I. INTRODUCTION

Usually in the construction of a new theory one invents a new classical theory and then quantizes it. For example, this was the procedure followed by Yang and Mills in the generalization of classical Maxwell electrodynamics to classical non-Abelian gauge theories. But one can think of another way: one can change the usual quantization prescriptions in order to obtain a new quantum field theory. It is possible that this may give insight into non-perturbative quantum field theory.

In Ref. [1] the hypothesis was put forward that the octonionic numbers can be generalized to octonion-like operators. Physically this means that one is dealing with a non-associative quantum theory. Mathematically it means that the corresponding algebra of operators is generated not only using the ordinary commutations relationships but also by introducing some quantum corrections connected with the rearrangement of brackets in products of operators.

One of the main problems for the physical interpretation of this hypothesized non-associative quantum theory is the probability interpretation of the theory. For the resolution of this problem we turn to quantum chromodynamics (QCD). In QCD there is the assumption that free quarks are not observable: one can observe only colorless objects like nucleons and mesons. We will apply this idea to the non-associative quantum theory: only colorless (white) quantities are observable. These white objects correspond to products of two or three non-associative operators. In order that this idea be self-consistent it is necessary that the colorless operators be combined into an associative subalgebra.

II. SHORT HISTORY OF NON-ASSOCIATIVITY IN PHYSICS

In this section we list some general textbooks and monographs on non-associativity, and give a short review of modern work into non-associative physics.

The monograph [2] surveys the role of some associative and non-associative algebras in particle physics. It concerns the interplay between division algebras – specifically quaternions and octonions. Selected applications of these algebraic structures are discussed: quaternion analyticity of Yang-Mills instantons, octonionic aspects of exceptional broken gauge, supergravity theories, division algebras in anyonic phenomena and in theories of extended objects in critical dimensions.

In the book [3], the author applies non-associative algebras to physics. The book covers topics ranging from algebras of observables in quantum mechanics, to angular momentum and octonions, to division algebra, triple-linear products and Yang - Baxter equations. The non-associative gauge theoretic reformulation of Einstein’s general relativity theory is also discussed.

A mathematical introduction to non-associative algebras and their application to physics can be found in Ref’s [4] and [5].

It has been known since the 1930s that quantum mechanics can be formulated in quaternionic as well as complex Hilbert space. The book [6] signals a major conceptual advance and gives a detailed development and exposition of quaternionic quantum mechanics for the purpose of determining whether quaternionic space is the appropriate arena for the long sought-after unification of the standard model forces with gravitation. The book also provides an
introduction to the problem of formulating quantum field theories in quaternionic Hilbert space and concludes with 
a chapter devoted to discussions on where quaternionic quantum mechanics may fit into the physics of unification.

In Ref. [7] the equations of motion arising from the Green-Schwarz Lagrangian for the superstring are solved for 
both commuting and anticommuting variables. The method of solution is to use an octonionic formalism for 
ten-dimensional vectors and spinors, and the solution is given in terms of a number of octonion parameters.

In Ref. [8] an octonion formalism is used to give a new mechanism for reducing 10 spacetime dimensions to 4 
without compactification. Applying this mechanism to the free, 10-dimensional, massless (momentum space) Dirac 
equation results in a particle spectrum consisting of exactly 3 generations.

A new matrix model is described in Ref. [4], based on the exceptional Jordan algebra. The author describes a 
compactification that reproduces, at the one loop level, an octonionic compactification of the matrix string theory in 
which SO(8) is broken to G2. Supersymmetry appears to be related to triality of the representations of Spin(8).

In Refs. [10], [11] it is shown that the three-cocycle arises when a representation of a transformation group is 
nonassociative, so that the Jacobi identity fails. The physical meaning is that when the translation group in the 
presence of a magnetic monopole is represented by gauge-invariant operators, a (trivial) three-cocycle occurs. The 
requirement that finite translations be associative leads to Dirac’s monopole quantization condition. It is interesting 
that three-cocycles can be important in the quark model with U(6)×U(6) algebra.

