High-Temperature Phonon Spectra of Multiferroic BiFeO$_3$ from Inelastic Neutron Spectroscopy

Mohamed Zbir
Institut Laue-Langevin, BP 156, F-38042 Grenoble Cedex 9, France

Helmut Schober
Institut Laue-Langevin, BP 156, F-38042 Grenoble Cedex 9, France, and,
Université Joseph Fourier, Unité de Formation et de Recherche (UFR) de Physique, F-38041 Grenoble Cedex 9, France

Narayani Choudhury
Department of Physics, University of Arkansas, Fayetteville, Arkansas 72701, USA

Ranjan Mittal, Samrath L. Chaplot
Solid State Physics Division, Bhabha Atomic Research Centre, Trombay, Mumbai 400 085, India

Sadequa J. Patwe, Srungarpur N. Achary, Avesh K. Tyagi
Chemistry Division, Bhabha Atomic Research Centre, Trombay, Mumbai 400 085, India

We report inelastic neutron scattering measurements of the phonon spectra in a pure powder sample of the multiferroic material BiFeO$_3$. A high-temperature range was covered to unravel the changes in the phonon dynamics across the Néel (T$_N$ ~ 650 K) and Curie (T$_C$ ~ 1100 K) temperatures. Experimental results are accompanied by ab-initio lattice dynamical simulations of phonon density of states to enable microscopic interpretations of the observed data. The calculations reproduce well the observed vibrational features and provide the partial atomic vibrational components. Our results reveal clearly the signature of three different phase transitions both in the diffraction patterns and phonon spectra. The phonon modes are found to be most affected by the transition at the T$_C$. The spectroscopic evidence for the existence of a different structural modification just below the decomposition limit (T$_D$ ~ 1240 K) is unambiguous indicating strong structural changes that may be related to oxygen vacancies and concomitant Fe$^{3+}$ → Fe$^{2+}$ reduction and spin transition.

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Multiferroism is the combination of two or more of the following properties: ferroelectricity, ferromagnetism and ferroelasticity. In particular, tuning the electric or magnetic properties by applying a magnetic or an electric field, respectively, is at the basis of new applications in microelectronics, spintronics, data storage and computing hardware. This explains the strong interest in multiferroic materials from a practical point of view. They unfortunately do not abound in nature and are often difficult to synthesize technologically. Within the most important ABO$_3$ perovskite family the scarcity of multiferroic properties is mainly due to the d-electrons of the B cation, which on one side are necessary for magnetism but on the other side tend to reduce the tendency for an off-centering ferroelectric distortion. A remarkable exception is bismuth ferrite BiFeO$_3$ (BFO). This material seems to be unique in exhibiting multiferroic behavior above room temperature. It is simultaneously ferroelectric, antiferromagnetic and ferroelastic, and is subject to crystallographic distortions. The mixture of these multiple order parameters involved in its phase transitions is believed to lead to a very rich phase diagram. The physical behavior of BFO is characterized by two largely different transition temperatures: antiferromagnetic with T$_N$ ~ 600 - 650 K and ferroelectric with T$_C$ ~ 1050 - 1100 K, and a polarization that can reach a very large value ~ 100 µC/m$^2$. The large value of the Curie temperature could be at the origin of the observed colossal spontaneous polarization through a strong ferroelectric ordering. The polarization in BFO is mainly caused by the Bi 6s$^2$ lone pair, so that ferroelectricity is induced primarily via this site (strong cation displacements). Another remarkable aspect of BFO is the occurrence of FeO$_6$ octahedra tilts accompanying the strong Bi$^{3+}$ displacements at room temperature. Below T$_N$ the magnetic ordering is non-collinear with a G-type-like cycloidal spin-spiral arrangement and the structure is incommensurate with an extremely long period of 620 Å. The coexistence of high-temperature magnetism and strong ferroelectricity makes BFO a material with physical properties of practical importance. Due to these exceptional characteristics, BFO has become one of the most studied multiferroic materials leading to a wealth of experimental and simulation results covering both structure and dynamics. The keen and continuous interest is equally motivated by the controversies raised by a priori incompatibility of phase diagram, occurrence and nature of phase transitions, assignment and characterization of frequency modes from different spectroscopy techniques (Raman, infrared, ...).

