Motion Analysis of Hexapod Robot with Eccentric Wheels

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Abstract
A new concept for developing hexapod robots using eccentric wheels is proposed in this work. Compared with the RHex robot, the proposed hexapod robot can greatly reduce the bumping of the robot body in both smooth ground and rocky terrain. Also, the developed hexapod robot possesses significant advantages over those with common circular wheels in traversing rocky and uneven terrain. Also, the control of the proposed hexapod robot is simple because each eccentric wheel has only one degree of freedom. This work focuses on the kinematics analysis of the proposed hexapod robot. Two types of gaits respectively named as the alternating tripod gait and the hexapod gait are proposed. With the alternating tripod gait, the robot can move continuously. But the hexapod gait is helpful in overcoming the resistant torque caused by the weight on the eccentric wheels. Besides, the effect of the eccentricity on the motion of the robot is analysed. The proposed hexapod robot can be used to detect the gas in underground mines.

Keywords: Hexapod robot; Eccentric wheel; Gas detection; Tripod gait; Hexapod gait; Motion analysis

Introduction
A hexapod robot is a robot that has six legs to walk or move. It is well known that a robot can be statically stable on three or more legs. Since a hexapod robot has several legs, it has a great deal of flexibility in how it can move. If some legs become disabled, the robot may still be able to walk. Furthermore, not all of the robot’s legs are needed for stability; other legs are free to reach new foot placements or manipulate a payload. Also, the robot is easily programmed to move around because it can be configured to many types of gaits. There are various designs of hexapod robots with certain functions and advantages. For instance, hexapod robots have been sketched in eight different designs, and every design has its different criteria, specifications, shapes, advantages and disadvantages [1].

Many hexapod robots are biologically inspired by hexapoda locomotion [2-10]. Hexapods may be used to test biological theories about insect locomotion, motor control, and neurobiology. Hexapod designs vary in leg arrangement. Insect inspired robots are typically laterally symmetric. Typically, individual legs range from two to six degrees of freedom. Hexapod feet are typically pointed, but can also be tipped with adhesive material to help climbing walls or wheels so the robot can drive quickly when the ground is flat. The researchers [6] developed a sixlegged walking robot that is capable of basic mobility tasks such as walking forward, backward, rotating in place and raising or lowering the body height. The authors described the first implementation of the neurobiological mechanisms in a physical hexapod robot that is capable of generating adaptive stepping actions with the same underlying control method as an insect [7].

Hexapod robots can be developed to undertake some interesting tasks. For instance, a kind of six-legged robot was developed by Ramesh and Kumar to monitor and perform household tasks independently. The robot legs movement or method of forward motion using legs is called gait. Most often, a hexapod robot is controlled by gait, which allow the robot to move forward, turn, and perhaps side-step. One important issue in the development of hexapod robots is to consider the motion and develop proper gaits for the robots [10-22]. For instance, feasible gait patterns were developed by Belter and Skrzypczynski [10] to control a real hexapod walking robot. The use of hybrid genetic gravitational algorithm for generation of the gait for the hexapod robot was described by Seljanko [12].

Gaits for a hexapod robot are often stable, even in slightly rocky and uneven terrain. There are varieties of gaits available. Some of the most common gaits are as follows: (1) alternating tripod gait; (2) quadruped; and (3) crawl. The famous gait used by hexapod robot is the tripod gait. In the tripod gait, there are always three feet of hexapod in contact with the ground. For example, the hexapods robots developed, were used this alternating tripod gait [17-20].

Motion of a hexapod robot may also be nongaited, which means the sequence of leg motions is not fixed, but rather chosen by the computer in response to the sensed environment. This may be most helpful in very rocky terrain, but existing techniques for motion planning are computationally expensive.

As mentioned by Rashid et al. [1], hexapod robots can be designed with certain functions and advantages. Most hexapod robots were designed with only legs. Some hexapod robots were designed with manoeuvrable wheels or combination of legs and wheels [5]. In general, the movement of robot by legs is good for rocky and uneven terrain. But the movement of robot by the wheels is faster than the movement of the robot by legs [1]. The RHex robot could be an exception because the motion of its six C shape legs is similar to the rotation of wheels [2-4].

