New remarks on the linear constraint self-dual boson and Wess-Zumino terms

Everton M. C. Abreu and Alvaro de Souza Dutra
Departamento de Física e Química, Universidade Estadual Paulista,
Av. Arirberto Pereira da Cunha 333, Guaratinguetá, 12516-410, São Paulo, SP, Brazil,
E-mail: everton@feg.unesp.br and dutra@feg.unesp.br
(March 27, 2002)

In this work we prove in a precise way that the soldering formalism can be applied to the Srivastava chiral boson (SCB), in contradiction with some results appearing in the literature. We have promoted a canonical transformation that shows directly that the SCB is composed of two Floreanini-Jackiw’s particles with the same chirality which spectrum is a vacuum-like one. As another conflictive result we have proved that a Wess-Zumino term used in the literature consists of the scalar field, once again denying the assertion that the WZ term adds a new degree of freedom to the SCB theory in order to modify the physics of the system.

11.10.Ef, 12.10.Gq, 04.65.+e

I. INTRODUCTION

The research in chiral bosonization has begun many years back with the seminal paper of W. Siegel [1]. Floreanini-Jackiw have offered later some different solutions to the problem of a single self-dual field [2] proposing a non-anomalous model. The study of chiral bosons has blossomed thanks to the advances in some string theories [3] and in the construction of interesting theoretical models [4]. They also play an important role in the studies of the quantum Hall effect [5]. The introduction of a soliton field as a charge-creating field obeying one additional equation of motion leads to a bosonization rule [6]. Stone [7] has shown that the method of coadjoint orbit [8], when applied to a representation of a group associated with a single affine Kac-Moody algebra, generates an action for the chiral WZW model [9], a non-Abelian generalization of the Floreanini and Jackiw (FJ) model.

A self-dual field in two dimensions is a scalar field which satisfies the self-dual constraint (self-dual condition) \( (\eta_{\mu\nu} + \epsilon_{\mu\nu}) \partial_\phi \phi = 0 \) or \( \phi = \phi' \), where a dot means time derivation and prime, space derivation. In the formulation of Floreanini and Jackiw [2], the space derivation of the field instead of the field itself satisfies the self-dual condition, i.e., \( (\partial_0 - \partial_1) \partial_1 \phi = 0 \), and the field violates the microcausality postulate [10].

Trying to overcome these difficulties, Srivastava [11] introduced an auxiliary vector field \( A_\mu \), coupled with a linear constraint and constructed a Lorentz-invariant Lagrangian for a scalar self-dual field. Although Harada [12] and Girotti et al [13] have pointed out consistency problems with the Srivastava model at the quantum level, the linear formulation strictly describes a chiral boson from the point of view of equations of motion at the classical level. Some methods were used to quantize the theory [14]. The extension to \( D = 6 \) was accomplished in [15] as well as its supersymmetric case [16].

On the other hand, the concept of soldering [17] has proved extremely useful in different contexts. The soldering formalism essentially combines two distinct Lagrangians manifesting dual aspects of some symmetry to yield a new Lagrangian which is destituted of, or rather hides, that symmetry. The quantum interference effects, whether constructive or destructive, among the dual aspects of symmetry, are thereby captured through this mechanism [18]. The formalism introduced by Stone could be interpreted recently as a new method of dynamical mass generation [19]. This technique parallels a similar phenomenon in two dimensional field theory known as Schwinger mechanism [19] that results from the interference between right and left massless self-dual modes of chiral Schwinger model [20] of opposite chiralities [18].

Furthermore, an important ingredient in the study of such kind of systems are the so called Wess-Zumino (WZ) terms [21], which are introduced in the theory in order to recover the gauge invariance [22]. In [23], it was proposed a new way of the derivation of the WZ counterterm. It was based on the generalized Hamiltonian formalism of Batalin and Fradkin [24] which have suggested a kind of quantization procedure for second-class constraint systems to which anomalous gauge theory belong [22,25]. The final action obtained, dependent on an arbitrary parameter, has been constructed in order to become the Srivastava model gauge invariant. The Lorentz invariance requirement has fixed the parameter in two possible values which generates two possible WZ terms. The result, with one of the WZ terms, after a kind of chiral decomposition, was that the SCB spectrum is composed of two opposite FJ’s chiral bosons, similarly to what happens with the Minimal Chiral Schwinger Model [26]. The conclusion, however, was that the WZ term so obtained have added a new physical degree of freedom, an antichiral boson, to the spectrum and therefore changes the self-dual field into a massless scalar. Besides, in another similar paper, Miao and Chen [27] have asserted that it is impossible to apply the soldering formalism [17] to solder two opposite chiral aspects of the model proposed by Srivastava, as was successfully accomplished in the Siegel and
Florenanini-Jackiw theories [28]. It was pointed out that the method was invalid in the linear formulation because of the inequivalence of Srivastava’s and Siegel and FJ’s. Hence, to promote the fusion, it was constructed a chiral counterterm [24] for the linear formulation of the chiral bosons. This counterterm was the same Wess-Zumino term mentioned above.

