A cost-effective device and methodology to compute aquifer transmissivity and piezometry from free-flowing artesian wells

Alix Toulier1,2,3 · Patrick Lachassagne3 · Heru Hendrayana4 · Arif Fadillah5 · Hervé Jourde3

Received: 16 September 2021 / Accepted: 2 June 2022 / Published online: 19 July 2022
© The Author(s) 2022

Abstract
Artesian aquifers offer interesting opportunities for water supply by providing a low-vulnerability groundwater resource that is easily abstracted without any installation of pumps or power supply costs. However, hydraulic tests are challenging to perform, notably where the piezometric head is above ground level with free-flowing wells not equipped with valves and open for years. This paper describes a low-cost, easy to reproduce and adaptable device, the free-flowing artesian well device (FFAWD), which is mainly designed with a set of PVC tubes equipped with a pressure probe and a valve. This device is used to perform hydraulic tests on free-flowing artesian wells, to measure the piezometric head of the aquifer and to compute its transmissivity. The practical use of the FFAWD is described and a method is proposed to compute the piezometric head and the transmissivity of the aquifer from this data set (free-flowing well discharge and pressure increase measurements) with any adapted analytical solution, using the Houpeurt-Pouchan method. Artefacts such as post-production effects, surge effects, and the impact of a leaky well are identified to avoid any misinterpretation. The FFAWD was applied to the volcano-sedimentary artesian plain of Pasuruan (Indonesia). The advantages and limitations of using the device, along with the interpretation methodology, are also discussed.

Keywords Equipment/field technique · Aquifer testing · Hydraulic properties · Free-flowing artesian well device · Indonesia

Introduction
Artesian conditions develop where the hydraulic head of an aquifer is higher than the topographic surface, allowing the free-flow of groundwater through artesian wells (and/or springs). Large artesian systems are widespread, such as the Great Artesian Basin in Australia (Flook et al. 2020; Habermehl 2020), the Dakota Sandstone in the USA (Meinzer and Hard 1925), and the Ordos Plateau in northwestern China (Jiang et al. 2018). Smaller volcanic systems also display artesian conditions, such as the Honolulu artesian basin in Hawaii (USA) (Wentworth 1951) and the volcano-sedimentary aquifer of Pasuruan in Indonesia (Toulier et al. 2019). Such artesian systems are of great interest insofar as the groundwater withdrawal does not require any pump installations or incur power supply costs. This is important in developing countries, notably where groundwater is used by low-income farmers (Khasanah et al. 2021). Moreover, these aquifers, where they are confined by an impervious layer, often provide very high-quality groundwater (in terms of microbiology and anthropogenic contaminants) due to the confined conditions.
Confined aquifers have been surveyed and studied in several places around the world for a long time, at least as early as the 19th century, notably the water wells drilled in the Artois region of the Paris Basin (France) from which the term “artesian” is derived (Margat et al. 2013). However, the term “artesian” may cause confusion since, with proper topographic undulation, flowing artesian wells can also develop in an unconfined aquifer (Jiang et al. 2020). Freeze and Cherry (1979) identified two mechanisms for the existence of flowing artesian wells which were named “geologically controlled” and "topographically controlled" (see Fig. 1). This study particularly focuses on the geologically controlled conditions related to a confined aquifer configuration (i.e. artesian aquifer). Accordingly, the term “free-flowing artesian well (FFAW)” is used in this paper.

Several studies, some including hydraulic tests, have demonstrated the elasticity and deformation properties of water-bearing layers in artesian aquifers (Meinzer 1928; Thomp-son 1929). Other studies have pointed out the complexity of such aquifers regarding the transmission of pressure changes (Legette and Taylor 1934; Versluys 1930) and the rate of spreading of the depression cone (Lohman 1965). However, hydrodynamic studies of artesian systems have mostly focused on only a few free-flowing artesian wells (e.g. in the Table Mountain Group aquifer in South Africa (Lin 2007), the Honolulu artesian basin in Hawaii (Nichols et al. 1996), the Dakota Sandstone in the USA (Meinzer and Hard 1925), and the Ordos Plateau in northwestern China (Wang et al. 2015). A better understanding of such aquifer systems needs a basin-scale hydrogeological characterization that can be undertaken using low-cost and easy to implement devices and methods.

Since the 1960s, several devices for flowing wells have been designed, such as the photographic method with a camera and manometer (Wyrick and Floyd 1961) or use of an ink-well mercury gage for water head monitoring (Lohman 1965). A more accurate device was proposed by Oberlander and Almy (1979), using an ultrasonic flowmeter. Recently, a device was designed by Sun and Xu (2014), integrating an ultrasonic flowmeter and pressure transmitter, and electrical conductivity (EC) and pH probes, all with connections to a data logger requiring an external power supply. Despite the progress in such devices, their use remains complex and laborious in remote locations lacking a power supply or inaccessible by car, for instance in agricultural areas with paddy fields. In addition, in some developing countries, the poor design of the well heads does not allow the use of classic devices such as ink-well manometers or any other valving equipment at the well head (Khasanah et al. 2021) as the well head will not resist the so-created pressure. Adding a length of transparent glass tubing with graduated scale has been a quite common practice to visualize and measure the piezometric level at flowing wells since Jacob and Lohman (1952). To date, no research has been published on a more sophisticated version of such devices. Therefore, this paper presents a new device that can be adapted for a wide roll-out on numerous free-flowing wells over a short period of time, notably during piezometric surveys.

This study proposes (i) a simple device and method, both cost-effective and easy to implement, without any need for an external power supply, and (ii) a data interpretation methodology, to compute the transmissivity of the aquifer and to access the piezometric head of free-flowing artesian wells.

This method is applied to the artesian volcano-sedimentary aquifer of Pasuruan, located at the foot of the Bromo-Tengger volcano (East Java, Indonesia), in order to draw its piezometric map, and to characterize its transmissivity. The advantages and limitations of using the device, along with the interpretation methodology and the obtained results (piezometry, transmissivity, conceptual model of the aquifer) are discussed.

Methodology

Basic concepts about artesian aquifers

The aim of the device and the associated data interpretation method is to perform measurements that can be used to estimate: (i) the hydraulic head \( h \) of the aquifer (Fig. 2), and (ii) the transmissivity \( T \) of the aquifer.

