Compact and Variable Radio Emission from an Active Galaxy with Supersoft X-Ray Emission

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Abstract

RX J1301.9+2747 is a unique active galaxy with a supersoft X-ray spectrum that lacks significant emission at energies above 2 keV. In addition, it is one of few galaxies displaying quasiperiodic X-ray eruptions that recur on a timescale of 13–20 ks. We present multipeoch radio observations of RX J1301.9+2747 using GMRT, Very Large Array (VLA), and Very Long Baseline Array (VLBA). The VLBA imaging at 1.6 GHz reveals a compact radio emission unresolved at a scale of <0.7 pc, with a brightness temperature of $T_b > 5 \times 10^7$ K. The radio emission is variable by more than a factor of 2.5 over a few days, based on the data taken from VLA monitoring campaigns. The short-term radio variability suggests that the radio emitting region has a size as small as $8 \times 10^{-5}$ pc, resulting in an even higher brightness temperature of $T_b \sim 10^{12}$ K. A similar limit on the source size can be obtained if the observed flux variability is not intrinsic and caused by the interstellar scintillation effect. The overall radio spectrum is steep with a time-averaged spectral index $\alpha = -0.78 \pm 0.03$ between 0.89 and 14 GHz. These observational properties rule out a thermal or star formation origin of the radio emission, and appear to be consistent with the scenario of episodic jet ejections driven by a magnetohydrodynamic process. Simultaneous radio and X-ray monitoring observations down to a cadence of hours are required to test whether the compact and variable radio emission is correlated with the quasiperiodic X-ray eruptions.

Unified Astronomy Thesaurus concepts: Active galactic nuclei (16); Accretion (14); Radio jets (1347); Relativistic jets (1390)

1. Introduction

Active galactic nuclei (AGNs) are powered by accretion of gas onto supermassive black holes (SMBHs) with $M_{BH} \sim 10^6 - 10^9 M_\odot$. They are considered to be scaled-up versions of Galactic black hole X-ray binaries (XRBs; $M_{BH} \sim 10 M_\odot$), because of the similarities seen from the accretion flow, such as rapid X-ray variability (Markowitz & Uttley 2005; McHardy et al. 2006), the relation between the X-ray and radio emission (Merloni et al. 2003; King et al. 2013), and the correlation between the X-ray spectral index and Eddington ratio (Yang et al. 2015; Ruan et al. 2019; Ai et al. 2020). X-ray observations of XRBs have revealed the existence of two characteristic accretion states, namely soft and hard states (Done et al. 2007). The soft state is dominated by the thermal emission from an inner accretion disk. As accretion rate drops, the Comptonized coronal emission at higher energies comes to dominate the X-ray spectrum (hard state).

It is well established that a flat-spectrum, compact jet is commonly observed during the hard state, which is, however, significantly quenched in the soft state (Fender et al. 2004). When sources transition from the hard to the soft accretion state, the radio emission begins to vary more dramatically, showing episodic jet ejection events (Miller-Jones et al. 2012; Bright et al. 2020). Such spectral state transitions and the relationships between jet ejections and accretion disk emission are still poorly understood in AGNs.

AGNs can be divided into radio-loud and radio-quiet populations according to the radio-loudness parameter, which is defined as the ratio of the flux densities between 6 cm and optical 4400 Å ($R = f_6/4400 \lambda$). Radio-loud AGNs are conventionally classified as those with $R \gtrsim 10$ (Kellermann et al. 1989). It has been found that the radio-loudness is anticorrelated with the Eddington ratios (Ho 2002; Greene et al. 2006), albeit with a larger scatter, implying that the jet radiation may be dependent on the accretion process. This seems supported by the low radio-loud fraction (∼7%, Stepanian et al. 2003; Zhou et al. 2006) observed in narrow-line Seyfert 1 galaxies (NLSy1s), a population of AGNs characterized by high accretion rates (Collin & Kawaguchi 2004; Komossa et al.)
2. Observation and Data Reduction

2.1. VLA

J1302 was not detected by Faint Images of the Radio Sky at Twenty cm (FIRST) using the Karl G. Jansky Very Large Array (VLA), with a 5σ upper limit on the peak flux of 0.95 mJy beam$^{-1}$. It was serendipitously detected in the deeper VLA 1.4 GHz imaging of the Coma cluster, with a peak flux density of 0.78 ± 0.11 mJy (Miller et al. 2009). To further study the origin of the radio emission, we observed J1302 with the VLA in three different bands, C, X, and Ku, centered at 6.0, 9.0, and 14.0 GHz, respectively. The C-band observation was performed in the B configuration on 2017 September 4 (project code: 17B-027), and the data were divided into 16 spectral windows with a total bandwidth of 2 GHz. The X-band observations were carried out eight times in the A configuration between 2015 July 5 and August 10 (project code: 15A-349). At the Ku-band, monitoring observations with a daily cadence were carried out in the C configuration between 2019 January 5 and January 12 (project code: 18B-115). All the observations were phase-calibrated using the calibrator J1310+3220, and 3C 286 was used for bandpass and flux density calibration. The total integration time is 30–35 minutes per band, with on-source time of 20 minutes at C-band, 10 minutes at X-band, and 12 minutes at Ku-band, respectively.

