Spectropolarimetric analysis of an active region filament

I. Magnetic and dynamical properties from single component inversions

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ABSTRACT

Aims. The determination of the magnetic filed vector in solar filaments is made possible by interpreting the Hanle and Zeeman effects in suitable chromospheric spectral lines like those of the He$^\text{i}$ multiplet at 10 830 Å. We study the vector magnetic field of an active region filament (NOAA 12087).

Methods. Spectropolarimetric data of this active region was acquired with the GRIS instrument at the GREGOR telescope and studied simultaneously in the chromosphere with the He$^\text{i}$ 10 830 Å multiplet and in the photosphere Si$\text{i}$ 10 827 Å line. As has been done in previous studies, only a single-component model was used to infer the magnetic properties of the filament. The results are put into a solar context with the help of the Solar Dynamic Observatory images.

Results. Some results clearly point out that a more complex inversion had to be performed. First, the Stokes $V$ map of He$^\text{i}$ does not show a clear signature of the presence of the filament. Second, the local azimuth map follows the same pattern as Stokes $V$; it appears that polarity of Stokes $V$ is conditioning the inference to very different magnetic fields even with similar linear polarization signals. This indication suggests that the Stokes $V$ could be dominated from below by the magnetic field coming from the active region, and not from the filament itself. This evidence, and others, will be analyzed in depth and a more complex inversion will be attempted in the second part of this series.

Key words. Sun: filaments, prominences – Sun: chromosphere – Sun: magnetic fields – Sun: infrared – Sun: evolution

1. Introduction

Solar filaments and prominences are cool chromospheric over-dense plasma structures embedded in the extremely hot and less dense corona. They appear as dark filamentary structures when seen on the disk as absorption in the core of some strong chromospheric lines (e.g., H$\alpha$ or Ca$\text{ii}$), other weak chromospheric lines such as the He$^\text{i}$ multiplets at 10 830 Å and 5876 Å ($D_3$), and in the extreme ultraviolet continuum. They are called prominences when they are seen as diffuse bright clouds at the limb as they scatter light from the underlying disk.

Magnetic fields play a fundamental role in the formation, support, and eruption of these structures. The topology of the magnetic field is a key point because the magnetic force can balance the solar gravitational force and support the plasma in places where the fields are upward-curved, forming dips. Although it is a fundamental ingredient, its topology is not well known. Different theoretical models have been developed proposing magnetic configurations with dipped field lines. Magnetic dips can be created by the weight of the prominence plasma (Kippenhahn & Schluter 1957) or they can exist in the absence of prominence plasma in force-free models as a horizontal flux rope (Aulanier et al. 1998; Kuperus & Raadu 1974) or a sheared arcade (Antiochos et al. 1994). Magnetic dips can even be created by a tangled magnetic field (van Ballegooijen & Cramer 2010), thus explaining prominences with vertical threads.

While intensity observations of prominence fine structure provide some clues to the magnetic topology, the only method for constraining theoretical models is the empirical determination of the prominence magnetic field from the inversion of spectropolarimetric data (Harvey 2006). The inference of prominence magnetic fields is not straightforward since there are only a few chromospheric spectral lines with sufficient opacity to sample the chromosphere, which in turn have such a wide and high formation region that they have to be modeled under complex non-local thermodynamic equilibrium (NLTE) effects, such as the atomic polarization and the Hanle effect (Landi Degl’Innocenti & Landolfi 2004).

The He$^\text{i}$ multiplets at 10 830 Å and 5876 Å are a suitable pair of diagnostics for such studies because they present a good compromise between sensitivity to chromospheric magnetic fields and complexity of the numerical modeling. The He$^\text{i}$ 10 830 Å multiplet has several advantages: it can be easily seen in emission in off-limb prominences (e.g., Orozco Suárez et al. 2014; Martínez González et al. 2015) or in absorption in on-disk filaments (e.g., Lin et al. 1998; Collados et al. 2003; Merenda et al. 2007; Kuckein et al. 2009; Sasso et al. 2011), and it is sensitive to magnetic fields in a wide range from dG to kG thanks to the joint action of atomic level polarization and the Hanle and Zeeman effects. These lines have been used since the 1970s (Leroy et al. 1977), and they were consolidated as a very useful diagnostic tool for this type of structures after Trujillo Bueno et al. (2002) demonstrated how the polarized light arises from selective absorption and emission processes induced by the solar anisotropic illumination and its dependence on the scattering...
geometry. Since then, these spectral lines have been increasingly used to infer the magnetic field vector in chromospheric structures.

Filaments can be categorized by their location on the Sun and are generally considered to have very different magnetic structures and formation processes. In one limit we find quiescent filaments (QSs), with lifetimes of up to a few months, hundreds of Mm in length and height, and magnetic field strengths on the order of a few tens of G (Trujillo Bueno et al. 2002; Casini et al. 2003; Merenda et al. 2006; Orozco Suárez et al. 2014; Martínez González et al. 2015). On the other limit, we find active region (AR) filaments that are formed on active regions or sunspots; they develop at lower heights in the solar atmosphere (<10 Mm, Aulanier & Démoulin 2003; Lites 2005), have short lifetimes (hours to days), are short (over 10 Mm), and have magnetic field values larger than those of QS filaments. Sometimes the term intermediate filaments is used when no clear classification as QS or AR is possible (Mackay et al. 2010).

The linear polarization of the He\textsc{i} 10830 Å in QS filaments is dominated by atomic level polarization induced by the anisotropic illuminating radiation field coming from lower layers (Trujillo Bueno et al. 2002; Martínez González et al. 2015). However, AR filaments have been found under a wider variety of conditions. For example, Kuckein et al. (2009) studied the magnetic field vector of an active region filament above a strongly magnetized region. Their signals were dominated by the Zeeman effect with almost no evidence of atomic polarization. They found, with a Zeeman-based Milne-Eddington (ME) inversion code, the highest field strengths measured in filaments to date, with values around 600–700 G. Their conclusion was that strong transverse magnetic fields are present in AR filaments. After that, Sassu et al. (2011, 2014) studied a complex flaring active region filament during its phase of increased activity with an ME inversion code (HuLx; Lagg et al. 2004) including the Hanle effect, as they detected atomic level polarization signatures in their observed profiles. They found values for the magnetic field strength in the range 100–250 G, requiring up to five independent atmospheric components coexisting within the same resolution element (≈1.2") to reproduce their line profiles. Another measurement was reported by Xu et al. (2012), who inverted the same filament as Sassu et al. (2011), but before the eruption during the stable phase. They used again the Zeeman-based ME inversion (HuLx\textsuperscript{3}; Lagg et al. 2009) because they did not find any clear signatures of atomic level polarization or the Hanle effect. Their observation displayed a section of the filament above the granulation with weaker inferred magnetic fields (≈150 G) and a second section above a strongly magnetized area, which returned much higher magnetic field strengths during the eruption (≈750 G).

At that time, the nondetection of signatures of the presence of atomic level polarization was quite surprising (Kuckein et al. 2009; Xu et al. 2012), Trujillo Bueno & Asensio Ramos (2007) and Casini et al. (2009) noted that, even for such strong fields, AR filament spectropolarimetric observations should show signatures of scattering polarization and the Hanle effect in normal conditions. To explain this, Trujillo Bueno & Asensio Ramos (2007) suggested that a reduction of the radiation field anisotropy due to the horizontal radiation inside the filament could reduce the atomic level polarization, while Casini et al. (2009) suggested that an unresolved magnetic field could also explain the observation.

Taking into account all these measurements, the highest inferred magnetic field values seem to be associated with filaments above highly magnetized areas. Based on this idea, Díaz Baso et al. (2016) suggested that filaments could be quite transparent to polarization, with the highest values for the magnetic field being produced by the active chromosphere below, and not from the filament itself. By adopting a two-component model (one slab for the filament and another for the chromosphere below) these authors reproduce the profiles in Kuckein et al. (2009) without suppressing the atomic polarization. The lack of atomic polarization found in Kuckein et al. (2009) could be due to a cancellation of the total atomic polarization signal from the two corresponding components. From their model, weak fields can be also inferred in AR filaments.

In the light of these results the magnetic field strength inferred in prominences is still a matter of debate. At present, a high-quality polarimetric observation is a challenge and the inference of the magnetic field vector in the Hanle regime is subject to several potential ambiguities (Orozco Suárez et al. 2014; Martínez González et al. 2015).

