An improved bound on axion-photon coupling from Globular Clusters

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We derive a strong bound on the axion-photon coupling \(g_{a\gamma}\) from the analysis of a sample of 39 Galactic Globular Clusters. As recognized long ago, the \(R\) parameter, i.e. the number ratio of stars in horizontal over red giant branch of sufficiently old stellar clusters, would be reduced by the axion production from photon conversions occurring in stellar cores. In this regard we have compared the measured \(R\) with state-of-the-art stellar models obtained under different assumptions for \(g_{a\gamma}\). We show that the estimated value of \(g_{a\gamma}\) substantially depends on the adopted He mass fraction \(Y\), an effect often neglected in previous investigations. Taking as benchmark for our study the most recent determination of the primordial He abundance, we obtain an upper bound \(g_{a\gamma} < 0.66 \times 10^{-10}\) GeV\(^{-1}\) at 95% confidence level. This result significantly improves the constraints from the previous analyses and is currently the strongest limit on the axion-photon coupling in a wide mass range.

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Introduction.— Axions are low-mass pseudoscalar particles, somewhat similar to neutral pions. Originally, they were introduced to explain the absence of CP violation in the strong interactions (QCD) \([1,2]\), a long-standing puzzle in particle physics known as the strong CP problem. Later on, it was also realized that the existence of such particles could account for most or all of the dark matter in the Universe. Specifically, axions with masses in the 10 \(\mu\)eV region would be cold dark matter candidates \([3,4]\) while for \(m_a \gtrsim 60\) meV they would attain thermal equilibrium at the QCD phase transition or later \([5,6]\), contributing to the cosmic radiation density and, subsequently, to the cosmic hot dark matter along with massive neutrinos \([7]\).

A generic property of axions is their two-photon coupling, specified by the Lagrangian \(\mathcal{L}_{a\gamma} = g_{a\gamma} E \cdot B\), where \(g_{a\gamma} = 2 \times 10^{-10}\) GeV\(^{-1}\) \(\zeta\) \((m_a/1\) eV\) and \(\zeta\) is a model dependent parameter of order one in many axion models. This relation defines the “axion line” in the \(m_a - g_{a\gamma}\) plane (see, e.g., \([8]\)). However, in recent years, a considerable attention has been devoted to the so-called Axion-Like-Particles (ALPs) which couple to photons, but do not satisfy the mass-coupling relation defined above for the QCD axions. Such light pseudoscalar particles emerge naturally in various extensions of the Standard Model (see, e.g., \([9]\)) and are phenomenologically motivated by a series of unexplained astrophysical observations. Among these, the seeming transparency of the universe to Very High-Energy gamma-rays \([10]\), the larger than expected white dwarf cooling rates \([11]\), and the quest for dark matter candidates (see \([12,13]\) and references therein).

As pointed out in a seminal paper by Pierre Sikivie \([14]\), the two-photon coupling \(a\gamma\) allows for efficient experimental searches of axions and ALPs. Indeed, in the presence of an external magnetic field, the \(a\gamma\) coupling leads to the phenomenon of photon-axion mixing \([15]\). This mechanism is the basis for direct searches of axions in light-shining-through-the-wall experiments (see e.g. \([16]\)) and axion dark matter in micro-wave cavity experiments (see e.g. the ADMX experiment \([17]\)). Furthermore, the \(g_{a\gamma}\) vertex would also allow for a production of axions via Primakoff process in stellar plasma \([18]\). The predicted solar axion spectrum is currently searched by the CERN Axion Solar Telescope (CAST) \([19]\), looking for conversions into X-rays of solar axions in a dipole magnet directed towards the sun. CAST searches with vacuum inside the magnet bores achieved a limit of \(g_{a\gamma} \lesssim 0.88 \times 10^{-10}\) GeV\(^{-1}\) for \(m_a \lesssim 0.02\) eV \([19]\), an excellent constraint for very light ALPs. For realistic QCD axions, CAST has explored the mass range up to 1.17 eV, providing the bound \(g_{a\gamma} \lesssim 2.3 - 3.3 \times 10^{-10}\) GeV\(^{-1}\) at 95% CL, by using \(^4\)He \([20]\) and \(^3\)He \([21,22]\) as buffer gas.

