Secular Evolution in Disk Galaxies

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Abstract

Self-gravitating systems evolve toward the most tightly bound configuration that is reachable via the evolution processes that are available to them. They do this by spreading – the inner parts shrink while the outer parts expand – provided that some physical process efficiently transports energy or angular momentum outward. The reason is that self-gravitating systems have negative specific heats. As a result, the evolution of stars, star clusters, protostellar and protoplanetary disks, black hole accretion disks and galaxy disks are fundamentally similar. How evolution proceeds then depends on the evolution processes that are available to each kind of self-gravitating system. These processes and their consequences for galaxy disks are the subjects of my lectures and of this Canary Islands Winter School.

I begin with a review of the formation, growth and death of bars. Then I review the slow (“secular”) rearrangement of energy, angular momentum, and mass that results from interactions between stars or gas clouds and collective phenomena such as bars, oval disks, spiral structure and triaxial dark halos. The “existence-proof” phase of this work is largely over: we have a good heuristic understanding of how nonaxisymmetric structures rearrange disk gas into outer rings, inner rings and stuff dumped onto the center. The results of simulations correspond closely to the morphology of barred and oval galaxies. Gas that is transported to small radii reaches high densities. Observations confirm that many barred and oval galaxies have dense central concentrations of gas and star formation. The result is to grow, on timescales of a few Gyr, dense central components that are frequently mistaken for classical (elliptical-galaxy-like) bulges but that were grown slowly out of the disk (not made rapidly by major mergers). The resulting picture of secular galaxy evolution accounts for the richness observed in galaxy structure.
We can distinguish between classical and pseudo bulges because the latter retain a "memory" of their disky origin. That is, they have one or more characteristics of disks: (1) flatter shapes than those of classical bulges, (2) correspondingly large ratios of ordered to random velocities, (3) small velocity dispersions $\sigma$ with respect to the Faber-Jackson correlation between $\sigma$ and bulge luminosity, (4) spiral structure or nuclear bars in the "bulge" part of the light profile, (5) nearly exponential brightness profiles and (6) starbursts. So the cleanest examples of pseudobulges are recognizable. However, pseudo and classical bulges can coexist in the same galaxy.

I review two important implications of secular evolution:

(1) The existence of pseudobulges highlights a problem with our theory of galaxy formation by hierarchical clustering. We cannot explain galaxies that are completely bulgeless. Galaxy mergers are expected to happen often enough so that every giant galaxy should have a classical bulge. But we observe that bulgeless giant galaxies are common in field environments. We now realize that many dense centers of galaxies that we used to think are bulges were not made by mergers; they were grown out of disks. So the challenge gets more difficult. This is the biggest problem faced by our theory of galaxy formation.

(2) Pseudobulges are observed to contain supermassive black holes (BHs), but they do not show the well known, tight correlations between BH mass and the mass and velocity dispersion of the host bulge. This leads to the suggestion that there are two fundamentally different BH feeding processes. Rapid global inward gas transport in galaxy mergers leads to giant BHs that correlate with host ellipticals and classical bulges, whereas local and more stochastic feeding of small BHs in largely bulgeless galaxies evidently involves too little energy feedback to result in BH-host coevolution. It is an important success of the secular evolution picture that morphological differences can be used to divide bulges into two types that correlate differently with their BHs.

I review environmental secular evolution—the transformation of gas-rich, star-forming spiral and irregular galaxies into gas-poor, "red and dead" S0 and spheroidal ("Sph") galaxies. I show that Sph galaxies such as NGC 205 and Draco are not the low-luminosity end of the structural sequence (the "fundamental plane") of elliptical galaxies. Instead, Sph galaxies have structural parameters like those of low-luminosity S+Im galaxies. Spheroidals are continuous in their structural parameters with the disks of S0 galaxies. They are bulgeless S0s. S+Im $\rightarrow$ S0+Sph transformation involves a variety of internal (supernova-driven baryon ejection) and environmental processes (e.g., ram-pressure gas stripping, harassment, and starvation).

Finally, I summarize how hierarchical clustering and secular processes can be combined into a consistent and comprehensive picture of galaxy evolution.
1.1 Introduction

These lectures review the slow ("secular") evolution of disk galaxies, both internally and environmentally driven. As a heuristic introduction at a 2011 winter school, they emphasize a qualitative and intuitive understanding of physical processes. This provides a useful complement to Kormendy & Kennicutt (2004), which is a more complete review of technical details and the literature. Since this is a school, my lectures will be as self-contained as possible. There will therefore be some overlap with the above review and with Kormendy (1981, 1982b, 1993b, 2008a, b); Kormendy & Cornell (2004); Kormendy & Fisher (2005, 2008) and Kormendy & Bender (2012).

1.1.1 Outline

The secular evolution of disk galaxies has deep similarities to the evolution of all other kinds of self-gravitating systems. I begin by emphasizing these similarities. In particular, the growth of pseudobulges in galaxy disks is as fundamental as the growth of stars in protostellar disks, the growth of black holes in black hole accretion disks and the growth of proto-white-dwarf cores in red giant stars. A big-picture understanding of these similarities is conceptually very important. The associated physics allows us to understand what kinds of galaxies evolve secularly and what kinds do not. This review discusses only disk galaxies; secular evolution of ellipticals is also important but is less thoroughly studied.

Galaxy bars are important as "engines" that drive secular evolution, so I provide a heuristic introduction to how bars grow and how they die. Then I review in some detail the evolution processes that are driven by bars and by oval disks and the formation of the various kinds of structures that are built by these processes. I particularly emphasize the growth and properties of pseudobulges. Based on this, I summarize how we recognize pseudobulges and connect them up with our overall picture of galaxy formation.

Two consequences (among many) of secular evolution are particularly important. I review the problem of understanding pure-disk galaxies. These are galaxies that do not contain classical bulges. We infer that they have not experienced a major merger since the first substantial star formation. Many have barely experienced secular evolution. We do not know how these galaxies are formed. Second, I review evidence that classical bulges coevolve with their supermassive black holes but pseudobulges do not.

Next, I discuss secular evolution that is environmentally driven. Here, I concentrate on the evidence that gas-rich, star forming spiral and irregular galaxies are transformed into gas-poor, "red and dead" S0 and spheroidal
galaxies. I particularly emphasize the properties of spheroidals – that is, tiny dwarfs such as Fornax, Draco and UMi and larger systems such as NGC 147, NGC 185 and NGC 205. These are, in essence, bulgeless S0 galaxies. And I review the various transformation processes that may make these objects.

Finally, I tie together our picture of galaxy formation by hierarchical clustering and galaxy merging (lectures by Isaac Shlosman, Nick Scoville and Daniela Calzetti) and the secular evolution that is the theme of this School.

### 1.1.2 Fast versus slow processes of galaxy evolution

Kormendy & Kennicutt (2004) emphasize that the Universe is in transition from early times when galaxy evolution was dominated by fast processes – hierarchical clustering and galaxy merging – to a future when merging will largely be over and evolution will be dominated by slow processes (Fig. 1.1).

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Fig. 1.1. Processes of galaxy evolution updated from Kormendy (1982b) and from Kormendy & Kennicutt (2004). Processes are divided vertically into fast (top) and slow (bottom). Fast evolution happens on a free-fall (“dynamical”) timescale, \( t_{\text{dyn}} \sim (G\rho)^{-1/2} \), where \( \rho \) is the density of the object produced and \( G \) is the gravitational constant. Slow means many galaxy rotation periods. Processes are divided horizontally into ones that happen internally in one galaxy (left) and ones that are driven by environmental effects (right). The processes at center are aspects of all types of galaxy evolution. My lectures are about slow processes, both internal (Sections 1.2 – 1.6) and environmentally driven (Section 1.7).
We have a well developed picture of galaxy formation that mostly involves the processes in the upper-right corner of Fig. 1.1. Quantum density fluctuations in non-baryonic, dynamically cold dark matter form immediately after the Big Bang and then get stretched by the expansion of the Universe. Gravity drives hierarchical clustering that causes these fluctuations to grow, separate out from the expansion of the Universe, collapse and form galaxy halos. The baryons first go along for the ride and later cool inside the halos to form stars and visible galaxies. Spiral galaxies form when halos quiescently accrete gas that dissipates and forms disks. Ellipticals form when galaxies collide and merge; then dynamical violence scrambles disks into ellipsoidal ellipticals. It is a convincing story, developed in Toomre (1977a); White & Rees (1978); Kauffmann et al. (1993); Steinmetz & Navarro (2002, 2003), and many other papers. Quoting Binney (2004), “Cold Dark Matter theory has now reached the point at which it should be admitted as a Candidate Member to the Academy of Established Theories, so that it can sit alongside the established theories of Maxwell, Einstein, and Heisenberg.”

Now we are making a transition to a time in the far future when the Universe will have expanded so much that most mergers that ever will happen will already have happened. Even now, major mergers – defined as ones in which the less-massive progenitor is within a factor of (say) 5–10 of the mass of the bigger progenitor – are uncommon. Minor mergers remain common now but will also get less common in the future. As this happens, more and more galaxies spend more and more of their time not undergoing fast and violent evolution events. And between such events – that is, between galaxy collisions and mergers – galaxies in isolation do not just sit and age their stars. Instead, galaxies evolve on slow timescales; that is, timescales that are much longer than the crossing time or the collapse time. We call such slow processes “secular”. At present, both fast and slow processes are important. It is easy to find (especially in cluster environments) good examples of galaxies whose histories have been dominated by fast processes. They are the ellipticals and the classical bulges of disk galaxies. Elsewhere (particularly in field environments), it is easy to find galaxies whose evolution has almost entirely been secular. Both of these types of galaxies are relatively easy to recognize. But it is also important to understand that both kinds of processes can be important in a single galaxy, and in particular, that a galaxy can contain both a classical (merger-built) bulge and a pseudo (secularly built) bulge. Recognizing this is difficult and indeed not always possible. We will spend some considerable effort on understanding how to differentiate classical and pseudo bulges.
Beginning with the seminal paper of Toomre (1977a), most work on galaxy formation over the last 35 years has concentrated on hierarchical clustering. The idea of secular evolution got its start at almost the same time; some of the earliest papers on the subject are Kormendy (1979a, 1979b, 1981) and Combes & Sanders (1981). But research on this subject remained for many years a series of largely isolated “cottage industries” that did not penetrate the astronomical folklore. This changed very rapidly in the last decade. In particular, Kormendy & Kennicutt (2004) aimed to combine the cottage industries into a general and well articulate paradigm on secular evolution that complements hierarchical clustering. Now, this subject has become a major industry. Whole meetings have been devoted to it. This is the motivation that underlies the present Canary Islands Winter School.

1.1.3 A comment about the name “pseudobulges”

As in Kormendy & Kennicutt (2004), I use the name “pseudobulge” for all high-density, distinct central components of galaxies that are grown slowly out of disks and not rapidly by galaxy mergers. They divide themselves into at least three subtypes that involve different formation processes. Boxy bulges in edge-on galaxies are bars seen side-on (Combes & Sanders 1981). Bars are disk phenomena. I will call these “boxy pseudobulges”. Second, dense central components are grown out of disks when nonaxisymmetries transport gas toward the center where it feeds starbursts. Often, these are recognizably more disky than merger-built bulges. But they are not guaranteed to be flat. Still, it is often useful to refer to them as “disky pseudobulges” when we need to differentiate them from boxy pseudobulges. Third, nuclear bars are a recognizably distinct subset of disky pseudobulges. What problem am I trying to solve by calling all of these “pseudobulges”?

Astronomers have a long history of inventing awkward names for things. For historical reasons, we have two different names for the products of major galaxy mergers. If a merger remnant does not have a disk around it, we call it an “elliptical”. But if an elliptical subsequently accretes cold gas and grows a new disk (e.g., Steinmetz & Navarro 2002), then we call it a “bulge”. In particular, I will call it a “classical bulge”. This is inconvenient when one wants to refer to all elliptical-galaxy-like merger remnants without prejudice as to whether they have associated disks. Some authors call these “spheroidal galaxies”. This is exceedingly misleading, because the same name is used for dwarf galaxies such as Draco and Fornax that are essentially bulgeless S0s (see Section 1.7 here). Another alternative is to call them “hot stellar systems”. This is misleading, because some ellipticals
have lower velocity dispersions than some pseudobulges and indeed also than some lenses (which certainly are disk components). I could define the term “ellipsoids” to mean both classical bulges and ellipticals. But this name has no constituency. So I will explicitly say “bulges and ellipticals” when I need to refer to both at once.

I do not want the same problem to happen with pseudobulges.

1.2 Self-gravitating systems evolve by spreading

This is the most fundamental section of this review. I want to give you a heuristic, intuitive understanding of why secular evolution happens in disk galaxies. And I want to show you how the evolution of essentially all self-gravitating systems is fundamentally similar. The theme of this Winter School is the disk-galaxy version of that more general evolution.

I made this point in Kormendy & Fisher (2008) and in Kormendy (2008a). However, it is important enough – especially at a school – that I repeat it here in detail. The following is a slightly expanded and paraphrased version of the discussion in Kormendy (2008a).

The general principle that drives the evolution of self-gravitating systems is this: it is energetically favorable to spread. That is, as energy or angular momentum is transported outward, the inner parts shrink and grow denser, while the outer parts expand, grow more diffuse, and, in some cases, escape the system. How to see this depends on whether the system is dominated by rotation or by random motions.

1.2.1 If dynamical support is by random motions

For systems that are dominated by velocity dispersion, the argument is given by Lynden-Bell & Wood (1968) and by Binney & Tremaine (1987). The essential point is that the specific heat of a self-gravitating system is negative. Consider an equilibrium system of $N$ particles of mass $m$, radius $r$ and three-dimensional velocity dispersion $v$. The virial theorem tells us that $2\text{KE} + \text{PE} = 0$, where the kinetic energy is $\text{KE} = Nm v^2/2$ and the potential energy is $\text{PE} = -G(Nm)^2/r$. The total energy $E \equiv \text{KE} + \text{PE} = -\text{KE}$ is negative. This is what it means to be a bound system. But the temperature of the system is measured by $v^2$: $mv^2/2 = 3kT/2$. So the specific heat $C \equiv dE/dT \propto d(-Nm v^2/2)/d(v^2)$ is also negative. In the above, $G$ is the gravitational constant and $k$ is Boltzmann’s constant.

The system is supported by heat, so evolution is by heat transport. If the center of the system gets hotter than the periphery, then heat tends to flow
outward. The inner parts shrink and get still hotter. This promotes further heat flow. The outer parts receive heat; they expand and cool. Whether the system evolves on an interesting timescale depends on whether there is an efficient heat-transport mechanism. For example, many globular clusters evolve quickly by two-body relaxation and undergo core collapse. Giant elliptical galaxies – which otherwise would evolve similarly – cannot do so because their relaxation times are much longer than the age of the Universe.

1.2.2 If dynamical support is by rotation

Tremaine (1989) provides a transparent summary of an argument due to Lynden-Bell & Kalnajs (1972) and to Lynden-Bell & Pringle (1974). A disk is supported by rotation, so evolution is by angular momentum transport. The “goal” is to minimize the total energy at fixed total angular momentum. A rotationally supported ring at radius \( r \) in a fixed potential \( \Phi(r) \) has specific energy \( E(r) \) and specific angular momentum \( L(r) \) given by

\[
E(r) = \frac{r}{2} \frac{d\Phi}{dr} + \Phi \quad \text{and} \quad L(r) = \left( r^3 \frac{d\Phi}{dr} \right)^{1/2}.
\] (1.1)

Then \( dE/dL = \Omega(r) \), where \( \Omega = (r^{-1} d\Phi/dr)^{1/2} \) is the angular speed of rotation. Disks spread when a unit mass at radius \( r_2 \) moves outward by gaining angular momentum \( dL \) from a unit mass at radius \( r_1 < r_2 \). This is energetically favorable: the change in energy,

\[
dE = E_1 + E_2 = \left[ -\left( \frac{dE_1}{dL} \right) + \left( \frac{dE_2}{dL} \right) \right] dL = -\Omega_1 + \Omega_2) \right] dL,
\] (1.2)

is negative because \( \Omega(r) \) usually decreases outward. “Thus disk spreading leads to a lower energy state. In general, disk spreading, outward angular momentum flow, and energy dissipation accompany one another in astrophysical disks” (Tremaine 1989).

1.2.3 Spreading in various kinds of self-gravitating systems

The consequences are very general. All of the evolution summarized in Fig. 1.2 happens because of the above physics.

Globular clusters, open clusters and the compact nuclear star clusters in galaxies are supported by random motions. Absent any gas infall, they spread in three dimensions by outward energy transport. The mechanism is two-body relaxation, and the consequences are core collapse and the evaporation of the outer parts.
Stars are spherical systems supported by pressure. They spread in three dimensions by outward energy transport. The mechanisms are radiation or convection mediated by opacity. Punctuated by phases of stability when nuclear reactions replace the energy that is lost, stellar evolution consists of a series of core contractions and envelope expansions. One result is red (super)giants containing cores that will become white dwarfs, neutron stars, or stellar mass black holes.

Protoplanetary disks are supported by rotation; they spread in two dimensions by outward angular momentum transport. The tendency toward energy equipartition between low-mass and high-mass objects has the consequence that big planets sink by flinging smaller planets outward. If the evolution results from the interaction of a big planet with a collective phenomenon such as a spiral density wave in gas or rubble, then the effect is the same. The results are hot Jupiters and colder Neptunes or rubble.

Protostars are spherical systems coupled to circumstellar disks by magnetic fields that wind up because of differential rotation. This drives jets that look one-dimensional but that really are three-dimensional; they
carry away angular momentum and allow the inner circumstellar disk to shrink and accrete onto the star (Shu et al. 1994, 1995).

An accretion disk around a black hole is supported by rotation, so it evolves by angular momentum transport. The evolution happens because of magnetic coupling between various parts of the accretion disk. The details are complicated, but the net effect is that some material flows outward as part of a jet and other material is accreted onto the black hole. Note again that pictures of this process -- whether observations of radio jets or artists’ conceptions of the accretion process -- almost always show narrow jets. But, as in the case of protostars, outward angular momentum transfer must be involved in order for some of the material to accrete onto the black hole.

Galactic disks are supported by rotation. They spread in two dimensions by outward angular momentum transport. Efficient engines are provided by bars and by oval disks. Like all of the above, the evolution is secular -- slow compared to the collapse time or crossing time of the disk. The growth of a pseudobulge in a galactic disk is as natural as the growth of a star in a protostellar disk and as the growth of a black hole in a black hole accretion disk. Only the processes that transport angular momentum are different.

This secular evolution is the subject of my paper and this Winter School.

\section*{1.2.4 What kinds of galaxy disks evolve secularly?}

For secular evolution to happen, a galaxy needs two things. It needs a driving mechanism such as a bar, a globally oval disk (Section 1.3.3), or global spiral structure. And disk spreading must be energetically favorable. Equation (1.2) tells us that it is more energetically favorable to transport angular momentum outward the more the angular rotation velocity $\Omega(r)$ decreases outward. This lets us divide galaxies into three types, as follows.

Galaxies that lack driving agents should not show strong secular evolution. Examples are unbarred galaxies with classical bulges and weak or no global spiral structure (e.g., M 31, NGC 2841 and NGC 4594, the Sombrero Galaxy). We will see that these objects generally do not show centrally concentrated molecular gas and star formation. We take this as an sign that secular evolution largely is not happening.

For galaxies with engines, Fig. 1.3 shows how the tendency to evolve depends on the mass distribution as revealed by the rotation curve $V(r)$. Where $V(r)$ increases proportional to $r$ (or even rather more slowly), the angular rotation velocity $\Omega(r)$ is constant (or very slowly decreasing outward). This means that it is not energetically favorable to evolve. This is the situation in an Scd galaxy like M 33, where we find no pseudobulge.
Fig. 1.3. Typical examples of spiral galaxies that do (NGC 4736, bottom) and do not (M 33, top) have mass distributions that are conducive to secular evolution. The top-left plots (Kormendy & Norman 1979) show a generic rotation curve $V(r)$ and associated angular velocity curves $\Omega(r) \equiv \frac{V(r)}{r}$ and $\Omega - \kappa/2$, where $\kappa$ is the epicyclic frequency. Where $V \propto r$, $\Omega = \text{constant}$ and secular evolution is not energetically favorable. Even where $V(r)$ is turning downward from $V \propto r$ toward $V = \text{constant}$, $\Omega$ decreases outward so slowly that secular evolution is disfavored. This is the situation throughout a galaxy like M 33 (top-right rotation curve and rotation curve decomposition, from Corbelli & Salucci 2000). M 33 has neither a classical bulge nor a significant pseudobulge. In contrast, NGC 4736 (image at bottom-left, from http://www.wikisky.org) has a rotation curve that decreases outward with radius, as derived by de Blok et al. (2008; bottom-right panel here). Disk spreading is energetically very favorable. Moreover, NGC 4736 is a prototypical strongly oval galaxy, so it has an engine for secular evolution. Not surprisingly, it is our best “poster child” for secular evolution – an unbarred galaxy with a pseudobulge identified by five classification criteria (Section 1.5.3).
The Corbelli & Salucci (2000) decomposition of the M 33 rotation curve into contributions due to the stellar disk, the gas disk and the dark matter halo reveals an additional reason why secular evolution is disfavored. The contribution of the dark matter to $V(r)$ is everywhere comparable to or larger than that of the visible matter. But dark halos are dynamically much hotter than disks. They do not participate in disk dynamics. The observation that the self-gravity of the disk is “diluted” by the gravity of the much stiffer halo is a further sign that secular evolution is disfavored.

Kormendy & McClure (1993) show that M 33 contains a nuclear star cluster (like a large globular cluster) but no significant evidence for a pseudobulge.

In contrast, if a galaxy has a flat rotation curve, then $\Omega \propto 1/r$ and secular evolution is energetically favorable (top-left panels of Fig. 1.3). Even more extreme are galaxies in which the rotation curve decreases outward. De Blok et al. (2008) conclude that the rotation curve of NGC 4736 decreases outward (Fig. 1.3, bottom-right). Under these circumstances, secular evolution should be especially important. In fact, NGC 4736 turns out to be our best “poster child” for secular evolution in an unbarred galaxy (see also Fig. 1.6, Section 1.3.3., Fig. 1.8, Fig. 1.28, Fig. 1.31, Fig. 1.35., Fig. 1.38, Table 1.3).

It will turn out that angular momentum redistribution and therefore radial mass transport happens mostly to gas. The need for gas disfavors early-type galaxies and favors late-type galaxies.

Putting all this together, we can already foresee what the observational review in the rest of this paper will reveal: Secular evolution in galaxy disks is, in the current Universe, happening mostly in intermediate-late-type (e.g., Sbc) galaxies. These are the galaxies in which pseudobulges turn out to be most prominent. Secular evolution is too slow to be important in the latest-type galaxies, because the mass distribution is too “fluffy”, and so it is not energetically favorable to transport angular momentum outward. And secular processes no longer transport much gas in S0 and Sa galaxies, because they no longer contain much gas. Nevertheless, (1) purely stellar secular processes are expected to happen in these galaxies, and (2) secular evolution is believed to have been important in the past, because many S0 galaxies are observed to contain disky pseudobulges.

I turn next to a discussion of our motivation and where it will lead us.

† This result depends on the assumption that the gas is on circular orbits everywhere in the galaxy and that asymmetries in the velocity field and in the galaxy image (Fig. 1.3, bottom-left) are due to warps. These assumptions are not valid. NGC 4736 has an oval disk (Bosma et al. 1977; Kormendy 1982b, 1993b; Kormendy & Kennicutt 2004; Fig. 1.8 here). A suitable analysis of the velocity field based on plausible axial ratios for the inner disk and outer ring has not been made. However, it is likely that the true rotation curve decreases outward more slowly than Fig. 1.3 suggests. Nevertheless, disk secular evolution is more energetically favorable in NGC 4736 than it is in most galaxies.
1.3 The study of galaxy evolution – structural components

An important goal of extragalactic astronomy is to understand the structure of galaxies as encoded, e. g., in the classification schemes of Hubble (1936), de Vaucouleurs (1959) and Sandage (1961, 1975). An updated version of Hubble classification is shown in Fig. 1.4, and a perpendicular cut through de Vaucouleurs’ classification volume at stage Sb is shown in Fig. 1.5. For each kind of galaxy, we want to understand the present structure and the formation and evolution processes which created that structure.

Our picture of galaxy formation by hierarchical clustering and our School’s subject of secular evolution are both important in creating the structures in Figs. 1.4 and 1.5. Ellipticals and classical (elliptical-galaxy-like) bulges of disk galaxies form by hierarchical clustering and major mergers. I review this in Section 1.8, and Isaac Shlosman discusses it in his lectures. Bulges are usually classical in S0–Sb galaxies. Secularly built pseudobulges are not distinguished in Hubble classification, but they are already important in some S0s, and they become the usual central component at type Sbc and in later types (Kormendy & Kennicutt 2004). Unlike these permanent components, spiral density waves are temporary features of disks that mostly last only as long as they have driving engines (Toomre 1977b, 1981).

Fig. 1.4. Revised Hubble classification (Kormendy & Bender 1996) recognizing the difference (the “E–E dichotomy”) between boxy, slowly rotating ellipticals that have cores and disky-distorted, more rapidly rotating and coreless ellipticals that are continuous in their properties with S0s. Ellipticals are understood to form via rapid processes; i. e., by major mergers and violent relaxation. These are reviewed in Section 1.8, where I discuss galaxy formation by hierarchical clustering. S0 and spheroidal galaxies (not included in Hubble types) form – I suggest – at least mostly by environmental secular evolution (Section 1.7). Spiral galaxies evolve partly by rapid processes (mergers make classical bulges, shown orange in the figure). However, the evolution of many spirals has been dominated by secular processes, including the formation of pseudobulges (also shown in orange, because Hubble classes do not distinguish between classical and pseudo bulges).
1.3.1 Inner rings “(r)” and outer rings “(R)”

Figure 1.4 omits several regular features in galaxy structure that we need to understand. The most important of these are encoded in de Vaucouleurs’ (1959) more detailed classification, illustrated here in Fig. 1.5. Rotate the “tuning fork” diagram in Fig. 1.4 about the E–S0 axis. In the plane of the page, de Vaucouleurs retains the distinction between unbarred (“SA”) and barred (“SB”) galaxies. The new, third dimension above and below the page is used for the distinction between galaxies that do or do not contain inner rings. Fig. 1.5 is a perpendicular cut through this classification volume.

Fig. 1.5. Perpendicular cut at type Sb through the galaxy classification volume as defined by de Vaucouleurs (1959). I am grateful to Ron Buta for this version from the de Vaucouleurs Atlas of Galaxies (Buta et al. 2007).
Figure 1.6 (top) illustrates the distinction (bottom half of Fig. 1.5) between SB(s) galaxies in which two global spiral arms begin at the ends of the bar and SB(r) galaxies in which there is a ring of stars and gas surrounding the ends of the bar and the spiral arms start somewhere on this ring. In Figures 1.5 and 1.6, there is a prominent, nearly straight dust lane on the rotationally leading side of the bar in SB(s) galaxies. Notwithstanding Fig. 1.5, there is generally no such dust lane in SB(r) bars (Sandage 1975). Note in NGC 2523 that the inner ring is patchy and blue and contains young stars, like the outer disk but unlike the relatively “red and dead” bar and (pseudo)bulge. This is a common property of inner rings.

Fig. 1.6. (top) Contrast SB(s) and SB(r) structure: (left) SB(s)bc galaxy NGC 1300 has two global spiral arms that begin at the ends of the bar. (right) The SB(r)bc galaxy NGC 2523 has a somewhat more multi-armed but still global spiral pattern with arms that begin from the inner ring, not necessarily at the end of the bar. (bottom) Galaxies with outer rings: (left) the (R)SB(lens)0/a galaxy NGC 1291 and (right) the (R)SA(lens)ab galaxy NGC 4736. The latter is a prototypical oval galaxy. It contains a pseudobulge that is identified by no less than five classification criteria from Section 1.5.3. NGC 2523 is a Hubble Heritage image; NGC 2523 is from Adam Block (NOAO/AURA/NSF); NGC 1291 and NGC 4736 are from Kormendy & Kennicutt (2004).
Figure 1.6 (bottom) shows another feature that is recognized by de Vaucouleurs and Sandage although it is not given a separate classification bin in diagrams like Fig. 1.5. Both barred and unbarred galaxies can contain outer rings “(R)” at approximately twice the radius of the inner disk.

The properties of inner and outer rings are discussed (for example) in Kormendy (1979b, 1981, 1982b), Buta (1990, 1995, 2011, 2012), Buta & Crocker (1991), Buta & Combes (1996) and Buta et al. (2007). I particularly use the following.

(a) Inner rings essentially always encircle the end of the bar.
(b) Outer rings typically have radii \(\sim 1.2\) times the radius of the bar. There is no overlap in the distribution of radii of inner and outer rings.
(c) Both inner and outer rings typically contain H\textsubscript{I} gas and star formation.
(d) Inner rings typically have intrinsic axial ratios of \(\sim 0.85 \pm 0.10\) with the long axis parallel to the bar (Buta 1995).
(e) Outer rings typically have intrinsic axial ratios of \(\sim 0.87 \pm 0.14\). In most galaxies, the long axis is perpendicular to the bar (as seen face-on), but a few outer rings are elongated parallel to the bar (Kormendy 1979b; Buta 1995).
(f) Figure 1.5 contains one mistake. There is no continuity between the inner rings in unbarred and barred galaxies. Instead, SA inner rings are similar to nuclear star-forming rings in SB galaxies (see Fig. 1.31 in Section 1.5.1). Nuclear rings are always much smaller than inner rings (Comerón et al. 2010).

All of the above structural properties are natural products of the secular evolution that I review in these lectures.

### 1.3.2 Lens Components “(lens)”

Lenses are the final morphological component that we need to recognize observationally and to understand within our picture of galaxy evolution. There is much confusion in the literature about lenses. It is unfortunate that de Vaucouleurs chose to use the name “lenticular” for S0 galaxies. I empathize: a bulge-dominated, edge-on S0 such as NGC 3115 or NGC 5866 is indeed shaped rather like an edge-on glass lens. But this is due to the combination of a thick bulge and a thin disk; it does not happen because these S0s contain lens components. In fact, most unbarred S0s do not contain lens components, whereas some Sa and Sb galaxies – particularly barred ones – do contain lens components. We need to overcome the confusion that results from use of the misleading name “lenticular galaxy”. In all of my papers including this one, I avoid use of the name “lenticular galaxy” and always call these objects “S0 galaxies”. And I try to identify lens components strictly using the following definition.
A lens component is an elliptical “shelf” in the brightness distribution of a disk galaxy. That is, it has a shallow brightness gradient interior to a sharp outer edge. Typical face-on lenses have axial ratios of \( \sim 0.85 - 0.9 \). Lenses occur most commonly in barred galaxies; then the bar almost always fills the lens in one dimension. NGC 1291 in Fig. 1.6 is an (R)SB(lens)0/a example of this configuration. Lenses can also occur in unbarred galaxies; the prototypical example is the SA(lens)0 galaxy NGC 1553 (Fig. 1.7). It is important to note that there is no overlap in the intrinsic ellipticity distributions of bars and lenses. Bars always have much smaller (pole-on) axial ratios of \( \leq 1/4 \). So bars and lenses are clearly different, even though both occur only in disk galaxies. A lens and an inner ring of the same size can occur together (e.g., NGC 3081). The properties of lenses are established in Kormendy (1979b) and in Buta (2011, 2012); Buta et al. (1996, 2007).

I will argue in Sections 1.4.3.4 – 1.4.3.6 that lenses are defunct bars. That is, following Kormendy (1979b, 1981, 1982b), I suggest that bars evolve away into lenses when the secular evolution that they drive increases the central mass concentration so much that the elongated bar orbits can no longer precess together at the same bar pattern speed \( \Omega_p \).

