Simulation of an Intra-Pulse Interaction Point Feedback for Future Linear Colliders

D. Schulte, CERN, 1211 Geneva, Switzerland

Abstract
In future normal-conducting linear colliders, the beams will be delivered in short bursts with a length of the order of 100 ns. The pulses will be separated by several ms. In order to maintain high luminosity, feedback is necessary on a pulse-to-pulse basis. In addition, intra-pulse feedback that can correct beam positions and angles within one pulse seem technically feasible. The likely performances of different feedback options are simulated for the NLC (Next Linear Collider [1]) and CLIC (Compact Linear Collider [2]).

1 INTRODUCTION
A vertical position displacement between the beam centres at the interaction point (IP) will cause luminosity reduction. Two main sources of beam jitter at the interaction point IP are expected. Firstly, the beam entering the final focus system may jitter in angle and position. At the IP, the resulting vertical position error, normalised to the beam size, and the resulting angle error, normalised to the beam divergence, are expected to have the same size. Secondly, transverse jitters of the final focus magnets, especially of the final doublet, will mainly change the position of the beams at the IP, not so much the angle. The jitter at the IP can thus be described by

$$\left(\frac{(\Delta y^2)}{\sigma_y^2}\right) = \left(\frac{(\Delta y'^2)}{\sigma_{y'}^2}\right) + \left(\frac{(\Delta_{ffs}y)^2}{\sigma_y^2}\right).$$

Here, $\Delta y$ and $\Delta y'$ are the offset and angle error of the beam at the IP, $\sigma_y$ and $\sigma_{y'}$ are beam size and divergence, also at the IP. $\Delta_{ffs}y$ is the contribution to the position error due to the final focus system. If it is large, the effect of the angle at the IP can be neglected.

2 BEAM-BEAM INTERACTION
When the beams collide with a vertical offset, they will receive a strong kick from the beam-beam interaction. The angle of the outgoing beam can therefore be used to measure the relative positions of the beams. The dependence of kick angle and luminosity on the position and initial angle have been simulated with the program GUINEA-PIG [3], varying both parameters. The luminosity $L$ as a fraction of the nominal $L_0$, is shown in Fig. 1, as a function on the relative beam position error and beam angle error. The kick angle is shown in Fig. 2 as a function of the offset. If the beams collide without an offset but with an angle, their initial angle is roughly preserved in the beam-beam interaction. For comparison: the beam divergence is $\sigma_{y'} \approx 26 \mu$rad for NLC and $\sigma_{y'} \approx 11.7 \mu$rad for CLIC.

3 POSITION FEEDBACK MODEL
In order to have a fast correction, corrector and beam-position monitor (BPM) need to be located close together. Here, they are located on the same side of the IP at a distance of 1.5 m, see Fig. 3. Thus the correction is not ap-
beam position error as a function of the gain $g$.

Figure 4: The luminosity loss in NLC (with feedback) for a beam position error as a function of the gain $g$.

Applied to the measured beam but to the other one. This significantly reduces the time necessary to transport the signal from the BPM to the kicker. The feedback response time $\tau_d$ is given by

$$\tau_d = \tau_p + \tau_k + \tau_{pf} + \tau_{kf} + \tau_s \quad (1)$$

Here, $\tau_p$ is the time the BPM electronics needs to measure the beam offsets and to process the data, $\tau_k$ is the response time of the kicker and $\tau_s$ is the transport time of the signal from BPM to kicker. $\tau_{pf}$ and $\tau_{kf}$ are the times of flight from the IP to the BPM and from the kicker to the IP, respectively. In the following, a total of $\tau_d = 20$ ns is assumed, half of which is due to $\tau_{pf} + \tau_{kf}$. The pulse lengths are 100 ns in CLIC and 266 ns in NLC.

The hardware for this feedback has not yet been designed. With a solid state amplifier it should be possible to correct an offset of $2\sigma_y$ [4], with an additional stage of tube amplification this may even be extended to $20\sigma_y$ [5].

