Abstract

Constrained Local Models (CLMs) are a well-established family of methods for facial landmark detection. However, they have recently fallen out of favor to cascaded regression-based approaches. This is in part due to the inability of existing CLM local detectors to model the very complex individual landmark appearance that is affected by expression, illumination, facial hair, makeup, and accessories. In our work, we present a novel local detector – Convolutional Experts Network (CEN) – that brings together the advantages of neural architectures and mixtures of experts in an end-to-end framework. We further propose a Convolutional Experts Constrained Local Model (CE-CLM) algorithm that uses CEN as a local detector. We demonstrate that our proposed CE-CLM algorithm outperforms competitive state-of-the-art baselines for facial landmark detection by a large margin, especially on challenging profile images.

1. Introduction

Facial landmark detection is an essential initial step for a number of research areas such as facial expression analysis, face 3D modeling, facial attribute analysis, emotion recognition and person identification [10, 17, 23]. It is a well-researched problem with large amounts of annotated data and has seen a surge of interest in the past couple of years.

Until recently, one of the most popular methods for facial landmark detection was the family of Constrained Local Models (CLM) [10, 22]. They model the appearance of each facial landmark individually using local detectors and use a shape model to perform constrained optimization. CLMs contain many benefits and extensions that many other approaches lack: 1) modeling the appearance of each landmark individually makes CLMs robust to occlusion [1, 22]; 2) natural extension to a 3D shape model and multi-view local detectors allow CLMs to deal naturally with pose variations [22, 18] and landmark self-occlusions [3]; 3) the Expectation Maximization-based model leads to smoothness of tracking in videos [22].

Despite these benefits, CLMs have been recently outperformed by various cascaded regression models [28, 35]. We believe that the relative under-performance of CLM based methods was due to the use of local detectors that are not able to model the complex variation of local landmark appearance as shown in Figure 1. A robust and accurate local detector should explicitly model these different appearance prototypes present in the same landmark.
In this paper we introduce a novel local detector called Convolutional Experts Network (CEN) that brings together the advantages of neural architectures and mixtures of experts in an end-to-end framework. CEN is able to learn a mixture of experts that capture different appearance prototypes without the need of explicit attribute labeling. To tackle facial landmark detection we present Convolutional Experts Constrained Local Model (CE-CLM), which is a CLM model that uses CEN as a local detector. Finally, CE-CLM is able to use the same pipeline for detecting landmarks in both frontal and profile through the use of multiple hypothesis testing.

We evaluate both the benefits of our CEN local detector and then CE-CLM facial landmark detection algorithm through an extensive set of experiments on two publicly-available datasets: 300-W [19], and Menpo Challenge [31].

2. Related Work

Facial landmark detection plays a crucial role in a number of research areas and applications such as facial attribute detection [15], facial expression analysis [17], emotion recognition and sentiment analysis [29].

Modern facial landmark detection approaches can be split into two categories: model and regression based. Model-based approaches often model both appearance and shape of facial landmarks explicitly with the latter constraining the search space and providing a form of regularization. Regression-based approaches on the other hand do not require an explicit shape model and landmark detection is directly performed on appearance.

Model-Based approaches find the best parameters of a face model that match the appearance of an image. A popular model-based method is the Constrained Local Model [10, 22] and its various extensions such as Constrained Local Neural Fields [2, 13] and Discriminative Response Map Fitting [1] which use more advanced methods of computing local response maps and inferring the landmark locations.

Another noteworthy model-based approach is the mixture of trees model [37] which uses a tree based deformable parts model to jointly perform face detection, pose estimation and facial landmark detection. A more recently-proposed 3D Dense Face Alignment method [36] updates the parameters of a 3D Morphable Model [5] using a CNN and has shown good performance on facial landmark detection of profile faces.

Regression-based models predict the facial landmark locations directly from appearance. Majority of such approaches follow a cascaded regression framework, where the landmark detection is continually improved by applying a regressor on appearance given the current landmark estimate in explicit shape regression [6]. Cascaded regression approaches include the Stochastic Descent Method (SDM) [28] and Coarse-to-Fine Shape Searching (CFSS) [35] which attempts to avoid a local optima by performing a coarse to fine shape search. Project out Cascaded regression (PO-CR) [27] is another cascaded regression example that updates the shape model parameters rather than predicting landmark locations directly.