In this work we have demonstrated that both conclusions are not really true. We have applied successfully the soldering formalism and showed that the interference on-shell of two SCB results in a massless scalar field. As another result, we have performed essentially a canonical transformation (CT) [29, 31] (as a special case of CT, we have used the dynamical decomposition [31], which promotes a separation of a chiral theory in its dynamical and symmetry parts) and the outcome showed, in an exact way, that the spectrum is already composed of two FJ’s chiral bosons with the same chirality confirming the well known result that the SCB has two degrees of freedom thanks to the linear constraint structure [32]. Besides, we have showed that the WZ term introduced in [23] is in fact a scalar field, i.e., it is composed of two FJ’s chiral bosons with the same chirality confirming the method was invalid in the linear formulation because of the self and anti-self dual systems put together. Then, suppose that after N repetitions, the non invariant piece end up being only dependent on the gauging parameters, but not on the original fields, there will exist the possibility of mutual cancelation if both self and anti-self gauged systems are put together. Then, suppose that after N repetitions we arrive at the following simultaneous conditions,

\[ S_{\pm}(\phi_{\pm})^{(0)} \to S_{\pm}(\phi_{\pm})^{(N)} = S_{\pm}(\phi_{\pm})^{(N-1)} - B^{(N)} J_{\pm}^{(N)} . \]

Here \( J_{\pm}^{(N)} \) are the \( N \)-iteration Noether currents. For the self and anti-self dual systems we have in mind that this iterative gauging procedure is (intentionally) constructed not to produce invariant actions for any finite number of steps. However, if after N repetitions, the non invariant piece end up being only dependent on the gauging parameters, but not on the original fields, there will exist the possibility of mutual cancelation if both self and anti-self gauged systems are put together. Then, suppose that after N repetitions we arrive at the following simultaneous conditions,

\[ \delta S_{\pm}(\phi_{\pm})^{(N)} \neq 0 \quad \text{and} \quad \delta S_{B}(\phi_{\pm}) = 0 , \]

with \( S_{B} \) being the so-called soldered action

\[ S_{B}(\phi_{\pm}) = S_{B}^{(N)}(\phi_{\pm}) + S_{B}^{(N)}(\phi_{\pm}) + \text{Contact Terms} , \]

where the Contact Terms are generally quadratic functions of the soldering fields. Then we can immediately identify the (soldering) interference term as,

\[ S_{int} = \text{Contact Terms} + \sum_{N} B^{(N)} J_{\pm}^{(N)} . \]

Incidentally, these auxiliary fields \( B^{(N)} \) may be eliminated, for instance, through its equations of motion, from the resulting effective action, in favor of the physically relevant degrees of freedom. It is important to notice that after the elimination of the soldering fields, the resulting effective action will not depend on either self or anti-self dual fields \( \phi_{\pm} \) but only in some collective field, say \( \Phi \), defined in terms of the original ones in a (Noether) invariant way

\[ S_{B}(\phi_{\pm}) \to S_{eff}(\Phi) . \]

Analyzing in terms of the classical degrees of freedom, it is obvious that we have now a bigger theory. Once such effective action has been established, the physical consequences of the soldering are readily obtained by simple inspection.
III. THE SOLDERING OF TWO SRIVASTAVA’S SELF-DUAL BOSONS

The Srivastava action for a left-moving chiral boson, is

$$L^{(0)}_{φ} = \partial_+ φ \partial_- φ + \lambda_+ \partial_- φ ,$$  \hspace{1cm} (8)

where we have used the light-front variables $\partial_{±} = \frac{1}{\sqrt{2}}(∂_0 ± ∂_1)$ and $λ_{±} = λ_0 ± λ_1$.

Following the steps of the soldering formalism studied in the last section, we can start considering the variation of the Lagrangians under the transformations, $δ φ = α$ and $δ λ_+ = 0$. We will write only the main steps of the procedure.

