THE EVOLUTION OF THE SCATTER OF THE COSMIC AVERAGE COLOR–MAGNITUDE RELATION: DEMONSTRATING CONSISTENCY WITH THE ONGOING FORMATION OF ELLIPTICAL GALAXIES

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ABSTRACT

We present first measurements of the evolution of the scatter of the cosmic average early-type galaxy color–magnitude relation (CMR) from $z = 1$ to the present day, finding that it is consistent with models in which galaxies are constantly being added to the red sequence through truncation of star formation in blue cloud galaxies. We used a sample of over 700 red sequence, structurally selected early-type galaxies (defined to have Sérsic index $>2.5$) with redshifts $0 < z < 1$ taken from the Extended Chandra Deep Field South (173 galaxies) and the Sloan Digital Sky Survey (550 galaxies), constructing rest-frame $U - V$ colors accurate to $<0.04$ mag. We find that the scatter of the CMR of cosmic average early-type galaxies is $\sim 0.1$ mag in rest-frame $U - V$ color at $0.05 < z < 0.75$, and somewhat higher at $z = 1$. We compared these observations with a model in which new red-sequence galaxies are being constantly added at the rate required to match the observed number density evolution, and found that this model predicts the correct CMR scatter and its evolution. Furthermore, this model predicts approximately the correct number density of "blue spheroids"—structurally early-type galaxies with blue colors—albeit with considerable model dependence. Thus, we conclude that both the evolution of the number density and colors of the early-type galaxy population paint a consistent picture in which the early-type galaxy population grows significantly between $z = 1$ and the present day through the quenching of star formation in blue cloud galaxies.

Key words: galaxies: elliptical and lenticular, cD – galaxies: evolution – galaxies: general – galaxies: stellar content – surveys

1. INTRODUCTION

One of the best-known and most powerful scaling relations of the early-type (elliptical and lenticular) galaxy population is the systematic reddening of their colors with increasing luminosity: the color–magnitude relation (CMR). The slope of the CMR is driven by a correlation between metallicity and mass (Faber & Jackson 1976; Kodama & Arimoto 1997; Terlevich et al. 1999; Trager et al. 2000; Gallazzi et al. 2006), while the scatter is determined by scatter in both age and metallicity, where it is generally thought that age is the dominant driver (Bower et al. 1992; Trager et al. 2000; Gallazzi et al. 2006, although Trager et al. 2000 argue that an anticorrelation between age and metallicity keeps the scatter of the early-type galaxy scaling relations relatively modest while allowing significant scatter in both age and metallicity). The scatter in this correlation is relatively small (Baum 1962; Visvanathan & Sandage 1977; Bower et al. 1992; Terlevich et al. 2001; McIntosh et al. 2005a). Because the color of stellar populations is strongly affected by their ages and metallicities (Worthey 1994), this correlation is a powerful probe of the formation and evolution of the stellar populations in early-type galaxies. The small intrinsic scatter found in some clusters (as little as $\sigma_{U-V} = 0.04$ mag in Virgo and Coma; Bower et al. 1992; Terlevich et al. 2001; although other clusters can have scatters approaching 0.1 mag; McIntosh et al. 2005a) gave considerable momentum to the notion that early-type galaxies formed the bulk of their stars at early times and that their stellar populations have aged essentially passively to the present day.

In the last few years, this position has been challenged by evidence from deep redshift surveys that the cosmic average red-sequence galaxy population (i.e., averaged over all environments) builds up in stellar mass by roughly a factor of 2 over the interval $z = 1$ to $z = 0$ through the addition of new red-sequence galaxies (Chen et al. 2003; Bell et al. 2004b; Cimatti 2006; Brown et al. 2007; Faber et al. 2007; Scarlata et al. 2007, although some of the papers argue for a buildup in stellar mass only in galaxies with $M_\star > 10^{11} M_\odot$). These “new” red-sequence galaxies are the result of truncation of star formation in some fraction of the blue cloud population (Bell et al. 2007) through, e.g., galaxy–galaxy merging (Bell et al. 2004b; Faber et al. 2007; Hopkins et al. 2007) or environmental processes such as strangulation or ram-pressure stripping (e.g., Kodama & Smail 2001).

Such a scenario makes strong predictions about what the scatter of the CMR and its evolution should be as a function of redshift (van Dokkum & Franx 2001); to first order the scatter is expected to be constant with redshift. The object of this paper is to quantitatively test this picture. We carefully measure the CMR evolution of galaxies selected to have concentrated light profiles and red colors—taken as a proxy for the early-type galaxy population—from $z = 1$ to the present day, and compare it to a toy model of a growing red sequence. We use the Sloan Digital Sky Survey (SDSS) for the low-redshift CMR measurement, and a sample of galaxies with spectroscopic redshifts and accurate Hubble Space Telescope (HST) colors from the Extended Chandra Deep Field South.
(CDFS hereafter) to probe the CMR out to \( z = 1 \). As it was a priori unclear how large the CMR scatter should have been, we adopted a conservative approach that optimized rest-frame color accuracy at the expense of sample size, choosing galaxies with spectroscopic redshifts and within relatively narrow redshift slices (to minimize \( k \)-correction uncertainties) and with color \( HST \) imaging (to minimize color measurement error). The data are described in Section 2. We describe the \( k \)-corrections and their uncertainties for the intermediate redshift sample in Section 3. We present our measurements of the intercepts and scatter of the CMR for color and structurally selected samples as a function of redshift in Section 4. In Section 5, we compare the observed results to stellar population models of increasing complexity, finally comparing it to a model for the growth of the red sequence through the truncation of star formation in blue cloud galaxies. We present our conclusions in Section 6.

