Research Article

Influence of Fluid Viscous Damper on the Dynamic Response of Suspension Bridge under Random Traffic Load

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Abstract

Fluid viscous dampers (FVDs) are widely used in long-span suspension bridges for earthquake resistance. To analyze efficiently the influences of FVDs on the dynamic response of a suspension bridge under high-intensity traffic flow, a bridge-vehicle coupling method optimized by isoparametric mapping and improved binary search in this work was first developed and validated. Afterwards, the traffic flow was simulated on the basis of monitored weigh-in-motion data. The dynamic responses of bridges were analyzed by the proposed method under different FVD parameters. Results showed that FVDs could positively affect bridge dynamic response under traffic flow. The maximum accumulative longitudinal girder displacement, longitudinal girder displacement, and longitudinal pylon acceleration decreased substantially, whereas the midspan girder bending moment, pylon bending moment, longitudinal pylon displacement, and suspender force were less affected. The control efficiency of maximum longitudinal girder displacement and accumulative girder displacement reached 33.67% and 57.71%, longitudinal pylon acceleration and girder bending moment reached 31.51% and 7.14%, and the pylon longitudinal displacement, pylon bending moment, and suspender force were less than 3%. The increased damping coefficient and decreased velocity exponent can reduce the bridge dynamic response. However, when the velocity exponent was 0.1, an excessive damping coefficient brought little improvement and may lead to high-intensity work under traffic flow, which will adversely affect component durability. The benefit of low velocity exponent also reduced when the damping coefficient was high enough, so if the velocity exponent has to be increased, the damping coefficient can be enlarged to fit with the velocity exponent. The installation of FVDs influences dynamic responses of bridge structures in daily operations and this issue warrants investigation. Thus, traffic load should be considered in FVD design because structural responses are perceptibly influenced by FVD parameters.

1. Introduction

FVDs were first used in the machinery and military industries. On account of their excellent energy dissipating capacity, they have been applied in structural vibration control under earthquakes. With structural vibration control as a key problem in safety operation of long-span bridges, FVDs are installed on many bridges to mitigate vibration and to serve as an effective seismic control device. In 1989, FVDs were first used on the Golden Bridge located in USA for increasing its seismic resistance. The identification test organized by the Highway Innovative Technology Evaluation Center had been a valid reference in subsequent application and specification preparation of FVDs [1]. The technology was first brought to China on the Chongqing Egongyan Yangtze River Bridge in 2000 and is now widely used in Yangtze River bridges [2]. Since FVDs are integrated with the bridge, they have various complex effects on bridge responses, such as girder displacement, pylon bending moment, and expansion joint displacement. The designation of optimum FVD parameters focuses on the response under earthquake excitation and has been investigated comprehensively. The research methods generally included numerical analyses, shake table tests, and data monitoring.
Different techniques have been proposed by scholars to ascertain the optimal parameters that can achieve ideal structural response [6–8].

Although FVDs’ effects under earthquake excitation have been widely studied, the dynamic responses of bridges, which are also vulnerable to vibrations excited by wind, temperature, and vehicles, have not been thoroughly examined. The most common dynamic response in the bridge life cycle is the frequent low-speed reciprocating motion, which is mainly caused by wind and traffic flow [9]. The corresponding service life of bridge accessories, such as expansion joints, is also influenced by this frequent reciprocating motion. FVDs can also absorb and dissipate energy imported from wind and traffic flow because of their dissipation capacity. The working conditions of supports, expansion joints, and suspenders can be improved by considering the daily longitudinal girder displacement in determining FVD parameters; the frequent reciprocating motion of main girder also can be effectively improved by using FVDs [10]. For a long-span bridge, the wind load may be more remarkable than vehicle load in transverse response of the bridge. Research shows that the dynamic responses of long-span suspension bridge under high winds and running trains are mainly influenced by strong winds when the wind is strong, but when the wind comes to low intensity, train load plays a decisive role in vertical displacement [11]. For the bridge dynamic response under wind and traffic flow, the wind load plays a major role in bridge lateral displacement. The vertical displacement is mainly controlled by the vehicle load [12]. Furthermore, scholars have made some studies on wind-induced vibration control and found that FVDs have different influences on various response indicators, which has an optimum interval for damping parameters [13, 14]. In addition to the wind-induced vibration, the vehicle-induced vibration of long-span bridges is also remarkable and the influences of FVDs are still indistinct. The daily movement of bridge structures under social vehicles is an important factor related to bridge accessories’ durability [5].

Variation of structural response indexes present different variation trends with changing parameters of FVDs, such as accumulative girder displacement, girder midspan bending moment, pylon longitudinal acceleration, and pylon bending moment. The specific influences of FVDs on the dynamic response of long-span suspension bridges under traffic load, which can be further referenced in the optimization of FVD parameters, should hence be analyzed.

