Emergent ultrafast phenomena in correlated oxides and heterostructures

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Abstract
The possibility of investigating the dynamics of solids on timescales faster than the thermalization of the internal degrees of freedom has disclosed novel non-equilibrium phenomena that have no counterpart at equilibrium. Transition metal oxides (TMOs) provide an interesting playground in which the correlations among the charges in the metal d-orbitals give rise to a wealth of intriguing electronic and thermodynamic properties involving the spin, charge, lattice and orbital orders. Furthermore, the physical properties of TMOs can be engineered at the atomic level, thus providing the platform to investigate the transport phenomena on timescales of the order of the intrinsic decoherence time of the charge excitations. Here, we review and discuss three paradigmatic examples of transient emerging properties that are expected to open new ﬁelds of research: (i) the creation of non-thermal magnetic states in spin–orbit Mott insulators; (ii) the possible exploitation of quantum paths for the transport and collection of charge excitations in heterostructures; (iii) the transient wave-like behavior of the temperature ﬁeld in strongly anisotropic TMOs.

Keywords: transition metal oxides, heterostructures, ultrafast dynamics, pump probe, electronic coherence, coherent transport, photon harvesting

(Some ﬁgures may appear in colour only in the online journal)

1. Introduction: emergent phenomena at ultrafast timescales

The dramatic advances in ultrafast science are unlocking the gate to the development of a multitude of complementary techniques to investigate condensed matter systems strongly driven out of equilibrium. Nowadays, different excitation schemes can be used to selectively stimulate speciﬁc degrees of freedom (for a comprehensive review see [1]): THz/infra-red radiation can couple with superconducting condensates and can be exploited to manipulate charge and spin gaps and to resonantly excite speciﬁc eigenmodes of the lattice; near infrared/visible light can be exploited to create non-thermal fermionic and bosonic distributions and to artiﬁcially manipulate the band populations; UV/x-ray pulses resonate with charge-transfer (CT) processes or other optical transitions that involve deep electronic levels. At the same time, the recent advance in the design and realization of multiple probing schemes is boosting the elaboration of a coherent picture of ultrafast phenomena in solids. The complete reconstruction of the charge, spin and lattice dynamics triggered by the sudden photo-induced quench of a system is
close to realization. Besides the well-established possibility of probing the dynamics of the dielectric function in a broad range of the electromagnetic spectrum (from fractions of THz to the ultraviolet), the development of table-top [2–4] and free electron laser (FEL) [5–7] based x-ray sources is opening new tantalizing opportunities, ranging from the direct mapping of the occupation of high binding-energy electronic states via time-resolved x-ray photoemission [8, 9] to the reconstruction of the spin and lattice dynamics via resonant x-ray diffraction [10–13].

In principle, the possibility of creating artificial initial states that evolve on a timescale shorter than the time necessary for the internal equilibration of the different fermionic and bosonic subsystems can be exploited to tackle many fundamental questions in condensed matter physics and to open completely unexplored fields [14–16]. For example, cold atoms trapped into artificial optical lattices have been long exploited for investigating the way quantum many-body systems relax after an initial quench [17, 18]. The possibility of creating optical lattices without imperfections and time/spatial fluctuations (phonons) enables the study of ideal solids in which the relevant interaction terms, such as the on-site Coulomb repulsion ($U$) and the hopping ($t$) are selectively tuned. Furthermore, the small energy scales involved and the almost complete decoupling from the environment rise the typical relaxation timescales to milliseconds, thus allowing the real time investigation of the way many-body excited states propagate and eventually thermalize in an artificial interacting system that mimics a specific microscopic Hamiltonian [17, 18].

Whereas cold atoms provide a clean test bench for theories, they are hardly exploitable to explore the non-equilibrium physics of real solids that constitute the building blocks for novel devices characterized by innovative functionalities [19] (see figure 1). Among the many solid-state systems of technological interest, strongly correlated materials (SCMs) [20, 21]—in which the strong short-ranged electronic interactions provoke the failure of the independent-electron approximation—provide a very interesting case-study for non-equilibrium physics [22, 23]. SCMs are inherently characterized by the intertwining of the charge, spin and lattice degrees of freedom, which gives rise to an impressive number of physical processes that can be simultaneously accessed. Nonetheless, the common perception is that the introduction of new variables—the excitation pathway and the time evolution—in the physics of correlated materials makes the treatment of these systems even more complex and pushes their modeling beyond any reliable theoretical scheme. Here, we will review some interesting cases in which the ultrafast capability of state-of-the-art techniques leads to the simplification of the physics of correlated materials and paves the way to the study of emergent phenomena that have no counterpart at equilibrium. This is particularly relevant at the nanometric scale and in few-atomic layers heterostructures, in which the timescales for the charge and energy propagation can be shorter than (or of the order of) the coupling with the thermal bath constituted by the spin and lattice fluctuations. In particular, transition-metal oxides (TMOs) are the ideal systems for exploring these phenomena [24]. As a consequence of the local correlations of the metal $d$ electrons, TMOs are always on the verge of multiple phase transitions. Furthermore, the possibility of controlling at the atomic level the construction of artificial blocks and heterostructures constitutes an additional knob that is expected to open exciting research fields [19].

Here, we will review and discuss three different paradigmatic examples of emergent phenomena at the ultrafast timescale:

(i) The magnetic dynamics in relativistic Mott insulators. $5d$ TMOs provide an interesting example of Mott insulators in which the local moments have also orbital character. The dynamical constraints related to the substantial spin–orbit coupling (SOC), to the peculiar characteristics of $d$ electrons and to the actual topology of the lattice allow to photoexcite transient non-thermal states. Furthermore, the possibility of photoinjecting local charge excitations that propagate in an artificial magnetic environment with no counterpart at equilibrium is expected to shed new light on the origin of the exotic magnetic properties of these materials.

(ii) Quantum-coherent phenomena in correlated oxide-heterostructures. When the size of the material is reduced to few atomic layers, the time necessary for collecting charge excitations is confined to the sub-10 fs timescale. This time is of the order of the decoherence time of the initial quantum wavefunction that is created by the absorption of a photon. We will argue that quantum-coherent effects, stemming from the propagation of local many-body excitations without loss of quantum-coherence, can be observed and potentially
exploited on the ultrafast timescale in few-atomic-layers oxide heterostructures.

(iii) Wave-like regime for the temperature propagation at the nanoscale. Describing the way the excess energy provided by an ultrashort light pulse propagates at the nanoscale is a very intriguing issue that challenges many well-established concepts. We will show that there exists a regime in which the temperature propagation exhibits an emergent wave-like behavior that can impact the thermal transport properties of TMO nanostructures.

2. The magnetic dynamics in relativistic Mott insulators

2.1. Spin–orbit Mott insulators: a platform for ultrafast magnetism

The capability of inducing, detecting, and reversibly switching the magnetization of materials on ultrafast timescales (from pico- to femto-seconds) and at atomic distances is an extremely urgent task for material scientists [25]. The incapable need and the ever-growing urgency are simply dictated by the daily increasing technological demand to overcome the limitations, in terms of speed and density, of today’s magnetic memories and, more in general, digital electronics (logic gates, storage devices, ...). This quest goes well beyond searching for a new material, which can optimize the actual technology, and regards the concurrent development of new ideas, tools and overall technologies to control the magnetic response of a functional material. One very promising route exploits ultrashort light pulses to photo-stimulate the emergence of novel magnetic states on timescales much shorter than the internal thermalization [26]. In particular, by exploiting the interplay between the electronic and spin degrees of freedom, it is possible to induce transitions towards transient non-thermal states, whose magnetic properties are different from those exhibited in the equilibrium state. As an example, ultrafast optical techniques have been proposed as a tool to directly manipulate the exchange coupling \( J_{\text{ex}} \) in Mott insulators [27, 28] and have been used to induce femtosecond magnetic switching in manganites [29] by exploiting an initial quantum-coherent magnetic regime on timescales faster than the coupling with the incoherent environment. Moreover, the intrinsic capability of being reversible makes these all-optical routes usually preferable with respect to ordinary chemical or surface doping. Along this line of thinking, it is urgent to find new classes of SCMs that can be efficiently used as playgrounds for inducing transient non-thermal magnetic states by means of ultrafast optical techniques.

Mott insulators are always characterized by a very strong antiferromagnetic coupling driven by the virtual hopping \( t_h \) of the electrons on neighboring sites, with an energy cost equal to the on-site Coulomb repulsion \( U \). The exchange energy in Mott insulators, which can assume very large values (up to \( \approx 150 \) meV), is given by \( J_{\text{ex}} = 2t_h^2 / U \) and regulates the dynamics of the localized spins on the correlated sites. Because \( J_{\text{ex}} \) originates from the electrostatic Coulomb repulsion and the Pauli principle, rather than from magnetic dipole forces, it can be directly modified by the change of the population of the Hubbard bands induced by photostimulation with ultrashort light pulses tuned across the Mott gap [27, 28]. Spin–orbit Mott insulators are emerging as a new interesting class of magnetic correlated materials. In these systems, the strong SOC gives rise to Mott insulating phases in which the local moments have also orbital character [30, 31], thus paving the way to the simultaneous control of both the magnetic state and the orbital occupation on the ultrafast timescale.

The family of 5d TMOs, such as iridium oxides, is considered as one of the most promising systems to investigate the ultrafast charge/orbital/magnetic dynamics in spin–orbit Mott insulators. In 5d TMOs one of the fundamental assumptions shared by almost all microscopic and phenomenological theories for strongly correlated systems—the presence of a single energy scale dominating over all others—dramatically fails. The increased average radius of the 5d orbitals, as compared to that of the 3d TMOS, simultaneously leads to the reduction of the on-site Coulomb repulsion (down to \( U \sim 1 \) eV) and to the increase of the hopping integrals (spin-orbit coupling strength up to \( t_h \sim 0.4 \) eV) and, consequently, of the bandwidth \( W \) [32]. As a consequence of the closeness of the \( U \) and \( W \) energy scales, neither a local Mott-like picture nor a delocalized Wannier scenario is fully appropriate to capture even the most basic physics of these compounds. As a further element, the large atomic number of the 5d metal ions makes the SOC extremely relevant (spin-orbit coupling strength up to \( \lambda_{\text{SOC}} \sim 0.7 \) eV) for the electronic and magnetic properties of the system [30, 33, 34]. The topology of the lattice, combined with the actual valence of the transition-metal ion, determines the orbital and spin effective interactions and, consequently, the possible orderings and critical temperatures of the system. As an example, the interplay of the lattice topology and SOC can lead to bond-directional magnetic interactions (Kitaev-like terms in the effective-spin Hamiltonian) [35] that drive a strong frustration of the magnetic ground state and the possible emergence of exotic spin-liquid phases at low temperatures [33, 36–38].