To shed some light and better understand the problems during the inference, we present a first analysis of ground-based spectropolarimetric observations of the He\textsc{i} 10830 triplet taken in an active region filament. We first describe the observations and then explain the diagnostic technique. We study the observations with state-of-the-art inversion codes including the Hanle effect and the Zeeman effect to retrieve the physics from the polarimetric signals. During this study we show the limitations of using a one-component model, as has been common practice. We then use the Bayesian framework to study the Hanle ambiguities, the uncertainties, and the sensitivity of some parameters in the inference.

2. Observations, context data, and filament evolution

The observations were carried out at the GREGOR telescope (Schmidt et al. 2012) on the 17 June 2014 using the GREGOR Infrared Spectrograph (GRIS; Collados et al. 2012). The slit (0.14” wide and 65” long) was placed over the target, an active region filament close to a sunspot in the active region NOAA 12087 at coordinates +187°, –327°, which correspond to a heliocentric angle of θ ≈ 23° (μ = cos θ = 0.92). Six scans of the full sunspot were taken with a scanning step of 0.14”, which provided us with a map of size 65” × 27″. The first scan started at 08:00 UT and the last one finished at 17:30 UT. Each one lasts ~15 min. The rotation compensation of the alt-azimuthal mount in GREGOR was not yet available, so we witnessed some image rotation effects, especially in the borders of the slit. By calculating the power spectrum of the continuum intensity in the quiet Sun we estimated the spatial resolution to be about 0.4″.

The observed spectral range spanned from 10 824 Å to 10 842 Å, with a spectral sampling of 18.1 mÅ pixel\textsuperscript{-1}. This spectral region contains the chromospheric He\textsc{i} 10830 Å triplet originating from the electron transition 2\textsuperscript{3}S\textsubscript{1} \rightarrow 2\textsuperscript{3}P\textsubscript{2,1,0}. It comprises a component at 10 829.0911 Å (J\textsubscript{0} = 0), usually known as the “blue” component, and two components at 10 830.2501 Å (J\textsubscript{0} = 1) and at 10 830.3397 Å (J\textsubscript{0} = 2), blended at solar chromospheric temperatures, and usually known as the “red” components. The GRIS spectral range with the above-mentioned spectral lines is displayed in Fig. 1 together with the average intensity spectrum of the quiet Sun of our observations.

We show one of the reconstructed maps of the observed active region in Fig. 2, where the x-axis represents the position.
along the slit and the y-axis is the scanning direction. The upper panel of the figure shows the Stokes I map of the observed region in the continuum at 10 841.3 Å, and the lower panel shows the same region in the core of the red component of the helium triplet at 10 830.3 Å, normalized to the continuum intensity of the quiet Sun. The filament is visible in the core of the HeI line with a length of about ~30′′ (22 Mm) and a width of ~3′′ (2 Mm). These images show that the observations were carried out under very good seeing conditions. The granulation pattern and chromospheric absorption features with subarcsecond fine structure are both prominently visible.

2.1. Reduction process

The standard data reduction procedure for GRIS (Collados 1999, 2003) was applied to all the data sets. This reduction includes bad pixel correction, dark current subtraction, flat-field correction, telescope and polarimeter calibration, demodulation, beam merging, and correction of residual fringes. To improve the signal-to-noise ratio of the data we averaged 2 spectral pixels and 4×4 spatial pixels, yielding a final spectral and spatial sampling of 36.2 mÅ pix⁻¹ and 0.55″ pix⁻¹, respectively, and a noise level in Stokes (Q, U, V) estimated from the standard deviation of the continuum, on the order of (4, 4, 6)×10⁻⁴ in units of the continuum intensity, I₀.

The next step is to correct spurious light trends and fringes that persist after the flat-fielding. The continuum intensity trends are corrected by comparison with the Fourier Transform Spectrometer (IFS; Neckel & Labs 1984) atlas. This atlas has a very high signal-to-noise ratio, no spectral stray light, and a very accurate continuum level. Following Allende Prieto et al. (2004) and Franz et al. (2015), the IIFS(λ) is modified to be comparable to our spectrum IQS(λ), generating a new intensity profile INFTS(λ):

\[ I_{\text{NFTS}}(\lambda) = \alpha G(\sigma) * I_{\text{IFS}}(\lambda) + (1 - \alpha) G(\sigma) * I_{\text{IFS}}(\lambda). \]  

In order to take into account the different spectral resolution of our instrument, IIFS(λ) is convolved with a Gaussian G(σ) with a standard deviation σ. Then, we add another term \((G(\sigma) * I_{\text{IFS}}(\lambda))\), which is the average over the same spectral range of the convolved spectrum; it does not depend on the wavelength. This allows us to characterize the amount of nondispersed spectrum (light that reaches the detector without passing through the grating) by the stray light factor α.

We create our IQS spectrum as an average of the quiet areas available in our observations to mimic the atlas. To compare the two spectra, we performed a wavelength calibration using the photospheric lines of the atlas. Consequently, our wavelength reference and line-of-sight (LOS) velocity is the photospheric average motion. After the calibration, the dispersion obtained is 18.10 ± 0.01 mÅ pix⁻¹.

The values of α and σ are unknown and can be calculated with a least-squares fit of the merit function

\[ \chi^2 = \sum_i [IQS(\lambda_i) - INFTS(\lambda_i)]^2 \cdot w_i, \]  

where \(w_i\) is a parameter to reduce the weight of the wavelengths of the telluric lines. This weight is introduced because the telluric lines vary too much between observations. This weight is also applied to other spectral lines that could be highly dynamic, such as the chromospheric HeI 10 830 Å. Figure 3 shows an example of the result when the values of α and σ are calculated, and the fringe pattern is obtained from the ratio IQS(λ)/INFTS(λ). This ratio \(f(\lambda)\) is then smoothed or fitted with a spline in our case and used to correct all the pixels of the map by multiplying each of the Stokes parameters by \(f(\lambda)\). For the data analyzed in this study, the values are α ~ 15% and σ ~ 70 mÅ.

For short-period fringes another method proved to be more efficient. These fringes are produced by interference due to multiple reflections on flat surfaces in the optical path. They are often corrected using Fourier filtering, but this standard procedure does not meet our requirements. We checked that this component is almost unpolarized and it is mainly seen in Stokes I. A first attempt to remove this component using Fourier or wavelet decomposition was unsuccessful; the periods of the fringes change along the spectrum, which makes it difficult to isolate them by simply using a threshold in the frequency domain. Thus, to remove this component we used a technique based on the Relevance Vector Machine method¹ (RVM; A python implementation of this tool can be found at https://github.com/aasensio/rvm
Tipping (2000) to decompose the original signal into two components, the clean spectra $I_0(\lambda)$ and the fringes $I_1(\lambda)$:

$$I(\lambda) = I_0(\lambda) + I_1(\lambda).$$

(Fringes have a narrow range of periods and amplitudes that are not a very high; most importantly, they are present over the entire spectral range, while spectral lines are present only in some parts of the spectrum. With these properties it seems convenient to use two dictionaries (in general, an incomplete non-orthogonal basis set) with different properties to decompose the two components. The first dictionary is made of Gaussian functions centered at several wavelengths $\lambda_j$ around the spectral lines with different widths $\Delta \lambda_j$. This dictionary is especially good at fitting the clean spectrum $I_0$ with just a few active elements. The second dictionary is made of sine and cosine functions of different periods $\omega_j$, similar to those of the fringes $I_1$. This dictionary is especially suited to fit the fringes with only a few active elements. This problem can be mathematically described as a linear regression problem with $N$ coefficients $\mathbf{w} = (w_0, w_1, ... , w_G, w_S)$ such that

$$I(\mathbf{w}, \mathbf{A}) = w_0 + \sum_{j=1}^{G} w_j \exp \left[ -\left( \frac{\lambda - \lambda_j}{\Delta \lambda_j} \right)^2 \right] + \sum_{j=0}^{(N-G)/2} w_j \sin(\omega_j \lambda) + \sum_{j=(N-G)/2+1}^{N} w_j \cos(\omega_j \lambda),$$

where $G$ is the number of Gaussian functions. We note that half of the $N-G$ coefficients are associated with the sine function and the other half with the cosines. We generated a dictionary with 3000 Gaussian functions and 400 sinusoidal functions with widths $\Delta \lambda$ between 5 and 10 pixels and frequencies $\omega$ between 0.4 and 0.8 pixel$^{-1}$. Given that the two dictionaries are very incoherent, it becomes hard to fit the spectral lines with the second dictionary and vice versa. For the continuum level, the free parameter $w_0$ is used. Therefore, the RVM method works by imposing a sparsity constraint on the coefficients of the dictionaries (forcing many elements of the dictionary to be inactive). With this method we managed to fit the spectrum at each position to separate the two contributions. Finally, the clean spectrum is obtained as the spectral line contribution $I_0(\lambda)$ without the fringes (see Fig. 4). In this figure, this routine is able to separate fringes with 60 sines and cosines and 100 Gaussian functions. Moreover, we do not have to worry about the Gaussians far from spectral lines because with the sparsity condition they are only activated if necessary. After this final step the data is ready to be analyzed.

