Numerical and parametric study of the yield stress limits of reinforcement bars in clay block masonry structures

Estudo numérico e paramétrico sobre o limite da tensão de escoamento da armadura na alvenaria estrutural de blocos cerâmicos

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Abstract: The Brazilian Standard Structural Masonry considers for the maximum tensile stress ($f_s$) of the reinforcements embedded in the grout in clay blocks with smooth surfaces several limits of the yield stress for the reinforcement ($f_{yk}$). This work aims to analyze the limits of the yield stress of reinforcement bars in clay block masonry structures by numerical and parametric analysis in push-out and pull-out tests, varying the type of grout and reinforcement diameter. A numerical study was performed using a 3D-model with the DIANA® software based on the Finite Element Method. The parametric study confirmed that the limits obtained in this research for reinforcement diameter of 8 mm, 10 mm, 12.5 mm and 16 mm are in agreement with the limits specified by the Brazilian Standard, with exception of the 20 mm diameter, which limit was lower than indicated by the Standard. The tensile stress limits of the embedded reinforcement progressively reduce with increasing rebar diameter, being the failure is dominated by the bond strength of the block/grout interface.

Keywords: yield stress, bond strength, block/grout interface, finite element, clay blocks.

Resumo: A norma brasileira de alvenaria estrutural considera para a tensão máxima de tração das armaduras ($f_s$) embutida no graute em blocos cerâmicos com superfícies lisas vários limites da tensão de escoamento do aço ($f_{yk}$). Este trabalho teve como principal objetivo analisar os limites da tensão de escoamento das armaduras inseridas na alvenaria estrutural de blocos cerâmicos por meio de análises numéricas e paramétricas em corpos de provas push-out e pull-out, variando o tipo de graute e diâmetro das armaduras. O estudo numérico dos modelos analisados foi feito pelo Método dos Elementos Finitos utilizando o pacote computacional FX+DIANA®. A análise paramétrica confirmou que os limites obtidos nesta pesquisa para armaduras com diâmetros de 8 mm, 10 mm, 12.5 mm e 16 mm estão em concordância com os especificados pela norma brasileira, com exceção da armadura de 20 mm de diâmetro, cujo limite ficou menor que o apontado pela norma. Dessa maneira, a tensão de escoamento da armadura embutida no graute diminui progressivamente com o aumento do diâmetro das barras, sendo a falha dominada pela tensão de aderência da interface que se cria entre as paredes dos blocos cerâmicos e o graute.

Palavras-chave: tensão de escoamento, tensão de aderência, interface bloco/graupe, elementos finitos, blocos cerâmicos.

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1 INTRODUCTION

Structural masonry is an important structural system that has significantly evolved over the years. Buildings have become increasingly tall, reaching 20 floors. Furthermore, the taller the building, the larger the compression levels and vertical loads that are attributed to wind action and torsion. In structural masonry, compression is usually resisted by filling the vertical holes with grout (liquid concrete with small aggregate), which increases the resistance of the masonry to compression [1].

With respect to traction on the walls, reinforcement bars that are properly coated with grout are generally used to solidify the compound because the resistance of masonry is low. Reinforcements are a solution to increase the tensile strength and thus improve the mechanical behavior of masonry under lateral loading [2].

When a wall is subjected to lateral action, one of its sides is compressed, whereas the other is subjected to traction. Under these conditions, internal tensions are observed on the grout/block interfaces because of the different deformation properties. By analyzing the internal components of the grout/block contact plane, it can be concluded that rupture is caused by slippage near the plane [3].

Soric and Tulin [4] concluded that two types of bond should be considered when evaluating the performance of reinforced masonry: the bond between reinforcing steel and grout, and the bond between the grout and internal faces of the concrete unit. The bond that can be developed between the reinforcement and surrounding grout is a complex phenomenon that is dominated by the interlocking action of the reinforcing bar ribs in the grout mass. However, the bond between the grout and surrounding masonry unit is primarily limited by the adhesion with the interface.

