An Intelligent Mining Model for Medical Diagnosis of Heart Disease Based on Rough Set Data Analysis

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Abstract

Medical databases have accumulated large quantities of information about patients and their medical conditions. The classification of a set of objects into predefined homogeneous groups is a problem with major practical interest in many fields, in particular, in medical sciences. It is well established fact that right decision at right time provides an advantage in medical diagnosis. Therefore, most important challenge is to retrieve data pattern from the accumulated voluminous data and dealing with the incomplete and vague information in classification and data analysis. Thus, the ultimate goal of this work is to present an intelligent model for mining and generating classification rules for medical diagnosis based on rough sets theory. Rough sets with Boolean reasoning discretization algorithm is introduced to discretize the data, then the rough set reduction technique is applied to find all reducts. Finally, a set of generalized rules for heart diagnosis was extracted. The proposed model shows a higher overall accuracy rates and generate more compact rules.

Keywords: Medical diagnosis; heart disease; classifications; Rough set theory; feature selection.

1) INTRODUCTION

Medical databases have accumulated large quantities of information about patients and their medical conditions. Relationships and patterns within these data could provide new medical knowledge [1, 2]. Analysis of medical data is often concerned with treatment of incomplete knowledge, with management of inconsistent pieces of information and with manipulation of various levels of representation of data. Existing intelligent techniques of data analysis are mainly based on quite strong assumptions (some knowledge about dependencies, probability distributions, large number of experiments), that are unable to derive conclusions from incomplete knowledge or cannot manage inconsistent pieces of information. The classification of a set of objects into predefined homogenous groups is a problem with major practical interest in many fields, in particular, in medical sciences [3].

Over the past two decades, several traditional multivariate statistical classification approaches, such as the linear discriminant analysis and the quadratic discriminant analysis, have been developed to address the classification problem. More advanced and intelligent techniques have been used in medical data analysis such as neural network, Bayesian classifier, genetic algorithms, decision trees, fuzzy theory, and rough set. Each one of these techniques has its own properties and features including their ability of finding important rules and information that could be useful for the medical field domain. Each of these techniques contributes a distinct methodology for addressing problems in its domain.

Rough set theory [4] is a fairly new intelligent technique that has been applied to the medical domain, and is used for the discovery of data dependencies, evaluates the importance of attributes, discovers the patterns of data, reduces all redundant objects and attributes, and seeks the minimum subset of attributes. Moreover, it is being used for the extraction of rules from databases. Many heuristic algorithms are proposed based on rough set theory, also numerous approached based on rough set theory and other theories are investigated to extract decision rules and reduce the dimensionality of dataset [5-18]. One advantage of the rough set is the creation of readable if-then rules. Such rules have a potential to reveal new patterns in the data material. Thus, the ultimate goal of this work is to present an intelligent Model for mining and generating classification Rules for Medical Diagnosis of Heart Disease based on rough sets theory.

2) PROBLEM FORMULATION

Heart disease describes a range of conditions that affect the heart. Diseases under the heart disease umbrella include blood vessel diseases, such as coronary artery disease; heart rhythm problems (arrhythmias); and heart defects you're born with (congenital heart defects), among others. In other words we can say that Heart disease is an umbrella term for any disorder that affects the structure and functions of the heart and circulation. The term "heart disease" is often used interchangeably with the term "cardiovascular disease." Cardiovascular disease generally refers to conditions that involve narrowed or blocked blood vessels that can lead to a heart attack, chest pain (angina) or stroke. Other heart conditions, such as those that affect the heart's muscle, valves or rhythm, also are considered forms of heart disease. There
are many types of heart disease, and each one has its own symptoms and treatment [19]. Fig. 1 shows the main types of heart disease.

The most common symptom of heart disease is chest pain and it is of four types, viz. typical angina, atypical angina, non-anginal pain and asymptomatic. The other symptoms included are blood pressure, cholesterol, blood sugar, electrocardiography, maximum heart rate, exercise, old peak, thallium scan, sex and age. Each patient’s treatment is different and depends on several factors. Thus, it is essential to identify certain rules and the chief factors so that a patient can identify the disease at an early stage. It can also reduce the financial burden of a patient.

The ultimate goal of this work is to present an intelligent model for mining and generating classification rules for medical diagnosis of heart disease based on rough sets theory. Here numerical and literature values based on different symptoms were collected to the heart disease have collected from literature [20]. We consider the diagnosis decision of the patients as the decision variable. The attributes that play major role in heart disease are presented in the decision table shown in Table 1, where to write it in a simple form and to make our analysis simple we used the coding shown in table 1.

