NuSTAR and XMM–Newton broad-band spectrum of SAX J1808.4–3658 during its latest outburst in 2015

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ABSTRACT
The first discovered accreting millisecond pulsar, SAX J1808.4–3658, went into X-ray outburst in 2015 April. We triggered a 100 ks XMM–Newton ToO, taken at the peak of the outburst, and a 55 ks NuSTAR ToO, performed 4 d apart. We report here the results of a detailed spectral analysis of both the XMM–Newton and NuSTAR spectra. While the XMM–Newton spectrum appears much softer than in previous observations, the NuSTAR spectrum confirms the results obtained with XMM–Newton during the 2008 outburst. We find clear evidence of a broad iron line that we interpret as produced by reflection from the inner accretion disc. For the first time, we use a self-consistent reflection model to fit the reflection features in the NuSTAR spectrum; in this case, we find a statistically significant improvement of the fit with respect to a simple Gaussian or diskline model to fit the iron line, implying that the reflection continuum is also significantly detected. Despite the differences evident between the XMM–Newton and NuSTAR spectra, the smearing best-fitting parameters found for these spectra are consistent with each other and are compatible with previous results. In particular, we find an upper limit to the inner disc radius of \( \sim 12 R_g \). In all the cases, a high inclination angle (\( > 50^\circ \)) of the system is required. This inclination angle, combined with measurements of the radial velocity of the optical companion, results in a low value for the neutron star mass (\(< 0.8 M_\odot \)), a result that deserves further investigation.

Key words: line: formation – line: identification – stars: individual: SAX J1808.4–3658 – stars: magnetic fields – stars: neutron – X-rays: binaries – X-rays: general.

1 INTRODUCTION
An accreting millisecond pulsar (hereafter AMSP) is a neutron star (NS) accreting mass from a low-mass companion star (\( \leq 1 M_\odot \)) and rotating at millisecond periods, as it is witnessed by the coherent pulsations in its X-ray light curve. This phenomenon is relatively rare among low-mass X-ray binaries (LMXBs) and is caused by the NS magnetic field, which is strong enough (given the accretion rate) to effectively funnel the accreting matter on to the magnetic poles. Most of the AMSPs are transient X-ray sources with recurrence times between two and more than 10 yr, and their outbursts usually last from a week to two months at most. SAX J1808.4–3658 (J1808 hereafter) is the first discovered AMSP (Wijnands & van der Klis 1998). The observed X-ray coherent pulsations are a fundamental probe of its dynamical and orbital state. A 60 ks long XMM–Newton observation of this source revealed a broad (\( FWHM \sim 2 \) keV) emission line at the energy of iron fluorescence emission (Papitto et al. 2009, P09 hereafter). This broad line has been confirmed by Suzaku, which observed the source the day after with compatible spectral parameters within the errors (Cackett et al. 2009). Such broadened features are ubiquitous among accreting compact objects. First discovered in active galactic nuclei (see e.g. Fabian et al. 2000, for a review), these were subsequently observed in Galactic X-ray binaries containing black holes (e.g. Miller et al. 2004) or NS (e.g. Cackett et al. 2010). To explain the broadness of these features, it is usually assumed that they originate from reprocessed emission of the accretion disc, illuminated by the primary Comptonized spectrum. Experimental results support the view that, in several cases, the accretion disc is truncated at few gravitational radii from the central mass. Here, Doppler shifts and relativistic boosting in a fast rotating plasma, along with the gravitational red-shift caused by the strong gravitational field of the compact object, distort the line profile asymmetrically, broadening its shape up to 1 keV. Their shape
thus depends on the geometry of the reflecting region of the disc, on the Keplerian velocity in the disc, and on its ionization state. In this case, the line parameters allow to derive several important physical features with unprecedented accuracy. We just mention here the inclination of the disc with respect to the line of sight, which, in some cases (e.g. Di Salvo et al. 2009), is derived with an accuracy of just a few degrees, and, most important, the inner disc radius, which, in some sources, is determined within 1–2Rg (where Rg = GMc2 is the gravitational radius). For these systems, the compelling discovery of a fast spinning (extreme Kerr) black hole has been claimed based on the fact that the inner disc radius derived from the fit of the iron line lies below 6Rg, which is the last stable orbit for a non-rotating (Schwarzschild) black hole (see e.g. Fabian 2005 for a review). Moreover, iron lines play a particularly important role if observed in pulsars, as they carry information about the magnetospheric radius. This radius indicates where in the disc stresses exerted by the magnetic field start to remove angular momentum from the matter. According to accretion theory, it depends on the magnetic field strength, on the accretion rate, and on the details of the interaction between the magnetic field and the accreting matter. Studies of the iron line profile could be hence a very powerful diagnostic tool to investigate the behaviour of matter in extreme gravitational fields and to effectively constrain the compactness (mass to radius ratio) of NSs or the spin parameter of black holes in X-ray binaries. However, some authors argued against the disc origin of broad iron lines, addressing the asymmetric broadening of these lines as caused by Compton down-scattering in a outflowing wind (e.g. Titarchuk, Laurent & Shaposhnikov 2009; see, however, Cackett & Miller 2013) or to pile-up distortions in CCD spectra (Ng et al. 2010; see, however, Miller et al. 2010 for extensive simulations of pile-up effects). Strong pile-up effects on the line profile can be excluded; in fact, it has been shown that there is a good agreement between spectral parameters derived from CCD-based spectra with those derived from gas-based spectrometers (see e.g. Cackett et al. 2012; Egron et al. 2013). More recently, observations with NuSTAR, which does not suffer from pile-up, have confirmed that iron line profiles in most LMXBs appear broad and asymmetric (see e.g. Miller et al. 2013; Degenaar et al. 2015; King et al. 2016; Sletor et al. 2016; Ludlam et al. 2017; and references therein).

Nevertheless an asymmetric broad iron line may be the effect of either reflection from a Keplerian disc or Compton broadening and/or down-scattering. However, if the origin of this line is from disc reprocessing, one would also expect the presence of a spectral hump between 20 and 40 keV due to Compton scattering of the primary spectrum by the disc. Indeed this reflection hump has been observed in the spectrum of some NS LMXBs (e.g. Yoshida et al. 1993; Piraino et al. 1999; Barrett et al. 2000; Fiacchini et al. 2007; Di Salvo et al. 2015), usually with reflection amplitudes (defined in terms of the solid angle Ω/2π subtended by the reflector as seen from the corona) lower than 0.3, indicating a spherical geometry of the illuminating corona. Therefore, the use of broad-band, moderately high-energy resolution spectra, together with the use of self-consistent reflection models able to simultaneously fit the iron line profile and the related Compton hump, are fundamental in order to probe the consistency of the parameters of the whole reflection component and the reliability of the disc parameters derived from the so-called Fe-line method (see also Matranga et al. 2017).

To date 22 AMSPs have been discovered since 1998 (see Patruno & Watts 2012; Campana & Di Salvo 2018 for reviews), the last ones discovered in 2018 (IGR J17379−3747, Sanna et al. 2018a, and IGR J17591−2342, Sanna et al. 2018b), and three transitional pulsars, including IGR J18245−2452, the only transitional pulsars that went into an X-ray outburst (Papitto et al. 2013b). Spectral studies at high resolution are fundamental in order to characterize their emission during outbursts (see e.g. Poutanen 2006 for a review). Besides an energetically dominating Comptonized component, one or two soft components are often detected if enough statistics and spectral resolution is guaranteed. These soft components are interpreted as the emission arising from the accretion disc and from the NS hot spots. One of the most frequently recurring AMSP is SAX J1808.4−3658 that goes into outburst more or less regularly every 2–3 yr. The light-curve shape is also very regular with outburst peak fluxes between 60 and 80 mCrab (2–10 keV), and a subsequent slow decay on a time-scale of 10–15 d until the source decays below 16 mCrab and enters a low-luminosity flaring state. Its spin frequency is constantly decreasing at a rate (∼5 × 10−16 Hz s−1) compatible with the one expected from dipole emission of a ∼1010 G rotating pulsar (Hartman et al. 2009; Sanna et al. 2017a).

