La Thuile 2014: Theoretical premises to neutrino round table

F. Vissani

INFN, Laboratori Nazionali del Gran Sasso and Gran Sasso Science Institute - L’Aquila, Italy

ricevuto il 31 Luglio 2014

Summary. — This talk, dedicated to the memory of G. Giacomelli, introduced the round table on neutrinos held in February 2014. The topics selected for the discussion are: 1) the neutrinoless double beta decay rate (interpretation in terms of light neutrinos, nuclear uncertainties); 2) the physics in the gigantic water Cherenkov detectors (proton decay, atmospheric neutrinos); 3) the study of neutrino oscillations (mass hierarchy and \( CP \) violation; other neutrino states); 4) the neutrino astronomy at low and high energies (solar, supernova, cosmic neutrinos). The importance of an active interplay between theory and experiment is highlighted.

PACS 11.30.Fs – Global symmetries (e.g., baryon number, lepton number).
PACS 14.60.Pq – Neutrino mass and mixing.
PACS 95.85.Ry – Neutrino, muon, pion, and other elementary particles; cosmic rays.

Neutrino physics is in a healthy state. Among the reasons of this pleasant situation, there are the important results that have been achieved in that field, as well as the possibility of conceiving/conducting new valuable experiments, the numerous installations and experimental sites, the available sources of support and funding, etc. One specific circumstance that contributes to make neutrino physics still valid and appealing is the vibrant connection between theory and experiment. This is something that derives us from the early times of neutrino physics and that gives rise to a lively, sometimes messy, interdisciplinary field, where nuclear physics, particle physics and astrophysics are involved. In order to stress the importance of this connection in the way that it deserves, I would like to dedicate this talk to Giorgio Giacomelli, one of the best experimentalists we ever had, always open to discuss, to assess the value, and whenever necessary, to test the best ideas. Moreover, I open the list of references just as in my previous talk at La Thuile, namely, with the review article of B. Pontecorvo [1] that summarizes the history of neutrino physics before 1983 in 4 tables, whose titles are,

I: from radioactivity to neutrino discovery;
II: from muon properties to \( V - A \);
III: from high-energy neutrinos\(^{(1)} \) to the standard model;
VI: neutrino astrophysics, astronomy, cosmology.

\(^{(1)} \) This is the same of “artificial (or long baseline) neutrino beams” in the modern parlance.
Most of the lines of research listed in these four tables are still pursued, and among them we note:

I: Neutrinoless double beta decay

II: Neutrino oscillations

III: Proton decay? (the question mark is as in Pontecorvo’s review.)

VI: Solar, supernova, high-energy cosmic neutrinos.

In the following, we will recall the main facts occurred since Pontecorvo’s review article and mention some possibilities of further development.

1. Neutrinoless double beta decay

In this section, we describe the present theoretical understanding of a hypothetical nuclear physics process, namely, the neutrinoless double beta decay \( (0\nu\beta^2) \) process, and consider the most relevant pending questions.

The existing experimental results have been summarized by M. Agostini, with particular emphasis on the investigations using \(^{76}\)Ge. The study of this nuclear species allows us to exclude the occurrence of \(0\nu\beta^2\) transition with half-life smaller than few times \(10^{25}\) yr after collecting a total exposure nearing 100 kg \(\cdot\) yr for \(^{76}\)Ge(\(^{2}\)). Although this exposure is about one million times smaller than those collected in proton decay search, it is quite remarkable since it concerns a rather peculiar nuclear species.

1.1. Importance of the process. – From a phenomenological point of view, we can describe \(0\nu\beta^2\) as a nuclear decay in which a pair of leptons (electrons) are generated. In other words, the \(0\nu\beta^2\) is an example of lepto-genesis process potentially measurable in the laboratory.

The \(0\nu\beta^2\) is forbidden in the Standard Model (SM) of elementary particles by the conservation of the lepton number \(L\). But \(L\) is just an accidental symmetry of the SM. In the more complete models that respect the gauge symmetry of the SM, and that allow for non-zero neutrino masses, it is typically violated.

In the SM, the lepton number \(L\) and the baryon number \(B\) (or equivalently the quark number \(Q = B/3\)) have the same theoretical status. Therefore, the search of \(0\nu\beta^2\) has a comparable importance to the search of proton decay, another hypothetical process where, this time, the baryon number \(B\) is instead violated (see sect. 2). (Recall that the processes of creation and of destruction are deeply linked in quantum field theory.)

The matter is made of atoms, or at a more fundamental level, of baryons (quarks) and leptons. These fermions are generically referred to as “matter”, in contrast with the bosons that are the particles that carry the forces. In this sense, we can say the hypothetical \(0\nu\beta^2\) and the proton decay are processes where the matter is created and

\(^{2}\) This limit was obtained by combining the entire set of experiments. We remind that: 1) a subset of the Heidelberg-Moscow collaboration claimed the discovery, but the claim is not confirmed; 2) for \(^{136}\)Xe exposure and background are both larger; the results are similar to \(^{76}\)Ge.
destroyed (while, of course, mass is neither created in the $0\nu2\beta$ process nor destroyed in the proton decay). The observation of $0\nu2\beta$ or of proton decay, or, even better, of both, would allow us to proceed toward a dynamical explanation of the cosmic baryon excess, a theoretical program first formulated by A. Sakharov [2].

