Field-Free Synthetic-Ferromagnet Spin Torque Oscillator

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We study the magnetization dynamics of spin valve structures with a free composite synthetic ferromagnet (SyF) that consists of two ferromagnetic layers coupled through a normal metal spacer. A ferromagnetically coupled SyF can be excited into dynamical precessional states by an applied current without external magnetic fields. We analytically determine the stability of these states in the space spanned by the current density and SyF interlayer exchange coupling. Numerical simulations confirm our analytical results.

The transfer of angular momentum between the magnetic layers of current-driven spin valves (spin-transfer torque) has not been so long ago predicted and experimentally confirmed. The implied efficient electrical control of magnetizations motivated the pursue of new research directions. When the current density exceeds a critical value, the spin-transfer torque can switch the magnetization to a different static configuration without the necessity of applied magnetic fields, which makes it attractive for next generation Magnetoresistive Random Access Memory (MRAM) application. Under an external magnetic field, the spin-transfer torque can also drive the magnetization into sustainable coherent oscillations spanning a wide frequency range from a few MHz to several hundred GHz. High frequency magnetic oscillations generate a coherent microwave voltage signal through the Giant Magnetoresistance (GMR) in metallic spin valves or through the Tunneling Magnetoresistance (TMR) in magnetic tunnel junctions (MTJs). This effect can be used in so-called spin-torque oscillators (STO), which has many advantages including wide tunability, very high modulation rates, compact device size, and high compatibility with standard CMOS processes. Thus STO is appealing for high frequency microwave applications including microwave emitters, modulators and detectors. However, the necessity of an applied magnetic field up to ~1 Tesla has greatly limited the potential of these STOs for microwave generation and wireless communication applications. Recently, various solutions have been proposed to enable zero-field operation, viz. STO with a perpendicularly magnetized fixed layer or spin valves with out-of-plane magnetized free layer. Magnetic vortex oscillators and wavy-torque STO by judicially choosing free and fixed layer materials with different spin diffusion lengths and a tilted magnetization of the fixed layer with respect to the film plane.

Recently, synthetic ferromagnets (SyFs) composed of two ferromagnetic layers separated by a very thin non-magnetic spacer have been used to replace the free layer of a spin valve or MTJ. SyF based spintronic devices have the advantage of higher thermal stability, smaller stray magnetic fields, faster switching speed and reduced threshold switching current as compared to single ferromagnetic free layers. Klein et al. predicted that an anti-ferromagnetically coupled SyF layer with uncompensated magnetization can generate microwave oscillations at zero applied magnetic field.

Here we predict that a ferromagnetically coupled SyF can also be driven into dynamical precessional states, which, however, are surrounded in parameter space by static canted states with non-collinear magnetizations. We use an analytical approach to determine the stability regimes of the SyF system and confirm results by numerical simulations.

We study a spin torque nanodevice with synthetic ferromagnetic free layers as shown in Fig. 1. The left ferromagnetic film forms the fixed polarizer with magnetization and the SyF consists of two ferromagnetic layers and of thickness with a paramagnetic spacer. The unit vectors describing the magnetization orientation are for FM, and for FM. For simplicity, we assume that the SyF layers...
are made of the same materials with identical saturation magnetization $M_s$. The exchange coupling strength reads $E_C = -JS\mathbf{m}_1 \cdot \mathbf{m}_2$, where $J$ and $S$ are the coupling energy per unit area and the cross section area of the sample, respectively. This corresponds to an effective coupling field $H_i^C = Jm_i/\mu_0 M_s$, where $i = 1, 2$ and $\mu_0$ is the vacuum magnetic susceptibility. $\mathbf{m}_1$ and $\mathbf{m}_2$ can be parallel or anti-parallel at zero applied field, corresponding to the non-local Ruderman-Kittel-Kasuya-Yoshida (RKKY) exchange ferromagnetic ($J > 0$) or antiferromagnetic ($J < 0$) coupling, respectively. The spacer between FM$_i$ and FM$_j$ is presumed thick enough that the RKKY coupling with the fixed layer is negligibly small. Although the dynamic dipolar coupling may be responsible for the apparent reduction of static magnetization or linewidth of the current-induced spin wave mode, it is estimated to be much smaller for our case compared to the shape anisotropy field and the other fields due to current-induced spin torque and interlayer exchange coupling and therefore disregarded.

