of memory as the previous block. The initial capacity can be any power of two.

The upper level of the array consists of atomic pointers, as allocating new buckets needs to occur atomically. The lower level consists of atomic integers, as the values of the elements need to be changed atomically.

Note that the arrays on the second level of the data two-level are implemented as std::vectors. These vectors exist only to specify initial size at runtime as opposed to compile time. The size never changes after initialization, and each vector is treated as a normal array on any subsequent accesses.

A. Progress and Correctness Guarantees

Like [1], our data structure provides a lock free progress guarantee and linearizable correctness property. The linearization points of our implementation are in similar places to those of [1] and [2]. All of the following specified lines are in parallel_vector.cpp. For pushback, line 178 under normal circumstances and line 162 if the vector does not have any elements left to pop. For popback, line 541 under normal circumstances and line 483 if the operation is completed in the combining phase. The vector is also lock free because at each of these linearization points, a CAS is attempted. If the current thread fails the CAS, by the definition of CAS [8], some other thread must have linearized a different operation at this time. At least one thread is making progress at all times, so our data structure must be lock free.

B. Synchronization Techniques

The key synchronization techniques used to provide these guarantees are atomic compare and swap (CAS) operations, descriptors, and the combining queue. CAS allows us to guarantee lock free progress using low level atomic instructions. Even if a particular CAS fails and we must return to the top of a loop, lock free progress is still guaranteed, because a CAS failure implies that another thread's CAS succeeded [8]. Descriptors allow us to provide the lock free guarantee for multiple variables at a time by using CAS on pointers instead of word-sized primitives [2]. Finally, the fixed sized combining queue maintains this guarantee by allowing every active operation to both add items to an open queue and assist with the combining phase, guaranteeing that all operations in the queue will complete, even if a particular thread is starved of computing time [1].

C. Modifications

We made a few changes to the implementation described by [1] for our own convenience.

- The value INT_MIN (from the climits package) is reserved to mean “marked” (or “logically removed”) in the underlying data storage. A node is marked by setting its value to INT_MIN, instead of bit stealing.
- The size of the first bucket is 2, changed from 8 in [2].

D. Improvements

To attempt to improve the vector, we made several additional modifications. First, in addition to keeping a thread-local copy of the size of the vector as described in the vector, we also keep a thread-local copy of the capacity of the vector. Our reasoning for why this might improve the performance of the vector is as follows: both pushback and combine check whether a new bucket needs to be allocated each time they attempt to insert a new item into the vector. To do this, they load the bucket where the new item would go from the shared vector and check whether the bucket is currently equal to null. This creates a point of contention and often times is unnecessary, especially as the size of the vector grows (since the bucket size doubles for each new bucket allocated, it is less frequent that a new bucket actually does need to be allocated as the vector becomes larger). To alleviate some of this contention in cases where it is obviously unnecessary to allocate a new bucket, we have each thread store a thread-local copy of the capacity, then, to check whether a new bucket needs to be allocated, the thread first checks the value of the thread-local copy of capacity and compares it to the index it would be inserting at next. If the index is smaller than capacity, then we know that a new bucket definitely does not need to be allocated (since the vector can never shrink in capacity, the thread-local value of capacity is a lower bound on the actual capacity of the vector). Otherwise, the thread loads the value of the bucket from the shared vector and checks if it is null in the same manner as before. We implement this modification by updating the thread-local copy of capacity every time a thread attempts to allocate a bucket. As stated above, the thread-local value of capacity is a lower bound on the actual capacity of the vector, and the thread still loads the bucket from memory when it thinks it may need to allocate a bucket, so this modification has no effect on the correctness of the vector.

Another way we attempted to improve performance was by updating the thread-local value of size in several places in addition to the locations described in [1]. Having a thread-local copy of a value be more consistent with the actual value makes it less likely for the actual value to be loaded unnecessarily. In [1], the thread-local copy of size is updated on read operations, write operations, and other places that modify the vector. We extend that to potentially updating the thread-local value of size any time a value from the vector is read at any point during execution. This includes several points in pushback and popback that were not included in [1] (to our knowledge, based on the pseudocode and explanations given). For example, the thread-local value of size is potentially updated any time a write descriptor is created. Our logic for this is as follows: if the value read from the vector is marked, that means that the index that was read from is greater than (or equal to) the actual size of the vector. Thus, if that index is smaller than the current value of the thread-local copy of size, then we know the index is a closer estimate to the actual size of the vector than the current value of thread-local copy is, and we should set
the thread-local value of size to the index. Since the thread-local copy is used only as an optimization in [1] (its value is only used for bounds-checking, and if a given index seems out of bounds when compared to the thread-local copy of size, the actual size of the vector is loaded to confirm), this modification has no effect on the correctness of the vector.

E. Advantages and Disadvantages

The major advantage of this implementation over other lock free implementations is its greatly improved performance compared to other resizable arrays that support pushback and popback. (More details are available in the performance section.) The major disadvantage of this implementation is shared by many other lock free data structures: it is quite complex. Even when compared to its close relative [2], the code doubles in length. Additionally, implementing this data structure in a practical environment requires the use of a non-standard lock free memory management solution.

F. Difficulties

While we eventually created a working implementation of the paper’s vector, we did encounter some roadblocks, due to the following issues.

