Monte Carlo simulations of a coarse grained model for an athermal all-polystyrene nanocomposite system

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Abstract: The structure of a polystyrene matrix filled with tightly cross-linked polystyrene nanoparticles, forming an athermal nanocomposite system, is investigated by means of a Monte Carlo sampling formalism. The polymer chains are represented as random walks and the system is described through a coarse grained Hamiltonian. This approach is related to self-consistent-field theory but does not invoke a saddle point approximation and is suitable for treating large three-dimensional systems. The local structure of the polymer matrix in the vicinity of the nanoparticles is found to be different in many ways from that of the corresponding bulk, both at the segment and the chain level. The local polymer density profile near to the particle displays a maximum and the bonds develop considerable orientation parallel to the nanoparticle surface. The depletion layer thickness is also analyzed. The chains orient with their longest dimension parallel to the surface of the particles. Their intrinsic shape, as characterized by spans and principal moments of inertia, is found to be a strong function of position relative to the interface. The dispersion of many nanoparticles in the polymeric matrix leads to extension of the chains when their size is similar to the radius of the dispersed particles.

Introduction

Nanocomposite polymeric materials consist of nanoparticles dispersed in a polymeric matrix. This new family of composite materials displays a variety of properties that attract great scientific and industrial interest. The practice of adding nanoscale filler particles to reinforce polymeric materials can be traced back to the early years of the composite industry. The design of such conventional composites has focused on maximizing the interaction between the polymer matrix and the filler. This is commonly achieved by shrinking the filler particles in order to increase the surface area available for interaction with the matrix. With the appearance of synthetic methods that can produce nanometer sized fillers, resulting in an enormous increase of surface area, polymers reinforced with nanoscale particles should show vastly improved properties. Nanomaterials fabricated by dispersing nanoparticles in polymer melts have the potential for performances exceeding those of traditional composites by far.

Even though some property improvements have been achieved in nanocomposites, nanoparticle dispersion is difficult to control, with both thermodynamic and kinetic processes playing significant roles. It has been demonstrated that dispersed spherical nanoparticles can yield a range of multifunctional behaviour, including a viscosity decrease, reduction of thermal degradation, increased mechanical damping, enriched electrical and/or magnetic performance, and control of thermomechanical properties. The tailored properties of these systems are very important to the manufacturing procedure, as they fully overcome many of the existing operational limitations. As a final product, a polymeric matrix enriched with dispersed particles may have better properties than the neat polymeric material and can be used in more demanding and novel applications. Therefore, an understanding and quantitative description of the physicochemical properties of these materials is of major importance for their successful production.

The physical and chemical behavior of this kind of materials depends on the nature of the nanodispersed phase. The characteristics of the surface of the particles significantly affect the behavior of the composite polymeric / particle system. In some cases, the dispersed nanoparticles in the polymeric matrix may aggregate. The presence of particles with grafted chains improves wetting effects in the system and suppresses aggregation, leading the material to dramatically different performance.

Extensive experimental work on all-polystyrene nanocomposites has been recently presented. Regarding the conformational properties, the dimensions of matrix chains, measured by neutron scattering techniques, indicate swelling induced by the dispersed tightly cross-linked nanoparticles. This effect occurs only when the radius of gyration of the chain is larger than the nanoparticle radius. The all-polymer composite system appears to be a stable blend even for small interparticle distances, suggesting that chain shape in the polymer matrix is highly distorted. As for the dynamic properties, the blend viscosity was found to demonstrate a non-Einstein-like decrease with nanoparticle volume fraction. It was suggested that this phenomenon scales with the change in free volume introduced by the nanoparticles, while the entanglements seem to be totally unaffected.

The effect of incorporating a spherical nanoparticle on the conformational properties of a polymer has been demonstrated by means of Monte Carlo (MC) simulations for dilute and semi-dilute solutions. These studies have been quite generic, employing a bead-spring and hard-sphere representation for the polymer and the nanoparticle, respectively. The most significant changes in structural properties and orientation occurred within the depletion layer. The effective interactions between two dispersed nanoparticles in a polymer solution have been quantified by calculating the potential of mean force through the expanded ensemble density of states technique. An oscillating long-range behaviour has been revealed.

Efforts have also been made to predict the aggregation or the dispersion of polymer nanoparticles in polymer matrix by thermodynamic modelling. Recent advances are thoroughly reviewed and include compressible regular solution free energy models based on modification of theories for binary polymer blends, and generalizations of integral equation theories such as the microscopic Polymer Reference Interaction Site Model (PRISM). The proposed models extend existing theories by incorporating specific nanoparticle-nanoparticle and nanoparticle-polymer contributions. The predicted phase diagrams indicate that such systems exhibit a rich variety of behaviours, including upper critical solution temperature-type, lower critical solution temperature-type, and hour-glass shape.

