The Impact of the Charge Barrier Height on Germanium (Ge) Detectors with Amorphous-Ge Contacts for Light Dark Matter Searches

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Abstract Germanium (Ge) detectors with ability of measuring a single electron-hole (e-h) pair are needed in searching for light dark matter (LDM) down to the MeV scale. We investigate the feasibility of Ge detectors with amorphous-Ge (a-Ge) contacts to achieve the sensitivity of measuring a single e-h pair, which requires extremely low leakage current. Three Ge detectors with a-Ge contacts are used to study the charge barrier height for blocking electrons and holes. Using the measured bulk leakage current and the D"ohler-Brodsky model, we obtain the values for charge barrier height and the density of localized energy states near the Fermi energy level for the top and bottom contacts, respectively. We predict that the bulk leakage current is extremely small and can be neglected at helium temperature (∼4 K). Thus, Ge detectors with a-Ge contacts possess the potential to measure a single e-h pair for detecting LDM particles.

1 Introduction

Light dark matter (LDM) especially low-mass dark matter in the MeV-scale has risen to become an exciting dark matter candidate in the past decade [1–4]. Despite various target materials having been used in the direct detection of Weakly Interacting Massive Particles (WIMPs, a popular dark matter candidate) for over three decades, all existing dark matter experiments are unable to detect MeV-scale dark matter since they are all sensitive to WIMPs with masses greater than a few GeV/c² [5–26]. More recently, Kadribasic et al. have reported a method of using solid state detectors with directional sensitivity to dark matter interactions to detect low-mass WIMPs below 1 GeV/c² [27]. CRESST has achieved a threshold of 20 eV with a small prototype sapphire detector [28]. DAMIC has claimed a sensitivity to ionization < 12 eV with silicon CCDs and consider their method to be able to reach 1.2 eV [29].

High-purity germanium (HPGe) detector technology has been used for dark matter searches since 1987 due to its high-purity [30]. Two main advantages of HPGe detector technology are its excellent energy resolution and high detection efficiency, which allow Ge detectors to reach a quite low energy threshold down to ∼0.5 keVee, where keVee represents electronic equivalent energy. This enables Ge detectors to be used for detecting low mass WIMPs of a few GeV/c². More recently, a Ge detector utilizing internal charge amplification for the charge carriers created by the ionization of impurities has been demonstrated theoretically to be a promising new technology for detecting MeV-scale dark matter [31].

A simple Ge detector is usually made of a block of HPGe crystal in which p+ and n+ electrical contacts have been fabricated on opposite sides of the block. The standard contact technology for Ge detectors are Li-diffused n+ contact for hole blocking and B-implanted p+ contact for electron blocking. This conventional contact technology is robust since both types of contacts are able to withstand high electric fields, and thus yield low charge carrier injection. However, there are drawbacks in this technology especially for the Li-diffused contacts. Due to its thickness and significant diffusion of Li at room temperature, the Li-diffused side is problematic for two main reasons. One is that the Li-diffused side usually forms a thick dead layer (∼1 mm), which is insensitive to charge carriers, and a transition layer (∼1 mm) between Li and Ge where charge carriers can be significantly trapped. The total thickness of the dead layer and the transition layer reduces the sensitive volume of a Ge detector. Another is that the Li-diffused side is difficult for segmentation in order to produce position-sensitive detectors, which are demanded increasingly by modern appli-
cations requiring not only excellent spectroscopy, but also particle tracking or imaging [32].

An alternative contact technology capable of producing detectors with a thin contact without a dead layer and a transition layer, as well as with fine spatial resolution is the amorphous-germanium (a-Ge) contact developed at Lawrence Berkeley National Laboratory (LBNL) [33–35]. The successful use of a-Ge contacts on Ge detectors has been verified by a series of previous studies conducted at LBNL [32, 36–41]. In addition, a large number of detectors with great detector performance have been fabricated successfully at LBNL using this technology. More recently, a dozen small detectors made from USD-grown crystals have also been fabricated successfully at the University of South Dakota (USD) [42, 43] using the same technology. With a-Ge contact technology, as shown in Fig. 1, a block of HPGe crystal was first coated with a thin film of high-resistivity a-Ge on all of its surfaces, then a thin film of low-resistivity metal (typically Al) was deposited on opposite sides of the crystal block. There are several advantages of this technology [44]: (1) simple fabrication process; (2) good bipolar blocking behavior, i.e. a-Ge contacts can block both hole and electron injection well; (3) thin contacts without a dead layer and a transition layer; (4) complete surface passivation, since a-Ge layers are common passivation materials; and (5) fine achievable contact pitches for segmentation.

