Formation of metallic magnetic clusters in a Kondo-lattice metal: Evidence from an optical study

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Magnetic materials are usually divided into two classes: those with localised magnetic moments, and those with itinerant charge carriers. We present a comprehensive experimental (spectroscopic ellipsometry) and theoretical study to demonstrate that these two types of magnetism do not only coexist but complement each other in the Kondo-lattice metal, Tb2PdSi3. In this material the itinerant charge carriers interact with large localised magnetic moments of Tb(4f) states, forming complex magnetic lattices at low temperatures, which we associate with self-organisation of magnetic clusters. The formation of magnetic clusters results in low-energy optical spectral weight shifts, which correspond to opening of the pseudogap in the conduction band of the itinerant charge carriers and development of the low- and high-spin intersite electronic transitions. This phenomenon, driven by self-trapping of electrons by magnetic fluctuations, could be common in correlated metals, including besides Kondo-lattice metals, Fe-based and cuprate superconductors.

The quantum mechanics’ Pauli principle, also known as the exclusion principle, postulates that a single orbital may accommodate no more than two electrons and, if it is doubly occupied, the electron spins must be paired. This principal is implicated in the electronic and magnetic properties of solids as the so-called exchange effect. In the Stoner model of ferromagnetism of weakly-correlated itinerant electrons (the form observed in the elemental metals iron, cobalt and nickel) electron bands can spontaneously split into up and down spins. This happens if the relative gain in an exchange interaction is larger than the loss in kinetic energy. On the other hand, in the Heisenberg model of localised magnetism in magnetic insulators (the form observed in compounds LaMnO3, CuF2, VO2, and many others) the electrons, involved in the exchange coupling, are localised by strong electronic correlations when the large on-site Coulomb repulsion U opens a well-defined gap for charge carriers; and an adequate description of the ground state properties of these systems in terms of the superexchange spin-orbital models has been suggested.

However, recently synthesised Pd-based ternary compounds of the form R2PdSi3, where R is a rare earth atom, have been found to have pronounced anomalies in resistivity, magnetization and susceptibility, associated in literature with their unusual or “novel” magnetic properties. These compounds descend from RSi2 compounds with the layered AlB2-type crystal structure, and have quasi-hexagonal symmetry [see Fig. 1 (a)]. The Tb rare-earth compound reveals the most intriguing regime of quasi-one-dimensional magnetism and anisotropic “spin-glass”-like behaviour (see Refs. [15–18] and references therein). In this compound the states at the Fermi level (EF) were found to be dominated by the highly conducting itinerant electrons of the Tb 5d1 orbital, whereas the Tb 4f states responsible for the large magnetic moment (of 9.68 μB, comparable to that of the free-ion Tb3+ value of 9.72 μB) were found to be localised deep below EF near 8 eV. In this paper we demonstrate that the unusual magnetic properties of Tb2PdSi3 are the result of complementary effects of itinerant and localised magnetism in the Kondo-lattice metallic state. The itinerant charge carriers interact with large localised magnetic moments of the Tb 4f states, forming regular lattices of self-organised ferromagnetic clusters below the Néel temperature TN = 23.6 K.

To elucidate the nature of electronic instabilities in the Kondo-lattice metal Tb2PdSi3, and the resulting unusual magnetic ordering phenomena, we used a comprehensive spectroscopic ellipsometry approach, which was successfully applied in our earlier studies of electronic correlations in the magnetic insulators.
So far the properties of the metallic Kondo-lattice compound Tb2PdSi3 have been discussed in terms of quasi-one-dimensional magnetism at high temperatures (near 55 K) and anisotropic ‘spin-glass’-like behaviour at low temperatures (< 10 K)\textsuperscript{11,12}. In particular, the broad peak in magnetic susceptibility near 55 K has been attributed to the magnetic correlations arising in one-dimensional spin chains, which have been intensively studied since the seminal paper by Bonner and Fisher\textsuperscript{13}. The peaks exhibit strong anisotropy in the paramagnetic state, also suggesting some similarities with quasi-one-dimensional systems. All the results convincingly demonstrate that some kind of long-range magnetic ordering sets in below \(T_N = 23.6\) K\textsuperscript{15–18}. However, the nature of the magnetism appears to be very complex, with strong evidence of ferromagnetic correlations and a complex ferrimagnetic type order in the basal plane, and a kind of anti-ferromagnetic correlations perpendicular to the basal plane, along the c-axis\textsuperscript{17}.