I use the notation SA(lens) and SB(lens), respectively, for unbarred and barred galaxies with lenses. Buta et al. (2007) uses the letter “el”; I do not do this only because it is difficult to distinguish “el” from the number 1.
It will turn out that lenses, outer rings, inner rings and pseudobulges are like the more familiar classical bulges, bars and disks in the sense that they are distinct components in the structure of galaxies that retain their essential character over many galaxy rotations. They are different from spiral arms, which are density waves in the disk that last—more or less—only as long as the “engine” that drives them. Still, there are many ways in which the above components can be combined into a galaxy. This results in de Vaucouleurs classifications that may be as complicated as (R)SB(r)bc or (R)SB(lens)0/a (NGC 1291 in Fig. 1.6). This complication makes many people uneasy. However, I emphasize: Every letter in such a complicated galaxy classification now has a physical explanation within our picture of secular galaxy evolution. It is a resounding testament to the educated “eyes” of classifiers such as Allan Sandage and Gerard de Vaucouleurs that they could pick out regularities in galaxy structure that ultimately were understandable in terms of galaxy physics.

1.3.3 Oval Disks

Fundamental to our understanding of the engines that drive secular evolution is the observation that many unbarred galaxies nevertheless are not globally axisymmetric. The inner disks of these galaxies typically have intrinsic axial ratios of $\sim 0.85$. Bars are more elongated (typical axial ratio $\sim 0.2$), but a much smaller fraction (typically $\lesssim 1/3$) of the disk participates. Observations indicate that oval disks are approximately as effective in driving secular evolution as are bars.

Oval galaxies can be recognized independently by photometric criteria (Kormendy & Norman 1979; Kormendy 1982b) and by kinematic criteria (Bosma 1981a, b). They are illustrated schematically and with observations of prototypical galaxies in Fig. 1.8. The photometric criteria are:

(a) The disk consists of two nested ovals, each with a shallow brightness gradient interior to a sharp outer edge.

(b) The outer oval has a much lower surface brightness than the inner oval. It can consist of a featureless disk (e.g., in an S0 galaxy) or spiral arms that make a pseudo (≡ not quite closed) outer ring or a complete outer ring.

(c) The nested ovals generally have different axial ratios and position angles, so they must be oval if they are coplanar. But the flatness of edge-on galaxies at these fairly high surface brightnesses shows that these disks are oval.

NGC 4736 and NGC 4151 are outer ring and outer spiral arm versions of oval galaxies (Fig. 1.8). I use the notation SA(oval) or SB(oval) exactly analogous to SA(lens) or SB(lens) for galaxies with oval disks.
Fig. 1.8. Criteria for recognizing unbarred oval galaxies shown schematically (top) and with observations of NGC 4736 and NGC 4151 (adapted from Fig. 9 in Kormendy & Kennicutt 2004). The image of NGC 4736 is from my IIIa-J plate taken with the 1.9 m Palomar Schmidt telescope. The image of NGC 4151 is from http://www.wikisky.org. The H\textsc{i} velocity contours of NGC 4736 and NGC 4151 are from Bosma et al. (1977a) and from Bosma et al. (1977b), respectively.
The kinematic criteria for recognizing ovals are that the velocity field is symmetric and regular, but:

(a) the kinematic major axis twists with radius;
(b) the optical and kinematic major axes are different; and
(c) the kinematic major and minor axes are not perpendicular.

Here observation (a) is equally consistent with a warp. But (b) and (c) point uniquely to an oval velocity field that is seen at a skew orientation. Given this conclusion, observation (a) then means that the intrinsic orientations of the outer and inner ovals are different. Usually, the outer oval is elongated perpendicular to the inner one, as seen face-on. My favorite poster child for secular evolution, NGC 4736, shows all of these effects. The classical Seyfert 1 galaxy NGC 4151 shows them even more clearly (Fig. 1.8).

Figure 1.9 shows four more oval galaxies. I use it to emphasize four points.

1. Oval galaxies are very recognizable and very common. It is curious that they have not better penetrated the astronomical folklore. Kormendy & Kennicutt (2004) show that they are important engines for secular evolution.

Fig. 1.9. Sequence of outer-ring galaxies that are structurally similar except that a bar embedded in the lens or inner oval structure ranges from strong at upper-left to invisible at lower-right. All images are from http://www.wikisky.org.
Secular Evolution in Disk Galaxies

(2) There is a complete structural continuity in outer ring galaxies from (R)SB objects that have strong bars to (R)SA objects that are completely barless. NGC 2859 is one of the best examples of an (R)SB(lens)0 galaxy in which the bar fills the lens in one dimension. Another excellent example is NGC 3945 (Kormendy 1979b: Fig. 1.17 and Fig. 1.24 here). NGC 3504 and NGC 3368 are two examples among many of galaxies that have well defined oval disks and extremely weak bars. I have typed them as (r,oval) and (s,oval) because there is a bright blue rim of star formation around the outside of the inner oval, exactly as in many (r,lens) galaxies. I am not aware of any measurements of the bar strength that take into account the oval structure. But the bars that are revealed by the 2MASS survey at $K'$ band must be only a few percent of the disk light. NGC 1068 is classified as unbarred by Sandage (1961) and by Buta et al. (2007); there is a hint of a bar in the 2MASS image (Jarrett et al. 2003). NGC 4736 is a purely unbarred, oval galaxy.†

(3) Albert Bosma has advocated for many years that (lens) and (oval) components are the early-Hubble-type and later-Hubble-type versions of the same kind of structure. For many years, I was unsure about whether or not to believe this. I am now convinced that Albert is exactly correct. The reasons are discussed in Sections 1.4.3.4 – 1.4.3.6. Here, I juxtapose (R)SB(lens) and (R)SAb(oval) galaxies in Fig. 1.9 to emphasize their similarity. I will continue to use this notation throughout this review, but I want to make it clear that I believe that (lens) and (oval) structures are fundamentally the same.

(4) There also is a continuity from complete outer rings (R) such as the one in NGC 2859 through spiral arms that are distorted until they almost closed to form what is called a “pseudoring” (R') as in NGC 3504 through to spiral arms that are less – but similarly – distorted as in NGC 4151 (Fig. 1.8 here) and NGC 1300 (compare Fig. 1.6 here with Fig. 13 in Kormendy 1979b). See de Vaucouleurs (1959); de Vaucouleurs et al. (1991: RC3) and Buta (2011, 2012) for further discussion.

All of these continuities prove to have important physical interpretations within our developing picture of disk-galaxy secular evolution. Most of them are reviewed in the following sections. The stellar dynamics of (R)S(r) galaxies are discussed in Lia Athanassoula’s (2012) third lecture. Further examples of the above structures are shown in Ron Buta’s (2012) lectures and in the de Vaucouleurs Atlas of Galaxies (Buta et al. 2007).

† The (R)SA(oval)ab galaxy NGC 4736 (Figs. 1.3, 1.6, 1.8, 1.28, 1.31, 1.35, 1.38) contains a nuclear bar but no main bar. The nuclear bar provides a “connection” to barred galaxies that is relevant in Section 1.5.2.8. But it is much too small to affect the overall evolution of the galaxy. NGC 4736 is therefore completely unbarred for the purposes of the present discussion. Similarly, NGC 1068 (Fig. 1.9) also has a nuclear bar but no main bar. I suggest that the connection between these two nuclear bars and their host oval disks is not an accident — that, in fact, oval disks are the late-type analogs of lenses and thus were once barred (see point 3). The hint is that some nuclear bars can survive even after the main bar has evolved away.
1.3.4 Classical versus physical morphology of galaxies

At the start of a new science, it is common to classify the objects under study into “natural groups” (Morgan 1951) whose members share observed characteristics that are judged to be important. The success of the taxonomy depends on how well the natural groups – the classification bins – prove to correlate with physics. The galaxy classification scheme of Hubble (1936) and Sandage (1961) as augmented by de Vaucouleurs (1959) won a Darwinian struggle between taxonomic systems because it succeeded best in ordering galaxies by properties that helped us to understand galaxy formation and evolution. Ron Buta (2012) reviews this subject in his lectures at this School.

It is important – and fundamental to the aims of this paper – to contrast morphological galaxy classification as practiced in the early days of extragalactic research with what becomes necessary as the subject matures. Sandage and Bedke (1994) emphasize the importance early on of not being led astray by preconceptions: “The extreme empiricist claims that no whiff of theory may be allowed into the initial classification procedures, decisions, and actions.” Nevertheless, every classifier chooses which features to consider as important and which to view as secondary. Hubble succeeded because he chose properties that became important to our understanding. Sandage recognizes this: “Hubble correctly guessed that the presence or absence of a disk, the openness of the spiral-arm pattern, and the degree of resolution of the arms into stars, would be highly relevant.” Hubble based his classification on choices made with future interpretation in mind.

In contrast (Kormendy 2004a): “At the level of detail that we nowadays try to understand, the time has passed when we can make effective progress by defining morphological bins with no guidance from a theory. [Breaking] down the wall between morphology and interpretation successfully has always been a sign of the maturity of a subject. For example, without guidance from a theory, how would one ever conceive of the complicated measurements required to see solar oscillations or use them to study the interior structure of the Sun? In the same way, we need the guidance of a theory to make sense of the bewildering variety of phenomena associated with galaxies and to recognize what is fundamental and what is not. This motivates a ‘physical morphology’ [Kormendy 1979a, b, 1981, 1982b; Kormendy & Kennicutt 2004], not as a replacement for classical morphology – which remains vitally important – but as a step beyond it. Physical morphology is an iteration in detail that is analogous to de Vaucouleurs’s iteration beyond the Hubble tuning fork diagram.”
One purpose of this review is to bring this process up to date. Our aim is to engineer the best one-to-one correspondence that we currently can between recognized types of galaxies or galactic building blocks and physical processes of galaxy formation.

It is reasonable to expect that an improved understanding of galaxies will show that an initial classification missed some physics. Also, some features of galaxies could not, early on, be observed well enough to be included in the classification. Two substantial additions and one small tweak to classical morphology are needed here. The small tweak is to recognize that nuclear star-forming rings are distinct from and often occur together with inner rings (r) in barred galaxies. This was point (f) in Section 1.3.1. The first major correction is to recognize and differentiate between real and counterfeit ellipticals (Section 1.7). The second is to recognize and differentiate between real and counterfeit bulges. The latter are “pseudobulges” (Section 1.5).

An essential aspect of physical morphology is to treat galaxies as being composed of a small number of building blocks, the distinct components in the mass distribution. The problem that this solves and the benefits that it provides were described as long ago as Kormendy (1979a):

“[Classical morphology] assigns a classification cell to each list of galaxy characteristics. As we look at galaxies more and more closely, the list of observed characteristics becomes alarmingly large. Thus the revised morphological types of de Vaucouleurs already require ‘about one hundred cells’ (de Vaucouleurs 1963) and still do not recognize features such as lenses. It is difficult to attach dynamical significance to the bewildering variety of forms that the system describes.”

In physical morphology, “we aim to identify as distinct components groups of stars or gas whose structure, dynamics, and origin can profitably be thought of as distinct from the dynamics and origin of the rest of the galaxy. . . . The large number of cells in classical morphology is now thought of as the many ways that components and their secondary behavior [such as spiral structure] can be combined to make a galaxy. The strength of this approach is twofold. It breaks up the complicated problem of galaxy structure into smaller and more manageable pieces to which it is easier to attach dynamical interpretations. Secondly, investigations of correlations and interactions between components are very efficient in suggesting previously unrecognized dynamical processes [emphasis added]. Thus the component approach provides an efficient framework for studies of galaxy dynamics.”

Throughout this review, my aim is to tweak the distinctions between galaxy components (and hence their names) until they are both correct descriptions and uniquely tied to physical processes of galaxy formation.
1.4 A Heuristic introduction to bars and spiral structure

Bars are the most important drivers for secular evolution in galactic disks; we will see them again and again throughout this School. For this reason, I now want to give you a heuristic introduction to bar dynamics and evolution. Lia Athanassoula (2012) will talk about this subject in more detail. Here, I concentrate on a simple version of the essential physics that you need to understand in order to have an intuitive feel for how bars form, grow and die. Bars are density waves in the disk. That is, the bar pattern rotates more-or-less rigidly at a single pattern angular velocity $\Omega_p$, whereas the angular velocity $\Omega(r)$ of material in the disk varies with radius. This is even more true of spiral structure: over most of a global spiral pattern, the stars and gas have $\Omega > \Omega_p$; they catch up to the spiral arms from behind, move through them in the rotation direction (lingering in the arms to give them their density enhancement) and then move on in the rotation direction toward the next arm. Since bars and spirals have some similarities, I briefly discuss spiral structure, too.

1.4.1 Orbital resonances in a galactic disk

Orbital resonances are the key to understanding bars and spirals. The main resonances – inner Lindblad resonance, corotation, and outer Lindblad resonance – will recur in many of the lectures at this school. I therefore need to introduce them in some detail.

The general orbit of a star in a galactic disk is an unclosed rosette, because the potential is not Keplerian (that is, the galaxy mass is distributed in radius and not all in one central point as in, for example, the Solar System).

Figure 1.10 shows disk orbits as seen in a frame of reference that rotates clockwise (orange arrow) at the pattern speed $\Omega_p$ of some coherent structure. In this figure, I show a spiral arm (red), because spirals almost always trail in the rotation direction (that is, the arm is convex in the direction of rotation). Thus it is easy to remember the rotation direction at a glance. I work in the epicyclic approximation (Mihalas & Routly 1968; Binney & Tremaine 1987) in which radial excursions are small. Then, at the radius where the stars and the pattern corotate, i.e., where $\Omega_p = \Omega$ (green), a stellar orbit is a small elliptical epicycle around the mean radius. The motion around the ellipse is counterclockwise, because the forward velocity is higher when the star is closer to the center than average. In the epicyclic approximation, the motion around the ellipse is simple harmonic. Corotation is the most important resonance in the galaxy, because the mean position of the star with respect to the global pattern never changes as long as $\Omega_p$ is fixed.
Fig. 1.10. Schematic illustration of galactic orbits as seen in a frame of reference that rotates clockwise (orange arrow) at the pattern angular velocity $\Omega_p$ of some coherent structure such as a spiral arm (red). The pattern stays fixed as we view it, whereas stars drift with respect to the pattern forward (clockwise) inside corotation and backward (counterclockwise) outside corotation. At the corotation resonance (green: $\Omega_p = \Omega$), a star with a small component of random velocity added to $\Omega$ executes simple harmonic motion counterclockwise around a closed ellipse (the “epicyclic approximation”). At the inner Lindblad resonance (blue: $\Omega_p = \Omega - \kappa/2$, where $\kappa$ is the epicyclic frequency), the stellar orbit is closed and the star executes two radial excursions for every revolution forward around the center. At the outer Lindblad resonance (red: $\Omega_p = \Omega + \kappa/2$), the orbit is closed and the star executes two radial excursions for every revolution backward around the center in the rotating frame. At other radii, several of which are shown, the stellar orbits are unclosed.
We will need the “epicyclic frequency” $\kappa$ of the small radial and azimuthal excursions around the mean motion,

$$\kappa^2 = \frac{2V}{r} \left( \frac{V}{r} + \frac{dV}{dr} \right),$$

(1.3)

where $V(r)$ is the rotation velocity as a function of radius $r$.

If we move slightly inward from corotation toward the galactic center, then a star oscillates around almost-closed ellipses while drifting forward with respect to the global pattern (leftmost orbit illustrated in Fig. 1.10).

Continuing toward smaller radii (next three orbits inward in Fig. 1.10), the forward drift gets faster until the backward loop disappears and we end up with an unclosed rosette orbit that involves somewhat more than two radial excursions for every revolution forward in the rotation direction around the center. It is clear that, as we move farther inward and the forward drift rate continues to increase, the orbit again becomes almost closed, now with almost exactly two radial excursions for every revolution (this is the second-innermost orbit shown in the figure).

Continuing toward still-smaller $r$, we arrive at “inner Lindblad resonance” (ILR) where the (blue) orbit is closed and the star executes exactly two radial excursions while it drifts forward with respect to the global pattern by one complete revolution around the center. This happens where $\Omega_p = \Omega - \kappa/2$. ILR is again an important resonance, because the star repeatedly has the same phase in its radial oscillation when it has the same position with respect to the global pattern. So the star interacts more strongly with the pattern near ILR than it does elsewhere in the disk. Moreover, ILR gives us a first-order understanding of bar dynamics, as discussed in the next section.

Starting at corotation and moving outward, stars drift backward with respect to the global pattern as seen in our rotating frame. At some large $r$, the orbit is closed as the star makes two radial oscillations for every revolution backward around the center (the orbit is not illustrated). This is “outer Lindblad resonance” (OLR), and it happens where $\Omega_p = \Omega + \kappa/2$.

The generic rotation curve $V(r)$ and frequencies $\Omega(r)$ and $\Omega(r) - \kappa(r)/2$ are shown in Fig. 1.3. Where $V \propto r$, $\kappa = 2\Omega$ and $\Omega - \kappa/2 = 0$. Where $V = \text{constant}$, $\kappa = \sqrt{2}\Omega$ and $\Omega - \kappa/2 = (1 - 1/\sqrt{2})\Omega$ decreases proportional to $\Omega$. In between, $\Omega - \kappa/2$ first rises and then falls with increasing $r$ as the rotation curve turns downward from $V \propto r$ to $V \simeq \text{constant}$. The radial range over which $\Omega - \kappa/2$ varies little with radius turns out to be crucial to the formation of bars and spiral arms. The evolving height and radial extent of the $\Omega - \kappa/2$ maximum proves to control the fate of bars. And the natural pattern speed for bars proves to be $\Omega_p \simeq \Omega - \kappa/2$. As follows:
1.4.2 Bars and spirals as almost-kinematic density waves

The essential insight into the dynamics of bars and global spirals is due to Lindblad (1956) and Kalnajs (1973; see Toomre 1977b for a lucid review). It is illustrated in Fig. 1.11. Especially for outward-rising rotation curves (M33) and even for nearly constant or falling rotation curves (M81), the angular precession rate $\Omega - \kappa/2$ of ILR orbits is small and nearly constant over much of the galaxy. Suppose that $\Omega - \kappa/2$ is exactly constant with $r$. Then: If closed ILR orbits are arranged to produce a trailing spiral enhancement in density (top left) or a straight bar (top right), the orbits will precess together at exactly the same $\Omega - \kappa/2$ and so will preserve the spiral or bar shape. These are purely kinematic density waves.

Fig. 1.11. (bottom) Frequencies $\Omega$, $\kappa$ and $\Omega \pm \kappa/2$ for almost-circular orbits in M33 (Shu et al. 1971) and M81 (Visser 1980). Both galaxies have large radial ranges in which $\Omega - \kappa/2 \approx$ constant and ILR orbits precess almost together. (top left) From Kalnajs (1973), elliptical ILR orbits aligned to produce a spiral density wave. (top right) From Englmaier & Gerhard (1997), examples of principal orbit families for a bar oriented at $-45^\circ$. The elongated orbits parallel to the bar are the $x_1$ family out of which the bar is constructed. If $\Omega - \kappa/2$ = constant with radius over the extent of the $x_1$ orbits, they precess together and preserve the bar shape. Interior to ILR, the $x_2$ orbits are perpendicular to the bar. (The almost-square orbit has four radial oscillations for each revolution; it is a 4:1 ultraharmonic resonance orbit.)
In practice, $\Omega - \kappa/2$ is not quite constant. To make real bars or spirals, it is the job of self-gravity to keep the orbits precessing exactly together.

This discussion is a heuristic argument for another important conclusion. The natural pattern speed of a bar or global spiral is $\Omega_p \simeq \Omega - \kappa/2$. Note in Fig. 1.11 that this is much slower than $\Omega$ over most of the galaxy. That is, stars and gas revolve around the galactic center more quickly than the pattern rotates; they catch up to the pattern from behind, participate in it for a time – lingering in the pattern and thereby enhancing its density (Toomre 1981) – and then continue onward in the forward rotation direction. For bars, corotation happens near the end of the bar or slightly beyond it (see Sellwood & Wilkinson 1993 for a review).

Some barred galaxies that have substantial (pseudo)bulges also have nuclear bars $\sim$ one-tenth of the radius of the main bar (Section 1.5.2.8). When the galaxy mass distribution is very centrally concentrated, $\Omega - \kappa/2$ has a high maximum at small radii (frequency curves for M 81 in Fig. 1.11). The natural pattern speed of a nuclear bar is roughly equal to the local value of $\Omega - \kappa/2$ and is therefore much higher than the pattern speed of the main bar. This is seen in numerical simulations (Debattista & Shen 2007; Shen & Debattista 2009) and in real galaxies (Corsini et al. 2003).

The $x_1$ family of closed bar orbits shown in Fig. 1.11 and the similar, non-periodic orbits that are trapped around them by the bar’s self-gravity involve large perturbations from circular orbits. Strong bars are nonlinear. Then the approximations that we have made are not accurate. In particular, the true pattern speed is rather larger than the local value of $\Omega - \kappa/2$ (e.g., Shen & Debattista 2009). Nevertheless, the epicyclic approximation still captures the essence of the physics (Ceverino & Klypin 2007).

In particular, for any realistic $\Omega_p \sim \Omega - \kappa/2$, there must be an inner Lindblad resonance in a centrally concentrated galaxy such as M 81, but there cannot be an ILR in a pure-disk galaxy such as M 33. Inside ILR, the closed “$x_2$ orbits” are elongated perpendicular to the bar (Fig. 1.11). So they cannot be used to construct the bar and to maintain its self-gravity. We will see in Section 1.5 that the secular evolution of a barred galaxy is in part to transport gas toward the center and thereby to build a pseudobulge. As secular evolution increases the central concentration of a barred galaxy, the inner maximum in $\Omega - \kappa/2$ gets higher and wider in radius. Therefore it gets more difficult for self-gravity to keep the decreasing number of $x_1$ orbits precessing together. Also, the number of (damaging) $x_2$ orbits increases. The bar gets weaker. Thus, bars naturally commit suicide by the secular evolution that they drive. This happens preferentially in early-type galaxies, not in galaxies such as M 33. All of these heuristic predictions prove to be accurate.
1.4.3 The growth, structural evolution and death of bars

This section is an overview of the life histories of bars – from rapid growth through secular evolution in “middle age” through eventual death – at the level that we need in this Winter School. I concentrate in this section on the bars themselves; the effects of bars on the other components in their galaxies will be the subject of later sections. I will not cover the rich dynamics of bars in their nonlinear phases. For this work, the best review is Sellwood & Wilkinson (1993). Contact between the complicated nonlinear dynamics that is reviewed there and the simplified story that I tell here is not always good. That’s where the frontier in this subject lies.

Here, I will summarize the most important bar evolution processes based on a series of seminal papers. Sellwood & Wilkinson (1993, hereafter SW93) provide more references, and Athanassoula (2012) reviews – and, indeed, advances – some of these subjects in her lectures at this School.

My orientation is a little different from that of SW93. They take – as much as possible, in this complicated subject – a formal approach rooted in the rigorous mathematics of galaxy dynamics. I take an observer’s approach. That is, I try to benefit as much as possible from the insight gained from analytical and $n$-body studies, but I also put equal emphasis on letting the observations suggest (or, in some cases, prove) which processes are at work. Sometimes observations hint that a process (e.g., evolution of bars to lenses) takes place even when the theory of such a process is not well formulated. But asking the right question is the efficient road to progress. So this observational guidance is very useful. One key is to remember which ideas are hypotheses and which are proven. And it is especially important not to overinterpret the temptingly rich array of possibilities that are inherent in this subject. I will try to be clear about the confidence with which various ideas are suggested. And I will emphasize what I believe are the most important remaining problems.

1.4.3.1 Bar instability

Massive, cold, rotating disks are famously unstable to the formation of bars (e.g., Ostriker & Peebles 1973; Toomre 1977b, 1981; SW93). Many $n$-body studies start with a stellar disk that is highly unstable and then follow the evolution of the bar that results. Most results that are derived in this way are probably realistic, modulo (important!) the neglect of gas and dark matter. However, it is important to realize that bar evolution almost certainly does not start this way. It is unrealistic to think that a disk grows axisymmetrically to a high mass, meanwhile using up its gas to make stars, and only then discovers (“Oh, my God!”) that it is bar-unstable.
In a paper entitled “Most Real Bars are Not Made by the Bar Instability”, Sellwood (2000) expresses a related worry. Most barred galaxies have enough central mass concentration so the bar essentially must have an ILR. That is, $\Omega - \kappa/2$ is similar to the curve for M 81 in Fig. 1.11. Our heuristic arguments in §1.4.2 then make plausible the result that also emerges from more detailed studies (e.g., Toomre 1981), namely that a bar instability never gets started when the resulting bar would have a strong ILR. Sellwood acknowledges and dismisses the possibility that the disk might not originally have allowed an ILR, i.e., that the central concentration was manufactured by the bar only after it formed. One piece of supporting evidence was a conclusion (Abraham et al. 1999) that strongly barred galaxies were rare at $z > 0.5$; this is now known to be incorrect (Jogee et al. 2004). More immediate was the concern that building up the central concentration weakens the bar. I will suggest below that bar suicide happens, and it happens at a measurable (pseudo)bulge-to-disk ratio. But I, too, have worried about why strong bars can coexist with strong ILRs. The evidence will suggest that, when the central mass grows slowly while the bar has a strong angular momentum sink, a nonlinear bar can – for a while – continue to grow even when it already has an ILR. But the more important point for the present section is this: present disk conditions do not favor the growth of bars by a simple instability.

Possible implications:

(a) Bar formation may be a threshold process that begins and then proceeds slowly and perhaps episodically (Sellwood 2000) as the disk grows massive enough with respect to its dark halo (see also Mihos et al. 1997).

(b) The formation of the stars that now make up the bars in early-type galaxies happened long ago in progenitor galaxies about which we know very little. E.g., the boxy bulge ≡ almost-end-on bar of our Galaxy is made of stars that are very old and enhanced in $\alpha$ elements (see Renzini 1999 for a review). So its stars formed over a period of $\lesssim 1$ Gyr. Gas fractions were much higher then than they are now (Genzel et al. 2006). Gas may be centrally important to bar formation. Observations of high-redshift disks that are nevertheless younger than our Galaxy’s bulge stars show surprises such as $\sim 10^8$ M$_\odot$ clumps and high velocity dispersions (Genzel et al. 2006; Förster Schreiber et al. 2009). The clumps are believed to form by violent instabilities, and they eventually merge to form at least some classical bulges (Elmegreen et al. 2008; Section 1.8.1 here). None of this sounds like the typical initial conditions assumed in n-body simulations of bar formation. We have no reason to be confident that we know how to start those simulations with realistic initial conditions.

(c) Contrariwise, a bar may form long after star formation makes the stellar disk. One way is thought to be through tidal tickling by neighboring galaxies (e.g.,
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Noguchi 1987, 1988; 1996, which also discusses gas infall; Gerin et al. 1990; Barnes et al. 1991; Mihos et al. 1997). It is difficult to test this (for example) by looking for an excess of barred galaxies in dense environments such as the Coma cluster. The reason is that any extra tendency to form bars where there are many galaxy encounters must compete with and may lose out to the stabilizing effects of disk heating (Marinova et al. 2012; see Kormendy & Bender 2012 for evidence that disk heating happens even in the Virgo cluster).

(d) Occam’s razor is a dangerous weapon. Answers are not guaranteed to be simple. All the above – i.e., a series of episodic, encounter-driven growth spurts that punctuate a steady, slower growth by outward angular momentum transport as envisaged by Sellwood (2000) – may happen. It is important to understand that global spiral structure connected with a bar or inner ring is a signature of outward angular momentum transport and therefore a sign that the bar is growing stronger.

In the next sections, I review the life histories of bars and the evolution that they drive in their host galaxies, keeping the above issues in mind. As needed, I emphasize where simulations do not yet include important physics. Limitations include (1) that many simulations do not include gas, and gas physics is variously but always importantly simplified, (2) that continued infall of gas and small galaxies is not included, (3) that feedback from hot young stars, from supernovae and from active galactic nuclei is generally not included and may be important, and especially (4) that simulated galaxies are usually not as multicomponent as real galaxies. Two-body relaxation is uninterestingly slow in galaxy disks. Evolution is driven by the interactions of stars and gas with collective phenomena. Physical morphology (§1.3.4) invites us to investigate the interactions of different nonaxisymmetric components in galaxies. This is where the action is.

1.4.3.2 N-body simulations:
Rapid bar growth via instability
followed by secular growth via angular momentum transport

Among the many published n-body studies of bar formation (SW93), I focus on Sparke & Sellwood (1987), because they analyze their simulation in ways that tell us what we need to know. The initial condition is an axisymmetric galaxy with a bulge-to-total ratio of 0.3. The bulge is a rigid Plummer (1911) sphere with size $\sim 1/5$ that of the disk. A rigid potential is a limitation: the bulge gives the galaxy an ILR, and it is interesting to see the (surprising lack of) consequences, but the bar and bulge cannot interact. The disk is a Kuz’mín (1956) – Toomre (1963) model, density $\propto 1/(a^2 + r^2)^{3/2}$, where $r$ is radius and $a$ measures the scale length of the density falloff. With a Toomre
(1964) axisymmetric stability parameter of $Q = 1$, the initial disk was very unstable. The disk contained 50,000 particles whose gravity was softened on a length scale of 0.1 $a$. Other limitations are that the model contains no gas and no “live” dark matter halo of simulated particles; both of these limit the extent to which the bar sees a sink for angular momentum that allows it to grow. More detailed simulations can now be run, but this subject does not get the attention that it deserves, and in particular, analyses are not usually as physically motivated and compelling as the one in Sparke & Sellwood (1987). There is much to be learned from this simulation, as follows.

Figure 1.12 shows the evolution of the disk density, and Fig. 1.13 shows the growth in amplitude of the bar and the evolution of the pattern speed of the bar and its associated spiral structure. Time is measured in natural units (discussed in Sparke & Sellwood 1987). Beginning immediately and extending to time 50, the disk rapidly grows a two-armed instability that is bar-shaped near the center and a global, two-armed spiral farther out. The bar rapidly grows stronger: more stars participate, the axial ratio of the bar decreases, the bar grows longer and its pattern speed decreases.

Figure 1.13 dramatically reveals the important result that the pattern speed of the bar is larger than the pattern speed of the spiral at all times. This is consistent with our heuristic argument: the bulge creates a near-central maximum in $\Omega - \kappa/2$, and the pattern speeds of the bar at relatively small radii and the spiral at relatively larger radii are comparable to but slightly larger than the local value of $\Omega - \kappa/2$. (Note: in Fig. 1.13, frequency $= 2\Omega_p$, because the pattern is bisymmetric.) Because $\Omega_p$ is smaller for the spiral than for the bar, the spiral continually shears away from the bar. It is no surprise that spiral arms do not necessarily start at the end of the bar, especially in galaxies such as NGC 2523, which have well developed inner rings and which therefore are dynamically mature.

Figure 1.13 makes it clear that the rapid, instability-driven initial growth of the bar is followed by a distinct later phase of secular growth, when the bar amplitude increases and $\Omega_p$ decreases more slowly than in the early, rapid phase. In this collisionless model, the outer disk has been heated so much that the spiral structure is weak during the secular phase (Fig. 1.12). In real galaxies, there are two reasons why the later growth is more dramatic. First, galaxies contain gas; (1) its response is stronger than that of the stars and, in fact, dissipative, and (2) gas also keeps the stellar disk cooler and more responsive, because the stars that form from it are formed with low velocity dispersions. Second, the dark halo in a real galaxy provides an additional sink for the disk angular momentum.
The bar ends roughly at corotation. Therefore, stars stream through the bar density wave in the forward direction. Analysis of the orbital structure of the late-stage model shows that – as expected – the bar is made almost exclusively of orbits trapped around the $x_1$ family of closed orbits that align with the bar. Despite the presence of an IRL, there are almost no orbits analogous to the $x_2$ family (the model has only 50,000 particles, and not all orbits were checked.) Additional details of the orbit structure are discussed in Sparke & Sellwood (1987).