### Table 1. Coding system for the Symptoms and decision attribute

| Attribute          | Attribute code | Attribute value  | Code of the Attribute value |
|--------------------|----------------|------------------|-----------------------------|
| Chest pain (CP)    | a1             | Typical angina   | 1                           |
|                    |                | A typical angina | 2                           |
|                    |                | Non-anginal pain | 3                           |
|                    |                | Asymptomatic     | 4                           |
| **Blood pressure (BP)** | **Type** | **1** | **2** | **3** | **4** |
|------------------------|----------|------|------|------|------|
| **Cholesterol (CH)-LDL** | **Type** | **1** | **2** | **3** | **4** |
| **Fasting Blood sugar (FBS)** | **Type** | **1** | **2** |
| **Electrocardiography (ECG)** | **Type** | **1** | **2** | **3** |
| **Maximum heart rate (MHR)** | **Type** | **1** | **2** | **3** |
| **Exercise (EX)** | **Type** | **1** | **2** |
| **Old peak (OP)** | **Type** | **1** | **2** | **3** |
| **Thallium scan (TS)** | **Type** | **1** | **2** | **3** |
| **Sex (SX)** | **Type** | **1** | **2** |
| **Age** | **Type** | **1** | **2** | **3** | **4** |
| **Type of diagnosis (TD)** | **Type** | **1** | **2** | **3** | **4** | **5** |

- **Blood pressure (BP)**: Normal, Medium, High, Very high
- **Cholesterol (CH)-LDL**: low, medium, high, Very high
- **Fasting Blood sugar (FBS)**: normal, high
- **Electrocardiography (ECG)**: normal, ST-T abnormal, hypertrophy
- **Maximum heart rate (MHR)**: medium, normal, high
- **Exercise (EX)**: false, true
- **Old peak (OP)**: low, risk, temble
- **Thallium scan (TS)**: normal, Fixed defect, Reversible defect
- **Sex (SX)**: male, female
- **Age**: young, mild, old, Very old
- **Type of diagnosis (TD)**: Hypertensive heart disease, Coronary heart disease, Heart failure, Potential patient, Cardiomyopathy
### Table 2. Decision table for heart disease diagnosis