Recent work has also used deep learning techniques for landmark detection. Coarse-to-Fine Auto-encoder Networks [32] use visual features extracted by an auto-encoder together with linear regression. Sun et al. [24] proposed a CNN based cascaded regression approach for sparse landmark detection. Similarly, Zhang et al. [34] proposed to use a CNN in multi-task learning framework to improve facial landmark performance by training a network to also learn facial attributes. Finally, Trigeorgis et al. [26] proposed Mnemonic Descent Method which uses a Recurrent Neural Network to perform cascaded regression on CNN based visual features extracted around landmark locations.

3. Convolutional Experts CLM

Convolutional Experts Constrained Local Model (CE-CLM) algorithm consists of two main parts: response map computation using Convolutional Experts Network (CEN) and shape parameter update using a Point Distribution Model. During the first step, individual landmark alignment is estimated independently of the position of other landmarks. During the parameter update, the position of all landmarks is updated jointly penalizing misaligned landmarks and irregular shapes using a point distribution model. We optimize the following objective:

$$\mathbf{p}^* = \arg\min_{\mathbf{p}} \left[ \sum_{i=1}^{n} -D_i(x_i; \mathcal{I}) + \mathcal{R}(\mathbf{p}) \right]$$

above, $\mathbf{p}^*$ is the optimal set of parameters controlling the position of landmarks (see Equation 3) with $\mathbf{p}$ being the current estimate. $D_i$ is the alignment probability of landmark $i$ in location $x_i$ for input facial image $\mathcal{I}$ (section 3.1) computed by CEN. $\mathcal{R}$ is the regularization enforced by Point Distribution Model (Section 3.2).

3.1. Convolutional Experts Network

The first and most important step in CE-CLM algorithm is to compute a response map that helps to accurately localize individual landmarks by evaluating the landmark alignment probability at individual pixel locations. In our model this is done by CEN which takes a $n \times n$ pixel region of interest (ROI) around the current estimate of a landmark position as input and outputs a response map evaluating landmark alignment probability at each pixel location. See Figure 2 for an illustration.

In CEN the ROI is first convolved with a contrast normalizing convolutional layer with shape $500 \times 11 \times 11$ which
This is achieved by using a special neural layer called Mix-

ReLU neurons.

performs Z-score normalization before calculating correla-
tion between input and the kernel. The output response map
is then convolved with a convolutional layer of $200 \times 1 \times 1$
ReLU neurons.

The most important layer of CEN has the ability to model
the final alignment probability through a mixture of experts
that can model different landmark appearance prototypes.
This is achieved by using a special neural layer called Mix-
ture of Expert Layer (ME-layer) which is a convolutional
layer of $100 \times 1 \times 1$ using sigmoid activation outputting
individual experts vote on alignment probability (since sig-
moid can be interpreted as probability). These response
maps from individual experts are then combined using non-
linear combination of neurons in ME-layer using a sigmoid activation.

Figure 2: Overview of our Convolutional Experts Network model. Input image is given and based on the estimate of the
landmark position a Region of Interest with size $n \times n$ is extracted from it. This small region goes through a Contrast
Normalizing layer with kernel shape $500 \times 11 \times 11$ which performs Z-score normalization before correlation
operation that outputs a $500 \times \tilde{n} \times \tilde{n}$ where $\tilde{n} = n - 10$. Afterwards, the response maps are input to a convolutional layer of
$200 \times 1 \times 1$ with ReLU units. Mixture of Expert Layer (ME-layer) learns an ensemble to capture ROI variations and uses
a convolutional layer of $100 \times 1 \times 1$ sigmoid probability decision kernels. The output response map is a non-negative and
non-linear combination of neurons in ME-layer using a sigmoid activation.

In simple terms, CEN is given an image ROI at iteration
$i$ as input and outputs a probabilistic response map evaluating individual landmark alignment. Thus fitting
the landmark $i$ in position $x_i$ follows the equation:

$$
\pi_i^x = p(l_i = 1, \hat{I} = I_{x_i})
$$

where

$$
\pi_i^x = \begin{cases}
1 & \text{if } l_i = 1, \hat{I} = I_{x_i} \\
0 & \text{otherwise}
\end{cases}
$$

In this equation, $\hat{I}$ is an indicator for landmark number $i$ being aligned. $I_{x_i}$ is the image ROI at location $x_i$ for the image $I$. The response maps $\pi_i^x$ (of size $\tilde{n} \times \tilde{n}$) are then used for minimizing Equa-
tion 1. The detailed network training procedure is presented in Section 4.1 including chosen parameters for $n$ at train and
test time. Our experiments show that ME-layer is crucial and
that making CEN model deeper does not change the performance.

