Prediction of Dynamic Responses of Flow-Induced Vibration Using Deep Learning

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Abstract: Flow-induced vibration (FIV) is a phenomenon in which the flow passing through a structure exerts periodic forces on the structure. Most studies on FIV focus on suppressing this phenomenon. However, the Marine Renewable Energy Laboratory (MRELab) at the University of Michigan, USA, has developed a technology called the vortex-induced vibration for aquatic clean energy (VIVACE) converters that reinforces FIV and converts the energy in tidal currents to electrical energy. This study introduces the experimental data of the VIVACE converter and the associated method using deep neural networks (DNNs) to predict the dynamic responses of the converter. The DNN was trained and verified with experimental data from the MRELab, and the findings show that the amplitudes and frequencies of a single cylinder in the FIV predicted by the DNN under various test conditions were in good agreement with the experimental data. Finally, based on both the predicted and experimental data, the optimal power envelope of the VIVACE converter was generated as a function of the flow speed. The predictions using DNNs are expected to be more accurate as they can be trained with more experimental data in the future and will help to substantially reduce the number of experiments on FIVs.

Keywords: deep learning; flow-induced vibration (FIV); renewable energy; dynamic response

1. Introduction

Interest in marine renewable energy has gradually been increasing worldwide, and various marine technologies have been developed for commercialization of the energy generated thereof. With more than 70% of the Earth’s surface covered by water, significant amounts of potential energy are stored in storm surges, sea waves, and resources in the form of heat and salts in the ocean. However, most marine renewable energy technologies have not yet been commercialized because of their low efficiencies and high cost of power generation compared to conventional fossil fuels. Recently, marine power generation technologies have been developed specifically for commercialization [1]. The vortex-induced vibration for aquatic clean energy (VIVACE) converter, a marine renewable energy technology, converts the hydrokinetic energy in water to electrical energy [2]. The VIVACE converter was invented and patented by the Marine Renewable Energy Laboratory (MRELab) at the University of Michigan and was developed based on the simple idea of maintaining and enhancing vortex-induced vibrations (VIVs) while maximizing flow-induced vibration (FIV), rather than suppressing them. Several lab-scale converters have been built and tested in the low-turbulence free surface water (LTFSW) channel at the MRELab since 2005 [2]. The research team has been investigating methods to improve the power output of the converter by enhancing the FIVs of multiple cylinders over a wide range of flow speeds. For this study, the MRELab provided the experimental data of a
single-cylinder converter to train our deep neural network (DNN) to predict the dynamic responses and power outputs of the converter.

FIVs are caused in various structures, such as bridges, buildings, and offshore structures resulting from fluid flows. One of the most common types of FIVs is the VIV, which was first observed by Leonardo da Vinci in 1504 [3].

VIV is generally caused by alternate vortex shedding on both sides of the cylinder like Figure 1, which causes periodic lift forces to act on the cylinder. Galloping is another type of FIV that has a lower frequency and a larger amplitude compared to VIV and is caused by the asymmetric motions of the shear layers. Galloping is a more powerful phenomenon than VIV and can occur for a cylinder with noncircular cross sections above a certain critical flow speed. The amplitude of the galloping continues to increase with the flow velocity until the structure is destroyed. In general, as the flow velocity increases, VIVs occur first, followed by galloping. Because of the destructive nature of FIVs in structures, most researchers have focused on its suppression. In 2006, however, the MRELab research team developed the VIVACE converter, where the kinetic energy of the fluid could be converted to electrical energy by enhancing and controlling the FIVs [4–6].

This study is concerned with predicting the amplitude and frequency of a single cylinder installed in the VIVACE converter by learning the FIV experiment data through a deep learning model. The study was conducted using experimental data provided by MRELab. When a neural network learns the test data and a deep learning model is constructed to predict the dynamic responses of FIVs for different conditions without learning, the results can be confirmed within a relatively short time. In addition, learning the experimental data under various conditions can be an alternative to statistical methods, such as regression analysis [7].

Therefore, in recent research, studies have been actively conducted on the system to predict data measured via experiments or with sensors by learning the deep learning model. Deep learning can be used not only for interpretation of incomplete and noisy input data but also for pattern recognition, classification, generalization, and abstraction while learning of large amounts of data [8]. In addition, the prediction model through data-based learning is highly applicable as it learns and builds the model relationships with key input and output variables compared to performance predictions using the traditional dynamic simulation tools [9].