A major challenge in simulating realistic nanocomposite materi-
als is that both the length and the time scales cannot be adequately treated by means of atomistic simulations because of the extensive computational load. This is why a variety of mesosopic techniques have been developed for these particular systems. Among them, Self-Consistent Field Theory (SCFT) seems to be a well-founded simulation tool. This method adopts a field-theoretic description of the polymeric fluids and makes a saddle-point (mean-field) approximation. Significant progress has been made in applying the SCFT to nanoparticle-filled polymer matrices in the dilute and semi-dilute region. A lattice-based simulation in the context of the Scheutjens-Fleer approximation has cast some light onto the equilibrium dispersion of nanoparticles with grafted polymer chains into dense polymer matrices, where the matrix and the brushes share the same chemical structure. An attempt to overcome the restrictions posed by the saddle-point approximation was made in. The coordinates of all particles in the system were explicitly retained as degrees of freedom. It was crucial to update simultaneously the coordinates and the chemical potential field variables.

In the same spirit of relaxing the mean field approximation, Balazs and coworkers have proposed a coupling of SCFT for the inhomogeneous polymers and density functional theory (DFT) for the nanoparticles. The extrema of the approximate energy functional created in this way correspond to the mean-field solution. Although the SCFT-DFT approach is quite promising, it is currently hindered by the difficulty in extending to systems for which reliable density functionals are not available.

A novel way of incorporating fluctuation effects in self-consistent mean-field theories has been recently proposed. The “Single Chain in Mean Field” simulation technique is particle-based and founded on an ensemble of independent chains in fluctuating, external fields. The fields mimic the effect of the instantaneous interactions of a molecule with its neighborhood. They are frequently updated using the spatially inhomogeneous density distribution of the ensemble. The explicit conformations of the molecules evolve by Monte Carlo. This technique has been very successful in describing the self-assembly and the ordering of block copolymers on patterned substrates encountered in processes such as nanolithography.

The present work examines the structure of a polymer matrix in the vicinity of polymeric nanoparticles. Particular attention is given to capturing the orientational effects and the chain conformation of the matrix in a dense, polymeric nano-filled composite. The analysis is based on a coarse grained Monte Carlo simulation method which can be readily applied to the complex three-dimensional nanocomposite system. Although the level of description is quite abstract (i.e. that of the freely-jointed chain for the matrix), the developed model tries to predict the behaviour of a nanocomposite with specific chemistry, namely of an all-poly styrene material. A main characteristic of the method is that it treats in a different manner the interaction between polymer and between polymer and particle: the former is accounted for through a suitable functional of the local densities, while the latter is described directly by an explicit interaction potential.

**Method**

**Polymer Coarse Grained Model**

The aim of the developed coarse grained model is to describe the properties of the nanocomposite material at mesoscopic length scales. The main parameters are the chain connectivity, the finite compressibility of the melt and explicit pairwise potentials for the van der Waals interactions between polymer segment - nanoparticle and nanoparticle - nanoparticle. The system is contained in volume $V$ at temperature $T$. The matrix consists of $n$ polymeric chains which are considered to obey the freely jointed chain model. Each chain consists of $N$ Kuhn segments. The bond length is kept fixed and is equal to the Kuhn length, $b$, of the specific polymer under consideration. The $n_p$ nanoparticles are represented as impenetrable spheres. The interaction energy $\mathcal{H}$ includes only non-bonded contributions:

$$\mathcal{H}(\bar{r}) = \mathcal{H}_{pp}(\bar{\rho}(\bar{r})) + \mathcal{H}_{pn} + \mathcal{H}_{nn}$$

where $\mathcal{H}_{pp}$ stands for the non-bonded interactions between the polymeric chains, $\mathcal{H}_{pn}$ for the interaction between polymeric segments and nanoparticles and $\mathcal{H}_{nn}$ for the interaction between nanoparticles.

An important difference in the treatment of polymer-polymer interactions compared to those arising because of the presence of the nanoparticle is that the former are taken into account through a suitable functional of the instantaneous local density $\bar{\rho}(\bar{r})$, while the latter are accounted for by a pairwise interaction potential. The local density is computed directly from the segment positions by a smoothing procedure. The non-bonded interactions $\mathcal{H}_{pp}$ are given by:

$$\beta \mathcal{H}_{pp}(\bar{\rho}(\bar{r})) = \frac{\rho_0}{N} \int d^3\bar{r} \left( \frac{\kappa_0 N}{2} [\bar{\rho}(\bar{r}) - 1]^2 \right)$$

where $\beta = \frac{1}{k_B T}$, with $k_B$ being the Boltzmann constant and $\rho_0$ is the average bulk number density of segments. Deviations of the local density from the average bulk value are restricted by the quadratic term which stems from Helfand’s approximation. Thus, the melt has a finite compressibility, which is inversely proportional to $\kappa_0$:

