MEASURING FUNDAMENTAL PARAMETERS OF SUBSTELLAR OBJECTS. I. SURFACE GRAVITIES

Subhanjoy Mohanty, 1 Gibor Basri, 2 Ray Jayawardhana, 3 France Allard, 4 Peter Hauschildt, 5 and David Ardila 6

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ABSTRACT

We present an analysis of high-resolution optical spectra for a sample of very young, mid- to late-M, low-mass stellar and substellar objects: 11 in the Upper Scorpius association, and two (GG Tau Ba and Bb) in the Taurus star-forming region. Effective temperatures and surface gravities are derived from a multiple-feature spectral analysis using TiO, Na I, and K I, through comparison with the latest synthetic spectra. We show that these spectral diagnostics complement each other, removing degeneracies with temperature and gravity in the behavior of each. In combination, they allow us to determine temperature to within 50 K and gravity to within 0.25 dex, in very cool young objects. Our high-resolution spectral analysis does not require extinction estimates. Moreover, it yields temperatures and gravities independent of theoretical evolutionary models (although our estimates do depend on the synthetic spectral modeling). We find that our gravities for most of the sample agree remarkably well with the isochrone predictions for the likely cluster ages. However, discrepancies appear in our coolest targets: these appear to have significantly lower gravity (by up to 0.75 dex) than our hotter objects, even though our entire sample covers a relatively narrow range in effective temperature (∼300 K). This drop in gravity is also implied by intercomparisons of the data alone, without recourse to synthetic spectra. We consider, and argue against, dust opacity, cool stellar spots, or metallicity differences leading to the observed spectral effects; a real decline in gravity is strongly indicated. Such gravity variations are contrary to the predictions of the evolutionary tracks, causing improbably low ages to be inferred from the tracks for our coolest targets. Through a simple consideration of contraction timescales, we quantify the age errors introduced into the tracks through the particular choice of initial conditions and demonstrate that they can be significant for low-mass objects that are only a few megayears old. However, we also find that these errors appear insufficient to explain the magnitude of the age offsets in our lowest gravity targets. We venture that this apparent age offset may arise from evolutionary model uncertainties related to accretion, deuterium burning and/or convection effects. Finally, when combined with photometry and distance information, our technique for deriving surface gravities and effective temperatures provides a way of obtaining masses and radii for substellar objects independent of evolutionary models: radius and mass determinations are presented in Paper II.

Subject headings: line: profiles — open clusters and associations: individual (Upper Scorpius, Taurus-Auriga) — stars: fundamental parameters — stars: low-mass, brown dwarfs — stars: pre–main-sequence — techniques: spectroscopic

1. INTRODUCTION

In the study of stars, there is perhaps no parameter more fundamental than stellar mass, which is pivotal in determining the entire evolutionary path traced by a star. With the discovery of brown dwarfs, mass determination has become particularly important at the bottom of the main sequence. After all, the very notion of brown dwarfs is predicated on mass: these are substellar objects, which is to say they are less massive than the hydrogen-burning limit of ∼80 M J. The derivation of ultralow masses has become particularly crucial in the light of new theoretical evolutionary models (although our estimates do not depend on the synthetic spectral modeling). We find that our gravities for most of the sample agree remarkably well with the isochrone predictions for the likely cluster ages. However, discrepancies appear in our coolest targets: these appear to have significantly lower gravity (by up to 0.75 dex) than our hotter objects, even though our entire sample covers a relatively narrow range in effective temperature (∼300 K). This drop in gravity is also implied by intercomparisons of the data alone, without recourse to synthetic spectra. We consider, and argue against, dust opacity, cool stellar spots, or metallicity differences leading to the observed spectral effects; a real decline in gravity is strongly indicated. Such gravity variations are contrary to the predictions of the evolutionary tracks, causing improbably low ages to be inferred from the tracks for our coolest targets. Through a simple consideration of contraction timescales, we quantify the age errors introduced into the tracks through the particular choice of initial conditions and demonstrate that they can be significant for low-mass objects that are only a few megayears old. However, we also find that these errors appear insufficient to explain the magnitude of the age offsets in our lowest gravity targets. We venture that this apparent age offset may arise from evolutionary model uncertainties related to accretion, deuterium burning and/or convection effects. Finally, when combined with photometry and distance information, our technique for deriving surface gravities and effective temperatures provides a way of obtaining masses and radii for substellar objects independent of evolutionary models: radius and mass determinations are presented in Paper II.

planemos and brown dwarfs are substellar, the distinction between the two is drawn at the fusion boundary of ∼13 M J; brown dwarfs undergo an initial phase of deuterium fusion, while planemos never harbor any fusion at all. The existence of isolated planemos with a few Jupiter masses, if proven, has significant consequences for both star and planet formation (Padoan & Nordlund 2002; Bate et al. 2002; Boss 2001). However, the key issue of whether the newly discovered free-floating objects really have planetary masses, or are simply misidentified brown dwarfs, remains unsettled for reasons we touch on below. Only a precise mass derivation can unambiguously resolve this question.

The empirical determination of substellar masses, though, has so far proven rather difficult. The most direct approach is to apply Kepler's laws to binary (or higher order) systems with known orbital parameters, in order to obtain a “dynamical mass.” If the components can be directly observed, then the mass can be related to their other properties, such as temperature and luminosity, and the dynamical mass results extended to other directly detected bodies for which a dynamical mass cannot be acquired (e.g., free-floating objects). However, suitable systems with brown dwarf components remain elusive (although a handful are now coming to light; e.g., Close et al. 2002; Potter et al. 2002; Lane et al. 2001). Dynamical masses for planemos in circumstellar planetary systems (i.e., extrasolar

1 Harvard-Smithsonian Center for Astrophysics, Cambridge, MA 02138; smohanty@cfa.harvard.edu.
2 Astronomy Department, University of California, Berkeley, CA 94720; basri@soleil.berkeley.edu.
3 Astronomy Department, University of Michigan, Ann Arbor, MI 48109; rayjay@astro.lsa.umich.edu.
4 CRAL, École Normale Supérieure, 46 Allée d’Italie, Lyon, 69364, France; fallard@ens-lyon.fr.
5 Hamburger Sternwarte, Universitaet Hamburg, 21029 Hamburg, Germany; phauschildt@hs.uni-hamburg.de.
6 Bloomberg Center for Physics and Astronomy, Johns Hopkins University, Baltimore, MD 21218; ardila@adcam.pha.jhu.edu.
planets) have been derived, but these objects have not been directly observed, so it is impossible to relate their masses to other physical properties. To date, with the exception of HD 209458, no substellar object—whether brown dwarf or planet—whose intrinsic spectrum has been observed has also been proven to be substellar by a direct, dynamical measurement of its mass. Conversely, no object outside the solar system with a dynamical substellar mass has actually been directly detected (again with the sole exception of HD 209458). Currently, the substellarity of all directly observed bodies is certified either through the lithium test or by the fact that their effective temperatures are below the minimum main-sequence temperature (Basri 2000). However, both tests can only indicate an upper limit to the mass, and not its precise value. Moreover, they are not useful at very early ages, when lithium is undepleted even in low-mass stars and substellar objects have not yet cooled sufficiently.

For these reasons, precise mass estimates for all directly observed substellar bodies have so far been obtained solely through comparison with theoretical evolutionary tracks. However, the evolutionary models remain largely untested in an absolute sense, and different groups have generated somewhat different tracks (e.g., Baraffe et al. 1998; Burrows et al. 1997; D’Antona & Mazzitelli 1994). Evolutionary modeling uncertainties arise from a variety of sources, such as the treatment of convection, choice of initial conditions and the modifying effects of any initial accretion phase. In addition, these uncertainties are exacerbated at the earliest ages and for very low masses (Baraffe et al. 2002). It is precisely for these ages and masses, however, that the evolutionary models are currently most widely used: to distinguish between stellar and substellar objects in young clusters (since the lithium and temperature tests are not robust at these ages), as well as to infer the actual substellar masses. For example, the planemo status of newly identified isolated bodies in young star-forming regions, mentioned earlier, depends entirely on the accuracy of the theoretical tracks. Therefore, given the burgeoning uncertainty in the tracks with decreasing mass and age, it would be extremely useful to have an independent method for determining mass, in order to check the theoretical predictions.

We present such a method here, which relies on an accurate measurement of surface gravity from high-resolution spectra. In a nutshell, we first derive surface gravities and effective temperatures ($T_{\text{eff}}$), by comparing our high-resolution optical spectra to the latest synthetic spectra. We then calculate radii and masses by combining our inferred gravity and $T_{\text{eff}}$ with photometry and distance measurements. In this paper, we present the gravity and temperature spectral analysis. The radius and mass calculations are presented in a companion paper (Mohanty et al. 2004, hereafter Paper II).

For cool, very low mass objects, the derivation of surface gravities from observed spectra is not trivial. A vast multitude of molecular and atomic spectral lines arise in their low-temperature photospheres; an adequate modeling of these is a prerequisite for inferring gravity (and $T_{\text{eff}}$). This has only become possible in the last several years, because of large advances in computing power and the compilation of increasingly comprehensive line lists. The resulting synthetic spectra are now routinely used to infer the $T_{\text{eff}}$ and model the colors of low-mass stellar and substellar objects (e.g., Allard et al. 2001; Schweitzer et al. 2001; Leggett et al. 2000, 2001; Burrows et al. 2000; Basri et al. 2000; Kirkpatrick et al. 1999). Here we take the next logical step, of using the synthetic spectra to derive surface gravities as well. $T_{\text{eff}}$ and gravity, together with empirical distance and photometry information, then allow us to calculate masses and radii without resorting to evolutionary model predictions.

Clearly, the validity of our analysis depends on that of the synthetic spectra; we will assess the veracity of these spectra at appropriate junctures. It must be pointed out, however, that synthetic spectra are essential even when masses are derived through comparisons with theoretical evolutionary models—either for translating observed spectral types to temperatures (when comparing the data to theoretical HR diagrams), or for converting theoretical temperatures and luminosities to expected photometry (when comparing the data to theoretical color-magnitude diagrams). In other words, both our technique, as well as analyses using evolutionary models, are limited by any shortcomings in the synthetic spectra.

In this paper we will derive, through spectral analysis, $T_{\text{eff}}$ and gravities for a sample of young, late-type (i.e., low-mass) pre–main-sequence objects belonging to the Upper Scorpius and Taurus regions. Since we observe them prior to their main contraction phase, we expect their surface gravities to be lower than in field objects of similar mass. By comparing our results to the predictions of evolutionary models, we will also test these models in the low-mass, young-age regime where they are most uncertain.

2. OBSERVATIONAL SAMPLE AND PROPERTIES

Our sample consists of 11 mid- to late-M objects in Upper Scorpius and two in Taurus. Our initial Upper Sco sample was culled from a study of this cluster by Ardila et al. 2000, hereafter AMB00). They chose objects that lie above the Leggett (1992) main sequence in both $I$ versus $R-I$ and $I$ versus $I-Z$ color-magnitude diagrams. Their saturation limits also excluded all objects with $I \leq 13.5$. This procedure selects for pre–main-sequence (PMS) objects roughly $\sim$M2 and later, but it is also subject to contamination by foreground low-mass stars, background giants, and reddened background stars (AMB00). Background galaxies are not expected to occur in the selected regions of the color-magnitude diagram (see AMB00 and references therein). AMB00 then obtained low-resolution optical spectra for a subset of their sample. In 20 of these, they detected H$\alpha$ in emission. The strength of the emission was used as further (although not ironclad) evidence of cluster membership.

Here we explore the very low-mass regime in Upper Scorpius. We originally included the 16 AMB00 objects with detected H$\alpha$ emission and spectral type M5 and later: these are the best candidates for lowest mass cluster members. Of these, we were able to observe 13 on HIRES at Keck I. We also observed an M7 Upper Scorpius candidate (USco 130) for which AMB00 had not obtained a low-resolution spectrum, bringing our total sample size to 14. The high-resolution
Barycentric and stellar radial velocity corrections were derived for each observed spectrum. We thank G. Marcy for the IDL routine to calculate barycentric corrections. Radial velocities ($v_{\text{rad}}$) were derived by measuring the peak position for cross-correlation functions between each star and a $v_{\text{rad}}$ standard. We chose Gl 406 (M6), with a known $v_{\text{rad}} = 19 \pm 1 \text{ km s}^{-1}$ (Martin et al. 1997), as our standard. As a check on the accuracy of our measurements, we have calibrated our Gl 406 spectrum on an absolute wavelength scale. We find its $v_{\text{rad}}$ is indeed $19 \pm 1 \text{ km s}^{-1}$, in complete agreement with Martin et al. (1997).

Our sample also includes GG Tau Ba and Bb, the two M-type components ($\sim$M6 and $\sim$M7.5, respectively) of the quadruple GG Tau system, located in the Taurus star-forming region. Parameters for Ba and Bb have previously been derived through comparison with theoretical evolutionary tracks (White et al. 1999; hereafter WGRS99); it is thus instructive to reanalyze them using our technique, and compare our results to the previous ones. High-resolution optical spectra of both objects were kindly supplied to us by R. White. Like the Upper Sco spectra, these too were obtained with Keck HIRES, and reduced in a similar fashion by R. White.

### 2.1. PMS Status and Cluster Membership

GG Tau Ba and Bb are already known to be bona fide PMS members of the Taurus complex (see WGRS99 and references therein). Consequently, we focus here on the Upper Sco targets. Optical high-resolution spectra yield four independent measures of PMS status and cluster membership: lithium (Li $i$) detection, H$_{\alpha}$ emission (already observed by AMB00 in our sample, but possibly overestimated because of blending effects at low resolution), the width of gravity-sensitive lines (e.g., Na $i$), and radial velocity measurements. In this paper, we discuss only those objects that are PMS members of Upper Scorpius by all four criteria, i.e., those with detected Li $i$, clear H$_{\alpha}$ emission at high-resolution, line widths intermediate between that of giants and field dwarfs, and $v_{\text{rad}}$ consistent with cluster membership. Below, we first discuss our observations of these four criteria, and then the reasons they robustly exclude all but PMS objects.

In 11 of our 14 objects, we detected Li $i$ at 6708 Å. No Li $i$ was seen in UscO 85, 99 and 121; as a result, these are not likely to be PMS members of Upper Scorpius, and we do not discuss them further. The Li $i$ profiles are plotted in Figure 1. The corresponding equivalent widths have been quoted in Jayawardhana et al. 2002, hereafter JMB02; they are mostly in the range $\sim 0.6$–$0.7$ Å. In UscO 128, we have a somewhat noisy Li $i$ detection. However, recent high-resolution spectra we obtained for this object, using the echelle spectrograph MIKE on the Magellan Baade Telescope, clearly show Li $i$ absorption. The Magellan detection is plotted in Figure 1; the corresponding equivalent width is 0.53 Å.

Our H$_{\alpha}$ detections have been discussed, the observed equivalent widths quoted, and the H$_{\alpha}$ line profiles shown in JMB02. We only note here that, in the 11 objects with detected Li $i$, H$_{\alpha}$ is strongly in emission, with equivalent widths ranging from $\sim 6$–$25$ Å. The H$_{\alpha}$ profiles and strengths are similar to those in dMe stars (see JMB02).

The purpose of this paper is to derive stellar parameters such as gravity from an analysis of various atomic and molecular lines. However, even a cursory examination can reveal whether the observed spectra are commensurate with expectations for a low-mass, few megayear old PMS sample. For such objects, theory predicts log $g \sim 3.0$–4.0 (Chabrier & Baraffe 2000). M giants have much lower gravities (log $g \sim 0$–2), while field
M and L dwarfs exhibit substantially higher ones ($\log g/C_2 \approx 5$). In all our objects, the gravity sensitive $Na_i$ doublet ($\lambda 8194$) is narrower than in field M dwarfs and much broader than in M giants of similar spectral type, as indeed expected at an intermediate gravity.

Finally, while we do not have proper motions for our sample, we do have radial velocities. The median $v_{rad}$ for Upper Scorpius is $-4.6 \pm 1$ km s$^{-1}$ (de Zeeuw et al. 1999, hereafter ZHB99; the velocity dispersion is not cited). We find $-4.5 \pm 1$ km s$^{-1}$ for our sample, which is completely consistent with the ZHB99 value. The Upper Scorpius OB association is a comoving group, so its members should have comparable velocities along all three spatial directions. The excellent $v_{rad}$ agreement thus makes it very likely that our objects are true members of this OB association. We also point out that our $v_{rad}$ rules out the possibility of interlopers from Upper Centaurus Lupus (UCL), another subgroup in Sco OB2 that somewhat overlaps the western edge of Upper Scorpius; the median $v_{rad}$ in UCL is $+4.9$ km s$^{-1}$ (ZHB99), well beyond our $v_{rad}$ error bars. We also note that USco 85, 99, and 121, which we do not consider to be Upper Scorpius members owing to non-detection, also differ in $v_{rad}$ by $\pm 15$ km s$^{-1}$ from our sample. This further establishes them as nonmembers.

M dwarfs in the field do not exhibit Lithium in their spectra, having depleted it fairly early in their descent to the main sequence. The detection of $Li_i$ in our objects thus precludes their being field M dwarfs. Field brown dwarfs (BDs) with mass $\gtrsim 0.06 M_\odot$ do show lithium, never having achieved core temperatures high enough to burn it. However, such BDs have spectral types $\sim L2$ and later, and $\log g \approx 5.5$ ($\gtrsim$gravity in field M dwarfs), by young-disk ages ($\sim 1$ Gyr). Both the M-type classification of our objects and their low gravity (as evidenced by their narrow $Na_i$ profiles) argue against their being field brown dwarfs.

Lithium detection alone does not necessarily exclude Li-rich giants (although these are comparatively rare). However, our $Na_i$ line profiles clearly imply gravities higher than in giants. Moreover, our detection of strong emission $H\alpha$ makes it very unlikely that our objects are isolated giants; $H\alpha$ in the latter is seen in absorption (at most, the line core is somewhat filled-in by chromospheric emission, but the line as a whole is still in absorption). Finally, while $H\alpha$ activity in giants can be somewhat enhanced when they are a part of Algol-type or RS CVn binaries (Richards & Albright 1999; Fox et al. 1994), the giants in these cases are always in the F–K spectral type range; our objects are mid- to late M. Reddening cannot lead us to infer spuriously late spectral types either: spectral types for our objects have been determined by AMB00 from low-resolution spectra, not colors, and our high-resolution observations imply M types as well (e.g., through the presence of strong TiO bands). In summary, the spectral type, $Li_i$ detection, $H\alpha$ activity, and high gravity imply that our objects are member stars of the Upper Scorpius OB association.

10. Usco 130 is the only exception, in that AMB00 do not have a spectrum for it, and derive a spectral type from colors alone. However, our high-resolution spectrum confirms AMB00's late-M classification of this object and precludes any misidentification due to reddening effects.
detection, dMe-like Hα emission and (relatively) higher gravity of our objects all argue strongly against any of them being giants.

