Effects of Acetylene Addition to the Fuel Stream on Soot Formation and Flame Properties in an Axisymmetric Laminar Coflow Ethylene/Air Diffusion Flame

Xinrong Xie, Shu Zheng,† Ran Sui, Zixue Luo, Shi Liu, and Jean-Louis Consalvi

ABSTRACT: The effects of adding acetylene to the fuel stream on soot formation and flame properties were investigated numerically in a laminar axisymmetric coflow ethylene/air diffusion flame using the open-source flame code Co-Flame in conjunction with an elementary gas-phase chemistry scheme and detailed transport and thermodynamic database. Radiation heat transfer of the radiating gases (H2O, C2H2, CO, and CO2) and soot was calculated using a statistical narrow-band correlated-k-based wide band model coupled with the discrete-ordinates method. The soot formation was described by the consecutive steps of soot nucleation, surface growth of soot particles via polycyclic aromatic hydrocarbons (PAHs)-soot condensation or the hydrogen abstraction acetylene addition (HACA) mechanism, and soot oxidation. The added acetylene affected the flame structure and soot concentration through not only chemical reactions among different species but also radiation effects. The chemical effect due to the added acetylene had a significant impact on soot formation. Specifically, it was confirmed that the addition of 10% acetylene caused an increase in the peak soot volumetric fraction (SVF) by 14.9% and the peak particle number density by about 21.1% (z = 1.5 cm). Furthermore, increasing acetylene concentration led to higher concentrations of propargyl, benzene, and PAHs and consequently directly enhanced soot nucleation rates. In addition, the increased H mole fractions also accentuated the soot surface growth in contrast, the radiation effect of the addition of 10% acetylene was much weaker, resulting in slightly lower flame temperature and SVF, which in turn reduced the radiant heat loss.

1. INTRODUCTION

Soot is a major undesired product in hydrocarbon combustion due to its adverse effects on energy efficiency, air pollution, and global warming.1,2 Adding inert or active additives to the primary hydrocarbon fuel can alter the sooting characteristics of fuel.2 It is hence essential to understand the soot formation and explore the effect of different additives in fuel. The fuel additives have been paid more and more attention in the past few years, as shown by the study of Kohse-Höinghaus et al.,3 when reviewing biofuel combustion chemistry. Acetylene has been recognized as the main soot precursor and important combustion intermediate species in hydrocarbon flames;4 it is necessary to study the effect of acetylene addition to the fuel on combustion.

Recently, He et al.5 studied the effect of adding N2 on soot formation in laminar methane, ethane, and propane diffusion flames. The results showed that the addition of N2 can inhibit the formation of soot through the dilution of the fuel concentration and changing the flame temperature. Zhang et al.6 pointed out that CO2 addition inhibited soot formation based on the analyses of dilution, thermal, and chemical effects of CO2 addition. Liu7 found that C2H3 mole fractions in ethanol flames decreased due to the dilution and thermal effects of CO2 addition, while the H mole fractions decreased due to the chemical effects of CO2 addition. Liu et al.8 revealed the chemical effects of adding CO2 in both fuel and oxidizer streams of a C2H4 diffusion coflow flame. It was shown that C2H3 concentration was only slightly reduced when CO2 was added in the fuel stream, while it decreased by about 10% when CO2 was added in the oxidizer. They further identified the key reaction steps that accounted for such chemical impacts of CO2 addition as CO2 + C2H2 → HCO + CO and CO2 + H → CO + OH.

To unravel the impact of H2 addition on soot inception and surface growth, many studies have been conducted for
ethylene/hydrogen/air diffusion flames. H₂ is an ideal energy resource because no carbon dioxide or soot is produced in hydrogen combustion. Hydrogen addition in hydrocarbon fuels can reduce the soot emission in diffusion flames⁹–¹¹ and improve the combustion efficiency¹²,¹³ and chemical activity.¹⁴,¹⁵ Specifically, the experimental investigation of Gülder et al.¹⁶ showed that H₂ addition in the fuel stream inhibited soot formation chemically in a C₂H₄/air laminar coflow flame. However, this chemical inhibition effect of H₂ addition did not exist in C₃H₈/air and C₄H₁₀/air flames. The simulations performed by Guo et al.¹¹ also verified that H₂ addition in a C₂H₄ diffusion flame inhibited soot formation, which was consistent with ref.¹⁶. The numerical results further suggested that the inhibiting effect of H₂ addition was caused by the higher concentration of molecular hydrogen in the lower flame region and the decreased H concentration in soot surface growth regions. Liu and Migliorini¹⁷ studied the influence of adding H₂ on soot formation in coflow laminar CH₄ diffusion flames. It showed that the addition of H₂ or He to CH₄/air flames reduced the soot yield. Lin et al.¹⁰ carried out samplings and simulations of soot formation in C₂H₄ and CH₄ flames with H₂ addition and discovered that H₂ had inhibition and promotion effects on soot in C₂H₄/air and CH₄/air flames, respectively.

