Parameter estimation for agenda-based user simulation

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Abstract
This paper presents an agenda-based user simulator which has been extended to be trainable on real data with the aim of more closely modelling the complex rational behaviour exhibited by real users. The trainable part is formed by a set of random decision points that may be encountered during the process of receiving a system act and responding with a user act. A sample-based method is presented for using real user data to estimate the parameters that control these decisions. Evaluation results are given both in terms of statistics of generated user behaviour and the quality of policies trained with different simulators. Compared to a handcrafted simulator, the trained system provides a much better fit to corpus data and evaluations suggest that this better fit should result in improved dialogue performance.

1 Introduction
In spoken dialogue systems research, modelling dialogue as a (Partially Observable) Markov Decision Process ((PO)MDP) and using reinforcement learning techniques for optimising dialogue policies has proven to be an effective method for developing robust systems (Singh et al., 2000; Levin et al., 2000). However, since this kind of optimisation requires a simulated user to generate a sufficiently large number of interactions to learn from, this effectiveness depends largely on the quality of such a user simulator. An important requirement for a simulator is for it to be realistic, i.e., it should generate behaviour that is similar to that of real users. Trained policies are then more likely to perform better on real users, and evaluation results on simulated data are more likely to predict results on real data more accurately.

This is one of the reasons why learning user simulation models from data on real user behaviour has become an important direction of research (Scheffler and Young, 2001; Cuayáhuítl et al., 2005; Georgila et al., 2006). However, the data driven user models developed so far lack the complexity required for training high quality policies in task domains where user behaviour is relatively complex. Handcrafted models are still the most effective in those cases.

This paper presents an agenda-based user simulator which is handcrafted for a large part, but additionally can be trained with data from real users (Section 2). As a result, it generates behaviour that better reflects the statistics of real user behaviour, whilst preserving the complexity and rationality required to effectively train dialogue management policies. The trainable part is formed by a set of random decision points, which, depending on the context, may or may not be encountered during the process of receiving a system act and deciding on a response act. If such a point is encountered, the simulator makes a random decision between a number of options which may directly or indirectly influence the resulting output. The options for each random decision point are reasonable in the context in which it is encountered, but a uniform distribution of outcomes might not reflect real user behaviour.

We will describe a sample-based method for estimating the parameters that define the probabilities for each possible decision, using data on real users from a corpus of human-machine dialogues (Section 3). Evaluation results will be presented both in terms of statistics on generated user dialogues and the quality of dialogue policies trained with different user simulations (Section 4).

2 Agenda-based user simulation
In agenda-based user simulation, user acts are generated on the basis of a user goal and an agenda (Schatzmann et al., 2007a). The simulator presented here is developed and used for a tourist in-
formation application, but is sufficiently generic to accommodate slot-filling applications in any domain.\(^1\) The user goal consists of the type of venue, for example hotel, bar or restaurant, a list of constraints in the form of slot value pairs, such as food=Italian or area=east, and a list of slots the user wants to know the value of, such as the address (addr), phone number (phone), or price information (price) of the venue. The user goals for the simulator are randomly generated from the domain ontology describing which combinations of venue types and constraints are allowed and what are the possible values for each slot. The agenda is a stack-like structure containing planned user acts. When the simulator receives a system act, the status of the user goal is updated as well as the agenda, typically by pushing new acts onto it. In a separate step, the response user act is selected by popping one or more items off the agenda.

Although the agenda-based user simulator introduced by Schatzmann et al. (2007a) was entirely handcrafted, it was realistic enough to successfully test a prototype POMDP dialogue manager and train a dialogue policy that outperformed a handcrafted baseline (Young et al., 2009). A method to train an agenda-based user simulator from data was proposed by Schatzmann et al. (2007b). In this approach, operations on the agenda are controlled by probabilities learned from data using a variation of the EM algorithm. However, this approach does not readily scale to more complex interactions in which users can, for example, change their goal midway through a dialogue.

