Latent Linear Adjustment Autoencoders v1.0: A novel method for estimating and emulating dynamic precipitation at high resolution

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Abstract. A key challenge in climate science is to quantify the forced response in impact-relevant variables such as precipitation against the background of internal variability, both in models and observations. Dynamical adjustment techniques aim to remove unforced variability from a target variable by identifying patterns associated with circulation, thus effectively acting as a filter for dynamically-induced variability. The forced contributions are interpreted as the variation that is unexplained by circulation. However, dynamical adjustment of precipitation at local scales remains challenging because of large natural variability and the complex, nonlinear relationship between precipitation and circulation particularly in heterogeneous terrain. Building on variational autoencoders, we introduce a novel statistical model—the Latent Linear Adjustment Autoencoder (LLAAE)—that enables estimation of the contribution of a coarse-scale atmospheric circulation proxy to daily precipitation at high-resolution and in a spatially coherent manner. To predict circulation-induced precipitation, the Latent Linear Adjustment Autoencoder combines a linear component, which models the relationship between circulation and the latent space of an autoencoder, with the autoencoder’s nonlinear decoder. The combination is achieved by imposing an additional penalty in the cost function that encourages linearity between the circulation field and the autoencoder’s latent space, hence leveraging robustness advantages of linear models as well as the flexibility of deep neural networks. We show that our model predicts realistic daily winter precipitation fields at high resolution based on a 50-member ensemble of the Canadian Regional Climate Model at 12-km resolution over Europe, capturing for instance key orographic features and geographical gradients. Using the Latent Linear Adjustment Autoencoder to remove the dynamic component of precipitation variability, forced thermodynamic components are expected to remain in the residual, which enables the uncovering of forced precipitation patterns of change from just a few ensemble members. We extend this to quantify the forced pattern of change conditional on specific circulation regimes. In addition, we briefly illustrate one of multiple possible further applications of the method: a weather generator that emulates climate model simulations of regional precipitation at high resolution by bootstrapping circulation patterns. Other potential applications include addressing detection & attribution at sub-continental scales, or statistical downscaling and transfer learning between models and observations to exploit the typically much larger sample size in models compared to observations.
1 Introduction

Precipitation is a key climate variable that is highly relevant for impacts such as floods or meteorological drought. Precipitation simulations at high-resolution (e.g., Prein et al., 2017) are required for adaptation planning for local and regional precipitation change in a warming climate. However, precipitation shows large natural variability (Deser et al., 2012), and its relationship with atmospheric circulation is complex and non-linear, in particular at local to regional scales and in heterogeneous terrain (e.g., Zorita et al., 1995). Moreover, projected changes in precipitation are unevenly distributed across the distribution of precipitation intensity (Allen and Ingram, 2002; Held and Soden, 2006; Pendergrass, 2018). Scaling rates depend on the return period, region, temperature and moisture availability (Prein et al., 2017), and changes in circulation during precipitation events (Shepherd, 2014; Fereday et al., 2018). Hence, it is a key challenge to identify, understand and interpret patterns of forced precipitation change in model simulations and observations.

Dynamical adjustment techniques have been developed to separate forced and internal variability via a co-interpretation of target variables such as temperature or precipitation using circulation information: A circulation proxy (such as a sea level pressure pattern) is used to estimate the circulation-induced (dynamic) contribution to temperature or precipitation variability. For example, dynamical adjustment of precipitation has revealed that the spatial pattern and amplitude of observed residual (predominant thermodynamic) precipitation trends at the scale of the entire Northern hemisphere mid- and high-latitude land area are in good agreement with the expected anthropogenically-forced trends from model simulations (Guo et al., 2019).

Similarly, in Europe, Fereday et al. (2018) showed that thermodynamic forced changes in future winter precipitation are in relatively good agreement among models, while large uncertainties remain in simulated forced circulation changes that may affect precipitation. While internal and forced components of precipitation variability and change can be decomposed in large ensembles of model simulations (Deser et al., 2012; von Trentini et al., 2019; Leduc et al., 2019), high resolution large ensembles are prohibitively expensive. It would be beneficial to be able to estimate and identify forced precipitation patterns from only a few ensemble members at impact-relevant regional spatial scales.

Techniques for dynamical adjustment have relied largely on linear regression (Wallace et al., 1995, 2012; Smoliak et al., 2015; Sippel et al., 2019) or circulation analogue techniques (Yiou et al., 2007; Deser et al., 2016). Because the fraction of variability that can be explained by these techniques is limited, dynamical adjustment has so far been applied on large spatial and temporal scales (e.g., Guo et al., 2019), and has also been more successful for temperature trends than for precipitation. Applying it to precipitation on local or regional scales at high-resolution remains a challenge.

Beyond techniques of dynamical adjustment, large-scale simulated patterns of climate variables have been used to emulate climate model simulations in order to generate larger samples of realizations of the climate system (combining dynamical internal variability and the forced response) for purposes like impact modeling (Link et al., 2019; Beusch et al., 2020; Alexeeff et al., 2018). While these approaches have been used successfully for emulating large-scale temperatures, emulating precipitation at local or regional scales at high temporal frequency remains challenging due to nonlinearity and the complexity of processes involved (Link et al., 2019; Beusch et al., 2020).
In this work, we leverage recent advances in machine learning to propose a novel statistical model—the Latent Linear Adjustment Autoencoder (LLAAE)—suitable for dynamical adjustment and emulating dynamically induced variability (and potentially further applications) in daily, high-resolution precipitation fields. In recent years, deep learning techniques have gained in popularity in machine learning due to large improvements in neural network architectures, optimization algorithms as well as computing power and frameworks. Among the class of deep generative models, the introduction of variational autoencoders (VAEs) (Kingma and Welling, 2014; Rezende et al., 2014) started a whole subfield in deep learning research. Among other things, the popularity of VAEs is due to their ability to generate realistic new images, in addition to being a powerful nonlinear dimensionality reduction technique. Our proposed Latent Linear Adjustment Autoencoder extends the standard VAE model appropriately to enable the climate applications of interest.

Specifically, during training the Latent Linear Adjustment Autoencoder encodes daily precipitation fields into a low-dimensional latent space and subsequently decodes them for reconstruction. In addition, we formulate the objective function such that the latent space can be regressed linearly on the circulation proxy. For dynamical adjustment, we use the estimate of the latent space based on circulation, which is then decoded for predicting daily precipitation fields at high spatial resolution. In other words, the final model is nonlinear, consisting of a linear part and a nonlinear part, where the latter is a deep neural network. It enables prediction of the portion of the precipitation field that can be explained by circulation (i.e., the dynamic component of precipitation). Beyond the dynamical adjustment application, the model can also be used to emulate dynamically induced variability in daily precipitation fields by bootstrapping the circulation patterns. Moreover, several further climate science applications of the Latent Linear Adjustment Autoencoder are conceivable, such as for example weather generators emulating regional climate model simulations, detection & attribution at sub-continental scales, or statistical downscaling, and are discussed further below.

In summary, the objectives of this paper are the following:

1. Introduce a novel statistical model—the Latent Linear Adjustment Autoencoder—as a versatile technique for applications in climate science, particularly for making better use of high-resolution climate simulations by estimating circulation-induced (dynamic) precipitation at high resolution from coarse-scale circulation information.

2. Illustrate the Latent Linear Adjustment Autoencoder by applying it to dynamical adjustment of daily high-resolution precipitation from simulations over Central Europe.

3. Illustrate that our technique can be extended to emulate the dynamic component of daily precipitation fields, akin to weather generators. More specifically, the LLAAE will be used to separate forced precipitation trends from internal variability.