Investigations of the vibrational dynamics could help...
to lift at least some of the controversies. Numerous Raman and infrared measurements show that the different phase transitions leave clear signatures in the vibrational modes. The limitation of optical spectroscopy to the Brillouin zone centre, however, prevents obtaining a complete picture of the interplay of dynamical and structural instabilities. In particular zone boundary modes could contribute to the unusual properties of BFO like the non-centrosymmetric positional shift, which induces ferroelectricity. The strong debate concerning the mode assignments from Raman and infrared spectroscopies just reflects the difficulties in establishing the structural phase diagram. It thus seems obvious that the structural information obtained from different diffraction techniques should be adequately complemented by spectroscopic investigations covering the full Brillouin zone. A concrete argument in favor of adopting such techniques, like inelastic neutron scattering (INS), arises from the fact that diffraction experiments allow to capture only the time-averaged structure with the consequence of missing subtle structural instabilities and distortions that perovskites are often subjected to. At complete odds with the importance of BFO, no INS measurements across both Neé and Curie transition temperatures have been attempted up to now. The present letter aims at closing this gap by probing phonon dynamics over the entire Brillouin zone and over a wide high-temperature range covering both the T_N and T_C. We devote particular attention to the crossing of the Curie temperature T_C where the ferroelectric-to-paraelectric transition occurs and concomitantly the electric polarization should show a sudden drop. Furthermore, within this high temperature domain some important changes in the electronic properties occur like the observed metal-to-insulator transition around 1200 K and a presumably high-spin to low-spin transition, resulting from the reduction of Fe^{3+} to Fe^{2+}. The latter, if it involves a large fraction of the ions, can lead to an increase in the cell volume and, therefore, should be accompanied by a strong dynamical signature.

Polycrystalline samples of BiFeO_3 were prepared by solid state reaction of stoichiometric amounts of Bi_2O_3 (Alfa, 99.5 %) and Fe_2O_3 (Alfa, 99.5 %). Bi_2O_3 was heated to 800 °C in order to avoid any carbonate or oxy-carbonate in the starting material. Fe_2O_3 was heated to around 300 °C in order to eliminate any adsorbed water molecules. Appropriate amounts of Bi_2O_3 and Fe_2O_3 were thoroughly homogenized using agate mortar pestle with acetone as grinding medium. The well homogenized powder sample was pelletized to a disk of about 1” diameter and 0.5” thickness and heated to 100-150 °C to remove any residual organic component. Further the pellet was inserted directly into a furnace with a preset temperature of 700°C and soaked for about 4 h and then quenched to ambient temperature by removing the sample from the hot zone of the furnace. At this stage the majority of sample formed as rhombohedral BiFeO_3. Further the pellet was crushed to powder and repelletized and heated in a similar manner at 850 °C for 4 h and quenched to ambient temperature. The sample obtained after this heat treatment was characterized by XRD recorded on a Philips Xpert-pro diffractometer in the angular range of 10-110° with a step width of 0.02° using Ni filtered Cu-K radiation. All the observed reflections could be assigned to BiFeO_3 (rhombohedral R3c). The powder XRD data was further analyzed by Rietveld refinement with the reported structural data for BiFeO_3. The final refined unit cell parameters a = 5.5775(2) and c = 13.8648(5) Å are in good agreement with parameters reported earlier for BiFeO_3.

The INS measurements were performed at the Institut Laue Langevin (ILL) (Grenoble, France) on 8 grams of powder sample prepared as described above. We used the cold neutron time-of-flight spectrometer IN6 operating with an incident wavelength $\lambda_i = 4.14$ Å (E_i = 4.77 meV), which provides a good resolution within the considered dynamical range for the anti-Stokes side. The data analysis was done using ILL software tools and the dynamical structure factor $S(Q, E)$, diffractograms and the generalized density of states (GDOS) were evaluated using standard ILL procedures without applying multi-phonon corrections.

We complement the experiment with density functional based ab-initio lattice dynamical calculations to (i) reproduce the observed generalized phonon density of states (GDOS) and (ii) to extract the partial (atomic) vibrational components contributing to the total spectrum. The starting geometry for the calculations was the experimentally refined structure in the rhombohedral phase R3c space group. A G-type magnetic ordering was assumed as a spin configuration to account for magnetism of Fe cations. Relaxed geometries, total energies and phonon frequencies were obtained within the 0 K first principles framework (which allows a correct treatment of the ground state), using similar computational procedure as described previously. In order to determine accurately all the force constants, the supercell approach was used for lattice dynamics calculations. A supercell ($8 \times a, 8 \times b, 8 \times c$) was constructed from the relaxed geometry containing 16 formula units (80 atoms). Total energies and Hellmann-Feynman forces were calculated for 18 structures resulting from individual displacements of the symmetry inequivalent atoms in the supercell, along with the inequivalent cartesian directions ±x, ±y, and ±z.

