Lessons from mixing OR methods in practice: using DES and SD to explore a radiotherapy treatment planning process

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Abstract
Mixing Operational Research (OR) methods is becoming more commonplace. Discrete-Event Simulation (DES) and System Dynamics (SD) are popular modelling methods previously applied to a range of situations for various purposes, which are starting to be mixed in healthcare. However, the practicalities of mixing DES and SD in practice remain unclear. Radiotherapy treatment is a complex multi-stage process where technology and best practice continue to evolve. This paper describes a project undertaken to explore the treatment planning process using mixed OR methods. It presents insights obtained through mixing OR methods within a real-world project. The model development process, the role of each modelling method and the benefits of undertaking a mixed OR methods project design are described. Lessons for mixing DES and SD, and more generally mixing OR methods, are discussed.

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Introduction
Discrete-Event Simulation (DES) and System Dynamics (SD) are widely applied modelling methods that have clearly demonstrated their potential benefit to healthcare (Taylor & Lane, 1998; Cooper et al, 2007). The potential for mixing the methods has been discussed within the broad simulation community (Renshaw, 1991; Morecroft & Robinson, 2006), and also with regard to healthcare (Brailsford et al, 2010). However, how the methods may be mixed within the Operational Research (OR) field, both in theory and in practice, remains a topic up for discussion (Brailsford et al, 2010). This paper seeks to contribute to the discussion around the need for modellers to connect the rationale for mixing methods with the realised benefits in practice (Howick & Ackermann, 2011). Therefore, this paper uses a real-life project mixing DES and SD in practice with a radiotherapy treatment centre to reflect on the value and practicalities of mixing in practice.

Background
In this section the two simulation methods are introduced and briefly compared. Interest in the literature in mixing methods, motivation from
the modelling community to utilise mixing and the areas where further work is needed are then discussed.

SD and DES have been successfully applied independently to a range of health systems (Brailsford & Hilton, 2001). Both are popular yet distinct methods in the systems modelling field and previous work has highlighted the potential to offer complementary insights with benefits found in mixing them (Brailsford et al, 2014). Few examples of reflections on the practice of mixing DES and SD exist (Viana et al, 2014), and how to successfully undertake a mixed methods modelling process in real life is unclear (Brailsford et al, 2010).

**Discrete-event simulation**

In DES the dynamics of the system are driven by events. This allows users to model the individual events experienced within a system and the stochastic nature of the simulation encourages representation of the variability encountered in real life (Robinson, 2003). DES is often used to represent systems at an operational level, where individual detailed interactions and experience of entities over time is important and the variation in service experienced may be a key measure. Overall, DES has a characteristic style but may be applied in a variety of ways and have different characteristics depending on the problem situation it is applied to.

The method has widespread appeal as it allows a modeller to produce a simulation that may be a direct physical representation of the system under study, at the individual entity level. The variability inherent in everyday life can be captured and the interaction effect of stochastic elements can be observed. However, DES does not explicitly seek to model feedback; development can be timely (and costly); and it is heavily dependent on data to inform the system behaviour.

**System dynamics**

SD is used to discover the underlying principles and behaviour of complex systems over time thus capturing the average flow of the system (Forrester, 1958). It is a variation of continuous simulation modelling and may be characterised by its ability to represent feedback in systems. Feedback exists where ‘an action-taker will later be influenced by the consequences of his actions’ (Roberts, 1978, p. 7), and a feedback system is one that contains two or more interconnected loops. The efficacy of SD is based on its ability to capture the whole system rather than focusing on short-term goals and single measures of performance, which can lead to ineffective conclusions (Taylor & Dangerfield, 2005). The method has broad application and is often used for strategic issues such as: policy analysis (Taylor & Lane, 1998) and assessing the potential impact of altering services (Taylor & Dangerfield, 2005). The method cannot easily represent uncertainty in the data (Doebelin, 1998) but is effective at representing large (uniform) populations and simulating these systems quickly. This is useful within Healthcare to evaluate the long-term impact of complex policies (Kuljis et al, 2007). Models are, in general, a macroscopic view of a system, with an interest in how the system structure impacts the system behaviour, recognising that the behaviour of individual components of a system is distinct from the behaviour of the system as a whole.