There are non-perturbative quantum processes that respect $B - L$ but violate the symmetry $B + L$ within the SM [3]. Since $0\nu2\beta$ violates $B - L$, one concludes that 1) this process is forbidden in the SM also at a non-perturbative level; 2) its observation would imply the existence of transitions that violate also $B$ at some level [3]. A link with the cosmological considerations mentioned above is quite plausible; indeed, it exists in several specific theoretical realizations of the program of Sakharov.

1.2. Connections with oscillations of ordinary neutrinos. – The discovery of neutrino oscillations (see [4,5] for reviews and sect. 3 for further discussion) and the consequent inference that the three ordinary neutrinos are endowed with mass, allow us to discuss in more concrete terms the rate of this process and to test the theoretical proposal of E. Majorana, namely, that neutrinos are real particles, just as the photon. More precisely, we wonder whether the neutrino mass eigenstates are real particles, which means to ask whether the masses $m_i \geq 0$ are included in the Lagrangian as $\sum_i m_i \nu_i^\dagger \nu_i / 2 + h.c.$ The combination of the three neutrino masses entailed by the $0\nu2\beta$ decay process is

$$m_{\beta\beta} = \left| \sum_{i=1}^{3} U_{e_i}^2 m_i \right|,$$

where $U_{e_i}$ are the mixing elements that define the electron neutrino state: $|\nu_e\rangle = U_{e_i}^* |\nu_i\rangle$. Unfortunately, oscillations probe only the absolute values of $|U_{e_i}|$, the squared mass difference between the closest mass levels $m_2^2 - m_1^2$; the remaining mass difference $m_3^2 - m_1^2$ is known up to its sign. In other words, we do not know whether $m_3$ is the heaviest state (normal hierarchy) or the lightest one (inverted hierarchy). Thus, a wide range of values for $m_{\beta\beta}$ are allowed, as shown in fig. 1 and as discussed in details in [6].

A priori, it is impossible to exclude the presence of other contributions to the transition rate. If the transition was observed, but the connection indicated by fig. 1 was not viable, an alternative interpretation would be necessary. But the first non-renormalizable operator that violates the lepton number implies Majorana neutrino masses and nothing else [7]. Thus, if the physics that explains neutrino masses is at very high energies and the subsequent (higher dimensional) operators are very suppressed, a one-to-one connection between the transition rate of the $0\nu2\beta$ and the Majorana masses holds true.

1.3. Nuclear physics aspects. – A major difficulty in the interpretation of this results arises when we convert the limit on the lifetime in terms of limit on the parameter $m_{\beta\beta}$, since this requires to describe precisely the nuclear structure of initial, final and intermediate nuclear species. This is summarized into a single adimensional parameter, the nuclear matrix element of the transition $M$. The half-life of the transition (connected to the rate $\Gamma$ by $T_{1/2} = \ln(2) \hbar / \Gamma$) is given by

$$\frac{1}{T_{1/2}} = G_{0\nu} \times M^2 \times \left( \frac{m_{\beta\beta}}{m_e} \right)^2,$$

where the first factor, called the phase space, has the dimensions of an inverse time; the electron mass $m_e$ is included only for convenience. For a long time, the researchers
believed that the uncertainties on $\mathcal{M}$ were as large as a factor of 2–3 [8]. This view was questioned when the first calculations with error-bars appeared [9], since they exhibited small errors.

Recently the old view returned in a new form. Indeed, it was shown that the smallness of the error depends essentially upon the assumption that the nucleonic charged current couplings, and in particular the axial coupling $g_A$, are known [10]. However, there are good reasons to believe that in the nuclear medium the value for this parameter is not the same as in vacuum, namely $g_A \approx 1.269$, but rather a more “quarkish” value $g_A \approx 1$; moreover, if the analogy with the double beta decay with two neutrino emission holds true, further downward renormalization is expected. The question of the renormalization in the nuclear medium should be considered a priority for this field of research, since $\mathcal{M}$ decreases approximately as $g_A^2$. As it is clear from fig. 1, it seems conservative to assume that the uncertainty on the matrix element is not small [10].

2. – Proton decay?

Here, we complete the discussion about proton decay and introduce the topic of neutrino physics with large water Cherenkov detectors.

2.1. NDE – or microphysics with the biggest detectors. – Various gauge models, such as $SU(5)$ and $SO(10)$, have motivated the search for proton (or nucleon) decay. Very stringent limits have been obtained by KamiokaNDE and Super-KamiokaNDE [11]; recall that the acronym NDE meant originally Nucleon Decay Experiment\(^\text{\textsuperscript{3}}\).

