Influence of Li$_2$O Incrementation on Mechanical and Gamma-Ray Shielding Characteristics of a TeO$_2$-As$_2$O$_3$-B$_2$O$_3$ Glass System

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Abstract: According to the Makishema–Mackenzie model assumption, the dissociation energy and packing density for a quaternary TeO$_2$-As$_2$O$_3$-B$_2$O$_3$-Li$_2$O glass system were evaluated. The dissociation energy rose from 67.07 to 71.85 kJ/cm$^3$, whereas the packing factor decreased from 16.55 to 15.21 cm$^3$/mol associated with the replacement of TeO$_2$ by Li$_2$O compounds. Thus, as a result, the elastic moduli (longitudinal, shear, Young, and bulk) were enhanced by increasing the Li$_2$O insertion. Based on the estimated elastic moduli, mechanical properties such as the Poisson ratio, microhardness, longitudinal velocity, shear velocity, and softening temperature were evaluated for the investigated glass samples. In order to evaluate the studied glasses’ gamma-ray shield capacity, the MCNP-5 code, as well as a theoretical Phy-X/PSD program, were applied. The best shielding capacity was achieved for the glass system containing 25 mol% of TeO$_2$, while the lowest ability was obtained for the glass sample with a TeO$_2$ concentration of 5 mol%. Furthermore, a correlation between the studied glasses’ microhardness and linear attenuation coefficient was performed versus the Li$_2$O concentration to select the glass sample which possesses a suitable mechanical and shielding capacity.

Keywords: mechanical properties; shielding properties; elastic moduli; Monte Carlo simulation

1. Introduction

The field of radiation physics concerns the development of protective materials that are used to absorb radiation. These radiation shields are defined as any material used to attenuate photons, and are typically placed between the radiation source and the worker or patient. These shields are becoming increasingly more necessary as more fields begin using radiation on a daily basis [1–5]. Fields such as medicine, food conservation, and agriculture all rely upon radiation to fully function. Despite the benefits of radiation present across various fields of work, high-energy particles or ionizing radiation can be extremely harmful to the human body if underexposed for a long time. Some side effects of radiation exposure may include acute radiation syndrome, cutaneous radiation injuries, and cancer development. Radiation shields work to minimize these effects and protect humans that may come into contact with ionizing radiation [6–9].

When selecting a radiation shield for a specific application, several characteristics of how the radiation is being used must be known to utilize the best possible material.
For example, concrete is commonly used against X-rays and neutrons, and is ideal for lining the walls of rooms. These properties make concretes suitable for lining the walls of nuclear reactors, for instance, but their lack of mobility and tendency to crack makes them unideal for other applications [10,11]. Other materials that have been used as radiation shields include alloys, composites, construction materials (such as granite and marble), and glass [12–16].

Glasses offer advantageous properties over other radiation shields because, in addition to their excellent shielding ability, they are transparent, are simple to manufacture, and can have a wide range of possible compositions. The structural, chemical, and shielding features of glasses can be changed by doping metal oxides and heavy metal oxides (HMOs) into the glass system. Metal oxides and HMOs act differently on the glass matrix, depending on their characteristics. There exist three different kinds of oxides: network formers, network modifiers, and intermediates [17–19].

Borate is commonly used as a glass former and is found in most commercial glasses. Borate can easily modify its coordination with three of four oxygen units to provide a strong and adjustable structural composition. This change increases its chemical and thermal resistance by creating non-bridging oxygens (NBOs). Additionally, borate glasses have a low viscosity, high chemical durability, high visible light transparency, low cost, and good mechanical stability. Despite the abilities of borate, it has a low density, which is undesirable by itself. Other metal oxides and HMOs are added to borate glasses to improve their density [20,21].

Tellurite, or TeO$_2$, is a glass intermediate with a high dielectric constant, a good electrical conductivity, transparency in visible and infrared light, and good solubility of rare-earth ions. Tellurite glasses can be used as planar waveguides and optical amplifiers in optical applications, but have also been used in radiation shielding applications. Tellurite has a high density and atomic number, making it a HMO [22,23]. Due to tellurite being an intermediate, it does not form a stable glass system by itself due to its weak connectivity. By pairing TeO$_2$ with oxides, such as B$_2$O$_3$, its stability can be increased. Borotellurite glasses have high stability and transparency and are used in fiber-optic communication systems and nonlinear optical devices.

In order to assess the capability of a medium to become a radiation shield, several parameters must be calculated and analyzed. These parameters are typically calculated experimentally, but simulations are often used to validate the obtained data. Simulations also offer the ability to test samples before spending the time and cost fabricating them, and if they demonstrate potential, they can then be experimentally examined. Simulations have also proven to be extremely reliable in correctly assessing the shielding ability of a sample across a wide range of energies [24,25].

The novelty of the present study lies in the application of the Makishima–Mackenzie (M–M) model to predict the elastic and mechanical characteristics of As$_2$O$_3$-B$_2$O$_3$-Li$_2$O-based tellurite glasses. Moreover, the radiation shielding properties of the mentioned glasses were evaluated using the Monte Carlo simulation method. Additionally, the accumulation of photons in air and inside the investigated glasses was calculated via the Phy-X/PSD program.

