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Citation for the original published paper (version of record):
Renaud, F., Romeo, A., Agertz, O. (2021). From giant clumps to clouds - I. The impact of gas fraction evolution on the stability of galactic discs. Monthly Notices of the Royal Astronomical Society, 508(1): 352-370. http://dx.doi.org/10.1093/mnras/stab2604

N.B. When citing this work, cite the original published paper.
From giant clumps to clouds – I. The impact of gas fraction evolution on the stability of galactic discs

Florent Renaud, Alessandro B. Romeo and Oscar Agertz

1 Department of Astronomy and Theoretical Physics, Lund Observatory, Box 43, SE-221 00 Lund, Sweden
2 Department of Space, Earth and Environment, Chalmers University of Technology, SE-41296 Gothenburg, Sweden

ABSTRACT

The morphology of gas-rich disc galaxies at redshift $z \sim 1–3$ is dominated by a few massive clumps. The process of formation or assembly of these clumps and their relation to molecular clouds in contemporary spiral galaxies are still unknown. Using simulations of isolated disc galaxies, we study how the structure of the interstellar medium and the stability regime of the discs change when varying the gas fraction. In all galaxies, the stellar component is the main driver of instabilities. However, the molecular gas plays a non-negligible role in the interclump medium of gas-rich cases, and thus in the assembly of the massive clumps. At scales smaller than a few 100 pc, the Toomre-like disc instabilities are replaced by another regime, especially in the gas-rich galaxies. We find that galaxies at low gas fraction (10 per cent) stand apart from discs with more gas, which all share similar properties in virtually all aspects we explore. For gas fractions below $\approx 20$ per cent, the clump-scale regime of instabilities disappears, leaving only the large-scale disc-driven regime. Associating the change of gas fraction to the cosmic evolution of galaxies, this transition marks the end of the clumpy phase of disc galaxies, and allows for the onset of spiral structures, as commonly found in the local Universe.

Key words: instabilities – methods: numerical – galaxies: formation – galaxies: high-redshift – galaxies: ISM.

1 INTRODUCTION

Over the last decade, developments in the modelling of galactic physics have significantly improved the realism of galaxy simulations. Models of stellar feedback in particular allow to successfully reproduce a number of observables of the overall structure of galaxies in cosmological context (Naab & Ostriker 2017), and also in the properties of their interstellar medium and star-forming clouds in isolated models (Grisdale et al. 2017, 2018, 2019). This is accompanied by formalisms and tools to analyse and characterize the structures of discs and their regimes of instabilities (e.g. Elmegreen 2010; Romeo, Burkert & Agertz 2010; Agertz, Romeo & Grisdale 2015). These works have mostly focused on contemporary disc galaxies, while their high redshift counterparts have often been neglected due to limited observational constraints on resolved star forming regions at $z \gtrsim 1$. However, gravitational lensing (Cava et al. 2018; Dessauges-Zavadsky et al. 2019) and forthcoming instruments like JWST open new perspectives.

At redshift $z \approx 1–3$, the morphology of disc galaxies is often dominated by discrete, massive star-forming clumps ($\sim 0.5–1$ kpc, $\sim 10^8$ $M_\odot$, Cowie, Hu & Songaila 1995; Elmegreen et al. 2007, 2009; Wylys et al. 2012; Swinbank et al. 2015; Zanella et al. 2015; Fisher et al. 2017; Guo et al. 2018). Surveys of high redshift galaxies show the dependence of the fraction of clumpy galaxies on the stellar mass and redshift, with more than half of the disc galaxies at $z \sim 3$ exhibiting clumpy morphologies (Guo et al. 2015). As the clumpy phase of galaxy evolution occurs at ‘cosmic noon’, i.e. the peak of the cosmic star formation rate (SFR; Madau & Dickinson 2014), it is of paramount importance in the assembly of the stellar populations observed in contemporary galaxies. Massive clumps have been invoked to participate in radial inflows and the assembly of the bulge (Noguchi 1999; Ceverino, Dekel & Bournaud 2010; Bournaud et al. 2014), in the bimodal distribution of stellar abundances in the Milky Way (Clarke et al. 2019; Khoperskov et al. 2021; Renaud et al. 2021), and even in the onset of kinematically thick discs (van Donkelaar et al., in preparation). Yet, fundamental properties of these clumps, like their lifetimes, are still debated (Genel et al. 2012; Mandelker et al. 2014, 2017; Oklopčić et al. 2017; see a discussion in Fensch & Bournaud 2021). One key problem is to explain when, how and how fast the transition from clumpy structures to spiral arms occurs along the course of galaxy evolution, and how this relates to mergers and to the gas accretion rate of galaxies (Bournaud et al. 2007; Agertz, Teyssier & Moore 2009; Dekel et al. 2009; Cacciato, Dekel & Genel 2012; Ceverino et al. 2012).

In the ‘bottom-up’ scenario, massive clumps assemble by mergers of smaller structures (Behrendt, Burkert & Schartmann 2016; Behrendt, Schartmann & Burkert 2019; Benincasa et al. 2019). The alternative ‘top-down’ hypothesis invokes the fragmentation of large structures into smaller sub-clumps (see a discussion in Behrendt et al. 2019). Observations of high redshift clumpy galaxies have not been able to tell the two scenarios apart, as they suffer from incompleteness in the detection of clumps (Tamburello et al. 2017; Faure et al. 2021). Furthermore dust has been suggested to bias the interpretation of the hierarchy of massive clumps (Buck et al. 2017). From a theoretical perspective, in order to disentangle the two options and establish which dominates under different physical conditions, it is necessary to assess the stability regimes of disc
galaxies, and their evolution with redshift. Inoue et al. (2016) conducted such an analysis using a suite of cosmological zoom simulations. By tracing the origins of massive clumps back to the pre-collapse protoclump region of the disc, they reported that, counter-intuitively, the material which eventually assembles into clumps lies in gravitationally stable regions, as estimated with a two-component stability criterion. To explain this contradiction, they invoked non-linear external mechanisms like mergers and tidal compression. Yet, a number of simulations of discs without a cosmological context successfully reproduce properties of clumpy galaxies (e.g. Bournaud et al. 2014; Perret et al. 2014; Fensch et al. 2017; Clarke et al. 2019).

The lack of a clear understanding of the nature and the formation process of massive clumps hinders the field of galaxy evolution, and prevents us from connecting the physics of gas-rich galaxies to that of contemporary discs, which is much better understood. The natural approach to address these questions is to use cosmological simulations of disc galaxies from high to low redshift. However, this suffers from two major drawbacks. First, the numerical cost of resolving star-forming clouds/clumps in cosmological simulations is still prohibitive and, at best, allows studying only a single or small number of cases. Secondly, by accounting for many mechanisms simultaneously active (gas accretion, mergers, intrinsic evolution), it is notoriously difficult to identify the physical role of a single parameter. For instance, in the cosmological zoom simulation VINTERGATAN, we found that the end of star formation in the thick disc coincides with both the epoch of the last major merger, and the end of the clumpy phase (Agertz et al. 2021; Renaud et al. 2021a, b), thus blurring the interpretation of the exact role of each mechanism.

As a complement to cosmological zoom simulations, in this paper we present results from controlled numerical experiments of several disc galaxies, where the only parameter changed is the gas mass fraction. This mimics the cosmological evolution of the gas fraction in disc galaxies, as observed from $z \sim 1$–2 to $z = 0$ (Saintonge et al. 2013). We introduce our simulation method in section Section 2. We analyse the structural properties of these discs (Section 3), and the physics of their instabilities (Section 4). For the first time, we consider the mutual effects of the three components (atomic gas, molecular gas, and stars) in the stability analysis, by applying the multicomponent formalism of Romeo & Falstad (2013) to simulated galaxies. We highlight the existence of two regimes of instabilities in gas-rich discs, with a transition scale between the two at a few 100 pc (Section 5).

2 METHOD

We simulate disc galaxies in isolation, i.e. without cosmological context, with the adaptive mesh refinement code RAMSES (Teyssier 2002). Apart from the cosmological aspects, the numerical method is identical to that of the VINTERGATAN simulation, i.e. it accounts for heating from a cosmological background (Haardt & Madau 1996), calibrated at redshift 0 for all simulations for simplicity, atomic, and molecular cooling down to 10 K, star formation at a fixed efficiency of 10 per cent per free-fall time above a density threshold of 100 cm$^{-3}$, and stellar feedback including winds, radiation pressure, type-II and Ia supernovae, and the production of oxygen and iron (see Agertz et al. 2021 and references therein for details). The baryonic mass threshold to refine the grid cells is $\approx 1700 \, M_\odot$. The resolution in the densest regions reaches 12 pc. All our analysis is conducted with this numerical resolution, but some quantities (like velocity dispersions) are measured using statistical tools over larger scales (‘beam sizes’) of 70 and 700 pc.

