THERMOMAGNETIC PROCESSING OF ALUMINUM ALLOYS DURING HEAT TREATMENT

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Abstract

Processing materials under magnetic fields is an under-explored technique to improve structure and mechanical properties in metals and alloys. Magnetic fields can alter phase stability, modify diffusion characteristics, and alter material flow substantially. In castings, magnetic fields can be used during melting of the alloy, during solidification, or during postprocessing operations such as heat treatment to achieve structural changes. This work investigates the effectiveness of thermomagnetic processing during heat treatment of Al alloys containing in the Al–Cu, Al–Si–Cu, and Al–Mg–Ce systems. We demonstrate an improvement in mechanical properties and a reduction in required heat treatment times for all alloys.

Keywords: aluminum alloys, heat treatment, magnetic field processing, hot isostatic pressing

Introduction

Work in ferrous materials has demonstrated that high magnetic field processing (HMFP) can induce meaningful changes in kinetics, phase equilibria, and solubility limits in the solid state. These processing routes can result in modified microstructures that, for example, retain alloying elements in solution. This potentially negates the need for a solution heat treatments and/or increase maximum solid solubility limits, improving the strength of the alloy. Though the strongest thermodynamic effects are found in materials with in ferro- or ferrimagnetic phases below their Curie point, nonmagnetic materials such as Al alloys can also be modified substantially by HMFP.

The Al–Cu-based 2xx alloy series has excellent mechanical properties at both room and elevated temperature, but in the as-cast state significant amounts of Cu segregation require a solution treatment. A long (8–12 h), high-temperature (510–530 °C) solution treatment is required to dissolve the Al–Cu intermetallics. After quenching to a supersaturated solid solution, a low-temperature (160 °C) aging treatment is used to form fine strengthening precipitates. If HMFP can retain more of the Cu in the as-cast dendrites, the energy-intensive solution heat treatment could be reduced or potentially eliminated.

3xx series alloys are currently used for the production of automotive cylinder heads produced by Eck Industries. Existing alloys like 319, which contain 6% Si and 3.5% Cu, are capable of only moderate room temperature and elevated temperature strength. There is high potential to reach strength targets in 3xx series alloys that contain both high levels of Si (up to 9%) and Cu (up to 5%). Conventional
treatment of this type of alloy is especially difficult as the Cu content requires long solution treatment times, which can cause coarsening of the Si particles. The accelerated kinetics of magnetic processing may allow large amounts of Cu into solution in times short enough to prevent coarsening of the Si particles.

HMFP exploration into Al alloys can reveal the threshold magnetic field strengths required to shorten processing times while giving equivalent or better mechanical properties. In this manuscript, HMFP of both a 2xx series Al–Cu (A206 and 242) and a 3xx series Al–Si–Cu (355) alloys is discussed. Additionally, the effect of magnetic field processing on Al–8Ce–10Mg alloy, developed in an Eck/Oak Ridge National Laboratory collaboration, was explored. Al–Ce–X 

Experimental Procedure

To evaluate the new HMFP processing method, Al alloy tensile test bars of series 2xx and 3xx of standard chemistries, which were obtained in the as-cast and T4 (solution treated only) conditions, underwent thermomagnetic processing and were compared to the T7 condition (solution treatment plus aging). Additionally, cast Al–Ce alloy samples underwent thermomagnetic processing. Thermomagnetic processing was conducted in 5-in. diameter, vertical warm-bore 9-T superconducting magnet system with a 9-in. long uniform DC magnetic field zone, produced by American Magnetics, Inc., and operated at Oak Ridge National Laboratory in the Advanced Processing Laboratory. That system is shown in Figure 1. Inductive heating of a graphite susceptor approximately 2 in.

Table 1. Summary of Processing Conditions for Various Alloys in This Study

| Alloy ID | Processing conditions |
|---------|-----------------------|
| A206 T4 Standard | 10 h at 530 °C (985 °F), NF |
| A206 T7 Standard | 10 h at 530 °C (985 °F), NF; 200 °C, 4 h, NF |
| A206-T4 | 510 °C, 2 h, 9 T, WQ |
| A206-T7 | 530 °C, 2 h, 9 T, WQ; 200 °C, 2 h, 9 T, FC |
| 242 | 516 °C, 2 h, 9 T, WQ; 205 °C, 1 h, 9 T, FC |
| 355 | 527 °C, 2 h, 9 T, WQ; 154 °C, 1 h, 9 T, FC |
| 8Ce10Mg | 500 °C, 2 h, 2, 5, or 9 T, WQ; 155 °C, 1 or 4 h, 2, 5, or 9 T, FC |

