Sensing-Aided Uplink Channel Estimation for Joint Communication and Sensing

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Abstract—The joint communication and sensing (JCAS) technique has drawn great attention due to its high spectrum efficiency by using the same transmit signal for both communication and sensing. Exploiting the correlation between the uplink (UL) channel and the sensing results, we propose a sensing-aided Kalman filter (SAKF)-based channel state information (CSI) estimation method for UL JCAS, which exploits the angle-of-arrival (AoA) estimation to improve the CSI estimation accuracy. A Kalman filter (KF)-based CSI enhancement method is proposed to refine the least-square CSI estimation by exploiting the estimated AoA as the prior information. Simulation results show that the bit error rates (BER) of UL communication using the proposed SAKF-based CSI estimation method approach those using the minimum mean square error (MMSE) method, while at significantly reduced complexity.

Index Terms—Sensing-aided communication, 6G, joint communication and sensing, Kalman Filter.

I. INTRODUCTION

Joint communication and sensing (JCAS) is regarded as one of the most promising techniques for dealing with the spectrum congestion problem in the future 6G networks, achieving wireless communication and sensing using the same transmit signals [1], [2], [3]. The uplink (UL) JCAS estimates sensing parameters from the UL channel state information (CSI) [4]. Therefore, the CSI is highly related to the environment sensing information such as the angle-of-arrival (AoA), delay (or range), and Doppler frequency for the signals between the base station (BS) and the user. Moreover, the CSI estimation is critical for realizing reliable communications.

The least-square (LS) method has been widely utilized for channel estimation due to its low complexity [5]. Nevertheless, its low CSI estimation accuracy may result in a large signal-to-noise ratio (SNR) loss for communications. To deal with this problem, the minimum mean square error (MMSE) method was proposed to improve the CSI estimation accuracy. However, the high complexity makes it challenging to be utilized in real applications [6].

Moreover, using the communication signals to estimate the sensing parameters, such as Doppler frequency, delay, AoA, and angle-of-departure (AoD), has attracted great attention. In [7], the authors proposed a joint AoA and Doppler frequency estimation method and used the AoA and Doppler estimation to conduct channel tracking and compensate for the Doppler shift. In [8], the authors jointly estimated the partial angular-domain channel and Doppler frequency offset (DFO), and a DFO compensation method was proposed based on the estimates. In [9], the authors proposed to use a tensor decomposition-based method to estimate the Doppler frequency, delay, AoA, and AoD. Moreover, the authors proposed a joint AoD and Doppler shift estimation method that iteratively refines the AoA and Doppler estimation. However, this method has a high complexity.

The CSIs can be treated as sequences containing amplitude fading and phase shifts, which are related to angular, time, and frequency domain indices. Kalman filter (KF) can suppress the varying noise terms in a sequence defined as state transfer [10]. In this letter, we propose a sensing-aided Kalman filter (SAKF)-based CSI estimation method for UL JCAS. Exploiting the estimated AoAs as the prior information to construct the CSI state transfer, we use a KF to iteratively suppress the noise terms in the initial CSI estimation. The improved CSI estimate leads to the smaller bit error rate (BER). Note that UL JCAS can estimate sensing parameters including AoA, Doppler frequency, delay, etc.; nevertheless, we only choose the AoA estimate as the prior information. This is because it is hard to obtain accurate Doppler and delay estimates in the presence of the carrier frequency offset (CFO) and timing offset (TO) [4]. Comparatively, AoA changes slowly and its estimation is not impacted by CFO and TO. Simulation results show that the proposed SAKF-based CSI estimation method can achieve BER performance approaching that of the MMSE method.

Notations: Bold uppercase letters denote matrices (e.g., \( M \)); bold lowercase letters denote column vectors (e.g., \( v \)); scalars are denoted by normal font (e.g., \( \gamma \)); the entries of vectors or matrices are referred to with square brackets; \((\cdot)^*\) and \((\cdot)^T\) denote Hermitian transpose, complex conjugate and transpose, respectively; \( M_1 \in \mathbb{C}^{M \times N} \) and \( M_2 \in \mathbb{R}^{M \times N} \) are \( M \times N \) complex-value and real-value matrices, respectively; for two
given matrices $S_1$ and $S_2$, $[v_{p,q}]_{(p,q) \in S1 \times S2}$ denotes the vector stacked by values $v_{p,q}$ satisfying $p \in S_1$ and $q \in S_2$; and $v \sim CN(m, \sigma^2)$ means $v$ follows a complex Gaussian distribution with mean $m$ and variance $\sigma^2$.

