Boosted Solar Light Absorbance in PdS₂/PtS₂ Vertical Heterostructures for Ultrathin Photovoltaic Devices

Lorenzo Bastonero, Giancarlo Cicero, Maurizia Palummo, and Michele Re Fiorentin*

ABSTRACT: Transition-metal dichalcogenides (TMDs) represent a class of materials whose archetypes, such as MoS₂ and WS₂, possess exceptional electronic and optical properties and have been massively exploited in optoelectronic applications. The layered structure allows for their exfoliation to two-dimensional samples with atomic thickness (≤ 1 nm), promising for ultrathin, ultralight devices. In this work, by means of state-of-the-art \textit{ab initio} many-body perturbation theory techniques, we focus on single-layer PdS₂ and PtS₂ and propose a novel van der Waals heterostructure with outstanding light absorbance, reaching up to 50% in the visible spectrum and yielding a maximum short-circuit current of 7.2 mA/cm² under solar irradiation. The computed excitonic landscape predicts a partial charge separation between the two layers and the momentum-forbidden lowest-energy state increases the carrier diffusion length. Our results show that the employment of vertical heterostructures with less conventional TMDs, such as PdS₂/PtS₂, can greatly boost light absorbance and favor the development of more efficient, atomic-thin photovoltaic devices.

KEYWORDS: photovoltaics, TMDs, van der Waals heterostructures, 2D materials, excitons

1. INTRODUCTION

Two-dimensional (2D) materials have elicited great attention over the last few decades thanks to their unique electronic and optical properties induced by their atomic-scale thickness.¹⁻³ A plethora of materials are currently under investigation, and particular interest has been focused on transition-metal dichalcogenides (TMDs) in their monolayer form. TMDs can be easily exfoliated to single layers and allow for largely tunable optoelectronic properties,⁴⁻⁵ thanks to the plentiful possible combinations of transition metal and chalcogen species. For instance, band gaps of monolayer TMDs range from 0.5 to 7.0 eV⁶ and can be both direct and indirect. This wide range of electronic properties can be further enriched by devising vertical van der Waals heterostructures (vdWHs)⁷⁻⁸ between a monolayer TMD and another 2D material, such as graphene⁹⁻¹⁰, black or blue phosphorene,¹¹⁻¹² hexagonal boron nitride,¹³⁻¹⁴ or a different TMD monolayer.¹⁵⁻¹⁶ vdWHs make it possible to realize devices that allow for the separation of the optically excited electrons and holes thanks to the valence and conduction band discontinuities of the two composing layers. Together with nanometer thickness and suitable band gaps, this feature makes TMD vdWHs appealing for the design of ultrathin, ultralight photovoltaic devices.¹⁷ In this respect, it is therefore necessary that the composing layers show significant light absorbance within the solar spectrum. For photon energies varying between 1.5 and 3 eV, widely studied TMDs show absorbance values that roughly range from 5 to 25% for MoS₂,¹⁸ to 20% for MoSe₂ or 17% for WS₂ and WSe₂.¹⁹ Their vdWHs exhibit similar behaviors, for instance, reaching peak values of 10% in MoS₂/WS₂,²⁰ and in MoSe₂/ WSe₂ or 15% in MoS₂/WSe₂.²¹ In combination with the incident AM1.5G solar flux \( \Phi_s(\omega)²² \), the absorbance \( \text{Abs}(\omega) \) determines the maximum short-circuit current that can be extracted from the solar cell as

\[
J_{sc}^{\text{max}} = e \int \text{d} \omega \text{Abs}(\omega) \Phi_s(\omega)
\]

assuming that all photogenerated charge carriers are collected. Common amorphous Si–H and GaAs solar cells in a single-pass configuration show \( J_{sc}^{\text{max}} \) values which lie around 25 and 35 mA/cm², for sample thicknesses above 1 μm, and quickly drop much below 1 mA/cm² when their thickness is decreased to around 1 nm.²³ In contrast, it has been predicted that a 1 nm-thick MoS₂/WS₂ vdWH displays a \( J_{sc}^{\text{max}} \approx 3.5 \text{ mA/cm}^2 \),²⁰ the same value obtained in Si–H or GaAs cells about 1 order of
3. RESULTS AND DISCUSSION

