Electronic structures and enhanced optical properties of blue phosphorene/transition metal dichalcogenides van der Waals heterostructures

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As a fast emerging topic, van der Waals (vdW) heterostructures have been proposed to modify two-dimensional layered materials with desired properties, thus greatly extending the applications of these materials. In this work, the stacking characteristics, electronic structures, band edge alignments, charge density distributions and optical properties of blue phosphorene/transition metal dichalcogenides (BlueP/TMDs) vdW heterostructures were systematically studied based on vdW corrected density functional theory. Interestingly, the valence band maximum and conduction band minimum are located in different parts of BlueP/MoSe2, BlueP/WS2, and BlueP/WSe2 heterostructures. The MoSe2, WS2 or WSe2 layer can be used as the electron donor and the BlueP layer can be used as the electron acceptor. We further found that the optical properties under visible-light irradiation of BlueP/TMDs vdW heterostructures are significantly improved. In particular, the predicted upper limit energy conversion efficiencies of BlueP/MoS2 and BlueP/MoSe2 heterostructures reach as large as 1.16% and 0.98%, respectively, suggesting their potential applications in efficient thin-film solar cells and optoelectronic devices.

Since the experimental discovery of graphene1, the two-dimensional (2D) materials have taken global interests owing to their distinguished physical and chemical properties, adaptability, as well as multi-functionality. Generally, 2D materials show markedly different electronic, optical, and catalytic properties compared to their bulk counterparts due to the quantum confinement effect. In recent years, pure elements 2D materials, such as black phosphorene2–4, silicene5, germanene6–7 and stanene8, as well as binary systems of monolayer hexagonal boron nitride9,10 (hBN), single-layer semiconducting transition metal dichalcogenides11,12 (TMDs), MXenes13,14 and so on are widely studied. Nowadays, the combinations of various 2D materials together raise the possibility of the designing of van der Waals (vdW) heterostructures15. These heterostructures possess significantly improved electronic and optical properties compared to 2D materials themselves due to the mutual interaction between the layers16. Till now, a great deal of efforts has been made to obtain many vdW heterostructures as the key materials for next generation energy and environment related devices. For instance, the graphene-based heterostructure shows improved electronic properties compared to the individual graphene17,18. Among them, the black phosphorene/graphene heterostructure presents high capacity in sodium-ion batteries19.

It is worth noting that the TMDs-based vdW heterostructures have obtained increasing interest due to their extraordinary electronic and optical properties. The electronic conductivity and photochemical performances are greatly enhanced in graphene/MoS2 heterojunctions20,21. The black phosphorene/MoS2 p–n diode as a photodetector shows a photodetection responsivity of 418 mA/W, which is nearly 100 times higher than the reported...
black phosphorus phototransistor\textsuperscript{22}. For WX\textsubscript{2}/MoX\textsubscript{2} (X = S, Se, Te) junction, spontaneous charge separation occurs when excitons diffuse to the junction, which is needed for photovoltaics\textsuperscript{9}. The MoS\textsubscript{2}/hBN heterostructure could serve as a prototypical example for band structure engineering of 2D crystals with atomic layer precision\textsuperscript{23}. The MoS\textsubscript{2}/AIN and MoS\textsubscript{2}/GaN vdW heterostructures exhibit high-efficiency photocatalytic activity for water splitting\textsuperscript{24,25}.

To date, the puckered structure of black phosphorene can be converted to a more symmetric buckled structure by certain dislocation of constituent phosphorus atoms, deemed as blue phosphorene (BlueP)\textsuperscript{26}. And the single-layer BlueP is nearly as thermally stable as monolayer black phosphorene\textsuperscript{26,27}. Due to the fact that both BlueP and TMDs monolayers share the same hexagonal crystal structure\textsuperscript{26,28}, it is possible to construct appropriate BlueP/TMDs vdW heterostructures. It is worth noting that the lattice parameter of BlueP matches with many TMDs (for example, MoS\textsubscript{2}, MoSe\textsubscript{2}, WS\textsubscript{2} and WSe\textsubscript{2}) perfectly. In this regard, investigating the electronic and optical properties of BlueP/TMDs vdW heterostructures is anticipated and of great interest and importance. In this work, the structural, electronic and optical properties of BlueP/TMDs (TMDs = MoS\textsubscript{2}, MoSe\textsubscript{2}, WS\textsubscript{2} and WSe\textsubscript{2}) vdW heterostructures were systematically studied using first-principles calculations based on the density functional theory (DFT). The band-decomposed charge density and optical spectra were evaluated to understand the nature of the bonding mechanism, charge transfer as well as the visible-light absorption ability of the BlueP/TMDs vdW heterostructures.

