Target Consistency for Domain Adaptation:
when Robustness meets Transferability

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Abstract

Learning Invariant Representations has been success-fully applied for reconciling a source and a target do-main for Unsupervised Domain Adaptation. In this work, we start by investigating the robustness of such methods under the cluster assumption’s prism, bringing new empirical evidence that invariance with a low source risk does not guarantee a well-performing target classifier. More precisely, we show that the cluster assumption is violated in the target domain despite being maintained in the source domain, indicating a lack of robustness of the target classifier. To address this problem, we demonstrate the importance of enforcing the cluster assumption in the target domain, named Target Consistency (TC), especially when paired with a loss that promotes (class-level) invariance. Our new approach results in a significant improvement in image classification and segmentation benchmarks over state-of-the-art methods based on invariant representations. Importantly, our method is flexible and easy to implement, making it a complementary technique to existing approaches for improving the transferability of representations. **Key-Words:** Domain Adaptation, Invariant Representations, Cluster Assumption.

1 Introduction

Deep learning (DL) models often show a weak ability to generalize on samples significantly different from those seen during training [BVHP18, ABGLP19, GGB19]. This inability to generalize out of the training distribution presents a significant obstacle to a controlled and safe deployment of DL models in real-world systems [AOS+16, Mar20]. To bridge the distribution gap, Unsupervised Domain Adaptation (UDA) [AOS+16, PY09] leverages labeled samples from a well-known domain, referred to as source, to generalize on a target domain, where only unlabeled samples are available. If labelling functions are equal across domains, a situation known as the covariate shift, then adaptation can be performed by weighting sample contributions in the loss [SKM07, SNK+08]. However, for high dimensional data, such as text or image, it is unlikely that source and target distributions share enough statistical support to compute weights [JSR19]. Learning domain Invariant Representations i.e., representations for which it is impossible to distinguish the domain they were sampled from, can bring together two domains which are different in the input space [GL15, LCWJ15]. This fundamental idea, and the corresponding theoretical target risk [BDBCP07, BDBC+10], has led to a wide variety of methods for adapting deep classifiers to new domains [LZWJ16, LZWJ17, LCWJ18].

Nevertheless, the invariance of representations does not always guarantee a low target risk. For instance, in the case of images, aligning source and target back-
grounds can be detrimental; it may incorrectly align source and target classes if the background is incorrectly correlated with a given class due to some collection bias [BVHP18, ABGLP19], phenomenon known as negative transfer [TS10]. Some theoretical works have investigated the question of negative transfer when label shift between source and target domains is observed [ZDCZG19, JSR19], revealing a fundamental trade-off between invariance and ability of predictions to match the true target label distribution [ZDCZG19]. Prior works address this trade-off by relaxing domain invariance with weighted representations [CMLW18, YLC+19, LCWJ18, CZWG20]. However, learning invariant, but transferable representations, remains an open problem. One of the main hurdles is the negative impact invariance has on discriminability, resulting in sub-optimal and sensitive target classification.

In the present work, we aim to provide a new understanding of the transferability of representations through the prism of the cluster assumption, a well-known semi-supervised learning paradigm. The cluster assumption states that if samples are in the same cluster in the input space, they are likely to be of the same class. When enforced on unlabeled samples, the model benefits from a significant gain in generalization [CSZ09, SBL+20, XDH+19] and robustness [CRS+19, HMC+20]. We show that enforcing the cluster assumption in the target domain, named Target Consistency (TC), with domain invariant representations goes beyond the role of a regularizer for high capacity features extractor as described in [SBNE18]. Crucially, we reveal that class-level invariance maximizes the gains induced by Target Consistency. By fooling one discriminator per predicted class, we promote positive interaction between TC and Class-Level Invariance (CLIV). Our contributions are:

- We show that domain invariance induces a significant model sensitivity to perturbations in the target domain, indicating that invariance is achieved by disregarding principles of robustness. Such evidence motivates our interest in enforcing the cluster assumption for improving the transferability of domain invariant representations.

- To amplify the effect of TC, we perform class-level invariance (CLIV) while enforcing the cluster assumption, promoting positive feedback between decision boundary updates and representation alignment.

- We show with extensive experiments on both classification and segmentation datasets that we reach state-of-the-art performances for methods based on invariant representations.

## 2 Related Work

### Domain Adaptation

The covariate shift adaptation has been studied by [HGB+07, GSH+09, SNK+08] and label shift with kernel mean matching [ZSMW13, DPS14] and Optimal Transport [RCFT18]. Since Importance Sampling based methods are limited to distributions that share enough statistical support [JSR19, DDF17], an important line of works focuses on learning domain Invariant Representations (IR) [GL15, LCWJ15] for reconciling two non-overlapping data distributions. IR has led to a furnished literature; Joint Adaptation Network which aligns joint distribution of representations across layers [LZWJ16], Conditional Domain Adaptation Network which performs the multilinear conditioning between representations and predictions [LCWJ18]. Recently, significant progress has been made towards learning more transferable representations. In the work [LLWJ19], it has been shown that invariance can be achieved by generating consistent intermediate representations, preserving their transferability. [CWLW19] brought to light that invariance often lead to poor discriminability of features, characterized by low rank representations. Therefore, they suggest to penalize the highest singular value of a batch of representations. [WJL+19] revisited the principle of batch normalization by building a transferable layer which aligns naturally mean and variance of representations across domains.

### Consistency Regularization

Consistency based semi-supervised methods [LA16, TV17, BCG+19, VLK+19, SBL+20] have enjoyed great success in recent years, closing the gap with their fully supervised counterparts. Such methods are based on a simple concept: the prediction function should produce similar outputs for similar inputs. By enforcing such a constraint, the resulting decision boundary will lie in low density regions echoing a more robust model. Semantically similar inputs can be obtained by a simple Gaussian noise injection [LA16, TV17], data augmentations [BCG+19, SBL+20], or adversarial attacks [MMKI18]. The regularizer added consists of a distance measure (e.g., $L^2$, KL divergence) between the function’s output of a clean and a perturbed input.
3 On the Vulnerability of IR

