Room temperature Peierls distortion in small diameter nanotubes

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By means of ab initio simulations, we investigate the phonon band structure and electron-phonon coupling in small 4-Å diameter nanotubes. We show that both the C(5,0) and C(3,3) tubes undergo a room temperature Peierls transition mediated by an acoustical long-wavelength and an optical q = 2kF phonons respectively. In the armchair geometry, we verify that the electron-phonon coupling parameter λ originates mainly from phonons at q = 2kF and is strongly enhanced when the diameter decreases. These results question the origin of superconductivity in small diameter nanotubes.

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Superconductivity (SC) has been recently discovered in the 4-Å diameter carbon nanotubes (CNTs) embedded in a zeolite matrix 1 with a transition temperature TC = 15 K, much larger than that observed in the bundles of larger diameter tubes 2. This has stimulated a significant amount of work at the theoretical level to understand the origin of the SC transition 2, 3, 4, 5, 6. While both reduced screening and quantum/thermal fluctuations disfavor superconductivity in 1D systems, early work on fullerenes 7 and nanotubes 8 suggested that the softening of the Raman modes under tube diameter reduction 9.

In 1D systems, the enhancement of the e-ph deformation potential should also favor the occurrence of Peierls, or charge density wave (CDW), transitions driving the system into an insulating phase. This possibility has been explored in early works on the basis of model Hamiltonians 10. The strength of the e-ph coupling was either extrapolated from its value in graphite or taken as an adjustable parameter. The Peierls instability transition temperatures TC\text{CDW} were estimated to be much smaller than room temperature: for instance, Huang et al. 10 find TC\text{CDW} ∼ 9.1 K for a C(5,5) tube. Further, long-wavelength optical 9 or acoustical 11 “opening the gap” phonon distortions have also been explored and the transition temperature was again predicted to be a few degrees Kelvin.

The Peierls transition in 4-Å diameter CNTs has not been addressed explicitly, except for a recent tight-binding exploration of the C(5,0) tube 12 and an ab initio study of the C(3,3) one 13. While the inclusion of electronic screening in the non-self-consistent approach 12 for the C(5,0) case yields a negligible TC\text{CDW}, the ab initio simulations predict for the C(3,3) tube a TC\text{CDW} temperature of ∼ 240 K. These results suggest that the C(5,0) tube is the only candidate for a SC transition at 15 K. However, such a large discrepancy between the two results call for a unified treatment of both nanotubes within a parameter-free approach.

In the present work, we study by means of ab initio simulations the phonon band structure and e-ph coupling in 4-Å diameter CNTs. We show that the C(5,0) and C(3,3) tubes both undergo a Peierls distortion with a critical temperature TC\text{CDW} larger than room temperature. While the distortion is associated with a long-wavelength acoustical mode in the C(5,0) case, the e-ph coupling is dominated by phonons at q = 2kF in the case of C(n,n) nanotubes with a coupling parameter λ which is strongly enhanced with decreasing diameter.

The electronic and vibrational properties are studied within a pseudopotential 14 planewave approach to density functional theory (DFT). We adopt the local density approximation (LDA) and a 50 Rydb cut-off to expand the electronic eigenstates. The phonon modes are calculated at arbitrary q-vectors using the perturbative DFT approach 12 (in what follows q- and k-vectors label phonon and electron momenta respectively). Special care is taken in sampling the electronic states around the Fermi level using an adaptative k-grid technique. The energy levels are populated using either a Gaussian broadening 15 or a Fermi-Dirac (FD) distribution within Mermin’s generalization 16 of DFT to the canonical ensemble. The latter technique explicitly accounts for the effect of temperature. We use a periodic cell allowing for 10 Å vacuum between the nanotubes.

We start by studying the nanotubes band structure after careful structural relaxation with a 25 meV FD distribution broadening (T ~ 300 K). The first important outcome of this calculation is the spontaneous zone-center deformation of the C(5,0) tube 18. From the D10h sym-
FIG. 1: Symbolic representations of the out-of-plane acoustical and optical modes at Γ for the phonon bands driving the Peierls instability in the (a) C(5,0) and (b) C(3,3) tubes, respectively.

FIG. 2: Band structures of (a) the “distorted” $D_{2h}$ C(5,0) nanotube and (b) the C(3,3) tube. The zero of energy has been set to the top of the valence bands and at the Fermi level, respectively.

metry, the structure relaxes to form an elliptic tube ($D_{2h}$ symmetry), as indicated by the arrows in Fig. 1(a), with principal axes of 3.83 Å and 4.13 Å.

The corresponding band structure is provided in Fig. 2(a). As a result of the reduction of symmetry, the repulsion of the hybridized $\sigma$-$\pi$ bands [10] at the Fermi level opens a $\sim 0.2$ eV band gap (LDA value). This implies that the C(5,0) nanotube undergoes a metallic-semiconducting transition with $T_{\text{CDW}}$ larger than room temperature. Following Ref. 8, such a transformation can be referred to as a “pseudo-Peierls” transition since it opens the band gap through a (long-wavelength) structural deformation.

