Photoplethysmography-Based Heart Rate Monitoring in Physical Activities via Joint Sparse Spectrum Reconstruction

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Abstract—Goal: A new method for heart rate monitoring using photoplethysmography (PPG) during physical activities is proposed. Methods: It jointly estimates spectra of PPG signals and simultaneous acceleration signals, utilizing the multiple measurement vector model in sparse signal recovery. Due to a common sparsity constraint on spectral coefficients, the method can easily identify and remove spectral peaks of motion artifact (MA) in PPG spectra. Thus, it does not need any extra signal processing modular to remove MA as in some other algorithms. Furthermore, seeking spectral peaks associated with heart rate is simplified. Results: Experimental results on 12 PPG datasets sampled at 25 Hz and recorded during subjects’ fast running showed that it had high performance. The average absolute estimation error was 1.28 beat per minute and the standard deviation was 2.61 beat per minute. Conclusion and Significance: These results show that the method has great potential to be used for PPG-based heart rate monitoring in wearable devices for fitness tracking and health monitoring.

Index Terms—Photoplethysmography (PPG), Heart Rate Monitoring, Sparse Signal Recovery, Compressed Sensing, Wearable Healthcare, Health Monitoring, Fitness Tracking

I. INTRODUCTION

With the emerging of smart-watches and smart wristbands for healthcare and fitness, heart rate (HR) monitoring using photoplethysmography (PPG) [1], [2] recorded from wearers’ wrists becomes a new research topic both in industry and academia. HR monitoring using PPG signals has many advantages over traditional ECG signals, such as simpler hardware implementation, lower cost, and no requirement of ground sensors and reference sensors as in ECG recordings.

However, during physical activities motion artifact (MA) contaminated in PPG signals seriously interferes with HR estimation. The MA is mainly caused by ambient light leaking into the gap between a PPG sensor surface and skin surface. The gap can be easily enlarged by hand movements during physical activities. Besides, the change in blood flow due to movements is another MA source [3]. Consequently, the PPG signal contains strong MA, while the heartbeat-related PPG component is weak. Therefore, estimating heart rate becomes very challenging. In [4], [5], several typical difficulties in HR estimation are discussed.

So far, many noise-reduction techniques have been proposed, such as independent component analysis (ICA) [6], adaptive noise cancelation (ANC) [7], [8], spectrum subtraction [9], Kalman filtering [10], wavelet denoising [11], and empirical mode decomposition [12], to name a few. But these techniques were mainly proposed for scenarios when MA is not strong.

The TROIKA framework [4] is a recently proposed method for scenarios when MA is extremely strong. It consists of signal decomposition, sparsity-based high-resolution spectrum estimation, and spectral peak tracking and verification. The signal decomposition aims to partially remove MA components which overlap with the heartbeat-related PPG components in the same frequency band, and also to sparsify the PPG spectra facilitating the sparsity-based high-resolution spectrum estimation. The spectral peak tracking with verification aims to correctly select the spectral peaks corresponding to HR, overcoming various unexpected situations such as nonexistence of HR-related spectral peaks. Experimental results have shown that the TROIKA framework has high performance during wearers’ intensive physical activities.

In this paper a new approach to HR estimation is proposed, which is based on JOint Sparse Spectrum reconstruction, denoted by JOSS. It exploits the fact that the spectra of PPG signals and simultaneous acceleration signals have some common spectrum structures, and thus formulates the spectrum estimation of these signals into a joint sparse signal recovery problem, called the multiple measurement vector (MMV) model [13]. Although the idea of using basic sparse signal recovery algorithms was initially proposed in TROIKA [4], the present approach is novel and has many advantages over TROIKA. The main novelty is the use of the MMV model for joint spectrum estimation, in contrast to the single measurement vector (SMV) model [4] in TROIKA. In the MMV model, the measurement vectors are PPG signals and acceleration signals. Thus, their spectra are estimated simultaneously. Using the MMV model has many benefits which cannot be obtained when using the SMV model:

- Based on theoretical analysis, given the same sparsity level and compression ratio, the MMV model is known to have much better reconstruction performance than the SMV model [13]–[15].
- Due to the common sparsity constraint of the MMV model [13] on the spectral coefficients, the spectral peaks of MA in the raw PPG spectra can be easily found by checking spectral peaks in the acceleration signal spectra.
at corresponding frequency bins.

