Layered semiconductors such as transition metal dichalcogenides (TMDs) offer endless possibilities for designing modern photonic and optoelectronic components. However, their optical engineering is still a challenging task owing to multiple obstacles, including the absence of a rapid, contactless, and the reliable method to obtain their dielectric function as well as to evaluate in situ the changes in optical constants and exciton binding energies. Here, we present an advanced approach based on ellipsometry measurements for retrieval of dielectric functions and the excitonic properties of both monolayer and bulk TMDs. Using this method, we conduct a detailed study of monolayer MoS$_2$ and its bulk crystal in the broad spectral range (290–3300 nm). In the near- and mid-infrared ranges, both configurations appear to have no optical absorption and possess an extremely high dielectric permittivity making them favorable for lossless subwavelength photonics. In addition, the proposed approach opens a possibility to observe a previously unreported peak in the dielectric function of monolayer MoS$_2$ induced by the use of perylene-3,4,9,10-tetracarboxylic acid tetrapotassium salt (PTAS) seeding promoters for MoS$_2$ synthesis and thus enables its applications in chemical and biological sensing. Therefore, this technique as a whole offers a state-of-the-art metrological tool for next-generation TMD-based devices.

**RESULTS**

Sample characterization

Monolayers of MoS$_2$ were prepared through chemical vapor deposition fabrication technology (Methods), leading to uniform, high-crystalline samples as confirmed by an exemplified optical raw data. SE has already been successfully applied to characterize TMDs. Although the results obtained show a similar trend of a dielectric function ($\varepsilon_1$), the absolute values of its real ($\varepsilon_1$) and imaginary ($\varepsilon_2$) parts differ by up to 50% between different measurements. These differences are caused by the sensitivity of the physical properties of TMDs to their dielectric surroundings, optically active defects, and the synthesis method. As a consequence, it is not clear which data should be used for the TMD-based device design; i.e., one has to measure optical constants for each sample in order to avoid mistakes. Hence, a reliable and reproducible technique for the TMDs dielectric function determination is in high demand.

In this work, we thus accurately investigated monolayer MoS$_2$ (synthesized via different methods) and found that the estimated values for optical constants are highly reproducible for the samples obtained under the same fabrication conditions. Apart from monolayer form, we also received optical constants for bulk MoS$_2$, which is now being actively investigated both theoretically and experimentally. Furthermore, optical constants of monolayer and bulk MoS$_2$ in near- to the mid-infrared region were determined and showed almost no absorption ($\varepsilon_2 = 0$) and high dielectric permittivity ($\varepsilon_1 > 12$ for monolayer and >16 for bulk), making this material an ideal platform for lossless subwavelength photonics in the infrared wavelength range. Besides, we present experimental evidence of the theoretically predicted transformation of the dark exciton into bright, which we explain by the presence of organic molecules on the monolayer.

**INTRODUCTION**

Two-dimensional (2D) materials possess unique electrical and optical properties, which make them suitable for a variety of practical applications in photonics and optoelectronics. In this regard, one of the most promising is a family of transition metal dichalcogenides (TMDs). These materials have already been successfully implemented in solar cells, ultrasensitive photodetectors, sensors, optical modulators, light emitters, and lasers, demonstrating even better performance than that of the devices based on graphene. Their low dimensionality confines electrons movement perpendicular to the layer and provides weak dielectric screening for the electric field outside the material, giving rise to strong Coulomb interaction. Therefore, upon light illumination, TMDs support tightly bound electron–hole pairs, named excitons, with the enormous binding energy of about 500 meV. Interestingly, not only monolayer but also bulk configurations of TMDs have an excitonic response, and, as a result, the high refractive index in the near- and mid-infrared spectral intervals following from large excitonic absorption and the Kramers–Kronig relations. More importantly, excitons play the dominant role in optical absorption, photoluminescence, and spin–valley dynamics in TMDs even at room temperatures allowing the room-temperature excitonic devices.

