Article

Lime Rate in Clayey Soils Influences Chemical Fertility and Sugarcane Yield

Murilo de Campos 1, Jorge Martinelli Martello 1, Gabriela Ferraz de Siqueira 1, Ariani Garcia 1, Daniele Scudeletti 1, Patricia Pereira Dias 1, Raffaella Rossetto 2, Juliano Carlos Calonego 1, Heitor Cantarella 3 and Carlos Alexandre Costa Crusciol 1,*

1 Lageado Experimental Farm, Department of Crop Science, College of Agricultural Sciences, São Paulo State University (UNESP), Botucatu 18610-307, SP, Brazil
2 São Paulo State Agency for Agribusiness Technology, Piracicaba 13400-970, SP, Brazil
3 Soils and Environmental Resources Center, Agronomic Institute (IAC), Campinas 13075-630, SP, Brazil
* Correspondence: carlos.crusciol@unesp.br

Abstract: Liming contributes to the alleviation of acidity in highly weathered soils. For sugarcane, the use of green harvest methods and new soil tillage systems requires an adjustment of lime application rates. In the present study, the effects of different lime rates and tillage systems on sugarcane performance and soil chemical fertility parameters were assessed. Three experiments were conducted in two locations between April 2015 and October 2019. The study design was a randomized block field study with four replicates. Four lime rates were applied once at sugarcane establishments in each soil tillage system and location: no liming (control); lime recommended rate (LRR); two times LRR (2 × LRR); and three times LRR (3 × LRR). The three soil tillage systems were conventional (CT), deep-strip (DT), and modified deep-strip tillage (MDT). Soil chemical fertility, leaf nutrient concentrations, and sugarcane yield components were analyzed, and correlations were identified by principal component analysis (PCA). The soil acidity was adequately alleviated in all tillage systems. Increasing the lime rate improved the lime distribution and soil fertility parameters. Applying lime at rates higher than LRR improved stalk and sugar yields, longevity, agronomic efficiency index (AEI), and correlated with a longer residual effect of liming, mainly in the last ratoon.

Keywords: conventional tillage; deep strip-tillage; furrower; localized tillage

1. Introduction

Brazil is recognized as the biggest producer of sugarcane (Saccharum spp.) in the world [1], and Brazilian research has contributed greatly to advances in agronomic management. In the 2021/2022 growing season, sugarcane stalk production of approximately 592 million tons is expected in Brazil [2]. Despite this high production, the average yield in Brazil is approximately 71.2 Mg ha⁻¹ [2], far below the potential of up to 200 Mg ha⁻¹ [3]. This gap highlights the need to evaluate new practices that can increase the efficiency and profitability of the sugar and energy industries. Improving yield efficiency while conserving the soil is an intrinsic concern in modern agriculture, and sugarcane cultivation is no exception. Sugarcane is a semi-perennial crop, and successive cuttings are accompanied by progressively declining stalk and sugar yields, mainly due to reduced soil fertility, soil compaction, and ratoon damage caused by machinery traffic [4].

Sugarcane cultivation is preferentially localized in humid tropical regions where the soil is mainly highly weathered and acidic [5,6]. Consequently, agronomic management to alleviate soil acidity is indispensable for sugarcane cultivation. Agricultural lime is the most commonly used soil acidity amendment, and its effects are well documented in the literature [7–9]. In short, lime has a double purpose as a source of calcium (Ca) and magnesium (Mg) and as a soil acidity amendment. Ca plays a fundamental role in cell...
wall structure and membrane formation [10,11], whereas Mg participates in all energy-dependent physiological processes and photosynthesis [12,13]. Carbonate hydrolysis of lime generates hydroxyl (OH\(^-\)) ions capable of reacting with hydrogen (H\(^+\)) ions, thereby increasing soil pH and effective cation exchange capacity (ECEC) [14].

For sugarcane, lime application is based on guidelines from regional bulletins calibrated to conventional soil tillage and burned-harvest systems [15]. Although conventional soil tillage remains the primary form of sugarcane tillage management, the advent of GPS-controlled machinery traffic has opened new possibilities for soil tillage systems, including localized tillage management [16,17]. In addition, green harvest methods, i.e., harvest without burning, are gaining ground in Brazil. These methods improve soil quality and structure by increasing soil organic matter (SOM), cycling, and storage capacity [18] but also necessitate readjustment of lime rates and forms of application depending on the tillage system adopted.

Under conventional soil tillage, lime incorporation is limited to the mobilized layer (approximately 0.4 m). Since the sugarcane root system can reach deeper layers [19], superficial lime incorporation might be ineffective in highly acidic subsurface soils. To enable deeper lime placement, sugarcane producers are increasingly adopting localized tillage management, such as deep strip-tillage on planting furrows, reserving inter-rows specifically for machinery traffic. However, the few available studies have primarily focused on soil physical evaluations and operational efficiency [16,17,20–24] rather than soil chemical fertility and soil acidity management. Addressing this gap is important, as chemical impediments can reduce the exploration of deeper layers by the plant root system, particularly in acidic soils [25,26].

We hypothesize that higher-than-recommended lime doses will enhance soil chemical fertility under deep strip-tillage due to the increase in vertical soil mobilization, which improves the arrangement and distribution of lime. Moreover, we hypothesize that, regardless of the tillage system, higher-than-recommended lime doses will contribute to acidity amendment long-term (residual effect), as reflected in increased stalk and sugar yields in clayey, acidic, and highly weathered soils. To test these hypotheses, in this study we evaluated the impact of increasing lime rates on soil acidity amendment and soil fertility throughout the soil profile and the yield of stalks and sugar under conventional, deep strip-tillage, and modified deep strip-tillage for the complete sugarcane growing cycle.

2. Results

Although differences were observed among the tillage systems, in general, lime application buffered soil pH efficiently and maintained acidity levels ranging from moderate (5.0–5.5) to slight elevated (>5.5) [27] in plant cane and first ratoon. The rates 2 and 3 \(\times\) LRR buffered the soil pH more efficiently than LRR in second and third ratoons, especially at depths \(\leq 0.6\) m at both locations (Figures S1a–h, S2a–h and S3a–h). The soil concentrations of Ca\(^{2+}\) and Mg\(^{2+}\) (Figures S1i–x, S2i–x and S3i–x) and the residual effect of liming were highest under MDT. The liming process distributed equivalent amounts of Ca and Mg under CT and DT but not MDT. Under CT and DT, the Ca and Mg inputs were 1065 and 510 kg ha\(^{-1}\) for LRR, respectively, at Macatuba, and 850 and 550 kg ha\(^{-1}\) for LRR, respectively, at Piraju. Under MDT, the same rate calculated for the total area was applied as concentrated bands. Given a row spacing of 1.5 \(\times\) 0.9 m (i.e., 2.4 m) and a furrower working width of 1.2 m, a double dose was strip incorporated by the furrower. Accordingly, under MDT, the Ca and Mg inputs were 2130 and 1020 kg ha\(^{-1}\) for LRR, respectively, at Macatuba and 1700 and 1100 kg ha\(^{-1}\), respectively, at Piraju.

Because base saturation (BS) is highly influenced by Ca\(^{2+}\) and Mg\(^{2+}\), the effects of the treatments on BS reflected the inputs of Ca and Mg. Under CT at Macatuba, BS was significantly higher under liming than in the control at depths \(\leq 0.6\) m under LRR and in all layers under 2 \(\times\) and 3 \(\times\) LRR, except in third ratoon, in which significant effects were observed only at depths \(\leq 0.6\) m (Figure S4a–d). In Piraju, BS increased with the lime rate
in the first layer (0.0–0.2 m) and at all depths in plant cane, at depths ≤ 0.6 m in first and second ratoons, and depths ≤ 0.4 m in third ratoon (Figure S4e–h).