1.1. Justification

Regarding the tension on the walls, because of the low resistance of masonry, reinforcement bars that are properly coated with grout are generally used to solidify the whole structure. International reference standards, such as British BS 5628-2 [5], European EC6-1 [6] and Australian AS 3700 [7], present an indirect limit for the maximum reinforcement diameter embedded in a grouted hole. However, the Brazilian Standard of Structural Masonry ABNT NBR 16868-1 [8] imposes limits directly for the maximum tensile stress (f_t) of the reinforcements and maximum reinforcement rate in a grouted hole.

The Brazilian Standard of Structural Masonry ABNT NBR 16868-1 [8] suggests that in clay blocks whit smooth surface the maximum tensile stress of the reinforcement embedded in the grout cannot be larger than the yield stress (f_yk) for 10 mm rebar diameters, 75% of its yield stress (0.75 f_yk) for 12.5 mm rebar diameters and 50% of its yield stress (0.5 f_yk) for 16 mm or more rebar diameters. This request is relevant for high rise buildings and for buildings in high-intensity seismic zones. Therefore, the present study is mainly to verify the need to establish such limits.

A better understanding of the behavior of structural masonry requires research on the block/grout interface, especially considering that wind loads become substantial for tall buildings causing significant traction on the bracing walls.

Sipp [9] studied the properties that affect the adherence between 5 types of ceramic blocks and two types of grouts. The push-out test was used to evaluate the bond strength mobilized by the combination of these different materials. In addition, the pull-out test was also employed for some block types, seeking a more realistic analysis of the bonding behavior on masonry elements. The results obtained in the push-out test prove that there is a wide variation in the results, depending on the type of block and grout employed. Some of the main characteristics that influenced these results were the shape of the block cells and the shrinkage of the grout. In the case of grout, the use of grout with higher compression resistance was responsible for the reduction in the results of the push test, precisely due to the reduction in the contact area caused by the shrinkage of the filler material.

Guarnieri [10] analyzed the influence of the structural ceramic block/grout adhesion on the mechanical behavior of the assembly in order to determine a value of adhesion tension. The author concluded that the grout/ceramic block adhesion is superior to the mechanical tensile strength of the ceramic block and, therefore, the rupture of the assembly will occur first in the block.

In this regard, Izquierdo et al. [11] studied the behavior of the block/grout interface of concrete and clay block masonry. Their study concluded that there is a good bond between the internal faces of the concrete blocks and grout, enough to prevent infill-slippage, and that the whole tensile strength of the usual reinforcement bars is achieved provided they are properly anchored. Nevertheless, for clay blocks, there is low bond between the interface of the clay blocks and grout, allowing for infill-slippage before the reinforcement bars reach their yield stress. In this way, numerical modeling of masonry structures can effectively be useful for better understanding of the mechanical behavior of masonry elements for scenarios different from those tested in the laboratory [2]. Therefore, this paper aims to
investigate the block/grout interface in clay blocks and verify the limits on the yield stress of the reinforcement by performing experimental and numerical tests, thereby enabling a parametric analysis. This study intends to draw the attention of technologists to the importance of ensuring the homogeneity of masonry by considering the bond to be a study parameter of the grout.

2 EXPERIMENTAL INVESTIGATION

This experimental investigation studied the masonry behavior using push-out specimens to determine the bond strength between the grout and clay unit, and pull-out specimens to study the behavior of the interface of the grout/block/reinforcement set. One type of block material (clay), two types of grout (large and small compressive resistance) and two rebar diameters (12.5 mm and 16 mm) were considered.

These laboratory tests were preceded by a set of material characterization tests. Statistical tests (Student's t test) were applied to evaluate the differences of the experimental results at a 5% significance level, for a better understanding of the results.

A detailed description of the experimental results was presented by Izquierdo et al. [11]. Figure 1 and Figure 2 show the nominal dimensions and test rig of the push-out and pull-out specimens, respectively. The experimental tests were carried out on servo-hydraulic universal machine INSTRON brand, model 8506, and the reading of the data was done with SYSTEM 5000 acquisition system.

