Optical multiband observations of BL Lacertae during the outburst of 2005

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ABSTRACT
The aim of our observations is to investigate the intranight variability properties and the spectral variability of BL Lacertae. 799 optical multiband observations were intensively made with the Beijing–Arizona–Taiwan–Connecticut (BATC) 60/90 cm Schmidt telescope during the outburst composed of two subsequent flares in 2005. The second flare, whose rising phase lasted at least 44 d, was observed with amplitudes of more than 1.1 mag in three BATC optical bands. In general, on intranight time-scale the amplitude of variability and the variation rate are larger at the shorter wavelength, and the variation rate is comparable in the rising and decaying phases within each band. A possible time-lag between the light curves in bands e and m, around 11.6 min, was obtained. Based on the analysis of the colour index variation with the source brightness, the variability of BL Lacertae can be interpreted as having two components: a ‘strongly chromatic’ intranight component and a ‘mildly chromatic’ internight component, which may be the results of both intrinsic physical mechanism and geometric effects.

Key words: BL Lacertae objects: general – BL Lacertae objects: individual: BL Lacertae – galaxies: photometry.

1 INTRODUCTION
BL Lacertae (BL Lac) is the prototype of BL Lac objects (BL Lacs). In the unified scheme of radio-loud active galactic nuclei (AGNs), BL Lacs and flat-spectrum radio quasars (FSRQs) are usually collectively termed as blazars. BL Lacs are characterized by non-thermal continuum emission across the whole electromagnetic spectrum with absent or weak emission and absorption lines (e.g. Stickel, Fried & Kühr 1993), variable and high polarization (e.g. Angel & Stockman 1980; Impey & Neugebaur 1988; Gabuzda et al. 1989), large amplitude and rapid variability at all wavelengths from radio to γ-rays (e.g. Ravasio et al. 2002; Böttcher et al. 2003) and superluminal motion of radio components (e.g. Denn, Mutel & Marscher 2000). BL Lac is a well-studied source that has been monitored in optical band for more than a century. Variability on both long and short time-scales has been observed by many authors (e.g. Racine 1970). Infranight optical variability (INOV) of this object was studied in detail during the long 1997 outburst. Nesci et al. (1998) reported multiband INOV based on the observations made in 1997 July. The source was never found to be stable during their campaign. They found that the amplitude of flux variation was always larger at shorter wavelengths and no apparent time-lags among the light curves in different wavebands could be detected. Speziali & Natali (1998) monitored BL Lac in three optical bands on three nights in 1997 August. Their results involved INOV on time-scale ranging from 30 min up to 3.5 h. They concluded that the magnitude of variability was larger at shorter wavelengths and the source showed a marked trend to become bluer when brighter. This chromatism of INOV was confirmed by many other authors (e.g. Matsumoto et al. 1999; Ghosh et al. 2000; Clements & Carini 2001). Papadakis et al. (2003) analysed the INOV, the time-scales of rising and decaying processes, and the time-lags between different optical bands. Their results showed that the variability amplitudes increased with increasing frequency. The rising and decaying time-scales were comparable within each band, but increased with decreasing frequency. The time-lag between the light curves in bands B and I was less than ~±0.4 h. They also detected significant spectral variations, which had the trend to become harder (bluer) as the flux increased.

In order to investigate the details of the physical processes and geometric conditions based on the brightness and spectral variability, BL Lac has been intensively monitored in four campaigns (see Ravasio et al. 2002; Villata et al. 2002; Böttcher et al. 2003; Villata et al. 2004a,b) by the Whole Earth Blazar Telescope collaboration from 1999 to 2003. Most of these optical multiband data were collected and analysed by Villata et al. (2004a). Their results from

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the analysis of colour index revealed that the variability had two components, long-term (a few days time-scale) ‘mildly chromatic’ variations and strong bluer-when-brighter chromatic short-term variations (intraday flares). Stalin et al. (2006) showed that BL Lac became bluer when brighter on intranight time-scale, while this trend was less significant on internight time-scale. Their results may also suggest that the variability of BL Lac has two components. They found that the dependence of the spectral variability on its brightness was different from that of S5 0716 + 714. On the contrary, some objects were reported to become redder when brighter. For example, Ramirez et al. (2004) presented that the spectrum of PKS 0736 + 017 became redder when brighter on both internight and intranight time-scales. This different property may be introduced by different physical processes or physical environments.

