Development of magnetic liquid metal suspensions for magnetohydrodynamics
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I. INTRODUCTION

Magnetohydrodynamic (MHD) phenomena involve the interaction of magnetic fields with fluid flows. For example, many planets and stars exhibit a spontaneous dynamo effect in which a magnetic field is generated by flow of a conducting fluid. This, and other MHD phenomena which depend on fluid flow advecting magnetic fields, occur at large magnetic Reynolds number $Re_m$, which is a characteristic ratio of advection to diffusion of magnetic fields in the flow.

We demonstrate how to suspend various magnetic and non-magnetic particles in liquid metals and characterize their properties relevant to magnetohydrodynamics (MHD). The suspending method uses a high conductivity liquid metal and eliminates oxidation from both metal particles and liquid, which allows the particles to be wetted and suspend into the liquid if the particles have higher conductivity than the liquid. With this process we were able to suspend a wide range of particle materials and sizes from $40 \text{ nm}$ to $500 \mu \text{m}$, into three different liquid metal bases, and volume fractions $\phi$ up to the liquid-solid transition $\phi_c$. By controlling the volume fraction of iron particles in liquid eGaIn, we increased the magnetic permeability by a factor of 5.0 and the electrical conductivity by 13% over that of the pure liquid metal, which gives these materials the potential to exhibit strong MHD effects on the laboratory scale that are usually only observable in the cores of planets and stars. By adding non-magnetic zinc particles, we increased the viscosity by a factor of 160 while keeping the magnetic and electrical properties nearly constant, which would allow independent control of MHD effects from turbulence. We show that the suspensions flow like Newtonian fluids up to the volume fraction of the liquid-solid transition $\phi_c$.  

A spontaneous dynamo in an unconstrained flow requires the highest $Re_m(\gtrsim 30)$ to achieve among MHD phenomena [5], so this $Re_m$ is our ultimate target goal for materials design. To achieve such high $Re_m$, liquid metals and plasmas are traditionally used in experiments because they are the fluids with the highest conductivities $\sigma$. To contain plasmas requires specific magnetic field arrangements and a laminar flow, which are challenges that have not yet been overcome to create a dynamo [6]. Liquid sodium is the preferred working fluid for dynamo experiments [5, 7–9] because of its high conductivity ($\sigma = 9.6 \cdot 10^6 \text{S/m}$) [10], but can be a challenge to work with because it has a high melting point and

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explodes on contact with water. Even then, experiments have had to be at least 0.5 m in size and have taken at least 7 years to create a dynamo [5, 7, 8]. Gallium, which has lower conductivity ($\sigma = 3.4 \cdot 10^6$ S/m) than sodium, has been suitable for observing other MHD phenomena such as the magneto-rotational instability which only require $Re_m > 1$ [11]. A limitation of liquid metals is that at temperatures at which they are liquid, all metals have negligible $\chi \approx 10^{-6} - 10^{-5}$, which is the other material parameter that affects $Re_m$. An increase in $\chi$ by itself is also of interest as forces on the material from magnetic fields are proportional to $\chi$. We propose to improve on the achievable range of $\chi$ and $Re_m$ by suspending magnetic particles into liquid metals to create a Magnetic Liquid Metal (MLM) with both large susceptibility $\chi$ from the particles and conductivity $\sigma$ from the liquid metals.

Suspending magnetic particles in liquid metals has been attempted before with limited success. Attempts to suspend pure iron or nickel particles in non-oxidized gallium failed to make suspensions [12–14]. On the other hand, nickel [13, 15] and FeNbVB [14] particles coated with silica were suspended in gallium. However, in one of those cases the liquid metal was intentionally oxidized to allow suspending silica-coated particles [15]. In the other cases, we can infer that the liquid metals were oxidized based on the pictures reported which appear dull, rather than shiny like a pure liquid metal [13, 14]. Because oxidized liquid metals have a thin oxidation film on their surface, they have a yield stress like a solid [16], and so do not flow as a Newtonian liquid as would likely be desired for MHD applications.

Martin et al. [17] suspended iron beads of diameter $d = 6.35$ mm into liquid gallium. They were able to achieve effective susceptibilities $\chi \approx 3$. These particles were larger than the capillary length ($\sqrt{\gamma/\rho g} = 3.2$ mm for gallium [18], where $\gamma$ is the surface tension, $\rho$ is the density and $g$ the gravitational constant), which means that they were heavy enough that the stress due to their weight ($\sim \rho gd = 500$ Pa) was larger than the stress from surface tension ($\sim \gamma/\rho g = 100$ Pa) due to the oxide layer [16]. Thus, particles could break through the surface to get into the bulk of the liquid metal regardless of surface tension or whether there was an oxidation layer. However, particles this large can break out through the surface just as easily, settle quickly under the effect of gravity, and are not expected to follow fluid flow due to their inertia, properties which may be undesirable in applications.

Magnetic particles have been successfully suspended into mercury, in which case it was implied that there was no oxidation [1, 19]. However, mercury is not a desirable liquid due to its toxicity. Furthermore, only very low volume fractions of magnetic particles were suspended in mercury; resulting in up to $\chi = 2 \cdot 10^{-4}$ for 2% by weight Fe-Ni-B particles [19] and $\chi = 3 \cdot 10^{-5}$ for a few percent iron particles coated with tin [1], in both cases this was too small to allow a significant increase in $Re_m \propto 1 + \chi$.

To address the weaknesses of previous attempts to suspend magnetic particles in liquid metals, we present in this paper a new suspending method that can be generally applied to suspend a variety of different metallic particles into different liquid metals. By removing and preventing oxidation of the metallic particles with a flux (i.e. an acid), we make the surface wettable by liquid metals which allows them to suspend into the liquid bulk. The flux also prevents and removes any oxide layer from the liquid metal so it behaves mechanically like a simple liquid [16]. The suspending method has the advantage that we can suspend both non-Brownian and Brownian particles; the latter is desirable so the particles do not settle or behave inertially. By increasing the volume fraction of magnetic particles suspended up to the liquid-solid transition we are able to tune $\chi$ and thus $Re_m$ over a wide range. We demonstrate this suspending method using liquid gallium and two of its alloys. These liquids have the advantage that they are liquid at or near room temperature, have low vapor pressure (i.e. they are not toxic like mercury [20]), and do not explode on contact with water like sodium, making them relatively easy to work with compared to other liquid metals. However, they do have the disadvantage that they corrode some metals, such as aluminum and copper [21]. We explain in detail in this article how this suspending process works generally for a variety of materials so it can be easily reproduced and extended in other laboratories.

By adding a third phase of non-magnetic particles into the suspension, we can additionally tune the viscosity $\eta$ of the fluid. This is useful in particular for tuning the Reynolds number $Re = \rho UL/\eta$ (or, equivalently, the magnetic Prandtl number $Pr_m = Re_m/Re$) independently of $Re_m$. Since both $Re$ and $Re_m$ scale with $U$ and $L$, independent control cannot be done over a significant range with liquid metals alone, and as a result both natural and experimental dynamos have always been at high $Re$ and turbulent [5, 7, 8]. Controlling separately the MHD control parameter $Re_m$ and the turbulence control parameter $Re$ will allow investigation of how each separately contributes to MHD phenomena.

