Vector-Boson Production of Light Higgs Pairs in 2-Higgs Doublet Models

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Abstract

At the Large Hadron Collider, we prove the feasibility to detect pair production of the lightest CP-even Higgs boson $h$ of Type II 2-Higgs Doublet Models through $qq^{(')} \rightarrow qq^{(')}hh$ (vector-boson fusion). We also show that, through the $hh \rightarrow 4b$ decay channel in presence of heavy-flavour tagging, further exploiting forward/backward jet sampling, one has direct access to the $\lambda_{Hhh}$ triple Higgs coupling – which constrains the form of the Higgs potential.

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1 Introduction

If only a light Higgs boson (with mass $M_h \lesssim 140 \text{ GeV}$) is found at the Large Hadron Collider (LHC), it may be difficult to tell whether it belongs to the Standard Model (SM) or indeed a model with an enlarged Higgs sector. For example, in the case of a CP-conserving Type II 2-Higgs Doublet Model (2HDM) [1]–[4], possibly in presence of minimal Supersymmetry (SUSY) – the combination of the two yielding the so-called Minimal Supersymmetric Standard Model (MSSM) – this happens in the so-called ‘decoupling region’, when $M_H, M_A, M_{H^\pm} \gg M_h$, for suitable choices of the other MSSM and 2HDM parameters, where - for the same mass - the $h$ couplings to ordinary matter in the SM are the same as in both the 2HDM and MSSM. Even in these conditions, however, it has been proved that one could possibly establish the presence of an extended Higgs sector by determining the size of the trilinear Higgs self-coupling $\lambda_{hhh}$ [5].

If the extended model is not in a decoupling condition, then it is generally possible to establish the presence of additional Higgs signals, $H, A$ and/or $H^\pm$ [6, 7]. However, even when this is the case, it may be difficult to distinguish, e.g., between a generic Type II 2HDM and the MSSM (unless, of course, one also detects the SUSY partners of ordinary matter and Higgs bosons). In fact, despite there exist well establish spectra among the four different masses in the MSSM (for fixed, say, $M_h$ and $\tan \beta$, the ratio of the vacuum expectation values of the two Higgs doublets in either model), it may well be possible that the additional 2HDM parameters arrange themselves to produce an identical mass pattern. However, such a degeneracy between the two models would not typically persist if one were able to also measure certain Higgs couplings, chiefly those among the Higgs bosons themselves (involving two or more such particles). In fact, while the measurement of only two among the four Higgs boson masses ($M_h, M_H, M_A$ and $M_{H^\pm}$) – or, alternatively, one such masses and $\tan \beta$ – would fix (at tree-level) all Higgs masses and couplings in the MSSM, this is no longer true in a generic Type II 2HDM [1], because of the freedom in selecting the free additional parameters. For example, the general CP-conserving Type II 2HDM that we are going to consider can be specified uniquely by seven parameters: $M_h, M_H, M_A, M_{H^\pm}, \beta, \alpha$ (the mixing angle between the two CP-even neutral Higgs states) and $\lambda_5$ (see eq. (2) later on). It may then happen that the first six of these are measured and found to agree with the MSSM pattern, but one would still need to measure $\lambda_5$ to verify that it is the Higgs sector of the MSSM that is present. One way to do so would be by measuring trilinear Higgs self-couplings, such as $\lambda_{hhh}$ and $\lambda_{Hhh}$. Alternatively, the measurement of the latter two couplings would constitute a test of the MSSM relations if one knew $M_h$ and $\tan \beta$ but not $\alpha$.

In this paper, we make the assumption that only one parameter is known, $M_h$, as may well happen at the LHC after only a $h$ resonance is detected. We further imply that all

\textsuperscript{2}Of the initial eight degrees of freedom pertaining to the two complex Higgs doublets, only five survive as real particles upon Electro-Weak Symmetry Breaking (EWSB), labelled as $h$, $H$, $A$ (the first two are CP-even or ‘scalars’ (with $M_h < M_H$) whereas the third is CP-odd or ‘pseudoscalar’) and $H^\pm$, as three degrees of freedom are absorbed into the definition of the longitudinal polarisation for the gauge bosons $Z$ and $W^\pm$, upon their mass generation after EWSB.
(potential) SUSY states are much heavier than ordinary particles (with the possible exception of the lightest SUSY particle, see footnote 4), thus effectively a decoupled MSSM setup. Under these circumstances, we then ask ourselves the following question. While trying to establish the presence of additional (single) heavy Higgs signals, which would then unmistakably distinguish between the SM and a scenario with an extended Higgs sector, would it also be possible to gather information on Higgs self-couplings from signatures involving two light Higgs bosons, hence by studying channels involving $h$ pair production, thereby possibly also distinguish between, e.g., a generic Type II 2HDM and the MSSM?

