On Improving Deep Reinforcement Learning for POMDPs

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Abstract

Deep Reinforcement Learning (RL) recently emerged as one of the most competitive approaches for learning in sequential decision making problems with fully observable environments, e.g., computer Go. However, very little work has been done in deep RL to handle partially observable environments. We propose a new architecture called Action-specific Deep Recurrent Q-Network (ADRQN) to enhance learning performance in partially observable domains. Actions are encoded by a fully connected layer and coupled with a convolutional observation to form an action-observation pair. The time series of action-observation pairs are then integrated by an LSTM layer that learns latent states based on which a fully connected layer computes Q-values as in conventional Deep Q-Networks (DQNs). We demonstrate the effectiveness of our new architecture in several partially observable domains, including flickering Atari games.

1 Introduction

Research in automated learning techniques that interact with the environment span a period of almost 50 years. Such form of learning is often referred to as reinforcement learning. In the past 3 decades, many reinforcement learning techniques based on fully and partially observable Markov decision processes (MDPs) have been successfully applied to a variety of problems including spoken dialog management [Levin et al., 2000], robotic control [Simmons and Koenig, 1995] and automated assistance in health care [Boger et al., 2005]. However, many of those applications were small scale. In contrast, the environment of many real-world applications is best modeled with a large number of states, which induces the “curse of dimensionality” haunting many reinforcement learning techniques. During the last decade, researchers improved the scalability of reinforcement learning approaches, however further advances are needed. In 2015, the success of Google’s AlphaGo caught the attention of many researchers and the public by demonstrating the potential of deep reinforcement learning [Silver et al., 2016]. Deep reinforcement learning combines reinforcement learning and deep learning, and has shown great success in solving a number of very challenging tasks that can be easily modeled as conventional reinforcement learning problems, but cannot be solved by conventional reinforcement learning approaches due to the high dimensionality of the state space, e.g., continuous control [Lillicrap et al., 2015], high-dimensional robot control [Stadie et al., 2015], and Atari Learning Environment benchmarks (ALE) [Bellemare et al., 2013].

Specifically, Deep Q-Networks (DQNs) can be used to effectively and efficiently play many Atari 2600 games [Mnih et al., 2015]. The idea is to extract convolved features of the frames as states and to approximate the Q-function over the states with a deep neural network. For instance, a DQN is trained to estimate the expected value of a policy based on the past four frames as input in Atari 2600 games. For most Atari 2600 games, four frames is sufficient to approximate the current state of the game. Generally speaking, the Atari games are treated as MDP problems, and DQNs are used to approximate the value functions of these MDPs. However, for some other real-world tasks including some Atari 2600 games, the problem is really a partially observable Markov decision process (POMDP) where the state of the environment may be partially observable or even unobservable, to the point where arbitrarily long histories of observations are needed to extract sufficient features for optimal action selection. Unfortunately, DQN is not suitable for those problems due to the assumption of complete observability of the state.

While POMDPs can naturally model planning tasks with uncertain action effects and partial state observability, finding an optimal policy is notoriously difficult. Since the state of the environment is not directly observable, a common approach consists of maintaining a distribution over the underlying state, known as a belief. The belief can be revised after
each action and observation according to Bayes’ theorem. In POMDPs, beliefs are equivalent to states in MDPs. However, since the space of beliefs is infinite and continuous, many previous POMDP techniques focus on identifying a finite subset of beliefs that are sufficient to approximate all reachable beliefs in order to decrease computational complexity [Kurniawati et al., 2008][Li et al., 2007].

Deep neural networks have the capability of extracting high-level features from raw sensory data, like raw image pixels, and have strong generalization abilities. Recent advances in deep learning suggest a new way of thinking for solving POMDP problems. However, very little work leverages deep reinforcement learning in partially observable environments. Among this work, [Egorov, 2015] adopted DQNs to solve conventional POMDP problems. A policy is obtained with a DQN that maps concatenated observation-belief vector pairs to an optimal action. Their work (we call it DBQN) is designed for model-based representations of the environment where the transition, observation and reward functions are already known. Thus, the belief can be estimated precisely with Bayes’ theorem and can serve as input to the neural network. However, in most real-world POMDP problems, the environment dynamics are unknown. To address this, [Hausknecht and Stone, 2015] adapted the fully connected network. However, in most real-world POMDP problems, the environment dynamics are unknown. To address this, [Hausknecht and Stone, 2015] adapted the fully connected structure of DQN with a recurrent network [Hochreiter and Schmidhuber, 1997], and called the new architecture Deep Recurrent Q-Network (DRQN). The proposed model recurrently integrates arbitrarily long histories of observations to find an optimal policy that is robust to partial observability. However, DRQNs consider only observation histories without explicitly including actions as part of the histories. This impacts negatively the performance of the approach as demonstrated in Sec. 4. [Lample and Chaplot, 2016] combined DRQN with handcrafted features to jointly supervise the learning process of 3D games in partially observable environments, however the approach suffers from the same problem as DRQN since it overlooks action histories. [Foerster et al., 2016] extended DRQN to handle partially observable multi-agent reinforcement learning problems by proposing a deep distributed recurrent Q-networks (DQRQN). The action history is explicitly processed by an LSTM layer and fed as input to a Q-network. In DQRQN, each action is forcibly decoupled from its associated observation despite the fact that action-observation pairs are the key to belief updating. As a result, the decoupling of actions and observations in DQRQN impacts negatively belief inference.

