Article

An Analysis of Creep Phenomena in the Power Boiler Superheaters

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Abstract: Higher temperatures of the power boiler superheater operation may lead to high strains caused by the creep phenomenon. This paper presents a determination of the maximum allowable operating temperature limited by the creep phenomenon for steam superheater SH3. The calculations are carried out first on the basis of applicable European standards. Then, calculations are performed based on conducted creep tests, a proposed creep model, and a finite element method (FEM) model. A detailed creep phenomenon analysis based on the conducted creep tests shows that stresses that determine the creep process are mainly caused by pressure. Normal stresses resulting from bending are mainly the effect of thermal expansion. These stresses undergo significant relaxation because of creep. The creep phenomenon analysis explains the equations of the European standards. The presented calculations enable estimation of a safe value of the operating temperature which is constant over time. The estimated time of safe operation does not take account of temperature spikes. For this reason, pressure elements working at high temperatures must be inspected regularly to assess their wear state.

Keywords: boiler; stress; creep; diagnostic system; numerical simulation

1. Introduction

A procedure aimed at evaluating the relationship between the plant operation strategies and its service life is presented by Stoppato [1]. Improving the boiler efficiency by raising the operating pressure and temperature values leads to high-temperature corrosion [2] and increased creep-related strains.

A detailed dynamic model of an industrial fire-tube boiler is presented in [3]. The obtained results provide practical information regarding the trade-off between the size of the boiler and its corresponding performance and controllability. Mechanical failures involve extremely the complex interaction of load, time, material, manufacturing processes, and environment. The result of the welding effect should be compensated in the structural design. Therefore, laser cladding can be also used as an additive manufacturing technology [4].

Many failures of elements of the power boiler superheaters are caused by the improper operation and the wrong support method of hanger tubes [5]. The hanger conditions in combination with thermal expansion and pressure loads cause stress concentration zones in superheaters and shorten the period of trouble-free operation. Elements subjected to high temperatures are exposed to phenomena such as creep, and time-dependent properties of materials should be considered [6].

The existing methods of designing pressure equipment according to international standards do not require detailed creep analysis, taking into account this phenomenon as a function of time. Dimensioning is based on simple equations assuming that the creep phenomenon is quasi-static. International standards do not describe the complexity of this phenomenon and the calculation...
method can be chosen by the constructor. It often causes damage to the structure due to the local stress concentrations, which are often omitted in simplified analyses, which rapidly affects the intensification of creep phenomena.

The paper presents an analysis of creep phenomena in the power boiler superheater SH3 [7]. Calculations are first carried out on the basis of applicable European standards and with the help of the FEM software to model large structures [8]. Then, calculations are performed based on conducted creep tests, a proposed creep model, a FEM model, and with the use of the software to analyze the nonlinear material behavior [9].

2. Basic Formulations

The heat transfer in solid materials is controlled by heat conduction. The thermal diffusion equation in three-dimensional Cartesian coordinates can be written as follows:

\[
\frac{\partial}{\partial x}\left( k \frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y}\left( k \frac{\partial T}{\partial y} \right) + \frac{\partial}{\partial z}\left( k \frac{\partial T}{\partial z} \right) = \rho \cdot c_p \frac{\partial T}{\partial t}
\]  

(1)

Introducing thermal diffusion \( a = k / (\rho \cdot c_p) \), the heat conduction equation takes the following form:

\[
\frac{\partial T}{\partial t} = a \cdot \nabla^2 T
\]

(2)

The stress field is described by three basic equations presented below:

\[
\sigma_{ij,j} + f_i - \rho \cdot u_{i,t} - \mu \cdot u_{i,t} = 0
\]

(3)

\[
\varepsilon_{ij} = \frac{1}{2}\left(u_{ij} + u_{ji}\right)
\]

(4)

\[
\sigma_{ij} = 2G\varepsilon_{ij} + \lambda\varepsilon_{kk}\delta_{ij} - \beta T \delta_{ij}
\]

(5)

Equation (3) is the force equilibrium equation, Equation (4) is the geometric equation and Equation (5) is the constitutive equation. For high temperatures and long-time operation, creep phenomena must be taken into account. The creep equation enables determination of the stress-and-strain distribution in a structural element.

