Why did Supernova 1054 shine at late times?

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Abstract. The Crab nebula is the remnant of supernova 1054 (SN 1054). The progenitor of this supernova has, based on nucleosynthesis arguments, been modeled as an 8 – 10 M⊙ star. Here we point out that the observations of the late light curve of SN 1054, from the historical records, are not compatible with the standard scenario, in which the late time emission is powered by the radioactive decay of small amounts of 56Ni. Based on model calculations we quantify this discrepancy. The rather large mass of 56Ni needed to power the late time emission, 0.06±0.02 M⊙, seems inconsistent with abundances in the Crab nebula. The late light curve may well have been powered by the pulsar, which would make SN 1054 unique in this respect. Alternatively, the late light curve could have been powered by circumstellar interaction, in accordance with scenarios in which 8 – 10 M⊙ stars are progenitors to ‘dense wind’ supernovae.

Key words: supernovae: general – supernovae: SN 1054

1. Introduction

The Crab nebula is among the best studied objects in the sky. Still, the nature of the progenitor star and many aspects of the explosion remain unclear. The ancient observations of SN 1054, conducted by astronomers in China and Japan, have been analyzed by Clark & Stephenson (1977). They conclude that SN 1054 was observable in daytime for 23 days and during night for some 650 days past explosion. Great attention has been directed to understand this light curve in terms of supernova theory (Minkowski 1971; Clark & Stephenson 1977; Chevalier 1977; Pskovskii 1977; Wheeler 1978; Collins, Clapsy, & Martin 1999, and references therein).

It is now widely accepted that SN 1054 was a core-collapse supernova, primarily due to the presence of the pulsar. That SN 1054 would have been a Type Ia supernova (SN Ia), an old suggestion that was recently aired by Collins et al. (1999), is clearly in conflict also with the large amount of mass in the filaments, and in particular with its hydrogen-rich composition. However, the idea that SN 1054 was a normal Type II supernova (SN II), as was first suggested by Chevalier (1977), is not unproblematic. The Crab filaments contain only 4.6 ± 1.8 M⊙ of material (Fesen, Shull, & Hurford 1997) and cruise at merely ~1400 km s⁻¹ (Woltjer 1972), which give a kinetic energy an order of magnitude less than the canonical value for core-collapse supernovae, 10⁵⁵ ergs. Some of this energy may also originate from the pulsar (Chevalier 1977). As the early observations of SN 1054 indicate a rather luminous explosion, Chevalier (1977) suggested that the missing mass and energy of the Crab resides in a hitherto undetected outer shell. That some material indeed exists outside the visible filaments was recently shown using HST observations (Sollerman et al. 2000).

Nomoto et al. (1982) constructed a detailed model for the progenitor of SN 1054. They argued that the progenitor must have been more massive than 8 M⊙ in order to leave a neutron star and less massive than ~10 M⊙ to be consistent with the observed metal abundances. An 8 – 10 M⊙ star would eject very little heavy elements (Nomoto et al. 1982). In particular, it would eject very small amounts of radioactive 56Ni, responsible for the late time emission of the supernova (Mayle & Wilson 1988). In this report we want to draw the attention to the long duration of the light curve of SN 1054, and point out that this cannot be explained within the standard supernova scenario, in which the powering of the emission at these late phases is due to radioactive decay of a very low mass of 56Ni.

2. Discussion

2.1. Supernova Light Curves

The early light curves of SNe II are powered by the explosion energy slowly diffusing out of the ejecta. The large diversity of light curve shapes in this phase (Patat et al. 1994) is largely due to variations in progenitor radius, envelope mass and composition, as well as in the explosion energy itself. At later phases (≥150 days), the light
curves of SNe II are often powered by the radioactive decay of $^{56}{\text{Co}} \rightarrow ^{56}{\text{Fe}}$, and then the late evolution is quite uniform (Patat et al. 1994). The $^{56}{\text{Co}}$ is itself the decay product of $^{56}{\text{Ni}}$, synthesized in the supernova explosion. The late light curve of the well studied SN 1987A was reproduced by models with 0.07 $M_\odot$ of $^{56}{\text{Ni}}$ (Kozma & Fransson 1998a,b), and most SNe II light curves do follow the decay rate of $^{56}{\text{Co}}$ (Barbon et al. 1984; Patat et al. 1994). In fact, the luminosity on the light curve tail can be used to determine the mass of ejected $^{56}{\text{Ni}}$, as has been done for several supernovae (see Sollerman, Cumming, & Lundqvist 1998, and references therein).

