Experimental study of the potential for thermal energy recovery with thermoelectric devices in low displacement diesel engines

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ABSTRACT

Improving the thermal efficiency of internal combustion engines is essential to reduce the operating costs and complaints with the increasing environmental requirements. Thermoelectric generators came up as an opportunity to reuse part of the heat loss with the exhausts. This paper evaluates the performance of a thermoelectric generator to improve the efficiency of a stationary diesel engine under different rotational speeds and torques. The data was obtained through CFD simulations and validated with experiments. The proposed solution uses a cooling system to control the temperature of the thermoelectric modules. The results show that the torque and the rotational speed of the engine are the most significant performance parameters of the thermoelectric generator, while the influence of the cooling water temperature has a minor but still significant influence. Additionally, the results show a change from 1.3% to 6.2% in the thermoelectric generator efficiency, while the exergy efficiency varies between 1.8% and 7.9%. The exergy balance indicates that most of the exergy is lost because of the irreversibilities in the thermoelectric generator and of the exergy loss with the exhausts. The exergy loss can be reduced by optimizing the design of the heat exchanger. Since the thermoelectric generator improved the engine efficiency by a marginal 0.2%–0.8%. Therefore, it is important to further research how to improve the design of heat exchangers for thermoelectric generators to increase their energy conversion efficiency and their impact on the energy efficiency of internal combustion engines.

1. Introduction

Internal combustion engines (ICE) are widely used in multiple applications, including transport, agriculture activities, industry, and power generation [1, 2, 3, 4, 5]. However, the increased exploitation of ICEs is one main driver of the accelerated depletion of fossil fuels and the large emissions of greenhouse gases and other pollutants [6, 7, 8, 9]. Commercial vehicles represent around 38% of the global consumption of fossil fuels [10] while accounting for 16.4% of the global emissions of CO₂ [11,12].

From 20% to 40% of the chemical energy in the fuel is converted into useful power during the operation of ICEs (i.e., depending on the engine cycle - gasoline or diesel - and technology), while 5% is dissipated by the friction in the mechanical components, and the remaining energy is loss as heat [13]. Based on the significance of heat losses in ICEs, the development and implementation of alternatives for heat recovery is a crucial commitment to meet the environmental standards of efficiency and operation. Consequently, the development of systems for waste heat recovery (WHR) has been gradually increasing interest [15]. There are different WHR systems available to reduce fuel consumption in ICEs by up to 10% [14].

In Colombia, stationary diesel engines are used to support electric power generation in non-interconnected areas [16]. Stationary diesel engines operate at high compression rates with a rather stable load, resulting in high exhaust temperatures, making them ideal technologies for WHR applications [17]. The development of WHR technologies includes the Rankine cycle [18], the Kalina cycle [19], the Rankine organic cycle [20, 21, 22], and the use of thermoelectric modules (TEM) [23]. Particularly, TEMs convert heat into electricity in the presence of a temperature gradient, based on the Seebeck effect [24, 25]. Additionally, TEMs include some advantages like the absence of moving parts, a compact structure, scalability, negligible maintenance costs, zero emissions, quiet operation, and high reliability [26]. Thermoelectric
Thermoelectric generators (TEG) integrate TEMs with a heat exchanger and a cooling system in [26].

Recently, several studies focused on the heat recovery potential of TEGs implemented in commercial and heavy-duty vehicles [27, 28, 29]. Studies discussing the application of TEGs focus on the influence of operational variables like the temperature of the surface s and the pressure drop, other aspects like the heat exchanger materials, or the characteristics of TEMs, on the overall conversion efficiency of TEGs [30, 31]. Accordingly, Liu et al. [32] discussed the flow distribution effects on temperature gradient and performance metrics of the heat exchanger. Moreover, Marvao et al. [33] compared the flow distribution effects on temperature gradient and performance metrics of the heat exchanger. Finally, Makki et al. [38] investigated a photovoltaic-thermoelectric generator using heat pipes aided by numerical models, evidencing that integrating TEGs with photovoltaic units can take advantage of the waste heat of the system, increasing the electric conversion efficiency.

Regardless of the extensive discussion addressing the integration of TEG into vehicles, most studies consider stationary operating conditions. These conditions are far from the real operating conditions in vehicles and represent an important limitation to estimate the energy recovery potential of TEGs accurately [33, 39, 40, 41, 42]. Engine load directly defines the composition, properties, flow, and temperature of the cooling flow and the turbulent interactions on the temperature distribution of TEMs, while Karri et al. [36] assessed different cooling flow rates to maximize the energy conversion in TEGs. On the other hand, Li et al. [37] performed an energy and exergy analysis of a hybrid photovoltaic-thermoelectric system, showing that a high concentration ratio combined with thermoelectric modules leads to higher efficiencies.

![Thermoelectric generator](image)

**Figure 1.** Thermoelectric generator.
exhaust, which influences the overall performance of TEGs [43, 44, 45]. Other aspects like the mitigation of polluting emissions and the influence on the fuel economy of the engine, which can stress the benefits of TEGs, are frequently excluded from studies.