Neutron diffraction studies of this compound in zero magnetic field revealed both the long- and short-range order\textsuperscript{15,17,18}. The long-range order (LRO) below \(T_N = 23.6\) K may be described as follows. The magnetic unit cell of Tb2PdSi3 is four times as big in the basal plane, contains four magnetic Tb\(^{3+}\) ions (at the 3\(f\) and 1\(a\) site positions of \(P6/mmm\) hexagonal symmetry), and is sixteen times as big along the c direction. While the Tb moments are lying within the basal plane, as illustrated by Fig. 1(b), the most intriguing is the spin sequence of the magnetic moments associated with the individual Tb\(^{3+}\) ions along the c direction. The neutron diffraction study\textsuperscript{18} suggests that for all 3\(f\) positions there is a spin-sequence of eight positive orientation of the Tb moments “++”, followed by their eight negative orientation “−−”. On the other hand, the magnetic moments at 1\(a\) positions generate a different spin-sequence, consisting of the alternating orientations “++−−++−−++−−”, as schematically presented in Fig. 1(c). The low-temperature short-range correlations (SRC) are suggested to arise from frustrated magnetic moments within the LRO, and are associated with the “spin-glass”-like behaviour detected in the magnetic susceptibility measurements\textsuperscript{15–18}. We argue that the complex “exotic” phases observed in this compound in an external magnetic field and the low-temperature “glassy” behavior are associated with self-organisation of magnetic clusters, which can merge into string-like droplets or striply microdomains, may be ordered or disordered.

Figure 1 | Structure and long-range magnetic order in Tb2PdSi3. (a) A simplified unit cell of Tb2PdSi3, neglecting the c-axis superstructure. (b,c) ab-plane and c-axis magnetic ordering patterns according to the results of neutron scattering study\textsuperscript{18}. Our main results are as follows. After a thorough study of the optical response of the Kondo-lattice metal Tb2PdSi3 at low energies, we discovered anisotropic anomalous optical spectral weight (SW) changes across the Néel temperature \(T_N = 23.6\) K, involving the free charge carrier (Drude) resonance and two midinfrared (MIR) optical bands at 0.2 eV and 0.6 eV. We found that a vast amount of the optical SW of the free charge carriers (of the Drude peak) is shifted to the optical band at 0.2 eV. The observed anomalous behaviour in the low-energy optical conductivity spectra below 0.2 eV can be associated with the opening of a pseudogap in the conduction band and reconstruction of the Fermi surface. These anomalies are driven by electronic correlations related to the free electron instability against self-trapping in metallic ferromagnetic clusters, rather than band structure effect. Localisation of electrons in these magnetic clusters leads to development of the high-spin (HS) and low-spin (LS) inter-site electronic transitions, which were determined by their anomalous behavior in our comprehensive temperature study around \(T_N\) at 0.2 and 0.6 eV, respectively.

