Status of some P-wave baryon resonances
and importance of inelastic channels

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Abstract

We analyze the current status of three P-wave baryon states \(N(1710)\frac{1}{2}^+\), \(N(1900)\frac{3}{2}^+\), and \(\Delta(1600)\frac{3}{2}^+\) as given in the Review of Particles Physics (RPP). Since the evidence for a particle's existence is linked to its RPP "star" rating, we discuss its subjective present definition. We also present the accumulating evidence supporting these states and give our new "star" rating recommendations.

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I. INTRODUCTION

In recent years, the field of light-flavor baryon spectroscopy has seen a tremendous increase in experimental activity. High-precision cross section and polarization data are now available, from numerous single and double-meson photoproduction experiments, and these have become the broadest source of information on new baryon states. The bi-annually released Review of Particle Physics (RPP) is the primary source of information relied upon by researchers in the field of baryon physics. The RPP tabulates baryon resonance candidates together with their properties and provides an assessment of their reliability, both overall and separately from pion and photon induced reactions. We have therefore focused our discussion on the ratings provided by this source.

The RPP assigns a star-ratings from one to four stars for baryon resonance candidates. The one and two-star states are rated from poor to fair, whereas the three and four-star states have a rating from likely to certain. These higher-rated states appear in the Baryon Summary Tables without reference to any star rating. The more detailed Particle Listings tabulate overall and reaction-specific star ratings for each resonance. The three P-wave baryon states, \(N(1710)\frac{1}{2}^+\), \(N(1900)\frac{3}{2}^+\), and \(\Delta(1600)\frac{3}{2}^+\), are presently given an overall three-star rating, which prompts the question: Have these states been confirmed or are they merely 'likely' to exist?

It should be mentioned that neither the definition of a star rating nor the ratings themselves have remained static since these states were identified. Many states were downgraded, with some three-star rated states being eliminated, between the 1982 [1] and 1984 [2] editions of the RPP. This upheaval was prompted by disagreements between newer measurements and the older existing data and analyses [3]. In particular, the \(N(1710)\frac{1}{2}^+\) was demoted from a 4-star to a 3-star status, while the \(\Delta(1600)\frac{3}{2}^+\) dropped from a 3-star to a 2-star status. As a result, the \(\Delta(1600)\frac{3}{2}^+\) was dropped from the Baryon Summary Table. Its status was later raised back to three stars [4], having been seen in subsequent analyses [5, 6] of the Virginia Tech and Kent State groups, the uncertainty in its properties preventing a 4-star rating.

Many topics related to the extraction of resonance properties, from the newly accumulated high-precision data, were subjects of discussions at the 2014 ECT* Workshop "Exciting Baryons: Design and Analysis of Complete Experiments for Meson Photoproduction" [7]. The presence of many experts in the field enabled a meeting where the status of prominent 3-star resonances
was discussed, along with possible modifications of the RPP \[8\] star ratings. One fact was unanimously agreed upon: "While most resonances have been discovered by analyzing $\pi N$ elastic scattering data only \[9\] \[11\], measuring other channels, photoproduction in particular, could confirm some questionable states, and possibly discover new ones."

It has recently been emphasized that the extraction of resonance information from $\pi N$ elastic amplitudes requires a detailed knowledge of inelastic channels \[11\] as some structures, such as the $N(1710)$, can be well described either as a pole or a complex branch point, associated with the $\rho N$ channel. With only elastic data, there is no clear way to distinguish between the two mechanisms, and the inelastic channel information is essential to resolve the ambiguity. This fact has only partially been incorporated into the primary analyses of the Karlsruhe-Helsinki (KH) \[12\], Carnegie-Mellon-Berkeley (CMB) \[13\], and George Washington University Data Analysis Center (GW DAC) \[14\], and some uncertainties have remained.

The KH analysis assumed that a nearly-unique set of amplitudes could be found for elastic $\pi N$ scattering if the constraints of isospin invariance and fixed-\(t\) analyticity were applied to a set of data with sufficiently small errors. This claim was supported by a series of mathematical physics studies from Sabba-Stefanescu \[15\]. Information from $NN \rightarrow \pi \pi$ scattering was also used through dispersion relations. The KH resonance parameters were initially extracted through a unitary Breit-Wigner plus background fit to the KH amplitudes. In a later analysis, the speed-plot method was used to determine associated pole parameters. In this way, information concerning inelastic channels was avoided.

