Analysis of Fat and Protein Content in Milk Using Laser Polarimetric Scatterometry

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Abstract: Monitoring the composition of milk products is an important factor in the management of dairy farms and industry. Information on the quantitative content of milk components is necessary to control milk quality, as well as to optimize dairy cow nutrition and diagnose their clinical condition. The content of fat and protein is considered the main criterion for determining the market value of milk. Increasing the efficiency of dairy production requires the use of inexpensive and compact devices that are capable of performing multicomponent analysis of milk both directly on the farm and in technological lines. We investigated the possibility of fast simultaneous determination of fat and protein content in milk by laser polarimetric scatterometry. The block-diagonal elements of the scattering matrix were measured for a series of commercially produced milk samples with the indicated fat percentage, which were diluted by volume with water. From the measured scattering matrices, the size distributions of fat droplets and casein aggregates were reconstructed. Using the size histograms, the content of fat and protein and protein-to-fat ratio in the studied milk samples are estimated.

Keywords: milk quality control; milk fat and protein; light scattering matrix; protein-to-fat ratio

1. Introduction
The quality of milk is directly related to its composition [1,2]. At present, there are no ready-made systems that provide simultaneous measurement of all milk components. Farms usually send milk samples to specialized laboratories for a comprehensive analysis of milk quality. The express analysis of milk and the determination of all its quality parameters are also important for the milk processing industry, since the supply of milk that is already separated by fat content and other parameters would reduce the time and financial costs of milk sorting. Rapid control of milk quality is important for prompt reaction to deviations of the physiological state of animals and for timely correction of food rations in the case of milk yield decrease.

Methods of non-destructive diagnostics of micro- and nanostructures of liquid dispersed systems are increasingly used for technological control in many industries. One of the main requirements for the automation of processes in the food industry is the need for a permanent assessment of the composition and physical properties of liquids and their mixtures at the most important stages of processing. However, the determination of the physical characteristics of food products using traditional monitoring methods is difficult if the analyzed product is in a polydisperse state, i.e., contains particles of vari-
ous sizes and shapes. On the basis of optical methods, it is possible to develop reliable and universal sensors for non-invasive monitoring of the composition of products in real time.

Currently, the accurate measurements of the concentration of milk components are performed, for example, using systems based on transmission/reflection of infrared radiation, which stand out due to high cost. Therefore, a less expensive system for measuring both fat and protein content, compact and easy to calibrate, combined with an increased level of accuracy, would have advantages in terms of reducing milk processing costs and improving quality control.

Techniques based on measuring the characteristics of light scattering (scatterometry) are a promising direction in the development of such systems. For example, the work in [3] reports on the development of inexpensive fiber sensors that measure backscattering (diffuse reflection) of multiple scattering liquids. Crofcheck et al. argue that similar sensors can be used to determine the content of milk fat in skim milk [4]. However, these studies did not take into account the change in the state of polarization upon scattering in a medium.

A method that measures changes in the polarization of scattered light in addition to the intensity of scattered light can provide additional information about the scattering particles and improve the accuracy of determining their microphysical parameters (for example, particle size). In particular, the angular dependences of the elements of the light scattering matrix (LSM) describing such a change in the state of light scattered by the dispersed medium make it possible to determine the number and size distribution of particles, as well as to distinguish solid particles from clusters consisting of smaller particles.

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Regarding the application of LPS to the analysis of milk composition, the light scattering theory implies that it has the potential to simultaneously determine the parameters of two dispersed components in milk, specifically fat and protein, since the structural model of their particles is initially known. We assume that different types of scattering particles of milk (fat and protein) make independent contributions to the measured elements of LSM. This assumption is acceptable under single-scattering conditions, which are achieved by appropriate dilution of milk samples. In our work, we experimentally tested the analytical capabilities of the method, and also offered an algorithm for solving the inverse scattering problem to reconstruct the size histograms and then determine the percentage of both fat and protein.
2. Materials and Methods

2.1. Milk Sample Preparation

For testing the ability of laser polarimetric scatterometry (LPS) to analyze milk composition, we experimented with a series of cow milk samples with a nominal fat percentage of 0.05%, 1.5%, 2.5% and 3.5–4.5% commercially produced using ultra-high-temperature (UHT) pasteurization and homogenization. Protein content was reported as 3.1 g per 100 g of product for all of these milk samples. In preparation for measurements, we subjected milk samples to 1000-fold dilution by volume with purified water obtained using a Milli-Q Integral 5 (Merck Millipore, Molsheim, France) with a pH of 5.5 under normal conditions. The degree of dilution was chosen by the need for the single scattering of light from dispersed particles in milk, which, in its original form without dilution, is a multiple scattering medium. Diluted samples from this set of milk fat were studied by LPS using the setup described in detail in [17]. The LPS setup with the laser wavelength 532 nm (second harmonic of diode-laser pumped Nd: YAG laser) is capable of measuring the full scattering matrix (also called Mueller matrix) as a function of the scattering angle for a 40 mL liquid sample placed in a cylindrical glass cuvette with a diameter of 40 mm.

