A Physics-Based Attack Detection Technique in Cyber-Physical Systems: A Model Predictive Control Co-Design Approach

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Abstract—In this paper a novel approach to co-design controller and attack detector for nonlinear cyber-physical systems affected by false data injection (FDI) attack is proposed. We augment the model predictive controller with an additional constraint requiring the future—in some steps ahead—trajectory of the system to remain in some time-invariant neighborhood of a properly designed reference trajectory. At any sampling time, we compare the real-time trajectory of the system with the designed reference trajectory, and construct a residual. The residual is then used in a nonparametric cumulative sum (CUSUM) anomaly detector to uncover FDI attacks on input and measurement channels. The effectiveness of the proposed approach is tested with a nonlinear model regarding level control of coupled tanks.

I. INTRODUCTION

Industrial cyber-physical systems play a crucial role in critical infrastructures and everyday life. Cyber-physical systems (CPSs) are constituted of physical processes (plants) communication and computation. Some examples of CPS include power grids, intelligent transportation systems, water distribution systems, aerospace systems, retail supply chain, etc. which are all based on safety critical processes [3]. Both cyber and physical components of a CPS are vulnerable to malicious attacks. Security of CPSs is of paramount importance to societies and governments. This importance has fueled a considerable research in the recent past; see survey papers [3], [4], [6], [7], [9], [20] and references therein. In general there are two possible approaches in attack detection: i) Information Technology (IT) based methods, and ii) Physics-based (Control-based) methods. Due to the presence of physical components in CPS, the states of the system need to follow strict rules of nature, e.g. laws of physics. For instance, in a power grid, voltage of buses and current flowing through lines need to follow Kirchhoff’s circuit laws. This important feature can be exploited to detect attacks in CPSs. In this paper, we focus on physics-based attack detection; hence, from now onward by attack detection, we imply physics-based attack detection. Although attacks can be complicated from an IT viewpoint, they tend to be rather naïve or unsophisticated from a control prospective [19].

Most attack detection methods are observer-based techniques in which an observer is designed to estimate states of the plant. The estimated state is then compared against the actual value (measured by sensors) and a time-series residual is formed. Then, an anomaly detector is used to decide—based on the residual time series—on the presence of an adversary agent having access to the control signal and/or measurement output [1]. The observer can be static or dynamic; for instance, the phase angle estimator in power grids is a static estimator [10]. Attack detection strategies can be broadly divided into two categories: active and passive. Passive strategies are those in which the detection mechanism does not affect the system. On the other hand, active strategies affect the control system by sending some unpredictable control commands and observing if sensors react as predicted. In [15] a physical watermarking based detection mechanism is presented in which a random noise of known distribution is injected to the plant and a stateful anomaly detector is used to detect attacks on the system.

In most attack detectors, the control and attack detection designs are carried out independently: the controller is designed first and, subsequently, the detection mechanism is formulated. Contrary, in this paper we co-design these two critical components and propose a joint control and attack detection mechanism using elements from model predictive control (MPC). MPC is an optimization-based controller which can handle different state and control input constraints. The control signal at each sampling time is the solution of a constrained discrete-time optimal control problem [8], [14], [17]. For linear time-invariant systems, the resulting optimization problem is convex which can therefore be efficiently solved using standard solvers. If the dynamical systems is nonlinear—such as the one considered in this paper, the MPC optimization problem becomes nonconvex.

We augment the standard MPC problem with an additional constraint which restricts the future state/output trajectory to remain within some time-invariant neighborhood of a carefully designed reference trajectory. The minimization of the MPC optimization problem involves the predicted states as well as inputs over the prediction horizon. The first component of the control vector is applied to the plant and the predicted outputs are used to construct the future reference trajectory. In fact, the reference trajectory at time $k$ is the $N$th component of the predicted trajectory provided as the minimizer of the MPC problem at time $k-N$ where $N$ is the prediction horizon. The difference between actual real-time output and the reference output trajectory is stored in a residual time-series. The residual is used in a non-parametric
cumulative sum (CUSUM) anomaly detector to decide on the presence of attack in control signal or measurement output.