3.1 Preliminaries

Domain Adaptation (DA) introduces two domains, the source and the target domains, on the product space $\mathcal{X} \times \mathcal{Y}$ where $\mathcal{X}$ is the input space and $\mathcal{Y}$ is the label space. Those domains are defined by their specific joint distributions of inputs $x \in \mathcal{X}$ and labels $y \in \mathcal{Y}$, noted $p(x, y)$ and $q(x', y')$, respectively. We refer to quantities involving the source and the target as $s$ and $t$, respectively, with exponent notation. Considering a hypothesis class $\mathcal{H}$, subset of functions from $\mathcal{X}$ to $\mathcal{Y}$, DA aims to learn $h \in \mathcal{H}$ which performs well in the target domain i.e. has a small target risk $\epsilon_t(h) := \mathbb{E}_{(x',y') \sim p}[\ell(h(x'),y')]$ where $\ell$ is a given loss. Unsupervised Domain Adaptation (UDA) considers the case where labeled samples are available in the source domain while the target domain is only represented with unlabeled samples. Learning Domain Invariant Representations (IR) is a key idea for reconciling two non-overlapping data distributions [GL15, LCWJ15]. A mainstream approach consists of learning a representation with a deep feature extractor such that a domain discriminator can not distinguish the target from source samples [GL15]. Provided a representation class $\Phi$, a subset of functions from the input space $\mathcal{X}$ to a representation space $Z$, a classifier class $\mathcal{G}$, a subset of functions from $Z$ to $\mathcal{Y}$, and noting $\mathcal{H} := \mathcal{G} \circ \Phi := \{g \circ \varphi; g \in \mathcal{G}, \varphi \in \Phi\}$, representations $\varphi \in \Phi$ are learned by achieving a trade-off between minimizing source classification error and fooling a domain discriminator [GL15], expressed as a function from $Z$ to $[0, 1]$. The role of representations in UDA has been theoretically investigated by Ben-David et al. in [BDTCP07], and extended in [BDT+10, MMR09, ZDCZG19], through a bound of the target risk:

Theorem 1 (From [BDTCP07] and [BDT+10]). Given a hypothesis class $\mathcal{H}$ and a hypothesis $h \in \mathcal{H}$:

$$\epsilon_t(h) \leq \epsilon_s(h) + d_{H \Delta H} + \lambda_H$$

where $d_{H \Delta H} := \sup_{h, h' \in \mathcal{H}} |\epsilon_s(h, h') - \epsilon_t(h, h')|$ and $\lambda_H := \inf_{h \in \mathcal{H}} \{\epsilon_t(h) + \epsilon_s(h)\}$. In particular, provided a representation $\varphi$, and applying the inequality to $\mathcal{G} \circ \varphi := \{g \circ \varphi; g \in \mathcal{G}\}$:

$$\epsilon_t(g\varphi) \leq \epsilon_s(g\varphi) + d_{G \Delta G}(\varphi) + \lambda_G(\varphi)$$

where $d_{G \Delta G}(\varphi) := \sup_{g, g' \in \mathcal{G}} |\epsilon_s(g\varphi) - \epsilon_t(g'\varphi)|$ and $\lambda_G(\varphi) := \inf_{g \in \mathcal{G}} \{\epsilon_s(g\varphi) + \epsilon_t(g\varphi)\}$.

On the one hand, Eq. (1) shows the role of the hypothesis class capacity for bounding the target risk. The lower the hypothesis class sensitivity to changes in input distribution, the lower $d_{H \Delta H}$. On the other hand, Eq. (2) puts emphasis on representations: if source and target representations are aligned i.e., $p(x') \approx q(x')$ for $z := \varphi(x)$, then $d_{G \Delta G}(\varphi)$ remains small.

3.2 Sensitivity in the Target Domain

Prior works [GL15, GUA+16, LCWJ15, LZWJ16, LZWJ17, LCWJ18] have greatly improved capacity to achieve a trade-off between source classification error and domain invariance of representations by minimizing $\epsilon'(g\varphi) + d_{G \Delta G}(\varphi)$ from Eq. (2). Clearly, maintaining a low $\lambda_G(\varphi)$ while learning domain invariant representations is crucial for a good adaptation. Some works bring theoretical evidence of its difficulty [ZDCZG19, WWKL19, JSR19] while pioneering works dig into that direction [LLWJ19, CWWL19, WJL19]. This difficulty is referred as non-conservative DA in [SBNE18] i.e., when the optimal joint classifier is significantly different from the target optimal classifier:

$$\inf_{h \in \mathcal{H}} \epsilon_t(h) \leq \epsilon_t(h^\lambda)$$

where $h^\lambda := \arg \min_{h \in \mathcal{H}} \epsilon_t(h) + \epsilon_s(h)$. Similarly, when provided with a representation $\varphi$, the optimal joint classifier differs from the target optimal classifier: $\inf_{\varphi \in \mathcal{G}} \epsilon_t(g\varphi) < \epsilon_t(g^\lambda\varphi)$ where $g^\lambda := \arg \min_{g \in \mathcal{G}} \{\epsilon_s(g\varphi) + \epsilon_t(g\varphi)\}$ (see Appendix for more details).

Importantly, mitigating at train time the risk of non-conservative DA is a difficult problem since target labels are involved in Eq. (3). Therefore, other tools need to be leveraged to detect non-conservative adaptation without the ground truth in the target domain. Following the insight from [SBNE18], we hypothesize that violation of the cluster assumption in the target domain is a strong indicator of a case of non-conservative DA. In such a case, a classifier with different source and target errors should exhibit a substantial sensitivity in the target domain to small input perturbations.\footnote{The violation of the cluster assumption is characterized by a decision boundary localized in high density regions of the target input space.}

Therefore, we analyze the robustness of a model trained to minimize the source risk, through its sensitivity to small perturbations in the input space. We follow [NBA+18] and compute the mean Jacobian norm.
as a proxy of the generalization at the level of individual target samples, and as a measure of the local sensitivity of the model on target examples:

$$
\mathbb{E}_{x^i \sim q} \left[ \| J (x^i) \|_F \right] \tag{4}
$$

where $J_{ij}(x) = \frac{\partial y_i}{\partial x_j}$ is the Jacobian matrix, $\|J\|_F$ is the Frobenius norm, and $\hat{y}_i$ is the output class probability for class $i$. For comparison, the source domain’s sensitivity can be computed similarly over source instances. By language abuse, we will refer to sensitivity in source and target domains as source and target sensitivity, respectively. The results obtained on 3 transfer tasks from Office-31 ($A \to D$, $W \to A$, $D \to W$) are shown in Fig. 2(c) and Fig. 2(d). As suspected, the target sensitivity is significantly higher compared to the source sensitivity. Importantly, when enforcing invariance of representations with Domain Adversarial Neural Networks (DANN [GL15]), sensitivity in the target domain decreases (for tasks $W \to A$ and $D \to W$) while remaining significantly higher than the source sensitivity. This validates our concern on non-conservative domain adaptation: even after features alignment, the resulting classifier still violates the cluster assumption in the target domain. To further investigate the regions of sensitivity, we examine the function’s behavior on and off the data manifold as it approaches and moves away from three anchor points. To this end, following [NBA+18], we analyze the behavior of the model near and away from target and source data along two types of trajectories: 1) an ellipse passing through three data points of different classes as illustrated in Fig. 2(a), and 2) an ellipse passing through three data points of the same class. Since linear combinations of images from the same class are likely to look like a realistic image, the second trajectory is expected to traverse overall closer to the data manifold.

Fig. 2(b) shows the obtained results. We observe that, according to the Jacobian norm, the model’s sensitivity in the vicinity of target data is comparable to its sensitivity off the data manifold. Inversely, the model remains relatively stable in the neighborhood of source data and becomes unstable only away from them, further confirming our hypothesis.

