White Light Emission from Thin-Film Samples of ZnO Nanocrystals, Eu\(^{3+}\) and Tb\(^{3+}\) Ions Embedded in an SiO\(_2\) Matrix

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Abstract: In this work, a method was developed to determine the concentration of Eu\(^{3+}\) and Tb\(^{3+}\) ions in a thin-film sample of SiO\(_2\), co-doped with ZnO-nanocrystals (ZnO-nc), to produce a sample of any desired colour in the International Commission on Illumination (CIE) colour space. Using this method, a white light emitting sample was fabricated. The thin-film sample combines red, green and blue emissions from the Eu\(^{3+}\) ions, Tb\(^{3+}\) ions and ZnO-nc, respectively, to create white light or light of any desired colour. The emissions at 614 nm and 545 nm from Eu\(^{3+}\) and Tb\(^{3+}\) ions, respectively, is due to the energy transfer from the excited ZnO-nc to the rare-earth (RE) ions. In this way, only a single excitation wavelength is needed to excite the ZnO-nc, Eu\(^{3+}\) and Tb\(^{3+}\) ions in the sample to produce emission of a desired colour from the sample. We developed an empirical 4th-degree polynomial equation to determine the concentrations of Eu\(^{3+}\) and Tb\(^{3+}\) ions to produce light of any desired colour in the CIE colour space. Based on the above empirical equation, the concentration of Eu\(^{3+}\) and Tb\(^{3+}\) ions for a white light emitting sample was found to be 0.012 and 0.024 molar fractions, respectively. The white light emission from the sample was confirmed by fabricating the sample using the low-cost sol–gel process. The stimulated emission spectra and the experimental emission spectra of the white light sample fit very well. The results presented in this work are important to develop energy efficient solid state lighting devices.

Keywords: zinc oxide nanocrystals; europium; terbium; white light; energy transfer; photoluminescence

1. Introduction

In recent years, white light emitting diodes have been widely studied [1–5] and developed for various solid state lighting applications. White light emitting diodes play an important role in applications, such as in displays, general lighting and automobile headlights. In most of these applications, the white light is produced either through i) a phosphor conversion ion in which a ultra-violet(UV)-blue light emitting diode (LED) is used along with a yellow phosphor or through ii) a combination of red, green and blue (RGB) LEDs [2].

In this work, we present a simple way to produce white light from thin-film samples containing semiconductor nanocrystal and lanthanide rare-earth (RE) ions. The UV-blue emission from zinc oxide nanocrystals (ZnO-nc) is combined with the red and green emissions from the RE ions, such as Europium (3+) and Terbium (3+), respectively, to produce white light. An advantage of using ZnO-nc, Eu\(^{3+}\) and Tb\(^{3+}\) ions to produce white light is that a thin-film sample of these materials embedded in SiO\(_2\) can be easily fabricated using the low-cost sol-gel process. In this material system, the ZnO-nc can be excited electrically or using a single excitation wavelength having photon energy higher than
the optical gap, which results in the excitation of the ZnO-nc. These excited nanocrystals can then relax through radiative de-excitation, non-radiative de-excitation and by transferring the energy to excite the Eu\(^{3+}\) and Tb\(^{3+}\) ions. The excited Eu\(^{3+}\) and Tb\(^{3+}\) ions, in turn, relax through the radiative de-excitation or non-radiative de-excitation process. The radiative de-excitation from the Eu\(^{3+}\) ions, Tb\(^{3+}\) ions and ZnO-nc results in the red, green and blue emissions, respectively.

There have been substantial studies demonstrating the energy transfer specifically from ZnO-nc to Eu\(^{3+}\) ions [6–18] and also from ZnO-nc to Tb\(^{3+}\) ions [19–23]. Previous works by our group have also reported on the study of the energy transfer mechanism, contribution and transfer efficiency from various ZnO-nc emission centers to Eu\(^{3+}\) ions [17,18,24] and Tb\(^{3+}\) ions individually [23]. Interestingly, there are very few works on co-doping both Eu\(^{3+}\) ions and Tb\(^{3+}\) ions together with ZnO-nc in the same SiO\(_2\) matrix. One such work on co-doping both Eu\(^{3+}\) ions and Tb\(^{3+}\) ions with ZnO-nc by Luo et al. was on the energy transfer process and the energy transfer mechanism from ZnO-nc to the two RE ions [25]. In the study by Luo et al. the energy transfer between the two RE ions themselves is also investigated, but it does not report on a pure white light emitting sample. In fact, we were unable to find any study where energy transfer from ZnO-nc to Eu\(^{3+}\) ions and Tb\(^{3+}\) ions was used to create a white light emitting sample.

White light emission from a material system of ZnO-nc and Eu\(^{3+}\) ions together with a different RE ion, namely Dy\(^{3+}\) (Dysprosium), has been reported by Luo et al. [26]. However, in the work by Luo et al. [26], the ZnO-nc are fabricated in powder form and the RE ion are embedded in the ZnO-nc. The nanocrystals are not embedded in a protective dialectic medium, such as SiO\(_2\). Furthermore, the white light sample reported in the work by Luo et al. [26] does not have pure white light emission (International Commission on Illumination (CIE) chromaticity coordinate \(x = y = z = 0.333\)). In general, we observe that the procedure to systematically obtain the concentration of the different constituent material in the white light emitting sample has not been reported.

