Calculation methods of noise immunity of the receivers under the mutual effect of tracking systems and complex tracking systems

I N Kartsan¹, Yu N Malanina², A O Zhukov³, ⁴, ⁵, R Yu Tsarev⁶ and V V Brezitskaya¹

¹ Reshetnev Siberian State University of Science and Technology, 31, Krasnoyarsky Rabochy Av., Krasnoyarsk, 660037, Russia
² Irkutsk State Transport University, Irkutsk, Russia
³ Institute of Astronomy of the Russian Academy of Sciences, 48, street Pyatnitskaya, Moscow, 119017, Russia
⁴ Sternberg Astronomical Institute, 13, Universitetsky pr., Moscow, 119234, Russia
⁵ Russian Technological University, 78, Vernadskogo Av., Moscow, 119454, Russia
⁶ Siberian Federal University, 82/6 Svobodny pr., 660041 Krasnoyarsk, Russia

E-mail: kartsan2003@mail.ru

Abstract. The article discusses the methods for improving the reliability and validity of the GLONASS signal. These methods reveal the principles of improving the signal reliability and validity by reducing the noise level from the received signal. The main attention is paid to the calculation of the noise immunity of the receivers under the mutual effect of tracking systems and complex tracking systems. The article deals with the noise immunity of coherent and non-coherent receivers, the noise immunity of the complex tracking systems.

1. Introduction
Currently, the issues related to the use of GLONASS and GPS navigation systems are widely studied [1-5]. The issues related to hardware and software are widely considered [6-12]. It should be noted that most researchers often emphasize two main systems GLONASS and GPS [13-17]. This article analyses the reduction of the noise influence on the navigation signal. In the receivers of satellite radionavigation signals (SRNS) the tracking systems are interconnected. This, in particular, determines the dependence of noise dispersions of equivalent observations on one of the parameters being monitored, on error estimation of another parameter being monitored by another tracking system. Such an interconnection of the tracking systems affects their noise immunity, therefore, the noise immunity of SRNS receivers is analyzed taking into account the mutual effect of various subsystems. In particular, the article analyzes the noise immunity of incoherent and coherent receivers. The method of calculation of noise immunity for the complex tracking systems is also shown.

2. Non-Coherent Receiver Immunity
The non-coherent receiver has two tracking systems: the delay and the frequency of the signal.
The noise variance of the equivalent observations, reduced to the signal delay, depends on the equivalent value of signal-to-noise $\tilde{q}_{e/n_0} = q_{e/n_0} \sin \left( \frac{\omega_c T}{2} \right)$, but the noise variance of the equivalent observations, reduced to the Doppler frequency, depends on the tracking errors for delay and Doppler frequency, $\tilde{q}_{e/n_0}^2 = q_{e/n_0} \rho^2(\varepsilon_r)$, where $\varepsilon_r$ and $\varepsilon_\omega$ are the errors resp. From the above expressions it can be seen that accounting of tracking errors leads to reduction in the equivalent signal-to-noise ratio, and, consequently, to a reduction in the noise immunity of the signal frequency tracking scheme and signal delay tracking scheme.

When calculating the receiver noise immunity, taking into account the mutual influence of the tracking systems, we will assume $\varepsilon_{r(\omega)} = \sqrt{D_{r(\omega)}}$, where $D_{r(\omega)}$ is the variance of the filtering error of the corresponding parameter determined from the dispersion equations of the corresponding tracking system.

Figure 1 shows the dependence of the signal frequency tracking suppression index taking into account the influence of the signal delay tracking error on its characteristics.

![Figure 1. Suppression index of signal frequency tracking.](image)

Figure 2 shows the dependences of the noise immunity index of the signal delay tracking on the effect of signal frequency tracking.

