Evaluation of the microstructure, optical properties and hopping conduction mechanism of rare earth doped Ba$_{0.85}$Ca$_{0.12}$RE$_{0.03}$Ti$_{0.90}$Zr$_{0.04}$Nb$_{0.042}$O$_3$ ceramics (RE = Ce$^{3+}$ and Pr$^{3+}$)

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The current research work examines the impact of Rare Earth (RE$^{3+}$) ion substitution on the structural, optical and conduction properties of a Ba$_{0.85}$Ca$_{0.12}$RE$_{0.03}$Ti$_{0.90}$Zr$_{0.04}$Nb$_{0.042}$O$_3$ (BCRETZN) (RE = Ce, Pr) ceramic compound produced via a solid-state route. The Rietveld method of the X-ray data revealed a tetragonal (P4mm) structure at room temperature for our ceramic compound. The morphology of the compound was explored using Scanning Electron Microscopy (SEM) as well as optical response and conduction behavior. The photoluminescence properties revealed that the BCCeTZN sample results in green and red photoemissions under laser excitation at 450 nm at RT. Furthermore, for the BCCeTZN sample, the photoluminescence data demonstrated that strong violet emission bands were acquired, at RT upon an excitation at 350 nm. The electrical conduction process was verified via the correlated barrier Hopping method. The scaling behavior suggests that the electrical conduction mechanism is independent of temperature. The existence of Ce$^{3+}$ and Pr$^{3+}$ ions in these materials could have important technological potential in new multifunctional devices.

1. Introduction

Perovskites with an ABO$_3$ general formula have gained a lot of interest over the past decades based on their potential applications and power in a variety of nanotechnology fields such as ferroelectric sensors, ceramic capacitors, optoelectronic devices, piezoelectric devices and actuators. Among these materials, BaTiO$_3$ (BT) is the most frequently used as a typical dielectric compound especially due to the elevated permittivity resulting from the interaction between dielectric behavior and structural deformation by means of Structural Phase Transitions (SPTs). These transitions are rhombohedral–orthorhombic–tetragonal–cubic and hexagonal [R–O–T–C–H] at −90 °C, 6 °C, 130 °C and 1432 °C, respectively, associated with the off-centering of the Ti cation. In effect, a relevant change in the behavior of the BT compound may be achieved via the incorporation or substitution of other ions in the Ti- and/or Ba-sites.

Concerning the optoelectronic applications, rare earth ions (Ln$^{3+}$) are useful substituted ions to enhance the functionality of BT. Commonly, Ln$^{3+}$ is used as an activator ion to achieve great luminescence characteristics. Furthermore, Ln$^{3+}$ can change the lattice properties and enhance the electrical behavior, in particular in terms of thermal evolution of permittivity and dielectric losses, as well as piezoelectric coefficients. C. Chalfouh et al. reported the impact of the substitution of Ba$^{2+}$ ions with lanthanide ions for example Pr$^{3+}$, Nd$^{3+}$ and Eu$^{3+}$ on the physical characteristics of BaTi$_{0.925}$(Yb$_{0.5}$Nb$_{0.5}$)O$_3$. The concurrent occurrence of ferroelectric and luminescence behavior in the titled system is considered most prospective for a novel collection of multifunctional electrooptic compounds.

Furthermore, (Ba,Ca)(Ti,Zr)O$_3$ (BCTZ) compounds have more recently been considered as a lead-free perovskite compounds presenting interesting piezoelectric properties. Several investigations have shown that the incorporation of Ln$^{3+}$ ions (Pr$^{3+}$, Ce$^{3+}$) in Ba$_{0.85}$Ca$_{0.15}$Ti$_{0.90}$Zr$_{0.04}$O$_3$ compound can enhance its functional process. For example, the Pr$^{3+}$ ions modified lead-free BCTZ compound exhibits enhanced piezoelectric and ferroelectric properties. This material was found to
be particularly suitable for energy harvesting applications, with an exceptional figure of merit. Moreover, R. Hayati et al. reported that the Ce$^{3+}$-modified lead-free BCTZ compound exhibited enhanced electromechanical, piezoelectric and ferroelectric process at room temperature. Finally, I. Zouari et al. also reported that improved piezoelectric, dielectric, electro-caloric and ferroelectric process of BT-based compound have been achieved via the incorporation of (RE$^{3+}$, Nb$^{5+}$) for Ti$^{4+}$ in B site and Ca$^{2+}$ for Ba$^{2+}$ in A site. Therefore, the study of lead-free perovskite materials presenting a combination of these different substitutions, with global formula (Ba$_{x}$Ca$_{y}$RE$_{z}$Ti$_{1-x-y}$Zr$_{x}$Nb$_{y}$O$_{3}$ (BCRETZN) appears as particularly interesting.

