High-energy emission as a test of the prior emission model for gamma-ray burst afterglows

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\textbf{ABSTRACT}

We study high-energy gamma-ray afterglow emission from gamma-ray bursts (GRBs) in the prior emission model, which is proposed to explain the plateau phase of the X-ray afterglow. This model predicts the high-energy gamma-ray emission when the prompt GRB photons from the main flow are up-scattered by relativistic electrons accelerated at the external shock due to the prior flow. The expected spectrum has the peak of $\sim 10–100$ GeV at around the end time of the plateau phase for typical GRBs, and high-energy gamma rays from nearby and/or energetic GRBs can be detected by current and future Cherenkov telescopes such as MAGIC, VERITAS, CTA, and possibly Fermi. Multi-wavelength observations by ground-based optical telescopes as well as Fermi and/or Swift satellites are important to constrain the model. Such external inverse-Compton emission may even lead to GeV–TeV gamma-ray signals with the delay time of $\sim 10–100$ s, only if the plateau phase is short-lived.

\textbf{Key words:} non-thermal—gamma rays: bursts

\section{1 INTRODUCTION}

High-energy gamma-ray emission from gamma-ray bursts (GRBs) has been expected for long years since EGRET detected several GRBs with GeV emission (e.g., Hurley et al. 1994). Recently, the Fermi Large Area Telescope (LAT) has detected high-energy ($\geq$ GeV) gamma rays from a fraction of GRBs (Abdo et al. 2009a; Abdo et al. 2009b; Abdo et al. 2009c). Those detections have given us not only clues to the prompt emission mechanism but also chances to test new physics such as the Lorentz-invariance violation predicted in quantum gravity theories (Abdo et al. 2009c). High-energy gamma rays can also be expected for afterglows. High-energy gamma rays from GRB 080916C, 090510 and 090902B could be attributed afterglow emission rather than the prompt emission (Kumar & Duran 2000; Ghirlanda et al. 2003; Gao et al. 2009).

Since the launch of the Swift satellite, early X-ray afterglow emission has been one of the mysteries. They are classified into three phases: the steep decay phase, the plateau phase and the normal decay phase (see, e.g., Nousek et al. 2004; O’Brien et al. 2006; Zhang et al. 2006; Dermer 2007; Genet et al. 2007; Ghisellini et al. 2007; Panaitescu 2007; Ulm & Beloborodov 2007). Various theoretical possibilities of high-energy emission have also been discussed by numerous authors, and modified forward shock models, where electrons accelerated at the shock lead to the synchrotron self-Compton (SSC) and/or external inverse-Compton (EIC) emission, have often been considered (see, e.g., Fan & Piran 2008, and references there in).

Recently, Yamazaki (2009) proposed an alternative model, in which the X-ray light curves can be explained by the difference between the X-ray onset time and the burst trigger time. This model is somewhat different from the prior activity model, where the interaction with the prior flow is important and the EIC emission can also be predicted (Ioka et al. 2004). In this work, we consider consequences of the prior emission model on high-energy emission. We show that multi-wavelength observations provide a useful test.

\section{2 THE PRIOR EMISSION MODEL}

Here, we briefly describe the prior emission model (Yamazaki 2009). This model is a kind of two-component
emission model, where prompt and afterglow emission are attributed to radiation from the main and the prior outflows, respectively. The behavior of light curves during the plateau phase is explained by the difference between the afterglow onset time and the trigger time. The onset time is usually set to the trigger time $t_0$ when the prompt emission starts, that is, $t_0 = 0$ is assumed. However, if $t_0 \neq 0$, the afterglow flux is written as $F_{AG} \propto t^{-\alpha_0} = (T + t_0)^{-\alpha_0}$. Since $F_{AG}$ is constant for $T < t_0$ and $F_{AG} \propto T^{-\alpha_0}$ for $T > t_0$, the light curve well matches the observed plateau phase as well as the subsequent normal decay phase. Here we assume that the prior outflow produces X-rays via external forward shock emission. Such a forward shock model is supported by the lack of spectral evolution across the transition from the plateau to the normal decay phase and the compliance of the “closure relations” in the normal decay phase after the transition (Liang et al. 2007a). However, it still has several problems in e.g., explanation of chromatic breaks, and avoiding too bright precursor emission (Yamazaki 2009).