In this paper, we propose a new architecture called Action-based Deep Recurrent Q-Network (ADQRQN) to improve learning performance in partially observable domains. Actions are encoded via a fully connected layer and coupled with their associated observations to form action-observation pairs. The time series of action-observation pairs is processed by an LSTM layer that learns latent states based on which a fully connected layer computes Q-values as in conventional DQNs. We demonstrate the effectiveness of our new architecture in several Atari 2600 games. Table[I] summarizes the main differences between ADRQN and other state-of-the-art deep Q-learning techniques.

2 Background

In this section, we give a brief review of Deep Q-Networks (DQNs), Partially Observable Markov Decision Processes (POMDPs) and Deep Recurrent Q-networks (DRQNs).

2.1 Deep Q-Networks

A sequential decision problem with known environment dynamics is usually formalized as a Markov Decision Process (MDP), which is characterized by a 4-tuple \((S, A, P, R)\). At each step, an agent selects an action \(a_t \in A\) to execute with respect to its fully observable current state \(s_t \in S\) and based on its policy \(\pi\). It receives an immediate reward \(r_t \sim R(s_t, a_t)\) and transitions to a new state \(s_{t+1}\). The objective of reinforcement learning is to find the policy that maximizes the expected discounted rewards \(R_t\)

\[
R_t = r_t + \gamma r_{t+1} + \gamma^2 r_{t+2} + \cdots \tag{1}
\]

where \(\gamma \in [0,1]\) is the discount factor. In MDPs, an optimal policy can be computed by value iteration [Sutton and Barto, 1998].

Q-Learning [Watkins and Dayan, 1992] was proposed as a model-free technique for reinforcement learning problems with unknown dynamics. It estimates the value of executing an action in a given state followed by an optimal policy. This value is called the state-action value, or simply Q-value as defined below:

\[
Q^\pi(s, a) = E(R_t | s_t = s, a_t = a) \tag{2}
\]

The Q-values can be learned iteratively according to the following rule while the agent is interacting with the environment:

\[
Q(s, a) = Q(s, a) + \alpha(r + \gamma \max_a Q(s', a') - Q(s, a)) \tag{3}
\]

In tasks with a large number of states, a common trick is to use a function approximator to estimate the Q-function. For instance, DQN [Mnih et al., 2015] uses a neural network parameterized by \(\theta\) to represent \(Q(s, a; \theta)\). Neural networks with at least one (non-linear) hidden layer and sufficiently many nodes can approximate any function arbitrarily closely. DQN is optimized by minimizing the following loss function:

\[
L_i(\theta_i) = E_{s,a,r,s'} \left[ \left( y_{i \text{target}}^t - Q(s, a; \theta_i) \right)^2 \right] \tag{4}
\]

where \(y_{i \text{target}}^t = r + \gamma \max_{a'} Q(s', a' | \theta^-_i)\) denotes the target value of the action \(a_t\) given state \(s_t\). Here \(\theta^-_i\) is cloned from \(\theta_i\) every fixed numbers of iterations. DQN uses experience replay [Lin, 1993] to store previous samples \(e_t = (s_t, a_t, r_t, s_{t+1})\) up to a fixed size memory \(D_t\). The Q-network is then trained by uniformly sampling mini-batches of past experiences from the replay memory. An important factor for the efficiency of DQN in AlphaGo and the Atari games is the assumption of full state observability that allows the neural network to use only one (or a few) observation(s) as input. Thus, DQN suffers inaccuracy in tasks with partially observable states.
2.2 Partially Observable Markov Decision Processes (POMDPs)