To shed more light on the INOV and spectral variation with respect to flux variation on both internight and intranight time-scales, we carried out dense observations on BL Lac. We describe the observations and data reduction in the following section. Section 3 gives the results of our observations. A summary is presented in Section 4.

2 OBSERVATIONS AND DATA REDUCTION

Our observations were carried out with a 60/90 cm f/3 Schmidt telescope, which is located at the Xinglong Station of the National Astronomical Observatories of China. The telescope is equipped with a 15-colour intermediate-band photometric system, covering a wavelength range of 3000–10 000 Å. A Ford Aerospace 2048 × 2048 CCD camera is mounted at its main focus. The CCD has a pixel size of 15 μm and its field of view is 58 × 58 arcmin², resulting in a resolution of 1.7 arcsec pixel⁻¹. The telescope and the photometric system are mainly used to carry out the Beijing–Arizona–Taiwan–Connecticut (BATC) survey (Zhou 2005).

We performed optical observations in the BATC e, i and m bands in a cyclic mode. Their central wavelengths are 4885, 6685 and 8013 Å, respectively. For good compromise between photometric precision and temporal resolution, the exposure times were 150 s in the BATC i band and mostly 240 s in the e and m bands. Because a frame size of 512 × 512 pixels (14.5 × 14.5 arcmin²) is large enough to cover BL Lac and its comparison stars, we only read out a frame size of 512 × 512 pixels of the CCD images. The readout time is about 5.6 s. So we can achieve a temporal resolution of about 12 min in each band. This quasi-simultaneous measurements enable us to investigate the colour variation. BL Lac was observed on 26 nights during the period from 2005 July 5 to November 18.

All images were processed with the automatic data reduction procedure including bias subtraction, flat-fielding, position calibration, aperture photometry and flux calibration. The adopted aperture radius was 4 pixels (6.8 arcsec), since the average full width at half-maximum of the object and the comparison stars was 3.5 arcsec. The inner and outer radii of the sky annulus were set as 3.5 arcsec. The inner and outer radii of the sky annulus were set as 0.0736 (JD 245 3617–245 3661). The amplitudes of variation during the time from 2005 July 5 to November 18. To carry out dense observations on BL Lac. We describe the observations and data reduction in the following section. Section 3 gives the results of our observations. A summary is presented in Section 4.

3 RESULTS

3.1 Light curves

The light curves in bands e, i and m are displayed in Fig. 1. Our photometry clearly shows that BL Lac is violent and varies from day to day during the period of our more than four months (JD from 245 3557 to 245 3693) monitoring. One can see two flares apparently from Fig. 1. The rising phase of the second flare lasted 44 d (JD 245 3617–245 3661). The amplitudes of variation during the second flare are 1.374, 1.252 and 1.174 mag in bands e, i and m, respectively. The variability amplitudes increased with increasing frequency. It is a pity that we did not completely record these two flares due to the weather conditions or other campaigns.

One can see that many fast oscillations superimposed on the long-term variations. Our multiband observations on many nights gave us the opportunity to intensively investigate the intranight variability. The criterion presented by Jang & Miller (1997) was adopted to decide whether the source was variable or not. It is defined as $C = \sigma_T/\sigma$, where $\sigma_T$ is the s.d. of the source magnitude, $\sigma$ is the s.d. of $\delta_i$.

Table 1. BATC magnitudes of the three comparison stars.

| Star ID | $e$ (mag) | $i$ (mag) | $m$ (mag) |
|---------|-----------|-----------|-----------|
| B       | 13.893 ± 0.011 | 12.148 ± 0.010 | 11.592 ± 0.005 |
| C       | 14.859 ± 0.018 | 13.970 ± 0.012 | 13.755 ± 0.012 |
| H       | 15.229 ± 0.025 | 13.913 ± 0.013 | 13.509 ± 0.010 |

Table 2. BATC e magnitudes of BL Lac.

| UT date yyyy/mm/dd | UT hh:mm:ss | JD (d) | Exposure time (s) | $e$ (mag) | $\epsilon e$ (mag) | $\delta e$ (mag) |
|-------------------|------------|-------|-------------------|-----------|-------------------|-----------------|
| 2005/07/05        | 19:05:25   | 245 3557.295 41 | 240 | 16.126 | 0.032 | -0.003 |
| 2005/07/05        | 19:19:26   | 245 3557.305 18 | 240 | 16.079 | 0.032 | 0.003 |
| 2005/07/06        | 19:20:50   | 245 3558.306 15 | 300 | 16.239 | 0.050 | 0.000 |
| 2005/07/15        | 17:59:35   | 245 3567.24976  | 240 | 16.011 | 0.078 | 0.029 |
| 2005/07/15        | 18:16:18   | 245 3567.261 23 | 240 | 16.008 | 0.064 | 0.036 |
Table 3. BATC $i$ magnitudes of BL Lac.