The remainder of this article is organized as follows. Section II is a detailed description of how to create MLM, with a process that can apply to a wide range of materials and particle sizes. Section III describes the samples characterized in later sections. Sections IV, V, and VI, give characterizations of the viscosity, magnetic susceptibility, and conductivity, respectively of suspensions of magnetic and in some cases also non-magnetic particles for a range of volume fractions up to the liquid-solid transition. Section VII describes how well these properties are retained over long periods. Section VIII is a quantitative discussion of how these material properties can be taken advantage of to reach the extreme parameter ranges required for MHD applications.
II. METHOD TO PRODUCE MAGNETIC LIQUID METALS

We used several liquid metals as base liquids for the creation of MLM suspensions. The main one used in this study was eGaIn which is an eutectic alloy of gallium and indium \cite{22} at the weight ratio 77/23 (melting point $T_{\text{melt}} = 15^\circ\text{C}$, density $\rho = 6250$ kg/m$^3$, surface tension $\gamma = 624$ mN/m \cite{23}, electrical conductivity $\sigma = 3.40 \cdot 10^6$ S/m \cite{24}). The two metals were mixed at 35$^\circ\text{C}$ and covered with a solution of hydrochloric acid (HCl), which cleans off and prevents oxidation \cite{16}. Despite the fact that indium is a solid at this temperature, the alloying of gallium indium is so favorable that it combines with liquid Gallium into the liquid alloy with stirring by a glass rod. Pure gallium ($T_{\text{melt}} = 29.7^\circ\text{C}$, $\rho = 6095$ kg/m$^3$, $\sigma = 3.7 \cdot 10^6$ S/m) and a eutectic alloy of gallium, indium and tin (weight ratio 68.5/21.5/10 respectively, $T_{\text{melt}} = -19^\circ\text{C}$, $\rho = 6440$ kg/m$^3$, $\sigma = 3.46 \cdot 10^6$ S/m) have also been used as base liquids. The gallium, indium and the eutectic alloy of gallium, indium and tin were purchased from Gallium Source and each have 99.99% purity.

When liquid metals are exposed to air, a thin solid oxide layer forms at the surface that appears dirty and dull (Fig. 1g), while the inside remains pure non-oxidized liquid metal protected from air. This oxidized liquid metal wets non-metallic surfaces and does not wet to metals or metal oxides \cite{16}. Indeed, we found that oxidized iron particles which were mixed with eGaIn did not suspend into the bulk – even with stirring vigorous enough for the particles to break the oxide skin on the liquid metal – and instead stuck to the oxide skin at the surface in equilibrium. This is true whether or not the eGaIn was recently washed in HCl beforehand so that the surface appeared shiny and conductive as in Fig. 1a, or if the eGaIn was highly oxidized as in Fig. 1g. The inability to wet in equilibrium suggests that the high interfacial tension between liquid metal and oxidized metal particles is a barrier to suspending particles in liquid metals. For a liquid to wet a solid, a rule of thumb is that the liquid should typically be less polarizable than the solid surface, so that the liquid-solid van der Waals attraction is stronger than the liquid-liquid attraction \cite{24, 25}. Thus, we propose that using a flux to remove the less-conductive oxide layer ($\sigma = 10^3$ S/m) from the iron particles to make the surface more conductive ($\sigma = 1.04 \cdot 10^6$ S/m) and thus more polarizable could enable eGaIn ($\sigma = 3.40 \cdot 10^6$ S/m) to wet the particles (much like soldering) and allow them to suspend. We use an acid solution as the flux, as in a pickling process \cite{26, 27}. Additionally, the acid can remove and prevent oxidation of the liquid metal to prevent a yield stress, allowing the liquid metal to flow like a simple liquid and form into a shape with a minimal surface area \cite{16} (Fig. 1a and Movie 1 \cite{28}).

The MLM were made by mixing the liquid metal (typically 2 mL) with varying volume fractions $\phi$ of metallic particles and a HCl solution at room temperature. Enough HCl was used to completely cover the metals so it cleaned off any oxidation and prevented further contact between the metals and air (typically 10 mL HCl for 2 mL of liquid metal). The mixing process is shown in Movie 2 \cite{28} for iron particles ($\rho = 7874$ kg/m$^3$) with mean diameter 29 $\mu$m (the median 90% range for particle diameters is 18-40 $\mu$m, and there are particles as small as 1 $\mu$m and as large as 219 $\mu$m) suspended in eGaIn at volume fraction $\phi = 10\%$ in a HCl solution with pH = 0.9. Particles that came into contact with the liquid metal absorbed and suspended into the bulk within a few seconds of contact. Contact could be achieved by initially placing the particles on top of the eGaIn before adding

![Fig. 1. Various phenomena observed in a suspension of 29 $\mu$m diameter iron particles in eGaIn, at values of volume fractions $\phi$ and applied constant inhomogeneous magnetic fields with peak magnitude $B$ given in the panels. (a) eGaIn ($\phi = 0$). (b) A suspension at $\phi = 20\%$, which appeared similar to the pure eGaIn. (c) A yield stress appeared for $\phi$ above the liquid-solid transition $\phi_c = 40.5\%$. (d) The Rosensweig instability (e) The magnetorheological effect. (f) The combined effects of panels d and e. The samples in panels a-f were rinsed with HCl to remove oxidation shortly before taking the pictures, and small amounts of remaining HCl are visible in some of the pictures. The dashed line between panels separates liquid and solid states (i.e. those with zero and non-zero yield stress). Liquid metal states appear shiny because they are conductive and can have smooth surfaces with minimal surface areas due to the surface tension of liquid. Solid states appear rough and less shiny because the particles poke through the liquid-air interface. They also have a yield stress that prevents them from flowing to obtain a minimal surface area. (g) A sample exposed to air without HCl, which oxidized, causing it to appear dirty and develop a yield stress. (h) A suspension stored for a a few weeks in HCl, after which samples tended to form a porous solid structure; the liquid state could be recovered by adding more HCl and shaking the sample.](image-url)
the HCl if the particles were big enough (≥ 1µm) to settle under gravity. Brownian particles (≤ 1µm) instead suspended into the HCl solution (appearing gray), in which case contact between the particles and liquid metal could be achieved by vigorous shaking or stirring of the solution for 30 minutes (after which the HCl solution became transparent).

A. Understanding the suspending process

To understand the role of particle oxidation, we can compare the standard experiment described in the previous paragraph with another in which instead initially oxidized iron particles were mixed with initially non-oxidized eGaIn, but before adding HCl. The eGaIn was rinsed in HCl immediately beforehand to clean off any oxidation, but the HCl was removed before adding the particles. Without HCl, the particles did not suspend into the bulk of the liquid metal, but instead tended to stick to the surface of the liquid metal. Once HCl was added and the oxidation removed [16], the particles absorbed into the bulk of the liquid metal (see Movie 3 [28]). This confirms that the oxidation must be removed from the particles by the flux for suspending to occur, in agreement with the hypothesis that higher conductivity non-oxidized iron surfaces (σ = 1.04 · 10^7 S/m) are easier to wet and suspend than iron oxide surfaces (σ = 10^3 S/m) [25].

