Spin-orbit-controlled metal–insulator transition in Sr$_2$IrO$_4$

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In the context of correlated insulators, where electron-electron interactions ($U$) drive the localization of charge carriers, the metal–insulator transition is described as either bandwidth- or filling-controlled. Motivated by the challenge of the insulating phase in Sr$_2$IrO$_4$, a new class of correlated insulators has been proposed, in which spin-orbit coupling (SOC) is believed to renormalize the bandwidth of the half-filled $\lambda$ = 1/2 doublet, allowing a modest $U$ to induce a charge-localized phase$^{1-3}$. Although this framework has been tacitly assumed, a thorough characterization of the ground state has been elusive$^{4,5}$. Furthermore, direct evidence for the role of SOC in stabilizing the insulting state has not been established, because previous attempts at revealing the role of SOC$^6$ have been hindered by concurrently occurring changes to the filling$^{8-10}$. We overcome this challenge by employing multiple substituents that introduce well-defined changes to the signatures of SOC and carrier concentration in the electronic structure, as well as a new methodology that allows us to monitor SOC directly. Specifically, we study Sr$_{2-x}$Ir$_x$O$_4$ ($T$ = Ru, Rh) by angle-resolved photoemission spectroscopy, combined with ab initio and supercell tight-binding calculations. This allows us to distinguish relativistic and filling effects, thereby establishing conclusively the central role of SOC in stabilizing the insulting state of Sr$_2$IrO$_4$. Most importantly, we estimate the critical value for SOC in this system to be $\lambda = 0.42 \pm 0.01$eV, and provide the first demonstration of a spin-orbit-controlled metal–insulator transition.

The familiar tools of chemical doping and pressure have provided straightforward access to both a filling-controlled (FC) and bandwidth-controlled (BC) metal–insulator transition (MIT) in conventional correlated insulators. In an effort to unveil the role of spin–orbit coupling (SOC) in the insulating behaviour of Sr$_2$IrO$_4$, and whether it can indeed drive a MIT, we have attempted to controllably dilute SOC in the valence electronic structure by substituting Ir ($\lambda_{\text{SOC}}$≈0.4 eV; refs. $^{11-13}$) with Ru and Rh ($\lambda_{\text{SOC}}$≈0.19 eV; refs. $^{14-16}$). Although these substituents have similar values of $\lambda_{\text{SOC}}$ and are both 4d ions with comparable values for $U$ (refs. $^{17,18}$) and ionic radii$^{19}$, they are otherwise distinct: Ru has one less electron than Rh, and is therefore associated with a markedly larger impurity potential. We will show through supercell tight-binding (TB) model calculations that this leads to a pronounced contrast in the consequences of Rh and Ru substitution: the larger impurity potential associated with Ru precludes a significant reduction of the valence SOC. By comparison, Rh is electronically more compatible with Ir, facilitating a successful dilution of SOC. We measure this evolution directly, through orbital mixing imbued by SOC, manifest experimentally in the photoemission dipole matrix elements. To comprehend all aspects of the MIT observed here for both Rh and Ru substitution, we consider individually the effects of filling (Fig. 1), correlations/ bandwidth (Fig. 2) and SOC (Figs. 3 and 4), ultimately concluding that the transition in Sr$_{2-x}$Ir$_x$O$_4$ is a spin–orbit-controlled MIT.

Having highlighted the three relevant aspects of the MIT, we begin our discussion by showcasing the changes both substituents introduce to the electronic structure of Sr$_2$IrO$_4$, as measured by angle-resolved photoemission spectroscopy (ARPES). Figure 1a–d summarizes ARPES spectra for $x = 0$; $x_{\text{Rh}} = 0.22$; and $x_{\text{Ru}} = 0.20, 0.40$. As reported previously$^{1}$, the pristine sample supports an energy gap, with a band maximum at $X$ at a binding energy of around $E_{\text{F}} = 0.25$eV. When substituting Rh, a pseudo-gapped metallic state forms for concentrations $x \geq 0.13$ (refs. $^{19-21}$). This is exemplified by our $x_{\text{Rh}} = 0.22$ data, shown in Fig. 1b,c. At comparable values of $x_{\text{Rh}}$, the system remains insulating (see $x_{\text{Rh}} = 0.20$ in Fig. 1d), and only when going as high as $x_{\text{Rh}} = 0.40$ (Fig. 1c,f) do we find that the MIT has been traversed$^{20-22}$, consistent with transport measurements$^{23}$.

