A Light Higgs at the LHC and the B-Anomalies

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Abstract

After the Higgs discovery, the LHC has been looking for new resonances, decaying into pairs of Standard Model (SM) particles. Recently, the CMS experiment observed an excess in the di-photon channel, with a di-photon invariant mass of about 96 GeV. This mass range is similar to the one of an excess observed in the search for the associated production of Higgs bosons with the Z neutral gauge boson at LEP, with the Higgs bosons decaying to bottom quark pairs. On the other hand, the LHCb experiment observed a discrepancy with respect to the SM expectations of the ratio of the decay of B-mesons to K-mesons and a pair of leptons, \(R_{K^{(*)}} = \frac{BR(B \rightarrow K^{(*)}\mu^+\mu^-)}{BR(B \rightarrow K^{(*)}e^+e^-)}\). This observation provides a hint of the violation of lepton-flavor universality in the charged lepton sector and may be explained by the existence of a vector boson originating from a \(U(1)_{L_\mu-L_\tau}\) symmetry and heavy quarks that mix with the left-handed down quarks. Since the coupling to heavy quarks could lead to sizable Higgs di-photon rates in the gluon fusion channel, in this article we propose a common origin of these anomalies identifying a Higgs associated with the breakdown of the \(U(1)_{L_\mu-L_\tau}\) symmetry and at the same time responsible to the quark mixing, with the one observed at the LHC. We also discuss the constraints on the identification of the same Higgs with the one associated with the bottom quark pair excess observed at LEP.
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I. INTRODUCTION

The discovery of a scalar resonance, with properties similar to the ones expected for the Higgs boson in the Standard Model (SM), has provided evidence for the realization of the simplest Higgs mechanism scenario of electroweak symmetry breaking. The couplings of the observed Higgs boson to the SM particles is within a few tens of percent of the ones expected
within the SM. Small deviations of these coupling with respect to the SM values are still possible, and are expected in extensions of the Higgs sector that occur in most beyond the SM scenarios. For this reason, since the Higgs discovery, apart from a precise determination of the Higgs couplings, the LHC has been looking for new scalar resonances, with the di-photon channel being one of the most sensitive ones. Recently, the CMS experiment reported a $2.9 \sigma$ excess in this channel [1], with a di-photon invariant mass of about 95.3 GeV. This excess was mildly present in the 8 TeV run [2], but became prominent only in the 13 TeV run. While the ATLAS experiment did not observe any significant excess in this mass region in the 8 TeV run [3], it has not yet reported the results of a similar search in the 13 TeV run.

Searches for Higgs boson resonances produced in association with the $Z$ gauge boson, with Higgs bosons decaying into bottom-quark pairs, were conducted at LEP. The combination of the results of the four experiments, ALEPH, DELPHI, L3 and OPAL, led to the presence of a $2.3 \sigma$ local excess at an invariant mass of about 95–100 GeV [4]. The agreement between the invariant mass of the excesses observed at LEP and CMS calls for a possible common origin of these two signatures [5–10].

On the other hand, the LHCb experiment has reported an intriguing hint of the violation of lepton-flavor universality in the decay of $B$-mesons into $K$-mesons and lepton pairs [11, 12], namely

$$R_K = \frac{BR(B \to K\mu^+\mu^-)}{BR(B \to Ke^+e^-)} = 0.745^{+0.097}_{-0.082}$$ (1)

while

$$R_{K^*} = \frac{BR(B \to K^*\mu^+\mu^-)}{BR(B \to K^*e^+e^-)} = 0.660^{+0.113}_{-0.074}.$$ (2)

A possible explanation of these anomalies may be provided by the introduction of a gauge boson associated with the $U(1)_{L_\mu-L_\tau}$ symmetry [13–22] or other flavor symmetry [23–26]. The absence of a coupling to electrons explains the deviation of the above ratios with respect to one, the value expected within the SM. In order to allow the coupling of the new gauge boson to the $B$ meson, one can introduce new vector like quarks that mix with the ordinary third and second generation quarks and that is charged under the new gauge symmetry, see the illustrative diagram in Fig. 1. Such a quark mixing may be induced by the vacuum expectation value of a new Higgs boson that is neutral under the SM gauge symmetries. The coupling of this Higgs boson to the vector like quarks can induce sizable couplings to photons
FIG. 1. Feynman diagram showing how the Higgs $\phi$ induces an off-diagonal coupling of the new gauge boson $Z'$ to the strange and bottom quarks via the mixing of the SM quarks with the heavy vector-like quark $\psi$. This process induces a contribution to the $C_{9}^{NP}$ effective operator which is responsible for the B-anomalies. A sizable coupling of the Higgs $\phi$ to di-photons and di-gluons will be induced via the coupling to the heavy quark, and hence $\phi$ could be potentially identified with the one observed by the CMS [1, 2] experiment in the di-photon channel.

and gluons, which could be searched in the di-photon channel. Similarly, a mixing of such a Higgs with the SM-like Higgs boson can induce a coupling to the SM gauge bosons, while couplings to quarks are induced by Higgs and quark mixing effects. Hence, such a Higgs can also be produced in association with gauge bosons, subsequently decaying to bottom quark pairs. Therefore, a very natural question is whether such Higgs boson can be identified with the one that is observed by the CMS and LEP experiments. We analyze the signal and existing constraints in this paper and answer this interesting question in the conclusion section.

In this article, we shall describe the simplest scenario that can lead to a realization of this idea. In section II we shall present the model and describe the interaction of the Higgs and gauge bosons. In section III we shall discuss the possibility that a Higgs boson associated with the breakdown of the new $U(1)_{L_{\mu}-L_{\tau}}$ symmetry leads to an explanation of the CMS excess and explain the constraints associated with a simultaneous explanation of the LEP excess. In section IV we shall discuss the explanation of the anomalies seen in B-meson decays. In section V we shall concentrate on the collider and flavor physics constraints on this model. Finally, we reserve section VI for our conclusions, and the appendices for technical details associated with the scalar mixing parameters and the obtention of the proper CKM matrix elements within this model.
II. A MODEL WITH AN EXTRA $U(1)$, LIGHT HIGGS AND HEAVY VECTOR-LIKE QUARKS

In this section, we shall introduce a gauge extension of the Standard Model (SM) to include two extra light Higgs $S$, $\phi$ and one extra gauge boson $Z'$ associated with the $U(1)_{L_\mu-L_\tau}$ symmetry [21, 27–50]. The gauge charge $L_\mu - L_\tau$ is not flavor universal, but diagonal. We also need one extra vector-like heavy quark $\psi_{L,R}$ charged under both SM gauge and $U(1)_{L_\mu-L_\tau}$. The model is minimal to address the light Higgs and B-anomalies. The SM and new physics (NP) particles are listed in Table I along with their gauge charges. $q^i_L$ ($u^i_R, d^i_R$) are the $i$th generation left-handed (right-handed) SM quarks, where $i = 1, 2, 3$ is the SM quark generation index. $\ell^e, \mu, \tau$ and $e^R, \mu^R, \tau^R$ are three generations of SM left-handed and right-handed leptons. $S$ and $\phi$ are NP Higgs bosons, which are singlet under the SM gauge symmetry and are responsible to give mass to $U(1)_{L_\mu-L_\tau}$ gauge boson $Z'$. The fields $\psi_{L,R}$ the chiral components of a vector-like heavy quark, which has the same SM charge as $q^i_L$ and also charged under $U(1)_{L_\mu-L_\tau}$. The charge assignments of $\phi$ and $\psi$ under the $U(1)_{L_\mu-L_\tau}$ symmetry need to satisfy the relation $Q^{\phi}_{\mu-\tau} = \pm Q^{\psi}_{\mu-\tau}$ to allow for the appropriate Yukawa couplings. Without loss of generality, it can be taken to be $Q^{\phi}_{\mu-\tau} = -Q^{\psi}_{\mu-\tau} = 1/2$. The anomaly-free condition is satisfied because $U(1)_{L_\mu-L_\tau}$ is vector-like in the NP particle content. It is also anomaly-free within the SM sector. The vacuum expectation value of the field $\phi$ may induce a mixing between the SM quarks and the NP heavy quarks. In the following sections, we will discuss the model in details in the Higgs, gauge boson and quark sectors.

A. The Higgs sector and gauge boson sector

In the Higgs sector of this model, we have two extra Higgs $S$, $\phi$. We can write down the Lagrangian for the Higgs bosons,

$$\mathcal{L}_{\text{Higgs}} = (D_\mu \phi)^\dagger \, D^\mu \phi + (D_\mu S)^\dagger \, D^\mu S$$

$$- \mu_S^2 \phi^* \phi - \lambda_S (\phi^* \phi)^2 - \mu_S^2 S^* S - \lambda_S (S^* S)^2 - \mu_2 H^\dagger H - \lambda (H^\dagger H)^2$$

$$- \lambda_{\phi h} (\phi^* \phi) (H^\dagger H) - \lambda_{S h} (S^* S) (H^\dagger H) - \lambda_{S \phi} (S^* S) (\phi^* \phi).$$

\[3\]
\begin{table}
\centering
\begin{tabular}{|c|c|c|c|c|}
\hline
Parameter & SU(3)C & SU(2)L & U(1)Y & U(1)_{L_\mu-L_\tau} \\
\hline
H & 1 & 2 & $\frac{1}{2}$ & 0 \\
q^i_L & 3 & 2 & $\frac{1}{6}$ & 0 \\
u^i_R & 3 & 1 & $\frac{2}{3}$ & 0 \\
d^i_R & 3 & 1 & $-\frac{1}{3}$ & 0 \\
\ell^e & 1 & 2 & $-\frac{1}{2}$ & 0 \\
\ell^\mu & 1 & 2 & $-\frac{1}{2}$ & 1 \\
\ell^\tau & 1 & 2 & $-\frac{1}{2}$ & -1 \\
e_R & 1 & 1 & -1 & 0 \\
\mu_R & 1 & 1 & -1 & 1 \\
\tau_R & 1 & 1 & -1 & -1 \\
S & 1 & 1 & 0 & 1 \\
\phi & 1 & 1 & 0 & $\frac{1}{2}$ \\
\psi_{L,R} & 3 & 2 & $\frac{1}{6}$ & $-\frac{1}{2}$ \\
\hline
\end{tabular}
\caption{The particle content and their SU(3)$_C \times$ SU(2)$_L \times$ U(1)$_Y \times$ U(1)$_{L_\mu-L_\tau}$ gauge charge. $i = 1, 2, 3$ is the SM quark generation index. $S$ and $\phi$ are the NP Higgs, and $\psi_{L,R}$ are vector-like heavy quarks. The charge assignment $Q^\phi_{\mu-\tau} = -Q^\psi_{\mu-\tau}$ allows for the appropriate Yukawa couplings. Without loss of generality, it is taken to be 1/2.}
\end{table}

The covariant derivative $D_\mu = \partial_\mu - ig_DZ'_\mu Q_{L_\mu-L_\tau}$, with $g_D$ the gauge coupling of $U(1)_{L_\mu-L_\tau}$. The first line in $\mathcal{L}_{\text{Higgs}}$ are kinetic terms for $\phi$ and $S$, which give mass to $Z'$ after symmetry breaking, and others are scalar potential terms. The couplings $\lambda_{\phi h}$, $\lambda_{Sh}$ and $\lambda_{S\phi}$ define the Higgs portal terms, which induce the mixing between scalars. The scalar $\phi$, $S$ and SM Higgs $H$ get vevs and can be expanded near the minimum as $\phi = \frac{1}{\sqrt{2}} (\phi^0 + v_D)$, $S = \frac{1}{\sqrt{2}} (s^0 + v_S)$ and $H = \left(0, \frac{1}{\sqrt{2}} (h^0 + v)\right)$.

The gauge boson $Z'$ has no mass mixing with the SM gauge bosons. Only the two kinetic terms in the first line of Eq. (3) give the $Z'$ mass, which reads

$$m_{Z'} = g_D \sqrt{\frac{1}{4}v_D^2 + v_S^2}.$$ (4)
In our analysis, we assume the observed 96 GeV di-photon excess observed at CMS is predominantly associated with the CP-even component of $\phi^0$. This means $\nu_D$ is nearly the same order of the SM Higgs vev $v$. If there is no another Higgs $S$, the $Z'$ mass is too light and severely constrained by di-jet and di-lepton constraints in Section IV A. We therefore introduce another scalar $S$ with unit charge under $U(1)_{L_u-L_e}$, and that contribute to the $Z'$ mass, as described above. Therefore, the $Z'$ mass can be as heavy as several TeV with a large value of $v_S$ and we treat it as a free parameter thereafter. In the later analysis, we could find out $m_{Z'} \sim 4.1$ TeV, thus $m_{s^0}$ should be of the same order. We shall not consider the phenomenology of such a heavy Higgs, as it could easily decouple from the SM Higgs and $\phi$ phenomenology. In our analysis, we assume $\lambda_{Sh}$ and $\lambda_{S\phi}$ small, so that complemented with the heaviness of $s^0$ we can neglect its mixing with the light Higgs bosons and only consider the mixing between $H$ and $\phi$. On the other hand, $S$ has different $U(1)_{L_u-L_e}$ charge to $\Psi_{L,R}$ and SM quarks. It will not affect the quark sector mixing and we do not need to consider it any more.