| UT date yyyy/mm/dd | UT h:m:s | JD (d) | Exposure time (s) | $i$ (mag) | $i_{\text{err}}$ (mag) | $\delta_i$ (mag) |
|--------------------|----------|--------|-------------------|----------|---------------------|----------------|
| 2005/07/05         | 19:09:31 | 245 3557.298 34 | 150 | 14.840 | 0.012 | −0.011 |
| 2005/07/05         | 19:24:42 | 245 3557.308 84 | 180 | 14.982 | 0.016 | 0.000 |
| 2005/07/06         | 19:28:01 | 245 3558.311 04 | 150 | 14.762 | 0.018 | 0.014 |
| 2005/07/15         | 18:05:46 | 245 3567.253 91 | 150 | 14.818 | 0.018 | 0.024 |

Table 4. BATC $m$ magnitudes of BL Lac.

| UT date yyyy/mm/dd | UT h:m:s | JD (d) | Exposure time (s) | $m$ (mag) | $m_{\text{err}}$ (mag) | $\delta_m$ (mag) |
|--------------------|----------|--------|-------------------|----------|---------------------|----------------|
| 2005/07/05         | 19:13:40 | 245 3557.301 27 | 240 | 14.258 | 0.013 | 0.003 |
| 2005/07/05         | 19:28:46 | 245 3557.311 52 | 240 | 14.245 | 0.014 | −0.003 |
| 2005/07/06         | 19:33:59 | 245 3558.315 19 | 300 | 14.410 | 0.018 | 0.000 |
| 2005/07/15         | 18:10:36 | 245 3567.257 32 | 240 | 14.205 | 0.017 | −0.005 |
| 2005/07/15         | 18:24:56 | 245 3567.267 33 | 240 | 14.205 | 0.017 | −0.010 |

Figure 1. Light curves in bands $e$, $i$ and $m$ from 2005 July 5 to November 18. Squares, circles and triangles in the large panels represent the BATC $e$, $i$ and $m$ magnitudes, respectively. Photometry errors are not plotted for clarity. Stars in the small panels represent the confidence of observations.

Because $\delta_i$ represents the variation of the comparison stars, $\sigma$ indicates the observational error that provides a more accurate determination of the actual error than the normal photometric error. $C$ is taken as the confidence level of variability. The source will be claimed to be variable at 99 per cent confidence level when $C \geq 2.576$. The object is decided to be variable only when $C \geq 2.576$ at least in two bands if it is monitored in three or more bands (Jang & Miller 1997; Stalin et al. 2006). To quantitatively analyse the INOV, the intranight variability amplitude is defined as (Heidt & Wagner 1996)

$$Y = \frac{100}{\langle D \rangle} \sqrt{(D_{\text{max}} - D_{\text{min}})^2 - 2\sigma^2} \text{ per cent},$$

where $\langle D \rangle$, $D_{\text{max}}$ and $D_{\text{min}}$ are the average, maximum and minimum of the magnitudes on one light curve. $\sigma$ is the same as what is described above.

There are 19 out of 26 nights on which the data points are more than five in each band. The confidence level of variability was calculated for these 19 nights in each band. According to the criterion described above, the object was variable on nine nights. The intranight variability amplitude, $Y$, was calculated for these nine ‘variable nights’. The variability amplitude in band $e$ is generally larger than those in bands $i$ and $m$. The average values are 1.22, 1.00 and 0.82 per cent, respectively. It is larger at the higher frequency. This is consistent with the results of Neschi et al. (1998), Speziali & Natali (1998) and Papadakis et al. (2003). In order to compare the variation rates of the light curves in different bands at both the rising and decaying phases, we fitted the light curves on the nine ‘variable nights’ with a linear model. The slope of the linear least-squares fitting is taken as the variation rate. Fig. 2 gives examples of linear fittings on four nights. One can see from Fig. 2 that the light curves in three bands are consistent with each other. All the analysis results are listed in Table 5, in which the universal date of observations (Column 1) is followed by the number of frames in each band (Column 2), the confidence level of variability with the label of being variable or not (Column 3, V/N indicates the source is variable or not), the intranight variability amplitude (Column 4), the variation rates and their errors in the rising and decaying parts (Columns 5 and 6). The statistical results show that the variation
Figure 2. Examples of intranight light curves on four nights. Filled squares represent the light curves in the BATC $e$ band. Filled circles and filled triangles represent the light curves of $i+1.0$ and $m+1.4$, respectively (shift just for clarity). The solid lines show the linear fittings to the rising and decaying parts of light curves.