No residual polarization is visible in the telluric lines. Thus, errors in the polarization calibration (which could appear as crosstalk) are significantly smaller than the Stokes $Q$ and $U$ signals that are the main focus of this work.

To precisely determine the reference direction for $Q > 0$ (an important parameter of our observation and inversion code), we tried to infer it directly from the observed maps. We found some discrepancies with the direction returned by the reduction pipeline. For the sake of consistency we calculated this direction using the observations. Given that we observed a relatively round sunspot, we made the assumption that the magnetic field is oriented radially (in the sky plane) from the center of the umbra, something that is indeed observed as we show in the next sections. We find the reference direction for $Q > 0$ by locating the direction where the integrated Stokes $Q$ profile is maximum, which should coincide with an almost zero Stokes $U$. This direction is different depending on the rotation of each scan.$^{2}$ For the fifth scan, the $Q > 0$ direction is at 23.7$^\circ$ and the disk center is at a direction of 120.3$^\circ$, both measured counterclockwise from the horizontal (slit) axis (see Fig. 2). The spine of the filament is at $\sim$42$^\circ$ from the horizontal axis.


2.2. Solar context

In order to put the GRIS observations in context, we made use of the data provided by some band-pass filters of the Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) instrument and the Helioseismic and Magnetic Imager (HMI; Scherrer et al. 2012) on board NASA’s Solar Dynamics Observatory (SDO; Pesnell et al. 2012). The top panel of Fig. 5 shows a SDO/HMI image at the continuum of 6173 Å of the NOAA 12087 region, which we analyze here. The red box in Fig. 5 outlines the GRIS field of view (FOV). The HMI spatial resolution is about $1.2''$ (Yeo et al. 2014). Due to the thermal structure of prominences, they can be seen in UV-EUV images. Several studies have

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Fig. 5. Active region NOAA 12087, with a contour showing our observed region (top) and AIA maps in the different wavelengths indicated at the top of each panel. Even though the filament seems to be aligned with the coronal loops that are linking the two sunspots, the filament is not detected in these maps.

Fig. 6. Time evolution of the flux (in arbitrary units) integrated over the active region area for some filters. The six gray areas define the intervals of each scan (~15 min).

Fig. 5 shows a very bright coronal loop linking the first and the third sunspot of the region (counting from left to right) in the AIA images. This brightness is enhanced in the feet and the apex of the loop. Our observed filament as seen in the core of He\textsc{i} is overlapped with a white contour. The He\textsc{i} absorption does not clearly correlate with any of the AIA channels. The reason might be that the filament we observed is low-lying, while the emission of higher coronal loops dominates the intensity measured in the AIA channels.

2.3. Evolution of the filament

During the day of the observation several flares occurred. In particular, at the same time as our spectropolarimetric measurements, a GOES class B5\textsuperscript{3} flare erupted in the central part of the active region inside our FOV. Since GOES observes the whole solar disk, we had to verify this, calculating the time evolution of the flux of the active region, which is shown in Fig. 6. We used different filters such as the AIA channels at 304 Å, 335 Å, 94 Å, and H\textalpha\ obtained by the GONG network (Hill et al. 1994).

Figure 6 displays a clear peak during the fourth scan. The energy is released close to the central part of the filament, but not exactly above the filament. Figure 5 shows this compact bright point at (170′′, −320′′). We see a sudden and intense variation in brightness from 09:35 to 09:46UT in the 94 Å and 304 Å channels, and a weaker brightening in the remaining filters. We do not detect either emission intensity profiles of the He\textsc{i} or a significant decrease in the intensity profiles during the flare, in con-

\textsuperscript{3} We recall that the class of each flare is chosen according to its X-ray flux detected by the NOAA GOES satellites in the wavelength range 1–8 Å.
two feet of the big loop, as some brightening at (200′′) layers above the filament, and the energy is redirected toward the X-rays. Another possibility is that the flare occurs at higher contrast to what has been found other studies (Sasso et al. 2011; Kuckein et al. 2015; Judge et al. 2015), possibly because our flare is one or two orders of magnitude less energetic than theirs Kuckein et al. 2015; Judge et al. 2015), possibly because our contrast to what has been found other studies (Sasso et al. 2011; Kuckein et al. 2015; Judge et al. 2015), possibly because our filament and the flares, if reconnection events are taking place, destabilize the filament structure seen in the He\textsc{i} triplet. After \( \lambda_{0} \) of the He\textsc{i} triplet does not exhibit an evident correlation with the filament, we can detect a strong signal coincident with the body of the filament in Stokes \( V \) for the Si\textsc{i} line at 10827.1 Å (in the left column) and for the red component of the He\textsc{i} triplet at 10830.3 Å (in the right column). White contours show the signal above three times the noise level. Solid line contours indicate positive signals while negative signals are displayed with dashed line contours. Red contours display the location of the absorption features (i.e., the filament). The linear polarization maps of the silicon line show strong signals in the penumbra of the sunspot. Although the Stokes \( Q \) amplitude of the He\textsc{i} triplet does not exhibit an evident correlation with the filament, we can detect a strong signal coincident with the body of the filament in Stokes \( U \). The average Stokes \( U \) signal at the line core within the filament is around \( 1.5 \times 10^{-3} I \).

Finally, in the last row of Fig. 8 we display the Stokes \( V \) maps for the Si\textsc{i} and He\textsc{i} lines. The Si\textsc{i} Stokes \( V \) map shows the polarity of the magnetic field in the whole area (pointing toward the observer in blue and away in red). Interestingly, the He\textsc{i} Stokes \( V \) map does not show any correlation with the filament at all and it is very similar to the photospheric map, but more diffuse. This contrast to what has been found other studies (Sasso et al. 2011; Kuckein et al. 2015; Judge et al. 2015), possibly because our filament and the flares, if reconnection events are taking place, destabilize the filament structure seen in the He\textsc{i} triplet. After \( \lambda_{0} \) of the He\textsc{i} triplet does not exhibit an evident correlation with the filament, we can detect a strong signal coincident with the body of the filament in Stokes \( V \) for the Si\textsc{i} line at 10827.1 Å (in the left column) and for the red component of the He\textsc{i} triplet at 10830.3 Å (in the right column). White contours show the signal above three times the noise level. Solid line contours indicate positive signals while negative signals are displayed with dashed line contours. Red contours display the location of the absorption features (i.e., the filament). The linear polarization maps of the silicon line show strong signals in the penumbra of the sunspot. Although the Stokes \( Q \) amplitude of the He\textsc{i} triplet does not exhibit an evident correlation with the filament, we can detect a strong signal coincident with the body of the filament in Stokes \( U \). The average Stokes \( U \) signal at the line core within the filament is around \( 1.5 \times 10^{-3} I \).

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Anisotropic radiative pumping, the Hanle effect, acts on the polar-
ization through the Hanle effect can be inferred from Fig. 8. In
the absence of magnetic fields, due to geometrical consid-
erations we expect all the linear polarization to be parallel to
the closest limb (Bommier et al. 1989; Trujillo Bueno et al.
2002). Since our Stokes $Q$ and $U$ profiles are not visible in
Stokes $V$. However, Fig. 8 shows that the linear polarization
signal is fundamentally contained in Stokes $Q$, while Stokes $U$
and Stokes $V$ are barely detectable. This modification of the
polarization is a clear signature of the magnetic field acting via
the Hanle effect (Landi Degl’Innocenti & Landolfi 2004).