Under DT at Macatuba, BS was higher in all limed treatments than in the control at all depths in plant cane, first and second ratoons and at depths ≤ 0.4 m in third ratoon (Figure S5a–d). At Piraju, lime application increased BS at depths ≤ 0.4 m in all growing seasons, regardless of the lime rate. At depths of 0.4 to 0.6 m, all rates of lime application increased BS in plant cane, whereas only 2 × and 3 × LRR increased BS in first ratoon, and only 3 × LRR increased BS in second and third ratoons (Figure S5e–h).

Compared to the control, BS was higher in the limed treatments under MDT at all lime rates, soil depths, and growing seasons, except at depths ≥ 0.8 m in third ratoon. In general, at Macatuba, BS increased with the lime rate, even in the most subsurface layers (Figure S6a–d). At Piraju, liming significantly increased BS at depths ≤ 0.6 m regardless of the lime rate and growing season. In third ratoon, only 2 × and 3 × LRR had significant effects from 0.2 to 0.6 m (Figure S6e–h).

BS above 60% is considered adequate for sugarcane according to the soil fertility recommendation bulletin of São Paulo State [27]. As the LRR was calculated by summing the lime recommendations for the uppermost surface layers (0.0–0.2 + 0.2–0.4 m), BS values reaching 60% at depths of at least 0.4 m were expected. In general, adequate results were observed in plant cane under all tillage systems when LRR was used; however, in subsequent growing seasons, BS was less than 60% under LRR even in the first layer, regardless of the tillage system. When higher lime rates were used, a greater residual effect was observed, mainly in first ratoon under CT and DT and in all ratoons under MDT. BS varied between the sites and was highest in the first layer. AS was significantly reduced by liming under CT regardless of rate at all depths in plant cane and first ratoon. In second and third ratoons, liming under CT increased AS at depths ≤ 0.6 m at Macatuba (Figure S4i–l) and Piraju (Figure S4m–p). Under DT, the effect of liming on AS was evident throughout the entire soil profile in plant cane and first ratoon and at depths ≤ 0.8 m in second ratoon, regardless of the rate. In third ratoon, liming reduced AS at depths ≤ 0.4 m at Macatuba (Figure S5i–l) and ≤ 0.6 m at Piraju (Figure S5m–p). Under MDT, liming significantly reduced AS at all rates and soil depths in plant cane, first and second ratoons and at depths ≤ 0.6 m in third ratoon at Macatuba (Figure S6i–l). At Piraju under MDT, AS was controlled by liming regardless of rate and depths in plant cane and at depths ≤ 0.6 m in all ratoons (Figure S6m–p).

The leaf concentrations of Ca and Mg increased with the lime rate at both locations but not in all growing seasons (Figures S4q,r, S5q,r and S6q,r). In general, there was no clear pattern of significant changes in the leaf concentrations of elements in any of the growing seasons, but on average, none of the values was outside the ranges proposed by ref. [28] for sugarcane (Table S1). Thus, the plants were considered well nourished regardless of treatment and tillage system.

Principal component analysis (PCA) was performed to identify the parameters explaining the variations in stalk and sugar yields. The PCA considered BS, AS, soil concentrations of Ca$^{2+}$ and Mg$^{2+}$, and soil depth as parameters (Figures 1–3). Regardless of the tillage system, eigenvalues ≥1 were present only in factor 1 (horizontal axis). In factor 2 (vertical axis), all eigenvalues were <1, and thus this factor was not considered (Tables S2–S4). The PCA revealed positive influences of Ca$^{2+}$, Mg$^{2+}$, and BS and negative influences of AS on stalk and sugar yields for both tillage systems and locations.

Under CT, correlations of BS and AS with stalk and sugar yields ≥ 10.701 were observed in all soil layers and locations, whereas Ca$^{2+}$ and Mg$^{2+}$ were correlated with stalk and sugar yields at depths ≤ 0.6 and 0.4 m, respectively, in Macatuba and at depths ≤ 0.4 and 0.6 m, respectively, in Piraju (Figure 1a,c; Table S2).
The PCA revealed positive influences of Ca\(^{2+}\), Mg\(^{2+}\), and BS and negative influences of AS on stalk and sugar yields for both tillage systems and locations. Figure 1. Projection of the dataset subjected to principal component analysis based on the correlations of stalk (St) and sugar (Sg) yields with (a,c) soil chemical attributes (Ca, calcium; Mg, magnesium; BS, base saturation; and AS, aluminum saturation) and depths (1, 0.0–0.2 m; 2, 0.2–0.4 m; 3, 0.4–0.6 m; 4, 0.6–0.8 m; and 5, 0.8–1.0 m); and (b,d) lime rate (C, control; R, recommended lime rate; 2, 2× recommended lime rate; 3, 3× recommended lime rate) at Macatuba and Piraju under conventional tillage (CT) for plant cane (PC) and first (1st), second (2nd), and third (3rd) ratoons.

Figure 2. Projection of the dataset subjected to principal component analysis based on the correlations of stalk (St) and sugar (Sg) yields with (a,c) soil chemical attributes (Ca, calcium; Mg, magnesium; BS, base saturation; and AS, aluminum saturation) and depths (1, 0.0–0.2 m; 2, 0.2–0.4 m; 3, 0.4–0.6 m; 4, 0.6–0.8 m; and 5, 0.8–1.0 m); and (b,d) lime rate (C, control; R, recommended lime rate; 2, 2× recommended lime rate; 3, 3× recommended lime rate) at Macatuba and Piraju under deep strip-tillage (DT) for plant cane (PC) and first (1st), second (2nd), and third (3rd) ratoons.
Figure 2. Projection of the dataset subjected to principal component analysis based on the correlations of stalk (St) and sugar (Sg) yields with (a,c) soil chemical attributes (Ca, calcium; Mg, magnesium; BS, base saturation; and AS, aluminum saturation) and depths (1, 0.0–0.2 m; 2, 0.2–0.4 m; 3, 0.4–0.6 m; 4, 0.6–0.8 m; and 5, 0.8–1.0 m); and (b,d) lime rate (C, control; R, recommended lime rate; 2, 2× recommended lime rate; 3, 3× recommended lime rate) at Macatuba and Piraju under deep strip-tillage (DT) for plant cane (PC) and first (1st), second (2nd), and third (3rd) ratoons.

Figure 3. Projection of the dataset subjected to principal component analysis based on the correlations of stalk (St) and sugar (Sg) yields with (a,c) soil chemical attributes (Ca, calcium; Mg, magnesium; BS, base saturation; and AS, aluminum saturation) and depths (1, 0.0–0.2 m; 2, 0.2–0.4 m; 3, 0.4–0.6 m; 4, 0.6–0.8 m; and 5, 0.8–1.0 m); and (b,d) lime rate (C, control; R, recommended lime rate; 2, 2× recommended lime rate; 3, 3× recommended lime rate) at Macatuba and Piraju under modified deep strip-tillage (MDT) for plant cane (PC) and first (1st), second (2nd) and third (3rd) ratoons.

Under DT, stalk and sugar yields were negatively correlated with AS in all soil layers in Macatuba and at depths ≤ 0.8 m in Piraju. For BS, Ca$^{2+}$, and Mg$^{2+}$, significant correlations with stalk and sugar yields were observed at depths ≤ 0.8, 0.6, and 0.4 m, respectively, in Macatuba and depths ≤ 0.4 m in Piraju (Figure 2a,c; Table S3).