Suh and Atreya¹⁸ discussed the chemical effect of H₂O dilution in diffusion laminar CH₄ flames by replacing nitrogen in the oxidant stream with argon and H₂O and found that flame temperature, OH radical concentration, and CO₂ concentration increased due to the addition of water vapor, which in turn suppressed CO concentration. However, the chemical pathway of water vapor was not clear. Liu et al.¹⁹ performed detailed numerical simulations of an axisymmetric diffusion laminar C₂H₄ flame with H₂O addition in the oxidizer to explain the chemical, radiative, and oxygen dilution effects of H₂O on soot formation. They confirmed that the primary pathway for the chemical effect of H₂O addition was mainly via the reaction H + H₂O → OH + H₂. With increased water vapor concentration, H radical concentration decreased, which in turn led to reduced polycyclic aromatic hydrocarbon (PAH) concentrations.

In addition, some studies were focused on the impact of dual additives on flame properties. Gu et al.²⁰ studied the effect of adding H₂ and CO₂ on soot formation in coflow axisymmetric C₂H₄ diffusion flames. The results showed that H₂ and CO₂ were more effective in inhibiting soot inception and soot surface growth, respectively. Sun et al.²¹ reported the effect of simultaneous H₂ and N₂ addition in C₂H₄/air diffusion flames. The results showed that the flame length increased/decreased when only H₂/N₂ was added and significantly decreased when both H₂ and N₂ were added. Furthermore, they also found that the primary particle diameter decreased in the presence of additional H₂ and N₂ in the fuel stream, while the flame temperature was not affected by H₂/N₂ addition. Ren²² used N₂, CO₂, and H₂O as dilution species to simulate the CH₄ laminar combustion characteristics. The results showed that the adiabatic flame temperature and burning velocity of CH₄ were decreased by the addition of N₂, CO₂, and H₂O, and the effect of the three species decreased with the decrease of the blending ratios. Mahmoud et al.²³ investigated the effects of H₂O and CO₂ addition as well as the coupling of H₂O and CO₂ addition in diffusion ethylene flames. They revealed that the addition of H₂O to fuel was more effective in suppressing soot formation and that of CO₂ to oxidizer was more effective in soot inhibition.

Although the effects of some additives on the fuel stream or oxidizer stream in different flames have been studied, the previous literature was mainly centered on the effects of H₂, H₂O, and CO₂ addition, while information on the effect of the addition of C₂H₄ on the fuel stream is limited. Zelepouga²⁴ studied experimentally the effect of adding acetylene and PAHs on soot formation in coflowing nonpremixed CH₄/oxygen and CH₄/oxygen-enriched flames. The results showed that the addition of acetylene and PAHs can enhance soot formation in the four reference flames, containing 21, 35, 50, and 100% of oxygen in the oxidizer stream. The increased soot volumetric fraction (SVF) induced by adding acetylene was significantly smaller due to PAH addition. Kunioishi et al.²⁵ discussed the effect of adding acetylene or benzene on the PAH growth process in a fuel-rich premixed flame by the modified program and found that production rates of pyrene increased due to the addition of acetylene in early positions of the flame; however, the pyrene concentrations were lower with acetylene addition. The effects of the addition of acetylene to fuel on the flame properties have not been reported in the literature. As a soot precursor, it is essential to understand the role of acetylene, an important combustion intermediate species in hydrocarbon flames. To this direction, the primary objective of the present work is to obtain the effects of the addition of acetylene on soot formation at atmospheric pressure, which were numerically studied in an axisymmetric diffusion laminar ethylene flame. This work investigates the flame structure and chemical and radiation effects of acetylene addition to the fuel. In particular, the detailed reaction pathways for the chemical effects of acetylene are identified.

### 2. NUMERICAL MODELS

The governing equations of mass, energy, momentum, species, and state were discretized in cylindrical coordinate (r, z). The equations have been elaborated in previous studies¹¹,²⁶ and were shown as follows. It is, however, worth mentioning that the momentum equations contain a gravity term and the energy equation contains a source term of thermal radiation.