To overcome the limitation of previous studies, the present study aims at characterizing the energy recovery potential of a TEG integrated into a low displacement diesel engine. To this end, the energy and exergy balances will be used. Additionally, an environmental and economic analysis will be developed to further highlight the performance of the TEG and its influence on the engine. To this end, experimental and simulated data of the TEG performance under different conditions will be used. Therefore, this paper contributes to characterizing the energy conversion efficiency of TEGs under different operating conditions as an energy recovery alternative in diesel engines. In what follows, Section 2 describes the methodology used in the study, the characteristics of the test bench, and the formulation of the energy analysis. Section 3 outlines the core findings and critically discusses the results. Finally, Section 4 provides the concluding remarks, limitations, and future perspectives.

2. Materials and methods

An experimental test bench was built, which includes a stationary diesel engine, a TEG, and a data acquisition (DAQ) system, which is described in this section.

2.1. Experimental setup

Figure 1 shows the drawings of the thermoelectric generator used during the experimental tests developed in this study.

The TEG includes a heat exchanger, a cooling system, 20 TEMs (model TEG1-12610-5.1), and a supporting structure. The TEMs are symmetrically distributed on both sides of the heat exchanger, with 10 TEMs on the upper surface and 10 on the lower surface. A thin layer of thermal putty was applied between TEMs and the hot and cold surfaces to improve the heat transfer. This reduces the air between the surface and TEMs, compensating for the surface irregularities. The number of TEMs used in the TEG was defined based on the available surface on the heat exchanger. The cooling ducts, located on the cold surface of TEMs, are used to control the temperature in this surface during the experiments, to define the impact of ambient temperature on the TEG performance. The cooling system circulates water that is cooled to a defined temperature in a chiller.

Figure 2 shows the electric configuration of the TEG.

In this case, TEMs are connected in series to a variable resistance (Rload) that is used to define the energy recovery potential of the TEG at different engine loads. Notice that the selection of the TEG array (series) is supported by the temperature gradient on the surface of the heat exchanger (i.e., the temperature variation of the surface between the inlet and the outlet of the TEG), which affects the electric efficiency of the TEMs.

The series arrangement was selected based on the fact that it yields higher efficiencies than the parallel arrangement, as demonstrated by Montecucco et al. [46]. This is explained by the lower voltage and higher current levels resulting in electric losses because of the Joule heating phenomena. The variable resistance adjusts the electric load according to the TEG performance (i.e., when the TEG reaches its maximum electric power generation capacity, the external resistance equals the resistance of the circuit of TEMs).

![Figure 2. Electric configuration of thermoelectric modules.](image)

![Figure 3. Experimental test bench.](image)
Based on the characteristics of the ICE, the backpressure introduced with the TEG on the exhausts must be under 2 kPa to prevent negative impacts on the energy efficiency of the engine (i.e., that the efficiency loss resulting from the backpressure surpass the efficiency gains obtained with the TEG). The latter is an important constraint in the design of TEGs to guarantee the adequate functionality of ICEs. Therefore, the heat exchanger must ensure the highest possible heat exchange rate without exceeding the pressure drop limit defined by the engine backpressure limit. A CFD simulation was implemented using OpenFOAM® to ensure the highest heat transfer rate in the heat exchanger while limiting the backpressure under 2.00 kPa. Results from the simulation show that the highest pressure drop resulting from the TEG was 1.20 kPa, which is lower than the 2.00 kPa admissible by the engine. Therefore, this design guarantees the normal operation of the engine.

Figure 3 displays a schematic representation of the complete engine test bench.

The instrumentation of the test bench is essential for data acquisition and monitoring. For this experiment, the temperatures at the input and output of the heat exchanger were measured with K-type thermocouples. Moreover, the pressures at the input and output of the TEG were measured using piezoresistive pressure sensors (model PSA-C01). Fuel consumption was measured with a gravimetric flow meter, while the combustion airflow was registered with an airflow meter (model 22680-7J600). The cooling water temperature was controlled with a chiller and a water pump that maintained a water flow rate of 6 L/min, keeping the cooling water temperature constant.

**2.2. Energy analysis**

Energy and exergy balances were used to assess the performance of the TEG.

**2.2.1. Energy balance of the TEG**

Figure 4 illustrates the input and output energy flows in the TEG system.

A flow of energy inputs the TEG with the gas flow through the heat exchanger, where part of the heat transferred is converted into electricity in the TEMs, while some heat is loss to the cooling water flow, and some heat is dissipated to the environment. The energy balance can be described by Eqs. (1), (2), and (3).

\[ \dot{Q}_{\text{TEG}} = \dot{W}_{\text{TEG}} + \dot{Q}_{\text{water}} + \dot{Q}_{\text{loss}} \]  
(1)

\[ \dot{Q}_{\text{TEG}} = \dot{m}_{\text{gases}} \cdot C_{p,\text{gases}} \left( T_{1} - T_{2} \right) \]  
(2)

\[ \dot{Q}_{\text{water}} = \dot{m}_{\text{water}} \cdot C_{p,\text{water}} \left( T_{3} - T_{4} \right) + \dot{m}_{\text{water}} \cdot C_{p,\text{water}} \left( T_{5} - T_{6} \right) \]  
(3)

where \( \dot{Q} \), \( \dot{W}_{\text{TEG}} \), \( T \), \( \dot{m} \) and \( C_{p} \) are the heat flow, electrical power generated by the TEG, temperature, mass flow rate, and specific heat, respectively.