It is assumed that the feedback changes the beam position by $\delta y$ after each measured bunch according to

$$\delta y = g \frac{\theta}{\sigma_y} \sigma_y$$

for a measured angle $\theta$. The gain factor $g$ is chosen to give optimal performance. The additional crossing angle, that results from the correction is orders of magnitude smaller than the beam divergence and can be neglected.

4 RESULTS OF POSITION FEEDBACK

Here, only position errors are considered. First NLC is discussed. In Fig. [4], the luminosity loss with a beam offset $\Delta y = 2\sigma_y$ is shown as a function of the gain $g$. As can be seen, $g = 0.06$ seems a good choice. Very small gains lead to a slow correction, very large ones to an over-correction. Both result in a larger luminosity loss. With $g = 0.06$, the luminosity loss is reduced by a factor 6, compared to the case without feedback. For a smaller offset of $\Delta y = 1/8\sigma_y$ about the same factor is found.

Two main sources of noise can lead to an increased luminosity loss with feedback: a bunch-to-bunch position jitter of the incoming beam, and the position resolution of the BPM. For the chosen gain $g = 0.06$, the additional loss induced by the feedback is very small, compared to the case without feedback. To estimate the required BPM resolution, simulations are performed with perfect beams and a position error of the BPM of $\sigma_{BPM} = 15 \mu m$ for a single bunch. The luminosity loss, averaged over 100 cases, is only $\Delta L/L = 0.7 \times 10^{-3}$. The limit on the BPM resolution seems therefore not to be very stringent compared to the resolutions that must be achieved in other parts of the machine.

For a very large offset of $\Delta y = 12\sigma_y$, the luminosity without feedback, is only 3.5% of the nominal value. If the feedback has the required correction range, it can recover 73% of the full luminosity. For the experiment, this can make the difference between a complete failure and still acceptable running conditions.

For CLIC, the machine with a centre-of-mass energy of 1 TeV is simulated. At higher energies, $E_{cm} = 3$ TeV or $E_{cm} = 5$ TeV, a large number of electrons and positrons will be produced during the collision of the two beams, in a process called coherent pair creation [6]; already at $E_{cm} = 3$ TeV, the number of these particles is about 20% of the number of beam particles. They induce a strong signal in the BPM, and due to their large angle could even hit it. Their properties need to be studied in detail before one can suggest a feedback for the high energy machines.

In CLIC at $E_{cm} = 1$ TeV, the feedback response time is assumed to be the same as in NLC. With the optimum gain $g = 0.005$, the luminosity loss is reduced by a factor 3. This is not as good as in NLC, since the bunch trains are shorter in CLIC. A BPM resolution of $\sigma_{BPM} = 15 \mu m$ leads to a luminosity loss of only $\Delta L/L = 1.2 \times 10^{-4}$. This is better than in NLC because of the lower gain and the slightly larger kick angle for an offset of $\Delta y = \sigma_y$.

5 INFLUENCE OF ANGLES

If the beams at the IP have angle jitters, this reduces the luminosity. In addition, the BPM measures the additional angle and the feedback tries to correct a non-existing offset. The latter problem can be solved by measuring the incoming beam angle error and subtracting it from the value measured by the feedback. Two options are discussed in reference [7], one suggested by M. Breidenbach. Both have some difficulties and neither correct the angle error, but only its effect on the position feedback. As shown below, this is not sufficient, because the luminosity loss will stay large. If the angle jitter is significant, an additional angle feedback is needed for each beam, as described below.

6 ANGLE FEEDBACK MODEL

Each angle feedback consists of a BPM and a strip-line kicker which are placed in the beam delivery section before the detector, see Fig. [5]. This assumes that the angle jitter is created before this system, as is to be expected. The BPM has to be at a phase advance of $(n + k + \frac{1}{2})\pi$ from the IP.
where an angle error at the IP can be measured as a position error. The kicker has to be closer to the IP at \( n\pi \), to be able to transport the signal in the same direction as the beam. Here, the angle at the IP can be corrected by applying a kick. One needs large beta-functions, at the BPM to have a small divergence and thus correction angle. Possible positions exist in the beam delivery system \([8]\). The kick angles have to be significantly larger than for the offset feedback \([7]\), and it may be difficult to achieve this.

