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Cosmological simulations using a static scalar-tensor theory

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Abstract. We present ΛCDM N-body cosmological simulations in the framework of a static general scalar-tensor theory of gravity. Due to the influence of the non-minimally coupled scalar field, the gravitational potential is modified by a Yukawa type term, yielding a new structure formation dynamics. We present some preliminary results and, in particular, we compute the density and velocity profiles of the most massive group.

1. Introduction

The problem of explaining the structure formation of the Universe is one of the most fascinating at the beginning of this new millennium. From the recent experimental developments and observations, cosmology has acquired the status of a high precision area of research [1]. In fact, recent and independent observational data measured in the CMBR on various angular scales [2, 3], in type Ia supernovae [4], as well as in galaxy surveys [5, 6], suggest that $\Omega = \Omega_\Lambda + \Omega_m \approx 1$, or that $\Omega_\Lambda \approx 0.73$ and $\Omega_m \approx 0.27$, implying the existence of dark energy and dark matter, respectively. However, the nature of dark components is still unknown. These observations favour the now standard ΛCDM cosmological model. Despite some problems on galactic scales revealed by numerical simulations, which could be explained with some alternative models (e.g. Warm Dark Matter), large scale structure simulations, predicted by the ΛCDM model, agree well with observations. Naturally, particular inflationary scenarios motivated by different particle physics theories have their own dark matter candidates, such as axion, neutralino, Higgs particle, among others, as well as a quintessence field [7, 8]. In order to include such particles in cosmological models one usually adds a scalar field (SF) equation to the general relativity field equations. One possibility is to couple this field non-minimally to gravity to have a scalar-tensor theory of gravity (STT).

In this work we present some results of the role played by a massive non-minimally coupled SF on the ΛCDM universe structure formation process. Our theoretical model is built from a general STT static SF which modifies the cosmological dynamics and the Newtonian gravity potential on particles; the dynamical full treatment of SF perturbations is now under development. We evolve a cosmological cube using...
standard ΛCDM equations with periodic boundary conditions, where the particles interact through the Newtonian force plus an additional term. The latter comes from a Yukawa type potential derived from the Newtonian limit of a STT. It should be noted that in the present work the SF does not replace the dark matter or dark energy, but rather coexists with them. To perform the simulations we have modified a standard serial treecode developed by one of us (MARM) [9] and Gadget 1 [10] in order to take into account the contribution of the Yukawa potential.

2. Evolution equations using a static STT

In a previous paper we found the solutions for the potential-density pair problem in the Newtonian limit of a scalar-tensor theory of gravity [11]. Here, we applied those results and found that the potential of a single particle of mass $m$ is given by [12]

$$\Phi_N = -\frac{G_N}{1 + \alpha} \frac{m}{r} (1 + \alpha e^{-r/\lambda}),$$

(1)

For local scales, $r \ll \lambda$, deviations from the Newtonian theory are exponentially suppressed, and for $r \gg \lambda$ the Newtonian constant diminishes (augments) to $G_N/(1 + \alpha)$ for positive (negative) $\alpha$. This means that equation (1) fulfills all local tests of the Newtonian dynamics, and it is only constrained by experiments or tests on scales larger than –or of the order of– $\lambda$, which in our case is of the order of galactic scales.

To simulate cosmological systems, the expansion of the Universe has to be taken into account. Here, we employ a cosmological model with a static scalar field which is consistent with the Newtonian limit given by Eq. (1). Thus, the scale factor, $a(t)$, is given by the following Friedmann model,

$$a^3 H^2 = H_0^2 \left[ \frac{\Omega_m + \Omega_m \alpha a^3}{1 + \alpha} + \left( 1 - \frac{\Omega_m + \Omega_\Lambda}{1 + \alpha} \right) a \right]$$

(2)

where $H = \dot{a}/a$, $\Omega_m$ and $\Omega_\Lambda$ are the matter and energy density evaluated at present, respectively. We notice that the source of the cosmic evolution is deviated by the term $1 + \alpha$ when compared to the standard Friedman-Lemaitre model. Therefore, it is convenient to define a new density parameter by $\Omega_i^\alpha = \Omega_i / (1 + \alpha)$. This new density parameter is such that $\Omega_m^\alpha + \Omega_\Lambda^\alpha = 1$, which implies a flat Universe, and this shall be assumed in our following computations, where we consider $(\Omega_m^\alpha, \Omega_\Lambda^\alpha) = (0.3, 0.7)$. For positive values of $\alpha$, a flat cosmological model demands to have a factor $(1 + \alpha)$ more energetic content ($\Omega_m$ and $\Omega_\Lambda$) than in standard cosmology. On the other hand, for negative values of $\alpha$ one needs a factor $(1 + \alpha)$ less $\Omega_m$ and $\Omega_\Lambda$ to have a flat Universe. To be consistent with the CMB spectrum and structure formation numerical experiments, cosmological constraints must be applied on $\alpha$ in order for it to be within the range $(−1, 1)$ [13, 14, 15, 16].