Probably the first attempt to apply the octonions in physics was the paper [12] describing an octonionic quantum 
mechanics. In Ref. [13] it is shown that some relation between octonions and string theory exists. In Ref. [14] an 
octonion geometry is described. In this paper a new geometrical interpretation of the products of octonionic basis 
units is presented and the eight real parameters of octonions are interpreted as the spacetime coordinates, momentum 
and energy. In Ref. [15] the non-associativity for the non-perturbative quantization of strongly interacting fields was 
introduced. A generalization of the quantum Hall effect where particles move in an eight dimensional space under 
an SO(8) gauge field is considered in Ref. [10]. The underlying mathematics of this particle liquid is that of the 
last normed division algebra, the octonions. In Ref. [16], in the framework of non-associative geometry, a unified description 
of continuum and discrete spacetime is proposed. In Ref. [17] it is shown that the non-associative extension of the 
group U(1) allows one to obtain a consistent theory of point-like magnetic monopoles having an arbitrary magnetic 
charge. Another recent application is the construction of a gauge theory on non-associative spaces [11], [22].

In Refs. [23], [24] a possible connection between quark confinement and octonions was investigated. The difference 
between the approaches presented in Ref. [23], [24] and here is that we consider octonion-like operators (not octonions) 
but in Refs. [23], [24] the quantum theory is based on the octonions not octonion-like operators. In Ref. [24] the quark 
field operators are

$$\hat{\psi}_i = \hat{q}^n_i u_n$$

where \(u_n\) are the split-octonions and \(q^n_i, q^n_j\) are the usual quark creation/annihilation operators. In the presented 
paper we introduce non-associative operators \(Q_i, q_i\) which are the non-associative generalizations of \(q^n_i, q^n_j\) operators.

### III. SOME GENERAL REMARKS ABOUT NON-ASSOCIATIVE ALGEBRA AND ASSOCIATORS/ANTIASSOCIATORS

Following the conventions of [11] we will consider non-associative operators \(q_i\) and \(Q_i\). These operators are generalizations of the split-octonion numbers \(\hat{q}_i\) and \(\hat{Q}_j\) to non-associative operators \(q_i, Q_i\). One can say that \(q_i, Q_i\) and \(\hat{q}_i, \hat{Q}_j\) are like \(q\) and \(c\)-Dirac numbers in the standard quantum mechanics (according to Dirac’s terminology \(q\)-numbers is noncommuting operators and \(c\)-numbers is ordinary commuting numbers).

We now make some remarks about the calculation of the associators/antiassociators. Let the operator \(A_1\) be some 
product of \(n\) non-associative operators \(q_i, Q_j\) and \(A_2\) be the same operator but with a different arrangement of the 
brackets. If \(\hat{q}_i, \hat{Q}_j\) are the corresponding split-octonions then \(A_1\) and \(A_2\) are the corresponding octonions after 
the replacement \(q_i \rightarrow \hat{q}_i\) and \(Q_i \rightarrow \hat{Q}_i\) and then

$$\tilde{A}_2 = \pm \tilde{A}_1.$$  \hspace{1cm} (2)

This permits us to define the corresponding quantum associator/antiassociator for the operators

$$A_2 - (\pm A_1) = \mathcal{A}.$$ \hspace{1cm} (3)

where \(\mathcal{A}\) is the associator for (+) and antiassociator for (−). We will assume that if \(A_{1,2}\) are the product of \(n\) operators 
then the quantum associator/antiassociator \(\mathcal{A}\) either is a new operator or is composed of only \(n - 1\) operators or less.
In Ref. [1] the quantum associators/antiassociators of products of three operators are introduced. In this Letter these definitions are a little changed

\[(Q_m Q_n) Q_p + Q_m (Q_n Q_p) = \epsilon_{mnp} \mathcal{H}_{3,1},\]  
\[(q_m q_n) q_p - q_m (q_n q_p) = \epsilon_{mnp} \mathcal{H}_{3,2},\]  
\[(q_m Q_n) q_p + q_m (Q_n q_p) = \epsilon_{mnp} \mathcal{H}_{3,3},\]  
\[(q_m q_n) Q_p - q_m (q_n Q_p) = \epsilon_{mnp} \mathcal{H}_{3,4},\]  
\[(Q_m q_n) q_p - Q_m (q_n q_p) = \epsilon_{mnp} \mathcal{H}_{3,5},\]  
\[(q_m Q_n) Q_p - q_m (Q_n q_p) = \epsilon_{mnp} \mathcal{H}_{3,6},\]  
\[(Q_m q_n) Q_p - Q_m (q_n Q_p) = \epsilon_{mnp} \mathcal{H}_{3,7},\]  
\[(Q_m q_n) q_p - Q_m (q_n q_p) = \epsilon_{mnp} \mathcal{H}_{3,8} \]

