Timing, polarimetry and physics of the bright, nearby millisecond pulsar PSR J0437–4715 – a single-pulse perspective

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ABSTRACT

Single pulses from radio pulsars contain a wealth of information about emission and propagation in the magnetosphere and insight into their timing properties. It was recently demonstrated that single-pulse emission is responsible for limiting the timing stability of the brightest of millisecond pulsars. We report on an analysis of more than a million single pulses from PSR J0437–4715 and present various statistical properties such as the signal-to-noise ratio (S/N) distribution, timing and polarimetry of average profiles integrated from sub-pulses with chosen S/N cut-offs, modulation properties of the emission, phase-resolved statistics of the S/N and two-dimensional spherical histograms of the polarization vector orientation. The last of these indicates the presence of orthogonally polarized modes (OPMs). Combined with the dependence of the polarization fraction on the S/N and polarimetry of the brightest pulses, the existence of OPMs constrains pulsar emission mechanisms and models for the plasma physics in the magnetosphere.

Key words: pulsars: general – pulsars: individual (PSR J0437–4715).

1 INTRODUCTION

Radio pulsars are highly magnetized, quickly spinning neutron stars that emit radio waves. A non-thermal emission mechanism, not yet understood despite decades of study, is responsible for emission in two beams aligned with the magnetic field axis of the pulsar. As the spin axis is misaligned with the magnetic field axis, the radio beams can sweep past Earth, producing a light house like effect of emission across the electromagnetic spectrum. Pulsars are extremely versatile laboratories of physics and observing them provides unique insights into physics at many scales. Neutron stars probe fundamental interactions via the ultradense matter and solid-state physics (e.g. Thorsett & Chakrabarty 1999; Antoniadis et al. 2013). Plasma physics in highly magnetized environments is relevant in the pulsar magnetosphere (e.g. Cairns, Johnston & Das 2004). Pulsars allow for tests of non-linear strong-field gravity, probing regions of phase space inaccessible by other means (e.g. Kramer et al. 2004; Ransom et al. 2014). Pulsar Timing Arrays are recently gaining momentum in their quest for the detection of gravitational waves (e.g. Sazhin 1978; Foster & Backer 1990; Shannon et al. 2013). Other types of experiments possible with pulsar observations include the derivation of a distance scale, study of the interstellar tenuous plasma and large-scale magnetic fields (Han et al. 2006; Deller et al. 2008; Noutsos et al. 2008; Beck 2009; Schnitzeler 2012), independent measurements of masses in the Solar system (Champion et al. 2010), development of a pulsar-based time-scale (Hobbs et al. 2012), and many more (e.g. Cordes et al. 2004).

Many of the aforementioned experiments are based on pulsar timing methodology, i.e. estimation of the mean time of arrival (ToA) of the pulse train. The precision attainable in such experiments is dependent on the pulse profile (i.e. the longitude resolved light curve of a pulsar), spin period, brightness of the pulsar and so called timing noise, that is any unexplained deviations of the pulse train arrival times from simple physical models.1 The most precise timing experiments are based on the observations of millisecond pulsars (MSPs), i.e. pulsars that have been spun up by mass accretion and the associated transfer of angular momentum from the companion star (Alpar et al. 1982) or directly through the accretion-induced collapse of a white dwarf (Freire & Tauris 2014).

Another way of studying pulsars is by analysing the single pulses emitted by the pulsar. While the average pulse profile is generally stable over time (Helfand, Manchester & Taylor 1975), every single pulse is different (Drake & Craft 1968b). Their amplitudes can be modulated temporally with or without a drift in phase (Cole 1970; Edwards & Stappers 2003). Some pulsars give off giant pulses

1 There is no widely accepted definition of timing noise and some authors include in this term only processes with certain spectral characteristics.
(e.g. Staelin & Reifenstein 1968; Cornella et al. 1969; Knight et al. 2006; Vigilius & Melatos 2009) and micropulses (Johnston et al. 2001), and some have high nulling fractions, that is the fraction of time when the emission of the pulsar is not detectable (Backer 1970b). The latter effect may be connected with the magnetospheric state and the spin-down rate (Kramer et al. 2006; Lyne et al. 2010).

The emission is not only often highly polarized but can also exhibit two orthogonally polarized modes (OPMs; Manchester, Taylor & Huguenin 1975; Backer, Rankin & Campbell 1976; Cordes, Rankin & Backer 1978; Backer & Rankin 1980; Stinebring et al. 1984). MSPs are typically less luminous and fainter than more slowly rotating pulsars. They also span much more quickly, reducing the signal-to-noise ratio (S/N) of individual pulses and increasing the volume of data by two or three orders of magnitude per unit observing time. For these reasons, single-pulse studies of MSPs are much more difficult. Such studies can shed light on the elusive nature of the pulsar emission mechanism, can help show whether there is a continuity of single-pulse properties from MSPs to slower pulsars, can provide an insight into plasma physics and can also be used to determine the fundamental limits of timing precision.