For the scalar mixing, after ignore the effect of $S$, we only consider two scalars $\phi^0$ and $h^0$ with five free parameters $\mu_\phi, \mu, \lambda_\phi, \lambda$ and $\lambda_{\phi h}$. The five parameters can be traded to five physical observables, two vevs $\nu_D$ and $\nu$, two masses $m_{\tilde{h}}$ and $m_{\tilde{\phi}}$, and one mixing angle $\sin \alpha$. $\tilde{h}$ and $\tilde{\phi}$ are the mass eigenstates and related to $\phi^0$ and $h^0$ by

$$\begin{pmatrix} h^0 \\ \phi^0 \end{pmatrix} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \tilde{h} \\ \tilde{\phi} \end{pmatrix}.$$ 

(5)

The five physical observables are the more useful model parameters. The relations with the old parameters are given in Appendix A.

**B. The quark sector**

After the scalar sector, we are going to specify the mixings between the SM quarks and heavy vector-like quarks, which are responsible to induce the flavor violating couplings needed for the explanation of the B-anomalies. The most general interactions in the quark sector are given by:

$$L_q = i \bar{q}_L^i \gamma_\mu \bar{q}_L^j + i \bar{u}_R^i \gamma_\mu u_R^j + i \bar{d}_R^i \gamma_\mu d_R^j + i \bar{\psi} \gamma_\mu \psi - m_{\psi} \bar{\psi} \psi - \left( \bar{q}_L^i y_u^{ij} H u_R^j + \bar{d}_L^i y_d^{ij} H d_R^j + H.c. \right) - \left( \sqrt{2} \lambda_{i} \bar{q}_L^i \phi \psi_R + H.c. \right),$$

(6)
where $q_L$ are left-handed SM quarks, $u_R$ and $d_R$ are up-type and down-type right-handed SM quarks. $\psi$ is the heavy vector-like quark, $H$ is the SM Higgs and $\phi$ is the NP Higgs. $i,j$ are the generation index, $y_u, y_d$ are the SM Yukawa couplings. $\tilde{H}$ is defined as $\tilde{H} \equiv i\sigma_2 H^*$. The $SU(2)_L$ doublet $\psi$ can be written as components $(\psi_u^3, \psi_d^2)$, which are mass degenerate.

After the scalars obtained vevs, the mass and interaction terms for quarks are,

$$
\mathcal{L}_{\text{Higgs}} = - \sum_{q=u,d} (\bar{q}_L^3, \bar{q}_L^2, \overline{\psi}_L^q) \cdot (M_q + \Lambda_q) \cdot (q_R^3, q_R^2, \psi_R^q)^T + H.c.,
$$

where the sum over $q = u, d$ goes over the components of $SU(2)_L$ doublet. Since SM quarks are not charged under $U(1)_{L_\mu - L_\tau}$, their Yukawa couplings are SM-like with 9 free parameters. For simplicity, we include only the third and second generation of SM quarks together with the heavy quark $\psi$ in Eq. (7), to illustrate the essence of NP phenomenology. To further simplify the calculation, SM Yukawa couplings are chosen to be flavor diagonal. We shall relegate to the Appendix the discussion of the obtention of the CKM matrix elements, which is not relevant for our analysis. Thus, the mass matrix $M_q$ and interaction matrix $\Lambda_q$ are

$$
M_q = \begin{pmatrix} m_q^3 & 0 & \lambda_3 v_D \\ 0 & m_q^2 & \lambda_2 v_D \\ 0 & 0 & m_\psi \end{pmatrix}, \quad \Lambda_q = \begin{pmatrix} \frac{m_q^3}{v} h^0 & 0 & \lambda_3 \phi^0 \\ 0 & \frac{m_q^2}{v} h^0 & \lambda_2 \phi^0 \\ 0 & 0 & 0 \end{pmatrix}.
$$

Note for the up-type quarks $u^3 = t$ and $u^2 = c$ and for down-quark $d^3 = b$ and $d^2 = s$. In the matrices $M_q$ and $\Lambda_q$, only the diagonal mass elements are modified when changing from $u$ to $d$, while the terms proportional to $\lambda_{2,3}$ stay the same. Since $\psi$ is heavy vector-like quark, the masses have the sequence $m_\psi \gtrsim m_q^3 > m_q^2$, where as we will show $\lambda_2 v_D > m_\psi$ is necessary to obtain a large enough mixing between heavy quarks and SM 2nd generation quarks. For the up sector, since the top quark mass is of the order of the weak scale, $m_q^3$ can be comparable with $m_\psi$. To avoid large mixing between the top and the 3rd generation, and hence large Yukawas to obtain the proper top mass, we further assume $\lambda_2 \gg \lambda_3$ which suggests the heavy quark mostly mixes with 2nd generation left-handed SM quarks. After
diagonalizing $M_q$, we get the mass of the quark mass-eigenstates,

\[ m_{\tilde{q}}^2 \approx m_q^2 - \frac{m_{\tilde{q}}^2 \lambda_2^2 v_D^2}{\lambda_2^2 v_D^2 + m_{\tilde{q}}^2 - m_q^2} = m_q^2 (1 - \tan^2 \theta_3), \tag{9} \]

\[ m_q^2 \approx m_q^2 \frac{m_{\tilde{q}}^2}{m_{\tilde{q}}^2 + \lambda_2^2 v_D^2} = m_q^2 \cos^2 \theta_2, \tag{10} \]

\[ m_{\psi}^2 \approx m_{\psi}^2 + v_D^2 \lambda_2^2 + \frac{\lambda_3^2 \lambda_2^2 v_D^2 (m_{\psi}^2 + m_q^2)}{\lambda_2^2 v_D^2 + m_{\psi}^2 - m_q^2} + m_q^2 \frac{\lambda_3^2 v_D^2 + m_{\psi}^2}{\lambda_2^2 v_D^2 + m_{\psi}^2} \approx m_{\psi}^2 + \lambda_2^2 v_D^2, \tag{11} \]

where in the last equality we only keep the leading term and we define $\tan \theta_2 \equiv \frac{\lambda_2 v_D}{m_{\psi}}$ and $\tan \theta_3 \equiv \frac{\lambda_3 v_D}{\sqrt{\lambda_2^2 v_D^2 + m_{\psi}^2 - m_q^2}}$. Following the mass and coupling assumption, $\tan \theta_3 \ll 1$. As explained above, to fit the B-meson decay anomalies, $\lambda_2 v_D$ needs to be larger than $m_{\psi}$, which suggests $\sin \theta_2$ and $\cos \theta_2$ are of $O(1)$. Note that the mass of $\tilde{\psi}_u$ and $\tilde{\psi}_d$ are almost degenerate, only different by small 2nd generation quark mass $m_{\tilde{q}}$ and coupling $\lambda_3$.

The mixing matrices $U_{L,R}^q$ connect flavor and mass eigenstates as

\[ (q^3, q^2, \psi^q)^T_{L,R} = U_{L,R}^q \cdot (\tilde{q}^3, \tilde{q}^2, \tilde{\psi}^q)^T_{L,R}, \tag{12} \]

where the states with tilde are the mass eigenstates for the quarks. The mixing matrices at leading order are

\[ U_L^q \approx \begin{pmatrix} 1 + \frac{1}{2} t_{\theta_3}^2 & 0 & t_{\theta_3} \\ -s_{\theta_2} t_{\theta_3} & c_{\theta_2} \left( 1 + \frac{m_{\tilde{q}}^2 t_{\theta_3}^2}{m_{\tilde{q}}^2} \right) & s_{\theta_2} \left( 1 + \frac{m_{\tilde{q}}^2 t_{\theta_3}^2}{m_{\tilde{q}}^2} - \frac{1}{2} t_{\theta_3}^2 \right) \\ -c_{\theta_2} t_{\theta_3} & s_{\theta_2} \left( 1 + \frac{m_{\tilde{q}}^2 t_{\theta_3}^2}{m_{\tilde{q}}^2} \right) & c_{\theta_2} \left( 1 - \frac{m_{\tilde{q}}^2 t_{\theta_3}^2}{m_{\tilde{q}}^2} + \frac{1}{2} t_{\theta_3}^2 \right) \end{pmatrix}, \tag{13} \]

\[ U_R^q \approx \begin{pmatrix} 1 & \frac{m_{\tilde{q}}^2}{m_{\tilde{q}}^2} t_{\theta_3} & \frac{m_{\tilde{q}}^3}{m_{\tilde{q}}^2} t_{\theta_3} \\ -\frac{m_{\tilde{q}}^2}{m_{\tilde{q}}^2} t_{\theta_3} & 1 & \frac{m_{\tilde{q}}^2}{m_{\tilde{q}}^2} s_{\theta_2} \\ -\frac{m_{\tilde{q}}^3}{m_{\tilde{q}}^2} t_{\theta_3} & -\frac{m_{\tilde{q}}^2}{m_{\tilde{q}}^2} s_{\theta_2} & 1 \end{pmatrix}, \tag{14} \]

where $s_{\theta_2}, c_{\theta_2}, t_{\theta_2}$ are abbreviations for $\sin \theta_2, \cos \theta_2$ and $\tan \theta_2$.

We see that $U_R^q$ is close to identity matrix with off-diagonal terms suppressed by small SM quark mass $m_{\tilde{q}_1,\tilde{q}_3}$ or $\tan \theta_3$. Because the heavy vector-like quark has the same gauge SM charge as the left-handed SM quarks, thus the mixing dominantly happens between the left-handed quarks. For the left-handed mixing $U_L^q$ in Eq. (13), the leading term are the same for up-type an down-type quarks, if neglecting the SM quark masses.
The SM Cabibbo-Kobayashi-Maskawa (CKM) matrix elements should be obtained from $V_{CKM} \equiv U^u_L U^d_L$. However, since we did not include off-diagonal matrix elements for the SM-quarks, all non-vanishing elements will be proportional to ratios of the SM-quark masses and the heavy fermion masses. In reality, the successful generation of CKM matrix needs to include the 1st generation SM quark mass and the off-diagonal terms in SM Yukawa couplings. In principle, with 9 free mass parameters in SM quark sector, there should be no problem to generate CKM matrix. We will demonstrate the generation of all the $V_{CKM}$ terms in the Appendix B, and show that it does not affect the NP phenomenology we are interested here.

After the discussion of the quark sector, it is worth to mention that the charged leptons can easily get mass with diagonal SM Yukawa terms. For neutrino mass and Pontecorvo–Maki–Nakagawa–Sakata (PMNS) matrix under gauge interaction $U(1)_{L_\mu - L_\tau}$, it is generally easy to accommodate. The reason is that $L_\mu - L_\tau$ gauge satisfies $\mu \leftrightarrow \tau$ permutation which leads to mixing angle $\theta_{23}$ close to maximal (45°) while having a vanishing mixing angle $\theta_{13}$ at leading order (see review [51]). Since neutrino mass is not relevant of the NP phenomenology we are interested in, we do not modify the lepton sector further.

