Observation of the quantum valley Hall state in ballistic graphene superlattices

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In graphene superlattices, bulk topological currents can lead to long-range charge-neutral flow and nonlocal resistance near Dirac points. A ballistic version of these phenomena has never been explored. We report transport properties of ballistic graphene superlattices. This allows us to study and exploit giant nonlocal resistances with a large valley Hall angle without a magnetic field. In a low-temperature regime, a crossover occurs toward a new state of matter, referred to as a quantum valley Hall state (qVHS), which is an analog of the quantum Hall state without a magnetic field. Furthermore, a nonlocal resistance plateau, implying rigidity of the qVHS, emerges as a function of magnetic field, and this plateau collapses, which is considered a manifestation of valley/pseudospin magnetism.

INTRODUCTION
The Berry phase (1) is considered an important tool for developing spintronics and valleytronics (2, 3) because it allows control over spin/valley degrees of freedom instead of charge degree of freedom. A particularly challenging problem is engineering the Berry phase through the bulk topological current, which is a descendant of the quantum Hall effect (QHE) (4–6) but can occur even in the absence of a magnetic field. Recent discoveries of the quantum anomalous Hall effect (7), which breaks time-reversal symmetry, and quantum spin Hall/topological insulators (8) are also variants of the QHE in terms of topology. Valley current in graphene (9–13) offers promise for realizing the bulk topological current in a (2+1)-dimensional Dirac fermion without a magnetic field (6). Furthermore, valleytronics (2) are expected to fulfill the requirements of the next generation of electronic devices, such as the valley field effect transistor (11, 14).

In monolayer graphene, which exhibits a Dirac-type relativistic energy dispersion (that is, a Dirac cone), one can induce broken inversion symmetry by placing graphene on a hexagonal boron nitride (hBN) substrate with a precise alignment angle near 0°, whereby a long-length moiré pattern appears between the graphene and the hBN lattice because of the 1.8% lattice mismatch between the graphene and the hBN (15–17). The moiré superlattice also induces a fractal energy spectrum under a magnetic field, which is known as Hofstadter’s butterfly (15–18). In these systems with broken inversion symmetry, the valley current can be generated and detected via the valley Hall effect (VHE), even in the absence of a magnetic field: the VHE is induced by the accumulated Berry curvature near the apex of the Dirac cone (that is, the hot spot) and is associated with the topological current (9–13). The valley Hall current has not yet been explored near the ballistic regime, and the longitudinal conductivity has always dominated the valley Hall conductivity, implying a small valley Hall angle that veils the nature of the VHE. Observing a coherent neutral long-ranged valley current through an all-electrical method requires nonlocal resistance measurements from a geometry smaller than or comparable to the mean free path (11).

RESULTS AND DISCUSSION
Toward this objective, we fabricated hBN/graphene/hBN heterostructures with one-dimensional Cr/Au contacts, as shown in Fig. 1 (A and B). Sharp increases in the longitudinal resistivity (ρxx) at backgate voltages Vg of approximately 0 and –21 V correspond to a Dirac point (DP) and a secondary DP (SDP), respectively (Fig. 1C). The emergence of the SDP is a consequence of band modulation due to the moiré superlattice resulting from the alignment of graphene and hBN crystals, indicated by the angle θ ~ 0°, which yields energy gaps at the DP and the SDP. With current and voltage terminals of I: 62, V: 53, Fig. 1C also shows the nonlocal resistance Rnl at zero magnetic field. Near the energy bandgap, the hot spots in the graphene due to the hBN, even without a magnetic field, give rise to the transverse bulk topological current, that is, the VHE, which in turn produces a chemical potential difference between terminals 5 and 3, that is, the inverse VHE. We observe a larger Rnl of the same order as h/2e2 (~12.9 kilohms, where h is the Planck constant and e is the elementary charge) at the SDP. Such a large Rnl cannot be explained by the ohmic contribution, assuming diffusive transport with a maximum of 1.5 ohms (see the Supplementary Materials). By contrast, the value of Rnl at the DP of approximately 1 kilohm is of the same order as that observed in the previous work (11), and the nonlocal transport at the DP is basically consistent with previous results, implying that bulk valley Hall current emerges and results in nonlocal transport in our device (11). Furthermore, essentially the same phenomena occur at the SDP in the high-temperature regime (see the Supplementary Materials), which implies bulk topological current. However, in the low-temperature regime, the value of Rnl at the SDP is even larger than that of ρxx. In this regime, Rnl is within the quantum limit; that is, it equals the quantized value h/2e2 (13) apart from a prefactor of order 1. Furthermore, our results indicate that the Rnl itself takes a quantum-limited value and exhibits rigidity under certain conditions, such as a magnetic field, as discussed below. We note that there is an influence of thermal cycles and charge impurities (see the Supplementary Materials). In particular, starting gate voltage fixes the disorder caused by charge impurities. The large disorder effects veil
the giant nonlocal resistance, and that is what happened in previous studies (11).

