Application of the Hertz formulation in the discrete element model of pressure-assisted sintering

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Abstract This paper presents the numerical modelling of initial powder compaction and pressure-assisted sintering performed by original viscoelastic discrete element model. The research is focused on the influence of the type of the model representing an elastic part of interparticle force. Two elastic contact models—linear and nonlinear Hertz model—have been implemented and used to analyse interaction of NiAl powder particles during compaction and sintering process. Numerical models have been validated using own experimental results. Microscopic effects (particle penetration) and macroscopic changes (relative density) have been compared. It has been shown that although both models represent properly macroscopic behaviour of the material at the sintering process, the Hertz model produces the results closer to the real experimental ones during the initial compaction stage. Evaluation of macroscopic quantities enables implementation of the discrete element model in the framework of the multiscale modelling framework which is currently developed for sintering processes.

Keywords Powder metallurgy · Sintering · Initial compaction · Elasticity · Discrete element method

1 Introduction

The discrete element method (DEM) is a relatively new numerical method developed intensively at present time by many investigators [1–3]. In DEM, a material is represented by a large assembly of particles interacting among one another with contact forces. A particle interaction model in the DEM can take into account different effects, which are related to the specific model application. The formulation of appropriate contact interaction of particles seems to be an essential requirement to model properly the material behavior in the macroscopic scale. Currently, DEM is a widely acceptable method and has become a popular and useful tool for modeling discrete systems, such as a powder particles interactions in the powder metallurgy processes [4–6]. Generally, the manufacturing process of powder metallurgy consists of initial powder compaction and pressure-assisted sintering, which is the most important stage of powder metallurgy processes. It involves the consolidation of bonded powders at elevated temperatures, close to the melting temperature. Modelling of powder metallurgy and sintering processes requires a special constitutive model for particle contact interaction in which the sintering driving forces, viscosity, elasticity, cohesive and thermal interactions play a significant role. Although deformation during sintering itself is governed mainly by the viscosity, the material does maintain certain elasticity [7,8]. Elastic effects influence the distribution of forces in the heterogeneous particulate material and have some importance to the evaluation of stresses during the initial compaction and pressure-assisted sintering process.

Elastic (or elastoplastic) effects modeled by DEM can be represented by several models. The most basic one—linear model, assumes the linear relation between the elastic normal force and particles penetration. The non-linear Hertz model was performed on the majority of elastic or elastoplastic models of powder compaction, such as [9]. More complicated (representing also plastic deformation) is the linear hysteretic spring model [1,10,11], which is the simplest version of some more complicated nonlinear-hysteretic
force laws [10,12]. A simple linear elastoplastic and adhesive contact model for spherical particles has been proposed in [13]. Plastic deformation of contacts during loading and elastic unloading, accompanied by adhesion are considered, for which the pull-off force increases with plastic deformation. A model assuming rigid plastic behaviour according to the Hollomon stress–strain curve has been developed by Storåkers et al. [14,15].

In the following paper the theoretical and numerical results from two most popular/classic elastic models employed as a components of viscoelastic discrete element model of powder metallurgy have been compared. The influence of linear and nonlinear Hertz model on the densification during initial compaction and sintering stage has been investigated. Moreover, the numerical results have been compared and validated by own experimental results. Proposed work is an extension of original viscoelastic discrete element model of sintering presented in [16].

2 Formulation of discrete element model

The numerical model of initial compaction and pressure-assisted sintering has been implemented within the framework of the discrete element method (DEM), which assumes that a particulate material can be represented as a collection of spherical particles interacting among one another. In the discrete element method, the motion of rigid spherical elements (particles) is governed by the standard equations of rigid body dynamics.

The presented discrete element model is a combination of the cohesionless contact model with friction (the Kelvin–Voigt system—Fig. 1a) for the initial powder compaction, heating (before sintering) and cooling (after sintering), and the viscoelastic model of sintering (the Maxwell system—Fig. 1b) with the addition of thermal element related to the effect of thermal expansion. The equations of motion has been integrated in time using an explicit central difference type algorithm, the so-called leap-frog method. The detailed formulation of models is described in [16].

