Common Frequency Hopping Spread Spectrum (FHSS) will be upgraded by us in our quantum harmonics system to randomly propagate atomic particles by photonically switching from one signal carrier (quantum tube, see our quantum harmonics paper) to other quantum channels in thereby achieved dynamic equilibrium beyond chaotic interference. Fermi-Dirac distribution function (see ref. 2) and (electrovacuum) solutions of the Einstein (Einstein-Maxwell) field equations are applicable. Same concept can be applied in our remote quantum loops space display system (see fig. 1) to constitute space computes and TVs (see fig. 2). We accordingly introduce here the notions of rotating quantum spring (fig. 1) to create a quantum ball, as in a ball lightning:

Fig1. Pictured quantum loops with integrated central quantum spring define the contours of their rotating plain as in a ball lightning (ref. 1) to create a 3D space plasma imagery display (fig. 2) in self-generated and contained e.m. field, as in a ball lighting (see ref. 3 Wand 4) to be activated by a tunable pulse laser via quantum prism or membrane.

We show here (fig. 2) the around the axis rotating central quantum spring, which sustains the quantum ball structure:

Fig2. Quantum spring
Ill.1. Ball lightning

Fig2. 3D quantum space display as in a ball lightning in ref. 1.

Ill.2. Ball lightning structure

Ill.3. Electron-ionic model of ball lightning
The electron-ionic model of ball lightning was represented by Sergey G. Fedosin, a physicist and the philosopher from Perm, Russia, and Sergey A. Kim, from Perm state university, in a number of works.

In this model, ball lightning is a cluster of the very hot ionized air with the positive charge in general, whose shell consists of the rapidly revolving electrons with the total current up to \(1.4 \times 10^5\) A. Ball lightning as whole is supported by the balance of the electromagnetic forces, which act between the charges. Positive ions inside the lightning are distributed freely as a result of the spherical symmetry, and attract to themselves the electrons of shell, retaining them from the dispersion.

According to the model the ball lightning is formed from two close branches of a linear lightning at the time of termination of current in the main channel with the subsequent closure of branches in a current ring.

Equatorial cross-section model of ball lightning as a distinct ring on the current sheet spheroidal shape. \(R\) - radius of rotation of ions in the equilibrium shell around the magnetic field with induction \(B\), \(r\) - radius of the outer electron shell.

Electronic currents in the shell create strong magnetic field inside the lightning. These currents are perpendicular to rotational axis, the diameter of rotation decreases to the poles, where magnetic field grows. This retains positive ions from the dispersion along the rotational axis due to the effect of magnetic bottle. Basic magnetic field inside the lighting is directed along the rotational axis. I.e., ions can move along the axis along the lines of magnetic field. From other side, the ions revolve in the circle perpendicularly to axis under the action of Lorentz force with respect to their thermal velocity. As a result at a certain distance from the axis of lightning appears the intersection of two ion flows, which is observed as the luminous shells inside the lightning. Emission from the shells appears from friction and recombination of the being intersected ion flows.

**Conclusion**

Theory predicts from the first principles the maximum diameter of ball lightning 34 cm. With the larger size the summary charge of lightning, which has positive sign, grows to the value of \(10^{-5}\) C and appears the electrical breakdown of air near the lightning. The energy of the lightning in this case reaches 10.6 kJ, the current in the shell \(1.4 \times 10^5\) A, the internal magnetic field of 0.5 Tesla.

Because of its charge ball lightning does not simply float under the action of the force of Archimedes, but it is retained by electric force from clouds and the induced charge on the Earth. The formula for the maximum radius of ball lightning has the form:

\[
r = \frac{mc^2}{qE_0},
\]
Derivation of the Fermi-Dirac Distribution Function

We start from a series of possible energies, labeled $E_i$. At each energy we can have $g_i$ possible states and the number of states that are occupied equals $g_i f_i$, where $f_i$ is the probability of occupying a state at energy $E_i$.