![Figure 2. Suppression index of signal delay tracking.](image)

From the comparison of the dependencies shown in Figures 1 and 2, it follows that the noise immunity of the non-coherent receiver is determined by the noise immunity of the signal frequency
tracking and is 33...41 dB for dynamic consumers (\(\sigma_u \geq 4g\)) and 41...45 dB for poorly dynamic consumers (\(\sigma_u \leq 0.5g\)).

3. Coherent Receiver Immunity

The coherent receiver monitors the delay and phase of the signal. Similar to the previous section, it can be shown that the signal phase tracking system has little effect on the noise immunity of the signal delay tracking system. Therefore, we consider only the effect of signal delay tracking on the noise immunity of the signal phase tracking scheme.

The effect of tracking error on the delay leads to a change in the equivalent signal-to-noise ratio in accordance with the formula \(\tilde{\epsilon}_{\tau} = q_{\epsilon/\nu_0} \rho^2(\epsilon_{\tau})\). Figure 3 shows the dependences of the suppression index of signal frequency tracking under the effect of signal delay tracking. The noise immunity of the coherent receiver is determined by the noise immunity of the signal phase tracking and is 34...36 dB for dynamic consumers (\(\sigma_u \geq 4g\)) and 33 dB...40 dB for poorly dynamic consumers (\(\sigma_u \leq 0.5g\)).

![Figure 3. Suppression index of independent signal phase tracking](image)

(on Y-axis is index \(K_n\), on X-axis is index \(\sigma_u\)).

The noise immunity of the coherent receiver is 4...5 dB lower than the noise immunity of the non-coherent receiver.

4. Receiver Immunity of the complex tracking system

In the complex tracking systems, the smoothing filter processes signals from the outputs of two or more discriminators. The above method of noise immunity calculation can be used in this case. We illustrate this by the example of a complex tracking system for delay and Doppler frequency shift of an non-coherent receiver.

The linearized tracking system is described by the equations

\[
\tilde{\tau}_k = \tilde{\tau}_k + K_{1,k} (\tilde{y}_{r,k} - \tilde{\tau}_k) + K_{2,k} (\tilde{y}_{v,k} - \tilde{v}_{k-1}),
\]

\[
\tilde{\tau}_k = \tilde{\tau}_{k-1} + T \tilde{v}_{r,k-1},
\]

\[
\tilde{v}_{r,k} = \tilde{v}_{r,k-1} + K_{3,k} (\tilde{y}_{r,k} - \tilde{\tau}_k) + K_{4,k} (\tilde{y}_{v,k} - \tilde{v}_{k-1}),
\]

the gains of this system are described by the ratios
\[ K_{1,k} = D_{11,k} / D_{\eta_k}, \quad K_{2,k} = D_{12,k} / D_{\eta_k}, \quad K_{3,k} = D_{12,k} / D_{\eta_k}, \quad K_{4,k} = D_{22,k} / D_{\eta_k}, \]

where \( D_{\eta_k} = D_{\eta_k} / (2\pi f_0)^2 \), the variance of filtering errors in the steady state are described by the formulas

\[ D_{11,ycm} = \sqrt{S_{\tilde{\eta}_k} S_{\tilde{\eta}_k} (1 + 2\sqrt{\rho}) / (1 + \sqrt{\rho})}, \quad D_{12,ycm} = S_{\tilde{\eta}_k} (1 + \sqrt{\rho}), \]

\[ D_{22,ycm} = \sqrt{S_{\tilde{\eta}_k} S_{\tilde{\eta}_k} (1 + 2\sqrt{\rho}) / (1 + \sqrt{\rho})}, \]

where \( S_{\tilde{\eta}_k} = S_{\tilde{\eta}_k} / (2\pi f_0)^2 \) and \( \rho = S_{\tilde{\eta}_k} / (S_{\tilde{\eta}_k} S_{\tilde{\eta}_k}) \) means dimensionless parameter.