2 Dynamical adjustment using statistical learning

Following Smoliak et al. (2015) and Sippel et al. (2019), we frame dynamical adjustment as a statistical learning problem. Let $Y \in \mathbb{R}^{h \times w}$ be the climate variable of interest on a spatial field of size $h \times w$ and let $X \in \mathbb{R}^p$ be input features. In the following,
we consider daily precipitation fields for $Y$ and empirical orthogonal function (EOF) time series of sea-level pressure (SLP) for $X$ as a proxy for circulation. The EOF time series are detrended (as described below) and scaled to unit-variance; in the EOF computation, we do not weight by area. A variety of climate variables instead of precipitation could be taken as $Y$; results for daily temperature can be found in Appendix C.

Let $X$ be the $n \times p$ matrix where each column contains one input feature with $n$ “observations”. Each “observation” data point is in our case a simulation from a Regional Climate Model (RCM), and each column corresponds to one of $p$ EOF components of SLP, from the RCM but at coarsened resolution. Let $Y$ be the $n \times h \times w$ tensor that represents the precipitation intensity for each “observation” data point in a spatial field. Below, we present our proposed statistical model, which estimates the circulation-induced component of precipitation $\hat{Y}_X$, $Y = f(X)$, (1)

where $f$ is a generic non-linear function. Let $\hat{R}$ denote the residuals $\hat{R} = Y - \hat{Y}_X$ that remain. Since $\hat{Y}_X$ is the precipitation explained primarily by variations in circulation, $\hat{R}$ is the precipitation primarily unexplained by circulation. If SLP is unaffected by external forcing, then this residual contains the signal induced by the thermodynamic component of the external forcing, since the variability due to circulation has been removed. If instead external forcing does affect SLP, then the dependence between $X$ and $Y$ that arises due to the common influence of the external forcing would bias the estimation of $f$. To avoid potential forced trends in SLP projecting onto the thermodynamic component of the external forcing in $Y$, we detrend the daily SLP EOF time series as follows. We ensure that they are orthogonal to the smoothed, first EOF of the January ensemble mean by regressing the time series against the ensemble mean, and using the corresponding residuals as input features $X$. The reasoning behind this step is that a forced trend in SLP will be approximately captured in the first EOF of the SLP ensemble mean. Here, we use the January ensemble mean as a proxy for December-February SLP. For simplicity, we refer to the detrended and scaled SLP EOF time series simply as the “SLP time series” in the following.

2.1 Latent Linear Adjustment Autoencoders: Proposed deep autoencoder model for dynamical adjustment

We build on variational autoencoders (VAEs; Kingma and Welling, 2014; Rezende et al., 2014), which can be understood as a (typically nonlinear) dimensionality reduction method. An autoencoder consists of an “encoder” $e$ that maps $Y$ to the low-dimensional latent space $L \in \mathbb{R}^l$, $L = e(Y)$, and a “decoder” $d$ which in turn maps $L$ to the reconstruction of $Y$, $\hat{Y} = d(L) = d(e(Y))$. This scheme is illustrated in Fig. 1, which depicts the reconstruction of precipitation fields. The VAE objective encourages the distribution of the latent space variables $L$ to be close to a chosen prior distribution, typically a standard multivariate Gaussian distribution, and also ensures that $\hat{Y} \approx Y$. The encoder and the decoder are parameterized as (deep) neural networks.

We extend the standard VAE model to make it suitable for dynamical adjustment by adding a linear component $h$ to the architecture. The linear component $h$ takes $X$ as input features and predicts the latent space variables $L$ of the VAE; thus we call the overall model the “Latent Linear Adjustment Autoencoder”. Using an appropriate training objective (see Eq. (3)), we enforce that when linearly predicting the latent space variables $L$ with $X$, $\hat{L} = h(X)$, the resulting decoded prediction...
\( \hat{Y}_X = d(\hat{L}) = d(h(X)) \) to be close to \( Y \). The motivation behind this loss function is that the combined model, which consists of the combination of \( h \) and \( d \), should explain as much variance in \( Y \) as possible, while using only the input \( X \). In other words, it should capture the circulation-induced signal in \( Y \). The advantage of combining the linear model \( h \) with the nonlinear decoder of the VAE \( d \) is that the overall model is very expressive while the estimation of \( h \) remains relatively simple.

In more detail, we consider the following objective to train the encoder \( e \) and decoder \( d \) with associated parameters \( \theta = (\theta_e, \theta_d) \) of our proposed Latent Linear Adjustment Autoencoder:

\[
\mathcal{L}_\theta = \mathcal{L}_{\text{VAE}} + \lambda \mathcal{L}_L.
\]

\( \mathcal{L}_{\text{VAE}} \) is the standard VAE objective for real-valued input data, consisting of a reconstruction loss and the Kullback–Leibler divergence between the distribution of the encoded inputs and the prior distribution of the latent space, here chosen to be a standard multivariate Gaussian distribution (for details see Kingma and Welling, 2014; Rezende et al., 2014). \( \mathcal{L}_L \) is the extension to the objective that we propose,

\[
\mathcal{L}_L = \|Y - \hat{Y}_X\|_2^2 = \|Y - d(h(X))\|_2^2,
\]

and \( \lambda \) is a tuning parameter that steers the relative importance of the two loss functions in the overall objective (Eq. (2)). The autoencoder and the linear model are trained iteratively in an alternating fashion. In the first step, the objective \( \mathcal{L}_\theta \) is optimized while \( h \) is treated as fixed. In a second step, the linear component \( h \) of the Latent Linear Adjustment Autoencoder is trained with squared error loss, treating the encoder and decoder parameters as fixed,

\[
\mathcal{L}_{\theta_h} = \|L - \hat{L}\|_2^2 = \|e(Y) - h(X)\|_2^2.
\]

The parameters of the encoder and decoder \( (\theta_e, \theta_d) \) and those of the linear model \( h, \theta_h \), are coupled, since the linear model aims to predict the latent space variables \( L \), which are subject to change during the training of the encoder and the decoder. At the same time, the autoencoder should be trained such that a linear regression from \( L \) on \( X \) achieves a small error in Eq. (3), which is accomplished with this procedure for training the components. In practice, we train the model using the Adam optimizer (Kingma and Ba, 2015). All details related to training the model, such as architecture and hyperparameter choices, as well as code to reproduce our experimental results, can be found in Appendix A.

After training the components \( e, d \) and \( h \), we no longer need the encoder to perform dynamical adjustment on unseen test data. This is illustrated in Fig. 2. We predict the latent space variables with the linear model \( h \), using the SLP time series as input \( X \). The resulting predictions are fed to the decoder, which outputs predictions of the spatial field based only on \( X \). In other words, we obtain the spatial field of precipitation which can be explained by circulation.

The spatial field is modelled jointly in our approach—the optimization is performed over the whole spatial field at once—in contrast to Sippel et al. (2019), where a separate model needed to be trained for each grid cell. The joint modeling of the daily high-resolution precipitation field as a function of coarse-scale circulation also enables several additional climate applications which are briefly discussed in Sect. 4.
3 Data and evaluation

3.1 Data

To evaluate our statistical model, we use the Canadian Regional Climate Model Large Ensemble (CRCM5-LE, (Leduc et al., 2019)) that is based on a dynamically downscaled version of the 50-member CanESM2 large ensemble (CanESM2-LE). CanESM2-LE is an initial-condition ensemble of climate change projections (Kirchmeier-Young et al., 2017) run with the Canadian Earth System Model (Arora et al., 2011), globally on a spatial resolution of 2.8°. CanESM2-LE combines so-called macro and micro initializations: to achieve different 1950 ocean states (the macro initialization), five historical spinup runs are branched from a long pre-industrial (1850) control run, to which small random atmospheric perturbations and then time-varying forcings are applied until 1950. Then, for the micro ensemble (where members have the same initial conditions in the ocean but differ in their atmosphere), a second set of random perturbations is applied in 1950 to generate 10 runs spanning 1950-2006 for each of the 5 historical spinups, with time-varying historical forcing scenario applied through 2006. The runs continue from 2006 until 2100 with RCP8.5 forcing (Kirchmeier-Young et al., 2017). This approach yields 50 approximately independent realizations of the climate system (Leduc et al., 2019). Each of the global simulations has been downscaled using the Canadian Regional Climate model version 5 (Martynov et al., 2013) to a resolution of approximately 0.11° (≈ 12 km) over Europe for the 1950-2099 period, which yields the regional large ensemble CRCM5-LE. More details about the modeling setup and evaluation of the simulations are available in Leduc et al. (2019).

