Large-scale shell-model analysis of the neutrinoless $\beta\beta$ decay of $^{48}$Ca

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We present the nuclear matrix element for the neutrinoless double-beta decay of $^{48}$Ca based on large-scale shell-model calculations including two harmonic oscillator shells ($sd$ and $pf$ shells). The excitation spectra of $^{48}$Ca and $^{48}$Ti, and the two-neutrino double-beta decay of $^{48}$Ca are reproduced in good agreement to experiment. We find that the neutrinoless double-beta decay nuclear matrix element is enhanced by about 30% compared to $pf$-shell calculations. This reduces the decay lifetime by almost a factor of two. The matrix-element increase is mostly due to pairing correlations associated with cross-shell $sd$-$pf$ excitations. We also investigate possible implications for heavier neutrinoless double-beta decay candidates.

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The observation of neutrino oscillations established the massive nature of neutrinos almost two decades ago [1]. Despite great progress in neutrino physics in recent years [2], some fundamental properties are still unknown, like the Dirac or Majorana neutrino nature (whether they are their own antiparticle), or the absolute neutrino mass-scale and hierarchy. The first question would be answered with the detection of neutrinoless double-beta ($0\nu\beta\beta$) decay. In this lepton-number violating process, a nucleus decays into its isobar with two less neutrons and two more protons, emitting two electrons and no (anti)neutrinos. Several international collaborations are running experiments to measure this process $^8$[3] or plan to do it in the near future $^7$[12], and have set impressive lower-limits for the $0\nu\beta\beta$ decay lifetimes, $\tau_{1/2}^{0\nu} > 10^{25}$ yr, for the most favourable cases.

In addition, $0\nu\beta\beta$ decay can determine the absolute neutrino masses and hierarchy if the nuclear matrix element (NME) of the transition, $M_{0\nu}$, is accurately known. The lifetime of the decay reads $^9$

$$\tau_{1/2}^{0\nu} \left( 0^+ \rightarrow 0^+_f \right) = \frac{1}{G_{0\nu}^2 |M_{0\nu}|^2 \left( \frac{m_{\beta\beta}}{m_e} \right)^2},$$

with $0^+_i$ ($0^+_f$) the initial (final) state, $G_{0\nu}$ a well-known phase-space factor $^{14}$, and $\left( m_{\beta\beta} \right)$ a combination of the absolute neutrino masses and the neutrino mixing matrix (the electron mass $m_e$ is introduced by convention).

Calculated NME values, however, differ by factors of two or three depending on the theoretical nuclear structure approaches used. This uncertainty severely limits the potential capability to determine the absolute neutrino masses with $0\nu\beta\beta$ decay. Among the NME calculations, shell-model results $^{13}$[17] are typically at the lower end, and it has been argued that this may be due to the relatively small configuration space that can be accessed by present shell-model codes $^{13}$. On the other hand, within the configuration space where the calculation is performed, the shell model can include various additional correlations compared to other approaches that yield larger NME values $^{13}$[21], like the quasiparticle random-phase approximation (QRPA) $^{22}$[24], the interacting boson model (IBM) $^{25}$, the energy density functional (EDF) $^{26}$[27], or the generator coordinate method (GCM) $^{28}$.

The doubly-magic $^{48}$Ca is the lightest isotope considered in $\beta\beta$ decay searches, including the CARVEL $^{29}$, CANDLES $^{30}$[31], and NEMO-III $^{32}$ experiments. Its $\beta\beta$ decay into $^{48}$Ti is ideally suited for shell-model calculations, which are very successful in this mass region for a wide variety of observables $^{33}$. In fact, the two-neutrino double-beta ($2\nu\beta\beta$) decay lifetime was predicted by a shell-model calculation $^{34}$ in very good agreement with the subsequent experimental detection $^{33}$.

In this Letter we present an improved calculation of the $0\nu\beta\beta$ decay NME for $^{48}$Ca based on the large-scale shell model in two harmonic oscillator shells ($sd$ and $pf$ shells). This significantly expands previous shell-model studies performed in the $pf$ shell $^{15}$[17][19] by increasing the number of single-particle orbitals from four to seven. We use the $M$-scheme shell-model code KSHELL $^{36}$, and allow up to $2\hbar\omega$ $sd$-$pf$ cross-shell excitations. The dimension of the largest calculation ($^{48}$Ti) is $2.0 \times 10^9$.

