Hybrid quantum gate and entanglement between a “stationary” photonic qubit and a flying optical state via a giant cross Kerr nonlinear effect

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Quantum information processing with hybrid protocols making use of discrete- and continuous-variable currently attracts of great interest because of its promising applications in scalable quantum computer and distant quantum network. By inducing a giant cross-Kerr nonlinearity between two cavities, we propose a general protocol for hybrid quantum gate and quantum entanglement with high fidelity between a stationary, discrete photonic qubit and a flying photonic state. Interestingly, our protocol can be used to conduct a controlled-Z quantum gate between a stationary microwave photon stored in a slowly-decaying microwave cavity and a flying optical photon, and therefore enable to build quantum network for distant superconducting quantum circuits.

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Introduction.— Hybrid quantum information processing (QIP) with the stationary discrete qubit and a flying photon can enable scalable quantum computation, distributed quantum information processing and distant quantum network [1,2]. The hybrid entanglement, as the heart of hybrid QIP, between a discrete single-photon qubit and a coherent-state field has only been demonstrated very recently by using heralded frequency conversion [3]. An entangling hybrid quantum gate being able to control the quantum state of a flying photon with a stationary discrete qubit in the quantum regime is highly demanded because it allows the linking of distant computation node to build a quantum network. The development of such quantum gate is “a pressing challenge” [4]. The hybrid quantum gate between a trapped atom and a flying photon has been reported in waveguide quantum electrodynamics (wQED) systems [5,6] and cavity quantum electrodynamics (cQED) systems [2,7,8]. However, a protocol for the hybrid quantum gate between a discrete photonic qubit and a flying photon is yet to be proposed.

Superconducting quantum circuits working in the microwave regime are building blocks for the most promising quantum computer [9] but can only communicate via their mutual interaction with microwave (mw) photons. Microwave photons, unlike optical photons, cannot be efficiently transmitted over long distances. To circumvent this challenge, schemes converting the quantum information between the mw and optical (mw-o) regimes have been proposed by using optomechanics [10] or spins [11]. The frequency conversion of classical photonic information with mechanical oscillator has been realized [12], but its quantum counterpart is lack. Very recently, wQED systems are exploited to create hybrid entanglement between a superconducting qubit and a flying photon [13]. However, hybrid quantum gate bridging the mw regime and the optical regime is lack of protocol.

The controlled-Z quantum gate is one of universal entangling quantum gate [7,14] and can be easily transferred to a controlled-NOT quantum gate [4]. It has been supposed to be realized in a cross-Kerr nonlinear optical medium. The giant optical Kerr and cross Kerr nonlinearity has been predicted theoretically in N-type atoms [15] and been observed in many experiments [16]. The cross Kerr nonlinearity has been widely considered as a toolkit for the phase-flip quantum gate between two flying photons for decades [17], but its validity for QIP of continuous variables is now questioned at the fundamental level [18,19]. In this letter, with a giant cross Kerr nonlinearity between a “good” cavity (g-cavity) and an one-side optical “bad” cavity (b-cavity) created by an ensemble of N-type atoms, we present a protocol for a hybrid controlled-Z quantum gate between a discrete photon stored in the slowly-decaying g-cavity and a flying photon encoded in polarization. The phase of flying photonic state reflected off the b-cavity is conditionally controlled by the quantum state of the g-cavity due to the giant cross Kerr nonlinearity. Interestingly, our protocol can conduct a hybrid quantum gate between a discrete mw photon and a flying optical photon and therefore allows the linking of distant superconducting quantum circuits. It can also generate the hybrid entanglement between a “stationary” discrete photonic qubit and a coherent-state field.

