Cosmologically Viable Low-energy Supersymmetry Breaking

Anson Hook
Maryland Center for Fundamental Physics, Department of Physics
University of Maryland, College Park, Maryland 20742, USA

Robert McGehee
Department of Physics, University of California, Berkeley, California 94720, USA and
Theoretical Physics Group, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA

Hitoshi Murayama
Department of Physics, University of California, Berkeley, California 94720, USA
Theoretical Physics Group, Lawrence Berkeley National Laboratory, Berkeley, California 94720, USA and
Kavli Institute for the Physics and Mathematics of the Universe (WPI),
University of Tokyo Institutes for Advanced Study, University of Tokyo, Kashiwa 277-8583, Japan

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A recent cosmological bound on the gravitino mass, $m_{3/2} < 4.7$ eV, together with LHC results on the Higgs mass and direct searches, excludes minimal gauge mediation with high reheating temperatures. We discuss a minimal, vector-mediated model which incorporates the seesaw mechanism for neutrino masses, allows for thermal leptogenesis, ameliorates the $\mu$ problem, and achieves the observed Higgs mass and a gravitino as light as 1–2 eV.

I. INTRODUCTION

Supersymmetry (SUSY) is a well motivated theory beyond the standard model. It offers a solution to the hierarchy problem and allows for gauge unification (see, e.g., [1]). Models with SUSY breaking at low energies are especially interesting because they imply light gravitinos which can be produced at colliders, enabling experimental tests of the SUSY-breaking mechanism [2]. Gauge mediation is the most studied way to do this [3–5].

However, the window on usual gauge mediation is quickly closing as cosmological and LHC bounds eliminate parameter space from both ends. Decreasing upper bounds on the gravitino mass from cosmological data are decreasing the upper bound on the SUSY-breaking scale, $\sqrt{F}$, because $m_{3/2} = F/\sqrt{3}M_P$. Increasing bounds on the gaugino masses from the LHC and the 125 GeV Higgs mass are simultaneously increasing the lower bound on $\sqrt{F}$.

For most of the gravitino-mass range, if it is the stable Lightest Supersymmetric Particle (LSP), it overcloses the Universe without an unnaturally low reheating temperature [6, 7]. Such a low reheating temperature makes baryogenesis difficult as well. In particular, thermal leptogenesis requires $T_R > 10^9$ GeV [8]. A very light gravitino, $m_{3/2} < 0.24$ keV, does not overclose the Universe even when it is thermalized. But it constitutes a hot (or warm) dark matter component and suppresses the structure of the Universe at small scales. According to a very recent study, CMB lensing and cosmic shear constrain its mass to be $m_{3/2} < 4.7$ eV [9]. Fig. 1 summarizes these cosmological bounds on $m_{3/2}$, as well as others, and demonstrates the shrinking parameter space for any models with gravitinos lighter than roughly $10^5$ GeV.

In minimal, gauge-mediated models, on the other hand, the 125 GeV Higgs mass requires a large stop mass. This implies $\sqrt{F} \gtrsim 10^3$ TeV. Hence, the gravitino is heavier than 300 eV for one messenger or 60 eV for five messengers, which is the maximum number allowed by perturbative gauge unification [13]. Therefore, minimal, gauge-mediated models are excluded if the reheating temperature is high.

This gravitino problem is often ignored in literature which attempts to achieve the 125 GeV Higgs mass via gauge mediation, e.g., using $A$ terms from RGE flow [14] or non-decoupling $D$ terms [15, 16]. A non-minimal Higgs sector or strongly coupled messengers may achieve $m_{3/2} \lesssim 16$ eV [17], but it is unclear if the gravitino mass can be pushed below 4.7 eV. These problems can be ameliorated by using the Next-to-Minimal Supersymmetric Standard Model (NMSSM) or Dirac-NMSSM [18], coupling the Higgs to messengers [19], or having a strongly coupled messenger sector [20–23]. However, these models are quite intricate.

In this paper, we elaborate on a simple, vector-mediated model proposed by Hook and Murayama which breaks SUSY at tree level with a $U(1)$ $D$ term and evades all gravitino bounds [24]. We discuss electroweak symmetry breaking (EWSB) in detail to obtain the correct Higgs mass while avoiding all LHC bounds on Minimal Supersymmetric Standard Model (MSSM) particles. We also introduce a new, $U(1)$ charge assignment where the righthanded neutrino is neutral to allow the seesaw mechanism for neutrino masses and thermal leptogenesis [25]. Additionally, this model produces a split spectrum usually found in gravity-mediated models [26].

