Observations and Spectral Modelling of the Narrow–Lined Type Ic SN 2017ein

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ABSTRACT
SN 2017ein is a narrow–lined Type Ic SN that was found to share a location with a point–like source in the face on spiral galaxy NGC 3938 in pre–supernova images, making SN 2017ein the first credible detection of a Type Ic progenitor. Results in the literature suggest this point–like source is likely a massive progenitor of 60–80 M⊙, depending on if the source is a binary, a single star, or a compact cluster. Using new photometric and spectral data collected for 200 days, including several nebular spectra, we generate a consistent model covering the photospheric and nebular phase using a Monte Carlo radiation transport code. Photospheric phase modelling finds an ejected mass 1.2–2.0 M⊙ with an $E_k$ of $\sim (0.9 \pm 0.2) \times 10^{51}$ erg, with approximately 1 M⊙ of material below 5000 km s⁻¹ found from the nebular spectra. Both photospheric and nebular phase modelling suggests a 56Ni mass of 0.08–0.1 M⊙. Modelling the [O i] emission feature in the nebular spectra suggests the innermost ejecta is asymmetric. The modelling results favour a low mass progenitor of to 16–20 M⊙ which is in disagreement with the pre–supernova derived high mass progenitor. This contradiction is likely due to the pre–supernova source not representing the actual progenitor.

Key words: supernovae: general–radiative transfer–supernovae: individual: SN2017ein

1 INTRODUCTION
Type Ic SNe are a sub-class of core collapse supernovae in which the progenitor star has lost all of its H envelope and all or almost all of its He envelope prior to collapse. The processes needed to strip this material is thought to be periods of significant mass loss driven by winds (e.g. Nomoto et al. (1995); Langer (2012)) or through some binary interaction mechanism. For high mass single star evolution, the LBV phase may be responsible for the significant mass loss that could produce H/He-stripped SNe, but this may not be able to reproduce low mass events such as SN1994I (Nomoto et al. 1994; Sauer et al. 2006). However, single star evolutionary models are often unable to effectively strip all the H required to produce Type Ib SNe and all the H/He required to produce the Type Ic SNe. Mass loss during a common envelope phase or Roche lobe mass transfer for stars evolving in a binary can explain stripping but can leave thin shells of He of low mass above the carbon and oxygen rich (CO) core (Nomoto et al. 1995; Yoon et al. 2010). This may explain the sometimes observed weak He i lines in Type Ic SNe (Elmhamdi et al. 2006; Prentice et al. 2018).

Several Type II SNe progenitors have been likely identified, summarised in Smartt (2009), and these observations have given some constraints on the possible progenitor mass distribution for Type II SNe, but no Type Ib/c progenitors have been definitively observed yet. The Type II identifications have suggested an upper limit for the observed red supergiants (RSG) to be near $\sim 17$ M⊙, while the theoretical upper limit was expected to be closer to 20-25 M⊙. This difference between the observed and theoretical upper limit is called the “RSG problem” (Smartt et al. 2009). This gap may be related to a poor understanding of late time stellar evolution and mass loss rates but is still an open question (Davies & Beasor 2018, 2020). For Type Ib/c SNe, the ejecta mass distribution is more varied compared to non-stripped SNe as shown in Prentice et al. (2019) and estimating the progenitor mass of these SNe from ejecta masses also results in a wide range of possible progenitor masses. In addition, the binary and single star channels for Type Ib/c SNe may contribute to the total number of Type Ib/c SNe at different $M_{ZAMS}$.

SN 2017ein was first detected by Ron Arbour on 2017...
May 25.97 (Arbour 2017), in the face on spiral galaxy NGC 3938. The object was classified soon after detection as an early Type Ic SN (Xiang et al. 2017). After the detection, Van Dyk et al. (2018); Kilpatrick et al. (2018); Xiang et al. (2019) used archival Hubble images and detected a point-like source at the same location of SN 2017ein, which would represent the first progenitor detection for a Type Ic SN. All three groups used a combination of methods to derive an estimated progenitor mass based on the observations of this point source. One method used is to calculate the colour, derived from observations using the two Hubble filters F555W and F814W, and compare these values to a set of single and binary star evolutionary tracks. Van Dyk et al. (2018) used a set of evolved rotating massive stars from MIST (Choi et al. 2016) and a set of binary star evolution models from BPASS V2.1 (Eldridge et al. 2017) and estimated a single star $M_{\text{ZAMS}}$ of $\sim$47–48 M$_\odot$ if the star evolved alone and a $M_{\text{ZAMS}}$ of $\sim$60–80 M$_\odot$ if the star evolved in a binary, depending on the metallicity of the stars. Xiang et al. (2019) used a set of evolved rotating massive stars from Georgy et al. (2012) and estimate a $M_{\text{ZAMS}}$ of $\sim$ 60 M$_\odot$. Assuming the point-like source was instead a compact blue cluster, all three groups estimate the $M_{\text{ZAMS}}$ to within the same mass range of the previous estimates using single or binary star conclusions. Using the nearby environment to constrain the properties of the star, under the assumption of a single phase of star formation, they again find a similar progenitor mass.

The semi-analytic Arnett fits (Arnett 1982) for $^{56}$Ni powered SNe as in Van Dyk et al. (2018) give an estimated $M_{\text{ej}}$ of 1–2 M$_\odot$, while a similar model in Xiang et al. (2019) finds a $M_{\text{ej}}$ of 0.9 ± 0.1 M$_\odot$. Both recognise that the estimated progenitor mass is far more massive than what the $M_{\text{ej}}$ estimates would suggest. Maund & Ramirez-Ruiz (2016) estimated a $M_{\text{ZAMS}}$ for the progenitor of SN 2007gr, using similar methods as above, to be $\sim$40 M$_\odot$. This is in contrast to the progenitor mass inferred from the low mass ejecta modelled from the nebular spectra by MazZali et al. (2010) of approximately $\sim$1 M$_\odot$, which would be analogous to a $\sim$15 M$_\odot$ progenitor.

In this work, we first present and discuss observations of SN 2017ein and the data reduction methods in Section 2, the resulting photometric light curves in Section 3, and the observed spectra in Section 4. Using this data, we model both the photometric and nebular phase of the spectral evolution and generate a bolometric light curve in Section 5. In Section 6, we discuss the synthetic model and its results with respect to stellar evolution and possible progenitor properties.

## 2 DATA COLLECTION

Observations of SN 2017ein began on 2017 May 28.91 (MJD 57901.91) with IO:I on the Liverpool Telescope (LT) (Steele et al. 2004), based at the Roque de los Muchachos Observatory, La Palma, Spain. The first LT spectroscopic observation was made with the SPectrograph for the Rapid Acquisition of Transients (SPRAT; Piascik et al. 2014) on 2017 May 29.04 (MJD 57902.04). Photometry was performed on sources in the exposures using a custom PYTHON pipeline, which called PYRAF to run standard IRAF routines. The instrumental magnitudes were then calibrated to Sloan Digital Sky Survey (SDSS; Ahn et al. 2012) standard stars in the field. SPRAT spectra were automatically reduced and the wavelength and flux calibration was done via the LT pipeline (Barnsley et al. 2012) and a custom PYTHON script. The spectra were then flux calibrated to the photometry.

