Flyback Converter with Quadratic Pre-Stage

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Abstract: - A flyback converter with an additional step-down stage with a tapped inductor is presented. The function of the converter is described and the voltage transformation rates for the continuous mode are derived. The dimensioning equations for the devices are given. The dynamic model is calculated and simulations are shown. The converter enables an isolated output and shows a wide range in the transformation rate. It is especially useful for small solar applications in addition to a micro-inverter.

Key-Words: - DC/DC converter, flyback converter, quadratic, modelling, simulation, dimensioning

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1 Introduction

The converter (Fig. 1) consists of a flyback stage with the active switch S1, the coupled inductors N_{21} and N_{22}, a secondary diode D_3 and an output capacitor C_2, and a first stage built with two magnetically coupled windings N_{11} and N_{12} (built as a tapped inductor or as an autotransformer), a capacitor C_1 and two diodes D_1, D_2. This first stage brings an additional quadratic step-down factor into the voltage transformation rate of the flyback converter. This converter is especially useful for high step-down ratios and when isolation of the output is necessary. For the whole area of power electronics and for the flyback converter cf. [1-3], the basic text for converters with a quadratic term in the voltage transformation rate is [4]. An overview of four converters with a low-side switch and tapped inductors at the output side is presented in [5]. Similar circuits, but with a tapped inductor at the input side, are treated in [6]. Further concepts and hints for the control can be found in [7-12]. The flyback part of the converter and the coupled windings in the pre-stage enable the designer to adapt input and output voltages with a large difference. The potential separation is another advantage of this converter, especially for security reasons. The converter has two modes in the continuous mode: mode M1 S and D_1, and mode M2 D_2 and D_3 are conducting. As with all flyback-based converters, the power range is up to about 200 W, because the energy which has to be transferred must by stored first in the magnetic elements.

2 Basic function in the steady-state case

For the description of the circuit in the steady-state case we assume ideal devices (that means no losses, and infinitesimally small switching times), continuous operation, and the capacitors are so large that the voltage across them does not change during one switching period (if we allow a significant voltage ripple, especially across C_1, one has to use the mean value). When the active switch is on (also diode D_1 is on during this mode), the input voltage U_1 minus the voltage across C_1 is across the series connection of the coupled windings N_{11} and N_{12}.

Fig. 1. Quadratic flyback converter with pre-stage.

The voltage across the separate windings can be calculated by the transformer law. The voltage across the capacitor is impressed on the primary winding N_{21} of the flyback transformer. When the switch S is turned off, the current through the coupled winding can only flow in the winding N_{12} and commutates to D_2. The magnetic flux has to be steady, therefore also the ampere windings have to
be steady and the current through $N_{12}$ must spring to a higher value so that the ampere windings do not change. The flyback transformer is demagnetized with the help of the secondary winding $N_{22}$. Therefore, one can write for the voltage-time balance for the winding $N_{12}$ and for the winding $N_{22}$

$$\frac{N_{12}}{N_{11} + N_{12}} (U_i - U_C) d = U_C (1 - d),$$

(1)

$$U_{cl} \frac{N_{22}}{N_{21}} d = U_2 (1 - d)$$

(2)

respectively. So one can write for the voltage across $C_1$ and the output voltage $U_2$ in dependence on the input voltage and with the duty cycle $d$ (the turn-on time of the active switch divided by the switching period) for the ideal converter in continuous inductor current mode

$$U_C = \frac{N_{12}}{N_{11} + N_{12} - N_{11} d} dU_i$$

(3)

$$U_2 = \frac{d^2}{1-d}(\frac{N_{12}}{N_{11} + N_{12} - N_{11} d}) \frac{N_{22}}{N_{21}} U_i$$

(4)

Choosing a winding ratio of one to one for $N_{11}$ to $N_{12}$ simplifies to

$$U_2 = \frac{d^2}{1-d}(\frac{1}{2-d}) \frac{N_{22}}{N_{21}} U_i.$$  

(4a)

Fig. 2 shows the voltage transformation rate for different winding ratios of the flyback stage. The coupled windings are chosen as bifilar windings with the winding ratio one to one. One can see that the converter has also a large voltage transformation factor when the winding ratio $N_{22}/N_{21}$ is high. When a small winding ratio is used, the converter is especially useful for step-down applications.

