Selective AP-sequence Based Indoor Localization without Site Survey

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Abstract—In this paper, we propose an indoor localization system employing ordered sequence of access points (APs) based on received signal strength (RSS). Unlike existing indoor localization systems, our approach does not require any time-consuming and laborious site survey phase to characterize the radio signals in the environment. To be precise, we construct the fingerprint map by cutting the layouts of the interested area into regions with only the knowledge of positions of APs. This can be done offline within a second and has a potential for practical use. The localization is then achieved by matching the ordered AP-sequence to the ones in the fingerprint map. Different from traditional fingerprinting that employing all APs information, we use only selected APs to perform localization, due to the fact that, without site survey, the possibility of obtaining the correct AP sequence is lower if it involves more APs. Experimental results show that, the proposed system achieves localization accuracy below 10 m with an accumulative density function (CDF) of 50% to 60% depending on the density of APs. Furthermore, we observe that, using all APs for localization might not achieve the best localization accuracy, e.g. in our case, 4 APs out of total 7 APs achieves the best performance. In practice, the number of APs used to perform localization should be a design parameter based on the placement of APs.

I. INTRODUCTION

Over the decades, there is an increasing interest in indoor localization due to the rapid growth of location-aware applications requesting room-level localization services. Wifi-based localization systems have been shown to be successful in different scenarios, with a state-of-art Wifi-based localization system being reported in the literature to achieve localization accuracy below 10 m [1]. The indoor localization systems can be classified into two categories, the model-based approach [2] and the fingerprinting-based approach [3] [4]. The model-based approach has to rely on a model to characterize the propagation of radio signals. In contrast, fingerprinting-based approach utilizing site survey of RSS in the area of interest achieves better localization accuracy, since it uses a database in which the impact of environments has been underlined in the construction of the database.

Unfortunately, there are some drawbacks in the traditional fingerprinting-based approaches, e.g. time consuming and labor intensive site survey to construct and update the fingerprint map [2] [3]. To overcome this problem, we propose an approach to avoid the laborious phase to collect measurements in environments. In particular, we construct the fingerprint map by cutting the layouts of the interested area into regions with the knowledge of positions of access points. The resulting fingerprint map is in essence a set of small connecting regions, obtained by cutting the lines connecting APs in the interested area in the middle without laborious site survey. This is equivalent to assuming a radio propagation model universal to all environments. The resulting fingerprint map can be easily constructed, with only the knowledge of locations of APs but regardless of the layout of interested area. Each region is then associated to an unique ordered sequence of APs (location signature). As a consequence, the proposed system can be deployed rapidly, while ensuring satisfactory localization accuracy competitive to existing systems. The proposed system might be applied to scenarios where the on-site data collection is not possible, for example disaster areas.

With this fingerprint map, the location signature is represented by an ordered sequence of APs according to RSS. In this case, we utilize the relative RSS among APs rather than the absolute RSS of each AP. Note that, although we classify our new system as fingerprinting-based approach, unlike existing fingerprinting-based approaches, it does not require any time-consuming site survey phase. The overwhelming overhead in constructing and updating the fingerprint map are also considerably reduced due to the less number of reference positions needed to characterize the fingerprint map.

However, when AP-sequence is used as location signature, with increasing number of APs involved in localization, the probability to have a correct measured signature decreases (since no site survey is performed), and resulting in matching against a wrong signature in the map and thus a wrong reference position. We therefore argue that the AP-sequence localization system based on employing RSS from all present transmitters might not be efficient. Motivated by this observation, in our proposed system, the location signature is represented by selected APs rather than all the available APs in the range. The rationale behind is that with less number of RSS, higher probability to obtain a correct measured signature is expected. Specifically, we propose a K-means based algorithm to efficiently select APs out of the total available APs for localization.

The rest of the paper is organized as follows. The system model underlined is presented in Sect. II. The proposed method to perform location estimation is illustrated in Sect. III. Experiments to evaluate the performance of the proposed system is carried out in Sect. IV. Last, we conclude this paper in Sect. V.

II. SYSTEM MODEL

Assume an indoor environment with windows, partitions, furniture, and equipments. Users equipped with Wifi receivers are able to scan APs in the proximity and measure RSS. The
locations of APs are assumed to be known as a prior. This is reasonable since in many commercial and industrial buildings, the AP locations are predetermined to optimize the network coverage and link quality. In case where the AP locations are not known, there are many reported ways to effectively locate the APs in practice [6].

Our fingerprinting-based localization system essentially consists of two phases. First, we obtain the offline fingerprint map consisting of multiple maps, each of which is constructed by using a combination set of APs used for localization. In total, there will be $C^n_k$ fingerprint maps, assuming we have $n$ APs in the environments, and $k$ APs are chosen for localization. Second, the user measures RSS from APs in the range and forms the measured location signature, then queries the corresponding fingerprint map to retrieve its location information by employing a matching method.

