DocTime: A Document-level Temporal Dependency Graph Parser

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Abstract

We introduce DocTime - a novel temporal dependency graph (TDG) parser that takes as input a text document and produces a temporal dependency graph. It outperforms previous BERT based solutions by a relative 4-8% on three datasets from modeling the problem as a graph-network with path-prediction loss to incorporate longer range dependencies. This work also demonstrates how the TDG graph can be used to improve the downstream tasks of temporal questions answering and NLI by a relative 4-10% with a new framework that incorporates the temporal dependency graph into the self-attention layer of Transformer models (Time-transformer). Finally, we develop and evaluate on a new temporal dependency graph dataset for the domain of contractual documents, which has not been previously explored in this setting.

1 Introduction

Understanding the temporal relations between events mentioned in a document is an important natural language task with applications in downstream tasks such as timeline creation (Leeuwenberg and Moens, 2018), time-aware summarization (Noh et al., 2020), temporal question-answering (Ning et al., 2020a), and temporal information extraction (Leeuwenberg and Moens, 2019). This area of research remains important yet challenging due to several limitations such as confounded modalities (eg. events that are certain to happen vs the ones that might happen), event ambiguity (eg. agreeing to terms of a contract vs signing a contract) and need for complete annotation of all event pairs for precise temporal localization (Yao et al., 2020a).

Early work densely annotated all pairs of events to address this problem (Cassidy et al., 2014), but was limited to short passages or adjacent sentences due to the $O(n^2)$ complexity of the task, especially for long documents. Recently this problem formulation was significantly simplified using temporal dependency trees (Zhang and Xue, 2019) and temporal dependency graphs (TDG) (Yao et al., 2020a) by only capturing the reference TIMEX or event to build a dependency graph to capture this information. This enabled the development of temporal dependency parsers (Zhang and Xue, 2018a; Ross et al., 2020a) to infer temporal relationships more robustly and efficiently.

We introduce DocTime - a state-of-the-art temporal dependency parser that parses document-level text to produce temporal dependency graphs. Unlike previous approaches using contextual features such as BERT(Ross et al., 2020b), our model utilizes a graph network and a novel path prediction loss to reason over long-range multi-hop dependencies while maintaining global consistency of temporal ordering of inter-dependent events.

To validate the utility of DocTime and our generated temporal dependency graph, we go one step further than prior work and explore the question of whether temporal dependency graphs are useful for downstream tasks by introducing Time-Transformer. It is a framework to incorporate temporal dependency graphs into existing transformer-based architectures without retraining from scratch. We demonstrate the usefulness of our proposed Time-Transformer on temporal NLI (Vashishtha et al., 2020) and time-sensitive question answering (Chen et al., 2021) tasks.

Prior work on temporal relationship extraction and temporal dependency parsing have been mostly limited to news (Zhang and Xue, 2019; Yao et al., 2020a; Pustejovsky et al., 2003a), narrative stories (Zhang and Xue, 2018b; Kolomiets et al., 2012) or clinical notes (Bethard et al., 2016). In addition to experimenting with existing temporal dependency parsing datasets, we introduce a dataset for temporal dependency graphs in a new domain - contractual documents, where temporal reasoning over events has real world legal and monetary implications for users.

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Our main contributions include:

- A novel document-level temporal dependency parser (DocTime) that predicts the temporal dependency graph from text in an end-to-end manner with a novel path prediction loss, which outperforms the current SOTA by a relative 4-8% on three datasets.
- Time-Transformer, a novel framework to incorporate Temporal Dependency Graphs into transformer models for downstream tasks without needing to retrain from scratch. Results on natural language inference and question answering with a new self-attention module show a relative 4%-10% improvement.
- Development of new document-level (>1500 words) TDG dataset in the domain of contractual documents (ContractTDG).

Figure 1: DocTime encodes rich token level embeddings from input document using structural, syntactic, and semantic graphs through BERT-GCN, WR-GCN and HyperGraph Conv layers, respectively. Token-level features are concatenated and passed through Iterative Deep Graph Learning (IDGL) to learn a noisy dependency structure over the TIMEX and Event entities. Graph U-net allows the model to incorporate longer range dependencies for predicting the final temporal dependency graph structure and relationships. The model is trained with a novel auxiliary path prediction loss to learn multi-hop connections in TDG.

2 Related Work

Temporal Dependency Parsing: Previous work has been devoted to pairwise classification of relations between events and time expressions, notably TimeBank (Pustejovsky et al., 2003b) and its extensions like Cassidy et al. (2014) annotated all relations. Pair-wise annotation have multiple problems including polynomial square complexity, global inconsistencies in predictions due to relation transitivity and forced annotation of vague relations (Ning et al., 2018). Prior work focuses on extracting temporal relations between event pairs in the same sentence or adjacent sentences (Goyal and Durrett, 2019; Ning et al., 2019a; Han et al., 2019a,c,b, 2020; Ballesteros et al., 2020; Zhao et al., 2020). TIMERS Mathur et al. (2021a) presented temporal relation extraction in long document.

Temporal Dependency Parsing (TDP): Temporal dependency trees were first proposed by Kolomiets et al. (2012). (Zhang and Xue, 2018b) provided the the earliest TDT corpus on news data and narrative stories, (Zhang and Xue, 2019) released the first English TDT corpus. Yao et al. (2020a) relaxed the assumption of single reference edge in dependency trees to form the improved TDG. (Zhang and Xue, 2018a) built an end-to-end neural temporal dependency parser using BiLSTM and Ross et al. (2020b) improved it further incorporating BERT. Our approach improves by modeling complex dependencies and introduces a new resource for TDG in contracts.

