Improved Multi-Verse Optimization (IMVO) Algorithm for Solving Economic Load Dispatch

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Abstract: This Paper Presents Improved Multi Verse Optimization (IMVO) to solve the economic load dispatch (ELD) problem. In this work the performance of basic MVO algorithm has been improved by hybridizing it with PSO algorithm. The objective of ELD Problem is to minimize the total generation cost by appropriate scheduling of load among generating units. The Proposed technique is applied for solving the ELD in two different test problems. At the end of this paper, the results obtained from MVPSO for solving ELD problem were compared with other well known existing methods which show MVPSO better than other techniques.

Keywords: IMVO, Economic Load Dispatch (ELD), Multi Verse Optimization (MVO), Particle swarm optimization (PSO)

I. INTRODUCTION

With large interconnection of electric networks, the energy crisis in the world, and continuous rise in prices, it is very essential to reduce the running charges of electricity generating unit. The efficient and optimum economic operation and planning of electric power generation systems have always occupied an important position in the electric power industry. By definition Economic Load Dispatch (ELD) can be defined as the method of determining the most efficient, low cost and reliable operation of a power system by generating electricity to supply the required load. The economic dispatch problem has been solved via many traditional optimization methods, including Gradient techniques, linear programming, Newton methods, and quadratic programming. Evolutionary programming is one of the technique to solve ELD problem, but it suffer from problem of iteration of dimensionality [1], meta-heuristic techniques such as genetic algorithm [3], bio-geography based algorithm [7], tabu search [8], grey wolf optimization [23], particle swarm optimization (PSO) [2], harmony search[16], hybrid gravitational search[15], cuckoo search (CS) [15] have successfully applied to ELD problem. In this paper ELD problem has been solved by improved multi-verse optimization(IMVO)

II. PROBLEM FORMULATION

The objective function of ELD problem is to minimize the total generation cost while satisfying the various constraint, when the required load of power system is being supplied. The objective function to minimized is given by the following equations:

\[ F_i(P_{gi}) = \sum_{i=1}^{n} \left( a_i P_{gi}^2 + b_i P_{gi} + c_i \right) \] (i)

Where:
- \( F_i \): Total fuel cost, Rs/h
- \( P_{gi} \): Unit power output of ith generator, MW
- \( n \): number of electric generating units
- \( a_i, b_i, c_i \): coefficient of fuel cost of ith generator, Rs/MW² h, Rs/MWh, Rs/h

Figure 1 Schematic Diagram of BBoiler turbine generator unit
III. IMPROVED MULTI-VERSE OPTIMIZATION (IMVO)

A. Particle Swarm Optimization

Particle swarm optimization, motivated by societal behavior of birds is a swarm-intelligence-based optimization algorithm which offers a population-based searching method by taking particles and moving them around in the search space for receiving the best solution for the problem. In PSO, particles move in a multi-dimensional search space, each particle regulates its position according to its own experience of neighboring particles, utilizing best position encountered by itself and its neighborhoods[2]. PSO is meta-heuristic optimization technique and provides a population-based search procedure for global optimization, having principal advantage of easy to perform and few parameters to adjust.

B. Multi-Verse Optimization

Multi-Verse Optimizer (MVO) [24] is a novel nature inspired algorithm proposed by Seyedali Mirjalili. MVO is motivated by the philosophy of multi-verse in astronomy. According to this theory there are many big bangs and each gives birth to a new universe. The term multi-verse stands opposite of universe, which refers to the existence of other universes in addition to the universe that we all are living in [24]. Multiple universes interact and might even collide with each other in the multi-verse theory. Three main concepts of the multi-verse theory (white hole, black hole, and wormhole).

A big bang can be considered as a white hole, it is also argued in the cyclic model of multi-verse theory that big bangs/white holes are created where the collisions between parallel universes occur. In contrast to white holes, black holes attract everything including light beams with their extremely high gravitational force [24]. Wormholes are those holes that connect different parts of a universe together and act as time/space travel tunnels where objects are able to travel instantly between any corners of a universe. Every universe has an inflation rate (eternal inflation) that causes its expansion through space. In MVO algorithm exploration of search space is done by utilizing the concepts of white and black holes while exploitation is assisted by wormholes. A universe is analogous to each solution and an object in that universe is analogous to each variable in the solution. An inflation rate is assigned to each solution, which is relative to the consequent fitness function value of the solution [24]. The following steps are done in order to do this

\[
U = \begin{bmatrix}
    x_1^1 & x_2^1 & \cdots & x_d^1 \\
    x_1^2 & x_2^2 & \cdots & x_d^2 \\
    \vdots & \vdots & \ddots & \vdots \\
    x_1^n & x_2^n & \cdots & x_d^n
\end{bmatrix}
\]  

(1)

where \(d\) is the number of parameters (variables) and \(n\) is the number of universes (candidate solutions):

\[
x_j^i = \begin{cases} 
  x_k^l, & r1 < NI(U_i) \\
  x_k^l, & r1 \geq NI(U_i)
\end{cases}
\]