As a reminder:

The hydraulic head \( h \) is defined according to the Bernoulli theorem (Banton and Bangoy 1997), as follows:

\[
h = \frac{u^2}{2g} + \frac{P}{\rho g} + z
\]

Fig. 1 a Geologically-controlled and b topographically-controlled free-flowing artesian wells (modified from Jiang et al. 2020)
where:

\[ h \text{ piezometric head of the aquifer (m)} \]
\[ u \text{ fluid velocity (m s}^{-1}) \]
\[ P \text{ water pressure at the measurement location (kPa), not taking into account the atmospheric pressure (water pressure minus atmospheric pressure)} \]
\[ \rho \text{ volumetric mass of water} (\times 10^3 \text{ kg m}^{-3} \text{ in standard conditions}) \]
\[ g \text{ acceleration due to gravity (9.81 m s}^{-2}) \]
\[ z \text{ elevation above a given datum (m)} \]

In porous media, the fluid velocity is very slow, allowing one to ignore the kinetic energy term \( \frac{1}{2} u^2 \), so the hydraulic head \( h \) can be simplified by the piezometric head \( H \) given by the following equation (De Marsily 1986):

\[ H = \frac{P}{\rho g} + z \quad (2) \]

A free-flowing artesian well (FFAW) has a piezometric head \( H \) that is higher than the topographic surface or, rather, higher than the top of the well head (WMO, W. M. O, and UNESCO 2012; Chen et al. 2018). However, an artesian well is not necessary flowing at the surface as illustrated in Fig. 2.

In the following parts of this paper, the developed device will be referred to as a “free-flowing artesian well device” (FFAWD).

**Design of the free-flowing artesian well device (FFAWD)**

The principle of the measurement method is to install the device on the well head (Fig. 3a), allowing the pressure to increase inside the device and be monitored. The device is built up as follows, from bottom to top (with spare parts respectively labeled from (I) to (V) in Fig. 3c):

- A PVC tube (labeled (I)) whose base diameter can be changed in the field to adapt to the well head diameter. It can also be equipped with an elbow tube in case the outlet of the free-flowing well is not vertical. This first tube comprises a smaller tube which is fixed inside to install and secure the pressure probe. Note that for pressure probes not compensated for atmospheric pressure, a barometer probe might be useful for such a compensation; however, as these measurements are performed during a short period of time (usually less than one hour), during which atmospheric pressure changes are expected to be very low, this is not mandatory. The pressure probe is easy to extract from the device, to download data when the measurement process is over, and is also easy to reinsert.
- A T tube (II) whose horizontal outlet is equipped with a valve.
- The vertical outlet (III) of the T tube is equipped by successively adding tube sections depending on the \( H \). Then, a transparent acrylic graduated pipe (IV) is connected with a last tube section, open at the top, which allows observation of the water level during the test. The top of this transparent pipe is equipped with an elbow outlet (V) to redirect the water flow if \( H \) is higher than the measuring device, to avoid wetting the technicians as well as to enable discharge measurements.

This study used a Van Essen TD-Diver pressure probe for water levels ranging from 0 to 10 m, with a +/- 0.5 cm precision and a resolution of 0.06 cm. The pressure was recorded at 1 s intervals. The PVC and acrylic pipes are 100 mm (4 inches) in diameter. Acrylic/PVC tubes, up to 6 m long, were connected to each other to measure high piezometric heads. Only the last tube is composed of a 2 m transparent acrylic pipe. A maximum water level of 8 m above ground surface was measured with this device.

**Measurement procedure**

First, it is important to select reliable free-flowing artesian wells without any visible leakage between the casing and the ground surface, since grouting can be of poor quality or non-existent in wells owned by farmers with modest means such as in Pasuruan. The wells with a concrete base, satisfactory grouting and a well head in good condition (no corrosion or breaking) were selected in priority. However, as seen later (Results section), some tested wells were leaking. It is also recommended to select wells with a vertical, open and straight pipe long enough to connect the device. Wells with a well head diameter less than 7-8 cm (3 inches) are not recommended as they are not strong enough for the device.
and may break during the test. A prior manual discharge measurement \((Q_0)\) allows a rough estimate of the number of PVC tubes required for the hydraulic test. Of course, the selected wells should meet the purpose of the study: for instance, a homogeneous spatial distribution to ensure an accurate piezometric map, or locations chosen to characterize the hydrodynamic properties (e.g., \(T\)) of various lithological units. Then, the measurement procedure comprises four main steps respectively illustrated in Fig. 3: 

Step 1. Discharge measurement: Measurement of the “steady” discharge of the free-flowing well \((Q_0)\). The fitting of an elbow on the vertical pipe improves the accuracy of the flow measurement, even if it may slightly reduce the discharge due to the slight increase of the piezometric head (in this study, the reduction is between 3 and 5%; this point is addressed in the Discussion section). The discharge measurement is performed manually with a bucket or any other graduated or gauged collection device (FFAWD) and measurement method through steps 1 to 4.
Step 2. Device installation:

a. The setting up and calibration of the pressure probe is carried out before setting it inside the device.
b. The device is installed on the well head with the valve open (Fig. 3a).
c. After a few minutes of flow stabilization (that can be regularly measured), as there is a change in piezometric head related to installation of the device ($P_{\text{in}}$), a discharge measurement is performed to estimate the “initial” well discharge ($Q_{\text{in}}$). As written above, it is recommended to perform several discharge measurements to reduce the uncertainty on this data.
d. The height parameters of the device are measured: at least, height from ground surface to well head ($d_1$) and from the well head to the exact position of the pressure probe ($d_2$).

Step 3. “FFAWD Recovery test”:

e. The valve is closed (Fig. 3a), which induces a rapid rise of the water level/pressure in the tube. The transformation of kinetic energy (water flowing up in the well tube at a significant velocity) into potential energy may cause some pressure fluctuations during the first few seconds after closure of the valve, as described further below. Then, the valve must not be closed too suddenly (closing duration: 2 to 3 s). The time at which the valve is closed must be noted. Nevertheless, it is also monitored by the pressure probe.
f. A “recovery period” of about 30 min is recommended during which the pressure build-up ($dP$) is monitored with the sensor until pseudo-stabilization of $H$. The choice of the duration of this period is discussed in the following sections.
g. Then the valve is re-opened and the finishing discharge ($Q_{\text{fin}}$) is measured (as well as the time of the measurements), similarly as in §3.c above.
h. Then the device is removed, and the discharge ($Q_0$) is measured (as well as the time of the measurements), similarly as in Step 1.

Step 4. GPS measurements: a differential global positioning system (GPS), Trimble R6, was used to measure the precise coordinates ($x$, $y$, $z$) of the well head (or any other fixed landmark), based on the satellite signals received both at the rover and base stations (Parkinson and Spilker 1996). The geoid height is corrected considering the gradient of the local geoid (Kasenda et al. 2000). Then, the ellipsoid height measurements are converted into meters above sea level (m a.s.l.) using a digital elevation model (USGS SRTM30 dataset). With the differential GPS used here, the relative precision in $z$ elevation between each well is about +/-10 cm.