It is the purpose of this paper to show that this is the case, so long that enough luminosity can be accumulated at the LHC, also in view of the Super-LHC (SLHC) option [8]. We will illustrate how we have come to this conclusion, i.e., after investigating the process [9]

$$qq^{(i)} \rightarrow qq^{(i)}hh \text{ (vector boson fusion)}, \quad (1)$$

with $q^{(i)}$ referring to any possible (anti)quark flavour combinations. The relevant Feynman diagrams corresponding to process (1) in both the MSSM and 2HDM considered here can be found in Fig. 1. In our selection analysis, we will resort to the extraction of two $h \to b\bar{b}$ resonances, in presence of the following signature:

- ‘four $b$-quark jets and two forward/backward-jets’.

This signature was already considered in Ref. [5] in the SM context (from which we will import some of the results).

Our paper is organised as follows. In the next section, we outline the computational procedure. Sect. 3 presents our numerical results and discusses these in various subsections. Sect. 4 contains our conclusions.

## 2 Calculation

We have assumed $\sqrt{s} = 14$ TeV for the LHC energy throughout. Our numerical results are obtained by setting the renormalisation and factorisation scales to $2 M_h$ for the signal while for the QCD background we have used the average jet transverse momentum ($p_T^2 = \sum_1^n p_T^{j,n}$). Both Higgs processes and noise were estimated by using the Parton Distribution Function (PDF) set MRST99(COR01) [18]. While the background calculations were based on exact tree-level Matrix Elements (MEs) using the ALPGEN program [19], all signal rates were obtained

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3The gluon-gluon production mode [10] was considered in Refs. [11] and [12] (see also [13]), and later on [14, 15], where – despite significant kinematic differences exist between signal and QCD noise – it was eventually shown that the extraction of the $gg \to hh \to b\bar{b}b\bar{b}$ signal is essentially impossible at the (S)LHC because of the overwhelming QCD noise, both reducible and irreducible. Recently, encouraging results on the cross-section for multi-Higgs boson production in the gluon-gluon production mode has been obtained in models beyond the SM and MSSM [16]. The possibility of using Higgs boson pair production more generally to access trilinear Higgs couplings has also been studied on the level of total cross-sections in [17].
through the same level of accuracy via programs based on the HELAS subroutines [20] – for the computation of the MEs – and VEGAS [21] or Metropolis [22] – for the multi-dimensional integrations over the phase space. As for numerical input values of SM parameters, we adopted the ALPGEN defaults.

Concerning the MSSM setup, the two independent tree-level parameters that we adopt are $M_A$ and $\tan \beta$. Through higher orders, we have considered the so called ‘Maximal Mixing’ scenario ($X_t = A_t - \mu/\tan \beta = \sqrt{3} M_{\text{SUSY}}$) [23], wherein we have chosen for the relevant SUSY input parameters: $\mu = 200 \text{ GeV}$, $A_b = 0$, with $M_{\text{SUSY}} = 5 \text{ TeV}$, the latter – as already intimated – implying a sufficiently heavy scale for all sparticle masses, so that these are not accessible at the LHC and no significant interplay between the SUSY and Higgs sectors of the model can take place. Masses and couplings within the MSSM have been obtained by using the HDECAY program [24].

Before giving the details of the 2HDM setup we are using, let us recall the most general CP-conserving 2HDM scalar potential which is symmetric under $\Phi_{1(2)} \rightarrow -\Phi_{1(2)}$ up to softly breaking dimension-2 terms (thereby allowing for loop-induced flavour changing neutral currents) [1],

$$V = m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left\{ m_{12}^2 \Phi_1^\dagger \Phi_2 + h.c. \right\} + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \left\{ \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + h.c. \right\}. \tag{2}$$

In the following, the parameters $m_{11}, m_{22}, m_{12}, \lambda_1, \lambda_2, \lambda_3$ and $\lambda_4$ are replaced by $v, M_h, M_H, M_A, M_{H^\pm}, \beta$ and $\alpha$ (with $v$ fixed). Hence, as intimated already, the CP-conserving 2HDM potential is parameterised by seven free parameters. Notice that from the scalar potential all the different Higgs couplings needed for our study can easily be obtained. (See [2, 3] for a complete compilation of couplings in a general CP-conserving 2HDM.)

In our 2HDM, we will fix $M_h$ and $M_H$ to values similar to the ones found in the MSSM scenario we are considering, by adopting three different setups:

1. $M_h = 115 \text{ GeV}, M_H = 300 \text{ GeV},$
2. $M_h = 115 \text{ GeV}, M_H = 500 \text{ GeV},$
3. $M_h = 115 \text{ GeV}, M_H = 700 \text{ GeV}.$

We always scan over the remaining parameters in the ranges

$$-\pi/2 < \alpha < \pi/2,$$

$$-4\pi < \lambda_5 < 4\pi,$$

$$0 < \tan \beta < 50,$$

\[4\]The only possible exception in this mass hierarchy would be the Lightest Supersymmetric Particle (LSP), whose mass may well be smaller than the lightest Higgs mass values that we will be considering. However, we have verified that invisible $h$ decays (including the one into two LSPs) have negligible decay rates.
100 GeV < M_A < 1000 GeV,
100 GeV < M_{H^\pm} < 1000 GeV.

