Mathematical model of the feedback between global supply chain disruption and COVID-19 dynamics

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The pandemic of COVID-19 has become one of the greatest threats to human health, causing severe disruptions in the global supply chain, and compromising health care delivery worldwide. Although government authorities sought to contain the spread of SARS-CoV-2, by restricting travel and in-person activities, failure to deploy time-sensitive strategies in ramping-up of critical resource production exacerbated the outbreak. Here, we developed a mathematical model to analyze the effects of the interaction between supply chain disruption and infectious disease dynamics using coupled production and disease networks built on global data. Analysis of the supply chain model suggests that time-sensitive containment strategies could be created to balance objectives in pandemic control and economic losses, leading to a spatiotemporal separation of infection peaks that alleviates the societal impact of the disease. A lean resource allocation strategy can reduce the impact of supply chain shortages from 11.91 to 1.11% in North America. Our model highlights the importance of cross-sectoral coordination and region-wise collaboration to optimally contain a pandemic and provides a framework that could advance the containment and model-based decision making for future pandemics.

Severe Acute Respiratory Syndrome Coronavirus 2 (SARS-CoV-2) is a virus that infects the upper and lower respiratory tract1,2 and is the causal agent of the Coronavirus Disease 2019 (COVID-19). In 2020, SARS-CoV-2 affected over 200 countries and territories and caused 117.8 million infections and 2.6 million fatalities after being declared a pandemic by World Health Organization (WHO). Despite a century of successful prevention and control efforts, infectious diseases remain an important global problem in public health and socioeconomic disruptions. COVID-19 is not the first virus that led to the global pandemic. Many people have drawn comparisons between COVID-19 and pandemics of influenza that occurred in 1918, 1957–1958, 1968, and 20093. The scientific consensus is that infectious disease emergence has accelerated in recent decades while the current ability to anticipate the next pandemic remains very limited4. To address challenges and risks in future pandemics, the dynamic interconnection between managerial decisions, infectious diseases, and shortages of the health care equipment must be considered.

The current global economic situation and ongoing recession were triggered by the COVID-19 pandemic, in part due to supply chain disruptions. Thus, there is a feedback such that infectious disease outbreaks not only deeply affect the world economy and global health, but also fundamentally change society's ability to contain the outbreak. During COVID-19, major enterprises owning more than 12,000 production facilities were shutdown due to quarantine policies, which lead to severe supply chain disruptions5,6 and a huge dip in international trade, which declined between 13 and 32%7. The shortage of critical health care resources due to supply chain disruptions and difficulties in international trade then had a significant impact on timely delivery of health care service8,9. Since the beginning of the pandemic, efforts by local health departments all over the world have sought to optimize response strategies to mitigate the outbreak. These efforts, however, have been halted by limited critical health care resources at different times and places10. The shortage of health care resources originates from surging demands caused by accelerating numbers of COVID-19 cases, misinformation, panic buying, and stockpiling11. Resource shortages not only raise health risks but also accelerate the spread of the disease, which

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exacerbates resource shortages in a vicious circle. With the accelerated spread of the disease, there is a pressing need to sustain the supply chain of critical items to prevent the detrimental feedback between the supply chain disruption and disease growth. This study fills this research gap by applying ecological and managerial knowledge to develop a tool that explicitly captures positive feedback in supply chain disruptions and infectious disease dynamics.

COVID-19 has brought a worst-case scenario affecting critical stock availability: a rapid surge in demand combined with the shortage of substantial raw materials due to global supply chain disruptions. Such a disruption in the supply chain network can also limit the development and delivery of vaccines. To mitigate resource shortages, simply demanding more critical medical supplies is not enough. There are only a few companies that have the expertise to manufacture these products and are able to ramp up production under global supply chain disruptions. For instance, sanitizer manufacturing companies in Australia started facing shortages of required raw materials and ingredients soon after increasing their capacity of producing sanitizing gel. Ford’s effort of building 50,000 ventilators in July was delayed due to part shortages and challenges in scaling up the part production. Avoiding such disruptions required that policymakers both guide these companies to maximize their production capacities and coordinate other industries into this effort to guarantee material supplies.

Advanced models and simulations must inform policymakers.

This pandemic revealed that even high income countries compromised the delivery of health care resources and services as a result of rapid spread and depletion of material stocks. Studies show that the shortage of health care resources in the USA, especially N95 masks, was predictable and preventable with publicly available supply chain data and a careful management strategy. Worldwide efforts to mitigate COVID-19 revealed the necessity of an data-driven model to represent changes in the evolving pandemic, which fuses the diverse data sources including required quantity, rate of use of health care resources and global supply chain data. As the virus’s global spread escalated, demand for surgical masks skyrocketed in China, beginning in February 2020. As the largest mask exporting country, China paused its export of face masks and began importing from Europe, Japan, and the United States to alleviate mask shortages. Awareness of such surge demands of health care resources has long-term impacts on managerial decisions and disease control. However, the growth of the epidemic creates even more turbulent supply chain and disease situations. It is challenging to foresee intuitively the outcomes from the complex interconnections in order to wisely distribute resources in the global supply chain.