Hydrodynamic response interpretation

Description of the hydrodynamic response

Under such artesian conditions, the “FFAWD recovery test” is divided into four main phases, some of these phases being named by Sun and Xu 2014 (Fig. 4):

Phase (i), the “adjusting period” ($t_0 \rightarrow t_1$): Sun and Xu 2014, during which the well is drilled, with a discharge different from nil after the aquifer is reached. Once the top of the aquifer is drilled, the well discharge increases rapidly while the piezometric head is imposed to the well head elevation;

Phase (ii), the “free-flowing” period ($t_1 \rightarrow t_2$): this follows the rapid opening of the well that triggers a decrease in discharge. This period is the focus of most studies dealing with free-flowing wells (see for instance Sun and Xu 2014). In contrast to all those studies, the wells in this study were drilled several months or years before the test, without any well closure period, so the free-flowing period was long enough to reach a steady state. The discharge is considered as steady (as well as the one of nearby wells), and the piezometric head at the well is consequently also considered as stabilized, except during phase 2 of the device’s installation. This issue of steady state is addressed in the Discussion section of the paper;

Phase (iii), the “FFAWD recovery test period” ($t_3 \rightarrow t_4$): the closure of the well as described in section ‘Design of the free-flowing artesian well device (FFAWD)’ allows the pressure to increase inside the device, until it reaches equilibrium with the aquifer piezometric head. In the vicinity of the well, the piezometric head in the aquifer also increases;

Fig. 3b, shows a typical pressure graph obtained during this procedure.
Phase (iv), the “Post-test period” \((t_4 \rightarrow t_{\infty})\): After reopening of the well and removal of the device, the well returns to its previous test conditions.

Each phase described above may enable computation of the aquifer hydrodynamic parameters through different interpretation methods, but the longer duration of two phases (the free-flowing and the FFAWD recovery test period) are considered to yield more robust results. The decrease of well discharge during the free-flowing period can be interpreted by a conventional method developed by Jacob and Lohman (1952), Hantush (1959) and Glover (1987). A simple approximation for the free-flowing well problem was provided by Swamee et al. (2002) using an error minimizing method to compute the discharge. Recently, the diagnostic plot method using the reciprocal rate derivative was adapted for the free-flowing test period by Sun et al. (2015). This phase is inappropriate in this study because the well discharge has been stabilized for a long time at the study site. Moreover, as discharge is generally measured with a lower precision than a piezometric head, this method is not very accurate, notably at the end of the test, when discharge variations decrease (see the Discussion section of the paper).

If the well is closed (again) after completion of a (short-duration) free-flowing period, the recovery test period (measurement of piezometric head) is steady state. The steady state is stopped by the installation of the FFAWD. It allows use of the Houpeurt-Pouchan transient state recovery method (HPTSRM, De Marsily 1986). “Then, the recovery curve is interpreted as a drawdown curve with the help of either Jacob’s or Theis’s method” (De Marsily 1986) or any other appropriate analytical solution. In other words, the HPTSRM involves interpretation of the “recovery” observed after the installation of the FFAWD and the closure of its valve as a “classical” pumping test. The only difference is a negative discharge \(Q_0\) instead of a positive one, and a rising piezometric head instead of a decreasing piezometric head. To the authors’ best knowledge, nobody has described the use of this part of the evolution of the piezometric head for free-flowing wells, and the use of the HPTSRM.

Such a “recovery” test is usually not sensitive to well losses (Willmann et al. 2007) and can be easily interpreted with any appropriate analytical solution, as provided for instance by the software AQTESOLV (Duffield and Court 2007). The Cooper and Jacob (1946) method was already successfully used in other confined aquifers (Jacob 1940, 1947; Jacob and Lohman 1952; Wyrick and Floyd 1961; Merritt 1995) and was used in this research. This analytical solution considers the following simplifying assumptions: a single-well test assuming a confined, homogeneous, isotropic aquifer, with a vertical and fully penetrating well, taking into account the discharge rate \(Q\) and the distance from the

**Computation of aquifer transmissivity**

This study only surveyed “old” wells in steady free-flowing state (without any continuous discharge measurement since their drilling). The steady state discharge is then attained during this long free-flowing period. This steady state is stopped by the installation of the FFAWD. It allows use of the HPTSRM. "Then, the recovery curve is interpreted as a drawdown curve with the help of either Jacob’s or Theis’s method" (De Marsily 1986) or any other appropriate analytical solution. In other words, the HPTSRM involves interpretation of the “recovery” observed after the installation of the FFAWD and the closure of its valve as a “classical” pumping test. The only difference is a negative discharge \(Q_0\) instead of a positive one, and a rising piezometric head instead of a decreasing piezometric head. To the authors’ best knowledge, nobody has described the use of this part of the evolution of the piezometric head for free-flowing wells, and the use of the HPTSRM.
The Cooper-Jacob logarithmic approximation of the Theis solution is given by:

\[ s = \frac{Q}{4\pi T} \ln \left( \frac{2.25Tt}{Sr^2} \right) \]  

(3)

where:

- \( s \): drawdown at the (observation) well (= well and recovery curve in this case) (m)
- \( Q \): discharge (here, before closing the valve) (m³ s⁻¹)
- \( T \): transmissivity (m² s⁻¹)
- \( t \): time since the start of pumping (= time since the beginning of the FFAWD recovery test period) (s)
- \( S \): storage coefficient (-)
- \( r \): the distance between the well and the observation well (piezometer), or the radius of the well in case of the observation is performed at the well itself.

Whence

\[ T = \frac{2.3}{4\pi} \cdot \frac{Q}{\Delta s} \]  

(4)

and

\[ S = \frac{2.25Tt_0}{r^2} \]  

(5)

where:

- \( \Delta s \): drawdown measured during one log cycle
- \( t_0 \): the time at which the Jacob straight line intersects the \( s = 0 \) line

Equation (4) is solved graphically with AQTESOLV on a semi-logarithmic grid by plotting values for the ratio of drawdown on the linear (Y) scale against corresponding values of time (t) on the logarithmic (X) scale. Then, the \( T \) value is calculated using the Cooper-Jacob matching-curve method (Jacob straight-line) and considering a constant derivative period of 1 log-cycle of \( t \) (\( \Delta s \)) (Renard 2005). Note that in this case it was not possible to calculate the storage coefficient (\( S \)) (Eq. 5), as the test is performed without a piezometer. This concern will be discussed in detail in the Discussion section. More complex analytical solutions than the Cooper-Jacob one can be used to interpret the test, if required considering the shape of the observed curves. It will be seen in the Results section that this was not necessary with the data set used here.