#### Continuity

\[
\frac{\partial }{\partial r}(ru) + \frac{\partial }{\partial z}(pu) = 0 \tag{1}
\]

#### Radial momentum

\[
n\nu \frac{\partial v}{\partial r} + pu \frac{\partial v}{\partial z} = -\frac{\partial p}{\partial r} + \frac{\partial }{\partial z}\left( \frac{\mu }{\rho } \frac{\partial v}{\partial z} \right) + \frac{2}{r} \frac{\partial }{\partial r}\left( \frac{ru}{\partial r} \right) - \frac{2}{3} \frac{\partial }{\partial r}\left( \frac{ru}{\partial r} \right) - \frac{2}{3} \frac{\partial }{\partial z}\left( \frac{ru}{\partial z} \right) + \frac{\partial }{\partial z}\left( \frac{\mu u}{\partial z} \right) - \frac{2\mu v}{r^2} + \frac{2\mu}{3} \frac{\partial}{\partial r}\left( \frac{ru}{\partial r} \right) + \frac{2\mu}{3} \frac{\partial}{\partial z}\left( \frac{ru}{\partial z} \right) \tag{2}
\]

#### Axial momentum

\[
\frac{\partial }{\partial r}(ru) + \frac{\partial }{\partial z}(pu) = 0
\]
were employed in the calculation of the statistical narrow-band correlated-k model, including H2O, C2H2, CO, and CO2. The soot absorption coefficient was 5.5 m−1, where λ and fλ are the wavelength and the volume fraction of soot, respectively. The absorption coefficient was obtained by inverting the cumulative distribution function using the four-point Gaussian integration scheme.34 The radiation transfer equation was calculated by the discrete ordinates method (DOM).35 More detailed calculations on the thermal radiation model can be found in refs 34 and 38.

2.3. Chemical Kinetic Mechanism. The reaction kinetic mechanism of C2H4 by the extended Apple, Bockhorn, Frenklach (ABF) mechanism29 was applied, which included 544 chemical reactions and 103 species. The gas-phase reaction mechanism reported by Apple et al.25 which contains PAHs up to pyrene (A4), was used in this study. It should be pointed out that a relatively new reaction mechanism for C2 hydrocarbons was developed by Slavinskaya and co-workers at Deutsches Zentrum für Luft und Raumfahrt (DLR)39 which was shown to perform better than the ABF mechanism in the prediction of soot concentration in the centerline region of a laminar coflow ethylene/air diffusion flame at atmospheric pressure. A recent study by Liu et al.40 showed that the DLR mechanism fails to predict the chemical effects of CO2 on soot formation suppression in a laminar coflow ethylene/air diffusion flame. Because of the high CO2 concentration in the C2H4 added combustion flame cases, the ABF mechanism was used in the present numerical study. Also, it has been shown in other studies that the coupling of the ABF mechanism and the soot model described above performed reasonably well in the prediction of soot properties in a laminar axisymmetric coflow ethylene/air diffusion flame.2,33

3. COMPUTATIONAL METHODS AND TEST CASES

3.1. Geometry of the Computational Domain. The laminar axisymmetric diffusional ethylene flames were discretized in a two-dimensional matrix region of 3.63 cm (r) × 12.20 cm (z) by 98 (r) ×160 (z) control volumes. Nonuniform meshes were applied to increase the resolution without excessively increasing the computational time. Ethylene (fuel) flowed from a tube of inner diameter 10.74 mm and wall thickness 1.03 mm. Air (oxidizer) flowed out of a concentric annular tube (inner diameter = 88.62 mm). The fuel stream velocity was 3.4 cm/s, and oxidizer velocity was 50 cm/s. Outlet temperatures of the air and ethylene streams were both 300 K. The criterion for simulation convergence was set as when the variation of maximum SVF was less than 1 × 10−5 in two consecutive iterations.

3.2. Numerical Scheme. The governing equations were solved using the control volume method. The convection term was solved using the upwind finite difference method, while the diffusion term was solved through the central differencing scheme. To speed up the convergence process, the discretization equations of soot number density, mass fraction, and gas composition were calculated through complete coupling, while those of pressure correction, energy, and momentum were solved by the tri-diagonal matrix algorithm (TDMA) method.

3.3. Test Cases. Seven test cases were considered to compare the different impacts on flame properties when either acetylene or a fictitious species acetylene was added. The fictitious acetylene (F4C2H4) in the simulations was invented to facilitate comparisons with real acetylene. It had the same

\[
\frac{\rho u}{r} + \rho u \frac{\partial u}{\partial z} = -\frac{\partial p}{\partial z} + \frac{1}{r} \frac{\partial}{\partial r} \left( r \mu \frac{\partial u}{\partial r} \right) + 2 \frac{\partial}{\partial z} \left( \mu \frac{\partial u}{\partial z} \right) - \frac{2}{3} \frac{\partial}{\partial r} \left( \frac{\mu}{r} \frac{\partial v}{\partial r} \right) - \frac{2}{3} \frac{\partial}{\partial z} \left( \frac{\mu}{r} \frac{\partial v}{\partial z} \right) + \frac{1}{r} \frac{\partial}{\partial r} \left( r \mu \frac{\partial v}{\partial r} \right) + \rho g_z
\]  

(3)