C. Light and heavy quark interactions

In this subsection, the flavor eigenstate scalars and quarks are rotated into mass eigenstates. In the mass eigenstate, the Yukawa interactions for scalars and quarks are,

$$L_{Higgs} \supset \frac{m_b}{v} \left( \frac{v}{v_D} t^2_{\theta_3} \left( \frac{m_b^2}{m_{\tilde{b}}^2} - c_{\theta_2}^2 \right) s_\alpha + \left( 1 - \frac{t^2_{\theta_3}}{2} \right) c_\alpha \right) \tilde{h} \tilde{b} \tilde{b} + \frac{m_b}{v} \left( \frac{v}{v_D} t^2_{\theta_3} \left( \frac{m_b^2}{m_{\tilde{b}}^2} - c_{\theta_2}^2 \right) s_\alpha - \left( 1 - \frac{t^2_{\theta_3}}{2} \right) c_\alpha \right) \tilde{\phi} \tilde{b} \tilde{b} + \frac{m_\tilde{b}}{v} \left( \frac{v}{v_D} t^2_{\theta_3} \left( \frac{m_b^2}{m_{\tilde{b}}^2} - c_{\theta_2}^2 \right) s_\alpha - \left( 1 - \frac{t^2_{\theta_3}}{2} \right) c_\alpha \right) \tilde{h} \tilde{\tilde{s}} \tilde{s} + \frac{m_\tilde{s}}{v} \left( \frac{v}{v_D} t^2_{\theta_3} \left( \frac{m_b^2}{m_{\tilde{b}}^2} - c_{\theta_2}^2 \right) s_\alpha - \left( 1 - \frac{t^2_{\theta_3}}{2} \right) c_\alpha \right) \tilde{\phi} \tilde{\tilde{s}} \tilde{s} + \frac{m_\tilde{\psi}}{v} \left( \frac{v}{v_D} t^2_{\theta_3} \left( \frac{m_b^2}{m_{\tilde{b}}^2} - c_{\theta_2}^2 \right) s_\alpha - \left( 1 - \frac{t^2_{\theta_3}}{2} \right) c_\alpha \right) \tilde{h} \tilde{\psi} \tilde{\psi} + \frac{m_\tilde{\psi}}{v} \left( \frac{v}{v_D} t^2_{\theta_3} \left( \frac{m_b^2}{m_{\tilde{b}}^2} - c_{\theta_2}^2 \right) s_\alpha - \left( 1 - \frac{t^2_{\theta_3}}{2} \right) c_\alpha \right) \tilde{\phi} \tilde{\psi} \tilde{\psi} + \left( b \rightarrow t, s \rightarrow c \right) + \ldots ,$$

where the diagonal interactions with scalars are given in Eq. (15). The dots in the last line are for the omitted off-diagonal interactions, which dominantly opens the decay of $\tilde{\psi}$.
into 2nd generation SM quarks. The decay width of process $\tilde{\psi}q \rightarrow \tilde{\phi}q^2$ is proportional to $c_\alpha^2 s_\theta^2 (m_\psi/v_D)^2$, while the other decays $\tilde{\psi}q \rightarrow \tilde{\phi}q^3$ or $\tilde{\psi}q \rightarrow \tilde{h}q^2$ are suppressed by either $t_\theta^2$ or $s_\alpha^2$. The off-diagonal interactions will not contribute to scalar $\tilde{h}$, $\tilde{\phi}$ couplings to gluon-gluon and photon-photon, thus they are irrelevant for the NP phenomenology.

The gauge interactions between $Z'$ and quark mass eigenstates at leading order are given below:

$$L_{Z'}^{\text{quark}} = -\frac{g_D}{2} t_\theta^2 c_\theta^2 Z'_\mu \bar{b}_L \gamma^\mu b_L - \frac{g_D}{2} Z'_L s_\theta^2 \bar{\tilde{s}} L \gamma^\mu \tilde{s} L$$

$$+ \frac{g_D}{2} Z'_\mu \left[ (t_\theta^2 - 1) c_\theta^2 \bar{\tilde{b}}_L \gamma^\mu \tilde{b}_L + (t_\theta^2 - 1) \bar{\tilde{s}}_d \gamma^\mu \Psi^d_R \right] + H.c.$$ 

$$+ \frac{g_D}{2} Z'_\mu \left[ -2 c_\theta^2 t_\theta^2 \bar{\tilde{b}}_L \gamma^\mu \tilde{b}_L - \frac{m_b}{m_\tilde{b}} t_\theta^2 b_R \gamma^\mu \tilde{b}_R \right] + H.c.$$ 

$$+ \frac{g_D}{2} Z'_\mu \left[ s_\theta^2 \bar{\tilde{b}}_L \left( \frac{t_\theta^2}{2} - 1 \right) \bar{\tilde{b}}_L \gamma^\mu \tilde{b}_L + \frac{m_s}{m_\tilde{s}} s_\theta^2 \bar{\tilde{s}}_d \gamma^\mu \Psi^d_R \right] + H.c.$$ 

$$+ (b \rightarrow t, s \rightarrow c), \quad (16)$$

where the first two lines are diagonal interactions, and the lines from three to five are off-diagonal interactions with quarks. Such interactions induce $Z'$ decay into $\tilde{\psi} + \tilde{b}, \tilde{s}$ for our benchmark point $m_{Z'} > m_\tilde{b}$. The interaction with up-type quarks are similar, simply by substitution $b \rightarrow t$ and $s \rightarrow c$. Note the flavor violating interaction in line three is required to solve the B-anomalies. However, it also induces $B - \bar{B}$ mixing and $b \rightarrow s\gamma$ via 1-loop, which constraints are investigated in Section V B.

The lepton interactions of $Z'$ are

$$L_{Z'}^{\text{lepton}} = g_D Z'_\mu \left[ \bar{\mu}_\gamma \gamma \mu - \bar{\tau}_\gamma \gamma \tau + \bar{\nu}_\mu L \gamma^\mu \nu_\mu L - \bar{\nu}_\tau L \gamma^\mu \nu_\tau L \right] + H.c., \quad (17)$$

Due to the charge assignments, in the absence of mixing, the $Z'$ coupling to leptons would be 2 times larger than the one to heavy quarks. We calculate the decay branching ratios (BR) for $Z'$ into heavy vector-like quark $\bar{\tilde{\psi}}\tilde{\psi}$, 2nd generation SM quarks $\bar{\tilde{s}}\tilde{s}$ and $\bar{\tilde{c}}\tilde{c}$, 2nd and 3rd generation SM charged leptons $\mu^+\mu^-$, $\tau^+\tau^-$ and neutrinos $\bar{\nu}_\mu \nu_\mu$, $\bar{\nu}_\tau \nu_\tau$. The width of the decay to 3rd generation quarks are suppressed by $t_\theta^4$. The only significant flavor off-diagonal decays for $Z'$ are to 2nd generation quark and heavy vector-like quarks $\bar{\tilde{s}}\Psi^d, \bar{\tilde{c}}\Psi^d \tilde{s}$ and $\bar{\tilde{c}}\Psi^u, \bar{\tilde{u}}\Psi^c$. The flavor off-diagonal decays for $Z'$ to 3rd generation are suppressed by $t_\theta^2$. The decay BRs for $Z'$ are given in Fig. 2.
Before closing this subsection, we calculate the leading order couplings between the SM \( Z \) boson and SM quarks, which are modified due to mixing effects,

\[
\mathcal{L}_Z = \frac{g}{c_W} \left( \frac{-1}{2} + \frac{1}{3} s^2_W \right) Z_\mu \left[ \bar{b}_L \gamma^\mu b_L + \bar{s}_L \gamma^\mu s_L + \bar{\psi}_L \gamma^\mu \bar{\psi}_L \right] \\
+ g Z_\mu \left[ \left( \frac{s^2_w}{3c_w} - \frac{m_b^2 t_{\theta_3}^2}{2m_c^2} \right) \bar{b}_R \gamma^\mu \bar{b}_R + \frac{s^2_w}{3c_w} \bar{s}_R \gamma^\mu s_R + \left( -\frac{1}{2} \frac{s^2_w}{3} - \frac{m_b^2 t_{\theta_3}^2}{2m_c^2} \right) \bar{\psi}_R \gamma^\mu \bar{\psi}_R \right] \\
+ g Z_\mu \left[ -\frac{m_b \bar{t}_{\theta_3}}{2m_c^2} \bar{b}_R \gamma^\mu \bar{\psi}_R + \frac{m_s}{2m_c^2} \bar{t}_{\theta_3} \bar{s}_R \gamma^\mu \bar{\psi}_R - \frac{m_b m_s}{2m_c^2} \bar{t}_{\theta_3} \bar{b}_R \gamma^\mu \bar{s}_R \right] + H.c. \\
+ (b \to t, s \to c, \frac{1}{3} \to \frac{2}{3}, \frac{-1}{2} \to \frac{1}{2}), \tag{18}
\]

where the \( Z \) coupling to left-handed quarks are exactly diagonal because the coupling of the new left-handed quarks are the same as the ones of the SM left-handed quarks. In the second line of Eq. (18), we see the \( Z \) coupling to right-handed SM quarks are approximately SM-like, apart from small corrections proportional to the quark masses. The third line contains the flavor off-diagonal interactions with SM \( Z \) and right-handed quarks. Although suppressed by small mixing angle \( t_{\theta_3} \) or by quark-mass factors, it is still necessary to check flavor violating processes in the top-quark sector, e.g. \( \bar{t} \to Z \bar{c}, Z \bar{u} \), which are covered in Section V B.
II. LIGHT HIGGS AND THE CMS EXCESS

In this section, we first discuss the light Higgs $\tilde{\phi}$ with mass 96 GeV and how it can resolve the excess in CMS data. Later, we use the $Z'$ in the same model to fit the $R_{K}^{(s)}$ excess.

The dominantly production channels at LHC are gluon-gluon fusion (ggF), associate production with $\tilde{t}\tilde{t}$, vector boson fusion (VBF) and associate production (VH). In the section II C, the coupling between $\tilde{\phi}$ and quarks are given. For $m_{\tilde{\phi}} = 96$ GeV, the coupling strength $\kappa$ is calculated, which is the coupling for $\tilde{\phi}$ divided by the coupling of SM-like Higgs with the same mass.

\[
\kappa_{\tilde{\phi}(\bar{b}b)\tilde{\phi}} = \frac{v_{D}}{\theta_{3}} t_{2} \left( \frac{m_{\tilde{t}/\tilde{b}}^{2} - m_{\psi}^{2}}{m_{\psi}^{2}} \right) c_{\alpha} - \left( 1 - \frac{t_{2}^{2}}{\theta_{3}^{2}} \right) s_{\alpha},
\]

\[
\kappa_{\tilde{\phi}(\bar{c}c)\tilde{\phi}} = \frac{v_{D}^{2}}{\theta_{2} c_{\alpha} + s_{\alpha}},
\]

\[
\kappa_{\tilde{\phi}V\bar{V}\tilde{\phi}} = -s_{\alpha},
\]

\[
\kappa_{\tilde{\phi}gg\tilde{\phi}} = \kappa_{\tilde{\phi}(\bar{t}t)\tilde{\phi}} + 2 \frac{v}{v_{D}} c_{\alpha} \left( s_{\theta_{2}}^{2} + \frac{t_{2}^{2}}{\theta_{3}^{2}} (1 + c_{\theta_{2}}^{2}) \right),
\]

\[
\kappa_{\tilde{\phi}V\bar{V}\tilde{\phi}} = -1.31 \kappa_{\tilde{\phi}gg\tilde{\phi}} + 0.31 \kappa_{\tilde{\phi}(\bar{t}t)\tilde{\phi}} + 0.31 \times \frac{5}{4} \frac{v}{v_{D}} c_{\alpha} \left( s_{\theta_{2}}^{2} + \frac{t_{2}^{2}}{\theta_{3}^{2}} (1 + c_{\theta_{2}}^{2}) \right),
\]

where $V = W, Z$. For $\kappa_{\tilde{\phi}gg\tilde{\phi}}$, the first term is the contribution from SM top quark, and the second term contains the contributions from heavy vector-like quarks $\tilde{\psi}^{u,d}$, therefore there is a factor of 2. For $\kappa_{\tilde{\phi}V\bar{V}\tilde{\phi}}$, the third term is again contribution from heavy vector-like quark, with $5/4$ from $\tilde{\psi}^{u,d}$ electromagnetic charge square comparing to top quark.