Finally, we note that in the optical conductivity spectra of the Fe-based superconductors, namely BaFe2As2 and Fe-chalcogenides, optical bands at around 0.2 eV and 0.6 eV, which evolve with electron- or hole-doping have been identified\textsuperscript{24–26}. In addition, the mid-infrared features at 0.2 eV and 0.6 eV are well-known and, according to numerous studies, are strongly pronounced in the optical conductivity spectra of all high-\(T_c\) cuprates, whereas they are absent in their dielectric phases\textsuperscript{27–29}. We can argue that electronic correlations lead here to the energy lowering due to self-trapping of charge carriers by magnetic fluctuations, thus giving rise to nanoscale inhomogeneities with a local magnetic ordering. The existence of these nanoscale inhomogeneities must manifest itself in the midinfrared optical conductivity as the high-spin (at around 0.2 eV) and low-spin (at around 0.6 eV) optical excitations.

Results

Wide-range optical response of Tb2PdSi3. Here we report the results of a spectroscopic ellipsometry study of a wide-range anisotropic dielectric response of high-quality single crystals of Tb2PdSi3. The available data on the optical properties of \(R_2PdSi_3\) ternary silicides and their parent compounds \(RSi_3\) is limited, to the best of our knowledge, to a single study of the room-temperature optical reflectivity in GdSi3 and ErSi3 polycrystalline films\textsuperscript{30}. The low- and high-temperature spectra of the real and imaginary parts of the dielectric function, \(\varepsilon(\omega) = \varepsilon_1(\omega) + i\varepsilon_2(\omega)\), in [100] polarisation are shown in Fig. 2. They demonstrate the main features of the a-axis dielectric response of Tb2PdSi3. At low energies, the dielectric function is dominated by a Drude-type response due to transitions within the conduction band, characterized by the free charge carrier scattering rate, \(\gamma_{tb}\) and the plasma frequency, \(\omega_p\). The zoomed-in low-energy part of the dielectric function is shown in the inset, where we also show \(\varepsilon_1(\omega)\) at intermediate temperatures between 10 and 250 K. At higher energies, broad optical bands associated with interband transitions can be identified by the resonance and antiresonance features that appear at identical energies in \(\varepsilon_2(\omega)\) and \(\varepsilon_1(\omega)\), respectively, obeying the Kramers-Kronig relations. The spectra can be well described in terms of the Drude-Lorentz model\textsuperscript{30}, with the results of the dispersion analysis summarised in Fig. 2 and in Table S1 (See Fig. S1 and Table S1 in the Supplementary Information to this paper). The optical response in the low-energy region is composed of a Drude peak and two bands centered in the MIR region at \(\omega_1 \approx 0.2\) eV and at \(\omega_2 \approx 0.6\) eV. At higher energies, we identify at least three interband transitions centered at 1.3, 1.7 and 3.4 eV. The c-axis dielectric function exhibits similar features in the optical response (not shown), however, compared to the a-axis spectra, we notice pronounced anisotropy in the range of the interband optical transitions, which appear at 2.2, 2.7 and 5.2 eV. The LDA
energies. Indeed, here the Drude response expands to higher photon energies with increasing temperature due to an increase in $\gamma_D$, together with simultaneous changes in the intensity and width of the MIR optical bands at 0.2 and 0.6 eV. Qualitatively different changes at low energies in the a- and c-polarized spectra indicate that the temperature changes for these competing effects are polarization dependent.

Anomalies induced by magnetic ordering. The anomalous behavior of the optical bands at $\omega_1 \approx 0.2$ eV and $\omega_2 \approx 0.6$ eV at low temperatures also becomes evident close to the magnetic phase transition, near $T_N = 23.6$ K. Here the difference spectra exhibit a dip, followed by a maximum around 0.6 eV. This feature has an asymmetric shape, with an extended tail at higher photon energies, where the second weaker maximum shows up around 1.2 eV. The latter exhibits a similarly anomalous behavior near $T_N$. One can compare the rearrangement of the SW due to these low-energy anomalies with the anharmonicity coming into effect at elevated temperatures.