Let $P_{0i}$ be the spin current polarization by $m_{0i}$ such that the spin current density in the two spacers are $P_{0j}$ and $P_{1j}$ with $j$ the electric current density. The corresponding spin-transfer torques on $\mathbf{m}_1$ and $\mathbf{m}_2$ are given by the projections:

\begin{align}
N_{\text{ST}1} &= \frac{\gamma \hbar}{2e\mu_0 M_s d_1} \mathbf{m}_1 \times [(P_{0} \mathbf{m}_0 - P_{1} \mathbf{m}_2) \times \mathbf{m}_1], \\
N_{\text{ST}2} &= \frac{\gamma \hbar}{2e\mu_0 M_s d_2} P_{1} \mathbf{m}_2 \times \mathbf{m}_1 \times \mathbf{m}_2,
\end{align}

with $\gamma$ the gyromagnetic ratio and $P_0$ ($P_1$) are in general functions of the angle $\theta = \angle(\mathbf{m}_0, \mathbf{m}_1)$ ($\angle(\mathbf{m}_1, \mathbf{m}_2)$).

Spin pumping causes enhanced damping in a ferromagnetic layer by emitting spin current into the adjacent non-magnetic layers. This emitted spin pumping current can exert a torque on the second layer. Disregarding the backflow and diffusion in the spacer layer, the torque density acting on $\mathbf{m}_i$ due to spin pumping from $\mathbf{m}_j$ can be written as

$$N_{\text{SPI}} = \beta \mathbf{m}_i \times \mathbf{m}_i - [(\beta \mathbf{m}_j \times \mathbf{m}_j) \cdot \mathbf{m}_i] \mathbf{m}_i$$

where $\beta$ is the effective enhanced damping due to spin pumping. It has been shown that Eq. (2) gives rise to a dynamic exchange interaction that can induce synchronization of the magnetization dynamics in two neighboring ferromagnetic layers even for wide spacers. In the results below we fully include the spin pumping. However, in contrast to multilayers excited by microwaves, we observe here only small corrections demonstrating the dominance of charge current-induced torques.

The dynamics is described by the coupled Landau-Lifshitz-Gilbert-Slonczewski (LLGS) equations:

$$\mathbf{m}_i = -\gamma \mathbf{m}_i \times \mathbf{H}_i + \alpha \mathbf{m}_i \times \dot{\mathbf{m}}_i - N_{\text{SPI}} - N_{\text{ST}i},$$

where $\alpha$ is the sum of the intrinsic Gilbert and the spin pumping induced damping. The effective magnetic fields $H_i$ consist of shape anisotropy and RKKY exchange coupling and can be written as

$$H_i = \frac{2K_s}{\mu_0 M_s} [\mathbf{m}_i \cdot \mathbf{e}_z] e_z + \frac{J \mathbf{m}_i}{\mu_0 M_s d_i}.$$  

For simplicity, we consider $d_1 = d_2 = d$ (equal magnetization) for the rest of the paper unless otherwise specified. We linearize Eq. (3) in the vicinity of four collinear equilibrium states, i.e. $\uparrow\uparrow, \uparrow\downarrow, \downarrow\uparrow, \downarrow\downarrow$, and assume $\mathbf{m}_i = \lambda_i \hat{e}_z + \mathbf{u}_i$ with $\lambda_i = \pm$ and $\mathbf{u}_i$ denoting the small transverse magnetization component. After the linearization and the Fourier transform $\mathbf{u}_i(t) = \int \tilde{\mathbf{u}}_i(\omega)e^{-i\omega t}d\omega/2\pi$, Eq. (3) becomes