We use the shell-model SDPFMU effective interaction $^{48}$, which describes well the shell evolution and the spectroscopy of neutron-rich nuclei in the upper $sd$ shell. The $pf$-shell part of this interaction is based on the GXPF1B interaction, which accounts very successfully for the spectroscopy of $pf$-shell nuclei $^{38}$[39]. While the SDPFMU interaction works reasonably well, a slightly revised one, SDPFMU-db, is introduced by reducing the shell gap of $^{40}$Ca to 5.8 MeV so as to reproduce the ob-
served $0^+_2$ level of $^{48}$Ca. The two-proton transfer reaction experiment [40] shows a large cross section to the $0^+_2$ state of $^{48}$Ca, suggesting sizable proton excitations from the $sd$ shell. The $0^+_2$ state obtained with the SDPFMU-db interaction shows 1.64 protons in the $pf$ shell consistently with this property, whereas the SDPFMU result finds only 0.22. The new SDPFMU-db interaction thus gives an improved description compared to SDPFMU.

Figure 1 shows the excitation spectra of $^{48}$Ca and $^{48}$Ti obtained with SDPFMU-db, which are in good agreement to experiment. The SDPFMU spectra is generally of similar quality, with the $0^+_2$ level of $^{48}$Ca too high by 200 keV. In contrast, a $pf$-shell calculation with GXPF1B gives the $0^+_2$ level in $^{48}$Ca 1.3 MeV higher than the experimental one. For the $0^+_2$ state in $^{48}$Ti, the $sd pf$-shell calculation with SDPFMU-db gives 1.0 MeV higher excitation energy than experiment, probably due to missing $4\hbar\omega$ excitations. The $2\hbar\omega$ components in the ground states of $^{48}$Ca and $^{48}$Ti are 22% and 33% for SDPFMU-db (14% and 20% for SDPFMU). Such sizable $2\hbar\omega$ excitations suggest that these interactions in the $sd pf$-configuration space capture sufficiently well cross-shell $sd pf$ excitations.

First we study the $2\nu\beta\beta$ decay of $^{48}$Ca. We calculate the Gamow-Teller $\beta^+$ and $\beta^-$ strengths, and compare them to experiments for the energy range up to 5 MeV [42, 43], so that we can extract the appropriate quenching factor $q$ of the $\sigma\tau$ operator for each calculation. We find $q = 0.71$ for both $sd pf$ interactions, and $q = 0.74$ for the $pf$-shell interaction, in accordance with previous $pf$-shell studies [33]. The similar quenching factor shows that it does not depend on missing $sd pf$ correlations. Then we calculate $2\nu\beta\beta$ decay matrix elements by summing contributions from 100 virtual $1^+$ intermediate states in $^{48}$Sc, and obtain $M^{2\nu} = 0.051 (0.045)$ MeV$^{-1}$ with the SDPFMU-db (SDPFMU) interaction, in good agreement with experiment, $M^{2\nu} = 0.046\pm0.004$ MeV$^{-1}$ [44]. In the $pf$-shell calculation with GXPF1B the result is very similar, $M^{2\nu} = 0.052$ MeV$^{-1}$, reflecting low sensitivity to the size of the shell-model configuration space in $2\nu\beta\beta$ decay. This is in contrast to the high sensitivity observed in Ref. [45]. The difference arises because in the present calculations all spin-orbit partners are always included.

We then calculate the $^{48}$Ca $0\nu\beta\beta$ decay NME in the $sd pf$ space including up to $2\hbar\omega$ configurations. It is given in the closure approximation as [13]

$$M^{0\nu} = \langle 0^+_2 | J^0 \rangle = M^{0\nu}_{GT} - \frac{q^2}{g_A} M^{0\nu}_F + M^{0\nu}_T,$$

with Gamow-Teller ($M^{0\nu}_{GT}$), Fermi ($M^{0\nu}_F$) and tensor ($M^{0\nu}_T$) terms classified according to the spin structure of the operator. The vector and axial coupling constants are taken to be $g_V = 1$ and $g_A = 1.27$, respectively. We set the closure parameter to $\langle E \rangle = 0.5$ MeV, found appropriate in the $pf$-shell calculation of Ref. [17]. We consider the inclusion of Argonne- and CD-Bonn-type short range correlations [16]. Two-body current contributions to the transition operator [17] are not included. The possible quenching of the $\sigma\tau$ operator in $0\nu\beta\beta$ decay is the matter of discussion [18], because compared to $2\nu\beta\beta$ decay the momentum transfer is larger, and the virtual intermediate states of the transition include additional multipoolarities. Therefore, similarly to most previous calculations, we do not quench the $\sigma\tau$ operator for $0\nu\beta\beta$ decay. A detailed discussion on the $0\nu\beta\beta$ decay operator $\tilde J^{0\nu}$ can be found in Ref. [16].
TABLE I. NME value for the \( ^{48}\text{Ca} \, 0\nu\beta\beta \) decay. The pf-shell calculation with GXPF1B is compared to the \( sdpf \, 2\hbar\omega \) results obtained with the SDPFMU-db and SDPFMU interactions. Total values (\( M^{\text{tot}} \)) are shown together with Gamow-Teller (\( M^{\text{GT}} \)), Fermi (\( M^{\text{F}} \)) and Tensor (\( M^{\text{T}} \)) parts. Argonne- and CD-Bonn-type short-range correlations (SRC) are considered.

