ACCRETION ONTO INTERMEDIATE-MASS BLACK HOLES IN DENSE PROTOGALACTIC CLOUDS

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ABSTRACT

We present the first results from two-dimensional simulations of radiatively efficient accretion of metal-free gas onto intermediate-mass black holes. We fix the shape of the spectral energy distribution of the radiation produced near the event horizon and study the structure of the irradiated low-angular-momentum accretion flow over 3 orders of magnitude in radius from the black hole, $10^{14}-10^{17}$ cm for a 100 $M_{\odot}$ black hole. The luminosity of the central source is made to be proportional to the rate at which gas accretes across the inner boundary, which we set just inside the sonic radius. We find that photoionization heating and radiation pressure modify the structure of the flow. When the ambient gas density is $10^{7}$ cm$^{-3}$, accretion is intermittent and on average reduced to 32% of the Eddington-limited rate, over 2 orders of magnitude below the “Bondi” rate evaluated ignoring radiation, in agreement with theoretical models. Even if the vicinity of the black hole is supplied with high-density gas, accretion is rendered inefficient through heating and radiation pressure.

Key words: accretion, accretion disks – black hole physics – galaxies: active – hydrodynamics – methods: numerical – quasars: general

1. INTRODUCTION

Known stellar-mass and intermediate-mass black hole candidates accrete through mass transfer from a stellar companion without exception. Rapidly accreting massive black hole candidates, such as in Seyfert galaxies and quasars, appear to be situated close to dusty, molecular, and highly inhomogeneous gas reservoirs, where cold, dense clumps are in free fall or are embedded in a hot, ionized, and tenuous confining medium. In neither case does the accretion flow resemble the laminar flow of the Bondi–Hoyle–Littleton solution. There is a distinct possibility, however, that massive black hole progenitor “seeds,” with masses $M_{\text{bh}} \gtrsim 100$ $M_{\odot}$ (Madau & Rees 2001), did pass through an early phase of quasi-radial accretion in protogalaxies, prior to significant dust enrichment and the emergence of a pervasive cold phase in the interstellar medium (e.g., Volonteri & Rees 2005; Alvarez et al. 2006, 2008; Johnson & Bromm 2007; Pelupessy et al. 2007; Di Matteo et al. 2008; Greif et al. 2008). This was the period immediately following the onset of atomic cooling, the epoch when protogalaxies experienced rapid growth due to cosmic infall and yet had potential wells too shallow to retain all of their newly synthesized metals.

Since the accretion rate in quasi-radial, Bondi-like accretion is proportional to gas density, Bondi-like accretion presents an appealing formation process for massive black holes: given the presence of sufficiently dense gas in a protogalactic nucleus, Eddington-limited accretion and mass exponentiation on a Salpeter timescale would proceed; stellar-size seed black holes would reach masses $\gtrsim 10^5$ $M_{\odot}$ inferred in high-redshift quasars in the cosmic time available to them (e.g., Haiman & Loeb 2001; Volonteri et al. 2003; Tanaka & Haiman 2008).

A potential flaw in this reasoning was noticed early, namely, that in the event of radiatively efficient accretion, radiative heating and radiation pressure may reduce the accretion rate (Shvartsman 1971; Buff & McCray 1974; Hatchett et al. 1976; Ostriker et al. 1976; Cowie et al. 1978; Stellingwerf 1982; Begelman 1985; Ricotti et al. 2008; Alvarez et al. 2008). The possibility of a transition to radiative-feedback-driven temporal intermittency, which has been evident in one-dimensional simulations of Compton-heated (Ciotti & Ostriker 2001) as well as Compton- and photoionization-heated and radiation pressure-driven (Sazonov et al. 2005; Ciotti & Ostriker 2007) accretion onto massive black holes in elliptical galaxies, has further complicated the assessment of quasi-radial accretion’s viability as a massive black hole formation process. If the accretion is indeed intermittent and episodic, how long is the duty cycle, how large is the average accretion rate, and does it permit evolution of seed black holes into quasars? Does episodic accretion proceed in bursts, where episodes of Eddington-limited rapid accretion alternate with near-complete radiative quenching and outflow, as one-dimensional models appear to suggest, or does the multidimensional nature of realistic irradiated accretion flows imply a damping of the fluctuations and convergence to a quasi-steady state characterized by a reduced accretion rate?

