Gravitational torques dominate the dynamics of accreted gas at $z > 2$

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ABSTRACT

Galaxies form from the accretion of cosmological infall of gas. In the high redshift Universe, most of this gas infall is expected to be dominated by cold filamentary flows which connect deep down inside halos, and, hence, to the vicinity of galaxies. Such cold flows are important since they dominate the mass and angular momentum acquisition that can make up rotationally-supported disks at high-redshifts. We study the angular momentum acquisition of gas into galaxies, and in particular, the torques acting on the accretion flows, using hydrodynamical cosmological simulations of high-resolution zoomed-in halos of a few $10^{11} \, M_\odot$ at $z = 2$. Torques can be separated into those of gravitational origin, and hydrodynamical ones driven by pressure gradients. We find that coherent gravitational torques dominate over pressure torques in the cold phase, and are hence responsible for the spin-down and realignment of this gas. Pressure torques display small-scale fluctuations of significant amplitude, but with very little coherence on the relevant galaxy or halo-scale that would otherwise allow them to effectively re-orientate the gas flows. Dark matter torques dominate gravitational torques outside the galaxy, while within the galaxy, the baryonic component dominates. The circum-galactic medium emerges as the transition region for angular momentum re-orientation of the cold component towards the central galaxy’s mid-plane.

Key words: cosmology: theory — galaxies: evolution — galaxies: formation — galaxies: kinematics and dynamics — large-scale structure of Universe —

1 INTRODUCTION

One of the successes of the $\Lambda$ cold dark matter ($\Lambda$CDM) model of the Universe is its ability to reproduce its large-scale structures observed in galaxy distribution (e.g. Efstathiou & Eastwood 1981, Springel et al. 2006). These structures form out of the initial tiny density fluctuations of the primordial density field and under the effect of gravitational forces, matter deparps from underdense regions to flow through cosmic sheets into filamentary structures. Matter then flows from these filaments towards high-density peaks that will later become halos. In the process, matter acquires kinetic properties (e.g. vorticity, Pichon & Bernardou 1999, Laigle et al. 2015) in its journey through voids, sheets and filaments of the cosmic web, which, in turn, impact the assembly of dark matter halos. Before shell crossing, baryons follow the same initial fate as dark matter (DM) and flow from underdense regions to sheets. Yet, as they flow in sheets, pressure forces prevent them from shell-crossing so that they lose their normal velocity component to the shock front, dissipating their kinetic energy acquired at large-scale into internal energy (eventually radiated away by gas cooling processes). Following potential wells created by dark matter, baryons also flow from sheets towards filamentary structures where they lose a second component of their velocity and reach a dense-enough state to efficiently cool radiatively, leading to a different structure in gas and DM density in filaments (Pichon et al. 2011, Gheller et al. 2016, Ramsøy et al. 2021).

At first order, galaxy formation is affected by the mass of their dark matter halo host and the local environment, as encoded by the local density on sub-Mpc scales, as it is assumed that baryons have the same past accretion history as dark matter (White & Rees 1978, Mo et al. 1998). These models have proven successful at explaining a number of observed trends, in particular against isotropic statistics, in the so-called halo model (Sheth et al. 2001), yet they fail to explain some effects such as spin alignments (Tempel & Libeskind 2013, Codis et al. 2015, Dubois et al. 2014b, Chisari et al. 2017), colour (Laigle et al. 2018, Kraljic et al. 2018, 2019) or star formation rates segregation (Malavasi et al. 2017, Kraljic et al. 2019, Song et al. 2021). Indeed, the cosmic web sets preferred directions of accretion of cosmological gas that fuels star formation in the galaxy, and affects the orbital parameters of the successive mergers. The detailed gas acquisition history, captured by the critical event theory developed in Cadiou et al. (2020), how much angular momentum (AM) is advected, as well as the origin of mergers should thus all impact the formation of the galaxy. Since the physical processes involved in dark matter halo formation differ from the baryonic processes operating during galaxy formation, one can expect that the cosmic web will have a specific impact on the formation of galaxies and may explain the disparity of their properties, such as morphology, in similar-looking dark matter halos.

In particular, at fixed halo mass and local density, properties of galaxies such as their colour or the kinematic structure vary with their location in the cosmic web. One key process in the differential evolution of galaxies is gas accretion. Indeed, at large redshifts, it
Figure 1. Density-weighted projections of the large-scale gas density (first and third rows) and the galaxy and CGM (second and fourth rows) of the six galaxies at $z = 2$. The virial radius, $R_{\text{vir}}$, $R_{\text{vir}}/3$ and $R_{\text{vir}}/10$ are shown as white, blue and green dashed circles respectively. They exhibit a complex large-scale structure made of filamentary cosmic streams and diffuse gas.
has been suggested that the accretion of gas is dominated by flows of cold gas funneled from the large scales to galactic scales (Birnboim & Dekel 2003; Dekel & Birnboim 2006). This mode of accretion has then been confirmed in numerical simulations using different methods (Keres et al. 2005; Dekel & Birnboim 2006; Ocvirk et al. 2008; Nelson et al. 2013), as the source of a significant fraction of the baryonic mass but also AM (Pichon et al. 2011; Kimm et al. 2011; Stewart et al. 2013; Stewart et al. 2017), which is decisive for several galactic properties (Ceverino et al. 2010; Agertz et al. 2011; Dekel et al. 2020; Kretschmer et al. 2020). It has also been proposed that these flows may feed supermassive black holes (Di Matteo et al. 2012; Dubois et al. 2012), which in turn affect the cold inflow rates (Dubois et al. 2013).

The cosmological origin of AM is explained by tidal torque theory (TTT, Peebles 1969; White 1984; Schäfer 2009). Though its predictions do not hold on a per-object basis (Porciani et al. 2002), it can be extended to show that, indeed, AM results from torques in the early Universe (Cadiou et al. 2021). These torques in turn encode the anisotropy of the environments, which biases the AM distribution to align it with the cosmic web (Codis et al. 2015). It is then expected that gas will fall in galaxies via cold flows, feeding disks with angular-momentum rich gas that is itself aligned with the tides of the cosmic web.