In the C(3,3) case, we do not observe any zone-center deformation leading the band structure away from the well-documented [20] zone-folding picture of two linear bands crossing at the Fermi level $E_F$. However, compared to the zone-folding analysis, the Fermi wavevector $k_F$ is no longer at $2/3$ ΓX but at $\sim 0.58$ ΓX so that $2\pi/2k_F$ is no longer commensurate with the unperturbed lattice (or commensurate with a very large supercell). This is a well documented effect of the curvature.

We further present in Fig. 3(a) the phonon band structure of the C(3,3) tube [21]. The most salient feature is the giant Kohn anomaly [22] at $q = 2k_F$ leading to a dramatic softening of a few phonon modes [20]. In particular, the optical band starting at $620 \text{ cm}^{-1}$ at Γ becomes the lowest vibrational state at $q = 2k_F$ [thick/dotted low lying band in Fig. 3(a)]. The associated atomic displacements, indicated in Fig. 1(b), correspond to an out-of-plane optical mode in agreement with the results of Ref. 12. This is consistent with the analysis provided by Mahan [27]: the coupling of electrons with out-of-plane optical modes should be enhanced away from zone-center and with decreasing diameter. The predominance of such a mode for e-ph coupling is a strong manifestation of the importance of curvature in small diameter tubes.

The value of the associated frequency at $q = 2k_F$ strongly depends on the energy distribution broadening used in the phonon calculation, as clearly illustrated in Fig. 3(a) by the difference between the thick and dotted lines. Using a 25 meV FD distribution ($T \sim 300$ K), we find a negative phonon mode $\omega_{2k_F,v=1}$ of $-200 \text{ cm}^{-1}$. This means that the C(3,3) tube undergoes a Peierls distortion with $T_{\text{CDW}}$ larger than room temperature [23]. Consequently, at the mean-field SC transition temperature measured for the 4 Å diameter CNTs ($T_{\text{SC}}=15$ K), the C(5,0) and C(3,3) tubes should both be semiconducting, seriously questioning the origin of superconductivity in small diameter tubes.

Our results are in good agreement with those of Ref. 13 concerning the C(3,3) tube, but contrast significantly with those based on a model for the interaction Hamiltonians and the electronic susceptibility [12]. We emphasize that our self-consistent treatment automatically includes the renormalization of both the e-ph and e-e interactions by electronic screening at the DFT level.

To study the influence of tube diameter on the soften-
the phonon band structure of the C(n,n) tubes with n=4 and 5. Again, we observe that the same optical band (thick low lying band) is softened at 2 and 5 \(\text{cm}^{-1}\). Again, we observe that the same optical band (thick low lying band) is softened at 2 and 5 \(\text{cm}^{-1}\). We limit ourselves to identifying the relevant phonon band structure of the C(3,3) tube. When the tube diameter decreases, however, the variation of the coupling varies from one band to another and is enhanced with the tube diameter decreases. However, the variation of the coupling varies from one band to another and is enhanced with the tube diameter decreases. However, the variation of the coupling varies from one band to another and is enhanced with the tube diameter decreases. However, the variation of the coupling varies from one band to another and is enhanced when the tube diameter decreases. However, the variation of the diameter differs from one mode to another and it is difficult to extract a simple scaling law. To further quantify the strength of the e-ph interaction, we can calculate the e-ph coupling matrix elements \(g_{\nu}(qk)\) and the coupling constant \(\lambda\):

\[
\lambda = \sum_{q,\nu} \lambda_{\nu,q} = 2N(E_F) \sum_{q,\nu} < |g_{\nu}|^2 > /\hbar \omega_{\nu,q} \tag{1}
\]

\[
< |g_{\nu}|^2 > = \int \frac{dk}{L_BZ} \sum_{n,n'} |g_{\nu}(qk)|^2 \frac{\delta (\omega_{k+n}) \delta (\omega_{k-n})}{N(E_F)^2}
\]

\[
g_{\nu}(qk) = \left( \frac{\hbar}{2M \omega_{\nu,q}} \right)^{1/2} < \psi^{\alpha}_{n}(qk) \omega_{\nu,q} \frac{\delta V}{\delta \omega_{\nu,q}} \psi^{\beta}_{n}(qk) \tag{3}
\]

Due to conservation of energy and momentum, only vibrational states around \(q = \Gamma\) and \(2k_F\) contribute to \(\lambda\), as the nesting factor \(n(q)\) quickly decays away from these points. At \(\Gamma\), only four modes contribute to \(\lambda\) due to symmetry considerations. They are the radial breathing mode (RBM), the optical out-of-plane (ZO) mode, and the in-plane optical longitudinal \(A_1(\text{L})\) and transverse \(A_1(\text{T})\) (G-band) modes (see Ref. 3) located respectively at 536 \(\text{cm}^{-1}\), 692 \(\text{cm}^{-1}\), 1354 \(\text{cm}^{-1}\) and 1431 \(\text{cm}^{-1}\) in the C(3,3) tube.

