Interacting dark matter and modified holographic Ricci dark energy plus a noninteracting cosmic component

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We investigate a spatially flat Friedmann-Robertson-Walker universe that has an interacting dark matter, a modified holographic Ricci dark energy (MHRDE), plus a third, decoupled component that behaves as a radiation term. We consider a nonlinear interaction in the dark component densities and their derivatives up to second order. We apply the $\chi^2$ method to the observational Hubble data for constraining the cosmological parameters and analyze the amount of dark energy in the radiation era for both MHRDE and holographic Ricci dark energy models. The former is consistent with the bound $\Omega_{\gamma}(z \approx 1100) < 0.1$ reported for the behavior of dark energy at early times while the latter does not fulfill it.

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I. INTRODUCTION

The current lore of modern cosmology indicates that 95 % of the matter-energy in the Universe is harbored in the dark sector composed of dark matter (DM) and dark energy (DE) \cite{1, 3}. Observations suggest that DM is a substantial nonbaryonic component that would be responsible for structure formation in the Universe \cite{3}. Likewise, DE has been the cornerstone of modern cosmology ever since the measurements of supernova type Ia have confirmed its central role in explaining the current speeding up of the Universe \cite{1}. The existence of DM and DE have been supported by observations such as cosmic microwave background and power spectrum of clustered matter among other probes \cite{1, 4}. Here we will work within the framework of dynamical DE by taking into account DE ansatz, $\rho_x$, the modified holographic Ricci dark energy (MHRDE) based on the holographic principle \cite{2}. The holographic DE model assumes that the quantum zero point energy density $\rho_{\Lambda} = 3c^2M_p^2/L^2$ is equal to DE density $\rho_x$ \cite{2}, being $L$, an infrared cutoff that will be related with a cosmological length \cite{7, 8, 10, 11, 12, 13}.\footnote{Electronic address: \texttt{chimento@df.uba.ar}}

Despite the lack of microscopic theory to describe DM and DE, their existence offers some of the most compelling evidence for physics beyond the standard paradigm. However there is an unavoidable degeneracy between DM and DE within Einstein’s gravity. There could be a hidden nongravitational coupling between them without violating current observational constraints, and thus, it is interesting to develop ways of testing different kinds of interactions in the dark sector.

The fraction of DE at recombination era should fulfill the bound $\Omega_{\gamma}(z \approx 1100) < 0.1$ in order for the DE model be consistent with the big bang nucleosynthesis (BBN) data. Uncovering the nature of DE, as well as its properties to high redshift, could serve as an invaluable guide to the physics behind the recent speed up of the Universe \cite{1}. Current and future data were examined for constraining the amount of dark energy at early times, and the data analyzed has led to an upper bound of $\Omega_{\gamma} < 0.043$ with 95% confidence level (C.L.) in case of relativistic early dark energy, while for a quintessence type of EDE has given $\Omega_{\gamma} < 0.024$, and although the DE component is not preferred, it is also not excluded from the current data \cite{2}. Another forecast for the amount of EDE was obtained with the Planck and CMBPol experiments \cite{13}; by studying the stability of the value $\Omega_{\gamma}(a \approx 10^{-3}) \approx 0.03$, it was found that 1σ error coming from Planck experiment is $\sigma_{\gamma}^{\text{Planck}} \approx 0.004$, whereas the CMBPol improved this bound by a factor of 4 \cite{13}.

In the present work we investigate a Universe that has an interacting dark sector, and a decoupled component that could mimic a radiation term. We constrain the cosmic set of parameters by using the Hubble data and the severe bounds found for DE at early times.