Fig. 4(a, b) shows relatively weak changes in the a- and c-polarized optical-conductivity spectra at low photon energies ($\hbar \omega = 0.05$–1.0 eV) around $T_N$ and presents the results of the Drude-Lorentz analysis at 10 K. Contributions from the Drude term and from the MIR optical bands at 0.2 and 0.6 eV can be clearly seen here. Panels (c) and (d) of the same figure emphasise the anomalous temperature dependence of the anisotropic MIR optical conductivity near $T_N$. The inset of Fig. 4(c) shows critical behavior of the peak intensity, $I_{0.6\text{eV}}$, of the 0.6 eV optical band, such that $(1 - \text{const} \times \hbar \omega_{\max})$ follows trends in the dc transport anomalies in the a-axis spectra near $T_N$ (See Fig. S1 and Table S1 in the Supplementary Information to this paper). And finally, we analyze the difference, $\sigma_1(\omega_0, 30$ K $)$ $-$ $\sigma_1(\omega_0, 10$ K $)$, of the spectra measured immediately above and well below $T_N$, which exhibits clear anisotropy in the corresponding a- and c-polarised spectra [Fig. 4(e, f)].

According to our dispersion analysis of the a-axis spectra (See Fig. S1 and Table S1 in the Supplementary Information to this paper), in addition to the changes associated with the Drude response, the oscillator strength of the optical band at 0.2 eV decreases, whereas the one at 0.6 eV increases above $T_N$. Low-energy downturn in this difference indicates that the crossing point for the SW transfer between the “head” of the Drude response and the higher-energy response is located near 0.06 eV. Above 0.06 eV, the changes due to the Drude response compete with the opposite changes associated with the MIR optical band at 0.2 eV. The cumulative changes of the Drude response and the involved MIR optical bands result in the creation of zero crossing points around 0.27 eV and 0.47 eV.

In order to quantify the SW involved in these anomalies, we have integrated the associated optical SW increment as $\Delta SW(\omega, \Delta T) = \int_0^{\omega} \sigma_1(\omega', \Delta T)d\omega'$. In this investigation the optical conductivity calculations reproduce the main features of the optical response of Tb$_2$PdSi$_3$ and its anisotropy reasonably well.

Fig. 3(a) shows the related a- and c-polarised optical-conductivity spectra, $\sigma_1(\omega) = \omega \varepsilon_2(\omega)/(4\pi)$, in which the MIR optical band at $\omega_2 \approx 0.6$ eV and the higher-energy bands are more pronounced than in $\varepsilon_2(\omega)$. Fig. 3(a) also reflects changes in the optical-conductivity spectra at elevated temperatures. In the a-polarized spectra, the high-energy optical bands at 1.3, 1.7, and 3.4 eV broaden, while their intensities decrease. The peak position of the strongly pronounced optical band at 1.7 eV exhibits a noticeable shift, and as a result, an isosbestic point appears in the temperature-dependent optical-conductivity spectra at 1.5 eV, associated with a displacement of the optical SW to lower photon energies. In the c-axis spectra, the broadening of the high-energy optical bands at 2.2 and 2.7 eV explains notable changes at photon energies between 1 and 2 eV.