For each simulation, a galaxy of total mass $7 \times 10^{11} \, M_\odot$ is initialized with the MAGI code (Miki & Umemura 2018) with a dark matter halo, a central bulge, and a gaseous disc. The mass resolution of the initial conditions is $1.3 \times 10^5 \, M_\odot$ for the dark matter, and $4.6 \times 10^4 \, M_\odot$ for the stars. The initial parameters are provided in Appendix A. The galaxy is placed at the centre of a 200 kpc cube, filled with an ambient medium of $10^{-5} \, \text{cm}^{-3}$. The haloes are truncated at a radius of 50 kpc, well-beyond the radial range considered in this paper, such that our analysis of the disc stability in unaffected by this artefact. All models are strictly identical, with total disc mass of $5.5 \times 10^{10} \, M_\odot$, a bulge mass of $0.3 \times 10^{10} \, M_\odot$. The only difference between the models is the relative mass of the stellar component and the gaseous disc, controlled by the gas fraction defined as

$$f_{\text{gas}} = \frac{M_{\text{gas}}}{M_* + M_{\text{gas}}}.$$  (1)

where $M_*$ sums the masses of the stellar disc and the bulge. (The bulge to total ratio remains the same in all models.)

We setup 3 models, with initial gas fractions of 15, 50, and 70 per cent. Because of star formation and outflows, and the lack of cosmological accretion, this fraction naturally decreases with time. After a relaxation phase of $\approx 100$–150 Myr, instabilities caused by the artificial initial conditions have vanished, and the star formation rate (SFR) stabilizes at $\approx 10$, 80, and 130 $M_\odot$ yr$^{-1}$, respectively. This epoch is used for all our analyses. The gas fractions in the discs (i.e. in a slab covering $\pm 2.5$ kpc above and below the mid-plane of the disc, i.e. 5 times the scale height of the disc in the initial conditions) at the epoch of analysis are approximately $f_{\text{gas}} = 10$, 25, and 40 per cent, and are used below to name the models: $\mathcal{F}10$, $\mathcal{F}25$, $\mathcal{F}40$. When measured in a sphere of 10-kpc radius, i.e. including coronal gas and stellar spheroid, these fractions are 15, 30, and 50 per cent. The stars formed out of gas during the simulation (as opposed to stars in the initial conditions) represent 3, 30 and 50 per cent of the stellar content of the discs, respectively.

To evaluate the fraction of atomic (H I) and molecular hydrogen (H$_2$), we use the cooling tables from RAMSES under the assumptions of collisional ionization equilibrium in each individual cell to determine the ionization level. Then, in the neutral medium, the H$_2$ fraction is computed using the Krumholz, McKeen & Tumlinson (2009) formalism. We then measure molecular gas to stellar mass ratios of 6, 15, and 30 per cent in our three simulations in the snapshots considered.

These simulations are not tailored to depict three evolutionary epochs of the same galaxy. For instance, the disc of a given galaxy is expected to grow radially between the epochs where its gas fraction is 40 and 10 per cent (Kretschmer, Agertz & Teyssier 2020; Agertz et al. 2021). Instead, the models presented here are rather part of a controlled experiment, where as few parameters as possible are changed between runs (in our case, only the initial gas fraction). For the same reason, we chose to consider three different simulations rather than a unique one studied at different epochs. Our simulations are therefore not directly probing an evolutionary effect, but rather the influence of a given parameter, which happens to evolve with redshift along galaxy evolution.

3 DISC STRUCTURE

3.1 Morphology

The gas and stellar density maps of the simulations at the epochs analysed are shown in Fig. 1. The different gas fractions lead to different disc structure, at both small and large scales. In $\mathcal{F}10$,
a grand-design spiral structure appears beyond the central kpc. However, spiral arms are not in place at higher gas fractions ($F_{25}$, $F_{40}$); the morphology there is rather dominated by less-organized gaseous and stellar clumps spanning a large range of sizes, and at no particular location within the disc. This resembles the morphology of clumpy discs, observed to be gas-rich galaxies at $z \sim 1–3$ (e.g. Adamo et al. 2013).

We note that all our discs contain cloud/clumps connected by elongated features. The main difference between the gas fractions is the relative importance of the two types of structures (spirals/elongated arms versus clouds/clumps). At low gas fraction, the elongated arms are clearly identifiable as spiral arms, and connect virtually all overdensities, as so-called beads on a string (Elmegreen & Elmegreen 1983, 2019; Renaud et al. 2013; Elmegreen, Elmegreen & Efremov 2018). The sizes of these clouds and stellar clumps appear to be capped by the width of the spiral arms, and thus set by a large-scale instability process. However, in the two gas-rich cases, the elongated features are sub-dominant with respect to massive, yet local, structures made of gaseous and stellar clumps. There, the sizes of clumps appear to be independent of their surroundings, suggesting that a local, sub-kpc process of instability plays a bigger role.

Contrarily to the spiral arms in $F_{10}$, the elongated structures have less-coherent orientations and lengths across the $F_{25}$ and $F_{40}$ discs. Their density profiles are also much shallower than that of the thinner spiral arms. This is largely due to the presence of an intermediate density medium in the interclump areas, while the interspiral arm medium of $F_{10}$ is significantly more diffuse and even absent in the molecular phase. A close examination of the morphology of the elongated features in $F_{25}$ and $F_{40}$ reveals that some of them, but not all, connect to clumps in the S-shape characteristic of tidal tails. Some of these tails form indeed from clump–clump interactions in the two gas-rich cases, which also participates in populating the interclump medium with intermediate density gas ($\sim 100 \, M_\odot \, pc^{-2}$ in both the atomic and molecular phases). This situation does not occur in $F_{10}$ where the clouds follow the organized motion of their spiral arm hosts, and very rarely interact.
three galaxies yield a power-law regime $\langle P \rangle \propto l^\alpha$ and the corresponding indices are indicated. Differences between the galaxies mostly appear at small scales (in the 3D regime of turbulence), and are caused by the response of the molecular phase to different instability regimes.

3.2 Scale-dependence of the gas structures

To quantify the differences in the organization of the ISM structure spotted by eye in the previous section, the top panel of Fig. 2 shows the power spectrum densities (PSDs) of the face-on gas surface density (atomic + molecular). The data in the grey-shaded area are likely affected by sampling issues due to our limited resolution, and is thus ignored in the interpretation. On the other hand, the largest scales shown here are close to the total size of the simulation volume, and thus suffer from undersampling.

At large and intermediate scales (from $\approx 150$ pc to $\approx 6$ kpc), the three galaxies yield a power-law regime $\langle P \rangle \propto l^\alpha$ with $\alpha \approx 1.5$, where $l$ is the spatial scale. This is compatible, yet a bit shallower, with the power spectra of H1 in the THINGS galaxies ($\approx 1.5$–2.5, Walter et al. 2008; Walker et al. 2014; Grisdale et al. 2017; Dib et al. 2021). While the different normalizations of the PSDs correspond to the different total gas masses, the similarity of the slopes for the 3 galaxies indicates that the organization of the ISM at these large and intermediate scales is largely independent of the gas fraction. Our results thus suggest that the variations of power spectra observed in real galaxies (notably at scales $\gtrsim 1$ kpc) are caused by other factors, possibly the mass and/or the size of the discs, and the inclination (see Dib et al. 2021, on the effects of inclination on the power spectra of H1 in simulated galaxies).

At $\approx 100$–150 pc, the PSDs transition into steeper regimes. Previous works showed that this transition corresponds to the scale-height of the disc, below which turbulence can develop inside the disc (i.e. at scales smaller than the disc scale-height) along the vertical dimension, in addition to the 2D modes in the plane of the disc (Elmegreen et al. 2001; Padoan et al. 2001; Dutta et al. 2009; Renaud et al. 2013). Since such turbulence has an imprint on the 3D structure of the ISM, its signature is also visible in projected maps, as shown here. At the epochs analysed, the gas component of our galaxies yields exponential scale-heights of 92, 145, and 170 pc, respectively, corresponding to the transition visible in the PSDs, and thus confirming this interpretation.

At scales smaller than the transition ($\lesssim 100$–150 pc), the PSDs of the three galaxies diverge: $F_{10}$ reaches a steep $\alpha \approx 4.0$, while the intermediate case ($F_{25}$) follows $\alpha \approx 2.3$. The power spectrum of the most gas-rich case ($F_{40}$) continuously gets steeper with decreasing scale, without converging towards a fixed value. It is, however, possible that it would converge at smaller scales, not accessible in our simulations. This divergence in slope indicates that the transition from large scales to small scales is not only caused by probing the 3D nature of turbulence, but that other mechanisms must be invoked at scales below $\sim 100$ pc. They also show that these mechanisms are scale dependent, and vary with the gas fraction.

