Branching Fractions of $\tau$ Leptons to Three Charged Hadrons

R. A. Briere,¹ G. P. Chen,¹ T. Ferguson,¹ G. Tatischevili,¹ H. Vogel,¹ N. E. Adam,² J. P. Alexander,² K. Berkelman,² V. Boisvert,² D. G. Cassel,² P. S. Drell,² J. E. Duboscq,² K. M. Ecklund,² R. Ehrlich,² R. S. Galik,² L. Gibbons,² B. Gittleman,² S. W. Gray,² D. L. Hartill,² B. K. Heltsley,² L. Hsu,² C. D. Jones,² J. Kandaswamy,² D. L. Kreinick,² A. Magerkurth,² H. Mahlke-Krüger,² T. O. Meyer,² N. B. Mistry,² J. R. Patterson,² D. Peterson,² J. Pivasri,² S. J. Richichi,² D. Riley,² A. J. Sadoff,² H. Schwarhoff,² M. R. Shepherd,² J. G. Thayer,² D. Urner,² T. Wilksen,² A. Warburton,² M. Weinberger,² S. B. Athar,³ P. Avery,³ L. Breva-Newell,³ V. Potlia,³ H. Stoeck,³ J. Yelton,³ K. Benslama,⁴ B. I. Eisenstein,⁴ G. D. Gollin,⁴ I. Karliner,⁴ N. Lowrey,⁴ C. Plager,⁴ C. Sedlack,⁴ M. Selen,⁴ J. J. Thaler,⁴ J. Williams,⁴ K. W. Edwards,⁵ D. Besson,⁶ X. Zhao,⁶ S. Anderson,⁷ V. V. Frolov,⁷ D. T. Gong,⁷ Y. Kubota,⁷ S. Z. Li,⁷ R. Poling,⁷ A. Smith,⁷ C. J. Stepaniak,⁷ J. Urheim,⁷ Z. Metreveli,⁸ K.K. Seth,⁸ A. Tomaradze,⁸ P. Zweber,⁸ S. Ahmed,⁹ M. S. Alam,⁹ J. Ernst,⁹ L. Jian,⁹ M. Saleem,⁹ F. Wappler,⁹ K. Arms,¹⁰ E. Eckhart,¹⁰ K. K. Gan,¹⁰ C. Gwon,¹⁰ K. Honscheid,¹⁰ D. Hufnagel,¹⁰ H. Kagan,¹⁰ R. Kass,¹⁰ T. K. Pedlar,¹⁰ E. von Toerne,¹⁰ M. M. Zoeller,¹⁰ H. Severini,¹¹ P. Skubic,¹¹ S.A. Dytyman,¹² J.A. Mueller,¹² S. Nam,¹² V. Savinov,¹² J. W. Hinson,¹³ J. Lee,¹³ D. H. Miller,¹³ V. Pavlunin,¹³ B. Sanghi,¹³ E. I. Shibata,¹³ I. P. J. Shipsey,¹³ D. Cronin-Hennessy,¹⁴ A.L. Lyon,¹⁴ C. S. Park,¹⁴ W. Park,¹⁴ J. B. Thayer,¹⁴ E. H. Thorndike,¹⁴ T. E. Coan,¹⁵ Y. S. Gao,¹⁵ F. Liu,¹⁵ Y. Maravin,¹⁵ R. Stroynowski,¹⁵ M. Artuso,¹⁶ C. Boulahouache,¹⁶ S. Blusk,¹⁶ K. Bukin,¹⁶ E. Dambsuren,¹⁶ R. Mountain,¹⁶ H. Muramatsu,¹⁶ R. Nandakumar,¹⁶ T. Skwarnicki,¹⁶ S. Stone,¹⁶ J.C. Wang,¹⁶ A. H. Mahmoor,¹⁷ S. E. Csorna,¹⁸ I. Danko,¹⁸ G. Bonvicini,¹⁹ D. Cinabro,¹⁹ M. Dubrovin,¹⁹ S. McGee,¹⁹ A. Bornheim,²⁰ E. Lipeles,²⁰ S. P. Pappas,²⁰ A. Shapiro,²⁰ W. M. Sun,²⁰ and A. J. Weinstein²⁰

(CLEO Collaboration)

