CTRL: Clustering Training Losses for Label Error Detection
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Abstract—In supervised machine learning, use of correct labels is extremely important to ensure high accuracy. Unfortunately, most datasets contain corrupted labels. Machine learning models trained on such datasets do not generalize well. Thus, detecting the label errors can significantly increase their efficacy. We propose a novel framework, called CTRL (Clustering TRaining Losses for label error detection), to detect label errors in multiclass datasets. It detects label errors in two steps based on the observation that models learn clean and noisy labels in different ways. First, we train a neural network (NN) using the noisy training dataset and obtain the loss curve for each sample. Then, we apply clustering algorithms to the training losses to group samples into two categories: cleanly labeled and noisily labeled. After label error detection, we remove samples with noisy labels and retrain the model. Our experimental results demonstrate state-of-the-art error detection accuracy on both image and tabular datasets under labeling noise. We also use a theoretical analysis to provide insights into why CTRL performs so well.

Impact Statement—Having a high-quality dataset is crucial for classification tasks, but a common problem is that many datasets have inaccuracies in their labeling. This can negatively impact the performance of machine learning models when applied to new, unseen samples. To address this issue, we present a label error detection algorithm that can filter out samples with corrupted labels. We found that machine learning models trained on cleaned data can achieve a balanced-class accuracy increase of over 10% when the noise rate is approximately 20%. This algorithm can identify and clean any classification dataset that may potentially have label errors.

Index Terms—Label error, memorization effects, neural networks (NNs), noisy labels, robust learning.

I. INTRODUCTION

NEURAL networks (NNs) have demonstrated success in numerous classification applications. Large and high-quality datasets are essential for the success of NN training. In general, it takes a lot of effort to label a large dataset manually. This process is also error-prone. Sometimes, it is not even feasible. Even well-known human-annotated datasets have been found to have significant labeling errors, e.g., ImageNet [1] is known to have close to 6% labeling error in its validation set [2]. Labels that are different from their true class are said to be noisy, else clean. In practice, each data instance belongs to one or multiple hidden true classes and we are only provided with observed labels that may potentially be erroneous. In fact, many popular datasets are not very clean [2]. It is also known that deep NNs can easily fit random labels. Models overfitted on bad training data have poor predictive power on clean test sets [3], [4].

Deep learning models also display memorization effects. They first memorize samples with clean labels (also called “early learning”) and then start adapting to samples with noisy labels after sufficient epochs of training. Large-capacity models can eventually memorize all samples. This phenomenon is independent of the optimizations used during training or the NN architectures employed [3]. Before overfitting, when all samples have close to zero losses, clean and noisy labels result in different loss curves due to the difference in how learning progresses for each type. This is exploited in many label error detection methods [5]. MentorNet [6] monitors the learning process and provides a curriculum to reweight samples. O2U-Net [7] finds label errors by sorting the average training loss of all samples. Wang et al. [8] detect label errors by classifying the loss curves. Arazo et al. [9] model loss distribution in every epoch to infer a sample’s probability of being wrongly annotated. Xia et al. [10] prevent NNs from overfitting bad samples through early stopping. Forouzesh et al. [11] propose a metric named susceptibility to assess the ability of NNs to memorize noisy labels. Early learning is theoretically analyzed in [12], [13].

Some methods demonstrate success against noisy labels by training NNs with selected samples [5]. Confident learning (CL) [14] and O2U-Net [7] train models over two rounds: first, they train models on the noisy dataset to detect errors, then detect and remove samples with wrong labels, and finally retrain the model on the clean data. Co-teaching [15] and Co-teaching+ [16] sort sample loss and perform dynamic sample selection during training. Some methods change labels and losses. For example, mixup [17] smooths both samples and labels through convex combinations of pairs of training instances.

In this article, we present an effective framework, called CTRL, to detect noisy labels. It relies on the observation that training progresses differently for clean and noisy labels.

CTRL is open-source: https://github.com/chang-yue/ctrl.
We apply clustering algorithms to loss curves to classify labels as either clean or noisy. We propose a metric for selecting clustering parameters, which provides flexibility when choosing the number of clusters and cluster number cutoffs. The metric also enables selection of different sensitivity levels for label error detection through windowing and majority voting. The main contributions of this work are as follows.

1) We introduce a label error detection method that finds noisy labels of samples by clustering their training loss trajectories.
2) After label error detection, we present label cleaning methods to enable retraining of the model on the cleaned dataset.
3) We verify the proposed method on popular benchmark datasets under both real-world and simulated noise; our method achieves state-of-the-art label error detection accuracy and comparable model classification accuracy to prior state of the art.
4) To enable better understanding of the mechanism behind the method, we theoretically analyze a binary classification problem to demonstrate that the presence of a training loss gap between clean and noisy labels is highly probable.

The article is organized as follows. We present related work in Section II. We describe the methodology in Section III. We present experimental results in Section IV. We conclude in Section V, mentioning future directions.

II. RELATED WORK

In this section, we discuss prior work on training NNs with noisy labels as well as background on label noise.

A. Training NNs With Noisy Labels

There are two main approaches to training NNs with noisy labels: (i) train directly in the presence of noisy labels and (ii) clean the dataset first and then train (also called sample selection). To train NNs in the presence of label errors, some works use noise-robust loss functions [18], [19], [20], [21], [22], some estimate noise transition rates first and then adjust outputs [23], [24], [25], [26], [27], [28], some weight samples non-uniformly [6], [29], [30], [31], and some update losses or labels [9], [17], [32], [33]. Other works demonstrate the effectiveness of removing label errors prior to model training [7], [14], [34].

Many works propose methods based on early learning, either implicit or explicit. Co-teaching [15] applies implicit sample selection during training. It trains two NNs simultaneously, and in every mini-batch, each NN selects a fraction of samples with small training losses and feeds them to its peer network as the batch training instances. The selection rate is large at the beginning (i.e., 1) and gradually decreases to 1 − τ, where τ depends on the estimated noise rate and the teaching scheduler. The intuitions behind Co-teaching are twofold. First, samples that have smaller losses are more likely to be clean; hence, each NN only selects the subset with small losses. Second, NN overfitting is more likely in later training stages; hence, Co-teaching feeds fewer samples to NNs in the end relative to the beginning. O2U-Net [7] explicitly selects noisy labels based on the average training loss of the samples. It calculates the mean training loss of each sample and sorts all samples by these losses. Moreover, to better differentiate noisy labels from clean ones, it uses cyclic learning rates. However, when the noise level is not high, for example, less than 20%, the average loss distribution is not obviously bimodal; it becomes more like a long tail with clean labels plus a much smaller shifted and reversed long tail with noisy labels. O2U-Net does not determine the cutoff between types of labels on its own and requires users to input the noise level first.

Wang et al. [8] detect label errors by recording and clustering sample loss curves. CTRL also finds label errors by clustering training losses. However, we add significant flexibility to the detection algorithm by enabling more parameter choices, a windowing technique, and a metric to select the best clustering parameters. We also provide experimental validation using both image and tabular datasets and show state-of-the-art performance. Jiang et al. [35] treat the loss curve of each sample as an additional attribute and then use an NN to reweight the samples. They do not explicitly filter out noise. Our method takes the full training trajectory as a feature of each sample and can automatically and explicitly detect errors. Self-filtering [36] leverages variability in noisy examples from past predictions to filter them. It introduces a module called memory bank that retains past predictions for each sample and updates them dynamically to aid selections for the next learning cycle. They also use a regularization term to penalize the overconfident outputs of the network to reduce sample selection bias. Our method, on the other hand, emphasizes simplicity and efficiency by solely focusing on the loss history. Liu et al. [12] theoretically analyze early learning under simplified settings and propose a regularization scheme to control memorization. Cheng et al. [37] provide a theoretical analysis of the memorization effect in relation to model capacity and suggest a representation-based regularizer to mitigate this effect. Dynamic instance-specific selection and correction (DISC) [38] is a method that employs a two-view-based backbone to derive confidence levels for individual image samples. It then implements a dynamic threshold approach, based on the historical memorization strength of each instance, to identify and correct data with noisy labels. Patel et al. [39] introduce an adaptive strategy for sample selection based on the posterior probability statistics of mini-batches. Some methods tackle NN memorization by stopping training earlier, after the NN learns clean data instances, but before it starts fitting on too many noisy data instances [10], [13], [40]. Li et al. [41] explore the influence of network structure on its resilience to inaccuracies in labels. They show that a network more closely aligned with the desired function is likely to produce more accurate predictive models.