Because the traffic load of the highway bridge is a complicated random process with strong randomness of vehicle type, weight, and quantity, the calculation matrix of random traffic flow–bridge coupling analysis is huge and will take a lot of computing resources. Thus, a high efficiency random traffic flow–bridge analysis system needs to be established. The traditional vehicle-bridge coupling analysis system, which is based on a numerical method, mainly includes the modal superposition method and full coupling theory [15]. The modal superposition method is more simple and practical than the latter, but the high-order modes of structures are hard to obtain, thereby negatively affecting the calculation precision [16]. The full coupling analytical method has the advantages of clear physical meaning and high precision. However, this method requires huge amount of time and lots of computing resources when applied to long-span bridges under large and highly random traffic flow. This paper developed a vehicle-bridge interaction system with high efficiency to analyze the dynamic response of a bridge with FVDs under a large and highly random traffic flow. This system was established based on the interhistory iteration method and optimized by iso-parametric mapping and improved binary search. Then, the traffic flow was simulated in accordance with the monitored data. Finally, the responses of the large-span bridge under traffic flow with different parameters of FVDs were studied.

2. Establishment of Vehicle-Bridge Interaction System

2.1. Finite Element Model of Bridge. The bridge model is established by the space truss model in ANSYS 15.0 [17]. Spine-beam, double-beam, and triple-beam models are widely used in the integral analysis of long-span bridges, and the grillage model and multiscale model are also used according to different requirements [18, 19]. Main cables and suspenders are usually simulated by the Link10 element, which can simulate the elasticity and plasticity of the structure. The pylon and girder are simplified into a two-node beam element and modeled by Beam4 element. The railings and deck paving are simulated by the Mass21 element. The entire structure is distributed into a number of elements and connected through the node on the boundary of adjacent elements. Given the demand for refined simulation of the vehicle-bridge interaction, a grillage model is utilized in this article to construct the prototype bridge to obtain detailed component response. The detailed information and feasibility of the model are proposed and validated in succeeding chapters.

2.2. Dynamic Vehicle Models. A vehicle is mainly composed of a car body, wheels, a shock mitigation system, and a damped system connecting different components. A vehicle dynamic model needs to be established before the vehicle-bridge coupling analysis is conducted. With these demands, some hypothesis is unavoidable in constructing the dynamic models. The mass of damper and spring components are ignored compared with the quality of the vehicle body. Vehicle model is generally divided into different rigid bodies that are connected by axle mass blocks and by elastic and damped components. According to previous research, the common Chinese highway vehicles can be divided into 17 types of 5 categories in accordance with vehicle axle distance, axle number, axle load, and vehicle load based on weight-in-motion data and Chinese automobile model manual [20, 21]. The vehicle classification is shown in Table 1.

The dynamic models are also provided based on different vehicle type. Taking three-axle vehicle as an example, the vehicle dynamic model of three-axle vehicle (double rear axle) is shown in Figure 1 [20]. The rigid body is usually deemed to have 6 degrees of freedom. As the vibration of the
vehicle in advancing direction is tiny compared to the distance travelled, the vibration of the vehicle body in advancing direction has few effects on the bridge. The bridge is mainly influenced by the integral movement of the vehicle in advancing direction. In order to reduce the complexity of vehicle model and the calculation, the degree of freedom in advancing is generally neglected in vehicle-bridge interaction analysis [22]. Thus, 5 degrees of freedom (vertical, horizontal, head nodding, side rolling, and head shaking) are considered for the integral vehicle. Each wheel has 2 degrees of freedom (vertical and horizontal). For the trailer, horizontal and head nodding degrees of freedom are neglected to derive the equation. Each vehicle body has 3 degrees of freedom, and each wheel has 1 degree of freedom.

### 2.3. Load Distribution Based on Quadrilateral Isoparametric Mapping

For the dynamic analysis under large random traffic flow, the positioning and loading of the contact point between the vehicle and the bridge should be a crucial issue. Bridge decks are typically simulated by grillage, solid, or shell elements in most models. The wheel load is simplified to a concentrated force acting on the bridge deck and then distributed to four adjacent nodes by four-node isoparametric mapping [23], which is the same as that of displacement in a two-dimensional plane, as shown in Figures 2 and 3.

The coordinate mapping equations are as follows:

\[
\begin{align*}
&x = \sum_{i=1}^{4} N_i(\xi, \eta) x_i, \\
y = \sum_{i=1}^{4} N_i(\xi, \eta) y_i, \\
N_i(\xi, \eta) &= \frac{1}{4} (1 + \xi \xi_i) (1 + \eta \eta_i),
\end{align*}
\]

