Long-Term Variations in Solar Activity: Predictions for Amplitude and North–South Asymmetry of Solar Cycle 25

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Abstract
In most of the solar cycles, activity in the northern and southern hemispheres peaks at different times. One hemisphere peaks well before the other, and at least one of the hemispheric maxima frequently does not coincide with the whole sphere maximum. Prediction of the maximum of a hemisphere and the corresponding north–south asymmetry of a solar cycle may help to understand the mechanisms of the solar cycle, the solar-terrestrial relationship, and solar-activity influences on space weather. Here we analysed the sunspot-group data from the Greenwich Photoheliographic Results (GPR) during 1874 – 1976 and Debrecen Photoheliographic Data (DPD) during 1977 – 2017 and studied the cycle-to-cycle variations in the values of 13-month smoothed monthly mean sunspot-group area in the whole sphere (WSGA), northern hemisphere (NSGA), and southern hemisphere (SSGA) at the epochs of maxima of Sunspot Cycles 12 – 24 and at the epochs of maxima of WSGA, NSGA, and SSGA Cycles 12 – 24 (note that solar-cycle variation of a parameter is expressed as a cycle of that parameter). The cosine fits to the values of WSGA, NSGA, and SSGA at the maxima of sunspot, WSGA, NSGA, and SSGA Cycles 12 – 24, and to the values of the corresponding north–south asymmetry, suggest the existence of a ≈132-year periodicity in the activity of the northern hemisphere, a 54 – 66-year periodicity in the activity of the southern hemisphere, and a 50 – 66 year periodicity in the north–south asymmetry in activity at all the aforementioned epochs. By extrapolating the best-fit cosine curves we predicted the amplitudes and the corresponding north–south asymmetry of the 25th WSGA, NSGA, and SSGA cycles. We find that on average Solar Cycle 25 in sunspot-group area would be to some extent smaller than Solar Cycle 24 in sunspot-group area. However, by inputting the predicted amplitudes of the 25th WSGA, NSGA, and SSGA cycles relationship between sunspot-group area and sunspot number we find that the amplitude (130 ± 12) of Sunspot Cycle 25 would be slightly larger than that of reasonably small Sunspot Cycle 24. Still it confirms that the beginning of the upcoming Gleissberg cycle would take place around Solar Cycle 25. We also find that except at the maximum of NSGA Cycle 25 where the strength of activity in the northern hemisphere would be dominant, the strength of activity in the southern hemisphere would be dominant at the maximum epochs of the 25th sunspot, WSGA, and SSGA cycles.

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1. Introduction

The existence of differences between the strengths of solar activity in the Sun’s northern and southern hemispheres is well known as the north–south asymmetry in solar-activity. It exists in most solar-activity phenomena (Hathaway, 2015). Besides this, it is also known that the epochs of maxima of solar cycles are not the same in the northern and southern hemispheres, that is in some solar cycles the maximum in one of the hemispheres does not coincide with the maximum of the total (whole sphere/visible whole disk) activity (e.g. see Figure 1 in Javaraiah, 2020, and also see McIntosh et al., 2013). In some solar cycles the activity peak occurs first in the northern hemisphere, and in some other cycles, it first occurs in the southern hemisphere. The existence of some systematic phase difference between the cycles of activity in the northern and southern hemispheres is also known (e.g. Zolotova et al., 2010; Norton and Gallagher, 2010; Muraközy and Ludmány, 2012; McIntosh et al., 2013; Ravindra, Chowdhury, and Javaraiah, 2021). There exist ≈12-year, ≈55-year, and ≈100-year periodicities in north–south asymmetry (Carbonell, Oliver, and Ballester, 1993; Verma, 1993; Javaraiah and Gokhale, 1997; Li et al., 2002; Deng et al., 2016; Javaraiah, 2020; Nagovitsyn, Osipova, and Nagovitsyna, 2021). However, the origin of these as well as the known short-term periodicities in the north–south asymmetry (e.g. Knaack, Stenflo, and Berdyugina, 2004; Ravindra and Javaraiah, 2015; Chowdhury et al., 2016; Mandal and Banerjee, 2016; Ravindra, Chowdhury, and Javaraiah, 2021) is not yet clear (Norton, Charbonneau, and Passos, 2014; Schüssler and Cameron, 2018; Nepomnyashchikh et al., 2019).

Our recent analysis indicates that the ≈12-year and ≈51-year periodicities of north–south asymmetry are manifestations of the differences in strengths of the corresponding periodicities in the northern and southern hemispheres and their origin might be connected to the configurations of giant planets (Javaraiah, 2020). It has been observed that in several solar cycles, there exist some differences in the maximum epochs of sunspot number and sunspot-area cycles (Hathaway, 2015). Recently, we have analysed the combined sunspot-group data from the Greenwich Photoheliographic Results (GPR) during 1874 – 1976 and the Debrecen Photoheliographic Data (DPD) during 1977 – 2017 and have predicted the north–south asymmetry in the average sunspot-group area at the maximum epoch of Sunspot Cycle 25 (Javaraiah, 2021). Here we analyse the aforementioned sunspot-group data and predict the north–south asymmetry at the maximum epochs of solar cycles in the northern and southern hemispheres. This may help in better understanding the solar dynamo and the solar-terrestrial relationship. Here our approach is different from that of Javaraiah (2021), where we have used the same method that was used in our earlier articles (Javaraiah, 2007; 2008; 2015). In those earlier articles the prediction was made based on the existence of a good correlation between the amplitude of a solar cycle and the sum of the areas of sunspot groups in the 0° – 10° latitude interval of the southern hemisphere just after around one year from the maximum of the preceding cycle (hereafter area-sum). Here we study the cycle-to-cycle variations in the maxima of Solar Cycles 12 – 24 in the average areas of sunspot groups in northern and southern hemispheres, as well as in the whole sphere, by determining the best-fit cosine functions to these data. In principle, from this method it is possible to make predictions for several upcoming solar cycles. However, due to the considerable uncertainties in the obtained best-fit cosine functions, here we make cautious predictions for the amplitude and north–south asymmetry of Solar Cycle 25 only.

