FUEL: Fast UAV Exploration using Incremental Frontier Structure and Hierarchical Planning

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Abstract—Autonomous exploration is a fundamental problem for various applications of unmanned aerial vehicles (UAVs). Existing methods, however, were demonstrated to have low efficiency, due to the lack of optimality consideration, conservative motion plans and low decision frequencies. In this paper, we propose FUEL, a hierarchical framework that can support Fast UAV Exploration in complex unknown environments. We maintain crucial information in the entire space required by exploration planning by a frontier information structure (FIS), which can be updated incrementally when the space is explored. Supported by the FIS, a hierarchical planner plan exploration motions in three steps, which find efficient global coverage paths, refine a local set of viewpoints and generate minimum-time trajectories in sequence. We present extensive benchmark and real-world tests, in which our method completes the exploration tasks with unprecedented efficiency (3-8 times faster) compared to state-of-the-art approaches. Our method will be made open source to benefit the community.

I. INTRODUCTION

Unmanned aerial vehicles, especially quadrotors have gained widespread popularity in various applications, such as inspection, precision agriculture, and search and rescue. Among the tasks, autonomous exploration, in which the vehicle explores and maps the unknown environment to gather information, is a fundamental component to enable effective operation.

Despite the various exploration planning methods presented in recent years, most of them are demonstrated to have deficient efficiency, prohibiting them from real-world usage. First of all, existing planners plan exploring motions in greedy manners, such as maximizing the immediate information gain, or navigating to the closest unknown region. The greedy strategies ignore global optimality and therefore result in low overall efficiency. Besides, most methods generate rather conservative motions in order to guarantee information gain and safety simultaneously in previously unknown environments. Low-speed exploration, however, disallows quadrotors to fully exploit their dynamic capability to fulfill the missions. Last but not least, many methods suffer from high computational overhead and can not response quickly and frequently to environmental changes. However, to enable faster exploration, it is desirable to replan new motion immediately whenever new information of the environment is available.

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Motivated by the above facts, this paper proposes FUEL, a hierarchical framework that can support Fast UAV Exploration in complex environments. We introduce a frontier information structure (FIS), which contains essential information in the entire space required by exploration planning. The structure can be updated efficiently and incrementally when new information is collected, so it is capable of supporting high frequency planning. Based on the FIS, a hierarchical planner generates exploring motion in three coarse-to-fine steps. It starts by finding a global exploration tour that is optimal in the context of accumulated environment information. Then, viewpoints on a local segment of the tour are refined, further improving the exploration rate. Finally, a safe, dynamically feasible and minimum-time trajectory is generated. The planner produces not only efficient global coverage path, but also safe and agile local maneuvers. Moreover, the planner is triggered whenever new regions are explored, so that the quadrotor always responses promptly to any environmental changes, leading to consistently fast exploration.

Fig. 1. A quadrotor autonomous exploration test conducted in a complex indoor scene. Video of the experiments is available at: https://www.dropbox.com/sh/oxl2giyawmv8j5o/AAAdsuF_ES2nWQ3sDhhaGc1a?dl=0.

(a) A cluttered environment for the exploration tests.

(b) The online built map and executed trajectory.

The open-source code will be released at https://github.com/HKUST-Aerial-Robotics/Fast-Planner
We compare our method with classic and state-of-the-art methods in simulation. Results show that in all cases our method achieves complete exploration in much shorter time (3-8 times faster). What’s more, we conduct fully onboard real-world exploration in various challenging environments. Both the simulation and real-world tests demonstrate unprecedented performance of our method compared to state-of-the-art ones. To benefit the community, we will make the source code public. The contributions of this paper are summarized as follows:

1) An incrementally updated FIS, which captures essential information of the entire explored space and facilitates exploration planning in high frequency.

2) A hierarchical planning method, which generates efficient global coverage paths, and safe and agile local maneuvers for high-speed exploration.

3) Extensive simulation and real-world tests that validate the proposed method. The source code of our system will be made public.

