X-ray line in Radiative Neutrino Model with Global $U(1)$ Symmetry

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Abstract

We study a three loop induced radiative neutrino model with global $U(1)$ symmetry at TeV scale, in which we consider two component dark matter particles. We discuss the possibility to explain the X-ray line signal at about 3.5 keV recently reported by XMN-Newton X-ray observatory using data of various galaxy clusters and Andromeda galaxy. Subsequently, we also discuss to show that sizable muon anomalous magnetic moment, a discrepancy of the effective number of neutrino species $\Delta N_{\text{eff}} \approx 0.39$, and scattering cross section detected by direct detection searches can be derived.

Keywords: Multicomponent Dark Matter Particles, X-ray Line, Muon $g - 2$, $\Delta N_{\text{eff}}$, Direct Detection

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I. INTRODUCTION

Neutrinos and dark matter (DM) physics apparently comes into a new physics beyond the standard model (SM). One of the elegant scenarios simultaneously to explain them is to generate the neutrino masses at multi-loop level \[1, 47, 48, 53, 54\], in which DM could be a messenger particle to tie the neutrinos to the Higgs boson. Thus we can naturally interpret the reason why the neutrino masses are so tiny.

In view of DM, two groups recently reported anomalous X-ray line signal at 3.55 keV from the analysis of XMN-Newton X-ray observatory data of various galaxy clusters and Andromeda galaxy \[55, 56\]. Once one applies the decaying DM scenario, such a X-ray line can be clearly explained by a 7.1 keV DM mass with small mixing angle; \(\sin^2 2\beta \approx 10^{-10}\), between DM and the neutrinos. Since the fact provides a lot of implications on the nature of DM, many works have been studied \[57–87\]. In our letter, we propose a model that such a small mixing can be generated at one-loop level, in which the neutrino masses are generated at three-loop level. To realize it, we introduce a global continuous \(U(1)\) symmetry. As a subsequent result of the additional symmetry, we can also explain the discrepancy of the effective number of neutrino species \(\Delta N_{\text{eff}} \approx 0.39\), which was suggested by Ref. \[88\]. As the other aspects, sizable muon anomalous magnetic moment and scattering cross section detected by direct detection searches can be derived.

This paper is organized as follows. In Sec. II, we show our model building including Higgs potential, neutrino masses, and muon anomalous magnetic moment. In Sec. III, we analyze DM properties including relic density, X-ray line, and the direct detection with multicomponent scenario. We summarize and conclude in Sec. VI.

II. THE MODEL

A. Model setup

We discuss a three-loop induced radiative neutrino model. The particle contents and their charges are shown in Tab.II. We add gauge singlet charged fermions \(E_L\) and \(E_R\), two gauge singlet Majorana fermions \(N_R\), and a gauge singlet Majorana DM \(X_R\). For new bosons, we introduce \(SU(2)_L\) doublet scalars \(\eta\), two singly-charged singlet scalars \((\chi_1^+, \chi_2^+)\), and a neutral singlet scalar \(\chi_0\) to the SM. We assume that only the SM-like Higgs \(\Phi\) and \(\chi_0\) have vacuum expectation values.
Table I: Contents of lepton and scalar fields and their charge assignments under $SU(2)_L \times U(1)_Y \times U(1) \times Z_2$.

(VEVs), which are symbolized by $v$ and $v'$ respectively. We also introduce a global $U(1)$ symmetry, under which $\Phi$ and $\eta$ do not have the charge in order not to couple to the goldstone boson (GB) $\eta$. $x \neq 0$ is an arbitrary number of the charge of $U(1)$ symmetry, and their assignments can realize our neutrino model at three loop level. The $Z_2$ symmetry assures the stability of DM that is the neutral component of $\eta$.