Figure 1D shows a logarithmic-scale intensity map of the longitudinal conductivity ($\sigma_{xx}$) as a function of $V_g$ and a magnetic field $B$ (applied perpendicular to the substrate). We observed the QHE of single-layer graphene near the DP and a Landau-fan diagram of Hofstadter’s butterfly. From the periodicity of $1/B$, we estimated the alignment angle between the graphene and hBN, $\theta = 0.7$ to 0.8°, and we estimated the moiré superlattice size to be approximately 11 nm. The mobilities in the sample were up to 250,000 cm$^2$/Vs near the DP and 180,000 cm$^2$/Vs near the SDP at 1.5 K (see the Supplementary Materials). We estimated the mean free path $L_F$ to be 1 to 2 $\mu$m, which is comparable to the sample geometry.

In small magnetic fields, we observed transverse resistance oscillation, as shown in Fig. 1E; we believe this originated from the so-called transverse magnetic focusing (TMF) effect (19). In a ballistic sample, the trajectory of a charged carrier is bent by Lorentz force under a magnetic field, and an injected carrier is focused by the cyclotron motion on the transverse electrode, causing the TMF effect. In our sample, we estimated the distance between the electrodes to be 2.8 $\mu$m, based on $B_F = (2h k_F i / e L_{eff}) = (2h(\pi n)^{1/2} / e L_{eff})$, where $B_F$ is the focusing magnetic field, $h$ is the reduced Planck constant given by $h/2\pi$, $k_F$ is the Fermi wave number, $i$ is the number of reflections at the edge; this estimated distance is consistent with the nominal center-to-center length of 2.5 $\mu$m. The TMF is apparent only when the carriers are not scattered while traveling from the injection electrode 6 to the detection electrode 5, thereby achieving the ballistic transport between the electrodes. All of these results confirm the ballistic character of our sample (see the Supplementary Materials).

We estimated the experimental energy gap based on the Arrhenius plots: $1/\rho_{xx} \propto \exp(-E_g/2 k_BT)$, where $E_g$ is the gap energy (=2$\Delta$) and $k_T$ is Boltzmann’s constant, as shown in Fig. 1F. The gaps were estimated as $E_g = 2\Delta$, being 32 and 14 meV at the DP and SDP, respectively, by linear fitting in the high-temperature region. The gap at the SDP is consistent with that predicted by Moon and Koshino (18), although the gap at the DP is much larger than the predicted value of 2 meV. Woods et al. (20) have observed gap openings of approximately 30 meV at the DP in commensurate graphene/hBN superlattices, which is consistent with our results. However, this point remains controversial, and Wang et al. (21) have reported recent data from angle-resolved photoemission spectroscopy that support different results. We consider that this point is closely connected to the crossover conditions of the transport picture discussed below. A comment is in order on the different scenarios between the DP and SDP. As discussed below, giant nonlocal resistance occurs only at the SDP in our sample.
A hypothesis is that it is attributable to the larger energy gap in the SDP. However, this point is controversial and contradicts our Arrhenius plots. It is also possible that the gap by the Arrhenius plot is different from the energy gap in the band structure. Because the DP shows a longer mean free path than the SDP, another scenario is that ballistic modes can contribute a negative nonlocal resistance, as discussed by Mayorov et al. (22). In contrast to the high-temperature observations, in the lower temperature region, the change of the slope from the Arrhenius form indicates that the carrier transport is dominated by variable range hopping inside the gap due to charge inhomogeneity.

We then investigated the resistances with different terminal configurations in our six-terminal device, and all of the quantum-limited resistance results consistently support the emergence of the quantum valley Hall state (qVHS). In the QHE, we have proposed two different pictures an edge picture and a bulk picture. Although it is unsettled which is valid, it is notable that each gives internally consistent results.