$$\kappa_0 = \frac{1}{k_B T \kappa_T \rho_0}$$

Although the coordinates of the particles, either polymeric segments or nanoparticles, are the degrees of freedom in our model, the local densities that appear in (??) are not defined by the microscopic expression $\bar{\rho}(\bar{r}) = \sum_{j=1}^{N} \sum_{i=1}^{n_p} \delta(\bar{r} - \bar{r}_{ij})$. Rather, they are obtained by a particle-to-mesh (PM) assignment technique. A uniform, rectangular grid with $n_{sites}$ sites is introduced. The local densities are defined on each site by applying a smoothing procedure to the bead’s position. As a consequence, a discretization parameter $\Delta L$ has to be introduced; it is the grid spacing. Phenomena and details of the system whose length scales are smaller than the $\Delta L$ parameter cannot be described accurately. Thus, this parameter sets the resolution level of our observations. It also defines a sort of microscopic cutoff, since it determines the range of interaction between neighboring beads. It follows that $\Delta L$ must not be less than the average distance between two beads. The value at which $\Delta L$ should be set depends strongly on the system of interest and the preferred smoothing procedure.

The assignment procedure of a polymeric bead to the sites of the rectangular grid is shown in Figure. The $i$-th segment of the $j$-th chain at position $\bar{r}_{ij}$ shown as a black dot, yields a contribution to a neighboring $m$-th site, shown as white dot, $\Pi [\bar{r}_{ij}, \bar{c}_m]$, where $\bar{c}_m$ is the position of the centre of the $m$th site and $\Pi$ the assignment function. The resulting normalized density at site $m$ is calculated as the sum of the contributions of all segments in the system, giving the instantaneous number of segments assigned to the site:

$$\bar{\rho}_m = \rho_{m}^{nor} \sum_{j=1}^{n} \sum_{i=0}^{N} \Pi [\bar{r}_{ij}, \bar{c}_m] \left( 1 - \frac{1}{2} (\delta_{j,0} + \delta_{j,N}) \right)$$

with $\delta$ the Kronecker delta.

The normalization constant $\rho_{m}^{nor}$ represents the segment number density that the site $m$ would have, provided that the melt was completely homogeneous without any density fluctuation, $\rho_{m}^{nor} = \frac{\rho_0}{n_p}$. But in reality, $\rho_{m}^{nor}$ is a smoothed version of $\rho_{m}$, with $\rho_0$ the average density of the melt.

$$\rho_{m}^{nor} = \left( \frac{\rho_0}{n_p} \right) \frac{\sum_{j=1}^{n} \sum_{i=0}^{N} \Pi [\bar{r}_{ij}, \bar{c}_m]}{\sum_{j=1}^{n} \sum_{i=0}^{N} \Pi [\bar{r}_{ij}, \bar{c}_m]}$$
Nanoparticle-polymer and nanoparticle-nanoparticle interaction

The effect of dispersing bare nanoparticles in the polymer matrix is explicitly accounted. Pairwise potentials describing the effective interaction between polymeric segment - nanoparticle, \( U_{pn}^{eff} \), and nanoparticle - nanoparticle, \( U_{nn}^{eff} \) are introduced. The overall explicit energetic effect is taken into account in the Hamiltonian by summing up these interactions for all possible pairs of nanoparticles and polymeric segments:

\[
\mathcal{H}_{pn}^{n} = \sum_{i=1}^{n} \sum_{j=1}^{n} U_{pn}^{eff} (\vec{r}_{i} - \vec{r}_{j}) 
\]

and

\[
\mathcal{H}_{nn}^{n} = \sum_{i=1}^{n-1} \sum_{j=i+1}^{n} U_{nn}^{eff} (\vec{r}_{i} - \vec{r}_{j}) .
\]

The reference energy level of the employed Hamiltonian (9) for the homopolymer melt is that of a melt with uniform density profile. In this case, the effective interaction energy between two polymeric beads is taken as zero. The effective potentials introduced in (9) and (10) should be such that, if the volume of the nanoparticles was occupied by bulk homopolymer, then the energy of the system would be zero. The insertion of a nanoparticle in a uniformly-distributed melt can be thermodynamically accomplished in two steps: a spherical volume of polymer, whose net interaction with the rest of the polymer matrix is \( U_{pp}^{equiv-p} \), is removed from the melt and a nanoparticle with equal volume is placed in its position, introducing a new net interaction \( U_{pn}^{equiv-n} \) with the remaining bulk polymer (Figure 2 from step A to step B). Thus, the net interactions between polymer-polymer should be subtracted from the net interactions between polymer-nanoparticle:

\[
U_{pn}^{eff} = U_{pn} - U_{pp}^{equiv-n} .
\]

