Enhanced Neutrino Emissivities in Pseudoscalar-mediated Dark Matter Annihilation in Neutron Stars

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Abstract

We calculate neutrino emissivities from self-annihilating dark matter (DM) ($\chi$) in the dense and hot stellar interior of a (proto)neutron star. Using a model where DM interacts with nucleons in the stellar core through a pseudoscalar boson ($a$) we find that the neutrino production rates from the dominant reaction channels $\chi\chi \rightarrow \nu \bar{\nu}$ or $\chi\chi \rightarrow a\bar{a}$, with subsequent decay of the mediator $a \rightarrow \nu \bar{\nu}$, could locally match and even surpass those of the standard neutrinos from the modified nuclear Urca processes at early ages. We find that the emitting region can be localized in a tiny fraction of the star (less than a few percent of the core volume) and the process can last its entire lifetime for some cases under study. We discuss the possible consequences of our results for stellar cooling in light of existing DM constraints.

Key words: dark matter – neutrinos – stars: neutron

1. Introduction

Dark matter (DM) is an essential ingredient of the standard cosmological model. We now know it constitutes nearly 85% of the universe matter density. However, despite the tremendous amount of progress that has been made in the search for this missing type of matter, both on theoretical and experimental fronts, its true nature remains an open question. The Standard Model (SM) of particle physics alone cannot explain the nature of DM, suggesting that it must be extended. Many theoretical model proposals have arisen aiming to explain the existing phenomenology (Bertone & Hooper 2016). The possible interplay between ordinary and DM could reveal interesting novel features, thus serving as the smoking gun evidence for the existence of a dark sector. As an example, one could cite a possible contribution to the reionization of the universe and the increase of gas temperature prior to the formation of neutron stars (Chuzhoy 2007) and Mapelli et al. (2006). In particular, the production of SM neutrinos from annihilation of proposed dark candidates, generically $\chi$, with energy $E_{\nu} \gtrsim m_\chi$ is of paramount importance for the description of internal dynamics and energetic balance in stellar scenarios. In order to be specific, for example, one can consider the solar context. A DM particle will be gravitationally captured by the Sun if, in scattering against solar nuclei, it falls below the local escape velocity. This accumulation mechanism can lead to a local stellar DM density higher than that of the galactic halo where it resides, potentially providing us with an opportune region in which to search for visible signatures (Kouvaris 2008; Rott et al. 2015; Vincent et al. 2015). Additionally, low density environments in solar-type stars could yield interesting features in the neutrino channel (Palomares-Ruiz & Pascoli 2008; Aartsen et al. 2017).

On the other hand, in denser stellar environments such as those leading to the formation of neutron stars (NSs), neutrinos are vastly produced as they are very efficient at releasing the excess of gravitational energy when a compact stellar object is formed from a more massive progenitor. It has now been more than 30 years since the supernova SN1987A event allowed us to glimpse the complex behavior of the neutrino internal dynamics and obtain confirmation of the existence of a preliminary neutrino trapping phase followed by a transparency era (Gusakov et al. 2004) from the neutrino telescopes on Earth (Yuksel & Beacom 2007). In addition, X-ray satellite measurements have also provided indications of the cooling sequence, for a catalog of isolated cooling NSs (see Vigano et al. 2013 and Yakovlev & Levenfish 1995). Although a global understanding of the extracted temperatures for these objects is still missing, the so-called minimal cooling mechanism has been successful at reproducing the trends of observed cooling curves (Page et al. 2004). When solving for the internal temperature profile $T(r,t)$ as a function of stellar radius $r$ and time $t$, one of the key ingredients that can dictate the energetic balance is the local energy emissivity, $Q_L = \frac{dE}{dt}$, i.e., the energy produced per unit volume per unit time, through a prescribed particle physics reaction.

In this work, we will be interested in obtaining astrophysical neutrino emissivities related to novel reaction channels involving DM undergoing self-annihilation processes inside the star. In particular, we focus on models in which DM particles communicate with the visible sector through a pseudoscalar mediator. These have been quoted to be well-motivated both from theoretical and from phenomenological grounds. Some of these models belong to a set of the so-called simplified type including Boehm et al. (2014), Wild (2016), Bauer et al. (2017), and Baek et al. (2017). As mentioned, they extend the SM by (at least) two particles, a DM candidate as well as a state that mediates the DM interactions with the visible sector, and are able to capture, with a minimal set of assumptions, some important features of more ultraviolet-complete (UV) theories while providing a (semi-)consistent
framework in order to analyze the experimental results (Banerjee et al. 2017).

In this setting, we will be interested in the dominant neutrino production processes, i.e., the s-wave process $\chi\chi \rightarrow \nu\bar{\nu}$ and the p-wave process $\chi\chi \rightarrow aa$, with subsequent decay $a \rightarrow \nu\bar{\nu}$. Although the previous reactions constitute the main neutrino emission channels in this model setting, additional reactions like, e.g., radiative $a$-emission or $\chi\chi \rightarrow aaa$ could also happen, but we will not consider them here as they are subdominant. As we will show, the two main reactions could provide a contribution to the standard astrophysical neutrino emissivities in NS environments of sizable magnitude at early times. The observability of such indirect effects caused by DM seems to be difficult nowadays, as it could be critically relying on the current and future X-ray and gamma satellites (NICER, eXTP, LOFT, ATHENA, CHANDRA).

2. Neutrino Emissivities from DM Annihilation

In this work we are interested in calculating neutrino emissivities from DM self-annihilation in dense and hot stellar interiors, i.e., that of a (proto-)NS. In order to carry out our calculation, we choose a model where DM particles interact with SM particles through a pseudoscalar mediator. These kinds of models are well-motivated, both from the theoretical and phenomenological point of view. With direct detection bounds being typically subleading in such scenarios, the main constraints arise from collider searches (meson bounds) and from indirect detection experiments (Banerjee et al. 2017). Examples recently used along this line include the coy DM model of Boehm et al. (2014) and others (Wild 2016; Baek et al. 2017; Bauer et al. 2017). Although popular, we must stress that these simplified models have some limitations, regarding construction itself, and when confronted with bounds from collider searches (Dolan et al. 2015; Goncalves et al. 2017).