Energy

\[
c_v \left( \frac{\partial T}{\partial r} + \mu \frac{\partial T}{\partial z} \right) = \frac{1}{r} \frac{\partial}{\partial r} \left( r \lambda \frac{\partial T}{\partial r} \right) + \frac{\partial}{\partial z} \left( \lambda \frac{\partial T}{\partial z} \right) - \sum_{k=1}^{KK+1} \left[ c_v \lambda_k \left( \frac{\partial Y_k}{\partial r} + \nu_k \frac{\partial T}{\partial z} \right) \right] - \sum_{k=1}^{KK+1} h_k W_\omega \kappa_k + q_v
\]  

(4)

Chemical species

\[
\frac{\partial Y_k}{\partial r} + \mu \frac{\partial Y_k}{\partial z} = -\frac{1}{r} \frac{\partial}{\partial r} \left( r \rho Y_k \nu_k \right) - \frac{\partial}{\partial z} \left( \rho Y_k v_k \right) + W_\omega \kappa_k \quad k = 1, 2, ..., KK
\]  

(5)

State equation

\[
\rho = \frac{p}{RT \sum_{k=1}^{KK+1} Y_k / W_k}
\]  

(6)

where v and u are the velocities in the radial (r) and axial (z) directions, respectively, T and ρ are the temperature and density of the mixture, λ is the mixture thermal conductivity, Wk is the relative molecular mass of the k-th species, cp is the specific heat of the mixture under constant pressure, cpk is the specific heat of the k-th gas species under constant pressure, mk is the mole production rate of the k-th gas species per unit volume, tk is the specific enthalpy of the k-th gas species, gk is the gravitational acceleration in the axial direction, μ is the viscosity of the mixture, Yk is the mass fraction of the k-th gas species, Vr and Vz are the diffusion velocities of the k-th gas species in the radial and axial directions, and KK is the total gas-phase species number.

2.1. Soot Formation Model. Because the simplified two-equation soot formation model based on acetylene was unable to predict the detailed physical and chemical processes, it was necessary to apply a more detailed model to study the influence of acetylene addition in this work.

The soot nucleation rate was determined using the collision rate of two pyrene (A4) molecules and also modified the parameter of van der Waals force.28 The following soot surface growth and oxidation processes were modeled using the HACA mechanism.29,30 The soot surface growth can also be caused by collisions between PAH and soot particles, which is generally called the PAH-soot condensation mechanism.31 The soot-PAH condensation efficiency was set at 0.5. For the HACA mechanism, the parameter of reactive soot surface α was set to 0.004 exp(10,800/T).32 Further details can be found in refs 4, 26, 32, and 33. This soot formation model has been extensively validated and employed in previous studies.8,32,33

2.2. Radiation Model. In the radiation model, the absorption coefficients of combustion products in each band
transport and thermodynamic properties as real acetylene but was chemically inert. It was radiating in Cases 4–5 and nonradiating in Cases 6–7.

The volume fraction compositions of the different cases are shown in Table 1. Case 1 represented the baseline condition with the fuel stream composed of pure ethylene. In Cases 2 and 3, 5 and 10% of C2H4 in the fuel stream were replaced by C2H2, respectively. The differences between Case 1 and Case 2 contain the global effect of acetylene. In Cases 4 and 5, 5 and 10% of the fictitious species FC2H2 were added to the fuel instead, respectively. FC2H2 was used to exclude the chemical effect from other effects so that the differences between Cases 2 and 4 were completely due to the chemical effect of acetylene addition. In Cases 6 and 7, 5 and 10% of nonradiating FC2H2 were added to the fuel stream, respectively, so that the differences between Cases 4 and 6 were only due to the radiation absorption of acetylene.

4. RESULTS AND DISCUSSION

Zhang et al.33 validated the soot model with the C2 mechanism in a diffusion C2H4 flame, and Gu et al. applied it in ref 20, where experimental results of H2 and CO2 addition effects were reproduced successfully. Therefore, it is adequate to assume that the simulation results of acetylene addition to the ethylene/air flames are at least qualitatively reliable.

In the following discussions, the cases with 10% C2H2 and FC2H2 in the fuel stream will be elaborated, while the cases with 5% C2H2 and FC2H2 will be only briefly mentioned because the latter will yield qualitatively same but less obvious results.

4.1. Global Effect of Acetylene Addition. Figures 1 and 2 depict the simulated temperature and SVF distributions for the different cases. Temperature distributions and the corresponding peak temperature (T_{\text{max}}) for the pure ethylene/air (Case 1) and 10% acetylene addition (Case 3) are compared in Figure 1a,b. T_{\text{max}} was 2037.6 K in Case 1, occurring vertically at 1.0 cm (z) above the burner exit and at the radial distance of 0.49 cm. This closely reproduced the literature hyperspectral experimental result in ref 41 (T_{\text{max}} = 2074.0 K at r = 0.51 cm and z = 1.01 cm).