**Comparability and complementarity**

An early comparison of SD with other forms of quantitative modelling is given by Randers (1980) and discussed by Lane (2000). Comparisons of SD specifically with DES are also made by Sweetser (1999), Brailsford & Hilton (2001), Morecroft & Robinson (2006), Tako & Robinson (2009, 2010) and Chahal & Eldabi (2008). However, many of these authors seek to place the two methods into two distinct boxes rather than highlight the similarities. Both methods are described as providing value and insight to the systems they seek to capture and the problems they aim to address. Both methods are suitable for providing increased understanding and aid decision-making and, in reality, the two methods demonstrate significant overlap.

All useful models are simplifications of reality but each method simplifies differing aspects of a system (Meadows, 1980; Pidd, 2003). Embedded within each method are its philosophical assumptions and principles. A primary concern when considering mixing methods is the issue of paradigm compatibility as both SD and DES have quite separate modelling philosophies (Lane, 2000). SD utilises feedback while adopting a system view to examine how causal structure results in observed behaviour. DES tends to focus on performance over time, illustrating how randomness influences behaviour (Tako & Robinson, 2009). However, these differing philosophical views, coupled with capturing a system and its problems at different levels of detail, may yield interesting alternative insights.

Both methods develop the understanding of a system (Tako & Robinson, 2009). DES often adopts an operational view to understand the detail complexity and explore different configurations (Chahal & Eldabi, 2008). SD may take a strategic view in order to appreciate how a system alters over time (dynamic complexity) and what impact the structure and feedback mechanisms have on the system (Owen et al, 2010). There is no question that each method has its place, but the primary difference is that DES does not obviously allow the user to understand the underlying mechanics of changing information and feedback; whereas these links and flows are transparent in SD (Tako & Robinson, 2010). The choice between DES and SD should be informed by the problem and the system (Borschchev & Filippov, 2004).

Although DES is a very powerful method, it is not possible to effectively capture problems dominated by dynamic or organisational complexity (Taylor & Lane, 1998). So, ‘by failing to appreciate the underlying feedback mechanisms, these interventions [DES] only have a limited effect’ (Taylor & Dangerfield, 2005, p. 659). SD offers a clear, considered approach to modelling systems but ‘is
NOT the only pebble on the beach and it is not the most appropriate approach to all problems at all times’ (Coyle, 1977, p. 355). It is Coyle’s own emphasis on the ‘NOT’ that forces the reader to acknowledge the strength of this statement. It would be easy to start to believe that SD is capable of tackling any system or indeed question thrown at it.

This discussion of SD and DES illustrates that it is not possible to simply map and compare the methods to reveal the potential for combination. It is necessary to obtain an understanding of the situation under study and then explore the potential modelling methods and whether it is appropriate and beneficial to mix them. The choice between DES and SD ‘often seems to be made based on an unknown, or at least unstated, user preference function’ (Koelling & Schwandt, 2005, p. 1322). If SD is efficient in policy design interventions and DES is efficient with policy implementation problems (Ceglowski et al, 2007), the question arises: can we have both? Simulation modelling can be time consuming (An & Jeng, 2005) and so could mixing methods help to reduce the time taken to produce useful, insightful models or increase the applicability and overall use of models?

**Mixing OR methods**

When embarking upon a simulation study two aspects should be examined to decide the focus of the study, and determine the level of accuracy and detail required in the model: the nature of the system (system) and the nature of the study (problem) (Pidd, 2004). Merely examining the problem perspective can be misleading (Lane et al, 2000). Indeed, Lorenz & Jost (2006) highlight the need for fitting the problem and system to the methods when combining paradigms. Method selection is often a personal choice and in practice the modeller can be guided by familiarity with a particular method (Brailsford & Hilton, 2000). Proponents of a specific method should take a ‘step back and assess which conceptual toolkit should be used’ (Chick, 2006, p. 22). Work exploring the model building process of SD and DES empirically supports this commonly held view that modellers will embark on a study without first considering alternative modelling methods (Tako & Robinson, 2010).

