Localization of Light in Photonics Lattices for All-Optical Representation of Binaries

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In this paper we present a novel conceptual method for all optical representation of binary numbers that could be used for all-optical binary logic components in optical digital computing, as well as for other applications. The new concept is based on effect of localization of light in specially designed binary photonics lattices whose central parts resemble the represented binaries, and the localizations occur due to breaking periodicities of the lattices. The proposed structures can be made with integrated photonics on-chip that are highly programmable and controllable. Most significantly, the working principle of the novel method doesn’t require nonlinear interaction between light and material, which is the most serious obstacle in the conventional method that uses optical transistors whose mechanism relies mainly on optical nonlinearity. We will discuss some technical challenges in developing the components.

Keywords: localization of light, all optical representation of binaries, photonics lattices, arrays of waveguides, optical digital computing

INTRODUCTION

Moore's Law predicts that the number of transistors on certain computer chips will double every 18 months, leading to a predicament in the modern era: traditional transistors are no longer able to keep up with current processing needs. Excessive heat slows down processor speeds due to their physical size limits, and metallic wires restrict the rate of signal transmission. Consequentially, doubling has already begun to falter due to the heat that is unavoidably generated from increasing the amounts of silicon circuitry compressed into small, finite spaces. Other fundamental challenges loom a few years away. Microprocessors currently have circuit features that are around 14 nm; by the early 2020s, they may reach 2-3 nm. At this small scale, electron behavior will be governed by quantum uncertainties that will make transistors hopelessly unreliable [1]. In light of these challenges, it is necessary to explore faster, more efficient technologies than classical electrical computing (EC) for future computing demands.

Optical computing (OC) possesses myriad advantages over current electrical computing (EC). Light does not have the same time response limitations of electronics, does not require insulators, and can even send hundreds or even thousands of photon signal streams simultaneously using different frequencies. Furthermore, optics allows for low-loss transmission and provides a large bandwidth; its multiplexing capability is well-suited for communicating several channels in parallel without interference. Photonics devices are compact, lightweight, inexpensive to manufacture, and better at storing information than magnetic materials. By replacing electrons and wires with photons and photonics structures, researchers have hoped to build a new generation of computers that work 100 million times faster than today's machines. Conservatively, an optical computer could perform more than $10^{17}$ bits operations per second—a huge difference compared to the gigabits ($10^9$) or
terahertz (10^{15}) per second rates which electronics are either current limited to or hoping to achieve [2–5]. Thus, OC represents a massive improvement over the computing capabilities presently available.

In addition, OC may be closer to realization than quantum computing (QC) – the only other computing technology known to be superior than current EC. However, quantum computers, including quantum simulators, are still in the relatively early stages of research. Most components of the future quantum computers have not been defined yet, and technologies will need time to develop these components once the prototypes are established. It is also unknown when they might become available and commercialized. More importantly, in principle, quantum computers would increase greatly (exponentially, for some problems) the efficiency of solving problems such as factoring large integers, combinatorial optimization, quantum physics, and quantum chemistry simulations. Many of those problems are classically intractable computing. However, quantum computers by design would be less efficient than classical counterparts in a vast majority of problems in science and technology [6, 7]. Meanwhile, over the past few decades, photonics technologies have achieved breakthroughs crucial for many important components of future optical computers. These include optical memory, optical logic gate, Si-waveguide nano- photonics structures, and more. Therefore, all-optical digital computers promise to perform computing operations at light speed in digital logic, which would revolutionize the field of information and communication with or without the successful developments of QC.