| SRC      | \( M^{\text{GT}} \) | \( M^{\text{F}} \) | \( M^{\text{T}} \) | \( M^{\text{tot}} \) | \( M^{\text{GT}} \) | \( M^{\text{F}} \) | \( M^{\text{T}} \) | \( M^{\text{tot}} \) |
|----------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| None     | 0.776             | -0.216            | -0.077            | 0.833             | 0.997             | -0.304            | -0.067            | 1.118             |
| CD-Bonn  | 0.809             | -0.233            | -0.074            | 0.880             | 1.045             | -0.327            | -0.065            | 1.183             |
| Argonne  | 0.743             | -0.213            | -0.075            | 0.801             | 0.953             | -0.300            | -0.065            | 1.073             |

The calculated values of NME are shown in Table I. The Gamow-Teller and Fermi parts, \( M^{\text{GT}} \) and \( M^{\text{F}} \), are enhanced in the \( 2\hbar\omega \) calculations by about 20% - 40% compared to the pf-shell calculations. The largest values are given by the SDPFMU-db interaction, which allows a stronger mixing of \( 2\hbar\omega \) configurations in the mother and daughter nuclei. The tensor contribution, \( M^{\text{T}} \), is almost unaffected by enlarging the configuration space. The 10% difference between the NME values obtained with the two \( sdpf \) shell-model interactions is similar to the uncertainty obtained with different pf-shell interactions [18].

Additional correlations beyond the sd-pf space are potentially relevant for the \( ^{48}\text{Ca} \) NME. To evaluate its effect, we have performed a \( 2\hbar\omega \) calculation including the pf and sdg shells, using the interaction from Ref. [48], which describes well negative parity states in neutron-rich calcium isotopes (sensitive to \( pf\text{-sdg} \) excitations). We find a small 5% change in the NME compared to the pf-shell result, consistent with the small cross-shell pf-sdg excitations (about 2%) in \( ^{48}\text{Ca} \) and \( ^{48}\text{Ti} \). This suggests that the sd-pf space captures the most relevant correlations beyond the pf shell for the \( ^{48}\text{Ca} \) NME.

Figure 2 compares different NME calculations for \( ^{48}\text{Ca} \). The total NME value in the \( sdpf \) configuration space, \( M^{\nu} = 0.96 - 1.18 \), is about 30% larger than the pf-shell GXPF1B result or other shell-model pf-shell values \( M^{\nu} = 0.78 - 0.92 \). This enhancement is important consequences for \( ^{48}\text{Ca} \, 0\nu\beta\beta \) decay experiments, as the decay lifetime is almost halved. The present NME value is 15% smaller than the result obtained by a pf-shell calculation including perturbatively the effect of the orbitals outside the pf configuration space, \( M^{\nu} = 1.30 \). In contrast, Fig. 3 shows that the present NME value is considerably smaller than IBM [22], non-relativistic [26] or relativistic [27] EDF values, and significantly larger than the QRPA result [22].

In the following we analyse the NME to understand the mechanisms responsible for the enhancement found in the \( 2\hbar\omega \) calculations, and explore possible implications for heavier \( 0\nu\beta\beta \) decay candidates. The operator for NME can be decomposed in terms of the angular momentum and parity, \( J^\pi \), to which the two-decaying neutrons are coupled [18]:

\[
M^{\nu} = \sum_{\pi} \langle 0^+_\pi | \sum_{i,j,k,l} M_{ij,kl}^{\nu} \frac{1}{2h} \hat{a}^\dagger_i \hat{a}^\dagger_j \hat{a}_k \hat{a}^\dagger_l | 0^+_i \rangle,
\]

where \( i,j,k,l \) label single-particle orbitals. This decomposition is shown in Fig. 3 for \( 0\hbar\omega \) (pf) and \( 2\hbar\omega \) (sdpf) calculations. The leading contribution to \( 0\nu\beta\beta \) decay comes from \( 0^+ \)-coupled pairs, while other \( J^\pi \) combinations suppress the NME. Figure 3 shows that the main difference between the \( 0\hbar\omega \) and \( 2\hbar\omega \) results is a 20% increase in the contributions of \( 0^+ \) pairs. In addition only the \( 2\hbar\omega \) calculation allows for negative-parity pairs, but its contribution is small. As also suggested in Ref. [51], these findings indicate that the NME is enhanced by the pairing correlations, which induce \( 0^+ \)-pair excitations, introduced by the additional sd-shell orbitals.