| U  | a1 | a2 | a3 | a4 | a5 | a6 | a7 | a8 | a9 | a10 | a11 | Type of diagnosis (d) |
|----|----|----|----|----|----|----|----|----|----|-----|----|-----------------------|
| X1 | *  | 4  | *  | *  | 2  | *  | *  | 2  | *  | 1   | *  | 1                     |
| X2 | 2  | 3  | *  | *  | *  | 3  | 1  | *  | *  | *   | 1  | 1                     |
| X3 | 3  | 1  | 1  | *  | 3  | *  | *  | *  | *  | *   | 1  | 1                     |
| X4 | 2  | *  | 1  | *  | *  | *  | *  | *  | 2  | *   | *  | 1                     |
| X5 | 3  | *  | *  | *  | 1  | *  | *  | *  | *  | 3   | 1  | 1                     |
| X6 | *  | *  | *  | *  | 2  | 2  | *  | *  | *  | 1   | 1  | 1                     |
| X7 | *  | *  | *  | *  | 1  | *  | 2  | *  | *  | 4   | 1  | 1                     |
| X8 | *  | 4  | 4  | *  | *  | *  | *  | *  | 3   | 2  | 1  |                       |
| X9 | *  | 4  | 4  | *  | *  | *  | 1  | *  | *  | *   | 1  | 1                     |
| X10| *  | 2  | 4  | *  | *  | *  | *  | 1  | *  | *   | 1  | 2                     |
| X11| *  | *  | 1  | *  | *  | 1  | 2  | 3  | *  | *   | 1  | 2                     |
| X12| 2  | 4  | *  | *  | *  | 1  | 1  | *  | 2   | *   | 1  | 2                     |
| X13| 3  | *  | *  | *  | 3  | 1  | *  | *  | 2   | *   | 1  | 2                     |
| X14| *  | 4  | *  | *  | *  | 2  | *  | 1  | *   | 1   | 1  | 2                     |
| X15| 2  | *  | 3  | *  | *  | *  | *  | 3  | 2   | 3   | 2  |                       |
| X16| 2  | 2  | *  | *  | *  | *  | *  | *  | 3   | 4   | 2  |                       |
| X17| 4  | 4  | 4  | *  | *  | *  | *  | *  | 4   | 4   | 2  |                       |
| X18| *  | *  | 1  | *  | *  | 3  | *  | *  | *   | *   | 1  | 2                     |
| X19| *  | 2  | 3  | *  | *  | *  | 3  | *  | *   | *   | 3  |                       |
| X20| 3  | *  | *  | *  | *  | 3  | 2  | *  | *   | 3   | 3  |                       |
| X21| 4  | 1  | 2  | *  | 2  | *  | *  | *  | *   | *   | 3  |                       |
| X22| *  | 4  | *  | *  | *  | *  | *  | *  | 2   | 1   | 3  |                       |
| X23| 3  | 1  | *  | *  | 1  | *  | *  | *  | *   | *   | 3  |                       |
| X24| *  | *  | *  | *  | *  | *  | 1  | 2  | 3   | *   | 1  | 3                     |
| X25| *  | 3  | 4  | *  | 2  | *  | 2  | *  | 2   | *   | 3  |                       |
| X26| *  | *  | *  | *  | 2  | *  | *  | *  | *   | 2   | 3  |                       |
| X27| *  | 4  | *  | *  | *  | *  | *  | 3  | 2   | *   | 4  | 3                     |
| X28| 2  | 2  | *  | *  | *  | *  | 1  | *  | 2   | 3   | 3  |                       |
| X29| *  | *  | *  | *  | *  | *  | 2  | *  | 3   | 3   | 3  |                       |
| X30| *  | *  | 1  | 1  | 3  | *  | *  | 3   | *   | 1   | 3  |                       |
| X31| 4  | 4  | *  | *  | *  | 1  | *  | *  | *   | *   | 3  |                       |
| X32| 1  | 4  | *  | *  | *  | 3  | 2  | *  | 4   | 3   | 3  |                       |
| X33| 3  | *  | 3  | *  | *  | *  | 2  | *  | *   | 3   | 3  |                       |
| X34| 3  | *  | 1  | *  | *  | *  | 2  | *  | 2   | *   | 4  |                       |
| X35| 4  | *  | *  | *  | *  | *  | 2  | *  | *   | *   | 4  |                       |
| X36| *  | *  | *  | *  | 2  | *  | *  | 1  | 1   | *   | 2  | 4                     |
| X37| 3  | *  | *  | *  | *  | *  | *  | *  | *   | *   | 4  |                       |
| X38| 2  | 2  | 2  | *  | *  | *  | 1  | *  | *   | *   | 3  | 4                     |
| X39| 3  | *  | 4  | *  | *  | *  | *  | 1  | *   | 1   | 4  |                       |
In this section, we will discuss the proposed rough sets scheme to analyze, mining and generating classification rules for medical diagnosis of heart disease. The scheme used in this study consists of two main stages: preprocessing and processing. Preprocessing stage includes tasks such as data cleaning, completeness, correctness, attribute creation, attribute selection and discretization. Processing includes the generation of preliminary knowledge, such as computation of object reducts from data and derivation of rules from reducts. Fig. 2 shows the overall steps in the proposed rough sets data analysis scheme.

With the aid of software called ROSETTA which is an RST analysis toolkit, rough sets with Boolean reasoning discretization algorithm is introduced to discretize the data, then the rough set reduction technique is applied to find all reducts of the data which contains the minimal subset of attributes that are associated with a class label for classification as shown in table 3. Finally, the rough sets dependency rules are generated directly from all generated reducts as shown in table 4.

3) ANALYSIS

In this section, we will discuss the proposed rough sets scheme to analyze, mining and generating classification rules for medical diagnosis of heart disease. The scheme used in this study consists of two main stages: preprocessing and processing. Preprocessing stage includes tasks such as data cleaning, completeness, correctness, attribute creation, attribute selection and discretization. Processing includes the generation of preliminary knowledge, such as computation of object reducts from data and derivation of rules from reducts. Fig. 2 shows the overall steps in the proposed rough sets data analysis scheme.

