Generation of heralded single photons beyond 1100 nm by spontaneous four-wave mixing in a side-stressed femtosecond laser-written waveguide

Zhizhong Yan, Yuwen Duan, L. G. Helt, Martin Ams, Michael J. Withford, and M. J. Steel
Centre for Ultrahigh bandwidth Devices for Optical Systems (CUDOS), MQ Photonics Research Centre, Department of Physics and Astronomy, Macquarie University, NSW 2109, Australia
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We demonstrate a monolithically integrable heralded photon source in a femtosecond laser direct written glass waveguide. The generation of photon pairs with a wide wavelength separation requires a concomitant large birefringence in the normal dispersion regime. Here, by incorporation of side-stress tracks, we produce a waveguide with a birefringence of $1.64 \times 10^{-4}$ and propagation loss as low as 0.21 dB/cm near 980 nm. We measure photon pairs with 300 nm wavelength separation at an internal generation rate exceeding $5.05 \times 10^6$/s. The second order correlations indicate that the generated photon pairs are in a strongly non-classical regime.

As the field of quantum integrated photonics has emerged over the last decade, a range of device platforms have been explored. One approach that offers complementary capabilities to traditional planar technologies is the direct inscription of waveguides in glass by a femtosecond laser [1,4]. The ability of the femtosecond laser direct write (FLDW) platform to write 3D circuits, manipulate polarization and incorporate tunability has enabled demonstrations of numerous quantum phenomena [5] including multiple photon interference [6], quantum walks [7,8], boson sampling [9,10], complex state preparation [11], and novel interferometry [12–14].

While the FLDW approach has proven flexible for photon processing, ultimately quantum photonics applications demand integration of photon sources and detectors in the same device. A common approach in other chip platforms is to use spontaneous nonlinear processes to generate correlated photon pairs [15]. Detection of a herald photon in one wavelength band or polarization state flags the imminent arrival of a partner photon in a complementary band or mode. Given the ubiquity of telecom fibers in the infrared and photon detectors in the visible, the two bands of 1530–1565 nm and 600–850 nm are both important target wavelength ranges for photon generation. Indeed creating one photon in each band is attractive as the short wavelength “signal” may be detected with efficient silicon avalanche photodiodes (APD) while the long wavelength “idler” is suitable for transport over fiber. In FLDW waveguides, however, the limited nonlinearity of silica-based glasses ($\sim 10^{-20}$ m$^2$/W) and typical waveguide lengths (under $\sim$10 cm), mean a photon generation strategy based on nonlinear optics might seem challenging. Nonetheless, classical nonlinear optics in laser written waveguides has been explored to a limited extent [16,17]. Moreover, some fibre sources of photon pairs are only centimeters long [18,19] and have optical mode areas comparable to FLDW waveguides [20], suggesting that correlated pair generation in silica FLDW waveguides is in fact viable.

In 2013, Spring et al. [21] reported photon pair generation by spontaneous four wave mixing (SFWM) in a silica laser written waveguide. Their experiment used a Ti:sapphire oscillator at $\lambda_p = 729$ nm as a pump source to generate signal and idler photons centered at $\lambda_s = 676$ nm and $\lambda_i = 790$ nm. The device has the added benefit of avoiding contamination from noise due to spontaneous Raman scattering which extends only up to $\sim 20$ THz from the pump, whereas the pump-idler separation was $\sim 64$ THz. A key to this experiment was the use of the form birefringence of the mildly elliptical waveguide to enable phase-matching despite the significant signal-idler separation.

In the present work, we take the next steps toward a telecom-band heralded photon source in silica FLDW waveguides by generating widely-separated pairs with the signal photons in the near-visible silicon APD band, and the idler photons reaching the sensitivity range of InGaAsP single photon detectors. Since the refractive index contrast of laser written waveguides is relatively small [6] (typically below $5 \times 10^{-3}$), the potential to significantly increase form birefringence so as to extend the signal-idler separation is likely small. Furthermore, large form birefringence also increases the coupling loss for monolithic integration to quantum photonic circuits, which usually rely on waveguides with several orders lower birefringence [9]. Thus, to achieve the required birefringence and provide a path towards even-larger birefringence and larger frequency shifts, we exploit the concept of stress-induced birefringence induced by a pair of additional FLDW tracks written parallel to the central waveguide [22]. With a pump at $\lambda_p = 957$ nm we generate photons centered at $\lambda_s = 830$ nm and $\lambda_i = 1130$ nm, the signal photons having a purity of approximately 0.93.