Fig. 1.12. Bar formation in the $n$-body simulation of Sparke & Sellwood (1987, Fig. 1). Times are in natural units that are discussed in their paper. Only one particle in ten is included, and the bulge component is not shown.
Fig. 1.13. Evolution of the bar in the n-body model of Sparke & Sellwood (1987). Panels (a) and (b) show the amplitude and phase of the bar as a function of time. A straight line is fitted to the phases at late times. It shows that the pattern speed decreases quickly during the early, rapid growth of the bar and then more slowly during the later, secular growth. The bottom panels show contours of the square root of the power in the bar or spiral perturbation as a function of frequency = $2\Omega_p$ and radius. Panel (c) is for the early part of the rapid growth (up to time 31) and panel (d) is for the slow growth phase at times 40 to 103. A very important conclusion is that the bar has a higher pattern speed than the spiral structure. Also, note that the pattern speeds of both the bar and the spiral arms decrease with time, as shown for the bar in panel (b). The smooth curves show $2\Omega$ (solid curve) and $2\Omega \pm \kappa$ (dashed curves) for the initial, axisymmetric model. They apply only approximately during the later, nonlinear phases. Nevertheless, it is clear that both the bar and the spiral have pattern speeds that are similar to but slightly larger than the local values of $\Omega - \kappa/2$. Also note that the bar develops despite the fact that it has an ILR. These are Figs. 2 and 3 from Sparke & Sellwood (1987). Similar results are illustrated in Bournaud & Combes (2002).
Fig. 1.14. Comparison of the $n$-body bar model of Sparke & Sellwood (1987: isodensity contours at right) with the SB0 galaxy NGC 936 (Kormendy 1983: isophote map at left). This is Fig. 6 from Sparke & Sellwood (1987).

Comparison to real SB0 galaxies shows that the $n$-body bar model of Sparke & Sellwood (1987) is realistic in many respects. It has the shallow density gradient and sharp outer edge of real bars in early-type galaxies. It has the rectangular shape observed, e.g., in NGC 936 (Fig. 1.14). And it shows qualitatively similar non-circular streaming motions. At the end of the simulation, the disk is too hot to allow much spiral structure; therefore, the bar has no “live” component with which it can effectively interact, and as a result, it is very robust. The situation in NGC 936 is similar: the Toomre (1964) stability parameter in the outer disk is $Q \simeq 3$ to 4, so essentially no small-scale structure is possible (Kormendy 1984b). Not surprisingly, the purely stellar-dynamical $n$-body model of Sparke & Sellwood (1987) is a realistic simulation of an SB0 galaxy but not of a gas-rich barred spiral.

Shortcomings of the model are easily linked to limitations in the physics:

(a) The model is two-dimensional and therefore cannot include orbital complexity (including chaos) that is fundamentally three-dimensional. In particular, the bar cannot buckle and hence thicken in the axial direction (Section 1.4.3.3).
(b) The lack of gas means that the model can simulate SB0 but not spiral galaxies.
(c) The bar cannot grow very much at late times because the disk gets too hot. The same problem is well known in the context of understanding spiral structure. Quoting Toomre (1990): “The gravitational forces involved in [spiral structure] have the unwelcome side effect that they tend to increase the mean epicyclic
motions of any stars . . . which take part. Typically, in just a few revolutions, these would-be participants become simply too ‘hot’ to contribute appreciably to any more fun. In other words, the vigor of these apparent ‘spiral instabilities’ was quickly recognized to doom any hopes for their longevity – unless one adds some form of cooling . . . such as might be natural in a gas but surely not in a disk of stars.” Toomre concluded that “It really seems as if we typically need at least to double the known amounts of reasonably active mass in the disks of Sc galaxies – beyond the gas amounts that they are known to possess – in order that such galaxies appear about as few-armed as they often are. *And from where can they have obtained . . . such relatively cool additional disk material if not from recent infall*” (emphasis added). So another limitation of the Sparke & Sellwood model – and of other $n$-body simulations – is the lack of continued cosmological infall of cold gas (Combes 2008a; Bournaud & Combes 2002).

(d) Lacking gas, the bar cannot commit suicide by transporting gas to the center and building a pseudobulge that makes it more difficult for $x_1$ orbits to precess together. I believe that $n$-body studies overestimate the robustness of bars when they give them no opportunity to increase the central mass concentration.

(e) Concurrently, the bar cannot continue to grow stronger if the model does not include a “live halo” of particles that can act as an angular momentum sink.

These comments are not meant to be critical of Sparke & Sellwood (1987). Sellwood & Carlberg (1984) recognize the importance of gas infall to the maintenance of spiral structure. Sparke & Sellwood (1987) is a clean study with the machinery that was available at the time. It focuses on fundamentals that we need to understand. Many $n$-body studies both before and since have led to similar conclusion and have further extended our understanding of bar evolution (e.g., Athanassoula 2003, 2005, 2012).

My remarks are meant to highlight how much this subject presents opportunities to students now. There is a danger that we may miss important physics because we do not yet observe the early stages of bar formation. This is an opportunity for observers of high-$z$ galaxies. Modulo this uncertainty: *I suggest that bars grow secularly via an ongoing competition between outward angular momentum transport that strengthens the bar and the buildup of pseudobulges that weaken the bar.* This competition allows some barred galaxies to have both strong bars and high-mass (pseudo)bulges that create (otherwise destructive) ILRs near the center.

Both the disk and the dark halo are angular momentum sinks. For the halo, this conclusion is based mostly on $n$-body simulations (e.g., Sellwood 1980, 2006, 2008; Athanassoula 2003, 2005; Athanassoula & Misiriotis 2002), but note that Valenzuela & Klypin (2003) conclude that the effect is often overestimated. For the disk, global spiral structure is the visible sign that the process is ongoing.
Cold gas is important to the evolution for many reasons. It makes the disk more responsive, both via its small velocity dispersion and by making new stars that keep the disk cold. Radial redistribution of gas is one product of angular momentum transport. And especially important is the conclusion reviewed in the next sections that gas driven inward to the center builds substantial pseudobulges in many galaxies. The natural frequencies at which ILR orbits want to precess therefore become less constant with radius. When this effect wins the above competition, the bar is weakened or destroyed. Continued cosmological infall of cold gas is central to all of these processes.

I argue in the rest of this review that many aspects of the above story are well understood but that many opportunities remain to be explored.

1.4.3.3 Vertical buckling of bars and the formation of box-shaped bulges

The vertical thickening of bars into “box-shaped bulges” is reviewed from a theoretical perspective in SW93 and from an observational perspective in Kormendy & Kennicutt (2004). My review here is brief.

N-body simulations show that strong bars thicken in the axial direction until they look peanut-shaped when viewed side-on and box-shaped when viewed at the most common orientations between side-on and end-on. The first paper to show this – Combes & Sanders (1981) – was one of the earliest papers on galaxy secular evolution. Two distinct processes are responsible.

Figure 1.15 shows the evolution of an $n$-body bar that, seen side-on, turns into a “box-shaped bulge” via a buckling instability in the axial direction (Raha et al. 1991). The instability happens after the bar is well formed, and

![Figure 1.15](image_url)
its growth is about as rapid as that of the original bar instability. Two bar rotations later, the bar has weakened considerably, grown more centrally concentrated, and become box- or peanut-shaped as seen side-on. The resemblance to box-shaped bulges in edge-on galaxies (Section 1.5.2.9), already noted by Combes & Sanders (1981) is compelling. Many other \( n \)-body studies reach similar results (e.g., Athanassoula & Misiriotis 2002; Athanassoula 2003, 2005; Athanassoula \textit{et al.} 2005; Shen \textit{et al.} 2010).

A second mechanism by which bars may thicken in the axial direction is via resonances between the rotation of the bar and the vertical oscillations of disk stars (e.g., Pfenniger 1984, 1985; Combes \textit{et al.} 1990; Pfenniger & Norman 1990, 1991; Pfenniger & Friedli 1991; Hasan \textit{et al.} 1993). When the vertical oscillation of stars is in resonance with the azimuthal rotation of a bar, each star repeatedly encounters the bar at a similar phase in its orbit. This pumps up the vertical velocity dispersion of disk stars and gives the center a boxy appearance when viewed edge-on. Unlike bar buckling, resonant heating is inherently a secular process.

The relative importance of these two processes in making the observed "box-shaped bulges" is not known. However, the most important conclusion appears robust regardless of the answer: when we see a boxy bulge in an edge-on galaxy, it is part of the bar and not a merger remnant. We therefore call these features "box-shaped pseudobulges". I return to them in Section 1.5, when I discuss the evolution that bars drive in their galaxies.

\subsection*{1.4.3.4 Bar suicide and the origin of lens components.
I. \textit{N}-body simulations
}

Early \textit{n}-body simulations suggested that bars are very robust (see SW93). The reason is now clear: those simulations contained no gas and so could not engineer big changes in the central concentration of the mass distribution. More recent simulations which allow the galaxy to grow a central mass – either "by fiat" or more naturally by rearranging the disk gas – show that \textit{bars tend to commit suicide by the secular evolution that they drive}. In particular, they force disk gas to fall toward the center, where it builds up a high-central-concentration pseudobulge, and this causes the bar to weaken. Pseudobulge growth is covered in later sections. The death of bars and their evolution – I suggest – into lens components is discussed here.

The earliest simulations of this process were motivated by the observation that most galaxies contain central supermassive black holes (Kormendy & Richstone 1995). The earliest paper that I know, Norman & Hasan (1990), already got essentially the modern answer: "It is estimated that a black hole with mass equal to 17\% the total mass is required to destroy the \([x_1]\) family
Secular Evolution in Disk Galaxies

of orbits and hence the bar.” No galaxy is known to have such a big black hole (Kormendy & Ho 2013), but we now know that a centrally concentrated pseudobulge – although less effective than a point mass – has a similar effect. Hasan & Norman (1990) is a detailed followup. Pfenniger & Norman (1990) concentrated on pseudobulge building by a combination of inward radial gas flow and resonant vertical heating, and they reached similar conclusions about bars destruction. Subsequent discussion has centered on the question of how much central mass is needed to affect a particular degree of bar weakening. Apparent disagreements between papers mainly result from the fact that fluffier central mass concentrations are less damaging to bars.

Why central mass concentrations are destructive is easy to see using Fig. 1.11 and was summarized in Section 1.4.2. As the central mass increases, the central maximum in \( \Omega - \kappa/2 \) becomes higher and broader in radius (see the panel for M81). This shrinks the radius range in which \( \Omega - \kappa/2 \) varies slowly with radius and in which it is possible to have \( \Omega_p \sim \Omega - \kappa/2 \). To put it differently, the radius range between ILR and corotation in which \( x_1 \) orbits align with the bar gets smaller. Recall that \( x_2 \) orbits interior to ILR align perpendicular to the bar. So, as the central concentration increases, there are fewer bar-supporting \( x_1 \) orbits, and they have a harder time all precessing at the same rate \( \Omega_p \sim \Omega - \kappa/2 \). As the bar potential weakens, self-gravity becomes less able to keep all the orbits precessing together. Once an orbit “escapes” from its alignment with the bar, it phase-mixes azimuthally in a short time. Even if there is no big change in orbital eccentricities, the long, thin shelf in surface brightness that makes up the bar will, I suggest (Kormendy 1979b), tend to phase-mix azimuthally into a lower-surface-brightness and more axially symmetric shelf in surface brightness that has the same sharp outer edge that the bar had. This is precisely a description of a lens component. It is part of the reason why I suggest that, as strong bars weaken, the stars that escape from them grow a lens. I suggest further that we see galaxies at all phases of this evolution: some have bars and no lenses; many have bars embedded in lenses of the same major-axis size, and some have lenses with no bars.

The rest of this section reviews further papers on bar suicide and observational evidence that lenses are defunct bars.

Combes (2008b, 2010, 2011) gives brief theoretical reviews of bar-to-lens evolution. She also reviews an additional important aspect of bar dissolution. When gas loses angular momentum and flows toward the center, the stellar bar receives that angular momentum that is lost by the gas. This makes the orbits rounder and the bar weaker. Papers that emphasize this effect include Bournaud & Combes (2002) and Bournaud et al. (2005).
Fig. 1.16. Death of an $n$-body bar as the central mass concentration is increased (adapted from Figs. 1, 2 and 3 of Norman et al. 1996). An initial axisymmetric disk was evolved to time 100, by which time a stable bar had developed (leftmost configuration shown in each of the three rows of particle distributions at the top). The top three rows show the time evolution as a point mass is grown at the center. Its mass shrinks from bulge size to zero size between $t = 100$ to $t = 150$. At the end, it makes up 0%, 3% and 7% of the mass of the disk (top row to bottom row). In the absence of a central point mass, the bar is stable (top). The bar is weakened progressively more as the central mass increases. The bar amplitude is shown in the middle panel. The bottom panel shows the $t = 200$ amplitude as a function of the final central point mass. Note that, whereas higher point masses more thoroughly destroy the bar, its amplitude is non-zero even for a 7% central point mass.
My lectures included an example from Norman et al. (1996) of an $n$-body simulation of the weakening of a bar by a growing central mass. This is illustrated in Fig. 1.16. A Kuz’min – Toomre disk that contains 75\% of the mass is the only component modeled with (50,000) “live” particles. The rest of the mass is in a rigid bulge. This is modeled as the sum of two Plummer spheres, initially of the same size; the aim was to let one of them shrink in radius once the bar was well established. The disk was initially given a Toomre stability parameter of $Q = 1$ ensuring that a bar would form. This already guarantees that the initial bar will coexist with a bulge whose $B/T$ ratio is typical of observed galaxies. Figure 1.16 shows that the inner part of the disk formed a bar by time 50; if nothing further was done to the model (top row of particle distributions and “no central mass” amplitude line in the middle panel), the bar remained stable in amplitude to time 200.

Between time 100 and time 150 (about four bar tumbling periods), the lower-mass “bulge” Plummer sphere was shrunk by a factor of 50 in radius. Note that this turns it effectively into a point mass, not a pseudobulge with a realistic scale length. No mass was added, so the overall equilibrium of the disk was essentially unaffected. But the amplitude of the bar decreased as the central point mass was shrunk. Even a 3\% central point mass reduced the bar amplitude substantially. A 7\% point mass killed it almost completely.

Norman et al. (1996) explored the mechanism whereby the bar is destroyed in some detail, both in the above, two-dimensional simulation and in three-dimensional simulations that give similar results. In essence, moving some mass to the center shrinks the phase space (e.g., radial range) of the $x_1$ orbits. As ILR moves outward, some $x_2$ orbits appear, and these do not support the bar. Some orbits become chaotic. At some point (time $\sim 140 \pm 5$ in Fig. 1.16), the bar coherence quickly breaks down and the disk becomes more axisymmetric. Note that the bar is not destroyed completely.

Norman and collaborators acknowledge that these are “highly idealized calculations intended to study just one aspect of the rich secular evolution of barred galaxies. The contraction of a rigid mass component is, of course, highly artificial,” and more to the point, the pseudobulges that weaken real bars have length scales $\sim 1/10$ those of their associated disks; they are not point masses. With Norman et al. (1996), we emphasize that the model is constructed so a relatively large bulge coexists comfortably with the bar. Figure 1.16 should be taken as a “proof of concept” of bar suicide, not as a definitive measurement of how much central mass concentration is required to achieve it. I use Norman et al. (1996) and not more detailed simulations as my example here because my purpose is primarily pedagogical, and I don’t want the essential theme to get lost in the details of orbit analysis.
The real world is substantially more complicated in ways that make it difficult to predict via simulations how much central mass concentration a bar can tolerate. No available simulation realistically follows the competition between (1) the bar growth that results from allowing the disk and dark halo to be angular momentum sinks, with the disk kept cold and continually replenished with cosmologically infalling gas, and (2) the secular evolution that builds up the central mass concentration and that thereby fights the growth of the bar. While the pseudobulge grows both through gas infall and star formation and (e.g., Norman et al. 1996) by the redistribution of stars, resonances such as (but not limited to) ILR sweep through the central regions and continually keep a fresh supply of material responsive to resonant interactions with the bar.

So it is no surprise that some papers suggest that central mass concentrations as small as a few percent of the disk mass are enough to destroy bars (e.g., Berentzen et al. 1998; Sellwood & Moore 1999; Hozumi & Hernquist 1999, 2005; Bournaud et al. 2002, 2005; Hozumi 2012) whereas others (e.g., Friedli & Benz 1993; Norman et al. 1996; Athanassoula et al. 2005) find that larger masses are necessary. These apparent disagreements are largely resolved by a fundamental conclusion due to Shen & Sellwood (2004): “For a given [central] mass, dense objects cause the greatest reduction in bar amplitude, while significantly more diffuse objects have a lesser effect” (emphasis added). The culprit in bar suicide is certainly not the central supermassive black hole (Shen & Sellwood 2004) or even a nuclear star cluster, since these typically have masses of \( \sim 0.2\% \) of the mass of a classical bulge and a smaller fraction of the mass of a pseudobulge or disk (see Kormendy & Ho 2013 for a review).

The results of Shen & Sellwood (2004) suggest that pseudobulges mainly are responsible for destroying bars. For a “soft” central mass whose size is comparable to that of a pseudobulge, Shen and Sellwood find that a 5% central mass decreases the bar strength to \( \sim 60\% \) of its undamaged value, whereas a 10% mass decreases the bar strength to \( \sim 1/3 \) of its undamaged value. Orbital analysis reveals that the bar dies because the phase space of \( x_1 \) orbits shrinks, and many \( x_1 \) orbits become chaotic as the bar decays. In most of these models, the dark matter halo was a rigid potential and therefore not an angular momentum sink. Test runs with a live halo show that the bar is then slightly harder to destroy. Similarly, the disk is dissipationless and does not accrete cold gas from the cosmological web, so it is not as good an angular momentum sink as the disk in a real spiral galaxy. Nevertheless, these results provide a realistic picture of what it takes to destroy a bar, at least as judged by a comparison with real galaxies (Section 1.4.3.5).
Fig. 1.17. Typical galaxies in which a bar fills a lens component in one dimension. This figure shows a sequence from a strong bar with essentially no lens (NGC 4643) through galaxies that have both bars and lenses (NGC 2950, NGC 4340, NGC 3945) to NGC 3081, which has an exceedingly weak bar embedded in a bright lens with a very bright, star-forming inner ring around the rim of the lens. The HST image at right is an enlargement of the inner ring, lens, bar and pseudobulge. In NGC 3081, the pseudobulge replicates the main B(r,lens) structure with a nuclear bar. All images are from http://www.wikisky.org except those of NGC 3801, which are from the de Vaucouleurs Atlas of Galaxies (Buta et al. 2007: left image) and HST (Buta et al. 2004: right image). Similar galaxies are shown in earlier figures. In Fig. 1.6, NGC 1291 is an (R)SB(lens)0/a galaxy similar to NGC 3945 here. In Fig. 1.9, NGC 2859 is an (R)SB(lens)0 galaxy similar to NGC 3945. The other galaxies in that figure are later-Hubble-type versions of the sequence shown here.
1.4.3.5 Bar suicide and the origin of lens components. II. Observations

Long before we knew of a process that could destroy bars, Kormendy (1979b, 1981, 1982b) suggested that bars weaken with time and evolve into lenses. Observations on which this suggestion was based include the following.

(a) Lens components are very common in barred galaxies; in the sample of 121 SB galaxies studied by Kormendy (1979b), 54% of SB0− SBa galaxies have lenses. The relative light contribution of the bar and lens varies widely from bar/lens $\gg 1$ to bar/lens $\ll 1$. Figure 1.17 shows such a sequence. I illustrate many B(lens) structures in these lectures to emphasize how common they are.

(b) Lens components occur but are rare in unbarred S0−Sa galaxies. Examples are shown in Figs. 1.7 and 1.18. It is likely that the inner “oval disks” in later-type (typically Sb) galaxies are lenses, too. If B $\rightarrow$ lens evolution occurs, this suggests that it goes nearly to completion (i.e., bar/total light $\rightarrow 0$) rarely in early-type galaxies and more commonly in mid-Hubble-type galaxies.

(c) Lens components and bars in early-type galaxies have similar radial brightness profiles; i.e., shallow surface brightness gradients interior to a sharp outer edge. The brightness profiles of the lenses measured in Kormendy & Bender (2012) are well fitted by Sérsic (1968) functions with $n \simeq 0.5$ (i.e., Gaussians).

(d) When bars and lenses occur together, the bar almost always fills the lens in one dimension (Kormendy 1979b, Buta et al. 2007; Buta 2011, 2012; Fig. 1.17 and references there). Points (c) and (d) imply that, to make a lens, it is sufficient to azimuthally phase-mix bar orbits. Points (a) and (b) hint that such a process occurs in many barred galaxies but that bars are completely destroyed only rarely. This is consistent with Section 1.4.3.4: moderate “soft” mass concentrations weaken bars but do not necessarily destroy them.

Fig. 1.18. The prototypical unbarred S0 galaxy with a lens is NGC 1553 (Fig. 1.7). This figure shows two more examples. NGC 2784 is from the de Vaucouleurs Atlas and NGC 3245 (rotated so north is at left) is from http://www.wikisky.org. The lenses are the elliptical shelves in surface brightness just outside the (pseudo)bulges. Several earlier figures show barless, late-type analogs which probably also are lenses (NGC 4736 in Figs. 1.3, 1.6 and 1.8; NGC 4151 in Fig. 1.8).
(e) Figure 1.19 shows a compelling observation that supports B → lens evolution. The top panels show rotation velocity $V$ and velocity dispersion $\sigma$ along the major axes of the barred S0(lens) galaxy NGC 3945 (Fig. 1.17) and the unbarred S0(lens) galaxy NGC 1553 (Fig. 1.7). The NGC 3945 bar is oriented along the minor axis, so the major-axis observations in Fig. 1.19 really measure the lens. The bottom panel shows $V/\sigma$ for these two galaxies plus NGC 2784 (Fig. 1.18) and two more SB0 galaxies. I conclude: (1) The inner part of each lens is hotter than its corresponding pseudobulge. That is, $\sigma$ is higher and $V$ is smaller in the lens than in the pseudobulge. (2) This behavior and the $V/\sigma$ radial profiles are the same in barred and unbarred lenses. (3) And $V/\sigma$ in these lenses is similar to $V/\sigma$ along the ridge line of the strong bar in NGC 936 (Kormendy 1983).

![Figure 1.19](image-url)
Thus the relative importance of ordered motions (rotation) and random motions is similar in lenses and bars, both observed and \( n \)-body-simulated. In particular, at about 40% of the radius \( r_{\text{_lens}} \) of the lens, \( V/\sigma \sim 0.8 \). Also, \( \sigma \) is the line-of-sight velocity dispersion, so the total velocity dispersion is likely to be at least a factor of \( \sqrt{2} \) larger. This means that the ratio of rotational kinetic energy to random kinetic energy is \( \sim 1/3 \) in the inner parts of both bars and lenses. That is, stellar orbits are similarly far from circular. Lenses are parts of disks (Freeman 1975), and yet they are hotter than their associated (pseudo)bulges. The close similarity of \( V^2/\sigma^2 \) in bars and lenses (cf. Bosma et al. 2010) means that it is relatively easy for bars to evolve into lenses – it is enough if \( x_1 \) orbits escape the persuasion to precess together that is supplied by bar self-gravity; it is not necessary to change their energies and angular momenta drastically.

(f) The fact that we see arbitrarily weak bars embedded in strong lenses is a powerful argument that these bars were once stronger (Kormendy 2004b). NGC 3081 in Fig. 1.17 is the best example. It contains an exceedingly faint bar, but almost all of the inner light is in the lens – which is much rounder – and the pseudobulge. Can we really imagine that one or two percent of the stars in a disk discover that they are bar-unstable, that they make a nice, highly elongated bar, and that most of the disk meanwhile stays just slightly oval? This is not what happens in \( n \)-body simulations of bar formation. There, essentially all of the disk participates in the instability, and most disk stars that live interior to the final radius of the bar participate in the bar. That's why \( n \)-body bars buckle in the axial direction – they are self-gravitating structures. Lenses, on the other hand, appear to be flat (e.g., Kormendy 1982b and Kormendy & Bender 2012). Thus the observation (Figs. 1.17 and 1.18) that there is a complete continuity from \( \text{bar}/\text{lens} \gg 1 \) to \( \text{bar}/\text{lens} \ll 1 \) to \( \text{bar}/\text{lens} = 0 \), together with the above results, strongly suggests that bars evolve into lenses. The fact that barless lenses are rare at early Hubble types implies that any evolution is relatively slow or that it stops when a galaxy gets transformed into an S0. The observation of barless ovals that appear to be equivalent to lenses in galaxies such as NGC 4736 and NGC 1068 implies that the evolution goes to completion more readily in galaxies that contain gas.

All of these suggestions are comfortably consistent with – and arguably could have been predicted from – our picture that bars drive secular evolution that builds up the central density by forming pseudobulges that are harmful to the survival of the bar.

I do not want to argue too forcefully for this picture. I especially do not want to suggest that bar \( \rightarrow \) lens evolution is the only thing that happens. But the most economical suggestion that is consistent with observations and simulations is that bars evolve away as they increase the central concentration of the galaxy. One result is lens components that have the same radii, shallow brightness gradients, and sharp outer edges as their parent bars. Some tests of this idea are suggested in Section 1.4.3.7.
1.4.3.6 Bar suicide and the origin of lens components.

III. What pseudobulge mass is required to destroy bars?

We get a preliminary idea of what $PB/T$ ratio divides SA and SB galaxies by examining values for intermediate-Hubble-type oval galaxies that are illustrated in this paper. Two more such galaxies are shown in Fig. 1.20. Table 1.1 shows the results. The sample is small. Also, $PB/T$ ratios of SAB galaxies vary widely, perhaps because the central concentrations of pseudobulges vary widely. Nevertheless, we derive a clean result, as follows.

Table 1 suggests that realistic pseudobulges with $PB/T \simeq 0.34 \pm 0.02$ are massive enough to destroy bars essentially completely and to convert them into lenses. This is a preliminary result, reported here for the first time.

Table 1.1. Pseudobulge-to-total luminosity ratios for barred and unbarred oval galaxies

| Galaxy       | Type      | $PB/T$      | Source                        |
|--------------|-----------|-------------|-------------------------------|
| NGC 2273     | SBa       | 0.19 ± 0.02 | Kormendy & Bender (2013)      |
| NGC 3393     | (R')SBab  | 0.27 ± 0.06 | Kormendy & Bender (2013)      |
| NGC 3081     | SAB0/a    | 0.11        | Laurikainen et al. (2010)     |
| NGC 3368     | SABab     | 0.25        | Kormendy & Bender (2013)      |
| NGC 4151     | (R')SABab | 0.327       | Gadotti (2008)                |
| UGC 3789     | (R)SAab   | 0.32 ± 0.03 | Kormendy & Bender (2013)      |
| NGC 1068     | (R)SAb    | 0.35 ± 0.05 | Kormendy & Bender (2013)      |
| NGC 4736     | (R)SAab   | 0.36 ± 0.01 | Kormendy & Bender (2013)      |

Fig. 1.20. Oval galaxies that bracket the $PB/T$ value which divides galaxies that do and do not have bars. The barred galaxy NGC 3393 has $PB/T = 0.27 \pm 0.06$; the unbarred galaxy UGC 3789 has $PB/T = 0.32 \pm 0.03$. This figure from Kormendy & Ho (2013) is based on Digital Sky Survey images from http://www.wikisky.org.
1.4.3.7 Remaining puzzles and suggestions for further work

Our understanding of the lives and deaths of bars is now reasonably well developed. A few particularly obvious problems and suggestions about how to address them are outlined below.

(a) How do bars form? Despite the long history of seeing violent instabilities when $n$-body systems are given small Toomre $Q$ by fiat, and despite convincing hints that tidal tickling helps, we understand bar formation less well than we think. We need to investigate bar growth both observationally by observing distant galaxies and by using simulations. Closely related and very important are (b) and (c).

(b) We need to study bar evolution via the competition between angular momentum sinks (the outer disk and dark halo), which make the bar grow stronger, and the increasing importance of ILR as the bar moves material inward, which makes the bar grow weaker. This is a complicated modeling job. But the great richness of possible interactions between nonaxisymmetric components is lost when the relevant components either are not included or are turned into fixed potentials. I do not criticize published papers for trying to distill clean subsets of the physics that we want to study. But there are effects that we cannot find if component interactions are switched off. In particular, it is likely that a bar can coexist with a more massive (pseudo)bulge if it grew in the context of the above competition.

(c) Including gas is critically important in studying bar evolution. Gas dissipation is essential for the inward flow of the material that builds pseudobulges. Whether recycled, not yet used up, or accreted from outside, gas helps to keep the disk cold enough to be responsive. Without it, $n$-body disks get so hot that spiral structure switches off and the disk gets less effective at absorbing angular momentum. Cosmological accretion of cold gas may be essential for realistic bar evolution.

(d) On the observational front, we need to measure the luminosity and mass functions of elliptical galaxies, classical bulges, pseudobulges and disks as a function of environmental density. Early observations demonstrate that the answers are different in clusters and in the field (Sandage et al. 1985a; Kormendy et al. 2010). But we need more quantitative measures of the relative importance of secular evolution and hierarchical clustering and merging as a function of environment.

(e) The idea that bars evolve into lenses needs to be tested further. Note how many relevant observations and theoretical hypotheses date from the 1980s. This is an opportunity for today’s students. We need absorption-line kinematic measurements of bars and lenses. We need photometry and component decomposition to see, e.g., whether the bar/lens luminosity ratio tends to be smaller as the (pseudo)bulge is more massive or more centrally concentrated. Caution: many decomposition codes use the assumption that each component has a flattening that is independent of radius. This is certainly wrong and commonly leads to unphysical conclusions (e.g., about numbers of components). And we need mass models to determine halo properties. There is much work to be done.
1.5 Secular evolution and the growth of pseudobulges

This section reviews the processes of secular evolution in disk galaxies and the structures that they produce. I begin with bar-driven evolution but also discuss why evolution happens in more than just barred galaxies. Much emphasis will be on the high-density central parts of galaxies that in the past were confused with merger-built bulges. As explained in Section 1.1.3, I call such components “pseudobulges” if — to the best of our knowledge — they were not made by mergers but rather were grown out of the disk.

The essential qualitative results of secular evolution were known more than 30 years ago at the time of my Saas-Fee lectures (Kormendy 1982b). From that review, Table 1.2 here lists the major structural components in galaxies and what we then thought we knew about their origin. All of the suggested formation mechanisms are strongly supported by more recent work and form the main subjects of these lectures. The only change that I have made in reproducing Table 1.2 is to remove a suggestion that the transition from

| Code | Component | Possible Formation Mechanism |
|------|-----------|------------------------------|
| Halo | Dissipationless collapse of ? during early phase of galaxy formation |
| Elliptical | Dissipationless collapse + mergers (star formation mostly precedes collapse) |
| E | Bulge |
| Thick Disk | |
| Thin Disk | Dissipational collapse (stars form after collapse) |
| S | Disk |
| Bar | Dynamical instability during collapse phase + later secular growth |
| (k) | Lens | Made from bar by destruction of resonance |
| (r) | Inner Ring | Disk material rearranged by bar |
| (R) | Outer Ring | Disk material rearranged by bar |
ellipticals and bulges to thick and thin disks is continuous. The only change in emphasis that I would make in reformulating the table now would be to emphasize major mergers as the origin of classical bulges and ellipticals and note that dissipation and starbursts occur naturally in wet mergers.