¹Carnegie Mellon University, Pittsburgh, Pennsylvania 15213
²University of Florida, Gainesville, Florida 32611
³University of Illinois, Urbana-Champaign, Illinois 61801
⁴Carleton University, Ottawa, Ontario, Canada K1S 5B6 and the Institute of Particle Physics, Canada M5S 1A7
⁵University of Kansas, Lawrence, Kansas 66045
⁶University of Minnesota, Minneapolis, Minnesota 55455
⁷Northwestern University, Evanston, Illinois 60208
⁸State University of New York at Albany, Albany, New York 12222
⁹Ohio State University, Columbus, Ohio 43210
¹⁰University of Oklahoma, Norman, Oklahoma 73019
¹¹University of Pittsburgh, Pittsburgh, Pennsylvania 15260
¹²Purdue University, West Lafayette, Indiana 47907
¹³University of Rochester, Rochester, New York 14627
¹⁴Southern Methodist University, Dallas, Texas 75275
¹⁵Syracuse University, Syracuse, New York 13244
¹⁶University of Texas - Pan American, Edinburg, Texas 78539
Abstract

From electron-positron collision data collected with the CLEO detector operating at CESR near $\sqrt{s}=10.6$ GeV, improved measurements of the branching fractions for $\tau$ decays into three explicitly identified hadrons and a neutrino are presented as $B(\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_\tau) = (9.13 \pm 0.05 \pm 0.46)\%$, $B(\tau^- \rightarrow K^- \pi^+ \pi^- \nu_\tau) = (3.84 \pm 0.14 \pm 0.38) \times 10^{-3}$, $B(\tau^- \rightarrow K^- K^+ \pi^- \nu_\tau) = (1.55 \pm 0.06 \pm 0.09) \times 10^{-3}$, and $B(\tau^- \rightarrow K^- K^+ \pi^- \nu_\tau) < 3.7 \times 10^{-5}$ at 90% C.L., where the uncertainties are statistical and systematic, respectively.

PACS numbers: 13.35.Dx
For hadronic $\tau$ decays, final states with kaons provide a powerful probe of the strange sector of the weak charged current. In this Letter, we present the improved measurements of branching fractions for $\tau^- \to \pi^-\pi^+\pi^-\nu_\tau$, $K^-\pi^+\pi^-\nu_\tau$, and $K^-K^+\pi^-\nu_\tau$ decays, and an improved upper limit for the phase space suppressed and Cabibbo-suppressed decay $\tau^- \to K^-K^+\pi^-\nu_\tau$. (Charge conjugate decays are implied). The decay mode $\tau^- \to K^-\pi^+\pi^-\nu_\tau$ has a significant contribution to the overall strange spectral function which can provide a direct determination of the strange quark mass and, potentially, precision extraction of the CKM element $V_{us}$ \cite{1}. The decay $\tau^- \to K^-K^+\pi^-\nu_\tau$ can proceed via both the vector and axial-vector currents \cite{2} and, therefore, has a sensitivity to the Wess-Zumino anomaly \cite{3}. The data used for this analysis were collected with the CLEO III detector \cite{4} located at the symmetric $e^+e^-$ Cornell Electron Storage Ring (CESR). The data sample consists of 3.26 fb$^{-1}$ taken on or near the $\Upsilon(4S)$, corresponding to $2.97 \times 10^6 \tau^+\tau^-$ pairs. The CLEO III detector configuration features a new four-layer silicon strip vertex detector, a new wire drift chamber, and, most importantly for this analysis, a ring imaging Cherenkov (RICH) particle identification system. Particle trajectories, momenta, and charges are measured with the tracking system, which uses hits from both the silicon detector and drift chamber. The specific ionization, $dE/dx$, measured in the drift chamber's 16 inner axial and 31 outer stereo layers is sensitive to the traversing particle's mass. The RICH detector \cite{5} surrounds the drift chamber, and uses 1 cm-thick LiF radiators to generate Cherenkov photons from the incident charged particles. These photons then propagate through a 20 cm-thick expansion volume of gaseous nitrogen at atmospheric pressure, and are detected by multi-wire proportional chambers filled with a mixture of triethylamine (TEA) and CH$_4$ gases, and localized by readout from 8 mm-square cathode pads located on a cylinder of $\sim$1 m radius. RICH particle identification is available over the central region of the detector, $|\cos \theta| < 0.83$, where $\theta$ is the polar angle with respect to the direction of the incident positron beam. A detailed description of the RICH performance can be found in Ref. \cite{6}. The electromagnetic calorimeter surrounds the RICH detector and measures the energy, position, and lateral shape of showers induced by charged and neutral particles. It contains 7784 16-radiation-length-long CsI(Tl) crystals, arranged in a barrel section ($|\cos \theta| < 0.83$) and two endcaps (0.83 $< |\cos \theta| < 0.95$). These components all operate inside a superconducting solenoid coil which creates a uniform magnetic field of 1.5 T. A muon detection system surrounds the solenoid coil with 1 m of iron absorber interspersed with Iarocci tube wire chambers operated in proportional mode.