To gather more clues on the origins of these differences, the bottom panel of Fig. 2 shows the PSDs of all the gas, of H1 only, and of H2 only, for the $F_{10}$ and $F_{25}$ cases, each normalized by their equivalent in the $F_{40}$ simulation. We first note that the relatively flat dotted curves indicate that the structure of H1 is comparable at all gas fractions, even at small scales. This phase, found typically at low-density, includes the outer envelopes of star-forming clouds, as well as the intercloud/arm regions.

Conversely, the PSDs of the H2 component differ significantly between our cases, and carry most of the differences in the PSDs at small scales seen in the top panel ($\lesssim 100$–150 pc). Therefore, the differences in the organization of the ISM occur mainly in the molecular phase, and is partly connected to the 3D regime of turbulence within the disc scale-height. This corresponds to the visual impression of different morphologies between the molecular clouds at low gas fraction and the giant clumps for higher $f_{\text{gas}}$, and thus of differences in the structure of the star-forming material, and ultimately in the clustering of star formation and feedback.

The PSDs of the different phases highlight similarities between the two highest gas fractions ($F_{25}$ and $F_{40}$), while $F_{10}$ is significantly different. This hints to a transition regime in the structure of the ISM, particularly in the molecular phase, for gas fractions $\approx 20$ per cent (see van Donkelaar et al., in preparation, for another measurement of this value). Additional simulations would be required to establish the details of such a transition. We suspect, however, that such details depend on other parameters, like galactic mass and/or morphology. Such an extensive study is beyond the scope of this paper.

Apart from different cooling processes, there is a priori no reason for the molecular nature of the small-scale structures to be responsible for the organization of the ISM. Rather, the accumulation of dense and cold gas in large and deep potential wells allows for the assembly of dense, cold and partly self-shielded clouds and clumps, in which the gas becomes molecular. In other words, the variation in the molecular content of discs is more likely a consequence than a cause of the overall structure of the ISM. In this case, the differences in the molecular gas structure should be detectable as different instability regimes, varying with the gas fraction, i.e. a different imbalance between turbulent pressure support, rotation, and gravity. The results from this section also suggest different instability regimes between large and small scales. We explore and validate these hypotheses in the Sections 4 and 5.2.
3.3 Gas density distributions and the origins of high SFRs

The top-panel of Fig. 3 shows the probability distribution functions (PDFs) of the volume density of gas in our simulations. All three cases approximately follow a lognormal functional form, as expected from turbulence theory (Hennebelle & Falgarone 2012). The main differences between the galaxies are a slight excess of intermediate density gas ($\sim 10^2$ cm$^{-3}$) in the low gas-fraction case, corresponding to spiral arms, and the maximum density increasing with the gas fraction, but only by a factor of $\approx 2$ between the extreme cases. By examining the ratios of the PDFs in H I and H$_2$ (bottom panel), we find again similarities between the $\mathcal{F}$25 and $\mathcal{F}$40, specially in H$_2$ up to the highest densities, i.e. in the clumps themselves. More important differences are found with the lowest gas fraction. In particular, we note a deficit of diffuse H I in the gas-rich galaxies, with differences amplifying with decreasing density. This corresponds to the efficient launch of galactic outflows due to the more vigorous SFR in the gas-rich cases compared to $\mathcal{F}$10.

In H$_2$, the PDFs are similar up to $\approx 400$ cm$^{-3}$, but in the denser media, the two gas-rich galaxies yield a significant excess of dense molecular gas with respect to the $f_{\text{gas}} = 10$ per cent case. Such a medium is found in the central-most regions of the individual clouds and clumps. This excess is due to more numerous dense structures, and also significantly larger volumes of dense gas in the massive clumps of the gas-rich galaxies, as suggested by the power spectra (Fig. 2). For instance, the molecular phase denser than $10^3$ cm$^{-3}$ spans regions typically $\approx 100$ pc wide in $\mathcal{F}$40, but only $30$ pc in $\mathcal{F}$10, thus corresponding to a factor $\approx 40$ smaller in volume. Therefore, the molecular structures in gas-rich galaxies are not significantly denser than in galaxies with lower gas fractions, but span larger volumes, thus corresponding to larger masses.

Between our most extreme simulations, the SFR varies by a factor of 13 but this is balanced when normalizing by the gas mass: the depletion time ($t_{\text{depl}} = M_{\text{gas}} / \text{SFR}$) changes by only a factor of 3. Therefore, the gas fraction of disc galaxies has a much stronger influence on the SFR than on the depletion time. In other words, the higher SFR of the gas-rich galaxies, compared to the case at low gas fraction, originates from larger amount of star-forming gas, rather than a more efficient (or more rapid) star formation. Despite the SFRs of our gas-rich examples (respectively 80 and 130 $M_\odot$ yr$^{-1}$ in $\mathcal{F}$25 and $\mathcal{F}$40) being similar to that at the peaks of starbursts in local galaxy mergers (e.g. $\sim 100$ $M_\odot$ yr$^{-1}$ in simulated major mergers of galaxies in the mass range considered here, Renaud et al. 2014a), the shapes of their PDFs are radically different. In interacting galaxies, a burst star activity correlates with the presence of an excess of dense gas, i.e. larger amounts of dense gas and higher densities (Renaud et al. 2019). This excess of dense gas implies reduced depletion times, i.e. fast star formation, typically $\sim 10^{-2}$–$10^{-3}$ Gyr in the local Universe for the galactic masses considered here (e.g. Martínez-Badenes et al. 2012; Díaz-García & Knapen 2020). In our isolated discs, however, the galactic-wide depletion times are $\approx 10^2$–$10^3$ yr in $\mathcal{F}$10, $\mathcal{F}$25, and $\mathcal{F}$40, respectively, i.e. comparable to that measured in isolated systems at low and high redshift ($\approx 0.1$–1 Gyr, see e.g. Bigiel et al. 2010; Saintonge et al. 2011; Leroy et al. 2013; Tacconi et al. 2013). Therefore, similar SFRs are reached in isolated gas-rich discs by forming many stars, and in local starbursting mergers by forming stars fast. This confirms that different physical mechanisms are active and/or that a turbulence of different nature is present at cloud/clump scales in different galaxy types, even with similar SFRs (Renaud et al. 2014a). The star formation prescription adopted in our models (i.e. a fixed efficiency of a few per cents per free-fall time) is supported by observations of nearby clouds in the Milky Way (e.g. Elmegreen et al. 2002; Krumholz & Tan 2007), but could well be different in extreme environments like turbulent gas-rich discs. This would then alter the details of the star formation activity in the massive clumps. However, our conclusions remain qualitatively valid for any star formation relation with a superlinear dependence on the density, as widely accepted.

4 DISC INSTABILITIES

Since our three galaxies are setup with the same disc-bulge-halo combination and masses, the morphological and structural differences noted above result from the different relative importance of the dissipative component (gas) on the stability regimes of the discs. This section presents how instabilities arise.

4.1 Radial profiles and the failure of single-component stability criteria

Under the approximation of an infinitesimally thin disc, the stability parameter for the individual component $i$ (gas or stars) reads

$$Q_i = \frac{k \sigma_i}{\pi G \Sigma_i},$$

(2)

where $k$ is the epicyclic frequency, $\sigma_i$ the radial velocity dispersion, and $\Sigma_i$ the surface density (see Safronov 1960; Goldreich & Lynden-Bell 1965 on the parameter for fluids, and Toomre 1964 on that for stars$^1$). These three terms represent the rotational support of the disc, the pressure force, and the self-gravity of the $i$-th component.

$^1$For the stellar component, one must apply the collisionless version of the Boltzmann equation (sometimes referred to as the Vlasov equation, but see Henon 1982 for historical considerations) to the phase-space distribution function. In this case, the factor $\pi$ is replaced with the numerical value $\approx 3.36$ coming from the derivation of a modified Bessel function. In practice, the difference on the stability regime between using $\pi$ and 3.36 is negligible (see Binney & Tremaine 2008, their fig. 6.13). We thus use the same numerical factor for all components.
Stability of galactic discs

Figure 4. Radial profiles of the surface densities (left), radial velocity dispersion (center), and $Q_i$ stability parameter (equation 2, right), for the atomic gas (top), molecular gas (middle), and stars (bottom). All quantities are measured on a scale of 700 pc, and radially binned at a scale of 1 kpc. The curves show the median value in each radial bin, and the shaded areas indicate the 1σ robust dispersion of the velocity dispersion.

respectively. Under this formalism, discs are traditionally considered unstable where $Q_i ≤ 1$.