**Results**

The lattice constants of monolayer BlueP, MoS\textsubscript{2}, MoSe\textsubscript{2}, WS\textsubscript{2} and WSe\textsubscript{2} were fully optimized and the values are 3.268, 3.164, 3.295, 3.165, 3.295 Å, respectively, which are in consistent with the reported data listed in Supplementary Table S1\textsuperscript{24,26,27,30–32}. The interlayer lattice mismatches between BlueP and MoS\textsubscript{2}, MoSe\textsubscript{2}, WS\textsubscript{2} and WSe\textsubscript{2} were evaluated to be +3.18%, −0.82%, +3.15% and −0.82%, respectively, which are all in an acceptable range and accessible in experimental synthesis. For each BlueP/TMDs heterostructure, six most possible stacking configurations with six special rotation angles between the adjacent layers were explored, as shown in Supplementary Fig. S1. The rotation angles of BlueP monolayer with respect to TMDs are 0°, 60°, 120°, 180°, 240° and 300°, respectively. All systems are geometrically optimized for getting stable atomic configuration. The difference of total energy between the six different stacking configurations compared with the most stable one, the interlayer distance between monolayer BlueP and TMDs, as well as the M − X (M = Mo, W and X = S, Se) and P−P bond lengths for the BlueP/TMDs heterostructures are listed in Supplementary Table S2. According to the total energy data for each configuration and Eq. (1), configuration (a) is the most stable structure for all the heterostructures. Interestingly, with the rotation of the BlueP monolayer with respect to TMDs, we can find in Supplementary Table S2 that the total energy and interlayer distance of the heterostructures increase and maximize when the rotation angle reaches 180° (configuration (d)) for all the four heterostructures.

In order to investigate the thermodynamic stability of the BlueP/TMDs heterostructures, the formation energies according to Eq. (2) were calculated to be −165.6, −210.5, −161.2 and −209.7 meV/unit-cell for BlueP/MoS\textsubscript{2}, BlueP/MoSe\textsubscript{2}, BlueP/WS\textsubscript{2} and BlueP/WSe\textsubscript{2} heterostructures, respectively. The negative formation energies indicate thermodynamic stability and the possibility to obtain the BlueP/TMDs heterostructures experimentally. On the other hand, the binding energies\textsuperscript{31} between BlueP and TMDs monolayers in BlueP/MoS\textsubscript{2}, BlueP/MoSe\textsubscript{2}, BlueP/WS\textsubscript{2} and BlueP/WSe\textsubscript{2} heterostructures are 16.11, 19.46, 15.69 and 19.38 meV/Å, respectively, which are in consistent with the typical vdW binding energy of around 20 meV/Å\textsuperscript{3} obtained by the advanced DFT calculations\textsuperscript{34}. Therefore, the above BlueP/TMDs heterostructures belong to vdW heterostructures. Considering the fact that each P atoms occupies ~5 Å\textsuperscript{2} space of the vdW interface, the vdW binding between the BlueP and TMDs layers are slightly stronger than that of bilayer black phosphorus from the Quantum Monte Carlo study\textsuperscript{4}.

The calculated angle of BlueP monolayer with respect to TMDs are 0°, 60°, 120°, 180°, 240° and 300°, respectively. For getting self-consistent results, we evaluated the accurate band gap values by Supplementary Table S2 that the total energy and interlayer distance of the heterostructures increase and maximize when the rotation angle reaches 180° (configuration (d)) for all the four heterostructures.

To understand the band offset nature of BlueP/TMDs vdW heterostructures, the band edge alignments, the negative formation energies and theoretically reported values, as summarized in Supplementary Table S1. Therefore, the above BlueP/TMDs heterostructures belong to vdW heterostructures. Considering the fact that each P atoms occupies ~5 Å\textsuperscript{2} space of the vdW interface, the vdW binding between the BlueP and TMDs layers are slightly stronger than that of bilayer black phosphorus from the Quantum Monte Carlo study\textsuperscript{4}.