Recent works have shown that the cold flows are subject to a variety of processes: they may fragment (Cornuault et al. 2018) or be disrupted by hydrodynamical instabilities (Mandelker et al. 2019), but they are also sensitive to feedback events (Dubois et al. 2013). In this context, Danovich et al. (2015) showed that in numerical simulations, cold flows are nevertheless able to feed galaxies with angular-momentum rich material (as speculated by Pichon et al. 2011; Stewart et al. 2013). In this study, it was shown that the AM acquired outside the halo at \( z = 2 \) is transported down to the circum-galactic medium (CGM): the gas then settles in a ring surrounding the disk, where gravitational torques spin the gas down to the mean spin of the baryons. Another study, albeit at larger redshifts, found that the dominant force was pressure (Prieto et al. 2017). Since there is not much freedom on the final AM of the galaxies, as constrained by their radius, the excess AM brought by cold flows has to be redistributed somehow before it reaches the disk.

The details of where this AM will end up are key to understanding the AM distribution in galaxies, but also to understanding to what extent their spin is aligned with the cosmic web. If the dominant torques acting on the AM are pressure torques, resulting from internal processes (SN winds, AGN feedback bubbles and hydrodynamical shocks), then the spin of the galaxy would likely be a result of chaotic internal processes and would lose its connection to the cosmic web. On the contrary, if gravitational torques dominate, then the spin-down of the cold gas is likely to drive a spin-up of either the disk or the dark matter halo, which themselves are the result of their past AM accretion history. In this last scenario, the details of which part(s) of the halo or the disk interact and exchange AM with the infalling material would constrain models aimed to understand the evolution of the spin of galaxies.

Historically, the study of cold accretion has been particularly challenging in numerical simulations. Early simulations using Smooth Particle Hydrodynamics (SPH) methods largely overestimated the fraction of gas accreted cold (see e.g. Nelson et al. 2013 for a discussion on this particular issue) as a result of the difficulty to capture shocks using SPH. Adaptive Mesh Refinement (AMR) simulations do not suffer from this caveat (Ocvirk et al. 2008), yet they fail at providing the Lagrangian history of the gas – in particular its past temperature – which is required to detect the cold-accreted gas.

In order to circumvent this limitation, most simulations relied on velocity-advected tracer particles (Dubois et al. 2013; Tillson et al. 2015). However, this approach yields a very biased tracer distribution that fails at reproducing correctly the spatial distribution of gas in filaments: most tracer particles end up in convergent regions (centre of galaxies, centre of filaments) while divergent regions are under-sampled. In order to reproduce more accurately the gas distribution, Genel et al. (2013) suggested relying on a Monte-Carlo approach where tracer particles follow mass fluxes instead of being advected. This was later improved to include the entire Lagrangian evolution of the gas through star formation and feedback, as well as AGN accretion and feedback (Cadiou et al. 2019).

The aim of this paper is to investigate the evolution of the AM of the cold and hot gas using cosmological simulations of group progenitors at \( z > 2 \). We provide a detailed study of the evolution of the AM of the cold and hot gas. In particular, the question of which forces are responsible for the spin-down and realignment of the AM of the gas accreted in the two modes of accretion (hot and cold) will be addressed.

Section 2 presents the numerical setup. Section 3 presents the AM evolution of the cold and hot gas. It follows the evolution of the magnitude and orientation of the AM and the different forces and torques at play in the different regions of the halos. It details the evolution of the magnitude and orientation of the AM and the different forces and torques at play in the different regions of the halos. In Section 4, we present their implication on the distribution of AM in the galaxy and the CGM. Finally, section 5 wraps things up and concludes.

In the following, we will adopt a similar naming convention as Danovich et al. (2015). We will write \( R_{\text{vir}} \) the virial radius of a halo. The outer halo is defined as the region between \( R_{\text{vir}} \) and \( R_{\text{vir}} / 3 \). The circumgalactic medium (CGM) is defined as the region between \( R_{\text{vir}} / 3 \) and \( R_{\text{vir}} / 10 \). The ‘disk’ is the region at radius \( r < R_{\text{vir}} / 10 \) where the galaxy is found.

2 METHOD

We describe the numerical setup in section 2.1. We then detail the equations driving the AM evolution in section 2.2, and the details of the extraction of the different torques in section 2.3. In section 2.4, we describe how we selected the cold gas being accreted on the halos in the simulations.

2.1 Simulations

We produced a suite of three zoomed-in regions in a 50h^{-1}cMpc-wide cosmological box, hereafter named S1, S2, S3. The three simulations contain six high-resolution halos with virial mass \( 4 \times 10^{11} \lesssim M_{\text{vir}} / M_\odot \lesssim 7 \times 10^{11} \) at \( z = 2 \), hereafter named A, B, C, D, E and F (see their properties in Table 1), containing only high-resolution dark matter (DM) particles within twice the virial radius of the halo at \( z = 2 \). We adopted a cosmology that has a total matter density of \( \Omega_m = 0.3089 \), a dark energy density of \( \Omega \Lambda = 0.6911 \), a baryonic mass density of \( \Omega_b = 0.0486 \), a Hubble constant of \( H_0 = 67.74 \text{km}s^{-1} \text{Mpc}^{-1} \), a variance at 8 Mpc \( \sigma_8 = 0.8159 \), and a non-linear power spectrum index of \( n_s = 0.9667 \), compatible with a Planck 2015 cosmology (Planck Collaboration 2015). We generated the initial conditions with MUSIC (Hahn & Abel 2011). The simulations are started with a coarse grid of 128^3 (level 7) and several nested grids with increasing levels of refinement up to level 11, corresponding to a DM mass resolution of respectively \( 6.3 \times 10^8 M_\odot \) and \( 1.5 \times 10^8 M_\odot \).
The halos are simulated with the adaptive mesh refinement code RAMSES (Teyssier 2002). Particles (dark matter, stars, black holes) are moved with a leap-frog scheme, and to compute their contribution to the gravitational potential, their mass is projected onto the mesh with a cloud-in-cell interpolation. Gravitational acceleration is obtained by computing the gravitational potential through the Poisson equation numerically obtained with a conjugate gradient method. Gravitational acceleration to the gravitational potential, their mass is projected onto the mesh with a cloud-in-cell interpolation. Gravitational acceleration is obtained by computing the gravitational potential through the Poisson equation numerically obtained with a conjugate gradient method.

