Electroweak Symmetry Breaking from SUSY Breaking with Bosonic See-Saw Mechanism

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We introduce the idea of bosonic see-saw mechanism in analogy with the see-saw mechanism. Bosonic see-saw is a new symmetry breaking mechanism and we apply it to explain electroweak symmetry breaking as an inevitable consequence of supersymmetry breaking. The breaking of electroweak symmetry occurs at tree level once supersymmetry is broken. Absence of color/charge breaking in this model is related to doublet-triplet splitting in grand unified theory. An extension of MSSM with a weak triplet shows very interesting results especially when \( \mu = 0 \). It provides the most natural understanding of why we have only electroweak symmetry breaking rather than having color/charge breaking. In the limit \( \mu = 0 \), the model predicts very light chargino mass, 104 GeV while Higgs is heavy, 130 GeV.

The standard model(SM) has a beautiful structure of explaining all the matters and forces except gravity in terms of quark/lepton(s) and gauge interactions. All the quarks and leptons are massless as long as electroweak symmetry is unbroken, and they can get mass from Yukawa interactions only after electroweak symmetry breaking. Within the framework of the standard model, Higgs potential can be arbitrary and we choose the sign of the coefficient of quadratic (quartic) term to be negative (positive) such that the Higgs potential has a desired mexican hat shape. It would not be easy to understand why the quadratic term has a negative sign while the quartic term is positive within the standard model.

The SM is just regarded as a low energy effective theory of some extended one and gauge hierarchy problem suggests a modification of the standard model at TeV scale. Supersymmetry(SUSY) \( \widetilde{\frac{\text{Higgs}}{\text{quarks and leptons}}} \) is one of the most promising candidates for it. In supersymmetric extensions of the standard model, we can get a better understanding of the electroweak symmetry breaking. First of all, the Higgs potential is no longer arbitrary and should be a sum of supersymmetric F/D terms and soft supersymmetry breaking terms. The quartic term is calculated from gauge couplings and is positive definite. The quadratic term (soft terms) is a sum of supersymmetric mass term (\( \mu \) term) and soft supersymmetry breaking terms which are calculable in certain mediation mechanism of supersymmetry breaking. In the minimal supersymmetric standard model(MSSM) with gauge mediated SUSY breaking \( \widetilde{\frac{\text{R}}{\text{F}}} \), a radiative correction by large top Yukawa coupling gives negative Higgs mass squared. If \( \mu \) were zero, the above picture might have been beautiful and could be considered as a possible explanation of the electroweak symmetry breaking. However, in reality, the electroweak symmetry breaking is a surprising cancellation of \( \mu^2 \sim (500 \text{ GeV})^2 \) and the Higgs soft scalar mass squared \( m_{H_0}^2 \). If \( \mu \) were slightly larger, we would never have the electroweak symmetry breaking. And if \( \mu \) were slightly smaller, the Higgs would develop its vacuum expectation value (VEV) exponentially larger than the weak scale. Thus it is desirable to consider models in which the weak scale electroweak symmetry breaking can be explained for a broad range of parameters.

In this paper we first introduce a simple idea called ‘bosonic see-saw mechanism’. We apply ‘bosonic see-saw mechanism’ to explain the electroweak symmetry breaking. When down type Higgs couples to the extra vector-like pair of Higgs, we can soften the little hierarchy problem. Finally we consider a model in which the electroweak symmetry is closely tied up to the supersymmetry

Let us briefly discuss the conventional see-saw mechanism explaining the lightness of neutrino masses \( \widetilde{\frac{\text{Higgs}}{\text{neutrinos}}} \). For \( \nu \), the left-handed neutrino which is an \( SU(2)_L \) doublet, and \( N \), a singlet, the possible interactions are

\[
\mathcal{L}_\nu = -M_{NN} + l_i H L_{N} + \text{h.c.},
\]

where \( H = (H^+, H^0) \) is the Higgs doublet and \( L = (\nu, l^-) \). After the electroweak symmetry breaking, it becomes

\[
M_{\nu} \left( \begin{array}{c} \nu \\ N \end{array} \right) = \frac{1}{2} \left( \begin{array}{c} 0 \\ m_D \\ M \end{array} \right) \left( \begin{array}{c} \nu \\ N \end{array} \right).
\]

where \( m_D = l_\nu(H^0) \). The lightest neutrino mass for \( m_D \ll M \) is then

\[
m_{\nu} = -\frac{m_D^2}{M}.
\]

