ATMOSPHERIC COMPOSITIONS OF THREE BROWN DWARFS AND IMPLICATIONS FOR THEIR FORMATION CONDITIONS

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ABSTRACT

The formation mechanisms and chemical compositions of brown dwarfs likely span a diverse range. If they are formed predominantly in isolation by gravitational collapse like dwarf stars then their compositions might follow those of dwarf stars, spanning a relatively narrow range in metallicities ($\sim$0.4 to +0.4 dex) and predominantly oxygen-rich (C/O $\lesssim$ 0.7). On the other hand, giant planets in the solar system are all super-solar in metallicity ([C/H] $> 0.5$ dex), which is thought to be a consequence of formation by core-accretion in a circumstellar disk. In this study we determine the atmospheric chemical compositions of three brown dwarfs and find them to be neither characteristic of dwarf stars nor giant planets. We derive high-precision atmospheric chemical abundances using high-S/N HST near-infrared spectra of three mid T Dwarfs which, together with two previously studied objects, display distinctly sub-solar metallicities and span C/O ratios of 0.4-1.0. These abundance patterns indicate either an old sub-stellar population and a multitude of formation environments or objects formed in circumstellar disks followed by ejection later. We show that for a simple synthetic model population of brown dwarfs with the same spectral-type as our sample the predicted age distribution is predominantly older than the Sun and, hence, more metal poor, consistent with our derived abundances. The diverse C/O ratios we find are indicative of different chemical reservoirs in their formation environments or different formation pathways. Our results open the possibility that cool brown dwarfs may provide important probes of early galactic chemical evolution and inhomogeneity.

Subject headings: brown dwarfs — stars: abundances — stars: atmospheres — radiative transfer

1. INTRODUCTION

We are now entering a new era in characterizing exoplanets and sub-stellar objects. Going beyond object detections, the field is now moving towards detailed characterization of the atmospheres of exoplanets (Madhusudhan et al. 2014b, 2016) and brown dwarfs (Apai et al. 2013; Helling & Casewell 2014) through spectroscopic observations. Encoded within a spectrum of an exoplanet or brown dwarf is information about the chemical composition and manifold physical processes in its atmosphere. State-of-the-art observations are now beginning to provide both the high precision and long spectral baseline required to place detailed constraints on the various physicochemical properties of these atmospheres. Such observations in recent years are already providing good constraints on the chemical compositions of exoplanetary atmospheres (see e.g., review by Madhusudhan et al. 2016). The most observed exoplanets to date are hot giant transiting exoplanets whose large scale-heights and high temperatures ($\sim$800-3000 K) make them particularly conducive to atmospheric observations. Chemical detections have also been reported for a few directly-imaged giant exoplanets (e.g., Konopacky et al. 2013; Barman et al. 2015). The atmospheric chemical compositions are in turn beginning to provide the first insights into the possible formation conditions and migration mechanisms of exoplanets (e.g., Oberg et al. 2011; Madhusudhan et al. 2014a).

Given their wide orbital separations directly-imaged giant planets bear several similarities to isolated brown dwarfs.

Both classes of objects have H$_2$-rich atmospheres with negligible levels of stellar irradiation, meaning that the internal heat dominates their spectra. Consequently, the atmospheric chemical compositions and physical processes in both classes of objects are expected to be quite similar for similar effective temperatures. The similarities in atmospheric properties make brown dwarfs exquisite analogs to investigate atmospheric processes and chemical compositions in exoplanets at large orbital separations. While there are only a handful of directly-imaged planets known with high-quality spectra, comparable or better quality spectra have been observed for numerous brown dwarfs using ground-based facilities (e.g., Burgasser et al. 2010). More recently, very high precision spectra (at SNR $\sim$1000) have also been obtained for several brown dwarfs using the HST Wide Field Camera 3 (WFC3) spectrograph in the near-infrared (Apai et al. 2013; Buenzli et al. 2013) leading to high-confidence detections of H$_2$O and detailed characterization of variability in these objects. Multi-wavelength datasets are also providing the long spectral baseline and high precision required to derive joint constraints on the chemical compositions, temperature profiles, and cloud coverage in these objects.