In the following sections, we will provide two examples of 5d TMOS (the sodium iridate, Na3IrO3, and the strontium iridate, Sr2IrO4) in which the interaction between the SOC and the topology of the lattice links the dynamics of local magnetic moments to the creation, propagation and recombination of photo-injected charge excitations. The out-of-equilibrium approach permits both to better address the leading interactions that determine the equilibrium properties and to produce transient non-thermal states with an emergent magnetic dynamics due to the coupling of the photo-injected electron–hole excitations with an “artificial” magnetic environment. These findings open new routes in the investigation and, possibly, in the optical control of novel excitations and of exotic phases (e.g. spin-liquid) in 5d TMOS.
2.2. Honeycomb-lattice sodium iridate

In Na$_2$IrO$_3$, the edge-sharing IrO$_6$ octahedra form skewed (with respect to the crystallographic axes) planes of Ir ions arranged in a honeycomb lattice (see figure 2). The octahedral crystal-field of the oxygen cage splits the Ir-5$d$ orbitals in two manifolds: $e_g$, much higher in energy and out of the scope of the present analysis, and $t_{2g}$, at lower energy and occupied by 5 electrons [39–41]. The actual distortions lift the degeneracy of the $t_{2g}$ manifold and affect the hopping amplitudes within and between the Ir hexagons [32, 42, 43]. The system exhibits an insulating gap of $\sim$340 meV [31] and quite complex magnetic properties: strong magnetic correlations below $\Theta_{\text{corr}} \sim 100$ K and a long-range ordered zig-zag phase below $T_K \sim 15$ K [41, 44, 45]. The large frustration parameter $\Theta_{\text{corr}}/T_K \sim 7$ suggests the tendency to form a low-temperature spin-liquid phase out of which the zig-zag order emerges.

2.2.1. Band-structure calculations. The complexity of the electronic and magnetic properties is usually treated starting from two opposite perspectives, which rely on different starting points to construct the basis which describes the electronic wavefunctions.

- The fully localized picture. The localized picture [30, 37, 38] builds on the assumption that the SOC splits the six $t_{2g}$ levels and returns four completely filled $J_{\text{eff}} = 3/2$ levels and two half-filled $J_{\text{eff}} = 1/2$ levels. This new arrangement of the levels opens up the possibility to get a single-band Mott insulator once the effect of even a small on-site Coulomb repulsion $U$ is properly taken into account. This $J_{\text{eff}}$ scenario leads to a description of the low-energy physics in terms of fully localized effective moments whose dynamics is determined by a Kitaev–Heisenberg Hamiltonian [37, 38]. The structure of the Kitaev-like term and, in particular, its strength with respect to the one of the ordinary Heisenberg term strongly depends on the actual value of the SOC ($\lambda_{\text{SOC}}$) and on the specific topology of the lattice and determines the most favorable arrangement of the effective moments. This issue is still open as the estimates present in the literature do not yet agree and lead to magnetic orderings not always compatible with the experimentally observed one. The 340 meV insulating gap and the strong magnetic frustration, along with the recent measurement of bond directional interactions, are fully compatible with the $J_{\text{eff}}$ scenario that, at the moment, is the most accredited picture to describe the low-energy magnetic dynamics.

- The delocalized picture: quasi molecular orbitals (QMOs). If one takes into account from the beginning the large oxygen-mediated hopping term ($\sim$250 meV) between neighboring Ir atoms, it seems reasonable to study the effects of the large SOC and of the small $U$ not on the local Ir--$t_{2g}$ levels, but on QMOs extending over the whole Ir hexagon. The QMOs are the exact basis states of a non-interacting, zero SOC, isolated hexagon of Ir ions and are built from linear combinations of Ir--$t_{2g}$ Wannier functions [32, 43]. In terms of QMOs, the effective residual hopping is reduced to smaller values and to shorter extents better justifying a subsequent perturbative approach in terms of $\lambda_{\text{SOC}}$ and $U$. As a matter of fact, the QMO scenario not only perfectly rationalizes the outcome of full-fledged (actual distortions and lattice
structure) relativistic band-structure calculations [32, 43], but it also accounts for the great variety of structures observed via photoemission and optical spectroscopy up to $2 \, \text{eV}$ [46], thus demonstrating its validity and efficiency.

2.2.2. The non-equilibrium experimental approach. In [47], a non-equilibrium approach has been adopted to investigate the interplay between the dynamics of the localized $J_{\text{eff}}$ moments and the delocalization of charge excitations on the Ir honeycombs (QMO picture). The possible link between the magnetic dynamics and the QMO picture is directly provided by the Na$_2$IrO$_3$ electronic band structure (see figure 2), that has been calculated by ab initio relativistic density functional theory (DFT). As already observed in several works [32, 42, 43, 48], the DFT-calculated density of states (DOS) presents five separated bands which are strongly reminiscent of the QMOs. The six QMOs localized on a particular hexagon can be grouped into the lowest-energy $B_{1u}$ singlet, the two doublets $E_{1g}$ and $E_{2u}$, and the highest-energy $A_{1g}$ singlet [32]. SOC mixes the three QMOs closer to the Fermi energy, splits the doublets and opens up a pseudogap [32, 43] that widens up to the experimental insulating gap when the Coulomb repulsion $U_{\text{eff}}$ is considered [46]. Interestingly, the QMO representation is fully compatible with the zig-zag ordered ground state observed at $T < T_K$: there exist three couples of QMOs that form linear combinations preserving both the spatial arrangement and the magnetic polarization of the zig-zag order. The $B_{1u} \pm E_{1g}^{(2)}$ modes are mostly confined to binding energies of the order of $0.5$–$1.5 \, \text{eV}$, with a resulting very small overlap with the states at the Fermi level, and feature a quite small overall net polarization. Instead, the $E_{1g}^{(1)} \pm E_{2u}^{(2)}$ modes, which are mainly located at $\sim 1 \, \text{eV}$ binding energy, are almost fully polarized according to the zig-zag pattern and are characterized by a non-zero overlap with both the occupied states right below the Fermi level and the empty states at $\sim +0.3 \, \text{eV}$. In order to recover the full DOS of the low-energy occupied states, it is however necessary to consider also the contribution from the $A_{1g} \pm E_{2u}^{(2)}$ modes, which are fully polarized and extend in energy from $\sim -0.3 \, \text{eV}$ to $\sim +0.7 \, \text{eV}$. The necessity of including more than one QMO combination to describe the valence—lower-Hubbard band (LHB) in the localized description—and the conduction—upper-Hubbard band (UHB) in the localized description—bands, suggests that the QMO picture, which captures the main features of the deep electronic states, is less efficient in describing the physics of the low-energy electronic excitations.

The $E_{1g}^{(1)} \pm E_{2u}^{(2)}$ QMO combination acts as perfect link between the low-energy dynamics and the high-energy electronic properties. Considering its significant overlap with the low-energy states close to the Fermi level and the almost full polarization of both the occupied states at $\sim -1 \, \text{eV}$ and the empty states at $\sim +0.3 \, \text{eV}$, it is natural to foresee a strong interplay between this QMO combination and electron–hole excitations photoinjected via ultrashort light pulses and eventually decaying and releasing energy to the zig-zag magnetic background. To test this scenario, Nembrini et al. focused on the ultrafast dynamics of the optical conductivity in the $1.4$–$2.1 \, \text{eV}$ energy range, that corresponds to the optical transitions from the occupied $E_{1g}^{(1)} \pm E_{2u}^{(2)}$ and $B_{1u} \pm E_{1g}^{(2)}$ QMOs to the empty conduction band [47]. The basic idea of the experiment is to use an ultrashort light pulse (photon energy $1.55 \, \text{eV}$) to photoinject local electron–hole excitations across the Mott gap and to exploit the high binding energy QMOs to map the delocalization of the charges into the Ir honeycombs and the subsequent coupling of QMO-like charge excitations with the zig-zag magnetic background. The experiment shows that the partial melting of the short-ranged zig-zag magnetic background is mapped into the rearrangement of the narrow $E_{1g}^{(1)} \pm E_{2u}^{(2)}$ QMOs, as expected on the basis of the DFT calculations.

The time- and frequency-domain data reported in [47], combined with single-color pump–probe measurements [49, 50], provide a comprehensive picture of the relaxation dynamics in Na$_2$IrO$_3$ (see figure 2).

(a) The initial photo-excitation with $1.55 \, \text{eV}$ photons creates a highly non-thermal distribution of electron–hole excitations across the Mott gap. Within $\sim 200 \, \text{fs}$, these excitations relax through electron–electron interactions and the coupling with optical phonons. This process leads to the fast accumulation of doublons (i.e. doubly occupied Ir sites) and holons (i.e. unoccupied Ir sites) at the bottom (top) of the UHB (LHB), whose recombination is prevented by the large value of the gap.

(b) As recently demonstrated in [49, 50], the interaction with the local magnetic environment drives the binding of these non-thermal excitations into local excitons. The effective doublon-holon interaction is mediated by the combined presence in the microscopic Hamiltonian of the Kitaev terms and of a weak Heisenberg-type ordering term and, consequently, grows with the distance and progressively trap them into pairs [49]. These constraints slow down the rate of energy exchange with the local magnetic background, which is completed only within few picoseconds.

(c) The localized photoexcited excitons degrade within few picoseconds via the delocalization on the Ir hexagons, thus recovering a quasi-molecular picture of excited charges immersed in a zig-zag background, characterized by a correlation length of the order of $1.5$–$2 \, \text{nm}$. As demonstrated in [32], such a short coherence length coincides with the length-scale necessary for a full tight-binding description of the Na$_2$IrO$_3$ band structure in terms of QMOs. Considering the almost full zig-zag polarization of the $E_{1g}^{(1)} \pm E_{2u}^{(2)}$ QMOs (see figure 2), the excess charge excitations in the UHB are intrinsically associated to the weakening of the zig-zag order, thus driving an effective heating of the spin background. As a feedback, the perturbation of the zig-zag magnetic order leads to a renormalization of the strongly coupled $E_{1g}^{(1)} \pm E_{2u}^{(2)}$ at $\approx 1 \, \text{eV}$ binding energy, that allows
and widely accepted [30]: the SOC splits the six $t_{2g}$ levels and returns two half-filled $J_{\text{eff}} = 1/2$ levels and four completely filled $J_{\text{eff}} = 3/2$ levels, further split in two doublets by a residual tetragonal (distortion) crystal field [54]. According to this scheme, the system behaves as a robust Mott insulator once the effect of the modest on-site Coulomb repulsion $U$ is properly taken into account [30]. The charge gap, estimated by optical conductivity [55] and resistivity [53] measurements is $\sim 100$ meV. The Sr$_2$IrO$_4$ magnetic properties can be efficiently described by a Heisenberg Hamiltonian [53, 54] with exchange terms up to third neighbors in plane ($J_{h} = 60$, $J_{hh} = -20$, and $J_{hhh} = 15$ meV) [53], while the out-of-plane term is as low as $J_z \approx 1$ $\mu$eV. The Heisenberg model accounts for the canted in-plane anti-ferromagnetic ordering with a critical Néel temperature of about 240 K [56].