3.2 Experimental setup

3.2.1 Target variables

We focus on precipitation as the target climate variable throughout the main text. A subset of results for temperature can also be found in Appendix C. For the precipitation fields we apply a square-root transformation to stabilize the autoencoder training; the results presented in Sect. 4 are based on transforming the results back to the original scale (mm·d⁻¹), except for some visualizations where indicated in the captions. The spatial fields we consider have 128x128 grid cells, i.e. they are a subset of the original 280x280 field, cropped around Central Europe (with boundaries 0-18.9°E and 42-54.8°N). We aggregate the data (which are hourly) to daily averages.

3.2.2 Input features

SLP is regridded to a spatial resolution of 1x1° before computing the EOFs as described in Sect. 2, so that the model predicts high-resolution precipitation from only a coarse-resolution proxy of atmospheric circulation. We aggregate the data (3-h) to daily averages. SLP data is also taken from the original 280x280, 0.12° resolution Euro-Cordex domain (WCRP, 2015) and regridded to a regular 1x1° grid that broadly covers the region of -15 to 35°E and 35-64°N (see Fig. 9 (top)).
3.2.3 Time periods and training/test splits

We use RCM simulation data from 1955 to 2100 to allow for 5 years of spinup. We train our model using daily data from December-February from 9 ensemble members (“kba”, “kbc”, “kbe”, “kbg”, “kbi”, “kbk”, “kbm”, “kbs”). The training data results in the main text are based on training data that comprises the years 1955-2070, the years 2071-2100 are used for testing. In Appendix B, we present results based on the shorter training time period from 1955-2020, using the same ensemble members. This corresponds to a reduction in the amount of training data points of approximately 43% and serves as a sensitivity test to the amount of training data. Furthermore, we evaluate our trained models on six the remaining 41 ensemble members that were entirely left out of training (“kbb”, “ket”, “keu”, “kev”, “kew”, “kex”). We refer to these as “holdout ensemble members”.

3.2.4 Evaluation of predictions

To illustrate the spatial coherence of our approach, we show 5 example target (daily) observations data points of $Y$, their reconstructions $\hat{Y}$, and the predictions $\hat{Y}_X$ from the holdout ensemble member “kbb” (Fig. 3). These examples are chosen for different percentiles of the distribution of the $R^2$ values (i.e., proportion of explained variance). As such they show the range between data points where the LLAAE performs relatively poorly to cases where the LLAAE performs well (in terms of $R^2$). To highlight the precipitation features, these examples are displayed after the data has been square-root-transformed. We compute the gridcell-wise mean squared error (MSE) of predictions $\hat{Y}_X$ and the proportion of explained variance ($R^2$) based on the daily data from the holdout ensemble member “kbb”. The results for the other holdout ensemble members are very similar. We further evaluate the predictions within a dynamical adjustment framework described in the next paragraph.

3.2.5 Dynamical adjustment

We evaluate the extent to which the forced response of precipitation can be uncovered with a small number of ensemble members using dynamical adjustment (e.g., Deser et al., 2016). Specifically, we quantify how well the long-term “forced response” (i.e., the average across all 50 ensemble members) can be approximated by the residuals of our predictions (the difference between precipitation simulated by the RCM and the circulation-induced component of precipitation predicted by the Latent Linear Adjustment Autoencoder). In other words, dynamical adjustment acts as a filter for short-term “circulation-induced” precipitation variability. Recall that we expect the residuals to contain primarily contain the thermodynamic component of change (Deser et al., 2016). In other words, dynamical adjustment acts as a filter for “circulation-induced” precipitation variability. However, it is important to stress that the residual is not a perfect proxy for thermodynamical change, because it may contain effects from feedbacks, remaining internal variability and circulation components not directly captured by SLP. Moreover, since the SLP data is detrended prior to the application of the method, long-term dynamical changes may even be part of the residuals. In addition to analysing the forced response of mean precipitation in seasonal precipitation totals, we evaluate the estimation of the forced precipitation response for two composites of atmospheric circulation based on EOF analysis of SLP.
4 Results and Discussion

4.1 Reconstructed and predicted spatial fields

We begin by showing a selection of reconstructed precipitation fields $\hat{Y}$ from the holdout ensemble member “kbb” (center, Fig. 3), which illustrates the skill of the encoder and decoder, and predictions $\hat{Y}_X$ (right, Fig. 3), which illustrate the skill of the linear latent model $h$, against the original RCM-simulated precipitation $Y$ (left, Fig. 3). The reconstruction quality, i.e. the similarity between the left and the center column, is quite high, though not all fine details are reproduced (which is to be expected). The predictions $\hat{Y}_X$ (right column) are computed using the linear model $h$ and the decoder $d$ with SLP time series as inputs. For the worst example (in terms of $R^2$; first row), the original spatial field shows that this corresponds to a day with very low precipitation while the LLAAE predicts larger precipitation in some regions (e.g. south of France), resulting in a very low $R^2$ value. For the other rows (25%-percentile–best example), the predictions resemble the original image fairly well. For dynamical adjustment we use the residuals $\hat{R}$, which are computed as the difference between the original fields $Y$ (left column) and the predictions (right column).

The proposed model yields spatially coherent predictions and explains a large proportion of the variance of $Y$. Skill of precipitation predicted with the Latent Linear Adjustment Autoencoder is quantified in Fig. 4, which shows the gridcell-wise MSE over all December-February days for the holdout ensemble member “kbb”. The spatial pattern of MSEs (Fig. 4) largely reflects the pattern of precipitation as simulated by the RCM. Prediction errors are high over heterogeneous terrain, likely linked to orographic precipitation, in particular on the western sides of mountain ranges such as the Alps in Central Europe, the Appenine in Italy, the Dinaric Alps in South-East Europe, and smaller ranges located in France and Germany. Prediction errors are also high at the west coast of the UK, whereas mean squared prediction errors appear relatively low over low altitude regions (e.g., northern France, Benelux, and north Germany). The spatial pattern of $R^2$ (the fraction of explained variance, Fig. 5) shows a more nuanced pattern dominated by a land-sea contrast. Over land, the circulation proxy generally explains a high proportion of variance (up to $\approx 90\%$), especially on the western slopes of mountain ranges, which receive a large fraction of their precipitation from large-scale circulation-induced events. In contrast, the fraction of variance explained by circulation-induced precipitation is smaller on the eastern sides of mountain ranges, and particularly low over oceanic regions (which we do not interpret in this study).