The RHex robot has a lot of excellent performance such as (1) running on reasonably flat, natural terrain at speeds up to 6 body lengths per second (just over 2.7 m/s); (2) climbing a wide range of stairs and slopes up to 45 degrees; (3) traversing obstacles as high as...
20 cm (about twice RHex’s leg clearance) and badly broken terrain with large rocks or obstacles; (4) walking and running upside down; (5) flipping itself over to recover nominal body orientation; (6) leaping across ditches up to 30 cm wide.

However, the RHex robot is not suitable for working in underground mines to detect gas. The reasons are: (1) Its violent bumping and collision of its body with the rocky terrain will be easy to cause sparks leading to explosion in detecting the gas in underground mines. (2) In such an application, the power of every motor is quite limited (only 3 watts). The motors used for the RHex robot cannot be so small. Otherwise, its powerful performance will be greatly compromised. (3) The gas detective robot has a sensor on top of a stick about 1.5 meters high, which stretches up from the robot body. So, walking and running upside down, flipping and leaping are not allowed even if these are good performance of the RHex robot.

In order to develop such a gas detective robot working in underground mines, a new concept for developing hexapod robots using eccentric wheels is proposed in this work. Compared with the RHex robot, the proposed hexapod robot can greatly reduce the bumping of the robot body in both smooth ground and rocky terrain. Also, the developed hexapod robot possesses significant advantages over those with common circular wheels in traversing rocky and uneven terrain. Also, the control of the proposed hexapod robot is simple because each eccentric wheel has only one degree of freedom.

This work focuses on the kinematics analysis of the proposed hexapod robot. In Section 2, the prototype of the proposed hexapot robot with eccentric wheels is briefly introduced. In Section 3, the tripod gait for both straight walking and turning is proposed. In Section 4, the hexapot gait is described. In Section 5, the motion analysis of the proposed hexapot robot is conducted. In Section 6, the advantages of the proposed hexapot robot over both RHex robot and those with common circular wheels in traversing rocky and uneven terrain are given in several situations. Finally in Section 7, some conclusions and discussions are summarized.

Hexapod Robot with Eccentric Wheels

As shown in Figure 1, the developed hexapod robot with eccentric wheels is traversing an obstacle. This robot is actually symmetric in three directions. First, the robot is symmetric about the central vertical section plane in the moving direction: three eccentric wheels (#1, #2 and #3) at the left-hand side and three eccentric wheels (#4, #5 and #6) at the right-hand side. Second, the robot is symmetric about the horizontal section plane passing through the axes of the middle eccentric wheels (#2 and #5). Third, the robot is also symmetric about the horizontal section plane passing through the axes of all six eccentric wheels. In other words, the upper and down parts of the robot are also symmetric about the horizontal section plane passing through the axes of all six eccentric wheels. Hence, the robot is able to walk even if it is overturned. In terms of structure, the developed hexapod robot is quite similar to the RHex robot in which open curved legs were used.

All six eccentric wheels have the same geometric parameters. Every eccentric wheel is driven independently by its own motor. In other words, the axes of wheels #1 and #4 (or wheels #2 and #5, or wheels #3 and #6) are concentric, but not the same. The backward motion of the robot is similar to the forward motion. Every eccentric wheel as shown in Figure 1 does not touch the ground all the time during the walking of the robot. The motion status of the eccentric wheel falls into two phases: (1) supporting phase, and (2) idling phase, as shown in Figure 2, where O is the center of the eccentric wheel; Q is the axis of the eccentric wheel (i.e., the revolute joint); P1 is the first contact point of the supporting phase during the forward walking; P2 is the contact point on the diameter passing through the axis Q of the wheel; P3 is the last contact point of the supporting phase during the forward walking. In other words, the supporting phase starts at the first contact point P1 and ends at the last contact point P3. Then, the idling phase starts after the contact point P1, and ends when the eccentric wheel contacts the ground at P1 again. Obviously, P1 and P3 are two transition contact points.