In terms of the Noether currents we can construct

$$δL^{(0)}_φ = J^μ_φ \partial_μ α ,$$  \hspace{1cm} (9)

where $μ = +, -, J_+^φ = 0$ and $J_-^φ = 2 \partial_+ φ + λ_+.$

The next iteration, as seen in the last section, can be performed introducing auxiliary fields, the so-called soldering fields

$$L^{(1)}_φ = L^{(0)}_φ - B_μ J^μ_φ ,$$  \hspace{1cm} (10)

and one can easily see that the gauge variation of $L^{(1)}_φ$ is

$$δL^{(1)}_φ = - 2 B_- δ B_+ ,$$  \hspace{1cm} (11)

where we have defined the variation of $B_±$ as $δB_± = δ ± α$, and we see that the variation of $L^{(1)}_φ$ does not depend on $φ$. It is the signal to begin the process with the other chirality, which is given by

$$L^{(0)}_ρ = \partial_+ ρ \partial_- ρ + λ_- \partial_+ ρ ,$$  \hspace{1cm} (12)

and again, let us construct the basic transformations $δ ρ = α$ and $δ λ_- = 0$.

The Noether’s currents are $J^ρ_+ = 2 \partial_+ ρ + λ_-$ and $J^-_ρ = 0$ and the variation of the final iteration is $δL^{(1)}_ρ = - 2 B_- δ B_+.$

Now we can see that the variation of $L^{(1)}_φ$ does not depend neither on $φ$ nor $ρ$. Hence, as explained before, we can construct the final (soldered) Lagrangian as

$$L_{TOT} = L_L \oplus L_R$$
$$= L^{(1)}_φ + L^{(0)}_ρ + B_+ B_-$$
$$= L^{(0)}_φ + L^{(0)}_ρ - B_+ J^+ - B_- J^- + B_+ B_- \hspace{1cm} (13)$$

which remains invariant under the combined symmetry transformations for $(φ, ρ)$ and $(λ_+, λ_-)$, i.e., $δ L_{TOT} = 0$.

Following the steps of the algorithm depicted in the last section, we have to eliminate the soldering fields solving their equations of motion which result in $B_± = J^±$ where $J^{±} = J^{φ, ρ}.$

Substituting it back in (13) we have the final effective Lagrangian density

$$L_{TOT} = (\partial_- φ - \partial_- ρ) (\partial_+ φ - \partial_+ ρ)$$
$$+ \lambda_+ (\partial_- φ - \partial_- ρ) - \lambda_- (\partial_+ φ - \partial_+ ρ) - \frac{1}{2} λ_+ λ_-$$
$$= \partial_- φ \partial_+ φ + λ_+ \partial_- φ - \lambda_- \partial_+ φ - \frac{1}{2} λ_+ λ_- \hspace{1cm} (14)$$

where the new compound field are defined as $Φ = φ - ρ$.

As we can see we have a second order term in the Lagrange multipliers. Solving the equations of motion for the multipliers, we obtain that,

$$λ_- = 2 \partial_- Φ \quad \text{and} \quad λ_+ = - 2 \partial_+ Φ \hspace{1cm} (15)$$

Substituting the equations (15) in (14) we have

$$L_{TOT} = - \frac{1}{2} \partial_μ Φ \partial^μ Φ \hspace{1cm} (16)$$

which represents the massless scalar field action.

Hence, we have demonstrated in a precise way that it is possible to use the soldering formalism to promote the fusion of two opposite SCB, in contradiction with the assertion done in [27]. Finally, one can conclude that, starting from these inconsistent Lagrangian densities, it is recovered, in the soldering procedure, a consistent model which is, in fact, the free scalar field. However, this result was not the expected one, but we will come back to this issue later.

In the next section we will investigate the spectrum of the Srivastava model constructing a canonical transformation [30], i.e., using the special case of the dynamical decomposition [31]. The objective is to analyze the result obtained by Miao et al [23] previously with the alternative construction of the Wess-Zumino term of the Srivastava theory.

