Machine learning in physics: The pitfalls of poisoned training sets

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Known for their ability to identify hidden patterns in data, artificial neural networks are among the most powerful machine learning tools. Most notably, neural networks have played a central role in identifying states of matter and phase transitions across condensed matter physics. To date, most studies have focused on systems where different phases of matter and their phase transitions are known, and thus the performance of neural networks is well controlled. While neural networks present an exciting new tool to detect new phases of matter, here we demonstrate that when the training sets are poisoned (i.e., poor training data or mislabeled data) it is easy for neural networks to make misleading predictions.

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I. INTRODUCTION

Machine learning methods [1–3] have found applications in condensed matter physics detecting phases of matter and transitions between these on both quantum and classical systems (see, for example, Refs. [4–9]). Different approaches exist, such as lasso [10, 11], sparse regression [12, 13], classification and regression trees [14–16], as well as boosting and support vector machines [17–21]. Neural networks [22, 23] are the most versatile and powerful tools, which is why they are commonly used in scientific applications.

Convolutional neural networks (CNNs), in particular, are specialized neural networks for processing data with a grid-like topology. Familiar examples include time-series data, where samples are taken in intervals, and images (two-dimensional data sets). The primary difference between neural networks and convolutional neural networks lies in how hidden layers are managed. In CNNs, a convolution is applied to divide the feature space into smaller sections emphasizing local trends. Because of this, CNNs are ideally-suited to study physical models on hypercubic lattices. Recently, it was demonstrated that CNNs can be applied to the detection of phase transitions in Edwards-Anderson Ising spin glasses on cubic lattices [24]. It was shown that the critical behavior of a spin glass with bimodal disorder can be inferred by training the model using data that has Gaussian interactions between the spins. The use of CNNs also results in a reduced numerical effort, which means one could potentially access larger system sizes often needed to overcome corrections to scaling in numerical studies. As such, pairing specialized hardware to simulate Ising systems [25–27] with machine learning techniques might one day elucidate properties of spin glasses and related systems. However, as we show in this work, the use of poor input data can result in erroneous or even unphysical results. This (here inadvertent) poisoning of the training set is well known in computer science where small amounts of bad data can strongly affect the performance of neural networks. For example, Steinhardt et al. [28] demonstrated that already small amounts of bad data can result in a sizable drop in the classification accuracy. References [29–31] furthermore demonstrate that data poisoning can have a strong effect in machine learning. Reference [32] focuses on adversarial manipulations [33, 34] of simulational and experimental data in condensed matter physics applications. In particular, they show that changing individual variables (e.g., a pixel in a data set) can generate misleading predictions. This suggests that results from machine learning algorithms sensitively rely on the quality of the training input.

In this work, we demonstrate that the use of poorly-thermalized Monte Carlo data or simply mislabeled data can result in erroneous estimates of the critical temperatures of Ising spin-glass systems. As such, we focus less on adversarial cases, but more on accidental cases of poor data preparation. We train a CNN with data from a Gaussian Ising spin glass in three space dimensions and then use data generated for a bimodal Ising spin glass to predict the transition temperature of the same model system, albeit with different disorder. In addition, going beyond the work presented in Ref. [32], we introduce an analysis pipeline that allows for the precise determination of the critical temperature. While good data results in a relatively accurate prediction, the use of poorly-thermalized or mislabeled data produce misleading results. This should serve as a cautionary tale when using machine learning techniques for physics applications.

The paper is structured as follows. In Sec. II we introduce the model used in the study, as well as simulation parameters for both training and prediction data. In addition, we outline the implementation of the CNN as well as the approach used to extract the thermodynamic critical temperature, followed by results and concluding remarks.

II. MODEL AND NUMERICAL DETAILS

To illustrate the effects of poisoned training sets we study the three-dimensional Edwards-Anderson Ising spin glass [35, 39] with a neural network implemented in TensorFlow [40]. The model is described by the Hamiltonian

$$\mathcal{H} = - \sum_{(i,j)} J_{ij}s_is_j,$$

where each $J_{ij}$ is a random variable drawn from a given symmetric probability distribution (either bimodal and Gaussian),
\( s_i = \pm 1 \) represent Ising spins, and the sum is over nearest neighbors on a cubic lattice with \( N \) sites.

