Generating Long-Lived Macroscopically Distinct Superposition States in Atomic Ensembles

Wei Qin 1, Adam Miranowicz 1,2, Hui Jing 1,3,† and Franco Nori 1,4,†

1Theoretical Quantum Physics Laboratory, RIKEN Cluster for Pioneering Research, Wako-shi, Saitama 351-0198, Japan
2Institute of Spintronics and Quantum Information, Faculty of Physics, Adam Mickiewicz University, 61-614 Poznań, Poland
3Key Laboratory of Low-Dimensional Quantum Structures and Quantum Control of Ministry of Education, Department of Physics and Synergetic Innovation Center for Quantum Effects and Applications, Hunan Normal University, Changsha 410081, China
4Department of Physics, The University of Michigan, Ann Arbor, Michigan 48109, USA

(Received 8 January 2021; revised 11 May 2021; accepted 2 July 2021; published 23 August 2021)

We propose to create and stabilize long-lived macroscopic quantum superposition states in atomic ensembles. We show that using a fully quantum parametric amplifier can cause the simultaneous decay of two atoms and, in turn, create stabilized atomic Schrödinger cat states. Remarkably, even with modest parameters these intracavity atomic cat states can have an extremely long lifetime, up to 4 orders of magnitude longer than that of intracavity photonic cat states under the same parameter conditions, reaching tens of milliseconds. This lifetime of atomic cat states is ultimately limited to several seconds by extremely weak spin relaxation and thermal noise. Our work opens up a new way toward the long-standing goal of generating large-size and long-lived cat states, with immediate interests both in fundamental studies and noise-immune quantum technologies.

DOI: 10.1103/PhysRevLett.127.093602

Introduction.—Schrödinger cat states, which are macroscopically distinct superposition states, express the essence of quantum mechanics. Such states are appealing not only for fundamental studies of quantum mechanics [1,2] but also for wide applications ranging from quantum metrology [3,4] to quantum computation [5–9]. So far, a large number of approaches [10–25] have been proposed to generate cat states. However, these cat states (especially of large size) are extremely fragile in a noisy environment, and their fast decoherence makes them impractical for applications. Thus, the ability to stabilize cat states, as an essential prerequisite for their various applications, is highly desirable. To address this problem, a two-photon loss has been engineered [26–29] and recently experimentally demonstrated [30–34]. Such a nonlinear loss can protect cat states against photon dephasing [29,35] but, unfortunately, not against the unavoidable single-photon loss. This implies a significantly limited cat-state lifetime. Single-photon loss has been considered to be the major source of noise in fault-tolerant quantum computation based on cat states [5–9]. Thus, the stabilization of large-size cat states for an extended time remains challenging.

Ensembles of atoms or spins have negligible spin relaxation; consequently, their major source of noise is spin dephasing, i.e., collective dephasing, local dephasing, and inhomogeneous broadening. This motivates us to engineer the simultaneous decay of two atoms of an ensemble (here denoted as “two-atom decay”) and then use it to stabilize atomic cat states. Such cat states could have a very long lifetime if the two-atom decay is possible. This is because such a decay may protect these atomic cat states against spin dephasing, which is a close analogy to the mechanism of using two-photon loss to suppress photon dephasing.

However, it seems to us that the two-atom decay, which is fundamentally different from two-photon loss, is still lacking. To implement it, here we propose to exploit fully quantum degenerate parametric amplification. More importantly, the lifetime of the resulting atomic cat states can be made up to 4 orders of magnitude longer than that of common intracavity photonic cat states (see Table I in [36]), i.e., equal superpositions of two opposite-phase coherent states. To ensure a fair comparison, these photonic cat states need to have the same size as our atomic cat states and also suffer from single-photon loss of the same rate as given for the signal mode. With a modest cavity decay time (∼16 μs), our cat-state lifetime can reach ∼20 ms. This is comparable to 17 ms [55], which is the longest lifetime of intracavity photonic cat states to date but which was achieved with an extreme cavity decay time (∼0.13 sec). As the cavity decay time increases, our cat-state lifetime can further increase but ultimately is limited to a maximum value determined by spin relaxation and thermal noise. For a typical spin relaxation time ∼40 sec [56,57], we can predict a maximum cat-state lifetime of ∼3 sec.

Physical model.—The central idea is illustrated in Fig. 1(a). To consider degenerate parametric amplification in the fully quantum regime, our system, inspired by recent experimental advances [31–33,58,59], contains two

---

*Key words: Quantum computing, quantum metrology, quantum cat states, quantum decoherence, quantum control*.
parametrically coupled cavities: one as a pump cavity with frequency $\omega_p$ and the other as a signal cavity with frequency $\omega_s$. We assume that the pump cavity is subject to a coherent drive with amplitude $\Omega$ and frequency $\omega_d$. The intercavity parametric coupling $J$ stimulates the conversion between pump single photons and pairs of signal photons. Furthermore, an ensemble of $N$ identical two-level atoms is placed in the signal cavity, and the atomic transition, of frequency $\omega_q$, is driven by a coupling $g$ to the signal photon. When $2\omega_q \approx \omega_p \ll 2\omega_s$, a pair of excited atoms can jointly emit a pump photon. The subsequent loss of the pump photon gives rise to the two-atom decay, which in turn stabilizes large-size, extremely long-lived cat states in the ensemble.