The number of possible ways - called configurations - to fit $g_i f_i$ electrons in $g_i$ states, given the restriction that only one electron can occupy each state, equals:

$$W_i = \frac{g_i^!}{(g_i - g_i f_i)^! g_i f_i^!}$$

This equation is obtained by numbering the individual states and exchanging the states rather than the electrons. This yields a total number of $g_i^!$ possible configurations. However, since the empty states are all identical, we need to divide by the number of permutations between the empty states, as all permutations can not be distinguished and can therefore only be counted once. In addition, all the filled states are indistinguishable from each other, so we need to divide also by all permutations between the filled states, namely $g_i f_i^!$.

The number of possible ways to fit the electrons in the number of available states is called the multiplicity function.

The multiplicity function for the whole system is the product of the multiplicity functions for each energy $E_i$

$$W = \prod_i W_i = \prod_i \frac{g_i^!}{(g_i - g_i f_i)^! g_i f_i^!}$$

Using Stirling’s approximation, one can eliminate the factorial signs, yielding:

$$\ln W = \sum_i \ln W_i = \sum_i \left[ g_i \ln g_i - g_i - (1 - f_i) \ln(g_i - g_i f_i) - g_i f_i \ln g_i f_i \right]$$

The total number of electrons in the system equals $N$ and the total energy of those $N$ electrons equals $E$. These system parameters are related to the number of states at each energy, $g_i$, and the probability of occupancy of each state, $f_i$, by:

$$N = \sum_i g_i f_i$$

and

$$U = \sum_i E_i g_i f_i$$

According to the basic assumption of statistical thermodynamics, all possible configurations are equally probable. The multiplicity function provides the number of configurations for a specific set of occupancy probabilities, $f_i$. The multiplicity function sharply peaks at the thermal equilibrium distribution. The occupancy probability in thermal equilibrium is therefore obtained by finding the maximum of the multiplicity function, $W$, while keeping the total energy and the number of electrons constant.

For convenience, we maximize the logarithm of the multiplicity function instead of the multiplicity function itself. According to the Lagrange method of undetermined multipliers, we must maximize the following function:

$$\ln W - a \sum_j g_j f_j + b \sum_j E_j g_j f_j$$

where $a$ and $b$ need to be determined. The maximum multiplicity function is obtained from:

$$\frac{\partial}{\partial (g_i f_i)} \left[ \ln W - a \sum_j g_j f_j + b \sum_j E_j g_j f_j \right] = 0$$
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which can be solved, yielding:

$$\ln \frac{g_i - g_i f_i}{g_i f_i} - a - b E_i = 0$$

or

$$f_i = f_{PD}(E_i) = \frac{1}{1 + \exp(a + b E_i)}$$

which can be written in the following form

$$f_{PD}(E_i) = \frac{1}{1 + \exp\left(\frac{E_i - E_F}{\beta}\right)}$$

with $b = 1/b$ and $EF = -a/b$. The symbol $E_F$ was chosen since this constant has units of energy and will be the constant associated with this probability distribution.

Taking the derivative of the total energy, one obtains:

$$dU = \sum E_i d\left(g_i f_i\right) + \sum g_i f_i dE_i$$

Using the Lagrange equation, this can be rewritten as:

$$dU = \beta d\left(\ln W\right) + \sum g_i f_i dE_i + E_F dN$$

Any variation of the energies, $E_i$, can only be caused by a change in volume, so that the middle term can be linked to a volume variation $dV$.

$$dU = \beta d\left(\ln W\right) + \sum g_i f_i \frac{dE_i}{dV} dV + E_F dN$$

Comparing this to the thermodynamic identity:

$$dU = TdS - pdV + \mu dN$$

The energy, $E_F$, equals the energy associated with the particles, $m$.

The comparison also identifies the entropy, $S$, as being the logarithm of the multiplicity function, $W$, multiplied with Boltzmann’s constant. The Fermi-Dirac distribution function then becomes:

$$f_{PD}(E) = \frac{1}{1 + \exp\left(\frac{E - E_F}{kT}\right)} \text{© B. Van Zeghbroeck, 1998}$$

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Citation: Solomon Budnik, "Photonic Displays in Augmented Reality". American Research Journal of Electronics and Communication Engineering; vol. 1, no. 1; pp: 23-27.

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