### 2.1 NGC 3938 - distance and reddening

The distance to the host galaxy, NGC 3938 is highly uncertain, and this has been discussed at length in both Van Dyk et al. (2018) and Xiang et al. (2019). The latter adopts $\mu = 31.38 \pm 0.3$ mag, while the former takes a range between 31.15 to 31.75 mag. We adopt the average of the average value between recent Tully-Fisher measurements of the distance toward NGC 3938$^1$, giving $\mu = 31.5$ mag. The dust maps of Schlafly & Finkbeiner (2011) indicate that extinction in the direction of NGC 3938 is $E(B-V)_{\text{MW}} = 0.019$ mag.

Reddening at the source has been extensively discussed in the literature. Estimating $E(B-V)_{\text{host}}$ from the host Na i D lines in our spectra gives a large range of values from 0.1 to 0.5 mag (Poznanski et al. 2012), but these spectra are low resolution, thus we defer to the value of $E(B-V)_{\text{host}} = 0.4$ mag given in Van Dyk et al. (2018) and Xiang et al. (2019) for their higher resolution spectra.

### 3 LIGHT CURVES

Figure 1 shows the ugriz light curves, given in Table 2, obtained with the LT over $\sim$ 240 days. SN 2017ein was discovered early, as evidenced by the rapid rise in the light curves. Only the rise of u-band is missed. As is typical for SE-SNe, the light curves peak progressively later in the redder bands. The peak of the u-band is 3–5 days before g-band, which is longer than the $\sim$ 1 day measured for similar objects (Taddia et al. 2018). The transient went behind the sun just as the light curves settled on to the decay tail.

A curious behaviour is seen in the later z-band evolution, which shows a dramatic decay in luminosity away from the linear decline normally seen in these types of events. Further investigation reveals that this is also seen to a lesser extent in r- and i-bands. The drop-off in SN 2017ein is pronounced when shown against the evolution of SN 2007gr, which is demonstrated in Fig. 2 for the r- and R-band light curves of SN 2017ein, the latter from (Xiang et al. 2019) and the R-band of SN 2007gr (Hunter et al. 2009). It can be seen that for the first $\sim$ 100 days the three light curves track each other but by the time the observations of SN 2017ein

| Table 1. Several relevant observational properties of SN 2017ein |
|-----------------|-----------------|
| $\alpha$        | 11:52:53.25     |
| $\delta$ (J2000)| +44:07:26.20    |
| Host            | NGC 3938        |
| $\mu$           | 31.5 mag        |
| $E(B-V)_{\text{MW}}$ | 0.019 mag    |
| $E(B-V)_{\text{host}}$ | 0.4 mag$^1$     |

$^1$ Van Dyk et al. (2014); Xiang et al. (2019)
were resumed there is a clear deviation. As the decline is seen in both SN 2017ein data sets we can conclude that this is intrinsic to the event and is not a consequence of a data reduction issue.

3.1 Pseudo-bolometric Light Curve
The $ugriz$ photometry allows the construction of a pseudo-bolometric light curve with SEDs covering 3000 – 10000 Å. It is constructed using the observed photometry, corrected for $E(B - V)_{\text{tot}}$ using the extinction law of Cardelli et al. (1989) and $R_v = 3.1$, which is then converted to a flux and the spectral energy distribution for each data integrated over the wavelength range. Finally, the bolometric luminosity was calculated using the luminosity distance derived from the distance modulus. $u$-band magnitudes were estimated for epochs when no $u$-band observations were taken by assuming a constant $u - g$ band colour for dates prior to the first observation and after the final $u$-band observation. The method is described in more detail in Prentice et al. (2016).

The pseudo-bolometric light curve is shown in comparison with a sample of SNe Ic in Fig. 3. When looking at the light curve properties in the photospheric phase, SN 2017ein is a typical SN Ic-7 (a narrow lined SN Ic as per Prentice & Mazzali 2017). The peak luminosity for the pseudo-bolometric light curve is $(2.5 \pm 0.3) \times 10^{42}$ erg s$^{-1}$ and is typical for SNe Ic-6/7. The characteristic time-scales, $t_{-1/2}$ and $t_{+1/2}$ measure the rise from luminosity at half maximum to maximum, and from maximum to half maximum respec-
The late time light curves of SN 2017ein deviate from SN 2007gr curve of the spectroscopically similar SN 2007gr (blue squares). R curve for the same object (red triangles) and the Xiang et al. (2019) R circle compared with SN 2007gr (black diamonds) and a sample of 9\(\pm\)2 d respectively (Prentice et al. 2016, 2019). This group is mainly defined by the separation of Fe ii \(\lambda\lambda 4924, 5018, 5169\) into three distinct components. This sub-class has diverse photometric properties, and includes SN 2011bm (Valenti et al. 2012), which has a rise time of > 35 days.

4.1 Line velocities

Figure 5 gives the line velocities of SN 2017ein as a function of time for Fe ii \(\lambda\lambda 5169, Na i D, Si ii 6355,\) and O i \(\lambda 7774\). Line velocities are measured from the centre of the absorption profile minimum, the uncertainty represents the width in velocity space of this minimum. The highest velocities are those in the classification spectrum (Xiang et al. 2017), at \(-12.8\) km \(\text{s}^{-1}\) and within a few days of explosion. It displays Fe ii and Na i at \(16000\) km \(\text{s}^{-1}\) while O i is at \(\sim 14000\) km \(\text{s}^{-1}\). This spectrum is the only one accessible to this work where the wavelength range covers the Ca ii NIR triplet, for which a velocity of \(19000\) km \(\text{s}^{-1}\) is measured.

The line velocities decrease rapidly over the course of a week, which further hints at the young nature of the transient. Comparison with the mean line velocities for a sample of Ic-6/7 SNe (Prentice et al. 2019) shows that the velocity curves are typical for a SE-SN of this type. The velocity curve also demonstrates that the line forming regions for each element overlaps, suggesting some degree of mixing within the ejecta. Some stratification is most noticeable between Si ii 6355 and the other elements. After maximum light the velocities all level off to between \(7000 - 9000\) km \(\text{s}^{-1}\).

4.2 Similar SNe

Figure 6(a) shows a small sample of Type Ic SNe compared to SN 2017ein at a epoch of approximately 1 week prior to bolometric peak. While these dates do not always reflect the epoch with respect to the explosion date, they offer a quick comparative view if the explosion date is not well constrained. SN 2017ein and SN 2007gr both share narrow features, with the Fe ii \(\lambda\lambda 4924, 5018, 5169\) lines being separated and easily identifiable. These features are only partially separated in SN 1994I and SN 2004aw, while SN 2002ap does not show the same Fe ii features. Figure 6(b) shows the same

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2 These values agree with those measured from a 4000 – 10000 Å pseudo-bolometric light curve (Prentice et al. 2016, 2019) to within the uncertainties of the measurements.
SNe approximately 2 weeks after the time of the bolometric max, with SN 2007gr and SN 2017ein showing similar spectral behaviour over the shared wavelength range. SN 1994I and SN 2004aw also share similarities with each other, with the exception of the dominant feature near 5500 Å, thought to be helium (Filippenko et al. 1995; Sauer et al. 2006). The nebular epochs in Figure 6(c) show fewer differences between the set of SNe with again, SN 2007gr showing the most similarity to SN 2017ein.