Mixing OR modelling methods raises many philosophical issues that Mingers & Brocklesby (1997), Mingers et al (1997) and Lane (2000) discuss at length. Jackson (1999) and Kotiadis & Mingers (2006) add to this discussion of the benefits and potential problems of mixing OR methods in general. Cultural and cognitive concerns impact the feasibility of a mixed OR methods project as organisations and individuals may not be open to the methodology. However, real-world problem situations are highly complex and multidimensional, and potentially may benefit from different paradigms to focus on different aspects of a situation.

**Mixing DES and SD**

Despite the limited selection of work that exists in the area, mixed DES and SD modelling is undertaken in a range of disciplines: Management Science, Mathematics, Computer Science and Engineering. The literature can be split into two groups: work describing a hypothetical or sample project selected by the modellers to illustrate a specific approach to mixing the methods, and real-life projects that have used mixed SD and DES to contribute to a problematic system (the focus of this paper).

Lane (2000) recommends using both DES and SD to develop a richer understanding of a problem and system. DES and SD have been mixed in a variety of ways (discussed in Morgan, 2013). This can range from the methods being used to provide comparative insights to the same problem with the same level of detail modelled, to the methods being fully integrated with each method influencing the other throughout the simulation time. Even the relatively low number of mixed DES and SD projects in the literature illustrates that philosophical, conceptual and technical concerns are no longer a barrier to mixing the methods. Mixing simulation methods is viewed by some as ‘no big deal’ (Pidd, 2012), but the modelling processes involved (and the benefits thereof) are unclear.

In practice, Djanatliev et al (2014) note that mixing methods was challenging and time intensive, but the initial effort will be rewarded through reuse in the design stages of later projects. Ingenuity, creativity and questionable assumptions may be required to fit a problem within a single modelling paradigm and so mixing methods may be the only appropriate choice (Viana, 2014). Zhu & Mostafavi (2014) focus on the challenge of the technical aspects of mixing DES and SD (as illustrated by a simple example), but no comment is made on the modelling process as a whole. All cases note similar key experiences of mixing methods from the modeller’s perspective: experience (in mixing and the methods) is required, it is challenging technically, and each problem is unique. Onggo (2014) adds to this emphasis that there are design decisions required in mixing methods (to decide whether to implement elements of models), and these design decisions form part of the modelling process. SD and DES have been successfully mixed but insight is still needed into a ‘practical methodology for combining SD and DES in a real context’ (Brailsford et al, 2010, p. 2294) and lessons for mixing OR methods in practice (Howick & Ackermann, 2011). It is unclear what design choices are made throughout a mixed methods modelling process.

The following section summarises an action research project undertaken to explore mixing DES and SD in practice. All stages of the project are discussed: from initial problem structuring (highlighting the unique roles SD and DES), model conceptualisation (considering complementarity of methods), to the final models developed in collaboration with stakeholders.

**Model development**

This section begins with a description of the action research project setting, followed by the problem structuring work undertaken by the modeller. A description of the
problem definition, the DES and SD models, respectively, and the model assumptions follows. The development of the models was an iterative process but is presented in two distinct sections for clarity.

Setting and research methodology
The Beatson West of Scotland Cancer Centre is Scotland’s largest cancer centre serving a population of 2.6 million. The centre provides holistic cancer care, but this project is focused specifically on radiotherapy, with the centre delivering over 300 doses of radiotherapy per day (www.beatson.scot.nhs.uk). Radiotherapy can be used to eradicate cancer cells to eliminate disease (radical treatment) or to relieve cancer symptoms (palliative treatment). Patient treatment is a complex, multistage process that intends to cause as little harm as possible to normal cells by aiming the treatment at the affected area of the body. It requires careful planning and has to be tailored to individual patient physiology. The key stages involved with radiotherapy are booking, simulation, planning and treatment. These are interrelated stages with feedback throughout as a patient’s treatment plan may need to be altered or scans may need to be redone. The department continued to face numerous strategic and operational issues, with external and internal influences, and this project provided the client with an opportunity to choose to examine these from a new perspective.

Action research was the overarching research methodology for this project. Action research is a cyclical and reflexive research, to generate living theories (McNiff & Whitehead, 2006). It is a systematic process of enquiry to enhance the outcome for clients, providing methods to improve intervention effectiveness (Stringer & Genat, 2004). The researcher was a participant in, rather than an impartial spectator of, a project. This meant the researcher engaged in and reflected on the model-building process in order to examine the applicability and challenges of mixing DES and SD. The setting of this research being a real, complex system enabled contribution of practical insights.