### 2.1 Random decision parameters

Each time the user simulator receives a system act, a complex, two-fold process takes place involving several decisions, made on the basis of both the nature of the incoming system act and the information state of the user, i.e., the status of the user goal and agenda. The first phase can be seen as an information state update and involves actions like filling requested slots or checking whether the provided information is consistent with the user goal constraints. In the second phase, the user decides which response act to generate, based on the updated agenda. Many of the decisions involved are deterministic, allowing only one possible option given the context. Other decisions allow for some degree of variation in the user behaviour and are governed by probability distributions over the options allowed in that context. For example, if the system has offered a venue that matches the user’s goal, the user can randomly decide to either change his goal or to accept the venue and ask for additional information such as the phone number.

The non-deterministic part of the simulator is formalised in terms of a set of random decision points (RDPs) embedded in the decision process. If an RDP is encountered (depending on the context), a random choice between the options defined for that point is made by sampling from a probability distribution. Most of the RDPs are controlled by a multinomial distribution, such as deciding whether or not to change the goal after a system offer. Some RDPs are controlled by a geometric distribution, like in the case where the user is planning to specify one of his constraints (with an inform act popped from the agenda) and then repeatedly adds an additional constraint to the act (by combining it with an additional inform act popped from the agenda) until it randomly decides not to add any more constraints (or runs out of constraints to specify). The parameter for this distribution thus controls how cautious the user is in providing information to the system.

Hence, the user simulator can be viewed as a ‘decision network’, consisting of deterministic and random decision points. This is illustrated in Figure 1 for the simplified case of a network with only four RDPs; the actual simulator has 23 RDPs, with 27 associated parameters in total. Each time the simulator receives a system act, it follows a path through the network, which is partly determined by that system act and the user goal and agenda, and partly by random decisions made according to the probability distributions for each random decision point \(i\) given by its parameters \(\theta_i\).

### 3 Training the simulator from data

The parameterisation of the user simulator as described in Section 2.1 forms the basis for a method for training the simulator with real user data. The parameters describing the probability distributions for each RDP are estimated in order to generate user behaviour that fits the user behaviour in the corpus as closely as possible. In order to do so, a sample based maximum likelihood approach is taken, in which the simulator is run repeatedly against the system acts in the corpus, and the random decisions that lead to simulated acts matching the true act in the corpus are recorded. The parameters are then estimated using the counts for each of the random decision points.
3.1 Parameter estimation

Before starting the process of matching simulated acts with true acts and collecting counts for the RDPs, the parameters are initialised to values corresponding to uniform distributions. Then, the simulator is run against all dialogues in the corpus in such a way that for each turn in a dialogue (consisting of a system act and a user act), the user simulator is provided with the system act and is run repeatedly to generate several simulated user response acts for that turn. For the first turn of a dialogue, the simulator is initialised with the correct user state (see Section 3.2). For each response, the simulator may make different random decisions, generally leading to different user acts. The decisions that lead to a simulated act that matches the true act are recorded as successful. By generating a sufficiently large number of simulated acts, all possible combinations of decisions are explored to find a matching act. Given the high complexity of the simulator, this sampling approach is preferred over directly enumerating all decision combinations to identify the successful ones. If none of the combinations are successful, then either a) the processing of the dialogue is ended, or b) the correct context is set for the next turn and processing is continued. Whereas the former approach aims at matching sequences of turns, the latter only aims at matching each user turn separately. In either case, after all data is processed, the parameters are estimated using the resulting counts of successful decisions for each of the RDPs.

For each RDP $i$, let $DP_i$ represent the decision taken, and $d_{ij}$ the $j$’th possible decision. Then, for each decision point $i$ that is controlled by a multinomial distribution, the corresponding parameter estimates $\theta_{ij}$ are obtained as follows from the decision frequencies $c(DP_i = d_{ij})$:

$$\theta_{ij} = \frac{c(DP_i = d_{ij})}{\sum_j c(DP_i = d_{ij})}$$

(1)

Random decision points that are controlled by geometric distributions involve potentially multiple random decisions between two options (Bernoulli trials). The parameters for such RDPs are estimated as follows:

$$\theta_i = \left(\frac{1}{n} \sum_{k=1}^{n} b_{ik}\right)^{-1}$$

(2)

where $b_{ik}$ is the number of Bernoulli trials required at the $k$’th time decision point $i$ was encountered. In terms of the decision network, this estimate is correlated with the average number of times the loop of the node was taken.

