RESULTS OF SPARO 2003: MAPPING MAGNETIC FIELDS IN GIANT MOLECULAR CLOUDS

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ABSTRACT

We present results from the Austral Winter 2003 observing campaign of SPARO, a 450 μm polarimeter used with a 2 m telescope at the South Pole. We mapped large-scale magnetic fields in four GMCs in the Galactic disk: NGC 6334, the Carina Nebula, G333.6−0.2, and G331.5−0.1. We find a statistically significant correlation of the inferred field directions with the orientation of the Galactic plane. Specifically, three of the four GMCs (NGC 6334 is the exception) have mean field directions that are within 15° of the plane. The simplest interpretation is that the field direction tends to be preserved during the process of GMC formation. We have also carried out an analysis of published optical polarimetry data. For the closest of the SPARO GMCs, NGC 6334, we can compare the field direction in the cloud as measured by SPARO with the field direction in a larger region surrounding the cloud, as determined from optical polarimetry. For purposes of comparison, we also use optical polarimetry to determine field directions for 9–10 other regions of similar size. We find that the region surrounding NGC 6334 is an outlier in the distribution of field directions determined from optical polarimetry, just as the NGC 6334 cloud is an outlier in the distribution of cloud field directions determined by SPARO. In both cases the field direction corresponding to NGC 6334 is rotated away from the direction of the plane by a large angle. This finding is consistent with our suggestion that field direction tends to be preserved during GMC formation. Finally, by comparing the disorder in our magnetic field maps with the disorder seen in magnetic field maps derived from MHD turbulence simulations, we conclude that the magnetic energy density in our clouds is comparable to the turbulent energy density.

Subject headings: galaxies: magnetic fields — ISM: clouds — ISM: magnetic fields — polarization — turbulence

1. INTRODUCTION

It is generally believed that the ionization fraction in interstellar clouds is sufficiently high for flux freezing to apply and that interstellar magnetic fields are thus well coupled to the gas. Furthermore, the fields may be strong enough to be dynamically important and thus may play important roles in star formation. These issues have been reviewed by Crutcher (2004). Furthermore, as reviewed by Mac Low & Klessen (2004), magnetohydrodynamic (MHD) turbulence is probably an important player in the star formation process.

Submillimeter polarimetry is a technique for mapping interstellar magnetic fields (Lazarian 2000) that is well suited for studying dense star-forming clouds. In particular, this method appears to have an advantage over the related technique of optical/near-IR polarimetry of background stars. Specifically, it has been shown by Whittet et al. (2001) and Arce et al. (1998) that grain populations residing in regions that are shielded from the interstellar radiation field have very low polarizing efficiency at optical/near-IR wavelengths. Moderate shielding (A_v = 1–2 mag) seems to be sufficient to sharply reduce the efficiency. By contrast, when we study the submillimeter emission from highly obscured regions (A_v ~ 30 mag) in a dense cloud, we find significant polarization (Crutcher et al. 2004). Thus, submillimeter polarimetry is especially useful for such regions.

This discrepancy between optical/near-IR polarization efficiency and submillimeter polarization efficiency, for highly obscured regions, is explained by Cho & Lazarian (2005) as an effect of grain size. Under the assumption that grains are aligned by the radiative torque mechanism (Dolginov 1972; Draine & Weingartner 1996, 1997), they show that in highly obscured regions only the largest grains will be aligned. They argue that these large aligned grains dominate the submillimeter emission but are relatively less important for the optical/near-IR extinction.

Maps of submillimeter/far-IR polarization usually cover relatively small sky areas, typically of order 10 arcmin^2 (Greaves et al. 2003; Hildebrand 2002; Dotson et al. 2000). Because giant molecular clouds (GMCs) usually extend over much larger sky areas, approaching a square degree, these small-scale maps have not been very useful for probing the large-scale, or global, magnetic field of a GMC. Not every submillimeter polarization map is small on the sky, however: the ARCHEOPS balloon-borne submillimeter polarimeter (Benoît et al. 2004) mapped the degree-scale submillimeter (850 μm) polarization of large sections of the Galactic disk. Binning their data to a resolution of several degrees, they obtain significant detections of polarization with magnetic field directions generally running parallel to the Galactic plane. Because the large-scale Galactic magnetic field determined from optical polarimetry is also known to run parallel to the plane (Mathewson & Ford 1970), the ARCHEOPS result
shows that the Galactic field penetrates into the dense gas that dominates the submillimeter emission. In contrast, the smaller scale far-IR/submillimeter polarization maps of GMCs in the disk show a wide range of inferred field directions and no preferred orientation with respect to the Galactic plane (see Fig. 21 of Hildebrand 2002).

The South Pole polarimeter SPARO is optimized for submillimeter polarimetry on angular scales larger than those typically accessible from ground-based submillimeter dishes, although not as large as those studied by ARCHEOPS. With SPARO we can map fields over a significant fraction of a GMC while still resolving field structure within the cloud. Here we present SPARO polarization maps for four GMCs in the Galactic disk. Each map extends over a sky area corresponding to several hundred square arcminutes.

2. OBSERVATIONS AND RESULTS

The observations were made at Amundsen-Scott South Pole station using the Viper 2 m telescope (Peterson et al. 2000; Kuo et al. 2004) together with Northwestern University’s submillimeter polarimeter, SPARO (Dotson et al. 1998; Renbarger et al. 2004). Radiation entering SPARO passes through a rotatable half-wave plate and is then divided into two orthogonal polarization components, each of which is detected by a separate He-cooled 9 pixel detector array. SPARO thus measures polarization simultaneously at nine sky positions, arranged in a $3 \times 3$ square pattern. Because the South Pole is an exceptionally good submillimeter site (Lane 1998), SPARO obtains extremely good sensitivity to spatially extended, low surface brightness emission. SPARO’s first observations, made during Austral Winter 2000, were reported by Novak et al. (2003). Here we present results from our second observing campaign that took place during 2003 April–August.

For the 2003 observations, the beam FWHM was determined to be $4' \pm 0.5'$, and the pixel-to-pixel separation was $3.3'$. The pointing accuracy was $\pm 1'$. SPARO’s spectral passband is centered at $\lambda_0 = 450 \mu$m, with fractional bandwidth $\Delta\lambda/\lambda_0 = 0.10$. Our data acquisition scheme involves carrying out standard "photometric integrations" at each of six half-wave plate rotation angles, successively (Hildebrand et al. 2000). Each photometric integration, in turn, involves rapidly switching the array footprint back and forth on the sky between the source position and a reference position. Reference signals are subtracted from source signals. We used two reference positions (Hildebrand et al. 2000), separated from the source position by $+0\cdot65$ and $-0\cdot65$ in cross-elevation, respectively.

Our data reduction procedures follow closely those described by Hildebrand et al. (2000) with one important difference. Hildebrand et al. (2000) describe how the “polarization signal” is computed from each photometric integration (see above) by taking the difference between signals from corresponding pixels of the two detector arrays and then dividing this by the sum of these signals (see their eq. [7]). This corresponds to dividing polarized flux by total flux. We found that for our observations the total flux was often not well determined by a single photometric integration, due to variations in atmospheric emission significantly above the level of the photon noise. These variations are usually referred to as “sky noise,” and they affect the total flux measurement but not the difference signals. In order to circumvent the problem, we developed a new method for computing the polarization signal, which we now describe.

We grouped our data into “sets” consisting of nine identical “half-wave plate cycles.” As described above, each such cycle involved six photometric integrations, each taken at a different half-wave plate angle. For each set, we computed a single value for the total flux, or signal sum, for each of the 9 pixels. We also computed, for each pixel, six values of the difference signal, one for each half-wave plate position. These six difference signals were then divided by the set-average total flux for the corresponding pixel. Our new technique for determining the polarization signal requires stable atmospheric transmission over timescales of 1 hr, corresponding to the duration of one set. On the basis of opacity measurements obtained with the CMU/NRAO tipper (Peterson et al. 2003), we estimate that signals were stable to $\pm 10\%$. A more detailed description of the new data analysis procedure is given by Li et al. (2005), and a similar procedure that was applied to data from the Hertz polarimeter is described by Kirby et al. (2005).