The rates of the light curves in band $e$ is larger than those in bands $i$ and $m$ both in the rising and decaying parts. It is larger in the shorter wavebands in general. The average values of the variation rate are 0.065, 0.057 and 0.042 in the $e$, $i$ and $m$ bands for the rising parts, respectively, while for the decaying phases, they are, respectively, $-0.064$, $-0.061$ and $-0.051$. The variation rates are comparable in the rising and decaying phases.

3.2 Time-lag

It can be noticed that the shape of the light curves in three bands are very similar (see Figs 1 and 2). To look for correlations and possible time-lags between them, the $z$-transform discrete correlation function (ZDCF: Alexander 1997) was applied to the light curves on ‘variable nights’ that were determined to have INOV. ZDCF is an improvement of the discrete correlation function (DCF). ZDCF applies $z$ transformation to the correlation coefficients and uses equal population bins rather than the equal time bins in DCF (Edelson & Krolik 1988). The calculation of ZDCF requires that the light curves must have at least 12 points (Alexander 1997). The ZDCFs between the light curves in bands $e$ and $m$ are illustrated in Fig. 3. The ZDCFs in three nights without enough observation points are not good. So we only use the good ZDCFs in three nights to obtain the result. The time-lag was calculated by three methods. $\tau_p$ is the time-lag corresponding to the maximum of ZDCF, $\tau_c$ and $\tau_g$ are the time-lags calculated as centroid (see Raiteri et al. 2003, 2005) and by Gaussian fit, respectively. They are listed in Table 6. The columns of Table 6 are the date of observation, the maximum of ZDCF and the time-lags by three methods followed by their errors. The time-lags reveal that the variations in band $e$ lead the variations in band $m$. The average of the time-lags by three methods is 0.194 h (11.6 min). It is in excellent agreement with the lag obtained by Papadakis et al. (2003) on 2001 July 5, 0.23 h between bands $B$ and $I$. These two results are all larger than 3 min obtained by Stalin et al. (2006) between bands $V$ and $R$ on 2001 October 22. But the different separation of band frequency must be considered. An upper limit to the possible time delay (10 min) between bands $B$ and $I$ of 0716+714 obtained by Villata et al. (2000) suggests that our result is reasonable. It should be treated with caution, since it is close to the temporal resolution of observation in each band.

3.3 Spectral variability

The relationship between the optical spectral variability and the brightness variation was investigated by many authors for a number of BL Lacs (see e.g. Speziali & Natali 1998; Papadakis et al. 2003;
Table 5. Results of the intranight variability analysis, all dates are in the same year 2005.