Mixup [17] reduces overfitting of noisy samples by smoothing the labels. It convexly combines and feeds pairs of samples and their labels to an NN. This decreases the effect of noisy labels because they no longer appear in a one-hot manner during training. Instead, they only take a portion of each sample-label pair. However, corrupted labels are still involved in NN training. CL [14] is a recent method based on cleaning the dataset first. It has state-of-the-art label error detection accuracy. CL first
breaks the datasets into folds and then trains and tests models using cross-validation. Based on the cross-validated probability predictions of the trained model on samples and their potentially noisy labels, CL counts, ranks, and prunes samples by obtaining a confusion-like matrix and estimating the joint distribution between observed and hidden labels, taking class-dependent confidence of the model into consideration. INCV [34] is a similar prior method that finds error annotations iteratively with increasing computation cost, whereas BBSE [42] assumes a less general form of label noise. We compare the performance of Co-teaching, mixup, CL, and CTRL in Section IV.

B. Label Noise

There are different types of noise. Some are modeled by a $|C| \times |C|$ noise transition matrix $T$, where $|C|$ denotes the number of classes. In this matrix, $T(i, j)$ represents the probability of a sample labeled as class $i$ given that its actual hidden class is $j$. Two properties describe the noise transition matrix. The first is noise level, which is the sum of all the off-diagonal entries divided by the number of classes. The second is sparsity level, which is the number of zero entries divided by the number of off-diagonal entries. In the case of symmetric noise, entries have the same value on the diagonal and a uniform probability off-diagonal. Asymmetric noise imposes fewer constraints. Hence, the transition probabilities need not be symmetric as above. In semantic noise, each instance has its own noise transition matrix. There is also open noise, which occurs when the ground-truth label set is different from the observed set. We test our method against both symmetric and asymmetric noise.

III. METHODOLOGY

In this section, we describe our methodology in detail.

Fig. 1 shows an overview of our methodology. First, we use a noise generator to create noisy labels if the dataset is originally clean. The input to the noise generator is the noise rate and the sparsity level of the noise transition matrix. We do not inject noise if the dataset already contains real-world noise. We then train a model using the noisy data and record the training losses. After that, we pass the model and loss matrix to our label cleaning algorithm, which outputs a binary mask (1 indicates clean and 0 noisy) and the cleaned training data. Finally, we retrain the model on the cleaned data and obtain its test accuracy. Algorithm 1 presents the mask computation process of CTRL.

The inputs are the matrix of training sample loss curves $L$, the provided labels $\tilde{y}$ which are potentially noisy, the number of samples $n$, and the set of label classes $C$. We first clamp any outliers in the loss matrix and smooth the loss curve for each sample by a mean filter. We then split $L$ into equal-length intervals by epoch number. After that, we further break the loss matrix by the provided label class and run the clustering algorithm for each class of samples. Lines 6–11 show the core clustering algorithm that classifies the samples based on their loss trajectories. We group the samples into $k$ clusters and assign $s$ clusters with larger areas under the loss curve as noisy. $k$ and $s$ are input parameters. In every window, we have a mask value for each sample. Finally, we sum up the mask scores across windows and classify a sample as noisy if it is marked as noisy in enough windows.

A. Loss Trajectories

During training, we record the loss of each data sample in every epoch. This results in a $|\text{samples}| \times |\text{epochs}|$ loss matrix $L$.

$$L := \begin{pmatrix}
    l_{1,1} & l_{1,2} & l_{1,3} & \ldots & l_{1,e} \\
    l_{2,1} & l_{2,2} & l_{2,3} & \ldots & l_{2,e} \\
    \vdots & \vdots & \vdots & \ddots & \vdots \\
    l_{n,1} & l_{n,2} & l_{n,3} & \ldots & l_{n,e}
\end{pmatrix}_{|\text{samples}| \times |\text{epochs}|}.$$

Based on the observation that clean and noisy samples have different loss curves, we apply a clustering algorithm to the loss curves to group labels into two classes. Fig. 2 shows an example of the average training losses of different label types on the well-known CIFAR-100 image dataset [43], with a 17% noise level and 60% sparsity level. The average loss gap between clean and noisy labels during most of the training is quite evident. The decreasing blue curve indicates that the NN consistently
Algorithm 1 Mask Computation

Input: loss matrix $L$, noisy label $\tilde{y}$, number of samples $n$, label class set $C$

Parameter: moving average size $a$, number of clusters $k$, number of selected clusters $s$, number of windows $w$, window threshold $t$

Output: mask $m$

1: Pre-processing: clamp $L$ by $2 \cdot \log |C|$; smooth each row of $L$ by the moving average size $a$.
2: Initialization: initialize clean votes $V \in \mathbb{R}^{n \times w}$ to 1; initialize mask $m \in \mathbb{R}^n$ to 0.
3: for $w_i = 0, 1, ..., w - 1$ do
4: compute window interval $(w_{start}, w_{end})$.
5: for $c$ in $C$ do
6: $p \leftarrow L [\tilde{y} = c, w_{start} : w_{end}]$
7: km_labels, km_centers $\leftarrow$ Kmeans $(p, k)$.
8: selected_ids $\leftarrow$ select Kmeans center ids with top sum.
9: for $j$ in selected_ids do
10: $V [\tilde{y} = c \land km\_labels = j, w_i] \leftarrow 0.$
11: end for
12: end for
13: end for
14: $v \leftarrow \text{sum } V$ along windows.
15: $m [v \geq t] \leftarrow 1.$
16: return $m$

CIFAR-100, 17% noise and 60% sparsity

Fig. 3. Average training losses for 10 randomly selected classes (based on noisy labels) from CIFAR-100, with 17% noise and 60% sparsity.

learns from clean samples. However, it does not learn well from the noisy samples initially, as demonstrated by the average losses staying roughly constant for a long time. As the loss gap increases, the gradient caused by noisy labels starts playing a more important role, and the model also starts learning from them. It eventually learns from every sample. We found similar gaps in all datasets we experimented with.

Another observation we make is that the loss curves are class-dependent. Fig. 3 shows the loss curves for 10 randomly selected classes (based on the noisy labels) from the same CIFAR-100 experiment described above. The losses are based on the provided labels, which are noisy. The class dependency phenomenon is more evident with ground-truth labels, i.e., with a clean dataset. Still, dividing samples based on their labeled class can improve label error detection accuracy, especially when the noise rate is not too high (e.g., less than 20%). We run the clustering algorithm on each class separately.

Although the average loss curves in Fig. 2 appear reasonably smooth, at the data sample level, they have a large variance. For example, Fig. 3 already shows much more fluctuations in the class-based loss curves than in the all-class averages. To smooth out the loss curves for each sample, we clamp losses to a threshold of $2 \cdot \log |C|$ (about two times the expected cross-entropy loss of a randomly initialized NN) and compute the moving averages with a window size of 5. In practice, we found that the effects of different loss thresholds and moving average window sizes are small.

The basic trends on loss curves are stable. Due to the fact that each point on the smoothed loss curve contains information from multiple epochs, we also tried using only a subset of the loss matrix for label error detection. We tested three sampling methods at various subsampling ratios. We sampled uniformly, sampled the middle numbers of epochs, or sampled epochs with high intra-epoch loss variances. We found that relative to the use of the full loss matrix, uniform subsampling by up to 8× demonstrates close performance. We present the test results and analysis of subsampling in Section IV-G.

B. Clustering Algorithm

Based on speed and robustness considerations, we use K-means as the core clustering algorithm. We would like our method to be applicable to large datasets. Among popular clustering algorithms, including DBSCAN [44] and BIRCH [45], only K-means and Gaussian mixture model (GMM) are time-efficient. We present a comparative analysis of K-means and GMM in Section IV-G. K-means is more robust in mask computation due to its one-hot cluster assignments, while GMM introduces greater uncertainty with its reliance on mixtures and soft assignments. Other advantages of K-means include speed and scalability; it is often faster, especially with large datasets.
On the other hand, GMM excels in accommodating clusters of diverse shapes and sizes and exhibits less sensitivity to outliers. Notably, there are cases where GMM outperforms K-means in mask accuracy. We encourage interested readers to explore both methods.

