Dynamics of COVID-19 under social distancing measures are driven by transmission network structure

Anjalika Nande\textsuperscript{1}, Ben Adlam\textsuperscript{1}, Justin Sheen\textsuperscript{2}, Michael Z. Levy\textsuperscript{2}, Alison L. Hill\textsuperscript{1*}

\textsuperscript{1}Program for Evolutionary Dynamics, Harvard University, Cambridge, MA, 02138
\textsuperscript{2}Department of Biostatistics, Epidemiology and Informatics, University of Pennsylvania, Philadelphia, PA 19104
* contact alhill@fas.harvard.edu

Abstract

In the absence of pharmaceutical interventions, social distancing is being used worldwide to curb the spread of COVID-19. The impact of these measures has been inconsistent, with some regions rapidly nearing disease elimination and others seeing delayed peaks or nearly flat epidemic curves. Here we build a stochastic epidemic model to examine the effects of COVID-19 clinical progression and transmission network structure on the outcomes of social distancing interventions. We find that the strength of within-household transmission is a critical determinant of success, governing the timing and size of the epidemic peak, the rate of decline, individual risks of infection, and the success of partial relaxation measures. The structure of residual external connections, driven by workforce participation and essential businesses, interacts to determine outcomes. These findings can improve future predictions of the timescale and efficacy of interventions needed to control similar outbreaks, and highlight the need for better quantification and control of household transmission.

MAIN TEXT:

Introduction

In less than five months the novel coronavirus SARS-CoV-2, the causative agent of COVID-19, has spread from an initial foci in Wuhan, China to nearly every corner of the globe. At the time of writing, over 300,000 deaths had been reported, which will likely move this emerging infection into the top five viral causes of death this year. Several clinical and epidemiological features of COVID-19 have contributed to its disastrous effects worldwide. The overlap in symptoms with many endemic and milder respiratory infections - such as influenza, parainfluenza, respiratory syncytial virus, and seasonal coronaviruses - make syndromic identification of cases difficult. The relatively high percentage of infected individuals who require hospitalization or critical care compared to seasonal respiratory infections has put an unprecedented burden on the healthcare systems of hard-hit regions. The important role of asymptomatic individuals in
transmitting infection makes symptom-based isolation ineffective. Perceived ambiguity about the case fatality risk from COVID-19 and misguided comparisons to seasonal influenza contributed to sluggish responses in many regions, in contrast to previous outbreaks of SARS and MERS.

In the absence of either a vaccine or antiviral therapy, and given the continuing limitations in testing capacity in most regions, the main tools implemented worldwide to control the spread of COVID-19 have been “non-pharmaceutical interventions” including “social distancing”, isolation of cases, and quarantine of contacts. All of these measures are crude attempts to prevent the person-to-person contact that drives the transmission of respiratory infections, and have been used since antiquity in attempts to control outbreaks of plague, smallpox, influenza, and other infectious diseases. Social distancing is a blanket term covering any measure that attempts to reduce contacts between individuals, without regards to their infection status. Within two weeks of identifying the original outbreak in Wuhan, a cordon sanitaire had been implemented around the entire Hubei province, prohibiting travel in or out of the region and requiring individuals to remain in their houses except to buy essential supplies. Elsewhere schools and universities have been closed, international travel has been limited, restaurants and retailers shuttered, mask-wearing encouraged or required, and stay-at-home orders put in place.

Mathematical models of COVID-19 transmission provided early support for the idea that social distancing measures could “flatten the curve” and reduce the potential for COVID-19 cases to overwhelm healthcare resources. An influential report from the Imperial College COVID-19 Modeling Team showed that suppression of the epidemic to levels low enough to avoid overflow of healthcare capacity would require an “intensive intervention package” that combined school closures, case isolation, and social distancing of the entire population, applied for the majority of time over 2 years [1]. Kissler et al also came to the conclusion that large sustained reductions in the basic reproductive ratio $R_0$ (the average number of secondary infections generated by an infected individual) would be needed, even after accounting for the potential role of seasonality in transmission [2]. Many more forecasting models predicted dramatic decreases in the burden of COVID-19 if interventions were enacted (e.g. [3,4]). Real-time and retrospective analyses of the growth rate of cases and deaths have suggested that in some settings the epidemic eventually slowed after the implementation of strong social distancing measures (e.g. in Wuhan and other Chinese cities [5,6], in Hong Kong [7], across European countries [8], French regions [9], or some US states [10,11]).

The observed dynamics of COVID-19 outbreaks following social distancing policies have been inconsistent, unpredictable, and the source of much confusion and debate in the general public and among epidemiologists. Declines in cases and deaths have not occurred uniformly across regions and have often only occurred after a long delay. The economic and social costs of these measures are immense: unemployment has surged, stock markets have plummeted, delivery of healthcare for non-COVID-19 conditions has been interrupted. Social isolation also brings on or exacerbates mental health conditions. Weeks after implementing strong interventions, many regions have continued to see increases in daily diagnoses and deaths. Does this mean the interventions are not working? Since the political will to sustain strict social distancing measures is waning in many places, it is important to understand the expected timescale to judge success
or failure. If stronger interventions - such as “shelter-in-place” orders or institutional isolation of mild cases - are needed to slow spread, when will we know this? What epidemiological and demographic features impact the timescale for epidemic waning, and how can we better predict the required duration of these measures for future outbreaks?

Social distancing measures reduce potentially-transmissive contacts occurring in schools, workplaces, social settings, or casual encounters, but they generally do so by confining individuals to their households without additional precautions. Thus, we would expect that the impact of social distancing measures might depend on the relative contribution of within-household transmission to disease spread, the distribution of household sizes, the number of households containing at least one infected individual at the time an isolation measure is enacted, and the amount of residual contact between households for the duration of the intervention. What do we know about these factors for COVID-19 or respiratory infections more generally, and how do they interact to determine epidemic dynamics after an intervention?

In this paper we examine the impact of COVID-19 clinical features and transmission network structure on the timing of the epidemic peak and subsequent dynamics under social distancing interventions. Using data from large-scale cohort studies, we parameterize a model tracking the progression of COVID-19 infection through different clinical stages. We combine this with data-driven transmission networks that explicitly consider household vs external contacts and how they are differentially altered by social distancing measures. We consider various scenarios for the efficacy of interventions in reducing contacts, heterogeneities in their adoption in different demographic groups, the relative role of transmission in different settings, and the timing of partial or complete relaxation of isolation measures. We evaluate both population-level outcomes as well as determinants of individual risk of infection. Our results show that even following the implementation of strong social distancing measures, the epidemic peak can occur weeks to months later, and the decline in cases can be extremely slow. The efficacy of within-household transmission plays a critical role in the timescale and overall impact of these measures. These findings provide an impetus for continued adherence to social distancing measures in the absence of immediate results, can inform planning for hospital capacity, and suggest that retrospective efforts to assess the efficacy of different intervention policies should account for these expected delays.

Results

Observed COVID-19 dynamics following social distancing interventions

To characterize the dynamics of COVID-19 following social distancing measures, we chose five regions from around the world with large outbreaks: the city of Wuhan, China, the Lombardy region of Italy, the Community of Madrid in Spain, New York City in the state of New York, USA, and the county of Los Angeles, California, USA (Figure 1). These regions each implemented strong “lockdown” measures (aka “stay-at-home” or “shelter-in-place” orders) within 3 weeks of their first COVID-19 case and provided data not just on cases and deaths but also on cases requiring hospitalization and ICU-level care (see Methods). In each setting, there was a long
delay between the implementation of social distancing and the peak incidence of cases (1.5-3 weeks) and deaths (2-3 weeks), or peak occupancy in hospitals and ICUs (~1 month). The timescale of the eventual decline in cases post-peak was much slower than the initial increase in cases in all regions, with a half-life between 10 and 24 days in all regions except Los Angeles, where the outbreak appears to have approximately plateaued but not yet begun decreasing. The goal of this paper was to understand the factors driving these post-intervention dynamics.

Figure 1: COVID-19 dynamics before and after lockdown interventions in five example regions. A) The city of Wuhan, China (8.5K km², 11.1M ppl), B) The Lombardy region of Italy (23.8K km², 10.1M ppl) C) The autonomous Community of Madrid in Spain (8.0K km², 6.6M ppl) D) New York City in the state of New York, USA (1.2K km², 8.2M ppl). E) The county of Los Angeles, California, USA (4.7K km², 9.8M ppl). “New cases” and “New deaths” are daily numbers of new reports, averaged over a 7 day window centered on the current day. For Lombardy, New York, and Los Angeles, “Hospitalized” and “ICU” are the total number of patients currently in regular hospital care or critical care, respectively. In Wuhan, the same time series are the number of patients currently categorized as having “severe” or “critical” infection (using the same definitions as in our model). In Madrid, due to data availability, these series are instead the daily number of new admissions (with 7-day smoothing).

**Modeling the spread and clinical progression of COVID-19**

We modified the classic SEIR compartmental epidemiological model to describe the dynamics of COVID-19 infection (Figure 2A). After infection, individuals pass through an ~ 5 day incubation period before developing asymptomatic or mild infection, which could include fever and cough or other symptoms. This stage lasts ~ 1 week and individuals are infectious for this duration. A portion of individuals progress to “severe infection”, which is typically characterized by pneumonia requiring hospitalization, and we assume averages 6 days. Some individuals progress further to “critical infection”, which requires ICU-level care that often includes mechanical ventilation, and some of these individuals eventually die (after ~ 8 days of critical
care), leading to an ~2% case fatality risk. At each stage, individuals who don’t progress or die, recover and are assumed to be immune for the duration of the outbreak. The duration of each stage of infection is assumed to be gamma-distributed with mean and variance taken from the literature. Infectious individuals can transmit to any susceptible individuals with whom they are in contact, with a constant rate per time for the duration of their infection. With our baseline parameters, the doubling time of infection is ~ 4 days, the basic reproductive ratio $R_0$ is ~3, and the serial interval is ~7 days, in agreement with epidemiological studies of COVID-19. A detailed description of the clinical definitions of different infection stages, the model behavior, and the model parameters is given in the Methods.

We then simulate infection spreading stochastically through a fixed, weighted contact network. As a baseline scenario, we consider a simple approximately well-mixed population where anyone can potentially transmit the virus to anyone else in the population. To more accurately capture human contact patterns, and how they are altered by social distancing measures, we constructed a two-layer network describing connections within households and external connections (Figure 3A). Each individual was assigned to a household and connected to everyone in their house. Household size distributions were taken from the 2010 United States census (average household size $n_{HH}$~2.5, full distribution shown in Figure 3B). External connections were constructed by randomly connecting individuals to people in other households. The distribution of the number of external connections was taken from detailed contact surveys that recorded daily interactions amenable to transmission of respiratory infections (average $n_{EX}$~7.5, standard deviation 2.5) [12,13]. While these sources inform the number of contacts, the probability of infection depends both on the number of unique contacts and on the time spent together and the intensity of the contact, which can be represented by weights in the network. We hypothesized that household and external contacts could have different effective weights. For example, individuals may spend 8-10 hours a day with coworkers or classmates, but only a few waking hours with household members, and so external contact could have higher weights. Alternatively, individuals may have more intense physical contact with household members, such as children or spouses with whom co-sleeping can occur. Since these weights are unknown, we considered a range of scenarios for the relative weights of household ($w_{HH}$) and external ($w_{EX}$) contacts, keeping the total transmission intensity (basic reproductive ratio $R_0$) constant. We also hypothesized that when individuals are isolated in their homes as a result of social distancing measures (e.g. school closures or work-from-home mandates), they may be spending significantly more time with household members and thus have a higher transmission rate. We modeled this by allowing the weight of household contacts to increase during an intervention.