2. Materials and Methods

2.1. Mechanical Properties

The mechanical features (Poisson ratio, microhardness, fractal bond conductivity, and longitudinal and shear velocities), as well as elastic moduli (EM) (Young, shear, longitudinal, and bulk), were investigated for five glass samples reported by [26]. The mentioned glass system contained TeO$_2$-As$_2$O$_3$-B$_2$O$_3$-Li$_2$O in composition. Based on the foundations approved by Makishema and Mackenzie [27,28], the EM were computed. The dissociation
energy \( (G_t) \) is a measure for the heat of formations (enthalpy) required to fabricated the glass system. The following equation describes it.

\[
G_t \left( \frac{kJ}{cm^3} \right) = \sum X_i G_i
\]  

\( X_i \) is fractional by mol of the constating compounds. The packing density is an essential factor related to the oxide and metal ionic radius \( R_o \) and \( R_M \). The \( V_t \) is evaluated using Equation (2), where \( V_i \) is the packing factor of the constituting compounds.

\[
V_t = \left( \frac{\rho}{MW} \right) \times \sum X_i V_i
\]  

The previously calculated values for \( G_t \) and \( V_t \) were used to compute Young (\( E \)), shear (\( K \)), longitudinal (\( L \)), and bulk (\( B \)) modules, as presented in Equations (3)–(6). In addition, some mechanical properties based on that derived from the EM were evaluated in Equations (7)–(9), such as the Poisson ratio (\( \sigma \)), the microhardness (\( H \)), softening temperature (\( T_s \)), and fractal bond connectivity (\( d \)) [29].

\[
E = 2 V_t G
\]

\[
B = 1.2 V_t E
\]

\[
S = \frac{3 EB}{9B - E}
\]

\[
L = B + \frac{3}{4} S
\]

\[
\sigma = 0.5 - \frac{1}{\sqrt{2}} V_t
\]

\[
H = \frac{(1 - 2\sigma)}{6(1 + \sigma)}
\]

\[
T_s = \frac{M_w}{\left( \rho_{glass} \times C \right)} \times V_s^2
\]

2.2. Gamma-Ray Simulation and Theoretical Calculations

The present study’s second aim is to report the radiation protection capacity for the investigated TABLi samples. In order to achieve the desired target, the MCNP-5 [30] and a theoretical calculation program named Phy-X/PSD [31] were used to evaluate the protection ability. Both previous programs used the chemical compositions and densities of the investigated glasses to evaluate the shielding factors. On the other hand, there are differences in the nuclear libraries, which used to extract the interaction cross-sections. The MCNP-5 used ENDF/B-VI.8 as a primary source, but the Phy-X/PSD used only the NIST database. The geometry used in the MCNP-5 simulation was illustrated in Figure 1 and discussed in detail in many publications [32–34]. Additionally, the investigated glasses’ chemical compositions were given in Table 1.
Table 1. The chemical composition of the investigated glass samples.

| Composition (wt%) | Density (g/cm³) | MW (g/mol) | Vm (cm³/mol) |
|-------------------|-----------------|------------|--------------|
| As₂O₃ | B₂O₃ | Li₂O | TeO₂ | TABLi5 19.217 | 40.574 | 1.451 | 38.757 | 3.71 | 102.95 | 27.72 |
| TABLi10 20.510 | 43.303 | 3.098 | 33.090 | 3.61 | 96.46 | 26.73 |
| TABLi15 21.988 | 46.424 | 4.982 | 26.607 | 3.50 | 89.98 | 25.72 |
| TABLi20 23.696 | 50.030 | 7.158 | 19.116 | 3.37 | 83.49 | 24.77 |
| TABLi25 25.692 | 54.244 | 9.701 | 10.363 | 3.19 | 77.01 | 24.14 |

