Critical flow and dissipation in a quasi–one-dimensional superfluid

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In one of the most celebrated examples of the theory of universal critical phenomena, the phase transition to the superfluid state of 4He belongs to the same three-dimensional (3D) O(2) universality class as the onset of ferromagnetism in a lattice of classical spins with XY symmetry. Below the transition, the superfluid density \( \rho_s \) and superfluid velocity \( v_s \) increase as a power law of temperature described by a universal critical exponent that is constrained to be identical by scale invariance. As the dimensionality is reduced toward 1D, it is expected that enhanced thermal and quantum fluctuations preclude long-range order, thereby inhibiting superfluidity. We have measured the flow rate of liquid helium and deduced its superfluid velocity in a capillary flow experiment occurring in single 30-nm-long nanopores with radii ranging down from 20 to 3 nm. As the pore size is reduced toward the 1D limit, we observe the following: (i) a suppression of the pressure dependence of the superfluid velocity; (ii) a temperature dependence of \( v_s \) that surprisingly can be well-fitted by a power law with a single exponent over a broad range of temperatures; and (iii) decreasing critical velocities as a function of decreasing radius for channel sizes below \( R \approx 20 \) nm, in stark contrast with what is observed in micrometer-sized channels. We interpret these deviations from bulk behavior as signaling the crossover to a quasi-1D state, whereby the size of a critical topological defect is cut off by the channel radius.

INTRODUCTION

Motivation

Helium is the only known element in nature that becomes a superfluid, with its small mass and weak polarizability cooperating to prevent solidification at atmospheric pressure as the temperature approaches absolute zero. For 4He, the ability to flow without viscosity below the \( \lambda \)-transition temperature, \( T_\lambda \), is a paradigmatic manifestation of emergent phenomena and macroscopic quantum coherence, driven by both interactions and bosonic quantum statistics. Its superflow with velocity \( v_s = (\hbar/n)\nabla\Phi \) is caused by a quantum-mechanical gradient of the wave function and a priori should only be limited by the Landau criterion of superfluidity. The existence of the roton minimum in the excitation spectrum sets this value to be \( v_s \approx 60 \) m/s. However, years of experiments (1) have shown that superfluid 4He exhibits a critical velocity that is well below \( v_s \). Although there is consensus that superfluid helium dissipates energy by creating vortex rings, the exact microscopic dynamics that govern the nucleation of topological defects remain an open problem in condensed matter physics.

At first glance, it would appear that this problem would only be exacerbated as the number of spatial dimensions decreases because enhanced thermal and quantum fluctuations should push \( T_\lambda \rightarrow 0 \). However, in the one-dimensional (1D) limit, the universal quantum hydrodynamics of Tomonaga-Luttinger liquid theory (2–4) should apply, providing a host of theoretical predictions including the simultaneous algebraic spatial decay of both density-density and superfluid correlation functions. Although there is a body of evidence of this exotic behavior in low-dimensional electronic systems (5–8) and ultra-cold low-density gases (9), the analogous behavior has yet to be confirmed experimentally in a highly correlated bosonic liquid. Here, the physics of superflow should be qualitatively altered, with the superfluid density \( \rho_s \) acquiring system size and frequency dependence (10). Furthermore, neutral mass flow transport properties should be strongly modified in 1D, with the superfluid velocity \( v_s \) exhibiting non-universal power law dependence on temperature and pressure. This crossover toward 1D is manifest in the main findings of our work: (i) a suppression of the pressure dependence of \( v_s \) for \( R \approx 3 \) nm indicative of enhanced dissipation via phase slips, (ii) a temperature dependence for \( v_s \) that can be described by a power law with a single exponent over a broad range of temperatures, and (iii) decreasing critical velocities as the radius decreases for channel sizes below \( R \approx 20 \) nm, behavior strongly deviant from what is observed in micrometer-sized channels.