Semi-structured interviews were used for the initial system exploration (discussed in the next section). Unstructured interviews with the client throughout the project were used to develop the models, the recordings of which were examined to generate insights into the model development process and mixing DES and SD. Modeller and researcher insights are provided alongside insights from the client through reflection (consisting of note-taking and maintaining a reflective diary).

Problem and system exploration
As the problem at the centre was not well defined it was necessary to examine potential areas for investigation and determine focus. The initial phase of the project was to explore the system and structure the problem by eliciting issues and views from stakeholders using techniques equally applicable to SD and DES. Causal mapping was utilised to focus on the beliefs, values and assumptions an individual has about the system and reveal issues in an unbiased manner, enabling the large amounts of information to be collated and detailed and holistic properties to be explored (Ackermann & Eden, 2005).

Individual interviews were conducted with seven stakeholders selected to represent a range of views held within the Radiotherapy Department, including management, clinicians and radiotherapy staff. These interviews were semi-structured and aimed to explore the system of interest, highlight aspirations, expose areas of concern and eventually lead to definition of the problem area(s). Interviews were mapped and merged to form a collective causal map of the system. This was examined to identify key themes and areas of focus for the project. Interviewees were asked to confirm that the resulting group map of the system was a fair representation of their views to ensure relevance.

The issue selected for the project was Treatment Complexity and Changes in Treatment Regime. This was a high priority issue, with DES-like and SD-like questions raised in relation to it, with a wide impact on the performance of the system. A fraction is the base unit of treatment during a visit to the radiotherapy department, delivered at regular intervals (such as daily). A phase of radiotherapy treatment consists of several treatment fractions. A single course of treatment is designed around a single treatment regime and may consist of one or more phases, requiring one or more treatment plans to be created. The complexity of these plans can vary for the different cancer types and the characteristics of the patient’s disease. Advances in radiotherapy research lead to new techniques becoming available and the centre must decide which treatments to make available to patients. The centre is subject to performance targets around the time taken between initial referral and receipt of first radiotherapy treatment fraction.

The nature of the problem is summarised in Figure 1. This diagram has been developed from the collective map and illustrates the aspirations of staff (seeking to maintain the Radiotherapy Department’s reputation for clinical excellence), while ensuring that the impact of implementing new regimes does not negatively impact Key Performance Indicators and equality of access for patients. It also reflects the impact changing radiotherapy regimes has on the capacity of the system by changing the time required imaging, planning and treating patients.

The maps and interviews were re-examined to determine the key questions being posed to inform the project methodology:

1. What is currently provided at the Centre, how quickly and with what variability? How is resource availability impacting equality of treatment across all patients?
2. What is the impact of changing treatment regimes and the mix of regimes? Is it possible to maintain current throughput?
3. What is the impact on different patient groups?
4. What can realistically be implemented and what resources would be required?
5. What would be the impact of a policy change regarding regimes?

These questions display both SD and DES characteristics. Mixing the methods would allow exploration of both goals, whereas adopting only one method would require several assumptions about behaviour to be made. In an SD model it would be necessary to assume all patients behave similarly; an SD model is not designed to reveal the range in variability patients may experience within the system. Conversely, within a DES it would be necessary to assume a fixed plan for the implementation of more complex regimes and not allow exploration of the systems propensity to cope with pressure (feedback within the system to reduce complexity).

Two key goals are extracted by examining the collective map and summarizing the questions:

Goal A: Explore the dynamics of government targets interacting with R&D adoption
Goal B: Examine the day to day impact of changing the complexity of treatment regimes

In this project, SD was used to capture the dynamic nature of the problem (Goal A), while DES was used to appreciate the impact on the day to day running of the centre (Goal B). It was felt that the two methods held explicit roles within the modelling intervention and that a complementary approach to modelling be adopted. In order to examine the day to day impact of changing treatment regimes it was necessary to develop an understanding of the general influence complex technology adoption can have on the system.

This section has outlined the system and problem definition process undertaken with the centre. This work led to the focus of the models, the questions to be addressed during the intervention and design of the combination of SD and DES. The following section presents the models developed with the centre.