Consequently, this work aims to investigate the structural, morphological, optical and hopping conduction process of BCRETZN (RE = Ce, Pr) produced by a solid-state route. The determination of their optical behavior allows to evidence photoluminescence properties. The analysis of electrical conductivity versus frequency allows a better understanding of the process of free and localized electrical charge carriers.

2. Materials and methods

2.1 Synthesis and sintering of Ba$_{1-x}$Ca$_{x}$RE$_{0.03}$Ti$_{0.97}$Zr$_{0.04}$Nb$_{0.04}$O$_{3}$ (RE = Ce, Pr) samples

The polycrystalline Ba$_{0.85}$Ca$_{0.15}$RE$_{0.03}$Ti$_{0.97}$Zr$_{0.04}$Nb$_{0.04}$O$_{3}$ (BCRETZN (RE = Ce, Pr)) samples were produced using solid-state route employing CaCO$_{3}$ (99%), BaCO$_{3}$ (99%), Pr$_{2}$O$_{3}$ (99%), CeO$_{2}$ (99%), TiO$_{2}$ (99%), ZrO$_{2}$ (99%) and Nb$_{2}$O$_{5}$ (99%).

The samples were calcined at 1000 °C for 24 h with intermediate grindings to remove impurities like carbon present, using temperature controlled programmable muffle furnace.

The calcined powder BCRETZN (RE = Ce, Pr) samples were pressed isostatically into circular pellet form under 8 t cm$^{-2}$ (of about 2 mm thickness) using a hydraulic press and at 1350 °C for 48 h in air with intermediate remilling and repulsive to obtain the final product.

2.2 Characterization of the samples

The crystalline phases of BCRETZN (RE = Ce, Pr) compounds were identified at RT using X-ray powder diffraction patterns acquired using a $\theta$/2$\theta$ diffractometer (“PANalytical X’Pert Pro” $\lambda$Cu-K$_{\alpha}$ = 1.5406 Å). The XRD patterns were recorded for 2$\theta$ values range of 20.00–70.00° with a step of 0.02°.

The phase determination was carried out by examining the locations and intensities of the peaks and comparing them with the International Center of Diffraction Data database patterns with the Highscore program.

In addition, structural examination was carried out utilizing the FULLPROF software. The crystallite size and internal microstrain parameters of the compounds were investigated by the Data Viewer software following Lorentzian and Gaussian distributions.

The microstructure and composition of the BCRETZN (RE = Ce, Pr) compounds were investigated utilizing Scanning Electronic Microscopy (SEM) (Phillips XL30) coupled with an Energy Dispersive X-ray (EDX).

Photoluminescence (PL) data were measured on a corner-stone 260 monochromator (from Oriel instruments) connected to an R955 photomultiplier (Hamamatsu, Japan).

A multi-line argon (Ar) Lasos laser, with an output power of 40 mW and 488 nm, 350 nm wavelength selection, was employed as the source of excitation respectively for BCPrTZN and BCcETZN compound.

For the conductivity measurements, the ceramic pellets were electroded by depositing silver on both sides of the sample. The conductance and capacitance were then measured using an impedance analyzer (Agilent 4294A) over a wide frequency range (40–10$^{4}$ Hz, AC signal amplitude 50 mV). A liquid nitrogen cooled cryostat (Janis Corporation) was utilized to achieve a temperature range between RT to 500 K.

3. Results and discussion

3.1 XRD and phase identification

Fig. 1(a) presents the room temperature XRD data of all the BCRETZN (RE = Pr, Ce) compounds. The results revealed a single-phase perovskite system without any secondary phase. This result confirms the incorporation of (Ca$^{2+}$, RE$^{3+}$) at the Ba site and (Zr$^{4+}$, Nb$^{5+}$) at the Ti site. This result is consistent with the calculated tolerance factor: $t = 1.050$ for BCcETZN and $t = 1.049$ for BCPrTZN, against 1.06 for BaTiO$_{3}$. Therefore, our samples are in the stable domain of the perovskite system and crystallize in the tetragonal structure.