We combine RICH and $dE/dx$ information to determine if a track appears more consistent with a pion or kaon identity. The deviation of the measured $dE/dx$ for any track from that expected under particle hypothesis $i$ ($i = e, \mu, \pi, K, p$) at that momentum, in units of the expected Gaussian width of the distribution, is defined as $\delta_i$. The $dE/dx$ resolution is about 6% for hadrons. For each detected charged particle track, the RICH detector response is condensed into a $\chi_i^2$-like variable for each particle hypothesis. The value of $\chi_i^2$ is derived from the number $N_i^\gamma$ of detected Cherenkov photons and their locations relative to the Cherenkov cone expected for a particle with that momentum and mass. Pions and kaons are distinguished from one another with the combined RICH-$dE/dx$ variable $\Delta \chi^2 = \chi_{\pi}^2 - \chi_{K}^2 + \delta_{\pi}^2 - \delta_{K}^2$. We identify a track as a pion (kaon) if $|\cos \theta| < 0.83$, $N_{\gamma}^\pi(N_{\gamma}^K) \geq 3$, $\Delta \chi^2 < (>)0$, and apply these criteria to three-prong-side tracks. For the pion in $\tau^- \to K^-K^+\pi^-\nu_\tau$, $|\delta_{\pi}| < 3.0$ alone is used, yielding $\sim$10% higher efficiency from a looser criterion as well as the region outside the RICH acceptance, 0.83 $< |\cos \theta| < 0.93$. The consequently higher $K$-fakes-$\pi$ rate is unimportant for this mode due to the dearth of three-kaon events.
We take advantage of the copious cascade decays $D^{*+} \to D^0\pi^+$ with $D^0 \to K^-\pi^+$, in which the charged kaon and pion can be tagged kinematically without reference to RICH or $dE/dx$ information, to measure the probability for pions and kaons to be correctly or incorrectly identified. This method measures the area above background of the $K^-\pi^+$ mass peak with and without the particle identification criteria to determine the efficiency and fake rates for both pions and kaons. We find that the efficiency for pion and kaon identification ranges from 80–95% over most of the momentum range of interest for this analysis (0.5–3 GeV/c), and that the probability for a pion to fake a kaon or vice versa ranges from 1–2% for momentum values of 0.5–2 GeV/c and rises to about 10–15% for momenta around 3 GeV/c, as shown in Fig. 1.

![Figure 1](image_url)

**FIG. 1:** Kaon (solid circles) and pion (open circles) identification efficiencies (top) and fake rates (bottom) as a function of their momenta for tracks already within $|\cos \theta| < 0.83$ as determined from $D^0 \to K^-\pi^+$ decays. Error bars are statistical only.

Events are required to have four well-measured charged particles in a one-versus-three topology (the two hemispheres being defined by the event thrust axis) and zero net charge. We use 1-prong $\tau$ leptonic ($e/\mu$) or hadronic decays ($\rho/\pi$) to “tag” the event. An electron tag requires the lone track to have $\delta_e > -2$ and $E/p$, the ratio of energy deposited in the calorimeter to track momentum, to satisfy $0.85 < E/p < 1.1$. These criteria attain $\sim 95\%$ efficiency and a pion-faking-electron probability less than 1%. A muon tag must have the lone track penetrate at least three (if $p < 2$ GeV/$c$) or five (if $p > 2$ GeV/$c$) absorption
lengths of material, which achieves 80–90% efficiency and a few percent pion-faking-muon probability for $p > 1$ GeV/c.