Within the metallic phase, the Fermi surface volume provides a direct measure of the hole doping introduced by the impurity atoms. We report a Brillouin zone coverage of 16% and 46% for Rh and Ru, respectively, corresponding to a nominal doping of 0.16 holes (at $x_{\text{Rh}} = 0.22$) and 0.46 holes (at $x_{\text{Rh}} = 0.40$) per formula unit. To within our level of certainty, each impurity atom then contributes approximately one hole carrier, with Ru perhaps contributing a somewhat larger number than Rh. This observation runs contrary to the expectations for a FC transition: despite contributing at least as many holes as Rh, the MIT critical concentration required for Ru is roughly double that of Rh. This precludes a transition described in terms of filling, despite earlier reports to the contrary$^{10}$. An explanation in terms of the modification to the crystal structure upon Ru substitution can be equally excluded: the smaller ionic radius of Ru causes a minimal reduction of octahedral distortions ($12^\circ$ to $10^\circ$) up to the concentrations used in our study$^{24}$. More importantly, such a reduction of distortions would increase the bandwidth$^{25}$, and the expected trend would be opposite to our observations.

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Alternatively, due to the presence of a sizable impurity potential for Ru (as discussed below), disorder effects could also be considered; however, recent studies regarding disorder in Mott systems point out that such effects would also push the critical concentration to lower values\(^{32}\), precipitating once again an earlier onset of metallicity in the Ru-substituted compounds.

Looking beyond the disparate critical concentrations associated with Ru and Rh substitution, analysis of the ARPES spectral features allows for a more thorough comparison of these materials to be made. The selected energy distribution curves (EDCs) cut through the valence band maximum for each doping in Fig. 2a (Ru) and 2b (Rh), reflecting the evolution of each material across the MIT. This coincides with a definitive Fermi level crossing in the EDCs of Fig. 2a,b, from which we can infer the critical concentrations to be \(x_{Ru} = 0.13 \pm 0.03\) and \(x_{Rh} = 0.30 \pm 0.10\) (this matches previous photoemission work on the Rh-substituted compound\(^{11-12}\); as for the Ru-substituted samples, those have not previously been studied by photoemission). As the interpretation of EDC lineshape is non-trivial\(^{16}\), we turn to an analysis of momentum distribution curves (MDCs) for a more quantitative analysis of the evolution of correlation effects. The MDC linewidth is directly related to the state lifetime and, by extension, to both electronic interactions and disorder\(^{25-26}\). Two representative MDCs are shown in Fig. 2c for \(x_{Ru} = 0.22\) and \(x_{Rh} = 0.40\). Widths from these, and other MDCs along the dispersion, are summarized in Fig. 2d. As can be inferred by a comparison of data from 20 K and 150 K, correlations—rather than thermal broadening—are the limiting factor in determining the MDC linewidth. Consideration of both \(x_{Ru} = 0.40\) and \(x_{Rh} = 0.22\) reveals remarkably similar interaction effects in the two compounds, despite their significant differences in composition and disorder. In addition, while spectral broadening at high binding energies precludes a precise evaluation of the bandwidth, we estimate the latter to be constant to within 10\% over the range of Rh/Ru concentrations considered.