During the first phase (see Fig. 1), we construct the fingerprint map by partitioning the environment into a set of regions, with each associated with a location signature. The traditional fingerprinting-based approach requires a laborious site survey phase to collect the radio signals in environments. In contrast, in this paper, by assuming a universal propagation model of AP, a region associated with a location signature is equivalent to a sub-area enclosed by cutting the lines connecting the APs in the middle, given the positions of APs.

During the second phase, i.e., online localization, the location signature is represented by an ordered AP sequence based on RSS. As an example, assume the number of available APs is $M$, the RSS of the $m^{th}$ AP is denoted as $S_m$. Arranging the RSS of all the $M$ APs in descending order, for example $(S_1, S_3, S_M, \cdots, S_5)$, the corresponding location signature will be given as $(1, 3, M, \cdots, 5)$.

Note that, although there might be many APs available in the WiFi network, only a subset of available APs are used for localization. This is because more APs involved in the localization leads to a lower probability to obtain a matched fingerprint, as shown in Fig. 2. This figure shows the variations of the signal strength from APs during a certain time at one test point. The correct AP sequence at this test point should be 3672154. In fact, due to many influencing factors from the environment, the measured AP sequence is often wrong, as can be seen from Fig. 2(a). Furthermore, we can observe that the probability to get a right fingerprint using four APs is much higher than using all APs (i.e., seven APs). This is why we propose to use selective-AP sequence to improve the probability to obtain a right signature. The subset of APs used is dynamically determined based on the measured RSS, and varies from position to position. An algorithm based on the K-means clustering will be employed for efficient and tractable selection of APs [5], with details shown in Section III-B. And the selected AP sequence will then match with the fingerprint map generated using the same set of APs.

### III. Localization Method

The localization system proposed in this paper uses the relative RSS rather than the absolute RSS for localization and has two stages, offline construction of fingerprint map and online localization, as shown in Fig. 1. Particularly, the offline stage neither needs any laborious site survey phase to collect the measurements nor requires any mathematical or analytical model to characterize the propagation of the radio signals. The resulting fingerprint map is comprised of multiple fingerprint maps, which are constructed by various combination sets of APs. In the online stage, a subset of APs is selected based on K-means clustering and a location signature based on RSS measurements is obtained. The measured location signature is then matched against the location signatures in the corresponding fingerprint map (e.g., if AP 124 is selected, then the AP sequence will match to the fingerprint map generated by AP 124) and the position information is obtained.

#### A. Offline Construction of Fingerprint Map

The fingerprint map is constructed by partitioning the interested area into a set of regions, with each associated with a location signature. Conventionally, the construction of fingerprint map requires offline site survey, involving measuring radio signals in every position in the environment. In contrast, in this paper, by adopting the ordered AP sequence based on RSS and assuming a universal propagation model for all
environments, a region associated with a location signature is equivalent to a sub-area enclosed by cutting the lines connecting the APs in the middle, given the locations of APs but without any site survey. The shape of each region depends on the displacements of the selected APs for localization.

It is expected that, the number of regions obtained depends on the number and the placement of APs. Typical fingerprint maps with 4 and 3 APs are given in Fig. 3(a) where the locations of the APs are shown by ○ for the \( n \)th AP, while the location signatures of different regions are denoted by ordered sets of APs, for example, \( n_1n_2n_3 \) and \( n_1n_2n_3n_4 \), with \( n_1, n_2, n_3, n_4 \) being the APs whose RSS arranged in descending order, e.g. \( RSS_{n_1} > RSS_{n_2} > RSS_{n_3} > RSS_{n_4} \). It can be seen that, with more APs involved, more regions are obtained, for example, 12 regions in Fig. 3(a) and 6 regions for Fig. 3(d).

Although we only show the maps of several sets of selected APs as examples, given the number of available APs in the network to perform localization, there will be multiple fingerprint maps for all possible combination sets of APs. Note that in this stage, the fingerprint maps for all possible combinations of APs are constructed. In the localization stage, the APs used to perform localization are selected dynamically using the K-means algorithm.

Given the fingerprint map, the localization accuracy of each region is computed as the average distance between all positions and the center of the region. Theoretically, higher localization accuracy can be achieved with more APs involved in localization.

In practice, the measured location signature might not be correct, for example, as shown in Fig. 2(a) the correct location signature is (3, 6, 7, 2, 1, 5, 4) while the measured location signature is (3, 6, 1, 7, 2, 4, 5) at \( t = 100s \). So if we use all APs for localization, the theoretical accuracy we can achieve is the best, but with high chance to make mistake. But if we use only 4 APs, then the accuracy is lower, but with higher chance to make it correct. Therefore, in practice, AP-sequence localization with less selected APs may offer better accuracy in the absence of site survey than using all AP for sequencing.