Tripod Gait

Straight walking

Referring to Figure 1, the six eccentric wheeled legs of the developed hexapod robot can be classified into two groups: Group A consists of wheels (#1, #3 and #5) which form a triangle. Group B consists of wheels (#2, #4 and #6) which form another triangle. The alternating tripod gait for the developed hexapod robot can be shown in Figure 3 and described as follows:

- Status 1 (initial status): All six eccentric wheels contact the ground at their transition points. The three wheels (#1, #3 and #5) of Group A contact the ground at contact point P1. But the three wheels (#2, #4 and #6) of Group B contact the ground at P2.
- Status 2: The three wheels (#1, #3 and #5) of Group A enter their supporting phase. But the three wheels (#2, #4 and #6) of Group B enter their idling phase. The rotation speed for the supporting phase is ωs and the rotation speed for the idling phase is ωi.
- Status 3: This is a transition status. Again, all six eccentric wheels contact the ground at their transition points. The three wheels (#1, #3 and #5) of Group A contact the ground at P3. But the three wheels (#2, #4 and #6) of Group B contact the ground at P1.
- Status 4: The three wheels (#1, #3 and #5) of Group A enter their idling phase. But the three wheels (#2, #4 and #6) of Group B enter their supporting phase.
- Status 5: Again, all six eccentric wheels contact the ground at their transition points. Just as Status 1, the three wheels (#1, #3 and #5) of Group A contact the ground at P1. But the three wheels (#2, #4 and #6) of Group B contact the ground at P2.

As Status 5 is exactly the same as Status 1, the total number of statuses in one cycle of the tripod gait for straight walking is four: two moving statuses and two transition statuses.

Turning

It is not enough for a robot to just move back and forth along a
straight line if it is required to undertake a specific task. In other words, the robot should have the ability to change its moving direction. Taking the left turn as an example, the alternating tripod gait can be shown in Figure 4 and described as follows:

• Status 1 (initial status): All six eccentric wheels contact the ground at their transition points. The four end wheels (#1, #3, #4 and #6) contact the ground at P3. But the two middle wheels (#2 and #5) contact the ground at P1.

• Status 2: The three wheels (#1, #3 and #5) of Group A enter their supporting phase. The rotation speed of two end wheels (#1 and #3) at the left-hand side is $-\omega_s$. Their contact points start from P3 and pass the shorter circular arc $\overparen{P3P1}$ of the wheel before reaching P1. As a result, the left-hand side of the robot obtains a backward speed. But the rotation speed of the middle wheel (#5) at the right-hand side is $\omega_s$. Its contact point starts from P1 and passes the shorter circular arc $\overparen{P1P3}$ of the wheel before reaching P3. As a result, the right-hand side of the robot obtains a forward speed. As the left-hand side of the robot obtains a backward speed and the right-hand side of the robot obtains a forward speed, the robot is turning left.

In the meantime, the three wheels (#2, #4 and #6) of Group B enter their idling phase. The rotation speed of the middle wheel (#2) at the left-hand side is $-\omega_i$. It starts from P1 and passes the longer circular arc $\overparen{P1P2}$ of the wheel before reaching P2. But the rotation speed of two end wheels (#4 and #6) at the right-hand side is $\omega_i$. They start from P3 and pass the longer circular arc $\overparen{P3P2}$ of the wheels before reaching P1.

• Status 3: This is a transition status. Again, all six eccentric wheels contact the ground at their transition points. But now, the four end wheels (#1, #3, #4 and #6) contact the ground at P1. The two middle wheels (#2 and #5) contact the ground at P3.

• Status 4: The three wheels (#1, #3, and #5) of Group A enter their idling phase. The rotation speed of two end wheels (#1 and #3) at the left-hand side is $-\omega_s$. Their contact points start from P3 and pass the shorter circular arc $\overparen{P3P1}$ of the wheel before reaching P1. As a result, the left-hand side of the robot obtains a backward speed. But the rotation speed of the middle wheel (#5) at the right-hand side is $\omega_s$. Its contact point starts from P1 and passes the shorter circular arc $\overparen{P1P3}$ of the wheel before reaching P3. As a result, the right-hand side of the robot obtains a forward speed. As the left-hand side of the robot obtains a backward speed and the right-hand side of the robot obtains a forward speed, the robot is turning left.
Figure 4: The tripod gait for left turn.

Figure 5: The torque caused by the weight.