The proposed relation between oxidation of the liquid metal and suspendability was tested by varying the pH of the HCl solution during the suspending process. For pH < 0.95 ± 0.05, the surface of the eGaIn appeared shiny, indicating an absence of an oxide layer, and the particles mixed into the bulk of the eGaIn to form a suspension. If instead the HCl solution had pH > 0.95 ± 0.05, the particles did not suspend into the bulk of the eGaIn even after sitting in contact with eGaIn in the acid bath for 24 hours or stirring the sample for 30 seconds. This critical pH value is consistent with Xu et al. [16], who observed that the oxide skin disappeared and wetting of eGaIn to metallic surfaces occurred only for pH ≤ 1 ± 0.15. Thus, at higher pH our eGaIn was oxidized, preventing it from wetting the particles. This confirms that oxidation removal from the liquid metal was also required to wet and thus suspend the particles into the liquid.

To remove oxidation from the particles in a humid atmosphere, the thermodynamically favored reaction is $Fe_2O_3 + 6HCl \rightarrow 2FeCl_3 + 3H_2O$, where the FeCl_3 precipitates into the solution [26]. Movies 1 and 3 [28] show respectively that enough oxidation removal from the liquid metal and particles happened in matter of seconds to allow the liquid metal to form a minimal surface and wet to non-oxidized metal surfaces [16].

Since the oxidation-removing reaction does not produce the gas bubbles observed in Movie 2 [28], another reaction must be going on as well. Once the oxidation is removed from the surface of the iron particles exposing the pure iron cores, a reaction that is expected between iron and HCl is

$$Fe + 2HCl \rightarrow FeCl_2 + H_2.$$  (1)

A flame test confirms that the gas bubbles released are H_2 gas. To test the consequence of this reaction, iron particles were placed in an HCl bath (initial pH = 0.69) and the pH was measured over time (Fig. 2). The error bars of 0.12 on pH represent the standard deviation of repetitions during calibration measurements. As the soaking time increased, the pH increased and the solution turned green, the characteristic color of FeCl_2, confirming Eq. 1. The bubble production was vigorous over a longer period of time in this experiment than when eGaIn was included in the suspending process, indicating the suspending of iron into eGaIn at least partially protected the iron from the HCl. If the iron particles were soaked in HCl for ≥ 2 · 10^4 s before contacting eGaIn, they no longer suspended in eGaIn and the pH increased slightly. Reducing the bath pH below the critical pH = 0.95 required initially for suspending did not enable these particles to suspend. This suggests that some consequence of the reaction other than the pH change prevented suspending. We hypothesize that the iron particle surfaces were converted to less conductive FeCl_2 (σ = 10^{-9} S/m) from the chemical reaction with HCl (Eq. 1), making them less conductive than eGaIn (σ = 3.40 · 10^6 S/m), thus preventing wetting and suspending. In summary, it appears the bubble producing chemical reaction between iron and HCl did not aid the suspending process, and hindered it.
if left to go on for several hours. Thus, suspending should occur if the eGaN, iron particles, and HCl are mixed in any order, as long as it does not take too long before the iron particles come in contact with the eGaN, and the HCl is in contact with the metals for a few seconds to remove any oxidation.

Now that we have a general understanding of the suspending process, we can explain why previous studies failed to suspend uncoated metallic particles into liquid metals [12–14], but could suspend particles with nonmetallic coatings into liquid metals [13–15]. The surfaces of the suspensions shown in those articles were not shiny, looking more like Fig. 1g, which is a clear indication of oxidation. The oxide layer prevented the liquid metal from wetting uncoated metal particles, but allowed it to wet nonmetals [16].

B. Robustness of the suspending process

To demonstrate the robustness of the suspending process for various liquid metal bases, the same 29 μm iron particles were also successfully suspended using the same process, but with the liquid eGaN replaced by the pure liquid gallium at 50°C (above its melting point of 29.7°C) or a eutectic alloy of gallium, indium and tin at room temperature. Using the same process, we also successfully suspended particles of various materials and sizes of particles (40 nm to 500 μm mean diameter) in eGaN, shown in Table I. Note that particles with diameter ≥ 1 μm tend to sediment in suspensions, and will not track fluid flow due to their inertia, features which may not be desirable in many applications. The table shows that particles with a higher conductivity σ than the liquid metal base (zinc, nickel, iron, and steel) were wetted and suspended into the bulk, while surfaces with lower σ (iron oxide, iron chloride, soda-lime glass, polystyrene, fused zirconia silica) were not wetted or suspended into the bulk. Titanium, nichrome and stainless steel surfaces were found to not be wetted, but we did not obtain particles of those materials to test whether they suspended. These observations confirm the proposal that the particles should be more conductive than the liquid metal to be wetted [25], and this is both a necessary and sufficient condition for suspending for the materials we tried.

C. Qualitative properties

Non-oxidized MLM (Fig. 1b) looked like pure liquid metal (Fig. 1a). It was shiny, indicating a conductive surface. The droplet flowed freely if its container was tilted, and the droplet would take a shape with minimal surface area at rest due to the high surface tension of the liquid, indicating a lack of a yield stress. In contrast, if the liquid metal surface was oxidized, it appeared less shiny and did not form a minimal surface (Fig. 1g).

When φ was increased above a critical volume fraction φc, corresponding to a liquid-solid transition, i.e. jamming transition [29] (φc = 40.5% for 29 μm diameter iron particles in eGaN), the particles became so densely packed that they poked through the liquid air-interface, making the surface appear rough or matte and less shiny, and resulting in a yield stress that allowed the sample to maintain shapes with non-minimal surface areas (Fig. 1c) [30].

Here we compare the magnetic properties of MLM to other ferrofluids and magnetorheological fluids, in which magnetic particles are usually suspended in oils rather than liquid metals. We exposed suspensions of 29 μm diameter iron particles in eGaIn to constant inhomogeneous magnetic fields with peak magnitude B at various volume fractions φ. For low φ and high B, MLM behaved as other ferrofluids; the surface deformed into sharp peaks that aligned with the magnetic field lines (Fig. 1d), a consequence of the Rosensweig instability [2]. For higher φ and lower B, the MLM exhibited the magnetorheological effect (Fig. 1e): a yield stress due to an induced dipole-dipole interaction between magnetic particles [31, 32]. For higher volume fraction samples at strong magnetic fields, the ferrofluid and magnetorheological effects could be observed at the same time (Fig. 1f). The yield stress fluid can still flow to deform under strong enough magnetic forcing, but the shape of the peaks is different than a Newtonian fluid because of the yield stress. The transition from a simple liquid to these magnetic states in response to introducing or removing a magnetic field happens in a fraction of a second and is reversible (Movie 4 [28]). All of these magnetic properties in MLM appear qualitatively similar to other ferrofluids and magnetorheological fluids.

