Prospects for observing strongly lensed supernovae behind Hubble Frontier Fields galaxy clusters with the James Webb Space Telescope

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(Published December 28, 2018)

ABSTRACT

Measuring time delays from strongly lensed supernovae (SNe) is emerging as a novel and independent tool for estimating the Hubble constant ($H_0$). This is very important given the recent discord in the value of $H_0$ from two methods that probe different distance ranges. The success of this technique will rely on our ability to discover strongly lensed SNe with measurable time delays. Here, we present the magnifications and the time delays for the multiply-imaged galaxies behind the Hubble Frontier Fields (HFF) galaxy clusters, by using recently published lensing models. Continuing on our previous work done for Abell 1689 (A1689) and Abell 370, we also show the prospects of observing strongly lensed SNe behind the HFF clusters with the upcoming James Webb Space Telescope (JWST). With four 1-hour visits in one year, the summed expectations of all six HFF clusters are $\sim 0.5$ core-collapse (CC) SNe and $\sim 0.06$ Type Ia SNe (SNe Ia) in F115W band, while with F150W the expectations are higher, $\sim 0.9$ CC SNe and $\sim 0.06$ SNe Ia. These estimates match those expected by only surveying A1689, proving that the performance of A1689 as gravitational telescope is superior. In the five HFF clusters presented here, we find that F150W will be able to detect SNe Ia (SNe IIP) exploding in 93 (80) pairs multiply-imaged galaxies with time delays of less than 5 years.

Keywords: strong lensing, supernovae, galaxy clusters

1. INTRODUCTION

Clusters of galaxies are gravitational lenses which magnify the light of objects behind them. In the line of sight of gravitational lenses, multiple images of background lensed supernovae (SNe) can be observed, and due to the variable nature of the objects, the difference between the arrival times of the images can be measured. Since the images have taken different paths through space before reaching us, the time-differences are sensitive to the expansion rate of the universe.Refsdal (1964) proposed to measure the value of the Hubble constant ($H_0$) from the time delays of multiply-imaged SNe (for a review of strong lensing gravitational time delays as a tool for cosmography, see Treu and Marshall 2016). With the first discovery of multiply-imaged SN in 2014 (Kelly et al. 2015), the feasibility of measuring the value of the $H_0$ with this method became possible (Vega-Ferrero et al. 2018; Grillo et al. 2018). This is particularly interesting since there is a recent discrepancy of $H_0$ value of at least $\approx 3\sigma$ from two independent cosmological probes (the cosmic microwave background (Planck Collaboration et al. 2016) and local distant ladders (Riess et al. 2016, 2018).

After the time delays of strongly lensed transient objects have been measured, extracting cosmological parameters requires knowledge of the lensing potential (e.g. Gunnarsson and Goobar 2003; Suyu et al. 2017). Notably, gravitational lens models suffer from the so-called mass-sheet degeneracy (Oguri and Kawano 2003), so very different lens models will still be able to predict similar time delays of the multiply-imaged background source. However, thanks to the homogeneous nature of Type Ia SNe (SNe Ia) lightcurves, the observation of
strongly lensed SNe Ia circumvents this problem because the magnification can be inferred directly. Conversely, if the background cosmology is assumed to be known, even a single magnified SNe Ia could be used to put constraints on the lensing potential (Patel et al. 2014; Nordin et al. 2014; Rodney et al. 2015). The magnification boost provided by the cluster lenses enhances the possibility of observing SNe at unprecedented distances, which enables to study their properties and their possible evolution with redshift that otherwise would be undetectable (Petrushevska et al. 2017). Furthermore, discoveries of high redshift SNe can be used to pinpoint the SN rates at very high redshifts ($z > 2$) where they are poorly measured (Sullivan et al. 2000; Gunnarsson and Goobar 2003; Petrushevska et al. 2016).

For the purpose of using them as gravitational lenses, here we focus on the galaxy clusters from the Hubble Frontier Fields (HFF) (Lotz et al. 2017) with the Hubble Space Telescope (HST). The HFF program consisted of imaging six clusters - Abell 2744, MACS J0416.1-2403, MACS J0717.5+3745, MACS J1149.5+2223, Abell S1063 and Abell 370 (their short names are listed in Table 1). Using these deep observations and complemented by many follow-up multi-wavelength imaging and spectroscopy, these massive clusters have been extensively modelled and dozens of multiply-imaged galaxies behind them have been confirmed (e.g. Jauzac et al. 2015; Karman et al. 2015; Limousin et al. 2016; Lagattuta et al. 2017; Mahler et al. 2018; Kawamata et al. 2018). New strong lens mass models of AS1063, as well as updated mass models of A2744 and MACSJ0416 have been published in (Kawamata et al. 2018, K18 hereafter) and (Mahler et al. 2018, M18). Those models exploit the novel dataset of very deep HST photometry and VLT/MUSE integral field spectroscopy. The large number of spectroscopic redshifts improves the ability of the models to predict accurate magnification and time delays. Therefore, strengthens the reliability of those model predictions and the outcome of this work. The models considered in this study are computed using two different parametric approaches. K18 is using the GLAFIC (Keeton 2001), whereas M18 uses Lenstool (Jullo et al. 2007). The choice of the type and the number of potential to model the cluster is the main differences between the two models (see Meneghetti et al. 2017 for more details).