The ggF, and the inclusive VBF and VH production cross-sections at 13 TeV LHC are given below [52]

\[
\sigma_{\tilde{\phi}ggF} = 76.3 \text{ pb} \times \left( \kappa_{\tilde{\phi}gg\tilde{\phi}} \right)^{2},
\]

\[
\sigma_{\tilde{\phi}VBF/VH} = 10.4 \text{ pb} \times s_{\alpha}^{2}.
\]

The dominant decay channels of $\tilde{\phi}$ have the following decay widths [53]

\[
\Gamma(\tilde{\phi} \rightarrow \bar{b}b) = 1.9 \text{ MeV} \times \left( \kappa_{\tilde{\phi}(\bar{b}b)\tilde{\phi}} \right)^{2}, \quad \Gamma(\tilde{\phi} \rightarrow \tau\tau) = 0.2 \text{ MeV} \times s_{\alpha}^{2}, \quad \Gamma(\tilde{\phi} \rightarrow c\bar{c}) = 0.09 \text{ MeV} \times \left( \kappa_{\tilde{\phi}c\bar{c}} \right)^{2},
\]

\[
\Gamma(\tilde{\phi} \rightarrow gg) = 0.16 \text{ MeV} \times \left( \kappa_{\tilde{\phi}gg\tilde{\phi}} \right)^{2}, \quad \Gamma(\tilde{\phi} \rightarrow \gamma\gamma) = 3.39 \text{ keV} \times \left( \kappa_{\tilde{\phi}V\bar{V}\tilde{\phi}} \right)^{2},
\]
The branching ratio for $\tilde{\phi}$ to $\tilde{b}\bar{\tilde{b}}$ and $\gamma\gamma$ are approximately

\[
BR(\tilde{\phi} \to \tilde{b}\bar{\tilde{b}}) = \frac{1.9 \times (\kappa_{\tilde{b}\bar{\tilde{b}}}^{\tilde{\phi}})^2}{1.9 \times (\kappa_{\tilde{b}\bar{\tilde{b}}}^{\tilde{\phi}})^2 + 0.2 \times \sin^2 \alpha + 0.16 \times (\kappa_{g\phi}^{\tilde{\phi}})^2 + 0.09 \times (\kappa_{\tilde{c}\bar{\tilde{c}}}^{\tilde{\phi}})^2} \\
BR(\tilde{\phi} \to \gamma\gamma) = \frac{3.39 \times 10^{-3} \times (\kappa_{\gamma\gamma}^{\tilde{\phi}})^2}{1.9 \times (\kappa_{\tilde{b}\bar{\tilde{b}}}^{\tilde{\phi}})^2 + 0.2 \times \sin^2 \alpha + 0.16 \times (\kappa_{g\phi}^{\tilde{\phi}})^2 + 0.09 \times (\kappa_{\tilde{c}\bar{\tilde{c}}}^{\tilde{\phi}})^2} \quad (27)
\]

To fit the 13 TeV CMS di-photon excess [1], one needs

\[
\sigma_{ggF} \times BR(\tilde{\phi} \to \gamma\gamma) \sim 0.085 \text{ pb}. \quad (28)
\]

We show the parameter space $\{\sin \alpha, \sin \theta_2\}$ which fits the CMS excess in Fig. 3, with $\sin \theta_2 \approx \lambda_2 v_D/m_\tilde{\psi}$. The cyan solid line provides 80% of CMS excess in Eq. (28), while the two dashed line are for 60% and 100% of the excess respectively. The benchmark point is denoted by a red star in the plot, and its parameters are also listed in Table II.

| model parameters | $m_\tilde{\phi}$ | $\sin \alpha$ | $\sin \theta_2$ | $\tan \theta_3$ | $m_\tilde{\psi}$ | $g_D$ | $v_D$ | $m_{Z'}$ |
|------------------|------------------|---------------|---------------|-----------------|-----------------|-------|------|--------|
| benchmark point  | 96 GeV           | 0.1           | 0.89          | 0.1             | 800 GeV         | 1     | 492 GeV | 4.1 TeV |

TABLE II. The benchmark point for the signal model which fits the CMS excess and solves the B-anomalies simultaneously.

From Fig. 3, the benchmark has $\sin \theta_2 = 0.89$, $m_\tilde{\psi} = \lambda_2 v_D / \sin \theta_2 = 800$ GeV and $v_D = 496$ GeV. This suggests $\lambda_2 \approx 1.4$ and the heavy quark mass dominantly comes from off-diagonal term $\lambda_2 v_D$. It is worth mentioning that since $\cos \theta_2 = 0.48$, the diagonal mass $m_{q^2}$ is larger than eigenstate mass $m_{q^2}$ due to the relationship $m_{q^2} = m_{q^2} \cos \theta_2$.

For the benchmark point, we list the 96 GeV Higgs branching ratios in Table III.

| process | $b\bar{b}$ | $\tau\bar{\tau}$ | $c\bar{c}$ | $gg$ | $\gamma\gamma$ | $WW^*$ | $ZZ^*$ | total |
|---------|------------|------------------|------------|------|----------------|--------|-------|-------|
| BR      | 15.9\%    | 1.66\%           | 18.23\%   | 63.9\% | 1.8 \times 10^{-3} | 8.3 \times 10^{-4} | 1.41 \times 10^{-4} | 1     |
| $\Gamma_i$ (MeV) | 0.019   | 0.022            | 0.002      | 0.077 | 2.18 \times 10^{-4} | 1 \times 10^{-4} | 1.7 \times 10^{-5} | 0.12 |

TABLE III. The decay widths and branching ratios for a 96 GeV $\tilde{\phi}$ and parameters set at the benchmark point values, given in Table II.
A. Constraints from SM Higgs measurements

In this subsection, we are going to check the limits from SM Higgs measurements. For convenience, we list the coupling strength $\kappa$ for the SM-like Higgs $\tilde{h}$ below,

$$
\kappa_{\tilde{t}\tilde{b}}^{\tilde{h}} = \frac{v}{v_D} \tan^2 \theta_2 \sin \alpha - \cos \alpha,
$$

$$
\kappa_{\tilde{s}\tilde{c}}^{\tilde{h}} = \frac{v}{v_D} \left( \frac{s_{\theta_2}^2 + \tan^2 \theta_3}{2} (1 + c_{\theta_2}^2) \right),
$$

$$
\kappa_{VV}^{\tilde{h}} = \cos \alpha,
$$

$$
\kappa_{gg}^{\tilde{h}} = \frac{2 v}{v_D} s_{\theta_2} \left( \frac{s_{\theta_2}^2 + \tan^2 \theta_3}{2} (1 + c_{\theta_2}^2) \right),
$$

$$
\kappa_{\gamma\gamma}^{\tilde{h}} = -1.31 \kappa_{eff}^{VV} + 0.31 \kappa_{eff}^{\tilde{t}\tilde{b}} + 0.31 \times \frac{5 v}{4 v_D} s_{\alpha} \left( \frac{s_{\theta_2}^2 + \tan^2 \theta_3}{2} (1 + c_{\theta_2}^2) \right).
$$

The most recent 13 TeV (36 fb$^{-1}$) constraints on SM Higgs coupling strength $\kappa$ are from CMS combined measurement [54],

$$
\kappa_{CMS13}^{t} = 1.09^{+0.14}_{-0.14}, \quad \kappa_{CMS13}^{W} = 1.12^{+0.13}_{-0.19}, \quad \kappa_{CMS13}^{Z} = 0.99^{+0.11}_{-0.11},
$$

$$
\kappa_{CMS13}^{g} = 1.14^{+0.15}_{-0.13}, \quad \kappa_{CMS13}^{\gamma} = 1.07^{+0.15}_{-0.18}. \quad (34)
$$

This CMS analysis includes ggF, VBF, VH and ttH productions, and various SM Higgs decay modes. For ATLAS, the production modes are the same, but only $H \to \gamma\gamma$ and $H \to ZZ \to 4\ell$ decay modes are included in the $\kappa$ analysis [55],

$$
\kappa_{ATLAS13}^{t} = 0.89^{+0.20}_{-0.15}, \quad \kappa_{ATLAS13}^{W} = 1.03 \pm 0.06,
$$

$$
\kappa_{ATLAS13}^{g} = 1.08^{+0.11}_{-0.10}, \quad \kappa_{ATLAS13}^{\gamma} = 0.93^{+0.09}_{-0.08}. \quad (35)
$$

It is clear that $\kappa$ from CMS and ATLAS are in agreement with each other. We took the $\kappa$ measurements as constraints and plot the corresponding contours at 90% confidence level (C.L.) in Fig. 3, with CMS in the left panel and ATLAS in the right panel.

Since in our signal model $\tilde{\phi}$ is produced from ggF and decay in di-photon channel, it is appropriate to pay special attention in the SM Higgs di-photon channel measurement as well. The most recent 13 TeV (36 fb$^{-1}$) measurements for SM Higgs property in the di-photon decay channel, from CMS [56] and ATLAS [57] give the following signal strengths
FIG. 3. The 90% C.L. constraints from SM-like Higgs precision measurements and the parameter space fitting the CMS [1] ("gg$\tilde{\phi}$ → $\gamma\gamma$") and LEP ("$e^+e^- → Z\tilde{\phi} → Z\bar{b}b$")[4] signals are plotted in $\sin\alpha − \sin\theta^2$ 2D plane with cyan and orange color shading denoting the signal regions. All the other color shaded regions are excluded from various experiments. All the constraints from CMS (ATLAS) are in the left (right) panel respectively. The constraints from SM-like Higgs coupling strength, denoted as "$\kappa$", are from CMS [54] and ATLAS [55] measurements at 13 TeV (36 fb$^{-1}$). The SM Higgs di-photon decay analysis in the gluon fusion production give signal strength $\mu_{ggF,h→\gamma\gamma}$ limits for CMS [56] and ATLAS [57]. The 90% C.L. exclusion regions are colored with dot-dashed boundaries. The parameter region consistent with the CMS ("gg$\tilde{\phi}$ → $\gamma\gamma$") and LEP ("$e^+e^- → Z\tilde{\phi} → Z\bar{b}b$") signals are the same in the left and right panels, and denoted by cyan and orange colors, respectively. The solid line shows parameters leading to an explanation of 80% of these signals, while the two dashed lines are consistent with an explanation of 60% and 100% of these signals, respectively. The red star denotes the parameters associated with the benchmark point shown in Table II.
for different production modes and the combined result,

$$
\mu_{\text{CMS}13}^{ggF,h\rightarrow\gamma\gamma} = 1.10^{+0.20}_{-0.18}, \quad \mu_{\text{CMS}13}^{VBF,h\rightarrow\gamma\gamma} = 0.8^{+0.6}_{-0.5}, \quad \mu_{\text{CMS}13}^{ttH,h\rightarrow\gamma\gamma} = 2.2^{+0.9}_{-0.8}, \quad \mu_{\text{CMS}13}^{\text{combined},h\rightarrow\gamma\gamma} = 1.18^{+0.17}_{-0.14}
$$

$$
\mu_{\text{ATLAS}13}^{ggF,h\rightarrow\gamma\gamma} = 0.81^{+0.19}_{-0.18}, \quad \mu_{\text{ATLAS}13}^{VBF,h\rightarrow\gamma\gamma} = 2.0^{+0.6}_{-0.5}, \quad \mu_{\text{ATLAS}13}^{ttH,h\rightarrow\gamma\gamma} = 0.5^{+0.6}_{-0.5}, \quad \mu_{\text{ATLAS}13}^{\text{combined},h\rightarrow\gamma\gamma} = 0.99^{+0.15}_{-0.14}
$$

The above measurements in the di-photon channel have improved the precision by factor of 2 compared to the ones with Run-I data [58], therefore we do not consider the Run-I constraints further. The most relevant and stringent constraint from the signal strengths is from $\mu_{ggF,h\rightarrow\gamma\gamma}$. The ATLAS result is barely consistent with SM at 1 $\sigma$. Thus, we give 90% C.L. (1.64 $\sigma$) constraints for CMS and ATLAS respectively in Fig. 3. The excluded parameter regions are plotted as magenta color with dot-dashed boundary.

### B. Simultaneous explanation of the CMS and LEP excesses.

In Fig. 3, we show the constraints from Higgs precision measurements, as well as the region consistent with the LEP excess, shown as the orange regions in both left and right panels of Fig. 3. While the CMS excess can be easily explained without being in tension with any current Higgs measurements, the simultaneous explanation of the CMS di-photon and LEP $b\bar{b}$ excesses can be only obtained for values of $s_{\theta_2} \simeq \pm 1$ and $s_\alpha \simeq 0.3$. It is easy to see that, for these values of the mixing angles $\kappa^{gg\tilde{h}}_{eff} \simeq 1.2$.

The large $\kappa^{gg\tilde{h}}_{eff}$ induces a sizable rate for the SM-like Higgs production in the gluon fusion channel. While such an enhancement is consistent with the current CMS measurement in the ggF channel, both in the di-photon as well as in the ZZ and WW final states, it is in tension with the current ATLAS measurement of the ggF production of SM-like Higgs bosons in the di-photon channel, see Eq. (37). This tension is clearly shown in the right panel of Fig. 3.

In summary, while the LEP and CMS excesses can be easily separately explained within this framework, a simultaneous explanation of the CMS and LEP excesses is in tension with the current ATLAS observations in the ggF channel. In the following, we shall concentrate on the benchmark model, which leads to an explanation of the CMS di-photon excess, and ignore the LEP $b\bar{b}$ excess. However, beyond the SM-like Higgs physics, all other phenomenological
aspects of this model would be only minimally affected by a change from the benchmark point
parameters to the region of parameters, where the LEP and CMS excesses are simultaneously
explained.

