POSSIBLE DETECTION OF AN EMISSION CYCLOTRON RESONANCE SCATTERING FEATURE FROM THE ACCRETION-POWERED PULSAR 4U 1626–67

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ABSTRACT

We present analysis of 4U 1626–67, a 7.7 s pulsar in a low-mass X-ray binary system, observed with the hard X-ray detector of the Japanese X-ray satellite Suzaku in 2006 March for a net exposure of ~88 ks. The source was detected at an average 10–60 keV flux of ~4 × 10−10 erg cm−2 s−1. The phase-averaged spectrum is reproduced well by combining a negative and positive power-law times exponential cutoff (NPEX) model modified at ~37 keV by a cyclotron resonance scattering feature (CRSF). The phase-resolved analysis shows that the spectra at the bright phases are well fit by the NPEX with CRSF model. On the other hand, the spectrum in the dim phase lacks the NPEX high-energy cutoff component, and the CRSF can be reproduced by either an emission or an absorption profile. When fitting the dim phase spectrum with the NPEX plus Gaussian model, we find that the feature is better described in terms of an emission rather than an absorption profile. The statistical significance of this result, evaluated by means of an F test, is between 2.91 × 10−3 and 1.53 × 10−5, taking into account the systematic errors in the background evaluation of HXD-PIN. We find that the emission profile is more feasible than the absorption one for comparing the physical parameters in other phases. Therefore, we have possibly detected an emission line at the cyclotron resonance energy in the dim phase.

Key words: pulsars: individual (4U 1626–67) – stars: magnetic field – X-rays: binaries – X-rays: stars

Online-only material: color figures

1. INTRODUCTION

Accreting binary pulsars are an ideal laboratory for studying the fundamental physics of radiative transfer of X-ray photons under strong (of the order of 1012 G) magnetic fields. A quite evident manifestation of such transfers is cyclotron resonance scattering features (CRSFs) observed in the spectra of many X-ray sources—the first being observed in Her X-1 (Trümper et al. 1978). CRSFs are caused by resonant scatterings between the Landau levels of electrons under the strong magnetic field near the surface of a neutron star. The cyclotron resonance energy, $E_a$, is strongly related to the magnetic field strength:

$$E_a = 11.6 B_{12} (1 + z_g)^{-1} \text{keV},$$

where $B_{12}$ is the magnetic field strength in units of 1012 G, and $z_g$ represents the gravitational redshift at the resonance point. To date, CRSFs have been detected from 16 accreting binary pulsars and their magnetic field strength has been measured (Mihara 1995; Coburn et al. 2002). However, the formation mechanism of CRSFs is not still fully understood due to the complex physics of resonant scattering and their continuum. Thus, the comparison of the CRSFs' parameters observed in different sources, at different luminosity and spectral states, is important to gain information on the physical processes taking place.

The Japanese X-ray satellite Suzaku, with its high-sensitivity hard X-ray detector (HXD; Takahashi et al. 2007), has discovered CRSFs from GX 304-1 (Yamamoto et al. 2011), successfully detected CRSFs from A0535+262 (Terada et al. 2006) in its lowest luminosity epochs, and performed detailed studies of the CRSFs of Her X-1 (Enoto et al. 2008), 4U 1907+09 (Rivers et al. 2010) and 1A 1118–61 (Suchy et al. 2011).

4U 1626–67 was observed by Suzaku in 2006 March. The source is a 7.7 s pulsar in a low-mass X-ray binary system with an orbital period of 42 minutes (Middleditich et al. 1981; Chakrabarty 1998). The X-ray spectrum shows low-energy emission lines from Ne and O (Angelini et al. 1995) and a feature at ~37 keV (Orlandini et al. 1998). The 37 keV absorption feature was discovered by BeppoSAX and interpreted as the fundamental CRSF. The 10–60 keV source flux is 4.4 × 10−10 erg cm−2 s−1 and the resonance energy corresponds to a magnetic field strength of ~3 × 1012 G (Orlandini et al. 1998). The broadband X-ray continuum exhibits a strong phase dependence as reported by HEAO-1 (Pravdo et al. 1979), Tenma (Kii et al. 1986) and RXTE (Coburn 2001). The cyclotron feature and the phase dependence variability provide information on radiative transfer in the plasma of the accretion column. In this paper, we used the 2006 March Suzaku observation of 4U 1626–67 to investigate the characteristics of the ~37 keV feature and the continuum in the phase-resolved spectra. The paper is organized as follows: we describe the observations from Suzaku and the data reduction procedure in Section 2, show the results of the timing and spectral analyses in Section 3, and finally provide a discussion and summary in Section 4.
2. OBSERVATIONS AND DATA REDUCTION