From our DFT calculations, we compute the equilibrium lattice parameters of the isolated monolayers to be $a_{\text{PdS}_2} = 3.53 \text{ Å}$ for 1T-PdS$_2$ and $a_{\text{PtS}_2} = 3.56 \text{ Å}$ for 1T-PtS$_2$, in excellent agreement with the literature. $^{47}$ By vertically stacking the two monolayers in the AA configuration, $^{48}$ we obtain the vdWH geometry represented in Figure 1c, whose equilibrium lattice parameter results in $a_{\text{vdWH}} = 3.57 \text{ Å}$ and interlayer distance in $d = 2.4 \text{ Å}$. The increase in the lattice parameter in the heterostructure can be traced back to the interaction between the layers and the reduced screening, as happens for multilayers of both PdS$_2$ and PtS$_2$. $^{49,50}$ The resulting strain can be estimated as $\epsilon = (a_{\text{vdWH}} - a)/a$, with $i = \text{PtS}_2$ and PdS$_2$. The highest value of $\epsilon$ is obtained for the PdS$_2$ layer, which is subject to about 1.1% tensile strain with respect to its equilibrium geometry. Hence, the monolayers undergo a very mild strain, which does not significantly affect the electronic properties of the system (c.f. Figure S3a in Supporting Information).

2. METHODS

2.1. DFT Calculations. All the DFT calculations reported in this work were performed using the Quantum ESPRESSO suite. $^{33−35}$ For all systems, we employed the Perdew–Burke–Ernzerhof functional $^{36}$ and fully relativistic, norm-conserving pseudopotentials $^{37}$ on a uniform $4 \times 4 \times 1$ Monkhorst-Pack $k$-point mesh. $^{38}$ A kinetic energy cutoff of 70 Ry was adopted. We introduced a 20 Å vacuum region along $z$, the direction perpendicular to the layer planes, to ensure the decoupling of the periodic replicas. In the studied systems, spin–orbit coupling effects can be sizeable and were accounted for in all calculations by means of a fully spinorial treatment. $^{39,40}$ Dispersion forces between the layers of the heterostructure were reproduced within the DFT-D3 semiempirical model. $^{41}$ Structure relaxation was assumed at convergence when the maximum component of the residual forces on the ions was smaller than $10^{-4}$ Ry/Bohr.

2.2. Many-Body Perturbation Theory Calculations. The optimized structures were studied by means of many-body perturbation theory methods as implemented in the YAMBO code. $^{42,43}$ The quasiparticle (QP) electronic structure was obtained within the non-self-consistent $G_0W_0$ approximation. A box cutoff along $z$ was applied on the bare Coulomb potential. The inverse dielectric matrix, $\varepsilon_{\text{QP}}^{-1}$, was obtained within the Godby-Needs plasmon-pole approximation model. $^{44,45}$ As a convergence parameter, we adopted the QP band gap value at the $\Gamma$ point and deemed satisfactory a convergence of this value within $50 \text{ meV}$. Convergence of the $G_0W_0$ calculations with respect to the simulation parameters is shown in Figure S1 in Supporting Information. Following the chosen convergence criterion, we chose a $20 \times 20 \times 1$ $k$-point mesh for all structures.

For both PdS$_2$ and PtS$_2$, 2000 bands were included in the calculation of the dielectric function $\varepsilon_{\text{QP}}^{-1}$ and a 20 Ry cutoff was set on the $G$ vectors in $\varepsilon^{-1}$.

Following refs 6, we obtain the correction to the band gap due to the number of bands included in the correlation self-energy $\Sigma_i$, by extrapolation to the limit of infinite bands, cf. Supporting Information, Figure S1c. For PdS$_2$ and PtS$_2$ monolayers, the calculations can then be performed with 1000 bands explicitly included in the sum and then corrected by the application of a rigid scissor operator of $-0.12 \text{ eV}$. For the vdWH, we employ 4000 bands and 20 Ry in the calculation of the dielectric matrix and 1000 bands in $\Sigma_i$, thanks to the adoption of Bruneval–Gonze terminators. $^{46}$