Finally, our Na i profiles are commensurate with subgiant gravities, as indeed expected for PMS objects. However, it is extremely unlikely that any of our objects are subgiant interlopers. The most convincing argument for this is simply that M-type subgiants are not expected to exist; the MS lifetime of M dwarfs is too long for any to have reached the subgiant stage yet. Additionally, the arguments made above, concerning the unlikelihood of Li i absorption and dMe-like Hα emission in giants, hold for subgiants as well. The PMS status of our final Upper Sco targets is thus very secure; moreover, their radial velocities suggest that they are very likely to be bona fide members of the Upper Scorpius association.

2.2. Rotation Velocity

Our method for deriving projected rotation velocities ($v \sin i$) is discussed in detail in Mohanty & Basri (2003). Briefly, we find $v \sin i$ through cross-correlating our target spectra with a template spectrum. We use only those echelle orders without emission features, broad stellar absorption lines, and telluric features. Cross-correlation functions are found in multiple orders ($\sim$6), and the average is used to determine $v \sin i$. White & Basri (2003) find that for very young objects, a template constructed by averaging a dwarf and giant spectrum is appropriate for spectral type $\sim$M6 and later, while a dwarf spectrum alone is more suitable for earlier types. Moreover, they find that for their sample of M-type Taurus objects, cross-correlating with an M giant spectrum yields $v \sin i$ lower by $\sim$8–9 km s$^{-1}$ than cross-correlating with an M dwarf spectrum. This is because the molecular lines in the giant have somewhat broader than in the dwarf, even though the giant is at lower gravity, presumably because of turbulence and/or non-LTE effects.11 Consequently, cross-correlating with a giant-dwarf averaged template yields intermediate $v \sin i$ values: $\sim$4–5 km s$^{-1}$ higher than with a giant alone, and $\sim$3 km s$^{-1}$ lower than with a dwarf (White & Basri 2003).

Our sample consists of M5–M8 objects, with four in the M5–M5.5 range. Gl 406 (M6, $v \sin i < 3$ km s$^{-1}$; Mohanty & Basri 2003) has been used as our dwarf template, and HD 78712 (M6IIIe; presumed nonrotating; White & Basri 2003) as our giant template. For our sample, our analysis agrees with that of White & Basri (2003), with one additional result. For objects with $v \sin i > 10$ km s$^{-1}$, the $v \sin i$ obtained through cross-correlation with the giant-dwarf averaged template differs by $\pm$2 km s$^{-1}$ from the $v \sin i$ obtained using either the dwarf or giant template alone. That is, at moderate to high rotation rates, the difference in $v \sin i$ implied by the three templates is small; this is to be expected, as rotational broadening overpowers other broadening mechanisms with increasing $v \sin i$ (this result is moot to the White & Basri [2003] work, since all but two of their Taurus objects have $v \sin i \leq 10$ km s$^{-1}$). At the same time, our precision in determining $v \sin i$, for any given template, is of order $\pm$2 km s$^{-1}$ (see Mohanty & Basri [2003] for detailed discussion). Now, we find $v \sin i > 10$ km s$^{-1}$ in all but five of our objects (regardless of whether the giant, dwarf, or averaged template is used), and greater than 15 km s$^{-1}$ in most. Therefore systematic errors in our $v \sin i$ due to any template mismatch are small, and in most cases less than our random errors. Our final $v \sin i$ values are given in Table 1; the Upper Sco ones have also been quoted earlier in JMB02. We note that the latter paper gives 5.5 ± 2 km s$^{-1}$ for USco 112, while here we find 8 ± 2 km s$^{-1}$. This is because all values in the former paper were derived using only giant-dwarf averaged templates, including in the M5–M5.5 objects. Here we use dwarf templates for these spectral types; since $v \sin i$ for this object is less than 10 km s$^{-1}$, the template change makes a (small) difference. All our other Upper Sco targets remain unaffected, for the reasons cited above. We also note that, because of instrumental broadening effects (see Mohanty & Basri [2003] for details), our lower limit for $v \sin i$ detection is $\sim$5 km s$^{-1}$.

3. SURFACE GRAVITY AND EFFECTIVE TEMPERATURE ANALYSIS

Having established the PMS nature of our sample and derived the projected rotational velocities, we are now ready to determine $T_{\text{eff}}$ and gravity. The synthetic spectra to which our data are compared are described in § 3.1, followed by a discussion of the modifications made to the models and data and of our fitting procedure, in § 3.2. Our method of analysis is detailed in § 3.3. We present the results in § 4, and the attendant implications in § 5.

3.1. Model Spectra

We use the latest version of synthetic spectra generated with the PHOENIX code (Allard et al. 2001; F. Allard et al. 2004, in preparation). Specifically, we use the models designated AMES-Cond-2002-version2.4. These incorporate the most recent AMES line lists for both TiO (Langhoff 1997; Schwenke 1998) and H2O (Partridge & Schwenke 1997). A good treatment of H2O is important for analyzing optical spectra, even though H2O opacity dominates only in the infrared (TiO opacity is more important in the optical). This is because the overall H2O opacity is larger, and its lines occur closer to the peak of the SED than those of TiO, at the low $T_{\text{eff}}$ in M types. Consequently, changes in the H2O opacity have a substantial effect on the atmospheric temperature structure and thus on the emergent spectrum even in the optical. A total of about 500 million molecular lines are currently included in the models; of these, ~307 million are lines of H2O, and ~172 million are of TiO (Allard et al. 2000, 2001). In this paper we use only solar-metallicity models ([M/H] = 0.0). While metallicity in the Upper Sco cluster has not yet been rigorously investigated, large deviations from solar are unlikely for nearby, young PMS objects (see also § 4.3.3).

Dust formation is another potentially important effect in the low-temperature atmospheres of M-type objects; grains affect both the atmospheric structure and the emergent flux. Current models include these effects. The “Dusty” models treat the case where grains form and remain suspended in the photosphere, while the “Cond” models are applicable when dust has settled (or “condensed”) out of the atmosphere. Both sets of models treat grain formation self-consistently, through chemical equilibrium calculations (see Allard et al. 2001). It is important to note, however, that under physical conditions where the chemical equations imply no grain formation, the Cond and Dusty models produce identical spectra: when no grains form, the treatment of grain settling or suspension is immaterial.
In field dwarfs, spectral analyses indicate that dust formation becomes important around M7 (Jones & Tsuji 1997), and dust settling at still later spectral types, ~L2 (e.g., Schweitzer et al. 2001). In lower gravity PMS objects like ours, no detailed empirical spectral analysis of photospheric dust has yet been carried out. Nevertheless, since the latest spectral types in our sample are ~M7−M7.5, it is possible, by analogy with field dwarfs, that dust begins to appear in their photospheres. To ascertain whether significant grain formation occurs in our objects, we have performed two tests: the first checks whether the synthetic spectra imply any photospheric dust in our sample, and the second examines whether our observed spectra show any empirical signatures of dust (independent of the synthetic spectra).

In the first test, we compare the spectra of our latest type objects to both the Dusty and Cond models. We find that the two yield identical $T_{\text{eff}}$ and gravities; i.e., for the best-fit $T_{\text{eff}}$ and log g, the models indicate no grain formation. In the spectral regions used in our $T_{\text{eff}}$ and gravity analysis (see § 3.3), grain effects first appear weakly in the models at ~2500 K, and strengthen with decreasing $T_{\text{eff}}$. The lowest $T_{\text{eff}}$ we derive, on the other hand, with either Cond or Dusty, are ~100 K higher. We have also examined whether the combined effects of $T_{\text{eff}}$ and dust can create misleading degeneracies; i.e., whether higher $T_{\text{eff}}$ models without grain formation can mimic lower $T_{\text{eff}}$ models with grains, yielding erroneous temperatures (and gravities). No degeneracies pertinent to our analysis are found. In the second test, we compare our observed PMS spectra to those of field M dwarfs of similar spectral type. This allows us to empirically gauge whether spectral signatures of photospheric grains, which are evident in the field dwarfs, arise in our sample as well. The detailed analysis is presented in Appendix A and summarized in § 4.3.1; here we simply state our conclusion that grain formation is negligible in our PMS sample.

In summary, our tests show that neither the synthetic spectra nor the observations imply any significant grain effects in our targets. Under the circumstances, we will show only Cond models in this paper; this is simply because, at the time of writing, these models were available to us over a larger range of $T_{\text{eff}}$ than the dusty ones.12 Once again, we emphasize that the “cond” appellation does not imply any grain formation or settling in our objects: fits to either Cond or Dusty models yield the same $T_{\text{eff}}$ and gravities.

The treatment of convection is also important for our sample. Currently available synthetic spectra and evolutionary models use a mixing length formulation, which seems to reasonably approximate the true convective transport mechanism (see Chabrier & Baraffe [2000] for a full discussion). In certain regimes, the actual value of the mixing length parameter ($\alpha$) that one adopts turns out to be unimportant, for the spectral and evolutionary modeling. For instance, for more evolved (i.e., higher gravity) low-mass (≤0.6 $M_{\odot}$) objects, varying $\alpha$ from 1 to 2 hardly affects the models. However, as Baraffe et al. (2002) point out, this is not true for the same low-mass objects during their PMS phase. At the low gravities associated with the initial contraction phase, changing $\alpha$ can affect the dissociation of H$_2$ in the deeper atmospheric layers, and hence the H$_2$ opacity, atmospheric structure, and emergent spectrum. Earlier generations of synthetic spectra, as well as some of the most widely used current evolutionary models, use $\alpha = 1$ in the PMS, low-mass stellar and substellar regime. However, full three-dimensional hydrodynamical simulations carried out very recently indicate that $\alpha \approx 2$ is a better approximation for mid-M types, both in the field as well as in the PMS phase (Ludwig 2003). Such simulations offer the best insight so far into the actual convection process (see Chabrier & Baraffe 2000); consequently, the latest synthetic spectra we use here incorporate $\alpha = 2$. We will address the mixing length issue further, when we contrast our results with the evolutionary track predictions.

Finally, the treatment of collisional pressure broadening of the alkali lines is important for our analysis, since we shall use these line profiles to derive gravities. A full exposition of the line-broadening treatment in the synthetic spectra is given by Schweitzer (1995); a summary can be found in Schweitzer et al. (1996). We briefly discuss broadening in § 4.3.4.

3.2. Modifications to Models and Data, and Fitting Procedure

In order to compare the synthetic spectra to the data, some modifications are necessary to both. The observed spectra are rotationally broadened; to simulate this, the models have been convolved with the appropriate velocity profiles (depending on the $r \sin i$ we derive independently of the models; see § 2.2). Moreover, the data have a finite instrumental resolution. The models have therefore been further broadened, by convolution with a Gaussian profile, to match our HIRES resolution of 31,000.

Our high-resolution data are not flux-calibrated. Comparison to the models thus requires some form of normalization. As described in the next section, we will analyze various spectral intervals, containing TiO band heads and alkali doublets. We have normalized the data in each of these intervals by a constant factor. The latter is the mean of the continuum over a small range of wavelengths; the range chosen depends on the echelle order. Note that in these cool objects, there is no “true” continuum, only a pseudocontinuum made up of millions of overlapping molecular lines; however, for brevity, we drop the “pseudo” appellation from here on. The models are normalized by the model-continuum mean over the same wavelength ranges, after correcting for radial velocity shifts relative to the data. Telluric lines, strong stellar lines that appear or disappear with changing $T_{\text{eff}}$ or gravity, or strong stellar lines that are not well-reproduced in the synthetic spectra, can all potentially skew the mean. The normalization wavelength ranges have been chosen, through intercomparison of all our data and models at different $T_{\text{eff}}$ and gravities, to specifically exclude such features. The spectra are checked during fitting to ensure that the normalizations are indeed correct, and not thrown off by, say, the appearance of random noise spikes in the data within the normalization wavelength range.

Recall that the data have also been flat-fielded, which removes the blaze function and reveals the intrinsic shape and slope of the continuum. Our normalization method then ensures that this innate stellar continuum, shaped by various opacity effects, remains undisturbed. That is, we have not attempted to normalize out the intrinsic appearance of the stellar continuum, in either the data or the models, through any further division by an overall fit to the continuum. In any given spectral region of interest, the data and models are “anchored”...
only over a small wavelength region—i.e., are scaled to ensure only that their continua overlap over this section—and are otherwise unconstrained. This allows us to compare the observed and predicted continuum behavior, and provides an additional check on the veracity of the synthetic spectra, as described shortly (§3.3).

Finally, the models were initially constructed in steps of 100 K in $T_{\text{eff}}$, and 0.5 dex in gravity. We will demonstrate in §4.1 that the TiO band heads and alkali doublets used in our analysis actually appear sensitive to even smaller changes in temperature and gravity. We have thus averaged models separated by 100 K to construct a model grid with 50 K resolution in $T_{\text{eff}}$; analogous averaging of models separated by 0.5 dex yields a grid with 0.25 dex resolution in $\log g$ (all averaging is done after normalizing the models in the manner described above). Such a procedure is justified: a perusal of the normalized synthetic spectra reveals that our spectral diagnostics—TiO band head strengths, alkali doublet line profiles, and shape and slope of the continua—all vary fairly linearly over $\sim$200 K changes in $T_{\text{eff}}$ and $\sim$1 dex changes in gravity, over the entire $T_{\text{eff}}$ and gravity range we will consider ($T_{\text{eff}} = 2500$–3000 K, $\log g = 3.0$–4.5).

Best fits to the synthetic spectra were initially found through visual inspection. In §4.1 we show that $T_{\text{eff}}$ and $\log g$ mismatches of 50 K and 0.25 dex respectively, between the models and data, are distinguishable by eye; mismatches at the 100 K and 0.50 dex level are obvious. We conservatively estimate errors of $\pm$50 K and $\pm$0.25 dex (see §§3.3 and 4.1). To check our results, we have also derived $\chi^2$ differences between the models and data (after excluding regions with telluric contamination), over a $\pm$100 K (in steps of 50 K) and $\pm$0.50 dex (in steps of 0.25 dex) range centered on the best-fit $T_{\text{eff}}$ and $\log g$ values derived by eye. In all cases our initial results, and our estimated errors, are validated: the $\chi^2$ values are always minimum for the visually identified best-fit model, models within 50 K and 0.25 dex of the best-fit one yield somewhat higher values of $\chi^2$, while models differing by 100 K or 0.50 dex from the best-fit one produce much larger $\chi^2$ values.

3.3. Method of Analysis

In order to determine $T_{\text{eff}}$ and gravity, we compare the observed high-resolution line profiles of various temperature- and gravity-sensitive species to synthetic spectra. Specifically, we examine the following:

1. The highly temperature-sensitive triple-headed band of titanium oxide (TiO) at 8432, 8442, 8452 Å.
2. The gravity- and temperature-sensitive doublet of the neutral atomic alkalis sodium (Na i; subordinate doublet at 8183, 8195 Å) and potassium (K i; resonance doublet at 7665, 7699 Å);
3. The overall shape and slope of the continuum over the entire HIRES orders in which the Na i and K i doublets are located; each order spans $\sim$100 Å.

In M types, TiO is the main source of optical continuum opacity. The strengths of many of the band heads of this molecule are very dependent on temperature (see Solf [1978] for detailed discussion). We make use of the triple-headed band at $\lambda\lambda$8432, 8442, 8452, identified as the electronic $E^\prime\Pi - N^\prime\Delta$ system (Solf 1978). Its response to changes in $T_{\text{eff}}$ and gravity is depicted in Figure 2, using the synthetic spectra.

It is clear that this TiO system is highly sensitive to $T_{\text{eff}}$ (increasing in strength with decreasing $T_{\text{eff}}$) and rather insensitive to variations in gravity. At a given $T_{\text{eff}}$, the band strengths change only slightly even for a large, 1 dex change in gravity (in the $\log g \sim 3.0$–4.0 range expected for low-mass PMS objects). At a given gravity, however, they vary significantly over only 100 K changes in $T_{\text{eff}}$ (specifically, the band heads at 8442 and 8452 Å; larger changes in $T_{\text{eff}}$ similarly affect the band head at 8432 Å as well). Indeed, as we will show later in comparisons to actual data, these bands enable us to distinguish $T_{\text{eff}}$ variations down to $\pm$50 K. This TiO system is thus an excellent temperature indicator.

However, since our goal is to fix gravity as accurately as possible, we cannot altogether ignore the small gravity dependence of these TiO bands. Figure 2 shows $^{14}$ that at such temperatures, increasing gravity (at a fixed $T_{\text{eff}}$) makes the 8442 and 8452 Å band heads slightly weaker, while decreasing gravity makes them a little stronger. $^{15}$ As a result a (large) change in gravity can compensate for a (small) change in $T_{\text{eff}}$, and neither quantity can be accurately fixed. Of course, a believable range in gravities and $T_{\text{eff}}$ can still be assigned by appealing to spectral type and/or theoretical evolutionary track considerations. However, given our stated purpose of testing the latter, this is unsatisfactory. What is needed is an additional spectral constraint on the TiO results.

This is provided by the Na i and K i alkali doublets, whose profiles also depend on both $T_{\text{eff}}$ and gravity. Let us consider Na i first. It’s variation with $T_{\text{eff}}$ and gravity is depicted in Figure 2. We see that the doublet strength increases with both decreasing $T_{\text{eff}}$ and increasing gravity. For example, either a 200 K decrease in $T_{\text{eff}}$ or a 0.5 dex increase in $\log g$ changes the line-profile similarly, making the line core slightly deeper and the line wings substantially broader (Fig. 2). $^{16}$ Indeed, the shape of the Na i doublet changes appreciably even for a 0.25 dex change in gravity (or equivalently, a 100 K change in $T_{\text{eff}}$). Like for TiO, this degeneracy between $T_{\text{eff}}$ and gravity precludes our using the Na i doublet, in isolation, to uniquely determine either quantity.

When considered together, however, TiO and Na i can fix both $T_{\text{eff}}$ and gravity very precisely. To see this, notice that the $T_{\text{eff}}$-gravity degeneracies act in opposite senses in TiO and Na i. That is, while decreasing $T_{\text{eff}}$ compensates for increasing gravity in the TiO bands considered here, an increase in $T_{\text{eff}}$ offsets a gravity increase in Na i. This behavior allows us to quickly converge on the correct $T_{\text{eff}}$ and gravity, if we demand that TiO and Na i fits be obtained at the same temperature and gravity. Deviations from the true gravity (or $T_{\text{eff}}$) leads to large discrepancies in the $T_{\text{eff}}$ (or gravity) implied by TiO and Na i.

$^{14}$ In this and following figures, the cited spectral differences may not always be completely obvious, given the reduced plot-scale we have had to adopt in the interests of space. However, plots in the electronic copy of the journal can be enlarged; the interested reader is requested to consult these.

$^{15}$ The 8432 Å band strength is clearly even less affected by gravity variations; we will ignore its gravity dependence henceforth, since the dependence is much too small to affect, or be useful for, our analysis.