2.1. Suzaku Observation of 4U 1626−67

*Suzaku* is the fifth Japanese X-ray satellite (Mitsuda et al. 2007) to be launched and is equipped with two different instruments. One instrument is an X-ray imaging spectrometer (XIS; Koyama et al. 2007), a charge-coupled device camera at the focus of the X-ray telescope (XRT; Serlemitsos et al. 2007), covering the 0.2−12 keV energy range. There are four XIS units; three of them (XIS-0, XIS-2, and XIS-3) are front-illuminated (FI) while the other one (XIS-1) is back-illuminated (BI). The other instrument is an HXD (Takahashi et al. 2007), which consists of PIN silicon diodes (HXD-PIN; 10−70 keV) and Gd2SiO5Ce (GSO; 50−600 keV) scintillators. 4U 1626−67 was observed by *Suzaku* on 2006 March 9 UT 01:18 through March 11 19:38 at “XIS nominal” pointing position. The XIS operated in standard clocking mode and included the “1/8 window” option in order to have a time resolution of 1 s, without a charge injection function.

2.2. Data Reduction Procedure

We used data produced by *Suzaku* pipeline processing version 2.0.6.13 with the calibration versions hxd-20090515, xis-20090403, and xrt-20080709, and the software version HEADAS 6.5.1.

XIS and HXD events were screened by using standard criteria. We discarded events collected when Earth’s limb was less than 5°, when Earth’s day–night boundary angle from the line of sight was less than 25°, or when the spacecraft was in an orbit phase within 436 s (for the XIS) or 500 s (for the HXD) of the South Atlantic Anomaly ingress/egress. For XIS-1, we also excluded events in the time interval between 2006 March 10 UT 06:58:30 and 07:20:54, because the cooling system was not properly working during this period. We accepted only XIS events with standard grades (0, 2, 3, 4, and 6) in the analysis.

XIS spectra and light curves were extracted from a circle with a radius of 4.3 arcmin centered at the source. Spectra from the three FI XIS sensors were summed together and the XIS intensity in the 0.4−10.0 keV energy band was ∼5 counts s−1 for each sensor. We accumulated the XIS background spectra from a source-free region having the same exposure area as that of the corresponding sensors. The derived background spectra were used to subtract the expected non X-ray background (NXB) model. Net exposures were accumulated for XIS-0 in the 0.4−10.0 keV range and with the HXD in the 10−50 keV range, respectively. The top panel of Figure 1 shows the hardness ratio of the above two panels. The gray solid line shows the average and the gray dotted lines show the ±3σ interval.

3. ANALYSIS AND RESULTS

3.1. Timing Analysis

For the arrival time of each XIS and HXD-PIN event, barycenter correction was performed with the tool aebarycen (Terada et al. 2008). We surveyed the HXD-PIN data by using a folding technique to obtain a best spin period of \( P_{\text{Suzaku}} = 7.67795(9) \) s. This period is consistent with the spin-down trend that started to be observed from 1990 onwards, and that is calculated by using the spin-down rate of \( \dot{P} \sim -4.8 \times 10^{-13} \text{ Hz s}^{-1} \) measured with the *Swift* satellite over the period 2004−2007 (Chakrabarty et al. 1997; Camero-Arranz et al. 2010).

XIS and HXD background-subtracted light curves of 4U 1626−67 are shown in Figure 1. The light curves are plotted using a time bin of 7678 s, a multiple of \( P_{\text{Suzaku}} \). The XIS and HXD light curves have an intensity variation of less than 7%, and the hardness ratio between them is approximately constant; the reduced chi-squared (\( \chi^2 \)) value is about 1 when fitting a constant model to the hardness ratio. The average and the 3σ level are shown in Figure 1. As a result, we confirmed that there is no significant spectral variation. Thus, X-ray spectra were extracted by using data over the entire observation.

3.2. Phase-averaged Spectrum

The top panel of Figure 2 shows the broadband 4U 1626−67 phase-averaged raw count rate spectrum normalized by a Crab Nebula spectrum that was observed for calibration purposes. XIS source data were normalized by using a canonical model of the Crab Nebula spectrum, since spectra from the Crab Nebula suffer from pile-up. HXD data were normalized by an HXD Crab Nebula spectrum observed on 2006 March 30 taken for the same observation parameters—position of the source with respect to the instrument FoV, grade criteria, and PIN threshold file (ae_hxd_pinthr_20060727.fits)—as for 4U 1626−67. The 4U 1626−67 source intensity is about 20 mcrab at 20 keV, and the normalized spectrum is characterized by three main features: a soft X-ray excess below ∼3 keV, as reported by several authors.
Figure 2. Phase-averaged background-subtracted spectra of 4U 1626−67 obtained with *Suzaku* XIS (black crosses denote XIS-FI data and light gray crosses denote XIS-BI data) and HXD (denoted by circles). Error bars are only for statistical predictions. The top panel shows the raw count rate energy spectra divided by those of the Crab Nebula. The middle panel shows the spectra in counts s$^{-1}$ keV$^{-1}$ along with the best-fit models (dotted lines): a blackbody, NPEX with Gaussian-absorption model, and photoelectric absorption (see the text for details). Plots are presented without removal of instrumental responses. The bottom panel shows the residuals between the actual data and the best-fit model. (A color version of this figure is available in the online journal.)