Since the equivalence ratio in diesel engines is less than one, the combustion gases can be considered as an ideal gas [47]. Therefore, the \( C_{p} \) of the exhaust gases are calculated as a function of temperature of the gas flow like [48]:

![Figure 4. Energy flows in the TEG.](image-url)
2.2.2. Exergy balance of the TEG

The heat exchanger, as following

\[
\dot{Q}_{\text{TEG}} = \dot{m}_{\text{fuel}} \cdot C_{p,\text{fuel}} \cdot (T_1 - T_0) - \dot{m}_{\text{air}} \cdot C_{p,\text{air}} \cdot \ln \left( \frac{T_1}{T_0} \right) - R \cdot \ln \left( \frac{P_2}{P_1} \right)
\]

(8)

where \( T_0 \) and \( P_0 \) are the reference environmental temperature and pressure, defined at 28 °C and 1 atm, respectively.

2.2.3. Energy balance of the engine

In practice, ICEs aim at converting the highest amount of the chemical energy of fuels into mechanical power.

After fuel combustion, a fraction of the energy released is transformed into mechanic power, while a significant share is loss through friction to the refrigeration system and with the exhausts (see Figure 5a). Using a TEG is possible to recover a fraction of the energy loss with the exhaust (see Figure 5b).

The energy balance of the engine-TEG system is calculated as shown in Eq. (11).

\[
\dot{Q}_{\text{fuel}} + \dot{Q}_{\text{air}} = \dot{W}_{\text{engine}} + \dot{W}_{\text{TEG}} + \dot{Q}_{\text{loss}} + \dot{Q}_{\text{gases}}
\]

(11)

where \( \dot{Q}_{\text{fuel}} \) represents the energy of the fuel and \( \dot{Q}_{\text{air}} \) account for energy loss in the engine and the TEG.

The energy of the fuel was calculated as a relation between the flow of fuel and its heating value (LHV), defined as 44.05 MJ/kg in this case [12]:

\[
\dot{Q}_{\text{fuel}} = \dot{m}_{\text{fuel}} \cdot \text{LHV}
\]

(12)

The output power (\( \dot{W}_{\text{engine}} \)) of the engine was calculated as a function of the torque (\( T_r \)) and of the engine rotation speed (\( N \)) like:

\[
\dot{W}_{\text{engine}} = 2 \pi \cdot N \cdot T_r
\]

(13)

The loss with the exhausts at the engine output (\( \dot{Q}_{\text{gases}} \)) was calculated as:

\[
\dot{Q}_{\text{gases}} = (\dot{m}_{\text{fuel}} + \dot{m}_{\text{air}}) \cdot C_{p,\text{gases}} \cdot T_r
\]

(14)

The energy efficiency for the ICE without TEG was calculated as follows.

\[
\eta_{\text{engine}} = \frac{\dot{W}_{\text{engine}}}{\dot{m}_{\text{fuel}} \cdot \text{LHV} + \dot{Q}_{\text{gases}}}
\]

(15)

Moreover, the energy efficiency for the ICE with TEG is calculated as:

\[
\eta_{\text{engine-TEG}} = \frac{\dot{W}_{\text{engine}} + \dot{W}_{\text{TEG}}}{\dot{m}_{\text{fuel}} \cdot \text{LHV} + \dot{Q}_{\text{gases}}}
\]

(16)

2.2.4. Exergy balance of the engine

The exergy balance for the engine-TEG system was calculated as the sum of the exergies... as shown in Eq. (17)

\[
\dot{E}_{\text{fuel}} = \dot{E}_{W,\text{engine}} + \dot{E}_{W,\text{TEG}} + \dot{E}_{\text{loss}} + \dot{E}_{\text{gases}} + \dot{E}_{\text{fuel}}
\]

(17)

where \( \dot{E}_{\text{fuel}} \), \( \dot{E}_{W,\text{engine}} \), \( \dot{E}_{W,\text{TEG}} \), \( \dot{E}_{\text{loss}} \), \( \dot{E}_{\text{gases}} \) and \( \dot{E}_{\text{fuel}} \) are the exergy of the injected fuel, the work carried out by the engine, the work generated by the TEG, the loss exergy, the exergy of the gases expelled into the atmosphere, and the destruction of exergy, respectively.

The exergy of the fuel (\( \dot{E}_{\text{fuel}} \)) is calculated like:

\[
\dot{E}_{\text{fuel}} = \dot{m}_{\text{fuel}} \cdot \text{LHV} \cdot \phi
\]

(18)

where \( \phi \) is the chemical exergy factor of the fuel. A chemical exergy factor of 1.072 is defined for commercial diesel [49].