The CMB analysis was similarly focused on the determination of a unique set of $\pi N$ elastic scattering amplitudes. Constraints were imposed such that the invariant amplitudes were analytic along 5 crossing symmetric hyperbolas in the Mandelstam plane. The partial wave analysis used constraints from a Regge exchange model in which lower partial waves were allowed to vary, with the higher waves fixed. Once determined, these $\pi N$ partial-wave amplitudes were included in an elaborate multi-channel analysis in order to determine resonance parameters. The formalism contained quasi-two-body channels $(\pi \Delta, \rho N, \eta N, \epsilon N, \omega N, \pi N^*, \rho \Delta)$, and a non-resonant $\pi \pi N$ channel. These inelastic channels were loosely constrained by isobar production cross sections \[16\]. Refinements to this multi-channel approach were subsequently carried out by the Zagreb group \[17\], emphasizing the influence of $\eta N$ production data, and by the Argonne-Pittsburgh group \[18\], which enforced more stringent constraints from isobar production data.

The GW DAC analysis was based on a Chew-Mandelstam parameterization of partial-wave amplitudes, building in branch cuts for the opening $\pi \Delta, \rho N$, and $\eta N$ channels. Forward and fixed-\(t\) dispersion relation constraint were imposed and satisfied interatively in a joint fit to both the constraints and the existing experimental data for $\pi N$ elastic scattering and $\eta N$ production data.

Noticeably absent from the above-described three PWA was the incorporation of existing $KY$ production data. In addition, the appearance of double-polarization data ($R$ and $A$) at at moderate energies \[19\] only after the KH and CMB analyses were completed, has also cast some doubt on the uniqueness of these elastic amplitudes.

The aim of this Communication is to show that by paying proper attention to inelastic channels we may first re-evaluate the status of "old" resonances (resonances which have been extensively discussed for decades), and then discuss and establish a level of confidence for newly discovered states. Photoproduction experiments, particularly those producing final-state mesons (such as $K, \eta, \eta', \omega$) beyond single pions \[20\] \[26\] have been and will continue to be crucial for the discovery of new resonances, as has been extensively discussed at ATHOS 2012 Workshop in Camogli 2012 \[27\] by E. Klempt \[28\].

II. $N(1710)1/2^+ - N(1710)P_{11}$

This resonance is a textbook example showing how the confidence level of a resonance’s existence changes through the application of different analysis techniques, and how our knowledge concerning the necessity of measuring and analyzing inelastic channels has matured over time.

As mentioned in the Introduction, this state though originally having a 4-star rating, was demoted to 3 stars in the 1984 edition of the RPP. The KH and CMB analyses, in spite of fitting mainly $\pi N$ elastic data, definitely required this state. Some older, and much simpler analyses based on the rather small base of inelastic data \[29\] \[35\] also required this state, so its existence was at least fairly certain. The change in star rating was a result of an overall re-evaluation of resonance criteria, and notable changes were made for almost all resonances.

Since the 1984 edition, we can separate various PWA attempts in two main categories: i) those that used mainly $\pi N$ elastic data, and ii) those that included several, or most of the dominant, inelastic channels. Below we summarize the findings of the most well-known efforts.

i) One of the most elaborate approaches, based almost exclusively on $\pi N$ elastic data was, as described above, performed by KH collaboration \[12\]. In their Breit-Wigner and speed-plot fits to the $P_{11}$ amplitude, they found clear evidence for the $N(1710)1/2^+$ state. Contrary to this, the GW DAC analysis, also heavily relying on $\pi N$ elastic data, did not find this state in its energy-dependent solution. These seemingly contradictory results can, however, be simultaneously understood remembering that, as has recently been demonstrated using Laurent+Pietarinen (L+P) technique in
single-channel analysis [11], some of the states with a lower confidence level can be alternatively explained either as resonances or as complex branch-points effects due to inelastic channel openings (ρN at W = 1708 - i 70 in particular). There is no way to distinguish between the two mechanisms if only the πN elastic scattering channel is analyzed. As a recent multi-channel analysis from the BuGa group finds a very small ΓπN/Γ branching fraction and elastic pole residue, we infer that πN elastic scattering is not optimal for a determination of its properties. However, by using the L+P technique it can be concluded that each of the two πN analyses is at least consistent with its existence, and no definite conclusion can be made without incorporating inelastic channels.

The Jülich coupled-channel model also did not see the N(1710)P11 state in their early publications [36, 37]. At that stage of their calculation, they had fitted πN elastic, and somewhat renormalized πN → ηN data, and a ρN complex branch point seemed to be sufficient to describe both of these sets of data. However, as we shall see later, when their calculation was expanded to include, in particular, strange inelastic channels [38], their conclusions changed.

ii) The first analysis which included inelastic data more extensively came from Kent State University (KSU) [39], using a multichannel approach constrained to fit both πN elastic and πN → ππN data. The existence of N(1710)P11 state was unambiguously detected because by choosing ππN channel they were able to keep ρN complex branch point effects well under control. This work was recently updated to include ηN, KA and single pion photoproduction channels [40], confirming their earlier conclusions.