With such a broad range of optoelectronic applications, it is vitally important to precisely know optical constants of TMDs, i.e., real and imaginary parts of the dielectric permittivity, $\varepsilon_1$ and $\varepsilon_2$. Nevertheless, the accurate determination of the optical constants of these materials is nontrivial owing to their complicated excitonic structure. Nowadays, atomically thin TMDs are characterized by a variety of optical techniques such as photoluminescence, absorbance, and micro-reflectance spectroscopy. Nevertheless, the most convenient way for precise determination of optical constant is spectroscopic ellipsometry (SE) because it allows extracting the dielectric function in a broad wavelength range directly from the raw data. SE has already been successfully applied to characterize TMDs. Although the results obtained show a similar trend of a dielectric function ($\varepsilon_1$), the absolute values of its real ($\varepsilon_1$) and imaginary ($\varepsilon_2$) parts differ by up to 50% between different measurements. These differences are caused by the sensitivity of the physical properties of TMDs to their dielectric surroundings, optically active defects, and the synthesis method. As a consequence, it is not clear which data should be used for the TMD-based device design; i.e., one has to measure optical constants for each sample in order to avoid mistakes. Hence, a reliable and reproducible technique for the TMDs dielectric function determination is in high demand.

In this work, we thus accurately investigated monolayer MoS$_2$ (synthesized via different methods) and found that the estimated values for optical constants are highly reproducible for the samples obtained under the same fabrication conditions. Apart from monolayer form, we also received optical constants for bulk MoS$_2$, which is now being actively investigated both theoretically and experimentally. Furthermore, optical constants of monolayer and bulk MoS$_2$ in near- to the mid-infrared region were determined and showed almost no absorption ($\varepsilon_2 = 0$) and high dielectric permittivity ($\varepsilon_1 > 12$ for monolayer and >16 for bulk), making this material an ideal platform for lossless subwavelength photonics in the infrared wavelength range. Besides, we present experimental evidence of the theoretically predicted transformation of the dark exciton into bright, which we explain by the presence of organic molecules on the monolayer.
and scanning electron microscopy (SEM) images shown in Fig. 1c, d. Indeed, monolayer uniformly covers the oxidized silicon with an average crystallite size of 8.4 μm, confirming the high quality of the samples. Next, we validated that synthesized MoS₂ is atomically thin using atomic force microscopy (AFM) and resonant Raman spectroscopy. The measured topography in Fig. 1b yields 0.7 ± 0.2 nm for film thickness, which is consistent with the previous results for monolayer²¹,³². Also, the Raman spectrum in Fig. 1e reveals intense photoluminescence, which is a distinctive property of monolayer MoS₂ thanks to its direct bandgap and bulk counterparts²⁴. Besides, the characteristic Raman spectrum in Fig. 1f exhibits all the features inherent to molybdenum disulfide³⁷, with thickness-dependent vibrational modes $E_{2g}^{1}=384$ cm⁻¹ and $A_{1g}=404$ cm⁻¹ corresponding to a monolayer, and thereby certifies MoS₂ is a just one-layer thick.