where \(\mathcal{H}_{3,i}\) are some operators which can be different for different \(i\): \(\rho_{1,2}, \delta_{1,2}, \gamma_{1,2}, \tau_{1,2}\) are some numbers and \(m,n = 1,2,3\). The self-consistency of the quantum associators and antiassociators [4] - [15] has been proved in Ref. [1] and [16] - [23] can be proved by similar manner that gives us

\[\rho_1 + \rho_2 = \delta_1 + \delta_2,\]  
\[\tau_1 + \tau_2 = \gamma_1 + \gamma_2.\]

The alternativity properties of the octonion-like operators \(q_i, Q_i\) remain former.

**IV. THE PRODUCT OF TWO WHITE OPERATORS**

Equations [12] - [23] indicate that if either the left or right hand sides has products like \(q_i Q_i\) then this product does not play a part in the associator/antiassociator. One can see that there is some similarity between \(q_i, Q_j\) and the annihilation and creation operators of quarks. The indices \(i = 1,2,3\) correspond to SU(3) colors = red, green, blue. Because of this we call these products \(q_i Q_j\) *colorless(white)* operators, i.e. the white operators, \(\mu_i, i = 1,2,3\) are

\[\mu_i = q_i Q_i,\]

here \(i\) is not summed over. Comparing with QCD \(q_i\) and \(Q_i(i = 1,2,3)\) are the generalizations of the annihilation and creation operators of quarks correspondingly. This comparison indicates that there are a few white operators with three factors

\[n_1 = (q_1 q_2) q_3\]  
\[n_2 = n_1^\dagger = Q_3 (Q_2 Q_1),\]

where these operators are Hermitian conjugates and any permutations of indices are possible.

The quantum associators/antiassociators in [12] - [23] are deduced in such a way that for any permutation of two factors in [12] - [23] the result would not depend on the way in which the brackets are arranged [1]. Additionally we will demand the same for the product of two colorless operators that is considered in this section.
For the calculation of the product of two white operators \((q_i Q_j)\) and \((q_j Q_i)\) we will introduce the following non-associative rules
\[
(q_i Q_j) (q_j Q_i) = (q_i Q_i) q_j + \alpha_1 (q_j Q_j) + \beta_1
\]
(29)
\[
(q_i Q_j) q_i = q_i ((q_j Q_j) Q_i) + \alpha'_1 (q_i Q_i) + \beta'_1,
\]
(30)
\[
(q_i Q_j) (q_j Q_i) = q_i (Q_i (q_j Q_j)) + \alpha_2 (q_i Q_i) + \beta_2
\]
(31)
here \(i, j\) are not summed over. Now we consider the following product
\[
(q_1 Q_1) (q_2 Q_2) = ((q_1 Q_1) q_2) Q_2 + \alpha_1 (q_2 Q_2) + \beta_1 = - (q_1 (Q_1 q_2)) Q_2 + q_2 Q_2 + \alpha_1 (q_2 Q_2) + \beta_1 =
\]
\[
(q_1 (q_2 Q_1)) Q_2 + q_2 Q_2 + \alpha_1 (q_2 Q_2) + \beta_1 = ((q_2 Q_2) Q_1) Q_2 + q_2 Q_2 + \alpha_1 (q_2 Q_2) + \beta_1 =
\]
\[
- q_2 ((q_1 Q_2) Q_1) - q_1 Q_1 + q_2 Q_2 + (q_2 Q_2) (\alpha_1 - \alpha'_1) + (\beta_1 - \beta'_1) =
\]
\[
- q_2 ((q_2 Q_2) Q_1) - q_1 Q_1 + q_2 Q_2 + (q_2 Q_2) (\alpha_1 - \alpha'_1) + (\beta_1 - \beta'_1) =
\]
\[
(q_2 Q_2) (q_1 Q_1) + (q_2 Q_2) (\alpha_1 - \alpha'_1 - \alpha_2) + (\beta_1 - \beta'_1 - \beta_2).
\]
(32)
This is the first way. Another way is
\[
(q_1 Q_1) (q_2 Q_2) = q_1 (Q_1 (q_2 Q_2)) + \alpha_2 (q_1 Q_1) + \beta_2 = - q_1 ((Q_2 Q_1) Q_2) + q_1 Q_1 + \alpha_2 (q_2 Q_2) + \beta_1 =
\]
\[
q_1 ((q_2 Q_1) Q_2) + q_1 Q_1 + \alpha_2 (q_2 Q_2) + \beta_2 = q_1 (q_2 Q_1) Q_2 + q_1 Q_1 + \alpha_2 (q_2 Q_2) + \beta_2 =
\]
\[
- q_1 ((q_2 Q_2) Q_1) + q_1 Q_1 + (q_1 Q_1) (\alpha_2 + \alpha'_1) + (\beta_2 + \beta'_1) =
\]
\[
((q_2 Q_2) Q_1) Q_1 + (q_1 Q_1) (\alpha_2 + \alpha'_1) + (\beta_2 + \beta'_1) =
\]
\[
(q_2 Q_2) Q_1 + q_1 Q_1 + (q_1 Q_1) (\alpha_2 + \alpha'_1) + (\beta_2 + \beta'_1) =
\]
\[
- (q_2 Q_2) Q_1 + q_1 Q_1 + (q_1 Q_1) (\alpha_2 + \alpha'_1) + (\beta_2 + \beta'_1) =
\]
\[
(q_2 Q_2) Q_1 + (q_1 Q_1) (\alpha_2 + \alpha'_1) + (\beta_2 + \beta'_1) =
\]
\[
(q_1 Q_1) (q_2 Q_2) + (q_1 Q_1) (\alpha_2 + \alpha'_1 - \alpha_1) + (\beta_2 + \beta'_1 - \beta_1).
\]
(33)
Comparing equations (32) and (33) we see that one should have
\[
\alpha_1 - \alpha'_1 - \alpha_2 = \alpha_2 + \alpha'_1 - \alpha_1 = 0,
\]
(34)
\[
\beta_1 - \beta'_1 - \beta_2 = \beta_2 + \beta'_1 - \beta_1 = \beta.
\]
(35)
Then we can calculate the commutator
\[
(q_1 Q_1) (q_2 Q_2) - (q_2 Q_2) (q_1 Q_1) = \beta.
\]
(36)
The pair of indices 1 and 2 can be replaced by any other.

