THE SPITZER EXTRAGALACTIC REPRESENTATIVE VOLUME SURVEY: THE ENVIRONMENTS OF HIGH-z SDSS QUASI-STEMellar OBJECTS

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ABSTRACT

This paper presents a study of the environments of SDSS quasi-stellar objects (QSOs) in the Spitzer Extragalactic Representative Volume Survey (SERVS). We concentrate on the high-redshift QSOs as these have not been studied in large numbers with data of this depth before. We use the IRAC 3.6–4.5 μm color of objects and ancillary r-band data to filter out as much foreground contamination as possible. This technique allows us to find a significant (>4σ) overdensity of galaxies around QSOs in a redshift bin centered on z ∼ 2.0 and an (>2σ) overdensity of galaxies around QSOs in a redshift bin centered on z ∼ 3.3. We compare our findings to the predictions of a semi-analytic galaxy formation model, based on the ACID MILLENNIUM simulation, and find for both redshift bins that the model predictions match well the source density we have measured from the SERVS data.

Key words: galaxies: clusters: general – galaxies: evolution – quasars: general

1. INTRODUCTION

The Spitzer Extragalactic Representative Volume Survey (SERVS; J.-C. Mauduit et al. 2011, in preparation) is a warm Spitzer survey at 3.6 and 4.5 μm which will cover an area of 18 deg2 in fields already extremely well studied and hence with a large amount of ancillary data. The survey reaches depths of ~1 μJy allowing L∗ galaxies to be observed out to z ∼ 5, thus making it ideal for studying the environments in which active galactic nuclei (AGNs) reside out to these epochs.

It is now widely accepted that high-luminosity AGNs harbor accreting supermassive black holes with masses of the order 109–1010 M⊙, implying that their host galaxies are among the most massive in existence at their respective epochs. Indeed, many studies have now shown that the most luminous types of AGNs preferentially reside within fields containing overdensities of galaxies (e.g., Hall & Green 1998; Best et al. 2003; Wold et al. 2003; Hutchings et al. 2009) as would be expected of the most massive galaxies at any epoch. These points support the idea that luminous AGN can be utilized as signposts to extreme regions of the dark matter density and thus the most massive dark matter halos (e.g., Pentericci et al. 2000; Ivison et al. 2000; Stevens et al. 2003) at high redshift. Combining this technique with large multiwavelength surveys, like the Sloan Digital Sky Survey (SDSS; Abazajian et al. 2009) which has identified more than 120,000 broadband quasi-stellar objects (QSOs) up to some of the highest measured redshifts (i.e., z = 6.4; Fan et al. 2003; Willott et al. 2003), has opened up a new era in AGN research.

Recently, the Spitzer Space Telescope has been at the forefront of this work due to its currently unique sensitivity to hot dust, which is an important component of most AGN unified theories (Antonucci 1993). It has also been utilized in the search for high-redshift galaxy clusters (e.g., Eisenhardt et al. 2008; Wilson et al. 2009; Papovich et al. 2010). Its wavelength range, particularly that of the Infrared Array Camera (IRAC; Fazio et al. 2004), provides the necessary extension needed to take cluster finding techniques to z > 1. Indeed, it has led to the highest known spectroscopically confirmed cluster to date (Papovich et al. 2010; Tanaka et al. 2010) at z = 1.62, found solely from an overdensity of IRAC sources in the XMM-LSS field of the Spitzer Wide-Area Infrared Extragalactic (SWIRE; Lonsdale et al. 2003) survey. Many of these methods make use of the color space that IRAC provides since it offers a useful way to select those galaxies that are most likely to be at high redshift. In addition, the negative k-correction caused by the 1.6 μm peak in stellar emission moving into the mid-infrared wave band means that IRAC can efficiently reach the depths required to study the high-redshift universe in technically achievable exposure times.

These features that have proved so useful for cluster finding are also very useful for the study of the environments of AGN at high-z. Recently, in Falder et al. (2010) overdensities were found at z ~ 1 in IRAC data around a large sample of SDSS QSOs and radio galaxies; it was also found that radio-loud AGNs reside in, on average, denser environments. The depth of these observations allowed for the detection of a ~0.7 L∗ galaxy at the redshift of the AGN (z ~ 1) and we could have detected an L∗ galaxy at z ~ 2. On the other hand, SERVS will allow the detection of L∗ galaxies at z ~ 5; see Figure 1. The main difference in the sample used by Falder et al. (2010) and the sample used in this paper is that SERVS is a blank field rather than a targeted survey. This means the sample of AGN is selected due to being in the survey region rather than based on other criteria related to the AGN. Hence, we will not have a sufficient number of powerful radio-loud AGNs to look for similar effects as seen in Falder et al. (2010) because these are...
in the universe for follow-up and have located high-redshift AGNs are extremely luminous and therefore detectable out to
their radio emission in large area radio surveys. Many authors have therefore used these signposts for high-density regions
and area that SERVS provides will allow us to see if luminous AGNs are found in overdensities at $z > 6$ with shallow wide surveys like the SDSS or by their radio emission in large area radio surveys. Many authors
have therefore used these signposts for high-density regions in the universe for follow-up and have located high-redshift
clusters and proto-clusters in observationally efficient ways (e.g., Pentericci et al. 2000; Stern et al. 2003; Venemans et al.
2007; Doherty et al. 2010; Galametz et al. 2010). At $z > 3$ only a handful of these proto-clusters have been detected to date,
mainly around individual radio galaxies (e.g., Overzier et al. 2006, 2008). Recently, in a study similar to this work Hatch et al.
(2011) have studied the environments of $z \sim 2.5$ AGNs in order to detect them at $z \sim 5$. This plot was made using the rest-frame $K$-band luminosity function of Cirasuolo et al. (2010) assuming no evolution past $z = 4$. All color conversions between bands are derived using a Bruzual & Charlot (2003) elliptical galaxy model with reddening of $E_{B-V} = 0.8$ applied according to the extinction law of Calzetti et al. (2000) and the HYPERZ software package (Bolzonella et al. 2000); this will be discussed at length in Section 4.2. The $k$-correction is calculated using this model from Bruzual & Charlot (2003) to place spectral energy distributions at various redshifts and comparing the rest-frame and observed-frame fluxes in the $K$-band filter.