System.— Now we begin the discussion of our idea and model with the description of our setup depicted in Fig. 1. We present a general protocol for a hybrid controlled-Z quantum gate between a flying optical photon reflected off a “bad” optical cavity (cyan) and a “stationary” photon stored in a “good” cavity (purple) with a high quality (Q). Figure 1(a) shows the setup for the mw-o controlled-Z quantum gate between a “stationary” mw photon stored in a 3D mw cavity and a flying optical photon. To do this, we make two tiny holes on the metal wall of mw cavity and put two highly reflective mirrors to form a Fabry-Perot cavity. An ensemble of NV centers in nanodiamond is inserted in the common region of the mw cavity and the Fabry-Perot optical cavity. This optical cavity supports two degenerate modes with left-circular (or \( \sigma_- \)) polarization (LCP) and right-circular (or \( \sigma_+ \)) polarization (RCP). The mw cavity mode couples to the transition of \( |s\rangle \to |A_2, m_i = 1\rangle \). It can be quickly initialized with a superconducting qubit [20]. The RCP(LCP) mode couples the transition between \( |A_2, m_i = -1\rangle \) and the optical excited state, \( |E, S\rangle \). A coherent laser beam...
drives the transition between $|\beta\rangle$ and $|\gamma\rangle$, which correspond to the states $|1\rangle, |2\rangle, |3\rangle, |4\rangle$ for Cs atoms. The state $|2\rangle$ decays to the states $|1\rangle$ and $|3\rangle$ with rates $\gamma_1$ and $\gamma_2$, respectively, while the state $|4\rangle$ decays to $|3\rangle$ with rates $\Gamma_1$ and $\Gamma_2$. The b-cavity (g-cavity) mode couples the transition $|2\rangle \leftrightarrow |1\rangle$ (|4\rangle \leftrightarrow |3\rangle) with a detuning $\delta$ ($\Delta$) and at a rate $g_0$ ($g_1$). A classical laser field $\Omega$ drives the transition $|2\rangle \leftrightarrow |3\rangle$ with a detuning $\delta$. Under the condition of $\Omega \gg g_0$, the atoms are dominantly trapped in $|1\rangle$. Then the Hamiltonian describing the interaction between the atoms and the cavities takes the form

$$H_C = \Delta\sigma_{44} + \delta\sigma_{22} + \Omega_g(\sigma_{23} + \sigma_{32}) + \eta\sigma_{21}\sigma_{12} + g_0\sigma_{43}\sigma_{12} + g_1\sigma_{42}\sigma_{12} + g_0\sigma_{21}\sigma_{12}.$$

Applying the perturbation theory and adiabatically eliminating the atoms, we obtain a rough estimation of the cross third-order susceptibility given by

$$\chi^{(3)}_{\text{cross}} \approx \frac{-2N\sigma_1d_{23}^2d_{23}^2}{\hbar^3\epsilon_0\nu} \frac{1}{(\Delta - i\Gamma_1 - i\gamma_1)(\Omega^2 + \Delta^2 + \Delta^2 + \gamma_1^2)},$$

where $d_{23}$ is the dipole moment of optical (mw) transition of $|2\rangle \leftrightarrow |1\rangle$ (|4\rangle \leftrightarrow |3\rangle), $\epsilon_0$ is the vacuum permittivity and $V_a$ is the volume of the nanodiamond or the whole atomic cloud. The photon-photon interaction strength can be obtained from $\Re[\chi^{(3)}_{\text{cross}}]$.

$$\eta \approx -\frac{2N\sigma_1d_{23}^2d_{23}^2}{\Delta^2 + (1 + \gamma_1)^2(\Omega^2 + \Delta^2 + \Delta^2)}.$$

The driving of the cavities can be described by $H_D = i\sqrt{2}\kappa\sigma_0(\beta_1\sigma_2 + \beta_2\sigma_1)$, where $\sigma_0$ and $\beta_1$ are the input driving the optical cavity and mw cavity, respectively. Thus we have the effective Hamiltonian for the cavity modes with the optical external input centered at frequency $\omega_{in}$ only

$$H_{\text{eff}} = (\Delta_{in} - i\kappa_1\sigma_0\sigma_2 + \Delta_{in}\sigma_1) + i\eta\sigma_0\sigma_1 + g_1\sigma_0\sigma_1 + g_0\sigma_0\sigma_1 + g_0\sigma_0\sigma_1 + g_1\sigma_0\sigma_1,$$

where $\Delta_{in}$ is the driving of the cavities.