\(^\text{\textsuperscript{3}}\) Other experiments conceived in the same years, whose names remind us of the prevailing theoretical ideas, are the NUcleon Stability EXperiment (NUSEX) [12] and the Monopole, Astrophysics and Cosmic Ray Observatory (MACRO) [13].
After more than 30 years, the predictions remain rather vague, not only due to the nuclear matrix elements, but also due to the incomplete formulations of gauge models. In order to understand the nature of the theoretical difficulties, it is sufficient to think to the Higgs sector of the extended models or to the mass spectra of the various unobserved particles. Notice that a lot of discussion concerned the search for the mode

\[ p \rightarrow K^+ \bar{\nu} \] (4)

motivated by the assumption that supersymmetry is at the TeV scale, where the decay is caused by a loop diagram involving superheavy triplets and supersymmetric particles. Of course, the fact that supersymmetry is still unseen does not strengthen the motivations to search for this specific decay mode.

On the other hand, there are interesting ideas on how to investigate further decay modes as this one with new experiments. The sensitivity that could be reached is shown in fig. 2, from [14]. In water, the efficiency is 14.6%, obtained summing the 2 methods used by SuperKamiokaNDE, and the background rate is 14/(Mton x yr); in argon, the efficiency is 97% and the background rate is 1/(Mton x yr) [14]. Note that the impact of the uncertainty on the background is not included, but at present this is large and it is especially relevant for the Cherenkov detectors, since background events should be soon observed. Summarizing, we see that an Argon detector would permit us to proceed in the zero-background condition for more than an order of magnitude, until the first atmospheric neutrino event will appear (putting aside the possible statistical fluctuations and the discussion of the systematics).

2'2. Mton water Cherenkov detectors and beyond. – Independently of the original motivations, Cherenkov detectors reached excellent results by studying atmospheric neutrinos; today, the acronym NDE usually refers to Neutrino Detection Experiment. The
HyperKamiokaNDE [15], discussed in the contribution of M. Shiozawa, will investigate
CP by long-baseline oscillations, continuing also the study of atmospheric neutrinos and
proton decay, and doing much more: e.g., monitoring core collapse supernovae.

The mass of HyperKamiokaNDE will be a fraction of Mton. In this sense, it can be
compared with the largest detectors of this type ever conceived/imagined for the study
atmospheric neutrinos: the PINGU project in the IceCube site and the possible plan of a
similar setup in the Mediterranean sea (ORCA). We will discuss further these detectors
in the next section and come back on the IceCube detector in the last one.

3. – Neutrino oscillations

Oscillations progressed greatly since Pontecorvo’s review. The main achievements are

– The theoretical finding [16] that the propagation inside the matter (e.g., Earth,
  Sun, supernova) modifies the oscillations\(^\text{\(\text{\(4\)}\)}\). This is called “matter effect”.

– The discovery of several anomalies and the confirmation of two of them, leading to
  the determination of two differences of masses, as mentioned in sect. 1’2.

– The measurement of the three mixing angles of the ordinary three neutrinos.

Here, we discuss the general attitude of this field of research and then focus on the issue
of measuring neutrino mass hierarchy. Finally, we briefly discuss the possibility that
there are other neutrinos in addition to the three known neutrinos.

3’1. Measurements or discovery?. – The question on whether the study of neutrino
oscillations is mainly a way to discover something new or, rather, it is a tool to measure
the oscillations parameters of the ordinary neutrinos has a certain importance. In fact,
these two attitudes lead to put emphasis on different aspects of the discussion, and
consequently, to invest the efforts on different types of experiments. I feel inclined toward
the second point of view, as I have described in La Thuile 2003 [4], but one should be
aware that this is not a universal attitude.

For instance, the idea that \(\theta_{13}\) was zero, until the contrary was proved, has been
lingering in our field, influencing the discussions. Even now various colleagues like to
dub the observational fact \(\theta_{13} \sim \phi^\circ\) as “unexpected” in talks or in written works, often
without feeling the need to offer a reference in support of this opinion or to justify such
a view with a scientific argument. Of course, I would like to contrast this prejudice with
the attitude that \(\theta_{13}\) could be just below the experimental limit and possibly within
reach, as it was\(^\text{\(\text{\(5\)}\)}\).

This situation shows that theoretical opinions offer opportunities, but they can also
expose us to risks. A healthy research field has to be able to consider a multitude of
opinions, rather than passively suffering the effect of the prevailing one [18]. Furthermore,
it is essential to formulate clearly the motivations of any specific theoretical proposal, at
least, just to learn something from its failure.

\(^\text{\(\text{\(4\)}\)}\) In essence, this is an additional refraction effect acting on electron (anti)neutrinos, that
works together with the refraction acting on the neutrino mass eigenstates, due to their masses.