However, despite decades of effort and progress made in related technical fields, the goal of an all-optical computer has remained largely unfulfilled. One of the reasons for this shortcoming is that optics are not suitable for carrying out calculations—at least in binary “0s” and “1s” [3]. It is important to note that some key components of an all-optical digital computer, such as devices that can optically perform the representation of binary and arithmetic operations, have not been successful for computing. Among the most challenging tasks: developing integrated on-chip, all-optical binary representation components, and searching for materials of high optical nonlinearity to provide low energy optical switches that could overcome the processing bottleneck to all-optical-computing. Optical computing is mostly analogue while electronic computing is digital. Digital optical computers were not able to compete with electronic computers due to the lack of appropriate optical components [3, 4]. These components must especially be implementable for practical use in compact devices. On the other hand, photons do not interact with each other in free space whereas electrons interact strongly through their Coulomb repulsion. Therefore, photons (light) can only interact with each other in the presence of electrons in a material, and the strength of optically nonlinear interaction is much weaker than that of electrons. The consequence of that is very undesirable. The processing elements for an optical computer would require more power and larger dimensions than those for a conventional electronic computer using transistors. Optically nonlinear systems tend to be sensitive to imperfections and perturbations, and that would cause instabilities in operations [5, 8, 9]. Developing methods of overcoming these limitations represents the new Frontier of research in optical computing.

In this paper, we will present the results of our recent investigation that could be used to develop all-optical binary representation components for optical computing and other applications. The proposed structures can be made with integrated photonics on-chip that are highly programmable and controllable. Most important, the working principle of the proposed method doesn’t require nonlinear interaction between light and material, thus avoiding the most serious obstacle in the conventional method that uses optical transistors whose mechanism relies mainly on optical nonlinearity [5, 8–12].

Our proposed method of optical representation of binary (ORB) is based on effects of localization of light in binary photonics lattices (BPL) that will be presented in detail in this paper. The BPLs can be made with current technologies such as multilayer fibers, laser-written waveguide arrays, and lithography etching Si-waveguides etc. As will be presented in this report, BPLs are designed with simple construction rules that resemble the binary numbers. The output localized distribution of photons (or powers) from BPLs can be used to represent binary numbers optically. Finally, we will point out some technical challenges in developing these components that can be used in real applications.

Our paper is organized as follows: Introduction. The construction of binary photonics lattices, and their uses for optical representation of binary numbers are presented in Binary Photonics Lattices for Binary Representation. Discussion and finally Conclusion.

**Binary Photonics Lattices for Binary Representation**

It is worth noting that the concept of binary photonics lattices originates from our previous works on quantum walks (QWs) in arrays of waveguides, especially the localization in quasi-periodic Fibonacci arrays of waveguides [13–15], and in our quasiperiodic Fibonacci multicore ring fiber (MCRF) [16]. The results from our previous works, in particular, the very good agreements between experiments and theoretical results on QWs [16], suggest that a photonics lattice composed with different waveguides that break periodicity of the normal lattices can create localizations of light in the system. Localization of light in arrays of waveguides have been investigated both with coherent [16–19] and quantum sources20 [20–23]. We have expanded our investigation to different structures, and among them, we found new structures—the binary photonics lattices (BPLs) that are simple but can be used for ORB that doesn’t require optical nonlinearity—a long sought component for optical digital computing.

**The Concept of Binary Photonics Lattices**

In this subsection we describe how to construct the BPLs and its use for ORB. First, let’s assume generally that we can represent binary numbers by two optical elements (binary), especially by two different single-mode (SM) waveguides A and B (denoted by
blue and orange solid circles in all figures, respectively). Furthermore, light confinement (localization) in waveguide (WG) A is stronger than in WG B, representing “1” and “0”, respectively, of the binary numbers. In our method of ORB, each number \( N \) whose binary representation \( BR_N \) is represented by a special array of waveguides or a binary photonics lattice (BPL) \( BPL_N \). Note that, in this definition of BPL, all WGs are placed in regular distances and evanescently coupled to the nearest-neighboring ones. The main function of \( BPL_N \) is to generate a spatial distribution of photons that resemble the binary representation of the number \( N \), and therefore perform ORB of the number. As will be seen, the \( BPL_N \) is constructed in a way that all digits of zeros “0s” and ones “1s” in \( BR_N \) are replaced and represented by waveguides \( B \) and \( A \) respectively, thus providing a unique but simple mapping from the number \( N \) to the \( BPL_N \).

