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ACOUSTIC SCALE FROM THE ANGULAR POWER SPECTRA OF SDSS-III DR8 PHOTOMETRIC LUMINOUS GALAXIES

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ABSTRACT

We measure the acoustic scale from the angular power spectra of the Sloan Digital Sky Survey III (SDSS-III) Data Release 8 imaging catalog that includes 872, 921 galaxies over ~10,000 deg² between 0.45 < z < 0.65. The extensive spectroscopic training set of the Baryon Oscillation Spectroscopic Survey luminous galaxies allows precise estimates of the true redshift distributions of galaxies in our imaging catalog. Utilizing the redshift distribution information, we build templates and fit to the power spectra of the data, which are measured in our companion paper, to derive the location of Baryon acoustic oscillations (BAOs) while marginalizing over many free parameters to exclude nearly all of the non-BAO signal. We derive the ratio of the angular diameter distance to the sound horizon scale "DA(z)/r_s = 9.212 ± 0.404" at z = 0.54, and therefore DA(z) = 1411 ± 65 Mpc at z = 0.54; the result is fairly independent of assumptions on the underlying cosmology. Our measurement of angular diameter distance DA(z) is 1.4σ higher than what is expected for the concordance ΛCDM, in accordance to the trend of other spectroscopic BAO measurements for z ≥ 0.35. We report constraints on cosmological parameters from our measurement in combination with the WMAP7 data and the previous spectroscopic BAO measurements of SDSS and WiggleZ. We refer to our companion papers (Ho et al.; de Putter et al.) for investigations on information of the full power spectrum.

Key words: distance scale – cosmological parameters – cosmology: observations – large-scale structure of universe

Online-only material: color figures

1. INTRODUCTION

Baryon acoustic oscillations (BAOs) imprint a distinct feature in the clustering of photons (i.e., cosmic microwave background, CMB), mass, and galaxies. Sound waves that propagated through the hot plasma of photons and baryons in early universe freeze out as photons and baryons decouple and leave a characteristic oscillatory feature in Fourier space and a single distinct peak in the correlation function approximately at the distance the sound waves have traveled before the epoch of recombination. The distance is called the “sound horizon scale” and determines the physical location of the BAO feature in clustering statistics (e.g., Peebles & Yu 1970; Sunyaev &

26 The scale observed in the mass is not exactly the distance traveled when recombination occurs as the momentum of the baryonic material means that the motion continues for a short time after recombination, until an epoch known as the baryon-drag epoch.

24 Hubble fellow.
25 SEPnet: www.sepnet.ac.uk.
Zeldovich 1970; Bond & Efstathiou 1984; Holtzman 1989; Hu & Sugiyama 1996; Hu & White 1996; Eisenstein & Hu 1998). CMB data provide an independent and precise determination of the sound horizon scale. Therefore, comparing this sound horizon scale to the observed location of the BAO from galaxy clustering statistics allows one to constrain the angular diameter distance and Hubble parameters, thereby providing information on the nature of dark energy. This approach is known as the “standard ruler test” (e.g., Hu & White 1996; Eisenstein 2003; Blake & Glazebrook 2003; Linder 2003; Hu & Haiman 2003; Seo & Eisenstein 2003). The BAO technique is considered an especially robust dark energy probe (Albrecht et al. 2006) for various reasons. First, its physical scale is separately measured from CMB data. Second, the nonlinear effects in the matter density field are still mild at the BAO scale (∼150 Mpc) such that the resulting systematic effects are small and can be modeled with low-order perturbation theories (e.g., Meiksin et al. 1999; Seo & Eisenstein 2005; Jeong & Komatsu 2006; Crocce & Scoccimarro 2006; Eisenstein et al. 2007; Nishimichi et al. 2007; Crocce & Scoccimarro 2008; Matsubara 2008; Padmanabhan & White 2009; Seo et al. 2008, 2010; Taruya et al. 2009). Third, the observational/astrophysical effects such as galaxy/halo bias and redshift distortions are likely smooth in wavenumber and do not mimic BAO such that they can be marginalized over (e.g., Seo & Eisenstein 2005; Huff et al. 2007; Sánchez et al. 2008; Padmanabhan & White 2009; Mehta et al. 2011; but see Dalal et al. 2010 and Yoo et al. 2011 for a possibility of an exotic galaxy bias effect).

In recent years, BAO has been detected in the galaxy distribution and used to constrain cosmology (Eisenstein et al. 2005; Cole et al. 2005; Hütsi 2006; Tegmark et al. 2006; Percival et al. 2007b, 2007a; Padmanabhan et al. 2007; Blake et al. 2007; Okumura et al. 2008; Estrada et al. 2009; Sánchez et al. 2009; Martínez et al. 2009; Gaztañaga et al. 2009; Percival et al. 2010; Kazin et al. 2010; Beutler et al. 2011; Crocce et al. 2011; Blake et al. 2011a, 2011b). Most of these studies have used a three-dimensional distribution of galaxies from spectroscopic surveys to constrain an isotropic distance scale $D_V(z)$ ($D_V(z) = [(1 + z)^2 D_A(z)cz/H(z)]^{1/3}$, where $D_A$ is the angular diameter distance and $H$ is the Hubble parameter using spherically averaged clustering statistics, while others have constrained $D_A(z)$ and $H(z)$ separately, using anisotropic clustering information.

Retrieving three-dimensional spatial information requires accurate redshift determination (i.e., spectroscopic surveys), demanding specialized spectrographs and surveys that typically take longer times. Multiband imaging surveys, on the other hand, can more quickly cover a large number of galaxies (low shot noise) and a large area of sky but provide only two-dimensional spatial information, assuming a realistic level of photometric redshift error, and therefore fail to retrieve information on $H(z)$.27 Another disadvantage of using the imaging data to make BAO measurements is an additional damping of the BAO due to projection effects and difficulty in applying BAO reconstruction. Nevertheless, imaging surveys can, in principle, provide larger and deeper surveys (Seo & Eisenstein 2003; Amendola et al. 2005; Blake & Bridle 2005; Dolney et al. 2006; Zhan & Knox 2006) and this prospect has motivated current and future imaging BAO surveys such as the Dark Energy Survey28 (The Dark Energy Survey Collaboration 2005), the Panoramic Survey Telescope and Rapid Response System29 (Kaiser et al. 2002), the Physics of the Accelerating Universe survey30 (PAU, Javalambre-PAU survey; Benítez et al. 2009), the Large Synoptic Survey Telescope31 (Tyson 2002), and Euclid32 (Beaulieu et al. 2010; Laureijs et al. 2011).

A number of previous works have analyzed and reported the cosmological constraints from the galaxy clustering of the imaging surveys (e.g., Tegmark et al. 2002; Blake et al. 2007; Ross et al. 2008; Sawangwit et al. 2011; Thomas et al. 2010, 2011; Crocce et al. 2011; Ross et al. 2011), but there have been only a few published works on the BAO measurement (Padmanabhan et al. 2007; Carrero et al. 2012). Our goal in this paper is to design a robust method for measuring the location of BAO in the angular power spectrum of imaging surveys and apply it to the final imaging data set of the Sloan Digital Sky Survey III (SDSS-III; York et al. 2000).

We use the DR8 imaging catalog of SDSS-III that includes photometric redshifts of luminous galaxies (hereafter “LGs”) between 0.45 < z < 0.65 over ∼10,000 deg2 (Ross et al. 2011); the spectroscopy from the SDSS-III Baryon Oscillation Spectroscopic Survey (BOSS; Eisenstein et al. 2011) is used to create a training sample and therefore to estimate the true redshift distribution of photometric galaxies. The angular power spectra are generated from the data using an optimal quadratic estimator (OQE), as presented in detail in one of our companion papers, Ho et al. (2012). Utilizing the estimated true redshift distribution, we construct a theoretical BAO template for the angular power spectrum, fit to the location of the observed BAO feature in the angular power spectrum, and derive the angular diameter distance to $z = 0.54$ in a manner independent of underlying dark energy models.

The angular clustering of galaxies contains more cosmological information than the scale of BAO. Redshift distortions on very large scales and the overall shape of the power spectrum (e.g., the matter-radiation equality feature) can provide additional information. However, in this paper, we take a very conservative approach and use only the most robust probe, the location of BAO, while excluding most of the non-BAO information. Ho et al. (2012, Paper I) present a more extensive study: it includes information of the full power spectrum and derive cosmological constraints. In parallel, another companion paper, de Putter, et al. (2012), measures the mass bound on the sum of neutrino masses using the same power spectra.