IV. THE DYNAMICAL DECOMPOSITION OF THE SRIVASTAVA MODEL

In the Hamiltonian formulation, canonical transformations can be sometimes used to decompose a composite Hamiltonian into two distinct pieces. A familiar example [29], is the decomposition of the Hamiltonian of a particle in two dimensions moving in a constant magnetic field and quadratic potential. It can be shown that this Hamiltonian can be separated into two pieces corresponding to the Hamiltonians of two one dimensional oscillators rotating in a clockwise and a anti-clockwise directions, respectively. Let us now make a canonical transformation analysis of the SCB. In this case, that the theory is already a chiral one, we will promote a dynamical decomposition of it, i.e., the theory will be decomposed in its dynamical and symmetry parts. If the theory is not invariant, the result will show only the dynamics of the system. To perform this we have to make a canonical transformation [30] in (8) using the Faddeev-Jackiw first-order procedure.
At this point, some interesting comments are in order. The inconsistencies of the SCB model at the quantum level, discussed in some works \([24][38]\), can be verified from another point of view. This is done by comparing the Lagrangian density of the SCB in Minkovisky space, i.e.,

\[
\mathcal{L} = \frac{1}{2} \partial_{\mu} \phi \partial^{\mu} \phi + \lambda_{\mu} (g^{\mu \nu} - \epsilon^{\mu \nu}) \partial_{\nu} \phi \\
= \frac{1}{2} \left( \dot{\phi}^2 - \phi'^2 \right) + \lambda (\dot{\phi} - \phi')
\]

(17)

where \(\lambda = \lambda_+\), with that of the bosonized version of the CSM

\[
\mathcal{L} = \frac{1}{2}(\partial_{\mu})^2 + \epsilon (g^{\mu \nu} - \epsilon^{\mu \nu}) \partial_{\nu} \phi A_{\nu} \\
+ \frac{a}{2} g^{\mu \nu} - \frac{1}{4} F_{\mu \nu}^2
\]

(18)

and to note that the former is in fact a particular case of the latter, where one should take care of the identifications: \(a = 0\) and \(A_{\mu} \to \lambda_{\mu}\), an external field with vanishing field strength. Now, one can relate the inconsistency of the SCB with that of the CSM with the regularization ambiguity parameter \(a = 0\), as shown by Girotti et al \([37]\). Now let us recover the discussion on the SCB, by doing its dynamical decomposition and then discussing how and why the WZ terms introduced in \([23]\) recover its quantum consistency.

The canonical momentum is defined by \(\pi = \dot{\phi} + \lambda\), and substituting it back in (17) to obtain the first-order form we have

\[
\mathcal{L} = \pi \dot{\phi} - \frac{1}{2} \pi^2 + \frac{1}{2} \lambda^2 - \frac{1}{2} \dot{\phi}^2 - \lambda \phi'\,.
\]

(19)

Now, as we have mentioned before, we have to do the following canonical transformation

\[
\phi = \eta + \sigma \quad \text{and} \quad \pi = \eta' - \sigma',
\]

(20)

which is defined as a dynamical decomposition. Notice that \(\phi\) is a chiral field already. So, in this way, this canonical transformation will allow us to know exactly what is the Srivastava chiral boson. Hence, substituting (21) in (18) we have as a result

\[
\mathcal{L}_{DD}^{(1)} = \dot{\eta} \dot{\eta} - \eta'^2 - \sigma' \dot{\sigma} - \sigma'^2 - 2 \lambda \sigma' - \frac{1}{2} \lambda^2.
\]

Again, solving the equations of motion for the \(\lambda\)-field we have \(\lambda = -2 \sigma'\), and, substituting back,

\[
\mathcal{L}_{DD}^{(2)} = \dot{\eta} \dot{\eta} - \eta'^2 - (\sigma' \dot{\sigma} - \sigma'^2).
\]

(21)

We can see clearly that this action represents two Floreanini-Jackiw’s (FJ) chiral bosons. Each one with the same chirality. This is caused by the fact that the Lagrange multiplier has acquired dynamics because of the linear constraint form. In fact, we are demonstrating that (17) has two degrees of freedom, represented in (21) by \(\eta\) and \(\sigma\), differently from Siegel’s approach, where \(\lambda\) is a pure gauge degree of freedom. This result corroborates the one found by Bazeia in \([22]\) analyzing the linear constraint chiral boson quantum mechanics. We can say that both particles in (21) act like a Gupta-Bleuler’s pair so that each chiral excitation destroys the other and the Hilbert space is composed of vacuum. This result confirms the one found in \([23]\).

Hence, in the soldering process of the SCB, each FJ’s chiral boson interact with its opposite chiral partner, so that the final result represents a scalar field. We can observe also that the linear constraint formulation of the chiral boson does not contain the Hull noton \([38]\), a non-mover field that cancels out the anomaly of the Siegel model (an alternative fermionic noton was introduced in \([39]\)), which is expected since the SCB is not gauge invariant.