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To understand the band offset nature of BlueP/TMDs vdW heterostructures, the band edge alignments, the total density of states (DOS) and orbital-resolved partial DOS were studied systematically, as illustrated in Fig. 1 and Supplementary Fig. S3. For getting self-consistent results, we evaluated the accurate band gap values by the hybrid-DFT method with 8% Hartree-Fock exchange energy based on the optB86b-vdW approach for all the monolayers and heterostructures, which exactly reproduces the experimental gap of monolayer MoS\textsubscript{2}. The calculated band gap using hybrid functional calculations for BlueP, MoS\textsubscript{2}, MoSe\textsubscript{2}, WS\textsubscript{2} and WSe\textsubscript{2} monolayers are 2.39, 1.90, 1.65, 2.08 and 1.75 eV, respectively. These results are in good agreement with previous experimental data\textsuperscript{11,30,38} and theoretically reported values, as summarized in Supplementary Table S1\textsuperscript{24,32,35–37}. As seen in Fig. 1, the band edge positions of these vdW heterostructures are located between CBM of BlueP and VBM of TMDs except for BlueP/MoS\textsubscript{2} heterostructure. The band gaps of BlueP/MoS\textsubscript{2}, BlueP/MoSe\textsubscript{2}, BlueP/WS\textsubscript{2} and BlueP/WSe\textsubscript{2} heterostructures using hybrid functional are 1.43, 1.28, 1.45 and 1.13 eV, respectively. As summarized in Supplementary Table S3, the band gaps of heterostructures are smaller than the corresponding TMDs monolayers, indicating that the forming of vdW heterostructure reduces the band gap values. From Supplementary Fig. S3, it is clearly seen that the VBM is mainly occupied by the Mo-4d or W-5d electrons in these four vdW
heterostructures. In contrast, the CBM primarily originates from the $3p$ electrons for BlueP/MoS$_2$, BlueP/WS$_2$, and BlueP/WSe$_2$ heterostructures; while for BlueP/MoSe$_2$ heterostructure, the CBM is mainly contributed by $4d$ electrons of Mo atoms. It is consistent to the band edge alignments analysis. As a result, the Fermi level ($E_F$) of BlueP/TMDs vdW heterostructures shifts and appears between the CBM of BlueP and VBM of TMDs.

The work function of a material is a critical parameter commonly used as an intrinsic reference for band alignment. It is seen from Fig. 1 that the predicted work functions of BlueP/MoS$_2$ heterostructures are smaller than pristine BlueP and MoS$_2$ monolayers; whereas, the work functions of BlueP/MoSe$_2$, BlueP/WS$_2$, and BlueP/WSe$_2$ heterostructures are smaller significantly than pristine BlueP but larger slightly than TMDs. Owing to the energy of the Se-$4p$ orbital higher than S-$3p$ orbital, the work functions of BlueP/MoSe$_2$ ($M$ = Mo, W) heterostructures are smaller than BlueP/MoS$_2$ heterostructures.

From the calculated band structures in Fig. 2, it is seen that all the BlueP/TMDs vdW heterostructures are identified as indirect band gap semiconductors owing to the indirect band gap nature of BlueP and the interlayer coupling effect in the heterostructures. The BlueP/MoS$_2$ heterostructures can be divided into two groups. Group I includes the BlueP/MoS$_2$ and BlueP/WS$_2$ heterostructures (showing in Fig. 2(a,c)), where VBM is located at the $\Gamma$ point and CBM is located at the K point. This is due to the fact that the BlueP monolayer shares similar valence band level at the $\Gamma$ point and conduction band level at the K point with single layer MoS$_2$ or WS$_2$. The band interactions coming from the formations of the heterostructures pull up the energy level of the valence band at the $\Gamma$ point and push down the energy level of the conduction band at the K point, which can also explain the variations of the band alignment as shown in Fig. 1(a,c). Group II involves the BlueP/MoSe$_2$ and BlueP/WSe$_2$ heterostructures (showing in Fig. 2(b,d)), where CBM is located between the $\Gamma$ and M points. Although VBM is located at the $\Gamma$ point for the BlueP/MoSe$_2$ heterostructure, and which is located at the K point for the BlueP/WSe$_2$ heterostructure, it is worth noting that the energy level of VBM at the $\Gamma$ and K points are very close in these cases. For these heterostructures, the BlueP monolayer present deeper conduction energy band levels than the MoSe$_2$ or WSe$_2$ single layer. Hence the VBM keeps the main features of the single layer MoSe$_2$ or WSe$_2$, and CBM represents the features of the BlueP monolayer between the $\Gamma$ and M points, which agrees well with the band alignment results in Fig. 1(b,d).