In the Newtonian limit of STT of gravity, the Newtonian motion equation for a particle $i$ is written as

$$\dot{x}_i + 2Hx_i = -\frac{1}{a^3} \frac{G_N}{1 + \alpha} \sum_{j \neq i} \frac{m_j (x_i - x_j)}{|x_i - x_j|^3} F_{SF}(|x_i - x_j|, \alpha, \lambda)$$

(3)

where $x$ is the comovil coordinate, and the sum includes all periodic images of particle $j$, and $F_{SF}(r, \alpha, \lambda)$ is

$$F_{SF}(r, \alpha, \lambda) = 1 + \alpha \left( 1 + \frac{r}{\lambda} \right) e^{-r/\lambda}$$

(4)
which, for small distances compared to \( \lambda \), is \( F_{SF}(r < \lambda, \alpha, \lambda) \approx 1 + \alpha \left(1 + \frac{r}{\lambda}\right) \) and, for long distances, is \( F_{SF}(r > \lambda, \alpha, \lambda) \approx 1 \), as in Newtonian physics.

We now analyze the general effect that the constant \( \alpha \) has on the dynamics. The role of \( \alpha \) in our approach is as follows. On one hand, to construct a flat model we have set the condition \( \Omega_m^\alpha + \Omega_\Lambda^\alpha = 1 \), which implies having \((1 + \alpha)\) times the energetic content of the standard \( \Lambda \)CDM model. This essentially means that we have an increment by a factor of \((1 + \alpha)\) times the amount of matter, for positive values of \( \alpha \), or a reduction of the same factor for negative values of \( \alpha \). Increasing or reducing this amount of matter affects the matter term on the r.h.s. of the equation of motion (3), but the amount affected cancels out with the term \((1 + \alpha)\) in the denominator of (3) stemming from the new Newtonian potential (1). On the other hand, the factor \( F_{SF} \) augments (diminishes) for positive (negative) values of \( \alpha \) compared to the \( \Lambda \)CDM model. For \( r \gg \lambda \) the dynamics is essentially Newtonian.

### 3. Results

We now present results for the \( \Lambda \)CDM model of the Universe model previously described. Because the visible component is the smaller one and given our interest to test the consequences of including a SF contribution to the evolution equations, our model excludes gas particles, but all its mass has been added to the dark matter. Therefore, our model is as follows. We start our simulation with an initial distribution of \( N = 2 \times 32^3 \) particles in a box with sides of \( 50 h^{-1} \) Mpc at \( z = 10 \). This case is similar to the one that comes with Gadget 1 [10]. At present epoch, \( \Omega_m^0 = 0, \Omega_\Lambda^0 = 0.3, \Omega_\Lambda^0 = 0.7, H_0 = 100 h \) km/s/Mpc, \( h = 0.7 \). We restrict the values of \( \alpha \) to the interval \((-1, 1) \) [13, 14, 15, 16] and use \( \lambda = 5 \) Mpc, since this scale turns out to be an intermediate scale between the size of the clump groups and the separation of the formed groups.

In Fig. 1 we show \( y-z \) snapshots at redshift \( z = 0 \) of our \( \Lambda \)CDM model. Fig. 1 (a) presents the standard case without SF, i.e., the interaction between bodies through the standard Newtonian potential. In (b) we show the case with \( \alpha = 1, \lambda = 5 \) Mpc. In (c) \( \alpha = -1/2, \lambda = 5 \) Mpc. In (d) \( \alpha = -1/4, \lambda = 5 \) Mpc. One notes clearly how the SF modifies the matter structure of the system. The most dramatic cases are (b) and (c) where we have used \( \alpha = 1 \) and \( \alpha = -1/2 \), respectively. Given the argument at the end of last section, in the case of (b), for \( r \ll \lambda \), the effective gravitational pull has been augmented by a factor of 2, in contrast to case (c) where it has diminished by a factor of 1/2; in model (d) the pull diminishes only by a factor of 3/4. That is why one observes for \( r < \lambda \) more structure formation in (b), less in (d), and lesser in model (c). The effect is then, for a growing positive \( \alpha \), to speed up the growth of perturbations, than of halos and then of clusters, whereas negative \( \alpha \) values \( (\alpha \to -1) \) tend to slow down the growth.