While this is the most probable explanation for such a deceleration, it was also proposed that the NS spin-down may be due to the emission of continuous gravitational waves (Bildsten 1998). This source is also characterized by a puzzling fast orbital period evolution (Di Salvo et al. 2008; Burderi et al. 2009; Hartman et al. 2009; Patruno et al. 2012; Sanna et al. 2017a). The time-scale of this evolution is so short (few × 106 yr) that a non-conservative evolution (e.g. the so-called radio-ejection model; Burderi et al. 2001) or large short-term angular momentum exchange between the mass donor and the orbit, caused by gravitational quadrupole coupling due to variations in the oblateness of the companion, are indicated as possible explanations (see Sanna et al. 2017a for a discussion). Such a conclusion might establish an evolutionary link between (at least some) AMSPs and the so-called black widow pulsars. To be confirmed, this scenario needs more measures, as quasi-cyclic period variations are expected in binaries (Arzoumanian, Fruchter & Taylor 1994).

SAX J1808.4−3658 was observed with XMM–Newton during its 2008 outburst (see P09 for details). During this 60 ks observation a broad iron line (σ = 1.1 ± 0.1 keV) was detected at an energy of ∼6.4 keV. Modelling this line according to the disc reflection hypothesis (diskline model) allowed P09 to place the inner radius of the reflecting region between 6 and 12Rg and the outer radius at about 200Rg. As SAX J1808.4−3658 is a pulsar, the inner radius can be interpreted as the magnetospheric radius, which is predicted by accretion theories to lie exactly between the coronation radius, which in the case of SAX J1808.4−3658 is at about 30 km, and the NS surface in order to allow the observation of X-ray coherent pulsations from the source (Ghosh & Lamb 1979). The statistics of the 2008 observation was nevertheless too low to discriminate between a symmetric and an asymmetric profile, although a disc interpretation is strongly favoured, as Compton broadening is not a viable explanation in a source whose Comptonized component originates at a large temperature (kT ≥ 30 keV, see e.g. Gierliński, Done & Barret 2002).

The main goal of this paper is to characterize the broad-band X-ray spectrum of the transient AMSP SAX J1808.4−3658, and in particular the iron line and other reflection features, with a larger statistics than in previous observations, taking advantage from the large exposure of the 80 ks–XMM–Newton observation and the broad-band coverage provided by the NuSTAR observation performed during the latest outburst from the source. This allows us to acquire the source broad-band spectrum and to constrain the reflection component properties such as the broad Fe emission line together with the expected Compton hump, therefore allowing to infer the properties of the accretion flow close to the NS. We report here on a detailed study of the reflection features and the fit, with a
self-consistent reflection model, of both the iron line profile and the associated Compton reflection hump at energies above 10 keV. In this spectrum, which includes hard-band data (up to 50–70 keV), the overall fractional amount of reflection is well determined by fitting the Compton hump. We can therefore test whether the observed iron line is consistent with this fractional amount of reflection. In this way, we can confirm independently (fitting a different outburst state and using different instruments) the inner disc parameters already obtained with XMM–Newton and Suzaku for the 2008 outburst.

2 OBSERVATIONS

SAX J1808.4–3658, went into X-ray outburst in April 2015, after more than 3 yr from its previous outburst in 2008. SAX J1808.4–3658 was observed by XMM–Newton on 2015 April 11 (ObsID: 0724490201) for a total observing time of about 110 ks, as a result of an anticipated target of opportunity (ToO) observation approved to observe the source during an outburst. During the observation, an abrupt drop-off of the count rate was visible in the EPIC/pn light curve caused by a problem with the Star Tracker, which led the satellite to be off-target for about seven hours, resulting in 80 ks effective on-source exposure. During the observation, the EPIC/pn camera was operated in timing mode to prevent photon pile-up and to allow the analysis of the coherent and aperiodic timing behaviour of the source (see Sanna et al. 2017a, for the timing analysis of these data). The EPIC/MOS cameras were switched off during the observation in order to allocate as much telemetry as possible to the pn in the case of high count rate, and the reflection grating spectrometer (RGS) was operated in the standard spectroscopy mode.

We have extracted source, background spectra and response matrices using the science analysis software (SAS) v.16.1.0, setting the parameters of the tools accordingly. We produced a calibrated photon event file using reprocessing tools epproc and rgsproc for the pn and RGS data, respectively. Before extracting the spectra, we searched for contaminations due to background solar flares detected in the 10–12 keV Epic-pn light curve, but we did not find periods with high background.

We also looked for the presence of pile-up in the pn spectrum; we have run the task epatplot and we did not find any significant contamination. The count-rate registered in the pn observation was around 450 c s⁻¹, which is below the limit for avoiding contamination by pile-up. Therefore, the source spectra were extracted from a rectangular region between RAWX ≥ 23 and RAWX ≤ 49. We selected only events with PATTERN ≤ 4 and FLAG = 0 as a standard procedure to eliminate spurious events. We extracted the background spectrum from a region included between RAWX ≥ 5 and RAWX ≤ 10. Finally, using the task rgscombine we have obtained the added source spectrum for RGS1+RGS2, the relative added background spectrum along with the relative response matrices. We have fitted RGS spectrum in the 0.5–1.8 keV energy range, whereas the pn spectrum in the 2.4–10 keV energy range. The spectral analysis of the XMM–Newton/EPIC-pn spectrum was restricted to 2.4–10 keV to exclude the region around the detector Si K-edge (1.8 keV) and the mirror Au M-edge (2.3 keV) that could affect our analysis, as well as to exclude possible residuals of instrumental origin below 2 keV that usually appear in case of bright sources observed in timing mode (see e.g. D’Ai et al. 2010; Egron et al. 2013).

In this paper, we also analyse data collected by the NuSTAR satellite. A ToO was requested to observe the source during the 2015 outburst in order to complement the XMM–Newton spectrum with high-energy coverage. The NuSTAR observation, obtained as Discretionary Time, was performed 4 d after the XMM–Newton observation, on 2015 April 15 (ObsID: 90102003002), for a total observing time of 55 ks, resulting in roughly 49 ks of exposure per telescope. Science data were extracted using NuSTARDAS (NuSTAR data analysis software) v1.7.1. Source data have been extracted from a circular region with 120 arcmin radius, whereas the background has been extracted from a circular region with 60 arcmin radius in a position far from the source. With the aim to get ‘STAGE 2’ events clean, we run the nupipeline with default values of the parameters and with the parameter SAAMODE set to optimized in order to eliminate high background events caused by the SAA passage. The average count rate during the NuSTAR observation was ∼35–40 c s⁻¹.

A type-I burst is present during the NuSTAR observation, at about 14 ks from the beginning of the observation. The burst profile is not complete since the rise phase was in coincidence with a gap in the light curve. The peak of the burst seems to reach approximately 200 c s⁻¹, about a factor of 4 the level of the persistent emission, and it lasted about 200 s. We eliminated a time interval of 250 s starting from 5 s before the rise of the burst, and checked that the spectra did not change significantly. Spectra for both detectors, FPMA and FPMB, were extracted using the nuproducts command. Corresponding response files were also created as output of nuproducts. A comparison of the FPMA and FPMB spectra, indicated a good agreement between them. We have therefore created a single added spectrum, with its corresponding background spectrum, ancillary response file and matrix response, using the addascaspec command. In this way, we obtained a summed spectrum for the two NuSTAR modules (see e.g. Miller et al. 2013). We fitted this spectrum in the 3–70 keV energy range, where the emission from the source dominates over the background.

In Fig. 1, we show the light curve during the 2015 outburst of SAX J1808.4–3658 obtained with the instruments, XRT and BAT, on board the Swift satellite. In this light curve, the dates of the XMM–Newton and NuSTAR observations are indicated with stars.

3 SPECTRAL ANALYSIS AND RESULTS

For spectral analysis, the EPIC/pn energy channels were grouped in order to have at least 20 counts per energy channel and to oversample the energy resolution element by no more than three channels.

Figure 1. Swift/BAT and XRT light curve during the 2015 outburst of SAX J1808.4–3658. The dates of the XMM–Newton and NuSTAR observations are indicated with stars.
RGS and NuSTAR spectra were grouped in order to have at least 20 counts per energy channel. The X-ray spectral package we use to model the observed emission is XSPEC v.12.9.1. For each fit, we have used phabs in XSPEC to model the photoelectric absorption due to neutral matter, with photoelectric cross-sections from Balucinska-Church & McCammon (1992) and element abundances from Anders & Grevesse (1989).