Figure 6: The hexapod gait for straight walking.
• Status 5: Again, all six eccentric wheels contact the ground at their transition points. Just as Status 1, the four end wheels (#1, #3, #4 and #6) contact the ground at P₆. But the two middle wheels (#2, #5) contact the ground at P₅.

As Status 5 is exactly the same as Status 1, the total number of statuses in one cycle of the tripod gait for turning is also four: two moving statuses and two transition statuses.

It can be seen that for the left turn, no matter in supporting phase or idling phase, the rotation speed of each wheel at the left-hand side of the robot is negative. But the rotation speed of each wheel at the right-hand side of the robot is positive. It can be easily deduced that for the right turn, the rotation speed of each wheel at the left-hand side of the robot will be positive. But the rotation speed of each wheel at the right-hand side of the robot will be negative.

There are some similarity and differences between the gait for straight walking and the gait for turning. Similarity: In each case, when the three wheels of Group A form a triangle at their supporting phase, the three wheels of Group B also form another triangle at their idling phase. After that, when the three wheels of Group A form a triangle at their idling phase, the three wheels of Group B also form another triangle at their supporting phase. This is why both gaits are called as alternating tripod gaits.

Difference: In the gait for straight walking, the three wheels of each group stand at the same transition contact point (Pᵢ or Pⱼ) at each transition status. The rotation speed of every wheel at the moving statuses is always positive. But in the gait for turning, the three wheels of the same group do not stand at the same transition contact point at the transition statuses. For instance, if the wheels (#1 and #3) at the left-hand side of the robot stand at P₁, the wheel (#5) at the right-hand side stands at P₃. Also, the sign of the rotation speed of the wheels at the left-hand side of the robot is different from the wheels at the right-hand side.

Hexapod Gait

As mentioned in the introduction, the proposed hexapod robot can be used as the mining robot for detecting the gas in underground mines. Hence, the power of the motors is quite small. Otherwise, it would be easy to cause sparks that could lead to explosion. On the other hand, the weight of the robot causes a resistant torque on the eccentric wheel as shown in Figure 5a because of the eccentricity. (Of course, when the axis Q lies at the other side of the vertical diameter through the center O, the torque caused by the weight becomes a kind of power source as shown in Figure 5b. The n in Figure 5 is the number of wheels contacting the ground at the same time. For the tripod gait, n=3. In order to reduce this resistant torque caused by the weight, one solution is to increase the number n of the wheels contacting the ground. If we can make all six wheels to contact the ground at the same time (i.e., n=6), the resistant torque caused by the weight on the wheel will decrease by half. To this end, the hexapod gait is proposed in this section.

Straight walking

The hexapod gait for the developed hexapod robot can be shown in Figure 6 and described as follows:

• Status 1 (initial status): All six eccentric wheels contact the ground at their transition points P₁.
• Status 2: All six wheels enter their supporting phase. This is a moving status.
• Status 3: All six eccentric wheels contact the ground at their transition points Pᵢ. This is a transition status.
• Status 4: The three wheels (#1, #3 and #5) of Group A enter their idling phase. But the three wheels (#2, #4 and #6) of Group B keep their poses at their transition points Pᵢ. This is an adjusting status.
• Status 5: The three wheels (#1, #3 and #5) of Group.

A contact the ground at their transition points Pᵢ. But the three wheels (#2, #4 and #6) of Group B still keep their poses at their transition points Pᵢ. This is a transition status.

• Status 6: The three wheels (#1, #3 and #5) of Group A keep their poses at their transition points Pᵢ. But the three wheels (#2, #4 and #6) of Group B enter their idling phase. This is an adjusting status.
• Status 7: All six eccentric wheels contact the ground at their transition points Pᵢ. This is a transition status, which is exactly the same as Status 1.

As Status 7 is exactly the same as Status 1, the total number of statuses in one cycle of the hexapod gait for straight walking is six: one moving status, two adjusting statuses and three transition statuses.