We now introduce our concrete model realization. We consider a model where the SM field content is extended by a Dirac fermion, $\chi$, with mass $m_{\chi}$, which plays the role of a DM candidate, and a pseudoscalar field, $a$, with mass $m_{a}$, which mediates the interaction of ordinary and dark sectors. The interaction Lagrangian of the model reads

$$L_I = -i \frac{g_{\chi}}{\sqrt{2}} a \bar{\chi} \gamma_5 \chi - ig_0 \frac{g_f}{\sqrt{2}} \bar{f} \gamma_5 f,$$  \hspace{1cm} (1)

where $g_{\chi}$ is the DM-mediator coupling, $g_f$ corresponds to the couplings to the SM fermions, $f$, and $g_0$ is an overall scaling factor. From the usual schemes used for matter couplings when introducing Beyond-SM motivated physics we will restrict for simplicity to the so-called flavor-universal, which sets $g_f = 1$ for all SM fermions. Let us recall, however, that there are other schemes where $a$ couples either to quarks or leptons exclusively, and with a flavor structure that will be treated elsewhere.

Typically, in these models DM phenomenology is controlled by four parameters, $m_{\chi}$, $m_{a}$, $g_{\chi}$, and $g_0 g_f$. In the range of $m_{\chi} < m_{\text{Higgs}}$ and $m_{a} < m_{\chi}$, the relevant annihilation processes into two-body final states (Abdullah et al. 2014; Arina et al. 2015) are s-wave $\chi\chi \rightarrow f \bar{f}$ and p-wave $\chi\chi \rightarrow aa$. As a remark, it is worth mentioning that, as presented, the most straightforward UV-completion of this setup would be in the framework of the two Higgs doublet model or models involving even more extended scalar sectors. However, one should keep in mind that additional interactions with extra scalars arise at tree level and that can introduce important phenomenological model-dependent features (Haber & O’Neil 2011).

Despite the limitations of simplified models, in our particular realization it is reasonable to expect that the very light mediators will not distort the relic density predictions due to the presence of additional annihilation channels involving these extra scalars as discussed in Banerjee et al. (2017).

DM abundance in our universe is likely to be fixed by the thermal freeze-out phenomenon: DM particles, initially present in our universe in thermal equilibrium abundance, annihilate with one another until chemical equilibrium is lost due to the expansion of the universe. The present-day relic density of these particles is predictable and it has been measured by Planck (Ade et al. 2016) to be $\Omega_{\text{CDM}} h^2 = 0.1198 \pm 0.0015$.

Due to the pseudoscalar portal considered here, this model provides spin-dependent interactions with nucleons (N) at tree level. In this way, the $\chi$-N interaction considered in direct searches is suppressed because it is the momentum dependent, see Freytsis & Ligeti (2011), Cheng & Chiang (2012), and Gresham & Zurek (2014) for details. Instead, the spin-independent cross section is not present at tree level but the effective interaction at one-loop can be constructed (Ipek et al. 2014). Estimations of both cross sections in vacuum are given in Freytsis & Ligeti (2011). Both features regarding the behavior of the cross section impact the capability of the star to capture DM during the stage of the progenitor and in the collapsed configuration, although they can compensate each other in the star lifetime in order to have a finite meaningful amount of DM populating the object (Kouvaris & Tinyakov 2011).

Usual model analysis considers sets of parameters with a variety of bounds at a different level of significance. Here, in order to be definite, we will restrict our analysis to three different sets of flavor-universal parameters that are not in conflict with existing phenomenology to describe light DM ($m_{\chi} \lesssim 30$ GeV) interactions with ordinary matter. We consider constraints from direct detection experiments (Bertone et al. 2005), cosmological bounds (Zel’dovich 1965), and collider bounds (Dolan et al. 2015). The masses and couplings used in this work appear in Table 1.

| Model | $m_{\chi}$ [GeV] | $m_{a}$ [GeV] | $g_{\chi}$ | $g_0$ |
|-------|-----------------|--------------|-----------|-------|
| A     | 0.1             | 0.05         | $7.5 \times 10^{-3}$ | $7.5 \times 10^{-3}$ |
| B     | 1               | 0.05         | $1.2 \times 10^{-1}$ | $2 \times 10^{-3}$ |
| C     | 30              | 1            | $6 \times 10^{-1}$   | $5 \times 10^{-5}$ |

Note. a We use flavor-universal $g_f = 1$. 

| Parameters Used in This Work as They Appear in the Interaction Lagrangian in Equation (1) | Table 1 |

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we estimate the parameters using MicroOmegas (Belanger et al. 2010) and direct detection cross sections at one-loop level (Freytsis & Ligeti 2011; Ipek et al. 2014).

According to the current stage of exploration of the phase space of masses and cross sections for DM candidates interacting with nucleons in ordinary matter, dense compact stars are believed to be suitable places to find this kind of matter. NSs are believed to be efficient DM accretors (Gould 1987). One of the key quantities that can dictate their internal stellar energetic balance is the local energy emissivity, \( Q_E = \frac{dE}{dV dt} \) (energy produced per unit volume per unit time, through a prescribed particle physics reaction). In this work, we will be interested in the annihilation reactions of DM into twobody fermionic states \( (f) \), \( \chi \chi \rightarrow \bar{f} f \) and two pseudoscalar boson states \( \chi \chi \rightarrow a a \) with subsequent decay \( a \rightarrow \bar{f} f \). Furthermore, we will discuss possible astrophysical consequences particularizing to the \( f = \nu \) neutrino channel.