- By comparing the spectral coefficients in the PPG spectrum and the acceleration signal spectra at the same frequency bins, we can cleanse the PPG spectra, achieving a similar result as spectral subtraction [16].

Due to the above benefits, the proposed approach does not require the signal decomposition and the temporal difference operations in TROIKA. Furthermore, the spectral peak tracking and verification in TROIKA can be largely simplified. Thus, the approach is more suitable for hardware implementation [17].

The rest of the paper is organized as follows. Section II presents the approach. Section III gives experimental results. Discussion and conclusion are given in the last two sections.

II. PROPOSED METHOD

This section first presents the motivations, and then proposes the JOSS method. The JOSS method has two parts. One part is joint sparse spectrum reconstruction using the MMV model, followed by a simple spectral subtraction. The second part is spectral peak tracking with verification. Note that before fed into JOSS, PPG signals and acceleration signals are first bandpass filtered.

A. Motivations

In [4] the following SMV model was used to estimate the sparse spectrum of a raw PPG signal,

$$y = \Phi x + v,$$  \hfill (1)

where $y \in \mathbb{R}^{M \times 1}$ is a segment of a raw PPG signal, $\Phi \in \mathbb{C}^{M \times N}$ is a redundant discrete Fourier transform (DFT) basis, $x \in \mathbb{C}^{N \times 1}$ is the desired solution vector, and $v \in \mathbb{R}^{M \times 1}$ models measurement noise or modeling errors. The redundant DFT basis is given by

$$\Phi_{m,n} = e^{j \frac{2\pi}{N} mn}, \quad m = 0, \ldots, M-1; \quad n = 0, \ldots, N-1$$  \hfill (2)

where $\Phi_{m,n}$ denotes the $(m,n)$th entry of $\Phi$. In the SMV model, a key assumption is that $x$ is sparse or compressive, i.e., most elements of $x$ are zero or nearly zero, while only a few elements have large nonzero values.

Based on this model, the estimated $k$th spectrum coefficient of the PPG signal, denoted by $s_k$, is thus given by

$$s_k = |\hat{x}_k|^2, \quad k = 1, \ldots, N$$  \hfill (3)

where $\hat{x}_k$ is the $k$th element of $\hat{x} \in \mathbb{C}^{N \times 1}$, the estimate of $x$.

Using sparse signal recovery algorithms to estimate spectra has advantages over conventional nonparametric spectrum estimation methods and line spectral estimation methods, such as high spectrum resolution, low estimation variance, and increased robustness [18].

In TROIKA [4] a raw PPG was first bandpass filtered and then cleansed by partially removing MA via a signal decomposition procedure. Then the cleansed PPG signal was processed by a temporal difference operation to further suppress low-frequency MA and enhance the harmonic components of heartbeat-related PPG components. Finally, the resulting signal was used to calculate its spectrum by an SMV-model-based sparse signal recovery algorithm.

However, the signal decomposition procedure cannot remove all prominent MA components. It has two drawbacks.

First, in this procedure, a spectral peak of MA in a raw PPG spectrum is identified by checking if there is also a spectral peak in an acceleration spectrum at the same frequency bin. However, both the PPG spectrum and the acceleration spectrum are calculated using Periodogram separately. Consequently, even caused by a common hand movement, the spectral peak in the PPG spectrum and the counterpart peak in the acceleration spectrum may not appear at the same frequency bin. (They may locate at two frequency bins that are close to each other.) Thus, the MA spectral peak in the raw PPG spectrum is not identified, and will remain in the PPG spectrum calculated by sparse signal recovery in a later stage.

Second, if an MA component has a dominant spectral peak locating close to the frequency bin at which the previously selected HR-related spectral peak locates, the MA component will be kept in the PPG signal.

To overcome the drawbacks, this work proposes using MMV-model-based sparse signal recovery to estimate spectra of PPG and acceleration signals jointly. Based on this method, one can easily and reliably cleanse PPG spectra by removing MA spectral peaks, similar as spectral subtraction.

