TORPOR AND OTHER PHYSIOLOGICAL ADAPTATIONS OF THE BADGER (TAXIDEA TAXUS) TO COLD ENVIRONMENTS

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Oxygen consumption (\(V_O\)) and heart rate were measured at ambient temperatures between +20 and -40 C. Basal metabolic rate was 0.3 cm\(^3\)/g\(\cdot\)h (65 beats/min), the body temperature was 38 C, the lower critical temperature (\(T_L\)) was 10 C, and conductance was 0.01225 cm\(^3\)/g\(\cdot\)h\(^0\)C. Fat composition of 79 adult badgers captured during the winter showed maximal fat deposition of 31% body weight in November. Fat stores were reduced 37% between November and March. The burrow temperature remained between 0 and 4 C throughout the winter. Badgers in outdoor enclosures during the winter of 1977-1978 reduced their above-ground exposure by 93% from November through February. Two badgers remained below ground for more than 70 consecutive days during the 1978-1979 winter. While below ground, one telemetered badger entered a state of torpor, on 30 occasions, characterized by a 50% reduction in heart rate (from 55 to 25 beats/min) and a 9 C reduction in body temperature (from 38 to 29 C). The torpor cycle lasted an average of 29 h (entrance—15 h, torpor—8 h, arousal—6 h). Each cycle provided a 27% or 81 kcal/cycle reduction in energy expenditure.

INTRODUCTION

Many temperate-zone mammals exhibit both behavioral and physiological adaptations to cold. One of the most effective behavioral mechanisms is to avoid extreme cold through the use of a burrow or den (Pruitt 1960; Vose and Dunlap 1968; Stephenson 1969; Brocke 1970). Reliance on a fossorial shelter may be reflected in an animal's quality of thermal insulation, its ability to lower its metabolic requirements through hypothermia, and its dependence upon fat storage during winter.

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The badger, Taxidea taxus, is a semi-fossorial mammal that remains below the ground for extended periods during mid-winter in response to cold (Harlow 1979a). McNab (1966) reported that fossorial rodents tend to have higher conductance (the reciprocal of insulation) than predicted by standard formulas. This same characteristic may be reflected by the badger. A high thermal conductance may restrict the badger's exposure to cold and consequent predatory activity during the winter, causing an increased reliance on fat reserves. In addition, the badger is an opportunistic feeder which relies primarily on small mammals, which may be more difficult to obtain during the winter (Lampe 1976). Badgers which are restricted to a winter den because of food shortage and cold may, therefore, have to reduce their energy requirements for activity and maintenance of body temperature (Mrosovsky 1976) in order to conserve fat stores.

Morrison (1960) stated that fat reserves in mammals within the size range of badgers would not be sufficient to sustain these animals over a winter season without a
substantial reduction in metabolism. However, he also suggested that there is little need for extensive hypothermia in mammals of this size because of their relatively large body mass and fat reserves. Bears, Ursus sp. (Nelson 1973; Folk 1974), the opossum, Didelphis marsupialis (Brocke 1970), and the European badger, Meles meles (Slonin 1952; Johansson 1957) are known to exhibit signs of torpor. It is possible that the American badger also has the ability to lower its body temperature and metabolic requirements during the winter while beneath the ground and thereby conserve energy.

It is, therefore, the purpose of this study to investigate the badger's (1) winter activity and behavioral avoidance of cold temperatures, (2) thermal insulation, (3) seasonal fat utilization, and (4) energy requirements during the winter in order to understand the badger's adaptations to conditions of cold and food scarcity.

MATERIAL AND METHODS

EXPERIMENTAL ANIMALS

Badgers were collected in Albany County, Wyoming, during the summers of 1977 and 1978 and maintained either in outdoor enclosures or in rooms exposed to outside temperature and photoperiod. Only female badgers weighing between 7.5 and 9.5 kg were used in this study. They were fed Purina Dog Chow consisting of 21%, 8%, and 4.5% crude protein, fat, and fiber, respectively, and with a gross energy content of 5.15 kcal/g.

