Comparison of highly-compressed C2/m-SnH12 superhydride with conventional superconductors

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Abstract

Satterthwaite and Toepke (1970 Phys. Rev. Lett. 25 741) predicted high-temperature superconductivity in hydrogen-rich metallic alloys, based on an idea that these compounds should exhibit high Debye frequency of the proton lattice, which boosts the superconducting transition temperature, \( T_c \). The idea has got full confirmation more than four decades later when Drozdov et al (2015 Nature 525 73) experimentally discovered near-room-temperature superconductivity in highly-compressed sulphur superhydride, H3S. To date, more than a dozen of high-temperature hydrogen-rich superconducting phases in Ba-H, Pr-H, P-H, Pt-H, Ce-H, Th-H, S-H, Y-H, La-H, and (La,Y)-H systems have been synthesized and, recently, Hong et al (2021 arXiv:2101.02846) reported on the discovery of C2/m-SnH12 phase with superconducting transition temperature of \( T_c \sim 70 \) K. Here we analyse the magnetoresistance data, \( R(T,B) \), of C2/m-SnH12 phase and report that this superhydride exhibits the ground state superconducting gap of \( \Delta(0) = 9.2 \pm 0.5 \) meV, the ratio of \( 2\Delta(0)/k_B T_c = 3.3 \pm 0.2 \), and \( 0.010 < T_c/T_F < 0.014 \) (where \( T_F \) is the Fermi temperature) and, thus, C2/m-SnH12 falls into unconventional superconductors band in the Uemura plot.
Comparison of highly-compressed $C2/m$-$SnH_{12}$ superhydride with conventional superconductors

I. Introduction

Satterthwaite and Toepke [1] were first who understood that hydrogen-rich compound should exhibit highest superconducting transition temperature: “…There has been theoretical speculation [2] that metallic hydrogen might be a high-temperature superconductor, in part because of the very high Debye frequency of the proton lattice. With high concentrations of hydrogen in the metal hydrides one would expect lattice modes of high frequency and if there exists an attractive pairing interaction one might expect to find high-temperature superconductivity in these systems also.” Mathematical rigorous description of Satterthwaite’s and Toepke’s idea [1] had been given 34 years later by Ashcroft [3].

In 2015 Drozdov et al [4] reported on experimental discovery of first near-room-temperature superconductor (NRTS) $H_3S$, which was also the first superhydride compound synthesized at megabar pressure level heated by laser pulses inside of diamond anvil cell. This technique is used since than to synthesize new NRTS phases, and to date more than a dozen high-temperature hydrogen-rich superconducting phases have been synthesised in Pr-H [5], Ba-H [6], P-H [7], Pt-H [8], Ce-H [9], Th-H [10,11], S-H [4,12-17], Y-H [18,19], La-H [20-24], (La,Y)-H [25] and CaH$_x$ [26,27] systems.

Recently, Hong et al [28] extended superhydride family by the discovery of $C2/m$-$SnH_{12}$ phase which exhibits the superconducting transition temperature of $T_c \sim 70$ K at pressure of $P = 190$ GPa. This experimental result is in a good accord with first-principles calculations performed in 2015 by Esfahani et al [29], who predicted $T_c = 83$-93 K for $C2/m$-$SnH_{12}$ phase compressed at pressure of $P = 250$ GPa. Despite Esfahani et al [29] predicted that $C2/m$-$SnH_{12}$ phase can be thermodynamically stable at $P \geq 250$ GPa, XRD studies [28] show that $C2/m$-$SnH_{12}$ phase is dominant at lower pressure range of $P \sim 200$ GPa. This difference can
be explained by an atomic disorder, hydrogen non-stoichiometry, etc., which are always (in some degree) real world samples features. It should be noted, that here we assume that calculated values for the electron-phonon coupling constant, $\lambda_{e-ph} = 1.25$, and logarithmic average phonon frequency, $\hbar \cdot \omega_{log} = 991$ K, reported by Esfahani et al [29] for $C2/m$-SnH$_{12}$ compressed at $P = 250$ GPa will be still valid for sample compressed at $P = 190$ GPa [28].

Hong et al [28] measured magnetoresistance curves, $R(T, B)$, up to applied magnetic field of $B_{appl} = 7$ T, from which, by applying analytical equation proposed by Jones et al [30]:

$$B_{c2}(T) = \frac{\phi_0}{2 \pi \xi^2(0)} \cdot \left( \frac{1-\left(\frac{T}{T_c}\right)^2}{1+\left(\frac{T}{T_c}\right)^2} \right)$$

(1)

where $\phi_0 = \frac{\hbar}{2e}$ is superconducting flux quantum, and $\xi(0)$ is the ground state coherence length, the ground state upper critical field was deduced as $B_{c2}(0) = 11.2$ T.

Here we perform further analysis of $R(T, B)$ data reported by Hong et al [28] with the purpose to extract the ground state amplitude of the superconducting energy gap, $\Delta(0)$, one of primary parameters of the superconducting state. In addition, we calculate the ratio of transition temperature to the Fermi temperature, $T_F$, to locate $C2/m$-SnH$_{12}$ phase in Uemura plot [31,32].