2.3. Direct observation of the ultrafast dynamics of magnetic correlations. Electronic and magnetic correlations play a critical role in the formation of transient non-thermal magnetic states, but an appropriate tool for probing the momentum and energy dependence of these correlations has been lacking so far. In [13] the first time-resolved magnetic resonant inelastic x-ray scattering experiment was performed to directly probe the magnetization dynamics in Sr$_2$IrO$_4$, after the impulsive photo-doping across the Mott gap. X-ray photons, produced by a FEL and tuned to the Ir $L_2$ resonance in order to couple with the spin degree of freedom via the resonant magnetic x-ray scattering mechanism, are used as probe. The possibility of measuring the momentum transfer $Q$, the energy loss $E_{\text{loss}}$, and the time delay between the pump and the probe, allows to fully characterize the transient magnetic response of the system. The experiment was performed at 110 K, well below the Néel ordering temperature. The ($-3, -2, 28$) magnetic resonant Bragg peak intensity, which is sensitive to the presence of 3D magnetic order, has been measured as a function of the time delay and the pump fluence. For fluences larger than $5$ mJ cm$^{-2}$, corresponding to the excitation of a substantial fraction of the sites within the illuminated volume, the residual intensity of the peak falls below 10% indicating the partial melting of the 3D order. Then, tuning the pump fluence at 6 mJ cm$^{-2}$, the RIXS energy loss spectra has been measured after the photo-excitation and compared to the unperturbed one. The spectra exhibit two main features: (a) a dispersing magnon and (b) an orbital excitation at $\approx 600$ meV corresponding to the excitation of a hole from the $J_{\text{eff}} = 1/2$ state to the $J_{\text{eff}} = 3/2$ one [53, 54, 57]. The intensity of the orbital excitation, which is proportional to the population of the two $J_{\text{eff}}$ states, is very similar before and after ($t = 2$ ps) the photo-excitation, thus giving an upper limit to the lifetime of the $J_{\text{eff}} = 3/2$ photo-excited carriers. On the other hand, the transient optical reflectivity measured at 1.55 eV (800 nm) clearly shows that an appreciable population of photo-excited carriers persists at 6 mJ cm$^{-2}$ and 2 ps time delay. From these two combined measurements, the authors argue that 2 ps is

Figure 3. Crystal and magnetic structure of Sr$_2$IrO$_4$. (A) Tetragonal unit cell with lattice parameters $a \approx 5.5$ Å and $c \approx 26$ Å. The blue, red, and purple circles represent Ir, O, and Sr atoms, respectively. (B) Canted antiferromagnetic structure of $J_{\text{eff}} = 1/2$ moments (arrows) within IrO$_2$ planes and their stacking pattern along the c axis. Adapted from [51]. Reprinted with permission from AAAS.

mapping the low-energy magnetic dynamics onto the variation of the optical properties at 1.4–1.7 eV.

These non-equilibrium results have two fundamental consequences. First, they show that the validity of the fully localized ($J_{\text{eff}}$) and quasi-delocalized (QMO) scenarios strongly depends on the energy scale considered: while the low-energy magnetic dynamics can be described within a picture of localized moments characterized by bonding-dependent (Kitaev) interactions, QMOs are the effective building blocks of the physics at binding energies larger than $\approx 1$ eV. Second, they demonstrate that the local demagnetization processes can be mapped into specific optical transitions in the near-infrared/visible energy range by exploiting the intertwining between the magnetic and orbital degrees of freedom (QMO). This finding provides a new tool for investigating and controlling the ultrafast magnetic dynamics and, consequently, for achieving a better understanding of the equilibrium properties of the system.

2.3. Square-lattice strontium iridate

In Sr$_2$IrO$_4$, the corner-sharing IrO$_6$ octahedra form IrO$_2$ planes perpendicular to the crystallographic $c$-axis, where the Ir ions are arranged in a square lattice (see figure 3). Because of a staggered in-layer rotation of the octahedra, the unit cell, which coincides with the magnetic unit cell, is formed by four IrO$_2$ layers [30, 51–53]. Similarly to Na$_2$IrO$_3$, 5 electrons occupy the $t_{2g}$ manifold induced by the octahedral crystal-field. Because of the simpler topology of the square lattice, which does not induce neither additional magnetic frustration nor privileged hopping paths, the localized $J_{\text{eff}}$ picture is solid
also the upper limit of the lifetime of electron–hole pairs, or
doubions, living in the upper and lower Hubbard bands [13].

The magnon dispersion measured by RIXS perfectly
agrees with the equilibrium excitation spectrum modeled via
the Heisenberg model [53]: the minimum (zero) resides at
\( Q = (\pi, \pi) \), the maximum (\( \sim 200 \) meV) at \( Q = (\pi, 0) \). Given
the extremely small inter-layer coupling, the ideally 3D
experimental dispersion essentially resembles the theoretical
two-dimensional (2D) one at equilibrium [53]. Despite the
collapse of the 3D magnetic order, magnons are observed in the
RIXS spectra at both \( Q \) points in the transient state after the
pump, with a dispersion practically identical to the
equilibrium one at \( Q = (\pi, 0) \) and slightly different at \( Q = (\pi, \pi) \).
These findings show that: (i) the 2D correlations retain their
Néel nature in the transient state up to 2 ps after the pump; (ii)
the melting of the 3D state is related to the destruction of the
inter-layer correlations. The differences at \( Q = (\pi, \pi) \), which
recovers only on a much longer time scale (100 to over 1000
ps), can suggest the difficulty of recovering low-energy
excitations with respect to high-energy ones (e.g. those at
\( \sim 200 \) meV and \( Q = (\pi, 0) \)). Moreover, the increase of the
low energy spectral intensity at \( Q = (\pi, \pi) \) and the related
depletion of the one at \( \sim 100 \) meV cannot be explained by
simple thermal heating, which would lead to a uniform
relative broadening, and the residual photo-excited carriers in
the transient state could be held responsible for them.

These results demonstrate that the photo-excitation of
carriers across the Mott gap can be used to create a non-
thermal magnetic state in which the equilibrium 3D magnetic
correlations have been melted (in less than \( \sim 0.3 \) ps), while
2D correlations transiently survive for a longer time (10–100
ps). The complete recovery of the 3D magnetic state requires
100–1000 ps (in agreement with the ratio \( J/J_s \)). The creation
of the artificial magnetic state with 2D correlations is crucially
connected to the presence of long-lived charge excitations in
the Hubbard bands. This finding opens the possibility of
developing selective charge-excitation protocols to transiently
control the magnetic state in strontium iridates.

2.4. Towards the ultrafast magnetic control in 5d materials

The two paradigmatic examples of the honeycomb-lattice
Na₂IrO₃ and the square-lattice Sr₂IrO₃ demonstrate that the
creation of non-thermal electronic populations can be
exploited to photoinduce transient magnetic states, which are
potentially tunable and reversible. The nature of these tran-
sient states crucially depends on the topology of the lattice, on
the strength and directionality of the short-range magnetic
interactions and on the lifetime and orbital character of the
charge excitations. Here we summarize the key concepts that
can be exploited for developing novel schemes for the
ultrafast manipulation of magnetic states in 5d TMOs:

- The interplay of SOC, correlations and topology of the
  lattice, typical of 5d TMOs and relativistic correlated
  materials in general, allows to map the local demagne-
  tization processes into specific optical transitions in the
  near-infrared/visible energy range. The other way
  around, the resonant photostimulation of high energy
  charge states with specific orbital components can be
  exploited to selectively trigger magnetic excitations.
- The competition between different magnetic configura-
  tions—e.g. zig-zag and stripy antiferromagnetic phases,
  typical of frustrated correlated magnets, can be exploited
  for achieving a controlled magnetic switching via the
  selective excitation of charge states coupled to magnetic
  correlations with different net magnetization in terms of
  spatial arrangement and polarization.

In the near future, we foresee that the use and develop-
ment of ultrafast techniques will become more and more
fundamental to understand how the magnetic dynamics of
correlated 5d materials can be functionalized and manipulated
by light. The combination of ultrafast photo-doping with the
chemical surface [58] doping will provide new opportunities
to discover additional emergent properties of scientific and
 technological interest.

3. Coherent electronics in few-atomic-layers
heterostructures

Controlling the electronic quantum coherence in solids at
ambient conditions is a long sought-after target in condensed
matter physics. Quantum pathways could be exploited to
coherently convert photons into charge excitations, thus
tremendously increasing the performances of optoelectronic,
spintronic and photovoltaic devices. The possibility of
quantum-coherently guiding and controlling electronic exci-
tations would provide the building block to develop robust
quantum systems that could be manipulated at ambient
conditions, with impact on quantum-information processes and
communication technologies [59]. Besides the technological
impact, the loss of quantum coherence in solids is usually the
primary relaxation mechanism and is mainly related to quazi-
elastic scattering processes. As a consequence, the direct
access to the decoherence timescales in materials is expected
to provide a new platform to investigate some of the most
fascinating and unexplored problems of condensed matter
physics, such as:

- The hierarchy of the interactions with the magnetic,
  orbital and lattice degrees of freedom in leading the
dephasing and the eventual thermalization of many-body
  excitations in TMOs and other correlated materials.
- The way quantum-coherent wavefunctions evolve into
  incoherent charge, spin and lattice excitations, whose
  propagation is regulated by incoherent transport laws.
- The possibility of manipulating the electronic properties
  of materials on the verge of correlation-driven phase
  transitions by creating suitable coherent superposition of
  quantum states that evolve faster than the decoherence
  processes.
- The conversion of optical excitations into electron–hole
  pairs, which can be collected along quantum-coherent
pathways for photon-harvesting applications in engineered heterostructures.

Unfortunately, the quantum nature of electronic excitations in solids at liquid nitrogen or ambient temperatures is usually washed out on the femtosecond timescale by the interaction with the incoherent fluctuations of the charge, phonon and spin backgrounds (thermal bath). The most common strategy to overcome this problem is to freeze the incoherent thermal bath by cooling down to extremely low temperatures (<2 K) and investigating, for example, the coherent effects on the steady-state transport of charges or optical excitons in semiconductor nano- or meso-structures [60].

An alternative approach consists in directly accessing and controlling the dephasing processes at high temperatures on their relevant timescales. However, the attempts to tune and exploit the electronic quantum coherence in correlated nanomaterials have so far been hindered by the lack of fundamental knowledge—both theoretical and experimental—of the mechanisms driving the ultrafast dephasing. In this section we will discuss and review the concepts and the most recent results that are expected to lay the foundation of this field.

### 3.1. The decoherence timescales in correlated materials

In solids, the simplest example of coherent transport is given by the Bloch oscillations. When electrons, described by Bloch wavefunctions, are free from any scattering process, they respond to a steady electric field $E$ in an oscillatory way, with period $T_B = 2\pi\hbar/aE$ ($a$ is the lattice constant, $e$ the electronic charge) [61]. Even though in bulk materials this period is much larger than the dephasing time, thus making oscillations hard to observe, the recent advances in the atomic-scale synthesis of oxide heterostructures [19] have opened very intriguing scenarios. For example, the polar nature of many TMO heterostructures, such as LaAlO$_3$/SrTiO$_3$ and LaVO$_3$/SrTiO$_3$, gives rise to intrinsic electric fields [62] corresponding to a potential slope of the order of 0.08 eV Å$^{-1}$. In these systems, the corresponding period of the Bloch oscillations is $T_B \sim 12$ fs, which is very close to both the expected dephasing time and the time necessary to eventually collect the charges across few atomic monolayers. This observation suggests the possibility of exploiting quantum-coherent pathways to enhance the conversion efficiency in suitable engineered few-monolayers systems, provided the excitations are collected faster than the time necessary to completely lose the initial quantum-coherence.