\(^\text{\(\text{\(5\)}\)}\) Curiously, this alternative attitude was supported by some theoretical models, where this
angle was argued to be close to the Cabibbo angle \(\theta_C \sim 13^\circ\), see e.g. [17]; evidently, other
ideas/models/views/prejudices have guided the discussions.
Fig. 3. – Numerical calculation of $\nu_e$ survival probability $P_{ee}$, for $\nu_e$ produced at the height of 15 km in the atmosphere and crossing the Earth. The regions at about 5–10 GeV (“atmospheric islands”) are those relevant for the study of the neutrino mass hierarchy. The mantle-core discontinuity causes the change at $\cos \theta_Z \sim 0.8$. The 3 “solar islands” above 0.1 GeV result from an interplay between matter effect and vacuum oscillations; the fuzzy contours are due to $\theta_{13}$ driven vacuum oscillations. From [4].

It is important to progress toward the measurements of the leptonic $CP$-violating phase and the discrimination of the type of mass hierarchy. I do not believe that the best approach is to prove that the leptonic $CP$-violating phase is non-zero, but rather, that we should measure this parameter. I consider remarkable that the first hints [19], and the existing experimental programs partly discussed in this round table, suggest that this measurement will be successfully achieved in the next years. Comparably, the experimental investigations of the neutrino mass hierarchy by means of oscillations seem to be more demanding. We discuss some of them in the next paragraph.

3-2. Probing the hierarchy by observing the Earth matter effect. – One of the reasons to study atmospheric neutrinos is to disentangle the neutrino mass hierarchy question by using the amplification of neutrino oscillations due to Earth matter. As it can be seen from fig. 3 (from La Thuile 2003 [4]) and fig. 4, reasonable conditions for this purpose could be obtained for certain directions and for neutrino energies of many GeV. Indeed it has been argued in [20] that the discrimination of the mass hierarchy could be possible using PINGU/ORCA like detector. Subsequent more realistic studies pointed out that the required exposure are quite large, of the order of tens of Mton × year, which could however be diminished by distinguishing track- from shower-events [21].

Another option consists in devising an experiment to maximize the effect. This was implemented in [22] with the use of 1) a conventional muon neutrino beam from pion decay; 2) a muon detector to identify 20–40 m tracks (5 m in water are $\sim$ 1 GeV); 3) a pair (source, detector) whose distance maximizes the effect. A beam of 6–8 GeV sent at (6000–8000) km (e.g., from Fermilab to Mediterranean Sea or from CERN to Lake Baikal) implies a difference between the two hierarchies of 30%. With $10^{20}$ protons on target
Fig. 4. – Survival probabilities of $\nu_e$ (green continuous/red dashed) and $\bar{\nu}_e$ (red continuous/green dashed) propagating through one Earth radius. Continuous/dashed lines are for normal/inverted hierarchy. The parameters $\theta_{23} = 42^\circ$, $\theta_{12} = 34^\circ$, $\theta_{13} = 9^\circ$, $\delta = 270^\circ$, $\Delta m^2_{12} = 7.5 \times 10^{-5} \text{eV}^2$, $\Delta m^2_{23} = 2.4 \times 10^{-3} \text{eV}^2$. The amplification of $\theta_{13}$ occurs for $\nu_e$ in normal hierarchy/for $\bar{\nu}_e$ in inverted hierarchy, and it is maximal at $\sim 7 \text{GeV}$. The wiggles due to $\theta_{13}$ driven oscillations at lower energies, as the oscillations with solar parameters at even lower energies are also visible.

Plot obtained by the web utility [23]; the agreement with fig. 3 at $\cos \theta_Z = 1/2$ is reasonable.

and 1 Mton detector, we have of $\sim 1000$ muons. The measurement of 30% difference is easy and the interpretation unmistakable; furthermore, one can even consider a run with $\bar{\nu}_\mu$ beam to revert the action of the matter effect.

3.3. Other neutrinos. – After the measurement of the $Z^0$ width [24], the proliferation of neutrino species apparently ended. The existence of 3 invisible fermionic decay channels (i.e., neutrinos) suggests the reliability of a correspondence between leptons and hadrons, proposed long ago. However, theorists have hypothesized the existence of neutral fermions of all sort of masses and without interactions with the $Z^0$, that could act as neutrinos in various situations. For instance, while cosmic (gravitational) probes agree with the number of standard neutrinos $N_\nu = 3$ for what concerns direct cosmological probes such as Planck or primordial nucleosynthesis, other observables, in particular galaxy counts, suggest a somewhat larger number of relativistic species.

Even more interesting are the manifestations of these hypothetical neutrinos in oscillation phenomena. In particular, the LSND anomaly [25] cannot be explained within an oscillation scheme with 3 neutrinos, whose masses are already fixed by other evidences of oscillations: see fig. 5. Thus, the existence of additional neutrinos, with masses in the eV range and small mixings with the ordinary neutrinos, has been hypothesized since long. This is widely discussed, also in review papers. E.g., [26] outlines the tension of the $N_\nu = 3 + 1$ neutrino interpretation, indicates relevant observables and attempts to identify the critical issues. Instead, [27] emphasizes the anomalies coming from reactor, gallium, cosmology and “provides motivations for a new round of measurements”(6).