### 3.2. Point Distribution Model and optimization

Point Distribution Models [9, 22] are used to both control
the landmark locations and to regularize the shape in
CE-CLM framework. Irregular shapes for final detected
landmarks are penalized using the term $\mathcal{R}(p)$ in the Equa-
tion 1. Landmark locations $x_i = [x_i, y_i]^T$ are parametrized
with $p = [s, t, w, q]^T$ in the following 3D PDM Equation:

$$
x_i = s \cdot R_{2D} \cdot (\bar{x}_i + \Phi_i q) + t
$$

where $\bar{x}_i = [\bar{x}_i, \bar{y}_i, \bar{z}_i]^T$ is the mean value of the $i$th landmark,
$\Phi_i$ a $3 \times m$ principal component matrix, and $q$ an
$m$-dimensional vector of non-rigid shape parameters; $s, R$
and $t$ are the rigid parameters: $s$ is the scale, $R$ is a $3 \times 3$
rotation matrix defined by axis angles $w = [w_x, w_y, w_z]^T$
($R_{2D}$ are the first two rows of this matrix), and $t = [t_x, t_y, t_z]^T$
is the translation.

Equation 1 can be optimized using Non-Uniform Regular-
ized Landmark Mean Shift (NU-RLMS) [2]. Given an
initial CE-CLM parameter estimate $p$, NU-RLMS iteratively
finds an update parameter $\Delta p$ such that $p^* = p_0 + \Delta p$,
approaches the solution of Equation 1 using Tikhonov regu-
larized least squares.

### 4. Experiments

In our experiments we first evaluate the performance of
Convolutional Experts Network and compare the perform-
ance with LNF [2] and SVR [22] local detectors. We
also evaluate the importance of the ME-layer for CEN
performance. Our facial landmark detection experiments
Table 1: Comparison between CEN, LNF [2] and SVR [22] using square correlation $r^2$ (higher is better) and RMSE (lower is better). To evaluate the necessity of the ME-layer we also compare to CEN (no ME-layer), a model with no non-negative constraint on the weights of ME-layer. Performance drop signals the crucial role of ME-layer.

| Detector                  | $r^2$ | RMSE $\times 10^3$ |
|---------------------------|-------|---------------------|
| SVR [22]                  | 21.31 | 66.8                |
| LNF [2]                   | 36.57 | 59.2                |
| CEN                       | 64.22 | 37.9                |
| CEN (no ME-layer)         | 23.81 | 65.11               |

explore the use of our model in facial landmark detection in images in especially challenging *in-the-wild* setting and with large variations in head pose. The CE-CLM and CEN training codes will be publicly available on multicomp.cs.cmu.edu/ceclm/.

4.1. CEN Experiments

In this section we first describe training and inference methodology of the CEN local detector. We then compare the performance of CEN with LNF [2] and SVR [22] patch experts followed by an ablation study of the ME-layer.

**Training Procedure:** for the following experiments CEN was trained on LFPW and Helen training sets as well as Multi-PIE dataset (see Section 4.2.1). During training, we place a Normal distribution centered around the ground truth location of the response map as the label. We use $19 \times 19$ ROI with a random offset from the ground truth location. A total of 6000 such regions (meaning there were $\approx 5 \times 10^5$ alignment samples) were used during training, and we used 2000 for testing. We trained 28 sets of CENs per landmark: at seven orientations $\pm 70^\circ, \pm 45^\circ, \pm 20^\circ, 0$ yaw; and four scales 17, 23, 30, and 60 pixel of interocular distance. To reduce the number of local detectors that needed to be trained we mirrored the local detectors at different yaw angles and used the same expert for left and right side of the face of the frontal view. ME-layer non-negative weights constraint was enforced using weight clipping during training. The optimizer of CEN was Adam ([14]) with small learning rate of $5 \times 10^{-4}$ and trained for 100 epochs with mini-batches of 512 (roughly 800,000 updates per landmark). Training each CEN model takes 6 hours on a GeForce GTX Titan X but once trained inference can be quickly done and parallelized.

