Ultra-stripped supernovae and double neutron star systems

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The evolution of close-orbit progenitor binaries of double neutron star (DNS) systems leads to supernova (SN) explosions of ultra-stripped stars. The amount of SN ejecta mass is very limited from such, more or less, naked metal cores with envelope masses of only $0.01 - 0.2 M_\odot$. The combination of little SN ejecta mass and the associated possibility of small NS kicks is quite important for the characteristics of the resulting DNS systems left behind. Here, we discuss theoretical predictions for DNS systems, based on Case BB Roche-lobe overflow prior to ultra-stripped SNe, and briefly compare with observations.

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1. Case BB RLO from Evolved Helium Stars in Close Binaries

Prior to the formation of the second neutron star (NS) in a double neutron star (DNS) system, the progenitor of the exploding star — a helium star (naked core) emerging from a common envelope (CE) evolution — is expanding during helium shell burning. For close binaries, this will cause a last and significant phase of mass transfer, so-called Case BB Roche-lobe overflow (RLO), which is important for two reasons: i) it strips the outer layers of the helium star very efficiently, leaving an almost naked metal core prior to the supernova (SN) explosion, and ii) it causes the first-born NS in the binary to accrete material and become a recycled radio pulsar. A similar episode of Case BB RLO from post-CE binaries can also produce a recycled NS in a binary with a massive white dwarf (WD) companion.

Some of the remaining questions to investigate in relation to this recycling process are: the decay of the B-field of the accreting NS, its accretion efficiency, and how the excess material (transferred towards the NS at a highly super-Eddington rate from the donor star) is ejected from the vicinity of the NS.

2. NS Accretion prior to and after Case BB RLO

When discussing the recycling of the first-born NS in a DNS system, we must first identify the possible phases of accretion onto this star. The following five phases are relevant: I) wind accretion in the high-mass X-ray binary (HMXB) phase, II) accretion during the CE phase, III) wind accretion from the naked helium (Wolf-Rayet) star, IV) Case BB RLO from the evolved helium star, and V) accretion of SN ejecta from the explosion of a very nearby naked core forming the second NS.

The amount of wind accretion in phases I and III is constrained by the lifetime of the massive hydrogen-rich star ($\sim 10$ Myr) and the subsequent naked helium star evolution ($< 1 \sim 2$ Myr), respectively, their wind mass-loss rates and the efficiency of NS accretion. For fast (supersonic) winds, the Bondi-Hoyle-like accretion
is rather inefficient. The accretion is more efficient for (sub)giant donors with slower winds. In some HMXB sources, so-called beginning atmospheric RLO might be at work. However, this later stage of evolution is relatively short lived. Furthermore, the accretion efficiency may be low as a consequence of propeller effects. These circumstances are also evident from X-ray luminosity functions of Galactic HMXBs, which indicate that less than about 10% of all HMXBs have a luminosity $> 10^{37}$ erg s$^{-1}$, corresponding to an accretion rate of $\sim 10^{-9} M_\odot$ yr$^{-1}$. All taken together, we estimate that the total amount of material accreted by the NS in these two phases is less than 0.01 $M_\odot$.

The accretion onto a NS embedded in a CE (phase II) has to be quite limited as evidenced from measurements of radio pulsar masses in post-CE binaries. A possible reason for this has recently been demonstrated to be caused by the density gradient across the gravitational capture radius imposing a net angular momentum to the flow, thereby significantly decreasing the accretion efficiency compared to Bondi-Hoyle accretion. It is likely that the amount of accreted matter during a CE phase could be as low as 0.01 $M_\odot$. Given that a stable accretion disk may not form around the NS within a CE, it is uncertain whether this small amount of matter will contribute to any recycling (spin-up) of the accreting NS at all.

Accretion of ejecta matter from the SN of a companion star (phase V) is expected to be highly insignificant in general, except for a few rare and very finetuned cases, and we will disregard this possibility in further discussions.

3. NS Recycling via Case BB RLO

Case BB RLO has recently been demonstrated to result in accretion onto the NS of $5 \times 10^{-5} - 3 \times 10^{-3} M_\odot$ for Eddington-limited accretion, and up to $10^{-2} M_\odot$ if allowing for accretion above the Eddington limit by a factor of three. The gain in spin angular momentum of the accreting NS can be expressed as:

$$\Delta J = \int n(\omega, t) \dot{M}(t) \sqrt{GM(t) r_{mag}(t) \xi(t)} dt,$$

where $n$ is the dimensionless accretion torque, $\omega$ is the fastness parameter, $t$ is time, $\dot{M}$ is the NS mass accretion rate, $G$ is the constant of gravity, $M(t)$ is the mass of the NS, $r_{mag}$ is the radius of the magnetosphere, and $\xi$ is a parameter depending on the geometric flow of the material ($\approx 1$ for accretion from a disk). This integral can roughly be approximated as a simple correlation between the equilibrium spin period in ms, $P_{\text{ms}}$ and the (minimum) amount of mass accreted, $\Delta M_{\text{eq}}$:

$$P_{\text{ms}} = \frac{(M/M_\odot)^{1/4}}{(\Delta M_{\text{eq}}/0.22 M_\odot)^{3/4}}$$