The instrumental polarization was determined by calibrating on the Moon and on the intensity peak of Sgr B2, following the same procedure that we used for our 2000 observations (Novak et al. 2003; Chuss 2002). The level of systematic error in our measurements is $<0.3\%$, which translates into an uncertainty in polarization angle of less than $9^\circ$ ($1.0%/P$).

We observed four GMCs: NGC 6334, the Carina Nebula, G333.6–0.2, and G331.5–0.1. Three of our targets were chosen for their high column density and large angular extent as determined from the dust opacity map of Schlegel et al. (1998). This map is derived by combining COBE DIRBE and IRAS ISSA maps. One of our targets, Carina, has somewhat lower dust opacity than the others. It was chosen for its high elevation ($\sim 60^\circ$ at the South Pole), which corresponds to higher atmospheric transmission. In Tables 1–4 we give the measured degree and angle of polarization and associated statistical errors for all sky positions having $P > 2\sigma_P$. Note that $\sim 80\%$ of the measurements have $P > 3\sigma_P$. All measured degrees of polarization are larger than $0.3\%$; i.e., they are above the level of systematic error. Figure 1 shows the

| Parameter | Value |
|-----------|--------|
| $P$       | $\Delta\alpha$ |
| $\Delta\beta$ | (%) |
| $\sigma_P$ | $\phi$ |
| $\sigma_\phi$ | |

$^{a}$ Offsets in right ascension and declination are measured in arcminutes relative to the J2000.0 position ($17^h20^m51.s0$, $-35^\circ45'26''$).

$^{b}$ Parameter $\phi$ is the angle of the $E$-vector of the polarized radiation, measured in degrees from north-south, increasing counterclockwise.
inferred magnetic field directions (that are orthogonal to the measured polarization directions) and the magnitudes of polarization (denoted by the lengths of the bars) superposed on *IRAS* 100 μm maps.

3. DISCUSSION

In this section we first give an overview of the characteristics of the four GMCs we observed (§3.1). Then we discuss the measured degrees of polarization (§3.2). In the remaining four subsections we deal with the inferred magnetic field directions, beginning with an overview of the statistics of these directions (§3.3), next comparing with mid-IR intensity maps (§3.4) and with information obtained from optical polarimetry of stars (§3.5), and finally discussing the relevance to theoretical ideas concerning formation and structure of GMCs (§3.6).

3.1. Characteristics of the Observed Clouds

3.1.1. The Carina Nebula

Perhaps the best studied of our four targets is the Carina Nebula (NGC 3372), a very bright emission nebula excited by OB star clusters and lying at a distance of about 2.7 kpc (§3.1.6) in the Carina spiral arm. Optical nebulosity and mid-IR emission extend over ~3° in Galactic latitude and ~2° in longitude (Smith et al. 2000), but most of the far-IR and radio continuum flux is concentrated in the central 1° × 1° region shown in Figure 1 (Shaver & Goss 1970; Zhang et al. 2001). The associated molecular clouds are referred to collectively as the Carina molecular cloud complex (Zhang et al. 2001). This complex is elongated in a direction roughly parallel to the Galactic plane, with an extent of about 3° (~140 pc) in Galactic longitude. The complex has a mass of about 7 × 10^5 M☉ (Grabelsky et al. 1988).

The bright central radio peak of the Carina Nebula consists of two main parts, Carina I and Carina II (Davidson & Humphreys 1997; Whiteoak 1994; Brooks et al. 2001), whose sky locations are indicated in Figure 1 with filled and open stars, respectively. Carina I (aka G287.4−0.6) is powered by the OB star cluster Tr 14, located a few arcminutes to the east of Carina I. Carina II (aka G287.6−0.6) is powered by another OB cluster, Tr 16, that contains η Carinae, a very massive (>100 M☉) evolved star. Star η Carinae is visible in Figure 1 as the flux peak located a few arcminutes southeast of Carina II, and this unusual star can also be seen in Figure 5, as the dominant source near the lower left corner of the Carina map.

Tr 14 and Tr 16 contain large numbers of unusually massive stars. Six of the 17 known O3-type stars in our Galaxy are found in these two clusters (Davidson & Humphreys 1997). Tr 14, which powers the region we mapped polarimetrically, is estimated to be only about 1 million years old (Walborn 1995). There is little evidence for ongoing formation of massive stars within the region encompassed by Tr 14, Tr 16, Carina I, and Carina II (Davidson & Humphreys 1997), but evidence for ongoing star formation has been found surrounding this region, especially to the southeast of

### Table 2: Polarization Results for Carina Nebula

| Δα* (arcmin) | Δδ* (arcmin) | P (%) | σP | φ | σφ |
|--------------|--------------|------|----|---|----|
| 4.36         | 1.67         | 1.74 | 0.41 | 50.6 | 6.7 |
| 5.71         | 4.68         | 1.61 | 0.27 | 71.2 | 4.8 |
| 7.05         | 7.70         | 0.71 | 0.3  | 3.6  | 11.9 |
| 1.34         | 3.01         | 1.4  | 0.36 | 42.4 | 7.3 |
| 2.68         | 6.02         | 1.12 | 0.17 | 30.7 | 4.3 |
| 4.02         | 9.03         | 1.98 | 0.23 | 163.9| 3.4 |
| 10.33        | 7.38         | 1.66 | 0.21 | 177.2| 3.6 |
| 0.62         | 2.68         | 5.45 | 0.41 | 8.5  | 2.2 |
| 4.68         | 5.71         | 2.67 | 0.34 | 15.4 | 3.6 |
| 3.34         | 8.72         | 2.04 | 0.41 | 35.2 | 5.8 |
| 9.03         | 4.02         | 4.46 | 0.44 | 12.2 | 2.8 |
| 7.7          | 7.05         | 4.28 | 0.45 | 26.7 | 3.0 |
| 6.35         | 10.06        | 3.67 | 0.46 | 21.7 | 3.6 |
| 10.7         | 8.39         | 1.99 | 0.76 | 37.9 | 10.9 |
| 9.36         | 11.37        | 2.27 | 0.87 | 52.2 | 11.1 |
| 3.34         | 8.72         | 1.74 | 0.41 | 50.6 | 6.7 |
| 4.68         | 5.71         | 1.61 | 0.27 | 71.2 | 4.8 |
| 6.02         | 2.68         | 0.71 | 0.3  | 3.6  | 11.9 |
| 0.33         | 7.38         | 1.4  | 0.36 | 42.4 | 7.3 |
| 1.67         | 4.36         | 1.12 | 0.17 | 30.7 | 4.3 |
| 3.01         | 1.34         | 1.98 | 0.23 | 163.9| 3.4 |
| 1.34         | 3.01         | 1.66 | 0.21 | 177.2| 3.6 |
| 0            | 2.18         | 0.12 | 0.19 | 169.1| 1.6 |
| 5.71         | 4.68         | 2.2  | 0.5  | 168.8| 6.5 |
| 4.36         | 1.67         | 4.79 | 0.31 | 4.3  | 1.8 |
| 10.06        | 6.53         | 4.5  | 0.93 | 148.2| 5.9 |
| 8.72         | 3.34         | 4.6  | 0.57 | 167.8| 3.5 |
| 7.38         | 0.33         | 6.14 | 0.51 | 179.1| 2.4 |
| 11.73        | 2           | 2.96 | 0.7  | 1.4  | 6.8 |
| 10.39        | 1.02         | 4.56 | 0.62 | 20.4 | 3.9 |