Formally, the expression for \( Q_E \) generically denotes the energy emission rate per stellar volume arising from fermionic or pseudoscalar pair production and can be written as (Esposito et al. 2002)

\[
Q_E = 4 \int d\Phi(E_1 + E_2) |\mathcal{M}|^2 f(f_1, f_2, f_3, f_4),
\]

with

\[
d\Phi = \frac{d^3p_1}{2(2\pi)^3E_1} \frac{d^3p_2}{2(2\pi)^3E_2} \frac{d^3p_3}{2(2\pi)^3E_3} \times \frac{d^3p_4}{2(2\pi)^3E_4} (2\pi)^4 \delta(p_1 + p_2 - p_3 - p_4),
\]

the 4-body \((12 \rightarrow 34)\) phase space element and \(|\mathcal{M}|^2\), the spin-averaged squared matrix element of the reaction considered. The additional factor \(f(f_1, f_2, f_3, f_4)\) accounts for the global phase space blocking factor due to the initial and final particle distribution functions, \( f_i \), \( i = 1, \ldots, 4 \) we will discuss below. \( \delta(\chi) \) is the four-dimensional delta function. We will denote \( p_1 = (E_1, p_1) \), \( p_2 = (E_2, p_2) \) as the incoming 4-momenta, while \( p_3 = (E_3, p_3) \), \( p_4 = (E_4, p_4) \) are the outgoing 4-momenta, respectively. The detailed associated Feynman diagrams are shown in Figure 1. Let us note that besides the quoted annihilation processes we consider, there may be additional pseudoscalar boson production s-wave \( \chi \chi \rightarrow a a \) (Abdullah et al. 2014), initial/final state radiation and internal bremsstrahlung processes \( \chi \chi \rightarrow \bar{f} f a \) or \( \chi \chi a \rightarrow \bar{f} f \) (Bell et al. 2017). However, since the cross sections for these processes are proportional to \( g_s^2 g_f^2 \) and \( g_s^2 g_f^2 \), respectively, they are subdominant in the case of a Dirac fermion DM candidate (Ibarra et al. 2013; Bringmann et al. 2017). Similarly, radiative \( a \)-production can arise from the SM particles’ interaction inside the star, but this process is found to be only relevant in the case of very light mediators \((\lesssim eV)\) like axions or Majorons (Farzan 2003; Sedrakian 2016).

Specifically, for the case of annihilation into fermionic pairs (left diagram in Figure 1) we label the emissivity as \( Q_E^{\bar{f} f} \). It includes the expression for the spin-averaged squared matrix element as

\[
|\mathcal{M}|^2 = \frac{g_s^2 g_f^2}{4} \frac{s^2}{(s - m_a^2)^2 + E_{[q]}^2 \Gamma^2}, \tag{4}
\]

where \( q^2 = s = (p_1 + p_2)^2 = (p_3 + p_4)^2 \) is the Mandelstam variable and \( E_{[q]} = \sqrt{|q|^2 + m_a^2} \). In this case

\[
f(f_1, f_2, f_3, f_4) = \frac{\Gamma}{E_{(E_3)(1 - f_f(E_3))(1 - f_f(E_4))},}
\]

and \( f_\chi, f_f \) are the local stellar distribution functions for DM and fermionic particles, respectively, containing density and temperature dependence we will discuss further below. \( \Gamma \) is the pseudoscalar particle decay width in the local medium through the reaction \( a \rightarrow \bar{f} f \). It is obtained using the optical theorem as

\[
\Gamma = \frac{1}{E_{[q]}} \text{Im} \Pi(q), \tag{6}
\]

where \( \Pi(q) \) is the pseudoscalar polarization insertion given by

\[
\Pi(q) = \frac{i g_f^2}{2} \int \frac{d^4k}{(2\pi)^4} \text{tr}[\gamma_5 G^0(k) \gamma_5 G^0(k + q)], \tag{7}
\]

and the corresponding cut of the associated tadpole diagram involves the fermion propagator \( G^0(k) \) including a vacuum and matter contribution (Chin 1977; Matsui & Serot 1982).

Using Equations (2) and (4), we can obtain an expression for the emissivity produced by the annihilation of DM particles into \( \bar{f} f \), \( Q_E^{\bar{f} f} \). Let us first deal with the integration over \( p_4 \) so that

\[
\int d^3p_3 \frac{2E_3(2\pi)^3}{2E_4(2\pi)^3} (2\pi)^4 \delta(p_1 + p_2 - p_3 - p_4) \tag{8}
\]

\[
= \int d(\cos \theta) d|\mathbf{p}_0 - E_3 - E_4| \frac{d^3|\mathbf{p}_0|}{4E_3E_4(2\pi)^3} d(\cos \theta) \delta(q_0 - E_3 - E_4),
\]

where \( \theta \) is the angle between \( \mathbf{p}_0 \) and \( \mathbf{q}_0 \), and \( q_0 = E_1 + E_2 \) for this annihilation channel. Besides, we can express the energy

\[
E_3(E_3 + q_0) = E_1(E_1 - q_0) = \frac{s}{2} = \frac{(p_1 + p_2)^2}{2} = \frac{(p_3 + p_4)^2}{2},
\]

\[
= \int d(\cos \theta) d|\mathbf{p}_0 - E_3 - E_4| \frac{d^3|\mathbf{p}_0|}{4E_3E_4(2\pi)^3} d(\cos \theta) \delta(q_0 - E_3 - E_4),
\]

\[
E_3(E_3 + q_0) = E_1(E_1 - q_0) = \frac{s}{2} = \frac{(p_1 + p_2)^2}{2} = \frac{(p_3 + p_4)^2}{2},
\]

\[
= \int d(\cos \theta) d|\mathbf{p}_0 - E_3 - E_4| \frac{d^3|\mathbf{p}_0|}{4E_3E_4(2\pi)^3} d(\cos \theta) \delta(q_0 - E_3 - E_4),
\]

\[
E_3(E_3 + q_0) = E_1(E_1 - q_0) = \frac{s}{2} = \frac{(p_1 + p_2)^2}{2} = \frac{(p_3 + p_4)^2}{2},
\]

\[
= \int d(\cos \theta) d|\mathbf{p}_0 - E_3 - E_4| \frac{d^3|\mathbf{p}_0|}{4E_3E_4(2\pi)^3} d(\cos \theta) \delta(q_0 - E_3 - E_4),
\]

\[
E_3(E_3 + q_0) = E_1(E_1 - q_0) = \frac{s}{2} = \frac{(p_1 + p_2)^2}{2} = \frac{(p_3 + p_4)^2}{2},
\]

\[
= \int d(\cos \theta) d|\mathbf{p}_0 - E_3 - E_4| \frac{d^3|\mathbf{p}_0|}{4E_3E_4(2\pi)^3} d(\cos \theta) \delta(q_0 - E_3 - E_4),
\]

