Covalency is Frustrating: La$_2$Sn$_2$O$_7$ and the Nature of Bonding in Pyrochlores under High Pressure—Temperature Conditions

Christian Childs,† Keith V. Lawler,§,○ Andrew L. Hector,§, Sylvain Petitgirard,¶ Ori Noked,‖ Jesse S. Smith,▲ Dominik Daisenberger, ▲ Lucile Bezacier,○ Marek Jura,♦ Chris J. Pickard,▲,△ and Ashkan Salamat*§,⊥

†Department of Physics and Astronomy and HiPSEC, University of Nevada Las Vegas, Las Vegas, Nevada 89154, United States
‡Department of Chemistry and Biochemistry and HiPSEC, University of Nevada Las Vegas, Las Vegas, Nevada 89154, United States
§Department of Chemistry, University of Southampton, Southampton SO17 1BJ, United Kingdom
¶Bayerisches GeoInstitut (BGI), University of Bayreuth, 95444 Bayreuth, Germany
‖Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts 02138, United States
▲High Pressure Collaborating Access Team at Advanced Photon Source, Geophysical Laboratory, Carnegie Institution of Washington, Argonne, Illinois 60439, United States
○Diamond Light Source Ltd., Didcot, Oxfordshire OX11 0DE, United Kingdom
□European Synchrotron Radiation Facility, BP 220, 38043 Grenoble, Cedex 9, France
●ISIS, STFC, Harwell Innovation Campus, Didcot, Oxfordshire OX11 0QX, United Kingdom
⊥Department of Materials Science & Metallurgy, University of Cambridge, 27 Charles Babbage Road, Cambridge CB3 0FS, United Kingdom
¶Advanced Institute for Materials Research, Tohoku University, Sendai 980-8577, Japan

ABSTRACT: Natural specimens of the pyrochlore (A$_2$B$_2$O$_7$) compounds have been found to retain foreign actinide impurities within their parent framework, undergoing metamictization to a fully amorphous state. The response to radionuclide decay identifies pyrochlore systems with having high radiation tolerance and tailored use in radioactive waste applications and radionuclide sequestration. High pressure is a powerful pathway to high density states and amorphization with parallels to radiation-induced processes. Here, La$_2$Sn$_2$O$_7$ is evaluated under extreme conditions via the combination of laser heating in a diamond anvil cell with X-ray diffraction and Raman spectroscopy. The measurements are supported by ab initio random structure searching and molecular dynamics calculations. A new ground state at 70 GPa is revealed, and high temperature annealing is fundamental to access its crystalline ground state and fully determine the structure. This crystalline phase (P2$_1$/c) retains its structural integrity during decompression and is fully recoverable to ambient conditions. The final state of the system is shown to be highly pathway dependent due to the covalent nature of the Sn—O bonding. The Tc pyrochlore, La$_2$Tc$_2$O$_7$, is analyzed for similarities in the bonding to determine the likelihood of an analogous pathway dependency to a final state.

INTRODUCTION

Pyrochlore oxides are a focus of intensive research, partly due to the large variety of physical and chemical properties that can be tuned by changes in composition.¹–³ As a result, there are significant applications of these systems in many areas of technological interest.¹–⁶ A strongly emerging area in materials-based research is the use of pyrochlore oxides as matrices to sequester and immobilize radionuclides, particularly actinides and Gd produced in the nuclear fuel cycle.⁷–⁹ This interest is motivated by the chemical stability, low swelling, and high radiation tolerance of pyrochlore materials. Additionally, natural pyrochlore ores are known to have actinide impurities, and several actinide dioxides adopt the related fluorite (CaF$_2$) structure.⁷,¹⁰ The properties of lanthanide-technetium pyrochlore oxides have also been investigated, as pyrochlore oxides may have use as a $^{99}$Tc waste form.¹¹

Natural pyrochlore ores are known to undergo metamictization to a fully amorphous form as are the synthetic pyrochlore actinide and lanthanide immobilization materials.¹² The alpha decay events and the kinetic energy recoil the associated nuclei of most radioactive actinides and lanthanides release large amounts of energy ($\sim$5 MeV). That energy introduces defects
in the crystal lattice, leading to amorphization, swelling, and increased dissolution rates of the pyrochlore materials. The energy damage can be emulated in the laboratory via ion irradiation of samples. The decay events happen over the long half-lives of the radionuclides being sequestered, providing continuous radiation damage to the host matrix, altering the requirements for long-term immobilization. Storage of nuclear waste necessitates structural stability over the half-life of the radionuclides being stored. Therefore, it is important to fully understand the structural behavior and stability of all candidate waste forms, including controlled amorphization, to better design long-term storage solutions.