### Computation of well-bore storage effect

To avoid any artefacts, it is first necessary to distinguish the well-bore storage effect, called the “post-production effect” (Ungemach et al. 1968; Forkasiewicz 1972) which occurs during the early stage of the FFAWD test, after the discharge of the well has stopped. During that period, it is impossible to estimate the transmissivity of the aquifer. For each well, information given by the derivative curve from Bourdet et al. (1989) is compared with a numerical estimation provided by Eq. (6) (Forkasiewicz 1972), that computes the duration of the “post-production effect”:

\[ t = \frac{25r_d^2}{T} \]  

(6)

where:

- \( t \): duration of the post-production effect (s)
- \( r_d \): radius of the tube constituting the FFAWD (m)
- \( T \): transmissivity (m² s⁻¹)

Then, FFAWD recovery tests were interpreted for 16 free-flowing artesian wells.

### Piezometric and Transmissivity mapping

The piezometric head \( H \) of the confined aquifer at the measured free-flowing well is obtained at the end of the “FFAWD recovery test period” (Fig. 4). In addition, other piezometric heads from manual measurements performed on flowing artesian springs, a lake and non-flowing artesian wells were also used to complete the dataset, as well as FFAW where the device was used, but without monitoring the head rise and thus computing \( T \) (see Table 1 and the electronic supplementary material (ESM)). The representativity of these different values of \( H \) will be discussed in the Discussion section.

### Case study

The free-flowing artesian well device (FFAWD) was applied in the artesian plain of Pasuruan covering about 200 km², located in the north of the Bromo-Tengger volcano in East Java, Indonesia. A detailed description of the geology and the aquifer conceptual model is provided by Toulier et al. (2019) and in the ESM.

Among all the free-flowing wells inventoried, 28 were selected (applying the criteria described in section Measurement procedure) for applying the device and developing
Table 1 | Characteristics of artesian water points and results obtained. The piezometric data refer to four types: artesian springs (AS), non-flowing artesian wells (NFAW), free-flowing artesian wells (FFAW) and surface water (LAKE). Transmissivity ($T$) is computed only at the FFAWs except those where the FFAWD was installed but where the test period was not monitored. For unmonitored FFAWDs, the piezometric head was only measured visually on the device at the end of the test.

| Water point description | FFAWD recovery test results | Piezometric head results |
|-------------------------|-----------------------------|-------------------------|
|                         | Well No. Name Type X (m) Y (m) Depth below ground surface (m b.g.s) Ground elevation from GPS (m a.s.l.) Casing diam. out (mm) Flow $Q$ in (L s$^{-1}$) FFAWD test duration ($t_3 \rightarrow t_4$) (s) Water level above ground surface (m a.g.s.) $T$ (m² s$^{-1}$) Post production effect duration (s) Computed Measured (m a.s.l.) Observed effects (Fig. 5) Reliability (see ESM) |                         |
|                         | 1 Umbulan AS 713304 9141736 - 31.95 - - - - - - - - 32.10 H1 |                         |
|                         | 2 Banyu Biru AS 717072 9143018 - 29.43 - - - - - - - - 28.47 H1 |                         |
|                         | 3 FD2 FFAW 717239 9142550 32 37.36 904 0.2 2999 0.99 3.10 × 10$^{-3}$ 23.4 40 Fig 5a 38.35 H1 |                         |
|                         | 4 Truck FFAW 717107 9144385 50 19.86 1146 8.0 - > 2.85 - - - - - - - - 22.71 H2 |                         |
|                         | 5 AWQ FFAW 716558 9142195 60 39.83 904 0.9 2093 0.74 8.83 × 10$^{-3}$ 8.4 20 Fig 5b 40.57 H1 |                         |
|                         | 6 FD1 FFAW 715390 9142385 103 38.22 904 1.9 1903 3.72 1.06 × 10$^{-3}$ 69.5 50 Fig 5b 41.93 H1 |                         |
|                         | 7 Pasir Well FFAW 715907 9143728 40 19.61 1146 8.6 < 300 3.14 - - - - - - - - 22.75 H2 |                         |
|                         | 8 BenbyAlix FFAW 716175 9144539 63 17.18 773 4.8 1973 2.46 3.45 × 10$^{-3}$ 21.4 25 Fig 5b 19.64 H1 |                         |
|                         | 9 BanyuCam FFAW 716969 9143232 66 29.32 1146 6.0 < 300 3.56 - - - - - - - - 32.88 H2 |                         |
|                         | 10 F8 FFAW 715723 9145698 40 15.86 904 10.0 < 60 7.47 - - - - - - - - 23.33 H2 |                         |
|                         | 11 Aqua Wash FFAW 714339 9146170 96 16.54 1400 15.0 - > 5.2 - - - - - - - - 21.74 H2 |                         |
|                         | 12 AW6 FFAW 720216 9146694 120 16.02 621 0.1 1924 3.68 2.91 × 10$^{-2}$ 2.5 150 Fig 5c 26.04 H1 |                         |
|                         | 13 Aqua Piozo FFAW 713213 9145881 70 19.61 904 12.7 25397 3.48 1.11 × 10$^{-2}$ 6.6 20 Fig 5b 23.09 H1 |                         |
|                         | 14 AW24 FFAW 713888 9144172 60 22.52 904 4.8 < 300 3.98 - - - - - - - - 26.50 H2 |                         |
|                         | 15 AW2 FFAW 709387 9149073 93 24.61 1146 6.0 2097 6.02 2.64 × 10$^{-3}$ 27.9 30 Fig 5a 30.63 H1 |                         |
|                         | 16 P13 NFAW 722866 9145631 30 28.95 1146 - - - 2.54 - - - - - - - - 26.41 H1 |                         |
|                         | 17 Ranu Grati LAKE 721382 9145180 120 23.30 - - - - - - - - - - - - - - 22.88 H1 |                         |
|                         | 18 Michel FFAW 714150 9144515 38 22.36 904 6.0 1420 3.68 2.91 × 10$^{-3}$ 2.5 150 Fig 5c 26.04 H2 |                         |
|                         | 19 AW27 FFAW 711747 9143399 60 32.63 904 4.3 1873 5.77 2.36 × 10$^{-3}$ 31.3 50 Fig 5a 38.40 H1 |                         |
|                         | 20 AW15 FFAW 712173 9142980 52 37.72 1146 6.7 679 2.86 1.00 × 10$^{-2}$ 7.4 10 Fig 5c 40.58 H2 |                         |
|                         | 21 B33 FFAW 710227 9143940 88 44.90 1146 2.1 610 1.13 4.05 × 10$^{-2}$ 1.8 15 Fig 5b 46.03 H1 |                         |
|                         | 22 West Umb FFAW 710267 9143352 133 44.29 1146 18.2 2129 5.08 4.32 × 10$^{-3}$ 1.7 15 Fig 5c 49.37 H2 |                         |
|                         | 23 AW16 NFAW 708369 9143299 140 66.20 1146 - - - 6.74 - - - - - - - - 59.46 H1 |                         |
|                         | 24 AW21 FFAW 708963 9145059 120 46.60 1146 3.2 1800 0.96 - - - - - - - - 47.56 H2 |                         |
|                         | 25 AW74 FFAW 709306 9145872 79 36.26 1146 3.1 1935 3.03 2.04 × 10$^{-3}$ 36.1 30 Fig 5c 39.29 H2 |                         |
|                         | 26 AW23 FFAW 711390 9145489 83 31.61 1146 5.2 1069 6.12 2.14 × 10$^{-3}$ 34.4 30 Fig 5a 37.73 H1 |                         |
|                         | 27 AW14 FFAW 711972 9147092 60 22.16 1146 8.0 225 2.12 2.62 × 10$^{-2}$ 2.8 20 Fig 5b 24.28 H1 |                         |
|                         | 28 B23 FFAW 707564 9147142 81 36.96 1146 11.2 2097 5.5 5.24 × 10$^{-3}$ 14.1 30 Fig 5b 42.46 H1 |                         |
|                         | 29 B19 FFAW 707594 9146821 150 37.88 904 35.0 < 60 7.26 - - - - - - - - 45.14 H2 |                         |
|                         | 30 AW33 FFAW 705998 9146529 200 44.48 904 12.7 < 60 7.69 - - - - - - - - 52.17 H2 |                         |
the methodology presented. That includes 16 FFAWD test interpretations, enabling one to compute the transmissivity and measure the piezometric head, and 12 FFAWD tests enabling only measurement of the piezometric head (the piezometric rise was not monitored). In addition, two non-flowing artesian wells, as well as two artesian springs and one lake supplied by the confined aquifer, were also considered for the piezometric mapping.