The casual reader may wish to skip to Section 5 directly. In what follows, we assume \( \Omega_m,0 = 0.3 \), \( \Omega_{\Lambda,0} = 0.7 \), and \( H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1} \) and a universally applicable Kroupa (2001) stellar IMF for stellar population modeling.

2. DATA

We use data from two different sources, depending on redshift. For galaxies with \( 0.5 < z < 1 \), we choose to determine accurate colors for galaxies with spectroscopic redshifts in the \( HST/GEMS \) survey of the CDFS. This is crucial for minimizing the color measurement error, placing the strongest possible constraints on the intrinsic scatter of the CMR. To complement this data set at low redshift, we use a sample drawn from the SDSS at \( z = 0.05 \).

2.1. Intermediate Redshift Data

For the intermediate redshift range, up to \( z = 1 \), we use data taken in the Extended CDFS (E-CDFS). A key ingredient is color \( HST \) imaging, taken from the GEMS and GOODS surveys. These data were used to estimate accurate galaxy colors within the half-light radius, and for selection by galaxy structure. A second key ingredient, required to make precise \( k \)-corrections, is accurate redshift measurements. For this investigation, a sample of objects with reliable spectroscopic redshifts was collected from a variety of sources. Insecure or uncertain spectroscopic redshifts were cross-checked with photometric redshifts from the COMBO-17 survey. The spectroscopic selection criteria are described in the Appendix and result in a final sample of 3440 galaxies with spectroscopic redshifts. We used 3030 galaxies in what follows; the remaining 410 objects could not be used either because they lacked data in one or more of the \( HST \) bands (211 galaxies), or because the object had a half-light radius smaller than 2 pixels (204 objects and five objects satisfied both criteria). Figure 1 shows the redshift distribution of the 3030 useable objects. We choose the three best populated redshift bins of width \( \Delta z = 0.1 \) at \( z \sim 0.55, 0.7, \) and 1.0 for our analysis. We made this selection for two reasons. First, the bins have to be quite narrow to minimize the contribution of \( k \)-correction (the wavelength range over which the interpolation must be done) uncertainties to the final error budget. Second, the best populated redshifts had to be used in order to obtain sufficiently populated color–magnitude diagrams (CMDs) for deriving CMR properties. In Figure 1, these redshift intervals are indicated by the shaded areas.

For further analysis, we rejected known IR and X-ray sources. IR sources were identified by comparison with MIPS 24 \( \mu \text{m} \) observations of the CDFS from Spitzer (Papovich et al. 2004). We use the 24 \( \mu \text{m} \) band owing to its high sensitivity to obscured star formation and active galactic nucleus (AGN) activity. The 80% completeness limit is 83 \( \mu \text{Jy} \), corresponding to approximate obscured SFR limits of \( (5, 10, 17) \) \( M_{\odot} \text{ yr}^{-1} \) at redshifts of 0.55, 0.7, and 1.0, respectively (Bell et al. 2007) using a Kroupa (2001) IMF. We further excluded galaxies detected in deep Chandra imaging of the CDFS. The coverage is nonuniform, with an exposure time of 1 Ms in the central pointing, and 250 ks per pointing in each of four flanking fields. These depths are sufficient to detect moderate-luminosity AGNs (\( L_{0.5-2 \text{ keV}} = 10^{41} - 10^{42} \) erg s\(^{-1} \)) over the whole redshift range of interest (Lehmer et al. 2005).

2.1.1. Colors and Magnitudes from GEMS Images

As the goal of this paper was to measure the scatter of the CMR as accurately as possible, we use high-accuracy \( HST \) colors for the construction of the CMR. For all objects with spectroscopic redshifts, we used GEMS postage stamps to measure accurate magnitudes in the F606W and F850LP passbands. We used the GALAPAGOS software package to cut postage stamps around the position of each object. Galaxy properties were adopted from a single-component Sérsic model (Sérsic 1968) fit to the two-dimensional galaxy luminosity profile using the package Galfit (Peng et al. 2002). We estimate colors within the observed half-light radius (not the intrinsic half-light radius \( r_{e,GALFIT} \) returned from fits to the light profile); such observed half-light radii are substantially larger than the

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\(^7\) Galaxy Evolution from Morphology and SEDs (Rix et al. 2004).
\(^8\) Great Observatories Origins Deep Survey (Giavalisco et al. 2004).
\(^9\) Classifying Objects by Medium-Band Observations in 17 Filters (Wolf et al. 2003, 2004).
\(^10\) Leaving in IR and X-ray sources gives similar results; we conservatively remove such sources in order to minimize the contribution of young stars and nonstellar light to the CMR scatter.
\(^11\) Galaxy Analysis over Large Areas: Parameter Assessment by Galfit (M. Barden et al. 2009).
To maximize the accuracy of the color information, we adopt F606W–F850LP colors, the F606W-image was convolved with a light in F850LP was contained. In order to determine accurate be the semimajor axis of the ellipse within which half of the total flux on a pixel-by-pixel basis; see H"außler 2007, Section 4.2.2 was accurate to within 1 part in a million in terms of total flux (this cut is only for illustration purposes and not used in what follows for any analysis; the actual redshift and magnitude-dependent cuts are given in Section 4.1). The gray shaded areas show the three redshift ranges used in this line (this cut is only for illustration purposes and not used in what follows for any analysis). The semimajor axis of the ellipse was measured. Figure 2 shows the distribution of the measured colors against redshift. Uncertainties in the measured fluxes include contributions from Poisson uncertainty, read noise, and uncertainty from inaccuracies in the assumed sky level (this contribution is equal to the half-light area in pixels times the sky level uncertainty in counts per pixel). Typical values for uncertainties in the determined magnitudes are around 0.007 (slightly higher for high redshifts and lower for smaller redshifts).