In our previous work (Petrushevska et al. 2016, 2018, hereafter P16 and P18), we used the galaxy clusters Abell 1689 (A1689) and A370 as gravitational telescopes to search for strongly lensed SNe. There, we showed the expectations of search campaigns that can be conducted with future facilities. The HST successor, James Webb Space Telescope (JWST; Kalirai 2018) is to be launched in 2021 and will carry the NIRCam instrument aboard with several near-infrared filters with the possibility of reaching unprecedented sensitivity. Since most of the light of nearby SNe is in the optical bands, these near-infrared filters are optimal for finding high-$z$ SNe, as their light is redshifted to the longer wavelengths. The aim of this article is to complement the previous work by extending the simulations to the remaining HFF clusters to determine the prospects for observing lensed SNe with the JWST.

### Table 1. Hubble Frontier Fields galaxy clusters considered in this work.

| Cluster | Short name | $N_{sys}$ | $N_{images}$ | $z_{max}$ |
|---------|------------|-----------|--------------|-----------|
| Abell 2744 | A2744 | 12 | 40 | 3.98 |
| Abell S1063 | AS1063 | 14 | 42 | 3.71 |
| MACS J1149.5+2223 | MACSJ1149 | 8 | 24 | 3.70 |
| MACS J0416.1-2403 | MACSJ0416 | 23 | 65 | 3.87 |
| MACS J0717.5+3745 | MACSJ0717 | 6 | 20 | 2.96 |

Table 1. Hubble Frontier Fields galaxy clusters considered in this work. Only the background systems with spectroscopic redshift and those bellow $z < 4.0$ are selected. The number of galaxies behind the cluster is given in column 3 and the number of multiple images of these galaxies in column 4. The highest redshift of these galaxies is given in column 5.

2. PROSPECTS FOR OBSERVING LENSED SUPERNOVAE BEHIND THE HFF GALAXY CLUSTERS WITH THE JWST

In the present study, we use the same procedures as in P16 and P18 for simulating surveys that can be performed with the JWST. We start by considering the multiply-imaged galaxies behind the five HFF galaxy clusters with names and properties are listed in Table 1. To avoid additional source of error, we select the background systems with spectroscopic redshift and those bellow $z < 4.0$, so that redshifting to the observers frame and cross-filter k-corrections (Kim et al. 1996) are meaningful. The total number of systems that satisfy these criteria is 64 which have 183 multiple images. We assume 4 visits to each galaxy cluster for easy comparison with the previous work with A1689 and A370 (P16, P18).

To obtain the expected SN rates for the systems behind the clusters, we estimated the specific star formation rates (SFR) and the stellar masses of the galaxies from multi-band HST photometry. The deep HST photometry of the clusters were obtained during the HFF program (Lotz et al. 2017), using three bands of the Advanced Camera for Surveys (ACS) and four bands of the
Wide Field Camera 3 (WFC3) and is publicly available\(^1\). As previously, the SFR and stellar masses were fitted with the help of the software package FAST\(^2\) (Kriek et al. 2009). The brightness of each multiply-imaged galaxy was corrected for the magnification which we obtained from the lensing models in K16 and K18 and has uncertainty of the the order of \(\sim 10 - 15\%\). In the case of A2744, we compared the magnifications from K18 with those from M18 and found good agreement. After the SFR and the stellar masses of each galaxy is estimated, the expected SN rate can be inferred. For core-collapse (CC) SN rate in units of yr\(^{-1}\), we used the relation:

\[
R_{CC} = k_{8}^{50} \cdot \text{SFR},
\]

because the progenitors of CC SNe are short-lived stars, so it is expected that they trace ongoing SFR. The SFR is given in in units \(M_{\odot}\text{yr}^{-1}\), and \(k_{8}^{50}\) is the scale factor, and is in P16, we used \(k_{8}^{50} = 0.007M_{\odot}^{-1}\). The SN Ia rates were obtained from the Scannapieco and Bildsten (2005) simple model

\[
R_{Ia} = A \cdot \text{SFR} + B \cdot M_{*},
\]

where \(A\) and \(B\) are constants, for which we used literature values from Smith et al. (2012), while the stellar mass \(M_{*}\) of the individual galaxies was taken from the FAST best fits. The magnifications of the galaxy images together with the SN rates of the unique galaxy systems are listed in Table 3.