If the tag-side track is not identified as an electron or a muon, tag-side calorimeter showers are then examined. If the invariant mass of the lone track and showers in the tagging hemisphere not matched to that track is below 0.5 GeV/$c^2$, the event is classified as $\pi$-tag. To establish a $\rho^- (\rightarrow \pi^- \pi^0)$-tag, we require a $\pi^0 \rightarrow \gamma \gamma$ candidate on the 1-prong side. For photon candidates, we select showers which do not match the projection of any charged track trajectories into the calorimeter, have energies exceeding 30 (50) MeV in the barrel (endcaps), and have compact lateral profiles consistent with those expected from electromagnetic showers. At least one photon from any $\pi^0$ candidate decay must be located in the barrel. We take the most energetic $\gamma \gamma$ pair which has invariant mass within $(-3.0, 2.5)$ standard deviations of $m_{\pi^0}$ (typically a window $\sim 30$ MeV/$c^2$ wide). After kinematically constraining the $\gamma \gamma$ pair to $m_{\pi^0}$, the invariant mass of this fitted $\pi^0$ candidate and the associated charged track, assigned the pion mass, is required to be consistent with the $\rho$ mass: $0.5 < m(\pi^- \pi^0) < 1.0$ GeV/$c^2$.

To suppress backgrounds with one or more neutral particles, we do not allow any shower in the event unassociated with a charged track or a $\pi^0$ participating in $\rho$-tagging with energy exceeding 100 MeV. After the event selection, the backgrounds with extra neutrals contribute 4.1%, 2.1% and 2.6% of the total observed events for the channels with 0, 1 and 2 kaons, respectively. In order to reject two-photon backgrounds (characterized by the missing momentum along the beam direction and low visible energy), the missing momentum must point into the CLEO detector ($|\cos \theta_{\text{miss}}| < 0.95$) and the visible energy must exceed 20% of the $e^+e^-$ center-of-mass energy. For all modes, we further demand that the three-prong mass, calculated using mass assignments determined from particle identification, lie below the $\tau$ mass. For the decay $\tau^- \rightarrow K^- \pi^+ \pi^- \nu_\tau$, a veto of $K_S^0$ candidates with $K_S^0 \rightarrow \pi^+ \pi^-$ within 10 MeV/$c^2$ of the $K_S^0$ nominal mass and a production vertex more than 1 cm from the primary interaction point is applied. Any $K_S^0$ content in both modes with two or more pions is treated as background, not signal.

Efficiencies and the remaining backgrounds are evaluated with Monte Carlo (MC) events from the KORALB \cite{7} ($\tau$-pairs) and JETSET \cite{8} ($q\bar{q} \rightarrow$ hadrons) generators passed through the GEANT-based CLEO detector simulation. Any MC event which has a tag-side particle which is truly $e^\pm$, $\mu^\pm$, $\pi^\pm$, $K^\pm$, or $\rho^\pm$ is considered signal for purposes of efficiency; other tags are considered background even if the three-prong side is a signal decay mode. For $\tau^- \rightarrow K^- K^+ K^- \nu_\tau$ decay, we generate signal MC samples according to phase space. The particle identification simulation models the general features of the efficiency and fake rates reasonably well (at the few percent level). We correct the Monte Carlo efficiencies and fake rates by hand, using momentum-dependent scale factors derived from measured and MC particle identification rates.

The corrected efficiencies for events in which one $\tau$ decays into a tag mode and the other into the relevant signal mode (integrated over all tag modes, which constitute about 72.4% of all $\tau$ decays), observed numbers of events in the data, and the expected numbers of $\tau$ and $q\bar{q}$ background events are given in Table I. There are substantial signals evident in all but the three-kaon mode. The largest backgrounds come from $\tau$ decays to three charged hadrons with a single misidentification of a pion or kaon. Many such events are eliminated by the restriction of three-prong mass to be below the $\tau$ mass. Each decay in Table I contributes the dominant background for the channel below it due to the particle misidentification. For the $\tau^- \rightarrow K^- K^+ K^- \nu_\tau$ decay, the $\tau$ background is not taken from the Monte Carlo sample,
but rather the measured $\pi$-fakes-$K$ rate is applied to the $K^-K^+\pi^-$ events in the data (many of which subsequently fail the three-prong mass restriction).

