Identification of Globular Cluster Stars in RAVE data II: Extended tidal debris around NGC 3201

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ABSTRACT

We report the identification of extended tidal debris potentially associated with the globular cluster NGC 3201, using the RAdial Velocity Experiment (RAVE) catalogue. We find the debris stars are located at a distance range of 1–7 kpc based on the forthcoming RAVE distance estimates. The derived space velocities and integrals of motion show interesting connections to NGC 3201, modulo uncertainties in the proper motions. Three stars, which are among the four most likely candidates for NGC 3201 tidal debris, are separated by 80° on the sky yet are well matched by the 12 Gyr, [Fe/H] = −1.5 isochrone appropriate for the cluster. This is the first time tidal debris around this cluster has been reported over such a large spatial extent, with implications for the cluster’s origin and dynamical evolution.

Key words: globular clusters: individual: NGC 3201 – Galaxy: kinematics and dynamics.

1 INTRODUCTION

Tidal tails or debris associated with globular clusters (GCs) are important substructures that carry significant information on the dynamical history of the clusters and their host galaxies. All Galactic GCs are expected to have lost mass through the escape of individual stars (e.g. Grillmair et al. 1995; Combes, Leon & Meylan 1999; Leon, Meylan & Combes 2000; Grillmair 2009; Jordi & Grebel 2010; Kunder et al. 2014; Fernández-Trincado et al. 2015). See also Baumgardt & Makino (2003) for a broad theoretical framework.

The most prominent example of mass-loss through individual stars is the GC Pal 5 with its associated tidal tails (e.g. Odenkirchen et al. 2001; Rockosi et al. 2002), a cluster that is currently undergoing disruption (Dehnen et al. 2004). While tidal tails are a direct sign of mass-loss, further evidence can be found in the cluster present day mass function (PDMF). Clusters showing a PDMF that is flat or inverted suggests that those objects have lost up to 90 percent of their initial mass (Webb & Leigh 2015). Note, however, that tails are not observed in all of these inverted PDMF clusters. Moreover, Küpper et al. (2010) found that the time variation of the tidal field need not lead to detectable overdensities within the tidal tails as suggested by Dehnen et al. (2004).

Using CN and CH as tracers of stars born in GCs, Martell & Grebel (2010) concluded that 17 percent of the present-day
stellar mass of the Galactic halo originated from dissolved GCs. Vesperini et al. (2010) used hydrodynamical simulations to estimate the fraction of the mass of the Galactic stellar halo composed of second-generation stars that originated in GCs. They found that the fraction is always < 8 per cent. There is evidence that the most luminous GCs in the Galaxy are the remnant nuclei of accreted dwarf galaxies (e.g. Sarajedini & Layden 1995; Bekki & Freeman 2003). Such cases could be identified by the presence of multiple populations and/or a spread in metallicity within the cluster and debris stars. Therefore, the metallicity spread could help to distinguish between a GC and a dwarf galaxy. Note that the origins of multiple populations in GCs are unclear to date, but they are not thought to be due to real age spreads (Gratton, Szened & Carretta 2004). In dwarf galaxies, however, the multiple populations reflect a true difference in stellar ages (Willman & Strader 2012). During the process of accreting dwarf galaxies, GCs that formed within dwarf galaxies also are accreted into the Galactic halo, e.g. the accretion of the Sagittarius dwarf galaxy, where several GCs within the dwarf galaxy are in the process of joining the Galactic GC population (Da Costa & Armandroff 1995; Law & Majewski 2010). Further, tidal tails are useful for constraining the global mass of the Galaxy and its luminosity. GC tidal tails can be some of the coldest and longest-lived substructures in the Milky Way halo (Murali & Dubinski 1999; Carlberg 2009). As stars in tidal tails are usually aligned with the orbit of the GC, their identification allows a better handle on modelling the cluster orbit, which in turn places constraints on the Galactic potential, barring any major disruption events such as interactions with molecular clouds.

In this work, we report the detection of potential extended tidal debris associated with NGC 3201, a low-mass halo GC. NGC 3201 has an extreme heliocentric radial velocity (RV) of 494 km s\(^{-1}\) and a highly retrograde orbit (Casetti-Dinescu et al. 2007), suggesting an extra-Galactic origin; an additional argument is its location on the ‘dwarf accretion’ arm in the age-metallicity diagram of Leaman, VandenBerg & Mendel (2013). Despite the large metallicity spread of at least 0.4 dex reported earlier by Gonzalez & Wallerstein (1998) and Simmerer et al. (2013), the latest studies suggest that a metallicity spread within the cluster members is unlikely (Mucciarelli et al. 2015).