This paper is organized as follows. In Section 2, we briefly summarize the imaging data. In Section 3, we summarize the method used in Paper I to generate angular power spectra. In Section 4, we describe details of the BAO fitting method used in this paper. In Section 5, we test our method and assumptions using mock data. In Section 6, we present an analysis of the DR8 imaging data and report the best-fit angular diameter distance to sound horizon ratio at $z = 0.54$. We show the robustness of our result and show the effect of correcting for the observational systematics. In Section 7, we discuss constraints on various cosmological parameters when our BAO measurement is combined with the WMAP7 data and other BAO measurements. Finally, in Section 8, we summarize the results in this paper.

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27 A fractional redshift error of 0.25% in 1 + z is at least required to recover $H(z)$ (Seo & Eisenstein 2003).
28 www.darkenergysurvey.org
29 www.pan-starrs.ifa.hawaii.edu
30 PAU: www.ice.cat/pau, Javalambre-PAU survey: http://j-pas.org/astro-ph
31 www.lsst.org
32 www.cosmos.esa.int/euclid
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Table 1
The Four Photometric Redshift Bins

| Bins   | $z_{ph}$ Range | $N_{gal}$ | $\sigma_{z_{ph}}$ | $z_{median}$ | $z_{mean}$ |
|--------|----------------|-----------|-------------------|--------------|------------|
| CMASS1 | 0.45–0.50      | 214,971   | 0.043             | 0.474        | 0.475      |
| CMASS2 | 0.50–0.55      | 258,736   | 0.044             | 0.523        | 0.526      |
| CMASS3 | 0.55–0.60      | 248,895   | 0.052             | 0.568        | 0.572      |
| CMASS4 | 0.60–0.65      | 150,319   | 0.063             | 0.617        | 0.621      |
| Total  | 0.45–0.65      | 872,921   | 0.541             | 0.544        | 0.544      |

Notes. $N_{gal}$ is the effective number of galaxies after weighting each object by $p_{\sigma_{z}}$, which is the probability that an object is a galaxy. The value of $\sigma_{z_{ph}}$ is the dispersion in redshift for each photo-$z$ bin.

2. DATA

We use the imaging data of the eighth and final data release (DR8; Aihara et al. 2011) of SDSS-III (York et al. 2000) that is obtained by wide-field CCD photometry in five passbands ($u$, $g$, $r$, $i$, $z$; see Fukugita et al. 1996; Gunn et al. 1998, 2006; Pier et al. 2003, for more technical and data release details). We use the photometric redshift catalog constructed as described in Ross et al. (2011).33 This catalog is selected from DR8 using the same criteria as the SDSS-III BOSS (Eisenstein et al. 2011) targets selected to have approximately constant stellar mass (CMASS; White et al. 2011). Photometric redshifts and probabilities that an object is a galaxy were obtained using a training sample of 112,778 BOSS CMASS spectra (to be released with Data Release 9 in July 2012).34 The final catalog covers 9913 deg$^2$ of sky and consists of 872,921 galaxies between 0.45 < $z$ < 0.65, which is an improvement in the survey area compared to the MegaZ-LRG DR7 catalog (Thomas et al. 2011; 723,556 objects over 7746 deg$^2$ for 0 $<$ $z_{ph}$ $<$ 0.5).

The estimated photometric error, $\sigma_{z_{ph}}$, increases from 0.04 to 0.06 over the redshift range (see Figure 10 of Ross et al. 2011). We define four photometric redshift bins, with widths similar to the photometric error, referred to as CMASS1, CMASS2, CMASS3, and CMASS4. Table 1 and Figure 1 show the distribution of each redshift bin to be less than 0.5% (of the total) and the error on the 68% width to be 0.8%–2% (of the width). The median and mean of the combined galaxy distribution are 0.541 and 0.544, respectively.

3. OPTIMAL QUADRATIC ESTIMATOR OF ANGULAR POWER SPECTRA

The auto and cross angular power spectra of the four redshift bins were generated using the OQE presented in Paper I, to which we refer the readers for more details of the OQE (also see Tegmark 1997; Hamilton 1997; Bond et al. 1998; Seljak 1998; Tegmark et al. 1998, 2002; Padmanabhan et al. 2003, 2007). To summarize, we parameterize the power spectrum with 35 step-function band powers and write the data covariance matrix as

$$C_{ij} = \langle \delta_i \delta_j \rangle = \sum_\beta p_{\beta} C_{\beta i}^{(\beta)} + N_{i} \delta_{i}^{j}, \quad (1)$$

where $\delta_i$ is the galaxy overdensity at the $i$th pixel at a given redshift bin, $p_{\beta}$ is the band power for a wave number bin $\beta$, $C_{\beta i}^{(\beta)}$ is the derivative of $C$ with respect to the band power $p_{\beta}$, and $N_{i}$ is the shot noise contribution to the covariance matrix, while $\delta_{i}^{j}$ is the Kronecker delta function. Assuming $\delta_{i}$ is Gaussian distributed, requiring the estimator to be unbiased and to have a minimum variance, we derive a band power estimator

$$p_{\beta} = F_{\beta \gamma}^{-1} \left[ \frac{1}{2} \delta_{i}^{\gamma} C_{\gamma}^{-1} C_{\gamma}^{(-1)} \delta - b_{\gamma} \right], \quad (2)$$

where $b_{\gamma}$ is the contribution from $N$ (i.e., $1/2tr[C_{\gamma}^{-1}C_{\gamma}^{(-1)}N]$), i.e., the shot noise, and $F$ is the Fisher information matrix:

$$F_{\beta \gamma} = \frac{1}{2} tr[C_{\gamma}^{-1}C_{\beta}^{(-1)}C_{\gamma}^{(-1)}]. \quad (3)$$

The variance of the band power is derived by

$$\text{Cov}[p_{\beta}, p_{\gamma}] = F_{\beta \gamma}^{-1}. \quad (4)$$

The expected value of band power, $\langle p_{\beta} \rangle$, is related to the power spectrum $p(\ell')$ at an integer $\ell'$ by the band window function $W_{\beta \ell'}$ (e.g., Knox 1999):

$$\langle p_{\beta} \rangle = \frac{d(p_{\beta})}{dp(p)} p(\ell') \cdot W_{\beta \ell'} p(\ell'), \quad (5)$$

and

$$W_{\beta \ell'} = F_{\beta \gamma}^{-1} \frac{1}{2} tr[C_{\gamma}^{-1}C_{\beta}^{(-1)}C_{\gamma}^{(-1)}]. \quad (6)$$

where $C^{(-1)}$ is the derivative of $C$ with respect to the power at an integer wavenumber $\ell'$. In this paper, we use the band power $p_{\beta}$ and the covariance matrix of the band power $F^{-1}$ derived in Paper I based on the equations above. The auto power spectra are shown in Figure 2. The cross-power estimates between different redshift bins were generated in a similar manner and used only for determining covariance between different redshift bins.
3.1. Gaussian Covariance Matrix

If the density field is nonlinear (i.e., non-Gaussian), our estimator remains unbiased, but it will be no longer a minimum variance estimator and the variance of the band power will differ from Equation (4). Although the galaxy density field at $z \sim 0.54$ is expected to be non-Gaussian on small scales, we are interested on linear and quasilinear scales ($\ell \lesssim 300$ near $z = 0.54$ corresponds to $k \lesssim 0.2 h$ Mpc$^{-1}$) where the non-Gaussianity is moderate and, moreover, the projection of the density field along the line of sight suppresses the remaining non-Gaussianity by the central limit theorem. Tegmark et al. (2002) show that the non-Gaussianity indeed has little effect on the error bars of the quadratic estimators of the angular power spectrum over the physical scales similar to ours.

As an independent check, in Paper I, we used $N$-body mocks (the details of these $N$-body mocks are discussed in Section 5.1 of this paper) to compare the Gaussian covariance matrix based on Equation (4) and the true dispersion among the estimated band powers of the two-dimensional projection of the nonlinear, mock galaxy field. From the comparison, we did not find an obvious indication that the Gaussian covariance matrix underestimates the true error of the estimator. Also Takahashi et al. (2011) and Ngan et al. (2012) have shown a negligible effect of non-Gaussian errors on the BAO measurement in multi-parameter fitting. We therefore believe that the Gaussian field assumption for the errors is sufficient for our analysis.