II. THE MODEL

We will apply the holographic principle \cite{2} to a cosmological model \cite{6} associating the infrared cutoff $L$ with the modified Ricci radius, thus we take $L^{-2}$ in the form of a linear combination of $\dot{H}$ and $H^2$. After that, the MHRDE $\rho_x = 3c^2M_p^2L^{-2}$ \cite{7, 8, 10, 11}, becomes

$$\rho_x = \frac{2}{\alpha - \beta} \left(\dot{H} + \frac{3}{2}H^2\right). \quad (1)$$

Here $H = \dot{a}/a$ is the Hubble expansion rate, $a$ is the scale factor and $\alpha, \beta$ are free constants. Introducing the variable $\eta = \ln(a/a_0)^3$, with $a_0$ the present value of the scale factor and $\dot{\eta} \equiv d/d\eta$, the above MHRDE \cite{11} looks like

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a modified conservation equation (MCE) for both cold DM \(\rho_c\) and the MHRDE with constant equations of state plus a continuity equation for the decoupled component named \(\rho_m\),
\[
\rho' = -\alpha\rho_c - \beta\rho_x, \quad \rho'_m + (\omega_m + 1)\rho_m = 0, \quad (2)
\]
after using the Friedmann equation,
\[
3H^2 = \rho + \rho_m, \quad (3)
\]
where \(\rho = \rho_c + \rho_x\) is total energy density of the interacting dark sector and \(\rho_m = \rho_{m0}a^{-3(\omega_m + 1)}\). In connection with observations on the large scale structures, which seems to indicate that the Universe must have been dominated by nearly pressureless components, we assume that \(\rho_c\) includes all these components and has an equation of state (EOS) \(p_c = 0\) while for \(\rho_x\) and \(\rho_m\) we have \(\omega_x = p_x/\rho_x\) and \(\omega_m = p_m/\rho_m\), respectively. So that the whole conservation equation (WCE) for the dark sector becomes
\[
\rho' = -\rho_c - (\omega_x + 1)\rho_x.
\]
In addition, the compatibility between the MCE (2) and the WCE yields a linear dependence of the equation of state of the MHRDE plus the third component. The statistical analysis is based on the chi-square function of the Hubble data
\[
\chi^2(\theta) = \sum_{k=1}^{12} \frac{[H(\theta, z_k) - H_{obs}(z_k)]^2}{\sigma(z_k)^2}, \quad (11)
\]
where the \(\theta\) parameters are the cosmological set of parameters, \(H_{obs}(z_k)\) is the observational \(H(z)\) data at the redshift \(z_k\), and \(\sigma(z_k)\) is the corresponding 1σ uncertainty \(13\). Using Eqs. (2), (3), and (11) one gets the Hubble parameter in term of the redshift \(x = 1 + z\) and the relevant cosmological parameters
\[
\frac{H(z)}{H_0} = \left[1 - \Omega_{m0}(J + (1 - J)x^{3n(1 + \delta)}) + \Omega_{m0}x^{3\alpha}\right]^{1/2}, \quad (12)
\]
\[ J[\theta] = \frac{\Omega_{z0}\Delta - \alpha(1 - \Omega_{m0})}{(1 + \delta)(1 - \Omega_{m0})} + 1 \]  

(13)

where we have used that \( B(1 - J) = AJ \) and the flatness condition: \( 1 = \Omega_{z0} + \Omega_{c0} + \Omega_{m0} \). Now, we perform the statistical analysis by minimizing the \( \chi^2 \) function for obtaining the best-fit values of the random variables \( \theta = \{\alpha, \beta, \delta, n, \Omega_{z0}, \Omega_{m0}, H_0\} \). The best-fit parameters \( \theta_c \) are those values where \( \chi^2_{\min}(\theta_c) \) leads to the local minimum of the \( \chi^2(\theta) \) distribution. If the goodness condition (GC) \( \chi^2_{2, o.f} = \chi^2_{\min}(\theta_c)/(N-n) \leq 1 \) is satisfied then the data are consistent with the considered model \( H(z|\theta) \).

