Research Article
Multiobjective Location Routing Problem considering Uncertain Data after Disasters

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1. Introduction

In recent years, man-made or natural disasters which caused huge casualties and economic losses occurred frequently in different regions and countries. Timely and effective rescue works are very important after disasters. The emergency logistics management mainly includes two aspects [1]: the facility location problem (FLP) and the vehicle routing problem (VRP). In fact, there is a close relationship between facility location problem and vehicle routing problem about emergency logistics, that is, location routing problem (LRP). Compared with the traditional transportation logistics, the facility location problem and vehicle routing problem about emergency logistics are more challenging and complex [2]. von Boventer [3] combined the facility location problem and the vehicle routing problem. Up to now, there have been abundant research results about LRP [4, 5].

After disasters, there are a high degree of uncertainties in all aspects, such as the relief demands and the path transport capacities. Three major methods for dealing with the uncertain parameters are stochastic programming, fuzzy method, and robust optimization method. Ahmadi-Javid and Seddighi [6] studied a stochastic LRP problem. The materials which were provided by facilities are random variables. Under uncertain demands in the short time after disasters [7], large scale emergency scheduling problems were studied, including the selection of supply points, route selection, the decisions of the transport quantities, and the distribution methods, and the fuzzy set was applied to express the uncertain demands. Zare Mehrjerdi and Nadizadeh [8] studied the LRP problem with capacity restrictions of the vehicles and the distribution centers. Triangular fuzzy number represented the uncertainty demands. Lu [9] considered the robust weighted P-center model, and the travel time and demands of affected points were all uncertain. Wang et al. [10] proposed a dynamic time-space network model. It was a network flow model with multistages and multimaterials. Robust optimization method was applied to deal with the uncertain demand. Wang et al. [11] proposed a multiobjective location routing model with split delivery. It optimized the allocation of reliefs after earthquake. The objectives were to minimize the travel time, to minimize the total costs including the fixed costs of the distribution centers and the vehicle transportation costs and to maximize the path reliability, but the demands of disaster points and the probabilities of available arcs were certain. Koç et al. [12] studied the LRP problem with time windows. It was a certain problem with heterogeneous fleets and with split delivery, and the objective was to minimize the total costs.
It can be seen from the existing literatures that there are little researches on LRP problem with uncertain parameters which are solved by robust optimization. In this paper, the robust optimization method is used to deal with the uncertain demands and the uncertain velocities between two disaster points on the paths. In addition, the most scholars take the cost as the objective of LRP problem. Actually, the distances and the travel time between two points after disasters will be affected, and we will pay the price. Then, the distance and travel time can be understood as the travel cost. In this paper, the half-time windows constraints are quoted, so the time when the materials reach the demand points cannot be later than the specified time. Thus, the timeliness of emergency rescues is improved. After disasters, all kinds of materials are in short supplies, so it is very important to possess adequate relief supplies. Therefore, the minimization of the total distribution costs is one of the objectives, and the maximization of the worst path satisfaction rates is the second objective. After incidents, the transport network will be destroyed. In order to find a better path, the maximization of path transport capacities is the third objective in this paper.

2. The Problem Description

Generally, the distribution network of reliefs after disasters is described as a graph $G = (V, E)$. $V$ is a vertex set, and $M = \{n+1, n+2, \ldots, n+m\}$ is a set of candidate distribution centers. We assume that there are no demands for a point in the set $M$. $N = \{1, 2, \ldots, n\}$ is disaster point set. $E = \{(i, j) : i, j \in V, i \neq j\}$ is effective arc set. $K = \{1, 2, \ldots, k\}$ is vehicle set. This paper considers the following three objectives:

1. Minimize total costs including fixed costs and vehicle transportation costs.
2. Maximize the minimum material satisfaction rates of demand points.
3. Maximize the transport capacities of the worst path. (The transport capacities are represented by the velocities of the vehicle.)