The system Hamiltonian in a frame rotating at $\omega_q$ is

$$ H = \sum_{i=p,s} \delta_i a_i^\dagger a_i + g(a_p S_+^i + a_s S_-^i) + \Omega(a_p + a_p^\dagger), $$

where $a_p$, $a_s$ are the annihilation operators for the pump and signal modes. $S_\pm = S_x \pm i S_y$, $\delta_p = \omega_p - \omega_d$, $\delta_s = \omega_s - \omega_d/2, \delta_q = \omega_q - \omega_d/2$. The collective spin operators are $S_a = \frac{1}{2} \sum_{j=1}^N \sigma_a^j$, with $\sigma_a^j$ (a = x, y, z) the Pauli matrices for the jth atom. The Lindblad dissipator, $\mathcal{L}(\rho) = \rho \sigma_p^\dagger - \frac{1}{2} \sigma_p^\dagger \rho - \frac{1}{2} \rho \sigma_p^\dagger$, describes the dissipative dynamics determined by

$$ \dot{\rho} = -i[H, \rho] + \sum_{i=p,s} \kappa_i \mathcal{L}(a_i) \rho, $$

where $\kappa_p$ and $\kappa_s$ are the photon loss rates of the pump and signal modes. Spin dephasing, spin relaxation, and thermal noise are discussed below.

We assume that $2\omega_q \approx \omega_p \approx \omega_d$, and the detuning $\Delta = \omega_s - \omega_d \gg \{g_{\text{col}}, J\}$. Here, $g_{\text{col}} = \sqrt{N}g$ represents the collective coupling of the ensemble to the signal mode. Then, we can predict a parametric coupling, $\chi = g_{\text{col}}^2 J/\Delta^2$, between atom pairs and pump single photons. Accordingly, the Hamiltonian $H$, after time averaging [60,61], becomes

$$ H_{\text{avg}} = \frac{\chi}{N} (a_p S_+^2 + a_s S_-^2) + \Omega(a_p + a_p^\dagger), $$

which describes a third-order process. The stronger second-order process has been eliminated with an appropriate detuning between $\omega_d$ and $2\omega_q$ (see [36]). To derive $H_{\text{avg}}$, we have considered the low-excitation regime, where the average number of excited atoms is much smaller than the total number of atoms.

We now adiabatically eliminate the pump mode $a_p$, yielding an effective master equation

$$ \dot{\rho}_{\text{ens}} = -i[H_{\text{ens}}, \rho_{\text{ens}}] + \frac{\kappa_{1\text{at}}}{N} \mathcal{L}(S_-) \rho_{\text{ens}} + \frac{\kappa_{2\text{at}}}{N^2} \mathcal{L}(S_-^2) \rho_{\text{ens}}, $$

where $H_{\text{ens}} = i\chi_{2\text{at}}(S_-^2 - S_+^2)/N$, and $\rho_{\text{ens}}$ represents the reduced density matrix of the ensemble. Here, $\chi_{2\text{at}} = 2\chi_2/\kappa_p$ and $\chi_{2\text{at}} = 2\chi_2/\kappa_p$ are the rates of the simultaneous decay and excitation of two atoms, respectively. Moreover, $\kappa_{1\text{at}} = (g_{\text{col}}/\Delta)^2 \kappa_s$ is the rate of the Purcell single-atom decay (see [36]), and we can tune it to be $\ll \kappa_{2\text{at}}$, as long as $\kappa_s \ll (g_{\text{col}}/\Delta)^2 \kappa_p$.

We note that the methods of Refs. [62–64] can lead to a Hamiltonian formally similar to $H_{\text{avg}}$. However, contrary to our method, the two-atom decay cannot be realized in those
methods assuming the strong cavity-photon loss. This is because those methods require a virtual cavity photon to mediate a third-order process, which indicates that the cavity-photon loss cannot be allowed to be strong; moreover, they also depend on a longitudinal coupling, which cannot be collectively enhanced in atomic ensembles.