We model the implementation of social distancing measures by reducing the weight of all external contacts (or all contacts in the well-mixed model) by a fixed % that we term the “intervention efficacy”. Alternatively, we could randomly remove a fixed % of contacts, but the results are very similar. Our model is similar to other models that have been used to describe the spread of COVID-19. A unique feature of our model is that it simultaneously captures the clinical progression of COVID-19 (as opposed to simpler SEIR models), a reasonable approximation of contact network structure (as opposed to well-mixed models), and realistic
distributions of the durations of states (as opposed to continuous-transition models which assume exponentially-distributed durations, and lead to unrealistically long tails in infection after strong interventions). We can simulate infections for the duration of the epidemic in less than 1 minute, in populations of a million, chosen to represent a typical metropolitan area.

**Prolonged clinical progression of COVID-19 leads to delay until decline in cases and deaths following an intervention**

We first considered the role of the clinical features of COVID-19 alone, in the delay from implementation to peak infections and deaths, by simulating our model in an unstructured population. The intervention was implemented when cumulative reported cases were ~200 per million and deaths ~5 per million (total infected ~1%), mirroring the timing of stay-at-home orders across major US metropolitan areas (see Methods). While we expect the number of new infections to begin decreasing immediately, newly infected individuals in the “exposed class (E)” (incubation period) cannot generally be tracked, since they are asymptomatic and not yet shedding enough virus to test positive. Instead, later stages of infection are monitored.

We found that under a perfect intervention, we expect ~2 days delay until the peak prevalence of mild infections, ~9 days for severe infections, and ~15 days for critical infections, suggesting that the requirements for healthcare capacity may peak quite a bit after implementation (Figure 2). In the more realistic scenario where the intervention is imperfect (70% effective), these timelines are significantly extended, for example to ~7, 17, and 30 days for mild, severe, and critical infections respectively. In most regions, individuals are reported at the time of diagnosis, and not tracked until recovery, and so case counts can only be used to track incidence rates, not prevalence levels. We consider a region where infections are only counted upon hospitalization (progression to severe class), and then find that peak incidence of cases occurs 7 and 11 days after an intervention that is 100% or 70% effective. Daily deaths peak much later: after 18 days (100% effective) to 35 days (70% effective). Under our parameter values, a 50% intervention “flattens the curve” but does not prevent spread, and incidence cases and deaths don’t peak until 13 and 15 weeks after the intervention, respectively. The total percent of the population infected over the course of the whole epidemic was reduced from ~92% to ~0.6% with a 100% effective intervention, but only to 58%, 3%, or 0.65% with a 50, 70% or 90% effective intervention.

The exact timings that we report here depend on the assumptions of our model, in particular, the average duration of each stage of infection (see Methods for details) as well as on the epidemic growth rate pre-intervention. However, the qualitative finding that peaks in case counts, hospitalizations, and deaths can be significantly delayed beyond when an intervention is implemented is a general finding for models tracking the natural history of COVID-19. Note that in our model, we assume that the intervention is adopted the same day it is instituted, whereas in reality, there may be a further delay until individuals are able to comply with the intervention.
Figure 2: Dynamics pre and post social distancing intervention in well-mixed populations. A) Model of COVID-19 clinical progression and transmission. The model is described in the text and detailed in the Methods. Social distancing interventions (red X) reduce the rate of transmission and the generation of new infections. The intervention was implemented on day 40. Solid line is mean and shaded areas are 5th and 95th percentile. Black dotted line shows the time the intervention began. B-E) Simulated time course of each clinical stage of infection under different intervention efficacies. The first three quantities are peak prevalence levels ($I_1$, $I_2$, $I_3$), while the latter two are peak daily incidence values. We assume that cases are diagnosed only at the time of hospitalization. Daily incidence values are moving averages using a 7 day window centered on the date of interest. Bars represent 5th and 95th percentile.

The relative contribution of household and external spread influences outcome of interventions

We hypothesized that the continual spread of COVID-19 within households after the implementation of social distancing measures could further delay peak cases and deaths, and increase the number of people infected despite the intervention. Using our network-structured model (see Methods) for household and external contacts, we simulated the implementation of interventions of increasing efficacy under different assumptions about the relative weight of the household vs external contacts. In addition, we examined the impact that the increased time spent with household members (and hence an increased transmission potential) after stay-at-
home policies begin could have on the outcome of an intervention and the timescale for disease elimination (Figure 3).

With our baseline assumption that household and external contacts had equal weight, we observed that cases declined rapidly under very strong interventions (Figures 3E and H), while imperfect interventions (e.g. ~80%) often resulted in very gradual decreases in cases over many months (Figure 3F). In both scenarios the eventual fraction of the population infected was dramatically reduced compared to the no intervention case, but these long timescales likely mean that costly social distancing policies cannot be maintained long enough for suppression of the epidemic to occur. This slow decline could be further compromised if the risk of transmission within a household increases under stay-at-home policies (Figure 3I). In this case the epidemic could continue to increase for months post-intervention before eventually declining, albeit still to a much lower final size than in the absence of interventions.

When the outcome of an intervention was measured by the total fraction of the population infected over the course of the outbreak, we found that there was a surprisingly complex relationship between the relative contribution of household and external contacts to transmission, and the intervention success (Figures 3G and J). Keeping the total $R_0$ constant, social distancing interventions are most effective when either external contacts have very high weights or when they have very low weights. In the former case (high external weight + low household weight), most of the pre-intervention transmission comes from outside the household, and the intervention is very effective at blocking this transmission (Figure 3K). At the time the intervention is implemented, many households are “seeded” with infections that originated outside the house (Figure 3L), but after the intervention, household transmission alone is not effective enough to lead to a new generation of infections in most houses, without seeding from the outside (i.e intervention efficacy <100%). When external contacts have low weight, the intervention is highly effective but for a different reason. Most transmission is inside the household and can continue post-intervention (Figure 3K), but very few households are seeded with infections (Figure 3L). The weak inter-household contacts are further weakened by the intervention and spillover between households is unlikely, meaning that the infection quickly burns through susceptibles within a household then dies out.

In the intermediate regime, where household and external contacts have approximately equal weight, social distancing interventions are less effective, and are very sensitive to imperfect efficacy. For example, when external contacts have ~1/3 the weight of household ones, each type of contact contributes equally to the overall pre-intervention $R_0$ (since there are ~3x the number of external contacts as household ones). With a 100% effective intervention, the final epidemic size is ~0.7%, but rises to ~7% with a 80% effective intervention (Figure 3G). The combination of enough household spread ($R_0^{HH} > 1$) to allow efficient transmission post-intervention within “seeded” households and enough external spread ($R_0^{EX} > 1$) to seed households before the intervention is implemented to allow post-intervention spillover of infections to other households is the most difficult case for control. These effects are exacerbated if we assume household transmission rates (contact weights) can increase post-
intervention (Figure 3J). For an 80% effective intervention, the final epidemic size can be 5-10-fold higher than expected due to increased chance of within-household transmission.

Figure 3. Dynamics pre and post social distancing interventions in network-structured populations with household and external transmission. A) Multi-layer network of transmission. Individuals have contacts within their households and with others outside the household. Household and external contacts may have different weights (e.g. different likelihood of transmission), due to for example different levels of physical contact or time spent together per day. Social distancing interventions (red X) remove or decrease the weight of external contacts. B) Distribution of household sizes. C) Distribution of the # of contacts (degree) within the household. D) Distribution of the # of contacts outside the household. E-F) Simulated time course of different clinical stages of infection under an intervention with efficacy of 100% (E) or 80% (F) at reducing external contacts, when household and external contacts have equal weight. Black dotted line shows the time the intervention began. G) The role of the relative importance of household vs external contacts in determining the outcome of the intervention, measured by the size of the epidemic. Epidemic final size is defined as the percent of the population who have recovered by day 300. H-J) Same as above but under the scenario where the weight of household contacts doubles post-intervention ($w_{HH} \rightarrow 2w_{HH}$, due to increased time spent in house). K) The contribution of household and external spread to the total $R_0$ value as a function of the relative weight of external contacts. L) The percent of households which are “seeded” with infection at the time the intervention was implemented (i.e. have at least one infected individual). In all scenarios the overall infection prevalence at the time intervention was started was identical.
**Residual household transmission can further delay time to see the impact of an intervention**

We found that the expected time to peak infections and deaths after a social distancing intervention was implemented could be increased dramatically when we accounted for household structure, and was sensitive to the relative importance of household and external contacts before and after the intervention (**Figure 4**). Under a 100% effective intervention (**Figure 4A**), the delays to peaks were driven mainly by the clinical progression alone, similar to the case of the well-mixed population, but were slightly extended due to residual spread restricted to a single household. In simulations it took around 2 weeks until peak hospitalizations and 3 weeks to peak critical care cases or daily deaths. However, under an imperfect but still strong intervention (e.g. 80% effective), the times to peak were much longer and sensitive to the relative weights of the external and household contacts (**Figure 4B**). Delay to peak cases was longest in the intermediate regime where external and household contribution to transmission was approximately equal. For example, when external and household weights were equal, it took an average of ~5.5 weeks to reach peak cases with mild symptoms, ~7 weeks until peak cases hospitalized with severe infection, and ~8.5 weeks to the peak of cases in critical care.

The daily incidence of new deaths didn’t peak for ~10 weeks.

The delays in time to peak were less extreme if external contacts had very high or very low weights relative to the weight of household contacts (**Figure 4B**). In the case of very high external weight, most individuals were infected from contacts outside their household before the intervention (**Figure 3L**). Household spread is relatively inefficient, and has only a minor contribution to the baseline $R_0$ value (**Figure 3K**). In most households, there is no further spread after the intervention is implemented. As a result, the epidemic peaked sooner: peak daily deaths occurred an average of ~3 weeks post 100% effective intervention and ~5 weeks post 80% effective intervention. On the other hand, when external weight is a lot lower as compared to the household, only a small fraction of households are seeded with infection by the time intervention is started (**Figure 3L**). Intervention is very effective at suppressing external transmission and so, even though household transmission continues during intervention it cannot spill over between households. This causes the epidemic to peak sooner as susceptibles in households get infected quickly and then the infection dies out. On average, peak daily deaths occurred ~3 weeks (100% effective intervention) and ~4 weeks (80% effective intervention) post intervention.

These results were exacerbated if we assumed that the importance of household contacts increased post-intervention (**Figure 4C**), due to increased time spent in close quarters. In that case, peaks increased to up to ~6 months for cases in critical care and daily deaths under an 80% intervention. With higher household weights, the efficacy of spread within a household was stronger, making new generations of infection post-intervention very likely to occur in households with at least one case. Then, these household infections are more likely to spill over into other households, even when most external contacts are eliminated by the intervention. Together, these effects allow for multiple generations of transmission to persist even after a strong intervention.
Figure 4: Time to epidemic peak after social distancing interventions depends on the relative roles of household and external transmission. A-C) Time to peak of different infection stages, measured as days post-intervention. A) Social distancing intervention with 100% efficacy at reducing external contacts (or all contacts in the case of a well-mixed network). B) Social distancing intervention with 80% efficacy. C) Social distancing intervention with 80% efficacy, and assuming that household weights double post-intervention ($w_{HH} \rightarrow 2w_{HH}$, due to increased time spent in the home). The first three quantities are peak prevalence levels ($I_1$, $I_2$, $I_3$), while the latter two are daily incidence values. We assume that cases are diagnosed only at the time of hospitalization. Daily incidence values are moving averages using a 7 day window centered on the date of interest. Bars represent 5th and 95th percentile. For each clinical stage included (each different color), the lighter-colored data point is the comparison to the well-mixed population, then the other points are for decreasing contributions of external connections and increasing role of household transmission.