The treatment of the effective interactions between two nanoparticles is more sophisticated. Their insertion in the melt, following the above thermodynamic way, requires two more additional steps with respect to the previous case. A second spherical volume of polymer is removed from the melt in the presence of one nanoparticle, whose net interaction with the rest of the system is \( U_{pn}^{equiv-n} \), and the second particle is inserted in the created volume, introducing new net interaction \( U_{nn}^{equiv-n} \) with the composite system (Figure 2 from step B to step C):

\[
U_{nn}^{eff} = U_{nn} - 2U_{pn}^{equiv-n} + U_{pp}^{equiv-n} .
\]

The coarse grained potentials describing the net interactions involved in (9) and (10) are derived on the grounds of Hamaker theory. A major advantage is that the existence of accurate atomistic potentials describing these interactions is exploited. The need to introduce empirically adjustable parameters is kept to a minimum. The integrated potentials are computationally effective. Each particle is treated as a collection of atoms which interact only with atoms of different particles:

\[
U_{pn} (r_{12}) = \int_{sphere_{1}} \int_{sphere_{2}} \rho_{1} (\vec{r}_{1}) \rho_{2} (\vec{r}_{2}) U_{LJ} (r_{12}) dV_{1} dV_{2} .
\]

where \( \rho_{1} \) and \( \rho_{2} \) stand for the density of interaction centres in each particle, \( r_{12} \) is the distance between the centres of the particles, and \( dV_{1}, dV_{2} \) the elementary volumes of each particle. The discrete distribution of the interacting atoms in each particle is assumed to be continuous and uniform. The shape of the particles is spherical. An analytical closed-form solution can be rigorously derived,
provided that the atomistic potential is Lennard-Jones 12-6. The pairwise interaction potentials used for polymeric segment and nanoparticles with the energy axis scaled by $k_B T$. The density of the nanoparticle is $1.15 \frac{g}{cm^3}$ and its radius is $R_n = 36 \, \text{Å}$. The radius of the polymeric segment interaction site $R_s$ is $6.7 \, \text{Å}$. The centre-to-centre distance is shifted by $R_s + R_p$ in the case of the polymeric segment-nanoparticle interaction (main figure) and by $2R_n$ in the case of nanoparticle - nanoparticle interaction (inset).

### Details of the Monte Carlo Simulations

All simulations were carried out in the canonical statistical ensemble (NVT). The temperature of the system was 400 K. The box was cubic and its edge length was 600 Å. It should be noted that, for all chain lengths, the edge length is greater than $4R_p$ with $R_p$ being the radius of gyration of a chain, so as to avoid finite size effects. The systems studied were strictly monodisperse, while the degree of polymerization of the chains $N$ was varied, with $N = 32, 64, 128$ and 256 beads. The corresponding molecular weights are 23, 47, 93 and 187 kg/mol, respectively. The number of chains in the systems is varied according to chain length so that the mean density of the polymer in the accessible volume is 0.97 g/cm$^3$. The Kuhn segment length $b$ is 18.3 Å, which is assigned to seven styrene monomers. The radius of the nanoparticle is 36 Å. The density of the crosslinked polystyrene nanoparticle is 1.15 g/cm$^3$. The characteristics of the systems studied, i.e. the degree of polymerization of the chain, the radius and the mean density of the crosslinked polystyrene nanoparticle, are in close connection with systems that have been studied experimentally by MacKay and co-workers.

In our initial calculations, a single nanoparticle is placed at the centre of the simulation box. The polymer chains are built randomly with the constraint that none of the polymeric beads overlaps with the nanoparticle. When more than one particles had to be contained in a configuration, then the nanoparticles were placed first at randomly selected positions, so that they did not overlap, and then the polymer was built around them. The initial configurations created by this method have large local density fluctuations. These fluctuations increase with increasing chain length. A zero temperature Monte Carlo optimization procedure took place in order...
attempted: 39.9 %

When the Monte Carlo proceeds, the internal shape of the chains is restructured by four intramolecular moves: the flip, the end rotation, the reptation and the pivot moves. The exact mix of moves and acceptance rates of the moves are given in Table 1 for pure melt polystyrene system. The nanoparticles are allowed to translate in random directions every 500 MC steps.