Empirical and theoretical considerations of single-pulse properties and studies of slow pulsars’ single-pulse emission have been undertaken in the past (e.g. most recently, Karastergiou et al. 2001, 2002; Karastergiou, Johnston & Kramer 2003b; Kramer et al. 2003; Karastergiou et al. 2003a; Melrose & Luo 2004; Melrose et al. 2006; Bhat et al. 2007; Weltevrede, Wright & Johnston 2012). The sample of MSP single-pulse studies is more limited but still numerous (Cognard et al. 1996; Jenet, Anderson & Prince 2001; Edwards & Stappers 2003; Jenet & Gil 2004; Knight et al. 2006; Burke-Spolaor et al. 2012; Zhuarvlely et al. 2013).

A perfect candidate among MSPs for single-pulse studies is PSR J0437−4715, discovered in the 70 cm Parkes Survey (Johnston et al. 1993), the brightest MSP known; a number of such studies have been undertaken previously (Johnston et al. 1993; Ables et al. 1997; Jenet et al. 1998; Vivekanand, Ables & McConnell 1998; Vivekanand 2000). Owing to the progress of technology and methodology, we present a study of a larger data set, recorded over a wider band, with fully calibrated polarization data.

In this paper, we focus on the relation between the single-pulse properties and the timing of PSR J0437−4715 as well as on the polarimetric properties of the single pulses. In Section 2, we describe our observations including the hardware used and details of data processing; Section 3 focuses on an analysis of the total intensity properties of PSR J0437−4715; the polarimetric properties are presented in Section 4; and we summarize our findings in Section 5.

2 OBSERVATIONS AND DATA PROCESSING

Observations of PSR J0437−4715 were recorded in two approximately hour-long sessions in 2011 November using the Parkes 64 m radio telescope and the central beam of the 21 cm multibeam receiver (Staveley-Smith et al. 1996). We used the CASPER Parkes Swinburne Recorder (CASPSR), an 8-bit baseband recorder and a digital signal processing system, capable of real-time phase-coherent dispersion removal over a band up to 400 MHz wide. DSPSR (van Straten & Bailes 2011) was used to process the real-sampled voltages from a 300 MHz wideband2 centred at 1382 MHz. In total 117.3 min of data were recorded, or about 1.2 million pulsar rotations, each resolved into 1024 phase bins. A 512 channel filterbank was created while performing phase-coherent dispersion removal assuming a dispersion measure of 2.64476 (Verbiest et al. 2008). Inter-channel dispersion delays were removed before dividing the data into single pulses and recording the data on a Redundant Array of Independent Discs. We point out that, if the ephemeris aligns the peak of the total intensity at phase zero, then the reference phase in DSPSR needs to be offset to 0.5 turns. Otherwise every single pulse will be split between two data files. All subsequent processing was performed using the PSRCHIVE software suite (Hotan, van Straten & Manchester 2004; van Straten, Demorest & Osloski 2012). The data were converted to PSRFITS format (Hotan et al. 2004) and checked for incorrect header parameters.

Narrow-band radio frequency interference (RFI) was removed by applying a median filter, i.e. comparing the total flux density in each channel with that of its 49 neighbouring channels. We attempted several methods of post-folding removal of impulsive RFI but all of them removed some of the brightest pulses, rendering automatic removal impractical. Jenet et al. (1998) demonstrated that single pulses of PSR J0437−4715 are much narrower than the average pulse profile. This allowed us to pre-select potential RFI by searching for wide pulses and visually inspecting all the pulses broader than 54 phase bins, the expected maximum width of a sub-pulse.3 Also, the top 1 per cent of pulses sorted by S/N were visually scrutinized as the data with unexpectedly high S/N is likely to be RFI. This inspection found that only 0.01 per cent of data is affected by strong impulsive RFI and thus we ignore its presence throughout the analysis. We note that since its incorporation into the DSPSR package, the method of spectral kurtosis (Nita et al. 2007; Nita & Gary 2010) is becoming increasingly popular for rejection of RFI during pulsar observations. Unfortunately, it cannot be applied to our data. The brightest pulses of PSR J0437−4715 are difficult to distinguish from RFI using methods that excise signal above certain thresholds (e.g. total power or kurtosis) because the sub-pulse width and dispersive smearing are smaller than the time-scale over which these statistics are computed.

In order to perform polarimetric calibration using measurement equation template matching (METM, van Straten 2013), we applied the following procedure: an eight-hour long observing track of PSR J0437−4715 observed within a month of the observing session in 2011 November was calibrated using the measurement equation modelling technique (van Straten 2004). A high S/N calibrated template, consistent with data presented by Yan et al. (2011), was obtained and this is presented in Fig. 1. For each hour session of our main data set, five-minute integrations were formed by integrating single pulses in a hierarchical manner to minimize rounding error. These five-minute integrations were used to derive properties of the receiver at the time of observation. This information was used to calibrate the single pulses. See van Straten (2013) for details of the outlined procedure. Observations of the Hydra A radio galaxy, which is assumed to have a constant flux density of 43.1 Jy at 1400 MHz and a spectral index of −0.91 (Scheuer & Williams 1968), were used to calibrate the flux density scale.