In this work, we fabricate thin-film samples of ZnO-nc in SiO\(_2\) co-doped with both Eu\(^{3+}\) ions and Tb\(^{3+}\) ions using the low-cost sol-gel process to create a pure white light emitting sample that can be excited using a single excitation wavelength. The concentration of Eu\(^{3+}\) and Tb\(^{3+}\) ions in the white light emitting sample is systematically obtained in this work. This is a continuation of our previous works [17,18,23,24]. The white light emission was achieved by first fabricating various thin-film samples of ZnO-nc in SiO\(_2\) with varying concentrations of Eu\(^{3+}\) and Tb\(^{3+}\) ions. The photoluminescence (PL) emission intensities from these samples were then used to obtain an empirical equation for the emission intensity as a function of Eu\(^{3+}\) ions and Tb\(^{3+}\) ions concentration. The empirical emission intensity equation was subsequently used to deduce the concentration of Eu\(^{3+}\) ions and Tb\(^{3+}\) ions, which give white light emission and orangish-white light emission. Using the deduced values of the Eu\(^{3+}\) and Tb\(^{3+}\) ion concentration, a white light emitting sample and an orangish-white light emitting sample were then fabricated using the sol-gel process to experimentally confirm the deduction. A white light emission and an orangish-white light emission from the two samples were demonstrated in this work. The knowledge and understanding gained from this work will be beneficial for the development of energy efficient solid state white lighting devices which use the energy transfer process from ZnO-nc to Eu\(^{3+}\) and Tb\(^{3+}\) ions, to produce light.

2. Materials and Method

In this work, the sol-gel process was employed in the fabrication of the thin-film samples due to the low-cost nature of this chemical process. Twenty-six different samples of ZnO nanocrystals (ZnO-nc) embedded in SiO\(_2\) matrix co-doped with varying concentration of Eu\(^{3+}\) ions and Tb\(^{3+}\) ions were fabricated, which are listed in Table 1. The samples in this work are labelled as Eu\(^{3+}\)_m:Tb\(^{3+}\)_n:ZnO-nc:SiO\(_2\) where \(m\) is the molar fraction of the concentration of Eu\(^{3+}\) ions calculated using the formula

\[
m = \frac{\text{moles of (Eu}^{3+}\text{)}}{\text{moles of (Eu}^{3+}\text{)+Tb}^{3+}\text{+Zn+Si})}
\]

and \(n\) is the molar fraction of the concentration of Tb\(^{3+}\) ions calculated using the formula

\[
n = \frac{\text{moles of (Tb}^{3+}\text{)}}{\text{moles of (Eu}^{3+}\text{)+Tb}^{3+}\text{+Zn+Si})}
\]

Note here that eight of these samples are...
the samples from our previous work which have been reported elsewhere [17,23], while the remaining eighteen samples were newly fabricated for this current work as indicated in Table 1. Furthermore, out of the total twenty-six different samples listed in Table 1, twenty-four of the samples were used to establish the empirical equation in this work, while the remaining two samples (Eu$^{3+}$0.012:Tb$^{3+}$0.024:ZnO-nc:SiO$_2$ and Eu$^{3+}$0.014:Tb$^{3+}$0.084:ZnO-nc:SiO$_2$) were used to confirm the empirical equation.

### Table 1. List of 26 samples fabricated using the sol-gel process.

| Samples from Previous Work               | Samples Newly Fabricated for Current Work                  |
|-----------------------------------------|-----------------------------------------------------------|
| Eu$^{3+}$0.04:Tb$^{3+}$0:ZnO-nc:SiO$_2$  | Eu$^{3+}$0.003:Tb$^{3+}$0.03:ZnO-nc:SiO$_2$               |
| Eu$^{3+}$0.06:Tb$^{3+}$0:ZnO-nc:SiO$_2$  | Eu$^{3+}$0.003:Tb$^{3+}$0.06:ZnO-nc:SiO$_2$               |
| Eu$^{3+}$0.12:Tb$^{3+}$0:ZnO-nc:SiO$_2$  | Eu$^{3+}$0.003:Tb$^{3+}$0.09:ZnO-nc:SiO$_2$               |
| Eu$^{3+}$0.16:Tb$^{3+}$0:ZnO-nc:SiO$_2$  | Eu$^{3+}$0.003:Tb$^{3+}$0.12:ZnO-nc:SiO$_2$               |
| Eu$^{3+}$0.004:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.004:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.008:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.008:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.012:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.012:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.016:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.016:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.020:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.020:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.024:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.024:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.028:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.028:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.032:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.032:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.036:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.036:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.040:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.040:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.044:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.044:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.048:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.048:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.052:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.052:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.056:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.056:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.060:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.060:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.064:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.064:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.068:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.068:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.072:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.072:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.076:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.076:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.080:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.080:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |
| Eu$^{3+}$0.084:Tb$^{3+}$0:ZnO-nc:SiO$_2$ | Eu$^{3+}$0.084:Tb$^{3+}$0:ZnO-nc:SiO$_2$                  |