2.2. LPS Method

The gist of the LPS method is in the sensitivity of the light scattering matrix (LSM) to dispersed milk components. For a macroscopically isotropic medium that contains identical numbers of randomly oriented scatterers and their mirror-symmetric counterparts, LSM \[ ||F|| \] (4 × 4) has a block-diagonal form [18,19]

\[
||F|| = \begin{bmatrix}
F_{11} & F_{12} & 0 & 0 \\
F_{21} & F_{22} & 0 & 0 \\
0 & 0 & F_{33} & F_{34} \\
0 & 0 & F_{43} & F_{44}
\end{bmatrix},
\]

(1)

where \( F_{12} = F_{21}, \ F_{34} = -F_{43} \). For spherical particles, \( F_{11} = F_{22}, \ F_{12} = F_{21}, \ F_{34} = -F_{43}, \ F_{43} = -F_{44} \), thus only four elements are independent. The dependence of element \( F_{11}(\theta) \) on the scattering angle \( \theta \) describes the scattering indicatrix of nonpolarized radiation.

As is known, fat globules in milk range from 0.1 to 15 μm in diameter [20,21]. Primary casein micelles are spherical with a size of about 10 nm. They tend to aggregate into secondary micelles, forming casein clusters that have a close packing with a size of about 100 nm [22,23]. As follows from the scattering theory [19], the clusters of densely packed spheres also have block-diagonal LSM.

To analyze the disperse composition, the measured LSM is represented as a weighted sum of the theoretical scattering matrices calculated for model particles with different sizes. The values of the corresponding weights that ensured a minimum of mean square deviations of the theoretical and experimental data determined the sought particle size distribution. In measurements of LSM, a dilution of milk samples is necessary to provide a single scattering mode, so that the representation of the measured LSM as a linear combination of LSM calculated for individual particles would be valid.

2.3. Retrieving the Size Distribution

To reconstruct the particle size distribution, the elements of experimental scattering matrix \( F_{ij} \) were represented as the sums of contributions from particles of various types [15]:

\[
F_{ij}(\theta_k) = \frac{\sum_p \alpha_p \cdot C_{pca} \cdot F_{ij}^{(p)}(\theta_k)}{\sum_p \alpha_p \cdot C_{pca}^{ij}},
\]

(2)

where \( \theta_k \) is a value of the scattering angle from a measured set \( \{\theta_k\} \), \( \alpha_p \) is the coefficient of the contribution into the scattering matrix from the particles of p-type, \( C_{pca} \) is the scattering cross section of p-type particles, and \( F_{ij}^{(p)}(\theta_k) \) are the matrix elements of
the p-type particles. The LSMs for particles of each type were calculated within the framework of the model of spherical scatterers.

The contribution coefficients \( a_i \) for particles of various types were determined, providing a minimum for the sum of squares of the deviations of the theoretical matrix elements (2) from the experimental ones \( \Phi([a_i]) \):

\[
\Phi([a_i]) = \sum_k \left[ (\Delta f_{11}(\theta_k))^2 + (\Delta f_{12}(\theta_k))^2 + (\Delta f_{13}(\theta_k))^2 \right],
\]

(3)

where for all elements except \( F_{11} \), the deviations are defined as:

\[
\Delta f_{ij}(\theta_k) = \left( f_{ij}^{(\text{theor})}(\theta_k) - f_{ij}^{(\text{exp})}(\theta_k) \right)/h_{ij},
\]

(4)

where \( h_{ij} \) is the measurement error of the matrix element. For \( F_{11} \), the deviation is defined as:

\[
\Delta f_{11}(\theta_k) = \left( |f_{11}^{(\text{theor})}(\theta_k) - f_{11}^{(\text{exp})}(\theta_k)| - 1 \right)/h_{11}.
\]

(5)

The Levenberg–Marquardt algorithm [24] was used to determine the values of the contribution coefficients \( a_i \) that ensure the minimum of the function. The array of \( a_i \) values gives us a size histogram through which the fat and protein contents of the milk sample can be calculated.