Clustered adoption of social distancing measures can further compromise efficacy

Our results so far have assumed that external contacts in the transmission network are random connections between pairs of individuals in the population, and that a social distancing intervention results in a uniform random reduction or deletion of these connections. In reality, human contact networks tend to be highly structured, with groups of individuals with high levels of interconnectedness and large variation between individuals in total contacts (e.g. [14,15]). Moreover, we don’t necessarily expect adherence to social distancing measures to be random. For certain occupations or in certain demographic groups, individuals are less likely to be able to work-from-home or otherwise reduce contacts outside the home. This can lead to clusters of individuals among whom contacts remain high despite interventions. We hypothesized that this clustered adoption of social distancing measures could lead to more residual transmission, longer times to peak cases and deaths, and longer times to eradicate infection from a given region.

To examine these effects, we constructed more realistically-structured, age-segregated external contact networks. The population was divided into four broad age groups: preschool-aged, school-aged, working-aged and elderly. Based on large-scale contact surveys and other
modeling studies [12,13,15–17], we broke down external contacts into four different layers - school, work, social and community (Figure 5A). Age groups determined network membership. School and work layers consisted of connections between individuals only belonging to the school-aged and working-aged groups respectively. Individuals belonging to all age groups were part of the social and community layers. We used a variety of data sources to construct the networks for each layer with degree distributions (both mean and variance in # of contacts) as well as levels of clustering (aka transitivity, a measure of interconnectedness) that matched data (see Methods). We assumed that during a social distancing measure, school contacts were completely removed, and that work, social, and other contacts were reduced by an amount equal to the intervention efficacy. For work contacts, we also considered the case where edges weren’t removed at random, but instead, certain “workplaces” were completely dissolved, whereas others remained (Figure 5C, top). With this implementation, the levels of clustering in the external network was high both before and after an intervention. Other studies have shown that such clustered adoption of preventive behavior can lead to lower than expected efficacy of vaccines and mass drug administration [18–21].

Interestingly, we did not find that most intervention outcomes were worse under this clustered adoption. Time to peak cases, hospitalizations and deaths were similar under random deletion of edges (Figure 5B, bottom) and under the correlated deletion scheme (Figure 5C, bottom). However, we found that the time until infection was eliminated from the population was much longer: increasing from ~ 180 days to ~ 220 days for population sizes of a million. Targeting demographic groups - where pockets of infection persist - with more aggressive cases-based measures and contact tracing may be necessary to reach elimination goals faster.

Figure 5: Clustered vs uniform adoption of social distancing measures. A) Schematic of the multi-layer network created to more realistically capture non-household contacts and how they are altered by social distancing measures. In each layer, the degree distribution and level of clustering were chosen to match data. The “community” layer represents any other contact not fitting in the other four categories. Colors of nodes represent four broad age groups that determine network membership and structure: preschool-aged (pink), school-aged (purple), working-aged (blue) and elderly (green). B) - C) Simulated time courses of infection in the presence of social distancing intervention with random (B) vs clustered (C)
adherence to measures. In both cases, all school connections were deleted post-intervention and 85% of connections were uniformly deleted at random in the social and community layers. In B) 85% of work connections were uniformly deleted whereas, in C) 85% of workplaces were dissolved, leading to clusters of disconnected vs connected individuals in the work layer of the network. The effective intervention efficacy for all layers combined was ~ 88% in both scenarios. Black dotted line shows the time the intervention began.

**Individual risk of infection depends on household size and occupation**

So far our evaluations of social distancing measures have focused on population-level outcomes such as the timing of the epidemic peak and the overall fraction of the population infected. However, these findings mask significant heterogeneity in individual risk. From our simulations, we extracted the individual probability of infection as a function of household size (Figure 6A), as well as in relation to the external contacts maintained after an intervention (Figure 6B). We found that the risk of infection increased dramatically with the household size: with our baseline parameters, it ranged from <0.2% for individuals living alone to 5.4% for households of size 7 (Figure 6A). These differences occurred independently of the relative weight of household vs external contacts. The supra-linear increase in risk with household size is driven by the fact that in larger households there is both more risk of seeding of infection from outside, as well as more individuals to spread to within the household leading to less chance of extinction of spread.

We also examined the increased risk faced by “essential workers”, or others who maintained contacts in their “work” networks during the time social distancing measures were in place (Figure 6B). Under more extreme distancing (~85% reduction in contacts), the relative risk of infection among workers relative to the population average was 1.6, while for individuals not working themselves but living in the same household as someone who was working was 1.4. In comparison, individuals belonging to households with no workers had a relative risk of 0.8. For a less effective intervention (~70%), these values were 1.6, 1.3 and 0.7 respectively. These findings highlight the risk faced by communities in which larger households are common and/or in which more individuals per household may maintain external connections despite social distancing measures.
Figure 6: Individual risk of infection depends on household size and worker status. A) Risk of infection versus household size in simulations. Risk of infection was calculated after 300 days. Bar colors represent different relative weights of external contacts (compared to household contacts). Dotted lines are the population level average infection levels for the same scenarios. B) Risk of infection versus worker status. A “worker” is defined as someone with an occupation in which they continue to work outside the home despite social distancing measures. Categories include being a worker yourself (red), living in a household with at least one other individual who is working (orange), or having no workers in the house (yellow). As a comparison the population average risk is shown (dotted line). Interventions that reduce the overall number of people working outside the home by 70% and 85% are shown (in all cases all schools are assumed to be closed and the same percent of social and community contacts are removed).

Expanding circles can be safe partial relaxation strategies only under certain conditions

As a step towards relaxing social distancing measures in settings where the incidence of cases and deaths has stabilized or is declining, some regions are proposing partial relaxation strategies whereby groups of households merge to form larger “expanded circles” or “bubbles”, but still minimize external contacts [22,23]. Such multi-household groups could have enormous social benefits, such as providing childcare relief and improving productivity of working parents, and reducing the mental health toll of social isolation. To examine when this strategy could be safely implemented without risking a rebound in cases, we randomly joined households 1, 2, or 3 months after the implementation of a strong social distancing measure (80 or 90% effective) (Figure 7).

We found that these household-merging strategies could be safe only if a few criteria were met. Firstly, they must be applied in the context of steadily declining cases and deaths (Figures 7B and D). In situations where infection levels had stabilized but were barely declining, forming bubbles always led to at least some resurgence of cases which returned to or exceeded peak levels (Figures 7A and C). Secondly, household bubble formation should ideally be accompanied by a further decrease in contacts outside the house (for example, only one
grocery trip per dual-family household instead of two) and a redistribution of the effective number of household contacts instead of allowing them to double (for example, by spending time with subsets of the dual household instead of all time as a complete group). Otherwise, a previously declining epidemic could instead stabilize at a persistent level (Figure 7B), or an otherwise stable epidemic could temporarily resurge (Figure 7A). We did not find a strong dependence on the timing of household bubble formation.

Clearly households with less external contacts would be at the least risk from merging with others, and these policies should only be encouraged in regions where general social distancing has clearly reduced the prevalence of infection. Similar to our findings in earlier sections, our predictions are more optimistic when household and external contacts contribute less equally to transmission.

**Figure 7: Effect of partially relaxing intervention by forming household bubbles.** Some time after a social distancing intervention was implemented, each household merges with another random household. In each resulting two-household “bubble”, all individuals are connected to all other individuals. A)-D) Simulated time courses of infection before and after social distancing interventions (with 80% vs 90% intervention efficacy) and after partial-relaxation by household merging. Top row: External contacts of individuals were unchanged after two households were merged, such that overall number of contacts increased. Bottom row: External contacts for individuals were reduced after two households were merged, such that overall number of contacts remained unchanged. In all cases, intervention was started 43 days after the onset of the epidemic (first black dotted line) and was relaxed after two months (60 days, second black dotted line).

**Discussion**

In this paper we show that the clinical and epidemiological features of COVID-19 interact to produce long expected delays between the implementation of a strong intervention to prevent
transmission and when its effects become apparent. Part of the delay is clinical. After infection, individuals pass through an asymptomatic incubation period before entering a phase of mild flu-like symptoms, and some fraction then require hospitalization. Documented deaths often occur after extended stays in critical care wards. The progression from initial infection to a reportable case (often at hospital admission) or death can be weeks, and is not interrupted by current interventions. In addition, social distancing measures reduce transmission outside the household, but in general they involve isolating individuals within their normal places of residence and thus do not prevent household transmission. They may in fact amplify it, by increasing the time household members spend together. If even a small fraction of households have been “seeded” with infection at the time an intervention is implemented, cases may continue to increase for multiple serial intervals. This residual transmission is exacerbated if weak inter-household connections remain, and especially if there are clusters of individuals less able to comply with social distancing measures, for example among communities with a high prevalence of “essential workers”.

Our results show that it is very difficult for interventions which only target transmission outside the house to effectively control the outbreak. Unless these interventions reduce the vast majority of contacts, ongoing transmission in households combined with occasional spillover to other households means that the epidemic may continue to increase long after social distancing begins and when it turns around, declines in cases can be extremely slow. We found that the relative contribution of household and external contacts to transmission was a critical determinant of the overall outcome of social distancing interventions, and the timescale over which effects could be observed. The number of contacts alone was not very informative for predicting intervention efficacy. It is not possible to predict the effect of an intervention that differentially affects household and external contacts by simply estimating the proportional reduction in the total $R_0$. For example, even if the component of $R_0$ from household transmission alone is greater than 1, infection cannot continue if external connections are substantially weakened. These findings highlight the need for more studies to determine the contribution of different types of contacts to transmission.

The role of household transmission in the spread of COVID-19 is still not clear. Several studies with detailed contact tracing have attempted to estimate the household “secondary attack rate”, i.e. the probability of transmission per susceptible household member when there is a single infected individual in the house. In a large study in Shenzhen, China, Bi et al estimated this rate at 11% [24]. In Guangzhou, China the estimate was 20% [25], in Beijing 23% [26], in Seoul, South Korea 16% [27] and in Taiwan, around 5% [28]. In a small German town with a large outbreak due to a superspreading event at a carnival, the household secondary attack rate was closer to 30% but decreased in larger households [29]. Liu et al considered a collection of known clusters involving close contacts in a single gathering (not just household, often group meals), and estimated a 35% secondary attack rate. Recently, a review by Curmei et al [30] attempted to collect all these estimates and correct them upwards by accounting for false negative rates of diagnostic tests and for asymptomatic infections. They reported estimates between 10-60%, with generally higher values in the US and Europe and lower values in Asia. Given that the average household size is relatively small in all these countries (~3 or less),
these numbers suggest that infection from outside the house must play a large role in order to explain the overall $R_0$ values observed. Many more studies have examined the role of household transmission in influenza spread, but the results are also equivocal: a review by Tsang et al found that household secondary attack rates varied from 1-40% across studies [31]. A massive cohort study from Japan recently shone some light on this complexity; finding that the risk of household influenza transmission was highly dependent on household structure and on the familial relationship between the primary and secondary case [32]. They also found that the relative role of external vs household spread was highly age-dependent, children were much more likely to be infected outside the home (~80% of risk), while for adults infection within the home dominated (50% or more).