### 3.1 The NuSTAR spectrum

We have started analysing the broad-band spectrum acquired with NuSTAR in the energy range of 3–70 keV. We fit the continuum emission with a soft blackbody and the Comptonization model nthComp in XSPEC (Zycki, Done & Smith 1999), modified at low energy by photoelectric absorption caused by neutral matter. This is a standard model to fit the broad-band continuum emission in NS LMXBs of the atoll class both in the soft and in the hard states (see e.g. Piraino et al. 2007; Di Salvo et al. 2009; Egron et al. 2013; Sanna et al. 2013; Di Salvo et al. 2015; and references therein) and provides also a good fit to the broad-band continuum emission in AMSPs (see e.g. Papitto et al. 2010, 2013a, 2016; Sanna et al. 2017b).

Because of the lack of sensitivity of NuSTAR at low energies, we had to fix the photoelectric equivalent hydrogen column density at $10^{22}$ cm$^{-2}$, which is the best-fitting value for this parameter obtained for the X-ray spectrum of SAX J1808.4–3658 observed by XMM–Newton during the 2008 outburst (cf. P09); in particular, the previous XMM–Newton spectrum also gave a quite small outer disc radius of 140–360 $R_g$ and a high inclination angle of the system with respect to the line of sight, $i \geq 70^\circ$. The best-fitting parameters are reported in Table 1. These parameters are very similar (compatible well within the errors) to the best-fitting parameters of the iron line component obtained from the XMM–Newton spectrum of SAX J1808.4–3658 during the 2008 outburst (cf. P09); in particular, the previous XMM–Newton spectrum also gave a quite small outer disc radius of 140–360 $R_g$ and a high inclination angle of $i \geq 60^\circ$.

The broad iron line profile seems to be compatible with reflection of the main Comptonization spectrum off the accretion disc, where the broadness of the profile is induced by the fast motion of the matter in the inner disc, and related (mildly) relativistic effects. However, if the iron line is produced by reflection then a Compton hump should be visible in the high energy part of the spectrum given that the source is in a hard state. To test this hypothesis we tried to substitute the diskline component with a self-consistent reflection model to fit both the iron line and the Compton hump. In particular, we used the relxillCp model (Gar{c}a et al. 2014), which models the irradiation of the accretion using an nthComp Comptonization continuum (Cp). Note that at the moment it is not possible to fit the temperature of the seed photons for the Comptonization component, that is fixed at 50 eV (Thomas Dauser, private communication). This should be anyway a good approximation for the case of SAX J1808.4–3658 given the low value we find for this component (see Tables 1 and 2).

The relxillCp model allows to determine the reflection fraction, defined as ratio of intrinsic intensity emitted towards the disc com-
pared to that escaping to infinity (see Dauser et al. 2016 for more details), the inclination angle of the system and the ionization parameter of the disc, given by log \( \xi \), where \( \xi = L_{2}\sqrt{r_{n}/r^{2}} \), where \( L_{2} \) is the luminosity of the incident X-ray spectrum, \( r_{n} \) is the electron number density in the emitting region, and \( r \) is the distance between the illuminating source and the emitting region. This reflection model includes the smearing component \( \text{relcom}^{1} \) in order to take into account Doppler and relativistic effects caused by the fast motion of the matter in the disc. Unless specified otherwise, the two emissivity indices (defined in order to be negative as in the case of the \( \text{diskline} \) parameter \( \text{Betor} \)) have been constrained in order to assume the same value and the dimension-less spin parameter \( a \) has been fixed to 0.

This model gives a good fit to the data, corresponding to a \( \chi^{2}/\text{dof} = 1300/1320 \). We find that fixing the iron abundance, \( A_{Fe} \), at two times the solar value the fit slightly improved returning a \( \chi^{2}/\text{dof} = 1297/1320 \), lower with respect to the previous fit with a \( \text{diskline} \), corresponding to a \( \Delta \chi^{2} = 9 \) with one extra degree of freedom. Letting the iron abundance free to vary, we find that its uncertainty could not be determined because the \( \chi^{2} \) was quite insensitive to its value; probably the energy resolution of \( \text{NuSTAR} \) is not enough to constrain this parameter. The spectral results are reported in Table 1, and in Fig. 3 (right-hand panel), we show the \( \text{NuSTAR} \) spectrum, the best-fitting model, and the residuals in units of \( \sigma \) with respect to the best-fitting model. We extrapolated the total 0.5–200 keV observed luminosity of the source during the \( \text{NuSTAR} \) observation, corresponding to \( (3.78 \pm 0.15) \times 10^{36} \text{ erg s}^{-1} \), assuming a distance to the source of 3.5 kpc (Galloway & Cumming 2006).

### 3.2 The \( \text{XMM–Newton} \) spectrum

In order to check the results obtained from the \( \text{NuSTAR} \) spectrum, we have fitted separately the \( \text{XMM–Newton} \) spectra (RGS and pn, energy range of 0.6–10 keV), using the same continuum model. Again, fitting only the continuum results in an unacceptable fit, with \( \chi^{2}/\text{dof} = 3489/1458 \), and clear residuals are present at the iron line energy and lower energies, at \( \sim 2.6 \text{ keV}, \sim 3.3 \text{ keV}, \text{ and } \sim 4 \text{ keV} \) (see Fig. 2, right-hand panel). These low-energy residuals are similar to those observed in other bright LMXBs of the atoll class in the soft state, as 4U 1705–44 (see e.g. Di Salvo et al. 2009; Ergon et al. 2013) or GX 3 + 1 (e.g. Piraino et al. 2012; Pintore et al. 2015). We therefore added to the continuum model four \( \text{diskline} \) components to fit the iron line and the other low energy features. The smearing parameters of the \( \text{diskline} \) fitting the low-energy lines were fixed to be the same of those of the \( \text{diskline} \) fitting the iron line. In this

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1More details can be found in the following webpage: http://www.sternwar.de.uni-erlangen.de/dauser/research/relxill/.

### Table 1. The best-fitting parameters of the spectral fitting of the \( \text{NuSTAR} \) (3–70 keV energy band) spectrum of SAX J1808.4–3658.

In all the cases, the continuum emission is described by a combination of a blackbody and the Comptonization component \( \text{nthComp} \), modified at lower energy by photoelectric absorption from neutral matter modeled with \( \text{phabs} \). The reflection component is fitted with a \( \text{diskline} \) component, or with the self-consistent reflection model \( \text{relxillCp} \). The blackbody luminosity is given in units of \( L_{36}/D_{10}^{2} \), where \( L_{36} \) is the bolometric luminosity in units of \( 10^{36} \text{ erg s}^{-1} \) and \( D_{10} \) the distance to the source in units of 10 kpc. The blackbody radius is calculated in the hypothesis of spherical emission and for a distance of 3.5 kpc. Smearing indicates the smearing component of the \( \text{diskline} \) and \( \text{relxillCp} \) models, respectively. Flux in the \( \text{nthComp} \) component is calculated in the 1–10 keV range, while total flux is calculated in the 1.6–70 keV band. Uncertainties are given at 90% confidence level. INDEF means that the error on the parameter could not be calculated being the \( \chi^{2} \) quite insensitive to its value.