In order to accept a point from the scan we also check that the following conditions are fulfilled: the potential is bounded from below, the \( \lambda_i \) fulfill the tree-level unitarity constraints of [25] and yield a contribution to \( |\Delta \rho| < 10^{-3} \). In short the unitarity constraints amounts to putting limits on the eigen values of the \( S \) matrices for scattering various combinations of Higgs and electroweak gauge bosons. We have followed the normal procedure [1] of requiring the \( J = 0 \) partial waves \( (a_0) \) of the different scattering processes to fulfill \( |\text{Re}(a_0)| < 1/2 \), which corresponds to applying the condition that the eigenvalues \( \Lambda_{Y_{\sigma \pm}} \) of the scattering matrices (or more precisely \( 16\pi S \)) fulfill \( |\Lambda_{Y_{\sigma \pm}}| < 8\pi \) [26]. In other words we allow parameter space points all the way up to the tree-level unitarity constraint \( |\text{Re}(a_0)| < 1/2 \). In order to investigate the sensitivity to this upper limit we will also report results as a function of the value of the maximal eigenvalue, \( \Lambda_{\text{max}} \). The spectrum of masses, couplings and decay rates in our 2HDM is the same as in Ref. [27], obtained by using a modification of HDECAY [24] (consistent with a similar manipulation of the program used in Ref. [28]). For each accepted point in the scan the partial decay rates for the different Higgs bosons are then calculated using HDECAY and also taking possible additional partial widths of the \( H \) into account.

While the parameter dependence of the MSSM Higgs sector renders the computation of the tree-level MSSM cross-sections rather straightforward (as the latter depends on two parameters only, \( M_A \) and \( \tan \beta \)), the task becomes much more time-consuming in the context of the 2HDM. In order to calculate the cross-sections in this scenario, they are schematically written as a combination of couplings and kinematic factors in the following way:

\[
\sigma_{\text{tot}} = \int \left| \sum_{i=1}^{5} g_i M_i \right|^2 d\text{LIPS} = \sum_{i=1}^{5} \sum_{j=1}^{5} g_i g_j \sigma_{ij},
\]

where all the explicit dependence on \( \alpha, \beta, \lambda_{Hhh} \) and \( \lambda_{hhh} \) is contained in the couplings \( g_i \):

\[
g_1 = \sin^2(\beta - \alpha), \quad g_2 = \cos^2(\beta - \alpha), \quad g_3 = \cos(\beta - \alpha) \lambda_{Hhh}, \quad g_4 = \sin(\beta - \alpha) \lambda_{hhh}, \quad \text{and} \quad g_5 = 1,
\]

whereas the dependence on masses and other couplings is in the factors

\[
\sigma_{ij} = \frac{1}{1 + \delta_{ij}} \int \left( M_i^\dagger M_j + M_j^\dagger M_i \right) d\text{LIPS}.
\]

Note that the sum over subamplitudes \( M_i \) also contains all interference terms and that colour factors etc. are included properly.\(^{6}\) The \( \sigma_{ij} \) are then calculated numerically for fixed masses. We can then get the cross-section in an arbitrary parameter space point by multiplying the kinematic factors with the appropriate couplings. However, there is a slight complication since the kinematic factor for the \( H \rightarrow hh \) contribution depends on the width \( \Gamma_H \) if there is a s-channel resonance and the width in turn depends on the couplings. In this case the kinematic factor scales as \( 1/\Gamma_H \) which is accounted for by assuming a fixed value for the width when the

\(^{5}\)Here, \( Z_2 \) refers to the \( Z_2 \) symmetry, \( Y \) is the hypercharge, and \( \vec{\sigma} \) is the total weak isospin.

\(^{6}\)We have carefully verified the integrity of our procedure.
kinematic factor is calculated and then rescaling the result with the true width when calculating
the contribution to the cross-section. Another complication is the dependence of the kinematic
factors on the Higgs masses, $M_A$ and $M_{H^\pm}$. The contributions of main interest, which contain
the $\lambda_{Hhh}$ and $\lambda_{hhh}$ couplings, only depend on these masses indirectly through the unitarity
constraints. At the same time there are other contributions to the cross-section which depend
explicitly on these masses. However, these contributions are very small in the parts of parameter
space of interest and can thus be safely neglected.