The samples were fabricated using an identical recipe described in our previous publications [17, 18,23,24]. In all the twenty-six samples, the molar ratio of Zn:Si in the samples was maintained at 1:2. The Eu$^{3+}$ ions and Tb$^{3+}$ ions are doped into the SiO$_2$ matrix by mixing Europium(III) nitrate pentahydrate and Terbium(III) nitrate pentahydrate salts, respectively, in the SiO$_2$ sol. After a 24 h ageing of the two different sols, namely SiO$_2$ sol and ZnO-nc sol, they were mixed together before being spin-coated on a Si substrate. These samples were then made into densified thin films by soft baking at 100 °C, followed by annealing at 450 °C using rapid thermal processing (RTP).

The thin-film samples were characterised by studying the photoluminescence (PL) emissions from the sample using SPEX Fluorolog-3 Model FL3-11 spectrofluorometer(Horiba, Edison, NJ, USA). The PL spectra were obtained by exciting the samples at 325 nm using the 450-W xenon short arc lamp of the spectrofluorometer attached to a monochromator and then measuring the emission intensity from the sample at each wavelength ranging from 340 nm to 635 nm using a photomultiplier tube (PMT) detector coupled to another monochromator.

### 3. Results and Discussion

As mentioned above, to obtain the right concentrations of Eu$^{3+}$ and Tb$^{3+}$ ions together with the ZnO-nc (which is fixed in this work), we need to establish an empirical equation of the PL intensity as a function of Eu$^{3+}$ and Tb$^{3+}$ ion concentrations. The empirical equation is derived based on the PL intensity data of the samples listed in Table 2. We show the PL spectra of some of the samples listed in Table 2 and Figures 1–3 below. Figure 1 shows the PL spectra of the SiO$_2$ films doped with ZnO-nc and varying concentrations of Eu$^{3+}$ ions, namely Eu$^{3+}$0.03:Tb$^{3+}$0:ZnO-nc:SiO$_2$, Eu$^{3+}$0.06:Tb$^{3+}$0:ZnO-nc:SiO$_2$, Eu$^{3+}$0.09:Tb$^{3+}$0:ZnO-nc:SiO$_2$ and the PL spectra of Eu$^{3+}$0.012:Tb$^{3+}$0:ZnO-nc:SiO$_2$ sample (the SiO$_2$ film doped with ZnO-nc only). These samples of ZnO-nc and Eu$^{3+}$ ions embedded in SiO$_2$ are the newly fabricated samples made for this current work (indicated in Table 1). The PL spectra of the other samples doped only with Eu$^{3+}$ ions and ZnO-nc in SiO$_2$, namely Eu$^{3+}$0.04:Tb$^{3+}$0:ZnO-nc:SiO$_2$, Eu$^{3+}$0.08:Tb$^{3+}$0:ZnO-nc:SiO$_2$, Eu$^{3+}$0.12:Tb$^{3+}$0:ZnO-nc:SiO$_2$ and Eu$^{3+}$0.16:Tb$^{3+}$0:ZnO-nc:SiO$_2$ samples have been previously published by our group [17] and hence, not shown in Figure 1. From the PL emission spectra, we clearly see
the signature emission peaks of Eu\(^{3+}\) ions at 590 nm and 614 nm for the samples with Eu\(^{3+}\) ions, corresponding to \(5D_0 \rightarrow 7F_1\) and \(5D_0 \rightarrow 7F_2\) transitions, respectively. These emissions which are due to the energy transfer process have been discussed in detail in our previous publication [17]. The PL spectrum of the SiO\(_2\) film containing only ZnO-nc (Eu\(^{3+}\)\(_0\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) sample), which is also included in Figure 1, shows the characteristic broadband emission of ZnO-nc ranging from 350 nm to 600 nm. The origin of the broadband emission from ZnO-nc together with a detailed discussion on the energy transfer process and contribution of energy transfer from ZnO-nc to Eu\(^{3+}\) ion has been reported in our group’s earlier work [17].

Table 2. International commission on illumination (CIE) \(x\), \(y\) and \(z\) chromaticity values of the twenty-four different samples used to establish the empirical equation of the PL intensity as a function of Eu\(^{3+}\) and Tb\(^{3+}\) ion concentrations.