IV. \( Z' \) AND THE B-ANOMALIES

After discussing the possibility of \( \tilde{\phi} \) fitting the CMS excess, we turn to the B-anomalies.
Integrating out the heavy gauge boson \( Z' \), there is an effective flavor violating operator with
down-type quarks [13],

\[
\mathcal{L}_{\text{eff}} = -\frac{g_D^2}{2m_{Z'}^2} s_{\theta_2} c_{\theta_2} t_{\theta_3} \bar{b}_L \gamma_{\mu} \bar{s}_L \mu \gamma^\mu \mu + H.c.
\]  

(38)

This can be related to the \( C_{9}^{NP} \) operator considered in Ref. [59–67]:

\[
\mathcal{H}_{\text{eff}}^{NP} = -\mathcal{L}_{\text{eff}}^{NP} = -\frac{4G_F \alpha_{em}}{\sqrt{2} 4\pi} (V_{tb} V_{ts}^*) C_9^{NP} \bar{b}_L \gamma_{\mu} \bar{s}_L \mu \gamma^\mu \mu + H.c.,
\]  

(39)

therefore, the coefficient \( C_9^{NP} \) can be rewritten as

\[
C_9^{NP} = \frac{g_D^2 v^2}{m_{Z'}^2} \frac{\pi}{\alpha_{em}} \frac{1}{V_{tb} V_{ts}^*} s_{\theta_2} c_{\theta_2} t_{\theta_3}.
\]  

(40)

Recent global fits include more data from experiments, e.g. angular observables from Belle
[68], and have found that the significance of NP contributions has increased [65, 66]. If one
restricts the analysis to lepton flavor universality violation process, the value \( C_9^{NP} = -1.56 \)
quoted above was obtained by a fit to the data by the authors of Ref. [65], with a significance
of 4.1 \( \sigma \), while the authors of Ref. [66] obtained a slightly different result, namely, \( C_9^{NP} =
-1.76 \), with a significance of 3.9 \( \sigma \). However, extending the analysis to a more complete
set of observables, namely all those included in Ref. [66], a best fit value of \( C_9^{NP} = -1.11 \)
is obtained, and the significance increases to 5.8 \( \sigma \). In our analysis, we shall consider the
values obtained from the fit in Ref. [65]. The alternative values of \( C_9^{NP} \) obtained in Ref. [66]
do not affect our phenomenological analysis in any significant way, since they can be easily
accommodated by few tens of percent changes in the mass of the gauge boson \( Z' \). After
plugging in the SM parameters \( (\alpha_{em} = 1/137, |V_{ts}| \sim 0.04) \), we obtain a requirement on NP
parameters,

\[
\frac{g_D^2}{m_{Z'}^2} s_{\theta_2} c_{\theta_2} t_{\theta_3} \sim 2.44 \times 10^{-3}\text{TeV}^{-2}.
\]  

(41)
FIG. 4. Left panel: the constraints on \( Z' \) in \( m_{Z'} - g_D \) 2D plane. The colored regions are excluded by the LHC search for heavy neutral gauge boson. The purple area is excluded by CMS 13 TeV search on di-leptons [69]. The cyan and red areas are excluded by ATLAS 13 TeV [70, 71] and 8 TeV di-lepton search [72]. The brown area is excluded by 7 TeV ATLAS search on di-leptons [73]. The blue line satisfies the requirement from B-anomalies. Right panel: Contours of constant values of \( \sin \theta_2 \), showing the dependence on this mixing angle of the coefficient \(-C_{9}^{NP}\) and the di-photon signal cross-section \( \sigma_{ggF}\text{BR}(\tilde{\phi} \to \gamma\gamma) \) at the 13 TeV LHC. All the parameters except from \( \sin \theta_2 \) are taken from Table II, and the red star denotes our benchmark point.

For the explanation of the \( R_K \) and \( R_K^* \) anomalies, we have chosen a benchmark with \( t_{\theta_3} = 0.1 \) and \( s_{\theta_2} = 0.89 \), which are consistent with the parameters shown by the red star in Fig. 3. For such a benchmark, one obtains a relationship between \( g_D \) and \( m_{Z'} \) given by \( \frac{m_{Z'}}{g_D} \simeq 4.1 \text{ TeV} \), which is shown as the blue line in the left panel of Fig. 4. In the right panel of Fig. 4, we show contours of constant values of \( \sin \theta_2 \), showing the dependence on this mixing angle of the coefficient \(-C_{9}^{NP}\) and the di-photon signal cross-section \( \sigma_{ggF}\text{BR}(\tilde{\phi} \to \gamma\gamma) \) at the 13 TeV LHC. We see that di-photon signal at CMS requires a large value of \( \sin \theta_2 \), while the explanation of the B-anomalies requires a moderate value of \( \sin \theta_2 \) since \(-C_{9}^{NP}\) is proportional to \( s_{\theta_2}c_{\theta_2} \).
A. Constraints on $Z'$

In Eq. (16), we have already presented the interactions of $Z'$ and in Fig. 2 we show the branching ratios of $Z'$. We find out that, depending on the $Z'$ mass, the dominant decay channel of $Z'$ are $Z' \rightarrow \bar{s}s\ (\bar{c}c)$, $Z' \rightarrow \bar{\psi}u\bar{\psi}u\ (\bar{\psi}d\bar{\psi}d)$, $Z' \rightarrow \mu\bar{\mu}$ (and $Z' \rightarrow \tau\bar{\tau}$) and $Z' \rightarrow \nu\bar{\nu}$ ($\nu\bar{\nu}$).

We now consider the constraints from $Z'$ searches at LHC. The search for new neutral gauge bosons decaying to di-lepton [69–73] and di-jet [74] put strong constraints on a possible $Z'$. After consider the $Z'$ production and decay branching ratios, in in the left panel of Fig. 4, we show the constraints in $g_D$ vs. $m_{Z'}$ 2D plane with benchmark parameters $\tan \theta_3 = 0.1$, $\sin \theta_2 = 0.89$ and $m_{\tilde{\psi}} = 800$ GeV. All the colored regions are excluded. The limits from di-jet are much weaker than di-lepton, because $Z'$ couples to SM quark only through heavy vector-like quark mixing while leptons are directly charged. Thus di-jet constraint is not shown in Fig. 4. The solution to B-anomalies requires $m_{Z'}/g_D \simeq 4.1$ TeV. It is plotted as a solid blue line and denoted as “$R(K)/R(K^*)$” in Fig. 4. To evade the constraints, $Z'$ must be heavier than about 4.1 TeV, while $g_D$ must be larger than about 0.8.

For $U(1)_{L_\mu - L_\tau}$ gauge boson, it is known that neutrino trident production $\nu_\mu N \rightarrow \nu_\mu N \mu^+ \mu^-$, where $N$ is nuclei, gives very stringent constraint [13, 75]. The recent results are from CHARM-II [76], CCFR [77] and NuTeV [78], which leads to constraint $m_{Z'}/g_D \gtrsim 540$ GeV for $m_{Z'} \gtrsim 10$ GeV [79]. It is easy to see that our benchmark point for model is safe from neutrino trident constraint. Observe that a simultaneous explanation of the B-anomalies and the LEP bottom forward-backward asymmetry with a single $Z'$ is not possible, since the latter demands a light $Z'$, with mass comparable to the $Z$ mass and significant couplings to the right-handed bottom quarks [80], what would lead to inconsistencies with the above constraints.

V. OTHER CONSTRAINTS

A. Constraints on the heavy quarks

The heavy vector-like quark is subject to constraints from LHC searches. Its mass is $m_{\tilde{\psi}} \simeq \sqrt{\lambda_2^2 v_D^2 + m_{\tilde{\psi}}^2}$, and it is about $m_{\tilde{\psi}} \simeq 800$ GeV for the benchmark point. At the LHC, such a quark would be produced by QCD processes and will predominantly decay into the $\tilde{\psi} \rightarrow \tilde{\phi}s/\bar{c}$ channels, followed by $\tilde{\phi} \rightarrow c\bar{c}, s\bar{s}, b\bar{b}$. There are other possible decay
channels, e.g. $\tilde{\psi}^u \rightarrow \tilde{q} q^3$ and $\tilde{\psi}^d \rightarrow \tilde{h} q^2$ however suppressed by either $t_{\theta_3}^2$ or $s_{\alpha_3}^2$, and $\tilde{\psi} \rightarrow Z q$ suppressed by small quark mass or $t_{\theta_4}$ (see Eq. (18)). The decay $\tilde{\psi} \rightarrow Z' \tilde{s}/\tilde{c}$ is also possible but is kinematically forbidden by the benchmark setup $m_{Z'} > m_{\tilde{\psi}}$. Therefore, the dominant constraints come from searches for heavy fermions which decay into three quarks. A recent relevant search is from ATLAS 13 TeV (36 fb$^{-1}$) looking for R-Parity violating (RPV) gluino at the LHC, which decays to three quarks [81]. It sets 95% C.L. upper limit on the cross section times branching ratio varies between 0.80 fb at gluino mass 900 GeV and 0.011 fb at gluino mass 1800 GeV. At LHC Run-I, ATLAS [82] and CMS [83] have a similar limit for RPV gluino at 8 TeV (20 fb$^{-1}$), which excludes gluino mass lower than 650 GeV if it decays into three light-flavor jets. In Fig. 5, we show the pair production cross-section of $\tilde{\psi}\tilde{\psi}$ at 13 TeV and 8 TeV [84, 85], including both $\tilde{\psi}^u$ and $\tilde{\psi}^d$. The limits on $\sigma \times BR$ from ATLAS and CMS are plotted as red and blue lines, while 13 TeV and 8 TeV are using solid and dashed lines respectively. The 13 TeV ATLAS data has stopped at 900 GeV and we extrapolate it down to 400 GeV with dotted line. From Fig. 5, it is clear that $\tilde{\psi}$ mass larger than 600 GeV are compatible with the 8 TeV constraints and ATLAS 13 TeV data requires $\tilde{\psi}$ mass larger than 650 GeV if the extrapolation is correct. The above limits are valid for $\tilde{\psi}$ decaying to three light flavor jets. The CMS 8 TeV search [83] has also set limit if it decays to $qqb$, and the constraint is slightly better than $qqq$ decay channel. The ATLAS 8 TeV search [82] has looked for $bbb$ decay channel, and the constraint is roughly the same as $qqq$ channel. The heavy vector-like quark $\tilde{\psi}$ can decay to $qbb$, if $\tilde{\phi} \rightarrow b\bar{b}$. Such decay does not match to three jets invariant mass reconstruction for either $qqb$ or $bbb$, therefore more possible combinatorial errors will reduce the signal efficiency. Moreover, it will pay double suppression from branching ratio $\tilde{\phi} \rightarrow b\bar{b}$. As a result, $\tilde{\psi}$ decays into three light flavor jets are more general and useful. In summary, our benchmark model is not excluded by the three jet resonance searches at LHC.