### 3 Voltage stress of the semiconductors

The normalized stress of the semiconductors can be calculated with the help of Kirchhoff’s voltage law (KVL). It is not helpful to replace the duty cycle by the output voltage, because these formulae would get very confusing. Therefore, we calculate them only in accordance to the duty cycle. From the input and the output voltage range for a given application the necessary duty cycle to achieve the highest stress has to be calculated and inserted into (5a, 6, 7, 8), respectively. This leads to maximum values. It is evident that the used devices must be chosen with a security factor of 30 to 100% depending on the application.

To get a clearer comprehension of how to get the voltage stress across the semiconductors, the voltages across the active switch $S$ and the three passive switches $D_1$ to $D_3$ are depicted in the figures Fig. 3 to Fig. 6.

Fig. 3 shows the voltage across the active switch. The voltage stress can be calculated during mode M2 according to

$$U_5 = U_{cl} \frac{N_{11} + N_{12}}{N_{12}} + U_1 + \frac{N_{22}}{N_{21}} U_2$$ .

(5)

Substituting the voltages across $C_1$ and the output voltage $U_2$ lead to the normalized voltage across the active switch

$$\frac{U_5}{U_1} = \frac{d^2 N_{11} - 2d N_{11} + N_{11} + N_{12}}{(N_{11} + N_{12} - d N_{11})(1-d)}.$$  

(5a)

Fig. 3. Voltage across the active switch $S$.

For the voltage across $D_1$ one gets

$$\frac{U_{D1}}{U_1} = -\frac{N_{11} + N_{12}}{(N_{11} + N_{12} - d N_{11})}.$$  

(6)
Fig. 4 shows the voltage across the diode D₁. 

For D₂ (Fig. 5) one gets

\[
U_{D2} = -U_1 + (U_1 - U_{C1}) \frac{N_{11}}{N_{11} + N_{12}}. \tag{7}
\]

This leads to

\[
\frac{U_{D2}}{U_1} = -\frac{N_{12}}{(N_{11} + N_{12} - dN_{11})}. \tag{8}
\]

Fig. 5 Voltage across D₂

For the necessary normalized reverse voltage of D₃ (Fig. 6)

\[
\frac{U_{D3}}{U_1} = -\frac{N_{22}}{N_{21}} \frac{dN_{22}}{(N_{11} + N_{12} - dN_{11})(1-d)}. \tag{9}
\]

Fig. 6 Voltage across D₃.

For the necessary normalized reverse voltage of D₃ for an equal number of windings of the coupled coils.

\[
\frac{U_{D3}}{U_1} = -\frac{N_{22}}{N_{21}} \frac{d}{(2-d)(1-d)}. \tag{10}
\]

4 Connection between the currents

To get an overview of the current stress of the elements, one has to inspect the currents through the capacitors. It is easy to construct the mean values of the currents. For the output capacitor one gets a graph which is shown in Fig. 7.

The current through the capacitor must be zero in the mean. Starting with the load current one can draw the current through the output capacitor (Fig. 7), (e.g. for a duty cycle of one third). Due to the charge balance one can write

\[I_{load} = I_{D3,2} - dI_{load}(1-d). \tag{11}\]

\(I_{D3,2}\) is the mean value of the current through D₃ referred to the duration of mode M2 and is equal to the mean value of the current during M2 through the secondary winding of the flyback transformer. During mode M2 the current through the secondary winding is therefore (Fig. 8)

\[I_{N22,2} = \frac{1}{1-d}I_{load}. \tag{12}\]
The current through the primary winding is zero in M2. The ampere-windings must be the same in the core. Therefore, one gets for the mean value of the current through $N_{21}$ in the first mode M1

$$I_{N21,1} = \frac{N_{21}}{N_{21}} \frac{N_{22}}{N_{21}} I_{Load}$$

(13)

Fig. 9 shows a sketch of the current through the primary winding with a winding ratio of $N_{21}:N_{22}=2:1$. The current during M1 in $N_{21}$ is half of the current through $N_{22}$ during M2. With the given winding ratio, we can draw the current through the primary winding, which has to be at the end of mode M1 half of the current as at the beginning of mode M2 in the secondary winding (the current linkage must be steady and the winding ratio is $N_{21}:N_{22}=2:1$).

$$I_{N21,1} = \frac{N_{21}}{N_{21}} \frac{N_{22}}{N_{21}} I_{Load}$$

(14)