WQ water quench, NF no field, FC furnace cool

Figure 1. ORNL’s 5-in. diameter, vertical warm-bore 9-T superconducting magnet system used for the Al thermomagnetic processing experiments.
emission scanning electron microscope (FEG-SEM) in the backscattered electron (BSE) imaging mode. Processed ASTM B108 samples were then tested for ultimate tensile strength (UTS), yield strength (YS) and % elongation using a United STM-100KN tensile testing machine with a crosshead speed of 0.5 in./min. Conventional mechanical test methods and results for all alloys are shown in Table 2. Included in these data are reference data for conventional heat treatment processing, as well as data gathered on the Al–8Ce–10Mg alloy through the Critical Material Institute (CMI) program. The CMI data are for a conventional T6 temper heat treatment and for a sample that received a hot isostatic pressing (HIP) step that is generally used on materials to reduce porosity and increase density.

Results and Discussion

2xx Alloys

Mechanical properties for all alloys and test conditions are summarized in Table 2 and displayed in Figure 2. Both conventionally heat-treated and thermomagnetically processed bars were produced from the same lot of material and cast into a permanent mold using a standard ASTM B108 test bar mold. All the bars in the T4 condition were tested after 7 days at room temperature. Test bars produced to the T7 temper were held for a minimum of 24 h between solution and age. The bars for both T4 and T7 were from the same production lot of castings. For A206 samples supplied in the as-cast condition, effective solutionization occurred within 2 h under the 9 T magnetic field, 80% faster than the standard 10-h cycle time. This was verified through the mechanical properties data (Table 2, Figure 2 left), which show that UTS above 55 ksi (379 MPa) and YS above 47 ksi (324 MPa) can be achieved after significantly reduced solution processing times when a 9-T magnetic field is applied. This improvement persisted with aging in the magnetic field, as A206-T7 processed in the magnetic field was stronger than the standard alloy aged for twice the time and the 5X longer solution treatment.

Alloy 242 was thermomagnetically processed via a solution (516 °C for 2 h) and aging (205 °C for 1 h) treatment in a 9-T field. Both conventionally heat-treated and thermomagnetically processed bars were produced in a green sand mold using a standard ASTM B26 test bar mold from the same lot of material. In Figure 3, optical micrographs display the untreated (left) and thermomagnetically processed (right) microstructures. The most notable effect is in the dissolution of the Cu-rich particles (eutectic phase) which previously decorated the grains in the as-cast condition. Normally, long (8–12 h), high-temperature (530 °C) solution treatment is required to dissolve the Cu, which is then captured in a supersaturated solid solution during quenching, followed by a 4-h aging or precipitation treatment at 200 °C. HMFP of this alloy accelerates that dissolution process and yields more solute in solid solution to form finer and more copious strengthening precipitates that would increase strength over non-HMFP processed samples. Compared to conventionally heat-treated A242-T77 the yield strength of the HMFP samples is 48% higher, while elongation remains above 1%. The combination of higher strength and equal ductility in a cast product suggests that a fine precipitate likely formed during aging due to the more homogeneous redistribution of solute atoms in the matrix during the solution treatment in the field.

3xx Alloy

Alloy 355 in the T6 condition was also thermomagnetically processed via a solution (527 °C for 2 h) and aging (154 °C for 1 h) treatment in a 9-T field. Both conventionally heat-treated and thermomagnetically processed bars were produced in permanent mold using a standard ASTM B108 test bar mold from the same lot of material. The mechanical properties for conventionally heat-treated bars were 31.6 ksi (208 MPa) YS, 43.4 ksi (327 MPa) UTS, and 4% elongation, so the HMFP technology achieved equivalent UTS and YS at 25% of the solution time for both the solution and aging treatments (Table 2).