\[
E_3(E_3 + q_0) = E_1(E_1 - q_0) = \frac{s}{2} = \frac{(p_1 + p_2)^2}{2} = \frac{(p_3 + p_4)^2}{2},
\]
\[ \delta(q_0 - E_3 - E_4) = \frac{\sqrt{m_\chi^2 + |q|^2 + |p_i|^2 - 2|p_i||q|\cos \theta}}{|p_i||q|} \times \delta(\cos \theta - \cos \theta_0) \Theta(q^2 \geq 4m_\chi^2), \]

where

\[ \cos \theta_0 = \frac{1}{2|p_i||q|}(q_0^2 - q_0^2 + 2q_0E_4), \]

and \( q^2 = q_0^2 - |q|^2 \). \( \Theta(x) \) is the Heaviside function. Equation (9) has been obtained using

\[ \delta[f(x)] = \sum_i \frac{\delta(x - x_0)}{|f'(x)|_{x_0}}, \]

with \( x_0 \) the zeros of \( f(x) \). Now, we use \( |p_i||d|p_i| = E_1dE_4 \). Imposing \( \cos^2 \theta_0 \leq 1 \), we obtain limits for the integration over \( E_4 \)

\[ E_4 \pm = \frac{1}{2} \left( q_0 \pm |q| \sqrt{1 - \frac{4m_\chi^2}{q^2}} \right). \]

In the same way, we use \( |p_i||d|p_i| = E_1dE_1 \) and \( |p_2||d|p_2| = E_2dE_2 \). After that, Equation (2) takes the form

\[
\begin{align*}
Q_E^\beta = & \frac{1}{2(2\pi)^5} \int_{m_\chi}^{\infty} dE_1 \int_{-E_1}^{E_1} dE_2 \int_{-E_2}^{E_2} dE_3 \int_{-E_3}^{E_3} dE_4 \\
& \times \int_{-1}^{1} \cos(\phi)q_0 \Theta(q^2 \geq 4m_\chi^2) \right. \\
& \times \int_{-1}^{1} \cos \theta \delta(\cos \theta - \cos \theta_0) f(f_1, f_2, f_3, f_4) \\
& \times \int |M_{\text{av}}| \frac{dE_4}{|q|},
\end{align*}
\]

where \( \phi \) is the angle between \( p_1 \) and \( p_2 \), \( E_3 = E_1 + E_2 - E_4 \),

\[ |q| = \sqrt{|p_i|^2 + |p_2|^2 + 2|p_i||p_2|\cos \phi}, \]

and \( |p_i| = \sqrt{E_1^2 - m_\chi^2} \), \( |p_2| = \sqrt{E_2^2 - m_\chi^2} \).

Instead of the DM annihilation into two pseudoscalars (middle and right diagrams in Figure 1), now the emissivity is labeled as \( Q_E^{\text{av}} \). In this case, when calculating the spin averaged matrix element one must note that

\[ |M_{\text{av}}|^2 = \frac{1}{2} \sum_{s,s'} |M_{s,s'}|^2, \]

where \( s \) and \( s' \) are the spin states of the DM particle. The squared matrix element finally reads,

\[
\frac{1}{2} \left( t - m_\chi^2 \right)^2 - m_\chi^2 \left( m_\chi^2 + 2m_\omega^2 \right) \\
+ \frac{(u - m_\chi^2)^2 - m_\chi^2 (m_\chi^2 + 2m_\omega^2)}{u - m_\chi^2} + 2m_\chi^2 - s \]

\[ \times \sin^2 \theta_3 \sin^2 \theta_3 \sin^2 \theta_3 |(k_1|k_2|p_3)\cos \theta_3 + (k_1|k_2|p_3)\cos \theta_3 | \cos \theta_3 | \cos \theta_3 |. \]

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where \( s = k^2 = (p_1 + p_2)^2 \), \( t = (p_1 - p_3)^2 = (p_4 - p_2)^2 \) and \( u = 2m_\chi^2 + 2m_\omega^2 - s - t \).

As we can see, now the matrix element not only depends on \( s \) but also on \( t \) and \( u \). Dealing with the integration to obtain the emissivity, it is convenient to write these variables as

\[ s = 2m_\chi^2 + 2E_1E_2 - 2|p_i||p_2| \cos \theta_12, \]

and

\[ t = m_\chi^2 + m_\omega^2 - 2E_1E_3 + 2|p_i||p_3| \cos \theta_13, \]

where \( \theta_j \) is the angle between \( p_j \) and \( p_i \).

In the same way that we did for the annihilation into fermions, we can write

\[ \int d^4p_3 \frac{1}{2E_3(2\pi)^2} \int d^4p_4 \frac{1}{2E_4(2\pi)^3} \delta(p_1 + p_2 - p_3 - p_4) \]

\[ = \int d^3p_1 \int d^3p_2 \frac{1}{4E_2E_4(2\pi)^2} \left[ \Theta(k_0 - E_3 - E_4) \right], \]

where we are denoting the four momentum \( k = (k_0, k) \) and \( \theta_i \) as the angle between \( p_i \) and \( k \). As obtained in Equation (9), we find

\[ \delta(k_0 - E_3 - E_4) = \frac{E_4}{|p_3||k|} \delta(\cos \theta_3 - \cos \theta_3,0). \]

being

\[ \cos \theta_3,0 = \frac{1}{2|p_3||k|}(|k|^2 + 2k_0E_3 - k_0^2). \]

Now, we can write the emissivity into two pseudoscalars as

\[ Q_{E}^{\text{av}} = \frac{1}{2(2\pi)^6} \int_{m_\chi}^{\infty} |k|d|k| \int_{m_\chi}^{\infty} \sqrt{E_2^2 - m_\omega^2} dE_2 \\
\times \int_{-1}^{1} \cos \theta_2 \frac{E_1 + E_2}{E_3} \Theta(k^2 - 4m_\omega^2) \\
\times \int_{E_1}^{E_3} dE_3 \int_{-1}^{1} \cos \theta_3 \delta(\cos \theta_3 - \cos \theta_3,0) \\
\times \int_{-1}^{1} \cos \theta_3 \delta(f(f_1, f_2, f_3, f_4)|M_{\text{av}}|^2, \]

where \( |p_1| = \sqrt{|k|^2 + |p_2|^2 - 2|k||p_2|\cos \theta_2} \), \( t = m_\chi^2 + m_\omega^2 - 2E_1E_3 + 2|p_3|( |k| \cos \theta_3 - |p_3| \cos \theta_3) \), and \( \cos \theta_23 = \cos \phi_3 \sin \theta_22 \sin \theta_21 + \cos \theta_2 \cos \theta_2 \cos \theta_2 \). We have used also the trigonometric relation \( |p_1| \cos \theta_3 = |k| \cos \theta_3 - |p_2| \cos \theta_23 \). The limits for the outgoing energy in the integral are

\[ E_3 \pm = \frac{1}{2} \left( k_0 \pm |k| \sqrt{1 - \frac{4m_\omega^2}{k^2}} \right). \]