The catalog we use is the SERVS data fusion catalog (M. Vaccari et al. 2011, in preparation). This matches the single-band SERVS IRAC 3.6 and 4.5 \( \mu m \) catalogs generated with the SExtractor software package (Bertin & Arnouts 1996), using a search radius of 1.0 arcsec, computes an average coordinate (for sources detected in both bands), and matches the resulting IRAC two-band catalog with ancillary photometric data sets from the far-ultraviolet to far-infrared wave band (e.g., GALEX, SDSS, CFHTCTIO/ESO/INT/KPNO/2MASS/UKIDSS/SWIRE) using a search radius of 1.5 arcsec. Since we will use the 3.6–4.5 \( \mu m \) color to select sources likely to be at the correct redshift, we therefore are, for the most part, restricted to using only those sources which are detected in both bands.

2. OBSERVATIONS AND SOURCE EXTRACTION

The primary observations used in this paper are those from the SERVS. This is a warm Spitzer survey using IRAC channels 1 and 2 (3.6 and 4.5 \( \mu m \), respectively). The data reach approximate 3\( \sigma \) depths of $\sim 1 \mu Jy$ (23.9 mag) at 3.6 \( \mu m \) and $\sim 2 \mu Jy$ (23.1 mag) at 4.5 \( \mu m \). Determining the depth of a large survey is non-trivial as the coverage is not uniform in depth due to the overlaps of the scan pattern. Small areas will therefore be deeper than the average, an important consideration when measuring source density. We therefore need to cut the catalog at a flux level which ensures equal depth throughout the maps.

Eventually, SERVS will cover 18 deg$^2$ of the extremely well studied fields from the SWIRE survey. In this paper, we make use of the SERVS overlap with the SDSS, thus restricting ourselves to the northern SERVS fields: Elais N1 (EN1) (1.01 deg$^2$ that overlaps the SDSS) and the Lockman Hole (4.93 deg$^2$). Full details of the fields, observations, and data reduction as well as the study of high-redshift clusters. Finding clusters beyond $z \sim 1.5$ is challenging and requires large, deep sky surveys; for example, Papovich et al. (2010) required all of the SWIRE survey (49 deg$^2$) to locate a $z = 1.62$ cluster. However, AGNs are extremely luminous and therefore detectable out to $z > 6$ with shallow wide surveys like the SDSS or by their radio emission in large area radio surveys. Many authors
have therefore used these signposts for high-density regions in the universe for follow-up and have located high-redshift
clusters and proto-clusters in observationally efficient ways (e.g., Pentericci et al. 2000; Stern et al. 2003; Venemans et al.
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mainly around individual radio galaxies (e.g., Overzier et al. 2006, 2008). Recently, in a study similar to this work Hatch et al.
(2011) have studied the environments of $z \sim 2.4$ radio galaxies. In their work they find potential proto-clusters around three of their six targets, with good evidence that the excess objects are blue star-forming galaxies. Furthermore, studying the environments of high-redshift AGNs may provide important constraints on the level of positive (e.g., Elbaz et al. 2009) or negative (e.g., Rawlings & Jarvis 2004) AGN-driven feedback on galaxies in the immediate environment of the AGN.

In this paper, we take advantage of the depth of SERVS to study the environments in which high-redshift QSOs reside. The layout of the paper is as follows: in Sections 2 and 3 we discuss the observations and the sample of QSOs, in Section 4 we describe our analysis, we present our results in Section 5 before comparing them to the previous work at $z \sim 1$ in Section 6 and to models in Section 7, we then finish with a summary in Section 8. Throughout the paper we have assumed a flat cosmology with $H_0 = 72$ km s$^{-1}$ Mpc$^{-1}$, $\Omega_m = 0.3$, and $\Omega_{\Lambda} = 0.7$. All magnitudes are quoted in the AB system unless explicitly stated otherwise.

![Figure 1](image-url). Limiting magnitudes in terms of $L_*$ vs. redshift for the INT $r$-band data (dashed line) as well as the SERVS 3.6\( \mu m \) and 4.5\( \mu m \) data (solid and dash-dot lines, respectively). Also shown for comparison is the SWIRE survey’s 3.6\( \mu m \) data (triple-dot-dash line) and the 3.6\( \mu m \) data used in Falder et al. (2010). Full details of the models used to construct this figure are given in the text.
3. SAMPLE

We identify QSOs in the SERVS regions by cross matching the SERVS source catalogs with the seventh data release of the SDSS quasar survey (Schneider et al. 2010) using the software package TOPCAT (Taylor 2005) to select the SDSS QSOs in the overlap regions. In total we find 46 QSOs in the SERVS northern fields; 5 in EN1 and 41 in the Lockman Hole. The small number in EN1 is due to the SDSS only overlapping a small portion of the observed region. These numbers include only QSOs that are at least 400 arcsec from the edges of the regions of equal coverage in both the ch1 and ch2 images. This allows us to study the environments out to these distances without any effects from the image edges. The distribution of the sample in the $L$–$z$ plane is shown in Figure 2. Six of the lower redshift QSOs are detected by the FIRST radio survey (Becker et al. 1995) at 1.4 GHz.

4. ANALYSIS

4.1. Radial Search Stacking

To study the QSO environments we have employed the relatively simple technique used in Best et al. (2003) and Falder et al. (2010). This involves placing a series of concentric annuli around each QSO and counting the number of sources that meet our selection criteria, described in more detail later in Section 4.2. We can then plot the source density as a function of radial distance for each QSO. The annuli are kept to a fixed area as the radial distance increases to keep the Poisson noise at a similar level from bin to bin. The QSOs themselves are excluded from the search because including them would bias the first annulus; this is done by not counting any sources within 1 arcsec of the QSO’s SDSS coordinates.

