A Hybrid Feature Selection Framework for Predicting Students Performance

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Abstract: Student performance prediction helps the educational stakeholders to take proactive decisions and make interventions, for the improvement of quality of education and to meet the dynamic needs of society. The selection of features for student’s performance prediction not only plays significant role in increasing prediction accuracy, but also helps in building the strategic plans for the improvement of students’ academic performance. There are different feature selection algorithms for predicting the performance of students, however the studies reported in the literature claim that there are different pros and cons of existing feature selection algorithms in selection of optimal features. In this paper, a hybrid feature selection framework (using feature-fusion) is designed to identify the significant features and associated features with target class, to predict the performance of students. The main goal of the proposed hybrid feature selection is not only to improve the prediction accuracy, but also to identify optimal features for building productive strategies for the improvement in students’ academic performance. The key difference between proposed hybrid feature selection framework and existing hybrid feature selection framework, is two level feature fusion technique, with the utilization of cosine-based fusion. Whereas, according to the results reported in existing literature, cosine similarity is considered as the best similarity measure among existing similarity measures. The proposed hybrid feature selection is validated on four benchmark datasets with variations in number of features and number of instances. The validated results confirm that the proposed hybrid feature selection framework performs better than the existing hybrid feature selection framework, existing feature selection algorithms in terms of accuracy, f-measure, recall, and precision. Results reported in presented paper show that
the proposed approach gives more than 90% accuracy on benchmark dataset that is better than the results of existing approach.

**Keywords:** Educational data mining; feature selection; hybrid feature selection

1 Introduction

Education is one of the main pillars of society. It polishes the character and intelligence of students. Current education system may not be suitable for the new and dynamic needs of the society. One major aspect of the new paradigm of the education system is to predict student performance beforehand. As the students are the main stakeholders of the educational systems, therefore by analyzing the student’s data and developing different predictions from it, academic organizations may meet the dynamic needs of the society. Moreover, the results of predictions can be helpful for making strategies to improve the quality of education. The better-quality education supports in building the skillful and featureful students. This gives the attention to analyze the academic data. Student performance prediction models help in analyzing the student data with the help of different data mining techniques. Furthermore, to facilitate student performance prediction, many student performance prediction models have been proposed. Student performance prediction models have received a significant amount of contemplation from both the research community and educational sector. Student performance prediction models tackle the problem of prediction of student grades [1], GPA (Grade Point Average) [2], CGPA [3], and Pass/Fail Course [4]. The goal of students’ performance prediction models in EDM (Educational Data Mining) is not only to achieve the high accuracy of prediction models but also to help the educational stakeholders in predicting the performance of students. The students are the main assets of any community and the main aim of any academic organization is to provide the quality education to its students. Moreover, the quality education supports in building the skillful and featureful students. Student performance prediction models help in analyzing the student data with the help of different data mining techniques. A lot of work has been done on the development of students’ performance prediction models. There are two main methods of developing student performance prediction models. One is supervised, and another is the unsupervised method. Classification is a type of supervised learning method. According to [5] around 71.4% of research articles on students’ performance prediction models are using a classification method. It is the top method for the performance prediction models [6]. In the classification method, the target variable is clearly defined as that which we want to predict whether grades, GPA, CGPA, or students PASS/FAIL. This motivated us to focus on the students’ performance prediction model with the help of the classification method.

Feature selection can play a prominent role in enhancing the accuracy of a prediction model. In student’s prediction model, the selected features play an important role not only in increasing the prediction accuracy but also in providing the base for the strategic plans for the educational environment. According to [7] information gain attribute evaluator is the best feature selection technique to improve the effectiveness of student prediction model. Whereas, [8] claims CFS subset evaluator as the best feature selection method for predicting the final semester examination performance of students. According to [9] there is not one common feature selection method which can be accurate for all datasets even for a common domain. There is a need to focus on the feature selection algorithms in the area of predicting the performance of students. The third main type of feature selection is hybrid feature selection, which combines the advantages of filter and wrapper feature selection. Unfortunately, there is only a single framework for hybrid feature selection.
The importance of feature selection methods in predicting students' performance, motivated us to develop a feature selection framework for students' performance prediction with better prediction accuracy. Furthermore, the design of existing hybrid feature selection framework also motivated us to focus on hybridization of feature selection algorithms to build a robust feature selection framework for student performance prediction.

Contributions: Followings are the contributions of this research in the domain of Educational Data Mining.

(a) First different benchmark datasets have been used to predict the student’s performance using feature selection.
(b) Second, importance of hybrid feature selection has been explored by comparing the results of hybrid feature selection algorithm, filter and wrapper on various students’ benchmark datasets.
(c) Limited work was done in students’ performance prediction using hybrid feature selection.
(d) A novel hybrid feature selection framework is proposed to predict the performance of students, with better results than existing hybrid feature selection method [10].

A lot of work has been done on the development of students’ performance prediction models. But the study of student’s prediction models is still inadequate in predicting the performance of students [11,12], especially in terms of prediction accuracy. So, this motivated us to focus on developing a feature selection framework for predicting the performance of students. Furthermore, this motivated us to build a feature selection framework that can be helpful for building a student performance prediction model, to help the educational stakeholders. This will not only be helpful for academic organizations to build strategic plans accordingly but also with the help of proposed hybrid feature selection framework, we can go to the next level of the education system which fulfills the needs of the current and futuristic society.