In the case of annihilation into pseudoscalars the phase space factor reads

\[ f(f_1, f_2, f_3, f_4) = f_1(E_1)f_2(E_2)f_3(E_3)f_4(E_4). \]

In this case, one should also take into account the further decay of each pseudoscalar into fermionic pairs and the availability of kinematical phase space through and additional Pauli blocking factor. Although not explicit, there is also a further local dependence on the DM density in the distribution function that will be discussed later in the manuscript.
2.1. Dense and Hot Stellar Scenario

In order to explain the physical relevance of the quantities under scrutiny obtained in the previous section, at this point we will particularize to that of a dense and hot stellar scenario. We will focus on a (proto-)NS. Briefly, an NS is mostly constituted by nucleons forming a central core at a density in excess of nuclear saturation density, \( \rho_0 \sim 2.4 \times 10^{14} \text{ g cm}^{-3} \). An average NS has a radius \( R \lesssim 12 \text{ km} \) and mass \( M \approx (1-1.5) M_{\odot} \) (mostly in its core) being thus a star with large compactness ratio \( \sim M/R \). For the sake of our discussion, we will consider a typical baryonic core density value \( \rho_0 = \rho_{\text{NS}} \sim 2 \rho_0 \). Regarding internal temperature and composition, NSs are born as hot lepton-rich objects with temperatures \( T \sim 20 \text{ MeV} \) evolving into cold \( T \sim 10 \text{ keV} \) neutron-rich ones, after a deleptonization era. Assuming dark and ordinary matter has coupling strengths at the level of current experimental search bounds, NSs are believed to be capable of accreting (and retaining) DM particles whose masses are larger than a few GeV from an existing galactic distribution.

Accretion of a dark component will proceed not only during the collapsed stage but also during most of the previous progenitor stellar lifetime at different epoch-dependent capture rates, \( C_\chi \). First, in the progenitor stages, the progressively denser nuclear ash central core is effectively opaque to DM and allows build up of an internal finite DM number density over time, \( n_\chi(r) \), where \( r \) is the radial stellar coordinate. Briefly, the progenitor with a mass \( (10-15)M_{\odot} \) is able to fuse lighter elements into heavier ones and thus its composition changes through the burning ages. Hydrogen first, and later the He, C, O, and the rest of the heavier elements up to Si proceed through the burning stages. Spin-dependent (mostly from H) as well as spin-independent \( \chi-N \) cross sections allow the gravitational capture of DM population inside the star. Coherence effects may play a role for slowly moving, low \( m_\chi \) incoming DM particles scattering nuclei off when their associated de Broglie wavelength is comparable to the nuclear size, and in this case the spin-independent cross section bears a multiplicative factor \( \sim A^2 \), where \( A \) is the baryonic number. Since the later burning stages proceed rapidly, the He-C-O stage gives the main contribution to the DM capture in the progenitor. As the thermalization times during this set of stages can follow the internal dynamics the collapsed star will have as a result a nonzero, mostly inherited, initial DM population.

In detail, the DM particle population number inside the star, \( N_\chi \), will not only depend on the capture rate \( C_\chi \) (Gould 1987) but also on the self-annihilation rate, \( C_\alpha \). Note that in the range of masses in the parameter sets we consider, evaporation effects (Krauss et al. 1986) as well as decay (Perez-Garcia & Silk 2015) do not substantially modify the DM population as the kinetic to gravitational potential energy ratio remains small.

Then the DM particle number, \( N_\chi \), can be obtained as a function of time \( t \) by solving the differential equation

\[
\frac{dN_\chi}{dt} = C_\chi - C_\alpha N_\chi^2, \tag{25}
\]

considering the two competing processes, capture and annihilation (Kouvaris & Tinyakov 2010)

\[
N_\chi(t) = \frac{C_\chi}{C_\alpha} \tanh\left[ \frac{t}{\tau} + \gamma(N_\chi,0) \right], \tag{26}
\]

where

\[
\gamma(N_\chi,0) = \tanh^{-1}\left( \sqrt{\frac{C_\chi}{C_\alpha}} N_\chi,0 \right) \tag{27}
\]

and

\[
\tau^{-1} = \sqrt{C_\chi C_\alpha}. \tag{28}
\]

At \( t = 0 \), when the proto-NS is born, a typical progenitor may have already provided an initial population

\[
N_\chi,0 = 1.5 \times 10^{39} \left( \frac{\rho_\chi}{\rho_{\chi,0}} \right) \left( \frac{1 \text{ GeV}}{m_\chi} \right) \left( \frac{\sigma_0}{10^{-43} \text{ cm}^2} \right)^2, \tag{29}
\]

where \( \sigma_\chi \equiv \sigma_{\chi-N} \) is the \( \chi-N \) scattering cross section. As this quantity is currently unknown, only experimental constrains exist for it. In the range of DM masses used in this work \( \sigma_\chi \in [10^{-46} - 10^{-35}] \text{ cm}^{-2} \) (Kavanagh 2017). Equation (29) assumes that the majority of the NS population can be found at galactocentric distances of a few kiloparsecs where \( \rho_\chi \sim 10^2 \rho_{\chi,0} \). We use \( \rho_{\chi,0} \sim 0.3 \frac{\text{GeV}}{\text{cm}^3} \) as the solar-circle DM density value.