We also note from the lower row of Fig. 9 that both Stokes $Q$
and $U$ profiles extracted from the filament show polarization in
the blue component ($\lambda$ in this figure) of the Hei multiplet.
Since the upper level of the blue level ($^3P_0$) has angular momentum
$J = 0$, it cannot be polarized and the emitted radiation has to be
unpolarized. The polarization is then a consequence of dichroism
because the lower level ($^3S_1$) has angular momentum $J = 1$ and
and can be polarized (Trujillo Bueno et al. 2002). We expect the sig-
als in the blue and red components to have opposite signs given
their polarizability, which is defined as a factor that depends on
the quantum numbers of the transition and accounts for the trans-
formation of the properties of the radiation field into atomic pop-
ulations. This is not the general behavior in our observations. We
discuss this issue in detail in the second part of the series. For the

3.2. General description of the helium profiles

In this section we describe the morphology of the observed Hei
Stokes profiles. In general, it is possible to have a quite pre-
cise idea of the main mechanism that dominates the polarization
signals in each region by the shape of the Stokes parameters.
Anisotropic radiative pumping, the Hanle effect, and the Zeeman
effect work together to shape the polarization of the Hei triplet.
Hence, when we refer to each Stokes parameter they are normali-
ted to their local continuum, $I_{LC}$, computed in the same pixel and
in the nearby spectral continuum region. More details are given in Sect. 3.3.2.

The strong absorption observed in Fig. 2 cause broader and
deeper Stokes $I$ profiles compared to the quiet regions. For a
pixel inside the filament we observe signatures of scattering
polarization (and likely Hanle effect) in Stokes $Q$ and $U$. As an
example, the lower four panels of Fig. 9 display typical Stokes
profiles of that area. The Hei profiles exhibit the usual single-
lobed symmetric shape in linear polarization (Trujillo Bueno
et al. 2002). Contrary to the Zeeman effect, the presence of
a magnetic field is not necessary in general to produce polar-
ization signals, which are generated by scattering processes.
However, the presence of a magnetic field affecting the polar-
ization through the Hanle effect can be inferred from Fig. 8.
moment, and given the small amplitude of the blue component, we neglect its effect on the single component inversion presented in this first analysis.

Far from the filament and close to the sunspot the linear polarization signals exhibit the typical Zeeman profiles in Stokes \( Q \) and \( U \). These profiles are characterized by three lobes in the linear polarization as we see from the profiles shown in the upper row of Fig. 9 that have been extracted from the penumbra of the sunspot. This region is Zeeman-dominated, and consequently for this spectral line the magnetic field strengths are expected to be in the hG–kG regime.

In order to visually localize each profile in the observed FOV and, consequently, which mechanism dominates the polarization signals, we classified the Stokes \( Q \) and \( U \) profiles using a \( k \)-means clustering algorithm (Hartigan & Wong 1979). Figure 10 shows the location of single-lobed profiles in red and three-lobed profiles in blue. The specific value of each pixel is set by the class-value \( C \) (+1 for single-lobed and −1 for three-lobed profiles) multiplied by the absolute value of its linear polarization signal: \( C \cdot |Q(\lambda_0)| + C_U \cdot |U(\lambda_0)| \), where \( C_Q \equiv \pm 1 \) and \( C_U \equiv \pm 1 \) depending on the shape of the profile in this Stokes parameter, and \( \lambda_0 \) is the center of the red component of the He \( i \) triplet at 10 830.3 Å. This product enhances those pixels where the classification is reliable and sets closer to zero those areas where the profile is very noisy. Finally, the result is normalized to the maximum value of the map.

Concerning Stokes \( V \), the whole map shows the typical antisymmetric circular polarization profile generated by the longitudinal Zeeman effect. We note that the Stokes \( V \) signal in the filament is weaker than in the sunspot. Sometimes, the regular shape is hard to distinguish because of the noise, but we can safely say that no orientation-induced signals like those of Martínez González et al. (2012) are found.

3.3. Inference of dynamic and magnetic properties

3.3.1. Photospheric inference

The Si \( i \) 10 827 Å line in the observed spectral range allows us to extract the thermodynamic and magnetic information of the photosphere below the filament. As described before, other photospheric Ca \( i \) lines are located a few angstroms toward the red (Joshi et al. 2016; Felipe et al. 2016), but the Si \( i \) 10 827 Å is enough to have an estimation of the photospheric magnetic field. Some studies have demonstrated that the formation of the Si \( i \) line presents some departures from local thermodynamic equilibrium (Bard & Carlsson 2008; Shchukina et al. 2017), with the core of the silicon line originating in the upper photosphere. Non-LTE effects are certainly non-negligible in the estimation of the temperature stratification, but the impact on the inferred magnetic field is limited (Kuckein et al. 2012a). For this reason we use an LTE inversion code, which is less accurate but faster than non-LTE inversion codes.

The Si \( i \) line has a moderate magnetic sensitivity with an effective Landé factor of \( \tilde{\lambda} = 1.5 \). We checked with the Stokes \( V \) response functions (RFs) to the magnetic field that the highest sensitivity is found close to \( \log(\tau) = −2.2 \) (Kuckein et al. 2012a; Felipe et al. 2016), where \( \tau \) corresponds to the continuum optical depth at 5000 Å. All the physical magnitudes inferred from the Si \( i \) line are displayed in the following at that height. The Si \( i \) 10 827 Å line was inverted using the Stokes Inversion based on Response functions code (Sir, Ruiz Cobo & del Toro Iniesta 1992),
which assumes LTE and hydrostatic equilibrium to solve the radiative transfer equation. We carried out a pixel-by-pixel inversion with an initialization of the inclination of the magnetic field given by the Stokes V polarity (45° if the blue lobe is positive and 135° if it is negative).

SIR inversions require an initial guess for the atmospheric model. We chose the Harvard-Smithsonian Reference model Atmosphere (HSRA, Gingerich et al. 1971), covering the optical depth range $-5.0 < \log(\tau) < 1.4$. We added to the HSRA model a magnetic field strength of 500 G. The inversions were performed in three cycles. The temperature stratification $T(\tau)$ was inverted using 2, 3, and 5 nodes in each cycle, and two nodes were used for magnetic field strength $B(\tau)$, magnetic field inclination $\Theta(\tau)$, and LOS velocity $V_{\text{LOS}}(\tau)$. The magnetic field azimuth $\Phi$ was set constant with height. The solar abundances were taken from Asplund et al. (2009), while the atomic data for the Si i 10 827 Å line was obtained from Borrero et al. (2003). The results of the inversion are shown in Sect. 4.

3.3.2. Chromospheric inference

To extract physical information from the chromospheric He i 10 830 Å triplet we used the inversion code HAnle and ZEeman Light (Hazel; Asensio Ramos et al. 2008). This code is able to infer the magnetic field vector from the emergent Stokes profiles considering the scattering polarization and the joint action of the Hanle and Zeeman effects. It assumes a slab of constant physical properties located at a certain height over the visible solar surface, illuminated by the photospheric continuum and permeated by a deterministic magnetic field. This slab model is fully described using nine parameters: the optical depth $\tau_0$ in the core of the red component, the damping parameter, the Doppler width, the LOS velocity of the plasma, the height, the heliocentric angle, and the three components of the magnetic field vector. The radiation anisotropy due to the center-to-limb variation is taken into account. Hazel modifies iteratively the parameters of the slab model in order to produce a set of synthetic Stokes spectra that best match the observed spectra using a least-squares algorithm.

As suggested in Asensio Ramos et al. (2008), we used a two-step procedure in the inversion process. First we obtained the optical depth, the velocity in the LOS, and the Doppler width from Stokes $I$. Then, we inferred the magnetic field vector using all the Stokes parameters, keeping the already inverted parameters fixed. To fully characterize the incident radiation field, we needed to determine the height $h$ of the filament above the solar surface. In our case, this height could not be measured since we saw the filament from above, as the LOS was almost perpendicular to the solar surface at that point. For this reason, we used a typical value of $h = 3'' \approx 2200$ km above the surface (Kuckein et al. 2012a; Yelles Chaoouche et al. 2012; Mackay et al. 2010) for the whole FOV, as we did not know a priori whether the filament was located much higher above the solar surface than the rest of the FOV. To validate our choice, we used the projected distance between the polarity inversion line obtained from the Si i and He i lines. Under the assumption that the polarity inversion line (PIL) lies roughly at the same local vertical position, we can use the projected distance in the sky and associate it to a difference in height. In our observation we find a difference of $\sim 1.5''$, which corresponds to $\sim 2000$ km using Eq. (1) in Joshi et al. (2016). Assuming an average formation height for the Si i line of $\sim 300$ km (Shchukina et al. 2017), we find that the filament lies at $h \sim 2300$ km above the surface, similar to the height that we use. We extend the discussion on the height of the filament in Sect. 5.3.