This paper has the following assumptions:

1. The disaster points and the candidate distribution centers are known and the capacities of the candidate distribution centers are large enough.
2. The available arcs and distances between two points on the transport network are known.
3. Because the reliefs are calculated by volume, different types of relief supplies can be regarded as a kind of material.
4. The relief demands of the demand points are greater than or equal to the amounts of supplies because of the materials shortage after disasters.
5. In this paper, we can only consider the disaster points which can be serviced by vehicles, and the disaster points which can be serviced by the special transportation methods (e.g., helicopters) are ignored.

The parameters and variables used in this paper are introduced in Notations.

3. The Multiobjectives LRP Model

3.1. Objective 1: Minimization of the Total Distribution Cost—$\min f_1$. In the location routing problem, it is necessary to determine the number and location of the distribution centers and to arrange the disaster points to the distribution centers, and the corresponding vehicle routing will be decided. Therefore, the total costs of the relief distributions include the fixed costs of distribution centers and the vehicle transport costs.

$$f_1 = \sum_{j \in M} f_j x_j + \sum_{k \in K} \sum_{(i,j) \in E} c_k d_{ij} y_{ijk}.$$  \hspace{1cm} (1)

3.2. Objective 2: Maximization of the Worst Path Satisfaction Rates—$\max f_2$. We hope that reliefs can reach the demand point timely and effectively after disasters, so we should consider the relief satisfaction rates of the demand points. We hope to maximize the relief satisfaction rates in affected areas, and the fairness of the relief distributions is taken into account. Therefore, the second objective is maximization of the worst satisfaction rates.

$$f_2 = \min_{i \in N} r_i,$$ \hspace{1cm} (2)

where $r_i = \sum_{k \in K} q_{ik}/D_i$, $\forall i \in N$, is called the relief satisfaction rate of demand point $i$. The demands of point $i$ are uncertain: $D_i \in [D_{i-}, D_{i+}]$, $\forall i \in N$, $0 \leq D_{i-} < D_{i+}$.

3.3. Objective 3: Maximization of the Worst Path Transport Capacities—$\max f_3$. The original paths after disasters are affected more or less. At this time, we take into account the path transport capacities, and the worst path transport capacities are maximized in this paper. The sum of velocities indicates the path transport capacities. The vehicle velocities are uncertain. Let $v_{ij} \in [v_{ij-}, v_{ij+}], \forall(i, j) \in E$, $0 < v_{ij-} < v_{ij+}$.

$$f_3 = \min_{k \in K} \sum_{(i,j) \in E} v_{ij} y_{ijk}.$$ \hspace{1cm} (3)

The following formulas are the constraint conditions. In addition, the constraints conditions (4), (5), (6), (7), (8), (9), (16), (17), and (18) of the literature [11] are still used in our study.

$$t_{ik} - t_{jk} + s_i + d_{ij} \leq M(1 - y_{ijk}), \hspace{1cm} \forall (i, j) \in E, k \in K,$$ \hspace{1cm} (4)

$$t_{ik} \leq \tilde{t}_i, \hspace{1cm} \forall i \in N, k \in K,$$ \hspace{1cm} (5)

$$\sum_{i \in N} \sum_{k \in K} q_{ik} \leq Q,$$ \hspace{1cm} (6)

$$\sum_{i \in N} q_{ik} \leq L_k, \hspace{1cm} \forall k \in K,$$ \hspace{1cm} (7)
\[ q_{ik} \geq 0, \quad \forall k \in K, \quad i \in N, \quad (8) \]
\[ y_{ijk} \in \{0, 1\}, \quad \forall (i, j) \in E, \quad k \in K. \quad (9) \]

Formulas (4) and (5) are the time window constraints. \( M \) is a large positive number. This article requires that the sum of travel time and the service time is not bigger than the set time. Constraint (6) shows that the total amounts of reliefs delivered from the distribution centers to the disaster points shall not exceed the total amounts of available reliefs. Constraint (7) ensures that the relief volume transported to the affected areas by vehicle cannot exceed the load capacities of vehicles. Constraints (8)-(9) ensure that the decision variables are 0-1 nonnegative variables.