**B. Online Localization**

The online localization is performed in three steps, 1) clustering APs based on their RSS by employing K-means clustering algorithm, 2) selecting one AP from each K-means cluster and forming the selected APs for localization, and 3) position estimation. The Step 1 and Step 2 are shown in Fig. 4.

1) Clustering by K-means: The K-means algorithm is a qualitative way to partition a group of data into a certain number of clusters (K clusters). In general, given a set of data \( x \) with Q data points \( x = \{x_q, q = 1, \ldots, Q\} \) to be partitioned into \( K \) clusters, the goal of K-means algorithm is to assign a cluster to each data point, so that the distance from the data points to the cluster is minimized. Mathematically, the K-means clustering method solves the following problem:

\[
\text{argmin}_{1 \leq k \leq K} \sum_{q=1}^{Q} d(x_q, x_k)
\]

where \( x_k \) is the set of points that belong to cluster \( k \) and \( d(x_q, x_k) \) denotes the distance between the data point \( x_q \) and the \( k \)th cluster. The distance \( d() \) can have various representations, for example the Euclidean distance given by \( |x_q - \mu_k| \) with \( \mu_k \) being the average of the data points in the \( k \)th cluster. Note that the problem [1] is not trivial (in fact it is NP-hard), so the K-means algorithm only hopes to find the global minimum, probably getting stuck in a different solution.

The K-means algorithm needs to be initialized. There are some commonly used initialization methods. In this paper, we simply form the initial \( K \) clusters by choosing the \( K \) APs with the \( K \) largest RSS. The effect of cluster initialization will be investigated in experiments.

2) Selection of AP set: After the K-means clustering, a number of \( K \) clusters are obtained. Next, from each cluster one AP will be selected to form a set of \( K \) APs, based on the method shown in Fig. 4. Note that, there might be multiple combinations of selected APs, since multiple APs might be in one cluster. In this case, we generate the AP sets by randomly selecting one AP from each cluster. The procedure to select a set of APs (i.e. select 4 APs from 7) can be seen in Fig. 5. The K-means clustering results is denoted with the red circle, and the resulted AP sequence is denoted with a blue circle.

3) Position Estimation: Once the AP set is generated, the measured location signature can be obtained by sorting the
APs with RSS in descending order. This signature is matched against the location signatures in the fingerprint map and the location information will be retrieved. Note that, there is not always a location signature in the fingerprint map to match the measured location signature. In this case, another AP set will be selected and a new measured location signature will be constructed. If all the AP sets have been selected and we fail to find a matched location signature in the fingerprint map, this test point will be declared as missed detection point.

IV. EXPERIMENTS

A. Experimental Setups

We evaluate the performance of our proposed localization system by experiments, with the two setups given in Fig. 6. Both environments consist of concrete walls (marked with black in Fig. 6), soft room partitions with windows (marked with grey in Fig. 6), furniture, and equipments. The setup in ECC also has concrete poles inside the room. The setup in Dover is a room of 60m×40m, while the setup in ECC is a room of 25m×14m. The proposed system is implemented using smart phones (Sony Z2) with Android version 4.4.2. We install 7 APs (ASUS RT-N12HP Wireless N3002) in both environments. The APs provide RSS values ranging from -70 dBm to -30 dBm. If there is no detection of the access point, we recorded the measurements at 20 test points. For each test point, the RSS values were measured every 300 ms and the observation time is 1 min.

The time used to generate the offline fingerprint map under different numbers of APs used for localization are listed in Table I. The experiments were conducted using an Intel Core i5-4200M@2.50GHz CPU with 4 GB RAM. We use a grid-based representation to compute the fingerprint map. For our implementation, the size of the grid is set to 0.2 m. As can be seen in Table I, we can generate all 35 fingerprint map within one second (to be exact 26.3 ms) for the case of 4 APs, which is negligible when compared to the laborious site survey phase in the traditional fingerprinting-based approaches.

B. Results and Analysis

The proposed selective AP-sequence based indoor localization system is evaluated in terms of localization accuracy, which is defined as the distance between the estimated position and the test points in meter. The experimental results are shown in Fig. 7.