II. RELATED WORK

A. Exploration Path Planning

Robotic exploration, which deals with the problem of mapping unknown environments quickly and completely, has been studied for years. Among the various proposed methods, the frontier-based approaches are one type of classic approaches. The methods are first introduced in [1] and evaluated more comprehensively afterwards in [2]. To detect frontiers in 3D space, a stochastic differential equation-based method is proposed in [3]. In the original method [1], the closest frontier is selected as the next target. [4] presented a different scheme of frontier selection to enable higher flight speed, which improves the exploration rate. In [5], a differentiable measure of information gain based on frontier is introduced, allowing path to be optimized with gradient information.

Sampling-based exploration, as another type of major approaches, generate viewpoints randomly to explore the space. These methods are closely related to the concept of next best view (NBV) [6], which computes covering views repeatedly to obtain a complete model of a scene. [7] first used NBV in 3D exploration, in which it expands RRTs with accessible space and executes the edge with highest information gain in a receding horizon fashion. The method was extended to consider uncertainty of localization [8], visual importance of different objects [9] and inspection tasks [10] later. To avoid discarding the expanded trees directly, roadmaps are constructed in [11, 12] to reuse previous knowledge. [13] maintains and refines a single tree continuously using a rewiring scheme inspired by RRT*. To achieve faster flight, [14] samples safe and dynamically feasible motion primitives directly and execute the most informative one.

There are also methods combining the advantages of frontier-based and sampling-based approaches. [15, 16] plan global path toward frontiers and sample path locally. [15] also presented a gradient-based method to optimize the local path. [17] samples viewpoints around frontiers and finds the global shortest tour passing through them. [18] generates inspection paths that cover the frontier completely using a sampling-based algorithm.

Most of existing methods make decision greedily and does not account for the dynamics of the quadrotor, which leads to inefficient global tours and conservative maneuvers. In contrast, we plan tours that efficiently cover the entire environment and generate dynamically feasible minimum-time trajectories to enable agile flight.

B. Quadrotor Trajectory Planning

Trajectory planning for quadrotor has been widely studied recently. There are two major categories of approaches, the hard-constrained and soft-constrained ones. Hard-constrained methods are pioneered by minimum-snap trajectory [19], which generates polynomial trajectories of the flat outputs of quadrotors through quadratic programming (QP). After it, a closed-form solution was presented [20]. Based on [19], [21]–[23] extract convex shapes safe regions and solve QP within them to generate smooth and safe trajectories. To obtain a more reasonable time allocation, fast marching [22], kinodynamic search [23] and mixed integer-based methods [24] are proposed. [22] also introduced an efficient Bézier curve-based method to guarantee feasibility.

Soft-constrained methods typically formulate trajectory generation as non-linear optimization trading off several objectives. Recently [25]–[30] applied them to the local replanning problem, in which the methods demonstrate attractive performance. The methods were revived by [31] and extended to continuous-time quadrotor trajectories [25] later. To relieve the issue of local minima, [26] initializes the optimization with collision-free paths. [27] introduces uniform B-splines and utilizes the continuity and locality properties of them for replanning. More recently, [28] further exploited B-splines and demonstrated fast flight in field tests, [28] is further improved with topological guiding paths and perception-awareness in [29, 30].

In this paper, we base our trajectory planning on [28] but extend it to optimize all parameters of B-splines. In this way, the total trajectory time can be minimized so that the unknown space is explored with higher navigation speed.

III. SYSTEM OVERVIEW

The proposed framework operates upon a voxel grid map. As illustrated in Fig.2, it is composed of an incremental...
Fig. 3. Incremental frontier detection and clustering. Top: detecting and removing outdated frontiers. Bottom: new frontier is detected (left) and PCA is performed, the large cluster is split into two smaller ones (right).

update of the FIS (Sect.IV) and a hierarchical exploration planning approach (Sect.V). Whenever the map is updated using sensor measurements, it is examined whether any frontier clusters are influenced. If so, FISs of influenced clusters are removed while new frontiers along with their FISs are extracted (Sect.IV). After that, the exploration planning is triggered, which finds global exploration tour, refines local viewpoints, and generates trajectory to a selected viewpoint successively (Sect.V). The exploration is considered finished if no frontier exists.