We also add additional baryonic physics relevant to the process of galaxy formation at 35 pc similar to the physics of NewHorizon (Dubois et al. 2021). The simulations include a metal-dependent tabulated gas cooling function following Sutherland & Dopita (1993) for gas with temperature above $T > 10^4$ K. The metallicity of the gas in the simulation is initialised to $Z_0 = 10^{-3} Z_\odot$ to allow further cooling below $10^4$ K down to $T_{\text{min}} = 10^3$ K (Rosen & Bregman 1995). Reionisation occurs at $z = 8.5$ using the Haardt & Madau (1996) UV background model and assuming gas self-shielding above $10^{-2}$ H cm$^{-3}$. Star formation is allowed above a gas number density of $n_0 = 10^3$ cm$^{-3}$ with a Schmidt law, and with an efficiency $\epsilon_{\text{ff}}$ that depends on the gravo-turbulent properties of the gas (for a comparison with a constant efficiency see Nunez-Castineyra et al. 2020). The stellar population is sampled with a Kroupa (2001) initial mass function, where $\epsilon_{\text{ff}} = 0.317$ and the yield (in terms of mass fraction released into metals) is 0.05. Type II supernovae are modelled with the mechanical feedback model of Kimm et al. (2013) with a boost in momentum due to early UV pre-heating of the gas following Geen et al. (2015). The simulations also track the formation of SMBHs and their energy release through AGN feedback. SMBH accretion assumes an Eddington-limited Bondi-Hoisey-Littleton accretion rate in jet mode (radio mode) and thermal mode (quasar mode) using the model of Dubois et al. (2012). The jet is modelled self-consistently by following the AM of the accreted material and the spin of the black hole (Dubois et al. 2014a). The radiative efficiency and spin-up rate of the SMBH are computed assuming the radiatively efficient thin accretion disk from Shakura & Sunyaev (1973) for the quasar mode, while the feedback efficiency and spin-up rate in the radio mode follow the prediction of the magnetically choked accretion flow model for accretion disks from McKinney et al. (2012). SMBHs are created with a seed mass of $10^5 M_\odot$ for S1 and $10^6 M_\odot$ for S2 and S3. For the exact details of the spin-dependent SMBH accretion and AGN feedback, see Dubois et al. (2021). Compared to NewHorizon, the main difference is that we do not boost the dynamical friction of the gas onto SMBHs. This likely result in our AGN feedback being weaker and may explain why our simulated galaxies have larger stellar-to-halo than what one would expect from abundance matching (see Table 1). A detailed investigation of the origin of this issue is however beyond the scope of the paper.

We extract halo catalogues using ADAPTAHOP (Aubert et al. 2004), using the ‘Most massive Sub-node Method’ and the parameters proposed in Tweed et al. (2009). The density is computed from the 20 nearest neighbours and we use a linking length parameter of $b = 0.2$. Figure 1 shows the projected gas density at $z = 2$ of the six simulated halos with their virial radius on top of each image as identified by the halo finder.

### 2.2 Evolution of the specific angular momentum

The equation driving the evolution of the specific angular momentum (sAM) of the gas $l = r \times v$, where $r$ and $v$ are respectively the distance and velocity of the gas with respect to the halo centre, is obtained from the equation of motion

$$\frac{\partial v}{\partial t} + (v \cdot \nabla)v = -\frac{\nabla P}{\rho} - \nabla \phi. \quad (1)$$

Table 1. Name of the halo, name of the simulation, virial mass of the halo and the stellar mass of their central galaxy at $z = 2$.

| Name | Simulation | $M_{\text{vir}}/10^{11} M_\odot$ | $M_*/10^{10} M_\odot$ |
|------|------------|-------------------------------|---------------------|
| A    | S1         | 3.66                          | 6.07                |
| B    | S2         | 7.82                          | 9.20                |
| C    | S3         | 6.64                          | 5.09                |
| D    | S1         | 7.29                          | 4.18                |
| E    | S1         | 5.23                          | 7.84                |
| F    | S3         | 4.63                          | 3.49                |

Figure 2. Volume rendering of the density isocontours of the cold gas around galaxy A at $z = 3.6$. The cold gas is found in infalling satellites, while the filamentary structure, which connects the large-scale structure filamentary structure to the galaxy (at the centre), is obvious.
Taking the time derivative of the sAM, we obtain that
\[
\frac{dl}{dt} = r \times \left( \frac{\partial v}{\partial t} + (v \cdot \nabla)v \right) + \left( \frac{\partial r}{\partial t} + (v \cdot \nabla)r \right) \times v. \tag{2}
\]

After trivial algebra, the rightmost part of the right-hand side vanishes. Using equations (1) and (2), the Lagrangian time derivative of the sAM then reads
\[
\frac{dl}{dt} = \tau_P + \tau_\phi, \tag{3}
\]
where \(\tau_P = -r \times \nabla P / \rho\) and \(\tau_\phi = -r \times \nabla \phi\) are the specific pressure and gravitational torques. Here \(P\) and \(\rho\) are the pressure and density of the gas and \(\phi\) is the gravitational potential. The potential is obtained from Poisson equation
\[
\nabla^2 \phi = 4\pi G \rho_{tot}, \tag{4}
\]

where \(\rho_{tot}\) is the total matter density (DM, stars, gas and SMBHs) and \(G\) is the gravitational constant.

### 2.3 Torque extraction

Most of the previous works (Danovich et al. 2015; Prieto et al. 2017) have studied the relative contribution of each torque to the AM evolution of the cold gas focusing in particular on their magnitude and direction, splitting the torques between pressure and gravitational torques. In this section, we provide an improvement over these past works by computing the gravitational torques from each source (stars, DM and the gas) separately. We also lay down a general method to compute gradients in post-processing in AMR codes, which we then use to compute pressure gradients, and in particular, pressure torques.