POMDPs generalize MDPs for planning under partial observability. A POMDP is mathematically defined as a tuple \((S, A, Z, T, O, R)\), consisting of a finite set of states \(S\), a finite set of actions \(A\), a transition function \(T: S \times A \rightarrow \Pi(S)\), a reward function depending on the state and the action and the action just performed \(R: S \times A \rightarrow \mathcal{R}\), a finite set of observations \(Z\) and an observation function \(O: S \times A \rightarrow \Pi(Z)\). As the true states are not fully observable any more, a belief is used to estimate the current state, defined as the probability mass function over the states and denoted as \(b = (b(s_1), b(s_2), \ldots, b(s_{|S|}))\), where \(s_i \in S, b(s_i) \geq 0\), and \(\sum_{s_i \in S} b(s_i) = 1\). Given the current belief \(b^t\), the next belief \(b^{t+1}\) is computed as follows:

\[
b^{t+1}(s_j) = \frac{O(s_j, a, z) \sum_{s_i \in S} T(s_i, a, s_j) b^t(s_i)}{P(z|a, b^t)}
\]

The expected immediate reward for an agent performing action \(a\) at the belief state \(b\) is computed as \(\rho(b, a) = \sum_{s_i \in S} b(s_i) R(s_i, a)\). The transition function among beliefs becomes \(\tau(b, a, b') = \sum_{z \in Z} P(b'|b, a, z) P(z|a, b)\) where \(P(b'|b, a, z) = 1\) if \(b' = SE(b, a, z)\), and 0 otherwise. An optimal policy \(\pi: \mathcal{R}^{|S|} \rightarrow A\) can be computed by value iteration:

\[
V(b) = \max_a [\rho(b, a) + \gamma \sum_{b'} \tau(b, a, b') V(b')]
\]

where \(\gamma\) is a discount factor for the past history. In practice, it is common to have the optimal policy represented by a set of linear functions (so called \(\alpha\)-vectors) over the belief space, with the maximum “envelop” of the \(\alpha\)-vectors forming the value function [Shani et al., 2013].

2.3 DRQN

DQN assumes that the agent has full knowledge of the state of the environment, i.e., the agent’s observation is equivalent to the state of environment. However, in practice, this is rarely true, even in some Atari games. For example, one frame of Pong does not reveal the ball’s velocity and its moving direction as shown in Fig. 1(a). In the game of Asteroids (Fig. 1(b)), parts of the image is concealed for several consecutive frames to challenge the player. Hence, these games are naturally POMDP problems. While the strategy of DQN is to utilize several consecutive frames as the input in the hope of deducing the full state, this works well only when a short limited history is sufficient to characterize the state of the game. For more complex games, the performance of DQN decreases sharply.

To tackle problems with partially observable environments by deep reinforcement learning, Hausknecht and Stone [2015] proposed a framework called Deep Recurrent Q-Learning (DRQN) in which an LSTM layer was used to replace the first post-convolutional fully-connected layer of the conventional DQN. The recurrent structure is able to integrate an arbitrarily long history to better estimate the current state instead of utilizing a fixed-length history as in DQNs. Thus, DRQNs estimate the function \(Q(o_t, h_{t-1}|\theta)\) instead of \(Q(s_t, a_t|\theta)\), where \(\theta\) denotes the parameters of entire network, \(h_{t-1}\) denotes the output of the LSTM layer at the previous step, i.e., \(h_t = LSTM(h_{t-1}, o_t)\). DRQN matches DQN’s performance on standard MDP problems and outperforms DQN in partially observable domains. Regarding the training process, DRQN only considers the convolutional features of the history of observations instead of explicitly incorporating the actions. However, as we argued in Sec. 1 and Eq. 3 in Sec. 2.2, the action performed is crucial for belief estimation. To that effect, we propose a new architecture for deep reinforcement learning with actions incorporated in histories to further improve the performance of deep RL in POMDPs. In the sequel, we will refer to our proposed architecture as ADQN (action-specific deep recurrent Q-learning Network).

3 ADQN - Action-specific Deep Recurrent Q-Network

Inspired by the aforementioned works, our goal is to propose a model-free deep RL approach that incorporates the influence of the performed action through time. More specifically, we couple the performed action and the obtained observation as the input to the Q-network. The architecture of our model is shown in Fig. 2.