B. Constraints from flavor physics

We start the discussion from $b \rightarrow s\gamma$ constraints. The SM branching ratio for $b \rightarrow s\gamma$ is given by [86]:

$$\frac{\text{BR}(b \rightarrow s\gamma)}{\text{BR}(b \rightarrow c\ell\bar{\nu}_\ell)} = \frac{6\alpha}{\pi} \frac{\left[\eta^{16}\frac{A_y}{3} + 8\left(\frac{\eta^{14}}{3} - \eta^{16}\right)A_g + C\right]^2}{I(m_c/m_b) \left[1 - \frac{2}{3\pi} \alpha_s(m_b) f(m_c/m_b)\right]} \left(42\right)$$
FIG. 5. The 95% C.L. constraints on the heavy vector-like quark pair production cross-section with subsequent decay into three light flavor jets. The 95% C.L. limits are from RPV gluino search at 13 TeV ATLAS [81] and at 8 TeV CMS [83] and ATLAS [82]. The 13 (8) TeV limits are plotted as solid (dashed) lines, and ATLAS and CMS are using red and blue color respectively. The black lines show the pair production cross-sections for $\tilde{\psi}$ at 8 TeV and 13 TeV.

where $\eta = \frac{\alpha_s(m_Z)}{\alpha_s(m_b)} = 0.548$, $I(m_c/m_b) = 0.58$ is the phase-space factor and $C' = -0.18$ is a coefficient from the operator mixing. The Wilson coefficients $A_\gamma(m_t^2/m_W^2), A_g(m_t^2/m_W^2)$ are defined as following:

$$\mathcal{L}_{\text{eff}} = GF \frac{\alpha}{8\pi^3} V_{tb} V_{ts}^* m_b \left[ A_\gamma s_L \sigma^{\mu\nu} b_R F_{\mu\nu} + A_g s_L \sigma^{\mu\nu} T^a b_R G^{a \mu\nu} \right] + H.c., \quad (43)$$

where $F_{\mu\nu}, G_{\mu\nu}$ are the photon and gluon field strengths. The SM CKM matrix values are given by [87]:

$$|V_{tb}| = 1.009 \pm 0.031, \quad |V_{ts}| = 0.04 \pm 0.0027. \quad (44)$$

For the formula for $A_{\gamma,g}$ from the SM $W$-loop, we refer to the appendix of Ref. [86]. In our model, the contributions to $b \rightarrow s\gamma$ decay come from $Z', Z$ flavor off-diagonal couplings in Eq. (16) and Eq. (18). We are not going to calculate the contributions directly, but only make an estimation for the order of magnitude comparing with the contribution from
W-loop. It is not difficult to estimate their contribution to the Wilson coefficients $A_\gamma, A_g$:

$$A_\gamma \sim \frac{1}{V_{tb}V_{ts}^*} \frac{m_b^2 m_\psi m_s}{m_\psi^2 z_L} \left[ A_{SM}^{m^2_b/m_\psi^2} \frac{m_\psi^2}{6 c_w} + A_{SM}^{m^2_s/m_\psi^2} \frac{m_\psi^2}{6 c_w} + \frac{1}{4} A_{SM}^{m^2_s/m_\psi^2} \right], \quad (45)$$

$$A_g \sim \frac{1}{V_{tb}V_{ts}^*} \frac{g^2 m_w^2}{4 g^2 m_\psi^2} t_{\theta_3} c_{\theta_2} s_{\theta_2} \left[ A_{SM}^{m^2_b/m_\psi^2} t_{\theta_3}^2 c_{\theta_2}^2 + A_{SM}^{m^2_s/m_\psi^2} s_{\theta_2}^2 + A_{SM}^{m^2_s/m_\psi^2} c_{\theta_2}^2 \left( \frac{t_{\theta_3}^2}{2} - 1 \right) \right]. \quad (46)$$

From the equation above, we can see that the contribution is either suppressed by $m_s^2/m_\psi^2$ or $m_b^2/m_\psi^2$, which leads to negligible contribution for the $b \to s\gamma$ decay. To be more explicit, we find that for $m_{Z'} \sim 4.1$ TeV, $g_D \sim 1$, $m_\psi \sim 800$ GeV and $t_{\theta_3} \ll 1$, we have:

$$\frac{A_\gamma}{A_{SM}} \sim 5 \times 10^{-6}, \quad \frac{A_g}{A_{SM}} \sim 4 \times 10^{-6}, \quad \frac{A_\gamma}{A_{SM}} \sim 3 \times 10^{-4} t_{\theta_3} c_{\theta_2} s_{\theta_2}, \quad \frac{A_g}{A_{SM}} \sim 4 \times 10^{-4} t_{\theta_3} c_{\theta_2} s_{\theta_2}, \quad (46)$$

which are very small and do not induce any relevant modification to the $b \to s\gamma$ decay rate. Note that the operator which explains the lepton-flavor universality violation in Eq. (39) will not contribute to $B_s \to \mu^+\mu^-$ decay, as our $Z'$ couplings to muon pair is vector-like [88].

Apart from the operator $\bar{b}_L \gamma^\mu s_L \bar{\mu} R\gamma^\mu$, there are also $\Delta F = 2$ flavor changing operators generated:

$$\mathcal{L}_{\text{eff}} = -\frac{g_D^2}{4 m_{Z'}^2} s_{\theta_2} c_{\theta_2} t_{\theta_3} \left( \bar{b}_L \gamma^\mu s_L \right)^2 - \frac{g^2}{4 m_{Z'}^2} \frac{m_b^2 m_s^2}{m_\psi^4} t_{\theta_3}^2 c_{\theta_2}^2 \left( \bar{b}_R \gamma^\mu \bar{s}_R \right)^2 + H.c. \quad (47)$$

Both operators will contribute to $B_s - B_s$ mixing, but we expect that the left-handed one dominates, as the right-handed one is suppressed by the masses of bottom and strange quarks, i.e.:

$$\frac{m_b^2 m_s^2}{m_\psi^4} \sim \frac{2 \times 10^{-13}}{(m_\psi/\text{TeV})^4} \quad (48)$$

The bound on the Wilson coefficient of the first operator is given by (see Table 1.1 of Ref. [89] and [90]):

$$\frac{g_D^2}{4 m_{Z'}^2} s_{\theta_2} c_{\theta_2} t_{\theta_3} < 5.0 \times 10^{-5} \text{ TeV}^{-2} \quad (49)$$

Combined with Eq. (41), we can derive the bounds on the combination of the mixing angles or the factor $g_D^2/m_{Z'}^2$:

$$s_{\theta_2} c_{\theta_2} t_{\theta_3} < 0.082 \quad \Rightarrow \quad m_{Z'} < g_D \times 5.8 \text{ TeV} \quad (50)$$

which is satisfied by our benchmark point ($s_{\theta_2} c_{\theta_2} t_{\theta_3} \simeq 0.041, m_{Z'}/g_D \simeq 4.1 \text{ TeV}$).
Next, we consider the searches for $tZ$ flavor changing neutral current in the top quark decays at LHC. The relevant interactions are

$$\mathcal{L}_{tZ} = g \frac{m_t m_{\tilde{c}}}{2m_{\tilde{\psi}}^2} t_{\theta_2} t_{\theta_3} Z_{\mu} \bar{t}_R \gamma^\mu \bar{c}_R + H.c.,$$

which will contribute to the decay channel $\tilde{t} \rightarrow Z \tilde{c}$ with branching ratio estimated as:

$$\text{BR}(\tilde{t} \rightarrow Z \tilde{c}) \sim \frac{m_t^2 m_{\tilde{c}}^2 t_{\theta_2} t_{\theta_3}^2}{2m_{\tilde{\psi}}^4}$$

The most stringent bound on such branching ratio comes from ATLAS search at 13 TeV (36 fb$^{-1}$) [91]. The results read

$$\text{BR}(\tilde{t} \rightarrow Z \tilde{c}) < 2.3 \times 10^{-4},$$

which sets a lower bound on our parameters,

$$\frac{m_{\tilde{\psi}}}{\sqrt{t_{\theta_2} t_{\theta_3}}} > 102 \text{ GeV}. \quad (54)$$

It is easy to see that such bound is satisfied in the region of parameters consistent with our benchmark point.

Finally, we discuss the constraints from flavor physics in the lepton sector. The gauge boson $Z'$ under $U(1)_{L_\mu-L_\tau}$ can contribute to tau lepton decay $\tau \rightarrow \mu \nu_\tau \bar{\nu}_\mu$ via 1-loop box diagram [13]. It excludes $Z'$ mass lower than 650 GeV for $g_D = 1$, and the benchmark point with a 4 TeV $Z'$ is quite safe with this limit.

VI. CONCLUSION AND SUMMARY

The recently observed anomalies in the decay of $B$-mesons into $K$-mesons and pair of leptons could be a possible hint of the violation of lepton-universality, one of the pillars of the SM phenomenology. In this work, we have provided a possible realization of the idea of explaining these anomalies by the presence of a new gauge boson $Z'$ of an $U(1)_{L_\mu-L_\tau}$ symmetry, that couple to leptons at tree-level, and to quarks via the mixing with vector-like quarks charged under the new gauge symmetry. The mixing of SM quarks with vector-like quarks needs to be induced by the presence of a new Higgs boson, charged under the new $U(1)_{L_\mu-L_\tau}$ symmetry.
In this work, we have discussed the possibility that such Higgs boson could be associated with the recent excess in the di-photon channel observed at the CMS experiment at the 13 TeV LHC run. We have shown that this is possible and provided the constraints on the quark-mixing parameters that could lead to such a possibility. An additional, naturally heavy, Higgs boson, contributing to the breakdown of the \( U(1)_{L_\mu-L_\tau} \) symmetry, but not to the quark mixing, is necessary in order to give the \( Z' \) gauge boson a sufficiently high mass to avoid the LHC constraints. A simultaneous explanation of these observables with the Higgs boson excess observed at LEP may be achieved in a way that is consistent with most observations, although it is in tension with the rate of the SM-like Higgs boson decaying to di-photons in the gluon fusion production channel measured by the ATLAS experiment in the 13 TeV LHC run.

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Appendix A: Scalar mixing parameters

In this section, we give the relation between the five free parameters \( \mu_\phi, \mu, \lambda_\phi, \lambda, \lambda_{\phi h} \) and the five physical observables \( v_D, v, m_\tilde{h}, m_{\tilde{\phi}}, \sin \theta \). The relation is given below,
$$v_D = \left( -\frac{\mu_\phi^2}{\lambda_\phi} \right)^{\frac{1}{2}}, \quad v = \left( -\frac{\mu}{\lambda} \right)^{\frac{1}{2}},$$

$$m_h = \sqrt{2\mu} = -\sqrt{2\lambda}v, \quad m_\phi = \sqrt{2\mu_\phi} = -\sqrt{2\lambda_\phi}v_D,$$

$$m_h^2 = \frac{1}{2} \left( m_\phi^2 + m_h^2 + \sqrt{(m_h^2 - m_\phi^2)^2 + 4\lambda_\phi^2v^2v_D^2} \right),$$

$$m_\phi^2 = \frac{1}{2} \left( m_\phi^2 + m_h^2 - \sqrt{(m_h^2 - m_\phi^2)^2 + 4\lambda_\phi^2v^2v_D^2} \right),$$

$$\tan 2\alpha = \frac{2\lambda_\phi hv_D}{m_h^2 - m_\phi^2}. \quad (A1)$$

**Appendix B: Limits from CKM matrix**

The most general interactions for $U(1)_{\mu-\tau}$ within the quark sector are given by:

$$\mathcal{L}_q = i\bar{q}^i_L \not{\!\!\!}q^j_L + i\bar{u}^i_R \not{\!\!\!}u^j_R + i\bar{d}^i_R \not{\!\!\!}d^j_R + i\bar{\psi} \not{\!\!\!}\gamma \psi - m_\psi \bar{\psi} \psi - \left( \bar{q}^i_L y^i_u \hat{H} u^j_R + \bar{q}^i_L y^i_d \hat{H} d^j_R + H.c. \right)$$

$$+ \lambda_1 \bar{q}^i_L \phi^* \psi_R + \lambda_2 \bar{q}^i_L \phi^* \psi_R + \lambda_3 \bar{q}^i_L \phi^* \psi_R + H.c. \quad (B1)$$

The mass matrix to generate CKM matrix in the quark sector are written in the basis of $(q_3, q_2, q_1, \psi)$. For up-type and down-type quarks, the mass matrices are

$$M_u = \begin{pmatrix} m_t & 0 & 0 & \lambda_3 v_D \\ m^u_{23} & m_c & 0 & \lambda_2 v_D \\ 0 & 0 & m_u & \lambda_1 v_D \\ 0 & 0 & 0 & m_\psi \end{pmatrix}, \quad M_d = \begin{pmatrix} m_b & 0 & 0 & \lambda_3 v_D \\ 0 & m_s & 0 & \lambda_2 v_D \\ m^d_{13} & m^d_{12} & m_d & \lambda_1 v_D \\ 0 & 0 & 0 & m_\psi \end{pmatrix}. \quad (B2)$$

In principle, all the matrix elements except the fourth line can be non-zero. Here we consider the simple matrices in Eq. (B2) to generate correct CKM matrix, with only three non-zero parameters in the off-diagonal terms for SM quark mass. To avoid modifying our existing results, we can set $\lambda_1 = 0$. Our notation is $M_{\text{diagonal}} = U_L^\dagger M U_R$, thus $q^\text{flavor}_R = U_R q^\text{mass}_R$ and $q^\text{flavor}_L = U_L q^\text{mass}_L$. Therefore, we have $\bar{u}^\text{flavor}_L \gamma^\mu W^+ \not{\!\!\!}\gamma^\mu \bar{d}^\text{flavor}_L = \bar{u}^\text{mass}_L \gamma^\mu W^+ V_{\text{CKM}} d^\text{mass}_L$, which results in the CKM matrix $V_{\text{CKM}} = U_L^{\text{wt}} U_L^{\dagger}$. The mass of quarks are slightly changed by the small non-zero off-diagonal terms $m^u_{23}, m^d_{13}$ and $m^d_{12}$. The SM quark masses at leading order
are
\[ m_t^2 = m_t^2 - \frac{v_D^2 (m_{23}^u \lambda_2 + m_t \lambda_3)^2}{v_D^2 \lambda_2 + m_{12}^2 - m_t^2} + (m_{23}^u)^2, \quad m_c^2 = m_c^2 \cos^2 \theta_2, \quad m_\tilde{a} = m_u \] (B3)

\[ m_b^2 = m_b^2 \left(1 - \frac{\lambda_3^2}{\lambda_2^2}\right) + (m_{13}^d)^2, \quad m_s^2 = \cot^2 \theta_2 \frac{m_d^2}{(m_{12}^d)^2 + m_d^2}, \]

\[ m_d^2 = m_d^2 + (m_{12}^d)^2 \left(1 + \cot^2 \theta_2 \frac{m_s^2}{m_d^2 + (m_{12}^d)^2}\right). \] (B4)

