Temperature-dependent magnetization dynamics of magnetic nanoparticles

A Sukhov\textsuperscript{1,2} and J Berakdar\textsuperscript{2}

\textsuperscript{1} Max-Planck-Institut für Mikrostrukturphysik, Weinberg 2, D-06120 Halle/Saale, Germany
\textsuperscript{2} Institut für Physik, Martin-Luther-Universität Halle-Wittenberg, Heinrich-Damerow-Strasse 4, 06120 Halle, Germany

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Abstract
Recent experimental and theoretical studies show that the switching behavior of magnetic nanoparticles can be controlled well by external time-dependent magnetic fields. In this work, we inspect theoretically the influence of temperature and magnetic anisotropy on the spin dynamics and switching properties of single domain magnetic nanoparticles (Stoner particles). Our theoretical tools are the Landau--Lifshitz--Gilbert equation extended to deal with finite temperatures within a Langevin framework. Physical quantities of interest are the minimum field amplitudes required for switching and the corresponding reversal times of the nanoparticle’s magnetic moment. In particular, we contrast the cases of static and time-dependent external fields and analyze the influence of damping for a uniaxial and a cubic anisotropy.

(Some figures in this article are in colour only in the electronic version)

1. Introduction

In recent years, there has been a surge of research activities focused on the spin dynamics and the switching behavior of magnetic nanoparticles \cite{1}. These studies are driven by potential applications in mass-storage media and fast magneto-electronic devices. In principle, various techniques are currently available for controlling or reversing the magnetization of a nanoparticle. To name but a few, the magnetization can be reversed by a short laser pulse \cite{2}, a spin-polarized electric current \cite{3,4} or an alternating magnetic field \cite{5–13}. Recently \cite{6}, it has been shown for a uniaxial anisotropy that the utilization of a weak time-dependent magnetic field achieves a magnetization reversal faster than in the case of a static magnetic field. For this case \cite{6}, however, the influence of the temperature and the different types of anisotropy on the various dependences of the reversal process have not been addressed. These issues, which are the topic of this present work, are of great importance since, e.g. thermal activation affects decisively the stability of the magnetization, in particular when approaching the superparamagnetic limit, which restricts the density of data storage \cite{14}. Here we study the possibility of fast switching at finite temperature with weak external fields. We consider magnetic nanoparticles with an appropriate size as to display a long-range magnetic order and to be in a single domain remanent state (Stoner particles). Uniaxial and cubic anisotropies are considered and shown to decisively influence the switching dynamics. Numerical results are presented and analyzed for iron–platinum nanoparticles. In principle, the inclusion of finite temperatures in spin dynamics studies is well established (cf \cite{19,20,23,15,16,1} and references therein) and will be followed here by treating finite temperatures on the level of Langevin dynamics. For the analysis of switching behavior the Stoner and Wohlfarth model (SW) \cite{17} is often employed. SW investigated the energetically metastable and stable positions of the magnetization of a single domain particle with uniaxial anisotropy in the presence of an external magnetic field. They showed that the minimum static magnetic field (generally referred to as the Stoner–Wohlfarth (SW) field or limit) needed to coherently reverse the magnetization is dependent on the direction of the applied field with respect to the easy axis. This dependence is described by the so-called Stoner–Wohlfarth astroid. The SW findings rely, however, on a static model at zero temperature. Application of a time-dependent magnetic field reduces the required minimum switching field amplitude below the SW limit \cite{6}. It was, however, not yet clear how finite temperatures will affect these findings. To clarify this point, we utilize an extension of the Landau–Lifshitz–Gilbert equation \cite{18} including finite
temperatures on the level of Langevin dynamics [19, 20, 23]. Our analysis shows the reversal time to be strongly dependent on the damping, the temperature and the type of anisotropy. These dependencies are also exhibited to a lesser extent by the critical reversal fields. The paper is organized as follows: section 2 presents details of the numerical scheme and the notations whereas section 3 shows numerical results and analysis for Fe$_{80}$Pt$_{30}$ and Fe$_{70}$Pt$_{30}$ nanoparticles. We then conclude with a brief summary.