The restoration of the size histogram was carried out by choosing 28 size channels; each channel is associated with a specific type of particles considered in the expansion (2): 1–20 channels are spheres (fat globules with relative refractive index \( n_r = 1.10 \)) and \( R \) varies in the channel from 0.05 \( \mu \)m (1st channel is limited to 0.05–0.0646 \( \mu \)m) to 8.34 \( \mu \)m (20th channel is limited to 6.46–8.34 \( \mu \)m). Channels 21–28 are aggregates (casein micelles with relative refractive index \( n_r = 1.18 \)); the sizes of aggregates vary from \( R_V = 34 \) nm (gyration radius \( R_g = 35 \) nm) in the 28th channel to \( R_V = 204.8 \) nm (gyration radius \( R_g = 238 \) nm) in the 21st channel. The size of an aggregate of spherical monomers \( R_V \) is defined as the radius of a sphere of equivalent volume:

\[
R_V = a \sqrt[3]{N},
\]

(6)

where \( N \) is the number of monomers in the aggregate and \( a \) is the radius of the sphere, whose volume is equal to the volume of monomer.

It was assumed that the size of the casein monomers is \( a = 10 \) nm, and the fractal dimension is \( D_f = 2.8 \). The reconstruction was carried out from the sum of the squares of the deviations of the experimental and theoretical values of the three elements \( F_{11}, f_{12}, f_{13} \) in the range of scattering angles 25–160\(^\circ\). The scattering matrices of model particles (for spheres) were calculated using the program that is based on the T-matrix method developed by Mishchenko [18] for an ensemble of randomly oriented spheroids.

In the calculations, the values of the elements \( f_{12}, f_{13} \) of the casein aggregates were assumed to be equal to the corresponding values of the elements of the Rayleigh matrix due to their small difference for the aggregates with monomer sizes much smaller than the wavelength [16]. The values of the element \( F_{11} \) and the scattering cross sections of casein aggregates were calculated in the Rayleigh–Gans–Debye approximation, which is valid under the conditions:

\[
2X_m|m - 1| \ll 1, \quad |m - 1| \ll 1, \quad X_m = \frac{2\pi a}{\lambda}
\]

(7)

where \( X_m \) is the size parameter of the monomer.
2.4. Determination of the Fat and Protein Content

The particle size distributions can be used to calculate the content of fat and protein in the milk. Define the fat of milk as:

\[ F_c = \frac{M_F}{M_{\text{milk}}}, \quad M_F = \bar{m}_F \cdot \bar{N}_F = \bar{m}_F \cdot p_F \cdot V_{\text{sca}}. \]  

\( \bar{m}_F \) is the average mass of one fat particle, \( \bar{N}_F \) is the number of fat particles in the scattering volume, \( p_F \) is the volume number density of fat particles in the scattering volume \( V_{\text{sca}} \).

\[ \bar{m}_F = \rho_F \sum_i \frac{4\pi}{3} r_i^3 \beta_i^F. \]  

\( \rho_F \) is the fat density (assume that \( \rho_F = 0.9225 \text{ g/cm}^3 \) [25].

The fraction of the fat particles with a radius \( r \) is:

\[ \beta_i^F = \frac{\alpha_i^F}{\sum_i \alpha_i^F}. \]  

\( \alpha_i^F \) is the contribution coefficient of the fat particles with radius \( r \) to the total amount of scattering.

Similarly, the average mass of one protein particle is:

\[ \bar{m}_{pr} = \rho_{pr} \sum_i \frac{4\pi}{3} r_i^3 \beta_i^{(pr)}. \]  

\( \rho_{pr} \) is the protein density (assume that \( \rho_{pr} = 1.3398 \text{ g/cm}^3 \) [25].

The fraction of the protein particles with radius \( r \) is:

\[ \beta_i^{(pr)} = \frac{\alpha_i^{(pr)}}{\sum_i \alpha_i^{(pr)}}. \]  

\( \alpha_i^{(pr)} \) is the contribution coefficient of the protein particles with radius \( r \) to the total amount of scattering. The mass of the total protein in the scattering volume is:

\[ M_{pr} = \bar{m}_{pr} \cdot \bar{N}_{pr} = \bar{m}_{pr} \cdot p_{pr} \cdot V_{\text{sca}} \]  

