Multiband coupling and nuclear softness in optical model calculations for even-even and odd-A actinides

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Abstract. A new dispersive multiband coupled channels optical model with soft-rotator “effective” deformations is proposed to describe nucleon scattering on even-even and odd-A actinides. The impact of the introduction of axial and non-axial dynamical deformations that describe nuclear softness is discussed. Softness and multiband coupling are shown to change compound-nucleus formation cross section by up to ≈10% for incident neutron energies below 1 MeV.

1 Introduction

Conventional coupled-channel analysis of nucleon scattering by collective nuclei considers a target to be either vibrational or rotational [1]. In the first case small vibrational deformations of a spherical nucleus cause perturbations of an optical potential; they are expressed through deformations using Taylor expansion of the potential. The second case describes well-deformed nuclei and uses multipolar expansion of the potential where both vibrational and/or rotational states can be combined [2, 3]. Actinides feature large static deformations in the ground state combined with excited vibrational bands that start above ≈500–600 keV of excitation energy in even-even actinides. Such nuclear structure could not be accommodated within existing “conventional” coupled-channel models. Moreover, rigid-rotor structure model overestimates energies of high-spin levels (e.g., difference is ≈10% for the 10+ level of the ground state band in even-even actinides) [4].

Coupled-channel models using more complex nuclear structure, e.g., a Soft Rotator Model (SRM) [5, 6], have been proposed to describe nucleon scattering on spherical “soft-nuclei”. While giving adequate results for structural materials, the SRM with potential decomposition around the spherical shape demonstrates poor performance for nucleon scattering on actinides. Those problems are traced to convergence problems of the potential expansion near the spherical shape for well-deformed nuclei. Therefore, new investigation was warranted.

How large is the impact of the multiple-band coupling and the account of softness of deformed nuclei on calculated cross sections for nucleon scattering on actinides? Unfortunately, almost all relevant inelastic scattering data in EXFOR [7, 8] for actinides describing neutron scattering excitation of levels from non-ground-state bands are obtained for neutron energies less than 3.5 MeV, and hence have a large component due to the compound-nucleus decay. The situation is more favorable for inelastic proton scattering experiments [9, 10] at 26 and 35 MeV. Measured (p,p′) data on several nuclei including 238U show considerable excitation of non-ground-state band levels, comparable with the excitation of the 6+ level from the ground-state band. The energy of incident protons (26 and 35 MeV) allows to assign these scattering data to a direct process, described by optical model only. This implies that the multiband coupled channels model that includes excited levels from additional bands is essential for accurate optical calculations, which goes in the same direction than Dietrich et al. findings for the extended GS rotational band [11].

A dispersive coupled channels rigid-rotor optical model for deformed nuclei [12–14] was used as a starting point of new development. That potential has been shown to be approximately Lane consistent [15] and use analytically calculated dispersive contributions [16]. Then, using linear Taylor expansion of an optical potential near axially deformed shape, a generalization of the model was proposed, that allowed to account for small dynamic deformations of statically deformed nuclei [17]. Underlying rigid-rotor structure of excited bands was preserved and dynamical deformations were assumed to be independent of the excited states and were taken as averaged over the whole corresponding excited band. “Effective” deformations for interband coupling were treated as adjustable parameters for both even-even and odd-A nuclides, and for the later vibrational excitations were neglected. As a next step the SRM, describing low-energy collective excited states of a soft deformed even-even nucleus below 1 MeV, was used...
to compute “effective” deformations [18]. This allowed to perform more robust and reliable calculations with an account of multiband coupling and softness of target nucleus on even-even targets.

Model-driven multiband coupling for odd-A nuclei and detailed analysis of main effects that arise from nuclear softness in coupled channels calculations are discussed within this work.