To get a better insight into the temperature-dependence of the a- and c-polarised optical-conductivity spectra, in Fig. 3(b, c) we plot the difference between $\sigma_1(\omega, T)$ and the respective low-temperature spectrum, $\sigma_1(\omega, 10$ K $)$. It can be seen here that the major temperature effects within the high-energy optical bands, discussed above, occur between 100 and 250 K and, therefore, can be associated with lattice anharmonicity effects. However, qualitatively different changes occur in the a- and c-polarised optical-conductivity spectra at low energies.
changes of the Drude response across $T_N$, $\Delta \sigma_{D}(\omega, 30 \text{ K, } 10 \text{ K})$, resulting from our dispersion analysis (See Fig. S1 and Table S1 in the Supplementary Information to this paper), are incorporated. For more accurate estimate of the associated energy scale, where the total optical SW obeys the f-sum rule\(^{32}\), an additional optical study at lower frequencies, which enables consistency in the dc limit $\sigma_D(\omega \to 0, T)$, is required. The resulting SW changes are presented in Fig. 4(e) in terms of the effective number of charge carriers per Tb atom, $\Delta N_{\text{eff}} = 2 \frac{V_m A \Delta \sigma}{\pi e^2}$, where $m$ and $e$ are the free-electron mass and charge, and $V = \sqrt{3} a^2 c/2$ is the unit cell volume corresponding to one Tb atom, expressed through the low-temperature lattice parameters $a = 4.0643$ Å and $c = 4.0502$ Å\(^{30}\). Alternatively, we estimate the optical SW associated with the contribution of charge carriers as $N_{\text{eff}}^D = \frac{2V_m (2\pi c)^2 \omega_p^2}{\pi e^2}$, which with $\omega_p = 2.703$ eV gives $N_{\text{eff}}^D(10 \text{ K}) = 0.308$ and with $\omega_p = 2.750$ eV gives $N_{\text{eff}}^D(30 \text{ K}) = 0.319$ (See Fig. S1 and Table S1 in the Supplementary Information to this paper). Hence, the SW changes of the Drude response across $T_N$, $\Delta N_{\text{eff}}^D(30 \text{ K, } 10 \text{ K}) = 0.011$, amount to 3.6% of the total low-temperature charge carrier SW, $N_{\text{eff}}^D(10 \text{ K})$. As evident from Fig. 4 (e), these SW changes are nearly compensated around the zero-crossing point at 0.47 eV, by the opposite changes of the SW of the optical band at 0.2 eV (which are in a good quantitative agreement with the SW amplitude around 0.2 eV across the spin-density-wave (SDW) transition at $T_{SDW} = 200$ K in the iron arsenide SrFe$_2$As$_2$\(^{36}\)). Therefore, the total SW gain across $T_N$ accumulated within the energy window $\hbar \omega \lesssim 1$ eV in the ab plane, $\Delta N_{\text{eff}}^D(30 \text{ K, } 10 \text{ K}) = 0.0036$ [see Fig. 4 (e)], amounts to 1.2% of the total charge carrier SW, $N_{\text{eff}}^D(10 \text{ K})$, and can be attributed to the SW gain of the optical band at 0.6 eV.

In the c-axis optical-conductivity spectra, in addition to the changes associated with the Drude response, the oscillator strength of the optical band at 0.2 eV decreases above $T_N$, while the one at 0.6 eV exhibits weak temperature dependence (See Fig. S1 and Table S1 in the Supplementary Information to this paper). Our analysis represented in Fig. 4 (f) shows that the SW changes of the Drude response across $T_N$ are nearly compensated at around 0.23 eV, by the opposite changes of the SW of the optical band at 0.2 eV. The total SW loss across $T_N$ within the energy window $\hbar \omega \lesssim 1$ eV in the c axis amounts to $\Delta N_{\text{eff}}^c(30 \text{ K, } 10 \text{ K}) = -0.0028$ [see Fig. 4(f)].

**Discussion**

We found that in the temperature range 10 K $\lesssim T \lesssim T_N$, anomalous changes of the optical SW in Tb$_2$PdSi$_3$ occur below 1 eV, including the Drude-type resonance and the MIR optical bands at 0.2 and 0.6 eV. We attribute these anomalies to electronic instabilities (many-body effects) caused by the nature of magnetism inherent
in this Kondo-lattice metal, which exhibits quasi-one-dimensional characteristics at higher temperatures and spin-glass-like behaviour at lower temperatures\textsuperscript{15–18}. The complex long-range magnetic order below $T_N$ is due to ferromagnetic correlations in the ferrimagnetic-type arrangements of the large Tb moments in the $ab$ plane, and antiferromagnetic correlations between the ferromagnetic clusters, alternatively ordered along the $c$ axis [see Fig. 1(b,c)]\textsuperscript{17}. The observed anomalous behaviour in the low-energy optical conductivity spectra below 0.2 eV can be associated with the opening of a pseudogap in the free charge carriers (Drude-type) response. As a result, the vast amount of optical SW of $\Delta \tau_{\text{eff}}(30 \text{ K}, 10 \text{ K}) \approx 0.011$ is shifted to the optical band at 0.2 eV, which we relate to electronic instability of the free charge carriers against the long-range ferromagnetic correlations in the $ab$ plane below $T_N$. The estimated amount of optical SW corresponds to a kinetic energy loss of the free charge carriers of about 5 meV, which correlates well with the characteristic temperature of the broad peak (55 K) in the $c$-axis ac susceptibility\textsuperscript{15–18}. This observation can explain the quasi-one-dimensional character of this Kondo-lattice metallic system displays above the $Néel$ temperature, and suggests the existence of the chain-type ferromagnetic clusters in this temperature range.