METABOLIC RESPONSE TO COLD TEMPERATURES

Oxygen consumption ($\dot{V}_O$) on six badgers was derived from the changes in composition of a measured flow of air through a 50-liter respirometer. Rate of flow was measured with a Datametrics model 800-L hot wire anemometer and maintained at 6 liters/min. A portion of this air, scrubbed of CO$_2$ and water, was measured for oxygen content with a Beckman M-3 paramagnetic oxygen analyzer, and $\dot{V}_O$, was calculated from formula number 10 of Depocas and Hart (1957). Oxygen consumption was determined between 1600 and 2200 MST at 10 C increments between $+20$ and $-40$ C on animals previously fasted for 16 h. The lower critical temperature ($T_{Lc}$) was determined by the method of Welch (1978) from the intersection of regression lines representing $\dot{V}_O$, at different ambient temperatures. Thermal conductance was obtained from the slope of the regression line representing $\dot{V}_O$, at temperatures below the $T_{Lc}$.

SEASONAL FAT MEASUREMENTS

Animal carcasses were collected during 1977–1978 from a local furrier and as road kills. Animals were sexed and the upper canine tooth removed for age determination by the cemental annuli technique (Crow 1972). Total body fat was determined for 79 adult badgers by specific gravity analysis (Brocke 1970). Animals were skinned and viscera removed, with the exception of genital organs, kidneys, and associated fat. The carcass was weighed in air to within 0.1 g and again while submerged in water with added detergent. From these weights, the specific gravity (SG) of each carcass was determined and % fat calculated from the formula: % fat = 100 - (4.56/SG) - 4.0. This assumes a density for fat tissue of 0.912 (Morales et al. 1945), and for lean tissue of 1.12, based on the lowest densities of badger carcasses (see Brocke 1970). Values obtained by this method were within 5% of those obtained from a chloroform/methanol extraction of whole carcasses.

The right femur was removed from each carcass, weighed to 0.001 g, and broken into shards. The shards were placed into a 30-ml Teflon centrifuge tube which contained a grid platform constructed so that the shards were supported over 5 ml of a chloroform/methanol (2:1) solution. When the shards were spun at 800 $\times$ g for 15 min, virtually all marrow fat was removed from the femur and dissolved in the solution. Fat content of the bone marrow was then determined by evaporating the chloroform/methanol solution and weighing the fat residue to 0.001 g.
HEART RATE AND BODY TEMPERATURE MEASUREMENT

Telemetry transmitters for heart rate and body temperature were developed (Weeks et al. 1978) and surgically implanted into the peritoneal cavities of badgers during the winter of 1977–1978 and again in the winter of 1978–1979. Stainless-steel electrocardiogram (EKG) electrodes leading from the transmitters were implanted 2 cm on either side of the sternum. Heart rate and \( \dot{V}_0 \) of badgers were determined simultaneously in the laboratory by using varying ambient temperatures to promote significant changes in metabolism (Holter et al. 1976). Telemetered animals weighing an average of 8 kg were released into separate outdoor enclosures made of cyclone fencing measuring 5 m on a side and extending 2 m beneath the ground with an enclosed bottom. Heart rate and body temperature signals transmitted from badgers within each enclosure were picked up by a ferrite rod antenna within polyvinylchloride (PVC) tubing buried 1 m below ground. Signals were processed by a digital/analog ratemeter (Harlow et al. 1979) and continuously recorded on an Esterline Angus model 402 multichannel recorder located in an insulated building 15 m from the enclosure.

BURROW TEMPERATURE AND BURROW USE

The temperature 6 cm above the ground and within two burrows was monitored continuously during the winter of 1977–1978 with a Dickerson 7-day Minicorder, model 42-2. To monitor burrow temperature, thermocouple probes from the recorder were pushed through the dirt plugging the entrance and as far into the burrow as possible.