* Offsets in right ascension and declination are measured in arcminutes relative to the J2000.0 position (10^h43^m15^s6, -59°33'34'').
TABLE 4
Polarization Results for G331.5—0.1

| Δα° | Δδ° | P (%) | σP | φ | σφ |
|-----|-----|-------|----|---|----|
| 1.67 | -4.36 | 0.4 | 0.07 | 62.2 | 4.7 |
| 3.01 | -1.34 | 0.48 | 0.04 | 167.3 | 2.5 |
| 4.36 | 1.67 | 0.47 | 0.04 | 133.1 | 2.6 |
| -1.34 | -3.01 | 0.44 | 0.07 | 120.8 | 4.6 |
| 0 | 0 | 0.3 | 0.05 | 5.8 | 4.7 |
| 1.34 | 3.01 | 0.46 | 0.04 | 132.4 | 2.8 |
| -3.01 | 1.34 | 1.14 | 0.11 | 123.2 | 2.8 |
| -1.67 | 4.36 | 1.87 | 0.11 | 192.2 | 1.8 |
| 5.71 | 4.68 | 1.37 | 0.14 | 137.5 | 2.8 |
| 7.05 | 7.7 | 1.12 | 0.19 | 121.3 | 4.8 |
| 8.38 | 10.7 | 1.97 | 0.24 | 116.3 | 3.5 |
| 2.68 | 6.02 | 1.26 | 0.11 | 129.9 | 2.4 |
| 4.02 | 9.03 | 1.06 | 0.25 | 121.8 | 6.6 |
| 5.36 | 12.04 | 4.07 | 0.59 | 117.9 | 4.2 |
| 1.02 | 10.39 | 3.32 | 0.38 | 122.3 | 3.3 |
| 2.35 | 13.39 | 4.02 | 0.6 | 114.6 | 4.3 |
| 10.7 | -8.38 | 1.65 | 0.55 | 30.3 | 9.5 |
| 12.04 | -5.36 | 1.5 | 0.56 | 33.0 | 10.6 |
| 6.02 | -2.68 | 1.43 | 0.29 | 151.6 | 5.8 |
| -6.02 | 2.68 | 2.4 | 0.38 | 120.6 | 4.6 |
| -7.7 | 7.05 | 2.45 | 0.77 | 113.8 | 9.1 |
| -12.04 | 5.36 | 1.14 | 0.44 | 120.2 | 11.0 |
| -10.7 | 8.38 | 3.11 | 0.84 | 127.0 | 7.7 |
| -2.35 | 13.39 | 12.3 | 0.37 | 132.2 | 8.6 |
| -1.02 | 10.39 | 1.23 | 0.29 | 116.0 | 6.7 |
| 0.33 | -7.38 | 0.69 | 0.3 | 94.8 | 12.7 |
| 10.39 | -1.02 | 0.81 | 0.29 | 158.7 | 10.2 |
| 11.73 | 2 | 1.23 | 0.31 | 138.8 | 7.3 |
| 13.08 | 5.01 | 1.29 | 0.26 | 133.5 | 5.9 |
| 7.38 | 0.33 | 3.55 | 0.42 | 125.7 | 3.4 |
| 8.72 | 3.34 | 2.81 | 0.43 | 124.4 | 4.4 |
| 10.06 | 6.35 | 3.27 | 0.45 | 124.9 | 3.9 |
| -0.33 | 7.38 | 1.94 | 0.23 | 125.6 | 3.4 |
| -4.68 | 5.71 | 3.55 | 0.42 | 125.7 | 3.4 |
| -3.34 | 8.72 | 2.81 | 0.43 | 124.4 | 4.4 |
| -2 | 11.37 | 3.27 | 0.45 | 124.9 | 3.9 |
| -6.35 | 10.06 | 2.94 | 0.44 | 121.4 | 4.3 |
| -5.01 | 13.08 | 2.88 | 0.76 | 131.0 | 7.6 |
| 0.01 | -13.08 | 0.91 | 0.42 | 110.3 | 13.2 |
| 6.35 | -10.06 | 1.04 | 0.26 | 114.1 | 7.2 |
| 7.7 | -7.05 | 0.62 | 0.25 | 127.6 | 11.6 |
| 2 | -11.73 | 1.54 | 0.34 | 128.1 | 6.4 |
| 3.34 | -8.72 | 1.26 | 0.25 | 112.4 | 5.8 |
| -7.05 | -7.7 | 0.91 | 0.42 | 110.3 | 13.2 |
| -5.71 | -4.68 | 1.04 | 0.26 | 114.1 | 7.2 |
| -4.36 | -1.67 | 0.62 | 0.25 | 127.6 | 11.6 |
| -10.06 | -6.35 | 2.22 | 0.52 | 123.2 | 6.7 |
| -8.72 | -3.34 | 1.54 | 0.34 | 128.1 | 6.4 |
| -7.38 | -0.33 | 1.26 | 0.25 | 112.4 | 5.8 |
| -11.73 | -2 | 2.42 | 0.48 | 135.4 | 5.6 |
| -10.39 | 1.02 | 2.35 | 0.46 | 126.5 | 5.6 |

* Offsets in right ascension and declination are measured in arcminutes relative to the J2000.0 position (16h11m59.80s, -51°28′40″).

NGC 6334 is an optically visible H region lying at a distance of 1.7 kpc (Neckel 1978; § 3.1.6). The radio map of Goss & Shaver (1970) shows ionized gas distributed over a region of 10 pc in size, while the optical nebulousness extends over a region of about 20 pc in extent (Gardner & Whiteoak 1975; Straw & Hyland 1989). The extent of the associated molecular gas is also about 20 pc (Dickel et al. 1977). From these maps we see that gas associated with NGC 6334 may not extend much beyond the region shown in Figure 1. Based on the CO map of Dickel et al. (1977), Straw & Hyland (1989) estimate a mass of 1.5 – 10⁶ M☉ for the entire cloud. Comparing the size and mass of NGC 6334 with values given above for the Carina molecular cloud complex and the l = 333° complex, we see that NGC 6334 may be somewhat smaller and less massive.

Just as they did for the case of G333.6—0.2, Sollins & Megeath (2004) present strong evidence of ongoing formation of massive stars in NGC 6334. They studied the source NGC 6334 I that lies toward the northern edge of the dense ridge of emission seen in Figure 1, and they found two molecular cores each containing 10³ M☉ of dense (10⁸ cm⁻³) gas, one of which corresponds to an ultracompact H region. Based on its distance (1.7 kpc; § 3.1.6) and on the Taylor & Cordes (1993) model, NGC 6334 is located in the Carina-Sagittarius spiral arm.

3.1.4. G331.5—0.1

Of our four targets, G331.5—0.1 is the one that has been studied least. This H region and six other nearby radio sources form a group having an extent of about 1° in Galactic longitude and about 0.5° in latitude (Amaral & Abraham 1991). The group is centered near l = 331°. Several of these radio sources can be seen in Figure 1, and several others lie beyond the southern and western edges of the image.

Not all of the members of this group have the same line-of-sight velocity, so it is generally believed that the group is a superposition of two unrelated complexes (Russell et al. 2005; Amaral...
Both complexes are elongated parallel to the Galactic plane, and they are separated not only in velocity but also in Galactic latitude. The complex containing G331.5\textasciitilde0.1, which is seen at (0\textdegree,0\textdegree) in Figure 1, has generally more positive latitudes and a higher negative velocity. This complex is referred to by Russeil et al. (2005) as ''the 87 km s\textasciitilde1 complex.'' The other complex, which contains the source G331.3\textasciitilde0.3, seen at (0\textdegree,N) in Figure 1, has generally more negative latitude and a lower negative velocity. It is referred to by Russeil et al. (2005) as the ''65 km s\textasciitilde1 complex.''

Except for G331.3\textasciitilde0.3, all major flux peaks seen in Figure 1 correspond to the 87 km s\textasciitilde1 complex.

For the most part, sky locations where we obtained polarimetry data correspond to the 87 km s\textasciitilde1 complex. About seven vectors lying at the southeast corner of our polarization map are closer to G331.3\textasciitilde0.3 than to any source in the 87 km s\textasciitilde1 complex, so they probably correspond to the 65 km s\textasciitilde1 complex. Note that many of these vectors are more nearly perpendicular to the Galactic plane, while the vectors for the rest of the map are more nearly parallel to it.

The distance to the 87 km s\textasciitilde1 complex is still uncertain, but Russeil et al. (2005) argue for a distance of 5.3 kpc (§ 3.1.6). The 65 km s\textasciitilde1 complex lies at 4.2 kpc, according to these authors. Molecular emission corresponding to the 87 km s\textasciitilde1 complex can be seen in the CO maps of Bronfman et al. (1989). The size and shape of this CO structure are similar to those measured for the 333\textdegree complex that contains G333.6\textasciitilde0.2 (§ 3.1.2), but the integrated intensity is somewhat lower. Factoring in the greater distance, the molecular mass of the 87 km s\textasciitilde1 complex could be comparable to that of the 333\textdegree complex. Despite the overall paucity of observations for G331.5\textasciitilde0.1, it does seem that evidence for ongoing formation of massive stars has been found. For example, at the position of this source we find a massive ammonia core (Vilas-Boas & Abraham 2000), CS emission (Bronfman et al. 2000), and strong methanol maser emission (Walsh et al. 1997).