B. Joint Sparse Spectrum Reconstruction Using the MMV Model

The MMV model is an extension of the SMV model, estimating solution vectors jointly from multiple measurement vectors. In estimating power spectra of multichannel signals, the model can be expressed as follows

$$Y = \Phi X + V,$$  \hfill (4)

where $Y \in \mathbb{R}^{M \times L}$ is the matrix consisting of $L$ measurement vectors, $\Phi$ is the redundant DFT basis as before, $X \in \mathbb{C}^{N \times L}$ is the desired solution matrix, and $V \in \mathbb{R}^{M \times L}$ represents measurement noise or model errors. A key assumption in the MMV model is that the solution matrix $X$ is row-wise sparse, that is, only a few rows in $X$ are nonzero while most rows are zero. This assumption is also referred to as the ‘common sparsity constraint’ [13].

To use the MMV model, the columns of the measurement matrix $Y$ are segments of PPG and simultaneous acceleration signals in the same time window. In the experiments of this work, $Y$ is formed by a segment of one channel of PPG and segments of three channels of simultaneous acceleration signals. Thus, $L = 4$. Each column of $X$ yields the spectrum of the corresponding signal.

Many sparse signal recovery algorithms have been proposed for this model [13], [15]. But not every algorithm is suitable, since here the matrix $\Phi$ is highly coherent, i.e., high correlation exists between neighboring columns of $\Phi$. This work adopts the Regularized M-FOCUSS algorithm [13], because it has fast speed and reliable performance even if $\Phi$ is highly coherent.
The joint sparse signal recovery has many advantages. Using the MMV model, we can recover unique solutions which are less sparse. For example, in [13] it is shown that the MMV model can ensure a unique solution with the number of nonzero rows $r_0$ satisfies

$$r_0 \leq \lceil (M + L)/2 \rceil - 1$$

(5)

where $\lceil \cdot \rceil$ denotes the ceiling operation. Instead, the SMV model can only recover unique solutions with the nonzero coefficient number $r_0 \leq \lceil (M + 1)/2 \rceil - 1$. These theoretical results are inspiring. In the present application problem, the number of spectral coefficients sometimes is large due to MA. Although bandpass filtering is generally used before spectrum estimation, the spectral coefficients in the pass band are still many, which is an adverse situation. The TROIKA framework uses signal decomposition to remove MA components in the pass band to sparsify the spectrum, but this procedure is not always effective as stated in Section II-A. In contrast, this situation is alleviated in the MMV model.

Besides, given the same sparsity level (i.e., the number of nonzero rows of $X$ in the MMV model equals to the number of nonzero coefficients of $x$ in the SMV model) and other same conditions, the MMV model can yield solutions with smaller errors than the SMV model [14], [19].

In practical use, the common sparsity constraint of the MMV model helps identify spectral peaks of MA in PPG spectra by using the spectral peaks in acceleration spectra. Since MA components in PPG signals have many common frequencies with simultaneous acceleration signals, the common sparsity constraint encourages the frequency locations of MA in PPG spectra to be aligned well with some frequency locations in acceleration spectra. Consequently, one can accurately remove the spectral peaks of MA in the PPG spectra. This benefit is more desirable when the heartbeat frequency is very close to a frequency of MA.

Fig. 1 shows an example. Taking a PPG signal and three simultaneous acceleration signals (shown in Fig. 2) to be the four measurement vectors in the MMV model, their spectra are jointly estimated, as shown in Fig. 1(a)-(d). Due to the common sparsity constraint on the estimated multichannel spectra, the frequency locations of MA in the PPG spectrum were exactly aligned with the frequency locations in the acceleration spectra. Thus, one can subtract the MA spectral peaks in the acceleration spectra from the PPG spectrum (refer to the next subsection for details), yielding a cleansed PPG spectrum.

![Fig. 1. Joint sparse signal recovery helps better identify and remove spectral peaks of MA in PPG spectra.](image)

The maximum value of spectral coefficients in acceleration spectra at $f_i$ is denoted by $C_i$. We can see there was only one spectral peak remained, locating at the 112th frequency bin, which exactly corresponded to the heartbeat frequency (estimated from simultaneous ECG).