2.2. The Low-Redshift Sample from the Sloan Digital Sky Survey

In order to explore the scatter of the CMR at low redshift, we use a sample of galaxies drawn from the SDSS Data Release 4 (Adelman-McCarthy 2006). We choose a sample of galaxies from the publicly available New York University Value-Added Galaxy Catalog (NYU VAGC; Blanton et al. 2005) in a very narrow redshift range $0.0495 < z < 0.0505$ (2053 galaxies). To maximize the accuracy of the color information, we adopt colors derived from “model” magnitudes—such magnitudes use the best-fit de Vaucouleurs or exponential models in the r band as a kernel for measuring fluxes in ugriz.$^{12}$ We $k$-correct the observed-frame ugriz model colors to rest-frame $U - V$ color using InterRest (the same method we use for the intermediate redshift data; see Section 3). Rest-frame magnitudes were calculated by $k$-correcting Sérsic model magnitudes (Blanton et al. 2003) from the NYU VAGC; such magnitudes are closer to the total magnitudes than Petrosian or model magnitudes. The formal random error in the final $U - V$ color is $<0.02$ mag from photometric error, with an estimated calibration error of $<0.04$ mag (assuming 0.01 mag calibration errors in g and r bands); random errors in $M_V$ are $\sim 0.1$ mag, dominated by systematic errors in how one defines sky levels and total magnitude.

3. K-Corrections

To compare measurements in a redshift-independent manner, we $k$-correct the observed-frame measurements into rest-frame properties (throughout this paper we use $M_{r,\text{rest}}$ and $(U - V)_{\text{rest}}$ although our conclusions do not depend on this choice). To do so we use the IDL implemented rest-frame interpolation code InterRest by E.N.T. (http://www.strw.leidenuniv.nl/~ent/InterRest; this work is based on an earlier version of the code). To derive the redshift-dependent transformation between observed and rest-frame colors (the algorithm is described in more detail in Appendix C of Rudnick et al. 2003), InterRest uses observed SEDs from a set of template galaxies: four empirical model spectra from Coleman et al. (1980), and one additional starburst template from Kinney et al. (1996); this is a subset of the default template set which is used to avoid degeneracies in color space.

These $k$-corrections were tested in two ways. First, one can use the $k$-correction routine to predict a F775W magnitude for galaxies in GOODS (where one has F606W, F775W, and F850LP). We show such a comparison in Figure 3, where one can see that the $k$-corrections give a scatter of $\sim 0.03$ and an equal amount of mean color offset. Second, we can compare the final rest-frame colors to the results of independent $k$-correction codes. Comparison to (lower accuracy) COMBO-17 colors shows a scatter of 0.12 mag and an offset of 0.06 mag, and comparison to a stellar population model-derived $k$-correction by E.F.B. and B.H. shows measurement-to-measurement scatter of less than 0.02 mag but overall rest-frame color offsets of $\sim 0.1$ mag (this results primarily from a difference between the 4000 Å break structure of the stellar population models and the observed ones used by InterRest). We conclude that the $k$-corrections of the HST-derived colors are accurate to a few hundredths of a magnitude (random error; this contributes to the scatter on the CMR; Taylor et al. 2009), with possible overall systematics of $\lesssim 0.1$ mag (affecting primarily the zero point of the CMR). We assume the $k$-correction errors to scale with the wavelength range over which the interpolation is done.

4. RESULTS

In this section, we present our analysis of the red-sequence CMR scatter and its evolution. First, we explain the selection criteria applied for red-sequence galaxies, then we discuss the actual measurement of the scatter of the red sequence at different redshifts $0.05 \leq z \leq 1.05$. With our precise magnitudes and

$^{12}$ We also used aperture magnitudes with aperture radii $5 < r \text{arcsec}^{-1} < 10$, finding similar or larger CMR scatter.
colors we have produced CMDs for four redshift intervals and plot them in Figure 4.

4.1. Selection of Red-Sequence Galaxies

Our selection criteria take care to choose only non-star-forming, early-type galaxies representing the red sequence and to reject blue galaxies, galaxies with disk structure, and galaxies with ongoing star formation and/or AGN activity.

First, we applied a color cut to exclude galaxies with obvious signs of star formation from the sample. For this we made use of the bimodality of the color distribution which is visible in the CMDs at all redshifts (Figure 4). The color cut was chosen to fall into the gap between blue and red objects (see also histograms in Figure 4). We used a tilted cut with the same slope for all samples. As the mean colors of the populations evolve with redshift, we take this into account by allowing the cut to evolve correspondingly. The cut applied here can be described as \((U - V)_{\text{rest}} > -0.085M_{V,\text{rest}} - 0.65 - 0.5z\). Small changes in the positions of the cuts do not influence the general results. In the diagrams, the cut is made visible by different shades of gray. The light gray points are objects bluer than the color criterion whereas the dark gray and black points indicate objects on the red side of the cut.

