Introducing the Eulalia and new Polana asteroid families: Re-assessing primitive asteroid families in the inner Main Belt

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The so-called Nysa–Polana complex of asteroids is a diverse and widespread group studied by Cellino et al. (Cellino, A., Zappalà, V., Doressoundiram, A., di Martino, M., Bendjoya, P., Dotto, E., Migliorini, F., 2001. Icarus 152, 225–237) as a dynamically linked asteroid family. It carries the name of two asteroids because it appears to be two overlapping families of different asteroid taxonomies: (44) Nysa is an E-type asteroid with the lowest number in the midst of a predominantly S-type cluster and (142) Polana is a B-type asteroid near the low-albedo B- and C-type cluster. The latter has been shown to be a very important source of primitive near Earth asteroids.

Using the data from the Wide-field Infrared Survey Explorer (WISE) mission we have re-analyzed the region around the Nysa–Polana complex in the inner Main Belt, focusing on the low-albedo population. (142) Polana does not appear to be a member of the family of low-albedo asteroids in the Nysa–Polana complex. Rather, the largest is Asteroid (495) Eulalia. This asteroid has never before been linked to this complex for an important dynamical reason: it currently has a proper eccentricity slightly below the range of most of the family members. However, its orbit is very close to the 3:1 mean motion resonance with Jupiter and is in a weak secular resonance. We show that its osculating eccentricity varies widely (e = 0.06–0.19) on short timescales (~1 Myr) and the averaged value diffuses (between e = 0.11–0.15) over long timescales (~100 Myr). The diffusive orbit, low-albedo, taxonomic similarity and semimajor axis strongly suggests that despite its current proper eccentricity, (495) Eulalia could have recently been at an orbit very central to the family. Hierarchical Clustering Method tests confirm that at an eccentricity of e = 0.15, (495) Eulalia could be the parent of the family. The “Eulalia family” was formed between 900 and 1500 Myr ago, and likely resulted from the breakup of a 100 to 160 km parent body.

There is also compelling evidence for an older and more widespread primitive family in the same region of the asteroid belt parented by Asteroid (142) Polana. This family, the “new Polana family”, is more extended in orbital elements, and is older than 2000 Myr.

1. Introduction

1.1. NEO origins

Near-Earth objects (NEOs) are temporary visitors in the region around the terrestrial planets, and significant work has gone into understanding their dynamical behavior and lifetimes. Gladman et al. (2000) and others found that NEOs have short lifetimes, only about 10 Myr on average. Gravitational perturbations from planets, collisions with the terrestrial planets, or loss into the Sun or ejection out of the Solar System limit their average lifetimes. Contrasted with the age of the Solar System, the much shorter NEO lifetimes suggest that today’s NEOs are simply the current incarnation of a constantly re-filled steady-state population. Cratering records (Grieve and Shoemaker, 1994; Stöffler and Ryder, 2001) find that the impact flux on the terrestrial planets and the Moon has been relatively constant on Gyr timescales, supporting the idea of a steady-state population.

The problem of how to refill NEO space from the seemingly static Main Asteroid belt was answered with the discovery that asteroids are quite mobile (Bottke et al., 2000, 2006). Thermal forces work via the Yarkovsky-effect to change asteroid’s semimajor axes over time (Farinella and Vokrouhlický, 1999; Bottke et al., 2000, 2006).
The work presented here develops the fundamental hypotheses to be tested by planned asteroid sample return missions. Dynamical evolution studies are critical to obtaining the maximum scientific benefit from these missions. Such studies support primary mission objectives to characterize the geologic and dynamic history of the target asteroids and provide critical context for their returned samples. In addition, compositional analyses of e.g., cosmochemical isotope ratios, radionuclide abundances, and nuclear track densities will, in return, provide important constraints on the dynamical evolution of the parent asteroid. This synergy will result in improved understanding of the dynamical pathways that transform IMB objects into NEOs. Furthermore, the OSIRIS-REx mission specifically will provide the first ground-truth assessment of the Yarkovsky effect as it relates to the chemical nature and dynamical state of an individual asteroid. These studies will provide important input to models of the evolution of asteroid families by Yarkovsky drift and delivery to orbital resonances in the IMB.

1.2. Asteroid families and the Nysa–Polana complex

The landscape of the inner Main Belt is dominated by a handful of asteroid families and a diffuse population of “background” objects (see Fig. 1). Among primitive, low-albedo, bodies the largest known family is the low-albedo component of the Nysa–Polana complex, followed by the Erigone family and the Sulamitis family (Nesvorný 2010; Nesvorný, 2010; Gayon-Markt et al., 2012; Campins et al., 2012). Following an asteroid breakup event, fragments are launched onto orbits that are distinct from, but similar to, the parent body. Specifically, their “proper orbital elements”, roughly the long-term average of their osculating orbital elements, remain linked over time (Zappalà et al., 1990, 1994; Knežević and Milani, 2003). Smaller fragments are typically launched with higher velocity, creating a size-dependent spread in orbital elements. Over time the thermal Yarkovsky effect induces a size-dependent drift in semi-major axis, such that smaller bodies drift faster, and thus further, over time than the larger bodies. Therefore families of asteroids are identifiable in two ways: clustering in proper orbital element space, and correlated shapes in size vs. semimajor axis due to size-dependent Yarkovsky drift (see Vokrouhlický et al., 2006a; Bottke et al., 2006).

In the context of NEO-delivery, the size, age and location of an asteroid family are important properties. First, the larger the family, the more potential asteroids that can be delivered. Second, the age of a family determines how far it has spread by the Yarkovsky-effect, where older families can spread further. Finally, the location of the family determines how far its fragments must drift via the Yarkovsky effect to reach a resonance. As we find with the Nysa–Polana complex, a location very near a resonance makes locating
the center and determining the age of the family much more difficult.

Not all asteroids are associated with a specific asteroid family. There are a similar amount of “background” objects in this region as there are members of an identified family (Gayon-Markt et al., 2012). This work will, however, focus on asteroid families for a few reasons. First, asteroid families imply a physical correlation between fragments. Thus, we may learn more about an interesting asteroid by studying a much larger and brighter parent body or a suite of associated family members. Second, families’ orbital elements evolve in a relatively simple way—objects drift in semimajor axis at a speed relative to the inverse of their size due to the Yarkovsky effect. This means that a family member that has drifted into a resonance can be followed by equal or smaller-sized members of the same family at the same time-delivery of objects can be correlated temporally.

The specific asteroid family targeted in this work is part of the larger Nysa–Polana complex (NPC)—which appears to be two overlapping asteroid families of different asteroid taxonomies. Their overlapping nature has made detailed study difficult, but now the large database of albedos measured by the WISE mission has made a study of each of the two components of the family possible (Masiero et al., 2011; Mainzer et al., 2011).

Section 2 describes the analysis of the families in the low-albedo component of the Nysa–Polana complex—seeking to find the family center, parent and age. Section 3 describes the known physical properties of the family and Section 4 analyzes a second primitive family in the same region.

2. Identification of the Eulalia family

As suggested in works by Zappalà et al. (1995), Cellino et al. (2001), and Nesvorny (2010) one component of the Nysa–Polana complex consists of low-albedo objects belonging to C-or B-type taxonomies (see also Campins et al., 2010). This work will re-analyze the low-albedo population of the inner Main Belt (at low inclinations and moderate eccentricities) in order to find the center, the parent and the age of any low-albedo families in this region. The first target is the low-albedo component of the Nysa–Polana complex seeking to constrain the center and find the parent of the family, followed by an age estimate.