FIG. 2: Three-hadron masses from data (solid circles) and MC, $\tau$-pair background (short dashes), $q\bar{q}$ background (long dashes), sum of background and signal (solid lines), for (a) $\tau^- \to \pi^-\pi^+\pi^-\nu_\tau$, (b) $\tau^- \to K^-\pi^+\pi^-\nu_\tau$, (c) $\tau^- \to K^-K^+\pi^-\nu_\tau$ and (d) $\tau^- \to K^-K^+K^-\nu_\tau$.

In Fig. 2 we show the three-hadron masses for the four modes considered here along with the results from the overlaid MC simulation. The two-particle substructure is presented in Fig. 3. Good agreement between the data and MC is observed [10, 11]. The $\tau^- \to K^-K^+\pi^-\nu_\tau$ mode can be used to measure the contribution from the Wess-Zumino anomaly, offering an alternative channel to $\tau^- \to \eta\pi^-\pi^0\nu_\tau$. A quantitative estimate requires determination of the structure functions [2], for which a substantially larger data sample would be needed.

Most sources of systematic uncertainty affect the four modes similarly. MC statistics for signal events add 1% uncertainty. The uncertainty in the number of $\tau$-pair events produced, and therefore in the normalization of the branching fractions, derives from the uncertainty of luminosity [12] (2%) and $\tau$-pair cross section (2%) [7]. Studies comparing track-finding efficiencies in the MC simulation to data result in a 0.5% per track uncertainty, added linearly to
FIG. 3: Mass distributions for two oppositely charged hadrons showing the data (solid circles) and MC \([\tau]\)-pair background (short dashes), \(q\bar{q}\) background (long dashes), sum of background and signal (solid lines) for (a) \(\tau^- \to \pi^- \pi^+ \pi^- \nu_\tau\) (two entries per event), (b) and (c) \(\tau^- \to K^- K^+ \pi^- \nu_\tau\), \((K^+ K^-\text{ and } K^+\pi^-\text{ masses, respectively})\) and (d) and (e) \(\tau^- \to K^- \pi^+ \pi^- \nu_\tau\) \((\pi^+ \pi^-\text{ and } K^- \pi^+\text{ masses, respectively})\).

| Mode            | data   | \(\tau\) bgd | \(q\bar{q}\) bgd | \(\epsilon\) (%) |
|-----------------|--------|---------------|------------------|------------------|
| \(\pi^- \pi^+ \pi^- \nu_\tau\) | 43543  | 3207±57       | 152±12           | 10.27±0.08      |
| \(K^- \pi^+ \pi^- \nu_\tau\)  | 3454   | 1475±38       | 57±8             | 11.63±0.12      |
| \(K^- K^+ \pi^- \nu_\tau\)    | 932    | 86±9          | 19±4             | 12.48±0.11      |
| \(K^- K^+ K^- \nu_\tau\)      | 12     | 4±2           | 0.4 ± 0.6        | 9.43±0.10       |

TABLE I: Candidate event yields for the data, estimated \(\tau\) and \(q\bar{q}\) background event totals, and overall efficiencies \(\epsilon\) for \(\tau\) three-prong decays.
become 2% for the entire event. Several effects are probed individually by tightening and/or relaxing an event selection criterion, recalculate the branching fractions, and assigning an uncertainty in how well the MC models reality based on the changes induced: allowing for an extraneously reconstructed track in signal events adds 2% uncertainty; one systematic error arising from the assumed absence of two-photon physics background is 0.5% which can be tested by imposing a harsh net transverse momentum of the three-prong side requirement of 3 GeV/c; uncertainty due to the background levels from decay modes with extra neutrals allowed in is estimated by relaxing the veto energy on extra calorimeters showers to as high as 250 MeV and found to be 1%; and variations of the remaining non-particle-identification selection criteria contribute an error of 1%. Uncertainty in $\tau$ branching fractions results in 1% error due to changes in $\tau$ backgrounds. The efficiencies of particle identification were studied exhaustively for variations with time (0.5%) or charged-track multiplicity (0.5%), bias of the efficiency-measuring technique (0.5%), the data/MC efficiency correction procedure (0.3%), which all sum in quadrature to 1% per pion or kaon, which then are added linearly for the event as a whole to 3% overall. When the branching fractions are broken out by individual tags, consistent results are obtained, verifying both the modeling of tag efficiencies and the lack of unexpected non-$\tau$ backgrounds which sometimes show up in the non-leptonic tags. Together these errors sum in quadrature to 5%, which applies to the branching fractions of all four modes.