In this model, the prior outflow is typically assumed to precede the main outflow producing the prompt emission, and then the afterglow is occurring during the prompt emission so that prompt photons are naturally up-scattered by electrons accelerated at the external shock as long as both jets are in the line of sight. The inverse-Compton emission is characterized by the EIC Compton Y parameter $Y_{EIC}$. Typical long GRBs have the luminosity of $L_{GRB} \sim 10^{51}$ erg s$^{-1}$ at the break energy of $E_b \sim 0.1$–1 MeV and the duration of $\Delta T \sim 10^{5.5}$ s, and then the expected EIC luminosity is very roughly written as $L_{EIC} \sim \min \left( \gamma_{EIC} L_{EIC, opt} \delta T, \Gamma_{EIC} \right)$, where $\gamma_{EIC} \approx \delta T / t_0 \sim t_s$ is the duration of the EIC emission (e.g., Fan et al. 2008). At $t_0$, by using the standard external forward shock model (e.g., Sari et al. 1998), we also obtain the bulk Lorentz factor of the prior outflow as $\Gamma \approx 4 \pi E_{\gamma,0} / m_e c^2$, and the external shock radius as $r \approx 2.3 \times 10^{15}$ cm $\sim \gamma_{EIC} E_{\gamma,0}^{-1/4} m_e^{-3/4}$, where $E_{\gamma}$ is the isotropic kinetic energy of the prior outflow and $n$ is the circumburst medium density. In the slow cooling case, $\gamma_{EIC} \sim \gamma_{EIC, opt}$, $Y_{EIC}$ can be approximated in the Thomson limit for $E < E_{K,1} \propto \gamma_{EIC} m_e c^2$ as $Y_{EIC}(E) \equiv \frac{e^{\gamma_{EIC} E}}{e^{\gamma_{EIC} E/2} + 1} \sim \gamma_{EIC} \tau_T$, where $E \sim \gamma_{EIC} m_e c^2$, $\gamma_{EIC} \sim (\sigma_T N_e/4\pi r^2)^{-1}$ is the Thomson optical depth, and $N_e$ is the number of electrons. However, the Klein-Nishina (KN) effect becomes important for $E > E_{K,1}$ and, in fact, we can see $\gamma_{EIC} E > \gamma_{EIC, opt}$. Then, in our case, the EIC emission at $E > E_{K,1}$ is dominated by radiation from electrons with $\gamma_e \approx E / \Gamma m_e c^2$ interacting with prompt photons with the energy of $E \approx \gamma_{EIC} m_e c^2 / E$ via the Thomson scattering. As a result, we have $Y_{EIC}(E) \equiv \frac{e^{\gamma_{EIC} E}}{e^{\gamma_{EIC} E/2} + 1} \sim \gamma_{EIC} \tau_T$, where $\gamma_e \sim \tau_T (\gamma_e / \gamma_{EIC})^{-p+1}$ for $\gamma_{EIC} \leq \gamma_e < \gamma_{EIC, opt}$ and $\gamma_e \sim \tau_T (\gamma_e / \gamma_{EIC, opt})^{-p+1}(\gamma_e / \gamma_{EIC, opt})^{-p}$ for $\gamma_{EIC} \geq \gamma_{EIC, opt}$, where $p$ is the spectral index of forward shock electrons. The resulting EIC emission is roughly expressed as (see, e.g., Guetta & Granot 2003; Nakar et al. 2009, for general discussions)

$$E_{EIC} \cdot F_{EIC}(E) \propto \begin{cases} \frac{E - \beta_t}{\beta_t} & (E < E_{K,1}) \\ \frac{E - \beta_t}{E_{K,2} - \beta_t} & (E_{K,1} \leq E < E_{K,2}) \\ \frac{E - \beta_t}{E_{K,2} - E} & (E_{K,2} \leq E) \end{cases}$$

(1)

where $E_{K,1} \equiv \Gamma \gamma_{EIC, m_e c^2}$ and $\beta_t \sim 1$ is the low-energy photon index of the prompt emission, and we have assumed the EIC cooling time by prompt photons, $t_{EIC}$, is long enough (see below). The electron minimum Lorentz factor $\gamma_m$ is estimated as $\gamma_{EIC} \sim 10^{14-1}$ at $t \sim 10^3$ s for typical GRB afterglows, where we can expect $E_{K,1} \sim 10 - 100$ GeV and $L_{EIC} \sim 10^{49}$ erg s$^{-1}$. The EIC emission discussed here is similar to that originally proposed for flares (e.g., Wang et al. 2006; Wei et al. 2006; Yu & Dai 2009). However, the KN effect is much more significant in our case, and the spectrum with the peak of $\sim 10 - 100$ GeV is different from that in flares. Note that the total radiation energy of the EIC emission cannot exceed the total electron energy input at the external shock of the prior outflow.