In the next section, we describe the data analysis. In Section 3 we present the results, and in Section 4 we present the conclusions and briefly discuss them.
2. Data Analysis

Here the data and the analysis are the same as in Javaraiah (2019). In Javaraiah (2021) and here, we have used the values of the amplitudes $R_M$, i.e. the highest value of 13-month smoothed monthly mean sunspot number, and the maximum epochs of sunspot cycles given by Pesnell (2018). These were determined by Pesnell (2018) from the time series of 13-month smoothed monthly mean values of Version 2 of the international sunspot number (SN) available at www.sidc.be/silso/datafiles. The updated GPR (1874–1976) and DPD (1977–2017) daily sunspot-group data were downloaded from the website fenyi.solarobs.unideb.hu/pub/DPD/ (for details, see Győri, Baranyi, and Ludmány, 2011; Baranyi, Győri, and Ludmány, 2016; Győri, Ludmány, and Baranyi, 2017). These data contain, besides the heliographic positions and other parameters, the corrected whole-spot area [msh: millionth of solar hemisphere] of each sunspot group for its each day observation. First, we determined the mean area of sunspot groups in the Sun’s whole sphere (WSGA), northern hemisphere (NSGA), and southern hemisphere (SSGA) during each calendar month of the years 1874–2017, and then we determined the 13-month smoothed monthly mean values and the corresponding standard errors ($s = \sigma/\sqrt{13}$, where $\sigma$ is the standard deviation). From the time series of the 13-month smoothed monthly mean values we obtained the values and the corresponding epochs of the following parameters during SN, WSGA, NSGA, and SSGA Cycles 12–24 (note that for brevity and convenience, solar-cycle variation of a parameter is expressed as a cycle of that parameter):

- $T_M$: epoch of SN cycle maximum,
- $T_W$: epoch of WSGA cycle maximum,
- $T_N$: epoch of NSGA cycle maximum,
- $T_S$: epoch of SSGA cycle maximum.

It should be noted that usually in a solar cycle, these epochs are not in an increasing or decreasing order. However, rarely there could be an order, and even all these four epochs of a solar cycle could be the same.

- RWA: value of WSGA at $T_M$,
- RNA: value of NSGA at $T_M$,
- RSA: value of SSGA at $T_M$,
- WAM: value of maximum of a WSGA Cycle,
- WNA: value of NSGA at $T_W$,
- WSA: value of SSGA at $T_W$,
- NAM: value of maximum of an NSGA Cycle,
- NSA: value of SSGA at $T_N$,
- NWA: value of WSGA at $T_N$,
- SAM: value of maximum of an SSGA Cycle,
- SNA: value of NSGA at $T_S$, and
- SWA: value of WSGA at $T_S$.

We calculated a best-fit cosine function to the cycle-to-cycle modulation in each aforementioned parameter, and by extrapolating the best-fit cosine curves we obtained the values of the above parameters for the 25th WSGA, NSGA, and SSGA cycles. We also calculated the best-fit cosine function to the cycle-to-cycle modulation of relative north–south asymmetry $(N - S)/(N + S)$, where $N$ and $S$ represent the values of the parameters that correspond to the northern and southern hemispheres, respectively, at the epochs of maxima of sunspot, WSGA, NSGA, and SSGA cycles. We predict north–south asymmetry at the corresponding
epochs of the 25th cycles. In the calculations of the best-fit cosine functions, the weights equal to the corresponding standard errors in the values of the parameters are used. All the linear least-squares fits were calculated by using the Interactive Digital Library (IDL) software FITEXY.PRO, which is downloaded from the website idlastro.gsfc.nasa.gov/ftp/pro/math/. An advantage of using this software is that the errors in both abscissa and ordinate values will be taken into account in the calculation of linear fits by the least-squares method.

3. Results and Predictions

In Table 1, we have given the 13-month smoothed monthly mean values of WSGA, NSGA, and SSGA at the epochs of maxima of SN, WSGA, NSGA, and SSGA of Cycles 12 – 14. Figure 1 shows the values of the parameters NAM, SAM, WAM, and RWA given in this table versus time (respective epochs). The large (small) error bars in the values of these parameters of most of the large (small) solar cycles are due to the strong (weak) fluctuations in the monthly mean sunspot-group area around the maximum epochs of the large (small) solar cycles. In Table 2, we give the information obtained from this figure and Table 1 about dominant hemisphere, phase-leading hemisphere, and the hemisphere coinciding with the whole sphere. In the same table, the difference between the epochs of \( R_M \) and WAM is also given. As we can see in Figure 1 and Table 2, in some solar cycles, North is dominant, and in some other cycles, South is dominant. In many solar cycles the maximum in one of the hemispheres does not coincide with the maximum of the total (whole sphere) activity. In some solar cycles the activity peak occurs first in the northern hemisphere, and in some other cycles, it occurs first in the southern hemisphere.

In the case of sunspot number, the amplitude of Solar Cycle 21 is larger than that of Solar Cycle 22, whereas, as can be seen in Figure 1, in the case of sunspot area the behavior is opposite to that of sunspot number, i.e. Solar Cycle 22 is larger than Solar Cycle 21 (Hathaway, 2015). This difference could be because the ratio of small to large numbers of sunspots/sunspot groups may be larger in Solar Cycle 21 than in Solar Cycle 22. The aforementioned opposite behavior is also found in the cases of whole sphere, northern, and southern hemispheres’ mean areas of sunspot groups (i.e. RWA, RNA, and RSA here) at the epochs of maxima of Solar Cycles 21 and 22 (see also Javaraiah, 2019). As we can see in Table 1, except in the case of SNA, this property exists in the case of all remaining parameters. The value of SNA of SSGA Cycle 21 is larger than that of SSGA Cycle 22. According to the Gnevyshev–Ohl rule (G–O: Gnevyshev and Ohl, 1948), an odd-numbered sunspot cycle is larger than its preceding even-numbered sunspot cycle. However,
Table 1 The values $[msh]$ of WSGA, NSGA, and SSGA at the epochs $T_M$, $T_W$, $T_N$, and $T_S$ of the maxima of SN, WSGA, NSGA, and SSGA cycles ($n = 12, 13, \ldots, 24$), respectively, determined from the corresponding time series of 13-month smoothed monthly mean areas of the sunspot groups in whole sphere, northern hemisphere, and southern hemisphere. The maximum $[R_M]$ values of SN are also given (all the maximum values are indicated with bold).