For real signal levels and dynamics of consumer movement, the parameter \( \rho \ll 1 \) and variance of filtering errors can be presented in a simplified form

\[ D_{11,ycm} \approx \sqrt{S_{\tilde{\eta}_k} S_{\tilde{\eta}_k}}, \quad D_{12,ycm} = S_{\tilde{\eta}_k}, \quad D_{22,ycm} = \sqrt{S_{\tilde{\eta}_k} S_{\tilde{\eta}_k}}. \]

In this case, the optimal filtering equations \( \tilde{v}_{r,k} = \tilde{v}_{r,k-1} + \tilde{K}_{4,k} \tilde{y}_{r,k} - \tilde{v}_{k-1} \) are also simplified, and the estimate of signal delay rate (Doppler frequency shift) is generated only by the signals from output of the frequency discriminator.

Therefore, the noise immunity of the tracking ring at the signal frequency does not depend on the characteristics of the delay tracking ring. The dependence of the suppression index for the signal frequency tracking in the considered case are shown in Figure 4.

Comparison of these dependencies with similar data shown in Figure 1 demonstrates that noise immunity has decreased slightly. This is explained by the fact that in this case the description of the Doppler frequency shift by the first order equation is accepted, and accordingly in the complex tracking system the frequency tracking ring also has the first order (smoothing filter of the first order). In this regard, it should be noted that the increase of the noise immunity of the tracking system with an increase in the order of the smoothing filter is also observed in other types of tracking systems (phase and signal delay).

**Figure 4.** Suppression index of frequency tracking ring

(on Y-axis is index \( K_n \), on Y-axis is index \( \sigma \)).

Figure 5 shows the suppression index graphs for the signal delay tracking ring, which indicate that the noise immunity of the delay tracking ring is virtually independent of the intensity of the consumer's
maneuvering. This is quite consistent with the fact that by $\rho << 1$ the dispersion of the signal delay filtering error does not depend on the intensity of the consumer acceleration. The noise immunity also varies slightly when the signal-to-noise ratio changes.

![Figure 5. Suppression index of frequency tracking ring](image)

(on Y-axis is index $K_n$, on Y-axis is index $\sigma^2 a$).

As above, the noise immunity of the receiver with the complex tracking system is determined by the noise immunity of the signal frequency tracking ring.

The dependences of the suppression index for various types of tracking systems given in this article can be used to calculate the critical signal-to-internal noise ratio $q_{c_{\text{in}d\theta}}$, at which the receiver still operates with the specified consumer characteristics. For the numerical calculation of this parameter, the ratio should be used

$$q_{c_{\text{in}d\theta}} = \frac{\Delta f_c}{K_1} \quad \text{or} \quad \tilde{q}_{c_{\text{in}d\theta}} = 10 \log \left( \frac{\Delta f_c}{E_i} \right).$$

So, for the standard accuracy signal and for the value of the suppression coefficient (receiver with integrated tracking system, the input power is dBHz

So, for a signal of standard accuracy $\Delta f_c \approx 1$ MHz and for the value of suppression index $\tilde{K}_1 = 38$ dB (the receiver with the complex tracking system, the input signal power is obtained in $\tilde{P}_c = -170$ dBHz) we have get $\tilde{q}_{c_{\text{in}d\theta}} = 22$ dBHz.

5. Conclusion
The article deals with the issues of signal noise reduction.

It should be noted that when analyzing the noise immunity of a non-coherent receiver, we have two systems: the signal delay tracking system and the signal frequency tracking system. In this case, the accounting of tracking errors leads to a decrease in the equivalent signal-to-noise ratio, and, consequently, to a reduction in the noise immunity of the tracking scheme.

The coherent receiver monitors the delay and phase of the signal. In the same way as the non-coherent receiver, after analyzing we can say that the signal phase tracking system has little effect on the noise immunity of the signal delay tracking system.

In complex tracking systems, the smoothing filter processes signals from the outputs of two or more discriminators. In addition, the noise immunity of the receiver with the complex tracking system is determined by the noise immunity of the signal frequency tracking ring.
Acknowledgements
This work was supported by the Ministry of Education and Science of the Russian Federation (State assignment to higher education institutions and research organizations in the field of scientific activity; agreement No. 2.7711.2017/8.9).