The length of time each badger spent in its burrow was determined with a directional photocell monitoring system placed at the burrow entrance (Harlow 1979b).

A Student t-test and least-squares regression were employed to examine differences between means and linear correlation of data, respectively (Neter and Wasserman 1974).

RESULTS

Basal metabolic rate (BMR) for badgers weighing an average of 9.0 kg was 0.3 cm³/g·h or 311 kcal/day, 14% below the 363 kcal/day value predicted from the equation \( M = 70 W^{0.75} \) (Kleiber 1975). The lower critical temperature \( T_{lc} \) was 10 C, while conductance was calculated as 0.01225 cm²/g/°C (fig. 1).

Body weight and lipid fraction of adult badgers increased during the summer and fall and peaked in November with an average weight of 8.05 kg and lipid fraction of 31% (figs. 2 and 3). Body weight and fat stores of animals in this population were reduced 15% and 37%, respectively, between November and March. Deposition of fat into bone marrow increased in these animals from August through February with no significant decline through March (fig. 4).

Burrow temperatures during the winter 1977–1978 remained between 0 and 4 C, while average weekly, above-ground minimum temperatures were between –5 and –15 C (fig. 5). Badgers in field enclosures

Fig. 1.—Oxygen consumption of six badgers and three coyotes described by least-squares regression over ambient temperatures between +20 and –40 C. The lines representing the coyote were constructed from data reported by Shield (1972).
during the winter of 1977–1978 reduced their above-ground activity by 93% from November through February. This was followed by a 220% increase in above-ground nocturnal activity by April, when temperatures were warmer (fig. 6). The 1978–1979 winter had ambient temperatures of about 10°C lower than the previous year. Two badgers monitored January through March remained below ground for 74 and 85 continuous days.

Heart rate of badgers was significantly (r = .97) correlated with oxygen consumption (fig. 7). The heart rate of badgers while below ground during February and March 1978 was about 65 beats/min (figs. 8 and 9), which corresponds to a metabolic rate of 0.32 cm³/g·h. Above-ground behavior consisted of foraging, feeding, and digging activities. During February, badgers were active above ground between 1500 and 0100 MST and had an average heart rate of 90 beats/min (0.42 cm³/g·h) (fig. 8). During March, badgers engaged in above-ground

![Fig. 2.—Seasonal changes in body weight for 79 adult badgers; closed circles represent means, vertical lines represent ±2 SE.](image2)

![Fig. 3.—Seasonal changes in body fat of 79 adult badgers; closed circles represent means, vertical lines represent ±2 SE.](image3)

![Fig. 4.—Seasonal changes in bone marrow fat for 79 adult badgers; closed circles represent means, vertical lines represent ±1 SE.](image4)
activity over a greater number of hours per day (1600–0600 MST) with an average heart rate of 150 beats/min (0.96 cm³/g·h) (fig. 9). During the winter 1978–1979, continuous telemetry signals were received for only one of the two badgers remaining constantly below ground. During this time, the heart rate was only occasionally elevated above 55 beats/min (0.27 cm³/g·h). In addition, on 30 occasions the badger entered torpor which was characterized by a drop of 9°C in body temperature and a 50% reduction in heart rate (fig. 10). Entrance into hypothermia was gradual, taking about 15 h at 0.55°C drop/h. Torpor, characterized by a body temperature of approximately 28°C and a heart rate of 21–30 beats/min, persisted an average of 8 h. Arousal was characterized by an almost simultaneous elevation of the heart rate and body temperature. Warming of the body was more rapid than cooling, taking only about 4 h at a rate of 2.22°C/h. The average cycle of torpor lasted 29 h from the initial reduction in heart rate to the end of arousal (defined as the return to a resting heart rate of 55 beats/min).

