1. Introduction

Periodically arranged structures of dielectric media are called photonic crystals \(^{1-4}\). They have photonic band gaps in which no electromagnetic wave can propagate. If the periodicity is changed locally by introducing a defect, localized modes appear in the band gap \(^{5-8}\). Such localization function of electromagnetic waves can be applied to various devices, for example resonators, waveguides, and antennas. Three dimensional dielectric lattices were designed by using graphical application of a computer aided designing (CAD) software, and acrylic diamond structures with alumina nanoparticles dispersion were formed by using micro stereolithography (\(\mu\)-STL) of a computer aided manufacturing (CAD) system. Fabricated precursors were dewaxed and sintered in the air to obtained full ceramics photonic crystals. The terahertz wave properties were measured by terahertz time domain spectroscopy (TDS) device. A complete photonic band gap to reflect the terahertz wave perfectly was observed, and showed good agreement with a theoretical simulation of plane wave expansion (PWE) method. Moreover, localization of the terahertz wave were observed in point or plane defects introduced into the diamond photonic crystals through an electromagnetic field analysis of transmission line modeling (TLM) method.

Keywords: Photonic Crystal, Band Gap, Dielectric Material, Terahertz Wave, Stereolithography
In this paper, the novel stereolithography process to fabricate the micro diamond photonic crystals by using the ceramic slurry with the nanoparticles will be introduced. And, the resonance and localization properties of the terahertz waves into various types of the structural defects introduced according to theoretical electromagnetic simulations will be demonstrated.

2. Photonic Band Gap Formation

Photonic crystals composed of dielectric lattices form band gaps for electromagnetic waves. These artificial crystals can totally reflect light or microwave at a wavelength comparable to the lattice spacings by Bragg deflection as shown in Fig. 1. Two different standing waves oscillating in the air and dielectric matrix form higher and lower frequency bands in the first and second Brillouin zones, respectively. The band gap width can be controlled by varying structure, filling ratio, and dielectric constant of the lattice. Structural modifications by introducing defects or varying the lattice spacing can control the propagation of light or microwaves. The band diagram of the photonic crystal along symmetry lines in the Brillouin zone is drawn theoretically. The Maxwell’s equations (1) and (2) can be solved by means of plane wave propagation (PWE) method, where \( \omega \) and \( c \) denote frequency and light velocity, respectively. Electronic and magnetic field \( E_{\omega}(r) \) and \( H_{\omega}(r) \) are described with the following plane wave equations (3) and (4), respectively. The periodic arrangement of dielectric constant \( \varepsilon(r) \) can be obtained as equation (5) form the crystal structure. \( G \) and \( k \) are reciprocal vector and wave vector, respectively.

\[
\begin{align*}
\n\mathbf{V} \times \left( \frac{1}{\varepsilon(r)} \mathbf{V} \times \right) \mathbf{H}_{\omega}(r) = \left( \frac{\omega}{c} \right)^2 \mathbf{H}_{\omega}(r) & \quad \cdots (1) \\
\mathbf{V} \times \left( \frac{1}{\varepsilon(r)} \mathbf{V} \times \right) \mathbf{E}_{\omega}(r) = \left( \frac{\omega}{c} \right)^2 \mathbf{E}_{\omega}(r) & \quad \cdots (2) \\
\mathbf{H}_{\omega}(r) = \sum_G \mathbf{H}_{\omega}(G) e^{i(k+G)r} & \quad \cdots (3) \\
\mathbf{E}_{\omega}(r) = \sum_G \mathbf{E}_{\omega}(G) e^{i(k+G)r} & \quad \cdots (4) \\
\varepsilon(r) = \sum_G \frac{\varepsilon(G)}{G} e^{i\pi r} & \quad \cdots (5)
\end{align*}
\]

3. Applications of Photonic Crystals

Fig. 2 shows expected applications of photonic crystal for light and electromagnetic wave control in various wavelength ranges\(^\text{29}\). Air guides formed in a photonic crystal with nanometer order will be used as the light wave circuit in the perfect reflective structure. When a light emitting diode is placed in an air cavity formed in a photonic crystal, an efficient laser emission can be enhanced due to the high coherent resonance in the micro cavity. While, millimeter order periodic structures can control microwaves effectively. Directional antennas and filters composed of photonic crystals can be applied to millimeter wave radar devices for intelligent traffic system (ITS) and wireless communication system. The perfect reflection of millimeter wave by photonic crystal will be useful for barriers to prevent wave interference. Terahertz waves with micrometer order wavelength are expected to apply for various types of sensors to detect other physical, chemical and living events. The micrometer order photonic crystals can applied for the terahertz wave cavities, filters and antennas.