2.1. Data sources

We have used the calculated albedos from Masiero et al. (2011) to study asteroids observed by the NASA WISE mission in the IMB with low albedo. The WISE mission measured fluxes in 4 wavelengths 3.4, 4.6, 12 and 22 μm, and combined with a NEATM thermal model calculated visible albedos, \( p_V \), and diameters \( D \) for over 100,000 Main Belt asteroids. Not all asteroids were observed and not all observed asteroids were detected the same number of times. Therefore errors on albedo and diameter can vary from object to object, and also the sample of objects is not complete at any diameter. However, this work is not aiming to build a definitive list of family members, rather the aims are better to understand the family structure in the inner Main Belt. This database gives accurate measurements for a representative sample of bodies.

Within this dataset there are 6702 asteroids in the inner Main Belt (2.1 AU < \( a < 2.5 \) AU) that are measured to have albedo, \( p_V < 0.1 \), by WISE and that also have synthetic proper orbital elements in the database of 318,112 objects as of May 2012 from the AstDys database http://hamilton.dm.unipi.it/astdys (see also Knežević and Milani, 2003). The Nysa–Polana complex (NPC) of asteroids is centered around \( e \sim 0.15 \) and \( i \sim 3^\circ \). Hence out of the entire IMB, we take a subset with orbital eccentricities 0.1 < \( e < 0.2 \) with \( i < 10^\circ \). This area is centered on the NPC, but contains a large portion of the entire IMB. The largest \( H \) value in this dataset is \( H = 18.8 \).

This subset of asteroids has a distinct “V-shape”, or rather half of a V-subset, in the distribution of the absolute magnitude \( H \) as a function of \( a \) (Fig. 2; see also Gayon-Markt et al., 2012). This V-shape is typical of asteroid families due to the size dependence of the Yarkovsky effect semimajor axis drift of the family members (see Vokrouhlický et al., 2006a or Bottke et al., 2006). This is expected since the selection of asteroids surrounding the Nysa–Polana complex should be dominated by low-albedo family members that are expected to show a correlation in semimajor axis and absolute magnitude. However, two half V-shapes are visible, indicating the possible presence of two families with asteroids of low albedo in the region. This section is focused on the higher density V-shape structure, with the other analyzed in Section 4.

2.2. The center of the low-albedo component of the Nysa–Polana complex

Identification and analysis of the low-albedo families in the inner Main Asteroid belt pose a few unique problems. First, half of the typical asteroid family “V”-shape is visible in Fig. 2, which suggests that the parent body is very close to the 3:1 mean motion resonance with Jupiter. So close, in fact, that we can assume that at least half of the family was immediately lost to the powerful resonance shortly after the formation of the family (though we do search for family members on the other side of the resonance). Second, the families are very extended, nearly reaching from the 3:1 to the \( v_6 \), suggesting an old age and increasing the possibilities of interlopers and confusion in determining family membership. Lastly, there may be more than one family.

Typically, asteroid families are centered on a known parent body as determined by Hierarchical Cluster Method (HCM) fitting. With a known center the next variable to match is the age of the family which is determined by the width of the bounding envelope due to the size-dependent Yarkovsky drift of the asteroids. However, in this case, the shape of the asteroid distribution was not aligned with the previously proposed parent Asteroid (142) Polana.
Given the uncertainty in both the center and boundaries of the family, we seek to constrain these one at a time. First, following Vokrouhlický et al. (2006a), the C parameter can be used to normalize asteroid distance from a possible family center by their size. The Yarkovsky drift rate is inversely proportional to an asteroid’s diameter, so removing this measureable allows a search for clustering of drift distances from possible asteroid family centers. The C parameter is defined

$$C = \Delta \alpha \times 10^{-H/5}$$  \hspace{1cm} (1)

where $H$ is the absolute magnitude of the asteroid and $\Delta \alpha = \frac{\pi}{2} T$ is the distance an asteroid has drifted from its initial semimajor axis ($a_{\text{init}}$) over a time $T$ at a rate $da/dt$. This formulation of $C$ normalizes each asteroid by its size, as the Yarkovsky drift rate is inversely proportional to its size $da/dt \propto D^{-1}$ such that $da/dt = (da/dt)_{0}(D/D_{0})$. For a simplistic asteroid family formation event where all bodies start with the same $a_{\text{init}}$ and similar spin axes, all family members will have the same $C$, since this value normalizes their drift rate by their size. This is simplified by ignoring both the spin-axis evolution over time and different $a_{\text{init}}$ for each asteroid due to the dispersion of fragments following the family-forming impact.

However, the C parameter can help search for the center of the family. The distribution of $C$ for a given $a_{\text{init}}$ would be flat for a random distribution of asteroids. If a family is present that had correlated $C$ values due to their common semimajor axis drift times, then for an $a_{\text{init}}$ near the center of the family there will be a spike in $C$ values. Thus, the C distribution can be re-calculated at different $a_{\text{init}}$, seeking the value that provide the tightest clustering of $C$. The search algorithm simply counted the number of asteroids in the maximum bin of $\Delta C = 4 \times 10^{-6}$ AU, and the range of $a_{\text{init}}$ was selected to cover the centers suggested by Fig. 2. As $a_{\text{init}}$ was varied from $a = 2.42$–2.51 AU, a clear trend was observed, with a peak at $a = 2.494$ AU (Fig. 3).

### 2.3. The diffusive orbit of (495) Eulalia

The previous section found the center of the family is best fit at $a \sim 2.494$ AU, which is very close to the 3:1 MMR with Jupiter nominally located at ~2.5 AU. In the selected subset of asteroids there is only one asteroid with 2.48 AU < $a$ < 2.5 AU with an absolute magnitude less than 12 and only three with $H$ less than 13. We have also searched known asteroids with proper elements in the same region, finding only a few with measured low albedo from IRAS or AKARI (Asteroids 877 and 2159, Tedesco et al., 2002; Usui et al., 2011), but both have inclinations around 3.5°, outside the boundaries of the estimated family. The only asteroid with suitable inclination, semimajor axis and absolute magnitude is (495) Eulalia, with $H = 10.8$ an albedo $p_v = 0.051$ and a diameter $D \sim 40$ km (Masiello et al., 2011). The synthetic proper orbital elements are $a = 2.4868$ AU, $e = 0.1184$, $i = 0.0438$ (Knežević and Milani, 2003). The synthetic proper eccentricity of $e = 0.118$ is well below the NPC family average, which is why it was never previously identified as a candidate parent for any of the Nysa–Polana complex.

However, the orbit of (495) Eulalia is extremely close the 3:1 mean motion resonance (MMR) with Jupiter. The location of this resonance is nominally at ~2.5 AU where a body has an orbital period 1/3 that of Jupiter. The location of the resonance is also a function of the small body’s orbital eccentricity, where larger eccentricities expands the location of the resonance in semimajor axis (see Wisdom, 1983, Wisdom, 1985). The boundary of the resonance itself is not precise, rather the chaoticity of an orbit increases as it approaches the resonance. Therefore the precise behavior of (495) Eulalia over time cannot be estimated trivially (see also Guillens et al., 2002).