Our OQE method does not trivially generate the covariance between different redshift bins. We first use the cross-power spectra between different redshift bins to derive the diagonal elements of the covariance of the auto power spectra between two different redshift bins, Cov[$p_β,z$, $p_β,z'$], using the Gaussian field assumption. Then, the off-diagonal elements, Cov[$p_β,z$, $p_γ,z'$], are obtained by multiplying the diagonal elements by the same correlation coefficients found for the covariance within a single redshift bin (i.e., Equation (4)), as the window function effect due to the survey mask is assumed identical to all the redshift bins. The full procedure is described in detail in Section 6.2.1 of Paper I.

4. METHODS

4.1. Outlines of the Fitting Method

Our goal is to robustly measure the location of the BAO scale, and therefore the distance scale $D_A(z)$, while minimizing possible effects from the assumptions made on the nonlinear or/and observational effects as well as cosmology during the fitting procedure. For example, it is non-trivial to properly model the evolution of the broadband power on the nonlinear scales, whether it is due to structure growth, redshift distortions, or galaxy bias. Therefore, we aim to exclude as much non-BAO signal as possible by marginalizing over the effect of the smooth broadband power. We measure the location of the BAO feature by fitting the observed auto (band) power spectrum $C_{obsz}(\ell)^{36}$ with the following fitting formula using a template power spectrum $C_{mz,\alpha}(\ell)$:

$$C_{obsz}(\ell) = B_{\alpha}(\ell)C_{mz,\alpha}(\ell/\alpha) + A_{\alpha}(\ell),$$

(7)

where $\alpha$, $B_{\alpha}(\ell)$, and $A_{\alpha}(\ell)$ are fitting parameters. The functional form for $B_{\alpha}$ and $A_{\alpha}$ is discussed in Section 4.2. The parameter $\alpha$ measures the angular location of the BAO relative to that of the fiducial cosmology. That is,

$$\alpha = \ell_{obsz}/\ell_{fid} = [D_A(z)/r_s]_{obs}/[D_A(z)/r_s]_{fid},$$

(8)

where $[D_A(z)/r_s]_{fid}$ is the fiducial angular location of the BAO in the template and $[D_A(z)/r_s]_{obs}$ is the measured angular location of the BAO. A value of $\alpha > 1$ suggests that the observed angular location of the BAO is smaller than that of the fiducial cosmology. For each redshift bin, $z$, free parameters $B_{\alpha}(\ell)$ and $A_{\alpha}(\ell)$ account for the smooth modification of the power spectrum from the template due to nonlinear structure growth and any scale-dependent bias. Finally, we use power spectra for CMASS1, CMASS2, CMASS3, and CMASS4 simultaneously and fit for a universal $\alpha$ while marginalizing over $B_{\alpha}$ and $A_{\alpha}$ independently at each redshift bin.

The template $C_{mz,\alpha}(\ell/\alpha)$ is constructed from the two-dimensional projection of three-dimensional power spectrum (Fisher et al. 1994; Padmanabhan et al. 2007). Including linear redshift distortions,

$$C_{mz,\alpha}(\ell) = \frac{2}{\pi} \int dk k^2 P_k(k, z) \times \left( \int dz \frac{dN_z}{dz} b(z) \frac{D(z)}{D(z = 0)} \left[ j_1(r(k, z)) - \beta j_1'(r(k, z)) \right] \right)^2,$$

(9)

where $r(k, z) = k(1 + z)DA_{z,fid}(z)$; $dN_z/dz$ is the normalized, true redshift distribution of galaxies for the corresponding photometric redshift bin (Figure 1); $j_1$ is the spherical Bessel function; $j_1'$ is the second derivative of the spherical Bessel function with respect to $r(k, z)$; $b(z)$ is a fiducial galaxy bias; $\beta$ is the fiducial redshift distortion parameter, $37$ and $D(z)$ is the linear growth rate. Due to the projection, redshift distortions significantly affect the broadband shape of the power spectrum only for $\ell < 30$; see the dashed and dotted lines in Figure 2 (see also, e.g., Nock et al. 2010).

Knowing $dN_z/dz$ precisely is critical for constructing the correct BAO location in the template. Note that thanks to the

36 Note that we switched the notation from $p_β$ to $C(\ell)$.

37 $\beta = \Omega_m^{2/3}(z)/b(z)$. 

Figure 2. Measured angular power spectra for the four redshift bins. The solid lines show the best fits derived in Section 6. The dashed line is the template for CMASS2 which is rescaled for clarity, with redshift distortions assuming a galaxy bias of 2. The dotted line is the template without redshift distortions.

(A color version of this figure is available in the online journal.)
extensive spectroscopic training set from the BOSS CMASS galaxies (112, 778 objects), we have an excellent determination of the redshift probability distribution for our photometric LG samples. Once we calculate the template $C_{m,A}(\ell)$ for the fiducial cosmology, we rescale the wavenumber with $\alpha$ to generate $C_{m,A}(\ell/\alpha)$ that fits the observed power spectrum in Equation (7) while marginalizing over the free parameters $B_m(\ell)$ and $A_m(\ell)$.

The term $P_m$ is generated by degrading the BAO portion of the fiducial, linear power spectrum with a nonlinear damping parameter $\Sigma_m = 7.527\left[D(z)/D(0)\right] h^{-1} \text{Mpc}$ to mimic the nonlinear evolution of the BAO due to the structure growth (Eisenstein et al. 2007):

\[
P_m(k, z_i) = [P_{\text{lin}}(k) - P_{\text{nw}}(k)] \exp \left[-k^2 \Sigma_m(z_i)^2 / 2\right] + P_{\text{nw}}(k),
\]

where $P_{\text{lin}}$ is the linear power spectrum at $z = 0$ derived from CAMB (Lewis et al. 2000) and $P_{\text{nw}}$ is the no-wiggle form, i.e., the power without BAO, calculated using the equations in Eisenstein & Hu (1998). The smoothing of the BAO is dominated by the width of the underlying redshift distribution, and the exact choice of $\Sigma_m(z)$ does not have a significant impact. For clarity we refer to $C_{m,A}(\ell)$, instead of $P_m$, as a "template" (angular) power spectrum and $P_m$ as a "base" power spectrum in this paper. We use a fiducial cosmology similar to the WMAP7 results (Komatsu et al. 2011) to define $P_m$ and $D_A, \text{fid}(z)$: $\Omega_m = 0.274$, $\Omega_\Lambda = 0.726$, $h = 0.7$, $\Omega_b = 0.046$, $n_s = 0.95$, and $\sigma_8 = 0.8$. These values produce the fiducial sound horizon scale, $r_s = 153.14 \text{Mpc}$, based on Eisenstein & Hu (1998), and the fiducial angular location of the BAO, $[D_A(z)/r_s, \text{fid}] = 8.858$ at $z = 0.54$.\footnote{Using the exact calculation of drag epoch rather than the fitting formula in Eisenstein & Hu (1998), we find $r_s = 149.18 \text{Mpc}$ for our fiducial cosmology. Therefore, $[D_A(z)/r_s]_{\text{fid}} = 8.813$ at $z = 0.54$.}

Note that in Equation (9) we assume that rescaling the sound horizon and angular diameter distance is equivalent to rescaling $\ell$ (i.e., the second equality of Equation (8)), which we call "$\alpha$ model." This will be a reasonable approximation when the thickness of the redshift distribution that is projected on the two-dimensional celestial surface is much larger than the scale of the clustering, i.e., in the limit of the Limber approximation. Based on the mock test in Section 5 and the robustness test in Section 6, the $\alpha$ model appears to be a good enough approximation for our choice of fitting range and parameterization.