Linguistically-aware Transformers: Recent works have investigated using linguistic features as a prior for Transformer models. Syntax-bert (Bai et al., 2021a) uses syntactic and constituency dependency on NLI and GLUE benchmarks. Coref-BERT Coreference-Informed Transformer (Liu et al., 2021) performs coreference-aware dialogue summarization. Temporal reasoning about event ordering can find applications in many tasks such as summarization (Noh et al., 2020), question answering (Chen et al., 2021; Ning et al., 2020b; Jin et al., 2020), commonsense reasoning (Qin et al., 2021), and natural language inference (Vashishtta et al., 2020). We propose to use TDG as priors to Transformer models to make them temporally-aware for use in downstream tasks.

3 DocTime: Document TDG Parsing

Task Formulation: Let document $D$ be defined as a sequence of $n$ tokens $[x_1, \ldots, x_n]$. The entire document can be seen as sequence of $m$ sentences $[s_1, \ldots, s_m]$. Each document has a set of $p$ events $E = [e_1, \ldots, e_p]$ and $q$ timexes $T = [t_1, \ldots, t_q]$, where $p, q \leq n$. The creation date of the document is represented by timestamp $t_{DCT}$. Yao

\footnote{https://github.com/contractTDG/ContractTDG_Dataset}
et al. (2020a) defines a temporal dependency graph (TDG) where each timex node always has a reference timex, which is the most specific narrative time related to the event (Pustejovsky and Stubbs, 2011). If such a narrative time is not available, the timex should be anchored to the DCT. An event node can either have a reference timex or be connected to a reference event, which is an event that provides the most specific temporal location. The task of temporal dependency graph parsing of a text document \( D \) results in a dependency graph \( G = (C, V) \), where \( C \) represents the set of all events, timexes and the document creation date (DCT). \( V \) is the set of all edges in the graph, where each edge represents a temporal relationship \( \Re \) between corresponding entity node pair \( V = \{(t_i, t_j), (e_i, e_j), (e_i, t_j)\} \forall i, j \in C \).

**Model Overview:** Figure 1 shows an overview of our network architecture for temporal dependency parsing. We first extract token level BERT features from the input document, which are then enriched by three graph networks that encode structural, syntactic, and semantic relationships. This is followed by Iterative Deep Graph Learning over the TIMEX and Event entities to learn an initial dependency structure. This is passed through a Graph U-net to allow the model to incorporate longer range dependencies before predicting the final temporal dependency graph and relationships. The model is also trained with a novel auxiliary path prediction loss.

### 3.1 Feature Encoding

We leverage the pre-trained BERT language model to obtain the embeddings for each token as follows: \( w_1, w_2, \ldots, w_n = \text{BERT}([x_1, x_2, \ldots, x_n]) \), where \( w_i \) is the embedding of the token \( x_i \). As document sequence lengths can be larger than 512, we use a sliding window encoding technique to encode whole documents. We average the embeddings of overlapping tokens of different windows to obtain the final representations. These token representations are enriched with slightly enhanced variants of the structural \( (G_{str}) \), syntactic \( (G_{syn}) \) and semantic \( (G_{sem}) \) graphs utilized by (Mathur et al., 2021b) for document-level temporal relationship extraction. The key differences are the use of BERT-GCN (Lin et al., 2021) to combine contextual and structural graph features, the addition of co-reference relationships to the syntactic graph, and the use of a hypergraph convolution (Bai et al., 2021b) to allow for token level features in the semantic graph. All aspects of these features and the changes are presented in Appendix B.

### 3.2 Temporal Dependency Prediction

We combine the learned representation for each entity node (timex, event, DCT) by concatenating the node embeddings learned from structural, syntactical and semantic graphs to obtain a \( D \)-dimensional feature vector for each of \( z \) entities in the document given by \( F(w_i) = g_i^{str} + g_i^{syn} + g_i^{sem} \), where \( \oplus \) represents concatenation. We retain only the enriched node embeddings for each word. We then utilize Iterative Deep Graph Learning (IDGL)\(^3\) (Chen et al., 2020) to dynamically learn an initial dependency graph structure from the combined node embeddings. Given a noisy graph input feature matrix \( F \in \mathbb{R}^{l \times D} \), IDGL produces an implicitly learned graph structure \( G^{*} = \{A^{*}, F, I_1\} \) with a jointly refined corresponding graph node embeddings \( F^{*} \) with adjacency matrix \( A^{*} \) by optimizing with respect to downstream link prediction task \( F_1 \) between entity nodes.

#### 3.2.1 Graph U-net For Higher Level Features

The Graph U-net (Gao and Ji, 2019) is a U-shaped graph encoder-decoder architecture containing two down-sampling graph pooling (gPool) layers and two up-sampling graph unpooling (gUnpool) layers with skip connections. gPool layers reduce the size of the graph to encode higher-order features, while the gUnpool layer restores the graph into its higher resolution structure, thereby promoting information exchange between entity pairs through an enlarged receptive field. Each graph pooling and unpooling layer is followed by a GCN layer to implicitly capture the topological information in the input graph. Taking the dynamically learned graph structure \( G^{*} \), a graph embedding layer converts input node features \( F^{*} \) into low-dimensional representations that are then passed through a graph U-net encoder-decoder \( \mathcal{O} \) to acquire entity-level relation matrix \( Y = \mathcal{O}(F^{*}), Y \in \mathbb{R}^{l \times l \times D'} \).