2 Literature Review

Improving the quality of education is one of the challenges for the educational institutions, the improvement in the quality of education is not only required for assembling a higher level of knowledge, but also providing effective facilities of education that can help students in achieving their academic objectives without any problem [13–15]. Identification of factors affecting the performance of students is very important to improve the quality of education [16]. Student performance prediction models help the educational institutions to increase the quality of education by analyzing the student’s data to make the academic strategic plans for the improvement of the student’s academic performance [17]. However the study on student performance prediction is still insufficient [11]. The performance of student prediction model mainly depends on the selected features from the under-considered dataset [18]. Feature selection helps in identification of suitable features from a dataset and hence very important for the student performance prediction models [19–23]. The main focus of existing feature selection methods in EDM is to improve the prediction accuracy of student performance prediction model henceforth, only focusing on the feature’s association with the target class. There are mainly two types of feature selection algorithms, filter, and wrapper feature selection algorithm. The main focus of existing student performance prediction models [24–28] is on using filter feature selection algorithm, and these existing feature selection algorithms have issues of ignoring dependencies and associative features (interaction of features with the classifier) [29]. The emphasis of existing research on student performance prediction using feature selection is on reducing the number of features to improve the prediction
accuracy of the model. The two main types of feature selection algorithms, filter and wrapper both have different pros and cons. Hybrid feature selection takes the advantages of both filter and wrapper feature selection approaches [30]. Hybrid feature selection IFSFS [30], is the hybridization of filter and wrapper feature selection algorithms and was proposed to diagnose the erythema to-squamous diseases. Hybridization of SU (Filter feature selection) and backward search strategy as a wrapper has various applications including hypertension diagnosis [31,32], prediction of the type of cancer in a cancer patient [33,34], bioinformatics [35], credit scoring [36,37] as well as in other domains [38]. The existing hybrid feature selection models in different domains of research try to retrieve the optimal features to obtain high prediction accuracy. But they have the foremost limitation in the flow of feature identification, as the features ignored in such hybrid feature selection methods are neither be evaluated in other levels. To the best of our knowledge, there exists a hybrid feature selection framework in EDM to predict the performance of students [39]. The existing hybrid feature selection is the combination of FCBF (filter feature selection) and SFS (wrapper feature selection), but it has the limitation of ignoring feature dependencies, and ignorance of highly associated features in the first phase of hybridization, and the problem in the flow of hybridization strategy, as one feature removed can never be evaluated further in the hybridization flow.

The identification of features from the student performance prediction to help the educational stakeholders is still a problem [40]. The reason for this is that the existing features selection algorithms lack in optimal identification of features. Majority of approaches in student performance prediction are based on the filter feature selection, hence the chance of ignoring uniquely associated features with the target class is high. The importance of hybridization in terms of utilizing the advantages of filter and wrapper feature selection gives the motivation to build a hybrid feature selection framework to obtain optimal features. The selected features for predicting the performance of students plays a vital role in building the strategic plans for the improvement in the quality of education, which in return can result in positive changes in the performance of students. So, the features identified through the educational datasets must not only be associated with the target class, but they must also be significant. The importance of feature significance and association with the target emphasizes on the integration of such type of features in a student dataset. It is necessary to remove the redundant features from a dataset, as well as keeping the associated and significant features in focus. Also, there may be features that can have the significant as well as associated feature properties, and these features must not be ignored during feature selection. Ignoring an optimal feature may lead to non-productive strategic plans for the improvement in the quality of education.

3 Methodology

The Fig. 1 describes the main process of the proposed optimized feature selection method for predicting the performance of students. The main phases of the proposed method are the identification of significant features and identification of highly associated features with the target class. The significant features and highly associated features are fused into a new hybrid feature vector by using early level feature fusion technique. The cosine feature selection equation is formulated to calculate the weights of significant features and the highly associated features. The proposed optimized feature selection method has given the concept of selecting the significant feature, associated feature, and hybrid feature. Whereas the proposed method defines hybrid features that are not only significant but also have an association with the target class. To obtain the optimized
features, the main steps of the hybrid feature selection framework using feature-level strategy are listed below along with a brief description.

**Figure 1:** Hybrid feature selection framework with feature fusion

### 3.1 Identification of Significant Features

Filter feature selection algorithm is performed in this step. The details of the step are explained in coming sections. Chi-square feature selection is used to statistically test the independence of a feature with the class label. It is being computed in different prediction models \[41,42\] to predict the student’s performance. In the proposed approach the chi-square feature selection algorithm is adjusted to compute the test of independence of the feature \(s_{fi}\) and class \(sc_{j}\).

If \(X^2(s_{fi},sc_{j}) = 0\) \hspace{1cm} (1)

Then the feature \(s_{fi}\) and the class \(sc_{j}\) are independent. This means that the feature \(s_{fi}\) does not contain any category information. Larger values of \(X^2(s_{fi},sc_{j})\), indicates the importance of category information the feature \(s_{fi}\) owns. Chi-square formula is presented through \textbf{Eq. (2)}.

\[
X^2(s_{fn},sc_{m}) = \frac{N(r_{nn}q_{nm} - p_{nn}s_{ij})^2}{(o_{ij} + p_{ij})(o_{ij} + s_{ij})(p_{ij} + q_{ij})(s_{ij} + q_{ij})} \tag{2}
\]
N is the total no of instances (students). The \( r_{ij} \) is the frequency that the feature \( sfv_i \) and the category \( sc_j \). \( pij \) is the frequency that features \( sfv_i \) occurs and does not belong to category \( sc_j \). \( cij \) is the frequency that category \( ci \) occurs and cannot contain feature \( sfv_i \). \( qij \) shows number of times neither \( sci \) nor \( sfv_i \) occur. So that mathematical equation of feature vector containing significant features \( Edf \) is presented through Eq. (3).

\[
Edf = \sum_{j=1}^{m} \sum_{i=1}^{n} X^2(sf v_n, sc_m) \quad (3)
\]

\( X^2(sf v_n,sc_m) = sfv(Edf) = X^2(sf v_i, sc_j) \neq 0 \)

Whereas \( Edf \) contains all \( sfv \) having the value of \( X^2 (sfv_i, sc_j) \) greater than zero. Whereas Eq. (4) presents the feature vector containing associated features.

\[
Edf = \{ f_{d1}, f_{d2}, f_{d3}, \ldots, f_{dn} \} \quad (4)
\]