$^{16}$ We note that at the $T_{\text{eff}}$ and gravities under consideration - 3000–2500 K and 3.0–4.0 dex—the Na i and K i doublets are unsaturated. In Fig. 2, this is evidenced for Na i by the slightly unequal core depths in the two components of the doublet.
Fig. 2.—Dependence of TiO and Na i on $T_{\text{eff}}$ and gravity, in the model spectra. In all panels of both left and right columns, the black spectrum is the synthetic spectrum at $T_{\text{eff}} = 2800$ K, log $g = 3.5$. We use this as a comparison template, to illustrate changes in TiO and Na i with varying $T_{\text{eff}}$ and gravity. In this and in the following plots all spectra are normalized by a multiplicative factor; multiple spectra in a plot are offset by additive constants for clarity.

**Top left:** The strong dependence of the TiO band heads (especially at 8442 and 8452 Å) on $T_{\text{eff}}$; decreasing $T_{\text{eff}}$ makes the bands deeper.

**Center left:** The weak dependence of TiO on gravity; at a given $T_{\text{eff}}$, the TiO band-strengths remain almost constant over a 1 dex range in log $g$.

**Bottom left:** TiO comparisons for the same gravities and temperatures shown for Na i in the large bottom right panel. While fits can be obtained to Na i with various $T_{\text{eff}}$/gravity combinations, the same combinations do not give simultaneous good fits to TiO; demanding simultaneous fits to TiO and Na i thus allows us to quickly converge on the correct $T_{\text{eff}}$ and gravity (see text).

**Top right:** The strong dependence of the Na i doublet on $T_{\text{eff}}$; decreasing $T_{\text{eff}}$ makes the doublet broader.

**Center right:** The strong dependence of the Na i doublet on gravity; at a constant $T_{\text{eff}}$, increasing gravity makes the doublet broader.

**Bottom right, large panel:** Degeneracy between $T_{\text{eff}}$ and gravity effects on the Na i doublet; a $T_{\text{eff}}$ increase (decrease) of 200 K almost exactly compensates for a gravity increase (decrease) of 0.5 dex, enabling a given Na i profile to be fitted by various $T_{\text{eff}}$/gravity combinations.

**Bottom right, small panel:** The $T_{\text{eff}}$ dependence of the continuum around the Na i doublet; while the doublet itself shows a $T_{\text{eff}}$-gravity degeneracy, the continuum is much more sensitive to $T_{\text{eff}}$ alone. Varying $T_{\text{eff}}$ produces continuum mismatches. Thus, while the 3000 K, log $g = 4.0$ and 2800 K, log $g = 3.5$ spectra are very similar in the profile of the Na i doublet (bottom right, large panel), the two spectra are clearly different in the surrounding continuum (bottom right, small panel). Demanding a simultaneous good fit to the Na i doublet and to the surrounding continuum provides an additional constraint on $T_{\text{eff}}$ and gravity.
An example of this fitting procedure is illustrated in Figure 2. Suppose an object has $T_{\text{eff}} = 2800$ K and $\log g = 3.5$ (represented in Fig. 2 by a synthetic spectrum with these parameters). Then we see that, assuming $\log g = 3.0$, a good fit is obtained to TiO at 2900 K but to Na i at 2550 K. On the other hand, assuming that $\log g = 4.0$ produces a good fit to TiO at 2750 K but to Na i at 3000 K. In the first case, Na i implies a much lower temperature than TiO; in the second case, it implies a much higher one. This is a direct consequence of the two facts discussed above: $T_{\text{eff}}$/gravity degeneracies act in opposite directions in TiO and Na i, and Na i is much more sensitive to gravity than TiO. This allows rapid convergence onto the actual gravity. In the example at hand, the disagreement between $T_{\text{eff}}$ (TiO) and $T_{\text{eff}}$ (Na i) at both $\log g = 3.0$ and 4.0, combined with the change in sign in $[T_{\text{eff}}$ (TiO)$-T_{\text{eff}}$ (Na i)] in going from 3.0 to 4.0, would immediately lead us to try an intermediate gravity, $\log g = 3.5$. At this gravity, we would infer 2800 K from both the TiO and Na i fits; $\log g = 3.5$, $T_{\text{eff}} = 2800$ K would thus be the finally adopted, and correct, parameters.

If our data were perfect, the complementary behavior of TiO and Na i discussed above would let us fix $T_{\text{eff}}$ and surface gravity to any desired precision. However, real data do not allow this. In particular, when comparing synthetic spectra to observations with finite resolution and nonzero noise, there is some intrinsic uncertainty in selecting the best-fit model. We will illustrate these uncertainties in more detail later in this paper; for now, we simply state their magnitude. At any given gravity, we cannot certify $T_{\text{eff}}$ to better than $\pm 50$ K from the TiO fits (e.g., in the example above, we would actually choose $2900 \pm 50$ K at $\log g = 3.0$, $2800 \pm 50$ K at 3.5, and $2750 \pm 50$ K at 4.0, from the TiO fits). Similarly, at a given $T_{\text{eff}}$, we are insensitive to gravity variations smaller than $\pm 0.25$ dex in the Na i fits. It is these uncertainties that finally set the precision of our derived parameters. Note that these errors refer to the precision of our measurements, as distinct from the absolute accuracy, i.e. veracity, of the derived parameters; the latter is of course dependent on the validity of the synthetic spectra, which will be discussed in later sections.

So far we have discussed Na i; the situation is analogous for the K i doublet (not shown). In the latter case, a $\sim 100–150$ K decrease in $T_{\text{eff}}$ mimics a 0.5 dex increase in $\log g$. Ideally, K i should be used, in conjunction with TiO, to provide an independent estimate of gravity which is as stringent as that from Na i. However, the K i doublet lies significantly blueward of Na i and thus has a poorer signal-to-noise ratio (S/N) in some of our faintest and reddest objects. In such cases, K i is less effective than Na i in constraining the gravity. However, we emphasize that even in these cases, the gravity indicated by K i is a good independent check on the gravity from Na i; in all our targets, the two estimates are fully mutually consistent.

Finally, we also use the shape of the continuum surrounding the Na i and K i doublets to constrain $T_{\text{eff}}$ and gravity (this analysis is possible because our normalization procedure leaves the continuum shape intact). As mentioned earlier, the continuum in M types is predominantly controlled by TiO; consequently, its behavior is very sensitive to $T_{\text{eff}}$. In particular, there are a number of temperature-sensitive TiO-bands immediately redward of both the K i and Na i doublets (e.g., $\lambda \lambda 7705, 7743$ in the $6\nu = -1$ sequence just redward of the K i doublet; $\lambda \lambda 8206, 8251$ in the $6\nu = -2$ sequence just redward of the Na i doublet; see Solf 1978), which determine the continuum in these regions. Fitting the continuum over the entire order that contains the Na i or K i doublet, therefore, permits us to break the degeneracy between $T_{\text{eff}}$ and gravity that affects the alkali doublets alone.

This is illustrated in Figure 2 for the Na i order. We see that, while the Na i lines alone can be fitted by various combinations of $T_{\text{eff}}$ and gravity, the surrounding continuum restricts the allowed range of $T_{\text{eff}}$ (and thus gravity). In essence, by fitting an alkali doublet (line core and wings) together with a large swathe of surrounding continuum, we obtain a simultaneous fit to two different species—the alkali on one hand and TiO on the other—each with different temperature and gravity sensitivities (TiO being largely dependent on $T_{\text{eff}}$, and the alkali doublet depending on both $T_{\text{eff}}$ and gravity). This greatly narrows the range of permissible $T_{\text{eff}}$ and gravity implied by the alkali fit. In Figure 2 we show that the continuum redward of the Na i doublet allows us to restrict $T_{\text{eff}}$ to at least $\pm 200$ K, and thus $\log g$ to $\pm 0.5$ dex. Unfortunately, the observed continuum in the Na i and K i orders contains a large number of closely spaced telluric lines, which at times makes a determination of the stellar continuum harder. For those of our objects most affected by telluric contamination, we cannot restrict $T_{\text{eff}}$ by this method to better than $\pm 200$ K; for the others, $\pm 150$ K can be achieved. This is less accurate than the $T_{\text{eff}}$ constraints possible with the triple-headed TiO band. Consequently, this band remains the best diagnostic for fixing $T_{\text{eff}}$, and thus gravity, when used in conjunction with the alkali doublets. However, the continua around the alkali doublets at least provide a very useful consistency check of the derived $T_{\text{eff}}$ and $\log g$ obtained from the triple-headed TiO band and alkali doublets, by restricting the allowed $T_{\text{eff}}$ to at least within $\pm 200$ K, and thus $\log g$ (from the alkali doublets) to $\pm 0.5$ dex.

To summarize, we use the triple-headed TiO band and Na i to simultaneously fix both $T_{\text{eff}}$ and gravity. The K i doublet provides an independent check of the derived gravity. Fitting each alkali doublet together with the surrounding continuum additionally constrains the $T_{\text{eff}}$ and gravities and provides a further check on the parameters derived from the TiO band heads and alkali doublets. Finally, we point out that our analysis also supports the validity of the synthetic spectra we use. To derive $T_{\text{eff}}$ and surface gravity, we demand that the same model parameters fit all our spectral diagnostics. It is not a priori clear that a given set of model spectra can actually satisfy this requisite—errors in the synthetic opacities may very well lead to inconsistencies between the fits to various diagnostics. Thus, the fact that the model spectra used here yield consistent results—that is, for any given object, we are able to fit all our spectral diagnostics with the same $T_{\text{eff}}$ and gravity model (as we will show shortly)—suggests that our derived parameters are fairly accurate in an absolute sense.

It is also very important to note that our $T_{\text{eff}}$ and gravity derivations are independent of extinction estimates. Our high-resolution analysis involves comparisons between the observed and synthetic spectra over wavelength ranges of $\pm 100$ Å. Over any given spectral region this small, the wavelength-dependent variation in extinction is negligible for our purposes: the extinction over any such section can be assumed to be constant. Of course, extinction will change the observed flux in our different spectral regions (TiO, Na i, K i), which are separated by more than 100 Å from each other, by different (multiplicative) constants. However, our spectra are not flux-calibrated to begin with. As described earlier, we have normalized the observed and synthetic spectra, in each of the spectral regions used in our analysis, by dividing by a numerical constant. As a result, any extinction is effectively
divided out of our data, and does not affect the final results of our analysis. This is an important advantage of our method: when stellar parameters are derived by comparing the data to theoretical color-magnitude or H-R diagrams, on the other hand, estimating the extinction is necessary a priori, and constitutes a significant source of uncertainty.

4. RESULTS

Our main results are (1) the USco targets span a \( T_{\text{eff}} \) range of \( \sim 300 \) K (2900–2600 K); (2) the gravities for objects with \( T_{\text{eff}} \approx 2750 \) K are roughly similar, with \( \log g \approx 4–3.75 \) (commensurate with theoretical expectations for the age of USco; § 5.1); and (3) gravity declines sharply for cooler objects, with \( \log g \approx 3.5–3.25 \) (which is at odds with predictions for a coeval sample, § 5.1). We illustrate these results through a discussion of our model fits.

In the interests of space, we will show only the best fits to a representative selection of objects from our sample. However, to demonstrate our fitting procedure and its robustness, we begin with a detailed analysis of two examples: USco 55 and 104 (§ 4.1). In § 4.1.1 we elucidate how their \( T_{\text{eff}} \) and \( \log g \) are obtained from fits to synthetic spectra and discuss the precision of our measurements. We show that our fits indicate a significant difference in gravity between the two. To confirm the validity of this result in a model-independent fashion, we undertake direct comparisons between their observed spectra in § 4.2. In § 4.3 we summarize the results for all our Upper Sco objects and present more examples of gravity variations within our sample. Various physical processes that could potentially skew our results are investigated in § 4.3; we conclude that their effects on our analysis are unlikely to be significant. The implications of our findings are discussed in § 5; in particular, we examine the fits to GG Tau Ba and Bb in § 5.4, in order to evaluate some of our hypotheses.

4.1. Two Test Cases: USco 55 and 104

4.1.1. \( T_{\text{eff}} \) and Gravity from Synthetic Spectra

Consider first USco 55. In Figure 3 we show fits at \( \log g = 3.5 \) and 4.0 (4.5 is not shown, but it is discussed below). At each gravity, we show the best-fit model to each of our diagnostics. All models have been rotationally broadened by a 12 km s\(^{-1}\) velocity profile, to match the observed \( v \sin i \) of this object.
At log $g = 3.5$, the best fit to the Na i and K i doublets is at $T_{\text{eff}} = 2600$ K. However, this is clearly not a good fit to the TiO band heads or to the continuum in the Na i order. Compared with the data, the triple-headed TiO band is much too strong in the model, especially at 8442 and 8452 Å. The TiO bands in the Na i continuum are also too strong, depressing the model continuum relative to the data. Conversely, a good fit to the TiO band heads and Na i continuum is found at this gravity with a $T_{\text{eff}} = 2850$ K model. The Na i and K i doublets in this substantially hotter case, however, are much too weak and narrow to fit the observations. The discrepancy between the $T_{\text{eff}}$ implied by the TiO band heads and the alkali doublets is thus $\sim 250$ K, with TiO suggesting the hotter model.

A similar situation exists at log $g = 4.5$ (not shown). The TiO band heads and the Na i continuum are now fitted by a 2800 K model (note that this is very similar, but not identical, to the $T_{\text{eff}}$ required at log $g = 3.5$; this is due to the [very weak] $T_{\text{eff}}$/gravity degeneracy exhibited by TiO, and alluded to earlier). However, this model produces much stronger Na i and K i doublets than observed. Instead, the best fit to the both alkali doublets is now found at $\sim 3000$ K, which is a very poor fit to the TiO band heads. The mismatch between the $T_{\text{eff}}$ from the TiO and the alkali doublets at log $g = 4.5$ is thus $\sim 200$ K, about the same as at log $g = 3.5$. However, unlike at log $g = 3.5$, TiO now indicates the cooler model. This immediately suggests that the true value of gravity lies between 3.5 and 4.5. Moreover, the TiO fits at both gravities indicate that $T_{\text{eff}}$ is somewhere in the 2800 to 2850 K range.

As illustrated in Figure 3, these expectations are borne out using models with log $g = 4.0$. At this gravity, good fits are obtained to all our diagnostic spectral regions in USco 55: TiO band heads, Na i and K i doublets, and continua surrounding the doublets—at $T_{\text{eff}} = 2800$ K. We point out in passing the telluric lines slightly bluerward of the blue lobe of K i; there are also telluric lines blended into this lobe that make it appear very slightly broader than the model. These lines are stronger in our fainter targets, and in general preclude our using the blue K i lobe in the analysis in all but the highest S/N cases (such as USco 55). At any rate, an excellent fit is obtained to at least the red lobe, as well as to the TiO and Na i regions. Consequently, we adopt $T_{\text{eff}} = 2800$ K, log $g = 4.0$ for USco 55.

What are the errors in our derived parameters? We address this in Figure 4. At our preferred gravity, log $g = 4.0$, we compare the observed TiO band heads to a model at 2800 K (our best-fit $T_{\text{eff}}$), as well as to models offset from 2800 K by 50 and 100 K. We see that a $T_{\text{eff}}$ variation of $\pm 100$ K makes a substantial difference: the 2700 and 2900 K models are obviously bad fits to TiO. Even a variation of 50 K makes a (small) difference. At 2850 K, the model band heads (particularly at 8442 Å) are evidently stronger, and the continuum redward of 8452 Å clearly depressed, compared to the data. At 2750 K, on the other hand, the model continuum is a good match to the data in the TiO order, but the 8452 Å band head appears somewhat weaker than observed. We therefore conservatively adopt a $T_{\text{eff}}$ error of $\pm 50$ K, at log $g = 4.0$, and rule out with high confidence deviations of $\pm 100$ K at this gravity.

Similarly, at our best-fit $T_{\text{eff}}$ of 2800 K, we compare the Na i doublet to a model at log $g = 4.0$ (our best-fit gravity), as well as to models offset from 4.0 by 0.25 and 0.5 dex (Fig. 4). The models at log $g = 4.0 \pm 0.5$ dex are clearly poor fits to the doublet. Even a 0.25 dex change makes a small difference. The model doublet at log $g = 3.75$ is (slightly) narrower than the data, while at log $g = 4.25$ it is clearly broader. Given these results, we conservatively adopt a gravity error of $\pm 0.25$ dex at $T_{\text{eff}} = 2800$ K and confidently rule out deviations of $\pm 0.5$ dex at this $T_{\text{eff}}$.

The above error analysis does not explore the full parameter space; we have examined TiO and Na i separately and have investigated the effect on each of varying only one parameter (either $T_{\text{eff}}$ or log $g$) while keeping the other fixed at our best-fit value. However, we have already shown previously (see Fig. 3 and accompanying discussion in text), by varying both $T_{\text{eff}}$ and gravity and simultaneously comparing TiO and Na i, that deviations of $\pm 0.5$ dex from log $g = 4.0$ can be completely ruled out at any $T_{\text{eff}}$. Similarly, we can easily show that deviations of $\pm 100$ K from $T_{\text{eff}} = 2800$ K can be confidently ruled at any gravity. To see this, imagine that $T_{\text{eff}} = 2900$ K. The weak $T_{\text{eff}}$/gravity degeneracy in TiO allows us to fit TiO at this temperature with log $g = 3.25$ (Fig. 4, bottom left, in blue). However, the Na i doublet can be fitted at $T_{\text{eff}} = 2900$ K only at a vastly different gravity of log $g = 4.25$ (Fig. 4, second panel from bottom right, in blue). Similarly, if we assume a $T_{\text{eff}}$ of 2700 K, a good fit to Na i is obtained at log $g = 3.75$ (Fig. 4, second panel from top right, in blue). However, no adequate fit can be found to TiO at this low $T_{\text{eff}}$ at any gravity; as discussed earlier, even log $g = 4.5$ requires a $T_{\text{eff}}$ of 2800 K to fit the band heads, while lower gravities require similar or higher $T_{\text{eff}}$. Thus $T_{\text{eff}} = 2800 \pm 100$ K are completely untenable, regardless of gravity, by our requirement that TiO and Na i give consistent parameters. Similar tests (not shown), using TiO and Na i intercomparisons, indicate that changing both $T_{\text{eff}}$ and gravity by only 50 K and 0.25 dex from the best-fit values give more consistent fits to the data compared to 100 K or 0.5 dex variations, but still not as good as obtained with the best-fit model (the mismatches between models and data are similar to those shown in Figure 4 for 50 K and 0.25 dex variations). All of this implies that our $T_{\text{eff}}$ and gravity are precise to at least $\pm 50$ K and $\pm 0.25$ dex. Finally, our $\chi^2$ tests confirm our best-fit values of $T_{\text{eff}} = 2800$ K and log $g = 4.0$, as well as errors of at most 50 K and 0.25 dex around these values. We therefore adopt $T_{\text{eff}} = 2800 \pm 50$ K and log $g = 4.0 \pm 0.25$ dex for USco 55.