Because spin glasses do not exhibit spatial order below the spin-glass transition, we measure the site-dependent spin overlap

\[
q_i = S_i^\alpha S_i^\beta ,
\]

between replicas \( \alpha \) and \( \beta \). In the overlap space, the system is reminiscent of an Ising ferromagnet, i.e., approaches for ferromagnetic systems introduced in Refs. [6, 2] can be used. For low temperatures, \( q = (1/N) \sum_i q_i \to 1 \), whereas for \( T \to \infty, q \to 0 \). For an infinite system, \( q \) abruptly drops to zero at the critical temperature \( T_c \). Therefore, the overlap space is well suited to detect the existence of a phase transition in a disordered system, even beyond spin glasses.

\section*{A. Data generation}

We use parallel tempering Monte Carlo [41] to generate configurational overlaps. Details about the parameters used in the Monte Carlo simulations are listed in Tab. I for the training data with Gaussian disorder. The parameters for the prediction data with bimodal disorder are listed in Tab. II.

\begin{table}[h]
\centering
\begin{tabular}{ccccccc}
\hline
\( L \) & \( N_{sa} \) & \( N_{sw} \) & \( T_{min} \) & \( T_{max} \) & \( N_T \) & \( N_{con} \) \\
\hline
8 & 20000 & 500000 & 0.80 & 1.21 & 20 & 100 \\
10 & 10000 & 400000 & 0.80 & 1.21 & 20 & 100 \\
12 & 20000 & 655360 & 0.80 & 1.21 & 20 & 100 \\
14 & 10000 & 1048576 & 0.80 & 1.21 & 20 & 100 \\
16 & 5000 & 1048576 & 0.80 & 1.21 & 20 & 100 \\
\hline
\end{tabular}
\caption{Parameters for the training samples with Gaussian disorder. \( L \) is the linear size of a system with \( N = L^3 \) spins, \( N_{sa} \) is the number of samples, \( N_{sw} \) is the number of Monte Carlo sweeps for each of the replicas for a single sample, \( T_{min} \) and \( T_{max} \) are the lowest and highest temperatures simulated, \( N_T \) is the number of temperatures used in the parallel tempering Monte Carlo method for each system size \( L \), and \( N_{con} \) is the number of configurational overlaps for a given temperature in each instance.}
\end{table}

\begin{table}[h]
\centering
\begin{tabular}{ccccccc}
\hline
\( L \) & \( N_{sa} \) & \( N_{sw} \) & \( T_{min} \) & \( T_{max} \) & \( N_T \) & \( N_{con} \) \\
\hline
8 & 15000 & 80000 & 1.05 & 1.25 & 12 & 500 \\
10 & 10000 & 300000 & 1.05 & 1.25 & 12 & 500 \\
12 & 4000 & 300000 & 1.05 & 1.25 & 12 & 500 \\
14 & 4000 & 1280000 & 1.05 & 1.25 & 12 & 500 \\
16 & 4000 & 1280000 & 1.05 & 1.25 & 12 & 500 \\
\hline
\end{tabular}
\caption{Parameter for the prediction samples with bimodal disorder. \( L \) is the linear size of the system, \( N_{sa} \) is the number of samples, \( N_{sw} \) is the number of Monte Carlo sweeps for each of the replicas of a single sample, \( T_{min} \) and \( T_{max} \) are the lowest and highest temperatures simulated, \( N_T \) is the temperature numbers used in parallel tempering method for each linear system size \( L \), and \( N_{con} \) is the number of configurational overlaps for a given temperature in each instance.}
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\section*{B. CNN implementation}

We use the same amount of instances used in Ref. [42] with 100 configurational overlaps at each temperature for each instance. Because the transition temperature with Gaussian disorder is \( T_c \approx 0.95 \) [42–44], following Refs. [6, 8, 45] for the training data, we label the convolutional overlaps with temperatures above 0.95 as "1" and those from temperatures below 0.95 as "0."