While the anisotropy of the radiation field used in Hazel to compute the density matrix is computed using the center-to-limb variation of the photospheric continuum (Cox 2000), the boundary condition used for the formal solution of the radiative transfer equation to get the emergent Stokes profiles can change from pixel to pixel, and it has to be provided to Hazel. Moreover, the data must be normalized to its local continuum $I_C$. This is sometimes difficult because the nearby Si i line has strong wings. Therefore, we used the inversion of SIR to model the Si i line profile. We extended the synthetic wing toward the He i line and then normalized the spectrum by the synthetic profile. The nearby telluric lines were also removed by modeling them wherever they are not blended with the He i triplet. We modeled the variation with time of the telluric lines by fitting a Voigt profile. After this correction we were ready to invert the data. Figure 11 displays an example of this normalization procedure showing the important contributions of the silicon and telluric lines. After applying this normalization, the filament absorption remains visible in the core intensity map, while the granulation pattern and the sunspot disappear.

To fix the reference system for these observations, we chose a projection of the X-axis on the plane of the sky in the radial direction pointing toward the disk center (i.e., the local azimuth angle is $\phi = 180^\circ$). The angle between the radial direction (X-axis) and the $Q > 0$ reference of the polarimeter ($\epsilon_1$, see Landi Degl’Innocenti & Landolfi 2004; Asensio Ramos et al. 2008) is $\gamma \sim 83^\circ$ for the fifth scan.

A reliable inversion of the He i multiplet required the above-mentioned spatial and spectral binning. Even after the rebinning, the polarimetric signals are only few times above the noise. Having a reliable determination of Stokes $V$ is fundamental in order to correctly infer the strength of the magnetic field. The reason is that between 10 and 100 G the He i 10 830 Å multiplet is in the Hanle saturation regime, where the linear polarization is only sensitive to the direction of the magnetic field and not to its strength. Therefore, the only way to infer the full magnetic field vector is through the full Stokes vector. The results of the inversion are shown in the next section.

\footnote{See the Hazel manual for a detailed explanation of how to carefully calculate these angles: http://aasensio.github.io/hazel/refsys.html}
4. Inversion results

4.1. Magnetic field vector in the LOS reference frame

Figure 12 shows the magnetic field strength, inclination, azimuth, and LOS velocity maps for the fifth scan, all of them in the LOS frame ($\Theta_B, \Phi_B$). We note that the azimuth and inclination of the He i line were transformed from the local reference frame (the one used by HAZEL) to the LOS reference frame to properly compare the silicon and the helium inversion. The photospheric magnetic field strength map shows a $\sim$2 kG sunspot with only half of the penumbra visible. In the chromosphere, the magnetic field strength of the sunspot reaches values of $\sim$1 kG.

The magnetic field strength map shows that the lowest values are associated with the location of the filament, especially in the chromosphere. The magnetic field strength of the area coinciding with the filament shows values around 50–150 G, similar to those quoted by Sasso et al. (2014). The LOS inclination map shows how the FOV is split into two polarities with a very narrow PIL following the filament in the chromosphere, but not as well aligned in the photosphere. Concerning the azimuth, and ignoring for the moment that other ambiguous solutions exist, the results show a penumbra with a clearly radial magnetic field. We can affirm this with confidence because we are only affected by the 180° ambiguity in this Zeeman-dominated region. The azimuth in the umbra is not reliably retrieved for He i since the magnetic field is more vertical and Stokes $Q$ and $U$ have lower amplitudes. Given the multiple potential solutions for the azimuth in the chromosphere, it is possible to find fields compatible with the observations that are parallel or perpendicular to the filament. We study this problem in more detail in Sects. 4.3 and 5.

4.2. Azimuth in the local frame

Because of the relative simplicity of solving the 180° ambiguity in the interior of the sunspot, we decided to transform the photospheric azimuths given in the LOS by HAZEL to the local reference system. To perform this disambiguation we used a simple potential field extrapolation using the vertical component of the magnetic field and selected the inferred solution at each pixel that is more aligned with the potential field (also called acute-angle comparison; Metcalf et al. 2006). The local Si i azimuth map is displayed in the upper part of Fig. 13. As expected, the magnetic field vector in the sunspot is pointing radially outward from the center of the umbra. In the area where the filament is located the azimuth is apparently aligned with it. However, we note that the potential field extrapolation is probably not the best approximation to the field topology due to the complexity of this region, which might introduce errors in the disambiguation.

The local azimuth map inferred by HAZEL is displayed in the middle panel of Fig. 13. In this case, the azimuth map is not disambiguated. An interesting observation is that there is a clear correlation between the azimuth and the inclination map displayed in Fig. 12. While in the LOS reference frame the longitudinal magnetic field information is purely contained in Stokes $V$ and the transversal information lies in Stokes $Q$ and $U$, in the local reference frame (the observation is not at disk center)
4.3. Ambiguous solutions

The main reason why we did not disambiguate the local azimuth map in the chromosphere is that there are many possible ambiguous solutions. The number of these ambiguous solutions depends on the specific regime of the magnetic field and on the scattering geometry. These ambiguities produce equally good fits to the observed Stokes profiles and they are then impossible to distinguish based on pure spectropolarimetric considerations.

In the plane of the sky the determination of the orientation of the magnetic field vector from the polarization profiles in the Hanle saturated regime suffers from two known ambiguities: the 180° ambiguity (fields with \( \Phi_B \) and \( \Phi_B + 180° \) give the same signal) and the Van Vleck or 90° ambiguity (fields with \( \Phi_B \) and \( \Phi_B \pm 90° \) give the same signals). We can estimate the other ambiguity solutions of the Hanle effect in the saturation regime with the recipe of Martínez González et al. (2015). They used a two-level atom with \( J_u = 0 \) and \( J_l = 1 \) in the optically thin limit. This is a relatively good approximation for the He I 10 830 Å blue component, but not for the red component. For that, with this first guess, we have to refine the solution with Hazelt. We apply this procedure for all pixels and display the number of compatible solutions per pixel in the lower panel of Fig. 13. In our field of view, similar to what was found by Schad et al. (2015), there is a non-negligible fraction of pixels with only one possible solution. The number of solutions increases to two inside both sunspots (one in the center and another in the upper right corner) and are due to the well-known 180° ambiguity. Away from the sunspot, where the magnetic field is weaker, more than three solutions appear. More than five solutions are found in regions where the signal is very low, due to the noise (all of them color-coded as “5”). Finally, in the region of the filament we find between three and four compatible solutions.

The geometry of the observation turns out to be important because it gives us the advantage, in some pixels, of having only one compatible solution. The areas with only one possible solution correspond to regions in which the Hanle and Zeeman effects act together. We defer the detailed study of these signals to Sect. 5.1.

4.4. Line-of-sight velocities

Line-of-sight velocities obtained from the inversions in both atmospheric layers are shown in Fig. 14. The wavelength calibration was done using the photospheric spectral lines and comparing the intensity of an average quiet-Sun region in our data with the FTS atlas (Neckel & Labs 1984). In the photosphere, the umbra is essentially at rest with respect to the velocity of the quiet Sun. At the upper photospheric level (\( \log(r) = -2.2 \)) the velocity in the FOV is between 1.5 km s\(^{-1}\) and -1.5 km s\(^{-1}\).

In the chromosphere, weak upflows are found along the PIL with velocities around 3 km s\(^{-1}\). We identify this flow structure as that typical of slowly rising emerging loop-like structures (e.g., Solanki et al. 2003; Xu et al. 2010), which suggests that this is an emerging \( \Omega \) loop, where cool material rises to chromospheric heights and then drains toward the footpoints of the loops. This could be identified with the ends of the filament where downflows are detected. The only difference between these arch filaments and our active region filament is that the filament material is aligned with the PIL, while their archs are mainly perpendicular. This scenario could be compatible with an emergent flux rope from the active region, presenting similar rising speeds to those of Kuckein et al. (2012b).