#### 3.1.1. Decoherence and the density matrix

In order to properly introduce the concept of dephasing of a generic pure quantum state $|\psi\rangle$, it is necessary to make use of the density matrix, $\hat{\rho}(t) = |\psi(t)\rangle \langle \psi(t)|$. For sake of simplicity, we limit the discussion to a two-level system, that accounts for the ground ($|\psi_0\rangle$) and excited ($|\psi_1\rangle$) states. Any form of quantum-coherent excitation prepares the system into a superposition of the ground and excited states: $|\psi\rangle = a_0(t)|\psi_0\rangle + a_1(t)|\psi_1\rangle$. Assuming that $a_0(t) = c_0(t) \exp(-i\omega_0 t)$, where $c_0(t)$ are slowly varying complex functions of time and $\omega_0 = E_0/h$ are the eigenfrequencies of the ground ($n = 0$) and excited ($n = e$) states, the matrix representation of $\hat{\rho}$ reads:

$$\hat{\rho}(t) = \begin{bmatrix} \rho_{00} & \rho_{0e} \\ \rho_{e0} & \rho_{ee} \end{bmatrix} = \begin{bmatrix} |c_0(t)|^2 & c_0(t)c_1(t)e^{-i\omega_0 t} \\ c_0(t)c_1(t)e^{i\omega_0 t} & |c_1(t)|^2 \end{bmatrix},$$

(1)

where $\omega_0 = (E_0 - E_e)/h$. In this form, the diagonal terms describe the time-dependent populations of the ground and excited states, while the off-diagonal ones define the coherences of the system, which can be related to the macroscopic polarization $P(t) = N/\sqrt{\hbar} (\rho_{0e} + \rho_{e0})$, via the atomic dipole moments $\mu_{0e} = \langle \psi_0 | \mu | \psi_e \rangle$ with density $N/V$. Importantly, the density matrix maintains exactly the same physical meaning in the case of statistical ensembles, where the matrix elements should be calculated as the averages over the population indexed by $s$: e.g. $\mu_{0e} = 1/N \sum_s \rho_{0e}^s$. Even though the microscopic treatment of the time-evolution of $\hat{\rho}$ strongly depends on the specific system considered and goes beyond the scope of the present work, the decoherence processes can be accounted for in a phenomenological way by introducing a decoherence timescale, $\tau_D$, that depends on the interaction with the environment and produces the exponential decay of the off-diagonal matrix elements:

$$\hat{\rho}(t) = \begin{bmatrix} |c_0(t)|^2 & e^{i\omega_0 t}c_0(t)c_1(t)e^{-i\omega_0 t}/\tau_D \\ e^{-i\omega_0 t}c_0(t)c_1(t)e^{i\omega_0 t}/\tau_D & |c_1(t)|^2 \end{bmatrix}$$

(2)

$\tau_D$ thus characterizes the evolution of a macroscopically quantum-coherent state into an incoherent statistical ensemble ($\rho_{0e}, \rho_{e0} \rightarrow 0$) and is determined by all the quasi-elastic primary relaxation processes that destroy the macroscopic coherence without altering the population of the levels. The precise knowledge of $\tau_D$ in solids represents the prerequisite for the design of experiments and theories aimed at measuring and describing the decoherence processes and the transport properties on the timescales shorter than those necessary to achieve the incoherent transport regime.

#### 3.1.2. Excitonic resonances in correlated materials

In order to observe coherent phenomena in solids, it is necessary to find well defined excitonic transitions, whose dephasing time can be accessed by ultrafast techniques. While the study of low-temperature excitons in semiconductors is a well established field [63], correlated materials and TMOs constitute an almost unexplored world, though very promising. Let us consider the antiferromagnetic Mott (or charge-transfer, CT) insulators, such as the copper oxides parent compounds. The lowest excitation is the CT of a localized Cu–3$d_{z^2}$ orbital to its neighboring O–2$p_{\alpha\beta}$ orbitals, with an energy cost $\Delta_{CT} \approx 1.5$–2 eV. In the optical conductivity, this process is revealed by a typical CT edge, which defines the onset of optical absorption by particle–hole excitations. However, the local CT excitation is a many-body process and can be dressed by structural deformations or rearrangements of the spin-background (lattice- or spin-polarons), or even form a bound state (Hubbard exciton...
(HE)), thus forming a local exciton which can hop in the lattice and in the ordered antiferromagnetic background. This physics is entirely contained in the ubiquitous structures that are observed at the CT edge of TMOs (see figure 4) and whose nature is still subject of intense debate [64–68]. From the linewidth of these resonances, which ranges between 0.2 and 0.4 eV, it is possible to estimate the upper bound of the excitonic lifetimes (1.5–3 fs). Although very short, these values are close to the current limit of ultrafast technologies that pushed the temporal resolution well below 10 fs [69–71]. However, the total linewidths in TMOs are usually severely affected by the inhomogeneous broadening related to the presence of defects or intrinsic electronic/lattice inhomogeneities typical of correlated materials [72].

The real dephasing time, which corresponds to the inverse of the homogenous contribution to the total linewidth, should be evaluated either by starting from microscopic theories or by developing suitable multi-dimensional ultrafast techniques, as discussed in section 3.4. We stress that similar physics is present in many correlated TMOs, such as vanadium oxides (LaVO₃, V₂O₅) and Ir-based relativistic Mott insulators (Sr₂IrO₄, Na₃IrO₃). The possibility of investigating the decoherence of excitonic resonances at the edge of the Mott (CT) gap is thus very general to many classes of TMOs that can be exploited for applications.

3.1.3. Time-domain models. In conventional materials, the decoherence of excitonic resonances is mainly driven by the direct exciton-exciton interactions, which can be limited by properly tuning the intensity of the light excitation, and by the scattering with bosonic fluctuations, such as the phonons, that is effective on the timescale \( h/\Omega_B \), \( \Omega_B \) being the typical boson frequency. When considering copper oxides, the strong on-site Coulomb repulsion \( U \) between two electrons occupying the same Cu–3d<sub>z</sub>–O<sub>2</sub>–3d<sub>z</sub> orbital introduces a new dynamics characterized by the energy scale \( J = 2\hbar^2/U \approx 120 \text{ meV} \), where \( \hbar \) is the nearest-neighbor hopping. The antiferromagnetic coupling \( J \) between neighboring sites arises due to the virtual hopping of holes into already occupied sites through Anderson’s superexchange mechanism. While the phonon cut-off in cuprates is about 70 meV, corresponding to a timescales of \( \sim 10 \text{ fs} \), the spectrum of the spin fluctuations extends up to \( 2J \sim 250 \text{ meV} \) \( (\hbar/2J \approx 3 \text{ fs}) \) and it is believed to constitute the primary scattering channel for the charge excitations photoinduced in copper oxides by the ultrashort pump pulses [1].

In the less favorable scenario, the quantum coherence of the excitonic resonances at the gap edge in Mott and CT insulators is lost at each hopping process. If we assume a typical hopping integral of 0.1–0.3 eV for TMOs, we can estimate a decoherence time in the order of 2–6 fs \( (\tau_B = \hbar/\hbar, \ h = 658 \text{ meV fs}) \). However, there are many effects that can concurred to increase this value: (i) the formation of dressed coherent quasiparticles is expected to increase the effective mass, thus reducing their mobility within the lattice [75, 76]; (ii) in multi-band systems, the possibility of hopping on the oxygen sub-lattice strongly reduces the effect of spin-fluctuations on the electron dynamics [77].
The ultrafast relaxation of HEs in Mott insulators has been directly tackled by studying a simplified version of the single-band Hubbard model. A generalized t–J model for insulators is obtained by performing a canonical transformation of the Hubbard model that, at the lowest order in t/U, decouples sectors with different numbers of HEs, thus accounting for the recombination of HEs [78, 79]. Within this model, the decay dynamics is given by a two-step process: (i) the formation of s-type HEs that are trapped at the bottom of the Mott gap; (ii) the decay of the bound holon-doublon exciton via multiamagnon emission, which is rather effective as a consequence of the strong charge-spin coupling in 2D systems. Using realistic values of J and \( t_h \) for cuprates, the estimated lifetime of HEs ranges from few holes to hundreds femtoseconds [78]. As a further step in reproducing the ultrafast dynamics in correlated insulators, the electron–phonon interaction can be accounted for by the Holstein model that includes the coupling with a dispersionless phonon mode. The relaxation in the full Hubbard–Holstein model driven out of equilibrium by an ultrashort light pulse has been recently performed on eight lattice sites [80]. At non-zero electron–phonon interaction, signature of the coherent evolution of the charge, spin and phonon populations are found to persist up to hundreds of femtoseconds.

The problem of the lifetime of photo-excited charge carriers in doped materials is even more difficult. At non-zero doping, strongly renormalized quasiparticles states at the Fermi level coexist with incoherent excitations at the energy scale of \( \Delta_{CT} \). The complete treatment of the problem requires solving the full Hubbard model out of equilibrium, which goes beyond the present capabilities. However, a suitable approximations is to study the dynamics of a single hole within the t–J model. The photoexcitation process is accounted for by suddenly raising the kinetic energy of the hole and letting it evolve in the spin-lattice background [74, 81–83] (see figure 4(b)). In general, the scattering with magnetic fluctuations is found to be the fastest relaxation process. The reason of the efficiency of the charge-spin scattering is that almost any hopping process leads to the perturbation of the antiferromagnetic spin background. In a square lattice, the lifetime of excited hopping time [74, 83]:

\[
\tau_D = \left( \frac{4t}{\Delta_{CT}} \right)^2 / 3.
\]

When considering the typical values of \( J \approx 120 \) meV and \( t_h \approx 360 \) meV for copper oxides, a relaxation time \( \tau_D \approx 4 \) fs is estimated.

This estimation of the timescale for the coupling with antiferromagnetic spin fluctuations in copper oxides has been also confirmed by the solution of the full Hubbard model with a non-equilibrium version of the dynamical cluster approximation [84]. In the Mott insulators, the relaxation rate of the high-energy photo-excited charge carriers is found to be \( \approx 10–20 \) fs. The relaxation process becomes more complex at finite doping, where the direct charge–charge interactions open additional scattering channels that lead to a faster relaxation of the photo-excited holes (electrons).

### 3.1.4. Time-domain experiments

The experimental study of the decoherence processes in correlated materials has been mainly hindered by the lack of suitable techniques to directly access the off-diagonal elements of \( \hat{\rho}(t) \), with a temporal resolution of the order of \( \approx 10 \) fs. Nonetheless, the use of broadband sub-10 fs pulses recently allowed to perform time-resolved spectroscopic measurements that provided important insights.

The decoherence of the HEs has been observed in the organic salt bis(ethylendenedithio)tetrathiafulvalene-difluorotraycanodimethane (ET-F2TCNQ) by performing broadband pump–probe experiments with \( \approx 9 \) fs pulses with a spectrum covering the 0.55–1 eV energy range. After the photoexcitation, the quantum interference between the HEs and ionized holon-doublon pairs, that are created when the holons and doublons move far apart in the 1D lattice, has been observed under the form of an oscillation at 25 THz (period of \( \approx 40 \) fs) [85]. These results confirm that, in Mott (CT) insulators, the photoexcited HEs maintain the initial quantum coherence on a timescale of several tens of femtoseconds.