3. Results and Discussion

3.1. Mechanical Properties

The selected TABLi samples have a density (ρ, g/cm³) that decreased linearly from 3.714 to 3.190 g/cm³, as shown in Figure 2. The decrease in the glass density is related to the compactness of the glass materials, which is predicted through the distribution density for boron, D (B), and distribution density for Li, D (Li). The D (B) and D (Li) were calculated and showed in Table 2, where both D (B) and D (Li) increased with an increasing Li₂O concentration in the glass network. Thus, the density of the samples decreased. Table 2 also showed that the boron-boron separation, r (B-B), lithium-lithium separation, r (Li-Li), and tellurium-tellurium separation, r (Te-Te), decreased with an increasing Li₂O concentration in the glass network. This can be ascribed to the replacement of Te ions with a higher ionic radius (R₆e = 2.22 Å) by a smaller Pauli ionic radius (R₆i = 0.56 Å) for Li ions. Moreover, both the molecular weight (MW, g/mol) and molar volume (Vₘ, cm³/mol) follow the ρ trend, where they decreased from 102.949 to 77.005 g/mol and from 27.719 to 24.140, for MW and Vₘ, respectively.
In order to compute the elastic moduli (EM), Young (Y), shear (K), bulk (B), and longitudinal (L), the Makishima–Mackenzie (M–M) model assumptions were applied. Thus, both the investigated TABLi glasses’ dissociation energy (Gt) and backing factor (Vi) were calculated. The Gt values were increased by replacing the TeO₂ with Li₂O compounds. This is attributed to the heat of formation (enthalpy, ∆Hf) of constituting compounds, where it is −561.2 kJ/mol for Li₂O and −270.3 kJ/mol for TeO₂. On the other hand, the glasses’ packing factor (Vi, cm³/mol) was computed for the TABLi glasses with the help of the values of the ionic radius of Te, B, As, Li, and O. Figure 3 displays a reverse relationship between the Vi and Li₂O concentration. The Vi values decreased from 16.55 to 15.215 cm³/mol, increasing TeO₂ substitution by Li₂O. This can be attributed to the replacement of Te ions with a higher ionic radius (R_{Te} = 2.22 Å) by Li ions with a smaller Pauli ionic radius (R_{Li} = 0.56 Å).
The TABLi glasses’ packing density ($V_t$) was reported based on the predicted $V_t$ values. $V_t$’s calculated values were 0.567 to 0.630, raising the ratio of Li ions in the glass network.

The elastic moduli ($Y$, $K$, $B$, and $L$) were reported for the investigated samples. Clearly, $Y$’s modulus decreased by increasing the $V_t$ values. But it is enhanced by increasing the $G_t$ of the TABLi glasses, as shown in Figure 4. This is due to the substitution of weak Ti-O bonds by strong Li-O bonds. Additionally, $Y$’s values enhanced from 80.120 to 90.579 GPa by raising the Li$_2$O between 5 and 25 mol%, respectively. The other moduli $K$, $B$, and $L$’s values follow the same trend as $Y$ when the Li$_2$O increases between 5 and 25 mol%.

The investigated glasses’ dissociation energy and packing factor versus the Li$_2$O concentration.

The hardness (GPa) is considered an important parameter for shielding materials such as concretes and bricks, but in the case of small-scale materials, such as glass, the term microhardness (H, GPa) is applied. It is used to describe the load which the material can stand over without deformations. The TABLi glasses’ microhardness presented in Figure 5 was enhanced from 4.900 to 5.199 GPa by increasing the Li$_2$O in the content. This can contribute to the increase in compactness of the material and decrease the $r$ (B-B),

![Graph showing the relationship between packing factor and dissociation energy](image)

**Figure 3.** The investigated glasses’ dissociation energy and packing factor versus the Li$_2$O concentration.

![Graph showing the relationship between elastic moduli and packing factor](image)

**Figure 4.** The elastic moduli ($Y$, $B$, $K$, and $L$) versus (a) packing factor and (b) dissociation energy.

![Graph showing the relationship between hardness and packing factor](image)

**Figure 5.** The hardness (GPa) is enhanced from 4.900 to 5.199 GPa by increasing the Li$_2$O in the content.
r (Li-Li), and r (Te-Te) by increasing the Li ions in the glass network (Table 2). The Poisson ratio (\(\sigma\)) describes the expansion ratio of the investigated TABLi glasses in the direction vertical to the loader direction. Figure 5 showed that the \(\sigma\) values also increase from 0.267 to 0.280 with the replacement of TeO\(_2\) with Li\(_2\)O content.

![Figure 5](image_url)

**Figure 5.** Variation in the Poisson ratio and microhardness for the fabricated TABLi glasses as a function of the Li\(_2\)O insertion ratio.

Softening temperature (\(T_g\), °C) was reported for the TABLi glasses based on the EM predicted previously (see Figure 6). It is clear that the \(T_g\)’s values increased from 464.9 to 525.8 °C. The increase detected in \(T_g\) values is due to the replacement of TeO\(_2\) with a lower melting point (MP) by a higher (i.e., Li\(_2\)O), where the MP\(_{\text{TeO}_2}\) = 733 °C and MP\(_{\text{Li}_2\text{O}}\) = 1570 °C.

![Figure 6](image_url)

**Figure 6.** Variation in the softening temperature (\(T_g\)) versus the Li\(_2\)O insertion ratio.
The fractal bond conductivity (d) for the investigated glass samples decreased from 2.20 to 2.06. This means that the d values are close to two. Thus, the investigated glasses possess a two-dimensional layer structure network.