**SD model**

A SD model (illustrated in Figure 2) was developed to capture the dynamics of how the department responds to increasing referral to first treatment times by managing working hours and reducing the complexity of the treatment regimes adopted. As more complex treatments are introduced the expected treatment time increases. The initial impact on treatment time is higher than the ‘expected’ average level because of overall experience within the department dropping and this learning process has an additional impact on the realized treatment time, which impacts the wait experienced by patients. Staff (in the first instance) will try to manage the queue by working longer hours, allowing complexity to be maintained. As referral to first treatment times continue to increase the system seeks to reduce the adoption of complexity to balance the system.

This model is used to illustrate system management necessary to ensure that referral to first treatment times experienced by patients do not exceed government targets (or some other desirable level) by adjusting the pattern of complex treatment adoption and work hours. Delay is built into the model to reflect the time it takes for referral to first treatment time to be reported to management and thus to allow for a change in behaviour. This model captures the pressure to drive down referral to first treatment times, illustrates the careful balance that needs to be maintained within the system and that treatment time needs to be managed carefully.

The model consists of nine stocks. ‘Impact of complexity’ and ‘complexity adopted’ are scalars, and ‘patients to treat’ is measured in number of patients. The remaining six stocks represent resource time (measured in hours of a
clinician’s time). As the level of treatment complexity available to radiotherapy physicists’ changes over time, the Beatson chooses to adopt complex regimes depending on the wait for treatment being experienced by patients.

The treatment process at the centre is modelled in SD as a single stock and flow, but may be broken down further using a DES to include the intricacies of the flow of patients. The SD model currently represents the average population behaviour within the system but further insights can be gained by considering the individualistic behaviour of patients and their respective treatment plans. The centre has numerous resource restrictions, varying treatment regimes and a range of routes a patient may take through the treatment process meaning that an increase in treatment complexity can have extensive and diverse impact on the wait time for some cohorts of patients.

DES model

The conceptual model of the DES is presented in Figure 3. The four core elements of the model are circled (booking, imaging, planning and treatment). This model was used to provide more representative insights into the knock-on impact of altering the treatment time or number of treatment fractions for different groups of patients. Individual patient characteristics, timetables and work plans can be more easily and transparently represented in DES (see Appendix A for a more detailed representation of the treatment process and Appendix B for the final model). The model provided better understanding of the referral to

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**Figure 2** Overview of the SD model of the centre – Treatment complexity impacting referral to first treatment times, which influences work hours and complex treatment adoption. Note that each stock of time realised (shown) has an equivalent time expected (not shown) that are used to illustrate the challenges of implementing a new treatment regime.

**Figure 3** Simple conceptual model of operational processes at the centre.
first treatment times experienced and the resulting variation across patients. This enabled the centre to carefully consider the adoption and implementation of such changes in regime, maintaining the throughput of the system and minimising the variation of referral to first treatment times experienced by patients, which reflects access to appropriate and timely treatment.

The DES model may be summarised by the following six stages and characteristics:

**Arrivals and booking:** The arrival of new patients into the Beatson is split according to 20 ICD10 cancer codes. Demand is static (to represent the current situation) with inter-arrival times exponentially distributed.

**Imaging:** Time spent on scanning machines depends on the type of cancer, the type of scan carried out and whether radical or palliative care is being provided. All treatment fractions per course are planned before first treatment.

**Treatment Planning:** Planning is undertaken by skilled radiotherapy physicists with the time taken dependent on the complexity of the treatment regime. Times were estimated by a senior radiotherapy physicist. The requirement for consultants during the planning process depends on the treatment regime.

**Treatment:** The centre has 11 treatment machines. Patients attend treatment for a number of fractions with each fraction being equal to one visit. The duration of a treatment fraction depends on the individual characteristics of the patient being treated.

**Resources:** Staff resources work according to shift patterns that do not change throughout the year of the baseline model (recruitment or commissioning of machines evaluated in scenarios). Activity (such as imaging, planning or treatment) in the model cannot commence until the required resources are available. Re-booked, re-scanned or re-treated patients are modelled to highlight the delays caused by unutilised slots and rework.