2 The receiver used during the observing sessions provided only 300 MHz of bandwidth.

3 By a sub-pulse, we refer to a single emission event within a single pulse, that is a single pulse can consist of multiple sub-pulses.
Figure 1. Top: the high S/N (∼20,000) template for PSR J0437−4715 created from 8.5 h of observations is shown along with the polarization angle in the top panel. In the bottom panel, the solid black line represents total intensity, the dashed red line corresponds to linear polarization while the dotted blue line represents the circular polarization. Bottom: here we show the same profile but zoomed in to facilitate examination of the details of the polarization curves in the lower profile.

3 TOTAL INTENSITY PROPERTIES

We begin the data analysis with a focus on the total intensity of single pulses. We present the distribution of the single-pulse intensity and dependence of the average pulse profile on the S/N threshold for data inclusion before discussing the impact of the pulse energy distribution on timing properties of PSR J0437−4715. We then analyse the implications of phase-resolved flux density distributions on plasma physics in the emitting region, and finally discuss the quasi-periodic stationary and drifting intensity modulation.

3.1 Distribution of instantaneous signal-to-noise ratio

The flux density distribution of PSR J0437−4715 single pulses has been presented previously by Jenet et al. (1998) and is consistent with our findings. Here, we present the distribution of instantaneous S/N, as measured according to two separate definitions. The first one is

\[ S/N = \frac{\sum_{i=1}^{N_{\text{on}}} (F_i - B)}{\sqrt{N_{\text{on}}\sigma_{\text{off}}}}. \]

where \( F_i \) is the pulse flux density in the \( i \)th on-pulse bin; \( B \) is the mean off-pulse flux density; \( N_{\text{on}} \) is the number of on-pulse phase bins and \( \sigma_{\text{off}} \) is the off-pulse root mean square (rms) flux density. The S/N defined in this way is independent of the number of the phase bins used to resolve the pulse period. We note that the S/N of a narrow pulse with high flux density can be the same as a broad pulse with smaller flux density, making the definition of S/N sensitive to RFI which is often broader than the single pulses. Therefore, we checked our results using an alternative definition:

\[ S/N_{\text{peak}} = \frac{F_{\text{max}} - B}{\sigma_{\text{off}}}, \]

where \( F_{\text{max}} \) is the maximum flux density; \( S/N_{\text{peak}} \) is a phase-resolution-dependent quantity but it is more useful for finding high flux density spikes in the data.

The pulsar signal travels through the interstellar medium on the way to Earth. This has several consequences, such as dispersion and interstellar scintillation, the latter of which causes the apparent flux density to vary significantly, both in time and frequency (see Rickett 1990, for a review). By chance, the apparent flux density was relatively stable during observations presented in this work and variations were within a factor of 2. To facilitate comparison of single pulses with similar intrinsic S/N, we use the normalized quantity \( S/N_n = \frac{S/N}{\langle S/N \rangle} \), where \( <S/N> \) is the mean S/N in a minute (compared to a refractive scintillation time-scale of the order of 1000 s, Gwinn, Hirano & Boldyrev 2006) centred on the given single pulse.

The peak of \( S/N_{\text{peak}} \) distribution, as seen in Fig. 2, corresponds to the expected maximum amplitude of the noise in every pulse as we have 1024 phase bins and thus expect a 3 standard deviations peak in each observation. The instantaneous median unnormalized S/N is 10. This immediately implies that stochastic wideband impulse-modulated self-noise (SWIMS) will be significant in the observations of this pulsar (Osłowski et al. 2011). Due to heteroscedasticity and temporal correlation of SWIMS, the ToA estimates of average pulse profiles of PSR J0437−4715 are biased (Cordes & Shannon 2010; Osłowski et al. 2011; Liu et al. 2012) increasing the rms of the timing residuals (i.e. the difference between the modelled ToAs and the observations) by a factor of 4. Osłowski et al. (2011) and Osłowski et al. (2013) have presented a statistical method of correcting this bias by characterizing the SWIMS in the pulse profiles.

Figure 2. Observed instantaneous S/N. The solid line is the distribution of S/N while the dashed line represents the distribution of \( S/N_{\text{peak}} \). Overlap of the two distributions at high S/N range suggests that the brightest pulses are also the most narrow.
3.2 Impact of a single pulse on the ToA estimate

This and the next two sub-sections focus on total intensity properties of PSR J0437–4715 which relate to timing. We begin here by measuring the impact of a single pulse on the ToA estimate before moving on to an analysis of the evolution of selectively integrated pulse profiles and their timing properties.

As demonstrated in Section 3.1, the instantaneous S/N of single pulses from PSR J0437–4715 often exceeds unity. In such a case, we expect the effect of a single pulse on the ToA estimated from an integration of some length to be directly measurable. In this section, we quantify the average impact of a single pulse on the ToA estimate. To achieve this goal, we implemented the following procedure:

(i) we integrated one minute of data and formed an average pulse profile,
(ii) this profile was timed against the template profile presented in Fig. 1,
(iii) we then removed the first single pulse from this minute of data and added the next single pulse that follows the original minute of integration,
(iv) finally we go back to the first step and average the profile.