Table 2. Mechanical Property Results for All Samples Evaluated

| Alloy Field | UTS (ksi) | YS (ksi) | %El |
|-------------|-----------|----------|------|
| As-cast A206 NF | 39.5 | 27.5 | 5 |
| A206 T4 Standard NF | 58.3 | 37.7 | 12.6 |
| A206 T7 Standard NF | 54.8 | 45.8 | 4.6 |
| A206-T4 9 T | 55.9 | 47.8 | 3.5 |
| A206-T7 9 T | 58.2 | 51.1 | 3.0 |
| 242 9 T | 62.8 | 50.0 | 5.5 |
| 242-T77 Standard NF | 35.0 | 26.1 | 1.8 |
| 355 9 T | 41.2 | 28.8 | 3.28 |
| 355-T6 Standard NF | 41.6 | 29.1 | 2.3 |
| 5 T | 37.4 | 30.5 | 2.47 |
| 5 T | 37.5 | 30.5 | 1.48 |
| 8Ce10Mg-1 h age 9 T | 36.5 | 30.5 | 1.15 |
| 9 T | 37.4 | 30.5 | 1.5 |
| 8Ce10Mg—4 h age 9 T | 38.1 | 30.6 | 1.31 |
| 8Ce10Mg-T6* 0 | 32.0 | 24.5 | 2 |
| CMI Project Typical 8Ce10Mg HIP (*) | 38.0 | 30.8 | 1.5 |

UTS ultimate tensile strength, YS yield strength, El elongation
In Figure 4, optical micrographs display the as-cast (left), conventionally heat-treated (middle), and thermomagnetically processed (right) microstructures. The phase fraction of grain boundary phases in the conventionally processed and HMFP conditions is statistically identical at 0.06 area fraction, as measured in ImageJ software. This is due to the lack of solubility of Si in the Al matrix. The primary grain boundary phase (dark contrast) is a Si-rich phase, and another phase (gray contrast), also found at the grain boundaries, was included in the phase fraction measurement and did not change in proportion in either condition. Upon conventional heat treatment, the Si-rich phase (darker contrast) underwent significant spheroidization and some coarsening compared with the as-cast microstructure. Spheroidization during heat treatment was less pronounced in the HMFP specimen, and less coarsening was observed both owed to the significantly shorter time held at the solutionizing temperature. To determine the difference between these samples, the particles were analyzed with ImageJ software. Figure 5 shows density plots of the particle circularity (1 being a perfect circle, 0 being a line) versus the reduced particle diameter (the diameter of a
circle having the same area of the particle) of the darker phase for the conventionally (left) and thermomagnetically (right) heat-treated conditions. It should be noted that this particular analysis was only valid for particles above 1 μm due to the resolution of the micrographs used. These data show particles with the distribution trending to smaller particles for the HMFP microstructure, supporting the qualitative observation of particle coarsening in the conventional no-field case. Morphologically, the microstructure of the HMFP specimen appears to be somewhere between that of the as-cast and the conventionally treated sample. For the no-field heat-treated condition, the circularity is much greater over the particle distribution and the highest particle density spans from ~2 to 4 μm, while for the HMFP specimen, the circularity is highest for particles of 2.5 μm and below, and the number density is more diffused over both circularity and reduced diameter. The highest number density for HMFP trends to the smaller reduced particle diameter. These data indicate that HMFP has the added effect of limiting spheroidization and coarsening while also effectively solutionizing. HMFP has been shown to limiting kinetic effects, such as nucleation and growth, in other materials, but a more rigorous microstructural study is necessary to elucidate those effects in Al alloys.

Al–Ce Alloy

A parametric study involving different high magnetic field strength levels (2, 5, and 9 T) was conducted on the Al–8Ce–10Mg alloy. This was done to determine the lowest magnetic field strength necessary to achieve the performance enhancements observed at the 9-T level. The data in Table 2 indicate that the 2-T level provides an industrially beneficial impact almost comparable to the 5-T level that exhibited the highest strength and ductility improvements in this study. From a commercial implementation/scalability perspective, the lowest magnetic field strength to achieve a cost-effective performance enhancement translates to the lowest cost superconducting magnet system required for the heat-treating process. The improvement observed at the 2-T level suggests that the majority of the property enhancement occurs approaching a threshold value of field strength that contributes most to the dissolution of solute during the solution heat treatment cycle,
accelerates the solution heat-treating and aging heat treatment processes, and achieves higher strengths after final aging in a field.