From XRD patterns, it may be seen that the most intense peak [110] has been displaced to lower 2$\theta$ values for BCcETZN compared to BCPrTZN (Fig. 1(b)), suggesting that the lattice parameters increase in the BCcETZN sample compared to BCPrTZN.

The refinement of XRD data was carried out utilizing Rietveld model (Fig. 1(c)).

The results confirm that the BCRETZN (RE = Ce, Pr) sample crystallizes at room temperature in the tetragonal (P4mm) phase. Moreover, the refined lattice parameters agree well with the previous observation. Indeed, the lattice parameters calculated for BCcETZN are slightly higher than those of BCPrTZN. These results are similar to those found in recent research.

The XRD obtained for BCRETZN (RE = Pr, Ce) samples are quite similar for undoped BaTiO$_{3}$. However, the refined occupancy factors suggest that the obtained stoichiometries present only small differences with the expected ones.

The refinement quality of the XRD data was estimated by utilizing adjustment parameters like goodness of fit $\chi^2$, the weighted pattern $R_w$ and the pattern $R_p$ (Table 1). We noticed a good agreement between the theoretical and measured XRD data.

The refined structural settings are given in Table 2. Therefore, the XRD patterns confirm that our compounds crystallize in tetragonal (P4mm) structure and that (Ca$^{2+}$, RE$^{3+}$) are incorporated at the Ba site and (Zr$^{4+}$, Nb$^{5+}$) at the Ti site.

3.1.1 Crystallite size and microstrain determination. The internal microstrain and size of the crystallite play a crucial role in the properties of compounds and their microstructure and
physical process. Their significance is related to their particular properties and potential utilization in advanced technological applications.

XRD pattern examination is among the most precise methods for finding crystals size\(^{22-24}\) and irregular movement strain of atoms with respect to their literature lattice in the lattice.\(^{25}\)

Furthermore, to explore the evolution in the microstructure of BCRTZN (RE = Ce, Pr) compounds, two micro-structural phenomena, namely crystallite size (\(D\)) and micro-deformation (\(\varepsilon\)), were determined based on the XRD peak broadening.

The XRD integral width (\(\beta\)) curve is primarily related to two parameters \(\beta_L\) (Lorentzian component of \(\beta\)) and \(\beta_G\) (Gaussian

Table 1 Experimental parameters for X-ray powder diffraction of Ba\(_{0.85}\)Ca\(_{0.12}\)RE\(_{0.03}\)Ti\(_{0.90}\)Zr\(_{0.04}\)Nb\(_{0.042}\)O\(_3\) (RE = Pr, Ce) samples at room temperature

|                      | \(\text{BaTiO}_3\) (ref. 21) | \(\text{Ba}_{0.85}\text{Ca}_{0.12}\text{Ce}_{0.03}\text{Ti}_{0.90}\text{Zr}_{0.04}\text{Nb}_{0.042}\text{O}_3\) | \(\text{Ba}_{0.85}\text{Ca}_{0.12}\text{Pr}_{0.03}\text{Ti}_{0.90}\text{Zr}_{0.04}\text{Nb}_{0.042}\text{O}_3\) |
|----------------------|-------------------------------|-------------------------------------------------|-------------------------------------------------|
| **Space group**      | \(P4mm\)                      | \(P4mm\)                                        | \(P4mm\)                                        |
| **Cell parameters**  |                               |                                                 |                                                 |
| \(a\) (\(\AA\))      | 3.996(1)                      | 4.0012(3)                                       | 3.9981(1)                                       |
| \(c\) (\(\AA\))      | 4.027(5)                      | 4.0212(3)                                       | 4.0034(8)                                       |
| \(c/a\)              | 1.0077                        | 1.0049                                          | 1.0013                                          |
| \(V\) (\(\AA^3\))    | 64.36(1)                      | 64.379(1)                                       | 63.995(2)                                       |
| **Agreement factors**|                               |                                                 |                                                 |
| \(R_p\) (%)          | 9.76                          | 9.54                                            | 6.64                                            |
| \(R_wp\) (%)         | 12.7                          | 10.15                                           | 7.24                                            |
| \(\chi^2\)           | 1.89                          | 2.60                                            | 2.70                                            |
| **Tolerance factor** | \(t\)                        | 1.060                                           | 1.050                                           | 1.049                                           |
| **Average crystallite size (nm)** |                     |                                                  |                                                 |
| \(D_{W-H}\) (nm)     | 253.2                         | 220.2                                           | 220.2                                           |
| \(\varepsilon\)      | 0.0707                        | 0.0707                                          | 0.052                                           |
component of $\beta$) that are related to the impact of $D$ and $\varepsilon_i$ respectively. It is defined as follows:

$$\beta_{\text{H-W}}^2 = \beta_L^2 \beta_{\text{H-W}}^2 + \beta_G^2 = \beta_L^2 + \frac{\beta_G^2}{\beta_{\text{H-W}}^2}$$

(1)

where $\beta_L = \frac{K \lambda}{D \cos \theta}$ and $\beta_G = 4\tau \tan \theta$.

Thus, XRD based deconvolution of these two parameters was performed utilizing eqn (2). This formulation is reported by Halder and Wagner (H-W). It is described as follows:

Table 2  Refinement structural parameters for $\text{Ba}_{0.85}\text{Ca}_{0.12}\text{RE}_{0.03}\text{Ti}_{0.90}\text{Zr}_{0.04}\text{Nb}_{0.042}\text{O}_3$ (RE = Pr, Ce) samples at room temperature

| Compounds                               | Atom | x     | y     | z     | Occupancy |
|-----------------------------------------|------|-------|-------|-------|-----------|
| $\text{BaTiO}_3$ (ref. 21)              | Ba   | 0     | 0     | 0     | 0.99      |
|                                         | Ti   | 0.5000| 0.5000| 0.4990(6)| 0.98     |
|                                         | O$_1$| 0.5000| 0.5000| 0.0920(4)| 0.99     |
|                                         | O$_2$| 0.5000| 0     | 0.5119(7)| 1.98     |
| $\text{Ba}_{0.85}\text{Ca}_{0.12}\text{Ce}_{0.03}\text{Ti}_{0.90}\text{Zr}_{0.04}\text{Nb}_{0.042}\text{O}_3$ | Ba   | 0     | 0     | 0     | 0.82      |
|                                         | Ca   | 0     | 0     | 0     | 0.10      |
|                                         | Ce   | 0     | 0     | 0     | 0.02      |
|                                         | Ti   | 0.5000| 0.5000| 0.3994(6)| 0.91     |
|                                         | Nb   | 0.5000| 0.5000| 0.3994(6)| 0.04     |
|                                         | Zr   | 0.5000| 0.5000| 0.3994(6)| 0.039    |
|                                         | O$_1$| 0.5000| 0.5000| 0.0147(4)| 0.98     |
|                                         | O$_2$| 0.5000| 0     | 0.479(0) | 1.99     |
| $\text{Ba}_{0.85}\text{Ca}_{0.12}\text{Pr}_{0.03}\text{Ti}_{0.90}\text{Zr}_{0.04}\text{Nb}_{0.042}\text{O}_3$ | Ba   | 0     | 0     | 0     | 0.84      |
|                                         | Ca   | 0     | 0     | 0     | 0.11      |
|                                         | Pr   | 0     | 0     | 0     | 0.02      |
|                                         | Ti   | 0.5000| 0.5000| 0.4034(2)| 0.89     |
|                                         | Nb   | 0.5000| 0.5000| 0.4034(2)| 0.040    |
|                                         | Zr   | 0.5000| 0.5000| 0.4034(2)| 0.040    |
|                                         | O$_1$| 0.5000| 0     | 0.01474(0)| 0.97    |
|                                         | O$_2$| 0.5000| 0     | 0.84476(0)| 1.99    |
\[
\frac{\beta_{hkl} \cos \theta}{\lambda} = \frac{k}{D} + \varepsilon^2 \frac{16 \sin^2 \theta}{\beta_{hkl} \lambda \cos \theta} \Rightarrow Y = \frac{k}{D} + \varepsilon^2 X
\]

where \( Y = \beta_{hkl} \cos \theta / \lambda \), \( X = 16 \sin^2 \theta / \beta_{hkl} \lambda \cos \theta \), \( \theta \) is Bragg’s diffraction angle, \( \lambda \) is \( \lambda_{Cu-K\alpha} = 1.5406 \) Å and \( k \) is about 4/3.