Let us mention that both capture and annihilation rates, will be intimately determined by the parameters of the model at hand, i.e., \( m_\chi, m_{\alpha}, g_0, g_\chi \) (we set \( g_\ell = 1 \)). In particular, the DM capture rate on the progenitor depends on the scattering cross section on nuclei (nucleons) that is proportional to the product of the couplings \( (\sim g_\ell^2 g_\chi^2) \) and the annihilation cross section proportional to the sum of \( (\sim g_0^2 g_\chi^2) \) and \( (\sim g_\ell^4) \) terms for the two reactions considered \( \chi\chi \rightarrow \ell\ell \) and \( \chi\chi \rightarrow aa \), respectively (Buckley et al. 2015).

For the three models considered in this work appearing in Table 1, the average progenitor capture rate allows a nonvanishing initial DM population, \( N_\chi,0 \). The annihilation rate, proportional to \( n_\chi^2(r) \), is negligibly small at that stage. Later, in the NS collapsed state and at a given galactic location with a corresponding ambient DM density \( \rho_\chi \), the capture rate, \( C_\chi \), is approximated up to factors of the order of unity by the expression (Gould 1987; de Lavallaz & Fairbairn 2010).

\[
C_\chi \simeq 1.8 \times 10^{25} \left( \frac{1 \text{ GeV}}{m_\chi} \right) \left( \frac{\rho_\chi}{\rho_{\chi,0}} \right) f_{\chi,N} \text{ s}^{-1}. \tag{30}
\]

A few remarks are due regarding this expression. \( f_{\chi,N} \) denotes a phenomenological factor dealing with the opacity of stellar matter. \( f_{\chi,N} \) depends on the ratio of the leading contribution of \( \chi-N \) scattering cross section \( \sigma_0 \) to the minimum geometrical cross section of an NS made of nucleons of mass \( m_N \) and defined as

\[
\sigma_0 = \frac{m_N R^2}{M} \sim 10^{-45} \text{ cm}^2. \tag{31}
\]

Thus this factor saturates to unity, \( f_{\chi,N} \sim 1 \), if \( \sigma_\chi \gtrsim \sigma_0 \). Otherwise, \( f_{\chi,N} \sim \frac{\sigma_\chi}{\sigma_0} \). Using Boehm et al. (2014) and Appendix D in Dolan et al. (2015), we consider the scattering cross section (at one-loop) in the appropriate kinematical limit in our compact star so that for the parameters used in this work \( f_{\chi} \) are effectively in the saturated regime.

The expressions in the literature for DM capture rates in dense objects are based on interactions with quarks (nucleons)
that in practice happen via a contact term (Freytsis & Ligeti 2011), possibly including form factors. Note that a more elaborate treatment would involve the calculation of the nonrelativistic limit of the (full) series of operators included in the Lagrangian under study. Such a detailed analysis is beyond the scope of this work and remains to be done. The usual phenomenological treatment, through the $f_{\chi} N$ factor, makes use of a lower bound to the global cross section with all relevant contributions in this realization picture. It is important to emphasize that the strength of the computed emissivity will depend on the number of DM particles remaining inside the star at any given time.

As thermalization times for DM particles in the light mass range we consider are consistently smaller than dynamical cooling times (Goldman & Nussinov 1989), inside the star the DM particle number density takes the form

$$n_{\chi}(r) = n_{0,\chi} e^{-\frac{m_{\chi}}{k_B T} r},$$

where $n_{0,\chi}$ is the central value, $T$ is the NS temperature, and $k_B$ is the Boltzmann constant. The gravitational potential is given by

$$\Phi(r) = \int_0^r \frac{GM(r')dr'}{r'^2},$$

where $M(r')$ is the NS mass inside a spherical volume of radius $r'$. So that assuming an approximately constant density core,

$$n_{\chi}(r) = n_{0,\chi} e^{-\frac{r}{r_H}},$$

with a thermal radius

$$r_H = \frac{3k_B T}{2\pi \rho_{\chi} m_{\chi}}.$$

Normalization requires $\int_0^R n_{\chi}(r) dV = N_{\chi}$ at a given time, as reflected by Equation (26). Note that potential limiting values of $N_{\chi}$ may arise from the fact that a fermionic $\chi$ would involve the existence of a Chandrasekhar critical mass for collapse (MacDermott et al. 2012). This possibility is safely not fulfilled as long as $N_{\chi}(t) < N_{\text{Ch}}$, where $N_{\text{Ch}} \sim (M_{\text{Pl}}/m_{\chi})^3 \approx 1.8 \times 10^{36} (1 \text{ GeV}/m_{\chi})^3$ with $M_{\text{Pl}}$ the Planck mass.

Let us now comment on the fact that inside the star the tiny DM fraction can be described by a distribution function of a classical Maxwell–Boltzmann type

$$f_{\chi} = f_{\chi}^{MB}(|p_i|, r) = \left(\frac{1}{2\pi m_{\chi} k_B T}\right)^{\frac{3}{2}} n_{\chi}(r) e^{-\frac{|p_i|^2}{2m_{\chi} k_B T}}, i = 1, 2,$$

and in the nonrelativistic scheme $E_i = \frac{p_i^2}{2m_{\chi}}, i = 1, 2$. The annihilation rate, $C_\alpha$, depends on the thermally averaged annihilation cross section inside the star, $(\sigma_{\alpha} \nu)$, for the two reactions considered in this work, see Figure 1. Therefore, the stellar $\chi$-distribution contained in the thermal volume region $\sim r_H^3$ determines the annihilation rate $C_\alpha \sim (\sigma_{\alpha} \nu)/V_{\text{th}}$ (Arina et al. 2015; Goncalves et al. 2017). Note that the presence of the phase space factor $(f_1 f_2 f_3 f_4)$ in Equation (2) will introduce further DM density and $T$ dependence into the vacuum standard calculation as a thermalized DM distribution exists inside the NS core. As for the outgoing fermions, the medium density effects will generally arise from the phase space blocking factors and collective effects (Cermeño et al. 2016a). In the case of neutrinos, we assume $f_{\nu} \sim 0$, although in cases where a trapped fraction $Y_{\nu} > 0$ exists it would further decrease the response.