II. $R(T,B)$ analysis

Primary task in the analysis of $R(T,B)$ data is to deduce the superconducting critical temperature, $T_c$, for which we recently proposed [33] to use a fit of experimental $R(T,B)$ data to a function:

$$R(T, B_{appl}) = R_0 + k \cdot T + \theta(T_{c onset} - T) \cdot \left( \frac{R_{norm}}{I_0 \left( F \cdot \left( 1 - \frac{T}{T_{c onset}} \right)^{3/2} \right)} \right)^2 +$$
\[
\theta(T - T_{c \text{onset}}) \cdot (R_{\text{norm}} + (k - k_1) \cdot T_{c \text{onset}} + k_1 \cdot T)
\] (2)

where \( R_0, R_{\text{norm}}, T_{c \text{onset}}, k, k_1, \) and \( F \) are free-fitting parameters, and \( \theta(x) \) is the Heaviside function.

The first two terms in the Eq. 2, i.e. \( (R_0 + k \cdot T) \), are introduced in Ref. 33 to adopt possible ohmic resistance in \( R(T,B) \) curve which appears as a result of metallic weak-links in NRTS sample in diamond anvil cell.

The third fitting term in Eq. 2 which approximates the superconducting transition:

\[
R(T,B_{\text{appl}}) = \frac{R_{\text{norm}}}{\left( I_0 \left( F \cdot \left(1 - \frac{T}{T_{c \text{onset}}}\right)^{3/2}\right) \right)^2}
\] (3)

was proposed by Tinkham [34] to fit experimental \( R(T,B) \) curves in HTS cuprate ceramics, where Tinkham [34] proposed to use:

\[
F = \frac{C}{2 \cdot B_{\text{appl}}}
\] (4)

where \( C \) is free-fitting parameter having unit of Tesla, and \( B_{\text{appl}} \) is applied magnetic field.

Physical background of Eq. 3 was explained by Tinkham [34] as: “... the specific predicted \( B^{3/2} \) dependence fits quite well with a variety of published data .... We also point out that the result ... would hold even if the functional form (which is in our case Eqs. 3,4) were replaced by some other similar function of \( U_0/k_B T \), so long as the form of (which is our Eq. 7) holds.”

In this explanation, Tinkham [34] mentioned the ratio \( U_0/k_B T \), where \( k_B \) is the Boltzmann constant, and \( U_0 \) is a magnetic flux creep activation energy:

\[
U_0 = \beta \cdot B_c^2 \frac{\phi_0 \zeta}{\mu_0 \mu_{\text{appl}}}
\] (5)

where, \( \beta \) is (presumed \( \sim 1 \)) a constant which absorbed all numerical factors, \( \zeta \) is superconducting coherence length, \( B_{\text{appl}} \) is applied magnetic field, and \( B_c \) is the thermodynamic field:
\[ B_c = \frac{\phi_0}{2\sqrt{2\pi} \lambda \xi} \]  

(6)

where \( \lambda \) is the London penetration depth. After further consideration, Tinkham [34] reported, that:

\[
\frac{u_0}{k_B T} = \frac{A}{B_{\text{appl}}} \cdot \left(1 - \frac{T}{T_{c\text{onset}}}\right)^{3/2}
\]

(7)

where \( A \) is a constant of Tesla unit. Thus, in overall, Eq. 3 can be considered as a good approximation for the Abrikosov vortex flux creep. However, as it is mentioned by Tinkham [34], there are no restrictions to use other fitting functions which approximate \( U_0/k_BT \) term in given superconductor.

As we discussed in previous paper [31], there is a significant disadvantage of Eq. 7, which remains in recent proposal for parameter \( F \) given by Hirsch and Marsiglio [35]:

\[
F = \frac{1}{2B_{c2(0)}}
\]

(8)

that Eq. 3 cannot be used to fit \( R(T, B_{\text{appl}} = 0) \) data, because the division by zero is prohibited. However, it was pointed out in Ref. 33, that there is no necessity for explicit use of \( B_{\text{appl}} \) in the expression for parameter \( F \), because \( B_{\text{appl}} \) is known from experiment. Based on this, \( F \) can be free-fitting unitless value, which describe the sharpness of the transition.

However, it should be stressed that as it was mentioned by Tinkham [34] that: “…some other similar function …” can be used as well. And based on this, particular deduced \( F \) values are linked to main fitting term of \( \left(I_0 \left(F \cdot \left(1 - \frac{T}{T_{c\text{onset}}}\right)^{3/2}\right)\right)^{-2} \) and as far as the goodness of fit is high, the fit will be in use to deduce \( T_{c\text{onset}} \) and \( T_c \) within established strict mathematical routine, while particular \( F \) value has no practical use.

The fourth fitting term in Eq. 2, i.e. \( (R_{\text{norm}} + (k - k_1) \cdot T_{c\text{onset}} + k_1 \cdot T) \), represents a linear rise in the \( R(T,B) \) curve above the onset transition temperature, \( T_{c\text{onset}} \). More details about different terms in Eq. 2 can be found in Ref. 33.
Thus, if $R(T,B)$ fit to Eq. 2 has converged, $T_c$ can be defined at any $\frac{R(T)}{R(T_c^{onset})}$ criterion, for which in this work we used the $T_{c,0.05}$ criterion:

$$\frac{R(T)}{R(T_c^{onset})} = 0.05$$  \hspace{1cm} (9)

Primary reasons why the superconducting critical temperature for highly-compressed superconductors should be defined at as low as practically possible $\frac{R(T)}{R(T_c^{onset})}$ ratio were discussed elsewhere [36]. Here we only point out that the use of $T_c^{onset}$ criterion, which utilizes in some, but not in all, reports on highly-compressed superconductors, can be objected by experimental fact that the change in $R(T)$ slope, or even sharp drop in $R(T)$, is observable at many phase transitions in condensed matter when structural phase transitions occur [37-39]. Classical example for this is the change in $R(T)$ slope at structural phase transitions $\alpha$-$\gamma$ and $\gamma$-$\varepsilon$ in iron [40,41].