In order to directly detect MeV-scale dark matter, a detector with the ability to measure a single electron-hole (e-h) pair is required, since both electronic recoils and nuclear recoils induced by MeV-scale dark matter are in the range of sub-eV to 100 eV [1]. Mei et al. has suggested direct detection of MeV-scale DM utilizing germanium internal charge amplification (GeICA) for the charge created by the ionization of impurities [31]. GeICA can reach a detection energy threshold as low as 0.1 eV, allowing a large portion of both electronic recoils and nuclear recoils in the range of sub-eV to 100 eV [1, 31] induced by DM to be accessible. For the DM-WIMPs interaction, the effective mass of WIMPs that contributed to the super-weak coupling strength is constrained between ∼1 MeV/c² to ∼100 MeV/c² by Xenon1T [45]. Therefore, the detectable recoil energy is also in the range of sub-eV to 100 eV, similar to the recoil energy spectrum induced by MeV-scale DM as shown in Fig. 2 [31]. In this sub-eV to ∼100 eV region, GeICA offers a very competitive sensitivity to detect LDM.

A conceptual GeICA detector can be made as a p-type point contact (PPC) detector. The size of the point contact can be as small as 0.5 mm to achieve low capacitance and high electric field. A low capacitance in sub picofarads (pF) is required to achieve ultra-low electronic noise. A high electric field near the point contact is needed to achieve the needed amplification factor for a GeICA detector. To achieve the sensitivity of detecting a single e-h pair induced by MeV-scale DM with GeICA detectors, one must be able to control the bulk leakage current much below 1 picoampere (pA). This is because one e-h pair corresponds to ∼pA if the drift time is on the level of ∼100 nanoseconds (ns) for a GeICA detector. For a GeICA detector with an amplification factor of 100, the size of signal would be 100 e-h pairs. This is equivalent to the number of e-h pairs produced by an electronic recoil with 300 eV energy in Ge assuming the average energy required to generate one e-h pair is 3 eV. Thus, low-noise electronics, as low as 40 eV-FWHM (full width at half maximum), demonstrated by Barton et al. [46] would allow us to achieve the ability of measuring a single e-h pair with a GeICA detector. This indicates that the detector leakage current must be minimized since the leakage current mimics the signal and hence becomes a significant source of background.

In general, there are three main contributions to the leakage current in a fully-depleted HPGe detector [32]: (1) charge carrier injection at the electrical contact, i.e. hole injection at the positive contact and electron injection at the negative contact; (2) charge flow along detector side surfaces; and (3) thermal generation of electron-hole pairs in the detector. The contribution from the thermal generation can be reduced to a negligible level by cooling the detector to liquid helium tem-
temperature. According to the studies in [32, 38], a guard ring structure shown in Fig. 3 can be used to mitigate the contribution to the measurement from the surface current component, leaving charge carrier injection at the electrical contacts as the main source of leakage current. It is worth mentioning that Barton et al. has demonstrated a low-leakage current of 0.02 pA at 30 K for a PPC detector with bias of 150 V [46]. The outer surface of this PPC detector was made with lithium diffused n-type contact for hole blocking and the inner point contact was made with the bipolar blocking of amorphous silicon. For a Ge detector made with a-Ge contact technology, the level of charge injected into the detector is dictated by the electron or hole energy barrier to charge injection, which is an important property of a-Ge contacts. The barrier heights of the a-Ge contacts depend on the fabrication method used to produce them. Therefore, a study of the electron or hole energy barrier to charge injection is necessary to optimize fabrication parameters and thus improve the detector performance especially in terms of reducing the leakage current, so that the detector will be able to reach low-energy threshold for MeV-scale dark matter detection.

