Composition and temperature dependence of the thermoelectric power of \( \text{Ni}_{2+x}\text{Mn}_{1-x}\text{Ga} \) alloys

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Abstract
The thermoelectric power (TEP) measurements have been carried out to investigate the changes in the electronic structure associated with the intermartensitic and martensitic transitions in \( \text{Ni}_{2+x}\text{Mn}_{1-x}\text{Ga} \) \((0 \leq x \leq 0.19)\). The samples have been characterized by ac magnetic susceptibility measurements. The correlation between the TEP and the microstructural changes sensitive to the increasing Ni content in \( \text{Ni}_{2+x}\text{Mn}_{1-x}\text{Ga} \) has been investigated. The changes in the density of states as reflected in the temperature variation of the TEP are consistent with the conclusions drawn from the Jahn–Teller mechanism of lattice distortion.

1. Introduction

\( \text{Ni}_2\text{MnGa} \) is a vastly studied ferromagnetic shape memory alloy with martensitic phase transformation taking place at \( T_M \approx 220 \text{ K} \) while the ferromagnetic order sets in at \( T_C = 370 \text{ K} \). The crystal structure at high temperature is the cubic \( \text{L}_2\text{1} \) and transforms into a modulated tetragonal state at low temperature \([1, 2]\). An important feature of the Ni–Mn–Ga alloys is the occurrence of differently modulated intermediate structures that are observed in between the initial and the final phase with the variation of temperature \([3]\). The low temperature crystal structure of the martensite is a periodic stacking sequence of the \{110\}_P planes along the \langle 1\bar{1}0\rangle_P direction of the initial cubic system. The phase transformation causes shuffling of atomic planes giving rise to modulations. These modulations are highly composition dependent and classification based on crystal periodicity like 5M (five layered), 7M (seven layered) or non-modulated (NM) tetragonal has been made \([4]\). Inelastic neutron scattering studies in the past have attributed the structural transformations to the phonon anomalies occurring in the parent phase. Here, an incomplete softening of the \{\zeta \zeta 0\} TA_2 phonon mode takes place at a particular...
wavevector $\xi_0$ (corresponding to the periodicity of the martensitic phase) with displacement along the [110] direction [5–7]. Such a phonon softening is believed to be due to contribution from electron–lattice coupling and nesting of the Fermi surface [8]. It is also known that alloys with low $T_M$ undergo a weak first order transformation to a micromodulated pre-martensitic phase at $\sim$260 K upon cooling [9]. It has been well established from earlier studies [10] that in Ni$_{2+x}$Mn$_{1-x}$Ga, increasing Ni content raises the martensitic transformation temperature and lowers the ferromagnetic transformation temperature until they coincide at $x=0.19$.

From electronic models of solids, the thermoelectric power of an alloy is known to be a function of the electron concentration, the effective mass of the electron, and the electronic scattering factor. All of these are influenced by the relative concentration of the constituent elements, lattice strain, microstructural changes, material processing and phase change. As the Ni content increases at the cost of Mn in the Ni–Mn–Ga system, there is an increase in the temperature of martensitic phase transformation. Accompanying this change is the variation in the TEP, thus making it a valued property for the phase transformation and the associated microstructural studies. Further, in metallic alloys, the value and the sign of the thermoelectric power coefficient depends on the features of the electronic bands in the vicinity of the Fermi level. Thus, TEP measurements in Ni$_{2+x}$Mn$_{1-x}$Ga should be very interesting, as they would reflect the changes in the band structure occurring due to structural transformation when $x$ is varied. With this aim, we present the TEP measurements in Ni$_{2+x}$Mn$_{1-x}$Ga with $0 \leq x \leq 0.19$ and its correlation with the microstructural changes that accompany the structural transformation.

### Table 1. Elemental distribution in Ni$_{2+x}$Mn$_{1-x}$Ga series as determined from EDX analysis, the average number of valence electrons per atom and the $T_M$ and $T_C$ obtained from ac susceptibility measurements.

| $x$ | $e/a$ | Ni  | Mn  | Ga  | $T_M$ (K) | $T_C$ (K) |
|-----|-------|-----|-----|-----|----------|----------|
| 0   | 7.5   | 50.8| 24.6| 24.6| 210      | 370      |
| 0.05| 7.54  | 51.0| 24.7| 24.3| 250      | 357      |
| 0.1 | 7.58  | 52.8| 22.5| 24.7| 280      | 342      |
| 0.13| 7.6   | 53.9| 21.5| 24.6| 300      | 342      |
| 0.16| 7.62  | 54.4| 21.2| 24.4| 315      | 337      |
| 0.19| 7.64  | 54.6| 20.8| 24.6| 334      | 334      |

2. Experimental details

Polycrystalline ingots of Ni$_{2+x}$Mn$_{1-x}$Ga with $x = 0, 0.05, 0.10, 0.13, 0.16$ and $0.19$ were prepared by arc-melting the constituent elements of 4 N purity under argon atmosphere. To attain a good compositional homogeneity the ingots were remelted four or five times with a weight loss of approximately $\leq 0.5\%$ and subsequently annealed at the temperature of 1000 K for 2–3 days in an evacuated quartz ampoule followed by quenching in cold water. The energy dispersive x-ray (EDX) analysis was carried out on all the ingots in order to determine the precise composition. As can be seen from the data in table 1, the ratios of the constituent elements are found to be nearly equal to that of the nominal compositions.