The exhaust exergy (\( \dot{E}_{\text{gases}} \)) and exergy loss (\( \dot{E}_{\text{loss}} \)) were calculated using Eqs. (19) and (20), respectively:

\[
\dot{E}_{\text{loss}} = \dot{m}_{\text{air}} \cdot \text{LHV} \cdot \phi
\]

(19)

\[
\dot{E}_{\text{gases}} = (\dot{m}_{\text{fuel}} + \dot{m}_{\text{air}}) \cdot C_{p,\text{gases}} \cdot T_r
\]

(20)
Table 1. Physicochemical properties of commercial diesel [12].

| Property                  | Units   | Value         | Standard         |
|---------------------------|---------|---------------|------------------|
| Cloud point               | °C      | 6.5           | ASTM D2500       |
| Flashpoint                | °C      | 76.0          | ASTM D93         |
| Density                   | kg/m³   | 821.5         | ASTM D1298       |
| Pour point                | °C      | 3.1           | ASTM D97         |
| Viscosity                 | cSt     | 2.64          | ASTM D445        |
| LHV                       | MJ/kg   | 44.05         | ASTM D240        |

\[
\dot{E}_{\text{loss}} = (\dot{m}_{\text{air}} + \dot{m}_{\text{fuel}}) \cdot \\
\left[ C_{p,gases} \cdot (T_2 - T_o) - T_o \cdot \left( C_{p,gases} \cdot \ln \left( \frac{T_2}{T_o} \right) - R \cdot \ln \left( \frac{P_2}{P_o} \right) \right) \right]
\]  

(19)

\[
\dot{E}_{\text{loss}} = \dot{Q}_{\text{loss}} \left( 1 - \frac{T_o}{T_1} \right)
\]  

(20)

where \( T_o \) and \( T_1 \) are the ambient temperature and the average surface temperature of the engine, respectively. The calculation of the entropy generation \( (S_{\text{gen}}) \) is developed as:

\[
S_{\text{gen}} = \frac{\dot{E}_{\text{loss}}}{T_o}
\]  

(21)

The exergy efficiency of the engine \( (\eta_{\text{engine}}) \) and the engine -TEG system \( (\eta_{\text{engine-TEG}}) \) are calculated as:

\[
\eta_{\text{engine}} = \frac{\dot{E}_{\text{product engine}}}{\dot{E}_{\text{fuel}}} = \frac{\dot{E}_{\text{W engine}}}{\dot{E}_{\text{fuel}}}
\]  

(22)

\[
\eta_{\text{engine-TEG}} = \frac{\dot{E}_{\text{product engine-TEG}}}{\dot{E}_{\text{fuel}}} = \frac{\dot{E}_{\text{W engine}} + \dot{E}_{\text{W TEG}}}{\dot{E}_{\text{fuel}}}
\]  

(23)

2.3. Experimental methodology

In total, nine operating points were selected for the experimental tests (see Figure 6).

The defined operating points defined consider three rotational speeds and three torques of the engine.

During the experiments, commercial diesel was used to fuel the engine. Table 1 shows the physicochemical properties of commercial diesel.

Table 2. Classification of the experimental test variables.

| Classification                  | Operational variable     | Unit | Nomenclature |
|---------------------------------|--------------------------|------|--------------|
| Response variables              |                          |      |              |
| - Mechanical engine power       | \( W \)                  |      | \( W_{\text{engine}} \) |
| - TEG electrical power          | \( W \)                  |      | \( W_{\text{TEG}} \)  |
| - Heat transferred to the walls of the exchanger | \( W \) | | \( Q_{\text{TEG}} \) |
| - Exergy destruction rate       | \( W \)                  |      | \( E_{\text{TEG}} \) |
| Input variables                 |                          |      |              |
| - Torque                        | Nm                       |      | \( T_{\text{e}} \) |
| - Rotation speed                | rpm                      |      | \( N \)      |
| - Cooling temperature \( ^\circ \text{C} \) | \( T \) | | \( T_{\text{air}} \) |
| Blocking and noise variables    |                          |      |              |
| - Fuel temperature \( ^\circ \text{C} \) | \( T_{\text{fuel}} \) | | \( T_{\text{fuel}} \) |
| - Environmental temperature \( ^\circ \text{C} \) | \( T_{\text{amb}} \) | | \( T_{\text{amb}} \) |
| - Air temperature \( ^\circ \text{C} \) | \( T_{\text{air}} \) | | \( T_{\text{air}} \) |
| Uncontrolled variables          |                          |      |              |
| - Inlet pressure \( \text{kPa} \) | \( P \) | | \( P \) |
| - Cylinder head temperature \( ^\circ \text{C} \) | \( T_{\text{cylinder}} \) | | \( T_{\text{cylinder}} \) |
| - Exhaust temperature \( ^\circ \text{C} \) | \( T_{\text{gases}} \) | | \( T_{\text{gases}} \) |

To clearly define the effect of the different operating parameters affecting the engine performance, an experimental design was used to plan the experimental test. Consequently, the operational variables were classified into response, input, blocking, and noise variables (see Table 2).