| Samples                        | \(X\)  | \(Y\)  | \(Z\)  |
|--------------------------------|--------|--------|--------|
| Eu\(^{3+}\)\(_0\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.258  | 0.328  | 0.414  |
| Eu\(^{3+}\)\(_{0.03}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.356  | 0.294  | 0.35   |
| Eu\(^{3+}\)\(_{0.04}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.369  | 0.298  | 0.333  |
| Eu\(^{3+}\)\(_{0.06}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.4313 | 0.281  | 0.288  |
| Eu\(^{3+}\)\(_{0.08}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.444  | 0.306  | 0.25   |
| Eu\(^{3+}\)\(_{0.09}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.496  | 0.33   | 0.174  |
| Eu\(^{3+}\)\(_{0.12}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.517  | 0.321  | 0.162  |
| Eu\(^{3+}\)\(_{0.16}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.546  | 0.314  | 0.14   |
| Eu\(^{3+}\)\(_{0.03}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.268  | 0.352  | 0.38   |
| Eu\(^{3+}\)\(_{0.04}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.244  | 0.309  | 0.447  |
| Eu\(^{3+}\)\(_{0.06}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.295  | 0.41   | 0.295  |
| Eu\(^{3+}\)\(_{0.08}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.301  | 0.431  | 0.268  |
| Eu\(^{3+}\)\(_{0.09}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.305  | 0.419  | 0.276  |
| Eu\(^{3+}\)\(_{0.12}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.332  | 0.456  | 0.21   |
| Eu\(^{3+}\)\(_{0.16}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.328  | 0.447  | 0.225  |
| Eu\(^{3+}\)\(_{0.03}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.414  | 0.334  | 0.252  |
| Eu\(^{3+}\)\(_{0.04}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.441  | 0.33   | 0.229  |
| Eu\(^{3+}\)\(_{0.09}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.481  | 0.321  | 0.198  |
| Eu\(^{3+}\)\(_{0.06}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.465  | 0.318  | 0.217  |
| Eu\(^{3+}\)\(_{0.08}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.484  | 0.308  | 0.208  |
| Eu\(^{3+}\)\(_{0.09}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.538  | 0.307  | 0.155  |
| Eu\(^{3+}\)\(_{0.03}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.49   | 0.309  | 0.201  |
| Eu\(^{3+}\)\(_{0.06}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.514  | 0.305  | 0.181  |
| Eu\(^{3+}\)\(_{0.09}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) | 0.545  | 0.3     | 0.155  |

Figure 1. The photoluminescence (PL) spectra of Eu\(^{3+}\)\(_0\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\), Eu\(^{3+}\)\(_{0.03}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\), Eu\(^{3+}\)\(_{0.06}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) and Eu\(^{3+}\)\(_{0.09}\):Tb\(^{3+}\)_0:ZnO-nc:SiO\(_2\) samples upon excitation using 325 nm excitation source.
To demonstrate a sample of desired colour (white light in this study), first, the physiologically perceived colour of the samples need to be deduced. This is achieved by calculating the chromaticity coordinates of the PL emission from the samples. The chromaticity coordinates are a standard defined by the International Commission on Illumination (CIE) which consists of three a standard defined by the International Commission on Illumination (CIE) which consists of three

Figure 2. The PL spectra of Eu$^{3+}:Tb^{3+}:ZnO$-nc:SiO$_2$, Eu$^{3+}:Tb^{3+}:0.03$ZnO-nc:SiO$_2$, Eu$^{3+}:Tb^{3+}:0.06$ZnO-nc:SiO$_2$ and Eu$^{3+}:Tb^{3+}:0.09$ZnO-nc:SiO$_2$ samples upon excitation using 325 nm excitation source.

Figure 3. The PL spectra of Eu$^{3+}:Tb^{3+}:ZnO$-nc:SiO$_2$, Eu$^{3+}:Tb^{3+}:0.03$ZnO-nc:SiO$_2$, Eu$^{3+}:Tb^{3+}:0.06$ZnO-nc:SiO$_2$ and Eu$^{3+}:Tb^{3+}:0.09$ZnO-nc:SiO$_2$ samples upon excitation using 325 nm excitation source.

Figure 2 shows the PL spectra of the SiO$_2$ films doped with ZnO-nc and varying concentrations of Tb$^{3+}$ ions, namely Eu$^{3+}:0$:Tb$^{3+}:0.03$:ZnO-nc:SiO$_2$, Eu$^{3+}:0$:Tb$^{3+}:0.06$:ZnO-nc:SiO$_2$ and Eu$^{3+}:0$:Tb$^{3+}:0.09$:ZnO-nc:SiO$_2$. Again, these samples of ZnO-nc and Tb$^{3+}$ ions embedded in SiO$_2$ are the newly fabricated samples made for this current work (indicated in Table 1). The PL spectra of the SiO$_2$ film doped only with ZnO-nc (Eu$^{3+}:0$:Tb$^{3+}:0$:ZnO-nc:SiO$_2$ sample) is also included the figure. The PL spectra of the other samples doped only with Tb$^{3+}$ ions and ZnO-nc in SiO$_2$, namely Eu$^{3+}:0$:Tb$^{3+}:0.04$:ZnO-nc:SiO$_2$, Eu$^{3+}:0$:Tb$^{3+}:0.08$:ZnO-nc:SiO$_2$, Eu$^{3+}:0$:Tb$^{3+}:0.12$:ZnO-nc:SiO$_2$ and Eu$^{3+}:0$:Tb$^{3+}:0.16$:ZnO-nc:SiO$_2$ samples have been published in our earlier work [23] and hence, not shown in Figure 2. Once again from the PL spectra, we observe the characteristic emission from the Tb$^{3+}$ ions at 489 nm, 545 nm, 586 nm and 621 nm in samples with Tb$^{3+}$ ions. These emissions correspond to $^5$D$_{4}$→$^7$F$_{6}$, $^5$D$_{4}$→$^7$F$_{5}$, $^5$D$_{4}$→$^7$F$_{4}$ and $^5$D$_{4}$→$^7$F$_{3}$ transitions, respectively. This energy transfer process and mechanism of energy transfer from ZnO-nc to Tb$^{3+}$ ions has been reported in detail in our previous publication [23].