IV. INCREMENTAL FRONTIER INFORMATION STRUCTURE

As presented in classic frontier-based exploration [1], frontiers are defined as known-free voxels right adjacent to unknown voxels, which are grouped into clusters to guide the navigation. Traditionally, the extracted information is too coarse to do fine-grained decision making. Besides, frontiers are retrieved by processing the entire map, which is not scalable for large scenes and high planning frequencies. In this work, we extract richer information from frontiers to enable more elaborate planning, and develop an incremental approach to detect frontiers within locally updated map.

A. Frontier Information Structure

A frontier information structure $FI_i$ is computed when a new frontier cluster $F_i$ is created. It stores all cells $C_i$ belonging to the cluster and the average position $p_{avg,i}$ of $C_i$. The axis-aligned bounding box (AABB) of the cluster $B_i$ is also computed, in order to accelerate the detection of frontier changes (Sect.IV-B). To serve the exploration planning (Sect.V), candidate viewpoints $VP_i$ are generated around the cluster. Besides, a doubly linked list $L_{cost,i}$ containing connection costs between $F_i$ and all other clusters is computed. Data stored by a FIS is listed in Tab.I.

B. Incremental Frontier Detection and Clustering

As depicted in Fig.3, every time the map is updated by sensor measurements, the AABB of the updated region $B_m$ is also recorded, within which outdated frontier clusters are removed and new ones are searched. It starts with going through all clusters and returning only those whose AABBs ($B_i$) intersect with $B_m$. Then, precise checks are conducted for the returned clusters, among which the ones containing cells that are no longer frontier are removed. These two processes are inspired by the broad/narrow phase collision detection algorithms, which eliminate most unaffected clusters in a fast way and significantly reduce the number of expensive precise checks.

After the removal, new frontiers are searched and clustered into groups by the region growing algorithm, similar to classic frontier-based method. Among the groups, the ones with small number of cells typically resulting from noisy sensor observations are ignored. The remaining groups, however, may contain large-size clusters which are not conducive to distinguishing distinctive unknown regions and making elaborate decisions. Therefore, we perform Principal Component Analysis (PCA) for each cluster and split it into two uniform ones along the first principal axis, if the largest eigenvalue exceeds a threshold. The split is conducted recursively so that all large clusters are divided into small ones.

C. Viewpoint Generation and Cost Update

Intuitively, a frontier cluster implies a potential destination to explore the space. However, unlike previous approaches which simply navigating to the center of a cluster, we desire more elaborate decision making. To this end, when a cluster $F_i$ is created, we generate a rich set of viewpoints $VP_i =$

Fig. 4. Generating candidate viewpoints for a frontier cluster. Within the cylindrical coordinate system centered at the average position of the cluster, points are sampled uniformly.

| Data            | Explanation                                                                 |
|-----------------|-----------------------------------------------------------------------------|
| $C_i$           | Frontier cells that belong to the cluster                                   |
| $p_{avg,i}$     | Average position of $C_i$                                                   |
| $B_i$           | Axis-aligned bounding box of $C_i$                                         |
| $VP_i$          | Viewpoints covering the cluster                                            |
| $L_{cost,i}$    | Doubly linked list of connection costs to all other clusters                |

TABLE I DATA CONTAINED BY A FIS $FI_i$ OF CLUSTER $F_i$. |
\{x_{i,1}, x_{i,2}, \cdots, x_{i,n_i}\} covering it, where \(x_{i,j} = (p_{i,j}, \xi_{i,j})\). VP, are found by uniformly sampling points in the cylindrical coordinate system whose origin locates at the cluster’s center, as displayed in Fig.4. For each of the sampled points \(p\) lying within the free space, the yaw angle \(\xi\) is determined as the one maximizing sensor coverage to the cluster, by using an yaw optimization method similar to [11]. The coverage is evaluated as the number of frontier cells that comply with the sensor model and are not occluded by occupied voxels. Then, viewpoints with coverage higher than a threshold are reserved and sorted in descending order of coverage. We reserve at most \(N_{\text{view}}\) viewpoints in \(VP_i\) \((n_i \leq N_{\text{view}})\) to make the local viewpoint refinement (Sect.V) tractable.