A. Related Literature

While the literature on attack detection is vast (see e.g. [16]) few works are based on a model predictive control design approach. In [2], the authors adopt a model-based approach in order to detect cyber-attacks in a linear system equipped with a model predictive controller. The problem is formalized as a binary hypothesis test. However, the MPC structure is assumed to be given, and no co-design is considered. A recent and interesting line of research is the one based on the design of set-theoretic receding-horizon control schemes, see for instance [12], [13]. In these works, a specific control architecture is designed so as to be able to detect and mitigate cyber-attacks affecting CPSs. In [22], an approach based on a receding-horizon control law is presented to mitigate replay attacks. In particular, stability is proved under some assumptions on the horizon length and the attack duration. The idea can also be used with false data injection attacks. An MPC-based attack detection using limit checking is introduced in [18]. A feasibility problem is solved online and if there does not exist a control vector being able to keep states within their safe limit during the predicted horizon, an attack is declared. We remark that all reviewed approaches are applied to linear systems, while in this paper we consider a nonlinear setup.

B. The sequel

The remainder of this paper is organized as follows. In Section II, we formulate the nonlinear MPC problem. The modified MPC problem along with proposed attack detection methodology are presented in Section III. A numerical example of industrial cyber-physical systems is presented in Section IV and some concluding remarks are reported in Section V.

Notations

Lowercase letters are used for vectors and uppercase ones for matrices. The symbol $X \succ 0$ (resp. $X \succeq 0$) is used to denote a positive (resp. positive semi-definite) matrix $X$. The set $\mathbb{N}_{>0}$ denotes the set of positive integers. While $y_k$ denotes the measured output at time $k$, the output predicted $\ell$ steps ahead at time $k$ is denoted as $y_{\ell|k}$. We use $u_{\ell|k}$ to denote the sequence of length $N$ of vectors $u_0|k, \ldots, u_{N-1}|k$; the same notation is used for output vector $y_{N|k}$. The Minkowski sum of $A$ and $B$ is denoted by $A \oplus B = \{a+b|a \in A, b \in B\}$.

II. Problem Formulation

Consider a nonlinear cyber-physical system (CPS) whose dynamics is governed by the nonlinear discrete-time system

$$x_{k+1} = f(x_k, (u_k + u_k^a)),$$

$$y_k = x_k + y_k^a,$$ (1a, 1b)

where $x_k \in \mathbb{R}^n$ is the state vector of the system at sampling time instant $k$, $u_k \in \mathbb{R}^m$ is the control signal to be applied to the system, $u_k^a \in \mathbb{R}^m$ represents an attack signal applied to the input at time $k$, $f : \mathbb{R}^n \times \mathbb{R}^m \rightarrow \mathbb{R}^n$ is a nonlinear map which assigns to a state vector $x_k$ and control vector $u_k$ the successor state $x_{k+1}$, $y_k$ is the measurement signal at time $k$, and $y_k^a$ is the attack signal at the output. We assume that all states are available for feedback. The controller is spatially distributed and the channels between controller-actuators and sensors-controller are established by some communication network, e.g. Internet or wireless, industrial Ethernet, Fieldbus, etc. We assume that malicious agents can gain access to these communication channels by compromising the security protocols, and as a consequence are able to inject their desired signals $u_k^a$ and $y_k^a$ to the system [1]. The objective is to design a model predictive controller for the system to be able to detect any possible attack on the control input and measurement signals. In the MPC framework, we usually restrict the output vector $y_k, \forall k \in \mathbb{N}_{\geq 0}$ to live in a set $\mathcal{Y}$. This can be due to safety limitations; for example, the level of liquid in a tank needs to be within its high and low limits or furnace temperature should not exceed a predefined value. Similarly, the control signal $u_k, \forall k \in \mathbb{N}_{\geq 0}$ is also required to remain in a set $\mathcal{U}$ which is to prevent any actuator saturation.