(6) Let us compare these two works using bibliometric criteria. The former one appeared 10 year ago, it is published and it has 4 authors, 49 pages and 11 citations/year. The latter appeared 2 years ago, it is a “white paper” and it has 187 authors, 269 pages and 96 citations/year.
Fig. 5. – The region to interpret LSND in terms of oscillations (yellow), compared with the bounds from other oscillation experiments (dotted line), with the bound from big-bang nucleosynthesis (BBN, red line), with the limit from the neutrino contribution to the energy density (dot-dashed line); recall that $\Omega_\nu h^2 = \sum m_i/93.5\text{eV}$. From [26].

Anyway, these anomalies are few $\sigma$ only and a coherent picture does not seem to emerge yet. Things are still evolving and new relevant information should appear soon. In similar cases, it is not easy to plan a new experiment. However, it remains crucial to formulate the scientific questions, that we want to address, as clearly as possible.

4. – Solar, supernova, high-energy cosmic neutrinos

Although it is useful to proceed with a separate discussion for low energy and high energy neutrinos, a very precise definition of the boundary is not necessary for our purposes, and we can set it at 1 GeV. Well below, there are neutrinos from a large variety of nuclear phenomena; well above, high-energy neutrinos plausibly coming from the astrophysical sources of the cosmic rays. In the middle, we have neutrinos from the Earth atmosphere, mentioned above in connection with oscillations. In view of the present interests and discussion, we will in fact focus the discussion on the neutrinos with the lowest ($\lesssim \text{MeV}$) and highest ($\gtrsim \text{PeV}$) energies.

4.1. Lowest energy neutrinos/Borexino and beyond. – The success of the Borexino experiment, that achieved unprecedentedly low energy thresholds, has motivated serious consideration about how to proceed with ultra-pure scintillating detectors. Along with Borexino, with KamLAND and with the fore-coming SNO+, this issue concerns the physics with much larger detectors, such as LENA and JUNO, of several ten of kton mass [28]. Indeed, there are various scientific reasons why such an extension is interesting. These include:

Geoneutrinos. Indeed, up to now Borexino and KamLAND have obtained a relatively small statistics; thus, they have only a moderate power to discriminate the various nuclear chains contributing to the signal [29].
Fig. 6. – Expected counting rate in Borexino from a galactic supernova at 10 kpc [31]. The two main neutral current (NC) channels are emphasized.

LOW-ENERGY SOLAR NEUTRINOS. We would like to see in real time the pp neutrinos, but also of the secondary chain of energy production, \textit{i.e.}, those from the CNO cycle. This goal could be achieved in the next years with (a possibly upgraded version of) Borexino.

OSCILLATION STUDIES WITH REACTOR NEUTRINOS, as suggested in [30]. At present, this is the main motivation of JUNO, as discussed in the contribution of J. Cao.

NEUTRAL CURRENT EVENTS FROM A GALACTIC Supernova. This category includes the $\nu + p \rightarrow \nu + p$ events that, due to the kinematic of the reaction and to the quenching of the light, select neutrinos of relatively high energies.

Figure 6 illustrates the last point [31]. Note that a large scintillator detector can contribute to many more physics issues. \textit{E.g.}, fig. 6 shows that the neutral current events can be measured also by the 15.1 MeV gamma from carbon de-excitation.

In passing, we offer a remark on a potentially interesting measurement, namely the detection of relic neutrinos from past supernovae (aka, diffuse neutrino background). This requires a good performance in the region of (20–40) MeV. The interaction rate and its uncertainty range was assessed in [32] using the observations of SN1987A, assumed to be a standard supernova, and the astronomical data. The prediction is (0.01–0.04) events per kton per year in a water Cherenkov detector, and similarly in a scintillator, which implies that the measurement will be quite demanding.

4’2. Highest-energy neutrinos/the beginning of the IceCube era. – The IceCube experiment has observed events that can be identified as showering neutrinos (\textit{i.e.}, not due to muon tracks) with energies as high as few PeV. This is quite impressive since the center of mass energy of the collision $s \sim 2E_\nu m_N \sim (2 \text{ TeV})^2$ is larger than the one directly probed, though it is believed that the partons, at this energy, are known from proton-proton collisions. Moreover, it is quite curious that at these energies the cross section is large enough, that the Earth is not anymore transparent to neutrinos.

The most recent data have been reviewed by J. Auffenberg at this meeting: they are 36 events, of which only 9 are up-going, 8 are tracks (\textit{i.e.}, muon events) one probably spurious. It is quite unlikely that these events are due to atmospheric neutrinos, but
in an extreme interpretation of this type, one should assume an unexpectedly large contribution from charm decay (prompt neutrinos). However, in this case we should not expect any significant flux of tau neutrino. Therefore, an observation of tau events would provide a strong support to the cosmic neutrino hypothesis.

