Emergence of Anchored Flux Tubes Through the Convection Zone

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ABSTRACT

We model the evolution of buoyant magnetic flux tubes in the Sun's convection zone. A flux tube is assumed to lie initially near the top of the stably stratified radiative core below the convection zone, but a segment of it is perturbed into the convection zone by gradual heating and convective overshoot motions. The ends ("footpoints") of the segment remain anchored at the base of the convection zone, and if the segment is sufficiently long, it may be buoyantly unstable, rising through the convection zone in a short time. The length of the flux tube determines the ratio of buoyancy to magnetic tension: short loops of flux are arrested before reaching the top of the convection zone, while longer loops emerge to erupt through the photosphere. Using Spruit's convection zone model, we compute the minimum footpoint separation $L_c$ required for erupting flux tubes. We explore the dependence of $L_c$ on the initial thermal state of the perturbed flux tube segment and on its initial magnetic field strength. Following an investigation of thermal diffusion time scales and the dynamic rise times of unstable flux tube segments, we conclude that the most likely origin for magnetic flux which erupts to the surface is from short length scale perturbations ($L < L_c$) which are initially stable, but which are subsequently destabilized either by diffusion of heat into the tube or by stretching of the anchor points until $L$ just exceeds $L_c$. In either case, the separation of the anchor points of the emergent tube should lie between the critical distance for a tube in mechanical equilibrium and one in thermal equilibrium. Finally, after comparing the dispersion of dynamic rise times with the much shorter observed active region formation time scales, we conclude that active regions form from the emergence of a single flux tube segment.

1. Introduction

In several recent theories of solar and stellar dynamos [Golub et al., 1981; Galloway & Weiss 1981; Deluca & Gilman 1986] magnetic fields are generated not in the convection zone, but
in a thin, convectively stable layer just below it. In order for this magnetic flux to emerge to
the photosphere where it can be observed, it must first make its way through the convection
zone. It is generally believed that magnetic buoyancy provides the force which pushes the
magnetic flux toward the surface (Parker 1979). Our goal in this paper is to use the thin
flux tube approximation of Spruit (1981) to study the emergence of buoyant loops of mag-
netic flux whose ends are still anchored in the stable layer below the convection zone. Our
approach is similar to that used by Moreno-Insertis (1986). Further details of our calcula-
tions may be found in Chou & Fisher (1989); henceforth Paper I, and Fisher et al. (1989),
henceforth Paper II. Here we present only the essentials.

2. Description of the Model

In the thin flux tube approximation, the tube diameter is assumed to be smaller than
any other relevant physical length scale, and the magnetic field is taken to be constant
across the tube. Furthermore, since the magneto-acoustic transit time across the tube will
be smaller than other time scales of interest, one may assume that there is always a balance
between the gas pressure outside the tube and the sum of gas plus magnetic pressure inside
the tube. One can think of a thin flux tube as a one-dimensional curve embedded in space.
Our flux tube is tied down at both ends to the bottom of the convection zone, with the
portion in between free to move in response to buoyancy, magnetic tension, and drag forces.
We take the flux tube to lie in a vertical plane, defined by a horizontal \( x \)– axis at the base
of the convection zone, and a vertical \( y \)– axis, and regard the height \( y \) of the the flux tube
as a function of \( x \) and time \( t \). The ends of the flux tube segment are anchored at \( x = 0 \) and
\( x = L \). In all the calculations discussed in this paper, we assume that the flux tube initially
\( (t = 0) \) lies flat at the bottom of the convection zone \( (y = 0) \). In the discussion below,
subscript \( e \) refers to the external plasma of the convection zone, and subscript \( i \) refers to the
plasma inside the flux tube.