We propose that the development of the Internet of Things (IoT) has created the conditions for the digitalization of supply chains, providing the essential data for addressing challenges during pandemics. Smart sensors and communication technologies are becoming more practical, which connects the global manufacturing assets, i.e., robots and machines, as a digital supply chain network. Digital supply chain connects the physical process, including, manufacturing process and supply chain activities to the virtual models, also known as a digital twin. The data and decisions simulated and optimized in the digital twin can be used to improve the performance of physical processes. Further, digitalization enables the supply chain to evolve over time adapting to disruption risks of manufacturers and changes in market environment, which substantially extends the mitigation capabilities of supply chain disruptions.

Here we report on a model coupling disease dynamics and the digital global supply chain network to understand the essential feedback between economic productivity and public health. Our approach makes use of real-world input-output trade data and ongoing disease data to represent the real-time risks and impacts of an infectious disease. A network proactive control (NPC) is formulated to create an agile and time-sensitive containment strategy, which optimizes worldwide managerial decisions considering predictive impacts on a daily basis. Using data-based simulations, we first investigate how different managerial strategies affect the coupled economic-epidemic dynamics and then project it to disease impacts on public health and the global economy. This new approach can be used as a stress-test tool to evaluate the robustness and resilience of the supply chain in public health emergencies, enabling a holistic impact analysis of cross-industry coordination and inter-region collaboration to contain emerging diseases. The proposed approach of coupling the disease dynamic network and the supply chain network can be used for other future events similar to the COVID-19 pandemic.

**Model**

**Model of supply chain disruption in a substantial demand change and quarantine policy.** Figure 1a shows a digital supply chain network including activities, people, entities, information, and resources across diverse industries. The arrow line represents the supplier-customer relationship between manufacturers in the supply chain. Figure 1c visualizes the model that accounts for feedback between shortages of health care resources, supply chain and local disease dynamics. Under pandemic conditions, production is disrupted due to restricted transportation, shortage of raw materials from suppliers caused by lockdown policies, and changes in demands, especially for critical health care products. Decision makers need to face local production disruptions while satisfying regional health care supply needs. Thus, regional disease dynamics are critical factors in making managerial decisions, i.e., dyed and reorganized nodes in Fig. 1c. Pandemic complicates challenges the supply chain management.

Demand for health care resources increased with the growth of pandemic. For example, masks are a health care resource in medical procedures and also recommended by WHO to provide an adequate protection against COVID-19 in public activities. In our model a disease-dependent demand function explicitly represents the surge in medical needs by correlating the demand with the number of infected and hospitalized individuals. In addition, the disease has a substantial impact by disrupting the production capacity for supplies due to quarantined labor force and constrained factory working hour. Studies have found the optimal lockdown policy to be dependent on the prevalence of disease in the local population. We also assume the optimal policy to...
be adopted, in which case we use a disease-dependent capacity function to connect production capacity to the current disease situation.

**Model of disease dynamics during the shortage of medical supplies.** Figure 1b shows a multi-patch (metapopulation) compartmental model that represents the kinetics of an epidemic in an idealized susceptible population of connected regions. Studies indicate that the proper usage of face masks can synergistically act together with social distancing to reduce the virus transmission rate. In addition, reliable access to health care resources, including medical supplies, devices, and therapy, is critical for hospitals to continue to function adequately and to deliver stable and adequate health care.

A shortage-dependent transmission function in the model calculates the transmission rate in each region according to the amount of health care resource shortage per capita. Items like masks and face shields are critical items for preventing COVID-19 as suggested by the WHO. The unsatisfied demands of health care resources impact the ability to adhere to ideal infection control, health worker safety and treatment thus changing the transmission of the disease. In COVID-19, special medical devices like ventilators have been required. One ventilator per patient is not possible due to the shortages of ventilators in many countries, which increases the death rate in the population. Our model includes a shortage-dependent fatality function that measures the death rate and recovery rate as functions of timely availability of supplies of health care resources.

**Results**

Considering the geographical separation and economical connections, five regions are selected and connected as a network to represent the world-wide pandemic and global supply chain, i.e., Asia, European Union (including United Kingdom), Latin America, North America, and Oceania. We aggregated all manufacturers that produce goods and services in each region, and considered the capability of trading among regions. Three data sets are used for estimating model parameters. In the disease network, the transmission rate is estimated on a daily basis by fitting pandemic data reported by Johns Hopkins University Center. Tourism data provided by the World Tourism Organization and international air travels history reported by the International Air Transport Association (IATA) are aggregated to approximate the connectivity among regions. A digital supply chain network is built from the Global Trade Analysis Project (GTAP) database (version 10). Industries are grouped into 10 sectors defined by GTAP. The human health and social work (HHS) sector are separated as a special sector to represent the expenditure on health care resources in human health and social work. Resources required by HHS are considered to correlate with the emergence of COVID-19, reflecting the surge in demands of critical medical supplies. Assuming each regional sector as a producer, the following information is obtained for each sector:
regional sector: (1) bill of material in production, (2) pre-pandemic production capacity and (3) cross-regional resource flows at equilibrium.