To train the different conditions and variables used in the experiment, data preprocessing steps, such as data regularization, were performed, and a deep learning model was constructed. To predict the amplitude and frequency of the cylinder as the output value, optimization was performed by adjusting the hyperparameters of the deep learning model. Using the deep learning model prediction responses of FIVs, we can reduce the number of experiments substantially and produce the optimal power envelope of the VIVACE converter more efficiently. The concepts and techniques of VIVACE using FIVs used in this study are described in Section 2. Section 3 describes data preprocessing and training in the development of deep learning models to predict the dynamic response of
FIVs. Section 4 decides on a new optical power envelope by verifying the dynamic response results of FIVs using the deep learning model and predicting untested data.

2. Power Generation Technology of VIVACE Converter Using FIVs

Contrary to previous efforts to suppress FIVs, which can destroy structures subject to fluid flows, the VIVACE converter utilizes and even enhances FIVs to harness the power from rivers and currents. The first prototype of the converter was developed at the end of 2003 and tested at MRELabs in 2004. The left side of Figure 2 shows the schematic of the simplest unit of the VIVACE converter, comprising a single circular cylinder suspended by springs and a power take-off system. On the right side of Figure 2, four of the units installed on the LTFSW channel at the MRELabs are shown [10].

The experiments were conducted in the flow range of $30,000 < Re < 120,000$ for the Reynolds number ($Re$) to harness the optimal power envelopes at various flow velocities [12]. The Reynolds number is defined by:

$$Re = \frac{U D}{\nu}$$

where $U$, $D$, and $\nu$ are the free stream velocity, the diameter of a circular cylinder, and the kinematic viscosity of fresh water, respectively.

All tests with the single cylinder with passive turbulence control (PTC) presented herein were performed in the LTFSW channel of the MRELabs. The measured turbulence intensity of the test section normalized by the free stream velocity was reported lower than 0.1% [1,4,6,10] and it is suitable for the experiments [13]. A virtual spring-damping (Vck) system, a servo-motor controller that replaces physical damping and springs were designed and built to investigate the effects of damping and spring stiffness on power generation [11]. A schematic of the design model is shown in Figure 3.

![Diagram of VIVACE module with coordinate system](image)

**Figure 2.** (Left) Simple schematic of the VIVACE module with coordinate system; (Right) four new VIVACE converters mounted on the LTFSW channel [10,11].
The first VIVACE converter was intended to utilize only VIV, as implied by the name. Because of the self-limiting characteristics of the VIV phenomenon, the harness power of the single-cylinder VIVACE converter is limited by its lock-in range and the self-limiting VIV characteristics. However, previous works on FIVs in circular cylinders have shown that fluid dynamic changes caused by attachments to the cylinders can cause galloping in circular cylinders [14]. In contrast to VIV, galloping is a vibration type with a short period compared to its high amplitude in a single degree of freedom and generally occurs in noncircular cross sections. Galloping is caused by motion-aiding forces, resulting in very high amplitude motions with the total system damping falling below zero and induction of negative aero/hydrodynamic damping. To overcome the shortcomings of VIV and initiate galloping, the MRELab team extensively investigated the effects of passive turbulence control (PTC), which is applied in the form of roughness strips attached to the cylinders [10,12,15]. This study shows that the selectively applied roughness on the cylinder surface can cause significant changes in the properties of the boundary or shear layers; accordingly, the cylinder responses may change. For some PTC positions, as shown in Figure 4, the PTC extends the upper VIV branch point to the reduced velocity \( U^* \approx 11 \) and increases fully from \( U^* = 12 \). The reduced velocity is defined by:

\[
U^* = \frac{U}{f_{nw}D}
\]
Figure 4. Flow induced motions (FIM) zone nomenclature for a circular cylinder with PTC [1].

The natural frequency of the system including added mass is defined by:

$$f_{nw} = \sqrt{\frac{K}{m_{osc} + m_{add}}}$$

where $K$, $m_{osc}$, and $m_{add}$ are the spring stiffness, oscillating mass, and added mass, respectively.

The transition range in which both VIV and galloping mechanisms coexist is $11 < U^* < 12$. Therefore, the synchronization region of FIVs, which covers both the alternately occurring VIV and galloping, increases rapidly. Thus, the VIVACE converter was able to harness higher quantities of power at over a wide range of speeds from 0.38 m/s to 1.45 m/s and maximum speed of the LTFSW channel. An optimal harnessed power curve is created by superimposing the results of the harnessed power calculated from different combinations of the damping and spring stiffness values, as shown in Figure 5.