We further decompose the NME in terms of the orbitals (sd or pf shell) occupied by the two \( ^{48}\text{Ca} \) neutrons and two \( ^{48}\text{Ti} \) protons involved in the decay:

\[
M^{\nu} = M_1^{\nu} + M_2^{\nu} + M_3^{\nu} + M_4^{\nu} + M_5^{\nu},
\]
with the \( M_{0\nu} \) components, sketched in Fig. 4 defined as

\[
M_{1\nu} = \langle 0^+_f | \hat{O}^{\nu}_0 (p_{pf} p_{pf}; n_{sd} n_{pf}) | 0^+_i \rangle,
\]

\[
M_{2\nu} = \langle 0^+_f | \hat{O}^{\nu}_0 (p_{pf} p_{pf}; n_{sd} n_{pf}) | 0^+_i \rangle,
\]

\[
M_{3\nu} = \langle 0^+_f | \hat{O}^{\nu}_0 (p_s p_{sd}; n_{sd} n_{pf}) | 0^+_i \rangle,
\]

\[
M_{4\nu} = \langle 0^+_f | \hat{O}^{\nu}_0 (p_{sd} p_{sd}; n_{sd} n_{pf}) | 0^+_i \rangle,
\]

\[
M_{5\nu} = \langle 0^+_f | \hat{O}^{\nu}_0 (p_{sd} p_{sd}; n_{sd} n_{pf}) | 0^+_i \rangle,
\]

where \( n_i (p_i) \) stands for neutrons (protons) in the \( i \) shell of \( ^{48}\text{Ca} \) (\( ^{48}\text{Ti} \)). Table II shows the different components in Eq. (4) for the SDPFMU-db calculation, as well as their decomposition in terms of the \( J^\pi \) of the decaying neutron pair [cf. Eq. (3)]. \( M_{1\nu} \), the only term allowed in the 0\( \omega \) calculation, is very similar in the \( pf \) and \( sd-pf \) spaces. On the contrary, \( M_{2\nu} \), \( M_{3\nu} \) and \( M_{4\nu} \) require 2\( \omega \) excitations in the mother and/or daughter nuclei (see Fig. 4). In fact, these terms are responsible for the enhancement of the NME in the \( sd-pf \) configuration space. Table II shows that, for \( M_{2\nu} \), \( M_{3\nu} \) and \( M_{4\nu} \), the contribution of \( 0^+ \) partners is dominant, about three times larger in magnitude than the other \( J^\pi \) pairs. This is in contrast to \( M_{1\nu} \), or \( pf \)-shell calculations, where the contribution of the \( 0^+ \) terms is 30% larger than the other \( J^\pi \) pairs. These results confirm that the pairing correlations inducing neutron and proton cross-shell \( sd-pf \) excitations are responsible for the enhancement of the NME.

The remaining term \( M_{5\nu} \) requires the two nucleons being in different orbitals (see Fig. 4, diagram v). These two neutrons cannot be coupled to \( J^\pi = 0^+ \), and are not involved in the \( 0^+ \) pair contributions. They instead produce strong cancellations, as shown in Table II consistently with the \( J^\pi \neq 0^+ \) contributions in Fig. 3.

The above discussion suggests that the enlargement of the model space produces two competing mechanisms to be considered in all \( 0\nu\beta\beta \) decays. On the one hand, additional pairing correlations in the mother and daughter nuclei, enhanced by two-particle–two-hole (2p-2h) excitations with respect to the original configuration space, increase the NME values, as seen in \( M_{1\nu} - M_{5\nu} \) for the \( ^{48}\text{Ca} \) decay. On the other hand, excitations in the initial and final nuclei outside the original space can increase \( J^\pi \neq 0^+ \) contributions as well. Assuming that these follow the same trends as in Fig. 3, this second mechanism will reduce the NME value, as seen in \( M_{5\nu} \) for \( ^{48}\text{Ca} \). Important contributions come from one-particle–one-hole (1p-1h) excitations. For the \( ^{48}\text{Ca} \) decay, however, 1p-1h excitations always change parity and do not contribute to \( 0^+ \) ground states, and this mechanism remains rather modest.