III. MATERIALS USED FOR CHARACTERIZATION

To characterize the properties of MLM relevant to MHD, we report in the following sections measurements of the viscosity η, magnetic susceptibility χ, and conductivity σ of MLM. As an initial attempt to survey the parameter space of material properties, three series of suspensions with different ratios of magnetic and nonmagnetic particles were measured. In each case we used the same iron particles with mean diameter 29 μm used primarily for our suspending process. To tune the viscosity η independently of the magnetic properties, we additionally suspended zinc particles with mean diameter 8 μm (nominally 6-9 μm, ρ = 7140 kg/m³). These particles are highlighted in bold in Table I.

The first series, referred to as φFe, consists of iron particles suspended in eGaN at various volume fractions. The two other series have a constant volume fraction of iron particles (10% and 25%, respectively) and a variable volume fraction of zinc particles, respectively referred to as 10%Fe/(φ-10%)/Zn and 25%Fe/(φ-25%)/Zn. When re-
TABLE I. The suspending method was demonstrated for a variety of magnetic and non-magnetic metallic particles suspended in eGaIn, listed in the table. The suspensions are ordered by decreasing electrical conductivity $\sigma$, showing that particle materials with higher $\sigma$ than eGaIn ($\sigma = 3.40 \times 10^6$ S/m, horizontal line), were wetted and suspended, while particle materials with lower $\sigma$ were not wetted or suspended. The particles in bold were those used for quantitative measurements in this paper. References for material source and purity (%): $^{a}$ U.S. Nano (99.9), $^{b}$ Alfa Aesar (97.5), $^{c}$ Chemical Store (99), $^{d}$ Chemical Store (99.5), $^{e}$ Chemical Store (97.7), $^{f}$ Steve Spangler Science (99.5), $^{g}$ iron was oxidized to obtain an iron oxide surface, $^{h}$ iron was reacted with HCl to obtain an iron(II) chloride surface.

| Material          | Source             | Mean Diameter ($\mu$m) | Conductivity (S/m) | Wetted & Suspended |
|-------------------|--------------------|------------------------|--------------------|--------------------|
| Zinc              | (see caption)      | 0.100, 8, 500          | 1.69 x 10$^7$      | yes                |
| Nickel            | Chemical Store (99)| 175                    | 1.47 x 10$^7$      | yes                |
| Iron              | (see caption)      | 0.040, 0.100, 0.90, 8$^d$, 29$^d$, 45, 450$^d$ | 1.04 x 10$^7$      | yes                |
| Steel             | Chemical Store (99.4)| 175                    | 1.10$^f$           | yes                |
| Stainless Steel   | McMaster-Carr     | Plate                  | 1.36 x 10$^6$      | no                 |
| Titanium          | McMaster-Carr     | Plate                  | 2.40 x 10$^6$      | no                 |
| Nichrome          | VWR(99)           | Wire                   | 6.67 x 10$^5$      | no                 |
| Iron Oxide$^d$    | Chemical Store (99.5)| 29                     | 10$^5$             | no                 |
| Iron(II) Chloride$^b$ | Chemical Store (99.5)| 29                    | 10$^{-9}$          | no                 |
| Soda Lime glass   | Mo-Sci Corp.      | Wire                   | 10$^{-13}$         | no                 |
| Polystyrene       | Sigma-Aldrich      | 200                    | 10$^{-15}$         | no                 |
| fused Zirconia Silica | Mo-Sci Corp.    | 100                    | 10$^{-18}$         | no                 |

![Figure 3](image-url)  
**FIG. 3.** Schematic of the modified rheometer set up to measure the viscosity and non-Newtonian properties of liquid metals with a HCl bath or argon atmosphere.

results are plotted as a function of volume fraction $\phi$ in the following figures, we refer to $\phi$ as the total volume of all solid particle phases divided by the total volume of the sample. For example, for the series 25%Fe/($\phi$-25%)Zn, $\phi = 55\%$ means the volume fraction of iron particles is 25%, and the volume fraction of zinc particles is 30%.

IV. RHEOLOGY

We performed rheology measurements to determine the conditions under which the suspensions flow like Newtonian liquids, and to obtain the viscosity $\eta$, the main adjustable material parameter in $Re$.

Rheology measurements were done using an Anton Paar MCR 302 rheometer in a modified parallel plate geometry [16]. A cross-section of the cylindrical geometry is shown in Fig. 3. The suspension was placed in the gap between parallel plates of width $d = 2 \pm 0.001$ mm, where the bottom plate is titanium, and the top plate ($D = 15.99 \pm 0.02$ mm) is acrylic. Neither surface was corroded or wetted by gallium, eGaIn or the suspensions [16]. The suspension extended beyond the outer edges of the top plate (which is unconventional for parallel plate rheology) and was contained in an acrylic cup (diameter 25.10 $\pm$ 0.05 mm, height 50 mm) to prevent spillage (a concern for the non-wetting liquids and large centrifugal forces). This containment caused the suspension to stick out above the top plate level by about 2 mm, as shown in Fig. 3. The cup also allowed the suspension to be completely covered with a hydrochloric acid (HCl) solution, filled up to 5±1 mm above the level of the bottom plate to completely cover and prevent oxidation of the liquid metal, which is known to greatly increase the apparent yield stress measured in a rheometer [16]. The temperature was maintained at 20.00 ± 0.01°C by a Peltier element underneath the thermally conductive titanium.

The torque $T$ on the tool attached to the top plate was measured while that tool was controlled to rotate at constant angular velocity $\omega$. The mean shear stress was calculated as $\tau = 16T/\pi D^2$ and the mean shear rate at the edge of the plate was calculated as $\dot{\gamma} = D\omega/2d$, which would correspond to the local field values for a Newtonian fluid in laminar flow in a traditional parallel plate geometry. Since our measurements do not satisfy these assumptions, these reported $\tau$ and $\dot{\gamma}$ serve more as approximate reference scales and do not necessarily correspond to local field values.

The shear stress $\tau$ is shown as a function of shear rate $\dot{\gamma}$ in Fig. 4 for suspensions of iron particles in eGaIn (se-
gies $\phi Fe$), for different volume fractions $\phi$. Each curve is the average of three cycles composed of increasing then decreasing logarithmic ramps from $\dot{\gamma} = 1$ to $1000$ s$^{-1}$ with a ramp duration of 60 minutes per decade of $\dot{\gamma}$, preceded by a pre-shear at $\dot{\gamma} = 1$ s$^{-1}$ for 60 seconds. The reproducibility of the curves on the repeated cycles confirmed that this pre-shear was enough to eliminate any effects of loading history. The increasing and decreasing ramps did not show any systematic difference (i.e., apparent hysteresis) for liquid states ($\phi < 40.5\%$ for series $\phi Fe$), indicating that this ramp rate was slow enough to achieve steady state. Each sample exhibited an apparent yield stress, corresponding to the plateau in the limit of small $\dot{\gamma}$, and a non-linear increase in $\tau(\dot{\gamma})$ from which we obtain the viscosity $\eta$ using the methods explained in Sec. IV B.