K-means employs one parameter, the number of clusters, $k$. Since mask assignment is binary in our methodology, we only need two final clusters. Therefore, we employ another parameter, the number of selected clusters, $s$, to divide multiple clusters into two groups when $k$ is greater than two. With $k$ clusters, we sort the sum of their cluster centers and denote samples from the top $s$ clusters as noisily labeled. We experiment with three values, i.e., $\binom{k}{s}$, $\binom{k}{1}$, and $\binom{k}{2}$.

### C. Controlling the Detection Sensitivity to Noisy Labels

To adjust the detection sensitivity to noisy labels, we employ a divide-and-vote approach. We divide the loss matrix into several windows and run the clustering algorithm on each window. Hence, each window outputs a mask. We then sum up all masks and apply a threshold function on the sum to make the final mask binary. Fig. 4 illustrates a four-window example containing five samples. The sum represents the total clean score (because 1 represents clean in a mask). Hence, it is the number of windows that classify the sample as clean. In this example, we apply a threshold $t = 3$ to the votes to yield the final mask. A smaller (larger) threshold would make the algorithm more (less) sensitive to label noise.

In this windowing technique, we introduced two more parameters: the number of windows $w$ and the window threshold $t$. In our experiments, we tested one, two, and four windows, and for each window choice $w$, we tried thresholds $t$ ranging from 1 to $\lfloor w/2 \rfloor + 1$. Hence, we have six $(w, t)$ pairs in all, i.e., $(1, 1)$, $(2, 1)$, $(2, 2)$, $(4, 1)$, $(4, 2)$, and $(4, 3)$.

### D. Determining the Best Mask

Our label error detection algorithm has four clustering parameters in all: number of clusters, number of selected clusters, number of windows, and the window threshold. We need a metric to obtain the best set of values for these clustering parameters. There is no conventional rubric to measure the quality of cluster assignments. One possible metric is the silhouette score [46]. For each sample, its silhouette coefficient denotes the scaled difference between its mean intra-cluster distance and its mean nearest-cluster distance. The silhouette score of a dataset is the average silhouette coefficients of all its samples. A drawback of the silhouette score is that it does not always select the best assignment. Our solution is to consider the training outputs in addition to the silhouette score. Thus, we use

$$
\text{score}(\mathbf{m}, L, \tilde{\theta}) = \text{silhouette}(\mathbf{m}, L) \times \left[ \text{train_acc}(\mathbf{m}, \tilde{\theta}) \times \text{loss_ratio}(\mathbf{m}, L) \right]^\alpha.
$$

This equation has two parts. The first part is the regular silhouette score, which measures clustering quality. The other part measures the mask quality by calculating the product of masked training accuracy and the ratio between mean marked-noisy sample loss and mean marked-clean sample loss. We use the last loss value of the smoothed loss curve which, in our case, is averaged over the last five epochs. The use of masked training accuracy helps because models tend to learn more correctly labeled samples than incorrectly labeled ones. This learning difference is also reflected in losses. We control the strength of the masked score by raising its power to $\alpha$, which depends on model convergence. When the model overfits to all samples, its masked training accuracy depends less on the quality of the mask because the model can correctly predict almost all training samples. In this case, the loss ratios are largely influenced by outliers and we should use a small $\alpha$ so as not to give the masked score too much weight. On the other hand, if the model is robust against noisy labels, it will demonstrate different convergence patterns for different label types. In this situation, the masked training accuracy and loss ratio reveal the quality of the mask, and we should assign a higher weight to the masked score. We can obtain information about model robustness by examining its loss histogram. The more the sample losses are concentrated in small loss values, the less robust the model is, because it overfits to all samples, including noisy ones.

With our selection of the model architecture and the training hyperparameters, CIFAR-10- and CIFAR-100-based NN models converge quite differently, with the CIFAR-10-based model being much more robust to label errors. Fig. 5 shows histograms of the mean loss over the last five epochs for the two datasets. Based on sample losses, we find that the CIFAR-10 model learns some samples well but leaves some samples unfitted, while the CIFAR-100 model overfits to almost all samples. We tried the following values of $\alpha$: 0, 0.25, 0.5, and 1. These four values scale the importance of masked accuracy and masked loss ratio from zero to being equally important as the silhouette score. We encourage interested readers to try other values of $\alpha$, such as 2. While they all generally result in better detection accuracies than other methods, different $\alpha$’s result in different masks. Hence, selecting a suitable value for $\alpha$ is still important. We chose 1 for CIFAR-10 and 0.25 for CIFAR-100 because the model overfitted less to CIFAR-10, making the masked training accuracy and loss ratio more distinguishable. We only use the silhouette score for tabular datasets because their training convergence is less stable. We show the results of

| $m_1$ | $m_2$ | $m_3$ | $m_4$ | Sum | $m$ |
|-------|-------|-------|-------|-----|-----|
| $\tilde{y}_1$ | 1 | 0 | 1 | 0 | 2 | 0 |
| $\tilde{y}_2$ | 0 | 0 | 1 | 0 | 1 | 0 |
| $\tilde{y}_3$ | 1 | 1 | 0 | 1 | 3 | 1 |
| $\tilde{y}_4$ | 1 | 1 | 1 | 1 | 4 | 1 |
| $\tilde{y}_5$ | 1 | 1 | 1 | 0 | 3 | 1 |

Fig. 4. Example of windowing. This example has 5 samples, 4 windows, and a threshold of 3.
using different \( \alpha \) values in Section IV-G. The choice of \( \alpha \) can be automated based on loss histograms. We find the curvature of the loss histogram (i.e., the concentration of the distribution) and its \( x \)-axis scale (i.e., the convergence of the model) are two important factors to consider when selecting \( \alpha \). It would be possible to build a simple ML model, e.g., a linear regressor, to model the relationship between the shape of the loss histogram and the best choice of \( \alpha \). However, training an ML model generally needs a large number of samples. We only have data from thirteen datasets, which is not sufficient. Thus, we leave this to future work.

**E. Cleaning the Dataset and Retraining the Model**

The next steps are to clean the dataset and then retrain the model using the cleaned data. The simplest way to clean is to remove all wrongly labeled samples. This method is efficient. There are many other ways to use the mask. We also tried keeping all samples but replacing bad labels with the model’s prediction, either dynamically (update every epoch during a training period) or statically (update before training by using the model trained in the first round). Under limited tests, the dynamic replacement method generally results in better test accuracies than the static method, and just pruning away bad labels outperforms both replacement methods. We present results obtained using these two label replacement methods in Section IV-G.

**F. Loss Gap Analysis for a Simple Problem**

We present a theoretical analysis of the loss gap using a similar setting to the one described in [12]. Consider a balanced two-class clean dataset that contains \( n \) independent samples in \( \mathbb{R}^d \). The feature \( x \) is sampled from

\[
\begin{align*}
x \sim \mathcal{N}(\mathbf{v}, \sigma_1^2 \mathbf{I}_{d \times d}) \quad & \text{if } y = +1, \\
x \sim \mathcal{N}(-\mathbf{v}, \sigma_2^2 \mathbf{I}_{d \times d}) \quad & \text{if } y = -1
\end{align*}
\]

where \( \|\mathbf{v}\| = 1 \) and \( \sigma^2 \) is small. Denote by \( \bar{y} \) the true hidden label and by \( \hat{y} \) the observed label. We use subscripts on \( x \) and \( y \) to index samples. Assume that for any sample \( i \)

\[
\bar{y}_i = \begin{cases} y_i, & \text{with probability } 1 - \Delta, \\
-\bar{y}_i, & \text{with probability } \Delta
\end{cases}
\]

where \( \Delta \in (0, 1/2) \) is the noise level. We use \( \mathcal{C} \) to denote the set of indices whose corresponding samples have clean labels and \( \mathcal{N} \) for the noisy ones.