#### 3.2.2 Temporal Dependency Link Prediction and Relation Classification

Given entity adjacency matrix \( A^{*} \) and entity-level relation matrix \( Y \), we use a bilinear function to map them to link and relation probabilities \( Z_l \) and \( Z_r \), respectively. Formally, we have \( Z_l = \sigma(YW_l Y + b_l) \) and \( Z_r = \sigma(A^{*}W_r A^{*} + b_r) \), where

\[Z_l = \sigma(W_l Y Y + b_l)\]

\[Z_r = \sigma(A^{*}W_r A^{*} + b_r)\]

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3\(^3\)Implementation: https://github.com/graph4ai/graph4nlp
TISA

Figure 2: Time-Transformer is a variant of pre-trained Transformer models that augments temporal knowledge into the self-attention layer during fine-tuning of the Transformer model on different downstream tasks. Input text is converted into a temporal dependency graph using DocTime parser. The graph is then converted into a set of masks that encodes the temporal relationship between each token (i.e. After, Before) using the novel Temporally-informed Self-Attention (TISA). TISA creates K masks to represent the (k)-hop distance between two nodes in TDG for aggregating information across longer ranges in the input. TISA uses hyperbolic feed-forward layer to learn the mask weights.

\[ L_{ce} = -\frac{1}{\sum_{i=0}^{l} N_i} \sum_{i=1}^{l} \sum_{j=1}^{N_i} \left( r_j^i \log P(r_j^i) + (1 - r_j^i) \log(1 - P(r_j^i)) \right) \]  

\[ L_{path} = -\frac{1}{\sum_{i=0}^{l} N_i} \sum_{i=1}^{l} \sum_{j=1}^{N_i} \left( \sum_{j=1}^{N_i} \log \mathcal{N}(\phi_i) + (1 - r_j^i) \log(1 - \mathcal{N}(\phi_i)) \right) \]  

Multi-task Training: Dependency link prediction and entity-level relation classification are correlated tasks and reinforce each other. We use multi-task training to optimize both tasks simultaneously using the path prediction cross entropy loss. The final optimization uses a weighted sum of the dependency link prediction loss and entity-level relation classification loss \( L = \lambda L_{l} + (1 - \lambda) L_{r} \), where the weighting factor \( \lambda \) is a hyperparameter.

4 Time-Transformer

We would also like to understand our temporal dependency parsing can be useful for downstream tasks requiring temporal reasoning. Here we introduce the Time-Transformer, which allow a TDG generated by DocTime to be combined with state-of-the-art transformer models for temporal tasks. The Time-Transformer augments the flow of information in a Transformer network via a temporally-informed self-attention mechanism. We first for-
mulate the Time-Transformer architecture in §4 and then construct of temporally-informed attention layers in §4.

**Architecture:** Time-Transformer was motivated by recent work incorporating syntax (Bai et al., 2021a) or co-reference graphs (Liu et al., 2021) into the transformer architecture to improve downstream tasks. In each case, these approaches encode additional knowledge from the sparse graphs as a masked self attention layer into the transformer. Figure 2 shows the architecture of Time-Transformer incorporating temporal knowledge into the self-attention layer during fine-tuning of the Transformer model. Input text is converted into a temporal dependency graph using DocTime parser. The graph is then converted into a set of masks that encodes the temporal relationship between each entity (i.e. After) explained in more detail in the next section: Temporally-informed Self-Attention. The input embedding (token+positional+attention masks) is passed through the Time-Transformer model which modifies the self-attention layer of the standard Transformer architecture with a temporally-informed self-attention layer to be fine-tuned on downstream tasks.

**TISA: Temporally-informed Self-Attention:** The TDG produced by DocTime is sparse and to effectively utilize the graph extracted by the temporal dependency parser for longer range temporal relationships, we utilize K self-attention layers that encode the temporal relationship if traversing K hops in the TDG as shown in 2. More formally starting from node A, the minimum number of hops (k) required to reach another node B can be regarded as k-hop distance between A and B, written as k-hop(A, B). We create K masks to represent the (k)-hop distance between two nodes to allow the model to aggregate information across longer ranges in the TDG. Specifically, a mask \( M \in \{0, 1, 2, \cdots, r\}^{n \times n} \) denotes if there is a relation between entity i and j, and n is the number of tokens in the input text. The value of the mask is the relationship type for i and j. It is found by inferring the relationship using Allen’s interval algebra (Allen, 1983) and is set to 0 if there is no relationship or set to “Overlap” if there is a conflict. We adopt a soft-mask learning strategy to enable the self-attention layer to re-weight the importance of each mask and avoid the problem of vanishing gradient. A hyperbolic feed-forward layer is used to learn the mask weights as research has shown it can avoid distortion of the feature space in graph representations (Ganea et al., 2018). The value of K is a hyperparameter that can be customized according to the nature of input dependency graph.

**Training Time-Transformer:** For each dataset, we optimize the hyper-parameters of Time-Transformer through grid search on the validation data. In all our experiments, we limit the maximum value of k-hop to 15. Detailed settings can be found in the appendix.

5 Experiment

5.1 Temporal Graph Parsing Datasets

We train and evaluate DocTime on three datasets. First is the Temporal Dependency Graphs (TDG) dataset (Yao et al., 2020a) made up of 500 Wikinews articles annotated with document-level temporal dependency graphs. Second is the Temporal Dependency Trees (TDT) dataset Zhang and Xue (2019) made from 183 documents derived from TimeBank (Pustejovsky et al., 2003a) annotated with a temporal dependency tree structure. The third dataset we created as part of this paper and is described in more detail below.