Figure 2a lists all sectors used in this study, and compares the demand inputs from other sectors if productions of each sector were to double. Increasing HHS production depends on inputs from many other sectors. The major inputs are from heavy manufacturing, mining, and extraction. Light manufacturing, other services, and transport and communication are dependent sectors also. A strong dependence emphasizes the need for sectoral coordination to ensure sufficient material supplies are available to increase the production of health care resources. Figure 2b shows the diversity of production and demand among regions, in terms of capacity, demand, and trade at equilibrium measured in millions of dollars. North America has the highest HHS capacity, import, and demand, followed by the European Union. Latin America and Oceania have low production capacity and low needs for HHS resources. Asia is a major export region. Regional diversity highlights the need for analyzing the risks of regional production disruptions, as well as the customization of the containment strategy for each region.

Cross-sector coordination. We study positive feedback between disease dynamics and supply chain disruption in a 100-day simulation of the model initialized by COVID-19 data on March 1st 2020. Managerial decisions are updated daily by a proactive control of the supply chain network with consideration of production and inventory constraints. The model considers the impact of managerial decisions in terms of disease control and economic losses seeking a balanced solution. With a higher capacity of producing HHS resources, this containment strategy tends to raise the HHS production to alleviate the shortage of HHS resources so as to reduce the spread of the disease. Figure 3a shows the results of a stress test to identify the vulnerable sectors in satisfying the demands from a health emergency. Results show that Grains and Crops is the least impacted sector among all countries due to its weak dependence on other sectors. Transport and Communication is the bottleneck sector that limits further increase of HHS production. Because the differences in regional capacities, sectoral impacts also vary. Asia and Oceania are impacted the most in their Heavy Manufacturing sector. Interestingly, the analysis shows that the shortage of Processed Food, and Livestock and Meat Products in Asia are significantly greater compared to other regions, which is consistent with the raise in the price of pork reported in Asian countries.43,44.

Figure 3b shows the shortages for four different HHS ramping-up scenarios. Despite the forced increase in capacity by the policy-maker, the capacity is dynamically updated according to the evolving disease situation by the disease-dependent capacity function. With increasing production capacity, the shortage of HHS does not reduce monotonically, but fluctuates around 40%. As a result, significant shortages are observed in other sectors, including Mining and Extraction, Transport and Communication, and Utilities and Construction, which overlap with dependent sectors in the Fig. 2a. Other sectors, such as Textiles and Clothing, suffer a remarkable shortage due to the shared input materials with the HHS resources, i.e., cloth and masks. Increase in the production capacity is not enough to meet the surge in demands due to the limitations of raw materials. Without coordinated sectors, ramp-up of production capacity incurs the overuse of materials in the existing stockpiles, which leads to further raw material shortage in the future, thus deepening the disruptions in producing HHS resources.

Figure 3c shows the sectoral impacts when sectors are coordinated, namely, all the other sectors are able to provide sufficient raw materials for HHS production. With increasing HHS production capacity, a clear decreasing trend of HHS shortage is observed, reducing from 60% to less than 20%. Note that even with sufficient
production capacity, shortages exist in Other Services and Utility and Construction, which require raw materials from the HHS resources for production.

Figure 4 shows the influence of improved HHS production on disease outcomes. As a benchmark, the number of fatalities is calculated based on simulation results according to the pre-epidemic production capacity. The percentage of reduction is calculated by comparing the total number of fatalities to the benchmark at each time.
instance. With coordinated supply chains, an increase in HHS capacity at early stage of pandemic substantially reduces the number of fatalities as well as the duration of the outbreak. A reduction in HHS shortage in the model reduces disease transmission rate, thus suppressing the number of newly added infections due to better personal protection. In addition, fatality rate decreases with more medical resupplies. As a result, the number of fatalities is reduced by 90% by doubling the capacity of HHS in March 2020.

**Lean resource management and regional collaboration.** We sought to confirm that key improvements are possible in lean management of HHS resources and regional collaboration by exploring the managerial decisions made in the model. Our analysis starts from March 1st 2020 based on COVID-19 data, and the model is simulated for 30 days based on equilibrium decisions. Then, a 100-day simulation is conducted based on three containment strategies: (1) pre-epidemic management strategy (PE): adopt the same managerial decisions as pre-pandemic; (2) optimization of digital supply chain strategy (ODS): adopt optimal digital supply chain managerial decisions considering the pandemic as a disturbance; (3) optimization of the coupled network model strategy (OCN): optimize the managerial decisions based on feedback in the model of coupled networks. Figure 5 shows the effectiveness of these containment strategies in terms of infections in different regions.

Figure 5a shows the actual number of infections during the COVID-19 pandemic, which is a benchmark for the proposed models. Figure 5b shows the number of infections in the PE strategy which skyrockets in the 3 months following March 2020. The magnitude of infections is similar to the actual numbers in Figure 5a, which suggests that the model is accurate in representing the real disease dynamics. Peak values of 4 regions including Asia, European Union, North America, and Latin America occur simultaneously around July 1st, leading to extremely high demands for critical medical supplies and severe global production disruptions, which poses extreme challenges in pandemic containment. Figure 5c shows the simulation results for the ODS strategy. In this case, infections are notably reduced due to the dynamic supply chain transformation achieved by NPC. Figure 5d shows simulation results for the OCN strategy. Using this strategy, it is observed that infections are reduced further and pandemic almost fades in July. Note that peaks of regional infections are staggered in both ODS and OCN strategies. Both these optimization-based containment strategies lead to a spatiotemporal separation of infection peaks to split stresses in supply chain. Moreover, these containment strategies also ensure that at least one of major HHS providers is available to support other regions in each period of time, thus preventing an intense growth of the disease.