Indeed, the behavior of \( Y \) according to \( X \) is linear. The intercept is given to determine \( D \) and the slope is \( \varepsilon^2 \). To determine the magnitude of \( D \) and \( \varepsilon \), the factor \( Y \) was graphed as a function of the factor \( X \). As indicated in Fig. 2, the plot demonstrated a quasi-linear trend for the BCRETZN (RE = Ce, Pr) compound. The \( D \) and \( \varepsilon \) magnitude were found using the

### Table 3. Quantitative analysis of Ba\textsubscript{0.85}Ca\textsubscript{0.12}RE\textsubscript{0.03}Ti\textsubscript{0.90}Zr\textsubscript{0.04}Nb\textsubscript{0.04}O\textsubscript{3} (RE = Pr, Ce) perovskites obtained by EDX and theoretically calculating atomic ratio

| Sample                  | Ba   | Ca   | Ce   | Ti   | Zr   | Nb   | O   | At% EDX analysis | At% calculation |
|-------------------------|------|------|------|------|------|------|-----|-----------------|-----------------|
| Ba\textsubscript{0.85}Ca\textsubscript{0.12}Ce\textsubscript{0.03}Ti\textsubscript{0.90}Zr\textsubscript{0.04}Nb\textsubscript{0.04}O\textsubscript{3} | 12.85 | 2.35 | 0.49 | 19.69 | 1.06 | 1.02 | 62.54 | 17.0 | 2.40 | 0.60 | 20 | 0.96 | 0.84 | 60 |
| Ba\textsubscript{0.85}Ca\textsubscript{0.12}Pr\textsubscript{0.03}Ti\textsubscript{0.90}Zr\textsubscript{0.04}Nb\textsubscript{0.04}O\textsubscript{3} | 15.25 | 2.38 | 0.35 | 18.42 | 0.76 | 0.80 | 62.04 | 17.0 | 2.40 | 0.60 | 20 | 0.96 | 0.84 | 60 |

Fig. 4. SEM picture of Ba\textsubscript{0.85}Ca\textsubscript{0.12}Ce\textsubscript{0.03}Ti\textsubscript{0.90}Zr\textsubscript{0.04}Nb\textsubscript{0.04}O\textsubscript{3} and Ba\textsubscript{0.85}Ca\textsubscript{0.12}Pr\textsubscript{0.03}Ti\textsubscript{0.90}Zr\textsubscript{0.04}Nb\textsubscript{0.04}O\textsubscript{3} samples.
linearly adjusted plot. Table 1 summarizes the obtained values. We notice that the values of $D$ and $\varepsilon$ are more important for the BCCeTZN sample than those of BCPrTZN ceramics.

### 3.2 Surface morphological and composition analysis

To explore the microstructure of the obtained sample, an EDX scanning was carried out at room temperature (Fig. 3). EDX findings support that there is no loss of incorporated components during the sintering with in experimental errors. The spectra reveal the presence of all chemical elements (Ba, Ca, Pr, Ce, Ti, Zr and Nb and O) introduced during the preparation of BCRETZN ($RE = Ce, Pr$) ceramic compound.

The experimental and theoretical concentrations for our samples is displayed in Table 3. EDX analysis showed that the experimental concentrations of the samples are smaller than the theoretical ones. This indicates that there is no successful integral reaction of stoichiometric input components, since no secondary phases are suggested by XRD analysis.

Therefore, it is reasonable to assure the substitution of ($Zr^{4+}$, $Nb^{5+}$) for $Ti^{4+}$ in B site and $Ca^{2+}$, $RE^{3+}$ for $Ba^{2+}$ in A site in our samples, which is consistent with our XRD result.

The SEM images illustrated in Fig. 4 for BCRETZN ($RE = Ce, Pr$) demonstrated that the surface of the original compound is composed of grains varying in size from 20 to 5 $\mu$m. Various geometries are evenly distributed on surface as has been proposed in similar perovskite ceramics with a varying chemical stoichiometry.

At higher magnification, we observe that all particles with a regular size of nearly 5 $\mu$m are evenly scattered on the surface, indicating that each particle consists of an agglomerate of a variety of crystallites.