2.1. The Basic Equations

The velocity of the plasma in the flux tube consists of the speed of the tube itself in the
direction normal to its length (denoted \( v_n \)) and the speed of plasma moving along the flux
tube (denoted by \( v_s \)). The equation of motion for the velocity component \( v_n \) is given by

\[
(\rho_e + \rho_i) \frac{dv_n}{dt} = \frac{B^2}{4\pi R} + \frac{(\rho_e - \rho_i)g}{\sqrt{1 + (\partial y/\partial x)^2}} - \frac{C_D \rho_e |v_n| v_n}{\sqrt{\pi A}}
\]  

(1)
where the terms on the right hand side of equation (1) correspond, respectively, to magnetic tension, buoyancy, and aerodynamic drag forces. The drag coefficient $C_D$ is taken to be unity. Note that the inertial term contains the “added mass” of the displaced external plasma flowing around the flux tube (see, e.g., Landau & Lifshitz 1959, §24). An insignicant centrifugal force due to parallel flows through bends in the flux tube has been neglected. Equation (1) must be supplemented by an equation relating the vertical motion of the tube to the velocity $v_n$ and the flux tube slope $\partial y/\partial x$. From geometrical considerations, we find at a fixed value of $x$

$$\frac{\partial y}{\partial t} = v_n \sqrt{1 + (\partial y/\partial x)^2}. \quad (2)$$

The radius of curvature $R$, the magnetic field strength $B$, and the flux tube cross-sectional area $A$ appearing in equation (1) are determined by

$$\frac{1}{R} = \frac{\partial^2 y/\partial x^2}{[1 + (\partial y/\partial x)^2]^{3/2}}; \quad P_e - P_i = \frac{B^2}{8\pi}; \quad BA = \Phi, \quad (3)$$

where $P_i$ and $P_e$ are the internal and external gas pressures, respectively, and $\Phi$ is the total magnetic flux. The numerical techniques used for solving equations (1) and (2) are described in Paper I.

The parallel flows of the plasma inside the flux tube can be calculated from equations (1) and (2) and mass conservation arguments (see Paper I). These flows turn out to be sufficiently slow that the plasma can be taken to be in hydrostatic equilibrium. If we make the same assumption regarding the external plasma (i.e., ignoring effects of convection), then it is straightforward to determine all the thermodynamic and magnetic variables as functions of height alone. This procedure is outlined below. It is not at all obvious a priori that the neglect of convective motions is justified. The presence of these motions could affect flux tube evolution in two ways. First, the convective motions could severely distort the shape of the flux tube. Second, convective motions introduce a turbulent pressure which perturbs hydrostatic equilibrium and this could affect the calculated magnetic field strength. We consider both effects in Paper I and conclude that the first effect could be important for some of the thinnest flux tubes we study, whereas the second is not important for any of the cases we have studied.

The structure of the background external atmosphere is taken to be the convection zone model of Spruit (1974). This atmosphere is slightly superadiabatic due to convective heat transport. The information in Spruit’s paper is sufficient to calculate the thermodynamic and magnetic quantities needed for our dynamic model. We assume that the plasma inside the flux tube is isolated from heat transfer and behaves adiabatically. There will of course be heat transport between the flux tube and its surroundings, but we have not included this specifically in the model. Our approach in this paper is to approximate the effects of
heat conduction by choosing a physically self-consistent value of the temperature difference between the flux tube and its environs (i.e. the parameter $\eta$ introduced below) at the base of the convection zone. This will be described further in the section on time scales for emerging flux tubes.

It is straightforward to derive an equation for $\beta$ \[ \beta \equiv \frac{8\pi P_e}{B^2} = \frac{P_e}{(P_e - P_i)} \] in terms of the height variation of the external temperature difference $\delta T \equiv T_e - T_i$ between the external and internal plasma; this avoids the numerical difficulty of subtracting two gas pressures which are nearly equal. Starting from the equilibrium equations

\[
\frac{dP_e}{dy} = -\rho_e g; \quad \frac{dP_i}{dy} = -\rho_i g
\]

one finds

\[
\frac{1}{\beta(\beta - 1)} \frac{d\beta}{dy} = -\frac{1}{\Lambda} \frac{\delta T/T_e}{1 - \delta T/T_e}
\]

where $\Lambda$ is the external pressure scale height. This has the solution

\[
\beta(y)^{-1} = \beta_0^{-1} \exp[-\gamma(y)] + \{1 - \exp[-\gamma(y)]\}
\]

where $\beta_0 = \beta(0)$ and

\[
\gamma(y) = \int_0^y \frac{dy'}{\Lambda(y')} \frac{\delta T(y')/T_e(y')}{1 - \delta T(y')/T_e(y')}
\]