The data were reduced using the Common Astronomy Software Applications (CASA, version 5.3.0) and the standard VLA data reduction pipeline (version 5.3.1). For the reduced data product, we inspected each spectral window and manually flagged channels affected by radio frequency interference (RFI). The calibrated data were imaged using the CLEAN algorithm with Briggs weighting and ROBUST parameter of 0, which helps to reduce side lobes and achieve a good sensitivity. The final cleaned maps have a typical synthesized beam of 2$''$ × 0$''$.8, 0$''$.2 × 0$''$.2, and an rms noise of 10, ~10–11, and ~8–12 μJy beam$^{-1}$ at the C, X, and Ku band, respectively. J1302 was clearly detected in all observations. We used the IMFIT task in CASA to fit the radio emission component with a two-dimensional elliptical Gaussian model to determine the position, and the integrated and peak flux density. The radio emission at the three bands is unresolved and no extended emission is detected. The compactness of the radio emission is confirmed by the ratios of the integrated and peak flux density, which are in the range 0.92–1.35, with a median of 1.09. For consistency, only peak flux densities are used in our following analysis. The VLA observation log and flux density measurements are presented in Table 1.

2.2. GMRT

J1302 was observed with the Giant Metrewave Radio Telescope (GMRT) at band 5 (central frequency of 1.37 GHz) on 2015 May 31 (project code: 28_039). The GMRT band 5 data were divided into 512 channels across a bandwidth of 33.3 MHz. Flux calibration was conducted using 3C 147 and 3C 286, whereas the nearby source 3C 286 was also used to determine the complex gain solutions. 3C 147 was observed for ~30 minutes in the beginning while 3C 286 was observed for 4 minutes after every 55 minutes of the J1302 scan and ~30 minutes at the end of observation. 3C 147, 3C 286, and J1302 were observed for ~30 minutes, ~65 minutes, and ~9.2 hr, respectively. The data from the GMRT observations were reduced using CASA (version 5.6.1) following standard procedures and by using a pipeline adapted from the CASa Pipeline-cum-Toolkit for Upgraded Giant Metrewave Radio Telescope data REDuction (Kale & Ishwara-Chandra 2021). We began our reduction by flagging known bad channels, and the remaining RFI was flagged with the flagdata task using the clip and tfcrop modes. In total, we flagged ~20% of the data. We ran the task tclean with the options of the multiscale multifrequency synthesis (Rau & Cornwell 2011) deconvolver, two Taylor terms (nterms = 2), and W-Projection (Cornwell et al. 2008) to accurately model the wide bandwidth and the noncoplanar field of view of GMRT. We also used a robust parameter of 0, imsize of 2500 pixels, and cell size of 0$''$.5 in task tclean. In addition, we performed a few rounds of phase-only self-calibration to improve the fidelity of imaging. The final image has a synthesized beam of...
Table 1  
Summary of the Radio Observations of RX J1301.9+2747