To perform global planning of exploration tour (Sect.V), a connection cost between each pair of clusters \((F_{k_1}, F_{k_2})\) is required. Let \(t_{lb}(x_{k_1,j_1}, x_{k_2,j_2})\) denotes a time lower bound when moving between two viewpoints \(x_{k_1,j_1}\) and \(x_{k_2,j_2}\), it is computed by:

\[
\begin{align*}
t_{lb}(x_{k_1,j_1}, x_{k_2,j_2}) &= \max \left\{ \frac{\text{Length}(P(p_{k_1,j_1}, p_{k_2,j_2}))}{v_{\text{max}}}, \frac{2\pi - |\xi_{k_1,j_1} - \xi_{k_2,j_2}|}{\xi_{\text{max}}} \right\}, \\
&= \min \left( \frac{\xi_{k_1,j_1} - \xi_{k_2,j_2}}{2\pi}, 1 \right) \end{align*}
\]

where \(P(p_{k_1,j_1}, p_{k_2,j_2})\) denote the shortest path between \(p_{k_1,j_1}\) and \(p_{k_2,j_2}\), \(v_{\text{max}}\) and \(\xi_{\text{max}}\) are the limits of velocity and angular rate of yaw. For each pair \((F_{k_1}, F_{k_2})\), we select the viewpoints with highest coverage and estimate the cost as \(t_{lb}(x_{k_1,1}, x_{k_2,1})\), in which \(P(p_{k_1,1}, p_{k_2,1})\) is searched using the A* algorithm.

Note that computing connection costs between all pairs of \(N_{\text{cls}}\) clusters from scratch requires \(O(N_{\text{cls}}^2)\) A* searching, which is considerably expensive. Fortunately, the costs can also be computed in an incremental manner. When any outdated clusters are removed (Sect.IV-B), associated cost items in \(L_{\text{cost},i}\) of all remaining FISs are erased. After that, connection costs from each new cluster to all other clusters are computed and inserted into \(L_{\text{cost},i}\). Suppose there are \(k_{\text{new}}\) new clusters in each frontier detection, the above update scheme takes \(O(k_{\text{new}} \cdot N_{\text{cls}})\) time. Practically, \(k_{\text{new}}\) is small and can be regarded as a constant factor, resulting in a linear time update of connection costs.

V. Hierarchical Exploration Planning

Instead of adopting greedy exploration strategies or generating conservative maneuvers, we produce global path to cover the frontiers efficiently and plan safe and agile motions for faster flight. Our planner takes inspiration from the recent hierarchical quadrotor planning paradigm [21, 22, 28], and make decisions in three phases, as showed in Fig.5.

A. Global Exploration Tour Planning

Our exploration planning begins with finding a global tour to cover existent frontier clusters efficiently. Inspired by [17], we formulate it as a variant of the Traveling Salesman Problem (TSP), which computes an open-loop tour starting from the current viewpoint and passing viewpoints at all clusters. We reduce this variant to an standard Asymmetric TSP (ATSP) that can be solved quickly by available algorithms, by properly designing the engaged cost matrix \(M_{\text{sp}}\).

Assume there are \(N_{\text{cls}}\) clusters totally, \(M_{\text{sp}}\) corresponds to a \(N_{\text{cls}}+1\) dimensions square matrix. The major part is the \(N_{\text{cls}} \times N_{\text{cls}}\) block composed of the connection cost between each pair of frontier clusters, which is computed as:

\[
M_{\text{sp}}(k_1, k_2) = M_{\text{sp}}(k_2, k_1) = t_{lb}(x_{k_1,1}, x_{k_2,1}), \quad k_1, k_2 \in \{1, 2, \cdots, N_{\text{cls}}\}
\]

As mentioned in Sect.IV-C, this information is maintained when frontiers are detected. Thus, the \(N_{\text{cls}} \times N_{\text{cls}}\) block can be filled without extra overhead.