The measured band power $C_{\text{obs}, z_i}(\ell)$ has a contribution from a range of wave numbers, which is described by a window function (Equation (6)). Due to the large and contiguous survey area, the window function is sharply peaked with little correlation with neighboring bands (Figure 3). We account for this window function effect in the fitting. That is, for each wavenumber band $l_A$ for the redshift bin $z_i$,

\[
C_{\text{obs}, z_i}(\ell_A) = \int_{0}^{l_A} [B_{\text{w}}(\ell) C_{\text{m}, A}(\ell/\alpha) + A_{\text{w}}(\ell)] W(\ell/\ell_A) d\ell.
\]

4.2. A Choice of $B(\ell)$ and $A(\ell)$

There are a few considerations to make when choosing the optimal parameterization for $B(\ell)$ and $A(\ell)$. We want $B(\ell)$ and $A(\ell)$ to be flexible enough to model and remove the broadband shape of the power spectrum. With the flexibility in $B(\ell)$ and $A(\ell)$, we also gain some tolerance on a possible, small difference between the BAO feature in the fiducial template and the observed feature by trading power between $B(\ell) C_{m, A}(\ell)$ and $A(\ell)$. On the other hand, an arbitrarily flexible $B(\ell)$ and $A(\ell)$ will undesirably mimic BAO even with the no-BAO template. An extensive test of the parameterization for $B(\ell)$ and $A(\ell)$ for the template fitting method is discussed in Seo et al. (2008), where they allow a large number of free parameters for $B$ and $A$ based on the spatially averaged power spectra from $N$-body realizations which correspond to a spectroscopic survey. With our photometric redshift uncertainty, a projection of the BAO from different distances introduces an additional damping in the feature, leaving higher harmonics other than the first much less distinct relative to the noise level. Therefore, we are forced to limit the flexibility in $B(\ell)$ and $A(\ell)$ more strictly than the case assumed in Seo et al. (2008) while still making sure that the BAO scale is correctly recovered. We choose a revised fitting range so that the broad band is well modeled despite the smaller number of $B(\ell)$ and $A(\ell)$.

Based on tests with mock catalogs (Section 5), we use a fitting range $30 < \ell < 300$ and a linear function in $\ell$ for $B_\ell$, and a constant $A_{\ell}$ (abbreviated with “A0B1” hereafter):

\[
B_{\ell}(\ell) = B_{\ell, 0} + B_{\ell, 1} \ell
\]

\[
A_{\ell}(\ell) = A_{\ell, 0}.
\]

Therefore, for four redshift bins, we fit for a total of 13 parameters including $\alpha$ using 100 band power measurements (25 bands per each redshift bin) so that the total degrees of freedom is 87.

4.3. Parameterizing $D_A(z)$

The observed location of the BAO peaks in a power spectrum is determined by the angular diameter distance at each redshift. In a sample selected using photometric redshift, the location of the BAO feature for a given redshift slice depends on an integration over the broad range of the true redshift distribution, rather than a distance at a single redshift, as evident in Equation (9). In an ideal case, we may attempt to constrain the redshift dependence of $D_A(z)$ over the entire spectroscopic redshift range in a non-parametric way (e.g., Percival et al. 2010) in the fitting process. In reality, the Fisher matrix analysis predicts an error of $\sim$4% on a single measurement of $D_A(z)$ for all our four redshift
bins combined. Also while the expected true redshift distribution has long tails (0 < z < 1), the distribution tends to peak sharply for each photometric bin so that most of the information for a given bin is well concentrated within ±σz. Third, for a reasonable range of cosmology, the shape of DA(z) does not evolve significantly between z = 0.45 and z = 0.65. We therefore expect little gain for designing our analysis to measure multiple DA(z)s, i.e., the evolution of DA(z) as a function of redshift. We instead design our fitting method to measure a single, more precise distance measurement at the redshift that contributes the most information. Based on the median and mean redshift of the photometric sample, we assign our measurement of DA to z = 0.54.

In detail, we assume DA, fid(z), given by the fiducial cosmology, and set

$$D_A(z) = \alpha D_{A, fid}(z).$$  \hspace{1cm} (14)

That is, we fix the shape of the DA(z) to be the same as DA, fid(z) and measure the amplitude of DA(z).

4.4. Clustering Evolution of Luminous Galaxies

In generating the template C\_m,n(\ell), we need to make a prior assumption on the evolution of the galaxy bias of LGs and the linear growth rate (Equation (9)). We consider two extreme cases of the galaxy clustering evolution: first, we assume that the overall clustering, b\_i D\_i, does not change with redshift, which we call “con-cluster.” Second, we assume that the bias does not change with redshift, which we call “con-bias.” The two cases make little difference in the final best fit of \alpha, mainly because the expected true redshift distribution sharply peaks within ±σz, compared to the galaxy clustering evolution. Note that by marginalizing over B\_zi at each photometric redshift bin z\_i, we take into account the evolution of galaxy clustering across different redshift bins whether we use “con-cluster” and “con-bias.” As a default, we fix b = 2 inside C\_m,n(\ell) (i.e., “con-bias,” and therefore the best-fit B\_zi can be approximately interpreted as b\_0(z\_i)).

5. TESTING THE METHOD

Before applying our fitting method to the real data, we want to validate, using mock catalogs, that our fitting method returns an accurate estimate of the BAO scale. In other words, we want to check that neither our process of deriving OQEs of band powers nor our fitting method biases the measured BAO scale.

5.1. N-body Mocks

We first use mocks generated from N-body simulations to show the sanity of our OQE estimator and our fitting method in the presence of nonlinearities. White et al. (2011) constructed 20 CMASS mocks based on a halo-occupation distribution modeling of the observed clustering of the CMASS galaxies that were obtained from the first semester data by BOSS. Therefore, these mocks represent almost the same galaxy bias and shot noise as our sample. As explained in Paper I in detail, we generate mock catalogs of our imaging data making use of these 20 CMASS mocks. We call these “N-body photomocks.” The cosmology used for generating these mocks is the same as our fiducial cosmology. The comoving volume of the original CMASS mock is \(1.5 h^{-3} \text{Gpc}^3\) and, to build N-body photomocks, we extract an octant of a spherical shell between \(r = 1.33 h^{-1} \text{Gpc}(z = 0.5)\) and \(1.45 h^{-1} \text{Gpc}(z = 0.55)\) from the origin (one corner of a simulation box) and project galaxies along the radial direction without introducing photometric redshift errors. For simplicity, we do not include redshift distortions, which will be visible only on very large scales (Figure 2), or the effect of the mask in generating these mocks. Each of the resulting N-body photomocks spans a \(\pi/2 \text{rad}^2\) (=5157 deg\(^2\)) and contains ~125,000 galaxies, which gives a level of shot noise that is very similar to CMASS2 and CMASS3. Since we use a sharp cutoff of galaxy distribution between \(z = 0.5\) and 0.55 for mocks while the observed galaxies have long tails in their redshift distribution, the amplitude of the mock power spectrum is overall boosted relative to the real data. Despite this overall boost, the signal-to-noise ratio per mode of each mock (i.e., the shot noise contribution) is very similar to CMASS2: both dotted lines cross the data points at the same wavenumber scale. The error bars of the averaged mocks are much smaller than CMASS2 due to a larger cosmic volume averaged over the mock data. In the bottom panel, we compare the BAO feature from these mocks (red points) and the theory template for CMASS2 (Equation (9)) (black line), divided by a smooth power spectrum \(C_{\ell, \text{sm}}\) where \(C_{\ell, \text{sm}}\) is derived with \(P_n = P_{nw}\). The mock power spectrum indeed has a BAO feature that is quite similar to that expected for CMASS2. For our purpose, the N-body photomocks therefore serve as reasonable mocks.

(A color version of this figure is available in the online journal.)
for CMASS2 (i.e., \(0.5 < z < 0.55\)), as shown in the bottom panel of Figure 4 where we compare the BAO feature from these mocks (red points) and the theory template for CMASS2 (Equation (9); black line), divided by a smooth power spectrum \(C_{\ell, \text{sm}}\). Therefore, the photoz-mocks serve as reasonable mocks for the observed power spectrum.

We repeat the procedure by placing an origin at 8 different corners of each simulation box and generate 8 sets (i.e., eight lines of sight) of 20 imaging mocks, i.e., a total of 160 mocks. Note that the eight lines of sight from each simulation box share a portion of volume and therefore are not independent of each other. We generate the template power spectrum based on the galaxy distribution of the mock catalogs using Equation (9).

To better detect a possible bias on \(\alpha\) when using our fitting method, we increase the signal-to-noise ratio by averaging many power spectra. We average power spectra of the 20 mocks for each configuration (i.e., each line of sight) and fit for \(\alpha\). For the eight configurations, using “A0B1” (i.e., with \(B_0 + B_1 \ell\) and \(A_0\), we show the derived best fits and the 68.3% range of the likelihood in Figure 5. The distribution of eight \(\alpha\) values appears slightly wider than what one would expect from a Gaussian distribution. However, it is not appropriate to compare this result with a Gaussian case, as the number of sets (i.e., eight) is too small to estimate the underlying distribution and the eight configurations are not independent from each other but share some portion of their volumes. If we ignore this dependence and treat all the 160 mocks as completely independent, the average of the 160 mocks gives 0.91(\(\pm 0.66\))% of bias. Overall, we do not see an obvious indication either that the best-fit \(\alpha\) from our OQE estimator is biased or that our fiducial fitting method introduces a bias by more than 1%.