### 3. Results

In this section, we explain our results regarding the emissivities in the NS astrophysical scenario particularizing to the case in which the final state fermions produced in the reactions depicted in Figure 1 are neutrino pairs. Neutrinos are weakly interacting SM fermions known to play a key role in the internal energy; dynamics of a massive stellar progenitor undergoing gravitational collapse. In such an event, most of the gravitational binding energy is emitted into neutrinos (and antineutrinos) of the three families. A very efficient cooling scenario emerges in the first $\sim 10^5$ years. Standard processes such as those present in the URCA or the modified URCA (MURCA) cooling (Friman & Maxwell 1979; Yakovlev et al. 2005) among others can release neutrinos with associated emissivities $Q_{E,\text{URCA}} \sim 10^{27} R (T/0.1 \text{ MeV})^6 \text{ erg cm}^{-3} \text{ s}^{-1}$ and $Q_{E,\text{MURCA}} \sim 10^{27} R (T/0.1 \text{ MeV})^8 \text{ erg cm}^{-3} \text{ s}^{-1}$, respectively. Typical energetic scales can be obtained from the conversion factor $1 \text{ MeV} \sim 10^{10} \text{ K}$. $R$ is a reduction function of the order of unity describing the superfluid effects in the neutron and proton branches of those reactions (Yakovlev & Levenfish 1995). We must keep in the mind the fact that these neutrinos effectively cool off the star as they leave, having scattered a few times with ordinary nucleon matter (Horowitz & Perez-Garcia 2003; Perez-Garcia 2010) after a first rapid trapping stage. In this way, processes with neutrino production in reactions involving nucleon components effectively release energy from the baryonic system as the associated neutrino mean-free path is relatively long $\lambda \sim 28 \text{ cm}(100 \text{ MeV}/E_{\nu})^3$. In analogy with what happens at the standard neutrino trapping stage in very young stars, when neutrinos have energies of dozens of MeV, it is expected that energetic neutrinos produced in reactions of DM annihilation could have mean-free paths that are very small, even at low stellar temperatures (in evolved stars) so they may not escape the dense medium so easily (Kouvaris 2008).

In Figure 2, the logarithm (base 10) of the energy emissivity for the process $\chi \chi \rightarrow \nu \bar{\nu}$ is shown as a function of temperature for the three sets of DM parameters $A$, $B$, and $C$ in Table 1, with dashed, dotted, and dashed–dotted lines, respectively. Baryonic density is fixed at $2\rho_0$. We also fix (for reference) the assumed number of DM particles at initial instant $N_{\chi} = N_{0,\chi}$. Note, however, that $N_{\chi}$ is time (and model) dependent as it rapidly decreases when the self-annihilation sets in. We give below a suitable fit where the actual $T$ and $N_{\chi}$ dependence is reflected. The baryonic density dependence is, however, weak. The standard physics cooling is depicted here by the MURCA emissivity (solid line) for the sake of comparison. Although the latter is not the only process that could possibly contribute to the effective standard cooling, all other processes capable of contributing are considered weaker at the temperature and density conditions considered in this work. Thus we take the standard processes to be represented by an upper limit to the currently used emissivities chosen as the MURCA processes. Note that we do not consider exotic meson condensates nor do we consider URCA emissivities, since stellar central densities required are usually higher than the one taken as reference here in order to provide the $Y_{\nu} \sim 11\%-15\%$ proton fraction.
the fast reaction. Furthermore, we assume that a possible neutrino trapping phase will not be significant, particularly at low $T$. However, at high $T$ it may produce a further reduction that has to be accounted for through a Pauli blocking factor. It must be included to take into account the time dependent nonvanishing leptonic fraction of the order of $Y_{\ell} \sim 0.1$ (Pons et al. 1999) until transparency sets in at $\sim 20$ s.

The trends depicted in Figure 2 with temperature and DM particle population dependence for models A, B, and C and for both reaction channels can be fit as

$$Q_E(T, N_\chi) = Q_0 \left( \frac{N_\chi}{N_{0,\chi}} \right)^2 \left( \frac{T}{1 \text{ MeV}} \right)^{-3}. \quad (37)$$

In Table 2, we give values for parameters $Q_0$ and $N_{0,\chi}$ for the reactions and models considered. We can see that around $T \sim 0.1$ MeV standard emissivities $\log_{10}(Q_E) \sim 21$ are as powerful as those from the DM annihilation processes in the thermal volume region $v_{th} \sim n_{th}$. However, since DM population is a decreasing function of time, one can expect that there will be a minimal number of $N_\chi$ particles to beat the MURCA processes for $T < 0.1$ MeV. We find $Q_E(T, N_\chi) > Q_{\text{MURCA}}$ for $T \in [0.01, 0.1]$ MeV for $N_\chi/N_{0,\chi} \gtrsim 10^{-3}$, $3.6 \times 10^{-6}$, $5.6 \times 10^{-6}$ for A, B, and C models, respectively. One should note that the $N_\chi$ self-consistently depends on temperature and how it dynamically changes with time. A fully detailed cooling simulation would yield the temporal sequence to determine the complete behavior. As this is not the goal here, we give instead an estimate on the time duration of the dominance of the DM annihilation channel, i.e., where it could beat the local MURCA processes from Equation (26). We obtain $t \lesssim 50$ s for models A and B while this condition is true at all times for model C. We note that all timescales are thus overlapping the standard transparency window for SM neutrinos.

In Figure 2, the logarithm (base 10) is shown for the reaction $\chi \chi \rightarrow \nu \nu$ with subsequent decay $\nu \rightarrow \nu \nu$. The number of DM particles is also fixed $N_\chi = N_{0,\chi}$ for reference using the same argument as with the $\chi \chi \rightarrow \nu \nu$ reaction in Figure 2. In this case, for a population $N_{0,\chi}$, the neutrino emissivity is largely enhanced with respect to the direct production of neutrinos $\chi \chi \rightarrow \nu \nu$. For model C (dashed–dotted line), $Q_E$ matches and surpasses the standard MURCA emission below $T \sim 0.5$ MeV, while for models B (dotted line) and A (dashed line) that happens for $T \sim 0.3$ MeV and $T \sim 0.1$ MeV, respectively. Values for the phenomenological fit in this channel are also provided in Table 2.