We will estimate two parameters and the rest of them will be taken as priors, this will be done until all parameters have been varied [Fig. 1], but for simplicity we will show some of these constraints only. As usual, in the case of two parameters, the 68.3%, 95.4% C.L. are made of the random data sets that satisfy the inequality \( \Delta \chi^2 = \chi^2(\theta) - \chi^2_{\min}(\theta_c) \leq 2.30, \Delta \chi^2 \leq 6.17 \) [Fig. 2].

The 2-dimensional CL obtained with standard \( \chi^2 \) function for two parameters is shown in Fig. 1 whereas the estimation of these parameters is briefly summarized in Table (I). In order to contrast the MHRDE ansatz with HRDE model, we performed the same estimation in both cases. We find the best-fit at \( \{n, H_0\} = (0.64, 73.606 km \text{s}^{-1} \text{Mpc}^{-1}) \) with \( \chi^2_{2, o.f} = 0.758 \) by using the same priors of the MHRDE ansatz except for the value taken by \( \alpha \). We also get the best-fit at \( \{\Omega_{z0}, H_0\} = (0.76, 73.81 km \text{s}^{-1} \text{Mpc}^{-1}) \) along with \( \chi^2_{2, o.f} = 0.760 \) [cf. Table (I)]. These findings show that both models are in agreement with the standard values of \( \Omega_{z0} \) and \( H_0 \) reported by the WMAP-7 project [17].

Using the pair \( \{n, H_0\} = (0.95, 74.09 km \text{s}^{-1} \text{Mpc}^{-1}) \) [Table (I)], we show in Fig. 2 the behavior of the decelerating parameter with the redshift; in particular, its present-day value is \( q_0 = -0.60 \), whereas for the HRDE model gives \( q_0 = -0.59 \), so both values are in agreement with the ones reported by the WMAP-7 [17]. In Fig. 2 we plot the density parameters \( \Omega_c, \Omega_\omega, \Omega_\Omega \) and find their present-day values for MHRDE model, namely, \( \Omega_{z0} = 0.73, \Omega_{m0} = 10^{-8} \), \( \Omega_{c0} \simeq 0.269 \), whereas HRDE ansatz leads to \( \Omega_{z0} = 0.79, \Omega_{m0} = 10^{-8} \), and \( \Omega_{c0} \simeq 0.208 \). The EOS for dark energy does not cross the phantom barrier \( \omega_x = -1 \), so the model does not exhibit a quintom phase.

We devote our attention to the behavior of DE at early times within the framework of interacting dark sector plus a decoupled third component. We begin by setting \( \alpha = 4/3 \) to get a radiation contribution in the total density, and, as is well known in the radiation era the stringent bound \( \Omega_x(z \simeq 1100) < 0.1 \) should be fulfilled by the model in order to be consistent with data coming from the recombination era. In the case of the HRDE model with \( \{\alpha, \beta, \delta, n, \Omega_{z0}, \Omega_{m0}, H_0\} = (4/3, -0.01, 0.01, 0.8, 0.76, 10^{-8}, 73.81 \text{ km s}^{-1} \text{Mpc}^{-1}) \) the fraction of DE is \( \Omega_x(z \simeq 1100) = 0.24 \); therefore, it does not satisfy this bound. For the MHRDE case, we take \( \{\alpha, \beta, \delta, n, \Omega_{z0}, \Omega_{m0}, H_0\} = (1.01, -0.01, 0.01, 0.9, 0.71, 10^{-8}, 73.94 \text{ km s}^{-1} \text{Mpc}^{-1}) \) along with \( \chi^2_{2, o.f} = 0.763 < 1 \). The latter case leads to an EDE with \( \Omega_x(z \simeq 1100) = 1.2 \times 10^{-8} < 0.1 \) that is consistent with both the bounds reported in [12], and with the future constraints achievable by Planck and CMBPol experiments [13] because at large redshifts we get some bounds for the DE such as \( \Omega_x(z \simeq 10^{10}) = 1.3 \times 10^{-27}, \Omega_x(z \simeq 10^{10}) = 5.8 \times 10^{-44}, \) and \( \Omega_x(z \simeq 10^{20}) = 7.23 \times 10^{-55} \). Then, taking into
account the third component as a radiation term or a nearly radiation contribution helped to validate our model concerning the present-day constraints, but also it shows that the value of the cosmological parameters selected are consistent with BBN constraints.