Note the sign of the lighter eigenvalue. As the determinant of the matrix is negative definite (\(-m_D^2\)) and the heavier one is nearly \( M \), the lighter eigenvalue is negative definite. The result is valid as long as \( m_D \ll M \). We can
make the mass term to be positive definite by the field redefinition of neutrinos. Therefore, this observation is not important for neutrinos (fermions) but it will turn out to be very important for later consideration.

Bosonic see-saw mechanism works for bosons instead of fermions (neutrinos). Although the mechanism works for any scalar fields (superfields), here we take Higgs as an example for a clear illustration. Supersymmetric extension of the standard model requires two Higgs chiral superfields $H_u$ and $H_d$. Suppose there is an additional massive pair $H_u'$ and $H_d'$, the electroweak doublets with the opposite hypercharge. Let $X = \cdots + F_X \theta^2$ be a superfield representing supersymmetry breaking $F = \langle F_X \rangle \neq 0$. For the superpotential

$$W = l_1 X H_u' H_d + M H_u' H_d',$$

the scalar mass squared matrix for $H_d, H_u'$ is

$$M^2 = \begin{pmatrix} 0 & l_1 F^* \\ l_1 F & |M|^2 \end{pmatrix}. \quad (5)$$

When $\sqrt{F} \ll M$, the lightest scalar mass squared becomes negative definite,

$$m_{H_d}^2 = -\left| l_1 F \right|^2 \cdot |M|^2.$$

Whenever $F \neq 0$, the mass squared is negative and we end up with symmetry breaking. Therefore, at tree level, we obtain the electroweak symmetry breaking as a consequence of supersymmetry breaking. We can do the same thing to $H_u$ instead of $H_d$. Note that the sign here is physical as the matrix is for scalar mass squared. It is called 'bosonic see-saw mechanism' as it is opposed to usual see-saw mechanism which works for the fermions.

The bosonic see-saw mechanism shows a similarity to the (fermionic) see-saw mechanism.

- There are heavy states. (heavy Higgs v.s. $N$)
- There are interactions between heavy and massless states. ($H_u'$ and $H_d$ v.s. $\nu$ and $N$)
- Off-diagonal elements are generated if fields get VEVs. ($X = \langle F_X \rangle \neq 0$ v.s. $H \rightarrow \langle H^0 \rangle \neq 0$)

The crucial difference is the negative sign of bosonic see-saw mechanism which can not be eliminated by rephasing scalar fields. In general, $\langle X \rangle \neq 0$ and we can redefine fields and couplings such that $\bar{X} = X - \langle X \rangle$ does not have a scalar VEV ($\langle \bar{X} \rangle = 0$). Then we obtain more general superpotential,

$$W = l_1 X H_u' H_d + l_2 X H_u H_d' + M H_u' H_d'. \quad (6)$$

Now Yukawa couplings are

$$W = l_u H_u \bar{Q} u^c + l_d H_d \bar{Q} d^c + l'_u H_u' \bar{Q} u^c. \quad (7)$$

From now on, we focus on the application of bosonic see-saw mechanism to the electroweak symmetry breaking. As we have two Higgs fields $H_u$ and $H_d$ in MSSM, there are three possibilities. First, $H_u$ couples to heavy Higgs. Second, $H_d$ couples to it. Finally, both of them couple to it. When there is no radiative correction, the first option looks the most natural. However, we know that top Yukawa gives large radiative corrections and the second option is the best. If both of them couple to heavy Higgs and $X$, we can not make them light and the third option does not work. Thus we consider only the second possibility in this paper.