| Component | Parameter | \( \text{NuSTAR} \) (3–70 keV) | \( \text{relxillCp} \) (3–70 keV) |
|-----------|-----------|-------------------------------|-------------------------------|
| \( \text{phabs} \) | \( N_{H} \times 10^{22} \text{ cm}^{-2} \) | 0.21 (fixed) | 0.21 (fixed) |
| \( \text{bbody} \) | \( kT_{BB} \) (keV) | 0.697 ± 0.015 | 0.672 ± 0.007 |
| \( \text{bbody} \) | \( L_{BB} \) (\( L_{36}/D_{10}^{2} \)) | 2.14 ± 0.09 | 1.79 ± 0.04 |
| \( \text{bbody} \) | \( R_{BB} \) (km) | 2.93 ± 0.14 | 2.88 ± 0.07 |
| \( \text{nthComp} \) | \( kT_{seed} \) (keV) | <0.29 | – |
| \( \text{nthComp} \) | \( \Gamma \) | 1.819 ± 0.006 | 1.868 ± 0.015 |
| \( \text{nthComp} \) | \( kT_{r} \) (keV) | 3.95 ± 0.13 | 0.21 (fixed) |
| \( \text{nthComp} \) | Flux \( (10^{-10} \text{ erg cm}^{-2} \text{ s}^{-1}) \) | 9.5 ± 1.4 | – |
| \( \text{diskline} \) | \( E_{\text{line}} \) (keV) | 6.56 ± 0.10 | – |
| \( \text{diskline} \) | \( I_{\text{line}} \) \( (10^{-14} \text{ ph cm}^{-2} \text{ s}^{-1}) \) | 8.6 ± 1.2 | – |
| \( \text{diskline} \) | \( E_{W} \) (eV) | 124 ± 19 | – |
| \( \text{Smearing} \) | \( \text{Betor} \) | –2.04 ± 0.19 | –1.95 ± 0.12 |
| \( \text{Smearing} \) | \( R_{in} \) (GMic{\(^2\)) | <7 | 14.9 ± 2.5 |
| \( \text{Smearing} \) | \( R_{out} \) (GMic{\(^2\)) | 520.55 ± 240 | 1000 (INDEF) |
| \( \text{Smearing} \) | \( \text{Incl} \) (deg) | >70 | 50.2 ± 2.5 |
| \( \text{relxillCp} \) | \( \text{Reffrac} \) | – | 0.62 ± 0.04 |
| \( \text{relxillCp} \) | \( \text{Feabund} \) | – | 2.1 ± 0.04 |
| \( \text{relxillCp} \) | \( \log \xi \) | 2.76 ± 0.07 | 3.73 ± 0.07 |
| \( \text{relxillCp} \) | Norm \( (\times 10^{-3}) \) | – | 0.14 |
| Total | Flux \( (10^{-9} \text{ ergs cm}^{-2} \text{ s}^{-1}) \) | 2.01 ± 0.12 | 2.02 ± 0.09 |
| Total | \( \chi^{2} \) (dof) | 1305.68 (1319) | 1296.66 (1320) |
Table 2. The best fit parameters of the spectral fitting of the XMM–Newton (0.6–10 keV energy band) and XMM–Newton + NuSTAR (0.6–70 keV energy band) spectra of SAX J1808.4–3658. In all the cases, the continuum is described by a combination of a blackbody and the Comptonization component nthComp, modified at lower energy by photoelectric absorption from neutral matter modeled with phabs. The reflection component is fitted with diskline components or with the self-consistent reflection model relxillCp. The blackbody luminosity is given in units of $L_{36}/D^2_0$, where $L_{36}$ is the bolometric luminosity in units of $10^{36}$ erg s$^{-1}$ and $D_0$ the distance to the source in units of 10 kpc. The blackbody radius is calculated in the hypothesis of spherical emission and for a distance of 3.5 kpc. Fluxes in the nthComp component are calculated in the 1–10 keV range, while total flux is calculated in the 0.6–10 keV band for the XMM–Newton spectrum and in the 1.6–70 keV band for the NuSTAR spectrum. Uncertainties are given at 90 per cent confidence level.

| Component | Parameter | relxillCp XMM–Newton (0.6–10 keV) | relxillCp XMM–Newton (0.6–70 keV) | relxillCp XMM–Newton (0.6–10 keV) |
|-----------|-----------|---------------------------------|---------------------------------|---------------------------------|
| phabs     | $N_H$ ($\times 10^{22}$ cm$^{-2}$) | 0.164 ± 0.006                  | 0.142 ± 0.011                  | 0.146 ± 0.011                  |
| bbody     | $kT_{BB}$ (keV)               | 0.103 ± 0.002                  | 0.109 ± 0.003                  | 0.112$^{+0.003}_{-0.002}$     |
| bbody     | $L_{BB}$ ($L_{36}/D^2_0$)    | 10.3$^{+0.9}_{-0.8}$         | 4.4$^{+1.2}_{-0.9}$           | 5.4 ± 1.1                      |
| bbody     | $R_{BB}$ (km)                 | 295 ± 17                      | 172 ± 25                      | 180 ± 20                      |
| nthComp   | $kT_{seed}$ (keV)             | 0.15$^{+0.02}_{-0.04}$        | –                              | –                              |
| nthComp   | $\Gamma$                     | 1.904 ± 0.008                 | 1.78 ± 0.04                   | 1.73 ± 0.03                   |
| nthComp   | $kT_{e}$ (keV)                | 4.7 ± 0.3                     | 7.2 ± 0.8                     | 6.2 ± 0.5                     |
| nthComp   | Flux ($10^{−10}$ erg cm$^{-2}$ s$^{-1}$) | 17.4 ± 0.9                  | –                              | –                              |
| diskline  | $E_{line}$ (keV)              | 2.665 ± 0.012                 | 2.666 ± 0.015                 | 2.664 ± 0.016                 |
| diskline  | $\lambda_{line}$ ($\times 10^{-4}$ ph cm$^{-2}$ s$^{-1}$) | 21.5 ± 1.9                    | 21 ± 3                        | 18 ± 3                         |
| diskline  | $E_{qW}$ (keV)                | 41 ± 6                        | 42 ± 6                        | 35 ± 11                       |
| diskline  | $E_{line}$ (keV)              | 3.394 ± 0.019                 | 3.31 ± 0.02                   | 3.28 ± 0.02                   |
| diskline  | $\lambda_{line}$ ($\times 10^{-4}$ ph cm$^{-2}$ s$^{-1}$) | 15.0 ± 1.5                    | 16 ± 3                        | 11.6 ± 1.6                    |
| diskline  | $E_{qW}$ (keV)                | 38 ± 6                        | 50 ± 8                        | 33 ± 11                       |
| diskline  | $E_{line}$ (keV)              | 3.99 ± 0.04                   | 4.06 ± 0.04                   | 3.99 ± 0.05                   |
| diskline  | $\lambda_{line}$ ($\times 10^{-4}$ ph cm$^{-2}$ s$^{-1}$) | 8.0$^{+0.7}_{-0.5}$          | 9.5 ± 1.3                     | 6.3$^{+1.1}_{-0.9}$           |
| diskline  | $E_{qW}$ (keV)                | 30 ± 4                        | 42 ± 7                        | 31 ± 9                        |
| diskline  | $E_{line}$ (keV)              | 6.70 ± 0.05                   | –                              | –                              |
| diskline  | $\lambda_{line}$ ($\times 10^{-4}$ ph cm$^{-2}$ s$^{-1}$) | 5.4 ± 0.6                     | –                              | –                              |
| diskline  | $E_{qW}$ (keV)                | 58 ± 8                        | –                              | –                              |
| Smearing  | $\delta$                      | −2.16 ± 0.10                  | −2.20 ± 0.04                  | −2.08$^{+0.01}_{-0.06}$      |
| Smearing  | $R_{in}$ (GM/c$^2$)           | 10$^{+3}_{-2}$                | 9.9$^{+1.9}_{-1.4}$           |
| Smearing  | $R_{out}$ (GM/c$^2$)          | >1032$^{−270}_{−750}$        | >900                          | >850                          |
| Smearing  | Incl (deg)                    | >58                           | 59.8$^{+4.2}_{−4.0}$          |
| relxillCp | Refl frac                     | 0.69$^{+0.27}_{−0.19}$        | 0.9$^{+0.4}_{−0.3}$           |
| relxillCp | Ahe abundance                 | 2 (fixed)                     | 2 (fixed)                     |
| relxillCp | log $\xi$                     | 3.72 ± 0.09                   | 3.78 ± 0.08                   | 2.4 ± 0.3                     |
| relxillCp | Norm ($\times 10^{-3}$)       | 2.64$^{+0.25}_{−0.36}$        | 2.4 ± 0.2                     |
| Total     | Flux ($10^{−9}$ erg cm$^{-2}$ s$^{-1}$) | 1.59 ± 0.02                  | 1.60 ± 0.07                   | 1.59 ± 0.22                   |

way, we get a significative improvement of the fit, corresponding to $\chi^2$/dof = 2094/1446. The best-fitting parameters of this fit are reported in Table 2, and in Fig. 3 (left-hand panel), we show the XMM–Newton spectrum, the best-fitting model, and the residuals in units of $\sigma$ with respect to the best-fitting model.

