A New Graphical User Interface for Teaching NMR

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Abstract The classical Nuclear Magnetic Resonance (NMR) vector model is known to be very effective and useful in teaching basic NMR 1D pulse sequences such as spin echo. For more complicated spin systems, density matrix calculation is often used. This method is known to be very complicated and not easy to follow after couple steps. Students usually get lost within the calculation and lose the physical meaning of the effect of different NMR pulses and other operations (chemical shifts, scalar-couplings) on the spin-system under investigation. As a compromise, another methodology has been developed which depends on the spin angular momentum operators. This is known as product operator formalism which involves less mathematical calculations, but still requires the user to know the correct outcome of different NMR pulses, scalar couplings and chemical shifts on different spin operators. We have developed product operator graphical user interface (OP-GUI) using MATLAB software that is capable of calculating product operators of up to four-coupled ½ spin systems. The effect of NMR pulses, scalar-coupling and chemical shifts on the spin system under investigation can be easily calculated. In this paper, several examples are given as prove of concept to show the capability and flexibility of the obtained OP-GUI in dealing with spin systems. We believe the obtained calculator is an effective teaching tool for new students in NMR and will help them to better understand and interpret complicated NMR pulse sequences applied on up to four weakly coupled ½ spin systems.

Keywords: teaching NMR, product operator formalism, NMR pulse sequences, GUI, MATLAB

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1. Introduction

In the past couple decades a large number of pulse NMR experiments have been developed to extract more information from the spin system under investigation. For the design, analysis and teaching these pulses, different methods have been followed. Many of the simple NMR pulse sequences were successfully explained using classical or semi-classical vector model [1] which relies on hand-waving to study the effect of different pulses on the magnetization vectors on the x, y, z directions. Unfortunately, this method has limitation on complicated pulse sequences. Therefore, for the analysis of more complex pulse experiments density matrix approach was often used [2,3,4,5]. This method involves extensive matrix manipulation and calculation. So often, one gets lost after couple introductory steps and gets away from the physical intuition. As a midway between these two approaches the product operator formalism has been introduced. Product operators rely on using angular momentum operators instead of matrices and originally intended to simplify the calculation. This technique brought a better tool for understanding many now used NMR pulse sequences that cannot be analyzed using the normal vector model. Product operator is a simple quantum mechanical method has been developed for the analytical description of multi-pulse NMR experiments on the weakly coupled spin systems [6-14]. There are many examples that appeared in the literature using product operators but mostly for simple two-spin systems and to less extend to three-spin systems. According to the authors of this study, there are still no examples of higher order spin groups such as four- spin systems treated in the literature using this approach.

In this article, we present an easy alternative tool for teaching various NMR pulse sequences to undergraduate students. This tool is Operator Product Graphical User Interface OP-GUI developed using MATLAB software that is capable to deal with up to four weakly ½ spin systems. The OP-GUI can be used effectively in teaching NMR students the effect of different pulse sequences on a spin system under investigation. The user can start from any of the known initial product operators to see the effect of the specified or arbitrary NMR pulses, chemical shift and coupling between the spin groups. The final result can be simplified to give better interpretation for the expected NMR signal.

2. Background

For a single ½ spin there are four spin operators; two transverse magnetization spin operators $I_x$ and $I_y$, the equilibrium magnetization spin operators $I_z$, and the unity...
operator $E/2$ (where $\frac{1}{2}$ is used for normalization purposes). It is not difficult to follow the effect of an NMR pulse on these operators using vector model.

For example a pulse of $\theta$ degrees along x-axis will tip the equilibrium magnetization ($M_z$ in vector model) by $\theta$ degrees. Given as: $M_z \rightarrow M_z \cos(\theta) + M_z \sin(\theta)$

However, in product operator, spin operators $I_x$, $I_y$, and $I_z$ are used instead ($I_z \rightarrow I_z \cos(\theta) + I_z \sin(\theta)$). The result shows the initial operator ($I_z$ in this case) is modified by $\cos(\theta)$ term plus a new operator ($I_y$ in this example) modified by the $\sin(\theta)$ term. In fact, this is the case in most of the transformation in product operators. In addition, for a single spin, chemical shift evolution in the transverse plane, on $I_y$, for instance, can be written as: $I_y \rightarrow I_y \cos(2\pi\omega t) - I_y \sin(2\pi\omega t)$. Where $t$ is the time interval in which the chemical shift is active and the whole term $2\pi\omega t$ represents the angle of rotation.