The radioactive energy from the decay of $^{56}{\text{Co}}$ is deposited in the supernova ejecta as $\gamma$-rays and positrons. The luminosity on the light curve tail from the $\gamma$-rays is given by $L_\gamma = \gamma F_\gamma M_{\text{Ni}} e^{-t/\tau_{\text{56Ni}}}$ ergs s$^{-1}$, where $F_\gamma$ is the fraction of the $\gamma$-rays trapped in the ejecta, $M_{\text{Ni}}$ is the amount of $^{56}{\text{Ni}}$ in solar masses, and 111.3 days is the e-folding time for the decay of $^{56}{\text{Co}}$. The positrons contribute $L_{\text{e}^-} = 4.45 \times 10^{41} M_{\text{Ni}} e^{-t/\tau_{\text{56Ni}}}$ ergs s$^{-1}$, assuming they are all deposited locally.

To determine the nickel mass from the observed filter light curves, the $\gamma$-ray trapping and the bolometric evolution have to be taken into account. In Figure 1 we use SN 1987A to illustrate these concepts. There we plot the bolometric light curve of SN 1987A (triangles) from Bouchet & Danziger (1993). The upper dashed line is given by the expressions above for a nickel mass of 0.07 $M_\odot$ (Suntzeff & Bouchet 1990) assuming full trapping of the $\gamma$-rays ($F_\gamma$=1). This line fits the light curve tail at epochs up to ~300 days, but later the observed luminosity falls below the luminosity expected for full trapping, due to an increasing leakage of $\gamma$-rays.

The $\gamma$-leakage can be illustrated using a simple model with a central radioactive source, where the deposition $F_\gamma = (1 - e^{-\frac{t}{\tau}})$, and the $\gamma$-ray optical depth evolves as $\tau = (t/t_1)^{-2}$ due to the homologous expansion. Here $t_1$ is the time when $\tau=1$. For SN 1987A, $t_1 \sim 610$ days gives a reasonable agreement with the bolometric magnitudes as shown by the dotted curve in Figure 1. This means that ~60% of the $\gamma$-rays were trapped at 650 days for SN 1987A.

Also plotted in Figure 1 is the $V$-band light curve of SN 1987A (square symbols, Suntzeff & Bouchet 1990). It can be seen that this filter light curve deviates substantially from the bolometric light curve after about 500 days. At these late phases, the ejecta temperature is low and most of the light is instead emitted in the infrared (Kozma & Fransson 1998a,b).

\subsection*{2.2. The late time luminosity of SN 1054}

The Crab is located at a distance of about 2.0 kpc (Trimble 1973) with an extinction of $E(B-V) = 0.52$ (Sollerman et al. 2000). From the historical records analyzed by Clark & Stephenson (1977) we know that SN 1054 faded from visibility some 650 days after discovery. The detection limit for night time observations was estimated to be 5.5 mag by these authors (Clark & Stephenson 1977). SN 1054 must thus have had an absolute $V$ (actually visual) magnitude of $M_V = -7.6$ at this epoch. In Figure 1 we have indicated this limit together with an error bar that encapsulates distances in the range 1500 – 2200 pc (Davidson & Fesen 1985), and an error of $\pm 0.04$ in $E(B-V)$. As a detection limit of 5.5 magnitudes may be regarded too high, we encapsulate it with conservative limits of 5.5$^{+0.7}_{-0.3}$. This is also included in the error bar in Figure 1.

The Crab progenitor has been modeled as an 8–10 $M_\odot$ star (Nomoto et al. 1982). The amount of $^{56}{\text{Ni}}$ ejected in such an explosion is supposed to be very small. Detailed calculations performed by Mayle & Wilson (1988) indicate that no more than 0.002 $M_\odot$ of $^{56}{\text{Ni}}$ should be ejected from supernovae with progenitors in this mass range.
The $^{56}\text{Ni}$ eventually decays to $^{56}\text{Fe}$ and thus the current amount of iron probes the mass of ejected nickel. Abundance analyses in the Crab are nontrivial, but indicate a subsolar iron abundance (Davidson 1978, 1979; Henry 1984; Bautista et al. 1996). For an ejecta mass of $4.6 M_\odot$, solar abundance corresponds to 0.006 $M_\odot$ of iron. This is consistent with a low mass of ejected nickel, as suggested by the explosion models of Mayle & Wilson (1988).