All the measurements were performed over a short period of time, from May to June 2018, to obtain a synchronous piezometric map. Table 1 reports the characteristics of the wells, springs and lake, along with the results obtained.

## Results

### Computation of hydrodynamic parameters

The FFAWD recovery test parameters for the 16 free-flowing wells are reported in Table 1. The semi-log curves (Fig. 5) show a post-production effect followed by a period of piezometric head rise corresponding to the aquifer response. Overall, three types of curves can be distinguished:

a. **Ideal FFAWD test with post-production** (Fig. 5a): the entire test does not seem to be disturbed by any external effects (except post-production). The inflection point of the drawdown curve after the post-production effect is followed by a second phase of constant rise over time (confined aquifer without any limit or leak) which enables computation of $T$. The slope of the line is steady after the end of post-production. The end of the post-production effect corresponds to the end of the hump in the derivative curve. It is visually delimited by the vertical black dotted line on Fig. 5.

b. **FFAWD test with surge** (Fig. 5b): the beginning of the FFAWD test is impacted by a water hammer effect due to the too fast closure of the well, which causes a sudden change in water velocity in the well (down to zero). The corresponding kinetic energy is converted into piezometric head (Vasquez 2010) and triggers sinusoidal fluctuations. This can mask the inflection point of the curve at the end of the post-production phase (and thus partly hide the post-production) but does not affect the part of the curve for which interpretation is critical to compute the transmissivity (Wyrick and Floyd 1961). As the authors experienced such surges during the tests, it is recommended in Step 3 in section Measurement procedure to close the valve slowly, particularly in wells with a high discharge (relative to well diameter).

c. **FFAWD test with leaks** (Fig. 5c): the inflection point of the post-production phase remains clearly visible. After
a first phase of constant recovery, recovery is influenced by leaks in the well or, less probably, from the aquifer itself (leakage). This leak effect reduces the slope of the curve, or even the piezometric head, at wells. The leakage increasing with time is interpreted by the de-clogging of the well annulus. The unaffected part of the curve (here on Fig. 5c between 10 and 100 s) should be used to compute the aquifer transmissivity. In the case of a leaky aquifer, the affected part of the curve can be interpreted with an appropriate analytical solution to characterize aquifer leakage parameters.

Some FFAWD recovery curves can combine the three types effects presented here (surge, post-production, and leaks), even though the post-production effect is often masked when there is a surge.

A compilation of the FFAWD test results shows that:

- The post-production duration ranges from a few seconds to 180 s depending on the well (30 s on average). A comparison of the durations of the post-production effect, computed from Eq. 6, and graphically determined, shows no significant discrepancies. Only well n°18 shows an inconsistent result but the transmissivity value used in Eq. 6 is probably overestimated as suggested by the leak effect (type c) considered for this well (Fig. 6a). Thus, globally, this post production effect is well understood and computed. The intercept or the regression curve (about 10 s) means that the observed post-production effects are about 10 seconds longer than the computed ones. This is surely due to an additional volume of the FFAWD that is larger in the section with the valve (Fig. 3) than elsewhere (tube only); in fact, the diameter of the tube was used to compute the theoretical duration of the post-production effect, and the section with the valve was not considered.

- The constant log-log derivative curves at long duration (e.g. between 80 to 1000 s in Fig. 5a) confirm that the response of the aquifer well follows the Cooper-Jacob straight line. A two-dimensional infinite acting radial flow model (IARF) can be assumed, describing a flow converging towards the circular cylinder of the well (Renard et al. 2009). Thus, no more complex analytical solution (for instance with well partial penetration effect) is required in this case study. The transmissivity results range from $10^{-2}$ to $10^{-4}$ m² s⁻¹, with an arithmetic average value of $10^{-3}$ m² s⁻¹.

Results for the Pasuruan artesian plain, Indonesia

The results of the FFAWD application including the piezometric and transmissivity maps are provided in the ESM.