To bring this story up to date, let’s start by revisiting the definition of a classical bulge. The clearest statement that captures the intention of morphologists such as Sandage and de Vaucouleurs is by Alvio Renzini (1999): “A bulge is nothing more nor less than an elliptical galaxy that happens to live in the middle of a disk.” There is a world of information hidden in this beguilingly simple definition:

First, what is an elliptical? Formally, this subject is beyond the scope of these lectures. We understand that ellipticals form by major galaxy mergers and not by secular processes. Still, we cannot understand pseudobulges without knowing something about classical bulges and ellipticals. Moreover, some lecturers at this school (notably Isaac Shlosman and Nick Scoville) focus on our standard picture of the evolution of structure by hierarchical clustering and galaxy mergers. I try to connect this story with our picture of secular evolution in Section 1.8. Some properties of elliptical galaxies and classical bulges are compared in Section 1.7. Here, I list the properties that we need in the present section. Classical bulges and elliptical galaxies

(a) have smooth, nearly elliptical isophotes;
(b) have Sérsic (1968) function \( \log I(r) \propto r^{-1/n} \) brightness profiles that fall steeply toward larger radii \( r \) with \( 2 \lesssim n \lesssim 4 \) for most bulges (e.g., Fisher & Drory 2008);
(c) satisfy the same “fundamental plane” correlations (Djorgovski & Davis 1987; Faber et al. 1987; Djorgovski et al. 1988; Bender et al. 1992) between the “effective radius” \( r_e \) that contains half of the total light, the “effective surface brightness” \( \mu_e \) at \( r_e \) and the total absolute magnitude \( M_V \) (Fisher & Drory 2008; Kormendy & Bender 2012) as illustrated here in Fig. 1.68 and
(d) generally rotate approximately as rapidly as oblate spheroidal stellar systems that have isotropic velocity dispersions and that are flattened mainly by rotation (e.g., Kormendy & Illingworth 1982).

Point (c) is the most important, because some of (a), (b) and (d) are shared by other kinds of ellipsoidal stellar systems called “spheroidals” (Section 1.7).

I adopt the Renzini definition, because it embodies the idea that I want to emphasize, namely that the definition of a component should be made in terms of its formation physics as well as its observed properties.

The problem with our definition is that it is difficult to apply, especially to galaxies that are not seen edge-on. Therefore it is common to use one of two surrogate definitions as illustrated in Fig. 1.21. When a galaxy disk is
seen nearly edge-on (e.g., NGC 4594, at center), then the part of the galaxy that is like an elliptical (e.g., M 87, at left) is the high-surface-brightness, centrally concentrated component that is thicker than the disk. When the galaxy is seen nearly face-on, we cannot see such a central thickening. But we know from galaxies like NGC 4594 that the brightness profile of the bulge is much steeper than that of the disk and extends, near the center, to much higher surface brightnesses than those of the disk. NGC 1353 in Fig. 1.21 shows a clear separation between the high-surface-brightness central (pseudo)bulge and the outer exponential disk. It also illustrates how we decompose the surface brightness profile of a face-on galaxy into bulge and disk parts that add up to the observed profile. Bulge-disk decomposition is discussed in Section 1.7.4.1. Here, I note the surrogate definition of a bulge that is used when a galaxy is seen nearly face-on: it is the central part of the galaxy that is defined by the extra light above the inward extrapolation of the outer, exponential or Sérsic disk profile. That is, the bulge-dominated part of NGC 1353 is the part at $r \lesssim 10''$. It happens to be a pseudobulge rather than a classical bulge, but this does not affect the surrogate definition.

The good news is that classifying bulges by using the surrogate definitions is easy. The bad news is that we don’t know what they are physically. That is, there is no guarantee that the surrogate definitions always identify central components that originate via the same formation physics. In fact, I will try to convince you in this section that the surrogate definitions often identify high-surface-brightness central components that are nothing like ellipticals, especially in late-type galaxies.
Therefore, I adopt a different approach that is more physically motivated but also more hazardous (Kormendy & Kennicutt 2004). I define classical bulges to be elliptical galaxies that happen to live in the middle of a disk. For this to make sense physically, we need to check that there exist central components of disk galaxies that have essentially all of the properties of comparable-luminosity elliptical galaxies. This check has been made; it is discussed in Sections 1.7.4.4 and 1.8.1. The intention is that classical bulges, like ellipticals, form via major galaxy mergers. In contrast, I define a pseudobulge as the dense central part of a galaxy – either a thick component that bulges above and below an edge-on disk or the extra light at small radii above the inward extrapolation of the outer disk profile – that was constructed from the disk by (mostly) secular processes. For this definition to make sense, we need to see convincing evidence that secular disk evolution happens and that it makes pseudobulges that we know how to identify. We have such evidence; the classification criteria are listed in Section 1.5.3. There turn out to be three generic kinds of pseudobulges (Fig. 1.22).

These definitions involve different practical problems. We always know what we are talking about physically. But it may be difficult to apply the classification criteria. I prefer this problem to the ones above that are inherent in a descriptive classification. My job in the rest of this section is to present the case for a physically motivated definition of pseudobulges.

Fig. 1.22. Powerpoint slide illustrating three kinds of pseudobulges. Section 1.5.2.9 discusses boxy pseudobulges as vertically buckled bars. Construction of disky pseudobulges is discussed here. For nuclear bars, see Section 1.5.2.8.
1.5.1 The response of gas to a rotating bar: 
Construction of outer rings, inner rings and pseudobulges

Figure 1.23 shows the fundamental results of bar-driven secular evolution. The disk spreads (Section 1.2). Gas at large radii gains angular momentum; it moves to still larger radii and is shepherded into an outer ring near OLR. This is identified with the outer rings in (R)SB galaxies (Fig. 1.24). Gas at small radii gives up some of its angular momentum and falls to the center. High-density gas likes to make stars; we see starbursts in Figs. 1.29 – 1.31. We identify the result as a pseudobulge. In between, gas is focused into a ring around the end of the bar, the inner ring seen in SB(r) galaxies (Fig. 1.24).

Fig. 1.23. Gas particle distributions in a “sticky particle” simulation of the response of cold gas to a rotating bar. The bar is not shown but, in each panel, is horizontal and has a diameter equal to that of the inner ring in the last panel. The panels show the gas response after 2, 3, 5 and 7 bar rotations (numbers at upper-right in each panel). The arrows in the first and last panels indicate the position of the inner Lindblad resonance (ILR), the corotation resonance (CR) and the outer Lindblad resonance (OLR). From Simkin et al. (1980).
Figure 1.24 shows the close correspondence between the features produced in the Simkin et al. (1980) simulation and the morphology of barred galaxies. More sophisticated hydrodynamic calculations clarify the physics (Fig. 1.26), but it is remarkable that just letting gas particles stick together when they collide is enough to reach the most basic conclusions.

Fig. 1.24. Examples of galaxies which show the morphological features that were produced in the sticky particle simulation of Simkin et al. (1980). NGC 3945 is from a photographic plate that I took with the Mount Wilson 100-inch telescope; the others are from the de Vaucouleurs Atlas of Galaxies (Buta et al. 2007). All four galaxies have complete or almost complete outer rings (R). ESO 426-2 and NGC 3081 have both an outer ring and an inner ring (r); such galaxies are rare. NGC 2217 contains a lens component that is filled by the bar in one dimension. NGC 3945 and NGC 3081 are also illustrated in Fig. 1.17. Additional galaxies with similar morphology are shown in Figs. 1.3, 1.6, 1.8, 1.9, 1.17, 1.36, 1.37 and 1.45.
Figure 1.25 explores the difference between SB(r) and SB(s) galaxies. Sanders & Tubbs (1980) investigated how the response of gas to a bar varies with bar pattern speed and strength. Fast bars have small corotation radii; e.g., $r_{\text{cor}}/(\text{disk scale length}) = 0.7$ in the bottom-left model panel. They drive SB(s) structure like that in NGC 1300. Slower bars end near corotation ($r_{\text{cor}}/a = 1.1$) and drive SB(r) structure like that in NGC 2523. Since bars slow down as they evolve (Fig. 1.13) and since it takes time to collect gas into an inner ring, we conclude that SB(s) galaxies are dynamically young and that SB(r) galaxies are dynamically mature.

Fig. 1.25. Contours of steady-state gas density in response to a bar (adapted from Sanders & Tubbs 1980, who also show intermediate cases). The bar is horizontal and has a length equal to four axis tick marks. The top row explores the effect of varying the ratio $M_B/M_D$ of bar mass to disk mass. The second row varies the bar axial ratio $b/a$. The third row varies the bar pattern speed, parametrized by the ratio $r_{\text{cor}}/a$ of the corotation radius to the disk scale length. The middle column is the same standard model in each row; it resembles the SB(r) galaxy NGC 2523. The left panels resemble the SB(s) galaxy NGC 1300. The right panels take the parameters to unrealistic extremes; they do not resemble real galaxies.
Consistent with this conclusion is the observation (Sandage 1975) that dust lanes on the rotationally leading sides of bars are common in SB(s) galaxies but rare in SB(r) galaxies (cf. Figs. 1.6, 1.24, 1.25). The gas between the inner ring and the pseudobulge has largely been depleted in SB(r) galaxies (see Kormendy & Barentine 2010: Fig. 1.46 here and Barentine & Kormendy 2012 for examples).

Sanders & Tubbs (1980) also investigated the effects of varying the strength of the imposed bar potential, measured both by the ratio of bar mass to disk mass \( M_B/M_D \) (top row of simulation results in Fig. 1.25) and by the axial ratio \( b/a \) of the bar (middle row of simulation results). Very weak bars (\( M_B/M_D = 0.13 \)) or bars that are not very elongated (\( b/a = 1/2 \), more like an oval disk than like a bar) produced weak SB(s) structure that does not resemble well developed SB(s) galaxies such as NGC 1300. Parameters that are more realistic in matching strongly barred galaxies (\( M_B/M_D = 0.53 \), \( b/a = 1.4 \), and \( r_{\text{cor}}/a = 1.1 \); i.e., the standard model shown in the middle column of model results) provided the best match to an SB(r) galaxy. This model shows a linear maximum in gas density that is parallel to the bar and offset from it in the forward rotation direction like the straight dust lanes in SB(s) galaxies. But the bar potential and gas content are imposed by the initial conditions; they are not self-consistently evolved from more axisymmetric initial conditions. This accounts for the (rarely observed) coexistence of the offset gas density maximum in the bar and the (r) structure. Finally, note that, when the bar is much stronger than bars in real galaxies (\( M_B/M_D = 2.7 \)) or much slower than in real galaxies (\( r_{\text{cor}}/a = 3 \)), the gas response fails to resemble that in observed galaxies.

Better simulations generally confirm and expand on the above conclusions (e.g., Salo et al. 1999; Rautiainen & Salo 2000; Rautiainen et al. 2005; Treuthardt et al. 2009; see Kormendy & Kennicutt 2004 for further review). In particular, detailed hydrodynamic models of the gas response in the region of the bar confirm the offset density maximum seen in the Sanders & Tubbs (1980) model and greatly clarify the nature of bar-driven secular evolution.

The most illuminating simulations are by Athanassoula (1992), shown here in Fig. 1.26. She explored the response of inviscid gas to an imposed bar, concentrating on the production of gas shocks and their relation to dust lanes. If the mass distribution is sufficiently centrally concentrated to result in an ILR, then she found that straight gas shocks – which we identify with dust lanes – are produced that are offset in the forward (rotation) direction from the ridge line of the bar. The “\( x_2 \) orbits” that align perpendicular to the bar inside ILR push the offset to be largest near the center. This is seen in Fig. 1.26 and Fig. 1.27 as well as in Fig. 1.5 and Fig. 1.6.
Fig. 1.26. Comparison of the gas response to a bar (Athanassoula 1992 model 1) with NGC 1365. The galaxy image is from the VLT and is reproduced courtesy of ESO. In the models, the bar potential is oriented at $-45^\circ$ to the vertical, parallel to the lowest-density (dark) part of the gas density grayscale distribution at upper-left. The bar axial ratio is 0.4 and its length is approximately half of the box diagonal. The top-right panel shows the velocity field; arrow lengths are proportional to flow velocities. Discontinuities in gas velocity indicate shocks at the narrow ridge lines of high gas density in the upper-left panel. High gas densities are identified with dust lanes in real galaxies. The model correctly reproduces the observations that dust lanes are offset in the forward rotation direction from the ridge line of the bar, that they are offset by larger amounts nearer the center, and that very near the center, they curve and become nearly azimuthal. The bottom-right panel shows the $\text{H} \, \text{I}$ velocity field of NGC 1365 from Lindblad et al. (1996). The contour interval is 20 km s$^{-1}$. The velocity contours crowd strongly in the dust lanes shown at lower-left (the scales of the two panels are slightly different). This supports the interpretation that the dust lanes are signatures of shocks in the gas velocity field. Shocks are signs that the gas loses energy. It must fall toward the center. In fact, NGC 1365 has high gas densities and active star formation in its bright center (Lindblad 1999; Curran et al. 2001a, b). Adapted from Fig. 7 of Kormendy & Kennicutt (2004).
The consequence of shocks is that they inevitably imply that gas flows toward the center. Because the shocks are nearly radial, gas impacts them at a steep angle. Therefore the velocity that is lost in the shock is mainly rotational. This robs the gas of energy and forces it to fall toward the center.

Important confirmation of these results is provided by the observation that H1 gas velocity contours crowd closely just where we observe dust lanes in optical images (e.g., NGC 1365 in Fig. 1.26 and NGC 1530 in Fig. 1.27). The H1 observations do not have high enough spatial resolution to prove that a shock must be present, but the rapid change in the velocity field coincident with the dust lane strongly supports the above evolution picture.

It is easy to get a heuristic understanding of the gas velocity field shown in Fig. 1.26. Gravitational torques produced by the bar accelerate the gas as it approaches the bar. As a result, it climbs to larger radii as it crosses the ridge line of the bar. Then, as it leaves the bar, the bar potential minimum is behind the gas and decelerates it. Incoming gas overshoots a little before it plows into the departing gas, so the shocks are nearly radial but offset from the ridge line of the bar in the rotationally forward direction.

Fig. 1.27. NGC 1530 is another excellent example of the crowding of H1 velocity contours at the position of the dust lane in an SBb galaxy. The image is from http://www.caelumobservatory.com/gallery/n1530.shtml courtesy of Adam Block. The velocity field is from Regan et al. (1997) courtesy of Michael Regan.
Do observations show central concentrations of gas in barred galaxies and in other galaxies (e.g., oval disks) in which the above secular evolution is expected to happen? And do they not show such central gas concentrations in the absence of engines for secular evolution? Figure 1.28 provides six examples of the general result that the answer is “yes”.

Fig. 1.28. Radial profiles of CO gas and stellar K-band surface brightness from the BIMA SONG (Fig. 20 from Kormendy & Kennicutt 2004, adapted from Regan et al. 2001). CO surface brightness is in magnitudes of Jy km s$^{-1}$ arcsec$^{-2}$ with zeropoint at 1000 Jy km s$^{-1}$ arcsec$^{-2}$. The stellar surface brightness profiles have been shifted vertically to the CO profiles. Morphological types are from the RC3 (de Vaucouleurs et al. 1991) and oval disks are identified in Kormendy & Kennicutt (2004). NGC 4736 is a prototypical pseudobulge also illustrated in Figs. 1.3, 1.6 and 1.8. All galaxies in this figure except NGC 7331 have structures that are expected to cause gas to flow toward the center. NGC 7331 is included to show the very different CO profile in a galaxy with a probable classical bulge (cf. Fig. 1.29).
What happens to the infalling gas? Concentrated into a small volume, it gets very dense. Crunching gas likes to make stars. The Schmidt (1959) – Kennicutt (1989, 1998a, 1998b) law that star formation rates increase faster than linearly with gas density makes this explicit (Fig. 1.32 here). Confirming our expectations, observations point to enhanced star formation, often in spectacular starbursts, near the centers of barred and oval galaxies. In particular, Spitzer Space Telescope mid-infrared observations in the 24 µm bandpass are sensitive to warm dust that reradiates light from hot young stars (Fig. 1.29). Survey results by Fisher (2006) and Fisher et al. (2009) show ubiquitous central star formation in medium- and late-type barred and oval galaxies but not in galaxies with classical bulges (Fig. 1.29).
More detailed views of this star formation are shown in Figs. 1.30 and 1.31. Figure 1.30 shows NGC 5236, a particularly close and well known example. The dust lanes on the rotationally trailing sides of the spiral arms are believed to have the same cause as the ones on the leading sides of the bar: they trace shocks where the gas enters the spiral arms. Star formation is triggered there by gas compression. Since $\Omega > \Omega_p$, the gas moves forward, beyond the shock, during the time that it takes stars to form. As a result, the ridge line of bright young stars and H II regions that “are strung out like pearls along the arms” (Baade 1963) is offset forward of the dust lanes. Our picture of how spiral density waves stimulate star formation and hence are traced by young stars is discussed in Roberts (1969); Dixon (1971); Shu et al. (1973) and Roberts et al. (1975) and is reviewed in Toomre (1977b).

Returning to bar-driven inward gas transport and its consequences, the central regions of NGC 5236 are dominated by intense star formation (Harris et al. 2001; Knapen et al. 2010). Similarly, the whole of the central region of NGC 1365 (Fig. 1.26) is undergoing a starburst (Kristen et al. 1997; Galliano et al. 2008; Elmegreen et al. 2009) A less intense but still prototypical example is NGC 1300 (Fig. 1.6; Knapen et al. 2006; Comerón et al. 2010).

Spiral galaxies in which there is no significant ILR and in which the spiral structure extends to the center can also have central starbursts (for example, NGC 4321, Knapen et al. 1995a, b; Sakamoto et al. 1995).

Fig. 1.30. M 83 = NGC 5236 is a prototypical face-on SAB(s)c galaxy with dust lanes on the trailing sides of the spiral arms and the leading sides of the bar. The center is undergoing a spectacular starburst. The left image is from the ESO VLT [http://www.eso.org/public/images/eso9949a/] with color balance tweaked to better match the enlargement at right, which is a Hubble Heritage image).
Nuclear starburst rings are particularly compelling examples of the star formation that – we suggest – results from inward transport of disk gas. Figure 1.31 shows examples. Three of these galaxies are barred, but NGC 4736 is in my prototypical unbarred, oval galaxy (Figs. 1.3, 1.6, 1.8). It emphasizes again that numerical simulations and observations both imply that oval galaxies evolve secularly in the same way that barred galaxies do.

Fig. 1.31. Nuclear star-forming rings in barred and oval galaxies (update of Fig. 8 in Kormendy & Kennicutt 2004). Sources: NGC 4314 – Benedict et al. (2002); NGC 1326 – Buta et al. (2000) and Zolt Levay (STScI); NGC 1512 – Maoz et al. (2001); NGC 4736 – Zolt Levay (STScI). The NGC 4736 panel was made from nonoverlapping images in the bandpasses indicated by the colors used in these RGB renditions. All colors are available in only two places around the ring, but they make it clear that this star-forming ring in a prototypical oval galaxy (see Figs. 1.3, 1.6 and 1.8) is closely similar to the other nuclear rings, which occur in barred galaxies. Note that these nuclear rings are distinct from and always smaller than the inner rings that encircle bars (see point (f) in Section 1.3.1).
The star formation discussed in this section is not associated with galaxy mergers and instead is closely connected with probable engines for secular evolution and with observed features (such as radial dust lanes in bars) which suggest that such evolution is in progress. We conclude with some confidence that it is building pseudobulges. Are the gas supplies and star formation rates (SFRs) consistent with reasonable growth times for pseudobulges of the observed masses?

Kormendy & Kennicutt (2004) address this for nuclear star-forming rings (Fig. 1.32). The rings have larger SFR densities $\Sigma_{\text{SFR}}$ and total gas densities $\Sigma_{\text{gas}}$ than do spiral galaxies in general, defining a Schmidt-Kennicutt relation similar to the well known $\Sigma_{\text{SFR}} \propto \Sigma_{\text{gas}}^{1.4}$. Absent continued gas infall, the

Fig. 1.32. Correlation between SFR surface density and total gas surface density for circumnuclear star-forming rings (filled squares) compared to disk-averaged values for spiral galaxies (filled circles) and the centers of these galaxies (open circles). The nuclear ring data are compiled in Kormendy & Kennicutt (2004, from which this figure is taken); the other data are from Kennicutt (1998b). Diagonal lines show gas consumption timescales if no additional gas is supplied to the central region.
currently available gas would be consumed in $\sim 0.2 - 2 \text{ Gyr}$. However, I have argued that the central gas is continually replenished. Thus the observed SFRs of $0.1 - 10 \, M_\odot \, \text{yr}^{-1}$ are consistent with the formation of pseudobulges with masses $\sim 10^8 - 10^{10} \, M_\odot$ over several Gyr. These values are reasonable.

Fisher et al. (2009) and Fisher & Drory (2010) use the Spitzer Space Telescope to study SFRs and star formation histories in classical and pseudo bulges in detail. They conclude (2009) that “All bulges are found to be forming stars irrespective of bulge type (pseudobulge or classical bulge). [However,] classical bulges have the lowest specific SFR [SFR per unit stellar mass], implying growth times that are longer than a Hubble time, thus the present-day SFR does not likely play a major role in the evolution of classical bulges. [In contrast,] at present-day SFRs, the median pseudobulge could have grown the present-day stellar mass in 8 Gyr. In almost all galaxies in our sample, the specific SFR of the bulge is higher than that of the outer disk. This suggests that almost all galaxies are increasing their $B/T$ through internal star formation. The SFRs in pseudobulges correlate with their structure. More massive pseudobulges have higher SFR density, this is consistent with the stellar mass being formed by moderate, extended star formation. Bulges in late-type galaxies have similar SFRs as pseudobulges in intermediate-type galaxies and are similar in radial size. However, they [have lower masses]; thus, they have much shorter growth times, $\sim 2 \text{ Gyr}$. Our results are consistent with a scenario in which bulge growth via internal star formation is a natural and near ubiquitous phenomenon in disk galaxies.”

I want to emphasize the contrast between star formation in major mergers and star formation during secular evolution (Kormendy & Kennicutt 2004). Merger starbursts last $\lesssim$ a few hundred million years. Most classical bulges and ellipticals are seen long after the assembly events that constructed them. Therefore, they are mostly seen to contain old stars. In contrast, secular evolution is inherently long-term. Except in S0 pseudobulges, we usually see star formation in action. If star formation is ubiquitous, it must be secular. As a result, ongoing star formation that is not observed to be associated with morphological indicators of a merger in progress (such as tidal tails) is the first pseudobulge classification criterion listed in Section 1.5.3.

We have a detailed picture of internal secular evolution in galaxy disks. Central molecular gas concentrations and starbursts are closely associated with bars and oval disks that act as evolution engines. They are not generally found in classical bulges. They are also closely associated with dust lanes and HI velocity crowding in bars that are signatures of secular evolution. These correlations argue in favor of internal secular evolution and against the idea that these features could be produced by large numbers of minor mergers.
1.5.2 The observed properties of pseudobulges

Quoting Kormendy & Kennicutt (2004): “How can we tell whether a (pseudo)bulge is like an elliptical or whether it formed secularly? The answer and the theme of this section is that pseudobulges retain enough memory of their disky origin so that the best examples are easily recognizable.” As we move from “proof of concept” into work on large samples of galaxies, we will have to face the difficulty that classification gets difficult when – as we must expect – both a classical bulge and a subsequently grown pseudobulge are present. In such cases, bulge-pseudobulge decomposition is necessary (e.g., Erwin et al. 2003). In this section, I discuss the properties of more prototypical, pure pseudobulges to show how they differ from classical bulges and ellipticals. Section 1.5.3 then lists the classification criteria, numbered according to the subsections in the following discussion.

1.5.2.1 Pseudobulges of spiral galaxies show ongoing star formation

As noted in the previous section, ongoing central star formation in relatively normal spiral galaxies that show no signs of a merger in progress is a strong pseudobulge indicator. The work by Fisher et al. (2009, 2010) shows that such star formation is generally present in morphologically classified pseudo but not classical bulges. If star formation is ubiquitous, it must be secular.

1.5.2.2 Pseudobulges are flatter than classical bulges

This is a two-part criterion. First, when the galaxy is highly inclined and the ellipticity profile $\epsilon(r)$ tells us the relative flattening of various components, pseudobulges are often (not always) seen to be flatter than classical bulges. Commonly a part of them is as flat as the associated outer disks. Second, pseudobulges in spiral (but not S0) galaxies usually show spiral structure all the way to the center of the galaxy. Classical bulges, like ellipticals, are essentially never flatter than $\epsilon = 0.6$. They cannot show spiral structure. This classification criterion can be applied even to face-on galaxies.

The connection between pseudobulge flatness and secular evolution has been made since the earliest papers on this subject. Kormendy (1993b) describes the prototypical pseudobulge in NGC 4736 like this: “The central brightness profile is an $r^{1/4}$ law that reaches the high central brightness characteristic of a bulge (Boroson 1981). However, the $r^{1/4}$-law component shows a nuclear bar and spiral structure to within a few arcsec of the center. Bars are disk phenomena. More importantly, it is not possible to make spiral structure in a bulge. Thus the morphology already shows that the $r^{1/4}$-law profile belongs to a disk. This is shown more quantitatively by [rapid rotation]”, which is discussed here in Section 1.5.2.3.
The importance of spiral structure is further emphasized by Courteau et al. (1996): “Many of these [late-type] galaxies [in their sample] show spiral structure continuing into the central regions. ... We invoke secular dynamical evolution and gas inflow via angular momentum transfer and viscous transport” as the interpretation of the disky central structure.

Spectacular examples of disky pseudobulges often with spiral structure emerge from HST imaging surveys. The best known of these is by Carollo and collaborators (Carollo et al. 1997, 1998; Carollo & Stiavelli 1998; Carollo 1999; Carollo et al. 1999, 2002; Seigar et al. 2002). They refer to bulges that are structurally unlike ellipticals as “irregular bulges” and note that: “The widespread presence of star formation in the irregular bulges support scenarios in which a fraction of bulges form relatively late, in dissipative accretion events driven by the disk.” Figures 1.33 and 1.34 show examples.

![NGC 1353 pseudobulge](image)

Fig. 1.33. NGC 1353 pseudobulge: the images show (left to right and top to bottom) the 2MASS JHK image with a field of view of 4′4 × 4′4 (Jarrett et al. 2003), an HST WFPC2 F606W image (Carollo et al. 1998), and an 18″ × 18″ zoom of the F606W image. The plots show surface photometry with the HST profile shifted to the K band; μ is surface brightness, ε is ellipticity and PA is position angle. A bulge-disk decomposition of the major-axis profile into a Sérsic function plus an exponential disk (curves) shows that a “bulge” dominates at radii r < 10″. This component is identified as a pseudobulge (1) because it has the same apparent flattening as the disk (compare the 18″ and large-field views), (2) because it shows small-scale spiral structure that can only be sustained in a disk, (3) because patchiness indicates the presence of dust and star formation and (4) because its Sérsic index n = 1.3 ± 0.3 is less than 2. From Kormendy & Kennicutt (2004) which shows more examples.
Figure 1.34 shows HST images of the central parts of Sa–Sbc galaxies. All show flat shapes, spiral structure, of patchy star formation. These are the central regions that, by the surrogate definitions, would be identified as the galaxies’ bulges. It seems safe to conclude that no one who saw these images would define bulges as mini-ellipticals that live at the centers of disks.
1.5.2.3 Pseudobulges are more rotation-dominated than classical bulges

Pseudobulges were first recognized because rotation is more important with respect to random motions than it is in classical bulges. Via the $V_{\text{max}}/\sigma - \epsilon$ diagram (Fig. 1.35) for galaxies such as NGC 3945 and NGC 4736, Kormendy (1982a, b) concluded that some “SB bulges are more disklike than SA bulges” and: “a significant fraction of the bulge in many SB galaxies may consist of disk gas which has been transported to the center by the bar. As the gas accumulates, it forms stars and builds up a centrally concentrated stellar distribution which is photometrically like a bulge but dynamically like a disk.” Again, the fundamental ideas about secular evolution have been with us for a long time. These results are brought up to date with more recent long-slit spectroscopy in Fig. 1.35. The result is that $V_{\text{max}}/\sigma$ is larger at a given $\epsilon$ in pseudobulges (most filled symbols) than in classical bulges (open symbols) or in ellipticals (crosses).

Fig. 1.35. Relative importance of rotation and random velocity as a function of ellipticity $\epsilon = (1 - \text{axial ratio})$ for various kinds of stellar systems. Here $V_{\text{max}}/\sigma$ is the ratio of the maximum rotation velocity to the mean velocity dispersion interior to $r_e$. The “Oblate” line describes oblate-spheroidal systems that have isotropic velocity dispersions and that are flattened by rotation; it is a consequence of the tensor virial theorem (Binney & Tremaine 1987). From Kormendy & Fisher (2008).
The disky dynamics of pseudobulges are beautifully illustrated by the SAURON team’s integral-field spectroscopy. This result is particularly important, so Figs. 1.36 and 1.37 show three examples in detail. In Fig. 1.36, the surface brightness profile tells us the part of NGC 4274 that the surrogate definitions would identify as the bulge. It dominates at \( r \lesssim 10'' \). The two-dimensional kinematic and line-strength maps then show that, compared to the rest of the inner parts of the galaxy, the component at \( r \lesssim 10'' \) rotates more rapidly, has a lower velocity dispersion, and has stronger H\beta absorption lines. The latter result means that the central disky structure is made of younger stars than the rest of the galaxy. As Falcón-Barroso et al. (2006) and Peletier et al. (2007a, b; 2008) note, all this is very consistent with our picture of bar-driven secular evolution.

Figure 1.37 shows closely similar results for the SB galaxies NGC 3623 and NGC 5689. It is remarkable how clearly the central component is a rapidly rotating, cold disk in all three galaxies. The younger ages of the pseudobulges also supports our evolution picture. Note again that all three galaxies are barred.

Fig. 1.36. SAURON integral-field spectroscopy of the disky pseudobulge of the Sa galaxy NGC 4274. The galaxy is barred, but the bar is foreshortened, because it is oriented nearly along the minor axis. It fills an inner ring, as is normal in SB(r) galaxies (Kormendy 1979b). The brightness profile (upper-right) is decomposed into a Sérsic (1968) function plus an exponential disk. The Sérsic function has \( n = 1.3 \), i.e., \( n < 2 \), as in other pseudobulges (Section 1.5.2.6). The pseudobulge dominates the light at radii \( r \lesssim 10'' \). The kinematic maps (Falcón-Barroso et al. 2006) show that this light comes from a disky component that is more rapidly rotating (center), lower in velocity dispersion (right), and stronger in H\beta line strength (left, from Peletier et al. 2007a) and hence younger than the rest of the inner galaxy. From Kormendy & Fisher (2008) as adapted from Peletier et al. (2007b, 2008).
Fig. 1.37. SAURON integral-field spectroscopy of the disky pseudobulges of the SB0 galaxy NGC 5689 and the SABa galaxy NGC 3623 (adapted from Falcón-Barroso et al. 2006). Again, both bars are oriented nearly along the minor axis. As in NGC 4274, the bar in NGC 3623 fills an inner ring. Also as in NGC 4274, the kinematic maps show that both galaxies contain pseudobulges that are prominently disky and more rapidly rotating (center), lower in velocity dispersion (right), and stronger in Hβ line strength (left) and hence younger than the rest of the inner galaxy. It is important to emphasize that pseudobulges generally show more than one (here: three) of the classification criteria listed in Section 1.5.3).

1.5.2.4 Pseudobulges have small velocity dispersions for their luminosities
Pseudobulges have smaller $\sigma$ than do classical bulges of the same $M_B$ (e.g., Kormendy & Illingworth 1983; Kormendy & Kennicutt 2004; Gadotti & Kauffmann 2009; cf. Falcón-Barroso et al. 2006; Peletier et al. 2007a). This could partly be due to low $M/L_B$ ratios resulting from young stars.
1.5.2.5 Almost all pseudobulges have bulge-to-total ratios $PB/T \lesssim 1/3$.