**Contract-TDG:** Understanding the temporal relationship of events in contracts is an important business problem, where understanding event timelines can have legal and monetary consequences. Previous work on temporal relationships has largely focused on clinical, news or narrative text, whereas to the best of our knowledge the contractual domain has not been explored for this problem. To construct this dataset, we used 100 contracts from the Atticus contracts dataset3 (Hendrycks et al., 2021), which were sourced from public domain SEC contracts. Due to the multi-page length of these documents, we limited the annotations to the first 1500 words. We did not include definition sections, since they did not contain many events of interest for this task. The documents have a 70-10-20 split for training, validation, and testing.

To obtain the TDG annotations required for our task, we followed the 5 steps procedure outlined by the original TDG dataset in (Yao et al., 2020b): (i) TIMEX Identification (TE), (ii) Identifying reference times for TE, (iii) Event identification, (iv) Identifying reference times for events, (v) Identifying reference events for events. Document Creation

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3[https://www.atticusprojectai.org/cuad](https://www.atticusprojectai.org/cuad)
Table 1: Comparison of ContractTDG data statistics to other temporal relation datasets. ContractTDG has fewer documents but comparable number of TIMEX/Events/relations.

```markdown
| Dataset                  | Docs | Timex | Events | Rel |
|--------------------------|------|-------|--------|-----|
| TimeBank (Pustejovsky et al., 2003b) | 183  | 1,414 | 7,935  | 6,148|
| TB-Dense (Cassidy et al., 2014)      | 36   | 289   | 1,729  | 12,715|
| MATRES (Ning et al., 2019b)         | 275  | -     | 1,790  | 13,577|
| TDT-Crd (Zhang and Xue, 2019)       | 183  | 1,414 | 2,691  | 4,105|
| TDG (Yao et al., 2020a)             | 500  | 2,485 | 14,974 | 28,350|
| Contract-TDG (Ours)               | 100  | 2354  | 11,752 | 12,909|
```

Table 2: Inter-Annotator Agreement (IAA) for the ContractTDG and TDG dataset. U = structure, L = structure + labels

```markdown
| Task                  | TDG (F1) | Contract TDG (F1) |
|-----------------------|----------|-------------------|
| 1: TIMEX ID           | 0.86     | 0.93              |
| 2: TIMEX RT           | 0.99     | 0.81              |
| 3: Event ID           | 0.79     | 0.76              |
| 4: RT ID (U)          | 0.67     | 0.83              |
| 5: RT ID (L)          | 0.61     | 0.75              |
| 5: RE ID (U)          | 0.59     | 0.85              |
| 5: RE ID (L)          | 0.52     | 0.79              |
```

Times (DCT) were provided as effective dates in the ATTICUS corpus.

Similar to (Yao et al., 2020b) for tasks 1 (TE) and 3 (Event ID), we used the Mechanical Turk platform to obtain two annotations to validate text spans of noisy TIMEXes extracted by HeidelTime software⁴ (Strötgen and Gertz, 2013) and verbs that were possible events. Disagreements were resolved by an expert annotator. However, for the reference tasks, we decided against using Mechanical Turk due to the difficulty and length of the contracts as well as the lower agreement faced by the original TDG system for the last two tasks. We instead used the BRAT annotation tool⁵ (Stenetorp et al., 2012) with an expert annotator for tasks 2, 4, and 5, following the (Yao et al., 2020b) guidelines. ContractTDG is annotated for four temporal relations - after, before, overlaps, and includes.

Table 1 compares the data statistics of the ContractTDG to previous temporal relationship datasets and temporal dependency corpora. Even though this dataset has many fewer documents than the TDG dataset, it has a large number of TIMEX, Events, and Temporal relationships due to the document length. Table 2 reports the F1 IAA metrics for ContractTDG dataset to directly compare to the original TDG dataset. For Tasks 1 and 3 we report IAA F1 for the two crowd sourced worker annotations and for the relationship tagging tasks (2,4,5), we report IAA metrics calculated on the test position (20% of the data) that was reviewed by two experts. The agreement is slightly lower for the TIMEX/Event identification tasks but higher for the three relationship tasks. We evaluate DocTime for dependency structure as well as structure+relation prediction for both development and test splits.

5.2 Time-Transformer Experiments for Downstream Tasks

We adopt Time-Transformer on BERT (Devin et al., 2019), RoBERTa (Liu et al., 2019a), BigBird (Zaheer et al., 2020a) and FiD (Izacard and Grave, 2021) for evaluation on two downstream tasks in §6.2. We utilized the official checkpoint for each pre-trained language model as provided by respective authors. First, we test Time-BERT and Time-RoBERTa on Temporal NLI dataset, which consists of 5 sub-datasets (Vashishtha et al., 2020) to study the effect of temporal reasoning for predicting event ordering and duration. Second, we run experiments on the TimeQA dataset (Chen et al., 2021) to evaluate the performance of Time-BigBird and Time-FiD for the long-document question-answering task. We report Exact Match (EM) and F1 scores as evaluation metrics on dev and test sets of easy and hard versions.

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⁴https://github.com/HeidelTime/heideltime  
⁵https://brat.nlplab.org/
Table 3: Results comparing performance of DocTime with baselines and ablative components on TDT, TDG, ContractTDG datasets. We majority and logistic regression baselines from (Zhang and Xue, 2018a). * indicates statistical significance over BERT Ranking Parser (Ross et al., 2020b) (p ≤ 0.005) under Wilcoxon’s Signed Rank test. Darker green represents better F1 performance on ablation studies. Bold denotes the best performing model. DocTime improves substantially over all datasets for both dependency structure and structure-relation prediction tasks. The ablation shows that semantic graph features prove to be most beneficial. Our proposed path prediction loss is critical for state-of-the-art performance of DocTime model.