To model the phase-averaged spectrum, we fit the data with a $\sim$0.24 keV blackbody for the soft excess, and a dip feature at $\sim$35 keV.

To model the phase-averaged spectrum, we fit the data with a power-law continuum, and a dip feature at $\sim$35 keV.

The best-fit model and its residuals are plotted in the lower panel of Figure 2. Above 3.5 keV only 1% of the NPEX negative term is contributed by the blackbody component. Therefore, hereinafter, we ignore XIS data below 3.5 keV and exclude the blackbody component from the fit.

To evaluate the statistical significance of the CRSF in the phase-averaged spectrum, first, we fit the spectrum with only NPEX continuum or NPEX × GABS model. The residuals of the NPEX with GABS model for energy bands above 3.5 keV are shown in Figure 3(a), and the best-fit parameters are listed in Table 1. Second, we tested the significance using the F test routine of Press et al. (2007). In this case, the F statistical value is defined as

$$F = \frac{\chi^2_1 / \nu_1}{\chi^2_2 / \nu_2},$$

where $\chi^2_1$ and $\chi^2_2$ are statistical chi-squared, $\nu_1$ and $\nu_2$ are degrees of freedom corresponding to the results of fittings using models 1 and 2 (in this case model 1 is only NPEX continuum and model 2 is NPEX with multiplicative component), respectively. The derived $F$ statistical value is 3.1, which indicates that the probability of chance improvement of the $\chi^2$ is $3.7 \times 10^{-12}$. Thus, the CRSF is a statistically significant feature in the phase-averaged spectrum. We also found that the residuals in Figure 3(a) have a complex structure near the Fe-emission line energy around 6.6 keV. The fit improves by the addition of a Gaussian Fe-line model with an energy of 6.62 keV, a width ($\sigma_{Fe}$) of 0.37 keV, and an equivalent width (EW) of 33.3 eV (Figure 3(b) and Table 1). These values are statistically significant.
consistent with the ASCA EW upper limit of <33 eV for an Fe-emission line in the 6.4–6.9 keV range (Angelini et al. 1995). The broad width may indicate the presence of an Fe-line absorption. If we replace the NPEX model by an exponential cutoff (ECUT, which is the parameter is unconstrained, strongly suggesting that the Fe-emission line structure is made by three lines or not, due to the energy resolution of XIS (∼150 eV). The X-ray unabsorbed fluxes in the 3.5–10 keV and 10–60 keV energy bands are 1.27^{+0.01}_{-0.04} \times 10^{-10} \text{ erg cm}^{-2} \text{s}^{-1} and 4.02^{+0.46}_{-0.85} \times 10^{-10} \text{ erg cm}^{-2} \text{s}^{-1}, respectively, and the hard X-ray flux is consistent with the BeppoSAX observation (Orlandini et al. 1998). Exchanging the GABS model with a cyclotron absorption model (CYAB; Mihara et al. 1990) also fits the data well (Figure 3(c) and Table 1).

If we replace the NPEX model by an exponential cutoff power-law model (ECUT, which is the powerlaw#higher # model in Xspec; White et al. 1983) and fit the data with a GABS model, we obtain an acceptable χ^2 value (see Table 1), but substantial residual structures are seen above 20 keV (Figure 3(d)). Although the CRSF energy agrees with BeppoSAX observations (Orlandini et al. 1998), the best-fit continuum model is inconsistent with BeppoSAX results.

### 3.3. Phase-resolved Spectra

Phase-resolved spectra acquired by HEAO-1, Tenma, and RXTE (Pravdo et al. 1979; Kii et al. 1986; Coburn 2001) show a strong phase dependence in the continuum emission of 4U 1626–67. Suzaku XIS and HXD folded light curves also indicate changes across the pulse (Figure 4). Specifically, while the 10–30 keV/3.5–10 keV ratio maintains the characteristics of the individual light curves, the 30–50 keV/10–30 keV ratio indicates spectral differences between phases 0.0–0.3 and the other phases.

To investigate spectral changes across the pulse, we divided the events into eight phase-resolved spectra (Figure 5) and normalized these spectra by the Crab Nebula spectrum by using the method described in Section 3.2 (Figure 6). The Crab Ratios show that the ~20 keV peak is more prominent at higher pulse flux. Additionally, the ratios flatten at lower pulse flux and the energy of the resonance feature changes. The resonance features are particularly outstanding in the dim phase spectrum (φ = 0.125–0.250), where the hardness ratio (Figure 4) shows a large change in these features.

