The JCMT BISTRO Survey: Magnetic Fields Associated with a Network of Filaments in NGC 1333

Yasu Doi1, Tetsuo Hasegawa2, Ray S. Furuya3, Simon Coude4, Charles L. H. Hull5, Doris Arzoumanian6, Pierre Bastien7, Michael Chun-Yuan Chen8, James Di Francesco9, Rachel Friesen10, Martin Howe11, Shu-ichiro Inutsuka12, Steve Mairs13, Masafumi Matsumura14, Takashi Onaka15, Sarah Sadavoy16, Yoshiho Shimajiri17, Mehrooosh Tahani18, Kohji Tomisaka19,20, Chakali Eswaraih21,22, Patrick M. Koch23, Kate Pattie24, Chang Won Lee25,26, Motohide Tamura27,30, David Berry28, Ta-Chung Chiu29,30, Jihye Hwang28,30, Wookjin Kwon28,31, Archana Soam28,32, Jia-Wei Wang28,32, Shih-Ping Lai26,32, Keeping Qiu33,34, Derek Ward-Thompson35,36, Do-Young Byun37,38, Jae-Hyun Yee39,40, Antonio Chrysostomou41,42, Keping Qiu33,43, Tie Liu44,45, Jason Fiege41, Erica Franzmann41,45, Takashi Onaka15,57, Tetsuya Zenko63, Chuan-Peng Zhang24,25, Masumichi Seta67, Kohji Tomisaka22,23, Keping Qiu33,34, Tie Liu61, Jason M. Kirk35, and Jean-François Robitaille72

1 Department of Earth Science and Astronomy, Graduate School of Arts and Sciences, The University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan
2 Institute of Astronomy and Astrophysics, Academia Sinica, 11F of Astronomy-Mathematics Building, AS/NTU, No. 1, Section 4, Roosevelt Rd., Taipei 10617, Taiwan
3 School of Astronomy and Space Science, Nanjing University, 163 Xianlin Avenue, Nanjing 210093, People’s Republic of China
4 Department of Physics, Engineering Physics and Astrophysics, Queen’s University, Kingston, ON, K7L 3N6, Canada
5 Department of Physics and Astronomy, Graduate School of Science, The University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan
6 Institute for Astronomy and Astrophysics, Academia Sinica, 11F of Astronomy-Mathematics Building, AS/NTU, No. 1, Section 4, Roosevelt Rd., Taipei 10617, Taiwan
7 National Astronomical Observatory of Japan, 676 Daedeok-dae-ro, Yuseong-gu, Daejeon 34055, Republic of Korea
8 Department of Physics and Astronomy, School of Science, The University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan
9 Department of Physics, Faculty of Science and Engineering, Meisei University, 2-1-2 Hodokubo, Hino, Tokyo 191-8506, Japan
10 Department for Physics, Engineering Physics and Astrophysics, Queen’s University, Kingston, ON, K7L 3N6, Canada
11 Department of Physics, Engineering Physics and Astrophysics, Queen’s University, Kingston, ON, K7L 3N6, Canada
12 Herzberg Astronomy and Astrophysics Centre, National Research Council Canada, 5071 West Saanich Rd., Victoria, BC V9E 1A1, Canada
13 KASI, 776 Daedeokdae-ro, Yuseong-gu, Daejeon 34055, Republic of Korea
14 National Radio Astronomy Observatory, 520 Edgemont Rd., Charlottesville, VA, 22903, USA
15 National Radio Astronomy Observatory, 520 Edgemont Rd., Charlottesville, VA, 22903, USA
16 National Radio Astronomy Observatory, 520 Edgemont Rd., Charlottesville, VA, 22903, USA
17 Division of Theoretical Astronomy, National Astronomical Observatory of Japan, Mitaka, Tokyo 181-8588, Japan
18 Department of Physics and Astronomy, The University of Western Ontario, 1151 Richmond Street, London, ON N6A 3K7, Canada
19 Department of Physics and Astronomy, The University of Western Ontario, 1151 Richmond Street, London, ON N6A 3K7, Canada
20 Department of Physics, Faculty of Science and Engineering, Meisei University, 2-1-2 Hodokubo, Hino, Tokyo 191-8506, Japan
21 Department of Physics and Astronomy, School of Science, The University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan
22 Department of Physics, Faculty of Science and Engineering, Meisei University, 2-1-2 Hodokubo, Hino, Tokyo 191-8506, Japan
23 Department of Physics, Engineering Physics and Astrophysics, Queen’s University, Kingston, ON, K7L 3N6, Canada
24 Division of Astronomical Sciences, School of Science, The University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan
25 National Astronomical Observatories, Chinese Academy of Sciences, People’s Republic of China
26 Department of Physics and Astronomy, University of Victoria, Victoria, BC V8P 1A1, Canada
27 National Astronomical Observatories, Chinese Academy of Sciences, People’s Republic of China
28 Korea Astronomy and Space Science Institute (KASI), 776 Daeedokdae-ro, Yuseong-gu, Daejeon 34055, Republic of Korea
29 University of Science and Technology, Korea, 217 Gajang-ro, Yuseong-gu, Daejeon 34113, Republic of Korea
30 KASI
31 Division of Astronomical Sciences, School of Science, The University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-0033, Japan
32 School of Astronomy and Space Science, Nanjing University, 163 Xianlin Avenue, Nanjing 210023, People’s Republic of China
33 School of Astronomy and Space Science, Nanjing University, 163 Xianlin Avenue, Nanjing 210023, People’s Republic of China
Abstract

We present new observations of the active star formation region NGC 1333 in the Perseus molecular cloud complex from the James Clerk Maxwell Telescope B-Fields In Star-forming Region Observations (BISTRO) survey with the POL-2 instrument. The BISTRO data cover the entire NGC 1333 complex (~1.5 pc × 2 pc) at 0.02 pc resolution and spatially resolve the polarized emission from individual filamentary structures for the first time. The inferred magnetic field structure is complex as a whole, with each individual filament aligned at different position angles relative to the local field orientation. We combine the BISTRO data with low- and high-resolution data derived from Planck and interferometers to study the multiscale magnetic field structure in this region. The magnetic field morphology drastically changes below a scale of ~1 pc and remains continuous from the scales of filaments (~0.1 pc) to that of protostellar envelopes (~0.005 pc or ~1000 au). Finally, we construct simple models in which we assume that the magnetic field is always perpendicular to the long axes of the filaments. We demonstrate that the observed variation of the relative orientation between the filament axes and the magnetic field angles are well reproduced by this model, taking into account the projection effects of the magnetic field and filaments relative to the plane of the sky. These projection effects may explain the apparent complexity of the magnetic field structure observed at the resolution of BISTRO data toward the filament network.

**Unified Astronomy Thesaurus concepts:** Interstellar medium (847); Interstellar magnetic fields (845); Interstellar filaments (842); Star formation (1569); Polarimetry (1278); Submillimeter astronomy (1647)

1. Introduction

It has long been recognized that the interstellar medium (ISM) is full of structures that can be identified as spatially elongated “filaments” (e.g., Schneider & Elmegreen 1979; Ungerechts & Thaddeus 1987; Abergel et al. 1994; Goldsmith et al. 2008; Schuller et al. 2009; Hennebelle & Falgarone 2012, for a review). Recent observations of thermal dust emission using Herschel revealed the omnipresence of filaments in the ISM, and more importantly their direct connection to star formation activity (e.g., André et al. 2010; Könyves et al. 2010; Men’shchikov et al. 2010;
Molinari et al. 2010; Miville-Deschênes et al. 2010; Arzoumanian et al. 2011; Peretto et al. 2012). Most (>70%) of the prestellar cores and Class 0 young stellar objects (YSOs) in low-mass star-forming clouds are located on filaments, especially in regions of the filaments that are thermally supercritical and thus gravitationally unstable (e.g., André et al. 2010, 2014; Könyves et al. 2015; Marsh et al. 2016). Additionally, YSOs show an age dependence with their distance to the nearest filament, which is consistent with the scenario that YSOs are born within these filaments and then drift away after birth with random relative velocities of \(\sim 0.1 \text{ km s}^{-1}\) (Doi et al. 2015; also see Stutz & Gould 2016).

All of these observations suggest that interstellar filaments play an essential role in the star formation process. Understanding the formation and evolution of these filaments is therefore crucial to understand the whole process of star formation.

Although the dominant mechanisms for filament formation and evolution are still under debate, many theoretical studies and numerical simulations suggest that interstellar magnetic fields (B-fields, hereafter) may play a significant role (e.g., Nagai et al. 1998; Kudoh & Basu 2008, 2011; Nakamura & Li 2008; Vázquez-Semadeni et al. 2011; Hennebelle 2013; Soler et al. 2013; Klassen et al. 2017; Inoue et al. 2018). Dense clouds are formed through collisional interactions in the ISM and the associated shock-compressed fluid dynamics. In this process, the B-field makes turbulent flows in the ISM more coherent along its field lines, naturally producing filamentary ISM structures that stretch in directions perpendicular to the mean B-field lines (see Hennebelle & Inutsuka 2019 for a recent review).

The plane-of-sky (POS) component of B-fields in dense molecular clouds can be traced by polarimetric observations of thermal continuum emission from interstellar dust particles (Heiles et al. 1993; Lazarian 2007; Hoang & Lazarian 2008; Matthews et al. 2009; Crutcher 2012). Aspherical dust particles irradiated by starlight are charged up by the photoelectric effect, as well as spun up as a result of radiative torques (RATs; Draine & Weingartner 1996; Draine & Weingartner 1997; Lazarian & Hoang 2007; Hoang & Lazarian 2008, 2014, 2016; Lazarian & Hoang 2008, 2019). These spinning particles are aligned with their rotation axes (i.e., their minor axes) parallel to the B-field orientation, resulting in preferential thermal emission polarized in the direction perpendicular to the field lines (Stein 1966; Hildebrand 1988).

Polarized dust emission thus can provide a direct trace of the morphology of the interstellar B-field. For example, some studies based on Planck and BLASTPol observations (e.g., Planck Collaboration et al. 2016a, 2016b, 2016c; Soler et al. 2017; Fissel et al. 2019) conclude that B-fields are observed to be mostly perpendicular to the long axes of dense filaments. Several ground-based polarimetry studies support these conclusions (Pattle et al. 2017; Ward-Thompson et al. 2017; Liu et al. 2018; Soam et al. 2019).