In this paper, we report the electron and hole energy barrier heights of RF-sputtered a-Ge contacts on three HPGe detectors with guard-ring structures fabricated at USD. All three detectors were made with the Ge crystals grown by us at USD. A theoretical model of the amorphous semiconductor electrical contact is presented in section 2, followed by the experimental methods in section 3. The data analysis and results are discussed in section 4, followed by the discussion and prediction in section 5. Finally, the conclusions are summarized in section 6.

2 Theoretical Model of Amorphous Semiconductor Electrical Contract

To implement strategies to optimize the a-Ge contact and thus minimize the detector leakage current, it is of great importance to understand the underlying physics of the amorphous semiconductor contacts. Thus, a main focus in this paper is to analyze our detector leakage current data based on a physical model of the amorphous semiconductor electrical contact.

Compared to a crystalline semiconductor, an amorphous semiconductor is a solid that lacks the long-range crystalline order of atoms. Amorphous semiconductor films are usually formed through evaporation [47], sputtering [36], or damage to a crystal lattice [48], while single-crystal semiconductors are produced using the Czochralski technique [49] or other crystal growing techniques, which require much more time and effort. Although atoms in amorphous semiconductors still arrange in a diamond-like structure, the density of defects states in amorphous semiconductors is much higher than that of crystalline semiconductors because of inefficient stacking of those diamond-like structures. Many of those defects are vacancies or voids, leaving "dangling bonds", which is a semiconductor valence state not occupied in a covalent bond [50]. Since the binding energy of dangling bonds is less than that of covalent bonds, the dangling bonds more easily contribute to electrical conduction. There are large number of defect states in the band gap of amorphous semiconductors [50]. Because of these defect states, charge carriers that would normally be forbidden to move in the gap region can move from defect to defect in a process called phonon-assisted hopping, which allows significant electrical conduction near the Fermi level in the gap region of amorphous semiconductors. This hopping conduction through the localized defect energy states near the Fermi level is the dominant source of charge movement in amorphous semiconductors [51].

In fact, the charge conduction in a metal also mainly occurs through electronic energy levels close to the Fermi energy. This similarity in conduction motivates the use of metal-semiconductor theory or Schottky theory [52] to describe the amorphous semiconductor contacts. A theoretical model about the current-voltage relationship for amorphous-crystalline semiconductor heterojunctions has been developed by Döhler and Brodsky during the 1970s [51, 55, 56]. Döhler and Brodsky concluded that the forward biased junction should be indistinguishable from those for a metal semiconductor junction and the reverse current should have no saturation but should show an exponential increase as the space charge lowers the barrier height. In the Döhler-Brodsky model, the state of thermal equilibrium in which the Fermi levels in the amorphous semiconductor and crystalline semiconductor coincide and an ideal contact without interface energy states was assumed. Thus, as described clearly in the energy diagrams presented in the most recent work by Amman [41], for the charge carriers at the Fermi level to be injected from the amorphous semiconductor to the conduction band of the crystalline semiconductor, there exists a potential energy barrier that inhibits such injection. This is the...
physical mechanism that leads to the bipolar blocking behavior of amorphous semiconductor contacts. The Döhler-Brodsky model was later applied successfully to the a-Ge contact on HPGe in the studies by Hull et al. [38], Looker et al. [32] and Amman [41]. Based on the Döhler-Brodsky model and Schottky theory [52, 57], for a p-type HPGe detector fabricated with a-Ge contacts when a negative bias voltage is applied to one of its contacts, the current normalized by the contact area, \( J \), is given by [32, 41]:

\[
J = A^* T^2 \exp[-(\varphi_h - \Delta \varphi_h)/kT] \\
\text{with } \Delta \varphi_h = \sqrt{2qV_dN_d/N_f}
\]

and,

\[
J = A^* T^2 \exp[-(\varphi_e - \Delta \varphi_e)/kT] \\
\text{with } \Delta \varphi_e = \sqrt{\varepsilon_0 \varepsilon_{Ge}/N_f(V_d - V_a)/t}
\]