II. SYSTEM MODEL

This section presents the UL JCAS system setup, and received signal model to provide fundamentals for demonstrating the SAKF-based CSI estimation method.

A. UL JCAS System Setup

We consider a UL JCAS system, where the BS and the user equipment (UE) are equipped with uniform plane arrays (UPAs), as shown in Fig. 1. UE moves at a low-to-medium speed. In the UL preamble (ULP) period, UE transmits the UL preamble signals, and BS uses the received training sequences in the preamble for CSI estimation, and the estimated CSI is further used to estimate sensing parameters. In the UL data (ULD) period, the BS demodulates the UL data signals of UE using the estimated CSI. For simplicity of presentation, we assume that there is one ULP in each packet for CSI estimation, and the ULPs are transmitted at an equal interval, denoted by $T_d^p$.

Orthogonal frequency division multiplexing (OFDM) signal is adopted as the transmit signal. The key parameters for the OFDM signal are denoted as follows. $P_t^U$ is the transmit power, $N_c$ is the number of subcarriers occupied by UE; $M_s$ is the number of OFDM packets used for each sensing parameter estimation; $d_{n,m}$ is the transmit OFDM baseband symbol of the $n$th OFDM symbol at the $m$th subcarrier $f_c$ is the carrier frequency, $\Delta f$ is the subcarrier interval, $T_s$ is the time duration of each OFDM symbol, $T_d^p = P_s T_s$, and $P_s$ is the number of OFDM symbols in each packet. The sensing parameter estimates are updated every $M_s$ packets.

B. UPA Model

This subsection presents the UPA model. The uniform interval between neighboring antenna elements is denoted by $d_a$. The size of UPA is $P \times Q$. The AoA for receiving or the angle-of-departure (AoD) for transmitting the $k$th farfield signal is $p_k = (\varphi_k, \theta_k)^T$, where $\varphi_k$ and $\theta_k$ are the azimuth and elevation angles, respectively. The phase difference between the $(p, q)$th antenna element and the reference antenna element is

$$a_{p,q}(p_k) = \exp [-j \frac{2\pi}{\lambda} d_a (p \cos \varphi_k \sin \theta_k + q \sin \varphi_k \sin \theta_k)],$$

where $\lambda = c/f_c$ is the wavelength of the carrier, and $c$ is the speed of light. The steering vector for the array is given by

$$a(p_k) = [a_{p,q}(p_k)]_{p=0,1,...,P-1; q=0,1,...,Q-1},$$

where $a(p_k) \in \mathbb{C}^{PQ \times 1}$. The sizes of the antenna arrays of the BS and the user are $P_t \times Q_t$ and $P_r \times Q_r$, respectively.

C. Received Signal Model

The frequency-domain received communication signal at the $n$th subcarrier of the $m$th OFDM symbol is expressed as [4]

$$y_{C,n,m} = \sqrt{P_t^U} d_{n,m} \sum_{l=0}^{L-1} \left[ e^{j2\pi m T_d^p [f_{C,l} + \delta_f(m)]} e^{-j2\pi n \Delta f [\tau_{C,l} + \delta_r(m)]} \times \mathbf{w}_{TX} \mathbf{a}(p_{RX,l}) \right] + \mathbf{n}_{n,m},$$

where $l = 0$ is for the channel response of the LoS path, and $l \in \{1, \ldots, L-1\}$ is for the $l$th non-LoS (NLoS) path; $\mathbf{w}_{TX} \in \mathbb{C}^{P_t \times Q_t \times 1}$ is the transmit beamforming (BF) vector, and $\mathbf{a}(p_{RX,l}) \in \mathbb{C}^{P_r Q_r \times 1}$ and $\mathbf{a}(p_{RX,l}) \in \mathbb{C}^{P_t Q_t \times 1}$ are the steering vectors for UL transmission and receiving, respectively; $\delta_f(m)$ and $\delta_r(m)$ are the carrier frequency offset (CFO) and timing offset (TO), respectively; $f_{C,l}$ and $\tau_{C,l}$ are the Doppler and delay of the $l$th path, respectively.

