The Flavour of Inflation

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Abstract. A new class of particle physics models of inflation based on the phase transition associated with the spontaneous breaking of family symmetry is proposed. The Higgs fields responsible for the breaking of family symmetry, the flavons, are natural inflaton candidates or waterfall fields in hybrid inflation. This opens up a rich vein of possible inflation models, all linked to the physics of flavour, with several interesting cosmological implications.

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The inflationary paradigm was proposed more than 20 years ago [1]. Yet, it has been only recently that its predictions have been firmly demonstrated to be consistent with observations [2]. In spite of this success, to date, the precise origin of the inflation field(s) and its relation with observations [2] is a matter of ongoing research, despite much effort done in this direction [3].

On the other hand, one of the greatest mysteries facing the Standard Model (SM) of particle physics is the origin of flavour structure of quarks and leptons, its masses and mixing angles. A common approach to understand this flavour structure, is to assume that the SM is extended by some horizontal family symmetry $G_F$ [4]. This symmetry may be continuous or discrete, and gauged or global. It must be broken completely, apart from possibly remaining discrete symmetries, at some high energy scale in order to be phenomenologically consistent. Such symmetry breaking requires the introduction of new Higgs fields called flavons, $\phi$, whose vacuum expectation values (vevs) break the family symmetry $\langle \phi \rangle \neq 0$. In addition, most of the family symmetry models rely on supersymmetry (SUSY) where besides the flavon superfields, additional “driving” superfields (usually singlets under $G_F$), associated with the vacuum alignment of the flavons, are present.

In this talk, we suggest that the phase transition associated with the spontaneous breaking of family symmetry is also responsible for cosmological inflation, a possibility we refer to as flavon inflation [5]. In other words, we propose to use flavour physics as a guideline for models of inflation and inflation to provide us with constrains on the flavour physics parameters.

Working in a supergravity framework, there are at least two possible flavon inflation scenarios that can arise: either the flavon fields play the role of the inflaton, or the driving fields play the role of the inflatons, whereas the flavons fields end inflation as waterfall fields in a (SUSY) hybrid inflation model. In what follows we present an example of each of these models.

Consider the situation where the inflatons are represented by the vacuum alignment of the family symmetry-breaking flavon fields $\phi_1, \phi_2, \phi_3$ with $\langle \phi_1 \rangle = \langle \phi_2 \rangle = \langle \phi_3 \rangle = 0$. In this case, combinations of the form $\phi_1 \phi_2 \phi_3$ can arise since for fields $\phi = (\phi_1, \phi_2, \phi_3)$, $\psi = (\psi_1, \psi_2, \psi_3)$ and $\chi = (\chi_1, \chi_2, \chi_3)$ each in the fundamental triplet $3$ representation of $A_4$, $\{\phi_1 \phi_2 \chi_3 + \text{permutations}\}$ forms an invariant.

For concreteness, let us look at the following toy model where the superpotential takes the form (this is similar to [8])

$$W = S \left[ \frac{(\phi_1 \phi_2 \phi_3)}{M_3^{n-2}} - \mu^2 \right]; \quad n \geq 1$$

and the non-minimal Kähler potential

$$K = |S|^2 + |\phi|^2 + \frac{k_2 |S|^2 |\phi|^2}{M^2_F} + \frac{k_1 |\phi|^4}{4M^2_F} + \frac{k_3 |S|^4}{4M^2_F} + \ldots$$

where $M^2_F = (8\pi G_N)^{-1/2} \sim 10^{18}$GeV is the reduced Planck mass. The supergravity F-term scalar potential can be calculated from the standard relation

$$V = e^{K/M^2_F} \left[ K^{ij} D_i W D_j \overline{W} - \frac{1}{2} \frac{|W|^2}{M^2_F} \right].$$

with $D_i W = \partial_i W + M^2_F W \partial_i K$. The global minimum is found from $D_i W = 0$ and $W = 0$, to be located at $\phi_i \sim M$, where $M = M_s (\mu/M_s)^{2/3n}$ is the symmetry breaking scale, and $S = 0$. For cosmological purposes, we

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1 A third scenario, which we do not consider here, is where both the flavon fields and the driving fields can play the role of inflatons in a multistage, multifield type of model [6].

2 Since $A_4$ is a discrete symmetry, there are no D-term contributions to the potential.
work in the limit $S \ll M_{Pl}$ and $\phi \ll M \ll M_{Pl}$. We look at the inflationary trajectory where $S$ picks a large mass and sits at its minimum at zero (this implies $\kappa_3 < -1/3$), whereas the flavon fields roll slowly from zero, where the family symmetry is restored, towards their true minimum. Defining the canonically normalised fields as $|\phi_i| \equiv \phi_i/\sqrt{2}$ and concentrating in the generic trajectory $\phi_1 \sim \phi_2 \sim \phi_3 \sim \phi$, the scalar potential during inflation becomes

$$V \approx \mu^4 \left[ 1 - \beta \frac{\phi^2}{2 M^2_{Pl}} - \gamma \frac{\phi^3}{M^3} + \cdots \right], \quad (4)$$

where $\beta = (\kappa_2 - 1)$ and $\gamma = 2/(\sqrt{6})^{3n/2}$. Using the standard slow roll inflationary parameters, ($\epsilon, \eta$), the spectral index $n_s$ is given by $n_s = 1 - 2\beta \left[ 1 + \frac{(3n-1)(1-\beta)}{(3n-2)\beta + 1}e^{\beta(3n-2)N} + \beta - 1 \right]$, for $\beta \neq 0$ and

$$n_s \approx 1 - \frac{6n-2}{(3n-2)\beta + (3n-1)},$$

for $\beta = 0$. The results are illustrated in figure [1]. The predictions for $n_s$ are close to the WMAPS year data, $n_s = 0.960 \pm 0.014$, for $n \geq 2$ and $\beta \lesssim 0.03$ (taking $N = 60$).