The next group of analyses was based on reviving 1979 Cutkosky CMB model, but the data base this time included some of the inelastic channels. First, a three-channel model appeared from Zagreb in 1995 [17] which had three coupled channels: the πN elastic channel was represented by KH80 partial waves, the second channel contained full available πN → ηN data base giving lower confidence to some higher energy data, and having the third, effective channel with no data to fit, but left open to allow the transfer of flux from first two channels to maintain the multi-channel unitarity. This model was followed by Argonne-Pittsburgh collaboration [18] which extended the number of channels and included additional inelastic channels like ππN for instance. In both cases N(1710)P11 was very strongly required. The Zagreb group in 2006 also offered the explanation that N(1710)P11 state can be explained as a continuum ambiguity effect, and that it entirely depends on measurements of the reaction π→KΛ data [49] did not require this state. This may, however, be due to a lack of multi-channel constraints (such as the reaction πN → KΛ discussed below) for a model very different from those discussed above, and lower coupling of N(1710)P11 state to photoproduction channel.

The analysis of the πN → KΛ reaction provides the best example for the importance of data from inelastic reactions. First, this reaction is isospin selective: only nucleon states are produced. Second, due to the self-analyzing power of Λ hyperon, the recoil asymmetry can be measured in an unpolarized experiment and the rotation parameter in an experiment with the polarized target. Furthermore, in the region around 1700 MeV the dominant contributions are expected to come from S and P waves which can be clearly separated in the analysis of three observables. Indeed two energy-dependent analyses (Jülich [35] and BuGa [50]) found a large contribution from the P11 wave with a clear resonant structure at 1700 MeV, as shown in Fig. 1 for BuGa solution and in Fig. 2 for the Jülich solution. This result was confirmed in the energy-independent analysis carried out by the Kent and BuGa groups.

![FIG. 1: (Color online) Partial wave analysis amplitude (left) and phase shift(right) of the inelastic πN → KΛ P11 wave. The band correspond to a variety of energy-dependent BuGa solutions, and points correspond to energy independent solution of ref. [50].](image-url)
 Until recently, the reason why different analyses gave conflicting results for the N(1710) $P_{11}$ confidence level was not entirely understood, and differences were accepted just as a fact. Thus, there was no reason to change the RPP star rating. The natural explanation, that the effects of complex branch-points might, in single-channel analyses, be confused with resonance effects, was first considered by the J"ulich-Zagreb collaboration [37], and more transparently explained by the efforts of the Zagreb-Tuzla group, by introducing the L+P expansion [11]. Therefore, a straightforward conclusion emerged: When a resonance in single-channel analysis can be confused with the effects of nearby complex branch-point, channels which are connected with this branch point must also be measured to clarify the distinction.

Summary

After realizing that complex branch points may in single-channel analysis give a false resonance signal, we can with certainty claim that multi-channel analyses (coupled-channel or combined single-channel ones) are essential to unambiguously establish the resonance existence. As all multi-channel analyses have shown the need for the N(1710)$1/2^+$ - N(1710)$P_{11}$ state, we believe that its existence has been proven beyond any doubt.

Recommendation

Raise the RPP confidence level of N(1710)$1/2^+$ state from 3* to 4*.

III. $\Delta(1600)3/2^+$ - $\Delta(1600)P_{33}$

This is still listed as a 3* resonance, in spite of the fact that its existence is confirmed in each of the KH, CMB, and GW DAC analyses. In addition, a re-analysis of the KH amplitudes, using the L+P method, finds that this cannot be described by a complex branch-point effect.

Even the earliest PWA analyses by Longacre [38, 39] confidently reported its existence. A revival of CMB method, extending the fitted data base of inelastic channels, independently by Zagreb and Argonne-Pittsburgh [17, 18] similarly find it. The same is true for the KSU [39, 40] and Giessen [42], and ANL-Osaka [44]. Finally, in the BuGa analysis, it is present without any doubt [45] in any combination of analyzed data.

While the existence of this state is clear, its mass and width (or pole parameters) are not consistent between the various determinations. The Breit-Wigner mass, for example, varies from 1510 ± 20 MeV, in the BuGa analysis, to 1706 ± 10 MeV, in the Kent State analysis; the width is similarly uncertain, varying from about 200 MeV to 500 MeV in various analyses finding this state.

Summary

The $\Delta(1600)P_{33}$ is confirmed to exist, though its resonance parameters have not been accurately determined.

Recommendation

In spite of the fact that its mass and width are still subject to sizable variations from analysis to analysis, we still believe that one should seriously consider raising the RPP confidence level of $\Delta(1600)P_{33}$ state from 3* to 4* if this implies existence is certain.