The archetypical pyrochlore oxide structure is a defect fluorite structure (Fd3m) with $1/8$th of the anion sites vacant and stoichiometry: $A_2B_2X_6Y_2$, $X = O^{2−}$, $Y = O^{2−}$, $OH^{−}$, $F^{−}$. The eight-coordinate $A^{3+}$ and six-coordinate $B^{4+}$ cation sites form edge-sharing coordination polyhedra whose shape change with composition and external constraints (e.g., pressure and temperature). The stability of the pyrochlore oxide is largely dependent on the ratio of the radii of the A-site and the B-site cations ($r_A/r_B$). The formation of the pyrochlore structure can be found in the cation radius ratio range between 1.46 ($Gd_2Zr_2O_7$) and 1.78 ($Sm_2Ti_2O_7$) under ambient conditions. The A-site cations are typically the nuclei to be sequestered, and the typical B-site cations and radii are Sn, 69 pm; Zr, 72 pm; and Ti, 60.5 pm. The cation radius ratio is also considered a good predictor of radiation tolerance because one of the main radiation damage mechanisms are cation antise defects. These defects result in an A cation on the B sublattice or vice versa, and their associated energy cost is directly proportional to the difference in cation radii. A second main factor contributing to the stability of the pyrochlore structure is the electronic configuration, predominately of the $B-O$ bond. It has been shown that zirconate pyrochlores exhibit better resistance to radiation damage than the titanates, attributed to the more ionic nature of Zr−O bonding. The ionicity of bonding with the typical B-site cations generally follows $Sn < Ti < Zr$.

The possibility of accessing high pressure pathways provides an alternative route to studying the structural stability of the pyrochlore structure with parallels to radiation-induced processes. High pressure conditions can introduce strain and defects into a crystal structure, raise its free energy, and give rise to structural and electronic transitions. If the kinetic energy required for a phase transition is too high, a material can often transition to an amorphous form. A number of pyrochlore compounds have been investigated under high pressure and have been shown to undergo pressure-induced amorphization (PIA). The pressure response and the occurrence of PIA are linked to the relative stabilizing forces in the solid-state structure of the pyrochlore oxide. While many pyrochlores exhibit PIA, there is no clear indication that the cation radius ratio is a reliable predictor for the existence of PIA. The cation radius ratio is also not a reliable predictor for the pressure of the critical onset of amorphization in the compounds that do exhibit PIA.

$L_{a_2}S_{n_2}O_7$ adopts the archetypal Fd3m pyrochlore structure at ambient conditions and is well within the stability region ($r_A/r_B = 1.681$). The goal of studying this model non-radioactive pyrochlore material is twofold: first, to better understand the chemistry of the pyrochlore oxides, and second, to elucidate controlled pathways to amorphous forms or extreme conditions stable phases. These pathways can then be applied as a pretreatment for radionuclide containing pyrochlores to achieve a waste form with a longer lifetime. An appropriate secondary containment system (glass, pressed ceramic, cement, etc.) could then be designed for the new waste form.

In this study, we investigate the structural behavior of $L_{a_2}S_{n_2}O_7$ under high temperature, high pressure, and high pressure—temperature conditions as outlined in Figure 1. The

![Figure 1](image.png)

**Figure 1.** A summary of the various techniques and analysis undertaken: (blue) experimental work, (green) theoretical work, and (red) the various states in which is the system is observed.

Fd3m structure exhibits a high degree of structural stability up to high temperatures. In contrast, the effects of strain/stress response on structural stability on the system shows pathways to two different recoverable final states. One pathway is to an amorphous form under nonhydrostatic conditions. The alternative pathway is a kinetically hindered first-order phase transition, preventing any reliable structural refinement. Laser-annealing at pressure produces a crystalline material that can be characterized using Rietveld refinement analysis. First principles simulations support the experimental findings and provide an explanation for the stability regions and behaviors observed.

### METHODS

Professor Neil Hyatt at the Department of Materials Science and Engineering, the University of Sheffield provided the $L_{a_2}S_{n_2}O_7$ sample. The sample was made by ball milling SnO2 and La2O3. Purity was confirmed by transmission electron microscopy (TEM), Raman, and X-ray diffraction (XRD). The $L_{a_2}S_{n_2}O_7$ sample was ground to a fine powder to ensure reliable averaging statistics from the powder diffraction experiments.
Isobaric heating was carried out on a Rigaku Smartlab (9 kW) diffractometer with Cu Kα X-rays (λ = 1.54056 nm), parallel incident beam, θ−2θ geometry, Dxtl 1D detector, and Anton Paar HTK hot stage. The sample was heated under air, and temperature was measured using a thermocouple located just under the sample. The lattice parameters were extracted from the high temperature XRD data using Le Bail refinement.