This paper is organized as follows. In Section 2, we describe the sample selection. The proper motion diagram and colour-magnitude analysis are described in Section 3. In Sections 4 and 5, we explore the space velocities, the integrals of motion and the metallicity distribution function of the tidal debris candidates. Finally, we present our conclusions in Section 6.

2 SAMPLE SELECTION

The RAidal Velocity Experiment (RAVE) provides precise radial velocities and stellar atmosphere parameters for 483 849 objects using medium-resolution spectra (\(R = 7500\)) in the Ca ii-triplet region (8410–8795 Å; Steinmetz et al. 2006). Using the fourth data release of the RAVE catalogue, RAVE–DR4 (Kordopatis et al. 2013), we apply the selection criteria developed in Anguiano et al. (2015) for data quality, where stars with an S/N > 10, cross-correlation coefficient R larger than five and classification flag set to ‘n’ were selected. From this sample, we further selected giant stars within the range 3600 < \(T_{\text{eff}}\) < 6000 K, log \(g\) < 3.5 and [M/H] < +0.0 dex. Most of the selected spectra have an S/N > 20. These stars have a typical error in radial velocity \(\lesssim 2\) km s\(^{-1}\). For this selection, we explore the radial velocity in the Galactic Standard of Rest frame (\(v_{\text{GSR}}\)) using the following formulae:

\[
v_{\text{GSR}} = v_{\text{LSR}} + 9\cos(l)\cos(b) + 12\sin(l)\cos(b) + 7\sin(b)\quad (1)
\]

\[
v_{\text{GSR}} = v + 220\sin(l)\cos(b),\quad (2)
\]

where LSR is the Local Standard of Rest, BSR is the Barycentric Standard of Rest\(^1\) and \(l\) and \(b\) are Galactic longitude and latitude, respectively. Numerical coefficients are in km s\(^{-1}\), where the coefficients in equation (1) are the adopted components of the solar velocity with respect to the LSR (Mihalas & Binney 1981; Piskunov et al. 2006), and the co-efficient in equation (2) is the adopted Galactic rotational velocity (Binney & Tremaine 2008). The resulting \(v_{\text{GSR}}\) was normalized by dividing by \(\cos(b)\). This normalization results in a ‘planar RV’ (i.e. the observed RV on the Galactic equator), which projects the velocities of the disc stars into a more compact distribution, facilitating the easier detection of outlier streams from the bulk motion of the disc stars.

Fig. 1 shows \(v_{\text{GSR}}/\cos(b)\) as a function of Galactic longitude and \(v_{\text{GSR}}\) as a function of latitude around NGC 3201, where background stars are shown in black dots, and in red symbols we highlight the location of NGC 3201 and candidates of tidal debris. Stars with very high RVs are relatively rare (Hawkins et al. 2015). We selected candidates of tidal debris by searching around a locus in \(v_{\text{GSR}}/\cos(b)\). Of these, 12 members within the tidal radius of NGC 3201 were reported in Anguiano et al. (2015) shown in red triangles, and two stars outside the tidal radius were reported in Kunder et al. (2014), shown in orange triangles. Here, we identify an additional nine candidates further to those already reported. We use open squares to represent the stars close to \(l = 276^\circ\), red dots to represent the candidates closer to the cluster and open circles to represent the two stars around \(l = 278^\circ\). The black dots are the other stars in the RAVE–DR4 sample that are not related to the cluster or stream. The potential tidal debris is well collimated ranging from \(\sim 70^\circ\) to \(+40^\circ\) in Galactic latitude, in a longitude width of \(4^\circ\). Table 1 lists all the stars analysed in this study.