Note that the electron temperature of the Comptonization component is much lower with respect to that measured with NuSTAR 4 d later, indicating that SAX J1808.4–3658 could have been in a soft state at the time of the XMM–Newton observation, in agreement with the presence of ionized discrete features in the spectrum. Note also that the XMM–Newton observation was acquired at the peak of the outburst and this is the first time that the SAX J1808.4–3658 spectrum has been observed with good energy resolution at the peak of an outburst. Substituting the diskline used for the iron line with the reflection model relxillCp, keeping the smearing parameters fixed to the corresponding smearing parameters of the other, low-energy disklines, returns a $\chi^2$/dof = 2100/1447, that is slightly worse than before ($\Delta\chi^2 \approx 6$), but with one extra degree of freedom. All the best-fitting parameters are consistent within the errors with the best-fitting values of the previous fit with disklines. As regards the reflection parameters, we fixed the iron abundance to 2, as in the case of the NuSTAR spectrum, the reflection fraction is compatible to that obtained with NuSTAR, although with a larger uncertainty, while the ionization parameter results to be much higher, log $\xi$ = 3.6–3.8, in agreement with the presence of features from highly ionized elements in the XMM–Newton spectrum. The best-fitting parameters of this fit are reported in Table 2. Note that some residuals are still present at ~7 keV, this is also visible in Fig. 3. To fit these residuals, we tried to add a Gaussian emission line at that energy, obtaining a $\chi^2$/dof = 2072/1444; the improvement of the fit is barely significant, corresponding to an F-test probability of chance improvement of $\sim 1.2 \times 10^{-8}$. We also tried to fit the iron abundance obtaining a preference for an overabundance, $A_{Fe}$ = 3.4 ± 0.7, but without a statistically significant improvement of the fit (F-test probability of chance improvement $\sim 1.3 \times 10^{-3}$ for the addition of one parameter).

3.3 Combined analysis of the NuSTAR and XMM–Newton spectra

In order to increase the statistics at the iron line energy and for the whole reflection component, we tried to fit together the NuSTAR

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and XMM–Newton spectra, using the best-fitting models obtained above. The two observations are not perfectly simultaneous, the NuSTAR observation being performed 4 d after the XMM–Newton observation taken at the peak of the outburst. Both the best-fitting continuum emission and the emission lines are very different between the two spectra. We therefore left most of the parameters free to vary between the two spectra and only few parameters were constrained to assume the same value for the two spectra; these are the equivalent hydrogen column density, N_H of the interstellar absorption, all the parameters of the smearing component and the iron abundance. Both the ionization parameter of the reflection component and the reflection fraction were quite different between the XMM–Newton and NuSTAR spectra (cf. Tables 1 and 2) and therefore we let these parameters free to vary between the two spectra. The low-energy disk lines are not required by the NuSTAR spectrum and hence are not included in the fit of the NuSTAR spectrum. Again, letting the iron abundance free to vary (but forced to assume the same value for the two spectra) we find an improvement of the fit, corresponding to a χ^2/dof = 3394.30/2770 (corresponding to an F-test probability of chance improvement of 4 × 10^{-5} for the addition of one parameter). The best-fitting value was N_K ≃ 3.4, while all the other parameters did not change significantly. However, we could not determine the error on this parameter, and therefore we preferred to keep the iron abundance fixed to two times the solar value. In Table 2 (last column), we report the best-fitting parameters obtained for this fit. In Fig. 4, we show the XMM–Newton and NuSTAR spectra together with the best-fitting model and residuals in units of sigma with respect to this model. Form visual inspection of Figs 3 and 4, some residuals are still evident in the XMM–Newton RGS (at ∼0.9, ∼1.3, and ∼1.6 keV) and pn spectra (at ∼7 keV). In order to fit these residuals, we tentatively add to the previous model three (Gaussian) absorption lines and an edge. The edge has a best-fitting energy of ∼7.4 keV and may be associated with mildly ionized iron (Fe XV-XVI). The centroid energies of the three absorption lines are 0.947 keV (possibly from Ne IX, resonance transition rest-frame energy 0.922 keV), 1.372 keV (possibly from Mg XI, resonance transition rest-frame energy 1.352 keV) and 1.596 keV, respectively. The latter is remarkably close to the resonant line of Al XII (rest-frame 1.598 keV). Note, however, that this element has a low cosmic abundance (∼3 × 10^{-6} in number of atoms with respect to H) and that this line has a significance of about 3.5σ; there is the possibility that this line is of instrumental origin, and we prefer not to discuss it further.

The first two absorption lines appear, instead, relatively broad (σ_Ne ≃ 0.035 keV and σ_Mg ≃ 0.015 keV, respectively), corresponding to velocity dispersion of ∼4 per cent and ∼1 per cent of the velocity of light, respectively. If our identification of the first two absorption lines is correct, then their energies appear to be blue-shifted with respect the corresponding rest-frame energies of ∼0.025 and ∼0.02 keV, respectively, corresponding to a velocity of ∼2.7 per cent and ∼1.5 per cent of the speed of light, possibly indicating the presence of an outflowing, weakly relativistic wind. Note that if the iron edge that we detect at 7.39 keV is indeed a line of instrumental origin, and we prefer not to discuss it further.

The addition of these components improved the quality of the fit, returning a χ^2/dof = 3186/2759, implying a decrease by Δχ^2 = 229 for the addition of 12 parameters with respect to the previous best fit. In this last fit, we decided to fix the outer disc radius at 1000R_g and the iron abundance at two times the solar value, and to include the low-energy disk lines also in the fitting of the NuSTAR spectrum. The line at 2.6 keV is indeed below the energy band used for the NuSTAR spectrum, and therefore, it was not included. The other two disk lines were included with all the parameters fixed to those of the XMM–Newton spectrum, except for the normalization that was left free to vary. We find that the line at 3.3 keV is indeed not necessary in the NuSTAR spectrum, with an upper limit on its equivalent width of 30 keV, while the addition of the line at 4.1 keV in the NuSTAR spectrum is significant at ∼3σ confidence level. All the other parameters are very similar (compatible within the associated errors) to those of the previous best fit; the most significant difference is in the ionization parameter of the NuSTAR spectrum for which we only get an upper limit of log ξ < 2 in agreement with the centroid energy of the iron line at ∼6.4 keV.

**Figure 3.** *Left: XMM–Newton RGS (black points) and pn (red points) spectra of SAX J1808.4–3658 in the energy range of 0.6–10 keV (top) and residuals in units of σ (bottom) with respect to the best-fitting model (see Table 2, third column). The model consists of a blackbody (dotted line), the Comptonization component *nvhComp* (solid line) and four disk lines (dashed lines) describing the reflection component, all multiplied by photoelectric absorption. *Right: NuSTAR spectrum in the energy range of 3–70 keV (top) and residuals in units of σ (bottom) with respect to the best-fitting model shown in the last column of Table 1.* The model components are also shown. From the left to the right: we see the blackbody component (dotted line), the Comptonization component plus the smeared reflection component modeled by *relxillCp* (solid line).
Figure 4. XMM–Newton (black and red points) and NuSTAR (green points) spectra of SAX J1808.4–3658 (top) and residuals in units of $\sigma$ (middle) with respect to the best-fitting model (see Table 2, last column). The model consists of a blackbody (with different temperatures for the XMM–Newton and NuSTAR spectra, dotted lines), the Comptonization component plus the smeared reflection component modelled by relxillCp (solid line), all multiplied by photoelectric absorption. Three disklines (indicated with dashed lines) are used to fit the XMM–Newton spectra but are not required for the NuSTAR spectrum. The total model is plotted on top of the data. Note that each spectrum is convolved with its response matrix and effective area, as well as the corresponding model and model components. In the bottom panel, we show the residuals in units of $\sigma$ with respect to the best-fitting model including the absorption components (see Table 3).

The results of this fit are shown in Table 3, and the residuals with respect to the best-fitting model are shown in the bottom panel of Fig. 4.

4 DISCUSSION

In this paper, we have analysed broad-band X-ray spectra acquired during the 2015 outburst of the AMSP SAX J1808.4–3658 observed by XMM–Newton and NuSTAR. The XMM–Newton ToO was performed at the peak of the outburst on 2015 April 11 for a total observing time of 110 ks, which resulted in an effective on-source exposure of $\sim$80 ks. The NuSTAR observation was performed approximately 4 d later, on 2015 April 15, and resulted in 49 ks of exposure per each of the NuSTAR modules. In this way, we have obtained a broad-band (from 0.6 to 70 keV), moderately high-resolution spectrum of the source.