As $H'_u$ and $H'_d$ couple to $X$ directly, they are the messengers of SUSY breaking and $M$ is the messenger scale. We can calculate soft terms mediated by gauge interactions. We also assume that there is a pair of color triplet Higgs fields which complete the messenger fields into $SU(5)$ multiplets. The soft terms from gauge mediation are positive definite [9].

$$m_{\Phi}^2 = \sum_i 2c_i \left( \frac{\alpha_i}{4\pi} \right)^2 \Lambda^2. \quad (8)$$

where $\Lambda = |l_2 F / M|$ and $c_i$ is the quadratic Casimir of $i$-th gauge group. Note that $l_1 \sim 10^{-2} l_2$ is required to have $\Lambda \sim 10$ TeV while $m_{\Phi}^2 \sim 100$ GeV. Till now the only difference with the usual MSSM is the tree level contribution from bosonic see-saw which is negative definite.

The most interesting consequence comes with the addition of the electroweak triplet $\Sigma$. Let us explain why we need $\Sigma$ and how it brings an interesting result. In MSSM, the nice mechanism of radiative electroweak symmetry breaking is spoiled by large $\mu$ term. Large $\mu$ term in MSSM is due to the fact that we have not seen Higgs yet. In MSSM, the quartic couplings are given by gauge couplings and Higgs mass is predicted to be light. $m_H^2 > 114$ GeV requires a large radiative correction and it is possible only with heavy stop. If stop is heavy, radiative corrections are too large and the electroweak symmetry breaking becomes large unless large $\mu$ term cancels it. The lightness of Higgs mass in MSSM is mainly due to the small quartic terms from gauge interactions and it can be relaxed if there are additional quartic couplings in the theory in addition to the usual D-term. Thus we consider the modification of MSSM to give the additional quartic terms.

The most transparent application of the bosonic see-saw mechanism comes out if $\mu = 0$. However, the limit $\mu = 0$ in MSSM poses several problems [10].

- Peccei-Quinn(PQ) symmetry and R symmetry
  As Higgs fields carry PQ and R charge and the symmetry is exact in the limit $\mu = 0$, once they get VEVs, there appears a massless Goldstone boson which is in conflict with experiments.

- Electroweak symmetry breaking
If $H_u$ gets a VEV from negative $m^2_{H_u}$, $H_d$ gets its VEV through $B_H\mu$ term. Therefore, if $\mu = 0$ ($B_H = 0$), the down-type quarks and charged leptons cannot get their masses.

- **Chargino mass**
  
  If $\mu = 0$, higgsino can get their mass only by the electroweak symmetry breaking and the lightest chargino mass is always lighter than $M_Z$ which cannot be compatible with the current bound on the lightest chargino mass, 104 GeV.

  These problems can be solved if extra fields are introduced. In NMSSM, an extra singlet replaces $\mu$ term. The singlet gets a VEV and it generates $\mu$ term effectively. Then the electroweak symmetry breaking is a fine tuning just as in MSSM. An alternative way is to introduce an extra weak triplet $\Sigma$ with no hypercharge.

  Then the electroweak symmetry breaking is a fine tuning of $\Sigma$ gets a VEV and it generates $\mu$ as the new sources for it.

  Let us consider another interesting limit $\mu = 0$ ($\mu$-less SSM), we can forbid $\mu$ term by a discrete symmetry, so called 'U parity', which is a $Z_2$ subgroup of Peccei-Quinn symmetry. Under the U parity,

  $$(H_u, u^c, \Sigma) \rightarrow - (H_u, u^c, \Sigma).$$

  The most general superpotential consistent with the U parity is

  $$W = \frac{M_\Sigma}{2} \text{tr} \Sigma^2 + l_{\Sigma_1} H_u \Sigma H_d + l_{\Sigma_2} H_u \Sigma H_d'$$

  These terms are enough to break PQ and R symmetry. At the same time chargino mass can be heavier than $M_Z$ as we have new sources for it.