The temperature difference is simply

\[
\delta T(y) = \delta T_0 - \int_0^y dy' (\nabla - \nabla_{ad}) \mu g/R_g
\]

where $\delta T_0 = \delta T(0)$, $\nabla \equiv (\partial \ln T/\partial \ln P)$, $\nabla_{ad} \equiv (\partial \ln T/\partial \ln P)_S$, and $\mu$ and $R_g$ are the mean mass per particle and the gas constant. The temperature difference at the bottom of the convection zone $\delta T_0$ is given in terms of parameters $\eta$ and $B_0$ by

\[
\delta T_0 = \eta T_e(0)/\beta_0
\]

where $\beta_0 = 8\pi P_e/B_0^2$. The quantity $B_0$ is the magnetic field strength at the base of the convection zone, and is one of the free parameters of the problem, while $\eta$ is a dimensionless measure of the temperature difference at the base of the convection zone, and is constrained to lie between 0 and 1. When $\eta = 0$, the internal temperature is equal to that of the surrounding plasma, whereas for $\eta = 1$, the density inside the flux tube is equal to that outside. Together with $L$ and $\Phi$, specification of $B_0$ and $\eta$ completely defines the flux emergence problem in our model.

Values of all these parameters are highly uncertain, so we have attempted to cover a wide range of parameter space. For most of our simulations, $B_0$ was chosen to be $10^4$ G, $10^5$ G, or $10^6$ G, and the flux $\Phi$ was taken as $10^{18}$ Mx, $10^{20}$ Mx, or $10^{22}$ Mx. Our choice of these values is discussed further in Paper I.
2.2. Example of a Simulation

To demonstrate our model, we briefly discuss the results of a single simulation. In this case, \( B_0 = 10^6 \) G, \( \Phi = 10^{18} \) Mx, \( \eta = 0 \), and \( L = 2 \times 10^{10} \) cm. The position of the tube at numerous times is shown in Figure 1. This flux tube is “unstable” and emerges from the top of the calculational domain without reaching an equilibrium configuration. Note that the upward motion of the flux tube slows significantly when its apex is roughly half-way through the convection zone. This indicates that the magnetic tension was almost strong enough to balance the buoyancy force. Had \( L \) in fact been only slightly smaller (\( \leq 1.97 \times 10^{10} \) cm), the flux tube would have been “stable” and would have stopped rising when the height of the flux tube apex \( y_a \approx 9 \times 10^9 \) cm. We explore this interesting behavioral dichotomy in the following subsection.

3. The Critical Length Scale

From the discussion in the previous section, it is apparent that for given values of the other parameters, a critical length \( L_c \) exists. For \( L < L_c \), the flux tube reaches a stable equilibrium, while for \( L > L_c \), an unstable eruption to the photosphere occurs. Therefore, a knowledge of the dependence of \( L_c \) on the other parameters is very important for understanding the nature of flux emergence. The magnetic flux \( \Phi \) affects the drag force and therefore the rate of rise, but it does not affect the relative balance between buoyancy and tension, so \( L_c \) is independent of \( \Phi \). To determine the dependence of \( L_c \) on \( \eta \) and \( B_0 \), we have used the numerical model described in the previous section. In Figure 2 we plot \( L_c \) as a function of \( \eta \) for \( B_0 = 10^4 \) G and \( B_0 = 10^6 \) G.

There are several features of Figure 2 worthy of mention. First, note that for fixed \( B_0 \), \( L_c \) increases as \( \eta \) increases from 0 to 1. This is easily explained by the decrease in the relative strength of magnetic buoyancy compared to magnetic tension as the temperature inside the flux tube decreases. Thus the footpoint separation \( L \) over which magnetic tension can overcome buoyancy is increased (recall that for fixed apex height tension will scale roughly as \( L^{-2} \)). Second, as \( \eta \) approaches 1 for fixed \( B_0 \), \( L_c \) approaches a finite value, even though the buoyant force goes to zero at the base of the convection zone. Since for \( \eta = 1 \), the initial horizontal state is an equilibrium configuration, one can perform a linear stability analysis of equations (1) and (2) (see Spruit & van Ballegooijen 1982, and Paper II) to obtain \( L_c \) analytically

\[
L_c = \sqrt{2/(1 - \nabla)} \pi \Lambda ,
\]

(10)

which is plotted as the horizontal long-dashed line in Figure 2. This analytic result corre-
Fig. 1.— Plot of the flux tube shape at times separated by $2 \times 10^5$ s.