Figure 6a summarizes the loss of production capacity of each region in the ODS strategy. Without considering positive feedback, North America and European Union suffer capacity losses in May (15.75% and 19.33%) and June (16.57% and 13.44%). As a comparison, production disruptions for European Union and North America are reduced to 2.11% and 12.15% in May and 0.9% and 3.86% in June respectively in the OCN strategy (Fig. 6b). The better recovery of production capacity results in more HHS resources that can be produced and distributed to other regions for disease control, thus leading to a quick production recovery, especially for regions with stronger industrial capabilities. Note that Latin America suffers a higher production disruption compared to other regions. Lack of capacity of HHS production makes Latin America unable to react to surges in HHS demands under a health emergency, which highlights the need for inter-regional collaboration.

Figure 6c,d show the trade history of the world’s supply chain corresponding to ODS and OCN strategies, respectively. Results from March 2020 are used as benchmark, representing inter-region collaboration simulated.
in the pre-pandemic strategy. Much stronger collaboration among regions is observed after April when NPC starts. Although Oceania and Latin America both lack the capacity to produce HHS resources, infections in Oceania are delayed, which reserves the production capacity in health care resource preparation ahead of time to contain the disease growth. In contrast, low capacity and high existing infections make Latin America rely on imports from other regions for disease control. The comparison shows that managerial decisions need to be made according to regional production capacity as well as the connectivity to other regions.

Although both containment strategies suggest similar managerial decisions in April, ODS containment strategy does not account for the positive feedback, and thus inaccurately forecasts changes in disease trends from historical medical supplies data. Due to positive feedback, a small difference in predictions may evolve into a distinct outcome for the disease. Asia and European Union receive 50% and 42% more HHS supplies from North America and Oceania in the OCN strategy. Although the importance of additional supplies might not be immediately recognised, it makes a significant long-term impact on containing the disease if applied at the early stages of pandemic. For example, Asia is the import region in the first two months. Increased imports in April and May slow down pandemic growth, which shortens production disruptions and reduces the demand from infected individuals and hospitals. As a result, Asia changes to an export region in June. Our coupled model predicts that the disease is significantly reduced in Latin America by the inter-region collaboration although that is the region hardest hit by the disease. Lower amount of infections in Latin American in turn reduce imported infections to other regions, and that slows the spread of disease.

In the ODS strategy, Asia needs to import HHS resources from other regions all the time. Due to limited health care resources, pandemic in Latin America starts to grow and requires more urgent medical aid from other regions, thus resulting in a totally different pandemic situation as shown in Fig. 5. In July, Latin America still needs to order health care resources to satisfy HHS demands from other regions, while these other regions start to export health care resources while experiencing severe pandemic (e.g., export from European Union). The consideration of positive feedback and the transparency of data regarding supplies enhances the OCN containment strategy, leading to a lean management of HHS resources to better control the growth in HHS demands and to limit the spread of disease.

Simulated past diseases in the current world. The basic reproduction number, \(R_0\), is an epidemiologic metric that describes how contagious an infectious disease is before mitigations start\(^45\). In our study, we consider NPIs (included in the approximated transmission rates) and health care resources (variables to be optimized) as two critical factors that mitigate the spread of disease. We set an initial \(R_0\) of SARS-CoV-2 as 3.7 following the previous research\(^46\) and parameterize the transmission rates by \(R_0\). Assuming that supply chain configuration, population size and NPIs remain the same, the expected impact of past infectious diseases, including Spanish Flu (1918)\(^47\), SARS (2003)\(^48\), H1N1 (2009)\(^49\), MERS (2014)\(^50\) and Ebola (2014)\(^51\), in the current world situation are demonstrated in Fig. 7.

Compared to other diseases, severe impacts from COVID-19 can be attributed to its extremely high reproduction. Lower available production capacity leads to higher supply chain disruption, which is expected to decrease with increasing \(R_0\), as shown in Fig. 7. The number of infected people significantly increases with \(R_0\) larger than...
and an epidemic could ensue. With modeling positive feedback in the coupled model and implementation of real-time NPC, our results indicate that a pandemic breakout occurs with a higher $R_0$ value, 1.14, and the number of infections grows almost linearly with increasing $R_0$. Feedback in our model alleviated the shortage of health care resources mitigating the spread of disease with reduced reproduction number (i.e., $R_t < R_0$). In our model, NPC can effectively leverage the dependency between health care resources and disease control leading to an improved containment strategy.