Table 1. Mixture of MC moves used for equilibration of pure melt of chains with 32 polymeric segments per chain

| Move          | % Attempted | % Accepted |
|---------------|-------------|------------|
| Rigid translation | 8 %         | 62.3 %     |
| Rigid rotation  | 8 %         | 42.7 %     |
| Rigid reflection| 8 %         | 39.9 %     |
| Rigid inversion | 8 %         | 37.5 %     |
| Rigid exchange | 8 %         | 35.5 %     |
| Flip           | 15 %        | 77.5 %     |
| End rotation   | 15 %        | 70.4 %     |
| Reptation      | 15 %        | 61.8 %     |
| Pivot          | 15 %        | 53.9 %     |

Results

Local polymer structure in the presence of a nanoparticle

The local structure in the vicinity of the nanoparticle at the Kuhn segment level is first studied through the radial mass density distribution from the surface of the nanoparticle, which is displayed in Figure 6. The beads of the polymer have been classified in 1.5-Å-thick spherical shells whose origin is nanoparticle’s centre. The distance of the closest segment from the nanoparticle surface is approximately equal to 7 Å, which corresponds to the radial distribution of segments and the position in each case does not depend on the number of Kuhn segments of the chain. This second peak is located roughly one segment diameter away from the first peak. Similar studies in the semi-dilute region have also shown that, as the polymer density was increased, the initially chain length-dependent peaks become independent. On the basis of the pertur-
bations in the total density profile from its bulk value, the thickness of the interface could be estimated as less than 40 Å. The typical length scale characterizing the density distribution in the vicinity of the nanoparticle is the depletion layer thickness δ, which is shown in the inset of Figure 6. The depletion layer can be defined as the zone next to the particle where there are no polymer monomers. It is an equimolar dividing surface. The number of segments depleted is estimated by an appropriate mass balance and leads to an expression of the form:

\[ (R_n + \delta)^3 - R_n^3 = 3 \int_{R_n}^{\infty} r^2 \cdot (1 - g(r)) \, dr \]  

(14)

where \( R_n \) is the radius of the nanoparticle and \( g(r) = \rho(r) / \rho_0 \) is the pair distribution function between the nanoparticle and the polymeric segments around it. As shown in the inset to Figure 6, the thickness of the depletion layer increases slightly with increasing the number of Kuhn segments in a chain. The value is close to the radius calculated for the segment’s spherical interaction site.

The local orientation of chain segments induced by the nanoparticle can be quantified by the second order Legendre polynomial \( P_2 \). An angle \( \theta \) may be defined by the bond vector of two consecutive Kuhn segments \( i \) and \( i+1 \) and the vector connecting the centre of the nanoparticle with the Kuhn segment \( i \). This angle is used to define the \( P_2 \) function: 

\[ P_2 = \frac{1}{2} (3(\cos^2 \theta) - 1) \]

\( P_2 \) would assume values of -0.5, 0.0, and 1.0 for bonds characterized by perfectly parallel, random, and perpendicular orientation relative to the surface of the particle, respectively. Figure 7 displays the radial distribution of \( P_2 \) from the centre of a nanoparticle, accumulated in 5-Å-thick bins. A given bond is assigned to the bin in which its \( i \) Kuhn segment resides. The bonds lying in the vicinity of the particle are structured and tend to be oriented tangentially to the interface. Chain length effects on the orientational distribution of bonds are weak. The tangential orientation tends to be stronger for the shortest chains examined. The shorter the chain, the more intense the orientational effects are. Kuhn segment orientation effects are weak beyond a distance of two Kuhn segment lengths from the particle surface. Similar behavior has been observed in molecular dynamics simulations of silica particles dispersed in a polyethylene-like matrix.43

One of the most important aspects of structure in polymer melts is the so-called “correlation hole” effect. It arises in dense polymeric fluids because of the melt’s incompressibility. Figure 8 shows the variation of the total and the intermolecular pair distribution functions between polymeric segments. The correlation hole effect is evident in the intermolecular distribution functions. On very short length scales, the total distribution function diverges as \( 1/r \) because of the intramolecular contribution dictated by the freely jointed model. This is an artificial effect, caused by the fact that chain self-intersection is not prevented in the freely jointed chains used in our calculations. In the regime of small distances, segments of other molecules are expelled from the volume of a reference chain and this gives rise to a correlation hole in the intermolecular pair distribution function. The spike in the total pair distribution function is an intramolecular feature, caused by pairs of segments connected directly by a Kuhn segment. If an atomistic description were used, this spike would be replaced by a series of intramolecular peaks reflecting the bonded geometry and conformational preferences of polystyrene molecules. On the other hand, for large length scales, the intermolecular distribution function approaches unity, as the intramolecular distribution function approaches zero. As shown in the inset of Figure 8, longer chains exhibit “correlation hole” effect for slightly longer distances.
**Chain structure in the presence of a nanoparticle**

Complementary to the study of local structure at the segment level, long range structural features may be revealed by probing properties at the level of entire chains. The distribution of the centre-of-mass (COM) of the entire chains around the nanoparticle, which is shown in Figure 9, is such an example. The COMs of the chains are classified in 4.5-Å-thick bins. It should be noted that the results at the level of the entire chains are more prone to statistical noise, because the number of binned chains is considerably smaller than the number of polymeric beads. There are polymeric chains whose COM position lies inside the nanoparticle. These chains engulf the nanoparticles. The shorter the polymeric chains, the more intense the penetration of the nanoparticles into the chains.