| Project | Date       | Array | ν_{obs} (GHz) | S_{int} (μJy) | S_{peak} (μJy Beam\(^{-1}\)) | rms (μJy Beam\(^{-1}\)) | Beam Size (PA) |
|---------|------------|-------|---------------|---------------|-------------------------------|--------------------------|----------------|
| 15A-349 | 2015 July 5| VLA   | 9.0           | 119.2         | 115.1                         | 10.1                     | 0.23 × 0.18 (84.21) |
|         | 2015 Aug 7 | VLA   | 9.0           | 154.7         | 154.4                         | 10.4                     | 0.18 × 0.17 (–22.89) |
|         | 2015 Aug 7 | VLA   | 9.0           | 123.3         | 126.4                         | 10.3                     | 0.18 × 0.17 (–62.03) |
|         | 2015 Aug 7 | VLA   | 9.0           | 141.6         | 143.4                         | 9.8                      | 0.19 × 0.18 (–87.24) |
|         | 2015 Aug 8 | VLA   | 9.0           | 78.4          | 57.9                          | 11.1                     | 0.39 × 0.17 (68.58)  |
|         | 2015 Aug 9 | VLA   | 9.0           | 89.0          | 84.6                          | 10.7                     | 0.18 × 0.17 (–23.63) |
|         | 2015 Aug 10| VLA   | 9.0           | 90.4          | 98.2                          | 10.0                     | 0.18 × 0.18 (–65.56) |
|         | 2015 Aug 10| VLA   | 9.0           | 144.5         | 131.2                         | 10.4                     | 0.20 × 0.18 (88.07)  |
| 17B-027 | 2017 Sep 4 | VLA   | 6.0           | 295           | 304                           | 10.2                     | 2.43 × 0.84 (–63.19) |
| 18B-115 | 2019 Jan 8 | VLA   | 14.0          | 183.7         | 174.8                         | 9.2                      | 2.12 × 1.19 (–69.92) |
|         | 2019 Jan 9 | VLA   | 14.0          | 162.6         | 173.6                         | 11.5                     | 2.09 × 1.19 (–67.75) |
|         | 2019 Jan 7 | VLA   | 14.0          | 188.5         | 154.8                         | 9.0                      | 2.16 × 1.22 (–68.15) |
|         | 2019 Jan 8 | VLA   | 14.0          | 176.5         | 180.6                         | 9.3                      | 2.33 × 1.21 (–65.13) |
|         | 2019 Jan 9 | VLA   | 14.0          | 183.4         | 158.9                         | 8.4                      | 2.00 × 1.24 (–69.84) |
|         | 2019 Jan 10| VLA    | 14.0          | 147.7         | 116.7                         | 8.7                      | 2.14 × 1.25 (–67.12) |
|         | 2019 Jan 12| VLA    | 14.0          | 179           | 139.8                         | 9.2                      | 2.08 × 1.24 (–67.62) |
| 28,039  | 2015 May 31| GMRT  | 1.4           | 764           | 735                           | 23.2                     | 2.40 × 1.97 (92.7)   |
| BS255   | 2017 Feb 14| VLBA  | 1.6           | 670           | 559                           | 32.5                     | 0.012 × 0.0066 (25.22) |
| AM868   | 2006 June 18| VLA   | 1.4           | 866           | 779                           | 117.2                    | …                       |
| VLASS\(^b\) | 2017 Nov 25| VLA   | 3.0           | 894           | 513                           | 107                      | 2.60 × 2.16 (–54.25) |
| AS110   | 2020 Oct 17 | ASKAP | 0.89          | 1880          | 1896                          | 348.2                    | 25.0 × 25.0 (0.00)   |

Notes.

\(^a\) Due to the poor imaging quality, the beam size cannot be measured using CASA.

\(^b\) VLA Sky Survey (VLASS) consists of three-epoch observations, each separated by approximately a period of 32 months (Lacy et al. 2020). Only the epoch I data are used in this paper. The last three rows represent the archival VLA and Australian Square Kilometre Array Pathfinder (ASKAP) data (Section 3.3).

2.4 × 2.0. The GMRT flux density measurements are shown in Table 1.

23. VLBA

We observed J1302 on 2017 February 14 using the Very Long Baseline Array (VLBA) with its 10 antennas (project code: BS255). The observing frequency was centered at 1.576 GHz in the L band. The observation was performed in the phase-referencing mode to a nearby strong compact radio source (J1300+28). Phase-reference cycle times were 4.5 minutes, with 3 minutes on-source and 1.5 minutes for the phase calibrator. We also inserted several scans of the bright radio source 3C 273 for fringe and bandpass calibration with an integration time of 2 minutes for each scan. The resulting total on-source time was 6 hr. To achieve sufficiently high imaging sensitivity, we adopted the observational mode Digital Down-converter System for Roach Digital Backend to use the largest recording rate of 2 Gbps, corresponding to a recording bandwidth of 256 MHz in each of the dual circular polarizations. The data from the VLBA experiment were correlated with the DiFX software correlator (Deller et al. 2011). We used the NRAO AIPS software to calibrate the amplitudes and phases of the visibility data, following the standard procedure from the AIPS Cookbook.\(^{12}\) The calibrated data were imported into the Caltech DIFMAP package (Shepherd 1997) for imaging and model fitting. The results are given in Table 1.

3. Results

3.1. Radio Variability Analysis

Using the flux density between 6 cm and optical 4400 Å (Shu et al. 2017), we derived the radio-loudness parameter \( R \sim 3.3 \). This suggests that J1302 is formally radio-quiet, because a radio-loud object is usually defined to have \( R > 10 \) (Kellermann et al. 1989). We investigated the radio variability based on the radio flux measurements from the VLRA monitoring observations at the X and Ku bands. As shown in Table 1, the radio emission of J1302 is variable on timescales of days to months (as short as a few hours within one day). Specifically, the maximum flux density is higher than minimum one by a factor of 2.6 at the X band, and the variability amplitude is a factor of 1.5 at the Ku band. To further inspect the radio variability in individual observations, we plot in Figure 1 the radio flux densities normalized to their time-average value for the X band (left) and Ku band (right), respectively. We note that the error on the peak flux density given by IMFIT task in CASA is likely underestimated, as it is smaller than the image off-source rms. To be conservative, the flux errors shown in Figure 1 were calculated as the sum in quadrature of map rms and calibration uncertainty that is assumed to be of 5% of the flux density (e.g., Panessa et al. 2022). It can be seen that the variability amplitude in the percent change in flux relative to the averaged one can be as high as \( \sim 50\% \) at the X band, while it is \( \sim 30\% \) at the Ku band. In the lower panel, we also show the percent flux changes for the phase calibrator (J1310+3220), which are at a level of only \( \lesssim 10\% \). This flux variability does not significantly correlated with that of J1302, indicating that the observed variability cannot be dominated by the variability of phase or flux calibrators.