Discussion

COVID-19 is neither the first nor the last pandemic that humanity will face. Risks of further pandemic outbreaks of other pathogens exist. Until now, most research has focused on the economic impact of public health interventions or on improving the accuracy of disease prediction, not the feedback between pandemic growth and supply chain disruption. Supply disruption not only slows down governments’ ability to respond, but also allows the disease to spread by limiting health care resources, which in turn increases demand. Our model views pandemic growth and supply chain disruption as mutually reinforcing pressures. In our model, supply chain and pandemic networks are coupled to analyze the mutual influence in HHS resource shortages, disease dynamics, and production disruption. The NPC algorithm provides agile and time sensitive containment strategies that control the disease by optimizing supply chain managerial decisions, which enhances availability of HHS resources while accounting for trade-offs between disease growth and economic loss.

Our discovery based on real-world data uses the status quo as benchmark to highlight the effectiveness of different containment strategies in what-if scenarios. The existing diversity in economy and public health status in different regions of the world are modelled to address the need for customization of disease containment and inter-region collaboration strategies. The significance of our analysis may be observed by contrasting results of Fig. 5. Foreseeing the positive feedback between supply chains and disease dynamics enhances our understanding of pandemic growth and supply chain disruption, leading to an agile and lean resource allocation strategy that effectively decelerates the spread of the disease and facilitates production recovery.

Shortage of key equipment and materials in health care delivery has been a significant challenge since the beginning of pandemic. Researchers acknowledge that ramping-up HHS resource production may not be as simple as raising the production capacity, but requires the coordination of raw materials. In addition, the recent surge in HHS demands was found to stress supply chain networks and deepen disruptions. The model we propose not only identifies bottlenecks in ramping up HHS production, but also indicates the minimal sector impacts. Although these discoveries do not reflect all the underlying causes of supply chain disruption, they significantly advance our ability to manage the situation by informing decision makers about vulnerable sectors that have to be coordinated and reinforced during an outbreak.

Given increased HHS production, enhanced inter-region collaboration at the start of pandemic would have shortened the pandemic period. Regional containment strategies are customized automatically in the model according to risk of infection, industrial structure and production capacity, leading to distinct roles of regions in a health emergency. Results highlight the need to strategically distribute the HHS stockpiles differently by region in order to prevent future resource shortages. The active control model of the supply chain network tends to distribute resources to regions with high HHS production capacity to prevent those regions from being disrupted due to lockdown policies caused by pandemic, thus improving long-term HHS production supplies.

Comparing results of OCN and ODS strategies, impacts of modeling positive feedback of disease dynamics and supply chain management was highlighted. The subtle difference in predicting disease dynamics and demands resulted in small shifts in managerial decisions at the early stage of pandemic. These subtle shifts led to a substantial divergence in long-term performance due to reinforcing pressures between disease growth and supply chain disruption. For instance, ignoring positive feedback values makes HHS export countries overestimate HHS demands thus being conservative in exporting, which in turn reduces the amount of HHS resources other regions receive. Increase in HHS shortages accelerates growth of disease, which in turn demands more HHS in...
the future, leading to a butterfly effect\textsuperscript{55}, where a small change in managerial decisions for a coupled nonlinear system can result in large differences in outcomes.

In the study of COVID-19, we quantitatively assessed the impacts of cross-sectoral coordination and agility in containing the outbreak. We explored different containment strategies for critical medical supplies to seek the best managerial outcome in terms of minimizing both the number of fatalities as well as the losses in meeting demands. In our model, managerial decisions are customized based on the ability of different world regions to produce required resources and the risk of infection in terms of transmission rate. Such customized decisions could lead to time-sensitive strategies, illustrating the importance of agility in prediction, lean resource management, and collaboration in pandemic control and economic recovery. Results of this study highlight the importance of cross-sectoral coordination and information transparency between manufacturers across the world to contain a pandemic.

In summary, we proposed a model to analyze the interactive effects of supply chain disruption and infectious disease dynamics using coupled production and disease networks built on global data. We explored different containment strategies for critical medical supplies to seek the best managerial outcome in terms of minimizing both the number of fatalities as well as the losses in meeting demands. Results show that applying active network control strategies leads to time-sensitive strategies, illustrating the importance of agility in prediction, lean resource management, and collaboration in pandemic control and economic recovery. In addition, results of this study highlight the importance of cross-sectoral coordination and information transparency between manufacturers across the world to contain a pandemic. Our model of feedback between supply chain disruption and disease dynamics can be used to quantify the impacts of new technologies, including artificial intelligence\textsuperscript{59}, industrial IoTs\textsuperscript{60} and advanced manufacturing technologies\textsuperscript{61} in containing the spread of disease. Thus, the proposed model can be used as a valuable tool to identify the bottlenecks of the supply chain and public health systems in future pandemics.

Methods

Coupled supply chain and disease networks. Each region is modeled as a patch with a disease model for simulating the disease dynamics and a production-inventory model for production scheduling and planning. In particular, we use an SEIRHD model of the disease with six compartments\textsuperscript{42}, including susceptible (S) reflecting the part of the population that could be potentially subjected to the infection, exposed (E) representing the fraction of the population that has been infected but is not infective yet, infected (I) representing the infective population after the latent period, hospitalized (H) representing the fraction of infected individuals who need hospitalization, recovered (R) representing the population that has successfully recovered from the infection, and dead (D) representing fatalities due to the disease. Production and inventory model of region $i$ is described by two states at each time $t$: (1) inventory level of type $k$ resource, $V_{i,k}(t)$; (2) backlogged demands for type $k$ resource, $U_{i,k}(t)$. We denote type $h$ resource as HHS resources. Thus, $V_{ih}(t)$, $U_{ih}(t)$ are the inventory level and demand for HHS resources in region $i$. Regional managerial decisions in region $i$, including production of type $k$ resource, $w_{i,k}(t)$ and distribution to the public $d_{i,k}(t)$, are decisions to be optimized in local inventory production planning. Resource production follows the bill of materials $M_{k,l}$, which specifies the amount of type $k$ resource required to produce a type $l$ resource. Parameters in production and inventory model are estimated by using the GTAP datasets.