The networks we use to simulate infection were parameterized based on detailed surveys that used “contact diaries” to track the number of individuals someone interacted with on a randomly chosen day [12,13]. Contacts were generally defined as physical contact or face-to-face conversations, and were meant to capture interactions thought to be important for the spread of droplet-borne respiratory infections like influenza and coronaviruses. The data that is easily accessible from these studies is the average number of daily contacts by age of each individual in the pair. However, these surveys also collected information on the duration, frequency, and physical nature of contacts, all of which could help inform estimation of the relative weights of different types of contacts, if it were made accessible. One limitation of these sorts of surveys is that they are “ego-centric”, meaning that they only inform the distribution of the number of contacts but not the higher order network structure, which can be important for infection spread [16,33]. When we constructed our multi-layer network of external contacts, we used additional information from other studies to include clustering and modularity in our networks. Another limitation is that certain contacts that might be relevant to respiratory infections may be missed in surveys. For example, transmission via contaminated surfaces can occur between individuals who have never directly interacted, as can transmission in group settings where air is shared (e.g. in fitness classes [34] or at restaurants [35]).

There are multiple strategies to augment social distancing policies by reducing household spread, and these have been implemented to different degrees in different countries. We have not considered such combination policies in our analysis, but other models have explored them in detail. Household spread would be reduced by earlier diagnoses of cases (as soon as symptoms begin), proactive testing of exposed household members of cases, options for out-of-home care for individuals with mild symptoms, or better education and assistance with individuals caring for sick household members to avoid infection, for example via household use of face masks and disinfectants [26]. Population-level contact tracing initiatives would obviously also help [36,37]. Early and influential modeling studies that provided the impetus for widespread social distancing policies around the world assumed these policies would be accompanied by case-based interventions that would reduce household spread (e.g. [8,38]), but these measures have not been uniformly adopted, and are still completely absent in most of the United States.
Clearly a major determinant of the efficacy of social distancing policies for COVID-19 is the fractional reduction in contacts, but quantifying this value is difficult. A variety of data sources can provide some information. Surveys conducted in Wuhan and Shanghai, China comparing contacts before and after COVID-19 lockdowns found that the average number of daily contacts was reduced from ~14 in Wuhan and ~20 in Shanghai to ~2, suggesting a more than ~95% reduction in external contacts [39]. In the US, nationally-representative polls by Gallup found that around three quarters of households were self-isolating [40], and estimated a median reduction in contacts between 80-95% for non-workers [41]. Since contact surveys are rare, measures of reductions in human mobility have been used as a proxy for contact rate reductions. Google [42] and Apple [43] provide reports on mobility changes based on user locations sourced from their smartphone mapping apps, as does Cuebeq [44]. Transit, a live-tracking and schedule-aggregating application for public transit, reports changes in service use [45], and SafeGraph publishes changes in foot traffic to different classes of locations [46].

Different measures of mobility often give very different estimates for the efficacy of social distancing interventions. For example, Klein et al found peak US national average reductions in both the radius of mobility and the number of events where device users came within near proximity of each other were about ~50%, whereas communing volume was reduced by ~75% [47,48]. For the same time period, Apple reported ~50% reductions in direction requests, Transit reported ~70% reduction in transit use, Google reported ~40% reductions in visits to retail locations and ~50% in visits to workplaces, and SafeGraph reported an ~80% reduction in foot traffic at bars but only a 20% reduction to grocery stores. Together these results suggest that our simulations assuming ~80% reduction in external contacts - which still often only results in mediocre outcomes - are likely overestimates, if anything, of reality. Wellenius et al attempted to infer the association between these mobility reductions and the particular social distancing policies that caused them. Using Google data they concluded that in the US, initial emergency declarations lead to ~10% reductions, that each additional policy led to another ~20% reduction, and that “shelter-in-place” orders resulted in additional ~30% reductions [49]. By comparing mobility changes to estimates of $R_0$ from case counts in countries around the world, Bergman et al estimated that each ~10% reduction in mobility resulted in an ~0.05 reduction in $R_0$ [50]. Interestingly, they also found two other results in agreement with our findings here: there was a long delay between reductions in mobility and reductions in inferred $R_0$ in many regions, and, the association between reductions in mobility and $R_0$ was weaker in regions who implemented large scale contact tracing, which likely reduces household transmission.

Our results highlight the importance of residual contacts between households that remain despite social distancing measures. Many of these contacts are likely to be driven by individuals who must continue to work. Our own analysis of occupations held by residents of Philadelphia, USA, population ~1.5 million, suggested that ~30% of workers had jobs that fell into categories flagged as “essential”. A review by Lan et al of case reports within the first month of the outbreak in multiple countries found that about 15% of these cases were clearly work-related, and that even earlier in the outbreak, this was as high as 50% [51]. A report released by the UK Office of National Statistics found COVID-19 related deaths were much higher in certain occupational groups (e.g. relative risk of 4.5 for male security guards and 2 for...
female care workers), and the UK Biobank found an 8x higher rate of COVID-19 diagnoses in healthcare workers compared to the general population. Major clusters of infection have occurred in workplaces as varied as call centers [27] and meatpacking plants [52]. Given the limited apparent ability to reduce workplace contacts and transmission, reducing household transmission or other external contacts may be even more important. Another strategy we have not considered is selective restructuring of contact networks to increase clustering and decrease mean path length, so that transmission risk is minimized without further reducing contacts [53].

Separate assumptions of our modeling approach could lead our predictions to be slightly pessimistic. We assume a baseline value of $R_0 \approx 3$, whereas some other studies have used values between 1.9 - 2.7 [1–3,37,54]. There are several reasons why we believe those estimates are likely a little too low. Firstly, they tended to assume very short serial intervals and infectious periods, whereas other studies have estimated longer serial intervals [24,55,56], particularly in the absence of quick isolation of mild cases, which is more likely to reflect what is going on in most of the world outside of east Asia. Secondly, those estimates often fit to cases counts that were doubling every 5-6 days, whereas in many settings doubling times were closer to 3 days early in the outbreak [57–60]. Finally, nearly all previous estimates of $R_0$ fit a randomly-mixing population (with or without age structure), whereas in our highly structured network population, higher $R_0$ values are needed to achieve the same doubling time. $R_0$ values as high as 3-6 have been estimated using rigorous epidemiological methods [6,38]. With lower $R_0$ values, any estimates of the % reduction in external contacts needed to achieve a certain rate of reduction of cases and deaths would be reduced. However, our main qualitative results about delays to epidemic peak and the complex role of household transmission hold.

Our results are not sensitive to our assumptions about the fraction of cases that progress to more serious clinical stages nor to the case fatality risk. However, our estimates for the timing of peak values do depend on the distribution of delays we assume, for example between symptom onset and hospitalization, or between ICU admission and death. There is variability in the estimates of these values across studies (see Methods), and these values likely differ by country, depending on the standard of care and the underlying health of the population. While we have considered wide intervals for the interpatient variation in these durations, we have not propagated uncertainty in the distribution of these values. We hope that by providing our code, researchers who are interested in specific contexts where these values may differ significantly can explore those scenarios. There are other factors which influence the delay between implementation of social distancing measures and peak cases and deaths that we have not included in our model. One factor is reporting delays, which may be especially long for deaths in certain regions. Another factor is that there could be a delay between implementation of distancing measures and adoption by a majority of the population.

By including more details of transmission network structure, we are able to examine effects that would not be apparent in well-mixed epidemic models. However, our population structure is still simplistic in many senses. For example, we do not explicitly model the dynamics of certain institutions that have been particularly hard-hit by COVID-19, such as retirement homes and long-term care facilities, prisons, and meat-packing plants. Understanding the unique contact
networks, transmission risks, host susceptibility, and mortality risks in these populations is an important area for future research. We also do not consider the potential for hospital-acquired transmission and the role of healthcare workers. Doctors, nurses, and other health professionals are reported to make up 5-10% of cases in some regions, and while increased testing is likely one factor driving these rates, it is clear that there are also unique risks to this profession.

Many studies are now attempting to estimate the degree to which different social distancing measures (e.g. school closures, stay-at-home policies) reduce the reproductive ratio or the exponential growth rate of cases. Our results point out a few challenges to these efforts. The long delays we describe in this paper mean that methods that fit simple growth functions to data and look for changes in their values may have trouble identifying effects. If there are a series of interventions that tend to be implemented in similar orders or at similar intervals across settings, and the goal is to estimate the effect of each (e.g. [8,61]), then the delays we describe here could lead to falsely attributing the effect of one intervention to another that occurs later (e.g. see [5] and comments in response). Some of these problems can be avoided by explicit use of mathematical models that take into account the prolonged clinical progression of COVID-19 (e.g. [9,62]), which is the first order cause of these delays. However, our results show that transmission network structure also plays an important role. Importantly, the amount by which overall transmission is reduced by social distancing measures and the delay until effects are seen depends on the relative role of household vs external transmission, which is unknown and may be different by setting.
References

1. Ferguson NM, Laydon D, Nedjati-Gilani G, Imai N, Ainslie K, Baguelin M, et al. Impact of non-pharmaceutical interventions (NPIs) to reduce COVID-19 mortality and healthcare demand. 2020; 20.
2. Kissler SM, Tedijanto C, Goldstein E, Grad YH, Lipsitch M. Projecting the transmission dynamics of SARS-CoV-2 through the postpandemic period. Science. 2020 [cited 16 Apr 2020]. doi:10.1126/science.abb5793
3. Davies NG, Kucharski AJ, Eggo RM, Gimma A, Group CC-19 W, Edmunds WJ. The effect of non-pharmaceutical interventions on COVID-19 cases, deaths and demand for hospital services in the UK: a modelling study. medRxiv. 2020; 2020.04.01.20049908. doi:10.1101/2020.04.01.20049908
4. Pei S, Shaman J. Initial Simulation of SARS-CoV2 Spread and Intervention Effects in the Continental US. medRxiv. 2020; 2020.03.21.20040303. doi:10.1101/2020.03.21.20040303
5. Pan A, Liu L, Wang C, Guo H, Hao X, Wang Q, et al. Association of Public Health Interventions With the Epidemiology of the COVID-19 Outbreak in Wuhan, China. JAMA. 2020 [cited 24 Apr 2020]. doi:10.1001/jama.2020.6130
6. Tian H, Liu Y, Li Y, Wu C-H, Chen B, Kraemer MUG, et al. The impact of transmission control measures during the first 50 days of the COVID-19 epidemic in China. medRxiv. 2020; 2020.01.30.20019844. doi:10.1101/2020.01.30.20019844
7. Cowling BJ, Ali ST, Ng TWY, Tsang TK, Li JCM, Fong MW, et al. Impact assessment of non-pharmaceutical interventions against coronavirus disease 2019 and influenza in Hong Kong: an observational study. Lancet Public Health. 2020;5: e279–e288. doi:10.1016/S2468-2667(20)30090-6
8. Flaxman S, Mishra S, Gandy A, Unwin HJT, Coupland H, Mellan TA, et al. Estimating the number of infections and the impact of non-pharmaceutical interventions on COVID-19 in European countries: technical description update. ArXiv200411342 Stat. 2020 [cited 8 May 2020]. Available: http://arxiv.org/abs/2004.11342
9. Prague M, Wittkop L, Clairon O, Dutartre D, Thiebaut R, Hejblum BP. Population modeling of early COVID-19 epidemic dynamics in French regions and estimation of the lockdown impact on infection rate. medRxiv. 2020; 2020.04.21.20073536. doi:10.1101/2020.04.21.20073536
10. Imperial College COVID-19 Response Team. State-level tracking of COVID-19 in the United States. Imperial College London; 2020 May. Report No.: 23. Available: http://www.imperial.ac.uk/medicine/departments/school-public-health/infectious-disease-epidemiology/mrc-global-infectious-disease-analysis/covid-19/report-23-united-states/
11. Pei S, Kandula S, Shaman J. Differential Effects of Intervention Timing on COVID-19 Spread in the United States. medRxiv. 2020; 2020.05.15.20103655. doi:10.1101/2020.05.15.20103655
12. Mossong J, Hens N, Jit M, Beutels P, Auranen K, Mikolajczyk R, et al. Social Contacts and Mixing Patterns Relevant to the Spread of Infectious Diseases. PLOS Med. 2008;5: e74. doi:10.1371/journal.pmed.0050074
13. Prem K, Cook AR, Jit M. Projecting social contact matrices in 152 countries using contact surveys and demographic data. PLOS Comput Biol. 2017;13: e1005697. doi:10.1371/journal.pcbi.1005697
14. Christakis NA, Fowler JH. The spread of obesity in a large social network over 32 years. N Engl J Med. 2007;357: 370.
15. Potter GE, Smieszek T, Sailer K. Modeling workplace contact networks: The effects of organizational structure, architecture, and reporting errors on epidemic predictions. Netw Sci Camb Univ Press. 2015;3: 298–325. doi:10.1017/nws.2015.22
16. Liu Q-H, Ajelli M, Aleta A, Merler S, Moreno Y, Vespignani A. Measurability of the epidemic reproduction number in data-driven contact networks. Proc Natl Acad Sci. 2018;115:12680–12685. doi:10.1073/pnas.1811115115