An alternative approach is offered by the study of the fraction of tracks $f$: In fact, the atmospheric hypothesis would lead to not less that $f = 1/2$ muon neutrinos, whereas the cosmic one would lead to $f = 1/3$ of muon neutrinos. Suppose to observe $n$ tracks out of $N$ events. If $f$ is the true (but unknown) fraction of muons, using $\Delta f^2 = -L/dL$ and the likelihood $L \propto f^n(1-f)^{N-n}$ we find

$$f = f_* \pm \sqrt{f_* (1-f_*) / N}, \quad \text{where} \quad f_* = \frac{n}{N},$$

that in our case reads $f = 0.20 \pm 0.07$. In order to reach a firm conclusion, a moderate increase in the statistics and a good understanding of the efficiencies of detection will be necessary [33]. Note that at the highest energies, it is not easy to measure the muon neutrino energy with IceCube, since the track is too long to be contained in the detector.

The flux above 60 TeV is about $E^2 \Phi \sim 10^{-8} \text{GeV}/(\text{cm}^2 \text{s sr})$. This is $1/3$ as originally estimated by Waxman and Bahcall [34], assuming that the energy in cosmic neutrinos equates the one evaluated from the observed highest energy cosmic ray spectrum. The flux could be attributed to a variety of cosmic sources, e.g. active galactic nuclei or perhaps gamma ray burst (though the search of events correlated in time with the gamma ray burst gave a null result). There could be a significant component, at present up to 25%, due to the region around the center of the Milky Way, even if on statistical basis the events are compatible with a uniform distribution in the sky. Note that if the knee of the all-particle spectrum is a property of the accelerator(s), and if we consider the corresponding neutrino flux, we would expect a cut at $3 \text{PeV}/20 \sim 150 \text{TeV}$ in the neutrino energy. This is one order of magnitude below the highest energy observed by IceCube.

These exciting results also renew the interest in other goals of high energy neutrino astronomy. In particular, it would be important to know the neutrino flux from galactic sources, either from a relatively wide object as the galactic center, already mentioned, or from quasi-point sources, as supernova remnants, molecular clouds illuminated by cosmic rays, pulsar wind nebulae, etc. As discussed in this meeting, this motivates adding an extended cosmic ray veto (surface detector) in IceCube (and it is of great interest for neutrino telescopes located in the Northern hemisphere, as Antares and the future Km3NET, both in the Mediterranean Sea, or NT1000 in Lake Baikal).

The search of galactic high energy neutrinos is tightly linked, in many cases, with the search of high energy gamma rays, as illustrated in fig. 7. Indeed, it has been shown that all gamma ray sources transparent to their gamma rays should release at least $(1 - 2) \times 10^{-13}$ photons per cm$^2$ per second above 20 TeV, in order to produce at least 1 muon per km$^2$ per year [35]. This remark points to an important synergy with the future gamma ray experiments that aim to measure in this window of energy, as LHAASO, or the large set of small telescopes of CTA.

5. – Conclusive remarks

Rather than attempting a provisional summary, that is probably of little or of no interest, I would like to conclude by returning on general considerations.
We could say that the review of Pontecorvo [1] concludes the pioneering stage of neutrino physics; but the progresses obtained in the subsequent thirty years, that we recalled only partly, are just impressive. We live in an exciting moment, however in order to plan at best the next steps forward, it is important to remain aware that the progresses are not only due to new and lucky circumstances, but also to certain specific features of this field of research. Among these positive features, we have the lively connection between theory and experiment.

It is quite evident that neutrino physics is assuming more and more the features of a “Big Science”, that implies large social groups and their characteristics dynamics: specialization, hierarchical organization, consensus, etc. These dynamics can have major effects on the field: e.g., increasing the separation between theory and experiment, encouraging an excess of speculative attitude among theorists(7), favoring the narrowing of the research fields or worse the lack of innovation. (Apparently, Pontecorvo himself had similar worries, as it is clear from his words [1]: The expenditure of resources has been justified, but one should neither underestimate the importance of high-energy neutrino physics, nor overestimate it. This is not pessimism, but an appeal to avoid routine.)

I consider of vital importance succeeding to maintain an active link between theory and experiment. This is needed not only to raise new questions and working hypotheses, but also to provide occasions of confrontation, of doubts and also of contradictions. Indeed, science requires a continuous assessment of the validity of the assumptions that are adopted and of the conclusions that are reached. This is possible if the scientific community is informed, competent and concerned, but also open-minded, diversified, and better if continuously renewed.

In my humble opinion, we should succeed in recognizing the increased role of various practical (political, economical) considerations in neutrino physics, but without

---

(7) I love the appeal to realism made by a character of the TV series Futurama in a dialog of “Mars University” episode: [Professor Farnsworth:] Nothing is impossible if you can imagine it! Thats what being a scientisit is all about! [Cubert:] No, that’s what being a magical elf is all about. It is amusing that, in the same episode, neutrinos are mentioned.
relegating the scientific debates to a marginal role. It is advisable that the decisions that concern the future of this field remain based on open and frank discussions among scientists, and I am glad to the Organizers for the occasion offered by this round table.