The details of our device are as follows. The central waveguide and side stress tracks (see Fig. 1 inset) were fabricated in a fused silica sample (Schott Lithosil) using a regeneratively amplified Ti:sapphire laser at 800 nm...
(repetition rate 1 kHz, pulse duration 120 fs). The laser beam was circularly polarized and focused into the glass with a 20× (NA 0.46) microscope objective at a depth of 170 μm below the surface. A slit was placed in the beam path to produce waveguides with a circular cross section [23]. For the central waveguides, eight writing passes were used to achieve the lowest propagation losses, with a pulse energy of 1.1 μJ. The total length of the central waveguide was 30 mm. Similar writing conditions were used for the stress side tracks, except that no slit was used and the pulse energy for the stress tracks was 0.3 μJ, much lower than that for writing the waveguides, while three writing passes were applied.

The two stress tracks were positioned 16 μm either side of the central waveguide. The stress tracks begin and end 2 mm in from the input and output facets, so that the total effective length of the region with enhanced birefringence is 26 mm. The propagation loss was measured by transmission measurements at three wavelengths, subtracting estimates of the coupling loss obtained from mode profile measurements. The measured losses were 0.29 dB/cm (λ = 808 nm), 0.21 dB/cm (980 nm) and 2.9 dB/cm (1550 nm), where the much larger loss at the longer wavelength is attributed to the more extended mode field interacting strongly with the stress field.

As the precise stress field and consequent effects of the stress tracks is difficult to model, we conducted a series of classical measurements to learn as much as possible about the phase matching conditions in our device before proceeding to quantum measurements. We first measured mode field diameters (MFDs) and polarization rotations to obtain a rough estimate of the birefringence; then refined this approximation with classical FWM measurements. Figure 1 shows MFD measurements at four wavelengths. The solid line is a fit to the MFD as a function of V-number [24] approximating the waveguide as a step-index device. Identifying an effective waveguide diameter of 6.1 μm (consistent with the DIC microscope measurement as shown in the inset to Fig. 1), we extract an estimate of the peak refractive index change in the central waveguide as 4 × 10^{-3}. Based on these measurements and silica material dispersion [25], we can calculate the expected phase-matching curves as a function of the pump laser wavelength for several conceivable values of birefringence, assuming that the birefringence is wavelength independent (see Fig. 2). In fact, as seen below, there will likely be some reduction in the birefringence with wavelength, but the precise amount is not understood at this time. The vertical line in Fig. 2 indicates the phase-matched signal and idler wavelengths if the pump is at 957 nm.

To obtain an estimate of the birefringence, as the expected beat length is on the mm scale, we took polarization rotation measurements at a range of wavelengths centered at 960 nm. Simple analysis [24] then indicates a birefringence value of order 1.8 ± 0.3 × 10^{-4} with the slow axis in the vertical direction (perpendicular to the line joining the side-stress features). To verify this measurement we performed a classical four wave mixing experiment using a tunable femtosecond Ti-Sapphire laser (Coherent Chameleon, 80 MHz repetition rate, 140 fs pulse width) to pump the FLDW waveguide. In the following, values of pump power were determined at the output facet of the chip for all parts of the experiment including the SFWM. We achieved more than 35 % throughput from the input to the output facet at wavelengths near

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**FIG. 1.** Measured MFD at four wavelengths (635 nm, 808 nm, 980 nm and 1550 nm) in horizontal (MFD_x) and vertical (MFD_y) directions. Mode profile images are shown for 808 nm and 1550 nm, respectively. The solid curve is a fit to the MFD based on a step-index approximation for the waveguide. The larger inset shows a differential interference contrast (DIC) microscopy image of the waveguide seen from above.