IV. CONCLUSION

We have considered a model of three components composed of an interacting dark sector with MHRDE and a noninteracting component. We have introduced a nonlinear interaction such that the dark mix interpolates between a cold DM regime at early times (after a radiation era) and a de Sitter phase in the far future.

In the case of 2D C.L., we have found that the MHRDE model leads to the best-fit at \((\Omega_m, H_0) = (0.71, 73.94\) km s\(^{-1}\) Mpc\(^{-1}\)) with \(\chi^2_{d.o.f} = 0.763\) [Fig.1] and Table 1, while the HRDE leads to a best-fit at \((\Omega_m, H_0) = (0.76, 73.81\) km s\(^{-1}\) Mpc\(^{-1}\)) plus a \(\chi^2_{d.o.f} = 0.760 < 1\). Both models are in agreement with the ones reported by the WMAP-7 project 17 and fulfill the GC. Using the best fit-value \((n, H_0) = (0.95, 74.09\) km s\(^{-1}\) Mpc\(^{-1}\)) [Table 1], we have shown that the behavior of the \(q(z)\) exhibits an accelerated phase at late times [see Fig. 2] and obtained that its present-day value is \(q_0 = -0.60\), whereas for the HRDE model yielded \(q_0 = -0.59\), so both values are in agreement with the ones reported by the WMAP-7. Since the HRDE model with \((\alpha, \beta, \delta, \eta, \Omega_x, \Omega_{m0}, H_0) = (4/3, -0.01, 0.01, 0.8, 0.76, 10^{-5}, 73.81\) km s\(^{-1}\) Mpc\(^{-1}\)) along with \(\chi^2_{d.o.f} = 0.760 < 1\), leads to an EDE \(\Omega_x(z \simeq 1100) = 0.24\), then this model does not fulfill the bound for EDE at the recombination era. On the other hand, for the MHRDE case we have taken \((\alpha, \beta, \delta, \eta, \Omega_x, \Omega_{m0}, H_0) = (1.01, -0.01, 0.01, 0.9, 0.71, 10^{-8}, 73.94\) km s\(^{-1}\) Mpc\(^{-1}\)) along with \(\chi^2_{d.o.f} = 0.763 < 1\). The latter case leads to an EDE \(\Omega_x(z \simeq 1100) = 1.2 \times 10^{-8} < 0.1\) which is consistent with both the bounds reported in 12, and with the future constraints achievable by Planck and CMBPol experiments 13.