We can relate the scale $M_s$ to the family symmetry breaking scale $M$ and the inflation scale $\mu$, via the amplitude of the density perturbation when it re-enters the horizon

$$\delta_H = \frac{2}{5} \sqrt{\frac{1}{2}} = \frac{1}{5\sqrt{3} M_{Pl}} V^{3/2} = 1.91 \times 10^{-5}.$$

With $M_s$ around the GUT scale ($M_{GUT} = 2 \times 10^{16}$GeV), we obtain $M \approx (10^{13}, 10^{14})$ GeV for $n = 2, 3, 4$, for all considered values of $\beta$. The numerical results are shown in figure [2]. Note that the choice $M_s = M_{GUT}$ is only an example. In principle $M_s$ can be much lower and thus also $M$ would be much lower (for example an intermediate scale $M_s \approx (10^{11}, 10^{13})$ GeV can give $M \approx (10^{11}, 10^{13})$ GeV, $\mu \approx (10^{10}, 10^{12})$ GeV).

The second scenario we consider has the driving fields (singlets under the family symmetry) acting as inflatons, whereas the flavon fields are the waterfall fields in a susy hybrid inflation. For this example we consider an explicit $SU(3)$ family symmetry model, already studied in the literature [3], where the symmetry breaking occurs in steps. For concreteness, we assume that it is in the last step that inflation takes place [4].

\footnote{A more general situation can arise if at each stage of family symmetry breaking, a stage of inflation also takes place, giving rise to a multistage flavon inflationary scenario [4].}
The relevant part of the superpotential which governs the final step of family symmetry breaking is given by
\[
W = \kappa S (\phi_{123} \phi_{123} - M^2) + \kappa' Y_{123} \phi_{23} \phi_{123} + \kappa'' Z_{123} \phi_{123} \phi_{123} + \ldots
\]
where the flavon fields \( \langle \phi_{23} \rangle \propto (0, 1, 1)^T \) and \( \langle \Sigma \rangle = \text{diag}(a, a, -2a) \) have already acquired a vev and are already sitting at their minima. \( S \) is the driving superfield for the flavon \( \phi_{123} \), i.e. the contribution to the scalar potential from \( |F_S|^2 \) governs the vev \( \langle \phi_{123} \rangle \). In addition, we take the non-minimal Kähler potential:
\[
K = |S|^2 + |\phi_{123}|^2 + |\phi_{123}|^2 + |Y_{123}|^2 + |\phi_{23}|^2 + |\phi_{23}|^2
+ |Z_{123}|^2 + \frac{\kappa_S |S|^4}{4M^2_{Pl}} + \frac{\kappa_{SZ} |S|^2 |Z_{123}|^2}{4M^2_{Pl}} + \ldots
\]
The inflationary trajectory occurs when the fields with larger vevs \( Y_{123}, \phi_{123}, \phi_{123} \) do not evolve, whereas those with smaller vevs, \( Z_{123} \) and \( S \) move towards their minimum at zero. Focusing on the D-flat directions and setting \( Y_{123} = \phi_{123} = \phi_{23} = 0 \) since they obtain large masses from the superpotential, the tree level scalar potential during inflation takes the form:
\[
V = \kappa^2 M^4 \left[ 1 - \gamma \frac{S^2}{M^2_{Pl}} - 2 \kappa_{SZ} \frac{S^2}{M^2_{Pl}} + \ldots \right],
\]
where \( S = \sigma / \sqrt{2}, |Z_{123}| = \xi / \sqrt{2} \) and \( \gamma = \kappa_{SZ} - 1 \). If the two coefficients in front of the mass terms for \( \sigma \) and/or \( \xi \) are sufficiently small these can drive inflation. In the single field case \( [11] \), where \( \sigma \) acts as the inflaton (choosing for instance \( \gamma < -1/3 \) such that the mass of \( \xi \) exceeds the Hubble scale) and taking into account loop corrections to the potential \([10]\), one finds that for \( \kappa_S \approx (0.005 - 0.01) \) and \( \kappa \approx (0.001 - 0.05) \), a spectral index consistent with WMAP5 year data \([2]\), \( n_s = 0.96 \pm 0.014 \), is obtained \([11]\). Finally, the scale \( M \) of family symmetry breaking along the \( (\phi_{123}) \)-direction is determined from the temperature fluctuations \( \delta T / T \) of the CMB to be \( M \approx 10^{13} \) GeV, about an order of magnitude below the GUT scale.

In summary, we proposed that there exists a non-trivial connection between the physics of flavour and that of inflation. The flavon fields responsible to break family symmetries, can act as inflatons or as waterfall fields in a hybrid inflation scenario, with the driving fields of flavour symmetries acting as inflatons. Because family symmetries have to be completely broken, flavon inflation avoids formation of unwanted relics like those associated to the breaking of GUT symmetries. Moreover, the symmetry breaking scale can be linked to that of inflation, thus making inflation a source of phenomenological information for the flavour sector of particle physics. We have shown briefly how this connection can arise, but it is clear that further relations between the parameters of inflation and those of the family symmetry structure can exist. For example, a detailed study of reheating, baryogenesis and (non-thermal) leptogenesis can be expected to reveal a more precise connection between these two sectors.

As a last remark, we point out that in the present proposal we did not intended to provide a solution to the well known \( \eta \) problem in theories of supergravity inflation. We have taken a more phenomenological approach, being more interested in the physics connecting family symmetries and inflation. It is possible to imagine, however, flavon inflation scenarios which avoid this problem, for example D-term flavon inflation and others.

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