Here we simply want to point out that the naked eye observations of SN 1054 at 650 days seem to be inconsistent with the standard scenario where supernovae from $8-10 M_\odot$ stars are powered at late times by the radioactive decay of very small amounts of $^{56}\text{Ni}$.

Even assuming full trapping and that all of the emitted flux emerges in the visual band, $(F_\lambda=1, M_V=M_{bol})$, just barely keeps the supernova shining at 650 days past explosion. The lower dashed line labeled ‘0.006’ in Figure 1 shows a full trapping, bolometric case for this amount of ejected $^{56}\text{Ni}$, and is fairly close to the lower limit of the luminosity needed for naked eye visibility of the supernova at 650 days.

This discrepancy is of course much more pronounced in the more realistic case when the conservative assumptions above are relaxed. For example, assuming that SN 1054 had the same $\gamma$-ray leakage and bolometric correction as SN 1987A, $\sim 0.05 M_\odot$ of $^{56}\text{Ni}$ would be required to reach $M_V = -7.6$.

### 2.3. Modeling

Clearly, it is too simplistic to directly compare SN 1054 with SN 1987A. To quantify the discrepancy mentioned above, we have therefore modeled SN 1054 in some detail. Lacking an explosion model, we base our input model on the available observations. We have adopted an ejecta mass of $4.6 M_\odot$ (Fesen et al. 1997) and a maximum velocity of 2300 km s$^{-1}$ (Clark et al. 1983; Davidson & Fesen 1985). We assume that the density and composition are constant throughout the ejecta. We use solar abundances from Cameron (1982) except for helium, for which we use a ratio of the mass fractions of helium and hydrogen, $X(\text{He})/X(\text{H})=2$ (e.g., Henry 1986).

A central source of radioactive $^{56}\text{Ni}$ is assumed. Calculations have been done for 0.006 $M_\odot$, 0.04 $M_\odot$ and 0.07 $M_\odot$ of $^{56}\text{Ni}$. The emission from SN 1054 is modeled in detail from 200 to 800 days. The code is fully described in Kozma & Fransson (1998a,b). In the decay of $^{56}\text{Co}$, $\gamma$-rays and positrons are emitted, and the thermalization of these is calculated using the Spencer-Fano formalism (Kozma & Fransson 1992). This time-dependent code successfully reproduces the detailed late time observations of SN 1987A (Kozma 2000).

With this model, we estimate that only 32% of the $\gamma$-rays were trapped at 650 days for SN 1054. The low trapping is of course due to the low mass of the ejecta, as compared to SN 1987A. In Figure 2 we plot the light curves for the SN 1054 model for two different amounts of ejected $^{56}\text{Ni}$. At 650 days, a smaller amount of the luminosity comes out in the V-band for the lower nickel-mass model. This is because low amounts of nickel means less heating, and as the temperature of the ejecta decreases the emission is pushed further into the infrared.

From Figure 2 we directly see that 0.006 $M_\odot$ of $^{56}\text{Ni}$ could not have provided the observed luminosity at 650 days. Instead, the model with 0.07 $M_\odot$ of $^{56}\text{Ni}$ (similar to the mass ejected in SN 1987A), comes close to a V-magnitude of 5.5 at day 650. Within the framework of this model, a mass of $^{56}\text{Ni}$ of 0.06$^{+0.02}_{-0.03} M_\odot$ was required to power the supernova light curve when it faded from night time visibility. This includes the errors estimated above for distance, reddening and naked eye-sensitivity. We have done the same calculations also for a filter similar to the eye sensitivity (Rhodopsin absorption curve, Kitchin 1991), but the deviation from the V-filter is small, 0.07 mag for the model with 0.07 $M_\odot$ of $^{56}\text{Ni}$ at 650 days. Finally, although according to Clark & Stephenson (1977) there is no reason to question the dates of the Chinese sightings, an error of $\pm20$ days in duration would introduce a 30% error in flux. We note that suggestions for alternative durations, although often based on less direct sources (e.g., Pskovskii 1977; Collins et al. 1999), usually argue for longer visibility of SN 1054, thus enhancing the problem of keeping it shining at late times.