2. Theoretical model

In what follows we focus on systems with large spins such that their magnetic dynamics can be described by the classical motion of a unit vector $\mathbf{S}$ directed along the particle’s magnetization $\mathbf{\mu}$, i.e. $\mathbf{S} = \mathbf{\mu}/\mu_S$ and $\mu_S$ is the particle’s magnetic moment at saturation. The energetics of the system is given by

$$\mathcal{H} = \mathcal{H}_A + \mathcal{H}_F$$

(1)

where $\mathcal{H}_A$ ($\mathcal{H}_F$) stands for the anisotropy (Zeeman energy) contribution. Furthermore, the anisotropy contribution is expressed as $\mathcal{H}_A = -D f(S)$, with $D$ being the anisotropy constant. The explicit form of $f(S)$ is provided below. The magnetization dynamics, i.e. the equation of motion for $S$, is governed by the Landau–Lifshitz–Gilbert (LLG) equation [18]

$$\frac{\partial \mathbf{S}}{\partial t} = -\frac{\gamma}{(1 + \alpha^2)} \mathbf{S} \times \left[ B_\alpha(t) + \alpha (\mathbf{S} \times B_\alpha(t)) \right].$$

(2)

Here we introduced the effective field $B_\alpha(t) = -(1/\mu_S)\partial \mathcal{H}/\partial \mathbf{S}$, which contains the external magnetic field and the maximum anisotropy field for the uniaxial anisotropy $B_\alpha = 2D/\mu_S$. $\gamma$ is the gyromagnetic ratio and $\alpha$ is the Gilbert damping parameter. The temperature fluctuations will be described on the level of the Langevin dynamics [19]. This means that a time-dependent thermal noise $\xi(t)$ adds to the effective field $B_\alpha(t)$ [19]. $\xi(t)$ is a Gaussian distributed white noise with zero mean and vanishing time correlator

$$\langle \xi(t')\xi(t) \rangle = \frac{2\alpha k_B T}{\mu_S \gamma} \delta_{i,j} \delta(t - t').$$

(3)

$i, j$ are Cartesian components, $T$ is the temperature and $k_B$ is the Boltzmann constant. It is convenient to express the LLG in the reduced units

$$b = \frac{B_e}{B_\alpha}, \quad \tau = \omega_\alpha t, \quad \omega_\alpha = \gamma B_\alpha.$$  

(4)

The LLG equation reads then

$$\frac{\partial \mathbf{S}}{\partial \tau} = -\frac{1}{(1 + \alpha^2)} \mathbf{S} \times \left[ b(\tau) + \alpha (\mathbf{S} \times b(\tau)) \right].$$

(5)

where the effective field is now given explicitly by

$$b(\tau) = -\frac{1}{\mu_S B_\alpha} \frac{\partial \mathcal{H}}{\partial \mathbf{S}} + \Theta(\tau)$$

(6)

with

$$\langle \Theta_i(\tau')\Theta_j(\tau) \rangle = \epsilon \delta_{i,j} \delta(\tau - \tau'); \quad \epsilon = \frac{2\alpha k_B T}{\mu_S B_\alpha}.$$ 

(7)

