A Category Theory Framework for Sense Systems

David Strohmaier*, Gladys Tyen*†
University of Cambridge
{david.strohmaier, gladys.tyen}@cl.cam.ac.uk

Abstract
Sense repositories are a key component of many NLP applications that require the identification of word senses, a task known as word sense disambiguation. WordNet synsets form the most prominent repository, but many others exist and over the years these repositories have been mapped to each other. However, there have been no attempts (until now) to provide any theoretical grounding for such mappings, causing inconsistencies and unintuitive results. The present paper draws on category theory to formalise assumptions about mapped repositories that are often left implicit, providing formal grounding for this type of language resource. We introduce notation to represent the mappings and repositories as a category, which we call a sense system; and we propose and motivate four basic and two guiding criteria for such sense systems.

Keywords: Sense Repositories, Word Sense Disambiguation, Category Theory

1. Introduction
Sense repositories are a key language resource for word sense disambiguation (WSD), semantic inference, specifying lexical relations, and other downstream tasks like question answering. For these purposes, researchers have created many sense repositories with varying levels of granularity, along with mappings between them. In particular, the popular WordNet synsets [Miller et al., 1990] [Fellbaum, 1998] have been mapped to many coarser-grained repositories. The value of systematically mapped repositories has been repeatedly shown [Navigli, 2006] [Palmer et al., 2007]. However, the particular characteristics of the mappings produced are often the byproduct of practical or engineering decisions, instead of being motivated by theoretical considerations. For example, clustered senses are restricted to one cluster per sense, whereas senses that are mapped to domain labels do not have this restriction and are often associated with multiple labels. Additionally, the lack of constraints on mappings often results in problems during implementation. For example, converting sense labels in a corpus from one type to another (e.g. synsets to domain labels) is not always consistent, because sometimes there are several correct labels.

The present paper provides the theoretical grounding to allow for more systematic understanding of mappings and how they might assist researchers in solving tasks such as WSD. As far as we know, no such theory has been proposed before. Our contributions are twofold:

1. Drawing from category theory, we formalise mapped sense repositories as a category which we call a sense system; and
2. Using category theoretic notation, we propose and formally describe criteria for such a sense system.

We hope that future researchers building or adapting sense repositories and mappings will find it useful to consider how their new language resource fits into our framework, and adjust their methodology accordingly. In the following sections, we first discuss the existing literature on sense repositories and mappings between them. We then introduce sense systems and present the surrounding category-theoretic notation. With these foundations in place, we propose and provide motivation for basic and guiding criteria for such sense systems.

2. Previous work
2.1. Word Sense Disambiguation
As suggested, word sense disambiguation (WSD), i.e. picking the correct sense of a word in a context, is one of the most prominent uses of sense repositories. Typically, a WSD classifier selects from a pre-determined and enumerative repository of candidate senses [Navigli, 2009]. Different NLP techniques for WSD have been developed over the years, including approaches based on lexical similarity, graphs, and supervised learning. Lesk [1986] offers an influential lexical similarity approach, which uses a) the overlap between context of the word to be disambiguated, and b) the dictionary entry of candidate senses, in order to select a sense. Graph-based approaches make use of the graph structure of some sense repositories such as WordNet and BabelNet to select senses [Moro et al., 2014].

In recent years, machine learning has become the dominant approach. WSD is treated as a supervised classification task, where a trained model selects from a pre-determined list of senses. Earlier methods depend on extracting feature vectors [Zhong and Ng, 2010] [Mihalcea and Faruque, 2004], while later methods make

* Both authors contributed equally.

† We refrain from using the term word sense disambiguation system in this paper to avoid any confusion with sense systems.
use of word embeddings (Mikolov et al., 2013) and shifted towards neural approaches (Kågebäck and Salomonsson, 2016; Vial et al., 2019; Wiedemann et al., 2019), giving rise to some of the best performing models in WSD. Word embeddings have also been used as features for non-neural machine learning methods (Iacobacci et al., 2016), as well as more traditional lexical similarity approaches (Oele and Noord, 2017).