The desired performance of the MPC controller is granted by the appropriate design of a cost function used in the optimization problem being solved at each sampling time. Assuming that $0$ is the equilibrium point of the system—in fact if $[x_k^T, u_k^T]^T \neq 0$ is the equilibrium point of the system [1], we can replace $f(x_k, u_k)$ by $f(x_k + x^*, u_k + u^* - x^*)$ so to have $0$ as the equilibrium point—the cost function $\ell(x, u) : \mathcal{Y} \times \mathcal{U} \rightarrow \mathbb{R}_{>0}$ penalizes the distance of the output $y_k$ and control input $u_k$ to the equilibrium point. A terminal cost is added to the cost function to ensure that the MPC policy stabilizes the system. With these ingredients in mind, we use the following finite-horizon cost to be minimized at time $k$:

$$\ell_N(y_{N+1|k}, u_{N|k}) = \sum_{j=0}^{N-1} \left( y_{j|k}^T Q y_{j|k} + u_{j|k}^T R u_{j|k} \right) + V_N(y_{k+N|k}),$$ (2)

where $Q \in \mathbb{R}^{n \times n}, Q \succ 0, R \in \mathbb{R}^{m \times m}, R \succ 0$ and $V_N(y)$ is the terminal cost designed based on the Lyapunov stability theory, see [8, Chapter 5] for further details. A terminal constraint of the form $y_{N|k} \in \mathcal{Y}_f$ is also included in the MPC optimization problem to guarantee stability. The terminal set $\mathcal{Y}_f$ is designed to grant stability to the MPC policy. With these notations, in an attack-free scenario the MPC optimization problem being solved at time $k$ is

$$\begin{align}
\min_{y_{N+1|k}, u_{N|k}} & \quad \ell_N(y_{N+1|k}, u_{N|k}) \\
\text{subject to:} & \quad x_{j+1|k} = f(x_{j|k}, u_{j|k}), x_{0|k} = x_k \\
& \quad y_k = x_k \\
& \quad y_{j|k} \in \mathcal{Y}, j \in [1, N] \\
& \quad u_{j|k} \in \mathcal{U}, j \in [0, N - 1] \\
& \quad y_{N|k} \in \mathcal{Y}_f.
\end{align}$$ (3a, 3b)

Denoting the minimizer of optimization problem (3) with
(y_{1|k}, \ldots, y_{N|k}, u_{0|k}, \ldots, u_{N-1|k})$, the MPC control law is
$u_k = u^*_o k$, meaning that only the first element of the optimal
control signal is applied to the system. The formulated MPC
problem (3) is for an attack-free scenario, i.e. $u^*_o k = y^*_o k = 0, \forall k \in \mathbb{N}_{>0}$. In the next section, we propose a modified
MPC problem along with a detection criterion which is able
to detect possible attacks on system (1).

III. ATTACK DETECTION ALGORITHM

We first discuss the class of attacks considered in this paper,
and then present the modified MPC controller and, finally
the detection procedure. Here, we specifically consider
the class of False Data Injection Attacks (FDI). In an
FDI attack, an attacker augments control and measurement
signals with his/her desired arbitrary data by manipulating
$u^*_o k$ and $y^*_o k$. Regarding the FDI attack we make the following
assumption.

Assumption 1: The attacker can modify control and mea-
surement signals by injecting its desired signals $u^*_o k, y^*_o k$;
however, it cannot access both control and measurement
channels at the same time, i.e. $\exists k: (u^*_o k \neq 0) \& (y^*_o k \neq 0)$.

Assumption 1 is important because if the attacker has access
to the model of the system and is able to modify both control
and measurement signals, he/she can design attack signals
$u^*_o k$ and $y^*_o k$ such that the attack remains covert, see [19]
for further details.