3 Results

In our investigation of the emerging hadronic final state, we will assume that $b$-quark jets
are distinguishable from light-quark and gluon ones and neglect considering $b$-jet charge de-
termination. Finite calorimeter resolution has been emulated through a Gaussian smearing
in transverse momentum, $p_T$, with $(\sigma(p_T)/p_T)^2 = (0.60/\sqrt{p_T})^2 + (0.04)^2$, for all jets. The
corresponding missing transverse momentum, $p_T^{\text{miss}}$, was reconstructed from the vector sum of
the visible momenta after resolution smearing. Finally, in our parton level analysis, we have
identified jets with the partons from which they originate and applied all cuts directly to the
latter, since parton shower and hadronisation effects were not included in our study.

3.1 Inclusive Signal Results

In this section, after a preliminary analysis of the Higgs mass and coupling spectra in the
MSSM and a general Type II 2HDM, we will start our numerical analysis by investigating the
model parameter dependence of the Higgs pair production process in (11) at fully inclusive level,
in presence of the decay of the latter into two $b\bar{b}$ pairs, with the integration over the phase
space being performed with no kinematical restrictions. This will be followed by an analysis of
the production and decay process pertaining to the Higgs signal of interest at fully differential
level, in presence of detector acceptance cuts and kinematical selection constraints. Finally, we
will compare the yield of the signal to that of the corresponding background and perform a
dedicated signal-to-background study including an optimisation of the cuts in order to enhance
the overall significance. We will treat the MSSM and 2HDM in two separate subsections.

3.1.1 MSSM

As representative of the low and high tan $\beta$ regime, we will use in the remainder the values of 3
and 40. We have instead treated $M_A$ as a continuous parameter, varying between 100 and 700
GeV or so. Before proceeding with the numerical analysis of the signal, it is worthwhile to
investigate both the Higgs mass and coupling dependence in the MSSM with respect to the two
input parameters $M_A$ and tan $\beta$. This is done in Figs. 2 and 3, respectively. In the latter, we

\footnote{Values of $M_A$ below 90 GeV or so are actually excluded by LEP for the lower tan $\beta$ value: see [29].}
study the case of (CP-even) MSSM Higgs boson couplings to gauge bosons (denoted by $G_{hVV}$ and $G_{HVV}$), wherein $V$ refers to either a $W^\pm$ or a $Z$. In the same figure, the symbol $\phi$ refers to the SM Higgs boson, with mass identical to that of the lightest MSSM Higgs state ($M_{\phi} = M_h$). While the pattern of masses has been well established in past literature, it is interesting to notice here that the product of the MSSM couplings entering process (1) is always smaller than in the SM case. However, in the MSSM, resonance enhancements can occur (such as in $H \to hh$), so that the actual MSSM production rates can in some cases overcome the corresponding SM ones (for $M_{\phi} = M_h$).

Fig. 4 presents the fully inclusive MSSM cross-section for the process of interest, as defined in (1), times (effectively) BR($hh \to b\bar{b}b\bar{b}$). The shape of the curves is mainly dictated by the interplay between phase space (see Fig. 2) and coupling (see Fig. 3) effects, with the exception of the region $M_A \gtrsim 220 \text{ GeV}$ and $\tan \beta = 3$, where the onset of the $H \to hh$ resonance is clearly visible. Cross-sections are generally sizable, particularly at low $\tan \beta$. The displayed rates however coincide to the ideal situation in which all final state jets are detected with unit efficiency and the detector coverage extend to their entire phase space, so that they only serve as a guidance in rating the phenomenological relevance of the process discussed.

A more realistic analysis is in order, which we have performed as follows. The four $b$-jets emerging from the decay of the $hh$ pair are accepted according to the following criteria:

$$p_T^b > 30 \text{ GeV}, \quad |\eta^b| < 2.5, \quad \Delta R_{bb} > 0.7,$$

in transverse momentum, pseudorapidity and cone separation, respectively. Their tagging efficiency is taken as $\epsilon_b = 50\%$ for each $b$ satisfying these requirements, $\epsilon_b = 0$ otherwise. In addition, to enforce the reconstruction of the two Higgs bosons, we require all such $b$’s in the event to be tagged and that at least one out of the three possible double pairings of $b$-jets satisfies the following mass preselection:

$$(m_{b_1,b_2} - M_h)^2 + (m_{b_3,b_4} - M_h)^2 < 2 \sigma_m^2,$$

where $\sigma_m = 0.12 M_h$. We further exploit ‘forward/backward-jet’ tagging, by imposing that the non-$b$-jets satisfy the additional cuts

$$p_T^{\text{fwd/bwd}} > 20 \text{ GeV}, \quad 2.5 < \eta^{\text{fwd}} < 5, \quad -2.5 > \eta^{\text{bwd}} > -5.$$