### 4 Target Consistency

#### 4.1 Consistency Regularization

To promote a more robust model and mitigate target sensitivity, we regularize the model predictions to be invariant to a set of perturbations applied to the target inputs. Concretely, we add to the objective function an additional Target Consistency term:

$$
\mathcal{L}_{TC}(\varphi, g) = \mathcal{L}_{VAT}(\varphi, g) + \mathcal{L}_{AUG}(\varphi, g)
$$

$$
= \mathbb{E}_{x^i \sim p} \max_{|r| \leq \epsilon} \left[ \| h(x^i) - h(x^i + r) \|_2 \right] \tag{5}
$$

$$
+ \mathbb{E}_{x^i \sim p} \left[ \| h(x^i) - h(\tilde{x}^i) \|_2 \right]
$$

Similar to [SBNE18], the first term incorporates the locally-Lipschitz constraint by applying Virtual Adversarial Training (VAT) [MMKI18] which forces the model to be consistent within the norm-ball neighborhood of each target sample $x^i$. Additionally, the second term forces the model to embed a target instance $x^i$ and its augmented version $\tilde{x}^i$ similarly to push for smooth neural network responses in the vicinity of each target data. With a carefully chosen set of augmentations, such a constraint makes sense since the semantic content of a transformed image is approximately preserved. Note that for more stable training, we follow
Mean Teachers (MT) [TV17] and use of an exponential moving average of the model to compute the target pseudo-labels (i.e., $h(x')$). Overall, $L_{TC}$ is in-line with the cluster assumption by promoting consistency to a various set of input perturbations, thus, forcing the decision boundary to not cross high-density regions.

**Augmentations.** For visual domain adaptation, and based on the recent success of supervised image augmentations [CZM+19, LKK+19, CZSL19] in semi-supervised learning [XDH+19, SBL+20] and robust deep learning [YLS+19, HMC+20], we propose to use a rich set of state-of-the-art data augmentations to inject noise and enforce consistency of predictions on target domain. Specifically, we use augmentations from AutoAugment [CZM+19]. Upon each application, we sample a given operation $o$ from all possible augmentations $O = \{ \text{equalize}, \ldots, \text{brightness} \}$. If the operation $o$ is applicable with varying severities, we also uniformly sample the severity, and apply $o$ to obtain the augmented target image $\tilde{x}' = o(x')$. However, applying a single operation might be solved easily by a high capacity model by memorizing the specific perturbations. To overcome this, we generate more diverse augmentations by mixing multiple augmented images (see Fig. 1). We start by randomly sampling $K$ operations from $O$ and $K$ convex coefficients $a_i$ sampled from a Dirichlet distribution: $(a_1, \ldots, a_K) \sim \text{Dir}(1, \ldots, 1)$. The augmented image $\tilde{x}'$ can then be obtained with an element-wise convex combination of the $K$ augmented instances of $x'$:

$$\tilde{x}' = \sum_{i=1}^{K} a_i o_i(x')$$

impelling the model to be stable, consistent, and insensitive across a more diverse range of inputs [ZSLG16, KKG18, HMC+20].

### 4.2 Target Consistency with IR

**Effects of Target Consistency.** Enforcing the target consistency gives us the ability to control the trade-off between a low target sensitivity, i.e., , a low violation of the cluster assumption and a low source risk. As described in [SBNE18], adding $L_{TC}$ to the objective function reduces the hypothesis class $\mathcal{H}$ to only include classifiers that are robust on both target and source domains, noted $\mathcal{H}_{TC}$. Through the lenses of domain adaptation theory (i.e., Eq. (1) from Theorem 1), by constraining the hypothesis space $\mathcal{H}$ to contain stable classifiers across domains, small changes to the hypothesis in the source domain will not induce large changes in the target domain [SBNE18]. Formally, this reduces the domain discrepancy $d_{\mathcal{H}_{TC},\mathcal{H}_{TC}} \leq d_{\mathcal{H},\Delta} \mathcal{H}$ based on the following inclusion $\mathcal{H}_{TC} \subset \mathcal{H}$.

However, viewing the effect of TC as a constraint on the hypothesis space (Eq. (1) from Theorem 1) does not explain the hidden interactions between TC and invariant representations (Eq. (2) from Theorem 1). To this purpose, we consider a target sample $x'$ near the decision boundary which is hard to adapt. Thus, its augmented version, $\tilde{x}'$, is likely to have a different predicted class. By enforcing TC, the model embeds $x'$ and $\tilde{x}'$ similarly to incrementally push the decision boundary far from class boundaries. Such incremental change might result in correcting the predicted class label. However, the underlying representations remain approximately the same, and the discriminator feedback does not reflect this predicted labels change. Now, consider that domain invariance is achieved by leveraging one discriminator per predicted class i.e., class-level invariance. The change of label due to the TC update will result in a switch of the discriminator used, subsequently reflecting the label change in the domain adversarial loss. This interaction between class-level invariance and decision boundary update is the key to the success of TC. Fig. 3 illustrates such an interaction.

**Class-level domain discriminator.** Similar to [PCLW18] and [CS19] that jointly align the input distributions and output classes for fine-grained alignment. We use CLIV, a well-suited Class-Level Invariance adversarial loss, which leverages one discriminator per predicted class. Let $D := (D_c)_{1 \leq c \leq C}$, a set of $C$ discriminators i.e., for $z \in Z, D(z) \in [0, 1]^C$, and noting $\cdot$ the scalar product in $\mathbb{R}^C$, CLIV is defined as follows:

$$L_{\text{CLIV}}(\varphi) := \inf_{D} \left\{ \mathbb{E}_{(x', y') \sim p}[y^* \cdot \log(D(z^*))] \\ + \mathbb{E}_{(x', y') \sim q}[y^t \cdot \log(1 - D(z^t))] \right\}$$

(6)

where given a sample $x$ with representation $z$ and output $\hat{y} := g(z)$, we weight the importance of discriminator $D_c$ in the adversarial loss using the output $\hat{y}$. It results into a class conditioning of the domain adversarial loss, where the ground-truths are used in the source domain and the predictions in the target domain.