A. Modified MPC Algorithm

Attack detection algorithms reported in the literature are
usually independent from the controller design process. Typi-
cally, the controller is designed first, and subsequently the
detection algorithm is formulated. In this paper, however,
we take a novel approach by co-designing the detection
algorithm and the controller. To this end, at each time $k$
we consider a future reference trajectory $\tilde{y}_j|k, j \in [1, N]$.
This constitutes a key ingredient of our approach, and is
formally defined later. Next, we add an extra constraint to
the MPC optimization requiring the actual output trajectory
$y_j|k, j \in [1, N]$ to remain within a specified time-invariant
neighborhoods of the reference trajectory

$$y_j|k \in \tilde{y}_j|k \oplus \mathcal{E}, j \in [1, N].$$

Therefore, the modified MPC problem to be solved at each
time $k$ reads as

$$\min_{y_{N+1|k}, u_{N|k}} \mathcal{L}_N(y_{N+1|k}, u_{N|k})$$
subject to:

$$x_{j+1|k} = f(x_j|k, u_j|k + a_j|k), x_0|k = x_k$$
$$y_j|k \in \mathbb{Y}, j \in [1, N]$$
$$y_j|k \in \tilde{y}_j|k \oplus \mathcal{E}, j \in [1, N]$$
$$u_j|k \in \mathbb{U}, j \in [0, N - 1]$$
$$y_{N|k} \in \mathbb{Y}_f.$$ (5b)

The motivation behind forcing the real-time output to re-
main within some time-invariant neighborhood of a reference
trajectory originates from the distributed model predictive
control literature, and in particular, [5]. In [5] authors con-
sider a distributed scenario where states and control inputs
of each node of the network affects the neighboring nodes.
Specifically, each node of the network enforces its real-time
trajectory to stay within some time-invariant neighborhood
of a reference trajectory. Nodes of the network receive the
predicted state and control input of their neighbors and
solve their local MPC problem by relying on the predicted
trajectories. Solution of the optimization problem defined
in (5), i.e. $(y^*_1|k, \ldots, y^*_N|k, u^*_0|k, \ldots, u^*_N-1|k)$, involves
predicted outputs $(\tilde{y}^*_1|k, \ldots, \tilde{y}^*_N|k)$. This information can be used as
the predicted reference trajectory $\tilde{y}_j|k$. In fact, the refer-
tence trajectory at time $k + N, \tilde{y}_k+N$ is the $N$th component
of the predicted output trajectory provided as the minimizer
of the MPC problem (5) at time $k, y^*_N+k|k$

$$\tilde{y}_k+N = y^*_N+k|k.$$ Therefore, by solving the MPC optimization (5), we gradu-
ally construct the reference trajectory.

The set $\mathcal{E}$ defines the closeness of the actual trajectory to
the future reference trajectory. Requiring the two trajectories
to be very close may result in a conservative control strat-
ey with poor performance. There is therefore trade-off in
selecting the set $\mathcal{E}$. Selecting a very small $\mathcal{E}$ compromises
the performance of the MPC control strategy while very large $\mathcal{E}$
leads to poor security.

B. Anomaly Detector

Anomaly detectors construct a series of residuals based on
which they decide on the occurrence of an attack on dynamical
systems. In observer-based anomaly detectors, the residual is the
difference between the actual states (or outputs) and the estimated ones. In this paper, on the contrary, we use as residual the difference between real-
time output $y_k$ and the reference output trajectory $\tilde{y}_k$. Two
models of detector are usually adopted in the literature: i)
stateless, and ii) stateful. In a stateless test, if the residual
$r_k = \|y_k - \tilde{y}_k\|$ exceeds some threshold $\gamma$, an attack
is declared. Contrary, in a stateful test, which is a statistical
test, a new statistic $S_k$ is constructed, which keeps track
of the residuals. There are a number of stateful anomaly
detectors in the literature, such as simple averaging over a
time window, exponential weighted moving average and,
non-parametric cumulative sum known as CUSUM. In this
paper, we adopt CUSUM statistic due to its popularity and
effectiveness. The CUSUM statistic $S_k$ is defined recursively
as $S_0 = 0$ and $S_{k+1} = max(0, S_k + r_k - \delta)$, where $\delta$ is chosen
such that it prevents the CUSUM statistic to grow constantly
in an attack-free scenario. An attack is declared if $S_k$ exceeds
the threshold $\gamma$. Then, the CUSUM statistic is restarted, i.e.
$S_{k+1} = 0$. The threshold $\gamma$ is usually selected by performing
extensive simulations. In fact, a small threshold may result
in frequent false positives while a large value of $\gamma$ can lead
to a detecting mechanism ignoring attacks.