The Primakoff process induced by the photon-axion coupling would also allow for indirect axion searches, via effects on stellar evolution. In this context, additional constraints on the axion-photon coupling have been obtained from astronomical observations of helium burning low and intermediate mass stars \([23,24,25,26]\). A recent analysis showed that a sufficiently large axion emission would affect the very existence of Cepheids variables in the mass range \(M \sim 8 - 12\) \(M_\odot\), providing the bound \(g_{a\gamma} < 0.8 \times 10^{-10}\) GeV\(^{-1}\) \([27]\). On the other hand, photometric studies of Globular Cluster (GC) stars provided the long-standing strong bound \(g_{a\gamma} \lesssim 10^{-10}\) GeV\(^{-1}\) for an axion mass lower than about 10 keV \([24,25]\).

Globular Clusters are gravitationally bound systems of stars populating the Galactic Halo. They are among the oldest objects in the Milky Way. Hence only low mass
stars ($M \lesssim 0.85 \, M_\odot$) are still alive and, therefore, observable. A typical GC harbors a few millions stars, so that the various evolutionary phases are well populated and distinguished from each other. In particular, one can easily locate the main sequence, corresponding to the core H burning phase, the red giant branch (RGB), during which the stellar luminosity is supported by the shell H burning, and the horizontal branch (HB), corresponding to the core He burning phase. The number of stars observed in a particular evolutionary phase is proportional to the corresponding lifetime, which is determined by the efficiency of all the relevant sources and sinks of energy. As early recognized, axions coupled to photons would significantly reduce the lifetime of stars in the HB, while producing negligible changes on the RGB evolution [27]. Therefore, $g_{a\gamma}$ can be constrained by measurements of the $R$ parameter, $R = N_{\text{HB}}/N_{\text{RGB}}$, which compares the numbers of stars in the HB ($N_{\text{HB}}$) and in the upper portion of the RGB ($N_{\text{RGB}}$).

The previous analyses were based on the assumption that the measured $R$ parameter is well reproduced, within 30%, by extant models of GC stars, without including axion cooling. It was recognized early on (see, e.g., [30–33]) that the $R$ parameter is sensitive to the helium mass fraction $Y$, which mainly affects the number of RGB stars. However, in the context of the axion bounds this dependence has been neglected. Indeed, even a considerable decrease of the HB lifetime caused by a large value of $g_{a\gamma}$ could be compensated by a suitable increase of the assumed He content. Because of this degeneracy, a proper evaluation of the axion constraints from the $R$ parameter relies on our knowledge of the He abundance in the GCs. However, He abundance measurements are particularly difficult for Globular Clusters stars. Nevertheless, since they are among the first stars appeared in the Universe, it is commonly assumed that the original He content of Galactic GCs practically coincides with the pristine He abundance.

As discussed below, for the star’s total metal abundance $[M/H] < -1.1$ the $R$ parameter is practically independent of the cluster age and metallicity. At larger metallicity, however, the so-called RGB “bump” is too faint to enter into the RGB star count and, in turn, the resulting $R$ is definitely larger. Therefore, in our analysis we considered only the 39 clusters with $[M/H] < -1.1$, for which we obtain a weighted average $R_{\text{ave}} = 1.39 \pm 0.03$, and assumed that all the stars of the 39 clusters sample share the same original He abundance. The small statistical error (about 2%) supports this hypothesis.

It has been suggested that some GCs may harbor He enhanced stellar populations (see [38]). Indeed, the presence of He-rich stars would lead to a certain overestimation of the $R$ parameter. However, He enhanced stars would be less massive than coeval stars with primordial He content, so that they would be located in the bluer part of the HB. Therefore, we have tested this possibility by restricting the cluster sample, considering only 18 clusters whose HB is not dominated by blue stars $^3$. The new weighted average $R_{\text{ave}} = 1.39 \pm 0.04$, practically coincides with the one obtained for the whole sample, thus supporting the usual assumption that the bulk of the Milky Way GCs is characterized by a unique and, hence, pristine He abundance.