Dielectric response analysis
To explore the dielectric response of the samples, we performed SE measurements (Fig. 1a) at multiple incident angles (Methods). In order to precisely retrieve the dielectric permittivity of MoS₂ from SE spectra and thus enable predictive capabilities for future optical engineering, it is imperative to introduce an accurate dielectric function model. The best route is to utilize the excitonic nature of the dielectric function, which is described by the TL oscillator model (Methods) since it captures the essential exciton features³⁸. It allows us to develop an algorithm described in the experimental section for MoS₂ dielectric response determination with the results displayed in Fig. 2. Apart from the dielectric function, we can analyze the peaks presented in the optical constants because our approach relies on the physical origin of the TMDs absorption, to be exact, on the material’s exciton resonances. As expected, all monolayer samples show similar behavior and values by that proving the reproducibility of the proposed method. Surprisingly, samples grown via PTAS-assisted technique have an additional peak at around 3.5 eV. Multiple experiments were conducted for different samples, and the additional peak appeared only for samples where PTAS molecules were used, as shown in Supplementary Fig. 3. Furthermore, we observed another peak at about 2.2 eV in all samples (with and without PTAS), which, to our knowledge, has not been reported in the literature on optical constants before. We assume that this peak is related to the excited states of A- and B-excitons. The latter have been theoretically predicted³⁵,⁴⁰ for the range 2.1–2.4 eV and experimentally observed in differential reflectance spectra for MoS₂ encapsulated between hexagonal boron nitride⁴¹. From Fig. 2b, we infer that the efficiency of this peak depends on the substrate. In particular, for MoS₂ samples on SiO₂/Si substrate, it is comparable with A- and B-excitons, while for those on quartz, it is barely visible in Fig. 2 (see Supplementary Fig. 1 for more details). Presumably, it is related to the interference effect caused by silicon oxide with the central wavelength $\lambda_0 \approx 570$ nm ($E = \hbar c/\lambda_0 \approx 2.2$ eV) defined by the Bragg–Snell law⁴². More importantly, the change of the substrate does not lead to the emergence of the peak at 3.5 eV for the samples synthesized without PTAS promoters; thus, it is independent of the substrate. Moreover, recent theoretical studies²⁴,⁴³ predicted that the environment

![Fig. 1](image-url) **Characterization of the monolayer sample.** a The scheme of the ellipsometry measurements. b AFM topography mapping and a cross-sectional profile of the edge of monolayer MoS₂ on SiO₂/Si substrate. The scan area was 4.5 × 2.1 μm². c Optical image of the MoS₂ on top of SiO₂/Si substrate. MoS₂ covers more than 97% of the surface. d SEM image of the MoS₂ revealing a high crystallinity of the samples with the crystallite size 8.4 ± 2.1 μm. e Photoluminescence of the monolayer MoS₂ due to the recombination of the A-excitons. High photoluminescence response due to monolayer MoS₂ being a direct gap semiconductor, unlike its bulk counterpart. f Resonant Raman spectrum of the MoS₂ film at excitation wavelength $\lambda = 632.8$ nm. The Raman spectral features are labeled according to Chakraborty and et al.³⁷. The positions of two first-order Raman modes, namely the $E_{2g}^{1}=384$ cm⁻¹ and $A_{1g}=404$ cm⁻¹, which are sensitive to the number of layers, correspond to a monolayer³⁷.
could transform dark states (i.e., ones that are not excited by light), into bright excitons, which can be excited with light, as could be in our case. These dark states usually are not accessible by light due to the required spin-flip and/or momentum transfer corresponding to spin- and momentum-forbidden electronic transitions. Nevertheless, Feierabend et al. theoretically demonstrated that the presence of organic molecules could change a momentum-forbidden dark exciton into a bright one, while our observation shows exactly the same trend: an additional peak at 3.5 eV appears only for monolayers MoS$_2$ with PTAS-molecules on top (see Supplementary Fig. 2).

In addition, our algorithm relies on the excitonic nature of absorption, permitting the track of individual exciton contribution into the dielectric function, as illustrated in Fig. 3a (see also the Methods section for more details). In the proposed approach, we exploit one TL oscillator for describing the individual excitonic transition. Therefore, each TL oscillator describes the physical properties of the corresponding exciton. More specifically, model parameters $E_0$ (oscillator central energy) and $C$ (oscillator broadening) giving a critical point and broadening, respectively. The best-fitting parameters are collected in Table 1 with the found critical points for the most studied A-, B-, and C-excitons in Fig. 3b.