We note that the B-field angle derived from polarization observations is the true 3D angle projected onto the POS. To understand the actual structure of the B-field and its relationship with surrounding ISM, we need to take into account their respective 3D structures (e.g., Tomisaka 2015; Planck Collaboration et al. 2016b; Tahani et al. 2018). Moreover, Planck and BLASTPol observations have limited spatial resolutions (>2/5) that are not sufficient to trace the B-field orientation within filaments.

Despite the importance of high-resolution polarimetry of filaments, observational studies of polarized dust emission that can spatially resolve individual star-forming regions had previously been limited to only the brightest parts owing to sensitivity limitations (e.g., Matthews et al. 2009). The recent addition of a polarimeter (POL-2; Bastien et al. 2011; Friberg et al. 2016) to the Submillimeter Common-User Bolometer Array 2 (SCUBA-2) camera (Dempsey et al. 2013; Holland et al. 2013) on the James Clerk Maxwell Telescope (JCMT) now enables us to trace global B-field structures in star formation regions in greater detail (i.e., with spatial resolutions comparable to or below the spatial scale of prestellar cores).

To investigate the role of B-fields in the star formation process in light of its association with filaments, we use submillimeter polarimetry observations from the B-fields in STar-forming Region Observations (BISTRO) survey, which utilizes SCUBA-2/POL-2 at the JCMT. A full description of the survey is given by Ward-Thompson et al. (2017). This survey is designed to cover a variety of nearby star-forming regions, with an initial focus on the Gould Belt molecular clouds. The regions published so far are Orion A (Pattle et al. 2017), M16 (Pattle et al. 2018), \(\rho\) Ophiuchus A (Kwon et al. 2018), \(\rho\) Ophiuchus B (Soam et al. 2018), \(\rho\) Ophiuchus C (Liu et al. 2019), Perseus B1 (Coudé et al. 2019), and IC 5146 (Wang et al. 2019). In this paper, we present new observational results of the NGC 1333 star-forming region in the Perseus molecular cloud obtained by the BISTRO survey.

NGC 1333 is currently the most active site of ongoing star formation in the Perseus molecular cloud complex, and it is one of the most active star formation regions within 300 pc of the Sun (Ungerechts & Thaddeus 1987; Bally et al. 1996; Sun et al. 2006; Bally et al. 2008; Jørgensen et al. 2008; Walawender et al. 2008). This region shows a strong concentration of interstellar material and is often regarded as a “hub” in the filamentary network of the Perseus region (Myers 2009). Furthermore, NGC 1333 itself displays a complicated filamentary structure (Hacar et al. 2017; also see Figures 1 and 2 of this work).

Ortiz-León et al. (2018) estimated a distance to NGC 1333 of 293 ± 22 pc by using Gaia DR2 parallax measurements. Zucker et al. (2018; see also Zucker et al. 2019) combined Gaia data with stellar photometry for individual CO velocity components and derived an average distance to NGC 1333 of 299 ± 3 pc. Following these results, we assume the distance to the region to be 299 pc throughout this paper, which leads to a spatial resolution of 0.02 pc or 4200 au for the 14″1 JCMT beam at 850 \(\mu\)m (FWHM). The typical width of filaments suggested by Herschel observations is ∼0.1 pc (Arzoumanian et al. 2011; Juvela et al. 2012; Alves de Oliveira et al. 2014; Koch & Rosolowsky 2015; Federrath 2016; Arzoumanian et al. 2019), which can be well resolved by the JCMT beam. NGC 1333 is, therefore, a suitable area to study the relationship between filaments and B-fields over the whole star-forming area. We aim to clarify this relationship in this paper.

This paper is organized as follows. First, in Section 2, we describe our polarimetric observations of NGC 1333, the data reduction process, and verification of the data compared with other observations. In Section 3, we describe the spatial structure of the B-field revealed by our BISTRO observations, with a focus on its relationship to the structure of the filaments.
In Section 4, we compare our data with low- and high-resolution data derived from Planck, interferometers, and optical and near-IR observations and discuss the multiscale distribution of the $B$-field in and around NGC 1333. In Section 5, we introduce a simplifying model, in which the $B$-field pattern is simplified to two spatial scans. We observed the two fields with approximately uniform coverage with these fields between 2017 August 16 and 2018 January 16 as a part of the BISTRO large program (project ID: M16AL004). We observed field 1 in the earlier half of the observational campaign before 2017 November 25 and observed field 2 in the subsequent observational period. Twenty exposures ranging from 42.2 to 42.7 minutes were devoted to both field 1 and field 2, for a total observational time of 28.3 hr. The atmospheric opacity at 225 GHz ($\tau_{225}$) ranged between 0.03 and 0.07, among which five observations of field 1 and four observations of field 2 were performed under very dry weather conditions (Grade 1: $\tau_{225} < 0.05$), and others were performed under dry weather conditions (Grade 2: 0.05 $\leq \tau_{225} < 0.08$). We conducted the observations when the target elevation angle was $>30^\circ$. The noise level of the observed data has a loose correlation with the expected air emission. We find a $\sim30\%$ difference of the noise level corresponding to the estimated range of the air emission $\tau_{225} \cdot \sec(z) = 0.04$–0.09, where $z$ is a zenith angle of the target. Since the difference in the noise level is insignificant, we use all the observational data to estimate the polarized and the total intensity maps.

2. Observation and Data Reduction

2.1. Observation

We observed NGC 1333 in 850 $\mu$m continuum using SCUBA-2/POL-2 on the JCMT. The JCMT has a primary diameter of 15 m and achieves an effective angular resolution of $14\arcsec$ at 850 $\mu$m if we fit the beam with a single Gaussian profile (Dempsey et al. 2013). Its new polarimeter POL-2 on the bolometer array SCUBA-2 (Holland et al. 2013) achieves a superior sensitivity compared with the previous-generation instrument SCUBAPOL (SCUPOL; Bastien et al. 2011; Friberg et al. 2016).

We scanned the sky with POL-2 at a speed of $8^\prime$ s$^{-1}$ and a data sampling rate of 200 Hz with a POLCV_DAISY spatial scanning pattern, which covers a field that is roughly $11^\prime$ in diameter. For this paper, the flux calibration factor (FCF) of POL-2 at 850 $\mu$m is assumed to be 725 Jy pW$^{-1}$ beam$^{-1}$ for each of the Stokes $I$, $Q$, and $U$ parameters. This value was determined by multiplying the typical SCUBA-2 FCF of 537 Jy pW$^{-1}$ beam$^{-1}$ (Dempsey et al. 2013) by a transmission correction factor of 1.35 measured in the laboratory and confirmed empirically by the POL-2 commissioning team using observations of the planet Uranus (Friberg et al. 2016).

We observed NGC 1333 at two positions, namely, field 1 ($\alpha = 03^h29^m03^s450$, $\delta = 31^\circ14^\prime34^\prime700$) and field 2 ($\alpha = 03^h29^m06^s350$, $\delta = 31^\circ20^\prime22^\prime500$). The POLCV_DAISY footprint has a central 3$''$ diameter with uniform coverage, and then the coverage decreases approximately linearly to the edge at 5$''$ from the center. Since our two observed positions are $583^\prime$ apart, we cover the whole NGC 1333 region with approximately uniform coverage with these two spatial scans. We observed the two fields between 2017 August 16 and 2018 January 16 as a part of the BISTRO large program (project ID: M16AL004). We observed field 1 in the earlier half of the observational campaign before 2017 November 25 and observed field 2 in the subsequent observational period. Twenty exposures ranging from 42.2 to 42.7 minutes were devoted to both field 1 and field 2, for a total observational time of 28.3 hr. The atmospheric opacity at 225 GHz ($\tau_{225}$) ranged between 0.03 and 0.07, among which five observations of field 1 and four observations of field 2 were performed under very dry weather conditions (Grade 1: $\tau_{225} < 0.05$), and others were performed under dry weather conditions (Grade 2: 0.05 $\leq \tau_{225} < 0.08$). We conducted the observations when the target elevation angle was $>30^\circ$. The

2.2. Pipeline Data Reduction and Reridding

We derived the spatial distribution of the Stokes $I$, $Q$, and $U$ parameters from their time-series measurements by using the STARLINK procedure $pol2map$ (Parsons et al. 2018, software version on 2018 November 17), which is adapted from the SCUBA-2 data reduction procedure $makemap$ (Chapin et al. 2013). We estimated this distribution on a grid with $4'' \times 4''$ pixels, which is a standard for this analysis pipeline.

The grid of the pipeline output is considerably smaller than the spatial resolution of SCUBA-2/POL-2 ($14\arcsec$). To match the pixel scale of our map to the spatial resolution of SCUBA-2/POL-2 and improve the signal-to-noise ratios ($S/N$s), we resample the $I$, $Q$, $U$ data with a $7\arcsec$ grid by applying a 2D least-squares fit of a second-order polynomial using a Gaussian kernel with FWHM = $14\arcsec$. To propagate error values estimated by $pol2map$ through the nonlinear polynomial fitting and estimate the error of the resampled $I$, $Q$, and $U$ data, we perform a Monte Carlo simulation by assuming a Gaussian distribution for the $pol2map$-estimated error. We repeat the polynomial fitting 1000 times with Gaussian random errors at each resampled position. We take the mean of 1000 samples as the estimated values and the standard deviation as the estimation error of each position. The estimation error tends to be smaller for the signals with better $S/N$s, as those signals generally give better-fitting results. In other words, the error for low-$S/N$ signals is nonlinearly enhanced. As a result, we exclude these low-$S/N$ signals from the subsequent discussion (see below).

Using the resampled $Q$ and $U$ data, we estimate polarization intensity $PI$ and its standard error ($\delta PI$) as follows:

$$PI = \sqrt{Q^2 + U^2},$$

$$\delta PI = \frac{\sqrt{(Q^2 \cdot \delta Q^2 + U^2 \cdot \delta U^2)}}{PI}.$$

The $PI$ shown above is a biased estimator because the errors in $Q$ and $U$ are squared and thus offsets the derived $PI$. We debias the $PI$ value to estimate the true $PI$ as follows:

$$PI_{\text{debiased}} = \sqrt{PI^2 - \delta PI^2}.$$

If the $S/N$ is high (e.g., $PI/\delta PI > 3$), the difference between the $PI$ and $PI_{\text{debiased}}$ is negligibly small (Wardle & Kronberg 1974; Naghizadeh-Khouei & Clarke 1993; Vailancourt 2006). In the following, we refer to $PI_{\text{debiased}}$ as the polarized intensity and describe this as $PI$ for simplicity.