Figure 5. Optimal harnessed power envelope of VIVACE converter with and without PTC [14].
The optimal harnessed power of a cylinder with PTC is larger than that of a smooth cylinder in the synchronization region of VIV. Further, when the flow velocity exceeds 1.2 m/s, the harnessed power curve increases sharply, reaching 49.35 W at a flow velocity of 1.45 m/s for $K = 2000$ N/m and $\zeta_{\text{harness}} = 0.16$; however, the smooth cylinder is asynchronous and can no longer supply power. The power calculated at 1.45 m/s is more than three times the maximum harnessed power of the smooth cylinder.

3. Deep Learning Model for Dynamic Response Prediction of FIVs

3.1. FIV Tested Data for Learning

Experiments were performed with the learning data using the second-generation Vck system developed by MRELab. Figure 6 shows the single-cylinder converter mounted in the LTFSW channel.

Figure 6. Schematic of the LTFSW channel and single cylinder converter [12].

The Reynolds number in the range of $30,000 < \text{Re} < 120,000$ and the flow velocity in the range of $0.395 \text{ m/s} < U < 1.315 \text{ m/s}$ were the tested data conditions used in this study. When the mass ratio ($m^* = m_{\text{osc}}/m_d$) was 1.343, the spring constant ($K$) was 400, 600, 755, 1000, and 1200 N/m, and the harness damping ratio ($\zeta_{\text{harness}}$) for each spring constant was 0.04, 0.08, 0.12, 0.16, 0.2, and 0.24. Table 1 and Figure 7 show the results for the dynamic responses of a single rigid circular cylinder mounted with PTC [11,12,14]. In addition, the specifications of the single cylinder oscillator model, along with the tested conditions, are summarized in Table 2.
Table 1. PTC parameters (P60).

| Parameter                                      | Value  |
|------------------------------------------------|--------|
| Placement angle \( (\alpha_{PTC}, \text{degree}) \) | 20     |
| Angular coverage of strip \( (\theta, \text{degree}) \) | 16     |
| Sandpaper plus tape thickness \( (P, \text{mm}) \) | 0.587  |
| Average grit height \( (k, \text{mm}) \)            | 0.26   |
| Total thickness of strip \( (T-P+k, \text{mm}) \)   | 0.847  |

![Configuration of passive turbulence control (PTC) on the cylinder](image)

Figure 7. Configuration of passive turbulence control (PTC) on the cylinder [11].

Table 2. Particulars of single-cylinder oscillator model.

| Particular          | Value          |
|---------------------|----------------|
| \( K \) (N/m)       | 400 600 755 1000 1200 |
| Temperature (°C)    | 20.5           |
| \( \mu \) (N·s/m²)  | 1.004 × 10⁻³   |
| \( v \) (m²/s)      | 9.940 × 10⁻⁷   |
| \( \varrho \) (kg/m³) | 999.72965     |
| D (m)               | 0.0889         |
| L (m)               | 0.89535        |
| \( m_{\text{displacement}} \) (kg) | 5.425        |
| \( m_{\text{oscillation}} \) (kg)                     | 7.285775      |
| \( m_{\text{added}} \) (kg)                           | 5.425          |
| \( \zeta_{\text{structure}} \)                         | 0.02           |
| \( f_{\text{water}} \)                                | 0.893 1.093 1.227 1.412 1.546 |

Through testing under the above conditions, the parameters to train the tested data of the single-cylinder amplitude and natural frequency of the system for the deep learning
model were first extracted. A total of six parameters were extracted, as follows: spring constant $K$, harness damping ratio of the system $\zeta_{\text{harness}}$, number of rotations of the induction generator to circulate the water in the LTFSW channel $f_{\text{motor}}$, natural frequency of the cylinder in water, $f_{n,\text{water}}$, reduced velocity $U^*$, and finally the Reynolds number $Re$. Correlation analysis was then performed to identify the effects of the extracted parameters on the dependent variables, amplitude (A/D), and frequency ($f_{\text{cyl}}$) of the cylinder. The correlation coefficient was calculated using the Pearson method in this study, which is a parametric correlation coefficient, as shown in Table 3.