Considering the fact that there is a significant spin-orbit coupling (SOC) effect in TMDs, we have calculated the band structures for all the five 2D monolayer materials and four heterostructures including the effect of SOC (illustrated in Supplementary Figs S4 and S5). It is seen that there is no significant SOC effect on band structure of BlueP. Otherwise, SOC splits off the double-degenerated transition metal (Mo or W) $d$ electron occupied valence band state at the K point for the TMDs monolayers and BlueP/TMDs vdW heterostructures. As a result of the band splitting, the VBM shift to the K point for the BlueP/MoSe$_2$ heterostructure. Apart from this, SOC slightly

Figure 1. Band alignments and work functions of monolayers and heterostructures using hybrid functional, referring to the vacuum level ($E_{\text{vac}}$). The black dashed lines illustrate $E_{\text{vac}}$; the black double-headed arrows and numbers are the calculated work functions $W$, and the green double-headed arrows and numbers are hybrid functional predicted band gap.
influences the predicted band structures without changing the characteristics and shapes of the band eigenvalues, which does not change the main results and conclusions of this work.

The calculated band-decomposed charge density is shown in Fig. 3, which provides us a vividly picture to understand the role of the constituent layers in BlueP/TMDs vdW heterostructures. The decomposed charge density was calculated for the lowest unoccupied molecular orbital (LUMO) and the highest occupied molecular orbital (HOMO). The HOMOs are mainly consists of the Mo-4d or W-5d electrons, while the LUMOs are mainly contributed by the P-3p electrons in BlueP/MoS₂, BlueP/WS₂ and BlueP/WSe₂ heterostructures, except for BlueP/MoS₂ heterostructure (its LUMO is mainly contributed by the Mo-4d electrons), which are in consistent
Eqs/uni00A0(6–9). Since all the vdW heterostructures show very similar tendency of the optical properties, we present the electrons and holes can be effectively separated in the BlueP/MoSe\(_2\) the electron donor and the BlueP layer as the electron acceptor in the corresponding heterostructures. The free conversion. Based on the distribution of charge densities, we found that the electrons are confined in the BlueP when excitons diffuse to the BlueP/MoSe\(_2\) monolayers of BlueP/MoSe\(_2\), BlueP/WS\(_2\) and BlueP/WSe\(_2\) heterostructures. Figure 4 presents the real parts of the dielectric function were examined and compared to the dielectric function of corresponding single-layer BlueP and TMDs. Figure 5 presents the real parts \(\varepsilon_1\) and imaginary parts \(\varepsilon_2\) of dielectric function of the hybrid and single systems. For all the BlueP/TMDs vdW heterostructures, both the real and imaginary parts of the dielectric functions show larger values than the individual single systems (see Fig. 5). There are two distinguished peaks in UV light regions (200–390 nm) and visible light regions (390–770 nm) from the imaginary parts of dielectric functions, indicating enhanced optical properties of all the BlueP/TMDs vdW heterostructures.

**Discussion**

Figure 6 shows the optical refractive index \(n(\lambda)\), extinction coefficient \(\kappa(\lambda)\), reflectivity coefficient \(R(\lambda)\) and absorption coefficient \(\alpha(\lambda)\) of BlueP/TMDs vdW heterostructures from the dielectric functions according to Eqs (6–9). Since all the vdW heterostructures show very similar tendency of the optical properties, we present the BlueP/MoSe\(_2\) heterostructure as an example in detail (see Fig. 6(b)). The refractive index \(n(\lambda)\) of BlueP/MoSe\(_2\) with the analysis of the electronic structures. The results reveal that CBM and VBM are localized in different monolayers of BlueP/MoSe\(_2\), BlueP/WS\(_2\) and BlueP/WSe\(_2\) heterostructures, resulting in different spatial distribution of the lowest energy electron-hole pairs. Therefore, the MoSe\(_2\), WS\(_2\) or WSe\(_2\) layer can be potentially used as the electron donor and the BlueP layer as the electron acceptor in the corresponding heterostructures. The free electrons and holes can be effectively separated in the BlueP/MoSe\(_2\), BlueP/WS\(_2\) and BlueP/WSe\(_2\) heterostructures, indicating the potential applications of these vdW heterostructures for optoelectronics and solar energy conversion. Based on the distribution of charge densities, we found that the electrons are confined in the BlueP layer, while the holes in the TMDs side. Therefore, it is expected that spontaneous charge separation occurs when excitons diffuse to the BlueP/MoSe\(_2\), BlueP/WS\(_2\) and BlueP/WSe\(_2\) heterostructures, which is beneficial for the microscopic understanding of the conduction channels. We have calculated the frontier states to further study the interlayer interactions and hybridizations of the BlueP/MS\(_2\) heterostructures (see Fig. S6), which are beneficial for the optoelectronic and photovoltaic applications. We have confirmed the appearance of the indirect to direct band gap transition in the BlueP/MoSe\(_2\), BlueP/WS\(_2\) and BlueP/WSe\(_2\) heterostructures under \(-0.47, +0.53\) and \(-0.47 V/Å\) external electric fields, respectively (see Fig. 4). Hence, the potential applications of these BlueP/TMDs vdW heterostructures are not restricted by their indirect band gap features.