To apply this formalism to our models, we adopt the resolution of 700 pc to post-process our simulations. The motivation for this scale is two-fold: (i) it corresponds to the typical resolution of the THINGS and HERACLES surveys of nearby disc galaxies (Walter et al. 2008; Leroy et al. 2009) and is within the range of large integral field spectroscopic surveys (e.g. SAMI: Croom et al. 2012; CALIFA: Sánchez et al. 2012; MaNGA: Bundy et al. 2015), and (ii) it fulfills the requirement of the formalism for the $Q_i$ parameters that the scales considered (here, 700 pc) are significantly greater than the scale-height of the discs (100–350 pc).

Fig. 4 shows the radial profiles of surface density, velocity dispersion, and $Q_i$ for the three components: atomic gas, molecular gas, and stars. All the quantities are derived using robust statistics, they are measured at the scale of 700 pc, and their profiles are binned at a scale of 1 kpc. To limit the numerical noise introduced when computing derivatives, the velocity curve of the galaxy is smoothed before computing $\kappa$ (using a Savitzky–Golay algorithm with a kernel size of 9 data points).

The density profiles of all components in all the discs are compatible with an exponential form. However, we note that such a profile is imposed in the initial conditions, and therefore the convergence toward the exponential shape cannot be rigorously demonstrated here (but see Elmegreen & Struck 2013; Struck & Elmegreen 2019).

Despite having a massive central clump, the gaseous components of the $F_{25}$ and $F_{40}$ cases yield shallower density profiles than at low gas fraction. The atomic component has a rather uniform distribution, and the radial variations are mostly seen in the molecular phase. The presence of the massive clumps introduces important local variations in the density profiles of H$_2$ at high $f_{gas}$, also seen in the stellar component but with lower amplitudes. Together with Figs 1 and 2, this confirms that the different morphologies caused by varying the gas fraction are mainly affecting the molecular gas and thus the young stars formed in these clumps.

The variations of $\sigma$ with galactocentric radius contradict the assumption of uniform velocity dispersions in disc galaxies (e.g. Obreschkow et al. 2016), and illustrates a process of disc heating (Goldbaum, Krumholz & Forbes 2015; Zhang 2016). This is particularly visible in the gas-rich cases, likely because of radial inflows of matter amplified by the presence of the massive clumps (Noguchi 1999; Dekel & Krumholz 2013). Interactions between gas flows and the clumps induce exchanges of angular momentum favoring inflow towards the galactic center. Conversely, in the $F_{10}$ galaxy with no clumps, a strong bar could in principle play a similar role (Emsellem et al. 2015; Romeo & Fathi 2015), but its absence in our simulation limits the radial inflow in $F_{10}$. The profiles of velocity dispersion are comparable to those observed in THINGS, HERACLES, and CALIFA galaxies (in H$_1$, see Tamburu et al. 2009, H$_1$ and H$_2$, see Romeo & Mogotsi 2017, and in the stars Mogotsi & Romeo 2019), with values of the other of a few 10 km s$^{-1}$, and variations of factors $≈ 2–5$ between the inner and outer galaxy. As noted for other quantities, the two gas-rich cases have similar behaviours, while the galaxy with a lower gas fraction stands apart.
The values and overall radial trends of the individual $Q_i$ are in qualitative agreement with those derived from observations at comparable resolution (his fig. 1, Romeo 2020), despite being slightly lower (because of surface densities higher than the observed average values). The profiles of $Q_i$ yield similar shapes and values in all our galaxies, showing that the differences in velocity dispersion discussed above are balanced by the gravitational term (surface density). For the gaseous components, the $\sigma$ variations in the profiles are similar in all three galaxies, but $Q_i$ has a significantly smaller dispersion in $\mathcal{F}25$ than in the gas-rich cases. This is driven by the higher SFR of the latter, where more young stars inherit the dynamical properties of the molecular gas, and increase the contrast with older populations. This however does not influence the overall profiles of $Q_i$, but only local values, at the positions of the star-forming clumps and young star clusters.

By ignoring the relative contribution of the three components to disc instability, this formalism cannot explain why our three cases yield different morphologies and structures, all other things being equal. Although appealing by their simplicity, the single-component stability parameter is unphysical at scales below the disc scale heights ($\lesssim 100–200$ pc), and thus out of the application range of the Safronov/Toomre formalism: it violates the assumption of infinitesimally thin discs. In addition to neglecting the multicomponent interplay as discussed above, applying equation (2) at this resolution would lead to unphysical results. Therefore, one must use another, more advanced, stability parameter.

4.2 Multicomponent stability analysis

For the rest of the paper, we adopt a different formalism for the stability analysis, as motivated by: (i) the need to account for multiple disc components, and (ii) the requirement of a parameter which is physically valid at scales below the disc scale heights.

4.2.1 Stability parameter and characteristic instability scale

To account for the different contributions of multiple components to the net stability regime of a galactic disc, Romeo & Falstad (2013) introduced the multicomponent parameter:

$$Q_{RF} = \left( \sum_{i} \frac{W_i}{\tau_i Q_i} \right)^{-1},$$

(3)

where $Q_i$ is the stability parameter of the $i$th component (equation 2). The term $\tau_i$ quantifies the stabilization effect due to the thickness of

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4This rigorously derived parameter differs from the Wang & Silk (1994) parameter ($Q_{WS} = Q_{RF}^{-1} + Q_{gas}$) by accounting for the thickness of the disc (through the term $\tau_i$, equation 4), and the different weights of the components (through the term $W_i$, equation 5), such that the net local dynamical regime is dominated by the most unstable component. See Jog (1996) and Romeo & Wiegert (2011) for discussions on the inaccuracy of the Wang & Silk parameter.
the disc, i.e. it increases the effective stability parameter $T_i Q_i$ of the $i$-th component when the matter is not vertically concentrated (Romeo 1994). It reads

$$T_i = \begin{cases} 
1 + 0.6 \left( \frac{\sigma_z}{\sigma_R} \right)^2, & \text{if } \left( \frac{\sigma_z}{\sigma_R} \right) \leq 0.5 \\
0.8 + 0.7 \left( \frac{\sigma_z}{\sigma_R} \right), & \text{else,}
\end{cases}$$

(4)

(see Romeo & Falstad 2013 for details and discussion on the accuracy of this parameter). The expression for $T_i$ accounts for the full diversity of cases observed in stellar discs (see Gerssen & Shapiro Griffin 2012; Pinna et al. 2018; Walo-Martín et al. 2021 on debated relations between $\sigma_z/\sigma_R$ and the morphological type of the galaxy).

In particular, the second case in equation (4) depicts systems tending towards highly isotropic kinematics, for instance when supported by dynamical heating and turbulence in the gaseous component and the young stars.\(^5\)

Finally, $W_i$ is used to attribute different weights to the components:

$$W_i = \frac{2 \sigma_m \sigma_i}{\sigma_m^2 + \sigma_i^2},$$

(5)

where $m$ identifies the component which locally dominates the net instability regime, i.e.

$$T_m Q_m = \min \{T_i Q_i\}.$$  

(6)

This formalism gives less weight to the components whose velocity dispersion is very different from the most unstable one. In this paper, we consider the three components $i \in \{ \text{HI, H}_2, * \}$ representing the atomic gas, the molecular gas, and the stars.

For both the Safronov/Toomre and the Romeo & Falstad parameters, a value greater than unity denotes stability, but only against axisymmetric perturbations, which explains why some galaxies are observed to have $Q > 1$ (Romeo & Mogotsi 2017). Invoking a higher threshold ($\geq 2–3$) is necessary to account for non-axisymmetric perturbations (Griv & Gedalin 2012), as well as for the dissipative nature of the gaseous components (Elmegreen 2011).

Once the component locally driving the instabilities is identified (as $m$, using equation 6), we compute the characteristic instability scale, i.e. the size of the region in which gravitational disc instabilities develop, as

$$\lambda_{RF} = \frac{2 \pi \sigma_m}{\kappa}.$$  

(7)

Contrary to the Safronov/Toomre $Q_i$, the $Q_{RF}$ parameter retains a physical meaning at scales below the disc scale height, since it is based on a dispersion relation that converges at small scales towards the Jeans regime of instability including rotation. Yet, it relies on the short wavelength and the epicyclic approximations (Binney & Tremaine 2008; Romeo & Falstad 2013). Appendix B shows that our simulations fulfill these important requirements in all regions of the galaxies, which validates these approximations.