Now let us examine USco 104. In Figure 5 we again show fits at log $g = 3.5$ and 4.0. At log $g = 4.0$, the TiO band heads are well matched by a 2750 K model. The Na i doublet in this model, however, is too broad and deep to fit the data; the model K i doublet is also slightly stronger than observed. At this gravity, both alkali doublets are well matched by a 3000 K model instead (strictly speaking, 3000 K fits the Na i doublet,

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17 Notice that at all the gravities and $T_{\text{eff}}$ shown, the models predict an absorption feature at $\sim 8196.5$ Å, in the red wing of the Na i doublet, which is absent in the data. Given the enormous number of molecular lines in M-type spectra and the as yet incomplete molecular data incorporated in the models, such minor discrepancies are not surprising. As evident in Fig. 3, this particular discrepancy does not affect our Na i fitting results, and we may safely ignore it.
Fig. 4.—Error analysis in USco 55. Left column: TiO data (black) compared to models (in color) at various $T_{\text{eff}}$ and $\log g = 4.0$. In red, we show the best fit to TiO ($\log g = 4.0$, $T_{\text{eff}} = 2800$ K) obtained in Fig. 3. In purple, we show models at $2800 \pm 50$ K. These fits are slightly worse, either in the band head strength or in the continuum redward of 8452 Å. In green, we show models at $2800 \pm 100$ K. The fits are clearly very poor. Collectively, this shows that TiO is sensitive to 100 K $T_{\text{eff}}$ changes and that $2800 \pm 50$ K is a good estimate of our $T_{\text{eff}}$ error. Right column: Na i doublet data (black) are compared to models (in color) at various $T_{\text{eff}}$ and gravities. Again, we show in red the best fit to Na i obtained earlier ($4.0, 2800$ K). In purple, we show models at the same $T_{\text{eff}}$, but with $\log g = 4.0 \pm 0.25$ dex. These fits are slightly worse. Better fits are obtained at the same gravities, but with $T_{\text{eff}} = 2800 \pm 100$ K (blue). However, these $T_{\text{eff}}$ are clearly not good fits to TiO (left column). Finally, in green, we again show models at $2800$ K, but with $\log g = 4.0 \pm 0.50$ dex. These are obviously poor fits. All this shows that once $T_{\text{eff}}$ is fixed by the TiO fits, Na i is very sensitive to 0.50 dex gravity changes; $\pm 0.25$ dex is a good estimate of our gravity error.
while a slightly lower $T_{\text{eff}}$, 2950 K, fits $K_i$.

Finally, the continua in the $Na_i$ and $K_i$ orders are well fitted by a 2750 K model at $\log g = 4.0$, in agreement with the $T_{\text{eff}}$ implied by the band heads; 3000 K is a poor fit to the continua (this is shown in Fig. 5 for the $Na_i$ order). The temperature discrepancy between the various diagnostics is thus $\sim 250$ K; $\log g = 4.0$ is clearly not viable. A similar analysis (not shown) also precludes $\log g = 3.0$.

At $\log g = 3.5$, the TiO band heads, the $Na_i$ and $K_i$ doublets, and the continua in the alkali orders are all fitted very well by a 2750 K model. An analysis similar to that for USo 55 again yields $T_{\text{eff}}$ errors of $\sim 50$ K and gravity errors of $\pm 0.25$ dex. For USco 104, therefore, we have $T_{\text{eff}} = 2750 \pm 50$ K and $\log g = 3.5 \pm 0.25$ dex. These values are confirmed by our $\chi^2$ tests.

All the preceding analysis illustrates the efficacy of using intercomparisons between the TiO band heads and the $Na_i$ doublet to determine temperature and gravity. The strong $T_{\text{eff}}$-dependence of TiO and the weakness of its dependence on gravity, combined with the strong gravity-sensitivity of $Na_i$ and the opposite sense of the $T_{\text{eff}}$/gravity degeneracy in TiO and $Na_i$ (which causes the difference in $T_{\text{eff}}$ implied by the two diagnostics to change sign on either side of the most appropriate gravity), allows us to quickly zero in on the best $T_{\text{eff}}$ and gravity values. Our fits also show the value of using the $K_i$ doublet to check the gravity obtained from $Na_i$ and the usefulness of fitting the continua surrounding the alkali doublets as a check on the $T_{\text{eff}}$ (and thus on the gravity). With the best-fit model spectrum, all our spectral diagnostics—TiO band heads, alkali doublets, and continua—are fitted remarkably well, while small deviations from the best-fit parameters cause large discrepancies between the models and data. This attests to the robustness of our fitting procedure.

Finally, as mentioned earlier, the fact that a unique best-fit model can be found at all suggests that the synthetic spectra are quite accurate in absolute terms. Errors in the model opacities can indeed lead to systematic offsets from the true $T_{\text{eff}}$ and gravity, when fitting any one of our diagnostic spectral regions. However, any such offsets are more likely to be different for each of these regions; it is unlikely that the opacity errors all conspire together to produce a model spectrum that fits all our diagnostics at the same $T_{\text{eff}}$ and gravity. The presence of such consistency in our fits supports the accuracy of the derived temperatures and gravities.

4.1.2. Empirical Evidence for Gravity Variation

Notice, now, that we find USco 104 and 55 to have gravities differing by 0.5 dex. We will soon see that even larger gravity

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19 The $K_i$ continuum shown in Fig. 5 does not clearly differentiate between the different $T_{\text{eff}}$ models.
differences also show up in our sample. This is one of the main results of this paper, whose significance will be discussed shortly (§ 5). For now, to drive home the point that this difference in gravities is real, and not an artifact of our fitting process, we directly compare the observed spectra of USco 55 and 104. Such a comparison cannot, of course, yield absolute values for $T_{\text{eff}}$ and $\log g$. It can indicate, however, if the relative values we infer from model fits are reasonable. In other words, we can test whether the similarities and differences between the observed spectra are consistent with the model prediction of different gravities.

In the top panel of Figure 6, we compare the TiO band heads in USco 55 and 104. The continua in the regions outside the band heads (i.e., blueward of 8432 Å) closely match each other, indicating that our relative normalization of the two spectra is good. Notice that the TiO band heads in USco 55, at ~8205 and 8250 Å, are slightly weaker, indicating that USco 55 is in fact very slightly hotter than USco 104 (as also indicated by the TiO band heads in the top panel 1).

![Figure 6](image-url)
than that of USco 55. This assertion is independent of any spectral-fitting and is implied simply by the known behavior of TiO with temperature (the potential effects of dust are not considered here; we have noted before, and will argue in detail in § 4.3.1, that grain formation is negligible in our targets). We note that differences in rotational velocity cannot be responsible for the observed mismatch in band head strengths: model-independent cross-correlations show that USco 55 and 104 have very similar $v\sin i$ (12 and 16 km s$^{-1}$, respectively; that their $v\sin i$ are indeed roughly equal is visually evident from the similar smoothness of the continuum molecular features in their spectra, in Fig. 6). If anything, the slightly larger velocity of USco 104 should cause its TiO band heads to be shallower, not deeper, than that of USco 55, if the intrinsic band head strengths were the same in both (in reality, tests show that the $\sim 4$ km s$^{-1}$ $v\sin i$ difference should have an observationally negligible effect on the observed band heads). A difference in $T_{\text{eff}}$ is thus strongly suggested by the data alone. This result qualitatively supports the (small, 50 K) $T_{\text{eff}}$ difference we found from our detailed fits.

Next we compare the Na i doublets observed in USco 55 and 104 (Fig. 6, middle panel). Clearly, Na i in USco 104 is somewhat weaker (both narrower wings and shallower core) than in USco 55. One might expect this if USco 104 were hotter: increasing $T_{\text{eff}}$ would damp the abundance of both Na i and the main perturber responsible for collisional broadening, H$_2$, producing a narrower, shallower doublet. But the preceding TiO comparisons show that USco 104 is actually cooler than USco 55, which should make Na i in 104 relatively stronger. In other words, the Na i doublet in USco 104 is comparatively weaker in spite of its lower $T_{\text{eff}}$. This strongly suggests that gravity in 104 is significantly lower: by decreasing both the pressure-broadening by H$_2$, as well as the abundance of Na i at any given optical depth, lower gravity leads to a weaker line; decreasing gravity sufficiently can compensate for the opposing effects of decreasing $T_{\text{eff}}$ on the Na i doublet (as indeed illustrated by the synthetic spectra as well, in Fig. 2; this is the source of the strong $T_{\text{eff}}$/gravity degeneracy in Na i in the models). Once again, we point out that rotation effects cannot lead to the observed profile differences: first, because the two objects have almost identical $v\sin i$, and tests show that the small $v\sin i$ difference would not have any discernible effect on these Na i profiles; second, because the slightly faster rotation of 104, if observable, would actually lead to (very slightly) broader Na i wings compared to USco 55, not manifestly narrower ones.

We also note that the difference in Na i profiles cannot be ascribed to normalization problems. In the bottom panel of Figure 6, we compare the entire Na i order of USco 55 and 104. The two continua generally overlap very well, indicating good relative normalization. Indeed, significant differences in the continua occur mainly at, and slightly redward of, the TiO band heads at 8206 and 8251 Å; the bands are stronger in USco 104. Thus, these TiO band heads also imply that USco 104 is cooler than 55, just like the TiO examined above.

Taken together, therefore, the TiO and Na i data alone strongly suggest that gravity in USco 104 is lower than in 55. This result is an empirical one, independent of any spectral-fitting; it rules out the possibility that the difference in gravities derived from our detailed fits is only an artifact of our fitting procedure. It is however conceivable that other real phenomena, e.g., cool spots, dust effects or varying metallicity, mimic gravity variations in the data. Once we have examined the rest of our Upper Sco sample and presented more examples of apparent gravity differences, we will consider (and argue against) such effects.

**4.2. Overall Results for Upper Sco**

The best fits to a representative selection of objects from our sample are shown in Figure 7. In each case, the “best-fit model” is defined as one that simultaneously fits all our spectral diagnostics. Specifically, we show the fit of this model to the triple-headed TiO band head and to the Na i doublet (which together fix $T_{\text{eff}}$ and gravity), as well as to the K i doublet and the continuum surrounding the Na i doublet (both of which provide independent checks on the derived parameters). We show only the red lobe of the K i doublet, since in most of the objects shown, the blue lobe is degraded by telluric contamination. A paucity of space also prevents our showing the fits to the continuum in the K i order; in all cases, however, the same model is also the best fit to this continuum. Our final adopted values are tabulated in Table 1. We note that the models reproduce the data, especially the triple-headed TiO band, Na i doublet and Na i continuum, remarkably well. This is a testament to the vast improvements in the atmospheric structure models, molecular and atomic line lists, and resulting synthetic spectra over the last several years.

In the red lobe of the K i doublet too, the fits are quite good, with two small caveats. First, the data for USco 53 appears slightly broader than the model. However, this is very likely due to an inadequately modeled absorption line at $\sim 7697$ Å (e.g., see best fit to USco 112 in Fig. 7 and to USco 55 in Fig. 3; the line appears well modeled in the former, but less so in the latter), which is blended into the K i red lobe at the high rotation velocity of USco 53, making the data seem a little broader. Second, the fit to the K i red lobe is clearly not as good in USco 109 and 130; this is due to the noisiness of the K i data (we make this point explicitly by showing the unsmoothed data for these two objects; the noise is obvious). Both objects are at the faint and red end of our sample; as mentioned in § 3.3, poorer S/N in the K i order is thus to be expected, since it occurs significantly blueward of our other diagnostic regions. Seeing conditions were moreover not optimal for USco 109; nevertheless, the best-fit model still reproduces the general shape of the line (except in the very core, where the data appears chopped by noise). Even in USco 130, which is one of our two faintest and reddest objects, the model matches the data passably well (and reproduces the line core accurately). For this object, we point out that the poorer quality of the K i fit cannot be ascribed to a problem with the synthetic spectra at the relatively low $T_{\text{eff}}$ and gravity derived (from the TiO and Na i fits): Figure 11 shows an excellent fit to the K i red lobe in GG Tau Bb, for which the S/N is much higher, at the same $T_{\text{eff}}$ and gravity; the poorer fit in USco 130 is indeed due to noise. For both USco 109 and 130, the TiO and Na i orders have much higher S/N, and the fits we obtain to these regions are clearly very good and give consistent values of $T_{\text{eff}}$ and log g. Moreover, we cannot improve the K i fits in either object by choosing any other $T_{\text{eff}}$/gravity combination; other such permutations also degrade the fits to TiO and Na i. We are therefore confident of the veracity of the $T_{\text{eff}}$ and gravity derived for USco 109 and 130 from the TiO band head and Na i fits, in spite of the poor quality of the K i data.

Finally, we point out the good agreement between the models and data in three other $T_{\text{eff}}$-sensitive TiO band heads: at $\sim 8206$ and 8251 Å in the Na i order, and at 7705 Å in the K i order (see Fig. 7, and best-fits in Figs. 3 and 5). At 8206 Å, the model band head seems slightly offset in wavelength from
the data. This is likely due to an inadequately modeled absorption feature just blueward of, and blended into, the model band head. However, the overall strength of this band head is the same in the data and models. At 8251 and 7705 Å, the agreement between the data and models is very good (the model-data agreement is perhaps best seen in USco 53, where the high \( v \sin i \) smooths the stellar spectrum considerably and allows the eye to avoid confusion from sharp noise and telluric features in the spectrum). This shows the usefulness of using the continuum in the Na \( i \) and K \( i \) orders to constrain \( T_{\text{eff}} \), and supports the \( T_{\text{eff}} \) (and thus gravities) we derive. We note in passing that this is the first time such good agreement between synthetic spectra and observations has been demonstrated, over such relatively large swathes of continuum at high-resolution, in the M spectral classes; this is another sign of the accuracy of the models used here.

Our model fits imply that \( T_{\text{eff}} \) in our Upper Sco sample ranges from about 2900–2600 K. This is more or less consistent with expectations for young M5–M8 PMS objects (Luhman (1999); we revisit this issue in later sections). However, we also find that surface gravity varies from log \( g \) ~ 4.0–3.25 (Table 1). Six of our objects have log \( g \) ~ 4, two have ~3.75, one has ~3.5, and two have ~3.25 (±0.25 dex errors in all cases), with lowest gravity in the coolest targets. This is seriously at odds with the predictions of theoretical evolutionary tracks, for a coeval sample of PMS objects at ~5 ± 2 Myr (the rough age of the Upper Sco cluster; § 5.1). While log \( g \) of 4.0–3.75 is commensurate with ~5 ± 2 Myr tracks, 3.5 or less is not, nor is a variation of ~0.75 dex; we will discuss this shortly (§ 5). First, we briefly discuss USco 104, 128, and 130, our coolest, lowest gravity objects.

For USco 104, we have presented a detailed spectral analysis in § 4.1.2, in order to show that a lower gravity is commensurate with the data. One can make a similar case for USco 128 and 130. We explicitly discuss USco 130 here; the arguments are analogous for 128. In Figure 8 we compare the observed triple-headed TiO band and the Na \( i \) doublet in USco 130 to those in USco 55 and 104. We note at the outset that rotational broadening effects are not germane to the following analysis: the difference in rotation velocity between USco 130 (\( v \sin i \) ~ 11 km s\(^{-1}\)) and either USco 55 or 104 (\( v \sin i \) ~ 12 km s\(^{-1}\), respectively) is ~2 km s\(^{-1}\), negligible compared to other broadening effects (e.g., pressure broadening).

First, we see that the TiO in USco 130 is significantly stronger than in 55 (especially in the \( \lambda \lambda 8442, 8452 \) band heads); this is why we have derived a lower \( T_{\text{eff}} \) for it (2600 K) than for 55 (2800 K). However, the strength of the Na \( i \) doublet is very similar in both. If both objects were the same gravity, then the Na \( i \) doublet in the appreciably cooler USco 130 should instead be much stronger (i.e., broader and deeper). The simplest explanation is that gravity is substantially lower.
in 130 than in 55, compensating for the much lower $T_{\text{eff}}$ of 130 and yielding very similar Na i profiles for both. Indeed, a closer look reveals that the doublet is slightly weaker (shallower core, narrower wings) in USco 130, suggesting that the temperature difference is more than compensated for by a gravity difference.\footnote{This may not be clear in the plot shown, but is evident if the plot in the electronic copy is blown up.} This model-independent analysis is completely consistent with our fits to the synthetic spectra, which yield $\log g = 3.25$ for USco 130 and $\log g = 4.00$ for USco 55.

Similarly, we see that the TiO bands in USco 130 are clearly stronger than in 104, which agrees with our model fit result that the former is cooler than the latter (by $\sim 150$ K). At the same time, we see that their Na i doublet profiles are very similar. Once more, if the two objects had the same gravity, Na i in USco 130 should be much stronger, since it is significantly cooler. This signifies that gravity in USco 130 is lower than in 104 as well, sufficiently so in order to offset the temperature differential between the two. This is in agreement with our model fit results of $\log g = 3.25$ in USco 130 and 3.50 in USco 104.

In fact, a careful examination shows that the line-wings in USco 130 are slightly broader than in 104 (although by much less than might be expected from the large $T_{\text{eff}}$ differential between the two, were their gravities the same). In other words, while the Na i profiles in USco 130, 104, and 55 are all very similar, the doublet in 130 is more accurately intermediate in strength between that of 104 and 55 (which is why the difference between the USco 104 and 55 Na i profiles is clearer, in Figure 6, than the difference between the profiles of USco 130 and either 104 or 55, in Fig. 8). What this implies is that, in the Na i profiles, a large gravity difference between USco 130 and 55 overcompensates for the large $T_{\text{eff}}$ difference, while a nearly as large $T_{\text{eff}}$ differential between USco 130 and 104 is not completely compensated for by a smaller gravity differential; meanwhile, the effect of the much smaller temperature difference between USco 104 and 55 is overwhelmed by a large difference in gravity. These conclusions, drawn from intercomparisons of the TiO and Na i data alone, are completely commensurate with the parameters derived from our fits: $T_{\text{eff}} = 2800$ K, $\log g = 4.0$ for USco 55, $T_{\text{eff}} = 2750$ K, $\log g = 3.5$ for USco 104, and $T_{\text{eff}} = 2600$ K, $\log g = 3.25$ for USco 104. The gravity variations in our sample implied by the synthetic spectra are thus not a spurious outcome of fitting uncertainties, but appear to be quite real.

We point out in passing that gravity fluctuations may also affect precise spectral typing. This is not very obvious in our sample, given the small range in spectral types covered (2.5 subclasses, derived by AMB00) and the relatively large typing uncertainties ($\pm 0.5$ subclasses; AMB00). Nevertheless, we note that USco 104 (M5) is one of the two earliest type objects in our sample, while we find it to be comparatively cool (2750 K); this discrepancy may be due to its significantly lower gravity ($\log g = 3.50$) compared with most of the other targets. Our results suggest that gravity-induced typing uncertainties are not overwhelming: the two coolest objects (USco 128 and 130 at 2600 K) are indeed assigned the latest types, despite having the lowest gravities. However, we cannot rule out errors at the $\pm 1$ subclass level, estimated from the range in types assigned by AMB00 to objects with different $\log g$ but the same $T_{\text{eff}}$ (e.g., see targets at 2750 K, Table 1). This does not affect our analysis, since we do not base any conclusions on the precise spectral types (we only refer at times to the range in types covered, which is very likely to be in the right ballpark). It prompts us to caution, nonetheless, that even in a roughly coeval sample, the ordering of objects by $T_{\text{eff}}$ and spectral type may not be identical, perhaps in part because of gravity effects, in the cool young PMS regime; this is worth keeping in mind for PMS spectral type to $T_{\text{eff}}$ conversion schemes.