The normal contact interaction for the initial powder compaction consists of a spring and a dashpot connected in parallel, thus the normal contact force $F_n$ is a sum of the elastic force in the spring $F_n^e$ and the viscous component $F_n^d$:

$$ F_n = F_n^e + F_n^d $$

Presented research considers two elastic models—linear (LM) and nonlinear Hertz model (HM)—as components of the Kelvin–Voigt and Maxwell models. In the case of LM, the relation between the elastic normal force $F_n^e$ and penetration $u_n^e$ of outer particles surfaces is linear and it can be represented by the formula [17]:

$$ F_n^e = k_n u_n^e $$

where $k_n$ is the particles stiffness determined similarly to [17]:

$$ k_n = 4 \beta E r_{eff} $$

where $\beta$ is the scaling parameter, $E$ is Young’s modulus, $r_{eff}$ is the effective radius:

$$ r_{eff} = \frac{r_i r_j}{r_i + r_j} $$

where $r_i$ and $r_j$ are particles radii.

Alternatively, the elastic part of the normal contact force $F_n^e$ can be presented in the form of the Hertz interaction model, which is the most classical nonlinear model used in particle collisions:

$$ F_n^e = \frac{4}{3} E_{eff} \sqrt{r_{eff}} u_n^e \frac{1}{2} $$

where $E_{eff}$ is the effective modulus of elasticity defined in terms of the Young’s moduli, $E_i$ and $E_j$, and the Poisson’s ratios, $\nu_i$ and $\nu_j$, of the two contacting particles:

$$ \frac{1}{E_{eff}} = \frac{1 - \nu_i^2}{E_i} + \frac{1 - \nu_j^2}{E_j} $$

The normal stiffness $k_n$ of Hertz model depends on the particle penetration $u_n^e$ and it can be obtained as the derivative

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**Fig. 1** Rheological schemes of: a cohesionless contact model with friction, b viscoelastic model of sintering [16]
of the relationship (5):

\[ k_n = \frac{dF_n^e}{du_n^e} = 2E_{eff} \sqrt{r_{eff} u_n^e} \]  \hspace{1cm} (7)

Penetration for particles indicating a spherical shape \( u_n^e \) is given by following equation consistent for both linear and Hertz model:

\[ u_n^e = d - r_i(T) - r_j(T) = d - (r_i + r_j)(1 + \alpha \Delta T) \]  \hspace{1cm} (8)

where \( d \) is the distance between particles centers, \( \alpha \) is thermal expansion coefficient and \( \Delta T \) is temperature increment.

The second component of Kelvin–Voigt model is the viscous one \( F_n^{d} \). It can be assumed to be a linear function of the normal relative velocity \( v_m \):

\[ F_n^{d} = c_n v_m = 2\xi \sqrt{\frac{m_i m_j k_n}{m_i + m_j}} v_m \]  \hspace{1cm} (9)

where \( c_n \) is the viscosity coefficient given as a fraction \( \xi \) of the system of two rigid bodies with the masses of \( m_i \) and \( m_j \) connected with a spring with the stiffness \( k_n \), which is given by Eqs. (3) or (7) for linear and Hertz models, respectively.

The tangential force in the Kelvin–Voigt model has been calculated using an algorithm based on the Mindlin and Deresiewicz non-slip solution of the contact problem [18], which is commonly used in the framework of the DEM, cf. [19]. The tangential force \( F_s \) is calculated incrementally, and its increments are given by the following expression:

\[ F_s = k_s v_{rs} \Delta t \]  \hspace{1cm} (10)

where \( k_s \) is the tangential stiffness described in [20], \( v_{rs} \) is the relative tangential velocity and \( \Delta t \) is the time step.