Then, the expected number of SNe in each galaxy is obtained by multiplying the SN rate and the control time. The control time is different for each SN type and it is the time that the SN light curve is above the detection threshold, thus is a function of the SN light curve, absolute intrinsic SN brightness, detection efficiency, extinction by dust and the lensing magnification. In Table 3, the galaxies that have positive control times in F150W band for all SN types are shown. The total CC control time was obtained by weighting the contribution from the various CC SN subtypes with their fractions and then summed. We obtain the final number of SNe by summing over the individual estimates from each multiple image in the system. The results are shown in Table 2 together with the previous estimates for A1689 and A370 from P18 for comparison. For more details regarding the estimates presented in this section, we refer to our previous work (Petrushevska et al. 2018, 2016; Goobar et al. 2009).

The total number of expected SNe of the five HFF clusters is \(\sim 0.4\) CC SNe and \(\sim 0.04\) SNe Ia in F115W band, while in F150W the expectations are higher, \(\sim 0.6\) CC SNe and \(\sim 0.04\) SNe Ia. Thus, the summed expectations of all six HFF clusters are comparable to what is expected by only monitoring A1689 as shown in Table 2. We note that these are a lower limits, since we have only considered the galaxies with spectroscopic redshift. With ongoing spectroscopic campaigns with instruments such as VLT/MUSE (e.g. Bina et al. 2016; Lagattuta et al. 2017; Mahler et al. 2018), more systems behind galaxy clusters will be confirmed.

### 3. SUMMARY AND CONCLUSIONS

The recent discovery of the first multiply-lensed SNe, SN Refsdal and iPTF16geu (Goobar et al. 2017), opened a new path to measure the expansion history of the Universe through monitoring time delays of strongly lensed SNe. Measuring time delays of strongly lensed SNe will provide independent and precise estimate of the Hubble constant, which will allow to shed light on the current tension regarding its value.

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\(^1\) http://www.stsci.edu/hst/campaigns/frontier-fields/

\(^2\) http://w.astro.berkeley.edu/ mariska/Fast.html

| Cluster   | \(N_{CC}^{a}\) | \(N_{Ia}^{b}\) | \(z_{max}^{c}\) | \(N_{gal}^{c}\) |
|-----------|----------------|----------------|----------------|----------------|
| A2744     | 0.02(0.01)     | 0.0012(0.0003) | 3.05           | 21             |
| AS1063    | 0.11(0.05)     | 0.007(0.0003)  | 3.12           | 36             |
| MACSJ1149 | 0.025(0.005)   | 0.005(0.001)   | 3.70           | 23             |
| MACSJ0416 | 0.19(0.06)     | 0.014(0.004)   | 3.29           | 49             |
| MACSJ0717 | 0.05(0.02)     | 0.007(0.005)   | 2.96           | 20             |
| A370      | 0.11(0.04)     | 0.02(0.01)     | 3.77           | 47             |
| A1689     | 0.7(0.3)       | 0.13(0.06)     | 3.05           | 66             |

| Cluster   | \(N_{CC}^{a}\) | \(N_{Ia}^{b}\) | \(z_{max}^{c}\) | \(N_{gal}^{c}\) |
|-----------|----------------|----------------|----------------|----------------|
| A2744     | 0.06(0.04)     | 0.006(0.004)   | 3.98           | 40             |
| AS1063    | 0.12(0.06)     | 0.008(0.004)   | 3.61           | 42             |
| MACSJ1149 | 0.08(0.02)     | 0.005(0.001)   | 3.7            | 42             |
| MACSJ0416 | 0.24(0.07)     | 0.016(0.005)   | 3.87           | 67             |
| MACSJ0717 | 0.12(0.07)     | 0.007(0.004)   | 2.96           | 20             |
| A370      | 0.3(0.1)       | 0.02(0.01)     | 3.77           | 47             |
| A1689     | 1.0(0.5)       | 0.14(0.07)     | 3.05           | 66             |
In the present study, we focused on SNe lensed by a galaxy cluster lenses, unlike other recent studies that make predictions for SNe being lensed by galaxies (e.g. Goldstein et al. 2018). In a previous work, we simulated possible JWST programs to obtain the expected number of SNe that have multiple images behind the galaxy clusters A1689 and A370 (P16, P18). Here, we have considered five Hubble Frontier Fields galaxy clusters as gravitational telescopes, motivated by the recent publications of new improved cluster models (K18 and M18). We presented here the magnifications and time delays of the multiple images of the background galaxies based on the lensing models of K18 and M18. We simulated the light curves of SNe that could explode in the multiply-imaged galaxies behind the galaxy clusters, and examined whether they will be detectable by the JWST/NIRCam bands F115W and F150W. Considering F115W, we found that JWST will be sensitive to at least 75 pairs of SNe Ia with multiple images exploding in the multiply-imaged galaxies with time delays of less than 5 years (the nominal duration of JWST). For the most common type of CC SNe, the SNe IIP, this number is slightly lower, 56, as they are on average fainter than SNe Ia. The same consideration, but for F150W gives better prospects, 93 (80) pairs of SNe Ia (SNe IIP) images because it is more appropriate for high-\(z\) SNe.