We have analysed in this way all of the single pulses in one hour of data, thus forming a ‘running ToA’ presented in Fig. 3. A typical ToA error estimate equals 58 ns. Note that we present only every 25th point, data and added the next single pulse that follows the original minute of integration,

We highlight two points in this plot around the −0.0025 abscissa value. These two timing residuals are separated by only 76.4 s and yet the difference between their estimates is 1500 ns, nearly 26 times the typical ToA error estimate. We can use these values to directly measure the bias introduced by SWIMS on the ToA estimate. Every single pulse between the two highlighted ToAs has affected the estimated ToA by 0.11 ns on average. While this number seems negligible, it implies that if an observer decided to postpone both the start and finish of a 1 min observation by 1 s, the estimated ToA would change by 19.1 ns on average. With next-generation radio telescopes, such as Five hundred metre Aperture Spherical Telescope (Nar 2006) or the Square Kilometre Array (Schilizzi, Dewdney & Lazio 2010) an observer might be satisfied with the achieved S/N ratio after a one-minute integration; however, the effect of SWIMS may dominate ToA estimates at frequencies similar to that of the observations presented in this work. At other frequencies, the relative importance of SWIMS will likely change.

Simulations performed with the ‘psrover’ application within PSRCHIVE show that a single pulse can affect the ToA even if it has only a fraction of the flux density of the average profile, especially if it is a wide pulse. In case of PSR J0437–4715 the sub-pulses are quite narrow but can have a very high flux density, as demonstrated in Fig. 4 and shown previously by Jenet et al. (1998). For the sake of visibility of the average pulse profile, the template’s flux density was artificially increased by a factor of 45. The energy in a single pulse can be larger than in the average pulse profile and concentrated over a much narrower phase range. The average pulse profile will be measurably different depending on the inclusion of this single pulse in the average, impacting the template matching algorithm used to derive the ToAs.

3.3 Average pulse profile dependence on sub-pulse S/N

We first present the dependence of the pulse profiles on the thresholds of S/N applied to the data used to create these profiles. Extending the ideas of Krishnamohan & Downs (1983), we divide our data into the following S/N ranges: [0.0, 0.5]; [0.5, 0.6); [0.6, 0.7]; [0.7, 0.8]; [0.8, 0.9]; [0.9, 1.0]; [1.0, 1.1]; [1.1, 1.2]; [1.2, 1.3]; The authors referred to the process of selective integration as gating which nowadays is often used to describe selecting a phase range of the pulse profile.
[1.3, 1.4); [1.4, 1.5); [1.5, 2.0); [2.0; 4.0); [4.0; 8.0); [8.0, 16.0); and >16.0. The average pulse profiles in a sub-set of these S/N ranges are plotted in Fig. 5. The averaged profiles were scaled to have the same peak intensity to facilitate comparison. The brightest pulses tend to occur near the peak of the template profile intensity. Shannon & Cordes (2012) have seen similar behaviour for PSR J1713+0747, which exhibits a correlation between the S/N of the single pulses and their ToA.

The investigation of Fig. 5 reveals that the two components distinguishable in the very centre of the profile are of nearly equal amplitudes when only the weakest pulses are integrated and the peak dominant in the average profile becomes more pronounced in the strongest pulses. In addition, in the average pulse profile formed from the weakest pulses, an additional component on the leading edge becomes visible. This component, present around pulse phase 0.47, can be seen in the template profile and should be included when modelling the pulse profile with analytical functions, see the bottom panel of Fig. 1.

We note that all of the profiles, even those constructed from the brightest pulses, exhibit the structure in the ‘wings’ identical to that of the average profile (see Fig. 6). This structure persists in all of the S/N ranges. Visual inspection of a number of the brightest single pulses, conducted during the search for RFI described in Section 2, reveals that not a single one of them has any visible emission in the wings phase region, and the vast majority of the single pulses are detected only in 20 phase bins near phase 0.5. The persistent presence of wings in the average pulse profile of these brightest pulses implies the presence of low-level emission, which is revealed only by averaging away the radiometer noise. This suggests that the pulsar magnetosphere is local, i.e. the presence of a bright single pulse does not affect other regions of magnetosphere, which continue to emit without being affected by any physical process that generated the bright emission.

As the high instantaneous S/N pulses are removed from data, the peak dominant in the average profile becomes more pronounced in the strongest pulses. In addition, in the average pulse profile formed from the weakest pulses, an additional component on the leading edge becomes visible. This component, present around pulse phase 0.47, can be seen in the template profile and should be included when modelling the pulse profile with analytical functions, see the bottom panel of Fig. 1.

Figure 5. Average pulse profile integrated using only data within given instantaneous normalized S/N ranges. The profiles were normalized to have the same peak flux density. The numbers in the label denote to the top end of the normalized S/N range. We used progressively darker colours to denote the different ranges. The lower limit of any range is the upper limit of the previous range, or 0.0 in the case of range denoted as 0.6. The inset in top-right corner zooms in on the peak region, i.e. from phase 0.488 to 0.516.

Figure 6. Average pulse profile integrated using only data within given instantaneous normalized S/N ranges. This figure is similar to Fig. 5, but this time the profiles were not re-normalized and we used logarithmic flux density scale to bring out the details in the profile wings.