*hook@umd.edu
robertmcgehee@berkeley.edu
hitoshi@berkeley.edu
hitoshi.murayama@ipmu.jp
We first review the basics of SUSY breaking via vector mediation. If we want a cosmologically viable, light gravitino and a naturally high reheating temperature, Fig. 1 clearly shows it must be very light. A first attempt is to use a low-energy, gauge-mediated model. However, normal, gauge-mediated models have gaugino and scalar masses at loop level. Then the low, SUSY-breaking scale results in spartners too light for the current LHC bounds. Thus, we want a low-energy, gauge-mediated model with scalar masses at tree level.

However, there is a “no-go theorem” against models which break SUSY at tree level [30–32]. The problem is the tree-level identity $\text{STr}(M^2) = 0$ which usually implies SUSY breaking cannot occur at the tree level. This is because anomaly cancellation requires both positive and negative $U(1)$ charges which gives some scalars negative soft masses at tree level from a $U(1)$ $D$ term.

In vector mediation, there are vector-like messenger fields. We assign positive $U(1)$ charges to all sfermions and negative charges to all vectorlike messengers. Their vectorlike masses overcome their negative soft masses so that no scalars are tachyonic. Thus, vector mediation allows tree-level scalar masses and a lower SUSY-breaking scale. This gives a lighter gravitino while getting the Higgs mass correct and avoiding current bounds on MSSM particles. The lower scale also ameliorates the so-called $\mu$ problem.

II. THE MODELS

The vector-mediated models [24] employ an $E_6$-inspired particle content that consists of three families of the fundamental representation decomposed into $SO(10) \times U(1)_V$ as

$$27 = \Psi(16, +1) \oplus \Phi(10, -2) \oplus S(1, +4),$$

where $\Psi$ contains the SM fermions and $\Phi$ contains two families of messengers and the MSSM Higgs doublets at tree level, but at the GUT scale. This resulted in a very weakly coupled gravitino and thus, very different collider and cosmology signatures [33].
with their color triplets. Because the messengers and Higgs color triplets have different couplings than the Higgs doublets, we distinguish between generations using subscripts with $\Phi_i \equiv (T_a, H_u) + (T_d, H_d)$ where $T$ are the color triplets. Since these Higgs color triplets’ masses are not at the grand-unified-theory scale, they prevent gauge unification. However, we can add two new electroweak doublets, uncharged under our $U(1)$, with the same mass as the Higgs color triplets in order to form complete $SU(5)$ multiplets and restore gauge unification. We also include a neutral particle $Z(0)$ and a vectorlike multiplet charged under $U(1)_Y$, $X(-4)$ and $Y(+4)$. These particles are responsible for SUSY breaking.

The superpotential for our model is

$$W = MSX + \lambda Z (XY - v_S^2)$$

$$- 2T_u T_d \left( \frac{g}{2} Y + \frac{k}{2} S \right) - 2H_u H_d \left( \frac{g_H}{2} Y + \frac{k_H}{2} S \right)$$

$$- \sum_{a=2}^{3} \Phi_a \cdot \Phi_a \left( \frac{g}{2} Y + \frac{k}{2} S \right)$$

$$+ \frac{\lambda S}{2} \sum_{a=2}^{3} \Phi_a \cdot \Phi_a \sum_{b=1}^{2} S_b + \kappa X \sum_{a=1}^{2} N_a S_a. \quad (2)$$

The three generations of $S$ are denoted $S_1$, $S_2$ and $S_3$. The first line in Eq. (2) breaks SUSY with an $F$ term and a positive $D$ term. The second and third lines are standard messenger interactions and generate the usual, gauge-mediated gaugino masses at one loop. We have allowed the MSSM Higgs doublets, $H_u$ and $H_d$, to have different couplings to $Y$ and $S$ than their color triplets, $T_u$ and $T_d$, in order to satisfy EWSB conditions. Each generation of $\Phi$ could have different couplings to $Y$ and $S$, but we set them equal to maximize the gaugino masses (see sect III). The fourth line gives the $S_{1,2}$ fermions masses by introducing two neutral fields $N_{1,2}$, while the $S_{1,2}$ scalars also acquire a mass from the $D$ term. We have the interaction $W \supset S_{1,2} \Phi \Phi$ in line four to allow $S_{1,2}$ and $N_{1,2}$ to decay so that they don’t overclose the universe.