A second selection criterion was applied to clean the sample of structurally late-type galaxies. For this the Sérsic index of the galaxy is used (for the GEMS galaxies, this is measured using GALFIT, while for the SDSS galaxies we adopt the Sérsic fits from Blanton et al. 2005). To be treated as part of the red sequence, a Sérsic index of \(n > 2.5\) is required. This cut successfully weeds out edge-on spirals from the sample (McIntosh et al. 2005b). These objects are shown as dark gray points. Regardless of color and Sérsic index, we reject galaxies with X-ray or 24 \(\mu m\) detections (for the CDFS data only; the SDSS sample we use lacks such information) as their colors may be substantially affected by UV-bright young stellar populations and/or an accreting supermassive black hole (although our results remain unchanged if these systems are not excluded from our analysis). These objects are shown in the CMDs with asterisks (X-ray) and diamonds (IR). The objects which qualified as red-sequence galaxies after these selection criteria are shown in black with error bars in the CMDs (number of red-sequence galaxies in the redshift bins: 563/38/102/31).

4.2. Fitting the Red Sequence

The goal of this paper is to measure the intercept of the CMR at a fiducial magnitude and its scatter, and to show the evolution of both the CMR intercept and scatter as a function of redshift (see Figure 4). The intercept is the color value of the relation measured at a specific magnitude (either the same magnitude value at all redshifts, or using a variable magnitude that attempts to account for the evolution of the population). The scatter is calculated using the IDL routine \texttt{robust_sigma}, which gives an outlier-resistant estimate of the dispersion of the color distribution using the median absolute deviation as an initial estimate and then weights points using Tukey’s Biweight as an robust estimator (this is the usual approach employed in this field; e.g., Bower et al. 1992; McIntosh et al. 2005a). We fit a simple linear function to the distribution of colors and magnitudes of the non-star-forming early-type galaxies under two assumptions:

1. We fit the data points in each redshift bin separately.
2. We choose to hold the slope fixed at all redshifts \(\geq 0.5\) to the value measured at \(z = 0.05\) from the SDSS.

The slope of the two methods are in some cases very different, but as the SDSS sample has many more objects and a larger dynamic range, this fit is much more reliable than the fits for the other bins. Further support for this assumed slope is given by the best populated GEMS bin around \(z = 0.7\), which shows nearly the same slope. We note that the determination of the intercept and scatter are not sensitive to our choice of fitting method (Table 1). The histogram of color offsets from the CMR with redshift-independent slope is shown in the inset panels of Figure 4 for early-type galaxies (black) and for all galaxies (gray). As the observed scatter contains contributions from intrinsic scatter and measurement uncertainty we estimate the intrinsic color scatter by subtracting the random color uncertainties in quadrature. The color uncertainties for the low-redshift galaxies were estimated by scaling the model \(u - r\) color uncertainties\(^{13}\) by \(d(U - V)_{\text{rest}}/d(u - r)\) and adding in quadrature a small empirically determined 0.015 mag contribution accounting for real scatter in \(U - V\) at a given \(u - r\): 
\[
\delta(U - V)^{2} = \[\delta(u - r)d(U - V)/d(u - r)^{2}\] + 0.015^{2}.
\]
If not further specified, we refer to the intrinsic scatter hereafter.

The color intercepts \((U - V)_{\text{rest}}\) of the fitted CMR at a fixed \(M_{V,\text{rest}} = -22\) are shown as a function of redshift in

\(^{13}\) Furthermore, the effect of excluding IR and X-ray detections from the red sequence is quite small and does not affect our results. The effect on the intercepts is around 1%. The values for intrinsic scatter would be a bit larger if IR and X-ray sources are included in the sample, changing for \(z = 0.55\) from 0.128 to 0.138, for \(z = 0.7\) from 0.126 to 0.133, and for \(z = 1.0\) from 0.207 to 0.216.

\(^{14}\) Recall that \(U - V\) is estimated from the \textit{ugriz} model colors using InterRest. Our choice of scaling from \(u - r\) uncertainty is reasonable: \(u, g,\) and \(r\) are the main determinants of \(U - V\), where \(g\) and \(r\) are relatively well-measured and the \(u\)-band uncertainty is factors of several larger.
Figure 4. $U - V$ rest-frame color against $M_V$ for four different redshift bins. The light gray points are objects below a tilted cut, dividing blue and red objects. This cut has a fixed slope and a redshift-dependent intercept. Depending on the Sérsic index the red objects are divided in a dark gray ($n < 2.5$) and a black sample ($n > 2.5$; with errorbars for the three intermediate redshift bins); the $n > 2.5$ red galaxies are retained in our analysis. Independent of color and Sérsic index IR (diamonds) and X-ray (asterisks) detections are rejected from the red-sequence sample. The dashed lines are fits to the red-sequence samples for the three redshift bins with $z \geq 0.5$. In the $z = 0.05$ panel, the fit is shown as a solid line (the position of this fit is shown in the other panels as the dotted line). A line with the same slope is shifted to the mean color value of the three other panels (solid line). Using these “fits” we calculated intercepts at $M_V = -22$. The small histograms show the color distribution measured as an offset from the relation. The complete distribution is shown in light gray, whereas the red sequence (the black points in the CMDs) is shown in black. The dashed vertical line shows the intercept of the fit (dashed line in the CMDs) at a magnitude value of $-22$. The solid vertical line shows the mean intercepts with the CMR scatter (rms) marked by the dotted vertical lines. The dash-dotted lines show the CMR intercept at $z = 0.05$. Overplotted is a Gaussian with mean and $\sigma$ defined by the mean color and rms of the red-sequence sample.