Second, conventional binary representation (BR) of a decimal number is a series of digits “0” and “1” with the unit digit being the rightmost one, and the higher orders of other digits are counted from the unit digit to the left. For example, \( 1 = 0 \cdot 2^1 + 1 \cdot 2^0 \) so the BR for decimal number 1 can be written as \( BR_1 = 01 \) and for number 2 is \( BR_2 = 10 \cdot 2^1 + 0 \cdot 2^0 \). Accordingly, we can represent these two \( BR_{1,2} \) by mapping them to two binary arrays of waveguides (BAW) such as \( BAW_1 = BA \) (representation for 01) and \( BAW_2 = AB \) (representation for 10). It’s worth mentioning here that mathematically we can add as many zeros “0s” as we want after the farthest left digit of a conventional BR, and those zeros do not have any meaning mathematically. Therefore, new expressions of these BRs can be re-written as \( BR_1 = 0\ldots0\ldots01 \) and \( BR_2 = 0\ldots0\ldots01 \) instead of 01 and 10 to present numbers 1 and 2, respectively. The bolden digits are for emphasizing the digits of the original BRs and are not necessary so that they will not be used in other formulae. This simple mathematics rule is very useful for us in designing BPLs to utilize photon distributions with localizations to perform ORB. Imagine that our \( BAW_1 \) has only two waveguides \( BA \) as described above. The evanescent coupling causes light power transferred back and forth between WGs \( A \) and \( B \) in just a distance of tens of microns. The output of photon distribution from the system is then very sensitive to the tolerance of propagation distance where the measurement is taken. It is shown in our previous works on both theory and experiment of single photon quantum walks in periodic and quasiperiodic photonics lattices, a reasonably large number of WGs are needed so that the distributions of photons are meaningful [13–15], especially for experimental implementations [16]. It is worth noting that the problem of single photon quantum walks is equivalent to the problem of propagation of coherent light in photonics lattices which is the one under consideration in this work [13–19]. This fact dictates us to construct BPLs that compose a reasonably large number of WGs, and at the same time the mapping \( BAW_N \leftrightarrow BR_N \) with \( 1 \leftrightarrow A, 0 \leftrightarrow B \) is always satisfied so that \( BAW_N \) can be used to represent the \( BR_N \) of number \( N \). Clearly, the expressions of BRs with adding “0s” described above helps us to construct photonics lattices with large numbers of WGs \( B\)s added on the left of the last WG in these BAWs. In doing that, we can construct photonics lattices that resemble structures of corresponding BRs that are implementable in experiments. For example, instead of constructing the \( BAW_1 = BA \) and \( BAW_2 = AB \) representing for \( BR_1 = 01 \) and \( BR_2 = 10 \), respectively, we now construct \( BAW_1 = B \cdot \ldots \cdot B \cdot BA \) and \( BAW_2 = B \cdot \ldots \cdot AB \) to represent numbers 1 and 2, respectively. Note that, the added WGs \( B\)’s is depicted by \( B \cdot \ldots \cdot B \cdot \ldots \cdot B \) to distinguish with the ones of the original binary array. The minimum number of waveguides \( N_{min} \) will be discussed in the next subsection.

Third, note that the BAWs that have just been constructed above are not symmetric in relation to the unit digit. As will be seen, the asymmetric structure poses a serious problem for realizing photon distributions that resemble binary numbers. Especially, if the first waveguide on the right -- the one representing unit digit, is chosen as input WG, then the asymmetric-induced disorder will create strong localizations at and around the input waveguide. In such situations, the output distributions of photons from BAWs hardly resemble the corresponding binaries that we are hoping for in the binary representation. To avoid that problem, we will develop a simple construction rule that requires a new concept of generalized binary representations (GBR) as will be presented in the following.