We also simulated possible JWST surveys to obtain the expected number of lensed SNe that have multiple images, and concluded that A1689 is the lens that offers the best prospects. The high-\(z\) SNe that will be discovered with the JWST can be spectroscopically followed with the new generation facilities such as the Extremely Large Telescope (Gilmozzi and Spyromilio 2007) and the Giant Magellan Telescope (Johns et al. 2012) which will start operate in the 2020s.

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APPENDIX

A.
Table 3. Properties of the multiply-imaged galaxies behind five HFF galaxy clusters. Time delays ($\Delta t$) of the multiply-imaged galaxies as predicted from the lensing model in K18 are listed in column 3. The time delays are measured relative to the first image in column 1. The reference image in each case is the one with the shortest path length between the galaxy and us. The time delays are with respect to the reference image. The magnification is given in magnitudes in column 4 and 5, and is computed using the lensing model in K18. Estimates of the core-collapse and SN Ia rates are given with 1$\sigma$ errors in column 6 and 7, respectively. Given that the star formation rate of the galaxy depends on the luminosity of the galaxy, it is dependent of the predicted magnification, thus the lensing model. In columns 8-14, the detectability of a lensed SN for the different SN types assuming a 27.5 mag in F150W, e.g. in a survey using 1 hour exposure of the JWST/NIRCam instrument. In order to be observable, the luminosity of both images must lie above the observation threshold.

| Images | $z$   | $\Delta t$ | $\Delta m_1$ | $\Delta m_2$ | $R_{CC} \times 10^2$ | $R_{Ia} \times 10^3$ | Detectable SN types |
|--------|------|------------|--------------|--------------|---------------------|----------------------|---------------------|
|        | d    | mag        | mag          | yr$^{-1}$    | yr$^{-1}$           |                      |                     |
| A2744  |      |            |              |              |                     |                      |                     |
| 1.3 + 1.1  | 1.688  | 2810(100)  | 1.52(0.04)   | 1.86(0.04)   | 1.84(0.42)          | 1.17(0.24)           | y y y y y y y y     |
| 1.3 + 1.2  | ...   | 3120(100)  | ...          | 1.86(0.06)   | ...                 | ...                  | y y y y y y y y y   |
| 2.2 + 2.1  | 1.888  | 8450(170)  | 1.10(0.04)   | 2.31(0.07)   | 0.12(0.09)          | 0.07(0.05)           | y y y y y y y y     |
| 2.2 + 2.4  | ...   | 8780(170)  | ...          | 2.03(0.09)   | ...                 | ...                  | y y y y y y y y y   |
| 3.3 + 3.1  | 3.980  | 6030(160)  | 1.40(0.05)   | 3.79(0.17)   | 0.41(0.20)          | 0.23(0.11)           | y y y y y y y y     |
| 3.3 + 3.2  | ...   | 6040(170)  | ...          | 3.75(0.12)   | ...                 | ...                  | y y y y y y y y y   |
| 4.3 + 4.1  | 3.580  | 12340(230) | 2.18(0.26)   | 1.69(0.06)   | 4.46(3.58)          | 2.92(2.39)           | y y y y y y y y     |
| 4.3 + 4.2  | ...   | 12010(220) | ...          | 2.34(0.06)   | ...                 | ...                  | y y y y y y y y     |
| 4.3 + 4.4  | ...   | 12680(240) | ...          | 2.33(0.29)   | ...                 | ...                  | y y y y y y y y     |
| 4.3 + 4.5  | ...   | 12680(240) | ...          | 2.55(0.17)   | ...                 | ...                  | y y y y y y y y y   |
| 6.1 + 6.2  | 2.019  | 2700(90)   | 1.35(0.04)   | 1.37(0.05)   | 0.53(0.03)          | 0.30(0.02)           | y y y y y y y y     |
| 6.1 + 6.3  | ...   | 1240(90)   | ...          | 1.78(0.05)   | ...                 | ...                  | y y y y y y y y     |
| 8.3 + 8.1  | 3.975  | 7370(180)  | 1.36(0.05)   | 3.53(0.14)   | 0.14(0.03)          | 0.08(0.01)           | y y y y y y y y     |
| 8.3 + 8.2  | ...   | 7370(180)  | ...          | 3.35(0.08)   | ...                 | ...                  | y y y y y y y y     |
| 10.3 + 10.1| 2.656  | 12280(220) | 1.24(0.05)   | 4.55(0.19)   | 0.016(0.003)        | 0.009(0.002)         | y y y y y y y y     |
| 10.3 + 10.2| ...   | 12270(220) | ...          | 4.66(0.21)   | ...                 | ...                  | y y y y y y y y y   |
| 24.3 + 24.1| 1.043  | 2630(80)   | 1.51(0.03)   | 2.34(0.03)   | 0.014(0.004)        | 0.008(0.002)         | y y y y y y y y y   |
| 24.3 + 24.2| ...   | 2600(90)   | ...          | 2.03(0.07)   | ...                 | ...                  | y y y y y y y y y y |
| 26.3 + 26.1| 3.054  | 2430(120)  | 1.35(0.04)   | 2.37(0.06)   | 0.11(0.10)          | 0.06(0.06)           | y y y y y y y y     |