#### 2.3.1 Gravitational torques

In the vicinity of galaxies, the different massive sources (DM, stars, gas) all contribute to the total gravitational potential \(\phi = \phi_{DM} + \phi_* + \phi_{gas}\) via their own Poisson equation
\[
\nabla^2 \phi_i = 4\pi G \rho_i, \tag{5}
\]

where \(\phi_i\) and \(\rho_i\) are the gravitational potential and the density of the component \(i\) (DM, stars, gas). One can then compute the specific forces resulting from each potential \(F_i = -\nabla \phi_i\) which can then be used to compute the specific torques at position \(r\)
\[
\tau_i = r \times F_i. \tag{6}
\]

In order to extract the torques resulting from each gravitational source, we have modified the code RAMSES to extract in post-processing the specific forces due to the different matter components (DM, gas, stars). This was performed by stripping down RAMSES to keep only the Poisson solver, applied to the density of each individual component.

#### 2.3.2 Pressure torques

The precise capture of shocks is fundamental to most astrophysical codes. These shocks then result in strong gradients which are usually captured by a few cells with a MUSCL-Hancock scheme. While numerical codes routinely deal with strong gradients, most AMR post-processing tools either do not provide any utility to compute them (pynbody, Pontzen et al. 2013; pymses, Guillet et al. 2013), or have gradient computing capacities that are not available for octree-based AMR datasets, as is the case with RAMSES (e.g., yt, Turk et al. 2011). The approach usually followed is to project data on a fixed resolution grid, which is then used to compute gradients using a finite-difference scheme. Even though this approach yields sensible results when the fixed grid resolution matches the AMR resolution, it yields null values when the AMR resolution is coarser and smoothes out the gradients when the AMR resolution is finer. Therefore, we will deal here directly with the physical quantities at the scale of the AMR grid.

Using a tree search algorithm, we have developed a post-processing tool that is able to compute finite-difference gradients directly on the AMR grid. The binary search algorithm ensures that any given location is found in at most \(N\) steps, where \(N\) is the number of AMR levels in the simulation (typically between 10 and 20). To do so, we have augmented the yt code (Turk et al. 2011) to enable the computation of gradients for octree AMR datasets (The yt Project, in prep.). The algorithm works as follows. (a) Loop over all octs in the tree. (b) Compute the positions of the \(4^3 = 64\) virtual cells centred on the oct and extending in \(\pm 2\Delta x\) in three directions. (c) Get the value of interest at the centre of each virtual cell from the AMR grid. If the virtual cell exists on the grid or is contained in a coarser cell, the value on the grid is directly used. If the virtual cell contains leaf cells, the mean of these cells is used. (d) Compute the gradient of the quantity using a centred finite-difference scheme on the \(4^3\) grid. (e) Store the value of the gradient in the central \(2^3\) cells.

### 2.4 Cold gas selection

The ratio of the total accreted mass with a maximum temperature below a given threshold \(T_{\text{max}}\) to the total gas mass – the cold fraction – is a widely reported quantity in the study of the cosmological gas accretion, dating back to Keres et al. (2005). In this paper, we use a constant temperature cut \(T \lesssim T_{\text{max}} = 2.5 \times 10^5\) K (see Appendix A

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\(^1\) Here we ignore SMBHs, as their gravitational potential may only dominate very close to the center of the galaxy.

\(^2\) The fiducial implementation solves the Poisson equation directly on the total matter density (gas + stars + DM).
Figure 4. Radial profile of the sAM in spherical shells in the cold phase (blue lines) and hot phase (red lines) for different redshift of accretion (each panel, as labelled). Error bars (shaded regions) are estimated from the standard deviation of the six galaxies. We show the virial radius (dotted gray line) and the edge of the CGM (dashed gray line). At \(2 \leq z < 3\), the cold gas enters the virial radius with a larger specific angular momentum than in the hot phase. Once it reaches the CGM (\(R_{\text{vir}}/3\)), the typical specific angular momentum is at all time comparable between the cold and the hot phase.

Figure 5. Thick line: median relative orientation of the sAM of the cold gas at \(R_{\text{vir}}\) compared to its value at \(3R_{\text{vir}}\) (left), at the edge of the CGM, \(R_{\text{vir}}/3\) (middle) and at the disk’s edge, \(R_{\text{vir}}/10\) (right) in the cold phase (blue lines) and hot phase (red lines). Error bars (shaded regions) are estimated from the standard deviation of the six galaxies. The orientation of the sAM is mostly conserved in the cold and hot phase between \(3R_{\text{vir}}\) and \(R_{\text{vir}}\). Between the virial radius, \(R_{\text{vir}}\), and the CGM, \(R_{\text{vir}}/3\), the orientation of the cold phase is better preserved than in the hot phase. This orientation is mostly lost between the CGM and the disk, \(R_{\text{vir}}/10\).

for a discussion on the effect of the threshold, see also [Nelson et al., 2013]. We define the ‘cold gas’ or ‘cold-accreted gas’ at redshift \(z_0\) as the particles that match all three criteria:

(i) the baryons have been accreted by \(z_0\), i.e. they are within the inner region of the halos \(r < 0.3R_{\text{vir}}\) at \(z = z_0\);
(ii) prior to accretion, the baryons were in the gas phase and never heated above the threshold temperature \(T_{\text{max}}\) from \(1.5R_{\text{vir}}\) to \(0.3R_{\text{vir}}\);
(iii) the baryons were never accreted on a satellite galaxy prior to their accretion in the main galaxy. In practice, this is done by excluding any particle found at any time at less than a third of the virial radius of any halo other than the main one.