There are subloop elimination constraints in order to avoid the subloop. The constraints proposed by Dror et al. [13] are applied in this paper. Let \( d_i \) indicate the outgoing degree of point \( i: d_i = \sum_{k \in K} \sum_{j \in V} y_{ijk} \ (i \in N) \).

\[ \sum_{k \in K} \sum_{j \in V} y_{ijk} \leq \sum_{i \in N} d_i - k, \quad (10) \]
\[ \sum_{k \in K} \sum_{i \in N} y_{ijk} \leq 1, \quad \forall (i, j) \in E, \quad k \in K, \]
\[ \sum_{k \in K} \sum_{j \in V} y_{ijk} \geq 1, \quad \forall i \in N, \]
\[ \sum_{j \in V} y_{ijk} \leq 1, \quad \forall i \in N, \quad k \in K. \]

### 4. The Solution Method of This Model

#### 4.1. Data Uncertainty Description and Robust Solution

The travel velocities of vehicles on each arc are uncertain, so the interval of the vehicles travel velocity on arc \((i, j)\) is \( v_{ij} \in [\underline{v}_{ij}, \overline{v}_{ij}] \), \( \forall (i, j) \in E, \quad 0 < \underline{v}_{ij} < \overline{v}_{ij} \). The relief demands on each point \( i \) are uncertain too. The relief demands on each point \( i \) are

\[ D_i = [\underline{D}_i, \overline{D}_i], \quad \forall i \in N, \quad 0 \leq \underline{D}_i < \overline{D}_i. \quad (11) \]

Let \( z = (X, Y) \) be a feasible scheme for the above model, where \( X = \{x_j \mid j \in M\} \) and \( Y = \{y_{ijk}, \ (i, j) \in E\} \). Let \( Z \) be the feasible solutions set, so a scheme \( z \in Z \) corresponds to a group of \( q_{ik}(z) \) and a path \( r(z) \). \( S = [\underline{D}_i, \overline{D}_i] \times [\underline{v}_{ij}, \overline{v}_{ij}], \quad \forall i \in N, \quad (i, j) \in E \) indicates Cartesian product of two intervals. \( s \in S \) is called a scenario. In order to facilitate the description of the problem, \( f_2, f_3 \) are changed equally.

\[ f'_2 = \max_{s \in S} \frac{D_i}{\sum_{k \in K} q_{ik}}, \quad (12) \]
\[ f'_3 = \max \left\{ \frac{1}{\sum_{(i, j) \in E} v_{ij} y_{ijk}}, \quad \forall k \in K \right\}. \quad (13) \]

Given a scenario, problems (12) and (13) are certain. In certain problem the objective function 2 is

\[ F_2(s) = \max_{z \in Z} f'_2(s, z). \quad (14) \]

We need to define the maximum velocities sum of path \( r(z) \) under the scheme \( z \) and the scenario \( s \).

\[ v(z, s, r(z)) = \max \left\{ \sum_{(i, j) \in r(z)} v_{ij}, \quad \forall k \in K \right\}. \quad (15) \]

\[ f''_3(s, z) = \max_{z \in Z} \frac{1}{v(z, s, r(z))}. \quad (16) \]

The objective function 3 is expressed by formula (17) under the scheme \( z \) and the scenario \( s \).

\[ F_3(s) = \max_{z \in Z} f''_3(s, z). \quad (17) \]

The robust deviations \( \text{dev}_2(z, s) \) and \( \text{dev}_3(z, s) \) about formulas (12) and (16) under the scheme \( z \) and the scenario \( s \) are indicated by formulas (18). Let \( z^*(s) \) be the optimal scheme of (14) and (17) under scenario \( s \).