To estimate the chaotic affects on (495) Eulalia due to its location near the 3:1 MMR with Jupiter, its long-term evolution was modeled. Based on the published uncertainties for its current osculating orbital elements, we integrated 1000 clone particles (created from the 6D hyper-ellipsoid in the osculating elements space compatible with today’s orbit). The clones were integrated using the SWIFT_MVS code, which is part of the SWIFT integration package (Levison and Duncan, 1994). All eight planets were included in the simulation, and each clone was treated as a test particle (feeling only the gravity of the planets). The simulations spanned 500 Myr (with some tests to 4 Gyr).

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**Fig. 3.** The top panel shows the number of bodies in the maximum bin for the $C$ value as a function of a center semimajor axis value ($a_{\text{init}}$). The bottom panel shows a histogram of $C$ values for all asteroids in the subset of WISE data (2.15 AU < $a$ < 2.5 AU; 0.1 < $e$ < 0.2; $i$ < 10°), for the best-fit family center location of $a = 2.494$ AU. The bin size is $\Delta C = 4 \times 10^{-6}$ AU, and the maximum is found at $C = 7.4 \times 10^{-5}$ AU.

**Fig. 4.** Eulalia’s orbital interactions with the 3:1 MMR with Jupiter and also a secular resonance $g_5 + g_6 = 2g_6$. The top panel shows the slow (relative to the orbital periods) circulation of the principal resonance angle $\sigma_{3:1} = 3\theta_{\text{Jupiter}} - 2\theta_{\text{Eulalia}}$ librating about 180° with a period of ~600 ky (where short-period oscillations were eliminated by digital filtering).
The specific behavior for any single particle at very short timescales (kyr) is dominated by the proximity to the 3:1 mean motion resonance (MMR) with Jupiter via the slow circulation of the principal resonance angle $\sigma = 3\lambda_{Jupiter} - \lambda - 2\sigma$ (where $\lambda$ is the orbital frequency of an orbit and $\sigma$ is the precession frequency of an orbit; see Fig. 4). On longer timescales the interaction with $g + g_s = 2g_s$ secular resonance results in the corresponding resonance angle $\sigma = \sigma + \epsilon_{Jupiter} - 2\sigma_{Saturn}$ librating about $180^\circ$ with a period of $\sim 600$ ky (where $g$, $g_s$, and $g_0$ are the proper frequencies associated with the precession of the asteroid, Jupiter and Saturn respectively). This interaction, together with other secular terms of the asteroid’s orbit, is responsible for osculating eccentricity oscillations between 0.06 and 0.19.

To analyze long-term stability and orbital evolution the entire suite of particles was considered with averaged orbital elements over 10 Myr time periods as a proxy for proper elements. Each particle’s averaged elements was sampled every 10 Myr, creating a distribution mapping the time spent at different orbits—specifically at different eccentricities (Fig. 5). The semimajor axis of the 1000 clones is quite constant with $a = 2.486–2.487$ AU, while the average eccentricity diffuses between $e = 0.11–0.15$, with most of its time spent at $e = 0.12$. From the limited run to 4 Gyr we find some clones are lost to the 3:1 MMR; at 2 Gyr only 30% of the clones are lost and at 4 Gyr only about 60% of the clones are lost. So despite being chaotic, the gravitational-only orbit of (495) Eulalia is surprisingly stable for long timescales.

The role of thermal effects on the dynamics of Eulalia may be important given the putative old age of the family. At $D \sim 40$ km its maximum drift rate over 1 Gyr is around 0.005 AU, which is larger than the diffusion found in semimajor axis in the long timescale integrations above. Also, given its precariously low near the 3:1 MMR, a drift of 0.005 AU could change its long-term evolution dramatically, including a slightly different orbit at the time of a possible family-forming impact. A more realistic estimate of its potential drift rate depends heavily on its obliquity and various thermal properties. Its rotation rate and obliquity have been estimated at $29.2 \pm 1.0$ h and $\sim 88^\circ$ (Binzel, 1987). Increasing the

![Fig. 5](image-url)

**Fig. 5.** The evolution for 500 Myr of a subset of 200 clones of (495) Eulalia. The large red dot shows the starting location for a single clone and also the current synthetic proper elements of (495) Eulalia, the black dots show the evolution of the orbit averaged over 10 Myr timescales. The dashed line is the nominal location of the 3:1 MMR separatix plotted as eccentricity as a function of semimajor axis (Nesvorný et al., 2002). The upper right panel shows the time spent by each of the 200 clones at different values of 10 Myr averaged eccentricity. The bottom right panel shows the same for semimajor axis. On longer timescales, during 1–2 Gyr, the $e = 0.15$ bin is occupied $\sim 13\%$ of the time. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
The HCM results for $e = 0.14$ and $e = 0.15$ show the traits of the typical asteroid family behavior, with a sharp jump in asteroid family membership numbers at a specific $V_c$, followed by a slow increase thereafter (Fig. 6). This is not surprising, as the low-albedo component of the Nysa–Polana complex has a mean eccentricity of $e = 0.152$. Neither case, however, shows the characteristic jump in family membership number after exceeding the critical velocity cutoff for the family, as seen in many examples of Vokrouhlický et al. (2006a). It is more similar to the results for the large and old family Eos (Vokrouhlický et al., 2006b). The $e = 0.15$ case has the lowest $V_c$ jump in family numbers, at $V_c = 100$ m/s, and thus $e = 0.15$ is the favored case.

One outcome from the initial HCM results is the inclusion of Asteroid (142) Polana in the family at $V_c = 100$ m/s (Figs. 7 and 8). It seems very clear from the results in Fig. 2 that multiple families are overlapping and being selected by the HCM routine. This highlights the problems with differentiating membership between the two families for the bodies within the Yarkovsky envelopes of each. The inclusion of this secondary family will pose problems in later sections when the bounding envelope of the "V-shape" distribution is used to calculate the age of the family. In fact, by estimating the lower bound of the family in $H$ vs. $a$ space by the Yarkovsky drift curves, we can eliminate numerous interlopers that belong to another family, rather than the low-albedo part of the Nysa–Polana complex.

The slope of the cumulative distribution of absolute magnitude $H$ value for the HCM-determined family members is sometimes used to help select viable ranges of $V_c$ from an HCM search. This calculation was performed on the selected family at each increment in $V_c$ (see Fig. 9). This calculation follows Vokrouhlický et al. (2006a), by using the power-law of the form $N(<H) \sim 10^{H}$ where $13.5 < H < 15.5$. The results show no clear trend, and rather a low $\gamma \sim 0.5$ compared to what is found for some young (a few 100 s Myr) families such as Ergione $\gamma \sim 0.8$ (Vokrouhlický et al., 2006a) and is closer to the entire asteroid belt population with $\gamma \sim 0.61$ (Ivezić et al., 2001). Young families can have a range of size frequency distributions with slopes sometimes dramatically different than the background population. Over time collisional evolution will change the size frequency distribution eventually driving it to similar values as the background (Morbidelli et al., 2002; Bottke et al., 2005). In this case, where there is no distinct in the size frequency distribution from the background, this property cannot be used to either secure its selection as a family or to make a statement about its age.

We adopt Asteroid (495) Eulalia as the parent of the low-albedo component of the Nysa–Polana complex – now referred to as the "Eulalia family". Its proper semimajor axis at $a = 2.488$ AU is adopted as the center of the family. In the next section we can determine the extent and age of the family by using the members found in this HCM clustering search, and we will use the family as defined by the HCM criteria with $V_c = 120$ m/s, which by visual inspection was preferable to the $V_c = 100$ m/s selection due to larger numbers without increasing the size of the family in $a$, $e$, or $i$. 