Returning now to the veracity of gravity variations in our sample, we must pause to ask whether any physical processes can mimic low-gravity effects on the spectral line profiles, causing us to infer systematically erroneous gravities (and $T_{\text{eff}}$, for that matter). We examine the four most plausible mechanisms: atmospheric dust, magnetically induced cool spots on the stellar surface, metallicity variations, and changes in the pressure-broadening of alkali lines.

### 4.3. Physical Effects Mimicking Low Gravity

#### 4.3.1. Dust

In § 3.1 we stated that the atmospheric models do not imply any dust formation in our PMS sample. That is, the data are fitted very well (as we have shown) by synthetic spectra in
which grain effects are not yet important (at least in the red spectral regimes we have analyzed); dust appears in our model spectra only at still lower temperatures. However, it is plausible that the treatment of grains in the models is inadequate. Perhaps dust does matter in our coolest targets: the relative weakness of the alkali doublets in these objects is really due to overlying continuum grain opacity and is misinterpreted as a signature of low-gravity by synthetic spectra that underestimate grain effects. Is this suggestion viable? We address this by comparing our mid- to late-M PMS sample to field dwarfs of similar spectral type. Dust opacity effects of the sort hypothesized here are known to be important in the latter (Jones & Tsuji 1997; Leinert et al. 2000); an analysis of their spectra can thus indicate whether grains contribute significantly to the spectral characteristics of our sample as well.

We perform this analysis in Appendix A, using a sample of field dwarfs that are homogeneous in gravity (log g $\sim 5.0$), metallicity (solar), and $v \sin \, i$, and span a similar range in spectral type as our PMS targets. The main result is that we find no significant signatures of dust in the PMS objects analogous to those seen in the dwarfs. Basically, the TiO bands in the dwarfs strengthen monotonically with decreasing $T_{\text{eff}}$ (i.e., later spectral type) until the onset of grain formation, at which point the bands reverse in strength and become monotonically weaker with later type. Where the reversal occurs depends on the wavelength of the specific TiO bands considered: bluer bands (e.g., around 7050 Å) are more strongly affected, and reverse strength at an earlier type, than redder bands (e.g., the $\sim$4440 Å ones used in our preceding $T_{\text{eff}}$ analysis). The strength of Na i doublet in the dwarfs is seen to follow the behavior of the 7050 Å TiO bands, reversing strength (although less markedly) as dust opacity kicks in. Most of these effects have been pointed out by other investigators as well; the underlying reasons are briefly discussed in Appendix A. In our PMS sample, however, we see no reversal in any of the TiO bands with decreasing $T_{\text{eff}}$, in spite of the weaker Na i we have found in the coolest targets. We conclude that dust cannot be responsible for the weaker alkali lines in the latter objects; gravity differences indeed seem to be the best explanation. In fact, the 7050 Å TiO bands (which are somewhat gravity sensitive as well, as spectral synthesis models indicate), while continuing to strengthen in our sample with decreasing $T_{\text{eff}}$, without ever reversing, do exhibit additional variations that correlate well with the gravities we derive from Na i; this further implicates gravity differences within our PMS sample. We mention in passing that a reduction in the neutral alkali strengths, such as we observe, cannot be ascribed to alkali depletion through molecule or grain formation: such effects, e.g., formation of alkali chlorides, appear only on progressing well into the L types.

The absence of grain effects in our targets is not too surprising, for three reasons. First, even if they were completely analogous to field M dwarfs, we would not expect to see very strong dust signatures even in our latest objects: at $\sim$M7, they lie at the threshold of dust onset in field dwarfs. Second, PMS objects of a given spectral type are thought to be somewhat hotter than dwarfs of the same type (e.g., Luhman 1999); as we discuss later, the $T_{\text{eff}}$ derived in this paper are consistent with this view. Higher $T_{\text{eff}}$ damps grain formation, so the onset of dust in the PMS phase might well occur at later spectral types than in field dwarfs. Finally, our PMS objects have much lower gravity than field M dwarfs; the attendant decrease in photospheric pressure can inhibit the coalescence of molecules into grains (see Leinert et al. 2000). At any rate, the absence of empirical dust signatures in our PMS spectra largely rules out grain effects skewing our gravity analysis.

4.3.2. Cool Spots

We have undertaken a detailed analysis of the effect of cool spots on our $T_{\text{eff}}$ and gravity determinations; we summarize our results here. We have considered changes in the observed line profiles induced by two phenomena: (1) the temperature contrast between a spot and the surrounding, hotter photosphere and (2) the lower “effective” gravity of a spot compared to the true surface gravity, due to the added presence of magnetic pressure (and thus a decrease in gas pressure) within the spot. We find that even when spot parameters are chosen to maximize their effect on the observed optical line profiles—a spot areal coverage of 50%, a temperature differential of 500 K with the surrounding hotter photosphere, and a (resulting) effective gravity 0.75 dex lower than the true surface gravity—the effect on our inferred $T_{\text{eff}}$ and gravity is small. Such spots cause us to derive a $T_{\text{eff}}$ lower by 150–200 K than the photospheric temperature and a gravity lower by 0.25 dex than the true surface gravity. Whether the lower inferred $T_{\text{eff}}$ can be called erroneous is a matter of taste: when a cool spot covers half the surface, the total bolometric flux is indeed lower than that from an unspotted star; insofar as $T_{\text{eff}}$ is a measure of this flux, our derived lower-than-photospheric value is not inaccurate. The difference between the true and inferred gravity is also not very high (the magnitude of this (systematic) change is of order the (random) error in our gravity determination). Note that spots with either an appreciably larger or smaller temperature differential with the photosphere affect our results even less (obviously true for a small temperature differential; for a large differential, the absolute flux contributed by the much cooler spot is negligible compared to the photospheric emission, so the final spectrum is almost entirely photospheric).

Second, even if we account for the possibility that our lowest gravity objects are actually underestimations by $\sim$0.25 dex, the gravity variations within our Upper Scorpius sample remain quite large ($\sim$0.5 dex). Third, our lowest gravity objects are also the coolest ones. In §5.4, we will revisit why this might be; here we point out that cool spots are not a viable explanation. There is no reason to suppose that spots are preferentially present only on the low-$T_{\text{eff}}$ objects, and not on the hotter ones as well (in fact, quite the contrary, if rotation affects activity, as usually supposed; see below). Then, the gravities inferred in some of our hotter objects would also be too low, again by $\sim$0.25 dex (indeed, we do see variations at this level in hotter objects). Spots may thus produce a spread of $\sim$0.25 dex in gravity over our sample, but not a (much larger) systematic difference in gravity between hotter and cooler objects. All of this implies that invoking spots does not change our basic result, that large gravity differences appear within our Upper Sco sample with decreasing $T_{\text{eff}}$. Finally, available data suggests that any cool spots that are present should generally be smaller than we assume. The covering fractions are usually of order a few percent; in the most spotted cases, the fraction may increase to $\sim$30%. Spot with covering fractions appreciably smaller than the 50% we assume would affect our results negligibly.

Finally, the covering fraction of cool spots is expected to increase with rotational velocity. However, USco 104, 128, and 130, the three objects with anomalous gravity (compared to the theoretical tracks) are not especially fast rotators. Indeed, USco 128 is the slowest rotator in our sample, while
USco 104 and 130 have moderate velocities, comparable to those in other Upper Sco objects that do not exhibit any gravity anomalies. It is true that we only have $v \sin i$; the true equatorial velocities of USco 104, 128, and 130 may be higher. By the same token, however, we would expect to see gravity variations among those objects in our sample with the highest $v \sin i$. This is not observed: although some of our hotter targets have $v \sin i$ approaching, or even exceeding, $50 \, \text{km \, s}^{-1}$, none of them evinces gravity anomalies. In short, if large cool spots are to blame for the behavior of USco 104, 128, and 130, one would have to postulate that such spots only besiege cool, slow to moderate rotators, and not slightly hotter, much faster rotating ones. This does not appear very likely: on the one hand, there is no particular reason to suspect such a strong $T_{\text{eff}}$-dependency in spots; on the other hand, there are good physical reasons to expect faster rotators to be more spotted.

In summary, cool spots are very unlikely to affect our $T_{\text{eff}}$ and gravity derivations. Even if they result in some small spread in gravity over our sample, they are unlikely to cause the large drop in gravity we find in the coolest objects within the sample.

### 4.3.3. Metallicity

In this work, we have assumed solar-metallicity (i.e., used synthetic spectra with $[\text{M/H}] = \log([\text{M/H}]/[\text{M}_{\odot}/\text{H}_{\odot}]) = 0.0$). However, variations in metallicity can potentially affect the temperatures and gravities we infer. Specifically, higher metallicity reduces the abundance of hydrogen particles (which are the main source of collisional broadening); it also implies a decrease in pressure at a given optical depth (because of higher opacity). Both effects tend to produce a narrower alkali line, just as decreasing gravity does (Schweitzer et al. 1996; Basri et al. 2000). Simultaneously, higher metallicity can also mimic lower $T_{\text{eff}}$, by making the TiO bands stronger (Leggett 1992), both because of an increase in abundance of titanium and oxygen and because of a decrease in temperature at a given optical depth (again, due to higher opacity). In summary, not accounting for an increase in metallicity can yield spuriously low $T_{\text{eff}}$ and gravity. Can this effect explain the presence of low-gravity objects at the cool end of our sample? We do not think so, for the following reasons.

Using synthetic spectra to fit the observed Na i and K i optical doublets (i.e., the same technique employed in this paper), Schweitzer et al. (1996) have examined in detail the effect of varying metallicity on the gravity inferred for the M8 field dwarf VB 10. They show that for fixed $T_{\text{eff}}$ (2700 K in their analysis, similar to the $T_{\text{eff}}$ derived for our coolest objects), increasing (decreasing) metallicity by 0.5 dex has the same effect on the alkali lines as decreasing (increasing) gravity by an equal amount. The implications of this are two-fold: (1) a change in metallicity is certainly capable of masquerading as a change in gravity; however, (2) the magnitude of the required metallicity shift is comparable to that of the perceived shift in gravity. Now, we derive $\log g \approx 3.25 \pm 0.25$ dex for the lowest gravity objects (USco 128 and 130), while the rest of the sample is mostly at $\sim 3.75 - 4.00$; the latter is also the range predicted by the theoretical tracks for mid- to late-M PMS objects at an age $\sim 5 \pm 2$ Myr (§ 5.1). Invoking metallicity variations instead then implies USco 128 and 130 are overabundant, compared to both solar and the rest of our Upper Sco sample, by $\sim 0.75$ dex, and by at least $\sim 0.25$ dex even taking the lower limit on predicted gravity and our $\pm 0.25$ dex errors in $\log g$ into account.

This is quite a substantial variation in abundance. Such a deviation from solar metallicity would be surprising for a young, nearby association; moreover, differences at this level are even more unlikely within a single association. Indeed, Padgett (1996) has analyzed a number of nearby star-forming regions (Taurus-Auriga, Ophiuchus, Chameleon, and Orion) and found solar abundance to within $\pm 0.1$ dex (i.e., $\pm 25\%$) in all of them; within a given region, the variation is at most at the same level. In light of this, the overabundance required in USco 128 and 130 ($\sim 2 - 4$ times solar) to produce the gravity effect we see appears implausibly high. Finally, we will show further on (§ 5.4) that a similar deviation from the tracks is found in the GG Tau B system as well: while gravity in GG Tau Ba agrees quite well with the predicted value, Bb has a gravity lower than expected by $\sim 0.25 - 0.5$ dex. Since Ba and Bb not only belong to the same star-forming region (Taurus) but also to the same bound stellar system, this effect is highly unlikely to result from a large difference in metal abundance between the two stars. These arguments lead us to conclude that metallicity variations are not a viable explanation for the range in gravities and consequent deviation from the theoretical evolutionary tracks (see § 5.1), implied by our spectral analysis.

### 4.3.4. Collisional Broadening

Through intercomparisons of the data alone, we have shown that the coolest objects in our sample have weaker alkali lines than hotter ones. We have argued that this cannot be due to the onset of dust opacity. The only other way to achieve this effect is through a weakening of the line-broadening mechanism in our coolest targets. This can happen in three ways: (1) if the intrinsic gravity in the coolest objects is lower, or (2) their alkali lines arise mainly in cool spots with lower gas pressure than the surrounding photosphere, or (3) their metallicity is higher. Comparing our data to the synthetic spectra, we find that the effective reduction in gravity required to reproduce the alkali profiles in our coolest targets is of order $0.50 - 0.75$ dex: either the gravity of these objects is truly lower by this amount than in the rest of the sample, or cool spots or metallicity variations mimic a gravity reduction of this magnitude. We have argued that spot or metallicity effects are highly unlikely to produce such a large offset, implying a real variation in intrinsic gravity.

However, one might argue that, while the empirical data comparisons certainly indicate a reduction in line broadening at the cool end of our sample, the magnitude of this effect is overestimated by the synthetic spectra. As noted earlier, metallicity variations (and thus inferred gravity fluctuations) of $\sim 0.1$ dex cannot be ruled out; cool spots may also mimic gravity effects at the $\sim 0.25$ dex level. Moreover, a reasonable age spread of $\sim 1 - 2$ Myr in the Upper Sco sample can lead to real shifts in gravity of $\sim 0.25$ dex (see § 5.1 and Fig. 9). Is it possible, therefore, that the gravity in the coolest objects is effectively only $\sim 0.1 - 0.25$ dex lower than in the hotter objects, and that the model spectra suggest a much larger variation due to an incorrect treatment of line broadening? We think not, for the following reasons.

Spots, metallicity differences, and/or an age spread should affect our entire USco sample equally. However, while a $0.25$ dex spread in derived $\log g$ is indeed seen in our hotter targets ($T_{\text{eff}} \sim 2750$ K) and may arise from any or all of these causes, we do not find larger, dramatic departures from expected gravities in this $T_{\text{eff}}$ regime—as we show in § 5, our $\log g$ for these objects are all in agreement with the evolutionary track predictions for the assumed age of Upper Sco (5 $\pm$ 2 Myr). This implies that the model treatment of line broadening at these temperatures is adequate; to produce the much larger drop in $\log g$ derived for our coolest objects, the
Fig. 9.—$T_{\text{eff}}$ vs. gravity for our Upper Scorpius and Taurus sample, compared to the Lyon98/00 predictions. All Upper Sco members are shown as filled circles, except the two coolest ones, USco 130 and 128 (diamonds). GG Tau Ba and Bb are the crosses. Objects with the same derived $T_{\text{eff}}$ and gravity have been slightly separated in $T_{\text{eff}}$, for clarity. Solid lines are isochrones in the Lyon98/00 model, at ages from 1 to 10 Myr. Dotted lines denote the evolutionary tracks for various masses in the Lyon98/00 model, from 0.20 to 0.01 $M_{\odot}$. The error bars on our measurements of $T_{\text{eff}}$ (±50 K) and gravity (±0.25 dex) are depicted at the bottom right. USco members with $T_{\text{eff}} \geq 2750$ K agree fairly well with the Lyon98/00 5 Myr locus. Cooler objects, however, appear much younger. Similarly, GG Tau Ba is not too far from the expected 1 Myr locus, but Bb seems much younger. The horizontal and vertical arrows, in the bottom left, indicate the change in $T_{\text{eff}}$ and log g (150 K and 0.25 dex, respectively) required if any object is afflicted by very large, cool spots (50% areal coverage, 500 K cooler than surrounding photosphere; see § 4.3.2); the diagonal arrow shows the combined change in position.

5. IMPLICATIONS

In § 5.1 we compare our derived $T_{\text{eff}}$ and gravities to the predictions of theoretical evolutionary tracks constructed by the Lyon group, which are currently the most widely used for low-mass stellar and substellar studies. We find significant discrepancies, implying either (1) problems in our analysis, or (2) a substantial $T_{\text{eff}}$-dependent age spread in our sample, or (3) problems with the theoretical tracks. Our arguments in § 4.3 indicate that, while there is certainly room for errors in our analysis, these do not seem likely to cause the large divergence between our results and the evolutionary predictions. We therefore concentrate on the two other possibilities. In § 5.2 we discuss various scenarios whereby a real, large age spread might arise; none seems particularly convincing. We further undermine the hypothesis of a real age spread by demonstrating, in § 5.3, that similar age discrepancies also appear for GG Tau Ba and Bb, which are almost certainly coeval. In § 5.4 we consider the remaining possibility—uncertainties in the evolutionary models—by examining some likely problems in the choice of initial conditions and treatment of convection.

5.1. Comparison to Theoretical Evolutionary Tracks

Recently, Preibisch et al. (2002) have derived a well-constrained age of 5 ± 2 Myr for the Upper Scorpius association. Their sample consists primarily of G, K, and early-M stars (i.e., somewhat higher mass objects than ours); the age has been derived through comparison with the theoretical isochrones of D’Antona & Mazzitelli (1994) and Baraffe et al. (1998). The Preibisch et al. result is fully consistent with the 5–6 Myr derived from the main-sequence turnoff of A and B stars in Upper Sco (de Zeeuw & Brand 1985; de Geus et al. 1989). It also agrees with the kinematic age of ~5 Myr, derived by tracing back the motions of stars in the association till the smallest configuration is reached (Blaauw 1991).

With these results in mind, we compare our derived $T_{\text{eff}}$ and gravities to those predicted by the theoretical evolutionary tracks of the Lyon group. In particular, we combine the models presented in Baraffe et al. (1998, hereafter BCAH98) and Chabrier et al. (2000b, hereafter CBAH00). The BCAH98 models cover masses from 0.02 to 1.4 $M_{\odot}$, while the CBAH00 ones extend from 0.001 to 0.1 $M_{\odot}$. Moreover, the latter models use synthetic spectra (as an outer boundary condition) that incorporate dust formation, while the spectra used in the older BCAH98 models neglect grains altogether.21 However, for the range of masses over which the two sets of tracks overlap, 0.02–0.1 $M_{\odot}$, and at least over the 1–10 Myr age range of interest in this paper, the temperatures and gravities predicted by both are almost identical, i.e., dust does not affect the predictions of these tracks at least above 0.02 $M_{\odot}$ for these ages. In order to compare our results to the theoretical predictions for a large range of masses, therefore, we have combined the BCAH98 and CBAH00 tracks. Specifically, we have adopted the BCAH98 models for masses greater than 0.02 $M_{\odot}$, and the CBAH00 models for lower masses. For the sake of concision, we will henceforth refer to this merged set of tracks as the Lyon98/00 model. One other point needs to be made, regarding the treatment of convection in the evolutionary tracks. BCAH98 models come in three mixing-length flavors: $\alpha = 1.0, 1.5$, and 1.9. However, only the $\alpha = 1$ models extend to masses below 0.6 $M_{\odot}$. Similarly, the CBAH00 tracks, which are restricted to masses $\leq 0.1 M_{\odot}$, exclusively use $\alpha = 1$. In other words, evolutionary models with $\alpha \neq 1$

21 We note that the synthetic spectra adopted in the BCAH98 and CBAH00 tracks, including the Dusty spectra, are significantly older generations than the ones considered in this paper, with some substantial changes in model opacities in the intervening years.
are not available for masses less than 0.6 $M_{\odot}$, which is precisely the mass-regime of interest for our mid- to late-M PMS sample. Consequently, the Lyon98/00 merged tracks we show are only for $\alpha = 1$. This will be important further on, when we attempt to understand discrepancies between our results and the model predictions in terms of uncertainties in the model treatment of convection.