∗ ∗ ∗

I thank G. Bellettini, G. Chiarelli, M. Greco, G. Isidori for invitation and support, together with M. Chizhov, S. Dell’Oro, E. Lisi, S. Marcocci, G. Pagliaroli, S. Recchia, F. Terranova for useful discussions, collaboration and help.

APPENDIX

Questions/remarks

STUDENKIN: The study of magnetic moments is potentially important to investigate the nature of neutrinos.

FV: This is certainly true, even if I am not aware of a convincing theoretical case or a clear observational hint for large magnetic moments. I suspect that supernova neutrinos could be considered valuable in this respect, despite the difficulties in modeling the relevant astrophysics, owing to the very intense magnetic fields.

BELLETTINI: How large is the Earth matter effect and what is its interplay with the other effects?

FV: This depends critically upon the specific experimental conditions. See e.g., the talk of Shiozawa for the case of Hyper-Kamiokande. The matter effect has been maximized and other effects, in particular leptonic $CP$ violation, do not play a significant role for the specific setup I considered above (i.e., muon detector + pion beam) [22].

AUFFENBERG: Don’t you think that cosmic neutrinos (in particular the PeV ones, that we observe in IceCube) belong to astrophysics as much as to particle physics?

FV: Absolutely yes, and I am not sure that we have much to gain in separating artificially one aspect from the other. In particular, I am not convinced that we can learn much on neutrino oscillations, on the contrary I am sure we can learn a lot from oscillations [33].

DE RUJULA: I would like to stress: i) the importance of the laboratory search for neutrino masses; ii) the interest to see directly the cosmic neutrino background.

FV: Thanks. I discussed these points a bit in the occasion of my previous talk at La Thuile (2003), however i) I agree that I did not emphasize sufficiently the first point in this talk, especially in view of the facts that KATRIN is almost to produce data, and that HOLMES offers interesting prospects [36]; ii) as for the second point, I believe that the most urgent matter is to make sense of the cosmological data, for what concerns the role of neutrinos and of their masses. The progress of sensitivity is impressive but caution in the interpretation is in my view necessary(8).

AGOSTINI: What do we know from the “black-box theorem” on neutrinoless double beta decay?

(8) 20 year ago, the hot+cold matter cosmology indicated neutrino masses of $\approx 2.4 \text{ eV}$ [37]; 10 year ago, $\sum m_i \approx 0.6 \text{ eV}$ [38]; today the hints for non-zero neutrino masses are half as small [39].
FV: Not much: the value of $m_{\beta\beta}$, expected from model independent loops, is of the order of $10^{-24}\text{eV}$ [40]; moreover, neutrinos could be Majorana particles even if $m_{\beta\beta}$ is zero and the neutrinoless double beta decay is due to other mechanisms, see e.g. [41].

BERTOLUCCI: How deep should be a neutrino decay tunnel of a 6000 km long baseline?

FV: The required neutrino energy is 3 times smaller than the one of the CNGS beam, thus a tunnel of half a km should suffice. For an inclination of 30 degrees, this means 250 m depth. (LNGS engineers told me that tunnel boring machines–TBM–can excavate such an inclined tunnel, its cost being about 10 Meuro.)

REFERENCES

[1] Pontecorvo B. M., “Pages in the Development of Neutrino Physics,” Sov. Phys. Usp., 26 (1983) 1038.

[2] Sakharov A. D., Pisma Zh. Eksp. Teor. Fiz., 5 (1967) 32, (JETP Lett., 5 (1967) 24).

[3] Hoopf G. ‘t, Phys. Rev. D, 14 (1976) 3432; (E-ibid. D, 18 (1978) 2199); Kuzmin V. A., Rubakov V. A. and Shaposhnikov M. E., Phys. Lett. B, 155 (1985) 30; Harvey J. A. and Turner M. S., Phys. Rev. D, 42 (1990) 3344.

[4] Talk by Vissani F. published in Proceedings of La Thuile 2003, Frascati Physics Series, edited by Mario Greco, Vol. 30 (INFN, Rome) 2003, p. 103.

[5] Strumia A. and Vissani F., “Neutrino masses and mixings and ..., hep-ph/0606054.

[6] Dell’Oro S., Marcocci S. and Vissani F., arXiv:1404.2616 [hep-ph].

[7] Weinberg S., Phys. Rev. D, 43 (1979) 1566; Phys. Rev. D, 22 (1980) 1694.

[8] Feruglio F., Strumia A. and Vissani F., Nucl. Phys. B, 637 (2002) 345; Bahcall J. N., Murayama H. and Pena-Garay C., Phys. Rev. D, 70 (2004) 033012.

[9] Rodin V. A. et al., Nucl. Phys. A, 766 (2006) 107; E., 793 (2007) 213.