To gain more insights into the engineered two-atom decay, we use the quantum Monte Carlo method [65]. In Figs. 1(b), 1(c), we plot a single quantum trajectory with the Hamiltonian $H$ and an initial state $|00\rangle|2\rangle$ (see [36] for more cases). Here, the first ket $|m_p, m_s\rangle$ ($m_p, m_s = 0, 1, 2, \ldots$) in the pair refers to the cavity state with $m_p$ pump photons and $m_s$ signal photons, and the second $|n\rangle$ ($n = 0, 1, 2, \ldots$) refers to the collective spin state $|S = N/2, m_z = -N/2 + n\rangle$, corresponding to $n$ excited atoms in the ensemble. The non-Hermitian Hamiltonian $H_{NH} = -i/2 \kappa_{at} a_p^\dagger a_p$ drives Rabi oscillations between $|00\rangle|2\rangle$ and $|10\rangle|0\rangle$, as shown in Fig. 1(b). The Rabi oscillations are then interrupted by a quantum jump $a_p$. We find from Fig. 1(c) that the jump leaves the system in its ground state $|00\rangle|0\rangle$, implying that single-photon loss of the pump mode causes the two-atom decay.

Stabilized manifold of atomic cat states.—When $\kappa_{at} = 0$, the dynamics of the effective master equation, Eq. (4), describes a pairwise exchange of atomic excitations between the ensemble and its environment, thus conserving the excitation-number parity. As demonstrated in [36], the ensemble is driven to an even cat state $|C_+\rangle = A_+ (|\theta, \phi\rangle + |\theta, \phi + \pi\rangle)$ if initialized in an even parity state, or to an odd cat state $|C_-\rangle = A_- (|\theta, \phi\rangle - |\theta, \phi + \pi\rangle)$ if initialized in an odd parity state. Here, $|\theta, \phi\rangle$, where $\phi = \pi/2$ and $\theta = 2 \arctan(|\alpha|/\sqrt{N})$, refers to a spin coherent state, and $A_{\pm} = 1/[2(1 \pm \exp(-2|\alpha|^2))]^{1/2}$. Moreover, $\alpha = i \sqrt{\Omega/\chi}$ is the coherent amplitude. The average number of excited atoms, $|\alpha|^2$, of the states $|C_\pm\rangle$ characterizes the cat size [55]. When assuming the initial state to be a spin coherent state $|\theta_0, \phi_0\rangle$, the steady state of the ensemble is confined into a quantum manifold spanned by the states $\{ |C_\pm\rangle |C_-\rangle \}$ and is expressed as $\rho_{\text{ens}}^{\alpha} = c_+ |C_+\rangle \langle C_+| + c_- |C_-\rangle \langle C_-| + c_{+\pm} |C_{\pm}\rangle \langle C_{\pm}|$, where $c_{+\pm} = 1/2 [1 + \exp(-2|\alpha|^2)]$ with $\alpha_0 = \sqrt{N} \exp (i\theta_0) \tan(\theta_0/2)$, $c_{-} = 1 - c_{+\pm}$, and $c_{+\pm}$ is given in [36]. To confirm these predictions, we numerically integrate [66,67], the master equation in Eq. (2), to simulate the time evolution of the preparation error $\eta = 1 - F$ in Fig. 1(d). Here, $F$ is the fidelity between the actual and ideal states. It is seen that, as expected, the ensemble states are steered into a stabilized 2D cat-state manifold with a high fidelity.

In the low-excitation regime considered above, the collective spin in fact behaves as a quantum harmonic oscillator. This allows us to map $S_\pm$ to a bosonic operator $b$, i.e., $S_\pm \approx \sqrt{N} b$, and thus to investigate cat states of large size ($|\alpha| \geq 2$) in large ensembles. The spin coherent state $|\theta, \phi\rangle$ accordingly becomes a bosonic coherent state $|\alpha\rangle$ such that the states $|C_\pm\rangle$ become $|C_\pm\rangle = A_\pm (|\alpha\rangle + |\alpha|\rangle)$. With the master equation in Eq. (2) and the bosonic approximation, we plot the time evolution of the preparation error $\eta$ in Fig. 2(a) and the Wigner function $W(\beta)$ for different times in Fig. 2(b). We find that a cat state of size $|\alpha|^2 = 4$ is obtained after time $t \sim 250/g_{\text{col}}$, or more specifically, $t \sim 4 \mu s$, for a typical collective coupling strength $g_{\text{col}}/2 \pi = 10 \text{ MHz}$ [56,68–71].

**FIG. 2.** (a) Time evolution of the preparation error $\eta$ of the states $|C_\pm\rangle$, $|C_-\rangle$, and $\rho_{\text{ens}}^{\alpha}$ under the bosonic approximation for different cat sizes $|\alpha|^2 = 2, 4$, and 6. The initial states are chosen as in Fig. 1(d). (b) Wigner function at times $t_1$, $t_2$, $t_3$, and $t_5$ shown on top of panel (a) for the $|\alpha|^2 = 4$ cat size. The first, second, and third rows correspond to the states $|C_\pm\rangle$, $|C_-\rangle$, and $\rho_{\text{ens}}^{\alpha}$, respectively. For all plots, we set $J = 3g_{\text{col}}$, $\delta_p = J^2/(20g_{\text{col}})$, $\kappa_p = 5 \chi$, and $\kappa_z = 0.3 \kappa_p$. 093602-3
**Suppressed spin dephasing.**—So far, we have assumed a model where there is no spin dephasing; however, there will always be some spin dephasing. Before discussing spin dephasing, let us first consider the rate $\gamma$ of convergence, i.e., how rapidly the steady cat states can be reached. To determine $\gamma$, we introduce the Liouvillian spectral gap, $\lambda = |\text{Re}[\lambda_1]|$, of the effective master equation in Eq. (4) for $\kappa_{1at} = 0$. Here, $\lambda_1$ is the Liouvillian eigenvalue with the smallest modulus of the real part. Since the gap $\lambda$ determines the slowest relaxation of the Liouvillian $[72]$, we thus conclude that $\gamma > \lambda$. In the inset of Fig. 3(a), we numerically calculate the gap $\lambda$ and find $\lambda \approx |\alpha|^2 \kappa_{2at}$ for $|\alpha|^2 \geq 2$.