**FIG. 2.** Calculated phase-matching curves under cross-polarization conditions of a fused silica FLDW waveguide using the same dimensions in Fig. 1, assuming constant birefringence values of 1.0 × 10^{-4} (blue, dash-dot line), 1.64 × 10^{-4} (red, solid line), 2.5 × 10^{-4} (green, dot line), and 4.0 × 10^{-4} (brown, dash line). The dashed line and dots indicate the operating parameters for the quantum characterization, with the black dot marking the idler wavelength for a birefringence of 1.64 × 10^{-4}.
800 nm with power readings over 500 mW for the classical FWM. A continuous wave diode laser with wavelength fixed at 976 nm was applied to seed the idler (long-wavelength) channel. The pump was launched with vertical polarisation and the seed laser with horizontal polarisation with the input beams combined on a polarisation beam splitter cube. The signal power spectrum at the output was collected by an optical spectrum analyser (OSA) after polarisation filtering to remove the strong pump power, followed by two short pass filters at 750 nm (cut-off suppression > 50 dB each). Due to the short waveguide length, the phase matching condition permitted a continuously observable signal spectrum above the noise level (-85 dBm) of the OSA over a pump tuning range of 838 nm to 848 nm. In the test, we also switched off the pump and seed lasers separately to confirm the FWM origin of the signal. By monitoring the power in the signal band around 737 nm, we extracted a birefringence in a range from 1.9 × 10⁻⁴ to 2.13 × 10⁻⁴, and verified the earlier identification of the vertical axis as the slow axis.

In developing the correlated photon pair source, our goal was to push the idler band as far as possible into the infrared entering the sensitivity regime of InGaAs single photon detectors (SPDs). In this work, we used a free-running InGaAs SPD (id-Quantique id-220). At the same time we wished to keep the signal photons in the detection band of silicon APD detectors. This was achieved by a shift in the pump wavelength into a range around 950 nm, which raises the question of whether the level of birefringence will be maintained with longer wavelength operation. Form birefringence, which is dominated by the regions of most rapid index change, is commonly relatively independent of wavelength. However, in our case the birefringence derives from the spatial sampling by the optical mode of the stress field around the central waveguide and the wavelength dependence of the mode area (see Fig. 1) is likely to vary this sampling and alter the birefringence. Unfortunately, the longer pump wavelength leads to significantly reduced available power (<150 mW) which was insufficient to observe a classical FWM signal with the OSA. Nevertheless, our classical characterization was sufficient to direct us to the correct wavelength ranges for observing spontaneous four wave mixing.

In the SFWM process, the expected photon pair rate is proportional to $\Delta \nu \left( \frac{\gamma P_0 L_{\text{eff}}}{4} \right)^2 \text{sinc}^2 \left( \Delta k L_{\text{eff}}/2 \right)$ where $P_0$ is the pump power, and $L_{\text{eff}}$ is the effective length that is limited by the propagation loss in the FLDW waveguide. The phase-matching term $\Delta k = 2k_p - k_i - k_s + \frac{3}{2} \gamma P_0$ is the same form as arises in the classical case, while $\Delta \nu$ is the effective bandwidth of the photon collection optics, here set by the 3 nm bandpass filter (BPF) in the signal arm.

Keeping the pump power $P_0$ constant at 100 mW, we let the pump wavelength vary, and monitored the singles count rate for the signal channel at 830 nm. This rate is expected to be modulated by the phase-matching conditions as the pump is tuned. The measured signal counts are shown as a function of the pump wavelength in Fig. 3 for two sample waveguides (solid lines). The maximum count rate for the first waveguide (#1) occurred at $\lambda_p = 957$ nm. For completeness, a second waveguide (#2) was also analysed. In this case the maximum count rate occurred at $\lambda_p = 958$ nm implying excellent reproducibility of the fabrication process, which promises generation of highly indistinguishable heralded photons. The dashed curve shows a calculation of the expected normalised rate $\text{sinc}^2 \left( \Delta k L_{\text{eff}}/2 \right)$ for a birefringence of $1.64 \times 10^{-4}$. The maximum value for waveguide (#1) is 977 CPS/mW, waveguide (#2) is 966 CPS/mW, both at 100 mW pump power.