Bulges with $B/T \gtrsim 1.2$ are classical.

Fisher & Drory (2008) study the properties of (pseudo)bulges in 79, S0–Sc galaxies to clarify our classification criteria. They show that, in general, different classification criteria agree in distinguishing pseudobulges from classical bulges. To do this work, they need first to classify bulges using purely morphological criteria (Fig. 1.38). This has the disadvantage that morphology alone cannot always identify pseudobulges in S0 galaxies. But it lets them study a large sample, and it allows a fair test of (for example) the already strong hint (see Kormendy & Kennicutt 2004) that the Sérsic indices of pseudobulges are smaller than those of classical bulges.

Fig. 1.38. Morphological features used by Fisher & Drory (2008; 2010) to classify bulges as classical or pseudo. Classical bulges have smooth, nearly featureless and nearly elliptical isophotes as do elliptical galaxies (NGC 3998, NGC 3031 = M81). Pseudobulges show one or more of the following: nuclear bars, spiral structure, or patchy star formation (bottom four galaxies). From Fisher & Drory (2010).
Fisher & Drory (2008) measure surface brightness profiles of their galaxies using *Hubble Space Telescope* (HST) archival images, their own large-field images from the McDonald Observatory 0.9 m telescope and images from archives such as the Sloan Digital Sky Survey (SDSS). Combining data from many sources provides accurate profiles over wide dynamic ranges. They decompose the brightness profiles into disk components with exponential profiles and (pseudo)bulge components with Sérsic (1968) function profiles. Figure 1.39 is an example.

This work further confirms the pseudobulge properties discussed in previous sections and provides several new results:

About half of early-type galaxies contain pseudobulges; almost all Sbc galaxies contain pseudobulges, and as far as we know, no Sc or later-type galaxy has a classical bulge (see Fig. 1.40). This is in excellent agreement with results discussed in Kormendy & Kennicutt (2004).

Pseudobulges are often as flat as their associated disks; classical bulges are thicker than their associated disks. NGC 3031 = M 81 and NGC 3169 in Fig. 1.39 are examples.

Fig. 1.39. Photometric decompositions of a galaxy with a classical bulge (M81, left) and one with a pseudobulge (NGC 3169). Classification is carried out as in Fig. 1.38. In the bottom panels, the filled circles are the major-axis profiles and the solid curves are the Sérsic function (pseudo)bulge, the exponential disk and their sum, which is almost invisible atop the data points. The fit is made between the vertical dashes; note that both galaxies contain nuclear star clusters (“nuclei”) in addition to their bulges. The Sérsic index and the fit RMS are given in the key. The middle panel shows the deviations of the fit from the data in more detail. The top panel shows the total ellipticity profile. From Fisher & Drory (2008).
Fig. 1.40. Logarithm of (pseudo)bulge-to-total luminosity ratio $B/T$ versus Hubble type. Bulges are classified as in Fig. 1.38. Black squares show how the average $B/T$ for pseudobulges and classical bulges together correlates with Hubble type as expected from its use as a Hubble classification criterion (Sandage 1961). Note: some pseudobulges have $\log B/T < -1.6$. From Fisher & Drory (2008).

Pseudobulge-to-total luminosity ratios are almost always $PB/T \lesssim 0.35$ (Fig. 1.40), consistent with the expectation that one cannot secularly convert almost all of a disk into a bulge (Kormendy & Kennicutt 2004). Small bulge-to-total luminosity ratios $B/T$ do not guarantee that a bulge is pseudo, but large $B/T \gtrsim 0.5$ guarantee that it is classical.

1.5.2.6 Most pseudobulges have Sérsic $n < 2$. Classical bulges have $n \geq 2$. Figures 1.33 and 1.36 show that the pseudobulges in NGC 1353 and NGC 4274 have Sérsic indices $n = 1.3 \pm 0.3$; i.e., almost-exponential brightness profiles. The pseudobulge in NGC 3169 (Fig. 1.39) has $n = 1.45 \pm 0.24$, which is still close to exponential. In contrast, the classical bulge of M81 has $n = 3.79 \pm 0.39$. This difference turns out to be a general result.

Kormendy & Kennicutt (2004) review the history of this result. The idea that bulges in late-type galaxies have nearly exponential (not $r^{1/4}$-law) brightness profiles dates back to work by Andredakis & Sanders (1994) and Andredakis et al. (1995). At first, no connection was made to pseudobulges; the result was just that $n$ is smaller in bulges of later-Hubble-type galaxies.
Then Courteau et al. (1996) carried out bulge-disk decompositions for > 300 galaxies and concluded that > 2/3 of them – especially at late Hubble types – are best fitted by double exponentials, one for the bulge and one for the disk. As a diagnostic of formation processes, Courteau et al. (1996) went on to examine the ratio $h_b/h_d$ of the scale lengths of the inner and outer exponentials. They found that $h_b/h_d = 0.08 \pm 0.05$ and concluded that: “Our measurements of exponential stellar density profiles [in bulges] as well as a restricted range of [bulge-to-disk] scale lengths provide strong observational support for secular evolution models. Self-consistent numerical simulations of disk galaxies evolve toward a double exponential profile with a typical ratio between bulge and disk scale lengths near 0.1 (D. Friedli 1995, private communication) in excellent agreement with our measured values”.

Fisher & Drory (2008) find closely similar results. The effective radii $r_e$ of pseudobulges and the scale lengths $h_d$ of their associated disks are coupled, whereas the same is not true for classical bulges. Specifically, the mean ratio is $<r_e/h_d> = 0.21 \pm 0.10$ for 53 pseudobulges but $<r_e/h_d> = 0.45 \pm 0.28$ for 26 classical bulges. Since $r_e = 1.678 h_b$ for an exponential, the above result for pseudobulges corresponds approximately to $<h_b/h_d> = 0.13 \pm 0.06$ (the conversion is approximate because the pseudobulges are not exactly exponentials). This confirms the results by Courteau et al. (1996) and similar results by MacArthur et al. (2003). Courteau and MacArthur did not calculate $h_b/h_d$ separately for classical and pseudo bulges and therefore found a correlation with Hubble type rather than different distributions of $h_b/h_d$ for the two types of bulges. But Courteau and MacArthur, like Fisher and Drory, interpreted the connection between bulge and disk properties as a sign that secular evolution and pseudobulge formation become more important at later Hubble types.

As a result of this and other work (see especially Weinzirl et al. 2009), the connection between pseudobulges and small Sérsic indices is by now well established. Classical bulges, on the other hand, have Sérsic indices like those of elliptical galaxies, which have $n \gtrsim 2$ (e.g., Kormendy et al. 2009, hereafter KFCB). Moreover, the Sérsic indices $n \simeq 2$ to 3 of ellipticals are well understood as natural results of their formation by major galaxy mergers (e.g., Hopkins et al. 2009a, c; see Kormendy et al. 2009 for a review). So the connection between the $n \gtrsim 2$ Sérsic indices of classical bulges with their formation by major mergers is also well established.

Therefore, even though we do not fully understand how disk secular evolution determines the resulting pseudobulge Sérsic indices, we see strong enough correlations between $n$ and other pseudobulge properties so that we can use the Sérsic index as a classification criterion (Figs. 1.41, 1.42).
Fig. 1.41. Correlations with (pseudo)bulge Sérsic index $n_b$ of (top to bottom) bulge absolute magnitude, effective brightness at (left) or averaged interior to (right) the half-light radius $r_e$ and effective radius $r_e$. The $V$-band data in the left plots are from Fisher & Drory (2008); the 3.6 $\mu$m-band Spitzer Space Telescope data in the right plots are from Fisher & Drory (2010). In all panels, the central components are classified morphologically as in Fig. 1.38.

Therefore classical bulges have Sérsic $n \geq 2$, whereas pseudobulges usually have $n < 2$. Note in Fig. 1.41 and in the earlier discussion of NGC 4736 that some pseudobulges do have Sérsic indices as big as $n \simeq 4$. Therefore it is always important to apply as many classification criteria as possible.

1.5.2.7 Fundamental plane parameter correlations

Figure 1.41 provides an introduction to the correlations between effective radius $r_e$, effective brightness $\mu_e$ at $r_e$, velocity dispersion $\sigma$ and bulge absolute magnitude $M_V$ (the “fundamental plane”). Classical bulges satisfy the fundamental plane correlations of elliptical galaxies. Some pseudobulges do so, too. But many have larger $r_e$ and fainter $\mu_e$ than do classical bulges.
Figure 1.68 updates the observation that classical bulges and ellipticals have the same correlations. Simulations of major galaxy mergers reproduce these correlations (e.g., Robertson et al. 2006; Hopkins et al. 2008, 2009b).

Earlier versions that emphasize pseudobulges are shown in Figs. 1.42 and 1.43. Many pseudobulges satisfy the correlations for bulges and ellipticals, but in general, they show substantially larger scatter.

![Figure 1.42](image_url)

**Fig. 1.42.** Structural parameter correlations for pseudobulges (blue), classical bulges (brown), ellipticals (red), and spheroidal galaxies (green). Pseudobulge data and most bulge points are from Fisher & Drory (2008). The ellipticals, five bulge points and the green squares are from Kormendy et al. (2009: KFCB). Green triangles show all spheroidals from Ferrarese et al. (2006) that are not in KFCB. Crosses show all spheroidals from Gavazzi et al. (2005) that are not in KFCB or in Ferrarese et al. (2006). Open squares are Local Group spheroidals (Mateo 1998; McConnachie & Irwin 2006). The bottom panels show major-axis Sérsic index $n$ and effective surface brightness $\mu_e$ versus galaxy or bulge absolute magnitude. The top panel shows $\mu_e$ versus effective radius $r_e$ (the Kormendy 1977b relation, which shows the fundamental plane almost edge-on). From Kormendy & Fisher (2008).
Figure 1.43 shows the $\mu_e - r_e$ correlation from Carollo (1999). I emphasize this version because it shows more extreme pseudobulges together with spheroidal galaxies, galactic nuclear star clusters and globular clusters. Spheroidals form a sequence perpendicular to the correlation for ellipticals (Figs. 1.42, 1.61). Globular clusters are different from both ellipticals and spheroidals (Kormendy 1985, 1987). The comparison that is important here is the one between bulges plus ellipticals, pseudobulges and galactic nuclei.

Figures 1.42 and 1.43 show that some pseudobulges satisfy the parameter correlations for classical bulges and ellipticals, but many deviate by having brighter $\mu_e$ (Kormendy & Bender 2012) or fainter $\mu_e$ (see also Falcón-Barroso et al. 2002; Kormendy & Fisher 2008; Gadotti 2009). All available data suggest that pseudobulges fade out by becoming low in surface brightness, not by becoming like nuclear star clusters. Nuclear star clusters are not faint versions of pseudobulges. Indeed, tiny pseudobulges and normal nuclei coexist in Scd galaxies like M 101 and NGC 6946 (Kormendy et al. 2010).

The fundamental plane is only secondarily useful for bulge classification. Many pseudobulges satisfy the correlations for classical bulges, so use of the correlations as the only classification method (Gadotti 2009; Gadotti & Kauffmann 2009) is not feasible. Extreme pseudobulges can be identified because their parameters deviate from the E correlations in Fig. 1.42, but these objects can usually be robustly classified using other criteria anyway.

Fig. 1.43. Effective surface brightness versus effective radius for various kinds of stellar systems (Carollo 1999; this version is from Kormendy & Fisher 2008).
1.5.2.8 Nuclear bars

Figure 1.44 shows examples of nuclear bars at the centers of barred and oval galaxies. Nuclear bars are well known phenomena (de Vaucouleurs 1959; Sandage 1961; Kormendy 1981, 1982b; Buta et al. 2007; Buta 2011, 2012). They are always much smaller than the main bars in which they are embedded. Observations are consistent with the suggestion that their physics is essentially the same as that of main bars. How they form is not known in detail, but it is reasonable to expect that the growth of stellar disky pseudobulges out of inflowing cold gas can result in a bar instability.

Pattern speeds $\Omega_p$ of nuclear bars are well predicted by Section 1.4.2. They live at small radii where stellar densities are high and where $\Omega - \kappa/2$ is large. So $\Omega_p \sim \Omega - \kappa/2$ should be larger for nuclear bars than it is for main bars. This is seen in $n$-body models (Debattista & Shen 2007; Shen & Debattista 2009). Direct measurement of $\Omega_p$ is difficult, but Corsini et al. (2009) use the Tremaine & Weinberg (1984) method on NGC 2950 and conclude that the main and nuclear bars have different pattern speeds. For present purposes, different $\Omega_p$ is sufficiently well established by the observation that nuclear bars have random orientations with respect to their main bars (Fig. 1.44).

Bars are disk phenomena. A nuclear bar therefore identifies a pseudobulge.

Fig. 1.44. Bars within bars. The main bar is rotated until it is horizontal. Contour levels are close together in intensity at large radii and widely spaced in intensity in the nuclear bars. NGC 3081 and NGC 1433 have inner rings. NGC 1291 is also shown in Fig. 1.6. NGC 3081 and NGC 3945 are shown in Figs. 1.17 and 1.24. The images are courtesy Ron Buta; this figure is from Kormendy & Kennicutt (2004). The nuclear bar in NGC 2950 (see above discussion) is illustrated in Fig. 1.17.
1.5.2.9 *Boxy pseudobulges are edge-on bars.*

Section 1.4.3.3 reviews how bars buckle and thicken in the vertical direction and consequently look like “box-shaped bulges” when seen edge-on. These are parts of disks, so I call them “boxy pseudobulges”. The one in our Galaxy is particularly clearcut, because we are close enough to it so that, from our perspective, the near side looks taller than the far side (Fig. 1.45).

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**Fig. 1.45.** The boxy pseudobulge = almost-end-on bar of our Galaxy in (bottom: from [http://www.nasaimages.org/luna/servlet/detail/nasaNAS~5~5~24223~127634:COBE-s-View-of-the-Milky-Way](http://www.nasaimages.org/luna/servlet/detail/nasaNAS~5~5~24223~127634:COBE-s-View-of-the-Milky-Way)) a COBE infrared view and (top) an $n$-body model from Shen *et al.* (2010). The top three model panels show the face-on and side-on views as projected and seen from far away. Seen almost side-on (top), the bar looks peanut-shaped. Seen almost end-on from the direction of our Sun (right-hand view), it looks boxy when seen from far away. Viewed instead from within our Galaxy at the position of the Sun (bottom model panel), the near side of the bar is significantly closer than the far side. Therefore the near side looks taller than the far side, exactly as in the COBE image (Blitz & Spergel 1991).
Observations which further show that boxy bulges are edge-on bars are reviewed in Kormendy & Kennicutt (2004). The well known example of NGC 4565 (Fig. 1.46, from Kormendy & Barentine 2010) turns out to be an SB(r) galaxy with a second, tiny pseudobulge at its center that is distinct from the boxy bar (Fig. 1.47).

Fig. 1.46. (a) Optical and (b, c) Spitzer 3.6 μm negative images of NGC 4565 shown at different stretches to emphasize (b) the boxy bar and (c) an inner ring and pseudobulge. The newly detected pseudobulge is the central bright dot. (d) Spitzer IRAC 8 μm negative image showing PAH emission and therefore star formation from the inner ring and outer disk. Because the inner ring is dark inside at 8 μm, we conclude that the dark inside seen at 3.6 μm is not caused by dust absorption. Rather, the ring really is dark inside. Therefore NGC 4565 is an SB(r)b galaxy, i.e., an almost-edge-on analog of NGC 2523 (bottom panel). The NGC 2523 image has been scaled so the inner ring has the same apparent radius as in NGC 4565 and rotated to the apparent bar position angle inferred for NGC 4565. We suggest that NGC 2523, if oriented as in the bottom panel and inclined still more until we observed it almost edge-on, would show the features seen in the NGC 4565 images.
Finding the tiny pseudobulge hidden inside the boxy bar of NGC 4565 solves a long-standing puzzle and cements an important implication for the statistics of \((P)B/T\) luminosity ratios. Compare NGC 4565 with any more face-on barred galaxy, such as NGC 2523 in Fig. 1.46. Face-on galaxies show a (pseudo)bulge, a bar, and an outer disk; i.e., three or more components. The edge-on galaxy NGC 4565 shows only a “boxy bulge” and a disk. As long as we thought that boxy distortions were minor features of bulges, this was no problem – many unbarred Sb galaxies have just a bulge and a disk. But if the box in NGC 4565 is an edge-on bar, then the galaxy contains a bar and a disk; i.e., only two components. This is not seen in face-on galaxies except at very late Hubble types. Where is the “bulge” in NGC 4565?

Figures 1.46 and 1.47 show the answer. The minor-axis profile of the boxy structure is exponential. Inside this structure, there is a clearly distinct, tiny central component that has \(n = 1.33 \pm 0.12\) and that therefore is a second, “disky” pseudobulge. The important implication is that \(PB/T = 0.06 \pm 0.01\) is much smaller than the value \(B/T \simeq 0.4\) (Simien & de Vaucouleurs 1986) for the box. Closely similar results are found for the edge-on “boxy bulge” galaxy NGC 5746 (Barentine & Kormendy 2012). Not counting boxy bulges because they are bars, \((P)B/T\) ratios are much smaller than we have thought for essentially all edge-on galaxies with boxy bulges. In particular, the classical-bulge-to-total ratio in our Galaxy is \(\sim 0\) (Shen et al. 2010).

![Fig. 1.47. Minor-axis profile of NGC 4565 from Kormendy & Barentine (2010). The dashed lines show a decomposition of the profile into components in order of increasing radius: a Seyfert nucleus (Ho et al. 1997) or nuclear star cluster that is not included in the fit, the pseudobulge (Sérsic), box-shaped bar (Sérsic) and outer halo (exponential). The solid line is the sum of the components.](image-url)
1.5.3 Pseudobulges classification criteria

The bulge-pseudobulge classification criteria updated from Kormendy & Kennicutt (2004) are listed here for convenience. They are identified by the number \( m \) in the Section 1.5.2. \( m \) in which they were discussed.

1. If the center of the galaxy is dominated by Population I material (young stars, gas and dust), but there is no sign of a merger in progress, then the bulge is at least mostly pseudo.

2. Pseudobulges often have disky morphology; e.g., their apparent flattening is similar to that of the outer disk, or they contain spiral structure all the way in to the center of the galaxy. Classical bulges are much rounder than their disks unless the galaxy is almost face-on, and they cannot have spiral structure.

3. Pseudobulges are more rotation-dominated than classical bulges in the \( V_{\text{max}}/\sigma - \epsilon \) diagram. Integral-field spectroscopy often shows that the central surface brightness excess over the inward extrapolation of the outer disk profile is a flat central component that rotates rapidly and that has a small velocity dispersion.

4. Many pseudobulges are low-\( \sigma \) outliers in the Faber-Jackson (1976) correlation between (pseudo)bulge luminosity and velocity dispersion. A similar signature is that \( \sigma \) decreases from the disk into the pseudobulge.

5. Small bulge-to-total luminosity ratios do not guarantee that a bulge is pseudo, but almost all pseudobulges have \( PB/T \leq 0.35 \). If \( B/T \geq 0.5 \), the bulge is classical.

6. Most pseudobulges have Sérsic index \( n < 2 \), whereas almost all classical bulges have \( n \geq 2 \). The processes that determine the small Sérsic indices of pseudobulges are not understood, but the correlation of small \( n \) with other pseudobulge indicators is so good that this has become a convenient classification criterion. Note, however, that some pseudobulges do have Sérsic indices as big as 4.

7. Classical bulges fit the fundamental plane correlations for elliptical galaxies. Some pseudobulges do, too, and then these correlations are not helpful for classification. But more extreme pseudobulges are fluffier than classical bulges; they have larger \( r_e \) and fainter surface brightnesses \( \mu_e \) at \( r_e \). These can easily be identified using fundamental plane correlations.

8. In face-on galaxies, the presence of a nuclear bar shows that a pseudobulge dominates the central light. Bars are disk phenomena. Triaxiality in giant ellipticals involves completely different physics – slow (not rapid) rotation and box (not \( x_1 \) tube) orbits.

9. In edge-on galaxies, boxy bulges are edge-on bars; seeing one is sufficient to identify a pseudobulge. The boxy-nonrotating-core side of the “E–E dichotomy” of elliptical galaxies into two kinds (Kormendy et al. 2009) cannot be confused with boxy, edge-on bars because boxy ellipticals – even if they occur in disk galaxies (and we do not know of an example) – are so luminous that we would measure \( B/T > 0.5 \). Then point (5) would tell us that this “bulge” is classical.

It is important always to apply as many classification criteria as possible.
1.5.4 Secular evolution and hierarchical clustering

We now have a well articulated paradigm of secular evolution in galaxy disks that complements our standard picture of hierarchical clustering. There is no competition between these two galaxy formation pictures – both are valid, and their relative importance depends on cosmological lookback time and on environment. I have emphasized that the Universe is in transition from early times when the rapid processes of hierarchical clustering were most important in controlling galaxy evolution to future times when galaxy merging will largely have finished and slow, internal processes will dominate.

In the present Universe, the mass in bulges (including ellipticals) and that in disks are roughly equal (Schechter & Dressler 1987; Driver et al. 2007; Gadotti 2009; Tasca & White 2011). Uncertainties are large, with estimated ratios of the mass in bulges to that in disks as large as $\sim 2$ (Fukugita et al. 1998). One reason is that the relative numbers of disks and merger remnants is a strong function of environment: disks predominate in the field, whereas most giant ellipticals live in galaxy clusters (Section 1.6.1).

The ratio of mass in classical bulges to that in pseudobulges has not yet been determined for large and unbiased galaxy samples. It is reasonable to expect that the ratio of masses is not large.

In contrast, the ratio of numbers of pseudobulges to numbers of classical bulges could easily be $\gtrsim 1$. Kormendy & Kennicutt (2004) estimated that most Sa galaxies contain classical bulges, that in Sb galaxies, classical and pseudo bulges are comparably common and that most Sbc galaxies contain pseudobulges. Recent work suggests that there are more pseudobulges at early Hubble types than Kormendy & Kennicutt thought (Fisher & Drory 2008; Weinzirl et al. 2009). S0 galaxies contain pseudobulges more often than Sa galaxies, consistent with parallel-sequence galaxy classifications in which S0s form a sequence in $(P)B/T$ that parallels the sequence of spirals (Section 1.7). At late Hubble types, Sc – Im galaxies appear never to contain classical bulges. Many Scd – Sm galaxies do not contain pseudobulges, either; M 33 is an example, and the main reason is that $\Omega(r)$ depends little enough on radius so that it is not energetically profitable to transport angular momentum outward (Section 1.2.4).

I conclude with a point of perspective from Kormendy & Kennicutt (2004). In the early 1970s, when I was a graduate student, Hubble classification was in active use, but we also knew about many regular features in galaxy disks, such as lens components, nuclear, inner and outer rings, nuclear bars and boxy bulges, that we did not understand and that often were not even included in the classification. We also knew many peculiar galaxies, no two of
which look alike; they did not fit comfortably into Hubble classification, and we did not understand them, either. Now both the peculiar galaxies and the structural regularities are becoming well understood within two paradigms of galaxy evolution that got their start in the late 1970s. The peculiar galaxies were once normal but now are undergoing tidal interactions or are galaxy mergers in progress (Section 1.8.1). And structures such as rings and lenses that are seen in many galaxies are products of the secular evolution of relatively isolated galaxy disks. Between collisions, galaxies do not just sit quietly and age their stellar populations. Galaxies represent snapshots of moments in time during dynamical evolution that goes on today and that will continue to go on for many billions of years to come.

1.6 Astrophysical implications of pseudobulges

The general implications of pseudobulges for galaxy formation are the main subject of this Winter School. Here, I focus on two additional astrophysical implications that came – at least to me – as a surprise. First is the challenge that classical-bulge-less galaxies (even ones that contain pseudobulges) present for our picture of galaxy formation by hierarchical clustering and merging. Second is the lack of any tight correlation between the masses of supermassive black holes and the properties of pseudobulges.

1.6.1 A challenge for our theory of galaxy formation by hierarchical clustering and merging: Why are there so many pure-disk galaxies?

Look at any movie of a numerical simulation of hierarchical clustering in action. Your overwhelmingly strong impression will be that the lives of dark matter halos are violent. They continually collide with and accrete smaller halos, which – by and large – approach from random directions. And virtually no halo grows large without undergoing at least a few major mergers between progenitors of comparable mass.

Given this merger violence, how can there be so many bulgeless galaxies? The puzzle has two parts. How does hierarchical clustering prevent the formation of classical bulges that are the scrambled-up remnants of the progenitor stars that predate the merger? And how does the merger assembly of galaxy halos prevent the destruction of large but very flat disks, at least some of which are made in part of old stars. Bulgeless disks are not rare.

† In this review, as in Kormendy et al. (2010), I will adopt the sufficient and practical definition that a “large” galaxy is one in which the circular orbit rotation velocities of massless test particles at large radii are $V_{\text{circ}} \geq 150$ km s$^{-1}$. 
Figure 1.48 shows the purest examples of this problem, the iconic late-type galaxies whose edge-on orientations make it clear that they have no classical bulges and no signs of pseudobulges. Such galaxies are common (Karachentsev et al. 1993; Kautsch et al. 2006). UGC 7321 is studied by Matthews et al. (1999a); Matthews (2000); Banerjee et al. (2010). IC 5249 is studied by van der Kruit et al. (2001). Matthews et al. (1999b), Kautsch (2009) and van der Kruit & Freeman (2011) review superthin galaxies.

It is a challenge to explain these galaxies. It helps that they are not large: Hyperleda lists rotation velocities of $V_{\text{circ}} = 95, 79, 97$ and $92$ km s$^{-1}$ for UGC 7321, IC 2233, IC 5249 and UGC 711, respectively. This is smaller than $V_{\text{circ}} = 135 \pm 10$ km s$^{-1}$ in M 33 (Corbelli & Salucci 2000; Corbelli 2003).

![Images of galaxies](http://www.wikisky.org)

Fig. 1.48. Edge-on, completely bulgeless, pure-disk galaxies. All images are from [http://www.wikisky.org](http://www.wikisky.org); the top galaxies are from the SDSS and the bottom ones are from DSS. The DSS images have a bluer color balance than the SDSS.
Explaining bulgeless disks is least difficult for dwarf galaxies. They suffer fewer mergers and tend to accrete gas in cold streams or as gas-rich dwarfs (Maller et al. 2006; Dekel & Birnboim 2006; Koda et al. 2009; Brooks et al. 2009; Hopkins et al. 2009d, 2010). Energy feedback from supernovae counteracts gravity most effectively in dwarf galaxies (Dekel & Silk 1986; Robertson et al. 2004; D’Onghia et al. 2006; Dutton 2009; Governato et al. 2010). Attempts to explain pure disks have come closest to success in explaining dwarf galaxies (Robertson et al. 2004; Governato et al. 2010).

Kormendy et al. (2010) conclude that the highest-mass, pure-disk galaxies are the ones that most constrain our formation picture. They inventory all giant galaxies ($V_{\text{circ}} \geq 150\,\text{km\,s}^{-1}$) at distances $D \leq 8\,\text{Mpc}$ within which we can resolve small enough radii to find or exclude even the smallest bulges. Table 1.3 documents the $B/T$ and $PB/T$ luminosity ratios for these galaxies. Giant, bulgeless galaxies are not rare. Figure 1.49 shows the most extreme galaxies in which $B/T = 0$ rigorously. Kormendy et al. (2010) emphasize

![Face-on, completely bulgeless, pure-disk galaxies. All four galaxies have bulge-to-total luminosity ratios of $B/T = 0$. They have the smallest pseudobulges in the local sample of giant galaxies (outer rotation velocities $V_{\text{circ}} > 150\,\text{km\,s}^{-1}$; for these galaxies, 174–210 km s$^{-1}$) in Table 1.3. The pseudobulge-to-total luminosity ratios $PB/T$ are given in the figure. Unless otherwise noted, the images are from http://www.wikisky.org or Kormendy et al. (2010).](image-url)
that “we do not have the freedom to postulate classical bulges which have arbitrary properties (such as low surface brightnesses) that make them easy to hide. Classical bulges and ellipticals satisfy well-defined fundamental plane correlations (Fig. 1.68). Objects that satisfy these correlations cannot be hidden in the above galaxies. So $B/T = 0$ in $4/19$ of the giant galaxies in our sample.” Seven more galaxies contain pseudobulges; since we believe that these are grown secularly out of disks and not made via mergers, these are pure-disk galaxies from the hierarchical clustering point of view. Four more galaxies contain classical bulges smaller than any that are made in hierarchical clustering simulations. Only M 31 and M 81 have classical bulges with $B/T \approx 1/3$, and only two more galaxies are ellipticals with $B/T = 1$

Fisher & Drory (2011) derive similar statistics in the $D \leq 11$ Mpc volume.

### Table 1.3

| Galaxy | Type | $D$ (Mpc) | $M_K$ | $M_V$ | $V_{circ}$ (km s$^{-1}$) | $B/T$ | $P B/T$ |
|--------|------|-----------|-------|-------|--------------------------|-------|---------|
| NGC 6946 | Scd | 5.9 | $-23.61$ | $-21.38$ | $210 \pm 10$ | 0 | $0.024 \pm 0.003$ |
| NGC 5457 | Scd | 7.0 | $-23.72$ | $-21.60$ | $210 \pm 15$ | 0 | $0.027 \pm 0.008$ |
| IC 342 | Scd | 3.28 | $-23.23$ | $-21.4$ | $192 \pm 3$ | 0 | $0.030 \pm 0.001$ |
| NGC 4945 | SBcd | 3.36 | $-23.21$ | $-20.55$ | $174 \pm 10$ | 0 | $0.036 \pm 0.009$ |
| NGC 5236 | SABc | 4.54 | $-23.69$ | $-21.0$ | $180 \pm 15$ | 0 | $0.074 \pm 0.016$ |
| NGC 5194 | Sbc | 7.66 | $-23.94$ | $-21.54$ | $240 \pm 20$ | 0 | $0.095 \pm 0.015$ |
| NGC 253 | Sbc | 3.62 | $-24.03$ | $-20.78$ | $210 \pm 5$ | 0 | $0.15$ |
| Maffei 2 | SBbc | 3.34 | $-23.0$ | $-20.8$ | $168 \pm 20$ | 0 | $0.16 \pm 0.04$ |
| Galaxy | SBbc | 0.008 | $-23.7$ | $-20.8$ | $220 \pm 20$ | 0 | $0.19 \pm 0.02$ |
| Circinus | SABbc | 2.8 | $-22.8$ | $-19.8$ | $155 \pm 5$ | 0 | $0.30 \pm 0.03$ |
| NGC 4736 | Sab | 4.93 | $-23.36$ | $-20.66$ | $181 \pm 10$ | 0 | $0.36 \pm 0.01$ |
| NGC 2683 | SABb | 7.73 | $-23.12$ | $-19.80$ | $152 \pm 5$ | $0.05 \pm 0.01$ | 0 |
| NGC 4826 | Sab | 6.38 | $-23.71$ | $-20.72$ | $155 \pm 5$ | $0.10$ | 0.10 |
| NGC 2787 | SB0/a | 7.48 | $-22.16$ | $-19.19$ | $220 \pm 10$ | $0.11$ | $0.28 \pm 0.02$ |
| NGC 4258 | SABbc | 7.27 | $-23.85$ | $-20.95$ | $208 \pm 6$ | $0.12 \pm 0.02$ | 0 |
| M 31 | Sb | 0.77 | $-23.48$ | $-21.20$ | $250 \pm 20$ | $0.32 \pm 0.02$ | 0 |
| M 81 | Sab | 3.63 | $-24.00$ | $-21.13$ | $240 \pm 10$ | $0.34 \pm 0.02$ | 0 |
| Maffei 1 | E | 2.85 | $-23.1$ | $-20.6$ | $(264 \pm 10)$ | 1 | 0 |
| NGC 5128 | E | 3.62 | $-23.90$ | $-21.34$ | $(192 \pm 2)$ | 1 | 0 |

**Note:** Galaxies are ordered from pure disk to pure elliptical by increasing pseudobulge-to-total luminosity ratio $PB/T$ and then by increasing bulge-to-total luminosity ratio $B/T$. Column (2): Hubble type. Column (3): Distance. Columns (4) and (5): Absolute magnitudes $M_K$ and $M_V$ are calculated from apparent integrated magnitudes (in $K$ band, from Jarrett et al. 2003; in $V$ band, preferably from HyperLeda, otherwise from NED). Galactic absorptions are from Schlegel et al. (1998). Column (6): Circular rotation velocity at large radii, $V_{circ}$, corrected to edge-on inclination. Values in parentheses are $\sqrt{2}V$. Columns (7) and (8) are averages of measured classical-bulge-to-total and pseudobulge-to-total luminosity ratios. Quoted errors are from the variety of decompositions in multiple sources. The smallest values are unrealistically optimistic estimates of the true measurement errors and indicate fortuitously good agreement between published values (e.g., for IC 342). Colons indicate uncertainty in the sense that no observational evidence suggests that this component is present but there is also no rigorous proof that a small contribution by this component is impossible. From Kormendy et al. (2010), who give sources.
Kormendy et al. (2010) conclude that giant bulgeless galaxies do not form the rare tail of a distribution of formation histories that include a few fortuitously mergerless galaxies. In the field, the problem of forming giant, pure-disk galaxies by hierarchical clustering is acute. In contrast, in the Virgo cluster, $\gtrsim 2/3$ of the stellar mass is in merger remnants. Therefore the problem of explaining pure-disk galaxies is a strong function of environment.

