Reliability modeling of Transport Systems: Influence of the Running-in Period of Life

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Abstract

Improving reliability in the context of transportation is of great importance. The running-in period allows material to increase its life duration and therefore its availability. This means the modelling of early failures, considering the specific distributions of failure time. Unlike the exponential distribution which is used for random failures, these distributions must have at least two parameters. Despite the fact that the log normal and normal distributions are frequently used to model the effects of aging, the Weibull distribution is probably the most universally used. With it, we can model the early and random failures as well as the effects of aging. The Weibull distribution (3 parameters) describes the situations in which some time $t_0$ must pass before a failure happens. It is equal to a two-parameter distribution with a right to a translation. This work consists of modelling the influence of running-in time over the duration of additional life.

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1. Introduction

The reliable assessments of mechanical systems are based on many parameters where the failure rates are the first considered. By default, databases are commonly used for reliability. For the most part, are collections of data [1] [2] and [3] and many others from the feedback experience for various sectors. Potential users of these are based on the fact that their materials are substantially similar and that the reliability of these databases can be transferred to their concerns. One can observe that the data of studied

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systems reliability are not homogeneous, as is sometimes suggested significant variations of the failure rates between bases. The causes are many: Materials have their own characteristics. Same type of system comes in a range of equipments whose reliability is different; operating conditions and operating environment vary between systems. Reliability of mechanical equipment is sensitive to loading, operating modes, stresses, failure modes considered, maintenance politicizes… These differences are highlighted between the sectors; to synthesize the data collected for each type of system often requires regrouping irrespective equipments to various intrinsic and extrinsic properties, regardless of characteristics. The use of these databases as input data of reliability assessments will therefore result in large uncertainties about the relevance of the results. The second point to be noted is that all the databases described above only provide constant failure rates. However, the mechanisms of degradation of mechanical components such as fatigue, vibration, la corrosion and other stresses creating wear phenomena, therefore the system ages. To this a running-in phase that usually causes failures in young systems can be added. In what follows, the running-in phase is to be modeled in order to highlight its importance in the total lifetime of the mechanism. The example cited in this study is the case of bearings that are virtually present in the majority of mechanical systems. Although their lifetime is relatively short compared to the entire mechanism in which are mounted, but their running-in phase provides a significant mechanical stability [4].

2. Failure rate base $\lambda(0)$

It has been seen earlier that the mechanical equipments rarely respond to a constant failure rate, synonymous with exponential probability distribution. Here, a model by the Weibull distribution with two parameters has been proposed. The failure rate is expressed as follows:

![Fig. 1.a: failure rate $\lambda_0(t)$ [5]](image1)

![Fig. 1.b: distribution law [5]](image2)

![Fig. 1.c: failure rate of a mechanical system [6]](image3)
\[ \lambda_0(t) = \frac{\beta}{\theta} \left( \frac{t}{\theta} \right)^{\beta - 1} \]  

(1)

With:
- \( \beta \) the shape parameter, unitless;
- \( \theta \) the scale parameter in units of time. Sometimes, expression (1) is found in a form that puts the parameter \( \lambda = \frac{1}{\theta} \.

This distribution is widespread in the reliability of mechanical systems as it allows to model three periods of system lifetime according to the parameter \( \beta \). Figures 1a, 1b and 1c, show respectively the different periods of lifetime, the corresponding behavior laws and the shape of the failure rates for mechanical systems.

- A running-in period, also known as \textit{infant mortality}, if \( \beta < 1 \). The failure rate is decreasing with time. Faults that appear in this first phase of life are typically due to faulty design or installation once the system started. Most of these failures can be avoided by test policies, before the introduction of equipment [7]. The running-in period may contribute substantially to the increase of the equipment lifetime. Some authors refer to the increase in wear after the running-in period [4] [8] [9] [10] [11].
- A phase called \textit{useful life}, if \( \beta \approx 1 \). The failure rate is then almost constant. Defects in removed equipment, the system is in its main phase of life. Failures that occur during this period are caused by random events independent of time and age of system.
- A phase of \textit{wear}, if \( \beta > 1 \). The failure rate is increasing with time. Stress, fatigue, corrosion etc. deteriorate the system, which increases the probability that a failure takes place during this period of time. The shape of the failure rate as represented during the three phases of lifetime, known as « bathtub curve » given in figures 1a, 1b and 1c. Databases typically provide only the failure rate of \textit{useful life}, assumed constant. Other distributions such as Gamma, Normalae, Log-Normale, Birnbaum-Saunders, inverse Gaussian and others may also be considered in the model.

To model the early failures, one must consider the specific distribution of failure times. Unlike the exponential distribution is used for random failures, these distributions must at least two parameters. Despite the fact that the normal distribution and normal log are frequently used to model the effects of aging, the Weibull distribution is probably the most universally used [12]. Using the latter, the early and random failures and also aging effects can be modeled.