![Figure 9. Chain centre of mass distribution, accumulated in 4.5-Å-thick bins, for N = 32 (continuous line), N = 64 (long-dashed line), N = 128 (short-dashed line) and N = 256 (dotted line).](image)

The overall shape of the chains is explored by determining their spans and the eigenvalues of their radius of gyration tensor. Spans are defined according to Rubin and Mazur: they are the dimensions of the smallest orthorhombic box that can completely enclose the chain segment cloud. Our analysis, presented for spans in Figure 10(a) leads to the conclusion that the overall shape of the segment cloud is strongly affected by the presence of the spherical nanoparticle. Near the surface of the nanoparticle, chains tend to expand along their main axis (largest span, $W_3$, increases) and shrink along the smaller ones (spans $W_2$ and $W_1$ decrease). The same tendency is revealed through an examination of the eigenvalues of the chain radius of gyration tensor. In the polymer melt, polymers have the shape of flattened ellipsoids. For an ellipsoid formed by a random walk model, the ratio of the three eigenvalues is reported to be $12 : 2 : 1$. In our simulations, even the smallest chains are in excellent agreement with this prediction, as far as the small and the medium ellipsoidal semiaxes ($L_1$ and $L_2$) are concerned. At shorter distances from the nanoparticle centre than the mean size of the chain, an expansion of the chains across their face of the nanoparticle is explored by computing order parameters. Near the surface of the nanoparticle, chains tend to expand along their main axis (largest span, $W_3$, increases) and shrink along the smaller ones (spans $W_2$ and $W_1$ decrease). The overall shape of chain segment cloud is dependent on position relative to the nanoparticle. The systems consists of chains with 32 Kuhn segments per chain and one nanoparticle of radius 36 Å.

![Figure 10. Overall shape of chains as a function of centre of mass position. (a, top) Spans of chains, normalized by their sum $W = W_1 + W_2 + W_3$. (b, bottom) Eigenvalues of the chain radius of gyration tensor $L_1^2, L_2^2, L_3^2$. These plots reveal that the overall shape of chain segment cloud is dependent on position relative to the nanoparticle. The systems consists of chains with 32 Kuhn segments per chain and one nanoparticle of radius 36 Å.](image)
here for the segments $S_n = (1/2) \left[ 3(\cos^2(\theta)) - 1 \right]$. The angle $\theta$ is formed between the larger span $W_3$ and the vector connecting the centre of the nanoparticle and the centre of mass of the chain. The same is done for the smallest span, $W_1$. Plotted in Figure 11(a) are the order parameters for the shortest and longest spans as functions of the chain centre of mass position. In the same fashion, $S_2$ is the order parameter of the eigenvectors corresponding to the greater and smaller eigenvalues (Figure 11(b)). In the interfacial region, we observe a strong tendency for the longest span to orient parallel to the surface and the shortest span to orient perpendicular to the surface of the nanoparticle. This tendency remains unchanged if, instead of spans, the principal axes of inertia (i.e., the eigenvectors of the radius of gyration tensor) are used as measures of shape (Figure 11(b)). The reorientation of chains is confined to a region whose width is commensurate with $R_g$.

\begin{align*}
\theta &= \sin^{-1}\left(\frac{R_g - R_0}{a}\right)
\end{align*}

Figure 11. (a, top) Order parameters for the longest and shortest spans of chains as functions of centre of mass position. (b, bottom) Order parameters for the eigenvectors corresponding to the largest and the smallest eigenvalues of the chain radius of gyration tensor as functions on the centre of mass position. The systems consists of chains with 32 Kuhn segments per chain and one nanoparticle of radius 36 Å.

**Chain conformation in the presence of many nanoparticles**

The values of radius of gyration $R_g$, relative to the value for the pure polymer melt $R_{g0}$, are shown in Figure 12 as a function of the nanoparticle volume fraction for the four different chain lengths used in this work. In general, an expansion of polymeric chains with increasing nanoparticle volume fraction is observed for all chain lengths. This expansion is maximal for 32 Kuhn segments per chain, where the radius of gyration $R_{g0} = 42$ Å is comparable to the radius of the nanoparticle $R_n = 36$ Å. It seems that there is a tendency of chains to swell when their dimension is equal to or approaches the dimension of the nanoparticle. This observation is in very good quantitative agreement with experimental data reported for the same system. In all other cases, the swelling due to the presence of the nanoparticles is hardly distinguished.