As stated, we want to construct special BPLs that can perform an optically binary representation without the need of optical nonlinearity as in the conventional method using optical transistors. In order to fulfill our goal, we will have to introduce a new concept of binary representation—using GBR instead of the conventional BR above. From now on, each number \( N \) will be represented by a generalized binary representation \( A_N \) in such a way that is symmetrically composed of two conventional binaries presented above. For example, symmetrical \( A_3 = 0\ldots0\ldots01\ldots0\ldots010\ldots0\ldots0 \) and \( A_2 = 0\ldots0\ldots01\ldots0\ldots010\ldots0\ldots0 \) for binaries of numbers 1 and 2, respectively, instead of \( BR_1 = 0\ldots0\ldots010\ldots0\ldots0 \) and \( BR_2 = 0\ldots0\ldots010\ldots0\ldots0 \) above. Again, the “0\ldots0\ldots0” are added “0s” that do not have any meaning in the binary representation. With the newly defined GBRs, we can apply the construction rule described above: the structure of each \( A_N \) can be mapped into a corresponding binary photonics lattice \( BPL_N \) in which these digits of “0s” and ones “1s” in \( A_N \) are mapped into waveguides \( B\) and \( A\)s, respectively. For example, \( BPL_1 = B \cdot \ldots \cdot BAB \cdot \ldots \cdot Band \ BPL_2 = B \cdot \ldots \cdot AB \cdot \ldots \cdot Bare \) now representing the binaries of numbers 1 and 2, respectively. Furthermore, our general definition of \( BPL_N \) includes an assumption that a coherent light beam is launched into the center waveguide of the lattice indicated by the red arrow, and that the minimum number of waveguides \( N_{min} \) will be discussed in the next subsection. As examples, we show in Figure 1 several numbers \( N \) and their GBR \( A_N \) and the corresponding \( BPL_N \) in the order from the left to the right.

Table 1 above shows the mapping from a decimal number \( N \) to its general binary representation (binary from now on for short) \( A_N \) and the representing binary photonics lattice \( BPL_N \). Note again that the general definition of \( BPL_N \) includes an assumption a coherent light beam is launched into the center waveguide of the lattice indicated by the red arrow.

### Optical Representation of Binary by Binary Photonics Lattices

In this subsection, we will present our simulation results that show clearly the new BPLs can be used to perform an optically
binary representation without optical nonlinearity as in the conventional method that uses optical transistors [5, 10–12]. It’s worth noting that our simulations are based on the beam propagation method (BPM) which is one of the most effective methods for simulating light propagation in complicated structures. The method of BPM has been first proposed by Feit and Fleck in the late 1970s [24, 25]. Since then, this method has been developed for vast applications and has been widely used in commercial software. We have developed our own MATLAB programs and successfully applied them to simulate complicated multimode cladding-pumped fiber amplifiers [26], and to design and optimize Yb-doped multicore fiber lasers in coherent Ising machines (CIM) [27, 28]. We have extended the method to simulate single photons QWs in periodic and quasiperiodic photonics lattices [13–15]. Furthermore, using the same approach, we have recently simulated and designed
for fabrication of the first quasiperiodic Fibonacci MCRFs for realizing localized quantum walks (LQWs) [16]. Our simulation results are in very good agreement with experiments of quantum walks (QWs) and LQWs in periodic and quasiperiodic MCRFs, respectively, [16]. We will present the main concept of the simulation method in the Supplement. More details of this method can be found in [23, 24] and our previous publications [13–16, 26–28]. The simulation results of coherent light beam propagation in BPLs are presented in the following paragraphs.

We show in Figure 2 simulation results of light propagations in BPLs $A_1, A_2, A_3,$ and $A_4$ all have 29 SM waveguides. The parameters used in our simulations are as follows. For WG $A$: $\Delta n = 0.0045$, WG $B$: $\Delta n = 0.0035$, where $\Delta n = n_{\text{core}} - n_{\text{clad}}$, $n_{\text{core}}$ and $n_{\text{clad}}$ are refractive indexes of the core and clad, respectively. $n_{\text{clad}} = 1.46$ is a typical value in silica fibers. All waveguides have the same core size of 4 $\mu$m, center-to-center separation $d = 8$ $\mu$m, and signal wavelength $\lambda = 1.55$ $\mu$m. At first glance, photon distributions at the output look very normal, similar to that of single-photon quantum walks with some localizations.

However, a closer look at the centers of these photon distributions in Figure 2 reveals some interesting patterns as shown in Figure 3. Figures 4, 5 below are the results for higher order BPLs $A_4$ to $A_7$, and all have 49 cores for presenting binary numbers from 4 to 7, respectively. Figure 4 shows the distributions of whole BPLs, meanwhile Figure 5 shows central parts of these distributions.