Figure 5. Velocities as measured from the absorption line minima. Also shown as dashed lines are the median line velocities for a selection of SNe Ic 6/7.

5 MODELLING

We present the model for SN 2017ein following the abundance tomography method (Stehle et al. 2005) used to model other SNe such as SN1994I (Sauer et al. 2006) and SN 2004aw (Mazzali et al. 2017). The spectra cover a temporal range of −12.5 days to +192 days with respect to the pseudo-bolometric peak, with a well sampled photospheric phase that covers the −12.5 to +34.2 day range and 3 nebular spectra at +140 to +192 days. Of the photospheric spectra, we select 6 spectra in total, three pre-$t_p$, and three post-$t_p$, that show the spectral evolution and have a good S/N.

We start with an initial density structure based upon a 22 $M_\odot$ progenitor model. This model is stripped of all H/He to produce a CO core of approximately 3.4 $M_\odot$ prior to core collapse. Teffs et al. (2020a) explored this model in detail as part of a parameter study that included four explosion energies of 1, 3, 5, and 8 foe, where 1 foe is defined as $1 \times 10^{51}$ erg. This model had good success in reproducing a set of observed spectra from multiple Type Ic SNe without fine tuning any parameters, so we treat the density and abundance structure of the 1 foe model as our base. Given the estimated ejecta properties in Van Dyk et al. (2018); Kilpatrick et al. (2018); Xiang et al. (2019) and the results from our parameter study from Teffs et al. (2020a), the initial CO core model is likely too massive to reproduce both the spectra and photometry due to a slower diffusion time post peak and the lack of similarity to SN 1994I shown in Teffs et al. (2020a). To find a better fit for SN 2017ein, we rescale the model using the method in Hachinger et al. (2009) by using equations 1 and 2.

\[
\rho' = \rho \left( \frac{E'_k}{E_k} \right)^{-3/2} \left( \frac{M'_ej}{M_{ej}} \right)^{5/2} 
\]

\[
v' = v \left( \frac{E'_k}{E_k} \right)^{1/2} \left( \frac{M'_ej}{M_{ej}} \right)^{-1/2}
\]

The primed variables in equations 1 and 2 are the new, rescaled variables and un-primed are the original variables. The model is re-scaled to some initial parameters for $E_k$ and $M_{ej}$, with the initial $M_{Ni}$ derived from the peak luminosity.
The scaled density profile is then used in our Monte Carlo light curve code, which tracks the emission and propagation of γ-rays and positrons produced by the decay of \(^{56}\)Ni, and subsequently \(^{56}\)Co, in to the homologously expanding ejecta as described in detail in Cappellaro et al. (1997). The outputted bolometric light curve is then compared to the observed pseudo-bolometric light curve and the process is repeated until the calculated light curve reproduces the observed light curve with reasonable accuracy.

The re-scaled model and its initial abundances are then used in our spectral synthesis code, described in detail in Mazzali & Lucy (1993); Lucy (1999); Mazzali (2000). This code reads in the composition and the density profile of the ejecta to produce a stratified model where each layer is defined by an observed spectrum and fitted abundances, photospheric luminosity \((L_{\text{ph}})\), and photospheric velocity \((v_{\text{ph}})\). These parameters are systematically changed until the synthetic spectrum best reflects the observed spectrum and its behaviours. By using abundance tomography, this allows us to create a stratified ejecta that gives us both the abundance and distribution of elements responsible for the formation of the spectral features. For elements that do not produce strong optical features or that produce features beyond the observed spectral wavelength range of SPRAT \((\lambda > 8000 \text{ Å})\), such as the strong Ca II feature near 9000 Å, we are unable to constrain the abundance of those elements.

Using these methods, we find a model with an \(M_{\text{ej}}\) of 1.6 ± 0.4 \(M_{\odot}\), 0.09 ± 0.01 \(M_{\odot}\) of \(^{56}\)Ni, and an \(E_{\text{k}}\) of 0.9 ± 0.2 foe that reproduces the bulk of the spectral features and the pseudo-bolometric light curves, with error estimates taken from the error analysis by Ashall & Mazzali (2020) and shown for simplicity in Table 3. In order to reproduce the velocity of the \(\text{O I} \lambda 7774\) line early in the spectra, the outermost region, or \(v > 12000 - 27000 \text{ km s}^{-1}\), is reduced in density by expanding the shell. This outer reduction in density may be a result of a low mass He shell not present in the initial model or some asymmetry.

| Mass \([M_{\odot}]\) | \(M_{\text{Ni}}\) \([M_{\odot}]\) | \(E_{\text{k}}\) \([10^{51}\text{erg}]\) | \(E_{\text{k}}/M_{\text{ej}}\) | \([10^{51}\text{erg}/M_{\odot}]\) |
|-------------------------------|-----------------|-----------------|---------------------|----------------|
| 1.6 ± 0.4 | 0.09 ± 0.01 | 0.9 ± 0.2 | 0.56 ± 0.05 |

5.1 June 1st, 2017; \(t_p = -6.2\) d, \(t_{\text{exp}} = +7\) d

The epoch shown in Fig. 7(a) is not the earliest available epoch, but shows good S/N with well defined features compared to the earlier spectrum. The best fit synthetic spectrum has a \(v_{\text{ph}}\) of 11 000 km s\(^{-1}\) and an \(\text{Log}_{10}(L_{\text{ph}}) = 42.295\) erg s\(^{-1}\). The \(v_{\text{ph}}\) and \(L_{\text{ph}}\) parameters can be modified by of 5-10 % before the fit starts to visibly suffer, and is discussed in more detail in Ashall & Mazzali (2020). This early observed spectrum has only a few strong features. The re-emission red of the C II line at 6500 Å is not well reproduced in the model and the synthetic C II lines are all slightly too broad. Despite this, the overall flux level and majority of features are well reproduced.

5.2 June 5th, 2017; \(t_p = -2.4\) d, \(t_{\text{exp}} = +11\) d

The best fit model spectrum in Fig. 7(b) has a \(v_{\text{ph}}\) of 9300 km s\(^{-1}\) and an \(\text{Log}_{10}(L_{\text{ph}}) = 42.395\) erg s\(^{-1}\). Most features are well reproduced in the synthetic model, but the C II features at 6500 Å is too broad when compared to the observed spectrum. In addition, the flux level in the near-UV is slightly under the observed spectrum, but is necessary to reproduce the remaining features.
5.3 June 7th 2017; $t_p - 0.4\, d$, $t_{\text{exp}} + 13\, d$

The model spectrum in Fig. 7(c) has a $v_{\text{ph}}$ of 8800 km s$^{-1}$ and an $\log_{10} (L_{\text{ph}}) = 42.410$ erg s$^{-1}$. The Fe II lines are very well reproduced at this epoch, but the flux level is lower than the observed in the 5000–6500 Å region. Similar to the previous epoch, more Fe-group material may improve this at the cost of the Fe II features. The C II line at 6200 Å is narrow in the observed spectrum, but too broad in the synthetic spectrum. There may be a feature near 5600 Å but is hard to discern due to noise in the spectrum. This may be a S i line or an early Sc II line but is not reproduced in our models.