Turning

Similarly, the hexapod gait for turning also falls into several statuses. Taking the left turn as an example, the hexapod gait can be shown in Figure 7 and described as follows:

• Status 1 (initial status): All six eccentric wheels contact the ground at their transition points. The three wheels (#1, #2 and #3) at the left-hand side contact the ground at P₁. But the three wheels (#4, #5 and #6) at the right-hand side contact the ground at P₆.
• Status 2: All six wheels enter their supporting phase. The rotation speed for the three wheels (#1, #2 and #3) at the left-hand side is −ω₁. So, the left-hand side of the robot obtains a backward speed. But the rotation speed for the three wheels (#4, #5 and #6) at the right-hand side is ω₆. So, the right-hand side of the robot obtains a forward speed. As the left-hand side obtains a backward speed and the right-hand side obtains a forward speed, the robot turns to the left. Hence, this status is a turning status.
• Status 3: All six eccentric wheels contact the ground at their transition points. The three wheels (#1, #2 and #3) at the left-hand side contact the ground at P₁. But the three wheels (#4, #5 and #6) at the right-hand side contact the ground at P₆. This is a transition status.
• Status 4: The three wheels (#1, #3 and #5) of Group.

A enter their idling phase. The rotation speed of the two wheels (#1 and #3) at the left-hand side is −ω₁. But the rotation speed of the wheel (#5) at the right-hand side is ω₅. The three wheels (#2, #4 and #6) of Group B keep their poses. This is an adjusting status.
• Status 5: All six eccentric wheels contact the ground at their transition points. The four end wheels (#1, #3, #4 and #6) contact the ground at P₁. But the two middle wheels (#2 and #5) contact the ground at P₆. This is a transition status.
• Status 6: The three wheels (#2, #4 and #6) of Group.

B enter their idling phase. The rotation speed of the wheel (#2) at
the left-hand side is $-\omega$. But the rotation speed of the wheels (#4 and #6) at the right-hand side is $\omega$. The three wheels (#1, #3, and #5) of Group A keep their poses. This is an adjusting status.

- **Status 7**: All six eccentric wheels contact the ground at their transition points. The three wheels (#1, #2, and #3) at the left-hand side contact the ground at $P_1$. But the three wheels (#4, #5, and #6) at the right-hand side contact the ground at $P_3$. This is a transition status, which is exactly the same as Status 1.

### Motion Analysis

#### Determination of geometric parameters

Referring to Figure 8, the central angle for the supporting phase is $\theta$, the angle between $P_1Q$ and $P_3Q$ is $\phi$, i.e., $P_1QP_3=\phi$. Hence, the displacement of the rotation axis $Q$ of the eccentric wheel can be given as $\phi$. In the above sections, we mentioned two transition contact points $P_1$ and $P_3$. But how to determine these two transition contact points? To do this, we need to determine some geometric parameters. First, one basic requirement for the robot is that the robot should keep the minimum height so that the bottom of its body cannot touch the ground. In other words, the minimum height $h_0$ of the rotation axis $Q$ of the eccentric wheel should be given at the design stage. Referring to Figure 8a, we get

\[|OD| = \sqrt{|OQ|^2 - |QD|^2} = \sqrt{r^2 - (h_0 - r)^2} \tag{1}\]

where $r$ and $e$ are respectively the radius and eccentricity of the eccentric wheel. So,
\[
\begin{align*}
\angle QD &= \tan^{-1} \left( \frac{\angle DQ}{\angle QD} \right) = \tan^{-1} \left( \frac{\sqrt{c^2 - (h_0 - r)^2}}{h_0 - r} \right) \quad (2) \\
\angle PQD &= \tan^{-1} \left( \frac{\angle PQ}{\angle PFD} \right) = \tan^{-1} \left( \frac{\sqrt{c^2 - (h_0 - r)^2}}{h_0 - r} \right) \quad (3)
\end{align*}
\]

From Equation (2) and (3), we get
\[
\phi = \angle P, Q_1 = 2 \angle P Q D = 2 (\angle Q D D - \angle P Q D)
\]
\[
= 2 \tan^{-1} \left( \frac{\sqrt{c^2 - (h_0 - r)^2}}{h_0 - r} \right) + \tan^{-1} \left( \frac{\sqrt{c^2 - (h_0 - r)^2}}{h_0} \right) \quad (4)
\]
\[
\theta = \angle P Q_1 = 2 \angle P Q_2 = 2 \tan^{-1} \left( \frac{\sqrt{c^2 - (h_0 - r)^2}}{h_0 - r} \right) \quad (5)
\]