The main focus of this study, as mentioned above, is to demonstrate a white light emitting sample by incorporating both Eu$^{3+}$ ions and Tb$^{3+}$ ions together with ZnO-nc in thin-film samples of SiO$_2$. 

![Figure 2](image1.png)

![Figure 3](image2.png)
Hence, samples with varying concentrations of both Eu\(^{3+}\) ions and Tb\(^{3+}\) ions together with a fixed concentration of ZnO-nc in SiO\(_2\) matrix were also fabricated. Figure 3 shows the PL spectra of some of the samples of SiO\(_2\) doped with Eu\(^{3+}\) ions, Tb\(^{3+}\) ions and ZnO-nc, namely Eu\(^{3+\,0.03}\):Tb\(^{3+\,0.03}\):ZnO-nc:SiO\(_2\), Eu\(^{3+\,0.06}\):Tb\(^{3+\,0.06}\):ZnO-nc:SiO\(_2\) and Eu\(^{3+\,0.09}\):Tb\(^{3+\,0.09}\):ZnO-nc:SiO\(_2\). Again, we also include the PL spectra of the sample doped only with ZnO-nc (Eu\(^{3+\,0}\):Tb\(^{3+\,0}\):ZnO-nc:SiO\(_2\) sample). In all of the samples with both Eu\(^{3+}\) ions and Tb\(^{3+}\) ions co-doped with ZnO-nc in SiO\(_2\), we clearly observe the emission peaks from Tb\(^{3+}\) ions at 489 nm and 545 nm, the emission peaks from Eu\(^{3+}\) ions at 590 nm and 614 nm and the relatively broader emission from ZnO-nc with peak intensity at 372 nm. These emissions from the Tb\(^{3+}\) and Eu\(^{3+}\) ions are the radiative de-excitations of the RE ions excited through the energy transfer process from excited ZnO-nc.

To demonstrate a sample of desired colour (white light in this study), first, the physiologically perceived colour of the samples need to be deduced. This is achieved by calculating the \(xyz\) chromaticity coordinates of the PL emission from the samples. The \(xyz\) chromaticity coordinates are a standard defined by the International Commission on Illumination (CIE) which consists of three values denoted by \(x\), \(y\) and \(z\). The CIE \(x\), \(y\) and \(z\) chromaticity coordinates are essentially normalised fractions which give a quantitative relation between the spectrum of emission from the sample and the colour perceived by the three different receptors in the human eye \([27]\). CIE \(x\), \(y\) and \(z\) chromaticity values are obtained using the following mathematical equations:

\[
X = \int_{0}^{\infty} I(\lambda) \overline{x}(\lambda) d\lambda \tag{1}
\]

\[
Y = \int_{0}^{\infty} I(\lambda) \overline{y}(\lambda) d\lambda \tag{2}
\]

\[
Z = \int_{0}^{\infty} I(\lambda) \overline{z}(\lambda) d\lambda \tag{3}
\]

\[
x = \frac{X}{X + Y + Z} \tag{4}
\]

\[
y = \frac{Y}{X + Y + Z} \tag{5}
\]

\[
z = \frac{Z}{X + Y + Z} = 1 - x - y \tag{6}
\]

where \(I(\lambda)\) is the emission intensity of the thin-film sample as a function of wavelength and \(\overline{x}(\lambda)\), \(\overline{y}(\lambda)\) and \(\overline{z}(\lambda)\) are the CIE colour-matching functions for the 1964 standard colorimetric observer which are essentially the spectral response of the three different receptors in the human eye \([27]\). The \(x\), \(y\) and \(z\) values, correspond to the degree of red, green and blue colours, respectively, as perceived by the human eye. This means, the greater the value of \(x\), the more red the sample looks. Similarly, the greater the value of \(y\), the more green the sample looks and the greater the value of \(z\), the more blue the sample looks.

Table 2 shows the \(x\), \(y\) and \(z\) values for the twenty-four samples used to establish the empirical equation in this work, calculated using the above Equations (1)-(6), which is also graphically represented in CIE 1964 colour space plot shown in Figure 4.
where work as the simulated intensity spectra obtained from these equations (not shown) does not show Tb polynomial equation in $m$ and 4th-degree polynomial equation is written as $Eu$ 4th-degree polynomial equation in two variables is optimum to represent the intensity spectra of the $ZnO-nc$ in $SiO_2$ listed in Table 2 which include 1) sample with only $ZnO-nc$ in $SiO_2$, 2) samples with $Eu$, $m$ and $ZnO-nc$ in $SiO_2$, 3) samples with $Tb$, $m$ and $ZnO-nc$ in $SiO_2$ and 4) samples with both $Eu$, $m$ and $Tb$ ions together with $ZnO-nc$ in $SiO_2$. Thus, the polynomial equations accounts for the interactions among all the constituents (RE ions and $ZnO$-nc).