In Figure 6 we compare distribution centers of BPLs $A_7$ (left panel), $A_8$ (center panel) and $A_{10}$ (right panel) with the binaries 7, 8 and 10, respectively. The panels in Figure 6 are arranged from...
the bottom to the top in each panel as follows: the 3D-distribution of the whole lattice, the center of 3D-distribution (where binary number is represented), the center of 2D-distribution, the center of BPL and finally, the binary number.

The results shown in Figures 3–6 are extraordinary in terms of the optical representation of binary: the BPLs can perform an optical representation of binaries without nonlinear interaction between light and material. Significantly, the working principle of the method doesn’t require optical nonlinearity, therefore avoiding one of the most challenging problems in developing optical digital computing, thus offering a feasible solution for long-sought components of optical digital computing. Furthermore, these BPLs structures can be made on-chip, integrated photonics devices that are essential for real application in optical computing.

DISCUSSION

Our simulation results in previous sections show clearly that the localization of light in the photon distributions in binary photonics lattices (BPLs) can be used to represent binary numbers linearly, meaning that no nonlinear interaction between the light and material is required. The centers of photon distribution of BPLs resemble the corresponding binaries so beautifully. As shown in Figure 1 (and Table 1)
the structures of BPLs look quite simple and straightforward to make. However, there are several important points in design and optimization that we would like to point out as follows.

First, it is easy to expect that the higher binary numbers, the higher numbers of cores in the BPLs. Our simulations show that the minimum number of BPL’s cores $N_{\text{min}}$ required for representing binary numbers are: 29 cores for representing binaries up to $2^2 = 4$, 49 cores for binaries up to $2^3 = 8$, and 69 cores for binaries up to $2^4 = 16$, and so on. If that rule of scalability is held, we would need about 1,300 cores to represent all binaries up to $2^{10}$ which is significant for applications. It is important to note that currently ultrafast lasers have been used to

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**FIGURE 6** | Center of distributions of BPLs $A_7$ (left panel), $A_8$ (central panel) and $A_{10}$ (right panel) resemble binaries 7, 8, and 10, respectively. See the text above for more details.

**FIGURE 7** | Light propagation in standard BPL $A_3$ in 5 mm (left panel), and modified BPL $A_3'$ (right panel). In the standard BPL, all cores $A$s have same index contrast $\Delta n_A$, and all cores $B$s have same index contrast $\Delta n_B$. In this example, the standard BPL $A_3$ (left) $\Delta n_A = 0.0045$ and $\Delta n_B = 0.0035$. In the modified BPL $A_3'$, all cores $A$s have same index contrast $\Delta n_A = 0.0045$ except for the center (input) core, which has lightly lower $\Delta n_A = 0.0042$, indicated by light blue color. All core $B$s have same index contrast $\Delta n_B = 0.0035$ as in the standard one. In each panel, lower figures show distributions at two different distances indicated by two red lines. Note that, the distribution in modified BPL is more unformed than that in standard BPL.
write waveguides in a photonics lattice of $49 \times 49 = 2,401$ waveguides [29].

Second, we would like to stress that although the principle of novel binary representation is quite simple, optimization for demonstration and applications would require a lot of effort. For example, Figure 7 above shows the evolution of two BPLs $A_3$ in 5 mm. The BPL $A'_3$ on the left panel is the standard one with its definition in Table 1. In Figure 2, all WG $A$s have the same index contrast $\Delta n_A$, and all WG $B$s have the same index contrast $\Delta n_B$. In examples shown in Figure 7, the standard BPL $A_3$ (left) $\Delta n_A = 0.0045$ and $\Delta n_B = 0.0035$. In the modified BPL $A'_3$, all WG $A$s have the same index contrast $\Delta n_A = 0.0045$ except for the center (input) core, which has a slightly lower $\Delta n_A = 0.0042$, indicated by a light blue color. All WG $B$s have the same index contrast $\Delta n_B = 0.0035$ as in the standard one. In each panel, lower figures show distributions at two different distances indicated by two red lines. Note that the photon distribution in all $A$-cores of the modified BPL is more unformed than that in the standard one. The effect is predictable since the central $A$ is also the input core and the light prefer to propagate in that input $A$ rather than in the other WG $A$s.