The parameters for the architecture of the convolutional neural network are listed in Tab. III We inherit the structure with a single layer from Ref. [8]. All the parameters are determined by extra validation sample sets, which are also generated from Monte Carlo simulations.

\begin{table}[h]
\centering
\begin{tabular}{ccccccc}
\hline
Number of Layers & 1 & Channels in each layer & 5 & Filler size & \( 3 \times 3 \times 3 \) & stride & 2 \\
Activation function & ReLU & Optimizer & AdamOptimizer(10\(^{-4}\)) & Batch size & \( 10^8 \) & Iteration & \( 10^8 \) \\
Software & TensorFlow (Python) & Hardware & Lenovo x86 HPC cluster with a dual-GPU NVIDIA Tesla K80 GPU and 128 GB RAM \\
\hline
\end{tabular}
\caption{CNN architecture, parameters, and hardware details.}
\end{table}

Note that we use between 4000 and 10000 disorder instances for the bimodal prediction data, which is approximately 1/3 of the numerical effort needed when estimating the phase transition directly via a finite-scaling analysis of Monte Carlo data, as done for example in Ref. [42]. As such, pairing high-quality Monte Carlo simulations with machine learning techniques can result in large computational cost savings.

\section*{C. Data analysis}

Because the configurational overlaps [Eq. (2)] include the information about phases, we expect that different phases have different overlap patterns similar to grid-like graphs. Therefore, in the region of a specific phase, it is reasonable to expect that the classification probability for the CNN to identify the phase correctly should be larger than 50\%. As such, it can be expected that when the classification probability is 0.5, the system is at the system-size-dependent critical temperature. A thermodynamic estimate can then obtained via the finite-size scaling method presented below.

Let us define the classification probability as a function of temperature and system size: \( p(T, L) \) which can be used as a dimensionless quantity to describe the critical behavior. From the scaling hypothesis, we expect \( p(T, L) \) to have the following behavior in the vicinity of the critical temperature \( T_c \):

\[
\langle p(T,L) \rangle = \tilde{F} \left[ L^{1/\nu_{\text{int}}} \left( T - T_c \right) \right],
\]

where \( \nu_{\text{int}} \) is the internal correlation length critical exponent.
where the average is over disorder realizations. Note that the critical exponent \( \nu_{\text{ml}} \) is different from the one calculated using physical quantities. Due to the limited system sizes that we have studied, finite-size scaling must be used to reliably calculate the critical parameters at the thermodynamic limit. Assuming that we are close enough to the critical temperature \( T_c \), the scaling function \( \tilde{F} \) in Eq. (3) can be expanded to a third-order polynomial in \( x = L^{1/\nu_{\text{ml}}} (T - T_c) \).

\[
\langle p(T, L) \rangle \sim p_0 + p_1 x + p_2 x^2 + p_3 x^3. \tag{4}
\]

First, we evaluate \( \nu_{\text{ml}} \) by noting that to the leading order in \( x \), the derivative of \( \langle p(T, L) \rangle \) in Eq. (4) with respect to temperature has the following form:

\[
\frac{d\langle p(T, L) \rangle}{dT} \sim L^{1/\nu_{\text{ml}}} \left[ p_1 + 2p_2L^{1/\nu_{\text{ml}}} (T - T_c) + 3p_3L^{2/\nu_{\text{ml}}} (T - T_c)^2 \right]. \tag{5}
\]

Therefore, the extremum point of \( \frac{d\langle p(T, L) \rangle}{dT} \) scales as

\[
\frac{d\langle p(T, L) \rangle}{dT} \bigg|_{T = T_c^*} \sim L^{1/\nu_{\text{ml}}}. \tag{6}
\]

A linear fit in a double-logarithmic scale then produces the value of \( \nu_{\text{ml}} \) (slope of the straight line), which is subsequently used to estimate \( T_c \). To do so, we turn back to Eq. (4) where we realize that the coefficient of the linear term in \( L^{1/\nu_{\text{ml}}} \) is the independent variable. The vertical dashed line shows the temperature where the slope vanishes, which corresponds to \( T_c \). (d) Finite-size scaling of the data using the previously-estimated value of \( \nu_{\text{ml}} \) and \( T_c \). The data collapse onto a universal curve indicating that the estimates are accurate.