Hence, we find that the abovementioned range of mass accreted via Case BB RLO corresponds to spinning up the NS to a resulting spin period of 11 – 350 ms. For a comparison, the observed range of spin periods of recycled NSs in DNS systems is currently spanning between 23 – 185 ms.
3. Correlation between DNS Orbital Period and Spin Rate

Given the relation between amount of accreted material and equilibrium spin rate of the recycled pulsar, we can predict a correlation between the orbital period and the spin period of recycled pulsars in DNS systems, since the amount of accreted mass is strongly dependent on the orbital period of the binary at the onset of Case BB RLO. This is illustrated in Fig. 1. Detailed calculations of Case BB RLO showing how the duration of the mass-transfer phase decreases with increasing initial orbital period is shown in Fig. 2. The wider the initial orbit of the NS–helium star system, the more evolved is the helium star when it fills its Roche lobe and the shorter is its remaining lifetime before it collapses and produces a SN explosion. Therefore, in wide binaries little mass is transferred to the NS prior to core collapse, and thus the recycling process is relatively ineffective. The spin period of such a marginally recycled pulsar will remain large. PSR J1930−1852 is an example of such a system. It has an orbital period of 45 days and a slow spin period of 185 ms.
Fig. 2. Mass-transfer rate as a function of time for 3.0 $M_\odot$ helium star donors with different values of initial orbital period at the onset of Case BB RLO. The time $t = 0$ is defined at the beginning of RLO for all systems. The duration of the RLO (and thus the amount of material transferred onto the NS) is seen to decrease with increasing orbital period. Thus recycling is inefficient in wider orbits, leading to slower spin periods of recycled pulsars in wide-orbit DNS systems. This figure was adopted from Ref. [5].

In Fig. 3 we have plotted the duration of the Case BB RLO prior to the SN explosion, as well as the remaining amount of helium envelope mass at the moment of the SN, as a function of initial orbital period at the onset of Case BB RLO. Since wide-orbit pre-SN systems are also expected to produce wide-orbit DNS systems after the SN explosion (especially if NS kicks are small, see discussion below) we expect that these systems, which are clearly seen to experience short-duration RLO and thus limited recycling, will produce relatively slow spinning recycled pulsars. Similarly, we expect the fastest spinning recycled pulsars in DNS systems to be found in close-orbit systems, such as PSR J0737$-$3039 which has a spin period of 23 ms and an orbital period of 2.4 hr.

5. Ultra-stripped SNe, NS kicks and DNS eccentricities

Ultra-stripped SNe can be either electron-capture SNe (EC SNe) or iron core-collapse SNe (Fe SNe). It has been shown that EC SNe are expected to have small explosion energies$^{21,22}$ and that they revive the stalled SN shock on a short timescale compared to the timescales of non-radial hydrodynamic instabilities pro-
Fig. 3. Duration of Case BB RLO (decreasing blue curve), and remaining helium envelope mass (increasing red curve), prior to the iron core-collapse SN as a function of initial orbital period. Wide-orbit (post-SN) DNS systems are thus expected to host pulsars which are only marginally recycled (as a result of their short-duration RLO) and which, in average, have higher eccentricities (as a result of their larger envelope mass ejected in the SN) than pulsars in close-orbit systems. This figure was adopted from Ref. [5].

Producing strong anisotropies\cite{23,24}. Their resulting kick velocities are most likely \(\lesssim 50 \text{ km s}^{-1}\), i.e. significantly smaller than the average kick velocities of the order \(400 \sim 500 \text{ km s}^{-1}\) imparted on young pulsars\cite{25}. It has also been argued\cite{9} that ultra-stripped Fe CCSNe might (in general, but not always) produce small NS kicks. The reasons for this are: i) their small amount of ejecta mass, compared to standard SNe, which leads to a weaker gravitational tug on the proto-NS\cite{24}, and ii) the small binding energies of their envelopes allowing for fast ejection, potentially before large hydrodynamical anisotropies can build up. Recent modelling of ultra-stripped SN explosions of evolved CO-stars\cite{26} confirms that their kick velocities are expected to be small in general. Nevertheless, in a few cases (PSR B1534+12 and PSR B1913+16) kicks of the order \(300 \text{ km s}^{-1}\) seem necessary to explain the orbital parameters of the DNS systems. Hence, we conclude that whereas ultra-stripped SNe might produce small kicks in general, larger kicks are possible in more rare cases – possibly caused by explosions of relatively more massive iron cores.

Finally, it is expected that ultra-stripped SNe (at least those which produce small kicks) result in relatively small DNS eccentricities in general. The reason for this is their small ejecta masses. It should be noted, however, that even small kicks (\(50 \text{ km s}^{-1}\)) can in some cases result in large eccentricities, depending on the
direction of the kick. In average, we do expect a trend of increasing eccentricities with increasing orbital period of DNS systems, given that the exploding star in wider pre-SN systems will possess (and thus eject) a larger envelope mass, cf. Fig. [11].

Detailed modelling of the recycling and spin-up of the accreting NS during Case BB RLO has to be investigated further. Initial studies indicate that the computed spin periods of the recycled NSs in DNS systems are indeed in good agreement with the observed values of 23 – 185 ms. Many (but not all) of the DNS systems also have small eccentricities and small systemic velocities (reflecting small kicks). Future modelling of the explosions are needed to investigate this further.

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