Table 1

| Redshift | Fixed Slope | Intrinsic Slope | Measured Scatter | Intrinsic Scatter |
|----------|-------------|-----------------|-----------------|------------------|
| $z = 0.05$ | $-0.087 \pm 0.006$ | $1.457 \pm 0.005$ | $0.124$ | $0.117$ |
| $z = 0.55$ | $-0.015 \pm 0.028$ | $1.206 \pm 0.021$ | $0.126$ | $0.124$ |
| $z = 0.70$ | $-0.066 \pm 0.014$ | $1.178 \pm 0.010$ | $0.127$ | $0.127$ |
| $z = 1.00$ | $0.010 \pm 0.047$ | $1.097 \pm 0.041$ | $0.210$ | $0.206$ |

Notes. “Fixed slope” means that the slope of the CMR is fixed to the $z = 0.05$ value for all redshifts (solid lines in Figure 4), while in the “Fit” columns the red sequence is fitted for each bin (dashed lines in Figure 4).

Figure 5. The solid errorbars denote the formal error in the mean intercept, calculated using bootstrapping, although recall that the actual, primarily systematic, uncertainty in the galaxy colors is $\sim 0.1$ mag. The dotted “errorbars” show our measurement of the CMR scatter, calculated as the resistant dispersion of the color offsets of the early-type galaxies from the CMR. The results are tabulated in Table 1. For comparison, intercept measurements from other studies (Blanton 2006; Franzetti et al. 2007; Cool et al. 2006) are shown in these plots together with our data. In the case of Blanton (2006) and Cool et al. (2006), we have $k$-corrected their values to rest-frame $U - V$ color using the $kcorrect$ software package, written by M. Blanton. We made sure that there is no significant difference ($\leq 0.03$ mag) between the rest-frame colors derived with $kcorrect$ and InterRest.
We find that the intercept of the CMR evolves by $\sim$0.3 mag in $U - V$ color between $z = 1$ and $z = 0.05$, in rough agreement with previous studies (e.g., Bell et al. 2004a; Franzetti et al. 2007; Blanton 2006; Taylor et al. 2008), although recall that systematic errors in the intercepts of the CMR are significant, $\sim$0.1 mag in $U - V$ rest-frame color. More importantly, we find a scatter of $\sigma_{U-V} \sim 0.1$ mag (Table 1) at all $z < 0.75$; the scatter at $z = 1$ appears to be somewhat larger (being consistent with Taylor et al. 2008). These values are somewhat larger than the scatter measured for local galaxy clusters ($0.04 < \sigma_{U-V} < 0.1$, where the scatter appears to vary from cluster to cluster; e.g., McIntosh et al. 2003a). We note that subtraction in quadrature of the individual galaxy measurement errors from the CMR scatter yields almost unchanged results, even for the low-redshift SDSS sample (where the scatter could decrease to $\sim 0.09$ mag). This shows that we measured a real scatter in the relation and not only a spread caused by measurement uncertainties. In particular, one should note that for the SDSS, spectral analysis of the drivers of the CMR scatter have demonstrated clear spectral differences between early-type galaxies of a given magnitude at the red and blue sides of the CMR (Gallazzi et al. 2006; Cool et al. 2006), demonstrating that the bulk of the CMR scatter is intrinsic.

5. INTERPRETATION

In the last sections, we described our measurements of the CMR intercept and scatter for cosmic average early-type galaxies at four redshifts between 1.0 and 0.05. We find a slowly evolving mean color, and an almost non-evolving scatter of $\sim$0.1 mag in $U - V$ rest-frame color. In this section, we build some intuition about possible interpretation of this result using stellar population synthesis modeling. We show first the evolution of single bursts, or populations of galaxies whose star formation is truncated at a particular time, in Sections 5.1 and 5.2. Note that the purpose here is not to test “monolithic collapse” models (those models are already ruled out by the observed buildup of the red-sequence population), rather it is to establish the basic model ingredients. In Sections 5.3 and 5.4 we ask and answer a simple question (similar in spirit to van Dokkum & Franx 2001): if the red sequence forms through ongoing and continuous truncation of star formation in previously star-forming systems, can one simultaneously reproduce the buildup of red-sequence galaxies and the scatter of the CMR?

5.1. The Evolution of Single Bursts

To get our bearings, we focus first on the evolution of the CMR intercept using single bursts of star formation. In what follows, we use the stellar population model 221997Fioc & Rocca-Volmerange16 (version 2.0, see Fioc & Rocca-Volmerange 1997, for the description of an earlier version of the model) to predict the evolution of galaxy colors and absolute magnitudes as a function of redshift.

The results are shown in Figure 6 for three different formation redshifts and for various metallicities. One can see that the evolution of the intercept of the CMR follows roughly the trends expected for the passive reddening and fading of ancient stellar populations. In the context of single bursts, the rate of change of the CMR intercept with redshift is related primarily to formation history, whereas the overall intercept is sensitive primarily to metallicity, with some sensitivity to age.

To compensate for the passive fading of the early-type population, we also measure the CMR intercept at a redshift-dependent absolute magnitude (black asterisks in Figure 6). We choose to adopt a model with metallicity $Z \approx 0.008$ and a formation redshift of 2 to estimate the evolution of the luminosity of an early-type galaxy as a function of redshift.17 and use this to calculate the absolute magnitude values at which we measure the intercept of the CMR (these absolute magnitudes are $-22.215.3$, $-21.9$, and $-20.8$ at $z = 1.0$, 0.75, 0.55, and 0.05, respectively). One can think of these intercepts as being measured at a given, redshift-independent, stellar mass. Because these intercepts reflect the evolution at a given stellar mass, we choose to focus on these values in what follows, as a more intuitive reflection of the likely evolution of the color of a given galaxy (or a mass/metallicity bin in the evolving galaxy population).