Based on this debiased $PI$, we estimate polarization fraction $P$, polarization angle $\psi$, and their standard errors ($\delta P$ and $\delta \psi$).
as follows:

\[ P = \frac{PI}{I}, \]

\[ \delta P = P \times \sqrt{\left(\frac{\delta PI}{PI}\right)^2 + \left(\frac{\delta I}{I}\right)^2}, \]

\[ \psi = 0.5 \times \arctan \frac{U}{Q}, \]

\[ \delta \psi = 0.5 \times \sqrt{(Q \cdot \delta U)^2 + (U \cdot \delta Q)^2} \frac{PI^2}{PF^2}. \]

We show the estimated spatial distributions of \( I \) and \( \psi \) in Figure 1 and that of \( PI \) in Figure 2. Since the typical rms noise in a Stokes \( I \) map for \( I < 25 \) mJy beam\(^{-1} \) is 2.3 mJy beam\(^{-1} \), we restrict our analysis in this paper to data where \( I \geq 25 \) mJy beam\(^{-1} \) (\( > 10\sigma \) compared to the background noise level). For the estimation of \( \psi \), we require \( PI/\delta PI \geq 3 \) in addition to the \( I \geq 25 \) mJy beam\(^{-1} \) threshold. For the restricted data with \( I \geq 25 \) mJy beam\(^{-1} \) and \( PI/\delta PI \geq 3 \), the typical rms noises are 1.1 mJy beam\(^{-1} \) for \( I \) and 0.9 mJy beam\(^{-1} \) for \( Q \) and \( U \), respectively. The minimum S/N value of \( I \) of the restricted data is \( (I/\delta I)_{\text{min}} = 13.7 \).

In the remainder of this paper, \( I, PI, P, \) and \( \psi \) are our observed values in 850 \( \mu \)m band unless otherwise stated.

2.3. Comparison with Previous SCUBA Results

Chrysostomou et al. (2004) observed NGC 1333 using SCUPOL. We compare our results with those obtained from archival data (Matthews et al. 2009) and check the consistency of the two data sets. Figure 3 shows the spatial distribution of two polarimetric data sets. The details of the comparison are described in Appendix A.

The observed \( Q \) and \( U \) values around IRAS 2 are nearly 0 for SCUPOL data, and we find a relative offset between SCUPOL and SCUBA-2/POL-2 of \( \sim 9 \) mJy beam\(^{-1} \) (see Appendix A and Figure A1). This offset leads to the difference in polarization angles between the two data sets around IRAS 2 (Figure 3).

By comparing our SCUBA-2/POL-2 data with interferometric observations with higher spatial resolutions (Hull et al. 2014), we find good consistency between the two data sets for all the regions including IRAS 2 (see Section 4.2 and Figure 11). Thus, the discrepancy in position angle between SCUBA-2/POL-2 and SCUPOL found at IRAS 2 is attributed to the measured offsets in \( Q \) and \( U \) values in the SCUPOL observations. We thus conclude that our BISTRO data from
SCUBA-2/POL-2 reliably trace polarized radiation and thus the B-field morphology in the observed region.

2.4. Comparison with the Total I, Q, U values Observed by Planck

The observed region in NGC 1333 has a size of $\sim 10' \times 20'$. Consequently, our observations are not sensitive to the diffuse emission, whose spatial scales are larger than the size of the observed region. Due to the need to remove the atmospheric signal, the pol2map pipeline estimates and subtracts a background signal in the observed region. This process further reduces the maximum spatial scale recovered to $\sim 5'$ and possibly is even lower (Chapin et al. 2013). In comparison, Planck Collaboration et al. (2018b) measured the total value of $Q$ and $U$, though with a low effective spatial resolution $\gtrsim 10'$ (Planck Collaboration et al. 2015, 2018a). Thus, both BISTRO and Planck data have complementary spatial scales.

We compare our JCMT 850 $\mu$m $I$, $Q$, and $U$ intensities with the Planck 353 GHz ($=850 \mu$m) observations to estimate the missing large-scale flux in our observational data. The details are described in Appendix B.

We find that the missing flux in $Q$ and $U$ makes a difference in the estimated B-field position angle at each position of $-0^\circ 2 \pm 8^\circ 2$ (the circular mean and the circular deviation). Note that throughout this paper, the mean and the standard deviation values of position angles are the circular means and
the circular standard deviations that are taking into account the 180° degeneracy of the polarization pseudo-vectors. The definitions of the circular mean and the circular deviation are given in Appendix C. The estimated offset value is negligible compared to the differences of the B-field orientation angles between individual filaments (see the discussion in Section 3.4), which means that the offset does not change the observed B-field morphology significantly.

3. Results

3.1. Spatial Distribution of I and PI

The estimated spatial distributions of I and PI are shown in Figures 1 and 2, respectively. The distribution of I shows an intricate filamentary structure throughout the observed region, which is in good agreement with results of previous JCMT/SCUBA-2 observations (e.g., the JCMT Gould Belt Survey; Hatchell et al. 2013). The spatial structure is dominated by components extending both parallel and orthogonal to the northwest–southeast direction. By eye, the physical scale of the filamentary structures we see is about 0.05–0.1 pc in width and about 0.3–0.5 pc in length. We will give quantitative identification of filaments and estimation of their physical scales in Sections 3.3 and 3.4.

Emission from known young stellar objects (YSOs) is also detected in I. The position and name of the main YSOs and infrared sources tabulated by Sandell & Knee (2001) are shown.

The filamentary structure of I is also well traced by PI (Figure 2). Indeed, we successfully detected the whole network of filaments in NGC 1333 in PI with an S/N of >3. To our knowledge, these data are the first time that polarized emission from entire filaments in a star formation region has been detected with a high spatial resolution of 0.02 pc. With these data, we can investigate in detail the relationship between filaments and the B-field for the first time.

While the distributions of I and PI show overall consistency with each other, there are also marked differences. For example, PI emission is noticeable in the south of SVS 13, but there is no corresponding distribution in I. On the other hand, in the region southeast of SVS 13, the PI emission is deficit compared to that of I. In the region northeast of SVS 13, we note a clear spatial break with the neighboring clamp. This break is found in both I and PI, as well as in, e.g., N$_2$H$^+$ line emission (Hacar et al. 2017). We reserve detailed investigations of these distributions for future studies.

3.2. Spatial Distribution of B-field

We show our observed B-field orientation in Figure 4 (white line segments). In the following, we assume that the polarized dust emission traces the POS orientation of the B-field due to RATs (Section 1), rotated by 90°. As shown in Figure 4, we
reveal a complicated B-field morphology associated with an intricate network of filaments in NGC 1333.

The orientation of the B-field shows a large diversity, which is shown as a broad distribution of the position angle histogram in Figure 5. The estimated circular mean and circular standard deviation of the orientation are $-46^\circ \pm 58^\circ$. The typical estimation error of the B-field orientation angle ($1\sigma$) is $4^\circ$ for the data with PL/\(\delta P\) > 5 and $5^\circ$ for the data with PL/\(\delta P\) > 3. The observed statistical scatter of the B-field orientation is much larger than the estimation error. The missing large-scale component that is not traced by the JCMT observations also cannot account for this large scatter, as the observation recovers almost all the total polarized emission (Section 2.4). Thus, we conclude that the B-field in NGC 1333 shows a large intrinsic diversity in its projected orientation.

A closer look at Figure 4 gives us the impression that the B-field orientation is not random on the smallest scale but instead appears to be correlated within individual filaments. For example, the B-fields around IRAS 4A, IRAS 4B, and IRAS 4C show perpendicular orientations with respect to the filament whose major axis is in a northwest—southeast direction. The B-fields around SVS 13A, SVS 13B, and SVS 13C are nearly orthogonal to the B-field around IRAS 4A, IRAS 4B, and IRAS 4C and also show nearly perpendicular orientations with respect to the filament whose major axis is in a northeast—southwest direction. On the other hand, the B-fields around HH 12 and its associated filament whose major axis is in a northwest—southeast direction show a nearly parallel orientation with respect to the filament.

Our earlier BISTRO observations of Orion indicate that B-fields lie orthogonal to filaments where the filament is gravitationally supercritical and aligned with the filament when the filament is gravitationally subcritical (Pattle et al. 2017; Ward-Thompson et al. 2017). In the following, we investigate the relative offset angle between the major axes of filaments and the B-field orientations, in light of the gravitational stability of individual filaments.

### 3.3. Identification of Emission Features

To examine the alignment of the B-field orientation with respect to the individual filaments described in Section 3.2 more quantitatively, we first need to identify ISM structures objectively. We identify local emission features (features, hereafter) in the Stokes I image. In addition to the I image, we refer to spectral line data and use radial velocity information to separate overlapping features projected on the POS. For this purpose, we adopt the N$_2$H$^+$ (1 − 0) line data taken at the IRAM 30 m Telescope with 30" spatial resolution and 0.08 km s$^{-1}$ spectral resolution (Hacar et al. 2017). We apply a density-based clustering method (Ester et al. 1996; Kriegel et al. 2011), which is an algorithm that can identify coherent data points above noise in a multidimensional space, to identify continuous emission features in the R.A.–decl.–V$_{LSR}$ datacube. Figure 6 shows the features identified with this method. A detailed description of the method is given in Appendix D, together with a justification for the choice of the spectral line.

As for feature #18, we arbitrary separate it into nearly straight parts, as indicated in Figure 6 (#18a, #18b, and #18c) to estimate the linear elongation of these features in later analyses (Section 3.4). We exclude #18c from the following analyses, as it is artificially defined, and hence it is difficult to estimate its actual orientation.
3.4. Local B-field Alignment to Filaments

Here we estimate the B-field orientations measured within the identified individual features. We analyze only the eight features with sizes $\geq 10$ independent beams so that we can estimate the mean position angles and the standard deviation of the B-field with reasonable accuracy.

We find that B-field orientations are self-consistent in particular directions for features #7, #13, #15, #18a, and #18b. In Figure 7, we show histograms of the B-field orientations measured within these features, together with their circular means (blue dashed lines) and circular standard deviations (blue dotted lines). The circular standard deviations of these orientations are $20^\circ$–$26^\circ$ (see Table 1). As shown in Figure 6, those features with concentrated B-field orientations have elongated spatial structures. Hereafter, we call these features “filaments.” We estimate the position angles of the major axes of the filaments by least-squares linear fits to their spatial structures in $I$, weighted by $I$ intensity. The estimated position angles are shown as red solid lines in Figure 7 (also see Table 1).