Below we consider collective spin dephasing $\gamma_{col} \mathcal{L}(S_z) \rho_{ens}$, local spin dephasing $\gamma_{loc} \sum_{j=1}^N \mathcal{L}(\sigma_j^z) \rho_{ens}$, and inhomogeneous broadening $\frac{1}{2} \sum_{j=1}^N \delta_j \sigma_j^z$. Here, $\gamma_{col}$ and $\gamma_{loc}$ are the collective and local dephasing rates, respectively. Moreover, $\delta_j = \omega_j - \omega_q$, where $\omega_j$ is the transition frequency of the $j$th atom and $\omega_q$ can be considered as the average of transition frequencies of all the atoms $[36]$. We assume that the distribution of $\delta_j$ has a linewidth $\Delta_{inh}$. The three sources of dephasing noise conserve the excitation-number parity of the superradiant subspace, where the cat states are created and stabilized. Thus, all these dephasing processes can be strongly suppressed by the two-atom decay as long as $\gamma \gg \{\gamma_{col}, \gamma_{loc}, \Delta_{inh}\}$ (i.e., $|\alpha|^2 \kappa_{2at} \gg \{\gamma_{col}, \gamma_{loc}, \Delta_{inh}\}$) (see [36] for more details). Figure 3(a) shows the dependence of such a dissipative suppression on the ratio $\kappa_{2at}/\gamma_{dep}$, assuming $\gamma_{col} = \gamma_{loc} = \Delta_{inh} \equiv \gamma_{dep}$. It is seen that for $\kappa_{2at} = 10 \gamma_{dep}$, corresponding to an ensemble coherence time of $\gamma_{dep}^{-1} \sim 27 \mu s$, a steady cat state is generated, implying a significant suppression of spin dephasing. We note that in Fig. 3(a) the error $\eta$ is limited by a small $N$, especially for $\kappa_{2at} = 10 \gamma_{dep}$, and a larger $N$ could lead to a smaller $\eta$ until the bosonic approximation is well satisfied.

**Cat-state lifetime.**—Let us now consider the cat-state lifetime $\tau_{at}$. According to the above discussions, the effects of spin dephasing on $\tau_{at}$ can be excluded. This lifetime is thus determined by the Purcell decay rate $\Gamma_{1at} = 2|\alpha|^2 \kappa_{1at}$ such that

$$\tau_{at} = \frac{1}{\Gamma_{1at}} = \left(\frac{\Delta}{g_{col}}\right)^2 \frac{1}{2|\alpha|^2 \kappa_{1at}}. \quad (5)$$

Note that intracavity photonic cat states, i.e., equal superpositions of two opposite-phase coherent states, rapidly decohere into statistical mixtures due to single-photon loss. The lifetime of such photonic cat states is thus given by $\tau_{ph} = 1/2|\alpha|^2 \kappa_{1at}$ [73]. Here, for a fair comparison, we have assumed the same cat size $|\alpha|^2$ as our atomic cat states, and the same single-photon loss rate $\kappa_{1at}$ as given for the signal cavity. It is seen that $\tau_{at}$ is longer by a factor of $(\Delta/g_{col})^2$ compared to $\tau_{ph}$. To make $\tau_{at}/\tau_{ph}$ larger, it is essential to increase $\Delta/g_{col}$. However, the rate $\kappa_{2at}$, which needs to be $\gg \gamma_{dep}$ as mentioned already, decreases as $\Delta/g_{col}$ increases. Thus, the ratio $\Delta/g_{col}$ has an upper bound for a given $\gamma_{dep}$. Experimentally, the coherence time $\gamma_{dep}^{-1}$ of NV-spin ensembles has reached $\sim 1$ ms with spin-echo pulse sequences [74,75], and if dynamical-decoupling techniques are employed, it can be even close to 1 sec [76]. In Fig. 3(b), the ratio $\kappa_{2at}/\gamma_{dep}$ for different $\gamma_{dep}$, as well as the ratio $\tau_{at}/\tau_{ph}$, is plotted versus $\Delta/g_{col}$. Assuming
a realistic parameter of $\gamma_{\text{deph}}^{-1} = 1$ ms, we find from Fig. 3(b) that in stark contrast to previous work on intracavity photonic cat states (see Table I in [36]), our approach can lead to an increase in the cat-state lifetime of up to 4 orders of magnitude for $\kappa_{\text{cat}} \approx 15 \gamma_{\text{deph}}$ and a very large cat size of $|\alpha|^2 > 4$. Correspondingly, for a typical single-photon loss rate of $\kappa_s/2\pi = 10$ kHz (i.e., a cavity decay time $\sim 16 \mu$s) [31], the lifetime of the $|\alpha|^2 = 4$ cat states resulting from our approach is $\sim 20$ ms.