Table 4: Accuracy comparison on the Temporal NLI dataset test set. Time-RoBERTa fine-tuned by utilizing temporal dependencies extract from DocTime model pre-trained on TDG dataset outperform all baselines provided by (Vashishtha et al., 2020)(see bold).

6 Results and Analysis

6.1 Temporal Graph Parsing

Performance of DocTime w.r.t. baselines: Table 3 compares the performance of DocTime against other baseline methods on TDT, TDG and ContractTDG. We also provide a majority baseline ContractTDG to evaluate whether the methods work better than a random label assignment as implemented in (Yao et al., 2020a). We also include the two current SOTA approaches for temporal dependency parsing: The BiLSTM attention-based Neural Ranking Parser proposed by (Zhang and Xue, 2018a)⁶ and the BERT Ranking Parser (Ross et al., 2020b) on each dataset. We also report results for a logistic regression baseline proposed by (Zhang and Xue, 2018a). Results in Table 3 show that DocTime outperforms both Neural and BERT Ranking Parser by a significant margin on the TDT (2-4%) TDG (5-6%) and ContractTDG (3-4%) datasets. We believe its primarily because they formulate temporal dependency parsing as a ranking task designed to select the best reference event/timex for each node. However, TDG parsing requires the model to be able to reason over multiple dependencies originating from each node while maintaining global consistency of temporal ordering of inter-dependent events. We perform experiments for dependency structure prediction and structure-relation prediction and find that predicting labeled dependency edges is a much more challenging task across all datasets. DocTime achieves state-of-the-art performance on all three datasets (see bold), and shows that it can successfully handle document-level long-range dependencies in the challenging ContractTDG dataset from the 6-12% relative improvement over the BERT based ranking parser. A more detailed analysis of performance per temporal relationship type can be found in the Appendix, where largest gains are seen for event-event pairs.

Ablation Study of DocTime: To assess the contribution of structure and syntactic and semantic graph features, we performed ablation experiments as reported in Table 3 highlighted in red. We also analyzed the effect of different types of training loss. We observe that removing the semantic graph consistently degrades performance, indicating the need for hypergraph learning over temporal arguments and RST features to capture document-level discourse relations. We see that removing structure graph reduced the performance to below the BERT Ranking Parser, as DocTime leverages BERT’s contextual learning through a structural graph. Syntactic graph adds incremental value to DocTime due to its relational learning of syntactic dependencies within each sentence through relational GCN. We evaluated the model performance in case all edges of the TDG are used for one forward pass and call it "Graph Prediction". Training the model by evaluating a single edge in one pass (similar to temporal relation prediction in (Pustejovsky et al., 2003b) is referred to as "Pairwise Prediction". We explore the impact of different training

⁶Used: http://github.com/yuchenz/tdp_ranking
Table 5: Results comparing F1 score and exact match (EM) performance of Time-BigBird and Time-FiD for QA task on easy and hard sections of TimeQA dataset. We evaluate the Transformer models in 3 settings - fine-tune on TimeQA; fine-tune TriviaQA; and fine-tune on NQ then TimeQA. Green shows improvement due to our proposed Time-Transformer model, while we see degradation due to Euclidean variant of Time-Transformer (E).

6.2 Application of Temporal Dependency Parsing for downstream tasks

We train the DocTime model on the TDG corpus, which can be used to infer a temporal dependency graph from raw text samples. We extract events and timexes using CAEVO (Chambers et al., 2014) for all data samples in train, validate, and test. The temporal dependency graph acquired for each document is used as a prior for Time-Transformer to perform downstream tasks.

Performance of Time-Transformer on Temporal NLI: The temporal NLI task requires a model to identify the semantic relationship (entailed, not-entailed) between the context and corresponding hypothesis sentence based on temporal information from text. The temporal dependency graphs extracted using the DocTime trained on the TDG corpus are used as prior for Time-BERT to perform entailment classification. Table 4 shows the test accuracies of Time-BERT-large, Time-RoBERTa-large and other competitive baselines [(Iyyer et al., 2015),(Conneau et al., 2017)] reported by (Vashishtha et al., 2020). The temporal information prior proposed in Time-Transformer helps the BERT and RoBERTa models perform much better on the NLI task. The accuracy improved by 1.5-2.3 F1 points by applying our framework on the RoBERTa model across the five subsets. We observe the performance gain in the case of the Euclidean version of Time-RoBERTa to be modest as compared to its hyperbolic counterpart.

Performance of Time-Transformer on TimeQA: The TimeQA task focuses on understanding the time scope of facts in the long text followed by answering questions conditioned on the query and the document using implicit temporal information. We then apply the DocTime model output trained on the TDG corpus to the Time-Transformer framework on BigBird and FiD language models for long document question answering task. Following (Chen et al., 2021), we experiment with three variants of pre-trained settings: (1) fine-tuned on the TimeQA training set; (2) fine-tuned on NQ/TriviaQA data; (3) fine-tuned on NQ/TriviaQA data and TimeQA. Table 5 shows the effectiveness of Time-BigBird and Time-FiD in consistently outperforming their corresponding baselines in all three settings. More specifically, we see a relative gain of 10-14% in F1 and exact match scores (EM) for both easy and hard sections of the dataset. It is impressive to note that the improvements due to the Time-BigBird and Time-FiD models are steady with different pre-training setups with the addition of only a few extra parameters to the baseline model. An important observation here is that the Euclidean versions of Time-BigBird and Time-FiD models show persistent performance deterioration across all settings for TimeQA. We attribute this phenomenon to our initial hypothesis behind using hyperbolic operations in the proposed Temporally-informed self attention (TISA) layer. As the text length grows, the complexity of geometric operations increases, leading to vectorial distortions in Euclidean spaces (Ganea et al., 2018). This is remedied by hyperbolic transformations of masked self-attention learning in the proposed Time-Transformer.