With the advent of atmospheric retrieval techniques for exoplanets (Madhusudhan & Seager 2009; Madhusudhan et al. 2011) there is now growing interest in using similar techniques for brown dwarf spectra to retrieve their atmospheric properties. Recently, Line et al. (2014, 2015) reported constraints on the atmospheric chemical abundances, temperature profiles, and bulk parameters of two brown dwarfs using their ground-based spectra in the near infrared. Given that the data quality for brown dwarfs is substantially better than that for exoplanets the former objects offer a valuable opportunity to constrain their atmospheric properties in unprecedented detail, and also to verify the models and retrieval techniques.

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In what follows, we discuss the target selection in section 2 and the observations in section 3. The modeling and retrieval approach is presented in section 4 and the results in section 5. We summarize our results and discuss the implications of the derived chemical compositions in section 6.

2. TARGET SELECTION

In the present study we focus on a small number of prime targets. In order to test and validate our atmospheric abundance retrieval process and to explore the abundances of a few relatively simple brown dwarfs with high resolution and well-understood robust observations, we turned to the sample of brown dwarfs we have previously observed with the Hubble Space Telescope’s Wide Field Camera 3 (HST/WFC3, MacKenty et al. 2010) in its near-infrared grism model (G141 grism). Data in this mode has been collected for brown dwarfs based on the following criteria: a) pre-selected sample of five T Dwarfs for comparative chemical characterization; b) well-understood robust observations, we turned to the sample of brown dwarfs we have previously observed with the Hubble Space Telescope’s Wide Field Camera 3 (HST/WFC3, MacKenty et al. 2010) in its near-infrared grism model (G141 grism). Data in this mode has been collected for brown dwarfs based on the following criteria: a) pre-selected sample of five T Dwarfs for comparative chemical characterization.

The chemical abundances in brown dwarf atmospheres could in turn provide new insights into their formation mechanisms. Our goal in the present work is to conduct such a detailed retrieval analysis for three mid T Dwarfs, which together with two previously published objects, provide a sample of five T Dwarfs for comparative chemical characterization.

In what follows, we discuss the target selection in section 2 and the observations in section 3. The modeling and retrieval approach is presented in section 4 and the results in section 5. We summarize our results and discuss the implications of the derived chemical compositions in section 6.

3. OBSERVATIONS AND COMPARISON TO MODELS

3.1. Observations and Data Reduction

The data used in this study have been obtained in our WFC3/G141 survey described in Buenzli et al (2014). As the data acquisition, reduction, and calibration have been discussed in detail in that paper, we only highlight here the essential reduction steps, differences from the original reduction, and the uncertainty analysis as these are pertinent for the current study.

For each of our targets we used the 19 spectra taken with HST/WFC3/G141 during a single HST orbit. Our reduction is based on a combination of the aXe pipeline and a self-developed set of IDL/python routines; in summary, our steps include basic reduction (bad pixel and flat field corrections), wavelength calibration and re-mapping of the spectrum, and spectral extraction (for details see Apai et al. 2013 and Buenzli et al. 2014). In this study we also applied an additional step, aperture correction, to correct for the slight wavelength-dependent losses during the spectral extraction. While a negligible effect for the original studies which focused on temporal variations of the spectrum, the aperture correction allows a more accurate measurement of the apparent flux density. We base our aperture correction on the relevant Instrument Status Report (WFC3 ISR 2011-05), which provides aperture corrections for a range of aperture sizes and wavelengths. We applied a linear interpolation in the aperture size dimension and a spline interpolation in the wavelength dimension to determine the aperture correction for our data and for each of our wavelength bins separately. As the final step, the spectra for each object were median-combined on an identically sampled wavelength grid.

3.2. Uncertainties

The HST/WFC3/G141 observations provided highly repeatable spectra and with very high signal-to-noise. The stability of the instrument allows us to characterize the uncertainties beyond what is possible for most ground-based observations. Specifically, the uncertainties in our data set are dominated by two sources: random white noise – primarily photon noise and read-out noise – and systematic errors affecting flux densities at all wavelengths – primarily caused by slight changes in the instrument and telescope state. We characterize the uncertainties through the standard deviation of the 19 spectra in each wavelength bin. The standard deviation varies from a fraction of the percent in continuum bands (where the object is the brightest) to about 2% of the flux density in water band (where the object is the faintest). We note that the standard deviation will not capture systematic changes that result, in effect, in slight changes of the efficiency of the instrument. While our analysis is largely insensitive to the precise absolute levels of the flux density, we estimate that such zero-point differences contribute at levels less than 0.5% based on our analysis of identical datasets presented in Apai et al. 2013.
the major opacity sources expected in H spheres are free parameters in the model. The model includes its central wavelength approximately in the mid-range of our simulations for the F140W filter, which is a broad-band filter with fundamental telescope parameters. We carried out our simulation. Correctly comparing the models to the observations requires matching their resolutions. We do this by reducing the resolution of the models, i.e. by convolving the model spectrum with the HST/WFC3 G141 spectra is low resolution for comparison with data, as discussed in section 3.3. Instrument point spread function and binned to the data resolution for uniform mixing ratios of the eight molecules (H\textsubscript{2}, H\textsubscript{2}O, CO, CH\textsubscript{4}, CO\textsubscript{2}, C\textsubscript{2}H\textsubscript{2}, HCN, NH\textsubscript{3}, and H\textsubscript{2}S), and collision-induced absorption (CIA) due to H\textsubscript{2}-H\textsubscript{2} and H\textsubscript{2}-He, obtained from the latest theoretical and experimental line databases currently available.