**Experiments:** we compare the performance of CEN local detectors over LNF and SVR patch experts. Table 1 shows the average performance for each individual landmark. Since alignment probability inference is a regression task we use squared Pearson correlation ($r^2$) and RMSE between the ground truth on test set and local detector output as a measure of accuracy. The train and test data for all the models are the same. On average CEN local detector performs 75.6% better than LNF and almost 200% better than SVR (calculated over $r^2$), which shows a significant improvement. While this is an average, for certain landmarks, views and scales performance improvement is more than 100% over LNF. This is specifically the case for 17 pixel interocular distance scale since the CEN is able to model the location of landmark based on a bigger appearance of landmark neighborhood in the image (more context present in the image).

We also evaluate the importance of the ME-layer in the CEN model in Table 1 called CEN (no ME-layer). We show that removing the non-negative constraint from the connection weights to final decision layer (essentially removing the model’s capability to learn mixture of experts) and retraining the network drops the performance significantly, almost to the level of SVR. This signals that ME-layer is a crucial and possibly the most important part of CEN model capturing ranges of variation in texture, illumination and appearance in the input support region while removing it removes the model’s capability to deal with these variations.

In Figure 3 we visualize the improvement of CEN over LNF local detectors across different landmarks such as eyebrow region, lips and jaw outline. The ground truth response map is a normal distribution centered around the position of the landmark. The output response map from CEN shows better certainty about the position of the landmark as its response map is more concentrated around the ground truth position compared to LNF.
4.2. CE-CLM Experiments

In this section we first describe the datasets used to train and evaluate our CE-CLM method for facial landmark detection in images. We first describe the datasets used, followed by the baselines employed and the results of the experiments.

4.2.1 Datasets

We evaluate our CE-CLM on two publicly available datasets: one within-dataset evaluation (300-W), one cross-dataset evaluation (tested on Menpo training fold) and one within (tested on Menpo test). We believe that the cross-dataset evaluation provides the strongest evidence for our model performance.

**300-W** [19, 21] is a meta-dataset of four different facial landmark datasets: Annotated Faces in the Wild (AFW) [37], iBUG [20], and LFPW + Helen [4, 16] datasets. We used the full iBUG dataset and the test partitions of LFPW and HELEN. This led to 135, 224, and 330 images for testing respectively. They all contain uncontrolled images of faces in the wild: in indoor-outdoor environments, under varying illuminations, in presence of occlusions, under different poses, and from different quality cameras. We use the LFPW and HELEN test sets together with iBUG for model evaluation (as some baselines use AFW for training).

**Menpo** Benchmark Challenge [30] dataset is a very recent comprehensive multi-pose dataset for landmark detection in images displaying arbitrary poses. The training set consists of 8979 images, of which 2300 are profile images labeled with 39 landmark points; the rest of the images are labeled with 68 landmarks. The test set consists of 7281 images (1946 profile), the labels for these images are not available and results are provided by challenge organizers. We only used the Menpo dataset for training our model for the challenge submission and not when comparing to the other baselines.

4.2.2 Baselines

We compared our approach to a number of established baselines for the facial landmark detection task, including both cascaded regression and local model based approaches. In all cases we use author provided implementations, meaning we compare to the best available version of each baseline and using the same methodology.

- **CFSS** [35] – Coarse to Fine Shape Search is a recent cascaded regression approach. It is the current state-of-the-art approach on the 300-W competition data [19, 7]. The model is trained on Helen and LFPW training sets and AFW.
- **CLNF** is an extension of the Constrained Local Model that uses Continuous Conditional Neural Fields as patch experts [3]. The model was trained on LFPW and Helen training sets and CMU Multi-PIE [11].
- **PO-CR** [27] – is a recent cascaded regression approach that updates the shape model parameters rather than predicting landmark locations directly in a projected-out space. The model was trained on LFPW and Helen training sets.
- **DRMF** – Discriminative Response Map Fitting performs regression on patch expert response maps directly rather than using optimization over the parameter space. We use the implementation provided by the authors [1] that was trained on LFPW [4] and Multi-PIE [11] datasets.
- **3DDFA** – 3D Dense Face Alignment [36] has shown state-of-the-art performance on facial landmark detection in profile images. The method uses the extended 300W-LP dataset [36] of synthesized large-pose face images from 300-W.
- **CFAN** – Coarse-to-Fine Auto-encoder Network [32], uses cascaded regression on auto-encoder visual features that was trained on LFPW, HELEN and AFW.
- **TCDCN** – Tasks-Constrained Deep Convolutional Network [34], is another deep learning approach for facial landmark detection that uses multi-task learning to improve landmark detection performance.
- **SDM** – Supervised Descent Method is a very popular cascaded regression approach. We use implementation from the authors [28] that was trained on the Multi-PIE and LFW [12] datasets.