The tangential stiffness \( k_s \) depends on the equivalent shear modulus \( G_{eff} \) and the particle overlap \( h \):

\[ k_s = 8G_{eff} \sqrt{r_{eff} u_n^e} \]  \hspace{1cm} (11)

The tangential force \( F_s \) is limited by the Coulomb friction:

\[ ||F_s|| \leq \mu |F_n| \]  \hspace{1cm} (12)

where \( \mu \) is the Coulomb friction coefficient.

The formulation of initial compaction model has considered only the elastic deformation of particles. Presented analysis concerns the relatively low values of external pressure and the hard and brittle NiAl material, thus the contribution of elastic deformation in the total one is a predominant. This effect has been studied in [20].

The viscoelastic model of sintering considers both elastic \( F_n^e \) and viscous \( F_n^v \) element connected in series (Fig. 1b). Presented Maxwell model indicates the equality of elastic and viscous forces and additive decomposition of the relative normal velocity between particles \( v_m \) into the elastic and viscous parts, \( v_{en}^e \) and \( v_{en}^v \), respectively. Taking into account following assumptions, we obtain the evolution equation for the force in the Maxwell branch:

\[ v_m = \frac{\dot{F}_n^e}{k_n} + \frac{F_n^v}{\eta} \]  \hspace{1cm} (13)

where \( F_n^v \) is the viscous force resulting from the mass transport mechanism of grain boundary diffusion during sintering process [6]:

\[ F_n^v = \eta v_m = \frac{\pi a^4}{8D_{eff}} v_m \]  \hspace{1cm} (14)

where \( \eta \) is the viscosity coefficient, \( a \) is the radius of cohesive neck and \( D_{eff} \) is the effective grain boundary diffusion coefficient:

\[ D_{eff} = \frac{D_{gb} \delta \Omega}{k_B T} \]  \hspace{1cm} (15)

where \( \delta \) is the thickness of the grain boundary, \( \Omega \) is atomic volume, \( k \) is the Boltzmann constant, \( T \) is the temperature and. \( D_{gb} \) is grain boundary diffusion coefficient dependent on temperature:

\[ D_{gb} = D_{0gb} \exp \left[ -\frac{\Delta H_{gb}}{RT} \right] \]  \hspace{1cm} (16)

where \( D_{0gb} \) is the pre-exponential factor of grain boundary diffusion, \( \Delta H_{gb} \) is the activation enthalpy of grain boundary diffusion, \( R \) is the gas constant.

The force in Maxwell branch is balanced by sintering driving force \( F_n^{sint} \) resulting from surface tension on particles grain boundary [6]:

\[ F_n^{sint} = -\pi \gamma_s \left[ 4r_{eff} \left( 1 - \cos \frac{\Psi}{2} \right) + a \sin \frac{\Psi}{2} \right] \]  \hspace{1cm} (17)

where \( \Psi \) is the dihedral angle and \( \gamma_s \) is the surface energy.

The initial neck radius \( a_0 \) depends on the initial penetration \( u_0 \) induced by the compaction. From simple geometrical considerations we have:

\[ a_0 = \sqrt{\frac{r_{eff} u_n^e}{2}} \]  \hspace{1cm} (18)
The growth of the radius of the interparticle grain boundary is governed by the following evolution law:

$$\dot{a} = -\frac{r_{\text{eff}}v_n}{a}$$  \hspace{1cm} (19)$$

The grain boundary radius $a$ grows until the sintering process is stopped. Its maximum at the equilibrium state is given by the following geometric relationship:

$$a_{\text{max}} = r_{\text{eff}} \sin \frac{\psi}{2}$$  \hspace{1cm} (20)$$

where $\psi$ is the dihedral angle determined according to the Young’s law which assumes that in the system consisting of two grains and a gas in the pore in the equilibrium we have equilibrium of surface tensions. The geometric parameters are defined in Fig. 2.

Following Martin et al. [21] the rotational motion of the particles and tangential interaction has been neglected in the present formulation of sintering. This should be favorable for particle rearrangements.