Given a spectral dataset, the model is coupled with a parameter estimation method to obtain joint constraints on the chemical composition and temperature structure of the planet. Given a parametric temperature profile and molecular abundances, the model computes the emergent spectrum of the object at a high resolution which is then convolved with the instrument point spread function and binned to the data resolution for comparison with data, as discussed in section 3.3.

We explore the model parameter space and fit models to the data using a Markov Chain Monte Carlo (MCMC) algorithm (Madhusudhan et al. 2011; Line et al. 2015) and determine the posterior probability distributions of the model parameters. Given the very high SNR of the data we also inflate the uncertainties in the observed spectrum by \∼2% of the maximum flux in the spectrum to account for any unaccounted systematics and/or model uncertainties (see e.g., Line et al. 2015). The model space includes a wide range of plausible temperature profiles and compositions, spanning models with oxygen-rich as well as carbon-rich compositions. Thus, the model has 17 free parameters: six for the chemical compositions, temperature profile, eight fundamental telescope parameters. We carried out our simulations for the F140W filter, which is a broad-band filter with its central wavelength approximately in the mid-range of our spectra. A comparison of the radial profile TinyTim provided to that measured perpendicular to the spectrum showed a very good match, verifying our approach.

4. ATMOSPHERIC MODELING AND RETRIEVAL METHOD

In order to retrieve the atmospheric compositions and temperature profiles from spectra we use an atmospheric retrieval method that has been widely used for exoplanetary atmospheres (Madhusudhan & Seager 2009, Madhusudhan et al. 2011). The retrieval method comprises of a parametric forward model of an exoplanetary atmosphere coupled with a Bayesian parameter estimation algorithm to retrieve the model parameters (e.g., the chemical compositions, temperature profile, etc.) given a spectral dataset. The model computes line-by-line radiative transfer for a plane-parallel 1-D atmosphere with the assumptions of hydrostatic equilibrium as described in Madhusudhan & Seager (2009). The composition and pressure-temperature (P-T) profile of the atmosphere are free parameters in the model. The model includes the major opacity sources expected in H\textsubscript{2} dominated atmospheres, namely H\textsubscript{2}O, CO, CH\textsubscript{4}, CO\textsubscript{2}, C\textsubscript{2}H\textsubscript{2}, HCN, NH\textsubscript{3}, and H\textsubscript{2}S, and collision-induced absorption (CIA) due to H\textsubscript{2}-H\textsubscript{2} and H\textsubscript{2}-He, obtained from the latest theoretical and experimental line databases currently available.

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5. RESULTS

In this section, we report the constraints on the atmospheric compositions of the three objects in our sample. The atmospheric retrieval allows us to place joint constraints on
the chemical abundances, the temperature profiles, and the macroscopic parameters such as gravity. The best fit model spectra to all the three objects are shown in Fig. 1 and the estimated compositions and their posterior probability distributions are shown in Table 2 and Fig. 2 respectively.

The high-precision HST WFC3 spectra enable us to detect and derive constraints on the mixing ratios of key molecular species which, in turn, help constrain the corresponding elemental abundances. As discussed in section 4 we place constraints on the abundances of H2O, CH4 and NH3 which are known to have strong spectral signatures in the WFC3 bandpass (1.1-1.7 μm). For H2-rich atmospheres, e.., of giant planets and brown dwarfs, it is expected that O and C are largely contained in H2O, CH4, and CO, over a wide range of temperatures [Madhusudhan 2012]. Furthermore, for temperatures below ~1300 K in the observable atmospheres at pressures below ~1 bar, H2O and CH4 contain all the O and C, respectively. Therefore, in our case for the current sample which fall in this temperature range the elemental abundances of O and C can be derived from the mixing ratios of H2O and CH4, respectively.

