Development of a broadband reflective T-filter for voltage biasing high-Q superconducting microwave cavities

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We present the design of a reflective stop-band filter based on quasi-lumped elements that can be utilized to introduce large dc and low-frequency voltage biases into a low-loss superconducting coplanar waveguide (CPW) cavity. Transmission measurements of the filter are seen to be in good agreement with simulations and demonstrate insertion losses greater than 20 dB in the range of 3 to 10 GHz. Moreover, transmission measurements of the CPW’s fundamental mode demonstrate that loaded quality factors exceeding $10^5$ can be achieved with this design for dc voltages as large as 20 V and for the cavity operated in the single-photon regime. This makes the design suitable for use in a number of applications including qubit-coupled mechanical systems and circuit QED.

The integration of bias circuitry into high-quality (low-loss) microwave cavities for controlling embedded components is an important technical issue for a range of topics that includes research with qubit- and cavity-coupled mechanical systems,[1–10] circuit QED,[11, 12] and quantum dynamics of nonlinear systems.[13, 14] In these scenarios, the applied potentials and currents serve a variety of functions such as maintaining a device’s operating state or establishing tunable electrostatic interactions between devices. However, if not carefully engineered, the introduction of the requisite circuitry can degrade the quality of a cavity through increased external circuit loading and radiative losses,[15] which generally have a detrimental effect on the given application.

In recent years, several solutions to this problem have been developed for dc biasing of superconducting coplanar waveguide (CPW) cavities. These cavities play an important role in the applications mentioned above due to their large electric field density[16, 17] and high intrinsic quality factors ($\simeq 10^6$).[18] The solutions put forth for biasing such cavities utilize either half-wavelength or quarter-wavelength traces for band-stop filtering or high-impedance isolation of the bias circuitry’s connections to the cavities.[19, 20] This has enabled operation of biased CPWs with loaded quality factors in the range of $10^3$–$10^4$ for several applications.[12, 14, 19, 21] However, the reliance on wavelength-specific isolation geometries results in a narrow band of controlled isolation around a specific operating frequency, which could be problematic in instances where multiple devices with different or tunable energy scales are integrated into the cavity and thus require broadband isolation. Important examples of this include proposed techniques for the dispersive read-out of a qubit-coupled nanoresonator embedded inside a CPW cavity.[2, 3] For such techniques to be feasible, the qubit and CPW, which can be detuned in energy by several GHz, should have linewidths comparable to or smaller than the nanoresonator-qubit coupling strength, which is controlled by a large dc voltage ($\sim 10^5$ V); this requires both the CPW and qubit to be well-isolated at their respective energies from the bias circuitry.

Here we report a design that overcomes the challenge of obtaining broadband isolation in low frequency lines of a CPW cavity by utilizing a superconducting reflective T-filter.[21] This design provides high cavity isolation covering most of the frequency range typically used by elements in planar circuit QED architectures. Moreover, it allows for application of dc voltages as high as 20
V to the CPW’s center trace with indiscernible distortion of the cavity’s fundamental mode and no measurable increase in the mode’s loss for quality factors exceeding 10⁶. This makes it an important new tool for investigations of quantum hybrid systems.

A schematic of the filtered CPW cavity is shown in Fig. 1(a). The cavity is formed in the standard manner from a section of Z₀ = 50 Ω planar transmission line that is isolated at its RF input and output ports (Ports 1 and 2 respectively) through the small capacitors C_in and C_out. These capacitors set the ends of the cavity to be voltage anti-nodes, resulting in standing-wave resonances with wavelengths λ = 2L/n, where L is the cavity length and n is an integer. In this work, we investigate the effect of the filter and low frequency circuitry on only the lowest-order mode, λ = 2L, which has a voltage node at the mid-point of the cavity.