3.4 Timing properties as a function of sub-pulse S/N

Because SWIMS begins to impact the ToA when the instantaneous S/N exceeds unity, it may be possible to limit the amount of such noise in the data by rejecting the brightest single pulses as identified by their normalized S/N. While such a procedure will reduce the S/N of the average pulse profiles, it may be beneficial as the noise will be closer to having equal variance in each pulse phase bin and being temporally uncorrelated; that is, the presence of SWIMS will be limited. We note that this will not completely remove the spectral correlations in the noise. In Table 1, we present the rms of the timing residuals for average profiles formed by integrating for one minute but including only single pulses with normalized S/N in the following ranges: S/Ns < 0.5; S/Ns < 1.0; S/Ns < 2.0; S/Ns < 4.0; S/Ns < 8.0 and the complementing ranges: >0.5; >1.0; >2.0; >4.0; >8.0. In this case, we have taken the identification of RFI into account and used only the data that was not flagged as affected by RFI. The table also contains the fraction of pulses that have been classified as belonging in the respective range.

The rms of the timing residual is marginally reduced for the data formed by rejecting the single pulses of S/Ns greater than 2, 4 or 8. The $\chi^2$/d.o.f. of the timing model is lower in these cases as well as for any other case when an upper limit on S/Ns is imposed. As high instantaneous S/N pulses are removed from data, the

Table 1. Rms of the timing residual for data formed by excluding single pulses in given S/Ns ranges. The rms of the timing residual is given in nanoseconds. The row highlighted in bold corresponds to standard timing technique.

| Included range | rms timing residual | $\chi^2$/d.o.f. | Fraction of pulses |
|----------------|---------------------|----------------|-------------------|
| S/Ns > 0.0     | 338                 | 39             | 1.000             |
| S/Ns > 0.5     | 316                 | 34.4           | 0.9625            |
| S/Ns > 1.0     | 340                 | 44.9           | 0.3669            |
| S/Ns > 2.0     | 931                 | 181.3          | 0.0204            |
| S/Ns > 4.0     | 3790                | 157            | 0.0007            |

5 We use the term ‘wings’ to refer to the phase region where the flux density is much lower than at the peak of the profile, e.g. from the first minima of the pulse profile on either side of the peak below flux density of 500 mJy in Fig. 1.
3.5 Observed electric field intensities and plasma physics

After decades of research and despite, many viable possibilities presented in the literature, the pulsar emission mechanism remains elusive. Following Cairns, Johnston & Das (2003a), we list the proposed linear processes including, but not limited to, linear acceleration and maser curvature emission (Luo & Melrose 1995; Melrose 1996, 2003, relativistic plasma emission (Melrose 1996; Asseo 1996) and a streaming instability into an escaping mode (Gedalin, Gruman & Melrose 2002). Non-linear processes have been proposed by several groups. The possibilities include direct conversion of plasma turbulence into electromagnetic emission (Weatherall 1997, 1998), soliton collapse (Asseo & Porzio 2006, and references therein) and an antenna mechanism (Pottelette, Treumann & Dubouloz 1992; Cairns & Robinson 2000). Most models of emission depend on the presence of dense plasma in the pulsar magnetosphere, exceeding the value expected in the classical model of Goldreich & Julian (1969) by orders of magnitude. A possible solution is that additional plasma is created in pair cascades in the acceleration gaps: polar (Sturrock 1971; Ruderman & Sutherland 1975), outer (Cheng, Ho & Ruderman 1986; Romani 1996) or slot (Muslimov & Harding 2003). Observation of highly energetic emission from pulsars suggest that the polar gap geometry is only viable for older pulsars while more energetic pulsars create plasma in either outer or slot gaps (Ravi, Manchester & Hobbs 2010) with the first one being favoured in a different study (Romani & Watters 2010).

An important aspect of emission is the interaction between plasma waves, driving particles and the background plasma in the magnetosphere. As pointed out in a series of papers by Cairns and collaborators (Cairns, Johnston & Das 2001; Cairns et al. 2003b; Cairns et al. 2003a), field statistics provide insight into plasma behaviour in the pulsar’s magnetosphere and these authors discuss two competing theories of such interactions. In brief, self-organized criticality (Bak, Tang & Wiesenfeld 1988; Bak 1996) describes systems interacting self-consistently without any preferred distance- or time-scales and predicts power-law distributions of intensities with indices typically in the range 0.5–2.0. Stochastic growth theory (SGT; Robinson 1992, 1995; Robinson, Cairns & Gurrent 1993; Cairns & Menietti 2001) in turn describes self-consistently interacting systems where the interactions take place in an independent homogeneous medium and introduce distance- and time-scales. This theory predicts a log-normal distribution of electric field.