A. Yield Stress

For the series $\phi Fe$, samples at $\phi < 40.5\%$ were observed to flow under the effect of gravity, form into shapes with minimal surfaces, and were shiny (as seen in Fig. 1b), characteristics of a liquid. In contrast, samples at $\phi > 40.5\%$ were observed to retain their shapes instead of flow under gravity (a consequence of their yield stress), and their surface appeared rough or matte due to the particles poking through the liquid-air interface (as seen in Fig. 1c). Some of the samples at $\phi > 40.5\%$ fractured underneath the tool during measurements, spilling out of the region beneath the plate and causing a systematic decrease of $\tau_y$ on successive ramps. Since these observations are all indicative of a liquid-solid transition, we define it as $\phi_c = 40.5\% \pm 0.5\%$ for the series $\phi Fe$, where the error represents the difference between $\phi_c$ and the $\phi$ of the nearest measurement point.

The yield stress $\tau_y$ was measured as the average stress $\tau$ over the ramps in the range $\dot{\gamma} < 5$ s$^{-1}$ in Fig. 4. The yield stress $\tau_y$ is plotted as a function of the volume fraction $\phi$ in Fig. 5. The error bars in Fig. 5 were measured as the standard deviation of $\tau$ values used to obtain $\tau_y$. Figure 5 reveals two different scaling regimes of $\tau_y$, with a sharp increase near $\phi_c$. Fitting the data in each regime by an exponential function with percentage errors as shown in Fig. 5 yields an intersection which is within 1.5% of $\phi_c$. This agreement suggests the sharp increase in yield stress is a result of the liquid-solid transition $[30]$. The small apparent yield stress $\tau_y$ observed in Fig. 4 for suspensions at $\phi < \phi_c$ is at first glance inconsistent with the conclusion that these states are liquid, since $\tau_y$ should be zero for a liquid. During these experiments, we observed that bubbles appeared at the suspension-acrylic interface, which may be H$_2$ gas as a result of a reaction between iron and HCl (Eq. 1). We note that the $\phi = 0$ suspension, which has no iron particles in it, had no resolvable yield stress $\tau_y$ (the measured value is below the rheometer resolution of $6.2 \times 10^{-2}$ Pa), confirming that the iron particles are needed to produce the apparent yield stress $\tau_y$. If gas bubbles formed in the sample, they could get stuck in between particles or the gap between the plates, which is comparable to the capillary length, which would resist flow with an apparent yield stress $\tau_y$. Similar trends of increasing apparent yield stress in $\phi$ up to $\phi_c$ due to increasing volumes of trapped bubbles in suspensions have been observed before $[30]$. To test whether the bubbles were responsible for the apparent yield stress $\tau_y$, we performed an experiment under an argon atmosphere in the flow chamber instead of the HCl bath, which still prevented oxidation of the liquid metal but did not produce any bubbles. As experiments under
where \( \text{Re} \) is the Reynolds number. As all the parameters other than \( \text{Re} \) are known for pure eGaIn (\( \eta = 1.86 \times 10^{-3} \text{ Pa·s} \)), \( \text{Re}_c \) was obtained by fitting Eq. 2 to the averaged ramps shown in Fig. 4 for pure eGaIn (\( \phi = 0 \)). By tuning the volume fraction of non-magnetic particles at fixed volume fraction of 10% iron particles (series 10%Fe/(\( \phi-10\% \))Zn), \( \eta \) was increased by a factor up to 160 without changing magnetic susceptibility \( \chi \).

Once \( \text{Re}_c \) was obtained from the calibration with pure eGaIn, then fits of Eq. 2 to data from Fig. 4 with \( \text{Re}_c \) fixed and \( \eta \) as a free parameter were used to obtain the viscosity \( \eta \) for suspensions. As this method relies on an empirical scaling in which we can only confirm the same scaling function holds for a range of Re where we fit for pure eGaIn, we only fit suspension data to the same range of Re (13.7 < \( \text{Re} \) < 13700). The corresponding fits of Eq. 2 to the averaged ramps shown in Fig. 4 are shown in Fig. 4 for each \( \phi < \phi_c \). With an average input error on the stress equal to the 39% standard deviation of the ramps. From this we obtain \( \text{Re}_c = 4.0 \pm 0.2 \) with a reduced chi-squared of about 1.

FIG. 6. Viscosity \( \eta \) of suspensions of various mixtures of particles in eGaIn (see key) as a function of volume fraction \( \phi \). Horizontal dashed line: \( \eta \) for pure eGaIn (\( \phi = 0 \)). By tuning the volume fraction of non-magnetic particles at fixed volume fraction of 10% iron particles (series 10%Fe/(\( \phi-10\% \))Zn), \( \eta \) was increased by a factor up to 160 without changing magnetic susceptibility \( \chi \).

B. Viscosity

Traditionally, the viscosity of suspensions would be obtained from a range where the shear stress \( \tau \) is proportional to the shear rate \( \dot{\gamma} \) in a laminar, or low Reynolds number flow. However, this flow regime where this scaling occurs is not directly accessible for liquid metals in a rheometer measurement due to the low viscosity and the high apparent yield stress \( \tau_y \). For instance, a yield stress occurring is not directly accessible for liquid metals in a flow chamber with dimensions large compared to the capillary length. Figure 1b already shows an example of this: the suspension trapping advantage of a hydrodynamic similarity scaling, in which the dimensionless variable \( \tau/\eta \dot{\gamma} \) is independent of \( \phi < \phi_c \). With an average input error on the stress equal to the 39% standard deviation of the ramps. From this we obtain \( \text{Re}_c = 4.0 \pm 0.2 \) with a reduced chi-squared of about 1.

The resulting values of \( \eta \) are shown in Fig. 6 for different volume fraction \( \phi \). The errors plotted are output errors of the fits of Eq. 2, which had an average of 20% for the suspensions. The trend of increasing \( \eta \) with \( \phi \) is typical of suspensions, although the increase does not achieve the divergence at \( \phi_c \) of idealized theory [35], as in practice this divergence tends to be cut off. The viscosity of the suspensions of iron in eGaIn increased up to 22 times higher than eGaIn at \( \phi = 40\% \), the maximum \( \phi \) we measured before the liquid-solid transition.

Since the viscosities of our suspensions are higher than eGaIn for which this technique was developed [16], we
also checked whether we could obtain viscosity values from a linear increase in stress with shear rate as is traditionally done for a low-Re flow. However, in the relevant range $Re_c < 4$, our measurements are always dominated by the apparent yield stress $\tau_y$ such that $\tau$ is within 8% of $\tau_y$ even at the highest viscosities reported in Fig. 6, so there is still no significant range to fit the viscosity to low-Re data [16].