17. Wrzus C, Hänel M, Wagner J, Neyer FJ. Social network changes and life events across the life span: A meta-analysis. Psychol Bull. 2013;139:53–80. doi:10.1037/a0028601

18. Salathé M, Bonhoeffer S. The effect of opinion clustering on disease outbreaks. J R Soc Interface. 2008;5:1505.

19. Kuylen E, Willem L, Broeckhove J, Beutels P, Hens N. Clustering of susceptible individuals within households can drive measles outbreaks: an individual-based model exploration. medRxiv. 2019; 2019.12.10.19014282. doi:10.1101/2019.12.10.19014282

20. Dyson L, Stolk WA, Farrell SH, Hollingsworth TD. Measuring and modelling the effects of systematic non-adherence to mass drug administration. Epidemics. 2017;18:56–66. doi:10.1016/j.epidem.2017.02.002

21. Parker DM, Tun STT, White LJ, Kajeechiwa L, Thwin MM, Landier J, et al. Potential herd protection against Plasmodium falciparum infections conferred by mass antimalarial drug administrations. eLife. 2019;8:e41023. doi:10.7554/eLife.41023

22. Roberts M. Coronavirus bubbles: Who is in yours? BBC News. 14 May 2020. Available: https://www.bbc.com/news/health-52637354. Accessed 1 Jun 2020.

23. Coletta A. Canadian provinces allow locked-down households to pair up — threatening hurt feelings all around. Washington Post. 8 May 2020. Available: https://www.washingtonpost.com/world/the_americas/coronavirus-canada-new-brunswick-newfoundland-double-bubble/2020/05/07/78e08960-8eec-11ea-9322-a29e75effc93_story.html. Accessed 1 Jun 2020.

24. Bi Q, Wu Y, Mei S, Ye C, Zou X, Zhang Z, et al. Epidemiology and transmission of COVID-19 in 391 cases and 1286 of their close contacts in Shenzhen, China: a retrospective cohort study. Lancet Infect Dis. 2020;0. doi:10.1016/S1473-3099(20)30287-5

25. Jing Q-L, Liu M-J, Yuan J, Zhang Z-B, Zhang A-R, Dean NE, et al. Household Secondary Attack Rate of COVID-19 and Associated Determinants. medRxiv. 2020;2020.04.11.20056010. doi:10.1101/2020.04.11.20056010

26. Wang Y, Tian H, Zhang L, Zhang M, Guo D, Wu W, et al. Reduction of secondary transmission of SARS-CoV-2 in households by face mask use, disinfection and social distancing: a cohort study in Beijing, China. BMJ Glob Health. 2020;5:e002794. doi:10.1136/bmjgh-2020-002794

27. Park SY, Kim Y-M, Yi S, Lee S, Na B-J, Kim CB, et al. Coronavirus Disease Outbreak in Call Center, South Korea. Emerg Infect Dis J. 2020;26. doi:10.3201/eid2608.201274

28. Cheng H-Y, Jiao S-W, Liu D-P, Ng T-C, Huang W-T, Lin H-H. Contact Tracing Assessment of COVID-19 Transmission Dynamics in Taiwan and Risk at Different Exposure Periods Before and After Symptom Onset. JAMA Intern Med. 2020 [cited 28 May 2020]. doi:10.1001/jamainternmed.2020.2020

29. Streeck H, Schulte B, Kuemmerer B, Richter E, Hoeller T, Fuhrmann C, et al. Infection fatality rate of SARS-CoV-2 infection in a German community with a super-spreading event. medRxiv. 2020;2020.05.04.20090076. doi:10.1101/2020.05.04.20090076

30. Curmei M, Ilyas A, Evans O, Steinhardt J. Estimating Household Transmission of SARS-CoV-2. medRxiv. 2020;2020.05.23.20111559. doi:10.1101/2020.05.23.20111559

31. Tsang TK, Lau LLH, Cauchemez S, Cowling BJ. Household Transmission of Influenza Virus. Trends Microbiol. 2016;24:123–133. doi:10.1016/j.tim.2015.10.012

32. Endo A, Uchida M, Kucharski AJ, Funk S. Fine-scale family structure shapes influenza transmission risk in households: Insights from primary schools in Matsumoto city, 2014/15. PLOS Comput Biol. 2019;15:e1007589. doi:10.1371/journal.pcbi.1007589

33. Miller JC. Spread of infectious disease through clustered populations. J R Soc Interface. 2009;6:1121–1134. doi:10.1098/rsif.2008.0524
34. Jang S, Han SH, Rhee J-Y. Cluster of Coronavirus Disease Associated with Fitness Dance Classes, South Korea. Emerg Infect Dis J. 2020;26. doi:10.3201/eid2608.200633

35. Lu J, Gu J, Li K, Xu C, Su W, Lai Z, et al. COVID-19 Outbreak Associated with Air Conditioning in Restaurant, Guangzhou, China, 2020. Emerg Infect Dis J. 2020;26. doi:10.3201/eid2607.200764

36. Peak CM, Kahn R, Grad YH, Childs LM, Li R, Lipsitch M, et al. Individual quarantine versus active monitoring of contacts for the mitigation of COVID-19: a modelling study. Lancet Infect Dis. 2020;0. doi:10.1016/S1473-3099(20)30361-3

37. Ferretti L, Wymant C, Kendall M, Zhao L, Nurtay A, Abeler-Dörner L, et al. Quantifying SARS-CoV-2 transmission suggests epidemic control with digital contact tracing. Science. 2020 [cited 22 Apr 2020]. doi:10.1126/science.abb6936

38. Sanche S, Lin YT, Xu C, Romero-Severson E, Hengartner N, Ke R. High Contagiousness and Rapid Spread of Severe Acute Respiratory Syndrome Coronavirus 2. Emerg Infect Dis J. 2020;26. doi:10.3201/eid2607.200282

39. Zhang J, Litvinova M, Liang Y, Wang Y, Wang W, Zhao S, et al. Changes in contact patterns shape the dynamics of the COVID-19 outbreak in China. Science. 2020 [cited 28 May 2020]. doi:10.1126/science.abb8001

40. Gallup, Inc. Three in Four in U.S. Have Self-Isolated in Their Household. In: Gallup.com [Internet]. 8 Apr 2020 [cited 31 May 2020]. Available: https://news.gallup.com/poll/307760/three-four-self-isolated-household.aspx

41. Gallup, Inc. Americans’ Social Contacts During the COVID-19 Pandemic. In: Gallup.com [Internet]. 21 Apr 2020 [cited 31 May 2020]. Available: https://news.gallup.com/opinion/gallup/308444/americans-social-contacts-during-covid-pandemic.aspx

42. COVID-19 Community Mobility Report. In: Google [Internet]. [cited 1 Jun 2020]. Available: https://www.google.com/covid19/mobility?hl=en

43. COVID-19 - Mobility Trends Reports. In: Apple [Internet]. [cited 1 Jun 2020]. Available: https://www.apple.com/covid19/mobility

44. Kunkel C. COVID-19 Mobility Insights. In: Cuebiq [Internet]. [cited 14 Apr 2020]. Available: https://www.cuebiq.com/visitation-insights-covid19/

45. How coronavirus is disrupting public transit. In: Transit App [Internet]. [cited 1 Jun 2020]. Available: https://transitapp.com/coronavirus, https://transitapp.com/coronavirus

46. U.S. Consumer Activity During COVID-19 Pandemic. In: SafeGraph [Internet]. [cited 1 Jun 2020]. Available: https://safegraph.com/dashboard/

47. Klein B, LaRock T, McCabe S, Torres L, Privitera F, Lake B, et al. Reshaping a nation: Mobility, commuting, and contact patterns during the COVID-19 outbreak. : 17.

48. COVID-19 Mobility United States. In: Gleam Project [Internet]. [cited 1 Jun 2020]. Available: https://covid19.gleamproject.org/mobility

49. Wellenius GA, Vispute S, Espinosa V, Fabrikant A, Tsai TC, Hennessy J, et al. Impacts of State-Level Policies on Social Distancing in the United States Using Aggregated Mobility Data during the COVID-19 Pandemic. ArXiv200410172 Q-Bio. 2020 [cited 23 May 2020]. Available: http://arxiv.org/abs/2004.10172

50. Bergman NK, Fishman R. Mobility Levels and Covid-19 Transmission Rates. medRxiv. 2020; 2020.05.06.20093039. doi:10.1101/2020.05.06.20093039

51. Lan F-Y, Wei C-F, Hsu Y-T, Christiani DC, Kales SN. Work-related Covid-19 transmission. medRxiv. 2020; 2020.04.08.20058297. doi:10.1101/2020.04.08.20058297

52. Dyal JW. COVID-19 Among Workers in Meat and Poultry Processing Facilities — 19 States, April 2020. MMWR Morb Mortal Wkly Rep. 2020;69. doi:10.15585/mmwr.mm6918e3