Nevertheless, several features of the observed low-energy optical conductivity anomalies are difficult to reconcile with a simple spin-density-wave scenario, where the SW, lost below the gap, accumulates above the gap. While in the $ab$ plane, the SW changes of the Drude response across $T_N$ are nearly compensated by the opposite changes of the SW of the optical band at 0.2 eV; and the SW accumulated by the optical band at 0.6 eV, $\Delta \tau_{\text{eff}}(30 \text{ K}, 10 \text{ K}) \approx 0.0036$ [see Fig. 4(e)], must be compensated at higher energies, which is in agreement with experimental observations in Fe-based superconductors and their parent compounds reported previously\textsuperscript{20–24}. This effect, which is accompanied by the low-energy optical-conductivity anomalies, requires further experimental and theoretical study. Additionally, the anomalous increase in the $dc$ conductivity in the $ab$ plane (see Fig. S1 and Table S1 in the Supplementary Information to this paper)\textsuperscript{31} can be largely accounted for by the reduced scattering rate of the charge carriers due to freezing out of the spin-flip scattering, caused by ferromagnetic ordering of the Tb 4f moments in the formed clusters. Interestingly, as we have discovered, the intensity of the 0.6 eV band simultaneously shows an anomalous decrease below $T_N$, indicating that the associated electronic excitation is suppressed by the frozen ferromagnetic alignment of the localised magnetic moments in the $ab$ plane [see inset of Fig. 3(c)]. We attribute this behaviour to the inter-site low-spin (LS) electronic excitation in an electron pair, where two electrons with antiparallel spins are residing on the same lattice site. An opposite observable trend in the behavior of the 0.2 eV band suggests that its origin can probably be attributed to the inter-site high-spin (HS) electronic excitation. In this case, two electrons with parallel spins are residing on the same lattice site, and the associated electronic excitation is enhanced by the frozen ferromagnetic alignment of the localised magnetic moments in the $ab$ plane. According to our earlier optical study of the insulating $d^2$ ($t_2g$) system YTiO$_2$\textsuperscript{32}, the contribution from the inter-site $d^0\rightarrow d^1$, $d^0\rightarrow d^0$ charge excitations to the optical response leads to four different excited states: a HS $T_1$ state at energy $U^* - 3J_{\text{H}}$, two degenerate LS states $T_2$ and $E$ at energy $U^* - J_{\text{H}}$, and a LS state $A_1$ at energy $U^* + 2J_{\text{H}}$, where $U^*$ is the effective Coulomb repulsion of the two electrons with opposite spins on the same orbital, and $J_{\text{H}}$ is the Hund’s rule coupling constant. There is an obvious analogy between 5d$^1$ system in Tb$_2$PdSi$_3$ and 3d$^1$ system in YTiO$_2$. Following that, we assign 0.2 eV to the HS-state transition and the 0.6 eV to the first LS state, and estimate the values of $U^*$ at $\approx 0.8$ eV and $J_{\text{H}}$ at $\approx 0.2$ eV. Thus, the next LS transition is expected at $\approx 1.2$ eV, in a good agreement with our observations [see Fig. 3 (b)].