3 PROPER MOTIONS, COLOUR–MAGNITUDE AND METALLICITY DISTRIBUTIONS

3.1 Colour–Magnitude Diagram

We use 2MASS bands J and K, (Skrutskie et al. 2006) to explore the photometric properties of the candidate tidal debris. From UCAC4 (Zacharias et al. 2013) we selected targets within \(0.3\) centred in NGC 3201. We chose 0.3 around the cluster in order to sample the region of sky around the cluster, including cluster members as well as a field sample in the direction of the cluster. Fig. 2 shows the RA and proper motion distribution for the selected field. The RA distribution in the left-hand panel of Fig. 2 shows the cluster stars can be identified to be within 0.05, after which the number density sharply drops, shown in vertical dashed lines. In order to further separate the cluster and background stars we compare the PM distribution against the PM distribution of another 0.3 field well outside the cluster. This background-only field, located at RA: 10:37:37, DEC: −46:54:45, and its PM distribution is plotted with a dashed line in the right-hand panel of Fig. 2. The solid black line

\(^1\) Here, we make use of the heliocentric radial velocities provided by RAVE. The difference between barycentric and heliocentric velocities is negligible for our purposes.
To build the CMD of NGC 3201, we selected stars that lie within a Gaussian of a FWHM of 3.2 mas highlights the likely cluster stars. A clear peak is seen in this field that represent the cluster stars. The red Gaussian in the PM distribution as well as those that lie inside the red Gaussian in the PM distribution. Stars that satisfy both these criteria are plotted as black filled circles in Fig. 3. All other stars within the 0.3 field are plotted as smaller grey dots. The candidates of the tidal debris are overplotted and numbered as per Fig. 1 and Table 1. The reddening towards NGC 3201 is $E(B-V) = 0.24$ mag (Harris 1996). From the tabulated extinction law table in Mathis (1990) we use $A(J)/A(V) = 0.282$.

![Figure 1. Radial velocity distribution in the GSR centroid at the position of NGC 3201, in the Galactic longitude range $275^\circ < l < 279^\circ$ (top panel) and in the latitude range $-90^\circ < b < 75^\circ$ (bottom panel). The top panel shows the line-of-sight velocity projected to the disc plane by a cos $b$ normalization while the bottom shows $v_{\text{GSR}}$. The numbered red open squares, open circles and red dots are the candidates of the extended tidal stream potentially associated with NGC 3201. Red and orange triangles are cluster members previously identified in Kunder et al. (2014) and Anguiano et al. (2015).](image-url)
Figure 2. Left: Right Ascension (RA) distribution for stars within a radius of 0.3 centred at NGC 3201. As expected, the peak of the distribution represents the cluster. The vertical dashed lines indicate where the number density drops, at 0.05 from the cluster centre. Right: the proper motion distribution in RA for the 0.3 field centred at NGC 3201 (solid line). The dashed line shows the proper motion distribution for a background-only field of 0.3 radius located away from the cluster. The red Gaussian distribution with a FWHM of 3.2 mas highlight the stars with a proper motion associated with NGC 3201.

Figure 3. Colour–magnitude diagram using the 2MASS $J$ and $K_s$ bands for members of NGC 3201 that satisfy the proper motion selection (filled circles), possible background stars within 0.3 of the cluster centre (grey dots) and the tidal debris candidates (red symbols as in Fig. 1). In green, blue and brown a Padova isochrone of the metallicity and age reported for NGC 3201 is plotted, shifted to distances of 2, 4.9, 6 kpc, respectively, and corrected for extinction. Hence $E(J - K_s)$ will be of the order of $\sim 0.07$ mag which does not affect the CMD significantly. Therefore, we do not apply any reddening corrections.

The isochrones in Fig. 3 were selected from Girardi et al. (2000) for [Fe/H] = −1.5 and age = 12 Gyr to match the metallicity and age reported for this cluster (Harris 1996; Marín-Franch et al. 2009). The Red Giant Branch (RGB) of NGC 3201 appears clearly in the CMD. We observed that most of the debris stars follow the RGB. The candidates are in good agreement with the selected isochrones of cluster age and metallicity, with any deviation from the nominal RGB depending on the distance from the cluster (see Section 4).