4.2. Galaxy Colors

In order to increase our sensitivity to galaxies at the same redshifts as the QSOs we have made use of the IRAC 3.6–4.5 $\mu$m color (i.e., ch1–ch2). To help decide on the correct color cuts we have made use of the HYPERZ software package (Bolzonella et al. 2000) and the stellar synthesis models of Bruzual & Charlot (2003). In the left panel of Figure 1 we show the color of six commonly used models versus redshift. These are a single burst model, four exponentially decreasing star formation rate (SFR) models with timescales $\tau = 1, 2, 3,$ and 15 Gyr designed to represent elliptical, S0, Sa, and Sc type galaxies, respectively, and a model with a constant SFR (Im). What is clear from Figure 3 is that with the exception of the burst model all the models produce a very similar 3.6–4.5 $\mu$m color; at most the

As we will be comparing our findings in this work to those from Falder et al. (2010) at $z \sim 1$ we aim to conduct the analysis in a similar way. In that work, two overdensities were reported, a sharp peak in the central source density within 300 kpc of the AGN and then a lower level overdensity extending out to at least 700 kpc. This pattern has also been seen elsewhere in the literature, for example, in Best et al. (2003) around powerful radio sources at $z \sim 1.6$ and by Serber et al. (2006) for SDSS QSOs. When we look for overdensities within 300 kpc in this sample, while many AGNs appear to have an overdense first annulus, they lack a significant detection. This is probably due to having far fewer targets in the sample. The sample used in Falder et al. (2010) contained a much larger number of AGNs (~170) than are present in any of our redshift bins or indeed the whole sample. Falder et al. (2010) also found that it was not possible to detect the 300 kpc scale overdensity with fewer than ~40 randomly chosen AGN, suggesting that the central peak in source density is a harder signal to detect than the larger scale overdensity.

To allow for easy comparison we use annular bins with a first bin physical radius of 700 kpc to match the largest search radius possible in the Falder et al. (2010) data, which was in turn fixed by IRAC’s field of view. To take into account the change in scale between different redshifts we adjust the angular bin sizes for each QSO based on its redshift. This means the bins are matched in terms of their physical size, where the radius of the first annulus is 700 kpc at the redshift of the QSOs.

To achieve a statistical result we will stack together the source density of the QSOs in two coarse redshift bins using the raw number counts. To ensure we are comparing like with like in the stacking analysis we adjust the flux range studied for each QSO to match the range in luminosity at the QSO’s redshift. This is done in each redshift bin by calculating what absolute magnitude the survey flux limit represents at the highest redshift in that bin, and then adjusting the flux cut to ensure this is matched for each of the other QSOs in that bin. As an upper limit we work out what flux a 10 $L^*$ galaxy would have at the maximum redshift of the redshift bin and apply an upper cut on sources with fluxes greater than this limit. The reason for choosing 10 $L^*$ is to ensure we are not cutting any likely associated galaxies, allowing for the significant uncertainty in the luminosity function at these high redshifts.

The reasoning for adopting this method of analysis is that at these high redshifts other methods such as $B_{\text{eq}}$ and two point correlation functions are difficult to calibrate correctly. The large error bars that result from the assumptions made about the luminosity function and $k$-correction at these redshifts make attaining a statistical result difficult.
burst model differs by only 0.15 mag. In the right panel we show the effect that reddening has on the 3.6–4.5 μm color; this is shown for the elliptical model without reddening along with two models with $A_v = 0.8$ and 1.6, added according to the Calzetti et al. (2000) reddening law. This plot shows that adding a reasonable amount of reddening can have a bigger effect on this color space at high-$z$ than the choice of star formation (SF) history. In all cases we have assumed a formation redshift for the models of $z = 10$. Changing this to $z = 100$ made virtually no difference, and although using $z = 5$ does make a difference, at most it makes the color bluer by ~0.1 mag at high-$z$. The key thing to note is that for $z > 1.3$ this color space provides a good method for selecting galaxies most likely to be at high redshift.

Since our sample spans a range of $0.3 < z < 5.3$, we apply different color cuts to encompass different parts of the sample. Where we interpret our results in terms of $L_*$, we use the elliptical model with $A_v = 0.8$ (see Figure 1). However, for our color cuts on the data we experiment with colors that would fit any of the models. There are several factors to consider here, first the real colors of galaxies will contain significant scatter. We only show two parameters that can scatter the colors, SF history and extinction, but in reality there will be more, not to mention the intrinsic scatter from measurement errors. In Papovich (2008) the scatter of the 3.6–4.5 μm color was shown by overplotting data with spectroscopic redshifts on to the model predictions; this was possible for $z < 3$ and it showed that there was a minimum of 0.2 mag of scatter at all redshifts. An especially problematic feature that Papovich (2008) reported was a population of galaxies at $z \sim 0.5$ with a significantly redder color than could be predicted by any model or with reddening. These galaxies will certainly contaminate the color space predicted to be occupied by high-$z$ galaxies. These issues create problems as encompassing a range of 0.4 mag of color space will mean we include a large foreground contamination, potentially washing out the signal from the high-$z$ galaxies we are interested in finding. It may prove correct that we are more sensitive to galaxies at the redshifts of interest by using a narrower region of color space which, while losing some galaxies at the correct redshift, means we remove more contamination. The distribution of IRAC 3.6–4.5 μm color from the SERVS source catalogs is shown in Figure 4. When compared to Figure 3 the spread of colors is reassuringly similar.

We therefore need a way of optimizing our color-cut criterion for each redshift range. Ideally this would be done using a spectroscopic sample of galaxies which are in the SERVS fields, similar to that used by Papovich (2008). We could then use different criteria and see which values return the most galaxies at the redshift of interest compared to other redshifts. However, the number of spectroscopic redshifts available in the SERVS fields, or in general at these high redshifts, is insufficient for this type of analysis. Instead, we conducted a Monte Carlo simulation to adjust the color-cut criteria used around the QSOs. This method allows both the upper and lower color cuts to be adjusted in steps within ranges determined from Figure 3. We then measured the source density for each Monte Carlo run and adopted the color cut which gave us the largest overdensity with respect to the background. This works on the assumption that the signal will peak when we include the most galaxies associated with the QSOs compared to contaminating galaxies. To get an idea of the probability that these overdensities are real, and not just noise spikes, we can then conduct the same experiment many times around randomly chosen locations in the SERVS maps, avoiding the locations of the QSOs in our sample.