Three high pressure compression runs were carried out. The first two runs were at room temperature using membrane-driven diamond anvil cells with 150 μm culets. Rhenium gaskets were indented to 20 μm with a starting hole size of 80 μm, and pressures were determined using ruby fluorescence methods. The first run was compressed with no pressure transmitting medium (PTM) up to 75 GPa at ID09a (λ = 0.41570 Å) of the European Synchrotron Radiation Facility (ESRF) using a MAR355 flatpanel detector. The second run was carried out using a He PTM for quasi-hydrostatic compression up to a final pressure of 61 GPa. The second run was investigated using angle-dispersive synchrotron X-ray diffraction at the high pressure beamline ECB P02.2 of PETRA III (μ using a He PTM for quasi-hydrostatic compression up to a pressure of 61 GPa. The second run was investigated using angle-dispersive synchrotron X-ray diffraction at the high pressure beamline ECB P02.2 of PETRA III (λ = 0.48281 Å) with a Perkin-Elmer detector. The third run was loaded with a NaCl PTM, and the sample was split into four parts defined as quadrants. NaCl was used as the PTM to allow for laser heating due to its thermally insulating properties. The diamonds in the third run had 300 μm wide. The sample was isothermally compressed to 67 GPa, and each quadrant was CO2 laser-heated with a different amount of laser power (Table S1, Supporting Information). X-ray diffraction after laser-heating at high pressure was taken at HPCAT at the Advanced Photon Source (APS) in Argonne National Lab (λ = 0.406626 Å). The recovered laser-heated sample was investigated using angular-dispersive X-ray diffraction at Diamond Light Source (λ = 0.42280 Å). All diffraction data were integrated and then analyzed using Fit2D26 and GSAS27,28. Indexing of the high pressure phase was conducted using the CrysFire package, selecting solutions that gave reflections for all observable Bragg peaks and a high figure of merit.

Ab initio random structure searching (AIRSS)24,25 was performed at 70 GPa using the Perdew–Burke–Ernzerhof (PBE)22,23 generalized gradient approximation (GGA) density functional29,30 in the plane wave code CASTEP.31 The basis set cutoff energy was set to 450 eV using ultrasoft pseudopotentials with valence configurations of 5s5p65d4 for La, 4d4s5p2 for Sn, and 2s2p4 for O.32 A Γ-centered Monkhorst-Pack k-point grid with spacing 0.07 × 2π Å−1 was used to sample the Brillouin zone.32 Additional ab initio simulations were done with the Vienna ab initio simulation package (VASP) version 5.4.1. These simulations used primitive (unless otherwise specified) representations of the unit cells and a k-point grid with 0.03 × 2π Å−1 resolution. The basis set cutoff energy was 600 eV using projector augmented wave (PAW)33 pseudopotentials formulated for PBE GW with valence configurations of 5s5p65d4 for La, 4d5s5p2 for Sn, and 2s2p4 for O, and 4s4p5s5d2 for Tc.34 Energy tolerances were set to 1 × 10−6 eV and force tolerances to 0.01 eV Å−1. Molecular dynamics trajectories were propagated for 10 ps with 2 fs time steps by NpT ensemble Langevin dynamics.35,36 The first half of the simulation equilibrated the system, and statistics were taken over the second half of the simulation. The atoms had a friction coefficient of 5 ps−1. The lattice degrees of freedom had a friction coefficient of 3 ps−1 and fictitious mass of 100 amu.36 The MD simulations used softer pseudopotentials (i.e. no La Se or Sn 4d45), a 400 eV basis set cutoff energy, and a 1 × 10−5 eV energy tolerance.

## RESULTS AND DISCUSSION

### Properties of the Ambient Phase

Thermal amorphization is a common way to prepare materials as nuclear waste forms (i.e. vitrification into glasses). Therefore, a sample of La2Sn2O7 was heated to 1050 K at 50 K intervals, while the structure was monitored by in situ X-ray diffraction to assess its thermal stability. The structure maintains a high degree of crystallinity over the whole temperature range (33.84 ≤ wR ≤ 36.94%) with a volume expansion of 1.90% (Figure S1 and Table S2, Supporting Information). The thermal volume expansion coefficient (α = 1/3(R3)/∂(R3)/∂(T)) extracted from the data is 6.805 × 10−6 K−1.37 MD simulations corroborate the phase stability because a cubic unit cell of La2Sn2O7 remains Fd3m up to 2000 K. The 2000 K MD simulation exhibits a slightly larger 6.81% volume expansion. La2Sn2O7 should remain Fd3m until the melting point (>2000 °C) because these findings along with other measurements in the literature show a high thermal stability.38,39 The system clearly melts in an MD simulation at 5000 K, but the exact melting temperature was not probed. The hysteresis from such a small simulation box would prevent an accurate determination.40,41