$L = 2 \times 10^{10}$ cm, $\eta = 0$

$B_0 = 10^6$ G, $\Phi = 10^{18}$ Mx

$\Delta t = 2 \times 10^5$ s
sponds very well to our numerical result for $\eta = 1$ and $B_0 = 10^4$ G, but it is about 10% smaller than the critical length (for emergence of the flux tube to the photosphere) which we find numerically for $\eta = 1$ and $B_0 = 10^6$ G. The reason for this interesting discrepancy is discussed in Paper II.

4. Time Scales for Emerging Flux Tubes

If magnetic flux emerges from the convective overshoot region and evolves according to our model, only those flux tubes we have labeled “unstable” ($L > L_c$) can reach the photosphere. The time required for the flux tube to rise through the convection zone is therefore of great interest. We assume that a flux tube is formed in the stably stratified region beneath the convection zone, and begins its buoyant rise when perturbed upward into the convection zone by gradual heating and convective overshoot motions. Before perturbation, the flux tube must be in mechanical equilibrium ($\rho_i = \rho_e$) as otherwise it would adjust by rising or sinking adiabatically [Parker 1979]. The nature of a perturbation is described by the two parameters $L$ and $\eta$. $L$ is the length scale of the perturbation, and $\eta$ measures its thermodynamic state. When $\eta = 1$, the perturbed flux tube is still in mechanical equilibrium ($\rho_i = \rho_e$), whereas if $\eta = 0$, the flux tube is in thermal equilibrium with its surroundings ($T_i = T_e$). The proper choice of $\eta$ for the perturbation can be made by comparing the thermal diffusion time at the bottom of the convection zone $\tau_{th}$ to the dynamic rise time $\tau_d$ for unstable $\eta = 1$ flux tubes. If $\tau_{th} >> \tau_d$, then $\eta = 1$ is the best description of the perturbation, whereas if $\tau_{th} << \tau_d$, then $\eta = 0$ is most appropriate. When the two are comparable, an intermediate value of $\eta$ is called for. The thermal diffusion time scale is given by (see Paper II)

$$\tau_{th} \approx 0.1 \frac{\rho_e^2 C_p a^2 \kappa_R}{16 \sigma T_e^3},$$

(11)

where $\sigma$ is the Stefan-Boltzmann constant, $\kappa_R$ is the Rosseland mean opacity [cm$^2$ g$^{-1}$], and $a = [\Phi/(\pi B_0)]^{1/2}$ is the radius of the flux tube at the base of the convection zone. The dynamic rise time $\tau_d$ for $\eta = 1$ can be obtained from the numerical simulations. Note that the thinner (smaller $\Phi$) flux tubes will have shorter thermal time scales and longer dynamic time scales. We find that $\tau_d$ does not depend strongly on $L$, provided $L$ exceeds $L_c$ by at least 5%. We therefore have used $L = 4 \times 10^{10}$ cm (cf. Figure 2) to compute our estimates of $\tau_d$. Computed values of $\tau_d$ and $\tau_{th}$ as functions of $\Phi$ and $B_0$ are shown in Table 1, along with the resultant values of $\eta$. We also include in Table 1 the “corrected” dynamical rise times (denoted $\tau_r$) using these self-consistent values of $\eta$ in the numerical simulations.

From the information in Table 1 and the critical length scales of Figure 2 it is now
Fig. 2.— Critical length scale as a function of $\eta$ for $B_0 = 10^6$ and $10^4$ G. The long-dashed horizontal line corresponds to the value from equation (10), and the short-dashed line corresponds to Parker’s (1979) isothermal result of $2\pi\Lambda$. 
possible to construct a general picture of flux tube evolution. For given values of $\Phi$ and $B_0$, perturbation length scales divide naturally into three ranges: short, $L < L_c(\eta = 0)$; medium, $L_c(\eta = 0) < L < L_c(\eta = 1)$; and long, $L_c(\eta = 1) < L$. If $\tau_{th} << \tau_d$ then only short flux tubes are stable, while longer flux tubes rise to the photosphere on the dynamical time scale. But if $\tau_{th} >> \tau_d$, both short and medium flux tubes are stable. Only the short flux tubes are “absolutely” stable, however, as the medium length tubes are able to rise quasi-statically on the thermal time scale as heat leaks into them. This is equivalent to gradually decreasing $\eta$ from 1 to 0. However, before $\eta$ reaches zero, a medium-$L$ flux tube will suddenly find itself with $L > L_c$, and will then erupt to the photosphere on the much shorter dynamic rise time.