Length scales

In this work, the mass flow rate of superfluid helium is measured in a capillary experiment through channels with radii as small as \( R \approx 3 \) nm and length \( L = 30 \) nm. To determine the effective dimensionality of this geometry, it is imperative to perform a comparative analysis of all possible relevant length scales. Unlike superconductors and superfluid 3He, which undergo BCS pairing, 4He has a very small coherence length on the angstrom scale: \( \xi(T) = \xi_0(1 - T/T_\lambda)^{-\frac{1}{2}} \), with \( \xi_0 = 3.45 \) Å and \( n \approx 2/3 \), making it technically difficult to fabricate a transverse confinement dimension with \( R \ll \xi \) approaching the truly 1D limit, as, for example, \( \xi_4 \approx 0.5 \) to 1.5 nm in the temperature range considered here. For \( T = 0.5 \) to 2 K, \( R \) can also be compared to the thermal de Broglie wavelength, \( \lambda(T) = \sqrt{2\pi\hbar^2/mk_B T} \approx 1 \) nm and a thermal length \( L_T = \hbar c_1/k_B T \approx 1 \) nm, where \( c_1 \approx 235 \) m/s is the first sound velocity of 4He. Another estimate of the effective dimensionality can be obtained by considering helium atoms confined inside a long cylinder of radius \( R \) with hard walls. In analogy with electrons confined in quantum wires, we compute the energy needed to populate excited...
single-particle transverse modes, and find that to fill the lowest excited transverse angular momentum state for a single helium atom, a temperature $T \sim \Delta_s/k_B \approx 3.5/R^2 \text{ nm}^{-2}$. K $\sim 0.4$ K for $R = 3$ nm is needed. These estimates, which mostly neglect interaction effects, would place our flow experiments in a mesoscopic regime, with confinement length and energy scales on the order of the intrinsic ones in the problem. However, recent ab initio simulations of $^4$He confined inside nanopores (11, 12) have demonstrated that classical adsorption behavior leads to an effective phase separation between a quasi-1D superfluid core of reduced radius and concentric shells of quasi-solid helium near the pore walls. This effect, which is likely also present in our channels, would tend to provide additional confinement, allowing us to investigate a nontrivial dimensional crossover.

Previous investigations of helium confined at the nanometer scale have focused on porous media such as in Vycor (13) and more recently in the zeolites and other mesoporous media. These studies have shown a possible new thermodynamic phase of $^4$He stabilized at low temperatures (14) as well as a nuclear magnetic resonance (NMR) signature of a 1D crossover for $^4$He (15). Although these advances are certainly considerable in the search for a strongly interacting 1D neutral quantum gas, our approach differs much in spirit from those cited above. In our experiment, the helium atoms are confined inside a single, nearly cylindrical pore, rather than in an extremely large number of them necessary to gain a signal for a macroscopic probe. This lone pore, or channel, is tailor-made from a pristine Si$_3$N$_4$ membrane that can be fabricated with radius ranging from $R \approx 1$ to 100 nm. The main advantage of our approach is that there is no ensemble averaging over pore distributions and/or potential defects of the sample. Its main drawback, however, is that traditional bulk measurement techniques, such as specific heat or NMR, most likely cannot be performed in a single nanopore containing only $\sim 10^4$ to $10^7$ helium atoms. Taken as a whole, these two approaches are complementary to one another and similar in spirit to “single-molecule versus ensemble-averaged” studies in other fields, such as nanoelectronics or molecular biology.