As the cavity loss rate $\kappa_s$ decreases, the lifetime $\tau_{\text{at}}$ further increases and ultimately reaches its maximum value, limited by spin relaxation and thermal noise (see [36] for more details). This maximum lifetime is given by $\tau_{\text{at}}^{\text{max}} = \Gamma_{\text{relax}}^{-1}$. Here, $\Gamma_{\text{relax}} = [2|\alpha|^2(1 + 2n_{\text{th}}) + 2n_{\text{th}}] \gamma_{\text{relax}}$ [77] is the cat-state decay rate arising from spin relaxation with a rate $\gamma_{\text{relax}}$ and thermal noise with a thermal average boson number $n_{\text{th}}$. For realistic parameters of $\gamma_{\text{relax}} = 2\pi \times 4$ mHz [56,57] and $T = 100$ mK, we can predict a maximum lifetime of $\tau_{\text{at}}^{\text{max}} \sim 3$ sec, which is more than 2 orders of magnitude longer than the longest lifetime, 17 ms, of the intracavity photonic cat states reported in Ref. [55].

**Conclusions.**—We have introduced a method to create and stabilize large-size, long-lived Schrödinger cat states in atomic ensembles. This method is based on the use of fully quantized degenerate parametric amplification to facilitate the simultaneous decay of two atoms, i.e., the two-atom decay. The resulting atomic cat states can last an extremely long time because of strongly suppressed spin dephasing and extremely weak spin relaxation and thermal noise. These long-lived cat states are promising for both fundamental tests and practical applications of quantum mechanics. Our work can further stimulate more efforts to create and protect macroscopic cat states or other fragile quantum states, and to use them to improve the performance of various modern quantum technologies.

We thank Carlos Sánchez Muñoz and Fabrizio Minganti for their valuable discussions. H. J. is supported by the National Natural Science Foundation of China (Grants No. 11935006 and No. 11774086) and the Science and Technology Innovation Program of Hunan Province (Grant No. 2020RC4047). A. M. is supported by the Polish National Science Centre (NCN) under the Maestro Grant No. DEC-2019/34/A/ST2/00081. F. N. is supported in part by Nippon Telegraph and Telephone Corporation (NTT) Research, the Japan Science and Technology Agency (JST) [via the Quantum Leap Flagship Program (Q-LEAP) program, the Moonshot R&D Grant No. JPMJMS2061, and the Centers of Research Excellence in Science and Technology (CREST) Grant No. JPMJCR1676], the Japan Society for the Promotion of Science (JSPS) [via the Grants-in-Aid for Scientific Research (KAKENHI) Grant No. JP20H00134 and the JSPS–RFBR Grant No. JPJSBP120194828], the Army Research Office (ARO) (Grant No. W911NF-18-1-0358), the Asian Office of Aerospace Research and Development (AOARD) (via Grant No. FA2386-20-1-4069), and the Foundational Questions Institute Fund (FQXi) via Grant No. FQXi-IAF19-06.