The comparison between our results and the tracks is shown in Figure 9. Three facts are immediately evident. First, in objects hotter than $\sim 2750$ K, our gravities (log $g \approx 3.75$–4.00) are commensurate with those predicted by the 5 ± 2 Myr tracks (indeed, consistent with precisely 5 Myr, within our ±0.25 dex measurement uncertainty). Second, we find a sharp drop in gravity for objects cooler than $\sim 2750$ K; USco 104, 128, and 130 are all much lower in log $g$ than hotter targets. Third, no such drop is predicted by the theoretical tracks, for roughly coeval objects at 5 ± 2 Myr. The Lyon98/00 models imply that, for objects with $T_{\text{eff}} \approx 2200$–3200 K, gravity variations arise predominantly from differences in age: 5 ± 2 Myr old bodies at these temperatures should all have log $g \sim 3.75$–4.00. Consequently, when combined with our derived parameters, the tracks predict a large age discrepancy between the hotter and cooler targets. Objects cooler than $\sim 2750$ K appear substantially younger than 5 ± 2 Myr because of their lower gravity. USco 104 (log $g \approx 3.5$) seems to have an age ≲ 1 Myr, while USco 128 and 130 (log $g \approx 3.25$) appear even younger. We emphasize that sliding our lowest gravity objects along the $T_{\text{eff}}$ axis—i.e., assuming a systematic error in our derived $T_{\text{eff}}$—leaves the discrepancy with the tracks largely unchanged: any given isochrone in the 5 ± 2 Myr range changes by <0.25 dex in log $g$ over the entire 1000 K range shown. Our divergence from the tracks implies a serious disagreement with the predicted gravities.

As an aside, we note that the evolutionary tracks predict masses corresponding to the $T_{\text{eff}}$ and gravities we find; the tracks for various masses are plotted in Figure 9. However, these are not necessarily the masses we derive eventually (Paper II), from a consideration of the observed photometry of our sample combined with our gravity estimates. In general, we will find that our USco masses are in the same ballpark as the model predictions (within the factor of 2 uncertainty in our mass determinations; Paper II). However, for USco 128 and 130 we will derive masses of $\sim 9M_{J}$–$14M_{J}$ (within a factor of 2), substantially lower than the model prediction of $\sim 30M_{J}$ (if the mass tracks in Fig. 9 are extrapolated down, at constant $T_{\text{eff}}$, to our gravity for these two objects). For GG Tau Ba and Bb, which are also plotted in Figure 9 and will be discussed shortly in this paper (§ 5.3), the models predict (again, extrapolating at constant $T_{\text{eff}}$ in Fig. 9) masses of 0.04 $M_{\odot}$ (Ba) and 0.02 $M_{\odot}$ (Bb); the final mass we derive in Paper II for Ba is significantly higher in comparison (0.12 $M_{\odot}$), but quite similar for Bb (0.028 $M_{\odot}$). We will revisit this issue in detail in Paper II; for now we simply caution that the mass tracks shown in Figure 9 are for comparison only, and do not signify the final masses we adopt for our sample. The real value of the $T_{\text{eff}} / \log g$ plot in Figure 9 lies in revealing that our gravities for GG Tau Bb, USco 128 and 130 (and to a lesser extent, USco 104) are completely inconsistent with the model gravities, for the estimated ages of the Taurus and Upper Sco complexes, regardless of the precise mass (or $T_{\text{eff}}$) we assign these objects over the entire 0.2–0.01 $M_{\odot}$ mass range shown (as well as at still lower masses; not shown here but see Paper II).

There are three possible explanations for the age (or equivalently, gravity) discrepancy between our results and the theoretical predictions. (1) Our spectral analysis is incorrect; (2) there is a real-age spread in our Upper Sco sample, with cooler objects being younger; or (3) the evolutionary tracks are problematic. However, we have demonstrated in § 4, through intercomparisons of the data alone, that our coolest USco objects indeed exhibit spectral signatures of relatively low gravity. We have further argued that these signatures are unlikely to arise from dust opacity, cool spot or metallicity effects. Finally, through a consideration of pressure-broadening in the alkali lines, we have argued that if our gravities for the hotter objects are correct (which allows them to agree with the Lyon tracks), then the magnitude of the gravity drop we derive for the coolest targets is likely to be roughly accurate as well. We therefore proceed under the assumption that our spectral analysis is by and large correct and turn our attention to the second and third of the possible explanations listed above.

5.2. Scenarios for Real Age Variations

If USco 104, 128, and 130 are truly ≲ 1 Myr old, then either they are not members of the Upper Sco association or some star formation has occurred much more recently in Upper Sco than previously suspected. Now, all the evidence firmly points to USco 104, 128, and 130 being PMS objects (see § 2.1). In that case, if they are not members of the association, either they must be PMS objects in the foreground or background that appear projected onto Upper Sco, or they must have physically traveled into Upper Sco from some other nearby star-forming region. The projection scenario is unlikely: there is no obvious evidence, from all the studies of PMS objects in Upper Sco so far, of contamination by background or foreground PMS objects. It would be very strange then, if in a small sample of 11 we found three such objects. On the other hand, the $\rho$ Ophiuchus dark cloud borders Upper Sco to the east and is known to harbor PMS objects younger than a million years. Is it possible that USco 104, 128, and 130 are actually members of $\rho$ Oph? We cannot discount this possibility without proper motion data. Moreover, in the few $\rho$ Oph T Tauri with measured radial velocities, the value (~25 km s$^{-1}$; G. Doppmann 2002, private communication) is similar to that in Upper Sco, so our $v_{\text{rad}}$ measurements cannot shed any light on the issue.

However, we can make the following plausibility argument. The core of the $\rho$ Oph dark cloud lies ~25$^\circ$, and the western edge ~20, from the observed positions of our three objects. Thus, if they are really ≲ 1 Myr old, and originally members of $\rho$ Oph, they must have space motions in excess of about 25 km s$^{-1}$, in order to have reached their present locations in the time since their birth. This is an implausibly large value. Given that the velocity dispersion of the molecular gas in $\rho$ Oph is a few km s$^{-1}$, the chance of any single isolated object, let alone three, having such a large velocity is miniscule. Indeed, 25 km s$^{-1}$ is of order the escape velocity from within an AU of a solar mass star. Ejection, through dynamical encounters, is thus a possibility. However, we consider it highly improbable that three of our 11 Upper Sco objects happen to be very young $\rho$ Oph members, originally in close orbit around a solar mass star, and eventually flung out in the direction of Upper Sco. Each of these steps has a very small probability, and their combined probability appears negligible. Proper motions are needed to settle this issue definitively.

The other way of accommodating the apparent youth of USco 104, 128, and 130 is to postulate very recent star formation in Upper Sco. While we cannot rule this out, it seems
very unlikely, given that there are no signs of this in the Preibisch et al. (2002) study. In other words, if three of our 11 objects, or ~25% of our sample, are so young, we would expect this effect to show up strongly in the latter study’s much larger sample. It does not, enabling Preibisch et al. (2002) to strongly constrain the age of the association to 5 ± 2 Myr. On the other hand, it is possible that real age variations are preferentially present at the latest spectral types; since the Preibisch et al. study consists predominantly of earlier spectral types than ours, this would explain why we see an effect while they do not. Is this likely? If one assumes that spectral type corresponds roughly to mass,22 then a spectral type-dependent star formation history implies a mass-dependent one. It is hard to imagine a scenario, however, that leads to the sudden birth of only very low-mass isolated objects, 5 Myr after higher mass stars have ceased to form. The Upper Sco cluster is also relatively free of molecular gas, further undermining the possibility of recent star formation.

On the other hand, it may be that USco 104, 128, and 130 have not formed in isolation at all, but rather in accretion disks around some other Upper Sco members within the last million years, and have subsequently been ejected. This would explain their relative youth, as well as remove the necessity of postulating recent isolated star formation in Upper Sco. There are indeed other Upper Sco PMS objects in the vicinity of USco 104, 128, and 130, around which the latter three may originally have formed. However, formation in an accretion disk, allied with an age much less than the parent star, seems plausible only if these three objects have roughly planetary masses. We will return to this scenario in § 5.4.

In summary, we see that a real age spread in our Upper Sco sample appears largely unlikely but cannot be completely ruled out. To test whether such a spread is indeed responsible for the discrepancy between our results and the theoretical tracks, it is better to consider objects that are almost certainly strictly coeval, such as different components of a single stellar system. We thus proceed to analyze GG Tau Ba and Bb, the two M-type members of the quadruple GG Tau system in Taurus. Our reason for choosing this specific system is that it has been studied extensively by other investigators; in particular, WGRS99 have previously compared its components to various evolutionary tracks, providing a frame of reference for our present analysis. At any rate, if our results in this case once again differ from the theoretical predictions, mirroring the situation in Upper Sco, then a substantial age spread specific to Upper Sco cannot be readily invoked to resolve the disagreement, and an explanation must be sought elsewhere.

5.3. $T_{\text{eff}}$ and Gravity in GG Tau B: Implications for Age Discrepancies

Our method of $T_{\text{eff}}$ and gravity determination for GG Tau Ba and Bb is analogous to that adopted for Upper Scorpius. The complete analysis is presented in Appendix B, and the fits obtained, which are excellent, are shown in Fig. 11; here we only state the results. First, we find $T_{\text{eff}}$ for Ba and Bb to be ~2800 and 2600 K, respectively;23 these are ~200 K lower than the previous estimates by WGRS99, acquired through comparison with the BCAH98 tracks. Second, while our gravity for Ba ($\log g \simeq 3.4$), together with our derived $T_{\text{eff}}$, gives a plausible age of ~1 Myr for this object (within our ±0.25 dex uncertainty in $\log g$), our gravity for Bb ($\log g \simeq 3.1$) makes it seem much younger. Finally, even adopting the higher WGRS99 temperature for Bb does not bring it into agreement with the 1 Myr track (although it improves the situation somewhat). These findings are depicted in Figure 9.

Our GG Tau result, therefore, is completely analogous to our Upper Sco one: there is a drop in gravity as we move from an object hotter than ~2750 K to one that is significantly cooler, and this drop, not predicted by the theoretical evolutionary models for coeval bodies, causes the models to imply a much lower age for the cooler object.

We pause here a moment to contrast our results with those of WGRS99 (see Appendix B for details). The latter authors plot GG Tau Ba and Bb on the theoretical H-R diagram (luminosity vs. $T_{\text{eff}}$) predicted by the BCAH98 models and state that these models are consistent with coevality in the GG Tau system. At first glance, this seems to directly contradict our result that the BCAH98 (or equivalently, Lyon98/00) tracks are not commensurate with coevality. However, the WGRS99 study is not, strictly speaking, a test of the tracks, since they do not fix the $T_{\text{eff}}$ for Ba and Bb a priori. Instead, the temperatures are only constrained to a 400 K range, defined by the $T_{\text{eff}}$ in giants and dwarfs of the same spectral type as Ba and Bb. Hence, what WGRS99 really find is the following: assuming coevality, the Lyon98/00 tracks predict $T_{\text{eff}}$ for GG Tau Ba and Bb that appear reasonable, i.e., lie somewhere between the dwarf and giant temperature scales. Indeed, Luhan (1999) carries out an identical analysis (assume coevality in GG Tau, in conjunction with the Lyon98/00 tracks) to define a PMS $T_{\text{eff}}$ scale. Without better a priori constraints on the $T_{\text{eff}}$ of Ba and Bb, WGRS99 do not strictly test whether the Lyon98/00 tracks actually predict coevality.

Our analysis is analogous to that of WGRS99, albeit with gravity replacing luminosity as one of the two parameters in the HR diagram. The difference is that our $T_{\text{eff}}$ and gravity for Ba and Bb are fixed in advance, independent of the Lyon98/00 models. Consequently, ours is stringent test of the evolutionary tracks, to the extent that the $T_{\text{eff}}$ and $\log g$ we infer from spectral fitting are accurate. We find that, when confronted with our more precisely determined parameters for the two objects, the Lyon98/00 tracks no longer predict coevality.

Can Ba and Bb really have different ages? Most of the formation scenarios we considered earlier for Upper Sco (e.g., staggered star formation), which might lead to such age variations, are not applicable to GG Tau Ba and Bb, since they clearly belong to the same stellar system. However, we also raised the possibility that planemos formed later in an accretion disk may be much younger than the parent star. Can this explain the much lower age inferred for Bb from the Lyon98/00 tracks? It appears not; in Paper II, we derive a mass of ~0.03 M$_{\odot}$ for Bb (independent of theoretical tracks), comfortably higher than a planemo. So far, nobody has suggested that brown dwarfs in binaries form in accretion disks much later than the parent star: even if they form from accretion disk instabilities (Bate et al. 2002), the process probably occurs very early in the system’s life—both because

22 Notwithstanding the spectral typing uncertainties we have discussed earlier, there is not much doubt that the mid- to late-M stars in our sample are on average cooler than the early-M (and earlier) stars in the Preibisch study. In the early contraction phase, evolutionary models indicate (see Fig. 9) that objects of a given (low) mass descend roughly along Hayashi tracks, with $T_{\text{eff}}$ approximately constant or, as one moves deeper into the substellar regime, decreasing with time. At a given age, cooler objects are then less massive than hotter ones, and younger cooler objects less massive still.

23 More precisely, we find 2775 ± 50 K for Ba and 2575 ± 50 for Bb.
that’s when the disk is massive enough to be (gravitationally) unstable and also to ensure that there’s enough unaccredited disk material left to form the brown dwarf. Thus, large age differences between the two components of GG Tau B seem unlikely to arise from differences in formation history.

The fact that we find the same disagreement with the tracks in Upper Sco as well as in GG Tau—the coolest objects appear implausibly young—suggests that the same underlying mechanism is responsible in both. That is, we may reasonably rule out a real age spread that would affect Upper Sco alone (e.g., young interlopers from ρ Oph). The one remaining explanation is that the theoretical evolutionary tracks are somehow inaccurate for these very young low-mass objects. This would not be too surprising, as has been pointed out by the theoretical modelers themselves (Baraffe et al. 2002): the lower in mass and age one goes, the more suspect are the calculations (especially for objects which have essentially just formed). We thus turn to a discussion of evolutionary model uncertainties and whether they can credibly explain our results.

5.4. Evolutionary Models Uncertainties

Baraffe et al. (2002) have recently discussed various sources of uncertainty in current theoretical evolutionary models for very young, low-mass PMS objects. The three most egregious ones they identify are the choice of initial conditions, accretion effects, and the treatment of interior convection. To this we will add uncertainties in deuterium-burning conditions. Let us examine initial conditions first.

In current evolutionary models, the calculations are begun at (i.e., a time \( t = 0 \) is assigned to) some specified point during the initial, fully convective, quasi-hydrostatic contraction phase of low-mass stars and substellar objects. The choice of this starting point is at present somewhat arbitrary; however, it obviously affects the model age (defined as time elapsed since \( t = 0 \)) implied for an object with an observed set of physical conditions: if the calculations are begun earlier in the contraction phase, the implied age will be larger. This uncertainty is nicely illustrated by Baraffe et al. (2002) through a comparison of models with varying initial gravities (for a given mass). Can this effect be responsible for our results?

The initial conditions assumed in the Lyon98/00 models are as follow. For objects with mass \( \geq 0.03 M_\odot \), the calculations begin at the point where deuterium (D) fusion starts; for lower masses, they begin at \( \log g = 3.5 \) (I. Baraffe 2003, private communication; see also Baraffe et al. 2002). Note in this context that, in the Lyon models, D fusion begins at \( \log g \sim 3.5 \) in a 0.1 \( M_\odot \) object, at \( \log g \sim 3.75 \) in a 0.03 \( M_\odot \) object, and at \( \log g \sim 4.0 \) in a 0.02 \( M_\odot \) object. Moreover, in this mass range, D burning lasts roughly from 1 to 15 Myr, with the fusion timescale increasing with lower mass (Chabrier et al. 2000a). During fusion, \( T_{\text{eff}} \) and luminosity remain practically constant (i.e., this is the “deuterium main sequence”); hydrostatic contraction resumes once the deuterium is exhausted. Objects less massive than about 0.012 \( M_\odot \) (12M_\odot), on the other hand, are below the minimum D-burning limit: they never achieve D fusion or halt in their contraction (until core degeneracy sets in much later). Given these considerations, we can estimate the errors in age in the Lyon models, as follows.

The Kelvin-Helmholtz contraction timescale (\( t_{KH} \)) applicable to our objects before D fusion begins, is \( (3GM^2_\odot/7R_\odot) / (4\pi R^4 \sigma T^4_{\text{eff}}) \) (valid for fully convective objects). In our case, where gravity and \( T_{\text{eff}} \) are the observables and the masses, gravities, and \( T_{\text{eff}} \) are low, it is profitable to express it as

\[
t_{KH} \approx 2 \left( \frac{g}{10^{3.5} \text{ cm s}^{-2}} \right)^{3/2} \left( \frac{M_*}{0.03 M_\odot} \right)^{1/2} \left( \frac{T_{\text{eff}}}{2700 \text{ K}} \right)^{-4} \text{ Myr.}
\]

(1)

Now, equation (1) is only applicable at a given instant in time; to make use of it, we need to connect it to the real age \( \tau \) of an object, where \( \tau \) is defined as the time it takes to contract from an infinite (i.e., relatively very large) radius to its present size. This is easily done if contraction (at any given mass) can be assumed to proceed at roughly constant \( T_{\text{eff}} \) (as seems approximately true for the masses considered here; Baraffe et al. 2002). Then, with equation (1), \( t_{KH} \equiv R/(dR/d\tau) \) can be simply integrated to find (Hartmann 1998)

\[
\tau \approx \frac{t_{KH}}{3},
\]

(2)

where \( t_{KH} \) is the present Kelvin-Helmholtz contraction timescale.\(^{24}\) Equations (1) and (2) capture the essential physics entering the current evolutionary models during the early, pre-D-fusion contraction phase of low-mass objects, although factors such as the precise treatment of convection can modify the results somewhat (mainly by affecting \( T_{\text{eff}} \) and its variations during collapse; see Baraffe et al. 2002). They can thus be used to form a rough, internally consistent estimate of the age errors in the models arising from the choice of initial conditions.