The reduced units are independent of the damping parameter $\alpha$. In the following sections we use extensively the parameter $q = \frac{k_B T}{D}$. $q$ is a measure for the thermal energy in terms of the anisotropy energy, and $d = D/(\mu_S B_\alpha)$ expresses the anisotropy constant in units of a maximum anisotropy energy for the uniaxial anisotropy and is always $1/2$. The stochastic LLG equation (5) in reduced units (4) is solved numerically using the Heun method, which converges in quadratic mean to the solution of the LLG equation when interpreted in the sense of Stratonovich [20]. For each type of anisotropy we choose the time step $\Delta \tau$ to be one-thousandth of the corresponding period of oscillations. The values of the time interval in non-reduced units for uniaxial and cubic anisotropies are $\Delta \tau_{\text{ua}} = 4.61 \times 10^{-15}$ s and $\Delta \tau_{\text{ca}} = 6.90 \times 10^{-13}$ s, respectively, thus providing us with correlation times on the femtosecond timescale. The reason for the choice of such small time intervals is given in [19], where it is argued that the spectrum of thermal-agitation forces may be considered as white up to a frequency of order $k_B T/\hbar$, with $h$ being the Planck constant. This value corresponds to $10^{-13}$ s for room temperature. The total scale of time is limited by a thousand such periods. Hence, we deal with around one million iteration steps for a switching process. Details of realization of this numerical scheme can be found in [21, 22, 20]. We note in passing that attempts have been made to obtain, under certain limitations, analytical results for finite temperature spin dynamics using the Fokker–Planck equation (cf [15, 16] and references therein). For the general case discussed here one has however to resort to fully numerical approaches.

3. Results and interpretations

We consider a magnetic nanoparticle in a single domain remanent state (Stoner-particle) with an effective anisotropy whose origin can be magnetocrystalline, magnetoelastic and surface anisotropy. We assume the nanoparticle to have a spherical form, thus neglecting the shape anisotropy contributions. In the absence of external fields, thermal fluctuations may still drive the system out of equilibrium. Hence, the stability of the system as the temperature increases becomes an important issue. The time $t$ at which the magnetization of the system overcomes the energy barrier due to the thermal activation, also called the escape time, is given by the Arrhenius law

$$t = t_0 e^{\frac{\alpha}{\gamma}},$$

(9)

where the exponent is the ratio of the anisotropy to the thermal energy. The coefficient $t_0$ may be inferred when $D \gg k_B T$ and for high damping [19] (see [25] for a critical discussion)

$$t_0 = \frac{1 + \alpha}{\alpha} \frac{\pi \mu_S}{2D} \sqrt{\frac{k_B T}{D}}.$$ 

(10)

Here we focus on two different types of iron–platinum nanoparticle: the compound Fe$_{80}$Pt$_{30}$ has a uniaxial anisotropy [26, 27], whereas the system Fe$_{70}$Pt$_{30}$ possesses
a cubic anisotropy [24]. Furthermore, the temperature dependence will be studied by varying $q$ (cf equation (8)).

For Fe$_{50}$Pt$_{50}$ the important parameters for simulations are the diameter of the nanoparticles, 6.3 nm, the strength of the anisotropy, $K_u = 6 \times 10^5$ J m$^{-3}$, the magnetic moment per particle, $\mu_p = 21518 \ \mu_B$, and the Curie temperature, \( T_c = 710 \ \text{K} \) [26, 27]. The relation between $K_u$ and $D_u$ is $D_u = K_u V_u$, where $V_u$ is the volume of Fe$_{50}$Pt$_{50}$ nanoparticles. In the calculations for Fe$_{50}$Pt$_{50}$ nanoparticles the following $q$ values were chosen: \( q_1 = 0.001, \ q_2 = 0.005 \) or \( q_3 = 0.01 \), which correspond to the real temperatures 56, 280 or 560 K, respectively (these temperatures are below the blocking temperature). The corresponding escape times are $t_q \approx 2 \times 10^{17}$ s, $t_{q_2} \approx 10^{15}$ s and $t_{q_3} \approx 7 \times 10^{13}$ s, respectively. In some cases we also show the results for an additional temperature $q_{03} = 0.0001$, with the corresponding real temperature equal to 5 K. The corresponding escape time for this is $t_{q_{03}} \approx 10^{100}$ s. These times should be compared with the measurement period, which is about $t_m \approx 5$ ns, endorsing thus the stability of the system during the measurements.