### 3. Powering scenarios

#### 3.1. Radioactive decay

If radioactivity alone powered the late time emission, the required mass of $^{56}\text{Ni}$ estimated above, 0.06$^{+0.02}_{-0.03} M_\odot$, is significantly higher than that obtained in the explosion.

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**Fig. 2.** Absolute V-band light curves for the Crab model. The upper curve is for 0.07 $M_\odot$ of $^{56}\text{Ni}$, while the lower curve is for 0.006 $M_\odot$ of $^{56}\text{Ni}$. The detection limit is the same as in Fig. 1.
models by Mayle & Wilson (1988), 0.002 M⊙. Although
the unknown mechanism of core-collapse explosions makes
the existing explosion models rather uncertain, including
the exact amount of nickel mass, there are other reasons
to believe that low mass SNe eject very small amounts of
56Ni. Galactic chemical evolution models imply that the
amount of iron produced by SNe II is already quite high,
and Samland (1998) even suggested that the lower mass
limit of stars producing iron should be 11–12 M⊙, instead
of the conventional 10 M⊙.

Nevertheless, the above arguments cannot conclusively
argue that SN 1054 did not eject the 0.06 M⊙ of 56Ni
required to maintain the late time luminosity. We there-
fore turn the attention to the measured abundances in the
Crab nebula.

Actually, only helium is enhanced in this supernova
remnant, while the abundances of C, N, O and Fe seem
to be (sub)solar (Davidson & Fesen 1985). In §2.2 we saw
that solar abundance of iron for 4.6 M⊙ ejecta corresponds
to 0.006 M⊙. The amount of 56Ni required to power the
late time light curve, 0.06±0.02 M⊙, would thus correspond
to a present iron abundance which is 9±1 times higher than
solar abundance.

If radioactivity powered the supernova, the iron must
be locked up in dust. Dust is clearly present in the nebula,
and it is nontrivial to determine the dust mass (Sankrit
et al. 1998), although estimates seem to indicate that the
dust mass is low (Davidson & Fesen 1983). Note that this
scenario would also require large amounts of other met-
als to be locked up in dust. As the iron-group elements
are produced in the very center of the exploding star,
we do not expect to find a large amount of iron, while
the CNO-abundance has not been enhanced. For example,
SN 1987A, which ejected 0.07 M⊙ of 56Ni, also ejected
almost 2 solar masses of oxygen. Even the 11 M⊙ model of
Woosley & Weaver (1995), which ejects 0.07 M⊙ of 56Ni,
and only 0.136 M⊙ of oxygen, provides an oxygen abun-
dance higher than solar. We believe that the scenario in
which SN 1054 was powered by 0.06 M⊙ of 56Ni, but where
all the nucleosynthesized metals are presently locked up in
dust, is not very convincing. We therefore briefly turn our
attention to alternative scenarios.

3.2. The Pulsar

If radioactivity did not power SN 1054 at late times, the
obvious candidate is the pulsar that powers the nebula
today. Already Chevalier (1977) suggested that the pulsar
could contribute to the late time supernova light curve.
In fact, unless the bulk of the iron is locked up in dust,
and circumstellar interaction was unimportant (see §3.3),
the pulsar would have to make up for all of the late time
luminosity, as 0.006 M⊙ of 56Ni could not have kept the
SN visible for more than ~ 500 days (Fig. 2).

There are many ways in which a pulsar can contribute
to the optical luminosity of a supernova. Accretion onto
the neutron star could be either spherical or in a disk, de-
pending on the angular momentum of the infalling matter.
A steady spherical accretion is supposed to reach a maxi-
mum Eddington luminosity of $L_{\text{Edd}} = 3.5 \times 10^{38}$ ergs s⁻¹,
and Chevalier (1989) suggested that this scenario might
be responsible for the late time luminosity of SN 1054. He
worried, however, about the fact that the accretion lumi-
nosity would not be able to escape from the vicinity of the
neutron star during the first months, as the luminosity is
trapped by the inflow (see also Benetti et al. 2000). As
shown in Figure 2, this need not be a problem, as even
a low mass of ejected 56Ni is able to keep the supernova
shining for some 500 days. If the accretion is mediated via
da disk, the luminosity could perhaps be even larger than
in the spherical case.