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**Fig. 2** Optical constants of monolayer and bulk MoS$_2$ as a function of photon energy. a The real part $\varepsilon_1$ and b the imaginary part $\varepsilon_2$ of the dielectric permittivity. The inset in Fig. 2b shows a comparison with previously published works for the A- and B-excitons. c Refractive index $n$ and d extinction coefficient $k$. Due to the presence of the PTAS molecules, an additional peak at 3.5 eV appears in the dispersion. For the tabular data, see Supplementary Tables 2–6.

**Fig. 3** Excitonic contributions to dielectric function for the monolayer MoS$_2$ with PTAS from Fig. 2. a The imaginary part of the dielectric function and contributions from individual Tauc–Lorentz oscillators (excitons) in it. b Comparison of the position of critical points for A-, B-, and C-excitons obtained from the oscillator’s peaks (solid lines) and the previously published experimental and theoretical works.
showing an excellent agreement with previously reported experimental\textsuperscript{24,27,45} and theoretical\textsuperscript{46,47} studies. It is also worth noting that excited states of A- and B-excitons have small binding energies, and, as a result, their energy should be approximately equal to the Coulomb-renormalized bandgap energy. In our case, the central energy ($E_b = 2.3$ eV) of the oscillator linked to the excited states of A- and B-excitons matches with the theoretically predicted value $2.3$ eV by Berghauser and Malic\textsuperscript{40}. Moreover, using $2.3$ eV as bandgap energy, we determine the binding energies for A- and B-excitons: $E_b^{\text{binding}} / E_b^{\text{binding}} = 2.3 - E_b = 450$ meV, which agree well with the results of analytic calculations for MoS$_2$ on SiO$_2$ substrate ($E_b^{\text{binding}} / E_b^{\text{binding}} = 460$ meV)\textsuperscript{40}. Regarding the peak at $4$ eV, it has not been investigated theoretically so far; even so, it was observed in multiple experiments\textsuperscript{28,29,40}, but whether its nature is excitonic remains unknown. At the same time, the TL oscillator perfectly describes it (Fig. 3a) and, thus, our results suggest its relation to a high energy exciton.

Further, to demonstrate the predictive capabilities of our method for the far-field measurements, we recorded the transmission spectrum and compared it with the transfer matrix calculations\textsuperscript{48} employing the optical constants obtained from SE analysis in Fig. 4a. The measured and calculated transmittance spectra plotted in Fig. 4b match perfectly within a spectrophotometer accuracy (of only 1%). For a complete picture, we also determined optical constants for bulk MoS$_2$ shown in Fig. 2a by exploiting the point-by-point inversion\textsuperscript{19} (Methods) and calculated its critical points (see Supplementary Table 1) presented in Supplementary Fig. 3. Similarly to a monolayer, it has almost no absorption (from $1240$ nm and up to $3300$ nm) as well as strong dielectric response ($\varepsilon = 18$) comparable with traditionally used in nanophotonics semiconductors\textsuperscript{50}, including Si ($\varepsilon = 13$), Ge ($\varepsilon = 18$), and GaSb ($\varepsilon = 15$), at the important telecommunication wavelength interval 1525–1565 nm. In summary, the proposed method has a solid physical background—the excitonic nature of the optical response in MoS$_2$\textsuperscript{19} and, therefore, could be potentially applied for any TMDs due to their similarity in the formation of excitons upon light illumination\textsuperscript{51}.

**Discussion**

In this work, we have presented a broadband (290–3300 nm) SE of monolayer MoS$_2$ grown on SiO$_2$ by atmospheric pressure chemical vapor deposition and bulk MoS$_2$. In ellipsometry data analysis, we took into account the dominating influence of excitons on the optical response of monolayer materials and resulted in Kramers–Kronig-consistent dielectric functions. It allows us to provide an insight into the exciton physics of monolayer MoS$_2$. In particular, we have observed a previously unreported bright exciton appearing only in monolayer MoS$_2$ samples fabricated by the PTAS-assisted growth process. We speculate that this bright exciton is a result of the dark-to-bright exciton transformation induced by the leftover PTAS molecules. Our results prove that the optical properties of monolayer MoS$_2$ are strongly affected by the environment and the fabrication technology. On the other hand, for bulk MoS$_2$, we note a very high dielectric constant exceeding that of traditionally used Si, GaSb, and Ge in near-infrared, which, combined with zero optical absorption, makes this material very promising for applications in integrated nanophotonics. From a broader perspective, our technique opens up great opportunities to tailor an optical response from van der Waals heterostructures and applications of 2D materials in bio- and chemical sensing.