3 Numerical results and discussion

Analogously to work performed in [20], a detailed investigation of interaction of two equal NiAl particles (with radii $R = 10 \mu m$) under compression has been carried out using the two elastic contact models presented earlier. The purpose of this study was to compare the force–penetration relationships for different models and model parameters (Table 1). In order to estimate of the external pressure exerted on the particle assembly, which is illustrated graphically in Fig. 3, the equations of LM and HM (Eqs. 2 and 5) have been transformed by dividing both sides by $4R^2$:

$$\frac{F}{4R^2} = 2\beta E \frac{u_n^e}{2R}$$  \hspace{1cm} (21)$$

$$\frac{F}{4R^2} = \frac{1}{3} \frac{E}{1 - \nu^2} \left( \frac{u_n^e}{2R} \right)^3$$  \hspace{1cm} (22)$$

It can be seen in Fig. 4 that the HM predicts a softer behavior in the standard range of hot pressing pressure up to 50

![Table 1 Material parameters for NiAl particles](image)

| Material constant | Parameter value |
|-------------------|-----------------|
| Density, $\rho_{\text{theo}}$ | 5910 kg/m$^3$ |
| Young’s modulus, $E$ | 183 GPa |
| Poisson’s ratio, $\nu$ | 0.318 |
| Friction coefficient, $\mu$ | 0.02 |
| Damping coefficient, $\xi$ | 0.9 |
| Stiffness scaling parameter, $\beta$ | 0.5 |
| Thermal exp. coefficient, $\alpha$ | $11.5 \times 10^{-6}$ K$^{-1}$ |
| Mean atomic volume, $\Omega$ | $1.2 \times 10^{-29}$ m$^3$ |
| Pre-exp. factor of GB diffusion, $D_{0\text{gb}}$ | $2.55 \times 10^{-5}$ m$^2$/s |
| Activ. enthalpy of GB diffusion, $\Delta H_{\text{gb}}$ | 184 kJ/mol |
| GB width, $\delta$ | 0.5 nm |
| Surface energy, $\gamma$ | 1.57 J/m$^2$ |
| Dihedral angle, $\psi$ | 145° |

![Fig. 3 Particle settings for numerical studies of compression of two equal particles](image)
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Fig. 4 Force versus penetration curves for compression of two equal spheres for different elastic contact models

MPa. In the case of LM, it indicates much higher stiffness, thus it produces higher resistance for particle penetration in the standard range of hot pressing pressure. Presented micromechanical analysis can be helpful to explain the mechanism during DEM simulations of initial powder compaction and further sintering of large particle assembly.

Maintaining the original particle size and particle size distribution (Fig. 5) determined experimentally [20], a cylindrical container of diameter 200 μm has been filled with 1751 particles (Fig. 6). Due to the size of DE model, the temperature evolution is prescribed and uniformly distributed in the specimen (heat transfer is neglected) similarly as in [21, 22]. It has been assumed that such a reduced geometric model with real particles size represents correctly initial compaction and sintering process in a real specimen with diameter of 120 mm. Moreover, intermetallic NiAl particles indicate the spherical shape (Fig. 7). This particular feature of applied powder can be great advantage of application of discrete element method and further validation of experimental and numerical results.

The particle specimen has been used in simulations of the die compaction and sintering. The powder placed in the cylinder has been subjected to the uniaxial compression exerted by the top plate loaded with a linearly rising pressure. Figure 8 presents the temperature and pressure profiles of simulation in sintering temperature of 1400 °C, sintering time of 30 min and external pressure of 30 MPa. As it can be seen, the transition of DEM models (from KV to Maxwell) occurs at the 0.5 of the melting point which corresponds to activation of grain boundary diffusion processes. From this point, the sintering starts, which is accompanied by activation of sintering driving force.