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**FIG. 1.** (Color online) Schematic diagram of setup controlling the reflection ($\hat{a}_{in}$) of an optical input $a_{in}$ with another cavity mode $\hat{a}_\mu$. (a) An ensemble of NV centers in nanodiamond couples simultaneously to a slowly-decaying three-dimension (3D) mw cavity and a fast-decaying optical Fabry-Perot cavity. (b) A cloud of N-type cold atoms interacts with two optical Fabry-Perot cavities. The ensemble of atom/NV centers induces a giant cross Kerr nonlinearity between two cavities.

**FIG. 2.** (Color online) Level diagram describing the interaction between mw ($g_1$) and photons ($g_0$) and an ensemble of NV centers in the nanodiamond. A classical laser field drives the transition between states $|2\rangle$ and $|3\rangle$ with a rate of $\Omega$. N-type atom has four levels, $|j\rangle$ with $j \in \{1, 2, 3, 4\}$, which correspond to the states $|1\rangle, |2\rangle, |3\rangle, |4\rangle$. The state $|2\rangle$ decays to the states $|1\rangle$ and $|3\rangle$ with rates $\gamma_1$ and $\gamma_2$, respectively, while the state $|4\rangle$ decays to $|3\rangle$ with rates $\Gamma_1$ and $\Gamma_2$. The b-cavity (g-cavity) mode couples the transition $|2\rangle \leftrightarrow |1\rangle$ (|4\rangle \leftrightarrow |3\rangle) with a detuning $\delta$ ($\Delta$) and at a rate $g_0$ ($g_1$). A classical laser field $\Omega$ drives the transition $|2\rangle \leftrightarrow |3\rangle$ with a detuning $\delta$. Under the condition of $\Omega \gg g_0$, the atoms are dominantly trapped in $|1\rangle$. Then the Hamiltonian describing the interaction between the atoms and the cavities takes the form

$$H_C = \Delta\sigma_{44} + \delta\sigma_{22} + \Omega_g(\sigma_{23} + \sigma_{32}) + \eta\sigma_{21}\sigma_{12} + g_0\sigma_{43}\sigma_{12} + g_1\sigma_{42}\sigma_{12} + g_0\sigma_{21}\sigma_{12} + g_1\sigma_{21}\sigma_{12}. \quad (1)$$

Applying the perturbation theory and adiabatically eliminating the atoms, we obtain a rough estimation of the cross third-order susceptibility given by

$$\chi^{(3)}_{\text{cross}} \approx \frac{-2N\sigma_1d_{23}^2d_{23}^2}{\hbar^3\epsilon_0\nu} \frac{1}{(\Delta - i\Gamma_1 - i\gamma_1)(\Omega^2 + \Delta^2 + \Delta^2 + \gamma_1^2)}, \quad (2)$$

where $d_{23}$ is the dipole moment of optical (mw) transition of $|2\rangle \leftrightarrow |1\rangle$ (|4\rangle \leftrightarrow |3\rangle), $\epsilon_0$ is the vacuum permittivity and $V_a$ is the volume of the nanodiamond or the whole atomic cloud. The photon-photon interaction strength can be obtained from $\Re[\chi^{(3)}_{\text{cross}}]$.

$$\eta \approx -\frac{2N\sigma_1d_{23}^2d_{23}^2}{\Delta^2 + (1 + \gamma_1)^2(\Omega^2 + \Delta^2 + \Delta^2)}.$$

The driving of the cavities can be described by $H_D = i\sqrt{2}\kappa\sigma_0(\beta_1\sigma_2 + \beta_2\sigma_1)$, where $\sigma_0$ and $\beta_1$ are the input driving the optical cavity and mw cavity, respectively. Thus we have the effective Hamiltonian for the cavity modes with the optical external input centered at frequency $\omega_{in}$ only

$$H_{\text{eff}} = (\Delta_{in} - i\kappa_1\sigma_0\sigma_2 + \Delta_{in}\sigma_1) + i\eta\sigma_0\sigma_1 + g_1\sigma_0\sigma_1 + g_0\sigma_0\sigma_1 + g_0\sigma_0\sigma_1 + g_1\sigma_0\sigma_1,$$

where $\Delta_{in}$ is the driving of the cavities.
where \( \Delta_{in} = \omega_b - \omega_a \) and \( [\hat{a}_{in}(\omega'_a), \hat{a}_{in}^\dagger(\omega_a)] = \delta(\omega'_a - \omega_a) \).