FIG. 1: Classification probabilities for different linear system sizes \( L \) as a function of temperature \( T \) for the prediction of the critical temperature of the bimodal Ising spin glass via a CNN trained with data from a Gaussian distribution. (a) Prediction probability for different system sizes \( L \) near the phase transition temperature. The different data sets cross at \( T_c = 1.122 \). (b) Measurement of \( \nu_{\text{ml}} \) by performing a linear fit in a double-logarithmic scale using the extremum points of the derivative of the prediction error with respect to the temperature. (c) Estimate of the critical temperature \( T_c \) using the coefficient of the linear term in Eq. (4) (normalized to 1) with \( L^{1/\nu_{\text{ml}}} \) as the independent variable. The vertical dashed line shows the temperature where the slope vanishes, which corresponds to \( T_c \). (d) Finite-size scaling of the data using the previously-estimated value of \( \nu_{\text{ml}} \) and \( T_c \). The data collapse onto a universal curve indicating that the estimates are accurate.

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FIG. 2: Classification probabilities for different system sizes \( L \) for an Ising spin glass with bimodal disorder. 1% of the labels have been mixed on average. There is no clear sign of the transition.

III. RESULTS USING DATA WITHOUT POISONING

Figure 1 shows results from the CNN trained with well-prepared (thermalized) data from a Gaussian distribution, predicting the phase transition of data from a Bimodal disorder distribution. Figure 1(a) shows the prediction probabilities for different linear system sizes \( L \) as a function of temperature \( T \). The curves cross in good agreement with previous estimates (see, for example, Ref. [42]). Finally, in Fig. 1(d), the data points are plotted as a function of the reduced variable \( x = L^{1/\nu_{\text{ml}}} (T - T_c) \) using the estimated values of the critical parameters. The universality of the scaling curve underlines the accuracy of the estimates.

IV. RESULTS USING POISONED TRAINING SETS

Although we have shown that the prediction from convolutional neural network can be precise, we still need to test how
poisoned data sets impact the final prediction. First, we randomly mix the classification labels of the training sample with a probability of 1%, i.e., with a training set of 100 samples, this means only one mislabeled sample on average. Then we train the network and use the same samples in the prediction stage. Compared to Fig. [1] Figure [2] shows no clear sign of a phase transition. This means that mislabeling a very small portion of the training data can strongly affect the outcome. Given the hierarchical structure of CNNs, errors can easily be amplified in propagation [46][47], which is a possible explanation of the observed behavior.

V. DISCUSSION

We have studied the effects of poisoned data sets when training CNNs to detect phase transitions in physical systems. Our results show that good training sets are a necessary requirement for good predictions. Small perturbations in the training set can lead to misleading results.

We do note, however, that we might not have selected the best parameters for the CNN. Using cross-validation or bootstrapping might allow for a better tuning of the parameters and thus improve the quality of the predictions. Furthermore, due to the large number of predictors, overfitting is possible. This, however, can be alleviated by the introduction of penalty terms. Finally, the use of other activation functions and optimizers can also impact the results. This, together with the sensitivity towards the quality of the training data that we find in this work suggest that machine learning techniques should be used with caution in physics applications. Garbage in, garbage out . . .

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Figure 3 shows the prediction results using data with only non-equilibrium labels were mixed, a transition cannot be clearly identified. This is strong indication that the training data need to be carefully prepared.

We have also studied the effects of poorly-thermalized prediction data paired with well-thermalized training data (not shown). In this case, the impacts on the prediction probabilities are small but not negligible.

Finally, we test the effects of poorly prepared training data—in this case, the training data are not properly thermalized. Figure 3 shows the prediction results using data with only 50% of the Monte Carlo sweeps needed for thermalization of the Gaussian training samples. Although 50% might seem extreme at first sight, it is important to emphasize that thermalization times (as well as time-to-solution) are typically distributed according to fat-tail distributions [48]. In general, users perform at least a factor 2 of additional thermalization to ensure most instances are in thermal equilibrium. As in the case where the labels were mixed, a transition cannot be clearly identified. This is strong indication that the training data need to be carefully prepared.

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FIG. 3: Classification probabilities for different system sizes $L$ for an Ising spin glass with bimodal disorder. The Gaussian training data are not thermalized. There is no clear sign of a phase transition.

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