$$\left(\dot{\tilde{\mathbf{u}}}_i + A\tilde{\mathbf{u}}_i + i\omega \mathbf{V}_i\right) = 0$$

with

$$A = \begin{pmatrix}
1 - i\alpha\lambda_1 & i\beta \lambda_2 \\
 i\beta \lambda_1 & 1 - i\alpha\lambda_1
\end{pmatrix},$$

$$\mathbf{V}_i = \frac{\alpha}{2\gamma} \begin{pmatrix}
\omega_0 (\lambda_1 0) + \omega_J (\lambda_2 -\lambda_1) \\
0 (\lambda_2 -\lambda_1) + \omega_J (\lambda_1 -\lambda_2)
\end{pmatrix},$$

with $\omega_0 = 2\gamma K_a/\mu_0 M_s$, $\omega_J = \gamma J/\mu_0 M_s d_i$, $\omega_J = \gamma J/\mu_0 M_s d_i$. The frequency of the normal modes are given by the eigenvalues of $\mathbf{W} = A^{-1} \mathbf{V}$, $\Omega_1$ and $\Omega_2$. When any of the $\Omega$ is positive, the system is unstable, implying that an infinitesimal perturbation will lead to magnetization dynamics with amplitudes that initially increase exponentially in time.

The above results allow us to calculate the stability regions for the $\uparrow\uparrow, \uparrow\downarrow, \downarrow\uparrow, \downarrow\downarrow$ phases in the space of typical experimental parameters: angle-independent $P_1 = P_2 = P = 0.5$, $d = 3$ nm, $K_a = 8 \times 10^4$ J/m$^3$, $J \sim 10^8$ A/cm$^2$ and $J \sim 1$ mJ/m$^2$. To analytically construct the stability diagram as shown in the top-left panel of Fig. (2a), we first calculate the eigenvalues for each given set of $[j, J]$ as given by Eq. (6). Then we determine whether any of the four collinear static states (different combinations of $[\lambda_1, \lambda_2]$) is stable or not. For example, both the imaginary part of the eigenvalues of $\uparrow\uparrow$ configuration $[\lambda_1 = +1, \lambda_2 = +1]$ are negative when $J \leq 0$. Therefore $\uparrow\uparrow$ is stable in the blue region. In this way, we quickly map the parameter space for any given set of $[j, J]$ and construct the entire stability diagram consisting of four collinear magnetization configurations. The spin torque drives the SyF to the parallel $\uparrow\uparrow$ configuration for negative currents $j$. For positive currents, the $\downarrow\uparrow$ configuration is preferred. These results can be understood from Eq. (1). In a small region the antiparallel $\uparrow\downarrow$ state exists for negative $J$ and small $j$ (i.e. in the vicinity of the negative vertical axis but not visible in the figure due to the scale). Although it seems that the $\downarrow\downarrow$ state also occupies

\[\text{(4)}\]
the fourth quadrant \( (j > 0, J < 0) \), this triangular region is hysteric, \textit{i.e.} \( \downarrow \downarrow \) and \( \uparrow \uparrow \) may both appear depending on the history.

Most importantly, there is a white/purple region in which none of the four static collinear states is stable, therefore it must be either in a dynamical STO or static canted state. To leading order of \( \alpha \), we find from Eq. (5) an approximate boundary for the white region:

\[
\begin{align}
\text{upper:} & \quad \omega J = \omega_f, \\
\text{lower:} & \quad \omega J = \sqrt{4\omega_0^2 + \omega_f^2 - 2\omega_0 + \alpha \frac{\omega_f^2}{\omega_J}},
\end{align}
\]

which is plotted as the black dashed lines in Fig. 2(a,b), matching the numerically obtained boundaries almost exactly. Eq. (7) is calculated from the eigenvalue analysis based on Eq. (3) with perturbation from the four static collinear states. This method is equivalent to that used by Bazaliy et al.\cite{Bazaliy2013}. A fully analytical solution for the boundary between STO and static canted phase turned out to be intractable due to the complexity of Eq. (5) for non-collinear states.