B-field orientations for other features, e.g., #9, #16, and #17, show more scattered distributions. In Figure 8, we show histograms of the B-field orientation measured within these features. Unlike the features described earlier, these show less apparent concentration in their B-field orientations. The circular standard deviations of these orientations are $34^\circ$ for feature #9, $52^\circ$ for feature #16, and $37^\circ$ for feature #17. We note that these features tend to be spatially isolated and less elongated, as seen in Figure 6. Thus, we cannot estimate well the position angles of these features. The observed B-field orientations in these features show radial (#17; IRAS 7) or random (#9, IRAS 2; #16, IRAS 5) distributions.

Previous studies concluded that the B-fields are observed to be mostly perpendicular to the main axis of dense filaments (e.g., Planck Collaboration et al. 2016a, 2016b, 2016c; Pattle et al. 2017; Soler et al. 2017; Ward-Thompson et al. 2017; Liu et al. 2018; Fissel et al. 2019; Soam et al. 2019). Three filaments in NGC 1333 (#7, #13, and #18b) show perpendicular B-field orientations, which is consistent with those studies. In our filaments, however, the B-fields are not always perpendicular to their major axes (e.g., #15 and #18a).

Here, we estimate the line mass of these filaments and their relative offset angle to the B-field, to compare our observations with the previous studies.

The estimated parameters of the filaments are shown in Table 1. We estimate the length and width of a filament based on the average distance of the filament data points along its major and minor axes from the center (arithmetic mean position) of the filament. These values correspond to half from the center of the filament to the endpoint. We thus multiply these values by four to estimate the length and width of the filament. The estimated widths are 0.06–0.07 pc, which is consistent with a typical observed width of filaments (Arzoumanian et al. 2011; Juvela et al. 2012; Palmeirim et al. 2013; Alves de Oliveira et al. 2014; Koch & Rosolowsky 2015; Arzoumanian et al. 2019).

We make a crude estimate of the mass of each filament by referring to the dust optical depth at 850 $\mu$m based on our $I$ map. We estimate the median value of $I$ in the background region ($I < 25$ mJy beam$^{-1}$; Section 2) and subtract that background value from the observed $I$. We refer an estimate of the dust temperature, whose spatial resolution is 36$''$, based on Herschel and Planck observations (Zari et al. 2016). The estimated dust temperatures range between 16.2 and 19.2 K, and the derived optical depths at 850 $\mu$m ($\tau_{850\mu m}$) range between $2 \times 10^{-4}$ and $2 \times 10^{-2}$. Thus, we assume an optically thin condition for the $I$ emission and estimate the column density by dividing $\tau_{850\mu m}$ by the dust opacity at 850 $\mu$m ($\kappa_{850\mu m}$) as follows: $N_H = \tau_{850\mu m}/\kappa_{850\mu m}$, where $\kappa_{850\mu m} = 8.0 \times 10^{-27}$ cm$^2$ H$^{-1}$ (Planck Collaboration et al. 2014; Nguyen et al. 2018). The estimated column density of each filament is shown in Table 1.

The total mass of each filament is estimated by summing up the derived column density encircled by the red contours in Figure 6. The estimated total mass and the line mass of each
Table 1

| ID # … | 7    | 13   | 15   | 18a  | 18b  |
|---------|------|------|------|------|------|
| Filament position angle (deg) | $-34.9 \pm 0.3$ | $42.9 \pm 1.7$ | $-32.3 \pm 0.7$ | $-18.1 \pm 0.1$ | $22.8 \pm 0.1$ |
| Length (pc) | 0.30 | 0.11 | 0.15 | 0.30 | 0.33 |
| Width (pc) | 0.074 | 0.059 | 0.064 | 0.066 | 0.069 |
| Column density ($10^{23}$ H-atom cm$^{-2}$) | $2.2 \pm 1.7$ | $5.4 \pm 5.3$ | $1.2 \pm 0.8$ | $2.1 \pm 1.7$ | $1.0 \pm 0.8$ |
| Mass ($M_\odot$) | 35 | 29 | 10 | 32 | 16 |
| Line mass ($M_\odot$ pc$^{-1}$) | 118 | 260 | 66 | 106 | 49 |
| Field position angle (deg) | $30 \pm 26$ | $-24 \pm 22$ | $-54 \pm 20$ | $-52 \pm 20$ | $-76 \pm 20$ |
| [Field − Filament Offset Angle$^g$ (deg) | $65 \pm 26$ | $67 \pm 22$ | $22 \pm 20$ | $34 \pm 20$ | $82 \pm 20$ |

Notes.

$^a$ The position angle estimated by an $I$-weighted linear fit to their spatial structures.

$^b$ Length and width are the length of the filaments along their major and minor axes.

$^c$ The column density of each filament estimated by converting $\tau_{\text{500um}}$. The mean and the standard deviation values are shown. See text for the conversion factor between $\tau_{\text{500um}}$ and the column density.

$^d$ The mass per unit length of each filament estimated as mass/length.

$^e$ The mass of each filament estimated as the sum of the column density.

$^f$ The circular mean position angle of the B-field and filament.

$^g$ The absolute angular difference between filament position angle and B-field position angle.

---

Figure 8. Same as Figure 7, but for the features that show relatively scattered B-field position angles (the circular standard deviation of the position angles $>30^\circ$).

Figure 9. Planck-observed B-field orientations in the Perseus molecular cloud (Planck Collaboration et al. 2018a) are shown as black line segments. Here, we set the spatial resolution of the Planck data as a $10^\prime$ FWHM Gaussian to achieve good S/N. The assumed beam ($10^\prime$) is shown in the upper left corner of the figure. Color scale is the dust optical depth at 353 GHz estimated by Zari et al. (2016). The western half of the Perseus molecular cloud complex is shown in this figure. Our observed area at NGC 1333 is marked in white.

We estimate the B-field orientation of a filament as the circular mean and the circular standard deviation of the B-field pseudo-vectors observed at the filament. The projected offset angles between the B-field and filaments tend to be large ($65^\circ$–$82^\circ$ for three filaments), which is consistent with the previous Planck and BLASTPol studies. Some of them, however, are significantly small ($22^\circ$ for #15 and $34^\circ$ for #18a), though their line masses are estimated to be $>60 M_\odot$ pc$^{-1}$ (Table 1). They are typical gravitationally supercritical filaments, and thus their parallel orientation to the local B-field is not in accordance with the Planck and BLASTPol observations. We present a possible model to explain the interesting projected offset angle distributions that we find for the massive filaments in NGC 1333 in Section 5.

4. Multiscale B-field Structures

Our polarization map covers a 1.5 pc $\times$ 2 pc region with a 0.02 pc spatial resolution. In this section, we compare the
B-field orientations from our polarization map with those from maps with broader spatial coverage or higher spatial resolution.

4.1. Global and Local B-field Observed with Planck, Optical, Near-infrared, and JCMT

We show the large-scale B-field observed across Perseus with Planck in Figure 9. As shown in the figure, Planck observed a fairly uniform global B-field for the whole Perseus molecular cloud, whose size is >10 pc (Planck Collaboration et al. 2018a).

The effective spatial resolution of the Planck data (10°) corresponds to ~0.87 pc at the distance of NGC 1333. On the other hand, the spatial resolution of the BISTRO data with JCMT is 14°1, which corresponds to ~0.020 pc, or ~43 times finer than that of Planck. Here, we compare the BISTRO B-field across NGC 1333 with the global B-field observed with Planck.

We show the Planck B-field in Figure 4 (yellow line segments) and its position angles in Figure 5 (black dotted lines), in addition to the BISTRO B-field. The Planck B-field orientation shows a smoothly and slowly varying field distribution with a position angle of ~41° ± 10° in our observed NGC 1333 area. This distribution is in contrast with the much more diverse one observed with SCUBA-2/POL-2, which shows a significantly larger scatter (~46° ± 58°). As described in Section 3.2, the large scatter in the B-field observed with JCMT is due to neither the observational uncertainties nor the missing large-scale flux that is not detected by JCMT. Thus, we conclude that the B-field orientation in NGC 1333 becomes significantly more complex at spatial scales below 1 pc.

Fluctuations in the B-field structure in a dense molecular cloud on <1 pc scales are also found by optical and near-infrared polarimetry as shown in Figure 10. Optical polarimetry of the Perseus molecular cloud around NGC 1333 by Goodman et al. (1990) and other references therein shows two different populations of polarization position angles. One population has a peak at ~−39° ± 15°75 and agrees with the B-field orientation obtained by Planck in the diffuse medium in the whole Perseus molecular cloud. It is also approximately parallel to many filaments such as #15 and #18a (Figure 7) and is characterized by a larger polarization percentages of P > 1.5% in the optical. The other population has a broader peak in position angles at 60° ± 25° (see footnote 75), has smaller polarization percentage values, and corresponds to field orientation with a perpendicular orientation to its major axis (see, e.g., filament #7). The two populations of vectors show no spatial distinction across the Perseus cloud complex. They coexist in projection throughout the entire Perseus cloud.

The near-infrared polarimetry by Alves et al. (2011) mainly covers a small area with a 5' diameter, south of the IRAS 4A and IRAS 4B protostars, while that by Tamura et al. (1988) covers a large area around NGC 1333. Both observations show B-field orientations peaking at ~−15° to ~−30°, in agreement with the Planck data near that position but almost perpendicular to the B-field at the protostars IRAS 4A and IRAS 4B.

Note that the Planck data measure the polarization from all dust grains visible in the effective 10°-wide beam covered by Planck, but optical and near-infrared polarimetry measures dichroic extinction of light by dust in a pencil-beam along the line of sight (LOS) to individual stars background to the cloud. This comparison with our JCMT map thus demonstrates that the field orientation inside dense molecular clouds shows considerable variation, which is in accordance with the finding mentioned above that the B-field is significantly distorted on scales <1 pc inside NGC 1333.

This distortion of the B-field is likely due to the interaction of the field with gas flows associated with filament formation and evolution. We will discuss this possibility in Section 6.