Now one can construct the current through the second winding of the coupled coils during mode M2

$$I_{N12,2} = \frac{N_{11} + N_{22}}{N_{11} + N_{12} - dN_{11}} \frac{N_{22}}{N_{21}} \frac{d}{1-d} I_{Load}$$

(15)

The ampere-windings must be the same at the end of M1 and the beginning of mode two

$$I_{N11}(N_{11} + N_{12}) = I_{N12,2} N_{12}$$

(16)

This leads to

$$I_{N12,1} = \frac{N_{12}}{N_{11} + N_{12} - dN_{11}} \frac{N_{22}}{N_{21}} \frac{d}{1-d} I_{Load}$$

(17)

The mean value of the input current is therefore

$$I_1 = \frac{N_{12}}{N_{11} + N_{12} - dN_{11}} \frac{N_{22}}{N_{21}} \frac{d^2}{1-d} I_{Load}$$

(18)

5 Dynamic model of the converter

5.1 Calculating the state equations

The state variables which form the state vector are

$$\mathbf{x} = (\phi_1, \phi_2, u_{C1}, u_{C2})$$

(19)

The fluxes $\phi_1$, $\phi_2$ are the state variables for the coupled coils, because the flux in the magnetic elements has to be steady. The currents in the windings are not steady and can spring. This causes overvoltages due to the unavoidable stray inductances. To reduce these overvoltages, snubber networks or overvoltage limiters have to be used. One can use simple RCD snubbers or networks, which recuperate the energy which is stored in the stray inductance into the input or into the output side of the converter to increase the efficiency [1, 2]. The flux is proportional to the current, the proportional factor is called inductance. One has to use the induction law

$$\mathbf{u} = \frac{d}{dt} \mathbf{\psi} = \frac{d}{dt} \mathbf{\phi}$$

When the flux $\mathbf{\psi}$ is changing, a voltage is induced. For a concentrated winding with the number of turns $N$, one can use the flux per winding $\mathbf{\phi}$. Therefore, one can write during stage M1 for the induction law

$$\frac{d\psi_1}{dt} = N_{12} \frac{d\phi_1}{dt} = \frac{N_{12}}{N_{11} + N_{12}} (u_1 - u_{C1})$$

(20)

The inductance can be calculated with the $A_L$-factor and the square of the number of windings according to

$$(N_{12} + N_{12})\phi_1 = \psi_1 = L_{12} i = A_L (N_{12} + N_{12})^2 i$$

(21)

For the magnetic core of the flyback transformer one can write

$$\frac{d\psi_2}{dt} = N_{21} \frac{d\phi_2}{dt} = u_{C1}$$

(22)

The connection between flux and the causing current

$$N_{21} \psi_2 = \phi_2 = A_L N_{21}^2 i$$

(23)

enables us to write for the derivatives of the voltages across $C_1$

$$\frac{du_{C1}}{dt} = \frac{1}{C_1} \left( \frac{\phi_1}{A_L (N_{11} + N_{12})} - \frac{\phi_2}{A_L N_{21}} \right)$$

(24)
During mode M2 the diodes D2 and D3 are conducting, the derivatives of the fluxes are therefore

\[
\frac{d\phi_{1}}{dt} = -\frac{u_{c1}}{C_{1}} \tag{27}
\]

\[
\frac{d\phi_{2}}{dt} = -\frac{u_{c1}}{C_{2}} \tag{28}
\]

With the help of the flux linkages

\[
N_{12}\phi_{1} = \psi_{1} = A_{N}N_{12}, i \tag{29}
\]

\[
N_{22}\phi_{2} = \psi_{2} = A_{N}N_{22}, i \tag{30}
\]

one can write for the state equations of the capacitors

\[
\frac{du_{c1}}{dt} = \frac{\phi_{1}(A_{N}N_{12})}{C_{1}} \tag{31}
\]

\[
\frac{du_{c2}}{dt} = \frac{\phi_{2}(A_{N}N_{22})-u_{c2}}{C_{2}} \tag{32}
\]