5.4 June 10th 2017; $t_p + 2.5\, d$, $t_{\text{exp}} + 15.5\, d$

The model spectrum in Fig. 7(d) has a $v_{\text{ph}}$ of 8300 km s$^{-1}$ and an $\log_{10} (L_{\text{ph}}) = 42.395$ erg s$^{-1}$. The region between 5200–5800 Å is poorly reproduced in this model despite the remaining features showing strong similarity. The next epoch shows these may be the beginnings of the Sc II features that become dominant in the next epoch. By this epoch, the C II line is blended, too weak, or largely absent and the Na i D line is beginning to become strong.

5.5 June 17th 2017; $t_p + 9.6\, d$, $t_{\text{exp}} + 23\, d$

By this epoch, the observed spectrum is relatively low in flux, noisy, and has a multitude of weak features in the spectrum. The model spectrum in Fig. 7(e) has a $v_{\text{ph}}$ of 6000 km s$^{-1}$ and an $\log_{10} (L_{\text{ph}}) = 42.225$ erg s$^{-1}$. The previously tentatively identified Sc II features are now strongly matching to the observed spectrum. The abundances of Sc and velocity range required to produce these lines are given in Figure 8. Increasing the velocity range or mass of Sc can cause these lines to dominate in the later spectra. The Fe II feature is too broad and deep, but is required for the rest of the spectrum to match. The region between 6200–7300Å has contributions from O i, Fe ii, and Ti ii lines and is difficult to match each one as the features are not strong and the spectrum is noisy.

5.6 June 21st 2017; $t_p + 13.5\, d$, $t_{\text{exp}} + 27\, d$

For the final photospheric epoch modelled in this work, the synthetic model Fig. 7(f) has a $v_{\text{ph}}$ of 4000 km s$^{-1}$ and an $\log_{10} (L_{\text{ph}}) = 42.10$ erg s$^{-1}$. At this phase, the photospheric velocity becomes harder to define as nebular emission, evident in the Ca ii NIR triplet in the wider wavelength range spectra given in Van Dyk et al. (2018); Kilpatrick et al. (2018); Xiang et al. (2019), is a non-negligible contribution to the total observed flux. As the spectral synthesis code strictly treats the photospheric phase, this prevents a hard definition of the photospheric velocity, so the photospheric velocity value is the one required by the spectral shape and total flux. Beyond that, the rest of the spectrum is well reproduced. The Na i D lines fit could be improved with the addition of more Fe ii re-emission or a stronger S i contribution.
Figure 8. Mass fraction of the most abundant elements in the best fit model and the density profile (in black) shown on the right y-axis. The grey lines represent the modelled epochs with the $v_{ph}$ values given in Sections 5.1 to 5.6.

Figure 9. Fits to the [O i] $\lambda\lambda$6300,6363 doublet for the October 28th 2017 spectrum of SN 2017ein using the same method as in Taubenberger et al. (2009). The region around the doublet is normalised and scaled before the fit is applied.

5.7 [O i] Asymmetry in the Nebular Spectra

The [O i] $\lambda\lambda$6300,6363 doublet is typically the strongest feature in the nebular spectra of Type Ib/c SNe and forms in a region free from other dominant features. The shape of this feature is often used as a probe for both the total oxygen mass of the innermost ejecta and as a way to estimate asphericity in these SNe. Taubenberger et al. (2009) modelled the emission line using a combination of up to 3 [O i] components, each comprising of two Gaussian features that form a simplified [O i] $\lambda\lambda$6300,6363 doublet emission. Fits using up to three components reflect several possibly ejecta geometries, such as spherical or aspherical as well as torus–like structures.

We apply this method on the October 28th spectrum in Fig. 9 and the following two epochs, but show only this epoch for simplicity as the results are similar. A similar [O i] profile is shown for the three nebular spectra in Figure 4. When compared to a set of other Type Ic in Figure 6, SN 2007gr and the others do not show a similar [O i] profile. The secondary bump near 6400 Å and the approximately equal flux values of the two doublet peaks suggested two blobs of oxygen shifted by $\pm$30 Å. Driven by this, we use three Gaussians comprised of a red and blue shifted blob and a central blended feature. We find a redshifted blob at a velocity shift of $-1200$ km s$^{-1}$ and a blueshifted blob at a velocity shift of $2000$ km s$^{-1}$. From Taubenberger et al. (2009), a combination of these three components best reflects an asymmetric ejecta.

5.8 Nebular Spectral Modelling

In order to establish the properties of the inner $M_{ej}$, $^{56}$Ni mass and distribution in particular, we modelled the nebular-epoch spectra of SN 2017ein. Three spectra are available, at rest-frame epochs of 160, 207 and 212 days from the putative time of explosion. They all show emission lines of the elements that are typically seen in SNe Ib/c. Unfortunately, the signal-to-noise ratio of the spectra is not always very high, especially in the blue. The region short of 5000 Å is extremely noisy, which makes it very difficult to use the strength of the [Fe ii] lines as a test for the mass of $^{56}$Ni. Although this somewhat limits our models, we still use the overall flux to estimate the Fe flux. The strongest lines that are seen are [O i] $\lambda\lambda$6300,6363 and Ca ii $\lambda\lambda$7291,7324. Mg i $\lambda$4570 may also be seen, while a broad emission near 5200 Å may be identified as a blend of [Fe ii] lines, but it is affected by noise.

A particularly interesting aspect of the spectra is the multi-peaked structure of the [O i] $\lambda\lambda$6300,6363 line. This is not uncommon in SNe Ib/c and in some cases, very widely
Following Axelrod (1980), ionization is assumed to be negligible (Kozma & Fransson 1998). Ionization balance is obtained matching impact ionization and the rate of recombination for each ion, which depends mostly on density. Level population is computed in NLTE, balancing the thermal heating rate with cooling via line emission. This takes place mostly via forbidden lines, but some permitted transitions that can be strong in emission and contribute therefore to cooling are also included, e.g. Ca II IR triplet and H&K. The nebula is assumed to be optically thin, therefore radiation transport is not performed. This is a reasonable approximation at late times. Line emission then tracks the distribution of the emitting elements and that of $^{56}$Ni.

Given the profile of the [O i] line, it is clear that a single, spherically symmetric emission component would not be able to reproduce the observations in detail. Therefore we take a different approach. Using the abundance distribution derived from the early-time spectra, we model the broad component of the emission, completing the mapping of the density and abundances at low velocities as required to optimise the fit. We then add a narrow, blue-shifted component to reproduce the narrow peaks in the observed [O i] line. Finally, we test our results by evolving the model to different epochs and comparing to the observations. We note a discontinuity in the light curve when one compares points near 150 days and 200 days (Fig. 1). This poses a problem for both nebular and light curve modelling, which are based on the same treatment of gamma-ray and positron deposition.