Tab. 1 shows the rates of the signal after the implementation of the constraints in eqs. (5)–(7) (hereafter, referred to as ‘acceptance and preselection cuts’ or ‘primary cuts’). While our process does yield non-negligible rates after the latter, it turns out that it is of no phenomenological relevance, even assuming very high luminosity. Firstly, in view of the fact that $b$-tagging efficiencies are not taken into account in this table: for the ‘4b-jet’ tagging option, one should multiply the numbers in Tab. 1 by $\epsilon_b^4$, that is, $1/16$. (Alternative approaches requiring a lesser

\[8\text{Here and in the remainder, the label } b \text{ refers to jets that are } b\text{-tagged while } j \text{ to any jet (even those originating from } b\text{-quarks) which is not.}\]
\[
\tan \beta = 3
\]

| \(M_A\) (GeV) | \(M_h\) (GeV) | \(\sigma(qq \rightarrow qq hh)\) [fb] | \(\sigma(\text{background})\) [fb] |
|---------------|---------------|-------------------------------|-------------------------------|
| 160           | 108           | 0.19                          | 218                           |
| 200           | 112           | 0.23                          | 232                           |
| 240           | 114           | 0.46                          | 229                           |

\[
\tan \beta = 40
\]

| \(M_A\) (GeV) | \(M_h\) (GeV) | \(\sigma(qq \rightarrow qq hh)\) [fb] | \(\sigma(\text{background})\) [fb] |
|---------------|---------------|-------------------------------|-------------------------------|
| 160           | 129           | 0.26                          | 224                           |
| 200           | 129           | 0.20                          | 224                           |
| 240           | 129           | 0.17                          | 224                           |

Table 1: Cross-sections for Higgs pair production via vector-boson fusion, process \(1\), after Higgs boson decays (relevant BRs are all included) and the acceptance and preselection cuts defined in \(5\)–\(7\), for two choices of \(\tan \beta\) and a selection of \(M_A\) values, assuming the MSSM in Maximal Mixing configuration (the corresponding values of \(M_h\) are also indicated in brackets). No \(b\)-tagging efficiencies are included here.

number of \(b\)-jets to be tagged as such were not successful either.) Secondly, the background rates, after the same cuts in eqs. \(5\)–\(7\), are always overwhelming the signal, despite our efforts in further optimising the cuts. For this reason, rather than dwelling upon the latter now, we postpone their discussion to the next subsection and simply conclude here that our channel is altogether inaccessible at both the LHC and SLHC in the context of the MSSM.

### 3.1.2 2HDM

As already alluded to, the parameter space of the general CP-conserving Type II 2HDM we are considering is quite large as it depends on seven unknown parameters. In order to get a feel for the dependence of the signal cross-section for the process \(qq \rightarrow qq hh \rightarrow qq b\bar{b} b\bar{b}\) we therefore present in Figs. \(5\) through \(7\) the results of our three selected scenarios, wherein we scan the allowed parameter space over 10000 randomly chosen points. (Note that similarly to the MSSM case we have included the \(\text{BR}(hh \rightarrow b\bar{b} b\bar{b})\) but not any 4\(b\)-jet tagging efficiency.)

Comparing with the cross-sections in the MSSM the main differences are due to the following:

- the triple Higgs couplings \(\lambda_{Hhh}\) and \(\lambda_{hhh}\) are not related to the gauge couplings;

- the different parameters can vary independently of each other.

Conversely, the kinematic factors in the two models will be the same for a given set of masses and widths of the different Higgs bosons. Therefore, in those cases, many features of the signal,

\(9\) We use the same definitions of these couplings as in [2].
such as the differential distributions, will be similar to those of the MSSM even though the normalisation can be completely different. In fact, comparing Fig. 4 with 5 through 7 we see that in the more general 2HDM the cross-sections can be more than two orders of magnitude larger than in the MSSM thus rendering a much larger potential for a detectable signal (as it will be discussed below). To be more quantitative on this we give in Tab. 2 the maximal inclusive cross-sections obtained in the scans for \( M_h = 115 \text{ GeV} \) and \( M_H = 300, 500 \) and 700 GeV.

In order to study the potential signal in more detail we first of all apply the same primary cuts as in the case of the MSSM, those listed in eqs. (5)–(7). The resulting cross-sections are given Tab. 2. Comparing with the cross-section without the primary cuts we see that the reduction is substantial, but even so the signal cross-section can still be more than two orders of magnitude larger than in the MSSM scenario considered in subsection 3.1.1 and it is comparable to the background (see Tab. 1, specifically for low \( \tan \beta \), where the \( M_h \) values in the two models are very similar).