We report clear detections of H2O, CH4, and NH3 in all the three objects. Figure 2 shows the posterior probability distributions of the various molecular mixing ratios in the atmosphere. We do not detect any other molecule, e.., CO or CO2. As shown in Table 2 we measure the H2O abundances (in log(H2O/H2)) of the three objects to be: -3.86 ± 0.10, -4.49 ± 0.12, and -4.30 ± 0.04. The CH4 abundances of the corresponding objects are -3.82 ± 0.04, -4.71 ± 0.13, and -4.66 ± 0.04, respectively. Given the high S/N of the HST observations our constraints on the molecular abundances are able to achieve precisions below ~0.15 dex, i.e. within a factor of 2, similar to that achieved by previous studies [Line et al. 2014, 2015]. Even so, the precisions are limited not by the quality of the data but by the jitter added to the original observational uncertainties to account for unaccounted systematics and/or missing physics in the models.

We find sub-solar C/H and O/H abundances and diverse C/O ratios in our sample. The abundance estimates are shown in Fig. 3 and Table 2. As discussed above, the C/H and O/H ratios are derived from the CH4 and H2O mixing ratios, respectively. This is justified as given the low temperatures of these objects (<1000 K) CH4 and H2O are expected to be the dominant carriers of C and O, respectively, which is further supported by the fact that we do not detect any CO in these objects. We find the C/H and O/H ratios to be sub-solar in all the objects irrespective of their C/O ratios, which range between ~0.35 and 1.0. Our derived abundances for the three systems follow a similar trend to that observed by [Line et al. 2015] in two other T Dwarfs. [Line et al. 2015] reported sub-solar O/H ratios for both their objects, while the C/H ratio was sub-solar for one and nearly solar (1-2× solar) for the second object.

We find a wide range of C/O ratios for our three objects, between oxygen-rich (C/O = 0.4) and carbon-rich (C/O = 1.0), while [Line et al. 2015] reported significantly carbon-rich ratios (C/O = 1-1.2) for both their objects. [Line et al. 2015] explained their low O/H ratios and high C/O ratios as possibly due to silicates, which are not observable, taking up some of the oxygen thereby causing an apparent oxygen-poor (or carbon-rich) composition in an atmosphere that is actually oxygen-rich. We have, therefore, corrected our observed O/H abundances for this effect by allowing the possibility of up to 20% of the oxygen locked in silicates; this number fraction of silicates is expected for a solar composition gas [Johnson et al. 2012, Moses et al. 2013]. Even with that correction we still find that the O/H ratios are sub-solar and the C/O ratios span a wide range (~0.35-1.0), suggesting that the systems of Line et al may actually be carbon-rich. Overall, the current sample of five objects, including ours and those from Line et al, suggest that all these objects are metal poor and span a diverse range of C/O ratios, both oxygen-rich and carbon-rich.

We also find evidence for sub-solar N/H in all the T Dwarfs in our study. We derive the N/H abundance from the NH3 mixing ratio. However, the N/H thus derived can also be considered as a lower limit since some of N can be bound in N2 which does not have strong spectral features. Fig. 3 shows the derived N/H abundances for the objects in our study as well as those from [Line et al. 2015] based on their NH3 abun-
Atmospheric Retrieval of Three Brown Dwarfs

The atmospheric chemical abundances in the five T Dwarfs studied to date reveal a population very different in elemental composition from main-sequence stars in the solar neighborhood. For example, in four of the five objects we find oxygen metallicities below 0.5×solar, i.e. [O/H] < -0.3. In contrast, over 90% of F, G, K main-sequence dwarf stars in the solar neighborhood have [O/H] > -0.3 (Brewer et al. 2016). Similarly, four of the five objects in our sample have C/O ratios greater than 0.7, whereas over 99% of F, G, K stars have C/O < 0.7. In particular, two of the objects in our current study have metallicities below 0.1×solar, i.e. [O/H] < -1, which is rarely found in dwarf stars. Therefore, the predominately sub-solar C and O abundances and the super-solar C/O ratios are incongruent with the abundance patterns observed in main-sequence stars in the solar neighborhood. Instead, such an abundance pattern leads to two interesting possibilities. Firstly, the abundance pattern is more reminiscent of the compositions of early generation stars which display significantly sub-solar metallicities and high C/Fe and/or C/O ratios (see e.g., Frebel & Norris 2015; Howes et al. 2015). It might then be the case that the T Dwarfs in the sample have very old ages, are probes of the early galactic composition, and open a new avenue to galactic archeology. On the other hand, a second possibility is that the objects in our sample did not collapse from a proto-stellar cloud but instead formed as giant planets. We discuss both possibilities below.