III. SAKF-BASED CSI ESTIMATION METHOD

In this section, we present the SAKF-based CSI estimation method. The UL JCAS scheme is shown in Fig. 2. In the ULP period, the UL CSI estimation at the $n$th subcarrier of the $m$th OFDM symbol is obtained via the LS method [5] as

$$\tilde{\mathbf{h}}_{C,n,m} = \frac{y_{C,n,m}}{d_{n,m}} = \mathbf{h}_{C,n,m} + \tilde{\mathbf{n}}_{n,m} \in \mathbb{C}^{P_t Q_t \times 1},$$

where $y_{C,n,m}$ is given in (3). $\mathbf{h}_{C,n,m}$ is the actual equivalent CSI, and $d_{n,m}$ is the preamble symbol with unit constant modulus.
A. AoA Estimation

We utilize the multiple signal classification (MUSIC) method to estimate AoAs. We stack all $M_s \times N_c$ CSI estimates (from $N_c$ subcarriers and $M_s$ packets) to obtain the matrix $\hat{H}_C \in \mathbb{C}^{P_l \times Q_l \times N_c M_s}$, where the $(m-1)N_c + n$th column of $\hat{H}_C$ is $\hat{h}_{C,n,m}$. Construct the correlation matrix of $\hat{H}_C$ as

$$\mathbf{R}_x = \left[ \mathbf{H}(\hat{H}_C)^H \right] / (M_s N_c)$$

According to the definition of $\hat{h}_{C,n,m}$, we can see that $\mathbf{R}_x$ does not contain $e^{j2\pi m T_s^p \delta_l(m)} e^{-j2\pi n \Delta f_r(m)}$. Specifically, $e^{j2\pi m T_s^p \delta_l(m)} e^{-j2\pi n \Delta f_r(m)}$ is compensated in $E[\mathbf{h}_{C,n,m}(\hat{h}_{C,n,m})^H]$ given $m$; for $E[\mathbf{h}_{C,n,m} \mathbf{n}_{C,n,m}]$, the expectations of the multiplication of noise and $e^{j2\pi m T_s^p \delta_l(m)} e^{-j2\pi n \Delta f_r(m)}$ are 0. Therefore, the AoA estimation is not prominently affected by the CFO and TO, while it is a challenging issue for estimating the range and Doppler [4]. Thus, AoA is the most suitable sensing parameter to refine the communication CSI.

Referenced to [11], applying eigenvalue decomposition to $\mathbf{R}_x$, we can obtain the eigen matrix as $\mathbf{U}_x$, and the noise subspace of $\mathbf{R}_x$ is $\mathbf{U}_N = [\mathbf{u}_x]_{L+1:L+P_l Q_l}$, where $\mathbf{U}_s = [\mathbf{u}]_{L}$ is the matrixes sliced from the $N_c$th to the $N_c$th columns of $\mathbf{U}$, and $L$ is the number of identified incident signals that can be determined by the minimum description length (MDL) method [12]. Then, the angle spectrum function can be obtained as [11]

$$f_a(p) = \mathbf{U}_N^H (\mathbf{U}_N^H)^H a(p).$$

Finally, the minimum points of $f_a(p)$ are found as the AoA estimates. Let $p_{\text{opt}}^{P,L,t}$ be $(\hat{\phi}_l, \hat{\theta}_l), l = \{0, \ldots, L-1\}$ denote the $l$th AoA estimate.