For two spins ($I_1$ and $I_2$) there are 16 possible product operators; $I_{1x}$, $I_{1y}$, $I_{1z}$, $I_{2x}$, $I_{2y}$, $I_{2z}$ are observable x and y components of the magnetization, $I_{1z}$, $I_{1y}$, $I_{2x}$, $I_{2y}$, $I_{1z}$, $I_{2z}$, $I_{2x}$, $I_{2y}$, $I_{2z}$ are the observable antiphase magnetization. $I_{1x}$, $I_{1y}$, $I_{1z}$, $I_{2x}$, $I_{2y}$, $I_{2z}$, $I_{2x}$, $I_{2y}$, $I_{2z}$, $I_{1z}$, $I_{2z}$, $I_{2x}$, $I_{2y}$, $I_{2z}$ are the observable unobservable z-components of spin groups independentl y. This is very useful because in many complex systems the scalar coupling among different spin groups might have different strengths and/or with different coupling durations. The drop-menu of the “J-Coupling” section gives the user the flexibility in applying the scalar coupling on four-spin groups independently. This is very useful because in many complex systems the scalar coupling among different spin groups might have different strengths and/or with different coupling durations. The drop-menu of the “J-Coupling” section includes different coupling durations (1/1, 1/2J, 1/4J and 1/8J) that can be chosen by the user for the final calculation. Information about chemical shift on any spin group up to four (chosen from the drop-menu) can be obtained by clicking on the “Chemical Shift” button with the option to simplify the result if the time interval of the chemical shift is known. In addition to that, the GUI provides the option to eliminate any unobservable product operator that might appear in the final answer by using the “Spin Operator Elimination” section. By clicking on any of the nine product operators in this section the term (of the final answer) includes the chosen operator will be eliminated. This simplifies the final result and provides the user more information on the predicted NMR signal.

The obtained OP-GUI is written and developed using MATLAB GUI development environment (GUIDE), based on a set of M-files each representing one of the program functions. Those M-files uses the power of MATLAB functions and symbolic toolbox in computing NMR product operator formalism. The detail of the spin operator transformation is given previously in many references [6,12]. The OP-GUI has different sections as shown in Figure 1. The top part is the input section where the initial spin operators need to be typed in. The notation used for different spins are $I_1$, $I_2$, $I_3$ and $I_4$ while spin operator components are typed in as $I_{1x}$, $I_{1y}$ and $I_{1z}$ and no subscriptions are used. The “Applied NMR Pulse” section shows different pulses that can be applied to up to 4-spins with specified or arbitrary angles $\theta$. The value of $\theta$ in degrees can be entered in the “Substitute Theta” area for further calculation. The “J-Coupling” section gives the user the flexibility in applying the scalar coupling on four-spin groups independently. This is very useful because in many complex systems the scalar coupling among different spin groups might have different strengths and/or with different coupling durations. The drop-menu of the “J-Coupling” section includes different coupling durations (1/1J, 1/2J, 1/4J and 1/8J) that can be chosen by the user for the final calculation. Information about chemical shift on any spin group up to four (chosen from the drop-menu) can be obtained by clicking on the “Chemical Shift” button with the option to simplify the result if the time interval of the chemical shift is known. In addition to that, the GUI provides the option to eliminate any unobservable product operator that might appear in the final answer by using the “Spin Operator Elimination” section. By clicking on any of the nine product operators in this section the term (of the final answer) includes the chosen operator will be eliminated. This simplifies the final result and provides the user more information on the predicted NMR signal.

The output of the OP-GUI appears on the “Result” section which can be copied by using the normal copy-paste method for further investigation. It is important to mention that, the user can start from any known product operators to see the effect of different operations from NMR pulses, chemical shifts, or scalar coupling to get better interpretation of the spin operator transformation.

4. Using the PO-GUI in Teaching NMR Experiments An easy example is shown in the “Result” section of Figure 1 of a scalar coupling between spins 1 and 3 (in a three-spin system). This is applied on the initial operator $I_{1x}$, $I_{2x}$ without affecting $I_{2x}$, as expected from the spin operator formalism and density matrix calculation which both require a lot of calculation. This example shows that, the user can start from any product operator to apply pulses with different durations and directions, scalar couplings, and chemical shifts. This gives students an excellent way to understand the effect of such processes on particular product operator and give them opportunity to modify or design a particular NMR pulse sequence to obtain a required NMR signal output. Below we will show several complete examples using the obtained PO-GUI. The first example is the spin-echo experiment which of course can be taught using the typical vector model. Later on, we will show other examples that cannot be interpreted using the classical vector model but successfully explained by our PO-GUI.
4.1. Spin-echo Experiment

The product operator formalism can be used for prediction of the NMR signal in the spin-echo experiment. Here we will use our PO-GUI to obtain the expected outcome. Figure 2 shows the pulse sequence for this experiment which includes two pulses; one of 90°, and the other of 180°, separated by an interval of time.