3.2 Proper motion diagram

We examine the proper motions of the tidal debris candidate using UCAC4. Fig. 4 shows the proper motion diagram for NGC 3201 cluster and debris stars selected for analysis as described in Section 2. The dashed lines show the nominal proper motion values for NGC 3201 at $\mu_\alpha \cos(\delta) = 5.28 \pm 0.32$ mas yr$^{-1}$, $\mu_\delta = -0.98 \pm 0.33$ mas yr$^{-1}$ (Casentini-Dinescu et al. 2007). We do not expect the proper motions to be the same for all stars in an extended tidal stream. For debris stars that lie in the same part of the sky as NGC 3201 we can expect similar proper motions as the GC itself, however, that will not hold for stream stars moving on the same orbit but located in a very different direction from NGC 3201. There are
three stars with high proper motions lying inside the tidal radius of the cluster and with a similar RV reported for NGC 3201 ($\mu_3 = -47.4, -18.2$ and $31.1$ mas yr$^{-1}$, respectively). The spread in proper motions for stars inside the tidal radius of NGC 3201 is likely due to larger uncertainties in crowded fields.

### 3.3 Metallicity distribution function

We also explore the RAVE-DR4 metallicities. Conservatively the metallicities are accurate to $\sim 0.2$ dex. We find the potential tidal debris (not including the cluster stars at $l = 277.2$ depicted in red triangles in Fig. 1) to range in metallicity from $-1.2$ to $-1.9$ dex, with the metallicity distribution function (MDF) peak around $-1.7$ dex. The black line in Fig. 5 shows the cumulative fraction for cluster members identified in RAVE by Anguiano et al. (2015), the dashed red line the fraction for the debris candidates and the grey-coloured line a back/foreground field around the cluster. A KS-test shows that the maximum difference in cumulative fraction is $D = 0.2$. Given the limited accuracy of the RAVE low-resolution spectra and small number statistics of this sample, it is difficult to assess if the spread in metallicity seen in the MDF is real.

### 4 SPACE VELOCITIES AND INTEGRALS OF MOTION SPACE

#### 4.1 Distances and space velocities

Velocities in a Cartesian Galactic system in the direction of the Galactic Centre and rotation at the Sun were obtained following the method developed by Johnson & Soderblom (1987). The velocities are defined in a right-handed Galactic system with $U$ pointing towards the Galactic Centre, $V$ in the direction of rotation, and $W$ towards the north Galactic pole. We used the new distances derived by Binney et al. (2014) for the forthcoming 5th Data Release (Kunder/Steinmetz private communication). For nine stars of our sample there are no RAVE distances available. As nine of these stars have Galactic coordinates close to NGC 3201, we use a simple reduced proper motion analysis to estimate their distances. We have the distance modulus

$$
\mu_J = J - H_J + 5 \log v_T - 3.379,
$$

where $v_T$ is the tangential velocity. We use the $v_T$ of NGC 3201 ($v_T = 124$ km s$^{-1}$) to compute the stellar distances for the nine stars that have Galactic coordinates similar to NGC 3201 and also similar RV. A change in the cluster distance of 1 kpc gives a variation in $v_T$ of $22$ km s$^{-1}$. We use this value to compute the errors in the distances. We also perform a reddening correction in the $J$ band using $A(J) = 0.216$ (Mathis 1990). The distances derived via the reduced proper motion analysis are consistent with the distances derived by Binney et al. (2014), where the mean difference is $1.7 \pm 0.8$ kpc for the five stars in common. In both cases, we find the tidal debris candidates are mostly located at distances ranging from 1 to 7 kpc with a peak around 4 kpc. The reported distance for NGC 3201 is $4.9 \pm 0.3$ kpc (Harris 1996). Fig. 6 shows the locations of the cluster and debris stars in the $U$, $V$ and $W$ plane.

The cluster members clump together in the phase space, $V (-460$ km s$^{-1}$), but show a spread of $\sim 200$ km s$^{-1}$ in the $U$ and $W$ velocities. This is most likely due to uncertainties in the proper
Figure 6. $U$, $V$, $W$ diagrams for the cluster and tidal debris candidates (symbols are as in Fig. 1). The grey area shows all the possible orbits computed using the mean values in RV, proper motions and DR5 distances reported for cluster members (red triangles) and $1\sigma$ variations. The green line is the orbit computed using the nominal RV, proper motion and distance values reported for NGC 3201 in the literature, $d = 4.9$ kpc and $\mu_{\alpha}\cos(\delta) = 5.28 \pm 0.32$ mas yr$^{-1}$, $\mu_{\delta} = -0.98 \pm 0.33$ mas yr$^{-1}$ (Harris 1996; Casertti-Dinescu et al. 2007).