For our purpose, here external driving, \( \beta_{in} \), of the g-cavity is tuned off. In contrast to the RCP input, the LCP incident photon is scattered by an empty cavity, i.e., \( \eta = 0 \).

Now we can discuss our hybrid quantum gate based on the effective Hamiltonian \( H_{eff} \). Using the input-output relation for the reflection of optical cavity \([25][26]\), the amplitude of reflection takes

\[
 r_s(\omega_a, \hat{N}_b) = \frac{-i(\omega_a - \omega_b + \eta_s\hat{N}_b) + \kappa_{eo} - \kappa_{o}}{i(\omega_a - \omega_b + \eta_s\hat{N}_b) + \kappa_{eo} + \kappa_{o}} , \tag{5}
\]

with \( \hat{N}_b = \hat{a}_b^\dagger \hat{a}_b, \eta_s = 0 \) for the LCP incident and \( \eta_s = \eta \) for the RCP one. The annihilation operator of the reflected field is given by \( \hat{a}_s = r_s(\omega_a, \hat{N}_b) \hat{a}_b \). If \( \omega_a - \omega_b = \eta_s \) and \( |\eta_s| \gg \kappa_{o} \), then we have \( r_s(\omega_a, \hat{N}_b) \approx -\epsilon e^{i\kappa_{eo}}\hat{N}_b \) and \( r_s(\omega_a) \approx 1 \). It means the LCP incident photon is always reflected and suffers a \( \pi \) phase shift, whereas the reflection of the RCP input is controlled by the state of the quantum cavity. If a continuous-wave (cw) RCP photon enters the b-cavity, it is reflected off the cavity without phase shift when \( \eta_s = 1 \). When \( \eta_s = 0 \), the RCP input photon is directly reflected off the cavity with a \( \pi \) phase shift. As a result, a cw RCP(LCP) incident photon in state \( |\omega\rangle = \hat{a}_b^\dagger(\omega)|\omega\rangle \), where \(|\omega\rangle \) is the vacuum state in open space, after reflected off the g-cavity, becomes \( r_s(\omega_a, \hat{N}_b)\omega \) \( \r(\omega, \hat{N}_b)|\omega\rangle \). The b-cavity mode \( \hat{a}_o \) is related to the incident mode \( \hat{a}_{in} \) via

\[
 \hat{a}_o(\omega_a, \hat{N}_b) = \frac{2\kappa_{eo}}{i(\omega_a - \omega_b + \eta_s\hat{N}_b) + \kappa_{eo} + \kappa_{o}} \hat{a}_{in}(\omega_a) . \tag{6}
\]

Here we choose \( \hat{a}_o \) and \( \hat{a}_{in} \) to be dimensionless operators. The photon-photon interaction \( H_I \) also induces phase shift \( \theta \) between the states \( |0\rangle \) and \( |1\rangle \) of the g-cavity mode, taking \( \theta = \eta_s \int (\hat{a}_o^\dagger(\tau)\hat{a}_o(\tau)) d\tau = \eta_s \int (\hat{a}_b^\dagger(\omega)\hat{a}_o(\omega))d\omega \).

Next we go to evaluate the performance of the hybrid quantum gate and the generated entanglement for a Gaussian-pulsed input \( s(t) = \frac{1}{\sqrt{2\pi}\sigma_\omega} e^{-t^2/2\sigma_t^2} \) on the input mirror of the b-cavity with a duration of \( \sigma_T = 5\kappa_{oo} \) corresponding to a spectrum \( f(\omega) = \frac{1}{\sqrt{2\pi}\sigma_\omega} e^{-(\omega-\omega_0)^2/2\sigma_\omega^2} \) and \( \sigma_\omega = 1/\sigma_T \).