To summarize, our model is trained by minimizing a trade-off between source Cross-Entropy ($CE$), Class-Level Invariance (CLIV) and Target Consistency (TC); given $\mu$ and $\nu$ tunable hyper-parameters,

$$L(g, \varphi) := L_{CE}(g, \varphi) + \mu L_{\text{CLIV}}(\varphi) + \nu L_{TC}(g, \varphi)$$

(7)

**Theoretical analysis.** We provide theoretical insights into the interaction between TC and class-level invariance. We consider $\varphi \in \Phi$ and $g \in \mathcal{G}$, which are
modified to obtain $\hat{\varphi}$ and $\hat{g}$ defined as the closest instances such that $\hat{g}\hat{\varphi}$ verifies TC. For instance, they can be obtained by minimizing $\ell_2(\varphi, \hat{\varphi}) + \ell_2(g, \hat{g}) + \lambda \cdot L_{TC}(\hat{g}, \hat{\varphi})$ where $\ell_2$ is an $L^2$ error. When enforcing TC, we expect to decrease the target error i.e., $\epsilon'(g\varphi) < \epsilon'(g\hat{\varphi})$. We assume that it exists $\rho \geq (1 - \epsilon'(g\hat{\varphi})/\epsilon'(g\varphi))^{-1}$ for any $(g, \varphi)$ i.e., the search of consistency always improves the target error. We note $\hat{y} := \hat{g}\hat{\varphi}(x)$, if $\hat{\varphi}$ is a large enough critic function space (See Appendix), we adapt the analysis from [BVC+20]:

$$\epsilon'(g\varphi) \leq \rho(\epsilon'(g\hat{\varphi}) + 8\sup_{t \in F}\{E_{(z^s, y^s)} \cdot p[z^s \cdot f(z^s)]\} - \mathbb{E}_{(z, \hat{y}) \sim q}[\hat{y}^t \cdot f(z^t)] + \inf_{t \in F}\epsilon'(f(\varphi))$$

(8)

Crucially, by observing that $\sup_{t \in F}\{E_{(z^s, y^s)} \cdot p[z^s \cdot f(z^s)]\} - \mathbb{E}_{(z, \hat{y}) \sim q}[\hat{y}^t \cdot f(z^t)]$ is an Integral Probability Measure proxy of $L_{CLIV}$, Eq. (8) reveals that class-level domain invariant representations can leverage feedback from an additional regularization, here the Target Consistency, to learn more transferable representations.

5 Experiments

5.1 Datasets

Office-31 [SKFD10] is the standard dataset for visual domain adaptation, containing 4,652 images in 31 categories divided across three domains: Amazon (A), Webcam (W), and DSLR (D). We use all six possible transfer tasks to evaluate our model. ImageCLEF-DA+ is a dataset with 12 classes and 2,400 images assembled from three public datasets: Caltech-256 (C), ImageNet (I) and Pascal VOC 2012 (P), where each one is considered as separate domain. We evaluate on all possible pairs of the three domains. Office-Home [VECP17] is a more difficult dataset compared to Office-31, consisting of 15,000 images across 65 classes in office and home settings. The dataset consists of four widely different domains: Artistic images (Ar), Clip Art (Ca), Product images (Pr), and Real-World images (Rw). We conduct experiments on all twelve transfer tasks. VisDA-2017 [PUK+17] presents a challenging simulation-to-real dataset, with two very distinct domains: Synthetic, with renderings of 3D models with different lighting conditions and from many angles; Real containing real-world images. We conduct evaluations on the Synthetic $\rightarrow$ Real task. For semantic segmentation experiments, we evaluate our method on the challenging GTA5 $\rightarrow$ Cityscapes VisDA-2017 semantic segmentation task. The synthetic source domain is GTA5 [RVRK16] dataset with 24,966 labeled images, while the real target domain is Cityscapes [COR+16] dataset consisting of 5,000 images. Both datasets are evaluated on the same classes, with the mean Intersection-over-Union (mIoU) metric.
Table 1: Average accuracy (%) of all tasks on image classification benchmarks for UDA. We compare our approach with similar methods based on invariant representations, evaluated using the same protocol. Results are obtained with a ResNet-50 unless specified otherwise. For detailed per task results, see the Appendix.

| Method        | Office-31 | ImageCLEF-DA | Office-Home | VisDA | VisDA (ResNet-101) |
|---------------|-----------|--------------|-------------|-------|-------------------|
| ResNet [HZRS16] | 76.1      | 80.7         | 46.1        | 45.6  | 52.4              |
| DANN [GUA+16]  | 82.2      | 85.0         | 57.6        | 55.0  | 57.4              |
| CDAN [LCWJ18]  | 87.7      | 87.7         | 65.8        | 70.0  | 73.7              |
| TAT [LLWJ19]   | 88.4      | 88.9         | 65.8        | 71.9  | -                 |
| BSP [CWLW19]   | 88.5      | -            | 66.3        | -     | 75.9              |
| TransNorm [WJL+19] | 89.3 | 88.5         | 67.6        | 71.4  | -                 |
| Ours           | 89.6      | 89.5         | 69.0        | 77.5  | 79.0              |

Table 2: Acc (%) on the 5 hardest Oce-Home tasks for TC ablation.

| Losses | Avg |
|--------|-----|
| $L_{CLIV}$ | 56.7 |
| $+L_{VAT}$ | 57.1 |
| $+L_{AUG}$ | 58.1 |
| $+L_{VAT} + L_{AUG}$ | 58.6 |
| $+L_{VAT} + L_{AUG}$ w/ MT | 58.9 |

Table 3: mIoU on GTA5 Cityscapes.

| Method            | DeepLab v2 mIoU |
|-------------------|-----------------|
| Adapt-SegMap [THS+18] | 42.4 |
| AdvEnt [VJB+19]   | 43.8            |
| Ours              | 44.9            |

5.2 Protocol

We follow the standard protocols for UDA [LZWJ17, LCWJ18, CPK+17]. We train on all labeled source samples and all unlabeled target samples and compare the classification accuracy based on three random experiments for classification and the mIoU based on a single run for segmentation. For classification, we use the same hyperparameters as CDAN [LCWJ18] and adopt ResNet-50 [HZRS16] as a base network pre-trained on ImageNet dataset [DDS+09]. As for CLIV and TC hyperparameters, we use $K = 4$, $\mu = 1$ and $\nu = 10$. We note that the method performs comparatively on a wide range of hyperparameter values making it robust for practical applications. For segmentation, we follow ADVENT [VJB+19] and use the same experimental setup with Deeplab-V2 [CPK+17] as the base semantic segmentation architecture with a ResNet-101 backbone and a DCGAN discriminator [RMC15]. We employ PyTorch [PGM+19] and base our code on official implementations of CDAN [LCWJ18] and ADVEN [VJB+19].

5.3 Results

For clarity and compactness, the average accuracy results of all tasks on standard classification benchmarks for UDA are reported in Table 1. The proposed method outperforms previous adversarial methods on all datasets. The gains are substantial when the source and target domain are more dissimilar, as in VisDA dataset. We conjure that this is a result of a large number of target instances available, enabling us to extract a significant amount of training signal with TC objective term to enforce the cluster assumption. Additionally, the method performs well with many categories, as is the case for Oce-Home dataset. Such gain is a result of the class-level invariance, which is empowered as the number of classes grows. We observe overall smaller improvements on Office-31 due to its limited size, and ImageCLEF-DA since the three domains are visually more similar. We further demonstrate the generality of the proposed method by conducting additional experiments on GTA5 Cityscapes task for semantic segmentation (Table 3), and observe a gain of 2.5 points over the baseline Adapt-SegMap [THS+18], confirming the flexibility of TC and its applicability across DA tasks.