Convergence of the BSE calculations with respect to the simulation parameters is shown in Figure S2 in Supporting Information. For PdS$_2$ and PtS$_2$, convergence is reached on a $30 \times 30 \times 1$ grid, with 200 bands and a 2 Ry cutoff on the static screening and 6 valence +6 conduction bands in the BSE kernel. In the case of the vdWH, the number of included bands is doubled.
Information). The equilibrium geometries of the isolated monolayers and the vDW are used to compute the electronic band structure at the $G_0W_0$ level, as reported in Figure 2. On top of the $G_0W_0$ quasiparticle energies, we solve the Bethe–Salpeter equation to obtain the light absorption spectrum and excitonic properties, Figure 3. 1T-PdS$_2$, Figure 2a, presents a direct band gap $E_{\text{gap},g} = 2.50$ eV and a direct gap $E_{\text{gap},\text{dir}} = 2.70$ eV in correspondence with the CBm. The optical absorbance $\text{Abs}(\omega)$ is shown in Figure 3a, together with the lowest-energy exciton (blue) and the two brightest states (red and green) contributing to the absorption peak. Their energies and binding energies are reported in Table 1. The shaded areas in Figure 2a mark the excitonic weights of excitons B (blue), G (green), and R (red), projected on the QP band structure. From the shaded regions in Figure 2a, it is possible to notice that the strongest transitions contributing to the excitons, rather than occurring at high symmetry points, take place at k-points at which the valence and conduction bands present a similar slope along the k-path, giving rise to the band-nesting phenomenon. This feature is responsible for large divergencies in the joint density of states (jDOS) which, in turn, influences the material dielectric function, enhancing light absorption. We notice that the absorption peak of monolayer 1T-PdS$_2$ falls around 2 eV and, remarkably, its absorbance reaches up to 55% in that range.

1T-PtS$_2$, Figure 2b, shows a peculiar Mexican-hat-shaped vTB, with a valence band maximum (VBM) and CBm midway between $M$ and $\Gamma$. Although VBM and CBm are closer in $k$-space, the resulting band gap is nonetheless indirect, $E_{\text{gap},g} = 3.05$ eV, while the direct gap is $E_{\text{gap},\text{dir}} = 3.1$ eV. The absorbance spectrum, Figure 3b, is blue-shifted with respect to 1T-PdS$_2$: the absorption peak is due to two excitons (green and red), at around 2.5 eV, and a dark exciton (blue) is the lowest-energy state, about 30 meV below. The peak in absorbance of PtS$_2$ is lower than the one of PdS$_2$ and reaches about 30%. Such a difference in absorbance can be traced back to the different orbital character of the electronic states in the vTB and bCB of the two monolayers. In PdS$_2$, we observe a sizeable participation of sulfur $p$ orbitals in the vTB states, in contrast to PtS$_2$, where $S p$ and Pt $d$ orbitals are almost equally contributing to the topmost valence band (c.f. Supporting Information Figures S4 and S5). The difference in the orbital character results in a stronger band-nesting for PdS$_2$ which, consequently, increases the jDOS, as shown in Figure S6a,b. Moreover, we determined that the independent-particle electric dipole matrix elements $d_{\nu k}$ of the transitions $\nu \rightarrow c$ at $k$, contributing to the absorption peak, are larger in PdS$_2$ than in PtS$_2$, c.f. Figure S6c. The larger jDOS and the stronger dipole elements thus cooperate to enhance the optical absorption of PdS$_2$ with respect to PtS$_2$.

In Figure 3b, at around 2.8 eV, it is also possible to notice a broader peak in the absorption spectrum, originating from states, close in energy, whose main dipole transitions involve the bCB and vTB.

Although less pronounced than in PdS$_2$, the contribution from the $p$-orbitals of the outer S layers to the vTB of PtS$_2$ is non-negligible, Figure S4. Therefore, in a vDW, the vTB of each monolayer is significantly affected by the presence of the facing one, resulting in a vWH vTB which shows sizeable

![Figure 2](image-url)  
Figure 2. $G_0W_0$ band structures of (a) 1T-PdS$_2$, (b) 1T-PtS$_2$, and (c) PdS$_2$/PtS$_2$ vDW aligned to the vacuum level. The shaded areas in red, green, and blue mark the excitonic weights of the R, G, and B states, respectively (see Figure 3). The violet ellipse in (c) indicates the indirect exciton $D$ with finite momentum $q_0$.