Thus, the rate previously defined is used in situations where one has to deal with early failures or the aging effects. This can be illustrated by considering the effect of accumulated operating time \( T_0 \) over the probability that the entity can survive an additional time \( t \). Assuming that it is defined \( R(t|T_0) \) as the reliability of an entity that has operated during the time \( T_0 \), the following equation can be written as:

\[ R \left( \frac{t}{T_0} \right) = \frac{R(T_0+t)}{R(T_0)} \]  

(2)

From the equation \( R(t) = \exp \left[ -\int_0^t \lambda(t)dt \right] \)  

(3)

We obtain \( R \left( \frac{t}{T_0} \right) = \exp \left[ -\int_0^{T_0} \lambda(t)dt \right] \)  

(4)

Time \( T_0 \) can be interpreted as the time of the running-in phase before the system is placed in service. The concern is whether this time contributes to the improvement or deterioration of the system. To do this, equation (2) was derived with respect to time \( T_0 \):

\[ \frac{d}{dT_0} R \left( \frac{t}{T_0} \right) = \frac{\lambda(T_0) - \lambda(T_0 + t)R \left( \frac{t}{T_0} \right)}{T_0} \]  

(5)

So, if \( \lambda \) decreases with time [i.e. \( \lambda(T_0) > \lambda(T_0 + t) \)], then the system can be improved. Otherwise, is to be deteriorated. In the running-in phase, the failure rate is decreasing in general.
The lifetime of a rolling bearing can be divided into two main phases which will be studied here:

**The running-in phase:** Forming the first few tens of thousands of cycles of the rolling bearing lifetime, during which the contact geometry and/or roughness, and surface residual stresses are stabilizing.

**The life time phase** which comes after the running-in phase and can last several million cycles. The running-in phase is the first stage of the lifetime of a bearing. However, this phase is very short and extremely important to the future life span of the rolling bearing because it fixes the steady state in terms of the parts in contact, residual geometry and stresses which are determining factors in resisting the fatigue [4] of mechanical parts.

The reliability relationship of the running-in phase can be written as follows:

\[
R \left( \frac{t}{T_0} \right) = \frac{\exp \left[ -\frac{(t + T_0)^m}{\theta} \right]}{\exp \left[ -\frac{T_0^m}{\theta} \right]} \tag{6}
\]

By putting \( t=T \) and solving for \( T \) we obtain:

\[
T = \theta \left\{ \ln \left[ \frac{1}{R(t)} \right] + \left( \frac{t_0}{\theta} \right)^{\frac{1}{m}} \right\} - T_0 \tag{7}
\]

By modeling the running-in phase according to the expression (7), we evaluate the importance of this phase on the additional useful life to the studied system. The results presented below clearly confirm the benefits of the running-in phase. Furthermore, a large enough time scale and decreasing from 180 to 4 years has been considered in order to scan a larger number of systems operating within these limits based on a predicted reliability and a shape parameter \( \beta \) ranging from 0.5 to 3, that is to say running-in phase to the aging phase.

### 3. Results and discussion

Figures 2a, 2b, 2c, 2d, 2e and 2f show the evolution of additional time to the useful life of the system. Two periods are compared, the running-in phase with a \( \beta \) value of 0.5 (running-in phase) and 0.9 (beginning of the useful phase for a scale parameter \( \theta \) varying from 180 to 5 years with a reliability of 0.90. It can be noticed that for running-in phase when the time \( T_0=0 \) lifetime is approximately 24 months. The addition of one month running-in gives an extra time to the duration of life of 12 months (figure 2a). Figures 2b and 2e respectively express the variation of added time to the useful lifetime for two different time scales 50 years and 30 years. It can be noted that for \( \beta=0.9 \) added time to the life time is almost zero.

![Fig. 2. a : \( \theta=180 \) years](image)
Fig. 2.b:  $\theta=50$ years

Fig. 2.c:  $\theta=30$ years

Fig. 2.d:  $\theta=10$ years

Fig. 2.e:  $\theta=5$ years
Fig. 2.f: $\theta=2$ years

Figures 3a, 3b, and 3c express the time variation added to the useful life depending on the essential parameter $\beta$. It can be noticed, for a value of $\beta = 1$, the opposite effect of added time to the useful life is much more pronounced for values of $\beta = 3$. Figure 3c shows that as the lifetime becomes shorter, with a shape parameter $\beta > 3$ (phase of wear), it can be seen that the opposite effect is in good agreement with the logical behavior of repairable systems.

Fig. 3.a: $\beta=1$, $\theta=180$ years

Fig. 3.b: $\beta=3$, $\theta=180$ years
Fig. 3.c: $\beta = 3, \theta = 20$ years

Figures 4a, 4b and 4c compare the evolution of additional time to lifespan depending on the parameter $\beta$. It can therefore be noticed, that the additional time to the future lifespan (useful) are more important with the decrease of coefficient $\beta$ which is completely logical. When the scale parameter decreases (figure 4c), it can be noticed that the running-in phase is very narrow.

Fig. 4.a : $\beta = (0.3, 0.4, 0.5 \text{ and } 0.9), \theta = 10$ years

Fig. 4.b : $\beta = (1, 3, 0.5 \text{ and } 0.9), \theta = 10$ years
4. Conclusion

The improved behavior of mechanical systems in contact and especially bearings that are almost omnipresent in the majority of rotating mechanical systems is conditioned by the conditions of commissioning. If the running-in phase is properly applied, this will lead to an appreciated operating lifetime. For bearings, whose lifespan is very short compared to that of the entity in which are mounted, this phase is highly recommended because it creates mechanical stability between the parts in contact with surfaces generally have asperities (roughness) which disappear during running-in. This period also provides a high wear resistance to rotating parts and lowers significantly the preventive and systematic maintenance costs.

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