The low field magnetic ac susceptibility was also measured in the temperature range 77–350 K. Thermoelectric power measurements were carried out in the temperature range 100–350 K in the warming cycle using the differential method, where the voltage difference $\Delta V$ developed across the sample due to the temperature difference $\Delta T$ is measured. The sample was kept between two highly polished copper plates, electrically insulated from the rest of
the sample holder. Two heaters attached to these copper plates served to raise the overall temperature of the sample and to maintain a temperature gradient across the length of the sample. A copper–constantan thermocouple operating in the differential mode was employed to monitor the temperature gradient, and the overall temperature of the sample was measured by a platinum resistance thermometer (Pt-100). By passing current through the heaters a heat pulse is generated, resulting in a thermo-emf $V_s$ across the sample. This voltage $V_s$ and that developed across the thermocouple $V_{th}$ are measured for different temperature gradients. The thermopower of the sample is obtained by multiplying the thermopower of the thermocouple, $S_{th}$, by the slope of the straight line obtained from the plot of $V_s$ versus $V_{th}$. The microstructure of Ni$_{2+x}$Mn$_{1-x}$Ga should reflect the variation of the crystal structure as the system evolves from L2$_1$ to 5M, 7M or NM structure. Figure 1 shows the surface morphology of $x = 0, 0.1$ and 0.13 samples, which clearly reflect these microstructural changes. The martensitic transformation temperature for $x = 0$ being at 210 K, the micrograph reflects the morphology of the austenitic phase. Surface morphologies seen for $x = 0.1$ and 0.13 are typical of a modulated structure.

3. Results

3.1. Ac susceptibility

Magnetic properties for the series were studied by carrying out the low field ac magnetic susceptibility ($\chi$) measurements as a function of temperature in the warm-up cycle, and the plots are shown in figure 2. The abrupt step-like features in $\chi$ are observed at phase transformation temperatures in all the samples. The onset of ferromagnetic transition is marked by a sharp rise in $\chi$ at $T_C$ followed by a sharp fall at the martensitic transformation temperature $T_M$. As the Ni content increases across the series, the two transitions approach each other until they merge for Ni$_{2.19}$Mn$_{0.81}$Ga at a temperature $\sim 330$ K. These observations are in agreement with those reported in [10, 11]. In addition to the features characteristic of the ferromagnetic and martensitic transformation, another feature is observed in $x = 0.10$ at around $T = 250$ K. This feature occurs when the sample is in the martensitic phase ($T_M = 285$ K), hence can be interpreted to be due to intermartensitic transition from one crystallographically modulated structure to the other [12]. The $T_C$ and $T_M$ for all samples as observed from the present susceptibility measurements are presented in table 1.

3.2. Thermopower (TEP)

Phase transformation involves a change in the free energy, and TEP, being sensitive to such changes, is expected to show signatures of the martensitic as well as magnetic transition. The thermoelectric power of the Ni$_{2+x}$Mn$_{1-x}$Ga series was measured in the range 100–350 K during warm-up and the data for all the samples are presented in figures 3 and 4. It has been shown in the past that the TEPs for shape memory alloys show signatures corresponding to martensitic transition [13–15]. Indeed, as the sample is warmed a dip in TEP is obtained and can be associated with the strong phonon softening that is known to occur near the martensitic transition. On further warming a change in slope of TEP is seen due to magnetic scattering of the charge carriers as $T_C$ is approached. Thereafter, TEP attains almost a constant value that changes only slightly with temperature. This behaviour can be more clearly seen in $x \geq 0.13$. With prior knowledge of $T_M$ and $T_C$ for all the samples obtained from the magnetic susceptibility measurements, the anomalies seen in TEP data could be identified. As seen from figure 3, for $x = 0$ the first dip at $\sim 210$ K is associated with its martensitic transformation. There is an additional anomaly occurring at $\sim 260$ K marked as $T_P$ in the figure. This feature
Figure 1. Optical microscopy images implicating different surface morphologies exhibited by (a) $x = 0$, (b) $x = 0.1$ and (c) $x = 0.13$.