Our experiments provide evidence that temporal dependency graphs extracted using DocTime and then utilized as a prior by temporally-
Figure 4: Impact of long-distance dependencies on Transformer models for TimeQA task. Plot shows the exact match (EM) accuracy vs length of input document for hard samples. We use BigBird and FiD fine-tuned on NQ + TimeQA as backbone models. Time-BigBird and Time-FiD maintain steady improvements over baseline models even with increase in input lengths.

| Corpus         | Model                                   | Structure + Relation (F1) | \[n=4000\] | \[n=8000\] | \[n=12000\] | \[n=16000\] |
|---------------|------------------------------------------|---------------------------|----------|----------|----------|----------|
| TD-Graphs     | Neural Ranking Parser (Zhang and Xue, 2018a) | 0.42                      | 0.53     | 0.64     | 0.66     | 0.66     |
|               | BERT Ranking Parser (Ross et al., 2020b)   | 0.53                      | 0.66     | 0.76     | 0.79     | 0.77     |
|               | DocTime                                  | **0.66**                  | **0.75** | **0.72** | **0.72** | **0.77** |
| Contract-TDG  | Neural Ranking Parser (Zhang and Xue, 2018a) | 0.57                      | 0.72     | 0.77     | 0.79     | 0.79     |
|               | BERT Ranking Parser (Ross et al., 2020b)   | 0.70                      | 0.84     | 0.85     | 0.90     | 0.91     |
|               | DocTime                                  | **0.75**                  | **0.86** | **0.89** | **0.90** | **0.94** |

Table 6: Performance (F1 score) of DocTime across timex-timex, event-timex and event-event pairs for dependency structure+relation prediction on TDG and ContractTDG datasets. DocTime outperforms all baselines on every setting.

Informal Transformer architectures such as Time-Transformer can improve the performance of several downstream tasks that require temporal reasoning at the sentence-level as well as at the document-level.

**Impact of Long-term Dependency on Time-Transformer performance:** We plot Fig. 4 to understand the capability of Transformer models to handle the long-term dependency in temporal reasoning on the TimeQA dataset. Plot shows the exact match (EM) accuracy vs length of the input document for hard samples. We use BigBird and FiD models fine-tuned on NQ + TimeQA as backbone models. BigBird’s performance degrades rapidly as the length increases to over 5000 tokens, while the FiD’s performance is quite uniformly distributed across different document lengths due to it’s strong capability to deal with long-term dependency. Time-BigBird and Time-FiD follow a similar trend and maintain steady improvements over their corresponding baseline models with increasing in input lengths.

**Space complexity analysis:** We choose RoBERTa-base as the base model to analyze the space complexity. Liu et al. (2019b) reported the number of trainable parameters in RoBERTa-Base to be about 123 million. Time-RoBERTa introduces an additional 2 million parameters in total due to k-hop mask learning in the TISA layer. Therefore, Time-BERT adds few parameters to the base model without affecting its original space complexity.

**Time Complexity analysis:** We assume the number of tokens in each sentence to be n and extract k-hop mask matrices from a text document is \(O(n^2)\) in the online inference phase. The time complexity of the Transformer embedding lookup layer is \(O(n)\). The TISA layer calculates the attention score in \(O(KD_qn^3)\) for both \(QK^T\) and learns the mask weights using a hyperbolic feedforward layer \((MW^M)\), where \(D_q\) is dimension of \(Q\) and \(K\) is the number of sub-networks. The time complexity of the Time-BERT remains the same for small enough value of \(k\) \((k \leq 15\) in experiments).

**7 Conclusion**

We present DocTime, a new temporal dependency parsing approach that improves upon previous approaches by integrating longer term temporal information through a graph network with a novel path prediction loss. Additionally, we are able to show how a TDG can be incorporated into Transformer networks with Time-Transformer to improve on down stream tasks for NLI and question answering. Finally we introduce a TDG dataset in a new domain (Contractual documents) to expand research in this temporal reasoning to a new application domain. Future works will aim to explore more ways for integrating temporal dependency graphs into neural architectures across different application domains. In future, we would like to explore temporal event mining to aid various social media applications such as improving hate speech detection (Mathur et al., 2018b; Chopra et al., 2020), analyzing temporality in suicidal ideation detection (Mishra et al., 2019; Mathur et al. 2020) and abuse detection (Gautam et al., 2020; Sawhney et al., 2021). The proposed Time-Transformer can find applications in augmenting financial tasks (Sawhney et al., 2020), affective computing (Mittal et al., 2021), and AI for social good (Mathur et al., 2018a) with temporal common sense reasoning.
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A Ethics Statement

We utilize two publicly available datasets - TDT and TDG for evaluating temporal dependency parser. We also curated dataset for TDG on contract documents. We source these contract documents from a publicly available resource - ATTICUS. We repurpose the document in this dataset for our task and provide new annotations. ContractTDG dataset does not violate any privacy as these documents are already in public domain. There is no human bias involved in such documents as they are business contracts filed on the SEC website. These documents do not restrict reuse for academic purposes and any personal information was already redacted before their original release. All documents and our experiments are restricted to English language. Temporal NLI and TimeQA datasets that are publicly available for research purposes. The crowd workers are paid a fair wage. There was no sensitive data involved in the studies.