Motion status of \( Q \)

Suppose that the eccentric wheel contacts the ground at \( P_i \) at the initial moment \( t = 0 \) as shown in Figure 8a. It will contact the ground at point \( p \) at the moment \( t \) as shown in Figure 8b from which we get
\[
\frac{\angle DQ}{\angle QD} = \tan^{-1} \left( \frac{\sin \angle Q D}{\cos \angle Q D} \right) = \tan^{-1} \left( \frac{\angle P Q}{\angle P Q D} \right) = \tan^{-1} \left( \frac{\sqrt{c^2 - (h_0 - r)^2}}{h_0 - r} \right) \quad (6)
\]

\[
\begin{align*}
|QD| &= |QO| \cos \angle QOD = c \cos \angle P Q O P \\
&= c \cos (\theta / 2 - \omega t). \\
\end{align*}
\]

The displacement of the center \( O \) of the eccentric wheel is
\[
x_0 = r \angle P Q O P = r \omega t, y_0 = r \\
\]
Hence, the displacement of the rotation axis \( Q \) of the eccentric wheel can be given as
\[
x = x_0 + |QD| - |QD| \quad (9)
\]
\[
y = y_0 + |QD| - c \cos (\theta / 2 - \omega t) \\
\]

Differentiating Eq.(9) with respect to time \( t \), the velocity of \( Q \) can be given as
\[
v_x = \dot{x} = r \omega + c \omega \cos (\theta / 2 - \omega t) \\
\]
\[
v_y = \dot{y} = c \omega \sin (\theta / 2 - \omega t) \quad (10)
\]

Differentiating Eq.(10) with respect to time \( t \), the acceleration of \( Q \) can be given as
\[
a_x = \ddot{x} = \omega^2 + c \omega \sin (\theta / 2 - \omega t) \\
a_y = \ddot{y} = -c \omega \cos (\theta / 2 - \omega t) \quad (11)
\]

Motion status of the robot

For straight walking, no matter which gait (the tripod gait or the hexapod gait) is used, all wheels in the supporting status have the same motion status. Hence, the motion status of the robot body is exactly the same as the motion of the rotation axis \( Q \) given by Equation (9) – (11).

For turning, the displacement, velocity and acceleration of the robot body in the vertical direction are respectively given as \( y_Q, \dot{y}_Q, \ddot{y}_Q \) which are the same as the straight walking. But in the horizontal direction, considering the symmetric structure of the robots, the turning (rotation in the horizontal plane) speed and acceleration can be given as
\[
\omega = \frac{2y_Q}{W_r} \\
\alpha = \frac{2a_y}{W_r} \quad (12)
\]

![Figure 9: The variation of \( \phi \) and \( \theta \) with respect to \( h_0 \) for given \( e = 0.030 \text{ m} \).](image)

![Figure 10: The variation of \( y \) with respect to \( e \) for \( h_0 = r \).](image)

![Figure 11: Displacement, velocity and acceleration vs time \( t \) for different \( e \) values.](image)
Where \( W \) is the width of the robot.

**Numerical results**

Referring to the developed prototype as shown in Figure 1, the dimension of the robot body is 0.362 m \( \times \) 0.232 m \( \times \) 0.071 m. The overall weight is about 58.9 N. The radius and eccentricity of the eccentric wheels are respectively 0.05 m and 0.03 m. The rotation velocity at the supporting phase is \( \omega_s = 4.0 \text{ rad/s} \).

The effect of the minimal height \( h_0 \) on \( \theta \) and \( \phi \): In general, the axis \( Q \) of the eccentric wheel should not lower than the center \( O \) of the wheel for the supporting phase, i.e., \( h_0 \geq r \). This is because the wheel cannot be designed too large for the limited structure of the robot. However, for different \( h_0 \), the two angles (\( \theta \) and \( \phi \)) are different. Figure 9 shows the variation of \( \theta \) and \( \phi \) with respect to \( h_0 \) for the given eccentricity \( e=0.03 \text{ m} \). It can be seen that for \( h_0=r=0.05 \text{ m}, \theta=180^\circ \) and \( \phi=118.073^\circ \). When \( h_0=r+e=0.08 \text{ m} \), both \( \theta \) and \( \phi \) are 0, because \( Q \) and \( O \) are on the same vertical diameter in this case.