Let us consider a two-layer sigmoid NN with parameter \( \theta \in \mathbb{R}^d \) that makes class probability predictions \( p \) for input \( x \) as follows:

\[
\begin{align*}
p(y = 1) &= \frac{1}{1 + e^{-\theta^T x}} , \\
p(y = -1) &= 1 - p(y = 1) .
\end{align*}
\]

In the beginning, we initialize \( \theta \) to 0, denoted as \( \theta_0 \). We use log loss for gradient descent, and for proof simplicity, we clamp each sample loss \( l_i \) to \( B \), where \( B \geq 1 \). The average loss is then

\[
l(\theta) = \frac{1}{n} \sum_{i=1}^{n} \min\{l_i(\theta), B\} = \frac{1}{n} \sum_{i=1}^{n} \min\{\log (1 + e^{-\hat{y}_i \theta^T x_i}), B\} .
\]

In the first epoch, \( l_i(\theta_0) = \log(2) < B \) because \( \theta_0 \) is zero. The gradient is then

\[
\nabla_{\theta_i} l(\theta_0) = \frac{1}{2n} \sum_{i=1}^{n} x_i \cdot \left( \tanh \left( \frac{1}{2} \theta_0^T x_i \right) - \hat{y}_i \right) = \frac{1}{2n} \sum_{i=1}^{n} -\hat{y}_i x_i .
\]

Also

\[
\mathbf{v}^T (-\nabla_{\theta_i} l(\theta_0)) = \frac{1}{2n} \sum_{i=1}^{n} \hat{y}_i \mathbf{v}^T x_i = \frac{1}{2n} \left[ \sum_{i \in \mathcal{C}} \mathbf{v}^T (\mathbf{v} + z_i) + \sum_{i \in \mathcal{N}} \mathbf{v}^T (-\mathbf{v} + z_i) \right] = \frac{1}{2n} \left[ \sum_{i \in \mathcal{C}} (1 + \mathbf{v}^T z_i) + \sum_{i \in \mathcal{N}} (-1 + \mathbf{v}^T z_i) \right] = \frac{1}{2} (1 - 2\Delta) + \frac{1}{2n} \sum_{i=1}^{n} w_i
\]

where \( z_i \sim \mathcal{N}(0, \sigma^2 \mathbf{I}_{d \times d}) \) is the added vector deviation on \( x_i \). The last step is derived from the fact that, without loss of generality, by taking \( \mathbf{v} \) as a standard basis vector and by the symmetry of the normal distribution, we can replace \( \mathbf{v}^T z_i \) by...
a scalar \(w_i\) where \(w_i \sim N(0, \sigma^2)\). By Hoeffding’s inequality, with probability \(\geq 1 - p\)

\[
v^T (-\nabla_{\theta_t} l(\theta_0)) \geq \frac{1}{2} (1 - 2\Delta) - O\left(\frac{\sigma}{\sqrt{n}} \sqrt{\log \frac{1}{p}}\right).
\]

Assume we use a learning rate of \(\eta\). Then, after the first epoch, we have \(\theta_1 = -\eta \cdot -\nabla_{\theta_t} l\). Based on the above analysis, with high probability, we conclude the following:

\[
\frac{v^T \theta_1}{\|\theta_1\|} \geq 1 - \tilde{O}\left(\frac{\sigma}{\sqrt{n}}\right).
\]

(2)

This indicates that we have a high chance of getting model parameters close to the optimal after one epoch. Liu et al. [12] give the derivation of gradient and parameter changes under a similar setting over more epochs and show that \(\theta_1\) would initially be well correlated with \(v\) for a period. This phenomenon is called early learning. However, the analysis gets much more complicated for ResNets on the CIFAR-10/CIFAR-100 datasets, in which there are complex relations between classes and each sample’s loss curve fluctuates under gradient descent. Hence, we need to consider a period larger than one epoch, e.g., the whole training duration.

Next, we analyze the loss gap between clean and noisy samples during early learning. For \(j \in C\)

\[
l_j(\theta) = \min \left\{ \log \left(1 + e^{-\theta^T(v + z_j)}\right), B \right\}
\]

\[
\leq e^{-\theta^T(v + z_j)},
\]

because \(\log(1 + x) \leq x\) for \(x \geq 0\). Knowing that \(\log(1 + x) \geq (1/(1 + x^{-1})) \geq 1 - x^{-1}\) for \(x > 0\), we have for \(k \in \mathcal{N}\)

\[
l_k(\theta) = \min \left\{ \log \left(1 + e^{\theta^T(v + z_k)}\right), B \right\}
\]

\[
\geq \min \left\{ 1 - e^{-\theta^T(v + z_k)}, B \right\}
\]

\[
= 1 - e^{-\theta^T(v + z_k)}.
\]

Taking the expectation on the difference between clean and noisy label losses, we get

\[
E[l_k(\theta) - l_j(\theta)] = E[l_k(\theta)] - E[l_j(\theta)]
\]

\[
\geq 1 - 2 \cdot E[e^{-\theta^T(v + z)}].
\]

The term \(1 - 2 \cdot E[e^{-\theta^T(v + z)}]\) bounds the expected loss gap between clean and noisy labels. It is independent of the label type.

\[
E\left[e^{-\theta^T(v + z)}\right] = e^{-\theta^T v} \cdot E\left[e^{-\theta^T z}\right]
\]

\[
= e^{-\theta^T v} \cdot \sum_{w \sim N(0, \sigma^2)} E\left[e^{\theta^T w}\right] \cdot e^{\frac{1}{2} \|\theta\|_2^2}.
\]

The smaller the \(\sigma\) or the larger the projection \(\theta\) has on \(v\), the larger the expected loss gap. Luckily, from (2), we know that it is not hard to obtain a good \(\theta\). Let us define the average losses of clean and noisy labels as \(l_{\text{clean}} = (1/n_c) \sum_{i \in C} l_i\) and \(l_{\text{noisy}} = (1/n_n) \sum_{i \in N} l_i\), respectively. By Hoeffding’s inequality on bounded variables and the union bound, we obtain with probability \(\geq 1 - p\)

\[
l_{\text{clean}} \leq E[l_{\text{clean}}] + O\left(\frac{B}{\sqrt{n_c}} \sqrt{\log \frac{1}{p}}\right),
\]

\[
l_{\text{noisy}} \geq E[l_{\text{noisy}}] - O\left(\frac{B}{\sqrt{n_n}} \sqrt{\log \frac{1}{p}}\right).
\]

For clean samples, the expectation of the average loss is the same as the expectation of the individual loss \(l_j(\theta)\) above. This is true for noisy samples \(l_k(\theta)\) as well. Therefore, during the early learning phase, with high probability

\[
l_{\text{noisy}} - l_{\text{clean}} \geq 1 - 2e^{-\theta^T v + \frac{1}{2} \|\theta\|_2^2} - O\left(\frac{1}{\sqrt{n}}\right).
\]

(3)

Inequality (3) explains the gap between the average losses, as illustrated by the two curves in Fig. 2.

IV. EXPERIMENTAL RESULTS

We test our label error detection method and compare it with previous methods on six image datasets, CIFAR-10 and CIFAR-100 [43], Animal-10N [47], Food-101 [48], Food-101N [49], Fashion-MNIST [50], and seven tabular datasets: Cardiotoxicography\(^2\), Credit Fraud\(^3\), Human Activity Recognition\(^4\), Letter\(^5\), Mushroom\(^6\), Satellite\(^7\), and Sensorless Drive\(^8\). Table I describes all datasets after processing. Dataset size ranges from thousands to a third of a million samples, and the number of classes ranges from 2 to 101. In practice, most datasets lie within this range. Each dataset is either split in a fixed manner if the training/test split is provided by the creator or split randomly by us. We resize images in Food-101 and Food-101N to squares of uniform size, use one-hot categorical features in tabular datasets, and employ principal component analysis to reduce the input dimension of the Human Activity Recognition dataset. Among the six image datasets, Animal-10N and Food-101N contain real-world label errors to which we can directly apply our method without introducing artificial label noise. We test our method based on simulated asymmetric noise of different noise and sparsity levels for the four image datasets. We use asymmetric noise because this type of noise is more common in practice. For each tabular dataset, we test the method under symmetric noise of different levels because it is infeasible to create asymmetric noise when the number of classes is small. For each dataset, we conduct multiple experiments using different random seeds and report the means and standard deviations. We evaluate different methods in terms of mask accuracy and the balanced-class test accuracy of models. A random seed controls noise creation, NN training, and split between training and test sets if the split is not originally provided.