In addition to several fits for NRTS materials, which we showed in our previous work [33], in Fig. 1 we fit $R(T,B=0)$ data for $Fm$-$3m$-LaH$_{10}$ phase ($P = 138$ GPa) for which experimental data has been recently reported by Sun et al [26]. The fit has high quality (with goodness of fit $R = 0.9981$) and deduced $T_c^{onset}$ and $T_{c,0.05}$ are indicated in Fig. 1.

All fits presented in the manuscript have been performed by utilizing the Levenberg-Marquardt approach in non-linear fitting package of the Origin2017 software.
Figure 1. $R(T,B=0)$ data and fit to Eq. 1 for $Fm\text{-}3m\text{-LaH}_{10}$ ($P = 138$ GPa), where raw data was reported by Sun et al [24]. 95% confidence bars are shown by a pink shaded area; goodness of fit is $R = 0.9981$.

III. Results

Fits to Eq. 2 of $R(T,B)$ data for $C2/m\text{-SnH}_{12}$ ($P = 190$ GPa) reported by Hong et al [28] are shown in Figs. 2,3, where Fig. 2 represents measurements performed at the “cooling” stage, while in Fig. 3 data and fits are shown for the “warming” stage. Despite a fact that $R(T,B)$ curves of $C2/m\text{-SnH}_{12}$ ($P = 190$ GPa) phase for “cooling” and “warming” stages are close to each other, these curves are not identical. For this reason, we deduce $T_{c,0.05} (B)$ for each stage with the purpose that full $B_{c2}(T)$ dataset will characterize as complete as practically possible the $C2/m\text{-SnH}_{12}$ phase. Results of the analysis are shown in Table 1.

It should be noted that $R(T,B)$ data for $C2/m\text{-SnH}_{12}$ ($P = 190$ GPa) reported by Hong et al [28] have linear ohmic term below transition temperature, which reflects the presence of metallic weak-links in the sample, which is accounted (as this mentioned above) by the term of $(R_0 + k \cdot T)$ in Eq. 2.
Table 1. Deduced $T_{c,0.05}(B)$ values for the “cooling” and the “warming” stages of C2/m-SnH$_{12}$ phase compressed at $P = 190$ GPa.

| Applied field, $B_{\text{appl}}$ (Tesla) | $T_{c,0.05}$ (cooling stage) (K) | $T_{c,0.05}$ (warming stage) (K) |
|-----------------------------------------|----------------------------------|----------------------------------|
| 0                                       | 63.5                             | 65.1                             |
| 1                                       | 57.9                             | 58.6                             |
| 2                                       | 52.4                             | 53.3                             |
| 3                                       | 47.2                             | 48.2                             |
| 5                                       | 35.9                             | 36.4                             |
| 7                                       | 24.8                             | 25.0                             |

In overall, all fits have high-quality, even for $R(T,B=0)$ (Figs. 2,a and 3,a) for which the double transition is observed. For the latter the goodness of fit, $R = 0.9986$, while for the rest $R > 0.9989$.

It should be clarified, that as far as we have defined the critical temperature, $T_c$, by the $\frac{R(T)}{R(T_{c\text{onset}})} = 0.05$ criterion (Eq. 9 and Table I), there is no any longer a need to write full designation, i.e. $T_{c,0.05}$, for this value because otherwise there will be a need to use the same subscript for other parameters, i.e. $B_{c2,0.05}(T)$, $\xi_{0.05}(0)$, $\Delta_{0.05}(0)$, etc.. Thus, in further analysis we omit the use of 0.05 designation in the subscripts, because when (which is implemented in many reports) $T_c$ and $B_{c2}(T)$ are defined by 50% of normal state resistance criterion, the designation of used criterion, i.e. $T_{c,0.50}$ and $B_{c2,0.50}(T)$, is always omitted (see, for instance, Ref. 28 where the latter criterion was used).
Figure 2. $R(T,B)$ data and fits to Eq. 1 for $C2/m$-SnH$_{12}$ ($P \approx 190$ GPa) measured at cooling stage (raw data reported by Hong et al [26]). Goodness of fit is: (a) 0.9985, (b) 0.9990; (c) 0.9993; (d) 0.9996; (e) 0.9996; (f) 0.9996.
Figure 3. $R(T,B)$ data and fits to Eq. 1 for $C2/m$-SnH$_{12}$ ($P \sim 190$ GPa) measured at warming stage (raw data reported by Hong et al [28]). Goodness of fit is: (a) 0.9987, (b) 0.9990; (c) 0.9992; (d) 0.9996; (e) 0.9996; (f) 0.9996.