The first row and column of \(M_{\text{sp}}\) are associated with the current viewpoint \(x_0 = (p_0, \xi_0)\) and \(N_{\text{cls}}\) clusters. Starting from \(x_0\), the cost to the \(k\)-th cluster is evaluated by:

\[
M_{\text{sp}}(0, k) = t_{lb}(x_0, x_{k,1}) + w_c \cdot c_c(x_{k,1}), \quad k \in \{1, 2, \cdots, N_{\text{cls}}\}
\]

where a motion consistency cost \(c_c(x_{k,1})\) is introduced, which is generally computed as:

\[
c_c(x_{k,j}) = \cos^{-1} \left( \frac{(p_{k,j} - p_0) \cdot v_0}{\|p_{k,j} - p_0\| \|v_0\|} \right)
\]

In this way, going back to the current viewpoint in any closed-loop tours contributes no extra cost, so each closed-loop tour always contains an open-loop one with identical cost. As a result, we can obtain the optimal open-loop tour by
depicted in Fig. 6. We found consecutive clusters whose exploration rate, by using a graph search approach, as from which we select the optimal set of viewpoints.

B. Local Viewpoint Refinement

The global tour planning finds a promising order to visit all clusters. Nonetheless, it involves only single viewpoint of each cluster, which are not necessarily the best combination among all viewpoints.

To this end, a richer set of viewpoints on a truncated segment of the global tour are considered to further improve the exploration rate, by using a graph search approach, as depicted in Fig. 6. We found consecutive clusters whose viewpoints on the global tour are closer than $R_{tf}$ to the current position. To simplify the notation, suppose that $F_i, 1 \leq i \leq N_{rf}$ are the considered clusters. We create graph nodes for their viewpoints $VP_i$ and the current viewpoint $x_0$. Then each node is connected to other nodes associated with the next cluster with a directed edge, which compose a directed acyclic graph capturing possible variation of the truncated tour. We utilize the Dijkstra algorithm to search for the optimal local tour $\Xi = \{x_{1,j_1}, x_{2,j_2}, \ldots, x_{N_{rf},j_{N_{rf}}}\}$ that minimizes the cost:

$$c_{df}(\Xi) = t_{ib}(x_0, x_{1,j_1}) + w_c \cdot c_c(x_{1,j_1}) + t_{ib}(x_{N_{rf},j_{N_{rf}}}, x_{N_{rf}+1,1}) + \sum_{k=1}^{N_{rf}-1} t_{ib}(x_{k,j_k}, x_{k+1,j_{k+1}})$$

which also consists of time lower bounds and motion consistency.

C. Minimum-time B-spline Trajectory

Given the discrete viewpoints, continuous trajectories are required for smooth navigation. Our quadrotor trajectory planning is based on a state-of-the-art method [28], which generates smooth, safe and dynamically feasible B-spline trajectories. We go one step further to optimize all parameters of B-splines, so that the total trajectory time is minimized to enable the quadrotor to fully utilize its dynamic capability.

As the quadrotor dynamics are differentially flat [19], we plan trajectories for the flat outputs $x \in \{x, y, z, \xi\}$. Let $X_{cb} = \{x_{c,0}, x_{c,1}, \ldots, x_{c,N_b}\}$ where $x_{c,i} = (p_{c,i}, \xi_{c,i})$ be the $N_b + 1$ control points of a $p_b$ degree uniform B-spline, and $\Delta t_b$ be the knot span. We find the B-spline that trades-off smoothness and total trajectory time, and satisfies safety, dynamic feasibility and boundary state constraints. It can be formulated as an following optimization problem:

$$\arg\min_{x_{c,i}, \Delta t_b} f_s + w_t T + \lambda_c f_c + \lambda_d (f_v + f_s) + \lambda_{bs} f_{bs}$$