Note that in this example the heartbeat frequency is close to the frequencies of MA. However, the proposed method correctly distinguishes the spectral peaks of MA from the spectral peak of heartbeat. This advantage cannot be gained by using conventional spectrum estimation algorithms such as Periodogram. Fig. 3 shows the results by using Periodogram and the same spectral subtraction. Due to the low-resolution of Periodogram and the leakage effect [4], the spectral peak corresponding to the heartbeat is incorrectly removed during spectral subtraction. Instead, a false spectral peak is remained in the final spectrum, locating at the 116th frequency bin, indicating a large error of about 5.9 beat per minute (BPM).

Due to the advantages of the MMV model, finding the spectral peak corresponding to heartbeat becomes easier. In the following subsections, a simple spectral subtraction method will be first described, and then a spectral peak tracking method is proposed.

### C. Spectral Subtraction

Thanks to the advantages of the MMV model, spectral subtraction is made simple (given one PPG spectrum and three acceleration spectra):

- **Step 1**: For each frequency bin $f_i (i = 1, \cdots, N)$, choose the maximum value of spectral coefficients in acceleration spectra at $f_i$, denoted by $C_i$.

- **Step 2**: For each frequency bin $f_i (i = 1, \cdots, N)$, subtract $C_i$ from the value of the spectral coefficient at $f_i$ in the PPG spectrum. Now we obtain a processed PPG spectrum. Denote by $P_{\text{max}}$ the maximum value of all coefficients in the PPG spectrum.

- **Step 3**: Set to zero all spectral coefficients with values less than $P_{\text{max}}/4$, yielding a cleansed PPG spectrum.

To ensure the spectral subtraction method effective, each of the PPG segment and acceleration segments should be
normalized to have the same variance (i.e., the same energy).

D. Spectral Peak Tracking

As in TROIKA, spectral peak tracking is another key part. In this work, the proposed spectral peak tracking approach is simpler with less tuning parameters than the one in TROIKA. The approach is also based on the observation that HR values in two successive time windows are very close if the two time windows overlap largely.

The spectral peak tracking method consists of four stages, namely initialization, peak selection, peak verification, and peak discovery.

1) Initialization: In the initialization stage wearers are required to reduce hand motions as much as possible for several seconds, and HR is estimated by choosing the highest spectral peak in the PPG spectrum.

In the proposed approach, the kurtosis of the PPG spectrum from 0.8 Hz to 2.5 Hz (corresponding to 48 BPM to 150 BPM) is used to classify whether hand motions are reduced sufficiently. When hand motions occur, the kurtosis is small; otherwise, it is very large. Thus, in the proposed approach, if the kurtosis is larger than 10, the current time window is determined to be in the initialization stage, and the highest spectral peak in the PPG spectrum from 0.8 Hz to 2.5 Hz is chosen; in the next time window the approach enters the next stage. If the kurtosis is smaller than 10, the current time window is not in the initialization stage, and thus no HR estimate is output; in the next time window, the approach still checks whether it is in the initialization stage.

2) Peak Selection: In this stage, the goal is to choose a peak in the PPG spectrum with the knowledge of estimated HR values in previous time windows. The flowchart is given in Fig. 4.

First, a search range is set, denoted by $R_1$. This search range is centered at the location of the previously estimated spectral peak. In particular, denote by $\text{prevLoc}$ the frequency bin corresponding to the previously estimated HR, and denote by $\text{prevBPM}$ the corresponding BPM value. Then $R_1 \triangleq [\text{prevLoc} - \Delta_1, \text{prevLoc} + \Delta_1]$, where $\Delta_1$ is a positive integer.

Next, in the search range $R_1$ we seek at most 3 spectral peaks. If find any, then choose the one closest to $\text{prevLoc}$. If not, then set another search range $R_2 \triangleq [\text{prevLoc} - \Delta_2, \text{prevLoc} + \Delta_2]$ with $\Delta_2 > \Delta_1$. If in this range we still cannot find any peak, then output $\text{prevLoc}$ and $\text{prevBPM}$. If find any, then select the one with the highest value.