**Model Parameters and Queuing convention:** The model runs for 1 year with a 4-week warm-up. All patients are attended to on a first come first serve basis at each server. Priority is given to patients returning to the planning stage over new arrivals to ensure timely arrival at treatment. There is no maximum time a patient will spend in the system before they leave voluntarily: all patients wait until they are able to be seen.

**Key Metrics:** In 2010 over 6,400 new referrals were received; 8,000 scans/images were taken; and over 100,000 treatment fractions delivered. On average, one referral requires one treatment course consisting of 1.4 phases, with 17 fractions per phase (increases to 24 fractions per phase for radical treatment patients). The centre is operational 13 hours a day, working to a 31-day target for referral to first treatment fraction. Initial analysis in the simulation found the average expected time would be 28.5 days. All treatments are manually booked at the same time ahead of the first visit. The number and frequency of appointments (time required between fractions) is determined by the radiotherapy physicist as part of the treatment plan, with most scheduled a day apart.

**Mixed methods design**

The design of this study was initially Sequential, using SD to explore the problem within the wider context of the system and develop initial understanding of the concepts involved, followed by DES to consider how to implement changes at ground level. Deeper, more technically interacting mixed method designs were kept in mind at all stages of model development as possible directions for the project. The modeller identified overlaps and points of exchange between the methods during the project.

In actuality, the models were developed iteratively with each model stage informing the developments made in the next (illustrated in Figure 4). The focus of the SD model was on the wider system behaviour and the DES intended to explore the physical processes within the centre. The differing model boundaries suited to each method made a comparison between the methods illogical/unsuitable. Development of the DES required significant insight into the system that it was possible to develop while constructing the SD model. The complementary use of DES allowed examination of the variation in the impact felt by increasing treatment times or changing the treatment mix. This developed understanding of the knock-on impact can then be used to inform the SD model and the relationship between treatment time and the resulting time a patient takes to progress through treatment (the wait). By examining the problem through a mixed methods lens allows the system to be analysed at several levels of detail and enables the wider policy issues to be explored.

In the past, the key contact for the project within the cancer centre had been drawn to data-intensive detailed analysis of the system that is not always practical because of data limitations. The current approach has enabled wider issues to be examined and the general impact of policies on the overall functionality of the system to be assessed before examining the impact at a patient level. It enabled new questions to be posed and reflections to be made on how the centre functions. In addition, the approach has highlighted what measures might be used to assess performance through discussion around the use of throughput vs referral to first treatment times vs treatment outcomes. The iterative model development also

![Figure 4](image-url)  
**Figure 4** Iterative mixed method design – Size of the ellipses are proportional to the detail included in and extent of the boundary of the model.
resulted in emergent learning from the models, with stakeholders developing their understanding of the system and the challenges faced alongside the modeller.

**Modelling results and insights**

This section describes the insights obtained from the models throughout the modelling process. Baseline models were agreed with the stakeholders and numerous scenarios were explored. Details of model runs are not included because of space limitations, but the impact of the model experimentation is discussed.

**SD modelling**

The SD model enabled the client to observe the impact of decisions stemming from the feedback structure of the system. Strategies to respond to an increasing amount of time required to prepare and deliver plans were explored to avoid an overall increase in the time at treatment machines. The impact of changing treatment regimes on staff working practices, such as the expected time needed to produce plans, the need for overall increase in the knowledge based of staff and increased frequency of training, were observed in the model.

A progressive implementation strategy was required to cope with the learning process involved with changing treatment regimes, whereby the times required for activities peak then return to an expected level (the target level for that regime). New regimes increase the time required to plan: as treatment regimes become more complex, more complex plans are required. Although the number of plans may decrease as the number of treatment courses per patient falls, the total time a planner spends per treatment plan will increase as complex treatments become common place. Reducing the number of treatment fractions can mean that higher doses are delivered per fraction and so more complex plans are required per treatment phase. This means more time is required to plan ahead of the first phase making government targets for timely access to this stage more challenging to meet.

The net effect of new regimes is to reduce staff and resource workload. Planning is the only part of the planning and treatment process that experiences an increase in workload. All other parts of the system will eventually experience a fall in demand per patient (although the number of patients will continue to increase). New regimes offer the opportunity for a progressive decrease in the number of treatment phases required per patient, a progressive increase in time required on treatment machine per session per patient but a decrease in the overall contact time on an expensive resource – treatment machines. Fewer phases implies fewer visits to hospital for the patient and overall shorter treatments.