3.2. Shielding Properties

The glass understudy’s effectiveness in resisting gamma quanta depends on the efficiency of the glass material in absorbing and attenuating incident gamma radiation. Therefore, essential shielding parameters such as radiation protection efficiency (RPE), linear attenuation (LAC), and mean free path (MFP) need to be studied. Awareness of these factors’ performances makes it reasonable to assess the protection efficiency of and the suitable applications for utilizing the glasses to resist radiation. Figures 7–12 illustrate the data of simulated radiation shielding parameters computed via the MCNP-5 simulation code. It can be perceived in Figure 7 that the RPE results are influenced by the applied gamma photons’ energy. The increment of the applied gamma energy leads to the decrement of the RPE values for the examined glasses. The following inferences can be interpreted from the examination of the reduction in the gamma radiation intensity with the variation of gamma energies. At low energies (0.0221–0.088 MeV), the investigated glasses appear to be effective at opposing incoming gamma radiation, with RPE values of approximately 100% for all investigated glasses. At the same time, the RPE values diminish with an increase in the gamma radiation intensity from 0.284 to 2.51 MeV based on the Li$_2$O concentration in the selected samples. The RPE values of the glasses with a high concentration of Li$_2$O (25% mol) have not exceeded 31% in the case of high gamma-quanta energy of 2.51 MeV. Thus, the obtained data for all investigated glasses illustrate that the glasses doped with 5% of Li$_2$O content are the preferable glasses that can be applied in the different radiation shielding implementations.

![Figure 7. Variation in the investigated glasses’ radiation protection efficiency (RPE) versus the photon energy.](image-url)
Figure 8. The studied glasses’ linear attenuation coefficient vs the energy.

Figure 9. The dependence of the (a) half-value layer and (b) mean free path on the incoming gamma photons.
Figure 10. Comparison between the MFP of the studied glasses with some known commercial glasses (RS253 and RS323-G19).

Figure 11. Variation of the investigated glasses’ half-value layer versus LiO$_2$ concentration.
Among the essential parameters of shielding properties is the linear attenuation coefficient ($\mu$), which is used to display the ability of glass material to resist and absorb gamma quanta. Here in the present investigation, the $\mu$ is varied between low and high values depending on two parameters: the intensity of gamma-quanta energy and the concentration of dopant (Li$_2$O) in the studied glass material. The simulated $\mu$ values are deduced from the interaction of the gamma-quanta intensity ($I$) with the glass material at the known thickness ($x$), and represented in the following formula: $\mu = \frac{\ln(10)}{x}$. The data of $\mu$ depends on the interaction type of gamma quanta, and are explained as follows and plotted in Figure 8: the first interaction is a photoelectric effect (PE) which is achieved in the low gamma-quanta energy range (0.0221–0.088 MeV), and the $\mu$ data have appeared with the maximum values.

Successively, the increment of gamma-quanta energy above 0.1 MeV leads to a drop in the $\mu$ data as a result of the new interaction, namely Compton scattering (CS). Compton scattering is preponderant, and the inverse relation between CS cross-section and quanta energy was detected where $\sigma_{CS} \propto E^{-1}$ [35].

The $\mu$ data are manifested with the maximum values at the low applied gamma-quanta energy (0.0221 MeV). It was reduced from 40.5 to 28.3 cm$^{-1}$ for 5% mol and 25% mol of Li$_2$O content in the investigated glasses. In contrast, the $\mu$ data are observed with the minimum values at the highest applied gamma-quanta energy, 2.51 MeV, where it varies in decrement from 0.14 to 0.12 cm$^{-1}$ for 5% mol and 25% mol of Li$_2$O content, respectively.

Furthermore, the $\mu$ data impacted the insertion of Li$_2$O concentration in the studied glasses. At stationary gamma-quanta energy, the $\mu$ data are diminished with the addition of Li$_2$O content from 5 mol% to 25 mol% due to the molecular weight decrease from 102.95 to 77.01 g/mol for 5 mol% and 25 mol% of Li$_2$O content. Therefore, the effective atomic number ($Z_{eff}$) decreases. The maximum data of $\mu$ lessened in-between 40.5 and 0.14 cm$^{-1}$ for the studied glasses with 5 mol% content of Li$_2$O. The minimum data varied in decrement 8.89–0.03 cm$^{-1}$ and established at the examined glasses with 25 mol% content of Li$_2$O. Finally, the replacement of TeO$_2$ content with Li$_2$O content procures the decrement of $\mu$ data due to the direct proportionality between the cross-section of CS and the effective atomic number where $\sigma_{CS} \propto Z_{eff}$.

Agreement was detected between the obtained $\mu$ data with the kinds in the literature concerned with various types of tellurite glasses [36–38].

The other parameter is the mass attenuation coefficient ($\mu/\rho$), which was computed via the MCNP-5 code based on the density of the investigated glasses, and compared with the theoretical data of $\mu/\rho$, which was detected by Phy-X/PSD. The difference $\Delta$ (%)
between the simulated and theoretical data was estimated by the next formula [39] and presented in Table 3:

$$\Delta(\%) = \left[ \frac{\left( \frac{\mu}{\rho} \right)_{MCNP} - \left( \frac{\mu}{\rho} \right)_{Phy-x/PSD}}{\left( \frac{\mu}{\rho} \right)_{MCNP}} \right] \times 100$$

(10)

The difference $\Delta(\%)$ observed did not exceed 10% between all investigated TABLi glasses.