**Table 3.** Correlation analysis for selecting the independent variables (N = 714).

|       | K    | $\zeta_{\text{harness}}$ | $f_{\text{motor}}$ | $f_{n,\text{water}}$ | $U^*$  | Re   | A/D | $f_{\text{cyl}}$ |
|-------|------|--------------------------|------------------|---------------------|--------|------|-----|-----------------|
| K     | 1.000|                          |                  |                     |        |      |     |                 |
| $\zeta_{\text{harness}}$ | 0.000 | 1.000                    |                  |                     |        |      |     |                 |
| $f_{\text{motor}}$ | 0.030 | 0.000                    | 1.000            |                     |        |      |     |                 |
| $f_{n,\text{water}}$ | 0.997 | 0.000                    | 0.030            | 1.000               |        |      |     |                 |
| $U^*$ | −0.500 | 0.000                   | 0.825            | −0.508              | 1.000  |      |     |                 |
| Re    | 0.030 | 0.000                    | 1.000            | 0.030               | 0.825  | 1.000|     |                 |
| A/D   | −0.244 | −0.334                 | 0.707            | −0.246              | 0.755  | 0.707| 1.000|                 |
| $f_{\text{cyl}}$ | 0.261 | −0.177                   | 0.277            | 0.260               | 0.065  | 0.277| 0.473| 1.000          |

Equation (1) shows the expression used to calculate the correlation coefficient of the Pearson method.

$$\text{Pearson Coefficient}(r) = \frac{n \sum X_i Y_i - \sum X_i \sum Y_i}{\sqrt{n \sum X_i^2 - \left(\sum X_i\right)^2} \sqrt{n \sum Y_i^2 - \left(\sum Y_i\right)^2}}$$

where $X = \text{Independent variable}$

$Y = \text{Dependent variables}$

$n = \text{Number of specimens}$

The four input values of the deep learning model selected through correlation analysis were: $K$, $\zeta_{\text{harness}}$, $U^*$, and $Re$. The variables $U^*$ and $Re$ were selected, which have large positive linear relationships with the amplitude of the cylinder. The variable $K$ was added as it had a relatively large correlation, and there were no other variables that correlated with the frequency compared to the amplitude of the cylinder. Finally, by adding $\zeta_{\text{harness}}$ with a negative correlation coefficient to the amplitude and frequency of the cylinder, the four selected input parameters are obtained. For the output parameters, the amplitude ratio A/D of the cylinder in FIVs and the cylinder frequency, $f_{\text{cyl}}$, at the nodes of the output layer, respectively, were predicted.

We constructed a dataset of 667 cases by VIVACE converter results and a untested dataset of 647 cases. Most of the tested data of the VIVACE converter was used as Training data, and some as test data to verify the general performance of the trained model. After verifying the general performance of the trained network, we input the untested data to predict the amplitude and frequency of the cylinder. The contents of the data classification are summarized in Table 4.
Table 4. Data classification for learning in deep learning models.

| Spring Constants (K) | ζharness for Training (No. of Training Data) | ζharness for Test (No. of Test Data) | Number of Total Data |
|----------------------|--------------------------------------------|------------------------------------|---------------------|
| 400                  | 0.04, 0.08, 0.12, 0.16, 0.2, 0.24 (150)     | -                                  | 150                 |
| 600                  | 0.04, 0.08, 0.12, 0.2, 0.24 (120)          | 0.16 (24)                         | 144                 |
| Tested data by VI-    |                                            |                                    |                     |
| 755                  | 0.04, 0.08, 0.12, 0.16, 0.2, 0.24 (138)    | -                                  | 138                 |
| 1000                 | 0.04, 0.08, 0.12, 0.2, 0.24 (115)          | 0.16 (23)                         | 138                 |
| 1200                 | 0.04, 0.08, 0.12, 0.16, 0.2, 0.24 (144)    | -                                  | 144                 |
| Untested data        |                                            |                                    |                     |
| 500                  | -                                          | 0.04, 0.08, 0.12, 0.16, 0.2, 0.24 (150) | 150                 |
| 700                  | -                                          | 0.04, 0.08, 0.12, 0.16, 0.2, 0.24 (150) | 150                 |
| 900                  | -                                          | 0.04, 0.08, 0.12, 0.16, 0.2, 0.24 (150) | 150                 |
| 1100                 | -                                          | 0.04, 0.08, 0.12, 0.16, 0.2, 0.24 (150) | 150                 |
| Total data           | 667                                         | 647                                | 1314                |

3.2. Deep Learning Model Structure

The structure of the neural network is composed of an input layer, a hidden layer, and an output layer. Here, the input layer receives the external inputs, and the hidden layer is located between the input and output layers and invisible to the outside. The output layer provides the results processed by the last hidden layer [8,9,16].

In this study, the neural network shown in Figure 8 is constructed. A fully connected neural network structure consisting of one input layer, one output layer, and five hidden layers is used. The number of hidden layers and the nodes in the hidden layers were trained for the specifications shown in Table 5, and the number of hidden layers and nodes with the lowest average error rate of the test data were selected.