In doped Mott (CT) insulators, such as doped cuprates, the timescale related to the coupling with short-range spin fluctuations has been recently inferred by broadband pump–probe measurements in different families of hole-doped copper oxides [74]. The temporal resolution \( < 10 \) fs, that is of the order of the timescale \( (1/2J) \) of the coupling with magnetic fluctuations, disclosed the possibility of directly observing the energy exchange between the initially photoexcited charge carriers and the bosonic bath, constituted by the phonons and magnetic fluctuations. The measured timescale, \( \tau_D \approx 16 \) fs, has been benchmarked against numerical calculations based on the \( t_h/J \) model, in which the relaxation of the photo-excited charges is achieved via inelastic scattering with short-range antiferromagnetic excitations [74].

#### 3.2. The transport problem in oxide heterostructures

As discussed in the previous section, the typical decoherence timescale for electron–hole excitations at ambient temperature in TMOs can range between 4 fs and several tens of femtoseconds, depending on the specific characteristics (charge carrier density, hopping \( t_h \)) of the system considered. The recent advances in ultrafast science made these timescales directly achievable, thus providing the platform for the study of coherent-transport phenomena in correlated materials.

From the technological standpoint, the possibility of tailoring the coherent dynamics on ultrafast timescales would have a dramatic impact on the working principle of few-atomic-layers oxide-based devices. To properly make the case, we start from a paradigmatic example, i.e. LaVO\(_3\)/SrTiO\(_3\) (LVO/STO) heterostructures (see figure 5), that have been recently suggested for photovoltaic applications [62]. At 300 K, LVO is an orthorhombic paramagnetic Mott insulator (direct gap of \( \approx 1.1 \) eV) with 2 electrons in the crystal-field split 3d–t\(_{2g}\) orbitals. The fundamental optical excitation is the transition from LHB to UHB, which corresponds to the transfer of an electron from one V atom to its neighboring V-site. At 140 K, LVO transforms into a monoclinic structure with an antiferromagnetic C-type order (\( c \)-axis ferromagnetic...
Figure 5. (a) Layer-by-layer density of states (DOS) of the LaVO$_3$/SrTiO$_3$ heterostructure as calculated by DFT+$U$ [62]. The blue and red colors indicate the DOS for each of the two inequivalent (opposite spin) V sites per layer. (b) Generation and collection of optical (e)–(h) excitations in the LaVO$_3$/SrTiO$_3$ heterostructure. Reprinted figure with permission from [62]. Copyright 2013 by the American Physical Society.

The working principle of the LVO–SrTiO$_3$ heterostructure provides a natural way of collecting the charges, the quasi elastic scattering processes, which dephase the initial wavefunction without changing the population, are expected to play a crucial role. While a large scattering rate would be detrimental for the collection of the charges, the absence of any scattering process would lead to Bloch oscillations without efficiently establishing any photocurrent. This naive expectation has been recently demonstrated by non-equilibrium dynamical mean-field theory (DMFT) simulation of the transport properties of a multilayer Mott insulator in which doublons and holes are created by photoexcitation [87].

The natural question emerging from these considerations is whether the timescale necessary to collect the charges is compatible with the emergence of transport phenomena along quantum walks, which can be faster and more efficient than classical ones [88, 89]. Considering the hopping terms estimated by local density approximation calculations combined with DMFT [86], we note that the most efficient channel for collecting charges along the c-axis (perpendicular to the (VO$_2$)$_2$ planes) in the orthorhombic phase is mainly related to the hopping between adjacent 3d$_{xy}$ orbitals, with a hopping integral $t_{3d_{xy}} \approx 190$ meV. In the low-temperature monoclinic phase ($T < 140$ K), the most favorable hopping is given by stacking of antiferromagnetic $ab$ layers. Interestingly, the orthorhombic LVO is one of the few Mott insulators which exhibits large quantum fluctuations at room temperature [86], in the sense that the orbital occupation of the $t_{2g}$ orbitals is strongly fluctuating with a frequency range which is determined by quantum effects instead of $k_B T$. However, these strong incoherent orbital fluctuations are almost completely suppressed in the monoclinic 140 K phase, when they turn into a phase-coherent condensate (orbital ordering) in which the orbital occupation assumes a well defined (phase stable) pattern in space and time. The exploitation of the LVO properties is based on the possibility of creating heterostructures in which the chemical/structural composition of each layer is controlled at the atomic scale [19]. Let us consider the multilayer structure constituted by 4 LVO unit cells interfaced to SrTiO$_3$, as suggested in [62]. DFT calculations (see figure 5) show the layer-by-layer density DOSs of the V–3d$_{xy}$ states. Interestingly, the shift of the bands between neighboring layers indicates the formation of a potential gradient between the (LaO)$^+$–(VO$_2$)$^-$ planes, that is estimated as high as 0.08 eV Å$^{-1}$. Furthermore, the intrinsic presence of conducting states (of $d_{xy}$ character) at the LVO/SrTiO$_3$ interfaces provides a natural way of collecting the electron–hole excitations generated within the LVO layers. The working principle of the LVO/SrTiO$_3$ heterostructure can be described by the following steps: (i) the absorption of an above-gap photon creates a many-body excitation $|\psi_i(\mathbf{r})\rangle$ that consists in a local doublon (doubly occupied V–3d$_{xy}$ orbital) and holon (unoccupied V–3d$_{xy}$ orbital) pair; (ii) the charged doublons and holons, subject to the intrinsic $E_{\text{int}}$, hop across the few LVO atomic layers and are collected by the two opposite interface conductive layers, thus generating a photocurrent.
the overlap between $3d_{xz}$ and $3d_{yz}$ orbitals with an hopping integral $t_{xz, yz} \simeq 150$ meV. Assuming that the photo-exciton is created in one of the internal LVO layers, the time necessary to collect the charges ($\tau_{\text{coll}}$) is given at the most by two times the inverse hopping integral, i.e. $\tau_{\text{coll}} = 6-8$ fs. This value is very close to the $\tau_D$ estimated in section 3.1, thus suggesting that the quantum laws may greatly affect the transport properties of nanoscaled TMO devices, such as LVO/STO heterostructures.

3.3. TMOs heterostructures: taking inspiration from nature

Unraveling the impact of quantum coherent effects on the macroscopic electronic properties of heterostructures at ambient conditions is one of the challenges of solid state physics and materials science. The local many-body charge excitations spread throughout and across the metal–oxygen planes until they are collected by the interface conductive states. During this process, the quantum excitations lose their coherence via the coupling with the fluctuating environment constituted by the spin, charge and lattice background. In this frame, the final goal would be the development of strategies to tune the transport regime from coherent to incoherent and exploit quantum effects to enhance the transport or create quantum-protected states that could be exploited for quantum technology applications. Many of the fundamental ideas to treat this problem have been developed in the context of quantum transport in bio-systems at physiological temperatures [90]. In this section we will briefly review the concepts that have been developed in the recent years to describe the quantum effects in bio-systems and we will discuss how these ideas could be exploited to achieve the full quantum-coherent control of transport in heterostructures and nanoscaled materials.

In the simplest quantum-transport models, complex interacting systems are treated as quantum networks of two-level systems (sites), mutually coupled via hopping amplitude and interacting with both a thermal bath and a continuum of states (the collector). The incoherent hopping motion of the charge excitation corresponds to the case in which $\tau_D$ is shorter than the hopping time and only the population of the multi-levels, i.e., the diagonal terms of the density matrix, contributes to the transport. Quantum-coherent effects can emerge, for example, when $\tau_D$ is much larger than the typical hopping time and, as a consequence, the off-diagonal terms of the density matrix can give rise to novel effects mainly related to the interference of the wavefunctions describing each site. Considering the case of photo-stimulated excitons propagating in a quantum network coupled to the environment, many concepts have been introduced to describe the way local excitations are generated, transported and collected in photosynthetic light harvesting complexes [90]. The study of coherent effects in bio-systems at physiological temperatures and the role of the coupling with the environment was largely boosted by the discovery that quantum coherence is preserved in Fenna–Matthews–Olson (FMO) bacteriochlorophyll complexes [91] and in marine algae [92] on timescales of the order of hundreds femtoseconds. As a consequence, the first stage of the energy transfer within the light harvesting complexes can be dominated by wave-like phenomena, that possibly enhance the collection efficiency by allowing the simultaneous probing of large areas of phase space to find the most efficient path.

In quantum-coherent models, the transport efficiency is strongly affected by the interaction with different environments, such as the coupling with the collector and the thermal bath. In general, the problem is treated by suitable master equations [89] that describe the time evolution of both the diagonal ($\rho_{ii}$) and off-diagonal ($\rho_{ij}$, with $i \neq j$) terms of the density matrix, where $i(j)$ labels the excited site. One of the simplest master equations which can be used to model the effects of different environments on excitonic transport is the Haken-Strobl master equation [93]:

$$\frac{\partial}{\partial t} \rho_{ij}(t) = -\frac{i}{\hbar} [H_{\text{eff}} \rho - \rho H_{\text{eff}}^\dagger]_{ij} - \frac{1}{\tau_D} \rho_{ij},$$

where $H_{\text{eff}}$ is an effective non-Hermitian Hamiltonian which describes the interaction with different dissipative environments, such as the collector where the excitation can be trapped. The effective non-Hermitian Hamiltonian can be written as $H_{\text{eff}} = H_0 + i\gamma_\text{ct}Q$. Here $H_0$ is the Hermitian Hamiltonian describing the closed system (which is the network of coupled two-level sites) and also includes the static (time-independent) disorder induced by the environment; $Q$ describes the dissipation in the continuum channel (collector or electromagnetic field) with strength $\gamma_\text{ct}$. The imaginary part ($\Gamma$) of the $r$th complex eigenvalue of $H_{\text{eff}}$ represents the decay width of the correspondent eigenstate. The quantum dephasing (the decay of the off-diagonal matrix elements) is accounted for by the second right term of equation (3) and represents the effect of the external bath which the network is coupled to. Physically, the dephasing is induced by time-dependent fluctuations of the site energies with amplitude proportional to $1/\tau_D$.

As the above simple model shows, quantum transport is affected by different parameters: the dephasing rate, the strength of static disorder and the strength of the coupling to the collector. Finding the optimal parameters is a difficult task since their interplay is highly non-trivial. Here we summarize the main concepts that emerged form the study of quantum transport in bio-molecules and that are expected to be of great relevance for the transport in heterostructures:

- **Superradiance** occurs when the energy levels of a quantum system are coherently coupled with a common decay channel. In short, it implies the existence of states with a cooperatively enhanced decay rate and it has been shown to have important effects on transport efficiency in open systems: for example, maximal efficiency in energy transport in the FMO system is achieved in the vicinity of the superradiance transition (ST). Superradiance, is usually reached only above a critical coupling strength with the continuum (in the overlapping resonance regime): $\Gamma/\Delta \geq 1$ where $\Gamma = \langle \Gamma \rangle$ is the average decay width and $\Delta$ is the mean level spacing of the closed system. Since the ST is due to the coherent constructive
Energy mismatches in disordered materials lead to directionality mechanism that enhances the transport efficiency for it counteracts the decoherence-driven localization. The coupling to a common decay channel, such as the collector, has been also found to promote an open-assisted energy transfer in quantum networks and light-harvesting complexes [93, 94].