\[
\varepsilon_c(t) = f(t, \sigma, T)
\]

(6)

In general, creep strain \( \varepsilon_c \), elastic strain \( \varepsilon \), plastic strain \( \varepsilon^{pl} \), and thermal strain \( \varepsilon^\theta \) together form summary strain, \( \varepsilon^{sum} \). The creep calculation algorithm requires the definition of a modified total strain \( \varepsilon' \):

\[
\varepsilon'_n = \varepsilon^{sum}_n - \varepsilon^{pl}_n - \varepsilon^\theta_n - \varepsilon^{sum}_{n-1}
\]

(7)

For multi-axial creep, all parts of Equation (7) are tensors containing corresponding components of strain. The modified strain field can also be written using the equivalent modified strain \( \varepsilon_{eq} \):

\[
\varepsilon_{eq} = \frac{1}{\sqrt{2(1+\nu)}} \left[ (\varepsilon'_{xx} - \varepsilon'_{yy})^2 + (\varepsilon'_{yy} - \varepsilon'_{zz})^2 + (\varepsilon'_{zz} - \varepsilon'_{xx})^2 + \frac{3}{2} \cdot (\varepsilon'_{xy})^2 + \frac{3}{2} \cdot (\varepsilon'_{yz})^2 + \frac{3}{2} \cdot (\varepsilon'_{zx})^2 \right]^{0.5}
\]

(8)

The equivalent stress can be calculated as:

\[
\sigma_{eq} = E \cdot \varepsilon_{eq}
\]

(9)
Next, based on Equation (6), strain $\varepsilon_{eq}$ and stress $\sigma_{eq}$, the increment in creep strain $\Delta \varepsilon^c$ is calculated. For a uniaxial state, it is defined as follows:

$$\Delta \varepsilon_{xx}^c = \frac{\Delta \varepsilon^c}{\varepsilon_{eq}} \cdot \varepsilon_{xx}'$$

(10)

For a multi-axial problem, the components of $\Delta \varepsilon^c$ are given by the following relations:

$$\Delta \varepsilon_{xx}^c = \frac{\Delta \varepsilon^c}{\varepsilon_{eq}} \cdot \frac{2\varepsilon_{yy}' - \varepsilon_{zz}' - \varepsilon_{xx}'}{2(1+\nu)}$$

$$\Delta \varepsilon_{yy}^c = \frac{\Delta \varepsilon^c}{\varepsilon_{eq}} \cdot \frac{2\varepsilon_{xx}' - \varepsilon_{yy}' - \varepsilon_{zz}'}{2(1+\nu)}$$

$$\Delta \varepsilon_{zz}^c = -\Delta \varepsilon_{xx}^c$$

$$\Delta \varepsilon_{xy}^c = \frac{\Delta \varepsilon^c}{\varepsilon_{eq}} \cdot \frac{3\varepsilon_{xy}'}{2(1+\nu)}$$

(11)

Elastic strains and total creep strains are calculated according to:

$$(\varepsilon_{xx})_n = (\varepsilon_{xx}')_n - \Delta \varepsilon_{xx}^c$$

$$(\varepsilon_{xx}')_n = (\varepsilon_{xx}')_{n-1} - \Delta \varepsilon_{xx}^c$$

(12)

The above equations are integrated with respect to time by means of the Euler method.

3. Analysis of Creep Phenomena

The maximum operating temperature $T_{w}$ of a selected structural element is found using European standards. In this algorithm, the following constraints are defined:

- maximum stresses are limited to allowable values for the initial time.
- maximum stresses are limited to allowable values for the time of 200,000 h under creep conditions (if a design lifetime is not specified), and creep strain should be less than 1% at 100,000 h (if design lifetimes is shorter than 100,000 h).

Next, the optimal solution is verified. A detailed analysis of the creep phenomenon is performed based on creep strain measurements. The temperature and stress distributions described by Equations (1)–(6) are calculated by means of a finite element method using the ANSYS [9] and the Auto Pipe [8] programs.

3.1. Calculation Based on European Standards

Due to high pressures (greater than 0.5 bar), the boiler pressure parts are subject to the European Directive 2014/68/EU [10]. For this reason, superheaters should be calculated according to harmonized standards EN 12952-3 [11] and EN 13480-3 [12], where a simple algorithm is presented.