The HVL and the MFP are the radiation protection factors used to minimize the applied gamma-quanta energy to a half and display the distance between successive interactions. Contrarily, the $\mu$ data of simulated HVL are observed to rise with the applied gamma-quanta energy and the addition of Li$_2$O concentration in the TABLi glasses, as shown in Figure 9. The following formulas are applied to estimate the HVL and MFP:

$$\text{HVL (cm)} = \frac{\ln 2}{\mu} \quad \& \quad \text{MFP (cm)} = \frac{1}{\mu}$$

(11)

The results presented in Figure 9 illustrate that an increment in the concentration of Li$_2$O in the glasses’ structure and the creation of supplementary absorption bands assist in the reality that for dopant Li$_2$O contents of 5–25 mol% in the investigated glasses, the HVL and MFP diminish by 1.5 times. The difference revealed that the insertion of Li$_2$O could significantly decrease the thickness of the investigated glasses, without losing efficiency and minimizing the costs of production. The HVL data that reached the maximum values at the high gamma-quanta energy of 2.51 MeV ranged from 4.9 to 5.7 cm for TABLi5 and TABLi25, respectively, as well as the MFP data, which varied in an increase of 7.1 and 8.2 for TABLi5 and TABLi25, respectively. Furthermore, the investigated glasses’ low HVL and MFP data are detected at the low applied gamma-quanta energy (0.0221 MeV). Moreover, the glasses’ understudy with the lower content of Li$_2$O (5 mol%) is considered better than glasses with a high content of Li$_2$O. Consequently, it can be used in radiation protection applications. Based on the MFP data, the present glasses are compared with the commercial glasses RS253 and RS323-G19 [40] and plotted in Figure 10. The comparison displayed that the MFP values of studied glasses are lower than RS253 and comparable with the synthetic glasses RS323-G19. This means the examined glasses are suitable for application in the radiation protection fields, especially the glasses with 5% mol of Li$_2$O content (TABLi5) since the mean voyaged distance between two photo interactions is small.

Figures 11 and 12 depict the injection of Li$_2$O concentration in the tellurite glasses that impacted the HVL and MFP data. The Phy-x/PD computer program was employed to theoretically estimate the HVL and MFP data of the synthetic glasses. It is plain in Figures 11 and 12 that the TABLi5 glasses have the lowest data of HVL and MFP while the TABLi25 glasses have the highest data at all chosen gamma-quanta energies (0.015, 0.15, 1.5, and 15 MeV), and this agrees with their simulated data.

Furthermore, the Phy-x/PD was employed to compute radiation protection items, including glasses’ effective atomic number ($Z_{\text{eff}}$), equivalent atomic number ($Z_{\text{eq}}$), as well as the accumulation factors, those being exposure buildup factors (EBF) and energy absorption buildup factor (EABF). Figures 13–18 depicted the acquired data, which were then addressed in the lines below.
Table 3. The mass attenuation coefficient of the chosen glasses.

| Energy (MeV) | TABLi5 | MCNP-5 | Phy- X/PSD | Δ (%) | TABLi10 | MCNP-5 | Phy- X/PSD | Δ (%) | TABLi15 | MCNP-5 | Phy- X/PSD | Δ (%) | TABLi20 | MCNP-5 | Phy- X/PSD | Δ (%) | TABLi25 | MCNP-5 | Phy- X/PSD | Δ (%) |
|-------------|--------|--------|------------|-------|---------|--------|------------|-------|---------|--------|------------|-------|---------|--------|------------|-------|---------|--------|------------|-------|
| 0.015       | 30.89  | 29.60  |            | -0.07 | 28.12   | 9.95   | -0.05      | 9.61  | 9.35    | 8.89   | 8.65      | 7.68  | 5.18    |
| 0.022       | 10.91  | 10.46  |            | -0.04 | 10.15   | 7.13   | -0.01      | 8.73  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.026       | 7.12   | 6.76   |            | -0.20 | 6.65    | 7.02   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.029       | 4.82   | 4.62   |            | -0.23 | 4.41    | 4.26   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.050       | 3.71   | 3.17   |            | -0.20 | 3.37    | 3.17   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.080       | 1.25   | 0.96   |            | -0.18 | 0.96    | 0.96   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.088       | 0.95   | 0.90   |            | -0.17 | 0.90    | 0.90   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.100       | 0.73   | 0.66   |            | -0.17 | 0.66    | 0.66   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.150       | 0.31   | 0.25   |            | -0.17 | 0.25    | 0.25   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.347       | 0.11   | 0.11   |            | -0.18 | 0.11    | 0.11   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.300       | 0.10   | 0.10   |            | -0.18 | 0.10    | 0.10   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.347       | 0.11   | 0.11   |            | -0.18 | 0.11    | 0.11   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.500       | 0.09   | 0.09   |            | -0.18 | 0.09    | 0.09   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.347       | 0.11   | 0.11   |            | -0.18 | 0.11    | 0.11   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 0.826       | 0.07   | 0.07   |            | -0.19 | 0.07    | 0.07   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 1.173       | 0.05   | 0.05   |            | -0.19 | 0.05    | 0.05   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 1.275       | 0.05   | 0.05   |            | -0.19 | 0.05    | 0.05   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 1.333       | 0.05   | 0.05   |            | -0.19 | 0.05    | 0.05   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 1.5         | 0.05   | 0.05   |            | -0.19 | 0.05    | 0.05   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 2.506       | 0.04   | 0.04   |            | -0.19 | 0.04    | 0.04   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 3           | 0.03   | 0.03   |            | -0.19 | 0.03    | 0.03   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 5           | 0.03   | 0.03   |            | -0.19 | 0.03    | 0.03   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 8           | 0.03   | 0.03   |            | -0.19 | 0.03    | 0.03   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 10          | 0.03   | 0.03   |            | -0.19 | 0.03    | 0.03   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
| 15          | 0.03   | 0.03   |            | -0.19 | 0.03    | 0.03   | -0.15      | 8.30  | 8.30    | 4.94   | 8.10      | 7.68  | 5.18    |
Furthermore, the Phy-x/PD was employed to compute radiation protection items, including glasses’ effective atomic number ($Z_{\text{eff}}$), equivalent atomic number ($Z_{\text{eq}}$), as well as the accumulation factors, those being exposure buildup factors (EBF) and energy absorption buildup factor (EABF). Figures 13–18 depicted the acquired data, which were then addressed in the lines below.