As a first step, we determine the width of the [O i] $\lambda$6300,6363 emission using a 1-zone approximation. A value $v = 5000 \text{ km s}^{-1}$ is found to be appropriate at all epochs, when line blending is accounted for. This confirms that most $^{56}$Ni, as well as a significant fraction of oxygen, must be located inside this velocity. The broad emission profile is reasonably symmetric, suggesting that a 1D approach is sufficient for the bulk of the inner ejecta. Using the model above, which has $M_{\text{ej}} \approx 1.6 M_{\odot}$ and $E_{\text{kin}} \approx 9.0 \times 10^{54} \text{ erg s}^{-1}$, we find that a $^{56}$Ni mass of $\approx 0.078 M_{\odot}$, combined with an oxygen mass of $\approx 0.86 M_{\odot}$, yields a good fit to the broad feature at day 160.

When including the other elements at low velocity, we need to remember that we have no direct handle on important elements such as silicon and sulphur, whose strongest emission lines are predominantly in the near-infrared (NIR). Depending on the amount of these elements that is included in the model, the overall mass can change significantly (e.g., Maeda et al. 2019). Here we chose to keep the total mass as defined by the early-time modelling, which limits the mass of Si to $\approx 0.60 M_{\odot}$ and that of S to $\approx 0.07 M_{\odot}$, most of which is at velocities between 3000 and 7000 km s$^{-1}$. Calcium is responsible for the second strongest observed emission line, Ca ii $\lambda\lambda$7291,7324. The strength of this semi-forbidden transition allows us to determine the local density, which we achieve by setting some degree of clumping in the ejecta. We use a volume filling factor of 0.1 for the inner ejecta, which is in line with previous results for SNe Ib/c (e.g., Mazzali et al. 2010), and a total Ca mass of $\approx 0.014 M_{\odot}$. The synthetic spectrum obtained for day 160 is shown in Fig. 10.

A narrow-line emission spectrum is then computed as a 1-zone model, and added to the broad-lined spectrum. A

![Figure 10](image-url)
1-zone approach is appropriate because, given the resolution of the observed spectra, the narrow emission profiles are only approximately described. Typically, the narrow [O i] emission has a velocity width of \( \approx 1100 \, \text{km} \, \text{s}^{-1} \), which means that the two components are individually observed. The fact that they are in a ratio of about 2/3 implies that the local density is quite high, so again we need to use a volume filling factor of 0.1 for this clump of material. We assume that this clump is mostly composed of oxygen and heated by \(^{56}\text{Ni}\) decay. This is obviously an over-simplification, as given its low blueshift the clump is likely to be residing inside the bulk of the ejecta and therefore to be exposed to radioactivity from the rest of the \(^{56}\text{Ni}\). In any case, under the approximation we used, it is sufficient to place \(0.10 \, \text{M}_\odot\) of oxygen in a clump heated by 0.023 \(\text{M}_\odot\) of \(^{56}\text{Ni}\) to reproduce the observed narrow emission. When added to the broad component, a reasonable fit is obtained for the whole profile (Fig. 10).

The profile decomposition performed above suggested the need for three components, but we do not need that when we compute our synthetic models: the two main narrow peaks correspond to [O i] 6300 and 6363, respectively, not to a blue-and red-shifted narrow component. A 3-component model may explain the small ledge near 6400 Å. It is actually more likely that these two ledges, if they are indeed real and not just due to noise, are features of the overall density/abundance distribution, as they are rather symmetric with respect to [O i] 6300, at velocities of \( \sim 4000 \, \text{km} \, \text{s}^{-1} \). The narrow-lined spectrum shows emission also in [O i] 5577, which is a tracer of recombination and which may correspond to an observed feature. It may also show several [Fe ii] lines, but these are too weak to be distinguished in the noisy observed spectra.

If we evolve the model to later epochs, we can only obtain a good fit to the observations if we apply multiplicative correction factors of 1.3 for the spectrum on day 207 and 1.6 for that on day 212. Such rapid changes in the luminosity are unlikely unless we invoke improbable sudden changes in the gamma-ray or positron opacities. We discuss this issue in further detail in Section 6.4.

In conclusion, the nebular models largely confirm that \(^{56}\text{Ni}\) is concentrated to low velocities, as is expected in a low-energy explosion. The mass of \(^{56}\text{Ni}\) that is derived, \( \sim 0.08 \, \text{M}_\odot\), is consistent with that obtained from the light curve. An interesting question is the origin of the oxygen-rich blue-shifted clump. We do not see evidence of a counter-clump at some red-shift. It is possible, but unlikely given the symmetric profiles of the broad emission features, that such a clump might exist but its emission is absorbed by the bulk of the ejecta. The innermost layers of the ejecta may be characterised by some degree of asphericity, which may have been imprinted upon them at the time of the explosion. The mass of the clump is however quite small, and it would be even smaller if we actually embedded it in the \(^{56}\text{Ni}\)-dominated inner ejecta. It does not seem too likely, given the small amount of material comprising the clump, that the asphericity is caused by jets, but if that is indeed the case the jet(s) were weak and easily choked inside the dense deep CO core of the star. Such events may indeed be quite common in SNe Ib/c (Piran et al. 2019), and possibly in all core-collapse SNe (Nakar & Piran 2017; Gottlieb et al. 2021)

5.9 Light Curve

We compute a synthetic light curve using a Monte Carlo code discussed in detail in Cappellaro et al. (1997) and Mazzali (2000). The code requires a choice of density structure and elemental abundances including \(^{56}\text{Ni}\). The code tracks the emission and propagation of \(\gamma\)-rays and positrons produced by the decay of \(^{56}\text{Ni}\), and subsequently \(^{56}\text{Co}\), into the expanding ejecta. The gamma ray and positron opacities are given by \(\kappa_- = 0.027 \, \text{cm}^2 \, \text{g}^{-1}\) and \(\kappa_+ = 7 \, \text{cm}^2 \, \text{g}^{-1}\) (Axelrod 1980). The deposited energy from the decay is recycled into optical photons and the resulting propagation is followed using a similar Monte Carlo scheme. The optical opacity is both time and metallicity dependent, which aims to reproduce the dominance of line opacity in the ejecta (Ashall et al. 2019; Mazzali 2000). This code is used initially to produce an approximate model for the model inputs in the spectral synthesis code. After the photospheric and nebular spectra are fit, any changes to the model in density or abundances are used to produce a final light curve shown in Fig. 11.

The mass of \(^{56}\text{Ni}\) required to match the flux level of the nebular spectra is approximately 0.08 \( \text{M}_\odot \) compared to the 0.1 \( \text{M}_\odot \) of \(^{56}\text{Ni}\) required to match the pseudobolometric light curve in Figure 3. Photometric observations for SN 2017ein cover only the ugriz bands which cover a wavelength range of 3000 – 10000 Å, with no UV or IR contributions. Sauer et al. (2006) used the NIR/IR flux from SN2002ap, scaled to SN1994I to calculate an estimated NIR (\( \lambda > 10000 \, \text{Å} \)) flux to generate a more complete bolometric light curve. SN2002ap was chosen due to being a Type Ic SNe with well sampled NIR photometry. For SN 2017ein, both its spectral evolution and light curve behaviour is similar to that of SN 2007gr (Valenti et al. 2008; Hunter et al. 2009), and has JHK band (10000 – 25000 Å) coverage for both near peak and late time epochs. We follow the same method described in Sauer et al. (2006) to generate a modified bolometric light curve.