Here, we present the first results from our program to investigate radiatively efficient accretion onto black holes embedded in a realistic galactic gaseous medium with the help of high-resolution hydrodynamic simulations. We do not attempt to simulate fluid flow and radiation emission mechanisms near the event horizon of the black hole; instead, we simply fix the shape of the spectral energy distribution of the radiation produced near the event horizon and simulate the irradiated fluid flow on radial scales spanning the sonic radius, where the photoheated fluid falls supersonically toward the black hole, and a much larger radius in the gas cloud that is entirely unaffected by the black hole’s radiative output, where boundary conditions for the accretion flow are set. This work is organized as follows. In Section 2, we concisely describe our numerical algorithm. A more detailed description and a suite of tests will be provided in a longer follow-up paper (S. M. Couch et al. 2009, in preparation). In Section 3, we describe our results with particular focus on the intermittency of the accretion flow. In Section 4, we compare our results to analytical models (Milosavljević et al. 2009, and references therein) and discuss the outlook for massive black hole formation through quasi-radial accretion.
2. NUMERICAL ALGORITHM

Here we describe numerical methodologies that we have implemented in the parallel adaptive-mesh-refinement (AMR) code FLASH (Fryxell et al. 2000), version 2.5, to facilitate our simulations of low-angular momentum accretion flow with a central ionizing source. The hydrodynamic solver used was the piecewise parabolic method (PPM), which is a higher order Godunov method. Contact steepening that sharpens contact discontinuities in the PPM module was disabled after we noticed that it led to spurious flow near stationary ionization fronts. By default, FLASH does not conserve angular momentum in two-dimensional cylindrical simulations. To simulate fluid motion in the azimuthal direction, we introduce the specific angular momentum \( l \equiv R \nu \rho \) as an additional conserved “mass scalar” quantity that is advected with the fluid. Equivalence with three-dimensional cylindrically symmetric equations of fluid dynamics is achieved by adding the centrifugal force to the total acceleration, \( \mathbf{a} = \mathbf{a}_{\text{grav}} + \mathbf{a}_{\text{rad}} + l^2 \mathbf{R}/R^3 \).

2.1. The Central Hole and the Central Ionizing Source

The simulations were carried out in cylindrical symmetry on a rectangular \((R, z)\) grid in two spatial dimensions, where \( R \) is the distance from the axis of symmetry. In what follows, \( r \) will denote the distance from the origin, \( r^2 = R^2 + z^2 \). A small spherical region \( r < r_{\text{hole}} \) was excluded from the hydrodynamical update; we refer to this region as the “hole.” A unidirectional “outflow” boundary condition, allowing only outflow from the simulated spatial domain and inflow into the central hole, was imposed at \( r = r_{\text{hole}} \). The gravitational acceleration was set to that of a Newtonian point mass located at the origin of the grid \( \mathbf{a}_{\text{grav}} = -GM_{\text{hole}} \hat{r}/r^2 \). The mass of the material flowing into the hole was added to the point mass \( M_{\text{hole}} \). Self-gravity of the fluid was ignored because, typically, the mass of the photoionized gas around the black hole was less than 1% of the mass of the black hole.

An isotropic source of ionizing radiation was placed at the origin of the grid. The total luminosity of the ionizing source between energies \( h\nu_{\text{min}} = 13.6 \text{ eV} \) and \( h\nu_{\text{max}} = 100 \text{ keV} \) was set to be proportional to the accretion rate into the hole,

\[
\int_{\nu_{\text{min}}}^{\nu_{\text{max}}} L_\nu d\nu = \epsilon M_{\text{hole}} c^2, \tag{1}
\]

where \( \epsilon \) is a radiative efficiency which was uniformly set to 0.1. The radiative spectral energy distribution was set to obey the power law \( L_\nu \propto \nu^{-3/2} \) and was calculated in 40 logarithmically spaced energy bins.