* Means do not care condition

| X40 | 2 | 3 | * | * | * | * | * | 1 | * | * | * | 4 |
|-----|---|---|---|---|---|---|---|---|---|---|---|---|
| X41 |   | 3 | * | * | * | * | * | 1 | * | * | * | 4 |
| X42 |   | 4 | 2 | * | 3 | * | * | * | * | 3 | 4 |
| X43 | 2 | * | * | * | 1 | * | 1 | * | * | * | 5 |
| X44 | 4 | * | 1 | * | * | * | * | 1 | * | 1 | 5 |
| X45 |   | 2 | 2 | * | 3 | * | 1 | * | 1 | * | 5 |
| X46 |   | * | 2 | * | * | * | * | * | 1 | * | 2 | 5 |
| X47 | 4 | 2 | * | * | * | * | 1 | * | 2 | 5 |
| X48 | 3 | * | 4 | * | * | * | * | * | 1 | * | 5 |

Fig. 2: the overall steps of the proposed intelligent model.
Table 3. Reducts of Table 2.

| Reduct                  | Support | Length |
|-------------------------|---------|--------|
| {a2, a5, a8, a9, a11}   | 100     | 5      |
| {a2, a3, a5, a8, a9, a11} | 100     | 6      |
| {a1, a5, a7, a8, a9, a11} | 100     | 6      |
| {a3, a5, a6, a7, a8, a11} | 100     | 6      |
| {a1, a2, a3, a5, a8, a11} | 100     | 6      |
| {a2, a3, a5, a7, a8, a10, a11} | 100     | 7      |
| {a2, a3, a4, a7, a9, a10, a11} | 100     | 7      |
| {a1, a3, a5, a8, a9, a10, a11} | 100     | 7      |
| {a1, a2, a3, a6, a7, a8, a11} | 100     | 7      |
| {a2, a3, a6, a8, a9, a10, a11} | 100     | 7      |
| {a1, a3, a4, a5, a6, a8, a11} | 100     | 7      |
| {a2, a3, a4, a6, a9, a10, a11} | 100     | 7      |
| {a1, a3, a5, a6, a8, a9, a11} | 100     | 7      |
| {a1, a2, a3, a4, a7, a9, a11} | 100     | 7      |
| {a3, a4, a5, a6, a8, a9, a10, a11} | 100     | 8      |
| {a1, a3, a4, a5, a6, a7, a9, a11} | 100     | 8      |
| {a1, a2, a3, a4, a5, a6, a9, a11} | 100     | 8      |