Summarized in a state-space description one gets for mode M2

\[
\frac{d}{dt} \begin{pmatrix} 
\hat{\phi}_{1} \\
\hat{\phi}_{2} \\
\hat{u}_{c1} \\
\hat{u}_{c2}
\end{pmatrix} = \begin{pmatrix} 
0 & 0 & -\frac{1}{N_{12}} & 0 \\
0 & 0 & 0 & -\frac{1}{N_{22}} \\
\frac{1}{A_{N}N_{12}C_{1}} & 0 & 0 & 0 \\
0 & \frac{1}{A_{N}N_{22}C_{2}} & 0 & -\frac{1}{C_{2}R}
\end{pmatrix} \begin{pmatrix} 
\hat{\phi}_{1} \\
\hat{\phi}_{2} \\
\hat{u}_{c1} \\
\hat{u}_{c2}
\end{pmatrix} \tag{33}
\]

### 5.2 Large signal model

Combining the equations for both modes by averaging leads to the nonlinear model (state space averaging)

\[
\frac{d}{dt} \begin{pmatrix} 
\hat{\phi}_{1} \\
\hat{\phi}_{2} \\
\hat{u}_{c1} \\
\hat{u}_{c2}
\end{pmatrix} = \begin{pmatrix} 
0 & 0 & -\frac{N_{11}+N_{12}-dN_{11}}{(N_{11}+N_{12})N_{12}} & 0 \\
0 & 0 & 0 & \frac{d}{(N_{11}+N_{12})N_{12}} \\
\frac{1}{A_{N}N_{11}C_{1}} & 0 & 0 & 0 \\
0 & 0 & 0 & -1
\end{pmatrix} \begin{pmatrix} 
\hat{\phi}_{1} \\
\hat{\phi}_{2} \\
\hat{u}_{c1} \\
\hat{u}_{c2}
\end{pmatrix} \tag{34}
\]

This model can be linearized and that leads to a small-signal model from which the transfer functions can be derived. Furthermore, one gets also the connection between the working point values.

### 5.3 Small signal model

All variables are written as the sum of the working point value marked by a capital letter with a 0 in the index and a perturbation term of this variable, marked by a small letter with a roof on top. This results in a small signal model around the operating point

\[
\frac{d}{dt} \begin{pmatrix} 
\hat{\phi}_{1} \\
\hat{\phi}_{2} \\
\hat{u}_{c1} \\
\hat{u}_{c2}
\end{pmatrix} = A \begin{pmatrix} 
\hat{\phi}_{1} \\
\hat{\phi}_{2} \\
\hat{u}_{c1} \\
\hat{u}_{c2}
\end{pmatrix} \tag{35}
\]

With the abbreviations for the matrixes

\[
A = \begin{pmatrix} 
0 & 0 & -\frac{N_{11}+N_{12}-dN_{11}}{(N_{11}+N_{12})N_{12}} & 0 \\
0 & 0 & 0 & \frac{d}{(N_{11}+N_{12})N_{12}} \\
\frac{1}{A_{N}N_{11}C_{1}} & 0 & 0 & 0 \\
0 & 0 & 0 & -1
\end{pmatrix}
\tag{36}
\]
With the working point flux of the flyback from the common form and the determinant calculus, the transfer function system can be transformed into the frequency domain. The state-space description combines the differential equations into one matrix system. The linear model can be used to calculate the load current connection of the flux in the flyback transformer with the load current:

\[
0 = \frac{D_0}{N_{11} + N_{12}} + \frac{1-D_0}{N_{11}} U_{C10} + \frac{D_0}{N_{11} + N_{12}} U_{C20}.
\]

From this equation one gets again (3). The second line leads to

\[
\frac{D_0}{N_{11}} U_{C20} = \frac{1-D_0}{N_{22}} U_{C20}.
\]

By easy calculation we get again (4). From

\[
\left( \frac{D_0}{A_2 (N_{11} + N_{12}) C_1} + \frac{1-D_0}{A_2 N_{12} C_1} \right) \Phi_{10} = \frac{D_0}{A_1 N_{12} C_1} \Phi_{20} = 0
\]

With the working point flux of the flyback transformer \( \Phi_{20} \) one gets for the flux at the working point in the first coupled coils \( \Phi_{10} \)

\[
\Phi_{10} = \frac{N_{11} + N_{12}}{N_{11} + N_{12} - D_0 N_{11}} \frac{D_0}{N_{21}} \Phi_{20}.
\]

From the last line of (34) we get the working point connection of the flux in the flyback transformer with the load current

\[
\frac{1-D_0}{A_1 N_{22} C_2} \Phi_{20} = \frac{U_{C20}}{R} = I_{LOAD}.
\]