* jinghui73@foxmail.com
* fnori@riken.jp

[1] W. H. Zurek, Decoherence, einselection, and the quantum origins of the classical, Rev. Mod. Phys. 75, 715 (2003).
[2] S. Haroche, Nobel lecture: Controlling photons in a box and exploring the quantum to classical boundary, Rev. Mod. Phys. 85, 1083 (2013).
[3] M. Kira, S. W. Koch, R. P. Smith, A. E. Hunter, and S. T. Cundiff, Quantum spectroscopy with Schrödinger-cat states, Nat. Phys. 7, 799 (2011).
[4] L. Pezzè, A. Smerzi, M. K. Oberthaler, R. Schmied, and P. Treutlein, Quantum metrology with nonclassical states of atomic ensembles, Rev. Mod. Phys. 90, 035005 (2018).
[5] T. C. Ralph, A. Gilchrist, G. J. Milburn, W. J. Munro, and S. Glancy, Quantum computation with optical coherent states, Phys. Rev. A 68, 042319 (2003).
[6] A. Gilchrist, K. Nemoto, W. J. Munro, T. C. Ralph, S. Glancy, S. L. Braunstein, and G. J. Milburn, Schrödinger cats and their power for quantum information processing, J. Opt. B: Quantum Semiclass. Opt. 6, S828 (2004).
[7] J. Gribbin, Computing with Quantum Cats: From Colossus to Qubits (Prometheus Books, New York, 2014).
[8] N. Ofek, A. Petrenko, R. Heeres, P. Reinhold, Z. Leghtas, B. Vlastakis, Y. Liu, L. Frunzio, S. M. Girvin, L. Jiang, M. Mirrahimi, M. H. Devoret, and R. J. Schoelkopf, Extending the lifetime of a quantum bit with error correction in superconducting circuits, Nature (London) 536, 441 (2016).
[9] W. Cai, Y. Ma, W. Wang, C.-L. Zou, and L. Sun, Bosonic quantum error correction codes in superconducting quantum circuits, Fund. Res. I, 50 (2021).
[10] G. S. Agarwal, R. R. Puri, and R. P. Singh, Atomic Schrödinger cat states, Phys. Rev. A 56, 2249 (1997).
[11] C. A. Sackett, D. Kielpinski, B. E. King, C. Langer, V. Meyer, C. J. Myatt, M. Rowe, Q. A. Turchette, W. M. Itano, D. J. Wineland, and C. Monroe, Experimental entanglement of four particles, Nature (London) 404, 256 (2000).
[12] D. Leibfried, E. Knill, S. Seidelin, J. Britton, R. B. Blakestad, J. Chiaverini, D. B Hume, W. M. Itano, J. D. Jost, C. Langer, R. Ozeri, R. Reichle, and D. J. Wineland, Creation of a six-atom ’Schrödinger cat’ state, Nature (London) 438, 639 (2005).
[13] A. Ourjoumtsev, R. Tualle-Broui, J. Laurat, and P. Grangier, Generating optical Schrödinger kittens for quantum information processing, Science 312, 83 (2006).
[14] A. Ourjoumtsev, H. Jeong, R. Tualle-Broui, and P. Grangier, Generation of optical ‘Schrödinger cats’ from photon number states, Nature (London) 448, 784 (2007).
[15] B. Vlastakis, G. Kirchmair, Z. Leghtas, S. E. Nigg, L. Frunzio, S. M. Girvin, M. Mirrahimi, M. H. Devoret, and R. J. Schoelkopf, Deterministically encoding quantum information using 100-photon Schrödinger cat states, Science 342, 607 (2013).
[16] T. Monz, P. Schindler, J. T. Barreiro, M. Chwalla, D. Nigg, W. A. Coish, M. Harlander, W. Hänsel, M. Henrich, and R. Blatt, 14-Qubit Entanglement: Creation and Coherence, Phys. Rev. Lett. **106**, 130506 (2011).

[17] H. W. Lau, Z. Dutton, T. Wang, and C. Simon, Proposal for the Creation and Optical Detection of Spin Cat states in Bose-Einstein Condensates, Phys. Rev. Lett. **113**, 090401 (2014).

[18] J. Etesse, M. Bouillard, B. Kanseri, and R. Tualle-Brouri, Quantum Manipulation of a Strongly Entangled Quantum State, Phys. Rev. Lett. **114**, 193602 (2015).

[19] J. Etesse, M. Bouillard, B. Kanseri, and R. Tualle-Brouri, Experimental Generation of Squeezed Cat States with an Operation Allowing Iterative Growth, Phys. Rev. Lett. **114**, 193602 (2015).

[20] C. E. Bradley, J. Randell, M. H. Abobeih, R. C. Berrevoets, M. J. Degen, M. A. Bakker, M. Markham, D. J. Twitchen, and T. H. Taminiau, A Ten-Qubit Solid-State Spin Register with Quantum Memory up to One Minute, Phys. Rev. X **9**, 031045 (2019).

[21] Y. Lu, S. Zhang, K. Zhang, W. Chen, Y. Shen, J. Zhang, J.-N. Zhang, and K. Kim, Global entangling gates on arbitrary ion qubits, Nature (London) **572**, 363 (2019).

[22] C. Figgatt, A. Ostrander, N. M. Linke, K. A. Landsman, D. Zhu, D. Maslov, and C. Monroe, Parallel entangling operations on a universal ion-trap quantum computer, Nature (London) **572**, 368 (2019).

[23] A. Omran, H. Levine, A. Keeling, G. Semeghini, T. T. Wang, S. Ebadi, H. Bernien, A. S. Zibrov, H. Pichler, S. Choi, J. Cui, M. Rossignolo, P. Rembold, S. Montangero, T. Calarco, M. Endres, M. Greiner, V. Vuletić, and M. D. Lukin, Generation and manipulation of Schrödinger cat states in Rydberg atom arrays, Science **365**, 570 (2019).

[24] C. Song, K. Xu, H. Li, Y.-R. Zhang, X. Zhang, W. Liu, Q. Guo, Z. Wang, W. Ren, J. Hao, H. Feng, H. Fan, D. Zheng, D.-W. Wang, H. Wang, and S.-Y. Zhu, Generation of multicomponent atomic Schrödinger cat states of up to 20 qubits, Science **365**, 574 (2019).