When selecting the peak closest to $\text{prevLoc}$, one may face a situation that two peaks have equal distance to $\text{prevLoc}$. (One has lower frequency and another has higher frequency.) To decide which peak should be selected, it is needed to predict whether current HR value will increase or decrease compared to the previously estimated HR value. This can be efficiently done by performing the Smoother algorithm in [20] on the spectral locations of $H$ previously estimated HR values, where $H \geq 10$. The smoothing parameter in the algorithm should be set to a small value such that we can predict local change of HR values.

Let $\text{curLoc}$ and $\text{curBPM}$ denote the frequency bin and associated BPM of the selected spectral peak, respectively.

3) Peak Verification: The previous stage sometimes can wrongly select a spectral peak associated with MA. Thus the verification stage is necessary. The flowchart is given in Fig. 5.
The verification method is based on an observation that the change of BPM values in two successive time windows rarely exceeds 12 BPM. If the difference between curBPM and prevBPM is larger than 12 BPM, then it is highly possible that the selected spectral peak is incorrect. So, curLoc and curBPM are reset to prevLoc and prevBPM, respectively.

However, when curLoc = prevLoc happens in multiple successive time windows, this indicates that the target spectral peak is lost. Thus, a discovery procedure is triggered.

4) Peak Discovery: Fig. 6 shows the flowchart of peak discovery. The Smoother algorithm is performed on the spectral locations of K previously estimated HR values to predict the spectral location of heartbeat in current time window. Different to the prediction in Peak Selection Stage, here the goal is to predict a macro-trend of HR evolution. So K is much larger than H, and the smoothing parameter is set to a large value. Since there is large uncertainty on the exact spectral location of HR, a larger search range is set than before. In particular, the search range is $R_3 = [\text{predictLoc} - \Delta_3, \text{predictLoc} + \Delta_3]$, where predictLoc is the predicted location, and $\Delta_3$ is a large integer.

III. EXPERIMENTAL RESULTS

A. Datasets

The JOSS algorithm was evaluated on the 12 PPG datasets initially used in [4]. Each dataset contains a channel of PPG, three channels of acceleration signals, and a channel of ECG, all recorded simultaneously from 12 healthy male subjects with age ranging from 18 to 35. In each dataset, the PPG signal was recorded from the wrist (dorsal) using a pulse oximeter with green LED (wavelength: 515nm). The three-channel acceleration signal was also recorded from the wrist using a three-axis accelerometer. Both the pulse oximeter and the accelerometer were embedded in a wristband. The ECG signal was recorded from the chest using wet ECG electrodes, from which the ground-truth of HR was calculated to evaluate algorithm performance. All signals were sent to a nearby computer via Bluetooth.

During data recording the subjects walked or ran on a treadmill with the following speeds in order: the speed of 1-2 km/hour for 0.5 minute, the speed of 6-8 km/hour for 1 minute, the speed of 12-15 km/hour for 1 minute, the speed of 6-8 km/hour for 1 minutes, the speed of 12-15 km/hour for 1 minute, and the speed of 1-2 km/hour for 0.5 minute.

All signals were initially sampled at 125 Hz. But in the present experiments the PPG signals and the acceleration signals were downsampled to 25 Hz. Some segments of these signals are shown in Fig. 2.

B. Experimental Settings

As in [4], a time window of 8 seconds was used to slide the simultaneous PPG signal and acceleration signals, with a step of 2 seconds. HR was estimated in each time window. Before
performing JOSS, all raw signals were bandpass filtered from 0.4 Hz to 4 Hz using the 2nd order Butterworth filter.

The Regularized M-FOCUSS algorithm [13] was used to estimate the solution matrix of the MMV model, with the parameter $p = 0.8$, the regularization parameter $\lambda = 10^{-10}$, and the spectrum grid number $N = 1024$. Its maximum iteration number was set to 4. Note that the TROIKA algorithm also used the M-FOCUSS algorithm to estimate sparse spectrum of PPG signals. However, in TROIKA, the M-FOCUSS algorithm was used to estimate the solution of the SMV model.