| Date (mm/dd) | Band (N) | C(V/N) | Y (per cent) | $S_A \pm E_A \times 10^{-2}$ | $S_D \pm E_D \times 10^{-2}$ |
|-------------|----------|--------|--------------|-----------------------------|-----------------------------|
| 07/15       | e (7)    | 2.217  |              |                             |                             |
|             | i (7)    | 1.264  |              |                             |                             |
|             | m (7)    | 1.845  |              |                             |                             |
| 08/25       | e (14)   | 4.385  | 2.09         | 7.7 ± 4.3                  |                             |
|             | i (14)   | 1.909  | 1.15         | 6.3 ± 0.7                  |                             |
|             | m (14)   | 4.489  | 0.93         | 3.4 ± 0.6                  |                             |
| 08/26       | e (9)    | 4.262  |              |                             |                             |
|             | i (9)    | 1.221  |              |                             |                             |
|             | m (9)    | 1.464  |              |                             |                             |
| 08/27       | e (8)    | 3.538  |              |                             |                             |
|             | i (8)    | 0.918  |              |                             |                             |
|             | m (7)    | 1.276  |              |                             |                             |
| 09/02       | e (6)    | 2.853  | 0.88         | 7.2 ± 3.9                  |                             |
|             | i (6)    | 3.187  | 0.39         | 5.2 ± 1.5                  |                             |
|             | m (6)    | 2.655  | 0.51         | 5.8 ± 1.2                  |                             |
| 09/03       | e (12)   | 1.785  |              |                             |                             |
|             | i (12)   | 0.934  |              |                             |                             |
|             | m (12)   | 1.136  |              |                             |                             |
| 09/05       | e (16)   | 3.349  | 1.12         | 3.5 ± 1.0                  |                             |
|             | i (16)   | 1.779  | 1.07         | 4.0 ± 0.3                  |                             |
|             | m (16)   | 4.008  | 0.91         | 3.0 ± 0.3                  |                             |
| 09/06       | e (11)   | 1.325  |              |                             |                             |
|             | i (11)   | 1.556  |              |                             |                             |
|             | m (11)   | 1.831  |              |                             |                             |
| 09/07       | e (20)   | 1.687  |              |                             |                             |
|             | i (20)   | 1.440  |              |                             |                             |
|             | m (20)   | 2.859  |              |                             |                             |
| 09/08       | e (24)   | 3.343  | 1.21         | 10.2 ± 2.0                 | −1.9 ± 0.6                  |
|             | i (24)   | 2.285  | 1.19         | 9.2 ± 0.7                  | −1.7 ± 0.2                  |
|             | m (24)   | 4.105  | 0.87         | 6.9 ± 0.7                  | −1.9 ± 0.3                  |
| 09/09       | e (9)    | 3.929  |              |                             |                             |
|             | i (13)   | 1.760  |              |                             |                             |
|             | m (13)   | 1.016  |              |                             |                             |
| 09/13       | e (14)   | 5.487  | 0.76         | −5.3 ± 1.2                 |                             |
|             | i (14)   | 5.605  | 0.85         | −7.7 ± 0.6                 |                             |
|             | m (14)   | 5.069  | 0.67         | −4.8 ± 0.7                 |                             |
| 09/14       | e (13)   | 2.712  | 1.00         | 5.9 ± 1.2                  |                             |
|             | i (13)   | 2.874  | 0.87         | 5.8 ± 0.4                  |                             |
|             | m (13)   | 3.047  | 0.73         | 3.6 ± 0.5                  |                             |
| 09/24       | e (17)   | 2.349  |              |                             |                             |
|             | i (17)   | 1.450  |              |                             |                             |
|             | m (17)   | 2.063  |              |                             |                             |
| 09/25       | e (8)    | 2.338  |              |                             |                             |
|             | i (8)    | 1.029  |              |                             |                             |
|             | m (8)    | 1.474  |              |                             |                             |
| 09/26       | e (8)    | 1.964  | 0.88         | 3.5 ± 2.7                  |                             |
|             | i (8)    | 5.477  | 1.15         | 6.2 ± 0.6                  |                             |
|             | m (8)    | 2.800  | 0.53         | 2.9 ± 0.7                  |                             |
| 10/17       | e (10)   | 1.384  |              |                             |                             |
|             | i (10)   | 1.332  |              |                             |                             |
|             | m (10)   | 1.624  |              |                             |                             |
| 10/18       | e (24)   | 3.306  | 1.41         | 2.8 ± 0.4                  |                             |
|             | i (24)   | 3.932  | 0.83         | 1.8 ± 0.1                  |                             |
|             | m (24)   | 2.992  | 0.93         | 1.9 ± 0.1                  |                             |
| 11/18       | e (17)   | 4.507  | 1.59         | 11.2 ± 1.8                 | −12.1 ± 3.8                 |
|             | i (17)   | 3.481  | 1.47         | 7.1 ± 0.4                  | −8.8 ± 1.3                 |
|             | m (17)   | 5.289  | 1.28         | 6.3 ± 0.5                  | −8.5 ± 1.0                 |

Based on our high temporal resolution observations, the spectral variability with the brightness was investigated in this section. The colour index $e - m$, which was calculated by coupling the BATC $e$ and $m$ magnitudes taken within 20 min, was adopted to denote the optical spectral slope. We took $(e + m)/2$ to denote the brightness of the source. In our analysis, the contribution of the host galaxy was not subtracted from the total flux densities. But the results are not strongly affected by the host galaxy, since it has colours similar to the AGN. Figs 4(a)–(c) display the relationship between colour index and brightness on three ‘variable nights’. Only the most densely observed three nights were plotted as examples; similar results can be obtained from the data on other ‘variable nights’. Solid lines are the best fits to the data points. $b$ is the fitted slope followed by its error. Fig. 4(d) gave the relationship between the obtained 258 colour indices and their brightness during our monitoring. One can obviously see that the values of $b$ for intranight points were larger than that in Fig. 4(d). It suggests that the spectral variability of the intranight fast flares and internight variability may be different. To decompose the intranight variation from the internight variation, we used the faintest magnitudes in bands $e$ and $m$ on each observation night to indicate the internight long-term variation. Then the intranight variations were obtained by subtracting the magnitudes from the maximum for each night. The relationships between the colour index and the brightness were drawn in Figs 4(e) and (f) for the internight variations and the intranight fast flares, respectively. The linear correlations are all significant at a 0.95 confidence level, while the slope of fast flares (0.674 ± 0.059) is larger than that of internight variations (0.137 ± 0.024). So the spectral variability reveals that the variability has ‘strongly chromatic’ intranight fast flares and ‘mildly chromatic’ internight variations. Our result is consistent with that of Villata et al. (2004a). The slopes in this work are larger than the slopes by Villata et al. (2004a), since the considered frequency separation in this work is larger than that in Villata et al. (2004a).