The inability to effectively remove foreground contamination with this color space for $z < 1.3$ makes the sub-sample at these redshifts harder to study with this method. At these low redshifts

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**Figure 3.** IRAC 3.6–4.5 μm (3.6–4.5 μm) color vs. redshift, per the Bruzual & Charlot (2003) stellar population models and the HYPERZ software package (Bolzonella et al. 2000). The left panel shows the range of colors produced with six different commonly used models. These consist of a single burst model, four exponentially declining SFR models representing elliptical, S0, Sa, and Sc type galaxies with $τ = 1, 2, 3,$ and 15 Gyr, respectively, and a model with a constant SFR (Im). All models have a formation redshift of 10 and no reddening. In the right panel we show the elliptical model without reddening and with two models with $A_v = 0.8$ and 1.6 applied according to Calzetti et al. (2000). This shows that a reasonable level of reddening is likely to have more of an effect on a galaxy’s color in this color space than its star formation history.
the available ancillary data are able to provide a better means to study environments using photometric redshifts or alternative color cuts. It is for this reason that in this paper we avoid the lowest redshift part of the sample. There are also far larger studies of such objects’ environments already in the literature (for example, Yee & Green 1987; McLure & Dunlop 2001; Wold et al. 2001; Kauffmann et al. 2008; and with Spitzer in Falder et al. 2010) and so we feel a study with the small number we have in this sample would add little to the work already done at these relatively low redshifts. In contrast, the environments of high-z QSOs have not been well studied in large numbers or with data of this depth before.

4.3. Ancillary Data Cuts

In addition to the IRAC color cut discussed in Section 4.2 we use the r-band data from the INT (which reaches a 5σ limiting magnitude of 24.2) to cut as much additional foreground contamination as possible. This will hopefully allow us to tackle to some degree the \( z \sim 0.5 \) galaxies mentioned previously that contaminate the color space of higher-z galaxies. The effect of cutting all sources with an r-band detection on the 3.6–4.5 \( \mu m \) color space is shown in Figure 4. The cut has the clear effect of removing around two-thirds of the sources with a negative 3.6–4.5 \( \mu m \) color, which is consistent with Figure 3 suggesting that these sources have \( z < 1.5 \). The other interesting feature is that very few sources with 3.6–4.5 \( \mu m > 0.2 \) are detected in the r band, which is again consistent with Figure 3, suggesting that these sources are likely to lie at \( z > 3 \).

4.4. Background Level

It is important to have a measure of the background level of sources expected in the field with which to measure any overdensities against. There are several ways in which this can be done, one would be to use a systematic offset from the target and measure the source density in that region. This is known as a blank or control field and provides an estimate of the local background level. Another method when working with a large survey such as SERVS is to use a global background where the average source density of a large area or the whole survey is used. There are advantages and disadvantages to each method; using the larger area washes out any fluctuations on small scales which might affect a local value. However, if these local fluctuations are of an amplitude which makes it important to take them into account in the background determination then a local background will help if it is close enough to the target. The trade-off with this method is that being too close may result in measuring the same structure of galaxies in both the background and target field.

Both methods have been experimented within this paper. The global background has been calculated for each of the two SERVS fields, EN1 and the Lockman Hole, by placing a series of 0.5 radius circles on to the catalogs and determining the average source density contained within them. The local values have been calculated by using the average source density in an annulus which is sufficiently far from the QSOs that it should not be measuring the same structure. These annuli have a maximum radius of 400 arcsec from the QSO to ensure none of them fall off the image edges. The inner radius is determined such that it should be 2 Mpc from the QSOs at their redshift. This should be far enough that we are not likely to be measuring the same large-scale structure that the QSOs reside in. Most evidence in the literature suggests that, except for the largest galaxy groups and clusters, most of their members are found within a radius <2 Mpc (for example, Hansen et al. 2005; Papovich et al. 2010).

Obviously the background levels have to be determined in an identical way to how we measure the source density in the environments of the QSOs and will be a different value for each color and r-band criterion that we use. The error on the background is calculated as the Poisson error on the raw number counts used for the background measurements. This is then scaled to the same area and added in quadrature to the error on the source density measurements to get the error on any overdensity.

4.5. Completeness

In order to account for the incompleteness of the Spitzer data near the flux limit of the survey we ran an extensive completeness simulation. This largely followed the process used in Falder et al. (2010) and full details are given there. It involved cutting out regions of the Spitzer images surrounding each QSO that measured 900 \( \times \) 900 arcsec, i.e., large enough to include all annuli used in our analysis. We then inserted 10,000 artificial sources into each of these cutouts for 40 different flux levels. To avoid increasing source confusion these were added in batches of 1000 which meant that they were never too close together that they could become confused with another artificial source. At each flux level we compared the number of inserted sources to those found in the source catalogs. We consider a source recovered if it is found within 1.2 arcsec (2 pixels) of the inserted location and within a factor of two of the inserted flux. The results of this analysis are measured for each annulus separately which then enables us to apply a completeness correction specific to each annulus. This means we account for missed area in the vicinity of bright stars or indeed the QSOs. It was shown in Falder et al. (2010) that the
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Figure 5. Mean completeness fit for the IRAC ch1 data, taken as the average of the completeness in the outer few annuli, therefore away from the bright QSOs.

To eliminate the scatter in the measured completeness curves we then fitted them with an empirical model of the form

$\text{Completeness} = \frac{(S/b)}{(b + cS^a)}$

where $S$ is the 3.6 $\mu$m or 4.5 $\mu$m flux density and $a$, $b$, and $c$ are constants that are fitted. It was found, however, that this model alone was unable to provide a good fit at the knee between the bright end and the steep slope; the data appear less complete here than is at most a 10% effect. It is suspected this effect is likely due to source confusion as the SERVS data are confused using the classical definition of 30 beams per source (J.-C. Mauduit et al. 2011, in preparation). In order to overcome this effect we instead fitted a power law to the data points when the completeness was greater than 0.70 (see Figure 5). The completeness is measured in both the 3.6 $\mu$m and 4.5 $\mu$m images. We are then able for each detected source in the real catalogs to calculate the correct completeness correction to apply by multiplying the completeness fraction corresponding to the measured 3.6 $\mu$m and 4.5 $\mu$m fluxes of the source.

We show the mean completeness curve for the 3.6 $\mu$m cutouts in Figure 5 based on the outer annuli, therefore away from the bright QSOs. To make a conservative cut at the 50% completeness level, we use the flux density at which we are 50% complete in the first annulus. This gives a mean 50% completeness at 3.6 $\mu$m of $1.50 \pm 0.11$ $\mu$Jy (23.46$^{+0.08}_{-0.07}$) and at 4.5 $\mu$m of $1.77 \pm 0.08$ $\mu$Jy (23.28$^{+0.05}_{-0.04}$). To be conservative we only use sources detected with fluxes greater than the highest flux level at which any of our QSO’s first annuli were 50% complete in each channel; these values are $1.71 \mu$Jy (23.32) at 3.6 $\mu$m and $1.89 \mu$Jy (23.21) at 4.5 $\mu$m.