The calculated plane-averaged electron density differences of BlueP/TMDs vdW heterostructures are shown in Supplementary Fig. S7 to better understand the nature of the bonding mechanism and the charge transfer between the BlueP and TMDs layers, where the magenta regions represent the charge accumulation, and the cyan regions represent depletion in the combined system relative to the two isolated components. As a result of the interlayer coupling effect, there is an obvious space charge accumulation region at the BlueP/TMDs heterointerfaces. In addition, the charge redistribution at the TMDs layer indicates that the formation of vdW heterostructures may affect the M–X bonds (M = Mo, W and X = S, Se).

To understand the effect of quantum confinement on the optical properties of BlueP/TMDs vdW heterostructures, the real \(\varepsilon_1\) and imaginary \(\varepsilon_2\) parts of the dielectric function were examined and compared to the dielectric function of corresponding single-layer BlueP and TMDs. Figure 5 presents the real parts \(\varepsilon_1\) and imaginary parts \(\varepsilon_2\) of dielectric function of the hybrid and single systems. For all the BlueP/TMDs vdW heterostructures, both the real and imaginary parts of the dielectric functions show larger values than the individual single systems (see Fig. 5). There are two distinguished peaks in UV light regions (200–390 nm) and visible light regions (390–770 nm) from the imaginary parts of dielectric functions, indicating enhanced optical properties of all the BlueP/TMDs vdW heterostructures.
below 300 nm is very close to that of BlueP, but is much higher than that of MoSe₂ above 500 nm. It is seen that extinction coefficient $\kappa(\lambda)$ of BlueP/MoSe₂ heterostructure is generally enhanced, especially in UV light ranges.
Moreover, the reflectivity coefficient $R(\lambda)$ of BlueP/MoSe$_2$ heterostructure is increased twice compared with the individual monolayers. More importantly, BlueP/MoSe$_2$ heterostructure shows substantial absorption in both visible light and UV light areas, while BlueP monolayer shows only UV light absorption and MoSe$_2$ monolayer shows absorption mainly in the visible light region. In addition, its absorption region around 300 and 500 nm is clearly enhanced. Generally speaking, it clearly shows that BlueP/TMDs vdW heterostructures are able to harvest the visible light and UV light more efficiently than the individual single systems. The similar phenomenon can be found in the hybrid GeH/graphene nanocomposite. The heterostructure formation can not only improve the charge separation of photo-induced electron-hole pairs but also broaden the light absorption range. Therefore, the BlueP/TMDs vdW heterostructures possess potential applications in efficient solar cells and ultrathin optoelectronic devices.

To go a step further, we introduced the estimation method by Shi et al. according to Eqs (10–13) to calculate the theoretical upper limit conversion efficiency of sunlight for BlueP, TMDs monolayers and BlueP/TMDs vdW heterostructures. The corresponding results are listed in Table 1. It is reported that WSe$_2$ monolayer has a strong optical absorbance and can be used to fabricate solar cells with light-to-electricity conversion efficiencies of $\sim$0.5%.

| System       | BlueP | MoS$_2$ | MoSe$_2$ | WS$_2$ | WSe$_2$ | BlueP/MoS$_2$ | BlueP/MoSe$_2$ | BlueP/WS$_2$ | BlueP/WSe$_2$ |
|--------------|-------|---------|----------|--------|---------|---------------|---------------|-------------|--------------|
| $P_1$        | 0.02  | 0.27    | 0.37     | 0.25   | 0.32    | 1.16          | 0.98          | 0.62        | 0.72         |

Table 1. Upper limit of the energy conversion efficiency $P$ (%) of sunlight to lowest-energy excitons for BlueP, TMDs monolayers and BlueP/TMDs vdW heterostructures.