2.2. Composition, Chemistry, and Thermodynamics

We simulated a six-species primordial fluid mixture of hydrogen and helium and their ions: \( \text{H}^+, \text{H}^0, \text{He}, \text{He}^+, \text{He}^{++}, \) and \( e^- \). Abundances of the six species were integrated in time with a chemical network that includes collisional ionization of \( \text{H}, \text{He}, \text{He}^+, \text{He}^{++} \), bidirectional charge exchange between \( \text{H}^+ \) and \( \text{He}^{++} \), as well as primary and secondary photoionization of \( \text{H} \) and \( \text{He} \). Secondary photoionization and heating by fast photoelectrons were implemented in accordance with the results of Shull & van Steenberg (1985) and Dalgarno et al. (1999). Photoionization and photoheating rates were calculated in a photon-conserving manner (see Section 2.3) from the local, extincted radiative fluxes.

Photoionization heating and collisional cooling of the fluid were operator-split from the hydrodynamic update. Cooling processes that were taken into account include bremsstrahlung, collisional ionization cooling of \( \text{H}, \text{He}, \text{He}^+ \), recombination cooling of \( \text{H}^+, \text{He}^+, \text{He}^{++} \), radiative recombination cooling of \( \text{He}^+ \), collisional excitation cooling of \( \text{H} \) and \( \text{He}^+ \), and Compton cooling to the cosmic microwave background. At the high gas densities in the simulations, the Compton cooling was negligible.

Number densities of all six species and the temperature of the gas were advanced simultaneously during the chemical and thermodynamic update with the Bulirsch–Stoer-type semi-implicit extrapolation mid-point method of Bader & Deuffhard (1983). Our implementation of the method closely follows that provided in the GNU Scientific Library (Galassi et al. 2006). This method utilizes the Jacobian matrix of the partial derivatives of the right-hand side of our seven coupled ordinary differential equations. We evaluate the partial derivatives analytically. Special care was taken to accurately integrate the abundance of the neutral and partially ionized fraction in a strongly photoionized gas. We carried the Richardson extrapolation sequence to four points, which was sufficient for numerical stability.

In the operator-split alternating hydrodynamical and chemothermodynamic update, the hydrodynamic step was globally constrained to not exceed 10% of the minimum electron abundance change timescale, \( \Delta \text{hydro} \leq 0.1 n_e/|\dot{n}_e| \), in combination with the usual Courant limit. The chemothermodynamic update is carried out in single or in multiple and possibly much shorter Bader–Deuffhard steps. The latter are individually limited in every cell by the timescale on which any of the six abundances and the temperature evolves, \( \Delta \text{BD} \leq \min[0.1 n_i/|\dot{n}_i|, 0.1 T/\dot{T}, \Delta \text{hydro}] \), where \( i = \text{H}, \ldots, e^- \) (see, e.g., Whalen & Norman 2006).

2.3. Line-of-Sight Radiative Transfer and Radiation Pressure

Here, we discuss our implementation of multifrequency photon-conserving line-of-sight radiative transfer and the resulting radiation pressure force. We calculate the line-of-sight optical depth \( \tau \nu \) from the central source to the faces of any rectangular zone along \( N_{\text{ray}} = 4 \) separate rays, \( k = 1, \ldots, N_{\text{ray}} \); the rays are equally spaced in angle as seen from the central source. We also calculate the optical depth to absorption within the zone along each of the rays \( \hat{\tau} \nu \). The effective flux at the zone center is calculated via (see, e.g., Mellema et al. 2006, and references therein)

\[
F_\nu = \frac{L_\nu}{4\pi r^2} \sum_{k=1}^{N_{\text{ray}}} \exp \left(-\hat{\tau}_{\nu}^{(k)}\right) \left[1 - \exp \left(-\hat{\tau}_{\nu}^{(k)}\right)\right]. \tag{2}
\]

The total photon absorption rates per chemical species \( i \) within the zone are then calculated via \( \Gamma_{i,\nu} = \sigma_{i,\nu} n_i V F_\nu / h\nu \), where \( V \) is the zone volume. In the limit in which the zone is very optically thick, \( \hat{\tau}_{\nu}^{(k)} \gg 1 \), we obtain

\[
\sum_i \Gamma_{i,\nu} \approx (h\nu)^{-1} F_\nu \left[\exp \left(-\hat{\tau}_{\nu}^{(k)}\right)\right] \Omega,
\]

where \( \Omega \) is the angular size of the zone as seen from the central source, and the extinction external to the zone is averaged over rays. The approximation in Equation (3) becomes exact in the limit \( N_{\text{rays}} \to \infty \), as it has to be to conserve photons.