3.2 User goal inference

In order to be able to set the correct user goal state in any given turn, a set of update rules is used to infer the user’s goals from a dialogue beforehand, on the basis of the entire sequence of system acts and ‘true’ user acts (see Section 4.1) in the corpus. These update rules are based on the notion of dialogue act preconditions, which specify conditions of the dialogue context that must hold for a dialogue agent to perform that act. For example, a precondition for the act `inform(area=central)` is that the speaker wants a venue in the centre. The user act model...
of the HIS dialogue manager is designed according to this same notion (Keizer et al., 2008). In this model, the probability of a user act in a certain dialogue context (the last system act and a hypothesis regarding the user goal) is determined by checking the consistency of its preconditions with that context. This contributes to updating the system’s belief state on the basis of which it determines its response action. For the user goal inference model, the user act is given and therefore its preconditions can be used to directly infer the user goal. So, for example, in the case of observing the user act inform(area=central), the constraint (area=central) is added to the user goal.

In addition to using the inferred user goals, the agenda is corrected in cases where there is a mismatch between real and simulated user acts in the previous turn.

In using this offline goal inference model, our approach takes a position between (Schatzmann et al., 2007b), in which the user’s goal is treated as hidden, and (Georgila et al., 2006), in which the user’s goal is obtained directly from the corpus annotation.

4 Evaluation

The parameter estimation technique for training the user simulator was evaluated in two different ways. The first evaluation involved comparing the statistics of simulated and real user behaviour. The second evaluation involved comparing dialogue manager policies trained with different simulators.

4.1 Data

The task of the dialogue systems we are developing is to provide tourist information to users, involving venues such as bars, restaurants and hotels that the user can search for and ask about. These venues are described in terms of features such as price range, area, type of food, phone number, address, and so on. The kind of dialogues with these systems are commonly called slot-filling dialogues.

Within the range of slot-filling applications the domain is relatively complex due to its hierarchical data structure and relatively large number of slots and their possible values. Scalability is indeed one of the primary challenges to be addressed in statistical approaches to dialogue system development, including user simulation.

The dialogue corpus that was used for training and evaluating the simulator was obtained from the evaluation of a POMDP spoken dialogue system with real users. All user utterances in the resulting corpus were transcribed and semantically annotated in terms of dialogue acts. Dialogue acts consist of a series of semantic items, including the type (describing the intention of the speaker, e.g., inform or request) and a list of slot value pairs (e.g., food=Chinese or area=south). An extensive analysis of the annotations from three different people revealed a high level of inter-annotator agreement (ranging from 0.81 to 0.94, depending on which pair of annotations are compared), and a voting scheme for selecting a single annotation for each turn ensured the reliability of the ‘true’ user acts used for training the simulator.

4.2 Corpus statistics results

A first approach to evaluating user simulations is to look at the statistics of the user behaviour that is generated by a simulator and compare it with that of real users as observed in a dialogue corpus. Several metrics for such evaluations have been considered in the literature, all of which have both strong points and weaknesses. For the present evaluation, a selection of metrics believed to give a reasonable first indication of the quality of the user simulations was considered.

4.2.1 Metrics

The first corpus-based evaluation metric is the Log Likelihood (LL) of the data, given the user simulation model. This is what is in fact maximised by the parameter estimation algorithm. The log likelihood can be computed by summing the log probabilities of each user turn $d_u$ in the corpus data $D$:

$$\text{LL}(D|\theta) = \sum_{u} \log P(d_u|\theta)$$

The user turn probability is given by the probability of the decision paths (directed paths in the decision network of maximal length, such as the one indicated in Figure 1 in bold) leading to a simulated user act in that turn that matches the true user act. The probability of a decision path is obtained by multiplying the probabilities of the decisions made at each decision point $i$ that was encountered, which are given by the parameters $\theta_{ij}$.