We do not use the usual $\mu$-term as it is not gauge invariant under $U(1)_Y$. Similar to the NMSSM, it is generated by the expectation values of $Y$ and $S$. We introduce the interaction $W \supset QT_d H_d$ to allow for the color triplets in $\Phi$ to decay. In order to prevent proton decay, we assign negative matter-parity to all SM fermions in $\Psi$ and to the color triplets in $\Phi$, but positive matter-parity to the electroweak doublets in $\Phi$.

In this paper, we consider two different charge assignments under a new $U(1)$: the original-charge assignment corresponding to $U(1)_Y$ and a new, seesaw-charge assignment corresponding to a different $U(1)_{SS}$. For clarity, we distinguish between these charge assignments using these subscripts and omit a subscript when talking about either charge assignment generally. We explore the viability of models with each of these charge assignments separately.

### III. Constraints Prior to EWSB

We explore the parameter space $(e, M, \lambda, v_S, \chi, k, g, k_H, g_H, \tan \beta)$ for both charge
assignments to find viable models with light gravitinos which avoid the cosmological bound \( m_3/2 < 4.7 \text{eV} \). Before we verify EWSB and the Higgs mass, we must impose some constraints on our parameter space. The first suppresses tunneling to the true vacuum.

The interactions in lines two and three of Eq. (2) which give rise to the gaugino masses at one loop also generate a supersymmetric vacuum. This true vacuum appears at

\[
X_0 = \frac{v^2}{2}\frac{k\Phi_0}{M}, \quad Z_0 = gM, \quad S_0 = -\frac{2gMv^2}{k^2 \Phi_0^2},
\]

where \( \Phi_0 \) is set by requiring the \( D \) term vanishes. We require the parameter space we consider to disallow substantial vacuum or thermal tunneling between the false and true vacua.

Before we verify EWSB and the Higgs mass, we must use the high-temperature approximation for the thermal bounce action, which avoids the cosmological bound \( m_3/2 \). We verify that \( S_{\text{Tr}} (M^2) = 0 \) along the straight line between the true and false vacua. We set \( \kappa = 0.1 \) for concreteness.

To illustrate that the vacuum and thermal tunneling rates are highly suppressed, we have chosen the representative values \((M = 2, \lambda = 4\pi, \chi = 0, k = 4\pi) \) and set \( g \) as small as possible before the lightest messengers go tachyonic (see Eq. (12) below). See Fig. 2 and Fig. 3.

\[
\Gamma \propto \exp \left( \frac{B}{C} \right)
\]

Figure 2. Vacuum bounce action for both charge assignments. We take the representative values \((M = 2, \lambda = 4\pi, \chi = 0, k = 4\pi) \) and set \( g \) as small as possible before the lightest messengers go tachyonic. We easily satisfy \( B > 450 \) for the Universe to be stable.

Both vacuum and thermal tunneling actions are approximately independent of \( \chi \) over the range of values we consider later. While \( \chi = 0 \) is not viable for the seesaw-charge assignment due to EWSB failure, these figures do not change for realistic values of \( \chi \). We allow different values of \((M, \lambda, \chi) \) when conducting a full parameter-space search. However, we always take \( k = 4\pi \) and minimize \( g \) in order to maximize the gaugino masses (see III).
Both actions are dramatically larger than in Ref. [24] because we are considering much smaller values of $e$. One can guess that a smaller value of $e$ makes the bounce actions much larger because when $e \to \infty$, $\Phi$ is tachyonic and there is no barrier between the false and true vacua. As there is a barrier for small $e$, by continuity, one expects that smaller $e$ gives larger barriers. In the limit $e \to 0$, we numerically find that the barrier height between the two vacua increases. This is the thin-wall limit and the bounce actions increase dramatically [37–49].