Table 3 shows the three considered levels for the torque and rotation speed of the engine (i.e., low, medium, and high).

In this case, a multilevel factorial experimental design 3² was used for the input variables, which resulted in nine experiments. Table 4 depicts the operating conditions of the engine for the nine operating modes during the experiments.

To reduce the variability of the experimental results, each test was run three times. Thus, a total of 27 experimental runs were developed. To ensure steady-state operating conditions during the experimental tests, the system started measuring after the temperature of the exhausts remained constant during 30 s. Afterward, the DQA system measured for 5 min.

Figure 7 shows the energy efficiency of the engine for different operating conditions.
The results show that the efficiency of the engine varies from 10% to 35% for the different operating conditions.

To evaluate the thermoelectric modules used in the experimental tests and evaluate their energy conversion efficiency, a comparative analysis of the conversion efficiency between the experimental ($\eta_e$) and ideal ($\eta_t$) performance was developed. The efficiencies were calculated as [50, 51]:

$$\eta_t = \frac{T_h}{3.41 \cdot T_h + 2.41 \cdot T_c} - \frac{T_c}{3.41 \cdot T_h + 2.41 \cdot T_c}$$  \hspace{1cm} (24)$$

$$\eta_e = \frac{V^2}{R \cdot m_g \cdot c_p \cdot \Delta T}$$  \hspace{1cm} (25)$$

where $T_h$ and $T_c$ are the temperature of the hot and cold side of the TEM, $V$ is the output voltage, $R$ is the load resistance, $m_g$ is the exhaust gas flow, $c_p$ is the specific heat capacity and $\Delta T$ is the variation of the exhaust temperature.

Figure 8 shows the comparative analysis of the energy conversion efficiency of TEMs.

The figure shows that there is an agreement between the efficiency experimentally measured and theoretically calculated. Thus, the results ensure that the thermoelectric modules are in good technical conditions.

Figure 9 shows the characteristic curves of the thermoelectric modules.

3. Results

This section discusses the experimental results of the study.

3.1. Effect of the external resistance ($R_{\text{load}}$)

Figure 10 shows the power generation in the TEG as a function of the electric resistance and operating conditions. The power generation reaches the highest output when the external electric resistance ($R_{\text{load}}$, see Figure 3) balances the sum of the TEMs electric resistances [52].

The results show that the power output in the TEG reaches a maximum at an average electric resistance of 60\,\Omega. For lower or higher values, the power output reduces significantly. These results are in agreement with other investigations discussing the integration of TEG into commercial vehicles [42]. Furthermore, increasing the torque and the rotation speed results lead to a significant increase in the electric power output in the TEG. This is explained because increasing the torque and rotational speed results in the higher temperature of the surface in the hot side of the TEMs.

Table 5 shows the hot side temperature of the TEMs for different operating conditions of the considered engine. These results are in agreement with other studies described in the specialized literature [53].
Figure 10. Power generation on the TEG.

Table 5. Hot side temperature of TEMs (°C).

| TEM | Torque [Nm] | Torque [Nm] | Torque [Nm] |
|-----|-------------|-------------|-------------|
| rpm | rpm         | rpm         | rpm         |
|     | 3400 | 3600 | 3800 | 3400 | 3600 | 3800 | 3400 | 3600 | 3800 |
| 1   | 65   | 96   | 104  | 117  | 135  | 150  | 156  | 176  | 187  |
| 2   | 86   | 97   | 105  | 118  | 136  | 151  | 157  | 177  | 188  |
| 3   | 85   | 96   | 104  | 117  | 135  | 150  | 156  | 176  | 187  |
| 4   | 83   | 94   | 102  | 115  | 133  | 148  | 154  | 174  | 185  |
| 5   | 88   | 92   | 100  | 113  | 131  | 146  | 152  | 172  | 183  |
| 6   | 86   | 97   | 105  | 118  | 136  | 151  | 157  | 177  | 188  |
| 7   | 86   | 97   | 105  | 118  | 136  | 151  | 157  | 177  | 188  |
| 8   | 86   | 97   | 105  | 118  | 136  | 151  | 157  | 177  | 188  |
| 9   | 88   | 94   | 102  | 115  | 133  | 148  | 154  | 174  | 185  |
| 10  | 88   | 94   | 102  | 115  | 133  | 148  | 154  | 174  | 185  |
| 11  | 87   | 98   | 106  | 116  | 137  | 149  | 155  | 175  | 186  |
| 12  | 89   | 99   | 104  | 120  | 135  | 150  | 155  | 175  | 186  |
| 13  | 88   | 98   | 105  | 118  | 133  | 152  | 154  | 174  | 185  |
| 14  | 82   | 93   | 103  | 117  | 134  | 150  | 152  | 172  | 183  |
| 15  | 78   | 90   | 99   | 114  | 129  | 145  | 153  | 173  | 184  |
| 16  | 85   | 96   | 107  | 116  | 138  | 153  | 155  | 175  | 186  |
| 17  | 85   | 95   | 106  | 120  | 134  | 149  | 155  | 175  | 186  |
| 18  | 87   | 98   | 103  | 116  | 137  | 152  | 158  | 178  | 189  |
| 19  | 85   | 96   | 100  | 113  | 131  | 149  | 153  | 173  | 184  |
| 20  | 82   | 92   | 104  | 116  | 135  | 150  | 156  | 176  | 187  |
3.2. Engine torque effects

Figure 11 shows the electric power output from the TEG for the defined operating conditions.