Deduced $T_c(B)$ values were used as raw $B_{c2}(T)$ data, which were fitted to upper critical field $s$-wave model [42]:

$$B_{c2}(T) = \frac{\phi_0}{2\pi \xi^2(0)} \cdot \left( \frac{\frac{1.77 - 0.43}{T_c^2} + 0.07 (T_c/T)^4}{1.77} \right)^{\frac{1}{2}} \cdot \left[ 1 - \frac{1}{2k_B T} \cdot \int_0^\infty \frac{de}{\cosh^2 \left( \frac{\sqrt{e^2 + 4\Delta^2(T)}}{2k_B T} \right)} \right]$$

(10)
where $k_B$ is the Boltzmann constant, and the amplitude of temperature dependent superconducting gap, $\Delta(T)$, is given by [43,44]:

$$
\Delta(T) = \Delta(0) \cdot \tanh\left(\frac{\pi k_B T_c}{\Delta(0)} \cdot \sqrt{\eta \cdot \frac{\Delta C}{C} \cdot \left(\frac{T_c}{T} - 1\right)}\right)
$$

(11)

where $\Delta C/C$ is the relative jump in electronic specific heat at $T_c$, and $\eta = 2/3$ for $s$-wave superconductors.

Eqs. 10,11 were used to extract $\xi(0)$, $\Delta(0)$, $T_c$ and $\Delta C/C$ in a variety of superconductors, for instance, in highly-compressed H$_3$S [42], magic-angle twisted bilayer graphene [46], V$_3$Si [47], Nd$_{0.8}$Sr$_{0.2}$NiO$_2$ [48] and iron-based superconductors [47]. Here we applied these equations to extract $\xi(0)$, $\Delta(0)$ and $\frac{2\Delta(0)}{k_B T_c}$ in C2/m-SnH$_{12}$ ($P = 190$ GPa).

Eqs. 10,11 have four-free fitting parameters, $\xi(0)$, $\Delta(0)$, $T_c$, and $\Delta C/C$, i.e. the same number as one in the standard fitting function for the pinning force density, $F_p(B_{appl})$. [48-51]:

$$
F_p(B_{appl}) = F_{p,max} \cdot \left(\frac{B_{appl}}{B_{c2}}\right)^p \cdot \left(1 - \frac{B_{appl}}{B_{c2}}\right)^q
$$

(12)

where $F_{p,max}$, $B_{c2}$, $p$ and $q$ are free-fitting parameters. Thus, Eqs. 9,10 can be characterized as a conventional mathematical tool in terms of the number of free-fitting parameters, where each deduced parameter has clear physical meaning.

It needs to be pointed out that $R(T,B)$ curves were measured at only six $B_{appl}$ values, i.e. $B_{appl} = 0,1,2,3,5,7$ T, which implies that conventional $B_{c2}(T)$ fit to Eqs. 10,11, where all four parameters are free, needs to be adopted for given $B_{c2}(T)$ dataset (it should be noted that usually [42,47] $B_{c2}(T)$ datasets have up to 30 raw upper critical field data). Thus, there is a need to reduce the number of free-fitting parameters in Eqs. 10,11. We used to fix $\frac{\Delta C}{C}$ value in our previous works [52-54] when experiments were performed over either a narrow temperature range, either at limited set of temperatures. Thus, we assumed that the relative...
jump in electronic specific heat at $T_c$ is equal to the Bardeen-Cooper-Schrieffer theory weak-coupling limit for $s$-wave superconductors $[43,44,55,56]$:

$$\frac{\Delta C}{C} = 1.43.$$  \hfill (13)

That left in this case just $T_c$, $\xi(0)$ and $\Delta(0)$ as free fitting parameters in Eqs. 10,11. $B_{c2}(T)$ data fit to the restricted Eqs. 10,11 is shown in Fig. 4, where it can be seen that the fit has narrow 95% uncertainty bands and deduced parameters are $T_c = 64.6 \pm 0.3 K$, $\xi(0) = 6.3 \pm 0.1 \text{ nm}$, $\Delta(0) = 9.15 \pm 0.51 \text{ meV}$, and

$$\frac{2\Delta(0)}{k_B T_c} = 3.28 \pm 0.18.$$  \hfill (14)

**Figure 4.** The upper critical field data, $B_{c2}(T)$, and data fit to Eqs. 3,4 for C2/m-SnH$_{12}$ ($P = 190$ GPa). $\frac{\Delta C}{C}$ was fixed to BCS weak-coupling limit of 1.43. 95% confidence bars are shown by a green shaded area; fit quality is $R = 0.9983$. 
IV. Comparison of C2/m-SnH12 with conventional superconductors

It might be appeared to be strange that deduced ratio of the gap amplitude to the transition temperature \( \frac{2\Delta(0)}{k_B T_c} = 3.28 \pm 0.18 \) is lower than \( s \)-wave BCS weak coupling limit of [43,44,55,56]:

\[
\frac{2\Delta(0)}{k_B T_c} = 3.53
\]  

(15)

However, if we assume that C2/m-SnH12 \((P = 190 \text{ GPa})\) has the Coulomb pseudopotential parameter, \( \mu^* = 0.13 \), which is weighted average value within many first principle calculations of NRTS materials (where \( \mu^* = 0.10-0.16 \) [5,6,9,10,18,25,29,57-71]), and, what is more important, that \( \mu^* = 0.13 \) was one of probable values used by Esfahani et al [29] in their predictive calculations for C2/m-SnH12 phase, than the ratio of \( \frac{k_B T_c}{\hbar \omega_{ln}} \) has got a value:

\[
\frac{k_B T_c}{\hbar \omega_{ln}} = \frac{83}{991} \approx 0.0838.
\]  

(16)

where \( \hbar = \frac{h}{2\pi} \) is the reduced Planck constant, and \( \omega_{ln} = \exp \left[ \int_0^{\omega_{ln}} \frac{F(\omega)}{\omega} d\omega \right] \), where \( F(\omega) \) is the phonon density of states.