C. Tuning the viscosity with non-magnetic particles

While the suspensions of iron particles in eGaIn exhibited a significant increase in viscosity $\eta$ on their own, $\eta$ can be tuned independently from the magnetic susceptibility $\chi$ by adding non-magnetic particles in addition to the magnetic particles already in the MLM suspension. We added zinc particles to fixed volume fractions of iron in each of the two series $10\%Fe/(\phi-10\%)Zn$ and $25\%Fe/(\phi-25\%)Zn$ as defined in Sec. III. For each of these series we measured stress $\tau$ vs. shear rate $\dot{\gamma}$ as in Fig. 4 (not shown for brevity). The corresponding yield stresses $\tau_y$ are shown in Fig. 5. The liquid-solid transition was $\phi_c = 38.5 \pm 0.5\%$ for series $10\%Fe/(\phi-10\%)Zn$, and $\phi_c = 54.8 \pm 0.2\%$ for series $25\%Fe/(\phi-25\%)Zn$, determined based on observation of the qualitative properties described in Sec. IV B. In each series, exponential functions were fit to $\tau_y(\phi)$ for each of the liquid and solid ranges, which intersected within 1.5% of $\phi_c$. We plot $\eta$ in Fig. 6 as a function of volume fraction $\phi$ up to the respective liquid-solid transition $\phi_c$ for each series. In general this indicates a range of parameter space in which $\eta$ can be varied. Of particular importance is the maximum range we could tune the viscosity $\eta$ by adding zinc particles for a fixed volume fraction of iron particles (so that $\chi$ remains constant). The maximum range we obtained was for the series $10\%Fe/(\phi-10\%)Zn$ where $\eta$ increased up to a factor of 160 before $\phi_c$ was reached.

D. Magnetorheological effect

The magnetorheological (MR) effect results in a yield stress due to an applied magnetic field $B$, as visualized for example in Fig. 1e. If the MR effect is strong enough, it could in principle produce a yield stress as a result of a self-generated magnetic field from a dynamo. To show an upper bound on the expected MR effect, we used a suspension with $\phi = 39\%$ iron particles in eGaIn (series $\phi Fe$), the maximum volume fraction of magnetic particles we could obtain in a liquid state. The suspension was placed in a magnetorheological cell (Anton Paar 1-Tesla Magneto-Rheological Device) with a parallel plate rheometer geometry, and a magnetic field $B$ was applied in the direction of the rheometer tool axis. The sample was sheared at a constant rate $\dot{\gamma} = 1 \text{ s}^{-1}$ (low enough that the total shear stress was dominated by the yield stress as in Fig. 4) while the magnetic field $B$ was changed quasistatically in a series of ramps of increasing then decreasing $B$. After the initial ramp, $\tau(B)$ did not exhibit any hysteresis. This approximation of a yield stress is shown as a function of the applied magnetic field $B$ in Fig. 7 for one of the later ramps.

For magnetic fields $B < 10^{-1}$ T, the shear stress leveled off at a value 2.5 orders of magnitude higher than what was measured in the parallel plate setup Fig. 3. This can be explained by the fact that when nominally $B = 0$ during the ramps, the MR cell still attracted small steel pins, indicating a remnant magnetization of the cell. If we instead demagnetized the cell before loading the suspensions, and measured at $B = 0$ before ramping $B$ up, the apparent yield stress was much lower, although still 70% higher than the value in Fig. 4. Thus, the plateau value of the apparent yield stress at low $B$ in Fig. 7 is a result of the remnant magnetization of the MR cell, and not an inherent property of the suspension.

For magnetic field $B > 10^{-1}$ T, the apparent yield stress increased with the applied magnetic field. We fit a power law with exponent 2 – typical of MR behavior [36] – to the data for $\tau > 1.46 \cdot 10^{-3}$ Pa in Fig. 7. While the MR effect could in principle modify MHD experiments, this effect remained weak at low magnetic field values. In Sec. VIII, we give calculations showing how this would compare to the hydrodynamic shear stress in potential MLM dynamo experiments.

V. MAGNETIC SUSCEPTIBILITY

We measured the magnetic susceptibility $\chi$ using a gradiometer [37]. It consists of two pairs of concentric inductor coils. Suspensions were placed in cylindrical containers of various aspect ratios (defined as length/diameter), and inserted inside one of the inner coils. An alternat-
ever, in detail, the uncertainty and a 2.5% standard deviation of repetitions were reported in detail in [39]. As an example to indicate the ratio of the particles [38]. These dependencies will be consistent within the run-to-run variation of the values as a function of volume fraction φ, for cylindrical samples with aspect ratios given in the key. The horizontal dashed line represents the nominal conductivity of eGaIn (σ = 3.40 × 10^6 S/m) [23], which are consistent within the 7% systematic error on following measurements is only 1.1%. The conductivity is then given by $\sigma = IL/\pi r^2U$. We confirmed the measured conductivity was independent of the applied current over the range from 80 to 105 mA with a ±10^-3 mA systematic error, which we averaged over to obtain the mean conductivity $\sigma$. The main source of error is the voltage measurement with a systematic error of 1 μV on typical measurements of 14 to 25 μV. To test for potential errors from particle sedimentation, the samples were manually shaken at a frequency of about 2 Hz with an amplitude of 15 cm during the measurements, but by comparison to stationary samples we found the shaking had no significant effect on the measurement.

Each cell was first used to measure the conductivity $\sigma$ of pure eGaIn. The values measured were within 1.1% of the nominal conductivity of eGaIn ($\sigma = 3.40 \times 10^6$ S/m) [23], which are consistent within the 7% systematic error on the voltage measurement. This calibration implies the systematic error on following measurements is only 1.1%.

FIG. 9. Electrical conductivity $\sigma$ as a function of volume fraction $\phi$ for different mixtures of particles in eGaIn indicated in the key. The horizontal dashed line represents the conductivity of the pure liquid metal ($\sigma = 3.40 \times 10^6$ S/m). Solid curve: Meredith & Tobias model [42] for iron particles in eGaIn ($\phi Fe$). The conductivity $\sigma$ only increased over that of pure eGaIn by no more than 42% for the series $25%Fe/(\phi - 25%)Zn$. This means $\chi$ will the main tunable parameter in $R_m$.

VI. CONDUCTIVITY

We measured the electrical conductivity $\sigma$ of suspensions using the Kelvin sensor method [41]. Suspensions were first cleaned with HCl, then the HCl was removed before the suspensions were placed in an acrylic tube with two corrosion-resistant steel electrodes. A different cell was used for each sample series, with radius $r = 3.55 \pm 0.01$ mm, and length between the electrodes $L = 45$ with a 2 mm variation between the cells. A direct current $I$ was applied through the length of the sample, while a voltmeter measured the voltage $U$ across the length of the sample with a second pair of electrodes. The conductivity is then given by $\sigma = IL/\pi r^2U$. We confirmed the measured conductivity was independent of the applied current over the range from 80 to 105 mA with a ±10^-3 mA systematic error, which we averaged over to obtain the mean conductivity $\sigma$. The main source of error is the voltage measurement with a systematic error of 1 μV on typical measurements of 14 to 25 μV. To test for potential errors from particle sedimentation, the samples were manually shaken at a frequency of about 2 Hz with an amplitude of 15 cm during the measurements, but by comparison to stationary samples we found the shaking had no significant effect on the measurement.

One sample of each series $10%Fe/(\phi - 10%)Zn$ and $25%Fe/(\phi - 25%)Zn$ was measured and were found to have $\chi$ consistent within the run-to-run variation of the values of series $\phi Fe$ with respectively $\phi = 10%$ and $\phi = 25%$ iron. This confirms that $\chi$ is unaffected by the volume fraction of zinc as long as the volume fraction of iron remains fixed.

