Understanding the Temperature Dependence of the Seebeck Coefficient from First-Principles Band Structure Calculations for Organic Thermoelectric Materials

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The Seebeck effect measures the electric potential built up in materials under a temperature gradient. For organic thermoelectric materials, the Seebeck coefficient shows more complicated temperature dependence than conventional systems, with both monotonic increases and nonmonotonic behavior, that is, first increasing and then decreasing. The mechanism behind the phenomenon is intriguing. Through first-principles calculations coupled with the Boltzmann transport equation, we demonstrate typical trends of the Seebeck coefficient with respect to temperature through band structure analysis. The bandgap and bandwidths of the valence band and conduction band jointly determine the effectiveness of thermal activation. Ineffective or effective thermal activation leads to a one- or a two-band transport behavior, respectively. Under the thermal-activation mechanism, Seebeck coefficient shows monotonic temperature dependence in a one-band model but nonmonotonic relationship in a two-band model. In particular, in the two-band model, Seebeck coefficient might show an ambipolar behavior, that is, its sign changes at high temperature.

Keywords: organic thermoelectric materials, Seebeck coefficient, band structure calculation, ambipolar thermoelectric transport, Boltzmann transport equation
**Introduction**

Organic thermoelectric materials (OTEs) have aroused great interests and have been rapidly developed in recent years. Compared with inorganic thermoelectric materials, OTEs show lower thermal conductivity, high cost-effectiveness, and low toxicity. Doping conducting polymers are very promising OTEs. Both p- and n-type polymers have rapidly developed with figure of merit $zT$ increases from $10^{-3}$ to 0.4. The effects of oxidation, pressure, and temperature have been studied. There have been many experimental results demonstrating the temperature dependence of Seebeck coefficient, $S$. For example, in 1986, Zhu et al. measured the Seebeck coefficient for $\beta$-(Bis(ethylenedithio)tetrathiafulvalene)-BrI$_2$ and surprisingly, Seebeck coefficients even change sign from negative to positive with increasing temperature, demonstrating an exotic ambipolar transport behavior. Such behavior has never been explained. Recently, Liu et al. have shown significant boosting effects of polaron bands in K-doped poly(Ni-ett), and the abnormal temperature dependence can be explained by polaron formation.

We note that a number of complicating factors (e.g., structural deformation, dominant dopant, and polaron formation) were included in previous work to understand the relationship between $S$ and $T$. In this work, we intend to avoid the complexation of doping, and we illustrate the abnormal Seebeck coefficient versus temperature behavior can be understood from electronic structures, as will be shown through different band structures with variant bandwidths and band gaps. We believe such a basic understanding can be extended to more complicated situations with only analysis for density of states (DOS).

Electronic structure calculations

The polymer backbones lie along the $X$ axis, and the vacuum layers along the $Y$ and $Z$ axes are large enough to ensure the isolated “ideal” polymer chains. The different functionals have been adopted for PPy and poly(Ni-ttftt). The projector augmented wave method with Perdew–Burke–Ernzerhof (PBE) for PPy and local-density approximation (LDA) + $U (U = 6.04 \text{ eV})$.

**Figure 1** (a) Chemical structure and (b) band structure and DOS of PPy.
for poly(Ni-ttftt) were adopted for the optimization of the lattice parameters of X axis and ionic positions and their electron structure calculations in the Vienna Ab initio Simulation Package.28

Thermoelectric transport coefficients calculations

In the Boltzmann transport theory,29 the electrical conductivity, $\sigma$, and Seebeck coefficient, $S$, are expressed as:

$$\sigma = e^2 \sum_k \left( -\frac{\partial f_0(\varepsilon_k)}{\partial \varepsilon_k} \right) v_k \tau_k$$  \hspace{2cm} (1)

$$S = \frac{e}{\sigma T} \sum_k \left( -\frac{\partial f_0(\varepsilon_k)}{\partial \varepsilon_k} \right) (\varepsilon_k - \varepsilon_F) v_k \tau_k$$  \hspace{2cm} (2)

where $f_0(\varepsilon_k) = \frac{1}{[\exp((\varepsilon_k - \varepsilon_F)/k_B T) + 1]}$ is the Fermi-Dirac distribution function; $\frac{\partial f_0(\varepsilon_k)}{\partial \varepsilon_k}$ is nonzero only when $\varepsilon_k$ locates within $k_B T$ near the Fermi level. $\varepsilon_k$ is the band energy at k-point; $\varepsilon_F$ is the Fermi energy; $v_k = (1/h) \nabla_{\varepsilon_k}$ is the group velocity; $\tau_k$ is the relaxation time due to scattering with phonons and/or disorders/impurities.