Conversely, particles that heated up at least once above the temperature threshold during their accretion will be referred to as ‘hot gas’ or ‘hot-accreted gas’. We stress that in the selection steps (i) and (iii), we include baryons in all phases, including in the stellar phase. Thanks to the Monte-Carlo tracer particle scheme we use, these baryons can be accurately traced back in time, including when moving from one phase to the other (see Cadiou et al. 2019 for more
Angular momentum dynamics dominated by gravity

3 RESULTS: RELATIVE TORQUING

3.1 The angular momentum magnitude

Before turn-around, gas acquires AM via torque from the cosmic web as captured by TTT (Hoyle [1949] Peebles [1969] White [1982] Cateni & Theuns [1996]). The subsequent evolution of the cold-accreted and hot-accreted gas may however differ. In order to study how the sAM evolves, one can study the Lagrangian evolution of the sAM of all gas accreted at the same time as a function of its radius, as shown on Fig. 4 and depending on its accretion mode. The figure presents the Lagrangian evolution of the sAM as a function of radius for the cold (blue lines) and hot gas (red lines). In all halos, the sAM of the gas decreases by a factor $\sim 4$ between $2R_{\text{vir}}$ and $R_{\text{vir}}/3$ in both accretion modes (cold and hot). We however note that at late times $2 < z < 3$, the sAM of the cold-accreted gas prior to its accretion is about twice larger than the hot-accreted gas, yet it ends up with a comparable one in the disk.

3.2 The angular momentum orientation

So far, we have only described the evolution of the magnitude of the sAM of the gas. In practice, the evolution of the orientation of the sAM evolves slightly differently. In order to quantify the evolution of the sAM orientation, we define for a parcel of gas the angle between its sAM at radius $R_1$ and its sAM at radius $R_2$ as

$$\cos \theta = \frac{I(R_1) \cdot I(R_2)}{|I(R_1)||I(R_2)|}.$$  

We emphasize here that this angle is measured individually for each tracer particle using its Lagrangian history, so that $I(R_1)$ may be measured at a different time than $I(R_2)$. Values close to one are found if the orientation is preserved, whereas random reorientations would yield values close to zeros. We measure $\cos \theta$ as a function of the time of crossing $R_{\text{vir}}$ for all particles in the cold- and hot-accreted gas in our six galaxies. We then compute the mean $\langle \cos \theta \rangle$ in the respective phase of each galaxy, and also show in Fig. 5 its median value from the sample of six galaxies. We show $\cos \theta$ measured between $R_{\text{vir}}$ and $3R_{\text{vir}}$ (left panel), between $R_{\text{vir}}$ and the outer edge of the CGM ($R_{\text{vir}}/3$, centre panel) and between $R_{\text{vir}}$ and the disk ($R_{\text{vir}}/10$, right panel). In all three panels, the reported time is always the time at which the particles crossed the virial radius. We see that most of the realignment happens in the CGM (right panel), where $\cos \theta$ drops to values close to $-\pi/2$ and only weakly greater than $0$.

We have presented in sections 3.1 and 3.2 that the cold gas retains its orientation and magnitude down to the CGM, while the hot gas starts realigning at a larger radius. Let us now study which torques are responsible for the spin-down and realignment of the gas. We split the total torques between pressure torques and gravitational torques, as was done in equation (3). The gravitational torques are further split between their DM, gas and stellar components following section 2.3.1 in order to assess the role of the various components. We then sum the specific torque exerted by each of the component on the gas in concentric shells and mass-average (using the gas tracer particle mass) it to obtain “angular-averaged profiles”.

We show on Fig. 6 angular-averaged profiles of the magnitude of each of the torque components, $\langle |\mathbf{\tau}| \rangle$, averaged over all six galaxies, for the gas accreted at $z = 3$ or earlier. The profiles are computed independently for the cold and the hot phase. Since we average the magnitude of torque, this allows us to quantify which torques dominate locally the evolution of the angular momentum. First, we observe that the radial profiles of the gravitational torques are comparable in both phases of the gas. This is expected since gravity is a non-local force and is thus independent of the local thermodynamical conditions of the gas. On the contrary, pressure torques, which depend on the local thermal structure of the gas, display significant differences between the cold and the hot phase. Between $2R_{\text{vir}}$ and $R_{\text{vir}}/3$, pressure torques in the hot phase are on average one order of magnitude larger than in the cold phase. We find no evidence of a

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3. Because our criterion to define cold/hot accretion depends on the entire thermal history during accretion, the analysis of the gas at two virial radii need to be done at least two free-fall times before the end of the simulation ($z = 2$) for it to have time to be accreted by the central galaxy.

4. As opposed to taking the magnitude of the averaged torque, as done later.
Figure 7. Mean angular-averaged profiles of specific gravitational torques (black) and specific pressure torques (red) integrated in spherical shells in different redshift bins. Compared to Fig. 6, we compute here the magnitude of the mean of the torques, $\| \tau \|$, rather than the mean of the magnitudes, $\sum \| \tau \|$; this yields the net contribution of each torque applied to each gas phase. The cold accreted gas (solid line) and the hot accreted gas (dashed lines) are computed for all six halos, the lines indicate the mean value form the sample of six halos and the shaded region show the standard deviation. At $\z < 4$, gravitational torques weakly dominate globally in the cold phase while at $\z > 6$, pressure torques dominate in the hot phase.

Figure 8. Ratio of the magnitude of the angular-averaged gravitational torques to the total torques in the cold phase (blue) and hot phase (orange). Where gravitational torques dominate, this ratio is close to 1. Where pressure torque dominate, it is close to 0. Importantly, gravitational torques prevail ($> 50\%$) throughout the halo in the cold phase at all redshifts and in the hot phase at $\z \leq 4$. 
Angular momentum dynamics dominated by gravity

3.4 Spatial and temporal coherence of torques

We have seen that, locally, pressure torques dominate over gravitational torques in the hot phase, and have comparable magnitudes in the cold phase. However, once averaged over all angles, the latter dominate over the former at late times. Let us now investigate the origin of this reversal by estimating the coherence of the torques.

With the same redshift cuts as in Fig. 7, we finally show in Fig. 8 the ratio of the net gravitational torques to the sum of the net torques in the cold and hot phases. This allows us to make more quantitative statements about the net torques in the cold and hot phases. Below \( z < 4 \), we report that gravitational torques are responsible for the majority of the torquing in the CGM and down to the edge of the disk in the cold and hot phase. In the cold phase, gravitational torques dominate at all times in the CGM, while in the hot phase, pressure torques dominate until \( z > 4 \); at \( z < 4 \), the dynamical evolution becomes marginally dominated by gravitational torques.

difference in the torques (both gravitational and pressure) in the two phases prior to entering the halo and once inside the CGM.