Since comparable results were observed at all 3 field strength levels, the microstructural evaluation of the 2-T sample will be discussed in this paper and will be compared with an as-cast sample as well as with a sample that received a HIP treatment (0 T, 100 MPa, 432 °C, 3, or 21 h). This particular Al–8Ce–1Mg sample was thermomagnetically processed via a solution (500 °C for 2 h) and aging (155 °C for 1 h) treatment in a 2-T field. In Figure 6, optical (top) and SEM BSE (bottom) micrographs show the effect of magnetic processing (right) compared to the HIP (middle) and as-cast (left) conditions. The HIP and magnetic field treatments result in similarly enhanced tensile properties (Table 2), and the effects on microstructure are not evident at these magnifications. Both the HIP (bottom middle in Figure 6) and the magnetically processed sample (bottom right in Figure 6) appear similar to the as-cast microstructure (bottom-left in Figure 6). Optical micrographs in Figure 7 show that there is some evidence of grain boundary pinning of Al grains in the samples processed in the magnetic field. Further investigation is necessary to understand the microstructure at higher magnification. As is the case for tempering age-hardening Al alloys, the mechanisms for the enhanced mechanical properties in the magnetically processed samples likely arise from microstructural features at a finer (tens of nanometers) scale, not observable with optical microscopy or SEM. The literature in the past decade suggests that a low-frequency magnetic field and magnetic fields in general, from a grain boundary engineering perspective, can decrease grain boundary segregation, produce more homogeneous distribution of hardening solute in the matrix phase, and result in more copious precipitation potentially facilitating the property enhancements observed in this investigation.

A noteworthy microstructural observation in the HIP and 2-T conditions was the effect of heat treatment on a detrimental Fe-rich phase that is present due to the small Fe concentration in the Al–8Ce–10Mg alloy. Figure 8 shows the morphology of this phase in the various conditions. The phase has a needle-like morphology that formed upon solidification in the cast structure. In the HIP condition at 432 °C, this phase began to agglomerate with the adjacent needles after 3 h and fully agglomerated and spheroidized after 21 h, while after thermomagnetic processing at 500 °C for 2 h, this phase remained needle-like, similar to the cast structure. Because HMFP is being investigated for both energy savings during the heat-treating process by dramatically reducing processing time and demonstrating enhanced tensile properties, processing times on the order of 21 h have not been evaluated.

Throughout this discussion of Al–8Ce–10Mg and other alloys, accelerated dissolution of solutionizable elements during the thermomagnetic processing treatments has been suggested as a mechanism for improved aging response, resulting in finer and more copious strengthening precipitates. This concept is supported by looking at the predicted phases present in this alloy as a function of temperature as shown in the CALPHAD-based plots depicted in Figure 9. Calculations have been made using the Thermo-Calc software and a user-defined thermodynamic database. The
assessments of the binary subsystems have been taken from Al–Ce, Al–Mg, and Ce–Mg, while ternary Al–Ce–Mg interactions have been reported in the literature. At the solution heat-treating temperatures (500 °C) used in this study, the alloy is almost at its predicted incipient melting temperature (501.13 °C) and is anticipated to be three-phase, Al, Al11Ce3, and τ (Al13Ce3Mg6) intermetallics. The left plot in Figure 9 does show that between ambient temperature and the solutionizing temperature, an additional Al140Mg89 compound exists and that the phase fractions undergo large modifications. The overall phase fraction of precipitates evolves from 37.04% at room temperature to 11.36% at 500 °C. More specifically, the phase fraction of precipitates involving Mg (solutionizable element) varies from 29.44% (room temperature) to 4.91% (500 °C). This is an equilibrium prediction and does not reflect the kinetics required during a heat treatment cycle to achieve that microstructure once a given room temperature microstructure has developed upon solidification and cooling of the casting. The right plot in Figure 9 highlights

Figure 7. Optical micrographs of thermomagnetically processed alloy Al–8Ce–10Mg showing pinning (arrows along faint grain boundaries) of some Al/Al grain boundaries

Figure 8. SEM BSE micrographs of alloy Al–8Ce–10Mg showing the effect of processing on the morphology of a Fe-rich phase
the difference between an equilibrium solidification path (similar to Figure 9 left) and a Scheil solidification path (deictive of casting solidification). As observed, the Al$_{140}$Mg$_{89}$ compound can even form at the end of the Scheil solidification compared to the solid-phase precipitation observed at equilibrium (Figure 9 left) and requires thermal treatment to be dissolved. It is those phases (Al$_{140}$Mg$_{89}$ and $\tau$) that need to dissolve to get all, or at least a significant amount, of the solute in solid solution to achieve the maximum strengthening response during the heat treatment cycle. The normally very lengthy solution heat-treating times for Al alloys reflect the significant time to get some dissolution, and therefore, the thermomagnetic processing appears to accelerate the kinetics during solution heat treating as manifested by increased strength without loss of ductility after heat treatment.

In conclusion, the results of this study on multiple different alloy systems clearly demonstrate that the HMFP technology achieves enhanced room temperature mechanical property performance at shorter processing times compared with conventional heat-treating practices. Of significance from a commercial implementation perspective, magnetic fields on the order of 2 T appear to exhibit most of the beneficial effects that field strengths up to 9 T produce, for the Al–8Ce–10Mg alloy. This suggests the possibility that the effect of lower field strength on enhanced performance may carry over to other age-hardening Al alloy systems.