Axions or ALPs with mass below a few keV could be produced in stellar interiors via the Primakoff process – the conversion of a photon into an axion in the fluctuating electric field of nuclei and electrons in the stellar plasma $^{22}$. Being weakly interacting, axions would efficiently carry energy outside the star, much like neutrinos do, providing an effective cooling mechanism.

In the following, we will neglect other possible couplings of axions with nucleons and electrons, since these are rather model dependent (see, e.g., [11]). If present, also these interactions would contribute to the energy-loss. In this respect, our limit on $g_{a\gamma}$ should be considered conservative.

Assuming a non-degenerate plasma and ignoring the plasma frequency, the Primakoff production rate is

$$
\epsilon_a = Z(\xi^2) \frac{g_{a\gamma}^2}{4\pi^2} \frac{T^7}{\rho} \sim 28 \frac{\text{erg}}{g} Z(\xi^2) g_{10}^2 T_4^7 \rho_4^{-1},
$$

where $g_{10} \equiv g_{a\gamma}/(10^{-10} \, \text{GeV}^{-1})$, $\rho_4 \equiv \rho/(10^4 \, \text{g/cm}^3)$,

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1. Here, we are using the standard spectroscopic notation for the relative abundances, $[M/H]= \log_{10}(Z/X) - \log_{10}(Z/X)_{\odot}$, where $X$ is the hydrogen mass fraction and $Z$ is the total mass fraction of all the elements except H and He, i.e., $Z=1-X-Y$.

2. The “bump” is an intrinsic feature appearing as a peak in the differential luminosity function of GCs. It originates when the H-burning shell crosses the chemical discontinuity left over by the convective envelope soon after the first dredge-up, slowing down the evolutionary timescale.

3. The selection has been made by including only clusters with $(n_B - n_V)/n_B + n_V + n_R < 0.8$, where $n_B$, $n_V$ and $n_R$ represent the number of HB stars bluer than the RR Lyrae instability strip, within the strip and redder than the strip, respectively [39].
$T_8 \equiv T/10^8 \text{K}$ and $Z(\xi^2)$ is a function, generally $\mathcal{O}(1)$ for relevant stellar conditions, of $\xi^2 \equiv (\kappa_S/2T)^2$, with $\kappa_S$ being the Debye-Huckel screening wavenumber.

In order to assess the axion effects on stellar evolution and derive a bond on $g_{a\gamma}$, we have computed several evolutionary sequences of stellar models, from the pre-main-sequence to the asymptotic giant branch, with different initial mass (M), RGB mass loss rate, metallicity ($Z$), helium mass fraction ($Y$) and axion coupling ($g_{a\gamma}$). The models were computed by means of FUNS (FULL Network Stellar evolution), an hydrostatic 1D stellar evolution code \[40,42\]. Axion effects have been introduced as an additional energy sink. The nonstandard cooling is provided by Eq. (1), appropriately modified to include the effects of electron degeneracy and of non-zero plasma frequency, relevant for the evolution during the RGB phase \[27\].

Besides axion induced effects, proportional to $g_{a\gamma}^2$, as expected from Eq. (1), variations of $R$ may be caused by changes of the parameters characterizing the cluster, such as age, metallicity or He content. Our numerical analysis shows negligible variations of $R$ for initial stellar masses in the range $0.82 \leq M/M_\odot \leq 0.84$ and metallicities in $0.0002 \leq Z \leq 0.001$, which correspond to cluster ages between 11.1 and 13.3 Gyr and $-1.9 \leq [M/H] \leq -1.1$, respectively. On the other hand, we find a linear dependence of $R$ on the He mass fraction of the cluster. The relation

$$R_{\text{th}}(g_{a\gamma}, Y) = 6.26 Y - 0.41 g_{a\gamma}^2 - 0.12,$$

(2)
describes very well our numerical results and shows the mentioned degeneracy between $Y$ and $g_{a\gamma}$. Evidently, an accurate determination of the He mass fraction in GCs is necessary to appropriately constrain the axion-photon coupling. Unfortunately measurements of helium abundance in GC stars are somewhat challenging. First of all, convection, rotational induced mixings and other secular phenomena, such as gravitational setting, modify the He abundance in the atmospheres of these stars. In addition, ultraviolet data are needed to perform He abundance analysis in stars, a spectroscopic window not achievable from Earth.