The first constraint complies with standard EN 13480-3. For the initial time, pipelines operate without creep conditions and the following criterion should be satisfied:

$$\sigma = \frac{Pd_0}{4e_n} + \frac{0.75iM_A}{Z} + \frac{iM_C}{Z} \leq f_R$$

(13)

The second constraint refers to the creep condition:

$$\sigma = \frac{Pd_0}{4e_n} + \frac{0.75iM_A}{Z} + \frac{0.75iM_C}{3Z} \leq f_{CR}$$

(14)

The stress intensification factor (0.75i) should be higher than or equal to 1.0. Equations (13) and (14) present longitudinal stresses caused by pressure, thermal expansion, weight, or other sustained
loads. The sum of longitudinal stresses should be smaller than or equal to the specified allowable stress value.

Allowable stress \( f_R \) is formulated as the ratio of the yield strength to the safety factor for the ambient or calculation temperature, which should comply with standard EN 13480-3.

Allowable stress \( f_{CR} \) (for creep) is the ratio of the mean creep rupture strength to the safety factor, which should comply with standard EN 13480-3 or standard EN 12952-3.

The forces and moments in the analyzed component caused by pressure, the coil thermal expansion and its weight can be calculated by the Auto Pipe program [8]. Auto Pipe uses one-dimensional finite elements to calculate the superheater coil displacements based on the static strength analysis. This method can identify the most loaded parts of the coil.

The Auto Pipe software also evaluates longitudinal stresses according to Equation (13) or (14) and shows their distribution in the analyzed component. Fulfilment of criteria for (13) or (14) can be checked without difficulty. The procedure for finding allowable stresses continues until the maximum operating temperature is determined. Subsequent iterations are carried out by means of the golden search method. Finally, the condition of the highest creep strain not exceeding 1% after 100,000 h should be checked. If the condition is not satisfied, the operating temperature must be reduced gradually. The algorithm for the highest creep strain calculation is presented in the next section.

3.2. Verification of Calculated Temperature Values Based on a Detailed Analysis of the Creep Phenomenon

A detailed analysis is performed to verify the solution obtained above. It is made for the most loaded part of a selected structural element using the ANSYS Mechanical package [9]. Creep constitutive equations in various studies are specific. In [13] constitutive models were established based on an isothermal creep method to describe the high-temperature creep behavior of SA-508.

The creep equation for the selected steel grade is built based on uniaxial homogeneous stress states realized in standard material testing [14]. A standard cylindrical tension specimen is heated up to temperature \( T = (0.3–0.5) T_m \) and loaded with the tensile force \( F \), which are kept constant during the experiment.

The measured data are approximated using a modified Garofalo creep equation [15]. The coefficients in this equation depict physical quantities. This model enables an adequate description of the first and the second stage of creep, but it also takes account of the third stage of the phenomenon. The proposed form of the creep equation is as follows:

\[
\varepsilon_c(t) = A \left( 1 - \exp \left( - \frac{t}{t_{II}} \right) \right) + \exp \left( c_3 \sigma - c_4 \right) t + \exp \left( - \frac{t}{\exp \left( c_1 + c_2 \ln(\sigma + 1) \right)^2} \right)
\]

(15)

The constants in Equation (15) are calculated based on the results of uniaxial creep tests conducted in Institute for Ferrous Metallurgy (IMZ) [16–19]. In order to find initial values for all coefficients in Equation (15) before the final multivariate approximation is carried out, the algorithm described below is applied.

Using measurement data, time to failure–stress pairs are generated. The created points are approximated using the following function:

\[
t_r = \exp \left( c_1 + c_2 \ln \left( \sigma + 1 \right)^2 \right)
\]

(16)

This equation makes it possible to find the time to rupture based on stress.

Next, minimum creep strain rate–stress pairs are used to find coefficients of the following function:

\[
\dot{\varepsilon}_{\text{min}} = \exp \left( c_3 \sigma - c_4 \right)
\]

(17)
Using this equation, it is possible to estimate the minimum creep strain rate as a function of stress. The minimum creep strain rate is calculated by interpolating creep strain versus time using a high-degree polynomial approximation.