5.4 Ablations

To examine the effect of each component of our proposed method, we conduct several ablations on the 5 hardest tasks on Office-Home, with and without the TC term, and with different variations of the TC loss.
Figure 4: Analyses. (a) Accuracy on VisDA-2017 with different number of mixed augmentations $K$. (b) and (c) The effect of TC on the target and source sensitivity for two Office-31 tasks ($A \rightarrow W$ and $A \rightarrow D$). (d) The error $\lambda$ of the ideal joint hypothesis $h^\lambda$. (e) A measure of domain discrepancy $d_A$.

The results are reported in Table 2. We observe that adding a consistency term, either VAT or AUG, results in a higher accuracy across tasks, with better results when smoothing in the vicinity of each target data point within the data manifold with AUG, instead of the adversarial direction using VAT. Their combination, with Mean Teacher (MT), results in an overall more performing model. We also conduct an ablation study on the effect of varying the mixing number $K$ to produce more diverse target images. Fig. 4(a) shows the results. Overall, we observe a slight improvement and more stable results when $K$ is increased, but over a certain threshold, the degree of noise becomes significant, heavily modifying the semantic content of the inputs and hurting the model’s performance. Most importantly, to show the importance of coupling TC with CLIV, we pair TC with DANN and CDAN losses. The obtained results in Table 4 show lower average accuracy and minimal gains when enforcing the cluster assumption in conjunction with such adversarial losses, confirming the importance of imposing class-level invariance when applying TC.

5.5 Analyses

Sensitivity Analysis. To investigate the impact of TC on the model sensitivity, we compare the mean Jacobian norm of models trained with various objectives (Figs. 4(b) and 4(c)). TC coupled with CLIV, greatly improves the model’s robustness on target, with a small increase in the source sensitivity.

Ideal Joint Hypothesis and Distributions Discrepancy. We evaluate the performances of the ideal joint hypothesis, which can be found by training an MLP classifier on top of a frozen features extractor on source and target data with labels. Fig. 4(d) provides empirical evidence that TC produces a better joint hypothesis $h^\lambda$, thus more transferable representations. Additionally, as a proxy measure of domain discrepancy [BDBC’10], we compute the A-distance, defined as $d_A = 2(1 - e^\lambda)$, with $\varepsilon$ as the error rate of a domain classifier trained to discriminate source and target domains. Fig. 4(e) shows that TC decreases $d_A$, implying a better invariance.

Qualitative Analysis. As shown in Fig. 5, the method produces locally consistent and globally coherent predictions for semantic segmentation.

Figure 5: Qualitative Results on GTA5 Cityscapes.

6 Conclusion and Future Work

In this work, we presented a new approach to address the lack of robustness of domain adversarial learning by promoting consistent predictions, named Target Consistency (TC), to a set of various input perturbations in the target domain. Crucially, even if our approach is derived from well-known strategies, i.e., class-level invariance and target consistency, we are the first to bring attention to their strong interaction, resulting in a significant improvement of the transferability of representations. Through extensive experiments, we show that our approach outperforms other methods based on invariant representations, validating our analysis. Finally, TC has the advantage of being orthogonal to recent works [LWJ19, CWLW19] for improving the transferability of invariant representations, thus, combining them is an interesting research direction.
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Target Consistency for Domain Adaptation: when Robustness meets Transferability

In this document, we provide supplementary materials for our work: Target Consistency for Domain Adaptation: when Robustness meets Transferability. We present detailed per task results for all the datasets, additional experimental details and some qualitative results. We also investigate the robustness of the proposed method through the lenses of Fourier analysis. Finally, we provide more details about the theoretical statements of the paper.

Detailed Results

Table 1: Accuracy (%) on Office-31 for unsupervised domain adaptation (ResNet-50)

| Method               | A → W | D → W | W → D | A → D | D → A | W → A | Avg |
|----------------------|-------|-------|-------|-------|-------|-------|-----|
| ResNet-50 (He et al. 2016) | 68.4±0.2 | 96.7±0.1 | 99.3±0.1 | 68.9±0.2 | 62.5±0.3 | 60.7±0.3 | 76.1 |
| DAN (Long et al. 2015) | 80.5±0.4 | 97.1±0.2 | 99.6±0.1 | 78.6±0.2 | 63.6±0.3 | 62.8±0.2 | 80.4 |
| RTN (Long et al. 2016) | 84.5±0.2 | 96.8±0.1 | 99.4±0.1 | 77.5±0.3 | 66.2±0.2 | 64.8±0.3 | 81.6 |
| DANN (Ganin et al. 2016) | 82.0±0.4 | 96.9±0.2 | 99.1±0.1 | 79.7±0.4 | 68.2±0.4 | 67.4±0.5 | 82.2 |
| ADDA (Tzeng et al. 2017) | 86.2±0.5 | 96.2±0.3 | 98.4±0.3 | 77.8±0.3 | 69.5±0.4 | 68.9±0.5 | 82.9 |
| JAN (Long et al. 2017) | 85.4±0.3 | 97.4±0.2 | 99.8±0.2 | 84.7±0.3 | 68.6±0.3 | 70.0±0.4 | 84.3 |
| GTA (Sankaranarayanan et al. 2018) | 89.5±0.5 | 97.9±0.3 | 99.8±0.4 | 87.7±0.5 | 72.8±0.3 | 71.4±0.4 | 86.5 |
| CDAN (Long et al. 2018) | 94.1±0.1 | 98.6±0.1 | 100.0±0.0 | 92.9±0.2 | 71.0±0.3 | 69.3±0.3 | 87.7 |
| TAT (Liu et al. 2019) | 92.5±0.3 | 99.3±0.1 | 100.0±0.0 | 93.2±0.2 | 73.1±0.3 | 72.1±0.3 | 88.4 |
| BSP (Chen et al. 2019) | 93.3±0.2 | 98.2±0.2 | 100.0±0.0 | 93.0±0.2 | 73.6±0.3 | 72.6±0.3 | 88.5 |
| TransNorm (Wang et al. 2019) | 95.7±0.5 | 98.7±0.3 | 100.0±0.0 | 94.0±0.2 | 73.4±0.4 | 74.2±0.3 | 89.3 |
| Ours | 94.8±0.8 | 99.1±0.2 | 100.0±0.0 | 93.6±0.9 | 76.8±1.3 | 73.4±0.7 | 89.6 |