2 “Effective” deformations

The key quantities of this approach — “effective” deformations — are in fact matrix elements of nucleus deformation operators. They indicate how nucleus shape changes upon transition between its states. Here we consider the following dynamic deformations of a nucleus shape: non-axial quadrupole, axial octupole, and volume conservation correction (see [17, 18]). This results in “effective” deformations:

\[
\begin{align*}
[\beta_2]_{\text{eff}} &= \langle \eta_i|\beta_2\rangle \langle \eta_i|\beta_3\rangle |\eta_i|, \\
[\beta_3]_{\text{eff}} &= \langle \eta_i|\beta_3\rangle \langle \eta_i|\beta_3\rangle |\eta_i|, \\
[\gamma_{20}]_{\text{eff}} &= \langle \gamma|\gamma\rangle \cos \gamma - 1 |\eta_i|, \\
[\gamma_{22}]_{\text{eff}} &= \langle \gamma|\gamma\rangle \sin \gamma \sqrt{2} |\eta_i|, \\
[\beta_2^2]_{\text{eff}} &= \langle \beta_3|\beta_2\rangle \langle \beta_2|\beta_3\rangle |\eta_i|, \\
[\beta_3^2]_{\text{eff}} &= \langle \beta_3|\beta_3\rangle \langle \beta_3|\beta_3\rangle |\eta_i|, \\
[\beta_0]_{\text{eff}} &= \frac{\beta_0}{4\pi} \left[ 2[\beta_2]_{\text{eff}} + [\beta_2^2]_{\text{eff}} + [\beta_3^2]_{\text{eff}} \right],
\end{align*}
\]

where \(\beta_2\) is the longitudinal quadrupole deformation with small vibrations \(\delta \beta_2\) around the static deformation of ground state \(\beta_{20}\), \(\gamma\) — transverse quadrupole deformation, \(\beta_3\) — octupole deformation, \(|\eta_i\rangle\) and \(|\eta_j\rangle\) are corresponding parts of the initial and final state nuclear wave-functions describing the low-lying collective states (they are typically factorized for different types of motion). These wave-functions may depend on nuclear spin due to rotational-vibrational interaction. “Effective” deformations serve as the strength that normalize the coupled channels matrix elements: \(\{\beta_2\}_\text{eff}\) and \(\gamma_{20}\)_\text{eff} control coupling to \(\beta\)- and \(\gamma\)-vibrational bands and also rotational stretching, \(\gamma_{22}\)_\text{eff} provides coupling to anomalous vibrational band with \(K = 2\), and \(\beta_0\)_\text{eff} describes an additional coupling due to the nuclear volume conservation condition.

As discussed in Ref. [17] treating these values as fitting coefficients avoid the use of nuclear structure models beyond the rigid rotor. However, to reduce the number of model parameters, it is far better to try to derive the “effective” deformations from an structure model. This also allows to apply the derived couplings for nuclei having less experimental data for the fit. Soft-rotator model [5] is a sound structure model that can achieve good description of the low-lying collective structure of even-even actinides. It can be used to calculate the “effective” deformations given by Eq. (1), but we do not know a comparable nuclear model for odd-A ones. We would like to consider not only the single-particle excitations for odd-A nuclei as done in Ref. [17], but also to consider the one-phonon collective core excitations as discussed in the next Section.

3 Approach to odd-A nuclides

Considering deformed heavy odd-A nucleus as an even-even core and an unpaired nucleon moving in the even-even core field, we can build a plausible description of low-lying collective states [19] with wave functions partially factorized by single-particle and core dynamic variables. But perturbational account of vibrational-rotational interaction, and strong coupling of single-particle and transverse vibration/rotation of the core hinder direct application of existing formalism. On the other hand for heavy nuclei with large \(A\) values the polarizing effects of the single unpaired nucleon should not affect the collective behavior of the core, in particular, nuclear softness, which is determined mainly by even-even core, and hence should vary smoothly for nearby nuclei like other collective properties, e.g., nuclear shape or deformations.