This feedback is relatively simple, and uses a constant gain for each bunch. The response time \( \tau_d \) is given by equation \([4]\). In the present case \( \tau_{pf} \) is negative, since the beam reaches the BPM before the IP. With signal transmission at the speed of light, one would obtain \( \tau_s + \tau_{pf} + \tau_{kf} = 0 \) and consequently \( \tau_d = \tau_p + \tau_k \). In the following, \( \tau_d = 15 \) ns is assumed.

### 7 RESULTS OF ANGLE FEEDBACK

The angle feedback is simulated for NLC. The optimum gain is determined in the same way as for the position feedback. If only angle errors were present, the luminosity loss would be reduced by a factor 6, as for the position feedback.

The required resolution for the BPM depends on the vertical beta-function at its position. It must correspond to a resolution of the beam angle in the IP of \( 0.2\sigma_y \), to achieve a luminosity loss of only \( \Delta L/L = 10^{-3} \) for perfect beams.

Finally, the combination of angle and position error is considered. Figure \([5]\) shows the fractional luminosity loss for a constant beam position error of \( \Delta y = 2\sigma_y \) as a function of the angle error. If no feedback is used, the luminosity loss is high. An additional angle error can increase it even more. If only a position feedback is used, which does not correct the angle error of the incoming beam, the luminosity loss is small as long as the angle errors are small. If \( \Delta y/\sigma_y \) becomes comparable to \( \Delta y/\sigma_y \), the loss is almost the same as without feedback. If one measures the incoming angle, and subtracts it from the measured value, the situation does not improve very much. If finally, a position feedback at the IP and an angle feedback for each beam are used, the luminosity loss is significantly reduced, independent of the initial angle error.

### 8 CONCLUSION

If the appropriate hardware can be built, the intra-pulse feedback at the interaction point offers a reduction of the luminosity loss due to pulse-to-pulse jitter by a factor of about 6 in NLC and 3 in CLIC. Even in case of a very large offset of 12 times the beam size, more than 70% of the luminosity is recovered in NLC. Without feedback the luminosity would be almost zero.

If the angle jitter is significant, it is not sufficient to correct the measured kick angle accordingly. To reduce the luminosity loss due to the angle errors, the described angle feedback is necessary. Whether it is feasible needs to be studied.

### 9 ACKNOWLEDGEMENTS

I would like to thank T. Raubenheimer for inviting me to SLAC, where I did most of the work presented. I am grateful to M. Breidenbach, P. Emma, J. Frisch, G. Haller, T. Raubenheimer and P. Tennenbaum for very helpful discussions.

### 10 REFERENCES

[1] NLC parameters can be found under URL [http://www-project.slac.stanford.edu/lc/local/AccelPhysics/AccelPhysics/AccelPhysics/index.htm](http://www-project.slac.stanford.edu/lc/local/AccelPhysics/AccelPhysics/index.htm).

[2] J.-P. Delahaye. The CLIC Study of a Multi-TeV e+e− Linear Collider. CERN/PS 99-005 (LP) (1999).

[3] D. Schulte. Study of Electromagnetic and Hadronic Background in the Interaction Region of the TESLA Collider. Phd thesis. TESLA-97-08 (1996).

[4] G. Haller, M. Breidenbach. Private communication.

[5] J. Frisch. Private communication.

[6] D. Schulte. High Energy Beam-Beam Effects in CLIC. PAC 1999, New York, USA and CERN/PS 99-017 (LP) (1999).

[7] D. Schulte. Simulation of an Intra-Pulse Interaction Point Feedback for the NLC. CLIC-Note 415 (1999).

[8] T. Raubenheimer and P. Tennenbaum. Private communication.