![Figure 8. Structure of the deep neural network used in this study.](image)
Table 5. Learning condition.

| Learning Condition | Range                          |
|-------------------|-------------------------------|
| Hidden layers     | 3, 5, 7, 9                    |
| Nodes             | Minimum of 48 to Maximum of 468 |
| Batch sizes       | 256, 512, 1024                |
| Learning rates    | 0.1, 0.01, 0.001              |
| Epochs            | 10,000–50,000                |

For the input values of the deep learning model, four values were extracted through correlation analysis and entered. The output values predict the amplitude A/D and cylinder frequency $f_{cyl}$ for the FIVs of the cylinder at the node of the output layer. The number of nodes for each hidden layer is set to $80 \times 64 \times 48 \times 32 \times 16$. Finally, before learning the classified data, the input values were normalized to uniformly match the input values between 0 and 1 for all results [17], as expressed by Equation (2).

$$
\bar{d} = \frac{d - \min v}{\max v - \min v}
$$

where $\bar{d} = \text{Normalized data}$

$d = \text{Data before normalize}$

$\min v = \text{Minimum value of the feature}$

$\max v = \text{Maximum value of the feature}$

3.3. Deep Learning Model Training

In this study, cross-validation was used to learn the overall characteristics of the experimental data and increase the reliability of the generalization performances of the deep learning models. There are various cross-validation methods available; however, the repeated random subsampling validation method, using which the ratio between the training and validation sets is adjusted and not affected by the number of training data, is employed as shown in Figure 9.

![Figure 9. Random subsampling validation method to reduce bias in the learning data by randomly extracting validation data for each iteration, thereby preventing underfitting and overfitting.](image)

The goal of the deep learning model optimization is to determine the values of the hyperparameters such that the learning of the neural network models and value of the loss function according to their results are minimized. Therefore, fine tuning was performed by controlling the number of nodes per hidden layer. The optimal number of nodes was selected by repeating the increase and decrease in the number of nodes. In
addition, the hyperparameters, such as learning rate, iteration, and batch size, that affect the neural network were adjusted.

Then, the functions for learning the deep learning model were selected. The activation function converts the sum of the input signals into output signals, such as the step function used in perceptrons. At the nodes of the hidden layers, the sum of the linear product of the data and its weight are calculated, and the threshold is applied to obtain the activation level [18]. In this study, the rectified linear unit (ReLU) activation function was used [19,20]. Compared to the sigmoid function, which has been majorly used in the past, the ReLU can be implemented with a simple formula, and the function also resolves the vanishing gradient problem, which was considered as a chronic problem in the deep learning model [21]. The function is expressed as a graph in Figure 10 and as an equation in Equation (3).

\[
f = \begin{cases} 
  0 & x < 0 \\
  x & x \geq 0
\end{cases}
\]  

(3)

Figure 10. Schematic of the ReLU function.

The optimization function accelerates the learning of the deep learning models and uses the Adam optimizer, which is efficient in terms of computational resources. The cost function uses the root mean square error (RMSE), and the He initialization is used for the weight initialization method. The He initialization method is to initialize the ReLU function and considers the characteristics of the input and output values rather than random initialization [22]. In this study, the He initialization method was used, as shown in Equation (4). The initialization for the ReLU activation function considers the characteristics of the input and output values, rather than random initialization. Depending on the characteristics of the data, when there were \( n \) nodes in the previous layer, a normal distribution with a square root of \( 2/n \) is used. This method was able to significantly increase the learning speed of the neural network, and it was confirmed that the loss function was reduced early in the learning process.

He Normal Initialization \( W \sim N\left(0, \text{Var}(W)\right) \)

\[
N = \text{Normal distribution} \\
W = \text{Weight between nodes} \\
\text{Var}(W) = \sqrt{\frac{2}{n_{in} + n_{out}}} \\
n_{in} = \text{Number of nodes in the previous layer} \\
n_{out} = \text{Number of nodes in the next layer}
\]

(4)

Learning was performed based on a batch size of 300. The learning rate determines the value of the weight that the neural network updates after learning. The deep learning model checks the RMSE every 1000 learnings and adjusts the learning rate and number of learning steps until the cost function is minimized. In the selection of the number of hidden layers, the greater the depth of the neural network hidden layer, the lower is the cost.
function. However, when the depth increased above a certain level, the cost function could not converge and showed divergence. In this study, the best-learned cost function with five hidden layers is shown in Figure 11, and the average error rate for each data structure of the neural network that completed learning is presented in Table 6.