Figure 13 reveals the effective atomic number ($Z_{\text{eff}}$) data that are designated to investigate the capacity of the synthetic glasses for serving in the implementations of gamma shielding. The data of $Z_{\text{eff}}$ are changed with the gamma-quanta energy (0.015–15 MeV) and the Li$_2$O concentration (5–25 mol%) in the examined TABLi glasses. The $Z_{\text{eff}}$ data are influenced by the gamma quanta interaction with the glass material. For low gamma-quanta energy range (0.015–0.1 MeV), the photoelectric effect (PE) interactions are dominant, and the maximum $Z_{\text{eff}}$ data seem to be where $Z_{\text{eff}}$ varied. After that, the $Z_{\text{eff}}$ data diminished when the gamma-quanta energy increased. However, unpredicted peaks are observed at gamma-quanta energy 0.0318 MeV.

Figure 14. The dependence of the studied glasses’ effective atomic number ($Z_{\text{eff}}$) on the LiO$_2$ concentration.

Figure 13. Variation of the studied glasses’ effective atomic number ($Z_{\text{eff}}$) versus the gamma photon energy.
Then, the Compton scattering interactions are begun to possess gamma-quanta energy in the range of above 0.1 MeV, and the data of $Z_{\text{eff}}$ are observed gradually in decrement where it altered with the atomic number ($Z$). The increase in gamma-quanta energy at high values leads to pair production, which varied with $Z^2$ [42]. Additionally, the $Z_{\text{eff}}$ data reduced, as illustrated in Figure 14.

Figure 14. The dependence of the studied glasses' effective atomic number ($Z_{\text{eff}}$) on the LiO$_2$ concentration.

Figure 15 offers the equivalent atomic number ($Z_{\text{eq}}$) at various gamma photon energy. It is estimated according to the values of $\mu/\rho$ in addition to the atomic numbers of elements ($Z_1$ and $Z_2$) related to the ratios $R_1$ and $R_2$ as well as the ratio for the examined glasses at stationary gamma-quanta energy. Thus, $Z_{\text{eq}}$ is estimated by the following formula ($Z_{\text{eq}} = \frac{R_1}{R_2}$).

Figure 15. The equivalent atomic number as a function of the energy.

Figure 16. The buildup factors versus the energy.

Furthermore, Figures 17 and 18 show that the EBF and EABF data impacted the penetration depth, which changes from 0.5 to 40 mfp at four specified gamma-quanta energies of 0.015, 0.15, 1.5, and 15 MeV, as well as the chemical composition of TABLi glasses.

Figure 17. The exposure buildup factor (EBF) dependent on the penetration depth values (PD) at some fixed energies.
had high values thanks to the third interaction as represented in the PP (Mahmoud et al., 2020; YS. Rammah et al., 2020).

Figure 16. The buildup factors versus the energy. Furthermore, Figures 17 and 18 show that the EBF and EABF data impacted the penetration depth, which changes from 0.5 to 40 mfp at four specified gamma-quanta energies of 0.015, 0.15, 1.5, and 15 MeV, as well as the chemical composition of TABLi glasses.

Figure 17. The exposure buildup factor (EBF) dependent on the penetration depth values (PD) at some fixed energies.

Figure 18. The EABF dependent on the penetration depth values (PD) at some fixed energies.

Figure 13 reveals the effective atomic number ($Z_{\text{eff}}$) data that are designated to investigate the capacity of the synthetic glasses for serving in the implementations of gamma shielding. The data of $Z_{\text{eff}}$ are changed with the gamma-quanta energy (0.015–15 MeV)
and the Li$_2$O concentration (5–25 mol%) in the examined TABLi glasses. The $Z_{\text{eff}}$ data are influenced by the gamma quanta interaction with the glass material. For low gamma-quanta energy range (0.015–0.1 MeV), the photoelectric effect (PE) interactions are dominant, and the maximum $Z_{\text{eff}}$ data seem to be where $Z^4$ varied. After that, the $Z_{\text{eff}}$ data diminished when the gamma-quanta energy increased. However, unpredicted peaks are observed at gamma-quanta energy 0.0318 MeV [41].