Table I. Number of fingerprint maps needs to be constructed and average time (in milliseconds) consumed to construct the fingerprint map using different number of selected APs out of total 7 APs.

| Number of selected APs | 2 | 3 | 4 | 5 | 6 | 7 |
|------------------------|---|---|---|---|---|---|
| Time used [ms]         | 9.4 | 21.8 | 26.3 | 25.4 | 9.2 | 1.3 |

Fig. 7(b) and Fig. 7(c) present the localization accuracy in terms of cumulative density function (CDF), given different initial seeds of K-means algorithm. The CDFs of accuracy obtained with different numbers of APs selected for localization are shown in Fig. 7(d) and Fig. 7(e), whereas Fig. 7(f) gives the CDFs of accuracy with various observation time.

1) Impact of initial seeds of K-Means algorithm: In the K-means clustering, the choice of APs in the initial K clusters affects the generation of AP sets and thus the localization accuracy. Given 4 APs out of 7 APs used for localization, the accuracy with different initial seeds is shown in Fig. 7(b) and Fig. 7(c) for two experimental setups, where the APs with RSS ordered in $n_1n_2n_3n_4$ are selected. It can be seen that, given the current placement of the 7 APs, the AP set with initial seed of 1234 has the best accuracy for both setups. The reason might be that, stronger signal strength is much more stable and reliable to reflect the position of the interested user, whereas weaker signal strength brings more uncertainty in position interpretation. The AP set with initial clusters of stronger RSS is therefore more robust to RSS fluctuations and a correct AP-sequence can be obtained. A CDF of 50% can be achieved for accuracy $<5m$ in both setups.

To our best knowledge, so far there is no WiFi fingerprinting indoor localization system based on RSS without offline site survey to construct the fingerprint map. In the near future, we would like to compare the performance of our approach with the state-of-the-art techniques.

2) Impact of the number of APs selected for localization: The localization accuracy achieved with different number of APs selected is shown in Fig. 7(d) and Fig. 7(e). It is observed that, the accuracy obtained using 7 APs for localization is not
the best, although theoretically using 7 APs gives the best performance. This is because that, with more APs involved, it is not always likely to have a correct AP-sequence in the fingerprint map, resulting in performance degradation.

We also investigate the probability of missed detection given different numbers of APs used for localization, as shown in Table II. Here missed detection means we could not find any matched fingerprint in the corresponding offline fingerprint maps (see Fig 7). It is observed that, with more APs used for localization, higher possibility of missed detection is expected. In our examples, when all 7 APs are used, 63% and 85% missed detection rate are observed, while when 4 out of 7 APs are used, zero missed detection can be achieved.

3) Impact of time duration to record measurements: The localization accuracy with various time durations (e.g. 3s, 10s, 30s, and 60s) to record the RSS measurements, is shown in Figure 7(d). As can be seen from this figure, a longer observation time gives a better localization accuracy. Since the Wifi signal is severely affected by surroundings, with insufficient measurements (i.e. shorter observation time), we are not able to get a robust estimation of the signal strength, which will lead to a worse localization accuracy. However, for the real-time applications, time consumption will be a key concern, therefore we propose to use probabilistic-based approaches (e.g. particle filter) as our future work to deal with the uncertainties.

V. CONCLUSIONS

This paper studies an indoor localization system employing selective ordered sequence of APs based on RSS without site survey. The proposed system is comprised of an offline phase to generate the fingerprint map and an online phase to dynamically select the AP as well as retrieve the location information from the fingerprint map. In contrast to existing indoor localization systems where time-consuming and laborious site survey is necessary, the fingerprint map of the proposed system is easily constructed by cutting the layouts of the interested area into regions with only the knowledge of positions of APs and assuming a universal propagation model. Employing ordered sequence of APs as location signature, the proposed system is more robust to signal fluctuations in indoor environments. Rather than using all APs available in the Wifi network, we use a selected set of APs to perform localization by employing K-means clustering algorithm. Experimental results show that, the proposed system achieves localization accuracy < 5m with a CDF of 50% to 60% depending on the density of APs. Furthermore, we provide experimental results in terms of localization accuracy and demonstrate that our proposed selective AP sequence performs better than using all APs for localization. The number of APs used to perform localization should be a design parameter based on the placement of APs, which will be further investigated in our future work. Another direction of our future work will be the comparison of our approach to the state-of-the-art.

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TABLE II. PROBABILITY OF MISSED DETECTION (7 APs IN TOTAL).

| No. APs used | 1  | 2  | 3  | 4  | 5  | 6  | 7  |
|-------------|----|----|----|----|----|----|----|
| Dover       | 0  | 0  | 0  | 0.15 | 0.41 | 0.63 |
| ECC         | 0  | 0  | 0  | 0.2  | 0.4  | 0.85 |

Fig. 7. (a): Snapshot of setup at ECC; (b),(c): localization accuracy with various initial seeds at Dover and ECC respectively; (d),(e): localization accuracy with various numbers of APs selected for localization at Dover and ECC respectively; (f): localization accuracy for various time durations at ECC.