### Technology Commercialization Viability

Since positive results in both heat-treating process energy efficiency and casting performance enhancement have been shown for the different alloy systems using thermomagnetic processing, the viability for potential commercial system designs was evaluated. Initially, performance enhancement was observed using a 9-T magnetic field during heat treatment; thus, a large-bore superconducting magnet system with that high field capability would be necessary. As seen in the concept drawing in Figure 10, a cryogen-free (conduction-cooled) 8-T superconducting high magnetic field system is viable with a 16-in. diameter (406 mm) warm bore that would be able to handle both a heating insert and large components.

The work presented here has demonstrated that magnetic field strengths of only 2 T are necessary to achieve a meaningful benefit. Superconducting system design becomes tremendously easier and significantly less expensive at low field strengths such as 2 T compared with 8 T or 9 T. Therefore, the 2-T, 24-in. diameter warm-bore re-condensing cryocooler superconducting magnet design from American Magnetics, Inc., shown in Figure 11 is industrially viable for some applications. That design concept readily allows for increasing the length of the uniform field zone to accommodate samples with industrial-scale dimensions in all directions. Although shown with a horizontal bore, the system could easily be built with a vertical bore to allow rapid dropping of the sample into a quench medium if required or accommodating both a heating and quenching insert in the magnet bore itself. A system shown in Figure 11 would cost nominally $700 K to $800 K. One important aspect of superconducting magnet systems is that they are typically set to persistent mode in operation, a state where the superconducting loop does not require electricity input to continue operation at field. This mode can be set to any field strength from zero
Figure 10. Concept drawing provided by Cryogenic Limited for an 8-T, cryogen-free (conduction-cooled) 16-in. (406 mm) diameter warm-bore superconducting magnet system

Figure 11. Concept drawing provided by AMI, Inc., for a 2-T, decondensing cryocooler-based, 24-in. (610 mm) diameter warm-bore superconducting magnet system
up to their maximum magnetic field design value, so procuring a system capable of higher magnetic field strengths can be used to cover a range of field magnitude needed in a production environment. It should be noted that implementation of TMP into production based solely on energy efficiency may be only marginally beneficial, but the potential for performance improvements otherwise unachievable in combination with efficiency can make the technology compelling in high value applications.

Impacts

Magnetic processing of Al castings could create significant savings in the manufacturing of Al castings, especially through heat treatment energy savings of up to 80% based on reductions in heat treatment times. Additionally, this technology will contribute to transportation fuel savings by enabling lighter weight vehicles with enhanced performance. The results clearly document the enhanced performance and energy savings potential of thermomagnetically processing cast (or wrought) Al alloys during either just the solution heat treatment cycle or both the solution heat-treating and aging process.

Conclusions

Thermomagnetic processing during solution heat treating and aging of cast Al alloys (206, 242, 355, and Al–8Ce–10Mg) resulted in yield strength (YS) improvement ranging from 10 to 48% and ultimate tensile strength (UTS) improvement of 16–37% over reported conventional values. In addition, all HMFP solution heat-treating and aging times employed in this study were significantly shorter than the conventionally required times. This indicates this technology could achieve significant energy savings when implemented in a production heat-treating environment. Microstructural analyses suggest that the high magnetic fields enable faster dissolution of solute during the solution heat-treating cycle, resulting in finer and more copious strengthening precipitates after the aging cycle. This would explain the increase in YS and UTS without loss of ductility via HMFP. This effect is coupled with limited coarsening and spheroidization, resulting in finer overall microstructure that contributes to the enhanced mechanical properties. Large-bore superconducting magnet systems that could handle production scale parts can be obtained in the marketplace, and as such, commercial implementation of HMFP, especially at the 2-T magnetic field level, can be realized if a return-on-investment calculation supported a path forward for a specific business sector. The results of this study on multiple different Al alloy systems clearly demonstrate that the HMFP technology achieves excellent, enhanced room temperature mechanical property performance at significantly shorter processing times compared with conventional heat-treating practices. Of significance from a commercial implementation perspective, magnetic fields on the order of 2 T appear to have the same beneficial effect as field strengths up to 5 and 9 T for the Al–8Ce–10Mg alloy which suggests this 2-T magnetic field strength may improve mechanical properties of age-hardening Al alloy systems for both cast and wrought product.

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