2. Clusters of senses are obtained by grouping fine-grained senses by various metrics, which typically approximate semantic similarity. For example, the semantic relations encoded in WordNet have been used to cluster WordNet synsets (Peters et al., 1998; Vial et al., 2019; Izquierdo et al., 2007). Similarly, Dolan (1994) clustered definitions from the LDOCE according to semantic information extracted from the dictionary. Agure and Lacalle (2003), working on clustering WordNet synsets, investigated 4 different sources of information to measure similarity: topic signatures, confusion matrices, translation equivalences, and the context of occurrence.

Senses within a cluster can be represented as dictionary definitions, embedding vectors, or otherwise — crucially, there is no unified way of determining its semantic content, as it often depends on the clustering technique. For example, clusters that are formed from hypernym/hyponym relations have explicit, shared semantic content, because each cluster member is a hyponym of the highest level hypernym. In other cases, such as WordNet synsets clustered according to confusion matrices, there may not be any semantic content explicitly associated with each cluster.

3. Domain labels are very coarse-grained senses represented by a word or short phrase that denotes a topic domain, such as biology, economics, etc. Domain label repositories aim to cover the largest semantic space with the fewest possible domain labels (Lacerra et al., 2020; Izquierdo et al., 2007). Mappings to domain labels can be determined manually, automatically, or both. For example, Magnini and Cavaglia (2000) began with a small set of manual annotations, then extended...
them automatically based on a semantic hierarchy. Camacho-Collados and Navigli (2017) produced their mappings according to similarity metrics and other heuristics, then evaluated a subset according to manual annotations. Many dictionary repositories like WordNet and the LDOCE also comes with manually annotated domain labels.

Unlike clusters, there is no way to ensure that all fine-grained senses can be mapped to a substantive domain, so a miscellaneous or “catch-all” label is sometimes used for un categorised senses. For example, the WordNet Domains Hierarchy (Benivogli et al., 2004) contains the label “factotum” for when no better label is available. Additionally, it is possible for fine-grained senses to be mapped to multiple domain labels.

4. Embedding vectors represent senses as a dense vector. Early word embedding techniques like Word2Vec (Mikolov et al., 2013) produce one embedding per word type, but later techniques such as ELMo (Peters et al., 2018) and BERT (Devlin et al., 2019) can be used to produce contextualised embeddings, which are effectively very fine-grained senses. Scarlini et al. (2020a; Scarlini et al., 2020b) have also created embeddings for WordNet synsets.

2.3. Mapping sense repositories

Most work on mapping sense repositories is motivated by a common concern: that WordNet synsets are too fine-grained to achieve reasonable results on the WSD task (Ide and Wilks, 2007; Lacerra et al., 2020). Some researchers advocate for multiple levels of grain, so that downstream applications are free to select the level as appropriate. For example, Palmer et al. (2004) employ WordNet synsets, synset groupings, and frame sets as three repositories at different levels of grain. It has been argued that there is no single correct repository of senses that is independent of the use case (Kilgarriff, 2003).

It has been established that using multiple mapped repositories can improve the performance on the WSD task, demonstrating the practical value of mappings. Navigli (2006) clustered WordNet synsets based on partial mappings to the Oxford Dictionary of English, and showed that this mapping-based clustering improved the performance on the WSD task. Similarly, Palmer et al. (2007) showed that the possibility of back ing off to coarse-grained sense groups improves WSD, further supporting the usefulness of mapping sense repositories of different grain.

None of this work, however, provides general theoretical grounding and restrictions for the mappings between multiple sense repositories. Formal features such as the transitivity of mappings are more often the result of practical exigencies and methodological choices rather than theoretical motivations. For example, some WordNet synsets were mapped to the Coarse Sense Inventory (CSI) indirectly via BabelDomains (Lacerra et al., 2020), suggesting that sense mappings are transitive. The present paper will make such implicit assumptions explicit using category theory.