### 3.2 Identification of Associated Features (Wrapper)

The second step is the identification of features associated with the target class. This step not only identifies the features with a high association with the target class, but also the dependencies between the features. This is not only important for the students but also for the teachers, as they may guide teachers to improve their capabilities in order to increase the quality of education [43]. To identify the associated features, SFS wrapper feature selection is computed. SFS feature selection is a heuristic search algorithm, that start with an empty set [44]. Each of the features in feature matrix \( SD_m \) is evaluated through SFS feature selection, wrapped by the SVM classification algorithm. Each of the features does the 10-cross-validation and calculates the average accuracy of the 10-cross-validation. The highest accuracy that is the least minimum of the functions that determines whether the evaluated feature should be added to the feature association vector. To identify the associated features with the target class, SFS wrapper feature selection is computed. SFS feature selection is a heuristic search algorithm, that start with an empty set [44]. Each of the features in feature matrix \( SD_m \) is evaluated through SFS feature selection, wrapped by the SVM classification algorithm. Each of the features does the 10-cross-validation and calculates the average accuracy of the 10-cross-validation. The highest accuracy that is the least minimum of the functions that determines whether the evaluated feature should be added to the feature association vector. The features selected by sequential forward search (SFS) in each of the rounds are evaluated through the wrapped classifier SVM. The features with high prediction accuracy in each of the round are selected. In order to avoid the overfitting issue, data is divided into 10 equal folds by 10-cross-validation. The feature with high accuracy in 10-folds is highly associated with the target class. And on each of the round, the selected features are added in \( Eaf \) feature vector. The feature vector \( Eaf \), contains the features associated with the target class, and is represented through Eq. (5):

\[
Eaf = \{ f_{a1}, f_{a2}, f_{a3}, \ldots, f_{an} \} \quad (5)
\]

### 3.3 Fusion of Significant and Associated Features Using Early-Level Feature Fusion Technique

The significant and associated features are fused using the early-level feature fusion strategy. The academic decisions based on these features can play a vital role in the improvement of quality education. Fusion of features is performed at two levels.

i. Level 1: Identification of projected features using cosine weighting.
ii. Level 2: Identification of highly associated features. Fusion is termed as the integration of different types of features in the process of feature selection [45]. There are different types of fusions, data fusion, decision fusion, and feature-level fusion. The main task of the proposed approach is related to features, therefore feature fusion is computed in the proposed approach, and furthermore, feature fusion is computed in different domains due to its simplicity. Feature Fusion is a technique in which different feature sets are fused into a single feature set/presentation. The main advantage of feature fusion is that the new union feature not only keeps the information about the feature but also eliminates the redundant information to a certain degree [46].

The selection of feature-level fusion helps in computing the hybrid feature selection mainly in two folds.

a) The main intention of proposed work is to develop a feature selection method that may identify the most dominating factors affecting the performance of students, feature-level fusion has the ability to derive the most important features from the feature sets involved in the fusion [45,47]. Therefore, taking this advantage in the account, the proposed approach adapted feature fusion.
b) Feature fusion can eliminate the redundant features [47]. As the redundant feature might affect the prediction accuracy of student performance models. So, this might help in elevating the prediction accuracy of the hybrid feature selection frame for student performance prediction.

Early-level fusion and late-level fusion are two main feature fusion strategies. However, late-level fusion is expensive in terms of learning efforts as it requires learning algorithm on each of the steps. Whereas late feature fusion also has an issue of the potential loss of correlation in fused space [48]. Combining the two feature vectors for prediction models is a challenging task. Early-level fusion is one of the feature-level fusion strategies to perform concatenation of two feature sets in a common feature vector [49]. In sum, the feature obtained through late-level feature fusion are highly associated with the target class. Whereas the main focus of the proposed approach is not only highly associated features with the target class but also feature dependencies and significance of features are also taken into account. As to make the proactive decision for the improvement in students’ performance and building different academic strategical plan the student data must be analyzed properly. So that early-level fusion strategy is adapted to fuse the significant feature vector $Ed_f$ and associated feature vector $Eaf$. This may lead towards the optimal selection of features for predicting the academic performance of students. Cosine similarity measure is used to calculate the similarity between the two vectors [50]. Similarity between the two vectors is computed by the cosine of the angle between the two vectors. There are different approaches for predicting the similarity between two vectors, these approaches include, cosine similarity, Jaccard coefficient, Spearman distance, etc. Out of all above-mentioned approaches cosine similarity is proven to work best [51–53], and also have retrieval effectiveness than other similarity measures. Whereas the existing similarity measures have the drawback that they give dominance to largest scale feature, and also existing similarity measures are sensitive to outlier [54]. Furthermore, the existing similarity measure is not the best choice when the similarity relations are complex [52]. Cosine similarity is used to measure the similarity between two vectors in different domains like pattern recognition face recognition [55], text classification [56], search engines [57]. Cosine similarity weights are computed to identify the optimal features and fusion of features vectors by tuning the parameters of cosine similarity measure in the proposed hybrid feature selection
framework. The weights are given to different features based on the similarities between these features. The fusion of the feature vectors $Edf$ and $Eaf$ is computed in two levels. Fig. 2 reflects the whole fusions step in proposed hybrid feature selection framework.

![Figure 2: Flow of fusion steps in hybrid feature selection framework](image)

### 3.3.1 Level 1: Identification of Projected Features Using Cosine Weighting

In this section, the level 1 of feature fusion technique for hybrid feature selection framework is explained in detail. The cosine similarity measure is the best choice as compared to the other similarity measures because of its ability of effectiveness and dealing with complex similarities. Fig. 3 shows a block diagram of the process of identification of hybrid features by fusing significant feature vector $Edf$ and associated feature vector $Eaf$ using cosine weights cpfw.

In the first step, the projected features $p$ are identified from the feature vectors. Whereas it is assumed that the projected features are defined as the features having a projection in $Edf$ and $Eaf$. So, hybrid features are highly important features as they may have highly associated with the target class as well as significant. Initialize a feature vector $daf$ as an empty feature vector. Whereas $daf$ is denoted as feature vector contacting projected features. Let $daf = \Phi$

Referring to section III.A, Eq. (4), $Edf$ presents a feature vector containing significant features.