Having analysed the observed anomalous low-energy optical conductivity behavior in a Kondo-lattice metal Tb$_2$PdSi$_3$, across $T_N$, we discovered that the SW changes of the optical band at 0.2 eV are in a quantitative agreement with the SW amplitude around 0.2 eV across the spin-density-wave (SDW) transition at $T_{SDW} = 200$ K in the iron arsenide SrFe$_2$As$_2$\textsuperscript{25}. In this compound, the ground state of the antiferromagnetic SDW instability of a stripe-type (or collinear) spin configuration was suggested to result from the nesting between the hole- and electron Fermi surfaces of itinerant electrons, rather than the superexchange interaction mediated through the off-plane As atoms\textsuperscript{25}. The origin of the low-energy twogap behavior, found in optical measurements, and of the higher-energy 0.6 eV optical feature is still unclear\textsuperscript{25}, which makes the nature of the driving force of the SDW instability in the iron arsenide compounds an open and a challenging question. Hence, some close qualitative and quantitative similarities with the optical features discussed in this optical study of the Kondo-lattice metal Tb$_2$PdSi$_3$ could be of a significant importance.

We note, however, that in the system we chose to study, the magnetic pattern is more complicated than a regular spin-density wave. Indeed, the long-range magnetic order arising at $T_N$ is characterized by different periods along the Tb 4f and 1a chains, whereas the short-range correlations seen below $T_N$ distort even this not particularly regular order. This is an additional evidence that we deal here with quite an irregular structure, most probably formed by spin chains of different lengths, which become frozen at lower temperatures, producing a spin-glass-like state observed in neutron diffraction experiments.

We conclude that the observed anomalous low-energy optical conductivity behavior in a Kondo-lattice metal Tb$_2$PdSi$_3$ occurs due to electron correlation rather than a band structure effect. We propose that magnetism of the large localised Tb 4f magnetic moments in the metallic ferromagnetic cluster is driven by the electron exchange instability at the Fermi level, similarly to instability of itinerant electrons. The optical SW redistribution involving the free charge carrier Drude resonance (broad and narrow), and the mid-infrared high-spin-(HS) and low-spin- (LS) state optical bands at 0.2 eV and 0.6 eV respectively, indicates electronic instability of the free charge carriers against coupling in the metallic ferromagnetic cluster. Thus, by observing the associated low-energy optical conductivity anomalies, one may elucidate further the evolution in the creation of magnetic clusters and estimate the amount of free carriers self-trapped by them in the Kondo-lattice metal.

In the first instance the magnetic clusters may arise from magnetic polarons\textsuperscript{25–28}, which are formed by large moments and free carriers. It is well known that small polarons in general may form string-like objects\textsuperscript{29–31}. In the present compound the magnetic polarons may display similar behaviour dictated by a large anisotropy and the quasi-one dimensional character of the magnetic ordering\textsuperscript{31–35}. Here, the lowest energy of the localised states corresponds to the small polarons assembled into ferromagnetic string clusters. In a single cluster, many free particles are self-trapped by the spin fluctuation involving many large Tb magnetic moments having the spin orientation parallel to the $ab$ plane. The spins of the trapped charge carriers and magnetic moments are collinear.

We estimated the size of these ferromagnetic string clusters, taking into account many-body effects of Coulomb interaction between electrons, their interaction with localised large moments, which are ferromagnetically ordered and coupled to each other due to some indirect exchange interaction, induced by itinerant charge carriers. The detailed mechanism of the string clusters formation is discussed in the Supplementary Information, here we only describe its main features. According to this mechanism, the itinerant charge carriers and the localised moments are forming together a potential well, where these charge carriers are self-trapped. Due to such a localisation, the kinetic energy of the trapped electrons increases, while at the same time their potential energy decreases. As a result, the total energy of the electrons in the clusters becomes smaller or comparable.
with the energy of itinerant charge carriers. The comparison indicates that a string with many trapped particles and magnetic moments may have lower total energy (including electronic, magnetic, and Coulomb contributions), as shown schematically in Fig. 5.