Under MDT, BS and AS were significantly correlated with stalk and sugar yields in all soil layers, whereas Ca$^{2+}$ and Mg$^{2+}$ were correlated with stalk and sugar yields at depths ≤ 0.4 and 0.8 m, respectively, in Macatuba. In Piraju, significant effects on stalk and sugar yields were observed at depths ≤ 0.6 m for BS and Ca$^{2+}$, ≤ 0.8 m for AS, and ≤ 0.4 m for Mg$^{2+}$ (Figure 3a,c; Table S4).

Under all tillage systems at both locations, all lime rates in the two first growing seasons, 2× and 3× LRR in second ratoon, and 3× LRR in the last growing season were associated with the yield parameters, except for the last growing season under DT at Piraju (Figures 1b,d, 2b,d, and 3b,d).

The absolute results also demonstrated the dependence of stalk and sugar yields on higher-than-recommended lime rates, regardless of the tillage system. In Macatuba, when all growing seasons were averaged, applying 2× and 3× LRR increased the stalk yield by 13.4 and 18.6 Mg ha$^{-1}$ under CT, 12.0 and 22.4 Mg ha$^{-1}$ under DT, and 7.0 and 8.8 Mg ha$^{-1}$ under MDT. The application of 2× and 3× LRR increased the sugar yield by 2.1 and 2.8 Mg ha$^{-1}$ under CT, 2.0 and 3.4 Mg ha$^{-1}$ under DT, and 1.0 and 1.5 Mg ha$^{-1}$ under MDT. When all growing seasons in Piraju were averaged, 2× and 3× LRR increased the stalk yield by 5.7 and 12.9 Mg ha$^{-1}$ under CT, 6.0 and 14.5 Mg ha$^{-1}$ under DT, and 10.7 and 22.0 Mg ha$^{-1}$ under MDT. Under 2× and 3× LRR, sugar yield increased by 1.4 and 2.7 Mg ha$^{-1}$ under CT, 1.3 and 2.6 Mg ha$^{-1}$ under DT, and 1.9 and 4.2 Mg ha$^{-1}$ under MDT. The sugar yield increased with the lime rate because it is based on stalk yield; however, in
in general, the sucrose concentration and TRS increased significantly when lime was applied regardless of the rate (Figures 4–6).

Figure 4. Sucrose (a), total recoverable sugar (TRS, b), and yields of stalks (c) and sugar (d) under increasing lime rates at Macatuba and Piraju under conventional tillage (CT) in plant cane and first, second and third ratoons. Different lowercase letters indicate significant differences between lime rates for each growing season (LSD, $p \leq 0.1$). The error bars express the standard error of the mean ($n = 4$).

Figure 5. Sucrose (a), total recoverable sugar (TRS, b), and yields of stalks (c) and sugar (d) under increasing lime rates at Macatuba and Piraju under deep strip-tillage (DT) in plant cane and first, second, and third ratoons. Different lowercase letters indicate significant differences between lime rates for each growing season (LSD, $p \leq 0.1$). The error bars express the standard error of the mean ($n = 4$).

Figure 6. Sucrose (a), total recoverable sugar (TRS, b), and yields of stalks (c) and sugar (d) under increasing lime rates at Macatuba and Piraju under modified deep strip-tillage (MDT) in plant cane and first, second, and third ratoons. Different lowercase letters indicate significant differences between lime rates for each growing season (LSD, $p \leq 0.1$). The error bars express the standard error of the mean ($n = 4$).

The agronomic efficiency index (AEI) was calculated to evaluate the efficiency of $2 \times$ and $3 \times$ LRR compared with LRR. In all cases, the AEI values of $2 \times$ and $3 \times$ LRR were above 100%, confirming the greater efficiency of higher-than-recommended lime rates compared with LRR. Under CT and DT, across the complete sugarcane cycle (summing the growing
seasons), the average AEI values indicated that 2× and 3× LRR were 73 to 149% more efficient than LRR in terms of stalk and sugar yields at Macatuba. At Piraju, the average AEI values for 2× and 3× LRR indicated approximately 20 to 50% greater efficiency. Under MDT, the average AEI values showed that the increase in stalk and sugar yield efficiency provided by 2× and 3× LRR was 24 to 35% at Macatuba and 31 to 70% at Piraju (Table 1).

Table 1. Increments of stalk and sugar yields and agronomic efficiency index (AEI) values as a function of lime rate at Macatuba and Piraju.

| Lime Rates | Stalks Yield Increase (Mg ha\(^{-1}\)) \(^1\) | AEI (%) \(^2\) | Sugar Yield Increase (Mg ha\(^{-1}\)) | AEI (%) |
|------------|---------------------------------|----------------|---------------------------------|--------|
|            | CT  | DT  | MDT | CT  | DT  | MDT | CT  | DT  | MDT | CT  | DT  | MDT |
| **2016**   |      |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 10.4| 9.5 | 11.8 | -   | -   | -   | 1.8 | 1.5 | 1.9 | -   | -   | -   |
| 2× LRR     | 20.2| 17.7| 15.7 | 194 | 186 | 133 | 3.8 | 2.8 | 2.7 | 207 | 187 | 143 |
| 3× LRR     | 24.2| 27.6| 16.6 | 232 | 290 | 141 | 4.5 | 4.0 | 3.2 | 245 | 266 | 170 |
| **2017**   |      |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 14.1| 11.9| 23.0 | -   | -   | -   | 2.9 | 2.3 | 3.8 | -   | -   | -   |
| 2× LRR     | 26.6| 24.4| 28.2 | 189 | 204 | 123 | 4.8 | 4.1 | 4.8 | 163 | 177 | 126 |
| 3× LRR     | 27.9| 33.0| 30.6 | 198 | 276 | 133 | 4.6 | 5.6 | 5.3 | 156 | 242 | 138 |
| **2018**   |      |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 14.7| 13.1| 25.6 | -   | -   | -   | 2.7 | 2.5 | 4.5 | -   | -   | -   |
| 2× LRR     | 29.9| 26.8| 33.4 | 204 | 204 | 131 | 4.8 | 5.2 | 5.1 | 178 | 213 | 113 |
| 3× LRR     | 34.9| 36.4| 34.2 | 238 | 277 | 134 | 5.3 | 6.0 | 5.6 | 194 | 246 | 123 |
| **2019**   |      |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 17.5| 25.5| 38.9 | -   | -   | -   | 3.3 | 4.8 | 7.0 | -   | -   | -   |
| 2× LRR     | 33.7| 39.1| 50.0 | 192 | 153 | 128 | 5.9 | 7.0 | 8.7 | 180 | 145 | 124 |
| 3× LRR     | 44.3| 52.6| 53.0 | 253 | 206 | 136 | 7.5 | 9.1 | 9.1 | 229 | 191 | 130 |
| **Complete** |     |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 14.2| 15.0| 24.8 | -   | -   | -   | 2.7 | 2.8 | 4.3 | -   | -   | -   |
| 2× LRR     | 27.6| 27.0| 31.8 | 195 | 180 | 128 | 4.8 | 4.8 | 5.3 | 180 | 173 | 124 |
| 3× LRR     | 32.8| 37.4| 33.6 | 232 | 249 | 135 | 5.5 | 6.2 | 5.8 | 203 | 224 | 135 |
| **2016**   |      |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 26.0| 22.6| 27.3 | -   | -   | -   | 4.4 | 4.5 | 4.7 | -   | -   | -   |
| 2× LRR     | 29.2| 25.4| 41.2 | 112 | 113 | 151 | 5.2 | 4.9 | 7.4 | 119 | 110 | 159 |
| 3× LRR     | 28.5| 27.0| 45.3 | 110 | 120 | 166 | 6.0 | 5.5 | 8.7 | 137 | 124 | 186 |
| **2017**   |      |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 29.5| 26.3| 27.7 | -   | -   | -   | 5.7 | 4.9 | 5.6 | -   | -   | -   |
| 2× LRR     | 40.0| 33.8| 36.5 | 136 | 128 | 132 | 8.1 | 7.0 | 7.3 | 143 | 144 | 129 |
| 3× LRR     | 41.1| 40.9| 47.5 | 139 | 156 | 172 | 8.3 | 7.9 | 9.6 | 147 | 162 | 170 |
| **2018**   |      |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 35.7| 37.9| 44.5 | -   | -   | -   | 6.5 | 6.7 | 8.3 | -   | -   | -   |
| 2× LRR     | 39.4| 44.1| 55.1 | 111 | 116 | 124 | 7.8 | 8.5 | 10.2 | 120 | 128 | 123 |
| 3× LRR     | 52.0| 54.7| 67.0 | 146 | 144 | 150 | 9.9 | 10.0 | 12.6 | 152 | 150 | 152 |
| **2019**   |      |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 20.9| 33.0| 37.4 | -   | -   | -   | 3.4 | 5.6 | 5.7 | -   | -   | -   |
| 2× LRR     | 26.3| 40.3| 46.5 | 126 | 122 | 125 | 4.3 | 6.2 | 7.0 | 125 | 111 | 124 |
| 3× LRR     | 41.9| 54.7| 65.2 | 201 | 166 | 175 | 6.6 | 8.7 | 10.4 | 192 | 154 | 184 |
| **Complete** |     |      |      |      |      |      |      |      |      |      |      |      |
| LRR        | 28.0| 29.9| 34.2 | -   | -   | -   | 5.0 | 5.4 | 6.1 | -   | -   | -   |
| 2× LRR     | 33.7| 35.9| 44.9 | 120 | 120 | 131 | 6.4 | 6.7 | 8.0 | 127 | 123 | 132 |
| 3× LRR     | 40.9| 44.4| 56.2 | 146 | 148 | 164 | 7.7 | 8.0 | 10.3 | 154 | 148 | 170 |