3. Formal notation for a sense system

We introduce the term sense system to denote an interconnected system of sense repositories and mappings. We represent a sense system as a small category $S$, where the object set of $S$, denoted by $\text{Ob}(S)$, is a set of sense repositories; and the homomorphism set or hom-set of $S$, denoted by $\text{Hom}(S)$, is a set of mappings between these repositories. The set of mappings from repository $R$ to repository $R'$ in $S$ is denoted by the hom-set $\text{Hom}_S(R, R')$. The general hom-set $\text{Hom}(S)$ is the union of all these repository-specific hom-sets.

Note that each $R$ in $\text{Ob}(S)$ only contains senses – other information such as word type exists separately (see Section 4.1.2) and we make no assumptions about the form or content of the senses themselves. Our sense system representation will be applicable regardless of whether the senses are dictionary definitions, embeddings, domain labels, or otherwise.

As a category, $S$ has the following two properties:

1. $\text{Hom}(S)$ is closed under function composition. If, in $\text{Hom}(S)$, $R$ is mapped to $R'$ and $R'$ is mapped to $R''$, then there must be some composite mapping that maps $R$ to $R''$ in $\text{Hom}(S)$.

2. Each repository in $\text{Ob}(S)$ has an identity function $id$ in $\text{Hom}(R, R)$ mapping $R$ to itself.

Both of these properties are trivially fulfilled by the common understanding of sense mappings. We conceptualise each mapping as a way of converting a label from one repository to another label from another repository. For example, if WordNet synsets are mapped to WordNet Domains, one could take a corpus like SemCor (Landes et al., 1998), which is labelled with WordNet synsets, and convert the synset labels to Domain labels.

Since there can be multiple ways of converting, in principle multiple mappings from one repository to another can coexist. For example, the WordNet 2.0 synset for amethyst is linked to three WordNet Domain labels, as seen in Figure 2. When encountering the word amethyst in SemCor, one could select a label randomly, or according to some arbitrary order, or by frequency, etc. Each of these methods would correspond to a different mapping between the two repositories.

Mappings in $\text{Hom}(S)$ have the following properties:

1. Mappings are unidirectional. A mapping from $R$ to $R'$ does not entail a mapping from $R'$ to $R$. While this property is often assumed, it is not always made explicit. For example, WordNet
synsets are often mapped to domain labels or clusters that are coarser-grained, making it impossible to reverse the mapping. Therefore, repositories are typically mapped from finer-grained ones to coarser-grained ones, not vice versa. Bidirectional mappings would only be possible between repositories that are of equal grain and mapped one-to-one to each other, e.g. when embeddings are created specifically for WordNet synsets (Scarlini et al., 2020a).

2. Mappings are not multivalued. That is, each mapping in \( \text{Hom}_S(R, R') \) maps each sense in \( R \) to at most one sense in \( R' \), though multiple senses in \( R \) can be mapped to the same sense in \( R' \).

This is consistent with the idea that mappings represent a way of converting labels (as suggested above), because each conversion method takes one input and gives only one output.

3. Mappings are total functions. A mapping from \( R \) to \( R' \) ensures that all senses in \( R \) are mapped to at least one sense in \( R' \).

In practice, there are some cases where mappings are not total. For example, Navigli (2006) partially mapped WordNet synsets to definitions in the Oxford Dictionary of English, leaving synsets that are not mapped to any ODE senses. There may also be repositories that were built for a reduced vocabulary, such as dictionaries for learners, or repositories that only contain certain types of words, such as English verbs (Green et al., 2001).

For the purposes of this theory, we follow Navigli (2006), Navigli and Ponzetto (2012), etc. and use \( \epsilon \) as a null value, so senses that are not mapped to anything are instead mapped to \( \epsilon \).

The category theoretic properties described in this section will be assumed throughout this paper. Formalising a sense system as a category posits very minimal assumptions about sense repositories and their mappings, and should therefore be applicable to most existing sense systems. However, such a flexible representation of sense systems is not very informative. Previous work on mapping repositories often impose further assumptions, resulting in sense systems that are more useful and informative. In the following sections, we formally describe these assumptions and formulate them as basic and guiding criteria for sense systems.