Conclusion

In summary, we have systematically studied the stacking configurations induced electronic structures, band edge alignments, charge density distributions and optical properties of BlueP/TMDs vdW heterostructures based on vdW corrected density functional theory. The negative formation energies as well as the good lattice match protect the thermodynamic stability of the BlueP/TMDs vdW heterostructures. All the BlueP/TMDs vdW heterostructures exhibit indirect gap characteristics. The VBM and CBM are localized in different parts of the BlueP/MoS$_2$, BlueP/WS$_2$, and BlueP/WSe$_2$ heterostructures. The MoSe$_2$, WS$_2$, or WSe$_2$ layer can be used as the electron donor and the BlueP layer can be used as the electron acceptor in the corresponding heterostructures. The BlueP/TMDs vdW heterostructures exhibit unusually stronger optical absorbance and energy conversion efficiency in the visible range. The results in this work provide a fundamental understanding and guideline for designing high performance optoelectronic and photovoltaic devices.

Methods

Density functional theory calculations. Our calculations were performed based on the density functional theory (DFT) in conjunction with the projector-augmented-wave (PAW) potential as implemented in the Vienna ab initio Simulation Package (VASP) For the exchange-correlation energy, the Perdew-Burke-Ernzerhof (PBE) version of the generalized gradient approximation (GGA) was used. The van der Waals density functional (vdW-DF) of optB86b was considered for all the calculations. The valence electron configurations for P, S, Se, Mo, and W were $3s^23p^3$, $3s^23p^5$, $4s^24p^4$, $4d^55s^2$, and $5d^66s^2$, respectively. A plane wave cutoff energy of 600 eV was used for the plane-wave expansion of the wave function. The first Brillouin zone was sampled with a fine grid of $7 \times 7 \times 1$ for structure optimization and $15 \times 15 \times 1$ for static calculation. A vacuum of 30 Å along the z direction (perpendicular to the BlueP/TMDs vdW heterostructures layers) was constructed to eliminate the interaction with spurious replica images. The atomic positions were fully relaxed until satisfying an energy convergence of $10^{-7}$ eV and force convergence of 0.01 eV/Å. Due to the fact that the PBE functional underestimates the band gaps of semiconductors, the accurate band gap values and optical properties were further calculated by the hybrid functional approach. As seen in Table S1 and Fig. S8, the standard optB86b-vdW functional underestimates the band gap of well-known monolayer MoS$_2$ by $\sim$0.13 eV. Comparing to the standard HSE06 hybrid functional with 25% Hartree-Fock exchange energy, we found that the 8% short range Hartree-Fock exchange energy based on optB86b-vdW can reproduce the experimental band gap of monolayer MoS$_2$ and other TMDs without much deviation of the lattice parameter. Considering the fact that there is no experimental results available for the band gap of monolayer BlueP, we choose monolayer MoS$_2$ as the reference to predict the band gap of
the BlueP/TMDs vdW heterostructures. It is worth noting that the proportion of the short range Hartree-Fock exchange energy influences the absolute values of the predicted band gap only, without changing the variation tendency of the formation of the vdW heterostructures. To further check our results, we have calculated the quasiparticle band gaps of the monolayers and heterostructures using the G$_0$W$_0$ approximation, which are listed in Tables S1 and S3 as well. As seen, our results agrees well with previously scGW results. It is interesting to find in Fig. S8, the G$_0$W$_0$ approximation shows very similar band gap variation pattern to the hybrid functional calculations.