| $n$ | $T_M$ | At maximum $R_M$ of SN | $T_W$ | At maximum WAM of WSGA |
|-----|-------|------------------------|-------|-----------------------|
|     |       | $R_M$ | RWA | RNA | RSA | $R_M$ | WAM | WNA | WSA |
| 12  | 1883.96 | 124.4 ± 12.5 | 1371 ± 122 | 414 ± 75 | 957 ± 105 | 1883.96 | 1371 ± 122 | 414 ± 75 | 957 ± 105 |
| 13  | 1894.04 | 146.5 ± 10.8 | 1616 ± 110 | 621 ± 57 | 995 ± 100 | 1894.04 | 1616 ± 110 | 621 ± 57 | 995 ± 100 |
| 14  | 1906.12 | 107.1 ± 9.2 | 1044 ± 140 | 761 ± 139 | 283 ± 43 | 1905.45 | 1161 ± 158 | 745 ± 137 | 416 ± 90 |
| 15  | 1917.62 | 175.7 ± 11.8 | 1535 ± 171 | 829 ± 124 | 707 ± 89 | 1917.54 | 1554 ± 165 | 853 ± 123 | 701 ± 92 |
| 16  | 1928.29 | 130.2 ± 10.2 | 1324 ± 123 | 631 ± 96 | 693 ± 65 | 1926.29 | 1467 ± 211 | 809 ± 181 | 658 ± 98 |
| 17  | 1937.29 | 198.6 ± 12.6 | 2120 ± 176 | 1309 ± 140 | 811 ± 108 | 1937.29 | 2120 ± 176 | 1309 ± 140 | 811 ± 108 |
| 18  | 1947.37 | 218.7 ± 10.3 | 2641 ± 210 | 1051 ± 121 | 1590 ± 237 | 1947.37 | 2641 ± 210 | 1051 ± 121 | 1590 ± 237 |
| 19  | 1958.20 | 285.0 ± 11.3 | 3441 ± 208 | 1749 ± 164 | 1693 ± 144 | 1957.96 | 3480 ± 239 | 1801 ± 153 | 1679 ± 166 |
| 20  | 1968.87 | 156.6 ± 8.4 | 1556 ± 82 | 951 ± 83 | 605 ± 46 | 1970.54 | 1628 ± 93 | 926 ± 70 | 701 ± 121 |
| 21  | 1979.96 | 232.9 ± 10.2 | 2121 ± 162 | 1064 ± 139 | 1057 ± 142 | 1981.71 | 2338 ± 177 | 1065 ± 134 | 1274 ± 193 |
| 22  | 1989.87 | 212.5 ± 12.7 | 2269 ± 193 | 1121 ± 124 | 1148 ± 118 | 1989.45 | 2591 ± 179 | 1401 ± 141 | 1190 ± 126 |
| 23  | 2001.87 | 180.3 ± 10.8 | 2157 ± 206 | 1073 ± 111 | 1084 ± 152 | 2002.20 | 2334 ± 179 | 951 ± 114 | 1383 ± 141 |
| 24  | 2014.29 | 116.4 ± 8.2 | 1600 ± 116 | 420 ± 40 | 1180 ± 144 | 2014.45 | 1629 ± 114 | 418 ± 40 | 1211 ± 143 |
| $T_N$ | At maximum NAM of NSGA | $T_S$ | At maximum SAM of SSGA |
|------|-----------------------|------|-----------------------|
|      | NWA | NAM  | NSA   | SWA | SNA  | SAM   |
| 12   | 1882.37 | 978 ± 145 | 476 ± 72 | 501 ± 116 | 1883.96 | 1371 ± 122 | 414 ± 75 | 957 ± 105 |
| 13   | 1894.12 | 1585 ± 115 | 649 ± 61 | 935 ± 115 | 1893.96 | 1585 ± 111 | 577 ± 55 | 1008 ± 99 |
| 14   | 1906.04 | 1109 ± 143 | 822 ± 135 | 287 ± 45 | 1907.45 | 1098 ± 129 | 512 ± 81 | 585 ± 103 |
| 15   | 1917.71 | 1492 ± 178 | 855 ± 116 | 638 ± 84 | 1917.62 | 1535 ± 171 | 829 ± 124 | 707 ± 89 |
| 16   | 1926.29 | 1467 ± 211 | 809 ± 181 | 658 ± 98 | 1928.21 | 1338 ± 121 | 584 ± 102 | 754 ± 57 |
| 17   | 1937.54 | 2088 ± 195 | 1374 ± 158 | 714 ± 109 | 1938.62 | 1855 ± 164 | 715 ± 91 | 1141 ± 151 |
| 18   | 1949.62 | 2060 ± 196 | 1200 ± 114 | 860 ± 153 | 1947.45 | 2625 ± 215 | 1011 ± 129 | 1614 ± 232 |
| 19   | 1959.54 | 2847 ± 233 | 2220 ± 227 | 627 ± 77 | 1957.79 | 3428 ± 257 | 1673 ± 183 | 1755 ± 142 |
| 20   | 1967.62 | 1596 ± 142 | 1108 ± 100 | 488 ± 73 | 1969.87 | 1549 ± 113 | 767 ± 103 | 783 ± 105 |
| 21   | 1979.37 | 2067 ± 164 | 1211 ± 111 | 856 ± 117 | 1981.96 | 2293 ± 199 | 976 ± 123 | 1317 ± 179 |
| 22   | 1989.45 | 2591 ± 179 | 1401 ± 141 | 1190 ± 126 | 1991.54 | 2405 ± 167 | 894 ± 129 | 1511 ± 189 |
| 23   | 2000.96 | 1831 ± 167 | 1122 ± 119 | 709 ± 65 | 2002.20 | 2334 ± 179 | 951 ± 114 | 1383 ± 141 |
| 24   | 2011.71 | 905 ± 116 | 687 ± 100 | 218 ± 40 | 2014.45 | 1629 ± 114 | 418 ± 40 | 1211 ± 143 |
sunspot-cycle pair (22, 23) violated this rule, i.e. $R_M$ of Sunspot Cycle 22 is larger than that of Sunspot Cycle 23. As we can see in Table 1, WSA values of WSGA cycle pair (22, 23) and SNA values of SSGA cycle pair (22, 23) satisfied the G–O rule, and the corresponding pairs of each of the remaining all parameters violated the G–O rule (here the G–O rule in WSA and SNA tentatively means that the cycle-to-cycle modulations in WSA and SNA indicate a poor fit, perhaps because the errors are underestimated.

By using the linear relationships shown in Figure 2, we get the values $1348 \pm 161$ msh and $542 \pm 177$ msh for WSA of WSGA Cycle 25 and SNA of SSGA Cycle 25, respectively. These values are larger than the corresponding observed values of WSGA Cycle 24 and SSGA Cycle 24 implying satisfaction of the G–O rule. By using the predicted value of WSA and the existence of reasonably good correlations (good linear relationships) between WSA and SAM, SAM and SWA, SWA and WAM, WAM and RWA, and RWA and $R_M$ we obtained the values for WAM of WSGA Cycle 25 and $R_M$ of Sunspot Cycle 25, which were found to be much larger than the corresponding values of the respective 24th cycles. We have not given them here because the aforementioned predicted values of WSA of WSGA Cycle 25 and SNA of SSGA Cycle 25 are to some extent unreliable. It should be noted that without prior knowledge about non-violation of the G–O rule by an upcoming even- and odd-numbered solar cycle pair, by using the G–O rule it is not possible to predict the amplitude of the odd-numbered solar cycle.