6. SUMMARY AND DISCUSSION

The atmospheric chemical abundances in the five T Dwarfs provide initial insights into their possible formation conditions. The sub-solar metallicities (C, O, and N) and diverse C/O ratios observed in the objects ostensibly suggest a formation mechanism similar to giant planets formed in a disk. Firstly, the low metallicities are consistent with the natural trend in giant planets where the metallicities decrease with planetary mass. In the solar system, the metallicities, represented by the C/H ratio, of the ice giants are ∼30-50×solar, that of Saturn is ∼10×solar and that of Jupiter is 3-5×solar (Atreya et al. 2016). An extrapolation of that trend would naturally suggest that brown dwarfs would have sub-stellar metallicities. Such a trend appears because the metallicity of a giant planet is governed by the amount of solids accreted during its formation relative to the amount of gas. Therefore, for a gas giant, where most of the mass is in the gas, the lower the total mass the higher its atmospheric metallicity. The maximum amount of solids accreted by the object is limited by the available mass of solids in the disk. Thus, given their jovian or super-Jovian masses, brown dwarfs forming in a disk could be expected to possess very low metallicities. On the other hand, the C/O ratio of the object is governed by the formation location of the object relative to the snow lines of the major condensates (Oberg et al. 2011; Madhusudhan et al. 2014a); the C/O ratio of the gas increases with distance. Assuming predominant gas accretion, objects forming within the H₂O snow line can have solar C/O ratios, objects forming beyond the CO snow line can have C/O ratios of unity. Therefore, it may be the case that the objects we sample formed in a circumstellar disk akin to planets and, if found as isolated today, may have been ejected out of their systems by dynamical encounters. This possibility would be in line with the indication of a possible large population of planetary-mass brown dwarfs, or free floating giant planets, as inferred from the overabundance of short-timescale microlensing events (Sumi et al. 2011; Clanton & Gaudi 2016).

6.2. Formation in Circumstellar Disks

The atmospheric chemical abundances of the five T Dwarfs provide initial insights into their possible formation conditions. The sub-solar metallicities (C, O, and N) and diverse C/O ratios observed in the objects ostensibly suggest a formation mechanism similar to giant planets formed in a disk. Firstly, the low metallicities are consistent with the natural trend in giant planets where the metallicities decrease with planetary mass. In the solar system, the metallicities, represented by the C/H ratio, of the ice giants are ∼30-50×solar, that of Saturn is ∼10×solar and that of Jupiter is 3-5×solar (Atreya et al. 2016). An extrapolation of that trend would naturally suggest that brown dwarfs would have sub-stellar metallicities. Such a trend appears because the metallicity of a giant planet is governed by the amount of solids accreted during its formation relative to the amount of gas. Therefore, for a gas giant, where most of the mass is in the gas, the lower the total mass the higher its atmospheric metallicity. The maximum amount of solids accreted by the object is limited by the available mass of solids in the disk. Thus, given their jovian or super-Jovian masses, brown dwarfs forming in a disk could be expected to possess very low metallicities. On the other hand, the C/O ratio of the object is governed by the formation location of the object relative to the snow lines of the major condensates (Oberg et al. 2011; Madhusudhan et al. 2014a); the C/O ratio of the gas increases with distance. Assuming predominant gas accretion, objects forming within the H₂O snow line can have solar C/O ratios, objects forming beyond the CO snow line can have C/O ratios of unity. Therefore, it may be the case that the objects we sample formed in a circumstellar disk akin to planets and, if found as isolated today, may have been ejected out of their systems by dynamical encounters. This possibility would be in line with the indication of a possible large population of planetary-mass brown dwarfs, or free floating giant planets, as inferred from the overabundance of short-timescale microlensing events (Sumi et al. 2011; Clanton & Gaudi 2016).
FIG. 4.— Distribution of ages and gravities of Mid-TDwarfs predicted by our fiducial evolutionary model assuming a flat star formation rate.

FIG. 5.— Distribution of ages and gravities of Mid-TDwarfs predicted by our fiducial evolutionary model assuming a star formation rate that is linearly declining in time.

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