Ultra-wideband Mitigation of Differential to Common Mode Conversion for Bended Differential Lines by Periodic Interdigital Structure

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Abstract—In this paper, a periodic interdigital structure for wideband mitigation of differential-to-common mode conversion at the bend discontinuity of differential lines is proposed. A hybrid inductance and capacitance compensation property is exhibited to suppress the common-mode noise of asymmetric transmission lines. An equivalent circuit model is given to explain the working principle of the presented periodic interdigital structure for differential pairs. In comparison with the traditional methods, steep and wideband suppression performances are both observed with the proposed design. Moreover, no additional area is required at the bend discontinuity for compensation. From the measured result, the differential-to-common mode conversion of the differential signals can be mitigated from DC to 10 GHz with a rejection level of $-20$ dB. The measurements agree well with the simulation predictions.

1. INTRODUCTION

Differential signals with its inherent characteristics of low crosstalk and high immunity to noise are widely employed in the high speed circuits [1]. However, due to the amplitude and phase unbalance of the asymmetric differential lines, especially at the corner of the bend differential signal, differential to common mode conversion noise is generated to deteriorate the integrity of the signal trace. Therefore, it is imperative to investigate the measures to compensate the bend discontinuity of the differential lines [2, 3].

In recent years, various techniques have been proposed to suppress the converted differential to common mode noise of the bend differential signals. Slow-wave structure is employed to compensate the phase difference between the inner and outer lines of the differential signals [4, 5]. In [6], the inductance compensation method is proposed to suppress the converted differential to common noise. In [7], a novel compensation scheme by using shunt capacitance is presented to minimize the time delay of the unbalanced differential lines. In [8], a curved compact PBG is proposed to mitigate differential-to-common mode conversion noise. However, the bandwidth for suppressing the converted noise is relatively narrow and extra spaces are required to design the noise filtering structure.

In this letter, a periodic interdigital structure is proposed to suppress the differential-to-common mode conversion at the bend discontinuity of the differential lines. An equivalent circuit model is built to explain the hybrid inductance and capacitance compensation behavior of the presented structure. No additional space is occupied for the differential lines. The converted noise suppression of proposed structure is maintained under $-20$ dB from DC to 10 GHz.
2. STRUCTURE DESIGN AND ANALYSIS

Figure 1 shows the schematic of the proposed compensated structure for the differential signals. Owing to the asymmetric structure at the corner of the bend differential signals, a phase imbalance is observed between the two differential lines. Periodic interdigital structures with large shunt capacitance are loaded on the inner line to compensate the phase difference of the bend discontinuous differential signals. Furthermore, the adjacent interdigital cells are connected by a narrow microstrip line, which can increase the inductance of the structure. Therefore, a hybrid inductance and capacitance compensation property is exhibited to suppress the common mode noise conversation of the bend differential pairs.

![Figure 1](image1.png)

**Figure 1.** The schematic of the proposed compensated structure: (a) bended differential pairs with periodic interdigital structure and (b) two adjacent interdigital cells connected with a narrow microstrip line.

From Fig. 1(a), the geometric parameters of the proposed compensate structure are described, where \( w \) is the width of the differential line, \( c \) the length of the chamfer of the differential line, and \( s \) the gap between the inner and outer lines. \( l_1 \) and \( l_2 \) are the lengths of input and output ports, and \( l_3 \) is the length of the differential line. Fig. 1(b) shows the structure notations between the two adjacent interdigital cells. \( s_{pi} \) and \( b_{pi} \) are the length and width of the narrow microstrip line, respectively. \( w_{pi} \) is the width of the interdigital structure unit. \( b_{pi2} \) and \( b_{pi3} \) are the widths of the two coupling lines of the interdigital structure, respectively. \( g_{pi1} \) and \( g_{pi2} \) are the gap sizes of the interdigital structure at different positions, respectively.