1 Increments in stalks and sugar yield relative to the control; 2 Agronomic efficiency index of two and three times the lime recommended rate (LRR) relative to the lime recommended rate (LRR) for stalk and sugar yields; 3 Complete sugarcane cycle (summed growing seasons).
Figure 5. Sucrose (a), total recoverable sugar (TRS, b), and yields of stalks (c) and sugar (d) under increasing lime rates at Macatuba and Piraju under deep strip-tillage (DT) in plant cane and first, second, and third ratoons. Different lowercase letters indicate significant differences between lime rates for each growing season (LSD, \( p \leq 0.1 \)). The error bars express the standard error of the mean (\( n = 4 \)).

Figure 6. Sucrose (a), total recoverable sugar (TRS, b), and yields of stalks (c) and sugar (d) under increasing lime rates at Macatuba and Piraju under modified deep strip-tillage (MDT) in plant cane and first, second, and third ratoons. Different lowercase letters indicate significant differences between lime rates for each growing season (LSD, \( p \leq 0.1 \)). The error bars express the standard error of the mean (\( n = 4 \)).

3. Discussion

In general, although the magnitudes of the effects varied, increasing the lime rate increased soil \( \text{Ca}^{2+} \) and \( \text{Mg}^{2+} \) concentrations and BS and decreased AS. These effects were observed at both sites but varied in intensity according to the lime rate and tillage system. The highest rates of liming reached deeper soil layers efficiently in plant cane and intermediate soil layers in subsequent ratoons. These findings are important since the distribution of plant roots tends to be concentrated in soil layers with higher fertility levels and high water availability [7,28].

Applying higher-than-recommended lime rates provided large inputs of Ca and Mg, but the concentrations of exchangeable Ca and Mg did not increase proportionally with the lime rate because lime reactivity is pH dependent [29]. As liming increases the soil pH, the reactivity of the lime decreases, contributing to downward or lateral displacement of the unreacted lime particles. When acidity is restored (below approximately 4.6 to 5.0 (\( \text{CaCl}_2 \))), the reactivity of the insoluble lime particles recovers [29,30], creating residual effects of liming. For perennial or semi-perennial crops, a greater residual effect of liming is desirable to counteract the progressive decline in soil fertility [4] and to avoid necrosis of root tips caused by Ca deficiency, which will compromise the efficient uptake of water and nutrients [31].

AS and BS are inversely proportional and thus equally important. Al species are highly pH dependent, and applying lime increases soil pH and decreases AS by complexing Al\( ^{3+} \) into Al-hydroxide species via hydrolysis [32]. The efficiency of lime placement varied even in the deepest layers, and vertical movement of lime was also observed. In general, soil pH increased throughout the soil profile under all tillage systems, indicating that neutralization occurred beyond the lime application point. Mobilization of fine lime particles, whether in association with organic compounds or not, can occur by chemical and physical mechanisms, such as the formation of an alkalinization front and displacement by water movement through the openings left by the roots in the soil [26,33].

Lime application positively or negatively impacts the availability of most elements [34]. Liming increased the soil and leaf concentrations of Ca and Mg not only as a direct source...
of these nutrients but also by increasing the effective cation exchange capacity (ECEC), which promotes the deprotonation of mineral and organic particles and, consequently, electrostatic adsorption of cations [33]. This phenomenon was clearly evidenced by the higher BS when lime was applied, especially at the highest rate.

Conversely, cationic micronutrients may be specifically adsorbed by soil organic matter (SOM) or CEC when the pH increases, and the formation of low-solubility species can decrease their availability [35]. In this study, the soil was mobilized and thoroughly mixed with the lime at tillage, and micronutrient fertilization was adequate at sugarcane establishment; consequently, higher-than-recommended lime rates did not have any important negative effects on cationic micronutrients, which remained within the recommended ranges for sugarcane [27].

Compared with the other analyzed parameters, the effects of lime application on sugarcane quality parameters were smaller. Lime application generally increased the sucrose concentration and TRS, regardless of the rate. The improvements in soil chemical conditions and Mg\(^{2+}\) availability provided by liming are primarily responsible for these increases in sugarcane quality parameters, as there is a direct relationship between the biosynthesis and transport of sucrose and Mg availability [36]. In addition, the climate conditions during the study were beneficial, with well-distributed periods of rainfall, and the hydric balance was positive at the full vegetative growth stage at both locations, which may have favored all treatments and decreased their response to liming.

The attributes that best explained the variations in stalk and sugar yields were identified by PCA. BS (positively) and AS (negatively) were highly correlated with stalk and sugar yields at all soil depths, highlighting the importance of adequate soil fertility in deeper layers. The PCA also revealed that the increases in stalk and sugar yields under higher-than-recommended lime rates were greatest after the first ratoon, implying a longer lasting residual effect of the highest lime rates.

The response to increasing lime rate appeared to be greater under CT and DT, as the AEI values of the highest lime rates were higher under CT and DT than under MDT, especially in Macatuba. Under CT and DT, lime was broadcast over the entire area and better distributed throughout the soil profile under the highest rates. The greater contact with soil in these systems enhanced the dissolution capacity of the lime particles [37,38]. By contrast, under MDT, LRR was sufficient because the lime was applied in concentrated bands targeted directly at the planting furrows; consequently, the effects of higher lime rates on yields were less pronounced. In Piraju, the greater clay content seemed to buffer the soil pH more efficiently, and the highest AEI was reached under MDT with the highest lime rates.

The cumulative stalk and sugar yields after four growing seasons confirmed the improvement in sugarcane performance under the highest lime rates. This improvement was primarily attributable to efficient soil acidity alleviation, mainly at depths ≤ 0.6 m, and long-term residual effects in these soils with high buffering capacity.