Similar to [28], $f_s$ is the elastic band smoothness cost:

$$f_s = \sum_{i=0}^{N_b-2} s_i^T R_s s_i, \quad s_i = x_{c,i+2} - 2x_{c,i+1} + x_{c,i}$$

in which $R_s$ is the penalty matrix:

$$R_s = \begin{bmatrix} w_s p & 0 \\ 0 & w_s \xi \end{bmatrix}$$

$T$ is the total trajectory time depending on $\Delta t_b$ and the number of B-spline segments:

$$T = (N_b + 1 - p_b) \cdot \Delta t_b$$

where $d(p_{c,i})$ is the distance of point $p_{c,i}$ to the nearest obstacle, which can be obtained from the Euclidean signed distance field (ESDF) maintained by the mapping module. $f_v$ and $f_s$ penalize infeasible velocity and acceleration:

$$f_v = \sum_{i=0}^{N_{tf}-1} \sum_{\mu \in \{x,y,z\}} P(\mu_{\max},|\dot{p}_{c,i,\mu}|) + P(\dot{\xi}_{\max},|\ddot{\xi}_{c,i}|)$$

in which the control points of derivatives are utilized:

$$X_{c,i} = \begin{bmatrix} \dot{p}_{c,i,x} & \dot{p}_{c,i,y} & \dot{p}_{c,i,z} \\ \dot{\xi}_{c,i} \end{bmatrix}^T = \frac{x_{c,i+2} - 2x_{c,i+1} + x_{c,i}}{\Delta t_b}$$

In Equ. 12, 13 and 14, the convex hull property of B-spline is utilized to ensure the feasibility efficiently. For brevity we refer the reader to [28] for more details.

Lastly, we set the 0-th to 2-th order derivatives at the start to the instantaneous state $(\dot{x}_0, \ddot{x}_0, \dddot{x}_0)$ for smooth motion. The 0-th order derivative at the end is also determined by
the viewpoint $x_{\text{next}}$ to be visited. In implementation we use cubic B-splines, so the associated cost is:

$$f_{bs} = \left\| \frac{1}{6}(x_{c,0} + 4x_{c,1} + x_{c,2}) - x_0 \right\|^2 + \left\| \frac{1}{2}(x_{c,0} + x_{c,1}) - \dot{x}_0 \right\|^2$$

$$+ \left\| \ddot{x}_{c,0} - \ddot{x}_0 \right\|^2 + \left\| \frac{1}{6}(x_{c,N_b-2} + 4x_{c,N_b-1} + x_{c,N_b}) - x_{\text{next}} \right\|^2$$

(17)

VI. RESULTS

A. Implementation Details

We set $w_c = 1.5$ in Equ.3 and 6. In global tour planning, the ATSP is solved using a Lin-Kernighan-Helsgaun heuristic solver [32]. In local viewpoint refinement, we reserve at most $N_{\text{view}} = 15$ viewpoints in each FIS and truncate the global tour within radius $R_d = 5.0$. For trajectory optimization, we use $w_{x,p} = 5.0$, $w_{x,L} = 2.5$, $w_t = 1.0$, $\lambda_c = \lambda_b = 10.0$, $\lambda_d = 2.0$ and $d_{\text{min}} = 0.4$ and solve the problem with a general non-linear optimization solver NLopt\(^2\). Cubic B-spline ($p_b = 3$) is used as the trajectory representation.

In all field experiments, we localize the quadrotor by a visual-inertial state estimator [33]. A volumetric mapping framework [34] is utilized to map the environments. Similar to [35], it builds an occupancy grid map and also maintains an ESDF to facilitate the trajectory planning. We use a geometric controller [36] for tracking control of the $(x, y, z, \xi)$ trajectory. We equipped our customized quadrotor platform with an Intel RealSense Depth Camera D435i. All the above modules run on an Intel Core i7-8550U CPU.

B. Benchmark and Analysis

We test our proposed framework in simulation. We benchmark it in a bridge scenario and a large maze scenario. Three methods are compared: the NBVP [7], the classic frontier method [1] and the rapid frontier method [4]. Note that no open source code is available for [4], so we use our implementation. In all tests the dynamic limits are set as $v_{\text{max}} = 2.0$ m/s and $\xi_{\text{max}} = 0.9$ rad/s for all methods. The FOVs of the sensors are set as $[80 \times 60]$ deg with a maximum range of 4.5 m. In both scenarios each method is run for 3 times with the same initial configuration.