The renormalizable Lagrangian for Yukawa sector, mass term, and scalar potential under these assignments are given by

$$L_Y = y_l \bar{L}_L \Phi e_R + y_\nu \bar{L}_L \eta e_R + y_{\chi_1} \bar{E}_L \chi_1^- + y_{\chi_2} \bar{E}_L \chi_2^- + y_N \chi_0 \bar{N}_R N_R$$

$$+ y_N \chi_0 \bar{N}_R X_R + M_E \bar{E}_L E_R + h.c.$$

$$\mathcal{V} = m_\Phi^2 |\Phi|^2 + m_\eta^2 |\eta|^2 + m_{\chi_1}^2 |\chi_1^+|^2 + m_{\chi_2}^2 |\chi_2^+|^2 + m_{\chi_0}^2 |\chi_0|^2 + \left[ \lambda_0 \Phi^T (i \sigma_2) \eta \chi_1^- \chi_0 + \lambda_0 (\chi_1^+ \chi_2^-)^2 + h.c. \right]$$

$$+ \lambda_1 |\Phi|^4 + \lambda_2 |\eta|^4 + \lambda_3 |\Phi|^2 |\eta|^2 + \lambda_4 (\Phi^T \eta)(\eta^T \Phi) + \left[ \lambda_5 (\Phi^T \eta)^2 + h.c. \right] + \lambda_6 |\Phi|^2 |\chi_1^+|^2$$

$$+ \lambda_7 |\eta|^2 |\chi_1^+|^2 + \lambda_8 |\Phi|^2 |\chi_2^+|^2 + \lambda_9 |\eta|^2 |\chi_2^+|^2 + \lambda_{10} |\chi_1^+|^4 + \lambda_{11} |\chi_2^+|^4 + \lambda_{12} |\chi_1^+|^2 |\chi_2^+|^2$$

$$+ \lambda_{13} |\Phi|^2 |\chi_0|^2 + \lambda_{14} |\eta|^2 |\chi_0|^2 + \lambda_{15} |\chi_1^+|^2 |\chi_0|^2 + \lambda_{16} |\chi_2^+|^2 |\chi_0|^2 + \lambda_{17} |\chi_0|^4 + \left[ \lambda_{18} (\Phi^T \eta)(\chi_1^+ \chi_2^-) + h.c. \right],$$

where the first term of $L_Y$ can generates the SM charged-lepton masses, and we assume $\lambda_0$, $\lambda_0'$, $\lambda_5$, and $\lambda_{18}$ to be real.

The scalar fields can be parameterized as

$$\Phi = \begin{pmatrix} w^+ \\ \frac{1}{\sqrt{2}}(v + \phi + iz) \end{pmatrix}, \quad \eta = \begin{pmatrix} \eta^+ \\ \frac{1}{\sqrt{2}}(\eta_R + i \eta_I) \end{pmatrix}, \quad \chi_0 = \frac{v' + \sigma}{\sqrt{2}} e^{iG/v'}.$$  

where $v \simeq 246$ GeV is the VEV of the Higgs doublet, and $w^\pm$ and $z$ are respectively GB which are absorbed by the longitudinal component of $W$ and $Z$ bosons. Inserting the tadpole conditions;
\[ \partial V / \partial \phi |_{\nu} = 0 \quad \text{and} \quad \partial V / \partial \sigma |_{\nu} = 0, \]
The resulting mass matrix of the CP even boson \((\phi, \sigma)\) is given by

\[
m^2(\phi, \sigma) = \begin{pmatrix} 2\lambda_1 v^2 & \lambda_{13} v v' \\ \lambda_{13} v v' & 2\lambda_{17} v'^2 \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} m_h^2 & 0 \\ 0 & m_H^2 \end{pmatrix} \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix},
\]

(II.4)

where \(h\) is the SM-like Higgs and \(H\) is an additional CP-even Higgs mass eigenstate. The mixing angle \(\alpha\) is given by

\[
\sin 2\alpha = \frac{2\lambda_{13} v v'}{m_h^2 - m_H^2}.
\]

(II.5)

The Higgs bosons \(\phi\) and \(\sigma\) are rewritten in terms of the mass eigenstates \(h\) and \(H\) as

\[
\phi = h \cos \alpha + H \sin \alpha,
\]
\[
\sigma = -h \sin \alpha + H \cos \alpha.
\]

(II.6)

GB appears due to the spontaneous symmetry breaking of the global \(U(1)\) symmetry.