4 SUMMARY

We monitored BL Lac with a high temporal resolution with BATC telescope during the period from 2005 July 5 to November 18. Many fast variations superposed on the long-term trend were recorded. The rising phase of the second flare lasted at least 44 d. During this rising process, the variability amplitudes are 1.374, 1.252 and 1.174 mag in bands $e$, $i$ and $m$, respectively. 799 optical multiband observations and 258 colour indices were obtained. By analysing the INOV, we conclude that for the intranight variability, the amplitude of variability is larger at the shorter wavelength, the variation rate is also larger at shorter wavelength and it is comparable in the rising and decaying phases within each band. An average time-lag between bands $e$ and $m$ was obtained by the method of ZDCF. It must be
Figure 3. ZDCFs of the light curves in bands $e$ and $m$ on six variable nights. Dashed lines show the maximum of the ZDCFs. Solid lines are the Gaussian fit lines.

Table 6. The time-lags between bands $e$ and $m$.

| Date   | Maximum | $\tau_p$ (h) | $\tau_c$ (h) | $\tau_g$ (h) |
|--------|---------|--------------|--------------|--------------|
| 09/08  | 0.724   | $0.142^{+0.001}_{-0.001}$ | $0.236^{+0.136}_{-0.091}$ | $0.276 \pm 0.082$ |
| 10/18  | 0.736   | $0.146^{+0.002}_{-0.001}$ | $0.156^{+0.064}_{-0.081}$ | $0.225 \pm 0.337$ |
| 11/18  | 0.770   | $0.312^{+0.287}_{-0.168}$ | $0.147^{+0.164}_{-0.167}$ | $0.107 \pm 0.095$ |

The jet is powered and accelerated by a supermassive black hole surrounded by an accretion disc (e.g. Ghisellini et al. 1998). Although the details are still under debate, this scenario can well explain most of the observation properties of BL Lacs (see e.g. Böttcher & Bloom 2000). The combination of ‘strongly chromatic’ intranight variability and ‘mildly chromatic’ internight variability is possible induced by both intrinsic mechanisms and geometrical effects. The ‘mildly chromatic’ component can be interpreted by the variation of Doppler factor on a spectrum slightly deviating from a power law (Villata et al. 2004a). The direction of the jet varies as the knots move relativistically on helical trajectories within a small angle with respect to the observer. The internight variations can be introduced by the variation of the direction of jet adding the spectrum slightly deviating from the power law. The ‘strongly chromatic’ component can be explained by particle acceleration and propagation by shock-in-jet events (e.g. Mastichiadis & Kirk 2002). The particles are accelerated by the shocks advancing down the jet, the optical synchrotron emission is enhanced due to the accelerated particles and the overdense magnetic field. This kind of shock-in-jet model will lead to a bluer-when-brighter phenomenon (Marscher & Travis 1996), which is the same as the spectral variability in this paper. The intranight component can also be explained by a simple model representing the variability of a synchrotron component (Vagnetti, 2002, 2003).
Figure 4. The relationship between colour index ($e - m$) and source brightness ($\frac{e + m}{2}$). Solid lines are the best fits to the data points. The fitted slope followed by its error is indicated with $b$, $r$ indicates the linear Pearson correlation coefficient of the best fit, and $P$ is the probability of $r = 0$. Panels (a), (b) and (c) – intranight data on 2005 November 18, September 8 and October 18, respectively; panel (d) – all data; panel (e) – internight component; panel (f) – intranight component.

Trevese & Nesci 2003). So the variability of BL Lac may be the results of both intrinsic mechanisms and geometric effects.

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