Machine learning for nanophotonics

Itzik Malkiel, Michael Mrejen, Lior Wolf, and Haim Suchowski

The past decade has witnessed the advent of nanophotonics, where light–matter interaction is shaped, almost at will, with human-made designed nanostructures. However, the design process for these nanostructures has remained complex, often relying on the intuition and expertise of the designer, ultimately limiting the reach and penetration of this groundbreaking approach. Recently, there has been an increasing number of studies in applying machine learning techniques for the design of nanostructures. Most of these studies engage deep learning techniques, which entail training a deep neural network (DNN) to approximate the highly nonlinear function of the underlying physical process of the interaction between light and the nanostructures. At the end of the training, the DNN allows for on-demand design of nanostructures (i.e., the model can infer nanostructure geometries for desired light spectra).

In this article, we review previous studies for designing nanostructures, including recent advances where a DNN is trained to generate a two-dimensional image of the designed nanostructure, which is not limited to a closed set of nanostructure shapes, and can be trained for the design of any geometry. This allows for better generalization, with higher applicability for real-world design problems.

Introduction

The inverse design of nanophotonic structures, obtaining a geometry for a desired photonic function (Figure 1a–b), has been a challenge for decades. When treated as a pure optimization problem, due to the highly nonlinear nature of the problem, hundreds to several thousands of iterations are required for a single design task, even with the most advanced algorithms, such as evolutionary or topology optimization algorithms (Figure 1c–d). Recently, modern machine learning algorithms, which have revolutionized a multitude of computer-assisted processes, from character and speech recognition, autonomous vehicles, and cancer diagnostics to name a few, have been applied to the inverse problem in nanophotonics and have demonstrated great promise.

The major contributions to date that have been published to date can be categorized into three categories (Figure 1d).

The first, and the most fundamental one, is obtaining a model that is capable of designing nanostructures from the same shape and material it was trained on. Attempts to devise such a model have largely failed, as there is no guarantee that the model will work with different materials or shapes. The second category incorporates models that are able to design geometries with shapes that are similar, but not identical, to the set of shapes used during training, but are still considered to be in the same family (i.e., the model can generalize to other shapes that are similar, but not identical, to the set of shapes it was trained on). Attempts to devise such a model have recently been presented where the parameters of the model are the pixel of a two-dimensional (2D) image, allowing a more versatile and general representation of structures.

The third category is a model that is able to design any geometry, with any shape, achieving what the deep learning community calls the generalization capability. The generalization ability of such models needs to be verified via a proper holdout test set (i.e., a test set) comprising structures sampled from a completely different distribution than the set the model was trained on. To this end, studies that provide a model that is able to design nanostructures for any spectra should exercise extra care in constructing a test set that would verify the generalization level of the model at hand.

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The categories discussed above are ordered by the complexity of the learning task, where each category relates to a different level of robustness or generalization. The most desirable capability is the last category, which can design any geometry with any shape.

Under the context of the model at hand and the assumption that a large volume of data is available for learning, the first step to achieve such a generic capability is to design a model that has enough degrees of freedom to allow the design of any geometry.

In this article, we review the topic of inverse design in nanophotonics based on deep learning architectures and compare the advantages and weaknesses of the main published approaches. We also expand our current approach toward the goal of inverse design of any nanostructure with at-will spectral response.

**Deep learning versus optimization and genetic algorithms**

The deep learning approach to inverse design in nanophotonics is still in its infancy and needs to be evaluated against more established optimization techniques that have been presented over the years. We therefore start with a general comparison, along the lines presented in Table I, between the deep learning approach and the classical approaches.
learning approach and genetic algorithms, the most widely used type of optimization algorithm, for the inverse design of nanophotonics devices.\textsuperscript{5,7,8}

A genetic algorithm is an optimization method inspired by natural selection. Such an algorithm can be used to solve optimization tasks by searching for a good solution among many possible solutions, with regard to a predefined set of constraints. This task is further defined by a fitness function that measures the quality of a candidate solution. The goal is to find a solution that maximizes the fit function subject to the constraints. In order to find a good solution, the algorithm, similar to natural selection, evolves generations of possible solutions. At the beginning of the process, the algorithm starts with a random set of simple solutions; it evaluates each one of them and then chooses which will be carried over to the next generation and how. Some possible solutions can move with no change to the next generation, some will be randomly mutated, and some will be randomly matched with other solutions, thus creating a new descendant candidate.