The temperature evolution of the dynamic structure factor $S(Q, E)$ (Figure 1) reveals considerable changes up to 1200 K. As a first step it is useful to concentrate on the elastic response in order to verify the phase properties. The diffraction patterns obtained from the time-of-flight data are reported on Figure 2(a). As indicated by the complete disappearance of the magnetic Bragg peak at 1.4 Å$^{-1}$ the system loses magnetic ordering close to 650 K. As the temperature increases further the intensities of the two Bragg features located at 1.6 and 2.3 Å$^{-1}$ decrease steadily reflecting the increased thermal motion of the ions. At $T_C$ (1050 - 1100 K) the diffraction pattern...
changes dramatically indicating that a structural phase transition took place. As the system is heated further there is a second abrupt change of the diffraction pattern at about 1200 K, i.e. slightly below the decomposition temperature $T_D = 1240$ K. These findings are consistent with recent powder neutron diffraction studies\textsuperscript{24} reporting the probable existence of three phases $\alpha$ ($T_\alpha < T_C$), $\beta$ ($T_\beta < T_\gamma < T_D$) and $\gamma$ ($T_\beta < T_\gamma < T_D$).

In view of the strong debate concerning the existence of these phases in the bulk material BFO, Figure 2(b) shows the phonon spectra, in terms of generalized density of states (GDOS) over the explored temperature range\textsuperscript{28}. In order to analyze the temperature-dependent dynamic response contained in the measured GDOS we use the ab-initio simulated spectrum as a reference point. Figure 2(c) compares calculated and observed phonon spectra in the ferroelectric $\alpha$ phase. In order to compare with experimental data, the calculated GDOS was determined as the sum of the partial vibrational densities of states $g_i$, weighted by the atomic scattering cross sections (as seen by neutrons) and masses: $\text{GDOS} = \sum_i (\sigma_i/M_i) g_i$, where $\sigma_i/M_i = 0.264$ (O), 0.207 (Fe), 0.044 (Bi); $i = \{\text{O, Fe, Bi}\}$. All the observed features are well reproduced by the calculations. The simulated phonon frequencies and intensity ratios between the different peaks are in good agreement with the measurements. Based on this we can consider that the experimental data validate the computational approach. We notice that our calculated GDOS matches also other available theoretical works\textsuperscript{29}. A more detailed look at the calculated phonons of BFO is shown in Figure 2(d). Therein the partial phonon density of states (PDOS) are represented. There is a contribution from all the atoms in the range 0 - 14 meV with an increasing amplitude as the atomic mass increases, i.e. Bi has the highest intensity in this region. The low-frequency region is separated from the rest of the spectrum by a gap (14-17 meV). Beyond 14 meV the Bi cations do not exhibit any dynamics. The Fe and O density of states are both strongly present in the mid-part of the spectrum spreading from 14 < $E$ < 45 meV. The oxygen stretch modes dominate at the highest frequency end of the spectrum (45 < $E$ < 70 meV). It should be noted that available high-temperature optical spectra\textsuperscript{16} shows a similar trend comparing to the presently reported phonon spectra in terms of temperature-dependent dynamical evolution of BiFeO$_3$.