4.2 Extraction of forced precipitation trends at high spatial resolution

In this subsection, we evaluate our predictions of the circulation-induced component in the framework of dynamical adjustment (Deser et al., 2016). That is, we test the extent to which the forced response of regional high resolution precipitation obtained from averaging across the full 50-member ensemble can be approximated by the residuals of our predictions from a single or from relatively few ensemble members. The thermodynamic component of the variation in precipitation, which is driven by temperature change and unrelated to dynamically-induced variability, should remain in the residuals (e.g., Deser et al., 2016). Dynamical adjustment, hence, acts to reduce short-timescale circulation-induced variability, thus increasing signal-to-noise ratios of the long-term, forced thermodynamic component (Deser et al., 2016).
The effect of dynamical adjustment can be seen in Fig. 6. It shows time series of domain-average (land only) December-February seasonal mean precipitation totals simulated by the high resolution RCM, the predictions of the circulation-induced component for three holdout ensemble members, and the forced response. All three RCM ensemble members show an increasing trend in seasonal mean precipitation totals across the 21st century, over which large inter-annual variability is superimposed. In contrast, the predicted circulation-induced components capture the inter-annual precipitation variability well, but they do not show discernible trends. Consequently, the residuals have relatively smoothly increasing trends, which match the magnitude of the forced precipitation trend well (Fig. 6, right panels). This demonstrates successful dynamical adjustment of continental-scale, seasonal mean precipitation seasonal precipitation totals using the Latent Linear Adjustment Autoencoder.

It is more challenging, however, to identify and evaluate the forced precipitation response at the local scale of individual grid points. To this end, Fig. 7 shows the spatial pattern of forced 50-year (2020-2069) precipitation trends, the pattern of dynamically adjusted precipitation trends, and “raw” precipitation trends in RCM simulations for three holdout ensemble members. The forced response of winter precipitation change is dominated by a north-south contrast. The northern part of the domain is projected to experience a precipitation increase in the 21st century, while decreases in precipitation are projected for the southernmost part of the domain (mainly over the Mediterranean Sea). Increases in winter precipitation across most parts of the domain are largely due to thermodynamic and lapse rate changes (e.g., Brogli et al., 2019). Locally, forced precipitation trends are larger over heterogeneous terrain, which may be due to forced dynamic components that are independent of SLP (Shi and Durran, 2014). The latter paper shows idealized simulations of the forced response of orographic precipitation, which is dynamic, but it is driven by changes in vertical velocity on the upslope side that enhances orographic precipitation, which could be separate from the changes in upslope wind speed and thus SLP. Vertical velocity and could increase because of the increasing moisture with warming.

However, large variability in individual ensemble members is superimposed on the signal of forced change (Fig. 7, right), consistent with the large role of internal variability even on multi-decadal time scales (Leduc et al., 2019). For example, ensemble member “kct” (second row) produces a relatively strong drying trend over northern Italy, which is entirely due to internal variability. The dynamically adjusted version of “kct” shows only very weak drying in northeast Italy, whereas it shows an increased precipitation trend consistent with the forced response at all other locations in northern Italy. Similar differences can be seen between the adjusted and unadjusted trends for the other holdout ensemble members. Overall, the correlation of 50-year trends at a single location from a single ensemble member with the trend in the 50-member forced response is rather low (R = 0.4, RMSE = 0.098). However, the dynamically adjusted single ensemble members are more strongly correlated with the forced response and capture it more accurately (R = 0.58, RMSE = 0.052). Hence, to Fig. 8 (top panel) shows the RMSE for the reconstruction of forced 50-year precipitation trends (i.e., the 50-member average), via dynamical adjustment and the averaging of original ensemble members, as a function of the number of ensemble members n. With an increasing number of ensemble members (n), the reconstruction RMSE of the forced response reduces considerably. Hence, dynamical adjustment is particularly useful when only few members are available; e.g., for small ensembles up to five members. If only one member is available, the reconstruction RMSE of the forced 50-year precipitation trend is...
reduced by more than half via dynamical adjustment. Conversely, to achieve the same RMSE of a single dynamically adjusted ensemble member, an ensemble average of about four to six members would be required (Fig. 8, top panel). On the other hand, for ensembles with more than about 14 members, dynamical adjustment does not improve the ability to reconstruct the forced response. Moreover, dynamical adjustment reduces not only the reconstruction RMSE, but also reduces the spread of the distribution across ensemble members, as indicated by the boxes and whiskers in Fig. 8 (top panel). The overall reduction of the reconstruction RMSE also holds particularly for specific circulation regimes (Fig. 8, middle and bottom panel), and is discussed in the next subsection.

4.3 Circulation regime specific Elucidating forced precipitation trends for specific circulation composites at high spatial resolution

While dynamical adjustment of long-term trends of temperature and precipitation has become a standard tool for the detection and of forced thermodynamic trends (Smoliak et al., 2015; Deser et al., 2016; Guo et al., 2019; Lehner et al., 2018), a bigger challenge is to assess forced trends in specific circulation regimes. One example would be summer heat waves related to specific circulation conditions (Jézéquel et al., 2018).

Thus, we assess to what extent the forced precipitation response can be uncovered under specific circulation conditions from a small number of ensemble members. We create composites of the dominant mode of atmospheric winter circulation over Europe as diagnosed by EOF analysis over the historical period (1955-2020) in the RCM simulations. The first EOF of the coarse-resolution SLP field is shown in Fig. 9 (top). The dominant mode has a meridional gradient, with low pressure anomalies over northern Europe and high pressure anomalies over the Mediterranean. Although the domain includes only a small fraction of the North Atlantic, the dipole character of the EOF spatial pattern resembles the North Atlantic Oscillation.

We now generate composites of ‘EOF1+’ and ‘EOF1-’ regimes by isolating days that exceed the 75th percentile (‘EOF1+’) and those that fall below the 25th percentile (‘EOF1-’) in terms of the first principal component (Fig. 9, bottom). Note that the principal component time series associated with EOF1 does not show any discernible trend until the late 21st century, and only a very minor change thereafter, so we do not expect large forced changes in the SLP variability patterns over Europe. On winter days with strong positive EOF1 (‘EOF1+’, roughly analogous to NAO+), i.e. a pronounced north-south pressure gradient, increased westerly winds bring mild and moist air from the Atlantic into Central Europe (Fig. 9, bottom left). Conversely, the opposite regime suppresses westerlies, hence inducing drier conditions on average (Fig. 9, bottom right) which are also accompanied by colder temperatures.

For the 50-year forced precipitation trend on ‘EOF1+’ winter days (obtained by averaging across all ensemble members), there is a more pronounced precipitation increase on the western slopes of the Alps and in most parts of the domain north and west of the Alps (Fig. 10, left panel). Meanwhile, precipitation decreases in the EOF1+ regime over southern Europe.

Raw simulations for sets of three holdout members show variable 50-year (2020-2069) precipitation trends under the ‘EOF1+’ regime (Fig. 10, right panel), where the spatial pattern of each set of three averaged members only weakly resembles the forced pattern (pattern RMSE = 0.174). The dynamically adjusted holdout members reveal a pattern that more closely
resembles the forced response pattern (Fig. 10, middle panel), where forced changes in mountainous regions are particularly well captured; the pattern RMSE is reduced substantially (RMSE = 0.085).

Forced precipitation trends for 2020-2069 under ‘EOF1-’ conditions differ from ‘EOF1+’ conditions due to a change in the synoptic situation: the forced spatial pattern has generally weaker precipitation changes (due to overall drier conditions during ‘EOF1-’), and precipitation increases are confined towards southeastern Europe (Fig. 11, left panel). Meanwhile, over large regions north and west of the Alps, precipitation changes only weakly under these circulation conditions. Spatial patterns of dynamically-adjusted ensemble members (Fig. 11, middle panel) have a closer correspondence to the forced pattern than to the spatial patterns of ‘raw’ 50-year trends (Fig. 11, right panel). Pattern RMSE The reconstruction RMSE of the forced response is again substantially reduced (RMSE=0.052 for dynamically adjusted grid cells, RMSE=0.086 for raw trends).