The intensity spectra of the $Eu$, $m$:$Tb$, $n$:ZnO-nc:SiO$_2$ samples can be described by using a polynomial equation in $m$ (the molar fraction of the concentration of $Eu$, $m$ ions) and $n$ (the molar fraction of the concentration of $Tb$, $n$ ions). In this work, the 3rd, 4th and 5th-degree polynomial equation in two variables were considered to model the PL emission of $Eu$, $m$:$Tb$, $n$:ZnO-nc:SiO$_2$ samples. The 1st and 2nd-degree polynomial equation in two variables were not considered in this work as the simulated intensity spectra obtained from these equations (not shown) does not show good fit with the experimentally obtained emission intensity values of the sample. We found that the 4th-degree polynomial equation in two variables is optimum to represent the intensity spectra of the $Eu$, $m$:$Tb$, $n$:ZnO-nc:SiO$_2$ samples and the justification for this is given below. Mathematically the 4th-degree polynomial equation is written as

$$ I(\lambda, m, n) = C_{00}(\lambda) + C_{10}(\lambda)m + C_{01}(\lambda)n + C_{20}(\lambda)m^2 + C_{11}(\lambda)mn + C_{02}(\lambda)n^2 $$

$$ + C_{30}(\lambda)m^3 + C_{21}(\lambda)m^2n + C_{12}(\lambda)mn^2 + C_{03}(\lambda)n^3 + C_{40}(\lambda)m^4 $$

$$ + C_{31}(\lambda)m^3n + C_{22}(\lambda)m^2n^2 + C_{13}(\lambda)mn^3 + C_{04}(\lambda)n^4, $$

where $I(\lambda, m, n)$ is the emission intensity of the $Eu$, $m$:$Tb$, $n$:ZnO-nc:SiO$_2$ sample at wavelength $\lambda$ and $C_{00}(\lambda)$, $C_{10}(\lambda)$, $C_{01}(\lambda)$, $C_{20}(\lambda)$, $C_{11}(\lambda)$, $C_{02}(\lambda)$, $C_{30}(\lambda)$, $C_{21}(\lambda)$, $C_{12}(\lambda)$, $C_{03}(\lambda)$, $C_{40}(\lambda)$, $C_{31}(\lambda)$.
C_{22}(\lambda), C_{13}(\lambda) \text{ and } C_{04}(\lambda) \text{ are the coefficients of the polynomial equation in } m \text{ and } n, \text{ which are unique for each wavelength } \lambda.

All the values of the coefficient of the polynomial in Equation (7), i.e., the values of all C, from C_{00}(\lambda) \text{ to } C_{04}(\lambda), \text{ for each emission wavelength (} \lambda) \text{ ranging from 340 nm to 635 nm were obtained using the MATLAB parametric fitting optimisation function which employs the linear least squares regression method to find these optimum values.} \text{ The goodness of the fit of Equation (7) was confirmed by comparing the experimentally obtained PL spectra of the twenty-four samples with those from the empirical Equation (7), which we will refer to as simulated spectra.}

To justify that the 4th-degree polynomial equation in two variables is optimum to represent the intensity spectra of the Eu^{3+}_{m}:Tb^{3+}_{n}:ZnO-nc:SiO_{2} \text{ samples, we first calculated the sum of the squares of the difference between the experimental emission intensity value and the simulated emission intensity value at each wavelength, which is known as residual sum of squares and denoted by RSS.} \text{ The RSS value was calculated for each of 3rd, 4th and 5th-degree polynomial equations.} \text{ RSS is mathematically is given by}

\begin{equation}
RSS = \sum_{\lambda = 340}^{635} (I_{E}(\lambda) - I_{S}(\lambda))^{2},
\end{equation}

where \( I_{E}(\lambda) \) is the experimental emission intensity value and \( I_{S}(\lambda) \) is the simulated emission intensity value. \text{ RSS for 3rd, 4th and 5th-degree polynomial equation are denoted by RSS}_{3}, RSS_{4} \text{ and RSS}_{5}, \text{ respectively.} \text{ To determine which polynomial equations is optimum to simulate the emission spectra, we then calculate and compare the percentage change of RSS from 3rd degree to 4th degree (denoted by } %RSS(3 \rightarrow 4) \text{) and 4th degree to 5th degree (denoted by } %RSS(4 \rightarrow 5) \text{).}

\text{This is given by:}

\begin{equation}
%RSS(3 \rightarrow 4) = \frac{RSS_{4} - RSS_{3}}{RSS_{3}} \times 100\%,
\end{equation}

\begin{equation}
%RSS(4 \rightarrow 5) = \frac{RSS_{5} - RSS_{4}}{RSS_{4}} \times 100\%.
\end{equation}

\text{The } %RSS(3 \rightarrow 4) \text{ and } %RSS(4 \rightarrow 5) \text{ values are given in Table 3.}