4. Basic criteria for sense systems

In this section, we formalise and motivate 4 basic criteria for sense systems. These criteria capture linguistic intuitions that are often implicitly assumed, while simultaneously accounting for downstream application concerns.

1. Correctness preservation: Mappings should preserve the correctness of sense labels in all contexts.

Intuitively, if the correct sense for a word token is mapped to another sense, this sense should also be correct. To formalise this criterion, we postulate the existence of a WSD oracle \( \Omega \), which evaluates to 0 or 1 depending on whether a given word token in a usage context has a given sense. Note that \( \Omega \) makes no assumption about the number of correct senses.

We formalise the preservation of correctness as follows:

\[
\forall R, R' \in \text{Ob}(S) \\
\forall m \in \text{Hom}_S(R, R') \\
\forall s \in R \\
\forall t \in T \\
\Omega(t, s) = 1 \Rightarrow \Omega(t, m(s)) = 1
\]

where \( t \) denotes any given word token from the set of tokens \( T \) covered by both \( R \) and \( R' \).

2. Candidacy preservation: Mappings should preserve the lexical candidacy of sense labels.
To introduce the concept of candidacy, we distinguish word types from word tokens: word tokens are words in a usage context; word types, also known as a lemma, refer to the abstract notion of a word, and is independent of morphological variants.

We postulate that word types exist separately for each repository $R$ as the set $W_R$, which are mapped to senses in $R$ like in a dictionary, i.e. each word type is associated with a set of candidate senses. We formalise this dictionary function as $d_R : W_R \rightarrow \mathcal{P}(R)$, where $\mathcal{P}(R)$ denotes the power set of $R$.

For a sense $s$ in $R$ to be a candidate for a word type $w$, the dictionary function $d_R$ must map $w$ to a set that contains $s$. For example, in WordNet 3.1, the word *manuscript* is mapped to the set of two synsets: “the form of a literary work submitted for publication”, and “handwritten book or document”. Both of these senses are candidates of *manuscript*.

Having introduced the dictionary function, candidacy preservation can then be formulated as follows: if a sense $s$ that is a candidate for a word type $w$ is mapped to another sense, that sense must also be a candidate for $w$. Formally,

\[
\forall R, R' \in \text{Ob}(S), \quad \forall w \in (W_R \cap W_{R'}), \quad \forall m \in \text{Hom}_S(R, R') \quad s \in d_R(w) \Rightarrow m(s) \in d_{R'}(w)
\]

### 3. Uniqueness criterion: There should be at most one mapping from one repository to another.

The uniqueness criterion states that for each pair of repositories $R$ and $R'$, there is at most one mapping from $R$ to $R'$, and at most one mapping from $R'$ to $R$, making $S$ a posetal or thin category. Note that this criterion is direction-sensitive, so for each pair of repositories, there can be at most two mappings, one in each direction. For example, SensEmBert embeddings are mapped one-to-one to WordNet synsets, and vice versa. This criterion prevents WordNet embeddings from being mapped to a different WordNet synset, or vice versa. Formally:

\[
\forall R, R' \in \text{Ob}(S) \quad |\text{Hom}_S(R, R')| = 1
\]

### 4. Connectivity: A sense system should be a connected category.

The connectivity criterion states that $S$ is a connected category, i.e. all repositories in $\text{Ob}(S)$ and their mappings in $\text{Hom}(S)$ must form a single connected graph. For example, WordNet synsets are mapped to CSI labels, but neither are mapped to or from, say, the *Macmillan English Dictionary*. This means that the sense system formed by these three repositories does not fulfil the connectivity criterion.

Formally, for any two repositories $R$ and $R'$ in $\text{Ob}(S)$, there is a sequence $R = R_0, R_1, R_2, \ldots R_n = R'$ where $(R_0, \ldots, R_n) \in \text{Ob}(S)$, and for each $i$ up to (but not including) $n$, there is at least one mapping in either $\text{Hom}_S(R_i, R_{i+1})$ or $\text{Hom}_S(R_{i+1}, R_i)$.