The downflows are found at both sides of the filament with velocities higher than 20 km s\(^{-1}\). These pixels also show several (at least two) well-separated components in Stokes \( I \) and Stokes \( V \). Pixels close to them do not show a clear two-component profile, but an extended wing toward red wavelengths. No clear indication of more than two components clearly separated in velocity is found, in contrast to Sasso et al. (2011).

Although a clear relation between the photosphere and chromosphere is hard to establish with our observations, it is tantalizing to associate the two small redshifted patches around (25°, 20°) in the photosphere with the chromospheric downflows, produced by material falling to the photosphere. These two patches in the photospheric map are localized to the left of the downflows because of the geometrical projection.
4.5. Doppler width and optical depth

Figure 15 shows the optical depth $\tau_R$ and the Doppler width $\Delta v_D$ resulting from the inversion of the helium profiles. The mean optical depth in the filament is clearly above 0.7. The maximum value of the optical depth of the filament calculated in this scan is 1.9, but it easily goes up to 2.3 for other scans in which it is more opaque. Values above $\tau_R = 1$ can be potentially affected by radiative transfer effects (Trujillo Bueno & Asensio Ramos 2007), not taken into account in the version of Hazen at the time of writing. These effects could potentially impact the inference of the magnetic field and its topology.

The Doppler width in the filament varies between 10 km s$^{-1}$ and 14 km s$^{-1}$. Higher values are concentrated in the downflows and they are artificially produced by Hazen misfits when trying to fit a pixel with two line profiles clearly separated with a single atmospheric component model. Although the Doppler width of the line can also be used as a tool to extract an upper limit to the temperature, we do not consider it to be a good idea. Many effects that produce unresolved velocities (like the fine structure of the filament with small-scale fibrils with potentially different plasma flows) also broaden the profiles, and we lack the means to calibrate their importance.

5. Bayesian inference

It is clear from Sects. 4.1–4.3 that the inference of the magnetic field vector in the chromosphere requires a careful identification of all ambiguous solutions. Additionally, it is of paramount importance to capture all the potential degeneracies among the physical parameters and return reliable error bars. For this reason, we carried out a Bayesian analysis to fully exploit the observations.

The Bayesian formalism has been applied previously in solar spectropolarimetry, for instance to analyze the magnetic field in the quiet regions of the solar photosphere (Asensio Ramos et al. 2007; Asensio Ramos 2009), to compare models of spectropolarimetric inversions (Asensio Ramos et al. 2012), or to estimate the magnetic field strength from magnetograms (Asensio Ramos et al. 2015). We present here the fundamental ideas of the formalism, although much more detailed information and instructive examples can be found in the mentioned studies (and references therein) and our Appendix A.

5.1. Multimodal inference

In the Bayesian framework, the most plausible model is the one that maximizes the posterior distribution. Given that several ambiguous solutions exist, the posterior probability distribution turns out to be multimodal. Each mode has its specific model parameter uncertainties, and sampling the posterior distribution is thus difficult. The importance of every mode located in the posterior is quantified by its evidence $p(D)$\footnote{To compare the “local” evidence of different modes, this value is not integrated over the totality of the parameter space but on a region surrounding the mode. Since the likelihood decreases away from the mode, the local evidence is mainly controlled by a region very close to the location of each mode.}. For two modes having the same maximum value of the posterior distribution (or, equivalently, the same likelihood when using flat priors), the larger the volume of the space of parameters compatible with the observations, the greater the evidence. In other words, given equally good fits, the evidence is greater for those solutions where the parameters can vary more without compromising the fit. Thus, the evidence may be seen as a quantitative implementation of Occam’s razor. However, as we show later, all the solutions occupy a similar volume in the parameter space with similar likelihoods, the main difference being the location in the parameter space. Therefore, from all available modes explored during the posterior sampling, we chose the set of modes for which the difference between its log-evidence and that of the maximum is smaller than 6, following the Jeffreys scale (Jeffreys 1961). We empirically checked that this threshold is ideal to distinguish all compatible solutions, and we discard any spurious modes obtained during the sampling.

When the posterior is as corrugated and multimodal as the ones we are dealing with, standard Markov chain Monte Carlo (MCMC) techniques can present problems; for example, the
widely used Metropolis–Hastings algorithm (Metropolis et al. 1953) could get trapped in local minima. To explore the parameter space MCMC standard methods generate new points close to the previous one, whose probability of acceptance depends on the likelihood ratio between the new and previous point. In this way, if the new point produces a higher likelihood it is accepted, while if it is worse it is accepted with a low probability depending on the ratio of likelihoods. On the other hand, the nested sampling method is a Monte Carlo technique where, after drawing the points (known usually as live or active points in this method) from the prior, they are sorted by their likelihoods. The lowest one is removed and replaced by a new point with a higher likelihood. In this way, we are continuously sampling layers with higher likelihoods independently of the location of the previous points.

For this reason, we used the MultiNest algorithm (Feroz et al. 2009), a Bayesian inference tool tailored to explore multimodal posteriors and estimate the evidence of each mode. MultiNest implements a nested sampling Monte Carlo algorithm (Skilling 2004) that is designed to calculate efficiently the evidence (Eq. (A.4)) and simultaneously sample the posterior distribution when the latter is multimodal and/or has strong degeneracies. During the sampling MultiNest infers the appropriate number of clusters from the set of points to separate each mode. Other details about this procedure are described in the original article (Feroz et al. 2009). By merging MultiNest and Hazelnut, we performed, for the first time, a Bayesian inference for observations in the He I multiplet.

One of the few free parameters of MultiNest is the number of live points \(N_{\text{live}}\), which is directly proportional to the final precision on the estimation of the evidence. A larger number provides a more accurate sampling, but increases the computing time. After exhaustive tests, we verified that \(N_{\text{live}} = 1000\) gives enough precision for our purposes. The computing time needed to infer each pixel is about 20 min, although it strongly depends on the number of free physical parameters.

5.2. Bayesian analysis of magnetic ambiguities

We analyze in detail one set of profiles that are representative of the observations in terms of the number of equivalent solutions. We study the ambiguities in the \((B, \Theta, \Phi)\) subspace. The rest of the thermodynamic parameters are estimated by a classical least-squares fit of Stokes I. We also infer the uncertainties \(\sigma_{\text{eq}}\) and \(\sigma_{\text{V}}\) from the observations by including them in the Bayesian analysis. This helps us to absorb any Gaussian-distributed systematic effect in the observations in these uncertainties.

We used uninformative flat priors for all the parameters. The priors span the ranges \((0, 2000)\) G, \((0, \pi)\), and \((−\pi, \pi)\) for the modulus, inclination, and azimuth of the magnetic field, respectively. We impose uniform priors in the range \((−7, −8.5)\) for the natural logarithm of the uncertainties, which corresponds to a standard deviation in the range \((2, 9) \times 10^{-4}\) in units of the continuum intensity\(^7\). This range is sufficient to correctly capture\(^8\) the posterior of the uncertainties and narrow enough to reduce the computing time with respect to having a wider range.

In order to gain insight into the number of ambiguous solutions and their physical origin, we have found it useful to make two inferences: one using only Stokes \(Q\) and \(U\), and another using only Stokes \(V\). The solution compatible with the full Stokes vector lies in the intersection of the posterior distributions of both inferences. In the following subsections we present individual cases where four, three, or one solution is compatible with the observed Stokes profiles.

After the inference and before the analysis, it is always a good practice to carry out posterior predictive checks using Hazelnut to synthesize the Stokes profiles with the parameters inferred from the posterior. An example of this is shown in Fig. 9, where we have drawn the Stokes profiles of two pixels with their maximum a posteriori best fit and a green shadowed region indicating the range of possible solutions obtained from the posterior distribution.