For heavier nuclei, these two competing effects need to be calculated in detail. While pairing correlations are most important for \( 0\nu\beta\beta \) decay, 1p-1h type excitations have smaller unperturbed energy difference than 2p-2h excitations, and can be sizable. The balance between the two mechanisms will determine the NME. For example, Ref. [50] found a 35% smaller NME value for \( ^{136}\text{Xe} \) when including up to 1p-1h excitations into the missing spin-orbit partners in the original shell-model configuration space. In contrast, Ref. [52] found a 20% increase in the \( ^{82}\text{Se} \) and \( ^{136}\text{Xe} \) NME values when considering 2p-2h excitations. A related competition between opposite-sign contributions was very recently suggested in Ref. [53] for \( ^{76}\text{Ge} \).

Finally, we estimate the NME beyond 2\( \omega \) \( sd-pf \) excitations. An exact diagonalization in the full \( sd-pf \) configuration space is not feasible with present computing capabilities. However this space can be handled in a seniority-zero approximation, that is, in a basis with all nucleons coupled in like-particle \( J^\pi = 0^+ \) pairs. In a given configuration space the NME is maximum in this limit, as higher seniority components only reduce their value [49]. A full \( sd-pf \) seniority-zero calculation with SDPFMU-db, performed with the \( J \)-coupled code NATHAN [33], shows that components beyond 2\( \omega \) excitations are negligible (less than 0.5%) in both \( ^{48}\text{Ca} \) and \( ^{48}\text{Ti} \). That is, \( N\omega \) excitations (\( N > 2 \)) only contribute to high-seniorities, thus they can only reduce the NME. This implies that the \( sd-pf \) pairing correlations enhancing \( 0\nu\beta\beta \) decay are completely captured by the 2\( \omega \) configurations included in the present calculations, and con-

| TABLE II. NME decomposition of Eq. (4), for a \( sd-pf \) 2\( \omega \) SDPFMU-db calculation without short-range correlations. The total value is shown along with the contributions of \( J^\pi = 0^+ \) and all remaining pairs. |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| \( M_{1\nu} \)   | \( M_{2\nu} \)   | \( M_{3\nu} \)   | \( M_{4\nu} \)   | \( M_{5\nu} \)   |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 0.915           | 0.168           | 0.269           | 0.220           | −0.454          |
| 4.193           | 0.364           | 0.379           | 0.255           | 0.000           |
| −3.278          | −0.196          | −0.109          | −0.035          | −0.454          |

FIG. 4. (color online) Diagrams associated with the NME decomposition in Eq. (4), classified in terms of the \( sd- \) or \( pf- \) shell orbitals occupied by the decaying neutrons (open circles) and created protons (filled circles). Initial (final) stands for \( ^{48}\text{Ca} \) (\( ^{48}\text{Ti} \)). Diagrams i-v correspond to \( M_{1\nu} - M_{5\nu} \), respectively.
sequently the results obtained in this work provide an upper-bound for the NME value in the full sd pf configuration space.

In summary, we have carried out large-scale shell-model calculations of $^{48}$Ca and $^{48}$Ti, for the first time including up to $2\hbar\omega$ excitations in the sd pf space. The excitation spectra of $^{48}$Ca and $^{48}$Ti, and the $2\nu\beta\beta$ decay of $^{48}$Ca are reproduced in good agreement to experiment. We find different sensitivities to the configuration-space size in $\beta$ decays; while the $2\nu\beta\beta$ decay NME is similar in the pf and sd pf shells, the $0\nu\beta\beta$ decay NME increases by about 30% to $M^{0\nu\beta\beta}\approx 1.1$. The NME enhancement, which almost halves the associated decay life time, is due to cross-shell sd pf pairing correlations. A seniority analysis shows that pairing effects in the sd pf space are completely captured by the $2\hbar\omega$ calculations, so that the present result suggests an upper value for the NME in the full sd pf space.

Correlations outside the sd-pf space have been evaluated to be small. Beyond present shell-model capabilities, they can be estimated with MBPT or GCM techniques, complementing the present result. Further efforts are needed to set a more definitive value for the $^{48}$Ca $0\nu\beta\beta$ decay NME, for instance by further enlarging the model space, improving the closure approximation, introducing two-body currents and/or a renormalization of the operator for the model space. Future plans include calculating NMEs for heavier $\nu\beta\beta$ decay candidates in extended shell-model configuration spaces. For these isotopes, competition between 1p-1h and pairing-like 2p-2h excitations in the present context will be of much interest, and their subtle balance should be evaluated precisely to obtain reliable NMEs.

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