5.2. Gaussian CMASS Mocks

We next test the accuracy of our fitting method using sets of mocks that have exactly the same noise properties as the real data. We generate many Gaussian mock power spectra using the covariance matrix for the real data described in Section 3.1, assuming that the effect of non-Gaussianity on this covariance is small as discussed before. In detail, in order to generate a theoretical LG power spectrum from which we derive Gaussian deviates, we find the best-fit band powers for the power spectra measurements of CMASS1, CMASS2, CMASS3, and CMASS4 over the entire wavenumber range (i.e., \(1 < \ell < 600\)), while deliberately using a slightly different choice of \(B(\ell)\) and \(A(\ell)\) (A2B0, i.e., with \(A_0 + A_1 \ell + A_2 \ell^2\) and \(B_0\))\(^{40}\) than our fiducial method; \(\alpha\) is fixed to be unity during this process. This approach allows us to construct theoretical power spectra for the fiducial cosmology while taking into account the realistic broadband shape of LGs. Using the four best-fit band power spectra and using the covariance matrix for the real data, we generate 500 sets of Gaussian CMASS mocks. For each set, the four CMASS mock power spectra therefore mimic CMASS1, CMASS2, CMASS3, and CMASS4 not only in terms of clustering but also in terms of the covariance among them. One of the mock CMASS2 is shown in the top left of Figure 6 in comparison to the real data.

We then apply our fiducial fitting method (A0B1) to the 500 CMASS mocks over \(30 < \ell < 300\). Since the mock data and the template use the same fiducial cosmology, we expect the average value of \(\alpha\), if unbiased, to be unity. The top right panel of Figure 6 shows the pdf distribution of the 500 best-fit \(\alpha\) values when we fit the mock data over \(30 < \ell < 300\) using A0B1. The mean and the standard deviation of \(\alpha - 1\) is 0.10(\(\pm 0.60\)%). After rescaling the standard deviation by the square root of the number of samples, the mean and the error associated with the mean value of \(\alpha\) is 0.10(\(\pm 0.30\)%), i.e., unbiased within 1 – \(\sigma\). Decreasing the number of free parameters to A0B0 causes a biased estimation of \(\alpha\) as large as 2% in \(\alpha\). We find that A1B0 also gives an unbiased result, while we find that parameterizations with more free parameters result in a non-negligible degree of bias on the BAO location.

The distribution has significant “tails” as shown in Figure 6. As a result, the standard derivation (6.60%) is much larger than the range that contains 68.3% of the distribution: \(\alpha - 1(\%) = 0.1 \pm 1.5\). That is, the distribution of \(\alpha\) appears wider than the Gaussian one. This result shows that the likelihood of \(\alpha\) is not necessarily Gaussian even if the power spectrum follows a Gaussian likelihood. This is because the transformation from power spectrum to \(\alpha\) is not linear. When a signal to noise of a data set improves, however, the likelihood of \(\alpha\) will eventually converge to Gaussian, as the log likelihood surface will be asymptotically quadratic near the maximum likelihood point. We have excluded a few catastrophic outliers (~1.2% of the samples for the fiducial case) that show \(\alpha - 1(\%) > 40\) in deriving these statistics.\(^{41}\) Obviously, these cases are not fitting to the BAO feature. Some of these catastrophic outliers show a factor of a few larger errors on \(\alpha\) than the rest of the samples, while others show a reasonable error associated with the best fit. We find that the reduced \(\chi^2\) of these catastrophic outliers are not necessarily large. While we exclude these extreme outliers so that the statistics of the distribution are not dominated by these occasions, we note that, in analyzing a real data,

\(^{40}\) We allow more flexibility in this operation, compared to our default choice, as the fitting range here is larger than our default case. Also we made the two parameterizations different to simulate some degree of blindness in measuring the broadband shape.

\(^{41}\) Excluding these outliers substantially decreases the standard deviation (from 10.4% to quoted 6.6%) and the bias on the mean (0.5% to the quoted 0.1%), while having a very small effect on the 68.3% of the distribution (from 4.65% to the quoted 4.5%–4.6%).
Figure 6. Top panel shows one of the Gaussian CMASS mocks for CMASS2 (magenta circles) in comparison to the real data (black squares). The solid lines show the best-fit model we used to generate the mocks. The other three panels show the distribution of the 500 best-fit $\alpha$ values of the Gaussian CMASS mocks. Top right panel: the template is generated using the same cosmology as one used for generating the mocks (i.e., $\Omega_{mh}^2 = 0.134$). The histogram shows the result using $A0B1$ over $30 < l < 300$. The black point with error bar shows the mean $\alpha - 1$ and the error associated with the mean. The black dot-dashed line near the center shows the expected best-fit $\alpha - 1$ for each cosmology. The red and magenta (only in the top second panel) dotted lines show the average error derived from the 500 mock values for the range for $\Delta \chi^2 = \pm 1$ and the range for the 68.3% of the likelihood, respectively. The blue dotted line shows the range that contains 68.3% of the distribution of the 500 best-fit $\alpha$s. The three values are quite similar. Bottom left: the distribution of the best-fit $\alpha$ of CMASS mocks when the template is built using $\Omega_{mh}^2 = 0.148$. Bottom right: using the template built assuming $\Omega_{mh}^2 = 0.127$. (A color version of this figure is available in the online journal.)

we expect to derive a very wrong value of BAO scale more likely than would be expected were this distribution perfectly Gaussian.

For the real data, we have only one realization and therefore need to check that the error we quote for the data will be closely approximating the 68.3% range of the sample distribution if we had more than one sample. For each CMASS mock set, we derive errors associated with the best-fit $\alpha$ by applying $\Delta \chi^2 = \pm 1$ or by deriving the width that contains 68.3% of the likelihood. On average, the resulting error on $\alpha$ for an individual CMASS mock is $\alpha - 1(\%) = 0.1^{+4.7}_{-4.4}$ and $0.1^{+5.2}_{-4.7}$ for $\Delta \chi^2$ of $\pm 1$ (dotted red lines in Figure 6) and the 68.3% width of the likelihood (dotted magenta lines), respectively; the latter is slightly larger than the former. These are reasonably similar to the 68.3% range of the best-fit distribution of the mocks, which was $\alpha - 1(\%) = 0.1^{+4.3}_{-4.3}$ (dotted blue lines). We therefore will quote the 68.3% range of the likelihood surface as our formal error for the real data.

5.3. Variations in the Template

In Section 5.2, we assumed that the fiducial cosmology used for constructing the template matched the true cosmology, and we could recover an unbiased result in this situation. In fact, we also need to confirm that our method is unbiased when the cosmology used in the analysis does not match the true cosmology. The shape of the BAO feature is determined by the matter density and the baryon density, which is well measured by the current CMB observations. Seo et al. (2008) investigated how the results of the template fitting depends on small deviations in $P_m$ and found that the effect is negligible (less than 0.02% bias on $\alpha$). As explained in Section 4.2, our method in this paper uses a smaller set of free parameters due to the lower signal-to-noise level of the real data$^{42}$ and, as a result, it is possible that the fitting result is more sensitive to the deviation in $P_m$. We therefore revisit this issue. Since $\Omega_b h^2$ is better measured than $\Omega_m h^2$ by the CMB data, we only vary $\Omega_m h^2$ from the fiducial value, while the current CMB constraint on $\Omega_m h^2$ is $0.1326 \pm 0.0063$ (Komatsu et al. 2011). In order to leave the shape of the angular diameter distance to redshift relation unchanged, we hold $\Omega_b$ fixed and vary $h$ accordingly.