B. KF-Based CSI Enhancement Method

Reshape $\hat{H}_{C,n,m} \in \mathbb{C}^{P_l \times Q_l}$ into $\hat{H}_{C,n,m} \in \mathbb{C}^{P_l \times Q_l}$, and $\hat{H}_{C,n,m} \in \mathbb{C}^{P_l \times Q_l}$ into $\hat{H}_{C,n,m} \in \mathbb{C}^{P_l \times Q_l}$. According to (3), if we treat the incident signal in the $l$th AoA as the observing signal, then $[\hat{h}_{C,n,m}^l]_{p,q}$ can be rewritten as

$$[\hat{h}_{C,n,m}^l]_{p,q} = [\hat{h}_{C,n,m}^l]_{p,q} + [\mathbf{I}^N_{n,m}]_{p,q} + [\mathbf{n}^N_{p,q}].$$

$$= \sqrt{P_T} [\mathbf{a}_{n,m,l} e^{-j2\pi m T_s^p \delta_l(m)} + [\mathbf{I}^N_{n,m}]_{p,q} + [\mathbf{n}^N_{p,q}].$$

$$= \sqrt{P_T} \sum_{p=0}^{P_l-1} [\mathbf{a}_{n,m,l} e^{-j2\pi m T_s^p \delta_l(m)} + [\mathbf{I}^N_{n,m}]_{p,q} + [\mathbf{n}^N_{p,q}].$$

According to (7), we can treat $[\hat{h}_{C,n,m}^l]_{p,q}$ as the noisy observation of $[\hat{h}_{C,n,m}^l]_{p,q}$. Let $\hat{A}_{P,l} = e^{-j2\pi m T_s^p \delta_l(m)}$ denote the state transfer factors. Then, according to (7), the state transfer of $\hat{H}_{C,n,m}^l$ in the $p$-axis and $q$-axis are expressed, respectively, as

$$[\hat{H}_{C,n,m}^l]_{p+1,q} = [\hat{H}_{C,n,m}^l]_{p,q} \hat{A}_{P,l} + \Delta_{P,l},$$

$$[\hat{H}_{C,n,m}^l]_{p,q+1} = [\hat{H}_{C,n,m}^l]_{p,q} \hat{A}_{Q,l} + \Delta_{Q,l}.$$
After being filtered by Algorithm 1, the noise term in the CSI estimation will be suppressed. Vectorize $\hat{H}^{(2)}_{C,n,m}$ as $\hat{h}_{C,n,m}^{(2)} = vec(\hat{H}^{(2)}_{C,n,m}) \in \mathbb{C}^{P_lQ_l \times 1}$. Then, we can use $\hat{h}_{C,n,m}^{(2)}$ to demodulate UL data signals with zero-forcing (ZF) receive BF [5].

The reasons that we choose AoA as the prior information rather than Doppler or delay estimates are as follows. The CSIs containing CFO and TO phase shifts are required for communication demodulation. It is complicated to accurately estimate the Doppler-plus-CFO and Delay-plus-TO at each packet. Even if we acquire the accurate Doppler and delay estimates at each packet, the CFO and TO can introduce unexpected errors into CSI enhancement procedures in Algorithm 1. Therefore, we choose AoA estimation as the prior information for KF to enhance the CSI estimation.

C. Complexity Analysis

In this subsection, we analyze the complexity of the above SAKF-based CSI estimation. The CSI estimation of the MMSE method can be expressed as [5]

$$\hat{h}_{MMSE} = R_{hh}^{-1} \left( R_{hh} + \sigma_N^2 I \right)^{-1} \hat{h}_{C,n,m}^{(2)},$$

(16)

where $R_{hh} = E(h_{C,n,m} h_{C,n,m}^H)$. Let $N = P_lQ_l$. The complexity of the LS method comes from the complex-value division, which is $\mathcal{O}(N^2)$. The MMSE method adds the matrix inverse and multiplication operations based on the LS method. Therefore, the complexity of the MMSE method is $\mathcal{O}(N^3)$. In contrast, the SAKF method adds scalar KF iterations with only two rounds of circulations and uses the estimated AoAs of JCAS without additional processing. Thus, the complexity of the SAKF method for JCAS system is $\mathcal{O}(N + 2N) = \mathcal{O}(3N)$.

IV. SIMULATION RESULTS

In this section, we present the simulation results of the BERs using the proposed SAKF method, compared with the LS and MMSE methods. The simulation parameters are listed as follows.