For Fe$_{70}$Pt$_{30}$ the parameters are as follows: the diameter of the nanoparticles is 2.3 nm, the strength of the anisotropy is $K_e = 8 \times 10^5$ J m$^{-3}$, the magnetic moment per particle is $\mu_p = 2000 \ \mu_B$, the Curie temperature is $T_e = 420 \ \text{K}$ [24] and $D_e = K_e V_e$ ($V_e$ is the volume). For Fe$_{70}$Pt$_{30}$ nanoparticles the values of $q$ we choose in the simulations are $q_4 = 0.01$, $q_5 = 0.03$ or $q_6 = 0.06$, which means that the temperature is respectively 0.3, 0.9 or 1.9 K. The escape times are $t_{q_4} \approx 10^{34}$ s, $t_{q_5} \approx 2 \times 10^{35}$ s and $t_{q_6} \approx 2 \times 10^{32}$ s, respectively. Here we also choose an intermediate value $q_{03} = 0.001$ and the real temperature 0.03 K, with the corresponding escape time equal to $t_{q_{03}} \approx 10^{30}$ s. The measurement period is the same, namely about 5 ns. All values of the escape times were given for $\alpha = 0.1$.

Central to this study are two issues: the critical magnetic field and the corresponding reversal time. The critical magnetic field we define as the minimum field amplitude needed to completely reverse the magnetization. The reversal time is the corresponding time for this process. In contrast, in other studies [6] the reversal time is defined as the time needed for the magnetization to switch from the initial position to the position $S_z = 0$; our reversal time is the time at which the magnetization reaches the close proximity of the antiparallel state (figure 1). The difference in the definition is important insofar as the magnetization position $S_z = 0$ at finite temperatures is not stable, so it may switch back to the initial state due to thermal fluctuations and hence the target state is never reached.

3.1. Nanoparticles having uniaxial anisotropy: Fe$_{50}$Pt$_{50}$

A Fe$_{50}$Pt$_{50}$ magnetic nanoparticle has a uniaxial anisotropy whose direction defines the $z$ direction. The magnetization direction $S$ is specified by the azimuthal angle $\phi$ and the polar angle $\theta$ with respect to $z$. In the presence of an external field $b$ applied in an arbitrarily chosen direction, the energy of the system in dimensionless units derives from

$$\tilde{H} = -d \cos^2 \theta - S \cdot b.$$  (11)

The initial state of the magnetization is chosen to be close to $S_z = +1$ and we aim at the target state $S_z = -1$.

3.1.1. Static field. For an external static magnetic field applied antiparallel to the $z$ direction ($b = -b e_z$) equation (11) becomes

$$\tilde{H} = -d \cos^2 \theta + b \cos \phi.$$  (12)

To determine the critical field magnitude needed for the magnetization reversal we proceed as follows (cf figure 1). At first, the external field is increased in small steps. When the magnetization reversal is achieved the corresponding values of the critical field versus the damping parameter $\alpha$ are plotted as shown in the inset of figure 3. The reversal times corresponding to the critical static field amplitudes of figure 3 are plotted versus damping in figure 4.

In the Stoner–Wohlfarth (static) model the mechanism of magnetization reversal is not due to damping. It is rather caused by a change of the energy profile in the presence of the field. The curves displayed on the energy surface in figure 2...
magnetization starts at \( \theta_0 = \frac{\pi}{3} \) of the magnetization. For the solution, we assume that the static field in equation (2) is applied parallel to the initial position alignment of the magnetization and the external field, the to different geometries in these systems. In contrast to our this reference differs, however, from the one given here due to different parameters for different temperatures averaged over 500 cycles. The critical static field amplitudes versus the damping parameters for different temperatures averaged over 500 cycles. The inset shows non-averaged data for \( q_1 = 0.01 \equiv 560 \) K.

mark the magnetization motion in the \( E(\theta, \phi) \) landscape. The magnetization initiates from \( \phi_0 = 0 \) and \( \theta_0 \) and ends up at \( \theta = \pi \). As can be clearly seen from the figure, reversal is only possible if the initial state is energetically higher than the target state. This ‘low damping’ reversal is, however, quite slow, which will be quantified more below. For the reversal at \( T = 0 \), the SW model predicts a minimum static field strength, namely \( b_{c1} = B / B_{K} = 1 \) (the dashed line in figure 3).