\[ \text{dev}_2(z, s) = f'_2(z, s) - f'_2(z^*(s), s), \]
\[ \text{dev}_3(z, s) = f''_3(z, s) - f''_3(z^*(s), s). \quad (18) \]

The robust costs of a scheme can be represented by the following problems:

\[ r_{c2}(z) = \max_{s \in S} \text{dev}_2(z, s), \quad (19) \]
\[ r_{c3}(z) = \max_{s \in S} \text{dev}_3(z, s). \quad (20) \]

The second objective and the third objective of the above problem can be expressed as follows:

\[ \min_{z \in Z} r_{c2}(z), \quad (21) \]
\[ \min_{z \in Z} r_{c3}(z). \]

Formula (21) implies minimizing the maximum of the robust deviations.

#### 4.2. Robust Cost Analysis

Because the uncertain demands and uncertain transport velocities are represented by continuous intervals, the scenario set is an infinite set. Therefore, it is very difficult to get the estimate values of \( r_{c2}(z), \ r_{c3}(z) \). To find the worst scenario under scheme \( z \) is an urgent problem. Let \( s_i(z) \) be a scenario introduced by scheme \( z \) on the point \( i \), and \( r(z) \) is the corresponding path for scheme \( z \). The following two assumptions are satisfied:

1. The demands of point \( i \) equal the corresponding upper bound \( D_i = \overline{D}_i \), and the demands of other points equal the corresponding lower bound \( D_i = \underline{D}_i \), \( j \neq i \).
(2) The transport velocities of arc on the path \( r(z) \) equal the corresponding lower bounds \( v_{ij} = \bar{v}_{ij} \) \((i, j) \in r(z)\), and the transport velocities of arc on the other paths equal the corresponding upper bounds \( v_{ij} = \bar{v}_{ij} \) \((i, j) \notin r(z)\). \( s_i(z) \) and \( s_i \) can be used to make the following changes.

**Lemma 1.** With the above introduction of \( s_i \) and \( \mathfrak{s} \), for a scheme \( z \),

\[
\begin{align*}
r_c^2(z) &= f_3^2 \left( \mathfrak{s}, z \right) - f_3^2 \left( \mathfrak{s}^*, (\mathfrak{s}) \right) \\
&= f_3^2 \left( s_i, z \right) - f_3^2 \left( s_i, z^* \left( s_i \right) \right), \quad (22) \\
r_c^3(z) &= f_3^3 \left( \mathfrak{s}, z \right) - f_3^3 \left( \mathfrak{s}, z^* \left( \mathfrak{s} \right) \right) \\
&= f_3^3 \left( s_i, z \right) - f_3^3 \left( s_i, z^* \left( s_i \right) \right),
\end{align*}
\]

where \( z^* \) and \( z^* \) are optimal schemes under the scenarios \( \mathfrak{s} \) and \( s_i \).

**Proof.** Taking the second objective function as an example, the third objective function can be proved by the same method. Let \( z^* \) be the optimal solution of problem (14), and \( (\mathfrak{s}, z^* (\mathfrak{s})) \) is the optimal solution of problem (19).

**Main Claim.** \((\mathfrak{s}, z^* (\mathfrak{s})) \) is the optimal solution of problem (19), so \( \mathfrak{s} \) is the worst scenario under scheme \( z \), and \( z^* \) is the optimal scheme of \( F_2 (s_i) \). Then the following formulas can be obtained:

\[
\begin{align*}
f_3^2 \left( s_i, z \right) - f_3^2 \left( s_i, z^* \left( s_i \right) \right) &= f_3^2 \left( \mathfrak{s}, z \right) - f_3^2 \left( \mathfrak{s}, z^* \left( \mathfrak{s} \right) \right) \\
&= f_3^2 \left( s_i, z \right) - f_3^2 \left( s_i, z^* \left( s_i \right) \right), \quad (23) \\
f_3^3 \left( s_i, z \right) - f_3^3 \left( s_i, z^* \left( s_i \right) \right) &= f_3^3 \left( \mathfrak{s}, z \right) - f_3^3 \left( \mathfrak{s}, z^* \left( \mathfrak{s} \right) \right) \\
&= f_3^3 \left( s_i, z \right) - f_3^3 \left( s_i, z^* \left( s_i \right) \right) .
\end{align*}
\]

