on average around 2.5e-6 m s$^{-1}$ for Noah-MP and much lower with 1.16e-6 for HTESSEL. These striking differences are in agreement with Samaniego et al. (2017), where a more exhaustive model comparison was performed. This study again highlights the need for a common protocol to assess parameter uncertainty in distributed models.

Third, using other TFs than the default ones leads to reductions in long-term ET that are less than 10% in magnitude for both models (compare the right columns in Figs. 5 and 6). A similar magnitude of influence by varied soil parameters on ET has been reported previously by Livneh et al. (2015) for mHM in the Mississippi River basin. There is no consistent pattern between models in regard to where these changes manifest themselves. An example for that are the Nebraska Sandhills. While ET is generally increased by TFs in HTESSEL in this region, the opposite is the case in Noah-MP. Direct interpretation of the interplay of soil parameters in the soil water hydraulics is easier with Noah-MP due to the simpler mathematical model for soil hydraulic parameterization. Noah-MP uses the Campbell parameterization to relate hydraulic conductivity to soil saturation (Campbell, 1974). In contrast, HTESSEL uses Mualem–van Genuchten parameterization (Genuchten, 1980), which leads to complex changes in moisture retention curves and hydraulic conductivity curves that are highly nonlinearly impacted by changes in model parameters (not all of them are shown here). Notably, models react to changes in (a limited number of) model parameters for the case of ET fluxes investigated here. Larger changes can be found for other fluxes of the water cycle and sub-annual timescales (not shown).

In spite of demonstrated differences in model forcing, configuration, and process parameterization, MPR-derived parameter fields significantly changed long-term model output. The harmonization and reproducibility of parameter estimation across models through MPR opens up an avenue to a deeper understanding of the relationship between predictors, parameters, and model parameterization.

4.5 Limitations and outlook

MPR was tested with compiler GNU Gfortran versions > 7.3, the NAG Fortran Compiler version > 6.2, and Intel ifort version > 18. These compiler configurations are tested continuously. We will invest further effort into developing MPR so that scalability on high-performance computers (HPCs) and parallelization is improved. A hybrid MPI and Open-MP parallelization will be applied. The need for support of advanced and massively parallel regridding and interpolation capabilities will likely lead to the integration of one of the existing remapping libraries used in GCM couplers in an upcoming version of MPR. The coupling of MPR to the LSM HTESSEL by extraction of hard-coded and hidden parameters and the development of TFs in an ongoing project will likely serve as a template that can be adapted for other models.

5 Conclusions

Parameter regionalization enables the creation of seamless parameter fields for complex distributed models that can otherwise only be inferred through calibration or by default values that are often obtained at inappropriate scales (Samaniego et al., 2017). MPR is a framework that regionalizes parameters through the application of transfer functions and aggregations to any spatiotemporal coordinate system. In this study, we introduced a complete rewrite of the MPR framework (Samaniego et al., 2010; Kumar et al., 2013b) to overcome the limitations of previous implementations and comparable software (for example, Mizukami et al., 2017). MPR is able to introduce new flexibility to mHM and other models accepting distributed parameters through the support of multiple grid structures and a more flexible configuration of the parameter estimation process. It is capable of reproducing effective parameter fields (Tóth et al., 2017) by applying transfer functions (Tóth et al., 2015), while also being able to remap and upscale the parameters onto every modeling unit (rectangular grids, HRUs, arbitrary shapes) required by the model. We demonstrated that parameter estimation not only exerts a strong influence on effective model parameter fields but also results in modified evapotranspiration simulated by land surface models, even when MPR is applied to only two sensitive parameters. The same holds true for models that use a tiling approach for handling subgrid heterogeneity.