We then performed spectral fitting to the phase-resolved spectra with the NPEX continuum and the Fe-emission line model in order to establish the pulse-phase dependence of the continuum and the CRSF. The Fe-line energy and the width of the Gaussian function were fixed at values obtained from the averaged spectrum. The parameters from the spectral fitting are listed in Table 2, and the ratios between the original data and the best-fit model are shown in Figure 7. We found that the ratio for the dim phase (φ = 0.125–0.250) spectrum exhibits a monotonic increase above 30 keV, and the residuals show evidence for the existence of an emission feature rather than an absorption (Figure 8(a)). In contrast, the other phases have a V-shaped ratio caused by a CRSF absorption feature. Moreover, the fitting results for the dim phase spectrum show that the Ap parameter is unconstrained, strongly suggesting that the continuum spectrum at the dim phase requires only the upper limit of the high-energy cutoff component. In other words, the result makes the NPEX model effectively a power-law times exponential cutoff model (cutoffpl in Xspec). The result is consistent with the trend that the 20 keV peak in the Crab Ratios is less prominent at lower pulse flux. We also tried other empirical models applied to an accretion-powered pulsar, ECUT, and a power law with Fermi–Dirac cutoff (Tanaka 1986), and find that their best-fit cutoff energies are consistent with 0. In other words, a power-law times an exponential cutoff model is the only one able to fit the dim phase spectrum. For this reason we fit the dim phase spectrum by using the NPEX model with fixed Ap = 0. As we can see in Table 2, the difference between the χ^2 values for freely selected Ap and for fixed Ap = 0 is negligible. Therefore, we henceforth fix Ap = 0 for the NPEX model when fitting the dim phase spectrum.

### Table 1: Best-fit Parameters for Phase-averaged Spectra of 4U 1626–67 (d.o.f. = degrees of freedom)

| Parameter | NPEX | NPEX with GABS | NPEX with GABS | NPEX with CYAB | ECUT with GABS |
|-----------|------|---------------|---------------|---------------|---------------|
| α | 0.31^{+0.04}_{-0.03} | 0.26^{+0.02}_{-0.01} | 0.29^{+0.02}_{-0.01} | 0.32^{+0.03}_{-0.02} | 0.65^{+0.06}_{-0.07} |
| kT (keV) | 5.3^{+0.1}_{-0.1} | 7.0^{+0.5}_{-0.4} | 6.7^{+0.2}_{-0.3} | 7.2^{+1.1}_{-0.4} | ... |
| Ec (keV) | ... | ... | ... | ... | ... |
| Er (keV) | ... | ... | ... | ... | ... |
| A0(×10^{-3}) | 8.1^{+0.4}_{-0.3} | 6.8^{+0.2}_{-0.2} | 7.2^{+0.3}_{-0.3} | 7.3^{+0.1}_{-0.2} | ... |
| A0p(×10^{-3}) | 4.6^{+0.3}_{-0.3} | 1.6^{+0.5}_{-0.4} | 1.8^{+0.5}_{-0.4} | 1.6^{+0.4}_{-0.5} | ... |
| A(×10^{-3}) | ... | ... | ... | ... | ... |
| EFeb (keV) | ... | ... | ... | ... | ... |
| σFe (keV) | ... | ... | ... | ... | ... |
| EWFe (eV) | ... | ... | ... | ... | ... |
| EC(keV) | ... | ... | ... | ... | ... |
| Eb (keV) | ... | ... | ... | ... | ... |
| σCRSF (keV) | ... | ... | ... | ... | ... |
| τ | ... | ... | ... | ... | ... |
| χ^2/d.o.f | 572.6/158 | 182.1/155 | 132.6/152 | 134.6/152 | 170.6/152 |

Notes.
- a Without Fe-emission line model.
- b Referring to Equation (1) and defined at 1 keV in units of photons keV^{-1} cm^{-2} s^{-1}.
- c Normalization of the power law. Defined at 1 keV in units of photons keV^{-1} cm^{-2} s^{-1}.


Next, we included the GABS model and refit the phase-resolved spectra. The resulting parameterized models fit all of the phase-resolved spectra well (see Table 3 and Figure 9), and residuals above 30 keV in the dim phase were eliminated (see Figure 8(b)). We also evaluate the significance of including a GABS component using the same method discussed in Section 3.1. The derived probabilities are summarized in Table 3, which shows that the absorption factor is not statistically significant in the dim phase. This significance did not change even when we adopted the CYAB model (as opposed to the GABS model as the cyclotron feature model) for spectral fitting.