4.2. Continuity of the B-field at Scales between 0.1 pc and 1000 au

Here, we compare our observations with the B-field orientations observed around YSOs by radio interferometers at higher spatial resolution. In Figure 11, we display the B-field structure as measured at 1.3 mm around IRAS 4A, IRAS 4B, SVS 13A, SVS 13B, and IRAS 2A: five young, embedded

---

75 The standard deviations given here are the arithmetic standard deviations estimated by Goodman et al. (1990). The arithmetic standard deviation and the circular standard deviation are not significantly different from each other if their values are 15° and 25° (see Appendix C and Figure C1).
Class 0 YSOs observed as part of the TADPOL survey (Hull et al. 2014) using the Combined Array for Research in Millimeter-wave Astronomy (CARMA; Bock et al. 2006). See Table 2 for the parameters of TADPOL data shown in Figure 11. The spatial resolution of the BISTRO ($\lambda = 14$ pc) data corresponds to 0.020 pc or 4200 au in these regions, while that of the TADPOL observation ($\lambda = 3$ au) corresponds to 0.0035–0.0051 pc or 720–1000 au at the distance of NGC 1333.

As found in Figure 11, our observed $B$-fields at $\geq 4200$ au scales are in good accordance with those observed by TADPOL, although our data exhibit a smoother distribution owing to the difference in spatial resolution. To check this consistency in further detail, we show histograms of $B$-field orientations observed with TADPOL in Figure 12, together with $B$-field orientations observed with BISTRO at the positions of various YSOs. The comparison between the TADPOL and the BISTRO $B$-fields is summarized in Table 3. The $B$-field orientations of SVS 13A and SVS 13B show clear differences from those of other locations in NGC 1333. The differences between the orientations of IRAS 4A, IRAS 4B, and IRAS 2A are not statistically significant, but they do show significantly different orientations from those of the global $B$-field observed by Planck ($\pm 7^\circ$; Section 4.1). The distribution of the $B$-field orientations that differ for each region is similar to that observed by BISTRO (Section 3.4).
Table 2
Parameters of CO (2–1) Emission Maps (Hull et al. 2014) Shown in Figure 11

| Region       | Beam Size (arcsec) | Intensity (mJy beam$^{-1}$) | Noise Level | Velocity (K km s$^{-1}$) | Redshifted Velocity Range (km s$^{-1}$) | Blueshifted Velocity Range (km s$^{-1}$) |
|--------------|--------------------|----------------------------|-------------|--------------------------|-----------------------------------------|----------------------------------------|
| IRAS 4A      | 2.52 × 2.33        | 10.9                       | 2.41        | 11.2 – 3.8               | –4.6 – –14.2                             |
| IRAS 4B      | 2.65 × 2.45        | 7.3                        | 3.12        | 22.5 – 9.8               | 3.4 – 12.5                               |
| SVS 13A & 13B| 3.49 × 3.18        | 3.6                        | 0.59        | 27.0 – 19.6              | –6.9 – –12.2                             |
| IRAS 2A      | 3.84 × 3.22        | 2.4                        | 2.07        | 27.0 – 10.1              | 2.6 – 5.8                                |

Figure 12. Comparison of B-field orientations observed by TADPOL and BISTRO for individual YSOs. Histograms are the orientations observed by TADPOL. Spatially independent line segments among those given in Figure 11 are shown. Thin blue dashed lines are the circular mean orientation of the TADPOL B-field, and thin blue dotted lines are the circular standard deviation around the mean value (±1σ). Thick red dashed lines are the B-field orientations at the YSO sources observed by BISTRO with 14″1 spatial resolution.

The observed circular standard deviation of the B-field orientation angle (18°–33°) is comparable to those in individual filaments observed with BISTRO (20°–26°; Table 1).

The BISTRO-observed B-field orientation angle at the position of each YSO with 14″1 spatial resolution agrees well with that observed by TADPOL (Figure 12 and Table 3). This consistency is also found in the previous observations of IRAS 4A (Minchin et al. 1995; Tamura et al. 1995; Girart et al. 1999; Chrysostomou et al. 2004; Attard et al. 2009) up to a maximum spatial resolution of 1″56 × 0″99 (∼500 au × 300 au) achieved by SMA (Girart et al. 2006). Considering the significant diversity of B-field orientation at spatial scales below 1 pc, we thus note that these field variations are continuous and follow the larger B-field structure as we go to smaller scales down to 1000 au (see also Galametz et al. 2018).

4.3. Misalignment of the B-field and Outflows from YSOs

Hull et al. (2013) and Hull & Zhang (2019, and references therein) examined the correlation between the direction of molecular outflows and B-fields in YSOs for a compilation of 30 low- and intermediate-mass sources in various regions in the whole sky. They found that the correlation is best explained by random orientations of outflows and B-fields. On the other hand, Galametz et al. (2018) observed a sample of 12 low-mass Class 0 envelopes in nearby clouds using the SMA and pointed out that the envelope-scale B-field is preferentially either aligned with or perpendicular to the outflow direction (e.g., Bally 2016; Lee et al. 2017; Pudritz & Ray 2019). Bipolar outflows are launched by the rotating accretion disk of the protostar and thus could be used to infer the orientation of the rotation axis (e.g., Bally 2016; Lee et al. 2017; Baug et al. 2020; Pudritz & Ray 2019). Accordingly, we can investigate further this correlation by studying how the rotation axes at the very centers of the NGC 1333 star formation cores are aligned and possibly influenced by the B-field orientation in the protostellar envelope (scale ∼ 1000 au).
Here, we compare outflow orientations with the B-fields observed with the JCMT toward all of the protostars with active outflows in NGC 1333. An advantage of our analysis with respect to that of Hull & Zhang (2019) is that we can compare outflow versus B-field orientation toward a large number (19) of protostars in a single star-forming region.

Stephens et al. (2017) examined the correlation of 57 position angles between CO (2–1) molecular outflows, observed by SMA at 1.3 mm wavelength, and local filaments for the entire Perseus cloud, including NGC 1333. They concluded that their correlation indicates random orientations of outflows with respect to filaments. Among these, we find 19 outflows in our observational field (Figure 13), including five outflows shown in Figure 11. We estimate the B-field orientation at each position of YSOs from our JCMT data with 14°1 spatial resolution. We assume that the BISTRO observations, though their spatial resolutions are ~4200 au, can trace the B-field orientation down to ~1000 au scale based on the discussion in Section 4.2.

Figure 14 shows the cumulative distribution function (CDF) of the projected angles between the outflows from Stephens et al. (2017) and the B-field orientations we measure with the JCMT. As shown in the figure, the CDF is consistent with random orientations. This random distribution is in accordance with previous studies (Ménard & Duchêne 2004; Curran & Chrysostomou 2007; Poidevin et al. 2010; Targon et al. 2011; Hull et al. 2013, 2014; Hull & Zhang 2019) and thus reconfirms the detachment of rotation axes at the centers of the star-forming cores from the larger-scale B-fields at ~1000 au protostellar envelope scales.

5. B-field Associated with Filaments in a Three-dimensional Space

Theoretical studies suggest that dense filaments form perpendicularly to the local B-field (Hennebelle & Inutsuka 2019 for a review). Since the observed position angles of B-fields and filaments are the results of projection onto the POS, it is important to understand the true 3D morphologies of such structures as a first step (Tomisaka 2015). Here, we make the simplifying assumption that the B-field lines are indeed perpendicular to the dense filaments in NGC 1333 (Section 3.4) and show that our observed offset angles can be explained by considering different inclination angles for these filaments with respect to the POS. Note that our model presented here is purely geometrical and does not take into account physical properties of filaments.

5.1. Effect of the 3D Orientation of the B-field and the Filament on the Observed Projected B-field Angle

Figure 15 shows our assumed configuration of a filament and a B-field in a 3D space. Tomisaka (2015) showed that a projected offset angle between a B-field and a filament (α in Figure 15) can be different from 90° even when they are perpendicular with each other in a 3D space, if we observe a filament that is inclined relative to the POS.
In Figure 15, we indicate the definition of relative angles that were introduced by Tomisaka (2015). The angle $\theta$ is the relative inclination angle of a filament with respect to the LOS. The angle $\phi$ is the rotation angle about the long axis of the filament. Tomisaka (2015) defined $\phi = 0^\circ$ when a $B$-field, which is orthogonal to the filament, is parallel with respect to the POS and perpendicular with respect to the LOS (see Figure 15(b)). These two angles ($\theta$ and $\phi$) are the two independent parameters that determine the orientation of a set of the filament and the $B$-field in a 3D space. The relative orientation angle between the filament and the $B$-field we observe is the projected angle onto the POS, as indicated in Figure 15(b). Tomisaka (2015) defined this projected offset angle as $\alpha$. The angle $\alpha$ is estimated as a function of $\theta$ and $\phi$ as follows:

$$\alpha = \frac{\pi}{2} - \arctan[\tan(\phi) \cdot \cos(\theta)] .$$

(1)

The angle $\gamma$ is the relative inclination angle of the $B$-field with respect to the POS. $\gamma$ is a dependent parameter of $\theta$ and $\phi$, as is the case of $\alpha$. The following equation expresses the relationship between these parameters:

$$\sin(\gamma) = \sin(\phi) \cdot \sin(\theta) .$$

(2)

As indicated in Equation (1), $\alpha$ can be significantly less than $90^\circ$ when $[\tan(\phi) \cdot \cos(\theta)] \gg 0$, in other words, $\theta < 90^\circ$ and $\phi > 0^\circ$. In that case, Equation (2) indicates that $\gamma > 0^\circ$ unless $\theta = 0^\circ$. That means that both the filament and the $B$-field are inclined with respect to the POS if the observed $\alpha$ is smaller than $90^\circ$. As a result, our model requires that a filament and the $B$-field both be inclined with respect to the POS if nearly parallel orientation between the filament and the $B$-field is observed. If the relative orientation between the filament and the $B$-field is orthogonal, our model requires that either or both the filament and the $B$-field be in the POS.

**5.2. Probability Distribution of Offset Angle Projected to the POS**

Here we estimate the probability distribution of observed offset angle $\alpha$ if the combination of a filament and a $B$-field shown in Figure 15 is randomly oriented in a 3D space. We then discuss the consistency of this probability distribution with the values observed by BISTRO and Planck.