The carrier frequency is set to 28 GHz [13], the antenna interval, $d_a$, is half the wavelength, the array size of the user is $P_r \times Q_r = 1 \times 1$, the number of paths is $L = 2$, $\sigma_N^2 = 0.1$, and the reflection factor for the NLoS path follows $\mathcal{CN}(0,0.1)$. The subcarrier interval is $\Delta f = 480$ kHz, the subcarrier number is $N_c = 256$, and the number of OFDM symbols for each packet is $P_s = 14$. The AoAs for the LoS and NLoS path are $\theta_{RX,0} = (16^\circ, 44^\circ)$ and $\theta_{RX,1} = (3^\circ, 32^\circ)$, respectively. The variance of the Gaussian noise is $\sigma_N^2 = 4.9177 \times 10^{-12}$ W. The transmit power is determined according to the given SNR and $\sigma_N^2$. UL SNR is defined as the SNR of each antenna element of BS. According to (3), the UL SNR is expressed as $\gamma_c = P_s^2 \sum_{l=0}^{L-1} |\hat{h}_{C,lX,1}|^2 / \sigma_N^2$.

Fig. 3 presents the AoA estimation RMSE under various array sizes, $M_s$, CFO and TO. Given the BS array size and $M_s$, the AoA estimation RMSEs under different TO and CFO are similar. This indicates that the AoA estimation is not prominently impacted by TO and CFO, as discussed in Section III-A. Moreover, when $\sigma_f = 240$ Hz, reducing either BS array size or $M_s$ leads to the increase of the AoA estimation RMSE, due to the reduced energy of processing symbols as shown in (5). The AoA estimation RMSE is considerably low even when $M_s = 2$, since the AoA estimation exploits the preamble symbols at all $N_c = 256$ subcarriers.

Fig. 4 presents the normalized MSE (NMSE) for CSI estimation when the BS array size is $8 \times 8$, $\sigma_f = 240$ Hz, under 4-QAM modulation. The NMSE is $NMSE = E\{ |\hat{h}_i - h_i|^2 \} / E\{ |h_i|^2 \}$, where $h_i$ and $\hat{h}_i$ represent the actual CSI and estimated CSI for each symbol, respectively. As the SNR increases, the NMSE decreases. It is shown that given the SNR, the NMSE of the proposed SAKF-based method is about 17 dB lower than that of the LS method, but 0.8 dB higher than that of the MMSE method.

Fig. 5 demonstrates the BERs using the SAKF, LS, and MMSE methods when the BS array size is $8 \times 8$, $\sigma_f = 5$ ns,
and $\sigma_f = 240$ Hz, under 4-QAM modulation. The required SNR to achieve the given BER for the SAKF method is about 1.8 dB lower than that for the LS method, but 0.2 dB higher than that for the MMSE method. This is because Algorithm 1 filters the CSI estimated by the LS method exploiting the estimated AoAs. This indicates that the proposed SAKF method can approach the MMSE method in BER performance with significantly reduced complexity.

Fig. 6 shows the BERs using the SAKF method when $\sigma_r = 5$ ns, and $\sigma_f = 240$ Hz, using various BS array sizes and $M_s$, under 4-QAM modulation. It can be seen that given the BS array size, the BERs under different $M_s$ are similar. This is because $M_s$ only influences the number of symbols for sensing and does not influence the processing SNR of the demodulation over each symbol, while the BS array size directly impacts the total energy of signals for both communication and sensing. Moreover, the AoA estimation RMSEs are considerably small in the studied SNR range, even when the SNR is too low for reliable communication, and the KF-based CSI enhancement can still work normally.

V. CONCLUSION

In this letter, we propose a SAKF-based UL channel estimation method for JCAS system. The KF exploits the AoAs estimated by MUSIC method as the prior information to refine the LS CSI estimation and improve the reliability of communication. Note that the proposed SAKF-based CSI estimation method can be extended to the cases with other AoA and initial CSI estimation methods. Simulation results show that the SNR required to achieve the given BER for the proposed SAKF-based method is about 1.8 dB lower than the LS method, and about 0.2 dB higher than the MMSE method, while at significantly reduced complexity.

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