\(^2\)https://archive.ics.uci.edu/ml/datasets/Cardiotoxicography
\(^3\)https://www.kaggle.com/datasets/mlg-ulb/creditcardfraud
\(^4\)https://www.kaggle.com/datasets/uciml/human-activity-recognition-with-smartphones
\(^5\)https://www.kaggle.com/datasets/nishan192/letterrecognition-using-svm
\(^6\)https://www.kaggle.com/datasets/uciml/mushroom-classification
\(^7\)https://www.kaggle.com/datasets/markjibrilmononutu/statlog-landsat-satellite-data-set
\(^8\)https://archive.ics.uci.edu/ml/datasets/dataset+for+sensorless+drive+diagnosis
We compare our results with the baseline method (in which the provided labels are used directly), Co-teaching, mixup, and CL. For Co-teaching, we set the forget rate to the actual noise rate and to 0.05 when there is no noise. This could be one of the reasons that Co-teaching performs well in some test cases. For mixup, we report the best result across $alpha_{mixup} \in \{1, 2, 4, 8\}$. CL employs five methods in all, based on different counting and pruning algorithms. We report the one with the best detection accuracy among the five. We also tested early stopping on CIFAR-10 and report the best result between the stopping epochs of 100 and 200. Co-teaching, mixup, and early stopping do not explicitly compute masks. Here, we treat samples with disagreements between their provided labels and the trained model’s predictions as noisy.

### A. Experimental Setup

We ran all experiments on Nvidia P100 GPUs and Intel Broadwell E5-2680v4 CPUs. We use the scikit-learn [51] packages for K-means computation and data processing. We train NNs using PyTorch [52]. We use Ray [53] for distributed computing.

### B. Noise Simulation

We conduct image experiments with asymmetric noise. However, our method can generalize to symmetric and semantic noise as well. With a clean dataset, the first step is to inject label errors with various levels of noise and sparsity, then test the methods under these scenarios. We use Cleanlab’s [14], [54] noise generation function to generate the noise transition matrix. With a given noise level, sparsity level, and random seed, Cleanlab first randomly generates the diagonal of the matrix, which averages to one minus the noise rate. It then distributes zero entries across the columns and generates noise rates for the remaining positions in each column. Fig. 6 presents an example of a noise transition matrix for CIFAR-10, with 20% noise and 60% sparsity.

![Fig. 6. Example asymmetric noise transition matrix for CIFAR-10, with 20% noise and 60% sparsity.](image)

We use Cleanlab’s function for this purpose, as it exhibited the highest precision among all the noise generators we investigated.

For CIFAR-10 and Fashion-MNIST, we test methods under noise levels of 0%, 10%, and 20%. For each noise level, we simulate sparsity levels of 0%, 20%, 40%, and 60%. For CIFAR-100, we employ a range of noise levels from 0% to 30% and sparsity levels of 0%, 30%, and 60%. With a larger number of classes (i.e., 100), due to the technical difficulties in generating a matrix targeted at arbitrary levels of noise and sparsity, the noise levels we can simulate depend on the sparsity levels. When both the noise and the sparsity levels are high (e.g., 30% noise and 60% sparsity), some label classes will have noise rates greater than 50%, which is impractical. Therefore, we only test noise rates not greater than 20% for most datasets. Thus, for Food-101, we employ a range of noise levels from 0% to 20% and sparsity levels of 0%, 20%, 40%, and 60%. Also, since it becomes infeasible to generate asymmetric transition matrices when the number of classes is small, we test all tabular datasets with 10% and 20% symmetric noise.

### C. NN Hyperparameters

A hyperparameter set contains the NN architecture, optimizer, batch size, number of epochs, and learning rates.
For image datasets, we employ the hyperparameter set provided by an open-source GitHub repository\(^3\) and do not tune it manually. We use ResNet-50 as the NN architecture and stochastic gradient descent with 0.9 momentum and $5 \times 10^{-4}$ weight decay as the optimizer. We start the learning rate at 0.1 and decay it using cosine annealing. We train models with a batch size of 128 for 200 epochs. We found that using a smooth learning rate decaying scheduler such as cosine annealing and setting its maximum number of iterations to some number slightly larger than the number of epochs helps CTRL detect label errors because this reduces NN overfitting. Hence, we set the cosine annealing iteration number to 250 for the mask computation round of CTRL. We use 200 (same as the number of epochs) for training of other models, i.e., Co-teaching’s training, mixup’s training, CL’s mask computation and retraining, and CTRL’s retraining. In the CL article \(^{[14]}\), the authors employed another hyperparameter set. We obtained better mask and test accuracies for CL with the above set; hence, we report results for CL using the new hyperparameter set. We also use this hyperparameter set for both Co-teaching and mixup. For Co-teaching, we run experiments using its original hyperparameter set and report the higher score across the two sets. For each tabular dataset, we use the same hyperparameter set for all training and retraining experiments. We use a fixed batch size of 1024, a learning rate of $10^{-3}$, 0 weight decay, and Adam optimizer. We conduct NN architecture search over three-layer and four-layer ReLU-activated NNs with various hidden sizes and numbers of epochs. We use grid search and select the hyperparameter set with the best cross-validated balanced-class accuracy on original training data. All methods share the same hyperparameters.

### D. Image Datasets

In this section, we discuss results on CIFAR-10, CIFAR-100, Food-101, and Fashion-MNIST. For each test case, we run three trials. The top half of Table II shows the mean mask accuracies computed on CIFAR-10 under various noise conditions. CTRL outperforms other methods in almost all cases. Generally, CTRL and CL perform better than Co-teaching, mixup, and early stopping. One advantage of CTRL is its flexibility: the mask selection metric we presented in (1) enables CTRL to try different noisy label detection sensitivity levels. CL, on the other hand, results in many false positives: it declares many labels to be erroneous when they are correct but just hard to learn. This is because it only considers the final model state. CTRL improves the label error detection accuracy by examining the entire training process. However, randomness in NN initialization and training may cause a higher variance in the learning process than in the final converged state, resulting in higher variances from CTRL in some cases.

After pruning the labeling errors, we retrain our model. Table II also shows the model test accuracies. CTRL is superior in most cases, though with higher uncertainties. CTRL performs worse when the noise level is 20% and sparsity level is 60%. This may be because CIFAR-10 has sufficient training samples and any noise in the dataset. In that case, the final retrained model by CTRL converges to a corrected but just hard to learn. This is because it only considers the final model state. CTRL improves the label error detection accuracy by examining the entire training process. However, randomness in NN initialization and training may cause a higher variance in the learning process than in the final converged state, resulting in higher variances from CTRL in some cases.

Table III shows the CIFAR-100 mask and test accuracy results. CTRL performs better than other methods in almost all cases. The performance gap between CTRL and other methods is larger on CIFAR-100 than on CIFAR-10. Compared with CL, our label error detection method is more robust to the increase in the number of classes because we do not need to perform any $|C| \times |C|$ matrix calculation as CL does. Tables IV and V show results for Food-101 and Fashion-MNIST, respectively. We use an $\alpha$ of 0 for Food-101 and an $\alpha$ of 0.5 for Fashion-MNIST. On Food-101, CTRL outperforms other methods on mask and model accuracy in all cases except when there is no noise in the dataset. In that case, the final retrained model by CTRL still has a test accuracy close to the best model. The Fashion-MNIST classification task is relatively simple. It has

### TABLE II

| Noise | 0 | 10 |
|-------|---|----|
| Sparsity | 0 | 20 | 40 | 60 |
| Baseline | 100 ± 0 | 90.1 ± 0.0 | 90.1 ± 0.0 | 90.1 ± 0.0 | 90.1 ± 0.0 | 80.1 ± 0.0 | 80.1 ± 0.0 | 80.1 ± 0.0 | 80.1 ± 0.0 |
| Co-teaching | 97.5 ± 0.1 | 92.7 ± 0.1 | 92.7 ± 0.2 | 92.8 ± 0.2 | 92.7 ± 0.2 | 85.1 ± 0.5 | 84.7 ± 0.4 | 84.9 ± 0.3 | 85.2 ± 0.2 |
| Mixup | 96.3 ± 0.5 | 87.8 ± 0.6 | 88.3 ± 0.6 | 87.5 ± 0.5 | 87.8 ± 0.3 | 80.0 ± 0.3 | 80.3 ± 0.5 | 80.5 ± 1.0 | 80.2 ± 0.5 |
| Early stopping | 97.9 ± 0.2 | 89.6 ± 0.1 | 89.3 ± 0.6 | 89.3 ± 0.3 | 88.9 ± 0.1 | 80.9 ± 0.6 | 80.6 ± 0.2 | 80.6 ± 0.2 | 80.4 ± 0.3 |
| CL | 98.0 ± 0.0 | 93.2 ± 0.0 | 93.4 ± 0.2 | 92.6 ± 0.3 | 93.5 ± 0.3 | 92.6 ± 0.1 | 92.9 ± 0.6 | 92.6 ± 0.2 | 92.8 ± 0.4 |
| CTRL | 97.9 ± 0.1 | 98.6 ± 0.1 | 98.4 ± 0.3 | 98.6 ± 0.3 | 98.4 ± 0.2 | 97.4 ± 0.2 | 97.5 ± 0.1 | 97.1 ± 0.3 | 96.2 ± 1.6 |