This minimum field measured with respect to the anisotropy field strength does not depend on the damping parameter \( \alpha \), provided the measuring time is infinite. For \( T > 0 \) the simulations were averaged over 500 cycles with the result shown in figure 3. The one cycle data are shown in the inset. Figure 3 evidences that with increasing temperature thermal fluctuations assist a weak magnetic field so as to reverse the magnetization. Furthermore, the required critical field is increased slightly at very large and strongly at very small damping, with the minimum critical field being at \( \alpha \approx 1.0 \). The reason for this behavior is that for low damping the second term of equation (2) is much smaller than the first one, meaning that the system exhibits a weak relaxation. In the absence of damping, higher fields are necessary to switch the magnetization. For high \( \alpha \), both terms in equation (2) become small (compared to a low damping case) leading to a stiff magnetization and hence higher fields are needed to drive the magnetization. For moderate damping, we observe a minimum of switching fields which is due to an optimal interplay between precessional and damping terms. Obviously, finite temperatures do not influence this general trend.

For the case of \( q_0 = 0 \), the Landau–Lifshitz–Gilbert equation of motion can be solved analytically in spherical coordinates. The details of the solution can be found in [20] (equations (A1)–(A8)). The final result of the solution in this reference differs, however, from the one given here due to different geometries in these systems. In contrast to our alignment of the magnetization and the external field, the static field in [20] is applied parallel to the initial position of the magnetization. For the solution, we assume that the magnetization starts at \( \theta = \theta_0 = \pi / 360 \) and arrives at \( \theta = \pi \). Note that the expression \( \theta \neq \pi / 360 \) is important only for 0 K, since the switching is not possible if the magnetization starts at \( \theta_0 = 0 \) (the vector product in equation (2) vanishes). The reversal time in the SW limit is then given by

\[
\tau_{\text{rev}} = g(\theta_0, b) \frac{1 + \alpha^2}{\alpha},
\]

where \( g \) is defined as

\[
g(\theta_0, b) = \frac{\mu_S}{2 \gamma D b^2} \left(1 + \ln \left( \frac{\sin(\theta_0)}{b - \cos \theta_0} \right) \right). \tag{14}
\]

From this relation we infer that switching is possible only if the applied field is larger than the anisotropy field and the reversal time decreases with increasing \( b \). This conclusion is independent of the Stoner–Wohlfarth model and follows directly from the solution of the LLG equation. An illustration is shown by the dashed curve in figure 4, which was a test to compare the appropriate numerical results with the analytical one. As our aim is the study of the reversal time dependence on the magnetic moment and on the anisotropy constant, we deem the logarithmic dependence in equation (14) to be weak and write

\[
g(b, \mu_S, D) \approx \frac{\mu_S}{\gamma} \frac{2D}{B^2 \mu_S^2 - 4D^2}. \tag{15}
\]

This relation indicates that an increase in the magnetic moment results in a decrease of the reversal time. The magnetic moment enters the Zeeman energy and therefore the increase in magnetic moment is very similar to an increase in the magnetic field. An increase of the reversal time with the increasing anisotropy originates from the fact that the anisotropy constant determines the height of the potential barrier. Hence, the higher the barrier, the longer it takes for the magnetization to overcome it.

For the other temperatures the corresponding reversal times (also averaged over 500 cycles) are shown in figure 4. In contrast to the case \( T = 0 \), where an appreciable dependence on damping is observed, the reversal times for finite temperatures show a weaker dependence on damping. If \( \alpha \rightarrow 0 \) only the precessional motion of the magnetization is possible and therefore \( \tau_{\text{rev}} \rightarrow \infty \). At high damping the...
system relaxes on a timescale that is much shorter than the precession time, thus giving rise to an increase in switching times. Additionally, one can clearly observe the increase of the reversal times with increasing temperatures, even though these times remain on the nanosecond timescale.