As discussed in the introduction, the primordial He is often adopted for GC stars. In any case, $Y_p$ represents a lower bound for the GC He mass fraction. Indirect estimations of $Y_p$ can be derived from Big Bang Nucleosynthesis (BBN) calculations \[13\]. In the Standard BBN scenario, the Planck experiment predicted $Y_p=0.24725 \pm 0.00032$ at 68 % confidence level, for the measured value of baryon density \[44\]. However, this result significantly depends on the expansion rate and, in turn, on the assumed number of neutrinos $N_{\text{eff}}$ \[43\]. Indeed, the Planck analysis finds $Y_p=0.254^{+0.041}_{-0.033}$ at 68 % confidence level \[44\], when $N_{\text{eff}}$ is left free.

Direct determinations of the primordial He are obtained by spectral analyses of low-metallicity extragalactic HII regions. The latest study by Izotov et al. \[36\] provides a trustable direct determination of the helium fraction, $Y_p = 0.254 \pm 0.003$, which is the benchmark value we consider in the present analysis.

The new bound for the axion-photon coupling.— In order to constrain the axion-photon coupling, we compare the average value of $R$ ($R_{\text{ave}}$) with the theoretical prediction ($R_{\text{th}}$). Assuming that the $R$ measurements are distributed as Gaussian variables, one can determine confidence levels for the different quantities. Our results are shown in Fig. 1. The vertical lines indicate, respectively, 68% CL (dark) and 95% CL (light) for $Y_p$ and $R_{\text{th}}$. The vertical rectangles indicate the 68% CL (dark) and 95% CL (light) for $g_{a\gamma}$. Previous bounds from HB lifetime \[27\], from the Cepheids observation \[34\], from CAST for light ALPs \[22,26\] and for QCD axions \[26\] are also shown.

![FIG. 1: $R$ parameter constraints to $Y$ and $g_{a\gamma}$. The vertical lines indicate respectively the 1σ (short-dotted curves) and 2σ (long-dotted curves) of $Y_p$. The dot-dashed vertical line indicate the preferred value of $Y_p$. The other bent curves correspond to the determination of $g_{a\gamma}$ as function of $Y$ from $R_{\text{th}}$ [Eq. (2)]. Specifically, the continuous curve corresponds to $R_{\text{th}} = R_{\text{ave}}$, while the short and long-dashed lines indicate, respectively, the 1σ and the 2σ ranges. The star represents the best fits for $Y_p = 0.254$. The shaded area delimits the combined 68% CL (dark) and 95% CL (light) for $Y_p$ and $R_{\text{th}}$. The vertical rectangles indicate the 68% CL (dark) and 95% CL (light) for $g_{a\gamma}$. Previous bounds from HB lifetime \[27\], from the Cepheids observations \[34\], from CAST for light ALPs \[22,26\] and for QCD axions \[26\] are also shown.](image)
and $R_{\text{th}}$, we find
$$g_{a\gamma} = 0.45^{+0.12}_{-0.16} \times 10^{-10} \text{ GeV}^{-1} \quad (68\% \text{ CL}),$$  
(3)
(the best-fit point is indicated with a star in Fig. 2) while
$$g_{a\gamma} < 0.66 \times 10^{-10} \text{ GeV}^{-1} \quad (95\% \text{ CL}).$$  
(4)
Given the slight discrepancy between the primordial value of $Y$ and the one inferred from $R_{\text{th}}$, one could be tempted to interpret our result as a hint for axions. However, its low statistical significance and the possible uncontrolled systematic uncertainties in the $R$ measurement suggest to thrust only the 2σ upper bound, coming from the combinations of the confidence levels of $R_{\text{th}}$ and $Y_p$, and shown by the light shaded area in the Figure. Of course, possible improvements of the observations may eventually lead to an increased confidence in a new physics effect.