V. INVISIBILITY PRINCIPLE

In (32) and (33) we have used an invisibility principle. This principle tells us that in a calculation with rearrangements of brackets in a product the white operator is invisible. This implies that if there is a colorless operator on the lhs or rhs then the corresponding quantum associator/antiassociator does not have any operators which were in the colorless operator.

For example, for the product of three operators we have
\[
q_m (Q_n q_n) + (q_m Q_n) q_n = q_m
\]
(37)
here the white operator is $Q_n q_m$ and the antiassociator has only $q_m$. This explains why in Eqs. (12) - (23) the quantum associators (antiassociators) have only one operator $q$ or $Q$.

For the product of four operators (29) we had

\[
(q_i Q_i)(q_j Q_j) - ((q_i Q_i) q_j) Q_j = \alpha_1 (q_j Q_j) + \beta_1
\]

(38)

also here $q_i Q_i$ is the white operator and consequently the associator can have only a term like $q_j Q_j$. According to the invisibility principle we have two white operators in equation (38), $(q_i Q_i)$ and $(q_j Q_j)$, and consequently

\[
\alpha_1 = \alpha_2 = 0.
\]

(39)

Then from equation (34) we see that

\[
\alpha_1' = 0
\]

(40)

and consequently

\[
(q_i Q_i)(q_j Q_j) = ((q_i Q_i) q_j) Q_j + \beta_1
\]

(41)

\[
(q_i (q_j Q_j)) Q_i = q_i ((q_j Q_j) Q_i) + \beta_1',
\]

(42)

\[
(q_i Q_i)(q_j Q_j) = q_i (Q_i (q_j Q_j)) + \beta_2,
\]

(43)

Let us calculate the Hermitian conjugation of equation (42)

\[
(q_i (q_j Q_j)) Q_i = q_i ((q_j Q_j) Q_i) - \beta_1'^* \tag{44}
\]

comparing this with (42) we see that

\[
\beta_1' = -\beta_1'^* \tag{45}
\]

This means that $\beta_1'$ is a pure imaginary number

\[
\beta_1' = -\beta_1'^* = i\hbar_2
\]