\(^{12}\) http://www.aips.nrao.edu/cook.html
To quantify the radio variability pattern of J1302 we calculated the debiased variability index \( V_{\text{rms}} \) (e.g., Barvainis et al. 2005). \( V_{\text{rms}} \) is similar to the fractional variability \( F_{\text{var}} \) that is commonly used in analyzing X-ray light curves (e.g., Vaughan et al. 2003). \( V_{\text{rms}} \) quantifies the variability amplitude in excess of uncertainties as a percentage of the mean flux,

\[
V_{\text{rms}} = \sqrt{\frac{S^2 - \langle \sigma^2 \rangle}{\langle F \rangle^2}},
\]

where \( S^2 \) is the variance of the light curve, \( \langle \sigma^2 \rangle \) is the mean squared flux errors that are the sum in quadrature of map rms and 5% flux calibration uncertainty, and \( \langle F \rangle \) is the mean flux density. A source is considered to be variable when \( V_{\text{rms}} > 0 \) by a significant amount. For J1302 we measured \( V_{\text{rms}}(9 \text{ GHz}) = 26 \pm 4\% \) and \( V_{\text{rms}}(14 \text{ GHz}) = 12 \pm 3\% \), respectively (Table 2).

In addition, we performed \( \chi^2 \) analysis to test the significance of variability in the light curve differing from a constant. For a nonvariable source, the value of reduced \( \chi^2 \) (i.e., \( \chi^2 / \text{degrees of freedom (dof)} \)) is expected to be 1. For a given \( \chi^2 \) value, we can derive the variability significance \( P_{\text{var}} = 1 - P(\chi^2; \text{dof}) \), where \( P(\chi^2; \text{dof}) \) is the probability to observe a \( \chi^2 \) larger than expected under the null hypothesis of no variability. According to the \( \chi^2 \) test, the \( X \)-band and \( K \)-band light curves shown in Figure 1 are variable at a confidence level of >99.99% and >99.94%, respectively, providing further evidence for the variability of J1302. Note that J1302 was observed three times on 2015 August 7 at 9 GHz, separated by \( \sim 1-2 \) hr, but the intraday variability amplitude was marginal with \( V_{\text{rms}}(9 \text{ GHz}) = 4.8 \pm 8.4\% \). However, a larger intraday variability amplitude of \( V_{\text{rms}}(9 \text{ GHz}) = 20 \pm 7\% \) was found for the observations performed between 2015 August 9 and 2015 August 10, indicating that the radio emission can vary on a timescale as short as a few hours.

![Figure 1](image)

**Figure 1.** Left panel: the normalized VLA peak flux densities relative to the mean flux at 9.0 GHz (\( S_{\text{9GHz}} \)). The lower panel shows the same normalized peak flux densities but for the phase calibrator J1310+3220. Right panel: the same as left, but for the radio light curve observed at 14 GHz.

### 3.2. Parsec-scale Radio Morphology

In Figure 2(a), we show the VLBA image of J1302 at 1.6 GHz. The source appears to be unresolved, which is very similar to the beam shape in size. Other than the central peak, no extended emission was seen above the image sensitivity of 0.098 mJy beam\(^{-1}\) (3\( \sigma \)). To measure the source size more accurately, we performed source fitting in the UV-plane to the total polarization intensity data using the \textsc{UV_FIT} task in the \textsc{GILDAS} software package. We found no additional components in the residual map (Figure 2(b)). The integrated flux density for the source in the UV-plane is \( \sim 655 \) \( \mu \)Jy, in good agreement with the flux density measured in the image plane using the \textsc{DIFMAP} package (Table 1). As shown in Figure 2(d), the VLBA source has a deconvolved size of \( 5.61 \text{ mas} \times 1.43 \text{ mas} \), indicating the extreme compactness of radio emission (\( < 0.7 \) pc at the redshift of J1302, \( z = 0.0237 \)). This is also consistent with the size measured using \textsc{DIFMAP}. The optical centroid reported by the Gaia DR3 (Gaia Collaboration et al. 2021) is marked as a black cross in Figure 2, which is R.A.(J2000) = 13\( ^{h} \)02\( ^{m} \)00\( ^{s} \)13806, decl. (J2000) = 27\( ^{\circ} \)46\( ^{\prime} \)57\( ^{\prime\prime} \)8496, with \( \sigma_{\text{R.A.}} = 0.18 \text{ mas}, \)