53. Block P, Hoffman M, Raabe IJ, Dowd JB, Rahal C, Kashyap R, et al. Social network-based distancing strategies to flatten the COVID 19 curve in a post-lockdown world.
54. Wu JT, Leung K, Bushman M, Kishore N, Niehus R, de Salazar PM, et al. Estimating clinical severity of COVID-19 from the transmission dynamics in Wuhan, China. Nat Med. 2020; 1–5. doi:10.1038/s41591-020-0822-7
55. Lavezzo E, Franchin E, Ciavarella C, Cuomo-Dannenburg G, Barzon L, Vecchio CD, et al. Suppression of COVID-19 outbreak in the municipality of Vo, Italy. medRxiv. 2020; 2020.04.17.20053157. doi:10.1101/2020.04.17.20053157
56. Li Q, Guan X, Wu P, Wang X, Zhou L, Tong Y, et al. Early Transmission Dynamics in Wuhan, China, of Novel Coronavirus–Infected Pneumonia. N Engl J Med. 2020;0: null. doi:10.1056/NEJMoa2001316
57. Ke R, Sanche S, Romero-Severson E, Hengartner N. Fast spread of COVID-19 in Europe and the US suggests the necessity of early, strong and comprehensive interventions. medRxiv. 2020; 2020.04.04.20050427. doi:10.1101/2020.04.04.20050427
58. Abbott S. Temporal variation in transmission during the COVID-19 outbreak. In: CMMID Repository [Internet]. 2 Mar 2020 [cited 9 Mar 2020]. Available: https://cmmid.github.io/topics/covid19/current-patterns-transmission/global-time-varying-transmission.html
59. Romero-Severson EO, Hengartner N, Meadors G, Ke R. Decline in global transmission rates of COVID-19 through May 6 2020. medRxiv. 2020; 2020.04.16.20062141. doi:10.1101/2020.04.16.20062141
60. Hsiang S, Allen D, Annan-Phan S, Bell K, Bolliger I, Chong T, et al. The Effect of Large-Scale Anti-Contagion Policies on the Coronavirus (COVID-19) Pandemic. medRxiv. 2020; 2020.03.22.20040642. doi:10.1101/2020.03.22.20040642
61. Banholzer N, Weenen E van, Kratzwald B, Seeliger A, Tschernutter D, Bottrighi P, et al. Impact of non-pharmaceutical interventions on documented cases of COVID-19. medRxiv. 2020; 2020.04.16.20062141. doi:10.1101/2020.04.16.20062141
62. Kohanovski I, Obolski U, Ram Y. Inferring the effective start dates of non-pharmaceutical interventions during COVID-19 outbreaks. medRxiv. 2020; 2020.05.24.20092817. doi:10.1101/2020.05.24.20092817
63. Wu Z, McGoogan JM. Characteristics of and Important Lessons From the Coronavirus Disease 2019 (COVID-19) Outbreak in China: Summary of a Report of 72 314 Cases From the Chinese Center for Disease Control and Prevention. JAMA. 2020 [cited 26 Feb 2020]. doi:10.1001/jama.2020.2648
64. Lauer SA, Grantz KH, Bi Q, Jones FK, Zheng Q, Meredith HR, et al. The Incubation Period of Coronavirus Disease 2019 (COVID-19) From Publicly Reported Confirmed Cases: Estimation and Application. Ann Intern Med. 2020;172: 577. doi:10.7326/M20-0504
65. Tindale L, Coombe M, Stockdale JE, Garlock E, Lau WYV, Saraswat M, et al. Transmission interval estimates suggest pre-symptomatic spread of COVID-19. medRxiv. 2020; 2020.03.03.20029983. doi:10.1101/2020.03.03.20029983
66. Zhou F, Yu T, Du R, Fan G, Liu Y, Liu Z, et al. Clinical course and risk factors for mortality of adult inpatients with COVID-19 in Wuhan, China: a retrospective cohort study. The Lancet. 2020;0. doi:10.1016/S0140-6736(20)30566-3
67. Yang X, Yu Y, Xu J, Shu H, Xia J, Liu H, et al. Clinical course and outcomes of critically ill patients with SARS-CoV-2 pneumonia in Wuhan, China: a single-centered, retrospective, observational study. Lancet Respir Med. 2020;0. doi:10.1016/S2213-2600(20)30079-5
68. Wölfel R, Corman VM, Guggemos W, Seilmaier M, Zange S, Müller MA, et al. Virological assessment of hospitalized patients with COVID-2019. Nature. 2020;581: 465–469. doi:10.1038/s41586-020-2196-x
69. Grasselli G, Zangrillo A, Zanella A, Antonelli M, Cabrini L, Castelli A, et al. Baseline Characteristics and Outcomes of 1591 Patients Infected With SARS-CoV-2 Admitted to
ICUs of the Lombardy Region, Italy. JAMA. 2020;323: 1574–1581. doi:10.1001/jama.2020.5394

70. Verity R, Okell LC, Dorigatti I, Winskill P, Whittaker C, Imai N, et al. Estimates of the severity of coronavirus disease 2019: a model-based analysis. Lancet Infect Dis. 2020;0. doi:10.1016/S1473-3099(20)30243-7

71. Guan W, Ni Z, Hu Y, Liang W, Ou C, He J, et al. Clinical Characteristics of Coronavirus Disease 2019 in China. N Engl J Med. 2020;0: null. doi:10.1056/NEJMoa2002032

72. Lewnard JA, Liu VX, Jackson ML, Schmidt MA, Jewell BL, Flores JP, et al. Incidence, clinical outcomes, and transmission dynamics of severe coronavirus disease 2019 in California and Washington: prospective cohort study. BMJ. 2020;369. doi:10.1136/bmj.m1923

73. Argenziano MG, Bruce SL, Slater CL, Tiao JR, Baldwin MR, Barr RG, et al. Characterization and clinical course of 1000 Patients with COVID-19 in New York: retrospective case series. medRxiv. 2020; 2020.04.20.20072116. doi:10.1101/2020.04.20.20072116

74. He X, Lau EHY, Wu P, Deng X, Wang J, Hao X, et al. Temporal dynamics in viral shedding and transmissibility of COVID-19. Nat Med. 2020;26: 672–675. doi:10.1038/s41591-020-0869-5

75. Ball F, Britton T, Sirl D. A network with tunable clustering, degree correlation and degree distribution, and an epidemic thereon. J Math Biol. 2012;66: 979–1019. doi:10.1007/s00285-012-0609-7

76. Li R, Rivers C, Tan Q, Murray MB, Toner E, Lipsitch M. Estimated Demand for US Hospital Inpatient and Intensive Care Unit Beds for Patients With COVID-19 Based on Comparisons With Wuhan and Guangzhou, China. JAMA Netw Open. 2020;3: e208297–e208297. doi:10.1001/jamanetworkopen.2020.8297

77. Gao Z, Xu Y, Sun C, Wang X, Guo Y, Qiu S, et al. A systematic review of asymptomatic infections with COVID-19. J Microbiol Immunol Infect. 2020 [cited 3 Jun 2020]. doi:10.1016/j.jmii.2020.05.001

Acknowledgments: This work was supported by grants from the US National Institutes of Health DP5OD019851 (ALH), R01AI146129 (MZL), and R01AI101229 (MZL). We thank Julianna Shinnick for help in data collection and attendees at the HIV Dynamics & Evolution Conference for helpful feedback.
METHODS

Model of COVID-19 spread and clinical progression

We use a compartmental epidemiological model, based on the classic SEIR model, to describe the spread and clinical progression of COVID-19 (Figure 2). The basic model structure is inspired by many studies on the natural clinical progression of COVID-19 infection. Infected individuals do not immediately develop severe symptoms, but instead pass through milder phases of infection first. For a nice summary, see Wu and McGoogan [63]. Susceptible (S) individuals who become infected start out in an exposed class E, where they are asymptomatic and do not transmit infection. Progression from the exposed stage to the infected stage I, where the individual is symptomatic and infectious, occurs at rate a. The clinical descriptions of the different stages of infection are given below. Infected individuals begin with mild infection ($I_1$), from which they either recover, at rate $\gamma_1$, or progress to severe infection ($I_2$), at rate $p_1$. Severe infection resolves at rate $\gamma_2$ or progresses to a critical stage ($I_3$) at rate $p_2$. Individuals with critical infection recover at rate $\gamma_3$ and die at rate $\mu$. Recovered individuals are tracked by class R and are assumed to be protected from re-infection for the duration of the epidemic. Individuals may transmit the infection at any stage, though with different rates. The transmission rate in stage $i$, $\beta_i$.

The clinical definitions of the infection stages are as follows:

- **Mild infection** - These individuals have symptoms like fever and cough and may have mild pneumonia. Hospitalization is not required (though in many countries such individuals are also hospitalized)
- **Severe infection** - These individuals have more severe pneumonia that leads to dyspnea, respiratory frequency <30/min, blood oxygen saturation <93%, partial pressure of arterial oxygen to fraction of inspired oxygen ratio <300, and/or lung infiltrates >50% within 24 to 48 hours. Hospitalization and supplemental oxygen are generally required.
- **Critical infection** - These individuals experience respiratory failure, septic shock, and/or multiple organ dysfunction or failure. Treatment in an ICU, often with mechanical ventilation, is required.

A summary of the variable definitions:

- **S**: Susceptible individuals
- **E**: Exposed individuals - infected but not yet infectious or symptomatic
- **$I_i$**: Infected individuals in severity class $i$. Severity increases with $i$ and we assume individuals must pass through all previous classes
  - $I_1$: Mild infection
  - $I_2$: Severe infection
  - $I_3$: Critical infection
- **R**: Individuals who have recovered from disease and are now immune
- **D**: Dead individuals
- **N=S+E+I_1+I_2+I_3+R+D** Total population size (constant)

To describe the average time course in a large, well-mixed population, the model can be represented by the following set of differential equations:
The basic reproductive ratio $R_0$ of this model is:

$$R_0 = N \frac{\beta_1}{p_1 + \gamma_1} + \frac{p_1}{p_1 + \gamma_1} \left( \frac{N p_2}{p_2 + \gamma_2} + \frac{p_2}{p_2 + \gamma_2} \frac{N p_3}{\mu + \gamma_3} \right)$$

which can also be expressed as, where $T_i$ is the duration of stage $i$ and $f_i$ is the probability of progressing (vs recovering) from stage $i$:

$$R_0 = N \beta_1 T_1 + N f_1 \beta_2 T_2 + N f_2 \beta_3 T_3$$

Our model makes several assumptions with regards to the clinical and epidemiological dynamics of COVID-19. We do not explicitly track asymptomatic infections, which have been estimated to be around 20% of infections [24] (but estimates range from 1% to 50%, reviewed in [77]). However, in our model asymptomatic infections can be considered to be part of the “mild infections” compartment. There is significant evidence that asymptomatic individuals are infectious, and with this assumption their infectiousness would be equal to those with mild infection. For simplicity we assume that critical infection always occurs after passing through a stage of severe infection, while in reality there appears to be some individuals who progress directly from mild to critical infection. Similarly, we assume that only individuals who have progressed to critical infection die, though there is now some evidence that death can occur unexpectedly in individuals who are not already hospitalized. We do not think that any of these assumptions affect the main conclusions of our paper, which does not focus on hospital resource use or morbidity/mortality estimates. In general our model allows for individuals at all stages of infection to transmit to others. However, for this paper we have assumed that only individuals with mild infection can transmit. We think it’s likely that an individual is most infectious during this stage, when they would still be in the community and feeling well enough to interact with others. We thus ignore transmission from hospitalized patients to their healthcare providers. We make the standard SEIR model assumption that the time until an infected individual experiences symptoms is the same as the time until they become infectious, whereas it has now been shown for COVID-19 that there is significant transmission risk starting ~1 day before...
symptom onset. While this disease feature is important for studies that examine symptom based case detection/isolation, for simplicity we have ignored this feature in our model, which doesn't focus on these issues. The serial interval produced by our model parameters agrees with observed values, and so we believe our timescales for infections spread are realistic. We do not explicitly consider age-dependent rates of infection or progression to more serious stages.