3.1.2. Alternating field. As was shown in [6, 7, 15] theoretically and in [5] experimentally, a rotating alternating field with no static field applied can also be used for the magnetization reversal. A circular polarized microwave field is applied perpendicularly to the anisotropy axis. Thus, the Hamiltonian might be written in the form of equation (11) and the applied field is

$$ b(t) = b_0 \cos \omega t \hat{e}_x + b_0 \sin \omega t \hat{e}_y, \quad (16) $$

where $b_0$ is the alternating field amplitude and $\omega$ is its frequency. For a switching of the magnetization the appropriate frequency of the applied alternating field should be chosen. In [15] analytically and in [6] numerically a detailed analysis of the optimal frequency is given which is close to the precessional frequency of the system. The role of temperature and different types of anisotropy have not yet been addressed, to our knowledge.

Figure 5 shows our calculations for the reversal process at two different temperatures. In contrast to the static case, the reversal proceeds through many oscillations on a timescale of approximately ten picoseconds. Increasing the temperature results in an increase of the reversal time.

Figure 6 shows the trajectory of the magnetization in the $E(\theta, \phi)$ space related to the case of the alternating field application. Compared with the situation depicted in figure 2, the trajectory reveals a quite delicate motion of the magnetization. It is, furthermore, noteworthy that the alternating field amplitudes needed for the reversal (cf figure 7) are substantially lower than their static counterpart, meaning that the energy profile of the system is not completely altered by the external field.

Figure 7 inspects the dependence of the minimum switching field amplitude on damping. The critical fields are obtained upon averaging over 500 cycles. The SW limit is always equal to 1 on this scale and this graph. In contrast to the static case, the critical fields increase with increasing $\alpha$. In the low damping regime the critical field is smaller than in the case of a static field. This behavior can be explained qualitatively by a resonant energy-absorption mechanism when the frequency of the applied field matches the frequency of the system. Obviously, at very low frequencies (compared to the precessional frequency) the dynamics resembles the static case.

The influence of the temperature on the minimum alternating field amplitudes is depicted in figure 7. With increasing temperatures, the minimum amplitudes become smaller due to an additional thermal energy pumped from the environment. The curves in this figure can be approached with two linear dependences with different slopes for approximately $\alpha < 1$ and for $\alpha > 1$; for high damping it is linearly dependent on $\alpha$; more specifically, it can be shown that for high damping the critical fields behave as

$$ b_{cr} \approx \frac{1}{\alpha} \alpha^2. \quad (17) $$
The proportionality coefficient contains the frequency of the alternating field and the critical angle \( \theta \). The solution (17) follows from the LLG equation solved for the case when the phase of the external field follows temporally that of the magnetization, which we checked numerically to be valid.

The reversal times associated with the critical switching fields are shown in figure 8. Qualitatively, we observe the same behavior as for the case of a static field. The values of the reversal times for \( T = 0 \) are, however, significantly smaller than for the static case. For the same reason as in the static field case, an increased temperature results in an increase of the switching times.

3.2. Nanoparticles with cubic anisotropy: Fe\(_{70}\)Pt\(_{30}\)

Now we focus on another type of the anisotropy, namely a cubic anisotropy, which is supposed to be present for Fe\(_{70}\)Pt\(_{30}\) nanoparticles [24]. The energetics of the system is then described by the functional form

\[
\tilde{\mathcal{H}} = -d(S^z_0)^2 + S^x_0 S^y_0 - S \cdot \mathbf{b},
\]

or in spherical coordinates

\[
\tilde{\mathcal{H}} = -d(\cos^2 \phi \sin^2 \theta + \cos^2 \theta \sin^2 \phi) - S \cdot \mathbf{b}.
\]

In contrast to the previous section, there are more local minima or in other words more stable states of the magnetization in the energy profile for the Fe\(_{70}\)Pt\(_{30}\) nanoparticles. It can be shown that the minimum barrier that has to be overcome is \( d/12 \), which is one-12th of that in the case of a uniaxial anisotropy. The maximal one is only \( d/3 \).