In each generation, all of the possible solutions are evaluated in order to search for the best fit, and the process terminates when a good solution is found or when a predefined threshold of the number of generations is reached. Although the nondeterministic search of the genetic algorithm could lead to the discovery of nontrivial solutions, genetic algorithms are not suitable for tasks where the computation of the fitness function is computationally demanding. The algorithm relies on evaluating every single possible candidate in every generation, so if the evaluation time is demanding, the process becomes intractable.

As a specific example, evaluating a single spectrum of a given three-dimensional (3D) geometry for a single polarization for that wavelength range takes at least one minute.
to several tens of minutes even when using efficient scattering calculations such as the discrete dipole approximation, as there is no analytical solution for the scattering of a general 3D geometry. This practical, simple runtime constraint makes a genetic algorithm not relevant to this type of task since each generation is composed of hundreds or thousands of experiments that demand hours of computations for each generation and days for a single design task.

In comparison to evolutionary algorithms and other similar stochastic optimization methods, mainstream learning techniques such as deep learning optimize a generic model during the training process. Although there may be a relatively long training process, using such a network to predict new samples typically takes less than 1 s. In the approach developed by the authors, training the network takes up to 3 h. When the training process is complete, each query takes 3 ms to compute. This way, given a query, deep learning would design a solution in 3 ms, while a genetic algorithm will perform thousands of simulations where each one of the simulations could take hours to perform.

We emphasize that the evolutionary approach is fundamentally different since for every single design task, it searches the parameter space over dozens (sometimes hundreds) of generations with each generation encompassing dozens or hundreds of individual designs (e.g., individuals). For this reason, the individuals should be simple enough to analytically solve for their electromagnetic response, otherwise the optimization

Table I. Performance comparison with respect to different parameters between different computational approaches (shallow neural network, deep neural network, and genetic algorithms).

| Parameter                  | Shallow Neural Network | Deep Neural Network | Genetic Algorithms |
|----------------------------|------------------------|---------------------|--------------------|
| Query run time             | Fast                   | Fast                | Slow               |
| AI technique               | Learning               | Learning            | Optimization       |
| Design/Retrieval quality   | Poor                   | Good                | Poor; see MSE results |

Note: AI, artificial intelligence; MSE, mean squared error.

Figure 4. Our previous work introduced a bilateral deep learning (DL) network able to predict the response (in two polarizations) of any of the structures defined in the “H” family (see main text). It also allows the design of “H” structures based on the required response. (a) The “H” geometry is parametrized to allow easy vector representation where the presence of Legs 1–5 is binarily coded (1 = leg present, 0 = leg absent). Note: $L_1$, $L_2$, $L_4$, and $L_5$ are Leg length; $L_3$ = Leg 3 length; $\phi$ = Leg 1 angle. (b) The network architecture allows the input of the horizontal and vertical spectrum vectors (sampled at 43 wavelength points each) as well as a material’s properties vector representation (43 parameters). This input is then fed into the first three fully connected 100 neuron (described by the solid black circles) layers followed by eight fully connected layers. The DL is given a (c) measured horizontal polarization (horizontal red double-headed arrow) and (d) vertical polarization (vertical blue double-headed arrow). (e) The predicted geometry, which is in good agreement compared to the geometry measured in scanning electron microscope (inset [c]). Comparison between the fed spectra and the predicted ones are found in (c, d). Note: DNN, deep neural network.
task will take a prohibitive amount of time and thus limit the usefulness of such an approach.

The deep neural network (DNN) approach is radically different. A DNN is trained on a set encompassing structures that are not trivial, for which the response must be calculated using time-consuming numerical approaches. However, once the data set is created and learned, this task is nonrecurring, and each design task takes only a query of the DNN, which takes only a few milliseconds.