The extension of these concepts to solid state systems would pave the way to the observation and exploitation of quantum-coherent phenomena in materials for technological applications. An interesting example of coherent control has been provided by the theoretical investigation of the interaction of two consecutive coherent light pulses with a one-dimensional Mott insulator [101]. The formation of bound states of charge carriers, i.e., holon-doublon excitons, is included in the model by considering an extended Hubbard model in which, besides the on-site Coulomb repulsion $U$, nearest neighbor electron–electron interactions (V) are also included. The main result is that, when the decoherence time of optically active excitations is of the order of the pulse length, the many-body system can be mapped onto an effective two-level system, and its dynamics can be rationalized in terms of a simple Rabi model [101]. As a consequence, the final energy after the interaction with the second pulse can be either enhanced or quenched depending on the time delay between the first and second pulses, as shown in figure 6(b). This effect, shown in figure 6, is the counterpart of the quantum-coherent time evolution of a two-level system interacting with an electro-magnetic field, which is described by the optical Bloch equations [102]. This result suggests the possibility of coherently controlling the electronic state of a correlated material by suitable excitation with light pulses as short as $\tau_\text{D}$.

TMOs provide the ideal platform to extend the concepts of superradiance, directionality, localization and noise-
assisted transport that have been introduced for addressing the transport properties of natural light-harvesting systems [100]. The starting point is that the energy of the ubiquitous CT transition usually matches most of the visible spectrum (1–3 eV) and can be thus used to directly probe and control the fundamental electronic decoherence processes on the sub-10 fs timescale [69]. Furthermore, correlated materials are characterized by the unique property that the dynamics of the quasiparticles at the Fermi level and of the high-energy excitations involving the Hubbard band (the CT transition in copper oxides) are strongly intertwined [73]. As a consequence, the decoherence dynamics of holon-doublon excitons is expected to be strongly affected by the onset of ordered states (either local or long-ranged), such as magnetic or charge-ordered phases. Therefore, an interesting and completely unexplored mechanism that could help in tailoring the ultrafast electronic decoherence in solids is the possibility of tuning the fluctuations of the thermal bath in the vicinity of a phase transition. In this regime the relevant incoherent fluctuations (spin, phonons, charges) transform into a phase-coherent condensate, such as magnetic, charge- and orbitally ordered states or high-temperature superconducting condensates. Besides the example of LVO, in which the quantum orbital fluctuations in the high-temperature orthorhombic phase condense into an orbitally ordered states at 140 K (see section 3.2), another paradigmatic example of the potentiality of TMOs is given by the Nd$_{2-x}$Ce$_x$CuO$_4$ family of copper oxides. When tuning the electron doping concentration ($x$), it is possible to move away from the antiferromagnetic insulating phase and explore interesting states such as: (i) bad metallic phase with long-range antiferromagnetic correlations [103]; (ii) insulating or bad metallic states with strong short-range antiferromagnetic fluctuations [103]; (iii) short-range (coherence length $\approx$ 2 nm) and fluctuating charge order [104], in which the electronic charges spontaneously tend to break the translational symmetry and form phase-ordered patterns; (iv) unconventional superconductivity at high temperatures, in which the condensation of the charge carriers into a phase coherent condensate induces the opening of a $\approx$ 40 meV gap with $d$-wave symmetry.

Wrapping up the concepts discussed in this section, we argue that TMOs provide the unique possibility of exploiting the physics of correlated materials to tune the decoherence processes in atomically thin heterostructures and devices. The exploitation of noise-assisted quantum-coherent phenomena such as super-transfer [105] and superradiant transitions [93] to increase the performances and efficiency of TMO-based devices would dramatically impact the current technology. However, some fundamental steps are still required to transform these opportunities into a real technological breakthrough:

- **Tuning the decoherence.** Coherent transport phenomena emerge in a limited region of the phase-space of the parameters $\tau_D$ and $\gamma_Q$. In order to control and tune quantum-coherent processes, it is necessary to develop protocols to span the entire phase space and continuously move from the incoherent to the coherent regime. The most promising strategy is to tune $\tau_D$ by exploiting the modification of the electronic coupling with the bosonic bath in the vicinity of a phase transition. In this perspective, TMOs provide a very interesting playground since they are always on the verge of multiple phase transitions as a consequence of the local correlations of the metal $d$ electrons. By finely tuning the temperature and doping, it is possible to turn strongly incoherent fluctuations of the charge, spin, lattice and orbital degrees of freedom into long-range ordered (and phase-coherent) states, such as magnetic phases, charge/orbital ordering and superconductivity, at temperatures ranging from 20 to 300 K.

- **Designing effective collectors.** One of the crucial parameters for the emergence of superradiant solutions in quantum networks is the coupling to the collectors, $\gamma_Q$. The state-of-the-art technologies for the synthesis of oxide heterostructures [19] enabled the layer-by-layer control of the chemical/physical properties of nanoscaled devices. For example, the spontaneous emergence of conductive layers at the interface of insulating oxides, such as LaAlO$_3$/SrTi$_3$ and LaVO$_3$/SrTi$_3$, provide a simple scheme for the design of 2D collectors that reside few atomic layers apart [106] and are characterized by high carrier mobility. Furthermore, the density of the interface conductive layers can be changed by controlling their mutual distance and their common temperature [106, 107], thus providing additional degrees of freedom for tuning the coupling with the collectors.

- **Tuning the hopping.** The hopping amplitude, $t_h$, has a twofold role in controlling the quantum-transport properties of few atomic-layers devices. On one hand, $t_h$ determines the fundamental timescale ($\hbar/t_h$) of the charge-hopping process between two adjacent layers; on the other hand, it controls the mean level spacing ($\Delta$) of the energy levels of the closed quantum network with respect to the energy of the non-interacting sites. Interestingly, $t_h$ strongly depends on the lattice structure of the material and on the orbital occupation of the TM $d$-bands [86], which can be controlled either statically, e.g. by tuning the temperature or the chemical composition, or dynamically, e.g. by resonant photoexcitation of interband transition or lattice modes [108].

- **Disorder.** The local disorder is expected to strongly impact the transport efficiency in the coherent regime, up to the point of driving the complete charge localization [97]. The disorder can be easily controlled by exploiting the intrinsic presence of defects in TMOs or by creating suitably designed disordered structures that could be controlled at the atomic scale.

- **Developing predictive models.** A key step is the development of predictive models for the description of coherent photodissociation and charge-collection processes in correlated oxides. The spreading of photoexcited carriers in Mott insulating heterostructures has been recently studied by means of DMFT solutions of the inhomogeneous Hubbard model [87]. While DMFT fully treats the local correlations of the TM $d$-orbitals and the
quantum nature of the many-body wavefunctions, only short-range spin fluctuations can be included as source of dissipative coupling with the environment. The coupling with phonons (restricted with specific dispersionless optical modes) could be included by means of the Hubbard–Holstein model. Considering the relevance of the coupling to the thermal bath and given the necessity of simulating in a simple way the spectral modifications of the noise, e.g. the transformation from an incoherent fluctuating bath to a phase-locked coherent state in the vicinity of charge and orbitally ordering phase transitions, the development of effective models based on appropriate master equations that can describe both coherent and incoherent hopping [89] is expected to boost the research in this field. The modeling of quantum-coherent processes in oxide heterostructures will guide the optimization of the experimental conditions necessary to observe and study coherent phenomena and will lead to the exploitation of these effects to improve the efficiency of transport in nanoengineered devices.

3.4. Multi-dimensional spectroscopies to access quantum decoherence

The development of strategies to exploit and control quantum coherent effects at the nanoscale crucially depends on the knowledge of the fundamental processes that regulate the dephasing of the electronic wavefunctions. Unfortunately, any attempt to investigate the electronic dephasing in solids at high-temperatures has been hindered so far by the difficulties in directly measuring the fundamental dephasing time of photoexcitations. For example, the linewidths measured by conventional optical spectroscopy are strongly affected by inhomogeneous broadening, which reflects the statistical distribution of impurities. This effect is particularly severe in TMOs, in which the strong correlations lead to intrinsic electronic and structural inhomogeneities. On the other hand, time-domain optical spectroscopies with ultrafast resolution emerged as a well-established tool to investigate the dynamics of correlated oxides [1]. Unfortunately, state-of-the-art ultrafast spectroscopies simply probe the population of a specific transition and remain blind to the fundamental decoherence processes. As a consequence, the relevant mechanisms that lead to the ultrafast loss of quantum coherence of charge excitons in metal oxides and the interplay between their dephasing and the onset of long-range ordered phases are still a major unexplored field.

In order to access the fundamental decoherence (or dephasing) processes described in the previous sections, it is mandatory to develop a technique with the following features:

- a time resolution as short as the typical decoherence timescale (few femtoseconds)
- capability of disentangling the real polarization dephasing from the population decay and from inhomogeneous effects.

One of the most promising approaches that could fulfill these requirements is the multi-dimensional spectroscopy [63, 109], which was developed over the past two decades in physical chemistry and atomic physics and is the optical analog of NMR used to study the decoherence of atomic wavefunctions and the energy transfer between vibrating molecules.

In particular, 2D spectroscopy directly accesses $\rho_{00}$, being based on the coherent interaction of three light pulses mediated by the third-order susceptibility, $\chi^{(3)}$, of the material [63, 109]. In the simplest picture (see figure 7(a)), the first pulse creates a macroscopic polarization, leaving the system in the coherent superposition of $|\psi_0\rangle$ and $|\psi_2\rangle$. The polarization oscillates in time with frequency $\omega_{\text{ph}}$ and decays on the dephasing timescale $\tau_\text{D}$. The second pulse, at time $t_2$, converts the macroscopic polarization into a population in the excited state, which does not oscillate but is reminiscent of the initial phase of the polarization. The third pulse, at time $t_3$ converts back to a coherent polarized state that radiates the measured signal field at time $t_3$. The 2D spectrum (see figure 7(b)) is generated, for each fixed $t_3$, by scanning $t_1$ and $t_2$ and taking the Fourier transform. 2D spectroscopy is considered the ultimate nonlinear technique [110], since it contains all the information that can be retrieved by 0D (conventional optics) and 1D spectroscopies, such as single- and multi-color pump–probe and multi-pulse techniques without the probe-frequency resolution [111–113]. On the other hand, 2D spectroscopy also contains fundamental information that is absent in 0D and 1D, such as:

- the possibility of determining whether two resonances are coupled or uncoupled [109]
- the capability of discriminating between homogeneous and inhomogeneous linewidths [109]
- the possibility of reconstructing the exciton migration and the charge-separation process [114].

This technique already showed that quantum phase-coherence is preserved in biological systems immersed in room-temperature baths [90–92] and unveiled many-body excitonic effects in semiconductors at low temperature (10 K) [115]. The possibility of extending 2D spectroscopy in the x-rays and in the THz frequency domain is expected to open new routes for the coherent spectroscopy of spins, valence electrons, and and core electronic excitations.