The application of dynamical adjustment to composites of specific circulation regimes raises the question as to whether the Latent Linear Adjustment Autoencoder may be applicable to understanding the dynamical component in extreme precipitation events. While the LLAAE may be able to fill an important gap in reconstructing the dynamical component of daily precipitation fields, possibly including days with extreme precipitation (at least, the component proportional to surface pressure), it exhibits a tendency to smooth predicted precipitation fields (Fig. 3), which would presumably result in somewhat underpredicted extreme events. However, a detailed evaluation of the LLAAE in the context of extreme events will be the focus of future work.

Overall, we conclude that dynamical adjustment enables approximating the forced response from high resolution simulations with just a small ensemble of about three ensemble only a few ensemble members. This is possible for both long-term trends in mean precipitation seasonal precipitation totals as well as for trends under more specific synoptic regimes. If only a small ensemble is available, RMSEs of circulation regimes. The improvement for the ‘EOF1+’ and ‘EOF1-’ circulation regimes can be evaluated from Fig. 8 (middle and bottom panel), where reconstruction RMSEs of forced 50-year precipitation trends, based on one ensemble member, are reduced by up to about a factor of two (Fig. 8) by using dynamical adjustment based on the Latent Linear Adjustment Autoencoder. To achieve a similar forced response reconstruction RMSE, an ensemble average of about four to six members would be required (Fig. 8) both for seasonal trends (top panel) and the trends under specific circulation composites.

5 Another potential application: Emulating dynamically-induced variability in daily precipitation fields

While we focus on dynamical adjustment, the proposed statistical model also lends itself to other applications. Here we describe how to leverage the to obtain a weather generator for

4.1 Dynamical adjustment uncertainties, computational costs and future applications

One of the main uncertainties in dynamical adjustment is the question of whether and how to detrend the climate data (circulation fields and/or precipitation) prior to dynamical adjustment. This is somewhat subjective, and often discussed as an inherent uncertainty in the literature (see, e.g. Deser et al. (2016); Lehner et al. (2017) and Lehner et al. (2018) for a discussion about trend removal). Forced changes in European winter SLP are highly uncertain, and models disagree on the sign and
patterns of forced circulation change (Fereday et al., 2018), while thermodynamic aspects are typically considered more robust across models (Shepherd, 2014; Fereday et al., 2018). Therefore, it is critical to ensure that the statistical model does not fit a thermodynamical, forced signal and hence only models the dynamical variability. For the results presented in this work, we orthogonalized SLP EOF time series with respect to the ensemble-mean SLP change over time (i.e., a very simplistic but generic “detrending”). Our analysis shows that the residuals after dynamical adjustment match the ensemble mean very well (Fig. 6). Hence, if a trend signal is included in the prediction of the dynamical component of the climate model. Concretely, by bootstrapping (Efron, 1979) the SLP time series we obtain a new (bootstrap) sample $X^b$ on the basis of which we can generate predictions for the latent space variables $\hat{L}^b = h(X^b)$, which can then be decoded as $\hat{Y}^b = d(\hat{L}^b)$.

There are various options how to obtain the bootstrap sample of the SLP time series. Here, we present a simple first approach. Specifically, we use a simple block bootstrap for the SLP time series, i.e. precipitation field (e.g., due to hypothetical remaining trend artefacts in the pressure field), this effect is likely to be small because the residuals match the ensemble mean (forced) trend very well. In Appendix B, we test an alternative simple detrending approach, where SLP is not detrended, but where we detrend precipitation using a simple method. However, we stress that our study is intended as a proof-of-concept study using Latent Linear Adjustment Autoencoders within a large ensemble context. Appropriate detrending choices for real-world applications (e.g., on observations), or an interpretation of forced changes into thermodynamical vs. we split the original SLP time series $X$ into non-overlapping blocks (here, we choose a block length of 50 days). To create a new bootstrap sample $X^b$, we resample these blocks with replacement until the number of resampled days has reached the number of original days. By repeating this procedure $B$ times, we obtain different bootstrap samples $X^b$ for $b = 1, \ldots, B$. As an alternative to this simple block bootstrap, one could employ more elaborate bootstrapping techniques, such as a parametric bootstrap.

Resampling the low-dimensional SLP time series and using the to produce the corresponding precipitation fields has the advantage of avoiding the more complex and costly operations that depend on the high-dimensional spatial field for emulation. Modelling the spatial dependencies directly is challenging, while our technique leverages the trained models $h$ and $d$ to represent the relationship between the SLP time series and the dynamic precipitation component.

### 4.2 Demonstration of the high-resolution precipitation emulator

A selection of example daily precipitation predictions (based on the original SLP time series $X$) and emulated predictions (based on different bootstrapped SLP time series $X^b$ for $b = 1, \ldots, 5$, all based on the holdout ensemble member “kbb”) are shown in Fig. 7. The first column shows the precipitation predictions based on the SLP time series from the holdout ensemble member “kbb”. The remaining columns show different emulated predictions $X^b$ for $b = 1, \ldots, 5$. As is to be expected, the emulated predictions based on the individual spatial fields are not visually distinguishable from the original predictions. Next, we quantitatively assess the extent to which the precipitation distributions and temporal dependencies are preserved.

To quantify the difference between the emulated and RCM precipitation frequency and amount distributions (Pendergrass and Hartmann, 2000), we compute the Perkins’ scores (Perkins et al., 2007). Note that the Perkins’ score is a linear transformation of the Total Variation distance on the locally constant density defined by the histogram. Concretely, to compare the distributions of the
predictions based on the coarsened RCM SLP time series to the predictions based on the bootstrapped SLP time series, we pool the predictions from six holdout. Another important question is how much training data is necessary to achieve the presented results. One may argue that it is computationally cheaper to estimate the forced response using a—say—9-member-ensemble mean, instead of training the LLAAE based on simulations from nine ensemble members (“kbb”, “ket”, “keu”, “kev”, “kew”, “kex”) and six emulated datasets (all based on as done in this work). Indeed, as machine learning algorithms are known to require rather large amounts of training data, “proving” the case of LLAAE dynamical adjustment in a large ensemble may not be as straightforward. While we have shown that dynamical adjustment based on LLAAEs reduces the number of ensemble members required to identify a proxy of the holdout ensemble member “kbb”). Pooling a number of timeseries has the advantage of reducing noise. We use the Perkins’ scores to compare the precipitation frequency distributions for each grid cell. This skill score varies between 0 and 1, where 1 is perfect and 0 has no overlap; 0.9 is a very good skill score. The underlying histograms have evenly spaced bins in log space with a bin width of 0.1. The results are shown in Fig. ?? . The Perkins’ scores are very high across all grid points, with little spatial variation. The domain mean is 0.983, with a standard deviation of 0.005. Hence, the emulated predictions maintain approximately the same frequency distribution of precipitation as the predictions based on the coarsened RCM SLP.

We furthermore compute the Perkins’ scores based on the amount distribution of precipitation (Pendergrass and Hartmann, 2014). To calculate the amount distribution, we first sum the amount of precipitation in each bin of the precipitation histograms. Subsequently, we normalize by the total amount of precipitation. Since the total amount of precipitation can differ between the predictions based on forced response for local-scale 50-year winter precipitation trends substantially (Fig. 8), this approach evidently requires several ensemble members for training. While the results shown here are based on training the Latent Linear Adjustment Autoencoder with data from nine ensemble members (1955-2070 period), we have tested that the accuracy remains virtually identical if trained with about 43% less training data (nine ensemble members, but training only on 1955-2020, Appendix B), thus highlighting robustness of the coarsened RCM SLP time series and the emulations, we also show the relative difference between the total amounts of precipitation. In other words, the Perkins’ scores only assess whether the two amount distributions have the same shape. The Perkins’ scores for all grid cells are displayed in Fig. ?? . Again, the Perkins’ scores are very high throughout the domain. The domain average is 0.982 with a standard deviation of 0.010. Figure ?? shows the difference in total precipitation in percent relative to the total RCM precipitation. Over land the variations are generally less than 5%, with the exception of some Alpine regions. method against reasonable changes to the amount of training data.