[10] Barea J., Kotila J. and Iachello F., Phys. Rev. C, 87 (2013) 014315.

[11] See e.g., Nishino H. et al. (Super-Kamiokande Coll.), Phys. Rev. Lett., 102 (2009) 141801; Phys. Rev. D, 86 (2012) 012006.

[12] See e.g., Fiorini E., “Nusex: The Mont Blanc Experiment” in Physics and Astrophysics With A Multikiloton Modular Underground Track Detector, Rome 1981, Proceedings, page 46; Aglietta M. et al. (NUSEX Coll.), Europhys. Lett., 8 (1989) 611.

[13] See e.g., Giacomelli G. et al. (MACRO Collaboration), Phys. Rev. Lett., 72 (1994) 608; Phys. Lett. B, 434 (1998) 451; Eur. Phys. J. C, 13 (2000) 453; Astrophys. J., 546 (2001) 1038.

[14] Gran Sasso, Cryogenic liquid detectors for future particle physics (Cryodet) Workshops, http://cryodet.lngs.infn.it/march2006/agenda/agenda.htm (March 2006) and http://cryodet.lngs.infn.it/agenda/CRYODET-2-agenda_fin.htm (June 2007).

[15] Nakamura K., Front. Phys., 35 (2000) 359; Aoki M., Hagiwara K. and Okamura N., Phys. Lett. B, 554 (2003) 121, [hep-ph/0208223].

[16] Wolfenstein L., Phys. Rev. D, 17 (1978) 2369; Mikheev S. P. and Smirnov A. Y., Sov. J. Nucl. Phys., 42 (1985) 834; Yad. Fiz., 42 (1985) 1441.

[17] Vissani F., JHEP, 11 (1998) 025; Phys. Lett. B, 508 (2001) 79, hep-ph/0111373.

[18] Vissani F., Mitra M. and Pagliaroli G., Nuovo Cimento C, 36 (2013) 1, 223.

[19] Capozzi F. et al., arXiv:1312.2878 [hep-ph].

[20] Akimov E. K., Razzaque S. and Smirnov A. Yu., JHEP, 02 (2013) 082; E., 1307 (2013) 026.

[21] Katz U. F. (for the KM3NeT Coll.), arXiv:1402.1022; Aartsen M. G. et al. (IceCube and PINGU Coll.s), arXiv:1306.5846.

[22] Lujan-Peschard C., Pagliaroli G. and Vissani F., Eur. Phys. J. C, 73 (2013) 2439.

[23] http://pbat1.mi.infn.it/ battiti/cgi-bin/oscil/index.x, code documentation in Battistoni G., Ferrari A., Rubbia C., Sala P. R. and Vissani F., hep-ph/0604182 and [14].
[24] Schael S. et al. [ALEPH, DELPHI, L3, OPAL, SLD Colls., LEP Electroweak Working Group, SLD Electroweak Group, SLD Heavy Flavour Group], Phys. Rep., 427 (2006) 257.
[25] Athanassopoulos C. et al. (LSND Coll.), Phys. Rev. Lett., 75 (1995) 2650.
[26] Cirelli M. et al., Nucl. Phys. B, 708 (2005) 215.
[27] Abazajian K. N. et al., “Light Sterile Neutrinos: A White Paper,” arXiv:1204.5379.
[28] Wurm M. et al. (LENA Coll.), Astropart. Phys., 35 (2012) 685; Li Y.-F. (JUNO Coll.), arXiv:1402.6143.
[29] Bellini G. et al. (Borexino Coll.), Phys. Lett. B, 722 (2013) 295; Gando A. et al. (KamiLAND Coll.), Phys. Rev. D, 88 (2013) 033001.
[30] Petrov S. T. and Piai M., Phys. Lett. B, 533 (2002) 94.
[31] Lujan-Peschard C., Pagliaroli G. and Vissani F., arXiv:1402.6953.
[32] Vissani F. and Pagliaroli G., Astron. Astrophys., 528 (2011) L1.
[33] Vissani F., Pagliaroli G. and Villante F. L., JCAP, 09 (2013) 017.
[34] Waxman E. and Bahcall J. N., Phys. Rev. D, 59 (1999) 023002.
[35] Vissani F. and Aharonian F., Nuc. Instrum Methods Phys. Res. A, 692 (2012) 5.
[36] Barker G. J. et al., arXiv:1309.7810 [hep-ex].
[37] Primack J. R. et al., Phys. Rev. Lett., 74 (1995) 2160.
[38] Allen S. W., Schmidt R. W. and Bridle S. L., Mon. Not. R. Astron. Soc., 346 (2003) 593.
[39] Wyman M. et al., Phys. Rev. Lett., 112 (2014) 051302; Battye R. A. and Moss A., Phys. Rev. Lett., 112 (2014) 051303.
[40] Duerr M., Lindner M. and Merle A., JHEP, 06 (2011) 091.
[41] Mitra M., Senjanovic G. and Vissani F., Nucl. Phys. B, 856 (2012) 26.