Our first attempt to couple the action and observation was to concatenate a fixed representation of the action with the observation vector directly, i.e., we utilized one-hot vectors to represent each action \(a \in A\). However, such concatenation did not yield good performance because the lengths of the action and observation vectors differ largely, which lead to numerical instability. In Atari games as well as many real-world POMDPs, the number of actions is far less than the dimensionality of the state representation. In conventional DQNs
Figure 2: The input action is an 18-D vector followed by a fully connected (IP) layer with 512-D outputs. A single 84 × 84 frame will be convolved as the observation via three convolutional layers with 32 8 × 8 filters with stride 2, and 64 4 × 4 filters with stride 1, respectively. The 512-D outputs of LSTM are fed to another fully connected layer and produce 18-D Q-values corresponding to 18 actions in Atari games.

and DRQN, the suggested dimensionality of the convolved features encoding the current state or observation is 3136 (after passing several convolutional and reshaping layers), while the number of actions is only 18 for the Atari games. To address this imbalance, we embed the one-hot action vectors by a fully connected layer into a higher dimensional vector (512-D is our experiments). Thus the representations of the actions and the observations are now more balanced.

Compared with DQN and DRQN, our model is able to remember the past actions, particularly the last performed action. Thus, we modified the transition \((s_t, a_t, r_t, s_{t+1})\) in the experience replay mechanism of the conventional DQN to \(\langle a_{t-1}, a_t, r_t, a_{t+1} \rangle\) in order to allow the framework to fetch the action-observation pair more conveniently. During the decision process for a given frame within training or the updating process of the neural network, the LSTM layer requires a sequence of action-observation pairs as its input. Thus, we store the transitions sequentially \(\langle a_{t-1}, a_t, r_t, a_{t+1} \rangle\) within each episode in the replay memory.

Ideally, the best strategy to estimate precisely the current state for a model-free POMDP problem is to integrate the entire transition history of each episode, which usually includes thousands of transitions for an Atari game. This also means that the LSTM layer needs to be unrolled for a large number of time steps which will increase significantly the training cost. In our experiments, the LSTM layer is unrolled for 10 time steps during training.

The entire process of our proposed approach is presented in Algorithm 1. First, we initialize the parameters of the Q-network and the Target network with \(\theta\) and \(\theta'\) respectively. For each episode, the first selected action is initialized to no-operation, the first hidden layer’s input is initialized with a zero vector and the first observation of each episode is initialized with the preprocessed first frame. At each time step, if the observation does not indicate “game over” (the end of the episode), we select an action based on the \(\epsilon\)-greedy strategy and execute the action. Accordingly, the immediate reward and the next observation of the screen will be obtained. The transition, once obtained, will be sequentially stored in the history of the current episode. To update the Q-network, we randomly sample a sequence of transitions \(\langle a_{j-1}, a_j, r_j, a_{j+1} \rangle\) to fit the unrolled LSTM layer. Then, the hidden layer \(h_{j-1}\) of the Q-network and the hidden layer \(h_j\) of the target network are obtained. The difference between these two network Q-values (i.e., Q-value \(y_j\) and Q-network value \(Q(h_{j-1}, a_{j-1}, a_j, \theta_j; \theta)\)) is used as the loss function to update the network parameters \(\theta\) via back propagation.

4 Experiments

In this section, we evaluate the training and testing performance of ADRQN with several Atari games and their flickering version.

4.1 Experiments setup

- **Flickering Atari game**: [Hausknecht and Stone, 2015] introduced a flickering version of the Atari games, which modified the Atari games by obscuring the entire screen with a certain probability at each time step, which introduces partial observability and therefore yields a POMDP. In their framework, before a frame is sent to the neural network as input, each raw screen is either fully observable or fully obscured with black pixels.

- **Frame skip Scheme**: We adopted the frame skip technique [Bellemare et al., 2013]. This mechanism is commonly used in most previous works of deep reinforce-
Algorithm 1 ADRQN

1: Initialize the replay memory $D$, # of iterations $M$
2: Initialize Q-Network and Target-Network with $\theta$ and $\theta^-$ respectively
3: for episode = 1 to $M$
4:     Initialize the first action $a_0 = no \ operation$,
5:     $h_0 = \emptyset$
6:     Initialize the first observation $o_1$ with the
7:     preprocessed first screen
8:     while $a_t \neq \text{terminal}$ do
9:         select a random action $a_t$ with the probability $\epsilon$
10:        else select $a_t = \arg\max_a Q(h_{t-1}, a_{t-1}, o_t, a_t; \theta)$
11:        execute action $a_t$
12:        obtain reward $r_t$ and resulting observation $o_{t+1}$
13:        store transition $(\langle a_{t-1}, o_t \rangle, a_t, r_t, o_{t+1})$ as one
14:        record of the current episode in $D$
15:        randomly sample a minibatch of transition sequences $(a_{j-1}, o_j, a_j, r_j, o_{j+1})$ from $D$
16:        compute Q-value of target network
17:        $y_j = \begin{cases} r_j, & o_{j+1} = \text{terminal} \\ r_j + \gamma \ \max_a Q(h_j, a_j, o_{j+1}; \theta^-), & o_{j+1} \neq \text{terminal} \end{cases}$
18:        compute the gradient of
19:        $(y_j - Q(h_{j-1}, a_{j-1}, o_j, a_j; \theta))^2$ to update $\theta$
20:     end while
21: end for