### Table 2

| Peak flux | Mean | Std. dev. | \( \chi^2 / \text{dof} \) | \( P_{\text{var}} \) | \( V_{\text{rms}} \) (%) |
|-----------|------|-----------|----------------|-----------------|----------------|
| J1302 \( S_{\text{9GHz}} \) \((\mu\text{Jy})\) | 113.9 | 32 | 51/7 | >99.99% | 26±4 |
| J1302 \( S_{\text{14GHz}} \) \((\mu\text{Jy})\) | 157 | 23 | 24/6 | >99.94% | 12±3 |
| Calibrator \( S_{\text{9GHz}} \) \((\mu\text{Jy})\) | 1.6 | 0.08 | 7/7 | 0.57 | 1.6±4.3 |
| Calibrator \( S_{\text{14GHz}} \) \((\mu\text{Jy})\) | 1.38 | 0.03 | 0.9/6 | 0.01 | ... |

**Note.** Calibrator refers to J1310+3220.
\( \sigma_{\text{decl.}} = 0.14 \text{ mas} \), and the astrometric excess noise of 1.35 mas. Considering the positional uncertainties of Gaia, the radio peak does not show any positional offset with respect to the optical centroid, indicating that the emission components at the two bands arise probably from the same region very close to SMBH.

The brightness temperature of compact radio emission can be estimated as (e.g., Ulvestad et al. 2005)

\[
T_b = 1.8 \times 10^9 (1 + z) \left( \frac{S_\nu}{1 \text{ mJy}} \right) \left( \frac{\nu}{1 \text{ GHz}} \right)^{-2} \left( \frac{\theta_1 \theta_2}{1 \text{ mas}^2} \right)^{-1} \text{ K},
\]

where \( S_\nu \) is the peak flux density in mJy at the observing frequency \( \nu \) in GHz, with \( \theta_1 \) and \( \theta_2 \) are the fitted FWHM of the major and minor axes of the Gaussian component in units of

\[ \text{milliarcseconds}. \]

Using the deconvolved size \( (\theta) \) derived from the VLBA image, we obtained a brightness temperature of \( \sim 5.0 \times 10^7 \text{ K} \). Note that the parsec-scale structure of J1302 is very compact and not resolved with the VLBA; only the upper limit on the source size can be constrained. Hence, the brightness temperature should be considered as a lower limit. Such a high brightness temperature allows us to exclude the star formation origin for the radio emission since \( T_b \) is typically lower than \( 10^6 \text{ K} \) as expected from star-forming processes (Pérez-Torres et al. 2021). The emission from young supernova remnants can also be ruled out, as the 1.4 GHz radio luminosity of J1302 \( (L_\nu = 7.3 \times 10^{20} \text{ W Hz}^{-1}) \) is higher than the majority of the radio supernova remnants, such as those studied in the starburst galaxy Arp 220 (Varenius et al. 2019).

In fact, despite different resolutions, the radio flux densities measured with the VLBA and GMRT are comparable to that obtained with the VLA about a decade ago at the similar band wavelengths.

Figure 2. VLBA 1.6 GHz image of J1302 and UV-plane source fitting result. Panel (a) and (c) shows the dirty source and beam images, respectively. The shape of the beam is shown in the left corner (gray filled ellipse) in panel (a). Panel (b) shows the residual map, which was imaged from visibilities (subtracted a two-dimensional Gaussian model in the UV-plane). There are no additional emission components in the residual map shown. Panel (d) is the modeled intrinsic source image. All panels have the same color scale. The radio source position (cyan plus sign) detected by VLBA is centered at R.A. \((J2000) = 13^\text{h}02^\text{m}00.1380^\text{s} \pm 0.00025 \) and decl. \((J2000) = +27^\circ46'59.8489'' \pm 0''00032 \). The black cross marks the optical centroid obtained from Gaia DR3. The circle denotes the Gaia 1 \( \sigma \) positional error, which is the sum in quadrature of the astrometric error and the uncertainty from astrometric excess noise.

\[ \text{Since J1302 is an extragalactic galaxy, we used the Gaia position without taking into account proper motions.} \]
Figure 3. The broadband radio spectrum of J1302. The flux density errors are calculated as the sum in quadrature of map rms and calibration uncertainty that is assumed to be 5% of the flux density (Section 3.1). The red line shows the best-fit power-law spectrum using the data from all observations. The resulting radio spectral index is \(\alpha = -0.78 \pm 0.03\). The error bars for the radio spectral index are estimated using Monte Carlo simulations (gray shaded region), assuming that the error on each flux density measurement follows a Gaussian distribution.

(Miller et al. 2009), disfavoring the scenario of transients as the origin of the radio emission, such as a supernova explosion, gamma-ray burst or TDE.