### 3.2 Signal-to-Background Differential Analysis

In this section, we will continue the discussion of our numerical analyses limitedly to the Type II 2HDM considered so far. In order to enhance the statistical significance \( S/\sqrt{B} \) we studied several differential distributions for signals and background with the event selection of eqs. (5)–(7), with the aim of introducing optimised cuts, allowing at the same time to keep the signal event numbers at a reasonable level. To begin with, for simplicity, we have limited ourselves to use the contribution from the \( H \to hh \) resonance to the signal for \( M_H = 300 \) GeV in a scenario where the cross-section is close to maximal, with \( \cos(\beta - \alpha) = 1 \), \( \lambda_{Hhh} = 1000 \) GeV and \( \Gamma_H = 30 \) GeV, when comparing with the background.

The most sensitive distributions, able to discriminate between the signal and background, turn out to be the minimum transverse momentum of the forward/backward jets and the next-to-minimum invariant mass of the \( b\bar{b} \) pairs, which we show in Fig. 8. (Although to a some more

| \( M_H \) (GeV) | \( \sigma(qq' \to qqq'h) \) [fb] | inclusive | primary | optimal | optimal, \( H \to hh \) |
|----------------|------------------|----------|--------|--------|------------------|
| 300            | 1453             | 71.9     | 31.2   | 25.8   |
| 500            | 396              | 25.3     | 11.4   | 7.7    |
| 700            | 80               | 7.1      | 3.3    | 2.0    |

Table 2: The maximal cross-sections in the 2HDM under consideration for \( M_h = 115 \text{ GeV} \), and \( M_H = 300, 500 \) and 700 GeV, respectively, with the following different cuts: inclusive, with primary cuts in eqs. (5)–(7), and with optimised cuts of eq. (8) in the latter case also when only considering the \( H \to hh \) resonant contribution.
limited extent, also the minimum $b\bar{b}$ invariant mass is useful.) Before selecting a specific set up, we performed also a systematic analysis of the significance for different combination of cuts 

$$30\text{ GeV} \leq m_{bb}^{\text{min}} \leq m_{bb}^{\text{next-to-min}} \leq 100\text{ GeV}, \quad 20\text{ GeV} \leq p_{T}^{\text{fwd}} \leq 60\text{ GeV}.$$  

The best optimised cuts, on top of the basic ones of eqs. (5)–(7), that we found are

\[ p_{T}^{\text{fwd/bwd}} > 40\text{ GeV}, \quad m_{bb}^{\text{min}} > 40\text{ GeV}, \quad m_{bb}^{\text{next-to-min}} > 80\text{ GeV}. \]  

We show in Fig. 9 the 4$b$ invariant mass distribution for three signals ($M_H = 300, 500$ and $700$ GeV with the widths $\Gamma_H = 30, 50$ and $200$ GeV, respectively) and the background after the optimised cuts of eq. (8) have also been imposed. For each of the three signals shown in the figure we have used the parameter space point which gives the maximal signal cross-section from the resonant $H \rightarrow hh$ contribution when restricting the width $\Gamma_H$ to be less than 30, 50 and 200 GeV, respectively. In this context we note that there are two effects which mainly determine the width of the signal distribution. On the one hand, the smearing of momenta we use gives a contribution to the measurable width of about 30 GeV. On the other hand, one of course has the intrinsic width of the $H$.

Taking suitable mass windows around the peaks for the different Higgs mass values illustrated in Fig. 9, we obtain the maximal signal cross-sections, event numbers and statistical significances quoted in Tab. 3. In order to calculate the signal cross-sections in the respective windows for different parameter space points, taking the actual width of the $H$ into account, we rescaled the contribution from the $H \rightarrow hh$ resonance with a factor $c_{M_H} \equiv (\arctan[2(M_H - m_L)/\Gamma_i] + \arctan[2(m_U - M_H)/\Gamma_i])$ where $m_L$ and $m_U$ are the lower and upper limits of the signal window, $\Gamma_i$ is the width of the signal distribution in parameter space point $i$ estimated from $\Gamma_i = \sqrt{\Gamma_{H_i}^2 + \Gamma_{4b}^2}$ with $\Gamma_{4b} = 30\text{ GeV}$ being the width of the $m_{4b}$-distributions from finite detector resolution. (Notice then that $c_{M_H}$ is a normalisation determined from scenarios with $\Gamma_{H_i} = 30, 50$ and $200$ GeV for the different $H$ masses.) Thus we approximate the cross-section in the $m_{4b}$ window as $\sigma_{\text{peak}} = c_{M_H} \sigma_{H \rightarrow hh}$. As a further requirement we also imposed that at least 50% of the signal cross-section after the optimal cuts comes from the $H \rightarrow hh$ resonance such that the would-be-signal would not be obscured by other non-resonant contributions.