So far, the use of 2D spectroscopy for the study of solid state systems has been mainly hindered by the limited temporal resolution of most setups ($\approx$100 fs) and by the low repetition rate (1 kHz) that forces the experiments to be performed at very high fluences and on semitransparent samples. However, the recent dramatic advances in fiber laser technology [71, 116] made available high-repetition rate sources (up to 2 MHz) with enough energy per pulse for producing and amplifying supercontinuum white-light. The use of suitably designed non-collinear optical parametric amplifiers allows to produce ultrashort broadband pulses with tunable frequency and repetition rate and whose frequency content can support pulses as short as 6 fs [71, 116]. To show the advantages of 2D spectroscopy with respect to broadband pump–probe techniques [1], we simulated the absorptive
2D spectra (see figure 7(b)) expected for the typical CT excitations in correlated oxides, taking into account the expected temporal resolution of the experiment (6 fs). Assuming a total linewidth of 400 meV (see figure 4 for the actual optical conductivity of specific materials), the inhomogeneously (bottom panel of figure 7(b)) and homogeneously (top panel of figure 7(b)) broadened cases are clearly disentangled in the 2D spectra. In contrast, any 1D (or 0D) optical spectroscopy would only access the integral with respect to $\omega_1$ of the 2D spectrum and would not be able to discriminate between the two cases.

In light of the concepts presented in this section, we foresee that the achievement of a temporal resolution of $\approx 6$ fs, which is of the order of the decoherence timescale in correlated oxides, in high-repetition rate 2D experiments would unlock the study and, possibly, the control of the quantum-coherent dynamics in oxide heterostructures. The possibility of exploiting quantum-coherent processes at ambient temperatures would stimulate the design of oxide heterostructures and nano-materials that preserve the quantum-coherence of the photo-stimulation and collect the photo-generated charges along quantum walks. The success in coherently converting photons into charge excitations in oxide-base devices would provide the building block to develop robust quantum systems that can be manipulated at ambient conditions, for future use in large-scale quantum-information processes and communication technologies [59]. These ideas and techniques could be naturally applied to a broad variety of functional oxides (e.g. manganites, vanadates, nickelates, iridates and iron oxides) that exhibit optically driven insulator-to-metal transitions, multiferroicity, magnetic superconductivity and to low dimensional solids (e.g. graphene and metal dichalcogenides).

4. Wave-like temperature propagation

After an impulsive excitation, the excess energy initially stored into the non-thermal electronic distribution is eventually shared among the fermionic and bosonic (e.g. phonons, magnetic fluctuations) degrees of freedom. On timescales longer than the time necessary for the internal thermalization, it is possible to define an effective temperature, larger than the initial one, that labels the thermodynamic distributions. However, when the typical dimensions of the system are scaled to the nanosize, the initial excitation can spread within the material faster than the internal thermalization time, thus leading to an unconventional description of the heat propagation process [117, 118]. Although the development of a microscopic model of this phenomenon is one of the challenges of nano-thermodynamics (with possible impact on the physics of granular media and liquid helium) [117], here we will treat the problem empirically by introducing a delay between the onsets of the heat flux, $q$, and of the temperature gradient, $\nabla T$. For sake of clarity we will briefly review the steps necessary to obtain the generalized heat propagation equation that can be applied to tackle the thermal problem at the nanoscale.
4.1. Generalized equation for the temperature field

In general, the balance of the energy exchanges is rationalized through a local conservation of energy equation:

\[ C \frac{\partial T}{\partial t}(x, t) = -\nabla \cdot q(x, t) + S(x, t), \]  

(4)

where \( C \) is the volumetric heat capacity and \( S(x, t) \) is the volumetric heat source [119] externally provided. The classical Fourier’s law is obtained by assuming a direct proportionality, at time \( t \), between the heat flux and the temperature gradient, i.e., \( q(x, t) = -\kappa_T \nabla T(x, t), \) \( \kappa_T \) being the thermal conductivity. While Fourier’s law is a good approximation for describing slow phenomena, it implicitly assumes that the onset of the heat flux and of the temperature gradient are simultaneous, which implies an infinite speed of heat propagation [119]. When considering fast timescales and small length-scales, two different scenarios can be analyzed:

(i) After the instantaneous establishment of the temperature gradient, a non-zero time, \( \tau_q \), is necessary to generate the heat flux. This delay is related to the microscopic interactions that lead to a very fast local thermalization, while the heat flux is delayed by specific dynamical constraints. A typical example is given by strongly anisotropic materials, such as iridium or copper oxides, in which the in-plane thermalization is driven very quickly by the coupling with spin fluctuations and phonons, while heat transport perpendicular to the TMO planes is strongly quenched by the small interlayer coupling. In this case, the constitutive equation relating the heat flux and the thermal gradient is modified into the Cattaneo–Vernotte model [119, 120]:

\[ q(x, t + \tau_q) = -\kappa_T \nabla T(x, t). \]

(ii) In the opposite limit, a heat flux is instantaneously established causing a temperature gradient at the delayed time \( \tau_f \). This condition, represented by the relation \( q(x, t) = -\kappa_T \nabla T(x, t + \tau_f) \), is attained, for example, when a fast ballistic propagation of the charge carriers anticipates the local thermalization of the system.

By combining the two previous limits into a single relation, it is possible to introduce the dual-phase-lag model [119], that describes the general constitutive relation between the heat flux and the temperature gradient:

\[ q(x, t) = -\kappa_T \nabla T(x, t + \tau_f) \]

(5)

By substituting the first order term of the Taylor series in the time variable of equation (5) into the energy conservation law at time \( t \) (equation (4)) and assuming \( S(x, t) = 0 \), it is possible to obtain the generalized partial differential equation for the temperature field:

\[
\left( \frac{\tau_f}{\alpha} \right) \frac{\partial^2 T}{\partial t^2} + \nabla^2 T(x, t) + \frac{1}{\alpha} \frac{\partial T}{\partial t} - \tau_T \frac{\partial \nabla^2 T}{\partial t} = 0,
\]

(6)

where \( \alpha = \kappa_T/C \) is the thermal diffusivity. Interestingly, equation (6) recalls a wave equation in which \( \sqrt{\alpha/\tau_f} \) is the speed of propagation and \( 1/\sqrt{\alpha/\tau_f} \) represents the diffusion length. The damping of the temperature wave is provided by a diffusive term and a third-derivative one. Equation (6) reduces to the conventional diffusion equation in the limit \( \tau_f, \tau_T \to 0 \), the latter implying an infinite speed of heat propagation. From equation (6) it is possible to extract the complex dispersion relation of the system, linking the wavevector \( k = |k| \) to the frequencies \( (\omega) \) of the propagating temperature waves:

\[ k^2(1 + i\omega\tau_T) = \frac{\tau_f}{\alpha} \omega^2 \left( 1 - \frac{i}{\omega\tau_f} \right). \]

(7)

4.2. Wave-like solutions

Oscillating solutions of equation (6) can be sought under the assumption that \( k \) and \( \omega \) entering in equation (7) are complex quantities. Having in mind the experimental configuration of ultrafast experiments, in which the laser impinges on one of the sides of the sample and acts as an initial volumetric heat source \( S(x, t) = 0 \), we are interested in studying how the given initial temperature profile evolves in time. As a consequence, we assume a real wavevector, while the frequency is given by the complex quantity \( \tilde{\omega} = \omega_I + i\omega_I \), where \( |\omega_I| = 2\pi/\tau_{osc} \) is the inverse of the oscillation period and \( \omega_2 = 1/\tau_{damp} \) is the inverse of the damping time. The onset of a wave-like regime is governed by the \( Q \)-factor \( Q = |\omega_I|/\omega_2 \), which discriminates the overdamped (\( Q \ll 1 \)) from the underdamped regimes (\( Q \gg 1 \)). For simplicity, we will consider the one-dimensional problem in which the spatial coordinate, \( z \), is perpendicular to the sample surface.

By substituting the complex frequency \( \tilde{\omega} \) into the dispersion relation given by equation (7), it is possible to obtain the analytic expressions of \( \omega_I \) and \( \omega_2 \) as a function of \( k \). Without entering into the details of the calculations, that will be presented elsewhere [121], it is possible to show that the nature of the admitted solutions strongly depends on the ratio \( \tau_T/\tau_f \). While non-oscillatory solutions, characterized by \( \omega_I = 0 \), are found for \( \tau_f > \tau_T \), i.e., when the heat flux precedes the establishment of a thermal gradient, a wave-like behavior of the temperature propagation may emerge in the case \( \tau_f < \tau_T \), i.e., when the temperature gradient is established before the onset of the heat flux. We can define a lower \( (k_{low}) \) and upper \( (k_{up}) \) bound for the wavevectors that can sustain oscillatory solutions:

\[ k_{low(upp)} = \frac{2}{k_T \tau_f} \left( \frac{\tau_f}{\tau_T} \right)^{1/2} \times \left( 1 - \frac{1}{2} \frac{\tau_f}{\tau_T} - (+) \sqrt{1 - \frac{\tau_f}{\tau_T}} \right). \]

(8)

In the range \( k_{low} < k < k_{up} \), the allowed complex frequencies
are:

\[ \omega_1 = \pm \sqrt{\frac{\alpha^2}{4} \left[ \frac{\tau_T}{\tau_q} \right]^2 k^4 + \frac{\alpha}{\tau_q} \left[ \frac{1}{2} \left( \frac{\tau_T}{\tau_q} \right) - 1 \right] k^2 + \frac{1}{4 \tau_q}} ; \]

\[ \omega_2 = \frac{1}{2 \tau_q} + \frac{\alpha}{2} \left[ \frac{\tau_T}{\tau_q} \right] k^2 \]

while, for \( k \leq k_{\text{low}} \) and \( k \geq k_{\text{up}} \) no oscillatory solutions are admitted, i.e., \( \omega_1 = 0 \).

The oscillating behavior of the temperature field, is better appreciated by inspecting the \( Q \)-factor:

\[ Q(k) = \begin{cases} \frac{4 \alpha \tau_T k^2}{(1 + \alpha \tau_T k^2)^2} - 1 & \text{for } k_{\text{low}} < k < k_{\text{up}} \\ 0 & \text{for } k \leq k_{\text{low}} \text{ or } k \geq k_{\text{up}}. \end{cases} \]

The most favorable condition to observe underdamped oscillations corresponds to the maximum \( Q \)-factor:

\[ Q_{\text{max}} = \frac{\tau_T}{\sqrt{\alpha \tau_T}} - 1, \]

that is obtained at the wavevector \( k_{Q_{\text{max}}} = 1/\sqrt{\alpha \tau_T} \).

Equation (11) suggests that the condition \( \tau_q \gg \tau_T \) is the prerequisite to observe wave-like effects of the temperature propagation in real materials.

4.3. Emergent phenomena at the nanoscale

As shown in section 4.2, emergent wave-like regimes of the temperature field may potentially be found in systems in which the condition \( \tau_q \gg \tau_T \) holds, i.e., a thermal gradient is very quickly established, while the heat flux follows at a later time \( \tau_T \).

Correlated TMOs provide a very interesting playground to investigate this physics. Their layered structure is characterized by strongly anisotropic conduction properties that can lead to a very fast in-plane thermalization and to a very slow out-of-plane heat propagation, thus favoring the emergence of the wave-like regime, as schematically shown in figure 8(a).