Gravitational torques are driven by DM all the way down to the galactic disk at \( R_{\text{vir}}/10 \), where the contribution from the stellar disk and the gaseous medium become comparable. In the cold phase, we find that pressure torques have the same magnitude as the DM gravitational torques in the circum-galactic medium and outside the halo, while they dominate by an order of magnitude in the hot phase. Let us recall that the origin of pressure torques are local by nature, while gravitational torques are sourced by the full matter distribution within the halo scale. As a consequence, we expect that gravitational torques are more coherent, i.e. their effect adds up, over large scales and over time. On the contrary, we expect pressure torques to have small-wavelengths short-timescales variations, so that their net contribution to torquing the gas may partially cancel out when averaged over large scales, hence over time when following the flow. To quantify this, we compute in Fig. 7 the magnitude of the angular-averaged torques, \( ||\langle \mathbf{\tau} \rangle|| \), in the cold and hot phases, as a function of accretion time. We note that the gravitational torques acting on the cold/hot accreted gas have the following hierarchy: DM gravitational torques dominate down to \( R_{\text{vir}}/10 \) where they become comparable to torques from the stellar disk. Interestingly, torques from gas are not dominant anywhere from \( 2R_{\text{vir}} \) to \( R_{\text{vir}}/10 \). For the sake of clarity, we only show the total gravitational torques, \( \mathbf{\tau} = \mathbf{\tau}_{\text{DM}} + \mathbf{\tau}_{\text{*}} + \mathbf{\tau}_{\text{gas}} \) instead of each individual component. We find that the net gravitational torques dominate over the net pressure torques in the cold phase (solid lines) at \( z \leq 4 \), and slightly less so in the hot phase (dashed lines), in the CGM. At high-redshift \( z > 6 \), this hierarchy reverses in the hot phase, which becomes dominated by pressure torques. Let us however note that at these redshifts, only a marginal fraction of the matter is accreted hot, as was shown on Fig. 3, so that the hot-accreted gas may be a highly-biased (sub)-sample. We also checked that the hierarchy of gravitational torques is the same as in Fig. 6: DM gravitational torques dominate gravitational torques outside the galactic disk, and baryons dominate inside of it.

With the same redshift cuts as in Fig. 7 we finally show in Fig. 8 the ratio of the net gravitational torques to the sum of the net torques in the cold and hot phases. This allows us to make more quantitative statements about the net torques in the cold and hot phases. Below \( z < 4 \), we report that gravitational torques are responsible for the majority of the torquing in the CGM and down to the edge of the disk in the cold and hot phase. In the cold phase, gravitational torques dominate at all times in the CGM, while in the hot phase, pressure torques dominate until \( z > 4 \); at \( z < 4 \), the dynamical evolution becomes marginally dominated by gravitational torques.

Figure 9. Projected map of the coherence of the gravitational torque and pressure torques (left and right panel respectively) around galaxy A at \( z = 2 \) in the cold gas phase. The effective smoothing scale is 1 kpc (pixel size). The virial radius is shown as a dashed line, a third of the virial radius is shown as a blue dashed line. Gravitational torques are coherent in the cold flows down to the edge of the CGM, while pressure torques very much less so. A qualitatively similar picture emerges for similar maps in the hot phase.

Figure 10. The radial profiles of the coherence of torques in the cold (solid) and hot (dashed) phases for the pressure torques (red) and gravitational torques (black). The coherence is defined as the ratio of the norm of the sum \( \sum_{\text{neigh}} \mathbf{\tau} \) to the sum of the norms \( \sum_{\text{neigh}} ||\mathbf{\tau}|| \) in a cell and its 26 neighbours. Gravitational torques are coherent over large scales, so that the sum of torques exerted on neighbouring gas cells adds up. On the contrary, pressure torques fluctuate on the scale of individual gas cells, so that their sum partially cancels out. Pressure torques have particularly large fluctuations in the cold phase at small radii.
4 DISCUSSION

4.1 Comparison to Danovich et al. (2015)

This work differs from Danovich et al. (2015) as follows (a) we make use of simulation with a similar maximum resolution of 30 pc but with a different code and different sub-grid models, (b) we rely on tracer particles which trace the history of gas elements, (c) we compute the gravitational torques from each component, (d) we compute the pressure torques directly in the AMR grid, and (e) we refer here to the AM per unit mass.

First, taken at face value, our results of Fig. 4 appear to be in conflict with their Figure 1, that showed that the cold gas has a spin parameter $2 - 3$ larger than the hot gas at the virial radius. Indeed, we find that both the cold and hot gas have comparable spin parameters in both phases for the pressure and gravitational torques. This illustrates that pressure torques have little spatial coherence, as expected, so that different locations of the cold flows may be either spin-up or spin-down. On the contrary, large patches of the cold flows undergo coherent gravitational torques that can add up. In the disk, all torque sources loose their long-range spatial coherence and appear noisy.

$\sum_{\alpha} r_{\alpha} \approx 500$ Myr to go

$\frac{2\pi}{3} - 1 \approx 26$ neighbours to the sum of the magnitudes, i.e.

$$r_{\alpha} = \left[ \sum_{i=1}^{27} \left\| \tau_{\alpha i} \right\| \right]$$

where $\alpha$ indicates which component we are interested in (gravitational, pressure) and $i$ runs over the indices of the central cell and its 26 neighbours. The grid we project onto has cells of size 500 pc and we thus measure fluctuations in the torques on ~1 kpc scales. Ratios close to one indicate regions where the torques add up, while ratios close to zero are found where torques lack spatial coherence and cancel out.

We show in Fig. 9 mass-weighted projected maps of the coherence ratio, $r_{\alpha}^c$, in the cold phase. Gravitational torques are coherent all the way to the CGM, while pressure torques much less so. This is quantified in Fig. 10 in which we show radial profiles of the ratio in both phases for the pressure and gravitational torques. This illustrates that pressure torques have little spatial coherence, as expected, so that different locations of the cold flows may be either spin-up or spin-down. On the contrary, large patches of the cold flows undergo coherent gravitational torques that can add up. In the disk, all torque sources lose their long-range spatial coherence and appear noisy.