Two series were built with six specimens for each series for the push-out test:
- Series ClG14: Clay block and grout G14
- Series ClG30: Clay block and grout G30
Four series were built with six specimens for each series for the push-out test:

- Series ClG14S12: Clay block, grout G14 and rebar diameters 12.5 mm
- Series ClG30S12: Clay block, grout G30 and rebar diameters 12.5 mm
- Series ClG14S16: Clay block, grout G14 and rebar diameters 16 mm
- Series ClG30S16: Clay block, grout G30 and rebar diameters 16 mm

Complementary tests were performed to characterize the masonry: compressive strength testing of cylindrical mortar specimens, cylindrical grout specimens, and units. The specimens were rectified to obtain regular and smooth surfaces.

The mean of the compressive strength for grout G14 and G30 used for filling the clay blocks was 14.18 MPa and 31.43 MPa, respectively. Grout G14 was designed to be weaker than grout G30.

The reinforcement rebars were subjected to tensile strength tests. Three 12.5 mm and 16 mm steel rebar samples were submitted to direct tensile tests. Table 1 shows the results obtained on the reinforcements used in clay blocks. The yield stress was calculated according to ABNT NBR 6892-1 [12].

### Table 1. Results of the steel reinforcements Ø 12.5mm and Ø 16 mm used in clay blocks.

| Diameter rebar (mm) | Area of reinforcement cross section (mm²) | Mean Ultimate Load (kN) | Mean Yield Load (kN) | Mean Ultimate Stress (MPa) | Mean Yield Stress (MPa) |
|---------------------|------------------------------------------|-------------------------|----------------------|---------------------------|------------------------|
| 12.5                | 125                                      | 93.32                   | 65.55                | 760.43                    | 534.15                 |
|                     |                                          | S.D                     | 1.30                 | 1.94                      | 10.58                  | 15.77                  |
|                     |                                          | C.V (%)                 | 2.95                 | 1.39                      | 2.95                   | 15.77                  |
| 16                  | 200                                      | 159.86                  | 117.32               | 795.05                    | 583.52                 |
|                     |                                          | S.D                     | 1.91                 | 3.28                      | 9.52                   | 16.30                  |
|                     |                                          | C.V (%)                 | 2.79                 | 1.20                      | 2.79                   | 2.79                   |

S.D: Standard Deviation. C.V: Coefficient of Variation

The bond strength was determined by dividing the maximum load applied by the area of the internal cavity surface of the unit. The average value of this area was 0.072 m². The results of the push-out tests are displayed in Table 2.

### Table 2. Results of the push-out tests [11].

| Series   | Mean Ultimate Load (kN) | S.D   | C.V (%) | Bond Strength (MPa) | S.D   | C.V (%) |
|----------|-------------------------|-------|---------|---------------------|-------|---------|
| ClG14    | 11.64                   | 1.32  | 11.31   | 0.16                | 0.02  | 8.87    |
| ClG30    | 14.02                   | 1.24  | 8.87    | 0.19                | 0.02  | 8.87    |

S.D: Standard Deviation. C.V: Coefficient of Variation

Table 3 shows the maximum stress of the pull-out clay block specimens for the four series. Figure 3 presents the results of the pull-out loads and the reference values of the yield load and the ultimate load, both obtained in the simple tensile test of the rebars, according to Izquierdo et al. [11].

### Table 3. Results of the pull-out of clay block specimens [11].

| Series   | Mean Ultimate Load (kN) | S.D   | C.V (%) | Mean Ultimate Stress (MPa) | S.D   | C.V (%) |
|----------|-------------------------|-------|---------|---------------------------|-------|---------|
| ClG14S12 | 48.47                   | 1.14  | 2.36    | 394.95                    | 9.31  | 2.36    |
| ClG30S12 | 59.26                   | 7.42  | 10.51   | 482.91                    | 50.75 | 10.51   |
| ClG14S16 | 48.96                   | 1.76  | 3.60    | 243.49                    | 8.76  | 3.60    |
| ClG30S16 | 60.11                   | 5.11  | 8.50    | 298.94                    | 25.40 | 8.50    |

S.D: Standard Deviation. C.V: Coefficient of Variation
The pull-out specimens built with reinforcement of 12.5 mm and 16 mm diameter reached an ultimate load less than the yield load of the referred bar. The maximum load of the specimens with the same type of grout obtained similar values. The Figure 3 shows that the failure of the pull-out specimens was determined by the type of grout.