Table 2: Accuracy (%) on ImageCLEF-DA for unsupervised domain adaptation (ResNet-50)

| Method               | I → P | P → I | I → C | C → I | C → P | P → C | Avg |
|----------------------|-------|-------|-------|-------|-------|-------|-----|
| ResNet-50 (He et al. 2016) | 74.8±0.3 | 83.9±0.1 | 91.5±0.3 | 78.0±0.2 | 65.5±0.3 | 91.2±0.3 | 80.7 |
| DAN (Long et al. 2015) | 74.5±0.4 | 82.2±0.2 | 92.8±0.2 | 86.3±0.4 | 69.2±0.4 | 89.8±0.4 | 82.5 |
| DANN (Ganin et al. 2016) | 75.0±0.6 | 86.0±0.3 | 96.2±0.4 | 87.0±0.5 | 74.3±0.5 | 91.5±0.6 | 85.0 |
| JAN (Long et al. 2017) | 76.8±0.4 | 88.0±0.2 | 94.7±0.2 | 89.5±0.3 | 74.2±0.3 | 91.7±0.3 | 85.3 |
| CDAN (Long et al. 2018) | 77.7±0.3 | 90.7±0.2 | 97.7±0.3 | 91.3±0.3 | 74.2±0.2 | 94.3±0.3 | 87.7 |
| TransNorm (Wang et al. 2019) | 78.3±0.3 | 90.8±0.2 | 96.7±0.4 | 92.3±0.2 | 78.0±0.1 | 94.8±0.3 | 88.5 |
| TAT (Liu et al. 2019) | 78.8±0.2 | 92.0±0.2 | 97.5±0.3 | 92.0±0.3 | 78.2±0.4 | 94.7±0.4 | 88.9 |
| Ours | 79.5±0.4 | 92.7±0.3 | 97.6±0.2 | 93.2±0.4 | 78.6±0.2 | 95.5±0.4 | 89.5 |
Table 3: Accuracy (%) on Office-Home for unsupervised domain adaptation (ResNet-50)

| Method                  | Ar→Cl | Ar→Pr | Ar→Rw | Cl→Ar | Cl→Pr | Cl→Rw | Pr→Ar | Pr→Cl | Pr→Rw | Rw→Ar | Rw→Cl | Cl→Rw | Pr→Avg |
|-------------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|
| ResNet-50 (He et al. 2016) | 34.9  | 50.0  | 58.0  | 37.4  | 41.9  | 46.2  | 38.5  | 31.2  | 60.4  | 53.9  | 41.2  | 59.9  | 46.1   |
| DAN (Long et al. 2015)   | 43.6  | 57.0  | 67.9  | 45.8  | 56.5  | 60.4  | 44.0  | 43.6  | 67.7  | 63.1  | 51.5  | 74.3  | 56.3   |
| DANN (Ganin et al. 2016) | 45.6  | 59.3  | 70.1  | 47.0  | 58.5  | 60.9  | 46.1  | 43.7  | 68.5  | 63.2  | 51.8  | 76.8  | 57.6   |
| JAN (Long et al. 2017)   | 45.9  | 61.2  | 68.9  | 50.4  | 59.7  | 61.0  | 45.8  | 43.4  | 70.3  | 63.9  | 52.4  | 76.8  | 58.3   |
| CDAN (Long et al. 2018)  | 50.7  | 70.6  | 76.0  | 57.6  | 70.0  | 70.0  | 57.4  | 50.9  | 77.3  | 70.9  | 56.6  | 81.6  | 65.8   |
| TAT (Liu et al. 2019)    | 51.6  | 69.5  | 75.4  | 59.4  | 69.5  | 68.6  | 59.5  | 50.5  | 76.8  | 70.9  | 56.6  | 81.6  | 65.8   |
| BSP (Chen et al. 2019)   | 52.0  | 68.6  | 76.1  | 58.0  | 70.3  | 70.2  | 58.6  | 50.2  | 77.6  | 72.2  | 59.3  | 81.9  | 66.3   |
| TransNorm (Wang et al. 2019) | 50.2 | 71.4  | 77.4  | 59.3  | 72.7  | **73.1** | 61.0  | 53.1  | 79.5  | 71.9  | 59.0  | 82.9  | 67.6   |
| Ours                     | **53.1** | **73.0** | **77.0** | **62.6** | **72.4** | **73.1** | **63.8** | **54.4** | **79.8** | **74.6** | **60.4** | **83.3** | **69.0** |

Table 4: Accuracy (%) on VisDA-2017

| Method                  | ResNet-50 | Synthetic → Real | Method                  | ResNet-101 | Synthetic → Real |
|-------------------------|-----------|------------------|-------------------------|------------|------------------|
| JAN (Long et al. 2017)  | 61.6      | ResNet-101 (He et al. 2016) | 52.4 |
| GTA (Sankaranarayanan et al. 2018) | 69.5 | DANN (Ganin et al. 2016) | 57.4 |
| CDAN (Long et al. 2018) | 70.0      | CDAN (Long et al. 2018) | 73.7 |
| TAT (Liu et al. 2019)   | 71.9      | BSP (Chen et al. 2019) | 75.9 |
| Ours                    | **77.5±0.7** | Ours             | **79.0±0.1** |

Table 5: Accuracy (%) on the 5 hardest Office-Home task for Target Consistency ablation (ResNet-50)

|                      | Ar→Cl | Cl→Ar | Pr→Ar | Pr→Cl | Rw→Cl | Avg    |
|----------------------|-------|-------|-------|-------|-------|--------|
| \(\mathcal{L}_{DANN}\)  | 45.2±0.7 | 48.8±0.5 | 46.8±0.2 | 43.5±0.3 | 53.6±0.3 | 47.6   |
| \(\mathcal{L}_{DANN} + \mathcal{L}_{VAT}\)  | 44.3±0.2 | 50.3±1.8 | 48.5±1.1 | 43.6±0.6 | 53.5±0.2 | 48.0   |
| \(\mathcal{L}_{DANN} + \mathcal{L}_{AUG}\)  | 46.2±0.4 | 55.3±0.5 | 53.2±1.4 | 46.0±0.4 | 55.6±0.5 | 51.3   |
| \(\mathcal{L}_{DANN} + \mathcal{L}_{VAT} + \mathcal{L}_{AUG}\)  | 46.3±0.6 | 53.5±1.0 | 54.7±0.7 | 46.2±0.7 | 56.3±0.9 | 51.4   |
| \(\mathcal{L}_{CDAN}\)  | 50.3±0.1 | 54.6±0.7 | 55.8±0.6 | 49.3±0.2 | 56.9±0.1 | 53.4   |
| \(\mathcal{L}_{CDAN} + \mathcal{L}_{VAT}\)  | 50.1±0.5 | 58.5±0.6 | 59.1±0.6 | 49.8±0.2 | 57.9±0.1 | 55.1   |
| \(\mathcal{L}_{CDAN} + \mathcal{L}_{AUG}\)  | 51.0±0.2 | 57.3±0.5 | 61.0±0.7 | 50.8±0.2 | 58.4±0.5 | 55.7   |
| \(\mathcal{L}_{CDAN} + \mathcal{L}_{VAT} + \mathcal{L}_{AUG}\)  | 51.5±0.2 | 60.9±0.3 | 61.4±0.9 | 51.7±0.2 | 59.1±0.5 | 56.9   |
| \(\mathcal{L}_{CDAN} + \mathcal{L}_{VAT} + \mathcal{L}_{AUG} / w MT\)  | 51.3±0.9 | 59.0±0.4 | 60.0±0.5 | 51.8±0.2 | 57.9±0.3 | 56.0   |
| \(\mathcal{L}_{CLIV}\)  | 52.6±0.8 | 60.1±0.3 | 60.6±0.9 | 52.1±0.7 | 58.3±0.4 | 56.7   |
| \(\mathcal{L}_{CLIV} + \mathcal{L}_{VAT}\)  | 52.4±0.6 | 60.1±0.5 | 61.2±0.9 | 53.1±0.2 | 58.9±0.8 | 57.1   |
| \(\mathcal{L}_{CLIV} + \mathcal{L}_{AUG}\)  | 53.1±0.5 | 62.3±0.6 | 62.6±0.8 | 53.1±1.0 | 59.5±0.3 | 58.1   |
| \(\mathcal{L}_{CLIV} + \mathcal{L}_{VAT} + \mathcal{L}_{AUG}\)  | 53.0±0.1 | **62.8±0.7** | 62.8±0.2 | 53.8±0.8 | **60.8±0.8** | 58.6 |
| \(\mathcal{L}_{CLIV} + \mathcal{L}_{VAT} + \mathcal{L}_{AUG} / w MT\)  | **53.1±1.5** | 62.6±0.1 | **63.8±0.7** | **54.4±0.6** | 60.4±0.6 | **58.9** |