Discussion

The FFAWD device

The device developed in the framework of this research (FFAWD) shows the following advantages:

![Figure 5](image_url)  
**Fig. 5** Representative piezometric head data recorded during the FFAWD tests at wells, sorted into three categories: a. well n°26: recovery curve without any visible influence, except for post-production effects, b. well n°8: recovery curve influenced by surge effect during the first tens of seconds of the test (=sinusoidal curve), the post-production is largely masked, and c. well n°20: recovery curve influenced by leaky well or internal leakage within the aquifer itself (in addition with post-production effect). All the FFAWD recovery test periods are interpreted with the Cooper-Jacob solution (red curves).
It is easy to build (PVC pipe and valve available everywhere in the world) and low cost: less than 100€, pressure sensor not included;

It is very fast (<10 min) to install on various diameter/discharge wells and easy to deploy in the field by 2 operators. It is much less convenient if the operator is alone, which must be avoided;

No external power supply is required;

The visibility of the water within the transparent pipe during measurements is important, notably to see and visually follow the evolution of the water level during its early phase, and to visually check the progress of the test. This also reassures the local population/owner of the well that the water is “still there”, even if the well ceases to flow during the test;

The obtained data are accurate and reliable.

The following shortcomings of the device could be resolved in the future:

Beyond 8 m of piezometric head above ground surface, the tubes (4 x 2 m) become unstable and a supplementary shoring system is necessary. A lightweight telescopic scaffolding as used in civil engineering could effectively stabilize the tubes. The diameter of the tubes could also be reduced to decrease the weight of the FFAWD during its operation, but with strong enough tubes to maintain the required rigidity of the device;

The use of other probes (e.g., CTD Diver) may provide monitoring of additional physico-chemical parameters during the hydraulic test (EC, temperature, pH, etc.). It might enable one to detect well leakage (Fig. 5c).

**Method of measurement**

First, the method using several PVC pipes (keeping a free water surface) was preferred to the method involving the closure of the artesian well. From the authors’ experience, the water pressure makes it very difficult to completely close the well. For instance, the free-flowing artesian well device (FFAWD) developed here is hard to maintain in place under such a high-pressure head (> 6 m) and would require an additional fixing system.

Even with the FFAWD, if the well grouting is not totally impervious (no grouting or casing/grouting too short and/or in poor condition), a leak between the well casing and the rock may appear during the test as diagnosed for wells n° 18, 20, 22 and 25 (Table 1; observed leakage effect as shown in Fig. 5c). Another type of leak may occur inside the aquifer itself, especially in open-hole wells where two water-bearing formations have different piezometric heads, such as in a multi-layered system classically found in volcano-sedimentary plains (Selles et al. 2015). Thus, the selection of free-flowing artesian wells with a good visual aspect is a priority before applying the device on large scale, even if it is not a guarantee of no leaks. A concrete base around the well head is a good indication that the well is probably less liable to leak, although this is not always the case. Nevertheless, most observations with leakage at the well enabled one to compute $T$.

As regards the duration of measurements, a recovery period of 30 min is appropriate because (i) it does not cut off water access to the local population for an excessive period (e.g. paddy field irrigation or domestic use); and (ii) most of the tested artesian wells with different configurations (transmissivity, discharge, depth, etc.) provided a well-defined Jacob’s straight line on the drawdown curve, allowing one to easily compute $T$.

**Data interpretation**

The interpretation of FFAWD recovery tests by the Cooper-Jacob method yields consistent transmissivity results in this case study, ranging over 1 to 2 orders of magnitude (from $10^{-2}$ to $10^{-4}$ m² s⁻¹). Transmissivity is probably overestimated for at least well n°18 which is influenced by leaks, with values of about $10^{-2}$ m² s⁻¹; but the analysis of the Bourdet derivative allows one to avoid possible bias related to (1) post-production effects (∼ well-bore storage) and (2) leaks related to the well casing or the aquifer itself, by applying the Cooper-Jacob straight line on a constant derivative period. Thus, there is finally no real issue with such leaks. In this case study, the simple Cooper-Jacob solution is appropriate to interpret the data. However, other more complex analytical solutions could be used if necessary to account for anisotropy and incomplete well effects, a discussion of which is beyond the scope of this paper.

The discharge $Q_m$ was used to calculate the transmissivity; it corresponds to the discharge measured before closing

---

**Fig. 6** Comparison of the duration of the post-production effect between computed values (Eq. 6 from Forkasiewicz (1972)) and values graphically determined from the derivative curve.
the valve of the device. Theoretically, it would have been better to use $Q_0$, measured before installing the FFAWD on the well head. However, the precision on $Q_0$ is usually lower than the one on $Q_{in}$ as discharge measurements are often hard to perform on a well head that protrudes little above the ground. Using $Q_{in}$ instead of $Q_0$ does not significantly influence the transmissivity computation. Measurements show that the discharge $Q_{in}$ is about 3 to 5% lower than $Q_0$ (depending on the length of the PVC connections installed); then, the computed transmissivity is about 3 to 5% lower than the actual one, and can easily be corrected with $Q_0$ measurements, although there is much lower accuracy than the $Q_{in}$ measurements. Experience gained during this research shows that the stabilization to $Q_{in}$ is very fast (not measurable in fact, the repeated $Q_{in}$ measures being within the uncertainty range of the stabilized $Q_{in}$ value).

FFAW tests are performed in such an aquifer where, due to the year after year abstraction increase, the piezometric level is declining with time and the discharge of each well is also declining. Thus, two FFAW tests performed at two dates separated by several years will have the following characteristics:

- The first test will exhibit a higher discharge than the second one, but also, consequently, a higher slope of the Cooper-Jacob straight line (Eq. 4);
- The second test will exhibit a lower discharge but also a lower slope of the Cooper-Jacob straight line.

Consequently, the computed transmissivity will be the same whatever the date of the completion of the FFAW test. In fact, as for any pumping test, there is no bias related to the discharge of the well during the pumping test. The computed transmissivity is the same whatever the discharge of the pumping test.

In this case study, the piezometric head measured at the end of the FFAWD test period (good reliability (H1) and medium reliability (H2) in Table 1), that rarely exceeded 30 min, was used to draw a piezometric map. However, not all recovery tests performed during this field campaign had the same duration. Moreover, the recovery was not totally completed during most tests, and the recovery rate is also well-dependent, as not all free-flowing wells have the same discharge; well discharge depends notably on the local hydrodynamic conditions ($T$ and $S$) and piezometric head. A sensitivity analysis to estimate these impacts on the computed piezometric head was thus performed and showed that the homogenization of the data may require a piezometric correction ranging, for this case study, between -0.70 and +0.79 m, but with 75% of the wells having corrections ranging only between -0.2 and +0.2 m. It then appears that, for this case study and the chosen application (basin-scale piezometric mapping for which about 1 m accuracy is enough), such a correction is not necessary. The conclusion would not be identical for a high-resolution piezometric mapping, at the scale of a civil engineering project for instance, requiring piezometric levels with a centimeter accuracy. The sensitivity analysis computation was performed at each well, based on the estimation of the time required to recover, with the transient-state Jacob analytical solution (De Marsily 1986), and the steady state drawdown at the well computed with the Dupuit analytical solution (De Marsily 1986), considering a complete recovery minus 1 m. For calculation, this study used a confined aquifer with a $10^{-4}$ storage coefficient, the transmissivity computed at the well and a geometry (distance to aquifer limits notably) similar to the one of the studied Pasuruan aquifer (less than 10 km).