FIG. 8. Magnetic susceptibility $\chi$ of suspensions of iron particles in eGaIn (series $\phi Fe$) as a function of volume fraction $\phi$, for cylindrical samples with aspect ratios given in the key. By tuning the volume fraction $\phi$ of magnetic particles, $R_m \propto 1 + \chi$ could increase by a factor up to 5.0 relative to pure eGaIn.
measurements. The conductivity $\sigma$ increased by 13% over that of eGaIn for the pure iron series $\phi$Fe, by 25% for 10%Fe/($\phi$-10%)Zn, and by 42% for 25%Fe/($\phi$-25%)Zn. This confirms that the high conductivity of the liquid is preserved in the suspensions, and increased in the direction of the higher conductivity particles that were added ($\sigma = 1.04 \times 10^7$ S/m for iron and $\sigma = 1.69 \times 10^7$ S/m for zinc). However, the increase is not as strong as in a simple mixture rule, for comparison. This increase is also low compared to the model for suspensions by Meredith and Tobias [42], shown in Fig. 9. This model was previously confirmed numerically over the conductivity range of our materials within a scatter of 10% [43]. Our measured conductivity is systematically lower than the predicted values by up to 35% in our parameter range, which suggests there might be some opportunity to further improve the conductivity of MLM with different surface treatments.

The measured small increase of the electrical conductivity $\sigma$ of no more than 42% for series 25%Fe/($\phi$-25%)Zn compared to the factor of 5.0 increase obtained for $1 + \chi$ with increasing volume fraction $\phi$ means the primary way to tune $Re_m$ will be to tune $\chi$ via the volume fraction of magnetic particles.

VII. RETENTION OF PROPERTIES OVER TIME

To determine how long the samples can retain their properties under conditions similar to potential MHD experiments, we stored MLM in HCl and tracked their properties over time. The pH of a suspension of $\phi = 30\%$ iron in eGaIn is shown in Fig. 2. The pH remained constant within 11% of the initial pH over 28 days, and the solution remained clear, indicating a lack of FeCl$_2$ formation. This indicates that suspending the iron particles in eGaIn provides some protection against the chemical reaction between iron and HCl (Eq. 1). When MLM were stored in HCl over several weeks without being stirred, the gas pressure in storage containers increased, and the MLM volume expanded with containers increased, and the MLM volume expanded with an apparently porous structure shown in Fig. 1h. The MLM also developed a weak yield stress such that the sample would not flow when the container was tilted. The tendency for this to occur was stronger with more iron in suspension. The pressure and porous structure are possibly due to the production of H$_2$ gas from the reaction of Eq. 1, while the solidification may be the result of oxidation. If more HCl was added to lower the pH, and the sample was shaken, the MLM returned to a liquid state and its original volume.

For a suspension of $\phi = 30\%$ iron particles in eGaIn that form these solid porous structures after 39 days of storage in HCl, adding HCl and shaking allowed the suspension to recover its original viscosity $\eta$, susceptibility $\chi$, and conductivity $\sigma$ within our resolution (20%, 2.5%, and 2.5%, respectively). After 5 months of storage, the MLM still recovered their original $\eta$ and $\sigma$. However, we observed a 6% decrease of $\chi_{eff}$ from its original $\chi_{eff}$ (larger than the 2.5% run-to-run variation). After 20 months, some samples formed white deposits (possibly due to the formation of FeCl$_2$), and some others rusted. Of those that could be returned to a liquid state, $\chi_{eff}$ was reduced by 80% compared to its original $\chi_{eff}$. Thus, none of our samples were recoverable after 20 months.

While working with MLM, we frequently ran into situations where the MLM would become oxidized due to exposure to air, as seen in Fig. 1g, for example when transferring samples between containers. If these oxidized MLM were mixed with HCl, the samples returned to a shiny liquid state, with viscosity $\eta$, susceptibility $\chi$, and conductivity $\sigma$ within resolution of their original values. If the samples were exposed to air for longer periods (up to 1 week), the process of cleaning with HCl took longer, and in some cases we had to change the HCl solution multiple times to return the MLM to a liquid state.

VIII. DISCUSSION AND CONCLUSIONS

In summary, we demonstrate how to make a novel class of materials: magnetic liquid metal (MLM), with high electrical conductivity $\sigma$ and magnetic susceptibility $\chi$, by suspending magnetic particles in liquid metal. The suspending process is general enough to apply to a wide range of particle materials and diameters from 40 nm to 500 µm (Table I), as well as three different liquid metal bases, and volume fractions $\phi$ up to the liquid-solid transition (e.g. $\phi_e = 40.5\%$ for iron particles in eGaIn). The suspending method uses a HCl solution as a flux to eliminate oxidation from both the metal particles and liquid, which allows the liquid metal to wet the particles as long as the particles have higher conductivity $\sigma$ than the liquid. The suspending method was designed to be easily reproducible in other laboratories as it does not require significant experience in any techniques, and the materials are easily purchased, relatively safe, and can be used at room temperature.

The magnetic susceptibility $\chi$ can be increased by suspending magnetic particles at different volume fractions $\phi$. MHD effects relating to the advection or generation of magnetic fields by fluid flow depend on $Re_m \propto \sigma(1 + \chi)$ which was increased by up to a factor of 5.6 compared to the pure liquid metal; for series $\phi$Fe, $1 + \chi$ increased by 5.0 (Fig. 8) and $\sigma$ increased by 13% ($\sigma = 3.9 \cdot 10^6$ S/m) at $\phi$ just below $\phi_e$ (Fig. 9). This is enough to reach a 2.0 times higher $Re_m$ in eGain-based MLM than liquid sodium ($\sigma = 9.6 \cdot 10^6$ S/m at a temperature $T = 120^\circ$C [10]) at the same values of $U$ and $L$. Furthermore, if these suspending techniques can be applied to liquid sodium, the material properties achieved should allow MHD experiments to reach $Re_m$ about 5 times higher than previous experiments, or alternatively shrinking the volume of the experiment by a factor of $5^4$, which would signifi-
above suspension parameters and controlling flow velocity in the range $U = 15$ m/s and $L = 0.1$ m. Region outlined in black: parameter range accessible with the above suspension parameters and controlling flow velocity in the range $U \leq 15$ m/s. Region outlined in red: parameter range accessible with the above suspension parameters and controlling $U \leq 15$ m/s for $L = 3$ m, corresponding to the size of the Maryland sodium facility [9]. Solid line: liquid sodium at $120^\circ$C, $U \leq 15$ m/s and $L = 3$ m [9]. Region outlined in green: parameter range proposed for plasma experiments [44]. Direct numerical simulations and plasma experiments are confined to the laminar regime below the dashed line ($Re \lesssim 2000$). For $Re_m \lesssim 1$ (dotted line), no significant MHD effects are expected. The arrows represent the direction that can be moved in the parameter space by tuning the corresponding labeled variable. MLM can be tuned to access both dimensions of the parameter space, spanning both turbulent and laminar regimes, and reaching a higher $Re_m$ than sodium for the same dimensions.

cantly reduce challenge and cost. To prevent sodium oxidation without causing an explosion, this would require a non-aqueous flux.