![FIG. 3. Normalized signal singles counts (at 830 nm) as a function of pump wavelength in the SFWM regime. The dashed curve shows the numerical calculation of the expected normalised rate $\text{sinc}^2 \left( \Delta k L_{\text{eff}}/2 \right)$ for a birefringence of $1.64 \times 10^{-4}$. The maximum value for waveguide (#1) is 977 CPS/mW, waveguide (#2) is 966 CPS/mW, both at 100 mW pump power.](image-url)
830 nm of $\sim 40\%$. The detector for the idler arm is an InGaAs infrared free-running single photon detector (id-Quantique id-220, with detection efficiency set to 20% and 10 $\mu$s dead time). The signal and idler count rates are shown in Fig. 5 (a). Note that the much longer dead time of the idler photon detector compared to the signal detector significantly degrades the effective detection time window when it detects higher rates of photon flux, leading to a reduction in the detection efficiency proportional to the idler photon rate. The detector thus exhibits a sub-quadratic (here approximately linear) dependence on the pump power Fig. 5 (b) shows the detected pairs by one silicon APD for signal photons and one InGaAs free-running detector (8% detector efficiency at 1130 nm) for idler photons. The optical coupling efficiencies are 11% and 2% in the idler arm and signal arm, respectively. These efficiencies were evaluated by comparing the ratio between the correlated pair counts and the singles counts in each arm excluding both detector inefficiencies. The losses include the contribution from the pair generation setup before the photon detection. The main source of loss is optical coupling from free space to the single mode fiber. The higher loss in the signal arm is associated with reflection loss from the dichroic mirror and the bandpass filter. Taking into account these losses, we estimate the internal pair generation rate to be $\approx 5.05 \times 10^9$ per second at 135 mW pump power.

To confirm the non-classical nature of the non-linear optical process, we studied the photon correlations through unheralded second order correlation function measurements [21]. Non-classical correlations are indicated by the violation of the Cauchy-Schwarz inequality

$$\left( g^{(2)}_{\text{ss}}[0] \right)^2 \leq g^{(2)}_{\text{ii}}[0] \cdot g^{(2)}_{\text{si}}[0] \cdot g^{(2)}_{\text{is}}[0],$$

where $g^{(2)}_{\text{ss}}[0]$, $g^{(2)}_{\text{ii}}[0]$, $g^{(2)}_{\text{si}}[0]$ are the self and one cross second order correlation functions.

The unheralded $g^{(2)}_{\text{ss}}[0]$ in the signal arm is obtained after polarisation filtering and spectral filtering (830/3 nm) to be $1.93 \pm 0.14$ at 135 mW pump power. This indicates that the single photons of the signal arm has a Schmidt mode purity of $\sim 93\%$. The unheralded $g^{(2)}_{\text{ii}}[0]$ is measured to be $1.21 \pm 0.50$ under this condition. Both $g^{(2)}_{\text{ss}}[0]$ and $g^{(2)}_{\text{ii}}[0]$ were measured by coupling the signal/idler arm photons into a 50:50 fibre coupler individually. The specific idler wavelength also limits the choice of suitable bandpass filter. If we were able to filter the idler arm to a bandwidth of 3 nm centred at 1130 nm, we would expect a similar Schmidt mode purity of $93\%$ as in the signal arm, however this would also reduce the rate of idler photons reaching the detector by around 90%, as the current unfiltered idler bandwidth is calculated to be approximately 30 nm.

The cross second order correlation $g^{(2)}_{\text{si}}[0]$ at the same pump power is $16.49 \pm 0.43$. Thus the violation of the Cauchy-Schwarz inequality is more than 26 standard de-
viations at the highest pump power level. Alternatively, the classical limit shown as the dashed line intersecting the right y-axis in Fig. 5(a) was obtained because no unheralded $g^{(2)}_{ss(ii)}[0]$ can exceed 2. From the plot, one can also conclude that the violation of the inequality holds for the entire range of pump powers.

The strong violation of the Cauchy-Schwarz inequality has confirmed that the SFWM result is within the quantum mechanical regime. The experimental SFWM result has demonstrated over 300 nm signal and idler separation. By adding stress tracks on both sides of a very low form birefringence waveguide, the source promises seamless integration with the photonic circuits on the same chip. The solution in this work provides opportunities not only for realizing telecom band idler photons while keeping signal photons in the efficient APD detection wavelength regime; but also for paving the critical way for monolithic photon generation and quantum states preparation on FLDW glass chips.

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