Izquierdo et al. [11] concluded that the bond load between the grout and clay block was 11.64 kN for grout G14 and 14.02 kN for grout G30, for a single grouting block. These loads multiplied by the number of grouting blocks used in the pull-out specimens (4 blocks) set important limits related to the grout/block bond. These values can be compared with the ultimate loads obtained in the pull-out tests, as shown in Table 4.

The results in Table 4 show that the ultimate loads of pull-out tests were approximately equal to the extrapolated limits of the push-out tests. The statistical analysis showed that these limits are not significantly different. Therefore, the pull-out specimens breached before the reinforcement bars reached its yield strength.

3 NUMERICAL MODEL

The numerical model applied to the study of the block/grout interface in the clay block masonry structures was defined using the Fx + DIANA® software program [13].

The numerical analysis was performed by two steps. In the first step, the validation of the numerical model was carried out based on the experimental results. The second step included a parametric analysis varying the rebar diameters on the pull-out specimens (8 mm, 10 mm and 20 mm).

The simplified micro-model was using in this study. Some researchers adopted micro-modeling approaches to study masonry as they represent its complex behavior very well. Mortar and two unit-mortar interfaces are lumped into a zero-thickness joint (modeled using an interface element) between expanded masonry units [2], [14], [15].

The Quasi-Newton iteration method (Secant) and a displacement convergence norm was used in the DIANA® software to solve the three-dimensional finite element model adopted in the push-out and pull-out specimens.

3.1 Finite Element Mesh

The mesh was composed of a HX24L solid element to represent the masonry units, grout and a TP18L solid element to represent the steel reinforcement (Figure 4). A Q24IF interface element was employed to represent the block/grout interface, grout/reinforcement interface and bed joints. The Q24IF element is an interface element between two planes...
in a three-dimensional configuration (Figure 5), suitable for three-dimensional models. Each node of this element has three degrees of freedom and the element is based on linear interpolation and Gaussian integration.

![Figure 4. (a) HX24L solid element of the units and grout and (b) TP18L solid element of the steel reinforcement used in the numerical modeling [13].](image1)

![Figure 5. Q24IF interface element [13].](image2)

The mesh convergence was done satisfactorily with three different refinement levels to evaluate its influence on the results. Table 5 and Table 6 show the number and size elements of the final mesh of the push-out tests and pull-out test, respectively.

### Table 5. Number and size elements of the push-out mesh.

|                       | Clay block | Grout | Block/grout interface |
|-----------------------|------------|-------|-----------------------|
| Elements number       | 1260       | 462   | 180                   |
| Size of elements (mm) | 10x10x40   | 10x10x40 | 40x10          |
| Subtotal              | 1722       |       | 180                   |
| Total                 | 1902       |       |                       |

### Table 6. Number and size elements of the pull-out mesh.

|                       | Clay block | Grout | Reinforcement | Block/grout interface | Grout/reinforcement interface | Bed joints masonry |
|-----------------------|------------|-------|---------------|-----------------------|-------------------------------|-------------------|
| Elements number       | 5040       | 1848  | 500           | 720                   | 180                           | 252               |
| Size of elements (mm) | 10x10x40   | 10x10x40 | 10x10x200   | 40x10                 | 10x200                        | 10x10             |
| Subtotal              | 7388       |       | 1152          |                       |                               |                   |
| Total                 | 8540       |       |               |                       |                               |                   |
3.2 Loading and Boundary Conditions

The push-out specimens consisted of a single clay block with one of its cavities completely grouted. The salient grout from the surface of the block at a distance of 30 mm was loaded in compression through a bearing plate at the top surface, while the block was supported only around the perimeter of the unit shells at the bottom surface. The pull-out specimens were built with four clay blocks in stack bond. The 4 blocks were grouted. The reinforcement rebar was subjected to a tensile load [11].

Similarly to the experimental tests (see Figure 1c and Figure 2c), the boundary conditions used in the push-out and pull-out specimens were restrictions of the displacements in the Z direction at half of the nodes of the bottom block. Two nodes of the symmetry axis were restricted in the X, Y, and Z directions to avoid numerical instability.