![Figure 4](url) Energy-resolved and background-inclusive pulse profiles of 4U 1626–67. Data were folded at $P_{\text{local}} = 7.67795$ s. Phase 0 corresponds to MJD 53803.000092755. The average background count rates of 3.5–10.0 keV, 10.0–30.0 keV, and 30.0–50.0 keV energy bands are 0.016 counts s$^{-1}$, 0.49 counts s$^{-1}$, and 0.086 counts s$^{-1}$, respectively.

### Table 2

| Pulse Phase | $\alpha$  | $kT$    | $A_n$ | $A_p$ | EW$_{Fe}^b$ | $\chi^2$/d.o.f |
|-------------|-----------|---------|--------|--------|-----------|----------------|
| 0.000–0.125 | $-0.02^{+0.05}_{-0.06}$ | $4.4^{+0.5}_{-0.3}$ | $6.7^{+0.8}_{-0.7}$ | $3.2^{+2.5}_{-1.9}$ | $27^{+38}_{-27}$ | 81.2/81 |
| 0.125–0.250 | $0.15^{+0.17}_{-0.11}$ | $5.1^{+0.7}_{-1.1}$ | $5.8^{+0.7}_{-0.5}$ | $<1.2$ | $81^{+28}_{-12}$ | 69.0/63 |
| 0.125–0.250 | $0.27^{+0.02}_{-0.02}$ | $6.1^{+0.5}_{-0.4}$ | $6.1^{+0.2}_{-0.2}$ | $0$ (fixed) | $84^{+13}_{-53}$ | 71.8/64 |
| 0.250–0.375 | $0.10^{+0.07}_{-0.06}$ | $4.2^{+0.2}_{-0.3}$ | $8.0^{+1.1}_{-0.7}$ | $4.9^{+2.5}_{-1.7}$ | $46^{+31}_{-8}$ | 93.4/97 |
| 0.375–0.500 | $0.51^{+0.11}_{-0.06}$ | $5.0^{+0.1}_{-0.1}$ | $11.8^{+1.9}_{-0.8}$ | $7.6^{+1.1}_{-0.7}$ | $21^{+16}_{-9}$ | 137.3/103 |
| 0.500–0.625 | $0.56^{+0.10}_{-0.10}$ | $5.3^{+0.1}_{-0.1}$ | $10.4^{+1.6}_{-1.3}$ | $7.2^{+0.6}_{-0.6}$ | $<22$ | 297.9/129 |
| 0.625–0.750 | $0.64^{+0.10}_{-0.09}$ | $5.2^{+0.1}_{-0.1}$ | $11.8^{+1.7}_{-1.5}$ | $8.4^{+0.7}_{-0.7}$ | $35^{+5}_{-10}$ | 259.0/108 |
| 0.750–0.875 | $0.53^{+0.09}_{-0.09}$ | $5.3^{+0.1}_{-0.1}$ | $9.8^{+1.4}_{-1.2}$ | $7.5^{+0.7}_{-0.7}$ | $35^{+17}_{-10}$ | 247.2/91 |
| 0.875–1.000 | $0.43^{+0.07}_{-0.07}$ | $5.3^{+0.2}_{-0.1}$ | $9.9^{+1.0}_{-0.9}$ | $5.7^{+0.7}_{-0.7}$ | $31^{+33}_{-27}$ | 117.5/89 |

Notes.

a Referring to Equation (1), and defined at 1 keV in units of photons keV$^{-1}$ cm$^{-2}$ s$^{-1}$.

b The energy and the width of the Fe-line are fixed at 6.62 keV and $\sigma_{Fe} = 0.37$ keV, respectively.
Table 3
Best-fit Parameters for Phase-resolved Spectra of 4U 1626−67, when Fitting by NPEX with GABS Model