\begin{align*}
R_g &= R_{g0} \left(1 + \frac{V_n}{V_p} \right)
\end{align*}

In the presence of many nanoparticles, structural features may be revealed by probing the pair distribution function between the nanoparticles and the polymer chain centres of mass. The COM of the chains are accumulated in 4.5-Å-thick bins (Figure 13). The pair distribution function depicted, is indicative of the engulfment of nanoparticles by the polymeric chains. There are polymeric chains of every chain length, whose COM position lies inside the nanoparticle. There is a remarkable difference between Figure 13 (many nanoparticles) and Figure 9 (one nanoparticle). In Figure 9, the COMs of longer chains are more depleted in the space occupied by the nanoparticle. In Figure 13, the shortest chains of $N = 32$ exhibit a tendency to surround the nanoparticles, having a clear maximum in their COM distribution inside the nanoparticle, very close to its centre, also outside the nanoparticle, some distance from its surface, with a minimum in between. Interestingly, with increasing distance the nanoparticle-chain centre of mass distribution goes through a minimum and then rises again a short distance away from the nanoparticle surface, because of the contribution of chains which are adsorbed to, but do not engulf the nanoparticle.

**Conclusions**

The structure of a polymer matrix surrounding an immersed spherical nanoparticle was studied in detail both at the segment and the chain levels. The simulation method employed relies on a hybrid Monte Carlo formalism. It is a field theoretic approach, based on the grounds of the self-consistent field, which can treat efficiently large systems. The system investigated bears great resemblance with an athermal, all-polystyrene nanocomposite material that has been studied experimentally. Several conformational properties of the system have been examined. At the segment level, an increase of the local polymer density around the nanoparticle is found. Density profiles are weakly dependent on the chain length. An increase of the degree of polymerization of the chain results in slightly increased thickness of the depletion layer. The bonds tend to ori-
ent parallel to the nanoparticle surface, as revealed by the second Legendre polynomial. All these effects have a characteristic length scale commensurate with the chain segment size.

At the chain level, chain centres of mass are able to penetrate the interior of the particle, as chains engulf the particle. This phenomenon is more pronounced when the radius of gyration of chains is comparable in size to the nanoparticle. The formation of chain pairs around the particle is suggested by the particle-polymer centre of mass pair distribution function. The size and the shape of the chains are also affected. A flattening of polymer molecules when their centre of mass is close to the nanoparticle centre is revealed by both the chain spans and the eigenvalues of the radius of gyration tensor. This deformation of the polymer molecules is small for long chains.

In the case of the dispersion of many nanoparticles, deformation of the chain shape is observed. The chains which share the same length scale with the dispersed particles tend to swell. This is in agreement with recent neutron scattering measurements. The radius of gyration increases with increased nanoparticle volume fraction.