As shown in Figure 1a,b, T_{\text{max}} increased by 11.8 K when 10% acetylene was added. Furthermore, the peak centerline temperature (T_{\text{max,cl,} r = 0}) decreased when 10% acetylene was added to C2H4/air flames, even though T_{\text{max}} was increased. The reason was that the soot concentration of the flame increased and the strong radiation absorption of the soot caused the highest temperature on the centerline to decrease. Besides the effect on the peak flame temperature in the annular region low in the flame, the centerline temperatures between about z = 3.5–6.7 cm became higher as acetylene was added to the fuel stream. Moreover, it was found that adding acetylene from 5 to 10% increased the peak soot volume fraction by about 5.4 and 8.5%. The distributions of CO and CO2 concentration with and without adding 10% C2H2 and FC2H2 are compared in Figures 4 and 5, respectively. It can be discovered that acetylene addition to fuel enhanced CO concentration in the flame, as shown in Figure 4a,b, and to a

Table 1. Compositions of the Fuel Stream of the Test Cases

| case | χ_{C2H4} | χ_{C2H2} | χ_{FC2H2} | remark         |
|------|---------|---------|-----------|----------------|
| 1    | 1       | 0       | 0         | pure C2H4     |
| 2    | 0.95    | 0.05    | 0         | C2H2 addition |
| 3    | 0.90    | 0.10    | 0         | C2H2 addition |
| 4    | 0.95    | 0       | 0.05      | radiating FC2H2 addition |
| 5    | 0.90    | 0       | 0.10      | radiating FC2H2 addition |
| 6    | 0.95    | 0       | 0.05      | nonradiating FC2H2 addition |
| 7    | 0.90    | 0       | 0.10      | nonradiating FC2H2 addition |

Figure 1. Distributions of temperature in the flames: (a) Case 1, (b) Case 3, (c) Case 5, and (d) Case 7.
lesser extent, enhanced the CO$_2$ concentration, as shown in Figure 5a,b. The addition of acetylene to ethylene/air fuel also had a slightly global effect on important species such as H$_2$, H$_2$O, and so forth, and the maximum mole fractions are shown in Table 2.

4.2. Chemical Effect of Acetylene Addition.

To study the chemical effect of C$_2$H$_2$ addition, the following discussion will be concentrated on the comparative results of adding 10% C$_2$H$_4$ and 10% FC$_2$H$_2$. Figure 6 displays the comparisons of $T_{\text{max}}$, $T_{\text{max,cl}}$, and peak SVF in the cases of pure ethylene (Case 1), the addition of 10% C$_2$H$_4$ (Case 3), and 10% FC$_2$H$_2$ (Case 5). In Case 5, the fictitious species FC$_2$H$_2$ had the same transport and thermodynamic properties as C$_2$H$_2$, but it was chemically inert. It can hence be used as a "placeholder" of C$_2$H$_2$ to exclude other effects but can only compare the chemical effect. It was shown that the chemical effect of the addition of acetylene resulted in an increase of $T_{\text{max}}$ by about 1.6% (2016.3 to 2049.4 K when FC$_2$H$_2$ and C$_2$H$_2$ were added) and led to increased peak SVF by about 14.9%. Moreover, the chemical effect of acetylene caused the $T_{\text{max,cl}}$ to decrease by 1.7%.

Figure 7 depicts the simulated radial profiles of SVF at five vertical positions, 0.14, 0.39, 2.40, 3.30, and 6.09 cm, in flames of pure C$_2$H$_4$ (Case 1), 10% C$_2$H$_2$ addition (Case 3), and 10% FC$_2$H$_2$ addition (Case 5) in the fuel stream. The five heights were selected at the vertical positions where the nucleation rate, PAH-soot condensation rate, surface growth rate through HACA, oxidation rate by OH, and soot oxidation rate by O$_2$ reached their peaks, respectively.

The chemical effect of 10% C$_2$H$_2$ addition is obviously promoting SVF at all five heights. The peak positions of SVF are closer to the centerline at the higher positions during oxidation processes as shown in Figure 7b. SVF was increased by enhancing soot surface growth and mitigating soot oxidation. Two peaks appeared during soot nucleation and PAH condensation processes (at $z = 0.14$ and 0.39 mm in Figure 7a, respectively), which were caused by the rapid increase of soot inception particles at the upstream regions when C$_2$H$_2$ was added. Furthermore, it is observed from Figure 7a that the difference between the red and blue curves at the height of 0.39 cm (only the first peak is considered here) is almost twice that at the height of 0.14 cm. From $z = 2.4$ cm to 6.09 cm, the discrepancies between the red and blue curves accentuated gradually, although the maximum difference is still lower than that of the first two heights ($z = 0.14$ and 0.39 cm). It can be concluded that upright along the flame height, the chemical impact of acetylene addition on SVF experienced a nonmonotonic trend, which first increased and then decreased, and finally increased again. These results also indicated that the chemical effect of addition of acetylene is greater on soot nucleation, surface growth by PAH-soot condensation, and HACA mechanism, while the impact on soot oxidation is trivial. The added fictitious acetylene FC$_2$H$_2$ did not participate in the chemical reactions and hence was not involved in soot production. In addition, the chemical contribution of O$_2$ to soot oxidation was greater than that of OH.