### 5.4 Working point values

Also the connections of the working point values result from the linearization process. From the first line of (34) one gets

\[
0 = \left( \frac{D_0}{N_{11} + N_{12}} + \frac{1-D_0}{N_{12}} \right) U_{C10} + \frac{D_0}{N_{11} + N_{12}} U_{C10} = 0.
\]

The numerator for the transfer function \( U_{C32}/D \) for the control signal can be written as (using Cramer’s law)

\[
Z_D = B_{22} s^3 + A_{22} B_{22} s^2 + \left( A_{22} A_{23} B_{32} - (A_{21} A_{22} + A_{21} A_{32}) B_{42} \right) s + A_{23} A_{24} A_{42} = s^4 + a_3 s^3 + a_2 s^2 + a_1 s + a_0
\]

The numerator of the disturbance output transfer function \( U_{C2}/U_1 \) is given by

\[
Z_{U1} = A_{23} A_{24} B_{32} = c_0.
\]

The transfer function between the output voltage \( U_2(s) \) and the control signal \( D(s) \) can be written according to

\[
G_{U2D}(s) = \frac{U_2(s)}{D(s)} = \frac{b_3 s^3 + b_2 s^2 + b_1 s + b_0}{s^4 + a_3 s^3 + a_2 s^2 + a_1 s + a_0}.
\]

For the influence of the disturbance (changes of the input voltage) one gets the transfer function

\[
G_{U2D}(s) = \frac{U_2(s)}{U_1(s)} = \frac{c_0}{s^4 + a_3 s^3 + a_2 s^2 + a_1 s + a_0}.
\]

### 5.5 Transfer function

The linear model can be used to calculate the transfer functions. These are useful for designing the controller, for drawing Bode plots and for doing simulations. The state-space description combines the differential equations into one matrix system. With the help of the Laplace transformation this system can be transformed into the frequency domain (s-domain). This leads to a linear equation system of forth order. Using Cramer’s algorithm and the determinant calculus, the transfer function can be calculated (another way is to construct a signal flow graph and apply Mason’s rule). Starting from the common form

\[
B = \begin{bmatrix}
\frac{D_0}{N_{11} + N_{12}} & \frac{U_{C10} N_{11} + U_{C12} U_{C10}}{(N_{11} + N_{12}) N_{12}} & \frac{U_{C10} + U_{C20}}{N_{11} + N_{12}} \\
0 & \frac{D_0}{N_{11} + N_{12}} & 0 \\
0 & -\frac{N_{11} N_{22} \Phi_{10} - \Phi_{20} (N_{11} + N_{12}) N_{12}}{A_2 (N_{11} + N_{12}) N_{12} N_{22} C_1} & 0
\end{bmatrix}
\]

\[
\frac{d}{dt} \begin{bmatrix}
\hat{\phi}_1 \\
\hat{\phi}_2 \\
\hat{\phi}_1 \\
\hat{\phi}_2
\end{bmatrix} = \begin{bmatrix}
0 & 0 & A_{13} & 0 \\
0 & A_{23} & A_{34} & 0 \\
0 & A_{42} & 0 & A_{44} \\
0 & B_{11} & B_{12} & 0
\end{bmatrix} \begin{bmatrix}
\hat{u}_1 \\
\hat{u}_2 \\
\hat{u}_1 \\
\hat{u}_2
\end{bmatrix}
\]

\[
B_1 \begin{bmatrix}
\hat{u}_1 \\
\hat{u}_2 \\
\hat{u}_1 \\
\hat{u}_2
\end{bmatrix} = 0
\]

6 Dimensioning

### 6.1 Dimensioning of the output capacitor \( C_2 \)

During the on-time of the active switch S, the capacitor has to supply the load. Choosing a voltage ripple \( \Delta u_{C2} \), the voltage decreases during M1 according to

\[
\Delta u_{C2} = \frac{1}{C_2} \int_0^t I_{Load} dt.
\]

Solving and rearranging leads to

\[
C_2 = \frac{1}{\Delta u_{C2}} \frac{I_{Load}}{f}.
\]
The equivalent series resistor of the capacitor causes a higher capacitor value.

6.2 Dimensioning of the coupled inductors \( N_{11} \) & \( N_{12} \)

With a chosen current ripple \( \Delta I_L \) when both windings are working in series, one gets for the inductor

\[
(N_{11} + N_{12})^2 A_L = \frac{(U_i - U_{C1})d}{\Delta I_L f} \quad (51)
\]

When a bifilar winding is chosen, one has to split the complete winding into two halves. Details how to dimension the necessary air gap are similar to the described procedure for the flyback transformer.