5.2. The Evolution of Galaxies with Truncated Star Formation

Motivated by the observational evidence for truncation of star formation in blue-sequence galaxies, leading to the ongoing buildup of the red-sequence galaxies at redshifts $z < 1$ (e.g., Bell et al. 2004b, 2007; Borch et al. 2006), we study the evolution of the colors of galaxies whose star formation has been truncated at a variety of redshifts $z \lesssim 1$. The purpose of this section is to get

15 The possible trend toward a bluer CMR intercept at very large clustercentric radii, arguably an environmental effect, would also increase the scatter of the cosmic average CMR relative to the cluster CMR (e.g., Terlevich et al. 2001; Pimbblet et al. 2002).

16 Projet d'Etude des Galaxies par Synth`ese Evolutive.

17 The choice between the formation redshifts in the range shown in the plot does not have a great influence on the results; to choose $z_f = 3$ instead would lead to a slightly smaller evolution in magnitudes, but the resulting difference in intercepts is smaller than 0.02 for all redshifts. A different choice in metallicity has also only very small effects. To choose $Z = 0.02$ (solar metallicity) would change the results even less than the change of formation redshift.
a feeling for the ingredients used for the modeling of the CMR evolution described in the next section. Figure 7 shows the rest-frame color evolution of a stellar population which forms stars at a constant rate from \( z_f = 2 \) to the truncation redshift \( z_{\text{trunc}} \). We plot the evolution of seven different truncation histories which all have a constant metallicity of \( Z = 0.02 \). The rightmost track has a truncation redshift very close to the formation redshift of the model, namely at \( z = 1.95 \). The other lines show the evolution of galaxies with smaller truncation redshifts (from left to right) from 0.2 to 1.2 in steps of 0.2. A general feature of such truncation models is a period of relatively rapid evolution onto the red sequence (timescales \( \lesssim 1 \) Gyr, as can be seen in Figure 7 and Blanton 2006; Schweizer & Seitzer 1992), and then relatively slow subsequent fading and reddening of the population.

### 5.3. Expectations for the Scatter Measurement

With these SF modeling ingredients in place, we are now in a position to ask what the evolution of the intercept and scatter of the CMR can tell us about the evolution of the early-type galaxy population. Obviously, we will be unable to address this issue completely, as we have seen that many factors influence the colors and magnitudes of galaxies: when star formation started, metallicity, when (if) star formation ends, and whether or not there is any residual star formation.

Instead, we limit ourselves to one well-defined question. Recent observations have measured a significant increase in the total stellar mass in the red-sequence galaxy population since \( z = 1 \) (Chen et al. 2003; Bell et al. 2004b; Bundy et al. 2005; Brown et al. 2006; Borch et al. 2006; Faber et al. 2007). This evolution manifests itself primarily in terms of an increasing space density of red-sequence galaxies at \( \lesssim L^* \) (Borch et al. 2006; Faber et al. 2007), and is most naturally interpreted as being fed by the truncation or quenching of star formation in massive blue galaxies (Bell et al. 2004b, 2007; Faber et al. 2007). In such a scenario, one expects a significant scatter in the CMR, because of the constant flow of recently star-forming galaxies onto the red sequence. Here, we will predict the CMR scatter implied by a constantly growing red sequence, and compare this predicted scatter with the observations. Such an exercise was carried out by van Dokkum & Franx (2001) for early-type galaxies in clusters; here, we extend their work to a cosmic average environment.

Our first ingredient is a toy model for the buildup in the number of red-sequence galaxies as a function of time. For all lines, star formation starts at \( z = 2 \) and the different lines denote a variety of different truncation redshifts (from left to right: 0.2–1.2 in steps of 0.2). The tiny black dots on the lines indicate the point on the evolutionary track a galaxy has reached 0.5, 1, and 2 Gyr, respectively, after the truncation of star formation (as labeled on the second line from the right). The symbols are the same as in Figures 5 and 6.
at all stellar masses equally.\textsuperscript{18} We describe the evolution of the number of red-sequence galaxies with a simple linear fit (in redshift) as shown in the small panel of Figure 8, compared with the measurements of the integrated stellar mass density of Borch et al. (2006). We then determine the derivative of this relation to get the change in stellar mass density with time. This is used to estimate the truncation rate by shifting the time axis by $-1$ Gyr—approximately the time taken to redden enough to satisfy our red-sequence cut (following Blanton 2006; see also Figure 7). In this way, we have a truncation rate history that is consistent with Borch et al. (2006) and can be used to estimate the evolution of the CMR scatter. To describe the truncation rate for epochs not covered by Borch et al. (2006), we choose to model the truncation rate as a constantly increasing function of time from $z_f \sim 5.5$ until $t_{\text{trunc}} = 0.9$. The influence of this choice on the results is negligible. The resulting number of truncated (pre-red sequence) galaxies—the integral of the truncation rate—as a function of cosmic epoch is also given in Figure 8.