4.2 Training

Compared to the other approaches, the key idea of our framework is to construct action-observation pairs as input to the LSTM layer to retain more representative features for the Q-network to learn recurrently. The actions are first encoded with one-hot vectors, then processed by a fully connected layer to construct a higher-dimensional vector that is concatenated with the output of the third convolutional layer for better numerical stability. As the LSTM layer will be unrolled for 10 time steps, we need to ensure that there are enough transitions to be stored in the replay memory $D$ so that we can sample a minibatch of the transition sequences of length 10 each time we update the entire network. In our experiments, we update the entire network until the replay memory is full. Moreover, the scores obtained by playing the games are not always stable since small changes of the weights may have a significant impact on the outcome [Mnih et al., 2013]. Thus, we adopt an adaptive setting as done in most previous works by replacing negative rewards by -1 and positive rewards by +1.

When training the flickering versions of Atari games, we set the probability of obscuring a frame to 0.5 as a compromise. A lower probability may prevent learning due to a large loss of information, and a higher probability may be less convincing that the transformed version is a POMDP. Besides, it is a fair setting to evaluate generalization performance since it divides the test interval into two subintervals evenly. The games Pong and Chopper Command are both trained under the setting of full observation and a 0.5 probability of obscuring a frame. The training performances of Pong and Chopper Command are shown in Fig. 3 and 4 respectively. The reported scores are based on averages of 10 and 100 episodes respectively.

Fig. 3 shows that ADRQN matches the performance obtained by DRQN and DDRQN, and even performs slightly better than DRQN and DDRQN in the conventional setting (full observation), while the improvements of ADRQN over DRQN and DDRQN in partially observable settings are very obvious. Additionally, although the results shown in Fig. 4 indicate that all of the three models can not obtain significant improvements when the frames are always observed (over the partially observable case) in Chopper Command, we can still observe that ADRQN performs well when the environment is partially observable. In general, our proposed model can lead to higher scores in partially observable settings during the training process, which supports the argument that action-observation pairs are important in POMDP problems.

4.3 Testing Evaluation

We also evaluate the well-learned DRQN and ADRQN models on the three games and their flickering version. We replay each game based on the learned model 10 times to obtain the average scores as our final results. The epsilon value used in testing evaluation for $\epsilon-greedy$ is set to 0.05, which is less than that used in the training process since we consider the model to be well trained. Table 2 summarizes the results obtained with full observations. ADRQN outperforms DRQN in general. While Table 3 demonstrates that ADRQN significantly outperforms DRQN when trained with half of the...
frames obscured, an interesting observation is that the testing results are generally better than the results obtained during the training process for both DRQN and ADRQN. This may be explained by the fact that different distribution of the concealed frames may render the problem more or less observable, to the extent that better results may be obtained in some cases.

4.4 Generalization Performance

To further demonstrate the advantages of ADRQN in dealing with environmental changes, we evaluate the generalization performance of DRQN and ADRQN on the flickering versions of the games.

**POMDP to MDP Generalization:** After being trained with observation probability of 0.5, we test the learned policy in settings with observation probabilities (0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0). The results are shown in Fig. 5. We observe that both DRQN and ADRQN consistently perform better with the increase of observation probability. When the observable probability reaches 1.0, the results obtained are close to the performance obtained by training with full observations, which further demonstrates that both models can effectively respond to environmental changes. ADRQN consistently outperforms DRQN.

**MDP to POMDP Generalization:** After being trained as an MDP by setting the observation probability to 1, we test the learned policy with different settings of the observation probability. As shown in Fig. 6, both the performances achieved by DRQN and ADRQN drop sharply as we increase the amount of missing information. Fig. 6(a) clearly demonstrates that ADRQN is more robust than DRQN.

5 Conclusion

In this paper, we propose an action-specific deep recurrent Q-Network (ADRQN) to enhance the learning performance in partially observable domains. The actions are encoded via a fully connected layer and coupled with convolutional observations to form action-observation pairs. The time series of action-observation pairs are then integrated by an LSTM layer to infer the latent states, based on which Q-values are computed by a fully connected layer similar to conventional DQNs. We demonstrated the effectiveness of the approach in several POMDP problems, including flickering Atari games.
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