6.3 Dimensioning of the fly-back transformer

For the primary winding one can calculate using the on-time of the active switch and a chosen current ripple \( \Delta I_{LN21} \)

\[
L_{N21} = \frac{U_{C1} d}{\Delta I_{LN21} f} \quad (52)
\]

The energy, which is stored in the magnetic core, consists of the energy in the ferrite material and in the air gap. From the theory of magnetics one knows the equation for the energy density

\[
\frac{B^2 H}{2} = \frac{W_{Mag}}{V} \quad (53)
\]

This leads for the magnetic circuit with an airgap to

\[
\frac{B^2}{\mu_0 H_r} V_{Fe} + \frac{B^2}{\mu_0} V_{Air} = \frac{LI^2}{2} \quad (54)
\]

Due to the fact that the relative permeability \( \mu_r \) of ferrite is much higher than that of the air which is only one, one can see that the energy is primarily stored in the air gap! One can now write approximately for the air gap volume \( V_{Air} \) and the air gap length \( l_{Air} \)

\[
V_{Air} \approx \frac{LI^2}{B^2} = \frac{I_{Air} A_{Fe}}{B^2} \quad (55)
\]

For a given core with a cross section of \( A_{Fe} \), a maximal allowable flux density \( B \) and a peak current \( I \) the necessary air gap can be calculated according to

\[
l_{Air} = \frac{LI^2}{B^2} \frac{\mu_0}{A_{Fe}} \quad (56)
\]

The so-called \( A_L \)-value for the chosen core depends on the air gap and can be found in the data sheet. The value of the inductor depends on this \( A_L \)-value multiplied by the square of the turns

\[
N_{21} = \frac{L_{N21}}{A_L} \quad (57)
\]

The inductance of the secondary winding can now be calculated with the help of

\[
L_{N22} = A_L N_{22}^2 \quad (58)
\]

7 Simulation

To get a better comprehension of the circuit, simulations with LT-Spice were done. The current through the load, the input voltage, the voltage across the capacitor \( C_{1} \), and the output voltage are shown up to down in Fig. 10. To avoid overload of the currents and voltages, the converter is started with increasing duty cycle as done during soft-start of a real converter. The duty cycle increases within the first 15 ms. The voltage across the capacitor \( C_{1} \) and the output voltage increase therefore continuously without significant overshot. After the soft-start has finished, the stationary case is reached within two milliseconds. At 20 ms an input voltage step occurs. Within three milliseconds a new steady-state case is reached. After 25 ms a load step occurs. The load is increased and the load current is now nearly double as the original value. Within 3 ms the new steady-state case is reached. At 30 ms the duty cycle is decreased and therefore the output voltage and the load current decrease, too.

Fig. 10. Up to down: load current, duty cycle, input voltage, voltage across \( C_1 \), output voltage.
coupled windings in a steady-state case. The winding ratio of the flyback transformer is \(N_{21}:N_{22}=2:1\), the winding ratio of the tapped inductor is \(N_{11}:N_{12}=1:1\). The step in the currents can be seen clearly. The plots show up to down: the control signal of the active switch, the current through the secondary winding of the flyback transformer, the current through the primary winding of the transformer, the current through the second half, and the current through the first half of the tapped inductor. For the model converter the capacitors were chosen to 330 µF, the inductivity of the windings of the tapped inductor are 40 µH, the primary inductor and the secondary inductor of the flyback transformer were chosen to 33 µH and 8 µH, respectively.

Fig. 11. (up to down): gate signal, current through the secondary winding of the flyback transformer, current through the primary winding of the flyback transformer, current through second half of the tapped inductor, and current through first half of the tapped inductor.

8 Conclusions

A flyback converter with a quadratic input stage realized with a tapped inductor (or autotransformer) was analyzed and material for the design was given. The coupling between the windings of the tapped inductor and of the flyback transformer should be strong. When higher winding ratios are necessary, the stray inductance is higher and a recuperative snubber or an overvoltage limiter should be used. Due to the coupled inductors and the quadratic term in the voltage transformation ratio, the converter can be adapted to a wide voltage range. Only one active switch is necessary and has to be controlled. The circuit is useful for a power range of up to a few hundred watts.

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