Similar computations with the same parameters were performed to check that all FFAWs can be considered in steady state before completion of the tests. They show that such a steady state is obtained in a few months after the drilling of the FFAW (2 to 3 months). As most studied FFAW were drilled years ago, this assumption is valid.

**Computing the aquifer storage coefficient**

From aquifer tests, it is well known (see for instance Kruseman and Ridder 1971; De Marsily 1986) that the storage coefficient cannot be computed from data obtained at the pumping well as there is a large uncertainty on the well effective diameter, and also as well clogging or over-development quite often shifts the drawdown curve. Such a shift, theoretically, has no influence on the computation of $T$ (notably if the discharge is steady), or it can be overcome. However, it strongly influences the location of the intersect of the Jacob straight line with the zero-drawdown line. Thus, an observation well (piezometer) is mandatory for that purpose, which wasn’t the case in the research report here. Additionally, for classical pumping tests, $S$ cannot be obtained from the recovery data (residual drawdown) obtained after the completion of a pumping with the Theis or the Cooper-Jacob methods (Todd and Mays 2005). Some authors, nevertheless developed new methods to compute the storage coefficient from single-step pumping test recovery data (Banton and Bangoy 1996; Ashjari 2013), from multi-step pumping test recovery data (Lee and Lee 2000) or from the Agarwal recovery test method (Trabucchi et al. 2018). However, all these methods require data from a piezometer. For free-flowing wells, some authors proposed to compute the storage coefficient based on single-well tests, by monitoring the drawdown and the discharge at the well after opening it (Jacob and Lohman 1952; Ojha 2004; Wendland 2008; Perina 2021) (i.e. the well is opened after a long period without flow). These authors claim that no piezometer is required since they assume the well to have an infinitesimal radius (i.e.
the “effective radius” of the well is used by Jacob and Lohman (1952). In the case reported here, no continuous discharge measurement was performed (nevertheless, instead, piezometric levels were observed, which is equivalent), no piezometer was available near the tested free-flowing wells, and the effective radius of the wells was unknown. Nevertheless, the storage coefficient was computed with the Cooper-Jacob method (Kruseman and Ridder 2000) and the real radius of the well (radius of tube). It resulted in physically unacceptable values: 13 values between $S = 3.10^{-83}$ and $3.10^{-9}$, and only three “more acceptable” values: $1.10^{-4}$, $3.10^{-6}$, and $9.10^{-6}$. This demonstrates, if any proof were needed, that $S$ can hardly be computed from data observed at the well. Moreover, the very low values of the computed $S$ suggest very small effective radius, and thus that most the wells in the study area are clogged (rather than overdeveloped).

As a solution to compute $S$, it would be worthwhile to build several FFAWDs. They could then be installed on nearby FFAWs to not only compute $T$ and $H$ at these different wells, but also to trigger interferences between them and thus enable the computation of the storage coefficient $S$ from the aquifer. A simple procedure is then:

1. The FFAWDs would be installed, and their valve closed on FFAWs surrounding the studied FFAW.
2. Then, after $H$ reaches an equilibrium at all these wells (this transient period being monitored to compute $T$ and $H$), sequences of closing and opening the valve at the studied FFAW would be performed. This FFAW and the surrounding ones (with closed valves) would be monitored.
3. These tests would be interpreted as for any pumping test performed with piezometers in an aquifer.

A first sensitivity analysis shows that such a $S$ computation should be feasible in such a confined aquifer where the drawdown propagates fast and far. Computations were performed with the Cooper-Jacob analytical solution with $T = 1.10^{-3}$ m² s⁻¹, $S = 1.10^{-4}$, and a tested FFAW with a 5 L s⁻¹ discharge. They show that interferences of about 30 cm are obtained at a distance of 200 m one hour after the valve is closed (or reopened). The interferences are about 80 cm at a 100 m distance, far enough to compute $T$ and $S$ from these data. The interferences are already 55 cm after half an hour at 100 m, but only a few millimeters at 200 m. Practically, on the Pasuruan aquifer, the tests applied on “piezometers” equipped with a FFAWD could be performed in a 100–150 m radius around the tested FFAW. This appears highly feasible considering the density of FFAWs in that area. In any other aquifer, the feasibility could be assessed a priori with such a rough computation.

### Case study: insights on the aquifer’s functioning

Based on the case study provided in the ESM, the transmissivities (from $10^{-2}$ to $10^{-6}$ m³ s⁻¹) are relatively high and very consistent with other volcanic contexts (Hunt 1996; Singhal and Gupta 2010; Charlier et al. 2011; Lachassagne et al. 2014; Selles 2014; Dumont et al. 2021). The groundwater flows northward from the northern flank of the volcano to the volcano-sedimentary aquifer of Pasuruan. The piezometric pattern indicates a recharge zone from the volcano and a discharge zone spreading in the plain through the free-flowing artesian wells and artesian springs’ outflows. The hydraulic gradients range from 0.001 to 0.01.

A periodic deployment of the FFAWD for piezometric surveys of the Pasuruan artesian basin could provide robust information about the evolution of the piezometry and be used as a decision support tool for water resources stakeholders.

### Conclusion

The design of a low-cost field-built device that is easy to reproduce and adaptable to various conditions, the free-flowing artesian well device (FFAWD), is described in this paper, as well as the method to set it up in the field, in aquifers where free-flowing wells are not valved and have been continuously flowing for months or years.

The principle of the method is (i) to install the FFAWD on the well head, its valve open, allowing to (ii) measure the discharge of the free-flowing well; then, (iii) to close the valve that allows the pressure to increase inside the FFAWD, and be monitored with a sensor. At the end of the test, (iv) the valve is open again; (v) the discharge is measured once more, and the FFAWD is uninstalled.

The obtained data set is the discharge of the free-flowing well, and pressure increase measurements after its valving with the FFAWD. The test is interpreted as a single-well pumping test. A method is proposed to compute the piezometric head and the transmissivity of the aquifer from this data set, using the Houpeurt-Pouchan method and any adapted analytical solution (such as the Cooper-Jacob analytical solution). Artefacts, such as post-production, surge effect, and impact of a leaky well, are identified and described to avoid any misinterpretation.