5.2.1. Four solutions

The pixel at \((24'', 25'')\) is a good example of a posterior with four modes. Figure 16 shows the joint (below the diagonal) and marginal (on the diagonal) posterior distributions for the magnetic field strength, and inclination and azimuth in the LOS frame. The samples and histograms in green correspond to the inference using only Stokes \(Q\) and \(U\), while those in gray were obtained using only Stokes \(V\). The presence of several modes is clearly seen in the joint posteriors. We show the solutions compatible with the full Stokes vector with red circles. The panels above the diagonal show the synthetic Stokes profiles for all the modes, demonstrating that they produce indistinguishable fits to the data.

The joint posterior distribution of the magnetic field strength and inclination in the LOS frame, \(p(B, \Theta_B|D)\), when only Stokes \(V\) is used presents a clear degeneracy, showing a hyperbolic-shaped posterior distribution typical of the Zeeman weak field regime, where only the product \(B \cos \Theta_B\) can be reliably estimated. In order to facilitate the recognition of the degeneracy, we overplot the dashed line \(B \cos \Theta_B = c\), where \(c\) is a constant.

This pixel is in the saturation regime of the Hanle effect. In this regime, the Hanle effect is not sensitive to the magnetic field strength, being only sensitive to the orientation of the field. In this case, we have the following potential ambiguities: \(\Phi_B, \Phi_B − \pi/2, \Phi_B + \pi/2, \Phi_B + \pi\). The green posterior (especially clear in the panel showing the joint posterior \(p(B, \Phi_B|D)\)) shows the four potential ambiguities in \(\Phi_B\) as four horizontal lines.

In the joint posterior \(p(\Theta_B, \Phi_B|D)\), we see how each degenerate value of the azimuth is compatible with two potential values for the inclination, generating a maximum of eight possible ambiguous solutions. All the solutions occupy a similar volume in the parameter space, as is seen from the green sampling, so the evidence is mainly controlled by the likelihood under our assumption of equal priors. Half of the points are discarded when the polarity of the field is taken into account in the inference through Stokes \(V\). The sign of Stokes \(V\) is such that only inclinations in the range \((0^\circ, 90^\circ)\) are favored by the observations. Therefore, we end up with the final four ambiguous solutions, shown with red circles. It is important to remember that some of the ambiguous solutions can have the same azimuth in the LOS and are only distinguished by their inclination.

For clarity, we only show the posterior distribution for the magnetic field strength up to 80 G. However, the green posterior goes down to zero as we increase the magnetic field because

\(^7\) We used MultiNest through the Python wrapper PyMultiNest (Buchner et al. 2014) available at http://github.com/JohannesBuchner

\(^8\) The Bayesian framework allows us not only to calculate the uncertainties of the parameters of the model, but also to infer the uncertainties of the observations given the model. This parameter absorbs the noise of the observations (sometimes difficult to calculate if we do not have enough continuum wavelength points), and also the inherent suboptimality of the model itself because it cannot reproduce some spectral features.
Fig. 16. Joint (below the diagonal) and marginal (in the diagonal) posterior distributions for the magnetic field strength, inclination, and azimuth in the LOS frame. The samples and histograms in green correspond to the inference using only Stokes $Q$ and $U$, while those using only Stokes $V$ are in gray. The analysis was carried out for a pixel with four compatible solutions, drawn in different colors in the upper diagonal panels. The solutions compatible with the full Stokes profiles are indicated with red circles.

Fig. 17. Same as Fig. 16, but for a pixel with three compatible solutions. The dashed Stokes profiles come from the rejected solution with the same polarity.

Fig. 18. Same as Fig. 16, but for a pixel with only one possible solution and using Stokes $Q$, $U$, and $V$ for the inference. Observed Stokes profiles (gray), synthetic profiles from the solution (green), and the rejected solution $\Theta_B + \pi$ (dashed) are shown in the upper diagonal panels.

the shape of Stokes $Q$ and $U$ does not fit the observations any longer. We note that the Hanle saturation regime starts at $\sim 10$ G and above this the linear polarization is no longer sensitive to the strength of the magnetic field, and the posteriors are flat.

5.2.2. Three solutions

A pixel representative of a posterior with three modes is the one at (4'', 5''). This pixel has three compatible solutions: two with the same LOS azimuth and one separated by $\pi/2$ to the other pair.

Figure 17 displays the same set of quantities as in the previous example, but for this new pixel. In principle this pixel is in the saturation regime of the Hanle effect, but in this case only three of the four solutions pass the Bayesian evidence test (see the joint posterior $p(\Theta, \Phi | D)$). The rejected point is very close to $\Theta_B = 90^\circ$, so it is associated with a field almost perpendicular to the LOS. The ensuing magnetic field strength needed to produce the observed Stokes $V$ signal with this orientation of the field is close to 350 G. This field is so strong that this solution is discarded because Stokes $Q$ and $U$ starts to show some Zeeman features that are not compatible with the observed profiles. This is clearly seen in the panel for Stokes $Q$, $U$, and $V$. The Stokes profiles of all three compatible solutions are displayed in the upper diagonal panels in solid lines, while the rejected solution is shown with the dashed line.

5.2.3. One solution

One of the most surprising conclusions of this work is that it is possible to find pixels in which only one solution is compatible with the observations. A good example of this is the pixel at (38'', 8''). The joint and marginal posterior distributions of this pixel are displayed in Fig. 18. The profiles are clearly close to the pure Zeeman regime for Stokes $Q$ and $U$, with the typical three-lobed profiles, but some contribution from scattering polarization still exists. The two effects act together and the 180$^\circ$ ambiguity in the azimuth disappears (Schad et al. 2013). The reason is that the Hanle contribution in the core of the Stokes $Q$ and $U$ has opposite signs for the two solutions, which produces a misfit in one of them. The Zeeman contribution to Stokes profiles depends on the inclination and azimuth of the magnetic field with respect to the LOS, while for the Hanle contribution, it also depends on the geometry in the local reference frame. For
our geometry ($\mu = 0.92$) the two solutions with a difference in the azimuth of 180° lead to a different geometry in the local frame and only one of them is compatible with the Hanle signals. Therefore, the observing geometry plays a key role, allowing us in some cases to reduce the number of compatible solutions to a single one.

This “self-disambiguation” is only possible in the intermediate regime between the Hanle and the Zeeman effect (~400–800 G), when the Hanle effect can generate slightly different profiles for the two solutions. The dashed lines in the Stokes profiles panels refer to the rejected solution ($\Phi_B + \pi$), being clearly unable to reproduce the profiles.

5.3. Height of the filament

When the observed structure is off the limb, imaging techniques can be used to estimate its height (Martínez González et al. 2015; Schad et al. 2016). On the contrary, for on-disk observations it is much more complicated since no straightforward technique for estimating the height is available. Using Bayesian inference we explore the feasibility of the inference of the height of the filament directly from the observations: the greater the height, the larger the anisotropy, which induces a stronger zero-field scattering polarization signal.

Some authors have tried to retrieve the height including it as an inversion parameter (Xu et al. 2010; Merenda et al. 2011), concluding that it can be inferred with high accuracy, solving possible debates in the interpretation of the topology (Judge 2009). Additional arguments based on 3D geometrical reconstructions (Xu et al. 2010; Solanki et al. 2003) have been used to calculate this height. However, it was noted by Asensio Ramos et al. (2008) that the height cannot be easily inferred from the observations unless some information about the topology of the field is fixed a priori (for instance, the inclination). Here, we demonstrate that not only is this the case, but the inference is even more difficult because both the magnetic field and the optical depth are degenerate with the height.

To analyze the reliability of inferring the height from the Stokes parameters, we chose the pixel at (22", 22") that lies inside the filament. We include all ten free variables in our Bayesian analysis: $B$, $\theta_B$, $\phi_B$, $r_B$, $A_{LOS}$, $v_{LOS}$, $h$, $\sigma_I$, $\sigma_{qu}$, and $\sigma_V$. Given that the number of free parameters is large, to decrease the computing time we use more restrictive priors for the inclination than before, trying to capture only one possible ambiguous solution. The prior for the height is flat and limited to the range (0", 15"). We carried out some tests to check that isolating one mode of the magnetic field does not affect our conclusion. As before, we add the uncertainty of the Stokes parameters as variables and impose a suitable Jeffreys prior. Sampling the unimodal posterior requires more than 100 min on a single CPU (3.4 GHz Intel Core i7).