Fig. 7. The Eulalia family members plotted as their proper inclination (top) and proper eccentricity (bottom) as a function of their semimajor axis (AU). The left plots show the selected family members and the right side shows the asteroids in the sample not selected as part of the family. This plot is done for $V_c = 120$ m/s, where Eulalia had an orbital eccentricity of $e = 0.15$, and the location of (495) is shown with a red square. Note that other large families, such as Ergione have been removed prior to the HCM. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Fig. 8. The Eulalia family members plotted as their absolute magnitude $H$ as a function of their semimajor axis (AU). This plot is done for a $V_c = 120$ m/s, where Eulalia had an orbital eccentricity of $e = 0.15$ and its location is shown with a red square. The top panel are the members found in the HCM search, and the bottom panel shows the asteroids in the sample not selected as part of the family. Note that other large families, such as Ergione have been removed prior to the HCM. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
2.5. Age estimate for the Eulalia family

The age of the family can be estimated by the spreading in semimajor axis of family members over time, which is a function of an asteroid’s size, thermal properties and spin axis (Bottke et al., 2006). The size or absolute magnitude of many Main Belt asteroids is well measured through the combination of recent WISE results, years of optical surveys such as Sloan Digital Sky Survey (SDSS) and past infrared surveys such as IRAS and WISE (some potentially important biases in the absolute magnitude values are discussed in Section 4). The thermal properties have been directly measured for only a few asteroids (see Delbô et al., 2007), but have been inferred for populations due to ensemble behavior for asteroid families with a range of ages (Bottke et al., 2006). The evolution of the spin axis of a body is related to its thermal properties and the thermal YORP-effect, and this behavior, though still being investigated, is constrained by asteroid family investigations (Vokrouhlický et al., 2006a; Bottke et al., 2006). Similarly, the initial distribution of fragment orbits following an asteroid impact provides an uncertain initial condition preceding the family spreading. Vokrouhlický et al. (2006a) have previously employed a complex fitting routine that simultaneously solves for family age, YORP reorientation timescales and strength, and a size-dependent initial velocity dispersion. Given the large extent of the Eulalia family, that at least half of the family is lost into the 3:1 MMR, and its location overlapping another primitive family, we focus here on the family boundaries in order to estimate family age. A more detailed method of the age determination, solving for YORP reorientation and the initial velocity dispersion, will be presented in later works.

The C distribution of asteroids was used to locate the center of the family, based on a cluster of similar values. A bounding C value for the family can be used to estimate an age for the family, based on the maximum Yarkovsky drift timescales. Using the C value we find,

\[ 0.2H = \log(\Delta a/C) \]  

(2)

where \( \Delta a = (da/dt)t \), and \( (da/dt) = (da/dt)_o(D_o/D) \) with \( (da/dt)_o \) being the maximum Yarkovsky drift rate for a diameter \( D_o \) ignoring any spin axis variation. It will be useful to use \( D = D_o \times 10^{10/5} / \sqrt{p_V} \), and combine them so that

\[ C = \left( \frac{da}{dt} \right)_o \sqrt{p_V} T \]  

(3)

where \( (da/dt) \) is \( \sim 3 \times 10^{-5} \text{ AU/Myr} \) for a 5 km asteroid in the inner Main Belt with a density of 2.5 g cm\(^{-3}\) and thermal conductivity \( K \sim 0.01 - 0.001 \text{ W m}^{-1} \text{ K}^{-1} \) (taken from Bottke et al. (2006)). The formulation uses a \( D_o = 1329 \text{ km} \), so the nominal drift rate (in AU/Myr) is,

\[ \left( \frac{da}{dt} \right)_o = 3.0 \times 10^{-5} \frac{2.5 \text{ g cm}^{-3}}{\rho} \left( \frac{5 \text{ km}}{D_o} \right) (\text{AU/Myr}) \]  

(4)

For an \( H = 0 \) with \( D_o = 1329 \text{ km} \) and a density of 1 g cm\(^{-3}\) the rate is \( \left( \frac{da}{dt} \right)_o = 2.8 \times 10^{-7} \text{ AU/Myr} \). There is no published measurement of the density of any family members, so we selected our nominal value of 1 g cm\(^{-3}\) for simplicity and the few measurements of C-type asteroids clustering around this value; with (379) Huenaa at \( \rho \sim 0.9 \text{ g cm}^{-3} \) (Marchis et al., 2008), and (253) Mathilde with \( \rho \sim 1.3 \text{ g cm}^{-3} \) (Yeomans et al., 1997) are two with accurate estimates. The drift rate is inversely proportional to the density, and thus this estimate can be a systematic source of error in our calculations. Now we can estimate the age based on the estimates for \( C \) by,

\[ T = C / \sqrt{p_V} \left( \frac{da}{dt} \right)_o \]  

(5)

with an albedo \( \sim 0.052 \) for (495) Eulalia.

To calculate the age of the family we are interested in the boundary of the \( C \) distribution, or the envelope of Yarkovsky lines for \( H \) as a function of \( a \). We devised a fitting routine whereby the value of \( C \) was varied and the ratio of asteroids with \( C \sim 8 \times 10^{-6} \text{ AU} \) was compared with \( C \sim 8 \times 10^{-6} \text{ AU} \). A strong contrast in numbers indicates the boundary of the family has been reached. This was done for all the members selected by the HCM routine for \( V_c = 120 \text{ m/s} \) in steps of \( \Delta C = 1 \times 10^{-6} \text{ AU} \) (where these bin sizes were selected via trial and error testing). Due to the increasing number of asteroids at greater \( H \) (smaller sizes), we measured this ratio for three different size ranges, \( 13.5 \leq H < 15 \leq H < 16 \leq H < 16.5 \). The average of the three ratios finds two peaks, at \( C = 9.2 \times 10^{-5} \text{ AU} \) and \( C = 10.5 \times 10^{-5} \text{ AU} \) (Fig. 10). The smaller value of \( C = 9.2 \times 10^{-5} \text{ AU} \) is favored by the smaller asteroids, while \( C = 10.5 \times 10^{-5} \text{ AU} \) is favored by the larger asteroids. This could be a real effect caused by thermal effects acting differently at small sizes, or simply confusion caused by interlopers.

The best fit boundaries are plotted in Figs. 11 and 12. Alone, these values of \( C \) would correspond to ages of \( T \sim 1440 \) and \( T \sim 1644 \text{ Myr} \). However, the calculation does not yet account for the initial fragment semimajor axis distribution produced immediately after the family forming event.