The control and attack detection algorithm is reported in
Algorithm 1. At each sampling time, we first receive the
actual measurement $y_k$ from the plant and construct the
Algorithm 1 Control and Anomaly Detection Algorithm

1: Input: $f, N, E, \gamma, \delta, y_0$
2: Output: attack

Initialization:
3: Construct a feasible reference trajectory $\tilde{y}_1, \ldots, \tilde{y}_N$
4: and set $k = 0$, attack = 0, $S_0 = 0$

Evolution:
5: while attack == 0 do
6: Receive $y_k$ from the plant
7: $S_{k+1} = \max(0, S_k + \|y_k - \tilde{y}_k\| - \delta)$
8: if $S_{k+1} > \gamma$ then
9: Set attack = 1
10: return attack
11: else end if
12: Solve the modified MPC problem \ref{eq:MPC}
13: Set $\tilde{y}_{k+N} = \tilde{y}_{k+N|k}$
14: Set $u_k = u_{0|k}$ and transmit $u_k$ to the plant
15: end while

CUSUM statistic $S_{k+1}$. If $S_{k+1}$ exceeds a carefully chosen threshold $\gamma$, an attack is declared. Next, the modified MPC problem \ref{eq:MPC} is solved, the reference trajectory is constructed $\tilde{y}_{k+N} = \tilde{y}_{k+N|k}$ and, the control signal $u_k = u_{0|k}$ is transmitted and applied to the plant.

IV. NUMERICAL SIMULATIONS

We ran extensive simulations to check the effectiveness of the presented approach. In particular, we tested the algorithm on a nonlinear system regarding level control of two coupled tank systems.

A. Level Control of Coupled Tanks

The schematic diagram of this system is shown in Fig. 1. The exchange of information between sensors/controller and controller/actuator are subject to false data injection attack. Levels of the two tanks are sensed and transmitted to the controller using level transmitters. The control signal is computed in the controller and then transmitted to the flow control valve to regulate the flow of liquid.

![Schematic diagram of the two coupled tanks system.](image)

Fig. 1. Schematic diagram of the two coupled tanks system. The exchange of information between sensors/controller and controller/actuator are subject to false data injection attack. Levels of the two tanks are sensed and transmitted to the controller using level transmitters. The control signal is computed in the controller and then transmitted to the flow control valve to regulate the flow of liquid.

The fluid is pumped from a reservoir into the top tank. There are an opening in the second tank, the fluid returns back into drainage of the fluid to the second tank. Similarly, due to an opening at the bottom of the tank which allows the fluid to be collected and returned to the reservoir. The goal is to control the fluid level in both tanks by manipulating the pump that connects the reservoir and Tank 1. The system dynamics can be computed using the conservation of mass and Bernoulli’s equation

$$\frac{dh_1}{dt} = \frac{c_1}{\rho A_1} u - \frac{c_2}{\rho A_1} \sqrt{h_1},$$
$$\frac{dh_2}{dt} = \frac{c_2}{\rho A_2} \sqrt{h_2} - \frac{c_2}{\rho A_2} \sqrt{h_2},$$

where $h = [h_1, h_2]^T$ is the state vector containing the level of liquid in the first and second tank respectively, $\rho$ is the density of the fluid, $A_1, A_2$ are the cross-sectional area of tanks 1 and 2 respectively, $c_1, c_2$ are coefficients related to the tanks opening, and, $u$ is the pump rate. There are a number of ways to discretize the continuous model \ref{eq:discretized}. Here, we use the first-order forward Euler approximation to construct a discrete-time model. To this end, selecting a desired sampling time $T$, the discretized model is

$$h_1(k+1) = h_1(k) + T \left( \alpha_1 u(k) - \alpha_2 \sqrt{h_1(k)} \right),$$
$$h_2(k+1) = h_2(k) + T \left( \alpha_2 \sqrt{h_1(k)} - \sqrt{h_2(k)} \right),$$