The result \([21]\) contradicts the result obtained in \([23]\) in the following way. There, firstly it was built a final action composed of the Srivastava action plus a WZ term with an arbitrary parameter. The Lorentz invariance fixed the parameter in two possible values which originated two different WZ terms. Hence, one of the actions obtained, after a kind of chiral decomposition, is shown to have two FJ’s particles of opposite chiralities, in an analogous fashion to what happens with the usual CSM \([40]\). Besides, the final Lagrangian obtained contain the BF fields \([24]\) used to construct the WZ term \([41]\). The conclusion was that the WZ term constructed have added a new degree of freedom to the theory in the form of an antichiral boson. On the other hand, we can see what is really happening through a careful analysis of the two WZ terms introduced in \([23]\). It is not difficult to see that the first WZ term defined in \([23]\), i.e.,

\[
\mathcal{L}_{WZ}^{(1)} = -\frac{1}{2} (\dot{\theta}^2 + 3 \dot{\theta}'^2) - \lambda (\dot{\theta} + \theta') - \frac{1}{2} \lambda^2,
\]

(22)

where \(\theta\) is the BF field, once integrated in the \(\lambda\) field, a chiral boson is recovered. Besides, if one takes the second WZ term introduced in \([23]\),

\[
\mathcal{L}_{WZ}^{(2)} = -\dot{\theta} \theta' - \theta'^2 - \lambda (\dot{\theta} + \theta') - \frac{1}{2} \lambda^2,
\]

(23)

and perform again the integration \(\lambda\), one gets nothing but the Lagrangian density of the free scalar boson. This result signals that the WZ term obtained by Miao et al \([24]\) is already composed of two opposite FJ’s particles. Obviously it really introduces the degree of freedom, because it is already there, in the WZ term, but it does not change the physics of the SCB model, since, as we saw above, this last is composed of vacuum.

Analyzing the interference aspects, we can apply the soldering formalism again, but now, let us do it using two actions of the type of (21), i.e.,

\[
\mathcal{L}_1 = \dot{\eta} \dot{\eta}' - \eta'^2 - (\dot{\sigma} \sigma' - \sigma'^2)
\]

(24)

\[
\mathcal{L}_2 = -\dot{\xi} \xi' - \xi'^2 - (-\dot{\omega} \omega' - \omega'^2)
\]

(25)
where $\eta, \sigma, \xi$ and $\omega$ are all FJ’s particles. We can see in Eqs. (24) and (25) that the fields $(\eta, \xi)$ and $(\sigma, \omega)$ form opposite chiralities particles pairs.

Performing the soldering procedure, one can easily see that the result is

$$\mathcal{L} = \frac{1}{2} (\partial_{\mu} \Psi) - \frac{1}{2} (\partial_{\mu} \Lambda)$$

(26)

where $\Psi = \eta - \xi$ and $\Lambda = \sigma - \omega$. This is the expected result, and not (16), since we know that the SCB have a vacuum-like spectrum. The soldering procedure in (26) discloses the same behavior as shown in [23].

The result (26) is quite different as the one shown in (16). Since it is well known that the soldering of two opposite FJ chiral bosons is a massless scalar field, we should expect that the fusion of two SCB would be two opposite scalar fields with the final vacuum-like spectrum. This difference can be explained [31] as we note that now, in each action of the Eqs. (24) and (25), we have two fields, i.e., the action can be separated in two different sectors, representing the FJ particles with the same chirality. So, in the interference process (soldering) each sector of each action interfere with its opposite partner. To obtain (16), note that we have only one sector in each action. In the interference process we have lost the information about the other sector, like a destructive interference. This does not occur in (26).

V. CONCLUSIONS

It is well known that the SCB has consistency problems. In this work we have used the soldering formalism to show that the interference on-shell of two Srivastava’s chiral bosons resulted in a scalar field. The other aspect of this result is that the soldering method recover the consistency of the SCB model, i.e., the fusion of opposites chiralities of the model results in a consistent theory. This contradicts the conclusion published in the literature, which asserts that it is impossible to apply the soldering procedure to the SCB due to the inequivalence of this model with relation to Siegel and Floreanini-Jackiw’s models.