Under these considerations to calculate “effective” deformations of an odd-A nucleus we use wave functions of an even-even nucleus, corresponding to a core of the odd one. In this case coupling between levels of GS, \(\beta\)-, and octupolar bands of odd-A nucleus can be calculated using SRM, being restricted only to bands built on the same single-particle state of the odd-A nucleus. This condition is needed as it maximizes the overlap of the single-particle wave functions of the initial and final states, being the single-particle overlap equal exactly one for the same single-particle state due to the orthogonality condition. Though many other low-lying collective bands exist for an odd-A nuclei, the discussed bands are expected to have the strongest coupling, and therefore, a maximum impact on the calculated optical-model cross sections.

The last missing piece in this scheme is the mapping of the odd-A nucleus states onto the corresponding even-even (“core”) states needed to calculate the coupling matrix elements. While vibrational quantum numbers can be used straightforwardly, spins require additional explanations. First, GS spin of an odd-A nucleus is determined by the full angular momentum of the corresponding single-particle state as the even-even core spin is zero. Hence the nucleus rotation (sequence of states along the rotational band) can be attributed to the core. Second, each rotational band of an odd-A nucleus in fact consists of two sub-bands (one with the lowest state and its satellite) with spin increment equal to 2. As a result, a typical even-even nucleus spin sequence is assigned to every sub-band of an odd-A nucleus. Example of such assignment can be seen in Table 1.

4 Calculation algorithm

Calculations were performed using the following scheme. First, recommended collective-level energies of even-even targets (assumed to be a core of an odd-A target) were retrieved from the ENSDF database [20] and used to fit
are typically factorized for different types of motion). The corresponding parts of the initial and final state nuclear wavefunctions: 

\[
\psi_{\text{gs}}(\beta, \gamma) = \psi_{\text{gs}}(\beta) \psi_{\text{gs}}(\gamma)
\]

which is directly linked to needed nuclear transmission coefficients for calculations of the compound-nucleus decay using the Hauser-Feshbach theory [21]. Most of results are shown as a symmetrized ratio of CN formation cross sections: \( R(A; B) = \frac{\sigma_{A \to \gamma B} \times \sigma_{B \to \gamma A}}{\sigma_{A \to \gamma B} \times \sigma_{B \to \gamma A}} \).

How calculated CN formation cross sections change upon the development of Lane-consistent dispersive coupled channels optical model? Fig. 1 compare predictions of 3 phenomenological optical model potentials fitted to the same experimental data: a rigid rotor potential RIPL 2408 [12–14]\(^1\) with 5 (for \(^{238}\text{U}\)) or 6 (for \(^{235}\text{U}\)) levels from the GS band in the coupling scheme; a multiband coupling potential from [17] with 20 levels from 5 bands (for \(^{238}\text{U}\)) or 16 levels from 3 bands (for \(^{235}\text{U}\)) that uses effective deformation as fitting parameters, and finally a potential developed in this work that considers nuclear softness, SRM derived “effective” deformations, and slightly larger coupling scheme. CN cross section predictions vary up to 300 mb (about 10%) for different models mainly below 1 MeV.

Derived inelastic cross sections for neutron scattering on \(^{235}\text{U}\) target using the three different optical models discussed above are compared in Fig. 2 with available experimental data in EXFOR [22–26] as well as with experimental data on \(^{238}\text{U}\) and \(^{232}\text{Th}\) targets allowed to build a regional optical potential model, and fit the static deformation parameters. For the considered odd-A nucleus, the scan data available allowed to fit the static deformations only, using the same potential derived from \(^{238}\text{U}\) and \(^{232}\text{Th}\) scattering. Description of experimental data is similar to what was achieved in Ref. [17] including the total cross section ratio for a pair of nuclides. However, current model has a lower number of parameters and more accurately predict scattering cross sections on odd-A targets. Calculations of nucleon induced reactions on \(^{238}\text{U}\) and \(^{233}\text{U}\) targets are used as examples to analyze and compare the changes due to the account of nuclear softness in optical model calculations. The coupling schemes and assigned core spins for \(^{235}\text{U}\) are shown in Table 1. \(^{235}\text{U}\) is chosen since ENSDF database for it has a maximum number of ready to-use rotational bands clearly assigned to vibrational collective excitations of the core built on the same single-particle state as the GS band.