![Figure 3](image-url)  
Figure 3. Absorbance $\text{Abs}(\omega)$ of (a) 1T-PdS$_2$, (b) 1T-PtS$_2$, and (c) PdS$_2$/PtS$_2$ vDW. The vertical bars mark the position and relative intensities of the R, G, and B excitons, respectively. In (c), the AM1.5G solar spectrum $\Phi(\omega)$ is reported in light yellow.

| Table 1. Transition Energies $E_{\lambda}$ [eV] and Exciton Binding Energies $E_b$ [eV] of the Analyzed Excitons (B = Blue; R = Red; and G = Green) |
|---|---|---|---|---|---|---|
| B | G | R | B | G | R | B | G | R |
| $E_{\lambda}$ | 1.91 | 1.95 | 2.04 | 2.20 | 2.48 | 2.49 | 1.49 | 1.53 | 2.11 |
| $E_b$ | 0.7 | 0.7 | 0.8 | 0.9 | 0.6 | 0.6 | 0.7 | 0.6 | 0.1 |
contributions from both PdS$_2$ and PtS$_2$ valence band states. In Figure 4, we show the k-resolved density of states (DOS) of the 1T-PdS$_2$/1T-PtS$_2$ heterostructure, projected on the orbitals of the atoms composing the two layers. The bands along the k-path are colored according to the difference between the DOS contributions from the two layers, allowing us to identify on which layer the electronic states at various k-points are spatially localized. As mentioned, the vdWH case, the inversion symmetry is broken; hence, its band structure shows spin–orbit splitting. The band gap is indirect, $E_g^{\text{vdWH}} = 1.72$ eV, between k-points $Q_x$ and $Q_y$, and notably smaller than each monolayer’s. The direct band gap is found to be $E_g^{\text{vdWH}} = 2.17$ eV in correspondence with $Q_z$. The electronic band gap reduction is an expected feature linked to the type-II alignment of the single TMD band structures, cf. Figure 2a,b, and the interaction between the two layers, which determines an upshift of the top valence band, and the increased electronic screening. This similarly entails a reduction in the optical band gap, as shown in Figure 3c. The absorption onset red-shifts to about 1.5 eV and stems from a bright exciton (labeled “green”, G) at 1.53 eV, cf. Table 1. This exciton is almost degenerate in energy with the lowest-energy, dark state (blue, B), whose constituting transitions take place at the same k-points as the green exciton but connect states with the opposite spin.

By means of eq 1 and the absorbance spectra in Figure 3, we can compute the maximum short-circuit currents that can be extracted from the monolayers and from the vdWH, in the idealized situation of total carrier collection at the electrodes. 1T-PtS$_2$ has a higher-energy absorption edge and a moderate absorption, resulting in $J_{\text{sc}}^{\text{max}} = 1.9$ mA/cm$^2$, while 1T-PdS$_2$ shows a lower absorption onset and outstanding absorbance values so that its maximum short-circuit current reaches 5.4 mA/cm$^2$. The vdWH shows less pronounced absorbance peaks than 1T-PdS$_2$; however, the optical gap falls at lower energy, optimizing sunlight absorption in the visible range. Hence, the short-circuit current of the heterostructure reaches 7.2 mA/cm$^2$, slightly lower than the sum of the $J_{\text{sc}}^{\text{max}}$ of the isolated monolayers. The predicted value of maximum short-circuit current is exceptionally high and can largely boost the efficiency of a device made with such a vdWH. As a comparison, the obtained maximum short-circuit current is twice the predicted value in MoS$_2$/WS$_2$ vdWH$^{55}$ and can be obtained with amorphous Si–H samples about 2 orders of magnitude thicker.

The brightest excitons, red and green, which induce the peaks in the absorption spectrum of the vdWH, vertically excite electrons and holes at k-points away from the CBM and VBM, respectively. In mono- and few-layer TMDs, intraband relaxation is very fast ($\lesssim 500$ fs)$^{52,53}$ therefore, we can expect a rapid relaxation of the optically active excitons to the dark, indirect exciton $D$, involving states at the CBM and VBM, violet ellipse in Figure 2c. The relaxation to this exciton, with finite momentum $q_D = Q_x - Q_y$ is energetically favorable, since $E_D = 1.15$ eV, smaller than the dark direct exciton $B$. Being momentum-forbidden, the radiative recombination of state $D$ is suppressed and, consequently, its lifetime is largely enhanced with respect to bright excitons.$^{54}$ Electron–hole recombination is therefore slowed down, and the carrier diffusion length increased. Hence, due to the indirect gap in the 1T-PdS$_2$/1T-PtS$_2$ heterostructure, we expect carrier diffusion lengths longer than 20 $\mu$m, as recently measured in the direct-gap WS$_2$/WSe$_2$ vdWH.$^{55}$ The expected sizeable diffusion length will then contribute to enhance the actual short-circuit current of the real device, by increasing the

Figure 4. 1T-PdS$_2$/1T-PtS$_2$ vdWH k-resolved projected density of states superimposed to the DFT band structure. Each state is colored according to the size of the contributions from PdS$_2$ (red) and PtS$_2$ (blue) orbitals.