In our system, the total Hall conductance, indicated by the topological number (5, 6), vanishes, and there is no a priori reason for edge states to exist. However, recent experimental and theoretical results support the existence of edge states, although their detailed character is determined by their fine electronic structures, which remain to be resolved (23, 24). A mechanism driven by the edge states predicts the giant nonlocal resistance in the quantum limit. Therefore, we calculated the resistances of different configurations using the Landauer-Büttiker formalism with multiterminal samples (25, 26) based on a minimal model in which two edge states for two valleys propagate in opposite directions along the edge, with only nonvanishing elements of the transmission matrix ($T$) between terminals given by $T_{j+1,j} = T_{j+1,j} = 1$, where $j$ is an integer, which corresponds to the terminal numbers. The current-voltage relationship is given by $I_j = e^2/h \sum_k (T_{jk} V_k - T_{kj} V_j)$, where $I_0$ is the current flowing out of the $k$-th electrode, $V_j$ is the voltage on the $j$-th electrode, and $T_{jk}$ is the transmission probability from the $j$-th to $k$-th electrode. Solving this equation with an experimental input on $I$ and $V$, we get $I$-$V$ relations and resistances. Figure 2 shows the resistances with different terminal configurations of a six-terminal sample. On the basis of the minimal model, we calculated the longitudinal resistance $R_{xx}$ of $(I: 14, V: 65)$ as $h/2e^2$, as shown by the dotted lines in Fig. 2B. We calculated the theoretical $R_{ad}$ of $(I: 61, V: 53)$, $(I: 61, V: 54)$, and $(I: 61, V: 43)$ to be $1/3$, $1/6$, and $1/9$ (unit, $h/e^2$), respectively, as shown by the dotted lines in Fig. 2C. Similarly, the $R_{ad}$ of $(I: 62, V: 53)$ and $(I: 62, V: 43)$ were $1/3$ and $1/9$ (unit, $h/e^2$), respectively, as shown by the dotted lines in Fig. 2D. Although the discrepancies between the theoretical predictions may originate from charge impurities (see the Supplementary Materials) and/or the intervalley scattering on the disordered edge with possible dephasing, each $R_{ad}$ is consistent with the theoretical value apart from fluctuations. Furthermore, the spiking behavior of the resistance is reproducible, and we attribute this effect to mesoscopic fluctuation, which can be viewed as a fingerprint of our device and gives an origin of departure from the quantized theoretical values. Their peaks are classified into two values in Fig. 2C and D, and the ratio of the two experimental $R_{ad}$ values is close to $1/3$, which implies the existence of channels, as proposed in the minimal edge-state model. Overall, all the longitudinal resistances and resistances with nonlocal geometries show a consistent picture. This is in analogy with the QHE, that is, the qVHS in our device. Although all of the $R_{ad}$ peak shapes were asymmetric and cubic scaling did not fit them at low temperatures, the peak shapes became smooth and fit cubic scaling at higher temperatures (see the Supplementary Materials) (11), part of which is also suggested by recent theoretical simulations (24).

Because the qVHS occurs in zero magnetic field with time-reversal symmetry due to the presence of hot spots, its collapse should be connected to the reconstruction of the electronic structure due to a magnetic field through the valley Zeeman energy ($V_{ZE}$), $E_{VZ} = 1/2g^*\mu_B B$, where $g^*$ is an effective $g$-factor and $\mu_B$ is the Bohr magneton. Koshino and Ando (27) give the theoretical $g^*$ of a single valley as $m^* = \Delta/\nu^2$, $g^* = 2 m^*/\nu^2$, where $m^*$ is the effective mass, $\nu$ is the free-electron mass, and $v$ is the Fermi velocity. In our sample, the $g^*$ was theoretically calculated to be approximately 2500 by using the following parameters: $\Delta = 7$ meV, which is obtained by the Arrhenius plots of the SDP in Fig. 1F, and $v = 1.2 \times 10^6$ m/s, which is determined by Shubnikov-de Haas (SDH) oscillations (see the Supplementary Materials). This $g^*$ value of the pseudospin is 1250 times larger than that of a free electron’s spin. Figure 3B maps the $R_{sd}$ as a function of $V_g$ and $B$, showing a robust plateau around the point of zero magnetic field from $B = -0.1$ to $+0.1$ T. This result indicates a rigid qVHS when $\Delta > 2E_{VZ}$ (Fig. 3A). After the breakdown of the plateau when $\Delta < 2E_{VZ}$ (Fig. 3A), $R_{ad}$ decreases with increasing magnetic field, approaching zero around 0.8 T (Fig. 3, B and C) and starting to increase in $B > 0.8$ T due to the occurrence of the quantum Hall states (Fig. 3B). The breakdown of the plateau indicates that nonlocal transport is no longer possible because of the breakdown of the hot spots. Actually, the value of $V_{ZE}$ at 0.1 T with $g^* = 2500$ is $E_{VZ} = 7$ meV, which agrees with the result for $\Delta = 7$ meV of the SDP. Because the model presented in the study of Koshino and Ando (27) is minimal, a prefactor of order 1 can occur in the valley Zeeman term, which is fixed by the details of the electronic structure at the SDP. In this scenario, in the low–magnetic field regime, we
assume that Landau levels are broadened/overlapped because of thermal effects and disorder. Actually, around the collapse of the plateau, we observe no Landau level and cannot detect the SdH signal (see the Supplementary Materials). We observed the clear Landau fan only above near 0.5 T in our sample, as shown in Fig. 1D. This nonlocal magnetoresistance behavior contrasts with the previously reported simple monotonic increase in $R_{nl}$ (11, 28). Our sample, which exhibited lower mobility in several thermal cycles and showed $R_{nl}$ of ~1 kilohm, did not show such a clear decrease in the magnetic fields (see the Supplementary Materials), and only samples within the quantum limit with high $R_{nl}$ showed the same behavior. By contrast, $R_{nl}$ in a high–magnetic field regime exhibits a butterfly pattern (see the Supplementary Materials), which should have a QHE origin, and the SdH-type signal does not occur in the low–magnetic field regime (29). As previously reported (28), with a high magnetic field, spin and energy flow should also affect $R_{nl}$ (see the Supplementary Materials).