3.3. Radio Spectrum

Figure 3 shows all the radio measurements available for J1302 based on our GMRT, VLA and VLBA projects. We also included the publicly available data from archival radio surveys such as the Rapid ASKAP Continuum Survey (McConnell et al. 2020), VLA-Coma (Miller et al. 2009), and VLASS (Lacy et al. 2020). We retrieved the public radio maps and then measured the integrated and peak flux density with CASA, following the same procedures described in Section 2.1. The results are shown in Table 1. Although most observations were taken at different epochs and various resolutions, the radio flux density appears to decrease with frequency, indicating a steep radio spectrum between 0.89 and 14 GHz. By fitting a power-law spectrum \(S_\nu \propto \nu^{\alpha}\) to the data points, we obtained a spectral index \(\alpha = -0.6\) for the Palomar Seyfert galaxies (Ho & Ulvestad 2001). Note that using the data obtained from the quasi-simultaneous observations only, i.e., the GMRT and VLA observations performed on 2015 May–August, the radio spectrum of J1302 can still be described by a steep power law with slope \(\alpha = -1.03 \pm 0.04\). Therefore, the emission from J1302 has a steep radio spectrum, even considering the time variability, suggesting that it may be related to optically thin synchrotron emission. We will discuss the implications of the steep radio spectrum in Section 4.

4. Discussion

We report radio variability on daily to monthly timescales in the supersoft AGN J1302 through VLA monitoring campaigns in 15 epochs on 2015 July–August and 2019 January. In addition, we detect an unresolved radio emission at a milliarcsecond scale with the VLBA, corresponding to <0.7 pc at the redshift of J1302. J1302 is one of few AGNs with X-ray QPEs, and has a low black hole mass \((M_{BH} \lesssim 10^6 M_{\odot})\) accreting at a high rate \((L_\text{bol}/L_{\text{edd}} \gtrsim 0.1\), Shu et al. 2017). The radio light curve is variable with an rms amplitude of 26 \(\pm 4\%\) and 12 \(\pm 3\%\) with respect to the mean flux density at the X band (9 GHz) and K\(_u\) band (14 GHz), respectively. Daily flux variation up to a factor of \(~2.6\) is also observed at the X band. Such highly variable radio emission is an unusual property for J1302 as a radio-quiet AGN (Section 3.1). Radio emission from radio-quiet AGNs could arise from different physical processes (Panessa et al. 2019), including star formation, outflow, and jet and accretion disk corona. We will discuss these scenarios in detail according to the radio flux variability, morphology, size, brightness temperature, and time-averaged spectral index.

4.1. Extrinsic Variability Caused by Interstellar Scintillation?

The radio flux variability, if it is intrinsic to the AGN, would be useful to distinguish the sources of radio emission. We first consider whether the observed variability might be induced by the effect of refractive interstellar scintillation (ISS). This process occurs when radio waves propagate through an inhomogeneous plasma of our Galaxy, which could cause intraday variability in some AGNs with compact radio emission (Lovell et al. 2003; Rickett 2007). The amount and timescale of radio variation caused by ISS depend on the Galactic electron column density along the line of sight and the observing frequency. Using the NE2001 free electron density model developed by Cordes & Lazio (2002), and the Galactic dispersion measure (DM),\(^{14}\) along the line of sight to J1302, we find that, at the position of J1302, the transition frequency between strong and weak-scattering regime is \(v_0 \sim 4.9\) GHz. Hence J1302 is in the weak-scattering regime at 9 and 14 GHz. In this case, we computed the fractional modulation index due to ISS (Walker 1998),\(^{16}\) which is \(m = 0.42\) at 9 GHz and \(m = 0.23\) at 14 GHz, respectively, comparable to that observed in J1302. This amount of modulation is expected to occur on a timescale of \(t_\rho \sim 2(v_0/\nu)^{1/2} h \sim 1.2\) hr. While J1302 is found to vary at 9 GHz on a timescale as short as a few hours, the variability amplitude can be as low as \(V_{\text{rms}} = 4.8 \pm 8.4\%\), which seems inconsistent with the prediction of the ISS effect. On the other hand, if ISS is the main mechanism responsible for the flux density variation, the angular size of the radio source should be similar to the first Fresnel zone, \(\theta_p \sim 8/\sqrt{D\nu} \sim 2.4\)–3.0\%as, where \(D\) (in kiloparsecs) is taken as the NE2001 model distance for DM =9.25 cm\(^{-1}\) pc, and \(\nu\) is the observed frequency.

4.2. Subkiloparsec Outflow

Although the radio emission is variable and observed at different epochs and resolutions, we can obtain a time-averaged radio spectral index of \(\alpha = -0.78 \pm 0.03\) between 0.89 and 14 GHz (Figure 3), suggestive of an optically thin steep spectrum.

\(^{14}\) https://pypi.org/project/pyne2001/

\(^{15}\) J1302 has a galactic coordinate of \((l, b) = 49^\circ138781, 87^\circ566837\). We used the DM of 9.25 cm\(^{-1}\) pc for J1302, which was derived from the pulsar J1239 +2453 \((b > 86^\circ)\) in the ATNF Pulsar Catalogue.