The magnetization of these nanoparticles is first relaxed to the initial state close to \( \phi_0 = \pi/4 \) and \( \theta_0 = \arccos(1/\sqrt{3}) \), whereas in the target state it is aligned antiparallel to the initial one, i.e. \( \phi_c = 3\pi/4 \) and \( \theta_c = \pi - \arccos(1/\sqrt{3}) \). In order to be close to the starting state for the uniaxial anisotropy case we choose \( \phi_0 = 0.2499\pi \), \( \theta_0 = 0.3042\pi \).

3.2.1. Static driving field. A static field is applied antiparallel to the initial state of the magnetization, i.e.

\[
b = -b/\sqrt{S(e_x + e_y + e_z)}. \tag{20}
\]

In figure 9 the trajectory of the magnetization in case of an applied static field is shown. Similar to the previous section the energy of the initial state lies higher than that of the target state. The magnetization rolls down the energy landscape to eventually end up by the target state. The trajectory the magnetization follows is completely different from the one for the uniaxial anisotropy. Figure 10 supplements this scenario of the magnetization reversal by showing the time evolution of the \( \mathbf{S} \) vector. Because of the different anisotropy type, the trajectory is markedly different from the case of the uniaxial anisotropy and a static field. Here we show only the \( \mathbf{S} \) magnetization component, even though the other components also have to be taken into account in order to avoid a wrong target state.

The procedure to determine the critical field amplitudes is similar to that described in the previous section. In figure 11 the critical fields versus the damping parameter for different temperatures are shown. For \( q_0 \), the critical field strength is smaller than unity. This is consistent insofar as the maximum
Figure 11. Critical static field amplitudes versus the damping parameters for different temperatures averaged over 500 cycles. The inset shows non-averaged data for $q_6 = 0.06 \equiv 1.9K$.

Figure 12. Reversal times corresponding to the critical static fields of figure 11 versus damping averaged over 500 cycles.

The effective field for a cubic anisotropy is $\frac{3}{2}B_A$. In principle, the critical field turns out to be constant for all $\alpha$ but for an infinitely large measuring time. Since we set this time to be about 5 ns, the critical fields increase for small and high damping. On the other hand, at lower temperatures smaller critical fields are sufficient for the (thermal-activation-assisted) reversal process.

The behavior of the corresponding switching times presented in figure 12 only supplements the fact of too low measuring time, which is chosen as 5 ns for a better comparison of these results with ones for uniaxial anisotropy. Indeed, constant jumps in the reversal times for $T = 0K$ as a function of damping can be observed. The reason why the reversal times for finite temperatures are lower is as follows: the initial state for $T = 0K$ is chosen to be very close to equilibrium. This does not happen for finite temperatures, where the system due to thermal activation jumps out of equilibrium (cf see figure 10).

3.2.2. Time-dependent external field. Here we consider the case of an alternating field that rotates in the plane perpendicularly to the initial state of the magnetization. It is possible to switch the magnetization with a field rotating in

the $xy$-plane but the field amplitudes turn out to be larger than those when the field rotates perpendicular to the initial state. For the energy this means that the field entering equation (19) reads

\[
b(t) = (b_0 \cos \omega_1 t \cos \phi_0 + b_0 \sin \omega_1 t \sin \phi_0 \cos \theta_0) e_x + (-b_0 \sin \omega_1 t \sin \phi_0 + b_0 \sin \omega_1 t \cos \phi_0 \cos \theta_0) e_y + (-b_0 \sin \theta_0 \sin \omega_1 t) e_z,
\]

where $b_0$ is the alternating field amplitude and $\omega_1$ is the frequency associated with the field. This expression is derived upon a rotation of the field plane by the angles $\phi_0 = \pi/4$ and $\theta_0 = \arccos(1/\sqrt{3})$.