To model connectivity in the system and the transmission between regions, the infection in region $i$ is affected by the number of infected individuals in other regions (due to interrelations such as travel), which creates a multi-patch disease network. We use $\beta_{ij}$ as the rate at which susceptibles in region $i$ are infected by infected individuals from region $j$. We assume that infections can be passed between any pair of regions, albeit possibly via intermediate regions. We assume that $\beta_{ij} \ll \beta_i$ to reflect the fact that between-patch transmission parameters are significantly smaller compared to within-patch transmission parameters. Cross-region trade and supplies connect regional inventories as a global production and supply chain network involving region-wise trade decisions, i.e. $d_{i,k}(t)$ for importing resources of type $k$ from region $i'$ to $i$. Summarizing above descriptions, we model dynamics of disease, inventory and demand in region $i$ using following set of equations:

$$S_i(t+1) = S_i(t) - S_i(t) \sum_j \frac{\beta_{ij}(t)I_j(t)}{N_j},$$  \hspace{1cm} (1)  

$$E_i(t+1) = E_i(t) + S_i(t) \sum_j \frac{\beta_{ij}(t)I_j(t)}{N_j} - \gamma_{IE}E_i(t),$$  \hspace{1cm} (2)  

$$I_i(t+1) = I_i(t) + \gamma_{IE} E_i(t) - (\gamma_{IR} + \gamma_{IH})I_i(t),$$  \hspace{1cm} (3)  

$$H_i(t+1) = H_i(t) + \gamma_{IH}I_i(t) - (\gamma_{HR} + \gamma_{HD})H_i(t),$$  \hspace{1cm} (4)  

$$R_i(t+1) = R_i(t) + \gamma_{IR}I_i(t) + \gamma_{HR}H_i(t),$$  \hspace{1cm} (5)  

$$D_i(t+1) = D_i(t) + \gamma_{HD}H_i(t).$$  \hspace{1cm} (6)
\[ V_{i,k}(t+1) = V_{i,k}(t) + \sum_{j} a_{i,j,k}(t) - o_{i,j,k}(t) - \sum_{k'} M_{k',k} w_{i,k'}(t) + w_{i,k}(t) - o_{i,k}(t), \]
\[ U_{i,k}(t+1) = U_{i,k}(t) + \delta U_{i,k}(t) - o_{i,k}(t), \]

where, \( N_i \) is the size of population of region \( i \), \( \gamma_H = \delta_H/\tau_I \), \( \gamma_R = (1 - \delta_H)/\tau_R \), \( \gamma_{IR} = (1 - \delta_D)/\tau_H \), where \( c \) is the percentage of infected individuals hospitalized, and \( \delta_D \) is the fatality rate. \( \tau_I \) and \( \tau_R \) represent the average infectious period and average hospital stay in days, respectively. In our analysis, we choose \( \gamma_{IR} = 1/5.2 \) days, \( \tau_I = 4.6 \) days, and \( \tau_R = 10 \) days according to values reported in previous studies. We fit the model to data of COVID-19 to find the coefficients \( \delta_D \), \( \delta_H \), and \( \delta_I \) at each time instant. The proposed modeling framework is generalized for different types, intensities, and duration of interventions to be implemented in each region, and thereby illustrates how these interventions impact disease dynamics and resulting number of infections and fatalities through time. In particular, we consider non-pharmaceutical interventions (NPIs) (e.g., social distancing) and the shortage of HHS resources for a set duration applied as a scaling of transmission rates for all infected individuals.

**Coupling functions.** Disease-dependent capacity function. Studies have confirmed the dependence of optimal lockdown policy on the disease fraction in the population, which links pandemic severity to production capacity. Assuming that optimal lockdown policy is adopted, available production becomes a function of existing disease situation, i.e., the percentage of infected and hospitalized. These simplifications allow us to describe a real-time evolving supply chain network, together with disease spreading on it, to evaluate the amount of production capacity available during pandemic, namely

\[ w_{i,k}(t) = e^{-\gamma_w \frac{I_i(t)}{k}}, \]

where \( \bar{W}_{i,k} \) is the pre-pandemic production capacity and \( \gamma_w \) is a scaling parameter designed such that only 1% production capacity remains available when the percentage of active infections reaches 1% of the total population.