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References

References

(1) Gersappe, D. Phys. Rev. Lett. 2002, 89, 058301.
(2) Balazs, A. C.; Emrick, T.; Russel, T. P. Science 2006, 314, 1107.
(3) Bansal, A.; Yang, H.; Li, C.; Benicewicz, B. C.; Kumar, S. K.; Schadler, L. S. J. Polym. Sci., Part B: Polym. Phys. 2006, 44, 2944–2960.
(4) Lee, J. Y.; Buxton, G. A.; Balazs, A. C. J. Chem. Phys. 2004, 121, 5531–5540.
(5) Bockstaller, M. R.; Thomas, E. L. Phys. Rev. Lett. 2004, 93, 166106.
(6) Shi, M.; Araki, T.; Ade, H.; Kilicoyne, A. L. D.; Fisher, R.; Sokolov, J. C.; Rafalovich, M. H. Macromolecules 2006, 39.
(7) Strafford, K.; Adhikari, R.; Pagonabarraga, I.; Desplat, J.-C.; Cates, M. E. Science 2005, 309, 2198–2201.
(8) Tuteja, A.; Duxbury, P. M.; Mackay, M. E. Phys. Rev. Lett. 2008, 100, 077801.
(9) Mackay, M. E.; Tuteja, A.; Duxbury, P. M.; Hawker, C. J.; Horn, B. V.; Guan, Z.; Chen, G.; Krishnan, R. Science 2006, 311, 1740.
(10) Mackay, M. E.; Dao, T. T.; Tuteja, A.; Ho, D. L.; Van Horn, B.; Kim, C. J.; Ho-Cheol and Hawker Nat. Mater. 2003, 2, 762–766.
(11) Doxastakis, M.; Chen, Y.-L.; Guzman, O.; de Pablo, J. J. J. Chem. Phys. 2004, 120, 9335–9342.
(12) Doxastakis, M.; Chen, Y.-L.; de Pablo, J. J. J. Chem. Phys. 2005, 123, 034901.
(13) Hall, L. M.; Jayaraman, A.; Schweizer, K. S. Curr. Opin. Solid State Mater. Sci. 2010, 14, 38–48, Polymers.
(14) de Luzuriaga, A. R.; Grande, H. J.; Pomposo, J. A. J. Chem. Phys. 2009, 30, 084905.
(15) Pomposo, J. A.; de Luzuriaga, A. R.; Etchemendy, A.; RodrÃ­guez, J. Phys. Chem. Chem. Phys. 2008, 10, 650.
(16) Arthi Jayaraman, K. S. Macromolecules 2008, 41, 9430–9438.
(17) Hall, L. M.; Schweizer, K. S. J. Chem. Phys. 2008, 128, 234901.
(18) Fredrickson, G. H. The equilibrium theory of inhomogeneous polymers; Clarendon Press, 2006.
(19) Surve, M. Pyamitsyn, V.; Ganesan, V.; Langmuir 2006, 22, 969–981.
(20) Surve, M.; Pyamitsyn, V.; Ganesan, V. Macromolecules 2007, 30, 434–534.
(21) Ganesan, V.; Khounlavong, L.; Pyamitsyn, V. Phys. Rev. E 2008, 78, 051804.
(22) Harton, S. E.; Kumar, S. K. J. Polym. Sci., Part B: Polym. Phys. 2008, 46, 351–358.
(23) Sides, S. W.; Kim, B. J.; Kramer, E. J.; Fredrickson, G. H. Phys. Rev. Lett. 2006, 96, 250601.
(24) Thompson, R. B.; Ginzbarg, V. V.; Matsen, M. W.; Balazs, A. C. Macromolecules 2002, 35, 1069–1071.
(25) Buxton, G. A.; Lee, Y. J.; Balazs, A. C. Macromolecules 2003, 36, 9631–9637.
(26) Lee, J. Y.; Shou, Z.; Balazs, A. C. Phys. Rev. Lett. 2003, 91, 136103.
(27) Daouals, K. C.; Muller, M. J. Chem. Phys. 2006, 125, 184904.
(28) Daouals, K. C.; Muller, M.; Pablo, J.; Nealey, P.; Smith, G. Soft Matter 2006, 2, 573–583.
(29) Detcheverry, F. A.; Pike, D. Q.; Nealey, P. F.; Muller, M.; de Pablo, J. J. Phys. Rev. Lett. 2009, 102, 197801.
(30) Detcheverry, F. A.; Kang, H.; Daouals, K. C.; Muller, M.; Nealey, P. F.; Pablo, J. J. Macromolecules 2008, 41, 4989–5001.
(31) Stoykovich, M. P.; Daouals, K. C.; Muller, M.; Kang, H.; de Pablo, J. J.; Nealey, P. F. Macromolecules 2010, 43, 2334–2342.
(32) Helfand, E.; Tagami, Y. J. Chem. Phys. 1972, 56, 3592.
(33) Dodd, L. R.; Theodorou, D. N. Mol. Phys. 1991, 72, 1313.
(34) Laradj, M.; Guo, H.; Zuckermann, M. J. Phys. Rev. E 1994, 49, 3199–206.
(35) Hienzen, P. C. Principles of colloid and surface chemistry, 2nd ed.; Dekker, 1977.
(36) Hamaker, H. Physica(Amsterdam) 1937, IV, 1058.
(37) Everaers, R.; Eijhoudt, M. Phys.Rev.E 2003, 67, 041710.
(38) Spyrion, T.; Tzoumanekas, C.; Theodorou, D.; Mäijler-Plathe, F.; Milano, G. Macromolecules 2007, 40, 3876–3885.
(39) Good, R. J.; Hope, C. J. J. Chem. Phys. 1971, 55, 111.
(40) Marsaglia, G. Ann. Math. Stat. 1972, 43, 645–646.
(41) Auð, R.; Everaers, R.; Grest, G. S.; Kremer, K.; Plimpton, S. J. J. Chem. Phys. 2003, 119, 12718.
(42) Aarts, D. G. L.; Tümer, R.; Lekkerkerker, H. N. W. J. Phys.: Condens. Matter 2002, 14, 7551–7561.
(43) Brown, D.; Marcadon, V.; MATTIA, P.; AlbÅFronà, N. D. Macromolecules 2008, 41, 1499–1511.
(44) Rubin, J.; Maozur, Macromolecules 1977, 10, 139–149.
(45) Theodorou, D. N.; Sutter, U. W. Macromolecules 1985, 18, 1206–1214.
(46) Picu, R. C.; Oszmosi, M. S. J. Chem. Phys. 2003, 118, 11239–11248.
(47) Mansfield, K. F.; Theodorou, D. N. Macromolecules 1990, 23, 4430–4445.
(48) Mansfield, K. F.; Theodorou, D. N. Macromolecules 1991, 24, 4295–4309.