where Eq. 1 describes the leakage current density from hole injection at the contact where the detector starts to deplete, and Eq. 2 describes the leakage current density, after the detector is fully depleted, from electron injection at another contact where a negative bias voltage is applied. The overall leakage current above full depletion is then the sum of Eq. 1 and Eq. 2. In the equations above, \( A^* \) is the effective Richardson constant, \( T \) is the temperature, \( \varphi_h \) and \( \varphi_e \) are the energy barriers to hole and electron injections, respectively, \( \Delta \varphi_h \) and \( \Delta \varphi_e \) are the barrier lowering terms which account for the lowering of hole and electron energy barrier, respectively, due to the penetration of the electric field into the a-Ge contacts, \( q \) is the magnitude of the electron charge, \( V_d \) is the reverse bias voltage applied across the detector, \( N_d \) is the net ionized impurity concentration of the detector, \( N_f \) is the density of localized energy states (defects) near the Fermi level in the a-Ge, \( k \) is the Boltzmann constant, \( \varepsilon_0 \) is the free-space permittivity, \( \varepsilon_{Ge} \) is the relative permittivity for Ge, \( V_d \) is the full depletion voltage and \( t \) is the detector thickness. Note that both Eq. 1 and Eq. 2 can be rewritten as:

\[
kT \ln\left(\frac{J}{A^* T^2}\right) = -\varphi_h + b_1 \sqrt{V_d} \quad \text{with } b_1 = \sqrt{2qN_d/N_f}
\]

and,

\[
kT \ln\left(\frac{J}{A^* T^2}\right) = -\varphi_e + b_2 (V_d - V_a)
\]

with \( q \) being the electric charge, \( m^* \) the effective mass of charge carriers, \( k \) the Boltzmann constant and \( \hbar \) the Plank constant. Note that \( A^* \) is the effective Richardson constant for thermionic emission, neglecting the effects of optical-phonon scattering and quantum mechanical reflection. For free electrons (\( m^* = m_0 \)), the Richardson constant \( A \) is 120 Amp/cm²/K² [52]. For p-type Ge in the <100>-direction [52],

\[
A^* = \frac{m_{th}^* + m_{hh}^* + m_{h,so}^*}{m_0}
\]

where \( m_{th}^* = 0.04m_0, m_{hh}^* = 0.28m_0 \), and \( m_{h,so}^* = 0.08m_0 \) [53]. Thus, \( A^* = 48 \text{ Amp/cm²/K²} \), which has been used in [54]. As discussed by pioneers in early publications [32, 38, 41], this effective Richardson constant may vary with the fabrication processes. However, we show that \( A^* = 48 \text{ Amp/cm²/K²} \) in this work to explain the behavior of our detector leakage current especially from the hole injection at the contact when the detector is partially depleted.

Eq. 1 and Eq. 2 clearly show that, at a given temperature, the energy barrier height plays a key role in the effectiveness of the charge injection blocking behavior of the amorphous electrical contacts. Based on the metal-semiconductor theory, the energy barrier height is, in general, determined by the work function of amorphous semiconductors, the electron affinity of crystalline semiconductors, and the interface states between amorphous and crystalline semiconductors [52]. Since the magnitude and energy distribution of the interface states are likely dependent on the preparation of the crystalline semiconductor surface and the deposition process of the amorphous semiconductor, it is not straightforward to determine the energy barrier height theoretically. In the data analysis of this work, we followed the method adapted by Amman [41] and treated the barrier height as a parameter to be determined from electrical measurements. To measure the barrier height from the data, Eqs. 1 and 2 can be rewritten as:

\[
kT \ln\left(\frac{J}{A^* T^2}\right) = -\varphi_h + b_1 \sqrt{V_d} \quad \text{with } b_1 = \sqrt{2qN_d/N_f}
\]
3 Experimental Methods

3.1 Detector fabrication

For the study in this work, we have fabricated three planar Ge detectors, USD-R02, USD-R03 and USD-W03, with a guard-ring structure on the top surface of each detector. As an example, Fig. 3 (left) shows the top view of one of the guard-ring detectors, USD-R03. Fig. 3 (right) presents the schematic cross-sectional view of a typical guard-ring detector fabricated at USD. For the details about how to convert an HPGe crystal into a planar detector with a guard-ring structure shown in Fig. 3, please refer to our previous work [42, 43]. Due to more uncertain handling processes involved before the a-Ge coating on the bottom contact, it is expected that the top and bottom contacts may not have the same quality. The dimensions of the three guard-ring detectors fabricated at USD for this study are shown in Table 1.