The heavy vector-like quark mass are the same as in Eq. (11). The expressions for off-diagonal CKM matrix at leading order are given by,

\[ V_{ub} = \frac{m_{13}^d}{m_b}, \] (B5)

\[ V_{us} = \frac{m_{12}^d m_s \cot \theta_2}{m_{12}^d + m_d^2}, \] (B6)

\[ V_{cd} = -\cot \theta_2 \frac{m_{12}^d m_s}{(m_{12}^d)^2 + m_d^2} - \cot \theta_2 \frac{m_{13}^d m_{23}^u}{m_b m_t} \simeq -V_{us}, \] (B7)

\[ V_{cb} = \cot \theta_2 \frac{m_{23}^u}{m_t}, \] (B8)

\[ V_{ts} = -\cot \theta_2 \frac{m_{23}^u}{m_t} - \cot \theta_2 \frac{m_{13}^d m_s}{m_b (m_{12}^d)^2 + m_d^2} \simeq -V_{cb}, \] (B9)

\[ V_{td} = \frac{m_{23}^u \cot \theta_2}{m_t} \frac{m_{12}^d m_s \cot \theta_2}{m_{12}^d + m_d^2} - \frac{m_{13}^d \star}{m_b} \simeq V_{cb} \times V_{us} - \frac{V_{ub}^*}{m_{13}^d \star}. \] (B10)

We require \(|V_{us}| \sim |V_{cd}| \simeq 0.225, |V_{cb}| \sim |V_{ts}| \simeq 0.043, |V_{ub}| \sim 0.004\) to satisfy the CKM matrix from PDG [87]. To realize \(|V_{td}| \sim 0.008\), we need \(m_{13}^d\) to be complex number. For our benchmark point \(\cot \theta_2 \sim 0.512\), the non-zero off-diagonal SM quark mass required by CKM matrix are

\[ m_{12}^d \simeq 0.01 m_d, \quad |m_{13}^d| \simeq 0.004 m_{\tilde{b}}, \quad m_{23}^u \simeq 0.084 m_{\tilde{t}}. \] (B11)

It is clear that they are sufficiently small comparing with the diagonal masses. Thus we successfully demonstrate that the generation of CKM matrix does not affect the new physics phenomenology we have discussed previously.

\[ [1] \text{CMS Collaboration,} \quad \text{Search for new resonances in the diphoton final state in the mass range between 70 and 110 GeV in pp collisions at } \sqrt{s} = 8 \text{ and } 13 \text{ TeV, Tech. Rep.} \]

CMS-PAS-HIG-17-013, CERN, Geneva, 2017.
[2] CMS Collaboration, Collaboration, Search for new resonances in the diphoton final state in the mass range between 80 and 110 GeV in pp collisions at $\sqrt{s} = 8$ TeV, Tech. Rep. CMS-PAS-HIG-14-037, CERN, Geneva, 2015.

[3] ATLAS Collaboration, G. Aad et al., Search for Scalar Diphoton Resonances in the Mass Range 65 – 600 GeV with the ATLAS Detector in pp Collision Data at $\sqrt{s} = 8$ TeV, Phys. Rev. Lett. 113 (2014), no. 17 171801, [arXiv:1407.6583].

[4] OPAL, DELPHI, LEP Working Group for Higgs boson searches, ALEPH, L3 Collaboration, R. Barate et al., Search for the standard model Higgs boson at LEP, Phys. Lett. B565 (2003) 61–75, [hep-ex/0306033].

[5] J. Cao, X. Guo, Y. He, P. Wu, and Y. Zhang, Diphoton signal of the light Higgs boson in natural NMSSM, Phys. Rev. D95 (2017), no. 11 116001, [arXiv:1612.08522].

[6] A. Mariotti, D. Redigolo, F. Sala, and K. Tobioka, New LHC bound on low-mass diphoton resonances, arXiv:1710.01743.

[7] A. Crivellin, J. Heeck, and D. Müller, Large $h \to bs$ in generic two-Higgs-doublet models, Phys. Rev. D97 (2018), no. 3 035008, [arXiv:1710.04663].

[8] P. J. Fox and N. Weiner, Light Signals from a Lighter Higgs, arXiv:1710.07649.

[9] U. Haisch and A. Malinauskas, Let there be light from a second light Higgs doublet, JHEP 03 (2018) 135, [arXiv:1712.06599].

[10] R. Vega, R. Vega-Morales, and K. Xie, Light (and darkness) from a light hidden Higgs, arXiv:1805.01970.

[11] LHCb Collaboration, R. Aaij et al., Test of lepton universality using $B^+ \to K^+ \ell^+\ell^-$ decays, Phys. Rev. Lett. 113 (2014) 151601, [arXiv:1406.6482].

[12] LHCb Collaboration, R. Aaij et al., Test of lepton universality with $B^0 \to K^{*0} \ell^+\ell^-$ decays, JHEP 08 (2017) 055, [arXiv:1705.05802].

[13] W. Altmannshofer, S. Gori, M. Pospelov, and I. Yavin, Quark flavor transitions in $L_\mu - L_\tau$ models, Phys. Rev. D89 (2014) 095033, [arXiv:1403.1269].

[14] A. Crivellin, G. D’Ambrosio, and J. Heeck, Explaining $h \to \mu^+\mu^-$, $B \to K^*\mu^+\mu^-$ and $B \to K\mu^+\mu^-/B \to Ke^+e^-$ in a two-Higgs-doublet model with gauged $L_\mu - L_\tau$, Phys. Rev. Lett. 114 (2015) 151801, [arXiv:1501.00993].

[15] W. Altmannshofer and I. Yavin, Predictions for lepton flavor universality violation in rare $B$ decays in models with gauged $L_\mu - L_\tau$, Phys. Rev. D92 (2015), no. 7 075022,
[arXiv:1508.07009].

[16] W. Altmannshofer, M. Carena, and A. Crivellin, \( L_\mu - L_\tau \) theory of Higgs flavor violation and \((g-2)_\mu\), Phys. Rev. D94 (2016), no. 9 095026, [arXiv:1604.08221].

[17] W. Altmannshofer, S. Gori, S. Profumo, and F. S. Queiroz, Explaining dark matter and B decay anomalies with an \( L_\mu - L_\tau \) model, JHEP 12 (2016) 106, [arXiv:1609.04026].

[18] R. Alonso, P. Cox, C. Han, and T. T. Yanagida, Flavoured \( B - L \) local symmetry and anomalous rare \( B \) decays, Phys. Lett. B774 (2017) 643–648, [arXiv:1705.03858].

[19] C. Bonilla, T. Modak, R. Srivastava, and J. W. F. Valle, \( U(1)_{B_3-3L_\mu} \) gauge symmetry as the simplest description of \( b \to s \) anomalies, arXiv:1705.00915.

[20] T. Nomura and H. Okada, A Zee-Babu type model with \( U(1)_{\mu-\tau} \) gauge symmetry, arXiv:1803.04795.

[21] C.-H. Chen and T. Nomura, Penguin \( b \to s\ell^+\ell^- \) and \( B \)-meson anomalies in a gauged \( L_\mu - L_\tau \), Phys. Lett. B777 (2018) 420–427, [arXiv:1707.03249].

[22] P. Ko, T. Nomura, and H. Okada, Explaining \( B \to K(\ast)\ell^+\ell^- \) anomaly by radiatively induced coupling in \( U(1)_{\mu-\tau} \) gauge symmetry, Phys. Rev. D95 (2017), no. 11 111701, [arXiv:1702.02699].

[23] A. Crivellin, G. D’Ambrosio, and J. Heeck, Addressing the LHC flavor anomalies with horizontal gauge symmetries, Phys. Rev. D91 (2015), no. 7 075006, [arXiv:1503.03477].

[24] A. Celis, J. Fuentes-Martin, M. Jung, and H. Serodio, Family nonuniversal \( Z' \) models with protected flavor-changing interactions, Phys. Rev. D92 (2015), no. 1 015007, [arXiv:1505.03079].

[25] A. Falkowski, M. Nardecchia, and R. Ziegler, Lepton Flavor Non-Universality in \( B \)-meson Decays from a \( U(2) \) Flavor Model, JHEP 11 (2015) 173, [arXiv:1509.01249].

[26] A. K. Alok, B. Bhattacharya, A. Datta, D. Kumar, J. Kumar, and D. London, New Physics in \( b \to s\mu^+\mu^- \) after the Measurement of \( R_{K^\ast} \), Phys. Rev. D96 (2017), no. 9 095009, [arXiv:1704.07397].

[27] X.-G. He, G. C. Joshi, H. Lew, and R. R. Volkas, Simplest \( Z' \) model, Phys. Rev. D44 (Oct. 1991) 2118–2132.

[28] S. Baek, N. G. Deshpande, X. G. He, and P. Ko, Muon anomalous \( g-2 \) and gauged \( L_\mu - L_\tau \) models, Phys. Rev. D64 (2001) 055006, [hep-ph/0104141].

[29] R. Foot, X. G. He, H. Lew, and R. R. Volkas, Model for a light Z-prime boson, Phys. Rev.
D50 (1994) 4571–4580, [hep-ph/9401250].

[30] E. Salvioni, A. Strumia, G. Villadoro, and F. Zirner, Non-universal minimal Z’ models: present bounds and early LHC reach, JHEP 03 (2010) 010, [arXiv:0911.1450].

[31] J. Heeck and W. Rodejohann, Gauged $L_\mu - L_\tau$ Symmetry at the Electroweak Scale, Phys. Rev. D84 (2011) 075007, [arXiv:1107.5238].

[32] W.-Z. Feng, P. Nath, and G. Peim, Cosmic coincidence and asymmetric dark matter in a stueckelberg extension, Phys. Rev. D85 (Jun, 2012) 115016.

[33] K. Harigaya, T. Igari, M. M. Nojiri, M. Takeuchi, and K. Tobe, Muon $g-2$ and LHC phenomenology in the $L_\mu - L_\tau$ gauge symmetric model, JHEP 03 (2014) 105, [arXiv:1311.0870].

[34] E. Ma, D. P. Roy, and S. Roy, Gauged $L_\mu - L_\tau$ with large muon anomalous magnetic moment and the bimaximal mixing of neutrinos, Phys. Lett. B525 (2002) 101–106, [hep-ph/0110146].

[35] M. Ibe, W. Nakano, and M. Suzuki, Constraints on $L_\mu - L_\tau$ gauge interactions from rare kaon decay, Phys. Rev. D95 (2017), no. 5 055022, [arXiv:1611.08460].

[36] A. Biswas, S. Choubey, and S. Khan, Neutrino Mass, Dark Matter and Anomalous Magnetic Moment of Muon in a $U(1)_{L_\mu - L_\tau}$ Model, JHEP 09 (2016) 147, [arXiv:1608.04194].

[37] F. Elahi and A. Martin, Constraints on $L_\mu - L_\tau$ interactions at the LHC and beyond, Phys. Rev. D93 (2016), no. 1 015022, [arXiv:1511.04107].

[38] S. N. Gninenko and N. V. Krasnikov, Probing the muon $g-2$ anomaly, $L_\mu - L_\tau$ gauge boson and Dark Matter in dark photon experiments, arXiv:1801.10448.

[39] J. Cao, L. Feng, X. Guo, L. Shang, F. Wang, P. Wu, and L. Zu, Explaining the DAMPE data with scalar dark matter and gauged $U(1)_{Le-L_\mu}$ interaction, Eur. Phys. J. C78 (2018), no. 3 198, [arXiv:1712.01244].

[40] A. Biswas, S. Choubey, L. Covi, and S. Khan, Explaining the 3.5 keV X-ray Line in a $L_\mu - L_\tau$ Extension of the Inert Doublet Model, JCAP 1802 (2018), no. 02 002, [arXiv:1711.00553].