- The code is very complex. The four most important methods (pushback, popback, AddToBatch, and Combine) are all quite long, with a lot of if-statements. This makes following the flow of the program difficult.
- The pseudocode has very few comments. Additionally, while the authors do explain how each method works, these explanations are not always detailed enough.
- Some things, like when to update the thread-local copy of size, are not included in the pseudocode and are only briefly mentioned in the explanations of the methods.
- The variable names are short, which makes understanding what their purpose is difficult.
- Some parts of the methods are omitted from the pseudocode, presumably for brevity. For example, the explanation of Combine mentions that the global combining queue should be nullified. However, this step is not present in the pseudocode.

IV. TRANSACTIONAL IMPLEMENTATION

For the Software Transactional Memory (STM) version of the vector, we used the Rochester Software Transactional Memory (RSTM) C++ library. To accomplish this, we first developed a sequential version of the vector described in [1] (i.e., the vector is implemented as a two-level array to avoid having to move elements upon re-sizing). Then, we replaced all operations on the shared vector with their transactional equivalents, allowing the vector to be shared across multiple threads in a thread-safe manner.

When testing our STM implementation, we varied the transaction size, which is defined as the number of operations completed in a single transaction. Initially, we set the transaction size to 1 and then increased the transaction size to 2 and then 4. There are various reason why the transaction size can affect the performance of a shared object that utilizes STM. With smaller transaction sizes, a transaction is less likely to fail since it is accessing less memory locations (and, thus, it is less likely to have to restart the transaction), so this can result in better performance. However, larger transaction sizes can have performance benefits as well. There is less overhead in creating and executing one large transaction as opposed to creating and executing many small transactions. The ideal transaction size can also be affected by the system the program is run on and the behavior of the program itself. We compare and explain the results across the different transaction sizes for our vector in the Performance section.

A. Improvements

Originally, when implementing the STM version of our vector, we simply placed the sequential versions of the methods in atomic blocks and replaced all operations on shared memory with their transactional equivalents. In our second iteration, the first modification we made was moving code that does not need to be executed atomically to outside of the atomic blocks. For example, calculating the indices in the two-level array that corresponds to a given index does not need to be calculated in the atomic block. Code in atomic blocks may need to be executed many times (if the transaction fails), so leaving this code in the atomic block can lead to repeated, unnecessary computation. The second modification we made was that, if a variable is being modified multiple times within an atomic block, we modified the code to only call “TM_WRITE” on that variable once at the end of the block. Having these extra writes in the atomic block leads to more shared memory accesses than are necessary. For example, when reserving space in the vector, the value of capacity is incremented each time a new bucket is allocated. Instead of writing this value each time it is incremented, we store the new value in a local variable, then write the value of capacity at the very end of the atomic block.

V. PERFORMANCE

The results for our concurrent and transactional implementations are shown in Fig. 1. We test each version of the vector with 1, 2, 4, and 8 threads and record the average time to execute 500,000 operations. We use three different operation ratios: (25% pushback, 25% popback, 25% read, 25% write); (60% pushback, 20% popback, 10% read, 10% write); and (40% pushback, 20% popback, 40% read, 0% write). For the STM version of the vector, we use transaction sizes of 1, 2, and 4 operations. All tests were run on a virtual machine running Ubuntu 18.04, using g++ version 7.3.0 as the C++ compiler.

As can be seen in Fig. 1, our concurrent implementation generally scaled very well as the thread count increased, especially compared to the STM implementation. One reason for this is that STM implementations generally do not scale well compared to other concurrent implementation. As the number of threads (and, thus, contention) increases, threads have to abort and restart transactions more often. The concurrent implementation, however, utilizes the combining queue.
described in [1], which is specifically designed to improve performance under high contention.

When comparing our unmodified (“LF V (U)”) and modified (“LF V (M)”) versions of our concurrent implementation, the modifications we introduced seemed to significantly improve performance, as our modified vector (whose modifications are described in Section III-D) scales much better than our unmodified vector. This could be due to the reduced contention on the vector as a result of introducing the thread-local copy of the vector’s capacity.

For the unmodified (“STM V (U)”) and modified (“STM V (M)”) versions of our STM implementation, our modifications generally seemed to improve performance as well. This is likely due to removing unnecessary accesses to shared memory and reducing repeated computation, as described in Section IV-A.

The performance of the STM vector was generally best with a transaction size of 1, although the difference is not significant. This is likely because aborts at higher transaction sizes are more costly than at lower transaction sizes, since more memory locations are being accessed in each transaction. This difference is more pronounced at higher thread counts, where higher contention causes aborts to be more likely.

VI. CONCLUSION

In [1], Walulya and Tsigas present a highly scalable vector. The cost of this performance boost is the resulting complexity of the code. We implement our own version of the lock-free vector with combining and add modifications to attempt to improve its performance. We then compare the performance of our implementations to a Software Transactional Memory (STM) implementation of the vector. The performance of these two versions of the vector is comparable at very low thread counts, but the lock-free vector with combining significantly outperforms the STM

Fig. 1. Performance results for different implementations with pushback, popback, random access write, and random access read.
vector at higher thread counts. This is likely due to the lock-
free vector’s use of a combining queue in order to alleviate
contention.

ACKNOWLEDGMENT

Very special thanks to Dr. Walulya for answering our questions about implementing his data structure.

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