\(^{16}\) In Walker (1998), the modulation index \(m\) is used to calculate the variability amplitude caused by ISS, which is defined as the ratio of the rms deviation to the mean value of the observed flux densities, \(m = \frac{V_{\text{rms}}}{\langle f \rangle} \).
Note that if using the data from GMRT 1.4 GHz, VLA 3, 6, and 14 GHz observations, which have similar resolutions (i.e., ∼2″), a consistent radio steep spectrum can be obtained (α = −0.70 ± 0.03). Laor et al. (2019) suggested that a subkiloparsec outflow interaction with the ambient interstellar medium could cause the optically thin radio emission in radio-quiet AGNs. However, since a nuclear outflow interaction were present, it would be resolved by our high-resolution VLBA observation into a number of clumpy structures or extended diffused emission (e.g., Yang et al. 2021; Yao et al. 2021). It is obviously incompatible with the VLBA imaging of J1302. On the other hand, there are no blueshifted absorption or emission lines in the X-ray and optical spectra suggestive of outflows. Hence the outflow interpretation for the radio emission seems disfavored.

### 4.3. Steady and Continuous Jet

Based on the high-resolution VLBA observation, J1302 has a high brightness temperature of $\gtrsim 5 \times 10^7$ K, which rules out the origin of radio emission from star-forming region or thermal processes (Section 3.2). Such a brightness temperature can place J1302 at the high end of the $T_b$ range for the radio cores detected in local Seyfert galaxies ($D \lesssim 22$ Mpc; Panessa & Giroletti 2013). If the flux variations in the radio light curve (Figure 1) are intrinsic to the AGN, the minimum variability on a timescale of 1 day can place a constraint on the source size of less than $8 \times 10^{-3}$ pc using the light-crossing time. Such a small source size suggests that the radio variability might originate from the innermost region of the AGN. Adopting the mean flux density at 9 GHz, this implies that the brightness temperature of the variable radio emission is $\gtrsim 9.4 \times 10^{11}$ K. Therefore, the brightness temperature is comparable to the inverse Compton catastrophe limit of $\sim 10^{16}$ K (Kellermann & Pauliny-Toth 1969), at which an emission region will radiate away most of its energy in X-rays via inverse Compton scattering in a timescale of days. The brightness temperature is, however, 1 order of magnitude higher than the equipartition temperature of $5 \times 10^{10}$ K (Readhead 1994), which is also usually used to indicate the intrinsic brightness temperature of the radio core in AGNs. The value was estimated by assuming that there is equipartition of energy between the radiating particles and the magnetic field, which is derived from a spectral cutoff due to synchrotron self-absorption (see details in Readhead 1994). Note that if the radio variability is extrinsic and caused by ISS, a similar limit on source size ($\omega_{isc} \sim 1.2 - 1.4 \times 10^{-4}$ pc constrained by the first Fresnel zone); hence the brightness temperature can be obtained. This implies that the radio emission could be associated with a jet. In this case, the jet could have a Doppler factor of $\sim 1$–10, depending on which intrinsic brightness temperature is taken. Hence, the beaming effect is not significant.

If the radio emission is from a steady and continuous jet, standard presumptions (by analog with XRBs) would be that J1302 is in the low-hard state, which is dominated by a hard X-ray power-law component at energies above 2 keV (Fender et al. 2004). However, X-ray emissions from J1302 have been supersoft, with more than 90% of photons having energies below 1 keV (Sun et al. 2013; Shu et al. 2017; Giustini et al. 2020), resembling the high/soft state observed in XRBs. High-resolution VLBI observations have found evidence of the presence of a jet feature in many local Seyfert galaxies (Panessa & Giroletti 2013) as well as radio-quiet NLSy1s with high accretion rates (e.g., Doi et al. 2013; Yao et al. 2021), either extending up to kiloparsec scales or being confined to the inner parsec regions due to the jet interaction with the circumnuclear gas medium. We do not find any extended structures in J1302 predicted by steady jets with the high-resolution VLBA observation. This suggests that the steady-jet model cannot account for the radio emission.

### 4.4. Episodic Jet Ejections

Given its high accretion rate ($L_{\text{bol}}/L_{\text{Edd}} \gtrsim 0.1$) and steep radio spectrum, one possible identity for J1302 is transitioning from the hard to soft state accompanied by an isolated radio ejection event, as observed in some XRBs (Corbel et al. 2001; Fender et al. 2004; Bright et al. 2020). It should be noted that J1302 is one of the few AGNs with X-ray QPEs detected, which are characterized by repetitive short-lived eruptions in the light curves. Strictly speaking, the X-ray eruptions in J1302 seem to be irregularly spaced in time rather than quasi-periodic (Giustini et al. 2020), which may be linked to the evolving corona as well as jet launching process (Wilkins & Gallo 2015; Gallo et al. 2019). Although no hard X-ray was detected in J1302, the ratio of 5 GHz to X-ray (0.3–2 keV) luminosity in the flare state is $3.4 \times 10^{-5}$, consistent with the relation for stars with active coronae (Laor & Behar 2008). In the quiescent state, the luminosity ratio is 1 order of magnitude higher ($L_{\text{5GHz}}/L_{0.3-2\text{keV}} = 7.7 \times 10^{-4}$), but still much lower than for radio-load AGNs. This analog suggests that a magnetically heated corona may be responsible for the radio emission of J1302. However, theoretical studies suggest that a flat synchrotron radio spectrum (between $\sim$1 and 300 GHz) would be expected from an X-ray corona (Ragnsinski & Laor 2016), which seems inconsistent with the steep spectrum observed in J1302 (Section 3.3). It should be noted that steep radio cores at milliarcsecond scales have also detected in other Seyfert galaxies, though they are not prevalent (e.g., Panessa & Giroletti 2013; Congiu et al. 2020), which usually indicate the presence of optically thin synchrotron emission.