According to the Lyon models, the \( T_{\text{eff}} \) at which 0.1, 0.03, and 0.02 \( M_\odot \) objects collapse are \( \sim 3000, 2700, \) and 2500 K respectively. In that case, from equation (1) and (2), all three reach \( \log g = 3.5 \) at \( \tau \approx 0.7 \) Myr, i.e., about a million years after beginning collapse from some very much larger initial radius. Moreover, a 0.03 \( M_\odot \) object reaches its D-burning phase (\( \log g \sim 3.75 \)) at \( \tau \approx 1.5 \) Myr. Thus, the 1 Myr isochrone in Figure 9 should actually run roughly parallel to the \( T_{\text{eff}} \) axis, at \( \log g \approx 3.5 \), instead of rising to \( \log g \sim 3.75 \) by 0.03 \( M_\odot \). By adopting their stated initial conditions, the Lyon isochrones make very low-mass objects, which are truly about 1 Myr old, appear too young by 1–1.5 Myr. By \( \tau \approx 2 \) Myr, however, the isochrone should no longer be a horizontal line. Now a 0.1 \( M_\odot \) object has already begun fusing deuterium (indeed, is nearing the end of its D-burning phase) and so remains at nearly the same conditions (\( \log g, T_{\text{eff}} \)) as at 1 Myr. However, 0.03 and 0.02 \( M_\odot \) bodies have contracted to \( \log g \approx 3.75 \) (which is the beginning of D burning for 0.03 \( M_\odot \)). Thus, the 2 Myr isochrone should closely resemble the curved Lyon 1 Myr track shown in Figure 9 (and the 3 Myr isochrone should look like the Lyon 2 Myr track and so on). In summary, the initial conditions adopted in the Lyon models produce (1) a general underestimation of age by \( \sim 1 \) Myr and (2) a significant overestimation of gravity (by \( \sim 0.25 \) dex) for 1 Myr old objects with mass \( \lesssim 0.03 M_\odot \). These results quantify the initial condition effects shown in Baraffe et al. (2002) and are vital for very low-mass, very young (1–few Myr old) objects.

\(^{24}\) Which initial radius contraction begins at is immaterial in the following sense: the integration produces a \( 1/R^3(\tau=0)\) term, in which the \( 1/R^3(\tau=0) \) part can be ignored as long as initial radius \( R(\tau=0) \) is simply much larger than the current radius \( R(\tau) \). In other words, the contraction timescale decreases very rapidly with increasing radius, so the time spent at the largest radii adds negligibly to the final age.
However, the above age (or gravity) offsets can account only marginally for our GG Tau results, and not at all for our Upper Sco ones. The gravities we derive for Ba and Bb are \( \log g \approx 3.375 \) and 3.125, respectively, while in Paper II, we derive masses of \( \sim 0.12 \) and 0.03 \( M_\odot \), respectively. Our formulae above then imply an age of \( \sim 1 \) Myr for Ba, but only 0.2 Myr for Bb. Even accounting for our uncertainty of \( \pm 0.25 \) dex in gravity (and the corresponding factor of 1.8 in mass) can push the age of Bb up to only 0.5 Myr. Furthermore, the \( \sim 1 \) Myr age from Ba is probably only a lower limit, since it has begun fusing deuterium by 1 Myr and thus remains at the same gravity and \( T_{\text{eff}} \), without contracting, till \( \sim 2 \) Myr.25 Thus, even under the best of circumstances, our gravity determinations yield an age difference of at least 0.5 Myr between Ba and Bb. It is not clear whether this age difference is admissible in current star/brown dwarf formation scenarios, for objects in the same system.

The situation is even more extreme in Upper Sco. For the objects with derived gravity of 3.75–4.0 (see Fig. 9), the ages inferred from equations (1) and (2) are \( \sim 3–5 \) Myr, in good agreement (within 1 Myr) with both the isochronal ages implied by the Lyon tracks (Fig. 9) and the expected age of Upper Sco. However, we derive \( \log g \approx 3.25 \) for USco 128 and 130, and a mass of only \( \sim 9M_\oplus \)–14\( M_\oplus \); this yields an age of merely \( \sim 0.3 \) Myr for these two objects. Even including the \( \pm 0.25 \) dex and factor of 2 uncertainty in our gravity and mass respectively (which gives a mass upper limit of \( \sim 20M_\oplus \)–30\( M_\oplus \), similar to the value found by AMB00 for USco 128), still implies an age of at most \( \sim 0.7 \) Myr (i.e., close to that of GG Tau Bb). Thus the age differential with the rest of Upper Sco seems to be of order 3–5 Myr.

These results can be summarized thus. A simple \( f_{\text{KH}} \) prescription, which encapsulates the evolutionary model calculations at early times (in the absence of D fusion), implies that all objects with mass \( \lesssim 0.1 \) \( M_\odot \), should have \( \log g \geq 3.5 \) dex by an age \( \geq 1 \) Myr. However, our lowest gravity bodies, presumably of age \( \gtrsim 1 \) Myr, have \( \log g \) lower than or marginally consistent with 3.5 dex. This produces age discrepancies in our sample that increase with estimated cluster age. If our lowest gravities are accurate, then somehow the contraction of these objects must be slowed down in an as yet unaccounted for manner.

One possibility is through accretion. As shown by Hartmann et al. (1997), strong accretion can retard the contraction if the thermal energy of the accreted material can provide the luminosity otherwise supplied through gravitational contraction. However, this requires that the incoming matter not radiate away all its excess energy before it has a chance to become well mixed into the interior and contribute to the object’s internal energy. Even assuming that such mixing can occur efficiently in our objects, one still requires that accretion is either ongoing or has ended only in the very recent past. Otherwise, since the Kelvin-Helmholtz timescales at the lowest gravities we find are very short (\( f_{\text{KH}} \approx 0.5 \) Myr), the objects would already have contracted to higher gravities. However, GG Tau Bb, USco 128 and 130 do not show any overt signs of accretion. For Bb, White & Basri (2003) can only find an upper limit to any accretion rate, at \( 10^{-10.5} M_\odot \) yr\(^{-1} \). Similarly, the high-resolution spectra of USco 128 and 130 do not indicate any substantial ongoing accretion (JMBO2; USco 128 also does not have any detectable millimeter emission, ruling out more than a few Earth masses of surrounding dust, and thus (presumably) any massive accretion disk (Klein et al. 2003). On the other hand, at least two components of the GG Tau system, Aa and Ab, have substantial accretion disks, and thus a small amount of ongoing accretion cannot be ruled out for Bb. Similarly, USco 128 does have a significant near-infrared excess indicating some disk material (Jayawardhana et al. 2003); while 130 does not show any near-infrared excess, the difficulty in detecting such excess in brown dwarfs suggests that an accretion disk is not completely implausible in this case either. Consequently, while there seems to be only a slim chance that contraction in these objects has been halted through accretion, the possibility cannot yet be eliminated; it needs to be checked through further observations.

A second, perhaps more attractive possibility is that D-burning begins earlier than the Lyon models anticipate. Imagine that for masses \( \lesssim 0.1 \) \( M_\odot \), D fusion really starts somewhere in \( \log g \approx 3.25–3.5 \) range: consistent with the lowest \( \log g \) values we derive, and lower by 0.25–0.5 dex than the D-burning gravities implied by the Lyon models for these masses. Then the positions of our Taurus and Upper Sco objects on the \( T_{\text{eff}} \)-gravity plane (Fig. 9) can easily be understood, without doing violence to the previously estimated ages of these clusters or requiring any age-spread within each cluster. We first outline how this scenario would explain our results, and then discuss its likelihood.

Consider GG Tau first. We suggest that the system is indeed \( \sim 1–2 \) Myr old, and D fusion has begun in both Ba and Bb. Then, since the fusion timescale at \( \sim 0.03 \) \( M_\odot \), is close to 5 Myr, the age derived for Bb from a \( f_{\text{KH}} \) formulation is only a lower limit on its true age. Its position on the \( T_{\text{eff}} \)-gravity plane actually indicates the conditions at which fusion is initiated; Bb will continue to remain there until deuterium is exhausted. The fusion timescale for Ba (\( \sim 0.1 \) \( M_\odot \)), however, is only about 1 Myr, so it may either be coming to the end of its D-burning phase or just past it. Its position then indicates either its fusion conditions or a slight subsequent contraction over less than 1 Myr since the end of fusion.26

Similarly, we suggest that our higher mass Upper Sco objects have all finished burning deuterium at \( \sim \log g \) of 3.25–3.5 and rapidly contracted subsequently to their observed gravities by the age of Upper Sco, USco 104 has just finished its fusion and contracted slightly less in the remaining time, and USco 128 and 130 are still in their D-burning phase. With regard to timescales, this scenario is possible because (1) the age of Upper Sco is expected to be \( \sim 5 \) Myr; (2) the D-burning timescale very quickly increases with decreasing mass, going from \( \lesssim 5 \) Myr for masses \( \gtrsim 0.03 \) \( M_\odot \), to more than 50 Myr for objects at the D-burning limit (\( \sim 0.012 \) \( M_\odot \))—this allows higher mass brown dwarfs to deplete deuterium over the lifetime of Upper Sco while lower mass ones continue fusion; and (3) the contraction timescale at \( \log g \) of 3.5–3.25 is very short, so even if D fusion happens at these gravities, objects that have finished fusion will very rapidly reach higher

\(^{25}\) Fig. 9 indicates that D burning has not yet begun in Ba, given its \( \log g \) and \( T_{\text{eff}} \). However, our mass for Ba (0.12 \( M_\odot \); Paper II) is higher than Fig. 9 implies; this is simply because we (mostly) find a given mass to be cooler (by \( \sim 200 \) K) than the Lyon models suggest (Paper II). If Ba is at 0.12 \( M_\odot \), it should indeed be in the D fusion phase by an age \( \sim 1 \) Myr (as seen by simply sliding Ba to the left by 200 K in Fig. 9).

\(^{26}\) For example, if D-fusion in Ba begins at \( \log g \approx 3.25 \), it would take Ba \( \sim 0.5 \) Myr to gravitationally contract to that point; it would remain there, burning D, for another 1 Myr, and then contract to \( \log g \approx 3.5 \) (consistent with our derived \( \log g \) after a further 0.5 Myr, bringing its total age to \( \sim 2 \) Myr (as expected for Taurus).
gravities (starting at \( \log g = 3.25-3.5 \), it only takes less than 2 Myr to contract to \( \log g = 3.75 \), and less than 4 Myr to reach \( \log g = 4.0 \)). Notice that a decrease in gravity, in going from objects more massive than about 0.03 \( M_J \), to less massive ones, is actually seen in the 10 Myr isochrone in Fig. 9, for exactly the same reasons we describe here: the higher masses have finished D burning and subsequently contracted somewhat, while the lower masses are still stuck in the D-fusion phase. However, the gravity change is much less dramatic than in our proposed scenario, simply because the contraction timescales are much longer at the higher gravities (compared to those in our scenario) at which D fusion occurs in the Lyon models.

Of course, this hypothesis can be contemplated only if USco 128 and 130 are above the D-burning minimum mass. We derive \( \sim 9 M_J - 14 M_J \) for them (Paper II), which is very close to the current theoretical D-fusion boundary of \( 12 M_J \) (as Saumon et al. [1996] point out, the value of this limiting mass has proved rather robust in the face of various theoretical improvements over the years). Moreover, our mass errors are about a factor of 2, so it is very plausible that USco 128 and 130 are capable of initiating D fusion.

The more important issue is whether current theoretical uncertainties can accommodate D fusion at a lower gravity. Given the highly complicated nature of ion/electron screening in the D-fusion calculations, especially at the lowest masses (Saumon et al. 1996), as well as remaining uncertainties in the interior structure (also exacerbated with decreasing mass), this scenario does not seem infeasible and is worth examining in future evolutionary models.

We also point out a crucial prediction of our hypothesis that D fusion might occur at lower-than-expected gravities. Objects with mass below the D-fusion boundary should not halt in their contraction due to nuclear burning; consequently, their gravities should be much higher, at ages up to a few tens of megayears, than those of the lowest mass brown dwarfs still in their fusion phase. As a result, there should be a sharp trough in the \( T_{\text{eff}} \)-gravity plane near the D-burning limit in young clusters, with objects at \( T_{\text{eff}} \) lower than the trough value certain to have planetary masses. The situation is somewhat analogous to the lithium-depletion boundary in the brown dwarf regime. This would be an exciting development if true. While the spectral signatures of deuterium are very hard to detect directly with current technology (Chabrier et al. 2000a), the spectral signatures of low/high gravity are much easier to decipher (as we have demonstrated in this paper); this would offer a clean way of identifying planetary mass objects in young clusters. Of course, this possibility needs to be carefully checked through further observations and D-fusion calculations, as noted above.

Baraffe et al. (2002) also examine uncertainties in the treatment of convection. Basically, at very low gravities (\( \log g \leq 3.5 \)), the deep atmosphere has extended superadiabatic layers (due to the suppressed production of \( H_2 \), and hence lower \( H_2 \) CIA opacity, at such gravities). As a result, the atmospheric \( P-T \) profile becomes very sensitive to the precise value of the mixing-length parameter \( \alpha \). This in turn affects the evolutionary models, which use the structure of the deep atmosphere as an outer boundary condition. At higher gravities, \( H_2 \) is produced efficiently, convection becomes essentially adiabatic, and the dependence on \( \alpha \) becomes negligible. As noted earlier, our synthetic spectra (for which the deep atmosphere is an inner boundary condition) use \( \alpha = 2 \), which agrees with the value indicated by the latest three-dimensional hydrodynamical simulations, while the Lyon models shown use \( \alpha = 1 \). However, Baraffe et al. (2002) have illustrated the effect of using \( \alpha = 2 \) atmospheres. At first glance, the attendant changes in the evolutionary tracks do not seem to improve the discrepancy in gravity between our measured values and the predicted ones for the coolest objects, since the influence of the mixing-length parameter is seen to mostly vanish by an age \( \geq 1 \) Myr. However, Montalban et al. (2004) have pointed out shortcomings in the mixing-length treatment of convection adopted in the Lyon89/00 models, arising from superadiabaticity effects. Montalban et al. have so far examined only hotter, more massive objects (\( T_{\text{eff}} > 4000 \) K), so the situation in the cool, low-mass regime is unclear. Moreover, as we point out above, the results of Baraffe et al. (2002) suggest that superadiabatic layers do not last much longer than \( \sim 1 \) Myr in our targets. Nevertheless, Baraffe et al.’s calculations were undertaken within the mixing-length framework. It remains to be seen whether the effects pointed out by Montalban et al., when applied to the \( \leq 1 \) Myr evolutionary stage of our targets (when superadiabaticity is important, even in the Baraffe et al. models), can produce changes to the evolutionary tracks that continue to be evident at ages greater than a million years. Certainly, at the gravities we find for our coolest targets, superadiabatic layers are expected. These issues must be considered in detail in future evolutionary models.

Finally, we point out that the Lyon98/00 tracks make use of an older generation of synthetic spectra than we employ here, with quite significant differences in opacity. In general, one should have a relatively small effect on the isochrones, since the time evolution of \( T_{\text{eff}} \) and luminosity is expected, in these low masses, to be a very weak function of opacity \( [L(t) \propto \kappa_R^{-1/3}, T_{\text{eff}}(t) \propto \kappa_R^{-1/10}] \); Burrows & Liebert 1993]. Nevertheless, it would be fruitful to construct new evolutionary models based on the latest opacities, to quantify any resultant change in the isochrones.

6. CONCLUSIONS

The primary conclusion of this paper is that it is quite feasible to derive fairly precise (0.25 dex) gravities in low-mass stellar and substellar objects. This can be accomplished with spectra of moderate S/N and high resolution (which generally require 8 m class telescopes), along with the most advanced model atmosphere and spectral calculations. If one performs this for objects whose radii can be found (this generally requires reasonably precise distances and photometry), then masses can be found well enough to distinguish planemos, brown dwarfs, and stars (see Paper II). Along with the gravity, we obtain a good effective temperature (\( \pm 50 \) K), which facilitates the conversion of a luminosity to a radius.

The basic reason for our success is that TiO is a spectral diagnostic that is strongly dependent on temperature and weakly dependent on gravity (and with the opposite gravity dependence of our atomic line diagnostics). Our gravity diagnostics are both subordinate and resonance neutral alkali lines (of potassium and sodium). They have both a temperature and gravity dependence and yield degenerate solutions in the two parameters. We therefore rely on TiO to break the temperature degeneracy, and the alkali lines then provide a gravity. We note that there are a number of other alkali lines that we have not yet employed (other lines of potassium and sodium, plus lines of rubidium, cesium, and lithium), which cover a range of wavelengths and have different strengths for different stellar temperatures. In the L dwarfs, a substitute for the TiO temperature diagnostic must be found (since TiO has condensed into dust). The metal hydride molecules (FeH and
CrH) are the obvious candidates. Properly developed, our methodology should work well over the range of substellar objects from mid-M through L (which encompass a range of masses from the planetary to stellar domains, depending on age). Indeed, once theoretical tracks have been properly computed and calibrated, one might be able to directly infer age as well (in principle).

Having applied our methodology to very young, low-mass objects in the Upper Scorpius and Taurus star-forming regions, we find (1) a good agreement between our gravities and the theoretical ones for most of our sample but (2) a significant discrepancy between the two for our coolest targets. We show that even without detailed comparison against model spectra, the data themselves suggest a sharp fall-off in gravity in the coolest objects. We have examined various processes and synthetic spectral uncertainties which might lead us to infer erroneous gravities (e.g., dust, cool spots, metallicity variations, and inadequacies in the model treatment of collisional broadening) and found that they are unlikely to give rise to the spectral effects we see: real gravity variations are indicated. Theoretical tracks would interpret this range of gravities as a range of ages, and we provide several arguments against that interpretation. The alternative is that the theoretical tracks are allowing the very low-mass objects to contract too quickly; the gravities we measure for them are lower than predicted. We discuss various ways in which this could happen and suggest remaining uncertainties in the model treatment of accretion, D-burning, and/or convection are most likely responsible. This means that the interpretation of masses and ages from isochrone analysis in young clusters is problematic at the moment for very low-mass bodies. Nonetheless, we show in Paper II that the interpretation of the faintest of these objects as low-mass brown dwarfs or planetary mass objects looks correct.

Finally, we point out that our spectral analysis is carried out in the optical, but it could potentially be accomplished at other wavelengths as well. In particular, the near-IR would be very interesting to explore. Such investigations have already begun: Doppmann & Jaffe (2003) and Doppmann et al. (2003) present a similar high-resolution study in the near-IR for higher mass, hotter PMS objects, while Gorlova et al., (2003) examine near-IR PMS substellar spectra, albeit at low-resolution. A high-resolution analysis of cool, very low-mass PMS objects would be extremely fruitful, especially for probing the youngest, most extincted bodies; we have recently embarked on a project to accomplish this.