5. RESULTS

In order to have suitable numbers of objects in each redshift range we have divided the sample into two redshift bins shown in Figure 2. The first is centered on $z \sim 2.0$ and spans the range $1.3 < z < 2.7$ and the second is centered on $z \sim 3.3$ and spans the range $2.8 < z < 3.8$. These bins were chosen since there is a natural divide in the sample at $z \sim 2.8$ which gives samples of 11 and 17 QSOs in the two bins. This is a trade-off between having enough QSOs in the sub-samples while restricting the sample to as small a fraction of cosmic time as is possible. As mentioned earlier for QSOs with $z < 1.3$ the color space is contaminated by lower redshift galaxies and these are already better studied in the literature. We also looked at the two $z \sim 5$ QSOs but failed to gain a significant detection of galaxies in their environments, which is not surprising for such a small sample.

5.1. $z \sim 2.0$ Sample

In the redshift range $1.3 < z < 2.7$ there are 17 QSOs of which two are detected by FIRST. These are 105001.04+591111.9 and 105039.54+572336.6 with radio luminosities of $\log_{10}(L_{1400}$/W Hz$^{-1}$ sr$^{-1}) = 25.39$ and 25.16, respectively (calculated using the FIRST radio flux and assuming a spectral index of 0.7). The flux limit at which we are 50% complete at the maximum redshift of this part of the sample corresponds to an absolute magnitude of $-23.4$ and so we restrict our search around each QSO to galaxies brighter than this value (note that we ignore the k-correction within the bin as this is at most a 0.02 mag effect). The adopted limit represents galaxies which are roughly 0.7 $L_\star$ or brighter in this redshift range.

To choose a color criterion for this sample we use Figure 3 to point us toward colors which may select galaxies at the redshift we are interested in. We then use our Monte Carlo code to vary both the upper and lower color cuts in steps within an appropriate range of model predictions. The results of this analysis are shown in Table 1 which shows that the most significant overdensity of 4.10$\sigma$ occurs in the stacked source density when a color criterion of $-0.25 < 3.6-4.5$ $\mu$m $< 0.15$ is used. In addition to the IRAC color cut, we remove sources detected in the $r$ band with an apparent magnitude brighter than 23.5. This criterion corresponds to removing objects that are $\sim 4L_\star$ or brighter according to our choice of models, meaning we are only excluding, if anything, the rarest galaxies associated with the QSOs.

The individual histograms of source overdensity versus radial distance for each of these 17 QSOs are shown in Figure 6; these show the source density with the local background level subtracted. One of these QSOs has a significant overdensity around it at $> 3\sigma$ level (given by Poisson statistics), while several of the other first annuli are more than 1$\sigma$ overdense, which suggests stacking may produce a robust signal. It is worth noting that neither of the two radio-loud QSOs (labeled) shows any sign of an overdensity, which means we are confident that they will not bias the stacked source density as the results of Falder et al. (2010) suggest they might, probably due to their comparatively low radio luminosity.

The resulting stacked source density is shown in Figure 7, which shows an overdensity within 700 kpc of the QSOs and is significantly above the local background level at the 4.10$\sigma$ (given by Poisson statistics) level. The next annulus is also above the background level hinting that the overdensity extends to around the 1 Mpc scale. If we exclude the QSO that has an
individually significant overdensity this reduces to the 3.3σ level suggesting that the overdensity we see in the stacked histogram is not just around that one object. The global background, while looking consistent in most cases, seems to be too high or low in a few cases, suggesting they are in a region with a locally high or low background density. Using the global background has the effect of increasing the detected overdensity to the 4.44σ level; we show where the global background level would be for comparison with a dotted line in Figures 6 and 7.

To put this choice of color cut into context we show a histogram of the 3.6–4.5 μm color space in Figure 8 for both the local background and the first annuli surrounding the QSOs; the bottom panel shows a histogram of the result of subtracting the local background from the first annulus. There is a clear overdensity significant at the 4σ level in the QSO fields, the location of which in this color space is consistent with it being in the redshift range of the QSOs.

When we run our Monte Carlo code 1000 times on batches of 17 random locations (to match the number of QSOs used) avoiding the QSO’s locations in the process, we find that we can generate similar-sized overdensities only 0.1% of the time in the same color space. This increases to only 0.5% of the time over all color space sampled in this analysis (see Table 1). We are therefore confident that this overdensity is real and associated with the QSOs at the 99.5% confidence level using this method.

The reason that this random field test does not generate Poisson statistics is that in reality galaxies are clustered, and so the probability of finding a second galaxy is not mutually exclusive of finding the first as is the case for the Poisson distribution. It is worth noting that if we apply a more simplistic color cut −0.25 < 3.6–4.5 μm, aimed only at removing only lower redshift galaxies, a 2.8σ (Poisson) overdensity still remains.

Physically, the overdensity in the first bin including a correction for completeness corresponds to, on average, 7–10 brighter than ~0.7 L∗ galaxies, with our choice of models. This number is in excess of the local field level around each QSO within ~700 kpc, taking into account the range spanned by the 1σ error bars in Figure 7.
Table 1
Set of Upper and Lower 3.6–4.5 μm Color Criterion Used for the Monte Carlo Analysis on the Sample Centered on z ∼ 2.0, along with Each Set’s Associated Poisson Significance