If both VB and CB contribute to transport, the effective total $S$ can be expressed as30:

$$S = \frac{S_{VB}\sigma_{VB} + S_{CB}\sigma_{CB}}{\sigma_{VB} + \sigma_{CB}}$$  \hspace{2cm} (3)

| Table 1 | The Elastic Constant, $C_{ii}$, Electron DP Constant, $E_{1(e)}$, and Hole DP Constant, $E_{1(h)}$ |
|---|---|---|---|
| Polymer | $C_{ii}$ ($10^{-8}$ J m$^{-1}$) | $E_{1(e)}$ (eV) | $E_{1(h)}$ (eV) |
| PPy | 8.766 | 5.57 | 4.86 |
| Poly(Ni-ttftt) | 7.379 | 4.39 | 1.85 |

Figure 2 | Total $S$ and $\sigma$, $\sigma_{VB}$ and $\sigma_{CB}$, and $S_{VB}$ and $S_{CB}$ of p- and n-type doping of PPy with 1.74 eV bandgap change with $T$. (a) to (c) are for p-doping. (d) to (f) are for n-doping. The location of Fermi level ($E_F$) in the insert indicates the doping concentration and type.
Here, $S_{VB}$ and $S_{CB}$ are the Seebeck coefficients for VB and CB, respectively, and $\sigma_{VB}$ and $\sigma_{CB}$ are the corresponding electrical conductivities. It is worth noting that $S$ is positive for hole and negative for electron transport in doped semiconductors.

**Relaxation time calculations**

Under the DP approximation with longitudinal phonon scattering, the relaxation time can be expressed as:

$$\frac{1}{\tau} = \left( \frac{2\pi}{\hbar} \right) \sum_{k, k'} |M(k, k')|^2 \delta(\varepsilon_k - \varepsilon_{k'}) (1 - \cos \theta),$$

where $\theta$ is the scattering angle between $k$ and $k'$, and $|M(k, k')|^2$ is the scattering matrix element, which takes the form $|M(k, k')|^2 = n_{F} T E_{2}/C_{u}$, where $E_{1}$ is DP constant and $C_{u}$ is elastic constant, in the long wave limit $k \rightarrow 0$. The thermoelectric (TE) transport coefficients were calculated based on the Boltzmann transport equation through BoltzTraP program. Last, the relaxation time was obtained from first-principles calculations.

**Results and Discussion**

First of all, the geometric structure of PPy was optimized, and its band structure was calculated (Figures 1a and 1b). The electron–phonon coupling is quantitatively described by DP constant and elastic constant in DP theory, and all DP constants and elastic constants are summarized in Table 1.

PPy can be easily p-doped. So, we placed the Fermi level inside VB, and the transport behavior in VB belongs to metallic behavior. The positive $S$ monotonically increases with increasing $T$ in Figure 2a, compliant with metallic behavior (Figure 2c, hollow line). This phenomenon can be explained by eq 3. In this case, eq. 3 is simplified to $S \approx S_{VB}$ because of $\sigma_{VB}/\sigma_{CB}/\sigma_{CB} = n_{F} + n_{F}$, Figure 2b) even at $T = 600$ K. These can be understood from two aspects: (1) the term of $\partial f_{0} / \partial k_{0}$ in CB is vanishingly small because of the large bandgap (1.74 eV) (Figure 1b). (2) The large bandgap also makes thermal activation from CB to VB impossible. So, there is hardly any electrons in CB even at high $T$. Therefore, VB is the only band participating in transport. This causality also applies to the situation of Fermi level inside CB (Figures 2d–2f). To summarize, the TE properties of PPy with the 1.74 eV bandgap belong to one-band transport behavior. For either p- or n-type doping, $|S|$ monotonically increases with increasing $T$.