The effect of the eccentricity \( e \) on \( \phi \): As shown in Figures 2-8, the central angle corresponding to the supporting phase is less than 180° (i.e., \( \theta<180^\circ \)). For the tripod gait, the rotation speed for supporting phase is much lower than the rotation speed for the idling phase (i.e. \( \omega_i<\omega_r \)) because the time \( T_i \) used for the supporting phase is the same as the time \( T_r \) used for the idling phase (i.e. \( T_i=T_r \)). For the hexapod gait, there are two adjusting statuses in one cycle, even if \( \omega_i>\omega_r \), the time interval between two moving statuses is long. In order to simplify the control of the tripod gait, we can make \( \omega_i=\omega_r \). This requirement leads to \( \theta=180^\circ \) and \( h_0=r \). When \( \theta=180^\circ \), for the hexapod gait, if we make \( \omega_i>\omega_r \) (say \( \omega_i=2\omega_r \)), the time interval between two moving statuses can be reduced. When \( h_0=r \), \( \theta=180^\circ \) does not change with \( e \). But \( \phi \) will change with respect to the eccentricity \( e \) as shown in Figure 10.

The effect of the eccentricity \( e \) on the motion of the robot: As mentioned in the above subsections, when \( h_0=r, \theta=180^\circ \). As the rotation velocity at the supporting phase for the developed prototype is \( \omega_s = 4.0 \text{ rad/s} \), we can calculate the time used for the supporting phase as \( T_s=0.785 \text{ s} \). In order to investigate the effect of the eccentricity \( e \) on the motion of the robot, several \( e \) values (0 m, 0.005 m, 0.010 m, 0.020 m, 0.030 m, 0.040 m, and 0.045 m) are chosen for comparison. Among these \( e \) values, \( e=0.030 \text{ m} \) is the eccentricity of the wheels adopted in the developed prototype robot. Substituting the above parameters into Equation (9) – (11), we can calculate the motion of the robot for straight walking. The results of one supporting phase \( T_s=0.785 \text{ s} \) can be given in Figure 11.

Figure 11a shows the horizontal displacement of the robot. Figure 11b shows the horizontal velocity of the robot. Figure 11c shows the horizontal acceleration of the robot. Figure 11d shows the vertical displacement of the robot.

Figure 11e shows the vertical velocity of the robot. Figure 11f shows the vertical acceleration of the robot. From Figure 11, we can see that when \( e=0 \), the horizontal displacement of the robot is a slant straight line. But the vertical displacement, the velocity and acceleration are all 0. This result is obvious and logical.

When \( e\neq 0 \), the variation of the displacement, velocity and acceleration with respect to time for different \( e \) values is similar and can be described as follows:

The horizontal displacement of the robot increases with respect to time. In the first half of \( T_s \), the horizontal velocity increases. At the moment \( t=T_s/2=0.393 \text{ s} \), it reaches its maximum. After that, the horizontal velocity decreases to its original value. The horizontal acceleration decreases with respect to time \( t \). At the moment \( t=T_s/2=0.393 \text{ s} \), it reaches 0. After that, the horizontal acceleration becomes negative. Similarly to the horizontal velocity, the vertical displacement increases in the first half of \( T_s \). At the moment \( t=T_s/2=0.393 \text{ s} \), it reaches its maximum. After that, the vertical displacement decreases to its original value. Similarly to the horizontal acceleration, the vertical velocity decreases with respect to time \( t \). At the moment \( t=T_s/2=0.393 \text{ s} \), it reaches 0. After that, the vertical velocity becomes negative. The vertical acceleration of the robot is always negative. In the first half of \( T_s \), it decreases. At the moment \( t=T_s/2=0.393 \text{ s} \), it reaches its minimum. After that, the vertical acceleration increases to its original value.

Referring to Eq.(12), the turning angular velocity is similar to the horizontal velocity as shown Figure 11b and the turning angular acceleration is similar to the horizontal acceleration as shown in Figure 11c.