In result, the plot of \( \frac{2\Delta(0)}{k_B T_c} \) vs \( \frac{k_B T_c}{\hbar \omega_{ln}} \) (which is often considered as an universal plot for phonon-mediated superconductors [72-75]), C2/m-SnH12 phase falls into the lower branch (Fig. 5), where its NRTS contemplate H3S is located [76].

It should be stressed, that in Fig. 5, a both fitting curves (red and cyan) and their 95% confidence band were not altered from ones in Fig. 4 in Ref. 76, because new fits were not performed (more details about these branches can be found in Ref. 76). It can be seen an unprecedented accuracy for the positioning of C2/m-SnH12 phase in the lower branch. It should be noted that data on the upper branch in Fig. 5 with a very high accuracy can be described by simple elegant equation (Eq. 24 in Ref. 76):
In Fig. 5,b we fit data for lower branch (i.e. for Pb_{0.5}Bi_{0.5}, Pb_{0.75}Bi_{0.25}, Ga, Bi, H_{3}S and C2/m-SnH_{12}) to equation [76]:

\[
\frac{2\Delta(0)}{k_B T_c} = A \cdot \left( 1 + 3.53 \cdot \left( \frac{k_B T_c}{\hbar \omega_{ln}} \right)^{1.29} \right)
\]

(18)

where A is free fitting parameter. It can be seen that 95% confidence band becomes narrower in Fig. 5,b in comparison with Fig. 5,a. Deduced parameter A = 2.86 ± 0.05 is practically undistinguishable from deduced A = 2.87 ± 0.06 reported in Ref. 76 for this parameter.

**Figure 5.** Full dataset of \( \frac{2\Delta(0)}{k_B T_c} \) vs \( \frac{k_B T_c}{\hbar \omega_{ln}} \) from Table IV of Ref. 74 and data points for highly-compressed H_{3}S and SnH_{12}. Fits to Eq. 17 (blue data points, red curve) and Eq. 18 (cyan curve) are shown. a - SnH_{12} does not include in the fit (the fit is a clone from one in Fig. 4 of Ref. 59). b - SnH_{12} does include in the fit. A = 2.86 ± 0.05 and R = 0.948. 95% confidence bars are shown by a cyan shaded area.
IV. C2/m-SnH12 in the Uemura plot

Uemura et al [31,32] reported empirical discovery that all unconventional superconductors, i.e. heavy fermions, cuprates, fullerenes and, later, to this list were added the iron-based superconductors [76,78] and hydrogen-rich superconductors [42,79-81], have the ratio of the superconducting transition temperature, $T_c$, to the Fermi temperature, $T_F$, within a narrow range:

$$0.01 \lesssim \frac{T_c}{T_F} \lesssim 0.05,$$  \hspace{1cm} (19)

while conventional superconductors have much smaller $\frac{T_c}{T_F}$ ratio:

$$\frac{T_c}{T_F} \lesssim 0.001$$ \hspace{1cm} (20)

It should be noted that maximal value of $\frac{T_c}{T_F} = 0.22$ is attributed Bose-Einstein condensates (BEC). Thus, further step to characterize the superconducting state in C2/m-SnH12 phase ($P = 190$ GPa) is to find the $\frac{T_c}{T_F}$ ratio for this compound.

The Fermi temperature can be calculated by an equation [76]:

$$T_F = \frac{\pi^2}{8k_B} \cdot \left(1 + \lambda_{e-ph}\right) \cdot \xi^2(0) \cdot \left(\frac{\alpha k_B T_c}{\hbar}\right)^2,$$ \hspace{1cm} (21)

where $\alpha = \frac{2\delta(0)}{k_B T_c}$, and $\lambda_{e-ph}$ is the electron-phonon coupling constant. For calculations we utilized $\lambda_{e-ph} = 1.25$ reported by Esfahani et al [29] who computed by first-principles calculations several parameters for C2/m-SnH12 phase. The rest of parameters in Eq. 21, i.e. $\alpha$, $T_c$, $\xi(0)$, we deduced from the analysis of $B_{c2}(T)$ data above.

In a result, calculated Fermi temperature is $T_F = 5,658 \pm 906$ K, and in the Uemura plot (Fig. 6), C2/m-SnH12 phase falls into unconventional superconductors band in a close proximity to YBa$_2$Cu$_3$O$_{7-\delta}$ cuprates and in the same $T_c/T_F$ band where all NRTS counterparts are located. To date, an understanding that NRTS materials exhibit unconventional
superconductivity is becoming more acknowledged [18,83,84], because if the superconducting transition temperature, $T_c$, in hydrogen-rich compounds was reasonably well predicted in some (and, what is important to stress, not in all) hydrogen-rich compounds, other calculated superconducting parameters, in particular, the ground state upper critical field and the ground state London penetration depth, are different from experimental values in several times.