where \(x\) and \(y\) denote the coordinates of the force point of the wheel load \(P_i\); \(x_i\) and \(y_i\) denote the \(i_{th}\) quadrilateral element point’s horizontal and vertical positions; \(\xi\) and \(\eta\) denote the corresponding values that \(x\) and \(y\) map from the quadrilateral element to the parent element; \(\xi_i\) and \(\eta_i\) denote known quantities, namely, the \(i_{th}\) node’s horizontal and vertical positions of the parent element; \(N_i(\xi, \eta)\) denotes a function of isoparametric point \((\xi, \eta)\); function value \(N_i\) denotes the \(i_{th}\) quadrilateral element point’s load distribution coefficient.
The unknown quantities $\xi$ and $\eta$ of bilinear equation (1) can be solved by Newton iteration to obtain the distribution coefficient $N_i$. Afterwards, the automatic loading of the wheel load can be realized. The iteration process is as follows:

$$\begin{bmatrix} \xi_k^{+1} \\ \eta_k^{+1} \end{bmatrix} = \begin{bmatrix} \xi_k \\ \eta_k \end{bmatrix} - J(\xi_k, \eta_k)^{-1} \begin{bmatrix} \sum_{i=1}^{4} N_i(\xi_k, \eta_k)x_i - x \\ \sum_{i=1}^{4} N_i(\xi_k, \eta_k)y_i - y \end{bmatrix},$$

where $J$ denotes a Jacobian matrix; $\xi_k$ and $\eta_k$ denote the calculated value of the $k_{th}$ iteration. The iteration is stopped when $\left\| \xi_k^{+1} - \xi_k \right\| < \varepsilon$ with the iteration error $\varepsilon$ set to $10^{-8}$.

The position information of four adjacent nodes is indispensable for realizing the automatic loading of the wheel load $P$. Binary search can effectively halve the scope in finding specific elements in ordered arrays. Thus, it can be extended for searching the coordinate range of the wheel loading. For example, the process of searching the longitudinal wheel loading point $x$ is shown in Figure 4, and the positioning for the lateral loading point $y$ is the same.

The detailed steps are as follows.

1. The node coordinates of the lane on which the vehicles drove are imported and sorted in ascending order to form a one-dimensional matrix.

2. Initialization: the value of “front” is set to 1; the value of “last” is set to the number of columns of the matrix formed in step 1.

3. Calculation of “mid”: “mid” = “round”((“front” + “last”)/2); “round” means rounding off.

4. The search ends when “mid” = “last.” The upper limit of the wheel x-coordinate in the one-dimensional matrix is “mid,” and the lower limit is “mid” – 1. Otherwise, whether the wheel x-coordinate is between “front” and “mid” is determined. If it happens, then “last” = “mid;” otherwise, “front” = “mid.”

5. Step 3 is executed until “mid” = “last.”

Equation (1) can be solved by Newton iteration after finding four adjacent nodes of the wheel load $P$. Then, the interpolated coefficient at each node can be obtained to calculate the distribution load. In order to reduce the computation of bridge-vehicle coupling, only the results of displacement and velocity of load acting point are output. Afterwards, based on the known interpolated coefficient, the velocity and displacement of load acting point are calculated to solve the bridge-vehicle interaction force.

2.4. Road Surface Roughness. Road surface roughness is an important factor that could cause a vehicle’s vertical vibration, which is directly related to the safety and comfort of the vehicle. Surface roughness can be described as a power spectral density function. The recommended power spectral density function is adopted in this study [24]. The function $G_d (n)$ is expressed as

$$G_d (n) = G_d (n_0) \left( \frac{n}{n_0} \right)^{-\omega},$$

(3)
where $G_d (n)$ denotes the power spectral density function (m$^2$/cycle); $n$ denotes spatial frequency per unit length (m$^{-1}$); $n_0$ denotes reference spatial frequency, $n_0 = 0.1$ m$^{-1}$; $G_d (n_0)$ denotes power spectral density under reference spatial frequency; and $\omega$ denotes the frequency exponent, and $\omega = 2$.

Road surface roughness is assumed to be a zero-mean stationary Gaussian random process. Thus, it can be generated through Fourier inversion as follows:

$$r(x) = \sum_{k=1}^{N} \sqrt{2G_d(n_k)} \Delta n \cos(2\pi n_k x + \theta_k),$$

where $\theta_k$ denotes the random phase angle uniformly distributed in $[0, 2\pi]$; $n_k$ denotes the $k_{th}$ reference spatial frequency.

The wheel-bridge relationship is assumed to be the point contact in constructing the vehicle-bridge interaction system. When the wheel comes into contact with the road surface, the vertical displacement of vehicle and bridge is the same and the bridge’s vertical displacement is deemed additional surface roughness to the vehicle. Thus, the additional surface roughness caused by bridge displacement and road surface roughness is superposed to constitute the equivalent roughness which is inputted as the vertical excitation source. For the $i_{th}$ wheel, the formula considering bridge displacement is expressed as

$$Z^i_v = Z^i_b + r_i(x),$$

where $Z^i_v$ denotes the vertical equivalent roughness considering bridge displacement, $r_i(x)$ denotes the surface roughness at the wheel-bridge contact point, and $Z^i_b$ denotes the displacement at wheel-bridge contact point.