This is a sign that AGN feedback, the physics popularly used to address the problem, is not the answer. The effectiveness of energy feedback depends on galaxy mass. In contrast, galaxies tell us that environment is the controlling factor. Giant, pure-disk galaxies (Fig. 1.49) are more massive than small ellipticals. And the thin disk of our Galaxy—which, given its boxy bar, is a giant pure-disk galaxy—contains stars as old as 10 Gyr (Oswalt et al. 1996; Winget & Kepler 2008). So I suggest that the solution to the pure-disk problem is not to use energy feedback to delay disk star formation in order to give the halo time to grow without forming a classical bulge. I believe that a viable solution must use the environmental dependence of the pure-disk galaxy problem in an essential way (e.g., Peebles & Nusser 2010).

### 1.6.2 Supermassive black holes do not correlate with pseudobulges

Kormendy & Ho (2013) review a modest revolution that is in progress in studies of supermassive black holes (BHs) in galaxy centers. For more than a decade, observed BH demographics have suggested a simple picture in which BH masses $M_\bullet$ show a single correlation each with many properties of their host galaxies (Fig. 1.50). Most influential was the discovery of a tight correlation between $M_\bullet$ and the velocity dispersion $\sigma$ of the host bulge at radii where stars mainly feel each other and not the BH (Ferrarese & Merritt 2000; Gebhardt et al. 2000; Tremaine et al. 2002; Gültekin et al. 2009). Correlations are also observed between $M_\bullet$ and bulge luminosity (Kormendy 1993a; Kormendy & Richstone 1995; Magorrian et al. 1998), bulge mass (Dressler 1989; McLure & Dunlop 2002; Marconi & Hunt 2003; Haring & Rix 2004); core parameters of elliptical galaxies (Milosavljević et al. 2002; Ravindranath et al. 2002; Graham 2004; Ferrarese et al. 2006; Merritt 2006; Lauer et al. 2007; Kormendy & Bender 2009), and globular cluster content (Burkert & Tremaine 2010; Harris & Harris 2011). These have led to the belief that BHs and bulges coevolve and regulate each other’s growth (e.g., Silk & Rees 1998; Richstone et al. 1998; Granato et al. 2004; Di Matteo et al. 2005; Springel et al. 2005; Hopkins et al. 2006; Somerville et al. 2008).

This simple picture is now evolving into a richer and more plausible story in which BHs correlate differently with different kinds of galaxy components. BHs do not correlate at all with galaxy disks (Kormendy & Gebhardt 2001;
Kormendy et al. 2011; Kormendy & Ho 2013), although some pure-disk galaxies contain BHs (see Ho 2008 for a review). And despite contrary views, (Ferrarese 2002; Baes et al. 2003; Volonteri et al. 2011), it is clear that BHs do not correlate tightly enough with dark matter halos to imply any special relationship between them beyond the fact that dark matter controls most of the gravity that makes hierarchical clustering happen (Ho 2007; Kormendy & Bender 2011; Kormendy & Ho 2013). So BHs coevolve only with bulges.

What about pseudobulges? They are closely connected with disks, but some contain BHs. The best example is our Galaxy (Genzel et al. 2010).

Hu (2008) finds, for a small sample, that BHs in pseudobulges have smaller $M_\bullet$ than BHs in classical bulges and ellipticals of the same $\sigma$. Graham (2008) reports the possibly related result that barred galaxies also deviate from the $M_\bullet - \sigma$ relation in having small $M_\bullet$, but interpretation is complicated by the fact that some of his barred galaxies contain classical bulges (e.g., NGC 1023, NGC 4258), some contain pseudobulges (e.g., NGC 3384, our Galaxy) and some contain both (NGC 2787). More definitively, results similar to Hu’s are found by Nowak et al. (2010) and by Greene et al. (2010).

Kormendy et al. (2011) and Kormendy & Ho (2013) now show for larger samples that pseudobulges correlate little enough with $M_\bullet$ so coevolution is not implied (Fig. 1.50). This simplifies the problem of coevolution by focusing our attention on galaxy mergers. It is a substantial success of the secular evolution picture that a morphological classification of bulges separates them into two kinds that correlate differently with BHs.

Fig. 1.50. Correlation of dynamically measured BH mass $M_\bullet$ with (left) $K$-band bulge absolute magnitude and (right) velocity dispersion averaged inside $r_e$. Pseudobulges with dynamical BH detections are shown with blue filled circles and those with $M_\bullet$ upper limits are shown with blue open circles. NGC 2787 may have both a small classical and a large pseudo bulge (Erwin et al. 2003); its blue symbol has a red center. Classical bulges and ellipticals are shown in ghostly light colors to facilitate comparison. This is a preliminary figure from Kormendy & Ho (2013).
1.7 Environmental secular evolution: The structure and formation of S0 and spheroidal galaxies

Research on internal secular evolution is now a major industry, but work on environmental secular evolution still is a series of important but disconnected cottage industries. We need to make the subject an integral part of our standard picture of galaxy evolution. This section reviews environmental secular evolution, following Kormendy & Bender (2012).

Our theme is that dwarf spheroidal (dSph) galaxies such as Draco and UMi and higher-luminosity Sph galaxies such as NGC 205 are transformed, “red and dead” spiral and irregular galaxies and that many S0 galaxies similarly are transformed earlier-type spirals. That is, Sph galaxies are bulgeless S0s. The easiest way to introduce this theme is using Fig. 1.51. This is one of the best-known extragalactic images, but it is not widely realized that it includes an easy way to form a mental picture of the difference between elliptical and spheroidal galaxies. In doing so, it speaks directly to the fundamental question: What is an elliptical galaxy (Fig. 1.52)?

Fig. 1.51. M31 (Sb, center), M32 (E, lower companion) and NGC 205 (Sph, upper companion) from the Digital Sky Survey via [http://www.wikisky.org](http://www.wikisky.org)
1.7.1 What is (and what is not) an elliptical galaxy?

In Fig. 1.51, M 31 is an Sb spiral with a classical bulge; $B/T = 0.34 \pm 0.03$ (Kormendy et al. 2010). Absent the disk, the bulge is indistinguishable from a smallish elliptical. M 32 is one of the finest true ellipticals, with a $V$-band absolute magnitude of $M_V \simeq -16.7$ (Kormendy et al. 2009). It is small and dense and commonly called a “compact elliptical” (cE). But compactness is not a disease; it is mandated by the physics that makes the Fundamental Plane (Figs. 1.57, 1.68). In fact, M 32 is an entirely normal example of a tiny elliptical (Kormendy et al. 2009). In contrast, NGC 205 is the most luminous example in the Local Group of a galaxy that satisfies the morphological definition of an elliptical but that differs quantitatively from ellipticals (as a result, it is typed “E5 pec”). NGC 205 has the same luminosity as M 32, $M_V \simeq -16.6$ (Mateo 1998). It looks different because it is larger, lower in surface brightness and shallower in surface brightness gradient. Measured quantitatively, these differences put NGC 205 near the bright end of a sequence of elliptical-looking galaxies that is disjoint from—in fact, almost perpendicular to—the sequence of ellipticals and classical bulges in Figs. 1.43, 1.57, 1.68 – 1.69 and 1.71. This means that NGC 205 is not an elliptical.

Fig. 1.52. What is an elliptical galaxy? Morphologically, the dwarf galaxy Leo I (top-middle panel) resembles the dwarf irregulars Leo A and GR 8 in its low surface brightness and shallow brightness gradient. But it resembles the giant elliptical M 87 in having elliptical isophotes and no cold gas. Since only the latter characteristics morphologically define ellipticals, Leo I is often called a “dwarf elliptical”. However, purely morphological criteria prove unable to distinguish objects that have different formation histories. Leo I turns out to be related to dI galaxies, not to ellipticals. So I do not call it a dwarf elliptical; rather, I call it a dwarf spheroidal (dSph) galaxy.
Finding gas and young stars in it supports this conclusion. We call such objects “spheroidal galaxies” (Sphs), adapting a name (“dwarf spheroidal”) that is in common use for smaller examples. The fact that NGC 205 has surface brightnesses similar to those of the disk of M31 is not an accident.

A variety of evidence leads to the conclusion that Sph galaxies are defunct late-type galaxies whereas classical bulges and ellipticals are the remnants of major galaxy mergers. This story is the subject of the present section.

Recall (Section 1.3.4) how classical morphologists attach no interpretation to descriptions, whereas physical morphologists try to construct a system in which classification bins uniquely separate objects that have different origin and evolution. I emphasized there that, even though classical morphologists try to avoid interpretation, they nevertheless makes choices about which features to view as important and which to view as secondary. Figure 1.52 illustrates how this results in a problem for classifying elliptical galaxies. In its isophote shape, Leo I resembles the elliptical galaxy M 87. However, in its surface brightness, it resembles the irregular galaxies Leo A and Gr 8. Hubble classification is based mainly on isophote shape, so it has been common to call galaxies like Leo I and NGC 205 “dwarf ellipticals” (e. g., Sandage 1961). But there has never been any guarantee that structural morphology identifies physically different kinds of objects. Figure 1.53 makes this point concrete.

Fig. 1.53. The danger of classifying using only morphology. Who does not belong?
Who does not belong in Fig. 1.53? The answer is of course well known (Fig. 1.54). Dolphins (Fig. 1.53, top right) are mammals, even though they are morphologically similar to sharks (Fig. 1.53, top left). To make a living, both need to be well streamlined, strong swimmers. Convergent evolution made them that way. In contrast, a leafy seadragon (Fig. 1.53, bottom right: http://picasaweb.google.com/1h/photo/cEq5cw1B2mufKXl0KJcg) is a kind of seahorse whose main need is good camouflage to avoid predators. So, even though it is a fish, its morphology has evolved to be very different from that of a shark. A “Hubble classification” of sea animals that was superficially based on visible structural characteristics could mistakenly combine sharks and dolphins into the same or closely related classification bins and could miss the more subtle (but more important) differences that distinguish sharks and sea dragons from dolphins and cows. Which parameters best distinguish the physical differences that are most important to us is not necessarily obvious without detailed study.

Convergent evolution happens to galaxies, too.
Why did we ever think that Leo I and NGC 205 are ellipticals? The answer is that research on galaxies began with descriptive classical morphology (e.g., Hubble 1936; de Vaucouleurs 1959; Sandage 1961), and then the above galaxies satisfy the definition of an elliptical. However, we will see in Fig. 1.59 that Sandage et al. (1985b) had no trouble in distinguishing between E and dE galaxies of the same luminosity. If this sounds surpassingly strange to you, you have the right reaction. I will come back to this point below.

Astronomers are conservative people – this is often healthy – and most people clung to the idea that galaxies like Leo I and NGC 205 are ellipticals even after hints to the contrary started to appear. Figure 1.55 shows an example. Ellipticals (filled circles) have higher surface brightness at lower galaxy luminosities, whereas “dwarf ellipticals” (open circles and crosses) have lower surface brightnesses at lower luminosities. M32 is consistent with the extrapolation of the E sequence. However, at that time, we thought that M32 is compact because it has been tidally truncated by M31 (King 1962; Faber 1973). Bingelli et al. (1984) therefore concluded that E and dE galaxies form a continuous but not monotonic sequence in surface brightness as a function of luminosity. Meanwhile, one could wonder whether the two sequences in Fig. 1.55 already hint at different formation physics.

Fig. 1.55. Parameter correlations for elliptical and “dwarf elliptical” galaxies from Bingelli et al. (1984). These authors suggested that giant and dwarf ellipticals form a continuous but not monotonic sequence in mean surface brightness as a function of absolute magnitude $M_{BT}$ and that M32 – which deviates prominently from this sequence – is pathological.
Fig. 1.56. Luminosity functions of (top) normal elliptical galaxies roughly from M32 to M87 and (bottom) spheroidal galaxies roughly from Draco and UMi to galaxies such as NGC 205 (Wirth & Gallagher 1984). At that time, “spheroidals” were commonly called “dwarf ellipticals”. This figure then shows that the smallest non-dwarf ellipticals have lower luminosity than the biggest dwarf ellipticals.

Wirth & Gallagher (1984) were the first to suggest that M32-like compact ellipticals and not the more diffuse galaxies like Draco and Leo I and NGC 205 form the faint end of the luminosity sequence of elliptical galaxies. This was based on a successful search for relatively isolated dwarf compact ellipticals which resemble M32. The new compact ellipticals and the well known ones that are companions to larger galaxies were found to lie along the extrapolation to lower luminosity of the correlations for normal ellipticals of parameters such as effective radius and velocity dispersion. With respect to this family of normal ellipticals, “the diffuse ellipticals are a distinct structural family of spheroids whose properties begin to diverge from those of the classical ellipticals at an absolute magnitude of $M_B \sim -18$. At $M_V = -15$, these two families differ in mean surface brightness by nearly two orders of magnitude. The key point to note for this discussion is that, in the range $-18 \lesssim M_B \lesssim -15$, both structural classes of elliptical galaxies coexist” (Wirth & Gallagher 1984). This implies that the luminosity functions of elliptical and spheroidal galaxies differ as shown in Fig. 1.56.

The Wirth & Gallagher (1984) paper was largely based on four newly found, free-flying compact ellipticals. The competing idea (Faber 1973) that compact ellipticals are tidally truncated was largely based on three galaxies, M32, NGC 4486B and NGC 5846A; then the diffuse dwarfs would be the faint extension of the E sequence. With both conclusions based on small numbers of galaxies, it was not clear which picture is correct. The rest of this section reviews the now very strong evidence that Wirth & Gallagher (1984) were presciently close to correct in almost every detail, including Fig. 1.56.
As a graduate student at Caltech in the early 1970s, I was brought up on the picture that ellipticals form a continuous, non-monotonic sequence in their structural parameters from the brightest to the faintest galaxies known. Then, in the 1980s, I gained access to two important technical advances. The first was CCD detectors that are linear in sensitivity over large dynamic ranges. The second was the Canada-France-Hawaii telescope (CFHT), which had the best “seeing” then available on any optical telescope. These allowed me to study the central structure of galaxies in unprecedented detail. The results revolutionized my picture of ellipticals. They confirmed and extended Wirth & Gallagher (1984), whose ideas I was not aware of until the end of my work. The story is instructive for students, so I describe it here in detail, abstracted from a popular article in *Stardate* magazine (Kormendy 2008b).

My CFHT surface photometry showed an unexpected result (Fig. 1.57). Ellipticals define the sequence of red points: less luminous ones are smaller and higher in surface brightness from M 87 to M 32. This much was expected; for bright galaxies, it is the correlation shown by the filled circles in Fig. 1.55. Importantly, the high-resolution CFHT photometry helps to fill in the gap between M 32 and the other ellipticals. This makes M 32 look less peculiar.

Fig. 1.57. Kormendy (1985, 1987) showed with much larger samples that E and Sph galaxies form disjoint sequences in parameter space (cf. Wirth & Gallagher 1984). Sphs (yellow) are not faint ellipticals (red). Instead, their parameter correlations are almost identical to those of dwarf spiral and irregular galaxies (blue). This figure shows approximate central surface brightness and King (1966) core radius, both corrected as well as possible for PSF blurring, versus $B$-band absolute magnitude.
The surprise was the behavior of the “dwarf ellipticals”, shown in Fig. 1.57 by yellow points. Using near-central parameters rather than parameters measured within the effective radii $r_e$ as in Fig. 1.55, it is clear that dwarf ellipticals do not satisfy the correlations for elliptical galaxies. Less luminous dwarf ellipticals are lower – not higher – in surface brightness. A gap has appeared between ordinary and dwarf ellipticals. Wirth & Gallagher’s (1984) conclusions are confirmed with a much larger sample.

Size and density are diagnostic of galaxy formation, so I realized at this point that dwarf ellipticals are not ellipticals at all. As one point after another got plotted and intermediate cases failed to show up, my previous picture of elliptical galaxies fell apart. Kuhn (1970) captures exactly what happens in a scientist’s mind when his understanding of a subject falls apart. Quoting Kormendy (2008b): “The first reaction was consternation. What have I screwed up? I checked my data reduction. I considered whether my galaxy sample could be biased. Nothing seemed wrong. Better data just led in an unexpected direction. I had to accept the new result: dwarf ellipticals are not ellipticals. But then we should not call them “dwarf ellipticals”. The smallest such companions to our Milky Way had sometimes been called dwarf spheroidals. So, to minimize the departure from tradition, I called all such objects “spheroidals”. The biggest ones in Virgo are only as luminous as an average elliptical, but they are giant spheroidals.”

“If spheroidals are not ellipticals, what are they? Kuhn describes what happens next. Deprived of the guidance of any previous understanding of a subject, a scientist in the midst of a scientific revolution does not know what to do next. In turmoil and in desperation, wild ideas get tried out, most of them wrong. I plotted in my diagrams all the other kinds of stellar systems that I knew about. I plotted globular clusters of stars [green points], spiral galaxy disks [two large blue plus signs, each an average for several galaxies from Freeman 1970], and irregular galaxies [blue plus signs]. The globulars were unconnected with ellipticals and spheroidals. But the irregulars and spirals were a surprise. They showed exactly the same correlations as the spheroidals. Aha! A new picture was emerging. Maybe spheroidals are related to spirals and irregulars. They have almost the same structure. They don’t contain gas and young stars, which are common in spirals and irregulars. And they have smoother structure. But I realized that, if the gas were removed or converted into stars, dynamical evolution of the now-gasless spheroidal would smooth out its formerly patchy structure within a few galactic rotations. We knew that the dwarf spheroidal companions of the Milky Way had varied star formation histories. A few contain only old stars, as ellipticals do, but most experienced several bursts of star formation,
and the most recent burst was a few billion or even as little as a few hundred million years ago. What are galaxies that have not yet had their last burst of star formation and that therefore still must contain gas? This is not a controversial question [Kormendy & Bender 1994]. They are irregulars. I realized: if we looked at the Milky Way’s dwarf spheroidals when the Universe was half of its present age, about half of them would still be irregulars. Irregulars have been turning into Sphs gradually over most of the history of the Universe. In the Virgo cluster, lots of processes can make this happen. The most obvious is ram-pressure stripping: as an irregular galaxy falls into Virgo for the first time, it rams into the million-degree gas that fills the cluster, and its cold gas gets swept away. It started to look like no accident that the irregulars in Virgo live around the outside of the cluster, while the center is inhabited by spheroidals [Binggeli et al. 1987]."

“Within a few days, I had a new picture. Spheroidals are defunct spiral and irregular galaxies converted by their environment to look like ellipticals. This helped our picture of galaxy formation, because we already knew that ellipticals form by galaxy mergers, whereas, quoting Tremaine (1981), ‘Dwarf elliptical satellite galaxies cannot form by mergers with other satellites since their relative velocities are too high.’ We were in trouble when we had to find a single formation process that could explain NGC 4472, one of the biggest galaxies in the nearby Universe, and dwarf spheroidals that are a million times less luminous and that look like fragile, gossamer clouds of stars [Fig. 1.58 here]. But they look like the smallest irregulars, minus gas and young stars [Fig. 1.52 here]. So this problem was solved. I reported these results [at a workshop in Rehovot, Israel], and they were well received.” The result that E and Sph galaxies are different is called the E – Sph dichotomy.

Fig. 1.58. Luminosity sequence of dSph satellites of our Galaxy. Fornax, Sculptor and Draco have absolute magnitudes of $M_V = -13.2$, $-11.1$ and $-8.8$, respectively (Mateo 1998), and correspondingly decreasing surface brightnesses (see Fig. 1.57). Draco is the cloud of faint stars in the right panel; the bright stars with the instrumentally-produced red halos are foreground stars in our Galaxy. Contrast M 87 in Fig. 1.52. Could M 87 and Draco really have similar formation histories, with different results only because changing the mass tweaks the formation physics? The results reviewed here imply that the answer is “no”. We now believe that M 87 is a remnant of the dynamical violence of galaxy mergers, whereas Draco formed quiescently as a dwarf irregular that lost its gas long ago. From Kormendy (2008b).
1.7.3 Mixed reactions to the E – Sph dichotomy

Scientific research is a quintessentially human enterprise, as reactions to the above result illustrate:

The essential theoretical understanding of why Sph and S+Im galaxies have lower stellar densities at lower galaxy masses followed immediately. Dekel & Silk (1986) “suggest that both the dI’s and the dE’s [here: dSphs] have lost most of their mass in [supernova-driven] winds after the first burst of star formation, and that this process determined their final structural relations. The dI’s somehow managed to retain a small fraction of their original gas, while the dE’s either have lost all of their gas at the first burst of star formation or passed through a dI stage before they lost the rest of the gas and turned dE.” Our story here adds detail on dI → dSph transformation processes but otherwise is based on exactly the above picture.

Reactions among observers have been more mixed. The reasons are many and revealing and occasionally entertaining; they range from innate conservatism to specific scientific arguments to turf wars. I will concentrate on the part of this history that is most instructive for students.

I already noted that many astronomers are conservative: they do not easily discard a picture that they believed in for many years. This is healthy – imagine what would happen if we chased, willy-nilly, after every outrageous idea that got proposed. It is prudent to treat new ideas with respect, but in a mature subject, it is uncommon for a long-held, well-supported picture to be completely wrong. The situation is more tricky when subjects are young and not yet well developed. This proved to be such a case. Nevertheless, it is understandable that people who had long been involved in research on dwarf galaxies reacted to the above developments with some ambivalence. In particular, the group of Sandage, Binggeli, Tammann and Tarenghi wrote a series of papers on the Virgo cluster in the mid-1980s, some before and some after the Wirth & Gallagher (1984) and Kormendy (1985, 1987) papers. Struggles with the new ideas were evident in some of the later papers. The nature of these struggles reveals how seeds of the new ideas could have been recognized in the older results. I belabor this point because the conceptual blindness that results when we embrace a paradigm of how nature works always threatens our ability to see something new. As you do your research, it is healthy to be careful and conservative but also prudent to ask yourself: Am I missing something because of paradigm-induced conceptual blindness? Kuhn (1970) provides a perceptive discussion of this subject.

Figure 1.55 already illustrated how one hint – the opposite slopes of the surface-brightness–luminosity correlations – was contained in previous work.
Figure 1.59 is a better illustration (Sandage et al. 1985b). It shows with data on Virgo galaxies the result that is shown schematically in Fig. 1.56. The luminosity function of ellipticals is bounded at high and low $L$. M 32 has normal properties for its low luminosity, but such tiny ellipticals are rare. In contrast, spheroidal galaxies (which Sandage et al. 1985b call “dEs”) never are very bright, but they get rapidly more common at lower luminosities until they are lost in the detection noise. The steep faint-end slope of the luminosity function had been recognized for a long time (Zwicky 1942, 1951, 1957) and is built into the well known Schechter (1976) analytic luminosity function. But, to the best of my knowledge, Sandage et al. (1985a, b) and Binggeli et al. (1988) were the first to measure luminosity functions separately for different morphological types of galaxies and to show that only Sph galaxies have luminosity functions that continue to rise with decreasing luminosity to the detection limit of the data. This is the solid result in Fig. 1.59. Here is the incongruity:

Sandage et al. (1985b) distinguish between elliptical and dwarf elliptical galaxies of the same luminosity. Quoting Kormendy & Bender (2012): “A dwarf version of a creature is one that, when mature, is smaller than the normal sizes of non-dwarf versions of that creature. . . . And yet, [Fig. 1.59] invites us to imagine that the smallest non-dwarf ellipticals are 20 times less luminous than the brightest ‘dwarf ellipticals’.”
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Sandage and collaborators recognized and struggled with this incongruity. Quoting Sandage & Binggeli (1984): “The distinction between E and dE types is made on morphological grounds alone, using surface brightness as the criterion. Normal E galaxies have a steep radial profile (generally following an $r^{-1/4}$ law) with high central brightness. The typical dE has a nearly flat radial profile, following either a King [1966] model with a small concentration index or equally well an exponential law. The morphological transition from E to dE is roughly at $M_B \simeq -18$, but there is overlap.”

Recognition of this difference dates back at least to Baade (1944): “NGC 147 and NGC 185 are elliptical nebulae of very low luminosity. In structure, they deviate considerably from what is considered the typical E-type nebula. In both objects the density gradient is abnormally low.” Binggeli et al. (1985) also recognized the quantitative similarity between spheroids and irregulars; their Virgo “membership criteria applied are: (1) dE and Im members have low surface brightness. . . .”. Soon afterward, Sandage et al. (1985b) admit that “We are not certain if this [E – dE dichotomy] is totally a tautology due merely to the arbitrary classification criteria that separate E from dE types . . . or if the faint cutoff in the [E luminosity function] has physical meaning related to the properties of E and dE types. In the first case, the problem would be only one of definition. In the second, the fundamental difference in the forms of the luminosity functions of E and dE types . . . would suggest that two separate physical families may, in fact, exist with no continuity between them (cf. Kormendy 1985 for a similar conclusion).” Revising a long-held picture can be uncomfortable.

Within a few more years, Binggeli et al. (1988) recognized that “The distinction [between] Es and dEs must almost certainly mean that the two classes are of different origin [Kormendy 1985, Dekel & Silk 1986]. This is also supported by the fact that the luminosity functions of Virgo Es and dEs [are different].” And Binggeli & Cameron (1991) concluded that “there are no true intermediate types between E and dE. The [E–dE] dichotomy is model-independent” (emphasis in the original).

But psychology did not lose its hold on people. Binggeli changed his mind: in a section entitled “The E–dE dichotomy and how it disappears”, Jerjen & Binggeli (1997) emphasize the observation that, in a plot of brightness profile Sérsic index versus $M_{BT}$, E and dE galaxies show a continuous correlation. They conclude that compact ellipticals like M 32 and its analogs in Virgo are “special” and that dEs form the extension of the ellipticals to low $L$. However, this is not the only relevant correlation. The observations which suggest the dichotomy had not disappeared. And the fact that one can find parameters of galaxies that are insensitive to the differences between two
types does not prove that the two types are the same. Many parameters are continuous between ellipticals and spheroidals. E.g., the content of heavy elements is not only a continuous function of luminosity for ellipticals and spheroidals, it is essentially the same continuous function for spirals and irregulars, too (e.g., Mateo 1998). If we looked only at element abundances, we would be blind to all structural differences encoded in Hubble types.

More recent criticisms of the E – Sph dichotomy are reviewed in Kormendy et al. (2009) and in Kormendy & Bender (2012). The arguments involve technical details such as sample size and profile analysis techniques. These are of less immediate interest, and any discussion of them quickly gets long. I therefore refer readers to the above papers for our answers to the criticisms. A few are relevant here and will be discussed below. But the best way to address uncertainty about the E – Sph dichotomy is to observe larger samples of galaxies and to address more general scientific questions, as follows.

### 1.7.4 Confirming the E–Sph dichotomy with large galaxy samples

Kormendy et al. (2009: KFCB) extend the sample size of the parameter correlations in Fig. 1.57 by measuring brightness profiles for all known ellipticals in the Virgo cluster and combining these with data on ∼275 Sph galaxies. Examples are shown in Fig. 1.60. Data from many sources were combined to construct composite profiles over large dynamic ranges. Sérsic functions fit most of the galaxy light to remarkable precision: over the fit ranges (vertical dashes in Fig. 1.60), the average RMS deviation = 0.040 mag arcsec$^{-2}$ for the whole KFCB sample. Kormendy (2009) further added ellipticals from Bender et al. (1992) and Sphs from Chiboucas et al. (2009). The updated Fig. 1.57 is shown in Fig. 1.61.

![Fig. 1.60. Surface brightness profiles of 3 galaxies from KFCB. NGC 4486 (M 87) is an elliptical galaxy with a central “core”; i.e., central “missing light” with respect to the inward extrapolation of the outer Sérsic function fit (black curve). NGC 4458 is an elliptical galaxy with central “extra light” above the inward extrapolation of the outer Sérsic fit. VCC 1185 is a Sph galaxy with a nuclear star cluster (type Sph,N) in addition to its Sérsic-function main body. This figure illustrates the robust profiles that are derived by using many images that provide data in overlapping ranges of radii (e.g., HST data near the center; large-field CFHT data at large r).](image)
Figure 1.61 strongly confirms the dichotomy between E and Sph galaxies as found in Kormendy (1985, 1987), Binggeli & Cameron (1991) and Bender et al. (1992, 1993). Note that the Sph sequence approaches the E sequence near its middle, not near its faint end.

Fig. 1.61. Global parameter correlations from KFCB and Kormendy (2009) with Sph galaxies in the Local and M81 groups updated from Kormendy & Bender (2012). This figure shows 90 ellipticals and 295 spheroidals. One elliptical plots in the Sph sequence when effective parameters are used; difficult cases such as this one were classified in KFCB using parameters measured at the radius that contains 10% of the total light. Reason: the E–Sph dichotomy is most pronounced when near-central parameters are used (contrast Fig. 1.57 with this figure).
The small-$r_e$, bright-$\mu_e$ end of the sequence of ellipticals is defined in part by galaxies like M 32 that are sometimes called “compact ellipticals”. As noted above, compact ellipticals are not a special class. They are continuously connected to brighter ellipticals in essentially all parameters. Moreover, M 32 is no longer unique, as it appeared to be in Fig. 1.57. We now know of a number of M 32 analogs (Binggeli et al. 1985; Lauer et al. 1995; Faber et al. 1997; KFCB). Figure 1.61 illustrates and KFCB reviews evidence that M 32 is normal for its low $L$. However, it is often suggested that these galaxies are compact only because they have been tidally stripped by much larger companions (e.g., Faber 1973; Ferrarese et al. 2006; Bekki et al. 2001; Chen et al. 2010). Kormendy & Bender (2012) review why it is not plausible that this is the explanation for why small Es are compact. This issue is important, so I enumerate the arguments here:

(a) Compact ellipticals are not always companions of brighter galaxies (Wirth & Gallagher 1984). Some are so isolated that no tidal encounter with a big galaxy is likely ever to have happened (e.g., VCC 1871: Kormendy & Bender 2012).