### Table 2

The information obtained by using Table 1 and Figure 1 about dominant hemisphere (DH), phase-leading hemisphere (LH), and whether the hemisphere coincides/is close to the whole sphere (CH) in a solar cycle ($n$). The corresponding differences between the values of parameters and between the epochs are given within parentheses. In the last column the differences between $T_M$ and $T_W$ are also given. In the 2nd column the “same” implies that there is no phase difference. In the 4th and 5th columns a zero/small absolute value indicates that the corresponding peaks are coincident/very close.

| $n$ | DH (NAM–SAM) | LH ($T_N – T_S$) | CH ($T_N – T_W$) | $T_M – T_W$ |
|-----|--------------|-----------------|-----------------|-------------|
| 12  | south (−481) | north (−1.59)   | south (−1.59/0.0) | 0.0         |
| 13  | south (−359) | same (0.16)     | both (0.08/−0.08) | 0.0         |
| 14  | north (237)  | north (−1.4)    | north (0.59/2.0) | −0.67       |
| 15  | north (148)  | same (0.09)     | both (0.17/0.08) | −0.08       |
| 16  | north (55)   | north (−1.92)   | north (0.0/1.92) | −2.0        |
| 17  | north (233)  | north (−1.08)   | north (0.25/1.33) | 0.0         |
| 18  | south (−414) | south (2.17)    | south (2.25/0.08) | 0.0         |
| 19  | north (465)  | south (1.75)    | south (1.58/−0.17) | −0.24       |
| 20  | north (325)  | north (−2.25)   | south (−2.92/−0.67) | 1.67       |
| 21  | south (−106) | north (−2.59)   | south (−2.34/0.25) | 1.75       |
| 22  | south (−110) | north (−2.09)   | north (0.0/2.09)  | −0.42       |
| 23  | south (−261) | north (−1.24)   | south (−1.24/0.0) | 0.33        |
| 24  | south (−524) | north (−2.74)   | south (−2.74/0.0) | 0.16        |
Figure 2 (a) $W_{SA_n}$ of an even-numbered WSGA cycle versus $W_{SA_{n+1}}$ of following odd-numbered WSGA cycle and (b) $S_{NA_n}$ of an even-numbered SSGA cycle versus $S_{NA_{n+1}}$ of following odd-numbered SSGA cycle. The horizontal and vertical error bars represent the standard errors of the abscissa and the ordinate, respectively; both are taken care of the calculations of linear least-square fits. The continuous line represents the best-fit linear relationship. The dotted lines (red) are drawn at one-rms (root-mean-square deviation) levels. The best-fit linear equation and the values of correlation coefficient $r$, $\chi^2$ and the corresponding probability (PROB), and rms are also shown. The filled squares (red) represent the predicted values of $W_{SA}$ and $S_{NA}$ at the epochs of maxima of WSGA Cycle 25 and SSGA Cycle 25.

We calculated the cosine fits to the values of the parameters of WSGA, NSGA, and SSGA Cycles 12 – 24 given in Table 1. In Figures 3, 4, 5, 6, we show the best-fit cosine curves. In Table 3, we give the results obtained by extrapolating the best-fit cosine curves of different parameters, i.e. the value of period, the predicted corresponding 25th cycle value of a parameter, and the values of rms and $\chi^2$. The cosine fit of each parameter seems to be reasonably good because only one (mostly the data point of Cycle 19) or at most two data points are outliers (away from the one-rms level). In principle, we can extrapolate the best-fit cosine curves for several cycles. However, the $\chi^2$-values are large, i.e. the cosine best fits are not very accurate. Therefore the corresponding results are only suggestive rather than compelling. Hence we restricted our conclusions to only the predictions for the corresponding 25th cycle (although the values obtained for the corresponding 26th cycle are also shown in Figures 3 – 6).

We can see in Table 3 that the periodicity in a parameter of the northern hemisphere is $\approx 132$ years, whereas it is 54 – 66 years in a parameter of the southern hemisphere, i.e. approximately half of that of the northern hemisphere. This is consistent with the similar results noticed in the earlier analysis (Javaraiah, 2019). Morlet wavelet analysis also sug-
Figure 3  Continuous curve represents the best-fit cosine function to the values (filled circles) (a) of RNA and (b) of RSA at the epochs of maxima of Sunspot Cycles 12–24, i.e. the values of NSGA and SSGA at $T_M$. The dotted curve (red) represents the one-rms level. The extrapolated portion is shown as a dashed curve, and the filled squares (red) represent the predicted values of RNA and RSA at the maximum epochs of Sunspot Cycles 25 and 26. The period (in number of solar cycles) of the cosine function is also shown. See also the details given in Table 3.

Figure 4  Continuous curve represents the best-fit cosine function to the values (filled circles) (a) of WNA and (b) of WSA of WSGA Cycles 12–24, i.e. the values of NSGA and SSGA at $T_W$. The dotted curve (red) represents the one-rms level. The extrapolated portion is shown as a dashed curve, and the filled squares (red) represent the predicted values of WNA and WSA at the maximum epochs of WSGA Cycles 25 and 26. The period (in number of solar cycles) of the cosine function is also shown. See also the details given in Table 3.

Gested that a $\approx 51$-year periodicity in the 13-month smoothed area of sunspot groups of the northern hemisphere is much weaker than that of the southern hemisphere (Javaraiah, 2020).

The cosine fits to the data of RWA, WAM, NWA, and SWA are found to be much more uncertain, and therefore we do not show them. We get the corresponding 25th cycle values of these parameters from the predicted values of the parameters given in Table 3:

\[
\begin{align*}
RWA &= RNA + RSA = 1317 \pm 123 \text{ msh}, \\
WAM &= WNA + WSA = 1402 \pm 124 \text{ msh}, \\
NWA &= NAM + NSA = 1082 \pm 100 \text{ msh}, \\
SWA &= SNA + SAM = 1354 \pm 116 \text{ msh}.
\end{align*}
\]

The rms appears large for the corresponding predicted value of a parameter of Solar Cycle 25 given Table 3. However, the range of values of the parameter is large, and the predicted value is at the minimum level of the corresponding long-term cycle (Gleissberg cycle). The uncertainties in the values of RWA, WAM, NWA, and SWA obtained above are reasonably small. They are determined as $\sqrt{(\text{rms}_N^2 + \text{rms}_S^2)}/13$, where rms$_N$ and rms$_S$ are the rms values of northern and southern hemispheres’ parameters, respectively.

We also determined the best-fit cosine function to the values of $R_M$ of SN Cycles 12–24. It is shown in Figure 7, and the details are also given in the last row of Table 3. The obtained value for $R_M$ of SN Cycle 25 is slightly larger than that of SN Cycle 24, but the former
Figure 5 *Continuous curve* represents the best-fit cosine function to the values *(filled circles)* (a) NAM, i.e. the maximum values of NSGA Cycles 12–24 and (b) NSA, i.e. the values of SSGA at $T_N$. The *dotted curve* (red) represents the one-rms level. The extrapolated portion is shown as a *dashed curve*, and the *filled squares* (red) represent the predicted values of NAM and NSA at the maximum epochs of NSGA Cycles 25 and 26. The period (in number of solar cycles) of the cosine function is also shown. See also the details given in Table 3.