To examine the behavior of the emulated precipitation fields across timescales, we compare the power spectra of the predictions based on the original SLP time series and the emulated predictions. For each grid point and each holdout ensemble member/bootstrap sample, we compute the smoothed power spectrum and average the resulting curves. (The power spectrum is computed using the R (R Core Team, 2020) function spec.pgram with a span of 20 of the Daniell smoothers.) Figure ?? shows the corresponding average power spectra. As can be seen, the distribution of power is well preserved in the emulated predictions. This shows that the coarse resolution RCM SLP blocks enable maintenance of physically plausible variations across timescales, which is a feature of Beyond the computational aspects, however, we anticipate the ultimate applications of LLAAE-based dynamical adjustment not on a large ensemble (where the forced response is typically approximated with the
ensemble average, (Deser et al., 2020)), but instead on simulations with models where only one or a few ensemble members may be available such as projections with regional climate models (Jacob et al., 2014). Hence, the results presented in this work are intended as a proof-of-concept study within a large ensemble. As the next step, we envision the application to different climate models (e.g., training on a large ensemble or multiple large ensembles, and application of the approach dynamical adjustment to models for which only a few simulations exist), and with ultimate application of the trained LLAAE on reanalysis SLP data. This would allow us to leverage the available data from climate model simulations while applying the method in a context where a direct calculation of the (n-member) ensemble mean is not possible. The transfer between climate models or towards reanalyses could explore adding other constraints or regularization to the linear model in the latent space, such as instrumental variables or anchor regression (Rothenhäusler et al., 2018) for distributional robustness (Meinshausen, 2018), which may benefit the robust applicability of LLAAEs (across different climate models or observations) without the need for re-training.

Because the bootstrapped samples depend entirely on the realizations that are available to draw from, we also test that the emulated realizations are not overly similar to one another. Recall that the six emulated realizations we consider above are all based on the holdout ensemble member “kbb”. Hence, we would like to assess whether the emulated data sets are more similar to the data from ensemble member “kbb”, compared to other holdout ensemble members. For this analysis, Fig. ?? (left panel) shows the averaged cross-correlation functions between the precipitation predictions based on (a) six emulated SLP time series data sets and (b) the generating holdout ensemble member (“kbb”) SLP time series, respectively. We evaluate the cross-correlations at each grid cell and average.

4.2 Alternative statistical and machine learning approaches

In principle, there are alternative approaches for statistical learning in the context of dynamical adjustment and also alternative options to employ deep neural networks. For instance, one could extend the method of Smoliak et al. (2015) or Sippel et al. (2019) by using a neural network instead of linear regression. In that case, however, one would have a separate fit for each grid point (i.e., not the 2D precipitation field as output). This would be computationally demanding and it is also questionable whether the resulting predicted spatial field would be as coherent. In contrast, the spatial field is modelled jointly in our approach—the optimization is performed over the whole spatial field at once. The joint modeling of the daily high-resolution precipitation field as a function of coarse-scale circulation also enables additional climate applications, one of which is outlined in Sect. ??.

Furthermore, one may wonder why the autoencoder is needed in the architecture of the LLAAE if the encoder is discarded when predicting dynamic precipitation from SLP. We contrast this averaged cross-correlation function with the cross-correlation functions of different holdout ensemble members (“ket”, “keu”, “kev”, “kew”, “kex”) with the holdout ensemble member “kbb” in the right panel of Fig. ?? In this analysis, if the former cross-correlations (left panel) are not significantly larger than the cross-correlations in the latter comparison (right panel), it would imply that a set of emulated SLP realizations based on one holdout ensemble member are sufficiently diverse. Indeed, we observe that the cross-correlations in the two comparisons are of the same order of magnitude and all are very small. Using the autoencoder for estimation allows us to link SLP EOFs as input with the 2D precipitation fields as output. Removing the intermediate stage of the autoencoder would constitute a challenging
estimation problem as the autoencoder helps to estimate the decoder. We are not aware of alternative ML algorithms for this input/output combination and the LLAAE is novel in this regard.

5 Conclusion and future work

In this work we have first introduced the Latent Linear Adjustment Autoencoder, which combines a linear model with the nonlinear decoder of a variational autoencoder. By combining a linear model, which takes a circulation proxy as input, with the expressive nonlinear (deep neural network) decoder, it can be easily trained, and allows for jointly modeling the dynamically-induced high-resolution spatial field of the climate variable of interest. The main methodological novelty is that we add a linear model to the variational autoencoder and include an additional penalty term in the loss function that encourages linearity between the circulation proxy and the latent space. This leverages the advantages of a linear relationship between circulation variables and latent space variables, hence enhancing robustness, while also benefiting from the advantages of deep neural networks (i.e., flexibility in modeling non-linearities, such as those that occur in high-resolution orographic precipitation).

Future work targeting climate applications could explore the robust transfer of LLAAE’s between different climate models, reanalyses data, or observations, by using ideas from transfer learning or distributional robustness (Meinshausen, 2018), for example through adding other constraints or regularization to the linear model in the latent space, such as instrumental variables or anchor regression (Rothenhäusler et al., 2018) for distributional robustness (Meinshausen, 2018). Enforcing distributional robustness may be particularly interesting in the context of transfer learning, i.e., training the on climate model simulations and applying the trained to observations without the need for re-training.

Second, as the main application, we have tested the applicability of the Latent Linear Adjustment Autoencoder to dynamical adjustment of high-resolution precipitation based on daily data at regional scales. Based on a circulation proxy, the Latent Linear Adjustment Autoencoder predicts dynamic (circulation-induced) precipitation at high resolution. An estimate of the forced precipitation response can then be separated from internal variability, leaving higher signal-to-noise compared to raw multidecadal trends. With only a small ensemble of about 3–one or two ensemble members, root mean squared errors are roughly halved compared to raw trends when estimating the forced response (see Fig. 8), leading to dynamically-adjusted spatial trend patterns that closely resemble those of the approximated forced response (i.e., the ensemble average over 50 members), despite large internal variability. Moreover, we have used dynamical adjustment with the Latent Linear Adjustment Autoencoder to extend the framework to uncover estimates of the forced response conditioned on specific circulation regimes. We illustrated this aspect for composites of days with prevailing westerly conditions and hence wet conditions over Western Europe (similar to NAO+ regimes), and conversely, for days with suppressed westerlies (similar to NAO-) and hence generally drier conditions in Western Europe. In both cases the Latent Linear Adjustment Autoencoder was able to provide a better estimate of the forced response (i.e., with reduced error) compared to raw trends.

Further use cases of the Latent Linear Adjustment Autoencoder may include further applications of dynamical adjustment, including transfer learning across different high resolution simulations such as EURO-CORDEX models (Jacob et al., 2014). Eventual application to observations for regional-scale detection and attribution of precipitation changes is anticipated.
More general applications, such as statistical downscaling of the circulation-induced component of precipitation variability in coarse-scale GCMs, or in order to reconstruct observations at high resolution based on the prevailing large-scale circulation, are also conceivable. Importantly, the Latent Linear Adjustment Autoencoder requires only a coarse-scale circulation proxy (like SLP) to generate an estimate of dynamic precipitation at high resolution.