Having established the thermal stability of the ambient phase, the stability against compression needs to be evaluated. A previous study claims the ambient phase of La2Sn2O7 is stable up to at least 17 GPa, with mostly crystalline Fd3m diffraction patterns up to 32 GPa.6 This has promising implications as a potential PIA pathway for pretreating pyrochlore radiowaste materials for long-term storage. However, there is a caveat to those results. A troublingly large amount (20–30%) of Sn disproportionated into a pure elemental phase as the material began to show a loss of crystallinity. The Sn disproportionation seemed to begin instantly upon compression. By 20 GPa, heavily distorted structure is reported. This is most likely a mix of La2Sn2O7, Sn, and La2Sn2−xO being fit as a single phase. To better understand the behavior of La2Sn2O7 as a function of pressure, compression using both non- and quasi-hydrostatic conditions was investigated.

The initial compression pathway was carried out non-hydrostatically (no PTM) to induce amorphization through pressure. The ambient phase is retained up to ~40 GPa. A broad feature appears in the XRD pattern at 8–9 degrees after 40 GPa. The broad feature becomes more and more apparent upon further compression until the amorphization of the sample (Figure 2). By 75 GPa, the sample is completely amorphized; as expected, the amorphous XRD diffraction pattern shifts to higher diffraction angles (75 GPa S(Q) of the
amorphized sample in Figure S2, Supporting Information). The amorphous system can be decompressed down to ambient conditions. At ambient conditions, there is no significant change beyond the expected main diffraction peak relaxing lower in 2θ (Figure 2, top left curve). This can be interpreted as a large hysteresis or even more likely an irreversible phase transition. The recoverability of the amorphous form clearly demonstrates that nonhydrostatic compression is a means for PIA pretreatment of radiowaste pyrochlores. Although, the pressures here are somewhat high for high-throughput treatment of waste forms.

Sluggish pressure induced transition and amorphization in nonhydrostatic compression experiments can be related to the sample’s microstructure evolution. Pressure introduces strain and defects into the lattice that build up until the elevated free energy forces a structural change. Local domains within the sample, as well as the deviatoric stress due to the sample geometry, often mean that phase transitions can occur across a wide range of measured pressures. The deviatoric stress is exacerbated by pressure gradients within the sample. Moreover, a simplistic yet useful model for nucleation and growth of a new high pressure phase shows that the material is in an extreme nucleation dominant regime at the nonhydrostatic experimental conditions. The critical radius for nucleation is very small in this regime. This scenario favors the creation of local nanocrystals that might be too small to be spatially coherent for X-ray diffraction, yielding the sample to be possibly X-ray amorphous. For the pyrochlore structure, it can also be predicted that such small nucleation centers will show increased propensity to become strictly amorphous, even to short-range order, given their energetic considerations. More hydrostatic conditions can increase the critical radius for nucleation and decrease the concentration of defects and the associated strain energy, thereby enabling the nucleation of viable high pressure phase crystallites in the sample.

The nonhydrostatic conditions were initially assumed to be the cause for amorphization. Therefore, high pressure compression using helium as a PTM was carried out to evaluate whether the previously observed amorphization is an indication of a frustrated phase transition to a higher density crystalline phase. Helium remains a liquid under compression up to a pressure of 12.1 GPa at 300 K. He has the lowest bulk modulus, hence the highest compressibility, of any known solid. It remains extremely soft with minimal nonhydrostatic stresses up to 150 GPa. Use of such a soft PTM is vital to investigations of structural changes under pressure with the minimum degree of deviatoric stress. Under RT compression in He PTM, the ambient phase of La2Sn2O7 is stable until a new phase emerges at 49.3 GPa. The transition goes to completion by 61 GPa (see Figure 2 (RHS)). Raman spectroscopy confirms the phase transition. The Raman band positions increase and intensities attenuate until all the bands disappear by 36 GPa (Figures S3 and S4, Supporting Information). After 36 GPa, the pattern is associated with an amorphous form’s density of states. However, the XRD data show a phase coexistence that makes it evident that the phase transition is kinetically hindered. The sluggish structural transition over such a pressure range leaves the new phase stressed and/or disordered as may be seen from the Debye–Sherrer rings (Figure 2). The phase coexistence of the high pressure and ambient systems confirms the first order nature of this transition. It is critical to note that due to the nature of the kinetically hindered first order transition, even using the softest available PTM is not sufficient to allow access to a fully crystalline state. This type of kinetically hindered phase transition is seen in many other examples of pyrochlore materials under pressure.

As Fd3m La2Sn2O7 remains highly crystalline under quasi-hydrostatic compression until 49.3 GPa, the equation of state (EoS) can be determined. The unit cell parameters extracted from the XRD data using Le Bail refinement (Figure S5 and Table S3, Supporting Information) show a 6.15% decrease in the cubic lattice constant from ambient pressure to 49.3 GPa. The third order Burch–Murnaghan (BM) EoS gives a bulk modulus of K0 = 183(4) GPa, K0′ = 3.7(3), and a reference volume of V0 = 153.15(1) Å3. At first glance, the BM EoS appears to describe the expected response of the system during compression with a tight fit of the V(P) data (Figure 3, inset).