This figure is in colour only in the electronic version.

is less intense than that occurring at $T_M$. A pre-martensitic transition is known to occur in Ni$_2$MnGa and its substitutional derivates that have a martensitic transformation temperature below 260 K [9]. Hence, the anomaly marked as $T_P$ in figure 3 is attributed to such a pre-martensitic transition. For $x = 0.05$, a broad spike-like feature is obtained in TEP instead of a narrow dip, as the difference in $T_M$ (=250 K) and $T_P$ (=260 K) is about 10 K and the signatures due to these two anomalies are not well resolved in the TEP data. Two dips are also seen in $x = 0.1$ (refer to figure 3). However, martensitic transformation occurs at 280 K in this
Thermoelectric power of Ni$_{2-x}$Mn$_{1-x}$Ga

Figure 2. Ac susceptibility as a function of temperature for Ni$_{2-x}$Mn$_{1-x}$Ga. The martensitic and ferromagnetic phase changes are marked by sudden step-like features at the respective $T_M$ and $T_C$ for all the alloys. A small jump in the $x = 0.1$ at 250 K indicates the intermartensitic transformation.

Figure 3. Thermopower as a function of temperature for Ni$_{2-x}$Mn$_{1-x}$Ga with $x = 0, 0.05, 0.1$. The line connecting the points is a guide to the eye. The features marked as $T_P$ and $T_M$ indicate the pre-martensitic and intermartensitic transitions respectively.

Hence the smaller dip at 250 K is an additional feature occurring in the martensitic regime. It may be noted that the susceptibility measurements for $x = 0.1$ also showed a signature at 250 K. Thus this anomaly can be related to intermartensitic transition. The TEP data for $x = 0.13$ and 0.16 are presented in figure 4 and show huge dips in TEP at $T_M$ followed by a steep rise indicative of magnetic scattering (shown by curved arrows in figure 4). The huge dips in these samples are expected due to stronger phonon softening than in the samples.
Figure 4. Thermopower as a function of temperature for Ni$_{2+x}$Mn$_{1-x}$Ga with (a) $x = 0.13$, (b) $x = 0.16$ and (c) $x = 0.19$. The line connecting the points is a guide to the eye. Arrows indicate the steep rise in TEP due to magnetic scattering.

with lower martensitic transition temperature [7]. For $x = 0.19$, martensitic and ferromagnetic transformations are known to occur at the same temperature. The TEP data for this sample indeed reflect this scenario, as can be seen from figure 4(c).

In addition to the above, another important feature is observed in TEP with the increasing Ni content. Figure 5 presents the derivative of TEP as a function of normalized temperature ($T/T_M$) for three representative samples. In the range $0.86 \leq T/T_M \leq 1.02$ there lies an inflection point that shifts from 0.88 to 0.98 in going from Ni$_2$MnGa to Ni$_{2.19}$Mn$_{0.81}$Ga.

4. Discussion

The martensitic transformation temperatures obtained from the ac susceptibility measurements agree with the literature values and confirm that the Ni$_{2+x}$Mn$_{1-x}$Ga with $0 \leq x \leq 0.19$ compositions are close to nominal. In addition, we observe an intermartensitic transition in the $x = 0.1$ sample at around $T = 250$ K in the susceptibility data. These observations are further supported by the anomalies seen at the similar temperatures in the TEP measurements.

Thermoelectric power data bring out many interesting features of the Ni$_{2+x}$Mn$_{1-x}$Ga series. Firstly, with increasing Ni replacing Mn atoms, the electron concentration increases, and this is best reflected in the austenitic phase of all samples. In this region, a systematic increase in the magnitude of TEP is seen with increasing Ni content. This can be attributed to the electronic filling in the conduction band that takes place due to the electron transfer
from the nearly full 3d band of Ni to the more than half filled 3d band of Mn. Further, TEP shows variations with changing concentration in the martensitic phase as well. For a typical ferromagnetic Heusler alloy, TEP goes through a minimum at \( \sim 0.4T_C \) at low temperature [16]. A minimum in TEP with a smooth parabolic type of variation is clearly seen for \( x = 0 \), 0.05 samples in the low temperature region, while for \( x = 0.1 \) onwards TEP does go through a minimum but thereafter does not show a typical \( T^2 \) type of dependence. A reduced \(|S|\) in samples with \( x \geq 0.1 \) implies that the conduction electrons are getting scattered strongly after entering the martensitic phase. Such a change occurs probably as a result of different nesting vectors formed due to differently modulated crystal structures in the martensitic phase. Thus the conduction electrons get condensed differently in these changing nesting vectors.