If we now consider the running character of DM population number as in the previous case we find $Q_E(T, N_\chi) > Q_{\text{MURCA}}$ in the interval $T \in [0.01, 0.1]$ MeV for $N_\chi/N_{0,\chi} \gtrsim 3 \times 10^{-5}$ and model A, while for model B $Q(T, N_\chi) > Q_{\text{MURCA}}$ in $T \in [0.01, 0.3]$ MeV when $N_\chi/N_{0,\chi} \gtrsim 5 \times 10^{-8}$. Finally $Q(T, N_\chi) > Q_{\text{MURCA}}$ in $T \in [0.01, 0.5]$ MeV for $N_\chi/N_{0,\chi} \gtrsim 3 \times 10^{-10}$ for model C. This last ratio for model C is achieved during the entire lifetime of the star while not for the other cases. For the biquasars production reaction and at the thermodynamical conditions in the scenario considered we obtain that typical values obtained for the $\alpha$-decay length are of the order of $\sim 10^2$ fm, making it a negligible contribution to the neutrino transport as their decay length is so tiny compared to stellar size.

At this point, it is worth noting that tighter restrictions on the validity of the coupling of DM to $u$–d–s quarks coming from including complementary experimental bounds, e.g., rare meson decays, could somewhat reduce the validity of models A and B. In addition, from isospin considerations, the $\chi$ coupling to neutrons and protons in the NS will also somewhat affect the results as the proton-to-neutron ratio inside the NS core is smaller than unity ($\sim 1/9$). As the ratio of coupling fulfills $|g_\chi/g_\nu| > 1$ when considering flavor-universal fermion couplings (Dolan et al. 2015) we expect
that the computed emissivities could be increased by a factor of \( \sim 10-100 \).

We have considered the local emissivities of the novel reaction involving self-annihilating matter in the thermal volume. We must emphasize that since there is no uniform distribution of DM inside the star, neutrinos being produced from nuclear reactions in the majority of the core volume will wash out the dark contribution early, when the temperature is high enough. However, later, as temperature decreases there is an effective competition of the very efficient dark central engine (located in a few percent of the core volume) and the colder core emission.

The radial extent of the DM annihilating inner region is correlated to the ratio of the thermal radius to the NS radius. It is defined as \( \xi = \sqrt{2} r_\text{th}/R \) and indicates the radial fraction where DM particles can be found. Since the crust region has a tiny mass, we will not consider this refinement here (Cermeño et al. 2016b). For the parameterizations A, B, and C analyzed in this work this ratio takes values of, e.g., \( \xi \in [0.03, 0.42] \) at \( T \sim 1 \text{ MeV} \), \( \xi \in [0.007, 0.11] \) at \( T \sim 0.1 \text{ MeV} \) and \( \xi \in [0.003, 0.04] \) at \( T \sim 0.01 \text{ MeV} \). The volume where the dark emitting region resides shrinks as \( \sim \sqrt{T} \).

As has been thoroughly studied, enhanced emissivities in the medium can have an impact on internal temperatures, temporal cooling sequence, and (un)gapped matter phases (Page & Reddy 2006; Page et al. 2013). In this regard, recent works (Page et al. 2011; Shternin et al. 2011) quote that the rapid cooling of the Cas A may be an indication of the existence of global neutron and proton superfluidity in the core. In addition, current observations of thermal relaxation of NS crusts indicates that even a small stellar volume fraction where fast neutrino emission reactions can take place would provide distinctive features. In detail, it has been shown (Brown et al. 2018) that even if there is a relatively small local volume where distortion from the standard energetic mechanisms is taking place inside the star, a fast neutrino reaction (Direct URCA) in a volume of \( \sim 1\% \) could explain the neutrino luminosities in the cooling curve of some particular objects like MXB 1659-29.

In the case presented in this work the long-term dark engine reaction \( \chi \chi \rightarrow aa \) could provide emissivities \( Q_{\text{em}}^{\chi} \sim 4 \times 10^{22} \text{erg cm}^{-3} \text{s}^{-1} \) for which the result is higher than that estimated for the \( Q_{\text{MXB1659-29}}^{\chi} \sim 1.7 \times 10^{21} \text{erg cm}^{-3} \text{s}^{-1} \) for \( T \sim 10^{8} \text{K} \). The stellar volume affected in the annihilating DM mechanism is, nevertheless, much smaller for this range of temperatures but still providing the same powerful emission. Besides the process discussed in this work, other ones such as rotochemical heating (Fernández & Reisenegger 2005) or hot blobs located at different depths in the crust in young NS (Kaminker et al. 2014) have been also treated in the literature adding more sources of energetic variability based on SM matter.

It remains for further work to explore more exhaustively the precise relation between the model parameters \( m_\chi, m_a, g_0, g_\chi \) (and \( g_\beta \)) and the energetic efficiency of the emission. This will impact the duration of the dominance of such emission from DM annihilation over standard processes and thus its potential observability. We believe that the qualitatively different picture arising from the DM self-annihilation process inside NS may be worthwhile to explore.

4. Conclusions

We have calculated the energy emissivity of self-annihilating DM from an existing stellar distribution into final state SM fermions. A pseudoscalar-mediated DM interaction with the ordinary nucleon matter has been used. Later, as an astrophysically relevant case, we have particularized to neutrinos as final states, and we have considered in detail those produced from s-wave channels \( \chi \chi \rightarrow \nu \nu \) or via pseudoscalar mediators p-wave \( \chi \chi \rightarrow aa \), and subsequent decay \( a \rightarrow \nu \nu \). In the inner stellar regions the radiation engine can encompass about \( \lesssim 1\% \) of the total stellar volume for \( T \lesssim 10^{10} \text{K} \) and the energy emissivity can be enhanced by orders of magnitude compared to the MURCA standard neutrino processes for parameter sets respecting constraints of direct detection limits, cosmological bounds or even tighter rare meson decay bounds. We have provided a phenomenological fit of emissivities including dependence of temperature and DM particle number. Taking as reference the usual standard temporal sequence of NS cooling behavior, we expect that, for the models analyzed in this work, model C (with \( m_a = 30 \text{ GeV}, m_a = 1 \text{ GeV} \)) could be effectively active during the whole life of the star. Although a detailed solution of the full evolution equation is out of the scope of this work it is reasonable to foresee that the contribution of this new dark mechanism to the set of already known standard cooling reactions will drive the star into internal dynamical self-adjustment that is likely to emerge with a distinctive temperature sequence whose observability remains to be properly analyzed in future works.

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