4. Geometry of Artificial Crystals

Typical photonic crystal structures were shown in

![Fig. 1 Principles of photonic band gap formations in periodic arrangements of dielectric materials. Two different standing waves with higher and lower frequencies are formed in a photonic crystal, and a forbidden gap is formed between these frequencies.](image)
A woodpile structure (a) with simple structure of stacked rods can form the perfect photonic band gap. Photonic crystals composed of GaAs or InP were fabricated by using semiconductor process techniques\(^\text{30}\). A light wave circuit (b) in the periodic structure of arranged AlGaAs pins is processed by using electron beam lithography and etching techniques\(^\text{31}\). A layered structure (c) composed of Si and SiO\(_2\) with the different dielectric constants realize light wave polarization and super prism effects\(^\text{32}\). These layers are stacked by using self-organized growing in alternate spattering and etching. An inverse opal structure (d) is composed of air spheres with FCC structure in TiO\(_2\), Si, Ge or CdS matrix\(^\text{33}\). At first, polystyrene spheres are arranged by using self-organization in colloidal solutions. Then, the slurry of these dielectric media is infiltrated into the periodic structure and sintered. The optical fiber (e) with photonic crystal structure can guide light efficiently along the central core\(^\text{34}\). Silica fibers and glass capillaries were bundled by wire drawing at high temperature. Diamond type photonic crystals (f) composed of TiO\(_2\), SiO\(_2\) or Al\(_2\)O\(_3\) can fabricated by using stereolithography and successive sintering process. The wider perfect band gap is obtained in microwave and terahertz wave frequency ranges.

**Fig. 2** Expected applications of the photonic crystal in various electromagnetic wavelengths.

**Fig. 3** Typical periodic structures of the photonic crystals with woodpile structure (a), patterned substrate (b), stacked layer (c), inverse opal structure (d), bundled fiber (e), and diamond structure (f).
5. Design of Diamond Structure

Electromagnetic band diagrams of diamond structures were calculated to determine their geometric parameters by the PWE method. The dielectric constant of the lattice used in the calculation was 10 for alumina. Fig. 4 (a), (b), and (c) show a unit cell of the diamond structure, the definition of the aspect ratio, and the calculated complete band gap width as a function of the aspect ratio, respectively. According to Fig. 4 (c), the band gap becomes the widest when the aspect ratio is 2.0. The wider the band gap, the easier it is to localize the electromagnetic waves when a defect is introduced. When the aspect ratio is 1.5, the lattice rods become thick and the band gap width is approximately 84% as much as that of 2.0. Thus, the aspect ratio of the diamond structure was designed to be 1.5. The lattice constant was 500 μm. The whole structure was 4 × 4 × 2 mm in size, consisting of 8 × 8 × 4 unit cells.

6. Fabrication of Dielectric Lattices

The three dimensional diamond lattices were designed by using a computer graphic application (Toyota Caelum Co. Ltd., Thinkdesign ver. 7.0). The graphic data was converted into a stereolithography (STL) file of a rapid prototyping format. After the slicing process of the three dimensional model into a series of two dimensional cross sectional data into thin sections, this data file was transferred to micro stereolithography equipment (D-MEC Co. Ltd., Japan, SI-C1000). In our system, photo sensitive acrylic resin dispersed with alumina particles of 170 nm in diameter at 40 vol. % was fed over the substrate from a dispenser nozzle. The highly viscous ceramic/resin paste was fed with controlled air pressure. It was spread uniformly by moving a knife edge. The thickness of each layer was controlled to 10 μm. A two dimensional pattern was formed by illuminating visible laser of 405 nm in wavelength on the resin surface. The high resolution has been achieved by using a digital micro-mirror device (DMD) and an objective lens. Fig. 5 shows a schematic illustration of the micro stereolithography system. The DMD is an optical element assembled by mirrors of 14 μm in edge length. The tilting of each tiny mirror can be controlled according to the two dimensional cross sectional data by using a computer. The three dimensional structure was built by stacking these micro patterns layer by layer. In order to avoid deformation and cracking during dewaxing, careful investigation for the dewaxing process is required. The precursors with diamond structures were heated at various temperatures from 100°C to 600°C while the heating rate was 1.0°C/min. The dewaxing process was observed in respect to the weight and color changes. Nanometer sized alumina particles could be sintered at 1500°C. The heating rate was 8.0°C/min. The density of the sintered sample was measured by the Archimedes method. The microstructure of the lattices was observed by using scanning electron microscopy (SEM).