In the case of the push-out specimens, vertical displacements were imposed on all nodes of the top of the grout (Figure 6a), and in the case of the pull-out specimens, vertical displacements were imposed on all nodes of the base of the reinforcement rebar (Figure 6b). The boundary conditions and loading were similar in the experimental tests.

3.3 Constitutive Models and Mechanical Properties

Total Strain Crack Model was used to characterize the crack distribution and nonlinear behavior of both the units and grout. According to the DIANA® software [13], this model describes the tensile and compressive behavior of the material with one stress-strain relationship in a coordinate system that is fixed upon crack initiation. Exponential and parabolic constitutive laws were used to describe the tensile and compressive behavior of clay masonry units respectively, as shown in Figure 7a and Figure 7b. The shear behavior during cracking was described via a shear retention model defined by a constant, see Figure 7c [16].

![Figure 6](image)

**Figure 6.** Vertical displacements of the (a) push-out and (b) pull-out specimens.

![Figure 7](image)

**Figure 7.** Mechanical behavior of the units used in numerical modeling: (a) tension, (b) compression, and (c) shear [13].
The mechanical properties are presented in Table 7 for masonry units and two types of grout and were determined during the characterization tests as presented by Izquierdo [11]. However, some properties that could not be obtained experimentally were calibrated by adjusting the numerical results with the experimental results. All mechanical properties units were considered in relation to its net area. The calibrated properties (indicated in the Table 7) were obtained according to Haach [16], Izquierdo [17], fib [18], Haach et al. [19], Diógenes [20] and Izquierdo [21].

**Table 7.** Mechanical properties of the Total Strain Crack Model (masonry units and grout).

| Parameters                                | Symbol/Units | Clay block   | Grout G14    | Grout G30    |
|-------------------------------------------|--------------|--------------|--------------|--------------|
| Elastic modulus (exp)                     | E (MPa)      | 9876.43      | 20521.17     | 29719.67     |
| Poisson (exp)                             | $\nu$        | 0.20         | 0.20         | 0.20         |
| Tensile strength (exp)                    | $f_t$ (MPa)  | 1.08         | 1.43         | 2.35         |
| Fracture energy for Mode I (cal)          | $G_f$ (MPa·mm)| 0.06         | 0.03         | 0.06         |
| Compressive strength (exp)                | $f_c$ (MPa)  | 30.92        | 14.18        | 31.43        |
| Fracture energy under compression (cal)    | $G_c$ (MPa·mm)| 5.51         | 3.19         | 5.57         |
| Shear retention (cal)                     | $\beta$      | 0.5          | 0.5          | 0.5          |

Experimental properties (exp). Calibrated properties (cal)

The model used for interface elements indicate that the block/grout interface and bed joints masonry was an interface cap model. This model was proposed by Lourenço and Rots [22], and further enhanced by Van Zijl [23] with modern plasticity concepts. This interface material model, also known as the “Composite Interface model” or “Cracking-Shearing-Crushing Model”, is appropriate to simulate fracture, frictional slip, and crushing along material interfaces, which are possible failure modes of masonry interfaces. The model includes a tension cut-off model to capture Mode I failure, a Coulomb friction envelope to describe Mode II failure and a cap model for compressive failure (Figure 8) [2], [24], [25].

![Constitutive model for masonry interfaces](image)

**Figure 8.** Constitutive model for masonry interfaces [22] adapted from Haach [16].

Table 8 shows the mechanical properties used for the Composite Interface Model of the block/grout interface and bed joints masonry. Most properties were obtained experimentally according to Izquierdo [17] and Oliveira [26]. Other properties (indicated in the Table 8) were obtained by calibrating the numerical and experimental model with similar raw material compositions based on previous work as Haach et al. [19], Oliveira [26], Capuzzo et al. [27] and Rahman and Ueda [28].

The normal stiffness ($k_n$) was calculated based on the results of the direct tensile tests carried out to characterize the tensile bond strength of the unit-mortar. The shear stiffness ($k_s$) was obtained through the results of the shear tests carried out on triplet specimens to characterize the shear behavior of clay unit-mortar interface interface [16], [19], [29].