Then, the Compton scattering interactions are begun to possess gamma-quanta energy in the range of above 0.1 MeV, and the data of $Z_{\text{eff}}$ are observed gradually in decrement where it altered with the atomic number ($Z$). The increase in gamma-quanta energy at high values leads to pair production, which varied with $Z^2$ [42]. Additionally, the $Z_{\text{eff}}$ data reduced, as illustrated in Figure 14.

Figure 15 offers the equivalent atomic number ($Z_{\text{eq}}$) at various gamma photon energy. It is estimated according to the values of $\mu/\rho$ in addition to the atomic numbers of elements ($Z_1$ and $Z_2$) related to the ratios $R_1$ and $R_2$ as well as the ratio for the examined glasses (energy > 1 MeV). The maximum data of $Z_{\text{eq}}$ are presented in Table 4 for TABLi5 and TABLi25 glasses, respectively.

The total flux of gamma quanta in the studied glass material can be determined by utilizing two main buildup and accumulation factors: the EBF and the EABF. The alteration of EBF and EABF data with the gamma-quanta energy for the TABLi5 and TABLi25 glasses is put forward in Figure 16. The EBF and EABF data are computed according to the $Z_{\text{eq}}$ values and the approximation of G-P fitting [43,44]. For instance, the $Z_{\text{eq}}$ data and the five factors of GP fitting are presented in Table 4 for TABLi5 and TABLi25 glasses, respectively.

Table 4. The GP fitting parameters for the TALBi5 sample at various gamma energies.

| E (MeV) | $Z_{\text{eq}}$ | EBF | EABF |
|---------|-----------------|-----|-----|
|         | $a$ | $b$ | $c$ | $d$ | $X_k$ | $a$ | $b$ | $c$ | $d$ | $X_k$ |
| 0.015   | 20.53 | 0.04 | 1.01 | 0.69 | 0.15 | 6.89 | 0.02 | 1.01 | 0.68 | 0.14 | 9.31 |
| 0.02    | 20.93 | 0.26 | 1.02 | 0.39 | 0.18 | 10.98 | 0.26 | 0.18 | 0.17 | 0.20 | 12.47 |
| 0.03    | 21.49 | 0.22 | 1.05 | 0.37 | 0.17 | 16.39 | 0.24 | 0.16 | 0.24 | 0.26 | 14.46 |
| 0.04    | 32.96 | 0.19 | 0.24 | 0.33 | 0.07 | 17.60 | 0.17 | 0.15 | 0.14 | 0.18 | 20.68 |
| 0.05    | 33.61 | 0.02 | 1.88 | 0.23 | 0.06 | 12.52 | 0.08 | 0.06 | 0.05 | 0.10 | 11.06 |
| 0.06    | 34.08 | 0.61 | 1.67 | 0.21 | 0.14 | 15.27 | 0.49 | 0.37 | 0.36 | 0.40 | 14.70 |
| 0.08    | 34.71 | 0.47 | 1.42 | 0.25 | 0.18 | 14.18 | 0.39 | 0.37 | 0.36 | 0.40 | 14.22 |
| 0.1     | 35.13 | 0.23 | 1.22 | 0.40 | 0.13 | 13.82 | 0.23 | 0.22 | 0.21 | 0.24 | 16.50 |
| 0.15    | 35.79 | 0.14 | 1.36 | 0.57 | 0.08 | 14.23 | 0.25 | 0.17 | 0.16 | 0.19 | 13.85 |
| 0.2     | 36.17 | 0.12 | 1.56 | 0.64 | 0.07 | 14.02 | 0.24 | 0.16 | 0.15 | 0.18 | 13.80 |
| 0.3     | 36.61 | 0.05 | 1.69 | 0.84 | 0.03 | 13.76 | 0.11 | 0.08 | 0.07 | 0.09 | 13.59 |
| 0.4     | 36.85 | 0.02 | 1.78 | 0.98 | 0.03 | 13.22 | 0.07 | 0.05 | 0.04 | 0.06 | 13.30 |
| 0.5     | 37.02 | 0.00 | 1.82 | 1.05 | 0.02 | 12.83 | 0.04 | 0.02 | 0.02 | 0.03 | 13.10 |
| 0.6     | 37.11 | 0.00 | 1.83 | 1.09 | 0.02 | 12.13 | 0.03 | 0.01 | 0.02 | 0.03 | 12.75 |
| 0.8     | 37.20 | 0.00 | 1.32 | 1.12 | 0.01 | 11.73 | 0.01 | 0.00 | 0.00 | 0.01 | 12.06 |
| 1       | 37.23 | 0.00 | 1.79 | 1.13 | 0.01 | 11.49 | 0.00 | 0.01 | 0.00 | 0.01 | 11.46 |
| 1.5     | 34.62 | 0.00 | 1.68 | 1.17 | 0.01 | 12.99 | 0.02 | 0.01 | 0.00 | 0.01 | 10.71 |
| 2       | 29.21 | 0.00 | 1.69 | 1.12 | 0.00 | 8.97 | 0.00 | 0.00 | 0.00 | 0.00 | 9.56 |
| 3       | 25.22 | 0.00 | 1.63 | 1.06 | 0.00 | 12.14 | 0.00 | 0.00 | 0.00 | 0.00 | 12.39 |
| 4       | 24.08 | 0.00 | 1.56 | 1.02 | 0.00 | 12.67 | 0.00 | 0.00 | 0.00 | 0.00 | 14.33 |
| 5       | 23.57 | 0.00 | 1.49 | 1.00 | 0.00 | 13.15 | 0.00 | 0.00 | 0.00 | 0.00 | 14.30 |
| 6       | 23.20 | 0.00 | 1.45 | 0.97 | 0.00 | 13.29 | 0.00 | 0.00 | 0.00 | 0.00 | 14.37 |
| 8       | 22.82 | 0.00 | 1.36 | 0.96 | 0.00 | 13.59 | 0.00 | 0.00 | 0.00 | 0.00 | 14.19 |
| 10      | 22.67 | 0.00 | 1.31 | 0.94 | 0.00 | 13.78 | 0.00 | 0.00 | 0.00 | 0.00 | 14.08 |
| 15      | 22.56 | 0.00 | 1.21 | 0.93 | 0.00 | 14.12 | 0.00 | 0.00 | 0.00 | 0.00 | 14.54 |
Figure 16 exhibits the variety of EBF and EABF data with the gamma-quanta energy up to 15 MeV. The EBF and EABF data seem to have their minimum values in the low gamma-quanta energy zone. This is due to the gamma photons passing through the studied glass material linked with the PE phenomena. In this region, the sharp peaks of both factors are reported around the quanta energy (0.0318 MeV). The increment of quanta energy leads to the increase in the accumulation of gamma photons inside the material, where the CS process is significant. The drop photons interacted with and penetrated the studied glass thickness while the rest of the photons are scattered to induce multiple interactions. In the CS region, the EBF and EABF data reach their maximum values. After that, it can be seen that the both factors began to decrease when the gamma-quanta energy had high values thanks to the third interaction as represented in the PF (Mahmoud et al., 2020; YS. Rammah et al., 2020).