We have thus determined that while doping effects are comparable for Ru and Rh, similar correlated metallic phases are observed at very different concentrations. To rectify this apparent contradiction, one must consider the context of the present MIT: it has been proposed that the correlated insulating phase in Sr\(_2\)IrO\(_4\) is stabilized by the strong SOC. This motivates consideration of the role SOC plays in the MIT for both Ru- and Rh-substituted compounds. The low-energy influence of SOC can be characterized by an effective value in the valence band, determined by the hybridization between atomic species as demonstrated in refs.\(^{30,31}\). This effect could cause a reduction of SOC effects in the valence band as a function of (Ru,Rh) substitution. We find the reduction of SOC to be strongly dependent on the presence of an impurity potential, which limits hybridization of host and impurity states, ultimately curtailing the dilution of SOC effects (see Supplementary Information). In light of the reported electronic phase separation for the Ru compound\(^{11-13}\), this suggests that such dilution of SOC may be more effective for Rh, providing a natural explanation for their disparate critical concentration in substituted Sr\(_2\)IrO\(_4\) compounds.

The model presented in the Supplementary Information to illustrate the mechanism of spin–orbit mixing can be made quantitative for the Ru/Rh iridates through consideration of impurity-substituted supercell models. Using density functional theory (DFT), at \(x = 0.25\) substitution, Fig. 3a shows good overlap between the Rh and Ir projected density of states (DOS). This can be compared against the same scenario for Ru in Fig. 3b, where the substituent DOS is found to align poorly with Ir. Such an offset, observed most clearly through consideration of the centre of mass of the Ru-projected DOS, has been reported previously for similar substitutions\(^{25-26}\). Calculating the band's centre of mass in terms of the projected densities of states for both, we find an impurity potential for Ru of 0.3 eV, which is close to the number found in refs.\(^{34,35}\) (0.25 eV) and agrees with Wannier calculations (0.2 eV) performed on the same supercells. This establishes a reasonable starting point from which we can explore the influence of doping on SOC effects in more detail. This was carried out through the development of a supercell TB model. We expanded a single iridium TB Hamiltonian (see Supplementary Information) to a 64-site supercell, randomly substituting a fraction \(x\) of sites with an impurity atom. For the sake of simplicity, the impurities are assumed to differ from Ir only in their \(\lambda_{SOC}\) (0.19 eV for both Ru and Rh, 0.45 for Ir), and on-site potential (0.0 eV for Rh and Ir, 0.25–0.05 eV for Ru). Similarly, octahedral distortions and electron correlations are neglected to better illustrate the energy shift of the \(j^{\text{eff}}\) states. We used the unfolding method\(^{26-31}\) to project bands into the original Brillouin zone. By averaging the resulting spectral function over 200 random
configurations, we observe a smooth evolution of effective SOC in this system, which depends strongly on the impurity potential.

The results are summarized in Fig. 3, with a representative unfolded spectrum \((x_{\text{Rh}} = 0.20)\) as plotted in Fig. 3c. We investigated the level spacing at \(k_{\text{app}} = \left( \frac{3\pi}{4}, 0 \right) \) where \(k\) is the Ir–Ir distance, as indicated by the vertical arrow in Fig. 3c. This marks the point at which we will later present experimental data. The change in splitting is seen clearly in Fig. 3d, where we plot a series of EDCs at \(k_{\text{app}}\) for models with a non-zero on-site impurity potential (Ru, red) and for those without (Rh, black). This doping dependence is summarized in Fig. 3d. The right vertical axis reflects the splitting observed at \(k_{\text{app}}\) and the left the value of \(\lambda_{\text{SOC}}\), that would produce the corresponding splitting in a model without substitutions (that is, for an overall uniform value of \(\lambda_{\text{SOC}}\)). This second axis serves to illustrate the effective SOC caused by substitution of Ir with Rh and Ru. From the progression in Fig. 3e it is evident that Rh should dilute SOC more efficiently than Ru: the black markers trace the interpolation between the values of Ir and Rh, indicated by the grey line. Meanwhile, the modelled impurity potential for Ru (0.25±0.05 eV) prevents successful dilution of SOC. The results in Fig. 3e suggest that the different critical concentrations for the two substrates can be attributed to a common parameter: a value for SOC of \(\lambda_{\text{c}} \approx 0.42 \pm 0.01\) (blue shaded area, Fig. 3e) yields critical concentrations \((x_{\text{Rh}} \approx 0.15\) and \(x_{\text{Ru}} \approx 0.3\)) that fit well with our experimental observations. The theoretical results presented in ref. 40 suggest that SOC in SrIrO\(_4\) is only marginally above the threshold for the insulating state, and that such a small change could drive the transition. The dilution of SOC is therefore found to provide a compelling theoretical picture of the transition.