The distributions of the signal cross-sections obtained in this way are given in Fig. 10. For illustration, the $5\sigma$ limits at LHC, assuming an integrated luminosity of 300 fb$^{-1}$, $\sigma_{\text{peak}} > 2.7 (2.3-3.3)$\textsuperscript{11}, $1.5 (1.3-1.8)$ and $0.8 (0.7-1.0)$ fb, for $M_H = 300, 500$ and $700$ GeV respectively, are

\textsuperscript{10}Note that the efficiency of these is rather insensitive to the actual Higgs mass values, so that we have used the same set for any choice of the latter.

\textsuperscript{11}The ranges given within parenthesis in this paragraph have been obtained by varying the factorisation/renormalisation scale for the background by a factor of two around the default value, which makes the corresponding cross-section decrease by 30 % or increase by 50 % respectively. The reason for this is that, being essentially a six-jet cross-section, the background rate is proportional to $\alpha_s^6$ and it is therefore quite sensitive to the renormalisation scale. We also note that our default scale ($p_T^2 = \sum_{i=1}^n p_T^{j,i}/n$) has conservatively been chosen to be small so, if anything, our estimate of the final signal-to-background rates should be regarded as conservative. In a real experiment one should of course attempt to use the sidebands for background normalisation.
Table 3: Number of events and significances for $M_h = 115$ GeV and $M_H = 300, 500, 700$ GeV in the respective best case scenarios, for a 4b-tagging efficiency of $(50\%)^4$ and after the optimised cuts of eq. (8). The assumed integrated luminosity at LHC and SLHC are 300 fb$^{-1}$ and 3000 fb$^{-1}$, respectively.

also illustrated and the fractions of parameter space points which gives cross-sections larger then this are 27 (24-30), 8 (5-12) and 0%, respectively. The corresponding numbers for the SLHC with 3000 fb$^{-1}$ are 43 (41-45), 31 (28-33) and 2 (0-2)%, respectively. Thus even at the SLHC we find no scope of observing a $M_H = 700$ GeV resonance in the channel under investigation.

Finally we have also investigated the effects of restricting the allowed parameter space from tree-level unitarity by putting harder constraints on the maximal eigenvalue of the scattering matrices, $\Lambda_{\text{max}}$. For this purpose, Fig. 11 shows the signal cross-sections obtained in the scan as a function of $\Lambda_{\text{max}}$. From the figure it is clear that the results (at least for $M_H = 300$ and 500 GeV) are not sensitive to the precise value used for applying the unitarity constraint. On the other hand, applying a much harder constraint of the order $\Lambda_{\text{max}} \lesssim 4(12)$ (instead of $\Lambda_{\text{max}} < 8\pi$) essentially leads to that the sensitivity for detection at the LHC is more or less washed out for $M_H = 300$ (500) GeV. The same also holds at the SLHC assuming an integrated luminosity of 3000 fb$^{-1}$.

4 Conclusions

We would like to conclude our paper by stating that, at both the LHC and SLHC, there exists a great potential to extract a $H \to hh \to 4b$ resonance when $M_h$ is constrained in the vicinity of 115 GeV. This is a crucial result if one recalls that the detection of a sole Higgs resonance and consequent extraction of an $M_h$ value may not point unambiguously to the underlying model of EWSB, not even in presence of further measurements of the heavier Higgs masses, $M_H, M_A$ and/or $M_{H^\pm}$.

For example, the 2HDM considered here may be realised in a configuration wherein all visible Higgs masses are degenerate with those of the MSSM. Under these circumstances, we have proved that

* it is not possible to extract an $H \to hh \to 4b$ resonance from vector-boson fusion in the MSSM (not even if $M_H$ is known) whilst
• the opposite case is true in a substantial fraction of the parameter space of our 2HDM (even if $M_H$ is not known), thereby enabling one to possibly measure the triple-Higgs coupling $\lambda_{Hhh}$.

The latter is a Lagrangian term, which is different between these two models even when their patterns of Higgs masses and couplings to SM objects are the same, that would give a unique insight into the underlying EWSB mechanism.

To be more specific our results show that in the most favourable scenario with $M_H = 300$ GeV up to 27 (43) % of the parameter space would give a 5σ signal at the (S)LHC assuming an integrated luminosity of 300 (3000) fb$^{-1}$ when using the standard tree-level unitarity requirement on the $J = 0$ partial waves, $\text{Re}(a_0) < 1/2$. These results are not sensitive to the precise value used for applying the unitarity constraint, albeit for very strong constraints the sensitivity for detecting the signal goes away. In the case of $M_H = 500$ GeV the fraction of parameter space probed is smaller with up to 8 (31) % giving a 5σ signal, whereas for $M_H = 700$ GeV there is essentially no sensitivity at all.

Despite we lack a full Monte Carlo simulation we believe to have incorporated the most critical aspects of the latter so that we do not expect more realistic studies (including parton shower, hadronisation, heavy hadron decays and detector effects) to affect too strongly our conclusions.