Another feature in TEP across the changing \( x \) is the overall behaviour of TEP for \( x = 0.19 \). As seen from figures 3 and 4 the overall magnitude of TEP in the entire temperature range increases systematically on going from \( x = 0 \) to 0.16, while \( x = 0.19 \) has a lower value of TEP. This behaviour of 0.19 to stand out in relation to others in the sequence is perhaps the consequence of its crystal structure. As stated earlier, the crystal structure of the martensitic phase of the Ni–Mn–Ga alloys depends on composition and temperature. Studies by Lanska et al [17] bring out a correlation between the tetragonality \((c/a)\) of the martensitic structure, \( T_M \) and average number of valence electrons per atom \((e/a)\). It is shown that in the \( e/a \) range of 7.61–7.72, different crystal structures, namely 5M, 7M or non-modulated, can be obtained upon undergoing martensitic transformation. In particular, 5M or 7M transformations occur in samples with \( T_M \) below \( T_C \). In the present study, the \( e/a \) values for samples range from 7.5 to 7.64 (refer to table 1) with \( x \geq 0.13 \) lying in the range 7.6–7.64. Also, the martensitic transition occurs in the ferromagnetic state except for \( x = 0.19 \). Thus in the martensitic region, the crystal structure for \( x = 0.13, 0.16 \) is modulated and for \( x = 0.19 \) it could be non-modulated [4, 17]. Also, as per the band model, there is a change in the width of the energy bands due to deformation of crystal structure and the degree of overlap of the associated orbitals changes. The fact that \( x = 0.19 \) has a non-modulated structure while \( x = 0.13, 0.16 \)
does contain modulation leads to deviation in the overall behaviour of TEP in Ni$_{12.10}$Mn$_{0.81}$Ga from the rest of the series.

Using the simple semi-classical result for thermal diffusion in metals, the total TEP for a ferromagnetic system can be expressed as

$$S = S_m + S_s$$

where $S_m$ is the magnetic contribution and

$$S_s = -\frac{1}{e\sigma T} \int (\epsilon - \mu) \frac{\partial f_0}{\partial \epsilon} \sigma(\epsilon) \, d\epsilon$$

where $f_0$ is the Fermi–Dirac distribution function, $\mu$ is the chemical potential and

$$\sigma = \int \sigma(\epsilon) \frac{\partial f_0}{\partial \epsilon} \, d\epsilon.$$  

It can be clearly seen that TEP is dependent on the density of states (DOS) near the Fermi level. The above result has been used to explain the TEP of shape memory alloy, NiTi assuming a DOS with a peak near the Fermi level [13].

The alloys in the present study are in the ferromagnetic state and hence the magnetic scattering can be assumed to be similar for all the samples. Thus change in TEP with respect to the concentration of alloys can be related only to changes in DOS at the Fermi level. Further, the band structure of Ni$_3$MnGa has been calculated and the compositions of bands that are active at the Fermi surface have been identified [18, 19]. According to these calculations there is a peak in the DOS just below the Fermi level comprising the minority spin Ni $e_g$ band. A peak is indeed seen in the temperature derivative of TEP near the martensitic transition temperature. This is presented in figure 5, where the temperature derivative of TEP with respect to normalized temperature ($T/T_M$) is plotted for three representative samples. Moreover, this peak shifts from 0.88 to 0.98 in going from Ni$_3$MnGa to Ni$_{12.10}$Mn$_{0.81}$Ga. Such a shift is an indication of changes occurring in the DOS within the martensitic phase. Upon martensitic transformation, a structural change from cubic to orthorhombic leads to lifting of degeneracy of the 3d levels. It is the splitting of energy sub-bands which are degenerate in the cubic phase that enables the electrons to redistribute themselves in order to lower the free energy. This is the well known band Jahn–Teller mechanism and has been observed in Ni$_3$MnGa using polarized neutron scattering [20]. For a martensitic transition to occur it is required that the peak in the DOS should have some asymmetry, whereby it has more weighting towards lower energies, and that the Fermi level is situated very close to the peak. From the present TEP data, the shift of the inflection point from 0.88 to 0.98 with increasing Ni content can be attributed to the movement of the Ni $e_g$ band towards the Fermi level, thereby leading to an increase in $T_M$.

5. Conclusion

Thermoelectric power measurements on the Ni$_{12+x}$Mn$_{1-x}$Ga with $0 \leq x \leq 0.19$ exhibit the signatures not only for the martensitic transitions but also the premartensitic and intermartensitic transitions in some of the compositions. Thermopower reflects the changes in the density of states consistent with the changes in the electronic structure due to the band Jahn–Teller effect. The increase in martensitic transformation temperatures with increasing Ni content can be related to the shifting of a peak in DOS at the Fermi level closer to $E_F$. The change in behaviour of TEP from that expected for a typical Heusler alloy, in the martensitic region, can be related to the differently modulated crystal structures formed upon martensitic transformation.
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