It can be seen that the main claim of Lemma 1 can be proved converting \( \mathfrak{s} \) to \( s_i \). We can finish this conversion by the following steps.

**Step 1.** The upper bound \( \mathcal{D}_i \) of point \( i \) substitutes \( D_i (\mathfrak{s}) \).

Before converting, since \((\mathfrak{s}, z^* (\mathfrak{s})) \) is the optimal solution of (19), \( f_3^2 (\mathfrak{s}, z) - f_3^2 (\mathfrak{s}, z^* (\mathfrak{s})) \geq 0 \). Therefore, \( \sum_{k \in K} q_{ik} (z^* (\mathfrak{s})) \geq \sum_{k \in K} q_{ik} (\mathfrak{s} (\mathfrak{s})) \). In the first conversion step, \( f_3^2 (\mathfrak{s}, z^* (\mathfrak{s})) \) cannot increase by more than \((\mathcal{D}_i - D_i (\mathfrak{s})) / (1 / \sum_{k \in K} q_{ik} (z^* (\mathfrak{s}))) \) in \( \mathcal{D}_i \geq D_i (\mathfrak{s}) \) and cannot increase because \((\mathfrak{s}, z^* (\mathfrak{s})) \) is the optimal solution of problem (19). Therefore, the value of \( f_3^2 (\mathfrak{s}, z) - f_3^2 (\mathfrak{s}, z^* (\mathfrak{s})) \) does not change because \( \mathcal{D}_i \geq D_i (\mathfrak{s}) \) and cannot increase because \((\mathfrak{s}, z^* (\mathfrak{s})) \) is the optimal solution of problem (19). Thus, the main claim is proven, as in Lemma 1.

The following theorem is obtained by Lemma 1, which greatly simplifies formulas (19) and (20).

**Theorem 2.** For any \( z \in Z \),

\[
\begin{align*}
rc_2(z) &= \max \left\{ \frac{\mathcal{D}_i}{\sum_{k \in K} q_{ik}} - f_3^2 \left( s_i, z^* \left( s_i \right) \right) \right\}, \\
r_c^3(z) &= \min \left\{ \frac{1}{\sum_{(i, j) \in r(z)} \bar{v}_{ij}} - f_3^3 \left( s_i, z^* \left( s_i \right) \right) \right\}. \\
\end{align*}
\]

**4.3. The Solutions of This Model.** Many practical problems need to optimize multiple objectives simultaneously. Sometimes these goals often compete with each other or contradict each other, so the definition of Pareto optimal solution is introduced.

(1) **Pareto Dominance.** Considering all objectives, if solution \( x_1 \) is at least as equal as \( x_2 \), and better than \( x_2 \) with at least one objective value, solution \( x_1 \) dominates \( x_2 \) (denoted as \( x_1 > x_2 \)). For minimizing \((f_1, \ldots, f_w)\), \( x_1 > x_2 \) if

\[
(\forall w \in \{1, 2, \ldots, W\} : f_w (x_1) \leq f_w (x_2)) \land (\forall w' \in \{1, 2, \ldots, W\} : f_{w'} (x_1) < f_{w'} (x_2)).
\]

(2) **Pareto Optimum.** A solution \( x_1 \) is called Pareto optimal or nondominated solution if and only if there is no any solution \( x_2 \) that satisfies \( x_2 > x_1 \).