**Balanced-class model test accuracy**

| Noise | 0 | 10 |
|-------|---|----|
| Sparsity | 0 | 20 | 40 | 60 |
| Baseline | 95.4 ± 0.1 | 89.5 ± 0.6 | 89.1 ± 0.4 | 88.9 ± 0.4 | 89.3 ± 0.5 | 80.0 ± 0.6 | 80.0 ± 0.7 | 79.9 ± 0.4 | 79.2 ± 1.0 |
| Co-teaching | 92.5 ± 0.1 | 90.6 ± 0.1 | 90.3 ± 0.3 | 90.3 ± 0.1 | 90.1 ± 0.2 | 88.5 ± 0.2 | 87.4 ± 0.2 | 87.6 ± 0.1 | 86.6 ± 0.8 |
| Mixup | 92.2 ± 0.3 | 89.9 ± 0.8 | 90.7 ± 0.7 | 91.2 ± 1.1 | 91.0 ± 0.6 | 89.2 ± 0.4 | 87.6 ± 0.7 | 89.1 ± 1.1 | 88.7 ± 0.2 |
| Early stopping | 92.1 ± 0.5 | 89.2 ± 0.5 | 90.2 ± 0.8 | 90.0 ± 0.7 | 89.3 ± 1.8 | 86.8 ± 0.7 | 83.0 ± 1.0 | 87.9 ± 0.9 | 87.8 ± 0.4 |
| CL | 95.2 ± 0.3 | 93.6 ± 0.2 | 93.5 ± 0.2 | 93.5 ± 0.4 | 93.3 ± 0.1 | 92.1 ± 0.4 | 92.4 ± 0.3 | 92.2 ± 0.3 | 92.6 ± 0.5 |
| CTRL | 95.1 ± 0.1 | 94.3 ± 0.1 | 94.0 ± 0.5 | 93.9 ± 0.4 | 94.2 ± 0.2 | 93.0 ± 0.5 | 93.0 ± 0.2 | 93.4 ± 0.2 | 92.2 ± 2.2 |

---

Note: Bold entries indicate the results of best-performing method.

---

\(^3\)https://github.com/kuangliu/pytorch-cifar
### TABLE III
CIFAR-100: Mask Accuracy and Model Test Accuracy Over Three Trials Under Asymmetric Label Noise

| Noise  | 0    | 4    | 5    | 7    | 13   | 15   | 17   | 22   | 24   | 27   |
|--------|------|------|------|------|------|------|------|------|------|------|
| sparsity | 0 | 0.0  | 5.7  | 6.0  | 6.2  | 6.3  | 6.5  | 6.6  | 6.9  | 7.0  |
| Mask accuracy | 0.0 | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  |

**Note:** Bold entries indicate the results of best-performing method.

### TABLE IV
FOOD-101: Mask Accuracy and Model Test Accuracy Over Three Trials Under Asymmetric Label Noise

| Noise  | 0    | 4    | 5    | 7    | 13   | 15   | 17   | 18   | 19   |
|--------|------|------|------|------|------|------|------|------|------|
| sparsity | 0 | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  |
| Mask accuracy | 0.0 | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  | 0.0  |

**Note:** Bold entries indicate the results of best-performing method.

### TABLE V
FASHION-MNIST: Mask Accuracy and Model Test Accuracy Over Three Trials Under Asymmetric Label Noise

| Noise  | 0    | 10   |
|--------|------|------|
| sparsity | 0 | 0.0  |
| Mask accuracy | 0.0 | 0.0  |

**Note:** Bold entries indicate the results of best-performing method.

10 classes and sufficient training samples for each class. Models trained by different methods generally have test accuracy gaps within 1%.

To train models on the CIFAR-10 dataset, we use one GPU and two 4GB CPU cores. It takes around five hours to train an NN from scratch on the vanilla dataset with our choice of training hyperparameters. The baseline, Co-teaching, and mixup methods only need one round of training. CL and CTRL require two rounds: one for mask computation and one for retraining. The total time cost for Co-teaching is around \(2 \times \) the vanilla training time because it trains two models simultaneously. For mixup, the total time cost is approximately \(1.5 \times \) the vanilla time cost. The time cost for mask computation varies by method. CL uses fourfold cross-validation by default, which triples the training time. After CL cross-validates the training set, it just needs seconds to compute the mask. CTRL only needs one-time full training before mask calculation, though it needs extra time and space to record and save the training.
TABLULAR DATASETS: MASK ACCURACY AND MODEL TEST ACCURACY OVER TEN TRIALS UNDER SYMMETRIC LABEL NOISE

| Noise level | Dataset | Cardio-tography | Credit Fraud | Human Activity | Letter | Mushroom | Satellite | Sensorless Drive |
|-------------|---------|----------------|-------------|----------------|--------|----------|-----------|-----------------|
| 10          | Baseline | 90.1 ± 0.0     | 90.2 ± 0.0  | 91.3 ± 0.0     | 90.0 ± 0.0 | 90.1 ± 0.0 | 90.2 ± 0.0 | 90.2 ± 0.0      |
|             | Co-teaching | 89.4 ± 0.2    | 83.1 ± 0.9  | 91.1 ± 0.1     | 88.4 ± 0.4 | 86.1 ± 0.3 | 91.6 ± 0.0 | 91.6 ± 0.0      |
|             | Mixup     | 87.9 ± 0.6    | 86.9 ± 0.5  | 95.2 ± 0.4     | 92.2 ± 0.2 | 92.0 ± 0.2 | 85.9 ± 0.4 | 79.3 ± 0.5      |
|             | CL        | 96.5 ± 0.3    | 95.2 ± 0.8  | 92.2 ± 0.5     | 94.8 ± 0.1 | 97.1 ± 0.3 | 93.5 ± 0.4 | 96.3 ± 0.1      |
|             | CTRL      | 98.7 ± 0.4    | 95.9 ± 0.4  | 97.9 ± 0.2     | 99.2 ± 0.1 | 99.9 ± 0.1 | 96.9 ± 0.5 | 99.4 ± 0.0      |
| 20          | Baseline | 80.1 ± 0.0    | 80.1 ± 0.0  | 80.2 ± 0.0     | 82.7 ± 0.0 | 80.0 ± 0.0 | 80.4 ± 0.0 | 80.2 ± 0.0      |
|             | Co-teaching | 76.5 ± 0.7    | 73.0 ± 2.2  | 82.0 ± 0.2     | 82.8 ± 0.1 | 78.1 ± 0.6 | 78.2 ± 0.2 | 82.6 ± 0.1      |
|             | Mixup     | 77.4 ± 0.7    | 78.6 ± 0.7  | 92.9 ± 0.7     | 85.4 ± 0.5 | 83.4 ± 0.5 | 75.9 ± 0.4 | 90.0 ± 0.6      |
|             | CL        | 92.9 ± 0.7    | 88.9 ± 1.3  | 85.3 ± 0.4     | 91.7 ± 0.4 | 90.7 ± 0.7 | 92.7 ± 0.2 | 89.8 ± 0.4      |
|             | CTRL      | 98.4 ± 0.3    | 94.7 ± 0.5  | 95.3 ± 0.3     | 98.4 ± 0.1 | 98.9 ± 0.2 | 95.7 ± 0.3 | 98.5 ± 0.1      |