| Pulse Phase | α | $kT$ (keV) | $A_1$ (×10$^{-4}$) | $A_2$ (×10$^{-5}$) | $E_{Fe}$ (keV) | $\sigma_{CRSF}$ (keV) | $\tau$ | EW$_{Fe}$$^b$ (eV) | $\chi^2$/d.o.f | $F$/PCI $^c$ |
|-------------|---|------------|-------------------|-------------------|---------------|------------------|-------|----------------|----------------|------------|
| 0.000−0.125 | 0.05$^{+0.18}_{-0.07}$ | 5.4$^{+3.8}_{-0.8}$ | 6.5$^{+0.5}_{-0.4}$ | <2.4 | 31.3$^{+2.3}_{-1.6}$ | 0.5$^{+0.5}_{-0.3}$ | >5 | < 57 | 66.9/78 | 1.169/2.45 × 10$^{-1}$ |
| 0.125−0.250 | 0.29$^{+0.26}_{-0.40}$ | 11.2$^{+4.4}_{-1.8}$ | 7.8$^{+10.8}_{-1.7}$ | 0 (fixed) | 26.3$^{+5.6}_{-4.1}$ | 5.4$^{+3.7}_{-1.2}$ | 15$^{+47}_{-3}$ | 43$^{+23}_{-28}$ | 85.3/94 | 1.061/3.87 × 10$^{-1}$ |
| 0.250−0.375 | 0.21$^{+0.29}_{-0.22}$ | 6.5$^{+2.6}_{-3.0}$ | 7.5$^{+1.0}_{-0.3}$ | <4.6 | 33.5$^{+1.1}_{-3.2}$ | 4.0$^{+2.8}_{-1.5}$ | 14$^{+15}_{-6.0}$ | 24$^{+37}_{-10}$ | 91.9/100 | 1.451−3.14 × 10$^{-2}$ |
| 0.375−0.500 | 0.40$^{+0.07}_{-0.07}$ | 5.6$^{+0.6}_{-0.2}$ | 9.8$^{+1.2}_{-1.9}$ | 5.0$^{+1.1}_{-2.0}$ | 37.1$^{+3.8}_{-2.9}$ | 3.9$^{+1.2}_{-1.1}$ | 23$^{+11}_{-6.5}$ | <45 | 133.6/126 | 2.178/7.62 × 10$^{-6}$ |
| 0.500−0.625 | 0.33$^{+0.07}_{-0.07}$ | 6.6$^{+0.5}_{-0.4}$ | 6.8$^{+0.9}_{-0.8}$ | 3.4$^{+0.9}_{-1.0}$ | 37.2$^{+2.2}_{-2.2}$ | 3.9$^{+1.2}_{-1.1}$ | 23$^{+11}_{-6.5}$ | <45 | 133.6/126 | 2.178/7.62 × 10$^{-6}$ |
| 0.625−0.750 | 0.38$^{+0.03}_{-0.03}$ | 6.4$^{+0.1}_{-0.1}$ | 8.0$^{+0.1}_{-0.1}$ | 4.2$^{+0.5}_{-0.1}$ | 36.8$^{+1.0}_{-0.9}$ | 4.0$^{+1.1}_{-0.8}$ | 20$^{+4}_{-3}$ | 39$^{+16}_{-19}$ | 83.6/105 | 3.012−1.63 × 10$^{-8}$ |
| 0.750−0.875 | 0.27$^{+0.06}_{-0.06}$ | 7.1$^{+0.8}_{-0.5}$ | 6.7$^{+0.7}_{-0.7}$ | 2.6$^{+1.0}_{-1.2}$ | 39.0$^{+2.5}_{-1.9}$ | 5.5$^{+1.4}_{-1.2}$ | 29$^{+20}_{-9}$ | 38$^{+26}_{-22}$ | 108.7/88 | 2.199/1.25 × 10$^{-4}$ |
| 0.875−1.000 | 0.37$^{+0.07}_{-0.07}$ | 8.0$^{+2.5}_{-2.5}$ | 7.6$^{+0.5}_{-0.5}$ | 1.4$^{+0.7}_{-0.7}$ | 43.3$^{+15.4}_{-8.5}$ | 10.0$^{+3.2}_{-3.2}$ | >10 | 30$^{+28}_{-28}$ | 90.4/86 | 1.256/1.45 × 10$^{-1}$ |

Notes.

a Referring to Equation (1) and defined at 1 keV in units of photons keV$^{-1}$ cm$^{-2}$ s$^{-1}$.

b The energy and the width of the Fe-line are fixed at 6.62 keV and $\sigma_{Fe} = 0.37$ keV, respectively.

c Referring to Equation (3), and PCI is probability of chance improvement of the $\chi^2$ by adding a new component.

Figure 5. Phase-resolved and background-subtracted XIS (FI: black symbols below 10 keV, BI: gray symbols) and HXD (black symbols over 10 keV) spectra of 4U 1626−67 for phases $\phi = 0.000−0.125$, 0.125−0.250, 0.250−0.375, 0.375−0.500, 0.500−0.625, 0.625−0.750, 0.750−0.875, and 0.875−1.000 from top to bottom, offset by multiples of 10$^{-2}$. Arrows denote the upper limit.

Since the GABS model reproduces an absorption feature, we fit the phase-resolved spectra by the NPEX plus a Gaussian model in which we allowed the Gaussian normalization to be both positive and negative. The derived parameters are shown in Table 4 and Figure 10. The results indicate that the emission line produces the residuals from the NPEX fitting in Figure 8(a).

We can evaluate how much the additional term improved the fit using the F test for additional terms (Bevington 1969).

Figure 6. Ratios between the phase-resolved and background-subtracted XIS and HXD spectra of 4U 1626−67 and those of the Crab Nebula. The XIS source data were normalized using the canonical model of the Crab Nebula since spectra from the Crab Nebula suffer from pile-up. Phases are indicated in the same manner as Figure 5, but are offset by multiples of 10$^{-2}$. Arrows denote the upper limit.
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Figure 7. Ratios between the data and best-fit NPEX-only model for each phase-resolved spectrum. Phases are indicated in the same manner as Figure 5. Arrows denote the upper limit.