**Advantages of the Eccentric Wheels**

As mentioned in the introduction section, the goal for developing the proposed hexapot robot with eccentric wheels is to detect the gas in underground mines. Avoiding potential explosion is the key point. Hence, any factor which could cause sparks is not expected. Although it has a lot of excellent performance, the RHex robot cannot satisfy this specific requirement because it has violent bumping and collision of its body with the rocky terrain. Also, its driving motor cannot be small enough (with a power less than 3 watts) to keep its all excellent performance.

Figures 12-14 can be used to exemplify the advantages of the proposed eccentric wheeled leg over the C shape leg of the RHex robot. Figure 12a shows the eccentric wheeled leg of the proposed hexapot...
As mentioned in the introduction section, in the tripod gait, there are always three feet of hexapod in contact with the ground. Obviously, the RHex robot is an exception.

Another violent bumping and collision of the RHex robot comes from the badly broken terrain. Referring to Figure 14b, as long as the width of a ditch is larger than the radius (i.e., $W > r$), the RHex C shape leg falls into the ditch. This results in violent bumping of the robot body. If the depth of the ditch is larger than the diameter (i.e., $H > 2r$), the whole C shape leg falls into the ditch and the bottom of the RHex robot body collides the ground. Such violent bumping and collision is not expected in a context of gas detection application in underground mines. Referring to Figure 14a, on the contrary, as long as the width of the ditch is less than the diameter (i.e., $W < 2r$), the eccentric wheeled leg will not fall down a distance more than the radius, no matter how deep the ditch is. Hence, on one hand, the eccentric wheeled leg greatly reduces the bumping of the robot body. On the other hand, it greatly reduces the possibility for the bottom of the robot body to collide the rocky terrain.

Another advantage of the proposed eccentric wheeled hexapot robot is: Its backward motion is exactly the same as its forward motion. This is because the eccentric wheeled leg is symmetric (Figures 12 and 14). But for the RHex robot, its backward motion is completely different from its forward motion. Actually, the RHex robot uses its backward motion for leaping and flipping itself. However, these violent bumping is not expected in a context of gas detection application in underground mines.

Figure 15 shows the situation for the proposed hexapot robot to traverse an obstacle which is higher than the radius of the wheel. For the common circular wheels with the axis $Q$ coinciding with the center $O$, it is impossible to traverse such an obstacle. But for the proposed hexapot robot, it is easy to climb and traverse this obstacle. This mainly depends on the motion of wheel #1 as shown in Figure 15a. Of course, wheel #4 as shown in Figure 15b also provides some assistance. Hence, the proposed eccentric wheel possesses significant advantages over the common circular wheel in climbing and traversing an obstacle.
Conclusions and Discussions

A new concept for developing hexapod robots using eccentric wheels was proposed in this work. Compared with the RHex robot, the proposed hexapod robot can greatly reduce the bumping of the robot body in both smooth ground and rocky terrain. Also, the developed hexapod robot possesses significant advantages over those with common circular wheels in traversing rocky and uneven terrain. This work focused on the kinematics analysis of the proposed hexapod robot.

- The proposed alternating tripod gait can make the robot to move continuously. If the central angle $\theta=180^\circ$, we can get $\omega_s=\omega_i$. All wheels can move with the same rotation velocity. This makes the control very easy. However, if the eccentricity $e$ is large and the power of the motor is small (For instance, the motors used in the mining robot for detecting gas in underground mines are very small), the weight could cause a big resistant torque on the three driving wheels. This could be a big burden for the robot.

- The hexapod gait benefits in overcoming the resistant torque on the wheels caused by the weight. With six driving wheels, the resistant torque caused by the weight on each wheel can be reduced by half. The disadvantage of the hexapod gait is that there are two adjusting statuses. If $\theta=180^\circ$ and $\omega_s=\omega_i$, the stopping time is twice of the moving time. Hence, for the hexapod gait, we have to make $\omega_i >> \omega_s$ depending on different applications of the robot.

- Based on the parameters used in the prototype, the motion analysis of the developed robot is conducted. The results for the cases with $e=0$ show that even if the rotation velocity $\omega$ of the wheels is constant during the supporting phase, the velocities of the robot in both horizontal and vertical directions cannot be constant.

The future work will focus on
- Dynamic modeling and analysis.
- Vision system development and remote control.
- Further experimental studies.

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