Note that not all selected metrics are metrics in the strict sense of the word; the term should therefore be interpreted as a more general one.
and $\theta_i$:

$$\log P(d_u|\{\theta_{ij}\}, \{\theta_i\}) =$$

$$\sum_{i \in I^m(u)} \log \left( \sum_j \theta_{ij} \cdot \delta_{ij}(u) \right) +$$

$$\sum_{i \in I^g(u)} \log \left( \sum_k (1 - \theta_i) \cdot \theta_i \cdot \mu_{ik}(u) \right)$$

where $I^m(u) = \{ i \in I^m| \sum_j \delta_{ij}(u) > 0 \}$ and $I^g(u) = \{ i \in I^g| \sum_k \mu_{ik}(u) > 0 \}$ are the subsets of the multinomial ($I^m$) and geometric ($I^g$) decision points respectively containing those points that were encountered in any combination of decisions resulting in the given user act:

$$\delta_{ij}(u) = \begin{cases} 
1 & \text{if decision } DP_i = d_{ij} \text{ was taken in any of the matching combinations} \\
0 & \text{otherwise} 
\end{cases}$$

$$\mu_{ik}(u) = \begin{cases} 
1 & \text{if any of the matching combinations required} \\
0 & \text{otherwise} 
\end{cases}$$

It should be noted that the log likelihood only represents those turns in the corpus for which the simulated user can produce a matching simulated act with some probability. Hence, it is important to also take into account the corpus coverage when considering the log likelihood in corpus based evaluation. Dividing by the number of matched turns provides a useful normalisation in this respect.

The expected Precision (PRE), Recall (RCL), and F-Score (FS) are obtained by comparing the simulated user acts with the true user acts in the same context (Georgila et al., 2006). These scores are obtained by pairwise comparison of the simulated and true user act for each turn in the corpus at the level of the semantic items:

$$PRE = \frac{\#(\text{matched items})}{\#(\text{items in simulated act})}$$

$$RCL = \frac{\#(\text{matched items})}{\#(\text{items in true act})}$$

$$FS = \frac{2 \cdot PRE \cdot RCL}{PRE + RCL}$$

By sampling a sufficient number of simulated acts for each turn in the corpus and comparing them with the corresponding true acts, this results in an accurate measure on average.

The problem with precision and recall is that they are known to heavily penalise unseen data. Any attempt to generalise and therefore increase the variability of user behaviour results in lower scores.

Another way of evaluating the user simulator is to look at the global user act distributions it generates and compare them to the distributions found in the real user data. A common metric for comparing such distributions is the Kullback-Leibler (KL) distance. In (Cuayáhuital et al., 2005) this metric was used to evaluate an HMM-based user simulation approach. The KL distance is computed by taking the average of the two KL divergences$^3$ $D_{KL}(\text{simulated}||\text{true})$ and $D_{KL}(\text{true}||\text{simulated})$, where:

$$D_{KL}(p||q) = \sum_i p_i \cdot \log_2(\frac{p_i}{q_i}) \quad (10)$$

KL distances are computed for both full user act distributions (taking into account both the dialogue act type and slot value pairs) and user act type distributions (only regarding the dialogue act type), denoted by KLF and KLT respectively.

4.2.2 Results

For the experiments, the corpus data was randomly split into a training set, consisting of 4479 user turns in 541 dialogues, used for estimating the user simulator parameters, and a test set, consisting of 1457 user turns in 175 dialogues, used for evaluation only. In the evaluation, the following parameter settings were compared: 1) non-informative, uniform parameters (UNIF); 2) handcrafted parameters (HDC); 3) parameters estimated from data (TRA); and 4) deterministic parameters (DET), in which for each RDP the probability of the most probable decision according to the estimated parameters is set to 1, i.e., at all times, the most likely decision according to the estimated parameters is chosen.

For both trained and deterministic parameters, a distinction is made between the two approaches to matching user acts during parameter estimation. Recall that in the turn-based approach, in each turn, the simulator is run with the corrected context to find a matching simulated act, whereas in the sequence-based approach, the matching process for a dialogue is stopped in case a turn is encountered which cannot be matched by the simulator. This results in estimated parameters TRA-T and deterministic parameters DET-T for

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$^3$Before computing the distances, add-one smoothing was applied in order to avoid zero-probabilities.
the turn-based approach and analogously TRA-S and DET-S for the sequence-based approach. The corresponding normalised (see Section 4.2.1) log-likelihoods are indicated by nLL-T and nLL-S.