However, the compression data is very oscillatory around the fit to a linearized form of the BM relation. The linearized form uses the Eulerian-finite strain (ḟ) vs normalized pressure (P), and it gives K0 = 188(3) and K0′ = 3.8(2) from the y-axis intercept and gradient of the linear fit, respectively. Rietveld refinement can be attempted to monitor the displacement of the free oxygen position (i.e. X in the archetypal stoichiometry with crystallographic label O2). O2 is the only atom in the asymmetric cell with a coordinate not set by the crystal symmetry, and it is likely the origin of the oscillatory behavior. However, in this case and the initial heating experiment, reliable statistics could not be extracted due to the presence of the heavier cations and their significantly higher X-ray scattering contribution.

As O2 could not be monitored experimentally, the response of the internal geometry to strain was simulated by creating a series of structures at differing volumes. The volumes were created by changing the lattice constant of the ambient structure and optimizing the atomic coordinates. By comparing the geometric parameters before and after the optimization, only the O2 atoms moved. Every other atom stayed on its Wyckoff site. Parsing the material into the conventional...
pyrochlore sublattices (A<sub>x</sub>Y and B<sub>x</sub>X<sub>x</sub>) confines the distortions in the geometry to the Sn sublattice. All the bond and dihedral angles in the Sn sublattice would remain constant if O<sub>2</sub> is kept fixed, yet Figure 4 shows they diverge from those values upon compression. In a perfectly regular octahedron, the O–Sn–O bond angles and the dihedral angles between the basal planes and the primary axes would all be 90°. Even without compression, the SnO<sub>6</sub> octahedra are irregular. This irregularity only increases upon compression. The picture that arises is that the SnO<sub>6</sub> octahedra are twisting and compressing the SnO<sub>6</sub> tetrahedral cages while their outward facing angles shrink to accommodate. Similar monotonous distortions from regularity are also observed in the LaO<sub>8</sub> cuboids. The combined effects of these rotations with the internal stresses preventing them in a real, nonannealed material is the cause of the observed oscillations in F(f).

The resistance to compression of the Sn–O bond and the decrease of the Sn–O–Sn angle signal a covalent nature to the bonding in the Sn sublattice, the metal–oxygen–metal angle in compounds is known to be a marker of the covalency of the bond. A strong overlap of Sn s states and O<sub>2</sub> p states at the bottom of the valence band around −6 eV exists in the site and angular momentum projected density of states for Fd<sub>3</sub>m La<sub>2</sub>Sn<sub>2</sub>O<sub>7</sub> (Figure S6, Supporting Information). Inspection of the band decomposed charge density shows 6 bands that are clearly a linear combination of Sn–O bonding orbitals wrapping around the SnO<sub>6</sub> tetrahedral cages (Figure 5). All the other bands in the valence band appear to be linear combinations of O 2p lone pair orbitals, although those closest in energy to the Sn–O2 covalent bands show a polarization toward the Sn atoms (Figure S7, Supporting Information). There is also an overlap between La p states and O1 s states around −12 eV. However, inspection of the band decomposed charge densities does not show signs of covalency (Figure S8, Supporting Information). The La–O overlap is just a fortuitous energetic overlap of semivalent atomic states. The bonding in the system is ionic between La and O and at least partially covalent between Sn and O2. In a three-center covalent bond between a metal–oxygen–metal unit, one of the metal–oxygen bonds disproportionates into an oxygen lone pair, while the other bond smears out over all three atomic centers. This provides a bond order of 0.50 for each metal–oxygen connection. There are 6 strongly covalent bands in La<sub>2</sub>SnO<sub>6</sub> primitive cell for 24 Sn–O2 connections, an apparent bond order of 0.25. This means that twice as many bond–lone pair disproportionations have occurred than in a three-center covalent bond, or that some of the bands that visually appear to be linear combinations of oxygen lone pair orbitals may actually be part of the covalent network. Either way, the oxygens in the Sn sublattice have more ionic character than if they had single or three-center covalent bonds to the Sn atoms.