(b) Compact Es do not have small Sérsic indices suggestive of tidal truncation. In fact, they have the same range of Sérsic indices $n \sim 2$ to 3.5 as isolated coreless ellipticals. For example, M 32 has $n \approx 2.9$, larger than the median value for coreless ellipticals. Numerical simulations show that major mergers of gas-poor galaxies like the ones in the nearby Universe make remnants that have exactly the above range of Sérsic indices (Hopkins et al. 2009a).

(c) Many Sph galaxies also are companions of bright galaxies, but we do not argue that they have been truncated and thereby made abnormally compact. An example is NGC 205, which is shown by the open square at $M_{VT} = -16.6$ in Fig. 1.61. It is much fluffier than M 32.

(d) Figure 1.68 below will show that the compact end of the E sequence is also defined by tiny bulges. Classical bulges and ellipticals have closely similar parameter correlations. Most classical bulges that appear in our correlation diagrams do not have bright companion galaxies.

(e) In Fig. 1.61, the ellipticals from M 32 to cD galaxies define projections of the “fundamental plane” correlations (Djorgovski & Davis 1987; Faber et al. 1987; Djorgovski et al. 1988; Bender et al. 1992). Its interpretation is well known: galaxy parameters are controlled by the Virial theorem modified by small nonhomologies. N-body simulations of major galaxy mergers reproduce the E-galaxy fundamental plane, not the Sph parameter sequence that is almost perpendicular to it (Robertson et al. 2006; Hopkins et al. 2008, 2009b).

Kormendy and Bender conclude: “some compact Es may have been pruned slightly, but tidal truncation is not the reason why the E sequence extends to the left of where it is approached by the Sph sequence in [Fig. 1.61].”
1.7.4.1 Classical bulges and ellipticals satisfy the same fundamental plane parameter correlations. I. Bulge-disk decomposition

Point (d) above anticipates the result of this subsection: classical bulges are essentially indistinguishable from elliptical galaxies of the same luminosity. This in turn was further anticipated when I defined classical bulges to be elliptical galaxies that happen to live in the middle of a disk. Here, the time has come to ante up the evidence by adding classical bulges to Fig. 1.61.

Figure 1.62 emphasizes the most important requirement for this analysis. For each disk galaxy, it is necessary to decompose the observed brightness distribution into (pseudo)bulge and disk parts. This is a fundamental part of the classification of the central component as classical or pseudo. It provides separately the parameters of the bulge and the disk, both of which we need. For some applications, a kinematic decomposition is also needed.

Photometric decomposition is the crucial requirement that allows us to ask whether classical bulges satisfy the parameter correlations for ellipticals. Absent such a decomposition, even the distinction between ellipticals and spheroidals is blurred. This is part of the reason why Ferrarese et al. (2006); Chen et al. (2010), and Glass et al. (2011) do not see the E–Sph dichotomy. If bulges and disks are combined in various proportions and then measured as one-component galaxies, it is inevitable that the resulting parameters will be intermediate between those of bulges and disks and that including them will blur the distinction between the bulge and Sph $\approx$ disk sequences in Fig. 1.61 (see Figs. 76 and 77 in KFCB and Figs. 1.63 and 1.64 here).

Fig. 1.62. (left) Sombrero Galaxy and (right) NGC 4762, the second-brightest S0 galaxy in the Virgo cluster. These galaxies illustrate why bulge-disk decomposition is necessary. NGC 4594 is an Sa galaxy with $B/T = 0.93 \pm 0.02$ (Kormendy 2011b). Without photometric decomposition, we measure essentially only the bulge. We learn nothing about the disk. If an S0 version of this galaxy (e.g., NGC 3115) were viewed face-on, it would be difficult even to discover the disk (Hamabe 1982). In contrast, NGC 4762 is an edge-on S0 with a tiny bulge; $B/T = 0.13 \pm 0.02$ (Fig. 1.63). Without photometric decomposition, we measure essentially only the disk. We learn nothing about the bulge.
The need for bulge-disk decomposition can best be understood using an analogy. Imagine studying a population of people, horses and people who ride on horses. Knowing nothing about them, one might measure parameters and plot parameter correlations (linear size, mass, . . .) to look for different physical populations and regularities within each population that might drive interpretation. We need to be careful, because some parameters (volume mass density within this analogy; mass-to-light ratio for galaxies) prove to be insensitive to structural differences. Still, careful parameter study is promising. But the biggest people are bigger than the smallest horses. If random people are paired with random horses and the resulting population of people+horses, together with some pure people and some pure horses, are analyzed as one-component systems, it is inevitable that a complete continuity will be found between people and horses. But it would be wrong to conclude that people are the same as horses. Rather, if one decomposes people and horses when they occur together and measures their parameters separately, it will be found that some parameter correlations clearly separate people of various sizes from horses of various sizes, even though their size distributions overlap. Further study will also show that certain special parameters (semi-trivially: number of arms versus number of legs in this analogy; near-central parameters in the cases of galaxies) are especially helpful in distinguishing the physically different populations that are under study. The one elliptical galaxy (red point) that lies within the sequence of Sphs (green points) in some panels of Fig. 1.61 was classified using central parameters (Fig. 34 in KFCB).

It feels strange to “beat this dead horse” (I’m sorry – I could not resist): the need for component decomposition has been understood for more than 30 years. It quickly became standard analysis (Kormendy 1977a; Burstein 1979; Kent 1985). It is still so now (Peng et al. 2002; Knapen et al. 2003; de Souza et al. 2004; Laurikainen et al. 2004, 2005, 2007; Courteau et al. 2007; Méndez-Abreu et al. 2008; Weinzirl et al. 2009). The structure (this section) and formation physics (Section 1.8) of bulges and disks are very different, and it blurs our vision of both to analyze them as single-component systems.

1.7.4.2 Small-bulge S0 galaxies and the transition from S0 to Sph galaxies
Kormendy & Bender (2012: KB2012) collect bulge and disk parameters from a variety of sources for or do photometry and bulge-disk decomposition of all S0 galaxies from the HST ACS Virgo Cluster survey (Côté et al. 2004; Ferrarese et al. 2006). This section reviews the results. Classical bulges are added to the parameter correlation diagrams in Fig. 1.68. But another and – it will turn out – especially interesting result will be to extend the Sph
sequence to higher luminosities. Kormendy & Bender (2012) conclude that Sph galaxies and S0 disks (but not bulges) are continuous in their parameter correlations. That is, Sph galaxies are bulgeless S0s.

Three galaxies serve here to illustrate the transition from S0 galaxies with large classical bulges and flat disks to Sph galaxies with no bulges and with structure that can be vertically disky or thick. We start with NGC 4762. Figure 1.62 shows that it differs from our canonical picture of Hubble classification (Sandage 1961) in which S0 galaxies are transition objects between elliptical and Sa galaxies. The bulge-to-total luminosity ratio $B/T$ is a classification parameter; $B/T \equiv 1$ for ellipticals, and $B/T$ is intended to decrease along the sequence E – S0 – Sa – Sb – Sc. With some noise, this is observed (Simien & de Vaucouleurs 1986). But Sidney van den Bergh (1976) already recognized that some S0 galaxies such as NGC 4762 have small bulges and, except for their cold gas content and spiral structure, are more similar in their overall structure to Sbc galaxies than they are to Sa galaxies. As an alternative to the Hubble (1936) “tuning-fork diagram”, he proposed a “parallel sequence classification” in which S0 galaxies form a sequence S0a – S0b – S0c with decreasing $B/T$ that parallels the sequence Sa – Sb – Sc of spiral galaxies with similar, decreasing $B/T$ ratios. Van den Bergh suggested that late-type S0 galaxies with small bulges are defunct late-type spiral galaxies that were transformed by environmental processes such as ram-pressure stripping of cold gas by hot gas in clusters. The KB2012 bulge-disk decompositions of NGC 4762 and similar galaxies quantitatively confirm van den Bergh’s picture, as follows.

The brightness profile of NGC 4762 measured along the major axis of the disk is shown in Fig. 1.63 (left). It shows a central bright and relatively round bulge and, at larger radii, three shelves in a very flat edge-on disk. The inner shelf is somewhat subtle, but the steep decrease in surface brightness between the middle and outer shelves is obvious in Fig. 1.62. What is this complicated structure? This may seem like a tricky problem, but in fact, it is easy. Relatively face-on galaxies that have two or three shelves in their brightness distributions are very common. The ones with two shelves are the oval-disk galaxies discussed in Section 1.3.3. To get a third shelf, it is just necessary to add an early-type bar – these have shallow radial brightness gradients interior to a sharp outer end. Now, the bar normally fills its attendant lens in one dimension (Section 1.4.3.4 and Fig. 1.17). But consider a non-edge-on SB(lens)0 galaxy such as NGC 2859 (Fig. 1.9) or NGC 2950 (Fig. 1.17) in which the bar has a skew orientation (not along either the apparent major or apparent minor axis). If we rotated either of these galaxies about a horizontal line through the center in the corresponding
figure until the galaxy was seen edge-on, its disk would show three shelves in its major-axis profile. Exterior to the bulge, the innermost shelf would be the bar, the next would be the lens, and the third would be the outer disk. This is how Kormendy & Bender interpret Fig. 1.63 (left). Thus NGC 4762 is an edge-on SB(lens)0 galaxy. Bars and lenses have shallow brightness gradients at small $r$, so profile decomposition is easy. The bulge Sérsic index $n = 2.29 \pm 0.05$ and round shape identify it as classical. Importantly, $B/T = 0.13 \pm 0.02$ is very small. So Kormendy & Bender (2012) classify NGC 4762 as SB(lens)0bc. Note in Fig. 1.63 (right) how measuring NGC 4762 as a single-component system (green point with brown center) mixes parameters of the classical bulge (brown point) and disk (green cross). Only after bulge-disk decomposition do we see that the tiny classical bulge of NGC 4762 helps to define the compact extension of the E–bulge parameter sequence.

Fig. 1.63. (left) Ellipticity and surface brightness along the major axis of NGC 4762 measured by fitting ellipses to the isophotes in the ACS and SDSS $g$-band images. The dashed curves show a decomposition of the profile inside the fit range (vertical dashes). The bulge, bar, lens and disk are represented by Sérsic functions with indices $n$ given in the figure. Their sum (solid curve) fits the data with an RMS of 0.033 V mag arcsec$^{-2}$. (right) Parameter correlations showing the results of the bulge-disk decomposition. The green filled circles with the brown centers show the total parameters measured by Ferrarese et al. (2006) for the bulge and disk together. They are connected by straight lines to the parameters of the bulge (dark brown filled circles) and disk (dark green crosses). From KB2012.
NGC 4452 is closely similar to NGC 4762 but is even more extreme. Figure 1.64 (left) shows that it, too, is an edge-on SB(lens)0 galaxy. The decomposition robustly shows that NGC 4452 has only a very tiny pseudobulge with \( n \simeq 1.06 \pm 0.14 \) (recall classification criterion (6) in Section 1.5.3) and \( PB/T = 0.017 \pm 0.004 \). This is an SB(lens)0c galaxy.
The parameter correlations in Figs. 1.63 and 1.64 serve to emphasize how bulge-disk decomposition improves our understanding of the E sequence. The small black filled dots show the parameters measured by Ferrarese et al. (2006) for the ACS Virgo cluster survey S0s. They do not violate the E sequence. But they do combine bulge and disk properties into one set of parameters, so they fail to show something that is very important. In each of these two galaxies, the bulge is tiny, comparable in luminosity to the smallest ellipticals. The classical bulge of NGC 4762 helps to define the extension of the E sequence toward objects that are more compact than any spheroidal. Even the tiny pseudobulge of NGC 4452 lies near the compact end of the E+bulge sequence (cf. Figs. 1.42 and 1.43, which show other, similarly compact and tiny pseudobulges). Figures 1.68 and 1.69 will summarize the parameter correlations for classical bulges and S0 disks, respectively. Here, I want to emphasize two things. First, there exist S0 galaxies with classical-bulge-to-total luminosity ratios \(B/T\) that range from almost 1 to essentially zero. The pseudobulge in NGC 4452 is so small that one cannot hide a significant classical bulge in that galaxy. Second, both NGC 4762 and NGC 4552 have vertically thickened and warped outer disks. Both galaxies have nearby companions. Kormendy & Bender (2012) interpret these results as indicating that the outer disks are tidally warped and being heated dynamically in the vertical direction. They present evidence that many other S0 and Sph galaxies in the Virgo cluster are dynamically heated, too. Thus NGC 4762 and NGC 4552 are “missing links” that have some properties of S0 galaxies and some properties of the brightest Sph galaxies.

NGC 4638 is even more spectacularly an S0 – Sph transition object. Figure 1.65 shows (bottom) the large-scale structure and (top) an embedded, edge-on disk and bulge in an enlargement from HST images. When we wrote KB2012, this structure was, to our knowledge, unique. Figure 1.65 (bottom) suggests that NGC 4638 is an edge-on S0 whose bulge happens to be very boxy. This would be interesting but not unique; boxy bulges are discussed in Section 1.5.2.9. But already in the bottom panel of Fig. 1.65, the structure looks suspiciously unusual: the brightness gradient in the boxy structure is very shallow, like that in its companion, the normal Sph,N galaxy NGC 4637. The top panel of Fig. 1.65 shows an almost-round, small bulge in NGC 4638 with a normal, steep brightness gradient. To our surprise, the brightness profile robustly shows (Fig. 1.66) that the outer boxy structure has a Sérsic brightness profile with \(n = 1.11 \pm 0.12\) characteristic of the main body of a Sph galaxy. This profile is not concave-upward, as it would be if the bulge and the boxy structure where part of the same component with \(n \gg 4\).
Fig. 1.65. (top) Color image of NGC 4638 = VCC 1938 made from the HST ACS g, mean of g and z, and z images. This image shows the edge-on disk and central bulge. Brightness is proportional to the square root of intensity, so the brightness gradient in the bulge is much steeper than that in the boxy halo. The very red foreground star near the NE side of the disk is also evident in the bottom image. (bottom) Color image of NGC 4638 = VCC 1938 from Wikisky. The brightness “stretch” emphasizes faint features, i.e., the extremely boxy, low-surface-brightness halo in which the S0 disk and bulge are embedded. The elongated dwarf to the west of NGC 4638 is the Sph,N galaxy NGC 4637. Like many other spheroidals, NGC 4637 is flatter than any elliptical. Note also that VCC 2048 (not illustrated) is another “missing link” galaxy with both S0 and Sph properties: like NGC 4637, it is flatter than any elliptical; its main body is clearly a Sph, but it contains an embedded, tiny S0 disk (see KB2012, from which the above images are taken).
Kormendy & Bender (2012) therefore conclude that NGC 4638 contains three structural components, and edge-on S0 galaxy that consists of an $n = 3.6 \pm 1.4$ classical bulge plus an $n = 0.5 \pm 0.1$ Gaussian disk embedded in a normal Sph galaxy with $n = 1.11 \pm 0.12$. I. e., NGC 4638 has the properties of both an S0 and a Sph galaxy. VCC 2048 is similar (Fig. 1.65 caption).

It is instructive to compare the parameters of the three components of NGC 4638 with their counterparts in pure S0 and Sph galaxies (Fig. 1.67). The classical bulge helps to define the compact end of the normal E–Sph parameter sequence. It is within a factor or $\sim 2$ as compact as M32. The disk proves to have the highest effective brightness of any S0 disk shown in Fig. 1.69. The reasons are (1) that it is edge-on, so the path length through it is large, and (2) that its profile is Gaussian rather than exponential; the strong outer truncation results in small $r_e$ and hence bright $\mu_e$. The boxy component is consistent with the extrapolation of the Sph sequence; it is the brightest Sph galaxy known in the Virgo cluster.

Fig. 1.66. Ellipticity $\epsilon$ and surface brightness $\mu_V$ along the major axis of NGC 4638 as measured on the HST ACS and SDSS g images. Dashed curves show a three-Sérsic-function decomposition of the profile inside the fit range (vertical dashes). The bulge is small, but it is classical. The disk has a Gaussian profile, as do many other S0s discussed in KB2012. Remarkably, the outer, boxy halo is clearly distinct from the bulge and disk and has a Sérsic index $n = 1.11 \pm 0.12$. The sum of the components (solid curve) fits the data with an RMS of 0.054 V mag arcsec$^{-2}$. From KB2012.
NGC 4638 lives in a high-density part of the Virgo cluster where strong dynamical heating is plausible. Kormendy & Bender interpret the boxy Sph part of the galaxy as the dynamically heated remnant of the outer disk. Because these stars are no longer part of a disk, the disk that remains has a strongly truncated, i.e., Gaussian profile.

KB2012 discusses additional evidence that higher-luminosity Sphs are, by and large, more disky. This is consistent with the suggestion that dynamical heating is one of the $S \rightarrow $ Sph transformation processes and that this heating has the smallest effect on the biggest, most robust galaxies.

Fig. 1.67. Parameter relations showing results of the bulge-disk-Sph decomposition of NGC 4638. The green circles with the brown centers show the total parameters measured by Ferrarese et al. (2006) for all components together. These points are connected by lines to the parameters of the classical bulge (brown circles), the disk (green crosses), and the Sph halo (green square). From KB2012.
1.7.4.3 Interim summary and road map

In Section 1.7.4.2, our discussion of the E–Sph dichotomy branched out in a new direction – the close relationship between Sphs and S0 galaxy disks. Section 1.7.5 pursues this. Meanwhile, it is useful to summarize where we are.

Section 1.7 is about environmental secular evolution. The “bottom line” will be that a variety of environmental processes appear to have transformed some intermediate-Hubble-type spiral galaxies into S0s and some late-type spiral and Magellanic irregular (Im) galaxies into Sphs. Sph galaxies will prove to be bulgeless S0s. “Missing link” galaxies that have some S0 and some Sph properties are the new subject that entered the above discussion.

Recall that we were in the process of investigating the E–Sph dichotomy. That is, even though they look similar, elliptical and spheroidal galaxies have quantitatively different structural parameters and parameter correlations. This implies that they have different formation histories – histories that we are in the process of deciphering. I reviewed the history of the above discovery, concentrating on how improved measurements and enlarged galaxy samples have strengthened the evidence for the dichotomy. Originally not recognized (Fig. 1.55), it was first found using small galaxy samples (Fig. 1.57) and since has been confirmed using 90 ellipticals and 295 spheroidals (Fig. 1.61). Our next aim has been to add classical bulges, to increase the sample size and to further show that tiny ellipticals are not compact because they are tidally stripped. This led us into a discussion of bulge-disk decomposition and a description of three example galaxies, two of which have classical bulges that are substantially as compact as the smallest ellipticals. In our standard picture of bulge formation by major mergers, these bulges would have formed before their attendant disks. It is implausible that such bulges are compact because they were tidally stripped.

The bulge parameters measured and collected in KB2012 now allow us to “pay the piper” in confirming our definition of bulges as (essentially) ellipticals that live in the middle of a disk. This is the subject of Section 1.7.4.4. I then return to Sph and S0 galaxies in Section 1.7.5.

1.7.4.4 Classical bulges and ellipticals satisfy the same fundamental plane parameter correlations. II. Results

Figure 1.68 shows the parameter correlations from Fig. 1.61 with 57 bulges added. Of these, 35 are known to be classical via their parameters and the discussion in the source papers (see the key). I also add 22 bulges from Baggett et al. (1998); they are shown with open circles, because we cannot be certain that they are classical. I examined all of these galaxies and ensured as well as possible (using Section 1.5.3) that their bulges are classical.
Figure 1.68 confirms the assumptions that underlie our definition of classical bulges: they satisfy the same parameter correlations as do ellipticals. Given the uncertainties in bulge-disk decomposition, there is no evidence that the scatter for classical bulges is different from that for ellipticals. This is an update of a result that has been found previously, e.g., by Fisher & Drory (2008, 2010: Fig. 1.41 here). Pseudobulges can satisfy these relations, but they have much larger scatter, and they fade out by becoming low in surface brightness, not by becoming compact (Figs. 1.42 and 1.43).
1.7.5 Sph galaxies are bulgeless S0 galaxies

Figure 1.69 shows Fig. 1.68 with the disks of S0 galaxies added. Kormendy & Bender (2012) conclude that spheroids are continuous in their parameter correlations with the disks (but not the bulges) of S0 galaxies. People call a galaxy an S0 if it has smooth, nearly elliptical isophotes and two components, a bulge and a disk. If it has no bulge and only one, shallow-surface-brightness-gradient component, we give it a different name – a spheroidal.

Fig. 1.69. Parameter correlations for ellipticals, bulges and Sphs with disks of 126 S0s added (green points outlined in black). Bulges and disks of S0 galaxies are plotted separately. The middle panel shows the Freeman (1970) result that disks of big galaxies tend to have the same central surface brightness $\mu_0 = \mu_e - 1.822$ mag arcsec$^{-2}$ for an exponential. We conclude that Sphs are continuous with the disks but not the bulges of S0 galaxies. Updated from KB2012.
Secular Evolution in Disk Galaxies

Fig. 1.70. Maximum rotation velocity of the bulge $V_{\text{circ, bulge}}$ (red points) and disk $V_{\text{circ, disk}}$ (black points) derived in bulge-disk-halo decompositions of the rotation curves of galaxies whose outer, dark matter rotation velocities are $V_{\text{circ}}$. Equality of the visible and dark matter rotation velocities is shown by the dotted line. Every red point has a corresponding black point, but many galaxies are bulgeless and then only a disk was included in the decomposition. This figure illustrates the well known rotation curve conspiracy, $V_{\text{circ, bulge}} \approx V_{\text{circ, disk}} \approx V_{\text{circ}}$ for the halo (Bahcall & Casertano 1985; van Albada & Sancisi 1986; Sancisi & van Albada 1987). It shows that the conspiracy happens mostly for galaxies with $V_{\text{circ}} \sim 200$ km s$^{-1}$. The lines are least-squares fits with variables symmetrized around 200 km s$^{-1}$. The bulge correlation is steeper than that for disks; bulges disappear at $V_{\text{circ}} \approx 104 \pm 16$ km s$^{-1}$. From Kormendy & Bender (2011) and Kormendy & Freeman (2013).

That bulges disappear where Fig. 1.69 suggests is shown in Fig. 1.70. Rotation curve decompositions confirm what our experience tells us: bulges disappear at $V_{\text{circ}} \sim 100$ km s$^{-1}$ or $M_V,\text{disk} \sim -18$ (Tully & Fisher 1977). There is noise; e.g., M 33 has $M_V,\text{disk} = -19.0$ and $V_{\text{circ}} \approx 135 \pm 10$ km s$^{-1}$ (Corbelli 2003) and no bulge (Kormendy & McClure 1993). But of course, we also expect that disks fade when they are transformed from S+Im to S0. Figure 1.70 is an important observational “target” for future work: the formation physics that underlies it is largely unknown. But there is ample evidence that bulges disappear approximately where the Sph and S0 disk sequences meet in Fig. 1.69. This is enough to explain the different names.

Kormendy & Bender (2012) suggest that the kink in the $\mu e^{-M_V}$ correlation that happens roughly at the transition from S0 disk to Sph tells us where the correlation turns into a sequence of decreasing baryon retention at lower galaxy luminosity. It is not an accident that this happens roughly where the bulge contribution to the gravitational potential well disappears.
1.7.6 Spiral and irregular galaxies have the same structural correlations as S0 galaxy disks and Sph galaxies

Kormendy’s (1985, 1987) conclusion that Sph galaxies are defunct dS+Im galaxies depended critically on the observation (Fig. 1.57) that they all have the same structural parameter correlations. That result was based on a small number of galaxies and has never been checked. KB2012 updates and extends this test with 407 galaxies that cover the complete luminosity range from the tiniest dwarf irregulars to the brightest Sc disks. Figure 1.71 shows that S+Im galaxies do indeed have the same parameter correlations as S0 disks and spheroidals. Therefore they are closely related.

Fig. 1.71. Fig. 1.69 correlations with disks of Sa–Im galaxies added (blue points for 407 galaxies from 14 sources listed in the keys). When bulge-disk decomposition is needed, the components are plotted separately. From KB2012.
1.7.7 A revised parallel-sequence classification of galaxies

Figure 1.72 shows our proposed revision of Sidney van den Bergh’s (1976) morphological classification scheme based on the foregoing observations.

Van den Bergh put S0 galaxies in a sequence that parallels the spirals; the classification parameter that determines the stage along either sequence is the (pseudo)bulge-to-total luminosity ratio, \((P)B/T\). Pseudo and classical bulges are not distinguished; in a classification based on small-scale images, this is the only practical strategy. Only \((P)B/T\) and not parameters such as spiral arm pitch angle determine the stage, so van den Bergh’s classification of spirals is not quite the same as Sandage’s or de Vaucouleurs’s. We do not address this issue. Figure 1.72 adopts van den Bergh’s theme of placing S0s and spirals in parallel sequences based only on \((P)B/T\).

Kormendy & Bender extend van den Bergh’s discussion in two ways.

(a) They resolve the uneasy aspect of van den Bergh’s paper that he listed no S0c or later-type S0 galaxies. Based on a comparison of \((P)B/T\) ratios of S0s with spirals of known Hubble type, they find several of the “missing” late-type S0s; e.g., the S0bc galaxy NGC 4762; the S0c galaxy NGC 4452 (Section 1.7.4.2). NGC 4452 is also singled out as an S0c by Cappellari et al. (2011), who independently propose a parallel-sequence classification based on kinematic maps. A few other S0cs are known (Laurikainen et al. 2011; Buta 2012).

(b) They place Sph galaxies in parallel with Im galaxies. They note that, in a more detailed classification that includes Sd and Sm galaxies, some Sphs (e.g., ones with nuclear star clusters) would be placed in parallel with late-type (especially Sm) spirals, and others (e.g., ones without nuclei) would be put in parallel with Im. Adding Sph galaxies at the late-type end of the S0 sequence for the first time finds a natural home for them in a morphological classification scheme.

Fig. 1.72. Revised parallel-sequence morphological classification of galaxies. The E types are from Kormendy & Bender (1996). Transition objects between spirals and S0s (van den Bergh’s anemic galaxies) exist but are not illustrated. Bulge-to-total ratios decrease toward the right; Sc and S0c galaxies have tiny or no pseudobulges. Sph and Im galaxies are bulgeless. From KB2012.
It is important to understand which observations lead to Fig. 1.7.\footnote{Allan Sandage (2004) accused Sidney van den Bergh of hermeneutical circularity in setting up his parallel-sequence classification, which – he thought – involved too much interpretation. A prosaic but sufficient paraphrase is “circular reasoning”. The basic idea is this: a morphological classification of galaxies should be set up based only on observations and not on interpretation (see Section 1.3.4). The aim is that regularities revealed by the classification will later aid interpretation. However, if some interpretation is used in setting up the classification, then the “aid” that the classification can provide is foreordained. This is circular reasoning. In practice, science is not as “black and white” as Sandage suggests. Even the greatest scientists (Sandage explicitly picked Hubble as one of these) set up classifications with future interpretation in mind. They make decisions about which observations to treat as relevant and which ones to treat as secondary. Van den Bergh did this faithfully; Sandage was just uneasy about how important those decisions were. It should be clear from these remarks that I respect both sides of the argument. In the end, further advances reviewed here have, I claim, vindicated van den Bergh’s decisions. For a classification to be successful, it must ultimately motivate a clearcut paradigm of interpretation. Van den Bergh’s parallel-sequence classification has done this.}

They involve quantitative parameter measurements, but they do not involve interpretation. First, the observations that establish E – S0 – Sph continuity:

(a) Galaxies with smooth, nearly elliptical isophotes, little cold gas and little star formation range in bulge-to-total luminosity ratio from $B/T = 1$ to $B/T = 0$. Here, the existence of a bulge component and the measurement of $B/T$ are based on quantitative surface photometry, on nonparametric measurements of structural parameters for elliptical and Sph galaxies by integrating the observed isophotes, on parametric (Sérsic-function-based) bulge-disk decomposition for disk galaxies, and on the resulting structural parameter correlations (Figs. 1.68, 1.69). When $B/T = 1$, we call the object an elliptical; when $1 > B/T > 0$, we call the central component a bulge and the outer component – if flat\footnote{This is to prevent confusion with cD galaxies, which have cluster-sized debris halos, not disks.} – a disk, and when $B/T = 0$, we call the galaxy a spheroidal.

(b) In the structural correlations between effective radius $r_e$, effective brightness $\mu_e \equiv \mu(r_e)$ and total absolute magnitude, Sph galaxies define a sequence that is continuous with the disks but not the bulges of S0 galaxies. There is some overlap in luminosity between Sphs and S0 disks.

(c) NGC 4762, NGC 4452, NGC 4638 and VCC 2048 are galaxies that have both S0 and Sph properties. We know this because all four galaxies are seen edge-on. All contain flat disks. Three contain a tiny (pseudo)bulge (VCC 2048 contains only a nuclear star cluster). The thick outer components of all four galaxies have parameters – including Sérsic indices $n \sim 1$ – that are indistinguishable from those of Sphs. That is, these galaxies consist of S0 central parts embedded in Sph or Sph-like outer halos. This helps to establish S0 – Sph continuity.

(d) Bigger Sph galaxies tend to be dynamically more S0-disk-like: they have larger ratios of rotation velocity to velocity dispersion (van Zee et al. 2004). Note: at all $L$, some Sphs rotate slowly (see KB2012 for a review).

These observations justify our conclusion that Sph galaxies are continuous in their properties with S0 disks, which in turn motivates our juxtaposition of Sph galaxies with S0cs. In essence, Sph galaxies are bulgeless S0s.
Observations that suggest parallel sequences of S+Im and S0+Sph galaxies:

(a) For every $B/T$ ratio that is observed in an S0 or Sph galaxy, there are S or Im galaxies that have corresponding, similar $B/T$ ratios. We see a continuous transition from S0 to E as $B/T \to 0$. We do not know whether SAs also have a continuous transition $B/T \to 0$. The Sombrero galaxy (NGC 4594) has one of the largest bulge-to-total ratios known, $B/T = 0.93 \pm 0.01$ (Kormendy & Bender 2013). I know no Sa with larger $B/T$. Thus it is prudent to retain a classification S0(0) that is intermediate between elliptical and both Sa and S0a.

(b) Except for details such as spiral structure, the *global* structure of spirals and S0s is similar. For any generic Sa, Sb, or Sc galaxy, there are similar S0a, S0b, or S0c galaxies. In particular, the bulges of spiral and S0 galaxies both satisfy the E parameter correlations. The fractions of classical and pseudo bulges are similar at similar stages along the tuning fork (Kormendy & Kennicutt 2004). And the disks of S+Im galaxies have almost the same parameter correlations as Sph galaxies and S0 disks (Fig. 1.71).

(c) Some Sph galaxies contain low-contrast spiral structure; therefore they contain embedded disks (Jerjen et al. 2000, 2001; Barazza et al. 2002; De Rijcke et al. 2003; Graham et al. 2003; Ferrarese et al. 2006; Lisker et al. 2006, 2007, 2009).

(d) Many dSph companions of our Galaxy contain intermediate-age stellar populations (Da Costa 1994; Mateo 1998: Fig. 1.73 here; Tolstoy et al. 2009). Both among the Galaxy’s satellites and in the larger HST ACS Nearby Galaxy Treasury Survey (Weisz et al. 2011a, b), dS, dIm and dSph galaxies have similar, heterogeneous star formation histories except that the star formation rate in dSph galaxies is currently zero. This is a matter of definition – if a dwarf contains gas and star formation, it is called dSph/dIm or dIm. The Virgo cluster contains several examples (Ferrarese et al. 2006; KB2012).

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Fig. 1.73. Star formation histories of dSph and dIm galaxies from Mateo (1998). Relative star formation rates are shown as a function of time since the Big Bang.
Similarly, some spiral galaxies in clusters contain gas only near their centers, and some S0s contain near-central gas and small amounts of star formation. This is discussed in Section 1.7.9. Here, it again means that some S0 galaxies are less different from some spiral galaxies than optical images would suggest.