**RESULTS**

**Mass flow measurements**

Above $T_s$, in the normal phase of helium, the flow through the nanopore is viscously dissipative and expected to follow the model developed for a short pipe by Langhaar (16). In this phase, we conducted pressure sweeps at constant temperature while monitoring the mass flow rate $Q_m$ as shown in Fig. 1 (A and B). In the absence of a chemical potential difference, the mass flow rate should go to zero. However, we observe a spurious signal as $\Delta P \rightarrow 0$ arising from evaporation at the walls of the channel. To determine this offset, the data were played in Fig. 1 (C and D), with the offset previously discussed subtracted. Previous work in Vycor (13) has found the superfluid transition to be suppressed to 1.95 K; however, the superfluid transition in our channels is observed at the temperature corresponding to the bulk value, 2.17 K. This is not surprising because we measure the total conductance of the nanopore channel and of the source reservoir in series, so the onset of superfluidity in the bulk is first observed at $T_s$. Considering only data below $T_s$, we can extract the superfluid velocities using the two-fluid model, where we assume $Q_{tot} = Q_n + Q_s = \nu_n \rho n + \nu_s \rho s R^2$ with the $n$ and $s$ subscripts denoting the normal and superfluid components of the fluid, respectively. Subtracting $Q_n$ from the total mass flow using Eq. 1 yields the superfluid portion of the flow with a velocity $v_s = Q_s/\pi R^2 \rho_s$. The superfluid density is taken from the bulk, as justified by previous work in Vycor (with a similar network pore size), albeit with a lower transition temperature (13). The extracted superfluid velocities are shown in Fig. 2A for the lower-pressure data sets, where linear response is expected to be a better approximation and where the data sets were taken over a large range of temperatures. An inspection by eye readily shows that the superfluid velocities are smaller in the $R \approx 3$ nm pore at similar pressures and temperatures. Such suppression of the flow velocity as the radius is decreased is in stark contrast with the bulk behavior and shows that dissipation is increasing as the radius of the pore approaches a few nanometers.

Near the bulk superfluid transition, it is well established that the superfluid density follows a universal power law form $\rho_s \sim (1 - T/T_s)^\nu$,

$$Q_n = \frac{8\pi L}{\alpha} \left( \sqrt{1 + \frac{\rho \gamma R^2}{52\pi L^2}} \Delta P - 1 \right)$$

where $\eta$ is the viscosity, $\rho$ is the density, and $\alpha$ is a coefficient to take into account the acceleration of the fluid at the pipe end (see the Supplementary Materials). In Fig. 1 (A and B), the solid line is a fit to the data with a radius of $R = 7.81 \pm 0.15$ nm and $3.14 \pm 0.11$ nm. The mass flow was then measured as a function of temperature across the superfluid phase transition $T_s$ at several pressures for both pores. These data are displayed in Fig. 1 (C and D), with the offset previously discussed subtracted. Previous work in Vycor (13) has found the superfluid transition to be suppressed to 1.95 K; however, the superfluid transition in our channels is observed at the temperature corresponding to the bulk value, 2.17 K. This is not surprising because we measure the total conductance of the nanopore channel and of the source reservoir in series, so the onset of superfluidity in the bulk is first observed at $T_s$. Considering only data below $T_s$, we can extract the superfluid velocities using the two-fluid model, where we assume $Q_{tot} = Q_n + Q_s = \nu_n \rho n + \nu_s \rho s R^2$ with the $n$ and $s$ subscripts denoting the normal and superfluid components of the fluid, respectively. Subtracting $Q_n$ from the total mass flow using Eq. 1 yields the superfluid portion of the flow with a velocity $v_s = Q_s/\pi R^2 \rho_s$. The superfluid density is taken from the bulk, as justified by previous work in Vycor (with a similar network pore size), albeit with a lower transition temperature (13). The extracted superfluid velocities are shown in Fig. 2A for the lower-pressure data sets, where linear response is expected to be a better approximation and where the data sets were taken over a large range of temperatures. An inspection by eye readily shows that the superfluid velocities are smaller in the $R \approx 3$ nm pore at similar pressures and temperatures. Such suppression of the flow velocity as the radius is decreased is in stark contrast with the bulk behavior and shows that dissipation is increasing as the radius of the pore approaches a few nanometers.