**METHODS**

**Materials**

Full area coverage monolayer samples purchased from the 2D Semiconductors Inc. and SixCarbon Technology. Samples from the 2D Semiconductors Inc. were synthesized by atmospheric pressure chemical vapor deposition (APCVD)\textsuperscript{11} on silicon wafers covered by a 285-nm-thick layer of SiO$_2$. During the synthesis, perylene-3,4,9,10-tetracarboxylic acid tetrapotassium salt (PTAS) was used to promote the nucleation and growth of MoS$_2$. At the same time, samples from the SixCarbon Technology were also synthesized with APCVD technology on sapphire (Al$_2$O$_3$) but without PTAS\textsuperscript{12}, and then transferred by water-assisted technique\textsuperscript{53} on SiO$_2$/Si substrate or quartz (SiO$_2$). Bulk 2H-phase MoS$_2$ crystals with low defect density, ultra-flat surfaces, and high crystallinity were also purchased from the 2D Semiconductors Inc.

**Samples characterization**

The SE measurements were performed on a variable-angle spectroscopic ellipsometer (VASE, J.A. Woollam Co.), as shown in Fig. 1a, over a wide wavelength range from 290 to 3300 nm (0.37–4.28 eV) in steps of 1 nm.

**Table 1.** Tauc–Lorentz parameters of the oscillators (excitons) from Fig. 3a ($\varepsilon_1^* = 2.84$).

| Oscillator | $A$ (eV) | $C$ (meV) | $E_0$ (eV) | $E_b$ (eV) |
|------------|----------|-----------|------------|-----------|
| #1 (A-exciton) | 142.1 | 51.5 | 1.744 | 1.858 |
| #2 (B-exciton) | 49.0 | 96.9 | 1.747 | 2.008 |
| #3 (Excited states of A- and B-excitons) | 23.6 | 463.7 | 1.526 | 2.308 |
| #4 (C-exciton) | 169.0 | 514.8 | 1.950 | 2.852 |
| #5 (Dark exciton) | 20.6 | 53.5 | 3.129 | 3.498 |
| #6 (E-exciton) | 1064.2 | 365.5 | 3.702 | 3.931 |

![Fig. 4 Predictive capabilities of the SE results for far-field calculations.](image-url)
The SE data were taken at multiple angles of incidence from 60° to 75° in steps of 5°. The thickness of each sample was independently determined by step height AFM measurements (NT-MDT Ntegra Aura). The quality of MoS$_2$ monolayer was assessed with a Horiba LabRAM HR Evolution confocal Raman microscope with He–Ne laser excitation ($\lambda = 632.8$ nm). The morphology characterization was performed by SEM (JEOL JSM-7001F), while the surface quality of the sample was evaluated by an optical microscope (Olympus BX51M). Cary 5000 UV–vis–NIR Spectrophotometer (Agilent Technologies) was used for recording transmittance spectra in the range of 290–2500 nm.

Ellipsometry analysis

The ellipsometry data for monolayer MoS$_2$ samples were analyzed as follows:

1. In this step, the number of layers is set. For our samples, we had three layers—Si, SiO$_2$, and MoS$_2$ (as it is shown in Fig. 1a). The upper one was the MoS$_2$ with the unknown optical constants and thickness of 0.7 nm obtained from AFM measurements shown in Fig. 1b. The interlayer had optical constants of silicon dioxide and a thickness of 285 nm. The substrate was a semi-infinite layer with the optical constants of silicon.