(3) **Pareto Front.** Furthermore, if \( x_1 \) is Pareto optimum (nondominated), then \( f(x_1) = \{ f_1 (x_1), \ldots, f_w (x_1) \} \) is said to be the nondominated vector. The set of all nondominated vectors is called Pareto front (or nondominated frontier).

The papers [14–17] are the common methods to solve multiobjective optimization problems. In this paper, genetic algorithm [17] is applied to solve the uncertain problem with half-time windows. The specific processes are as follows.

**1. Initial Population.** According to the characteristics of the LRP problem, each chromosome includes three substrings.

\[
X^t_g = \left\{ \begin{array}{c}
\begin{array}{c}
\left( x_{p1}^t, x_{p2}^t, \ldots, x_{pkl}^t \right) \\
x_{p1}^t,
\end{array} \\
\begin{array}{c}
\left( x_{p1}^t, x_{p2}^t, \ldots, x_{pml}^t \right) \\
x_{p2}^t,
\end{array} \\
\ldots
\end{array} \right\}, \quad g = 1, 2, \ldots, NP.
\]

We can calculate three objective function values through decomposing \( X^t_g \) [11]. Choose the worst scenario according to Sections 4.1 and 4.2. Transport time is calculated based on the distances between the points and the velocities of the vehicle (ignoring the distribution time of distribution centers). If the sum of travel time and service time are greater than \( b_i \), the transport capacities of path are punished, and the transport
capacities are updated to \( b_i \) (transport capacity)/(transport time + service time).

(2) **Mutation Operation.** Variation vectors can be obtained through mutating. In order to avoid being trapped in local optimum, this paper introduces the inversion sequence variation method for each substring of chromosome [18]. It randomly chooses two notes within a chromosome and then reverses their contents. The following two formulas are the examples. Parent is [5 6]2378914], and child is [5 6]9873214] after reversing.

(3) **Crossover Operation.** Crossover operation is applied to obtain the trail vector \( U_g^t \) after mutation operator. According to the literature [19], the two points crossover method is used in \( U_g^t \), and single point crossover method is applied to produce \( u_g^1, u_g^2, u_g^3, \) and \( u_g^4 \) which constitute the trail vector \( U_g^t \).

\[
U_g^t = \left( \begin{array}{c}
(u_{g1}, u_{g12}, ..., u_{g2k}) \times N_g^t, \\
(u_{g21}, u_{g22}, ..., u_{g2k}), \\
(u_{g31}, u_{g32}, ..., u_{g2k}), \\
(u_{g41}, u_{g42}, ..., u_{g2k})
\end{array} \right)
\]

(27)

(4) **Selection Operation.** The weighted method [20] is applied to sort individuals in population. \( \lambda_1 \) is selected randomly on interval \((0.1, 0.3]\), and \( \lambda_3 \) is obtained randomly on interval \((0.3, 0.5]\). Because the satisfaction rate is less than 1, it is easy to lose with the total costs and the total path velocities, so we select \( \lambda^t \) on interval \([500, 1000]\) randomly. Then, we let \( \lambda_3 = \lambda^t \times N \) (N is the number of disaster points).

(5) **Steps of Genetic Algorithm**

(S1) Generate initial population \( X_0 \) of size NP randomly.

(S2) The variation population is obtained by the variation process, and trail population is obtained by the crossover operation.

(S3) Combine the parent population \( X_t \) and trial population \( U_t \) together to form population \( R_t \).

(S4) Compute the objective values for each chromosome in \( R_t \).

(S5) Determine the values of \( \lambda_1, \lambda_2, \) and \( \lambda_3 \), and compute the value of \( F = \lambda_1 (-f_1) + \lambda_2 f_2 + \lambda_3 f_3 \) and sort individuals based on \( F \).

(S6) Select the first NP individuals as the next generation population.

(S7) Stop the procedure if the generation \( t \) is bigger than maxgen (maximum of iteration times); else turn to (S2).