The results show that the power output from the TEG increases with the increased engine torque for all the rotational speeds. Likewise, the power output from the TEG increases with the rotational speed for all the engine torques. This is explained because the higher flow of energy in the exhausts through the heat exchanger results from the higher combustion temperatures supported by the increased fuel consumption with higher engine torques and rotational speeds [9].

In general, increasing the torque by 1 Nm doubles the output power in the TEG. Moreover, increasing the rotational speed of the engine by 200 rpm increases the power output in the TEG by 28%.

3.3. TEG cooling water temperature effect

Figure 12 shows the variation of the electric power output in the TEG for the different cooling water temperatures considered in the experimental tests.

Results show that reducing the cooling water temperature increases the electric power output. Since the gradient of the temperature in the TEMs increases for lower cooling water temperatures. Thus, increasing the output voltage. Reducing the cooling water temperature by 5 °C increases the power output in the TEG by an average of 18%.

In ICES, the loss with the gases varies from 30% to 35% of the energy input with the fuel. Friction losses account for some 5% of the fuel energy, while the cooling system accounts for 30%–40%, and the useful energy accounts for 25%–30%. A fraction of the heat loss can be recovered using TEGs to produce electricity. The use of DC-to-DC converters (power units) permits to matching of the output voltage of the TEG to the voltage required in the engine [54].

3.4. TEG energy analysis

Figure 13 shows the allocation of the energy balance in the TEG.

Results show that reducing the cooling water temperature increases the TEG power output while increasing the energy loss with the cooling water. In total, from 65% to 75% of the energy is loss to the cooling water, while 19%–31% is dissipated as heat to the environment. In this case, 4%–6% of the energy is recovered into electric power.

The conversion efficiency of TEGs is usually less than 5%. The higher efficiency obtained in this study is mainly explained by the type of heat exchanger used in the TEG (see Figure 1). This heat exchanger has longer residence times of the exhaust, leading to higher heat exchange rates and higher surface temperatures on the hot side of TEMs. With this design, the TEMs recover more energy into electricity, which is an improvement contrasted to other heat exchanger geometries used in TEGs, as discussed in the specialized literature [53]. Furthermore, the efficiency values higher than 5% obtained for a cooling temperature of 17 °C on the cold surface of TEMs (see Figure 13) are explained by the higher temperature gradient in the TEMs that increases the conversion efficiency. Another significant factor is the technical characteristics of the TEMs used, which can operate under high temperatures (max. 300 °C).

Low conversion efficiencies in the TEG are a consequence of the low conversion efficiencies of TEMs because the current materials available have low conversion efficiencies, as well as because of negative physical phenomena such as the Thomson effect [26]. Therefore, the authors
considered that the development of new materials would help to increase the efficiency of these devices.

Figure 14 illustrates the variation of the energy conversion efficiency in the TEG for different operating conditions.

Results show that the energy conversion efficiency of the TEG varies between 1.29% and 6.15%, increasing for lower values of the cooling water temperature for all the engine operating conditions, which is explained by an increment of the temperature gradient, as explained before (see Figure 12).

Regardless of the relatively low energy conversion efficiency, the adequate use of the electric power output from TEGs is a sound approach to reduce the fuel consumption of ICES that leads to reduced airborne emissions [25]. Moreover, contrasted to WHR technologies like the ORC, the TEG has lower costs, and technological complexity requires less space and has higher reliability. These advantages can contribute to the widespread implementation of TEGs as a WHR alternative in vehicles.

3.5. TEG exergy analysis

Figure 15 shows the allocation of the exergy balance in the TEG. Results show that reducing the cooling water temperature leads to higher electric power output, explained by the higher temperature gradient in the TEMs and the reduction of energy losses. In the process, the exergy loss with the exhausts and the exergy destruction account for most of the exergy input to the TEG (i.e., from 70% to over 80%). As compared to the energy balance, the exergy loss with the cooling water is little in the process. On average, increasing $5^\circ\text{C}$ in the cooling water temperature decreases exergy losses by 0.82%.

Figure 16 shows the variation of the exergy efficiency for different operational conditions.

Results show that reducing the cooling water temperature increases the exergy efficiency of the TEG for all the engine operating conditions. Like energy efficiency, increasing the engine torque and rotational speed also result in higher levels of exergy efficiency.