The superiority of the MPR approach toward standard parameter estimation approaches was first demonstrated by Samaniego et al. (2010); Kumar et al. (2013b); Samaniego et al. (2017) and is now available for use with many other models. This is possible because MPR is designed to flexibly, modular, and as easy to use as possible. We provide an API that users can easily modify and that can be successfully tightly coupled to the hydrologic model mHM. As such, we invite implementation of further transfer functions (TFs) and upscaling operators in other distributed modeling code. MPR provides a way forward in addressing many current challenges regarding the estimation of distributed parameter fields in the Earth system model community (as postulated by Van Looy et al., 2017), such as coupled parameterizations and TF validation in large-scale applications. It serves as a protocol for systematic development of new TFs and aggregation schemes or upscaling approaches. As such, it makes the whole process of parameter estimation transparent and reproducible. It can easily produce time- or process-dependent parameters (e.g., tillage systems, swell or shrink behavior of clay minerals). MPR can also be used to combine multiple predictors to obtain new TFs (e.g., soil and land use.
predictors for plant root parameters or topology and climate for snow parameters). Most importantly, MPR enables users to specifically consider multiple commonly neglected uncertainty sources inherent in the geophysical data, TF, and up-scaling functions. It is valuable for large-scale environmental models, where there is a current lack of effective parameter estimation, sensitivity analysis, and calibration (Beck et al., 2016).

Appendix A: Data processing

A1 Processing of input data for minimal working example

1. Download the data from the server (https://files.isric.org/soilgrids/former/2017-03-10/data/, last access: 16 January 2022; please note that the use of this data source is discouraged by the data providers as a newer version of SoilGrids is available), with the bulk density (fine earth), clay content, sand content, and soil organic carbon content (fine earth fraction) for all available soil depths at the original resolution of 250 m.

2. Transform the data from the tiff to the NetCDF format, clip the selected domain, and merge the different layers into one file per variable (script in annex).

3. Download the target grids (e.g., for the ICON model (Zängl et al., 2015) grids, refer to http://icon-downloads.mpimet.mpg.de/mpim_grids.xml, last access: 16 January 2022) following the SCRIP convention (Jones, 2010) for storing grids in the NetCDF format.

4. Select an example TF from the literature (e.g., Weynants et al., 2009).

5. Construct a configuration file mpr.nml for MPR in the native Fortran namelist format (Fig. 2).

Appendix B: Model descriptions

B1 mHM

mHM conceptualizes the dominant hydrological processes on the land surface through multiple reservoirs. The processes of canopy interception, snow accumulation and melting, water infiltration into the soil and percolation to the groundwater, evaporation and transpiration, runoff generation, and river routing are accounted for on a spatially explicit grid. The model has been applied in a wide range of applications and has been shown to be able to fulfill the flux-matching criterion over multiple scales (Samaniego et al., 2017).

B2 SoilHydroGrids

An increasing number of publications on high-resolution land surface datasets has led to the development of derivative datasets providing model parameters. Usually these datasets are available for a fixed resolution and domain only. Here, we demonstrate how MPR can be used to apply the TFs and remap the result on the domain and resolution as required. MPR is capable of reproducing the EU-SoilHydroGrids dataset (SHG) (Tóth et al., 2017) at a given 250 m and 1 km resolution.

B3 Noah-MP

Noah-MP simulates the terrestrial water, energy, and carbon budget and estimates fluxes between various storage components in the biosphere, lithosphere, and hydrosphere. Its predecessor Noah (Ek et al., 2003) was superseded by Noah-MP by implementing multi-parameterization options and improved physics for various ecohydrological processes. For each grid cell, the vertical model structure was discretized into one canopy layer using a semi-tile approach, three snow layers, four soil layers, and an unconfined subsurface layer.

B4 HTESSEL

HTESSEL calculates water, energy, and carbon fluxes and storage across the land surface and uses a tiling approach to represent different land covers within one model grid cell. It uses 20 plant functional types to describe vegetation and constant soil properties throughout the soil column. The soil has a standard depth up to 2.89 m.