| Lower Cut | Upper Cut | σ_{Poisson} | Monte Carlo (%) |
|-----------|-----------|-------------|-----------------|
| −0.30     | 0.10      | 3.22        | 0.50            |
| −0.30     | 0.15      | 4.01        | 0.10            |
| −0.30     | 0.20      | 3.32        | 0.60            |
| −0.30     | 0.25      | 3.13        | 1.00            |
| −0.30     | 0.30      | 3.18        | 1.00            |
| −0.25     | 0.15      | 4.10        | 0.10            |
| −0.25     | 0.20      | 3.37        | 0.40            |
| −0.25     | 0.25      | 3.17        | 0.80            |
| −0.25     | 0.30      | 3.21        | 0.80            |
| −0.25     | 0.35      | 3.23        | 0.40            |
| −0.25     | 0.40      | 4.08        | 0.00            |
| −0.25     | 0.45      | 3.29        | 0.50            |
| −0.20     | 0.10      | 3.07        | 1.00            |
| −0.20     | 0.15      | 3.12        | 1.20            |
| −0.15     | 0.10      | 2.60        | 1.20            |
| −0.15     | 0.15      | 3.56        | 0.20            |
| −0.15     | 0.20      | 2.72        | 1.80            |
| −0.15     | 0.25      | 2.50        | 3.10            |
| −0.15     | 0.30      | 2.56        | 3.20            |
| −0.10     | 0.10      | 2.03        | 3.80            |
| −0.10     | 0.15      | 3.12        | 0.50            |
| −0.10     | 0.20      | 2.23        | 4.30            |
| −0.10     | 0.25      | 2.00        | 7.41            |
| −0.10     | 0.30      | 2.08        | 7.01            |
| −0.05     | 0.10      | 1.50        | 10.11           |
| −0.05     | 0.15      | 2.76        | 1.00            |
| −0.05     | 0.20      | 1.79        | 9.21            |
| −0.05     | 0.25      | 1.56        | 13.71           |
| −0.05     | 0.30      | 1.65        | 12.11           |
| NA        | −0.20     | 0.70        | 31.03           |
| 0.20      | NA        | −0.84       | 78.18           |

Notes. Also shown is the percentage of times that this significance was achieved in the Monte Carlo simulation around random points for this color criterion. The color criterion that gives the most significant overdensity is shown in bold. The bottom two color steps are designed for comparison to look above and below the region of color space at which we expect to find an overdensity, as would be expected these two criteria do not produce a significant overdensity.

5.2. z ∼ 3.3 Sample

In the bin that spans the redshift range 2.8 < z < 3.8 there are 11 SDSS QSOs. Using Figure 2 we again experiment, as in Section 5.1 with our Monte Carlo method of adjusting the color cuts. The results of this analysis are given in Table 2 which shows that a color criterion of 0.20 < 3.6−4.5 μm < 0.45 provides the largest overdensity. We again hope to minimize contamination from the foreground by cutting all sources detected in the r band with an apparent magnitude brighter than 23.5. In this redshift range this criterion corresponds to cutting objects that are ∼4 L_∗ or brighter, according to our choice of models, ensuring once again we are only excluding, if any, the rarest galaxies associated with the QSOs. The flux at which we are 50% complete corresponds to an absolute magnitude of −24.4 at the maximum redshift of this sample range and so we restrict the search around each QSO to galaxies brighter than this limit (we ignore the k-correction within the bin as this is at most a 0.2 mag effect). Our adopted limit represents galaxies which are roughly 1.1 L_∗ or brighter in this redshift range.

Figure 7. Stacked source overdensity before being corrected for completeness vs. radial distance for the 17 QSOs in the redshift range of 1.3 < z < 2.7. The first bin has a radius of 700 kpc and the other bins are of the same area as the first. The error bars show the Poisson error on the number counts. The dashed line shows the subtracted local background level (zero level) determined from an annulus of 2 Mpc–400 arcsec from the QSOs. The dotted line shows, for comparison, the global background as determined from taking the average source density in large apertures over the SERVS fields.

Figure 8. Histograms showing the IRAC 3.6–4.5 μm color of sources in the SERVS catalogs. In the top panel the dotted line shows the averaged local background source density surrounding the QSOs in the z ∼ 2.0 sample and the dashed line shows the averaged source density inside the first annulus surrounding these QSOs. The bottom panel shows the result of subtracting the local background from the source density in the first annulus.

The individual histograms of source density versus radial distance for each of these 11 QSOs are shown in the top
Figure 9. Showing the individual source overdensity vs. radial distance for the 11 QSOs in the redshift range 2.8 < z < 3.8. The first bin has a radius of 700 kpc and the other bins are of the same area as the first. The error bars show the Poisson error on the number counts. The dashed line shows the subtracted local background level (zero level) determined from an annulus of 2 Mpc−400 arcsec from the QSOs. The dotted line shows, for comparison, the global background as determined by taking the average source density in large apertures over the SERVS fields. Also labeled are the QSO’s redshifts and absolute SDSS $i$-band magnitudes. This is the source density before being corrected for completeness.

Though there are no statistically significant overdensities, many of the first annuli are more than 1$\sigma$ (given by Poisson statistics) with one 2$\sigma$ above the local background level.

The stacked source density is plotted in Figure 10 which shows a clear peak in the source density within 700 kpc of the QSOs. This peak is significantly above the local background at the 2.62$\sigma$ (given by Poisson statistics). Looking at the individual histograms (Figure 9) we again find that there is evidence to suggest that using local background subtraction is the right approach. However, using a global background in the stacking process has little effect on the result, only reducing the significance to the 2.55$\sigma$ level. We find that if we allow our search to be slightly more sensitive by going down to the flux at which we are 30% complete the stacked source density in this color space becomes more significantly overdense (3.2$\sigma$), see Table 2. This is further evidence that the result is likely to be real since we get a stronger signal despite relaxing our conservative flux cut. We use the source density from the 50% completeness analysis for comparison to other work.

In Figure 11, we show the 3.6–4.5 $\mu$m color space for the local backgrounds and first annulus for this sample along with the result of subtracting the local background. There is a clear overdensity at the \sim$2.6$ level in the color space chosen. The result of this test is thus consistent with the detected overdensity being at the redshift of the QSOs in this part of the sample. When we run our Monte Carlo code 1000 times on batches of 11 random locations, avoiding these QSOs, we find that in this color space we can generate similar sized overdensities only 0.1% of the time. If we extend this to all the color space used in the analysis (see Table 2) then this increases to 11.9%. Using the more sensitive 30% completeness flux limit this improves such that in the color space chosen we only get a 3.2$\sigma$ overdensity 0.1% of the time, and over all color space 5% of the time.