Table 4. The rough sets dependency rules generated to diagnose the heart disease

| Rule                                                                 | LHS Coverage | RHS Coverage |
|---------------------------------------------------------------------|--------------|--------------|
| a2(4) AND a5(2) AND a8(2) AND a9(*) AND a11(*) => d(1)              | 0.020833     | 0.111111     |
| a2(3) AND a5(*) AND a8(*) AND a9(*) AND a11(*) => d(1)              | 0.020833     | 0.111111     |
| a2(1) AND a5(3) AND a8(*) AND a9(*) AND a11(*) => d(1)              | 0.020833     | 0.111111     |
| a2(*) AND a5(*) AND a8(*) AND a9(2) AND a11(*) => d(1)              | 0.020833     | 0.111111     |
| a2(*) AND a5(1) AND a8(*) AND a9(*) AND a11(3) => d(1)              | 0.020833     | 0.111111     |
| a2(*) AND a5(*) AND a8(*) AND a9(*) AND a11(1) => d(1)              | 0.020833     | 0.111111     |
| a2(*) AND a5(1) AND a8(*) AND a9(*) AND a11(4) => d(1)              | 0.020833     | 0.111111     |
|   | Formula                                                                 |   |   |
|---|------------------------------------------------------------------------|---|---|
| 8 | $a_2(4) \land a_5(*) \land a_8(*) \land a_9(3) \land a_{11}(2) \Rightarrow d(1)$ | 0.020833 | 0.111111 |
| 9 | $a_2(4) \land a_5(*) \land a_8(3) \land a_9(*) \land a_{11}(*) \Rightarrow d(1)$ | 0.020833 | 0.111111 |
|10 | $a_2(2) \land a_5(*) \land a_8(1) \land a_9(*) \land a_{11}(*) \Rightarrow d(2)$ | 0.020833 | 0.111111 |
|11 | $a_2(*) \land a_5(*) \land a_8(2) \land a_9(3) \land a_{11}(*) \Rightarrow d(2)$ | 0.020833 | 0.111111 |
|12 | $a_2(4) \land a_5(*) \land a_8(*) \land a_9(2) \land a_{11}(*) \Rightarrow d(2)$ | 0.020833 | 0.111111 |
|13 | $a_2(*) \land a_5(3) \land a_8(*) \land a_9(2) \land a_{11}(*) \Rightarrow d(2)$ | 0.020833 | 0.111111 |
|14 | $a_2(4) \land a_5(2) \land a_8(*) \land a_9(*) \land a_{11}(1) \Rightarrow d(2)$ | 0.020833 | 0.111111 |
|15 | $a_2(*) \land a_5(*) \land a_8(*) \land a_9(3) \land a_{11}(3) \Rightarrow d(2)$ | 0.020833 | 0.111111 |
|16 | $a_2(2) \land a_5(*) \land a_8(*) \land a_9(3) \land a_{11}(4) \Rightarrow d(2)$ | 0.020833 | 0.111111 |
|17 | $a_2(4) \land a_5(*) \land a_8(*) \land a_9(*) \land a_{11}(4) \Rightarrow d(2)$ | 0.020833 | 0.111111 |
|18 | $a_2(*) \land a_5(3) \land a_8(*) \land a_9(*) \land a_{11}(1) \Rightarrow d(2)$ | 0.020833 | 0.111111 |
|19 | $a_2(2) \land a_5(*) \land a_8(3) \land a_9(*) \land a_{11}(*) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|20 | $a_2(*) \land a_5(*) \land a_8(*) \land a_9(*) \land a_{11}(3) \Rightarrow d(3)$ | 0.041667 | 0.133333 |
|21 | $a_2(1) \land a_5(2) \land a_8(*) \land a_9(*) \land a_{11}(*) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|22 | $a_2(4) \land a_5(*) \land a_8(*) \land a_9(*) \land a_{11}(1) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|23 | $a_2(1) \land a_5(1) \land a_8(*) \land a_9(*) \land a_{11}(*) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|24 | $a_2(*) \land a_5(*) \land a_8(2) \land a_9(3) \land a_{11}(1) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|25 | $a_2(3) \land a_5(2) \land a_8(*) \land a_9(2) \land a_{11}(*) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|26 | $a_2(*) \land a_5(2) \land a_8(*) \land a_9(*) \land a_{11}(2) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|27 | $a_2(4) \land a_5(*) \land a_8(3) \land a_9(2) \land a_{11}(4) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|28 | $a_2(2) \land a_5(*) \land a_8(1) \land a_9(*) \land a_{11}(3) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|29 | $a_2(*) \land a_5(*) \land a_8(*) \land a_9(2) \land a_{11}(3) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|30 | $a_2(*) \land a_5(3) \land a_8(*) \land a_9(*) \land a_{11}(1) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|31 | $a_2(4) \land a_5(*) \land a_8(*) \land a_9(*) \land a_{11}(*) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|32 | $a_2(*) \land a_5(*) \land a_8(3) \land a_9(2) \land a_{11}(4) \Rightarrow d(3)$ | 0.020833 | 0.066667 |
|33 | $a_2(*) \land a_5(*) \land a_8(2) \land a_9(*) \land a_{11}(*) \Rightarrow d(4)$ | 0.041667 | 0.222222 |
|34 | $a_2(*) \land a_5(2) \land a_8(1) \land a_9(1) \land a_{11}(2) \Rightarrow d(4)$ | 0.020833 | 0.111111 |
|35 | $a_2(*) \land a_5(*) \land a_8(*) \land a_9(*) \land a_{11}(*) \Rightarrow d(4)$ | 0.020833 | 0.111111 |
|36 | $a_2(2) \land a_5(*) \land a_8(*) \land a_9(*) \land a_{11}(3) \Rightarrow d(4)$ | 0.020833 | 0.111111 |
CONCLUSION
In this paper, an intelligent data analysis approach based on rough sets theory for mining and generating classification rules for heart disease diagnosing. Further these suitable rules are explored to identify the chief characteristics affecting the relationship between heart disease and its attributes. This helps the decision maker a priori detection of the heart disease. The obtained results are in good agreement with previous studies. The technique has been simplified logic-based rules, reduces the time and resources required to building knowledge. an extension work of using rough sets with other intelligent systems like neural networks, genetic algorithms, fuzzy approaches, and so forth, will be considered in the future work.

ACKNOWLEDGMENTS
The author thank Prince Sattam bin Abdulaziz University, Deanship of Scientific Research at Prince Sattam bin Abdulaziz University for their continuous support and encouragement.

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