While the explosion models match the observed ugriz+ NIR light curve, the bolometric light curve from our synthetic spectral modelling is too luminous by 5-10%. This mismatch is likely the missing UV flux not taken into account in addition to the standard errors inherent to the observations and the modelling process that is discussed later.
The modified inner density and $^{56}\text{Ni}$ distribution required to match the nebular spectra is used to generate a second model. The modified model has a bolometric light curve that reproduces both early phase and late time phases fairly well. As only the innermost ejecta is modified, the spectra in Fig. 7 are unchanged.

6 DISCUSSION

6.1 Model Properties

The initial model in this work is based upon the CO core of a 22 M$_\odot$ progenitor model evolved at solar metallicity, with no binary, then stripped of all helium and exploded at 1 foe. The initial model with no modifications failed to reproduce the spectra and the light curve as did the higher $E_k$ models in Teffs et al. (2020a) using the same initial progenitor. This required us to modify the CO core model in order to best fit the observed spectra and light curve to get the results in Section 5.

Based upon the estimates given in Van Dyk et al. (2018); Kilpatrick et al. (2018); Xiang et al. (2019) and the similarity to SN 2007gr in Fig. 6, we re–scaled the mass of the model to get a $M_{ej}$ of 1.6 M$_\odot$ and the energy to match the relatively low velocity lines. We do note that re–scaling a model in either or both $E_k$ and $M_{ej}$ may not reflect the properties of an evolved CO core of the re–scaled mass. Based upon only the photospheric modelling, we suggest that the $M_{ej}$ of SN 2017ein is within the range of 1.2–2.0 M$_\odot$, using the error estimates from Ashall & Mazzali (2020). The $E_k$ was modelled to be $\sim$0.9 foe. These values place the $E_k/M_{ej}$ ratio to be $\sim$0.56 foe/M$_\odot$ for the best fit model. Comparing these ratios to those found in Prentice & Mazzali (2017), the $E_k/M_{ej}$ ratio for our model is on the low end. Both SN 1994I and SN 2004aw have $E_k/M_{ej}$ ratios near 1 foe/M$_\odot$, but show broader spectral features than SN 2017ein or SN 2007gr. Using the classification system from Prentice & Mazzali (2017), both SN 1994I and SN 2004aw are defined as Type Ic–6 due to the blending of two of the three primary Fe ii lines while SN 2017ein is a Type Ic–7. For modelled SNe, as the classification increases from very blended Type Ic–3 to narrow lined Type Ic–7, the $E_k/M_{ej}$ ratio decreases. Based on this, the low $E_k/M_{ej}$ ratio found for SN 2017ein, which is the first SN Ic–7 to undergo this kind of analysis, fits in with the previous trend. The modelling of the nebular phase spectra also matches the model from the photospheric phase.

6.1.1 Scandium

From day 15 and onward, the region near 5500Å contains two features between the strong Fe ii and Na i lines. A similar pair of lines were seen in SN 2007gr and Valenti et al. (2008) suggested these are Sc ii lines but no abundance tomography model has been done for that event. Sc ii lines have been observed in Type II SNe, such as SN 1987a (Mazzali et al. 1992) and the line velocities of the 5527 and 6245 Å Sc ii lines were measured in the Type II SNe 2012A, 1999em, 2005cs and 2009bw, summarised in Tomasella et al. (2013) Millard et al. (1999) tentatively identified Sc ii in several spectra of SN1994I as well but Sauer et al. (2006) were unable to reproduce the identified Sc ii line without producing other unwanted spectral lines.

For the models in Fig. 7, a small mass of Sc is located between 8300 – 11000 km s$^{-1}$. These two features are best fit in the June 17th or June 21st spectra, (Fig. 7(e–f)). The addition of Sc ii produces a set of lines between 6000–7000 Å, but this is also combined with Fe ii, Si ii, and various other weaker features. The June 10th spectrum shows what may be the beginnings of the Sc ii lines, but the synthetic model has a weaker flux in this region. Increasing the Fe ii mass can cause re–emission of flux into this area, improving the flux level but can produce unwanted behaviour in other regions of the spectrum or for later spectra. The earlier spectra do not show strong evidence for Sc ii and the flux at the later epochs is fairly low. Increasing the mass of Sc ii at a higher velocity can reproduce both the two lines and re–emits flux towards the Na i D region, reducing the depth of that feature but producing much stronger features in this epoch and later epochs between 6000–7000 Å that are not observed. Sulphur can also produce the redder feature, but given the constraints on S/Si ratio from explosive nucleosynthesis (1/3 – 1/5), increasing the amount of sulphur to produce this line requires too much Si in the outer region. One can also use Cr to reproduce part of the bluer line, but the mass and location of the material needed in the model produces too many unobserved lines if the feature is solely formed from Cr, in addition to the lack of a physical origin for such high amounts of Cr.

6.1.2 Helium

Similar to other Type Ic SNe, SN 2017ein has been suggested to have some amount of He in the outer atmosphere. The synthetic model in Fig. 7 contains no He, and only Na is required to produce the feature at 5875Å with good success throughout all the synthetic spectra. The two weaker optical He i lines at 6678 and 7065 Å are not present or easily identifiable in any of the spectra and we have no NIR spectra to cover the stronger 10830 and 20581 Å lines. Due to these factors, we would have to solely rely on the He i 5875 line to determine if He is present in the model. As this feature is dominant in the same region in which the Na i D line is located, this is difficult. Hachinger et al. (2012) and Teffs et al. (2020b) found that up to 0.06–0.14 M$_\odot$ of He could be present before the optical and NIR He i lines are strong and easily identifiable, with a much lower amount of “hideable” He if only NIR lines are considered.

Figure 12 shows the four earliest epochs with a total $M_{He}$ $\sim$0.01 M$_\odot$ above a $v_{ph} >$ 9300 km s$^{-1}$. The addition of He to this model (blue line in Fig. 12) reproduces the primary optical He i line at 5875 Å to an adequate degree, but the lack of the weaker He i lines at 6678 and 7065 Å makes a single line fit hard to interpret as the model without He also matches the features adequately. Increasing the amount of He beyond the $\sim$0.01 M$_\odot$ can drastically strengthen the optical features beyond what is seen in the observed spectra. For SN 1994I, in which the 5875 Å region shows a stronger feature than in other Type Ic SNe, the possible signature of He ii is relatively weak and short lived. Models for SN 1994I with and without He can often reproduce the bulk behaviour, suggesting that if He is present in SN 1994I, and by relation SN 2017ein, the contribution from He would be mini-
eral, especially compared to He dominated features in Type Ib SNe. As concluded in Hachinger et al. (2012) and Teffs et al. (2020b), a combination of optical and NIR He I lines are needed to determine how much He is present in Type Ic SNe.