Having demonstrated this evolution of SOC via substitution and its ability to provide a natural explanation for the transition in SrIr\(_{1-x}\)Ru\(_x\)O\(_4\), we aimed to substantiate these predictions experimentally. To establish a convenient metric for SOC, we leveraged the symmetry constraints of the photoemission matrix element. Dipole selection rules allow transitions from only certain orbitals: because \(d_{xz}\) (\(d_{xy}\)) is even (odd) in the experimental scattering plane, states composed of this cubic harmonic are only observable with \(\pi\) (\(\sigma\)) polarization. As SOC mixes these orbitals into linear combinations prescribed by the \(j_{\text{pl}}\) construction, we quantified SOC by comparing the ratio of even/odd states at strategically chosen points in the Brillouin zone where these symmetry-based selection rules are most well defined. In the absence of SOC, the state along \(\Gamma-X\), (defined in Fig. 4) in SrIrO\(_4\) would be of pure \(dx_z^2\) character: any photoemission from this state using \(\sigma\) polarization is forbidden. SOC would then lift this selection rule, allowing the \(dx_z^2\) state to be observed with \(\pi\) polarization. This ratio of even/odd states at \(\pi\) polarization is a natural measure of SOC.

Motivated by the supercell calculations, we investigated the progression of \(M_{\text{eff}}^x / M_{\text{eff}}^y\) as a function of SOC, demonstrating the possibility for a direct measure of \(\lambda_{\text{SOC}}\) via ARPES.

**Fig. 3 | Reduction of SOC through supercell analysis.** a, b, Plot of an analysis of the impurity potentials of Rh (a) and Ru (b) in Sr\(_2\)IrO\(_4\), calculated by density functional theory. The grey background represents the total density of states (DOS), normalized by the number of transition metal (TM) sites. The black curves show the Ir projected DOS (pDOS) per Ir ion in the 25% substituted calculation in states per eV (st eV\(^{-1}\)), while the orange and green coloured curves reflect the pDOS per substituent ion for Rh and Ru, respectively. The arrows indicate the centre of mass for the projected bands.

c, Supercell calculated spectrum for \(x_{\text{Rh}} = 0.2\) obtained after unfolding. The effective splitting is indicated in red. d, Cuts (EDCs) for different concentrations of dopants at the position of the red arrow in c (\(k_{\text{app}} = \left( \frac{3\pi}{4}, 0 \right) \)). The substituted atoms have different SOC and on-site energy. We use \(\lambda_{\text{SOC}} = 0.19\) eV and \(\varepsilon_i = 0.0\) eV for Rh (black) and \(\lambda_{\text{SOC}} = 0.19\) eV and \(\varepsilon_i = 0.25\) eV for Ru (red). e, Progression of the splitting between the outermost peaks for simulations in d for Rh (black markers) and Ru (red markers). For Rh, a linear interpolation is plotted between the end members of the phase diagram. For Ru, the resulting range of splitting for \(\varepsilon_i = 0.25 \pm 0.05\) is indicated by red shaded rectangles. The critical concentrations obtained from our measurements are indicated by the black (Rh) and red (Ru) vertical shaded areas. The blue shaded area indicates the inferred \(\lambda_{\text{c}} = 0.42 \pm 0.01\).
light. To compare the different samples, we consider constant energy maps at the energy that places the state of interest at  $k_{\text{exp}} = \left( \frac{x_{\text{SOC}}}{x_{\text{exp}}}, 0 \right)$.