[41] S. Baek, Dark matter contribution to $b \to s \mu^+ \mu^-$ anomaly in local $U(1)_{L_\mu - L_\tau}$ model, Phys. Lett. B781 (2018) 376–382, [arXiv:1707.04573].

[42] F. Elahi and A. Martin, Using the modified matrix element method to constrain $L_\mu - L_\tau$ interactions, Phys. Rev. D96 (2017), no. 1 015021, [arXiv:1705.02563].

[43] K. Asai, K. Hamaguchi, and N. Nagata, Predictions for the neutrino parameters in the
minimal gauged $U(1)_{L_\mu - L_\tau}$ model, Eur. Phys. J. C77 (2017), no. 11 763, [arXiv:1705.00419].

[44] Y. Kaneta and T. Shimomura, On the possibility of a search for the $L_\mu - L_\tau$ gauge boson at Belle-II and neutrino beam experiments, PTEP 2017 (2017), no. 5 053B04, [arXiv:1701.00156].

[45] A. Biswas, S. Choubey, and S. Khan, FIMP and Muon $(g - 2)$ in a $U(1)_{L_\mu - L_\tau}$ Model, JHEP 02 (2017) 123, [arXiv:1612.03067].

[46] Y. Tang and Y.-L. Wu, Flavor non-universal gauge interactions and anomalies in B-meson decays, Chin. Phys. C42 (2018), no. 3 033104, [arXiv:1705.05643].

[47] P. Ko, T. Nomura, and H. Okada, A flavor dependent gauge symmetry, Predictive radiative seesaw and LHCb anomalies, Phys. Lett. B772 (2017) 547–552, [arXiv:1701.05788].

[48] G. Arcadi, T. Hugle, and F. S. Queiroz, The Dark $L_\mu - L_\tau$ Rises via Kinetic Mixing, arXiv:1803.05723.

[49] A. Kamada, K. Kaneta, K. Yanagi, and H.-B. Yu, Self-interacting dark matter and muon $g - 2$ in a gauged $U(1)_{L_\mu - L_\tau}$ model, arXiv:1805.00651.

[50] A. Biswas, S. Choubey, and S. Khan, Inverse seesaw and dark matter in a gauged B – L extension with flavour symmetry, arXiv:1805.00568.

[51] Z.-z. Xing and Z.-h. Zhao, A review of $\mu - \tau$ flavor symmetry in neutrino physics, Rept. Prog. Phys. 79 (2016), no. 7 076201, [arXiv:1512.04207].

[52] LHC Higgs Cross Section Working Group Collaboration, D. de Florian et al., Handbook of LHC Higgs Cross Sections: 4. Deciphering the Nature of the Higgs Sector, arXiv:1610.07922.

[53] LHC Higgs Cross Section Working Group Collaboration, J. R. Andersen et al., Handbook of LHC Higgs Cross Sections: 3. Higgs Properties, arXiv:1307.1347.

[54] CMS Collaboration Collaboration, Combined measurements of the Higgs boson’s couplings at $\sqrt{s} = 13$ TeV, Tech. Rep. CMS-PAS-HIG-17-031, CERN, Geneva, 2018.

[55] ATLAS Collaboration Collaboration, Combined measurements of Higgs boson production and decay in the $H \to ZZ^* \to 4\ell$ and $H \to \gamma\gamma$ channels using $\sqrt{s} = 13$ TeV pp collision data collected with the ATLAS experiment, Tech. Rep. ATLAS-CONF-2017-047, CERN, Geneva, Jul, 2017.

[56] CMS Collaboration, A. M. Sirunyan et al., Measurements of Higgs boson properties in the
diphoton decay channel in proton-proton collisions at $\sqrt{s} = 13$ TeV, arXiv:1804.02716.

[57] ATLAS Collaboration, M. Aaboud et al., Measurements of Higgs boson properties in the diphoton decay channel with 36 fb$^{-1}$ of pp collision data at $\sqrt{s} = 13$ TeV with the ATLAS detector, arXiv:1802.04146.

[58] ATLAS Collaboration, G. Aad et al., Measurement of Higgs boson production in the diphoton decay channel in pp collisions at center-of-mass energies of 7 and 8 TeV with the ATLAS detector, Phys. Rev. D90 (2014), no. 11 112015, [arXiv:1408.7084].

[59] W. Altmannshofer and D. M. Straub, New Physics in $B \to K^{*} \mu \mu$, Eur. Phys. J. C73 (2013) 2646, [arXiv:1308.1501].

[60] W. Altmannshofer and D. M. Straub, New physics in $b \to s$ transitions after LHC run 1, Eur. Phys. J. C75 (2015), no. 8 382, [arXiv:1411.3161].

[61] W. Altmannshofer and D. M. Straub, Implications of $b \to s$ measurements, in Proceedings, 50th Rencontres de Moriond Electroweak Interactions and Unified Theories: La Thuile, Italy, March 14–21, 2015, pp. 333–338, 2015. arXiv:1503.06199.

[62] A. Greljo, G. Isidori, and D. Marzocca, On the breaking of Lepton Flavor Universality in $B$ decays, JHEP 07 (2015) 142, [arXiv:1506.01705].

[63] S. Descotes-Genon, L. Hofer, J. Matias, and J. Virto, Global analysis of $b \to s \ell \ell$ anomalies, JHEP 06 (2016) 092, [arXiv:1510.04239].

[64] T. Hurth, F. Mahmoudi, and S. Neshatpour, On the anomalies in the latest LHCb data, Nucl. Phys. B909 (2016) 737–777, [arXiv:1603.00865].

[65] W. Altmannshofer, P. Stangl, and D. M. Straub, Interpreting Hints for Lepton Flavor Universality Violation, Phys. Rev. D96 (2017), no. 5 055008, [arXiv:1704.05435].

[66] B. Capdevila, A. Crivellin, S. Descotes-Genon, J. Matias, and J. Virto, Patterns of New Physics in $b \to s \ell^+ \ell^-$ transitions in the light of recent data, JHEP 01 (2018) 093, [arXiv:1704.05340].

[67] W. Altmannshofer, C. Niehoff, P. Stangl, and D. M. Straub, Status of the $B \to K^* \mu^+ \mu^-$ anomaly after Moriond 2017, Eur. Phys. J. C77 (2017), no. 6 377, [arXiv:1703.09189].

[68] Belle Collaboration, S. Wehle et al., Lepton-Flavor-Dependent Angular Analysis of $B \to K^* \ell^+ \ell^-$, Phys. Rev. Lett. 118 (2017), no. 11 111801, [arXiv:1612.05014].

[69] CMS Collaboration, V. Khachatryan et al., Search for narrow resonances in dilepton mass spectra in proton-proton collisions at $\sqrt{s} = 13$ TeV and combination with 8 TeV data, Phys.
[70] **ATLAS** Collaboration, M. Aaboud et al., *Search for high-mass new phenomena in the dilepton final state using proton-proton collisions at √s = 13 TeV with the ATLAS detector*, *Phys. Lett. B761* (2016) 372–392, [arXiv:1607.03669].

[71] **ATLAS** Collaboration, M. Aaboud et al., *Search for new high-mass phenomena in the dilepton final state using 36 fb⁻¹ of proton-proton collision data at √s = 13 TeV with the ATLAS detector*, *JHEP* 10 (2017) 182, [arXiv:1707.02424].

[72] **ATLAS** Collaboration, G. Aad et al., *Search for high-mass dilepton resonances in pp collisions at √s = 8 TeV with the ATLAS detector*, *Phys. Rev. D90* (2014), no. 5 052005, [arXiv:1405.4123].

[73] **ATLAS** Collaboration, G. Aad et al., *Search for high-mass resonances decaying to dilepton final states in pp collisions at s**(1/2) = 7-TeV with the ATLAS detector*, *JHEP* 11 (2012) 138, [arXiv:1209.2535].

[74] CMS Collaboration, *Searches for dijet resonances in pp collisions at √s = 13 TeV using data collected in 2016.*, Tech. Rep. CMS-PAS-EXO-16-056, CERN, Geneva, 2017.

[75] W. Altmannshofer, S. Gori, M. Pospelov, and I. Yavin, *Neutrino Trident Production: A Powerful Probe of New Physics with Neutrino Beams*, *Phys. Rev. Lett. 113* (2014) 091801, [arXiv:1406.2332].

[76] **CHARM-II** Collaboration, D. Geiregat et al., *First observation of neutrino trident production*, *Phys. Lett. B245* (1990) 271–275.

[77] **CCFR** Collaboration, S. R. Mishra et al., *Neutrino tridents and W Z interference*, *Phys. Rev. Lett. 66* (1991) 3117–3120.

[78] **NuTeV** Collaboration, T. Adams et al., *Neutrino trident production from NuTeV*, in *High-energy physics. Proceedings, 29th International Conference, ICHEP’98, Vancouver, Canada, July 23-29, 1998. Vol. 1, 2*, pp. 631–634, 1998. hep-ex/9811012.

[79] K. Fuyuto, W.-S. Hou, and M. Kohda, *Z’ induced FCNC decays of top, beauty, and strange quarks*, *Phys. Rev. D93* (2016), no. 5 054021, [arXiv:1512.09026].

[80] D. Liu, J. Liu, C. E. M. Wagner, and X.-P. Wang, *Bottom-quark Forward-Backward Asymmetry, Dark Matter and the LHC*, *Phys. Rev. D97* (2018), no. 5 055021, [arXiv:1712.05802].

[81] **ATLAS** Collaboration, M. Aaboud et al., *Search for R-parity-violating supersymmetric...*
particles in multi-jet final states produced in p-p collisions at $\sqrt{s} = 13$ TeV using the ATLAS detector at the LHC, \texttt{arXiv:1804.03568}.

[82] \textbf{ATLAS} Collaboration, G. Aad et al., \textit{Search for massive supersymmetric particles decaying to many jets using the ATLAS detector in pp collisions at $\sqrt{s} = 8$ TeV}, \textit{Phys. Rev.} \textbf{D91} (2015), no. 11 112016, \texttt{[arXiv:1502.05686]}. [Erratum: Phys. Rev.D93,no.3,039901(2016)].

[83] \textbf{CMS} Collaboration, S. Chatrchyan et al., \textit{Searches for light- and heavy-flavour three-jet resonances in pp collisions at $\sqrt{s} = 8$ TeV}, \textit{Phys. Lett.} \textbf{B730} (2014) 193–214, \texttt{[arXiv:1311.1799]}.

[84] S. El Hedri, A. Kaminska, M. de Vries, and J. Zurita, \textit{Simplified Phenomenology for Colored Dark Sectors}, \textit{JHEP} \textbf{04} (2017) 118, \texttt{[arXiv:1703.00452]}.

[85] M. Czakon, M. L. Mangano, A. Mitov, and J. Rojo, \textit{Constraints on the gluon PDF from top quark pair production at hadron colliders}, \textit{JHEP} \textbf{07} (2013) 167, \texttt{[arXiv:1303.7215]}.

[86] R. Barbieri and G. F. Giudice, \textit{b → sγ decay and supersymmetry}, \textit{Phys. Lett.} \textbf{B309} (1993) 86–90, \texttt{[hep-ph/9303270]}.

[87] \textbf{Particle Data Group} Collaboration, C. Patrignani et al., \textit{Review of Particle Physics}, \textit{Chin. Phys.} \textbf{C40} (2016), no. 10 100001.

[88] A. J. Buras, F. De Fazio, and J. Girrbach, \textit{The Anatomy of Z' and Z with Flavour Changing Neutral Currents in the Flavour Precision Era}, \textit{JHEP} \textbf{02} (2013) 116, \texttt{[arXiv:1211.1896]}.

[89] G. Isidori, \textit{Flavor physics and CP violation}, in \textit{Proceedings, 2012 European School of High-Energy Physics (ESHEP 2012): La Pommeraye, Anjou, France, June 06-19, 2012}, pp. 69–105, 2014. \texttt{arXiv:1302.0661}.

[90] A. Lenz, U. Nierste, J. Charles, S. Descotes-Genon, A. Jantsch, C. Kaufhold, H. Lacker, S. Monteil, V. Niess, and S. T’Jampens, \textit{Anatomy of New Physics in B – $\bar{B}$ mixing}, \textit{Phys. Rev.} \textbf{D83} (2011) 036004, \texttt{[arXiv:1008.1593]}.

[91] \textbf{ATLAS} Collaboration, A. Durglishvili, \textit{Search for tZ Flavour Changing Neutral Currents in top-quark decays with the ATLAS detector}, \texttt{arXiv:1712.09802}.