\subsection*{3.1.5. Comparison of the Four GMCs Observed}

All four SPARO targets are associated with massive GMCs (10^5\textasciitilde10^6 M_\odot) and ongoing or recent formation of massive stars.
Using IRAS results as their database, Kuiper et al. (1987) did a comparative study of 65 of the brightest southern molecular clouds in the Galaxy, including our four targets. They calculated 60/100 μm color temperatures and column densities. For NGC 6334, G333.6–0.2, and G331.5–0.1, temperatures were in the range 40–43 K. These values are near the peak of the distribution for the 65 sources. For the Carina Nebula, a color temperature of 48 K was found. This value lies in the upper tail of the distribution. Column densities for Carina were significantly lower than for our other three targets. One explanation for these differences is that Carina is more evolved than the others, so more gas has been dispersed and more energy has been released to heat the dust. This would be consistent with the observed fact that massive stars do not seem to be currently forming within the region corresponding to our polarimetric map of Carina (§ 3.1.6).

### 3.1.6. Methods Used to Determine Cloud Distances

For purposes of comparing our results with optical polarization (§ 3.5) and estimating physical scales corresponding to the SPARO beam size (§ 3.6) we require accurate estimates of the distances to our targets. Distance determinations for these targets fall into two categories: stellar distance estimates (e.g., spectroscopic parallax) and kinematic distance estimates, based on the Galactic rotation curve. The latter solution is multivalued, providing a “near distance” and a “far distance.” Using the spectroscopic parallax method, Neckel (1978) obtained distance estimates for OB stars presumed to be associated with NGC 6334. On this basis, they derive a distance of 1.7 ± 0.3 kpc for this cloud.

The star clusters Tr 16 and Tr 14 that power the Carina Nebula are separated by about 15 pc on the sky. The maps in Smith et al. (2000) show that this nebula is reasonably isolated on the sky, so it seems likely that the two clusters lie at roughly the same distance. Distances to these clusters and to specific stars within them have been obtained by Carraro et al. (2004), Davidson et al. (2001), Freymhammer et al. (2001), Rauw et al. (2001), Tapia et al. (2003), and Vazquez et al. (1996). These six independent estimates have a mean of 2.7 kpc and a standard deviation of 0.4 kpc. Our distance estimate does not change significantly if we drop the requirement that the two clusters must lie at the same distance and instead simply estimate the distance to Tr 14, which is the cluster that powers the far-IR flux peak that we mapped polarimetrically with SPARO.

For G333.6–0.2 and G331.5–0.1, distance estimates are kinematic. For G333.6–0.2, we adopt the value 3.0 kpc, given by Sollins & Megeath (2004) and Colgan et al. (1993). Other values found in the recent literature are 3.5 kpc (Russell et al. 2005) and 2.8 kpc (Vilas-Boas & Abraham 2000). The far kinematic distance of about 11 kpc can be ruled out because Russell et al. (2005) detect optical emission from six sources in the \( f = 333\)° complex (which they refer to as “CO cloud 1”). For G331.5–0.1, it is again the near distance that is almost always quoted, but in this case it is not as easy to rule out the far distance. The strongest discriminative appears to be the comparison of absorption and emission spectra carried out by Dickey et al. (2003) that places G331.5–0.1 at the near kinematic distance, which is given by Russell et al. (2005) as 5.3 kpc.

### 3.2. Measured Polarization Magnitudes

Hildebrand et al. (1999) show the distribution of measured magnitudes of 350 μm polarization for a large sample of measurements, obtained from polarization maps that generally sample smaller spatial scales in comparison with our SPARO maps. The mean magnitude in the Hildebrand et al. (1999) sample is 1.6%, while ours is slightly higher at 2.0%. Several factors could account for this difference. First note that in Figure 1, the higher degrees of polarization usually are found in regions with lower column density, a trend that has also been seen in smaller scale maps (Matthews & Wilson 2000; Henning et al. 2001; Lai et al. 2002; Crutcher et al. 2004). Since the SPARO data sample regions of generally lower column density in comparison with the regions studied by Hildebrand et al. (1999), this effect could explain why SPARO sees higher polarization. On the other hand, SPARO’s large beam averages over more field disorder, which would tend to reduce the polarization magnitude. Another effect that could be important is the improved data analysis method (§ 2), which removes the bias toward low polarization magnitude (Li et al. 2005). Finally, note that Vaillancourt (2002) present evidence for structure in the polarization spectrum, so the modest wavelength difference (350 μm vs. 450 μm) could be important.

### 3.3. Statistics of the Inferred Magnetic Field Directions

Figure 2 shows the distribution of projected magnetic field position angles, for the entire sample of measurements for all four clouds. The position angle is given in Galactic coordinates, with 0° corresponding to Galactic north-south, and with position angle increasing in the counterclockwise direction. Note that the measurements tend to cluster near the dark vertical line at position angle 90°, corresponding to magnetic fields running parallel to the Galactic plane. Relatively few measurements are found near the left- and right-hand extremes of the histogram, corresponding to fields orthogonal to the plane. We can explain this by supposing that large-scale magnetic fields in GMCs are generally parallel to the even larger scale Galactic fields in the regions surrounding these clouds, which are known to run preferentially parallel to the Galactic plane (Mathewson & Ford 1970). Much of the remainder of this paper is devoted to exploring the validity of this conclusion and its implications.

As a first step, we break the histogram in Figure 2 into four separate histograms, one for each of our four target GMCs. This is shown in Figure 3, where we also show vertical dotted lines indicating the mean position angle for each cloud. The method we use to calculate this mean is described in the paragraphs below. For three of the four clouds, the mean field direction is nearly
parallel to the Galactic plane, but for NGC 6334 the mean is almost perpendicular to the plane.

Because the field direction measurements wrap around, with \(0^\circ = 180^\circ\), the mean position angle is actually undefined. However, it is clear that each cloud has a well-defined peak in the distribution of angles (Fig. 3). We have devised a technique for estimating the position of this peak, based on the formalism of Stokes parameters (see, e.g., Jackson 1999). Two of the four Stokes parameters, \(Q\) and \(U\), contain information about the state of linear polarization of a light beam. They are related to the intensity of linearly polarized flux \(I_{PF}\) and angle of polarization "\(\phi\) via

\[
Q = I_{PF} \cos(2\phi), \quad U = I_{PF} \sin(2\phi).
\]

Our method is as follows: For a given cloud, we first compute \(Q_i\) and \(U_i\) for each sky position \(i\) where we have detected polarization. Note that by summing these to form \(Q_{\text{sum}}\) and \(U_{\text{sum}}\), one can determine the polarization state that would be measured by an imaginary polarimeter that acts by combining all flux from the region studied by SPARO and making one polarization measurement on it. However, since our goal is to study the global field of each cloud, we do not want regions having high column density to be given more weight than regions having low column density. Furthermore, we do not want regions having high grain alignment efficiency to be given more weight than regions with low efficiency. Accordingly, to ensure that each sky position will be given equal weight, we compute

\[
Q'_i = Q_i / I_{PF}, \quad U'_i = U_i / I_{PF}
\]

and then average all values of \(Q'_i\) and \(U'_i\) for a given cloud to form \(\bar{Q}'\) and \(\bar{U}'\). From these “equal weight” average values we can derive a mean polarization angle for the cloud using the formalism in equation (1). We refer to the mean magnetic field direction obtained in this way as the “equal weight Stokes mean,” \(\theta_{\text{EWSM}}\). Note that because the total flux and degree of polarization cancel out in equation (2), \(\theta_{\text{EWSM}}\) is actually determined using only the measured angles of polarization. No other information is required. Our method for computing \(\theta_{\text{EWSM}}\) also yields another parameter that we refer to as the “order parameter,” defined as \(o = \frac{\sqrt{(\bar{Q}'^2 + \bar{U}'^2)}}{2}\). For a set of polarization measurements all having the same position angle, we obtain \(o = 1\). For a set of measurements having position angles uniformly spaced over a full \(180^\circ\), we obtain \(o = 0\). We use this parameter in \(\S\) 3.5.3 and 3.6.1.