\( \bar{m}_{pr} \) is the average mass of one protein particle, \( \bar{N}_{pr} \) is the number of protein particles in the scattering volume, and \( p_{pr} \) is the volume number density of protein particles in the scattering volume. The volume number density of both fat and protein particles can be expressed through the scattering coefficient [6]:

\[ p = p_F + p_{pr} = p_{pr} \left( 1 + \frac{p_F}{p_{pr}} \right) = \frac{4\pi}{C_{\text{sca}}} \cdot I(\theta) \cdot \frac{R_{\text{tot}}(\theta)}{I_{\text{tot}}(\theta)} \cdot \frac{n_{\text{solv}}^2}{n_{\text{tot}}^2}. \]  

\( I(\theta) \) is the experimental value of scattering intensity; \( C_{\text{sca}} \) is the mean scattering cross section for one particle; \( F_{11}(\theta) \) is the mean value of the element \( F_{11} \); \( R_{\text{tot}}(\theta) \) and \( I_{\text{tot}}(\theta) \) are the scattering coefficient and scattering intensity of toluene, which is commonly used as a calibration fluid [26]; \( n_{\text{tot}} \) and \( n_{\text{solv}} \) are the refractive indices of toluene and solvent (in the case of milk, water).

Next, using the entire set of the contribution coefficients \( \alpha_i \) from particles of all sorts (fat and protein):

\[ \{\alpha_i\} = \left\{ \left\{ \alpha_i^F \right\}, \left\{ \alpha_i^{(pr)} \right\} \right\}. \]  

We can calculate:

\[ C_{\text{sca}} = \sum_i \alpha_i \cdot C_i^{\text{sca}}, \quad F_{11}(\theta) = \frac{\sum_i \alpha_i \cdot C_i^{\text{sca}} \cdot F_{11}(\theta)}{\sum_i \alpha_i \cdot C_i^{\text{sca}}}. \]  

\( C_i^{\text{sca}} \) is the scattering cross section for the particles of the \( i \)-th type. The whole mass of milk is:
\[ M_{\text{milk}} = \rho_w \cdot (V_{\text{scat}} - \bar{N}_p \cdot \bar{v}_p - \bar{N}_{pr} \cdot \bar{v}_{pr}) + \bar{m}_p \cdot \bar{N}_p + \bar{m}_{pr} \cdot \bar{N}_{pr}. \]  

(17)

\[ \rho_w \] is the density of water; \( \bar{v}_p, \bar{v}_{pr} \) are the average volumes of one particle of fat and protein, respectively, which can be calculated as:

\[ \bar{v}_p = \frac{\bar{m}_p}{\rho_p}, \quad \bar{v}_{pr} = \frac{\bar{m}_{pr}}{\rho_{pr}}. \]  

(18)

Thus, to determine the content of fat and protein, it is necessary to obtain a size histogram \( \alpha_i \) for the milk sample.

3. Results

3.1. Scattering Matrix Measurements

In experiments, the block-diagonal elements of LSM \( F_{11}, f_{12}, f_{33}, f_{34} \) were measured as functions of the scattering angle in the range of scattering angles 15–160° for milk samples with a nominal fat percentage of 0.05%, 1.5%, 2.5%, 3.5–4.5%, diluted with water 1000 times by volume. The corresponding graphs of the angular dependences of the matrix elements are shown in Figure 1. By \( f_{ij} \), we mean matrix elements \( F_{ij} \) normalized to \( F_{11} \) (\( f_{ij} = F_{ij} / F_{11} \)). The absolute measurement error of the normalized matrix elements was 0.03.

![Figure 1. LSM elements \( F_{11}, f_{12}, f_{33}, f_{34} \) as functions of the scattering angle, experimentally measured at a light wavelength 532 nm for cow milk samples with nominal fat percentages: 0.05% (shown in green), 1.5% (shown in black), 2.5% (shown in blue), 3.5–4.5% (shown in red), diluted 1000 times by volume with water.](image)

As can be seen in Figure 1, the angular profiles of the matrix elements exhibit a monotonic dependence on the fat content in milk in the following ranges of scattering angles: ~50–120° (\( F_{11} \)); ~40–120° (\( f_{12} \)); ~80–150° (\( f_{33} \)) n ~100–140° (\( f_{34} \)).
3.2. Particle Size Distributions

We reconstructed the particle distributions over sizes based on the scattering matrix data (Figure 1) for cow milk with nominal fat percentages of 0.05, 1.5, 2.5 and 3.5–4.5%. The corresponding size histograms are shown in Figure 2. In each of the graphs, the fractions of fat particles and casein aggregates are shown in different colors. Typical sizes of casein aggregates are 40–200 nm. Fat particles are characterized by the presence of large (2–7 microns) and small (60–200 nm) portions. The fraction of particles of the fine portion is small, amounting to $10^{-6}–10^{-4}$.