### 2.5. Motion Equations of Vehicle-Bridge Interaction

The interhistory iteration method is adopted to construct the highway vehicle-bridge coupling analysis system given the technique’s remarkable efficiency under high-intensity traffic flow [25]. Unlike time step iteration, each step of the interhistory method involves full-time calculation. The bridge dynamic response under external load can be computed by any commercial analysis software with several iteration steps, thereby addressing the limitation of the programming calculation in the traditional method.

The bridge and vehicle dynamic equations can be expressed as follows:

$$\begin{align*}
M_v \ddot{Z}_v + C_v \dot{Z}_v + K_v X_v &= F_v, \\
M_b \ddot{Z}_b + C_b \dot{Z}_b + K_b X_b &= F_b,
\end{align*}$$

where $M_v$, $C_v$, and $K_v$ denote the global mass, damping, and stiffness matrices of the train subsystem, respectively; $M_b$, $C_b$, and $K_b$ denote the global mass, damping, and stiffness matrices of the bridge subsystem, respectively; $X_v$ and $X_b$ denote the displacement vectors of the train subsystem and the bridge subsystem, respectively; $\dot{Z}_v$ and $\dot{Z}_b$ denote the velocity vectors of vehicle and bridge, respectively; and $\ddot{Z}_v$ and $\ddot{Z}_b$ denote the acceleration vectors of bridge, respectively; and $F_v$ and $F_b$ denote the force vectors of vehicle and bridge, respectively.

Wheels are assumed to always be in contact with the bridge deck while the vehicle is moving, so the shock mitigation system and suspension system are deformed with bridge vertical deformation and surface roughness. The dynamic equations of the vehicle-bridge coupling system can be expressed as (7). The interaction force between the vehicle and the bridge is a function of vehicle motion, bridge motion, and road surface roughness stated by $Z_v$, $Z_b$, and $i$.

$$\begin{align*}
F_v &= F_v(Z_v, \dot{Z}_v, \ddot{Z}_v, Z_b, \dot{Z}_b, \ddot{Z}_b, i), \\
F_b &= F_b(Z_v, \dot{Z}_v, \ddot{Z}_v, Z_b, \dot{Z}_b, \ddot{Z}_b, i).
\end{align*}$$

The coupling relationship between the vehicle and bridge subsystems is established by simultaneously solving (6) and (7) and then solved by the interhistory iteration method. The iteration process is realized by MATLAB R2014a [26], while the bridge model constructed in ANSYS 15.0 is used to output the bridge response. Each step of interhistory iteration for the bridge and the vehicle is separate and involves full-time calculation. Thus, the method will occupy reduced computer storage, generate accurate computations, and have the advantages of a clear aim and ease of operation. The convergence is checked by the interaction force between the vehicle and the bridge and defined as $\|F_v^i - F_v^{i+1}\| < 0.1$. The detailed process is plotted in Figure 5.

### 3. Validation of the Established Analysis System by Field Load Test

#### 3.1. Prototype Bridge and the FE Model

To validate the vehicle-bridge interaction analysis system and to analyze the influence of FVDs under random traffic flow, a three-dimensional finite element model of a long-span suspension bridge is constructed in ANSYS 15.0 as the research object (Figure 6). The bridge has a span of 896 m, a steel truss main girder with the deck slab width of 26 m, and a rigid central buckle. The detailed information of the bridge is as follows.

1. The sag-span ratio of main cable is 1:10. The longitudinal distance in each suspender is 12.8 m. The steel girder adopts Warren truss stiffening beam with the height of 6.5 m and width of 26 m, the minimum segment length is 6.4 m, and the standard segment length is 12.8 m. The pylon adopts a concrete portal frame structure. One pylon is 117.6 m high and another pylon is 122.2 m high.

2. The main cable consists of 127 galvanized high-strength prefabricated parallel steel wire strands; each steel wire strand consists of 127 steel wires with a diameter of 5.1 mm. Suspender is pin jointed with main cable and girder, and each consists of 91 galvanized high-strength prefabricated parallel steel wires with a diameter of 5.2 mm.

3. The material parameters have been modified according to the measured features of the bridge: elastic modulus of main cable is $1.94 \times 10^{11}$ Pa,
The elastic modulus of girder is $2.13 \times 10^{11}$ Pa, elastic modulus of pylon is $3.48 \times 10^{10}$ Pa, the density of pylon is 2663 kg/m$^3$, the density of the truss element is 8646 kg/m$^3$, and the density of main cable is 8020 kg/m$^3$.

The pylon, central buckle, and main girder are modeled using Beam4 element. In order to simulate the lane load, four longitudinal girders were built in the model. Each lane load was exerted on the corresponding longitudinal girder. The main cables and suspenders are simulated using Link10 element, and the railings and deck paving are simulated using Mass21 element. The boundary conditions of the pylon foundation are simulated as fixed connection. The line displacement of the main cable at the anchorage point is constrained in three directions. The simulation of the vertex and tangential point of the cable saddle are realized through the node coupling. The vertical and horizontal displacement of the end of the girder is limited and the rotational degree of freedom is released.