**DISCUSSION**

Conductance is an exponential function of body weight and can therefore be predicted from the general formula: $C = 1.02 W^{-0.305}$ (Herreid and Kessel 1967). The observed value of 0.01225 cm³/g/h/°C was 16% higher than the predicted value of 0.01027 cm³/g/h/°C for a 9.0 kg animal. Gettinger (1975) found low values of conductance for fossorial animals and expressed this as an adaptation for preventing excessive heat loss. McNab (1966), however, characterized fossorial rodents as having high conductance as a means of limiting the heat load incurred during active digging. It is difficult to explain the high conductance values observed for the temperate-zone badger during winter in terms of the need to dissipate heat, but it may indeed be

![Fig. 5.—Average burrow temperatures and average minimum weekly above-ground temperatures, December through March 1977–1978; temperatures were measured 1.5 m within and 6 cm above the entrance of two burrows.]

![Fig. 6.—Average daily time above ground for four adult badgers within outdoor enclosures, November 1977 through April 1978; brackets represent ±1 SE.]
associated with the thermal buffering effect of the burrow. The coyote, Canis latrans, is generally nonfossorial and, as a result, is exposed to cold temperatures for longer periods than the badger during the winter. Insulation of the badger is significantly lower \( P < .005 \); \( F^* \)-statistic of error sum of squares [SSE] [Neter and Wasserman 1974, p. 163]) than insulation calculated from data presented by Shield (1972) on coyotes similarly tested (fig. 1). Conditions associated with burrows (see Swan 1974) could reduce winter thermal stress to the badger and therefore be correlated with a higher thermal conductance (lower insulation).

The BMR of badgers is 30% below that predicted by Iverson's (1972) equation for mustelids and 14% below that predicted by Kleiber's (1975) equation for an animal of its body mass. The low rate of metabolism could be associated with problems of balancing an energy budget with limited energy reserves (McNab 1966). For example, squirrels, which reduce their energy requirements by hibernating, deplete only about 66% of their fat reserves through the winter (Fisher and Manery 1967). Badgers likewise deplete only about half of their fat stores during winter. In addition, bone marrow fat, which is used as an indicator of an animal's condition (Cheatum 1949; Franzmann and Arneson 1976), showed no significant depletion by March, indicating that badgers still had adequate fat reserves. These large fat deposits at the end of winter may be a result of low energy requirements caused by the badger's behavioral avoidance of cold temperatures and its low metabolic rate.

In the present study, oxygen consumption and heart rate were highly correlated, and the curve fell midway between those obtained by Lampe (1976) from two female badgers on a treadmill. Heart rate was therefore used to estimate metabolic ex-

\[ Y = 0.053 + 0.0045X \]

**Fig. 7.**—Least-squares regression line of heart rate and oxygen consumption for two badgers at rest and at different stages of activity.

**Fig. 8.**—Changes in the time spent above ground \( (A) \) and changes in heart rate \( (B) \) by badgers during February 1978. Time spent above ground for four badgers is expressed in fractions of an hour and represents hourly values averaged for the month; brackets represent \( \pm 1 \) SE. Symbols represent sunrise and sunset. Heart rate of two badgers is expressed as the monthly average over 1-h periods; vertical lines represent the range.
penditures of badgers monitored in field enclosures. By correlating heart rate to \( V_{O_2} \) and using a conversion factor of 4.8 kcal/1 O\(_2\), we calculated the daily energy expenditure for a 15-h rest (65 beats/min), 9-h active (90 beats/min) cycle for badgers during February 1978 as 322 kcal/day. This increased to 480 kcal/day in March with an 11-h activity period. Lampe (1976) calculated that, during the summer, the badger must detect, pursue, and consume 1.7 gophers (418 kcal) each day in order to balance energy expenditures. Badgers during the 1977–1978 winter in Wyoming may have augmented their nutrient requirements through predatory activity. This is implied by the presence of daily foraging activity within the enclosures and by only moderate fat utilization, as indicated by carcass analysis of field animals. The more severe 1978–1979 winter, however, was associated with prolonged restriction below ground by badgers within the enclosures. These animals had a daily energy expenditure of 240 kcal, which is about 25% lower than that observed in February of the previous year and 13% below the BMR calculated in the laboratory.