  Soft supersymmetry breaking terms are

  $$V_{\text{soft}} = m^2_{H_u} |H_u|^2 + m^2_{H_d} |H_d|^2 + m^2_{\Sigma} \text{tr} \Sigma^2 + M_{\Sigma} H_u \Sigma H_d + BM_{\Sigma} \text{tr} \Sigma^2 + \text{h.c.}$$

  The neutral component of $\Sigma$ gets a VEV once $H_u$ and $H_d$ get VEVs,

  $$v_{\Sigma} = \frac{l_{\Sigma_1} M_{\Sigma}}{m^2_{\Sigma} + M^2_{\Sigma} + B_{\Sigma} M_{\Sigma} + \frac{1}{2} l_{\Sigma_2}^2 v^2}.$$  \hspace{1cm} (11)

  $v_{\Sigma} < 9$ GeV is obtained if $m_{\Sigma}$ is larger than the electroweak scale.

  Let us go back to the calculation of soft terms. As our messenger fields have direct couplings with matter/Higgs fields, there are additional contributions. The Yukawa mediated ones are calculated using the formalism of analytic continuation into superspace.

  $$\Delta m^2_{H_u} = \left[ \frac{3 \alpha_{\Sigma_2}^2}{4 \pi^2} + \frac{\alpha_{\Sigma_2} \alpha_{l_2}}{4 \pi^2} \right] \Lambda^2$$

  $$\Delta m^2_{H_d} = \left[ - \frac{\alpha_{\Sigma_2} \alpha_{l_2}}{2 \pi^2} \right] \Lambda^2$$

  $$\Delta m^2_{\Sigma, u^c} = \left[ - \frac{\alpha \alpha_{\Sigma_2}}{8 \pi^2} \right] \Lambda^2$$

  $$\Delta m^2_{\Sigma} = \left[ \frac{3 \alpha_{\Sigma_2}^2}{4 \pi^2} + \frac{3 \alpha_{\Sigma_2}^2}{4 \pi^2} + \frac{\alpha_{\Sigma_2} \alpha_{l_2}}{4 \pi^2} - \frac{5 \alpha_{\Sigma_2}}{4 \pi^2} \right] \Lambda^2,$$

  where $\alpha = \frac{\alpha_{\Sigma_2}}{\alpha_l}$ is the $SU(2)$ gauge coupling and $\alpha_l = \frac{\alpha}{4\pi}$ are similarly defined Yukawa couplings for $f = t, b, \tau$. We assume $l_2' \ll 1$ and neglects its contribution. Other Yukawa couplings are also neglected as they are small. The effects are summarized as follows.

  - **$H_d$**: Soft scalar mass squared is negative at the tree level from the bosonic see-saw mechanism. There are threshold corrections from gauge and Yukawa interactions and the sign is opposite. If Yukawa and gauge couplings are of similar size, the threshold corrections at the messenger scale cancel with each other. Therefore, negative mass squared at the tree level dominates.

  - **$H_u$**: Threshold corrections at the messenger scale are positive for both gauge and Yukawa contributions. We have slightly larger $m^2_{H_u}$ compared to the MSSM with gauge mediation. We should also consider negative one loop correction from messenger scale to the weak scale $- \frac{1}{\alpha} m_l^2 \log \frac{\Lambda}{m_l}$.

  - **$\Sigma$**: Threshold corrections are positive for gauge and Yukawa contributions. Thus we get $m^2_{\Sigma}$ heavier than other soft scalar masses which is necessary to suppress the VEV of $\Sigma$ compared to $H_u$ and $H_d$.

  - **Third generation** $Q, u^c (\rightarrow$ stop) Threshold correction from Yukawa mediation is negative. We get lighter stop mass compared to the MSSM which makes the negative contribution to $m^2_{H_u}$ smaller than usual.