$Edf = \{fd_1, fd_2, fd_3, \ldots, fd_n\}$
Figure 3: Block diagram of level1 of projected feature selection framework using fusion

Referring to section III.B, Eq. (5), \( E_{af} \) presents feature vector containing associated features. 
\[
E_{af} = \{ f_{a_1}, f_{a_2}, f_{a_3}, \ldots, f_{a_n} \}
\]

Cosine similarity weights are introduced to identify the projected features \( p_{af} \) with the fusion \( E_{df} \) and \( E_{af} \). The similarity between the two feature vectors can be measured using cosine similarity technique [58]. Eq. (6) presents the cosine similarity equation for the identification of projected features.

\[
c_{pfw} = \text{sim}(E_{df}, E_{af}) = \frac{E_{df} \cdot E_{af}}{|E_{df}| |E_{af}|}
\]

where \( E_{df}, E_{af} = \{ f_{d_1} f_{a_1}, f_{d_2} f_{a_2}, \ldots, f_{d_n} f_{a_n} \} \) and values of \( \text{sim}(f_{a_i}, f_{d_i}) \) will either be 0, or 1.

a) If \( \text{sim}(f_{d_i}, f_{a_i}) = 0 \) then \( c_{pfw} = 0 \) and \( f_{d_i} = c_{pfw} \) & \( f_{a_i} = c_{pfw} \). Furthermore, \( f_{d_i} \) and \( f_{a_i} \) are ignored in this step.

b) If \( \text{sim}(f_{d_i}, f_{a_i}) = 1 \) then \( c_{pfw} = 1 \) and \( f_{d_i} = c_{pfw} \) & \( f_{a_i} = c_{pfw} \)

Therefore, this feature is added as a projected feature in projected feature vector \( d_{af} \).

The above mentioned point a, presents that if the similarity between two features say \( f_{d_i} \) and \( f_{a_i} \) from feature vector \( E_{df} \) and \( E_{af} \) is 0, then it indicates that feature is not similar so that they are ignored. Whereas line 2 presents that if the similarity between two features say \( f_{d_i} \) and \( f_{a_i} \) from feature vector \( E_{df} \) and \( E_{af} \) is 1, then it indicates that feature is similar so that they are added to
projected feature vector $daf$. So that projected feature vector $daf$ contains all the projected feature with $cpf_w = 1$.

3.3.2 Level 2: Identification of Highly Significant Feature ($Edf^+$) and Identification of Highly Associated Features ($Eaf^+$)

The level 2 of feature fusion step in proposed hybrid feature selection framework identifies the highly significant and highly associated feature with the fusion of significant feature vector $Edf$, associated feature vector $Eaf$, and projected feature vector $pf$ feature vectors using cosine feature weights. Whereas Fig. 4 explains the identification of $Edf^+$ and $Eaf^+$ by using cosine feature weights. Basically, the level 2 of feature fusion in hybrid feature selection framework further consists of two steps, in first step uniquely significant features are identified. Whereas in the second step uniquely associated features are identified.

![Figure 4: Block diagram of level 2 of hybrid feature selection framework using fusion](image)

**Uniquely significant feature identification:** $Edf^+$ is initialized as an empty set. Whereas $Edf^+$ is considered as a feature vector, containing all uniquely significant features, especially these features are not projected over associated features. Referring to equation, $Edf$ presents a feature vector containing significant features.

\[ Edf = \{f_{d1}, f_{d2}, f_{d3}, \ldots, f_{dn}\} \]
 presents projected feature vector, and \( cpfw \) is the weight of projected features in \( \text{daf} \). fusion of \( \text{Edf} \) and \( \text{daf} \) using \( csfw \). whereas \( csfw \) is the cosine weight for uniquely significant features. Eq. (7) presents the cosine weight for uniquely significant features.

\[
csfw = \text{Edf} - cpfw \tag{7}
\]

where Eq. (8) presents the cosine weight for uniquely significant feature identified from \( \text{Edf} \) and \( \text{daf} \).

\[
cpfw = \frac{\text{sim}(\text{Edf} , \text{Eaf})}{||\text{Edf}||||\text{Eaf}||} = \frac{\text{Edf} . \text{Eaf}}{||\text{Edf}||||\text{Eaf}||} \tag{8}
\]

The values of \( csfw \) will either be 0 or 1.

a) If \( csfw == 1 \) then \( fd_i = csfw \), so that feature \( fd_i \) is ignored and not added to \( Edf^{+} \).

b) If \( csfw == 0 \) then \( fd_i = csfw \), so that \( fd_i \) is added in \( Edf^{+} \) feature vector.

Line 1 shows that if the value of \( csfw \) become 1, then it shows the similarity between the features in \( \text{Edf} \) and feature in \( \text{daf} \). So that feature is not considered as a uniquely significant feature. Whereas line 2 shows that if the value of \( csfw \) is 0, the feature has no projection, so that is considered a uniquely significant feature, and hence added to \( Edf^{+} \). In sum, the projections of \( \text{daf} \) feature vectors are compared with \( \text{Edf} \) in this step. The similarity between the weights of the \( \text{Edf} \) and \( \text{daf} \) is checked in such a way that features having no projections with associated feature vectors are added in the \( \text{Edf}^{+} \) feature vector.

\( Edf^{+} = \) Feature vectors contains uniquely significant features.

Uniquely associated feature identification : \( \text{Eaf}^{+} \) is initialized as an empty set. Whereas \( \text{Eaf}^{+} \) is considered as a feature vector, containing all uniquely associated features. \( \text{daf} \) is compared with \( \text{Eaf} \). The similarity between the features of the \( \text{Eaf} \) and \( \text{daf} \) is checked in such a way that the features having similarity will be computed in \( \text{Eaf}^{+} \) feature vector. Referring to section III.B, Eq. (5), \( \text{Eaf} \) presents feature vector containing associated features.

\[ \text{Eaf} = \{fa_1, f a_2, f a_3, \ldots, f a_n\} \]

Fusion of \( \text{Eaf} \) and \( \text{daf} \) using \( cafw \). Whereas \( cafw \) is the cosine weight for the uniquely associated features. The Eq. (9) presents the mathematical equation for calculating the uniquely associated features.

\[
cafw = \text{Eaf} - cpfw \tag{9}
\]

where Eq. (10) presents the cosine weight for identifying the \( i \)th feature.

\[
cafwi = \text{Eafi} - \frac{f d_i . f a_i}{||f d_i||||f a_i||} \tag{10}
\]

And values of \( cafw \) either 0, or 1. i. If \( cafw == 1 \) and \( fa_i = cafw \) . Furthermore, \( fa_i \) and \( dafi \) are ignored, ii. If \( casfw == 0 \) and \( fa_i = cafw \), then \( fa_i \) is added in \( \text{Eaf}^{+} \) feature vector. \( \text{Eaf}^{+} = \) Feature vectors having features uniquely associated features with the target class .In sum line 1 shows that if the features are projected on significant features with the target class, then they are neglected and not added to the \( \text{Eaf}^{+} \). Whereas line 2 shows that the features are considered as uniquely associated as having no projections on significant features, and hence such features are
added to $Eaf^+$. As a result of level 1, level 2 of feature fusion three types of feature vectors are identified $Edf^+$, $Eaf^+$, and $daf$.