Table 3 continued
Table 3 (continued)

| Images  | $z$     | $\Delta t$ | $\Delta m_1$ | $\Delta m_2$ | $R_{\text{CC}} \times 10^2$ | $R_{\text{Ia}} \times 10^3$ | Detectable SN types |
|---------|---------|-------------|---------------|---------------|-----------------------------|---------------------------|-------------------|
|         |         | d           | mag           | mag           | yr$^{-1}$                   | yr$^{-1}$                 |                   |
| 26.3 + 26.2 | ... | 2320(120)   | ...           | 2.70(0.06)   | ...                        | y y y y y y y y y y     |
| 30.3 + 30.1 | 1.025 | 1380(80)    | 1.59(0.04)    | 1.86(0.06)   | 0.04(0.01)                | 0.02(0.01)               | y y y y y y y y y y |
| 30.3 + 30.2 | ... | 1970(80)    | ...           | 2.05(0.11)   | ...                        | y y y y y y y y y y     |
| 34.3 + 34.1 | 3.785 | 1260(130)   | 1.57(0.04)    | 4.87(0.85)   | 1.65(1.63)                | 0.93(0.91)               | y y y          |
| 34.3 + 34.2 | ... | 1200(130)   | ...           | 5.12(0.47)   | ...                        | y y y         |
| 42.3 + 42.1 | 3.692 | 5690(150)   | 1.43(0.05)    | 1.58(0.05)   | 0.38(0.25)                | 0.21(0.14)               | y y y          |
| 42.3 + 42.2 | ... | 7980(170)   | ...           | 0.87(0.06)   | ...                        | y y y         |
| 42.3 + 42.4 | ... | 7990(180)   | 1.43(0.05)    | 0.88(0.06)   | ...                        | y y y         |
| 42.3 + 42.5 | ... | 8320(220)   | ...           | -0.76(0.19)  | ...                        | y y y         |

AS1063

| Images  | $z$     | $\Delta t$ | $\Delta m_1$ | $\Delta m_2$ | $R_{\text{CC}} \times 10^2$ | $R_{\text{Ia}} \times 10^3$ | Detectable SN types |
|---------|---------|-------------|---------------|---------------|-----------------------------|---------------------------|-------------------|
|         |         | d           | mag           | mag           | yr$^{-1}$                   | yr$^{-1}$                 |                   |
| 1.3 + 1.1 | 1.228 | 2080(70)    | 1.78(0.02)    | 2.84(0.06)   | 1.29(0.68)                | 0.76(0.40)               | y y y y y y y y y y |
| 1.3 + 1.2 | ... | 2030(70)    | ...           | 2.95(0.07)   | ...                        | y y y y y y y y y y     |
| 2.3 + 2.1 | 1.259 | 8930(120)   | 1.23(0.02)    | 3.12(0.05)   | 0.47(0.25)                | 0.29(0.15)               | y y y y y y y y y y |
| 2.3 + 2.2 | ... | 8950(120)   | ...           | 3.07(0.05)   | ...                        | y y y y y y y y y y     |
| 4.3 + 4.1 | 1.258 | 6470(100)   | 1.35(0.02)    | 3.70(0.08)   | 0.008(0.002)              | 0.005(0.001)             | y y y y y y y y y y |
| 4.3 + 4.2 | ... | 6470(100)   | ...           | 3.67(0.08)   | ...                        | y y y y y y y y y y     |
| 5.3 + 5.1 | 1.397 | 4450(110)   | 1.31(0.03)    | 1.64(0.03)   | 4.42(1.75)                | 2.55(0.96)               | y y y y y y y y y y |
| 5.3 + 5.2 | ... | 7790(100)   | ...           | 1.31(0.04)   | ...                        | y y y y y y y y y y     |
| 6.3 + 6.1 | 1.428 | 9900(150)   | 1.35(0.03)    | 2.12(0.04)   | 4.52(2.11)                | 2.70(1.18)               | y y y y y y y y y y |
| 6.3 + 6.2 | ... | 10510(160)  | ...           | 2.07(0.06)   | ...                        | y y y y y y y y y y     |
| 7.1 + 7.2 | 1.837 | 4800(200)   | 1.43(0.03)    | 1.79(0.04)   | 2.21(1.38)                | 1.25(0.76)               | y y y y y y y y y y |
| 7.1 + 7.3 | ... | 3570(160)   | ...           | 2.15(0.04)   | ...                        | y y y y y y y y y y     |
| 11.3 + 11.1 | 3.117 | 3350(180)   | 1.61(0.04)    | 3.43(0.08)   | 0.16(0.02)                | 0.09(0.01)               | y y y y y y y y y y |
| 11.3 + 11.2 | ... | 3370(170)   | ...           | 3.31(0.06)   | ...                        | y y y y y y y y y y     |
| 14.3 + 14.1 | 3.118 | 19540(290)  | 1.04(0.03)    | 1.80(0.14)   | 0.51(0.04)                | 0.29(0.02)               | y y y y y y y y y y |
| 14.3 + 14.2 | ... | 17640(250)  | ...           | 1.95(0.04)   | ...                        | y y y y y y y y y y     |
| 15.3 + 15.1 | 3.060 | 25110(270)  | 0.96(0.02)    | 2.05(0.04)   | 0.34(0.03)                | 0.19(0.01)               | y y y y y y y y y y |
| 15.3 + 15.2 | ... | 24710(250)  | ...           | 2.42(0.04)   | ...                        | y y y y y y y y y y     |
| 17.3 + 17.1 | 3.606 | 21380(280)  | 1.00(0.03)    | 2.24(0.05)   | 2.02(1.82)                | 1.16(1.01)               | y y y y y y y y y y |