In addition to the RF ports, a third port (Port 3) is connected to the mid-point of the cavity through a planar, low-pass T-filter, which allows for DC and low-frequency (< 2 GHz) voltage biasing of the cavity’s center trace. The T-filter design, Figs. 1(a) and (b), consists of a single section of two meander-line inductors (L_F) located on opposite ends of an interdigitated shunt capacitor (C_F) to the ground plane. Looking into the filter from Port 3 (or from point a) it is intuitive how the filter element allows for low-frequency biasing and wide-band, high-frequency isolation of the cavity: At low frequencies (ω ≪ ω_F ≡ √(2LFC_F)), the filter’s inductive reactances are negligible compared to the capacitive reactance and load impedance, so any signal incident on the filter passes through unattenuated; on the other hand, when ω ≳ ω_F, the input impedance of the filter tends toward Z_in = jωL_F, and hence signals incident on Port 3 are strongly reflected from the almost strictly imaginary impedance, i.e. γ ≡ Z_in/Z_out ≈ 1. An analytical model using lumped-elements for the filter components predicts that the filter transmission (S_{21}) should roll off as S_{21} ≈ Z_F/Z_{2p} (ω/ω_F)³ for ω > ω_F, where Z_F ≡ √(2L_FC_F) is the characteristic impedance of the filter. This yields an insertion loss that increases at 60 dB/decade. Of course, this estimate neglects the parasitic reactance of the filter elements, which plays a dominant role in limiting IL over the frequency range explored here and is discussed in more detail below.

The CPW resonator, Fig. 1(b), is composed of a center line of width 6 µm and length of L = 11 mm, and it is separated from the ground planes by a gap of width 3 µm, resulting in a characteristic impedance of 50 Ω and resonance frequency ω₁/2π ≈ 5.3 GHz. The interdigitated capacitor and the meander inductors that compose the filter have a central trace width and line-spacing of 2 µm. The capacitors and inductors were engineered to have nominal values of L_F = 10 nH and C_F = 1.5 pF, corresponding to ω_F/2π ≈ 2 GHz and Z_F = 115 Ω. Both the CPW and the filter were fabricated by first DC-sputtering 120 nm thick Nb film on top of 500 µm thick resistivity silicon wafer (ρ > 10 kΩ·cm). This was followed by patterning the design using photolithography and RIE-based dry-etch with Ar:BCl3:Cl₂. Finally, the coupling capacitors C_in and C_out were made using electron-beam lithography and aluminum evaporation. For this study, the coupling capacitors were made symmetrically (i.e., C_in = C_out ≡ C_k), and three different values were utilized: C_k = 1, 2 and 2.5 fF, denoted as devices I, II, and III respectively. The values of C_k were estimated using ANSYS Q3D for the geometry shown in the inset of Fig. 1b with capacitor overlaps ℓ = 5, 15, 20 µm.

We began the experimental characterization of the CPW-filter design by performing transmission and reflection measurements of the filters fabricated without the CPW (Fig. 2). These measurements were done in a dip probe at T = 4.2 K using an Agilent N5230A network analyzer. No cryogenic attenuators or amplifiers were used for these initial measurements. From the transmission measurements, S_{21} is observed to cut off around 2 GHz, with a roll-off of 60 dB/decade up to 4 GHz, in agreement with both the analytical estimation and Sonnet simulations. For frequencies above 4 GHz the simple lumped-element model of the individual filter components can no longer be used to accurately describe the filter’s response. In particular, the parasitic capacitance C_P of each inductor is seen to limit the filter’s insertion loss: heuristically, C_P contributes a reactance (−1/ωC_P) that becomes comparable to the inductive reactance (ωL_F); this causes the total inductor impedance to decrease and ultimately vanish at the self-resonance frequency (−1/√L_FC_P ≈ 12 GHz), resulting in a maximum in S_{21}. More quantitatively, Sonnet simulations predict a maximum in S_{21} at 12 GHz; the simulated charge and current profiles confirm this maximum corresponds to the lowest-order self-resonance of the inductors - additional simulations show that, with simple design changes to reduce C_P, the stop-band could be extended to at least 14 GHz. Despite the influence of C_P, the insertion losses remain in excess of 20 dB up to ~10 GHz. Moreover, it is important to note the reflective nature of the filter between 3 GHz and 10 GHz, which is evident from the near unity value of S_{11} measured within the band.

Next, transmission measurements of complete filtered CPW circuits were conducted at milli-Kelvin temperatures (Fig. 3). Each sample was mounted in a light-tight copper box and magnetic shield, both of which were anchored to the mixing chamber of a dilution refrigerator; all measurements were made at the base temperature of the fridge, which was measured to be between 20 mK and 30 mK. An optically-isolated voltage source connected to Port 3 through a heavily-filtered (> 100 dB of attenuation at 5 GHz) coaxial line was used to supply DC voltages, V_{dc}, to the devices. The input microwave line to
FIG. 2. Measured and simulated transmission ($S_{21}$) and reflection ($S_{11}$) characteristics of a reflective T-filter (see inset) from 0.1 to 15 GHz. The black circles (red squares) represent the magnitude of $S_{21}$ ($S_{11}$) measurements at 4 K using a network analyzer calibrated to account for the probe’s cable losses and delay. The solid black (dashed red) line is the magnitude of $S_{21}$ ($S_{11}$) simulated using Sonnet for this filter’s geometry. The dotted lines represent $S_{21}$ and $S_{11}$ calculated with an analytical expression that treats the filter’s components as lumped-elements.