All of the above baselines were trained to detect either landmarks without face outline (49 or 51), or with face outline (66 or 68). For each comparison we used the biggest set of overlapping landmarks as all the approaches share the same subset of 49 feature points. For evaluating detections on profile images (present in Menpo dataset), we use the subset of shared landmarks in ground truth images and detected ones. Since the annotations of Menpo profile faces differ slightly from the 68 landmark scheme we unify them by removing the two chin landmarks and using linear interpolation to follow the annotated curve to convert the 4 eyebrow landmarks to 5; and 10 face outline landmarks to 9. This still constitutes a fair comparison as none of the approaches
4.2.4 Landmark Detection Results

As common in such work, we use commutative error curves of size normalized error per image to display landmark detection accuracy. We also report the size normalized median per image error. We report the median instead of the mean as the errors are not normally distributed and the mean is very susceptible to outliers. For 300-W dataset we normalize the error by inter-ocular distance (IOD), for Menpo dataset (containing profile faces) where one of the eyes might not be visible we instead use the average of width and height of the face on training set and diagonal size of the face on test set.

Results of landmark detection on the 300-W dataset can be seen in Table 2 and Figure 4. Our approach outperforms all of the baselines in both the 68 and 49 point scenarios (except for PO-CR in the 49 landmark case on the iBUG dataset). The improved accuracy of CE-CLM is especially apparent in the 68 landmark case which includes the face outline. This is a more difficult setup due to the ambiguity of face outline and which a lot of approaches (especially cascade regression based ones) do not tackle.

Our Menpo dataset experiments are two fold: first we perform a cross-dataset experiment were we train the model without any training data from Menpo. We evaluate the model on Menpo train set and compare to a number of state-
of the art approaches. Figure 5 and Table 3 show our model outperforming all of the baselines on this difficult task. The performance improvement is especially large on profile faces, which SDM, CFAN, DRMF, and PO-CR approaches are completely unable to handle. We also outperform the very recent 3DDFA model which was designed for large pose face fitting. As these results are on a cross-dataset evaluation, they demonstrate how well our method generalizes to unseen data and how well it performs on challenging profile faces.

In the second experiment we retrain the CEN network using Menpo train data. We observed that simply using Menpo train data and starting from randomly initialized CEN network weights does not achieve satisfactory results. However using Curriculum Learning paradigm [8], by starting from 300-W and Multi-PIE which are easier datasets and then moving to Menpo training data after 100 epochs, we were able to successfully train the CEN network for another 50 epochs. We believe that diversity in Menpo required a better prior on CEN network parameters to be able to converge properly. After the training we use the CEN trained on Menpo as local detectors for CE-CLM for Menpo test set. Our performance on the withheld Menpo test set is reported in Figure 7. Please note that the error computation is based on a different normalization (face size diagonal). Due to the labels of the Menpo test set being withheld we are not able to provide direct comparisons on this set with other baselines. For example fits see Figure 6.

Figure 7: Results of our facial landmark detection on the withheld Menpo test dataset. Size normalized MAE for frontal is 0.020 and for profile is 0.037.

5. Conclusion

In this paper we introduced Convolutional Experts Constrained Local Model (CE-CLM), a new member of CLM family that uses a novel local detector called Convolutional Experts Network (CEN). Our proposed local detector is able to deal with varying appearance of landmarks by internally learning an ensemble of detectors, thus modeling landmark appearance prototypes. This is achieved through a Mixture of Expert Layer, which consists of decision neurons connected with non-negative weights to the final decision layer. In our experiments we show that this is a crucial part of the CEN, which outperforms previously introduced local detectors of LNF and SVR by a big margin. Due to this better performance CE-CLM is able to perform better than state-of-the-art approaches on facial landmark detection and is both
more accurate (Figure 4) and more robust, specifically in the case of profile faces (Figure 5). Figure 6 shows a visual comparison between CE-CLM, CFSS and CLNF landmark detection methods on a set challenging images. CE-CLM is able to accurately align landmarks even in profile faces.

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