The differential equation version of our model is available as an online simulation tool in which users can explore the effects of these assumptions of model structure as well as parameter values on model outputs: [https://alhill.shinyapps.io/COVID19seir/](https://alhill.shinyapps.io/COVID19seir/)

**Stochastic network implementation**

To avoid the assumptions inherent in formulating an epidemiological model as differential equations (e.g. assuming a well-mixed population, deterministic dynamics, and exponentially-distributed durations of each infection stage), we implement the model as a stochastic process simulated on a transmission network.

We believe that this implementation is important for our research questions, for a few main reasons. Firstly, respiratory infections are spread by close physical contact that occurs in highly structured contact networks, which impact the growth rate of outbreaks, the relationship between an individual’s inherent infectiousness and the basic reproductive ratio $R_0$, the variability in secondary infections between individuals, and the effects of control measures on spread. Secondly, differential equations implicitly assume that the durations of infection stages are extremely long-tailed, which can lead to unrealistic conclusions about the timescale of the epidemic response to control measures as well as to the relationship between the early growth rate, serial interval or generation time, and $R_0$. Finally, we believe it is important to model the uncertainty in epidemic trajectories that arises from the inherent stochasticity of transmission.

In our stochastic formulation, we assumed that the duration of each stage of infection was gamma-distributed, with both the mean and variance taken from the literature. Individuals were connected with a fixed, weighted contact network that determined the potential paths of transmission. The network is represented as a sparse matrix to save memory (a list of the index of each node in an edge, along with the edge weight). The model was implemented with a discrete time stochastic process that tracked the state of each individual and the time since they first entered that state. The model was implemented in Python using JAX, a framework for generating high-performance code optimized to run on GPUs. Our code was entirely run in the cloud on Google Colab. The code is available at: [https://github.com/alsnhll/COVID19NetworkSimulations](https://github.com/alsnhll/COVID19NetworkSimulations)

**Model parameters**

We estimated the distribution of the duration of each stage of infection from the literature. For the incubation period, we used an estimate of $5\pm 4$ days from [24,64], which is consistent with most other estimates. The duration of mild infection, which we assume is roughly equal to the infectious period, can be estimated from a few different sources: a) the duration of mild
symptoms, b) the time from symptom onset to hospitalization (e.g. time to progress to severe stage), or c) the duration of viral shedding via sputum or throat swabs, d) inferred from both the incubation period and the "serial interval" between symptom onset in an index case and a secondary case they infect. Considering (d), we took an estimate of the serial interval from Bi et al [24], who used a large cohort of transmission pairs and reported values separately for situations where the index case was not isolated or hospitalized during mild infection. Similar values were found in [54,56]. Some other studies have estimated smaller values (e.g. [37]), likely due to rapid isolation of symptomatic cases in Asia, but another very comprehensive study in Italy estimated up to 10 days [55]. This value implies an infectious period of 6±2 days. This is relatively consistent with estimates of the time from symptom onset to hospitalization [38,65–67], and is roughly equivalent to the time at which average viral loads drop 4-5 orders of magnitude from peak values [68].

The duration of severe infection in our model is equivalent to the time from hospital admission to recovery for individuals who did not progress to the critical stage, or the time from hospital admission to ICU admission (since critical cases require ICU-level care). Since it is hard to find direct estimates of this duration, we instead used estimates of the total time from symptom onset to ICU-admission (e.g. combined length of mild + severe infection) [66,67], and subtracted the inferred duration of mild infection. This led to an estimate of 6±4.5 days. We estimated the duration of critical infection (the length of ICU stay) directly from cohort studies to be 8 +/- 6 days [66,69]. With these estimates, we verified that the total time from symptom onset to death/recovery agreed with data (~20±10 days) [54,66,70]. Note that we assumed that the duration of each stage of infection was independent of the previous stage and was also independent of the eventual outcome.

In each stage of infection, an individual can either progress to the next stage or recover, and the probability of each was also estimated from the literature [5,63,71]. These large clinical cohort studies estimated that ~ 20% of infections required hospitalization (i.e. progress to severe stage), ~5% require ICU care (i.e. progress to critical stage), and an overall case fatality risk of 2%. This leads to probabilities of progression of 0.2 from I₁ → I₂, 0.25 from I₂→ I₃, and 0.4 from I₃ → D. However, there is significant uncertainty in these values. More recent estimates suggest the rates of progression to more serious stages of infection might be lower after correcting for asymptomatic/undiagnosed cases in China [70], but in contrast, recent studies from the US suggest higher rates of ICU admission and death among hospitalized patients compared to in Asia [72,73]. Since the results of our paper focus on the timing of the peaks of different infection stages but not on the prevalence at these peaks, they are not sensitive to these assumptions.

We chose a value of the transmission rate β such that the early epidemic doubling time was ~ 4 days (growth rate r = 0.17/day) and the basic reproductive rate R₀ = 3. While some studies have estimated R₀ values as low as 2, these have generally used estimates based only on the serial interval which are mathematically problematic, used short estimates of the serial interval that are influenced by rapid case isolation in Asia as opposed to longer values found in other studies.
that correct for this, and fit to longer doubling times that what was observed early in the outbreak in the US and Europe.

The time at which we implemented interventions in our simulations was chosen to occur at a realistic time in the epidemic relative to real responses to COVID-19. To estimate this time for a typical US metro area, we downloaded case and death counts for each US county and aggregated them into the top 50 largest metro areas. Then we collected the time that stay-at-home orders were implemented in each of these regions, and looked at the median cumulative case and death counts by that day, and chose our intervention time to match those values. We found that there were on average around 200 cases per million inhabitants at time of stay at home intervention (range [30,1000]), and ~5 [0-20] deaths per million. We assumed that reported “cases” are hospitalized individuals only (I₂ + I₃). These values were recreated in our simulation in well-mixed populations on Day 40, which we used as the intervention time. At this time, ~0.5% of the population had ever been infected (including E, I₁, I₂, I₃, R, and D). Since the median day shelter-in-place orders were implemented across these metros was April 1, Day 0 in our simulation corresponds to ~ Feb 20. For simulations in other networks, we kept R₀ constant but due to the population structure, the exponential growth rate of the epidemic varied between different values of the household and external contact structure. Thus for each structure we chose slightly different intervention start times to keep the infection prevalence consistent across comparisons. The start times varied from Day 43 (when \(w_{EX}/w_{HH} = 3, 1\)), Day 45 (when \(w_{EX}/w_{HH} = 1/3\)) to Day 55 (when \(w_{EX}/w_{HH} = 1/9\)).

### Table 1: Model parameters for duration of each stage of infection

| Infection stage                  | Mean | STD | Source                                           |
|----------------------------------|------|-----|--------------------------------------------------|
| Exposed (incubation period)      | E    | 5   | 4 [24,64]                                        |
| Mild infection                   | I₁   | 6   | 2 Estimated to agree with serial interval and [38,65–68,74] |
| Severe infection                 | I₂   | 6   | 4.5 Estimated to agree with time to ICU admission |
| Critical infection               | I₃   | 8   | 6 Estimated to agree with [66,69] and time to recovery/death |
| Serial interval                  | 8    | 4.5 | Derived from above, agrees with [24,54,55]        |
| Hospitalization (avg, w or w/o ICU stay) | 8    | 6   | Derived from above                               |
| Hospital (incl. ICU stay)        | 14   | 7.5 | Derived from above                               |
Table 2: Model parameters for probability of progressing from each stage of infection

| Infection stage                  | Probability of progression | Source       |
|---------------------------------|----------------------------|--------------|
| Exposed (incubation period)     | E                          | 1            |
| Mild infection                  | I₁                         | 0.2          | [5,63,71]    |
| Severe infection                | I₂                         | 0.25         | [5,63,71]    |
| Critical infection              | I₃                         | 0.4          | [5,63,71]    |

Well-mixed network structure

We approximated a well-mixed population by randomly connecting each individual to 100 other individuals in the population. While a truly “well-mixed” network would connect every one to everyone else, with the large population sizes we use (10^6), this would require huge amounts of memory and negate the computational efficiency of using sparse matrices to represent the networks. Since in reality each individual will only transmit to a few others before recovering, any uniform random network with a large degree is a good approximation to a fully-connected network.

Two-layer household network structure

Construction: We constructed a weighted two-layer network, consisting of a layer for within-household connections and another for external connections. Individuals were first assigned households using the distribution of household sizes in the United States (data obtained from the 2010 census, mean household size \( n_{HH} \sim 2.5 \)). All individuals in a household were connected to each other. Each individual was then assigned random external contacts. The degree distribution for external connections was obtained from contact survey data that recorded daily interactions of individuals [12,13]. This data was originally collected for a subset of countries and then projected to other countries using a wide range of demographic data. The contacts are age structured and include the type, duration, location and frequency of the contact. These surveys were designed to capture interactions relevant to the spread of respiratory diseases, and include interactions consisting of either physical contact or close face-to-face conversations. From this data, we obtained daily non-household contacts by summing ‘work’, ‘school’ and ‘other’ contacts. For the United States there were on average \( n_{EX} \sim 7.5 \pm 2 \) (mean...
± standard deviation) daily non-household contacts, equivalent to 3x household contacts. The variance was obtained by the variance in the mean across all age groups. We assigned external degrees to individuals following a binomial distribution with this mean and standard deviation. This assignment was done randomly and did not depend upon the size of the person’s household. The network layer was created by giving ‘stubs’ to individuals equal to their external degrees. These stubs were then randomly paired between individuals in the population to create connections. In addition to the number of contacts, the probability of infection also depends upon the duration and intensity of the contact. We assigned weights \((w_{HH}, w_{EX})\) to the two layers of the network to account for this. We considered different scenarios (keeping \(R_0\) fixed) where, \(w_{HH} = 1\) and varied \(w_{EX} = 3, 1, 1/3, 1/9\) to reflect the relative importance between household and external contacts.

**Intervention:** Intervention, corresponding to social distancing measures, was modeled by reducing the weight of the external layer, \(w'_{EX} = (1 - \epsilon)w_{EX}\) where, \(\epsilon (0 \leq \epsilon \leq 1)\) is the ‘intervention efficacy’. Household contacts were either unaffected \((w'_{HH} = w_{HH})\) or doubled \((w'_{HH} = 2w_{HH})\) during intervention, to represent the increased time spent with household members.

**Partial relaxation of intervention:** We modeled a scenario of partial relaxation of social distancing measures in which every household could “merge” with another household. This relaxation altered the household layer so that all households in the network were paired with another random household and the two were merged to create a fully-connected joint household \((n'_{HH} \sim 5)\). We considered two scenarios for how the external layer changed during partial relaxation of intervention. In the baseline scenario, the external layer was the same as during intervention. In a second scenario, the number of external contacts per individual was reduced so that the average number of total contacts was the same before and after merging \((n'_{EX} = n_{EX} - n_{HH})\). This partial relaxation was only conducted for the scenario where household and external connections had the same weight \((w_{HH} = 1\) and \(w_{EX} = 1)\).

**Individual probability of infection as a function of household size:** We computed the individual probability of infection retrospectively, after the epidemic had died out, for the case of a 100% effective intervention. We counted the number of individuals who were ever infected by the end of the epidemic and calculated the corresponding distribution of their household sizes. This is a conditional probability that gives the probability of household size, given that an individual was infected \(P(HH\ size|inf)\). The probability of infection given household size was then calculated using Bayes’ rule, \(P(inf|HH\ size) = P(HH\ size|inf) * P(inf)/P(HH\ size)\) where, \(P(inf)\) is the fraction of the total population that was infected during the epidemic and \(P(HH\ size)\) is the distribution of the household sizes in the population. The probability was averaged over 10 iterations of the simulation.