the CPW included 70 dB of cryogenic attenuation, which was distributed between refrigerator stages. On the return line, two circulators provided a total of $\sim 30$ dB of isolation between the CPW and the first-stage amplifier, a cryogenic HEMT, which was anchored to the 4 K stage. The output from the HEMT was amplified and mixed down to MHz frequencies using a standard heterodyne circuit, and then digitized using an Alazar ATS9870 card. From the digitized data, the complex transmission $S_{21}$ through the device was recovered and corrected for amplifier gain, cable loss and phase delay.

Figure 3 (a) shows the amplitude of a transmission spectrum ($S_{21}$) measured for device II at large microwave power, $P = -100$ dBm at Port 1, corresponding to a mean cavity photon number $N \approx 10^5$, and for $V_{dc} = 0$ V and 20 V applied to Port 3; Fig. 3 (b) displays the corresponding data for low $P$ for Device I ($P = -155$ dBm and $N \approx 1$). The traces are representative of transmission measurements of all the samples studied here, and are well-fit to the standard complex expression[17] for $S_{21}$ of a CPW’s fundamental mode without the dc filter (solid and dotted lines in the plot). It is evident from the data that for biases as high as $V_{dc} = 20$ V there is no resolvable change in the shape of the resonance or the mode’s quality factor. Also shown are measurements of $S_{31}$ (Fig. 3(a), inset), which is defined as the transmitted signal measured at Port 3 for voltages incident on Port 1 with Port 2 terminated in 50Ω. The peak of $S_{31}$ is seen to be $\sim 30$ dB smaller than the corresponding measurements of $S_{21}$, indicating a high degree of isolation through port 3.

Similar fits of $S_{21}$ data enable extraction of $Q_L$ for the full range of parameters $V_{dc}$, $C_k$, and $P$ that we investigated (Fig. 4). We find for both high and low $P$ that $Q_L$ increases proportionally to $\sim 1/C_k^2$, with values as high as $Q_L = 2.5 \times 10^6$ measured for device I. The observations are consistent with estimates of $Q_L$ (solid and dashed lines, Fig. 4), which we define through $1/Q_L \equiv 1/Q_i + 1/Q_C$. Here $1/Q_C$ accounts for losses to external circuitry through the coupling capacitors. [17] Internal cavity losses are represented by $1/Q_i$, which we estimate from the cavities’ insertion losses and fits to $S_{21}$; we use $Q_i = 0.7 \times 10^6$ at high power (solid line) and $Q_i = 0.2 \times 10^6$ at low power (dashed line), where unsaturated two-level systems make a greater contribution to the internal dissipation. [25] We can estimate the contribution to $Q_i$ from the losses through the filter us-
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In conclusion, we have reported a simple, effective, and well-modeled filter design for introducing dc and low-frequency voltages into high-quality superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities. The high isolation, large stop-band (e.g. Fig. 3), and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities.

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![FIG. 4.](image)

Loaded quality factors $Q_L$ of all the devices studied in this work plotted versus $C_k$ for the full range of $V_{2c}$ and $P$. Quality factors were determined from fits to cavity’s $S_{21}$ response (e.g. Fig. 3). Error bars are determined by the $2\sigma$ uncertainty estimated from the fits.

\[ \frac{ILF}{S_{31}(\omega_c)/S_{21}(\omega_c)} \] Specifically, for device II (the only device for which $S_{21}$ was measured; Fig. 3(a), inset), we see that $ILF = -30$ dB, indicating that 0.1% of the power escapes through the filter in comparison with the coupling capacitors. This corresponds to a filter quality factor of \( \sim \sqrt{1000}Q_C = 3 \times 10^6 \), and suggests that this bias circuit design could be integrated, with small or negligible impact, into cavities with $Q_L$ as high as $\sim 10^6$.

In conclusion, we have reported a simple, effective, and well-modeled filter design for introducing dc and low-frequency voltages into high-quality superconducting CPW cavities. The high isolation, large stop-band and small cavity loading make this a versatile design that could be integrated in superconducting CPW cavities and transmission line feeds, or into traces leading to stand-alone superconducting devices for a large range of cryogenic applications.

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