**High Pressure Crystalline Phase.** The kinetic hindrance of the phase transition at 61 GPa, even in a helium PTM, prevents any reliable indexing of the unit cell of the newly accessed high density phase based on the quasi-hydrostatic compression data. AIRSS was employed to help identify the unknown phase. The structure searches made use of space group symmetry and allowed up to 4 formula units per unit cell. The only constraints placed on the generated structures were minimum interatomic distances to prevent sampling unreasonable structures: O–O 2.53 Å, O–Sn 1.96 Å, O–La 2.31 Å, Sn–Sn 3.26 Å, Sn–La 3.29 Å, and La–La 3.65 Å. AIRSS identified three possible, energetically viable solutions: P<sub>2</sub>1/c, 0 meV; C2<sub>1</sub>/c, 105 meV; and Pbn<sub>2</sub>, 177 meV (Figure S9, Supporting Information). However, the quality of the XRD pattern is insufficient to permit a reliable match even with the AIRSS solutions. Our inability to index the new phase makes the need to thermally anneal this (or any) kinetically hindered structural phase transition quite clear, independent of the choice of PTM.

To that end, an alternative type of sample loading was prepared to test different thermal annealing conditions while in the thermodynamic stability region of the new high density phase. The top inset in Figure 6 shows the quadrant layout of the La<sub>2</sub>SnO<sub>6</sub> loading in a DAC at 67 GPa in a NaCl PTM. Each quadrant was laser heated with increased power density (lowest power and duration), most of the features are from the NaCl PTM. The NaCl features persist in the other XRD patterns but become less dominant as features from the sample take precedence. Laser annealing at or above 3.9 MW/cm<sup>2</sup>, quadrants 2–4, produces a crystalline sample with a varying degree of crystallinity. The crystallinity increases with temperature. The highest intensity (quadrant 4, 8.0 MW/cm<sup>2</sup>) for a
build-up of elemental Sn upon compression is most likely an extreme temperatures and pressures, so the previous report of a concern in high temperature experiments, but there is no pressure) upon heating. Decomposition/disproportionation is R AIRSS calculations (Figure 7, AIRSS solution at c 5.75590(2), b = 5.3657(6) Å, c = 9.7935(5) Å, β=90.381(5°). Rietveld refinement reveals the same P21/c phase (Figure 7, a = 9.39975(9), b = 5.75590(2), c = 10.68544(7) Å, β=89.9341(1)°, wR_p = 2.0% and R_p = 1.1%) when the sample is decompressed back down to ambient pressure. The quality of the data enabled full refinement of all the atomic position in the cell (Table S4, Supporting Information). This includes the anion positions, thus providing a reliable structure model of the new phase.

During the laser heating experiments, it can be estimated that quadrant 4 achieved a temperature in excess of 2500 K. This demonstrates a robust thermal stability of the P21/c phase quite similar to the Fd3m phase at ambient conditions. MD simulations show that a single unit cell of the P21/c phase remains crystalline at 70 GPa and 5000 K with a 7.17% volume expansion (Figure 8). The volume expands through a dilation of the b- and c-crystallographic axes coupled with a slight contraction of the a-axis. More remarkably, a cubic unit cell of the Fd3̅m phase at 70 GPa and 5000 K appears to transform into the P21/c phase (Figure 8), albeit without perfect crystalline ordering. A primitive unit cell of the Fd3̅m phase transforms into a cell resembling the C2/c AIRSS solution at 70 GPa and 5000 K. A primitive Fd3̅m cell contains only 22 atoms, so it cannot access the 44 atom P21/c cell. In contrast, a cubic unit cell of the Fd3̅m phase at 70 GPa and 2000 K remains in the same phase. This shows that the small box size is artificially stabilizing the Fd3̅m phase compared to experiment. However, a large enough thermal kick overcomes the artificial stabilization and allows the system to access one of the more favorable high pressure polymorphs. Though the length and time scales of the MD simulations are too small to properly show nucleation or melting, they are of sufficient quality to confirm the following: the Fd3̅m phase transforms into the P21/c phase at high pressure and temperature, and the P21/c phase is thermally stable up to at least the experimental temperatures (by comparison the Fd3̅m phase melts by 5000 K at 0 GPa).

As in the Fd3̅m phase, the site and angular momentum projected density of states for P21/c La₃Sn₃O₇ at 70 GPa shows a strong overlap of Sn s states and O p states for the 8 bands at the bottom of the valence band (Figure S10, Supporting Information). The band decomposed charge densities for these bands show a covalency between the Sn and O. Unlike the covalency in the Fd3̅m phase, the Sn–O covalent network does not connect with all the oxygen atoms in the SnO₆ octahedra. The network is square bipyramidal with one oxygen per octahedra not connected (i.e. no density between the Sn and O). These noncovalent oxygens are the same atoms in each SnO₆ octahedra that is not connected to another Sn but rather is a part of 3 La atoms’ polyhedra. That connectivity is clearly driving their bonding to be predominantly ionic, like O1 in the Fd3̅m phase. Eight bands describing 8 octahedra each with 5 Sn–O connections gives an apparent Sn–O bond order of 0.20, lower than that in the Fd3̅m phase. Also like the Fd3̅m phase, the band below the valence band exhibits density overlap between La and O atoms. However, in this case it is more clearly just an energetic overlap of semivalent states. The charge densities of the bands are even more obviously atom localized than in the Fd3̅m phase (Figure 9). The ambient P21/c structure has the same electronic structure as the 70 GPa structure (Figure S11, Supporting Information), and the perseverance of the Sn–O covalent network provides an explanation as to why the phase is easily recoverable to ambient conditions.