The statistical value, hereafter called \( F_\chi \), is defined as

\[
F_\chi = \frac{(\chi^2_1 - \chi^2_2)/\nu_2}{\chi^2_2/\nu_2}.
\]

(4)

Each suffix denotes model 1 and 2, NPEX only and NPEX + Gaussian model, respectively. The derived probability from \( F_\chi \) also summarized in Table 4. The results show that the data support the presence of the emission line in the dim phase with \( F_\chi \) of 7.688, corresponding to a probability of chance improvement of \( \chi^2 \) of \( 1.9 \times 10^{-4} \). The residuals of the fitting are shown in Figure 8(c). The obtained resonance energy, \( E_a = 40.5^{+13.7}_{-14.7} \) keV, is statistically consistent with those observed in the other phases.

To examine the chance probability of improvement of the derived \( F_\chi \) value, we simulate the spectra following a procedure similar to Section 5.2 of Protassov et al. (2002). First, we simulate 10,000 data sets using “fakeit” in XSPEC Version12 according to the NPEX \(( A_p = 0 \)\) model with parameters fixed at best-fit values listed in Table 2, same instrumental response, background files, and same exposure time. Each data set is binned using same binning as that used for real data. Second, we fit the simulated data using only NPEX \(( A_p = 0 \)\) and NPEX \(( A_p = 0 \)\) + Gaussian model allowing their normalization to be negative. Third, we calculate the \( F_\chi \) derived by these two model fittings. Last, we evaluated the number of simulated spectra with \( F_\chi \) exceeding the 7.688, which is derived by fitting of real data to estimate the approximate probability. The derived histogram of the \( F_\chi \) is shown in Figure 11 and the evaluated chance probability is \( 3.0 \times 10^{-4} \) which is consistent with the \( F_\chi \) value obtained from real data using Equation (4). In order to evaluate the effect of systematic error of the HXD-PIN NXB model, we also refit the dim phase spectrum taking into account the 3\% systematic errors of HXD-PIN. The \( F_\chi \) is \( 7.688^{+2.523}_{-2.490} \) and the probability is between \( 2.91 \times 10^{-3} \) and \( 1.53 \times 10^{-5} \). Therefore, even though the NXB level of HXD-PIN is underestimated, we have possibly detected the emission line at the cyclotron resonance energy in the dim phase. Although there is a \( 85\% \) possibility that the structure in the dim phase is produced by an absorption feature, we stress that the continuum requires a hard component with a large cutoff energy, in addition to a wide and deep absorption feature, as seen in Figure 12. Furthermore, the \( kT \) value at the dim phase matches those at the other phases with the emission model, whereas a large jump in the value is required with the absorption model, as shown in Figure 9.

4. DISCUSSION

We observed the 4U 1626–67 pulsar with the Suzaku satellite in 2006 March. The pulse period determined by the HXD-PIN
of Suzaku is $P_{\text{Suzaku}} = 7.6779(9)\, \text{s}$, and this value agrees with that reported by Camero-Arranz et al. (2010). In the pulse phase-averaged spectra, the fundamental CRSF is clearly detected at $37.4^{+1.0}_{-0.9}\, \text{keV}$ (GABS model) and the continuum emission is better reproduced by the NPEX model than the ECUT model. Phase-resolved spectral analyses consistently show strong phase dependence, both in the continuum emission and in the CRSF, particularly in the dim phase. Quantitatively,
Figure 10. Fit parameters as a function of pulse phase for 4U 1626−67. Best-fit values by NPEX plus Gaussian model (Table 4) are plotted.

Figure 11. Observed value of the $F_{\chi}$ plotted as dashed line against probability histogram of $F_{\chi}$ obtained by 10,000 simulations (see the text).

the positive component of the NPEX model vanishes near the dim phase, and the CRSF in the dim phase is reproduced by using a Gaussian-shaped emission line model. The statistical significance of the emission line using the Bevington (1969) $F$-test routine is $2.91 \times 10^{-3}$ and $1.53 \times 10^{-5}$ taking into account the systematic errors in the background evaluation of HXD-PIN. The results mean that even if the real NXB level of HXD-PIN is 3% higher, which is the worst case of underestimating the NXB level, the significance is still around $3\sigma$ level. Thus, we have possibly detected the emission line at the cyclotron resonance energy in the dim phase.

In this section, we discuss the nature of the accretion column on the magnetic pole of the neutron star that produces a cyclotron emission line at the dim phase rather than an absorption feature.