We now present numerical solutions of the LLGS Eq. (3) including damping, spin torque and RKKY coupling. We summarize the dynamics of the coupled \( \mathbf{m}_1 \) and \( \mathbf{m}_2 \) in Fig. 2(b), in which we confirm the phase boundaries in the analytical analysis in Fig. 2(a). In addition, we can now map the STO phase by the purple color. The rest of the white region consists of static canted states. In Fig. 2(c) we show the six different SyF configurations that may exist depending on the current and RKKY coupling strength. Point 5 corresponds to an STO state, in which both \( \mathbf{m}_{1,2} \) are undergoing large angle precessions, which result in a large magnetoresistance oscillations attractive for applications.

For the STO phase, we study the power spectrum of the magnetoresistance due to the magnetization oscillation of \( \mathbf{m}_{1,2} \), which is approximated by \( R(t) = R_0 + \Delta R_0 \mathbf{m}_0 \cdot \mathbf{m}_1 + \Delta R_2 \mathbf{m}_1 \cdot \mathbf{m}_2 \). Fig. 2 also shows the Fourier transform of \( \mathbf{m}_0 \cdot \mathbf{m}_1 \) (left) and \( \mathbf{m}_1 \cdot \mathbf{m}_2 \) (right) as a function of current density \( j \) at \( J = 0.25 \text{ mJ/m}^2 \) (corresponding to the black line in Fig. 2(b)). The clear higher order harmonic modes are evidence of the non-linearities in the STO dynamics. Fig. 3 also demonstrate that the oscillation frequency of the device can be continuously tuned by the current at zero applied magnetic field and thus potentially be utilized for nano-scale microwave applications. It should be noted that the frequency range can be further tuned by tens of GHz by adopting a larger \( K_u \) or taking into account the easy-plane anisotropy field (demagnetization field).

The STO phase studied in this work differs from that studied by Klein et al.\cite{Klein2013}. The STO phase found by Klein et al. arises only in an anti-ferromagnetically \( (J < 0) \) coupled uncompensated SyF \( (M_1 = M_2d_1S < M_2d_2S = M_2) \), in which the total magnetization for the SyF is opposite to that of \( \mathbf{m}_0 \). However, the STO phase found in our study appears in the ferromagnetically coupled SyF with \( J > 0 \) and does not require \( M_1 \neq M_2 \). Furthermore, we were not able to reproduced the STO phase found by Klein et al. for an uncompensated and antiparallel SyF. We checked the effect of an angular dependence of the prefactor \( P \) that take into account the effects of a spin accumulation. The boundaries of the white region will shift noticeably, but we find no qualitative changes. The differences with Ref. 39 might be due to other details.

\[ \begin{align}
\text{FIG. 2. (Color online) Dynamical phase diagram in the parameter space of currents and RKKY coupling strengths. (a) Phase diagram calculated analytically by Eq. (3), none of the four states \( \uparrow \uparrow, \uparrow \downarrow, \downarrow \uparrow, \downarrow \downarrow \) is stable in the white region. (b) Phase diagram calculated by numerically solving the LLGS Eq. (3). The purple are the STO phase, and the white one the canted state. (c) The time evolution of the polar angles \( \theta_{1,2} = \angle(\mathbf{m}_{1,2}, \mathbf{z}) \) at the six different points indicated in the phase diagram. In the third subfigure of (c), the solid and dashed lines correspond to different sets of initial conditions.}
\end{align} \]
in handling spin transport.

Finally, we note that our approach can be readily extended from bi-layer to multilayer systems in which each layer is exchange-coupled with its neighbouring layers (unpublished). This may provide a novel route to effectively synchronize a large network of spin torque oscillators.

In conclusion, we predict that the ferromagnetically coupled SyF can be driven into STO states without the need of applying magnetic fields. The resulting STO states display large angle precession, therefore generating a large power output. In addition to dynamical STO states, static canted states are also possible in the same structure at slightly different applied current densities. Our findings may guide the experimental effort towards the field-free STO for real applications.

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