\text{Table 3. Percentage change in the RSS value from 3rd-degree to 4th-degree and 4th-degree to 5th-degree polynomial equations.}

| Samples | Percentage Change |
|---------|-------------------|
|         | RSS\%(3\rightarrow4) | RSS\%(4\rightarrow5) |
| Eu^{3+}_{0}:Tb^{3+}_{0}:ZnO-nc:SiO_{2} | 90.44% | 5.22% |
| Eu^{3+}_{0.09}:Tb^{3+}_{0.09}:ZnO-nc:SiO_{2} | 76.27% | 9.85% |
| Eu^{3+}_{0.03}:Tb^{3+}_{0.03}:ZnO-nc:SiO_{2} | 48.91% | 2.64% |
| Eu^{3+}_{0.03}:Tb^{3+}_{0.03}:ZnO-nc:SiO_{2} | 98.21% | 4.48% |

\text{Figure 5 shows the simulated intensity spectra obtained using the 3rd, 4th and 5th-degree polynomial equation in two variables together with the experimental emission intensity spectra of four of the Eu^{3+}_{m}:Tb^{3+}_{n}:ZnO-nc:SiO_{2} \text{ samples, namely Eu^{3+}_{0}:Tb^{3+}_{0}:ZnO-nc:SiO_{2}, Eu^{3+}_{0.09}:Tb^{3+}_{0.09}:ZnO-nc:SiO_{2}, Eu^{3+}_{0.03}:Tb^{3+}_{0.03}:ZnO-nc:SiO_{2} and Eu^{3+}_{0.03}:Tb^{3+}_{0.03}:ZnO-nc:SiO_{2}. We observe that the simulated emission spectra obtained using the 3rd, 4th and 5th-degree polynomial equation have a good fit with the experimental emission intensity values. The 3rd-degree polynomial equation simulated spectra of the Eu^{3+}_{0.03}:Tb^{3+}_{0.03}:ZnO-nc:SiO_{2} \text{ sample is an exception and does not show good fit as seen in Figure 5d. For the particular sample, the emission peak at 545 nm and 614 nm does not fit well with the experimental emission intensity values.}

\text{From Table 3 we see that the } %RSS(3 \rightarrow 4) \text{ vary from 48% to 98%, while } %RSS(4 \rightarrow 5) \text{ are all less than 10% for the four samples presented in Figure 5. This shows that the improvement of the simulated spectra from 4th to 5th-degree polynomial is much smaller compared to the improvement of the}
simulated spectra from 3rd to 4th-degree polynomial. Hence, the 4th-degree polynomial equation in two variables was chosen to represent the experimental intensity spectra of the Eu$^{3+}$:Tb$^{3+}$:ZnO-nc:SiO$_2$ samples in this work.

Figure 5. Cont.
The measured PL spectra are shown in Figures 6 and 7, respectively. As expected, we obtained Tb very well. In short, we have successfully demonstrated that we are able to design and fabricate using a single wavelength excitation.

In Figure 6 and Figure 7 also shows that the stimulated and the experimental spectra fit very well. In the CIE colour space, the values were $m = 0.012$ and $n = 0.024$. We then fabricated two sample, namely Eu$^{3+}_{0.012}$:Tb$^{3+}_{0.024}$:ZnO-nc:SiO$_2$ for a white light sample and Eu$^{3+}_{0.014}$:Tb$^{3+}_{0.084}$:ZnO-nc:SiO$_2$ sample. The measured PL spectra are shown in Figures 6 and 7, respectively. As expected, we obtained a white light emission corresponding to $x = 0.451$, $y = 0.354$ and $z = 0.194$, which was found to be $m = 0.014$ and $n = 0.084$. We then fabricated two sample, namely Eu$^{3+}_{0.012}$:Tb$^{3+}_{0.024}$:ZnO-nc:SiO$_2$ for a white light sample and Eu$^{3+}_{0.014}$:Tb$^{3+}_{0.084}$:ZnO-nc:SiO$_2$ sample. The measured PL spectra are shown in Figures 6 and 7, respectively. As expected, we obtained a white light emission from the white light sample, Eu$^{3+}_{0.012}$:Tb$^{3+}_{0.024}$:ZnO-nc:SiO$_2$, as shown in Figure 6. Figures 6 and 7 also shows that the stimulated and the experimental spectra fit very well. In short, we have successfully demonstrated that we are able to design and fabricate Eu$^{3+}_{m}$:Tb$^{3+}_{n}$:ZnO-nc:SiO$_2$ samples which emit light of any desired colours in the CIE colour space, using a single wavelength excitation.

![Figure 5](image-url)  
Figure 5. The simulated and experimental emission intensity spectra of four Eu$^{3+}_{m}$:Tb$^{3+}_{n}$:ZnO-nc:SiO$_2$ samples, namely (a) Eu$^{3+}_{0}$:Tb$^{3+}_{0}$:ZnO-nc:SiO$_2$; (b) Eu$^{3+}_{0.09}$:Tb$^{3+}_{0}$:ZnO-nc:SiO$_2$; (c) Eu$^{3+}_{0}$:Tb$^{3+}_{0.09}$:ZnO-nc:SiO$_2$ and (d) Eu$^{3+}_{0.03}$:Tb$^{3+}_{0.03}$:ZnO-nc:SiO$_2$.