5. **Numerical Experiment**

Parameter setting is NP = 5 \times (m + n); mutation probability is \( p_m = 0.7 \); crossover probability is \( p_c = 0.7 \).
Table 1: Required number of vehicles.

| Vehicle type   | 10 points | 100 points | 1000 points |
|----------------|-----------|------------|-------------|
| Large vehicle $k_1$ | 10        | 100        | 1000        |
| Medium vehicle $k_2$ | 6         | 60         | 600         |
| Small vehicle $k_3$  | 9         | 90         | 900         |

Table 2: Vehicle parameters.

| Vehicle type   | Vehicle capacity $L_k$ (cm$^3$) | General velocity $v_j$ (km/h) | Unit transportation cost $c_k$ (yuan/km) |
|----------------|----------------------------------|--------------------------------|----------------------------------------|
| Large vehicle $k_1$ | $600 \times 250 \times 175$ | 50                             | 10.0                                   |
| Medium vehicle $k_2$ | $280 \times 200 \times 145$ | 30                             | 3.1                                    |
| Small vehicle $k_3$  | $231 \times 150 \times 130$  | 20                             | 1.7                                    |

Table 3: Calculation results.

| Examples | Total costs | Satisfaction rate (%) | Path velocity |
|----------|-------------|------------------------|---------------|
|          | Mean value of approximate Pareto fronts | Approximate Pareto solution | Mean value of approximate Pareto fronts | Approximate Pareto solution |
| 3-10     | 8150.1      | 5811                   | 55.48         | 55.44         | 643.8333         | 1098          |
| 3-100    | 34625       | 25263                  | 64.28         | 62.77         | 8644.1           | 8761          |
| 3-1000   | 158910      | 139560                 | 59.35         | 59.80         | 89865            | 88913         |
| 6-100    | 42807       | 38976                  | 60.57         | 64.49         | 8554             | 8575          |
| 6-1000   | 129560      | 116650                 | 54.89         | 60.01         | 11145            | 12270         |
| 10-100   | 43869       | 48567                  | 58.99         | 59.62         | 8097.4           | 8329          |
| 10-1000  | 137980      | 118960                 | 58.67         | 61.13         | 87660            | 89437         |

available path are uncertain, and the robust optimization is applied to deal with the uncertainty. The genetic algorithm is applied to solve a number of numerical examples; the results show that the algorithm is very stable and effective for this problem. Finally, the method of solving the problem can also apply simulated annealing algorithm or nondominated sorting genetic algorithm.

Notations

(1) Parameters

$m$: The number of candidate distribution centers
$n$: The number of disaster points
$k$: The number of vehicles
$f_j$: The fixed costs of distribution center $j$, $\forall j \in M$
$v_{ij}$: The velocity of arc $(i, j)$
$D_i$: The demands of disaster point $i$, $\forall i \in N$
$Q$: The available quantities of reliefs on the transport network
$q_k$: The unit transportation cost of vehicle, $\forall k \in K$
$L_k$: The load capacities of vehicle $k$, $\forall k \in K$
$t_{ik}$: The time of vehicle $k$ starting service at point $i$, $\forall i \in N, k \in K$
$b_i$: The latest service time at point $i$, $\forall i \in N$.

(2) The Variables

$x_j$: $\{1$, if the distribution center $j$ is set up; 0, otherwise$, \forall j \in M$
$y_{ijk}$: $\{1$, if the point $i$ is in front of point $j$ on the path of the vehicle $k$; 0, otherwise$, \forall k \in K, (i, j) \in E$
$z_{ik}$: $\{1$, if the point $i$ is on the path of the vehicle $k$; 0, otherwise$
$q_{ik}$: The relief supply quantities transported by the vehicle $k$ to point $i$, $\forall i \in N, \forall k \in K$
$V_{F_k}$: $\{1$, if the last demand point serviced by vehicle $k$ is point $i$; 0, otherwise$, \forall i \in N, k \in K$

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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