The acquisition of the NMR signal starts after the second pulse. The user starts to use the OP-GUI by simply entering the initial spin operator \( I_{1z} \) in the input section of and then apply the pulse sequence (according to Figure 2) till gets to the final result. The solution steps are copied directly from the output section of the OP-GUI and are pasted below:

- Apply pulse 90_1x
- \( \uparrow \downarrow -I_{1y} \)
- Apply chemical shift
- \( \uparrow I_{1y}\cos(2\pi t\omega) - I_{1x}\sin(2\pi t\omega) \)
- Apply J_12 coupling
- \( \uparrow I_{1y}\cos(2\pi J_{12}t)\cos(2\pi t\omega) - I_{1x}\sin(2\pi J_{12}t)\sin(2\pi t\omega) - 2I_{1x}I_{2z}\sin(2\pi J_{12}t)\cos(2\pi t\omega) - 2I_{1y}I_{2z}\sin(2\pi J_{12}t)\sin(2\pi t\omega) \)
- Apply pulse 180_1x
- \( \uparrow 2I_{1y}I_{2z}\sin(2\pi t\omega)\sin(2\pi J_{12}t) - I_{1x}\sin(2\pi t\omega)\cos(2\pi J_{12}t) - 2I_{1x}I_{2z}\sin(2\pi J_{12}t)\cos(2\pi t\omega) - I_{1y}\cos(2\pi J_{12}t)\sin(2\pi t\omega) \)
- Apply J_12 coupling
- \( \uparrow -I_{1y}\cos(2\pi J_{12}t)\cos(2\pi t\omega) - I_{1x}\sin(2\pi J_{12}t)\sin(2\pi t\omega) \)
- \( \uparrow \) - substitution
- \( \uparrow -I_{1y} \)

It is obvious that the predicted NMR signal will be on the \(-y\) axis as expected if one uses the typical vector model method [1].
4.2. DEPT Experiment for Two-Spin System

In this section a more advanced NMR experiments will be demonstrated using our calculator. Obviously these cannot be explained by using the typical NMR vector model and require extensive calculation if one uses either density matrix or operator product formalism. Distortionless Enhancement by Polarization Transfer (DEPT) experiment is widely used to simplify spectra of carbonyl groups in complex molecules [6,15,16,17]. DEPT experiment results in an enhancement of the intensity of the low natural abundance X-nuclei (such as carbon) by using nuclei of high natural abundance (such as hydrogen). Both nuclei are irradiated with specific pulses but the acquisition is on the X-nuclei channel as shown below. In the following I1 refer to Hydrogen and I2 pulse sequence of spin groups starting with two -spin groups (CH) as demonstrate the use of our calculator for different number shown in Figure 3.

Figure 3. Distortionless Enhancement by Polarization Transfer (DEPT) pulse sequence

The intensity of the X-nuclei signal depends on the length of the last Hydrogen pulse (θ) and on the number of protons coupled to the X-nuclei. Below we will demonstrate the use of our calculator for different number of spin groups starting with two-spin groups (CH) as shown below. In the following I1 refer to Hydrogen and I2 refer to Carbon nuclei.