3.2 Detector characterization

After each detector was fabricated, it was loaded in a variable-temperature sample cryostat as shown in Fig. 4. This cryostat is provided by LBNL. The small size of this cryostat makes for faster vacuum pumping and cooling to base temperature. The variable-temperature stage shown in Fig. 4 has a temperature sensor and a small heater attached so that the temperature of this stage can be uniformly elevated above the liquid nitrogen temperature. The base temperature is about 79 K, while the maximum is in excess of 200 K [32] with the LakeShore 335 temperature controller shown in Fig. 5. Also shown in Fig. 5 are the required signal processing electronics and measurement electronics to conduct electrical and spectroscopy measurements. The diagram presented in Fig. 6 shows how we performed the electrical and spectroscopy measurements using the electronics shown in Fig. 5. The detector was virtually grounded through the transimpedance amplifier.

To extract the barrier height by using the theoretical model (Eqs. 5 and 6) described in section 2, the $I$-$V$ (current-voltage) curve needs to be measured for each detector. To validate the current-voltage data from each detector used in this work, it is necessary to verify that each detector is a workable detector. The following measurements have been conducted for each detector operated at $\sim$79 K for this verification: (1) leakage current as a function of the bias voltage ($I$-$V_L$) from both guard-ring and center contacts; (2) capacitance as a function of the bias voltage ($C$-$V_C$) from center contact; (3) spectroscopy measurement with a radiation source of Cs-137 from center contact. The leakage current level reflects the quality of the a-Ge contacts. The $C$-$V_C$ measurements allowed us to determine the full depletion voltage of the detector and the impurity concentration of the crystal. The energy resolution information can be obtained from the spectroscopy measurement. More details about how we conducted the electrical ($I$-$V_D$, $C$-$V_C$) and spectroscopy measurements with the electronics shown in Fig. 5 are stated in our previous work [42]. The testing results including the full depletion voltage ($V_D$), the leakage current at full depletion voltage ($I_L$) at the center contact, crystal impurity concentration from $C$-$V_C$ measurements, the full width at half maximum (FWHM) at 662 keV and the FWHM of a pulser.
peak, which determines the noise level of the detector, are shown in Table 2 for each detector. As an example, Fig. 7 and Fig. 8 show the C-Va curve and the energy spectrum of Cs-137 source measured by the detector USD-R03 at 79 K. Also shown in Fig. 8 is an artificial peak due to the injected pulses from the high voltage line to measure the detector noise in terms of FWHM.

4 Data Analysis and Results

When collecting leakage-current data at a given temperature for each detector, the detector depletion process can either start from the top or bottom contact depending on the polarity of the bias voltage applied to the detector. With the detector configuration shown in Fig. 4, a p-type detector starts to deplete from the top (bottom) contact with a negative (positive) bias voltage applied to the bottom contact. As mentioned in section 2, if a detector can be fully depleted with the depletion starting from the top contact, one can determine \( \phi_h \) and \( N_f \) for the top contact and \( \phi_e \) and \( N_f \) for the bottom contact by fitting the \( J-V_a \) data to Eqs. 5 and 6. Similarly, if a detector can be fully depleted with the depletion starting from the bottom contact, then \( \phi_h \) and \( N_f \) for the bottom contact and \( \phi_e \) and \( N_f \) for the top contact can be determined as well. That is, \( \epsilon_h \), \( \epsilon_e \) and \( N_f \) can all be estimated if the detector can be fully depleted when depleting from both top and bottom contacts.