The damping effect is an output resistive force that depends on the relative velocity of the damping device. Equation (8) is recommended to calculate the produced damping force [27]. FVDs are simulated using Combin37 element. As shown in Figure 7, the FVDs are longitudinally settled on both sides of the midspan as a connection of the girder and the pylon, with two dampers on each side.

$$F = K|v|^a \text{sign}(v),$$

where $F$ denotes the damping force, $K$ denotes the damping coefficient, $v$ denotes the relative velocity between the ends of the damping device itself, sign denotes the sign function, and $a$ denotes the velocity exponent.

The data of the bridge were collected when the prototype bridge just finished the construction. Existing research shows that the conditions of road surface roughness of new bridges in China are most A grade in accordance with ISO 8608 [24, 28]. So the road surface roughness is set to A grade and generated based on specified parameters in ISO 8608, as shown in Figure 8.

### 3.2. Accuracy Validation by Field Load Test

The numerical analysis result is compared with the result of dynamic experiment to verify the accuracy of the proposed method. The basis of the validation is the uniformity of theoretical model and actual bridge. Thus, the FE model in this article was constructed according to measured material properties and cable forces. Referring to existing researches, the accuracy of FE model can be considered as acceptable when the errors between the calculated and measured frequencies are less than 5% [29, 30]. The measured frequencies of the bridge are compared with the numerical results in Table 2. It can be seen that the numerical results are comparable to the
measured results. The maximum frequency error is 4.37% and all errors are less than 5%, which proves the correctness of the FE model.

Then the dynamic strain and vertical acceleration of mid-span are measured to validate the proposed method. The measuring point of the dynamic strain is set on the top chord of the steel trusses in the middle of midspan. The measuring point of vertical acceleration is set on the bridge deck at the same place. The driving position of trucks and measuring points are shown in Figure 9; the detailed vehicle dynamic parameters are shown in Table 3 [31]. Three test conditions are settled for the validation: (1) two three-axle trucks passing through the bridge at a constant speed of 20 km/h, (2) two three-axle trucks passing through the bridge at a constant speed of 30 km/h, and (3) two three-axle trucks passing through the bridge at a constant speed of 50 km/h.

| Vibrating direction | Order | Measured result | Numerical result | Error (%) |
|--------------------|-------|-----------------|-----------------|-----------|
| Horizontal         | 1     | 0.071           | 0.07            | 1.41      |
|                    | 2     | 0.183           | 0.175           | 4.37      |
|                    | 1     | 0.131           | 0.134           | 2.29      |
|                    | 2     | 0.185           | 0.182           | 1.62      |
| Vertical           | 3     | 0.292           | 0.282           | 3.42      |
|                    | 4     | 0.394           | 0.38            | 3.55      |
| Torsional          | 1     | 0.348           | 0.342           | 1.72      |
|                    | 2     | 0.434           | 0.425           | 2.07      |
VX_he measured results are extracted and compared with those obtained by the analytical solution on the basis of the proposed method. VX_he comparison of dynamic strain results under different vehicle velocities is shown in Figure 10. It can be seen that the changing trends of two curves are consistent in Figure 10. By comparison, the peak value of the dynamic strain of 50 km/h is higher than 20 km/h and 30 km/h. VX_he peak value of measured dynamic strain of 50 km/h is 30.03 while that of 20 km/h and 30 km/h is 26.6 and 27.9. It indicates that the maximum dynamic strain increases with the vehicle velocity. In Figure 10(a), the error of peak values of two curves is 1.35%. In Figure 10(b), the error of peak values of two curves is 1.12%. In Figure 10(c), the error of peak values of two curves is 0.3%. VX_he comparison results indicate that the validity and accuracy of the proposed method are acceptable.

The midspan acceleration of measured result and the proposed method is shown in Figure 11. As the noise of measured acceleration is more obvious than that of strain and cannot be eliminated, the comparison of acceleration is not as good as that of strain. But the variation trends of measured result and the proposed method are also consistent. The consistence of changing trends of the vertical acceleration also proves the accuracy of the proposed method.

4. Traffic Flow Simulation Based on Monitored Data

The response of long-span suspension bridges under traffic flow is mainly influenced by traffic flow density and total vehicle weight. The investigation focuses on the FVDs’ influence on the bridge dynamic responses under traffic flow; thus the key variables are FVD parameters while the traffic flow needs to remain unchanged. Monitored traffic data gathered by weigh-in-motion system are processed to form typical traffic load to obtain the response of the studied structure [32]. The data collection site lies in Zhangjiawan bridge at the G104 highway in Zhejiang province of China, which is a coastal developed area. The vehicles include cars, vans, trucks, and trailers. The WIM data were measured in two lanes and collected more than 10,000 vehicles through one-month monitoring. In order to eliminate the sick data, the vehicles have low weight (less than 0.5 t) and high speed (more than 120 km/h) filtered in preprocessing the data coming from weigh-in-motion system.