The mass matrix \(M_\pm^2\) of the singly-charged scalar boson \((\eta^\pm, \chi_1^\pm)\) is given by

\[
M_\pm^2 = \begin{pmatrix} m_{\eta^\pm}^2 + \frac{\lambda_{14} v^2}{2} & \frac{\lambda_0 v v'}{2} \\ \frac{\lambda_0 v v'}{2} & m_{\chi_1^\pm}^2 + \frac{\lambda_{15} v'^2}{2} \end{pmatrix}.
\]

(II.7)

The mass eigenstates \(h^\pm, H^\pm\) are defined by introducing the mixing angle \(\theta\) as

\[
\begin{pmatrix} \eta^\pm \\ \chi_1^\pm \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h^\pm \\ H^\pm \end{pmatrix},
\]

(II.8)

where the mixing angle \(\theta\) is given by

\[
\sin 2\theta = \frac{\lambda_0 v v'}{m_{h^\pm}^2 - m_{H^\pm}^2}.
\]

(II.9)

The other mass eigenstates are given as

\[
m_{\chi_2^\pm}^2 = m_{\chi_2}^2 + \frac{1}{2} (\lambda_8 v^2 + \lambda_{16} v'^2),
\]

(II.10)

\[
m_{H_R}^2 = m_{\eta_R}^2 + \frac{1}{2} \lambda_{14} v'^2 + \frac{1}{2} (\lambda_3 + \lambda_4 + 2\lambda_5) v^2,
\]

(II.11)

\[
m_{H_I}^2 = m_{\eta_I}^2 + \frac{1}{2} \lambda_{14} v'^2 + \frac{1}{2} (\lambda_3 + \lambda_4 - 2\lambda_5) v^2.
\]

(II.12)
B. Neutrino mass matrix

The Majorana neutrino mass matrix $m_\nu$ is derived at three-loop level from the diagrams depicted in Fig. II, which is given by

$$
(m_\nu)_{ij} = \frac{\lambda'_0}{(4\pi)^6} \sum_{\beta=1}^2 \sum_{\gamma=1}^2 [(y_\eta)_i(y_{\chi_2})_\beta M_N^{\beta\gamma}(y_\chi_2)_\gamma] \sin^2 \theta \cos^2 \theta \times 
$$

$$
\left[ F_1 \left( \frac{m_{h^+}^2}{M_E^2}, \frac{m_{h^+}^2}{M_E^2} \right) + \frac{2}{2} F_1 \left( \frac{m_{H^+}^2}{M_E^2}, \frac{m_{H^+}^2}{M_E^2} \right) - 2 F_1 \left( \frac{m_{h^+}^2}{M_E^2}, \frac{m_{H^+}^2}{M_E^2} \right) \right],
$$

(II.13)
where $M_N \equiv y_N v'/\sqrt{2}$ the loop function $F_1$ is computed as

$$F_1(X_1, X_2) = \int d^3x \frac{\delta(x + y + z - 1)}{z(z - 1)} \int d^3x' \frac{\delta(x' + y' + z' - 1)}{z'(z' - 1)} \int d^3x'' \frac{\delta(x'' + y'' + z'' - 1)}{x'' + z''X_1 - y''\Delta(X_2)},$$

(II.14)

with

$$\Delta(X_2) = \frac{y'M^2_{\beta\nu} + z'M^2_{\chi_2}}{M^2_E} - x'\Delta'(X_2), \quad \Delta'(X_2) = \frac{x + z\frac{M^2_{\chi_2}}{M^2_E} - yX_2}{z(z - 1)},$$

(II.15)

where we define $d^3x \equiv dx dy dz$, $d^3x' \equiv dx' dy' dz'$, and $d^3x'' \equiv dx'' dy'' dz''$. To obtain the neutrino masses reported by Planck data \[89\]; $m_{\nu} < 0.933$ eV, the following is required

$$\lambda_{0y_\eta^2}M_N \left[ F_1 \left( \frac{m^2_{\mu^+}}{M^2_E} \right) + F_1 \left( \frac{m^2_{h^+}}{M^2_E} \right) - 2F_1 \left( \frac{m^2_{\mu^+}}{M^2_E} \right) \right] < 1.17 \text{ MeV},$$

(II.16)

where we we fix $\theta = \pi/4$ for simplicity, and $y_\eta^2 \approx 4\pi$ to obtain the sizable muon anomalous magnetic moment as discussed below.

C. muon anomalous magnetic moment

In principle, we obtain the LFV process from the terms which are proportional to $y_\eta$. Especially, $\mu \rightarrow e\gamma$ process gives the most stringent bound. However since we can fix $y_\eta$ to be the diagonal matrix \(^1\), we can simply avoid such kind of processes. So we move on to the discussion of the muon anomalous magnetic moment.