Fig. 6 shows the radial profiles of $Q_{RF}$ and $\lambda_{RF}$. $Q_{RF}$ shows that the discs are marginally stable, with almost no radial dependence. We note an overall decrease of $Q_{RF}$ with increasing $f_{gas}$ at all radii.

\(^5\)In our galaxies, the ratio $\sigma_z/\sigma_R$ is almost everywhere greater than 0.5, and often greater than unity. This contrasts with observational data of nearby discs, and is probably caused by the high SFRs in our models, and also possibly by numerical heating.
be invoked, likely during the collapse and assembly phase of the clouds. These processes are highly non-linear, and thus cannot be included in a formalism like the one adopted here. Nevertheless, our results suggest different regimes of instabilities between low and high gas fractions, at least at the scales of their main morphological differences, i.e. below a few 100 pc.

As noted by Romeo & Mogotsi (2017) with observational data, the radial variations of $\sigma_i$ (Fig. 5) have a negligible impact on $Q_{RF}$, which remains flat over a large radial range. These authors, however, noted an important effect on the size of the unstable regions. This further calls for a local study to complement our analysis using 1D radial profiles. To this end, the top and middle rows of Fig. 7 shows the maps of $Q_{RF}$ and $\lambda_{RF}$ computed at a scale of 70 pc. These maps illustrate the azimuthal variations lost in the 1D radial profiles. Within the discs ($\leq 10$ kpc), the lowest values of $Q_{RF}$ coincide with the structures in molecular gas. In $F_{20}$, this corresponds to the spiral arms and the clouds they host, as expected. In this galaxy, this is also where $\lambda_{RF}$ reaches its local minima, with instability scalelengths shorter than 1 kpc. The structure of this unstable medium highlights a characteristic size of 240 pc (as found on a PSD of the maps of Fig. 7, not shown), set by the separation of the spiral arms.

The $F_{25}$ and $F_{40}$ cases show a number of features at scales greater than 1 kpc, notably at high $Q_{RF}$, and long $\lambda_{RF}$. These correspond to areas of low density between the clumps. Such underdensities result from disc dynamics (e.g. the interarm medium) and the vigorous stellar feedback that affects the distribution of gas at these scales. While the former is set by gravity and thus affects both the stars and the gas, the latter carves bubbles in the gas only, leaving the stellar component mostly unaffected. As a consequence, these two effects leave different signatures on $Q_{RF}$ and $\lambda_{RF}$: in underdensities caused by large-scale dynamics, both the stellar and gas densities are low, as well as the radial velocity dispersions. As a result, $Q_{RF}$ tends to be high while $\lambda_{RF}$ remains short (e.g. at $x, y \approx -3$ kpc, 3 kpc in $F_{25}$, and $-2$ kpc, 2 kpc in $F_{40}$). This corresponds to

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**Figure 7.** Maps of the $Q_{RF}$ stability parameter (equation 3, top), of the instability scalelength $\lambda_{RF}$ (equation 7, middle), and of the component dominating the instability regime (identified by the parameter $m$, equation 6, bottom). All quantities are computed at a scale of 70 pc. Contours in red indicate stellar surface densities of 3 and 300 M$_\odot$ pc$^{-2}$, to guide the eye.
long time-scales of the secular, adiabatic evolution of the disc (\( \sim 100–1000 \) Myr). Conversely, feedback bubbles are regions of low density gas, but without any particular deficit of stars. There, the expansion of the bubble and the turbulence injected by feedback increase the velocity dispersion isotropically, and thus also in the radial direction. Combined with the reduced density of gas, and the moderately affected density of stars, this leads to both \( Q_{\text{RF}} \) and \( \lambda_{\text{RF}} \) being high (e.g. at \( x, y \approx 2 \) kpc, \( 6 \) kpc in \( F'25 \), and 0 kpc, \( -2 \) kpc in \( F'40 \)). The time-scales associated with stellar feedback are usually significantly shorter than those associated with disc dynamics, and such differences could thus translate into different instability regimes, as illustrated in Section 4.2.3.

By using the two-component (gas and stars) framework for stability analysis from Romeo & Wiegert (2011) and Inoue et al. (2016) noticed that the material assembling into clumps lies in regions with \( Q > 1 \). This result is not directly comparable to ours, as it only concerns the clump material traced back to its origin before the formation of the clump, while we characterize the instabilities over the entire disc, independently of the fate of the gas. The gas that assembles into clumps evolves through a range of stability states, as gas recycling is set by disc dynamics and feedback. The time-scales of these cycles vary with local and global conditions (density gradients, coupling scale of feedback to the ISM, shear etc., see Semenov, Kravtsov & Gnedin 2017), such that the moment of the onset of clump formation varies from clump to clump, and from galaxy to galaxy. The (necessary) simplification of measuring the \( Q \) parameter at an arbitrary epoch before the assembly of the clumps also supposes that clumps form as the monolithic collapse of a single gas region, which might not be correct for all clumps (Behrendt et al. 2019; Renaud et al., in preparation).

By not separating the atomic and molecular phases, the \( Q \) parameter used in Inoue et al. (2016) underestimates the contribution of the molecular gas to the stability (see Romeo & Falstad 2013). Although this is probably negligible in the interarm medium at low gas fractions (which is almost exclusively atomic), it is not the case in the medium hosting the formation of clumps, i.e. the spiral arms at low \( f_{\text{gas}} \), and the interclump medium of gas-rich discs (see the next section). Our results confirm that material in between clumps can be found with \( Q_{\text{RF}} < 1 \), thus very likely the seeds of future clumps.

To explain their finding of \( Q > 1 \) in future clump material, Inoue et al. (2016) invoke external processes, of cosmological origin, like minor mergers, stream accretion and tidal compression as non-linear processes missing in the theoretical formalism, to explain the discrepancy with their simulations. While such effects are present in galaxies, particularly at high redshift, our study using isolated galaxies shows that they are not necessary to explain the formation of massive clumps, and that internal instabilities are sufficient to drive the formation of massive clumps.

**4.2.2 Drivers of instabilities**

The last row of Fig. 7 shows the maps of \( m \), identifying the component which dominates the instability regime (equation 6). Fig. 8 complements this analysis by showing, as a function of gas density, what fraction of mass lies in regions where the stability regime is driven by each component. At least \( \approx 50 \) per cent of the gas mass is in regions of \( m = \bullet \), at virtually all densities in the \( F'10 \) and \( F'25 \) galaxies. This confirms the prominent role of stars in driving instabilities in nearby spiral galaxies (Romeo & Fathi 2016; Romeo & Mogotsi 2017; Marchuk & Sotnikova 2018). The next section shows that the majority (but not all) of these stellar-driven instabilities are coupled with the gaseous phase, and thus that the stars can drive gaseous instabilities.\(^6\)

![Figure 8](https://example.com/figure8.png)

Figure 8. Fraction of the gas mass in regions where the instability is set by the atomic, the molecular and the stellar component, as a function of the gas density. Approximative distinctions between different media are shown at the top, for reference. While most of the mass is in star-driven instability regions, this fraction strongly depends on the density, and the gas fraction of the galaxy.

\(^6\)The formalisms of the stability parameters do not capture the full range of perturbations (e.g. non-axisymmetric), and thus the actual value of \( Q_{\text{RF}} \) cannot be quantitatively linked to the collapse of structures nor to the star formation activity. An approximate threshold of \( Q_{\text{RF}} \approx 2–3 \) is used to distinguish between stable (\( Q_{\text{RF}} \gtrsim 2–3 \)) and unstable (\( Q_{\text{RF}} \lesssim 2–3 \)) regions. The precise value of the critical stability level is still questioned (Romeo & Fathi 2015), since it is influenced by complex phenomena such as non-axisymmetric perturbations and gas dissipation, whose effects are difficult to quantify (recall Section 4.2.1). We rather focus here on relative differences between galaxies and media, in particular on which component is the least stable one.
that the assembly of massive clumps is favoured at high \( f \). The instabilities appear at larger scales in gas-rich cases, suggesting instabilities. There, higher gas fractions translate into larger \( Q \) density PDFs between the three galaxies in this regime (Fig. 3), indicates that a larger medium (again, the similarities in \( \lambda \) opposed to smaller clouds at low \( f \)) of gas density, separating the drivers of instabilities. The dependence on the gas fraction is mostly visible in the gas-driven instabilities (left and center).