Third, it is very important to point out that the binary representation of BPLs can be nearly preserved when the light...
propagates in one section of BPLs, as shown in the section between two red dotted lines in Figure 7. We will call it the binary presentation section–BPS. In real applications, we want to maximize BPS so that the measurements have a high tolerance along the length of the whole structure. Highly overlapping BPSs of all BPLs in applications are also preferable. Those will require a lot of optimization efforts.

Finally, we would like to discuss the effect of imperfection in the representation. We show in Figures 8, 9 the distributions of two BPLs A2 having 29 cores and 49 cores, respectively, with cores positions are 5% disorder displaced around regular places.

It is clear from Figures 8, 9 that the larger the core number, the cleaner the distribution at the center cores where we want to utilize for binary representation. The reason for that is there is an interference between the outside cores and the center ones. The larger the core numbers, the weaker the interference and cleaner the binary representation. Further investigation includes optimization to minimize the distortion with imperfection will be needed. The results in Figures 8, 9 also present challenges in manufacturing of binary lattices with large number of waveguides in which tolerances of only few percentages are acceptable for imperfections in variation of waveguides spacing, refractive indexes, diameters.

At this point, we would like to point out that all parameters used in our simulations are very normal ones in waveguide photonics or glass fibers. For example, the waveguides have the same core size of 4 μm, the center-to-center separation between the nearest cores is 8 μm, and the index difference between the core and cladding of WG B is Δn = 0.0035, and WG A is 0.0045. Therefore, fabrication of this structure doesn’t require very special materials and technologies. BPLs with numbers of cores from 50 to 70 are good enough to demonstrate the concept. However, for real applications, especially for digital optical computing, more than 1,300 cores would be needed.

Finally, we would like to stress that our proposed method using localization of light in special designed photonics lattices are for all optical representation of binaries. These structures that can be used for different applications, including optical computing, in incorporating with other components such as decoders, multipliers and/or logics gates, especially if these components are based on waveguides platform as investigated in Refs. [30–32].

CONCLUSION

In this work we proposed new binary photonics lattices (BPL) to perform optical representation of binary numbers. The BPLs are constructed symmetrically with two binary arrays of evanescently coupled waveguides. A beam of coherent light is launched into the central core and its propagation in the binary lattices can generate localizations of light in central parts that resemble the binaries we want to represent. Here, the light localizations occur due to the breaking periodicities of the lattices of two different SM waveguides, one represents 0, the other represent 1. Our simulations show the localizations in BPL's photon distribution resemble binary structures, and therefore can be used to represent these binaries optically without the requirement of nonlinear interaction between light and material. Our results in this work can be considered as a conceptual method proposed for all optical representation of binaries. The proposed method is simpler to operate and control as compared with the conventional method using optical transistors that relied mainly on optical nonlinearity, which is one of the most challenging problems to be overcome in developing all-optical digital computing. Furthermore, the BPL structures can be made with integrated on-chip, that are highly programmable and controllable. Those are critical features for real applications.

METHODS

In this work our modeling and simulations are based on beam propagation method (BPM), one of the most effective method for simulating light propagation [24, 25]. We have developed our own Matlab code of BPM for simulating the problem of single-photon quantum walks in arrays of waveguides or photonics lattices [13–15], which is the same for coherent light propagation in the lattices [16–21]. Our BPM simulations of single photon QWs or coherent light propagation have been validated experimentally in periodic and quasiperiodic multicore ring fibers (MCRFs) [16].

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

AUTHOR CONTRIBUTIONS

DTN proposed the idea of binary photonics lattices (BPL), performed the design and simulation. DAN and NFB helped develop the methodology and the applications of BPLs. All authors contributed to writing this paper.

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Conflict of Interest: Authors DTN, DAN, and NFB were employed by the company Corning Inc.

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