The next step is to build a more realistic truncation model (see Figure 7): instead of choosing one particular truncation time as in Section 5.2, we instead draw truncation times from the truncation time distribution in Figure 8. We choose 12 “observation” redshifts between $z = 0$ and $z = 1.1$; at each we draw 1000 galaxies from this truncation\textsuperscript{19} history shown in Figure 8 resulting in samples of galaxies with different truncation redshifts, but the same formation redshift $z_{\text{start}} = 3$ for all galaxies.\textsuperscript{20} Due to this variety of truncation redshifts, the galaxies in the samples experienced periods of passive evolution of different lengths. This then gives a distribution of galaxy colors at each redshift of interest; for display purposes in Figures 9 and 10 we have added a small random offset in redshift. We assume no ongoing low-level star formation in red-sequence galaxies; while potentially unrealistic, it allows us to estimate the expected scatter from truncation alone.\textsuperscript{21}

In order to separate between the effects of age and metallicity scatter on the CMR scatter, we first consider the effects of formation history alone in Figure 9. One can see a considerable color scatter from the ongoing accretion of recently truncated galaxies, along with some low-level bimodalities caused by kinks in the time evolution of colors for some metallicities (see, e.g., Figure 6). For solar metallicity $Z = 0.02$, the color evolution is smooth, giving no “pile-ups” in color space. The strong influence of metallicity on the color of the red sequence can also be seen in this plot.

In Figure 10, we show our expectation for the evolution of the CMR intercept and scatter as a function of redshift. We have drawn galaxies from a log-normal distribution in metallicity with mean $\log_{10}[\text{metallicity}]=-1.2$ and scatter 0.1 dex which is held constant over redshift (Figure 11).\textsuperscript{22} This distribution was chosen to approximately match the observed CMR intercept and scatter, but it is interesting to note that this value of metallicity scatter is consistent with the estimated intrinsic scatter in metallicity of present-day early-type galaxies of $\sim 0.1$ dex from Gallazzi et al. (2006). We show the mean and scatter (calculated with the same estimation algorithm as the scatter in the observed relations) of the distribution as solid lines. The resulting distribution agrees well with the scatter measurements at the redshifts 0.05, 0.55, and 0.7. At $z = 1.0$, the measured scatter exceeds the model prediction (allowing for more scatter in star formation histories). The results are presented in Table 2.

| $z$  | Measured Scatter | Intrinsic Scatter |
|------|------------------|------------------|
| 0.05 | 0.124            | 0.117            |
| 0.55 | 0.124            | 0.124            |
| 0.7  | 0.127            | 0.127            |
| 1.0  | 0.210            | 0.206            |

The results of this paper do not change significantly if a burst of star formation occurs before truncation, as might be expected in a gas-rich galaxy merger.\textsuperscript{23} The results of this paper do not change significantly if a burst of star formation occurs before truncation, as might be expected in a gas-rich galaxy merger.

\textsuperscript{21} One could argue we will estimate lower limits to the scatter of the CMR with this approach. Such an argument has merit, but would neglect (as we also have) the influence of any age/metallicity anticorrelation on the CMR scatter (as observed by, e.g., Trager et al. 2000).

\textsuperscript{22} Our assumption of a redshift-independent scatter is clearly an oversimplification; yet, in the context of our model in which each galaxy has its own single metallicity it is a defensible one. In reality, the metallicity may evolve if there is any low level residual star formation in early-type galaxies (indeed, if there is an age–metallicity relation in the stars in an individual galaxy, its light-weighted age can evolve as the galaxy ages even in the absence of star formation).
of the cosmic-averaged early-type galaxy population and are constrained to reproduce the observed buildup of the early-type galaxy population.

5.4. Blue Spheroids

So far, we have made no particular assumption on the mechanism by which galaxies quench their star formation and join the red sequence. In this section, we explore a rather more specific scenario: galaxies structurally transform into an early-type galaxy (e.g., through galaxy merging) before reddening on to the red sequence. Such a scenario predicts that there should be a nonegligible population of blue spheroids—i.e., galaxies that are structurally early-type but have blue colors. In this context, we present a range of predictions for their abundance, requiring that blue spheroids (1) have colors at least 0.25 mag bluer in $U-V$ than the locus of red-sequence galaxies at that redshift and (2) are at least a given time $t_{\text{recognize}}$ from the truncation (or spheroid creation) event. This latter criterion is introduced to allow for a delay $t_{\text{recognize}}$ between the event that truncated star formation (e.g., a galaxy merger) and the galaxy becoming recognizably early type; in what follows we explore the range $0 \leq t_{\text{recognize}} \leq 0.4$ Gyr, motivated by simulations of galaxy mergers. The ratio of blue spheroids to the total number of spheroidal galaxies (red and blue spheroids) $N_{\text{BS}}/(N_{\text{RS}} + N_{\text{BS}})$ is measured as a function of redshift and is shown in Figure 12 for three different values of $t_{\text{recognize}}$.

There are two key points to take away from Figure 12. First, the predicted blue spheroid fraction depends sensitively on one’s choice of $t_{\text{recognize}}$ (and therefore, also, details of the star formation history and dust content of the galaxy). Second, despite this uncertainty, the range in model prediction is in reasonable agreement with observed blue spheroid fractions (e.g., $N_{\text{BS}}/(N_{\text{RS}} + N_{\text{BS}}) \sim 0.06$ at $z \sim 0.6$ from Häußler 2007)24. The fraction observed by Bamford et al. (2009) for the relevant mass range is slightly higher than in our models, but as they used a different method these values might not be directly comparable. Recall that this toy model was constructed to explore the implications of the growth of the red sequence through the truncation of star formation in blue galaxies. Here, we have shown that such a model reproduces simultaneously the evolution of the intercept and scatter of the CMR since $z = 1$ and the blue spheroid fraction at intermediate redshift. Such an analysis lends considerable weight to the notion that the early-type galaxy population has grown considerably between redshift one and the present day through the truncation of star formation in blue galaxies (through mergers or some other physical process).