6.2 Progenitor Implications

The modelled values for the ejecta mass, explosion energy, and $^{56}$Ni mass in this work are similar to the approximate fits from either the pseudo-bolometric light curve or the multiband photometry, in Van Dyk et al. (2018). However, the estimated $M_{ej}$ from the progenitor masses found in Van Dyk et al. (2018); Kilpatrick et al. (2018); Xiang et al. (2019) show a significant disparity. The ejecta masses from both the single star or binary star masses are in the range of 4-8 $M_\odot$. Figure 13, derived from spectral models and summarised in more detail in Mazzali et al. (2017), shows that a correlation exists between $M_{ej}$ and $E_k$. Placing a SN with 4-8 $M_\odot$ and $E_k \sim 1 \times 10^{51}$ erg in this plane would result in a significant outlier compared with other modelled SN Ic. Taking that same $E_k$ and the $\sim 2 M_\odot$ ejecta mass found in this work, gives a point that does align with other objects.

The modelling of SN 2017ein in this work uses the abundance tomography method that has been used often for a wide variety of SE-SNe. This is a multi-variable approach to modelling SNe, and combined with photometric and nebular fits can produce a consistent model that reproduces both the photometry and the early and late time spectra within the limitations of the modelling framework. Recent work by Ashall & Mazzali (2020) focused on how changes in the model parameters, such as $v_{ph}$, $L_{ph}$, and $M_{ej}$ can alter a fitted synthetic spectrum and found that modelling both the photospheric and nebular phase spectra results in approximately 5–10% error bars for both the $E_k$ and $M_{ej}$. They also suggested that a well fitted spectrum seems to prefer a single combination of $L_{ph}$ and $v_{ph}$ with a synthetic spectrum deviating from the fit with a 5–10% change in either or both the $L_{ph}$ and $v_{ph}$.

Using the modelled ejecta mass of $1.5 \pm 0.4 M_\odot$, we can first consider the low mass (i.e. $M_{ZAMS} \leq 22 M_\odot$) models from Woosley et al. (1993, 1995); Woosley & Weaver (1995). The $M_{ZAMS}$ models that best reproduce a 1.2–2.1 $M_\odot$ CO core are those in the 16–20 $M_\odot$ range. These models are all a result of single star evolution. For the same model set, a $M_{ZAMS} > 35 M_\odot$ Wolf-Rayet stage star has mass loss that produces CO cores with a narrow final mass range of $\sim 2–4 M_\odot$. Pols & Dewi (2002) find a much higher CO core mass for the same mass range, as the resulting CO core masses are highly dependent on the Wolf-Rayet stage mass loss rates used (Yoon 2017).

If we consider that the progenitor is a He star that has evolved in a binary, such as those generated by Woosley (2019) and exploded in Ertl et al. (2020), we can find mass cases where its possible that the resulting He envelope can be lost. In particular, He stars of masses 3.5-5 $M_\odot$, reflecting a $M_{ZAMS}$ of 15-20 $M_\odot$, were found to have either a rapid He envelope expansion that could transfer mass or depending on the choice of mass loss rates, could lose their He envelopes through stellar winds. The CO core masses for this range (1.3-2.7 $M_\odot$) also matches the model derived in this work.
The explosion properties of these models in Ertl et al. (2020) are within the range of our modelled $E_k$ and synthesised $M_{NI}$ as well, but their $E_k$ and $M_{NI}$ relation is not well constrained due to approximations taken in the production of $^{56}$Ni. In addition, “off the shell” SNe models often do not replicate the spectra and photometry of observed SNe, so additional care should be taken.

As mentioned previously, the progenitor properties determined by Van Dyk et al. (2018); Kilpatrick et al. (2018); Xiang et al. (2019) suggests a massive star with an $M_{ZAMS}$ $\sim 60$–80 $M_\odot$, that with reasonable assumptions results in a 4–8 $M_\odot$ ejecta mass. This is at odds with the approximate modelling methods used in those works that find an $M_{ej}$ closer to 1–2 $M_\odot$. In addition, our modelling also favours a low $M_{ej}$ of 1.6 $\pm$ 0.4 $M_\odot$ as well. This is not the first time a contradiction between an estimated progenitor mass derived from pre-supernova imaging and modelling as arisen. The nebular phase of SN 2007gr was modelled by Mazzali et al. et al. (2009) to have $\sim$1 $M_\odot$ of ejecta below 5000 km s$^{-1}$ with an estimated explosion energy of 1 foe. Other estimates for SN 2007gr give an $M_{ej}$ of 2–3.5 $M_\odot$ by Valenti et al. (2008) and $\sim$1.2 $M_\odot$ from Drout et al. (2011), both with a similar energy range of $\sim$1 foe. These ejecta estimates favour a low mass progenitor, around 15–18 $M_\odot$ as well. Maund & Ramirez-Ruiz (2016) estimates a much higher progenitor mass of 40 $M_\odot$ by associating the progenitor with nearby stellar populations although with SN 2007gr, no object was detected in the pre-supernova images.

The pre-supernova imaging is limited to two Hubble images and Kilpatrick et al. (2018) and Xiang et al. (2019) show a slight offset in the position of the compact source and the supernova. While this offset is well within the error bounds in the methods used, a combination of this and the contradictory modelling results may suggest that the progenitor is instead a faint star within the line of sight of the compact source. Follow up Hubble imaging by other groups is planned and would determine if the compact source remains after SN 2017ein dims.

An alternative explanation is to assume that the progenitor star is a massive star or in a massive binary that matches the pre-supernova imaging and is stripped of all H/He resulting in 4–8 $M_\odot$ of ejecta at the point of collapse. At collapse, a significant fraction of this material forms a massive remnant with the explosion still ejecting 1-2 $M_\odot$ of material. This would allow both the modelling in this work and the pre-supernova imaging to be correct. The resulting remnant mass would be in the range of 2–6 $M_\odot$, which is in the range of observed black hole x-ray transients (Wiktorowicz et al. 2014) and within some theoretical ranges for massive stars, depending on mass loss and binary/single star evolution (Fryer et al. 2012). Van Dyk et al. (2018); Kilpatrick et al. (2018); Xiang et al. (2019) all consider both binary/single star evolution as a possible candidate. This explanation is partially fine tuned, as it arbitrarily requires a particular black hole mass to form at collapse for both results to work together.

### 6.3 $^{56}$Ni Mass

Approximately $\sim$0.1 $M_\odot$ of $^{56}$Ni was required in the photospheric models with 0.08 $M_\odot$ required in the nebular model. Given the estimated error in both the observational data and the modelling, a difference of 0.02 $M_\odot$ is reasonable. Other SNe modelled using a combination of both photospheric and spectral methods show a soft correlation between $^{56}$Ni mass and $E_k$ with lower $^{56}$Ni masses favouring lower ejecta masses (Mazzali et al. 2017). $^{56}$Ni masses found from photometric methods typically find similar results (Drout et al. 2011; Lyman et al. 2016; Prentice et al. 2019). The most notable of these is SN 1994I, discussed previously, which is estimated to have a similar $M_{ej}$ of 1-2 $M_\odot$, an $E_k$ of $\sim$1 foe, and $^{56}$Ni mass of $\sim$0.07 $M_\odot$, with some dependence on the reddening assumed.