Lastly, beyond dynamical adjustment, we have illustrated how to leverage a further broad application of the Latent Linear Adjustment Autoencoder within climate science may lie in the area of model emulation (Castruccio et al., 2014; Beusch et al., 2020). For example, the LLAAE approach may help to emulate dynamically-induced variability in daily precipitation fields, where the Latent Linear Adjustment Autoencoder may be leveraged as a weather generator of the dynamical component. After training the LLAE, predictions for the latent space variables can be generated based on new samples of the SLP time series, obtained for instance via bootstrapping or from a coarse-resolution GCM, which then would allow to emulate daily precipitation dynamics at high spatial resolution. While modelling the spatial dependencies directly is challenging, this technique may leverage the trained models to represent the relationship between the SLP time series and the dynamic precipitation component. Thus, this approach has the advantage of avoiding the more complex and costly operations that depend on the high-dimensional spatial field for emulation. While the results we have presented are promising in the sense that they produce realistic spatial and temporal patterns of daily precipitation over Central Europe, leveraging the relationship between large-scale circulation and precipitation, the technique should be adapted to and evaluated in more detail in the context of specific use cases.

Overall, the Latent Linear Adjustment Autoencoder may prove a versatile tool for climate and atmospheric science, specifically for modeling relationships between large-scale predictors and local and nonlinear precipitation at high resolution.

Appendix A: Experimental details

In this section, we detail the architecture used for the encoder and decoder of the proposed model. Additionally, we report the most important hyperparameters. All further details can be found in the accompanying code; see the “Code and data availability” section below for details. For the encoder and the decoder we use three convolutional layers and one residual layer (He et al., 2016) with filter sizes 16, 32 and 64 and a kernel size of 3. The dimensionality of the latent space $L$ is chosen to be 400. For the SLP time series we extract 750 components such that the linear model $h$ receives 750 predictor variables as input and has 400 target variables. The model is trained using the Adam optimizer (Kingma and Ba, 2015) for 100 epochs with a learning rate of $10^{-3}$. The penalty weight $\lambda$ in Eq. (2) is set to 1.

Appendix B: Additional experimental results for dynamical adjustment of daily precipitation

As discussed in the main text, one of the main uncertainties in dynamical adjustment is how to ensure that the statistical model does not fit a thermodynamic, forced signal and hence only models the dynamic internal variability. Fitting a forced signal can potentially be mitigated by (i) an appropriate choice of the training period and (ii) suitable pre-processing of the data. Furthermore, another important question is how much training data is necessary to achieve the presented results, even though
we do not see the ultimate use case of LLAAEs to be used for dynamical adjustment in large ensembles (also see the discussion in Sec. 4.1). To address these points and to further corroborate our results, we perform two additional analyses to understand the sensitivity of the LLAAE to (i) the training period choice, (ii) the amount of training data as well as (iii) the sensitivity to different detrending approaches.

### B0.1 Training on the time period 1955-2020

We train on the shorter period from 1955-2020 (as opposed to 1955-2070), using the same nine ensemble members as described in the main text. This corresponds approximately to a 43% reduction in training data, but more importantly, this restricts the training to a period with relatively modest precipitation change. We then reproduce the analysis with this model trained on (i) this shorter time period; and (ii) less data. We find that the $MSE$ and $R^2$ performance measures indicate very robust results with respect to these changes in the input data (see Fig. A1 and A2). Furthermore, the dynamical adjustment analysis based on the shorter training period reveals almost identical results as compared to the longer 1955-2070 training period. That is, the residual variability is much closer to the ensemble mean forced response (see Fig. A3). This sensitivity analysis thus provides support that our method is robust to (i) a shorter time period and (ii) less training data points.

### B0.2 Detrending precipitation

The question of whether and how to detrend prior to dynamical adjustment is open, somewhat subjective, and often discussed as an inherent subjective choice and uncertainty in dynamical adjustment papers (see, e.g. Deser et al. (2016); Lehner et al. (2017) and Lehner et al. (2018) for a discussion about trend removal). Here, in addition to the results presented above, we test an alternative simple detrending approach: SLP is not detrended, but we detrend precipitation using a simple LOESS smoother, fitted on the ensemble (seasonal) means at every location and subtracted from every day individually. (Furthermore, we here use the shorter 1955-2020 period for training the model.) For the dynamical adjustment analysis, we then compute the residuals based on the non-detrended precipitation data and our predictions (from the model trained on the detrended precipitation data; see Fig. A4). This analysis suggests that this approach to detrend precipitation is too simplistic since the residuals of the dynamical adjustment analysis underestimate forced changes (the ensemble mean) to some extent (Fig. A4). There are several possible reasons for this:

1. Precipitation change cannot be modelled by a single additive mean change across the whole distribution. For instance, precipitation change is known to increase the variance of the precipitation distribution (Pendergrass et al., 2017). Hence, by subtracting the estimated, seasonally averaged precipitation trend we may have not fully removed the trend for wet days. Developing a more refined approach to remove the forced precipitation changes from daily data is non-trivial and beyond the scope of this work.

2. There may be some dynamically-induced changes in precipitation, but it would be hard to evaluate this without any additional simulations where dynamical effects and thermodynamical effects could be separated.
Overall, we conclude that our simple SLP detrending (without detrending precipitation) is a useful approach for introducing LLAAEs as a versatile tool for dynamical adjustment, as demonstrated by the fact that the residuals of individual ensemble members after dynamical adjustment match the ensemble mean trend of precipitation very well (e.g., Fig. 6). However, we acknowledge that considerations around whether and how to detrend the data prior to dynamical adjustment are crucial, especially for real-world applications (also see the discussion in Sect. 4.1).

Appendix C: Experimental results for dynamical adjustment of daily temperature

The following results are based on temperature anomalies. In Fig. A5, we show examples from the holdout ensemble “kbb” of (i) original temperature fields \( Y \) (left column), (ii) reconstructions \( \hat{Y} \) (center column), and (iii) predictions \( \hat{Y}_X \) (right column). The reconstruction quality, i.e. the similarity between the left and the center column, is quite high, even though not all fine details are reproduced. For dynamical adjustment, we use the residuals, which are computed as the difference between the original fields (left column) and the predictions \( \hat{Y}_X \) (right column). The predictions are computed using the linear model \( h \) and the decoder \( d \) with SLP time series as input. As can be seen, the proposed model yields spatially-coherent predictions and explains a large proportion of the variance of \( Y \).

Figure A6 shows the gridcell-wise MSE and Fig. A7 shows the \( R^2 \) statistics for the holdout ensemble “kbb”.

Code and data availability. The Latent Linear Adjustment Autoencoder model is free and open source. It is distributed under the MIT software license which allows unrestricted use. The source code is available at the following GitHub repository: https://github.com/christinaheinze/latent-linear-adjustment-autoencoders. A snapshot of the source code used to generate the results presented in this manuscript is available at https://doi.org/10.5281/zenodo.3957494 (Heinze-Deml, 2020a). The pretrained models can be obtained from https://doi.org/10.5281/zenodo.3950044 (Heinze-Deml, 2020c). Finally, the input data is available at https://doi.org/10.5281/zenodo.3949747 (Heinze-Deml, 2020b).