We are interested in the case where the EIC flux exceeds the SSC flux of the afterglow. Therefore, we need to estimate the SSC flux to see whether the EIC emission is observable or not. The characteristic energies in the SSC emission are obtained as (e.g., Sari & Esin 2001; Zhang & Mészáros 2001)

$$E_{SSC}^m \simeq 2.3 \times 10^3 \text{ eV } g_{-1}^4 \frac{1}{\epsilon_{-1}} \frac{1}{B_{\perp -2}} \frac{E_{\gamma,53}^3}{n_0^{-3/4}} t_4^{-3/4} t_4^{3/4}$$

(2)

$$E_{SSC}^\prime \simeq 2.2 \times 10^{10} \text{ eV } \epsilon_{-1}^2 \frac{1}{B_{\perp -2}} \frac{E_{\gamma,53}^3}{n_0^{-3/4}} (1 + Y)^{-4} t_4^{3/4}$$

where $\epsilon$ and $\epsilon_e$ are the fractions of the shock energy transferred to the downstream fields and non-thermal electrons, respectively, and $g(p) = \frac{1}{\sqrt{p}}$ for $p > 2$. For $\epsilon > \epsilon_e$, we have $Y \sim Y_{SSC} \sim \sqrt{(\gamma_{EIC, m_e c^2} / \epsilon_{-1} g(p))}$. (e.g., Sari & Esin 2001; Zhang & Mészáros 2001) unless the EIC cooling is more important than the synchrotron and SSC cooling. In the slow cooling case, the SSC spectrum is expressed as $F_{SSC} \propto E_{SSC}^{-\gamma/2}$ for $E_{SSC} < E_{SSC}$, $F_{SSC} \propto E_{SSC}^{-\gamma/2}$ for $E_{SSC} < E_{SSC}$ and $F_{SSC} \propto E_{SSC}^{-\gamma/2}$ for $E_{SSC} < E_{SSC}$. Here $F_{SSC}$ is the cutoff energy determined either by the pair-creation opacity or the KN limit (e.g., Zhang & Mészáros 2001). Note that only the first SSC component is important, since the second SSC component is typically negligible due to the KN suppression in the optically thin synchrotron scenario. The energy flux at the SSC peak is evaluated as

$$F_{E_{SSC}} \cdot F_{E_{SSC}} \simeq 9.7 \times 10^{-9} \text{ GeV cm}^{-2} \text{ s}^{-1} \frac{Y_{SSC}}{(1 + Y_{SSC})^{p/2}}$$

$$\times g_{-1}^2 \frac{1}{\epsilon_{-1}} \frac{1}{x_{-1} B_{\perp -2}} \frac{2}{3} \frac{E_{\gamma,53}^2}{t_4^{3/2}} D_{28}^{-2}$$

(4)

by which we normalize the SSC spectrum. The temporal behavior would change after the jet break time of $t_j \sim 10^5$ s (Rhoads 1999), but we focus on the behavior before $t_j$.

3 THE RESULTING GAMMA-RAY FLUX

In this work, we shall use the following approximate formula in order to calculate the EIC emission. The EIC flux observed at $t$ is written as (e.g., Aharonian & Atoyan 1993; Fan et al. 2008; Toma et al. 2009)

$$F_{EIC}(E) \equiv \frac{3}{2} \sigma_T (1 - \cos \theta) \int d\theta \int d\nu \frac{f_{GRB}(\nu)}{\nu^{\alpha + 1}} dN_e \int dy \frac{f_{GRB}(\nu)}{\nu^{\alpha}}$$

$$\times \frac{B_{\nu}}{4\pi} \left( 1 + \Gamma \theta^2 \right)^{\alpha}$$

$$\left[ 1 - 2y + 2y^2 + \frac{\xi^2}{2(1 - \xi)} \right]$$

(5)