**DES modelling**

The base scenario highlighted the sensitivity of the system because of how close to capacity it is functioning. Any peaks in demand can cause the system to tip queue growth out of control. Experimentation revealed that increasing the flexibility of consultant work patterns (to be available at different areas throughout a week) generates a greater improvement in time to reach treatment than sharing patients between consultant groups.

Increasing patient access to more complex treatment regimes requires investment in staff and treatment delivery machines. The system is able to cope with the first marginal increase in access, but all other scenarios require adjustments to be made to the system. The model highlighted that additional machines are needed in order to maintain waiting targets if more than 25% of radical patients receive complex treatment regimes. Providing access for all radical patients to the more complex treatment regimes requires the time taken in treatment planning to reduce significantly (through investment in training) or more staff.

Changing capacity marginally was found to have a significant impact on the ability of the system to cope with demand, and reduce patient referral to first treatment times. The system copes on paper, but when the variation in arrivals of patients is taken into account there is a high chance of the system becoming unable to cope and failing to meet targets. In reality all staff will strive to ensure treatment is received in a timely fashion and the best possible care is provided.

Work is already undertaken outside of calculated work hours in order to meet patient needs and unless this is accounted for proposals such as extending working days may have a greater impact on staff workload than predicted. The scenarios modelled in this project were a subset of possible future setups of the system that gave stakeholders the opportunity to confirm or challenge beliefs about the system.

**Insights from iterative modelling**

The iterative mixed method design benefited the project by enabling insights from one method model to inform the development of the other method model. Maintaining two models encouraged the modeller to limit the complexity of each by carefully considering what detail and boundary to capture within each model. This meant that the first iteration of the SD model captured a strategic view and highlighted that more (operational) detail was needed into the stages of the treatment process. Then, by modelling the treatment process (in DES) and exploring the required parameters, resources and constraints, the model highlighted important concepts to include in the SD model. That is, that the DES model provided feedback to the strategic level of the original questions posed, enabling the questions to be formulated more precisely and the SD model to be adjusted.

**Lessons from practice**

During the model development process the modeller kept detailed notes and (where possible) recordings of key meetings with the client. As part of the action research methodology, three reflective cycles were undertaken to generate client and modeller insights. The following three
Paragraphs discuss the insights obtained, grouped according to: the modellers reflections on the project exploration methodology, the value of the models generated as observed from the modellers perspective and researcher perspective reflections on the value of the models and the process.

The use of causal mapping as a problem structuring tool provided the modeller with a method open to capturing a broad range of issues, without being specifically DES or SD focused. On reflection, the use of the problem structuring process enabled the modeller to engage with the individual views and the two simulation methods enabled representation of the system at two levels of focus.

Both SD and DES had explicit roles to play. In relation to the questions posed around changing treatment regimes, the two models agree on the direction of the impact on the system, with SD able to illustrate the range and scale of the impact of some changes, and the DES illustrating the ability of the system to cope on a day to day basis. The use of SD modelling enabled exploration of the value of changing to more complex treatment regimes. DES modelling aided identification of process restrictions and limitations. Both models were used to develop understanding of the system while building a case for/against policy changes. They present two complementary views of the system, with each adding value to the other through the understanding developed during the modelling process. Both methods revealed different perspectives on the system, with insight from the use of one method informing the development of the other model as well as its own.

Positive feedback on the project was received from all stakeholders, but with each finding value in the process at different points (from the initial mapping to the final communication of model results). By the end of the project stakeholders appeared to have accepted the roles of the models, and that the SD model represented some important relationships that impacted upon the DES and so the DES should not be taken in isolation. The two models highlighted that stakeholders with only operational questions and issues need to appreciate the wider system for relationships they may fail to consider. This is not only an outcome of the model but also may be a generalisation for a nested system view.

Discussion

OR methods are mixed in practice to: deal with problems in complex systems, support stages of a project, obtain specific benefits from specific methods and overcome shortfalls of methods (Howick & Ackermann, 2011). The rationale for mixed DES and SD projects are similar: the most suitable (or only) way to answer the questions raised, the client requested specific method(s), the system is unique and complex, the desire to do something different, the need to obtain comparative insights, the apparent stages of insight required. These can broadly be split into two groups: personal preferences of the modeller and/or the client and the specifics of the problem and system.