The size-dependent velocity dispersion of the fragments due to the asteroid impact creates a distribution of \( a_{\text{init}} \) preceding any Yarkovsky drift. Again, following Vokrouhlický et al. (2006a), we can estimate size-dependent \( a_{\text{init}} \) for collision outcomes with different velocity dispersions, where here we calculate another \( \Delta a \) as the distance from the center of the family,

\[ \Delta a = \frac{n}{n} V_f + C(e) \]  

(6)

where \( n \) is the mean motion of the target asteroid and \( V_f \) is the transverse velocity of the fragment and \( C(e) \) simply denotes other eccentricity-dependent terms. We can use a very idealized equation,
We have not yet estimated the total mass in the family or estimated the size of the parent of the family. This calculation is made later in Section 3.1, finding a parent body $D = 100–160$ km. That is used as a guide here since the velocity dispersion should be similar to the parent body escape speed that scales linearly with the parent body size. So we include calculations of the estimated size-dependent $\Delta a$ due to the initial collision event with $V_0 = 50$ m/s and $V_0 = 150$ m/s (see the red lines in Figs. 11 and 12). Since the $\Delta a$ from the initial fragment displacement follows the same 1/$D$ relationship as the Yarkovsky drift, we can relate the initial fragment distribution in terms of $C$, and simply subtract off this $C$ and re-calculate the age from the total Yarkovsky drift. These distributions correspond to a maximum initial semimajor axis $C = 1.13 \times 10^{-3}$ AU and $3.39 \times 10^{-3}$ AU, such that the best-fit bounding value of $C = 9.2 \times 10^{-5}$ AU, would simply be a $C = 8.07 \times 10^{-3}$ AU and $5.81 \times 10^{-3}$ AU, which correspond to ages of $T = 1264$ and 910 Myr. While for $C = 10.5 \times 10^{-5}$ AU, would correspond to total ages of $T = 1468$ and 1114 Myr.

The relationship between these calculations are shown in Fig. 12, where the black line is the $\Delta a$ due to Yarkovsky drift from a center at $a = 2.488$ AU with an age of 1160 Myr. The red lines are the $\Delta a$ due to the fragment velocity dispersion of 50 and 150 m/s. From these calculations we find the age of the family between 900 and 1500 Myr.

One important caveat in these simplistic age calculations is the role of obliquities changes due to the Yarkovsky-O’Keefe-Radzievskii-Paddack (YORP) effect (Rubincam, 2000; Vokrouhlický and Čapek, 2002; Bottke et al., 2002). The YORP effect acts by the asymmetrical reflection and re-emission of thermal radiation to affect the rotation state of an irregularly shaped body. When the YORP effect changes the obliquity of an asteroid, the semimajor axis drift rate due to the Yarkovsky effect will also change. The preferred spin states are those that maximize the Yarkovsky drift ($0^\circ$ and $180^\circ$), such that family members with initial obliquities resulting in slow Yarkovsky drift are expected to evolve over time to a faster-drifting state. Large uncertainty exists in modeling the evolution of the YORP re-orientation of obliquities due to the YORP evolution of the rotation rate as well and complications at very high and very low spin rates. An estimate of re-orientation timescales is $\sim 300–600$ Myr for $\sim 5$ km objects (Vokrouhlický and Čapek, 2002; Čapek and Vokrouhlický, 2004). Objects well above this size are then likely to have not experienced a full YORP re-orientation since the formation of the family. Any dramatic effects due to YORP cycles for this family would therefore not be significant for asteroids larger than $H < 14$ to be conservative.

One possible tracer of $V_0$ would be family members reaching the other side of the 3:1 resonance (for $a > 2.5$ AU). Given the center of the family and the Yarkovsky drift boundaries from the asteroids with $a < 2.5$ AU, we selected the subset of asteroids with $a > 2.5$ AU that would host any family members. There is no clear evidence of a high density of asteroids around the Yarkovsky lines (Fig. 13), confirmed by the distribution of $C$ values around an $a_{\text{min}} = 2.487$ AU. The lack of existence of, or inability to detect, members on the far side of the 3:1 MMR limits the $V_0$ for the fragment distribution. Very large velocity distributions would place many asteroids on orbits beyond the 3:1 MMR, where they could be observable today. For a conservative boundary of the 3:1 MMR of $a \sim 2.51$ AU at the relevant eccentricities of $0.1 < e < 0.2$ a $V_0 = 50$ m/s would only place some objects of $H > 15$ beyond the resonance, while at $V_0 = 150$ m/s only some with $H > 13.5$. While a substantial mass of the family can be contained in bodies of these sizes and smaller, it also implies a large fraction of the mass never made it past the 3:1 MMR. Thus the $V_0$ estimates used in this work, presented to bracket possible ranges of fragment velocity dispersion, also are consistent with the lack of a clear family signature across the 3:1 MMR.
Fig. 13. Asteroids measured by WISE to have \( p_V < 0.1 \) with \( 0.1 < e < 0.2 \) and inclination \( < 10^\circ \) with semimajor axis \( a > 2.5 \) AU. The Yarkovsky line for the family boundary at \( C = 9.2 \times 10^{-5} \) AU is the solid black line. The red lines represent a simple initial dispersion for a velocity dispersion of fragments for \( V_0 = 50 \) m/s and \( V_0 = 150 \) m/s. This selection of asteroids, matching the orbital properties of the detected family but on the other side of the 3:1 MMR show no sign of a family signature. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

3. Properties of the Eulalia family members

3.1. The SFD and total mass of the Eulalia family

The size frequency distribution of the family can be estimated from the objects selected in the HCM routine, using the power-law of the form \( N(<H) \sim 10^{-3H} \). In Section 2.4 a \( \gamma \) for only the range of \( 13.5 < H < 15.5 \) was compared to the background, now we consider the size distribution of all prospective family members, using it to estimate the mass of the entire family.

Simply summing the mass of all observed bodies is a quick estimate of the original parent’s size. However, we are only now detecting half of the family, as the other half were launched into, or very quickly entered, the 3:1 MMR and were lost. There is another factor of two, as only bodies launched to smaller semimajor axis survive the initial displacement from the parent, but then any asteroid with an initial outward Yarkovsky drift will very quickly drift into the 3:1 MMR. Similarly, the dataset is missing objects as the WISE survey is not complete, even at large sizes. A comparison of the WISE survey and database of known asteroids, for large asteroids in the inner Main Belt, found that it detected \(~80\%\) of all asteroids with \( H < 10 \), with that fraction dropping to \( 55\% \) for \( H < 15 \). Combined with the previous family scaling factor of 4, scaling by 5 to account for the \( ~80\% \) WISE detection efficiency is closer, though this scaling factor should grow at smaller sizes. Finally, the numbers are scaled at each size according to the WISE detection efficiency. It should be noted that collisional evolution could play a major role in altering the family SFD over time, and this should be considered in future models.

The integrated size for the selected family members from the \( V_c = 120 \) m/s HCM routine is \( D = 68.6 \) km (the black line in Fig. 14). Note that this includes a limiting \( H \) vs. \( a \) criteriora to eliminate interlopers. When a factor of 4 for the loss of \( 3/4 \) of the family to the 3:1 MMR is accounted for (except the largest body, parent Eulalia) the estimate increases to \( D = 100.1 \) km (blue line in Fig. 14). Finally, a full factor of 5, accounting for the survey limitations, equals a body with \( D = 107.2 \) km (red line in Fig. 14). The final correction for size-dependent WISE detection efficiency increases the size to \( D = 121.2 \) km (green line in Fig. 14).

Since only the largest bodies are detected with very high efficiency, an alternative method to estimate total family mass is needed. An alternative method relies on the size frequency distributions for asteroid families derived from Smoothed Particle Hydrodynamics (SPH) simulations of catastrophic asteroid impacts that are coupled to \( N \)-body gravitational simulations of their reaccumulation (Durda et al., 2007; Benavidez et al., 2012). This method matches size frequency distributions between simulations and observations at large fragment sizes, and then uses the simulation to estimate how much unobservable material may also belong to the family. One SPH and \( N \)-Body asteroid collision simulation was selected from the suite of simulations by Benavidez et al. (2012). It used a 100 km basalt rubble pile target with a 3 km/s 34 km impactor hitting at a 15° angle. The largest remnant in the simulation outcome is \( D = 29.8 \) km, slightly smaller than (495) Eulalia (\( D = 40 \) km). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

3.2. Observed physical properties

The WISE mission facilitated the analysis of this family while also providing some physical characterization of its constituents. Other public databases and catalogs of observations are available to assess the physical properties of the family members. Here we summarize the available data.