6. DISCUSSION AND CONCLUSIONS

The evolution of the scatter of the red sequence is an important source of information about the evolutionary history of
the red-sequence/early-type galaxy population. In this paper, we constructed high-accuracy CMRs at four different redshift ranges using accurate color and spectroscopic redshift information. We used a sample of over 3000 galaxies in the CDFS, in conjunction with a local reference sample of galaxies from the SDSS, to understand the redshift evolution of CMR scatter. We used images from the GEMS survey taken with the Advanced Camera for Surveys (ACS) onboard HST to provide both high-resolution morphologies (to classify galaxies as early-type) and to measure accurate colors within the half-light radius. In order to calculate accurate $k$-corrections to rest-frame passbands, we used spectroscopic redshifts compiled from a variety of sources. At all redshifts, we apply a structure and color cut to isolate early-type red-sequence galaxies; at intermediate redshift we were able also to excise star-forming galaxies and AGN from the sample using X-ray and 24 μm information.

The resulting scatter of the CMR is $\sim$0.1 mag in $U - V$ color at $z = 0.05$, 0.55, and 0.7, and somewhat higher at $z = 1.0$. This scatter is comparable to those found in some local galaxy clusters (e.g., A85 and A754 of McIntosh et al. 2005a; their Table 8) and larger than that found for the Coma and A496 clusters ($\sigma_{U - V} \sim 0.05$ mag; Bower et al. 1992; Terlevich et al. 2001; McIntosh et al. 2005a). We note in passing that a better observational handle on the environmental dependence of the scatter of the CMR, with special attention being paid to possible cluster-to-cluster differences, would be highly desirable (but is clearly beyond the scope of this paper).

We explored the implications of a measured CMR scatter of $\sigma_{U - V} \sim 0.1$ mag on our understanding of the evolution of early-type galaxies. The CMR scatter can be influenced by when star formation started, when star formation stopped, residual star formation, and metallicity. Thus, it is not straightforward to turn the measured CMR scatter into robust constraints in this multidimensional space.

We adopted instead a simple approach. The evolving number density of red-sequence galaxies has been measured—assuming that this evolution in number density is from the quenching of star formation in galaxies with roughly constant star-formation rate before quenching, we have a prediction (motivated by other observations) for the quenching/truncation history of galaxies going on to the red sequence. We have also a measurement of the present-day metallicity scatter of early-type galaxies from Gallazzi et al. (2006). Thus, we have both elements in place where we can predict the evolution of the CMR scatter. Importantly, this model—in which new red-sequence galaxies are being constantly added at the rate required by observations of red-sequence galaxy number density—predicts the correct scatter in the colors of these red-sequence galaxies.
Furthermore, this model predicts approximately the correct number density of blue spheroids—galaxies which are structurally early-type but have blue colors—although admittedly with considerable model dependence. Thus, we conclude that these different observations—the evolution of the number density of red-sequence galaxies, the evolution of the intercept and scatter of the CMR, and the blue spheroid fraction—paint a consistent picture in which the early-type galaxy population grows significantly between $z = 1$ and the present day through the quenching of star formation in blue cloud galaxies.

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APPENDIX

SPECTROSCOPIC REDSHIFT SAMPLE

In order to study the evolution of the scatter of the red sequence, one must use a sample of galaxies with spectroscopic redshifts. Toward this end, we compiled a catalog of spectroscopic redshifts from a variety of sources, listed below.

We used the data of some projects which surveyed the entire CDFS but a better coverage is reached for the GOODS field (see also Figure 13). A collection of spectroscopic redshifts for the CDFS can be found in the “Master Catalog of CDFS spectroscopy” (http://www.eso.org/science/goods/spectroscopy/CDFS_Mastercat/). We used data from one paper included in this catalog (Szokoly et al. 2004). Also the VVDS (VIMOS/VLT Deep Survey; Le Fèvre et al. 2004), FORS2 (Franzetti, P., et al. 2007, A&A, 465, 711), GOODS-S (Le Fèvre et al. 2004), VIMOS FORS2 DR 3.0 (Vanzella et al. 2008), and G00s (Ravikumar et al. 2007) and S. Koposov et al. 2009, in preparation. Also the spectroscopic redshifts were taken without further testing. These are

1. VVDS—4 (confidence level 100%) and 3 (95%).
2. FORS2—A (solid redshift determination) and B (likely redshift determination).
3. Szokoly et al. (2004)—3.0 (reliable redshift determination with unambiguous X-ray counterpart) and 2.0 (likely redshift determination).
4. Ravikumar et al. (2007)—secure observations.

In the case of insecure or unknown data quality, the spectroscopic redshifts were tested against photometric redshifts from the COMBO-17 survey. In such cases, we used only those spectroscopic redshifts which differ by less than 0.1 from the photometric ones. In total, this leads to a sample of 3440 objects (3030 useable for this project). See Figure 13 for the positions on the sky of the objects used for flux measurements. The total numbers of objects of each catalog is listed in Table 3. The combined sample covers a roughly constant fraction of about 20% of the galaxies in the relevant magnitude range (20 mag $< M_I < 22$ mag) and then drops off toward fainter magnitudes with a fraction of about 10% for $M_I < 24$ mag. Red and blue galaxies show a similar behavior.

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Table 3

| Redshift Catalog | Number of Objects Used |
|------------------|------------------------|
| VVDS (Le Fèvre et al. 2004) | 629 |
| Szokoly et al. (2004) | 38 |
| GOODS-FORS2 DR 3.0 (Vanzella et al. 2008) | 464 |
| Ravikumar et al. (2007) | 303 |
| S. Koposov et al. 2009, in preparation | 510 |
| VIMOS DR 1.0 (Popesso et al. 2009) | 1086 |
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