Figure 6. $T_c$ vs $T_F$ plot where the $C2/m$-$\text{SnH}_{12}$ ($P = 190$ GPa) phase is shown together with main superconducting families: elemental superconductors, heavy-fermions, pnictides, cuprates, and near-room-temperature superconductors. Reference on original data can be found in Refs. 31,32,42,77-82. Boundary lines for BCS superconductors, for Bose-Einstein condensates and for $T_c/T_F = 0.05, 0.01$ are shown.

V. Conclusions

Recently, Hong et al [28] discovered a new highly-compressed $C2/m$-$\text{SnH}_{12}$ superhydride phase which exhibits the superconducting transition temperature of $T_c = 70$ K at pressure of 190 GPa. Here we analyse the magnetoresistance data in this phase and deduce the ground state superconducting gap of $\Delta(0) = 9.15 \pm 0.51$ meV and the ratio of $2\Delta(0)/k_BT_c = 3.28 \pm 0.18$. Taking in account results of first principles calculations for this phase performed by
Esfahani et al [29], we calculate the Fermi temperature $T_F = 5,658 ± 906 K$ in this phase, which means that in the Uemura plot [31,32], this new superhydride falls to unconventional superconductors band, where all other hydrogen-rich counterparts, including near-room-temperature superconductors, are located.