Considering these results, it is now clear why this material exhibits a kinetically hindered first order phase transition. It is transitioning from one covalent network about the Sn atoms to another. The Sn octahedra in the P21/c phase are even less regular than in the Fd3̅m phase. The Sn–O distances now vary for each atom, and each of the three planes containing 4 O and the Sn are no longer flat. The oscillations in the F(0) EoS (Figure 3) are now more easily explained as the resistance of
the covalent network to compression coupled with the pressure induced phase coexistence and its accompanying transformation of the character of the covalent network, leading to anisotropic strains. The covalent to covalent translation is the source of the frustration in the phase transformation and is also the likely cause behind the previously observed frustrated phase transformations in other pyrochlores. By comparison to previous studies, we can assert that the covalency in pyrochlores should decrease in the order Sn > Ti > Zr. The leading cause of amorphization is antisite defects and a sublattice with increased covalent character should more strongly resist those defects. Therefore, Sn pyrochlores should be the more stable and tolerant to radiation damage crystalline materials, especially in their high pressure annealed phases.

Implications for Tc Pyrochlores. Despite all the interest in actinide and lanthanide pyrochlores, there has only been one study to date investigating technetium pyrochlore oxides. However, Tc pyrochlore oxides represent an interesting candidate waste form material. For instance, unlike actinides, is a weak β emitter (293 keV), so the material would experience a significantly reduced amount of radiation-induced amorphization. Tc is only known to

**Figure 7.** A comparison of XRD patterns of the various states of the sample investigated, from bottom: (a) ambient phase, (b) recovered P21/c: (a = 9.39975(9), b = 5.75590(2), c = 10.68544(7) Å, β = 89.9341(1)°), (c) P21/c postlaser-heating at 67 GPa (a = 8.3376(4), b = 5.3657(6), c = 9.7935(5) Å, β = 90.381(5)°), (d) quasi-hydrostatically compressed at 61 GPa, (e) nonhydrostatically compressed at 75 GPa, and (f) recovered nonhydrostatically compressed.

**Figure 8.** Final snapshots of the MD simulations at 70 GPa and 5000 K of a P21/c (left) unit cell along (001, top) and (100, bottom), and an Fd3m (right) unit cell along (100, top) and (001, bottom). La−O connectivities not shown, and the colors are the same as in Figure 5.

**Figure 9.** (left, middle) Representative charge density of Sn−O covalent bonding bands in P21/c La2Sn2O7. (right) A representative band where the La and O densities of state exhibit overlap. The colors are the same as those in Figure 5.
present as Tc(IV) and Tc(VII) in solid-state oxides. Tc would need to occupy the B-site as Tc(IV), as shown to be the case in lanthanide (but not La) Tc pyrochlores. Tc(IV) species have generally low volatility and are also much more readily retained chemically compared to higher valent oxo species. Tc(IV) is also the most environmentally immobile form. Immobilizing 99Tc(IV) in a stable material would provide an ideal long-term storage solution. It would also eliminate the issue of upward of 70% of the Tc volatilizing away during vitrification at \( \sim 1100 \) °C into a borosilicate glass, the current strategy for a 99Tc waste form at the Hanford site. Some groups have attempted to trap Tc(IV) as a dopant in iron-oxide materials such as magnetite, Fe3O4. When a Tc-doped magnetite sample is heated to 600 °C, the surface Tc oxidizes and volatilizes off. By 700 °C, even the bulk Tc migrates to the surface, oxidizes, and volatilizes off. The inability of that material to retain Tc(IV) significantly reduces its utility for vitrification or storage in geologic repositories.

A thermally stable material that better incorporates Tc(IV) would be an ideal waste form. We have already demonstrated that La2Sn2O7 is a thermally stable material to upward of 2000 °C in both of its phases. It would be quite significant if La2Tc2O7 is analogous to La2Sn2O7. There is reason to believe that is the case given the similarities between Tc and Sn: Tc is known to form covalent bonds with O, the covalent radius of Sn is 1.40 Å and 1.38 for Tc. The electronic structure of the octahedral Sn(IV) is 0.69 Å compared to 0.645 Å for Tc(IV). The electronic structure of \( \text{Fe}_3\text{Si}_2\text{O}_7 \) at 0 GPa and \( \text{P}_2\text{O}_5 \) at 70 GPa can be compared to that of La2Sn2O7, to test for a similarity between the materials. The Tc pyrochlore structures were obtained by substituting Tc for Sn and allowing the structure to fully relax. Tc(IV) has three d electrons that are not ionic or bonding with the ligands. As the Tc atoms are surrounded by ligand, those d electrons may localize entirely on-atom. To account for the potential localization, the rotationally invariant single parameter Hubbard DFT+U correction \( U_{\text{eff}} = 4.0 \) eV was applied to the Tc d states along with a high spin guess. Ferromagnetic (FM) ordering was used because it is the simplest spin ordering for on-atom localization. While other spin orderings may have lower energy, the FM solution’s geometry and electronic structure will be similar enough to make general conclusions.