Based on our \( J-V_a \) measurements, detectors USD-R02 and USD-R03 can be fully depleted only when the depletion started from the top contact since the bottom contact cannot withstand high electric field penetration. For detector USD-W03, it can be fully depleted with depletion starting from both top and bottom contacts. Thus, for both detectors USD-R02 and USD-R03, we are able to determine \( \phi_h \) and \( N_f \) for the top contact and \( \phi_e \) and \( N_f \) for the bottom contact, while for detector USD-W03, we are able to determine \( \epsilon_h \), \( \epsilon_e \) and \( N_f \) for each contact. In this work, the detector USD-R03 was used as an example to show how \( \phi_h \) and \( N_f \) for the top contact and \( \phi_e \) and \( N_f \) for the bottom contact were determined. Fig. 9 shows the measured center contact leakage current density as a function of bias voltage at 90 K from the detector USD-R03. By fitting the plotted data of \( kT \ln \left( \frac{J}{(A^*T^2)} \right) \) as a function of \( V_a \) below full depletion to Eq. 5 with \( k = 8.62 \times 10^{-5} \) eV/K, \( T = 90 \) K, \( A^* = 48 \) A/cm²/K², \( q = 1.6 \times 10^{-19} \) C, \( N_d = 3.78 \times 10^{10} \) cm⁻³, as shown in Fig. 10, we were able to determine \( \phi_h \) and \( N_f \) for the top contact and \( \phi_e \) and \( N_f \) for the bottom contact. Using the parameters extracted from the fit shown in Fig. 10, the hole contribution to leakage current can be estimated for all applied voltage values (red line in Fig. 11) and subtracted from the \( J-V_a \) data. At this point, only leakage current from electron injection at the bottom contact remains and there should be no current below full depletion voltage, which are the black dots in Fig. 11. The values of \( \phi_e = 0.28 \) eV and \( N_f = 1.50 \)
Table 2 A summary of detector performance for three guard-ring detectors used in this work. $V_d$ and $I_d$ denote the full depletion voltage and the measured center contact leakage current at full depletion voltage, respectively. The FWHM at the pulser peak represents the detector noise level.

| Detectors | $V_d$ (V) | $I_d$ (pA) | Crystal impurity concentration from C-V measurements ($\text{cm}^{-3}$) | FWHM at 662 keV (keV) | FWHM of pulser peak (keV) |
|-----------|---------|-----------|-------------------------------------------------|-----------------|-----------------|
| USD-R02   | 700     | 1         | $2.93 \times 10^{10}$ | 1.57            | 1.01            |
| USD-R03   | 1400    | 1         | $3.78 \times 10^{10}$ | 2.12            | 1.23            |
| USD-W03   | 1300    | 1         | $2.60 \times 10^{10}$ | 2.35            | 1.33            |

Fig. 9 Measured leakage current density plotted as a function of bias voltage at 90 K for detector USD-R03 with the configuration shown in Fig. 4.

×10^{18} \text{eV}^{-1}\text{cm}^{-3} \text{ for the bottom contact can then be obtained by fitting the plotted data of } kT\ln(J/(A^*T^2)) \text{ as a function of } V_d \text{ after full depletion to Eq. 6 with } V_d = 1400 \text{ V, } \varepsilon_0 = 8.85 \times 10^{-14} \text{ C/V/cm and } \varepsilon_{Ge} = 16 \text{ and } t = 0.81 \text{ cm, as shown in Fig. 12. To reduce the systematic uncertainty in the determination of } \phi_b, \phi_e \text{ and } N_f, J-V_d \text{ characteristics were measured at several different temperatures for each detector. Table 3 shows the average values of } \phi_b, \phi_e \text{ and } N_f \text{ for all temperatures for the corresponding a-Ge contact on each detector. The error quoted for each value represents the difference between the average value and the individual value obtained at different temperatures. The small differences among the values of } \phi_b, \phi_e \text{ and } N_f \text{ for each of the guard-ring detector indicates that our detector fabrication process is consistent and reliable (see Table 3).}

5 Discussion and Prediction

Since the fabrication of Ge detectors with a-Ge contacts has been demonstrated to be consistent and reliable at USD, we can predicate the bulk leakage at liquid helium temperature (~4 K) assuming that the charge barrier height and the density of states near the Fermi energy level are independent of temperature below 77 K. As an example shown in Fig. 13, the parameters of the barrier height and the density of localized energy states for each contact have been used to predict the leakage as a function of temperature using the the Döhler-Brodsky model. The result shows that the bulk leakage quickly approaches nearly zero when temperature approaches 4 K. Based on the leakage current density predicted in Fig. 13, we can also predict the number of electrons injected at the contacts as a function of the electrical field at 4 K for a PPC Ge detector with 7 cm in diameter and 5 cm in height. The area of the point contact is assumed to be 0.01 cm$^2$ and the data-taking time is assumed to be one year (see Fig. 14).
The values of $\phi_h$, $\phi_e$ and $N_f$ determined by fitting the plotted data of $kT \ln(J/(A^* T^2))$ as a function of $V_a$ to eqs. 5 and 6 for the corresponding a-Ge contact on each detector. For the top contact of the detector, USD-R02, due to a flat distribution of the $J-V_a$ data before full depletion, it was safe to assume no electrical field penetration into the contact, i.e. $\Delta \phi_h = 0$ or $N_f \rightarrow \infty$.