**Five-layer network structure**

We constructed a non-weighted 5-layer (1 household and 4 external) network for an age-structured population with realistically structured external layers. The population was divided into four age groups: preschool aged (ages 0-5), school-aged (ages 5-19), working-aged (ages
19-64) and elderly (ages 65+). The distribution of ages in the United States was obtained from the 2018 World Bank Age Structure data which consists of the population divided into 5-year age groups. In addition to the broad age groups, we also kept track of the 5-year age group that an individual belonged to. The contact survey data [13] used to construct the 2-layer network was also predominantly used here to determine the statistical properties of the layers.

Household layer: The household layer was constructed in the same manner as in the 2-layer network. Individuals were assigned to fully-connected households using the distribution of household sizes in the United States from the 2010 census data (mean household size, $n_{HH} \sim 2.5$).

School layer: The school layer contained connections between the school-aged age group in the population. This external layer was constructed using the technique described by Ball et al [75], where a network layer with a given degree distribution and correlations among connections (i.e. “clustering” or “transitivity”) can be constructed. The degree distribution in this layer was obtained from the school contact survey data [13], which estimated that the school-going population in the United States, on average, had $n_{SCHOOL} \sim 7.3 \pm 1.8$ school-related contacts daily. The variance was obtained by the variance in the mean across the school-aged (5-19) age groups. Individuals were assigned degrees randomly from a binomial distribution with this mean and standard deviation. The age-structure of contacts at school suggests a significant level of clustering by age group. To create correlated connections, the method of Ball et al requires two additional parameters: The number of groups $n$ to divide the population into, and $r$, which is roughly the extent to which individuals within the same group are connected. $r = 1$ corresponds to individuals being connected only within their group whereas $r = 0$ implies completely random connections without any correlation with members of their own group. Averaged over the school age groups (5-19), we found that $\sim 57\%$ of school contacts for an individual belonged to their own age group. Since there are three 5-year age groups in our school-aged population, we divided our population into those three groups ($n = 3$) and chose $r = 0.57$.

Work layer: The work layer consisted of connections between the working-aged group in the population. This layer was constructed similarly to the school layer. We obtained the mean and standard deviation in number of daily work contacts from the contact survey data (5.0 $\pm$ 2.3). The variance was obtained by the variance in the mean across working-aged (20-64) age groups. Individuals were randomly assigned a work-place degree from a binomial distribution with the mean and standard deviation. Then we used a separate study by Potter et al that mapped real work-place networks to estimate the level of clustering (transitivity), at $\sim 0.1$ [15]. Note that Potter et estimated a higher degree, since their network contained total contacts in a work network and not just the daily contacts as given by the contact survey data, but the coefficient of variation is similar. We again used the Ball et al technique [75] to create clustering in the network. High transitivity can be achieved by choosing appropriate correlation parameters $n$ and $r$. We assumed this clustering arose from the fact that people belonging to the same work-place have a higher chance of being connected to each other. According to NAICS (North American Industry Classification System), $\sim 80\%$ of businesses in the United States have $\leq 10$ employees.
employees and so for the sake of simplicity, we assigned each individual to a ‘work-place’ of size ten \( n = \frac{\text{# of working individuals}}{10} \). We picked \( r = 0.8 \) in order to have a high level of transitivity \( \sim 0.12 \) while also ensuring inter work-place connections.

**Friend (social contacts) layer:** The friend layer represents social contacts of people, their ‘friend circles’. Individuals were assigned to fully-connected friend groups, where friend groups consisted of people belonging to the same age group (preschool, school, working, elderly). The distribution of sizes of these friend groups were obtained from Wrzus et al [17], which is a meta-analysis of the effects of age on social networks. From their data, we estimated that the mean sizes of friend groups for individuals less than 20 years of age is \( \sim 7 \), that for the working age population \( \sim 7 \) and \( \sim 5 \) for the elderly. These constitute total social contacts for the individuals and not just their daily interactions as given by the contact survey data. The ‘other’ category in the contact survey data [13] gives the number of daily interactions that an individual has that are not within the household, at school or at the work-place. In our network, the friend layer and the community layer together constitute this ‘other’ category. According to the data, averaged over the age groups, there are \( 4.3 \pm 1.9 \) such interactions for an individual in the United States. The variance was obtained by the variance in the mean across all age groups. Since the total social contacts are much higher than this daily value, we scaled the sizes of the friend groups \(( n_{\text{FRIEND}} \rightarrow n_{\text{FRIEND}}/4)\) to reflect daily social contacts. The scaling factor was chosen to ensure that the community layer didn’t end up being too sparse. We chose to do this instead of creating a weighted network for the sake of simplicity. The friend group sizes were drawn using the negative binomial distribution to account for the large variance (estimated variance post scaling: 6.25, 2.5, 1.75 for the three age-groups) seen in the data.

**Community layer:** This layer constitutes the additional random contacts an individual has during the course of their day. As mentioned previously, together with the social layer this constitutes the ‘other’ category in the contact survey data. We chose the average degree for this layer, \( n_{\text{COMM}} \sim 1.72 \pm 0.76 \) such that the combined degree for the two layers matches what is seen in the data. We used a binomial distribution and assigned degrees randomly to the individuals. This layer was constructed in the same manner as the external layer in the 2-layer network. It amounts to using the Ball et al [75] technique with \( n = 1 \) and \( r = 0 \).

**Intervention:** The social distancing intervention was modeled by deleting a certain percentage of external connections. School connections were always completely deleted during intervention, whereas social and community connections were deleted depending upon what we termed as the ‘efficacy’ of intervention. For example, 85% efficacy corresponds to deleting 85% of contacts in these layers. We considered two scenarios for the effect of intervention on the work-layer. In one case, similar to the social and community layer, a percentage of work contacts was deleted depending upon the intervention efficacy. Random deletion of connections leads to a large reduction in the transitivity of the work layer, from \( \sim 0.12 \) to \( \sim 0.02 \). In the second case, the effect of intervention was modeled as a clustered deletion of workplaces instead. For example, 85% intervention efficacy corresponds to 85% of workplaces being dissolved. Clustered deletion still maintains a high level of transitivity \( \sim 0.10 \) in the work layer.
Note as all school connections were completely deleted during intervention, the total effective efficacy of intervention was a bit higher than that for the social, community and work layers. For example, 85% efficacy in these external layers corresponds to a total efficacy of 88%.

**Probability of infection for an individual working during intervention:** We calculated the probability of infection for two intervention efficacies (85%, 70%) at day 300 after the start of the outbreak. We first obtained the fraction of the infected people (at day 300) who were still working during the intervention. This gives the conditional probability that an individual was working during intervention given that they were infected, \( P(\text{working|inf}) \). We calculated the probability of infection given that an individual was working during intervention using Bayes' rule, \( P(\text{inf|working}) = P(\text{working|inf}) \times P(\text{inf})/P(\text{working}) \) where, \( P(\text{inf}) \) is the fraction of the total population that was infected by day 300 of the epidemic and \( P(\text{working}) \) is the fraction of the total population that was working during intervention. The probability was averaged over 10 iterations of the simulation.

**Probability of infection for an individual living with working household members during intervention:** This was also calculated at day 300 of the epidemic for the two intervention efficacies and, averaged over 10 iterations of the simulation. We obtained the fraction of the infected people (at day 300) who had at least 1 household member who was working during intervention. This corresponds to the probability that an infected individual had at least one working household member during intervention, \( P(\text{HH working|inf}) \). As before, the probability of infection given that an individual was living with working household members during intervention was then calculated using Bayes’ rule, \( P(\text{inf|HH working}) = P(\text{HH working|inf}) \times P(\text{inf})/P(\text{HH working}) \) where, \( P(\text{inf}) \) is the fraction of the total population that was infected by day 300 of the epidemic and \( P(\text{HH working}) \) is the fraction of the total population that had at least one working household member during the intervention.

**Probability of infection for a non-working individual with no working household members during intervention:** This was calculated in the same way as the other probabilities. We obtained the fraction of the infected people (at day 300) who were not working and had no working household member, \( P(\text{HH not working|inf}) \). As before, the required probability was then calculated using Bayes’ rule, \( P(\text{inf|HH not working}) = P(\text{HH not working|inf}) \times P(\text{inf})/P(\text{HH not working}) \) where, \( P(\text{inf}) \) is the fraction of the total population that was infected by day 300 of the epidemic and \( P(\text{HH not working}) \) is the fraction of the total population that was not working and had no working household members during the epidemic.

**COVID-19 Data**

**Wuhan, China:** Data from Wuhan, China was obtained from the two daily situation reports published each day: [http://wjw.wuhan.gov.cn/ztzl_28/fk/yqtb/index_11.shtml](http://wjw.wuhan.gov.cn/ztzl_28/fk/yqtb/index_11.shtml). We extracted new cases, new deaths, the number of individuals currently hospitalized with severe infection (which we took as a proxy for “hospitalized”) and the number of individuals currently hospitalized with “critical” infection (which we took as a proxy for individuals in the ICU). Data was already digitized by Li et al [76] for January and February ([https://github.com/c2-d2/COVID-19-wuhan-](https://github.com/c2-d2/COVID-19-wuhan-).
guangzhou-data); we added data into March. For some dates the numbers of severe and critical cases were only reported for the entire province of Hubei, and in those instances, following Li et al, we assumed the proportion of those attributable to the city of Wuhan was equal to the proportion of currently active cases occurring in Wuhan. The vast majority of the Hubei outbreak took place in Wuhan.

**Lombardy, Italy:** Data on daily new cases and deaths as well as current patients hospitalized or in ICU for the Lombardy region of Italy was downloaded from Github repository maintained by the Department of Civil Protection in Italy: [https://github.com/pcm-dpc/COVID-19](https://github.com/pcm-dpc/COVID-19).

**Madrid, Spain:** Data for daily new cases, daily deaths, daily new hospital admissions, and daily new ICU admissions were obtained from an online application maintained by the National Center for Epidemiology, using data from the Ministry of Health: [https://cnecovid.isciii.es/covid19/](https://cnecovid.isciii.es/covid19/). In the “documentation and data” section of the application there is a link to a .csv file with all the data used in the web app.

**New York City, New York, USA:** Daily new cases and deaths were downloaded from the Github repository of the New York City Department of Health and Mental Hygiene: [https://github.com/nychealth/coronavirus-data](https://github.com/nychealth/coronavirus-data). Number of currently individuals hospitalized or in ICU by date was obtained from the Github repository for digital news platform The City, who obtains this data directly from the New York state governor’s office: [https://github.com/thecityny/covid-19-nyc-data](https://github.com/thecityny/covid-19-nyc-data)

**Los Angeles County, California, USA:** Daily new cases and deaths were obtained from the Github repository maintained by the Los Angeles Times newspaper: [https://github.com/datadesk/california-coronavirus-data](https://github.com/datadesk/california-coronavirus-data). The number of individuals currently in the hospital or ICU was obtained from the California Health & Human Services Open Data Portal: [https://data.chhs.ca.gov/dataset/california-covid-19-hospital-data-and-case-statistics/resource/6cd8d424-dfaa-4bde-9410-a3d656e1176e?view_id=b23b0158-a85d-4bf2-95b1-96f7556f7342](https://data.chhs.ca.gov/dataset/california-covid-19-hospital-data-and-case-statistics/resource/6cd8d424-dfaa-4bde-9410-a3d656e1176e?view_id=b23b0158-a85d-4bf2-95b1-96f7556f7342).