Suppose a filament is on the POS and perpendicular with respect to the LOS ($\theta = 90^\circ$). In this case, $\alpha$ is always $90^\circ$ regardless of the value of $\phi$ (the rotation angle about the long axis of the filament). Thus, the associated probability distribution shows a strong concentration at $90^\circ$. On the other hand, if a filament is nearly parallel with respect to the LOS and perpendicular with respect to the POS ($\theta \approx 0^\circ$), $\alpha$ becomes any value depending on the value of $\phi$. Thus, the associated probability distribution is uniform between $0^\circ$ and $180^\circ$ in this case.

For other values of $\theta$, the associated probability distributions are between these two extreme cases. The distribution shows a loose concentration to $\alpha = 90^\circ$ (the perpendicular projected orientation of the filament and the $B$-field), and the degree of concentration increases at larger $\theta$. In Figure 16, we show the probability distribution of $\alpha$ for $\theta = 30^\circ$ (the dotted line in the figure) and $\theta = 60^\circ$ (the dashed line in the figure).

When filaments are oriented randomly in a 3D space, the distribution of their inclination angle $\theta$ is more likely to be $90^\circ$ and less likely to be $0^\circ$ with a dependence of $P(\theta) \propto \sin(\theta)$. Taking into account this dependence, we estimate the probability distribution of $\alpha$ when the inclination and rotation angles ($\theta$ and $\phi$) of filaments are completely random, as shown in Figure 16 as a solid line. As shown in the figure, the $\alpha$ value shows a higher probability to be perpendicular than to be parallel. The probability that $\alpha$ is observed to be perpendicular ($\alpha = 90^\circ \pm 30^\circ$) is $66\%$, while the probability that $\alpha$ is observed to be parallel ($\alpha = 0^\circ \pm 30^\circ$) is $14\%$.

This higher probability in perpendicular orientation is consistent with the preferentially perpendicular orientation of the $B$-field with respect to the dense filaments found in Planck, BLASTPol, and ground-based observations (Planck Collaboration et al. 2016a, 2016b, 2016c; Patte et al. 2017; Soler et al. 2017;
Figure 16. Probability distributions of the projected offset angle $\alpha$ between the filament and the $B$-field. The solid line indicates the total probability assuming random orientation of both the filament and the $B$-field while keeping their relative angle as $90^\circ$. The dashed line shows the probability when $\theta = 60^\circ$. Keeping the inclination angle of the $B$-field with respect to the POS $\gamma = 30^\circ$ gives the same probability distribution. The dotted line shows the probability for $\theta = 30^\circ$ or $\gamma = 60^\circ$.

The Astrophysical Journal, 899:28 (23pp), 2020 August 10

Doi et al.

Ward-Thompson et al. 2017; Liu et al. 2018; Fissel et al. 2019; Soam et al. 2019). Thus, our model, where we assume that a filament and the $B$-field are orthogonal in a 3D space, can successfully reproduce these observational results.

We can also consider a random orientation of filaments in a globally uniform $B$-field with a fixed inclination angle $\gamma$ to the POS. In our model, the filament and the $B$-field are orthogonal straight lines and thus interchangeable. As a result, probability distributions for fixed $\theta$ shown in Figure 16 (the dotted line for $\theta = 30^\circ$ and the dashed line for $\theta = 60^\circ$) also demonstrate probability distributions for fixed $\gamma$ with random orientation of filaments. The dotted line corresponds to the case of $\gamma = 60^\circ$, and the dashed line corresponds to the case of $\gamma = 30^\circ$.

Referring to the Planck-oberved $\alpha$ distribution of star formation regions, we note that the level of concentration around $90^\circ$ is different from region to region (see probability distributions shown in Figures 3 and 4 of Planck Collaboration et al. 2016c). This difference in concentration is consistent with our estimated probability distributions for different $B$-field inclination angles (fixed-$\gamma$ cases in Figure 16). Thus, the difference could be attributable to the difference in the inclination angle of the large-scale local $B$-field.

In NGC 1333, we find that three out of five cases are perpendicular and one or two cases are parallel (Table 1). This result is roughly consistent with the probability expected from random orientation of both filaments and the $B$-field. Also, the case of $\gamma = 30^\circ$ (the dashed line in Figure 16) gives nearly the same probability as $P[\alpha = 90^\circ \pm 30^\circ] = 55\%$ and $P[\alpha = 0^\circ \pm 30^\circ] = 18\%$.

We thus claim that filament formation in a global $B$-field that has $\sim 30^\circ$ inclination with respect to the POS is a plausible scenario to explain the observed distribution of polarization vectors associated with filaments in NGC 1333. The considerable variation in the $B$-field orientations of individual filaments within NGC 1333 suggests that the $B$-field may locally be modified by filaments, most probably due to their formation and evolutionary processes. Our model thus indicates that filaments, which may form in random orientations, are likely to modify the $B$-field locally but keep the relative orientation between the local $B$-field and filaments perpendicular to each other.

6. Discussion

Our data reveal for the first time a complex $B$-field structure across the entire star formation region of NGC 1333. This network is found on scales smaller than the smooth distribution of the global $B$-field probed by Planck (Section 4.1). For scales of $\sim 1-0.01$ pc, the complex $B$-field structure observed by BISTRO shows overall consistency with archival interferometric observations with higher spatial resolutions (Section 4.2). Here, we discuss possible causes of this increasing complexity of the $B$-field at smaller scales.

One possible cause is a dynamical interaction of the molecular outflows from YSOs, which may perturb the surrounding ISM and thus affect the $B$-field morphology. For example, it has been proposed that molecular outflows can disrupt the parent clouds around YSOs and terminate star formation (“stellar feedback”; e.g., Colin et al. 2013).

In Figure 11, we plot CO molecular outflows associated with some NGC 1333 YSOs, together with the local $B$-fields observed by both BISTRO and TADPOL. We find, however, no sign of gas interaction in the observed $B$-field morphologies shown in Figure 11. This lack of interaction is also the case for the $B$-field morphology of the entire NGC 1333 region (Figure 13; see also Poidevin et al. 2010), although many outflows are found in NGC 1333 (Knee &Sandell 2000; Hatchell & Dunham 2009; Arce et al. 2010; Curtis et al. 2010; Plunkett et al. 2013). Two exceptions, however, include the warped $B$-field morphologies seen around HH 12 and SVS 3, which could be due to interactions with local ISM, i.e., an outflow from SVS 13B (HH 12, e.g., Walawender et al. 2008) and a reflection nebula around SVS 3, respectively.

Another possible cause is a deformation of the $B$-field associated with individual filaments, as we demonstrated that the observed local $B$-field intersects with individual filaments with uniform offset angles in a 3D space (Section 3.4). Furthermore, we recognize that the filaments and local $B$-fields are presumably perpendicular to each other (Section 5).

We show a spatial scale dependence of the angular dispersion of the $B$-field orientations in NGC 1333 in Figure 17. The angular deviation is significant at spatial scales below $\sim 0.3$ pc, which corresponds to the typical length of the filaments (Table 1). This trend becomes more prominent if we select the data points whose central positions are on the filaments in NGC 1333 (“filament” in Figure 17). The angular dispersions of “filament” show no further considerable increase at smaller scales, suggesting that the $B$-field associated with filaments mainly deforms at the scale of the filament length and keeps its structure below that scale.

Indeed, the observed spatial scale dependence of the $B$-field structure in NGC 1333 is consistent with a proposed mechanism for creating a filamentary cloud. In an ideal MHD regime, gas flows along the $B$-field onto the cloud much faster than perpendicular to the field. As a result, long structures can be formed even in a highly supersonic environment, with the $B$-fields acting as both the guiding rails of gas flow and the reinforcement. The outcome is a long filamentary cloud with a $B$-field oriented roughly perpendicular to the long axis of the cloud (e.g., Inutsuka et al. 2015; Inoue et al. 2018; Li & Klein 2019). These studies show that the
projection effect can lead to incorrect interpretations of the physical shape of the clouds.

In fact, large-scale shock compression of the Perseus molecular cloud, including NGC 1333, is suggested by other observations. The LOS velocity distributions of H I and CO lines suggest compression of the molecular cloud by an expanding ISM shell associated with the Per OB2 association (Sancisi 1974; Sun et al. 2006; Shimajiri et al. 2019). Furthermore, the LOS B-field morphology around the molecular cloud (Tahani et al. 2018; see also Tahani et al. 2019) hints at deformation of the large-scale B-field by the compressed molecular cloud.

Deformation of the B-field at the filament length scale and the uniform B-field orientations associated with individual filaments suggest that the formation and evolutionary process of filaments cause significant changes in the B-field morphology with respect to the global B-field observed by Planck. Once a filament is formed, the filament and its B-field maintain a constant angular orientation down to protostellar cores. The existence of filaments in NGC 1333 that are misaligned with each other suggests that the compression mechanism may have acted multiple times with different overall orientations (Inutsuka et al. 2015), which caused the complicated configuration of the B-field in NGC 1333.

Our model, in which we assume the perpendicular orientation of filaments and the associated B-field, is in good accordance with our observations. The model, however, does not exclude the possibility that filaments and the B-field may have relative orientations that differ from perpendicular. By checking the applicability of our model to other regions where observational data of sufficient spatial resolution are available, we can better examine the plausibility of this model.

A diffuse ISM cloud, which is subcritical against magnetic pressure, becomes supercritical if its column density exceeds a threshold value of \( N_H \sim 10^{21} \text{ cm}^{-2} \) (Crutcher 2012). The ISM in this column density range can be the site of filament formation. We should keep in mind that our observations with the JCMT are limited to regions of \( N_H > 10^{23} \text{ cm}^{-2} \), which are much higher than the threshold value. To achieve a thorough understanding of the filament formation process, we should aim at making direct observations of the B-field in the ISM with column densities down to \( 10^{21} \text{ cm}^{-2} \) at high spatial resolution. HAWC+ on board SOFIA pioneers polarimetry of low column density gas around bright star-forming regions (e.g., Chuss et al. 2019; Santos et al. 2019). Extensive observations can be conducted by future space-borne facilities (e.g., André et al. 2019; Leisawitz et al. 2019).

7. Conclusions

We performed submillimeter polarimetric observations using SCUBA-2/POL-2 at the JCMT and revealed the POS projections of the B-field of the active star formation region NGC 1333 as a part of the BISTRO survey. Our observations cover spatial scales of about 0.02–1 pc, which are crucially important for the formation of the filaments in the star-forming ISM. These data mark the first time that the B-field structure across an entire star formation region has been revealed on these spatial scales.