The field statistics have been studied so far for the Vela pulsar in the aforementioned series of papers by Cairns and collaborators, as well as for PSR J1644–4559 and PSR J0953+0755 in a later work (Cairns et al. 2004). Smirnova (2006) demonstrated that the intensity of PSR J0953+0755 is distributed log normally at certain phases. The Crab pulsar is known to emit giant pulses which are very narrow and highly energetic emission events (Staelin & Reifenstein 1968; Hankins et al. 2003). To check if MSPs also show such pulses, Knight et al. (2006) studied four MSPs. The authors found that PSR J0218+4232 emits giants pulses with a power-law distribution of energies. Burke-Spolaor et al. (2012) studied the field statistics for a sample of 315 pulsars, including two MSPs, PSR J1439–5501 and PSR J1744–2934, but these distributions were not phase-resolved. The MSPs were found to have non-Gaussian and non-log-normal distribution of energies. Another related study of MSPs was done previously by Cognard et al. (1996), who studied the giant pulses from PSR J1939+2134. They found that the amplitudes of these pulses follow power-law distributions for the pulsars from both the main- and inter-pulse.

While power-law distributions of the electric field have been interpreted in the past as evidence of non-linear processes in the pulsar’s magnetosphere, the observed indices did not agree with theoretical predictions. Cairns et al. (2003b) proposed an explanation for this discrepancy. They argue that power-law distributions can be mimicked by two plasma wave populations that follow either log-normal statistics, as predicted by SGT, or normal statistics. Cairns, Robinson & Das (2002) present a convolution technique that also applies to electromagnetic fields originating from different source regions. This explains the unexpected indices of power-law distributions without the need to invoke non-linear processes.

To calculate the distribution of the electric field’s magnitude, we substitute the variables and ensure proper normalization:

$$P \left( \log_{10} E \right) = 2E^2 P(I),$$

where $I$ is the intensity and $E$ is the magnitude of the wave electric field. We note that in practice, to avoid rejecting very low flux density samples, an arbitrary offset is added to the observed flux density, following the method of Cairns et al. (2004). We are interested only in the shape of the magnitude distribution and such an absolute offset does not complicate interpretation while allowing more samples to be included in the estimates of the distribution in question.

The measured phase-resolved electric field probability density functions (PDFs) are shown in the top of Fig. 7 for a few chosen phase ranges. The PDFs in the off-pulse and low flux density regions (not shown) are well fit by a Gaussian distribution. The first three flux density distributions shown, representative of distributions for phases where the pulsar flux density is significant but not near its peak value, are well fit by a log-normal distribution, consistent with SGT predictions. An investigation of both the low and high flux density tails of the distribution reveals that a better fit may be obtained by a convolution of two populations, as suggested by Cairns et al. (2003b). This behaviour, already demonstrated for a number of pulsars, provides further support for the hypothesis that plasma in the pulsar magnetosphere is well modelled by SGT. The four PDFs for phases 0.488 to 0.508 (shown in the top of Fig. 7) correspond to phases near the peak of the total intensity. Strong deviations from log-normality approaching a power-law distribution are visible, with a significant population of pulses with very high magnitudes. We note that the flux density distribution in the notches, i.e. the ‘w’ shaped feature (see e.g. Dyks, Rudak & Rankin 2007) of the average pulse profile visible around phase 0.7 of Fig. 1, is indistinguishable from the distribution in nearby phases.

3.6 Intensity modulation

Many pulsars exhibit periodic intensity modulations. Sometimes the modulation function is stationary while in other cases it drifts with respect to pulse phase. The drifting phenomenon was first
Figure 7. Top: phase-resolved electric field magnitude probability density function. PDFs in seven chosen phase ranges, each integrated over 1/256 turns of phase and centred on the values denoted in the top right of the plot, are shown. For the vast majority of pulse phases (not shown), the distribution is very similar to that of the phase range centred on 0.293. The remaining plotted phase ranges are all near the peak of the pulse profile. Bottom: the same quantity but colour coded and plotted as a function of pulse phase. All the visible excursions towards higher values correspond to peaks of the average pulse profile.

discovered by Drake & Craft (1968a) by visual inspection of sequences of single pulses. We have searched our data for evidence of such phenomena by calculating longitude-resolved fluctuation spectra (Backer 1970a, 1973; Backer, Rankin & Campbell 1975) and two-dimensional fluctuation spectra (also referred to as harmonic-resolved fluctuation spectra, Deshpande & Rankin 2001; Edwards & Stappers 2002). An implementation of both of these spectrum calculations is available as the ‘drifting_subpulses’ application within the PSRCHIVE software suite.

We found no evidence of either stationary or drifting quasi-periodic intensity modulation. This places constraints on some models of the PSR J0437–4715 emission mechanism. Gil & Krawczyk (1997) modelled PSR J0437–4715 by assuming that the wings of the profile are the result of sub-pulse drift in the conal component of the beam. The lack of sub-pulse drift is consistent with a previous study by Vivekanand et al. (1998) at a frequency of 327 MHz. In the model of Jones (2012), lack of drifting in PSR J0437–4715 implies that this pulsar spins such that the relative orientation of rotation spin and polar-cap magnetic flux density is positive; i.e. the axes are closer to being aligned than anti-aligned; as it is the opposite direction of spin that provides the physical basis for phenomena such as nulling, drifting and mode switching. In brief, this is related to the physics of the polar cap; no existing model can explain the existence of electron–positron pair production regions (known as sparks) in the cases of aligned magnetic and spin axes. In the opposite case, their existence and, as a consequence, the phenomenon of nulling and drifting comes naturally (Ruderman & Sutherland 1975; Jones 2010, 2011).