Elasto-plastic behavior was adopted for the reinforcements through the yield criterion of the Von Mises model. These properties were obtained experimentally as presented by Izquierdo et al. [11]. Table 9 shows the mechanical properties used in this model.
Table 8. Mechanical properties of the Composite Interface Model (block/grout interface and the bed joints masonry).

| Parameters                                | Symbol/Units | Block/grout interface | Block/grout interface | Bed joints masonry |
|-------------------------------------------|--------------|-----------------------|-----------------------|-------------------|
| Normal stiffness (exp)                    | $k_n$ (MPa/mm) | 1.00                  | 1.00                  | 11.71             |
| Tangential stiffness (exp)                | $k_t$ (MPa/mm) | 1.76                  | 1.19                  | 11.71             |
| Cohesion (exp)                            | $f_v$ (MPa)  | 0.16                  | 0.19                  | 0.20              |
| Friction coefficient (exp)                | $\tan \phi$ | 0.70                  | 0.70                  | 0.250             |
| Dilatancy coefficient (exp)               | $\tan \Psi$ | $1.00 \times 10^{-4}$ | $1.00 \times 10^{-4}$ | 1.723             |
| Residual friction coefficient (exp)       | $\tan \phi_r$ | 0.39                  | 0.39                  | 0.29              |
| Confining normal stress (exp)             | $\sigma_u$ (MPa) | $-1.18$               | $-1.18$               | $-1.37$           |
| Exponential degradation coefficient (cal)  | $\delta$     | 1.85                  | 1.85                  | 0.29              |
| Tensile strength (exp)                    | $f_t$ (MPa)  | 0.23                  | 0.23                  | 0.29              |
| Fracture energy for Mode I (exp)          | $G_{fI}$ (MPa·mm) | 0.02                  | 0.02                  | 0.02              |
| Fracture energy for Mode II (exp)         | $G_{fII}$ (MPa·mm) | 0.19                  | 0.24                  | 0.22              |
| Cap critical compressive strength (exp)   | $f_c$ (MPa)  | 3.15                  | 3.15                  | 3.05              |
| Shear traction control factor (cal)        | $C_s$        | 4.00                  | 4.00                  | 4.00              |
| Compressive fracture energy (cal)         | $G_{fc}$ (MPa·mm) | 1.18                  | 1.18                  | 5.00              |

Experimental properties (exp). Calibrated properties (cal)

Table 9. Mechanical properties used for the Von Mises model (reinforcement).

| Parameters                                | Symbol/Units | Ø 12.5 mm | Ø 16 mm |
|-------------------------------------------|--------------|-----------|---------|
| Elastic modulus (exp)                     | $E$ (MPa)    | 198513.12 | 200844.39 |
| Poisson (cal)                             | $\nu$        | 0.30      | 0.30    |
| Yield stress (exp)                        | $f_y$ (MPa)  | 556.24    | 588.60  |

Experimental properties (exp). Calibrated properties (cal)

The grout/reinforcement interface was considered in the linear regime with $k_n = 5$ MPa/mm and $k_t = 100$ MPa/mm.

4 VALIDATION OF THE NUMERICAL MODEL

The calibration of the numerical model was performed based on the comparison between the numerical and experimental results and failure modes.

4.1 Push-Out Tests

Figure 9 shows a comparison between the experimental and numerical behavior of the push-out tests corresponding to the CIG14 series and Figure 10 for the CIG30 series. Figure 11 displays the grout slippage of the numerical and physical models of the CIG14 series.

![Figure 9. Validation of numerical results of the CIG14 series of push-out tests: (a) force vs displacement diagrams and (b) mean maximum load.](image-url)
Figures 9 and 10 showed that the numerical model adequately predicts the same response of experimental push-out tests. The maximum difference between both models was less than 2%. Therefore, it can be said that the numerical push-out model was calibrated.

Figure 11 shows that the numerical model characterizes the performance of the physical push-out model.