The values of parameters has been determined by own reference studies presented in [23] and confirmed with experimental data giving good correspondence [24–26]. The
activation enthalpy of grain boundary diffusion, $\Delta H_{gb}$, has been treated as a fitting parameter. The obtained value of $\Delta H_{gb}$ of intermetallic material is in correspondence with experimental measurements [27] and the empirical approximation for BCC materials (NiAl) [28].

Figure 9 presents the evolution of relative density of NiAl specimen during initial powder compaction and pressure-assisted sintering. Moreover, the graph shows the experimental results obtained by own studies, which have been widely described in [16,20,29]. The whole simulation has been divided into subsequent stages: loading, heating, sintering, cooling and unloading. The results show that the discrete element model reproduces correctly macroscopic behavior of the material during each stages of hot pressing process. It can be seen the substantial growth of relative density during initial compaction (loading) and sintering stage just after transition from Kelvin–Voigt to Maxwell model. As it can be expected, the heating and cooling stages are accompanied by keeping the relative density at the same level.

Numerical simulations have been performed by both HM and LM as elastic part of Kelvin–Voigt and Maxwell models. Analyzing the simulation performed in 30 MPa of pressure, it can be seen visible change of material densification between HM and LM during the loading stage (Fig. 10). From the beginning we have a high densification rate for both models in the initial phase caused by particle rearrangement and the density changes slower in the later phase, at a higher density, when the rearrangement of the particles is more difficult. In the intermediate and final stage the deformation of the particles becomes a more important densification mechanism. The evolution of the relative density predicted by HM is similar to that determined experimentally in the contrast to LM. Due to the lower stiffness, the densification of HM specimen is higher and before heating and sintering process the material indicates the relative density close to the experimental one. Differences between the numerical results obtained with different models are relatively large. This is because the differences between the force-indentation curves predicted by the compared models in the range of contact pressure in our studies are relatively high, cf. Fig. 4.

Obtained results of LM have been performed by taking $\beta$ parameter as 0.5. Better agreement between results from LM
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4 Conclusions

This paper presents the numerical and experimental analysis of hot pressing of NiAl powder with an emphasis on the best possible representation of its main stages: initial powder compaction and pressure-assisted sintering. The numerical study has been performed within the discrete element framework. In the paper, an original viscoelastic model of hot pressing has been used. The present work has been aimed to compare the elastic linear and Hertz models as the components of discrete element models of initial powder compaction and pressure-assisted sintering. Numerical models have been validated using own experimental results. Microscopic effects (particle penetration) and macroscopic changes (relative density) have been compared. As the numerical results are quite similar in the sintering stage, the initial compaction (loading stage) indicates the substantial differences in the case of higher external pressure (30 MPa). Especially for these conditions, Hertz model is more realistic and gives better agreement with experimental results. Due to the higher stiffness, linear model shows less penetration relative to Hertz one, which was confirmed by simply analysis of two-particle compression.

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Appendix

The kinetics of sintering during experiments have been evaluated by the study of the densification change in time. The sintering processes in sintering temperature of $T_S = 1400 \, ^\circ\text{C}$ and external pressure of 5 and 30 MPa were interrupted at different time instants (measurement points) in order to study the evolution of density. The measurement points have been selected basing on the scheme in Fig. 11. The sintering degree was assessed based on the relative density, $\rho_{\text{rel}}$, defined as the ratio of the measured bulk (apparent) density $\rho$ to the theoretical density $\rho_{\text{theo}}$ for the fully dense material:

$$\rho_{\text{rel}} = \frac{\rho}{\rho_{\text{theo}}}$$

Results of density measurements are provided in Table 2.
Table 2 Experimental density measurements for sintering of the NiAl powder

| Temperature/pressure $T_s$ (°C)/$p$ (MPa) | Density measurement points |
|------------------------------------------|-----------------------------|
| 1400/5                                   | 0.788 0.804 0.887 0.902 0.907 0.922 |
| 1400/30                                  | 0.888 0.905 0.917 0.978 0.985 0.992 |

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