In the most straightforward (e.g. $\alpha \omega$ or $\alpha^2 \omega$) kinematic dynamo models the oscillatory nature of the solar cycle is due to periodic conversion of poloidal to toroidal magnetic field and back via the mechanisms of stretching by differential rotation and the $\alpha$-effect (which is usually attributed to net helicity in convective or convective overshoot motions). The dynamo period is therefore at least as great as the time necessary to reorient and stretch poloidal field into toroidal field. For these dynamos to work, therefore, magnetic flux must remain in the dynamo region long enough for reorientation to occur, i.e., for a significant fraction of the solar cycle. The conclusions drawn below are based on this premise. An alternative picture is that the dynamo generates fields on a much shorter time scale, in which case our arguments below do not hold. In that case, however, the period of the solar cycle itself remains unexplained and some additional unknown mechanism must be invoked to account for it.

From a comparison of the time scales in Table 1 with the length of half a solar cycle (roughly 11 years or $3.4 \times 10^8$ s), some tentative conclusions about the nature of the flux tube perturbations can be drawn. First, note that the rise time $\tau_r$ of unstable flux tubes is always much shorter than the duration of the solar cycle. If there were a continuous source of perturbations with length scales $L > L_c$, then magnetic flux could not remain stably submerged on time scales much longer than $\tau_r$. One therefore concludes that such perturbations are either rare or nonexistent. Indeed, if convective overshoot motions are responsible for the flux tube perturbations, one would expect typical perturbation length scales to be of order the eddy size, which in mixing length theory is roughly the pressure scale height near the bottom of the convection zone, i.e. $6 \times 10^9$ cm. This is significantly less than any of the $L_c$ values in Figure 2. A perturbation with $L > L_c$ would require coherent action on the part of several adjacent eddies. Assuming this to be unlikely, the magnetic flux which does eventually emerge must originate from perturbations in the short or intermediate $L$ range. We consider two possibilities.

First, if the separation $L$ between anchor points is truly fixed in time, then only those
perturbations in the intermediate $L$ range can emerge at all, since short $L$ perturbations result in completely stable structures. Furthermore, only those combinations of $B_0$ and $\Phi$ which give rise to $\eta = 1$ in Table 1 are viable, i.e. those flux tubes with $\Phi \approx 10^{22}$ Mx. In that case, we expect magnetic flux to emerge to the surface on thermal diffusion time scales and to have a footpoint separation between $L_c(\eta = 0)$ and $L_c(\eta = 1)$.

The second possibility is that there is stretching of the anchor point separation $L$ past $L_c$ after a stable short $L$ perturbation has been made. There are two possible mechanisms for this. In the first instance, stretching could be accomplished by differential rotation, for example, if the anchor points differ in latitude. The second mechanism is the thermal heating of the anchor points themselves. This may cause a gradual “unzipping” of the flux tube segment, until the footpoint separation exceeds $L_c$. The time scale for this to occur depends on a number of factors, including how deeply buried the remainder of the flux tube is in the overshoot region. This is discussed further in Paper II. Here again, for either mechanism, we expect the anchor point separation of emerging flux to lie in the range $L_c(\eta = 0) < L < L_c(\eta = 1)$.

As a final point, note that the dispersion in rise times for individual flux tubes with different values of $\Phi$ (a month or more – see Table 1) is much greater than the formation times of active regions (typically 2-3 days). We believe this indicates that active regions are formed from a single emerging flux tube. If many tubes of differing sizes were perturbed simultaneously, or if a single flux tube became highly fragmented near the bottom of the convection zone, one would expect the emergence of flux to be dispersed over a much greater time corresponding to the difference in rise times between small $\Phi$ (e.g., $10^{18}$ Mx) and large $\Phi$ (e.g., $10^{22}$ Mx) flux tubes. Any fragmentation therefore probably takes place in the topmost portion of the convection zone when the tube is emerging most rapidly.