If we compare the photometry and spectra of SN 2007gr to that of SN 2017ein, we find similarities at both early and late epochs, excluding the latetime drop in the $r$-band. Mazzali et al. (2009) used the nebular phase spectra of SN 2007gr and estimated a total $M_{ej}$ of 1–1.5 $M_\odot$. Several other estimates for SN 2007gr are summarised in Van Dyk et al. (2018) but Drout et al. (2011) uses a multiband fit and gets a similar mass and an $E_k$ $<1$ foe which results in an $E_k/M_{ej}$ ratio less than 1, similar to what we have found for SN 2017ein, which explains the similarity in spectra. This similarity allows us to approximate the NIR contribution of SN 2017ein in the total observed flux. The addition of this flux increases the peak luminosity by approximately 10–20%. This requires a slight increase in $^{56}$Ni mass in the explosion model, from 0.08 to 0.1 $M_\odot$, slightly different from the nebular model. The light curve from the synthetic model was still too bright, but falls within the observational error estimates and the 5-10% missing UV flux not considered in the other light curves.

### 6.4 Late Time Nebular and Photometry

We note in Section 3 and in Fig 2 that the late time photometry at $\sim$200 days after $t_{exp}$ shows a larger magnitude drop in the $r$, $i$, and $z$-bands post 150 days, than in the $g$-band. This additional drop results in the bolometric light curve not following a linear decay as seen in other $^{56}$Ni powered SNe (Fig. 3).

As mentioned in Section 5.8, the first nebular spectrum model can be powered by a similar mass of $^{56}$Ni to that of the early light curve, but the next two phases show a drop in flux that is inconsistent with the initial model unless a multiplicative factor is included to the total flux. In the next few subsections we discuss possible explanations to explain this drop.

#### 6.4.1 Fallback

The reduction of overall flux seen in the nebular model can be explained by removing mass from the model between the first and final nebular phase epochs. This reduction in mass results in less material being heated and therefore less overall flux for the entire wavelength range. Using accretion as a primary energy source is often used to explain super luminous events with broad early light curves, of which SN 2017ein has neither. If we consider the semi-analytic model for accretion powered SNe found in Dexter & Kasen (2015), we can assign

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3 Note, it is currently suspected that the use of ‘Arnett’s rule’ for SE-SNe may lead to a $\sim$50% overestimate in $M_{NI}$ (e.g., Woosley et al. 2020).
the luminosity from accretion to only an arbitrary fraction of the total luminosity, with the majority of the luminosity from a $^{56}\text{Ni}$ decay model. A fit in this manner would see any fallback that occurs soon after the explosion be of low mass, low accretion rate, or have a very low efficiency of energy transfer; all of which would only be needed to add to the total luminosity 100 days after peak. Given the 100 days of missing data, a fit of this nature is arbitrary and fine tuned.

The other alternative is that the fallback only occurs at some late time ($t > 50$ days). This may be induced through late time CSM interaction which produces a strong enough reverse shock to cause the innermost material to fallback to the remnant (Dexter & Kasen 2013) or some other dense enough material. If this did occur, the material would have had to been ejected many years prior to the collapse for it to be at such a distance from the star. However, there is no evidence of any CSM interaction in the spectra nor the light curve, unless it occurred in the 100 days when the event was behind the sun, but this would be an unlikely convenience.

6.4.2 Secondary Energy Sources

As mentioned in Section 6.4.1, late time CSM interaction could generate fallback and is thought to be a common energy source for superluminous SNe or those with long lasting light curves. The typical conditions used to suggest CSM interaction are not found in either the light curve or the spectra. Given the drop in bolometric flux at day 150, the interaction phase would need to occur and stop during the 100 days the SN was not observed, and the drop we see is the fall of the light curve towards a $^{56}\text{Ni}$ decay curve.

A magnetar as a primary or secondary energy source is invoked when the $^{56}\text{Ni}$ mass required is too high or the light curve is broad and long lasting. Both our light curve code and semi-analytic models for $^{56}\text{Ni}$ decay as a primary energy source reproduce the early phase quite well without requiring significant amounts of synthesised $^{56}\text{Ni}$. Given that only the late time ($t > 140$ d) shows deviation from a typical $^{56}\text{Ni}$ decay model, a magnetar model would have to only show evidence in this late phase, or have a turnover point close to day 140 which is difficult to explain.

6.4.3 Time Dependent Gamma-ray Opacity

Allowing for a time dependant $\gamma$-ray opacity can reduce the total flux of the later two epochs that matches the multiplicative factor. This would also alter the bolometric light curve as less flux is trapped. However, we know of no mechanism that can arbitrarily change the $\gamma$-ray opacity over the time span of a month.

7 CONCLUSIONS

In this work, we model the light curve and the photospheric and nebular phase spectra to find a self consistent model for SN 2017ein. This model has an $M_{\text{ej}}$ of 1.6 $\pm$ 0.4 $M_\odot$, an $E_k$ of 0.9 $\pm$ 0.2 foe, and a $M_{\text{Ni}}$ of 0.09 $\pm$ 0.02 $M_\odot$. These parameters are required to reproduce the narrow lined spectra and compare favourably to a progenitor mass of 16–20 $M_\odot$. The drop in the late time photometry and nebular flux is unexplained using our models, but the lack of spectroscopic data at $\lambda > 8000$ Å, combined with the fading brightness of the object at late times makes the mechanism responsible for these deviations hard to determine. Common mechanisms that are often invoked to explain peculiar light curves do not seem to apply in this case, barring very exotic situations.

Deriving a progenitor mass from the pre-supernova imaging results in an estimated mass in the 40–80 $M_\odot$ range, depending on a single or binary star evolution or a compact cluster. Under reasonable assumptions for mass loss and evolution, this $M_{\text{ZAMS}}$ results in an $M_{\text{ej}}$ of 4–8 $M_\odot$. This is a strong contradiction between the modelled results and the observed estimations.

The evidence from the SN itself favours the model properties found in this work. As the progenitor and ejecta mass increase, the required binding energy that results in a successful explosion typically increases. The narrow lines and measured line velocities do not favour high energy models. High mass events also typically have broader light curves, which SN 2017ein also does not show. Similarly, as the $E_k$ and $M_{\text{ej}}$ increases, the $^{56}\text{Ni}$ mass synthesised typically increases. The $^{56}\text{Ni}$ mass in this work does not match that of high energy and mass events. These results are all contradictory if one assumes a massive progenitor and a resulting large $M_{\text{ej}}$.

The pre-supernova observations show a slight offset in the supernova position and that of the point source. This offset is not significant, but combined with the contradictory results regarding explosion properties suggests the likely chance that the progenitor is not associated with the point like source and is a faint object within the line of sight. Exotic situations, such as a massive remnant with a low mass ejecta could link the two results, but is a fine tuned mechanism with weak explanation. Further Hubble imaging after the SN 2017ein fades will hopefully solve this problem.

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DATA AVAILABILITY

Data will be made available on the Weizmann Interactive Supernova Data Repository (WISEREP) at https://wiserep.weizmann.ac.il/.

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