The muon anomalous magnetic moment has been measured at Brookhaven National Laboratory. The current average of the experimental results is given by \[90\]

$$a_{\mu}^{\text{exp}} = 11659208.0(6.3) \times 10^{-10},$$

which has a discrepancy from the SM prediction by $3.2\sigma$ \[91\] to $4.1\sigma$ \[92\] as

$$\Delta a_{\mu} = a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = (29.0 \pm 9.0 \text{ to } 33.5 \pm 8.2) \times 10^{-10}.$$  

(II.17)

We have a contribution on the this process through the term of $y_\eta$, as can be seen in Fig. 2. The formula is given as

$$\Delta a_{\mu} = \frac{1}{2(4\pi)^2} |y_\eta|^2 \left( \frac{m_{\mu}}{M^2_E} \right)^2 \left[ F_2 \left( \frac{m^2_{\eta^R}}{M^2_E} \right) + F_2 \left( \frac{m^2_{\eta^L}}{M^2_E} \right) \right],$$

(II.18)

\(^1\) We expect that the mixing of MNS can be obtained by $y_{\chi_2}$ and $M_N$. 

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where

\[ F_2(x) = \frac{1 - 6x + 3x^2 + 2x^3 - 6x^2 \ln x}{6(1 - x)^4}. \]  

(II.19)

FIG. 2: Diagram of the muon anomalous magnetic moment.

We can obtain sizable muon anomalous magnetic moment

\[ \Delta a_\mu \approx 1.5 \times 10^{-9}, \]  

(II.20)

if we set \( y_\eta \approx \mathcal{O}(\sqrt{4\pi}) \) that is limit of the perturbative which is within the 2\(\sigma\) error, theory, \( M_E \approx \mathcal{O}(300) \) GeV that comes from the analogy of the slepton search of LHC [93], and \( m_{\eta_R} \approx m_{\eta_I} = 67.83 \) GeV, which can be obtained from the DM analysis as can be seen in the next section.
III. DARK MATTER PARTICLES

We have two DM candidates $X_R$ and $\eta_R$, which do not interact each other at tree level. Hence two component scenario can be taken in consideration. Since $X_R$ can be expected to explain the X-ray line at 3.55 keV, its mass $M_X \equiv y_X v'/\sqrt{2}$ be 7.1 keV. On the other hand, since $\eta_R$ is expected to be detected direct detection searches such as LUX [94], its mass range be $m_{\eta_R} \approx O(10^{-80})$ GeV [95], where we restrict ourselves the mass be less than the mass of the SM gauge bosons to forbid the too large cross section. Hereafter we simply assume that the number density of DMs is the same rate, that is, $\Omega_{X_R}h^2 : \Omega_{\eta_R}h^2 = 1 : 1$. Also we suppose that both are assumed to be the cold DMs, and the mixing of $\alpha$ sets to be zero to analyze the cross section of the relic density because it is not so sensitive to the cross section.

A. $X_R$ dark matter

The dominant relativistic cross section of $X_R$, which is $2X_R \to H \to 2G$ via s-channel, is given by

$$\langle \sigma v \rangle_{\text{rel}} \approx \frac{M_X^6}{4\pi v'^4} \frac{v_{\text{rel}}^2}{(4M_X^2 - m_H^2)^2}. \quad (\text{III.1})$$

To obtain the correct relic density $\Omega_{X_R}h^2 = 0.12/2$ [89], the required cross section be

$$\langle \sigma v \rangle_{\text{rel}} \approx 3.06 \times 10^{-8} \text{ GeV}^{-2}. \quad (\text{III.2})$$

Once we set $v' \approx 1$ GeV, $m_H$ be

$$m_H \approx 1.421 \times 10^{-5} \text{ GeV} \approx 2M_X. \quad (\text{III.3})$$

The above result implies that a mild fine-tuning is needed.

Here we consider the contribution of GB to the effective number of neutrino species $\Delta N_{\text{eff}} \approx 0.39$ suggested by [88]. It can be realized when the appropriate era of freeze-out of the Goldstone boson is before muon annihilation while the other SM particles are decoupled. Thus it corresponds to $T \approx m_\mu$, where $T$ is the temperature of the universe. The scattering of the Goldstone boson with the SM particles occurs through the Higgs exchange. Then the interaction rate be the same order as the Hubble parameter at $T \approx m_\mu$. Considering the above process, one leads to the following

\footnote{Since the decay rate of the $H$ is very tiny as well as the one of $h$, we neglect these contributions.}
relation [34],

\[
\sin 2\alpha \approx \sqrt{\frac{4(vv')^2(m_h m_H)^4}{(m_h^2 - m_H^2)^2 m_\mu^2 m_{pl}}} \approx 7.33 \times 10^{-14},
\]

(III.4)

where \(m_{pl} \approx 1.22 \times 10^{19}\) GeV, and \(m_\mu \approx 0.106\) GeV.