Next, we found the groups in the system using a friend-of-friend algorithm and select one of the most massive ones. The chosen group is located approximately at \( y = 19 \) Mpc, \( z = 12 \) Mpc, and it is labeled with the letter “G” in Fig. 1(a). The group was analyzed by obtaining their density profiles and circular velocities. In Fig. 2(a) we show the density profiles for this group. The more cuspy case is for \( \alpha = 1 \) and the less cuspy is for \( \alpha = -1/2 \).

In Fig. 2(b) we show, for the same group, circular velocity curves, computed using \( v_c^2 = G N M(r)/r \). The case with \( \alpha = 1 \) corresponds to higher values of \( v_c \), since this
Figure 1. $y$–$z$ snapshots at $z = 0$ of a $\Lambda$CDM universe. See text for details.

Figure 2. (a) Density profiles for one of the most massive groups at $z = 0$ of a $\Lambda$CDM universe. The group is located approximately at $y = 19$ Mpc, $z = 12$ Mpc, labeled with “G” in Fig 1(a). Vertical scale is in units of $\rho_0 = 10^{10} M_\odot h^{-1}/(h^{-1} \text{kpc})^3$. (b) The corresponding circular velocity.
depends on how much accumulated mass there is at a distance $r$ and this is enhanced by the factor $F_{SF}$ for positive values of $\alpha$.

The groups are at most 2 Mpc in size at $z = 0$, which means that the inner structure is such that $r < \lambda$, being affected by the factor $F_{SF}$ as explained at the end of section 2. While for $r > \lambda$ the overall structure formation process is governed by Newtonian physics, which is the reason why the overall structure of the models in Fig. 1 is similar.

4. Conclusions

We have used a general, static STT that is compatible with local observations by the appropriate definition of the background field constant, i.e. $< \phi > = \frac{1}{N(1 + \alpha)}$. A direct consequence of our approach is that the amount of matter (energy) has to be increased for positive values of $\alpha$ and diminished for negative values of $\alpha$ with respect to the standard $\Lambda$CDM model in order to have a flat cosmological model. Quantitatively, our model demands to have $\Omega/(1+\alpha) = 1$ and this changes the amount of dark matter and energy of the model for a flat cosmological model, as assumed.

The general gravitational effect is that the interaction including the SF changes by a factor $F_{SF}(r, \alpha, \lambda) \approx 1 + \frac{\alpha(1 + \frac{r}{\lambda})}{1 + \frac{\lambda}{r}}$ for $r < \lambda$ in comparison with the Newtonian case. Thus, for $\alpha > 0$ the growth of structures speeds up in comparison with the Newtonian case. For the $\alpha < 0$ case the effect is to diminish the formation of structures. For $r > \lambda$ the dynamics is essentially Newtonian.

Using the resulting modified dynamical equations, we have studied the structure formation process of a $\Lambda$CDM universe. We varied the amplitude and sign of the strength of the SF ($\alpha$) in the interval $(-1,1)$ and performed several 3D-simulations with the same initial conditions. From our simulations with different values of $\alpha$, we have found that the inclusion of SF changes local dynamical properties of the most massive group considered, and accordingly the density profile and circular velocity, however, the overall structure is somewhat similar. Here, we notice that we have also studied other massive groups, in particular one smaller group located approximately at $y = 16.5$ Mpc, $z = 22$ Mpc in Fig. 1(a). The trends are quite similar to the most massive group, so that our conclusions prevail.

In this work we only varied the amplitude of the SF ($\alpha$) leaving the scale length ($\lambda$) of the SF unchanged. After some preliminary runs, the increase of $\lambda$ enhances the structure formation process for $\alpha$ positive, and the decrease of $\lambda$ makes the structure grow at a slower rate. In a future work we will study an ampler space parameter and with a much better resolution. Also, the cosmological initial conditions will be constructed using the matter density field corresponding to the modified gravity.

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