Other systematics vary from mode to mode, which will be referred to in the order they appear in Table I. To estimate uncertainties from $q\bar{q}$ backgrounds, we compare event totals above the $\tau$ mass between the data and $q\bar{q}$ MC, and assign an additional ~50% (relative) uncertainty from the observed differences. This results in uncertainties of 0.2%, 2%, 1%, and 3% for the four modes, respectively. An overall scale uncertainty in the fake rate per pion or kaon of 0.25% (absolute) is estimated by comparing measured results to those predicted by the RICH simulation, cross-checking with MC for possible bias in the fake-rate measurement technique, examining the rate of the forbidden $\tau^- \rightarrow K^+\pi^-\pi^-\nu_\tau$ (which is dominated by $\tau^- \rightarrow \pi^+\pi^-\pi^-\nu_\tau$ with a pion faking a kaon), and estimating the error from the momentum-reweighting correction procedure. This fake rate uncertainty propagates to the branching fractions differently because of different levels of feed-down: 0.1%, 9%, 2%, and 12%, respectively. The $K^-K^+\pi^-$ mode substructure is not well understood, and variations in the possibilities result in a 2% uncertainty in the efficiency. The three kaon mode substructure is completely unknown and assumed to occur via phase space with no assigned error. The remaining modes appear to be adequately described by the models used. Adding these contributions together in quadrature with the common sources results in total relative systematic uncertainties of 5%, 10%, 6%, and 14%, respectively.

For all decay modes, the yields are obtained from the numbers of the observed events with the backgrounds subtracted, the measured branching fractions (with $K^0_S$ excluded from the modes with two or more pions) are

\begin{align*}
B(\tau^- \rightarrow \pi^-\pi^+\pi^-\nu_\tau) & = (9.13 \pm 0.05 \pm 0.46)\%, \\
B(\tau^- \rightarrow K^-\pi^+\pi^-\nu_\tau) & = (3.84 \pm 0.14 \pm 0.38) \times 10^{-3}, \\
B(\tau^- \rightarrow K^-K^+\pi^-\nu_\tau) & = (1.55 \pm 0.06 \pm 0.09) \times 10^{-3}, \\
B(\tau^- \rightarrow K^-K^+K^-\nu_\tau) & < 3.7 \times 10^{-5} \text{ at } 90\% \text{ CL.}
\end{align*}

The errors are statistical and systematic, respectively. For the decay $\tau^- \rightarrow K^-K^+K^-\nu_\tau$, the upper limit is obtained according to the procedure described in the PDG [13] with both statistical and systematic errors taken into account. This represents the first direct
measurement of $\mathcal{B}(\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu_{\tau})$ with three pions explicitly identified, and our result is in good agreement with the PDG fitted value derived from the PDG constrained fit to the measurements of $\tau^- \rightarrow (3\pi^-) \nu_{\tau}$ decays with and without identified charged kaons \cite{13}. The measurement of $\mathcal{B}(\tau^- \rightarrow K^- K^+ \pi^- \nu_{\tau})$ is consistent with the previous value \cite{13} and improves upon the precision previously attained by a factor of two. Our result $\mathcal{B}(\tau^- \rightarrow K^- \pi^+ \pi^- \nu_{\tau})$ is more precise than and consistent with both the CLEO \cite{14} and OPAL \cite{15} results, while it is larger than the ALEPH \cite{16} value by nearly three standard deviations. The upper limit for the Cabibbo-suppressed decay $\tau^- \rightarrow K^- K^+ K^- \nu_{\tau}$ has been improved over the PDG value \cite{13} by a factor of five. Taken together, these measurements significantly enhance our understanding of the kaon content of three-prong $\tau$ decays.

We gratefully acknowledge the effort of the CESR staff in providing us with excellent luminosity and running conditions. This work was supported by the National Science Foundation, the U.S. Department of Energy, the Research Corporation, and the Texas Advanced Research Program.

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