[25] K. X. Wei, I. Lauer, S. Srinivasan, N. Sundaresan, D. T. McClure, D. Toyli, D. C. McKay, J. M. Gambetta, and S. Sheldon, Verifying multipartite entangled Greenberger-Horne-Zeilinger states via multiple quantum coherences, Phys. Rev. A **101**, 032343 (2020).

[26] Y.-H. Chen, W. Qin, X. Wang, A. Miranowicz, and F. Nori, Shortcuts to Adiabaticity for the Quantum Rabi Model: Efficient Generation of Giant Entangled Cat States via Parametric Amplification, Phys. Rev. Lett. **126**, 023602 (2021).

[27] C. C. Gerry and E. E. Hach III, Generation of even and odd coherent states in a competitive two-photon process, Phys. Lett. A **174**, 185 (1993).

[28] L. Gilles, B. M. Garraway, and P. L. Knight, Generation of nonclassical light by dissipative two-photon processes, Phys. Rev. A **49**, 2785 (1994).

[29] R.I. Karasik, K.-P. Marzlin, B. C. Sanders, and K. B. Whaley, Criteria for dynamically stable decoherence-free subspaces and incoherently generated coherences, Phys. Rev. A **77**, 052301 (2008).

[30] M. Mirrahimi, Z. Leghtas, V. V. Albert, S. Touzard, R. J. Schoelkopf, L. Jiang, and M. H. Devoret, Dynamically protected cat-qubits: A new paradigm for universal quantum computation, New J. Phys. **16**, 045014 (2014).

[31] M. J. Everitt, T. P. Spiller, G. J. Milburn, R. D. Wilson, and A. M. Zagoskin, Engineering dissipative channels for realizing Schrödinger cats in SQUIDs, Front. ICT **1**, 1 (2014).

[32] Z. Leghtas, S. Touzard, I. M. Pop, A. Kou, B. Vlastakis, A. Petrenko, K. M. Sliwa, A. Narla, S. Shankar, M. J. Hatridge, M. Reagor, L. Frunzio, R. J. Schoelkopf, M. Mirrahimi, and M. H. Devoret, Confining the state of light to a quantum manifold by engineered two-photon loss, Science **347**, 853 (2015).

[33] S. Touzard, A. Grimm, Z. Leghtas, S. O. Mundhada, P. Reinhold, C. Axline, M. Reagor, K. Chou, J. Blumoff, K. M. Sliwa, S. Shankar, L. Frunzio, P. J. Schoelkopf, M. Mirrahimi, and M. H. Devoret, Coherent Oscillations inside a Quantum Manifold Stabilized by Dissipation, Phys. Rev. X **8**, 021005 (2018).

[34] R. Lescanne, M. Villiers, T. Peronnin, A. Sarlette, M. Delbecq, B. Huard, T. Kontos, M. Mirrahimi, and Z. Leghtas, Exponential suppression of bit-flips in a qubit encoded in an oscillator, Nat. Phys. **16**, 509 (2020).

[35] A. Grimms, N. E. Frattini, S. Furi, S. O. Mundhada, S. Touzard, M. Mirrahimi, S. M. Girvin, S. Shankar, and M. H. Devoret, Stabilization and operation of a Kerr-cat qubit, Nature (London) **584**, 205 (2020).

[36] J. Cohen, Autonomous quantum error correction with superconducting qubits, Ph.D. thesis, PSL Research University, 2017.

[37] See Supplemental Material, which includes Refs. [36–53], at http://link.aps.org/supplemental/10.1103/PhysRevLett.127.093602 for details about the generation of steady atomic cat states, the detailed analyses and comparisons of atomic and photonic cat-state lifetimes, and more discussions on suppressing the effects of spin dephasing.

[38] F. Reiter and A. S. Sørensen, Effective operator formalism for open quantum systems, Phys. Rev. A **85**, 032111 (2012).

[39] V. V. Albert and L. Jiang, Symmetries and conserved quantities in Lindblad master equations, Phys. Rev. A **89**, 022118 (2014).

[40] M. Brune, E. Hagley, J. Dreyer, X. Maître, A. Maali, C. Wunderlich, J. M. Raimond, and S. Haroche, Observing the Progressive Decoherence of the “Meter” in a Quantum Measurement, Phys. Rev. Lett. **77**, 4887 (1996).

[41] Z. Wang, M. Pechal, E. A. Wollack, P. Arrangoiz-Ariolla, M. Gao, N. R. Lee, and A. H. Safavi-Naeini, Quantum Dynamics of a Few-Photon Parametric Oscillator, Phys. Rev. X **9**, 021049 (2019).

[42] F. Assemat, D. Grosso, A. Signoles, A. Facon, I. Dotsenko, S. Haroche, and L. Sun, Demonstration of Controlled-Phase Gates between Two Error-Correctable Photonic Qubits, Phys. Rev. Lett. **124**, 120501 (2020).