Appendix C: Model configuration for application

C1 mHM

MPR is required in order to reproduce the model parameters created by the internal version of MPR in mHM version 5.10 (Samaniego et al., 2019) and consequently the same model results. The fact that mHM incorporates various auto-calibration approaches that need control over the parameter estimation process necessitates a tight coupling of mHM to MPR in Fortran. We configured MPR to represent the complex interplay of model parameters. The configuration for mHM encompassed the use of over 100 different Data_Array instances with over 60 TFs (see the configuration in the Supplement). The mHM code was refactored and adapted to allow for the passing of global parameters from mHM to MPR and to allow the effective parameter fields to be received.

C2 SoilHydroGrids

SoilHydroGrids is based on the SG dataset (Hengl et al., 2017) at 250 m and an aggregated 1 km resolution. Linear
functions and decision tree-based functions were used for the TFs (Tóth et al., 2015). A collection of relevant soil hydraulic parameters for the European domain are provided in SHG. We selected the subdomain of the Netherlands for the parameter saturated hydraulic conductivity, as it shows a large degree of variability in this region. The MPR configuration file is attached in the Supplement.

C3 Noah-MP

We use the default WRF-Hydro parameterization process (version 3.6) at NCAR (2020), except for the radiative transfer option where a modified two-stream option was used. Meteorological model forcings were taken from the NLDAS-2 dataset (Xia and NCEP/EMC, 2009). The 1/8° spatial resolution and hourly temporal resolution of the forcing variables (air temperature, precipitation, specific humidity, wind speed, surface pressure, downward shortwave radiation, and downward longwave radiation) also constitute the chosen model resolution for Noah-MP. The SG dataset (Hengl et al., 2017) was used to estimate soil parameters, whereas the MODIS-IGBP (Friedl et al., 2010) dataset was used to derive vegetation parameters. In the default setup, soil textural data was averaged over the soil column and classified into 12 classes using the Staff (1993) scheme. Finally, the dominant type within a model grid cell was used. The exact parameters were then derived from class-specific default values provided in the lookup tables. These default values were derived by applying a set of TFs (Cosby et al., 1984) to the mean textural properties of the respective soil class. Vegetation parameters were also estimated based on the default values for each effective land cover class. The Noah-MP model version 3.9 was used and slightly modified to explicitly allow for two specific spatially distributed model parameters to be read. We used the default soil layering of horizon boundaries at depths of 0.1, 0.4, 1.0, and 2.0 m.

In addition to this default setup, we used MPR to estimate the soil parameters SATDK (soil-saturated hydraulic conductivity) and MAXSMC (maximum soil moisture content). Noah-MP shows a substantial sensitivity to both of these parameters along a gradient of hydro-climate conditions in the CONUS (Cuntz et al., 2016). The two parameters were estimated directly on a high-resolution soil dataset using the following continuous TFs: TF 1 (Cosby et al., 1984), TF 2 (Saxton and Rawls, 2006), and TF 3 (Vereecken et al., 1989, 1990). TF 1 is used in Noah-MP as a default option, TF 2 was later introduced as an option in Noah-MP version 4.0, and TF 3 was chosen in this study to demonstrate the effect of a TF based on soil samples from outside the study domain. The arithmetic mean was used to upscale the parameters to the model resolution, except for the vertical scaling of $K_s$ along the soil horizons for which the harmonic mean was used. The parameters REFSMC (soil moisture content at field capacity) and WLTSMC (soil moisture content at wilting point) were rescaled by the ratio of the default and modified $\theta_s$ values ($\theta_{s, \text{ref}} = \theta_{s, \text{ref}} \cdot \theta_s^{\prime}/\theta_s$).

The Noah-MP model was run for 28 years at an hourly time step from 1980 to 2007. We allowed the model to run for an entire period and used the resulting state variables as initial conditions for the final run. The final evaluation period covered the decade 1991–2000. The hourly simulation results were aggregated to mean annual values.