4.2 Pull-Out Tests

Figure 12 to Figure 15 show a comparison of the experimental and numerical behavior of the pull-out tests for the ClG14S12, ClG14S16, ClG30S12 and ClG30S16 series, respectively.
Figure 13. Validation of numerical results of the ClG14S16 series of pull-out tests: (a) force vs displacement diagrams and (b) mean maximum load.

Figure 14. Validation of numerical results of the ClG30S12 series of pull-out tests: (a) force vs displacement diagrams and (b) mean maximum load.

Figure 15. Validation of numerical results of the ClG30S16 series of pull-out tests: (a) force vs displacement diagrams and (b) mean maximum load.

The numerical behavior for the ClG14S12, ClG14S16, ClG30S12 and ClG30S16 curves were similar to the physical model. The maximum difference between experimental and numerical model was less than 6% in all series. Therefore, it can be said that the numerical pull-out model was calibrated.

Grout slippage was observed in all of the tested numerical and experimental series (see Figure 16).
5 PARAMETRIC ANALYSIS

After the validation of the numerical model, a parametric analysis was performed for the pull-out test varying the rebar diameters of the steel reinforcement (8 mm, 10 mm and 20 mm) and two types of grout (large and small compressive resistance).

Steel rebar samples of the 8 mm, 10 mm and 20 mm diameter were submitted to the direct tensile test described by Kataoka and El Debs [30] under the same test conditions of the reinforcement rebars of this study (12.5 mm and 16 mm). The yield load obtained for the 8 mm steel rebar was 31.01 kN, the 10 mm steel rebar was 44.94 kN and the 20 mm steel rebar was 178.19 kN.

5.1 Rebar Diameters of 10 mm

Figure 17a is the load vs displacement diagram of the numerical model for the series with G14 and G30 grout and rebar diameters of 10 mm. The experimental yield is also highlighted in the Figure 17a.

As shown in Section 2, the bond load between the grout and clay block was 11.64 kN for G14 grout and 14.02 kN for G30 grout, for a single grouting block (see Table 1). These loads, multiplied by the number of grouting blocks used in the pull-out specimens (4 blocks), established important limits related to the grout/block bond. The value for the G14 grout was 46.56 kN and for the grout G30 was 56.12 kN.

Figure 17b is the maximum load for these two series (41.11 kN and 41.26 kN) compared with the values of the load limited by bond obtained experimentally (46.56 kN for G14 and 56.08 kN for G30).

Figure 16. Displacement of the grout according to (a) the numerical model and (b) physical model of the CIG14S12 series.

Figure 17. Pull-out tests with rebar diameters of Ø10 mm (a) parametric results (load vs displacement diagrams) and (b) maximum load.
The maximum loads obtained in the numerical model was 41.11 kN and 41.26 kN for ClG14S10 and ClG30S10 series, respectively. These values represent a maximum difference of 9% in relation to experimental yield load of the 10 mm steel rebar (44.94 kN). This difference can be considered low since simplifications and approximations are used in the numerical model. Therefore, both yield loads (experimental and numerical) were considered the same.

The numerical model stopped converging once these values were reached. Figure 17a illustrates that the grout did not slip in relation to the clay block webs for 10 mm of rebar diameters.

Figure 17b shows that the ultimate load numerical (41.11 kN and 41.26 kN) was lower than the load limited by experimental bond for both grouts (46.56 kN and 56.08 kN), respectively. Therefore, this research concluded that the failure for pull-out specimens of 10 mm steel rebars was dominated by the yield load of the reinforcements and not by bond load.

The pull-out test with 8 mm steel rebars was not carried out numerically because the experimental yield load for this reinforcement was 31.01 kN. This value is less than the load limited by experimental bond for both grouts (46.56 kN and 56.08 kN). For that reason, the failure will be due by the yield stress of the steel bar and not by the bond strength of the clay block/grout interface.

5.2 Rebar Diameters of 20 mm

Figure 18 shows the results obtained in the parametric study using rebar diameters of 20 mm.