The value of $t_{II}$ is the time to reach the minimum creep rate, which depends on the amount of tension in the creep test. For the initial value of $t_{II}$, an average value of all analyzed stresses is assumed.

The first and the second stage of creep are described by the following equation:

$$\varepsilon_c(t, \sigma) = A \left( 1 - \exp\left( -\frac{t}{t_{II}} \right) \right) + \varepsilon_{\text{min}} t$$

Parameter $A$ can be calculated from the measured data and previously determined parameters ($\varepsilon_{\text{min}}, t_{II}$). The average of all analyzed stresses is adopted as the initial value.

All three creep stages are described by the following relation:

$$\varepsilon_c(t, \sigma) = A \left( 1 - \exp\left( -\frac{t}{t_{II}} \right) \right) + \varepsilon_{\text{min}} t + \exp\left( \frac{t}{t_r} - K \right)^M$$

All parameters in Equation (15) are finally obtained by means of the Lavenberg-Marquardt method.

4. Numerical Example

The proposed algorithm is applied for the steam superheater SH3 [7,20]. It is the part of the boiler installation presented in Figure 1, where all pipe coils 1 (dimensions: 44.5 × 6.3) are supported by hanger tubes 2 (dimensions: 44.5 × 6.3) and by plate 4, which is welded between pipes 2. The pipe coil passes through the membrane wall 3 and goes to the inlet or the outlet header. Details A and B in Figure 1 illustrate the geometry of the superheater pipes. Hanger tubes 2 are anchored at their upper part, where tension can be adjusted appropriately. The purpose of the tension adjustment is to compensate for thermal expansion [20].
Figure 2) by plate (labeled 4 in Figure 1). Seven rows of the hanger tubes support steam pipes (labeled 1 in Figure 2). The hanger tubes are anchored at their upper part, which is in accordance with the boundary conditions of the hanger pipes at the transition through the upper wall. Additionally, the upper wall tension of the hanger tubes is included.

Calculated pressure, $P$, acting on the internal surface of the pipes equals 284 bar. The adopted method of the coil support by means of the plate allows the superheater pipes displacement of up to 5.5 mm in the vertical direction. The boundary conditions in the Auto Pipe program are realized by two methods of support and one tension, see Figure 3: Anchor, Guide, Cut Short. The coefficient of friction between the pipes and the supporting plate is 0.3.

The superheater failure-free operation is possible only if the tension of the hanger tubes is appropriately adjusted to avoid rupture of the superheater coil at its anchorage to the membrane wall.

Figure 3. Method of superheater SH3 support: 1—Anchor, 2—Guide, 3—Cut Short.
The superheater coil is made of Super 304H steel, which is often used for the steam superheater components due to its high heat resistance and improved properties at elevated temperatures. The steel chemical composition is presented in Table 1 [21].

### Table 1. Chemical composition of Super 304H steel.

| C   | Si  | Mn   | P   | S   | Cu  | Cr   | Ni  | Nb | B  | N   | Al  |
|-----|-----|------|-----|-----|-----|------|-----|----|----|-----|-----|
| 0.07–0.13 | Max  | Max  | 0.0040 | 0.0010 | 3.50 | 19.0 | 7.5  | 0.30 | 0.0001 | 0.05 | 0.0003 |

#### 4.1. Calculation Based on European Standards

For all iterations, maximum stresses occur at point A—as shown in Figure 4. In the first iteration, the operating temperature $T$ equals 650 °C, and pressure $P$ acting on the internal surface of the pipes is 284 bar. The longitudinal stress distributions at the initial time in the new component (without creep phenomenon) and after 200,000 h of the component work under creep conditions are obtained from Equations (13) and (14). The maximum longitudinal stress occurs at point A. It equals $\sigma = 158$ MPa and $\sigma_C = 90$ MPa at the commencement and after 200,000 h of operation, respectively. Both values are not higher than the allowable values of stress $f_R = 319$ MPa and $f_{CR} = 105.3$ MPa.