Finally, Fig. 9 shows the median \( Q_{RF} \) and \( \lambda_{RF} \) as functions of gas density, separating the drivers of instabilities. The dependences on \( f_{gas} \) are mostly visible in the regions with gas-driven instabilities. There, higher gas fractions translate into larger \( Q_{RF} \) and \( \lambda_{RF} \), at virtually all densities, but particularly in the interclump medium (\( \sim 1–1000 \) cm\(^{-3} \)). As shown in Fig. 8, gaseous drivers are particularly important in this density range, corresponding to the material potentially available for the assembly of future clumps, and/or to fuel existing clumps with gas. Even in the most gas-rich cases, the values of \( Q_{RF} \) at these intermediate densities depict unstable regimes, and thus promote the assembly and collapse of gas structures. Furthermore, the increase of \( \lambda_{RF} \) with \( f_{gas} \) shows that the instabilities appear at larger scales in gas-rich cases, suggesting that the assembly of massive clumps is favoured at high \( f_{gas} \) (as opposed to smaller clouds at low \( f_{gas} \)). However, we recall that \( \lambda_{RF} \) is not a direct indicator of the size of future clumps, and that other, non-linear, regulation mechanisms intervene during the later stages of their formation. While the size of the clumps remains difficult to predict, the existence of large \( \lambda_{RF} \) at high \( f_{gas} \), yet with similar density PDFs between the three galaxies in this regime (Fig. 3), indicates that a larger \( \lambda_{RF} \) translates into more massive clumps. Here again, the similarities in \( \lambda_{RF} \) and the density PDF in the interclump medium of the two gas-rich galaxies (\( F^{25} \) and \( F^{40} \)) explains the resemblances in the masses of their clumps (see Renaud et al., in preparation).

In the regions with \( m = \star \), the picture is more complicated. At low densities (where stars are the main drivers of instability, recall Fig. 8), high values of \( Q_{RF} \) denote stable (in \( F^{25} \) and \( F^{40} \)) or marginally stable (\( F^{10} \)) media. In the interclump density range (\( \sim 1–1000 \) cm\(^{-3} \)), stellar-driven instabilities concern a smaller fraction of the mass, but lower values of \( Q_{RF} \) account for the unambiguous instabilities with \( Q_{RF} < 2–3 \) (i.e. below the stability threshold, as noted above), as also seen in the clumps themselves (\( \gtrsim 10^3 \) cm\(^{-3} \)). However, the associated scalelengths show no clear dependence on the gas fraction, further highlighting the role of the gas phase in driving the differences between molecular clouds and massive clumps.

To summarize, the stellar-driven instabilities concern the majority of the surface (Fig. 7) and the mass (Fig. 8) in all galaxies. The weakening, yet persistence, of this dominance even at high \( f_{gas} \) explains the clear, yet mild, global trend of \( Q_{RF} \) decreasing with \( f_{gas} \) noted in Fig. 6. However, it is preferentially the gas-driven instabilities that lead to the formation of the star-forming clumps from the gas at intermediate densities, and the scale of such instabilities correlates with the gas fraction.

### 4.2.3 Decoupling

From the analysis above, it remains to be established if instabilities driven by one component can affect the others. Fig. 10 shows the loci of the 70 pc \( \times \) 70 pc regions in the parameter plane for gas and star instabilities, i.e. the ratio of individual \( Q \) parameters for the molecular and stellar components, versus that of their velocity dispersions. In the shaded area, a component is dynamically too hot to respond to the instability driven by the other and is thus decoupled from the one driving the instability (Bertin & Romeo 1988; Romeo & Wiegert 2011, see Romeo & Falstad 2013 for details). 30, 18, and 9 per cent of the regions lie in the decoupled regime for \( f_{gas} = 10, 25, \) and \( 40 \) per cent, respectively, with approximately half of them in the stellar-dominated phase in each galaxies.

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**Figure 9.** As function of the gas density, median \( Q_{RF} \) (top) and \( \lambda_{RF} \) (bottom) in regions where the instabilities are driven by the atomic gas (left), the molecular gas (center) and the stars (right). The shaded area indicates the 1\( \sigma \) robust dispersion. Values at the edges of the density range shown suffer from low-numbers statistics. Clear dependences on the gas fraction are mostly visible in the gas-driven instabilities (left and center).
Figure 10. Parameter plane of gas and star dominated instabilities, with quantities measured in 70 pc × 70 pc beams. For clarity, only 1 per cent of the points are shown. The shaded area at small $s$ indicates the regime where the stellar and the molecular component are decoupled (see Romeo & Falstad 2013 for details). In the other regime, a given component responds to the instabilities driven by the other. Histograms in the top and right-hand panels indicate the distribution of regions for our three gas fractions, with dotted lines marking the median values, and error bars showing the robust standard deviation.

All the decoupled regions lie in the intermediate range of densities ($0.1–500 \text{ cm}^{-3}$). By comparing with the galactic-wide means at the same densities, we find that the decoupled regions yield a higher Mach number (by a factor $\approx 1.5–2.0$), in all galaxies. Similarly, the median $Q_{\text{RF}}$ and $\lambda_{\text{RF}}$ are slightly higher in the decoupled regions (by factors $\approx 1.2–2.5$ and $\approx 1.3–1.8$ respectively). Following the discussion in Section 4.2.1, this suggests that feedback plays an important role in the decoupling mechanism. Yet, the decoupled regions also yield a higher average shear$^7$ than the galactic-wide averages (by a factor $\approx 1.7–2.8$), which implies a contribution from large-scale dynamics too, like the differential rotation of the discs.

To explore this hypothesis further, Fig. 11 shows the position of the decoupled regions in the galaxies. In all three cases, they are found at the edge of dense regions (e.g. spiral arms and massive clumps). Furthermore, a visual inspection reveals that a majority of the decoupled regions are preferentially found on the trailing side of these dense structures (all galaxies spin counter clockwise). The only exceptions are decoupled regions within the central kpc, i.e. in a special dynamical environment not discussed here. In Fig. 10, we visually find more decoupled regions near the portions of spirals with a high pitch angle, but the absence of clear spiral structures in the gas-rich cases forbids firmly drawing comparable conclusions in these galaxies. Renaud et al. (2014b) showed that high pitch angles favour the organization of star-forming structures in beads-on-a-string along spiral arms, as opposed to spurs or feathers formed by Kelvin–Helmholtz instabilities at low pitch angles. Because of asymmetric drift, young stars from these regions tend to preferentially inject feedback on the trailing sides of the spirals (Renaud et al. 2013, their fig. 14). In other words, the role of large-scale dynamics noted above is to favour an efficient injection of feedback in specific regions, but it is ultimately the feedback itself that decouples the gas and stellar components.

However, most of the regions lie in the coupled regime of instability, i.e. with one component experiencing instabilities driven by the other. The projected distributions of points shown in the side panels of Fig. 10 indicates a correlation between $s = \sigma_{\text{H_2}} / \sigma_*$ and $f_{\text{gas}}$, compatible with the findings of Burkert et al. (2010) and Krumholz & Burkert (2010). The opposite trend exists with $q = Q_{\text{H_2}} / Q_*$, despite larger scatters. This further confirms that, while the importance of the stellar component in driving instabilities anticorrelates with $f_{\text{gas}}$, the high number of decoupled regions at low $f_{\text{gas}}$ (i.e. a large volume where stars are not directly affected by the gaseous instabilities, and thus by the variations of $f_{\text{gas}}$) explains the only weak evolution of the overall instability regime with $f_{\text{gas}}$ (as noted in Figs 8 and 7).

4.3 Effects of resolution and beam smearing

As shown in Figs 4 and 5, measuring quantities (densities, velocity dispersions) at large scales implies that distinct physical regimes could be blended together, thus skewing the results. Beam smearing is a well-known example of such a distortion caused by the contamination of the velocity dispersion by the differential rotation of discs (Davies et al. 2011; Bacchini et al. 2019; 2020; Ejdetjärn et al., in preparation).

To assess the severity of this problem, in this section we repeat our analysis of the instability regime of our models but using the quantities measured at scales of 700 pc (recall Fig. 4). Fig. 12 compares the maps of $Q_{\text{RF}}$ measured at 700 pc resolution, with those measured at 70 pc and then convolved with a Gaussian kernel of 700 pc. Doing so allows us to eliminate the effects of resolution (beam size), and rather identify the regions where the differences indicate a scale dependence of the physics of instabilities. The same exercise applied to $\lambda_{\text{RF}}$ is shown in Appendix C.

At first sight, the two sets of maps seem comparable as they show features with approximately the same morphologies and sizes. However, the maps of the differences (shown in the bottom row of Fig. 12) highlight important local variations. When focusing on the galactic disc (i.e. within the central $\approx 10$ kpc), the amplitude of the differences and the surface they cover increase with $f_{\text{gas}}$. In $\mathcal{F}10$, we find no clear correlation between the amplitude of the difference and the presence of structures like spiral arms and clouds (which host the lowest values of $Q_{\text{RF}}$, as noted in Fig. 7), suggesting big similarities in the physics of instabilities between the 70 and 700 pc scales. In other words, instabilities at low-gas fraction are mainly set by galaxy-scale dynamics (at least down to scales of 70 pc). At higher gas fraction, however, the maps of Fig. 12 yield important differences, in particular in the dense clumps, and irrespectively of the underlying values of $Q_{\text{RF}}$. This indicates that different physical regimes are probed when examining the discs at 70 and 700 pc, and thus suggests a transition scale between our two resolutions. We examine and quantify this in Section 5.2.