4.1 Comparison with previous spectral results

SAX J1808.4–3658 has been previously observed with good-energy resolution by XMM–Newton and Suzaku, approximately 1 d apart, during the 2008 outburst. In that occasion, a broad iron line was de-
tected in both the XMM–Newton and Suzaku spectra, with very similar profiles, and was fitted by a diskline (see P09; Cackett et al. 2009). The inner disc radius derived in this way was \( R_{\text{in}} = 8.7 \pm 0.4 R_g \), using XMM–Newton (P09) and \( R_{\text{in}} = 13.2 \pm 2.5 R_g \) from a joint fit of the XMM–Newton and Suzaku spectra (Cackett et al. 2009), respectively. In both cases, the inner disc radius was consistent with being inside the co-rotation radius, which is the radius at which the magnetosphere rotation velocity equals that of an assumed Keplerian disc, \( R_{\text{co}} = (GM_\text{NS}/\Omega^2)^{1/3} \), where \( M_\text{NS} \) is the NS mass and \( \Omega \) its spin angular velocity. For the case of SAX J1808.4–3658, the co-rotation radius is \( R_{\text{co}} = 31 m_{1.4} \) km, where \( m_{t.4} \) is the NS mass in units of \( 1.4 M_\odot \). This has to be compared with the inner disc radius inferred from the reflection component, that is \( R_{\text{in}} < 25.6 m_{1.4} \) km (at 90 per cent confidence level, P09). This is thought to be a necessary condition in order to observe coherent pulsations in accreting pulsars and to avoid efficient propeller ejection of matter due to the centrifugal barrier (according to the standard theory of accretion onto fast rotators, see e.g. Ghosh & Lamb 1979). Assuming that the inner disc (as measured by the Fe line) is truncated at a magnetospheric radius this implies a magnetic field strength of \( \sim 10^8 \) gauss at the magnetic poles (Cackett et al. 2009). Interestingly, this estimate is consistent with other independent estimates of the magnetic field strength in this source based on completely different arguments (see e.g. Di Salvo & Burderi 2003; Burderi et al. 2003, 2006; Sanna et al. 2017a; and references therein). Also, both the XMM–Newton and Suzaku spectra gave a low ionization state of iron, inferred from the line centroid always consistent with 6.4 keV (corresponding to the rest-frame energy of the K \( \alpha \) transition of

| Component | Parameter | XMM–Newton (0.6–70 keV) | NuSTAR |
|-----------|-----------|-------------------------|--------|
| phabs     | \( N_H (\times 10^{22} \text{ cm}^{-2}) \) | 0.125 ± 0.011 | |
| edge      | \( E_{\text{cut}} (\text{keV}) \) | 7.39 ± 0.05 | |
| edge      | \( \tau (\times 10^{-2}) \) | 3.3 ± 0.6 | |
| gauss     | \( E_{\text{line}} (\text{keV}) \) | 0.947 ± 0.006 | |
| gauss     | \( \sigma (\text{keV}) \) | 0.035 ± 0.007 | |
| gauss     | \( I_{\text{line}} (\times 10^{-4} \text{ ph cm}^{-2} \text{ s}^{-1}) \) | -18.4 ± 3.5 | |
| gauss     | \( E_{\alpha W} (\text{eV}) \) | 5.0 ± 1.1 | |
| gauss     | \( E_{\text{line}} (\text{keV}) \) | 1.372 ± 0.006 | |
| gauss     | \( \sigma (\text{keV}) \) | 0.015 ± 0.006 | |
| gauss     | \( I_{\text{line}} (\times 10^{-4} \text{ ph cm}^{-2} \text{ s}^{-1}) \) | -4.2 ± 1.2 | |
| gauss     | \( E_{\alpha W} (\text{eV}) \) | 2.3 ± 0.7 | |
| gauss     | \( E_{\text{line}} (\text{keV}) \) | 1.596 ± 0.014 | |
| gauss     | \( \sigma (\text{keV}) \) | 0.03 ± 0.02 | |
| gauss     | \( I_{\text{line}} (\times 10^{-4} \text{ ph cm}^{-2} \text{ s}^{-1}) \) | -4.8 ± 2.3 | |
| diskline  | \( E_{\text{line}} (\text{keV}) \) | 4.3 ± 1.6 | |
| diskline  | \( I_{\text{line}} (\times 10^{-4} \text{ ph cm}^{-2} \text{ s}^{-1}) \) | 32 ± 6 | |
| diskline  | \( E_{\alpha W} (\text{eV}) \) | 72 ± 12 | |
| diskline  | \( E_{\text{line}} (\text{keV}) \) | 3.34 ± 0.02 | |
| diskline  | \( I_{\text{line}} (\times 10^{-4} \text{ ph cm}^{-2} \text{ s}^{-1}) \) | 21.9 ± 0.3 | |
| diskline  | \( E_{\alpha W} (\text{eV}) \) | 71 ± 14 | |
| diskline  | \( E_{\text{line}} (\text{keV}) \) | 4.13 ± 0.04 | |
| diskline  | \( I_{\text{line}} (\times 10^{-4} \text{ ph cm}^{-2} \text{ s}^{-1}) \) | 10.8 ± 1.8 | |
| diskline  | \( E_{\alpha W} (\text{eV}) \) | 48 ± 10 | |
| Smearing  | \( \beta \text{tor} \) | -2.30 ± 0.04 | |
| Smearing  | \( R_{\text{flight}} (\text{GM}/c^2) \) | <8.2 | |
| Smearing  | \( R_{\text{rat}} (\text{GM}/c^2) \) | 1000 (fixed) | |
| Smearing  | Incl (deg) | 68 ± 4 | |
| bbody     | \( kT_{\text{BB}} (\text{keV}) \) | 0.111 ± 0.004 | 0.505±0.07_0.33
| bbody     | \( L_{\text{BB}} (L_{360}/D_{10}^2) \) | 2.7 ± 0.8 | 1.6±0.10_0.3
| bbody     | \( R_{\text{BB}} (\text{km}) \) | 130 ± 21 | 4.9±0.15_0.08
| nthComp   | \( \Gamma \) | 1.77±0.02_0.04_0.03 | 1.93±0.06_0.08
| nthComp   | \( kT_{\alpha W} (\text{keV}) \) | 7.3 ± 0.8 | 69±0.15_0.05
| relxillCp | Reff frac | 0.78±0.07_0.2 | 0.35±0.06_0.06
| relxillCp | Fe abund | 2 (fixed) | |
| relxillCp | \( \log \xi \) | 3.64 ± 0.12 | <2
| relxillCp | Norm (×10^{−3}) | 2.7±0.2 | 4.14±0.10_0.09
| Total     | \( \chi^2 \) (dof) | 3186.45 (2759) | |
neutral or moderately ionized iron), and a high inclination angle of the system with respect to the line of sight, always above 50°.

Our analysis of the XMM–Newton and NuSTAR spectra of SAX J1808.4–3658 during the 2015 outburst gave remarkably similar results as regards the smearing parameters, both when fitting the iron line profile with a diskline and when using a self-consistent reflection model. These results are also very similar to those obtained for the 2008 XMM–Newton observation (P09). To show the agreement between these results we report in Table 4 the results obtained by P09 from the XMM–Newton observation performed in 2008 and our results from the NuSTAR spectrum obtained in 2015 when fitting the line profile with a diskline. Again we find a low ionization parameter, a large inclination angle (i > 70°), and a small inner disc radius (less than 7 Rg, corresponding to Rin < 15 m1.4 km). Even when we fit together the XMM–Newton and NuSTAR spectra with a self-consistent reflection model, we get disc parameters very similar to those obtained with the simple diskline. In particular for the NuSTAR spectrum, the ionization parameter, log ξ, is less than 2.7; the emissivity index of the disc is around 2 (compatible with the presence of a central illuminating source); the inclination angle is quite high, >50°; and the inner disc radius is constrained between (best estimate) 7.5 and 11.5Rg, corresponding to 16–24 km for a 1.4M⊙ NS, well within the co-rotation radius. Note that, despite the fact that the spectrum is typical of a hard state, the inner disc radius is quite close to the NS surface, implying that the disc is truncated not too far from the compact object in the hard state. This is also observed in other NS/LMXBs in the hard state (see Di Salvo et al. 2015, and references therein) and, as noted above, is a necessary condition to avoid a strong propeller effect in the case of a pulsar.