In the part of spectral peak tracking, $\Delta_1 = 15$, $\Delta_2 = 25$, and $\Delta_3 = 30$. The smoothing parameter used in the Peak Selection Stage was set to 5 and $H = 10$, while in the Peak Discovery Stage the smoothing parameter was set to 20 and $K = 30$.

### C. Performance Measurement

The ground-truth HR was calculated from the original raw ECG signals (sampled at 125 Hz) by manually picking the R-peaks one by one in each time window. No R-peak detection algorithm was used, in order to avoid any possible detection errors. These ground-truth HR values are now available in the PPG datasets [4] for performance evaluation.

The measurement indexes in [4] were used. One was the average absolute error (in BPM), defined as

$$\text{Error}_1 = \frac{1}{W} \sum_{i=1}^{W} |\text{BPM}_{\text{est}}(i) - \text{BPM}_{\text{true}}(i)|$$  \hspace{1cm} (6)

where $\text{BPM}_{\text{true}}(i)$ denotes the ground-truth of HR in the $i$-th time window, $\text{BPM}_{\text{est}}(i)$ denotes the estimated HR, and $W$ is the total number of time windows.

The second was the average absolute error percentage, defined as

$$\text{Error}_2 = \frac{1}{W} \sum_{i=1}^{W} \frac{|\text{BPM}_{\text{est}}(i) - \text{BPM}_{\text{true}}(i)|}{\text{BPM}_{\text{true}}(i)}$$  \hspace{1cm} (7)

The third index was the Bland-Altman plot [21]. The Limit of Agreement (LOA) was used, which is defined as $[\mu - 1.96\sigma, \mu + 1.96\sigma]$, where $\mu$ is the average difference between each estimate and the associated ground-truth against their average, and $\sigma$ is the standard deviation.

Pearson correlation between ground-truth values and estimates was also adopted.

### D. Results

Table I and Table II list the average absolute error (Error1) and the average absolute error percentage (Error2) of the proposed JOSS algorithm on all 12 datasets, respectively. To show its superiority, it was compared with the recently proposed TROIKA algorithm. For direct comparison, TROIKA was also performed on the PPG and acceleration data sampled at 25 Hz. The results in Table I and Table II show that JOSS had better performance than TROIKA. Averaged across the 12 datasets, the absolute estimation error (Error1) of JOSS

For several datasets, the initial recordings contain strong MA, probably due to device adjustment after the recording system turned on. For these recording segments, both algorithms did not output HR estimates. Thus the algorithms' performance was not evaluated on these segments. These excluded segments were the first 12 seconds of Set 2, the first 8 seconds of Set 3, the first 2 seconds of Set 4, the first 2 seconds of Set 8, the first 6 seconds of Set 10, and the first 2 seconds of Set 11.
Table I
Comparison of JOSS and TROIKA in terms of average absolute errors (Error1) on the 12 datasets sampled at 25 Hz.
The unit is BPM. SD denotes standard deviation.

|       | Set 1 | Set 2 | Set 3 | Set 4 | Set 5 | Set 6 | Set 7 | Set 8 | Set 9 | Set 10 | Set 11 | Set 12 | Average |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|--------|--------|---------|
| JOSS  | 1.33  | 1.75  | 1.47  | 1.48  | 0.69  | 1.32  | 0.71  | 0.56  | 0.49  | 3.81   | 0.78   | 1.04   | 1.28 (SD=2.61) |
| TROIKA| 2.87  | 2.75  | 1.91  | 2.25  | 1.69  | 3.16  | 1.72  | 1.83  | 1.58  | 4.00   | 1.96   | 3.33   | 2.42 (SD=2.47) |

Table II
Comparison of JOSS and TROIKA in terms of average absolute error percentage (Error2) on the 12 datasets sampled at 25 Hz. SD denotes standard deviation.

|       | Set 1 | Set 2 | Set 3 | Set 4 | Set 5 | Set 6 | Set 7 | Set 8 | Set 9 | Set 10 | Set 11 | Set 12 | Average |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|--------|--------|---------|
| JOSS  | 1.19% | 1.66% | 1.27% | 1.41% | 0.51% | 1.09% | 0.54% | 0.47% | 0.41% | 2.43%  | 0.51%  | 0.81%  | 1.01% (SD=2.29%) |
| TROIKA| 2.18% | 2.37% | 1.50% | 2.00% | 1.22% | 2.51% | 1.27% | 1.47% | 1.28% | 2.49%  | 1.29%  | 2.30%  | 1.82% (SD=2.07%) |

Fig. 8. Estimation results on Dataset 8. The estimated HR trace by JOSS was almost the same as the ground-truth of HR trace, while TROIKA got errors sometimes.