### 4.1. Motivation

#### 4.1.1. Correctness preservation

This criterion is endorsed by virtually all existing mappings. Without this assumption, existing mappings would be unusable. Nonetheless, repositories occasionally contain errors, particularly ones which are automatically mapped. Because of this, manual annotations are more highly valued (Pradhan and Xue 2009), while automatically mapped repositories are often evaluated afterwards to reveal errors. For example, [Seppala et al. (2016)](#) checked their automatically generated mappings against their manually identified mappings for medicine-related words, and discovered that only 85% were correctly identified automatically. They also found two “obvious mistakes” made during manual annotation, which were promptly corrected.

Since mappings are not multivalued (section 3), preserving correctness allows us to cross-check labelled data for any inconsistencies. Using the word *mouse* as an example, one annotator or classifier might select the WordNet synset referring to the rodent, and another might select the WordNet Domain label of “computer science”. Since the rodent synset is not mapped to “computer science”, we know (by *modus tollens*) that there was a disagreement between the two annotators/classifiers, even though they make use of different sense repositories.

Note that the correctness preservation is only defined with respect to the selection of the correct sense, but does not place any restrictions on candidacy and word type.

#### 4.1.2. Candidacy preservation

Candidacy preservation is intuitive from a semantic perspective. If a word sense $s$ is mapped to a semantically more encompassing word sense $s'$, it must be the case that this broader sense is also a candidate. This criterion is trivially fulfilled by clustering-based approaches, but is not typically explicitly stated for repositories.

A violation would only occur if an instance of a word type could carry the sense $s$ without also being able to carry $s'$ in any context. Such a violation would suggest that $s'$ has some semantic specificity that $s$ lacks. For example, the WordNet synset mind.n.01 (with the gloss definition “that which is responsible for one’s
thoughts and feelings; the seat of the faculty of reason” is a candidate sense for the word types brain, head, psyche, and nous. If this synset is mapped to a domain label called “anatomy”, it would be a violation of candidacy preservation, because “anatomy” is not a candidate sense for “psyche” or “nous”. Relatedly, candidacy preservation is required for a straightforward way of comparing granularity levels for each word type: by counting the number of senses. For example, WordNet 3.1 contains 42 senses for head, while the online Oxford Learner’s Dictionary contains 20. If we map all of WordNet’s synsets to OLD entries and preserve candidacy, we can postulate that the 20 senses are coarser-grained than the 42 in WordNet. On the other hand, if we do not preserve candidacy, it may be the case that semantic content was lost in applying the mapping, and hence the fewer senses of the Oxford Learner’s Dictionary might not be more coarse-grained, but just leave semantic gaps.

4.1.3. Uniqueness

For many existing mappings that were produced through clustering (Dolan, 1994; Vial et al., 2019), the uniqueness criterion is assumed implicitly, because each sense can belong to at most one cluster. The same is true for embedding-based senses that are mapped one-to-one to a dictionary-based repository. However, there are other types of mappings that do not fulfill this criterion. As mentioned in Section 3, WordNet Domains maps the synset for amethyst to the domains of “chemistry”, “geology”, and “jewellery”. Similarly, the Coarse Sense Inventory (CSI) (Lacerra et al., 2020) maps the synset for abattoir to “craft, engineering, and technology”, “art, architecture, and archaeology”, and “food, drink, and taste”. We argue that enforcing the uniqueness criterion provides several benefits:

1. Repositories in S would form a partial preorder, which would roughly correspond to the notion of granularity. Since mappings are total and cannot be multivalued, the range (or image) of the mapping must have cardinality less than or equal to that of the domain. The cardinality thus reflects a notion of granularity that is measured numerically.

2. There would be more consistency when converting between labels. For example, Izquierdo et al. (2007) mapped each WordNet synset to one Base Level Concept (BLC), so one could consistently convert from the former to the latter. A WSD tool or downstream application that uses BLC-annotated corpora can automatically make use of a WordNet-annotated corpus such as SemCor (Landes et al., 1998), because the labels can be directly converted into BLCs.