We draw the following conclusions:

1. We detect polarized emission \( PI \) from an intricate network of filaments in the observed region (\( \sim 1.5 \text{ pc} \times 2 \text{ pc} \)) with a column density above \( \sim 10^{22} \text{ H cm}^{-2} \).
2. While the observations by Planck revealed a rather uniform and slowly varying B-field structure over the entire Perseus molecular cloud, our observations show a highly complex B-field structure in NGC 1333. This difference cannot be attributed to the missing flux in the JCMT observations. We instead propose that the B-field changes its intrinsic structure on scales <1 pc.
3. The observed B-fields around active YSOs with the JCMT (4200 au resolution) show overall consistency with higher spatial resolution interferometric data (1000 au resolution), indicating that the B-field structure remains broadly continuous between \( \sim 1 \text{ pc} \) and 1000 au spatial scales.
4. We find no correlation between the B-field position angles near YSOs as traced by BISTRO and the rotation axes of the YSOs as inferred from molecular outflows.
5. The B-fields associated with individual filaments show a uniform orientation angle that is not equal to the orientation angles of the global B-field or those of other filaments. Projected offset angles of local B-fields to filaments are also different from filament to filament, ranging from orthogonal to nearly parallel.
6. We successfully reproduce the observed variety of offset angles by using a simple model, in which the B-field and the long axis of a filament are perpendicular to each other.
in a 3D space. Since the observed offset angle is a projection of the true state of affairs onto the POS, the observed angle can be significantly narrower than 90°. It can even be nearly parallel (0°) if both the B-field and the filament are significantly inclined with respect to the POS. Random orientations of the B-field and filaments in a 3D space can reproduce the observed distribution of the offset angle. A B-field that has a constant inclination angle of ~30° with respect to the POS and a random orientation of filaments can also reproduce consistently the observed distribution of the offset angle.

7. We demonstrate that observed offset angle is more likely to be perpendicular than to be parallel, even if the filament and the B-field are perpendicular with each other in a 3D space but randomly oriented with respect to the LOS. This result is consistent with previous observations using Planck and BLASTPol that showed that offset angles tend to be perpendicular. Random orientations of filaments in a B-field that have a constant inclination angle with respect to the POS show different probability distributions of the offset angle, ones that are relatively less likely to be perpendicular if the B-field has a larger inclination angle with respect to the POS. This different inclination angle of the B-field can be an explanation of the differences of the offset angle distribution between regions found by Planck observations.

The authors thank the anonymous referee for their advice and suggestions, which improved the manuscript. The James Clerk Maxwell Telescope is operated by the East Asian Observatory on behalf of the National Astronomical Observatory of Japan; Academia Sinica Institute of Astronomy and Astrophysics; the Korea Astronomy and Space Science Institute (KASI); the Operation, Maintenance and Upgrading Fund for Astronomical Telescopes and Facility Instruments, budgeted from the Ministry of Finance (MOF) of China and administrated by the Chinese Academy of Sciences (CAS); and the National Key R&D Program of China (No. 2017YFA0402700). Additional funding support is provided by the Science and Technology Facilities Council of the United Kingdom and participating universities in the United Kingdom and Canada. SCUBA-2 and POL-2 were built through grants from the Canada Foundation for Innovation. This research used the facilities of the Canadian Astronomy Data Centre operated by the National Research Council of Canada with the support of the Canadian Space Agency. This research has also made use of the SIMBAD database and of NASA’s Astrophysics Data System Bibliographic Services. Part of the data analysis was carried out on the open-use data analysis computer system at the Astronomy Data Center, ADC, of the National Astronomical Observatory of Japan. This research has been supported by Grants-in-Aid for Scientific Research (25247016, 18H01250, 19H01938) from the Japan Society for the Promotion of Science and a crowdfunding run by academist project No. 25 (https://academist-xf.com/projects/25). Simon Coudé is supported by the Université Sciences Research Association, which operates the SOFIA Science Center under contract NNA17BF53C with the National Aeronautics and Space administration. C.L.H.H. acknowledges the support of both the NAOJ Fellowship and JSPS KAKENHI grant 18K13586. Doris Arzoumanian acknowledges support by FCT/MCTES through national funds (PIDDAC) by the grant UID/FIS/04434/2019. F.K. and L.F. acknowledge support from the Ministry of Science and Technology of Taiwan, under grant MoST107-2119-M-001-031-MY3 and from Academia Sinica under grant AS-IA-106-M03. C.W.L. is supported by the Basic Science Research Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Education, Science and Technology (NRF-2019R1A2C1010851). M.K. was supported by Basic Science Research Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Science, ICT & Future Planning (No. NRF-2015R1A1A01052160). Di Li acknowledges support by NSFC grant No. 11725313. W.K. was supported by the New Faculty Startup Fund from Seoul National University and by the Basic Science Research Program through the National Research Foundation of Korea (NRF-2016R1C1B2013642).

Facilities: JCMT (SCUBA-2/POL-2), Planck, CARMA, SMA, IRAM.
Software: Starlink (Currie et al. 2014), astropy (Astropy Collaboration et al. 2013), dbscan (Hahsler et al. 2019).

Appendix A

Comparison with Previous SCUBA Results

The detection of the polarized emission with SCUPOL 
(Chrysostomou et al. 2004) was limited to the regions around 
SVS 13, IRAS 2, and IRAS 4, which are particularly bright 
objects (see Figure 3). In contrast, our SCUBA-2/POL-2 data 
trace the global distribution of I and PI across the entirety of 
NGC 1333, meaning that we have achieved a significant 
 improvement in sensitivity from SCUPOL to SCUBA-2/POL-2. 
To make a direct comparison of the two data sets, we regrid 
the I, Q, and U data of SCUPOL with the same procedure that 
was applied to our SCUBA-2/POL-2 data and obtain I, Q, and 
U maps with the same spatial grids. Note that archival data of 
SCUPOL are raw data in units of volts and not corrected for the 
variation of the FCF values, which may vary by ~20% between 
individual exposures (see Section 3 of Matthews et al. 
2009). The uncertainty of each sample is not archived. 
Therefore, we assume constant uncertainty for I, Q, and U 
values, respectively, and apply intensity-weighted fits for 
regridding. We estimate the observational error as the statistical 
scatters of fitting residuals for the regridding.

We show the correlations between SCUPOL and SCUBA-2/ 
POL-2 in Figure A1 to check the consistency of the two data 
sets. The estimated correlations are

\[ I_\text{SCUBA-2/POL-2} [\text{mJy beam}^{-1}] = (227 \pm 18) \cdot I_\text{SCUPOL} + (\pm 156 \pm 68) [\text{mV}] \]

\[ Q, U_\text{SCUBA-2/POL-2} [\text{mJy beam}^{-1}] = (165 \pm 12) \cdot Q, U_\text{SCUPOL} + (1 \pm 2) [\text{mV}] \].

The estimated FCF values for SCUPOL data (227 ± 18 for I 
and 165 ± 12 for Q and U) are within the 20% variation of the 
expected FCF value for SCUPOL (207 ± 13 Jy beam^{-1} V^{-1} ;
Jenness et al. 2002). See Section 2.3 for the discussion on the 
offsets in Q and U between SCUBA-2/POL-2 and SCUPOL 
and the resultant B-field position angle difference around 
IRAS 2.
Appendix B

Comparison with the Total I, Q, U Values Observed by Planck

To estimate the missing large-scale flux that is not recovered by JCMT, we compare our JCMT 850 μm I, Q, and U intensities with the Planck 353 GHz (=850 μm) observations (Planck Collaboration et al. 2018b). We assume a circular beam with a diameter of 14″ for the JCMT data and convert them to units of surface brightness [MJy sr⁻¹]. For the Planck data, we transform the original Planck Q and U data that are given in Galactic coordinates to the values in equatorial coordinates to make the comparison. We refer to Table 2 of Planck Collaboration et al. (2018b) for the intensity unit conversion and color correction. The correction factor assumes a modified blackbody spectrum with a spectrum index of β_d = 1.5 and a dust temperature of T_d = 19.6 K.

The spatial extent of our observed area is not enough to correlate the JCMT and Planck data, as the effective spatial resolution of Planck polarimetry data (10′) is comparable to the size of our observation region. Therefore, we estimate the Stokes I, Q, and U intensities at the center of our observed region (R.A. = 3h29m00s, d ecl. = 31°17′00″) with 10′ spatial resolution for both BISTRO and Planck data and estimate the offsets.

The estimated values are

\[ I_{\text{Planck}} = 23 \, \text{MJy sr}^{-1}, \quad I_{\text{JCMT}} = 20 \, \text{MJy sr}^{-1}, \]
\[ Q_{\text{Planck}} = -0.13 \, \text{MJy sr}^{-1}, \quad Q_{\text{JCMT}} = 0.008 \, \text{MJy sr}^{-1}, \]
\[ U_{\text{Planck}} = 0.42 \, \text{MJy sr}^{-1}, \quad U_{\text{JCMT}} = 0.03 \, \text{MJy sr}^{-1}. \]

The spatially smoothed I, Q, and U of the JCMT are always smaller in absolute values compared to those of Planck, supporting that the observation by JCMT does not recover the
large-scale component of the emission. The estimated offsets then become

\[
I_{\text{Planck-JCMT}} = 2.69 \text{ MJy sr}^{-1} \\
= 9.9 \text{ mJy (14''1 - beam)}^{-1}, \\
Q_{\text{Planck-JCMT}} = -0.14 \text{ MJy sr}^{-1} \\
= -0.51 \text{ mJy (14''1 - beam)}^{-1}, \\
U_{\text{Planck-JCMT}} = 0.39 \text{ MJy sr}^{-1} \\
= 1.42 \text{ mJy (14''1 - beam)}^{-1}.
\]

The estimated offsets of \( I \) are significant (\( \sim 4\sigma \)), while those of \( Q \) and \( U \) are comparable to the uncertainties in our data. For example, the median values of the uncertainties are \( \delta Q = 0.88 \text{ mJy beam}^{-1} \) and \( \delta U = 0.91 \text{ mJy beam}^{-1} \), respectively. Thus, the offset values estimated above correspond to 0.58\( \sigma \) and 1.56\( \sigma \), respectively, or less than two times the observational errors. The difference between the B-field position angles with and without considering the offset values is \( -0.2 \pm 8.2^\circ \) (the circular mean and the circular deviation) if we restrict our analysis to the data with \( PI/\delta PI \gtrsim 3 \), which is applied to the discussion of \( \psi \) throughout this paper.