The magnetization trajectories depicted in figure 13 reveal two interesting features: firstly, particularly for small damping, the energy profile changes very slightly (due to the smallness of $b_0$) while energy is pumped into the system during many cycles. Secondly, the system switches mostly in the vicinity of local minima to acquire eventually the target state. Figure 14 hints at the complex character of the magnetization dynamics in this case. As in the static field case with a cubic anisotropy the critical field amplitudes shown in figure 15 are smaller than those for a uniaxial anisotropy. Obviously, the reason is that the potential barrier associated with this anisotropy is smaller.
in this case, giving rise to smaller amplitudes. As before, an increase in temperature leads to a decrease in the critical fields.

The reversal times shown in figure 16 exhibit the same feature as in the cases for uniaxial anisotropy: with increasing temperatures the corresponding reversal times increase. A physically convincing explanation of the (numerically stable) oscillations for the reversal times is still outstanding.

4. Summary

In this work we studied the critical field amplitudes required for the magnetization switching of Stoner nanoparticles and derived the corresponding reversal times for static and alternating fields for two different types of anisotropies. The general trends for all examples discussed here can be summarized as follows: firstly, increasing the temperature results in a decrease of all critical fields regardless of the anisotropy type. Anisotropy effects decline with increasing temperatures, making it easier to switch the magnetization. Secondly, elevating the temperature increases the corresponding reversal times. Thirdly, the same trends are observed for different temperatures: the critical field amplitudes for a static field depend only slightly on $\alpha$, whereas the critical alternating field amplitudes exhibit a pronounced dependence on damping. In the case of a uniaxial anisotropy we find the critical alternating field amplitudes to be smaller than those for a static field, especially in the low damping regime and for finite temperatures. Compared with a static field, alternating fields lead to smaller switching times ($T = 0$ K). However, this is not the case for the cubic anisotropy. The markedly different trajectories for the two kinds of anisotropies endorse the qualitatively different magnetization dynamics. In particular, one may see that for a cubic anisotropy and for an alternating field the magnetization reversal takes place through the local minima, leading to smaller amplitudes of the applied field. Generally, a cubic anisotropy is smaller than the uniaxial one, giving rise to smaller slope of critical fields, i.e. smaller alternating field amplitudes.

It is useful to contrast our results with those of reference [15]. Our reversal times for AC fields increase with increasing temperatures. This is not in contradiction with the findings of [15] insofar as we calculate the switching fields first, and then deduce the corresponding reversal times. If the switching fields are kept constant while increasing the temperature [15] the corresponding reversal times decrease. We note here that experimentally known values of the damping parameter are, to our knowledge, not larger than 0.2. The reason why we go beyond this value is twofold. Firstly, the values of damping are only well known for thin ferromagnetic films and it is not clear how to extend them to magnetic nanoparticles. For instance, in FMR experiments damping values are obtained from the widths of the corresponding curves of absorption. The curves for nanoparticles can be broader due to randomly oriented easy anisotropy axes and, hence, the values of damping could be larger than they actually are. Secondly, due to a very strong dependence of the critical AC fields (e.g. figure 7) they can even be larger than static field amplitudes. This makes the time-dependent field disadvantageous for switching in an extreme high damping regime.

Finally, as can be seen from all simulations, the corresponding reversal times are much more sensitive a quantity than their critical fields. This follows from expression (13), where a slight change in the magnetic field $b$ leads to a sizable difference in the reversal time. This circumstance is the basis for our choice to average all the reversal times and fields over many cycles. This is also desirable in view of an experimental realization, for example, in FMR experiments or using a SQUID technique quantities like critical fields and their reversal times are averaged over thousands of cycles. The results presented in this paper are of relevance to heat-assisted magnetic recording, e.g. using a laser source. Our calculations do not specify the source of thermal excitations but they capture the spin dynamics and switching behavior of the system upon thermal excitations.

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