To reveal the role of bandgap in the TE properties, we studied metal coordinated polymer poly(Ni-ttftt) (Figures 3a and 3b). The calculated bandgap is 0.12 eV, consistent with the previous result. Since the nickel-coordinated polymers can be n-doped in the experiment, we first placed the Fermi level inside CB. We find that the Seebeck coefficient has an ambipolar behavior, namely, at relatively low-temperature range, negative $S$ nonmonotonically changes with increasing $T$, and at very high $T$, the sign of $S$ changes, shown in Figure 4a. Such ambipolar behavior can be explained again by eq. 3. At very low $T$, eq. 3 is simplified to $S = S_{CB}$ because of $\sigma_{VB}/\sigma_{CB}/\sigma_{CB}$, (Figure 4b), so only CB participates in the transport. As $T$ increases, $\sigma_{VB}/\sigma$ and $\sigma_{CB}/\sigma$ get close. So, the transport behavior is determined by CB (metallic model behavior, Figure 4c, cross line) and VB (semiconductor model behavior, Figure 4c, hollow line) together. As $T$ continues to rise, $\sigma_{VB}/\sigma$ and $\sigma_{CB}/\sigma$ get closer, even $\sigma_{VB}/\sigma$ and $\sigma_{CB}/\sigma$, and $S_{VB}$ and $S_{CB}$, according to eq. 3, the sign of $S$ becomes positive, leading to an exotic ambipolar behavior. The large $\sigma_{VB}$ at high $T$ is attributed to thermal activation, and the thermal activation is attributed to a small bandgap. Overall, under the thermal-activation mechanism, the two-band model determines that $S$ nonmonotonically changes with increasing $T$, that is, first increases at low $T$, then decreases at high $T$, and its sign changes at much higher $T$.

Then we placed the Fermi level inside the VB of poly(Ni-ttftt) to look at p-type doping. Figure 4d shows that positive $S$ monotonically increases with increasing $T$. Figures 4e and 4f show that the impact of $\sigma_{VB}/\sigma > \sigma_{CB}/\sigma$, which means that eq. 3 will be simplified to $S \approx S_{VB}$. So, VB is the only band participating in the transport, and the temperature dependence of $S$ is consistent with the VB transport behavior (Figure 4f, hollow line).

For poly(Ni-ttftt), the trends of $S$ with increasing $T$ of p- and n-type doping are completely different. This can be attributed to the difference in bandwidths of VB and CB. The bandwidths of VB and CB are 0.86 and 0.31 eV, respectively, that is, relatively big difference. The wider...
the bandwidth, the smaller the effective mass, or the better for transport. So, at high $T$, given the fixed small bandgap, the relationship between $\sigma_{VB}/\sigma$ and $\sigma_{CB}/\sigma$ is quite different, that is, $\sigma_{VB}/\sigma \sim \sigma_{CB}/\sigma$ for $n$-type doping and $\sigma_{VB}/\sigma \gg \sigma_{CB}/\sigma$ for $p$-type doping. According to eq. 3, $n$- and $p$-type doping of poly(Ni-ttftt) correspond to two- and one-band transport model, respectively, which can explain the nonmonotonic and monotonic relationship between $S$ and $T$. In particular, at $T > 400$ K, $S$ of $n$-type doping becomes positive, that is, ambipolar behavior. It is most interesting to mention here that in 1986, Zhu et al. have already observed the very first ambipolar thermopower for (BEDT-TTF)$_2$BrI$_2$, a donor–acceptor-type organic conductor, for which the Seebeck coefficient looked quite similar to Figure 4a. Currently, we are investigating in more details for such exotic behavior.

Based on the above results, we conclude that, given a small bandgap, if the bandwidths of VB and CB are of small difference, VB and CB will participate in transport together for both $n$- and $p$-type doping. To obtain a small bandgap, the scissor operator in Boltztrap program was adopted to PPy, with small differences of bandwidths of CB and VB. Results show that (1) as the bandgap gets smaller, the relationship between $S$ and $T$ becomes nonmonotonic for Fermi level inside VB or CB (see Supporting Information Figure S4), (2) when the bandgap is small enough, $\sigma_{VB}/\sigma$ and $\sigma_{CB}/\sigma$ are close at high $T$, which means the transport model is a two-band model for Fermi level inside VB or CB (see Supporting Information Figure S5) and $S$ nonmonotonically changes with increasing $T$. In short, when the bandgap is small enough, the bandwidth effect of VB and CB should be considered to determine the transport model.

Conclusions

OTEs have been found to demonstrate vastly different temperature dependent of Seebeck coefficient, indicating
rich physics behind the complicated thermoelectric transport behavior. Through first-principles computational study, we revealed the relationship between band structure (bandgap and bandwidth) of OTEs and the temperature dependence of Seebeck coefficient for some model polymer systems. For the case of large bandgap, when thermal activation can be excluded, only one band (VB or CB) contributes to transport. If the bandgap is small enough, the bandwidth effect of VB and CB should be considered to determine the transport model. Specifically, (1) if the bandwidths are of big difference, the transport model depends on the doping type. When Fermi level is placed in the narrow band, the thermally activated electrical conductivity from the broadband should be considered at high T. So, both VB and CB participate in transport together. When Fermi level is located in the broadband, the thermally activated electrical conductivity of narrow band can be ignored even at very high T. So, only the broadband participates in transport. (2) If the bandwidths are of small difference, VB and CB will participate in transport together for the Fermi level inside VB or CB.

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