Table 3 continued
| Images      | z     | $\Delta t$ | $\Delta m_1$ | $\Delta m_2$, $R_{CC} \times 10^2$, $R_{Ia} \times 10^3$ | Detectable SN types |
|------------|-------|------------|--------------|-------------------------------------------------|-------------------|
| 17.3 + 17.2 | 1.170 | 2.2170(290) | 2.12(0.11)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 19.3 + 19.1 | 1.035 | 860(100)    | 1.82(0.03)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 19.3 + 19.2 | 1.140 | 1400(150)   | 2.32(0.13)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 44.1 + 44.2 | 2.976 | 7580(140)   | 1.27(0.03)   | 0.38(0.02) 0.22(0.04) | y y y y y y y y y |
| 44.1 + 44.3 | 4.300 | 4030(160)   | 1.82(0.04)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 59.3 + 59.1 | 1.875 | 1140(150)   | 1.59(0.04)   | 1.80(0.14) 0.10(0.03) | y y y y y y y y y |
| 59.3 + 59.2 | 2.290 | 1140(150)   | 1.82(0.05)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 70.1 + 70.2 | 3.713 | 9910(180)   | 1.25(0.03)   | 0.09(0.03) 0.05(0.05) | y y y y y y y y y |
| 70.1 + 70.3 | 3.173 | 1730(150)   | 1.33(0.03)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |

**MACSJ1149**

| Images      | z     | $\Delta t$ | $\Delta m_1$ | $\Delta m_2$, $R_{CC} \times 10^2$, $R_{Ia} \times 10^3$ | Detectable SN types |
|------------|-------|------------|--------------|-------------------------------------------------|-------------------|
| 1.3 + 1.1  | 1.488 | 5950(200)  | 1.33(0.04)   | 2.37(0.35) 0.15(0.14) | y y y y y y y y y |
| 1.3 + 1.2  | 1.650 | 6500(200)  | 1.74(0.09)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 2.1 + 2.2  | 1.894 | 840(210)   | 4.69(0.54)   | 0.05(0.02) 0.03(0.01) | y y y y y y y y y |
| 2.1 + 2.3  | 2.840 | 840(200)   | 4.75(0.44)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 3.3 + 3.1  | 3.129 | 3150(300)  | 5.82(1.28)   | 3.47(0.75) 0.25(0.01) | y y y y y y y y y |
| 3.3 + 3.2  | 3.360 | 3560(300)  | 2.63(0.07)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 4.3 + 4.1  | 2.949 | 9950(300)  | 2.33(0.09)   | 2.07(0.35) 0.19(0.21) | y y y y y y y y y |
| 4.3 + 4.2  | 10500| 10500(320)| 1.99(0.06)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 5.3 + 5.1  | 2.800 | 14230(300)| 1.30(0.05)   | 1.30(0.37) 0.80(0.23) | y y y y y y y y y |
| 5.3 + 5.2  | 14290| 14290(300)| 2.70(0.06)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 13.3 + 13.1| 1.240 | 920(80)    | 1.82(0.03)   | 0.13(0.04) 0.08(0.02) | y y y y y y y y y |
| 13.3 + 13.2| 1.990 | 990(60)    | 3.23(0.10)   | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 14.3 + 14.1| 3.703 | 3340(440)  | 4.17(0.27)   | 0.008(0.002) 0.005(0.001) | y y y y y y y y y |
| 14.3 + 14.2| 3330(450)| 4.30(0.27) | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |
| 29.3 + 29.1| 3.214 | 4340(280)  | 1.42(0.05)   | 0.09(0.21) 0.05(0.12) | y y y y y y y y y |
| 29.3 + 29.2| 5870(280)| 1.63(0.07) | 0.25(0.01) 1.6(0.01) | y y y y y y y y y |

**MACSJ0416**

| Images      | z     | $\Delta t$ | $\Delta m_1$ | $\Delta m_2$, $R_{CC} \times 10^2$, $R_{Ia} \times 10^3$ | Detectable SN types |
|------------|-------|------------|--------------|-------------------------------------------------|-------------------|
| 1.3 + 1.1  | 1.896 | 1270(120)  | 1.72(0.04)   | 2.02(0.46) 1.16(0.26) | y y y y y y y y y |