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where $v$ is a correlation length critical exponent found experimentally to be close to $2/3$. Considering a slowly varying quantum-mechanical wave function with a phase $\Phi$, the kinetic energy of the superfluid is given by $p_s v_s^2 / 2 = p_s (\hbar^2 / 2m^2) |\nabla \Phi|^2$. From scale invariance, we expect that near $T_s$, the mean square of the superfluid velocity should scale with the correlation length $\xi_s(T) = v_s^2 \sim 1/\xi_a(T)^2 \sim (1 - T/T_s)^{2\nu}$. This result is, strictly speaking, valid only at temperatures very close to $T_s$, $(1 - T/T_s) \lesssim 0.1$. From this hyperscaling analysis, there is no reason to expect power law behavior in the superfluid velocity over a wide range in temperature away from $T_s$. However, in the data shown in Fig. 2A, a power law $v_s(T) = v_{s0} (1 - T/T_s)^\nu$, where $v_{s0}$ is the superfluid critical velocity at $T = 0$ K, was used to fit all the data. A log-log plot of $v_s$ versus the reduced temperature is shown in Fig. 2B for the 3.14-nm pore. For this radius, where very little pressure dependence on the flow is observed, the power law yields an exponent 0.53 ± 0.04 and 0.47 ± 0.06 for the low-pressure (482 mbar) and higher-pressure (827 mbar) data set, respectively, and their critical velocities at zero temperature are $v_{s0} = 15.2 \pm 1$ m/s and $16.6 \pm 1$ m/s. In contrast, the larger pore (7.81 nm) displays a significantly distinct exponent 0.66 ± 0.05 and zero-temperature superfluid critical velocity $v_{s0} = 30.1 \pm 2.4$ m/s. Although not a proof, given the limited range in temperature explored, the appearance of a smaller non-universal exponent as the dimensionality is reduced is consistent with expectations from quantum hydrodynamics in 1D where increased non-universal exponent as the dimensionality is reduced is consistent with expectations from quantum hydrodynamics in 1D where increased fluctuations should prohibit long-range order.

**Dissipation mechanisms**

Other important features of the flow data not previously observed are (i) the extremely weak pressure dependence below $T_s$ for the smaller pore, and (ii) an overall decrease in critical velocity as the channel size is reduced, in contrast to the behavior $v_s = \mu \ln (a / a_0)$, where $a_0$ the size of the vortex core, predicted by Feynman and found in larger channels (see the Supplementary Materials). The former is a hallmark of the macroscopic phase coherence that exists in a superfluid phase, in sharp contrast with the Euler prediction of a classical inviscid fluid, $v_s = \sqrt{2AP/\rho_s}$. Using the Gibbs-Duhem relation to convert a pressure to chemical potential difference, energy conservation dictates that there must exist a dissipation mechanism in the channel with a rate $\Gamma$ such that $\hbar^2 = \frac{m\rho}{\rho_s} - \frac{1}{2} \frac{m v_s^2}{\rho_s}$. From our data, it is clear that the dissipation rate must be flow (pressure)-dependent. The question of how energy is dissipated in superfluids has a long history, beginning with the proposal of Anderson (17) that, in analogy with the Josephson effect in superconductors, a steady-state non-entropic flow may be achieved at a critical velocity $v_s$ via a mechanism that unwinds the phase of the order parameter in quanta of $2\pi$. Such “phase slips,” occurring at rate $\Gamma$, correspond to a process whereby the amplitude of the order parameter is instantaneously suppressed to zero at some point along the channel and can be driven by either thermal or quantum fluctuations. Momentum conservation dictates that such events can only occur in the presence of broken translational invariance along the pore (18).

Microscopically, dissipation occurs through the creation of quantized vortex rings, the topological defects of superfluid hydrodynamics. In our experiments, the size of critical vortex ring $R_c$ plays a crucial role, and it is determined by the equilibrium condition between the relative frictional force between the normal and superfluid component and the hydrodynamic forces acting on the ring in the presence of flow. Energetically, this manifests as a competition between a positive vortex energy that scales linearly with radius and a negative kinetic core energy scaling like its area. Langer and Fisher (19) found $R_c \sim 3$ nm below $T_s$, exactly the length scale of the smallest pore considered here. When $R < R_c$, the maximum size of a vortex ring is constrained by the radius of the channel, and thus the energy barrier for their creation is lowered, leading to increased dissipation and an upper bound on $v_s$, set by the Feynman critical velocity. The suppression in the observed critical velocity at $T = 1.5$ K as a function of decreasing radius shown in Fig. 2C can then be interpreted as a crossover to a regime where flow is dominated by the physics of the channel. As the channel radius continues to decrease further, it is expected that backscattering of helium atoms at low temperature in the guise of...
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