First, the monitored data are statically initialized to separate vehicles in carriageway and passing lane according to the statistical property of lane distribution. As the statistical analysis in hours can reflect the randomness and the peak hours of traffic flow, hourly traffic flow is often used in traffic load analysis [32, 33]. The WIM data were divided into 24 hours each day and the total vehicle weight of each period was calculated. For the bridge, the density of dynamic response is directly influenced by the external load. In order to obtain the most obvious response, the vehicles with maximum total vehicle weight in an hour are screened out as the basic data of the traffic flow. Figure 12 shows the maximum total vehicle weight of each hour in a month. The left road of two lanes of the advancing direction in China is passing lane and the right is carriageway. The maximum vehicle weights in an hour along the passing lane and the carriageway are 1115.31 t and 759.78 t, respectively. The corresponding vehicle data are chosen as the basic data to simulate traffic flow. The detailed information of vehicle type is shown in Figure 13; it can be seen that the proportion of small and medium cars in traffic is larger than trucks.
Figure 10: The comparison of dynamic strain results. (a) 20 km/h; (b) 30 km/h; (c) 50 km/h.

Figure 11: Continued.
The detailed simulation process is shown in Figure 14. As the prototype bridge is bidirectional with four lanes and the monitored data only have two lanes, the chosen vehicle data...
are used to simulate sparse flow and dense flow separately that can be loaded on both sides of the bridge simultaneously. The traffic condition is divided into sparse flow and dense flow that the headway of the former exceeds 3 s and that of the latter is less than 3 s [34]. Statistical analysis on the WIM data indicates that the vehicle headway of the dense and sparse flow obeys gamma distribution. The key parameters are shown in Table 4. The corresponding vehicle headways are generated according to statistical properties. Figure 15 shows the vehicle headways of dense flow in passing lane. Then, combined with vehicle data, a bidirectional traffic flow with a dense upstream flow and a sparse downstream flow is formed to load on the bridge.

5. FVD Effect under Traffic Flow

According to existing research, the service life of bridge accessories, such as expansion joints and FVDs, is closely related to the deformation and fatigue properties of the components under external loads [35]. An accumulative friction slide distance that exceeds the design value is an important precipitating factor, and also it will lead to component damage in which traffic flow accounts for most of the accumulative displacement. Maximum girder displacement is a critical factor that determines whether the working condition of a bridge accessory is in the design range. Thus, the longitudinal accumulative girder displacement and maximum longitudinal girder displacement are selected as the typical indexes of the vibration control effect of FVDs under traffic flow. In JT/T 926-2014, the damping velocity exponent is specified into seven classes (0.1, 0.2, 0.3, 0.4, 0.5, 0.6, and 1), and no limitation exists for the damping coefficient, whose value commonly ranges from 1000 kN/(m/s)α to 20000 kN/(m/s)α [13, 27]. The damping coefficient is set to 1000 kN/(m/s)α, 2500 kN/(m/s)α, 5000 kN/(m/s)α, 7000 kN/(m/s)α, 10000 kN/(m/s)α, 15000 kN/(m/s)α, and 20000 kN/(m/s)α to analyze the FVDs’ effects with representative combinations of parameters.

**Table 4: Parameters of vehicle headway.**

| Operation state | Distribution type | Lane          | Distribution parameters |
|-----------------|-------------------|---------------|-------------------------|
| Sparse flow     | Gamma distribution| Carriageway   | α: 0.2954, β: 0.0038    |
|                 |                   | Passing lane  | α: 0.4005, β: 0.0149    |
| Dense flow      | Gamma distribution| Carriageway   | α: 7.4072, β: 3.5829    |
|                 |                   | Passing lane  | α: 7.7043, β: 3.7311    |

Figure 14: Flowchart of traffic flow generating.

Figure 15: Vehicle headways of dense flow in passing lane.
Nonlinear time history analysis under traffic flow is conducted using the bridge-vehicle interaction system established in Section 2. The main girder of the suspension bridge is directly influenced by FVDs, so the girder response varies as shown in Figures 16–18. The installation of FVDs provides the following benefits: longitudinal displacement and accumulative displacement decrease noticeably with an enlargement in the damping coefficient and a decrease in the velocity exponent. The girder midspan bending moment also decreases with increased damping coefficient and decreased velocity exponent. When the velocity exponent exceeds 0.4, the influence on girder midspan bending moment is not remarkable. But when the velocity exponent is below 0.4 and the damping coefficient exceeds 7000 kN/(m/s)$^\alpha$, the girder midspan bending moment noticeably declines with increased damping coefficient and decreased velocity exponent.