Physically this overdensity with a correction for completeness corresponds to on average 2–5 brighter than $\sim$1.1 $L_*$ galaxies,
Table 2

| Lower Cut | Upper Cut | $\sigma_{c50}$ | MC %$_{c50}$ | $\sigma_{c30}$ | MC %$_{c30}$ |
|-----------|-----------|----------------|---------------|---------------|---------------|
| $-0.10$   | $0.30$    | $0.94$         | $28.50$       | $1.29$        | $23.00$       |
| $-0.10$   | $0.35$    | $1.33$         | $19.90$       | $1.77$        | $14.70$       |
| $-0.10$   | $0.40$    | $1.36$         | $18.80$       | $1.83$        | $14.00$       |
| $-0.10$   | $0.45$    | $1.63$         | $13.90$       | $2.08$        | $9.10$        |
| $-0.05$   | $0.30$    | $1.17$         | $22.10$       | $1.49$        | $19.40$       |
| $-0.05$   | $0.35$    | $1.57$         | $14.70$       | $1.99$        | $11.70$       |
| $-0.05$   | $0.40$    | $1.60$         | $13.50$       | $2.05$        | $11.30$       |
| $-0.05$   | $0.45$    | $1.88$         | $10.00$       | $2.31$        | $7.60$        |
| $0.00$    | $0.30$    | $0.79$         | $31.90$       | $1.08$        | $26.20$       |
| $0.00$    | $0.35$    | $1.24$         | $20.70$       | $1.64$        | $16.10$       |
| $0.00$    | $0.40$    | $1.27$         | $19.20$       | $1.70$        | $15.80$       |
| $0.00$    | $0.45$    | $1.58$         | $14.10$       | $1.98$        | $10.90$       |
| $0.05$    | $0.30$    | $1.61$         | $10.80$       | $1.77$        | $11.50$       |
| $0.05$    | $0.35$    | $2.04$         | $6.90$        | $2.33$        | $5.40$        |
| $0.05$    | $0.40$    | $2.06$         | $7.10$        | $2.38$        | $5.40$        |
| $0.05$    | $0.45$    | $2.37$         | $4.20$        | $2.66$        | $3.50$        |
| $0.10$    | $0.30$    | $1.18$         | $19.40$       | $1.36$        | $17.60$       |
| $0.10$    | $0.35$    | $1.69$         | $9.60$        | $2.01$        | $7.30$        |
| $0.10$    | $0.40$    | $1.71$         | $9.90$        | $2.06$        | $7.50$        |
| $0.10$    | $0.45$    | $2.06$         | $6.00$        | $2.38$        | $4.30$        |
| $0.15$    | $0.30$    | $1.59$         | $10.20$       | $1.95$        | $5.70$        |
| $0.15$    | $0.35$    | $2.14$         | $4.40$        | $2.62$        | $2.20$        |
| $0.15$    | $0.40$    | $2.14$         | $4.40$        | $2.65$        | $2.60$        |
| $0.15$    | $0.45$    | $2.51$         | $1.70$        | $2.99$        | $0.70$        |
| $0.20$    | $0.30$    | $1.60$         | $9.20$        | $2.11$        | $2.80$        |
| $0.20$    | $0.35$    | $2.22$         | $2.90$        | $2.86$        | $0.70$        |
| $0.20$    | $0.40$    | $2.19$         | $2.90$        | $2.85$        | $0.50$        |
| $0.20$    | $0.45$    | $2.62$         | $1.10$        | $3.22$        | $0.10$        |
| $0.45$    | NA        | $0.46$         | $37.80$       | $0.23$        | $41.70$       |
| NA        | $0.05$    | $0.55$         | $36.10$       | $0.75$        | $31.90$       |

*Note.* This is shown both for the analysis down to the conservative 50% completeness limit ($c50$) and the 30% completeness limit ($c30$).

with our choice of models, in excess of the local field level around each QSO within $\sim 700$ kpc.

5.3. Comparison between Redshift Bins

To compare our two sub-samples we re-analyze the $z \sim 2.0$ sample such that we are only sensitive to galaxies with absolute magnitudes brighter than $-24.4$, to match the sensitivity of the $z \sim 3.3$ sample, again neglecting the $k$-correction which is a 0.02 mag effect. In doing this we find 3–6 galaxies brighter $\sim L_*$ around the $z \sim 2.0$ sample. Hence, the population of massive, brighter than $\sim L_*$, galaxies around the two samples seems to be comparable. This is certainly good evidence that the massive (larger than $L_*$) galaxies in proto-clusters are already in place by $z \sim 3–4$, where to date only a handful of detections have been made predominantly around individual high-$z$ radio galaxies (e.g., Overzier et al. 2006, 2008). This picture fits in with the idea of downsizing where massive galaxies form and cluster before those of lower mass (Cowie et al. 1996; Heavens et al. 2004).

6. COMPARISON WITH PREVIOUS WORK AT $z \sim 1$

In this section we compare our results to the previous work at $z \sim 1$ by Falder et al. (2010). The data for the $z \sim 1$ sample are sensitive to galaxies with an absolute magnitude of $-23.0$. We therefore looked again at the data from Falder et al. (2010) using a 700 kpc annulus and restricting ourselves to flux limits which mean that we our sampling the same absolute magnitude range with our choice of models, in excess of the local field level around each QSO within $\sim 700$ kpc.

To compare with the $z \sim 2.0$ sample in which we are sensitive at $z \sim 1$ as in the samples discussed here using the SERVS data. To compare with the $z \sim 2.0$ sample in which we are sensitive...
to an absolute magnitude of $-23.4$ we apply a $k$-correction of 0.4 mag and re-analyze the $z \sim 1$ data down to an absolute magnitude of $-23.0$. This gives 4–6 galaxies within 700 kpc compared to the 7–12 around the $z \sim 2$.0 sample. In the $z \sim 3.3$ sample we are sensitive to galaxies with absolute magnitudes of $-24.4$, again applying a $k$-correction of 0.4 mag we re-analyze the $z \sim 1$ data down to an absolute magnitude of $-24.0$. This gives 1–2 galaxies within 700 kpc compared to the 2–5 around the $z \sim 3.3$ sample. On face value therefore it suggests that the number of galaxies around $z \sim 1$ sample is lower. This may well be the case and would fit in with the idea of downsizing of the AGN population where AGNs at higher redshift are those in bigger groups or clusters than at lower redshift (Romano-Diaz et al. 2010). However, it is likely that the color selection that we use in this work means we are more efficiently removing contamination and therefore detecting a higher signal, this may go some way to explaining the difference.