Van den Bergh’s (1976) “anemic galaxies” are omitted from Fig. 1.72 for simplicity, but they are galaxies that are intermediate in properties between spiral and S0 galaxies. Their contain only low-amplitude spiral structure star formation. The transition from S to anemic to S0 looks continuous.

Thus a substantial collection of morphological and structural parameter observations motivate our suggested parallel-sequence galaxy classification. We revise it to place Sph galaxies at the end of the S0 sequence, juxtaposed with the latest-type spirals and irregulars. It is important to note three things. We do not intend to imply that the luminosity function of galaxies is the same at all stages of the tuning fork. Indeed, we already know that Im and Sph galaxies tend to have lower luminosities than earlier-type S and S0 galaxies. Second, we do not mean to imply that galaxies are equally abundant at every stage of either the S+Im or the S0+Sph sequence. Indeed, it is clear that S0c galaxies are much rarer than Sphs or earlier-type S0s. This provides a hint for interpretation. But it is not a reason to change the classification. And third, we do not intend to fix what isn’t broken. Our suggestion of a parallel-sequence classification is not meant to replace Hubble classes. We propose Fig. 1.72 as a complement to Hubble classification, useful because it encodes a different collection of observations that are relevant to a different collection of questions about formation physics.

1.7.8 Parallel-sequence classification and bimodality in the galaxy color-magnitude relation

Work on galaxy formation nowadays concentrates on the history of star formation in the Universe and on understanding stellar populations. The iconic observation that current work tries to explain is the color bimodality of galaxies in the color-magnitude relation as revealed by the Sloan Digital Sky Survey (SDSS) at low redshifts (Strateva et al. 2001; Bernardi et al. 2003; Kauffmann et al. 2003a, b; Hogg et al. 2002, 2004; Blanton et al. 2003, 2005; Baldry et al. 2004) and by HST studies of galaxies at high redshifts. Figure 1.74 shows this result and illustrates how the E – S0 – Sph arm of the parallel-sequence tuning fork relates to it. The bright end of the prominent and thin red sequence consists of ellipticals, S0s, and some early-type spirals. But their luminosity functions are bounded at low L. When the red sequence is extended fainter, it must become dominated by Sphs at $M_V \ll -18$. The deepest surveys detect this (Blanton et al. 2005; Drory et al. 2009).
1.7.9 $S+Im \rightarrow S0+Sph$ galaxy transformation processes

The natural interpretation of the observations discussed in this section is that S0 and Sph galaxies are defunct, “red and dead” versions of spiral and irregular galaxies that have been transformed by physical processes to be discovered. Most of these turn out to be environmentally driven and slow.

The relative ordering and positioning of galaxies in the parallel-sequence classification is justified on purely observational grounds based on choices of which results to use in the classification and which to regard – for present purposes – as secondary. However, it would be disingenuous to pretend that I and many others have not been thinking about the underlying formation and evolution processes for a long time. This is inevitable in a world where no observational curiosity goes uninterpreted for long. In fact, there are many candidate processes. Astronomers frequently argue about which of many compelling theories are correct. My experience is that these arguments go on longest when everybody is correct. This is one of those occasions.
Candidate S+Im → S0+Sph galaxy transformation processes are reviewed in KB2012. Here, I list them briefly including only the most important supporting observations:

(a) The main internal evolution process was already mentioned in Section 1.7.3. Below a fiducial mass that corresponds to $V_{\text{circ}} \approx 100 \text{ km s}^{-1}$, i.e., just where bulges disappear (Fig. 1.70) and therefore galaxy names get changed from S0 to Sph (Fig. 1.69), supernova-driven winds are expected to expell a larger fraction of a galaxy's baryons from lower-mass objects regardless of whether they now are irregular or spheroidal (e.g., Larson 1974; Saito 1979; Dekel & Silk 1986; Vader 1986; Schaeffer & Silk 1988; see Hensler et al. 2004; Stinson et al. 2007 for two among many more recent discussions). This is why I suggested that the decreasing surface brightnesses of Sph and Im galaxies at lower luminosities (Fig. 1.71) is a baryon retention sequence.

(b) The most thoroughly studied external transformation process is ram-pressure stripping of cold gas by hot gas in clusters and perhaps groups of galaxies. Suggested by Gunn & Gott (1972), the idea has varied in popularity. It has never gained widespread acceptance, perhaps in part because Dressler (1980) argued that it was not the main cause of the morphology-density relation that spiral galaxies get less abundant whereas S0 galaxies get more abundant at higher galaxy densities in clusters. Dressler argued that this result does not strongly depend on cluster richness. However, examination of his Fig. 8–10 (see Fig. 25 in KB2012) shows that the ratio of S0 to S galaxies increases from low-concentration clusters to high-concentration clusters to X-ray-emitting clusters. An alternative hypothesis is that ram-pressure stripping happens more easily in clusters of all richness than simple energy arguments suggest. More recent results bear this out:

Compelling evidence for ongoing ram-pressure stripping is provided by Hα and H\textsc{i} observations of spiral galaxies in the Virgo cluster (Chung et al. 2007; Kenney et al. 2004, 2008). Figure 1.75 shows some of these results. Many spiral galaxies embedded in the X-ray gas that fills the cluster center show remarkable H\textsc{i} tails. The above authors interpret them as cold gas that trails behind the galaxy after having been stripped from the galaxy by the hot gas in the cluster. The spectacular Hα filaments that point from the tidally disturbed NGC 4438 toward the hot-gas-rich NGC 4406 (top panel in Fig. 1.75) are similarly interpreted as ram-pressure stripped. Also, many spirals near the center of the cluster are much smaller and more depleted in H\textsc{i} than are galaxies in the cluster outskirts (Cayatte et al. 1990; Chung et al. 2009). Kormendy & Bender (2012) note that “the three most depleted galaxies illustrated in Fig. 8 of Chung et al. (2009) are NGC 4402, NGC 4405 and NGC 4064. They have a mean absolute magnitude $M_V = -19.4 \pm 0.2$. Virtually all Sphs are fainter than this. If even the deep gravitational potential wells of still-spiral galaxies
Fig. 1.75. The large panel shows 0.5 – 2.0 keV X-ray brightness contours in the Virgo cluster as measured with ROSAT by Böhringer et al. (1994). Superposed are grayscale images of galaxies with H\(_{\text{i}}\) tails indicative of ongoing ram-pressure gas stripping (white or black contours). The H\(_{\text{i}}\) images are from Chung et al. (2007); Kenney et al. (2004); Abramson et al. (2011). The color inset image and large image at top show the H\(_{\alpha}\) emission filaments that extend from NGC 4438 to NGC 4406 (Kenney et al. 2008). Each small inset image shows the galaxy centered on its position in the cluster, but the panels are magnified. This figure is adapted from Fig. 4 in Chung et al. (2007) and is reproduced from KB2012.
suffer H1 stripping, then the shallow potential wells of dS+Im galaxies are more likely to be stripped.” Substantial additional evidence also suggests that ram-pressure stripping is more effective than we thought (see KB2012 and van Gorkom & Kenney 2013 for reviews).

Can ram-pressure stripping still happen in the Local Group’s much shallower gravitational potential well? Compelling observations which indirectly suggest that the answer is “yes” are shown in Fig. 1.76. Close companions of our Galaxy, of M 31, and of other nearby giant galaxies are almost all spheroidals; distant companions are irregulars; Sph/Im transition galaxies tend to live at intermediate distances, and larger irregulars “survive” at closer distances to their giant companions (Einasto et al. 1974; van den Bergh 1994a, b, 2007; Mateo 1998; Skillman et al. 2003; Bouchard et al. 2009; McConnachie 2012). Hints of similar effects in larger satellites are seen in the Zurich Environmental Study (ZENS: Cibinel et al. 2012). Like previous authors, Kormendy & Bender suggest that “ram-pressure stripping can happen even in environments that are gentler than cluster centers. It may be indirect evidence for a pervasive warm-hot intergalactic medium (WHIM: Davé et al. 2001) that is difficult to detect directly but that may be enough to convert dwarf irregulars into spheroidals.”

All this evidence suggests that ram-pressure stripping is one of the processes that transforms late-type, gas-rich and star-forming galaxies into red and dead S0 and Sph galaxies.

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**Fig. 1.76.** From Mateo (2008), the ages of the youngest stellar populations in dwarf galaxy companions versus Galactocentric or M 31-centric distance $R$. Except for the Magellanic Clouds, all close companions of our Galaxy and of M 31 are spheroidals. Distant companions are irregulars except for three free-flying dSphs (pink points). The Sph/Im transition galaxies mostly lie at intermediate distances.
Galaxy harassment is a dynamical process that should operate wherever objects orbit repeatedly through rapidly varying gravitational potential fields, especially in virialized clusters of galaxies with velocity dispersions that are much larger than the internal velocities of galaxies. It is the cumulative effect of many encounters with other galaxies and with the cluster potential. Simulations show that it strips outer mass, heats disks and promotes gas inflow toward the center that presumably feeds star formation (Moore et al. 1996, 1998; Lake et al. 1998). A variant is tidal stirring of dwarf galaxies on elliptical orbits around our Galaxy or M 31 (Mayer et al. 2001a, b, 2006). Kormendy & Bender concur with the above authors in suggesting that harassment converts late-type disks into spheroidals and more robust, earlier-type spirals into hotter systems that resemble S0s. A benefit of this picture is that inflowing gas can feed star formation; this helps to explain why S0 disks and spheroidals – which must fade substantially after star formations stops – do not have much lower surface brightnesses than current versions of S+Im progenitors (see Ferguson & Binggeli 1994 for a review of this problem). Gravity is not negotiable. Its effects are clean. It is encouraging how many observations can be tied together into a coherent picture if harassment is one of the galaxy transformation processes:

1) Dynamical heating plausibly explains why faint spheroidals are not flat, why many bright spheroidals contain disks (either observed directly when seen edge-on or inferred from their spiral structure), and why the outer parts of our “rosetta stone” galaxies NGC 4762, NGC 4552, NGC 4638 and VCC 2048 are vertically thick whereas their more robust inner parts are flat.

2) Sph and Im galaxies have similar distributions of axial ratios (Ferguson & Sandage 1989; Binggeli & Popescu 1995). The latter authors conclude that “there is no evidence for a difference between the flattening distributions of nucleated dE.N and classical (giant) Es”. However, in my experience, many Sph,N galaxies are flatter than any elliptical. NGC 4637 in Fig. 1.65 and VCC 2048 in Fig. 10 of KB2012 are examples. Ferguson & Sandage note that “The similarity of flattenings of dE (bright, no N) and Im types removes one of the previous objections to the hypothesis that some dwarf ellipticals could be stripped dI’s”. The exact engineering needs further study, but dynamical heating added to the fact that the smallest galaxies are not flat anyway provides a promising way to explain the flattening observations.

3) Intrachannel light is believed to consist of stars that have been stripped by harassment from individual galaxies. In the Virgo cluster, it is irregular and still in the early stages of formation (Mihos et al. 2005, 2009; Arnaboldi et al. 1996, 2002, 2004; Castro-Rodríguez et al. 2009; Arnaboldi & Gerhard 2010). In rich clusters, it is widely observed (Thuan & Kormendy 1977; Adams et al. 2005; Krick & Bernstein 2007; Gonzalez et al. 2007; Okamura 2011). When intrachannel light is very bright, it is called a “cD halo” (Morgan & Lesh 1965;
Oemler 1976; Schombert 1988). These halos are robustly understood to consist of tidally liberated stars and disrupted galaxies (Richstone 1976; Dressler 1979; Kelson et al. 2002). If gravitational harassment can produce all these effects, it is difficult to see how the mere heating of smaller galaxies could be avoided.

4) Kormendy & Bender (2012) suggest that the “new class of dwarfs that are of huge size (10000 pc in diameter in the extreme) and of very low surface brightness of about 25 B mag arcsec$^{-2}$ at the center” discovered by Sandage & Binggeli (1984) are “spheroidals that have been harassed almost to death”.

5) Anisotropic dynamical heating is a natural way to try to explain triaxial and slowly rotating Sphs (e.g., Bender & Nieto 1990). This idea is consistent with the observation that the brightest Sphs are in many cases the most disky and rapidly rotating ones. However, unusually violent encounter histories can allow a small number of Sphs to be anisotropic even at the highest masses.

6) Carefully engineered encounter histories can make Sph galaxies that have kinematically decoupled subsystems, even counterrotation of the harassed outer parts with respect to the inner galaxy (De Rijcke et al. 2004; González-García et al. 2005). Counterrotating systems are seen in VCC 510 (Thomas et al. 2006).

(d) Starvation of continued infall of cold gas from the cosmological structure hierarchy is frequently discussed as an S+Im $\rightarrow$ S0+Sph transformation process (e.g., Larson et al. 1980; Balogh et al. 2000; Bekki et al. 2002; Boselli et al. 2009). Absent such infall, star formation at currently observed rates generally uses up the available gas in a few Gyr (Larson et al. 1980; Boselli et al. 2009). Given the observation that the center of the Virgo cluster and a fortiori the centers of rich clusters of galaxies are dominated by hot gas (e.g., Fig. 1.75), it is difficult to see how starvation can be avoided. These are not environments where low-density cold gas can survive to feed continued accretion onto galaxies for billions of years after the cluster acquires a large velocity dispersion.

Thus many processes (1) may explain the growing dark matter dominance (i.e., baryon deficiency) of lower-mass dwarf galaxies and (2) can potentially transform S+Im galaxies into S0+Sph galaxies. Kormendy & Bender (2012) emphasize that “the relevant question is not ‘Which one of these mechanisms is correct?’ It is ‘How can you stop any of them from happening?’ It seems likely to us that all of the above processes matter.”

In this regard, I conclude by emphasizing the following points.

Most papers (Boselli et al. 2009 is an exception) investigate one process; when they get into trouble explaining some particular observation, they conclude that this process is not the answer. If all above processes happen, then there is more potential to understand all of the diagnostic observations. Theorists like to ask clean questions, investigating one process at a time. There are good reasons for this. But Nature does everything together.
Eventually, we will have to do likewise if we expect to understand galaxy evolution. The hellishly complicated interplay of different processes is a feature, not a bug. We cannot avoid this problem forever.

Second, one observation that is frequently cited to disfavor ram-pressure stripping and strangulation is that bulges are systematically bigger in S0s than in spirals (e.g., Dressler 1980). But (i) small pseudobulges in late-type spirals skew the distribution of S-galaxy bulges to smaller luminosities; if such galaxies are transformed before secular evolution has time to make pseudobulges, the result is a Sph, not an S0. Then it will not be counted among the S0s. Also, (ii) the distribution of S0 bulges is skewed toward high luminosity by the frequent misclassification of the highest ellipticals as S0s (KFCB). This happens because their high Sérsic indices $n \gg 4$ give them a “core-halo” appearance that persuades classifiers to call them S0s. An example is the elliptical galaxy NGC 4406, which is classified S0 by Sandage & Tammann (1981). Similarly, giant ellipticals are commonly classified S0$_3$ when they contain nuclear dust disks; e.g., the elliptical NGC 4459 (KFCB).

(iii) When accurate bulge-disk decompositions are carried out, the folklore that S0 galaxies mostly have large bulges is not confirmed. Among S0s discussed in KFCB and in KB2012, about half have $(P)B/T < 0.5$ and six have $(P)B/T \lesssim 1/3$, the value for the Sb galaxy M 31. Finally, (iv) the distribution of $B/T$ in the progenitor galaxies of any transformation process is a strong function of environment – bulgeless disks are preferentially made in the field, and merger remnants are preferentially made in clusters such as Virgo (Kormendy et al. 2010). So field spirals do not fairly sample the potential progenitors of S0 galaxies in clusters.

Another observation that is frequently cited to disfavor ram-pressure stripping and strangulation is that S0s have higher surface brightnesses than spirals. Disk fading that follows the shutdown of star formation might lead us to expect the opposite effect. But Fig. 1.71 shows little sign of such an effect. Note that the surface brightnesses of both S0 and spiral disks are not corrected for inclination, so they are treated in the same way. However, internal absorption is important in spirals and not in S0s. So internal-absorption-corrected surface brightnesses of spiral galaxy disks would be brighter than those of S0 disks. Also, harassment – like any effect that rearranges angular momentum – persuades some gas to fall toward the center and should increase the surface brightness there via star formation.

Finally, Kormendy & Bender (2012) point out that $S \rightarrow S0$ transformation does not require the removal of all gas nor the quenching of all star formation. Some S0s still contain gas, especially molecular gas near their centers (e.g., Welch & Sage 2003; Sage & Wrobel 1989; Thronson et al. 1989; Devereux...
& Young 1991; Young et al. 1995). These S0s form stars. The Virgo spirals whose outer H\textsc{i} distributions are truncated have normal central molecular gas content (Kenney & Young 1986). We do not need to solve the problem of removing all gas from the deepest parts of galaxy potential wells.

It is clear that much work – much complicated work – is still needed on the messy baryonic physics of galaxy evolution. But I am encouraged to think that the still unknown details of the various transformation processes do not threaten our overall picture that at least some S0s and likely all Sph galaxies are defunct spiral and irregular galaxies.

### 1.7.10 Environmental secular evolution – “An Idea Whose Time Has Come”

Morphological observations such as those encoded in the parallel-sequence classification of Fig. 1.72 lead to the robust conclusion that many S0s are closely related to spiral galaxies and that essentially all Sph galaxies are closely related to the latest-type spirals and irregulars. Figure 1.72 does not directly tell us what that relationship is. However, in recent years, rapidly improving observations of transformation processes in action, including H\textsc{i} and H\textalpha{} tails, relatively recent star formation in dSph galaxies, vertically thick outer disks in interacting S0s and “rosetta stone” galaxies with both S0 and Sph properties, strongly imply that some or all of a collection of environmental processes transform spiral and irregular galaxies into red and dead S0 and spheroidal galaxies. This happens especially in rich clusters, but small galaxies can suffer transformation even in relatively quiescent environments such as the Local Group. Kormendy & Bender (2012) suggest that “environmental secular evolution is An Idea Whose Time Has Come.”

### 1.8 Toward a Comprehensive Picture of Galaxy Formation

This section ties together our standard picture of galaxy formation by hierarchical clustering (lectures by Shlosman, Scoville, Calzetti) with our School’s subject of secular evolution (lectures by Athanassoula, Binney, Buta, Peletier, van Gorkom and me). For pedagogical reasons, it is useful to introduce this standard picture here. Shlosman (2012) provides more detail.

What is at stake for future work? We have a formation paradigm: quantum density fluctuations in non-baryonic dark matter form immediately after the Big Bang and then get stretched by the expansion of the Universe; gravity drives hierarchical clustering that causes the fluctuations to grow, separate, collapse and form galaxy halos; the baryons cool inside the halos to form stars and visible galaxies. Spirals form when halos accrete gas that dissipates and forms disks. Ellipticals form when galaxies collide and merge;
then dynamical violence scrambles disks into ellipsoidal Es. This picture is well supported by theory and observations. What are the remaining puzzles—the cracks in the paradigm? They are short-cuts to progress.

First, what is understood? Hierarchical clustering of dark matter initial density fluctuations is nowadays calculated in exquisite detail (Fig. 1.77). Results are in excellent agreement with observations of large-scale structure.

Our job is illustrated in Fig. 1.78. Hierarchical clustering of dark matter is well understood (background image). More tricky is the physics of baryonic galaxy formation within dark halos. It is possible that all remaining problems with our formation picture on galaxy scales are problems of baryonic physics.

Fig. 1.77. The Millennium Simulation (Springel et al. 2005) is the iconic example of an n-body calculation of the formation of large-scale and galaxy-sized structures via hierarchical clustering of primordial quantum density fluctuations that have been stretched by the expansion of the Universe and increased in contrast by self-gravity.
The good news is that ellipticals are fairly well understood. Simulations of the hierarchical growth of galaxies suggest that they change back and forth between spiral and elliptical, depending on whether their recent history was dominated by a major merger or by cold gas dissipation (Fig. 1.79). Today’s students did not live through the revolution in our understanding that resulted from Toomre’s (1977a) introduction of mergers to our lexicon of galaxy formation. I therefore review this subject briefly.

The first bad news is that we do not know how to form bulgeless galaxies. Continued bulge growth is inherent to the story in Fig. 1.79. Once you have a bulge, you cannot get rid of it. This problem was reviewed in Section 1.6.1.

The other bad news is that galaxy formation by hierarchical clustering of cold dark matter still has problems on the size scales of individual galaxies. Reviews of the subject run the gamut from very optimistic (Primack 2004) to sober (Silk & Mamon 2012) to very pessimistic (Kroupa 2012). This is a sign of a subject in flux—of cracks in the paradigm. These are opportunities.

The comfortable news is that we have a growing understanding of secular evolution in disk galaxies. It happens now in low- and intermediate-density environments. But finding pseudobulges in Virgo S0s shows that it had time to happen even in the progenitor environments of some present-day clusters.
Fig. 1.79. Example of the evolution of a single galaxy by hierarchical clustering (Steinmetz & Navarro 2002, 2003). Colors denote old stars, young stars < 200 Myr old and cold gas (see keys). Scale bars are 5 kpc in all panels. Panel (a) shows the most massive progenitor at $z = 4$; it already contains both old stars and a gas disk. In panel (b), a classical bulge forms in a major merger at $z \approx 3$ and then regrows a disk by later infall of cold gas. Panel (c): at $z = 1.8$, the galaxy looks like an early-type spiral with a dense bulge surrounded by a young disk. Panel (d): At $z \approx 1.6$, tidal forcing by a companion shown in the $z = 1.2$ image triggers a bar. The satellite is accreted at $z = 1.18$, but the bar prominent in the young component survives for several more Gyr. Panel (e): At $z = 0.7$, the galaxy merges with another galaxy that has about half of its mass. The result is an elliptical galaxy at $z = 0.27$. This could accrete more gas and form a Sombrero-galaxy-like system, but it cannot get rid of its large bulge.
1.8.1 Formation of ellipticals by major galaxy mergers

It is hard to describe to today’s students what a revelation it was when Alar Toomre (1977a) presented his hypothesis that all ellipticals are created from progenitor disk galaxies by the dynamical violence of galaxy collisions and mergers. The feeling had been that stars are too small to collide, so interacting galaxies merely pass through each other. We missed two points. First, tidal effects are easily strong enough to scramble cold, rotating disks into dynamically hot ellipticals. Doing this work takes energy out of the orbits and soon causes the galaxies to merge. Second, large and massive halos of dark matter surround visible galaxies and give them much bigger collision cross sections than we thought when we saw only the visible stars. It is no accident that the merger picture became established soon after we realized that dark matter is real (Faber & Gallagher 1979). Mergers-in-progress turn out to explain a whole zoo of previously mysterious peculiar galaxies (e.g., Figs. 1.80–1.82). Toomre’s suggestion that mergers make all ellipticals is, as far as we know, exactly correct. And Toomre’s (1980) additional hypothesis that mergers make classical bulges robustly looks to be exactly correct, too.

Fig. 1.80. Formation of peculiar galaxies such as NGC 4676 (“the mice”) by ongoing gravitational encounters. Such encounters explain most objects in (e.g.) Arp’s (1966) Atlas of Peculiar Galaxies. (top) Hubble Heritage image. (bottom left) Our view of the initial conditions and (bottom right) the moment when the configuration matches the galaxies for an n-body simulation (Barnes 1998, 2004) of two infinitely thin disks (blue particles) embedded in spherical dark halos (red particles).
I was in the audience for Toomre’s (1977a) talk; we all remember it as a historic moment. But not everyone was immediately captured by the new ideas, and I confess that I was a partial agnostic for longer than most. Kormendy (1989) was a late paper that tried to keep merger enthusiasm from getting out of control. Its point is still correct – the sequence of increasing density in smaller ellipticals (Fig. 1.68) is a sequence of increasing dissipation with accompanying starbursts during formation. As emphasized all along by Toomre, merger progenitors generally contain gas; crunching gas likes to make stars, and so star formation is an integral part of spiral-spiral mergers.

By ∼ 1990, we understood that ultraluminous IRAS galaxies (“ULIRGS”) are prototypical dissipative mergers in progress (Joseph & Wright 1985; Sanders et al. 1988a, b; Sanders & Mirabel 1996; Rigopoulou et al. 1999; Dasyra et al. 2006a, b; see Dasyra et al. 2006c and KFCB Section 12.3.2 for reviews). Figure 1.81 shows the most famous example. Dust-shrouded starbursts generally dominate the far-infrared luminosity $L > 10^{12} L_\odot$ (see Joseph 1999 and KFCB for reviews). Their structural parameters are consistent with the E fundamental plane (Kormendy & Sanders 1992; Doyon et al. 1994; Genzel et al. 2001; Tacconi et al. 2002; Veilleux et al. 2006; Dasyra et al. 2006a, b). Stellar velocity dispersions $\sigma \approx 100$ to 230 km s$^{-1}$ show that local ULIRGs are making moderate-luminosity ellipticals; i.e., the disky-coreless side of the E–E dichotomy in Figs. 1.4 and 1.60 (Genzel et al. 2001; Tacconi et al. 2002; Dasyra et al. 2006a, b; c).

Fig. 1.81. Arp 220, the prototypical Ultraluminous Infrared Galaxy, an elliptical galaxy being formed by a dissipative merger accompanied by a dust-shrouded starburst. At left is a Hubble Heritage image. The HST NICMOS JHK image at right reveals two remnant nuclei separated by $0.98 \approx 360$ pc (Scoville et al. 1998).
Central to the rapid acceptance of the merger picture was the extensive observational evidence for mergers in progress that was published by François Schweizer (e.g., 1978, 1980, 1982, 1987, 1996). Figure 1.82 shows the particularly convincing example if NGC 7252 (the “atoms for peace” galaxy). It has both diagnostic tidal tails and “ripples” or “shells” in the light distribution that trace edge-on caustics of wrapped former disks. Shells, too, became standard merger diagnostics (Malin & Carter 1980, 1983; Schweizer & Seitzer 1988). Shells are seen in absorption as well as in stars; an example of the explanation of a previously mysterious peculiar galaxy as an S0 that contains an accreted and now phase-wrapped dust disk is NGC 4753 (Steiman-Cameron et al. 1992). The correlation that stronger fine structure such as shells is seen in ellipticals with younger stellar populations (bluer colors and stronger Hβ absorption lines) further supported the merger picture and filled in the evolution time sequence between mergers in progress and old, completely relaxed and phase-mixed ellipticals (Carter et al. 1988;}

![NGC 7252](image)

Fig. 1.82. NGC 7252 is another prototypical merger-in progress that is making an elliptical galaxy (Schweizer 1982). Two tidal tails that point in roughly opposite directions and that have opposite velocity differences with respect to the systemic velocity are the simplest diagnostic signature of a merger in progress (see the seminal paper by Toomre & Toomre 1972). The essential point is that dynamical clocks run most slowly at the largest radii, so remnant tidal tails persist long after the main bodies of interacting galaxies have merged. For HI observations and n-body models of NGC 7252, see Hibbard et al. (1994, 1995, 1996).
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Schweizer et al. 1990; Schweizer & Seitzer 1992). Compelling further support was provided both by detailed HI observations (e.g., Hibbard et al. 1994, 1995, 1996, 2001a, b – see http://www.nrao.edu/astrores/HIroguess) and especially by n-body simulations (the master of the art is Josh Barnes 1988, 1989, 1992). Simulations further confirmed that mergers dump huge amounts of gas to galaxy centers, thereby feeding starbursts (e.g., Barnes & Hernquist 1991, 1992, 1996; Mihos & Hernquist 1994; Hopkins et al. 2009a). By the time of the reviews of Schweizer (1990, 1998); Barnes & Hernquist (1992), Kennicutt (1998c) and Barnes (1998), the merger revolution in our understanding of elliptical galaxies was a “done deal”.

A variant of the merger picture involves the observation that many high-z galaxies are dominated by $10^8 - 10^9$ $M_\odot$, kpc-size star forming clumps (e.g., Elmegreen et al. 2005, 2007, 2008a, 2009a, b; Bournaud et al. 2007; Genzel et al. 2008; Förster Schreiber et al. 2009;Tacconi et al. 2010). Bournaud’s galaxy UDF 1668 (Fig. 1.83) is remarkably similar to the initial conditions used by van Albada (1982) to simulate the collapse of lumpy initial conditions. He showed (Fig. 1.83 here) that relatively gentle collapses produce Sérsic-function profiles with $n \approx 2 - 4$ like those in real classical bulges (e.g., Fisher & Drory 2008). This is confirmed in modern n-body merger simulations (e.g., Hopkins et al. 2009a).

Fig. 1.83. Mergers of two galaxies that consist mostly of stars make Sérsic (1968) function remnants with indices $n \sim 2 - 4$. An early illustration of this is van Albada (1982), whose initial conditions look remarkably similar to the clumpy high-z galaxy UDF 1666 studied by Bournaud et al. (2007). It is an example of the clump instability picture discussed by Elmegreen et al. (2008b). Van Albada’s initial conditions were parameterized by the ratio of twice the total kinetic energy to the negative of the potential energy. In virial equilibrium, $2T/W = 1$. For smaller values, van Albada found that gentle collapses ($2T/W < 0.5$) make Sérsic profiles with $n < 4$, whereas violent collapses ($2T/W \approx 0.2$) make $n \approx 4$. This is a sign that the clumps discussed by Elmegreen et al. (2008b) merge to make classical bulges.
Elmegreen et al. (2008b) model gas-rich galaxy disks in the early Universe and find that they violently form clumps like those observed (Fig. 1.84). The clumps quickly merge and make a high-Sérsic-index bulge. It rotates slowly. Rotation velocities decrease with increasing distance from the disk plane. So these are classical bulges, and this is a variant on the merger picture. From many colorful conversations with Allan Sandage, I suspect that he would have welcomed this “ELS with lumps” picture (ELS = Eggen et al. 1962).

Fig. 1.84. A variant of the merger picture involves high-z disks that are unstable to the formation of large clumps which quickly merge to form a classical bulge. It has ellipsoidal (not cylindrical) rotation (bottom). From Elmegreen et al. (2008b).
1.8.2 Mergers and secular evolution both happen in a hierarchically clustering Universe

“It is impossible to remove the problem of galaxy formation from its cosmological context of hierarchical clustering” (Jones 1992). Begun in papers like White & Rees (1978), our picture of hierarchical clustering has reached a remarkable level of sophistication. The Millennium Simulation is one example from a vast literature. I want to emphasize again that the merger formation of elliptical galaxies that was discussed in Section 1.8.1, the secular evolution of disk galaxies that was discussed in Sections 1.2 – 1.6, and the environmental secular evolution that was discussed in Section 1.7 all happen within the cosmological context of hierarchical clustering. Much work remains to be done in connecting the story of galaxy formation on the kpc scales of most studies of individual galaxies with the Mpc scales where n-body dark matter simulations are at their best. Current work is dominated by the complicated physics of baryons, including the effects of reionization, dissipation, star formation, energy feedback and active galactic nuclei. We like to think that galaxies are mature objects and that our job is to study galaxy evolution to see how they got that way. But $\sim 2/3$ of the baryons in the Universe do not yet live in galaxies or have not yet cooled and formed stars (e.g., Fukugita et al. 1998; Davé et al. 2001; Read & Trentham 2005). Galaxy formation is much less “finished” than we like to think! Our job is far from finished, too. For all of us students of galaxies, this is good news.

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Note added November 2013: This review was finished and submitted in mid-June 2012. The astro-ph version is essentially identical to the published paper except for differences in spelling (British there and American here) and for improvements here in a few figures. The present version remains up to date except for one important new paper by Sellwood (2013). This is a broad review of the theory of “Secular Evolution in Disk Galaxies” that overlaps some of the present subjects but that also discusses many additional fundamental topics. It is an important complement to the present paper and to Kormendy & Kennicutt (2004).

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