4. Materials and Methods

4.1. Location, Soil, and Climatic Characterization of Experimental Areas

Three experiments in two sugarcane commercial sites were simultaneously carried out in Macatuba (Zilor group: 22°29’ S and 48°47’ W, 515 m of elevation) and in Piraju (Raízen group: 23°07’ S 49°24’ W, 645 m of elevation), State of São Paulo, Brazil (Figure S7). The field trials were conducted for four harvests, from the plant cane cycle plus three regrowth (from April 2015 to August 2019). According to the Köppen classification, the predominant climate for both locations is tropical humid with a hot summer (Cwa). The average rainfall, temperature, and hydro-climatic balance [39,40] are presented in Figure S8. Both soils were classified as Rhodic Hapludox [41], and their chemical [42] and texture characterization [43] are presented in Table S5.
4.2. Treatments and Experimental Design

Four lime rates (control, no liming; lime recommended rate (LRR) calculated by the base saturation (60%) method (sum of the soil layers from 0.0 to 0.2 and 0.2 to 0.4 m) [15]; two times LRR (2 × LRR); and three times LRR (3 × LRR)) were all applied at the sugarcane establishment using randomized block design with four replicates. Considering the most used soil tillage systems in sugarcane, conventional and deep-strip tillage were used. For the deep-strip tillage, two main patterns of lime broadcasting were chosen. Due to the complex dataset, each tillage system described below was individually analyzed only as a function of increasing lime rates.

A brief scheme of the soil tillage systems is given in Figure 7 and they were characterized by the operations: Conventional soil tillage system (CT)—this is the standard system with lime broadcast and incorporated (heavy offset disc harrow, subsoiler, and leveling disc harrow on 0.3–0.4 m) over the entire area (Figure 7a); deep strip-tillage system (DT)—the lime was broadcast over the entire area and incorporated into strips with a furrower (a rotary hoe with a working depth of 0.3 to 0.4 m and a subsoiling rod with a working depth and width of 0.7 m and 1.2 m, respectively) only at the planting rows (Figure 7b); modified deep strip-tillage system (MDT)—3/4 of the lime quantity was broadcast over the soil surface in localized bands, and 1/4 was distributed into the soil profile at 0.4 and 0.6 m through the subsoiling rod (lime storage compartment linked to the subsoiling rod) (Figure 7c). The term “modified” indicates the lime was broadcast concentrated in localized bands and further strip incorporated by the furrower.

![Figure 7. Illustration of the soil tillage systems; (a) conventional tillage system, (b) deep-strip tillage system, and (c) modified deep-strip tillage system, equipment, and the disposition of sugarcane plants.](image)

The LRR for Macatuba (CaO and MgO concentration of 30 and 17%, respectively; relative efficiency, 95%) and Piraju (CaO and MgO concentration of 28 and 23%, respectively; relative efficiency, 82%) were evaluated considering a proportional relative efficiency of 100% and the respective lime doses for both sites and tillage systems are in Table 2.
Table 2. Lime doses and forms of application under different soil tillage systems.

| Soil Tillage System | Lime Application | CT ¹ | DT ² | MDT ³ |
|---------------------|------------------|------|------|-------|
|                     | Broadcasted (over the Entire Area) | Broadcasted (over the Entire Area) | Broadcasted on Planting Furrow | Incorporated |
| Lime doses Mg ha⁻¹ | Macatuba (Rhodic Hapludox) |  |
| Control ⁴          | 0.0              | 0.0  | 0.0  | 0.0   |
| LRR ⁵              | 5.0              | 5.0  | 3.8  | 1.2   |
| 2 × LRR ⁶          | 10.0             | 10.0 | 7.5  | 2.5   |
| 3 × LRR ⁷          | 15.0             | 15.0 | 11.3 | 3.7   |
| Control ⁴          | 0.0              | 0.0  | 0.0  | 0.0   |
| LRR ⁵              | 4.0              | 4.0  | 3.0  | 1.0   |
| 2 × LRR ⁶          | 8.0              | 8.0  | 6.0  | 2.0   |
| 3 × LRR ⁷          | 12.0             | 12.0 | 9.0  | 3.0   |

¹ Conventional soil tillage system; ² Deep strip-tillage system; ³ Modified deep strip-tillage system; ⁴ No limestone application; ⁵ Limestone recommended rate [27]; ⁶ Two times limestone recommended rate; ⁷ Three times limestone recommended rate.

The sugarcane varieties CTC 20 in Macatuba and CTC 11 in Piraju were mechanically planted (18 viable buds m⁻¹ at about 0.3–0.4 m depth) immediately after liming using spacing of 1.50 × 0.90 m (double-combined row) and traffic system control. The experimental plots (20 m in length × 12 m in width) were constituted by 5 double rows per plot. The base fertilization consisted of applying 500 kg ha⁻¹ of an NPK formula 06-28-24 in Macatuba and 600 kg ha⁻¹ of an NPK formula 10-25-25 in Piraju. Additionally, 40 kg ha⁻¹ of S were applied as elemental sulfur pastilles also at sugarcane establishment. The micronutrients zinc (Zn, 10%), boron (B, 1.8%), molybdenum (Mo, 0.12%), copper (Cu, 0.6%), and manganese (Mn, 1.2%) were applied separately in fillets 60 days after planting at a dose of 200 kg ha⁻¹. The regrowths (ratoons) were managed by topdressing applications of 650 kg ha⁻¹ of an NPK formula 18-07-28 in Macatuba and 600 kg ha⁻¹ of an NPK formula 20-05-28 in Piraju. Both sites also received 40 kg ha⁻¹ of S as elemental sulfur pastilles. The ratoons did not receive the lime application and other agricultural management practices were performed according to the sugar mill protocols.

4.3. Soil Chemical Analysis

The soil was sampled using a two-inch tubular sampler immediately after the sugarcane harvests, at depths from 0.0 to 1.00 m, stratified on each 0.2 m only considering the sugarcane planting furrows. The soil samples were air-dried and passed through a 10 mesh (2-mm) sieve. The pH (0.01 M CaCl₂; 1:2.5, soil:solution) was determined using a previously calibrated FiveEasy Mettler Toledo potentiometer. The exchangeable calcium (Ca²⁺), magnesium (Mg²⁺), and potassium (K⁺) were extracted by ionic exchange resin and determined by atomic absorption spectroscopy (Shimadzu 9300) and by flame photometry (PFP7 model, Jenway, Staffordshire, UK), respectively. The exchangeable aluminum (Al³⁺) (extracted by 1 mol L⁻¹ KCl solution) and potential acidity (H + Al) (extracted with 1 mol L⁻¹ calcium acetate solution) were both determined by titration with ammonium hydroxide (0.025 mol L⁻¹ [42]). The soil fertility parameters were calculated as follows: (1) base saturation (BS,%) = (SB/CECp) × 100, in which SB is the sum of cations that do not hydrolyze under normal soil pH conditions (Ca²⁺ + Mg²⁺ + K⁺) and the CECp is the potential cation exchange capacity (CECp = (SB + (Al+H))); (2) aluminum saturation (AS,%) = (Al³⁺/CECp) × 100. in which the CECp is the effective cation exchange capacity (CECp = CEC + BS + Al³⁺).

4.4. Foliar Diagnosis

Ten leaves (top visible dewlap) were sampled in the two central rows at full vegetative growth collecting the middle third length. The plant material was dried (60 °C until
constant mass), milled, and the concentrations of N, P, K, Ca, Mg, S, Cu, Fe, Mn, Zn, and B were determined [44].