On the other hand, episodic ejections of magnetized plasmoids in the innermost region of the AGN could be invoked to explain the radio emission. By analogy with the coronal mass ejection in solar physics (Lin & Forbes 2000, Yuan et al. 2009) proposed a magnetohydrodynamical model for episodic ejection of plasmoids from black holes associated with the closed magnetic fields in an accretion flow. In the model, magnetic field loops are twisted to form flux ropes because of the turbulence of the accretion flow. With the magnetic energy gradually accumulated to reach a threshold, the flux rope loses its equilibrium and is thrust outwards in a catastrophic way, leading to magnetic reconnection. The magnetic energy is released in this process and converted into the energy of thermal electrons in plasmoids associated with the ejection of the flux rope, which then emit strong synchrotron radiation. Since the plasmoid ejecta can be considered as single blobs, they expand almost adiabatically after leaving the accretion disk and can quickly become optically thin in the radio band (Yuan et al. 2009), explaining the steep spectrum. If this is the case, the episodic X-ray eruptions in J1302 may be regulated by magnetohydrodynamic process as well (Li et al. 2017). A high degree of polarization and polarization angle change would also be expected during the multiband flares. Simultaneous radio and X-ray monitoring observations, particularly in the X-ray eruption state, are
4.5. Comparison to Other Supersoft AGNs

In addition to J1302, two other AGNs having supersoft X-ray spectra are 2XMM J123103.2+110648 and GSN 069. The latter two sources were also observed with the VLA on 2017 November, in the same program as J1302 (17B-027). GSN 069 has weak radio emission, with a flux density of $S_{\text{6GHz}} = 61 \pm 25 \mu Jy$, while J1231+1106 was not detected with a 5σ upper limit of 38.6 μJy. Following the X-ray QPEs detected in GSN 069, an X-ray/radio campaign has been carried out, and no significant radio variability during QPEs is found (Minuzzi et al. 2019). The inferred radio spectral index is steep ($\alpha = -0.7$), consistent with that measured in J1302, suggesting a radio origin from optically thin synchrotron emission. However, the ratio of 5 GHz to X-ray (0.3–2 keV) luminosity in the QPE state is $4.5 \times 10^{-7}$, about 2 orders of magnitude lower than that for J1302, indicating either the radio emission or the flaring X-ray emission has different origins between the two objects. Owing to its faint radio flux density (<100 μJy), using the VLBA to image the parsec-scale structure of radio emission in GSN 069 is challenging.

5. Conclusion

We present GMRT, VLA, and VLBA observations of the supersoft AGN J1302, which revealed compact radio emission with a size of <0.7 pc. The radio emission is variable on a daily timescale at both 9 and 14 GHz, implying that the radio emitting region can have a size as small as $8 \times 10^{-4}$ pc, with a high brightness temperature of $T_b \sim 10^{12}$ K. If the observed flux variability is not intrinsic and caused by the ISS effect, a similar limit on the source size can also be obtained ($\sim 1.2 \times 10^{-4}$ pc). The radio spectrum is steep with a time-averaged spectral index $\alpha = -0.78 \pm 0.03$ between 0.89 and 14 GHz, suggesting that it may be related to optically thin synchrotron emission. These observational properties rule out the radio origin from star formation activities, subkiloparsec outflows, or AGN corona. Optically thin jet ejection driven by a magnetohydrodynamic process seems to be the most favored scenario. The magnetohydrodynamic model can be tested with future more sensitive polarimetric observations, which predicts a high degree of polarization in the radio emission.

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Software: CASA (v5.3.0 and v5.6.1; McMullin et al. 2007), AIPS (Greisen 2003), DiFX software correlator (Deller et al. 2011), DIFMAP (Shepherd 1997), GILDAS.18

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Additional note: The supersoft X-ray spectra of J1302 and GSN 069 are found to show QPEs with similar properties, as mentioned in the text. The note is included to clarify the observed variability and the associated variability in the radio emission. The radio emission is variable on a daily timescale at both 9 and 14 GHz, and the time-averaged spectral index is $\alpha = -0.78 \pm 0.03$ between 0.89 and 14 GHz, suggesting a relation to optically thin synchrotron emission. These properties rule out the radio origin from star formation activities, subkiloparsec outflows, or AGN corona. The magnetohydrodynamic model is supported by the observed high degree of polarization in the radio emission.

18 https://www.iram.fr/IRAMFR/GILDAS