What is the origin of the emission feature in the dim phase? Nagel (1981) pointed out that if the photons originate from an optically thick accretion column (with a Thomson optical depth $\tau_T > 1$) without temperature and density gradients, the CRSF is expected to be an absorption feature with Comptonized spectra. In contrast, if the photons originate from an optically thin accretion column ($\tau_T < 1$), the CRSF is expected to be an emission feature with a free–free continuum. To compare this theoretical model with the Suzaku spectra, the unfolded spectra in the on-phase ($\phi = 0.625–0.750$) and the dim phase ($\phi = 0.125–0.250$) are shown in Figure 13. Qualitatively, our observed results are consistent with the theoretical predictions; the Wien hump disappears with the appearance of an emission-like feature. This resemblance suggests that we observed the
cyclootron resonance scattering emission feature caused by collisional excitation of a Landau level, followed by radiative deexcitation. The deciding factor as to whether we observe absorption spectra or emission spectra is thus the optical depth of the accretion column, and for the case of 4U 1626−67, since change occurs according to the spin phase, changes in optical depth arise from changes in viewing angle.

The optical depth, $\tau$, is generally expressed as

$$\tau = n_e \sigma l.$$  \hspace{1cm} (5)

Here, $n_e$ is the electron number density, $\sigma$ is the scattering cross section, and $l$ is the plasma length-scale through which a photon passes. In a strong magnetic field, where the strength of the field is greater than the thermal energy, the scattering cross section depends on the direction of photons relative to the magnetic field vector. According to Herold (1979), the scattering cross section of photons averaged over the energy and the (ordinary and extraordinary) modes is described by

$$\sigma_1 \approx \sigma_T \left( \frac{\bar{E}}{E_a} \right)^2,$$  \hspace{1cm} (6)

when the photons have energies far less than $E_a$, and they propagate parallel to the magnetic field. Here, $\sigma_T$ is the Thomson scattering cross section and $\bar{E}$ is the mean photon energy. Thus, the optical depth propagating parallel to the magnetic field, $\tau_\parallel$, is

$$\tau_\parallel \approx n_e \sigma_T \left( \frac{\bar{E}}{E_a} \right)^2 l_\parallel.$$  \hspace{1cm} (7)

In contrast, the averaged cross section for photons propagating perpendicular to the magnetic field, $\sigma_\perp$, can be approximated by

$$\sigma_\perp \approx \sigma_T,$$  \hspace{1cm} (8)

and the optical depth propagating perpendicular to the magnetic field, $\tau_\perp$, is

$$\tau_\perp \approx n_e \sigma_T l_\perp.$$  \hspace{1cm} (9)

Therefore, from Equations (7) and (9) we see that the optical depth is anisotropic, and the probability of Comptonization of photons depends on the direction in which the photons are propagating through the plasma. This anisotropy of optical depth in the Comptonization process is expected to cause the phase dependence of the Wien hump.

To verify the phase dependence of the Wien hump, we again fit the phase-resolved spectra by the NPEX model, except for the dim phase, where the $kT$ value are instead fixed at the phase-averaged value (Table 1) by assuming thermal equilibrium. Here, the CRSF is described by the GABS model and the spectral fits are found to be acceptable. Figure 14 shows the background-subtracted pulse profile for the 10–30 keV energy band and compares this with values of $A_p$ plotted as a function of the pulse phase. These two plots clearly agree. In other words, X-ray fluxes in the 10–30 keV range are represented by only the Wien hump. Since, as described above, radiation is caused by the optical depth of scattering, the dim phase corresponds to the optically thin phase. Therefore, this result is explained correctly by our prediction.

To estimate the value of $\tau_\parallel$ qualitatively, we use the simple assumptions that the plasma is in thermal equilibrium and that the accretion column is homogeneous. Under these conditions, $\bar{E}$ is equal to the electron temperature. Therefore, the ratio between $\tau_\parallel$ and $\tau_\perp$ is estimated by using the observed $kT \sim 6.71$ keV and the $E_a \sim 37.4$ keV derived from fitting the phase-averaged spectra by the NPEX with GABS model (Table 1):

$$\frac{\tau_\parallel}{\tau_\perp} \approx \left( \frac{\bar{E}}{E_a} \right)^2 \frac{l_\parallel}{l_\perp} \approx \left( \frac{kT}{E_a} \right)^2 \frac{l_\parallel}{l_\perp} = 3.2 \times 10^{-2} \frac{l_\parallel}{l_\perp}.$$  \hspace{1cm} (10)

Thus, if the difference between $l_\parallel$ and $l_\perp$ is small ($l_\parallel \sim l_\perp$), the
optical depth for the dim phase spectra is approximately one or two orders of magnitude lower than that in the bright phase. If we assume that the Thomson optical depth of the bright phase is around 10, the cyclotron resonance scattering absorption feature can be seen as an emission feature at a certain viewing angle.

In the future, we plan to further investigate the radiative transfer of photons in the accretion column through theoretical studies that take into account emission power.

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