- **Initial Spin Operator**
- ▶ I1z
- Apply pulse 90_1y
- ▶ I1x
- Apply J_12 coupling
- ▶ I1x*cos(2*π*J_12*t) + 2*I1y*I1z*sin(2*π*J_12*t)
- Apply J_coupling time t=1/2J
- ▶ 2*I1y*I1z
- Apply pulse 90_2y
- ▶ I1x + I2x
- Apply J_13 coupling
- ▶ I1x*cos(2*π*J_13*t) + I2x*cos(2*π*J_13*t) + 2*I1y*I1z*sin(2*π*J_13*t) + 2*I2y*I1z*sin(2*π*J_13*t)
- Apply J_coupling time t=1/2J
- ▶ 2*I1y*I1z + 2*I2y*I1z
- Apply pulse 90_3y
- ▶ I1z + I2z
- Apply J_13 coupling
- ▶ I1z*cos(2*π*J_13*t) + I2z*cos(2*π*J_13*t) + 2*I1y*I2y*sin(2*π*J_13*t)
- Apply J_coupling time t=1/2J
- ▶ 2*I1y*I2y + 2*I2y*I2y
- Apply pulse θ_1x
- ▶ 2*I1y*I3y*(I1z*cos(θ) - I1y*sin(θ)) + I2z*cos(θ)*sin(θ) + 2*I1y*I3y*I2z*cos(θ)*sin(θ) + I2z*cos(θ)*sin(θ)
- Apply pulse θ_2x
- ▶ 2*I1y*I3y*(I1z*cos(θ) - I1y*sin(θ)) + I2z*cos(θ)*sin(θ) + 2*I1y*I3y*I2z*cos(θ)*sin(θ) + I2z*cos(θ)*sin(θ)
- Apply pulse 0_1x
- ▶ 2*I1y*I3y*(I1z*cos(θ) - I1y*sin(θ)) + I2z*cos(θ)*sin(θ) + 2*I1y*I3y*I2z*cos(θ)*sin(θ) + I2z*cos(θ)*sin(θ)
- Apply pulse 0_2x
- ▶ 2*I1y*I3y*(I1z*cos(θ) - I1y*sin(θ)) + I2z*cos(θ)*sin(θ) + 2*I1y*I3y*I2z*cos(θ)*sin(θ) + I2z*cos(θ)*sin(θ)
- Apply pulse J_13 coupling
- ▶ 2*I1y*I3y*(I1z*cos(θ) - I1y*sin(θ)) + I2z*cos(θ)*sin(θ) + 2*I1y*I3y*I2z*cos(θ)*sin(θ) + I2z*cos(θ)*sin(θ)
- Apply pulse J_23 coupling
- ▶ 2*I1y*I3y*(I1z*cos(θ) - I1y*sin(θ)) + I2z*cos(θ)*sin(θ) + 2*I1y*I3y*I2z*cos(θ)*sin(θ) + I2z*cos(θ)*sin(θ)
- Apply Pulse 90_4y
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply pulse θ_3x
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply pulse 0_3x
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply J_23 coupling
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply Pulse 90_5y
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply J_13 coupling
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply pulse 0_4x
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply J_13 coupling
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply pulse 0_5x
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply J_23 coupling
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply Pulse 90_6y
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- Apply J_13 coupling
- ▶ 2*I1y*I3y*I2z + 2*I2y*I3y*I1z
- The final NMR signal is modulated by sin(θ) as expected from the product operator formalism or density matrix calculation [14,18].

4.3. DEPT Experiment for Three-spin System

For three-spin group, I1 and I2 represent the two hydrogen spin groups (in CH2) and I3 represents carbon (in CH2) and the scalar coupling is between I1 and I2. I3. The initial spin operator is the two hydrogen groups I1 and I2 and the scalar coupling is between I1 and I2. The full solution, using the OP-GUI, is shown below:

- **Initial Spin Operator**
- ▶ I1z + I2z
- Apply pulse 90_1y
- ▶ I1x + I2x
- Apply pulse 90_2y
- ▶ I1x + I2x
- Apply J_13 coupling
- ▶ I1x*cos(2*π*J_13*t) + I2x*cos(2*π*J_13*t) + 2*I1y*I1z*sin(2*π*J_13*t)
- Apply J_coupling time t=1/2J
- ▶ 2*I1y*I1z + 2*I2y*I1z
- Apply J_13 coupling
- ▶ 2*I1y*I1z + 2*I2y*I1z
- Apply pulse 90_3y
- ▶ 2*I1y*I1z + 2*I2y*I1z
- Apply J_13 coupling
- ▶ 2*I1y*I1z + 2*I2y*I1z
- Eliminate the non-observable operator I_2x
DEPT experiment is modulated by hydrogen pulse duration, for different spin groups produce. On the other hand, for proton pulse of 135°, CH proton pulse, only singly protonated carbon (in CH) will and CH3 will phase up while CH2 will phase down. In this case is: pulse sequence four-spin groups (CH3). The final answer of changing the pulse duration (by changing 4 which shows how the final NMR signal changes by the previous examples is graphically represented in Figure 4.

```
2*I3x*I1y*sin(2*π*J_23*t)*sin(0)*t - 2*I3y*cos(0)*sin(2*π*J_23*t)*sin(0) + 4*I2y*I13y*11z*cos(2*π*J_13*t)*cos(0)*t - 2*I3x*I1x*cos(2*π*J_13*t)*cos(0)*t - 2*I3y*cos(0)*sin(0)*t - 2*I3x*I1y*cos(0)*sin(0) - 2*I3x*I1z*cos(2*π*J_13*t)*cos(2*π*J_23*t)*cos(0)*sin(0) + 8*I1y*I2y*I3y*cos(θ)*sin(θ) - 2*I3x*I1x*cos(θ)^2 + 2*I3x*I2y*sin(θ)^2 - 2*I3y*cos(θ)*sin(2*π*J_13*t)*sin(2*π*J_23*t)*sin(θ) + 2*I3x*I1y*sin(θ)^2 - 2*I3x*I1z*cos(2*π*J_13*t)*cos(θ)*sin(2*π*J_23*t)*sin(θ) + 4*I1y*I3y*I2z*cos(2*π*J_23*t)*cos(θ)*sin(θ) + 4*I2y*I3y*I1z*cos(2*π*J_13*t)*cos(θ)*sin(θ) + 4*I1y*I3y*I2z*cos(2*π*J_23*t)*cos(θ)*sin(θ) + 4*I2y*I3y*I1z*cos(2*π*J_13*t)*cos(θ)*sin(θ).```

Apply J_coupling time \( t = \frac{1}{2J} \)