The scalar potential along the straight-line, tunneling path is quartic in one scalar field. This potential is characterized by a single, dimensionless parameter $\delta$ which can take values between 0 and 2 [38]. The thin-wall limit corresponds to the limit $\delta \to 2$. In this limit, the analytic, vacuum bounce action is proportional to $(2 - \delta)^{-3}$ and the analytic, thermal bounce action is proportional to $(2 - \delta)^{-2}$. For the parameters taken in Ref. [24], $\delta = 1.6$. We consider points in parameter space which are much closer to the thin-wall limit with $\delta \geq 1.996$.

The gaugino masses are generated from one-loop diagrams with the messengers in the three families of fields. All fermions in $\Phi$ have the same mass $M_{\Phi} = g Y_0$. Taking into account the kinetic mixing in Eq. (7), the boson components all have the mass matrix

$$
\begin{pmatrix}
M^2_{\Phi} + Q_{H_u} e D + Q^Y_{H_u} g' \chi D \\
k_F S
\end{pmatrix} =
\begin{pmatrix}
k_F S \\
M^2_{\Phi} + Q_{H_d} e D - Q^Y_{H_u} g' \chi D
\end{pmatrix},
$$

where $Q_{H_u}$ is the $U(1)$ charge of fields in the 5 of $\Phi$, $Q_{H_d}$ is the charge of fields in the 5 of $\Phi$, $F_S = M X_0$, and $D = e Q_X (X^T \delta^X - Y^T \delta^Y) > 0$. $Q_X = -Q_Y$ since $X$ and $Y$ form a vectorlike multiplet. For the bosons in the color triplets, this is the correct mass matrix under the appropriate replacement $Q^Y_{H_u} = +1 \to Q^Y_D = -\frac{1}{3}$. We leave the $U(1)$ charges unspecified since we find viable models for both charge assignments. The MSSM Higgses have the same mass matrix under the replacement $k \to k_{\Phi}, g \to g_H$ (see Eq. (4)).

We calculate the one-loop gaugino masses using Eq. (2.3) in Ref. [41]. All three families’ color triplets and electroweak doublets contribute to the gaugino masses. The on-shell gluino mass enhancement from $(s)$top loops is calculated using SOFTSUSY (discussed below) [46–49].

The gaugino masses are maximized when there is a large mass hierarchy in Eq. (12). We ensure a large hierarchy by choosing parameters where the lighter scalar is light ($\approx 1$ TeV). The gaugino masses are also proportional to the fermion masses so we prefer larger $g$ and larger $Y_0$. In order to increase the gaugino masses in units of $v_S$, we thus set $k = 4\pi$ and choose $g$ such that the lighter scalar in Eq. (12) is near 1 TeV. These are the prescriptions we used in Figs. (2) and (3) and allow smaller $v_S$.

We set $v_S$ by satisfying all current, gaugino-mass bounds. The ATLAS bound on the gluino mass is roughly 2.03 TeV [12], while the CMS bound is 1.95 TeV [43]. The ATLAS bound on the Wino mass is roughly 620 GeV, unless the Bino is heavier than 350 GeV, in which case it is 720 GeV [44]. The Wino bound is the most stringent from direct searches. So, we use it to estimate $v_S$ before EWSB. But we find getting the correct Higgs mass is generally harder and therefore, determines $v_S$ after EWSB (see below).

The gravitino mass is given by

$$m_{3/2} = \frac{V}{3M_{Pl}^2},$$

where $M_{Pl} = 2.4 \times 10^{18}$ GeV. For a viable model, we require $m_{3/2} < 4.7$ eV [9].

We always set $\chi$ negative to make $m_{3/2}$ lighter and help EWSB (see Eq. (12)). Since $\tilde{\epsilon}$ has the greatest $U(1)_Y$ charge, $\tilde{Q}_e = +1$, we determine how negative $\chi$ can be by requiring that $\tilde{\epsilon}$ is not tachyonic.

We also require that the massive $U(1)$ boson does not mix too much with $W$ and $Z$ to affect the $\rho$ parameter. We conservatively require that $\delta \rho < 10^{-3}$ which imposes that $(\frac{\epsilon v}{M_{Pl}^2})^2 < 10^{-3}$, where $\epsilon$ is the Higgs vacuum expectation value and $M_{Pl}$ is the mass of our $U(1)$ boson [45].