4.5. Sugarcane Stalk and Sugar Yields and Agronomic Efficiency Index (AEI)

The stalks (topped at apical bud height and defoliated) were weighed in four sequential meters at two central rows and the values were extrapolated to hectares calculating stalk yield (Mg ha\(^{-1}\)). After that, the cleaned stalks were processed to determine the apparent percentage of sucrose by polarization and total recoverable sugar (TRS, kg of sugar per Mg of stalk) [45,46]. The sugar yield was estimated by: (3) Sugar yield (Mg ha\(^{-1}\)) = (TRS × Stalk yield / 1000. After collecting the samples for stalks and sugar yield, the sugarcane was mechanically harvested (non-burning) in both sites (Macatuba: plant cane, first, second, and third ratoons in October 2016, October 2017, October 2018, and September 2019, respectively; and Piraju: plant cane, first, second, and third ratoons in December 2016, December 2017, December 2018, and November 2019, respectively).

The agronomic efficiency index (AEI) by the use of higher-than-recommended rates of lime was calculated by the ratio of stalk and sugar yields applied at the same lime rate for each growing season, as follows: (4) AEI (%) = \(\frac{(Y_2 - Y_1)}{(Y_3 - Y_1)} \times 100\), where \(Y_1\) = sugarcane stalks or sugar yield in the treatment control; \(Y_2\) = sugarcane stalks or sugar yield using 2 or 3 × LRR; and \(Y_3\) = sugarcane stalks or sugar yield using LRR. The AEI determined the increments of stalk and sugar yields compared with the control (increased yields) and considered the ratio of the increment under 2 or 3 × LRR to the increment under LRR, expressed as a percentage. Accordingly, values above 100% indicate that the higher lime rate was more efficient than LRR, while values below 100% indicate that LRR was more efficient than the higher lime rate. Values near or equal to 100% indicate no difference in efficiency between the lime rates.

4.6. Statistical Analysis

Data were submitted for analysis of variance (ANOVA) with subsequent comparison of means. Fisher’s test, supported to the least significant difference (LSD), was performed comparing soil chemical and fertility attributes for each soil depth, foliar diagnosis, and yield components in the same growing season. The 0.1 level of probability was used at all tests.

To identify that the major soil attributes and the sampled depths correlated with sugarcane stalks and sugar yield, the principal component analysis (PCA) technique was constructed separately for each tillage system and location using Pearson’s correlation coefficients \((p \leq 0.1)\) and determined through the Kaiser rule, considering eigenvalues >1 or explaining over 85% of the total variance [47]. Correlations > 10.701 were considered based on the number of paired values [48]. The average values of all growing seasons were used for both active (stalk and sugar yield) and supplemental (soil attributes at the corresponding depths) factors in PCA. All tests were performed by using the statistical software package from Statistica [49].

5. Conclusions

The present study assessed the effects of increasing lime rates on chemical fertility parameters throughout the soil profile and sugarcane performance during the complete sugarcane growing cycle under different tillage systems. In general, regardless of the tillage system, soil acidity was adequately alleviated, and increasing the lime rate improved the distribution of lime in the soil profile and soil fertility. The highest lime rates provided more pronounced residual effects.

Because micronutrient fertilization was adequate, higher-than-recommended lime rates did not negatively impact the nutritional status of the plant. Stalk and sugar yields and the AEI were positively impacted by higher-than-recommended rates, but sucrose concentration and TRS were less responsive to the lime rate, regardless of the tillage system.

Positive correlations of the yield parameters with soil Ca\(^{2+}\) and Mg\(^{2+}\) concentrations and BS were observed in PCA, mainly at depths ≤ 0.6 m under DT and at all soil depths
under CT and MDT. Conversely, AS was negatively correlated with stalk and sugar yields at all depths, regardless of the tillage system. In addition, higher sugarcane yield and longevity were associated with a higher residual effect of liming, mainly in the last ratoon.

The stalk and sugar yields were highest at the higher-than-recommended lime rates, regardless of the tillage system and location. When all growing seasons were averaged, the AEI was highest under CT and DT in Macatuba and under MDT in Piraju.

This study provides solid information for chemical assessments of clayey soils, but similar studies in medium-textured and sandy soils are also necessary due to the widespread cultivation of such soils with sugarcane in Brazil.

Supplementary Materials: The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/plants11162110/s1. Figure S1: Soil pH. Figure S2: Soil pH. Figure S3: Soil pH. Figure S4: Base saturation in Macatuba (BS; a–d) and Piraju (e–h), aluminum saturation in Macatuba (AS; i–l) and Piraju (m–p), and Mg\(^{2+}\) in Macatuba (q–t) and in Piraju (u–x) across the soil profile under increasing lime rates on conventional soil tillage system (CT) for plant cane, first, second, and third ratoon. Different lowercase letters indicate significant differences between lime rates for the same depth and growing season (LSD, \(p \leq 0.1\)). Error bars express the standard error of the mean (\(n = 4\)). Figure S5: Base saturation in Macatuba (BS; a–d) and Piraju (e–h), aluminum saturation in Macatuba (AS; i–l) and Piraju (m–p) across the soil profile under increasing lime rates and leaf concentration of calcium (Ca; q) and magnesium (Mg, r) in Macatuba and Piraju on conventional soil tillage system (CT) for plant cane, first, second, and third ratoon. Different lowercase letters indicate significant differences between lime rates for the same depth and growing season (LSD, \(p \leq 0.1\)). Error bars express the standard error of the mean (\(n = 4\)). Figure S6: Base saturation in Macatuba (BS; a–d) and Piraju (e–h); Aluminum saturation in Macatuba (AS; i–l) and Piraju (m–p) across the soil profile under increasing lime rates and leaf concentration of calcium (Ca; q) and magnesium (Mg, r) in Macatuba and Piraju on deep-strip tillage system (DT) for plant cane, first, second, and third ratoon. Different lowercase letters indicate significant differences between lime rates for the same depth and growing season (LSD, \(p \leq 0.1\)). Error bars express the standard error of the mean (\(n = 4\)). Figure S7: Geographic location of the experimental sites; Figure S8: The average of monthly rainfall, temperature, and hydro-climatic balance (mm) in the 2015/2019 growing season for (a) Macatuba and (b) Piraju; Table S1. Average leaf concentration of each element in both tillage systems, growing seasons, and locations. Table S2. Principal component analysis for soil fertility parameters and the concentration of calcium (Ca\(^{2+}\)) and magnesium (Mg\(^{2+}\)) for conventional soil tillage system (CT). Table S3. Principal component analysis for soil fertility parameters and the concentration of calcium (Ca\(^{2+}\)) and magnesium (Mg\(^{2+}\)) for conventional soil tillage system (CT). Table S4. Principal component analysis for soil fertility parameters and the concentration of calcium (Ca\(^{2+}\)) and magnesium (Mg\(^{2+}\)) for deep-strip tillage system (DT). Table S5. Principal component analysis for soil fertility parameters and the concentration of calcium (Ca\(^{2+}\)) and magnesium (Mg\(^{2+}\)) for modified deep-strip tillage system (MDT). Table S5. Soil chemical attributes and texture characterization prior to the experiment.

Author Contributions: Conceptualization, R.R., J.C.C., H.C. and C.A.C.C.; methodology, R.R., J.C.C., H.C. and C.A.C.C.; validation, R.R., J.C.C., H.C. and C.A.C.C.; formal analysis, M.d.C., J.M.M., G.F.d.S., A.G., D.S. and P.P.D.; investigation, M.d.C., J.M.M., G.F.d.S., A.G., D.S. and P.P.D.; resources,
R.R., J.C.C., H.C. and C.A.C.C.; data curation, M.d.C., R.R., J.C.C., H.C. and C.A.C.C.; writing—original draft preparation, M.d.C.; writing—review and editing, M.d.C., G.F.d.S. and C.A.C.C.; visualization, M.d.C., G.F.d.S. and C.A.C.C.; supervision, R.R., J.C.C., H.C. and C.A.C.C.; project administration, G.F.d.S., J.C.C. and C.A.C.C.; funding acquisition, R.R., J.C.C., H.C. and C.A.C.C. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research was funded by São Paulo Research Foundation (FAPESP/BIOEN)—grant number 2014/20593-9 and in part by the Coordenação de Aperfeiçoamento de Pessoal de Nível Superior—Brasil (CAPES)—Finance Code 001” for funding the first author’s scholarship.