1) Bridge Scenario: Firstly, we compare the four methods in a $10 \times 20 \times 5$ m\(^3\) space containing a bridge, as showed in Fig.7. We show the fastest exploration progress of each method among all tests in Fig.8 and list the statistics in Tab.II, which indicates that we achieve much shorter exploration time and smaller time variance. As can be seen, the overall exploration path of our method is significantly shorter, primarily because we plan tour globally. The executed path is also smoother, since we refine motion locally and generate smooth trajectory. Finally, we are able to navigate at a higher flight speed, owing to the minimum-time trajectory planning.

2) Large Maze Scenario: We also compare the methods quantitatively in a large maze environment shown in Fig.9. The explored space is $20 \times 80 \times 3$ m\(^3\) large. The resulting statistics and exploration progress are also presented in Tab.II and Fig.8. In this scenario, all the benchmarked methods take long time to reach full coverage, due to the complexity of the scene. In contrast, our method complete the exploration 4+ times faster in average. Path executed by the four methods
Fig. 9. Path generated by the proposed method (blue), classic frontier method [4](red), rapid frontier method [1] (green) and NBVP [7](pink).

Fig. 10. Experiments in an indoor scene composed of two room: a small one with tables and chairs (top left), a large room deployed with obstacles (top right).

after completion are displayed in Fig.9.

C. Field Exploration Tests

To further validate the proposed method, we conduct extensive field experiments in both indoor and outdoor environments. In all tests we set the dynamics limits as $v_{\text{max}} = 1.5 \text{ m/s}$, $a_{\text{max}} = 0.8 \text{ m/s}$ and $\dot{\xi}_{\text{max}} = 0.9 \text{ rad/s}$. Note that we do not use any external device for localization and only rely on the onboard state estimator.

First, we present fast exploration tests in two indoor scenes. The first scene is shown in Fig.1, within which we deploy dozens of obstacles and the quadrotor should perform 3D maneuvers to map the unknown space and avoid obstacles simultaneously. We bound the space to be explored with a $10 \times 6 \times 2 \text{ m}^3$ box. One sample map and the flight trajectory is presented in Fig.1. The second indoor scene is a larger environment including two rooms, where one room is similar to scene 1 and the other is a part of an office containing tables and chairs. The space is bounded by a $15 \times 11 \times 2 \text{ m}^3$ box. The quadrotor starts by exploring the large room, after which it proceeds to the small one. The second scene, the online generated map and trajectory are shown in Fig.10. Note that in the two scenes the quadrotor starts out at a spot with low visibility, so it only maps a small region of the environment at the beginning. Finally, to validate our method in natural environments, we conduct exploration tests in a forest. The size of the area to explore is $11 \times 10 \times 2 \text{ m}^3$. The experiment environment and the associated results are displayed Fig.11.

The above experiments demonstrate the capability of our method in complex real-world scenarios. They also show the merits of our autonomous quadrotor system, among which the state estimation [33] and mapping modules [34] are also crucial to fulfill the real-world tasks. Video demonstration of all experiments is available (Fig.1), we refer the readers to it for more details.

VII. Conclusions

In this paper, we propose a hierarchical framework for rapid autonomous quadrotor exploration. An incrementally maintained FIS is introduced to provide the exploration planning with essential information. Based on FIS, a hierarchical planner plans exploration motions in three sequential steps, which finds efficient global tours, selects a local set of optimal viewpoints, and generates minimum-time local
trajectories. The method makes decisions in high frequency to respond quickly to environment changes. Both benchmark and real-world tests show the competence of our method.

As most methods do, currently our method assumes that state estimation is good enough and the side effects of pose drift can be ignored. However, error in state estimation exists generally and has great influence on the generated map. Error in state estimation can be ignored. However, error in state estimation exists generally and has great influence on the generated map especially in large-scale environments. In the future we plan to consider the state estimation uncertainty in our method and conduct autonomous exploration in larger scenes.

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