5 Results

Results are presented for the compound nucleus (CN) formation cross sections as this is a very sensitive quantity, which is directly linked to needed nuclear transmission coefficients for calculations of the compound-nucleus decay using the Hauser-Feshbach theory [21]. Most of results are shown as a symmetrized ratio of CN formation cross sections: \( R(A; B) = \frac{\sigma_{A \to \gamma B} \times \sigma_{B \to \gamma A}}{\sigma_{A \to \gamma B} \times \sigma_{B \to \gamma A}} \).

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| Table 1. Coupling scheme for \(^{233}\text{U}\) and \(^{235}\text{U}\). |
|---|---|---|---|---|---|---|
| \(^{233}\text{U}\) | \(^{238}\text{U}\) |
| \(E_{\text{tot}}\) | \(I^\pi\) | \(E, \text{MeV}\) | \(I^\pi\) | \(E, \text{MeV}\) |
| GS band | GS band |
| 0\(^+\) | 5/2\(^+\) | 0.000 | 0\(^+\) | 0.000 |
| 2\(^+\) | 9/2\(^+\) | 0.092 | 2\(^+\) | 0.045 |
| 4\(^+\) | 13/2\(^+\) | 0.229 | 4\(^+\) | 0.148 |
| 6\(^+\) | 17/2\(^+\) | 0.411 | 6\(^+\) | 0.307 |
| 8\(^+\) | 21/2\(^+\) | 0.635 | 8\(^+\) | 0.518 |
| GS band satellite | GS band satellite |
| 0\(^+\) | 7/2\(^+\) | 0.040 | 10\(^+\) | 0.776 |
| 2\(^+\) | 11/2\(^+\) | 0.155 | 12\(^+\) | 1.077 |
| 4\(^+\) | 15/2\(^+\) | 0.315 | 2\(^+\) | 1.060 |
| 6\(^+\) | 19/2\(^+\) | 0.518 | 3\(^+\) | 1.106 |
| 8\(^+\) | 23/2\(^+\) | 0.762 | 4\(^+\) | 1.163 |
| Octupole band | Octupole band |
| 1\(^-\) | 5/2\(^-\) | 0.749 | 1\(^-\) | 0.680 |
| 3\(^-\) | 9/2\(^-\) | 0.838 | 3\(^-\) | 0.732 |
| Octupole band satellite | Octupole band satellite |
| 1\(^-\) | 7/2\(^-\) | 0.790 | 5\(^-\) | 0.827 |
| 3\(^-\) | 11/2\(^-\) | 0.916 | 7\(^-\) | 0.966 |
| \(\beta\)-vibration band | \(\beta\)-vibration band |
| 0\(^+\) | 5/2\(^+\) | 1.311 | 0\(^+\) | 0.993 |
| \(\beta\)-band satellite | \(\beta\)-band satellite |
| 2\(^+\) | 7/2\(^+\) | 1.347 | 2\(^+\) | 1.037 |
| 4\(^+\) | 11/2\(^+\) | 1.341 | 4\(^+\) | 1.131 |
| \(\gamma\)-vibration band | \(\gamma\)-vibration band |
| 0\(^+\) | 7/2\(^+\) | 1.269 | 0\(^+\) | 0.927 |
| 2\(^+\) | 9/2\(^+\) | 1.056 | 2\(^+\) | 0.966 |
| 4\(^+\) | 11/2\(^+\) | 0.1056 | 4\(^+\) | 1.056 |
The second or third level from the GS band. This result is also qualitatively in agreement with (p,p') experimental works [9, 10].