Recent advances in DNNs for nanophotonics

In this section, we review recent advances in DNNs applied to the inverse design problem of nanophotonic devices. Recently, we introduced the bidirectional neural network for the design of nanostructures (Figure 4). The bidirectional model, which proceeds from the optical response spectrum to the nanoparticle geometry and then back, solves both the inverse problem of designing a nanostructure and the direct problem of inferring the optical characteristics of the designed geometry. The advantages of the bidirectional model are twofold. First, this model is able to streamline the design process by retrieving an immediate prediction for the optical properties of the designed nanostructure. In this model, the designer can match the desired spectra (as depicted in Figure 1a) with the recovered spectra, which can also be used in understanding the confidence level of the model for the specific design. Second, a bidirectional model allows co-adaptation between both directions, leading to better robustness and higher stability for the predictions.

The model we introduced was trained on synthetic data centered around different variants of the H shape, and was also applied on measured spectra from nanofabricated materials from our laboratory. This model was the first neural-based architecture applied for the design of a nanostructure, but its architecture is inherently limited to the H family (Figure 4). To date, this is the only experimental demonstration of geometry prediction capability of a deep learning network.

Ma and co-workers introduced a model for the design of chiral metamaterials incorporating two bidirectional networks along with a synthetic data set composed of a vectorized representation of geometries associated with materials, reflection...
spectra, and circular dichroism spectra. The dual bidirectional model comprises two networks, a primary network and an auxiliary network. The primary network predicts the back and forth geometry encoding vector and its associated reflection spectra (Figure 5a). The auxiliary network predicts the back and forth geometry (represented as an encoding vector) and its associated circular dichroism spectra. Both networks are separately trained using the previously discussed data set. The authors show that a model that combines both the auxiliary network and the primary network yields more accurate predictions.

Sajedian and co-workers suggest a neural network that solves the direct problem of inferring spectra for a given geometry (Figure 6). This problem can be solved via (slow) simulations, and is considered to be more feasible compared to the ill-posed inverse problem of inferring a geometry for on-demand spectra.

Liu and co-workers propose a generative adversarial network (GAN)—an algorithm that uses two neural networks that contest each other to generate new data—for generating 2D nanostructure images from spectra (Figure 7). The authors created a synthetic data set of geometries associated with multiple families, such as squares, circles, sectors, crosses, and shapes from the Modified National Institute of Standards and Technology (MNIST) data set (which incorporate handwritten digits [numbers]). The authors demonstrated the ability of the model to randomly design test samples from each one of the families previously discussed, using a model that was trained with samples from all families. This evaluation corresponds to Category 1 previously presented in Figure 1d, as the model task is to infer geometries from the same template it already saw in the training (this time, only with different attributes such as sizes and angles).

During a second evaluation, Liu and co-workers tested a higher level of generalization, which correlates to the second category previously described. In this evaluation, the authors used a holdout test set composed of a complete subfamily set of geometries. Specifically, and to showcase the capability of their approach, the authors decided to keep all of the samples that correspond to digit “5” from the MNIST family in a holdout test set and trained their model on the rest of the data set. They reported the topologies of the predicted geometry and the original (i.e., ground truth) geometry differ considerably (the predicted geometry comprised a variation of the digit “3”), but the overall spectra of the predicted geometry possess similar features to the input spectra, with some discrepancies in a few specific locations.

In addition, the authors argue that without GAN training, their model collapses and generates images of random pixels. When optimizing an inverse function of a single network, one can often obtain a solution that satisfies the inversion criteria; however, this does not create a valid input, as has been shown in the case of adversarial examples. This is why, similar to the mapping between MNIST and SVHN (the Street View House Numbers) digits results presented, a GAN loss is needed. An alternative way for GANs to improve generalization may be to rely on activations from multiple layers of the direct network, as is done in the perceptual loss.

As previously mentioned, we introduced a model able to infer geometries of the same or similar shapes it was trained on (Category 1), which have variable sizes, angles, and the permittivity (epsilon) of the host materials. However, in order to be able to design any geometry, one needs to allow for larger degrees of freedom. Specifically, our model architecture was designed to retrieve coding vectors that encode the geometry shape to the “H” family. To circumvent the inherent limitation of this encoding, further degrees of freedom were obtained as we asked the model to predict each edge presence, the length of the edge, and the angle between the inner edge and the top right edge.
Toward generalization

Recent work in computer vision has suggested pix2pix, a neural-based model that learns to map images from the source domain to the target domain. Given an input image, the model learns to generate images according to some ground truth image labels. Applied on different types of data sets, pix2pix showcases the ability of neural networks to generate realistic images that preserve different types of underlying logic, such as mapping gray images to color images, facade labels to images, maps to aerial views.