The bottom left panel of Figure 6 shows the distribution of the best-fit $\alpha$ of 500 Gaussian CMASS mocks when the

$^{42}$ Seo et al. (2008) use an N-body volume of $320 h^{-3} \text{Gpc}^3$, as a comparison.
template is built using $\Omega_m h^2 = 0.148$ (i.e., 10% away from $\Omega_m h^2 = 0.134$ used for the mocks). We again use the fiducial, A0B1 parameter set and a range of $30 < \ell < 300$. We find that using a smaller number of parameters, i.e., A0B0, makes the result more vulnerable to the variations in the template. Based on the sound horizon scale and $h$ in this cosmology, we expect $\alpha - 1(%) = 1.6$ (the dashed vertical line). The average of the best fit is $\alpha - 1(%) = 1.96 \pm 0.31$, and therefore we recover the correct BAO scale. The bottom right panel of Figure 6 shows the distribution of $\alpha$ using $\Omega_m h^2 = 0.127$, i.e., $-5\%$ away from the true value used for generating the mocks. We expect $\alpha - 1(%) = -2.10$ while we measure $-1.84 \pm 0.27$; we recover the expected value. We also have tested A1B0: we find a moderate bias for $\Omega_m h^2 = 0.148$ due to asymmetric tails, while the bias is overall less than 0.6%. This parameterization therefore would be a reasonable choice as well given the level of signal to noise of our data.

In the next section, we will apply the same test to the real data and show that the measured BAO scale does not change as a function of the fiducial cosmology assumed for the template. In addition to the assumption we made for $P_m$, we have also assumed a fiducial relation of angular diameter distance to redshift. We will show that we recover the same result over a range of angular diameter distance to redshift relationship.

Summarizing our mock tests, we find that the angular power spectra produced by our OQE code (Ho et al. 2012) show no strong sign of a bias in its BAO feature and that “A0B1” is a good choice of parameterization over $30 < \ell < 300$ for our data quality and therefore returns the correct BAO scale within 0.3% over a reasonable range of variations in our assumption.

6. RESULTS: DR8 IMAGING DATA

6.1. Best-fit Angular Location of BAO

We apply our fitting method to the DR8 imaging data and constrain the angular location of the BAO. Figure 7 shows our best-fit result using the combinations of CMASS1, CMASS2, CMASS3, and CMASS4. The red lines/points show the best-fit $C_\ell$ with the BAO template in comparison to the measured data (black squares with error bars). Both the data points and the best fits are divided by a smooth fit $C_{\ell,\text{sm}}$ that is derived by recycling the best-fit $\alpha$, $B_\ell(\ell)$, and $A_\ell(\ell)$ for $C_\ell$ but with $P_m = P_m^0$. The range of red points shows the range of the fitting, i.e., $30 < \ell < 300$. In the figure, we denote the best universal fit $\alpha$ with the associated errors that correspond to the 68.3% range of the likelihood distribution: we derive $\alpha - 1(%) = 6.61^{+1.36}_{-1.61}$. The reduced $\chi^2$ at the best fit is 1.20 for 87 degrees of freedom, and the probability of having a reduced $\chi^2$ value that exceeds this value is 11%. The inset in Figure 8 shows the measurement of the reduced $\chi^2$ for the DR8 data in comparison to the Gaussian CMASS mock distribution. We find that 12% of the mocks show $\chi^2$/dof > 1.2, which is similar to the expected 11%. The left panel of Figure 8 shows the resulting $\chi^2$ surface along $\alpha$ when marginalized over other parameters (red line). Note that due to the oscillatory feature of the BAO both in the data and the template there are local minima around the global minimum of $\chi^2$. As implied in the figure by the extent of the red line, when we derive the 68.3% range of the likelihood, we only include $\chi^2$ over $0.85 < \alpha < 1.35$, avoiding the local minima beyond this range.

The right panel of Figure 8 shows a stacked $C_\ell/C_{\ell,\text{sm}}$ of the four panels of Figure 7. Note that the stacking is done...
simply to better illustrate the BAO feature we measured and no fit is conducted using this stacked points. We perform this stacking procedure as follows. We rescale the wavenumbers of the four power spectra by \(D_A(z) / D_A(z_{\text{fid}})\) assuming the fiducial cosmology, where \(D_A(z_{\text{median}})\) is the median redshift for each redshift bin. We overlay the band powers of the four redshift bins based on the translated wavenumbers, re-bin the wavenumbers of the combined data while inversely weighting each band power by its error. We apply the same procedure to the smooth power spectra \(C_{\ell, sm}\). The solid red line is the best fit for CMASS2 after its wavenumber is translated to \(z = 0.54\), as a comparison.

Interpreting \(\alpha - 1(\%) = 6.61\) requires our determination of the redshift to which this measurement corresponds. Strictly speaking, the best-fit value of \(\alpha\) represents a constant ratio of the observed \(D_A(z)/r_s\) to the fiducial \(D_A(z_{\text{fid}})/r_s\) assumed in the template. The black solid and dashed lines (with a shade) in Figure 9 show what the best fit and the \(1 - \sigma\) error on \(\alpha\) imply in this strict interpretation. However, although the redshift dependence of \(D_A(z)\) we assume spans \(z \sim 0 - 1\), most of the galaxies are within \(z = 0.45\) and 0.65 with a peak of the distribution near \(0.5 < z < 0.55\). Therefore, it is reasonable to consider that the best-fit value \(\alpha(D_A(z)/r_s)\) represents \(D_A(z)/r_s\) near \(z = 0.5 - 0.55\). The median and the mean of the weighted galaxy distribution are \(0.541\) and \(0.544\), respectively. We therefore adopt \(z = 0.54\) as the characteristic redshift that our BAO measured scale represents.

To show that the best-fit BAO scale indeed does not depend on the cosmology we assume for \(D_A(z)/r_s\), we repeat our fitting with templates constructed using different cosmologies. In detail, we vary the equation of state of dark energy, \(w\), by \(\pm 0.2\), such that \(D_A(z)/r_s\) at \(z = 0.54\) varies by \(\sim 3.4\% - 3.7\%\), i.e., slightly less than the \(1 - \sigma\) range associated with the best-fit \(\alpha\). In other words, we are testing the consistency of our answer by varying the template by \(\sim 1 - \sigma\) from the fiducial case of \(\alpha\). Using a template with \(w = -1.2\), the best fit gives \(\alpha - 1 = 2.98^{+8.11}_{-4.48}\%\) and, with \(w = -0.8\), \(\alpha - 1 = 10.21^{+5.02}_{-4.85}\%\).

The top panel of Figure 9 shows the best-fit \(D_A(z)/r_s\) (\(= \alpha D_A(z)/r_s\)) using the three different templates. The solid lines show the best fit and the dotted lines show a \(1\sigma\) range of \(D_A(z)/r_s\). The bottom panel displays ratios of the best-fit...
$D_A(z)/r_s$ using no-$\Lambda$CDM templates with respect to the best-fit $D_A(z)/r_s$ using our fiducial $\Lambda$CDM template. From the top and the bottom panel, one sees that the three different templates have a very similar shape in $D_A(z)$ over $z = 0.45$–$0.65$, once the absolute difference is absorbed into $\alpha$. The three templates return virtually the same $D_A(z)/r_s$ at $z = 0.54$: they are consistent within 0.3%. We therefore quote the best fit using our fiducial $\Lambda$CDM template as our official measurement: $D_A(z)/r_s = 9.212^{+0.416}_{-0.404}$ at $z = 0.54$. Using the current WMAP7 constraint on the sound horizon at drag epoch, $153.2\pm1.7$ Mpc, we derive angular diameter distance $D_A(z) = 1411\pm65$ Mpc at $z = 0.54$. Table 2 summarizes our best-fit BAO location and the derived distance scale.

We further test the robustness of our result by constructing templates using various cosmologies. Figure 10 shows the best-fit $D_A(z)/r_s$ at $z = 0.54$ assuming $w$CDM, $\omega$CDM, $\Lambda$CDM, and assuming different values of $\Omega_m h^2$. For the range of cosmologies we have investigated in this paper, the best fit varies less than 1% in the acoustic scale while the 1σ error is ~4.5%. The errors vary slightly more than the variations in the best fit, especially when the template cosmology deviates substantially from the concordance cosmology. We also test a different parameterization than the fiducial choice, A1B0, which has marginally passed the mock test (i.e., a likely bias of $\sim 4.6\%$ on $\alpha$ based on the result in Section 5.3). A1B0 gives $\alpha - 1 = 7.5\%$, which is consistent with the fiducial result within 1%.

If we remove the BAO in the template (the blue line in Figure 8), we essentially fail to constrain $\alpha$. This means that the flexibility in our fitting is sufficient that the broadband shape information cannot constrain $\alpha$. Therefore, we conclude that our measurement of $D_A(z)/r_s$ is mainly from the BAO information.