```
* I3y*cos(θ)*sin(θ)
* I3x*I1y*cos(θ)*sin(θ)
* I3x*I1z*cos(2*π*J_13*t)*cos(θ)*sin(θ)
* I3x*I1z*cos(2*π*J_13*t)*cos(θ)*sin(θ)
* I3x*I2z*cos(2*π*J_23*t)*cos(θ)*sin(θ)
* I3x*I2z*cos(2*π*J_23*t)*cos(θ)*sin(θ)
```

The final result for the case of three-spin system in DEPT experiment is modulated by \( \cos(θ)\sin(θ) \). Of course the user can go one step further in using the same pulse sequence four-spin groups (CH3). The final answer in this case is:

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* 3.0*I4y*cos(θ)^2*sin(θ)
```

Which indicates that the result is modulated by \( (\cos(θ))^2\sin(θ) \). Both results are predicted by density matrix and product operator formalism [18]. The final answer of the previous examples is graphically represented in Figure 4 which shows how the final NMR signal changes by changing \( θ \) in the DEPT pulse sequence. For example, for spectra acquired at 45°, all the protonated signals will phase up. In the case of 90° proton pulse, only singly protonated carbon (in CH) will produce. On the other hand, for proton pulse of 135°, CH and CH3 will phase up while CH2 will phase down.

### Figure 4. NMR signal intensity in DEPT experiment versus last hydrogen pulse duration, for different spin groups

#### Notes
All the source files, executable files and the OP-GUI are available for free, and can be obtained by writing an email to the corresponding author of this article.

#### References

[1] Benn, R., H. Günther, Angew. Chem. 22(5): 350-380, 1983.
[2] Abragam, A, The Principles of Nuclear Magnetism. London: Oxford University Press, 1963.
[3] Slichter, C, Principles of Magnetic Resonance, 2nd Ed. New York: Springer-Verlag, 1990.
[4] Goldman, M, Quantum Description of High-Resolution NMR in Liquids, Oxford: Clarendon Press, 1990.
[5] Ernst, R. R., G. Bodenhausen, A. Wokaun, Principles of Nuclear Magnetic Resonance in One and Two Dimensions, Oxford: Clarendon Press, 1987.
[6] Sørensen O.W., G.W. Eich, M-H. Levitt, G. Bodenhausen, R.R. Ernst, Prog. NMR Spectrosc. 16: 163-192, 1983.
[7] Packer K.J., & K. M. Wright, Molecular Physics. 50(4): 797-813, 1983.
[8] Howarth M.A., L.Y. Lian, G.E. Hawkes, & K.D. Sales, J. Magn. Reson. 68 (3): 433-452, 1986.
[9] Chandrakumar N., S. Subramanian, Modern Techniques in High Resolution FT NMR, New York: Springer, 1987.
[10] Hore J.P., R.J. Jones, S. Wimperis, NMR: The Toolkit, New York: Oxford Univ. Press, 2000.
[11] Van deVen F.J.M., & C.W. Hilbers, J. Magn. Reson. 54 (3): 512-520, 1983.
[12] Shriraj, J, Concepts Mag. Reson. 4(1): 1-33, 1992.
[13] Wei G., & R. F. Snider, Magn. Reson. 7(2): 153-163, 1995.
[14] Sørensen O. W., Prog. NMR Spectrosc. 21:503-569, 1989.
[15] Nolis P., T. Parella, Curr. Analy. Chem. 3(1): 47-68, 2007.
[16] Doddrell D.M., D.T. Pegg, & M.R. Bendall (1982). J. Magn. Reson. 54:1-15.
[17] Chandrakumar, N. J. Magn. Reson. 60(1): 28-36, 1984.
[18] Gheorghe D. Mateescu and Adrian Valerin, 2D NMR Density Matrix and Product Operator Treatment, Prentice Hall, 2003.