![Loss (RMSE) function per epoch.](image)

**Figure 11.** Loss (RMSE) function per epoch.

**Table 6.** Average error rate by data in a learned neural network.

| Output | Error (%) | Train Average Error | Validation Average Error | Test Average Error * |
|--------|-----------|---------------------|--------------------------|---------------------|
| A/D    | 6.35      | 13.05               | 15.96                    |                     |
| fcyl   | 3.12      | 8.47                | 11.29                    |                     |

* Only include Tested data by VIVACE converter.

### 4. Deep Learning Model Prediction

#### 4.1. Prediction Results of Data Tested Through VIVACE Converter

In this study, test data were applied to a deep learning model constructed using neural network learning to predict the dynamic responses of FIVs via deep learning. First, we investigated the results when $\zeta_{\text{harness}} = 0.16$ at $K = 600$ and 1000 N/m extracted from the experimental data. It was confirmed that the predicted results of the test data applied to the learned neural network followed the trends of the VIV and galloping phenomena throughout the experiment. Figures 12 and 13 below show the predicted results of cylinder amplitude and frequency of the test data extracted from the experimental data. The error rate was predicted to be within 5% compared with the actual experimental data. However, relatively large errors occurred in the initial section, where the VIV phenomenon started occurring, and the transition section from the VIV to the galloping section.
Figure 12. Cylinder amplitude (left) and frequency (right) with the real/predicted values for $\zeta_{\text{harness}} = 0.16; K = 600 \, \text{N/m}$.

Figure 13. Cylinder amplitude (left) and frequency (right) with the real/predicted values for $\zeta_{\text{harness}} = 0.16; K = 1000 \, \text{N/m}$.

Next, the power curve obtained by the VIVACE converter was calculated using the predicted results of the amplitude and frequency of the cylinder. The equation used in the calculation is the actual equation used for the experiment with the VIVACE converter and is represented by Equation (5). Figure 14 shows the power curve of the VIVACE converter, which is calculated using the amplitude and frequency of the cylinder.

\[
\text{Power}_{\text{harness}}(W) = 4\pi^2 \zeta_{\text{harness}} \sqrt{\frac{K}{m_{\text{osc}}}} \left(\frac{D}{A} \cdot f_{\text{cyl}}\right)^2
\]

\[\zeta_{\text{harness}} = \text{Harness damping ratio}\]

\[K = \text{Spring constant}\]

\[m_{\text{osc}} = \text{mass of oscillation}\]

\[D = \text{Cylinder diameter}\]

\[A = \text{Amplitude of cylinder}\]

\[f_{\text{cyl}} = \text{Frequency of cylinder}\]
4.2. Prediction Results of Untested Data

In this study, we confirmed the validity of the power curves through experiments with the VIVACE converter and the above predicted results. Therefore, the amplitude and frequency of the cylinder were predicted for each input data $\zeta_{\text{harness}}$ in the learned neural network model in the range of $K = 500, 700, 900,$ and $1100 \text{ N/m}$, which are in the untested range. Figure 15 shows the power curves, using which the optimal power envelope with the maximum power for each $Re$ according to the flow velocity is shown in Figure 16. The optimal power envelope is a curve expressed to obtain the highest power generation and high efficiency by the $Re$, by considering the effects of the mass ratio, spring stiffness, and harness damping ratio. The combination curve is created by combining the experimental and predicted curves. By comparing the predicted optimal power curve using the deep learning model and optimal power curve prepared via the previous experiments, new $K$ and $\zeta_{\text{harness}}$ values with optimal power were obtained when $m^*$ was 1.343.
Figure 16. Optimal power envelope for the predicted, experimental, and combination curves.

Table 7 lists the optimal power curve values that combine the experimental results of the VIVACE converter with those predicted through deep learning.