Using the formulas given in Section 1, the estimated fat content is equal to 0.002, 0.011, 0.024, and 0.042 and the estimated casein content is equal to 0.026, 0.030, 0.035, and 0.038 for cow milk with nominal fat percentages of 0.05, 1.5, 2.5 and 3.5–4.5%, respectively. The corresponding protein-to-fat ratio values are 13, 2.7, 1.5, and 1.1, respectively.

Figure 2. Size histograms retrieved from the scattering matrix data in the range of scattering angles of 25–160° for diluted samples of cow milk with nominal fat percentages: (a) 0.05%, (b) 1.5%, (c) 2.5% and (d) 3.5–4.5%. The histograms are normalized. The red bars correspond to protein, and the blue bars correspond to fat.

4. Discussion

The results of measurements of the light scattering matrix for samples of industrial cow milk with different fat content, diluted with water, showed that the values of the block-diagonal matrix elements change with a change in the fat content of the milk. Experimentally found differences in the values of matrix elements for milk samples with a nominal fat percentage of 0.05%, 1.5%, 2.5%, 3.5–4.5%, diluted with water 1000 times by
volume, allow us to conclude that the LSM elements $F_{11}$, $f_{12}$, and $f_{33}$ are the most sensitive to fat content. The values of these elements can serve as a direct analytical signal in a fat content sensor analyzing diluted milk samples. In order to simultaneously determine the content of fat and protein, an algorithm for solving the inverse problem was developed.

The measured values of fat and protein percentage turned out to be close to nominal, except for low-fat milk (0.05%). The discrepancies between the manufacturer’s declared and the fat content determined experimentally can be explained by the indirect nature of the method used, namely: first, measuring the dependences on the scattering angle of matrix elements, then solving the inverse problem of retrieving the distribution of dispersed particles under the assumption that the dispersed medium is two-component, and, finally, the actual fat content calculation. In this case, of course, errors may arise due to errors in experimental measurements, the approximation of the used model of a dispersed medium, errors in the algorithm for solving the inverse problem and determining the volume concentration of particles. Improving the accuracy of the final result can be achieved by increasing the number of readings during experimental measurements and refining the model used to interpret them. This includes the possible consideration of the size distribution of monomers, the clarification of the size of the monomers in casein aggregates and the fractal dimension of aggregates, taking into account the non-sphericity of the shape of fat particles and Rayleigh scattering by water molecules.

The complexities of the problem to be solved for determining the fat content should include not only two (many) components of the dispersed medium, but also the bimodality of the distribution of fat particles (Figure 2). Moreover, the number of larger particles (2–7 microns) is 2–4 orders of magnitude less than the number of smaller particles (70–200 nm), but nevertheless their contribution to the total scattering intensity is noticeable. The proposed approach allows us to take this circumstance into account and, in addition, to determine the content of casein in milk, and thus also assess the protein-to-fat ratio. It is worth noting that the size of the fat particles in the measured milk samples is rather small if compared with raw milk, where fat particles can reach a size of 100 microns. This fact is apparently related to milk homogenization.

Alternatively, it is possible to obtain the size distribution of dispersed particles by the method of dynamic light scattering (DLS) [27] or from the measured scattering indicatrix solely. However, even in these cases, the correct determination of the milk fat alone requires an interpretation model of a multicomponent medium and solving the inverse scattering problem. Compared to the registration of only the scattering intensity or the correlation function, the registration of the polarization characteristics (the elements of the scattering matrix) can improve the accuracy of the solution of the inverse problem.

The experimental results obtained indicate that the LPS method is capable of determining the content of fat and casein in milk. In comparison, for example, with the DLS method [27], the proposed method for solving the sample problem allows retrieving the individual contributions to the scattering intensity from fat and protein particles and does not require the extraction of these components from a milk sample. Thus, it is possible to determine at once the content of both of these components.

Although the proposed method for the measurement of the fat and protein content in milk involves sampling with dilution, the analysis of milk parameters itself takes a relatively short time within a minute, which allows this method to be classified as an express analysis. On the basis of the described measuring principle, it is possible to develop a compact and relatively fast sensor of fat and protein percentage, which could be in demand in dairy farms and dairy industries.
5. Conclusions

Our experimental tests showed that the laser polarimetric scatterometry is a promising technique for the development of convenient and inexpensive analyzers of milk composition for regular operation on dairy farms or milk processing lines.

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