Tables 1 and 2 give the results on the training and test data respectively. The results show that in terms of log-likelihood and KL-distances, the estimated parameters outperform the other settings, regardless of the matching method. In terms of precision/recall (given in percentages with 95% confidence intervals), the estimated parameters are worse than the handcrafted parameters for turn-based matching, but have similar scores for sequence-based matching.

The results for the deterministic parameters illustrate that much better precision/recall scores can be obtained, but at the expense of variability as well as the KL-distances. It will be easier to train a dialogue policy on such a deterministic simulator, but that policy is likely to perform significantly worse on the more varied behaviour generated by the trained simulator, as we will see in Section 4.3.

Out of the two matching approaches, the sequence-based approach gives the best results: TRA-S outperforms TRA-T on all scores, except for the coverage which is much lower for the sequence-based approach (33% vs. 59%).

### 4.3 Policy evaluation results

Although the corpus-based evaluation results give a useful indication of how realistic the behaviour generated by a simulator is, what really should be evaluated is the dialogue management policy that is trained using that simulator. Therefore, different parameter sets for the simulator were used to train and evaluate different policies for the Hidden Information State (HIS) dialogue manager (Young et al., 2009). Four different policies were trained: one policy using handcrafted simulation parameters (POL-HDC); two policies using simulation parameters estimated (using the sequence-based matching approach) from two data sets that were obtained by randomly splitting the data into two parts of 358 dialogues each (POL-TRA1 and POL-TRA2); and finally, a policy using a deterministic simulator (POL-DET) constructed from the trained parameters as discussed in Section 4.2.2. The policies were then each evaluated on the simulator using the four parameter settings at different semantic error rates.

The performance of a policy is measured in terms of a reward that is given for each dialogue, i.e. a reward of 20 for a successful dialogue, minus the number of turns. A dialogue is considered successful if the system has offered a venue matching the predefined user goal constraints and has given the correct values of all requested slots for this venue. During the policy optimisation, in which a reinforcement learning algorithm tries to optimise the expected long term reward, this dialogue scoring regime was also used.

In Figures 2, 3, and 4, evaluation results are given resulting from running 3000 dialogues at each of 11 different semantic error rates. The curves show average rewards with 95% confidence intervals. The error rate is controlled by a hand-

| PAR  | nLL-T  | nLL-S  | PRE   | RCL   | FS    | KLF   | KLT   |
|------|--------|--------|-------|-------|-------|-------|-------|
| UNIF | −3.78  | −3.37  | 16.95 (±0.75) | 9.47 (±0.59) | 12.15 | 3.057 | 2.318 |
| HDC  | −4.07  | −2.22  | 44.31 (±0.99) | 34.74 (±0.95) | 38.94 | 1.784 | 0.623 |
| TRA-T | −2.97  | −     | 37.60 (±0.97) | 28.14 (±0.90) | 32.19 | 1.362 | 0.336 |
| DET-T | −∞    | −     | 47.70 (±1.00) | 40.90 (±0.98) | 44.04 | 2.335 | 0.838 |
| TRA-S | −2.13  | −     | 43.19 (±0.99) | 35.68 (±0.96) | 39.07 | 1.355 | 0.155 |
| DET-S | −∞    | −     | 49.39 (±1.00) | 43.04 (±0.99) | 46.00 | 2.310 | 0.825 |

Table 1: Results of the sample-based user simulator evaluation on the Mar’09 training corpus (the corpus coverage was 59% for the turn-based and 33% for the sequence-based matching approach).

| PAR  | nLL-T  | nLL-S  | PRE   | RCL   | FS    | KLF   | KLT   |
|------|--------|--------|-------|-------|-------|-------|-------|
| UNIF | −3.61  | −3.28  | 16.59 (±1.29) | 9.32 (±1.01) | 11.93 | 2.051 | 2.180 |
| HDC  | −3.90  | −2.19  | 45.35 (±1.72) | 36.04 (±1.66) | 40.16 | 1.780 | 0.561 |
| TRA-T | −2.84  | −     | 38.22 (±1.68) | 28.74 (±1.57) | 32.81 | 1.405 | 0.310 |
| DET-T | −∞    | −     | 49.15 (±1.73) | 42.17 (±1.71) | 45.39 | 2.478 | 0.867 |
| TRA-S | −2.12  | −     | 43.90 (±1.72) | 36.52 (±1.67) | 39.87 | 1.424 | 0.153 |
| DET-S | −∞    | −     | 50.73 (±1.73) | 44.41 (±1.72) | 47.36 | 2.407 | 0.841 |