Controlled-Z quantum gate for polarization qubit.– Here we evaluate the hybrid quantum gate which can impose a \( \pi \) phase flip on a flying qubit encoded in polarization with the quantum state of the g-cavity mode. We use the notations \( |R(\omega)\rangle = \hat{a}_b^\dagger(\omega)|\omega\rangle \) and \( |L(\omega)\rangle = \hat{a}_b(\omega)|\omega\rangle \) for indicating an incident photon with frequency \( \omega \) and RCP or LCP, respectively. The Gaussian input photon with spectrum \( f(\omega) \) encoded in the RCP(LCP) can be denoted as \( |R\rangle = \int f(\omega)|R(\omega)\rangle d\omega \) \( \{L\rangle = \int f(\omega)|L(\omega)\rangle d\omega \) \([5][14]\). Initialy, the g-cavity is prepared in \( |\alpha\rangle \), and the incident photon in \( |\alpha\rangle L + |\beta\rangle R \). Ideally, the controlled-Z gate converts the initial states in the way of \( |0, L\rangle \rightarrow |0, L\rangle, |0, R\rangle \rightarrow |0, R\rangle, |1, L\rangle \rightarrow |1, L\rangle \) and \( |1, R\rangle \rightarrow |1, R\rangle \).

This process defines a target unitary, \( U = U_{ target} = |0, L\rangle(0, L) - |0, R\rangle(0, R) - |1, L\rangle(1, L) + |1, R\rangle(1, R) \).

For the incident pulse with the spectrum \( f(\omega) \), our system scatters the states as \( |0, L\rangle \rightarrow |0\rangle \otimes \int f(\omega)|R_s(\omega, 0)|L(\omega)\rangle d\omega, |0, R\rangle \rightarrow |0\rangle \otimes \int f(\omega)|R_s(\omega, 0)|L(\omega)\rangle d\omega, |1, L\rangle \rightarrow |1\rangle \otimes \int f(\omega)|R_s(\omega, 0)|L(\omega)\rangle d\omega, |1, R\rangle \rightarrow e^{i\theta}|1\rangle \otimes \int f(\omega)|R_s(\omega, 0)|L(\omega)\rangle d\omega + e^{i\theta}|1\rangle \otimes \int f(\omega)|R_s(\omega, 0)|L(\omega)\rangle d\omega \).

Its
the generated state into one of Kitten states (\(|\pm\rangle\)). The solid (dashed) lines are for 4\(\eta/2\kappa_0 = 2.2\) (4\(\eta/2\kappa_0 = 4.2\)).

fidelity can be evaluated as \(F_{\text{ent}} = |\langle\Psi_\text{final}|\Psi_{\text{gen}}\rangle|^2 = \int |f(\omega)|^2 \left[(\alpha^2/\kappa_0)\Psi_\text{gen}^*(\omega,0)\alpha(\omega) + (\alpha(\omega))\Psi_\text{gen}^*(\omega,1)\alpha(\omega))|d\omega|^2\right]

We take \(\alpha = 1\). The phase shift roughly approximates to 4\(\eta|\alpha|^2/\kappa_0\) if the bandwidth of the incident photon is much smaller than \(\kappa_0\) and \(\kappa_0 \approx \kappa_0\). As shown in Fig. 4(a), the fidelity oscillates as the external coupling rate \(\kappa_0\) and the photon-photon interaction strength \(\eta\) increase because the phase shift \(\theta\) is mostly a linear function of \(\kappa_0/\kappa_0\) and \(\eta\). Figure 4(a) shows the dependence of the fidelity on the external coupling. We take 4\(\eta|\alpha|^2/\kappa_0 = 3 \times 2\pi\). When \(\kappa_0 = 0.83\kappa_0\), \(\theta/2\pi = 2.03\) and the fidelity is \(F_{\text{ent}} = 0.83\). While the fidelity decreases to \(F_{\text{ent}} \approx 0.61\) when \(\kappa_0 = 0.99\kappa_0\) yielding \(\theta/2\pi \approx 2.88\). The larger discrepancy of \(\theta\) and \(2\pi\) when \(\kappa_0 = 0.99\kappa_0\) causes the decrease of the fidelity in comparison with the case of \(\kappa_0 = 0.83\kappa_0\). Similar influence of the phase shift \(\theta\) can be seen in Fig. 4(b) in which we take \(\kappa_0 = 0.99\kappa_0\). It can be seen that the fidelity oscillates fast as a cosine function as \(\theta/2\pi \sim 4\eta|\alpha|^2/\kappa_0\). By carefully choosing 4\(\eta|\alpha|^2/2\kappa_0 = (3.19, 4.21, 5.24)\) leading to \(\theta/2\pi \sim (3.07, 4.05, 5.04)\), we obtain \(F_{\text{ent}} = (0.86, 0.89, 0.91)\). Note that the optimal photon-photon interaction and the achieved fidelity are also dependent on the mean photon number, \(|\alpha|^2\), of the incident field state. If we quickly correct the phase shift on the g-cavity mode by inducing a dispersive interaction with the initializing qubit/atoms after the quantum gate operation, we may achieve a high fidelity robust against the variety of the external coupling and the photon-photon interaction. Obviously, measuring the g-cavity mode in the basis of \(|\pm\rangle = (|0\rangle + e^{i\alpha}|1\rangle)/\sqrt{2}\) will project the generated state into one of Kitten states \(|\pm(\pm)\rangle\) with the same fidelity but 50% probability for each.