In a study of the European badger, Johansson (1957) showed that many aspects of the animal's annual cycle are similar to those of hibernators. In addition, Slonin (1952) observed an instability of body temperature and metabolism in the European badger during winter similar to that observed in bears. More definitively, the

![Fig. 9.—Changes in the time spent above ground (A) and changes in heart rate (B) by badgers during March 1978. Time spent above ground for four badgers is expressed in fractions of an hour and represents hourly values averaged for the month; brackets represent ±1 SE. Symbols represent sunrise and sunset. Heart rate of two badgers is expressed as the monthly average over 1-h periods; vertical lines represent the range.](image)

![Fig. 10.—Body temperatures (A) and average heart rate (B) of a badger entering, within, and arousing from torpor during December and January 1978–1979. The lines depicting entrance to and arousal from torpor describe least-squares regressions of body temperatures. Heart rate is expressed as the average over 1-h periods; vertical lines represent the range.](image)
present study has demonstrated the ability of the American badger to enter a state of shallow torpor. Induction into torpor may be in response to cold temperatures and food deprivation. It appears that the badger utilizes its ability for short-term hypothermia only during the coldest months of winter. In addition, Harlow (1979a) showed that badgers fasted 30 days had a 22% reduction in basal metabolism. Therefore, both factors may be acting in concert to cause the badger to go hypothermic.

Body temperature and metabolism during the torpor cycle are close to predicted values. For example, Swan (1974) characterizes torpor by a reduction in metabolism along a temperature coefficient (Q10) slope of about 2.0. The badger had a Q10 of 2.15 as its metabolism dropped from 0.26 cm3/g·h at 37 C to 0.13 cm3/g·h at 28 C. In addition, animals with Q10 values near 2.0 are characterized by a 7.18% drop in VO2, per °C (Morrison 1960). From this relationship, the predicted VO2 of a badger that dropped its body temperature 9 C would be 0.130 cm3/g·h, which closely approximates the 0.133 cm3/g·h calculated from heart rate while in torpor. Assuming a specific heat of tissue to be 0.82 kcal/kg/°C (Hart 1951), it would require 59.8 kcal to raise the temperature of an 8-kg animal by 9 C. It required 60.2 kcal to bring the badger's temperature from 28 C to 37 C, very close to the predicted expenditure. However, the 4 h required for this arousal were 1.5 h longer than predicted by the formula: °C/min = 2.035-0.04 (Bartholomew 1972). It has long been known that small heterothermic mammals warm up more rapidly than large ones. As a consequence, Pearson (1960) believes that large mammals cannot afford the time necessary to enter and emerge from torpidity each day. Torpor, however, was observed in the badger only during the cold months of December and January and did not occur every day. Periods of lowest body temperature varied in length from 6 to 18 h with an average 29-h torpor cycle from entrance to the end of arousal. In addition, normothermic periods were not characterized by foraging activity but by states of rest or sleep. As a consequence, the time required for the badger to arouse is insignificant as long as the torpor cycle provides an energy saving. Energy expenditure during the 29-h torpor cycle required 220 kcal for an 8-kg animal. Entry into torpor accounted for 26% of the total energy spent in the torpor cycle, and torpor itself accounted for 31.5%. The remaining 42.5% was used during arousal. If the badger slept continuously with a heart rate of 55 beats/min for the same period, it would expend 300 kcal. Therefore, torpor provided the badger a 27% energy savings or 8.5 g of fat during the period of an average cycle. This would amount to a total of 255 g of fat, which would allow the badger an extra 10 days of rest without food during early spring to act as a buffer against bad weather and food scarcity.

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