$^7$We evaluate the shear as the quadratic sum of the off-diagonal terms of the Jacobian matrix of the velocity field, computed with first-order finite differences over the scalelength of 70 pc. This quantity can be interpreted as the squared rotational frequency term of a local centrifugal force. See Renaud et al. (2015) for details.

$^8$For consistency, the maps at 700 pc are also convolved with the same Gaussian, to account for the non-zero effects of the wings of Gaussian distributions.
In all cases, the regions where the instabilities are decoupled are almost exclusively found in the areas of small differences between the two sets of maps. This confirms that the decoupling is not an artefact caused by our choice of resolution, but instead results from a real physical process. The preferential locations of these regions on the edges of large features seen on the bottom row of Fig. 12 indicate that the decoupling is closely associated with the transition between the two instability regimes suggested above. In Section 4.2.3, we showed that feedback plays a more important role in the decoupling than dynamical effects. Therefore, the change of instability regime is likely driven by hydrodynamics.

In summary, our approach shows that the differences between high resolution smoothed by large Gaussian kernel and low resolution are not only differences in the scatter around the mean quantity within each beam, but also a fundamental difference of the mean itself. As a result, smoothing out the fluctuations by increasing the beam size does not lead to the same values as directly measuring quantities over large beams. Therefore, this indicates that differences between high and low resolution are non only caused by small-scale variations within the beams, but also by fundamental physical differences between the instability regimes at small and large scales.

5 Scale-dependence of the instability regimes

5.1 Methodology

To evaluate the scale dependence of the instability regime in the discs, we centre our analysis on the galactocentric radius $R_0 = 4.5$ kpc, as indicated in Fig. 11. This radius is selected to probe a large variety of structures. To measure the relevant physical quantities, we select the volume between $R_0 - l/2$ and $R_0 + l/2$, and of height above the disc plane between $-l/2$ and $+l/2$, where $l$ is the scale considered in the analysis. In this volume, we define $N = [2\pi R_0 l]$ cylinders of diameter $l$ and height $l$, with their centres uniformly distributed in azimuth along the galactic circle of radius $R_0$. The cylinders do not necessarily coincide with sub-structures in the discs like clumps or spirals. In each cylinder, we measure the surface density $\Sigma$ and the radial velocity dispersion $\sigma$ of the gaseous and the stellar component. We then compute the median and robust standard deviation of the $N$ values of these quantities. Note that if a majority of the cylinders do not contain mass, as it is the case at small scales in H$_2$, these medians are null. We repeat the process by varying the scale $l$ between $l_{\text{min}} = 40$ pc and $l_{\text{max}} = 4$ kpc. Finally, we compute the derivative of the relations of the medians of $\Sigma$ and $\sigma$ with the scale $l$ to obtain the indexes $a$ and $b$ defined as

$$\Sigma \propto l^a \quad \text{and} \quad \sigma \propto l^b.$$  

This approach is similar to that in Agertz et al. (2015) who applied it to galaxies with low gas fractions. To avoid biases in our measurements, the cylinders are not centred on specific structures like clumps. In fact, since the interclump medium represents a large fraction of the surface of the disc, the cylinders are more likely found in between dense structures. Then, we expect high values of $a$ at scales where cylinders start to encompass clumps, especially in the molecular phase which shows stronger density contrasts than the smoother distributions of atomic gas and stars (recall Fig. 2).

5.2 Instability regimes

Based on the values of $a$ and $b$, Romeo et al. (2010, see also Romeo & Agertz 2014; Agertz et al. 2015) identified a set of instability regimes, the most important of which are briefly presented here.

(i) Regime A: $a < 1$ and $b < (a + 1)/2$. Pressure drives the evolution of the disc at small scales, gravitation at intermediate scales, and rotation at large scales. This corresponds to Toomre-like instabilities.

(ii) Regime A’: $a > 1$ and $b > (a + 1)/2$. Similar as before, as Toomre-like instabilities, but with the scales of dominance of pressure and rotation reversed.

(iii) Regime B: $b = (a + 1)/2$. The gravitation and pressure terms have the same dependence on scale, and thus the medium follows the virial scaling (i.e. $\sigma^2 \propto \Sigma$).

(iv) Regime C: $a < 1$ and $b > (a + 1)/2$. Self-gravity dominates the instability towards small scales, while pressure and/or rotation tend to stabilize the large scales (e.g. a cold, non-turbulent disc).

(v) Regime D: $a > 1$ and $b < (a + 1)/2$. Self-gravity dominates the instability towards large scales, while pressure and/or rotation tend to stabilize the small scales (e.g. a non-rotating, non-turbulent sheet).

Fig. 13 shows the dependence of the surface density and radial velocity dispersion with scale, and identifies the scales under regime A (Toomre-like). As reported by previous works (Romeo et al. 2010; Romeo & Agertz 2014; Agertz et al. 2015) and suggested by many of the results presented above, the instability regime evolves between...
the small and large scales. In our simulations, the details of this evolution are complex and vary between galaxies and components. However, we can highlight the general trend that the components lie in regime A at large scales, and transition to regime D at smaller scales. The transition scale between the two regimes varies with $f_{\text{gas}}$ for the atomic and stellar components. At low gas fraction, these components are in the Toomre-like regime down to small scales ($\sim 200$ pc in H$_1$, and down to our resolution limit in stars). At larger $f_{\text{gas}}$, this transition occurs at larger scales ($\approx 600$ pc in H$_1$, and $\approx 200$ pc and $\approx 800$ pc in stars for $F_{25}$ and $F_{40}$, respectively). This demonstrates that the transition between disc instabilities (at large $l$) and clump instabilities occurs at scales which increase with the gas fraction. This confirms that massive clumps in gas-rich discs are spatially more extended than clouds at lower $f_{\text{gas}}$.

The two gas-rich cases share, once again, similarities, especially in the gas components. The transition scale in the molecular phase is approximately independent of $f_{\text{gas}}$, which suggests that Toomre-like instabilities set the scales of the gas clumps in their atomic phase, but not in the molecular gas, confirming our findings of Section 4.2.2. Although the exact reason is difficult to identify, this could mean that collapsing or collapsed structures are dense enough to decouple from the dynamical influence of large-scale instabilities.

The regimes A', B, and C are almost inexistent in our simulations, and only found in a few measurements at the smallest scales: $l \leq 500$ pc in H$_2$ for A', and $l \leq 100$ pc in H$_1$ for C, and not for the stars. These measurements are subject to numerical noise and should thus be taken with caution, but we note a tendency of gravity to become the main driver of the response of the media at sub-cloud scales, at all gas fractions. If confirmed with simulations at higher resolution, this would indicate that the gas fraction of a disc galaxy only influences the instability regime leading to the formation and assembly of the clouds/clumps but that, once the clumps are formed, the instabilities within the clouds are always set by a dominance of...
Figure 13. Surface density (top) and radial velocity dispersion (bottom) of the gas (left) and the stars (right), as functions of scale $l$. Raw data is shown by points, with the shaded areas indicating the uncertainties, accounting for the sample size (i.e. the number of cylinders $N$). Solid lines are a smoothed version, for clarity. The solid horizontal lines indicate the range of scales under regime A of instability (Toomre-like), and the dotted line show that under the regime D. In all the components of all the galaxies (except for the stars in $F_{10}$), a transition between a disc-driven and a clump-driven regime of instability occurs at scales of a few 100 pc.

gravity, with only a mere regulation from turbulence. As noted in Section 4.2.2, this picture evolves when the clumps form stars and feedback increases the turbulence within the clumps. However, at this stage of the star formation process, the gas remains coupled to stellar-driven instabilities in the gas-rich galaxies.

In the interclump medium, we have shown that feedback plays a more important role in the decoupling than gravitational effects (Section 4.2.3). There, pressure stabilized the small-scales (regime D). This confirms that the change in instability regime is driven by hydrodynamics.