We calculate radiation pressure associated with photoionization and Thomson scattering. The radiation pressure force is added to the gravitational force of the central point mass. We ignore line resonance radiation altogether and also ignore any diffusion of ionizing radiation (see, e.g., Ritzerveld 2005).
2.4. Mesh Refinement and Initial Conditions

We simulate a cylindrical domain in the upper hemisphere \(0 < (R, z) < 1 \text{pc}\) with 18 levels of mesh refinement. Since each AMR block contains \(8 \times 8\) zones, the maximum spatial resolution in the simulation is \(\Delta x \sim 3 \times 10^{12} \text{cm}\). We require that the central hole, with radius \(r_{\text{hole}} = 10^{14} \text{cm}\), is always resolved at the highest level of mesh refinement. We achieve pseudo-logarithmic gridding by capping the resolution at radius \(r\) with \(\Delta x > \frac{1}{4} \text{yr}\) where we choose \(\eta = 0.1\); this prevents the use of excessive resolution far from the central hole. The simulation domain initially contained uniform-density partially ionized gas, with initial electron abundance of \(\chi_{e} = 0.5\), at temperature \(10^4 \text{K}\) and density \(n_{H} = 10^5 \text{cm}^{-3}\). The initial value for the central point mass was \(100 \, M_{\odot}\).

3. RESULTS

The central accretion rate, shown in Figure 1, oscillates between values close to, and occasionally mildly exceeding the Eddington limit, \(\dot{M}_{\text{max}} \sim \dot{M}_{\text{Edd}} \sim 2 \times 10^{-6} \, M_{\odot} \, \text{yr}^{-1}\), and a rate lower by an order of magnitude, \(\dot{M}_{\text{min}} \sim 2 \times 10^{-7} \, M_{\odot} \, \text{yr}^{-1}\). The accretion rate is approximately periodic with a mild trend toward an increasing period separating consecutive peak episodes; the period varies between 250 yr and 350 yr. Accretion rate falloff following a maximum is roughly exponential, as may be expected when photoheating and photoionization radiation pressure in the ionized region surrounding the black hole drive down the accretion rate (see Section 3 in Milosavljević et al. 2009). The average accretion rate and luminosity are \(\langle \dot{M} \rangle = 4.6 \times 10^{39} \, \text{g} \, \text{s}^{-1}\) and \(\langle L \rangle = 4.2 \times 10^{39} \, \text{erg} \, \text{s}^{-1}\), which says that on average, the black hole accretes at 32% of the Eddington limit. The average accretion rate is still only \(-0.2\%\) of the isothermal “Bondi” accretion rate \(\dot{M}_{\text{Bondi}} = \frac{3}{2} \pi \beta (GM_{\text{bh}})^{2} n m_{p} / c_{s}^{3}(\infty)\), calculated ignoring radiative feedback, for an ambient sound speed of \(c_{s}(\infty) = 14 \, \text{km} \, \text{s}^{-1}\).

During a central accretion maximum, electron scattering and photoionization radiation pressure drive an outflow in the ionized gas within the \(\text{H} \, \text{II}\) region that has neutral fractions \(\chi_{H} \sim 10^{-4} \sim 10^{-5}\) (Figure 2, lower panels). This leads to rarefaction and exponential drop in central accretion. Meanwhile, as radiation pressure subsides, gas near the edge of the \(\text{H} \, \text{II}\) region accelerates inward. This acceleration is driven by a gas pressure imbalance near the edge; the imbalance was inherited from the preceding accretion maximum when an outward radiation pressure force balanced an inward gas pressure gradient force. The outflow intersects with the inflow, and the infalling gas ultimately arrives at the edge of the central hole and gives rise to a new accretion maximum. The longest timescale in the cycle is the inward acceleration and infall time, which is here a factor of \(-3\) shorter than the radial sound crossing time of the \(\text{H} \, \text{II}\) region with typical temperature \(T_{\text{H} \, \text{II}} \sim 4 \times 10^{4} \, \text{K}\).