Figures 19 and 20 show that the variation trend of longitudinal pylon displacement and acceleration increases accordingly with the increase in the velocity exponent or the decrease in the damping coefficient. Figure 21 shows that the variation trend of the pylon bending moment is relatively
complex; it increases with the damping coefficient when the velocity exponent $\alpha < 0.3$ but decreases and then increases with increased damping coefficient when $0.3 \leq \alpha < 1$.

Figure 22 shows that the suspender force is also influenced by FVDs, which is caused by the reciprocating motion of the main girder. The maximum suspender forces were induced by vehicles only; it may cause a relative displacement between the girder and the main cable. The changing law is similar to that of maximum longitudinal pylon displacement.

The extreme values of each index are shown in Table 5. The FVDs evidently influence the longitudinal girder displacement and pylon acceleration. The maximum control efficiency of the girder displacement reaches 33.67%. The accumulated longitudinal girder displacement can be reduced by 57.71%. These results mean that FVDs can remarkably decrease the daily reciprocating motion of related components. Although the maximum reduced rate of the pylon longitudinal displacement is only 2.02%, the maximum pylon acceleration can be reduced by 31.51%. The pylon bending moment and suspender force are less affected in that the maximum control efficiencies are less than 2%.

Once the damping coefficient and velocity exponent are determined, the damping force under normal working...
conditions can be calculated by (8) on the basis of the corresponding damping velocity shown in Figure 23. As shown in Figure 24, the damping force of a partial damping coefficient and velocity exponent is around or exceeds the specified value for a single FVD in Chinese standard [27]. The damping coefficient has an apparent influence on the damping force of the FVDs only when the velocity exponent is relatively small. Preceding results reveal that the longitudinal girder displacement is the most significant response of the structure, but its variation tendency is nonlinear. A large damping coefficient improves the FVD effects, but the effect of improvement is not proportional to the damping coefficient. An excessive damping coefficient brings increased damping force, so the design force of FVD must be high enough to burden the external load. Otherwise, the FVD would be working in limit state under the dense traffic flow, which is adverse to its durability.

By contrast, low velocity exponent results in an evident improvement, especially for FVD performance and girder displacement, thereby potentially making FVD a valid vibration mitigation device in daily operation. Figures 25 and 26 show the time history curves of the maximum girder displacement and accumulative girder displacement when the velocity exponent is 0.1. The accumulative girder
displacement decreases noticeably when the damping coefficient $C < 5000\,\text{kN/(m/s)}^\alpha$, but when the damping coefficient $C > 5000\,\text{kN/(m/s)}^\alpha$, the accumulative girder displacement decreases slightly with increased damping coefficient. The benefits of an excessive damping coefficient are not proportional to the costs of it.

But for the low velocity exponent, the manufacturing process of this type of FVD is complicated and its durability

Table 5: Peak values of bridge dynamic response.

|                          | $W_{pm}$ (m) | $W_{de}$ (m) | $M_g$ (kN·m) | $W_{tm}$ (m) | $a_t$ (m/s²) | $M_t$ (kN·m) | $F_s$ (kN) |
|--------------------------|--------------|--------------|--------------|--------------|--------------|--------------|------------|
| Minimum value            | 0.3931       | 1.8845       | 1157         | 0.1554       | 0.010        | 170548       | 391.65     |
| Maximum value            | 0.5741       | 4.2352       | 1246         | 0.1586       | 0.0143       | 171652       | 397.15     |
| Without damper           | 0.5926       | 4.4561       | 1246         | 0.1586       | 0.0146       | 171481       | 397.25     |
| Maximum control efficiency| 33.67        | 57.71        | 7.14         | 2.02         | 31.51        | 0.54         | 1.41       |

Figure 22: Maximum suspender force $F_s$.

Figure 23: Maximum value of damping velocity $V_c$. 
Figure 24: Maximum value of damping force $F$.

Figure 25: Time history curve of maximum girder displacement ($\alpha = 0.1$).

Figure 26: Time history curve of accumulative girder displacement ($\alpha = 0.1$).
may be limited. So the influence of the velocity exponent also is investigated. When the damping coefficient is $5000 \text{kN} / (\text{m/s})^\alpha$, the time history curves of the maximum girder displacement and accumulative girder displacement are shown in Figures 27 and 28. It can be seen that the decreasing of velocity exponent has little influence on the maximum girder displacement while the common vibration is reduced. According to Figure 28, the accumulative girder displacement can be reduced obviously with the decreased velocity exponent. That is because traffic load is different from the seismic excitation which has the characteristics of short time but strong intensity. Traffic load is generally a low intensity but long term process. The low velocity exponent brings evident benefits for the bridge response under traffic flow.

According to the results, the damping coefficient $C > 5000 \text{kN} / (\text{m/s})^\alpha$ and the velocity exponent $\alpha = 0.1$ are the best parameters for FVDs under traffic flow. The damping coefficient does not need to be too high. However, the FVDs application should consider a variety of factors, such as wind and earthquake. So if the velocity exponent has to be increased, combined with Figure 16, the benefit of low velocity exponent reduced when the damping coefficient is high enough and the damping coefficient can be enlarged to fit with the velocity exponent for the best effect of reducing the response under traffic flow.