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APPENDIX A

DUST EFFECTS

Here we investigate dust formation in our PMS sample by comparing their spectral properties to those of field M dwarfs of similar type. The M dwarfs chosen are Gl 406 (M6 V), VB 8 (M7 V), VB 10 (M8 V), and LHS 2924 (M9 V), all well-known spectral standards for their types. In these stars, later type is supposed to correlate well with decreasing $T_{\text{eff}}$ (e.g., Jones & Tsuji 1997). In order to isolate $T_{\text{eff}}$-related dust effects as much as possible, we have chosen stars likely to have very similar metallicities and gravities. Spectral analyses indicate that all four are consistent with solar metallicity (Leggett et al. 2000, 1998; Schweitzer et al. 1996). Gravity is constrained by the fact that these are all main-sequence dwarfs belonging kinematically to the old disk population (Leggett 1992; corresponding, at least in a statistical sense, to ages $\geq 3$ Gyr). This largely precludes their being young low-gravity objects still in the contraction phase. The BCAH98 and CBAH00 evolutionary models (expected to be quite accurate for older MS dwarfs, notwithstanding any uncertainties in the PMS stage; e.g., Segransan et al. 2003) indicate that masses between $\sim 0.08$ and $0.3~M_\odot$ (which adequately cover the expected range for M6–M9 MS dwarfs) all have $\log g \sim 5.0$, spanning at most $\sim 0.25$ dex, by a few gigayears. The rough gravities derived so far from spectral syntheses of these objects (Leggett et al. 1998, 2000; Schweitzer et al. 1996) are also consistent with minimal gravity variation. At any rate, since $T_{\text{eff}}$ is expected to be primarily responsible for determining the spectral type ordering of these dwarfs, and since their spectral effects considered below do change quasi-monotonically (increasing, then decreasing) with type, we can safely assume we are tracking $T_{\text{eff}}$-related effects, and ignore any small gravity or metallicity variations in our qualitative analysis here. Finally, we can ignore $v\sin i$ effects: VB8, VB10 and LHS 2924 all have comparable $v\sin i$ ($6$–$10$ km s$^{-1}$), and we have artificially broadened Gl 406 (intrinsically less than $3$ km s$^{-1}$) to $7$ km s$^{-1}$ to match the others.

In Figure 10 we show three spectral regions in the M dwarfs—the triple-headed TiO band at $\sim 8440$ Å (same region used for our PMS $T_{\text{eff}}$ analysis), the TiO bands at $\sim 7050$ Å, and the Na i doublet at $\sim 8200$ Å (same region used for PMS gravity analysis). Three effects are immediately apparent: (1) the $8440$ TiO bands increase monotonically in strength with decreasing temperature, from M6 V to M8 V, and then reverse strength at still lower $T_{\text{eff}}$, becoming weaker by M9 V; (2) the $7050$ TiO bands show a similar behavior, but reverse strength at an earlier spectral type (M8 V), i.e., at a higher $T_{\text{eff}}$, than the $8440$ bands; and (3) the Na i doublet behaves analogously to the $7050$ bands, reversing strength by M8 V and becoming weaker with still later type (lower $T_{\text{eff}}$). These effects can be understood through $T_{\text{eff}}$-dependent dust formation. Initially, no dust forms, while the abundance of TiO and Na i increases with decreasing $T_{\text{eff}}$, making their lines stronger with later type. As $T_{\text{eff}}$ continues to decrease, dust begins to form, simultaneously depleting TiO from the gas phase (since TiO becomes sequestered in grains) and increasing the continuum opacity. Consequently, the TiO absorption bands and the Na i doublet now weaken with later type. Moreover, dust opacity increases with shorter wavelength. As a result, its effects are manifested first (i.e., at an earlier type, or higher $T_{\text{eff}}$) in the bluer TiO bands at...
Fig. 10.—Dust effects in field M dwarfs, compared to USco sample. Top left: Comparison of 8440 Å TiO bands in a spectral sequence of M dwarfs. Top right: Comparison of 7550 Å TiO bands in the same M dwarfs. Bottom left: Comparison of Na i doublet in the same M dwarfs. Bottom right: Comparison of 7050 Å TiO bands in our PMS sample. With increasing dust opacity, the M dwarfs first show a reversal in the strength of the 7050 TiO bands and Na i doublet, and, at later spectral types (i.e., lower $T_{\text{eff}}$), in the 8440 Å TiO bands. No such reversal in the 7050 bands is apparent in our PMS sample. See § 4.3.1 and Appendix A.
7050 Å, and only later in the redder bands around 8440 Å. Qualitatively, one might expect Na, occurring at an intermediate wavelength (8200 Å), to be affected at an intermediate spectral type/$T_{\text{eff}}$; our analysis here shows that it follows the behavior of the 7050 Å TiO bands more closely. Finally, since dust appears in the 7050 bands before it does in the 8440 ones, the magnitude of the reversal in the former is larger than in the latter at a given spectral type/$T_{\text{eff}}$; e.g., by the time the 8440 bands reverse around M9 V to become weaker than at M8 V, the 7050 bands are already much weaker than at M8 V (Fig. 10).

Turning now to our PMS objects, we have already illustrated the behavior of their 8440 TiO bands and Na doublets in earlier sections. In Figure 10 we plot the trend in their 7050 TiO bands as $T_{\text{eff}}$ decreases. Note that our $T_{\text{eff}}$ are derived from the 8440 bands assuming no dust, so decreasing $T_{\text{eff}}$ actually means increasing strength in the latter bands. We see that, as our derived $T_{\text{eff}}$ declines, the 7050 band strength either remains roughly constant, or increases (the reason for this variable increase in strength is discussed shortly). Most importantly, this TiO band shows no reversal with lower $T_{\text{eff}}$, even in those objects with anomalously weak Na. This implies that our ordering of objects by $T_{\text{eff}}$ is correct and that dust is unimportant in our PMS sample and cannot explain our Na results.

To see this, consider USco 55, 104, and 130. As discussed in the main text, the Na doublet in USco 130 is slightly weaker, and in 104 much weaker, than in USco 55; meanwhile the 8440 TiO bands increase steadily in strength from USco 55 to 130 (Figs. 6 and 8). This is surprising at first, since deeper 8440 bands usually imply lower $T_{\text{eff}}$, and Na should strengthen with decreasing $T_{\text{eff}}$. However, our M dwarf analysis above shows that burgeoning dust opacity can make the Na lines weaker with declining $T_{\text{eff}}$, even as the 8440 bands continue to deepen; the question is whether this is what is happening in our PMS objects. We do not think so, based on the 7050 TiO results. The M dwarf spectra reveal that the latter bands should show a strong reversal when dust produces a reversal in Na, even if no dust effect is apparent in the redder 8440 bands. The fact that we see no weakening at all of the 7050 bands in USco 104 and 130 compared to 55—these bands are about the same strength as in USco 104 and 55, and stronger in 130—argues convincingly that dust is not responsible for the Na behavior in our PMS objects.

Finally, it is also interesting that the 7050 bands in USco 104 are about the same strength as in 55. Of course, this may simply be because their $T_{\text{eff}}$ are so similar: perhaps the 7050 bands are not as sensitive to a small $T_{\text{eff}}$ change as the 8440 ones. However, we suggest that gravity may play a role as well. To illustrate this clearly, we compare the behavior of 104 to that of USco 109 (same $T_{\text{eff}}$ as 104, but significantly higher gravity; Table 1), and USco 112 (significantly higher $T_{\text{eff}}$ than 104 and 109, but the same gravity as 109; Table 1). In Figure 10 we see that the 7050 bands in 109 are deeper than in 112, as expected from their $T_{\text{eff}}$ difference (derived from the 8440 bands). However, while the 7050 bands in 104 are also slightly deeper than in 112, the difference is smaller than between 109 and 112 (Fig. 10). Since 109 and 104 appear to have exactly the same $T_{\text{eff}}$ (i.e., indistinguishable 8440 bands; not shown), this suggests that there is some other factor distinguishing the two; their disparity in gravity is the obvious choice (they also differ by ~8 km s$^{-1}$ in $v \sin i$, but tests show that this has negligible effect on the depth of the strong 7050 bands). In fact, our synthetic spectra also indicate that lower gravity, at a given $T_{\text{eff}}$, causes the 7050 bands to weaken slightly. In other words, while the behavior of the observed 7050 TiO bands strongly suggests no dust formation in our PMS sample, it does support the gravity variations we have deduced earlier.

APPENDIX B

GG Tau: $T_{\text{eff}}$ AND GRAVITY

GG Tau is a PMS quadruple system in the Taurus-Aurigae star-forming region ($D = 140$ pc). It is a hierarchical system composed of two binaries: GG Tau A and GG Tau B. The two components of the first, Aa and Ab, are separated by ~0"25 (~35 AU); the two components of the second, Ba and Bb, are separated by ~1\'48 (~207 AU). The separation between the two binary systems is ~10\'1 (~1414 AU). A circumbinary disk is also observed around GG Tau A (e.g., Guilloteau et al. 1999).

WGRS99 find spectral types of K7 ±1 and M0.5 ± 0.5 for Aa and Ab, respectively, and M5 ± 0.5 and M7 ± 0.5 for Ba and Bb. High-resolution spectra of the GG Tau A system show low levels of continuum excess, or veiling, indicating some ongoing accretion in this binary (Gullbring et al. 1998). In GG Tau B, however, WGRS99 detect no accretion-induced continuum excess in either component; they infer an upper limit of $10^{-9} M\odot$ yr$^{-1}$ for the accretion rate in both Ba and Bb. They also find a $v \sin i$ of 9 ± 1 km s$^{-1}$ in Ba, and 8 ± 1 km s$^{-1}$ in Bb. In a later detailed analysis, Luhan (1999) find M5.5 for Ba and M7.5 for Bb. Still more recently, White & Basri (2003) derive spectral types of M6 and M7.5, and $v \sin i$ of 8.1 ± 0.9 and 6.6 ± 2.0 km s$^{-1}$, for Ba and Bb, respectively. They also put more stringent upper limits on any possible accretion, at less than $10^{-9.9}$ and $10^{-10.3} M\odot$ yr$^{-1}$ for Ba and Bb.

The four components of GG Tau are very likely to be coeval, as WGRS99 argue. Using this fact, they estimate the age and component masses of the system, in the following manner. Extinctions are found for the four components using the derived spectral types and comparing the optical and near-infrared colors to those of field dwarf spectral standards. Luminosities are then determined by applying bolometric corrections to the dereddened photometric magnitudes. Values of $T_{\text{eff}}$, however, are not precisely derived a priori, but assumed to be intermediate between those of giants and dwarfs of the same spectral types (the rationale for this is discussed shortly; note also that WGRS99 adopt the dwarf $T_{\text{eff}}$ scale of Leggett et al. [1996], which is noteworthy for our discussion further on). At the K7–M0.5 types of Aa and Ab, the dwarf and giant $T_{\text{eff}}$ are nearly identical, so the $T_{\text{eff}}$ of these two components is essentially “fixed.” At the later types of Ba and Bb, however, the dwarf and giant scales diverge, and thus the $T_{\text{eff}}$ of these two is only constrained to a rather broad range of ~400 K. WGRS99 then compare these luminosity and $T_{\text{eff}}$ estimates to the predictions of the theoretical evolutionary tracks constructed by various groups. In all the different models examined, a unique isochrone can be found that simultaneously fits Aa and Ab; i.e., all the models successfully predict the coevality of these two stars. Not all, however, are capable of also fitting Ba and Bb with the same track. That is, using the track that fits Aa and Ab, many of the models predict $T_{\text{eff}}$ for Ba and/or Bb that are outside the assumed “acceptable” range (delimited by the dwarf and giant $T_{\text{eff}}$ scales). WGRS99 use this fact to distinguish between the different models. They find that the BCAH98 models (Lyon98/00 in our
We have checked the values we quote here against the Lyon98/00 models directly, for the masses found by WGRS99.

We adopt log $T_{\text{eff}}$ of 3.5, 2650 K can be excluded. Bottom row: Same, but for Bb. Both log $g = 3.00$, $T_{\text{eff}} = 2550$ K and log $g = 3.25$, $T_{\text{eff}} = 2600$ K models are good fits to all the Bb spectral regions shown. We adopt log $g = 3.125$, $T_{\text{eff}} = 2575$ K. We also show that log $g = 3.50$, 2650 K is a poor fit to TiO (although it is a good fit to the K $i$ doublet; not shown). Consequently 3.5, 2650 K can be excluded.

Barnes et al. (1998) nomenclature) are to be preferred, since these predict $T_{\text{eff}}$ for Ba and Bb that are commensurate with the $T_{\text{eff}}$ range assumed for the latter. Thus, the BCAH98 models are consistent with the coevality of all four components of GG Tau, but only within the broad $T_{\text{eff}}$ range assumed for Ba and Bb. Indeed, WGRS99 finally adopt, for Ba and Bb, the $T_{\text{eff}}$ implied by the BCAH98 models themselves; this is essentially assuming coevality to determine $T_{\text{eff}}$ (Luhman [1999] explicitly uses this procedure to define a PMS $T_{\text{eff}}$ scale), under the sole constraint (apart from known luminosity) that the $T_{\text{eff}}$ so derived falls within a wide range of acceptable values. Whether BCAH98 models actually predict coevality when $T_{\text{eff}}$ is better constrained is not addressed by WGRS99 (as distinct from our analysis, which attempts to rigidly restrict $T_{\text{eff}}$ before comparing to model tracks).

The WGRS99 comparison to BCAH98 models yields an age of 1.5 Myr for the GG Tau system and masses of $0.38 \pm 0.10$, $0.68 \pm 0.03$, $0.12 \pm 0.02$, and $0.044 \pm 0.006$ $M_\odot$ for Aa, Ab, Ba, and Bb. For Ba and Bb, the $T_{\text{eff}}$ implied by the BCAH98 tracks are 3050 and 2820 K, and the gravities are log $g = 3.75$ and 3.65, respectively. WGRS99 note that the Ba is then $\sim 40$ K hotter than an M5 dwarf, while Bb is $\sim 140$ K hotter than an M7 dwarf (using dwarf temperatures from Leggett et al. [1996, hereafter L96]).

We have derived $T_{\text{eff}}$ and log $g$ for Ba and Bb using HIRES optical spectra kindly supplied to us by R. White. Unfortunately, the spectrograph setting used by White excludes the Na $i$ doublet, as well as the blue component of the K $i$ doublet, although it does include the TiO order we have used for our Upper Sco sample. However, in the very high S/N spectrum obtained by R. White, even the single component of the K $i$ doublet in the spectra turns out to be capable of adequately constraining the gravity, while the TiO order, as before, is an excellent $T_{\text{eff}}$ indicator. In Figure 11 we plot our synthetic fits to the data. The fits obtained are evidently remarkably good. For GG Tau Ba, we are unable to distinguish between log $g = 3.25$, $T_{\text{eff}} = 2750$ K and log $g = 3.50$, $T_{\text{eff}} = 2800$ K. We thus adopt the average, log $g = 3.375$, $T_{\text{eff}} = 2775$ K, with errors of $\pm 0.25$ dex and $\pm 50$ K, respectively. Similarly for Bb, we obtain log $g = 3.125 \pm 0.25$ dex, $T_{\text{eff}} = 2575 \pm 50$ K.

The comparison between our results and the Lyon98/00 models have been presented in § 5.3. Here we briefly discuss our differences with the $T_{\text{eff}}$ found by WGRS99. Our temperatures for both Ba and Bb are $\sim 200$ K lower than the WGRS99 results. This makes our values somewhat lower than even the dwarf $T_{\text{eff}}$ that WGRS99 quote (from L96), for their spectral types for Ba and Bb.

The gravities implied by BCAH98 are not explicitly quoted in WGRS99. However, they can easily be calculated from the luminosities, $T_{\text{eff}}$ and masses supplied. We have also checked the values we quote here against the Lyon98/00 models directly, for the masses found by WGRS99.
Bb. This is noteworthy, since WGRS99 assume that PMS temperatures should be intermediate between the giant and dwarf scales (i.e., somewhat higher than dwarf values). Let us first state what the rationale for this assumption is. In general, it is found that the optical spectra of mid- to late-M PMS stars are well reproduced by the averaged spectra of dwarfs and giants of the same spectral type (for earlier M types, dwarf spectra alone seem better; see White & Basri 2003). In fact, types are often assigned to these cool PMS objects on the basis of the giant and dwarf spectral types that in combination reproduce the PMS spectrum (this is the procedure adopted by WGRS99 for GG Tau Ba and Bb; see, e.g., WGRS99; Luhman 1999; White & Basri 2003). As a rough estimate, therefore, it is perhaps not unreasonable to suggest that the temperatures of such PMS objects, just like their spectra, are intermediate between those of giants and dwarfs.28 In this light, the lower-than-dwarf $T_{\text{eff}}$ we derive may appear troubling.

However, recent revisions in the field dwarf $T_{\text{eff}}$ scale, as well as in the spectral types of Ba and Bb, remove any cause for anxiety. As mentioned earlier, Ba and Bb have now been pushed to somewhat later types (M7.5 for Ba, and M5.5–6 for Bb), compared to the WGRS99 estimates. Concurrently, Leggett et al. (2000, hereafter L00) have derived $T_{\text{eff}}$ for a large sample of disk and halo M dwarfs (M1–M6.5), by fitting low-resolution optical to near-infrared spectra with (low-resolution versions of) the same models we have used. For M5 dwarfs, they find $T_{\text{eff}} \sim 2900$ K, for M5.5, ~2800 K, and for M6–M6.5, ~2600 K. Their sample does not include any dwarfs M7 or later.29 In general however, M7–M7.5 dwarfs should be cooler than the M6–M6.5 ones. The L00 result for the M6–M6.5 types then implies $T_{\text{eff}} \leq 2500$ K for M7–M7.5; this is also supported by the results of Leggett et al. (2001). These values are likely to be more accurate than those WGRS99 compile from L96; the new models used by L00 fit the observed SEDs much better than the substantially older models in L96. Importantly, these new temperatures for mid- to late-M dwarfs are 100–200 K lower than the L96 estimates. If these newer values are compared to our $T_{\text{eff}}$ for Ba and Bb, then Bb is ~100 K hotter than an M7–M7.5 dwarf. In fact, this is very similar to what WGRS99 find by comparing the BCAH98 predictions to the older L96 dwarf scale. This is not surprising: while our $T_{\text{eff}}$ for Bb is ~200 K cooler than the WGRS99 one, the dwarf temperature scale has also been lowered by roughly the same amount. Similarly, since L00 find M5.5–M6 dwarfs to be at ~2800–2600 K, our $T_{\text{eff}}$ for Ba (2800 K) is at least comparable to the new dwarf scale (which is what WGRS99 found using the older L96 scale), and perhaps ~200 K hotter. Thus, our $T_{\text{eff}}$ estimates for both Ba and Bb are completely consistent with a PMS temperature scale intermediate between that of dwarfs and giants, once recent improvements in the dwarf $T_{\text{eff}}$ scale and in the spectral type of Ba and Bb are taken into account.

28 The other rationale is that an intermediate PMS scale agrees with the BCAH98 predictions (Luhman 1999). However, while this makes such a scale very useful for comparing different samples to the same set of tracks, it is clearly not germane to our analysis, since we wish to probe the intrinsic veracity of the tracks.

29 It does include one metal-poor (M/H ~ −0.5) M7 sub-dwarf; at 2900 K, it is as hot as many M5 objects. Low metallicity usually leads to a higher $T_{\text{eff}}$; this sub-dwarf is thus not representative of M7–M7.5 dwarfs.
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