B Details on Graph Feature Extraction

B.1 Structural Graph Features

The Structural Graph ($G_{str}$) enriches the token level features with a hierarchical textual structure formed by grouping word tokens into lists of sentences that bind together to form the text document. Prior work has shown that transductive graph learning over $G_{str}$ can help learn the long range word-word dependencies set several sentences apart through hierarchical text modeling (Yao et al., 2019). The directed edges of the Structural Graph encode the following relationships: (1) Document-Sentence Affiliation, which connects each document-node to a sentence-node; (2) Sentence-Word Affiliation, which joins each sentence node to its constituent word nodes; (3) Sentence-Sentence Adjacency and (4) Word-Word Adjacency, which preserve sequential ordering for consecutive sentence and word nodes, respectively. For the structural graph, a sentence node embedding $s_i$ is obtained by passing sentences through a pre-trained SentenceBERT model (Reimers and Gurevych, 2019) and the document node embedding $D$ is calculated as the average of all sentence embeddings ($D = \sum_{i=0}^{m} v_i$).

BertGCN (Lin et al., 2021) combines the advantages of both large-scale pre-training and transductive learning. We input the structural graph $G_{str}$ to BertGCN model\(^7\) where each node represents a word, a sentence or the document. BertGCN processes the input node feature matrix sequentially through a Bert model to fine-tune each node to learn local contextual representations. This is followed by passing the learned node feature matrix through two layers of graph convolution to take advantage of global influence propagation through graph edges across multi-hop nodes.

B.2 Syntactic Graph Features

Syntactic cues are useful priors for learning based NLP tasks (Kiperwasser and Ballesteros, 2018). Pre-trained transformer models can capture certain syntactic information implicitly (Hewitt and Manning, 2019) but Jawahar et al. (2019) showed that BERT needs to be trained with deeper layers for handling harder cases involving long-distance dependency information. Moreover, past studies have pointed to the existence of multi-hop coreferring expressions in document-level text due to anaphora and cataphora (Joshi et al., 2020).

$G_{syn}$ is made of separate nodes to represent each constituent word $w_i$ in the document. For each document, there is also a set of co-reference clusters $\{C_1, C_2, \cdots, C_u\}$ referring to the same entities in the graph. We define four types of directed edges in $G_{syn}$ as described below where $\xi$ denotes the set of syntactic dependency arcs inside sentences, $S_{w_i}$ denotes root of the sentence in which $w_i$ belongs, and $S_{w_j} \rightarrow S_{w_j}$ represents whether sentences containing words $w_i$ and $w_j$ are adjacent.

\[
\epsilon_{syn}(i, j) = \begin{cases} 
\text{dependency} & \text{if } (w_i, w_j) \in \xi \\
\text{reversion} & \text{if } (w_j, w_i) \in \xi \\
\text{coreference} & \text{if } w_i, w_j \in C_w \\
\text{self-loop} & \text{if } i == j \\
\text{root-adjacency} & \text{if } w_i == S_{w_i}, \\
& w_j == S_{w_j}, \\
& S_{w_i} \rightarrow S_{w_j}
\end{cases}
\] (3)

The first two edge types are introduced to allow information flow along and against syntactic arcs between intra-sentential dependency relations to enrich contextually learned embeddings of each word. We connect parse tree roots of adjacent sentences to encode document level long-range syntactic relatedness between sentences. We add an undirected edge between word nodes if both belong to the same co-reference cluster. Inspired by (Kipf and Welling, 2016), self-loop edges are added for better message passing iterations. $G_{syn}$ is instantiated

\(^7\)Implementation Used: https://github.com/ZeroRin/BertGCN
as a gated variant of Weighted Relational Graph Convolutional Network (WR-GCN) (Zhang et al., 2020) with \( k \)-layers. WR-GCN can able to model diverse relations in a heterogeneous graph by treating different types of edges with unequal weights assigned during message passing.

### B.3 Semantic Graph Features

Semantic Role Labeling (SRL) parses text sequences to recognize the predicate-argument structure in the sentence to answer who did what and when. Anchoring verb events to their temporal argument spans extracted from semantic parsing helps infer event relationships with their associated time expressions. This can be complemented by discourse features in the form of RST connections can help leverage long-range document-level interactions between phrase units (Bhatia et al., 2015) and identify background-foreground events (Aldawsari et al., 2020) and improve temporal relationship parsing (Mathur et al., 2021b). We utilize Document-level Rhetorical Structure Theory (RST) parser (Shi et al., 2020) to organize contiguous semantic text spans of a document into a hierarchical dependency structure labeled with their rhetorical relations.

\( G_{\text{sem}} \) consists of individual nodes for each constituent word \( w_i \) in the document. Discourse units and temporal arguments may span several word tokens \( \{w_1, w_2, \ldots w_k\} \). We add two types of directed edge connections between - (1) event verb predicate - temporal argument edge (\( \varepsilon_i \)) such that \( (w_e \rightarrow \{w_1, w_2, \ldots w_k\} \in \varepsilon_i) \); (2) Rhetorical pair edges (\( \varepsilon_d \)) labelled by the type of the rhetorical relation \( \{(w_1, w_2, \ldots w_i) \rightarrow \{w_1, w_2, \ldots w_j\} \in \varepsilon_d \)).

\[
\varepsilon = \begin{cases} 
w_e & \{w_e, \ldots w_k\} \in \varepsilon_i \\
\{w_1, \ldots w_i\} & \{w_1, \ldots w_j\} \in \varepsilon_d 
\end{cases}
\] (4)

The nature of edge connections in \( G_{\text{sem}} \) extends beyond pairwise interactions as each edge may connect to one or more word nodes. Hence, we formulate the semantic graph as a hypergraph (Feng et al., 2019) where an edge can join an arbitrary number of vertices. We construct \( G_{\text{sem}} = (\nu, \varepsilon, W) \) where \( \nu \) is the set of all word nodes \( w_i \), and \( \varepsilon \) is the subset of hyperedges such that \( \varepsilon = \varepsilon_i \cup \varepsilon_d \). Each hyperedge \( e \) is assigned a positive weight corresponding to the type of edge relation and is stored in a diagonal matrix \( W \in \mathbb{R}^{|e| \times |e|} \). The semantic graph is learned using hypergraph convolution layers (Bai et al., 2021b) to obtain discriminative node embeddings for each word node.