Soot nucleation, surface growth by PAH-soot condensation and HACA mechanism, and oxidation are the primary processes influencing SVF. Therefore, it is of considerable significance to explore the dominant chemical pathways of the
additional C$_2$H$_2$ in C$_2$H$_4$/air diffusion flames that influence these processes.

The soot nucleation step is directly controlled by the PAH precursor species, which includes only pyrene (A$_4$) in the applied formation model of soot. Hence, it is of significance to examine the change of A$_4$ concentrations due to the additional

Table 2. Maximum Mole Fractions of H$_2$, H$_2$O, H, and OH

| case     | H$_2$\(_\text{max}\) | H$_2$O\(_\text{max}\) | H\(_\text{max}\) | OH\(_\text{max}\) |
|----------|------------------------|------------------------|------------------|------------------|
| pure C$_2$H$_4$ | 4.09 x 10^{-2} | 1.28 x 10^{-1} | 4.37 x 10^{-3} | 5.87 x 10^{-3} |
| 10% C$_2$H$_2$ | 4.10 x 10^{-2} | 1.26 x 10^{-1} | 4.39 x 10^{-3} | 5.94 x 10^{-3} |

Figure 4. Predicted CO distribution in the flames: (a) Case 1, (b) Case 3, and (c) Case 5.

Figure 5. Predicted CO$_2$ distribution in the flames: (a) Case 1, (b) Case 3, and (c) Case 5.
acetylene. Figure 8 displays the radial distributions of A4 concentrations in pure C2H4/air flames (Case 1) with 10% C2H2 addition (Case 3) and 10% FC2H2 addition (Case 5) at the height of 0.2, 0.5, and 1.5 cm. Specifically, the relative increments of maximum A4 mole fractions are 13.3, 17.8, and 23.5% at the three different heights, respectively. The chemical actions of acetylene increased the A4 concentration in the annular area above the burner, resulting in higher nucleation rates of soot. It is certain that the distribution of the soot inception rate is consistent with the change trend of the A4 concentration. The increased A4 concentration in the initial period of soot formation indicated that the surface growth condensation rate was also high. Because the first ring structured species in the soot formation model is benzene (A1), which controls the subsequent larger PAH formation, it is also necessary to study the chemical effect of addition of acetylene on A1 concentration. The calculated radial profiles of A1 concentration at the three vertical positions are shown in Figure 9. It is clear that the concentration of A1 increased along with the radial and flow directions, which is aligned with the A4 results shown in Figure 8. Considering the bottleneck role of

Figure 6. Comparisons of the maximum temperature, the maximum centerline temperature, and the maximum SVF of Cases 1, 3, and 5.

Figure 7. Distributions of SVF at the height of (a) 0.14, 0.39, and 2.40 cm and (b) 3.30 and 6.09 cm of Cases 1, 3, and 5.

Figure 8. Simulated A4 mole fractions of Cases 1, 3, and 5 at z = 0.2, 0.5, and 1.5 cm.

Figure 9. Simulated A1 mole fractions of Cases 1, 3, and 5 at z = 0.2, 0.5, and 1.5 cm.
A1 in the formation process of PAHs, it is necessary to analyze in detail the reaction pathway of A1. As stated in refs. 4, 19, 34, and 42 the production steps of A1 are

\[
C_2H_3 + C_2H_5 \leftrightarrow A_1(R234) \tag{7}
\]

\[
n-C_4H_5 + C_2H_2 \leftrightarrow A_1 + H(R296) \tag{8}
\]

\[
1-C_6H_6 + H \leftrightarrow A_1 + H(R348) \tag{9}
\]

\[
n-C_6H_2 \leftrightarrow A_1 + H(R354) \tag{10}
\]

Among them, the self-combination step of C3H3 is the primary pathway of A1 formation in C2H4/air flames.4 The simulated C3H3 mole fractions at the three heights are shown in Figure 10, where the relative increments of peak C3H3 mole fraction are 9.1% (0.2 cm), 14.2% (0.5 cm), and 14.1% (1.5 cm). Obviously, the presence of additional C2H2 chemically promoted the C3H3 concentration at all positions. Furthermore, acetylene had a stronger chemical effect at higher positions and the peak position moved toward the centerline position.