Table 2: Results of the sample-based user simulator evaluation on the Mar’09 test corpus (corpus coverage 59% for the turn-based, and 36% for sequence-based matching).
The policy that was trained using the hand-crafted simulator (POL-HDC) outperforms the other policies when evaluated on that same simulator (see Figure 2), and both policies trained using the trained simulators (POL-TRA1 and POL-TRA2) outperform the other policies when evaluated on either trained simulator (see Figure 3 for the evaluation on UM-TRA1; the evaluation on UM-TRA2 is very similar and therefore omitted). There is little difference in performance between policies POL-TRA1 and POL-TRA2, which can be explained by the fact that the two trained parameter settings are quite similar, in contrast to the handcrafted parameters. The policy that was trained on the deterministic parameters (POL-DET) is competitive with the other policies when evaluated on UM-DET (see Figure 4), but performs significantly worse on the other parameter settings which generate the variation in behaviour that the dialogue manager did not encounter during training of POL-DET.

In addition to comparing the policies when evaluated on each simulator separately, another comparison was made in terms of the average performance across all simulators. For each policy and each simulator, we first computed the difference between the policy’s performance and the ‘maximum’ performance on that simulator as achieved by the policy that was also trained on that simulator, and then averaged over all simulators. To avoid biased results, only one of the trained simulators was included. The results in Figure 5 show that the POL-TRA2 policy is more robust than POL-DET, and has similar robustness as POL-HDC. Similar results are obtained when including UM-TRA1 only.

Given that the results of Section 4.2 show that the dialogues generated by the trained simulator more closely match real corpus data, and given that the above simulation results show that the POL-TRA policies are at least as robust as the
other policies, it seems likely that policies trained using the trained user simulator will show improved performance when evaluated on real users.

However, this claim can only be properly demonstrated in a real user evaluation of the dialogue system containing different dialogue management policies. Such a user trial would also be able to confirm whether the results from evaluations on the trained simulator can more accurately predict the actual performance expected with real users.

5 Conclusion

In this paper, we presented an agenda-based user simulator extended to be trainable on real user data whilst preserving the necessary rationality and complexity for effective training and evaluation of dialogue manager policies. The extension involved the incorporation of random decision points in the process of receiving and responding to a system act in each turn. The decisions made at these points are controlled by probability distributions defined by a set of parameters.

A sample-based maximum likelihood approach to estimating these parameters from real user data in a corpus of human-machine dialogues was discussed, and two kinds of evaluations were presented. When comparing the statistics of real versus simulated user behaviour in terms of a selection of different metrics, overall, the estimated parameters were shown to give better results than the handcrafted baselines. When evaluating dialogue management policies trained on the simulator with different parameter settings, it was shown that: 1) policies trained on a particular parameter setting outperform other policies when evaluated on the same parameters, and in particular, 2) a policy trained on the trained simulator outperforms other policies on a trained simulator. With the general goal of obtaining a dialogue manager that performs better in practice, these results are encouraging, but need to be confirmed by an evaluation of the policies on real users.

Additionally, there is still room for improving the quality of the simulator itself. For example, the variation in user behaviour can be improved by adding more random decision points, in order to achieve better corpus coverage. In addition, since there is no clear consensus on what is the best metric for evaluating user simulations, additional metrics will be explored in order to get a more balanced indication of the quality of the user simulator and how the various metrics are affected by modifications to the simulator. Perplexity (related to the log likelihood, see (Georgila et al., 2005)), accuracy (related to precision/recall, see (Zukerman and Albrecht, 2001; Georgila et al., 2006)), and Cramér-von Mises divergence (comparing dialogue score distributions, see (Williams, 2008)) are some of the metrics worth considering.

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