The ultimate numerical load for both series (48.12 kN and 60.46 kN) were similar than their respective experimental load limited by bond (46.56 kN and 56.08 kN). The maximum difference between experimental and numerical load was of about 8%. The other hand, the experimental yield load (179.19 kN) of 20 mm of steel rebar diameter was significantly larger than the numerical load for both series (48.12 kN and 60.46 kN). Therefore, the reinforcement of Ø 20 mm embedded in both series has not reached its yield limit.

Figure 18a shows that the column of the grout inside the clay blocks slipped for both grouts. Therefore, with the use of 20 mm diameter rebar, the effect was the same as the 12.5 mm and 16 mm reinforcement rebars, where the masonry limit state depends on the bond strength of the block/grout interface for the specific grout type.

5.3 Comparative analysis according to Brazilian Standard Structural Masonry ABNT NBR 16868-1 [8]

The parametric study provides a summary of the ultimate stress of the pull-out test of clay blocks based on the yield stress of the steel bar, for several reinforcement diameters, see Table 10.
Table 10. Ultimate stress of the pull-out tests of clay blocks with respect to the yield stress of the steel rebar for different diameters.

| Rebar Diameters (mm) | G14     | Ultimate Stress | G30     |
|----------------------|---------|----------------|---------|
| Ø 8                  | 100% $f_{yk}$ | 100% $f_{yk}$ |
| Ø 10                 | 100% $f_{yk}$ | 100% $f_{yk}$ |
| Ø 12.5               | 74% $f_{yk}$  | 90% $f_{yk}$  |
| Ø 16                 | 42% $f_{yk}$  | 51% $f_{yk}$  |
| Ø 20                 | 27% $f_{yk}$  | 33% $f_{yk}$  |

As previously mentioned, the Brazilian Standard Structural Masonry ABNT NBR 16868-1 [8] imposes limits directly for the maximum tensile stress ($f_s$) of the reinforcement embedded in the grout in clay blocks with smooth surfaces. These limits are:

- $f_{yk}$ for steel rebars of Ø10 mm
- 0.75 $f_{yk}$ for steel rebars of Ø12.5 mm
- 0.50 $f_{yk}$ for steel rebars of Ø16 mm or more.

The limits obtained in this research (Table 10) are in agreement with the limits specified by the Brazilian Standard for 10 mm, 12.5 mm and 16 mm reinforcement diameter. However, the limits for 20 mm of diameter (27% $f_{yk}$ and 33% $f_{yk}$) do not coincide with the limit of the Brazilian Standard (50% $f_{yk}$). This research concluded that these limits reduce progressively with increasing rebar diameter. The other hand, more studies need to be done and the bond stress at the grout/block interface should be considered during the design development to guarantee safety.

6 CONCLUSIONS

In this paper a numerical analysis was performed to analyze the limits of the yield stress of reinforcements in clay block masonry structures. The parametric analysis was carried out by varying the rebar diameter (8 mm, 10 mm, and 20 mm) and type of grout (large and small compressive resistance) in pull-out specimens.

The following conclusions are:

- The numerical analysis showed that the computer models of the push-out and pull-out specimens adequately represented the behavior of the physical models, and thus can be used in parametric analysis.
- The pull-out tests with rebar diameters of 8 mm and 10 mm showed that the reinforcements embedded in the grout reached their yield stress without slippage. This feature demonstrated that the anchorage length used in this work was appropriate. The grout did not slip in relation to the clay block webs.
- The pull-out tests with clay blocks, large and small compressive resistance grout and reinforcement bars with diameters of 12.5 mm, 16 mm and 20 mm showed slippage of the grout's column before the reinforcement rebars achieved their yield stresses. The failure was dominated by the lack of a sufficient bond strength of the clay block/grout interface.
- The limits achieved in this research for 8 mm, 10 mm, 12.5 mm and 16 mm diameters bars are in agreement with the limits specified by the Brazilian Standard Structural Masonry ABNT NBR 16868-1 [8]. However the limit for steel rebars with 20 mm of diameter was less than specified by the standard. The authors of this paper suggest 25% $f_{yk}$ for Ø20 mm as a reference point for future investigations, while a comprehensive research program covering the bond between different clay blocks and grout infills is not performed.
- Two types of bond strengths that occur in the reinforced masonry should be considered during the design: grout/reinforcement bond and block/grout bond.

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