Having obtained the empirical equation for the emission intensity of the Eu$^{3+}_{m}$:Tb$^{3+}_{n}$:ZnO-nc:SiO$_2$ sample as a function of Eu$^{3+}$ ions concentration ($m$) and Tb$^{3+}$ ions concentration ($n$), we then used the empirical Equation (7) to generate the emission intensity spectra of Eu$^{3+}_{m}$:Tb$^{3+}_{n}$:ZnO-nc:SiO$_2$ samples for every value of $m$ and $n$ ranging from 0 to 0.090 with a difference of 0.001. The CIE $x$, $y$ and $z$ chromaticity values were then calculated for each of the simulated emission intensity using Equations (1) to (6). We found that for a white light emission corresponding to $x = y = z = 0.333$ in the CIE colour space, the values were $m = 0.012$ and $n = 0.024$. We also determined the Eu$^{3+}$ ions and Tb$^{3+}$ ions concentrations for CIE chromaticity values (chosen arbitrarily), $x = 0.451$, $y = 0.354$ and $z = 0.194$, which was found to be $m = 0.014$ and $n = 0.084$. We then fabricated two sample, namely Eu$^{3+}_{0.012}$:Tb$^{3+}_{0.024}$:ZnO-nc:SiO$_2$ for a white light sample and Eu$^{3+}_{0.014}$:Tb$^{3+}_{0.084}$:ZnO-nc:SiO$_2$ sample. The measured PL spectra are shown in Figures 6 and 7, respectively. As expected, we obtained a white light emission from the white light sample, Eu$^{3+}_{0.012}$:Tb$^{3+}_{0.024}$:ZnO-nc:SiO$_2$, as shown in Figure 6. Figures 6 and 7 also shows that the simulated and the experimental spectra fit very well. In short, we have successfully demonstrated that we are able to design and fabricate Eu$^{3+}_{m}$:Tb$^{3+}_{n}$:ZnO-nc:SiO$_2$ samples which emit light of any desired colours in the CIE colour space, using a single wavelength excitation.

![Figure 6](image-url)  
Figure 6. The simulated and experimental emission intensity spectra of Eu$^{3+}_{0.012}$:Tb$^{3+}_{0.024}$:ZnO-nc:SiO$_2$ sample. The inset shows the image of the sample emitting white light upon exciting the sample using 300 nm UV led light.
Figure 7. The simulated and experimental emission intensity spectra of Eu\(^{3+}\)\(_{0.014}\):Tb\(^{3+}\)\(_{0.084}\):ZnO-nc:SiO\(_2\) sample. The inset shows the image of the sample emitting orangish-white light upon exciting the sample using 300 nm UV led light.

4. Conclusions

In conclusion, in this work we have developed a method to determine the concentration of Eu\(^{3+}\) ions and Tb\(^{3+}\) ions in a thin-film sample of SiO\(_2\) co-doped with ZnO-nc (Eu\(^{3+}\)\(_m\):Tb\(^{3+}\)\(_n\):ZnO-nc:SiO\(_2\) samples) to produce a white light emitting sample or a sample emitting any desired colour in the CIE colour space. Based on the PL data of our samples having various Eu\(^{3+}\) and Tb\(^{3+}\) ion concentrations and fixed ZnO-nc concentration, we established a 4th-degree polynomial equation in \(m\) (the molar fraction of the concentration of Tb\(^{3+}\) ions) and \(n\) (the molar fraction of the concentration of Tb\(^{3+}\) ions) to determine the values of \(m\) and \(n\) to produce a white light or any desired colour emitting sample. The sample combines the red, green and blue emissions from the Eu\(^{3+}\) ions, Tb\(^{3+}\) ions and ZnO-nc, respectively, to create the white light or any desired colour emission. The emissions from Eu\(^{3+}\) ions and Tb\(^{3+}\) ions are due to the energy transfer from ZnO-nc to the RE ions. Hence, only a single excitation wavelength, which is used to excite the ZnO-nc, is required to produce various colour emissions. For a white light emitting sample, the values of \(m\) and \(n\) are found to be 0.012 and 0.024, respectively. Similarly, for a sample with CIE chromaticity values (chosen arbitrarily), \(x = 0.451\), \(y = 0.354\) and \(z = 0.194\), the values of \(m\) and \(n\) correspond to 0.014 and 0.084, respectively. We showed that the stimulated and the experimental spectra of these two samples fit very well. The Eu\(^{3+}\)\(_{0.012}\):Tb\(^{3+}\)\(_{0.024}\):ZnO-nc:SiO\(_2\) sample, indeed, gives a white light emission. The results presented in this work are important to develop energy efficient solid state lighting devices of any desired colour, such as white light emission, using a single excitation wavelength. In general, this knowledge will help in the development of devices using semiconductor nanocrystals as sensitisers to excite RE ions which have wide ranging application in lasers, optical amplifiers, lighting and display technologies.

Author Contributions: V.M. performed the experimental work, analyzed the data, and started the write-up. K.P. initiated and supervised the research work and improved the manuscript for submission and publication.

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