Table 3 continued
| Images   | $z$  | $\Delta t$ | $\Delta m_1$ | $\Delta m_2$ | $R_{CC} \times 10^2$ | $R_{Ia} \times 10^3$ | Detectable SN types |        |
|---------|------|------------|---------------|---------------|----------------------|----------------------|---------------------|--------|
|         |      | yr$^{-1}$  | mag           | mag           | yr$^{-1}$            | yr$^{-1}$            | Ia      | IIP | IIb | IIc | faint$^b$ |
| 1.3 + 1.2 | ...  | 1.89(0.07) | ...           | ...           | ...                 | ...                 | y       | y   | y   | y   | y       |
| 2.3 + 2.1 | 1.893 | 2.04(1.11) | 1.16(0.04)    | 0.52(0.05)    | 0.33(0.04)            | y        | y       | y   | y   | y       |
| 3.3 + 3.1 | 1.989 | 0.93(0.05) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 4.3 + 4.1 | 1.989 | 1.17(0.04) | 1.40(0.24)    | 0.90(0.14)    | y        | y       | y   | y   | y       |
| 4.3 + 4.2 | ...  | 0.87(0.06) | ...           | ...           | y        | y       | y   | y   | y       |
| 5.4 + 5.2 | 2.095 | 2.53(0.07) | 0.64(0.38)    | 0.39(0.21)    | y        | y       | y   | y   | y       |
| 7.3 + 7.1 | 2.086 | ...         | 2.67(0.06)    | 0.061(0.001)  | 0.035(0.001)         | y        | y       | y   | y   | y       |
| 7.3 + 7.2 | ...  | 2.55(0.08) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 10.3 + 10.1| 2.298 | 1.77(0.05) | 1.01(0.21)    | 0.60(0.12)    | y        | y       | y   | y   | y       |
| 10.3 + 10.2| ...  | 1.36(0.07) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 11.3 + 11.1 | 1.006 | 6.01(0.55) | 0.01(0.01)    | 0.01(0.01)    | y        | y       | y   | y   | y       |
| 11.3 + 11.2 | ...  | 5.95(1.80) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 13.3 + 13.1 | 3.223 | 1.88(0.05) | 1.79(0.87)    | 1.14(0.61)    | y        | y       | y   | y   | y       |
| 13.3 + 13.2 | ...  | 0.57(0.05) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 14.1 + 14.2 | 1.637 | 0.93(0.12) | 5.07(0.09)    | 2.86(0.38)    | y        | y       | y   | y   | y       |
| 14.1 + 14.3 | ...  | 1.33(0.05) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 15.3 + 15.1 | 2.336 | 1.69(0.05) | 0.29(0.09)    | 0.16(0.05)    | y        | y       | y   | y   | y       |
| 15.3 + 15.2 | ...  | 0.62(0.06) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 16.1 + 16.2 | 1.964 | 1.86(0.13) | 4.52(1.91)    | 2.56(1.06)    | y        | y       | y   | y   | y       |
| 16.1 + 16.3 | ...  | 1.32(0.05) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 17.3 + 17.1 | 2.218 | 2.38(0.13) | 4.80(1.29)    | 2.74(0.70)    | y        | y       | y   | y   | y       |
| 17.3 + 17.2 | ...  | 3.21(0.21) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 23.1 + 23.2 | 2.091 | 0.22(0.10) | 2.27(0.61)    | 1.29(0.34)    | y        | y       | y   | y   | y       |
| 23.1 + 23.3 | ...  | 1.05(0.03) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
| 27.3 + 27.1 | 2.107 | 1.84(0.03) | 0.33(0.37)    | 0.20(0.20)    | y        | y       | y   | y   | y       |
| 27.3 + 27.2 | ...  | 2.48(0.11) | ...           | ...           | ...                 | y        | y       | y   | y   | y       |
### Table 3 (continued)