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**Figure 14.** Energy conversion efficiency of the TEG for different operating conditions.

**Figure 15.** Exergy balance of the at 6 Nm and 3800 rpm.
3.6. Energy efficiency of the ICE – TEG system

Figure 17 shows the energy balance of the ICE-TEG system for the engine operating at 6 Nm and 3600 rpm. Results show that out of the energy output from the engine with the exhaust, the TEG recovers from 2.6 to 3.3%, which accounts for 0.64–0.81% of the energy input to the engine.

Figure 18 shows the variation of the energy efficiency of the ICE – TEG system in the range of operating variables considered. The results show that the highest efficiency is obtained for 6 Nm at 3600 rpm, which coincides with the highest efficiency operating point of the ICE, in which the engine operates with the highest flow and energy content of the exhausts.

Table 6 compares the energy efficiency of the ICE operating with and without the TEG. The results show that, in total, the introduction of the TEG improved the efficiency of the ICE-TEG system from a low 0.18%–0.81%. The energy of the system increases. These results highlight the need to further research the design of TEGs to upgrade the conversion efficiency of their designs.

3.7. Exergy efficiency of the ICE – TEG system

Table 7 includes the entropy generation, calculated with Eq. (6), for the operation modes of the TEG considered in the study. Results show that the entropy generation increases with the torque in the engine. Moreover, at 3600 rpm and rotational speed, the entropy generation has a minimum, which is explained by the highest efficiency of ICE for this operating condition. Reducing the cooling water temperature reduces the entropy generation in the TEG. On average, reducing
the cooling temperature by 5 °C results in a reduction of 2% in the entropy generation.

Figure 19 shows the exergy balance of the ICE – TEG system.

Similarly, the results show that from the exergy output from the engine with the exhaust, the TEG recovers from 6.1% to 7.7% of the gas energy, which accounts for 0.61%–0.77% of the exergy input to the engine.

Figure 20 shows the variation of the ICE – TEG system for the range of operating conditions considered.

Similarly, the results show that the highest efficiency is obtained for 6 NM at 3600 rpm, coinciding with the highest efficiency operating point of the ICE.

Table 8 compares the exergy efficiency of the ICE operating with and without the TEG for the different operating conditions considered.

The results show that, in total, the introduction of the TEG improved the efficiency of the ICE-TEG system from 0.17% to 0.76% with the proposed system.

3.8. Influence of the TEG on the emissions of the ICE

Since the TEG reduces the demand for fuel in ICEs, a reduction of the emissions can be expected in the engine. Figure 21 shows the emissions of CO, CO₂, NOₓ, and smoke opacity in the ICE operating with and without the TEG.

Results show that the operation of the ICE with the TEG reduces the emission of pollutants in the engine. Reducing the cooling temperature reduces the emission of pollutants in the ICE, which is explained by the increased efficiency of the TEG in this case. Contrasted to the operation without TEG, the use of the TEG reduces the emissions of CO by 3.8%, 2.9%, and 1.9% cooling water temperatures of 17 °C, 22 °C, and 27 °C.
Similarly, the emissions of CO₂ were reduced by 3.9%, 2.9%, and 1.9%, while the emissions of NOₓ were reduced by 4.3%, 3.4%, and 1.4%, and the smoke opacity was reduced by 3.9%, 2.7%, and 2.1%, respectively.

3.9. Economic analysis

An economic assessment was developed to evaluate the economic viability of the TEG discussed in this study. The assessment considers the total construction and assembly cost and the economic savings from the TEG.

The cost of the TEG is calculated using the Eq. (26).

\[ C_T = C_{TEM} + C_{Exh} + C_c + C_f + C_M \]  \hspace{1cm} (26)

where \( C_{TEM} \) is the cost of the thermoelectric modules, \( C_{Exh} \) is the cost of the heat exchanger, \( C_c \) is the cost of the rectangular ducts (see Figure 1), \( C_f \) is the total manufacturing cost and \( C_M \) is the cost of accessories/miscellaneous.

The economic costs are provided in Table 9. The economic savings of the TEG are associated with the reduction of fuel consumption because of the energy savings. The economic savings are calculated as [55].

\[ E_{TEG} = \left( \frac{\dot{m}_{fuel}[\text{kg}]/[\text{s}]}{W_{engine}[\text{kW}]} \times 3600 \right) \cdot W_{TEG}[\text{kW}] \cdot \frac{p_f[\text{USD}]/[\text{kg}]}{t_p} \]  \hspace{1cm} (27)

where \( p_f \) is the price of fuel (1.3USD/\text{kg}) and \( t_p \) is the engine operating time (\( t_p = 24 \text{ hours/day} \)).

Figure 19. Exergy balance of the ICE – TEG system (ICE operating condition: 6 Nm and 3800 rpm).