### Table 7. Parameters for optimal harness and converted power curve for combination power.

| Re    | K (N/m) | $\zeta_{\text{harness}}$ | Power (W) |
|-------|---------|-------------------------|------------|
| 35,292| 400     | 0.12                    | 0.7        |
| 38,869| 400     | 0.12                    | 1.0        |
| 42,447| 600     | 0.16                    | 1.5        |
| 46,024| 600     | 0.2                     | 3.0        |
| 49,602| 700     | 0.24                    | 4.3        |
| 53,179| 700     | 0.24                    | 5.3        |
| 56,756| 900     | 0.24                    | 7.0        |
| 60,334| 900     | 0.24                    | 8.4        |
| 63,911| 1000    | 0.24                    | 9.3        |
| 67,489| 1200    | 0.24                    | 9.2        |
| 71,066| 1200    | 0.2                     | 8.4        |
| 74,644| 1200    | 0.12                    | 4.9        |
| 78,221| 1200    | 0.08                    | 4.2        |
| 80,010| 1200    | 0.08                    | 3.5        |
| 81,799| 1200    | 0.12                    | 5.6        |
| 85,376| 1200    | 0.12                    | 6.8        |
| 88,954| 1200    | 0.16                    | 7.9        |
| 92,531| 1200    | 0.16                    | 8.5        |
| 96,109| 1200    | 0.16                    | 9.0        |
| 99,686| 1200    | 0.2                     | 9.9        |
| 103,264| 700   | 0.24                    | 10.7       |
| 106,841| 700   | 0.24                    | 11.6       |
| 110,418| 700   | 0.24                    | 12.5       |
| 113,996| 1200  | 0.2                     | 14.2       |
| 117,573| 1200  | 0.2                     | 16.8       |
5. Conclusions

This study involved the development of a deep learning model that can predict the cylinder amplitudes and frequencies by training the FIV experimental data from the MRELab team with a neural network. Using four input values for deep learning model training, we performed data preprocessing, and the cylinder amplitudes and frequencies were predicted as output values. The experimental data obtained through the VIVACE converter was used as training data, with some used as test data to verify the generalization performance of the learned neural network. After validating the generalization performance of the network, the untested data were input to predict the cylinder amplitudes and frequencies of the VIVACE converter. The optimal power curves were calculated from the cylinder dynamic responses predicted by the deep learning model, and the results were compared with the experimental results. In conclusion, a new optimal harnessed power curve was created by combining the experimental results of the VIVACE converter and the predicted results through deep learning. The findings of the experimental study are thus summarized as follows:

1. The deep learning model was trained to predict the dynamic response of the cylinder amplitude and frequency. When compared with the actual experimental results, an average error rate of approximately 10% was observed for the mean values of the cylinder amplitude and frequency.

2. The optimal power curve was calculated using the amplitude and frequency of the cylinder predicted by deep learning. It was further verified by comparing with the actual experimental results, and the new optimal power envelope was created by the predicted dynamic response of the cylinder.

3. A new optimal harness power curve was created to obtain the maximum power according to the flow velocity when \( m^* = 1.343 \), compared with the optimal power envelope calculated through the experiment.

4. A part of the experimental conditions was classified into test data and predictions were obtained using the deep learning model. The results confirmed the possibility of identifying the dynamic responses of the cylinder under the conditions experimented before the VIVACE converter experiment.

Based on the above results, the deep learning model adequately predicted the experimental results of the dynamic response of the cylinder in the VIVACE converter, but the error rate was rather large in the region where the initial VIV phenomenon occurred or in the transition region. These regions require various experimental data and research conditions because of the complexity of the phenomenon itself, which is difficult to accurately measure even in actual experiments. However, due to the complexity of the phenomenon itself, experimental data and research under various conditions are required to replace the experiment. While this study predicts the dynamic response for a single cylinder, it can be used to predict the dynamic response for each cylinder in an entire system with multiple cylinders. In the future, it is expected that this work will be helpful for the initial stage of experiments by learning the experimental data of the VIVACE converter under various conditions and calculating the optimum power in the early stages of the experiment in advance.

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**References**

1. Kim, E.S. Synergy of Multiple Cylinders in Flow Induced Motion for Hydrokinetic Energy Harnessing. Ph.D. Thesis, University of Michigan, Ann Arbor, MI, USA, 2013.

2. Bernitsas, M.M.; Raghavan, K.; Ben-Simon, Y.; Garcia, E. VIVACE (vortex induced vibration aquatic clean energy): A new concept in generation of clean and renewable energy from fluid flow. *J. Offshore Mech. Arct. Eng.* 2008, 130, 041101.

3. Sun, H.; Kim, E.S.; Bernitsas, M.P.; Bernitsas, M.M. Virtual spring-damping system for flow-induced motion experiments. *J. Offshore Mech. Arct. Eng.* 2015, 137, 061801.

4. Bernitsas, M.M.; Ben-Simon, Y.; Raghavan, K.; Garcia, E. The VIVACE converter: Model tests at high damping and Reynolds number around 105. In Proceedings of the 25th International Conference on Offshore Mechanics and Arctic Engineering, Hamburg, Germany, 4–9 June 2006; ASME: New York, NY, USA, 2008; pp. 639–653.