Table 6: mIoU on GTA5 → Cityscapes. AdvEnt+MinEnt* is an ensemble of two models.

| Method                  | mIoU |
|-------------------------|------|
| ResNet-101 (He et al. 2016) | 75.8  |
| Adapt-SegMap (Tsai et al. 2018) | 86.5  |
| AdvEnt (Vu et al. 2019) | 89.9  |
| Ours                     | **91.0** |

AdvEnt+MinEnt* (Vu et al. 2019) | 89.4  | 33.1 | 81.0 | 26.6 | 26.8 | 27.2 | **33.5** | **24.7** | **83.9** | **36.7** | 78.8 | **58.7** | **30.5** | **84.8** | **38.5** | **44.5** | **1.7** | **31.6** | **32.4** | **45.5** |
Experimental Details

Augmentations
For the set of possible augmentations $O$, we follow AutoAugment (Cubuk et al. 2019) and use the augmentations shown in Fig. 1. We note that when mixing augmentations (i.e., $K > 1$), we also add the possibility of composing augmentations, e.g., for $K = 3$, we give the possibility of sampling a pair of augmentations, so that a given of the operation $o_i$ might be composed of two operations $o_i = o_{i1} \circ o_{i2}$.

![Augmentations](image.png)

**Figure 1:** An example of the possible augmentations to be applied on a given input image.

For semantic segmentation, we limit $O$ to only contain photometric augmentations to avoid changing input coordinate-space, i.e., we remove `translate_x`, `translate_y`, `rotate`, `shear_x` and `shear_y` from $O$. However, it is possible to maintain the geometric transformations and use a bilinear resampler to bring back the outputs of the augmented image into the coordinate-space of the clean image.

Mean Teacher
The objective of the consistency loss in Paper Eq 5. is to incrementally push the decision boundary to low-density regions on the target domain. However, using the current model $h$ as both a teacher, generating pseudo-labels for the target examples, and as a student, producing the current predictions over perturbed inputs, might result in an unstable training, where a small optimization step can result in a significantly different classifier, hurting the target generalization performance. To solve this, we follow Mean Teachers (MT) (Tarvainen and Valpola 2017), and use an Exponential Moving Average (EMA) of the student model $h$ weights as a teacher $h^t$, where the weights $\theta_t^t$ of the teacher model at a training step $t$ are defined as the EMA of successive student’s weights $\theta$:

$$
\theta_t^t = \alpha \theta_{t-1}^t + (1 - \beta) \theta_t
$$

(1)

where $\beta$ is a momentum term that controls how far we reache into training history. The teacher model can be used to generate the pseudo-labels $h^t(x^t)$ for a more stable optimization procedure.
Target Consistency for Semantic Segmentation

To demonstrate the generality of target consistency, we propose to adapt it for segmentation tasks. Given the dense nature of semantic segmentation, where we predict class assignment at each spatial location, we remove the local consistency constraint $\mathcal{L}_{\text{VAT}}$, since even small perturbations at the pixel level might significantly change the local appearance, making the task of predicting consistent labels impractical. Additionally, we constrain the target consistency to be only photometric augmentations to conserve the input coordinate-space. We follow (Tsai et al. 2018) and adopt adversarial learning in the output space rather than representation space, taking advantage of the structured outputs in semantic segmentation that contain spatial similarities between the source and target domains, the adversarial network is applied at a multi-level to perform output space adaptation at different feature levels effectively. We refer the reader to Section 4 of (Tsai et al. 2018) for more details on multi-level output space-based adaptation.

Implementation

For the implementation, we use PyTorch (Paszke et al. 2019) deep learning framework and base our implementation on the official implementations of CDAN (Long et al. 2018) and ADVEN (Vu et al. 2019). All experiments are done on a single NVIDIA V100 GPU with 32GB memory. In terms of the hyperparameters, for classification, we adopt mini-batch SGD with a momentum of 0.9 and the learning rate annealing strategy (Ganin et al. 2016) with an initial learning rate of $10^{-2}$. As for segmentation, the model is trained using mini-batch SGD and a learning rate $2.5 \times 10^{-4}$, momentum 0.9 and weight decay $10^{-4}$, and Adam optimizer (Kingma and Ba 2014) for the discriminator with learning rate $10^{-4}$, both with a polynomial learning rate scheduler (Chen et al. 2017).

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1 https://github.com/thuml/CDAN
2 https://github.com/valeoai/ADVENT
Figure 2: Fourier Analysis of Model Robustness on Source and Target. An illustration of the Fourier sensitivity heatmaps on the source and target domains for a ResNet-50 trained with different objectives. Each pixel of the heatmap is the error of the model when all of its inputs are perturbed with a single Fourier basis vector.

To further examine the lack of target robustness in DA, we investigate a common hypothesis in robust deep learning (Hendrycks et al. 2020), where the lack of robustness is attributed to spurious high-frequency correlations that exist in the source data,
that are not transferable to target data. To this end, we follow (Yin et al. 2019), and measure the model error after injecting an additive noise at different frequencies. Concretely, we resize all of the data to $96 \times 96$ images, we then add, at each iteration, $96 \times 96$ Fourier basis vector corresponding to an additive noise at a given frequency, and record the model error over either source or target data when such basis vector is added to each image individually (see Section 2 of (Yin et al. 2019) for more details). Fig. 2 shows the Fourier sensitivity heatmaps on source and target, for a ResNet-50 trained with different objectives. Each pixel of $96 \times 96$ heatmaps shows the error of the model when the inputs are perturbed by a single Fourier basis vector, in which the error corresponding to low-frequency noise is shown in the center, and high frequencies are away from the center. We observe that the model is highly robust on source across frequencies and the different objectives, but becomes quite sensitive to high-frequency perturbations on target when trained on source only or with a DANN objective. However, such sensitivity is reduced when enforcing the cluster assumption on the target domain, indicating a possible suppression of the spurious high-frequency correlations found in the source domain.
Qualitative Results

**Qualitative Results.** Fig. 3 illustrate qualitative results for semantic segmentation. Additionally, we visualize the feature representations of \( \mathbf{D} \to \mathbf{A} \) task of Office-31 with t-SNE (Maaten and Hinton 2008) in Fig. 4. We observe that our method produces a well aligned source and target features. This shows the benefits of coupling consistency regularization with class level discrimination.