Finally, we are currently pursuing other work along the directions outlined here, covering the case of lightest (neutral) Higgs boson pair production in the case of Higgs-strahlung and in association with heavy quarks [30].

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Figure 1: Feynman diagrams for $q_1q_2 \rightarrow q_3q_4h_5h_6$. Depending on the (anti)quark flavour combination, the $W^\pm$- and $Z$-mediated graphs may not interfere. Besides, for final state (anti)quarks of different flavours, only half of the diagrams survive.
Figure 2: The masses of the neutral CP-even Higgs bosons as a function of the CP-odd one, for two choices of $\tan \beta$, assuming the MSSM in Maximal Mixing configuration.
Figure 3: The relevant couplings of the neutral CP-even Higgs bosons entering the production process in (1) as a function of the CP-odd Higgs boson mass, for two choices of $\tan \beta$, assuming the MSSM in Maximal Mixing configuration.
Figure 4: The inclusive cross-sections (as defined in the text) for vector-boson fusion in (I), followed by $hh \to b\bar{b}b\bar{b}$ decays, as a function of the CP-odd Higgs boson mass, for two choices of $\tan\beta$, assuming the MSSM in Maximal Mixing configuration.
qq → qqhh → qqbb in 2HDM, \( m_h = 115 \) GeV, \( m_H = 300 \) GeV

Figure 5: The dependence of the inclusive cross-section \( qq' \rightarrow qq'h'h \rightarrow qq'b'b \) in the 2HDM under consideration on the different parameters when scanning over 10000 parameter space points for \( M_h = 115 \) GeV and \( M_H = 300 \) GeV. (Note that \( M_A \) and \( M_{H\pm} \) are free parameters.)
Figure 6: The dependence of the inclusive cross-section $qq \rightarrow qqhh \rightarrow qqbb$ in the 2HDM under consideration on the different parameters when scanning over 10000 parameter space points for $M_h = 115$ GeV and $M_H = 500$ GeV. (Note that $M_A$ and $M_{H^\pm}$ are free parameters.)
Figure 7: The dependence of the inclusive cross-section $qq^{(\prime)} \rightarrow qq^{(\prime)}hh \rightarrow qq^{(\prime)}b\bar{b}b\bar{b}$ in the 2HDM under consideration on the different parameters when scanning over 10000 parameter space points for $M_h = 115$ GeV and $M_H = 700$ GeV. (Note that $M_A$ and $M_{H\pm}$ are free parameters.)
Figure 8: The distribution of the next-to-minimum $b\bar{b}$ invariant mass (left) and of the minimum tagging jet transverse momentum (right) for the signal (cross section for $qq^{(i)} \rightarrow qq^{(i)}hh \rightarrow qq^{(i)}b\bar{b}b\bar{b}$ in a close to best-case scenario for $M_H = 300$ GeV) and the background. The basic cuts of eqs. (5)–(7) are imposed.
Figure 9: The differential cross-section $d\sigma(qq' \rightarrow qq'h\rightarrow qq'b\bar{b})/dm_{4b}$ in the best case scenarios for $M_H = 300, 500$ and 700 GeV obtained when scanning over the available parameter space restricting the width $\Gamma_H$ to be less than 30, 50 and 200 GeV, respectively. When calculating the signal distributions the actual widths have been assumed to be $\Gamma_H = 30, 50$ and 200 GeV, respectively.
Figure 10: Distributions of the resulting cross-sections $qq \to qqhh \to qqbbbb$ in the 2HDM under consideration using the optimal cuts obtained in a scan over 10000 parameter space points (the area is normalised to 1 for the cross-section with optimal cuts) for three different sets of Higgs boson masses as indicated in the respective plots. The solid line shows the results with optimal cuts, the dashed line shows the resonant contribution from the $H \to hh$ processes and the long dashed line shows the resonant contribution in the respective signal windows requiring that at least 50% of the cross-section comes from the $H \to hh$ resonance. The vertical line corresponds to the $5\sigma$-limit at LHC assuming 300 fb$^{-1}$ and the integral of the curves to the right of it gives the percentage of parameter space points where the resonant cross-section is larger than this.
Figure 11: The distributions in resulting signal cross-sections $qq^{(i)} \rightarrow qq^{(j)} hh \rightarrow qq^{(i)} b\bar{b} b\bar{b}$ in the 2HDM under consideration using the optimal cuts obtained in a scan over 10000 parameter space points as a function of the maximal eigenvalue $\Lambda_{\text{max}}$ of the scattering matrix for three different sets of Higgs boson masses as indicated in the respective plots. The upper (lower) horizontal line corresponds to the 5$\sigma$-limit at (S)LHC assuming 300 fb$^{-1}$ (3000 fb$^{-1}$).