In Table I we report the parameter \(\lambda(\nu,q \subseteq \{\Gamma\})\) defined as the \(q\)-sum of all the \(\lambda_{\nu,q}\) (see Eq. 1) for \(q\) in the neighborhood of \(\Gamma\) on a given \(\nu\)-band [30]. This coupling strength varies from one band to another and is enhanced when the tube diameter decreases. However, the variation with the diameter differs from one mode to another and it is difficult to extract a simple scaling law.

We now discuss the e-ph coupling at \(q = 2k_F\). The strong variation of the lowest frequency \(\omega_{2k_F,\nu=1}\) with temperature raises the question of the meaning of \(\lambda_{2k_F,\nu=1}\) calculated with the \(g_{\nu}\) and \(\omega_{\nu}\) values obtained from \textit{ab initio} calculations. The difficulties have been clearly exposed in Ref. 12. If one is interested in studying the SC transition, one faces the difficulty that at the experimental T\(_{SC}\), the self-consistent \(g_{2k_F,\nu}\) and \(\omega_{2k_F,\nu}\) values are those of the CDW phase. As T\(_{CDW}\) is larger than any realistic SC transition temperature, we will not attempt to estimate T\(_{SC}\) with e-ph vertices and ph-propagator properly “undressed” from the CDW instability 12. We limit ourselves to identifying the relevant modes and providing the values for \(\lambda_{2k_F,\nu=1}\) obtained above T\(_{CDW}\), which are those that matter for transport measurements in the normal state.

While the \(g_{2k_F}\) parameters are rather stable with temperature above T\(_{CDW}\), the phonon frequencies still vary significantly. Following Ref. 12, we provide an upperbound for \(\omega_{2k_F,\nu}\) by removing the Kohn’s anomaly. Namely, we assume that around \(q = 2k_F\),

\[
\omega_{2k_F,\nu}^2 = (\omega_{2k_F,\nu}^0)^2 + A \times \ln \left[ (q - 2k_F)/(q + 2k_F) \right] \tag{4}
\]

and fit the \(\omega_{2k_F,\nu}^0\) bands by a cubic polynomial for \((\omega_{2k_F,\nu}^0)^2\) plus the logarithmic term that we subtract to obtain the bare phonon frequency. The important “undressed” bands (corresponding to \(\omega_{2k_F,\nu}^0\) are represented by dashed lines in Fig. 3(a). The related frequencies and \(\lambda_{2k_F,\nu}\) values are underlined in Table I This treatment is applied to both states presenting the largest Kohn anomaly, but its effect is clearly more pronounced for the low-lying \(\nu = 1\) band.

Using the \(\omega_{2k_F,\nu}^0\) frequencies leads to providing a lower bound for the corresponding \(\lambda_{2k_F,\nu}\) e-ph parameter. Even in that limit, we observe that the coupling with modes at \(q = 2k_F\) is significantly larger than with long-wavelength phonons. As at zone-center, few modes with \(q = 2k_F\) couple to the electrons and the strength of the coupling is significantly enhanced with decreasing diameter. In the C(3,3) case, we obtain in the undistorted phase a density of states \(N(E_F) = 0.4\) states/eV-cell-spin, yielding an e-ph potential \(V_{\nu e} = \lambda/N(E_F) = 440\) meV. This is larger than that in the fullerenes (60-70 meV), but it is not sufficient to lead to any significant T\(_{SC}\) value. The much larger density of states in the “D10h” C(5,0) tube \((N(E_F) = 1.8\) states/eV-cell-spin)
may lead in principle to a large $T_{SC}$ value. However, as shown above, the prevailing structure around the experimental $T_{SC}$ temperature is the insulating $D_{2h}$ one.

In conclusion, we have shown that the “metallic” C(5,0) and C(3,3) nanotubes undergo a Peierls transition with a critical temperature larger than 300 K. Our results are derived within Mermin’s generalization of DFT to finite temperature systems and do not rely on models for the e-ph interactions nor the electronic susceptibility. Additional physical ingredients (interaction with the zeolite network, possible defective structure, Luttinger liquid character, etc.) might reconcile these results with the experimentally observed SC transition at $T_{SC}$=15 K.

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[30] The domain of integration is defined by the extent of $n(q)$ around $\Gamma$. We have observed that $\lambda(q, \nu)/n(q)$ is nearly independent of $q$ in this domain. This greatly helps in calculating $\lambda$ as $n(q)$ can be calculated with arbitrary precision by fitting the electronic bands around $\pm k_F$. 

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