The phonon dynamics as a function of temperature consistently reflects the suite of phase transitions deduced from the diffraction data. Apart from some indication for a broadening of the spectra in the oxygen dominated region beyond 45 meV the magnetic transition leaves a rather weak trace in the phonon spectrum. It is mainly characterized by the appearance of strong paramagnetic scattering at the location of the magnetic Bragg peaks when the transition is passed (Figure 1). The broadening of the phonon bands and concomitant filling of the gap continues when heating within the polar ferroelectric $\alpha$-phase (770 - 1100 K). This indicates a very strong anharmonicity of the phonon dynamics in this phase. The phonon modes are most affected by the transition at $T_C$ (1050 - 1100 K) where BFO changes from the polar ferroelectric $\alpha$-phase to a paraelectric intermediate $\beta$-phase. This holds in particular for the low-frequency part of the spectrum and makes the statement that these modes could provide coupling of magnetism and ferroelectricity all the more plausible. In the $\beta$ phase (1100 - 1170 K), the intermediate frequency part is subject to a considerable downshift resulting in a complete filling of the gap that was separating the intermediate and low-energy regions. The system undergoes a second phase transition around 1200 K to reach a third structural phase ($\gamma$) as clearly reflected in the phonon spectra. The weight of the low-energy phonon modes diminishes when compared to the $\alpha$ and $\beta$ phases in favor of two new strong features at 20 and 35 meV. These phase transitions unravel changes across various ferroic order parameters that are separated over a temperature range.

As ferroelectricity and magnetism in BFO are driven by the Bi and Fe sites, respectively, the partial PDOS reveal clearly the frequency ranges where they contribute. Interestingly, the ferroelectric-to-paraelectric phase transition involves large changes in the dynamics of the Bismuth cations in terms of vanishment of the related off-centered displacements. The abrupt change observed in both phase transitions ($\alpha \rightarrow \beta$ and $\beta \rightarrow \gamma$) confirm that they are of a first order nature. These results provide a reliable support to other works using different techniques\textsuperscript{11,24,25}. As already mentioned, the oxygen contribution to the observed phonon spectra changes considerably upon heating. It is fully smeared out and concomitantly lost intensity in the $\gamma$-phase. This is indicative of a weakening of Fe-O bonding leading finally to bond breaking with the consequence of oxygen release and vacancy creation. This result is quite interesting since it provides a strong argument for the occurrence of the high-spin to low-spin transition mentioned above, and which is a consequence of the reduction of Fe$^{3+}$ to Fe$^{2+}$ to maintain the charge balance due to the presence of oxygen vacancies\textsuperscript{3,24,25}. Similar dynamic effects have been seen in superionic oxygen conductors with an open oxygen network structure\textsuperscript{30}. The newly visible vibrational features in the $\gamma$ phase at 20 and 35 meV could be due to an increase in cell volume after Fe reduction (Fe$^{3+}$ → Fe$^{2+}$) which results in a red shift of closely similar modes observed in the $\alpha$ phase at 25 and 40 meV, respectively.

In summary we have carried out inelastic neutron scattering measurements of the phonon spectra of BiFeO$_3$ which is a unique model system and multiferroic material with multiple order parameters. We have found a strong temperature evolution that indicates both strong anharmonicity and subtle dependence of phonons on structural details. The phonon modes are most affected by the transition at the Curie temperature $T_C$. Three phases $\alpha$, $\beta$ and $\gamma$, in agreement with and in support of other works\textsuperscript{24,25}, are highlighted by their clearly different vi-
spin transitions, previously inferred via diffraction of a high-temperature metal-insulator and Fe$^{3+}$ → Fe$^{2+}$ spin transitions, previously inferred via diffraction experiments, looks very plausible and the present results are consistent with these findings. The high temperature neutron diffractions and optical data have been associated with spin changes and also decomposition and neutron diffractions and optical data have been associated with spin changes and also decomposition and our results reveal large changes in the phonon density of states, consistent with these findings. We estimate that these results are of considerable relevance for the field of multiferroism in general and for multiferroism in this specific material, in particular. They provide valuable arguments to better interpret and support results obtained with other techniques.

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FIG. 1. (Color online) Temperature-dependent evolution of the experimental Bose-factor corrected dynamical structure factor $S(Q, E)$ of BFO. For clarity, a logarithmic representation is used for the intensities; dark red and dark blue refers to strong and weak amplitudes, respectively.
FIG. 2. (Color online) Temperature dependence of diffraction patterns (a) and phonon generalized density of states (G DOS) spectra (b) of BFO extracted from time-of-flight measurements on IN6. Simulated total GDOS and the related partial atomic contributions from *ab-initio* calculations are shown in (c) and (d), respectively. On the same plot (c) the calculated GDOS is compared with a measured spectrum. For the sake of clarity diffractograms and all spectra in (a), and (b), (c) and (d), respectively, are vertically shifted with respect to each other. For a better visibility, stability regions and characteristic temperatures $T_N$ and $T_C$ are highlighted with different colors on (a) and (b).