The longitudinal stress distribution after 200,000 h and the maximum longitudinal stress location are presented in Figure 4. The maximum longitudinal stress occurs at point A. It equals 650 °C, and pressure $P$ acting on the internal surface of the pipes is 284 bar. The longitudinal stress at point A equals 319 MPa and 105.3 MPa.

The longitudinal stress distribution after 200,000 h and the maximum longitudinal stress location are presented in Figure 4. The maximum longitudinal stress occurs at point A. It equals 650 °C, and pressure $P$ acting on the internal surface of the pipes is 284 bar. The longitudinal stress distribution at the initial time in the new component (without creep phenomenon) and after 200,000 h of the component work under creep conditions are obtained from Equations (13) and (14). The maximum longitudinal stress occurs at point A. It equals $\sigma = 158$ MPa and $\sigma_C = 90$ MPa at the commencement and after 200,000 h of operation, respectively. Both values are not higher than the allowable values of stress $f_R = 319$ MPa and $f_{CR} = 105.3$ MPa.

The longitudinal stress distribution after 200,000 h and the maximum longitudinal stress location are presented in Figure 4. The maximum longitudinal stress occurs at point A. It equals 650 °C, and pressure $P$ acting on the internal surface of the pipes is 284 bar. The longitudinal stress distribution at the initial time in the new component (without creep phenomenon) and after 200,000 h of the component work under creep conditions are obtained from Equations (13) and (14). The maximum longitudinal stress occurs at point A. It equals $\sigma = 158$ MPa and $\sigma_C = 90$ MPa at the commencement and after 200,000 h of operation, respectively. Both values are not higher than the allowable values of stress $f_R = 319$ MPa and $f_{CR} = 105.3$ MPa.

The second iteration is made for 700 °C. At this temperature, the maximum stress exceeds the allowable values, see Table 2. The maximum allowable operating temperature of the SH3 steam superheater is found at 665 °C.

### Table 2. Maximum longitudinal stress.

| Temperature (°C) | Stress $\sigma$ (MPa) | Stress $\sigma_C$ (MPa) | Yield Strength (MPa) | Allowable Stress (MPa) (See Section 3.1) |
|------------------|------------------------|------------------------|----------------------|------------------------------------------|
|                  | $f_R$                  | $f_{CR}$               | $\sigma_C/f_{CR}$   |
| 650              | 158                    | 90                     | 172                  | 319.0                                    |
| 700              | 167                    | 92                     | 160                  | 252.5                                    |
| 665              | 160                    | 90                     | 160                  | 296.5                                    |

#### 4.2. Verification of the Final Solution Based on a Detailed Analysis of the Creep Phenomenon

Based on experimental data [16–19], a creep model is built for Super 304H steel. The coefficients in Equation (15) are calculated for the optimal temperature established in the previous sub-section, i.e., 665 °C. The resulting creep model and the measured creep strain curves at 665 °C are shown in Figure 5.
A detailed analysis is conducted for the most loaded part of the superheater located close to point A, see Figure 4. The ANSYS Mechanical package is used for the strength analysis [9]. The Solid 185 finite element is used to discretize the part under consideration.

The initial analysis performed in the ANSYS program is based on a typical solution for the theory of elasticity. The boundary conditions, the equilibrium, geometric (Cauchy), and constitutive equations are used to determine the unknown displacement, strain, and stress distributions.

The developed finite element model must be loaded with pressure and end loads [22].

The end loads are represented by displacements obtained from the Auto Pipe program at point C (located 400 mm from point A, see Figure 6). In order to check the model accuracy, the Auto Pipe program end displacements and rotations (transformed to displacements) are applied to an ANSYS auxiliary pipe and equivalent stresses were compared. For the ANSYS Mechanical analysis, the boundary conditions correspond to those for the Auto Pipe—with the tension of the hanger tubes [20].