Disease-dependent demand function. There is a broad range of estimates of critical medical supplies required to care for COVID-19 patients, which vary depending on the number, speed, and severity of infections. Thus, we created a function to characterize how governments and households issue orders to their manufacturers under pandemic. Demands are separated into commercial resources, \( b U_{i,k}, k \neq h \) and HHS resources, \( b U_{i,h} \). Additional HHS resources are considered to depend on the severity of pandemic and correlated to the number of existing infected individuals \( I_i(t) \) and hospitalized individuals \( H_i(t) \). The product demands of other sectors remain the same as pre-pandemic, namely

\[ \delta U_{i,h}(t) = \gamma_I I_i(t) + \gamma_R H_i(t) + a_{i,k}(t), \]

\[ \delta U_{i,k}(t) = a_{i,k}(t), \quad \forall k \neq h, \]

where \( \gamma_I \) and \( \gamma_R \) are parameter set to keep a susceptible individual and an infected individual on a daily basis (we assume \( \gamma_I = 0.0001, \gamma_R = 0.002 \)), which are roughly estimated based on the direct medical costs of MERS coronavirus. \( a_{i,k}(t) \) is daily consumption of resources of type \( k \) during the pre-pandemic period.

Shortage-dependent transmission function. To model the transmission rate, we consider three elements for each region \( i \), including a base transmission rate \( \beta_0(t) \) representing the transmission rate without any NPI measures, a health care coefficient \( c_{H,i}(t) \) representing reduction in the transmission rate due to proper usage of HHS resources, and an NPI coefficient \( c_{N,i}(t) \) representing the reduction in transmission rate due to change in economic activity and NPI such as social distancing and curfew. We define \( c_{H,i}(t) = 1 - \frac{2(1 - P_i)}{1 + e^{\frac{2(1 - P_i)}{2} \gamma_{IR} \frac{H_i(t)}{k}}} \), where \( P_i \) is the minimum protection measure with zero health care stocks (\( P_i = 0.5 \), reflecting 50% effectiveness of HHS products if used properly). Based on these coefficients, the disease transmission rate \( \beta_i(t) \) of region \( i \) is expressed as

\[ \beta_i(t) = \beta_{i,0}(t)c_{N,i}(t)c_{H,i}(t). \]

Shortage-dependent fatality function. This function models the feedback between the shortage of health care resources and the fatality rate \( \delta_D \). Denote the transition rates from hospitalized to recovered and to dead as a function of the fatality rate \( \delta_D \), namely, \( \gamma_{IR} = (1 - \delta_D)/\tau_R \) and \( \gamma_{HD} = \delta_D/\tau_H \). We define \( \delta_D \) as the fatality rate of hospitalized individuals assuming sufficient health care resources. \( \delta_D \) measures the increment of the fatality rate under the shortage of health care resources. Under this assumption, we model the fatality rate as a time-varying variable depending on the shortage in health care resources, namely

\[ \delta_D(t) = \delta_D_0 + c_h(t)\delta_D_1, \]

where \( c_h \) is 0 when health care resources are sufficient, and is 1 when there is no stock of health care resource. All parameters are calculated directly from real-world data or from parameter fitting unless specified.
Parameter fitting. We use the data reported by Johns Hopkins University Center\(^3\) from January 22, 2020 to September 24, 2020 as our dataset for parameter fitting of coupled model. Data includes time-series of daily updates on the new infected cases, fatalities and recovered cases. The objective is to identify parameters of the compartmental model in such a way that the simulated data matches the data as much as possible. The simulated data are obtained by numerically solving the model in Eqs. (1)–(6) using an integration algorithm.

A two-step fitting process is performed to obtain the best parameters for the system of disease dynamics consisting of six regions. In the first step, we considered the disease in each region independently without considering the cross-coupling terms (\(\beta_{ij}, i \neq j\)) in the dynamics. To accomplish the parameter identification, we solved a nonlinear constrained least-squares problem for each region to minimize the cost function between the model prediction and the data. We devised the cost function as a sum of the mean square error for daily infected and fatalities. We did not include the recovered individuals in the cost function since the definition of recovery and parameter estimation approach fit the data with a reasonable accuracy. Model parameters for each region regarding the initial number of exposed individuals (number of infected and recovered cases for the SEIHRD model was considered. Also, due to lack of information in the equations (i.e., not infectious) and those reported in data (i.e., cured) might not be consistent. The initial number of infected and recovered cases for the SEIHRD model was considered. Also, due to lack of information regarding the initial number of exposed individuals (\(E_0\)), it was assumed to be five times of the initial number of infected individuals. To capture rapidly changing social scenarios particularly during the initial period of the COVID-19 spread, we split the integration interval into sub-intervals of 20 days, and the best parameters (\(\beta_i, \delta_{iH}, \delta_{iR}\)) were found at each sub-interval (the parameters are assumed to be constant in each sub-interval).