Unknown in these scenarios is the fraction of the lu-
minosity escaping in different bands. In fact, the full Ed-
dington luminosity would have to fall in the visible band to
make SN 1054 observable at 650 days ($3.5 \times 10^{38}$ ergs s⁻¹
corresponds to $M_{\text{bol}} = -7.7$). This appears to be rather
unlikely.

Pulsar nebulae in supernovae, with special attention
to the Crab, were investigated by Chevalier & Fransson
(1992). Unfortunately, they did not address the question
highlighted here, the luminosity of SN 1054 at 650 days.
In their scenario, the pulsar powers a bubble that shocks
and ionizes the supernova ejecta, and their calculations
suggested that 1.5% of the total pulsar luminosity could
be converted to radiation. This would be too low to account
for the luminosity of SN 1054 at day 650. However, if
the pulsar bubble is a significant source of synchrotron emis-
ion (Chevalier 1996), the efficiency might be higher.
Another interesting possibility is that the pulsar was born
with a very rapid spin period (see Atoyan 1999), and thus
a very high initial spin-down luminosity.

In summary, although not investigated in detail, there
are several ways in which a pulsar could contribute to
the luminosity of supernovae. This has so far never been
unambiguously observed. If the pulsar was indeed respon-
sible for the late light curve, this would make SN 1054 a
unique case.

3.3. Circumstellar interaction

Another mechanism important for supernova light curves
is interaction with circumstellar material (CSM). Circum-
stellar interaction is responsible for the emission at late
phases for a number of supernovae, such as SNe 1979C,
1980K, 1988Z, 1993J and 1995N. Such interaction can
maintain a SN luminosity of several $10^{38}$ ergs s⁻¹ for
many years (e.g., Chugai, Danziger, & Della Valle 1995).
In this respect, we note that the Crab could fit into the
scenario of 8 – 10 M⊙ stars being progenitors to the so
called ‘dense wind’ supernovae (Chugai 1997), where the
supernova ejecta interact with a dense superwind from the
progenitor star.
The dense wind must have extended out to $\gtrsim 6 \times 10^{16}$ cm for a maximum ejecta velocity of $v_{ej} \sim 10^4$ km s$^{-1}$. This means that the wind started $\gtrsim 2(v_{ej}/v_w)$ years before the SN breakout. Here $v_w$ is the wind velocity. Comparing with the line fluxes in Chevalier & Fransson (1994), we find that the late light curve can be explained if $M/v_w$ was typically in excess of $10^{-5} M_\odot$ yr$^{-1}$/km s$^{-1}$. Here $M$ is the mass loss rate during the supernova. The swept up wind should in this case now coast freely outside the present nebula. However, no sign of ejecta, or swept up wind, moving at velocities of order $10^4$ km s$^{-1}$ has been identified (e.g., Fesen et al. 1997).

Chugai & Utrobin (1999) suggested that SN 1054 was similar to the low-energy ($\sim 4 \times 10^{50}$ erg) event SN 1997D (Turatto et al. 1998; Benetti et al. 2000), and that no fast ejecta exist. In this case, circumstellar powering of the late light curve could be more difficult as the luminosity of the circumstellar shock scales as $\propto v_{ej}^3$. Furthermore, in a low-energy explosion, the peak luminosity is more likely to be lower, and Chugai & Utrobin (1999) therefore suggested that circumstellar interaction was important for SN 1054 also at the early phase. A low-energy explosion model with a circumstellar shell was explored already by Falk & Arnett (1977), and they found a high efficiency in the conversion of shock energy to visual light during the peak, in accordance with the suggestion of Chugai & Utrobin (1999). Although there is thus no direct support for circumstellar interaction as the cause for the late emission in the Crab, it is still premature to rule out this possibility.

4. Summary

SN 1054, the creation of the Crab nebula and the Crab pulsar, is the typical example of an $8 - 10 M_\odot$ supernova. Such supernovae are expected to eject only minute amounts of $^{56}$Ni, and here we demonstrate that SN 1054 could not have been powered by such a small mass of nickel at late times. The required amount of $^{56}$Ni, $\sim 0.06 M_\odot$, is much larger than suggested by abundance analyses of the Crab, and we therefore discuss alternative solutions. The pulsar may have powered the supernova, which would make SN 1054 unique in this respect. Alternatively, the progenitor of SN 1054 could have had a dense wind and the supernova could then have been powered by circumstellar interaction.

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