The partial density of states for \( \text{Fe}_3\text{Si}_2\text{O}_7 \) at 0 GPa and \( \text{P}_2\text{O}_5 \) at 70 GPa show that the Tc to Sn analogy holds true (Figures S12 and S13, Supporting Information). The key difference between the two systems is the nature of the B-site d electrons. The 4d electrons in Sn are semivalent, whereas in Tc they sit above the oxygen lone pairs at the top of the valence band. Both structures adopted the anticipated atom localized d electrons \( S = \frac{3}{2} \). The value of \( U_{\text{eff}} \) was chosen based on a study of another Tc(IV) oxide, \( \text{TcO}_2 \), so it should be reliable and transferable to this problem. However, this behavior raises interesting questions about the phase diagram. Is there a high pressure transition to a semimetallic or fully metallic state? Where do metallic transitions happen relative to the structural phase transition into the \( \text{P}_2\text{I}_2\text{I} \) phase? How are the metallic transitions affected by changing the identity of the A-site cation? The answer to those questions could have great ramifications on the preparation of Tc pyrochlores and their long-term behavior in a repository.

**CONCLUSION**

Several different methods and approaches were undertaken to provide an in-depth understanding of La2Sn2O7, its responses to temperature and pressure, and the underlying chemistry behind it.Beginning with the ambient conditions characterization of the starting material, this work reveals a high purity single phase material with a marked thermal stability owing to the covalent network covering the Sn sublattice. Non-hydrostatic compression leads to pressure-induced amorphization, while quasi-hydrostatic conditions reveal La2Sn2O7 undergoing a kinetically hindered first order phase transition beginning around 49.3 GPa. It can be deduced that the kinetic hindrance combined with no PTM leads to deviatoric stresses which cause pressure-induced amorphization. Laser annealing is required to fully transform compressed La2Sn2O7 into its high pressure phase. Structure searching, molecular dynamics, and Rietveld refinement identify the high pressure phase as \( \text{P}_2\text{I}_2\text{I} \) symmetry. Inspection of the electronic structure of the \( \text{P}_2\text{I}_2\text{I} \) phase reveals a covalent network about the Sn atoms that differs from that of the \( \text{Fd}_3\text{m} \) phase. The large change required to facilitate the transition between the two different bonding networks is the leading cause of the kinetic hindrance. On the other hand, the persistence of the bonding in the \( \text{P}_2\text{I}_2\text{I} \) phase to ambient conditions is a likely reason behind its recoverability. It is interesting to consider which
La$_2$Sn$_2$O$_7$ have very similar electronic structures in both the 

This work aimed to explore structure properties in pyrochlores to consider the implications for their improved usage as waste forms for radionuclides. La$_2$Tc$_2$O$_7$- and La$_5$Sn$_2$O$_7$ have very similar electronic structures in both the Fd$ar{3}$m and P$_2_1$/c phases. This provides a new candidate waste material that could trap Tc in its environmentally immobile Tc(IV) state and simultaneously be robust against pressure and temperature. Nonhydrostatic compression shows promise as a route for preparing initially amorphous waste forms for other radionuclides. However, the 61 GPa amorphization pressure is likely too high for practical preparations. The choice of the A- and B-site cations (or mixed compositions) will need to be carefully considered to balance the robustness of the covalent network and the mechanical work required for either pressure-induced amorphization or accessing a crystalline phase more tolerant of extreme conditions. The build-up of radiation damage at different pressures will be a vital additional input into the system’s energy landscape. High pressure experiments on ion irradiated samples need to be done to further understand the structural stability of nuclear waste forms. The introduction of temperature to radioactive samples under pressure can potentially reveal even more insights. The interplay between pressure and radiation induced structural transformations.

**ASSOCIATED CONTENT**

Supporting Information

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**AUTHOR INFORMATION**

**Corresponding Authors**

*E-mail: salamat@physics.unlv.edu.*

*E-mail: keith.lawler@unlv.edu.*

**ORCID**

Keith V. Lawler: 0000-0003-1087-5815

Andrew L. Hector: 0000-0002-9964-2163

**Notes**

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