3.2.1. Albedo distribution

From the WISE mission, there are calculated albedos for each object in the dataset used here. We compare the albedo distribu-
tion of the bodies found by the HCM routine for $V_c = 120 \text{ m/s}$, with the $C = 9.2 \times 10^{-5} \text{ AU}$ boundaries.

We find only a slightly tighter cluster of albedo values in this sample compared to the background (Fig. 15). Given that the entire sample is less than $p_V < 0.1$, and typical formal errors in albedo measured by WISE are $\sim 0.008$ for $H < 15$ and $\sim 0.018$ for the entire sample, a clear cluster in albedo was unlikely. The bulk of the asteroids included in the family are small objects, the distribution may be dominated by objects with larger errors in their measurement due to their small sizes. The 128 objects with $H < 15$ show no clear distinction from the entire sample of 1563 selected for these boundaries of the family (Fig. 15). Pravec et al. (2012) found that there is divergence between $H$ values found in the MPC database and those measured through an observational campaign, where the MPC values are systematically too small, reaching a maximum mean offset of $-0.4$ to $-0.5$ around $H = 14$. This would lead to albedo estimates that are slightly too large and becomes significant and systematic at $H$ above 10. The WISE calculated albedos relied on the $H$ values in the MPC database, and this therefore could account for a source of error as well.

3.2.2. SDSS colors

The Sloan Digital Sky Survey (SDSS) observed 471,000 moving objects, for which 220,000 observations were matched to 104,000 different asteroids. The photometry was done in five wavelengths and is a valuable tool for establishing taxonomic relationships for large groups of asteroids. The five wavelengths can be combined in numerous ways in order to capture the many possible features found in visible spectra of different asteroid types, but a common method is to compare the $i - z$ colors as a function of $a^*$ (where the $i$ filter is centered at 769 nm, the $z$ at 925 nm and $a^*$ is the derived first principal component for the distribution of asteroid colors in the SDSS $r - i$ vs. $g - r$ color–color diagram). The former measures the depth of the 1 μm silicate absorption bands mainly due to olivines and pyroxenes, the latter is a proxy for the slope of the spectra (see Fig. 3 in Parker et al. (2008)). In this space, primitive asteroids of the C- and B-types are typically found with negative slope ($a^* < 0$).

Here we matched 668 asteroids from selected family bounded by the $C = 10.5 \times 10^{-5} \text{ AU}$ that were also measured by SDSS, and have plotted them on the same axes and color scheme as Parker et al. (2008). As expected, the family is tightly clustered in the region dominated by primitive asteroids (Fig. 16). Without more significant quantitative analysis, it is clear that cluster is actually much tighter than that found for all primitive bodies. However, it is also clear that the cluster is not tight enough to use SDSS colors as a tool to differentiate members from different family associations.

3.2.3. Known spectra

Asteroid (495) Eulalia was observed on 11 June 2007 at the NASA IRTF with the SpeX instrument between 0.7 and 2.5 μm (Fieberg-Beyer et al., 2008; Fieberg-Beyer, 2011). There are no clear features for the (495) Eulalia spectral reflectance, with only a minimal upturn in the spectra beyond 2.0 μm (Fig. 17). As the parent of the family this spectra is potentially valuable in finding differences between members of it and the neighboring background. However, flat and featureless spectra are somewhat common for low-albedo objects, which does not aid the determination of family membership for an asteroid with unknown affiliation.

There exists numerous databases to search for spectra of other family members, and two visible spectra (Asteroids 1076 and 2509) were found among the Small Main-Belt Asteroid Spectroscopic Survey (SMASS; Xu et al., 1995, 1996) and two (Asteroids 495 and 3999) in the second phase of that survey (SMASSII; Bus and Binzel, 2002). An additional two objects found in the family using the $C = 10.5 \times 10^{-5} \text{ AU}$ boundaries (see Fig. 11) were observed in SMASS database (Asteroids 1768 and 2809). No objects were found in the S3052 database (Lazzaro et al., 2004) or in the PDS release of multiple IRTF surveys (Bus, 2011).

The data in longer, near-IR, wavelengths is even more sparse. As mentioned above (495) Eulalia, was observed with the IRTF SpeX instrument as part of a campaign to study objects near the 3:1 MMR. As part of the wider asteroid survey, the MIT-UH-IRTF Joint Campaign for NEO Reconnaissance (http://smass.mit.edu/), there are near-infrared observations of Asteroids (1076) Viola and (1768) Appenzella. (1076) Viola, which belongs to the Eulalia family, is plotted with (495) Eulalia (Fig. 17) and shows similar morphology throughout, in particular they have a similar slope beyond 2.0 μm. Asteroid (1768) Appenzella is within the Yarkovsky boundaries for both families, and is thus plotted alone. It shows an upturn starting around 1.0 μm, with a much shallower slope than found for (142) Polana (discussed below).

Fig. 15. The gray-filled histogram shows the relative distribution of albedos for all of the 6702 bodies selected for this study ($p_V < 0.1$), while the black outline histogram shows the distribution for the selected Eulalia family members inside the $C = 9.2 \times 10^{-5} \text{ AU}$ boundary. The dotted line is the albedo distribution for only the subset of the family members with $H < 15$, accounting for 128 of the 1563 total members plotted here.

Fig. 16. The members of the Eulalia family (open diamonds; $C = 10.5 \times 10^{-5} \text{ AU}$) and all the SDSS observed asteroids plotted as $i - z$ colors as a function of the slope $a^*$ where the $i$ filter is centered at 769 nm, the $z$ at 925 nm and $a^*$ is the derived first principal component for the distribution of asteroid colors in the SDSS $r - i$ vs. $g - r$ color–color diagram. The color scale is that used by Parker et al. (2008) that associates colors with locations on this color–color plot. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
the visible “ear” of the family located at 2.2 AU < a < 2.25 AU and 15.5 < H < 16.5. We simply selected a few objects in this orbital range and ran the HCM at varying \( V_c \) checking to see whether any clump would acquire the characteristic shape in \( H \) vs. \( a \) space.

The first test was done with Asteroid (2446) Lunacharsky. This asteroid has proper orbital elements of \( a = 2.355 \) AU, \( e = 0.154 \), \( i = 3.178^\circ \), and is also one of the few in this region with published visible and near infrared spectra. The HCM results for this body show that there is a highly diffuse and extended association with few family members found below a velocity cutoff of \( V_c = 150 \) m/s (Fig. 18, bottom). However, the association linked by HCM at \( V_c = 180 \) m/s and larger shows the distinct signs in the \( H \) vs. \( a \) space of a correlated family and the family size increases quickly.