The mixing between \(X_R\) and the active neutrinos can be obtained at one-loop level as depicted in Fig 3 and it is given by

\[
\beta_{X_R-\nu} = \frac{M_E y_X y_\nu}{2\sqrt{2}(4\pi)^2 M_X} \int_0^1 dx \ln \left[\frac{x + (1 - x)\Delta_{h^+}}{x + (1 - x)\Delta_{H^+}}\right] \approx 7.1 \times 10^{-6},
\]

(III.5)

where \(\Delta_{h^+} \equiv m_{h^+}^2/M_E^2\) and \(\Delta_{H^+} \equiv m_{H^+}^2/M_E^2\). When \(\Delta_{h^+}\) and \(\Delta_{H^+}\) are larger than 1 and

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**FIG. 3:** Mixing between neutrinos and DM.
\( y_\eta y_\chi_1 \approx 0.001 \), we obtain
\[
\lambda_0 = \frac{m_{H^+}^2 - m_{h^+}^2}{\nu \nu'} \approx 1.91 \times 10^{-6} \left( \frac{M_E}{\text{GeV}} \right)^2 \approx 0.172, \tag{III.6}
\]
combining with Eq. (II.9).

**B. \( \eta_R \) dark matter**

The dominant relativistic cross section of \( \eta_R \), which is \( 2X_R \rightarrow H \rightarrow 2G \) via s-channel and \( 2X_R \rightarrow 2H \), is given by
\[
(\sigma v)_{\text{rel}} \approx \frac{5\lambda_{14}^2}{64\pi m_{\eta_R}^2}.
\]
To obtain our relic density \( \Omega_{\eta_R} h^2 = 0.12/2 \), the required cross section be
\[
(\sigma v)_{\text{rel}} \approx 5.41 \times 10^{-9} \text{ GeV}^{-2}. \tag{III.8}
\]
Once we set \( \lambda_{14}^2 \approx 0.001 \), we obtain
\[
m_{\eta_R} \approx 64.38 \text{ GeV}. \tag{III.9}
\]

**C. Direct Detection**

\( \eta_R \) can be tested by the spin independent elastic scattering cross section, and it form is give by
\[
\sigma \approx \frac{0.079}{\pi} \left( \frac{m_p}{m_{\eta_R} v} \right)^2 \left( \frac{(\lambda_3 + \lambda_4 + 2\lambda_5) v}{m_h} \cos \alpha + \frac{\lambda_{14} v'}{m_H^2} \sin \alpha \right)^2 \text{GeV}^2, \tag{III.10}
\]
where \( m_p \approx 0.938 \) GeV is the proton mass. The current lowest bound of \( \sigma \) can be found by the experiment of LUX, which be around \( \mathcal{O}(10^{-45}) \) cm\(^2\) at \( m_{\eta_R} \approx 64 \) GeV. Inserting all the fixed parameters, we can satisfy this constraint if
\[
\lambda_3 + \lambda_4 + 2\lambda_5 \leq 0.011. \tag{III.11}
\]

**IV. CONCLUSIONS**

We have constructed a three-loop induced neutrino model with a global \( U(1) \) symmetry, in which we have naturally explained the X-ray line signal at about 3.5 keV with \( X_R \) recently reported by

\footnote{The \( t \)- and \( u \)-processes through the term of \( y_\eta \) can be negligible because of the \( d \)-wave suppression.}
XMN-Newton X-ray observatory using data of various galaxy clusters and Andromeda galaxy. Subsequently, we have also shown that sizable muon anomalous magnetic moment within $2\sigma$ error, which is around $1.5 \times 10^{-9}$. The effective number of neutrino species $N_{\text{eff}} \approx 0.39$ can be derived at an appropriate parameter set due to the additional symmetry. Since our model has two DM candidates that does not interact each other due to the $U(1)$ symmetry, another candidate ($\eta_R$) can be tested by the current direct detection searches such as LUX.

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Radiative models of the lepton mass are sometimes discussed with Non-Abelian discrete symmetries due to their selection rules. See for example such kind of models:
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