Fig. 9. The Bland-Altman plot of the estimation results on the 12 datasets. The LOA was [−5.94, 5.41] BPM.

IV. Discussions

A. On the Experiments

In the experiments the subjects had yellow skin-color and the LED light was green. Skin-color and LED light are known factors that affect characteristic of PPG signals, and thus affect algorithm performance. Evaluating the proposed algorithm’s performance at other skin-color and LED light will be the future work.

Studies have shown that the PPG pulse rate variability is a surrogate of heart rate variability when subjects are at rest [22]. However, when body movements occur, the correlation between PPG pulse-to-pulse intervals and ECG beat-to-beat intervals is not very high, and the correlation varies largely at different anatomical measurement sites [3]. Therefore, it is more reasonable to compare the ground-truth HR and the estimated HR in an ‘average’ level, instead of comparing each single cardiac cycle period. In the present experiments, the ground-truth HR was calculated from ECG in the time window of 8 seconds by the formula 60C/D (in BPM), where C was the number of cardiac cycles in the time window and D was the duration (in seconds) of these cycles [4]. And the estimated rate value, and y indicates the associated estimate. The Pearson coefficient was 0.993.
HR was calculated from the spectrum of PPG in the same time window. These calculation methods actually obtain averaged heartbeat periods in each time window, which is relatively resistant to the beat-to-beat interval variability.

B. Advantages and Possible Improvement Approaches of JOSS

As shown in the experiments, JOSS works well at low sampling rates. This is a desirable advantage over algorithms that only work well at high sampling rates, since a low sampling rate means low energy consumption in data acquisition and in wireless transmission, which can largely extend battery life in wearable devices.

JOSS exploits a common sparsity structure in the spectra of PPG signals and simultaneous acceleration signals by using the MMV model in sparse signal recovery. The MMV model is known to be superior to the basic sparse signal recovery model used in TROIKA. It is worth noting that there are many other structures in the spectra of PPG and acceleration signals which can be exploited. Thus, more advanced sparse signal recovery models may be used to further improve spectrum estimation performance and HR estimation performance, such as the model exploiting magnitude correlation among spectra [15], [23].

Gridless joint spectral compressed sensing [18], [24] is another promising framework to reduce HR estimation errors. When HR frequency does not locate at a frequency grid, estimation errors are unavoidable, and the PPG spectrum calculated from the MMV model may be less-sparse. This may result in some difficulties for conventional sparse signal recovery algorithms. But gridless joint spectral compressed sensing can potentially solve this issue.

There are other possible approaches to improve HR estimation. One approach is applying smoothing techniques to estimated HR traces, such as the median filtering. However, most effective smoothing algorithms perform offline. Thus this technique may be an effective approach when strict real-time is not required.

Although JOSS does not require an extra noise-removal modular, using a noise-removal modular can improve its robustness to MA. For example, JOSS can also adopt the signal decomposition modular used in TROIKA to partially remove MA before joint sparse spectrum reconstruction. Of course, this increases processing time, power consumption, and circuit design complexity if implemented in VLSI or FPGA.

V. Conclusion

In this work a PPG-based heart rate monitoring method was proposed for fitness tracking via smart-watches or other wearable devices. The method uses the multiple measurement vector model in sparse signal recovery to jointly estimate sparse spectra of PPG signals and simultaneous acceleration signals. Due to the common sparsity constraint on the spectral coefficients, identifying and removing spectral peaks of MA in PPG spectra is easier. Thus, it does not need an extra signal processing stage to remove MA as in other algorithms. This largely simplifies the whole algorithm. Besides, it works well for data sampled at low sampling rates, thus saving energy consumption in data acquisition and wireless transmission. Therefore, the proposed method has potential to be implemented in VLSI or FPGA in wearable devices.

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