2. Note that some authors fit the thickness of the monolayer as well as optical constants$^{28,35}$. However, such an approach leads to overestimation or underestimation of the optical constants due to the high correlation between the thickness and optical constants for atomically thin samples$^{28,36}$, which allows one to reliably determine only the product of complex refractive index and the thickness from ellipsometry spectra alone.

3. Optical constants of the MoS$_2$ monolayer are fitted point-by-point$^{54}$ to ellipsometry spectra using the Levenberg–Marquardt algorithm.

4. Finally, the parameters of $N$ TL oscillators

\[
N = \frac{\Delta E C(E - E_0)}{\left( E - E_0 \right)^2 + C_1^2}
\]

where $E$ is the photon energy, $A$ is the strength of the oscillator, $C$ is the broadening term, $E_0$ is the optical band gap, and $E_0$ is the peak central energy. The real part $\varepsilon_1$ of the dielectric function is derived from the expression of $E_0$, using the Kramers–Kronig integration. Then, $\varepsilon_1$ is constructed as a step 2 via changing the constant $\varepsilon_1$ in order to take into account electronic transitions at higher energies. The advantages of TL oscillators in the case of TMDs are described in detail in our recent work$^{28,35,36}$.

Bulk MoS$_2$ was thick enough (~1 nm) for implementation of usual spectroscopic analysis for one interface problem by the formula$^{36}$

\[
\varepsilon_1 + i \varepsilon_2 = \sin^2 \psi \left( 1 + \tan^2 \varphi \left( \frac{1 - p}{1 + p} \right) \right)
\]

(2)

where $\varphi$ is the angle of incidence, $p$ is defined via ellipsometry equation

\[
\rho = \tan \psi \exp(i \Delta)
\]

(3)

where $\psi$ and $\Delta$ are the measured quantities in ellipsometry, showing the change of the light polarization after reflection from the sample. All ellipsometry analysis was carried out in a software package WAVASE$^{32,35}$.

The quality of the ellipsometry model is defined via mean squared error (MSE), which is given by

\[
MSE = \frac{1}{p - m} \sum_{j=1}^{p} \left( \rho_{\text{exp}} - \rho_{\text{cal}} \right)^2
\]

(4)

where $p$ is the total number of data points taken, $m$ is the number of fitting parameters, $\rho_{\text{exp}}$ and $\rho_{\text{cal}}$ are experimental and calculated values of the data point$^{36}$. A lower value of MSE represents a better match between the model and the experiment. For all our samples, MSE was in the range from 1 to 8, which, in the case of the complicated excitonic structure of the dielectric function of 2D materials, is a very good result. Since MoS$_2$ is an anisotropic material, what we obtained is the in-plane component of dielectric tensor because, according to the Snell law, due to a high refractive index of MoS$_2$, ~4, the refracted lightwave propagates almost normally to its surface. As a result, the electric field mostly interacts with the in-plane component, which justifies our isotropic treatment of the spectra.

DATA AVAILABILITY

The datasets generated during and/or analyzed during this current study are available from the corresponding author on reasonable request.

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**AUTHOR CONTRIBUTIONS**

Y.V.S., A.V.A., and V.S.V. suggested and directed the project with help from T.S. and A. Y.N. G.A.E. and Y.V.S. designed and fabricated the samples. G.A.E., D.I.Y., S.M.N., D.E.T., and Y.V.S. performed the measurements and analyzed the data. A.Y.N., T.S., A.A.V., and D.G.B. provided theoretical support. G.A.E., Y.V.S., A.A.V., D.G.B., T.S., A.Y.N., A.V.A., and V.S.V. contributed to the interpretation of the experimental results. G.A.E., A.A.V., and V.S.V. wrote the paper. All authors contributed to discussions and commented on the paper.

**COMPETING INTERESTS**

The authors declare no competing interests.

**ADDITIONAL INFORMATION**

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**Correspondence** and requests for materials should be addressed to V.S.V.

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