As we have shown, the largest source of systematic error is the adopted helium mass fraction. Certainly the primordial He provides a lower bound to the GC He. One may argue that some chemical evolution occurred before the formation of the GC system so that their He content may be larger than the one we have assumed. On the other hand, the He content of the solar system provides a very conservative upper bound for the GC He. The He abundance in the early solar system is an input parameter of Standard Solar Models and its value is mostly constrained by the present solar system age, as derived by means of radioactive dating techniques of terrestrial and meteoritic materials. Piersanti et al. [45] found $Y_\odot = 0.269$ (vertical dot-dashed line in Fig. 1) in good agreement with other extant Standard Solar Models. By using this solar He mass fraction, instead of $Y_p$, we find a higher upper bound, namely $g_{a\gamma} < 0.76 \times 10^{-10} \text{ GeV}^{-1}$ (95% CL). However, this assumption would imply that no chemical evolution was occurred during the 8 Gyr elapsed between the GC and the solar system formation, in contrast with many well-known astronomical evidences. Therefore, the result obtained by adopting the Izotov et al. [34] result for the primordial He is definitely more realistic.

In Table I we summarize the various bounds obtained under the different assumptions on $Y$. Obviously, our analysis relies on the reliability of the adopted stellar models of RGB and HB stars. In the Appendix we will give a short summary of the state-of-the-art. A detailed study of the relevant uncertainties will be extensively presented in a forthcoming paper.

Discussion and Conclusions.— We have obtained a new and more stringent bound on the axion-photon coupling constant $g_{a\gamma}$ from an updated analysis of the $R$ parameter in 39 Galactic GCs. Our constrain, given in Eq. (4), represents the strongest limit on $g_{a\gamma}$ for QCD axions in a wide mass range. Only in the case of cold dark matter axions there is a stronger constrain, $g_{a\gamma} \lesssim 10^{-15} \text{ GeV}^{-1}$ from ADMX, and only for a narrow range around $m_a \sim 1 \mu \text{eV}$ [47]. As evident from Fig. 1, our result improves the previous long-standing bound from GCs [27], $g_{a\gamma} \lesssim 10^{-10} \text{ GeV}^{-1}$ and the more recent one from Cepheid stars, $g_{a\gamma} \lesssim 0.8 \times 10^{-10} \text{ GeV}^{-1}$ [34]. Moreover, it is a factor $\sim 4$ better than the current experimental bound on QCD axions from the CAST experiment (see Fig. 1). This is also the strongest constraint for generic ALPs, except in the extremely low mass region $m_a \lesssim 10^{-10} \text{ eV}$. There, a more stringent limit $g_{a\gamma} \lesssim 1 \times 10^{-11} \text{ GeV}^{-1}$ [48] or even $g_{a\gamma} \lesssim 3 \times 10^{-12} \text{ GeV}^{-1}$ [49] has been derived from the absence of $\gamma$-rays from SN 1987A.

Ultra-light ALPs with such a small coupling would play an important role in astrophysics. A particularly intriguing hint for these particles has been recently suggested by Very High-Energy gamma-ray experiments [24]. Indeed, photon-axion conversions in large-scale cosmic magnetic fields would reduce the opacity of the universe to TeV photons, explaining the anomalous spectral hardening found in the Very High-Energy gamma-ray spectra [50]. In particular, for realistic models of the cosmic magnetic field, this scenario would require $g_{a\gamma} \gtrsim 0.2 \times 10^{-10} \text{ GeV}^{-1}$ and $m_a \lesssim 10^{-7} \text{ eV}$ [51].