Integrating and dividing the ARPES intensity within the indicated regions of Fig. 4a–d yields the ratio $M_{\text{ex}}^c / M_{\text{ex}}^d$. We can proceed to make a quantitative connection with an effective SOC strength by plotting the experimental data points alongside the simulated curve in Fig. 4e. The latter has been normalized to the experimental data for pristine Sr$_2$IrO$_4$, allowing for an effective $\lambda_{\text{SOC}}$ strength to be extracted for the Rh/Ru-substituted samples. This analysis yields $\lambda_{\text{SOC}}$ values of 0.443 ($x_{\text{Rh}} = 0.10$), 0.424 ($x_{\text{Rh}} = 0.10$) and 0.408 eV ($x_{\text{Rh}} = 0.16$). A connection to the supercell calculations can be made through these $\lambda_{\text{SOC}}$ values: the associated impurity concentrations in Fig. 3e agree remarkably well with the actual experimental values shown in a–d. Error bars are calculated from the standard deviation over the integrated range in energy. The top axis in e indicates the substitution required to produce the SOC value on the bottom axis, predicted by the supercell calculations in Fig. 3e. The dashed lines indicate the expected effective SOC from the nominal concentrations of the Rh-substituted samples.

**Online content**

Any methods, additional references, Nature Research reporting summaries, source data, extended data, supplementary information, acknowledgements, peer review information; details of author contributions and competing interests; and statements of data and code availability are available at https://doi.org/10.1038/s41567-019-0750-y.

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Methods
Single crystals of Sr$_2$Ir$_{1-x}$Rh$_x$O$_4$ were grown with nominal concentrations of $x_{\text{Rh}} = 0.0, 0.10, 0.16, 0.22$ and measured with electron probe microanalysis to be within 0.01 of their nominal concentration. Crystals of Sr$_2$Ir$_{1-x}$Rh$_x$O$_4$ were grown with nominal concentrations of $x_{\text{Rh}} = 0.10, 0.20, 0.40$. Measurements were carried out at the SIS beamline at the Swiss Lightsource (Rh-substituted samples) and at the Merlin beamline at the Advanced Lightsource (Rh- and Ru-substituted samples). All measurements were performed on freshly cleaved surfaces, where the pressure during measurement and cleavage was always lower than $3.3 \times 10^{-10}$ mbar. Measurements used for inference of spin–orbit coupling values were performed with 64 eV photons, using light polarized perpendicular to the analyser slit direction ($\sigma^-$ polarization). The rotation axis of the manipulator for acquisition of the Fermi surface was parallel to the slit direction. The sample was mounted such that the Ir–O bonds ($\Gamma$–$X$) were aligned to this axis of rotation. Temperatures were chosen to be as low as possible while mitigating the effects of charging and are reported in the figure captions. A tight-binding model was constructed from a Wannier orbital calculation using the Wannier90 package\textsuperscript{50}. The Wannier90 calculations were performed on results from DFT calculations done with the Wien2k package\textsuperscript{51,52}. Supercell and matrix element calculations were performed using the chinook package\textsuperscript{53}. Further details are provided in the Supplementary Information. The DOS calculations presented in Fig. 3 were performed with the Wien2k package\textsuperscript{51,52}. Supercell and matrix element calculations were performed using the chinook package\textsuperscript{53}. Further details are provided in the Supplementary Information. The DOS calculations presented in Fig. 3 were performed with the Wien2k package. The supercell configuration assumed a single layer with eight TM ions per unit cell. The presented results at $x = 0.25$ are similar to those found for $x = 0.125$ and $x = 0.5$.

Data availability
The data represented in Figs. 2 and 3 are available as source data in Supplementary Data 2 and 3. All other data that support the plots within this paper and other findings of this study are available from the corresponding author upon reasonable request.

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Author contributions
B.Z. and A.D. conceived the experiment. B.Z., E.R. and M.M. collected the experimental data. N.X., M.S. and J.D.D. provided experimental support. G.C., S.C., K.U., J.B., H.T. and B.J.K. grew the single crystals. B.Z. and R.P.D. performed data analysis. B.Z. performed simulations, with input from R.P.D., I.S.E. and A.D. B.Z., R.P.D. and A.D. wrote the manuscript, with input from all authors. I.S.E. and A.D. supervised the project. A.D. was responsible for overall project direction, planning and management.

Competing interests
The authors declare no competing interests.

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