[43] B. P. Venkatesh, M. L. Juan, and O. Romero-Isart, Cooperative effects in closely packed quantum emitters with collective dephasing, Phys. Rev. Lett. **120**, 033602 (2018).

[44] H. Hattermann, D. Bohner, L. Y. Ley, B. Ferdinand, D. Wiedmaier, L. J. Säker, R. Kleiner, D. Koelle, and J. Fortagh, Coupling ultracold atoms to a superconducting
C. W. S. Chang, C. Sabin, P. Forn-Diaz, F. Quijandria, A. M. Vadraj, I. Nsanzineza, G. Johansson, and C. M. Wilson, Observation of three-photon spontaneous parametric down-conversion in a superconducting parametric cavity, Phys. Rev. X 10, 011011 (2020).

A. Vrajitoarea, Z. Huang, P. Groszkowski, J. Koch, and A. A. Houck, Quantum control of an oscillator using a stimulated Josephson nonlinearity, Nat. Phys. 16, 211 (2020).

O. Gamel and D. F. V. James, Time-averaged quantum dynamics and the validity of the effective Hamiltonian model, Phys. Rev. A 82, 052106 (2010).

W. Shao, C. Wu, and X.-L. Feng, Generalized James’ effective Hamiltonian method, Phys. Rev. A 95, 032124 (2017).

L. Garziano, V. Macrì, R. Stassi, O. Di Stefano, F. Nori, and S. Savasta, One Photon can Simultaneously Excite Two or More Atoms, Phys. Rev. Lett. 117, 043601 (2016).

V. Macrì, F. Nori, S. Savasta, and D. Zueco, Spin squeezing by one-photon–two-atom excitation processes in atomic ensembles, Phys. Rev. A 101, 053818 (2020).

L. Garziano, A. Ridolfo, A. Miranowicz, F. Falci, S. Savasta, and F. Nori, Atoms in separated resonators can jointly absorb a single photon, Sci. Rep. 10, 21660 (2020).

M. O. Scully and M. S. Zubairy, Quantum Optics (Cambridge University Press, Cambridge, England, 1997).

J. R. Johansson, P. D. Nation, and F. Nori, Quipit: An open-source Python framework for the dynamics of open quantum systems, Comput. Phys. Commun. 183, 1760 (2012).

J. R. Johansson, P. D. Nation, and F. Nori, Quipit 2: A Python framework for the dynamics of open quantum systems, Comput. Phys. Commun. 184, 1234 (2013).

Y. Kubo, F. R. Ong, P. Bertet, D. Vion, V. Jacques, D. Zheng, A. Dréau, J.-F. Roch, A. Auffèves, F. Jelezko, J. Wrachtrup, M. F. Barthe, P. Bergonzo, and D. Esteve, Strong Coupling of a Spin Ensemble to a Superconducting Resonator, Phys. Rev. Lett. 105, 140502 (2010).

Y. Kubo, I. Diniz, A. Dewes, V. Jacques, A. Dréau, J.-F. Roch, A. Auffèves, D. Vion, D. Esteve, and P. Bertet, Storage and retrieval of a microwave field in a spin ensemble, Phys. Rev. A 85, 012333 (2012).

S. Putz, D. O. Krimer, R. Amsuess, A. Valookaran, T. Noebauer, J. Schmiedmayer, S. Rotter, and J. Majer, Protecting a spin ensemble against decoherence in the strong-coupling regime of cavity QED, Nat. Phys. 10, 720 (2014).

T. Astner, S. Nevlacisil, N. Peterschofsky, A. Angerer, S. Rotter, S. Putz, J. Schmiedmayer, and J. Majer, Coherent Coupling of Remote Spin Ensembles via a Cavity Bus, Phys. Rev. Lett. 118, 140502 (2017).

F. Minganti, A. Biella, N. Bartolo, and C. Ciuti, Spectral theory of Liouvillians for dissipative phase transitions, Phys. Rev. A 98, 042118 (2018).

S. Haroche and J.-M. Raimond, Exploring the Quantum: Atoms, Cavities, and Photons (Oxford Univ. press, New York, 2006).
[74] E. L. Hahn, Spin echoes, Phys. Rev. 80, 580 (1950).

[75] P. L. Stanwix, L. M. Pham, J. R. Maze, D. Le Sage, T. K. Yeung, P. Cappellaro, P. R. Hemmer, A. Yacoby, M. D. Lukin, and R. L. Walsworth, Coherence of nitrogen-vacancy electronic spin ensembles in diamond, Phys. Rev. B 82, 201201(R) (2010).

[76] N. Bar-Gill, L. M. Pham, A. Jarmola, D. Budker, and R. L. Walsworth, Solid-state electronic spin coherence time approaching one second, Nat. Commun. 4, 1743 (2013).

[77] M. S. Kim and V. Bužek, Schrödinger-cat states at finite temperature: Influence of a finite-temperature heat bath on quantum interferences, Phys. Rev. A 46, 4239 (1992).