In summary, we measured nonlocal transport of the ballistic graphene/hBN aligned superlattices with one-dimensional edge contacts. Giant $R_{nl}$ with the order of quantum resistance was observed even at zero magnetic field, indicating the occurrence of the qVHS. Therefore, we conclude that the mechanism driven by the edge states is a more likely scenario for the giant nonlocal resistance in the quantum limit than a bulk-related interpretation. Furthermore, the $R_{nl}$ plateau, which implies a rigidity of the qVHS, emerged as a function of magnetic field, and we also observed its collapse, which we considered a manifestation of valley/pseudospin magnetism. Such an unconventional magnetism should have the potential for engineering the energy-band structure even with a weak magnetic field as well as for spintronics applications.

MATERIALS AND METHODS
Sample fabrication
First, hBN flakes were exfoliated by applying Scotch tape to a poly-methyl methacrylate (PMMA)/polyacrylic acid (PAA)/Si substrate, and then, the substrate was floated on a water surface to isolate the PMMA layer from the Si substrate by dissolving the PAA layer in water. The 16-nm-thick hBN flake was then aligned with a graphene flake exfoliated onto a Si substrate with 90-nm-thick SiO$_2$ using a homemade atomic layer transfer system (30). The graphene and hBN were carefully aligned along their long edges, and the graphene remained in contact with the hBN flake, forming a graphene/hBN stack. This stack was then aligned with a 20-nm-thick hBN flake that also remained attached to the stack. After removing the PMMA with acetone, we obtained an hBN/graphene/hBN stack on a SiO$_2$/Si substrate. The sample was annealed at 300°C for 30 min in an Ar/H$_2$ atmosphere before atomic force microscopy (AFM) imaging. The AFM image is shown in fig. S1. The Hall bar geometries are indicated by the black lines. We carefully defined the Hall bar geometry so as to include as few bubbles as possible in the channel region, and the sample was then etched into the Hall bar geometry by reactive ion etching using SF$_6$. The one-dimensional Cr/Au contacts (31) were deposited by electron beam (EB) evaporation followed by EB lithography with a 125-kV acceleration voltage.

Fig. 3. Nonlocal magnetoresistance in graphene superlattices. (A) Schematics of the measurement setup (left) and the energy band structure in magnetic fields (right), which show how the band structure is reconstructed when the magnetic field is included. In the band structure, we do not take into account the role of orbital magnetism for simplicity, which leads to broadened Landau bands overlapped due to disorder and finite-temperature effects. (B) $R_{nl}$ (at 1.5 K) is mapped as a function of $V_g$ and $B$ as shown in (C). (C) $R_{nl}$ versus $B$ for five $V_g$’s near the SDP, marked with the same color as arrows on the top of (B). Black arrows show the regime where the energy gap with hot spots is kept, linking to the white dashed lines in (B).
Measurement setup
All of the measurements were performed using both four-terminal dc and low-frequency lock-in techniques (around 17 Hz and ac excitation current of 1 to 10 nA), both of which give consistent results, and measurements were performed in variable temperature cryostats (two types of cryostats were used: base temperatures were 5 and 1.5 K, respectively) with superconducting magnets. All of the experimental data presented in this paper were obtained from the same sample with different cooling cycles from room temperature to below 10 K.

SUPPLEMENTARY MATERIALS
Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/4/5/eaaq0194/DC1

Supplementary Text
fig. S1. False-color AFM image of our hBN/graphene/hBN stack.
fig. S2. Influence of thermal cycles and charge impurities on our device.
fig. S3. Shubnikov-de Haas oscillation and estimation of the Fermi velocity.
fig. S4. Magnetotransport in our ballistic hBN/graphene/hBN sample.
fig. S5. Temperature dependence of the nonlocal resistance Rnl.
fig. S6. Magnetic field dependence of the Rnl.

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