The existence of a transition scale of the instability regime at a few 100 pc explains the differences in physical regimes noted in Section 4.3 (between 70 and 700 pc, i.e. on each sides of the transition) for the gas-rich cases: since the massive clumps have sizes of the order of 1 kpc, a given beam can have a large fraction of its area in the clump-driven regime of instability. Therefore, measuring a single value of $Q_{RF}$ at 700 pc or an average of values measured at 70 pc do not lead to the same conclusion as shown in Section 4.3. At low gas-fraction, however, the stellar component lies in the same regime of instability at all the scales considered here. Since the stars are the main driver of instability in $F_{10}$ (Figs 7 and 8), the transition seen in the gas phases has only a weak impact on the results, which explains the weak dependence of the values of $Q_{RF}$ with the scale, as noted in Fig. 12.

From the absence of a clear transition-scale in the dominant component (stars) of our $F_{10}$ simulation, our results predict that the instability regime of contemporary, local disc galaxies can be correctly assessed observationally even at low resolution. The new and next generations of high resolution surveys of local discs could provide valuable insights on this aspect (e.g. Leroy et al. 2021). However, the transition from the disc-driven to clump-driven instability regime that we found at higher gas fraction calls for sub-100 pc resolution in high-redshift discs.

6 CONCLUSIONS

Using hydrodynamical simulations of isolated galaxies, we study the impact of the gas fraction on the dynamics of discs. Our main results are as follows:

(i) The scale dependence of the structure of the ISM at large scales ($\gtrsim 100$ pc) does not significantly depend on the gas fraction. Below this scale, however, in addition to a transition to the 3D regime of turbulence seen in all cases, gas-rich galaxies yield shallower power spectra than discs at low gas fractions. These differences arise in the molecular gas.

(ii) In comparison with local molecular clouds, the massive clumps of gas-rich galaxies are not significantly denser, but span larger volumes. Their star formation activity is thus not particularly more efficient, but only more productive (i.e. higher SFRs but similar depletion times).

(iii) Our results confirm the inadequacy of the Toomre-$Q$ criteria to assess the stability of realistic discs. They however validate the formalism of the multicomponent parameter of Romeo & Falstad (2013). Furthermore, this formalism allows to probe scales smaller than the disc scale-height, as now commonly done in observational surveys of nearby discs.

(iv) Most of the instabilities are driven by the stars, even at high gas fraction. However, the gas is the most unstable component in the interclump medium of gas-rich galaxies. While the formation of molecular clouds at lower gas fraction is set by stellar instabilities, the material available for the formation of massive clumps at high $f_{gas}$ lies in volumes where instabilities are preferentially driven by the gas. This remains valid during the assembly phase of the clumps, until star formation starts.

(v) After the onset of star formation, feedback originating from the high SFR strongly strengthens the turbulence support within massive clumps, which tends to stabilize the gaseous phase. Then, the stellar...
component takes over as the driver of instabilities. The stellar and gaseous instabilities in the clumps are coupled, meaning that the gas reacts to the driving from the stars. In turn, this maintains the star formation activity in the clumps, despite high levels of feedback.

(vi) Decoupling between the stellar and gas phases occurs at the edge of dense regions, where feedback increases the gas velocity dispersion without significantly altering the stellar component. This process appears to be particularly efficient on the trailing side of spiral arms with high pitch angles, indicating an indirect role of the galactic-scale dynamics.

(vii) A too low resolution can lead to a misinterpretation of the stability regime of galaxies, in particular in gas-dominated discs. Since gas-rich disc galaxies are found at high redshift and thus observed with limited angular resolution, our results are a word of caution for the interpretation of the dynamics of clumpy galaxies inferred from observations. They also advocate against direct comparisons between studies at different spatial resolutions, for instance using gravitational lensing.

(viii) A transition is found in the instability regime of all galaxies, at a few 100 pc. At large-scale, disc dynamics sets a Toomre-like regime of instabilities, while the cloud/clump-driven regime takes over at smaller scales. This is particularly important in the clumpy galaxies, but is mitigated at low gas fraction, where the (dominant) stellar component lies in a disc-driven regime at all scales.

(ix) On almost all the aspects studies in this paper, we note strong resemblances between our two gas-rich cases, while the galaxy at low gas fraction systematically stands apart. Therefore, an important change in the instability regime, of the dynamics and of the structure of disc galaxies occurs for \( f_{\text{gas}} \approx 20\% \). This allows for the transition from clumpy turbulent discs towards spiral galaxies.

Our results, in particular on the variation of the physics regimes probed at different resolution, provide insights for the observational programs able to capture this range of scales (e.g. PHANGS-ALMA; Leroy et al. 2021). They also warn that these questions become even more critical in gas-rich disc galaxies as found at redshift \( z \approx 1–3 \), and that limited resolution for such distant objects could cause severe misinterpretations on the physical state of the systems.

By varying the gas fraction in our disc galaxies, we mimic the evolution of one property of galaxies across cosmic time. In principle, one could translate the gas fractions of our simulation into epochs of galaxy evolution, and even redshift, by comparing them with the fraction reported in observational surveys. However, the lack of cosmological context and thus of a self-consistent evolution of the galaxies forbids us to draw firm conclusions on the exact nature of the transition from the clump-dominated phase of galaxy evolution in gas-rich discs, and the spiral-dominated phase at lower gas fractions (see also Elmegreen & Elmegreen 2014). Although our controlled experiments highlight the impact of a specific parameter on the dynamics, other aspects like the disc growth, gas accretion, and galaxy mergers would draw a more complex picture. Our conclusions thus call for further studies, both observational and theoretical, on the onset of the secular regime of disc galaxy evolution.

**ACKNOWLEDGEMENTS**

We thank Bruce Elmegreen, Andreas Burkert, Angela Adamo, and Kearn Grisdale for their constructive input, and the referee for a detailed report. FR and OA acknowledge support from the Knut and Alice Wallenberg Foundation. OA acknowledges support from the Swedish Research Council (grants 2014-5791 and 2019-04659). The simulations have been performed on the Tetralith supercomputer hosted at NSC and accessed through a SNIC allocation.

**DATA AVAILABILITY**

The data underlying this article will be shared on reasonable request to the corresponding author.

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APPENDIX A: INITIAL CONDITIONS

Table A1 lists the initial conditions given to the MAGI code to setup the models.

| Parameter | Value |
|-----------|-------|
| Dark matter halo (NFW) | |
| Mass \([10^{10} \text{ M}_\odot]\) | 65.0 |
| Scale length [kpc] | 28 |
| Truncation radius [kpc] | 50 |
| Bulge ( Hernquist) | |
| Mass \([10^{10} \text{ M}_\odot]\) | 0.3 |
| Scale radius [kpc] | 0.4 |
| Truncation radius [kpc] | 10 |
| Discs (exponential) | |
| Total mass \([10^{10} \text{ M}_\odot]\) | 5.5 |
| Stellar mass \([10^{10} \text{ M}_\odot]\) | 4.6 |
| Gas mass \([10^{10} \text{ M}_\odot]\) | 0.9 |
| Scale radius [kpc] | 3.0 |
| Scale height [kpc] | 0.5 |
| Truncation radius [kpc] | 20 |

Table A1. Initial conditions. The three values correspond to the \(F^{10}, F^{25}, \) and \(F^{40}\) models, respectively.
Figure B1. Validation of the short-wavelength and epicyclic approximations, at high (left) and low resolution (right). In the high resolution case, only 1 per cent of the points are displayed, for clarity. All regions lie above unity, and more than 95 per cent are above 10 (see equation B1).

**APPENDIX B: SHORT-WAVELENGTH AND EPICYCLIC APPROXIMATIONS**

Fig. B1 demonstrates the validity of our approach on the instability analysis, by showing that the simulations fulfill the short-wavelength and the epicyclic assumptions. The former states that the inverse of the characteristic instability wavenumber should be much smaller than the galactocentric radius, i.e. $\lambda_{RF} / 2\pi \ll R$ (see Romeo & Falstad 2013). The latter imposes that the characteristic velocity dispersion is negligible with respect to the epicyclic velocity, i.e. $\sigma_m \ll \kappa R$. Equation (7) shows that these two conditions are equivalent, and can written as

$$\frac{2\pi R}{\lambda_{RF}} = \frac{\kappa R}{\sigma_m} \gg 1. \quad \text{(B1)}$$

Fig. B1 shows that all regions from our stability analysis fulfill this condition, at both high and low resolution, and for all gas fractions: more than 99 per cent of the regions having a ratio greater than 3, and more than 95 per cent are above 10. Therefore, this validates the short-wavelength approximation made in the stability analysis.

**APPENDIX C: $\lambda_{RF}$ AT LOW RESOLUTION**

Fig. C1 shows the comparison between high and low resolution maps of the $\lambda_{RF}$. As noted for $Q_{RF}$ (Fig. 12), the differences found here depict a change of the physical regime of instabilities between the two scales considered.
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Figure C1. Same as Fig. 12, but for $\lambda_{RF}$. 

MNRAS 508, 352–370 (2021)