where $y \equiv \frac{\xi_{-1} m_e c^2}{2(1 - \cos \theta) \nu} e^{\gamma_{EIC} E}$ and $\xi \equiv \frac{(1 + 1)(1 + \gamma_{EIC} E)}{2 \Gamma_{EIC} m_e c^2}$. Scattering angles $\theta$ and $\theta'$ of EIC photons are measured in the central engine frame and the comoving frame, respectively, and $\theta' (t) \equiv \frac{2\theta_{c,t} - \theta_{c,t}}{\theta_{c,t}}$ and $\theta_{c,t} \equiv \frac{\theta_{c,t}}{\xi_{-1}}$, where
we have considered that the duration of prompt emission 
\( \sim \Gamma \Delta T /[1 + z] \) in the comoving frame is smeared as 
\( \Delta' / c \simeq \Gamma /[1 + z] \). The EIC suppression factor \( f_{\text{EIC}} \) is
expressed as 
\[ f_{\text{EIC}} = \min \left[ 1, \left( \frac{1 + \beta_{b}}{1 + \beta_{b} / \Gamma} \right)^{1/2} \right], \]
which becomes important if the EIC cooling is more relevant than the
synchrotron and SSC cooling (e.g., Wang et al. 2004).
The function \( G(\varepsilon) \) represents the spectral shape of seed
prompt photons with energy \( \varepsilon \) in the comoving frame
(e.g., \( \varepsilon^{b} = (1 + z) E_{b}^{b} / 2 \Gamma \)), where \( G(\varepsilon) = \left( \varepsilon / \varepsilon^{b} \right)^{-\beta_{b} + 1} \) for
\( \varepsilon < \varepsilon^{b} \) and \( G(\varepsilon) = \left( \varepsilon / \varepsilon^{b} \right)^{-\beta_{b} + 1} \) for \( \varepsilon \leq \varepsilon^{b} \), respectively.
The jet opening angle \( \theta_{j} \) is also set to \( \theta_{j} = 0.1 \) for both
the prior and the main flows. As for the electron distribution
of the prior flow, we exploit the standard external
forward shock model (e.g., Sari et al. 1998) and adopt the
following parameter set: \( E_{b} = 10^{52.5} \) erg, \( n = 1 \) cm\(^{-3}\),
\( \epsilon_{e} = 0.1, \epsilon_{B} = 0.01 \) and \( p = 2.4 \). For the prompt
emission, the seed photon spectrum is assumed to be
a broken power-law spectrum with \( \beta_{b} = 1 \) for \( E < E_{b} \)
and \( \beta_{b} = 2.2 \) for \( E_{b} \leq E \). One might think that our
approximation using a broken power law is not valid,
since the prompt emission from some bursts such as GRB
090510 may have an extra component above \( \sim 100 \) MeV.
However, even if we take into account this, our results
are not changed because of the KN suppression at high
energies. The high-energy cutoff due to the pair-creation
is given by \( E_{\text{cut}} \sim 4 \) GeV \( (L_{\text{GRB}, 51}^{b})^{1/2} \Gamma_{14}^{1} \epsilon_{b}^{1/2} (1 + z)^{-1} \)
(e.g., Lithwick & Sari 2001; Gupta & Zhang 2008; Murase & Ioka 2008) and we assume that the cutoff behavior as \( 1/[1 + \gamma_{\gamma}(E)] \) for simplicity (Baring 2006).
The low-energy cutoff due to the synchrotron self-absorption
is given by \( E_{\text{aa}} \sim 60 \) eV \( (L_{\text{GRB}, 51}^{b})^{1/2} \Gamma_{14}^{1} \epsilon_{b}^{1/2} (1 + z)^{-1} \)
assuming that the radiative efficiency is order of unity
(e.g., Razzake et al. 2004). We consider the following two
parameter sets for the other quantities. One expresses
typical GRBs: \( L_{\text{GRB}}^{b} = 10^{51.5} \) erg s\(^{-1}\), \( \Delta T /[1 + z] = 10^{5.5} \) s,
\( E_{b} = 100 \) keV, \( \Gamma_{0} = 10^{2.5} \) and \( r_{i} = 10^{14} \) cm. The other
set expresses optically bright GRBs: \( L_{\text{GRB}}^{b} = 10^{49.5} \) erg s\(^{-1}\),
\( \Delta T /[1 + z] = 10^{15.5} \) s, \( E_{b} = 10 \) eV, \( \Gamma_{0} = 10^{2.5} \) and
\( r_{i} = 10^{15.5} \) cm. Such a case is also considered here,
because bright optical emission was observed for some
GRBs and the ratio of the optical flux to the gamma-ray
fluence \( \mathcal{R} \equiv \mathcal{F}_{\text{GRB}, 0.1} / \mathcal{F}_{\text{GRB}, 3} \) is \( \sim 10 \) for GRB
041219A (Vestrand et al. 2004) and \( \sim 100 \) for GRB
990123 (Briggs et al. 1999). In order to demonstrate
detectable cases, we hereafter show spectra and light
curves only for \( z = 0.3 \) with cosmological parameters
\( H_{0} = 71 \) km s\(^{-1}\) Mpc\(^{-1}\), \( \Omega_{M} = 0.3 \), and \( \Omega_{\Lambda} = 0.7 \).