| Images       | $z$   | $\Delta t$ | $\Delta m_1$ | $\Delta m_2$ | $R_{CC} \times 10^3$ | $R_{Ia} \times 10^3$ | Detectable SN types |
|--------------|------|------------|--------------|--------------|---------------------|---------------------|-------------------|
|              | d    | mag        | mag          | yr           | yr^{-1}             | yr^{-1}             |                   |
| 29.1 + 29.2  | 2.285| 5420(160)  | 0.95(0.03)   | 3.07(3.76)   | 5.19(1.50)          | 2.99(0.83)          | y y y y y y y     |
| 29.1 + 29.3  | ...  | 2510(160)  | ...          | 1.20(0.04)   | ...                 | ...                 | y y y y y y y     |
| 29.1 + 35.2  | 3.492| 6150(200)  | 0.97(0.05)   | 0.85(0.09)   | 0.47(0.02)          | 0.27(0.03)          | y y y             |
| 35.1 + 35.3  | ...  | 3450(170)  | ...          | 1.40(0.04)   | ...                 | ...                 | y y y             |
| 38.3 + 38.1  | 3.440| 9100(240)  | 1.05(0.04)   | 1.44(0.06)   | 0.25(0.03)          | 0.14(0.02)          | y y y             |
| 38.3 + 38.2  | ...  | 9650(310)  | ...          | 0.84(0.14)   | ...                 | ...                 | y y y             |
| 44.3 + 44.1  | 3.290| 1120(160)  | 1.17(0.04)   | 1.29(0.05)   | 1.21(0.06)          | 0.80(0.70)          | y y y             |
| 44.3 + 44.2  | ...  | 240(150)   | ...          | 1.84(0.07)   | ...                 | ...                 | y y y             |
| 47.3 + 47.1  | 3.253| 10030(220)| 0.78(0.04)   | 2.05(0.07)   | 0.33(0.02)          | 0.208(0.001)        | y y y             |
| 47.3 + 47.2  | ...  | 10370(260)| ...          | 1.40(0.07)   | ...                 | ...                 | y y y             |
| MACSJ0416    |      |            |              |              |                     |                     |                   |
| 49.3 + 49.1  | 3.871| 6110(190)  | 1.06(0.04)   | 0.49(0.07)   | 0.53(0.02)          | 0.29(0.01)          | y y               |
| 49.3 + 49.2  | ...  | 1160(200)  | ...          | 0.86(0.04)   | ...                 | ...                 | y y               |
| 55.2 + 55.1  | 3.292| 14810(220)| 0.66(0.03)   | 1.61(0.04)   | 0.23(0.12)          | 0.15(0.09)          | y y y             |
| 86.3 + 86.1  | 3.292| 3130(180)  | 0.92(0.03)   | 1.35(0.04)   | 0.51(0.36)          | 0.32(0.20)          | y y y             |
| 86.3 + 86.2  | ...  | 6930(200)  | ...          | 0.79(0.11)   | ...                 | ...                 | y y y             |
| MACSJ0717    |      |            |              |              |                     |                     |                   |
| 1.5 + 1.1    | 2.963| 52870(1220)| 1.79(0.09)   | 5.24(0.56)   | 0.42(0.04)          | 0.24(0.02)          | y y y y y y y     |
| 1.5 + 1.2    | ...  | 52840(1200)| ...          | 4.40(0.16)   | ...                 | ...                 | y y y y y y y     |
| 1.5 + 1.3    | ...  | 52940(1260)| ...          | 4.17(0.20)   | ...                 | ...                 | y y y y y y y     |
| 1.5 + 1.4    | ...  | 51460(1420)| ...          | 2.41(0.17)   | ...                 | ...                 | y y y y y y y     |
| 3.3 + 3.1    | 1.855| 17210(1610)| 1.32(0.04)   | 2.32(0.09)   | 0.34(0.10)          | 0.19(0.05)          | y y y y y y y     |
| 3.3 + 3.2    | ...  | 16510(1460)| ...          | 2.98(0.06)   | ...                 | ...                 | y y y y y y y     |
| 4.3 + 4.1    | 1.855| 18020(400) | 1.52(0.05)   | 2.91(0.09)   | 0.79(0.40)          | 0.44(0.22)          | y y y y y y y y   |
| 4.3 + 4.2    | ...  | 15250(430) | ...          | 1.68(0.06)   | ...                 | ...                 | y y y y y y y y   |
| 12.2 + 12.1  | 1.710| 7020(340)  | 1.46(0.05)   | 1.74(0.08)   | 0.99(0.19)          | 0.57(0.10)          | y y y y y y y y   |
| 12.2 + 12.3  | ...  | 1580(520)  | ...          | 2.05(0.04)   | ...                 | ...                 | y y y y y y y y   |
| 13.3 + 13.1  | 2.547| 22600(820) | 1.73(0.04)   | 1.96(0.06)   | 12.74(9.23)         | 7.17(5.14)          | y y y y y y y     |

*Note: All SN types are detectable with the exception of faint.*
Table 3 (continued)

| Images   | z   | $\Delta t$ | $\Delta m_1$ | $\Delta m_2$ | $R_{cc} \times 10^2$ | $R_{Ia} \times 10^3$ | Detectable SN types |
|----------|-----|-------------|--------------|--------------|----------------------|----------------------|---------------------|
|          |     | d (mag)     | mag (yr$^{-1}$) | yr$^{-1}$ | Ia | IIp | IIl | IIin | Ib | Ic | faint$^a$ |
| 13.3 + 13.2 | ⋮   | ⋮            | 7560(820) | ⋮            | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | ⋮ | y | y | y | y | y | y | y | y |
| 14.2 + 14.1 | 1.855 | 14630(530) | 1.45(0.03) | 2.01(0.28) | 1.93(0.88) | 1.09(0.49) | y | y | y | y | y | y |
| 14.2 + 14.3 | ⋮   | ⋮            | 10710(940) | 2.58(0.08) | ⋮ | ⋮ | ⋮ | y | y | y | y | y | y |

$^a$Population of intrinsically faint CC SNe (M$_B > -15$) which could be contributing importantly in the CC SN rates. See e.g. ? for a discussion.