(46)

where $\hbar_2$ is some constant. The Hermitian conjugation of (41) gives us

\[
(q_i Q_i)(q_j Q_j) = q_i (Q_i (q_j Q_j)) + \beta_1^* \tag{47}
\]

here we have replaced $i \leftrightarrow j$. Comparing with (47) we have

\[
\beta_2 = \beta_1^*. \tag{48}
\]

For simplicity we suppose that $\beta_{1,2}$ are imaginary numbers, too

\[
\beta_2 = \beta_1^* = -\frac{i}{2}\hbar_2 \tag{49}
\]

where $\hbar_2'$ is some constant. In this case (41)-(43) are

\[
(q_i Q_i)(q_j Q_j) = ((q_i Q_i) q_j) Q_j + \frac{i}{2}\hbar_2 \tag{50}
\]

\[
(q_i (q_j Q_j)) Q_i = q_i ((q_j Q_j) Q_i) + i\hbar_2, \tag{51}
\]

\[
(q_i Q_i)(q_j Q_j) = q_i (Q_i (q_j Q_j)) - \frac{i}{2}\hbar_2, \tag{52}
\]

Finally the commutator (38) is

\[
(q_1 Q_1)(q_2 Q_2) - (q_2 Q_2)(q_1 Q_1) = 0 \tag{53}
\]

The application of this principle to the product of three white operators gives us

\[
\left[(q_i Q_i)(q_j Q_j)\right](q_k Q_k) = (q_i Q_i) \left[(q_j Q_j)(q_k Q_k)\right] \tag{54}
\]

here the repeated indices are not summed over. Equation (54) tells us that the colorless operators are associative at least at the level of the product of three white operators.
VI. OBSERVABLES IN A NON-ASSOCIATIVE QUANTUM THEORY

The next important question in a non-associative quantum theory is the probability interpretation. Generally speaking, the non-associative theory has problems here because any non-associative quantum theory may have a matrix representation but such a representation will be non-associative. We want to avoid this problem using the experience from QCD. In QCD free quarks are unobservable. Only colorless mesons and nucleons are observable. We would like to apply this lesson from QCD to non-associative quantum theory: in a non-associative quantum theory the physical observables are represented only by white operators. In this case we avoid the problems of non-associative quantum theory since the colorless operators are associative operators according to the invisibility principle.

VII. DISCUSSION AND CONCLUSIONS

In this paper we have obtained some quantum associators/antiassociators for the product of four operators where we considered white operators only. The corresponding quantum associators/antiassociators were deduced using the invisibility principle which implies that white operators are invisible for the determination of the corresponding associators/antiassociators.

To resolve the problem connected with the probability interpretation of a non-associative quantum theory we postulated that the observables in this theory are represented only by colorless (white) operators. This means that the real observables are composite objects with an inner structure which is unobservable. The unobservable degrees of freedom are similar to “hidden variables” in the corresponding “hidden variables theory” which is alternative to standard quantum mechanics. The difference is that in such theory the hidden parameters were introduced as classical degrees of freedom, but in the non-associative quantum theory the hidden parameters are quantum degrees of freedom.

Let us note two alternative views of these invisible degrees of freedom: the first is that the non-associativity is a fundamental property; the second is that the non-associativity is some approximate description of a strongly interacting quantum system (as in QCD or gravity). In the first case some aspects of Nature will always be hidden. In the second case the white object is similar to a nucleon where three quarks are confined by the SU(3) gauge field. In this case the non-associative quantum theory is similar to the four-fermion model of the weak interaction before the introduction of $SU(2) \times U(1)$ Standard Model.

Another problem is how one can define field operators from the creation/annihilation $q_i, Q_i$ operators considered here? What equations describe the dynamics of such a non-associative quantum field? In this connection we note that in Ref. 25 an octonionic version of Dirac’s equation was formulated.

The idea that the real elementary particles are composite fields which are constructed from more fundamental constituents is not new. In Ref. 26 a model is constructed where “ternons” are the fundamental constituents. In Ref. 27 a preonic, composite model of quarks and leptons is presented. The difference with the non-associative approach presented here is that in our case the constituent non-associative physical quantities are unobservable in principle. But the question as to whether non-associativity plays a role in Nature is far from being resolved since the model presented here is a simple, toy model. Our aim was only to show that it is possible to construct a quantum theory with (anti)associative relationships in addition to the ordinary (anti)commutations relationships. The real algebra of strongly interacting quantum fields may be much more complicated.

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