Remarkably, the coupling ranges discussed in this letter are accessible by new independent laboratory searches, such as the planned upgrade of the photon regeneration experiment ALPS at DESY [20, 52] and the next generation solar axion detector IAXO (International Axion Observatory) [53]. This confirms, once again, the nice synergy between astrophysical arguments and laboratory searches to corner axions and axion-like particles.

| TABLE I: axion-photon coupling bounds |
|--------------------------------------|
| $R$ | $Y$ | $g_{a\gamma}$ |
|--------------------------------------|
| bounds from $Y_p$ |
| up 95% | 1.33 | 0.269 | 0.66 |
| - | up 68% | 1.36 | 0.257 | 0.57 |
| - | central value | 1.39 | 0.254 | 0.45 |
| - | low 68% | 1.42 | 0.251 | 0.29 |
| - | low 95% | 1.45 | 0.248 | 0.00 |
| bounds from $Y_p^{\text{SBBN}}$ |
| up 95% | 1.33 | 0.2478 | 0.50 |
| - | up 68% | 1.36 | 0.2475 | 0.42 |
| - | central value | 1.39 | 0.2472 | 0.31 |
| - | low 68% | 1.42 | 0.2469 | 0.15 |
| - | low 95% | 1.45 | 0.2466 | 0.00 |
| bounds from $Y_\odot$ |
| up 95% | 1.33 | 0.269 | 0.76 |
| - | up 68% | 1.36 | 0.269 | 0.71 |

4 Serenelli et al. [44], by adopting the helioseismic determination of the present-day solar surface He abundance, found a slightly larger value, i.e. $Y_\odot = 0.278$. 
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Appendix A: Astrophysical uncertainties.—In the context of the present study, energy sources and sinks are the most important phenomena to take under control, because they directly affect stellar lifetimes. During the RGB phase, the nuclear energy production is regulated by the $^{14}$N(p,$\gamma$)$^{16}$O, which acts as a bottleneck of the shell H burning. After a dedicated experimental investigation made by the LUNA collaboration [54], a very accurate measurement of the astrophysical factor for $^{14}$N(p,$\gamma$)$^{16}$O is now available down to about 70 keV. The uncertainty of the reaction rate between 50 and 100 MK is lower than 10%. Concerning the HB phase, the $^4$He(2$\alpha$, $\gamma$)$^{12}$C and the $^{12}$C($\alpha$, $\gamma$)$^{16}$O reactions compete during the core H burning. For the triple-$\alpha$ reaction rate the uncertainty at the temperature of the core-He burning is expected to be lower than 10% [55, 56]. Definitely larger uncertainties affect the $^{12}$C($\alpha$, $\gamma$)$^{16}$O reaction. A recent R-matrix analysis, which includes all the available direct measurements [57], confirms previous finding [58], but reduces substantially the error bar. At $E=300$ keV they find $S(300) = 161 \pm 19_{\text{stat}}^{+8}_{\text{sys}}$. For the models presented here we have used the rate of [58]. Note, however, that the $^{12}$C($\alpha$, $\gamma$)$^{16}$O reaction only contributes to the energy production during the last 10-15% of the HB lifetime. Its rate mostly affects the final amount of C and O left in the core at the end of the He burning [59]. Asteroseismic studies of pulsating white dwarf may be used to evaluate the internal chemical stratification and, in turn, to constrain core He burning models [60]. As shown in [59], the C/O near the WD center also depends on the extension of the convective core that develops during the He burning. In particular, it was found that by means of the same treatment of convection we have adopted in the present study for HB models, the best agreement with the C/O measured in pulsating WDs is obtained when the $^{12}$C($\alpha$, $\gamma$)$^{16}$O reaction rate suggested [58] and confirmed by [57] is adopted. In other words, the WD constraint implies that a variation of the modeled convective boundary requires a corresponding compensative change of the $^{12}$C($\alpha$, $\gamma$)$^{16}$O rate. More relevant for the present analysis is that this compensation limits the possible variations of the HB lifetime, the quantity explicitly used in the R parameter calculation. Concerning energy sinks, plasma neutrino loss plays a fundamental role in the RGB evolution. We adopt the latest neutrino rate reported by Esposito et al. [61], which is in excellent agreement with previous independent calculations [62, 63].