Next, it is also important to investigate the resulting difference of C3H3 mole fractions to further reveal how the chemical effect of acetylene promoted soot formation. C3H3 is produced largely via reactions of CH2 and CH*2 with acetylene. The combination reactions are as follows

\[
C_2H_2 + CH_2 \leftrightarrow C_3H_3 + H(R193) \tag{11}
\]

\[
C_2H_2 + CH*2 \leftrightarrow C_3H_3 + H(R194) \tag{12}
\]

By examining the reaction rates,4,19 it was confirmed that the abovementioned two reactions account for approximately 90% of C3H3 production in ethylene/air-diffusion flames. Consequently, C3H3 concentrations were promoted in the presence of additional C2H2 (see Figure 10). The increased reaction rates of R193 and R194 were due to the higher C2H2 mole fractions (see the radial distributions of acetylene in Figure 11). Moreover, radial distributions of CH2 concentrations at the three vertical positions of Cases 1, 3, and 5 are shown in Figure 12. Specifically, the relative increment of the CH2 concentration at the height of 1.5 cm as shown in Figure 12, due to the chemical effect of addition of acetylene, reached 9.9%. It was identified that CH2 was produced primarily through

\[
R146(C_2H_2 + O \leftrightarrow CH_2 + CO) \tag{13}
\]

The addition of acetylene in the fuel stream significantly increased the C2H2 concentrations at the three vertical positions in the flames, as shown in Figure 11, which consequently formed more CH2 via R146.

It was also noticed that the presence of additional acetylene significantly increased the peak CO mole fraction and also enhanced the peak CO2 mole fraction to a smaller extent. For instance, 10% C2H2 addition caused an increase of 9.6% in the maximum CO concentration (see Figure 4b,c) but only about 3.7% in the maximum CO2 concentration (see Figure 5b,c). It can also be observed from Figures 4 and 5 that acetylene addition increased the concentrations of CO and CO2 along the symmetric centerline. The increment of CO2 concentration was mainly via

\[
CO + OH \leftrightarrow CO_2 + H(R31) \tag{14}
\]

and that of CO was primarily via

\[
C_2H_2 + O \leftrightarrow CH_2 + CO(R146) \tag{15}
\]
Because C₂H₂ is considered to be the only species that promotes soot growth via the HACA mechanism, it is necessary to further explore the reaction pathways of C₂H₂ formation. The chemical effect of adding acetylene to the fuel caused a sharp increase in acetylene concentration in the vicinity of the centerline and until the peak position of acetylene concentration, which remained basically unchanged at the edge of the burner. It is well accepted that C₂H₂ is primarily produced via thermal decomposition of C₂H₄ and the reactions of C₆H₆ with OH and H

\[
\text{C}_2\text{H}_4 \leftrightarrow \text{C}_2\text{H}_2 + \text{H}_2 (R164)
\]

\[
\text{C}_2\text{H}_3 + \text{OH} \leftrightarrow \text{C}_2\text{H}_2 + \text{H}_2\text{O} (R160)
\]

\[
\text{C}_2\text{H}_2 + \text{H} \leftrightarrow \text{C}_2\text{H}_3 + \text{H}_2 (R158)
\]

The majority of C₂H₃ was created from C₂H₄ via the step

\[
\text{C}_2\text{H}_4 + \text{H} \leftrightarrow \text{C}_2\text{H}_2 + \text{H}_2 (R166) \quad (19)
\]

The radial profiles of C₂H₃ at three vertical positions are shown in Figure 13.

\[\text{R}_{\text{c}}=0.2, 0.5, \text{and } 1.5 \text{ cm}.\]

It is evident from the abovementioned analysis that C₂H₃ addition in the C₂H₄ fuel stream chemically enhanced the nucleation rates and also influenced the surface growth rates. The surface growth processes included H-abstraction reactions and C₂H₂ addition reactions to form active sites. The key reactions Csoot* + C₂H₂ ↔ Csoot-H + H (20) and Csoot-H + H ↔ Csoot* + H₂ (21) were hence promoted according to the HACA mechanism. As pointed out in refs 29 and 43 the rate of acetylene addition is determined by the HACA mechanism. The forward (positive) reaction rate of H-abstraction is much higher than that of the reverse reaction. Thus, the increased H concentration (see Figure 14) via C₂H₃ + O ↔ HCCO + H (R144) (22) facilitated the production of more active sites, which in turn led to higher surface growth rates of soot.