7. Measurement of Electromagnetic Wave

In recent years, terahertz waves have received extensive attentions and investigations since they have a lot of interesting and applicable features in various fields such as materials, communication, medicine, and biology. It is possible to detect gun powders and ceramic blades hidden in bags, clothes,
and envelopes by using terahertz waves since they can penetrate plastic, paper, and clothes without radiation damage to living bodies\(^4\). It is also possible to identify toxic drugs because they have spectral fingerprints or absorption spectra\(^5\). Moreover, they can distinguish cancerous areas from healthy areas due to the different absorption rates\(^6\). A terahertz wave attenuation of transmission amplitudes through the diamond photonic crystals were measured by using a terahertz time domain spectrometer (TDS) apparatus (Advanced Infrared Spectroscopy Co. Ltd., Japan, Pulse-IRS 1000). Fig. 6 shows the schematic illustration of the measurement system. Femto second laser beams were irradiated into a micro emission antenna formed on a semiconductor substrate to generate the terahertz wave pulses. The terahertz waves were transmitted trough the micro patterned samples perpendicularly. The dielectric constant of the bulk samples were measured through a phase shift counting. Diffraction and resonation behaviors in the dielectric pattern were calculated theoretically by using a transmission line modeling (TLM) simulator (Flomerics, UK, Microstripes Ver. 7.5) of a finite difference time domain (FDTD) method.

8. Alumina Photonic Crystals

An alumina dispersed resin precursor fabricated by the micro stereolithography is shown in Fig. 7. The lattice constant of the formed diamond structure was
500 μm. The spatial resolution was approximately 0.5 μm. The weight and color changes as a function of temperature are shown in Fig. 8. The sample color changed into black at 400°C due to carbonizing of resin. It became white at 600°C suggesting burning out of resin. Thus, the dewaxing process is considered to start at 200°C and complete at 600°C. The dewaxing temperature was optimized to be 600°C. Through the dewaxing and sintering processes, ceramic diamond structures were successfully obtained. Fig. 9 shows (111), (100) and (110) planes of the sintered diamond structure composed of the micrometer order alumina lattice. The lattice constant was measured as 375 μm. The deformation and cracking were not observed. The linear shrinkage on the horizontal axis was 23.8 % and that on the vertical axis was 24.6 %. It is possible to obtain the uniform shrinkage by designing an appropriate elongated structure in the vertical direction for compensation to the gravity effect. The relative density reached 97.5 %. Dense alumina microstructure was formed, and the average grain size was approximately 2 μm. The measured dielectric constant of the lattice was about 10.

9. Terahertz Wave Spectroscopy

The terahertz wave attenuation of the transmission amplitude through the alumina diamond structure for Γ·L <111>, Γ·X <100> and Γ·K <110> crystal direction is shown in Fig. 10. The forbidden gap is formed at the frequency rage of 0.32 - 0.49, 0.35 - 0.53 and 0.35 - 0.52 THz in transmission spectra for Γ·L <111>, Γ·X <100> and Γ·K <110> directions, respectively. A common band gap was observed in every direction at the frequency range from 0.35 to 0.49 THz, where the electromagnetic wave cannot transmit through the crystal and is totally reflected in all directions. The measured band gap frequencies were compared with calculation results by the plane wave expansion method as shown in Fig. 11. The band diagram of the photonic crystal along symmetry lines...
in the Brillouin zone is drawn theoretically by the PWE method. The opened circles mean the higher and lower edges of the measured band gaps. These frequency ranges of opaque regions corresponded to the calculation. According to the photonic band diagram, it was demonstrated that a complete photonic band gap opened between 0.35 and 0.49 THz. When a gap is formed, there are two types of the standing wave modes with the wavelength corresponding to periodicity of the dielectric lattices at the frequencies of the each band edges as shown in Fig. 1. The lower frequency mode concentrates the wave energy in the dielectric region, whereas the higher frequency mode concentrates in the air region.