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[1] A. G. Riess et al., Astron. J. 116, 1009 (1998).
[2] M. Tegmark et al., Phys. Rev. D 69, 103501 (2004).
[3] R. W. Schnee, [arXiv:1101.5205].
[4] D.J. Eisenstein, et al, Astrophys. J. 633, 560 (2005).
[5] S. D. Hsu, Phys. Lett. B 594 (2004) 1; M. Li, Phys. Lett. B 603 (2004) 1; R. Horvat, Phys. Rev. D 70 (2004) 087301.
[6] L.N. Granda, A. Oliveros, Phys.Lett.B 671 199-202 (2009).
[7] I. Durán and D. Pavón, Phys.Rev.D 83 023504 (2011).
[8] L. P. Chimento, M. Forte and M. G. Richarte, [arXiv:1106.0781].
[9] Luis P. Chimento and Martín G. Richarte Phys. Rev. D 84 123507 (2011), [arXiv:1107.4816].
[10] Luis P. Chimento and Martín G. Richarte Phys. Rev. D 84 123507 (2011), [arXiv:1107.4816].
[11] S. Carneiro, [arXiv:gr-qc/0206064]; Shinichi Nojiri, S. D. Odintsov, Gen.Rel.Grav. 38 1285-1304 (2006); S.del Campo, J.C. Fabris, R. Herrera, W. Zimdahl, [arXiv:1103.3441]; J. Lu, Emmanuel N. Saridakis, M. R. Setare, Lixin Xu, JCAP 1003 031 (2010); Masashi Suwa, Takanari Nihei, Phys.Rev.D 81 023519 (2010); A. Aviles, L. Bonanno, O. Luongo, H. Quevedo, Phys. Rev. D 84 103520 (2011); L. Bonanno, G. Iannone, O. Luongo, [arXiv:1101.5798]; Tian-Fu Fu, Jing-Fei Zhang, Jin-Qian Chen, Xin Zhang, Eur. Phys. J. C 72 (2012) 1932; Moulay-Hicham Belkacemi, Mariam Bouhmadi-Lopez, Ahmed Errahmani, Taoufiq Ouali, Phys. Rev. D 85 083503 (2012); Mariam Bouhmadi-Lopez, Ahmed Errahmani, Taoufiq Ouali, [arXiv:1104.1181]; Mónica I. Forte, Martín G. Richarte, [arXiv:1206.1073]; Luis P. Chimento, Mónica I. Forte, Martín G. Richarte, [arXiv:1206.0179]; Jianbo Lu, Yuting Wang, Yabo Wu, Tianqiang Wang, Eur. Phys. J. C (2011) 71 1800; Zhenhui Zhang, Song Li, Xiao-Dong Li, Xin Zhang, Miao Li, [arXiv:1204.6135]; Yi Ling, Wen-Jian Pan, [arXiv:1205.0299]; Yuting Wang, Lixin Xu, Phys. Rev. D 81 083523 (2010); Zhuo-Peng Huang, Yue-Liang Wu, [arXiv:1205.2130]; Yun Chen, Zong-Hong Zhu, Lixin Xu, J.S. Alcaniz, Phys.Lett.B 698 175-182 (2011); R. Horvat, Phys.Lett.B 693 596-599 (2010); Ahmad Sheykhi, Phys. Rev. D 84 107302 (2011); Sandro M. R. Michelelli, Phys. Rev. D 85 123536 (2012).
| Priors                                                                 | Best fits       | $\chi^2_{\nu}$ |
|-----------------------------------------------------------------------|-----------------|----------------|
| $(\alpha, \beta, \delta, \Omega_{x0}, \Omega_{m0}) = (1.01, -10^{-2}, 10^{-3}, 0.73, 10^{-8})$ | $(n, H_0) = (0.95, 74.09)$ | 0.766          |
| $(\alpha, \beta, \delta, n, \Omega_{m0}) = (1.01, -10^{-2}, 10^{-3}, 0.9, 10^{-8})$        | $(\Omega_{x0}, H_0) = (0.71, 73.94)$ | 0.763          |
| $(\alpha, \beta, \delta, \Omega_{x0}, H_0) = (1.2, -10^{-2}, 0.1, 0.73, 74.20)$         | $(n, \Omega_{m0}) = (0.63, 10^{-8})$ | 0.764          |
| $(\alpha, \delta, n, \Omega_{x0}, \Omega_{m0}) = (1.26, 0.1, 0.8, 0.73, 10^{-8})$       | $(\beta, H_0) = (0.09, 74.09)$ | 0.771          |
| $(\alpha, \beta, \Omega_{x0}, \Omega_{m0}, H_0) = (1.2, -10^{-2}, 10^{-3}, 0.73, 10^{-8}, 74.2)$ | $(\delta, n) = (0.1, 0.63)$ | 0.764          |
| $(\beta, n, \Omega_{x0}, \Omega_{m0}, H_0) = (-10^{-2}, 0.4, 0.73, 10^{-8}, 74.2)$     | $(\delta, \alpha) = (0.25, 1.37)$ | 0.766          |

TABLE I: Observational bounds for the 2D C.L. obtained in Fig. (1) by varying two-parameters.