**IV. CONSTRAINTS AFTER EWSB**

We use SOFTSUSY to calculate radiative EWSB. Our inputs into SOFTSUSY are the gaugino masses, trilinear couplings, sfermion masses, $m^2_{H_u}$, $m^2_{H_d}$, and $\tan \beta$. We can read off the MSSM Higgs parameters from Eq. (12):

$$
\mu = g_H Y_0, \quad m^2_{H_u} = Q_{H_u} e D + \frac{1}{2} g' \chi D, \quad B_H = k_{\Phi} F_S, \quad m^2_{H_d} = Q_{H_d} e D - \frac{1}{2} g' \chi D.
$$

The soft, SUSY-breaking $A$ terms are all 0 in our models at tree level. SOFTSUSY effectively sets $\mu$ and $B_H$ as output boundary conditions and therefore, $k_{\Phi}$ and $g_H$ in our models.

We only input the above boundary conditions at tree level. We input the gaugino masses at one-loop level, but do not include QCD enhancements to $M_3$ or other, higher-order corrections. This is slightly inconsistent as we run SOFTSUSY with the 3-loop renormalization group equations and calculate the lightest MSSM Higgses both at 2-loop and 3-loop level. When calculating the Higgses at 3-loop, SOFTSUSY also defaults to adding 2-loop Yukawa and $g_3$ threshold corrections to $m_t$ and $m_b$.

EWSB itself is a strong constraint. If a point in parameter space has successful radiative EWSB, there are still many additional constraints we check before considering it viable. In order to approximate EWSB using SOFTSUSY, the correction to the MSSM, Higgs-quartic coupling, $\lambda_h = m_h^2/v^2$, must be sufficiently small. We

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5 R. M. thanks Simon Knapen on this point.
require our Higgs mass to be accurate to 0.5 GeV. This places an upper bound at roughly
\[ \delta \lambda_h = g_R^2 + \frac{1}{2} Q_R^2 e^2 + \frac{1}{2} g' \chi < 0.002. \] (15)
This is a conservative limit because the quartic couplings due to the $F$ term and the $D$ term of heavy fields decouple and the effect is in general smaller. We do not bother including a term proportional to $k_H^2$ since $k_H \ll g_R^2$ generically. Eq. (15) is also conservative because the $g_R^2$ piece vanishes in the limit of large or small $\tan \beta$. Due to the upper bound on $\delta \lambda_h$, Eq. (15) lets us only consider $\epsilon < 0.021$. We find viable models only occur for smaller values of $\epsilon$. This a nontrivial check because $(k_H, g_H)$ are set by the output boundary conditions from SOFTSUSY.

Requiring the Higgs mass to be 125 GeV is the strongest constraint and sets the overall scale $v_S$ in our models. If $v_S$ is set to satisfy the gaugino constraints, the stop masses are too light to lift the Higgs mass. When searching for viable models, we estimate $v_S$ by satisfying the Wino constraint and then explore parameter space by increasing this $v_S$ by some factor between $\sim 2 - 3$.

We require that the output top Yukawa is still perturbative. We calculate $y_t$ using Eq. (62) in Ref. [50] using the top mass in Ref. [51]. We require that $y_t < 0.94$. We also require that the other neutral scalar Higgses are not too light. As a conservative constraint, we require the mass of the heavier CP-even neutral scalar, $H^0$, to be larger than 580 GeV [52]. We require the mass of the CP-odd neutral scalar, $A^0$, to avoid the $\tan \beta$-dependent, ATLAS bounds in Fig. 10 b of Ref. [53].

Since SOFTSUSY includes loop corrections to the gluino, we make sure the output gluino is still heavier than 2.03 TeV. SOFTSUSY also gives the spectrum of the neutralinos and charginos. We make sure to avoid the bound on $\tilde{\chi}_1^2$ and $\tilde{\chi}_2^0$ as a function of $\tilde{\chi}_1^0$ given in Ref. [44].

V. SUSY SPECTRA AND BEST MODELS

Fig. 4 shows our search through parameter space for viable models with the seesaw-charge assignment, $Q_{SS}$, and the original-charge assignment, $Q_O$. The points correspond to viable points in the parameter space $(e, M, \lambda, v_S, \chi, k, g, k_H, g_H, \tan \beta)$ for which all of the constraints are satisfied. We show viable points when we calculate the Higgs mass at both the 2-loop and 3-loop level in SOFTSUSY. The 3-loop calculation generally yields a lighter Higgs which requires a greater $v_S$ to obtain 125 GeV. This yields a heavier gravitino and explains the separation of viable points between the 2-loop and 3-loop calculations.