Figure 6 *Continuous curve* represents the best-fit cosine function to the values *(filled circles)* (a) SNA, i.e. the values of NSGA at $T_S$, and (b) SAM, i.e. the maximum values of SSGA Cycles 12–24. The *dotted curve* (red) represents the one-rms level. The extrapolated portion is shown as a *dashed curve*, and the *filled squares* (red) represent the predicted values of SNA and SAM at the maximum epochs of SSGA Cycles 25 and 26. The period (in number of solar cycles) of the cosine function is also shown. See also the details given in Table 3.

Figure 7 *Continuous curve* represents the best-fit cosine function to the values *(filled circles)* of $R_M$, i.e. the values of the amplitudes of Sunspot Cycles 12–24. The *dotted curve* (red) represents the one-rms level. The extrapolated portion is shown as a *dashed curve*, and the *filled squares* (red) represent the predicted values of SN at the epochs of maxima of Sunspot Cycles 25 and 26. The period (in number of solar cycles) of the cosine function is also shown. See also the details given in Table 3.

has a large uncertainty (rms value). Moreover, the cosine fit of $R_M$ is not good, since the corresponding $\chi^2$ is very large.
Table 3  The periods of best-fit cosine functions of the different parameters given in Table 1 and the parameter values (msh, in the case of a parameter of area) in Solar Cycle 25 predicted by extrapolating the best-fit cosine curves. The corresponding values of rms and $\chi^2$ are also given. Note that the average period of solar cycles is 11.03 ± 1.18-year (Pesnell, 2018).

| Parameter | Period [cycles] | Period [years] | Pred. Cycle 25 | rms | $\chi^2$ |
|-----------|-----------------|----------------|----------------|-----|-----------|
| RNA       | ≈ 12            | ≈ 132          | 491            | 255 | 66        |
| RSA       | ≈ 6             | ≈ 66           | 826            | 358 | 118       |
| WNA       | ≈ 12            | ≈ 132          | 522            | 283 | 69        |
| WSA       | ≈ 5.8           | ≈ 64           | 880            | 345 | 69        |
| NAM       | ≈ 12            | ≈ 132          | 627            | 294 | 46        |
| NSA       | ≈ 4.9           | ≈ 54           | 455            | 210 | 64        |
| SNA       | ≈ 12            | ≈ 132          | 461            | 242 | 47        |
| SAM       | ≈ 5.5           | ≈ 61           | 893            | 342 | 67        |
| $R_M$     | ≈ 12.3          | ≈ 136          | 123            | 33  | 141       |

Figure 8  Scatter plot of RWA during Sunspot Cycles 12–24 versus WAM during WSGA Cycles 12–24. The continuous line represents the linear least-square best-fit to the data. The dotted line (red) represents the one-rms level. The obtained linear equation and the values of the corresponding $r$, rms, $\chi^2$, and PROB are given. The filled square (red) represents the predicted value of RWA, i.e. the value of WSGA at the epoch of $R_M$ of Solar Cycle 25.

Figure 8 shows the correlation between WAM and RWA. Obviously, there exists a high correlation between WAM and RWA. The corresponding linear least-squares best-fit is highly statistically significant ($\chi^2 = 2$, PROB = 0.998). Using the above predicted value of WAM in WAM–RWA relationship shown in Figure 8, we get the value 1348 ± 96 msh for RWA of SN Cycle 25, which seems to be more reliable than the value of RWA obtained above by summing the values predicted for RNA and RSA (note that the value of $\chi^2$ corresponding to the best-fit cosine function of RSA is very high). However, the two values are almost equal.

In Figure 9, we compare the predicted values of the parameters at the epochs of the maxima of the 25th SN, WSGA, NSGA, and SSGA cycles with the observed values of the corresponding 24th cycles. As we can see in this figure, there is an indication that except at the peaks of both the NSGA Cycles 24 and 25 where the activity in the northern hemisphere looks to be negligibly larger than that in southern hemisphere, in all the remaining other occasions, including at the epoch of $R_M$, the southern hemisphere is dominant. The difference between the predicted values of all northern and southern hemispheres’ parameters of the 25th cycles at a given epoch is not significant with respect to the large uncertainties in these values, suggesting that there exists no significant north–south asymmetry in Solar Cycle 25, whereas most of the corresponding differences of the 24th cycle seem to be statistically significant. The overall pattern of Solar Cycle 25 would be closely similar to that of Solar
Cycle 24. The value predicted here for RWA is much larger than the value \( \approx 701 \) msh of RWA (i.e. \( A_W \)) predicted by Javaraiah (2021) by a different method, which is much smaller than the RWA of Solar Cycle 24. The above predicted values of RWA and WSA are reasonably smaller than the corresponding values of Solar Cycle 24, and there are no significant differences in the corresponding values of WNA. The predicted value of WAM of Solar Cycle 25 is also slightly smaller than that of Solar Cycle 24, suggesting that on average Solar Cycle 25 in sunspot-group area would be smaller than the corresponding Solar Cycle 24. However, the uncertainties in the predicted values of Solar Cycle 25 are large. Therefore all the above results are only suggestive rather than compelling.

As shown in Figures 5 – 7 of Javaraiah (2021), here we also attempted to determine the linear relations between RWA and \( R_M \), RWA and RNA, and RWA and RSA. Here in the calculations of linear least-squares fit the errors in the values of both abscissa and ordinate are taken into account, whereas in that earlier article, only errors in the ordinate values were considered. None of the corresponding linear least-squares best fits was found to be reasonably statistically significant, that is the corresponding values of \( \chi^2 \) are found to be very large, and, obviously, the corresponding values of PROB are found to be very small (\( \leq 0.07 \)). If we use in Equation 5 of Javaraiah (2021) the values \( \approx 1317 \) msh and \( \approx 1348 \) msh obtained/predicted above for RWA (i.e. \( A_W \) in that article), then we get 129 \( \pm 19 \) and 131 \( \pm 19 \), respectively, for \( R_M \) of Sunspot Cycle 25. Each of these values of \( R_M \) of Sunspot Cycle 25 is slightly larger than the observed value of \( R_M \) of Sunspot Cycle 24. As already mentioned above, the predicted values of RWA of Solar Cycle 25 are considerably smaller than the observed value of RWA of Solar Cycle 24. However, this comparison seems to be not genuine because the latter is an outlier (far from one-rms level) in the \( A_W – R_M \) linear relationship shown in Figure 6 of Javaraiah (2021).