  The most challenging phenomenological constraint comes from chargino mass bound combined to the precision data. The chargino mass is obtained from Yukawa interactions (A : Higgsino-Wino-Higgs and B : Higgsino-$\psi_{\Sigma_2}$-Higgs) in the $\mu$-less theory. $A$ is the gauge coupling and $B$ is a new Yukawa coupling $l_{\Sigma_2}$ that violates custodial $SU(2)$ symmetry. The bound on the precision variable $T$ ($T < 0.6$) restricts $l_{\Sigma_2}$ ($l_{\Sigma_2} < 0.6$). For $l_{\Sigma_2} \sim 1$, we obtain the lightest chargino mass to be 104 GeV which is the bound from LEP II. The chargino masses are 104, 119, 252 GeV for $l_{\Sigma_2} = 1, (M_2, M_{\Sigma}) = (120, 150)$ GeV. Note that if we allow nonzero $\mu$, we can satisfy the chargino mass bound with a smaller $l_{\Sigma_2}$. More precise calculation of $T$ is needed as we deal with light spectrum (charginos are near 100 GeV). For the neutralinos, the lower mass bound 40 GeV is easily satisfied.
gives $m_{H_u}^2 < 0$ at the messenger scale and $m_{H_d}^2$ is driven to be negative by RG running to the weak scale. Both $m_{H_u}^2$ and $m_{H_d}^2$ are negative at the weak scale and the minimum is at around $\tan \beta = \frac{v_u}{v_d} \sim O(1)$. Unlike in the MSSM, the potential is not bound from below for $m_{H_u}^2 < 0$, $m_{H_d}^2 < 0$ as the new quartic coupling $l_1$ prevents them from running away along D-flat direction.

In this paper we proposed a new mechanism to understand the electroweak symmetry breaking. As $H_d$ couples directly to the messenger of supersymmetry breaking, the soft scalar mass squared is negative by the bosonic see-saw mechanism when supersymmetry is broken. The soft scalar mass squared of $H_u$ is driven to be negative and the symmetry breaking minimum is at around $\tan \beta = \frac{v_u}{v_d} \sim O(1)$. There is a new $SU(2)_L$ triplet $\Sigma$ which couples to $H_u$ and $H_d$. The lightest chargino mass is predicted to be light due to the absence of supersymmetric mass $\mu$ and lies just above the current mass bound $104$ GeV. The lightest Higgs mass is heavy as we have a new quartic coupling. All the soft parameters appear from gauge mediation and new Yukawa(Higgs) mediation gives negative contributions to $H_d$ and the third generation $Q$ and $u^c$ (stop) and positive contributions to $H_u$ and $\Sigma$. The contributions of Yukawa(Higgs) mediation softens the little hierarchy problem of MSSM. As Higgs can be heavy, the fine tuning problem is no longer severe.

The setup considered here naturally arise from the five dimensional geometric setup \cite{16}. The orbifold GUT fixes the location of gauge and Higgs fields to be in the bulk and the distant brane is a source of supersymmetry breaking. In this case Higgs is very special and can feel the supersymmetry breaking directly. The massive vector-like fields introduced here is just the massive Kalazza-Klein towers of bulk Higgs fields. Gaugino mediation can be considered at the same time as there is no symmetry preventing the couplings of supersymmetry breaking fields with gauge sector. In the orbifold GUT, the doublet-triplet splitting of Higgs fields is explained by the boundary condition (or orbifold projection) and the setup given in this paper naturally arises from higher dimensions. More precisely, only $H_u$ should be bulk fields as in \cite{17}. The setup has been studied to understand the top/bottom mass hierarchy without large $\tan \beta$ in \cite{17}. Furthermore, the smallness of $l_1$ compared to $l_0$ can be explained by the zero mode localization of $H_d$ \cite{18, 19, 20}.

We proposed a new idea called 'bosonic see-saw mechanism'. Once supersymmetry is broken, at same time it gives the VEV to the Higgs fields, i.e., quarks and leptons get their masses. The mechanism works nicely even if $\mu = 0$ though we need additional weak triplet. The chargino remains light (near 104 GeV) when $\mu = 0$ and it is robust against radiative corrections. Higgs is heavy (about 130 GeV before considering radiative corrections) but the full spectrum of Higgs can be obtained only after considering the radiative corrections and we leave the detailed calculation of it for future work. The bosonic see-saw mechanism can be applied differently in other problems.

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