Note that for three of our four clouds, the mean field angle \(\theta_{\text{EWSM}}\) is within \(15^\circ\) of the Galactic plane (Figs. 3 and 4). For a set of clouds having a random distribution of \(\theta_{\text{EWSM}}\) we would expect on average only one cloud in six to have \(\theta_{\text{EWSM}}\) within \(15^\circ\) of the plane. If we choose four random angles between \(0^\circ\) and \(180^\circ\), the probability for obtaining at least three of the four within the interval \(90^\circ \pm 15^\circ\) is only \((4 \times 5 + 1)/6^4 = 0.0162\). Therefore, this is unlikely to be a chance alignment. The most likely explanation is the one we advanced in the first paragraph of this section: large-scale magnetic fields in GMCs are preferentially parallel to the fields in the even larger scale regions of the Galaxy that surround these clouds. We explore this issue further in \(\S\) 3.5, where we also examine the case of the discrepant cloud NGC 6334.

**Fig. 3.—** Histograms of magnetic field directions for all SPARO measurements, broken down by cloud. For each panel, a vertical dotted line shows the mean magnetic field direction for the cloud, computed as described in \(\S\) 3.3. Position angle is measured in Galactic coordinates, as in Fig. 2.
3.4. Comparisons with Midcourse Space Experiment (MSX) Maps

Polycyclic aromatic hydrocarbon molecules (PAHs) can be used as a tracer of massive star formation (Peeters et al. 2004). These molecules absorb far-UV photons emitted by stars and transfer the energy into vibrational modes associated with molecular stretching and bending. The PAHs then cool by emitting IR radiation, mostly in the wavelength range 3–11 μm. The 8 μm emission shown in Figure 5 is mostly, although not entirely, due to PAHs. The main exception is that some of the point sources seen in these images correspond to stars surrounded by hot dust.

The 3–11 μm PAH spectrum depends significantly on the charge states (see Fig. 2 of Allamandola et al. 1999; Peeters 2002), which are determined by the ratio of the illuminating UV radiation field to the electron density, $G_0/n_e$. In regions having high $G_0/n_e$ the ionized states of PAH dominate, while for low $G_0/n_e$ it is the neutral states that are more common. In the ionized state, the intensity of the 8 μm emission is much higher. In crossing the boundary of an H ii region, $n_e$ changes dramatically but $G_0$ changes relatively little. The result is a sharp change in the 8 μm brightness at the boundary of an H ii region. This effect can be seen in the 8 μm map of Carina shown in Figure 5. The shapes of the bipolar H ii bubbles seen in this figure are very close to shapes seen in the superbubble simulations of Silich & Franco (1999).
OB stars ionize their surroundings, and the ionization pressure wave propagates outward from the star-forming region. The speed of propagation is inversely proportional to the density of the ambient interstellar medium (ISM), so H II regions usually grow fastest along the direction perpendicular to the Galactic plane. This explains the bipolar morphology of the H II bubbles (Silich & Franco 1999; Smith et al. 2000).

Note that the magnetic field directions we determined for Carina closely follow the boundaries of the two expanding H II bubbles (Fig. 5). This can be understood as the effect of the expansion of the bubble on the magnetic field. In this model, we must assume that the expansion of the ionization front is accompanied by bulk gas motion, such that gas is generally flowing in a direction that points away from the center of the bubble. This is reasonable as the ionized gas will be heated and will tend to expand. In this case the gas just beyond the edge of each bubble will be compressed in a direction perpendicular to the bubble edge. Under flux-freezing conditions, such compression will have a strong effect on the magnetic field. The result will be that the field will tend to be parallel to the compression front (see, e.g., Novak et al. 2000), precisely as we observe in Carina.

However, there is an alternative explanation that could account for the observed parallelism between the edges of the bubble and the field without requiring a compression front. To see this, note that gas expansion, under flux-freezing conditions, will always cause distortions in the ambient magnetic field regardless of the existence or nonexistence of a compression front external to the bubble. A concrete example is provided by the model of Tomisaka (1998) where it is the magnetic tension rather than external gas pressure that acts to resist the expansion of the bubble.

The bubble-like structures seen in Carina are much more striking than the structures seen in the three other 8 µm maps shown in Figure 5. This may indicate that, in comparison with our other three targets, Carina has suffered a relatively greater amount of disruption induced by star formation. If so, that would explain why Carina shows more variation in inferred magnetic field direction in comparison with the other SPARO targets (Fig. 3). This interpretation is consistent with what we learned from the comparison between the four clouds (§ 3.1.5).

High-resolution radio polarization measurements of galaxies show that the magnetic field is well aligned with spiral arms (Neininger 1992; Neininger & Horellou 1996; Patrickeyev et al. 2005). Because field disorder is star formation, one might argue that the lesser degree of uniformity of the fields in Carina is a result of the near coincidence of the line of sight and the tangent to the Carina spiral arm at the location of the cloud. (The angle between the line of sight and the arm tangent is ~20°, much lower than for NGC 6334 or G33.6–0.2.) However, the strong correlation between the fields and the bubble boundaries shows that the main reason for the field disorder is star formation.

G33.6–0.2 also contains bipolar PAH bubbles. These can be seen in the image shown in Figure 5, at position (0°10, –0°05) and (0°0, 0°05). They are much easier to see in the recently obtained Spitzer GLIMPSE images (B. Whitney 2005, private communication). In contrast to the case of Carina, our polarization map for G33.6–0.2 covers a region significantly larger than the area containing the bubbles. The field in G33.6–0.2 is basically uniform, but note that the field lines running near the “Galactic north” edge of the northern bubble appear to be pushed outward by the bubble. NGC 6334 also shows bubble-like structures in Figure 5, but the strongest such structures occur at locations for which we have no SPARO polarization data.

3.5. Comparison with Stellar Polarization Data

It has been shown that Galactic magnetic fields tend to be parallel to the Galactic disk on large scales. For example, optical polarization measurements for stars more than 2 kpc show inferred field directions that are mostly parallel to the plane (Mathewson & Ford 1970). As discussed in § 3.3, our observations suggest that on the scales of our SPARO polarization maps (much smaller than 1 kpc), this tendency is still evident. This can be understood if the processes that act to accumulate diffuse gas and thereby form a GMC do not significantly alter the mean magnetic field direction in the ISM. But in this case, how do we account for the outlier NGC 6334? One answer to this question is suggested by the fact that even though the large-scale Galactic field is parallel to the disk, there are nevertheless spatial fluctuations in the Galactic field that occur on scales that are larger than the size of a GMC (e.g., Mathewson & Ford 1970). If NGC 6334 happened to form in a region where such fluctuations had resulted in a field significantly different from the large-scale average, then this could explain the discrepancy.

In principle, this idea can be tested by comparing SPARO results for each cloud with the field direction in the surrounding diffuse medium as sampled by optical polarimetry of stars. In practice, we have only been able to do this for NGC 6334, the closest of our four targets. Here we describe the results of this analysis, which was carried out using a stellar polarization database published by Heiles (2000). Since this database was created by combining many previous polarization catalogs, it is referred to by the author as an “agglomeration.” When computing the field direction in the surrounding diffuse medium, we must choose a length scale to characterize this larger region. The natural choice is the accumulation length, defined so that the cube of this length corresponds to the volume of diffuse ISM containing a gas mass equal to the mass of a GMC. Williams et al. (2000) estimate an accumulation length of 400 pc for the Galactic disk.

A stellar polarization measurement gives the mean field direction, weighted by density of dust particles, along the line of sight. To determine the field in a particular region, one must subtract the foreground polarization, inferred from foreground stars, from that measured for background stars (e.g., Marraco et al. 1993). In our analysis of the Heiles (2000) database, we carry out such subtractions. Stellar distance measurements are important because we will rely on them to define the foreground and background stars for a given region. Based on comparisons among the various catalogs that he has agglomerated, Heiles (2000) estimates a typical distance uncertainty of about 20%.