The stress distributions close to point A for the initial state and after 200,000 h are presented in Figures 7 and 8, respectively. At the start of operation, the highest stress is caused mainly by bending due to the material thermal expansion. After 200,000 h, the maximum stress is lower and it is caused mainly by pressure. In order to determine the most crucial stress after 200,000 h, linearization of equivalent stresses on the wall thickness is carried out, as shown in Figure 9. The time-dependent stress relaxation for a point where stress concentration occurs is illustrated in Figure 10. At the initiation of operation the stress is considerable, but after 10,000 h, it diminishes quickly.
The time-dependent stress relaxation for a point where stress concentration occurs is illustrated as Stress $\sigma_{\text{HMH}} = 91.2$ MPa at point A1 which is reached after $t = 700$ h, and at point A2 after $t = 2100$ h. After $t = 200,000$ h the stresses in the superheater are much lower than the limit.
A1 and A2 do not exceed 1% after 100,000 h, which means that the condition presented in Section 3 is satisfied. The creep curves for points A1 and A2 are shown in Figure 11. The creep equivalent strains for points A1 and A2 are mainly the effect of thermal expansion. These stresses undergo significant relaxation because of creep. A detailed analysis of the creep phenomenon explains why the last term in Equation (14) produced by thermal expansion is much less significant compared to the last term in Equation (13). At this temperature, these stresses are large enough to produce a growth in the creep strain. The maximum operating temperature for steam superheater SH3 at 665 °C is limited by the creep phenomenon. For a stress of 91.2 MPa, corresponding to time \( t = 700 \) h at point A1, strain \( \varepsilon_{\text{HMH}, A1} = 0.06\% \), and at point A2 \( (t = 2100 \) h) \( \varepsilon_{\text{HMH}, A2} = 0.11\% \).

5. Conclusions

The maximum operating temperature \( T_{\infty} \) limited by the creep phenomenon is calculated using the golden search method. Two types of strength analysis of superheater coils are described. The first type is based on European standards, which establish the maximum allowable operating temperature for steam superheater SH3 at 665 °C. The second analysis is based on the creep equation. A detailed analysis is performed to verify the optimal solution. An ANSYS analysis reveals that the initial stress value is decreased by about 55%. According to the EN 13480-3 standard, this decrease is smaller and equals 44%. A detailed creep phenomenon analysis based on the conducted creep tests shows that stresses that determine the creep process are mainly caused by pressure. The maximum stress after 200,000 h is 75.13 MPa, while the membrane stress is 73.4 MPa. Normal stresses resulting from bending are mainly the effect of thermal expansion. These stresses undergo significant relaxation because of creep. A detailed analysis of the creep phenomenon explains why the last term in Equation (14) produced by thermal expansion is much less significant compared to the last term in Equation (13).
The presented calculations enable estimation of a safe operating temperature which remains constant in time. The estimated time of safe operation does not take temperature spikes into account. For this reason, pressure elements working at high temperatures must be inspected regularly to assess their wear state.

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**Nomenclature**

- $A$: the highest creep strain at the end of the first stage of creep, -
- $c_p$: specific heat capacity, J/(kg·K)
- $c_1$: experimental constant, ln(h)
- $c_2$: experimental constant, ln(h)/ln(MPa)$^2$
- $c_3$: directional factor for the second stage of creep, (ln(1/h))/MPa
- $c_4$: coordinate of the $t$-intercept for the second stage of creep, ln(1/h)
- $d_o$: pipe outer diameter, mm
- $e_n$: pipe thickness, mm
- $f_{RR}, f_{CR}$: allowable stresses, MPa
- $G$: Lame constant, MPa
- $i$: stress intensification factor, -
- $k$: thermal conductivity, W/(m·K)
- $K, M$: coefficients describing the destruction process intensity, -
- $M_A$: moment caused by weight and other sustained loads, Nm
- $M_C$: moment caused by thermal expansion, Nm
- $P$: pressure, MPa
- $t$: time, h
- $t_{II}$: time marking the beginning of the second stage of creep, h
- $T$: temperature, °C
- $T_m$: the material melting point, °C
- $u$: displacement vector, m
- $x, y, z$: Cartesian coordinates, m
- $Z$: the pipe section modulus, mm$^3$
- $\beta$: thermal expansion coefficient, 1/K
- $\varepsilon_c(t)$: actual normal creep strain, -
- $\varepsilon$: strain tensor, -
- $\lambda$: Lame constant, MPa
- $\nu$: Poisson’s ratio, -
- $\rho$: density, kg/m$^3$
- $\sigma$: normal stress, MPa
- $\sigma$: stress tensor, MPa
- $n$: time step (subscripts)

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