To determine the configuration of the heterostructure stacking, the energy difference $\Delta E$ was written as the following equation:

$$\Delta E = E_i - E_0$$  \hspace{1cm} (1)

where $E_0$ is the total energy of the most stable configuration, and $E_i$ is the total energy of each configuration. To examine the stability of the heterostructures, the formation energy was obtained according to the following equation:

$$E_{\text{form}} = E_{\text{total}}^{\text{BlueP/TMDs}} - E_{\text{total}}^{\text{BlueP}} - E_{\text{total}}^{\text{TMDs}}$$  \hspace{1cm} (2)

where $E_{\text{total}}^{\text{BlueP/TMDs}}$, $E_{\text{total}}^{\text{BlueP}}$ and $E_{\text{total}}^{\text{TMDs}}$ represent the total energies of BlueP/TMDs, BlueP and TMDs in one unit-cell, respectively. In addition, we have added the calculated equation of binding energy to evaluate the strength of the vdW force in BlueP/TMDs vdW heterostructures according to the following equation:

$$E_{\text{binding}} = E_{\text{total}}^{\text{BlueP/TMDs}} - E_{\text{total}}^{\text{BlueP} + \text{TMDs}}$$  \hspace{1cm} (3)

where $E_{\text{total}}^{\text{BlueP} + \text{TMDs}}$ is the sum of the total energy of mutually independent single-layered BlueP and TMDs fixed in the corresponding heterostructure lattice. The work function $W$ was obtained by the following expression:

$$W = E_{\text{vac}} - E_F$$  \hspace{1cm} (4)

where $E_{\text{vac}}$ is the energy of a stationary electron in the vacuum nearby the surface, $E_F$ is the Fermi energy level. In addition, the plane-averaged electron density difference along the perpendicular direction to the interface was calculated according to the following equation:

$$\rho_\text{BlueP/TMDs} = \rho_\text{BlueP} - \rho_\text{TMDs}$$  \hspace{1cm} (5)

where the $\rho_\text{BlueP/TMDs}$, $\rho_\text{BlueP}$ and $\rho_\text{TMDs}$ are the charge density of BlueP/TMDs vdW heterostructures, BlueP and TMDs systems, respectively.

**Optical properties.** Optical properties are described by the photon wavelength dependent dielectric function $\varepsilon(\lambda) = \varepsilon_1(\lambda) + i\varepsilon_2(\lambda)$, which is mainly contributed from the electronic structures. The refractive index $n(\lambda)$ and the extinction coefficient $\kappa(\lambda)$ are determined from $\varepsilon_1$ and $\varepsilon_2$ using

$$n(\lambda) = \sqrt{\frac{\varepsilon_1(\lambda)}{\varepsilon_2(\lambda)}}$$  \hspace{1cm} (6)

and

$$\kappa(\lambda) = \sqrt{\frac{\varepsilon_1(\lambda)}{\varepsilon_2(\lambda)}}$$  \hspace{1cm} (7)

where $\lambda$ is the photon wavelength. The reflectivity and absorption coefficient were calculated by

$$R(\lambda) = \frac{(n - 1)^2 + \kappa^2}{(n + 1)^2 + \kappa^2}$$  \hspace{1cm} (8)

and

$$\alpha(\lambda) = \frac{2\pi\varepsilon_2}{\lambda}$$  \hspace{1cm} (9)

The estimated upper limit to the converted power $P$ is based on the overlap between the solar spectrum and the absorbance:

$$P = \frac{\int_{0}^{\lambda_{\text{max}}} W(\lambda)\alpha(\lambda)C(\lambda)d\lambda}{\int_{0}^{\lambda_{\text{max}}} W(\lambda)d\lambda}$$  \hspace{1cm} (10)

where $\lambda_{\text{max}}$ is the longest wavelength that can be absorbed by ultrathin materials and is determined by the lowest-exciton energy $E_g$ (i.e., the minimum band gap of the material),
\[ \lambda_{\text{max}} = \frac{hc}{E_g} \]  

and \( W(\lambda) \) is the solar spectral irradiance at Air Mass 1.5. \( A(\lambda) \) is the directionally averaged absorbance of BlueP/TMDs monolayers and BlueP/TMDs vdW heterostructures according to \(^{44}\):  

\[ A(\lambda) = 1 - e^{-\alpha(\lambda)d} \]  

where \( \alpha \) is the absorption coefficient, and \( d \) is the thickness of the simulation cell perpendicular to the layers. The term \( C(\lambda) \) is the conversion factor to account for the fraction of the photon energy converted to lowest-exciton energy (i.e., the thermalization loss).

\[ C(\lambda) = \frac{\lambda^2}{hc} \]  

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Author Contributions

Q.P. performed the DFT calculations. B.S., B.W. and Z.S. designed the research. Q.P., Z.W. and B.S. analyzed the data. All authors wrote the paper.

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