Other way of analyzing the impact of non-GS-bands is to estimate the changes in CN formation cross section upon removal of band levels from the coupling scheme with the fixed optical potential. Fig. 4 shows the results of such calculation. Truncation of the coupling scheme leads to a significant change of CN formation cross section (typically up to 10%) for incident energies lower than several MeV with the greatest influence of levels from β-vibration rotational band. However, this effect is probably overestimated as compensation and redistribution of inelastic cross sections occur if we refit the experimental data with the reduced coupling scheme.

5.2 Nucleus stretching

Nuclear softness also describes the stretching of a nucleus due to centrifugal forces that lead to the reduction of the energy of the high-spin levels. This property allows a much better description of the experimental energies of the GS band using a SRM, and is expected to have an impact on calculated cross sections. Only GS band levels were left in the coupling scheme and volume conservation correction was disabled to evaluate this effect alone. Fig. 5 shows the difference in calculated CN formation cross section upon enabling the stretching effect. It reaches more than 10% for projectile energy under few MeV, highlighting the importance of nuclear stretching even when only GS band levels are coupled. This effect could not be considered in Ref. [17], as all rotational-vibrational bands in that work were assumed to be rigid. Note that softness leads to non-conservation of the projection of the angular momentum on the deformation axis (quantum number $K$). Therefore, the wave function of SRM includes mixture in the quantum number $K$ as derived in Ref. [17], but not used in cross-section calculations there.

5.3 Volume conservation

Nuclear volume conservation correction can be enforced using nuclear softness by introducing a dynamical monopolar deformation. Fig. 6 demonstrates introduced changes in calculated CN formation cross section. The significance of this effect is clearly seen, however calculated changes are partially caused by changes in the octupole deformation of a nucleus, so real dynamic (caused by softness) effect is lower than shown on fig. 6.

6 Conclusions

The proposed application of Lane-consistent dispersive multiband coupled channels optical model with SRM “effective” deformations to odd-A nuclei may potentially allow building a unified regional optical potential with multi-band coupling for both even-even and odd-A actinides. Such potential will couple multiple rotational-vibrational bands and assume that actinides are statically

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**Figure 2.** Calculated nonelastic cross sections (dashed) for neutron scattering on $^{239}$U using three dispersive optical model potentials: RIPL 2408 – rigid-rotor GS band coupling [12–14], multiband coupling with fitted “effective” deformations [17], and current model with SRM-derived multiband coupling. Derived experimental nonelastic neutron scattering cross sections from EXFOR [22–26] (black points) and Dietrich [27] (red points) are compared to calculations. Note that the direct inelastic cross sections of the first two excited levels were also included as quasi-elastic cross sections to derive the plotted non-elastic cross section $\sigma_{\text{nonel}}$. Calculated CN formation cross section using the new SRM model is shown as solid line for comparison.
well-deformed nuclei which are soft to axial and non-axial dynamical vibrations.

Three phenomenological optical model potentials fitted to almost the same experimental data, but with different coupling schemes and nuclear structure information, give prediction of the compound nucleus formation cross sections. These calculated CN formation cross sections show an spread of up to 300 millibarns (about 10%) for $^{238}$U and $^{233}$U below 1 MeV.
The impact of the introduction of the SRM description on calculated cross sections on both even-even and odd-A actinides was analyzed on examples of $^{238}$U and $^{233}$U targets. The effect of multiband coupling, centrifugal nucleus stretching, and volume conservation are shown to be important for accurate CN formation cross section calculations, with smaller impact for odd-A nuclei as intuitively expected. Coupling to the vibrational $\beta$-band appears to have the largest influence on the results. Direct excitation of multiband coupling, centrifugal nuclear interactions, with smaller impact for odd-$\alpha$ actinides was analyzed on examples of $^{238}$U and $^{233}$U nuclei.

Fitting of data for other odd-A actinides requires thorough analysis of their low-lying level structure that goes beyond the information currently available in the ENDSF database [20, 31, 32]. An alternative approach may involve the use of SRM and developed local systematics of SRM parameters to estimate the energy of expected collective bands needed for the coupled-channel optical model description.

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