4.2 Impact of gravitational interactions and role of the CGM

At large radii, the evolution of the AM follows the tides imposed by the cosmic web, as explained by TTT (e.g. Codois et al. 2012, 2015). The gas then flows on the forming galaxy *via* two different channels: the hot and cold accretion modes, in particular for massive enough galaxies at $z \gtrsim 2$ (Birnboim & Dekel 2003, Keres et al. 2005, Dekel & Birnboim 2006, Ocvirk et al. 2008, Nelson et al. 2013). The pre-dominance of one or the other channel can be used to understand the formation of disky galaxies and the internal evolution of the galaxy. Indeed, in cold flows, the gas is able to penetrate deep in the halo and can feed the galaxy with fresh gas: we confirm that it does so with a steady AM orientation down to the CGM ($R_{vir}/3$), in agreement with previous findings (Pichon et al. 2011, Stewart et al. 2013).

In numerical simulations, it has been observed that cold gas has a higher AM at larger radii, as measured by their spin parameter (Kimm et al. 2011, Tillson et al. 2015, Danovich et al. 2015) which is up to one order of magnitude larger than that of the DM. However, in the CGM and the disk, the spin parameter of the gas is found to be only three times larger than that of the DM at the same location, and the nature of the torques leading to this spin-down is still debated today. Danovich et al. (2015) argued that the dominant torques, in halos of mass $\sim 10^{12} M_\odot$ at $1.5 < z < 4$, are gravitational torques regardless of the distance to the galaxy. Focusing on a massive halo of $3 \times 10^{10} M_\odot$ at $z \geq 6$, Prieto et al. (2017) found that, for those objects, the dominant torques were from pressure torques. In this work, we find that pressure torques are locally dominant in the hot-accreted gas and are comparable to the DM gravitational torques in the outer halo. While pressure forces can act locally as the dominant forces, we found that their net contribution is subdominant in the cold phase until $z = 2$, and in the hot phase until $z \approx 4$. We found that this reflects the lack of large-scale coherence of pressure torques, which can-
cel out when averaged over large scales. Conversely, gravitational forces, which depend on the distribution of matter on larger scales, are able to coherently torque the infalling gas, resulting in most of the spin-down signal.

The net effect of the gravitational forces is to spin-down the accreted gas. Indeed, non-spherical mass distributions are able to exchange angular momentum through gravitational interactions with the accreting gas. One possible reason is the following: under the effect of gas infall, the DM halo and the disk becomes slightly elongated which in turn creates a tide that will torque the hot gas down. In order to quantify the polarisation of the halo and disk induced by the gas in the halo and in the cold phase, one could decompose the gravitational potential created by these two components and verify if it indeed creates such tidal features. This is however beyond the scope of the current paper. Using the torque magnitudes of Fig. 6, the typical angular momentum of the gas upon its entry in the halo ($\sim 10^7 \text{km s}^{-1} \text{kpc}$) would be depleted in a time $t_{\text{f,DM}}(R = R_{\text{vir}}) \approx (10^3 \text{km/s/kpc})/(2 \text{km/s/kpc Myr}^{-1}) \approx 500\text{Myr}$, which is about one free-fall times $t_{\text{ff}} = 500\text{Myr}$ at $z = 2$. In our simulations, we find that cold-accreted gas falls in about one free-fall time, while hot-accreted gas takes in average $1000 \pm 500\text{Myr}$ to fall from $3R_{\text{vir}}(z = 2)$ to $R_{\text{vir}}(z = 2)/3$ where $R_{\text{vir}}(z = 2)$ is the final virial radius of the halo at $z = 2$. Since the hot gas lingers outside the CGM, torques, and in particular pressure torques, have more time to erase its initial direction set at cosmological scales. This induces a weaker alignment compared to the cold-accreted gas as we observed in Fig. 5. Interestingly, even though the hot accreted gas lingers for longer, we note that its alignment with its pre-accretion direction is not entirely lost until $R_{\text{ff}}/3$.

As reported in Rosdahl & Blazitz (2012), the trajectory of the cold gas is different and follows a mostly radial (with a non-null impact parameters) free-fall trajectory. In our simulation, the cold gas typically takes $500 \pm 350\text{Myr}$ to go from $3R_{\text{vir}}$ to $R_{\text{ff}}/3$, which is roughly equal to the typical torque-down timescale, so that cold-accreted gas has less time to be reoriented. As the cold gas plunges into the halo, the influence of the disk increases up to the point where torques become dominated by stars. Interestingly, the radius at which most of the AM, orientation included, has been lost coincides with the edge of the disk at $R_{\text{vir}}/10$. This is in broad agreement with Figures 16 and 17 of Danovich et al. (2015), which found that the torques generated by the disk increase significantly at $\sim R_{\text{vir}}/10$, where they act to realign the angular momentum of infalling material to the plane of the disk spin. This may be an indication that the disk is actually responsible for the realignment, and will require further work to understand the coupling between the accreted material and the stellar disk, the gaseous disk and the CGM. In this scenario, the AM of the freshly accreted material would align with the CGM spin and the galactic spin and, since this gas will later be mixed in the disk and eventually form stars, this would provide an explanation for the observed alignment of the CGM’s spin and the galactic spin measured in simulations, but not with the halo’s spin as a whole. [Bailin et al. 2005] [Tenneti et al. 2015] [Velliscig et al. 2015] [Chisari et al. 2017] [Welker et al. 2017, 2018]. This hypothesis could be addressed following a similar analysis as was done in this paper, but isolating further the gravitational torques from the CGM and from the galaxy alone: this will be the topic of future work.

4.3 Effect of cold flows stability on AM transport

Cornuault et al. (2018) proposed that cold flows do not survive within the halo. They suggested that they instead fragment into (unresolved) clouds, while their internal pressure increases. In the process, the kinetic energy of the gas funnelled in turbulence is dissipated as the result of radiating more thermal energy due to the more efficient mixing between the cold and hot phase, effectively loosing the shielding effect usually assumed for cold flows. In this scenario, turbulence in cold flows could contribute to efficiently mix the angular-momentum rich cold gas to the hot gas. This would likely result to a diffusion of the AM of the cold gas into the hot medium and increase the relative importance of pressure torques to the problem of the AM transport.