10. Point Defect of Air Cavity

A diamond structure introduced by an air cubic defect with the same dimension as the unit cell is Fig. 12. The transmission spectrum along the $\Gamma$-X $<$100$>$ direction is shown in Fig. 13. Two peaks were observed in the band gap at the frequencies 0.42 and 0.46 THz, respectively. Measured peak frequencies were compared with the simulation by the TLM method as seen in Fig. 14. They were in good agreement with the simulation. The first peak in Fig. 13 was named mode A, while the second one mode B. The electric field distributions of these modes were simulated by the TLM method. Fig. 15 (a) and (b) show cross sectional images of the distributions. In the images, the red area indicates that the electric field intensity is high, whereas blue and green area indicates it is low. Thus, it was considered that the mode A concentrated the oscillation energy of a half wavelength with an antinode in the cube. Also, the
mode B concentrated the energy of a half wavelength on the sides of the cube with a node in the cube. Therefore, it was confirmed that the defect introduced structure localized terahertz waves.

11. Plane Defect of Twinned Lattices

Twinned diamond structure composed of the mirror symmetric alumina lattices is shown in Fig. 16. The plane defect forms parallel to the (100) crystal plane. The transmission spectrum for the Γ-X <100> crystal direction of the twinned diamond structure is shown in Fig. 17. The localized mode forms in the photonic band gap. At the transmission peak of 0.41 THz in frequency, the incident terahertz wave localized in the plane defect, and the amplified wave propagated to the other side of the crystal sample. The measured band gap region and the peak frequency of the localized mode were compared with the calculated spectrum by the TLM method as shown in Fig. 18. They were in good agreement. Subsequently, the electric field distribution in the twinned diamond lattices was simulated. Fig. 19 shows cross sectional images of the distributions. Incident terahertz wave is resonate and localized in the plane defect region between the twinned diamond lattices. The amplified electromagnetic wave by multiple reflections can transmit through the photonic crystal. Therefore, the transmission peak will be formed in the band gap. The three dimensional photonic band gap structure
to form the localized mode can be applied to the terahertz wave filters.

12. Terahertz Wave Beam Emitter

A modified diamond photonic crystal with the plane defect between the twinned lattice structures is shown in Fig. 20. The lattice structures of one and two periods were arranged on the right and left side of the plane defect, respectively. The incident direction of the terahertz wave was from the left to the right. In the measured transmission spectrum, one localized mode peak was observed in the band gap at the frequencies of 0.41 THz. The measured
band gap region and peak frequency of the localized mode were compared with calculations by the TLM method. They had good agreement. Subsequently, the electric field distribution in the twinned diamond lattices was simulated. Fig. 21 shows cross sectional images of the distributions. Incident terahertz wave is resonate and localized in the plane defect region. The amplified electromagnetic wave by multiple reflections can transmit preferentially for the right direction through the diamond lattice with only one period of the diffraction lattices. On the right side of the sample, the radiation pattern shows the plane wave expansion. The micro photonic crystal with the twinned ceramic lattice of the diamond structure can be applied to a terahertz beam emitters.

13. Conclusion

Three dimensional micrometer order photonic crystals with a diamond structure composed of acrylic resin including alumina nanoparticles at 40 vol. % by using micro stereolithography a structural joining process. By the careful optimization of process parameters regarding dewaxing and sintering, dense alumina micro lattice structures were fabricated successfully. The sintered photonic crystal of alumina formed a complete band gap at the terahertz region from 0.35 to 0.49 THz. Localized modes were obtained by introducing a point defect of air cubic cavity and a plane defect between twinned diamond structures, which were in good agreements with the simulation by TLM method. It is expected that these three dimensional photonic band gap structures can be applied to control terahertz waves.

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