### C Training Setup

**Hyperparameter:** Hyper-parameters for DocTime were tuned on the respective validation set to find the best configurations for different datasets. We summarize the range of our model’s hyper parameters such as: number of hidden layers in WR-GCN/BERT-GCN/HyperGraphGCN \( \{1, 2, 3\} \), size of hidden layers in WR-GCN/BERT-GCN/HyperGraphGCN \( \{64, 128, 256, 512\} \), BERT embedding size (768). Dropout \( \delta \in \{0.2, 0.3, 0.4, 0.5, 0.6\} \), learning rate \( \lambda \in \{1e-5, le-4, 1e-3, 1e-2, 1e-1\} \), weight decay \( \omega \in \{1e-6, le-5, le-4, le-3\} \), batch size \( b \in \{16, 32, 64\} \) and epochs \( (\leq 100) \), \( \epsilon \)-sparsity \( \in [0, 1] \), IDGL smoothness ratio=0.5, IDGL sparsity ratio=0.5, IDGL connectivity ratio=0.5, size of hidden layers in Graph U-net \( \{64, 128, 256, 512\} \).

**Loss Function and Inference:**

**Time-Transformers** are trained using Cross Entropy loss with Adam optimizer. Across both TempNLI and TimeQA datasets, we found the best results correspond with the use of Adam optimiser set with default values \( \beta_1 = 0.9 \), \( \beta_2 = 0.999 \), \( \epsilon = 1e-8 \), weight-decay of 5e-4 and an initial learning rate of 0.001.

DocTime uses cross entropy loss for structure prediction. For structure+relation classification, it uses the path prediction loss as defined in Methodology.

**Computing Infrastructure:**

DocTime and Time-Transformers are written in PyTorch library and were trained on 4 and 6 Nvidia GeForce RTX 2080 GPU, respectively. **Average Runtime:** DocTime takes a maximum of approximately 5 hrs to train once on TDG datasets. Time-BERT, Time-RoBERTa take 3 hrs to fine-tune on TempNLI. Time-BigBird, Time-FiD takes 8.12 hours to fine-tune, respectively.

**Dataset Access**

- [Links to download TDT dataset](https://github.com/yuchenz/crowdsourced_EN_TDT_corpus)
- [Link to download TDG dataset](https://github.com/Jryao/temporal_dependency_graphs_crowdsourcing)
- [Link to download Temporal NLI dataset](https://github.com/sidsvash26/temporal_nli)
- [Link to download TimeQA dataset](https://...
Table 7: Performance (F1 score) of DocTime across timex-timex, event-timex and event-event pairs for dependency structure+relation prediction on TDG and ContractTDG datasets. DocTime outperforms all baselines on every setting.

D Hyperparameters

Table 8 show the Training hyperparameters of DocTime for TDT, TDG, ContractTDG datasets.

E More Results

Performance across different relation types:

We analyze the benefits of DocTime for different types of relations in document-level TDG datasets in Table 7. We report F1 scores for structure+relation prediction for timex-timex, event-timex and event-event pairs. We observe a relatively smaller performance gap between the BERT Ranking parser and DocTime for event-timex relations. However, DocTime shows relatively stronger performance for event-event relations. This phenomenon can be attributed to the fact that both datasets tend to have event-event links between event pairs that are on an average closer in word distance, whereas a higher ratio of event-timex and timex-timex pairs are several sentences apart. DocTime can integrate long-range interdependencies between entity pairs that are several sentences (or paragraphs in Contract TDG) apart.
| Hyperparameters                      | TDT | TDG | Contract |
|-------------------------------------|-----|-----|----------|
| Dropout Ratio                       | 0.5 | 0.5 | 0.5      |
| Optimizer                           | Adam| Adam| Adam     |
| Input Dimension (Structural Graph)  | (n,768) | (n,768) | (n,768) |
| Input Dimension (Syntactic Graph)   | (n,768) | (n,768) | (n,768) |
| Input Dimension (Semantic Graph)    | (n,768) | (n,768) | (n,768) |
| Hidden Dimension (WR-GCN)           | 256 | 256 | 64       |
| Number of hidden layers (WR-GCN)    | 2   | 2   | 2        |
| Hidden Dimension (BERT-GCN)         | 256 | 256 | 64       |
| Number of hidden layers (BERT-GCN)  | 1   | 1   | 1        |
| Hidden Dimension (HyperGCN)         | 256 | 256 | 64       |
| Number of hidden layers (HyperGCN)  | 2   | 2   | 2        |
| Epochs                              | 20  | 20  | 20       |
| Batch Size                          | 8   | 8   | 16       |
| Learning Rate                       | 2e-5 | 2e-5 | 2e-5    |
| Activation Function of Linear layers| ReLU| ReLU| ReLU     |

Table 8: **Hyperparameters Details**: Training hyperparameters of DocTime for TDT, TDG, ContractTDG