Using idealised simulations, Mandelker et al. (2016), Padnos et al. (2018), Mandelker et al. (2019), Sparre et al. (2019), and Aung et al. (2019) showed that cold flows may be sensitive to the Kelvin-Helmholtz depending on redshift and the mass of the central object. In particular, they showed that thin-enough filaments can be destroyed before reaching the galaxy. In this last case, the cold gas would effectively lose its angular momentum to the hot halo before interacting with the galaxy. However, the effect of gravitational torques would likely be similar, though they may act for a longer time before the gas plunges into the CGM. Interestingly, these studies also suggested that cold flows may entrain the neighbouring hot gas as they fall in while slowing down the infall of the cold gas (Mandelker et al. 2020), which may result in an efficient mixing of the AM at the boundary of the cold flows. Berlok & Pfrommer (2019) suggested that the mixing may be decreased if one considers magnetised flows with field lines parallel to the flow, as a result of a magnetic tension working against the Kelvin-Helmholtz instability, while thermal conduction can also have an important effect on stabilising the mixing process (Armillotta et al. 2016) [Kooij et al. 2021]. Simulations in the cosmological with enhanced spatial resolution (with hyper-Lagrangian refinement scheme) in the CGM have been realised but show contradictory results about the effect on the cold-gas mass content of the CGM (Van de Voort et al. 2019; Peeples et al. 2019) [Suresh et al. 2019] [Hummels et al. 2019], while the effect on the galaxy remains elusive.

Dubois et al. (2013) showed in a high redshift $z > 6$ massive halo that the AGN activity is able to significantly decrease the cold gas mass reaching the CGM and modify the filamentary structure up to the outer regions. Nelson et al. (2015) showed that AGN feedback is able to significantly increase the infall time of the cold gas. The overall effect is to increase the infalling time of the cold gas, which, if large enough, would allow torques to erase the initial direction of the cold-accreted gas, as is already the case for the hot accretion.

The exact role of the various feedback processes on the transfers of angular momenta in the various CGM phases and onto the central galaxy will need to be elucidated; we defer this to future work.

5 CONCLUSION

Using a set of high-resolution zoom-in simulations including the physics for star formation, SN and AGN feedback from NewHorizonDuo (Dubois et al. 2021), we have studied the evolution of the AM of gas accreted via the cold and the hot mode around six group progenitors at $z \geq 2$. We also presented new numerical methods to extract the contributions of the different forces and torques (gravitational and pressure torques).

We found that the mode of accretion has little impact on the evolution of the magnitude of the sAM, but has a small but noticeable effect on its direction. Cold-accreted gas better retains its initial direction down to the CGM (see also Tillson et al. 2015 their figure 8). This initial alignment is however mostly lost once the gas reaches the disk, regardless of its accretion mode. We have provided a de-
Spin-up by cosmic web
cold accretion
large scale filament

Figure 11. Summary sketch of the evolution of the AM of the accreted gas and of the dominant torques applied on it. Outside the virial radius, DM torques dominate these torques. In the outer halo, DM torques dominate, except at high $z$ in the hot phase, where pressure torques dominate the dynamics. In the CGM, gravitational torques (DM, star and gas) dominate at $z < 4$. At $z \geq 4$, pressure torque also contribute to the dynamics of the cold phase, while they dominate in the hot phase. These torques lead to the spin down of the accreted gas in the CGM, while the realignment of the AM happens at a closer radius for the cold-accreted gas. The CGM emerges as the interface between the large-scale cosmic web and the galactic disk where most of the realignment and AM redistribution happens.

tailed analysis of the torques acting on the accreting material, revealing that pressure torques are locally larger than gravitational torques in the hot-accreted phase, and are comparable in the cold-accreted phase. Once averaged over all angles, we find that the net DM gravitational torques dominate the global evolution of the AM in cold gas, especially at later times. In the hot-accreted phase, however, the contribution of the gravitational torques is significantly reduced, and only dominates at $z < 4$.

Our findings support models in which most of the AM is able to flow down to the CGM where gravitational torques redistribute it to the DM and the disk component through gravitational interactions, effectively transporting AM from the scales of the cosmic web into the CGM (Pichon et al. 2011). At high-redshift, the emerging picture is that the spin of the gas, acquired at cosmological scales, is indeed transported mostly unimpaired in cold flows up to the CGM (see Fig. 11). Upon reaching the CGM, most of the spin’s amplitude has been lost to other components, yet its orientation is still partly preserved (within 60°). A key qualitative difference of gas torquing specifically within the inner region of the CGM seem to be the growing impact of torques from the disc itself, which has its own local (partially de-correlated) orientation, reflecting the geometry of past accretion. As the contributions from such torques become dominant the flow finally flips one last time. This highlights the crucial role played by the CGM interface between the cosmic web and the disk, which appears as the missing piece of the puzzle between the large-scale cosmological angular momentum acquisition, dictated by tidal torque theory, and the formation of the embedded stellar disk, later shaped by secular evolution and feedback processes.

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DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

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APPENDIX A: IMPACT OF TEMPERATURE CRITERION

To assess the robustness of our temperature selection, different temperature cuts have been tested. The results are shown on Fig. A1 for absolute temperature cuts (left column, from top, to 10^3 K; T ≤
2.5 \times 10^5 \text{K} and \( T \leq 5 \times 10^5 \text{K} \) or temperature cuts relative to the virial temperature (right column, from top to bottom \( T/T_{\text{vir}} \leq 1/2, 1 \) and 2). In the range explored, all temperature cuts lead to the same conclusion that at high redshift, all the accretion is through cold flows. For the mass range presented in this paper, the cold gas fraction decreases to a few percents by \( z = 2 \). Finally, our results are qualitatively unchanged when using a different temperature cut, though the difference in evolution between cold and hot mode becomes blurred with lower thresholds.
$T \leq 10^5 \text{K}$

$T \leq T_{\text{vir}}/2$

$T \leq 2.5 \times 10^5 \text{K}$

$T \leq T_{\text{vir}}$

$T \leq 5 \times 10^5 \text{K}$

$T \leq 2T_{\text{vir}}$

**Figure A1.** Evolution of the cold fraction for different temperature cut criterion.