3.5.1. Evidence of Bias in the Heiles Database

Besides foreground distance, another factor that is relevant to the problem of foreground effect subtraction is extinction. For the Heiles (2000) database, Figure 6 shows how the selective extinction, E(B – V), varies with distance. Each point represents the mean E(B – V) for stars within a 100 pc interval. In Figure 6 we have included only stars having |b| < 0.1, where b is the Galactic latitude. The figure shows that the selective extinction grows quite linearly up to ~1.5 kpc, with a slope close to 0.6 mag kpc⁻¹ given by Spitzer (1978). Beyond this distance, the extinction tends to level off. There are three effects that could contribute to this flattening of the extinction curve: (1) There is more dust nearer to the Sun than farther from it (i.e., we live within a local density enhancement). (2) The database is biased against stars that have both large distances and large extinctions. Such stars would be relatively faint, so in a flux-limited sample there could be a selection effect that tends to exclude them. We refer to this selection...
effect as “Kapteyn universe bias.” (3) For a fixed latitude, sight lines to more distant stars extend to larger distances away from the Galactic plane, where there is less dust.

Because we have restricted $b$ to $\pm 0.1\degree$, we can be reasonably sure that explanation 3 does not play a large role. This is because no sight line in our sample extends farther than 5 pc from the Galactic plane, for distances up to 3 kpc. A distance of 5 pc is much smaller than the scale height of the H I gas (Spitzer 1978). Given that the dust density should be highest at the location of the spiral arms and that the Sun is situated about halfway between two such arms, each about 2 kpc distant (Xu et al. 2006), it seems highly unlikely that explanation 1 could account for all of the flattening seen in Figure 6. Thus, explanation 2 must play a significant role.

Kapteyn universe bias can introduce uncertainties in the correction for foreground polarization. For this reason, we believe that using the data of Heiles (2000) to study regions much beyond 1.5 kpc will give unreliable results. We have chosen to study regions as far as 1.7 kpc so that we can include the vicinity of NGC 6334 ($d = 1.7 \; \text{kpc}$; § 3.1.6). The next closest source, Carina, lies at a distance of 2.7 kpc, well into the flat part of the extinction curve. In § 3.5.4 we show that Kapteyn universe bias does not affect our main conclusions for regions as far as 1.7 kpc.

3.5.2. Choice of Cells for Analysis

In our analysis of the Heiles (2000) database, we divide the nearby ($d \leq 1.7 \; \text{kpc}$) regions of the Galactic plane into “cells” with dimensions roughly corresponding to the accumulation length ($\sim 400$ pc; second paragraph of § 3.5). One such cell is centered on NGC 6334. For each cell, we collect data from Heiles (2000) and apply a correction for foreground polarization in order to estimate the mean magnetic field direction within that cell. For the NGC 6334 cell, we compare this result with the mean field direction inferred from the SPARO data. The other cells serve as comparison regions.

Our cells are cuboids in $(l, b, d)$-space, where $l$ and $b$ are Galactic longitude and latitude and $d$ is distance from the Sun. All cells are centered on $b = 0^\circ$ and centered on one of three possible values of $d$: 0.7, 1.2, and 1.7 kpc. As viewed from far above the Galactic plane, they tile the local region of the Galactic disk, forming three complete $360^\circ$ rings of cells, with the whole pattern centered on the Sun. The angular size of a cell along its $l$-dimension decreases with distance so that we can keep the corresponding spatial scale (measured in pc) approximately constant. Thus, the number of cells in a given ring increases with the $d$-value of that ring. The cells’ angular size along the $b$-dimension also decreases with distance, for the same reason. The cells’ linear sizes deviate somewhat from 400 pc, especially along the $b$-dimension, for reasons explained below.

For each cell, we construct foreground (background) cells that are similar to the main cell but centered on the near (far) face of the main cell (see Fig. 7). As described in the next section, the polarization measurements for “foreground stars” (stars lying within the foreground cell) are used to correct the polarization measurements for each “background star” (star lying in the background cell), thus providing a set of rough estimates for the stellar polarization induced by dust lying within the main cell.

As noted above, our intent was to have cells with dimensions corresponding to the accumulation scale, estimated to be 400 pc. We modified the in-plane spatial footprint of each cell, $(\delta l, \delta d)$, from (400 pc, 400 pc) to (300 pc, 500 pc) in order to take into account the uncertainty in stellar distances. This is why the three rings are separated by 500 pc in $d$. At the distance of our farthest background cells, centered at $d = 1.7 + 0.25 = 1.95$ kpc, the 20% distance uncertainty translates to approximately 400 pc. Thus, even after increasing $\delta d$ to 600 pc or higher while preserving nonoverlapping cells would have resulted in a sample containing only two rings of cells rather than three, as there would not have been enough space for the foreground cells corresponding to the closest ring of main cells.

For each ring, we adjusted $\delta l$ slightly from 300 pc so that the full $360^\circ$ are covered by an integer number of cells. For the 1.7 kpc ring, the longitudinal dividing lines of the cells are chosen so that one cell is centered on NGC 6334. For the two closer rings, we have arbitrarily chosen $l = 0^\circ$ as a dividing line.

The size of the cells along the direction perpendicular to the Galactic plane $(bb)$ has been set at 120 pc. The reason that we chose such a relatively small value for $bb$ is related to the scale height of Galactic gas. Since the thickness of the H I disk is 240 pc (Spitzer 1978), setting $bb$ to 400 pc would have resulted in the inclusion of relatively high latitude background stars having relatively little line-of-sight dust within the main cell. The polarization induced by this relatively small column of dust would have been very small, so the inferred foreground-corrected polarization angles corresponding to these stars would have been very uncertain. Because our method for determining the mean magnetic field angle for each cell (§ 3.5.3) gives equal weight to each background star, the use of $bb = 400$ pc would have thus resulted in loss of accuracy. We chose $bb$ to equal half of the thickness of the H I disk in order to preferentially sample the denser part of this gas layer. Note also that all four of the GMCs observed with SPARO lie within 30 pc of the Galactic plane. The resulting $(\delta l \times \delta b)$ sizes are $24^\circ \times 10^\circ$, $15^\circ \times 6^\circ$, and $10^\circ \times 4^\circ$ for rings at $d = 0.7, 1.2$, and 1.7 kpc, respectively. Finally, note that for the NGC 6334 cell we have explored the effect of increasing $bb$ (§ 3.5.5).

3.5.3. Selection and Processing of Stellar Polarization Data for a Single Cell

In order to correct for the effects of foreground polarization, we use the method introduced by Marraco et al. (1993). For each
star in the background cell, we first collect a subset of the stars in the foreground cell, chosen to have sky coordinates reasonably close to those of the background star (Fig. 7). Then linear functions of $l$ and $b$, $q(l, b) = c_1 + c_2 l + c_3 b$ and $u(l, b) = c_4 + c_5 l + c_6 b$, are fitted to the normalized Stokes parameters, $q_f$ and $u_f$, of the subset of foreground stars. Next, the contributions of the dust in the main cell to the Stokes parameters of the background star, $q_b$ and $u_b$, are estimated by $q_b = q(l_0, b_0)$ and $u_b = u(l_0, b_0)$, where $(l_0, b_0)$ are the coordinates of the background star. In this way we can estimate the polarization introduced to the background star by dust in the particular main cell under study. We refer to this as the polarization residue and it contains information about the magnetic field direction in the cell.

During the analysis, several criteria are used to reject stars. First, stars with nonpositive values for selective extinction are not used. Also, a background star is rejected if it has fewer than four corresponding foreground stars (Fig. 7). Although three stars are sufficient for the fit, we found that occasionally they will lie close to a straight line on the sky, thus making the fit very unreliable. A background star having polarization residue below 0.2% is also rejected as being too close to the 0.1% accuracy of the Heiles (2000) database.

For three cells in our sample, we show in Figure 8 the polarization residues for all unrejected background stars. The mean field direction for a given cell is estimated by the equal weight Stokes mean $\theta_{\text{EWSM}}$ of the polarization residues. Cells containing fewer than five polarization residues are rejected. A total of 22 of the 75 cells in our study survive this cut. A further cut is made based on the order parameter (o.p.; Fig. 3.3). Figure 8 illustrates how the order parameter is related to the degree of uniformity in the field directions given by the polarization residues. We see that for the cell with o.p. = 0.21, one would not conclude that the overall field direction for the cell is constrained in any way, so the mean field direction determined for this cell has little meaning. For the cell with o.p. = 0.41, however, the vectors suggest that there is a well-defined mean field direction. The criterion we used is o.p. $\leq$ 0.3, which results in rejection of half of the remaining 22 cells.