(2)

where \(x_j^i\) indicates the jth parameter of ith universe, \(U_i\) shows the ith universe, \(NI(U_i)\) is normalized inflation rate of the ith universe, \(r1\) is a random number in \([0, 1]\), and \(x_k^l\) indicates the jth parameter of kth universe selected by a roulette wheel selection mechanism. The formulation of this mechanism is as follows:

\[
\begin{cases} 
  x_j^i + \text{TDR} \times \left( (ub_j - lb_j) \times r4 + lb_j \right); r3 < 0.5 \\
  x_j^i - \text{TDR} \times \left( (ub_j - lb_j) \times r4 + lb_j \right); r3 \geq 0.5
\end{cases} \quad \text{if } r2 < \text{WEP}
\]

\[
x_j^i
\]

\[
r2 \geq \text{WEP}
\]
where \( X_j \) indicates the jth parameter of best universe formed so far, TDR is a coefficient, WEP is another coefficient, \( lb_j \) shows the lower bound of jth variable, \( ub_j \) is the upper bound of jth variable, \( x^{i,j}_t \) indicates the jth parameter of ith universe, and \( r_2, r_3, r_4 \) are random numbers in [0, 1]. There are two main coefficients herein: wormhole existence probability (WEP) and travelling distance rate (TDR). The former coefficient is for defining the probability of wormhole’s existence in universes. It is required to increase linearly over the iterations in order to emphasize exploitation as the progress of optimization process. Travelling distance rate is also a factor to define the distance rate (variation) that an object can be teleported by a wormhole around the best universe obtained so far. In contrast to WEP, TDR is increased over the iterations to have more precise exploitation/local search around the best obtained universe. The adaptive formulator both coefficients are as follows[24]:

\[
WEP = \text{min} + 1 \times \left( \frac{\text{max} - \text{min}}{L} \right)
\]

Where \( \text{min} \) is the minimum (0.2 in this paper), \( \text{max} \) is the maximum (1 in this paper), \( l \) indicates the current iteration, and \( L \) shows the maximum iterations.

\[
TDR = 1 - 1^{1/p} \left( \frac{L}{1} \right)^{1/p}
\]

Where \( p (=6) \) defines the exploitation accuracy over the iterations. The higher \( p \), the sooner and more accurate exploitation/local search. In the MVO algorithm, the optimization process starts with creating a set of random universes. At each iteration, objects in the universes with high inflation rates tend to move to the universes with low inflation rates via white/ black holes. Meanwhile, every single universe faces random teleportation in its objects through wormholes towards the best universe. This process is iterated until the satisfaction of an end criterion.

C. Basic Steps Of Hybrid Mvo-Pso Algorithm

1) Initialize the population and form the solution space.
2) Run MVO
3) Generate minimum values for all individuals
4) Pass these individuals to the PSO as starting points
5) Give the updated positions back to MVO.
6) Run till stopping criteria is met.

Flowchart of IMVO
IV. RESULTS & DISCUSSION

IMVO has been used to solve ELD problem in two test framework for exploring its optimization potential. In this technique iteration has been performed are 500 in each test framework and 50 is the number of search agent.

A. Experimental Model 1: Number of Generating Unit is 3

The statistical data for 3-generators and $B_{mn}$ i.e. the loss coefficient matrix is procured from reference 15 and is provided in Appendix A.1. The ELD for 3-generators is explaining as suggested composite approach and foremost result had been contrasted by MVO. Also the fuel cost of different algorithms which had been applied to the same test model is contrasted with obtained results from the hybrid approach for demand load of 350MW, 450MW and 500MW in Table 1.

| Sr.No. | Power Demand (MW) | Conventional Method [15] | Cuckoo Search Algorithm [15] | MVO | IMVO |
|--------|-------------------|--------------------------|-----------------------------|------|------|
| 1      | 350               | 18570.7                  | 18564.5                     | 18564.4841 | 185624.4839 |
| 2      | 450               | 23146.8                  | 23112.4                     | 23112.416 | 23112.363 |
| 3      | 500               | 25495.2                  | 25465.5                     | 25465.526 | 25465.469 |

B. Experimental Model 1: Number of Generating Unit is 6

The input data for six generators and $B_{mn}$ i.e. the loss constant matrix is obtained from reference 15 and is mentioned in Appendix A.2. The economic load dispatch is expressed with mix approach and the outcomes obtained is contrasted with particle swarm optimization, cuckoo search algorithm and whale optimization algorithm for an instance of fuel cost delivering load demand of 600MW, 700MW and 800MW in Table 2.

| Sr.No. | Power Demand (MW) | Conventional Method [15] | Cuckoo Search Algorithm [15] | MVO | IMVO |
|--------|-------------------|--------------------------|-----------------------------|------|------|
| 1      | 600               | 32096.58                 | 32094.7                     | 32094.285 | 32091.135 |
| 2      | 700               | 36914.01                 | 36912.12                    | 36912.065 | 36907.007 |
| 3      | 800               | 41898.45                 | 41896.900                   | 41896.291 | 41889.571 |

Figure 2 Convergence curve of MVO & MVPSO with power demand 500 MW

Figure 3 Convergence curve of MVO & MVPSO with Power Demand 700 MW
V. CONCLUSION
In this paper ELD problem has been solved by improved multi-verse optimization (IMVO). The result of IMVO are compared for three unit and six unit generating unit system with other techniques. The algorithm is programmed in MATLAB (2009a) software package. The result show effectiveness of IMVO for solving economic load dispatch.

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