This has motivated us to explore the model promoting a canonical transformation in the specific form of a dynamical decomposition, which permitted us to decompose the action in its dynamical parts. This procedure showed us that the SCB is in fact formed by two Floreanini-Jackiw’s chiral bosons of the same chiralities. Again, the contradiction with the current literature is evident since one well known publication affirms that the WZ term introduced a new degree of freedom to the theory resulting in two Floreanini-Jackiw’s chiral bosons of opposite chiralities, a chiral boson and an antichiral boson. This is not really true, since we saw that in fact the WZ term used consists of two degrees of freedom, i.e., the two FJ’s opposite chiral particles. So, one can say that it is obvious that this WZ term should introduce new degrees of freedom because it is composed by the fields that appeared. Now, with each SCB composed of two fields, after the fusion through the soldering formalism, we have obtained two scalar fields with a negative signal between them. This result shows that the spectrum of the soldered action is vacuum-like.

VI. ACKNOWLEDGMENTS

The authors would like to thank C. Wotzasek and S. J. Gates Jr. for valuable discussions. EMCA is financially supported by Fundação de Amparo à Pesquisa do Estado de São Paulo (FAPESP). This work is partially supported by Conselho Nacional de Pesquisa e Desenvolvimento (CNPq). FAPESP and CNPq are brazilian research agencies.
[15] Y. G. Miao and H. J. W. Müller-Kirsten, “Self-duality of various chiral boson actions”, hep-th 9912066.
[16] A. A. Deriglazov, Theor. Math. Phys. 92 (1992) 748.
[17] K. Harada, Int. J. Mod. Phys. A 6 (1991) 3399.
[18] E. M. C. Abreu, R. Banerjee and C. Wotzasek, Nucl. Phys. B 509 (1998) 519.
[19] J. Schwinger, Phys. Rev. 128 (1962) 2425.
[20] R. Jackiw and R. Rajaraman, Phys. Rev. Lett. 54 (1985) 1219.
[21] J. Wess and B. Zumino, Phys. Lett. B 234 (1990) 93.
[22] L. D. Faddeev and S. Shatashvili, Phys. Lett. B 167 (1986) 255; K. Harada and I. Tsutsui, Phys. Lett. B 183 (1987) 311; O. Babelon, F. A. Schaposnik and C. M. Viallet, Phys. Lett. B 177 (1986) 385.
[23] Y. G. Miao, J. G. Zhou and Y. Y. Liu, Phys. Lett. B 323 (1994) 169.
[24] I. Batalin and E. S. Fradkin, Nucl. Phys. B 279 (1987) 514; Phys. Lett. B 180 (1986) 157.
[25] L. D. Faddeev, Phys. Lett. B 145 (1984) 81; M. Kobayashi, K. Seo and A. Sugamoto, Nucl. Phys. B 273 (1986) 607.
[26] W.H. Kye, W.T. Kim, J.K. Kim, Phys. Lett. B 268 (1991) 59; A. de Souza Dutra, Phys. Lett. B 286 (1992) 285.
[27] Y. G. Miao and C. H. Chen, Commun. Theor. Phys. 30 (1998) 317.
[28] R. Amorim, A. Das and C. Wotzasek, Phys. Rev. D 53 (1996) 5810.
[29] G. Dunne, R. Jackiw and C. Trugenberger, Phys. Rev. D 41 (1990) 661.
[30] R. Banerjee and S. Ghosh, Phys. Lett. B 482 (2000) 302.
[31] E. M. C. Abreu and C. Wotzasek, Phys. Rev. D 58 (1998) 101701.
[32] D. Bazeia, Mod. Phys. Lett. A 6 (1991) 1147.
[33] C. Wotzasek, Mod. Phys. Lett. A 8 (1993) 2509.
[34] For a review see: C. Wotzasek, “Soldering Formalism: theory and applications”, [hep-th 9806005].
[35] E. M. C. Abreu, A. Ilha, C. Neves and C. Wotzasek, Phys. Rev. D 61 (2000) 025014.
[36] R. Amorim and A. Das, Phys. Rev. D 54 (1996) 4177.
[37] H.O. Girotti, H.J. Rothe, K.D. Rothe, Phys. Rev. D 33 (1986) 514.
[38] C. M. Hull, Phys. Lett. B 206 (1988) 234; Phys. Lett. B 212.
[39] D. Depireux, S. Gates and B. Radak, Phys. Lett. B 236 (1990) 408.
[40] A. de Souza Dutra, Phys. Lett. B 286 (1992) 285.
[41] T. Fujiwara, Y. Igarashi and J. Kubo, Nucl. Phys. B 341 (1990) 695.