We determined the best-fit linear relation between the 13-month smoothed monthly mean values of sunspot-group area and SN. Figures 10, 11, and 12 show the relations between
Figure 10 Scatter plot of 13-month smoothed monthly mean northern hemisphere’s sunspot number (SNN) versus NSGA during the period 1992 – 2017 (300 data points). The continuous line (red) represents the linear least-squares best-fit to the data. The dotted line (red) represents the one-rms level. The obtained linear equation and the values of the corresponding $r$, $r_{\text{rms}}$, $\chi^2$, and PROB are given. The predicted values of SNN at the epochs of $R_m$, WAM, NAM, and NSA of the 25th SN, WSGA, NSGA, and SSGA cycle are also shown.

Figure 11 Scatter plot of 13-month smoothed monthly mean southern hemisphere’s sunspot number (SNS) versus SSGA during the period 1992 – 2017 (300 data points). The continuous line (red) represents the linear least-squares best fit to the data. The dotted line (red) represents the one-rms level. The obtained linear equation and the values of the corresponding $r$, $r_{\text{rms}}$, $\chi^2$, and PROB are given. The predicted values of SNS at the epochs of $R_m$, WAM, SNA, and SAM of the 25th SN, WSGA, NSGA, and SSGA cycle are also shown.

NSGA and SNN, SSGA and SNS, and WSGA and SN_T, where the subscripts N, S, and T indicate north, south, and total. All these linear relationships are statistically highly significant (the values of PROB are high). By using in these relations the values predicted above for RWA, RNA, RSA, WNA, WSA, NAM, and SAM we get/predict the values of SNN, SNS, and SN_T (it is nothing but $R_M$ at the epoch of $R_M/RWA$) of Sunspot Cycle 25 and the corresponding values at the maxima of the 25th NSGA cycle, SSGA cycle, and WSGA cycle. The predicted values are also shown in Figures 10–12 and listed in Table 4, and in Figure 13.
Figure 12 Scatter plot of 13-month smoothed monthly mean whole-sphere (total) sunspot number ($S_{NT}$) versus WSGA during the period 1874–2017 (1713 data points). The continuous line (red) represents the linear least-squares best-fit to the data. The dotted line (red) represents the one-rms level. The obtained linear equation and the values of the corresponding correlation coefficient $r$, rms, $\chi^2$, and PROB are given. The predicted values of $S_{NT}$ at the epochs of $R_M$, WAM, NAM, and SAM of the 25th SN, WSGA, NSGA, and SSGA cycles are also given. The value of $S_{NT}$ obtained by using RWA predicted from the WAM–RWA relationship shown in Figure 8 is also given.

Table 4 Predictions for the values of SN in northern hemisphere ($S_{NN}$), southern hemisphere ($S_{NS}$), and whole sphere ($S_{NT}$) at the epochs $T_M$, $T_W$, $T_N$, and $T_S$ of the maxima of 25th SN, WSGA, NSGA, and SSGA cycles, respectively, by using in the linear relationships shown in Figures 10–12 the values of the different parameters predicted from their respective best-fit cosine functions. The symbol $^a$ indicates that the value of RWA is obtained from the WAM–RWA relationship shown in Figure 8 (note that $S_{NT}$ at $T_M$ is the same as $R_M$). In the last column of the bottom panel, we give the values of $S_{NT}$ obtained by summing the corresponding predicted values of $S_{NN}$ (top panel) and $S_{NS}$ (middle panel).

| Predictions for the values of $S_{TN}$ | Predictions for the values of $S_{NN}$ | Predictions for the values of $S_{NS}$ | Predictions of for the values of $S_{NT}$ |
|----------------------------------------|----------------------------------------|----------------------------------------|----------------------------------------|
| At the epoch                           | Predicted value                        | Used value of                          | At the epoch                           | Predicted value | Used value of $S_{TN}$ + $S_{NS}$ |
| $T_M$                                  | 45 ± 4.4                               | RNA                                    | $T_M$                                  | 127 ± 12        | RWA $\approx$ 118                      |
| $T_W$                                  | 48 ± 4.4                               | WNA                                    | $T_W$                                  | 135 ± 12        | WAM $\approx$ 126                      |
| $T_N$                                  | 57 ± 4.4                               | NAM                                    | $T_N$                                  | 106 ± 12        | NWA $\approx$ 98                       |
| $T_S$                                  | 43 ± 4.4                               | SNA                                    | $T_S$                                  | 131 ± 12        | SWA $\approx$ 122                      |

$^a$ Indicates that the value of RWA is obtained from the WAM–RWA relationship shown in Figure 8 (note that $S_{NT}$ at $T_M$ is the same as $R_M$). In the last column of the bottom panel, we give the values of $S_{NT}$ obtained by summing the corresponding predicted values of $S_{NN}$ (top panel) and $S_{NS}$ (middle panel).
we compare these predicted values of Sunspot Cycle 25 with the corresponding observed values of Sunspot Cycle 24. The values shown in Figure 13 for $R_M$ of Solar Cycle 25 are considerably larger than the value (86 ± 18) predicted earlier by Javaraiah (2021) by using the value predicted for RWA from a different method. As we can see in Figure 13, the values predicted here for $R_M$ of Solar Cycle 25 also appear to be slightly larger than that of Solar Cycle 24 (the corresponding difference is negligible if we take the uncertainty into account). There is also a suggestion that the activity in the southern hemisphere is dominant in Solar Cycle 25, similarly to the case of sunspot-group area shown in Figure 9, except at the peak of NSGA, in all the remaining cases including the case of $R_M$ (see Figure 13). The southern hemisphere’s peak may coincide with whole sphere’s peak. In fact, the overall pattern of the predicted values of Solar Cycle 25 closely resembles that of Solar Cycle 24. Opposite to that seen in Figure 9 for the case of sunspot-group area, in Figure 13, there is a suggestion that on average Sunspot Cycle 25 would be slightly larger than Sunspot Cycle 24. The reason for this difference is not clear, but one possibility is that the ratio of small to large sunspots during the maximum of Solar Cycle 25 would be larger than that during the maximum of Solar Cycle 24. However, the differences between Solar Cycles 24 and 25 in sunspot-group area and also between Sunspot Cycles 24 and 25 are statistically insignificant. On the other hand, properties of sunspot-number and sunspots-area cycles are not exactly the same. For example, the well-known Waldmeier effect of sunspot cycles is not present in the cycles of sunspot-group area (Dikpati, Gilman, and de Toma, 2008; Javaraiah, 2019). In several solar cycles, there exist some differences in the maximum epochs of sunspot-number and sunspot-area cycles, and there are also differences in the relative heights of the peaks of some sunspot-number and sunspot-area cycles.

As already mentioned above, because the cosine best fits of most of the parameters are not very accurate, although the area–SN linear relationships have small rms values, it may be still difficult to draw a definite conclusion from these predicted values about the domi-
The continuous curve represents the best-fit cosine function to the values of the relative north–south asymmetry (a) in RWA, i.e. \( \frac{RNA - RSA}{RNA + RSA} \), (b) in WAM, i.e. \( \frac{WNA - WSA}{WNA + WSA} \), (c) in NWA, i.e. \( \frac{NAM - NSA}{NAM + NSA} \), and (d) in SWA, i.e. \( \frac{SNA - SAM}{SNA + SAM} \). The dotted curve (red) represents the one-rms level. The period (in cycles) of the best-fit cosine function is also shown. The dashed portion of the curve is obtained by extrapolation, and the filled squares (red) represent the predicted value of the north–south asymmetry in the corresponding parameters of Solar Cycles 25 and 26.