6. Conclusions

In this study, bridge dynamic response with FVDs under traffic flow was analyzed on the basis of monitored data. For rapid analysis under high-intensity traffic flow, a bridge-vehicle coupling method optimized by isoparametric mapping and improved binary search was developed and validated. Then, traffic data with extreme total vehicle weight in an hour were screened out from monitoring data to simulate traffic flow. Lastly, the simulation analysis of the bridge with FVDs under traffic flow based on monitored data was accomplished. Various indicators of the bridge are affected to different degrees by variations in the FVD parameters. The results show that vehicle-bridge coupling analysis method optimized by isoparametric mapping and improved binary search based on the interhistory method was validated. The method’s findings were consistent with the experimental results; therefore, the proposed method can be used in vehicle-bridge coupling analysis under high-intensity traffic flow.

For the prototype bridge, the results show that FVDs’ settlement positively impacts bridge dynamic response under traffic flow. The traffic load should be considered in FVD design, as the dynamic response is remarkably influenced by FVD parameters. A reasonable FVD design can effectively reduce the accumulative longitudinal girder displacement, maximum longitudinal girder displacement, and longitudinal pylon acceleration whose maximum control efficiency, respectively, reaches 57.71%, 33.67%, and 31.51%, the girder bending moment also can decrease by 7.14%, and the maximum control efficiencies of other indexes were less than 3%.

This study also shows an increase in the damping coefficient and a decrease in the velocity exponent that can reduce the response of key indexes. However, an excessive damping coefficient will bring negligible improvement and may lead to high-intensity work under traffic flow, thereby adversely affecting component durability. A low velocity exponent will result in evident improvement, especially for FVD performance and girder displacement, and plays a role in maintaining low-velocity movement. The benefits of low velocity exponent reduced when the damping coefficient is high enough. When the velocity exponent has to be increased, the damping coefficient can be enlarged to fit with the velocity exponent.
Note that the research and conclusions in this paper focus on the FVDs' influence on the bridge response under traffic flow. In a subsequent research program, FVDs effects on bridge dynamic response under the combined action of wind and traffic loads and the comprehensive optimization of FVD parameters will be investigated.

Appendix

\(K_{i\text{ul}}^i\) and \(K_{i\text{ur}}^i\) denote the vertical spring stiffness of the \(i\)th axle in upper suspension (N/m):
\[
K_{i\text{ul}}^i = K_{i\text{ur}}^i.
\] (A.1)

\(K_{i\text{yl}}^i\) and \(K_{i\text{yr}}^i\) denote the lateral spring stiffness of the \(i\)th axle in upper suspension (N/m):
\[
K_{i\text{yl}}^i = K_{i\text{yr}}^i.
\] (A.2)

\(K_{i\text{dl}}^i\) and \(K_{i\text{dr}}^i\) denote the vertical spring stiffness of the \(i\)th axle in lower suspension (N/m):
\[
K_{i\text{dl}}^i = K_{i\text{dr}}^i.
\] (A.3)

\(K_{i\text{yl}}^i\) and \(K_{i\text{yr}}^i\) denote the lateral spring stiffness of the \(i\)th axle in lower suspension (N/m):
\[
K_{i\text{yl}}^i = K_{i\text{yr}}^i.
\] (A.4)

\(C_{i\text{ul}}^i\) and \(C_{i\text{ur}}^i\) denote the vertical damping of the \(i\)th axle in upper suspension (N/s/m):
\[
C_{i\text{ul}}^i = C_{i\text{ur}}^i.
\] (A.5)

\(C_{i\text{yl}}^i\) and \(C_{i\text{yr}}^i\) denote the lateral damping of the \(i\)th axle in upper suspension (N/s/m):
\[
C_{i\text{yl}}^i = C_{i\text{yr}}^i.
\] (A.6)

\(C_{i\text{dl}}^i\) and \(C_{i\text{dr}}^i\) denote the vertical damping of the \(i\)th axle in lower suspension (N/s/m):
\[
C_{i\text{dl}}^i = C_{i\text{dr}}^i.
\] (A.7)

\(C_{i\text{yl}}^i\) and \(C_{i\text{yr}}^i\) denote the lateral damping of the \(i\)th axle in lower suspension (N/s/m):
\[
C_{i\text{yl}}^i = C_{i\text{yr}}^i.
\] (A.8)

\(L_i\) denotes the distance from the center of mass of car body to the \(i\)th axle.
\(b_i\) denotes half of the lateral wheel spacing.
\(h_i\) denotes the vertical distance from the center of mass of car body to the upper plane of the spring.
\(h_s\) denotes the vertical distance from the center of mass of car body to road surface.

Data Availability

The raw/processed data required to reproduce these findings cannot be shared at this time as the data also form part of an ongoing study.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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