### 3.4 Model Training

The features are further training using SVM classification algorithm. SVM is selected in the proposed approach due to its high generalization ability and history of achieving high accuracy in datamining [59]. 10-fold cross validation is performed to evaluate the robustness of proposed hybrid feature selection framework, and high-frequency feature matrix is obtained by applying the frequency criterion. The hybrid features are divided into ten folds using 10-fold cross-validation. Whereas the model is trained using the SVM classification algorithm. The SVM classification algorithm is being used due to its flexibility in dealing with educational parameters in prediction models [60,61]. SVM linear kernel is adjusted with the help of the optimization function of the linear kernel function. The Eq. (11) presents SVM linear kernel function is [62]:

$$K(x_n, x_i) = (x_n, x_i)$$

The kernel functions have the ability to whereas, SVM kernel functions have the ability to transform the dataset space into a high dimension. Each of the kernels has optimized function to obtain high performance [63]. For SVM linear kernel the penalty value $C$ is an optimized function. The value of $C$ is optimized to obtain a better classification prediction for the proposed approach. Furthermore, the selected features are trained on SVM linear kernel and then tested and evaluated through different evaluation measures. The detailed of each of the evaluation measure is explained in next section.

### 3.5 Evaluation Measures

The performance of the proposed approach is measured through prediction accuracy, precision, recall, and f-measure. These evaluation matrices are widely used in different domains such as information retrieval, machine learning, sentiment analysis and EDM [34,61]. Let $D$ be a student dataset, containing “n” number of features for “m” number of students. Let $SD_m$ be n-size student data feature matrix; the size of the feature vector for each example within data matrix $SD_m$ is “n” and “m” is the number of examples. Each feature of the vector contains data related to the students’ information relevant to his/her educational activity.

### 3.6 Size of $S$ Feature Vector = Size of Feature Vector

Dimension of feature matrix=Number of examples in dataset $D$.

$$SD_{m,n} = \{sf v_{1,1}, sf v_{1,2}, sf v_{1,3}, \ldots, sf v_{1,n}$$

$$sf v_{2,1}, sf v_{2,2}, sf v_{2,3}, \ldots, sf v_{2,n}$$

$$sf v_{3,1}, sf v_{3,2}, sf v_{3,3}, \ldots, sf v_{3,n}$$

$$\ldots$$

$$sf v_{m,1}, sf v_{m,2}, sf v_{m,3}, \ldots, sf v_{m,n}\}$$

Hybrid feature selection framework using fusion is evaluated on prediction accuracy, precision, recall, and f-measure evaluation measures. The detail of this topic is explained further, **Prediction Accuracy**: Accuracy is the ratio between the correct predictions. The Eq. (13) shows the accuracy formula for evaluation of hybrid feature selection framework with fusion. It is used to measure
the effectiveness of the prediction model. However, how minority classification of minority classes cannot be shown by accuracy evaluation measure. Also, accurately predicting the positive outcome is not adequate.

\[
\text{Accuracy} = \frac{\text{Number of students correctly classified by the proposed framework}}{\text{Total number of students}}
\]  
(13)

\[
\text{Recall} = \frac{\text{Number of Pass students classified by the Proposed framework}}{\text{Total number of pass students}}
\]  
(14)

Recall and Precision: As a good prediction model must have successful positive and successful negative predictions as well. Henceforth precision and recall evaluation measure is also used to evaluate the proposed hybrid feature selection framework. Eqs. (14) and (15) present the recall and precision calculations for the evaluating the proposed hybrid feature selection framework.

\[
\text{Precision} = \frac{\text{Number of Pass students identified by the Proposed framework}}{\text{Total number of pass students classified by the proposed framework}}
\]  
(15)

\[
F - \text{Measure} = \frac{2 \times (\text{Precision} \times \text{Recall})}{\text{Precision} + \text{Recall}}
\]  
(16)

F-measure: It considers both precision and recall. The results are also evaluated through the, to get the classification of instances with respect to the target class. equation presents the mathematical Eq. (16) for calculating f-measure. In sum, these evaluation measures can give a deeper insight into the performance of the proposed hybrid feature selection framework. So that proposed hybrid feature selection is not only validated in terms of accuracy, but also in terms of precision, recall, and f-measure. This section presented the proposed hybrid feature selection framework using fusion. Each level of the proposed framework is discussed in detail. The methodology of identification significance features, identification of associated features and identification of projected features towards significance and associated features is discussed in detail. Furthermore, the cosine-based feature fusion through cosine weighting is explained in detail. This section also discusses the model training and evaluation measures that evaluate the proposed approach. The next section presents the simulation results of the proposed approach on benchmark students’ datasets.

4 Result and Discussion

To check the robustness of a hybrid feature selection, a dataset with a varying number of features and instances are required. Henceforth to empirically evaluate the proposed hybrid feature selection framework using fusion, four benchmark datasets of students’ academic records from different educational domains are selected, to check the robustness, as the robustness in feature selection can be evaluated through variations in the number of instances or variations in the number of features [64]. These four datasets sets are benchmark datasets and are publicly available. The dataset acquired from different databases have different attributes from each other, hence presents a different set of challenges which have not been studied altogether previously. Four
different student’s benchmark datasets have been used in the proposed research, due to their diversity in nature of datasets in terms of a number of features, no of instances and belonging to different areas of education, to show the robustness of the proposed hybrid feature selection framework for student performance prediction.