A small inner disc radius is also implied for most of the other AMSPs for which a spectral analysis has been performed and a broad iron line has been detected in moderately high resolution spectra. The AMSP IGR J17511–3057, observed by XMM–Newton for 70 ks and RXTE (Papitto et al. 2010), shows both a broad iron line and the Compton hump at ~30 keV. In this case, the inner disc radius was at >40 km for a 1.4M⊙ NS, with an inclination angle between 38° and 68° (see also Papitto et al. 2016). The AMSP and transitional pulsar IGR J18245–2452 observed by XMM–Newton (Papitto et al. 2013b) showed a broad iron line at 6.7 keV (identified as Kα emission from Fe XXV) with a width of ~1.6 keV corresponding to Rα ≃ 17.5Rg or ~36.7 km for a 1.4M⊙ NS. For comparison, the inner disc radius derived from the blackbody component was 28 ± 5 km. The (intermittent) AMSP HETE J1900–2455, observed by XMM–Newton for ~65 ks (Papitto et al. 2013a), showed a broad iron line at 6.6 keV (Fe XXIII–XXV) and an intense and broad line at ~0.98 keV, visible both in the pn and in the RGS spectrum, compatible with being produced in the same disc region. In this case, the inner disc radius was 25 ± 15 Rg, with an inclination angle between 27° and 34°. The (intermittent) AMSP SAX J17489.9–2017c), observed by XMM–Newton for ~115 ks and INTEGRAL (Pintore et al. 2016), was caught at a relatively high luminosity of ~5 × 1037 erg s−1 corresponding to ~25 per cent of the Eddington limit for a 1.4M⊙ NS, and, exceptionally for an AMSP, showed a spectrum compatible with a soft state. Comptonization component (~2 keV) and shows an additional hard X-ray emission described by a power law (photon index Γ ~ 2.3), typically detected in LMXBs in the soft state (see e.g. Di Salvo et al. 2000). In addition, a number of broad (Gaussian σ = 0.1–0.4 keV) emission features, likely associated with reflection processes, have been observed in the XMM–Newton spectrum. A broad iron line was observed at an energy of ~6.7–6.8 keV, consistent with a Fe XXV Kα transition produced in the disc at a distance of ~20–43 Rg (~42–90 km) with an inclination angle of ~38°–45°. The other broad emission lines may be associated with K-shell emission of highly ionized elements and are compatible with coming from the same emission region as the iron line. A moderately broad, neutral Fe emission line has been observed during the 2015 outburst of IGR J00291 + 5934 observed by XMM–Newton and NuSTAR (Sanna et al. 2017b). Fitted with a Gaussian profile the line centroid was at an energy of 6.37 ± 0.04 keV with a σ = 80 ± 70 eV, while using a diskline profile, the line parameters were poorly constrained. Finally, the newly discovered AMSP MAXI J0911–655, observed by XMM–Newton and NuSTAR (Sanna et al. 2017c), shows the presence of a weak, marginally significant and relatively narrow emission line in the range of 6.5–6.6 keV, modelled with a Gaussian profile with σ ranging between 0.02 and 0.2 keV, which was identified with Kα emission from moderate to highly ionized iron.

4.2 Detailed discussion of the NuSTAR and XMM–Newton spectra: similarities and differences

The use of a self-consistent reflection model instead of a diskline for the NuSTAR spectrum of SAX J1808.4–3658 gives an improvement of the fit (corresponding to a Δχ2 ≃ 9 with one parameter less). This demonstrates that the Compton hump is significantly detected in the spectrum and that the line profile parameters are in good agreement with those needed to fit the whole reflection component. The best-fitting results strongly suggest a moderate overabundance of iron by approximately a factor between 2 and 3. However, this overabundance may be indicative of a disc density higher than the value of 1015 cm−3 assumed in the rexlit model. Indeed, García et al. (2016) have shown that the iron abundance is sensitive to the density used in calculating the reflection model, and that when assuming a higher-density disc a lower iron abundance is obtained (see also García et al. 2018, and references therein). Hence, this overabundance should be confirmed using appropriate reflection models in which the density in the disc can be varied. There are versions of the rexlit model that allow to vary the disc density, although at the moment these models have a high-energy cut-off of the illuminating continuum fixed to 300 keV, that is much higher than the temperature of the Comptonization continuum we find in the spectrum of SAX J1808.4–3658.

We have also fitted the value of the outer radius of the emitting region in the disc; this parameter should be always let free to vary in high statistics spectra, since it strongly correlates with the inclination angle of the system and fixing this parameter may result in an artificially narrow uncertainty for the inclination angle. In all our fitting, the value of the outer radius of the emitting region in the disc, was quite underdetermined, although compatible (within the large uncertainties) with the value derived by P09 during the 2008 outburst (130 ± 320 Rg). Usually in other bright LMXBs, when it is possible to let this parameter free, the best-fitting value is most of the times very high, above 2500 Rg (see e.g. Di Salvo et al. 2009; Iaria et al. 2009), as it should be expected if the entire disc is illuminated and emits a reprocessed spectrum. However, SAX J1808.4–3658 is a transient with short outbursts, and therefore during the outburst at least the innermost part of the disc is emptying in few days. This means that the disc, over which reflection takes place, may have a ring-like shape with an outer disc radius which is relatively close to the inner disc radius. Therefore, it is possible that the small outer disc radius inferred from the reflection component in SAX J1808.4–3658 during the 2008 outburst may be an indication that the accretion disc was already emptying or that some disc
parameters may change abruptly towards the outer disc in short-duration outbursts. Unfortunately, we were not able confirm this result with these observations. Future observations at high energy resolution and high statistics (perhaps taken during the decay phase of the outburst) might be able to confirm this finding that may give important information on the evolution of the accretion disc in this kind of transients.

The best-fitting continuum model that we find for the NuSTAR spectrum of SAX J1808.4–3658 is also very similar to that already used by P09 to fit the XMM–Newton spectrum during the 2008 outburst, with the difference that P09 used two soft components, a blackbody (at a temperature kT ~ 0.4 keV) and a multicolour disc blackbody (at kT_\text{in} ~ 0.2 keV), and a power law to fit the Comptonization component, while we use a blackbody and a Comptonization model that include a soft (Wien spectrum) component as a seed photon. In our fit, the seed photon temperature for Comptonization (kT_\text{seed} < 0.29 keV) is comparable to the disc blackbody temperature reported by P09, and a spherical radius of the emitting region of ~3 km, a factor of ~2 lower than the blackbody radius reported by P09. The value of the equivalent hydrogen column to the source is very precisely determined by the XMM–Newton spectrum, N_H ≈ 0.15 × 10^{22} cm^{-2}, and is slightly lower than that derived by P09 during the 2008 outburst.

On the other hand, the XMM–Newton spectrum of SAX J1808.4–3658 taken in 2015 looks quite different from the 2015 NuSTAR spectrum and the 2008 XMM–Newton spectrum of the source. The blackbody component is found at a low temperature, ~0.1 keV, very close to the seed photon temperature (kT_\text{seed} ≈ 0.15 keV), and the corresponding radius of the blackbody emitting region, assuming a spherical geometry and not considering colour corrections, results to be 150–200 km, much larger than the inner radius inferred from reflection features (cf. Table 2). The Comptonization spectrum appears much softer, with an electron temperature around 5–8 keV. Moreover, several emission lines are observed in the XMM–Newton spectrum, identified with K α transitions of highly ionized (He-like) elements (S XVI – rest-frame energy 2.623 keV, Ar XVII – rest-frame energy 3.323 keV, Ca XIX – XX – rest-frame energy 3.902 and 4.108 keV, respectively, and Fe XXV – rest-frame energy 6.70 keV). The smearing parameters of these lines are compatible to be the same, and appear very similar to what we find for the smearing parameters of the NuSTAR spectrum ( emissivity index −2.1 to 2.3, inner radius 6–18R_\odot, outer radius ~1000R_\odot, inclination 50°–65°). When we try to fit the reflection component (Fe line and Compton hump) with the self-consistent reflection model relxill, we find parameters very similar to those obtained for the NuSTAR spectrum, except for a high value of the ionization parameter (log \xi ~ 3.7), in agreement with the high energies of the emission lines, which would require log \xi > 2. Most probably the XMM–Newton spectrum of SAX J1808.4–3658 taken in 2015 corresponds to a transition spectrum, in line with the fact that the XMM–Newton observation was taken at the very beginning of the outburst, that evolved to the more standard NuSTAR spectrum a few days after. If this is the case, SAX J1808.4–3658 experienced a soft to hard transition at the beginning of the outburst, that has never been observed before for an AMSP. Note that a spectral transition has been observed for the 11 Hz X-ray pulsar IGR J17480-2446 in the globular cluster Terzan 5 during its X-ray outburst in 2010 (Papitto et al. 2012). However, in that case, a hard to soft state transition was observed during the outburst rise. Unfortunately, the lack of high-energy coverage strictly simultaneous to the XMM–Newton observation of SAX J1808.4–3658 does not allow us to put further constraints on the high-energy spectrum, or to look for the presence of hard continuum components or a complex reflection component.