Figure 15 shows the reaction rate of soot surface growth Rₜ for the cases of C₂H₄/air flame (Case 1), 10% C₂H₂ (Case 3), and 10% FC₁₁₂ (in the fuel stream (Case 5)). The enhanced 10% maximum surface growth rate was attributed to the chemical effect of acetylene. As reported in ref 44, the surface growth rate of soot is the product of soot surface area per unit volume (Aₜ) and the specific surface growth rate of soot. Figures 16 and 17 provide the predicted distributions of these quantities at the vertical positions of 0.2, 0.5, and 1.5 cm in Cases 1, 3, and 5. It was found that the Aₜ increased, while the specific surface growth rate of soot showed the opposite due to the C₂H₂ addition, which means that the increased Aₜ, not the specific surface growth rate of soot, caused the higher Rₜ. It was also found that the difference of Aₜ was larger than that of the specific surface growth rate of soot (between the blue and red curves), indicating that the chemical effect of acetylene on the larger surface growth rate was caused by the higher Aₜ.

Figure 18 depicts the calculated number density of soot particles at the same three heights. The specific surface area is equal to the product of the number density and the particle size.

The particle size was determined by the specific surface growth rate of the soot, while the number density was controlled by the nucleation rate. As shown in Figures 17 and 18, the chemical effect of acetylene decreased the surface growth rate by about 2.6% (at z = 1.5 cm), while the particle number density increased by about 21.1% (at z = 1.5 cm), manifesting that the larger number density of the soot particle was dominated by the higher nucleation rate.

4.3. Radiative Effect of Acetylene Addition. The radiative effect of acetylene addition to the fuel was “frozen” via the use of the fictitious on-radiating FC₁₁₂ in Case 7 for comparison with Case 5 (of radiating FC₁₁₂). In both cases, the chemical effects of C₂H₂ were excluded. Figures 2c,d and 3c,d depict the 2D distributions of temperature and SVF, respectively. With 10% acetylene addition, the temperature decreased about 1 K and the SVF decreased only 0.01 ppm due to the radiative effect at the same position. To further amplify the radiation effect of adding acetylene on the flame properties, 40% C₂H₂ and 40% FC₁₁₂ with nonradiation acetylene were added to the fuel streams.

5. CONCLUSIONS

A numerical simulation was performed to investigate the effects of acetylene addition in the fuel stream on soot formation in an atmospheric-pressure laminar C₂H₄/air diffusion flame using the open-source code Co-Flame. A soot model based on nucleation by PAH collision, surface growth by PAH-soot condensation or HACA mechanisms, and oxidation reaction was used in conjunction with a detailed C₂ gas-phase chemistry model. The chemical effect of C₂H₂ addition in the fuel stream was “isolated” from other effects by
introducing FC2H2 inert species to the chemical reaction mechanism using seven cases of numerical simulation. The present results revealed that 10% acetylene addition in the fuel stream increased the peak flame temperature by 11.8 K and the peak SVF by 8.5%. It was observed that 10% acetylene addition had strong chemical effects, while on the contrary, it had weak radiative effects on the flames. The main reaction pathways of acetylene were obtained through the steps of C2H4 ↔ C2H2 + H2, C2H3 + H ↔ C2H2 + H2, and C2H3 + OH ↔ C2H2 + H2O. Numerical results showed that the chemical effect of 10% acetylene caused the peak flame temperature to increase by 33 K and the peak SVF by 14.9% but caused the peak centerline temperature to reduce by 1.7%. The added acetylene chemically enhanced the concentrations of A4, A1, and C3H3 in the early period of soot formation. In addition, the chemical effect of acetylene resulted in higher particle number density,
soot specific surface growth rate, and $A_S$, leading to increased soot inception and surface growth rates.

**AUTHOR INFORMATION**

**Corresponding Author**
Shu Zheng — School of Energy, Power and Mechanical Engineering, North China Electric Power University, Beijing 102206, China; orcid.org/0000-0002-6107-8931; Email: shuzheng@ncepu.edu.cn

**Authors**
Xinrong Xie — School of Energy, Power and Mechanical Engineering, North China Electric Power University, Beijing 102206, China
Ran Sui — Department of Mechanical and Aerospace Engineering, Missouri University of Science and Technology, Rolla 65409, Missouri, USA; orcid.org/0000-0003-3758-7506
Zixue Luo — State Key Laboratory of Coal Combustion, Huazhong University of Science and Technology, Wuhan 430074, Hubei, China
Shi Liu — School of Control and Computer Engineering, North China Electric Power University, Beijing 102206, China
Jean-Louis Consalvi — Aix-Marseille Université, IUSTI/UMR CNRS 7343, Marseille Cedex 13 13453, France

Complete contact information is available at: https://pubs.acs.org/10.1021/acsomega.1c00740

**Notes**
The authors declare no competing financial interest.

**ACKNOWLEDGMENTS**

S.Z. was supported by the National Key Research Development Program of China (no.2017YFB0601900), the National Natural Science Foundation of China (nos. 51976057, 51922040, and 51827808), the Fundamental Research Funds for the Central Universities (nos. 2020JG005 and 2019QN014), and the Foundation of State Key Laboratory of Coal Combustion (no. FSKLCCA2104).

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