**Data Availability Statement:** Not applicable.

**Acknowledgments:** To the National Council for Scientific and Technological Development (CNPq) for an award for excellence in research of the authors Juliano Carlos Calonego, Heitor Cantarella, and Carlos Alexandre Costa Crusciol. To the agricultural Raizen and Zilor Sugar mill groups for the concession of experimental areas and analytical support.

**Conflicts of Interest:** The authors declare no conflict of interest.

**References**

1. FAOStat Area, Production and Productivity of Sugarcane, Food and Agriculture Organization of the United Nations, Statistics Division. Available online: [http://www.fao.org/faostat/en/#data/QC](http://www.fao.org/faostat/en/#data/QC) (accessed on 11 August 2022).

2. Conab. *Companhia Nacional Do Abastecimento. Acompanhamento Da Safra Brasileira de Cana de Açúcar. Safra;* Conab: Brasília, Brazil, 2021.

3. Monteiro, L.A.; Sentelhas, P.C. Potential and Actual Sugarcane Yields in Southern Brazil as a Function of Climate Conditions and Crop Management. *Sugar Tech.* 2014, 16, 264–276. [CrossRef]

4. Crusciol, C.A.C.; Rossato, O.B.; Foltran, R.; Martello, J.M.; Nascimento, C.A.C.D. Soil Fertility, Sugarcane Yield Affected by Limestone, Silicate, and Gypsum Application. *Commun. Soil Sci. Plant Anal.* 2017, 48, 2314–2323. [CrossRef]

5. Bernardo, R.; Lourenzani, W.L.; Satolo, E.G.; Caldas, M.M. Analysis of the Agricultural Productivity of the Sugarcane Crop in Regions of New Agricultural Expansions of Sugarcane. *Gest. Prod.* 2019, 26, e3554. [CrossRef]

6. Schaefer, C.E.G.R.; Fabris, J.D.; Ker, J.C. Minerals in the Clay Fraction of Brazilian Latosols (Oxisols): A Review. *Clay Miner.* 2021, 46, 137–154. [CrossRef]

7. Caires, E.F.; Haliski, A.; Bini, A.R.; Scharr, D.A. Surface Liming and Nitrogen Fertilization for Crop Grain Production under No-till Management in Brazil. *Eur. J. Agron.* 2015, 66, 41–53. [CrossRef]

8. Miotto, A.; Tietcher, T.; Kaminski, J.; Brunetto, G.; De Conti, L.; Tietcher, T.L.; Martins, A.P.; Rheinheimer dos Santos, D. Soil Acidity and Aluminum Speciation Affected by Liming in the Conversion of a Natural Pasture from the Brazilian Campos Biome into No-Tillage System for Grain Production. *Arch. Agron. Soil Sci.* 2020, 66, 138–151. [CrossRef]

9. Cunha, G.O.M.; Almeida, J.A.; Ermanni, P.R.; Pereira, E.R.; Brunetto, G. Composition, Chemical Speciation and Activity of Ions in the Solution of Brazilian Acid Soils. *Rev. Bras. Ciências Agrárias—Brazilian J. Agric. Sci.* 2018, 13, e5542. [CrossRef]

10. Hepler, P.K. Calcium: A Central Regulator of Plant Growth and Development. *Plant Cell* 2005, 17, 2142–2155. [CrossRef]

11. Merinó-Gergichevich, C.; Alberdi, M.; Ivanov, A.G.; Reyes-Díaz, M. Al3+-Ca2+ Interaction in Plants Growing in Acid Soils: Al-Phytotoxicity Response to Calcareous Amendments. *J. Soil Sci. Plant Nutr.* 2010, 10, 217–243.

12. Koch, M.; Busse, M.; Naumann, M.; Jákli, B.; Smit, I.; Cakmak, I.; Hermans, C.; Pawelzik, E. Differential Effects of Varied Potassium and Magnesium Nutrition on Production and Partitioning of Photoassimilates in Potato Plants. *Physiol. Plant.* 2019, 166, 921–935. [CrossRef]

13. Cakmak, I.; Kirby, E.A. Role of Magnesium in Carbon Partitioning and Alleviating Photooxidative Damage. *Physiol. Plant.* 2008, 133, pp. 692–704. [CrossRef]

14. Fageria, N.K.; Baligar, V.C. Chapter 7 Ameliorating Soil Acidity of Tropical Oxisols by Liming For Sustainable Crop Production. *Adv. Agron.* 2008, 99, 345–399.

15. Cantarella, H.; van Raij, B.; Quaggio, J.A. Soil and Plant Analyses for Lime and Fertilizer Recommendations in Brazil. *Commun. Soil Sci. Plant Anal.* 1998, 29, 1691–1706. [CrossRef]

16. Scarpare, F.V.; de Jong van Lier, Q.; de Camargo, L.; Pires, R.C.M.; Ruiz-Correa, S.T.; Bezerra, A.H.F.; Gava, G.J.C.; Dias, C.T.S. Tillage Effects on Soil Physical Condition and Root Growth Associated with Sugarcane Water Availability. *Soil Tillage Res.* 2019, 187, 110–118. [CrossRef]

17. Barbosa, L.C.; Magalhães, P.S.G.; Bordonal, R.O.; Cherubin, M.R.; Castioni, G.A.; Rossi Neto, J.; Franco, H.C.J.; Carvalho, J.L.N. Untrafficked Furrowed Seedbed Sustains Soil Physical Quality in Sugarcane Mechanized Fields. *Eur. J. Soil Sci.* 2021, 72, 2150–2164. [CrossRef]

18. Tenelli, S.; Bordonal, R.O.; Cherubin, M.R.; Cerri, C.E.P.; Carvalho, J.L.N. Multilocation Changes in Soil Carbon Stocks from Sugarcane Straw Removal for Bioenergy Production in Brazil. *GCB Bioenergy* 2021, 13, 1099–1111. [CrossRef]

19. Battie Laclau, P.; Laclau, J.P. Growth of the Whole Root System for a Plant Crop of Sugarcane under Rainfed and Irrigated Environments in Brazil. *F. Crop. Res.* 2009, 114, 351–360. [CrossRef]
20. Marasca, I.; Lemos, S.V.; Silva, R.B.; Guerra, S.P.S.; Lanças, K.P. Soil Compaction Curve of an Oxisol Under Sugarcane Planted After In-Row Deep Tillage. *Rev. Bras. Cienc. Solu* 2015, 39, 1490–1497. [CrossRef]

21. Barbosa, S.M.; Silva, B.M.; de Oliveira, G.C.; Benevenute, P.A.N.; da Silva, R.E; Curi, N.; da Silva Moretti, B.; Silva, S.H.G.; Norton, L.D.; Pereira, V.M. Deep Furrow and Additional Liming for Coffee Cultivation under First Year in a Naturally Dense Inceptisol. *Geoderma* 2020, 357, 113934. [CrossRef]

22. Li, X.; Wei, B.; Xu, X.; Zhou, J. Effect of Deep Vertical Rotary Tillage on Soil Properties and Sugarcane Biomass in Rainfed Dry-Land Regions of Southern China. *Sustainability* 2020, 12, 10199. [CrossRef]