### 4.3 Binary inclination and mass of the neutron star

As stated above, despite the differences between the XMM–Newton and NuSTAR spectra we find quite similar values for the parameters of the reflection component and relativistic smearing. We therefore tried to fit simultaneously these spectra in order to increase the statistics of the reflection features and improve the constraints on the corresponding best-fitting parameters. We therefore let free to vary all the parameters of the continuum emission, except for the N_H, which was not constrained in the NuSTAR spectrum alone, and tied together the parameters of the relativistic smearing, with the iron abundance fixed at two times the solar value. Fitting the XMM–Newton and NuSTAR spectra together, we could get a precise estimate of the inner disc radius, which is constrained between 7.5 and 11.5R_\odot, while the best estimate of the system inclination, constrained between 58° and 64°, comes from the fitting with relxillCp of the XMM–Newton spectrum (see Table 2).

We also find evidence in the XMM–Newton spectrum of the presence of some absorption discrete features (see Table 3), namely an absorption edge at ~7.4 keV from neutral or mildly ionized iron and at least two absorption lines, possibly from K α transitions of highly ionized (He-like) Ne IX (at 0.947 keV) and Mg XI (at 1.372 keV). These lines appear relatively broad (implying a velocity dispersion of \sigma_v ~ 1 per cent c) and blue-shifted at a velocity a

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Table 4. Comparison of the best-fitting diskline parameters obtained for the 2008 outburst as observed in the 60-ks XMM–Newton observation (P09) and for the 2015 outburst as observed by NuSTAR (this paper). For comparison we also show the best-fitting diskline parameters obtained for the 2015 80-ks XMM–Newton observation, when the source appears to be in a soft state. Bol L_X is the bolometric luminosity extrapolated in the 0.05–150 keV energy range during the observation and assuming a distance to the source of 3.5 kpc.

| Parameter       | XMM–Newton (2008) | NuSTAR (2015) | XMM–Newton (2015) |
|-----------------|-------------------|---------------|-------------------|
| E_\text{in} (keV) | 6.43 ± 0.08       | 6.38 ± 0.10   | 6.70 ± 0.05       |
| B_{\text{tor}}  | ~2.3 ± 0.3        | ~2.0 ± 0.2    | ~2.16 ± 0.10      |
| R_0 (GM/c^2)    | 8.7 ± 0.4         | <7            | 1.2^{+0.3}_{-0.2} |
| R_{\text{out}} (GM/c^2) | 127 ± 318 | 280 ± 1070   | 760 ± 1780   |
| Incl (deg)      | >75               | >70           | >58               |
| EqW (eV)        | 120 ± 20          | 120 ± 20      | 58 ± 8            |
| Bol L_X (erg s^{-1}) | 6.6 × 10^{36} | 3.6 × 10^{36} | 3.1 × 10^{36} |

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few per cent the speed of light. If confirmed, these lines may suggest the presence of a weakly relativistic outflowing wind towards the observer. Absorption lines from ionized elements are usually observed in high-inclination (60°–70°) sources (see e.g. Pintore et al. 2014, and references therein) and therefore their presence in the XMM–Newton spectrum may support the possibility of a high inclination, $i \sim 60°$, in SAX J1808.4–3658.

This estimate is compatible with previous estimates based on the fitting of the iron line profile during the 2008 outburst observed by XMM–Newton (Cackett et al. 2009; P09), and is also consistent with the inclination of $60° \pm 5°$ given by Ibragimov & Poutanen (2009) from a detailed analysis of the 2002 outburst from the source, as well as with the inclination range from 36° to 67° given by Deloye et al. (2008) studying the optical modulation along the orbital period of the system observed during a quiescence period in 2007; these authors also suggest a pulsar mass $M_\text{p} > 2.2 M_\odot$. A high inclination is qualitatively in agreement with the claim of a massive NS ($> 1.8 M_\odot$) and a low-mass companion star, a brown dwarf with $< 0.1 M_\odot$, as suggested by Bildsten & Chakrabarty (2001) (see also Di Salvo et al. 2008; Burderi et al. 2009). Finally, a recent estimate of the inclination angle to the system comes from a time-resolved optical imaging of SAX J1808.4–3658 during its quiescent state and 2008 outburst. A Markov chain Monte Carlo technique has been used to fit the multiband light curve of the source in quiescence with an irradiated star model, and a tight constraint of 50$^{+25}_{−15}$ deg has been derived on the inclination angle (Wang et al. 2013). This implies a constraint on the mass of the pulsar and its companion star, which are inferred to be $0.97^{+0.22}_{−0.21} M_\odot$ and $0.04^{+0.02}_{−0.01} M_\odot$ (both at 1σ confidence level), respectively.

However, high values for the inclination angle of the system look at odd when considered together with optical estimates of the radial velocity of the companion star. From phase resolved optical spectroscopy and photometry of the optical counterpart to SAX J1808.4–3658, obtained during the 2008 outburst, Eleber et al. (2009) reveals a focused spot of emission at a location consistent with the secondary star. The velocity of this emission is estimated at $324 \pm 15 \text{ km s}^{-1}$; applying a ‘$K$-correction’, the authors estimate the velocity of the secondary star projected on to the line of sight to be $370 \pm 40 \text{ km s}^{-1}$ (see also Cornelisse et al. 2009). This estimate, coupled with a high inclination angle of the system, gives very low values for the NS mass, and has been used to argue against the presence of a heavy NS in this system. In fact, the pulsar mass can be estimated using the following relation: $M_1 \sin^3 i / (1 + q)^2 = K_2^2 P_{\text{orb}} / (2 \pi G)$, where $M_1$ is the pulsar mass, $q = M_2 / M_1$ is the mass ratio of the system, $P_{\text{orb}}$ is the orbital period of the system, and $K_2$ is the radial velocity of the companion star of mass $M_2$. Using the estimated radial velocity of the companion star together with our best-fitting value for the inclination angle, we find a pulsar mass in the range: $M_1 = 0.5 \div 0.8 M_\odot$. This range of masses for an NS is unacceptable and casts serious doubts on the estimates of the radial velocity of the companion and/or on a high inclination angle for the system.

A possibility we can imagine is that the reflection is measuring the inclination with respect to the sight of the inner part of the accretion disc, which may be different from the binary inclination. If the inner accretion disc is tilted with respect to the orbital plane, for instance because of the action of the NS magnetic field, such that the inner disc is observed at high inclination, then this could explain why measured inclination of the inner disc can be different from the binary inclination. However, this would not explain the high inclination angle measured by Wang et al. (2013) during X-ray quiescence.

The other possibility is that the problem comes from measurements of the companion radial velocity. Note that the reported measurements of the radial velocity $K_2$ are still affected by large uncertainties. This is because these measurements are taken during X-ray outburst and are affected by the presence of the accretion disc and the strong irradiation of the companion star. These estimates should therefore be confirmed in order to obtain a reliable estimate of the NS mass.

5 CONCLUSIONS

In summary, we have reported a detailed spectral analysis of the XMM–Newton and NuSTAR spectra of SAX J1808.4–3658 during the latest outburst in 2015. The main results of this study are described in the following. The XMM–Newton spectrum, taken for the first time at the beginning of the outburst, appears to be much softer than what is usually found for this source and quite puzzling, while the broad-band NuSTAR spectrum, acquired a few days after, gives results perfectly compatible with those found from the XMM–Newton observation performed in 2008. Despite the differences present between the XMM–Newton and NuSTAR spectra taken in 2015, we could fit simultaneously the smeared reflection component in these spectra. In particular, we find that the reflection component requires a ionization parameter of $\log \xi \sim 2.4$ for the NuSTAR spectrum and a higher value, $\log \xi \sim 3.8$ for the XMM–Newton spectrum, and strong evidence of an overabundance of iron by a factor of 2 with respect to the solar abundance, although this may be due to a relatively high density in the disc. Also, the smearing parameters are very similar to those found with XMM–Newton during the 2008 outburst. The emissivity index of the disc is $\sim −2$, consistent with a dominating illuminating central source, and we find that the upper limit to the inner disc radius is $\sim 12 R_\odot$, compatible with an inner disc radius smaller than the corotation radius. We also give a precise measure of the inclination angle of the system, which results around 60°, in agreement with previous spectral results, as well as with the results of fitting the reflection component in each spectrum with empirical models (disklines). A high-inclination angle for this system is also supported by the presence of absorption discrete features in the XMM–Newton spectrum, although these detections should be confirmed by further spectroscopic studies. The high inclination of the system with respect to our line of sight, when combined with available measurements of the radial velocity of the optical companion, poses, however, a problem as regards the correct determination of the mass of the NS in this systems, and therefore deserves further investigation.

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