motion (see also Anguiano et al. 2015), and therefore although the phase space can help decipher space velocity correlations within the tidal debris candidates, we caution against imposing a strict criteria in the $U$, $V$, $W$ plane to select tidal debris members. These objects reported in Kunder et al. (2014); Anguiano et al. (2015) are highlighted as red/orange triangles. The debris candidates have velocities ranging from $+120$ to $-180$ km s$^{-1}$ in $U$, while in the $V$ component they range from $-500$ to $-100$ km s$^{-1}$ and in $W$ we find values from $-220$ to $+250$ km s$^{-1}$. In the $U$–$V$ plane, the extended candidates appear to form an arc-like structure going from negative to positive values in $U$, while the $V$ velocity approaches the velocity of the cluster members. In the $V$–$W$ plane, is clear that even the member stars show a spread in $W$ velocity. In principle, stars inside a GC tidal radius should follow similar velocities. For the stars inside the tidal radius we re-computed the velocities using a nominal distance for these stars of 4.9 kpc. We found that the spread is even larger, suggesting problems with proper motions in crowded fields. We used GalPy (Bovy 2015) to calculate orbits backward in time over 6 Gyr. The grey area in Fig. 6 shows all the possible orbits computed using the mean values in RV, proper motions and RAVE-DR5 distances reported for cluster members (red triangles) and $1\sigma$ variations. We found a large spread in orbits. In the $U$–$V$ plane most of the tidal debris candidates are inside the area drawn by the orbits while in the $V$–$W$ plane, five tidal debris stars are within the region of the orbits, and three candidates with negative $W$ values lie close to (but not inside) the regions predicted by the orbits.

4.2 Angular momentum

Fig. 7 shows the $(J, J_z)$ space for the cluster and debris stars associated with NGC 3201. To propagate the non-independent random errors in the angular momentum we used a Monte Carlo evaluation taking into account the uncertainties in distances and space velocities. If these are conserved quantities, the debris candidates would share the same orbital plane. In an axisymmetric potential, $J_z$ should be a constant value for the tidal debris candidates when
and 7. These same stars also match the isochrone of NGC 3201's area. Note that in our adopted right-handed convention, σ within 2σ99 per cent confidence limit. We found four debris candidates have similar angular momentum values to the cluster to within the errors. One large square, one large circle and two dots (see Fig. 7) are within 2σ area. Note that in our adopted right-handed convention, positive Jz values represent a retrograde orbit. In this framework a typical Milky Way population will have negative Jz value and will lie on the left-hand side of Fig. 7.

5 CONCLUSIONS
Exploring the radial velocity in the Galactic Standard of Rest frame (vGSR) in the RAVE-DR4 catalogue we detected extended tidal debris which may be associated with the halo GC, NGC 3201. Due to the extended nature of the debris and the resulting projection effects, traditional membership indicators such as positions on the CMD or proper motions are not applicable. Therefore, verifying the membership of the tidal debris is not trivial.

The space velocities and orbital motions show interesting features, the interpretation of which is however impacted by uncertainties in proper motions and distances. If we enforce that tidal debris from NGC 3201 should share common J, Jz and should lie inside the predicted orbits in U, V, W, then we have four candidates, noted as a large square, large circle and two small dot symbols in Figs 6 and 7. These same stars also match the isochrone of NGC 3201’s age and metallicity displaced by a distance corresponding to 2 kpc (see Fig. 3). We highlight that these three stars are located at −12°, +21° and −62° angular extent on the sky from the cluster centre, together spanning 80° across the sky.

The confirmation of tidal debris around NGC 3201 could help to understand two-body interactions in the cluster and evaporation processes; it would also be a tell-tale sign of its origins, currently speculated to be extra-Galactic in nature due to its high radial velocity and retrograde orbit. No other tidal debris of such a large spatial extent has been reported around this cluster to date. The presented sample is limited in size to reliably calculate orbits and subsequent implications on the Galactic potential. However, the brightness of the tidal debris candidates makes a detailed follow-up chemical abundance analysis via high-resolution spectroscopy relatively straight-forward. Further exploration of tidal debris around NGC 3201 is encouraged, in particular, a search for lower-mass stars, which although fainter, have been shown to preferentially reside in tidal tails (e.g. Combes et al. 1999; Koch et al. 2004).

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