Our results for the case of typical GRBs are shown in
Figs. 1 and 2. As is expected, the EIC peak is located at
\( E_{\text{KN}, 51} \sim 10–100 \) GeV. For this parameter set of \( \epsilon_{e} / \epsilon_{B} = 10 \)
and \( p = 2.4 \), the EIC flux is larger than the SSC flux
above \( \sim 10 \) GeV when \( 10^{2} \) s \( < T < 10^{3.5} \) s. The EIC
flux is suppressed for a while just after the trigger time,
because prompt photons interacting with relativistic elec-
trons come from backwards (\( \theta \sim 0 \)). Later, seed photons
enter the prior flow with the angle \( \theta \neq 0 \), which contribute
to the EIC flux. In Fig. 1, one can see that the KN
suppression is prominent above \( \sim 10–100 \) GeV and the EIC
peak is comparable to the SSC peak. The resulting spec-
tra are basically explained by Eq. (1). We can also see that
the duration of the EIC emission is \( \Delta t_{\text{EIC}} \sim t_{0} = 10^{2.5} \) s,
since the EIC emission lasts until we observe prompt pho-
tons entering the prior flow with \( \theta \sim 1/\Gamma \). It is expected
that Fermi can detect the SSC afterglow emission at \( \sim 0.1–1 \) GeV. For closer and/or energetic bursts, we could even see
the EIC bump in gamma-ray light curves at \( \sim 10 \) GeV. In
order to detect high-energy gamma rays with energy larger
than 10 GeV, more suitable detectors are Cherenkov tele-
sopes such as MAGIC, VERITAS and future Cherenkov
Telescope Array (CTA). Although no firm signals have
been hunted so far (Abdo et al. 2007; Albert et al. 2007;
Aharonian et al. 2009), fast follow-up observations are
important to test the model. Note that the attenuation for
the pair-creation process by the cosmic infrared background
becomes important at such high energies. In all the figures we
show, this attenuation is taken into account, using the low-IR model developed by Kneiske et al. 2004. Here, the pair echo emission is not included since it is beyond the scope of this work, although it could affect the observed afterglow emission if the intergalactic magnetic field in voids is weak enough (e.g., Razzaque et al. 2003; Murase et al. 2009).

In Figs. 3 and 4, our results for a optically bright burst are shown. When copious optical/ultraviolet prompt photons are emitted from the main flow, we may observe the EIC emission dominant over the SSC emission above \( \sim 10 \) GeV. Although the situation depends on parameters, our results have suggested that observations of high-energy gamma rays provide important clues to testing the model in which the EIC emission is naturally expected, as well as observations at X-ray and optical bands (Liang et al. 2009). The strategy for testing the model is as follows. First, we need to determine relevant afterglow parameters for the prior flow. When afterglows are well observed at X-ray and/or optical bands, the parameters such as \( p, \epsilon_B \) and \( \epsilon_e \) are determined in the context of the standard external forward shock theory. Furthermore, parameters on the prompt emission, such as \( L_{GRB} \) and \( E_b \), can also be determined from observations, so that the EIC emission can be predicted. Another uncertain parameter \( r_i \) does not change our results for typical GRBs as long as \( r_i < r \). In particular, when \( \epsilon_B/e_e \) and/or \( p \) are large enough, the EIC flux becomes relatively larger than the SSC flux. Detections of characteristic features such as the EIC bump may support this model. The EIC peak is typically located at \( \sim 10–100 \) GeV due to the KN effect. Therefore, ground-based gamma-ray observatories, such as MAGIC, VERITAS, High Energy Stereoscopic System Observatory (HESS), and CTA should be important, although very-high-energy gamma rays have not yet been observed so far for any GRBs (Abdo et al. 2007; Albert et al. 2007; Aharonian et al. 2009). However, the detection rate of both the EIC and SSC emissions may not be large, because the rate of bursts occurring at within \( z \sim 0.3 \) is estimated as \( \sim \)a few events per year (e.g., Liang et al. 2007b). The detection rate also depends on several factors such as the detector sensitivity and field of view.