The largest bodies linked to this association are Asteroids (142) Polana and (112) Iphigenia with proper elements \( a = 2.418 \) AU, \( e = 0.157 \), \( i = 3.215^\circ \) and \( a = 2.434 \) AU, \( e = 0.094 \), \( i = 3.195^\circ \) respectively (Iphigenia is linked at \( V_c = 180 \) m/s and Polana at \( V_c = 190 \) m/s). The orbital element distribution of the selected asteroids is quite large in eccentricity, spanning \( 0.1 < e < 0.2 \), but more tightly clustered in inclination between \( 1^\circ < i < 5^\circ \). Each of these large asteroids are in distinct clusters determined by their eccentricity, where (142) Polana is in the midst of the high eccentricity grouping and (112) Iphigenia with the smaller low eccentricity grouping (Fig. 19).

4.1. The “new Polana” family

Beyond the clear correlation of the asteroids in the Eulalia family as seen in Fig. 2 and analyzed in the previous sections, there appears to be a possible second family in the same dataset. The lack of asteroids with \( a < 2.3 \) AU and \( H < 14 \) is clear and defies even the expected dropoff in the number of asteroids with decreasing semimajor axis due to the inclination-dependent effects of the \( V_c \) resonance and eccentricity limits of Mars crossing orbits. The high density of objects with \( 15 < H < 17 \) and \( 2.1 \) AU < \( a < 2.3 \) AU has the characteristic “ear” of an asteroid family seen at higher semimajor axis for the Eulalia family due to the Yarkovsky semimajor axis drift.

This possible family suffers from the same, and even amplified, difficulties found in analyzing the Eulalia family: a center near a powerful resonance, overlapping with another family and possibly a very old age. In many tests below we will remove the Eulalia family from the data set (using previously defined boundaries) in an attempt to measure only the possible background family.

4.1.1. HCM of the background family

Given the very diffuse nature of this possible family with an unknown parent, we reverse the procedure used before, and begin with an HCM test to make sure there is, in fact, an orbital correlation among the high density region of asteroids. Given the very low density of large objects, this HCM test was centered on the heart of the visible “ear” of the family located at 2.2 AU < \( a < 2.25 \) AU and 15.5 < \( H < 16.5 \). We simply selected a few objects in this orbital range and ran the HCM at varying \( V_c \) checking to see whether any clump would acquire the characteristic shape in \( H \) vs. \( a \) space.

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4. Discussion

An important aspect to the analysis of the Eulalia family is the possibility of a larger, older family with similar orbits and similar low albedo. Here we investigate and characterize this proposed family with some of the tools used above. This family is even more extended and diffuse and much of the analysis is beyond the scope of this current work.

4.1. The “new Polana” family

Beyond the clear correlation of the asteroids in the Eulalia family as seen in Fig. 2 and analyzed in the previous sections, there appears to be a possible second family in the same dataset. The lack of asteroids with \( a < 2.3 \) AU and \( H < 14 \) is clear and defies even the expected dropoff in the number of asteroids with decreasing semimajor axis due to the inclination-dependent effects of the \( V_c \) resonance and eccentricity limits of Mars crossing orbits. The high density of objects with \( 15 < H < 17 \) and \( 2.1 \) AU < \( a < 2.3 \) AU has the characteristic “ear” of an asteroid family seen at higher semimajor axis for the Eulalia family due to the Yarkovsky semimajor axis drift.

This possible family suffers from the same, and even amplified, difficulties found in analyzing the Eulalia family: a center near a powerful resonance, overlapping with another family and possibly a very old age. In many tests below we will remove the Eulalia family from the data set (using previously defined boundaries) in an attempt to measure only the possible background family.

4.1.1. HCM of the background family

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The first test was done with Asteroid (2446) Lunacharsky. This asteroid has proper orbital elements of \( a = 2.355 \) AU, \( e = 0.154 \), \( i = 3.178^\circ \), and is also one of the few in this region with published visible and near infrared spectra. The HCM results for this body show that there is a highly diffuse and extended association with few family members found below a velocity cutoff of \( V_c = 150 \) m/s (Fig. 18, bottom). However, the association linked by HCM at \( V_c = 180 \) m/s and larger shows the distinct signs in the \( H \) vs. \( a \) space of a correlated family and the family size increases quickly.

The largest bodies linked to this association are Asteroids (142) Polana and (112) Iphigenia with proper elements \( a = 2.418 \) AU, \( e = 0.157 \), \( i = 3.215^\circ \) and \( a = 2.434 \) AU, \( e = 0.094 \), \( i = 3.195^\circ \) respectively (Iphigenia is linked at \( V_c = 180 \) m/s and Polana at \( V_c = 190 \) m/s). The orbital element distribution of the selected asteroids is quite large in eccentricity, spanning \( 0.1 < e < 0.2 \), but more tightly clustered in inclination between \( 1^\circ < i < 5^\circ \). Each of these large asteroids are in distinct clusters determined by their eccentricity, where (142) Polana is in the midst of the high eccentricity grouping and (112) Iphigenia with the smaller low eccentricity grouping (Fig. 19).

4.1.2. The center and age of the new Polana family

We focus on (142) Polana and (112) Iphigenia due to their size and the suggestions from the \( H \) vs. \( a \) plot that they are near the center of the family. Differentiating them is difficult due to these similarities, other than (142) Polana being embedded in a larger and denser grouping in eccentricity. When these groups are separated and plotted as \( H \) vs. \( a \), it is clear that (142) Polana is associated with the extended family structure (Fig. 20). Meanwhile (112) Iphigenia is associated with objects with larger \( H \) and larger \( a \), that are near the highest-density region of the Eulalia family. It is possible that if the Eulalia family was linked with a larger \( V_c \) in the HCM routine that many of these objects would be added to the Eulalia family.
Thus, the extended family here appears to be associated with Asteroid (142) Polana, and we use its proper semimajor axis $a = 2.418$ AU as the nominal center of the family. The using the same fitting routine as before, we then measure a best-fit at $C = 16.9 \times 10^{-5}$ AU (Fig. 19). This fit was substantially easier due to the dramatic density fall-off, and the measured best-fit $C$ value is nearly twice as large as for the Eulalia family. This $C$ directly correlates to $T = 2845$ Myr, not accounting for the initial velocity dispersion of the fragments following the collision. We can use the same initial velocity dispersions of $V_0 = 50$ m/s and $V_0 = 150$ m/s, despite not having a solid estimate of parent body size, which puts the age range of the Polana family at $\sim 2000–2500$ Myr. However, uncertainty about YORP reorientation of spin axes adds age uncertainty which becomes increasingly important at increasingly larger asteroid sizes for older families. This adds substantial uncertainty to the upper boundary of this age estimate, and the conservative estimate is simply an age greater than 2000 Myr.

4.1.3. Significance test of “new Polana” shape

Given the low density of asteroids in the WISE dataset at low $a (<2.3$ AU) and $H (<13)$, it is fair to question if the characteristic shape of the new Polana family is not simply a statistical fluke caused by decreasing asteroid density near the $v_0$ secular resonance. Specifically, if the gaping hole in the sample with $a < 2.3$ AU and $H < 13$ is due simply to statistical fluctuations, then the boundary of the new Polana Yarkovsky “V-shape” may simply be an artifact and not the edge of an asteroid family.

A simple test of the significance of this was to take the entire distribution of asteroids in our dataset and randomly re-distribute them while preserving the orbital and size distributions. More simply, the values of $a, e, i$ and $H$ were each separately randomized 1000 times. A test of number of asteroids with $a < 2.3$ AU and $H < 13$ was performed for each. The WISE dataset has only four asteroids in this region, while the average number found in this region was 15.7, and the smallest number was 5 for all 1000 iterations (Fig. 22).