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Figure 1. Illustration of a standard autoencoder model: The spatial fields \( Y \) are fed to the encoder \( e \) which maps them to the latent space variables \( L \) (illustrated in blue). These are in turn fed to the decoder \( d \) which computes a reconstruction of the input, \( \hat{Y} \).
Figure 2. Illustration of the Latent Linear Adjustment Autoencoder *after training*: The input features $X$ (illustrated in gray) are fed to the linear model $h$ which yields a prediction for the latent space variables $L$ (illustrated in light blue). These are in turn fed to the decoder which computes a prediction of the spatial field based on $X$ only, $\hat{Y}_X$. Training the models $e$, $d$ and $h$ is performed iteratively in an alternating fashion.
Figure 3. Examples of (i) original precipitation fields (left column), (ii) reconstructions (center column), and (iii) predictions (right column). The examples are chosen such that the $R^2$ value of the prediction increases from top to bottom: The first row shows the worst example in the holdout dataset, the last row shows the best example, and the remaining rows show examples at the 25%-, 50%- and 75%-percentiles, respectively. For better visibility, data are square-root-transformed. Hence, the units are $\sqrt{\text{mm}} \cdot \text{d}^{-1}$. 
Figure 4. Mean-squared error (MSE, based on precipitation data in mm·d$^{-1}$) for each grid cell for the precipitation predictions.
Figure 5. Proportion of variance explained ($R^2$) for each grid cell for the precipitation predictions.
Figure 6. Dynamical adjustment of the full domain (land grid cells only) using autoencoders. (left) seasonal mean precipitation totals simulated by three members of the high-resolution RCM in black (top: ‘kbb’, middle: ‘kct’, bottom: ‘kcu’), the predicted (‘circulation-induced’) component for three ‘holdout’ ensemble members (blue) and the forced response (average across all 50 members, red). (right) Residuals from the prediction (black dots) and the forced response (red).
**Figure 7.** Dynamical adjustment of 50-year winter precipitation trends (2020-2069). (Left column) Forced precipitation response (2020-2069 linear winter precipitation trends averaged over *all* 50 ensemble members). (Middle Column) Linear 50-year winter precipitation trends in three randomly selected dynamically adjusted ensemble members (top: ‘kbb’, middle: ‘kct’, bottom: ‘kcu’). (Right column) Linear 50-year winter precipitation trends in the original ensemble members (top: ‘kbb’, middle: ‘kct’, bottom: ‘kcu’). (Bottom row) Scatter **plot** **contour lines** of 50-year precipitation trends in the forced response against 50-year precipitation trends over land in dynamically adjusted (middle) and originally simulated ensemble members (right).
Figure 8. Reduction in RMSE as a function of 50-year trends, calculated by averaging $n$ members, compared to 50-year trends using 50-member ensemble average (‘forced response’). RMSE’s are based on land grid cells only and shown for averaging $n$ original ensemble members (black) and averaging $n$ dynamically adjusted ensemble members (red). Trends are calculated over the entire DJF season (top), and only for EOF1+ (middle) and EOF1- situations (bottom). Boxplot whiskers indicate 2.5th and 97.5th percentiles (boxes show 25th and 75th percentiles) of RMSE distribution obtained from bootstrapping from the 41 holdout ensemble members used in dynamical adjustment.
Figure 9. (top) First Empirical Orthogonal Function of Sea Level Pressure over the full domain of the regional model. (Bottom) Winter precipitation anomalies for the 25% of days that show the strongest (left) and weakest (right) projection on the pattern of the first EOF (i.e., days with a strong zonal SLP gradient and hence dominant westerly flow (left), and days with weak to absent zonal SLP gradients (right)).
Figure 10. Dynamical adjustment of 50-year winter precipitation trends (2020-2069) under the ‘EOF1+’ regime (25% of all days that project strongest on the first EOF, i.e., that show a strong westerly flow). (Left column) Linear forced winter precipitation trends under the ‘EOF1+’ regime (2020-2069). (Middle Column) Linear 50-year winter precipitation trends in an average of three randomly selected dynamically adjusted ensemble members. (Right column) Linear 50-year winter precipitation trends in an average of three corresponding original ensemble members. (Bottom row) Scatter plots of 50-year precipitation trends in the forced response against 50-year precipitation trends over land in dynamically adjusted (middle) and originally simulated ensemble members (right).
Examples of (i) predictions based on the original input data $X$ (leftmost column) and (ii) emulated predictions based on bootstrapped input data $X^b$ (remaining columns). Here, we show emulated examples from five different bootstrap samples $X^b, b=1,...,5$. For better visibility of the precipitation features, the figure shows square-root-transformed data. Hence, the units are $\sqrt{\text{mm} \cdot \text{d}^{-1}}$.

Perkins' scores for the frequency distribution
Figure 11. Dynamical adjustment of 50-year winter precipitation trends (2020-2069) under the ‘EOF1-’ regime (25% of all days that project weakest on the first EOF). (Left column) Linear forced winter precipitation trends under the ‘EOF1-’ regime (2020-2069). (Middle Column) Linear 50-year winter precipitation trends in an average of three randomly selected dynamically adjusted ensemble members. (Right column) Linear 50-year winter precipitation trends in an average of three corresponding original ensemble members. (Bottom row) Scatter plots of 50-year precipitation trends in the forced response against 50-year precipitation trends over land in dynamically adjusted (middle) and originally simulated ensemble members (right).
Figure A1. Perkins’ scores—Training 1955–2020: Mean-squared error (MSE, based on precipitation data in mm · d⁻¹) for each grid cell for the amount distribution precipitation predictions.
Figure A2. Relative difference in total precipitation between the original and the emulated predictions (Training 1955-2020: Proportion of variance explained (in % $R^2$) for each grid cell for the precipitation predictions.)
Figure A3. Average power spectrum—Dynamical adjustment of (i) the original predictions—full domain (black) and grid cells only and but training only based on 1955-2020. (Left) Seasonal precipitation totals simulated by three members of the emulated predictions—high-resolution RCM in black (red top: ‘kbb’, middle: ‘kct’, bottom: ‘kcu’). The power spectra are averaged over grid points and six samples (i.e., six different ‘circulation-induced’) component for three ‘holdout’ ensemble members and six different bootstrapped data set (blue) and the forced response (average across all 50 members, respectively red). Frequency is displayed in cycles per day (Right) Residuals from the prediction (black dots) and the spectrum is scaled such that the area under the curve equals the variance of the signal forced response (red).
Figure A4. Left: Average cross-correlation functions between six different emulated data sets. **Dynamical adjustment** of dynamically-induced precipitation and the predicted dynamically-induced precipitation based on the original input data **full domain** (from ensemble member “kbb”), respectively. The cross-correlation functions are computed at each land grid cell but training only based on 1955-2020 and averaged over the whole spatial field. **Right:** Equivalent computation, contrasting the predicted dynamically-induced precipitation with precipitation detrended instead of five holdout SLP before model training and dynamical adjustment. **(Left)** Seasonal precipitation totals simulated by three members of the high-resolution RCM in black (“top: ‘kbb’, middle: ‘kct’”, “bottom: ‘kcu’, ‘kcv’, ‘kew’, ‘kcx’”) with the predicted (‘circulation-induced’) component for three ‘holdout’ ensemble member “kbb”. The cross-correlations in the right members (blue) and left panel are of the same order of magnitude and **forced response** (average across all very small 50 members, red). The difference between (Right) Residuals from the two cross-correlation functions is irrelevant due to the small magnitudes prediction (black dots) and can hence be disregarded the forced response (red).
Figure A5. Temperature anomalies. Examples of (i) original temperature fields $Y$ (left column), (ii) reconstructions $\hat{Y}$ (center column), and (iii) predictions $\hat{Y}_X$ (right column).
Figure A6. Temperature anomalies. Mean-squared error (MSE) for each grid cell for the temperature predictions.
Figure A7. Temperature anomalies. Proportion of variance explained ($R^2$) for each grid cell for the temperature predictions.