Furthermore, in order to interpret the mechanism of the presented periodic interdigital structure in detail, a simplified equivalent circuit model between the two adjacent interdigital cells is built in Fig. 2. A hybrid inductance and capacitance characteristic is exhibited. \( C_{p1} \) and \( L_1 \) stand for the capacitance and inductance of the coplanar waveguide (CPW) in the interdigital structure, respectively. \( C_g \) is the coupling capacitance of the interdigital structures. \( C_{pi2} \) and \( L_2 \) are the capacitance and inductance of the narrow microstrip line between the two adjacent interdigital capacitor.

![Figure 2](image2.png)

**Figure 2.** Simplified equivalent circuit of the two interdigital structures connected with a narrow microstrip line.
The capacitance $C_{\pi i}$ and inductance $L_i$ are calculated as [9]:

\[ C_{\pi i} = \varepsilon_r \varepsilon_0 \frac{S_i}{h} \]  
\[ L_i = l_i L_{\text{pul}} \]

where $i$ is equal to 1 and 2, respectively. $S_i$ and $l_i$ are the area and length of the microstrip line, respectively. $\varepsilon_r$ and $\varepsilon_0$ are the permittivity of the substrate and free space, respectively. $L_{\text{pul}}$ is the inductance of the CPW per unit length and can be calculated by:

\[ L_{\text{pul}} = Z_{\text{CWP}} \sqrt{\varepsilon_{\text{eff}} c} / c \]

where $\varepsilon_{\text{eff}}$ and $Z_{\text{CWP}}$ are the effective dielectric constant and impedance of the CPW, respectively.

The gap capacitance $C_g$ of the interdigital structure can be derived by:

\[ C_g = 3 \frac{\varepsilon_0 (1 + \varepsilon_r) b_{\pi 2}}{\pi} \cosh^{-1} \left( \frac{2b_{\pi 2} + g_{\pi 2}}{g_{\pi 2}} \right) + \frac{\varepsilon_0 (1 + \varepsilon_r) (b_{\pi 1} + b_{\pi 2})}{2} \cosh^{-1} \left( \frac{b_{\pi 1} + b_{\pi 2} + g_{\pi 2}}{g_{\pi 2}} \right) + 4 \frac{\varepsilon_0 (1 + \varepsilon_r) (w_{\pi i} - g_{\pi 1})}{\pi} \cosh^{-1} \left( \frac{w_{\pi i}}{g_{\pi 1}} \right) \]

From above analysis, it can be observed that the internal coupling capacitance $C_g$ of the periodic interdigital structure and the inductance $L_2$ of the narrow microstrip line have a great effect on the compensation capacitance and inductance of the bend differential line.

In order to evaluate the propagation characteristics of the proposed compensated structure for the differential signals, various EM computation methods are presented to calculate the scattering performances [10, 11]. As shown in Fig. 3(a), the influence of the number of the periodic interdigital cells on the differential to common mode conversion noise suppression performance is analyzed. With the increase of the number of the interdigital cells, the capacitance is enlarged to compensate the phase difference of the discontinuity of the bend differential lines. It is obviously found that the conversion noise can be prohibited greatly with increasing number of interdigital structures.

Furthermore, the inductance of the narrow microstrip line between the adjacent interdigital cells also has an effect on the differential to common mode conversion noise mitigation. From Fig. 3(b), the noise suppression depth becomes deeper with the increase of $s_{\pi i}$, which can increase the compensated inductance of the bend differential lines. By employing the periodic interdigital cells, a hybrid inductance and capacitance characteristic is introduced to compensate the phase imbalance of the bend discontinuity of the differential lines. The differential to common mode conversation noise is suppressed sufficiently.
Moreover, the influences of the frequency dependent parameters of the dielectric on the scattering parameters of the proposed differential signal lines structure are analyzed. From Fig. 4(a), with decrease of the effective relativity of the substrate, the upper cutoff frequency of the differential-to-common mode noise conversion is increased, and the bandwidth is enlarged correspondingly. Furthermore, the loss tangent, one of the typical frequency depended parameters, also has a significant impact on the transmission performances. As can be seen from Fig. 4(b), if the loss tangent of the dielectric is increased, the attenuation level of the differential-to-common mode noise conversion at high frequency is steepened.