The viscosity $\eta$ can be increased independently of the magnetic susceptibility $\chi$ at a fixed volume fraction of magnetic particles by additionally suspending varying volume fractions of non-magnetic particles. By approaching the liquid-solid transition $\phi_c$, we were able to increase $\eta$ by factor of 160 for series $10\% Fe/\phi-10\% Zn$ (Fig. 6).

The parameter space in terms of $Re_m$ and $Re$ that could be achieved based on our measured range of $\chi, \sigma, \eta$, and $\rho$, and calculated $\rho$ based on the densities and volume fractions of materials is shown in Fig. 10. A modest experiment scale of $L = 0.1$ m and $U \leq 15$ m/s is large enough to reach $Re_m = 37$, above the threshold for a spontaneous dynamo ($Re_m = 30$)[5]. Fixed material properties (i.e., $\chi, \sigma, \eta, \rho$, and $\rho$) only allow movement along a diagonal line of slope 1 in the parameter space by varying $U$ or $L$, as is the case for liquid sodium at a temperature of $120^\circ$C shown in Fig. 10. On the other hand, the ability to independently control the material properties by suspending different particles allows access to both dimensions of the parameter space. The material properties of the fluid in MHD are typically characterized by the magnetic Prandtl number ($Pr_m = Re_m/Re$) which can only be varied slightly for pure liquids by changing temperature. With MLM, we achieved a range from $Pr_m = 1.6 \cdot 10^{-6}$ for pure eGaN, up to $Pr_m = 6.2 \cdot 10^{-4}$ (a factor of 440) just below the liquid-solid transition for series $25\% Fe/\phi-25\% Zn$.

The existing approaches to MHD cannot span the laminar-to-turbulent transition; liquid metal experiments are always turbulent, and direct numerical simulations and plasma experiments are confined to the laminar regime due to computational cost and flow instabilities, respectively. For example, the parameter range of proposed helium plasma experiments with temperature $T = 1.0 \cdot 10^4 - 5.6 \cdot 10^5$°C, $U \lesssim 10$ km/s and $L = 3$ m [44] are shown in Fig. 10. Figure 10 suggests that MLM could span could span from the turbulent to the laminar regimes of $Re$ as a result of the ability to increase the viscosity $\eta$. For example, $Re \approx 1600$ could be reached for the highest $Pr_m$ we found (corresponding to $\phi = 55\%$ for the series $25\% Fe/\phi-25\% Zn$) while still achieving $Re_m \geq 1$ (the minimum threshold for most MHD phenomena), assuming a fixed $\chi = 2.2$, $\rho = 6923$ kg/m$^3$, $\sigma = 4.9 \cdot 10^6$ S/m and $\eta = 0.2$ Pa-s. Thus, an experiment carefully designed to take advantage of this small available laminar parameter range in Fig. 10 would allow the first approach to MHD that could span between the turbulent and laminar regimes and connect to the parameter regime of direct numerical simulations.

A self-generated magnetic field in a dynamo could in principle generate a MR effect in MLM. If we extrapolate the fit of the data in Fig. 7 down to a magnetic field of $B = 4 \cdot 10^{-3}$ T (the value measured in the Cadarache dynamo [5]), the yield stress induced by the magnetic field would be $\tau_y \approx 0.7$ Pa, negligible compared to the hydrodynamic shear stress given by the latter term of Eq. 2 $\tau = (\eta^2 Re^{3/2})/(\rho L^2 Re_c^{1/2}) \approx 22$ Pa for the lowest stress experiments we propose, i.e., laminar MHD at $Re \approx 1600$, where $\eta = 0.2$ Pa-s, $\rho = 6923$ kg/m$^3$ and $L = 0.1$ m. Therefore, if the magnetic field is self-generated as in a Cadarache-type dynamo and not applied by an external source, it is expected that the samples will remain in a liquid state during the experiments without a significant MR effect.

The other aspect of MHD is the Lorentz force on fluid flow due to magnetic fields, which also increases with $\chi$. One source is a dynamo effect which creates an induced magnetic field which applies a Lorentz force on the induced current. While this feedback mechanism exists in astrophysical MHD, no laboratory experiment has reached this regime yet. This regime could be achieved if the ratio of Lorentz stress to inertial stress $N^* = 2\sigma(1+\chi)^2 H^2 L/f \rho U$ becomes comparable to one. We fix the parameters values $L = 0.1$ m, $f \approx 0.02$ as a typical value for a friction factor [45], and an induced magnetic field of $H = 3 \cdot 10^4$ A/m (the value obtained in
the Cadarache dynamo at the threshold $Re_m = 30$ [5]). Since $N^*$ decreases with $U$, and $Re_m$ increases with $U$, we can adjust $U$ to find the value of $N^*$ at which the minimum $Re_m = 30$ for a dynamo can still be obtained for different materials. We obtain $N^* = 0.07$ for liquid sodium ($\sigma = 9.6 \cdot 10^{-6} \text{S/m}$, $\rho = 927 \text{ kg/m}^3$), $N^* = 0.2$ for our suspensions of $\phi = 40\%$ iron in eGaIn (series $\phi Fe$, with $\chi = 4.0$, $\sigma = 3.9 \cdot 10^{-6} \text{S/m}$, $\rho = 6900 \text{ kg/m}^3$), and $N^* = 2$ for a hypothetical suspension of liquid sodium with $\phi = 40\%$ iron particles (assuming $\chi = 4$, $\sigma = 9.6 \cdot 10^{-6} \text{S/m}$, $\rho = 3700 \text{ kg/m}^3$). This suggests that MLM with eGaIn could have Lorentz forces with a noticeable effect on the flow, while Lorentz forces could potentially be dominant for MLM using sodium.

The tunable range of viscosity $\eta$, conductivity $\sigma$, and relative permeability $1 + \chi$ for the materials reported are expected to be typical of MLM, but with some opportunity for improvement. The independently tunable range of $\eta$ is expected to be insensitive to material, rather it depends on how far $\phi$ is from the liquid-solid transition $\phi_c$ [30, 35]. There is potential that $\eta$ could be increased beyond the factor of 160 we obtained; for example, a 3.5 decade increase of $\eta$ with $\phi$ has been achieved with non-MLM suspensions while remaining Newtonian [46]. Since our measured $\sigma$ is systematically lower than predicted values by up to 35% in our parameter range [42], there might be some opportunity to further improve the conductivity with different surface treatments. The increase in $\chi$ with magnetic particles was also predicted to be insensitive to the material as long as it is ferromagnetic [38], so we expect increases in $Re_m$ of order 1-10 for nearly spherical particles. It also remains to be seen if $\chi$ will retain the higher values achieved with large sample aspect ratios (Fig. 8) or attain the even larger values predicted for larger particle and sample aspect ratios [38] in a turbulent flow where the magnetic field is not uniform or aligned with the sample or particles. If so, extreme sample aspect ratios could be taken advantage of in specific experiments to achieve much higher $\chi$.

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