3. In a similar vein, evaluation metrics that depend on converted labels would be more reliable. A WSD classifier using BLCs can easily be evaluated according to SemCor, because there is only one correct BLC that each word is mapped to. On the other hand, if WordNet synsets are mapped to multiple BLCs, it is not clear how the classifier should be evaluated. The BLCs might all be considered correct, resulting in inflated scores; or if a random one is chosen, the scores may not accurately reflect the classifier’s performance.

4. In conjunction with function composition (see Section 3), the uniqueness criterion would also enforce transitivity. Consider WordNet synsets, WordNet topics, and WordNet Domains in Figure 1 if the mappings between these repositories fulfill the uniqueness criterion, there would only be at most one mapping between each repository, as in Figure 3. Under function composition, \( n \circ m = p \) (where \( n, m, \) and \( p \) correspond to mappings in Figure 3).

One might argue that the domain labels for amethyst and abattoir should not be interpreted as separate labels, but instead as a set containing all relevant domains; so one would map WordNet synsets to the power set of CSI or Domain labels. However, adapting classifier models (for WSD or otherwise) to handle multiple labels instead of one is not always straightforward, so ideally a sense system should only contain sets of senses, not sets of sets of senses. Another practical solution is to designate one main CSI or Domain label for each WordNet synset, so that all conversions and comparisons will be made according to one label. This main label could be chosen based on inter-annotator agreement or frequency or another metric, as long as it is consistent across all synsets. Other non-designated labels can still be made available for classifiers that can handle multiple labels.

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This correspondence of course only applies to the range, but not the whole co-domain. In practice, mappings are usually surjective (so the co-domain is the range) — exceptions are limited to newer or more specialised vocabulary. For example, English WordNet (https://en-word.net/) contains the definition of dab that refers to the dance move, which is not in Princeton WordNet 3.1.
4.1.4. Connectivity

Previous work on WSD have focused on building mappings between repositories rather than a complete sense system, so connectivity is rarely assumed. However, in the few cases where more than two repositories were mapped (Gella et al., 2014; Palmer et al., 2004), the resulting sense systems do fulfil the connectivity criterion.

The connectivity criterion on its own is not very informative, but it enables other criteria by extending their benefits to the rest of the sense system. After all, an unconnected sense system technically fulfils all the other criteria in this paper, but is not very useful. As mentioned above, the previous three criteria each had their own practical and theoretical benefits: 1) correctness preservation allowing cross-checking; 2) candidacy preservation allowing comparison of grain level; and 3) uniqueness allowing consistent label conversion. If the connectivity criterion is fulfilled, these benefits can be extended to any two repositories in \( \text{Ob}(S) \).

With a sufficient number of repositories in \( \text{Ob}(S) \), one can leverage these benefits on a larger scale, opening up new opportunities for WSD research. For example, ensemble classifiers based on different sense repositories can be built: if there are three WSD classifiers that use senses from \( R, R' \), and \( R'' \) respectively, their outputs can be aggregated and cross-checked, as long as \( R, R', \) and \( R'' \) are connected to each other in a single graph.

5. Guiding criteria for sense systems

While all criteria listed in this paper are desirable for various reasons, the basic criteria are ones which can be fulfilled both in theory and in practice, while the guiding criteria may be impossible to fulfil in certain situations, and should be considered more as approximate guidelines than strict criteria. In addition to the 4 basic criteria, we propose two additional guiding criteria:

1. Non-contradiction: Mappings cannot exist between senses that semantically contradict each other.

The non-contradiction criterion forbids mappings between senses whose (strict) implications contradict each other. Examples of such contradictions can easily be found in the literature: the word monograph has (at least) two fine-grained senses, one referring to the physical printed volume by an author, another referring to the abstract piece of work instantiated by such a volume. These two senses might be mapped to one coarse-grained sense in a different repository, where it is categorised as a physical object. Thus arises a contradiction where the fine-grained sense referring to the abstract work is mapped to a coarse-grained sense referring to a physical object.