References
[1] Kudymov V I, Brezitskaya V V, Zelenkov P V, Kartsan I N and Malanina Yu N 2018 IOP Conf. Ser.: Mater. Sci. Eng. 450(1) 052009
[2] Chebotarev V E, Brezitskaya V V, Kovaliev I V, Kartsan I N, Malanina Yu N and Shemyakov A O 2018 IOP Conf. Ser.: Mater. Sci. Eng. 450(1) 022029
[3] Kartsan I N, Zelenkov P V, Tyapkin V N, Dmitriev D D and Goncharov A E 2015 IOP Conf. Ser.: Mater. Sci. Eng. 94(1) 012010
[4] Yuronen Yu P, Yuronen E A, Ivanov V V, Kovaliev I V and Zelenkov P V 2015 IOP Conf. Ser.: Mater. Sci. Eng. 450(1) 022029
[5] Kartsan I N, Tyapkin V N, Dmitriev D D, Goncharov A E, Zelenkov P V and Kovaliev I V 2016 IOP Conf. Ser.: Mater. Sci. Eng. 155(1) 012017
[6] Kartsan I N, Tyapkin V N, Dmitriev D D, Goncharov A E, Zelenkov P V and Kovaliev I V 2016 IOP Conf. Ser.: Mater. Sci. Eng. 155(1) 012018
[7] Kartsan I N, V Tyapkin N, Dmitriev D D, Goncharov A E, Zelenkov P V and Kovaliev I V 2016 IOP Conf. Ser.: Mater. Sci. Eng. 155(1) 012019
[8] Kartsan I N, Zelenkov P V, Tyapkin V N, Dmitriev D D and Goncharov A E 2016 IOP Conf. Ser.: Mater. Sci. Eng. 122(1) 012010
[9] Tyapkin V N, Fateev Yu L, Dmitriev D D, Kartsan I N, Zelenkov P V, Goncharov A E and Nasyrov I R 2016 IOP Conf. Ser.: Mater. Sci. Eng. 122(1) 012035
[10] Kartsan I N, Fateev Y L, Tyapkin V N, Dmitriev D D, Goncharov A E, Zelenkov P V and Kovaliev I V 2016 IOP Conf. Ser.: Mater. Sci. Eng. 155(1) 012020
[11] 2017 The project Pseudolite Instruments Available from http://www.ni.com
[12] Astrium F S E 2012 Theoretical approach for the optimization of pseudolite pulsing scheme and the implementation of participative receivers Satellite Navigation Technologies and European Workshop on GNSS Signals and Signal Processing, (NAVITEC) 2012 6th ESA Workshop pp 1-8
[13] Tyapkin V N, Garin E N, Dmitriev D D and Ratushniak V N 2016 Study characteristics of coordinate measurement in the ground system of navigation based pseudo satellites Telecommunications and Radio Engineering 11 132-6
[14] Gladyshev A B, Dmitriev D D, Veysov E A and Tyapkin V N 2017 A hardware-software complex for modelling and research of near navigation based on pseudolites J. Phys.: Conf. Ser. 803
[15] Dmitriev D D, Gladishev A B, Tyapkin V N and Fateev Yu L 2016 Hardware-software complex for studying the characteristics of GNSS receiver International Siberian Conference on Control and Communications SIBCON 2016
[16] Gladyshev A, Dmitriev D, Kremez N and Garin E 2016 Simulator of signals based on modular instrumentation to test GNSS receivers, which measure the angular position of the object Intern. Scientific. Conf. "Reshetnevreading (Krasnoyarsk) pp 260-2
[17] Dmitriev D D, Ratushniak V N, Gladyshev A B and Kremez N S 2016 Hardware-software complex simulation processes positioning and measurement of the spatial orientation of the spacecraft in geostationary orbit Telecommunications and Radio Engineering 11 141-4