To study the non-periodic modulation, we present in Fig. 8 the phase-resolved modulation index, i.e. the standard deviation of the intensity normalized by the mean intensity. The on-pulse regions on the edge of the profile, where the average flux density is low, show very high modulation. This is a typical behaviour seen in many other pulsars (see e.g. Taylor, Manchester & Huguenin 1975; Krishnamohan & Downs 1983; McKinnon 2004). The central region of the pulse profile shows a local maximum of the modulation. We note that all of the values are above the critical value of 0.3 which corresponds to purely Gaussian intensity modulation (McKinnon 2004).

4 POLARIMETRY

Pulsars are highly polarized sources and no study of pulsar emission can be complete without a description of the polarized flux density. In this section, we analyse the properties of the polarized emission of PSR J0437–4715. We begin by discussing the dependence of polarization on the S/N. Afterwards, we describe the detection of OPMs.

4.1 Polarization dependence on S/N

As in Section 3.3, we now investigate the polarization properties of the single pulses in chosen S/N ranges. As previously noted, when average profiles are formed by selectively integrating single pulses, the structure of the wings of the profile remains similar, with only the ratio of the peak flux density to flux density in the wings changing. In particular, the brighter pulses have more flux density between the local peaks of total intensity in the wings than the weaker pulses. An example of the pulse profile constructed from the 1 per cent brightest pulses as defined by their S/Npeak is shown in Fig. 9. Here, the Stokes parameters in the wings of these pulses are consistent with those of the template profile at most phases. However, the brightest pulses have a different polarization profile and degree of polarization in the centre of the averaged pulse profile as readily visible by comparing the bottom panel of Fig. 9 with...
Single pulses of PSR J0437–4715

Figure 9. Top: the average pulse profile of the brightest one per cent of sub-pulses. Bottom: zooming in on the lower parts of the profile reveals that all the Stokes parameters are consistent within the noise with the template. Meaning of various lines is the same as in Fig. 1.

The low-level emission appears independent of the emission in the central part as its properties are consistent with those of the template profile. The PA curve of the brightest pulses also follows the relevant curve of the template profile, except that the transition between the orthogonal modes occurs at an earlier phase in Fig. 1, i.e. later phase in Fig. 9.

The change in the polarization degree is also visible when we investigate it in the data formed from selective integration in the same S/N regimes as considered previously. Fig. 10 shows how the degrees of linear and circular polarization change across the integration ranges within 40 phase bins from phase 0.459 to 0.498, i.e. where the biggest difference in polarized pulsed profiles in Fig. 9 is visible. Note that the degree of linear polarization is calculated as \( \left( \sum |Q_i| + |U_i| \right) ^{1/2} / \left( \sum I_i \right) \) and that of circular polarization as \( \sum |V_i| / \sum I_i \), where summation is over phase bins in the aforementioned phase range and no bias removal was performed. However, because we calculate the degree of polarization based on the averaged profiles, there is no significant bias in the measurement. The steady rise of polarized flux density in the central part of the pulse profile with increasing S/N threshold is apparent, possibly due to the enhanced coherence of the emission mechanism responsible for the brighter pulses.

4.2 Phase-resolved polarization histograms

We also analysed the polarimetric properties of PSR J0437–4715 while preserving phase resolution. In this section, we present figures similar to figs 1 and 2 in Edwards & Stappers (2004). We first present the distribution of polarization angles derived from every single pulse in Fig. 12. The top panel shows the total intensity template profile with a few special phases marked with grey and red highlights. The bottom plot shows an unweighted phase-resolved histogram of polarization angles, normalized by the maximum value across all phases, with the perceived intensity of the image linearly dependent on the value of the histogram bin in both colour and black-and-white print, using the Cubehelix colour coding scheme (Green 2011). The polarization angle is plotted twice for clarity. We...
Figure 11. Examples of bright sub-pulses. The two pulses in the top exhibit the swing of circular polarization. See the text for more details.

point out the unusual distribution of the polarization angle near the peak of the pulse profile and polarization angle values close to 45°.

We also calculate the phase-resolved histograms of Stokes parameters on the Poincaré sphere. We implemented this using the Hierarchical Equal Area iso Latitude Pixelation of a sphere (HEALPIX, Górski et al. 2005) with the resolution parameter set to 3, corresponding to 768 pixels on the sphere. The generation of Poincaré sphere histograms was performed with the ‘psrpol’ application within the PSRCHIVE framework. This application reads in every sub-pulse and, for each pulse phase, computes the appropriate pixel on the sphere corresponding to the polarization vector and weights the contribution to that pixel by the polarized flux density. In this way, we obtain a separate histogram of polarization vector for all pulse phases. We present a few chosen Poincaré spheres in Figs 13 and 14 (an animation showing the evolution of the Poincaré sphere with the rotation phase can be obtained from the corresponding author). The first of these figures corresponds to the phase marked in red in Fig. 12, while the second one shows the remaining phases marked in Fig. 12 in grey. We note that the mean of the polarization vector varies significantly across the pulse phase, well beyond the variance of the polarization at any phase.