To compare doping elements, we remark that the BCPrTZN compounds have a smaller grain sizes than the BCCrTZN compound. This phenomenon agrees with the result obtained from the XRD profile (Fig. 1).
We conclude that the incorporation of Pr$^{3+}$ ions can strongly reduce the size of ceramic than Ce$^{3+}$ ion to form BCRETZN (RE = Ce, Pr) ceramic.

As reported in ref. 29, the existence of various grain sizes with long-term annealing leads to the formation of irregularly-shaped grains and, therefore, porosity can be deceased.

This behavior is the impact of the optical response.

3.3 Photoluminescence properties

Fig. 5(a) displays the PL spectra of BCP$\text{Pr}_2$TZN compounds measured at room temperature. The absorption of photons at 450 nm resulted in the excitation of the $^3P_0$ level of Pr$^{3+}$.

The PL spectra resulted in green and red emissions in the 530 nm to 700 nm range, excited utilizing the 450 nm light, in which the green light of Pr$^{3+}$ ions revealed, in visible range, two emission peaks situated at 530 nm and 546 nm assigned, respectively, to the $(^3P_1 \rightarrow ^1H_0)$, $(^3P_0 \rightarrow ^1H_0)$ transitions.

Whereas, the red emission indicated five emission peaks situated at 600, 617, 649, 669 and 682 nm, and assigned to the $(^1D_2 \rightarrow ^3H_4)$, $(^1P_0 \rightarrow ^3H_4)$, $(^1P_0 \rightarrow ^3F_2)$, $(^1P_1 \rightarrow ^3F_3)$ and $(^3P_1 \rightarrow ^3F_4)$ transitions, respectively. It should be noted that the highest emissions are seen at 617 and 649 nm (Fig. 5(a)).

Under laser excitation at 450 nm, we observed that the PL spectra are composed of strong green and red emissions for the BCP$\text{Pr}_2$TZN compound at RT, corresponding to the transitions $(^3P_0 \rightarrow ^1H_0)$, $(^3P_0 \rightarrow ^1H_0)$, respectively.

The room temperature emission spectra ($\lambda_{ex} = 350$ nm), of the BCCe$\text{Pr}_2$TZN compound in the UV-Vis region is displayed in Fig. 5(b). We noticed a broad asymmetric blue band at 380–500 nm that is ascribed to the allowed parity transitions of the lowest component of 5d state to $^2F_{5/2}$ and $^2F_{7/2}$ levels of Ce$^{3+}$ ions. Both emissions are centered at 389 and 416 nm.

The PL spectra at RT of the BCCe$\text{Pr}_2$TZN compound upon a 350 nm laser excitation demonstrated the strong emission peak near 389 nm attributed to the 5d state to $^2F_{5/2}$ levels of Ce$^{3+}$ ions.

3.4 AC-conductivity study

Fig. 6(a and b) demonstrates the distribution of conductivity ($\sigma(\omega)$) against temperature and frequency of the BCRETZN (RE = Ce, Pr) compounds.
The charges shifted as a result of the applied field and contributed to the electrical behavior of BCRETZN (RE = Ce, Pr) samples.

We notice the $\sigma(\omega)$ rose with the frequency. Consequently, it departed from its $\sigma_{dc}(\omega)$ value and independence with frequency up to about $10^4$ Hz.

Furthermore, $\sigma(\omega)$ exhibited diffusion that moved to a higher frequency with rising temperatures for our samples.

The variation of the slopes $\sigma(\omega)$ was found in higher and lower frequency regions. The apparent low frequency plateau is frequency independent, which relates to $\sigma_{dc}(\omega)$ and indicates long-distance mobility of charge carriers. This low frequency plateau increased with increasing temperature, resulting in long-distance motion of the charge carriers.

For our case, data of $\sigma(\omega)$ of BCRETZN (RE = Ce, Pr) compounds could be divided into two areas: at low-frequency $\sigma_{dc}(\omega)$ region (R-I) and in the region with a strong frequency-dependent conductance at higher frequency (R-II).

According to Funke, this behavior may be explained on the basis of the Jump Relaxation Model (JRMs) in which the two contrasting relaxation processes failed and successful hops occurred.