| Detectors | Top Contact | Bottom Contact |
|-----------|-------------|----------------|
| USD-R02  | $\phi_h = (0.31 \pm 0.01)$ eV | $\phi_e = (0.30 \pm 0.00)$ eV |
|           | $N_f = (4.68 \pm 3.32) \times 10^{17}$ eV$^{-1}$cm$^{-3}$ | $N_f = (4.68 \pm 3.32) \times 10^{17}$ eV$^{-1}$cm$^{-3}$ |
| USD-R03  | $\phi_h = (0.285 \pm 0.005)$ eV | $\phi_e = (0.28 \pm 0.00)$ eV |
|           | $N_f = (4.34 \pm 0.11) \times 10^{18}$ eV$^{-1}$cm$^{-3}$ | $N_f = (4.34 \pm 0.11) \times 10^{18}$ eV$^{-1}$cm$^{-3}$ |
| USD-W03  | $\phi_h = 0.31$ eV | $\phi_e = (0.295 \pm 0.005)$ eV |
|           | $\phi_e = (0.31 \pm 0.00)$ eV | $\phi_e = (0.29 \pm 0.00)$ eV |
|           | $N_f = (2.25 \pm 0.02) \times 10^{18}$ eV$^{-1}$cm$^{-3}$ | $N_f = (1.94 \pm 0.04) \times 10^{18}$ eV$^{-1}$cm$^{-3}$ |

**Fig. 12** A fit of the plotted data of $kT \ln(J/(A^* T^2))$ as a function of $V_a$ above full depletion to Eq. 6. Based on the fit, the two free parameters in Eq. 6 were determined to be, $\phi_e = 0.28$ eV and $b_2 = 2.76 \times 10^{-6}$ e.

**Fig. 13** Calculated center contact leakage current density from hole injection at the top contact and electron injection at the bottom contact of the detector, USD-R03, at a negative bias voltage of 2000 V with the configuration shown in Fig. 4. The leakage current density was estimated based on the contact model parameters extracted from the fits to the measured data shown in Fig. 10 and Fig. 12.

As can be seen in Fig. 14, the number of charge carriers injected from the contacts are so small (nearly 0) for a PPC detector at a high field up to $10^5$ V/cm.

**6 Conclusions**

Three guard-ring detectors fabricated from USD-grown crystals are used to measure the bulk leakage current. By applying a well-understood Richardson constant into the Döbler-Brodsky model, we have determined the charge barrier height for electrons and holes separately for the top and bottom contacts of three detectors. The density of localized energy states near the Fermi level has also been obtained for the top and bottom contacts of the three detectors. We conclude that the bulk leakage current at helium temperature is negligible, as shown in Fig. 13. As we stated earlier, the thermal emission in the bulk of Ge detector is extremely low at $\sim 4\, \text{K}$, corresponding to a negligible level. The surface leakage is inversely proportional to the resistivity of a-Ge, corresponding to a level of $\sim \text{pA}$ at nitrogen temperature. Using a guard-ring structure, the surface leakage current can be separated from the bulk leakage current. Since the surface leakage current has a strong dependence on temperature due to the resistance increases as temperature decreases, the surface leakage current is expected to be nearly zero at $\sim 4\, \text{k}$.

Thus, the surface leakage will not contribute to the charge read-out from the central contact. Therefore, we conclude that the Ge detectors with a-Ge contacts possess the potential to achieve the sensitivity to measure a single e-h pair, which can be created by extremely low-energy recoils induced by LDM in terms of an extremely small bulk leakage current at liquid helium temperature, as shown in Fig. 14.
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