As a comparison, Carnero et al. (2012) derived $3.90(\pm0.38)$ deg as an angular size of the BAO at $z = 0.55$ using the angular correlation function (Crocce et al. 2011) of SDSS DR7 imaging data (Abazajian et al. 2009). If we translate their result to $z = 0.54$, using our fiducial cosmology, their best fit of 3.96 deg is in an excellent agreement with our measurement of $4.039^{+0.185}_{-0.175}$ deg at $z = 0.54$ from the angular power spectra despite the different two-point statistics each study used. On the other hand, the precision of our measurement is much better than that of Carnero et al. (2012), where they measure the BAO location within 9.7%. The discrepancy arises partly because of the larger survey-area coverage in this work (i.e., a 1.4 times larger survey area) and a smaller redshift bin width ($\Delta z = 0.05$ compared to their $\Delta z = 0.1$) we used to project galaxies, but the main difference appears due to the difference in the uncertainty in the modeling. For example, Carnero et al. (2012) added a large systematic uncertainty to their result in order to reflect the uncertainty associated with $dN/dz$ due to choosing galaxies based on their photometric redshift. In our work, on the other hand, $dN/dz$ is quite well determined by the extensive training set (less than 0.5% error in the mean/median and 0.8%–2% error in the width of $dN/dz$, compared to the 1% error in the mean/median and 9% error in the width in Carnero et al. (2012; Crocce et al. 2011) and a template with a precise BAO location is generated given the redshift distribution and cosmology. Our analysis therefore is quite immune to the most of the systematic errors they account for. We observe approximately 1% of variations in the measurement of the BAO location depending on the choice of fiducial cosmology and parameterization, and we doubt that propagating the uncertainty on our $dN/dz$ to the distance measurement would contribute a systematic error bigger than this. The overall systematic effect of 1% that we infer has very small effect when added quadratically to our current error of 4.5%.

### 6.1. Significance of Detection

A reasonable concern regarding our measurement is whether or not we have fitted to only the BAO feature, or whether the result is offset due to noise spikes, which is obviously related to the significance of detection. The conventional method of

### Table 2

| $z$ | 0.54 |
|-----|-----|
| Assumptions | $r_s$/fid |
| $[D_A(z)/r_s]_\text{fid}$ | 153.14 Mpc using Eisenstein & Hu (1998) |

| Results | Best-fit $\alpha$ |
|---------|------------------|
| Best-fit $D_A(z)/r_s$ | $1.066\pm0.0487$ |
| Best-fit $r_s/[D_A(z)(1+z)]$ | $9.212\pm0.404$ |
| Best-fit $D_A(z)$ | $4.039^{+0.175}_{-0.135}$ deg |

| Results using the prior, $r_s = 153.7\pm1.7$ Mpc (WMAP7) |

#### Note.
Our best-fit BAO location and the derived distance scale.

#### Figure 10.
Best-fit $D_A(z)/r_s$ for various template cosmologies. We also show the result using a different parameterization (labeled with “Concordance ACDM (A1B0)” using A1B0) and the result with systematics correction (labeled with “Concordance ACDM (SYS)”): The one in the square box and the dotted vertical line are our fiducial choice: $D_A(z)/r_s = 9.212^{+0.416}_{-0.404}$ at $z = 0.54$. The results are consistent within 1%.

(A color version of this figure is available in the online journal.)
determining significance of BAO detection is to use a template with (i.e., BAO template) and without BAO information (i.e., no-BAO template) and observe the difference between χ² values of the two best fits. Using A0B1, we derive Δχ² = 4, which can be conventionally interpreted as a 2σ detection of BAO. However, such detection level depends on the choice of parameterization used in each of the two likelihoods.

We reconsider this issue of the detection level. Various observations including WMAP7 (Komatsu et al. 2011) and galaxy surveys (e.g., Blake et al. 2011b) have already shown that BAO feature exists. Given the signal-to-noise ratio level of our data, we are interested in how likely we have fitted to a BAO feature not a noise feature, rather than detecting the existence of BAO. Therefore, rather than fitting the power spectra with a no-BAO template, we shall fit many realizations of the power spectra with a BAO template and see how often we derive the correct BAO scale. For a large sample variance, the BAO feature in the power spectrum may be wiped out by noise (e.g., Cabrè & Gaztañaga 2011). Our mock test, Figure 6, shows that in the presence of the sample variance that is the same as our data, we recover the true acoustic scale within ~4.6% in 68.3% of the time. Obviously, we are not fitting to a BAO feature in the tails of the distribution. We therefore rephrase our detection level: our measurement is likely to recover the true BAO scale within 4.6% in 68.3% of cases, assuming that BAO exists.

With the same spirit, we can define a detection level differently. With a premise that BAO exists in the density field, we quote the plateau height of the χ² contour of the BAO fit as a detection level as well, as this height indicates how confidently we have measured the acoustic scale (see Xu et al. 2012; Anderson et al. 2012 for the same argument). A nice feature is that the plateau height is closely tied to the precision (i.e., the width of the same likelihood). From the left panel of Figure 8, the plateau height is Δχ² ~ 12 indicating a 3.5σ detection of the acoustic scale.

6.2. Effect of Systematics

A number of observational systematics can potentially contaminate the observed galaxy clustering: stellar contamination, seeing variations, sky brightness variations, extinction, and color offsets (Schlafly et al. 2010). However, as long as the systematics do not introduce a preferred scale similar to the BAO scale, i.e., if the systematics only introduce a smooth component in the power spectrum up to a sample variance, our results would not depend on the contamination from systematics. Paper I moreover has shown that the effect of the survey systematics is small. We therefore have not included the systematic corrections for our main result. In this section, however, we use power spectra that were corrected for the systematics using the method introduced in Paper I (also see Ross et al. 2011 for a similar method for the correlation function) and observe the effect of the systematics on the result.

The method in Paper I assumes that the effect of systematics is small and linear. In Fourier space, therefore, we assume that the following equation holds for each wave band ℓ:

\[ \hat{δ}_c(\ell) = \hat{δ}_{g,c}(\ell) + \sum_s ε_{c,s}(\ell) δ_{sa}(\ell), \]  

where \( \hat{δ}_c(\ell) \) is the observed galaxy density field at the \( z_i \)th redshift bin, \( \hat{δ}_{g,c}(\ell) \) is the true galaxy density field, and \( δ_{sa} \) are the variation of systematics across the sky. We only include the dominant three systematics identified in Paper I: stellar contamination, seeing

![Figure 11](attachment:figure11.png)

*Figure 11. Best-fit result after systematics correction using the combinations of CMASS1, CMASS2, CMASS3, and CMASS4 and using A0B1. We derive \( α = 1.070 \pm 0.047 \), which is quite similar to the result before systematics correction. The black data points in the four panels with error bars show the measured \( C_ℓ \) after systematics correction divided by a smooth fit \( C_{ℓ,\text{sm}} \) at CMASS1, CMASS2, CMASS3, and CMASS4. The red lines represent the best-fit \( C_ℓ \) and the red circles show the best-fit band power \( C_ℓ \) after the window function effect is considered.*
such as on the reduced improvement in the statistics after the systematics correction, is fairly robust against the systematics effects. The overall \( \alpha \) correction within 1% of the correction is consistent with the fit before the systematics correction. The spectroscopic surveys show that the systematics correction, while the effect of different BAO measurements in a two-dimensional space of variations, and sky brightness variations. The sum over \( s_a \) is a sum over these different systematic effects. If we assume that there is no intrinsic correlation between the systematics and the underlying large-scale structure, i.e., \( \langle \delta z_i \delta z_j \rangle = 0 \), we can solve for \( \epsilon_{zi,a} \) using the measurements of galaxy power spectra (i.e., \( \langle \delta g,zi \rangle \)) and the cross-power spectra between galaxies and the systematics (i.e., \( \langle \delta g,\delta g \rangle \)), as presented in Paper I. The error on the band power is minimally propagated: the error is quadratically increased by the amount of the final correction, after taking into account the number of wave modes.