5. Conclusions

We have developed a model, based on the thin flux tube approximation of Spruit (1981), for studying the emergence of magnetic flux through the convection zone when the footpoints of the flux loop are anchored a distance $L$ apart in the stable layers below. Figure 1 shows the evolution of a flux tube whose footpoints are sufficiently far apart ($L > L_c$) to allow it to rise to the top of the convection zone. We have used our model to explore the critical length $L_c$ separating flux tubes which form stable magnetic loops in the convection zone ($L < L_c$) from those which erupt through the photosphere ($L > L_c$). Figure 2 shows the dependence of $L_c$ on the temperature defect parameter $\eta$ for two values of the field strength at the base of the convection zone $B_0$, $10^4$ G, and $10^6$ G. We find that for perturbations on
## Table 1: Flux Tube Time Scales

|                  | $B_0 = 10^6$ [G] | $B_0 = 10^5$ [G] | $B_0 = 10^4$ [G] |
|------------------|------------------|------------------|------------------|
| **Uncorrected ($\eta = 1$) rise time $\tau_d$ [s]** |                  |                  |                  |
| $\Phi = 10^{22}$ [Mx] | $8.3 \times 10^5$ | $6.4 \times 10^6$ | $3.9 \times 10^7$ |
| $\Phi = 10^{20}$ [Mx] | $1.8 \times 10^6$ | $1.1 \times 10^7$ | $4.7 \times 10^7$ |
| $\Phi = 10^{18}$ [Mx] | $5.3 \times 10^6$ | $3.0 \times 10^7$ | $8.1 \times 10^7$ |
| **Thermal diffusion time $\tau_{th}$ [s]** |                  |                  |                  |
| $\Phi = 10^{22}$ [Mx] | $2.7 \times 10^4$ | $2.7 \times 10^5$ | $2.7 \times 10^6$ |
| $\Phi = 10^{20}$ [Mx] | $2.7 \times 10^5$ | $2.7 \times 10^6$ | $2.7 \times 10^7$ |
| $\Phi = 10^{18}$ [Mx] | $2.7 \times 10^3$ | $2.7 \times 10^4$ | $2.7 \times 10^5$ |
| **Self-consistent $\eta$** |                  |                  |                  |
| $\Phi = 10^{22}$ [Mx] | 1.0 | 1.0 | 1.0 |
| $\Phi = 10^{20}$ [Mx] | 0.0 | 0.0 | 0.5 |
| $\Phi = 10^{18}$ [Mx] | 0.0 | 0.0 | 0.0 |
| **Corrected rise time $\tau_r$ [s]** |                  |                  |                  |
| $\Phi = 10^{22}$ [Mx] | $8.3 \times 10^5$ | $6.4 \times 10^6$ | $3.9 \times 10^7$ |
| $\Phi = 10^{20}$ [Mx] | $6.7 \times 10^5$ | $3.1 \times 10^6$ | $8.6 \times 10^6$ |
| $\Phi = 10^{18}$ [Mx] | $2.1 \times 10^6$ | $9.8 \times 10^6$ | $1.7 \times 10^7$ |
length scales $L > L_c(B_0, \eta)$ the rise time is short compared to the duration of the solar cycle. Under the assumption that the solar cycle can be modeled as a kinematic (e.g., $\alpha \omega$ or $\alpha^2 \omega$) dynamo model operating below the convection zone, we conclude that such perturbations must therefore be rare or nonexistent. We speculate that the magnetic flux which does erupt through the photosphere forms initially from perturbations with $L < L_c$, resulting in stable structures. These are subsequently destabilized either by thermal diffusion or by stretching of the anchor points until $L$ exceeds $L_c$. In either case, we expect that the anchor point separation $L$ should fall roughly within the range $L_c(\eta = 0)$ to $L_c(\eta = 1)$. The rise time of flux tubes is the time scale for conduction of heat into the tube in the first case, and the stretching time in the second case. Finally, we argue that active regions are formed from the emergence of a single flux tube segment.

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