It is important to note that the energies of string clusters having different lengths are very close to each other. In general, we expect to find a very broad distribution of such clusters at the temperature above \( T_s \) and, possibly, also below this temperature. Such magnetic clusters give rise to the tail in the density of states, which appears at high temperatures, this state survives until the short-range order in the basal plane as seen in the magnetic neutron scattering\(^{15-18} \). At high temperatures, the sample was mounted on the cold finger of a He-flow cryostat with a base pressure of \( 0.75-6.0 \) eV were performed with a home-build ellipsometer of rotating-analyzer type, where the angle of incidence is \( 70.0^\circ \). For the temperature-dependent measurements, the sample was mounted on the cold finger of a He-flow cryostat with a base pressure of \( 2 \times 10^{-10} \) Torr at ambient temperature. We used the home-build ellipsometer with incidence angles ranging from \( 65^\circ \) to \( 85^\circ \) in combination with the Bruker IFS 66/s FT-IR spectrometers for the MIR and NIR measurements in the photon energy range of \( 50 \) meV \( -1.0 \) eV.

**Methods**

**Crystal growth.** Careful selection and handling of high-purity starting materials and the control of oxygen impurities during the whole preparation process was essential. The polycrystalline seed rods were prepared from bulk pieces of rare earth, transition metal, and silicon of purity 99.9\% or better which were arc-melted several times in a water-cooled copper crucible under Ar atmosphere to reach homogeneity. The high-quality single crystals of \( \text{TbPdSi}_3 \) were grown by the floating-zone method with optical heating at melting temperatures \( > 1500 \) °C from near-stoichiometric polycrystalline feed rods. Post-growth heat treatment was used to improve the actual structure of grown crystals. Composition, microstructure and the perfection of the crystals structure of the samples were investigated by chemical analysis, optical metallography and scanning electron microscopy. The crystallographic orientation of single crystals was determined by the X-ray Laue back scattering method\(^{14,15} \).

**Experimental approach.** In our experiments we used ellipsometry approach. This method offers significant advantages over conventional reflection methods in studying metallic systems as (i) it is self-normalizing and does not require reference measurements, and (ii) full complex dielectric response \( \epsilon(\omega) = \epsilon_1(\omega) + i \epsilon_2(\omega) \) and the related optical-conductivity spectra, \( \sigma(\omega) = \omega \epsilon_2(\omega)/(4\pi) \), can be obtained directly without a Kramers-Kronig transformation. The complex dielectric response of \( \text{TbPdSi}_3 \) single crystals was investigated in a wide spectral range using a set of home-built ellipsometers at Max-Planck-Institut für Festkörperforschung, Germany. The VIS and UV measurements in the photon energy range of 0.75–6.0 eV were performed with a home-build ellipsometer of rotating-analyzer type, where the angle of incidence is \( 70.0^\circ \). For the temperature-dependent measurements, the sample was mounted on the cold finger of a He-flow cryostat with a base pressure of \( 2 \times 10^{-10} \) Torr at ambient temperature. We used the home-build ellipsometer with incidence angles ranging from \( 65^\circ \) to \( 85^\circ \) in combination with the Bruker IFS 66/s FT-IR spectrometers for the MIR and NIR measurements in the photon energy range of \( 50 \) meV \(-1.0 \) eV.

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Author contribution:
N.N.K. carried out the measurements and analysed the data. Y.H., W.L. and G.B. synthesised the single crystals. T.N.F. and A.V.B. participated in the data analysis. N.N.K., K.I.K. and F.V.K. wrote the manuscript. K.I.K. and F.V.K. supervised the project.

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