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References

[1] Satterthwaite C B and Toepke I L 1970 Superconductivity of hydrides and deuterides of thorium Phys. Rev. Lett. 25 741-743
[2] Ashcroft N W 1968 Metallic hydrogen: a high-temperature superconductor? Phys. Rev. Lett. 21 1748-1749
[3] Ashcroft N W 2004 Hydrogen dominant metallic alloys: high temperature superconductors? Phys. Rev. Lett. 92 187002
[4] Drozdov A P, Eremets M I, Troyan I A, Ksenofontov V, Shylin S I 2015 Conventional superconductivity at 203 kelvin at high pressures in the sulfur hydride system Nature 525 73-76
[5] Zhou D, et al 2020 Superconducting praseodymium superhydrides Sci. Adv. 6 eaa6849
[6] Chen W, et al. 2021 High-pressure synthesis of barium superhydrides: Pseudocubic BaH$_{12}$ Nature Communications 12 273
[7] Drozdov A P, Eremets M I and Troyan I A 2015 Superconductivity above 100 K in PH$_3$ at high pressures arXiv:1508.06224
[8] Matsuoka T, et al 2019 Superconductivity of platinum hydride Phys. Rev. B 99 144511
[9] Chen W, Semenok D V, Huang X, Shu H, Li X, Duan D, Cui T and Oganov A R 2021 High-temperature superconductivity in cerium superhydrides arXiv:2101.01315
[10] Semenok D V, Kvashnin A G, Ivanova A G, Svitlyk V, Fominski V Yu, Sadakov A V, Sobolevskiy O A, Pudalov V M, Troyan I A and Oganov A R 2020 Superconductivity at 161 K in thorium hydride ThH$_{10}$: Synthesis and properties Materials Today 33 36-44
[11] Wang N, et al 2021 A low-$T_c$ superconducting modification of Th$_4$H$_{15}$ synthesized under high pressure Superconductor Science and Technology 34 034006
[12] Einaga M, et al 2016 Crystal structure of the superconducting phase of sulfur hydride Nature Physics 12 835-838
[13] Mozaffari S et al 2019 Superconducting phase diagram of H$_2$S under high magnetic fields Nat. Commun. 10 2522
[14] Minkov V S, Prakapenka V B, Greenberg E, Eremets M I 2020 Boosted $T_c$ of 166 K in superconducting D$_3$S synthesized from elemental sulfur and hydrogen Angew. Chem. Int. Ed, 59 18970-18974
[15] Matsumoto R, et al. 2020 Electrical transport measurements for superconducting sulfur hydrides using boron-doped diamond electrodes on beveled diamond anvil Superconductor Science and Technology 33 124005
[16] Huang X, et al 2019 High-temperature superconductivity in sulfur hydride evidenced by alternating-current magnetic susceptibility National Science Review 6 713-718
[17] Laniel D, et al 2020 Novel sulfur hydrides synthesized at extreme conditions Phys. Rev. B 102 134109
[18] Troyan I A, et al. 2021 Anomalous high-temperature superconductivity in YH$_6$ Advanced Materials, in press https://doi.org/10.1002/adma.202006832
[19] Kong P P, et al. 2019 Superconductivity up to 243 K in yttrium hydrides under high pressure arXiv:1909.10482
[20] Somayazulu M, et al. 2019 Evidence for superconductivity above 260 K in lanthanum superhydride at megabar pressures Phys. Rev. Lett. 122 027001
[21] Drozdov A P, et al 2019 Superconductivity at 250 K in lanthanum hydride under high pressures Nature 569 528-531
[22] Sakata M, et al. 2020 Superconductivity of lanthanum hydride synthesized using AlH$_3$ as a hydrogen source Superconductor Science and Technology 33 114004
[23] Hong F, et al 2020 Superconductivity of lanthanum superhydride investigated using the standard four-probe configuration under high pressures Chinese Physics Letters 37 107401
[24] Sun D, et al 2020 High-temperature superconductivity on the verge of a structural instability in lanthanum superhydride arXiv:2010.00160
[25] Semenok D V, et al 2020 Superconductivity at 253 K in lanthanum-yttrium ternary hydrides arXiv:2012.04787
[26] Ma L, et al 2021 Experimental observation of superconductivity at 215 K in calcium superhydride under high pressure arXiv:2103.16282
[27] Li Z W, et al 2021 Superconductivity above 200 K observed in superhydrides of calcium arXiv:2103.16917
[28] Hong F, et al 2021 Superconductivity at ~70 K in tin hydride SnH$_4$ under high pressure arXiv:2101.02846
[29] Mahdi Davari Esfahani M, et al 2016 Superconductivity of novel tin hydrides (Sn$_n$H$_m$) under pressure Sci. Rep. 6 22873
[30] Jones C K, Hulm J K, Chandrasekhar B S 1964 Upper critical field of solid solution alloys of the transition elements Rev. Mod. Phys. 36 74-76
[31] Uemura Y J 1997 Bose-Einstein to BCS crossover picture for high-$T_c$ cuprates Physica C 282-287 194-197
[32] Uemura Y J 2019 Dynamic superconductivity responses in photoexcited optical conductivity and Nernst effect Phys. Rev. Materials 3 104801
[33] Talantsev E F and Stolze K 2021 Resistive transition of hydrogen-rich superconductors Superconductor Science and Technology, accepted, https://doi.org/10.1088.1361-6668/abf23c
[34] Tinkham M 1988 Resistive transition of high-temperature superconductors Phys. Rev. Letters 61 1658-1661
[35] Hirsch J E and Marsiglio F 2021 Nonstandard superconductivity or no superconductivity in hydrides under high pressure Phys. Rev. B 103 134505
[36] Talantsev E F 2020 Advanced McMillan's equation and its application for the analysis of highly-compressed superconductors Superconductor Science and Technology 33 094009
[37] Antonova O V and Volkov A Yu 2012 Changes of microstructure and electrical resistivity of ordered Cu-40Pd (at.%) alloy under severe plastic deformation Intermetallics 21 1-9
[38] Volkov A Yu and Kazantsev 2012 Impact of the initial state on the structure and properties of the ordered CuAu alloy The Physics of Metals and Metallography 113 62-71
[39] Volkov A Yu, Novikova O S and Antonov B D 2013 The kinetics of ordering in an equiatomic CuPd alloy: A resistometric study Journal of Alloys and Compounds 581 625-631
[40] Ohta K, Kuwayama Y, Hirose K, Shimizu K and Ohishi Y 2016 Experimental determination of the electrical resistivity of iron at Earth’s core conditions 534 95-98
[41] Deng L, Seagle C, Fei Y and Shahar A 2013 High pressure and temperature electrical resistivity of iron and implications for planetary cores Geophysical Research Letters 40 33-37
[42] Talantsev E F 2019 Classifying superconductivity in compressed H2S Modern Physics Letters B 33 1950195
[43] Gross F, et al. 1986 Anomalous temperature dependence of the magnetic field penetration depth in superconducting UBe13, Z. Phys. B 64 175-188
[44] Gross-Alltag F, Chandrasekhar B S, Einzel D, Hirschfeld P J and Andres K 1991 London field penetration in heavy fermion superconductors Z. Phys. B 82 243-255