Figure 14 shows the predicted values of the 25th cycle, except at the epoch of NAM, in all the remaining cases, including at the epoch of \( R_M \), the southern hemisphere. On the other hand, uncertainty in the relative north–south asymmetry of any two quantities is much smaller than those of the corresponding absolute values (Javaraiah and Gokhale, 1997). Therefore we calculated the relative north–south asymmetry in RWA, WAM, NWA, and SWA and determined the cosine fit to the relative north–south asymmetry in each of these quantities. It would help, besides to find the long-term periodicity in north–south asymmetry of each quantity, to predict the north–south asymmetry in the corresponding quantities of future cycles. Figures 14a, 14b, 14c, and 14d show the best-fit cosine curves of the relative north–south asymmetry in RWA, WAM, NWA, and SWA, respectively. The best-fit cosine curves suggest the existence of \( \approx 6 \)-cycle (66-year), \( \approx 6 \)-cycle (66-year), \( \approx 4.5 \)-cycle (50-year), and \( \approx 5.5 \)-cycle (61-year) periodicities for the north–south asymmetry in RWA, WAM, NWA, and SWA, respectively. We have extrapolated the best-fit cosine curves and predicted the relative north–south asymmetry in these quantities at the epochs of \( R_M \), WAM, NAM, and SAM, respectively. Most of these values do not significantly differ from zero.
sphere is dominant during both Solar Cycles 24 and 25. There is a suggestion that overall the asymmetry in Solar Cycle 25 would be smaller than that of Solar Cycle 24.

4. Discussion and Conclusions

In most of the solar cycles, activity in the northern and southern hemispheres peaks at different times, that is at least one of the hemispheric maxima frequently does not coincide with the whole sphere (total) maximum. Typically, one hemisphere peaks well before the other, and the maximum of the whole-Sun area or sunspot number can be the peak in one hemisphere, or the peak in the other hemisphere, or something in between. Predictions for each hemisphere’s maximum and the corresponding north–south asymmetry of a solar cycle may help to understand the mechanisms of the solar cycle, the solar-terrestrial relationship, and solar-activity influence on space weather. Here we analysed the GPR and DPD sunspot-group data during 1874 – 2017 and studied the cycle-to-cycle variations in the values of WSGA, NSGA, and SSGA at the epochs of the maxima of Sunspot (SN) Cycles 12 – 24 and at the epochs of the maxima of the 12th to 24th WSGA, NSGA, and SSGA cycles. We find that, except in the cases of SSGA at the peak of WSGA and NSGA at the peak of SSGA, in all the remaining cases the G–O rule is violated by the solar cycle pair (22, 23). Using the G–O rule, we obtained a value of SSGA at the maximum of WSGA Cycle 25 that is much larger than the value of SSGA at the maximum of WSGA Cycle 24. Similarly, we obtained a value of NSGA at the maximum of SSGA Cycle 25 that is also found to be larger than the value of NSGA at the maximum of SSGA Cycle 24. However, these predictions are somewhat unreliable because the G–O rule cannot be used to predict the amplitude of an odd-numbered solar cycle without prior knowledge about non-violation of this rule by the corresponding pair of even- and odd-numbered solar cycles. We determined the best-fit cosine functions to the values of each of the parameters given in Table 1. We find that there exists a ≈132-year periodicity in all the northern hemisphere’s parameters and the 54 – 66-year periodicity in all the southern hemisphere’s parameters. By extrapolating the best-fit
cosine curves we make cautious predictions for the values of the parameters of the corresponding 25th cycles. The sums of the predicted values of the parameters of northern and southern hemispheres represent the predictions for the corresponding value of the whole sphere. It is found that the amplitudes of the 25th WSGA and SSGA cycles would be to some extent smaller than those of the corresponding 24th cycle. The amplitude of the 25th NSGA cycle would be almost the same as that of the corresponding 24th cycle. The value of WSGA at the maximum epoch of Sunspot Cycle 25 would also be smaller than that at the maximum epoch of Sunspot Cycle 24, i.e. the overall Solar Cycle 25 in sunspot-group area would be smaller than Solar Cycle 24 in sunspot-group area. We obtained a good linear relationship between the 13-month smoothed monthly mean SN and sunspot-group area in the whole sphere and also in the northern and southern hemispheres. By inputting the predicted values of RWA, RNA, and RSA in these relationships we obtained the values of SN at the epochs of the maxima of the 25th SN, WSGA, NSGA, and SSGA cycles. The obtained value $(130 \pm 12)$ of $R_M$ of Sunspot Cycle 25 is found to be slightly larger than that of Sunspot Cycle 24. Except at the maximum of NSGA Cycle 25 where the north is found to be dominant in strength of activity, the values of SN at the maxima of WSGA Cycle 25, SSGA Cycle 25, and Sunspot Cycle 25 the south is found to be dominant. The cosine best-fits to the values of the corresponding north–south asymmetry in WSGA, NSGA, and SSGA at the maxima of the 12th to 24th SN, WSGA, NSGA, and SSGA cycles suggest the existence of 50–66-year periodicities in the north–south asymmetry and the same aforementioned pattern of hemispheric dominance. Overall, the present analysis suggests that the amplitude of Solar Cycle 25 would be slightly larger than that of Solar Cycle 24 and the activity in the southern hemisphere would be dominant.

All the parameters of the solar cycles of a hemisphere have the same periodicity, implying that different parameters of the hemisphere are at different phases of the same long-period cycle; that is, the epochs of different parameters of the northern hemisphere represent different phases of the same cosine wave of $\approx 132$-year period, and the different parameters of the southern hemisphere represent different phases of the same cosine wave of 54–66-year period. The large difference in the periods of the cosine waves of northern and southern hemispheres’ activity may be responsible for varying phase differences between 11-year cycles of northern and southern hemispheres’ activity. It may be worth finding why there exists a large difference in the long-term periodicities in northern and southern hemispheres’ activity (which is beyond the scope of the present analysis).