Balanced-class model test accuracy

| Noise level | Dataset | Cardio-tography | Credit Fraud | Human Activity | Letter | Mushroom | Satellite | Sensorless Drive |
|-------------|---------|----------------|-------------|----------------|--------|----------|-----------|-----------------|
| 10          | Baseline | 95.6 ± 1.4    | 93.4 ± 0.9  | 78.7 ± 0.9     | 89.5 ± 0.5 | 94.7 ± 0.8 | 87.8 ± 0.5 | 93.1 ± 1.5      |
|             | Co-teaching | 97.1 ± 1.1    | 88.7 ± 2.5  | 89.7 ± 0.6     | 95.8 ± 0.4 | 97.6 ± 0.8 | 89.0 ± 0.3 | 98.7 ± 0.1      |
|             | Mixup     | 96.5 ± 1.8    | 93.9 ± 1.2  | 89.1 ± 0.7     | 93.5 ± 0.2 | 99.9 ± 0.1 | 85.7 ± 1.4 | 94.7 ± 0.5      |
|             | CL        | 96.0 ± 1.4    | 93.5 ± 1.3  | 88.8 ± 0.6     | 94.5 ± 0.5 | 99.3 ± 0.3 | 88.2 ± 0.5 | 98.9 ± 0.1      |
|             | CTRL      | 97.5 ± 1.0    | 94.3 ± 1.2  | 88.9 ± 0.5     | 95.8 ± 0.5 | 99.9 ± 0.1 | 88.7 ± 0.3 | 99.0 ± 0.1      |
| 20          | Baseline | 92.9 ± 2.0    | 90.8 ± 2.4  | 70.1 ± 0.9     | 82.4 ± 0.9 | 86.1 ± 1.3 | 86.7 ± 0.6 | 81.8 ± 9.3      |
|             | Co-teaching | 77.2 ± 1.7    | 86.0 ± 1.7  | 88.6 ± 0.8     | 95.1 ± 0.4 | 95.0 ± 1.6 | 88.5 ± 0.3 | 97.9 ± 0.1      |
|             | Mixup     | 94.7 ± 1.8    | 92.3 ± 0.9  | 86.1 ± 1.2     | 94.2 ± 0.3 | 99.2 ± 0.5 | 85.3 ± 0.8 | 91.3 ± 0.5      |
|             | CL        | 94.3 ± 1.5    | 91.1 ± 1.2  | 87.3 ± 0.7     | 93.1 ± 0.7 | 95.5 ± 0.7 | 87.7 ± 0.4 | **98.3 ± 0.2**  |
|             | CTRL      | 96.9 ± 1.2    | 95.7 ± 1.1  | 86.4 ± 0.6     | 94.4 ± 0.6 | **99.2 ± 0.2** | 88.0 ± 0.6 | 98.1 ± 0.2      |

Note: Bold entries indicate the results of best-performing model.

### E. Tabular Datasets

Experiments with tabular datasets follow a similar workflow. However, they involve some additional data processing such as scaling and one-hot encoding. Since NNs exhibit less stable behavior on tabular datasets, we perform ten trials for label error detection and retraining. Table VI shows mean mask accuracy and retrained balanced-class test accuracy under 10% and 20% symmetric noise. In label error detection, CTRL outperforms other methods in all cases. Its superiority increases as labels become noisier. CTRL also performs better on model test accuracy for most datasets. However, although CTRL finds masks with more than 95% accuracy, it still underperforms Co-teaching in model training on Human Activity Recognition and Satellite, in which Co-teaching learns fewer training samples than other methods (based on mask accuracy). These two datasets are also the hardest to learn when noise is present; i.e., the methods achieve accuracies in the 80% range on these two but in the 90% range on the others. Thus, it is better to drop all confusing samples in datasets like Human Activity Recognition and Satellite.

### F. Real-World Noisy Datasets

We also run CTRL on Animal-10N and Food-101N: datasets that contain real-world labeling errors in the training sets. They have clean test sets. Animal-10N contains five pairs of confusing animals crawled from online search engines. Food-101N contains images of food recipes classified in 101 classes, also collected from the Internet. Table VII shows a summary of our results. We set α to 0 for both datasets. CTRL’s estimated noise rates are close to those estimated by the dataset creators. The balanced-class accuracies also show that models trained on cleaned data perform better than models trained using the original noisy data.

### G. Ablation Studies

Tables VIII, IX, and X present results for some additional experiments on CIFAR and tabular datasets. We show in bold the rows that were reported in Sections IV-D and IV-E. We tested the following.

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Note: Bold entries indicate the results of best-performing model.
TABLE VIII
CIFAR-10: ADDITIONAL MASK ACCURACY AND MODEL TEST ACCURACY RESULTS

| Noise sparsity | 0     | 0     | 20    | 40    | 60    | 0     | 20    | 60    | 0     | 20    | 60    |
|---------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| alpha = 0     | 97.9 ± 0.1 | 98.6 ± 0.1 | 98.0 ± 0.9 | 97.7 ± 0.3 | 97.6 ± 0.7 | 96.2 ± 2.3 | 94.8 ± 2.9 | 95.6 ± 1.6 | 91.1 ± 5.2 |
| alpha = 0.25  | 97.9 ± 0.1 | 98.6 ± 0.1 | 98.4 ± 0.3 | 98.6 ± 0.3 | 98.4 ± 0.2 | 97.6 ± 0.1 | 97.5 ± 0.1 | 96.7 ± 1.0 | 95.9 ± 1.5 |
| alpha = 0.5   | 97.9 ± 0.1 | 98.6 ± 0.1 | 98.4 ± 0.3 | 98.6 ± 0.3 | 98.4 ± 0.2 | 97.6 ± 0.1 | 97.5 ± 0.1 | 97.1 ± 0.3 | 95.9 ± 1.4 |
| alpha = 1     | 97.9 ± 0.1 | 98.6 ± 0.1 | 98.4 ± 0.3 | 98.6 ± 0.3 | 98.4 ± 0.2 | 97.4 ± 0.2 | 97.5 ± 0.1 | 97.1 ± 0.3 | 96.2 ± 1.6 |
| GMM           | 45.4 ± 1.6 | 98.1 ± 0.7 | 97.8 ± 1.2 | 97.8 ± 0.6 | 96.7 ± 0.2 | 93.9 ± 1.4 | 92.5 ± 2.2 | 93.0 ± 2.1 | 90.9 ± 3.5 |

TABLE IX
CIFAR-100: ADDITIONAL MASK ACCURACY AND MODEL TEST ACCURACY RESULTS

| Noise sparsity | 0     | 0     | 20    | 40    | 60    | 0     | 20    | 60    | 0     | 20    | 60    |
|---------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| alpha = 0     | 96.7 ± 0.1 | 98.2 ± 0.4 | 98.0 ± 0.1 | 96.9 ± 0.2 | 97.0 ± 0.2 | 96.0 ± 0.4 | 95.4 ± 0.3 | 94.8 ± 1.2 | 92.0 ± 0.3 | 89.7 ± 1.0 |
| alpha = 0.25  | 96.7 ± 0.1 | 97.8 ± 0.1 | 97.0 ± 0.0 | 95.6 ± 0.1 | 96.9 ± 0.3 | 95.7 ± 0.2 | 93.2 ± 0.5 | 94.8 ± 0.2 | 93.2 ± 0.2 | 90.9 ± 1.2 |
| alpha = 0.5   | 96.7 ± 0.1 | 97.8 ± 0.1 | 97.0 ± 0.0 | 95.6 ± 0.1 | 96.8 ± 0.1 | 94.1 ± 0.5 | 91.4 ± 1.5 | 89.4 ± 2.0 | 85.6 ± 0.5 | 82.7 ± 0.3 | 83.8 ± 7.1 |
| GMM           | 96.8 ± 0.2 | 97.7 ± 0.0 | 97.0 ± 0.1 | 95.4 ± 0.0 | 96.8 ± 0.3 | 95.9 ± 0.4 | 93.2 ± 0.5 | 95.8 ± 0.4 | 93.3 ± 0.2 | 91.6 ± 1.1 |

1) Use of different $\alpha$ values to determine the best mask, as described in (1).
2) Use of GMM as the core clustering algorithm.
3) Use of a subset of the loss matrix for label error detection.
4) Application of iterative NN pruning during the first training round.
5) Retraining of the model by replacing noisy labels with model predictions, either dynamically or statically.

$\alpha$, GMM, subsampling, and pruning are involved in the label error detection process. Hence, we report the mask accuracy for these methods. Label replacement occurs in the cleaning and model retraining phase. Hence, we report the retrained model test accuracy using the mask from Tables II, III, and VI. To implement iterative pruning, we prune and unprune the NN by 60% from the 10%-th epoch to the mask from the 90%-th epoch alternatively, with a cyclic period of 20 epochs. To implement static label
replacement, we replace the values of noisy labels that CTRL detects with the predictions made by the model trained in the first round. To implement dynamic label replacement, we only include noisy labels from the 50%-th epoch to the 90%-th epoch during retraining. Their values are updated by the model’s prediction at each epoch.