The Tab. 1 presents a brief description of four benchmark datasets, related to variations in number of instances, and number of features. The number of instances in student datasets actually presents the number of records in a particular dataset. Tab. 1 shows the number of instances in Math, LMS, CS, and PLang datasets. PLang dataset contains 649 number of instances (records of students) that are greater in a number of instances than other three datasets. Furthermore, Tab. 1 shows that CS dataset contains the smallest number of instances as compared to other datasets. The reason for selecting datasets having different instances and different attributes is to evaluate the proposed framework in terms of its performance being robust or otherwise. Tab. 1 shows the number of features in Math, LMS, CS, and PLang dataset. It shows that Math and PLang dataset contains 32 number of features, however, these two datasets have a different number of instances as shown in Tab. 1. Furthermore, LMS dataset contains 16 features, and CS contains the smallest number of features as compared to the other three datasets. Hence, Math, LMS, CS and PLang dataset different from each other in terms of a number of students’ records present in them and number of features/attributes in these four datasets.

Table 1: Dataset’s description in brief

| Dataset | Number of instances | Number of attributes and classes |
|---------|---------------------|---------------------------------|
| Dataset 1: Math DS | 395 | 32 Attributes and 2 classes |
| Dataset 2: LMS DS | 480 | 16 Attributes and 3 classes |
| Dataset 3: CS DS | 344 | 11 Attributes and 2 classes |
| Dataset: Plang DS | 649 | 32 Attributes and 2 classes |

Simulation Environment: The simulations to implement proposed hybrid feature selection framework for EDM were conducted on machine incorporated with core i5. Python 2.7 version is used as an editor, whereas PYcharm Edu IDE was set up as the development environment.

4.1 Prediction Accuracy of Proposed Hybrid Feature Selection Framework

To validate the performance of the proposed hybrid feature selection framework accuracy of hybrid feature selection framework is evaluated. Accuracy is defined as the fraction of correctly predicted observations to the total observations [65–67]. The model with better accuracy is considered as the best prediction model [68]. So that accuracy of the proposed approach will give the ratio of correctly classified students in a pass or fail a class, over the total number of students. Accuracy gives the overall effectiveness of the proposed hybrid feature selection framework. Furthermore, accuracy gives effectiveness over existing feature selection framework and feature selection algorithm by comparing the results of accuracy on benchmark students’ datasets of proposed feature selection framework with existing feature selection framework, and feature selection algorithms. In this section, the accuracy of proposed hybrid feature selection framework is compared with existing feature selection framework, and other feature selection algorithms like FCBF, Information Gain, and CFS, feature selection algorithm and with proposed hybrid feature selection framework.
Referring to Tab. 2, the results in Fig. 5 presents the comparison of prediction accuracy of existing Feature selection framework with the proposed hybrid feature selection framework [39]. The red bar shows the proposed framework and the black bar shows the existing hybrid feature selection framework [39] in Fig. 5. The x-axis shows the results four benchmark datasets and the y-axis shows the percentage value of prediction accuracy on four benchmark datasets. It is clearly observed that the prediction accuracy of the proposed feature section on all datasets show better result than existing hybrid feature selection framework. So that it is retrieved through the result that proposed feature selection perform better in terms of prediction accuracy than existing feature selection framework. As the existing framework overlooks the prediction model [69], and neglect the optimal features. Hence the correctly classified instances of proposed hybrid feature selection are greater than existing hybrid feature selection framework [39]. Fig. 6 shows the comparison of the Prediction Accuracy of existing FCBF filter feature selection algorithm [70] with proposed hybrid feature selection framework. The x-axis shows the results on four benchmark datasets and y-axis shows the percentage values of FCBF and proposed feature selection framework on four datasets. Fig. 6 shows that the proposed feature selection framework outperforms than FCBF on all selected benchmark datasets. It means that a number of students correctly classified by FCBF on each of the four datasets is much less than the proposed feature selection framework. So that it is retrieved through the result that proposed feature selection perform better in terms of prediction accuracy than FCBF feature selection algorithm. Also, the results reported in the existing literature [39] also shows that the prediction accuracy using FCBF feature selection shows prediction accuracy less than the prediction accuracy of proposed hybrid feature selection framework to predict the performance of students.

| Dataset   | Proposed hybrid feature selection | Existing hybrid feature selection | FCBF | Information gain (IG) | CFS |
|-----------|---------------------------------|---------------------------------|------|------------------------|-----|
| Math DS   | 92.91                           | 87.34                           | 87.59| 88.35                  | 87.85|
| LMS DS    | 75                              | 67.71                           | 67.50| 67.50                  | 70.21|
| CS DS     | 87.21                           | 85.47                           | 85.47| 85.47                  | 85.76|
| PLang DS  | 90.91                           | 85.05                           | 84.75| 83                     | 88.36|

### 4.2 Precision of Proposed Hybrid Feature Selection Framework Using Fusion

The hybrid feature selection performance is validated through the precision and recall. However, to show the classification of minority classes in a prediction model the precision of proposed hybrid feature selection framework is performed. Precision is the fraction of the retrieved instances that belong to the target class. In precision of the proposed feature selection framework gives the ratio of the total number of pass students classified correctly, over the number of students classified as pass. In sum, it shows how accurately the pass, students are identified correctly. Larger the number of pass students correctly classified means that educational stakeholder can build productive academic plans for the improvement in the performance of students. In this section, the precision results of proposed hybrid feature selection framework on four benchmark datasets are compared with exiting feature selection framework, and feature selection algorithms
for predicting the performance of students. Referring to Tab. 3 shows the comparison of the precision of existing hybrid feature selection framework [39] with the proposed feature selection framework. The red bar shows the proposed framework and black bar shows the existing hybrid feature selection framework in Fig. 7. The x-axis shows the results four datasets, and the y-axis shows the percentage value of precision on four datasets. It is clearly observed that the precision of the proposed feature selection all datasets show a better result than existing hybrid feature selection framework. Moreover, the number of correctly-classified students by the proposed feature selection framework is greater than existing hybrid feature selection framework. So that it is retrieved through the result that the proposed hybrid feature selection framework performs better in terms of precision than existing feature selection framework.