We formalise the non-contradiction criterion as follows:

\[
\forall R, R' \in \text{Ob}(S) \\
\forall m \in \text{Hom}_S(R, R') \\
\forall s \in R \\
s \models P \Rightarrow \neg(m(s) \models \neg P)
\]

where \( \models \) indicates strict entailment and \( P \) is any proposition.

Note that the correctness criterion does not entail the non-contradiction criterion. In the monograph example, the mapping fulfils the correctness preservation because a WSD oracle would consider the coarse-grained sense to be correct, despite the contradiction.

2. Inter-annotator agreement: Mappings should correspond to a partial preorder of inter-annotator agreement levels.

It has been observed that, when annotating corpora with senses from a given sense repository, inter-annotator agreement tends to drop when the repository is more fine-grained (Ng et al., 1999;Navigli, 2009). Therefore, if \( R \) is coarser-grained than \( R' \), one can expect agreement levels to be higher when annotating corpora with senses in \( R \), compared to \( R' \).

We formalise this criterion as follows:

\[
\forall R, R' \in \text{Ob}(S) \\
(\exists m \in \text{Hom}_S(R, R')) \Rightarrow (a(R) \leq a(R'))
\]

where \( a \) refers to the inter-annotator agreement, defined by \( a : \text{Ob}(S) \rightarrow \mathbb{R} \). \( \exists m \in \text{Hom}_S(R, R') \) means that there is at least one mapping from \( R \) to \( R' \).

5.1. Motivation

5.1.1. Non-contradiction

Non-contradiction is considered a guiding criterion because, while it is desirable, it is also a difficult criterion to meet. Firstly, some sense representations (such as embeddings) do not come with explicit semantics, so it would be impossible to determine if their implications contradict one another. Secondly, semantic implications are often subtle and difficult to identify: even WordNet, a repository known for its fine-grained senses, does not distinguish the two senses in the monograph example above.
However, mappings that do meet the non-contradiction criterion can be useful in downstream tasks that require natural language inference, such as question answering or information extraction. For example, with the correct sense labels, an information extraction tool could eliminate the possibility of an abstract book having the same referent as a physical monograph. Alternatively, mappings that do not meet the criterion might cause errors in these downstream applications. For the question “When was this monograph created?”, a question-answering system might incorrectly assume the physicality of the object in question, and describe the time when the monograph was printed instead of when the text was written.

Some sense repositories that are formed through clustering techniques do not contain any semantic content. For example, clustering WordNet synsets based on confusion matrices (Agirre and Lacalle, 2003) would create clusters that are not explicitly associated with a label or definition. These mappings trivially fulfil the non-contradiction criterion. However, there are also clustering techniques where this criterion does apply: for example, Navigli (2006) makes use of the hierarchical semantic structures in the Oxford Dictionary of English to cluster WordNet synsets. As a result, the clusters produced are associated with a textual definition and other semantic information.

5.1.2. Inter-annotator agreement

We previously demonstrated that mapped repositories in a posetal sense system (fulfilling the uniqueness criterion) form a partial preorder of granularity. If the inter-annotator agreement criterion is fulfilled, mapped repositories would also form a partial preorder of inter-annotator agreement levels. This criterion is considered a guiding criterion because, unlike basic criteria, it cannot be directly enforced — researchers have no reason to artificially inflate or lower inter-annotator agreement. Additionally, this criterion cannot be applied to sense representations that are not used for human annotation, such as word embeddings. Nevertheless, this criterion not only reflects existing expectations for a sense system, but strong violations suggest that the sense distinctions of the coarse-grained sense repository are unnatural, i.e. not in accordance with human linguistic intuitions, since the annotators appear to struggle more despite a reduction in labels.

6. Conclusion

This paper develops a representation of sense systems as categories, and proposes a list of criteria that serve as guidelines for future sense repositories and mappings. The list is by no means exhaustive, as there are other properties that may be desirable depending on the downstream application. A sense system that fulfills our list of criteria brings multiple benefits and opportunities to the WSD task: not only does it provide theoretical grounding for sense mappings, it also opens up other opportunities to improve existing WSD tools, such as extending them to ensemble classifiers that can croscheck annotation from multiple sense repositories.

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