![Figure 3: Qualitative Results on GTA5 → Cityscapes.](image)

![Figure 4: T-SNE of the adapted features of, left: ResNet-50, center: DANN, right: Ours, trained on D → A task of Office-31. Blue: Source D; Red: Target A.](image)

**Toy Dataset.** To show the effect of TC on the decision boundary, we conduct a toy experiment on the rotating two moons dataset, where the target samples are obtained by rotating the source points by \( 45^\circ \), comparing the learned decision boundary when we train on source only, with a DANN objective, and when using TC. As shown in Fig. 5, the TC terms helps push the decision boundary away from dense target regions, resulting in a well performing prediction function across domains.

![Figure 5: Effect of TC on two moons dataset. Red and green points are the instances of the two classes of the source domain. Blue points are target samples generated by rotating source samples. The black line shows the learned decision boundary, when using only source samples, with a DANN objective and with target consistency.](image)
**Non-conservative Domain Adaptation**

**Theorem 1** (From Ben-David et al. 2007 and Ben-David et al. 2010). *Given a hypothesis class \( \mathcal{H} \) and a hypothesis \( h \in \mathcal{H} \):*

\[
\epsilon'(h) \leq \epsilon^*(h) + d_{H\Delta H} + \lambda_H
\]

where \( d_{H\Delta H} := \sup_{h', h'' \in \mathcal{H}} \epsilon^*(h, h') - \epsilon'(h, h'') \) and \( \lambda_H := \inf_{h \in \mathcal{H}} \{ \epsilon^*(h) + \epsilon'(h) \} \). In particular, provided a representation \( \varphi \), and applying the inequality to \( \mathcal{G} \circ \varphi := \{ g \circ \varphi : g \in \mathcal{G} \} \):

\[
\epsilon'(g\varphi) \leq \epsilon^*(g\varphi) + d_{G\Delta G}(\varphi) + \lambda_G(\varphi)
\]

where \( d_{G\Delta G}(\varphi) := \sup_{g, g' \in \mathcal{G}} |\epsilon^*(g\varphi) - \epsilon'(g'\varphi)| \) and \( \lambda_G(\varphi) := \inf_{g \in \mathcal{G}} \{ \epsilon^*(g\varphi) + \epsilon'(g\varphi) \} \).

On the one hand, Eq. (2) shows the role of the hypothesis class capacity for bounding the target risk. The lower the hypothesis class sensitivity to changes in input distribution, the lower \( d_{H\Delta H} \). On the other hand, Eq. (3) puts emphasis on representations: if source and target representations are aligned i.e., \( p(z^s) \approx q(z^t) \) for \( z := \varphi(x) \), then \( d_{G\Delta G}(\varphi) = 0 \).

One of the main difficulties of DA is achieving the optimal trade-off between source classification error and domain invariance of representations by minimizing \( \epsilon^*(g\varphi) + d_{G\Delta G}(\varphi) \) from Eq. (3), while maintaining a low \( \lambda_G(\varphi) \). This difficulty is referred as *non-conservative DA* in (Shu et al. 2018) i.e., when the optimal joint classifier is significantly different from the target optimal classifier:

\[
\inf_{h \in \mathcal{H}} \epsilon'(h) < \epsilon'(h^*) \quad \text{where} \quad h^* := \arg \min_{h \in \mathcal{H}} \epsilon^*(h) + \epsilon'(h)
\]

**Theoretical Analysis**

We provide theoretical insights into the interaction between TC and class-level invariance. We consider \( \varphi \in \Phi \) and \( g \in \mathcal{G} \), which are modified to obtain \( \tilde{\varphi} \) and \( \tilde{g} \) defined as the closest instances such that \( \tilde{g}\tilde{\varphi} \) verifies TC. For instance, they can be obtained by minimizing \( \ell_2(\varphi, \tilde{\varphi}) + \ell_2(g, \tilde{g}) + \lambda \cdot L_{TC}(\tilde{g}, \tilde{\varphi}) \) where \( \ell_2 \) is an \( L^2 \) error. When enforcing TC, we expect to decrease the target error i.e., \( \epsilon'(\tilde{g}\tilde{\varphi}) < \epsilon'(g\varphi) \). Noting \( \rho := (1 - \epsilon'(\tilde{g}\tilde{\varphi})/\epsilon'(g\varphi))^{-1} \) and \( \tilde{y} := \tilde{g}\tilde{\varphi}(x) \), F a large enough critic function space, we adapt the theoretical analysis from (Bouvier et al. 2020):

\[
\epsilon'(g\varphi) \leq \rho \left( \epsilon^*(g\varphi) + s \sup_{f \in F} \{ \mathbb{E}_{(x, z^s) \sim p}[y^s \cdot f(z^s)] - \mathbb{E}_{(x, z^t) \sim q}[\tilde{y}^t \cdot f(z^t)] \} + \inf_{f \in F} \epsilon'(f) \right)
\]

More precisely, F has the following properties (Bouvier et al. 2020):

\begin{itemize}
  \item (A1) \( F \) is symmetric (i.e. \( \forall f \in F, -f \in F \)) and convex.
  \item (A2) \( \mathcal{G} \subset F \) and \( \{ f \cdot f' : f, f' \in F \} \subset F \).
  \item (A3) \( \forall \varphi \in \Phi, f_D(z) \mapsto \mathbb{E}_D[Y|\varphi(X) = z] \in F \).
  \item (A4) For two distributions \( p \) and \( q \) on \( Z, p = q, \) and \( 1 \leq c \leq C, \) if and only if,
\end{itemize}

\[
\text{IPM}(p, q; f_c) := \sup_{f \in F} \{ \mathbb{E}_p[f_c(Z)] - \mathbb{E}_q[f_c(Z)] \} = 0
\]

where \( f_c \) is the \( c \)--th coordinate of \( f \).

Crucially, by observing that \( \sup_{f \in F} \{ \mathbb{E}_{(x, z^s) \sim p}[y^s \cdot f(z^s)] - \mathbb{E}_{(x, z^t) \sim q}[\tilde{y}^t \cdot f(z^t)] \} \) is an *Integral Probability Measure* proxy of \( L_{C\Delta I} \), Eq. (6) reveals that class-level domain invariant representations can leverage feedback from an additional regularization, here the Target Consistency, to learn more transferable invariant representations.

Eq. (6) is obtained by applying Bound 4 (Inductive Bias and Guarantee, equation 14) from (Bouvier et al. 2020) by leveraging the inductive design:

\[
\epsilon'(\tilde{g}\tilde{\varphi}) < \epsilon'(g\varphi)
\]
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