For CIFAR datasets, different $\alpha$’s result in similar masks when the noise rate is low. The choice of $\alpha$ becomes more important when more noisy labels are present because models start to overfit smaller portions of the training samples. For tabular datasets, setting $\alpha$ to 0 yields better mask accuracy, likely caused by less stable loss convergence. With our selection of $\alpha$, we get comparable detection accuracies in most experiments if we replace the core clustering algorithm with GMM, except being less stable in a few cases. On CIFAR, CTRL generally performs better when it samples more points from the loss curve. This is especially helpful when noise rates are high. However, since we applied a mean filter of size 5 on the loss curve before mask computation, we find that uniformly subsampling the loss trajectory by up to 8× only degrades the mask accuracy by less than 2 points. Subsampling can even improve CTRL’s detection accuracy in many cases on the tabular datasets, indicating that tabular datasets suffer from high-frequency signals in their loss curves. To increase the loss difference between clean and noisy labels, we apply iterative pruning to NNs. However, NN pruning only helps in a few cases. In addition to simply removing noisy labels, we test including noisy labels during model retraining but replace them with the model predictions, either statically or dynamically. We find that simple filtering outperforms label replacements in most cases.

### H. Comparison of Methods and Discussions

Among the methods we tested, mixup enhances learning robustness through convex smoothing of label pairs. Co-teaching selects a fraction of samples with the smallest losses in each mini-batch, starting from 1 and decaying over training. CL explicitly removes samples by counting and ranking cross-validated predictions. CTRL classifies samples using windowed loss curve clustering and filters out those with a large area under the loss curve. All methods are straightforward to implement, with mixup and Co-teaching being applicable during training, while CL and CTRL are applied during postprocessing. They all require setting certain parameters beforehand: mixup needs a $\alpha_{\text{mixup}}$ for smoothing strength, Co-teaching requires a forget rate, CL offers five pruning algorithms, and CTRL needs an $\alpha$ to

![Table X](image-url)

**Table X**

| Noise level | Dataset | Cardio- | Credit | Human | Letter | Mushroom | Satellite | Sensorless Drive |
|-------------|---------|---------|--------|-------|--------|-----------|-----------|------------------|
|             |         | tography | Fraud  | Activity |       |           |           |                  |
| 10          | alpha = 0 | 98.7 ± 0.4 | 95.9 ± 0.4 | 97.9 ± 0.2 | 99.2 ± 0.1 | 99.9 ± 0.1 | 96.9 ± 0.5 | 99.4 ± 0.0 |
|             | alpha = 0.25 | 98.7 ± 0.4 | 95.8 ± 0.6 | 90.7 ± 0.1 | 91.9 ± 0.1 | 99.0 ± 0.5 | 96.5 ± 0.3 | 90.7 ± 0.1 |
|             | alpha = 0.5 | 98.5 ± 0.4 | 95.7 ± 0.5 | 90.7 ± 0.1 | 91.9 ± 0.1 | 95.0 ± 2.0 | 96.5 ± 0.3 | 90.7 ± 0.1 |
|             | alpha = 1 | 98.5 ± 0.4 | 95.8 ± 0.5 | 90.7 ± 0.1 | 91.9 ± 0.1 | 93.8 ± 1.5 | 95.4 ± 1.8 | 90.7 ± 0.1 |
|             | GMM | 98.7 ± 0.6 | 95.9 ± 0.4 | 97.9 ± 0.2 | 99.2 ± 0.1 | 99.7 ± 0.5 | 96.8 ± 0.5 | 99.4 ± 0.0 |
| 20          | uniform, 2x | 98.7 ± 0.4 | 95.9 ± 0.4 | 98.0 ± 0.2 | 99.2 ± 0.1 | 99.9 ± 0.1 | 97.0 ± 0.5 | 99.4 ± 0.0 |
|             | uniform, 4x | 98.7 ± 0.5 | 95.9 ± 0.4 | 98.1 ± 0.2 | 99.2 ± 0.1 | 99.9 ± 0.1 | 96.9 ± 0.5 | 99.5 ± 0.0 |
|             | uniform, 8x | 98.7 ± 0.5 | 95.9 ± 0.4 | 98.2 ± 0.2 | 99.2 ± 0.1 | 99.9 ± 0.1 | 96.9 ± 0.5 | 99.4 ± 0.0 |
|             | middle, 2x | 98.7 ± 0.4 | 95.9 ± 0.4 | 91.4 ± 0.9 | 94.0 ± 1.1 | 99.4 ± 0.2 | 96.5 ± 0.4 | 90.5 ± 0.1 |
|             | middle, 4x | 98.6 ± 0.5 | 95.7 ± 0.6 | 91.1 ± 0.5 | 92.9 ± 0.5 | 98.9 ± 0.4 | 96.4 ± 0.3 | 90.4 ± 0.1 |
|             | middle, 8x | 98.6 ± 0.5 | 95.6 ± 0.6 | 91.2 ± 0.5 | 92.6 ± 0.2 | 98.6 ± 0.5 | 96.4 ± 0.2 | 90.4 ± 0.0 |
|             | var, 2x | 98.4 ± 0.6 | 96.0 ± 0.4 | 98.0 ± 0.2 | 99.2 ± 0.1 | 99.9 ± 0.1 | 96.0 ± 0.3 | 99.4 ± 0.0 |
|             | var, 4x | 98.0 ± 1.3 | 95.8 ± 0.5 | 98.4 ± 0.2 | 99.2 ± 0.1 | 99.9 ± 0.1 | 96.2 ± 0.7 | 99.4 ± 0.0 |
|             | var, 8x | 98.0 ± 1.3 | 95.7 ± 0.5 | 98.7 ± 0.2 | 99.0 ± 0.1 | 99.7 ± 0.2 | 96.5 ± 0.9 | 99.5 ± 0.1 |
|             | pruning | 98.4 ± 1.2 | 94.6 ± 1.1 | 97.8 ± 0.3 | 99.1 ± 0.1 | 99.7 ± 0.1 | 99.5 ± 0.0 | 99.5 ± 0.0 |
|             | remove | 97.5 ± 1.0 | 94.3 ± 1.2 | 88.9 ± 0.5 | 95.8 ± 0.5 | 99.9 ± 0.1 | 88.7 ± 0.3 | 99.0 ± 0.1 |
|             | static | 95.8 ± 1.4 | 93.5 ± 0.9 | 78.7 ± 0.9 | 89.5 ± 0.5 | 94.7 ± 0.8 | 87.8 ± 0.5 | 93.1 ± 1.5 |
|             | dynamic | 97.4 ± 1.1 | 93.9 ± 1.2 | 86.6 ± 0.7 | 94.9 ± 0.3 | 99.9 ± 0.1 | 88.9 ± 0.4 | 97.6 ± 0.3 |

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compute the metric score. While all these methods are generally beneficial when the dataset contains label errors, CTRL typically offers state-of-the-art results. Even though all the methods extend training time, the increase is not substantial.

V. CONCLUSION AND FUTURE DIRECTIONS

In this article, we introduced a method named CTRL for label error detection in multiclass datasets. Experimental results showcase state-of-the-art error detection accuracy on both image and tabular datasets. CTRL is compatible with any model that has an associated training loss curve. Common model types, such as multilayer perceptrons, convolutional NNs, and transformers, can all benefit from it. It can be seamlessly integrated into the data cleaning phase of existing machine learning pipelines. Upon evaluating its effectiveness for model retraining, we conclude that when label errors are present, it’s preferable to clean (i.e., remove data instances with erroneous labels) rather than retain them.

There are some limitations to CTRL. First, compared to the baseline method, CTRL requires additional time and space to execute. Second, it discards samples deemed noisy, which is not always effective. Exploring alternatives to simply removing samples or replacing labels based on the mask could be beneficial. Third, CTRL results in greater variance in the test accuracy of retrained models because its error detection is more affected by the training process. There are numerous avenues to improve CTRL. Alternative clustering methods, such as those based on NNs, could be employed. The loss-based clustering approach could also be adapted for regression tasks. The primary challenge with regression tasks is the less concentrated loss distribution. For regression, it might be essential to project the loss distribution onto a more bounded spectrum, for instance, by taking the logarithm of loss values. Another option is to employ early stopping during the cleaning round; we do not need to wait for the model to converge fully during the error detection phase. A promising direction could be to induce larger loss gaps between clean and noisy labels in the initial training round. Selecting training hyperparameters that emphasize differences between clean and noisy labels in the initial training round.

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