To investigate the relative importance of radiation pressure compared to heating, we continued the simulation shown in Figures 1–3 with the radiation pressure force artificially set to zero. The heating-only simulation exhibited a significantly higher, super-Eddington mean accretion rate and a rapid, monthly variability reflecting an episodic heating to the Compton temperature and convective transport at \(r \sim r_{\text{hole}}\). The longer period (\(~300\) yr) behavior observed in the simulation with the radiation pressure was absent in the heating-only simulation.
The very high accretion rate observed in the heating-only simulation is a potential artifact of \( r_{\text{hole}} \) being much larger than the sonic radius in this simulation, but if we spatially resolved the sonic radius in the high-accretion-rate regime, the Courant-limited time step would have become prohibitively short.

Figure 3(a) shows that the radius of the H II region surrounding the black hole reaches an asymptotic value of \( r_{\text{son}} \sim 6 \times 10^{16} \text{ cm} \). This only somewhat smaller, by 46%, than the crude estimate obtained for hydrogen-only cloud in Milosavljevi´c et al. (2009). The region \( r < r_{\text{son}} \) is not entirely free of neutral gas; during accretion minima, as seen in the two left panels of Figure 2, dense clumps form in the gas that has been expelled by radiation pressure and is now falling back toward the black hole, and the regions in the dense clumps’ shadows recombine. The range of radii that is shaded in Figure 3(a) contains a multiphase medium. The densest neutral clumps that form near the edges of the H II region are six times denser than the ambient gas, but this density is not sufficient to resist photoevaporation and dispersal during accretion maxima. Figure 3(b) shows that the flow into the central hole is typically supersonic with sonic radius located at \( r_s \sim 2 \times 10^{14} \text{ cm} \), but during accretion maxima, shock heating in the infalling gas drives subsonic flow to the brink of the excited hole at \( r_{\text{hole}} = 10^{14} \text{ cm} \).

4. CONCLUSIONS AND DISCUSSION

We have simulated accretion from a uniform, high-density (10^7 cm\(^{-3}\)) metal-free protogalactic cloud onto an intermediate-mass black hole. At radii from the black hole smaller than the size of the excised region, 10^{14} cm, the accretion was assumed to be radiatively efficient. We find that a compact H II region forms around the black hole. The accretion is intermittent due to alternating radiation pressure-driven expulsion and external pressure-driven fallback. The average accretion rate is \(< 1\% \) of the Bondi accretion rate calculated ignoring the radiation’s influence, and \( \sim \frac{1}{2} \) of the Eddington-limited rate.

The numerical results are consistent with the predictions of our toy model for episodic quasi-radial accretion (Milosavljevi´c et al. 2009), where we suggested that photoionization heating and photoionization radiation pressure within the compact H II region are the dominant accretion-suppression mechanisms. We also suggested that Ly\( \alpha \) line resonance radiation pressure, which we do not account for in the simulations presented here, should further reduce the accretion rate. The intermittency is qualitatively similar to that seen in one-dimensional simulations of the accretion of hot irradiated gas onto black holes in elliptical galaxies by Ciotti & Ostriker (2007), where Compton heating and photoionization heating were both observed to be significant drivers of the accretion intermittency; we emphasize, however, that the gas densities, temperatures, and gravitational potential depths in elliptical galaxies are very different than the ones considered here.

The simulation in which the accreting fluid was endowed with small angular momentum corresponding to maximum circularization radius equal to \( r_{\text{hole}} \) exhibited similar intermittency and only a slightly reduced average accretion rate, consistent with Krumholz et al. (2005, and references therein). In contrast with the nonrotating simulations that did not contain axial outflows, narrow polar outflows form that resemble some of those found by Proga (2007) and Proga et al. (2008) in simulations of accretion flows irradiated by a quasar. The accretion intermittency and inflow–outflow behavior that we observe is qualitatively similar to that seen in Proga et al., but additional tests are needed to ascertain whether our axial outflows are physical.

The overall goal is to combine the highly resolved simulations presented here with large-scale cosmological simulations of how the first galaxies formed at the end of the cosmic dark ages (e.g., Greif et al. 2008). Those simulations can resolve the central gas flows to within \( \sim 0.01 \text{ pc} \), where we can implement subgrid prescriptions based on the calculations done here. An important challenge will be to derive prescriptions for the feedback from black hole accretion that are applicable to a wide range of protogalactic conditions. We will report on these efforts elsewhere (S. M. Couch et al. 2009, in preparation).

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