For the seesaw-charge assignment, $\chi$ is always close to its maximum value to help alleviate $m_{H_u}^2 > m_{H_d}^2$. However, it is not possible to take $\chi$ large enough to make $m_{H_u}^2 \leq m_{H_d}^2$ without making $\tilde{\epsilon}$ tachyonic. EWSB works due to negative, one-loop corrections to $m_{H_u}^2$ from (s)tops at the geometric mean of the stop masses. In particular, the one-loop corrections to $m_{H_u}^2$ from the (s)tops are
\[ \Delta m_{H_u}^2 = \frac{N_C y_t^2}{(4\pi)^2} \left( m_{\tilde{t}_R}^2 \ln \frac{m_{\tilde{t}_R}}{\mu^2} + m_{\tilde{t}_L}^2 \ln \frac{m_{\tilde{t}_L}}{\mu^2} \right) \]
\[ - m_{\tilde{t}_R}^2 - m_{\tilde{t}_L}^2, \] (16)
where $N_C = 3$ is the number of colors. At the renormalization scale, $\mu_R^2 = m_{\tilde{t}_R}^2 m_{\tilde{t}_L}^2$, this correction is negative as long as the stop masses are not too separated. This negative correction, in addition to the kinetic mixing $\chi$, enables EWSB in models with the seesaw-charge assignment.

Fig. 5 shows why representative points in parameter space are excluded by the aforementioned constraints for the seesaw-charge and original-charge assignments when we calculate the Higgs mass at the 3-loop level. The most exclusive constraint is getting the Higgs mass correct. Points toward the bottom and left of these figures correspond to a Higgs which is too light. For the seesaw-charge assignment, the other MSSM Higgs scalars are often too light when the Higgs is too light. Points to the far right are excluded because $\delta \lambda_h$ from Eq. (15) is too large and the MSSM approximation breaks down.

The viable models with the lightest gravitinos are illustrated in Fig. 6. The equivalent figures with $m_h$ calculated at the 3-loop level are similar, with their spectra shifted slightly up.

SOFTSUSY requires $\mu$ to be 9.74 TeV and 11.4 TeV for the original- and seesaw-charge assignments, respectively, reducing the $\mu$ problem from the Planck scale to the 10-TeV scale. One might be confused that the gauginos are near the sfermions. This is simply an artifact of maximizing the gaugino masses in units of $v_S$ before EWSB. The lightest gravitino masses for these 3-loop calculations are 1.9 eV and 2.3 eV for the original- and seesaw-charge assignments, respectively. Optimistically, we see that we can obtain gravitino masses as light as 1.0 eV and 1.4 eV for the original- and seesaw-charge assignments when we calculate the Higgs at 2-loop level. Even being conservative and calculating the Higgs mass at the 3-loop level still yields a sufficiently light gravitino to evade the current cosmological bound $m_{3/2} < 4.7$ eV.

VI. CONCLUSION - DISCUSSIONS

We expand on the previous work of Hook and Murayama by finding models with lighter gravitinos, calculating EWSB, and enabling EWSB in models with the new, seesaw-charge assignment by introducing $U(1)$ kinetic mixing. Unlike typical, gauge-mediated models, we find that our vector-mediated models are cosmologically viable with light gravitinos. As can be extrapolated from Fig. 4 going to larger values of $\epsilon$ generally allows for lighter gravitinos. Since we use SOFTSUSY
to approximate EWSB in our models, we only consider \( e \leq 0.01 \) to avoid invalidating this approximation. If we calculate EWSB without SOFTSUSY, we cannot consider values of \( e \) much larger because the vacuum and thermal tunneling rates begin to matter. For values of \( e \geq 0.1 \), we can no longer choose \( k \) and \( g \) to maximize the gaugino masses with respect to \( v_S \). Satisfying the gaugino-mass bounds then increases \( v_S \) which increases the gravitino mass. It is very interesting that the best we can do is not too far away from current cosmological limits. Near-future improvements in cosmological data, such as improvements in cosmic shear measurements at DES and Hyper Suprime-Cam, could completely rule out low-energy SUSY breaking.

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Figure 6. Low-lying spectra for the seesaw-charge and original-charge models with the lightest gravitino when $m_h$ is calculated at the 2-loop level.

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