**Figure 5:** Comparing the prediction accuracy of proposed feature selection with FCBF

**Figure 6:** Comparing the prediction accuracy hybrid feature of proposed framework with existing work
Table 3: Validation of proposed hybrid feature selection framework in terms of precision

| Dataset   | Proposed hybrid feature selection | Existing hybrid feature selection | FCBF | Information gain (IG) | CFS |
|-----------|-----------------------------------|-----------------------------------|------|------------------------|-----|
| Math DS   | 94                                | 92                                | 92   | 91                     | 92  |
| LMS DS    | 76                                | 68.6                              | 68.6 | 68.66                  | 71  |
| CS DS     | 95                                | 91                                | 91   | 89                     | 91  |
| PLang DS  | 93                                | 90                                | 90   | 88                     | 88  |

Figure 7: Comparing the precision of proposed framework with existing framework

Fig. 8 shows the comparison of the precision of existing FCBF filter feature selection framework with proposed hybrid feature selection framework. The red bar shows the proposed framework and purple bar shows the existing FCBF filter feature selection algorithm in Fig. 8. The x-axis shows the results four datasets, and the y-axis shows the percentage values of precision by applying FCBF and proposed feature selection framework on four datasets. The results in Fig. 8 depicts that the number of students correctly classified by FCBF algorithm on all selected datasets is much less than the number of correctly classified students by proposed feature selection framework. Hence it is retrieved through the result that proposed feature selection perform better in terms of precision than existing FCBF feature selection algorithm. Fig. 9 shows the comparison of the precision of existing IG (Information Gain) filter feature selection algorithm with proposed feature selection framework. The red bar shows the proposed framework and light blue line bar shows the existing IG filter feature selection algorithm in Fig. 9. The x-axis shows the results four benchmark datasets, and the y-axis shows the percentage value of f-measure on four datasets. It is clearly observed that the precision of the proposed feature selection on all selected datasets show a better result than existing IG feature selection algorithm. So that it is retrieved through the result that proposed feature selection perform better in terms of precision than existing IG filter feature selection algorithm.
Figure 8: Comparing precision of proposed hybrid feature selection framework with FCBF

Figure 9: Comparing precision of proposed hybrid feature selection framework with information gain

Fig. 10 shows the comparison of the precision of existing CFS (Correlation based feature selection) filter feature selection algorithm with proposed hybrid feature selection framework. The x-axis shows the results four datasets, and the y-axis shows the percentage value of precision on four datasets. It is clearly observed that the precision of the proposed feature section on Math, LMS, CS, and PLang datasets show better result than existing CFS feature selection algorithm. So that it is retrieved through the result that proposed feature selection perform better in terms of precision than existing CFS filter feature selection algorithm.

4.3 Recall of Proposed Hybrid Feature Selection Framework Using Fusion

The recall is another important measure to evaluate the efficiency of selected features [7]. The recall is the fraction of the target class recognized as an actual class [71,72]. It gives the ratio of correctly classified students belong to a particular class, over a total number of students. So
that the recall results of proposed hybrid feature section framework present the ratio of correctly classified pass students over the total number of students. Henceforth, recall results of the proposed hybrid feature selection framework depicts, the worth of the selected features by proposed hybrid feature selection framework on pass class. In sum, recall gives the percentage that at which extend feature selected by the proposed approach framework can be affected on the performance of students. Tab. 4 presents recall results of proposed hybrid feature selection framework, existing feature selection framework, and FCBF, Information gain, CFS, feature selection algorithms on four benchmarking students’ datasets (having diversity in number of features, number of instances, and educational domains). Referring to Tab. 4, the results in Fig. 11 presents the comparison of recall of existing hybrid feature selection framework [39] with the proposed feature selection framework. The x-axis shows the results four datasets, and the y-axis shows the percentage value of precision on four datasets. It is clearly observed that the recall of proposed feature section on all selected datasets show better result than existing hybrid feature selection framework.

![Comparing Precision of Proposed Hybrid Feature Selection Framework with CFS Feature Selection](image)

**Figure 10:** Comparing precision of proposed hybrid feature selection framework with CFS

**Table 4:** Validation of proposed hybrid feature selection framework in terms of recall

| Dataset | Proposed hybrid feature selection | Existing hybrid feature selection | FCBF | Information gain (IG) | CFS |
|---------|-----------------------------------|----------------------------------|------|------------------------|-----|
| Math DS | 95                                | 89                               | 90   | 92                     | 90  |
| LMS DS  | 76.33                             | 68.66                            | 68.66| 69                     | 71.33|
| CS DS   | 88                                | 87                               | 87   | 87                     | 87  |
| PLang DS| 94                                | 89                               | 88   | 88                     | 88  |
Comparing Recall of Proposed Feature Selection Framework with Existing Framework Feature Selection Framework

So that it is retrieved through the result that proposed feature selection perform better in terms of recall than existing feature selection framework. Fig. 12 shows the comparison of Recall of existing FCBF filter feature selection framework with proposed hybrid feature selection framework. The x-axis shows the results four datasets, and the y-axis shows the percentage values of precision by applying FCBF and proposed feature selection framework on four datasets. The results shown in Fig. 16 depicts that there is greater number of incorrectly classified students than correctly classified. Students for each class (pass, fail) by applying FCBF algorithm on Math, LMS, and PLang datasets. Whereas the results depict that there is a much smaller number of incorrectly classified students for each class on Math, LMS, and PLang datasets by applying proposed feature selection framework. The results also depict that FCBF and proposed feature selection framework show similar results on CS dataset. It means the rate of correctly classified students for a class over the total number of students in a class, the percentage is equally resulted by FCBF and proposed feature selection. However, it is also noticed that CS dataset contains a smaller number of features than other three datasets. Moreover, the recall So that it is retrieved through the result that proposed feature selection perform better in terms of recall than existing FCBF feature selection algorithm.