Next, we use the fitted parameters as an initial guess to fit the coupled equations (1) and (2) simultaneously for all regions considering the cross-coupling terms. The disease in each region is connected to that of other regions by cross-transmission terms, \(\beta_{ij}, i \neq j\). To identify the best parameters for the coupled model, we fix values of \(c_i\) and \(d_i\) and search for the best transmission matrix \(G\) that fits the data. We define the transmission matrix \(G\) as \(G_{ij}(t) = \epsilon p_{ij}(t)\beta_{ij}(t), i \neq j, G_{ii}(t) = \beta_{ii}(t), i = j\), where \(p_{ij}\) is a coefficient proportional to the number of daily travels from region \(j\) to region \(i\) adjusted by the change in the international air travels reported by International Air Transport Association (IATA) since starting pandemic\(^6\), and \(\epsilon\) is a fixed small number (\(\epsilon \ll 1\) reflecting that cross-coupling has considerably smaller effect on the disease transmission compared to the internal transmission. We find the best \(\beta_i\) of each time \(t\) by using a moving window. It is observed that the suggested model and parameter estimation approach fit the data with a reasonable accuracy. Model parameters for each region is shown in Fig. 8.

Network proactive control. Coupled model of disease and supply chain networks can be used to predict impacts of managerial decisions and to yield a proactive containment strategy. Due to the nonlinearity in the disease dynamics and coupling functions, linear approximation with Taylor series is implemented. Parameters of the coupled model are updated in each time point to enhance the accuracy of the approximation. For a specific time point \(t\), linearized disease dynamics, Eqs. (1)–(6), of time \(t\) follow

\[
S_i(t+1) = -\mu_0 + (1 + \mu_i^1)S_i(t) + \sum_j \mu_j^2 I_j(t) + \sum_j \mu_j^3 U_{i,j}(t) + \epsilon_i^1,
\]

\[
E_i(t+1) = -\mu_0 - \mu_i^1 S_i(t) - \sum_j \mu_j^2 I_j(t) - \sum_j \mu_j^3 U_{i,j}(t) + (1 - \gamma_{EI})E_i(t) - \epsilon_i^1,
\]

\[
I_i(t+1) = I_i(t) + \gamma_{EI} E_i(t) - (\gamma_{HI} + \gamma_{IR}) I_i(t),
\]

\[
H_i(t+1) = H_i(t) + \gamma_{HI} I_i(t) - \tau_H H_i(t),
\]

\[
R_i(t+1) = R_i(t) + \gamma_{IR} I_i(t) + \gamma_{HR} H_i(t) + \mu_i^1 U_{i,j}(t) + \epsilon_i^2.
\]
\[ D_j(t + 1) = D_j(t) + \gamma_{iD}(t)H_i(t) - \mu_1^i U_{i,k}(t) - \epsilon_2^i, \]

where
\[ \mu_1^i = \frac{\partial S_i(t + 1)}{\partial S_i(t)} \bigg|_{S_i(t), E_i(t), U_{i,k}(t), I_j(t)} = -\sum_j \frac{\beta_{i,j}(\theta_j(t), U_{i,k}(t))I_j(t)}{N_j}, \]
\[ \mu_2^{ij} = \frac{\partial S_i(t + 1)}{\partial I_j(t)} \bigg|_{S_i(t), E_i(t), U_{i,k}(t), I_j(t)} = -\frac{\beta_{i,j}(\theta_j(t), U_{i,k}(t))S_j(t)}{N_j}, \]
\[ \mu_3^{ij} = \frac{\partial S_i(t + 1)}{\partial U_{i,k}(t)} \bigg|_{S_i(t), E_i(t), U_{i,k}(t), I_j(t)} = \frac{2S_i(t)I_j(t)\gamma_{CN,j}(t)\beta_0(P_l - 1)}{N_j(P_l + 1)} \frac{10^6 \epsilon_{ij}^u U_{i,k}(t)}{(1 + e^{10^6 \epsilon_{ij}^u U_{i,k}(t)})^2}, \]
\[ \mu_4^i = \frac{\partial B_i(t + 1)}{\partial U_{i,k}(t)} \bigg|_{S_i(t), E_i(t), U_{i,k}(t), I_j(t)} = \frac{H_i(t)\tau_{hi}\delta_{pi}}{1 + P_l} \frac{10^6 \epsilon_{ij}^u U_{i,k}(t)}{(1 + e^{10^6 \epsilon_{ij}^u U_{i,k}(t)})^2}, \]
\[ \epsilon_1^i = -[\mu_1^i, \mu_2^{ij}, \mu_3^{ij}, \mu_4^i][S_i(t), I_j(t), U_{i,k}(t)]^T, \]
\[ \epsilon_2^i = -\mu_4^i U_{i,k}(t). \]

The disease-dependent capacity function in Eq. (9) is also linearized to obtain
\[ w_{i,k}(t) \leq -e^{-\frac{\mu_{i,k}(t)}{N_i}}I_i(t) + \left(1 + \frac{\gamma_{i}I_i(t)}{N_i}\right)e^{-\frac{\mu_{i,k}(t)}{N_i}}\bar{W}_{i,k}. \]
The code will be available upon the request.
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Author contributions
X.L., A.G. and B.I.E. designed the study and developed the algorithm. X.L. and A.G. contributed equally to developing coupling functions and performing the numerical simulations with input from B.I.E. X.L. formulated the supply chain network and developed the NPC. A.G. formulated the disease model and conducted parameter fitting. J.D. and P.R. provided feedback in model formulation and data interpretation. X.L. and A.G. analyzed results and wrote the initial draft with help from all authors. All authors reviewed and approved the manuscript. B.I.E. supervised the project.

Competing interests
The authors declare no competing interests.

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