This test did not specifically test if the V-shape was a fluke, but rather whether the stark absence of asteroids at lower $H$ was random. Finding that it is clearly significant suggests that the density contrast seen is related to actual correlated family and supports the existence of the new Polana family.

One alternative explanation for the lack of large low-albedo asteroids inside of $\sim 2.3$ AU is simply that this is the innermost edge to C-type asteroids in the asteroid belt. It is long known that primitive bodies predominately in the outer asteroid belt (Gradie and Tedesco, 1982), and some recent work has investigated various means to “implant” primitive bodies in the asteroid belt from more distant regions of the Solar System (Levison et al., 2009; Walsh et al., 2011). Levison et al. (2009) focus on capture of D- and P-type asteroids during the Solar System instability associated with the Late Heavy Bombardment, and they find a good match to the distribution of these taxonomic classes, with the inner edge of both populations around $\sim 2.6$ AU. Walsh et al. (2011) focused on the
origin of the C-class populations that are possibly scattered into the asteroid belt much earlier in Solar System history. This work shows a steep decline in primitive asteroid numbers at decreasing semimajor axis, and theoretically could be responsible for the absence of large primitive bodies inside of 2.3 AU.

4.2. Spectral hints at two families

The albedo distribution, SDSS colors and visible spectra of objects in the family regions are very similar and not useful to distinguish between families. Therefore any available spectra—especially in the near-infrared—may be able to differentiate family membership.

There is published near-IR spectra for one asteroid, (2446) Lunacharsky (de León et al., 2012), that could be a member of the proposed Polana family, and it is plotted with (142) Polana, the candidate parent (Fig. 17, also see Fig. 4 in de León et al. (2012)). Both objects show similar positive slopes beyond 1.0–1.2 μm, similar negative slopes in the visible and generally very similar morphologies.

Asteroid (495) Eulalia shows no clear feature at 1.0 or 1.2 μm in contrast to (142) Polana. There is also a clear slope difference between the two family parents beyond 1.0 μm, which has recently been studied as a diagnostic tool by de León et al. (2010) and Ziffer et al. (2011) to differentiate primitive asteroids with otherwise very similar featureless visible spectra. The hint of distinction between family parents, including additional candidate family members, is tantalizing for the possibility that near-infrared spectra could distinguish membership between the two families for the numerous smaller bodies that fall within the Yarkovsky boundaries of both. Similarly, this is enticing as a possible tool to distinguish a possible origin for primitive NEOs that have likely originated in this region of the asteroid belt, especially future space-mission targets (for example, see panel d of Fig. 17 that displays the spectrum for NEO 1999 RQ₃₆, the baseline target for NASA’s OSIRIS-REx sample return mission).

5. Conclusions and future work

The structure and past evolution of the families in the inner Main Belt are critically important in order to understand the history and evolution of the asteroid belt as well as the delivery of asteroids to NEO orbits. We have found that the primitive population in the inner Main Belt is dominated by a few very old and large families. The low-albedo component of the Nysa–Polana complex is an asteroid family parented by Asteroid (495) Eulalia. The family’s age is between 900 and 1500 Myr, and the parent body had a size between 100 and 165 km. We have also found evidence for the existence of an older and larger family centered on (142) Polana, dubbed here the “new Polana” family. This family is parented by (142) Polana and formed more than 2000 Myr ago.

In light of this work, it appears that the major contributors of primitive NEOs could be the Eulalia and new Polana family. Our dataset is limited to H < 18.8, and therefore we cannot directly observe how the smallest members (H > 18.8) of the family are behaving. We can, however, extrapolate based on the Yarkovsky curves, and estimate the H value where the Yarkovsky curve crosses a major resonance. Asteroids with a larger H can reach that resonance by simple Yarkovsky drift, while those with smaller H cannot. This method ignores complications due to YORP cycles, or other effects such as collisions, that may have a different size-dependence than the Yarkovsky effect.

In particular, we are interested in where the curves cross the v₆ resonance, as it is efficient at delivering NEOs. The new Polana family, being older, is delivering asteroids up to H ~ 16, while the Eulalia family is only now contributing bodies of H ~ 17.5. Each family has also contributed a large fraction of their total families into the 3:1 MMR. Most of these asteroids would have been directly placed into the resonance immediately following the family formation event, and therefore would have resulted in more of an rapid influx, rather than the slow and measurable contribution via the v₆ resonance. Further dynamical models beyond the scope of this work may also help to better discern the flux from each family to NEO orbits over time via both the v₆ and 3:1 MMR.

One implication of the location of both families near the 3:1 MMR, is that nearly all surviving family members have drifted inward from the family center over time. This inward drift requires a retrograde spin sense, which is a property that can be determined with lightcurve observations. It is possible to change the spin sense of an asteroid, by either collisions or YORP reorientation. Both families show an absence of small objects near the center of the family, suggesting that most have continued their inward drift without a substantial number suffering a spin–axis reorientation. This supports the implication that most members of both families should be retrograde rotators.

Each of the three proposed NEO space mission targets (1999 RQ₃₆, 1999 JU₃, and 1996 FG₃₄) are almost certainly (>90%) delivered from the inner region of the Main Asteroid belt, following the well-studied dynamical pathway from the Main Belt to NEO-orbits (Bottke et al., 2000, 2002; Campins et al., 2010; Walsh et al., 2012). More specifically, they appear to have come from the v₆ resonance at 2.15 AU, which is the dominant supplier of NEOs (Bottke et al., 2002), and their current low inclination is indicative of similarly low inclination orbits in the Main Belt. Though entire works are dedicated to understanding the origin of these specific objects, the two families studied here are likely the dominant sources of primitive NEOs. These conclusions have been reached previously in works by Campins et al. (2010) finding the Nysa–Polana complex as the likely source of 1999 RQ₃₆ (now probably from the Eulalia family), or Gayon-Markt et al. (2012) finding that the background (now largely belonging to the new Polana family) is an equal or greater contributor of primitive NEOs.

A major part of this work was the description of relatively new techniques to detect and analyse very diffuse and old asteroid families. Despite significant previous work on these topics, the discovery of both families was greatly aided by the use of the WISE albedo data, which allowed specific analysis of low-albedo objects.
Beyond the advantage of focusing on asteroids with similar physical properties, it also removed the "noisy" background of high-albedo asteroids which otherwise would have convoluted the HCM tests (resulting in the HCM linking the huge chunks of the asteroid belt). Thus the slew of new data allows a pre-selected subset of the asteroid belt from which to detect possible family correlations.

The possible pitfalls of these technique are that the portion of the asteroid belt selected could be biased or incomplete. Asteroids not included in the subset of data, those not observed by WISE for example, need to be tracked down in further iterations of the work to build a full list of family members. Though this work attempted to search for all possible parent members using numerous databases, (495) Eulalia required special dynamical care to be recognized as the parent, a task not realistic for a larger survey of very old families.

Finally, there are potentially vast implications in assigning much of what was considered to be the background of the asteroid belt to an older family, the new Polana family. While this family was particularly difficult to find, even while scouring a small subset of the entire database of asteroids, it highlights what might still be lurking in the data. How much of the background is actually part of old and diffuse families? If we continue with this exercise and continue to discover old and diffuse families will there be any background left, and what does this tell us about the origin of the asteroid belt? Certainly, the answers to these questions are beyond the scope of this project, but hopefully the flood of data from current and future spacecraft (the ESA Gaia mission for example) and larger ground-based surveys might help to answer these.

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