The best-fit cosine functions of sunspot-number data have already indicated that Solar Cycle 25 is a reasonably small cycle and constitutes the minimum of the upcoming new Gleissberg cycle (Javaraiah, Bertello, and Ulrich, 2005; Javaraiah, 2017). A number of studies on long-term variations in solar activity by using different techniques have also predicted Dalton-minimum-like characteristics around Solar Cycle 25 (Javaraiah, 2015; Gao, 2016; Coban et al., 2021). In the present analysis, we also find the same. However, whether Solar Cycle 25 will be smaller or larger than the reasonably small Solar Cycle 24 is yet to be established. Many authors predicted the amplitude of Solar Cycle 25 by using different techniques (for recent reviews, see Petrovay, 2020; Nandy, 2021). Some authors predicted a small amplitude, some others predicted a large amplitude for Solar Cycle 25, and a larger number of authors predicted that it would be approximately the same size as Solar Cycle 24.

It is widely believed that the strength of polar fields at the minimum of an upcoming solar cycle is a good physically oriented precursor to predict the strength of the solar cycle. From this method and in flux-transport dynamo models, it is predicted that Solar Cycle 25 would have the same size or slightly larger than that of Solar Cycle 24 (Nandy, 2021; Kumar et al., 2021), and our prediction here closely agrees with it. As already mentioned earlier,
we found a specific method (Javaraiah, 2007), and using it we predicted a small value for the amplitude of Solar Cycle 25, strongly implying that Solar Cycle 25 will be considerably smaller than Solar Cycle 24 (Javaraiah, 2015; 2017; 2021). However, the predictions made in the present analysis by using a basic method suggest that Solar Cycle 25 in sunspot-group area would be slightly smaller than Solar Cycle 24 in sunspot-group area, but Sunspot Cycle 25 would be slightly larger than Sunspot Cycle 24. A reason for this discrepancy in our present and earlier predictions for Sunspot Cycle 25 is not known to us. There are some inconsistencies in both earlier and present analyses. Regarding the earlier method, in the case of Solar Cycle 24 its second SN peak (coinciding with the strong southern hemisphere’s peak; see Figure 1) is taken into account because it is substantially larger than its first peak (coinciding with the weak northern hemisphere peak), whereas in the case of most of the previous cycles the respective first peak is taken into account because it is larger than the corresponding second peak. In addition, since the uncertainties in the measured areas of sunspot groups are not known, in the earlier analyses the linear least-squares fit calculations were not included the uncertainties in the area-sums (sums of the areas of sunspot groups; see Section 1). Here we repeated the earlier calculations by taking 10% of the area-sums for their uncertainties (note that $R_M$ values have 5% – 10% uncertainties). None of the best-fit linear relations, namely, between the area-sum and $R_M$ and area-sum and RWA, etc., are found statistically significant (PROB values are found considerably small). However, the 10% uncertainties in the area-sums seem to be underestimated. To get a reasonably large PROB, it seems necessary to use 20 – 25% of the area-sums for their uncertainties, which may be too unrealistic. In the present analysis the results of best-fit cosine functions are suggestive rather than compelling (best-fit cosine functions have to some extent large $\chi^2$-values). The predictions made from our earlier method are based on the existence of a strong connection (high correlation) between consecutive cycles. The values predicted here from the long-term cyclic trends in the data might be to some extent overestimated. Further investigations are needed to conclude whether our present or earlier predictions will be right or wrong. On the other hand, the value predicted in the present analysis for the amplitude of Solar Cycle 25 is only slightly larger than that of the reasonable small Solar Cycle 24 and considerably smaller than the average amplitude 178.7 of solar cycles (Pesnell, 2018). Hence in the present analysis we confirmed that the beginning of the upcoming Gleissberg cycle would take place around Solar Cycle 25 (see the cosine curve in Figure 7).

Our present predictions (see Table 4) for Solar Cycle 25 are somewhat comparable to the following predictions made by different authors using different techniques. Rigozo et al. (2011) by extrapolating the sunspot-number time-series spectral components estimated a maximum sunspot number of 132.1 for Solar Cycle 25. Cameron, Jiang, and Schüssler (2016) by using a flux-transport dynamo model simulated a value of dipole moment around 2020, i.e. around the beginning of Solar Cycle 25, and suggested that Solar Cycle 25 will be of moderate amplitude, not much higher than that of Solar Cycle 24. Pesnell and Schatten (2018) applied a precursor method by using the SODA Index, which is determined by polar magnetic fields and the spectral index, predicted a large amplitude ($135 \pm 25$) for Solar Cycle 25. Jiang et al. (2018) used a solar surface flux-transport model and predicted that the peak sunspot number of Solar Cycle 25 is $125 \pm 32$. Petrovay et al. (2018) using coronal green-line data as a precursor predicted 130 for the amplitude of Solar Cycle 25. Bhowmik and Nandy (2018) using magnetic-field evolution models for the Sun’s surface and interior predicted that Solar Cycle 25 will be similar or slightly stronger than Solar Cycle 24. Du (2020) using the rate of decrease in the smoothed monthly mean sunspot number over the final three years of Solar Cycle 24 predicted $130.0 \pm 31.9$ for the amplitude of Solar Cycle 25. Kumar et al. (2021) used the polar-precursor method and predicted $126 \pm 3$ for the amplitude.
of Solar Cycle 25. Ahluwalia (2022) using data for sunspot numbers and geomagnetic indices (aa/Ap) and their heuristic methodology inferred that Solar Cycle 25 may be as active as Solar Cycle 24 ruling out a Dalton-like minimum in the 21st century. Upton and Hathaway (2018) using an advective flux-transport code found evidence that during Solar Cycle 25, the southern hemisphere will be more active than the northern hemisphere. Gopalswamy et al. (2018) used a precursor method (microwave-imaging observations) and predicted that the sunspot-number peaks of southern and northern hemispheres during Sunspot Cycle 25 will be 89 and 59, respectively. These indicate a considerable north–south asymmetry corresponding to the amplitude of Solar Cycle 25 and that the activity would be dominant in the southern hemisphere. Werner and Guineva (2020) using auto-regressive models of different order predicted 117 for the amplitude of Solar Cycle 25 and that solar activity would be dominant in the southern hemisphere. Pishkalo (2021) using the absolute values of the mean polar magnetic fields during the two-year interval just before the cycle minimum in northern and southern hemispheres as precursors predicted 66 ± 17 and 83 ± 21 for northern and southern hemispheres’ amplitudes of Solar Cycle 25. Labonville, Charbonneau, and Lemerle (2019) from a data-driven solar cycle model predicted a low amplitude for Solar Cycle 25 and the northern hemisphere about 20% more than the southern hemisphere. Our earlier analysis (Javaraiah, 2021) also suggested that at the epoch of maximum of the Solar Cycle 25 the activity will be about 20% more in northern hemisphere than that in southern hemisphere, whereas our present analysis suggests that the southern hemisphere would be dominant. According to the international panel to forecast Solar Cycle 25, the amplitude of this cycle would be 115, which is almost the same as the amplitude of Solar Cycle 24 (see www.swpc.noaa.gov/news).

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Data Availability All data generated or analysed during this study are included in this article.

Declarations

Conflict of Interest The author declares that he has no conflicts of interest.

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