Fig. 13 shows the comparison of f-measure of existing CFS filter feature selection algorithm with proposed feature selection framework on all datasets. The red bar shows the proposed framework and blue bar shows the existing CFS filter feature selection algorithm in Fig. 13 (referring to results in Tab. 4). The x-axis shows the results four datasets, and the y-axis shows the percentage value of f-measure on four datasets. It is clearly observed that f-measure of proposed feature section on all datasets show a better result than existing CFS feature selection algorithm. So that it is retrieved through the result that proposed feature selection perform better in terms of f-measure than existing CFS filter feature selection algorithm.
4.4 F-Measure of Proposed Hybrid Feature Selection Framework Using Fusion

To evaluate the performance of the proposed hybrid feature selection framework, f-measure results of hybrid feature selection framework on four benchmark datasets are evaluated. F-measure is commonly used in EDM that gives a maximum value, in case, there is a balance between the values of precision and the recall evaluation measures [71]. F-measure is the harmonic mean of precision and recall. This measure also conveys the balance between precision and recall evaluation measures. The equation of obtaining f-measure is as follows through equation. In this section the f-measure results of the proposed hybrid feature selection framework are evaluated on four benchmarks students’ datasets, and these results are compared with the precision results of existing

![Figure 12: Comparing recall of proposed hybrid feature selection framework with FCBF feature selection](image)

![Figure 13: Comparing recall of proposed hybrid feature selection framework CFS feature selection](image)
feature selection framework and feature selection algorithms (like FCB, Information Gain, CFS) on four benchmark students’ datasets, in order to validate the proposed hybrid feature selection framework.

Tab. 5 presents f-measure results of proposed hybrid feature selection framework, existing feature selection framework, and FCBF, Information gain, and CFS, feature selection algorithms on four benchmarking students’ datasets (having diversity in the number of features, number of instances, and educational domains). Fig. 14 shows the comparison of f-measure of existing hybrid feature selection framework with the proposed feature selection framework.

Table 5: Validation of proposed hybrid feature selection framework in terms of F-Measure

| Dataset | Proposed hybrid feature selection | Existing hybrid feature selection | FCBF | Information gain (IG) | CFS |
|---------|----------------------------------|----------------------------------|------|-----------------------|-----|
| Math DS | 94                               | 91                               | 91   | 91                    | 91  |
| LMS DS  | 76                               | 68.3                             | 68.6 | 68.6                  | 70.6|
| CS DS   | 95                               | 89                               | 91   | 89                    | 89  |
| PLang DS| 93                               | 89                               | 90   | 88                    | 88  |

Figure 14: Comparing F-Measure of proposed hybrid feature selection framework with existing hybrid feature selection framework

The x-axis shows the results of four datasets, and the y-axis shows the percentage value of f-measure on four datasets. It is clearly observed that the f-measure of proposed feature section on Math, LMS, CS, and PLang datasets show better result than existing hybrid feature selection framework. So that it is retrieved through the result that proposed feature selection perform better in terms of F-measure than existing feature selection framework. Fig. 15 shows the comparison of
F-Measure of existing FCBF filter feature selection framework with the proposed feature selection framework. The x-axis shows the results four datasets, and the y-axis shows the percentage values of FCBF and proposed feature selection framework on four datasets. Fig. 15 depicts that the f-measure results of FCBF on selected datasets are less than the proposed feature selection framework. So that it is retrieved through the result that proposed feature selection perform better in terms of f-measure than FCBF feature selection algorithm. Fig. 16 shows the comparison of F-Measure of existing IG filter feature selection framework with the proposed feature selection framework. The x-axis shows the results four datasets, and the y-axis shows the percentage values of IG and proposed feature selection framework on four datasets.

![Comparing F-Measure of Proposed Feature Selection Framework with FCBF Feature Selection](image)

**Figure 15:** Comparing F-Measure of proposed hybrid feature selection framework with FCBF feature selection

Fig. 16 depicts that the F-measure results of IG on all datasets are less than the proposed feature selection framework. So that it is retrieved through the result that proposed feature selection perform better in terms of f-measure than IG feature selection algorithm. Fig. 17 shows the comparison of f-measure of existing CFS filter feature selection algorithm with proposed feature selection framework. The red bar shows the proposed framework and green line bar shows the existing CFS filter feature selection algorithm in Fig. 17. The x-axis shows the results four datasets, and the y-axis shows the percentage value of f-measure on four datasets. It is clearly observed that f-measure of proposed feature section on four benchmark datasets show better result than existing CFS feature selection algorithm. So that it is retrieved through the result that proposed feature selection perform better in terms of f-measure than existing CFS feature selection algorithm. Above mentioned results show that proposed hybrid feature selection framework performs better on four benchmark datasets with a varying number of feature and instances, as compared to other feature selection algorithm as well as existing hybrid feature selection in EDM. In sum, the results concluded that the proposed hybrid feature selection outperforms than other existing hybrid feature selection and existing feature selection algorithms. Hence the proposed hybrid feature selection framework is validated.
5 Conclusion

This research identifies the suitable feature selection algorithms for identification of optimal features for predicting the performance of students. The proposed hybrid feature selection framework overcomes the issues identified in existing hybrid feature selection framework [39], as well as in other hybrid feature selection algorithms [31,33,73]. The proposed hybrid feature selection framework contributed to the body knowledge of EDM is such a way that it identifies the optimal features that are significant as well as associated with the target class. The two-level feature fusion added a novel contribution in state-of-the art of students’ performance prediction to obtain the optimal selection of features. The proposed hybrid feature selection framework not only identifies the optimal features but also perform better in terms of accuracy, precision, recall, and f-measure than the existing hybrid feature selection framework [39] for predicting the performance of students. Furthermore, the proposed hybrid features selection framework has the ability to
perform better on a different number of features and instance. As the proposed hybrid feature selection framework is validated on benchmark datasets with the different number of features, and a different number of instances to show is robustness. Future Directions: In future hybridization of different filter and wrapper feature section will be considered for further accuracy improvement of students’ performance prediction model. In future other stakeholders of education like teachers will also be considered for prediction model.

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