Feasibility.— As mentioned in model section, the g-cavity with a decay rate of \(\kappa_0 = 10^{-3}\kappa_0\) can be considered as “stationary” and its loss is negligible during quantum gate operation. Therefore, the realization of the proposed quantum gate crucially relies on the available photon-photon interaction in both the mw-o and the o-o quantum gates. In both versions, we can easily engineer the system that \(\Omega_c = 10\gamma_0\). For the mw-o version, the g-cavity can be initialized with a superconducting transmon \([31]\). We use an ensemble of NV centers in nanodiamond with a number density \(\rho_N = 5 \times 10^{18} \text{ cm}^{-3}\) \([32]\) to induce the giant cross-Kerr nonlinearity between the mw and optical cavities. We take \(\Delta/2\pi \sim 0.1 \text{ MHz} \Rightarrow (\Gamma_1 + \gamma_2) (\Gamma_1 \approx \gamma_2 \approx 2\pi \times 3 \text{ kHz} \approx 1 \text{ MHz})\), \(g_\mu/2\pi \sim 1 \text{ MHz}\). A nanodiamond with a volume of \(\sim 0.7 \times 10^{-8} \text{ cm}^{-3}\) including \(3.5 \times 10^{12}\) NV centers can generate a photon-photon interaction of 4\(\eta|\alpha|^2/2\kappa_0 = 2.2\). With such intercavity nonlinearity the fidelity and distance of the quantum gate can be \(F_G = 0.98\) and \(D_G = 0.006\). To conduct the o-o quantum gate, a cloud of cold Cs atoms is applied to generate the photon-photon interaction. A second cloud of cold atoms is applied to initialize the g-cavity. Typically, we have \(\gamma_3 \approx 2\pi \times 5 \text{ MHz} \Rightarrow \Gamma_1 \approx 0.006\). The single-atom coupling can be \(g_\mu/2\pi \approx 2\pi \times 0.5 \text{ MHz}\) or even stronger \([23]\). We take \(\Delta/2\pi \approx 2 \times 50 \text{ MHz}\). Thus, A cloud of \(\sim 6900\) atoms allows to obtain \(F_G = 0.98\) and \(D_G = 0.006\). Note that we can tune the classical driving to adjust the photon-photon interaction and then achieve the optimal fidelity. It is also noticeable that we can prepare the g-cavity in the superposition state of \(|\alpha_0|0\rangle + \beta_0|N_0\rangle\) with \(N_0 > 1\) to guarantee a high fidelity quantum gate when \(\eta\) is small \([31]\).

**Conclusion.**— With a giant intercavity cross-Kerr nonlinearity we have proposed a general protocol for a controlled-Z quantum nonlinear interaction between the mw-o quantum gate entangling a discrete photonic qubit and a flying photon. In particular, our protocol can be applied to conduct a hybrid quantum gate between the mw regime and the optical regime: controlling the phase of the reflected flying optical qubit encoded in polarizations via the quantum state of the mw photon stored in the 3D mw cavity. Such hybrid mw-o quantum gate is an important resource for building a scalable long-distance quantum network for superconducting quantum circuits. Moreover, our protocol allows to create hybrid entanglement between a discrete photonic qubit and a flying coherent-state field, and to generate a flying state via measurements.

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