Based on the aforementioned analysis, the design procedure of the presented compensated structure can be summarized as follows: Firstly, the compensated capacitance and inductance can be calculated with the phase difference between the inner and outer lines at the bend discontinuity. Secondly, the number of the periodic interdigital cells can be determined with the noise suppression performance. Then, the initial parameters of the interdigital structure and the narrow microstrip line can be derived with the compensated capacitance and inductance. Finally, the specific sizes of the proposed structure is optimized with the EM simulator according to the designed predictions.

3. SIMULATION PREDICTION AND MEASUREMENTS

In order to verify the above analysis and design, a prototype circuit sample as shown in Fig. 5 is fabricated. The bend differential line is fabricated with the standard printed circuit board technique. FR-4 material with relative permittivity of $\varepsilon_r = 4.4$ and loss tangent of $\tan \delta = 0.02$ is employed as substrate. The thickness of the substrate and copper are $h = 1.6\, \text{mm}$ and $t = 0.035\, \text{mm}$, respectively. By using full wave EM simulator Ansys HFSS, the final structure parameters are optimized as: $b_{pi1} = 0.15\, \text{mm}$, $b_{pi2} = 0.212\, \text{mm}$, $b_{pi3} = 0.5\, \text{mm}$, $g_{pi1} = 0.2\, \text{mm}$, $g_{pi2} = 0.15\, \text{mm}$, $g_{pi3} = 0.8\, \text{mm}$, $w = 1.75\, \text{mm}$, $s = 0.75\, \text{mm}$, $s_{pi} = 0.5\, \text{mm}$, $l_1 = 8.25\, \text{mm}$, $l_2 = 10\, \text{mm}$, $l_3 = 16\, \text{mm}$, and $c = 1\, \text{mm}$. The scattering properties of the proposed structure are measured by the VNA Keysight N5227B.

Figure 6 shows the measured differential-to-common mode conversion result of the proposed compensation structure associated with the simulation prediction. Moreover, the scattering parameter of the uncompensated bend differential is also listed for comparison. As can be seen from the figure, the differential-to-common mode conversion can be reduced from DC to 10 GHz with a suppression level of $-20\, \text{dB}$. In comparison with the uncompensated structure, the converted common-mode noise can be mitigated efficiently. The measured result agrees well with the simulated one. Small discrepancy is
observed with the error in the manufacturing process and the welding of the SMA joint.

Furthermore, the differential-to-common-mode conversion results for different compensation structures of bend differential line are listed in Table 1 for comparison. It can be seen from the table that compared with the traditional compensated structure, good performances of wideband and steep suppression level are both observed with the proposed structure. Moreover, no additional area is required for the bend differential lines.

Table 1. Comparison with previous works using the compensation structure in internal line.

|       | Size ($\lambda_0 \times \lambda_0$) | Rejection level (dB) | Rejection bandwidth (GHz) | Occupy area |
|-------|-------------------------------------|----------------------|---------------------------|-------------|
| [4]   | N/A                                 | −20                  | DC-10                     | Occupy      |
| [6]   | 0.5 × 0.5                           | −16.67               | DC-6                      | Occupy      |
| [7]   | N/A                                 | −15                  | DC-4                      | Occupy      |
| Proposed | 0.83 × 0.83                     | −20                  | DC-10                     | No occupy   |

$\lambda_0$ is the wavelength at the center frequency of suppression bandwidth.

4. CONCLUSION

In this paper, a periodic interdigital structure is presented to suppress the differential to common mode conversion noise at the bend discontinuity of differential lines. An equivalent circuit model is built to explain the mechanism of the structure. In comparison with the uncompensated bend differential lines, a wideband and steep suppression of differential to common mode conversion noise is obtained with the proposed structure. Moreover, no additional occupying area is required for the bend differential line, which can be more useful for the multi-channel and miniaturized circuit system.

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