We have calculated EIC spectra, assuming that both the jet opening angles and axes of the prior and main outflows are the same. As is discussed in Yamazaki (2009), it might not be the case to avoid the bright precursor emission. However, we can still expect the EIC emission. Even though the afterglow is dim in the early time, the prior outflow jet expands sideways, and the jet edge crosses the line of sight, so that the prompt photons from the prior outflow come to the observer through the prior outflow (independently of the prompt emission mechanism). In this case, the EIC emission occurs although the resulting flux is reduced by a factor of 2 at most. However, if the jet axes of the two flows are different and the prompt emission occurs at \( r_i \gg r \), then the EIC emission may not occur.

1 As long as the model is applicable. We may need to select bursts without chromatic breaks, since the model cannot explain them.

**Figure 3.** The same as Fig. 1, but for the optically bright GRB with \( L_{GRB} = 10^{59.5} \) ergs\(^{-1} \), \( \Delta T/(1+z) = 10^{1.5} \) s, \( E_b = 10 \) eV, \( \Gamma_0 = 10^{1.5} \) and \( r_i = 10^{15.5} \) cm.

**Figure 4.** The same as Fig.1, but for the parameter set used in Fig. 3.

In Figs. 3 and 4, we see again that the duration of the EIC cooling of electrons accelerated at the external shock is important, i.e., \( 2 \pi \Delta t > 1 \), so that the resulting spectra can be modified from the simpler estimate neglecting the EIC cooling (Sari & Esin 2003; Nakar et al. 2009). Furthermore, the afterglow emission itself would be affected by the EIC cooling and the SSC flux would also be suppressed. The EIC flux can dominate over the SSC flux above \( \sim 10 \) GeV. Hence, if the prior emission model is real, we should detect \( \sim \) GeV photons by Fermi and \( > a \times 10 \) GeV photons by Cherenkov telescopes such as MAGIC, for such optically bright bursts. It also allows us to test the model.

**4 SUMMARY AND DISCUSSION**

In this work, we have studied the EIC emission predicted in the prior emission model and demonstrated that the EIC flux can be larger than the SSC flux at around the end time of the plateau phase above \( \sim 10 \) GeV. Although the situation depends on parameters, our results have suggested that...
The EIC emission studied in this work might be useful as a test for other two-component models. For example, the EIC emission can also be expected in the late prompt emission model \cite{Ghisellini07}, which may be potentially important. In addition, high-energy gamma-ray afterglows might also be produced by hadronic mechanisms (for reviews, see Mészáros 2006, Zhang 2007, Fan & Piran 2008). This possibility is not in our focus, but it can be relevant if the baryon loading is large enough \cite[e.g.,][]{Peer05}. Further complications may arise by flares, references there in). Further complications may arise by flares, references there in). For suffi- ciently small $t_0$, the EIC process can be very efficient small $r$ leads to large $\delta_{\text{EIC}}$, so that the EIC luminosity can roughly become the maximum, i.e., the afterglow electron luminosity, as $L_{\text{EIC}} \sim L_{\gamma} \sim \epsilon_{\gamma} \delta_{\text{EIC}} \propto E_{\gamma} \sim 10^{55}$ erg s$^{-1}$ erg and $z \sim 1$. For sufficiently small $t_0$, the EIC process can be very efficient small $r$ leads to large $\delta_{\text{EIC}}$, so that the EIC luminosity can roughly become the maximum, i.e., the afterglow electron luminosity, as $L_{\text{EIC}} \sim L_{\gamma} \sim \epsilon_{\gamma} \delta_{\text{EIC}} \propto E_{\gamma} \sim 10^{55}$ erg s$^{-1}$ erg and $z \sim 1$. 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