Using the analysis described above, we obtain mean field directions for 11 cells, and their distribution is shown in Figure 9. More than half of the cells have magnetic field angles within 30° of the Galactic plane, and the equal weight Stokes mean of the 11 angles is 103°, which is reasonably close to the direction of the Galactic plane. The cell corresponding to NGC 6334 is shaded in Figure 9. Note that NGC 6334 falls in the same bin in this figure as it did in Figure 4, where we showed the distribution of the GMC field directions determined by SPARO. The polarization residues for the NGC 6334 cell are shown in the top panel of Figure 8.
3.5.4. Correction for the Effects of Kapteyn Universe Bias

As discussed in §3.5.1, there is evidence for Kapteyn universe bias in the Heiles (2000) database. If we assume that this bias is the only effect contributing to the flattening of the extinction curve of Figure 6, then we can derive a “bias correction” that we can apply to the Heiles database in order to remove the bias. Although it is not clear that all of the flattening is due to Kapteyn universe bias (§3.5.1), we nevertheless apply this correction in order to get a rough idea of the possible effects of the bias on our analysis.

Our bias correction is based on the reasonable assumption that the bias affects the normalized Stokes parameters $q$ and $u$ in the same way that it affects the measured values of selective extinction. The correction works as follows: First, we extend an extrapolation of the linear portion of the extinction curve over the full range of distances (see Fig. 6, dotted line). We assume that this would be the measured extinction curve in the absence of the bias. Next, we multiply all of the normalized Stokes parameters measured for stars having $d \geq 1.5$ kpc by a correction factor that depends on distance and is determined by taking the ratio of the extinction value given by the extrapolation (dotted line) to that given by the data themselves (estimated by the horizontal line).

If we apply this bias correction to the Heiles data before using it in our analysis, we find that 10 cells (rather than 11) survive the various cuts. The resulting distribution of magnetic field directions for these cells is shown in Figure 10. Note that the peak corresponding to fields parallel to the Galactic plane is somewhat stronger. The NGC 6334 cell is again indicated as a shaded box, and its field direction is essentially unchanged. (Note that many of the stars we use in our analysis have distances less than 1.5 kpc, so for these stars the bias correction has no effect.)

There are two reasons to suspect that our correction for Kapteyn universe bias may be too strong. First, if Kapteyn universe bias is not the only reason for the flattening of the extinction curve, then we will be overcorrecting. The second reason is that some of the cuts we made on the data may have served to eliminate background stars with relatively stronger bias (the “$P/C21 < 2\%$” cut) and also cells with relatively stronger bias (the “$o.p. > 0.3$” cut). (To understand the effect of the o.p. cut, note that the Kapteyn universe bias tends to dilute the “real” polarization residues and thus could reduce the agreement among vectors in a cell.) In this case, applying the bias correction to the surviving cells, which have relatively weaker bias, will result in overcorrection. Keeping these possibilities in mind, all we can conclude from our analysis is that our best estimate for the true distribution of field directions probably lies somewhere between the histograms of Figures 9 and 10.

In §3.3 we noted that three of our four GMCs have mean magnetic field directions lying very close to the Galactic plane and that the probability of this being due to chance alignment is very low. There remained the problem of understanding the outlier, NGC 6334. The result of our study of the local Galactic field on $\sim 400$ pc scales is that the NGC 6334 region turns out to again be an outlier. Specifically, in terms of the angular displacement of its field from the orientation of the Galactic plane, the NGC 6334 cell is either the third highest of 11 (Fig. 9) or the highest of 10 (Fig. 10), depending on whether or not the bias correction is
applied. We conclude that the most likely explanation for the discrepant SPARO result for NGC 6334 is that the cloud formed in a somewhat unusual region of the Galaxy, where the field direction (on ~400 pc scales) is nearly perpendicular to the Galactic plane. As a whole, our results for the four clouds suggest that the mean field direction inside a GMC is roughly parallel to that in a surrounding region having size approximately given by the accumulation length.

3.5.5. Dependence on Assumed Distance of NGC 6334 and Cell Size

We concluded above that the cell corresponding to NGC 6334 is an outlier with respect to the distribution of cell field directions. Next we show that this conclusion is reasonably robust in the sense that it does not depend sensitively on the precise distance assumed for NGC 6334, nor on the precise cell dimensions.

As noted in § 3.1.6, the uncertainty in the distance to NGC 6334 is given as 0.3 kpc. This is due to systematic, not statistical, errors (Neckel 1978). We have repeated the analysis for this cell while displacing its center in 100 pc increments along the line of sight away from the nominal value of 1.7 kpc. For distance values of 1.5, 1.6, 1.7, 1.8, and 1.9 kpc, we find magnetic field directions (measured counterclockwise from Galactic north) of ~21°, 5°, 20°, 37°, and ~23°. For cells centered at 1.4 and 2.0 kpc, there are fewer than five background stars, which is below our threshold for analysis as discussed in § 3.5.3. Although there is thus significant variation with distance, in all five cases the field direction is closer to being perpendicular to the Galactic plane than to being parallel to the plane.

We changed the size of the cell centered on NGC 6334 to examine the effect on field direction. Shrinking any of the three dimensions to half the original size will not change the mean field direction by more than 8°. Increasing the size along either the line-of-sight or latitude directions will not change the mean field direction by more than 15°. Finally, if we increase the dimension along the longitudinal direction by a factor of 2, the o.p. drops from 0.41 to 0.25, leading to rejection of the cell (see § 3.5.3).

3.6. Comparisons with Simulations

3.6.1. Estimating Magnetic Field Strength from the Degree of Field Disorder

Better constraints on magnetic field strengths in molecular clouds are needed in order to constrain theories of star formation (Crutcher 2004). In principle, the method of Chandrasekhar & Fermi (1953) can be used to derive the field strength from the dispersion in measured submillimeter polarization directions (Ostriker et al. 2001; Heitsch et al. 2001). In practice the effects of beam dilution complicate this issue (Heitsch et al. 2001; Houde 2004), and this problem is especially severe for SPARO due to the 4' beam size. For this reason, we instead make a direct comparison of the degree of disorder in field angle seen in our measurements with that seen in three-dimensional MHD turbulence simulations of GMCs presented by Ostriker et al. (2001), after first smoothing the latter to the coarse resolution of SPARO. We again use the order parameter (o.p.; § 3.3) to quantify the disorder in magnetic field direction.

Ostriker et al. (2001) use their numerical simulations to follow the time evolution of initially smooth, self-gravitating, isothermal gas. The initial velocity field corresponds to Komolgorov-type turbulence with Mach number equal to 14. The initial magnetic field is uniform, but three models are considered with three different field strengths corresponding to $\beta = 1, 0.1, \text{and} 0.01$, where $\beta = c_s^2/v_A^2$, $c_s$ is the sound velocity, and $v_A$ is the Alfvén velocity. During the evolution, the turbulence decays and the Mach number drops. Snapshots of density, velocity, and magnetic field structure are shown for various Mach numbers.

Ostriker et al. (2001) give simulations of optical polarization measurements for background stars observed through their simulated clouds. It is assumed that all grains along the line of sight have equal polarization efficiency. Two such optical polarization maps are given, both corresponding to $M = 7$, with $\beta = 1$ and 0.01, respectively (Figs. 22 and 23 of Ostriker et al. 2001). The corresponding $\beta = 0.1$ map is not shown, but the authors note that it is very similar to the $\beta = 1$ case. We have obtained the $\beta = 0.1$ map from E. Ostriker (2005, private communication), and we average the o.p. values obtained from these two maps and refer to the average values as the o.p. for the “$\beta \geq 0.1$ case.”