Furthermore, Figures 17 and 18 show that the EBF and EABF data impacted the penetration depth, which changes from 0.5 to 40 mfp at four specified gamma-quanta energies of 0.015, 0.15, 1.5, and 15 MeV, as well as the chemical composition of TABLi glasses.

Figures 17 and 18 manifested the exchange of EBF and EABF data with the penetration depth (PD) at identified gamma-quanta energy (0.015, 0.15, 1.5, and 15 MeV) prominently. The photon accumulation inside the glass material is associated with the distance that photons will travel as well as the time spent inside the investigated material. The low EBF and EABF data are identified at the short traveling distance (0.5 mfp), while the highest data was achieved at the long traveling distance (40 mfp). Moreover, the alteration of Li2O within the examined glass material was due to the elevation of EBF and EABF.

Figure 19 showed the variation of the LAC and the microhardness (H) versus the Li2O concentration. The LAC of the investigated samples diminished while the H values enhanced by increasing the Li2O substitution ratio. The glass sample with Li2O content of 5 mol% (TABLi5) has the highest LAC (LAC = 0.276 cm⁻¹) at energy 0.662 MeV, but the microhardness of the mentioned sample is relatively low (H = 4.900 GPa). In contrast, the sample with Li2O content of 25 mol% (TABLi25) has the lowest LAC value (LAC = 0.236 cm⁻¹), but it has the highest H value (H = 5.199 GPa). Thus, the correlation showed in Figure 19 is used to predict which sample has both LAC and H suitable values. According to this relation, the sample with a suitable LAC and H contains around 16 mol% of Li2O concentration. The microhardness of this glass (i.e., containing 16 mol% of Li2O) is around 4.055 GPa, and the LAC is about 2.585 cm⁻¹.

![Graph showing the relationship between microhardness and linear attenuation coefficient](image_url)

**Figure 19.** Relationship between the microhardness and the linear attenuation coefficient (LAC) for the various investigated samples.
4. Conclusions

The microhardness and softening temperature, elastic moduli and Poisson ratio were calculated based on the M–M model. The microhardness and Poisson ratio were enhanced by the replacement of the TeO$_2$ by the Li$_2$O. The H values increased from 4.90 to 5.20 GPa, and σ values rose from 0.267 to 0.280, raising the Li$_2$O concentration between 5 and 25 mol%, respectively. The elastic Young, shear, longitudinal, and bulk modules were enhanced by increasing the Li ions in the glass network. Also, the shielding characteristics showed that the LAC was diminished with the replacement of Te by Li ions in the glass network. The LAC decreased from 30–90 to 24.40 cm$^{-1}$ at 0.015 MeV when the Li$_2$O concentration increased between 5 and 25 mol%, respectively. The HVL and MFP values increased by raising the Li$_2$O concentration in the glass network. Additionally, the accumulation of photons in air EBF and inside the glass layers (EABF) was increased by increasing the Li$_2$O concentration.

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