C4 HITESSEL

Meteorological forcing data were taken from the ERA5 dataset (ECMWF, 2019). The 1/4° spatial resolution and 3-hourly temporal resolution of the forcing variables (air temperature, precipitation (rain and snow), specific humidity, wind speed, surface pressure, downward shortwave radiation, and downward longwave radiation) also constitute the chosen model resolution for HITESSEL.

We used a process parameterization based on the default configuration presented in the development branch CY47R1 of HITESSEL (nemk_CY47R1.0_v6b_cmfdmr_mpr). In addition to this default setup, we used MPR to estimate the six soil parameters of the Mualem–van Genuchten model for the hydraulic conductivity curve (Eq. 1) and soil moisture retention curve (Eq. 2). These parameters were estimated directly on the SG dataset (Hengl et al., 2017) using the following TFs: categorical TF 1 based on lookup table values (HYPRES, 1997), continuous TF 2 (Zacharias and Wösten, 2007) with the estimation of only the four parameters of Eq. (2), and continuous TF 3 (Wösten et al., 2001). Soil textural data were averaged over the soil column for TF 1 and classified into 7 classes using the HYPRES soil texture triangle (HYPRES, 1997; Wösten et al., 1999) with some additions for organic soils. Finally, the dominant type within a model grid cell was used. The exact parameters were then derived from class-specific default values provided in the lookup tables. TF 1 is used in HITESSEL as the default option. The arithmetic mean was used to upscale the parameters to the model resolution, except for the vertical scaling of $K_s$ along the soil horizons, for which the harmonic mean was used.

The HITESSEL model version CY47R1 was used and modified to explicitly allow for the reading of spatially distributed model parameters. We used the default soil layering of horizon boundaries at depths of 0.07, 0.28, 1.0, 2.0, and 2.89 m. Due to limitations in the HITESSEL solver for the soil physics processes, we enforced vertically homogeneous soil parameters.

The HITESSEL model was run for 8 years at a daily time step from 1979 to 1986. We allowed the model to run for an entire period and used the resulting state variables as initial conditions for the final run. The final evaluation period covered the years 1979 to 1986. The 3-hourly simulation results were aggregated to mean annual values.
Appendix D: Templates for user-defined functions

```fortran
abstract interface
  function transfer_func_alias(x, param) result(func_result)
    ! import the double precision kind specification and custom
type
import dp, InputFieldContainer
!> an array containing the predictor variables (access values
through 'data_p' property)
type(InputFieldContainer), intent(in) :: x(:)
!> an array containing the TF parameters
real(dp), intent(in) :: param(:)
!> the resulting TF result
real(dp), allocatable :: func_result(:)
!! allocate the func_result to the size of the predictors
(all have the same size)
allocate(func_result(size(x(1)$/data_p)))
!! enter the TF function here
func_result = x(1)$/data_p + x(2)$/data_p * param(1)
end function transfer_func_alias
end interface
```

Figure D1. Template for user-defined TFs as an abstract interface.

```fortran
abstract interface
  real(dp) function upscale_func_alias(array, weights, p)
! import the double precision kind specification
import dp
!> the array of subgrid values (no missing values)
real(dp), dimension(:), intent(in) :: array
!> the array of weights (same shape as array)
real(dp), dimension(:), intent(in), optional :: weights
!> an optional parameter passed to the function (power mean)
real(dp), intent(in), optional :: p
end function upscale_func_alias
end interface
```

Figure D2. Template for user-defined upscale operators as an abstract interface.
Appendix E: Inventory of operators in transfer functions and for upscaling

Table E1. Table of operators that can be specified in a string for the property transfer_func in the configuration file mpr.nml. They are directly parsed to the Fortran code.