Following the pix2pix approach, and by building upon our previous work, we recently published the spectra2pix model, which aims to expand our capabilities to the second or even third more desirable categories. The model focuses on solving the inverse problem of inferring a nanostructure geometry.
from a given spectrum and material properties. Compared to the previous bidirectional model, the spectra2pix architecture supports the generation of any geometry by training the model to regress the raw pixel values of the 2D images of the geometries at hand. The training task is enforced by optimizing the spectra2pix model to minimize a pixelwise loss term, applied on the generated image with the ground truth image. In this new work, we published a new version of our data set, incorporating the 2D images of the geometries. The data set and the code can be found on Github.15

In spectra2pix, we utilize the data set from References 5 and 7. This data set comprises ~13 K samples of synthetic experiments, where each sample is associated with a geometry, a single polarization (vertical or horizontal), and material properties. By pairing the polarization, we formed ~6 K experiments comprising the quadruplet of horizontal spectrum, vertical spectrum, epsilon host dielectric, and 2D image of the geometry. The epsilon host dielectric values vary in the range of 1.0 to 3.0.

The geometries are composed of different combinations of edges, which together form a template with the shape “H.” All three data parts, geometry, spectrum, and material properties are represented as vectors. Using spectra2pix, we were able to transform the previously discussed data set from the vectorized representation of the geometry encoding into 2D binary images comprising geometry shapes. A sample of the transformed images, along with the matched spectra of each geometry can be seen in Figure 8. The transformed data set is available for the public on Github.15

The architecture of spectra2pix is composed of two parts. The first part is built upon our previous work and utilizes three representations of a different part of the input data (two polarizations and host material). A few key properties of the second part of the architecture were adapted from pix2pix work, for which, following the fully connected sequences, the spectra2pix model reshapes the internal vectorized representation into a 2D matrix and utilizes a sequence of convolutional layers. The last layer in this model is a convolutional layer, with a single filter, which outputs a 2D image of the desired geometry.

To study the ability of spectra2pix to generalize, we split the previously discussed data set into train, test, and validation sets. The test set contains all of the geometries of the shape “L” and its variants. The train set contains all of the rest of the experiments (H family shapes), leaving 5% as a holdout validation set. The spectra2pix network was trained for 1 M training steps. We used the validation set for early stopping. At the end of the training, we used the model to infer geometries for the test set.

Figure 9 shows a representative sample from the test set predictions. Each row represents a different query. The left column (Figure 9a) displays the input spectra (both vertical and horizontal polarization), the middle (Figure 9b) presents the generated geometry, and the right (Figure 9c) showcases the ground truth label. These results indicate that the spectra2pix is fairly able to generate unseen geometries sampled from a different distribution than what the model was trained on.

Compared to the research reported in Reference 5, in the spectra2pix work, we utilize our model and showcase its ability to converge without GAN training, and more importantly, we demonstrate a successful generalization ability of the model to design a complete unseen subfamily set of geometries, taken from a somewhat different distribution the model was trained on. This generalization capability is associated with category two previously described.

Conclusions

The use of machine learning techniques, and deep learning in particular, has spawned huge interest over the past few years in the nanophotonics communities, due to the great promise these techniques offer for the inverse design of novel nanophotonic devices and functionalities.

In this article, we have reviewed the main advances that have occurred in the past four years. We discussed the advantages and weaknesses of the different approaches presented so far, and...
introduced our spectra2pix network, a model composed of ultimate degrees of freedom, which conceptually allows the design of any 2D geometry. In addition, we presented the ability of spectra2pix to successfully generalize the set design of a completely unseen subfamily of geometries. Our results highlight the importance and the generalization ability of DNNs toward the goal of inverse design of any nanostructure with at-will spectral response.

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