The ensuing posterior distributions (joint and marginal) are displayed in Fig. 19. The posterior distribution seems to be quite localized for all variables, except for the height. Its marginal posterior is practically flat, almost indistinguishable from the assumed prior. For the joint posteriors, it displays a very strong correlation with many of the remaining parameters. For instance, changing the height by 15° can be compensated easily by barely modifying the optical depth from 1.2 to 1.04. The same happens with the inclination of the field, where a small change of 4° compensates the change in height. Finally, changes of only 10 G in the magnetic field strength can also compensate for the same change in height, in agreement with Schad et al. (2013). Therefore, this analysis shows that while height cannot be inferred accurately because its effect can be easily compensated for with other parameters, the rest of the parameters are obtained with very small uncertainty.

6. Summary and conclusions

In this article we showed a first analysis of ground-based spectropolarimetric observations acquired with GRIS (GREGOR, at Observatorio del Teide) of the He i 10 830 triplet in an active region filament. The active region was located in a flaring area. Although the profiles do not show any peculiar signature, the fast evolution of the filament (e.g., with the absorption strongly changing in consecutive scans of ~15 min) is a sign of the activity of the area.

The observed polarization signals in the filament show single-lobed linear polarization profiles, which is indicative of optical pumping by an anisotropic illumination and, potentially, the action of the Hanle effect. These linear polarization signatures were close to the noise level ($5 \times 10^{-4}I_c$). We were able to measure them as a result of our high spectropolarimetric sensitivity and a noise reduction process. Longer integration times than the ones used here are necessary to increase the signal-to-noise ratio and study the weak polarization signals present in these chromospheric structures. The low signal-to-noise ratio of the observations from other studies, such as Xu et al. (2012), might be the reason why they could not detect the linear polarization signals due to scattering, hence neglecting atomic polarization in their analysis.

We have studied the observations with Hazel, a state-of-the-art inversion code that includes the Hanle and Zeeman effects, to retrieve the physical properties from the polarimetric signals. Using a one-component model, as is customary in other studies, magnetic field strength values around 50–150 G were found.

We also applied the Bayesian framework using Hazel and MultiNest to explore the solutions in the parameter space and compute posterior distributions. This Bayesian inversion cannot compete in speed with the standard inversion algorithms, but it can be used to investigate in detail the accuracy of the inversions and the sensitivity of the parameters to the noise, and to give confidence intervals to all the parameters. Using this technique, we studied how many solutions are compatible with the analyzed profiles depending on the geometry of scattering and the magnetic field regime. In addition, we applied it to the inference of the height, concluding that this parameter cannot be constrained, at least at our noise level.

Some results clearly point out that a more complex inversion than a single-component model had to be performed. First, the Stokes V map of He i does not show a clear signature of the presence of the filament. Second, the inferred azimuth map follows the same pattern as Stokes V, as if the polarity of Stokes V were conditioning the inference. This indication suggests that the Stokes V could be dominated by the magnetic field from the underlying active region, and not from the filament itself (Díaz Baso et al. 2016). Then, a more complex model is needed to explain the observations and avoid misinterpretations due to oversimplified models (Milić et al. 2017). A deeper study of these features is performed in the second part of this series, studying in detail all the evidence of the limitations of a single-component model.
Fig. 19. Histograms and correlations of the posterior distributions of each physical parameter. The label at the top of each column provides the median and the uncertainty defined by the 16th and 84th percentiles (equivalent to the standard 1σ uncertainty in the Gaussian case). Also, the contours are shown at 0.5, 1, and 2σ.

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Appendix A: Bayesian framework

Bayesian inference provides the most complete approach to parameter inference. The inference problem relies on the calculation of the posterior probability distribution function (PDF) \( p(\theta|D) \) of a set of \( M \) parameters \( \theta \) (in this case the vector of physical quantities of the model) that is used to describe a given observation \( D \). This posterior distribution describes our updated state of knowledge of the parameters after taking the data \( D \) into account. Bayes’ theorem allows us to calculate the posterior distribution for \( \theta \),

\[
p(\theta|D) = \frac{p(\theta)p(D|\theta)}{p(D)}, \quad (A.1)
\]

where \( p(\theta) \) is the prior and represents our a priori knowledge in the model parameters. It is usual to have some initial information about the physical parameters. For instance, an estimation of the range of variation of the physical parameters, although sometimes it can be a very rough range (e.g., only positive values). This information is incorporated into a prior distribution. In the simplest case we can assume that all the parameters are statistically independent, so that the prior distribution can be written as

\[
p(\theta) = \prod_{i=1}^{M} p(\theta_i), \quad (A.2)
\]

where \( \theta \) are the parameters included in the model and \( M \) is the number of these parameters. When the only physical information available is the range of variation of the parameters, we use uninformative priors with a uniform probability distribution inside the range and zero otherwise.

The second term of the Bayes’ equation \( p(D|\theta) \) is the likelihood, which measures the probability that the data \( D \) were obtained (measured) assuming given values for the model parameters \( \theta \), i.e., it gives information about how well the parameters predict the observed data. In the case of the inversion of Stokes profiles, the data \( D \) that we are facing consists of a set of four vectorial quantities, i.e., the wavelength dependence of the four Stokes parameters.

Under the assumption of uncorrelated Gaussian noise in the data\(^{10} \), the likelihood is given by

\[
p(D|\theta) = \prod_{i=0}^{3} \prod_{j=1}^{N} \frac{1}{\sigma_i \sqrt{2\pi}} \exp \left( -\frac{[S_{i}\text{obs}(\lambda_j) - S_{i}\text{syn}(\theta, \lambda_j)]^2}{2\sigma_i^2(\lambda_j)} \right), \quad (A.3)
\]

where \( S_{i}\text{obs}(\lambda_j) \) is the observed Stokes parameter \( S = (S_0 = I, S_1 = Q, S_2 = U, S_3 = V) \) at wavelength \( \lambda_j \); \( S_{i}\text{syn}(\theta, \lambda_j) \) is the emergent synthetic Stokes parameter when the forward problem is solved in a given atmospheric model parameterized by the vector of parameters \( \theta \); and \( \sigma_i(\lambda_j) \) is the standard deviation of the noise for each Stokes parameter and wavelength point. Strictly speaking, the noise in the observed Stokes profiles follows a Poisson distribution because it comes mainly from photon noise. However, for consistency with other works, we chose the noise to be normally distributed, which will be a good approximation if the number of photons is high enough. Although we focused on wavelength-independent noise, the formalism allows us to straightforwardly accommodate wavelength-dependent noise in the likelihood. Therefore, if the information is available, it is possible to include other sources of uncertainty such as data reduction residuals, cross-talk, and fringes.

Finally, the denominator \( p(D) \) in Eq. (A.1) is the Bayesian evidence or marginal posterior, which is a normalization factor that has turned out to be important in our analysis, as shown in the main text. Since the posterior is a probability distribution, its total integral (or sum, if the space is discrete) must equal one. Therefore, the evidence can be written as

\[
p(D) = \int p(D|\theta) p(\theta) \, d\theta. \quad (A.4)
\]

For parameter inference, the information for a single parameter can be obtained from the marginal posterior, obtained from the posterior by integrating over the rest of parameters (marginalization):

\[
p(\theta_i|D) = \int p(D|\theta) \, d\theta_{i-1} \, d\theta_{i+1} \ldots \, d\theta_M. \quad (A.5)
\]

The two-dimensional posterior distribution where we have marginalized the whole posterior distribution to all the parameters less two of them, i.e.,

\[
p(\theta_i, \theta_j|D) = \int p(D|\theta) \, d\theta_{i-1} \, d\theta_{i+1} \ldots \, d\theta_{j-1} \, d\theta_{j+1} \ldots \, d\theta_M, \quad (A.6)
\]

is commonly known as the joint posterior.

Once the posterior distribution \( p(\theta|D) \) is known, the position of the maxima (in our case the posterior is multimodal) gives the most probable combination of parameters that reproduces the observational data. Moreover, we can analyze in detail the confidence levels of the parameters, degeneracies, ambiguities, and the rest of the problems that arise in typical inversion codes. Therefore, our objective is then to sample the posterior distribution and to find the combination of parameters that produce these maxima.

\(^{10}\) It is true that a remaining correlation might exist among the measured Stokes parameters because they are in fact obtained with a modulation process. Therefore, cross-talk and other instrumental effects might “correlate” the noise in the four Stokes parameters.