For grains aligned by a uniform magnetic field, the degree of optical polarization is linearly proportional to column density, while the submillimeter polarization magnitude has no dependence on column density (for low optical depth). This illustrates that it is the submillimeter polarized flux rather than the submillimeter polarization magnitude that will generally be proportional to the optical polarization magnitude. Accordingly, when we bin optical polarization vectors to SPARO’s resolution, we combine them as if they were polarized flux, using the method of Stokes parameters. In principle, we should combine Stokes parameters derived from each simulation resolution element that lies within a 4' SPARO beam, but Ostriker et al. (2001) only give optical polarization vectors for a 12×12 grid of points. However, this grid is dense enough to provide many optical vectors per SPARO beam (see below) so it should be sufficient for reasonable estimates.

The length $L$ of each side of the cubical simulation box of Ostriker et al. (2001) is not well defined, but by assuming a temperature of 10 K and a mean density of 100 cm$^{-3}$, they obtain $L = 8$ pc for the $M = 7$ simulations. For NGC 6334, where our beam size is approximately 2 pc, we thus obtain 16 simulated SPARO vectors from each simulated cloud map (each vector is derived from binning nine simulated optical vectors). The resulting o.p. values are 0.97 and 0.15 for $\beta = 0.01$ and $\beta \geq 0.1$, respectively. For G333.6–0.2, we obtain only four simulated SPARO vectors (each comes from binning 36 simulated optical vectors), and we find o.p. values of 0.98 and 0.35 for the low- and high-$\beta$ cases, respectively. G331.5–0.1 is too distant for meaningful comparisons.

Our results for the Carina Nebula are not suitable for comparison with the turbulence simulations of Ostriker et al. (2001).
The reason is that these authors simulated the inertial range of the turbulence, with a Kolmogorov-type energy spectrum over the entire 8 pc simulation cube. Our observation of Carina, on the other hand, shows field structure determined by the ~10 pc scale curvature of the \textit{H} \textsc{ii} bubbles (Fig. 5), not a turbulent cascade in the inertial range. The field structure is the result of energy injection, with bubbles depositing energy directly into the field on ~10 pc scales.

The simulated turbulence maps correspond to the case in which the initial field direction is perpendicular to the line of sight, so the o.p. values we have derived from the simulations are in fact upper limits. Figure 24 of Ostriker et al. (2001) shows that the angle between the field and the line of sight has a dramatic effect on the degree of disorder in the inferred field directions.

From our maps of NGC 6334 and G333.6–0.2, we obtain o.p. values of 0.73 and 0.80, respectively, indicating that $\beta = 0.01$ is preferred over $\beta \geq 0.1$. The product of $\beta$ with the square of the Mach number gives the “turbulent beta,” $\beta_\text{t}$, which provides a direct comparison of magnetic and turbulent energy densities. We see that our comparison strongly favors $\beta_\text{t} = 0.5$ over $\beta_\text{t} \geq 5$, implying that the magnetic energy density is comparable to the turbulent energy density.

There are two main limitations to our comparison of SPARO data with simulations. First, there is a relatively small overlap between the smaller spatial scales of the simulations and the larger scales of the SPARO data. Secondly, the assumption that all grains have equal polarizing efficiency is probably wrong (Cho & Lazarian 2005). Despite these questions, it seems difficult to reconcile our observations of reasonably uniform fields with models having very weak fields.

### 3.6.2. Comparing Fields inside GMCs with Larger Scale Galactic Fields

We showed in § 3.3 that three of our four target GMCs have mean field directions, determined from SPARO data, that are within 15° of the Galactic plane. As noted, the probability for obtaining this result by pure chance is below 2%. This suggests a correlation between GMC fields and the larger scale Galactic field. NGC 6334 is the outlier in our sample of four GMCs, having its mean field rotated 70° clockwise from the plane. In § 3.5 we used the Heiles (2000) stellar polarization database to examine Galactic fields on scales roughly corresponding to the GMC accumulation length (~400 pc). We obtained mean field directions for a set of 10–11 regions, one of which is centered on the closest of our four targets, NGC 6334, while none of the other SPARO targets are close enough to obtain reliable determinations of field direction from the Heiles database. Within this sample of 10–11 regions, we again find a tendency for the “accumulation-scale field” to be parallel to the Galactic plane (Figs. 9 and 10), and we find that NGC 6334 is again an outlier in the distribution, having its accumulation-scale field more aligned with the Galactic latitude direction than with the Galactic longitude direction. We can explain both the tendency for fields in GMCs to align with the Galactic plane and also the agreement of the field direction in NGC 6334 with the direction of the Galactic field local to NGC 6334 by supposing that fields in GMCs are generally parallel to the local Galactic fields.

Is this effect seen in simulations of GMC formation? MHD simulations of the process whereby gas uniformly spread through a galactic disk becomes concentrated into GMCs via self-gravitating instabilities have been carried out, for example, by Kim & Ostriker (2001) and Kim et al. (2003). The work by Kim & Ostriker (2001) included only two dimensions (thin disk limit), and the particular instabilities that they studied for the Galactic disk (as opposed to the Galactic center) took too long to develop. They were thus judged to be unlikely candidates for GMC formation unless they could be enhanced by additional agents. Nevertheless, for purposes of comparison with our observations we note that their model M23 (Fig. 13 of their paper) shows continuity and alignment between fields inside dense clouds and those in the lower density surrounding medium, while their model M10 (Fig. 12 of their paper) shows no such correlation. The main difference is the field strength.

In principle, comparisons of such models with our results could test theories for GMC formation, but in practice such comparisons may lead to ambiguous results, for present simulations. The problem is that the simulations seem to produce only clouds having angular momentum perpendicular to the Galactic plane. For the two-dimensional simulations this is true by definition, but even in the three-dimensional simulations of Kim et al. (2003) we find that angular momentum of collapsing gas clouds is orthogonal to the plane, presumably because it is inherited from Galactic shear. In this case the predominant mode for field distortion is to shear the fields out into spiraling patterns, with the spiral lying in the Galactic plane (Fig. 12 of Kim & Ostriker 2001). Unfortunately, because SPARO sight lines extending from the Sun to disk GMCs are parallel to the plane, the in-plane spiral field distortion patterns described above will be indistinguishable from the case of continuous, ordered fields extending into GMCs with no or little change in direction.

Could the correlation we observed between GMC fields and local Galactic fields be merely a consequence of field twisting induced by clouds rotating preferentially about axes orthogonal to the Galactic plane? While we cannot rule this out, it is worth noting that observations of GMCs in M33 (Rosolowsky et al. 2003) have failed to find a strong tendency for cloud rotational axes to be perpendicular to the disk of this spiral galaxy. Thus, it seems that the more likely explanation for the correlations we have discovered is that Galactic fields do indeed pass into GMCs with little change in direction. When more realistic MHD simulations are available that better match the recent observational data on cloud rotation axes, it will be interesting to compare them with our observations of magnetic field structure.

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**REFERENCES**

Allamandola, L. J., Hudgins, D. M., & Sandford, S. A. 1999, ApJ, 511, L115
Amari, L. H., & Abraham, Z. 1991, A&A, 251, 259
Arce, H. G., Goodman, A. A., Bastien, P., Manset, N., & Sumner, M. 1998, ApJ, 499, L93
Becklin, E. E., Frogel, J. A., Neugebauer, G., Persson, S. E., & Wynn-Williams, C. G. 1973, ApJ, 182, 125
Benolken, A., et al. 2004, A&A, 424, 571
Bronfman, L., Alvarez, H., Cohen, R. S., & Thaddeus, P. 1989, ApJS, 71, 481
Bronfman, L., Nyman, L. A., & May, J. 1996, A&A, 115, 81
Brooks, K. J., Storey, J. W. V., & Whiteoak, J. B. 2001, MNRAS, 327, 46
Carraro, G., Romaniello, M., Ventura, P., & Patat, F. 2004, A&A, 418, 525
Caswell, J. L., & Haynes, R. F. 1987, A&A, 171, 261
Chandrasekhar, S., & Fermi, E. 1953, ApJ, 118, 113
Cheung, L. H., Frogel, J. A., Hauser, M. G., & Gezari, D. Y. 1980, ApJ, 240, 74
Cho, J., & Lazarian, A. 2005, ApJ, 631, 361
Chauss, D. T. 2002, Ph.D. thesis, Northwestern Univ.
Colgan, S. W. J., Haas, M. R., Erickson, E. F., Rubin, R. H., Simpson, J. P., & Russell, R. W. 1993, ApJ, 413, 237