The most notable feature of the polarization patterns visible in Figs 12, 13 and 14 is the presence of OPMs (Stinebring et al. 1984) near the peak flux density of the total intensity at the phase 0.508. The modes appear to be not perfectly orthogonal. While the presence of OPMs is expected for this pulsar based on its average profile (Navarro et al. 1997), to our knowledge this is the first direct detection of OPMs in an MSP. More surprisingly, we do not detect OPMs at different phases, where the emission is dominated by one mode despite the complicated shape of the polarization angle curve across spin phase. This suggests that the emission may originate in several regions (Navarro et al. 1997), in contrast to the conclusion of Gil & Krawczyk (1997). Furthermore, based on the presence of OPM near the peak of the pulse profile and the rapid swing of polarization angle shown in Fig. 12, we support the idea that the impact parameter is of the order of a few degrees (Navarro et al. 1997), consistent with the fit of a relativistic rotating vector model to the polarization angle sweep (Gil & Krawczyk 1997). In such a case, the variations of polarization angle across the spin phase can be caused by the emission originating close to the surface, where deviations from dipolar structure of the magnetic field is still strong, or from deformations further out in the magnetosphere (Ruderman 1991).

We also do not see annuli as seen by Edwards & Stappers (2004) in the case of PSR B0329+54; however, we do see deviations from a Gaussian distribution of polarization, for example in the...
Figure 12. Logarithm of the phase-resolved distribution of polarization angle is shown in the bottom panel, while the top panel shows a total intensity template with a few chosen phases of interest marked in grey and red.

Figure 13. Lambert equal area azimuthal projection of the Poincaré sphere interrupted at the equator at phase 0.508, marked in red in Fig. 12. To avoid heavy distortions, the projection is interrupted at the equator and the other hemisphere is plotted on the right-hand side. The intensity of the sphere is proportional to the value of the histogram in the given point on Poincaré's sphere. OPMs are clearly visible. The black lines and the large black dot at their intersection correspond to four meridians (longitudes of $0^\circ$, $90^\circ$, $180^\circ$ and $270^\circ$) and the north pole of the Poincaré sphere, which corresponds to fully left hand circularly polarized radiation. The red squares mark the poles of each hemisphere. Colour coding is the same as in Fig. 12.

fourth-last panel in Fig. 14, corresponding to the spin phase equal 0.547. Detection of the modes near the peak intensity is expected from the shape of the polarization angle curve and the increased modulation index. The association of OPMs with highly modulated emission has been first noted by McKinnon (2004) and explained statistically by van Straten (2009). Furthermore, Dyks et al. (2007), Dyks, Rudak & Demorest (2010) argue that PSR J0437–4715 is likely to exhibit OPMs and that the trailing side of the pulse profile is dominated by the extraordinary polarization mode, as this mode can explain the creation of the notches by assuming curvature emission from thin plasma streams. We note that soliton emission seen only in the leading part of the profile is also expected to result in the extraordinary mode.

We can now tie together several of our results, namely that the brightest pulses preferentially occur in the leading component, switch to a different polarization mode at a later phase, and are more
Figure 14. Lambert equal area azimuthal projection of the Poincaré sphere interrupted at the equator near the phases 0.293, 0.336, 0.449, 0.465, 0.492, 0.504, 0.547, 0.574, 0.645, 0.684, marked in Fig. 12 in grey. The projections are presented in reading order with two projected hemispheres per phase range. Colour coding and meaning of all marks is the same as in Fig. 13.
polarized. By selectively integrating the brightest pulses, we extend the phase region in which their polarization properties dominate the average profile, thus delaying the transition to the second polarization mode. Finally, since the brightest pulses occur preferentially where one of the modes dominates, their average profile exhibits less depolarization by the superposition of OPMs.

5 CONCLUSIONS

We have presented a study of PSR J0437−4715 sub-pulse properties in the 21 cm band. We attempted to reduce the post-fit arrival time residual by minimizing SWIMS via rejection of the sub-pulses with the highest flux density while taking scintillation into account. While we have not achieved a significant improvement in the timing precision, we demonstrated that the rms of the timing residual and the statistical goodness of the timing model fit can be improved by rejecting the brightest sub-pulses and demonstrated a correlation between the average ToA and the S/N of the sub-pulses as a consequence of the leading component dominating the mean profile of brightest pulses. Phase-resolved histograms of the pulse intensity have log-normal distributions in a range of pulse phase, consistent with predictions of the SGT of plasma waves. We discovered that there is a strong increase of the degree of polarization, both linear and circular, with the pulse intensity. A special class of the brightest pulses has polarization features compatible with those expected from a relativistic soliton. Finally, we presented the phase-resolved histograms of polarization angle and polarization vector. These reveal the existence of two OPMs in a narrow phase range, for the first time directly detected in an MSP. The modes show slight deviation from orthogonality. Throughout most of the pulse phase, the emission is dominated by one mode and the other is not visible, if present.

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