7. COMPARISON WITH GALAXY FORMATION MODELS

In this section we compare our findings with predictions from the Durham semi-analytic galaxy formation model of Bower et al. (2006), which is based on the ΛCDM MILLENNIUM simulation (Springel et al. 2005). They populate the dark matter halos created by the MILLENNIUM simulation with galaxies using their semi-analytic formula, GALFORM. The MILLENNIUM simulation is an N-body simulation consisting of a box with sides of $500 h$ Mpc$^{-1}$ in comoving units containing $10^{10}$ particles of mass $8.6 \times 10^5 M_\odot h^{-1}$. The simulation started from an initial set of density perturbations at $z = 127$ calculated analytically, which is then allowed to evolve under the influence of only gravity to the present day. Snapshot catalogs of the structures (dark matter halos) that formed and merged in the box were saved at 64 epochs and it is these on to which the Durham galaxies are added. The choice of the Durham model is partly based on the fact that they give their galaxies central black-hole masses (see Bower et al. 2006 for details), which we use to compare to our QSOs, but also because it has recently shown to be one of the best-fitting models to the observed luminosity function at $z < 4$ (Cirasuolo et al. 2010). However, as with all current models there are still some issues with both the faint- and bright-end predictions (e.g., Cirasuolo et al. 2010; Henriques et al. 2010).

In order to compare our findings with what is predicted by the Durham model we have queried the catalogs for each subset of our QSO sample. We have generated catalogs from the model which contain objects with luminosities a factor of two fainter than we are sensitive to in each of the redshift ranges. This allows us to show how the predictions change if we have underestimated or overestimated our survey depth within a reasonable range. For each redshift range we query the model catalogs at the closest snapshot to the mid-point of the redshift range. We have then searched these catalogs for objects around galaxies with black-hole masses greater than three different values ($M_{\text{bh}} > 10^{8.50}, 10^{8.75}$, and $10^{9.0} M_\odot$).

This procedure should replicate as closely as possible what we have done with the SDSS QSOs in SERVS, as by observing the fields around luminous high-$z$ QSOs we know we are centering on large black holes at the redshift of the QSO. It is not currently possible for most of our sample to measure the black-hole masses using virial methods as even the Mg ii line moves out of the SDSS spectral range at $z = 2.25$. However, we know that these high-luminosity QSOs must be hosted by some of the largest black holes at any given epoch. One way to quantify this is through using Eddington arguments to place lower limits on the black-hole masses of our QSOs. Using the SDSS absolute $i$-band magnitude with a bolometric correction of 15 (Richards et al. 2006), we can make the assumption that the QSOs are accreting at the Eddington limit and so their bolometric luminosity is equal to their Eddington luminosity. This then allows us to place a lower limit on the mass of black hole required to power each QSO, using the relationship between Eddington luminosity and black-hole mass from Rees (1984). We present the results of this analysis on the right-hand axis of Figure 2 showing the range of black-hole mass lower limits for each part of the sample. It is worth noting that there are no black holes in the model at $z \sim 3.3$ that have a mass $> 10^{9.25} M_\odot$, hence why we did not extend the range of black holes we searched around to better match our range in Figure 2.

We are able to query the full simulation box for the higher redshift part of our sample, but for the lower redshift part we have to restrict the volume queried to a $350 h$ Mpc$^{-1}$ on a side box due to the time restriction on queries. This is not an issue, however, because at lower redshift the population of large black holes is, as would be expected, higher and so we require less area to find the same number of suitable targets. As the longest wavelength that the model produces is the $K$ band we use our modeled $K = 3.6 \mu m$ color from Section 4.2 to match to our observations. To account for the effect of in reality measuring counts in a cylinder we search within our physical search radius of 700 kpc in two dimensions of the simulation and then within 3 Mpc in the third dimension. This effect as described in Yee & Ellingson (1995) increases the sources detected by a factor of $\sim 1.5$. We can then compare the measured overdensity, which we assume is all associated with the QSOs, to the number of comparable galaxies we find in the model catalogs within the same radius.

The results of this comparison are shown in Figure 12. The gray shaded band shows the $1\sigma$ error on the number of galaxies we have found surrounding our QSOs in each case, and the error bar shows where we estimate we have reached down to in terms of galaxy absolute magnitude with our analysis. The lines then show the number of galaxies predicted by the model within the same cylindrical search area for galaxies with three different central black-hole masses.

Interestingly, in both cases we find that our detected source density matches well with the predictions of the models. In the $z \sim 2.0$ redshift bin the model predictions for the $10^{8.50}$ and $10^{8.75}$ $M_\odot$ black holes fall within the $1\sigma$ error bars of our measured source density. In the $z \sim 3.3$ redshift bin the model predictions for the $10^{8.75}$ and $10^{9.00}$ $M_\odot$ black holes fall within the $1\sigma$ error bars of our measured source density. It is worth noting that in our estimates of the black-hole masses of our sample the $z \sim 3.3$ part of the sample has on average larger black-hole masses due to its on average higher luminosity.

8. SUMMARY

In this paper, we have undertaken a study of the environments of SDSS QSOs in the deep SERVS survey using data from Spitzer’s IRAC instrument at 3.6 $\mu$m and 4.5 $\mu$m. We concentrate our study on the high-redshift QSOs as these have not previously been studied with statistically large samples or with data of this depth. These are highly luminous QSOs $M_i \lesssim -26$ and hence harbor massive black holes $M_{\text{bh}} \gtrsim 10^8 M_\odot$. In contrast, the environments of lower redshift QSOs have been studied in detail with much larger samples (Falder et al. 2010). We split the $z > 1$ QSOs up into two sub-samples depending on their
redshift, this allows us to apply different source selection criteria to each sample. The criteria we apply are a combination of an IRAC 3.6–4.5 μm color selection and a cut of sources detected above a certain brightness in the ancillary r-band data from the INT.

Using this method we are able to detect a significant (>4σ) overdensity of galaxies around the QSOs in the sub-sample centered on z ~ 2.0 and (>2σ) in the sub-sample centered on z ~ 3.3, providing further evidence that high-luminosity AGN can be used to trace clusters and proto-clusters at these epochs. We compare the number counts of L* or brighter galaxies around each sample and find them to be comparable, suggesting the massive galaxies in proto-clusters are in place by z ~ 3–4 which is consistent with the idea of downsizing. We then compare these findings to those of Falder et al. (2010) at z ~ 1 and find that the overdensities found in this work are slightly larger than those found in Falder et al. (2010). However, it is likely that the color selection used in this work allows for a more efficient detection of possible companion galaxies and therefore this difference may well not be a real effect.

We then compare our results to the predictions from the Durham (Bower et al. 2006) galaxy formation model, built on top of the Millennium simulation (Springel et al. 2005) dark matter halo catalogs. In both cases we find the model predictions are within the 1σ error bars of our measured source density.

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