5. Kim, E.S.; Oh, K.M.; Park, H. Assessment of theoretical annual energy production in the coast of South Korea using tidal current energy converters utilizing flow induced vibration. *J. Energy Eng.* 2019, 28, 65–72.

6. Lee, J.H.; Bernitsas, M.M. High-damping, high-Reynolds VI: Tests for energy harvesting using the VIVACE converter. *Ocean Eng.* 2011, 38, 1697–1712.

7. Cho, Y.I.; Oh, M.J.; Seok, Y.S.; Lee, S.J.; Roh, M.I. Resistance estimation of a ship in the initial hull design using deep learning. *Korean J. Comput. Des. Eng.* 2019, 24, 203–210.

8. Shin, S.; Bae, J.; Kim, H.; Kim, S.; Kim, S.; Lee, J. Estimation of environmental costs based on size of oil tanker involved in accident using neural network. *J. Ocean Eng. Technol.* 2012, 26, 60–63.

9. Seong, N.; Choi, K.; Choi, W. Development and evaluation of predictive model for fan air flow velocity according to artificial neural network input variables. *J. Korean Inst. Archit. Sustain. Environ. Build. Syst.* 2019, 13, 191–202.

10. Kim, E.S.; Bernitsas, M.M.; Kumar, R.A. Multicylinder flow-induced motions: Enhancement by passive turbulence control at 28,000< Re= 120,000. *J. Offshore Mech. Arct. Eng.* 2013, 135, 021802.

11. Kim, E.S.; Bernitsas, M.M. Performance prediction of horizontal hydrokinetic energy converter using multiple-cylinder synergy in flow induced motion. *Appl. Energy* 2016, 170, 92–100.

12. Sun, H.; Kim, E.S.; Nowakowski, G.; Mauer, E.; Bernitsas, M.M. Effect of mass-ratio, damping, and stiffness on optimal hydrokinetic energy conversion of a single, rough cylinder in flow induced motions. *Renew. Energy* 2016, 99, 936–959.

13. Walker, D.T.; Lyzenga, D.R.; Ericson, E.A.; Lund, D.E. Radar backscatter and surface roughness measurements for stationary breaking waves. *Proc. R. Soc. Math. Phys. Eng. Sci. Ser. A* 1996, 452, 1953–1984.

14. Kim, E.S.; Sun, H.; Park, H.; Shin, S.; Chae, E.J.; Ouderkerk, R.; Bernitsas, M.M. Development of an alternating lift converter utilizing flow-induced oscillations to harness horizontal hydrokinetic energy. *Renew. Energy Sustain. Energy Rev.* 2021, 145, 111094.

15. Park, H.; Kim, E.S.; Bernitsas, M.M. Sensitivity to zone covering of the map of passive turbulence control to flow-induced motions for a circular cylinder at 30,000 < Re < 120,000. *J. Offshore Mech. Arct. Eng.* 2017, 139, 021802.

16. Park, E.T.; Lee, Y.H.; Kim, J.; Kang, B.S.; Song, W.J. Numerical prediction of temperature-dependent flow stress on fiber metal laminate using artificial neural network. *Trans. Mater. Process.* 2018, 27, 227–235.

17. Oh, S.; Lim, C.; Park, B.; Lee, J.; Shin, S. Deep neural networks for maximum stress prediction in piping design. *Int. J. Fuzzy Logic Intell. Syst.* 2019, 19, 140–146.

18. Ahn, S. Deep learning architectures and applications. *J. Intell. Inf. Syst.* 2016, 22, 127–142.

19. Nair, V.; Hinton, G.E. Rectified Linear Units Improve Restricted Boltzmann Machines. In Proceedings of the 27th International Conference on Machine Learning (ICML-10), Haifa, Israel, 21 June 2010; pp. 807–814.

20. Haru, K.; Saito, D.; Shouno, H. Analysis of Function of Rectified Linear Unit Used in Deep Learning. In Proceedings of the 2015 International Joint Conference on Neural Networks (IJCNN), Killarney, Ireland, 12–17 July 2015; pp. 1–8.

21. Lee, J.; Yoo, S.; Shin, S.; Kang, D.; Lee, S.; Lee, J. Fault diagnosis of bearings using machine learning algorithm. *J. Korean Soc. Mar. Eng.* 2019, 43, 455–462.

22. He, K.; Zhang, X.; Ren, S.; Sun, J. Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet classification. In Proceedings of the IEEE International Conference on Computer Vision, Santiago, Chile, 7–13 December 2015; pp. 1026–1034.