where—assuming identical tanks—$\alpha_1 = 1.75$ and $\alpha_2 = 0.1544$. We remark that more sophisticated discretization method such as Runge–Kutta can be used which results in a more complex discrete dynamics and consequently a more complex MPC optimization problem, see [8, Chapter 11]. The objective is to design an MPC controller to control the level of tank 2 at 0.95. The saturation level of flow control valve is set to 1 which means the following constraint on the control signal should hold all the time

$$0 \leq u(k) \leq 1, \quad \forall k \in \mathbb{N}_{>0}.$$

In order to prevent any overflow in both tanks, we require the fluid level $h(k)$ to remain below 1. Hence, the following state constraint should be respected all the time

$$[0] \leq h(k) \leq [1], \quad \forall k \in \mathbb{N}_{>0}.$$

The MPC framework formulated in Section II is for regulation problems. To consider a tracking problem, the cost needs to be modified as

$$\ell_N(h_{N+1|k}, u_{N|k}) = \sum_{j=0}^{N-1} \left( (h_{j|k} - \bar{h}_{j|k})^T Q(h_{j|k} - \bar{h}_{j|k}) + u_{j|k}^T R u_{j|k} \right) + V_N(h_{k+N}).$$
Tank 2 and keep its liquid level at 0.2 to detect the attack. In particular, we use the CUSUM anomaly detector

\[ S_0 = 0, S_{k+1} = \max(0, S_k + \|y(k) - \tilde{y}(k)\|_2 - 0.01), \]

where \( y \) is the (deceived) sensors measurement at time \( k \) and \( \tilde{y} \) is the predicted value of the levels at time \( k \). Figure 3 shows both residual \( \|y(k) - \tilde{y}(k)\|_2 \) as well as CUSUM statistic. We remark that the same FDI attack scenario as the one reported in Fig. 2 is used to evaluate the effectiveness of the detection mechanism. The detection threshold—the parameter \( \gamma \) in Algorithm 1—is selected to be 0.1. As it can be seen from the inset in Fig. 3, the residual \( \|y(k) - \tilde{y}(k)\|_2 \) remains below 0.01 meaning that the proximity constraint (8) is respected in the absence of any attack. Starting from \( t = 50 \) sec, the residual starts to increase resulting in an increase in the CUSUM statistic. At \( t = 5.92 \) sec, the CUSUM statistic exceeds 0.1 and the FDI attack is detected.

Any sensor measurement inevitably carries some noise. To see the effect of noise on the performance of the proposed detection mechanism, we add a white Gaussian noise with zero mean and 0.002 standard deviation to the sensor measurement from both Tanks 1 and 2. The simulation reported in Fig. 4 shows that the presence of noise does not have a negative effect on the performance, hence confirming the robustness to noise of the proposed approach.

We next consider an FDI attack on the control input \( u \). A simulation reporting an attack on the control signal is shown in Fig. 5. The attacker compromises the control signal applied to the system and augments the actual control signal \( u(k) \) with an attack signal \( u^a(k) \)—shown in the bottom graph in Fig. 5. We remark that a smaller attack signal cannot bring the system to an unsafe region and hence is automatically rejected using the MPC controller. Specifically, if the attack signal on the control input is small, the MPC controller is
able to reject it by manipulating its designed control signal $u(k)$ and hence the attack signal will not have an adverse effect on the performance of the controlled system.

V. CONCLUSION

An approach to co-design a controller controlling the system and an attack detector to detect false data injection attacks in control inputs and measurements is reported in this paper. In a model predictive controller framework, we consider a nonlinear system and require the future trajectory of the outputs to remain in some time-invariant neighborhood of a reference trajectory. Deviation of the real-time trajectory from the reference trajectory—at any point in time—is considered as a residual and used in a non-parametric cumulative sum (CUSUM) anomaly detector to detect attacks.

Future research considers extending the proposed approach to distributed industrial control systems.

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