**Appendix C**

**Definitions of the Circular Mean and the Circular Standard Deviation of Polarization Pseudo-vectors in Directional Statistics**

To summarize the statistical distributions of polarization position angles, we need to take into account the 180° degeneracy of the polarization pseudo-vectors. This accounting is especially necessary where the pseudo-vectors have large-angle variations, which is the case for NGC 1333. For example, if we estimate the standard deviation of randomly distributed angles, the estimated deviation saturates at \( \pi/\sqrt{12} \text{ [rad]} \) = 51°56' and does not represent the actual angular variation (Serkowski 1962; Poidevin et al. 2010).

We can utilize directional statistics to avoid this difficulty (see also Tang et al. 2019). In the directional statistics, each angle \( \theta_i \) is represented by a unit vector whose phase angle is \( \theta_i \). We can sum the individual vectors and estimate the mean angle as the direction of the resultant vector. Thus, the circular mean position angle \( \bar{\theta} \) is defined as follows:

\[
\tan(2\bar{\theta}) = \frac{\sum_{i=1}^{n} \sin(2\theta_i)}{\sum_{i=1}^{n} \cos(2\theta_i)}.
\]

Note that we need to take into account the 180° degeneracy of the pseudo-vectors instead of the 360° degeneracy of normal vectors, and thus we multiply the individual angles by 2.

The mean resultant length of the composite vector \( \bar{R} \), which is the length of the resultant vector divided by the number of vectors \( n \), is defined as follows:

\[
\bar{R} = n^{-1} \sqrt{\left( \sum_{i=1}^{n} \cos(2\theta_i) \right)^2 + \left( \sum_{i=1}^{n} \sin(2\theta_i) \right)^2}.
\]

If the distribution of angles \( \theta_i \) has no deviation (\( \theta_i \equiv \) const. and unit vectors are totally aligned), the mean resultant length \( \bar{R} = 1 \). On the other hand, \( \bar{R} = 0 \) if \( \theta_i \) are totally random. Thus, \( \bar{R} \) can be used as an indicator of the angle deviation.

When the distribution of \( \theta_i \) follows a wrapped normal distribution, which is a normal distribution around the unit circle, \( \bar{R} \) is expressed as follows (e.g., Mardia & Jupp 1999):

\[
\bar{R} = \exp\left(-\frac{(2\nu)^2}{2}\right),
\]

where \( \nu \) is the standard deviation of the normal distribution. Note that we multiply \( \nu \) by 2 in this equation because we estimate the angle variation of \( 2 \times \theta_i \).

The circular standard deviation \( \nu \), which is the standard deviation of the position angles, is then defined as follows:

\[
\nu = \sqrt{-2 \ln \bar{R}}.
\]

This definition is useful because \( \nu \) equals the (normal) standard deviation when the deviation is much smaller than the 180° ambiguity of the pseudo-vectors.

We display a comparison between the normal standard deviation and the circular standard deviation in Figure C1. While the normal standard deviation saturates at 52°, the circular standard deviation correctly estimates the standard deviation of the population distribution even if the deviation exceeds 50°.

**Appendix D**

**Identification of Emission Features Using Density-based Clustering**

We identify emission features in the observed region by applying a clustering analysis to a 3D distribution of ISM emission. The spatial structure of the ISM is well traced by the observed 850 \( \mu \text{m} \) continuum intensity (\( I_{850,\mu\text{m}} \); see Figure 4). To separate overlapping ISM features projected on the POS, we utilize LOS velocity information from molecular line emission.
Hacar et al. (2017) estimated the 3D structure of the ISM in the NGC 1333 region by using $N_2H^+$ molecular line data. The data have a spatial resolution of $30''$ and a spectral resolution of 0.08 km s$^{-1}$. We show the correlation of $I_{850 \mu m}$ and an integrated intensity of $N_2H^+$ ($I_{N_2H^+}$) in Figure D1. Note that we smooth $I_{850 \mu m}$ to the spatial resolution of $I_{N_2H^+}$ ($30''$) and show the data where we estimate the B-field position angles ($PI/ SPI \geq 3$) in this figure.

As seen in Figure D1, most of the data points show tight correlation between $I_{850 \mu m}$ and $I_{N_2H^+}$ (black filled circles in the figure). On the other hand, there are some data points that are out of the correlation (gray filled circles in the figure). The deviating points are the data in the reflection nebula around two B-type stars BD $+30^\circ$459 and SVS 3 ($<2''$ from one of the two). Black filled circles are the data points from other regions.

Thus, we conclude that the $N_2H^+$ emission is a good tracer of the ISM also traced by $NH_2$ as a tracer of the LOS distribution of the ISM as was done by Hacar et al. (2017). Note that we evaluate the spatial structure of ISM traced by $I_{850 \mu m}$ with a $14''$ resolution, while the spatial resolution of $N_2H^+$ data is $30''$. To construct a 3D position–position–velocity (PPV) datacube, we regrid the $N_2H^+$ data and estimate the line profile at each $I_{850 \mu m}$ data point. The line profiles are scaled so that the integrated intensities are equal to $I_{850 \mu m}$ at each position.

To identify the 3D structure of the ISM, we apply a statistical cluster analysis on the obtained PPV datacube. We utilize density-based clustering (Ester et al. 1996; Kriegel et al. 2011) to the data set. It is a general statistical method that recently has begun to be applied to classify astronomical sources in a multidimensional data space (e.g., Beccari et al. 2018, 2020; Jerabkova et al. 2019). This method can identify clusters in a multidimensional space not only for their crests but also for their spatial extent, without assuming that their underlying spatial structures are filamentary or clumpy. Thus, this method is suitable to extract ISM structures from our PPV datacube. We convert the PPV intensity data into discrete values in units of 5 mJy beam$^{-1}$ and apply the density-based clustering to this data set. We show the result of this density-based clustering in Figure D2. The main ISM structures in the region are successfully extracted. A drawback of this method based on the LOS velocity is that it cannot identify ISM structures with large velocity dispersion. For example, we cannot identify the structure at and around the IRAS 4 complex, and the cloud that contains IRAS 2 is fragmented. These misidentifications are attributable to perturbation by active YSOs. Thus, the identified structures shown in Figure D2 represent quiescent ISM structures in the region.

ORCID iDs

Yasuo Doi @ https://orcid.org/0000-0001-8746-6548
Tetsuo Hasegawa @ https://orcid.org/0000-0003-1853-0184
Ray S. Furuya @ https://orcid.org/0000-0003-0646-8782
Simon Coudé @ https://orcid.org/0000-0002-0859-0805
Charles L. H. Hull @ https://orcid.org/0000-0002-8975-7573
Pierre Bastien @ https://orcid.org/0000-0002-0794-3859
Michael Chun-Yuan Chen @ https://orcid.org/0000-0003-4242-973X
James Di Francesco @ https://orcid.org/0000-0002-9289-2450
Rachel Friesen @ https://orcid.org/0000-0001-7594-8128
Martin Houde @ https://orcid.org/0000-0003-4420-8674
Shu-ichiro Inutsuka @ https://orcid.org/0000-0003-4366-6518
Steve Mairs @ https://orcid.org/0000-0002-6956-0730
masafumi Matsumura @ https://orcid.org/0000-0002-6906-0103
Takashi Onaka @ https://orcid.org/0000-0002-8234-6747
Sarah Sadavoy @ https://orcid.org/0000-0001-7474-6874
Yoshito Shimajiri @ https://orcid.org/0000-0001-9368-3143
Meenhoosh Tahani @ https://orcid.org/0000-0001-8749-1436
Kohji Tomisaka @ https://orcid.org/0000-0003-2726-0892
Chakali Eswaraiah @ https://orcid.org/0000-0003-4761-6139
Patrick M. Koch @ https://orcid.org/0000-0003-2777-5861
Kate Pattle @ https://orcid.org/0000-0002-8557-3582
Chang Won Lee @ https://orcid.org/0000-0002-3179-6334

---

Figure D1. Correlation between the 850 $\mu$m continuum intensity and the integrated intensity of the $N_2H^+$ line (Hacar et al. 2017). Gray filled circles are the data points around the two B-type stars BD $+30^\circ$459 and SVS 3 ($<2''$ from one of the two). Black filled circles are the data points from other regions.
Dempsey, J. T., Friberg, P., Jenness, T., et al. 2013, MNRAS, 430, 2534
Doi, Y., Takita, S., Ootsubo, T., et al. 2015, PASJ, 67, 50
Draine, B. T., & Weingartner, J. C. 1996, ApJ, 470, 551
Draine, B. T., & Weingartner, J. C. 1997, ApJ, 480, 633
Enoch, M. L., Young, K. E., Glenn, J., et al. 2006, ApJ, 638, 293
Ester, M., Kriegel, H.-P., Sander, J., & Xu, X. 1996, in Proc. Second Int. Conf. on Knowledge Discovery and Data Mining (KDD-96), ed. E. Simoudis, J. Han, & U. M. Fayyad (Cambridge, MA: AAAI Press), 226
Federrath, C. 2016, MNRAS, 457, 375
Fissel, L. M., Ade, P. A. R., Angilè, F. E., et al. 2019, ApJ, 878, 110
Friberg, P., Bastien, P., Berry, D., et al. 2016, Proc. SPIE, 9914, 99140D
Galametz, M., Maury, A., Girart, J. M., et al. 2018, A&A, 616, A139
Girart, J. M., Crutcher, R. M., & Rao, R. 1999, ApJL, 525, L109
Girart, J. M., Rao, R., & Marrone, D. P. 2006, Sci, 313, 812
Goldsmith, P. F., Heyer, M., Narayanan, G., et al. 2008, ApJ, 680, 428
Goodman, A. A., Bastien, P., Myers, P. C., & Ménard, F. 1990, ApJ, 359, 363
Hacar, A., Tafalla, M., & Alves, J. 2017, A&A, 606, A123
Hahm, S., Picklenbrook, M., & Doran, D. 2019, Journal of Statistical Software, Articles, 91, 1
Hatchell, J., & Dunham, M. M. 2009, A&A, 502, 139
Hatchell, J., Wilson, T., Drabek, E., et al. 2013, MNRAS, 429, L10
Heiles, C., Goodman, A. A., McKee, C. F., & Zweibel, E. G. 1993, in Protostars and Planets III, ed. E. L. Levy & J. I. Lunine (Tucson, AZ: Univ. Arizona Press), 279
Hen实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。实体被替换，不能确定。