Here, we will focus on copper oxides and, in particular, on the Bi$_2$Sr$_2$CaCu$_2$O$_8$ (Bi2212) family that exhibits the most anisotropic transport properties. In general, the conduction properties of copper oxides are dominated by the charge carriers that occupy the Cu–3d orbitals within the Cu–O planes (ab-planes, see figure 8(b)). The strong tendency to delocalization, driven by the very large in-plane hopping integral \( \tau_l \sim 0.3 \) eV is contrasted by the strong effective interactions. At moderate doping concentration (~15%) the electronic interactions give rise to a strong coupling with the bosonic fluctuations of both magnetic and phononic origin [112]. The fastest scattering process is likely to be related to the coupling with the short-ranged antiferromagnetic fluctuations that persist when the system is doped [122]. It has
been recently shown [74] that the excess kinetic energy provided by the pump pulse is completely released to the magnetic background within a timescale of ~50 fs. It is thus reasonable to assume $\tau_T = 50$ fs as the time necessary for the local thermalization between charge carriers and spin fluctuations and for the onset of the temperature gradient after an anisotropic pump excitation. The electron–phonon coupling eventually drives the complete thermalization between the electronic, magnetic and phononic degrees of freedom on a timescale of ~1 ps. We underline that, even in bulk materials, the pump excitation is intrinsically anisotropic, being the energy absorption confined within a penetration length of ~20–200 nm depending on the material. As we will discuss later, ‘artificial’ gradients can be induced by nanostructuring the material under investigation.

Notably, the transport properties of copper oxides are strongly anisotropic, being the interlayer hopping limited to $t_{1L} \approx 15$ meV [127]. As a consequence, the strong in-plane scattering makes the c-axis conductivity almost completely incoherent. In Bi2212, the c-axis optical conductivity can be as small as 0.01 $\Omega^{-1}$ cm$^{-1}$, in contrast to an in-plane conductivity of the order of 5000 $\Omega^{-1}$ cm$^{-1}$ [128]. In a similar way, the electronic thermal conductivity is reduced from ~1 Wm$^{-1}$K$^{-1}$ in the ab-plane to ~3 x $10^{-4}$ Wm$^{-1}$K$^{-1}$ when considering the interlayer thermal transport. The natural consequence of this strong anisotropy is that any possible heat exchange perpendicular to the Cu–O planes is strongly delayed as compared to the in-plane thermalization that is effective on the sub-100 fs timescale.

This observation naturally suggests a possible building block for designing materials in which the wave-like propagation of the temperature field can be observed and exploited. Given the difficulty of estimating $\tau_T$ from both first-principles and experiments, we will consider the value of ~1 ps as a lower bound. This value, which represents a conservative estimate, corresponds to the reasonable assumption $\tau_q/\tau_T = t_0/t_{1L}$.

Considering the electronic problem related to the heat propagation along the c-axis in Bi2212, we obtain $\alpha \sim 10^{-3}$–$6.5 \times 10^{-2}$ m$^2$s$^{-1}$ in the 300–20 K temperature range, as reported in table 2, while $\tau_T/\tau_T > 20$. From equation (8) and assuming $\tau_T = 1$ ps, it is possible to calculate the upper ($k_{ap} \sim 400–50$ nm$^{-1}$ at $T = 300–20$ K) and lower ($k_{low} \sim 5–0.63$ nm$^{-1}$ at $T = 300–20$ K) bounds of the wavevectors compatible with temperature oscillations. While $2\pi/k_{ap}$ corresponds to a fraction of the interatomic distance and cannot be experimentally achieved, $\lambda_T = 2\pi/k_{low} = 1–10$ nm provides the maximum wavelength that can sustain an oscillatory behavior. These values are compatible with the geometric constraints that can be applied by nanostructuring copper oxides and other TMOs. In figure 8(c) we report the dispersion relations of the oscillating solution at $T = 20$ K, as calculated by equation (9). At the wavevector $k \sim 5$ nm$^{-1}$, corresponding to $\lambda_T \sim 1.2$ nm, the oscillation frequency is $\omega_T \sim 4$ rad s$^{-1}$ and the $Q$-factor is compatible with the observation of oscillations with period of ~1.6 ps.

The physics discussed in the current section suggests the possibility of engineering realistic nanostructured systems in which, on the picosecond timescale, the temperature propagation is described by a wave equation instead of the typical diffusion law.

Obviously, this regime can be achieved and observed only on fast timescales [118], i.e. before the damping washes out coherent effects and restores the “classical” behavior. The possibility of controlling layer-by-layer the growth of TMOs [19] opens intriguing perspectives: by creating heterostructures with typical dimensions of few nanometers, it is indeed possible to exploit the novel wave-like regime of the temperature field. In these systems, the local temperature increase could be manipulated at the nanoscale by exploiting interference effects, thus opening an entirely new field in nano-thermodynamics. Furthermore, the possibility of creating superlattices with periodicity of the order of few atomic cells could lead to the design of artificial bandstructures for the temperature waves, thus opening to the development of waveguides, cavities and frequency filters for the temperature field.

Far from pretending of being exhaustive, the above discussion aims at demonstrating that, for realistic materials, it is possible to investigate an emergent wave-like regime for the temperature propagation on ultrafast timescales. The numbers reported in table 2 should be considered as an example of the physics that could be investigated at the nanoscale. The concepts here proposed can be easily extended to many different cases. Although in the previous discussion we focused on the electronic temperature of the specific copper oxide Bi$_2$Sr$_2$CaCu$_2$O$_8$, similar effects are expected also when considering the lattice temperature. For example, in Bi2212 the largest value of $\alpha$ for the phonon case (6.3 $\times$ $10^{-4}$ m$^2$s$^{-1}$ at 20 K) leads to the possibility of observing wave-like regimes at smaller wavevectors, corresponding to length scales of the order of tens of nanometers. For sake of completeness we report the relevant data for the phonon case in table 2.

Similar concepts can also be extended to the spin temperature in systems characterized by short-range magnetic correlations. As an example, let us consider iridium oxides, which are characterized by a strong anisotropy of the magnetic dynamics. As discussed in section 2, the ratio between the in-plane and out-of-plane magnetic exchange can be as high as $J_{1L}/J_{2L} \sim 6 \times 10^4$. Under non-equilibrium conditions, the strong anisotropy leads to a very fast in-plane thermalization of the magnetic fluctuations ($\tau_T \sim 100$ fs) while the heat flux perpendicular to the Ir planes is strongly delayed by the small interlayer magnetic coupling. As a conservative estimation, we assume $\tau_T = 10^4$T$^{1/2}$ and we use the electronic heat capacity and thermal conductivity of Sr$_2$IrO$_4$ (SIO), reported in table 1, as the upper bound of the magnetic contribution. The large $\tau_T/\tau_T$ turns out to be favorable to observe undulatory effects of the effective temperature of magnetic fluctuations in iridium oxides. At wavevectors compatible with the dimensions of the SIO unit cell along the c-axis (~25 Å), the oscillation frequency is about $\omega_T \sim 5 \times 10^{-4}$ rad ps$^{-1}$, with $Q > 1$. Many strategies could be devised in order to tune the wavelength and the period of the coherent oscillation of the magnetic temperature. For example, larger values of the $\alpha$ parameter could be obtained by increasing the thermal
optimally doped ($T_c = 85$ K) Bi2212 crystals are taken from [123, 124, 125]. These values are representative of the specific heats and thermal conductivities of other families of copper oxides, such as YBa$_2$Cu$_3$O$_7$ and La$_{2-x}$Sr$_x$CuO$_4$. $C$ and $\kappa_T$ of nearly optimally doped ($T_c = 85$ K) Bi2212 crystals are taken from [123, 124, 125]. These values are representative of the specific heats and thermal conductivities of other families of copper oxides, such as Na$_2$IrO$_3$.

Table 2. Lattice specific heat ($C$), thermal conductivity ($\kappa_T$) and thermal diffusivity ($\alpha$) of copper oxides. $C$ and $\kappa_T$ of nearly optimally doped ($T_c = 85$ K) Bi2212 crystals are taken from [123, 124, 125]. These values are representative of the specific heats and thermal conductivities of other families of copper oxides, such as YBa$_2$Cu$_3$O$_7$ and La$_{2-x}$Sr$_x$CuO$_4$.

| Temperature ($T$) | Specific Heat ($C$) | Thermal Conductivity ($\kappa_T$) | Thermal Diffusivity ($\alpha$) | Thermal Time ($\tau_T$) | Velocity Length ($\lambda$) |
|------------------|---------------------|----------------------------------|-------------------------------|------------------------|--------------------------|
| K                | J m$^{-3}$ K$^{-1}$ | Wm$^{-1}$K$^{-1}$ | m$^2$s$^{-1}$ | ps | nm ps$^{-1}$ | nm |
| Bi$_2$Sr$_2$CaCu$_2$O$_8$ (Bi2212) | | | | |
| Electrons        | 300                 | $3.3 \times 10^4$             | $3.0 \times 10^{-4}$          | $1.0 \times 10^{-8}$ | 0.05 | $<1$ | $<0.10$ | $>0.10$ |
|                  | 50                  | $4.0 \times 10^3$             | $2.5 \times 10^{-4}$          | $6.5 \times 10^{-8}$ | 0.05 | $<1$ | $<0.25$ | $>0.25$ |
|                  | 20                  | $4.0 \times 10^2$             | $2.5 \times 10^{-4}$          | $6.5 \times 10^{-7}$ | 0.05 | $<1$ | $<0.80$ | $>0.80$ |
| Sr$_2$IrO$_4$    |                     |                                 |                               |                        |                           |       |
| Electrons/       | 300                 | $1.5 \times 10^7$             | $1.5 \times 10^{-7}$          | $1 \times 10^{-10}$   | 0.1 | $\approx 1000$ | $\approx 3 \times 10^{-4}$ | $\approx 0.3$ |
| magnetic         | 50                  | $2.5 \times 10^5$             | $2.5 \times 10^{-8}$          | $1 \times 10^{-10}$   | 0.1 | $\approx 1000$ | $\approx 3 \times 10^{-4}$ | $\approx 0.3$ |
| fluctuations     | 20                  | $1.0 \times 10^4$             | $1.0 \times 10^{-8}$          | $1 \times 10^{-10}$   | 0.1 | $\approx 1000$ | $\approx 3 \times 10^{-4}$ | $\approx 0.3$ |

conductivity via chemical doping of the Mott insulating phase. Furthermore, the use of strongly frustrated magnetic systems in proximity of a 3D magnetic transition could provide an additional knob to tune the magnetic heat capacity. A paradigmatic system is Na$_2$IrO$_3$ that exhibits a zig-zag phase transition at $T_N = 15$ K. In the 70–15 K temperature range, the heat capacity is dominated by the contribution of the short-range 2D magnetic fluctuations, giving rise to $C_{\text{mag}} \approx 4 \times 10^4$ J m$^{-3}$ K$^{-1}$. The dramatic changes of the magnetic heat capacity in the vicinity of $T_N$ could be exploited to manipulate the wave-like nature of the magnetic temperature propagation in heterostructures or nanoscaled devices.

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