The latter is produced when ions hop to proximate locations and return to their original location. This dispersion is caused by a greater unsuccessful jump. Generally, electrical conduction is explained by the relationship known as Jonsher’s power:

$$\sigma(\omega) = \sigma_{dc} + \sigma_{dc}(\omega) = \sigma_{dc} + A \times (2\pi \omega)^n, \quad 0 \leq n \leq 1 \quad (3)$$

In the equation above, $\sigma_{dc}$ is the dc conductance, $A$ is a constant related to temperature, “$n$” is the frequency exponent. This exponent is an important parameter. Indeed, it allows to understand the mechanism of conduction in the sample. Each conductance graph has a dispersive region with a slope $A(2\pi \omega)^n$ corresponding to the answers of grain boundaries and grains.

Similarly, P. Barranco et al. had suggested that deflection of $n$ may be described on the basis of the jump of energy carriers between both sites assigned to the polarizability of compound.

In the current search, the conductance data fitting in accordance with eqn (3) could not trace the modification of “$n$” with temperature.

Fig. 7(a and b) shows fitted conductance measurement for $T = 400$ K, an example, for both compounds.

The evolution of “$n$” for both compounds is demonstrated in Fig. 8(a and b), revealing the changing of the conduction phenomena. We note a decrease in “$n$” with temperature increase, indicating that Correlated Barrier Hopping (CBH) is the most suitable conductance for R-II data. This provides the contribution of large polaron hopping conductance to BCRETZN (RE = Ce, Pr) compounds.

In our case, $\sigma_{dc}$ is calculated by the expression:

$$\sigma_{dc}(\omega) = \frac{nN_p e^0 R_0}{24}$$

where, “$n$” is number of polarons, $N$ denotes localized states density, $N_p$ denotes localized states density, $e_0$ denotes the permittivity of the free space.

In this mode of electrical conduction, potential barrier ($W_m$) is defined in the CBH method as below:

$$n = 1 - \frac{6k_BT}{W_m + k_BT \ln(\omega \tau_0)} \quad (5)$$

To approximate the $W_m/K_B T$ large, the parameter “$n$” was reduced:

$$n = 1 - \frac{6k_BT}{W_m} \quad (6)$$

The $W_{m\text{-Ce}}$ and $W_{m\text{-Pr}}$ were calculated from the linear adjustment of experimental values $1 - n$ versus temperature. Their magnitudes were $W_{m\text{-Ce}} = 0.047$ eV and $W_{m\text{-Pr}} = 0.088$ eV (Fig. 8(a and b)).

Fig. 9(a and b) shows the decreased electrical conductivity $\sigma(\omega)/\sigma_{dc}(\omega)$ as a function of the decreased $\omega/(\sigma_{dc}T)$ values. All the measurements were practically overlapping.
They were approximately one line. This phenomenon is called the Time–Temperature Superposition Principle (TTSP). In fact, this suggests that the temperature relationship is integrated in the increase of charge carrier density without having a direct effect on the conductance phenomenon.

In addition, \( \sigma(\omega)/\sigma_0(\omega) \) ratio is measured by the formula:

\[
\frac{\sigma(\omega)}{\sigma_0(\omega)} = F \frac{\omega}{\sigma_0(\omega)} \frac{1}{T}
\]

where \( F \) is a constant.

The overlap of data at various temperatures suggests that the electrical ionic conduction mechanism in our compounds is not connected to temperature; however, it is connected to a short distance assigned to electrode polarization effect, in low-frequency range and at high temperature.

4. Conclusion

In conclusion, BCERTZN (RE = Ce, Pr) compounds were prepared using a solid-state route. XRD data refined using Rietveld method indicated that the BCERTZN (RE = Ce, Pr) compounds crystallize in tetragonal structure. The morphology of the BCERTZN (RE = Ce, Pr) ceramic was examined by SEM.

Strong red emission bands were observed for the BCPrTZN sample and strong green emission bands were found at RT upon laser excitation at 450 nm, corresponding to the transitions \( ({}^3P_0 \rightarrow {}^3H_4) \), \( ({}^3P_0 \rightarrow {}^3F_2) \), respectively. For BCCeTZN sample, upon excitation of a laser at 350 nm at RT, we found strong violet emission corresponding to the transition \( 5d \rightarrow {}^2F_{3/2} \).

The electrical conduction process of our compounds have been examined depending on the frequency at various temperatures.

The coexistence of optical and electrical conduction characteristics may lay the foundation for improvement of a potential material for application in optoelectronic or photonic devices.

Conflicts of interest

There are no conflicts to declare.

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