Figure 20. Variation of the exergy efficiency of the ICE – TEG system.
The cost of fuel is determined as

\[ \rho_f = \frac{1.07 \text{ USD}}{\text{litre}} \times \frac{1000 \text{ litre}}{1 \text{ m}^3} \times \frac{1 \text{ m}^3}{821.5 \text{ kg}} = 1.3 \text{ USD/kg} \] (28)

The payback duration \( (P_b) \) is calculated as [57].

\[ P_b = \frac{C_{\text{TEM}} + C_{\text{Exh}} + C_c + C_f}{E_{\text{TEG}}} \] (29)

Figure 22 shows the economic savings for the different water-cooling temperatures considered.

The results show that reducing the cooling temperature by 20% increases the economic savings by 11%. The savings for one year, considering the continuous use of the engine (i.e., 24 h/day), account for 86 to 107.97 USD/kW for cooling temperatures between 17°C and 27°C.

Figure 23 shows the payback period of the TEG for the different water-cooling temperatures considered.

The results show a payback period of nearly 5 years, which is similar to other TEGs reported in the literature [55, 57]. This payback period should be significantly lower for bigger engines, with higher power.

### Table 8. Exergy efficiency of the ICE operating with and without the TEG.

| Torque [Nm] | Engine speed [rpm] | Exergy efficiency [%] | Without TEG | With TEG |
|-------------|--------------------|-----------------------|-------------|----------|
|             |                    |                       | Cooling water temperature |
|             |                    |                       | 17°C | 22°C | 27°C |
| 4           | 3400               | 24.72                 | 24.94 | 24.93 | 24.89 |
|             | 3600               | 26.23                 | 26.54 | 26.47 | 26.44 |
|             | 3800               | 24.39                 | 24.76 | 24.68 | 24.65 |
| 5           | 3400               | 26.81                 | 27.24 | 27.19 | 27.13 |
|             | 3600               | 28.54                 | 29.09 | 29.00 | 28.94 |
|             | 3800               | 26.33                 | 26.99 | 26.90 | 26.81 |
| 6           | 3400               | 29.09                 | 29.85 | 29.70 | 29.59 |
|             | 3600               | 32.21                 | 32.98 | 32.90 | 32.81 |
|             | 3800               | 28.15                 | 28.91 | 28.84 | 28.76 |

### Table 9. Economic costs (USD).

| Type | Unitary costs | Units | Manufacturing and assembling costs | Total Costs |
|------|---------------|-------|------------------------------------|-------------|
| $C_{\text{TEM}}$ | $38.5$ | 20 | $770$ | $770$ |
| $C_{\text{Exh}}$ | $154$ | 1 | $103$ | $257$ |
| $C_c$ | $103$ | 2 | $103$ | $309$ |
| $C_m$ | $26$ | | | $26$ |
| **Total** | | | $1,362$ | |
outputs. Furthermore, in countries with high fuel costs, the payback period should be lower than the one obtained in this study.

4. Conclusions

This study introduced the analysis based on the first and second law of thermodynamics to assess the impact of the torque and rotation speed of the engine and the cooling water temperature on the performance of TEGs. The map performance of the TEG and the engine is an adequate and novel approach to highlight the characteristics of TEGs to easily identify the operating characteristics and efficiencies of these devices.

The results highlight the significance of an adequate selection of the external electric resistance based on the operating conditions of the engine, thus guaranteeing the highest energy recovery in the TEG. The incorrect definition of electric resistance can significantly affect the performance of TEGs. Moreover, the analysis showed that the engine torque has more influence on the performance of the TEG than the engine rotational speed. Particularly, the power generation was increased for the maximum torque and rotational speed of the engine. On the other hand, the cooling water temperature significantly influences the TEG performance, and on average, reducing 5 °C results in an 18% increment, upgrading the efficiency of the TEG operation. Furthermore, implementing the TEG during the operation of the ICE reduced the emissions of CO, CO₂, NOₓ, and smoke opacity between 2% and 4%.

The exergy balance of the TEG shows that 31.6%–32% of the exergy is loss with the exhaust flow, while the exergy destruction accounts for 44%–47%. Therefore, there is still room to improve the performance of the TEG. Overall, a more detailed assessment is required to define the avoidable and unavoidable exergy destruction in the TEG, to define how to prevent the avoidable exergy destruction.

Overall, incorporating the TEG in ICES stand as a significant opportunity to increase energy efficiency and reduce the emission of pollutants. Implementing a transient analysis in the TEG is an opportunity to optimize its performance, which is the subject of future studies. Other opportunities to improve efficiency include the development of advanced construction materials and more efficient cooling systems to upgrade the energy conversion in TEGs.

Declarations

Author contribution statement

Ramírez-Restrepo, R. & Duarte-Forero, J.: Conceived and designed the experiments; Performed the experiments; Analyzed and interpreted the data; Contributed reagents, materials, analysis tools or data; Wrote the paper.

Sagastume-Gutiérrez, A. & Cabello-Eras, J.: Analyzed and interpreted the data; Contributed reagents, materials, analysis tools or data; Wrote the paper.

Hernández, B.: Performed the experiments; Analyzed and interpreted the data; Wrote the paper.

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The authors declare no conflict of interest.

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