Figures 11 and 12 show the best-fit results when we use the power spectra after systematics correction. We derive \( \alpha = 1 - 7.012^{+1.57}_{-1.63} \). The reduced \( \chi^2 \) has slightly improved to be 1.09. The difference in \( \chi^2 \) between using the BAO template and the no-BAO template has increased to 6.2 after systematics correction, from the previous 4.0 without systematics correction. The plateau height of the \( \chi^2 \) contour of the BAO fit increased to \( \sim 13 \) from \( \sim 12 \). The right panel of Figure 12, in comparison to Figure 8, shows that the systematics correction, while the effect is small, improves the fit on large scales (\( l < 100 \)).

Figure 10 shows that the best-fit value with the systematics correction is consistent with the fit before the systematics correction within 1% of \( \alpha \), demonstrating that the BAO fitting is fairly robust against the systematics effects. The overall improvement in the statistics after the systematics correction, such as on the reduced \( \chi^2 \), motivates the usage of the method in Paper I for future surveys, which can be further improved with a more careful error propagation during the correction. Given the small effect of the systematics on the BAO measurement, we take the result without the systematics correction as our main result in order to be conservative in the error estimation.

7. DISCUSSIONS: COSMOLOGICAL IMPLICATIONS

We combine our measurements of \( D_A(z = 0.54) \) with recent spectroscopic BAO measurements. The spectroscopic surveys report \( D_A(z) \) that contains both the information along the line of sight, \( H(z) \), and the information on the transverse direction, \( D_A \). In Figure 13, we present the distance-to-redshift relations of different BAO measurements in a two-dimensional space of \( D_A(z) \) and \( H(z) \). Our measurement of \( D_A(z = 0.54) \) appears as the black horizontal line with the shaded region representing the associated error. We also show the measurements of \( D_A(z = 0.2)/r_s \) and \( D_A(z = 0.35)/r_s \) from Percival et al. (2010) for SDSS DR7 (Abazajian et al. 2009) as red shades with magenta lines and \( D_A(z = 0.6)/r_s \) from Blake et al. (2011b) for the WiggleZ data over \( 0.2 < z < 1 \) (Drinkwater et al. 2010) as a blue line and shade. The black square points (along the dotted line) show the expected \( D_A(z) \) and \( H \) at \( z = 0.2, 0.35, 0.54, \) and...
Figure 14. Reddish contours: constraints on cosmological parameters after combining all BAO measurements shown in Figure 13 and the WMAP7 constraints (blue shaded contours). The green lined contours show the constraints without our measurement. The left panel shows flat \( \Lambda \)CDM case and the right panel shows \( o \)CDM with \( w = -1 \). The reddish lined degenerate contours in the top left show the constraint from our data alone when using the current CMB prior on \( \Omega_m h^2 \) (i.e., \( 0.1326 \pm 0.0063 \)). The black line in the top right panel shows \( \Omega_K = 0 \).

A color version of this figure is available in the online journal.

0.6 for our fiducial \( \Lambda \)CDM. Note that the measurements beyond \( z = 0.35 \) have a tendency to imply the location of the BAO at a smaller scale than the concordance \( \Lambda \)CDM (i.e., a larger \( D_A(z) \) than the fiducial cosmology), including our \( D_A \) measurement \((\sim 1.4\sigma \) away)\(^{44}\). Due to nonlinear structure formation and galaxy bias, we expect about \( \lesssim 0.5\% \) of bias toward a smaller value on the measured BAO scale for galaxy bias of \( \lesssim 2.5 \) \cite{PadmanabhanWhite2009,Seoetal2010,Mehetaal2011;also see Smithetal2008andCroceScoccimarro2008} for references that first pointed out the nonlinear bias on the BAO scale), which has not been accounted in these measurements. Such correction will slightly improve the consistency between the BAO measurements and the concordance \( \Lambda \)CDM, but it is overall a very small effect for the current level of errors. The circles along the dashed line and the crosses along the dot-dashed line in Figure 13 show the expected \( D_A(z) \) and \( H(z) \) based on our best-fit \( w \)CDM and \( o \)CDM cosmologies from COSMOMC \cite{LewisBridle2002} that will be explained below.

We use COSMOMC \cite{LewisBridle2002} to combine BAO measurements from the various galaxy surveys with the WMAP7 data \cite{Komatsuetal2011} to derive constraints on cosmological parameters. For BAO measurements, we use \( D_V(z = 0.2)/r_s \) and \( D_V(z = 0.35)/r_s \) from SDSS DR7 \cite{Percivaletal2010}, \( D_V(z = 0.44)/r_s \), \( D_V(z = 0.60)/r_s \), and \( D_V(z = 0.73)/r_s \) from WiggleZ\(^{45}\) and \( D_A(z)(0.54)/r_s \) from this work. The WMAP7 data provide the sound horizon scale and the distance to the last scattering surface and therefore, in combination of the BAO measurements from the galaxy

\(^{44}\) On the other hand, Gaztañaga et al. \cite{2009MNRAS.398..501G} has measured \( cz/H_0 = 7.94(\pm 0.26 \pm 0.15) \) using the BAO feature along the line of sight, which is consistent with 8.08 that is predicted from the concordance \( \Lambda \)CDM.

\(^{45}\) For COSMOMC, we use the three-redshift slice representation of the WiggleZ data from Blake et al. \cite{2011MNRAS.414.1560B}, i.e., \( 0.2 < z < 0.6, 0.4 < z < 0.8, \) and \( 0.6 < z < 1.0 \), accounting for the covariance among them, while in Figure 13 we show the result for the whole redshift range \((0.2 < z < 1.0)\).
Table 3
The Derived Cosmological Parameters

| $\Omega_m$ | $\Omega_CDM$ |
|------------|--------------|
| 0.2912 ± 0.0070 | 0.2939 ± 0.0170 |
| 0.6884 ± 0.0392 | 0.6748 ± 0.0175 |
| −1.0185 ± 0.1862 | Fixed at $w = -1.0$ |
| 0.7088 ± 0.0270 | 0.7118 ± 0.0172 |
| Fixed at $\Omega_K = 0.0$ | −0.057 (−0.0067) ± 0.0058 |

Notes. Marginalized fit and errors associated with the fit on selective parameters that are derived using COSMOMC (Lewis & Bridle 2002) for two different cosmologies. The values inside the parentheses show the best-fit values.

1. We derive $D_A(z)/r_s = 9.212^{+0.416}_{-0.404}$ at $z = 0.54$. Using the current WMAP7 constraint on the sound horizon at drag epoch, $153.2 \pm 1.7$ Mpc, we derive angular diameter distance $D_A(z) = 1411 \pm 65$ Mpc at $z = 0.54$. Without a BAO feature in the template power spectrum, we cannot constrain a distance scale; the distance information we derive is therefore dominated by the BAO feature for our choice of parameterization.

2. Our measurement of the distance scale is quite insensitive to the fiducial cosmology we assume for building the template. For a wide range of cosmologies we have investigated in this paper, the best fit varies less than 1% in the acoustic scale while the 1σ error is ∼4.5%.

3. The angular distance scale we derive is 1.4σ higher than the concordance ACDM model. When combined with three other BAO measurements from SDSS DR7 (Abazajian et al. 2009) spectroscopic surveys at $z = 0.2$ and 0.35 (Percival et al. 2010) and WiggleZ (Blake et al. 2011b) at $z = 0.6$, we find a tendency of cosmic distances measured using BAO to be larger than the concordance ACDM for $z \gtrsim 0.35$. Adding our measurement with these BAO measurements in the presence of WMAP7 prior therefore shifts the best-fit $\Omega_m$ slightly larger than the concordance cosmology.

In this paper, we have aimed at deriving a robust and conservative BAO information from the angular clustering of galaxies. We find that an accurate determination of the true redshift distribution of galaxies is crucial for a good photometric BAO measurement. Although the details of the method would and should vary for the conditions of different surveys, we hope that the approach described in this paper serves as a valuable reference for the analyses of future photometric BAO surveys.

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8. CONCLUSION

We have measured the acoustic scale from the SDSS-III DR8 imaging catalog using 872,921 galaxies over ∼10,000 deg$^2$ between 0.45 < $z$ < 0.65. Galaxies are binned into four different redshift slices where the width of each slice is 0.05, which is approximately the error associated with photometric redshift determination. Angular power spectra are generated using an OQE, as presented in Paper I. We use ∼110,000 SDSS III BOSS galaxies as a training sample to derive the true redshift distribution of the galaxies in the imaging catalog and therefore build reasonable template power spectra. We fit the templates to the measured angular power spectra and derive the best-fit acoustic scale while marginalizing over sufficient free parameters to exclude any non-BAO signal.