Figure 5. Side (upper panels) and top (lower panels) views of the square modulus excitonic wave function $|\Psi_{\lambda\mu}(r)\rangle = |r\rangle|\xi_\lambda\rangle$ for states $\lambda = D$ (a) and $\lambda = G$ (b). In both (a,b), the electron is marked by the green diamond and kept fixed on PdS$_2$. 

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https://doi.org/10.1021/acsami.1c11245
collection probability, thus positively impacting on the efficiency of the cell. These efficiency boosting factors, that is, very large absorbance and increased diffusion length, can then counterbalance the limited charge separation due to the mixed PdS\textsubscript{2}–PtS\textsubscript{2} states in the tVB, cf. Figure 4, that could also act as recombination centers. Indeed, the optically excited electrons will populate states which are well spatially localized on the PdS\textsubscript{2} layer, while the holes will still present a sizeable delocalization on both monolayers. In Figure 5a, we show the square modulus of the $D$ exciton wave function as a function of the hole position $\Psi_{D}(\mathbf{r}_{e} = r')^{2}$, when the electron is fixed at $r'$ on the PdS\textsubscript{2} layer, in a region with maximum probability density. The electron is marked by the green diamond on the PdS\textsubscript{2} layer. The electron and hole show a peculiar in-plane spatial separation, due to the electronic orbitals involved in $D$. As a comparison, in Figure 5b, we report the square modulus of the bright, $G$ exciton wave function, with fixed electron in the same position. It is evident that the $G$ and $D$ excitons are not spatially indirect between the two layers, and their wave functions involve both PdS\textsubscript{2} and PtS\textsubscript{2}. From Figure 5a, it is possible to notice that the hole is fairly delocalized on both layers and it is possible to obtain the probability of finding the hole on the PtS\textsubscript{2} layer as $\int_{z_{0}} \Psi_{D}(\mathbf{r}_{e} = r')^{2} \approx 50\%$, where $z_{0}$ defines the intermediate plane between the two monolayers. This provides us with an estimate of the charge separation probability, given that the hole distribution varies little when the electron position is moved in the region of sizeable probability density, concentrated on PdS\textsubscript{2}. The estimated charge separation is not complete, however, its magnitude, combined with the encouraging properties previously highlighted, can be nonetheless adequate for viable applications of the proposed vdWH. Moreover, it has been proven that spatially indirect excitons inducing interlayer charge separation can be enhanced by applying strain\textsuperscript{5,57} to the heterostructure or controlled through electric fields,\textsuperscript{56} thus conceivably leaving room for further efficiency improvements.

4. CONCLUSIONS

The field of nanoscale photovoltaic devices is still in open development and appears alluring for its potential to compete with conventional systems. The intrinsic advantages of ultrathin, ultralight devices urge the research activities toward improved efficiency and design. The employment of monolayer TMDs in heterostructures has been proposed and investigated, with most attention paid to group-VI TMDs, such as MoS\textsubscript{2} and WS\textsubscript{2}, which have provided encouraging results. A key factor for choosing TMDs for this type of application resides in their large light-electron coupling, which results in sizeable light absorbance. Our worked the remarkable properties of two, less common, TMDs, PdS\textsubscript{2} and PtS\textsubscript{2}, which can be positively employed in the domain of photovoltaics. In particular, the uncommon absorbance of 1T-PdS\textsubscript{2} is inherited by the low-strain vdWH with PtS\textsubscript{2} which also shows a very favorable optical gap at around 1.5 eV. This translates into exceptionally high maximum short-circuit currents, $J_{SC}^{max} = 7.2$ mA/cm\textsuperscript{2}, about twice the values previously reported for MoS\textsubscript{2}/WS\textsubscript{2} vdWH. Although the predicted charge separation is partial, the high absorbance, together with the extended carrier diffusion length, due to the indirect electronic band gap, can turn out very advantageous for improving the efficiency of nanometer-thick photovoltaic devices.

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