23. Everett, M.A.; de Risely, E.A.; da Luis, A.S.D.; da Antonio, C.S.J.; de Emmerson, R.M.; Leonardo, R.B.; de Jessika, L.O.S.; Regina, M.Q.L. Soil Porosity and Density in Sugarcane Cultivation under Different Tillage Systems. *Afr. J. Agric. Res.* 2016, 11, 2689–2696. [CrossRef]

24. Martins, M.B.; de Almeida Prado Bortolheiro, F.P.; Testa, J.V.P.; Sartori, M.M.P.; Crusciol, C.A.C.; Lanças, K.P. Fuel Consumption Between Two Soil Tillage Systems for Planting Sugarcane. *Sugar Tech* 2021, 23, 219–224. [CrossRef]

25. Parecido, R.J.; Soratto, R.P.; Perdoná, M.J.; Gitari, H.I.; Dognani, V.; Santos, A.R.; Silveira, L. Liming Method and Rate Effects on Soil Acidity and Arabica Coffee Nutrition, Growth, and Yield. *J. Soil Sci. Plant Nutr.* 2021, 21, 2631–2625. [CrossRef]

26. de Vargas, J.P.R.; dos Santos, D.R.; Bastos, M.C.; Schaefer, G.; Parisi, P.B. Application Forms and Types of Soil Acidity Corrective: Changes in Depth Chemical Attributes in Long Term Period Experiment. *Soil Tillage Res.* 2019, 185, 47–60. [CrossRef]

27. van Raij, B.; Cantarella, H.; Quaggio, J.A.; Furlani, A.M.C. Interpretação de Resultados de Análise de Solo. In *Recomendações de adubação e calagem para o Estado de São Paulo*; van Raij, B., Cantarella, H., Quaggio, J.A., Furlani, A.M.C., Eds.; Editora IAC: Campinas, Brazil, 1997; pp. 7–12.

28. Spirinonello, A.; van Raij, B.; Penatti, C.P.; Cantarella, H.; Morelli, J.L.; Orlando Filho, J.; de Landell, M.G.A.; Rossetto, R. Cana de Açúcar. In *Recomendações de Adubação e Calagem para o Estado de São Paulo*; van Raij, B., Cantarella, H., Quaggio, J.A., Furlani, A.M.C., Eds.; Editora IAC: Campinas, Brazil, 1996; pp. 59–61.

29. Calegari, A.; Tiecher, T.; Hargrove, W.L.; Radisky, R.; Tessier, D.; de Tourdonnet, S.; Guimarães, M.F.D.; dos Santos, D.R. Long-Term Effect of Different Soil Management Systems and Winter Crops on Soil Acidity and Vertical Distribution of Nutrients in a Brazilian Oxisol. *Soil Tillage Res.* 2013, 133, 32–39. [CrossRef]

30. Rheinheimer, D.S.; Santos, E.J.S.; Kaminiski, J.; Bortoluzzi, E.C.; Gattiboni, L.C. Alterações de Atributos Do Solo Pela Calagem Superficial e Incorporada a Partir de Pastagem Natural. *Rev. Bras. Ciência Solo* 2000, 24, 797–805. [CrossRef]

31. Rheinheimer, D.S.; Tiecher, T.; Gonzatto, R.; Zafar, M.; Brunetto, G. Residual Effect of Surface-Applied Lime on Soil Acidity Properties in a Long-Term Experiment under No-till in a Southern Brazilian Sandy Ultisol. *Geoderma* 2018, 313, 7–16. [CrossRef]

32. Taiz, L.; Zeiger, E. *Plant Physiology*, 6th ed.; Sinauer Associates Inc.: Sunderland, MA, USA, 2017.

33. Li, W.; Johnson, C.E. Relationships among PH, Aluminum Solubility and Aluminum Complexation with Organic Matter in Acid Forest Soils of the Northeastern United States. *Geoderma Reg.* 2016, 271, 234–242. [CrossRef]

34. Bossolani, J.W.; dos Santos, F.L.; Meneghette, H.H.A.; Sanches, I.R.; Moretti, L.G.; Parra, L.F.; Lazarini, E. Soybean in Crop Rotation with Maize and Palisade Grass Intercropping Enhances the Long-Term Effects of Surface Liming in No-till System. *J. Soil Sci. Plant Nutr.* 2021, 21, 119–130. [CrossRef]

35. Miransari, M. Soil Microbes and the Availability of Soil Nutrients. *Acta Physiol. Plant.* 2013, 35, 3075–3084. [CrossRef]

36. Auler, A.C.; Caires, E.F.; Pires, L.F.; Galetto, S.L.; Romaniw, J.; Charnobay, A.C. Lime Effects in a No-Tillage System on Inceptisols. *Geoderma Reg.* 2019, 16, e00206. [CrossRef]

37. Garcia, A.; Crusciol, C.A.C.; Craym, J.M.; Nascimento, C.A.C.; Martello, J.M.; de Siqueira, G.F.; Tarumoto, M.B. Magnesium as a Promoter of Technological Quality in Sugarcane. *J. Soil Sci. Plant Nutr.* 2020, 20, 19–30. [CrossRef]

38. Joris, H.A.W.; Caires, E.F.; Scharr, D.A.; Bini, A.R.; Haliski, A. Liming in the Conversion from Degraded Pastureland to a No-till Cropping System in Southern Brazil. *Soil Tillage Res.* 2016, 162, 68–77. [CrossRef]

39. Rolim, G.S.; Sentelhas, P.C.; Barbieri, V. Planilha No Ambiente Excel® Para Os Cálculos de Balanços Hídricos: Normal, Seqüencial, de Cultura e de Produtividade Real e Potencial. *Rev. Bras. Agrometeorol.* 1998, 6, 133–137.

40. Thornthwaite, C.W.; Mather, J.R. *Instructions and Tables for Computing Potential Evapotranspiration and the Water Balance*; Publications in Climatology No 3; Laboratory of Climatology: Philadelphia, PA, USA, 1957; Volume 10, 66p.

41. Soil Survey Staff. *Soil Survey Manual Soil Science Division Staff Agriculture Handbook No. 18*; Soil Survey Staff: Washington, DC, USA, 2017.

42. van Raij, B.; Andrade, J.C.; Cantarella, H.; Quaggio, J.A. *Análise Química Para Avaliação Da Fertilidade de Solos Tropicais*; Instituto Agronômico: Campinas, Brazil, 2001.

43. Gee, G.W.; Or, D. Particle Size Analysis. In *Methods of Soil Analysis: Physical Methods*; Dane, J.H., Toop, G.C., Eds.; Soil Science Society of America: Madison, WI, USA, 2002; pp. 255–293.

44. Malavolta, E.; Vitti, G.C.; de Oliveira, S.A. *Avaliação Do Estado Nutricional Das Plantas: Princípios e Aplicações*, 2nd ed.; Associação Brasileira para Pesquisa da Potassa e do Fosfato: Piracicaba, Brazil, 1997.

45. Tanimoto, T. The Press Method of Cane Analysis. *Hawaii. Plant. Rec.* 1964, 57, 133–150.

46. Fernandes, A.C. *Cálculos Na Agroindustria Da Cana-de-Açúcar*, 3rd ed.; STAB—Açúcar, Álcool e Subprodutos: Piracicaba, Piracicaba, 2011.

47. Kaiser, H.F. The Varimax Criterion for Analytic Rotation in Factor Analysis. *Psychometrika* 1958, 23, 187–200. [CrossRef]

48. Manly, B.F.J. *Multivariate Statistical Methods: A Primer*, 2nd ed.; Chapman & Hall: New York, NY, USA, 1994.

49. StatSoftstatistica 7.0 Software 2005.