| Operator | Type          | Description |
|----------|---------------|-------------|
| +        | binary operator | --          |
| -        | binary operator | --          |
| **       | binary operator | --          |
| /        | binary operator | --          |
| max      | binary operator | --          |
| min      | binary operator | --          |
| exp      | unary operator  | --          |
| sqrt     | unary operator  | --          |
| log10    | unary operator  | --          |
| log      | unary operator  | --          |
| abs      | unary operator  | --          |
| (        | delimiter      | --          |
| )        | delimiter      | --          |
| if       | conditional statement | --          |
| else     | conditional statement | --          |
| then     | conditional statement | --          |
| where    | conditional statement | --          |
| end      | conditional statement | --          |
| <=       | relation operator | --          |
| <        | relation operator | --          |
| >=       | relation operator | --          |
| >        | relation operator | --          |
| ==       | relation operator | --          |
| .and.    | logic notation  | --          |
| .or.     | logic notation  | --          |
| .not.    | logic notation  | --          |
| sin      | trigonometric function | --          |
| cos      | trigonometric function | --          |
| tan      | trigonometric function | --          |
| tanh     | trigonometric function | --          |
| acos     | trigonometric function | --          |
| asin     | trigonometric function | --          |
| atan     | trigonometric function | --          |
| atan2    | trigonometric function | --          |
| cosh     | trigonometric function | --          |
| sinh     | trigonometric function | --          |

Table E2. Table of operators that can be specified in a string for the property upscale_ops in the configuration file mpr.nml. The values $x$ of the array with size $n$ (with indices $i$) are passed to the operator with weights $w$ of the same size.

| Operator | Equation                              | Description                  |
|----------|--------------------------------------|------------------------------|
| p, p = 0 | $\prod_{i=1}^{n} x_i^{w_i}$          | geometric mean               |
| $p, p \in \mathbb{R}$ | $\left( \sum_{i=1}^{n} x_i^{p \cdot w_i} \right)^{\frac{1}{p}}$ | power mean                   |
| min      | $\min \{x_i\}$                      | minimum                      |
| max      | $\max \{x_i\}$                      | maximum                      |
| sum      | $\sum_{i=1}^{n} x_i$                 | sum                          |
| var      | $\sum_{i=1}^{n} w_i (x_i - \bar{x})^2$ | variance                     |
| std      | $\sqrt{\sum_{i=1}^{n} w_i (x_i - \bar{x})^2}$ | standard deviation          |
| laf      | $\min\{x_i \mid j \in 1, \ldots, |x| \}$ : largest area fraction |
|          | $\forall i : w_i \leq w_j$          |                              |

**Code availability.** The MPR software (Schweppe et al., 2021) is publicly available and the code development can be found at https://git.ufz.de/chs/MPR/ (last access: 16 January 2022). The code is published under the GNU GPLv3 license. The code can be compiled by any recent Fortran compiler supporting the Fortran2008 standard and needs the netcdf-fortran library. In order to automatically add TFs to the code with a preprocessing script, the Python library f90nml (Ward et al., 2021) must be installed. The documentation framework for (MacMackin, 2018) is used to create the documentation (Schweppe et al., 2021), which hosts a tutorial, documentation, and extensive overview of the source code.

**Data availability.** We used the following third-party datasets: SoilGrids1km (Hengl et al., 2014), originally downloaded from: ftp://ftp.soilgrid.org/data/recent/, last access: 25 July 2018, it now is partly available under https://files.isric.org/soilgrids/former/2017-03-10/data/, last access: 16 January 2022 (https://doi.org/10.1371/journal.pone.0105992), SoilGrids250m (Hengl et al., 2017), originally downloaded from: ftp://ftp.soilgrid.org/data/recent/, last access: 25 July 2018, it is now partly available under https://files.isric.org/soilgrids/former/2017-03-10/data/, last access: 16 January 2022 (https://doi.org/10.1371/journal.pone.0169748), EU-SoilHydroGrids (Tóth et al., 2017), MODIS-IGBP (Friedl et al., 2010), NLDAS-2 forcing dataset (Xia and NCEP/EMC, 2009), and the ERA5 forcing dataset (ECMWF, 2019, https://doi.org/10.24381/cds.bd0915c6).

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