[45] Talantsev E F, Mataira R C, Crump W P 2020 Classifying superconductivity in Moiré graphene superlattices Scientific Reports 10 212
[46] Talantsev E F 2020 In-plane p-wave coherence length in iron-based superconductors Results in Physics 18 103339
[47] Talantsev E F 2020 Classifying superconductivity in an infinite-layer nickelate Nd0.8Sr0.2NiO2 Results in Physics 17 103118
[48] Kramer E J 1973 Scaling laws for flux pinning in hard superconductors J. Appl. Phys. 44 1360-1370
[49] Dew-Hughes D 1974 Flux pinning mechanisms in type II superconductors Philosophical Magazine 30 293-305
[50] Oh S, et al 2007 Lorentz-force dependence of the critical current for SmBCO coated conductor J. Appl. Phys. 102 043904
[51] Iida K, Hänsch J and Tarantini C 2018 Fe-based superconducting thin films on metallic substrates: Growth, characteristics, and relevant properties Appl. Phys. Rev. 5 031304
[52] Talantsev E F, Crump W P, Island J O, Xing Y, Sun Y, Wang J, Tallon J L 2017 On the origin of critical temperature enhancement in atomically thin superconductors 2D Materials 4 025072
[53] Talantsev E F, Crump W P, Tallon J L 2017 Thermodynamic parameters of single- or multi-band superconductors derived from self-field critical currents Annalen der Physik 529 1700197
[54] Talantsev E F, Crump W P, Storey J G, Tallon J L 2017 London penetration depth and thermal fluctuations in the sulphur hydride 203 K superconductor Annalen der Physik 529 1600390
[55] Bardeen J, Cooper L N, and Schrieffer J R 1957 Theory of superconductivity Phys. Rev. 108 1175-1204
[56] Eliashberg G M 1960 Interactions between electrons and lattice vibrations in a superconductor Soviet Phys. JETP 11 696-702
[57] Duan D, et. al. 2014 Pressure-induced metallization of dense (H2S)2H2 with high-Tc superconductivity Scientific Reports 4 6968
[58] Errea I, et al 2020 Quantum crystal structure in the 250-kelvin superconducting lanthanum hydride Nature 578 66-69
[59] Heil C, di Cataldo S, Bachelet G B and Boeri L 2019 Superconductivity in sodalite-like yttrium hydride clathrates Physical Review B 99 220502(R)
[60] Durajski A P 2016 Quantitative analysis of nonadiabatic effects in dense H$_2$S and PH$_3$ superconductors Sci. Rep. 6 38570
[61] Liu H, Naumov I I, Hoffmann R, Ashcroft N W and Hemley R J 2017 Potential high-$T_c$ superconducting lanthanum and yttrium hydrides at high pressure PNAS 114 6990-6995
[62] Errea I et al 2015 High-pressure hydrogen sulfide from first principles: A strongly anharmonic phonon-mediated superconductor Phys. Rev. Lett. 114 157004
[63] Durajski A P and Szcześniak R 2018 Structural, electronic, vibrational, and superconducting properties of hydrogenated chlorine J. Chem. Phys. 149 074101
[64] Chen J, Cui W, Shi J, Xu M, Hao J, Durajski A P, and Li Y 2019 Computational design of novel hydrogen-rich YS–H compounds ACS Omega 4 14317-14323
[65] Alarco J A, Talbot P C and Mackinnon I D R 2018 Identification of superconductivity mechanisms and prediction of new materials using Density Functional Theory (DFT) calculations J. Phys.: Conf. Ser. 1143 012028
[66] Semenok D V, Kvasnin A G, Kruglov I A, and Oganov A R 2018 Actinium hydrides AcH$_{10}$, AcH$_{12}$, and AcH$_{16}$ as high-temperature conventional superconductors J. Phys. Chem. Lett. 9 1920-1926
[67] Sun Y, Lv J, Xie Y, Liu H, and Ma Y 2019 Route to a superconducting phase above room temperature in electron-doped hydride compounds under high pressure Phys. Rev. Lett. 123 097001
[68] Hou P, Belli F, Bianco R, Errea I 2021 Strong anharmonic and quantum effects in Pm-3n-AIH$_3$ under high pressure: A first-principles study arXiv: 2102.00072
[69] Camargo-Martínez J A, et al 2019 High-$T_c$ superconductivity in H$_3$S: pressure effects on the superconducting critical temperature and Cooper pair distribution function Supercond. Sci. Technol. 32 125013
[70] Camargo-Martínez J A, et al 2020 The higher superconducting transition temperature $T_c$ and the functional derivative of $T_c$ with $\alpha^2F(\omega)$ for electron–phonon superconductors J. Phys.: Condens. Matter 32 505901
[71] Durajski A P, Wang C, Li Y, Szcześniak R, Cho J-H 2021 Evidence of phonon-mediated superconductivity in LaH$_{10}$ at high pressure Annalen der Physik https://doi.org/10.1002/andp.202000518
[72] Mitrovic B, Zarate H G, Carbotte J P 1984 The ratio $2\Delta_0/k_BT_c$ within Eliashberg theory Phys. Rev. B 29 184-190
[73] Marsiglio F and Carbotte J P 1986 Strong-coupling corrections to Bardeen-Cooper-Schrieffer ratios Phys Rev B 33 6141-6146
[74] Carbotte J P 1990 Properties of boson-exchange superconductors Rev. Mod. Phys. 62 1027
[75] Nicol E J, Carbotte J P 2015 Comparison of pressurized sulfur hydride with conventional superconductors Phys. Rev. B 91 220507(R)
[76] Talantsev E F 2020 Double-valued strong-coupling corrections to Bardeen-Cooper-Schrieffer ratios Superconductor Science and Technology 33 124003
[77] Qian T, et al. 2011 Absence of a hololike Fermi surface for the iron-based $K_{0.8}$Fe$_{1.7}$Se$_2$ superconductor revealed by angle-resolved photoemission spectroscopy Phys. Rev. Lett. 106 187001
[78] Hashimoto K, Cho K, Shibauchi T, Kasahara S, Mizukami Y, Katsumata R, Tsuizhara Y, Terashima T, Ikeda H, Tanatar M A, Kitano H, Salovich N, Giannetta R W, Walmsley P, Carrington A, Prozorov R, Matsuda Y 2012 A sharp peak of the zero-temperature penetration depth at optimal composition in BaFe$_2$(As$_{1-x}$P$_x$)$_2$ Science 336 1554-1557
[79] Talantsev E F 2020 An approach to identifying unconventional superconductivity in highly-compressed superconductors Superconductor Science and Technology 33 124001
[80] Talantsev E F 2020 Unconventional superconductivity in highly-compressed unannealed sulphur hydride *Results in Physics* **16** 102993

[81] Talantsev E F 2019 Classifying hydrogen-rich superconductors *Materials Research Express* **6** 106002

[82] Ye J T, *et al.* 2012 Superconducting dome in a gate-tuned band insulator *Science* **338** 1193

[83] Dogan M and Cohen M L 2021 Anomalous behavior in high-pressure carbonaceous sulfur hydride *Physica C* 1353851 ([https://doi.org/10.1016/j.physc.2021.1353851](https://doi.org/10.1016/j.physc.2021.1353851))

[84] Wang T, *et al.* 2021 Absence of conventional room temperature superconductivity at high pressure in carbon doped H$_3$S *arXiv*:2104.03710