IV. N(1900)3/2$^+$ - N(1900)$P_{13}$

This state is a good example of a resonance which appears to couple weakly to the $\pi N$ elastic channel. Consequently, the N(1900)$3/2^+$ was not reported by the KH, CMB, and GW DAC analyses. However, the KSU analysis [39], which had additional constraints from $\pi \pi N$ channels, did report it; this finding was confirmed in a recent update to the KSU analysis [40]. Consequently, the RPP has retained the state as a 2* resonance only.

Using the KH80 partial waves [12], and an analytically smoothed version of the same analysis KA84 [51], the L+P method has unambiguously detected a N(1900)$P_{13}$ state in these amplitudes, unreported until now ([1928 ± 18 ± 2)] + i (152 ± 40 ± 9) for KH80 and (1920 ± 17 ± 1) + i (215 ± 37 ± 2) for KA84]. Here, however, it was also stressed that this structure in the $P_{13}$ partial wave, near 1900 MeV, can alternatively be explained by complex $\rho N$ branch-point, so new measurements were needed. Therefore, we may say that two “old” PWA do contain evidence for the N(1900)$P_{13}$ state: KSU, which reported it, and KH80, where it remained undiscovered until recently.

Other evidence has come from the ANL-Osaka analysis [44], which included inelastic channels and...
reported the $N(1900)P_{13}$, whereas an earlier EBAC analysis \cite{Roos1991} of $\pi N$ scattering did not. Another claim comes from the Giessen fit of 2002 \cite{Giessen2002} which emphasizes its coupling to the $\omega N$ channel.

The breakthrough came with new photoproduction experiments. This state was solidly established in the BuGa coupled-channel analysis \cite{Manley1991, Saleski1991} making use of very precise $K\Lambda$ and $K\Sigma$ cross sections and polarization data. When the resonance was introduced with varying mass, the $\chi^2$ as a function of the imposed mass showed striking minima for both these reactions \cite{Manley1991} and even evidence for its decay into $N\eta$. Presently, the reaction $\gamma p \rightarrow p\pi^0\pi^0$ is being studied and it is found that the state decays via $\Delta(1232)\pi$ with a branching ratio of about 65%. In the cascade $N(1900)3/2^+ \rightarrow N(1520)3/2^-\pi^0 \rightarrow N2\pi^0$, the presence of $N(1900)3/2^+$ can be identified even without partial wave analysis when the decay pattern $N^+(1900) \rightarrow N(1520)3/2^-\pi^0 \rightarrow N\pi^0\pi^0$ from polarized photons is compared to the pattern expected for different $N^+(1900)$ spin-parities \cite{Manley1991}. The $N(1900)P_{13}$ was also confirmed in an effective Langrangian resonance model analysis of $\gamma p \rightarrow K^+\Lambda$ \cite{Roos1991}, and in a covariant isobar-model single channel analysis of $\gamma p \rightarrow K^+\Lambda$ \cite{Roos1991}. The discovery of $N(1900)P_{13}$ is a very clear example of the importance of the photo-production data for establishing the existence of new baryon states. Already the $\gamma p \rightarrow K\Lambda$ total cross section measured by the CLAS collaboration \cite{Roos1991} shows a double-peak structure with the second peak at 1900 MeV, indicating a contribution from a resonant state (or set of states) with this mass. The analysis of the CLAS differential cross section and the recoil asymmetry \cite{Roos1991} shows that this state has total spin $J \leq 3/2$. The determination of the quantum numbers of this state is further clarified from the analysis of CLAS data \cite{Roos1991} double-polarization observables $C_x$ and $C_z$, measured in the $\gamma p \rightarrow K\Lambda$ and $\gamma p \rightarrow K\Sigma$ reactions. These data clearly demonstrated that the state, which is responsible for the peak in the total cross section, has quantum numbers $J^P = 3^+$. Finally we want to point out that there are indications in the single channel, event-based analysis of $\omega$ photoproduction from CLAS \cite{Roos1991}, and in the BuGa multi-channel analysis \cite{Manley1991}, that there could be two $N(1900)P_{13}$ states with close masses. If confirmed, this could alter properties of the state, but still its existence is unquestionable.

**Summary**

The evaluation of this state confirms earlier conclusions. Single channel analysis of $\pi N$ elastic data is difficult, and can only give alternative (resonance vs. complex branch point) explanations. Inclusion of some data from $\pi N$ channel in KSU analysis \cite{Roos1991} selects the resonance alternative, and the CLAS photoproduction data in the $K^+\Lambda$ channel fully confirmed the state.

**Recommendation**

Raise the RPP confidence level of $N(1900)3/2^+$ state from $3^+$ to $4^+$.

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