The key difference between the two methods, and benefit to the project, observed by the researcher during the modelling intervention was the different world views of the problem and system a modeller is able to adopt with each method. Although each method may be adapted to create a model similar to the other, the overall philosophies of each method encourage the modeller to think of the system in terms of two different perspectives. These are often referred to as the operational and the strategic perspectives. These two terms are often pigeonholed to imply that DES and SD are only applicable to systems that conform to these respective perspectives. However, it should be noted that these terms do not represent two different types of system but rather two views the modeller might take of a system: the operational perspective is one that considers how the system can be made to function (such as what shift pattern needs to be applied), and the strategic perspective is one that considers what makes the system function (such as what is the maximum hours staff should be working).

Considering the realised benefits of mixing methods, from the client’s perspective, their beliefs about behaviour of the system were challenged. The use of both DES and SD enabled stakeholders to view the radiotherapy treatment process both as an operational system that needed to minimise the time patients wait for treatment, but also as a larger interacting system. This led to a change in understanding by stakeholders; an appreciation of the need to explore how strategic decisions influence day-to-day activity and can present unforeseen challenges (SD informing DES) and the long-term knock-on impact of operational decisions (DES informing SD). From the modeller’s perspective, personal perceptions of the system were also challenged. Cycling between methods encouraged explicit consideration of what is really needed in the models, leading to a fresh perspective of the system.

Could the same insights have been achieved without mixing? In this project, it may have been possible technically to represent both models within a single software package. However, that is not to say that it would have only been a single method that the modeller was adopting. Embarking on the project with only the view to use one of the methods may not have led to the same outputs. It comes down to modeller choice and modeller insight. It is up to the modeller (along with the client) to decide on the detail and boundary of the project, which in turn informs the method(s) used. Exhaustive scenario testing may have led to the conclusion about the dynamics of new treatment regimes. But, talking through the adoption of new treatment regimes with the stakeholders and representing the process as a SD model enabled their suspicions to be made clear without the need for extensive scenario analysis. Healthcare models need to be able to represent the different levels at which different individuals view the system.

Within the project at the Beatson, the two perspectives offered by the two methods boil down to how the resources could or should be allocated throughout the system to cope with the demand, and what factors impact these resources. This project demonstrates that answers to
both are needed to obtain an insightful view on the system. Considering only how to allocate the resources (utilising only DES) may have led to poorly informed conclusions. Similarly, using only SD within the project would have required the method to be stretched to include stochastic events, individual entities and detail complexity. Therefore, in this project, trying to apply SD in isolation may have resulted in utilising an enriched mixed method design.

This modelling project utilised SD first, followed by DES as it was intended that the SD model would capture a larger system view. Equally a modeller may choose to use DES first in the same situation to obtain a detailed insight into a smaller part of the system before modelling the wider system. The order in which methods are used reflects a modeller’s preference, the information available to a modeller at the time and what the project required.

Healthcare systems are complex, with a history as a setting for simulation, and so offer rich settings for research into modelling processes. Although the modeller was required to develop an understanding of this complex system in order to build the models, this was not the largest hurdle of the project. The main challenge was how to conceptualise a mixed method model. This was achieved by iteratively developing the models that in turn highlighted points of commonality and complementarity, revealing points of interaction between the models. Just like using any method (such as SD or DES) it may be deduced that it takes practice and guidance to mix methods. Simple example models illustrate the functionality of mixing methods, but may oversimplify the development process by failing to demonstrate the struggle to decide how the model will work. A review of mixed OR method projects highlighted how ‘many people do not consciously reflect on or articulate their methodological decisions’ (Howick & Ackermann, 2011). There exists a need for OR modellers to connect the rationale for mixing (the expected benefits) with the actual benefits and outputs of the project. This paper has sought to provide an example of a mixed SD and DES modelling project where the modeller consciously reflects on the process throughout.

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Appendix A

Figure A1

Detailed conceptual model of the operational processes at the centre.

Appendix B

Figure B1  Detailed DES model of the centre – Modelling resource workload from patient referral to treatment.