The FFAWD was successfully applied on the volcano-sedimentary artesian plain of the Bromo-Tengger volcano (Indonesia) for transmissivity and piezometric mapping.

The advantages and limitations of the device and method are discussed, as well as perspectives such as the way to homogenise $H$ data sets with various durations of the recovery period or various $T$ and piezometric heads, and the way to compute the storage coefficient of the aquifer. It also
demonstrates the kind of simple but accurate instrument that can be built from local store-bought items when budgetary limitations prohibit the purchases of more sophisticated equipment.

The roll out of this device can help in improving the conceptual model of other artesian basins worldwide. It can also provide useful data to set up a numerical model for water resources management, to support implementation of solutions to guarantee the long-term groundwater resource sustainability.

Supplementary Information The online version contains supplementary material available at https://doi.org/10.1007/s10040-022-02505-5.

Acknowledgements This research was carried out as part of a PhD thesis in the framework of the Rejoso Kita project, which is co-directed by Danone AQUA, the International Centre for Research in Agroforestry (ICRAF), the Social investment of Indonesia (SII) and the CKNet foundation, with the financial support of Danone Indonesia. Scientific and logistic support from Gadjah Mada University is gratefully acknowledged. The authors gratefully acknowledge the partnership and authorizations provided by the Ministry of Research, Technology and Higher Education of Indonesia (RISTEKDIKTI) and the Bromo Tengger Semeru National Park (TNBTS). Dr M.S.N. Carpenter post-edited the English style and grammar in an early version. The executive editor Cliff Voss, the editor J.C. Comte and the two anonymous reviewers are also warmly thanked for their careful reviews which helped to improve the manuscript.

Declarations

Conflict of interest On behalf of all authors, the corresponding author states that there is no conflict of interest.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit http://creativecommons.org/licenses/by/4.0/.

References

Ashjari J (2013) Determination of storage coefficients during pumping and recovery. Groundwater 51:122–127. https://doi.org/10.1111/j. 1745-6584.2012.00917.x
Banton O, Bangoy L (1996) A new method to determine storage coefficient from pumping test recovery data. Groundwater 34:772–777. https://doi.org/10.1111/j.1745-6584.1996.tb02069.x
Banton O, Bangoy LM (1997) Hydrogeologie. Multiscience environnementale des eaux souterraines [Hydrogeology. Environmental multiscience of groundwater]. Presses de l’Université du Québec/AUPELF
Bourdet D, Ayoub JA, Pirard YM (1989) Use of pressure derivative in well test interpretation. SPE Form Eval 4:293–302. https://doi. org/10.2118/12777-pa
Charlier JB, Lachassagne P, Ladouche B, Cattan P, Moussa R, Voltz M (2011) Structure and hydrogeological functioning of an insular tropical humid andesitic volcanic watershed: A multi-disciplinary experimental approach. J Hydrol 398:155–170. https://doi.org/10. 1016/j.jhydrol.2010.10.006
Chen J, Wilson CR, Famiglietti JS, Scanlon BR (2018) 4.12 - Groundwater storage monitoring from space. In: Liang S (ed) Comprehensive Remote Sensing. Elsevier, Oxford, pp 295–314
Cooper HH, Jacob CE (1946) A generalized graphical method of evaluating formation constants and summarizing well-field history. Trans Am Geophys Union;14
De Marsily G (1986) Quantitative hydrogeology. Groundwater hydrology for engineers. Academic press
Duffield GM, Court H (2007) AQTESOLV for windows version 4.5 user’s guide
Dumont M, Reninger PA, Aunay B, Pryet A, Jougnot D, Join JL, Michon L, Martelet G (2021) Hydrogeophysical characterization in a volcanic context from local to regional scales combining airborne electromagnetism and magnetism. Geophys Res Lett 48:1–11. https://doi.org/10.1029/2020GL092000
Flook S, Fawcett J, Cox R, Pandey S, Schöning G, Khor J, Singh D, Suckow A, Raiber M (2020) A multidisciplinary approach to the hydrological conceptualization of springs in the Surat Basin of the Great Artesian Basin (Australia). Hydrogeol J 28:219–236. https://doi.org/10.1007/s10040-019-02099-5
Forkasiewicz J (1972) Interprétation des données de pompages d’essai pour l’évaluation des paramètres aquifères. Aide-Mémoire [Inter- pretation of pumping tests data for the determination of aquifer parameters. Aide-mémoire]
Freeze RA, Cherry JA (1979) Groundwater. Prentice-Hall, Inc., Englewood Cliffs
Glover RE (1987) Transient groundwater hydraulics. Water Resource Publications, LLC, Colorado
Habermehl MA (2020) Review: The evolving understanding of the Great Artesian Basin (Australia), from discovery to current hydro-geological interpretations. Hydrogeol J 28:13–36. https://doi.org/ 10.1007/s10040-019-02036-6
Hantush MS (1959) Nonsteady flow to flowing wells in leaky aquifers. J Geophys Res 64:1043–1052. https://doi.org/10.1029/jf064i008p 01043
Hunt CD (1996) Geohydrology of the Island of Oahu, Hawaii
Jacob CE (1940) On the flow of water in an elastic artesian aquifer. EOS Trans Am Geophys Union 21:574–586. https://doi.org/10.1029/TR021i002p000574
Jacob CE (1947) Radial flow in a leaky artesian aquifer. EOS Trans Am Geophys Union 28:481–484. https://doi.org/10.1029/TR028 i003p00481
Jacob CE, Lohman SW (1952) Nonsteady Flow to a Well Of Constant Drawdown. Am Geophys Union 33:10
Jiang XW, Wan L, Wang XS, Wang D, Wang H, Wang JZ, Zhang H, Zhang ZY, Zhao KY (2018) A multi-method study of regional groundwater circulation in the Ordos Plateau, NW China. Hydrogeol J 26:1657–1668. https://doi.org/10.1007/s10040-018-1731-4
Jiang XW, Cherry J, Wan L (2020) Flowing wells: Terminology, history and role in the evolution of groundwater science. Hydrolog Earth Syst Sci 24:6001–6019. https://doi.org/10.5194/hess-24-6001-2020
Kasenda A, Komara AM, Sutisna S (2000) The indonesian gravity field and the geoid model. In: Rummel R, Drewes H, Bosch W, Hornik H (eds) Towards an Integrated Global Geodetic Observing System (IGGOS). Springer, Berlin Heidelberg, pp 245–247
