Probing the geometry of copper and silver adatoms on magnetite: quantitative experiment versus theory†

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Accurately modelling the structure of a catalyst is a fundamental prerequisite for correctly predicting reaction pathways, but a lack of clear experimental benchmarks makes it difficult to determine the optimal theoretical approach. Here, we utilize the normal incidence X-ray standing wave (NIXSW) technique to precisely determine the three dimensional geometry of Ag and Cu adatoms on Fe3O4(001). Both adatoms occupy bulk-continuation cation sites, but with a markedly different height above the surface (0.43 ± 0.03 Å (Cu)) and 0.96 ± 0.03 Å (Ag)). HSE-based calculations accurately predict the experimental geometry, but the more common PBE + U and PBEsol + U approaches perform poorly.

Density functional theory (DFT) has become an indispensable tool in modern catalysis research, allowing us to understand long-observed trends in reactivity and unravel complex reaction mechanisms.1 Rapid advances in computational power have fueled efforts to screen, and even predict catalysts from first principles,2–4 but real predictive power requires adsorption energies and reaction barriers to be quantitatively correct. This must begin with an accurate description of the catalyst, but there is little in the way of solid experimental benchmarks5 to test the different exchange–correlation functionals,6–11 van der Waals corrections, both (semi-) empirical12–14 and non-empirical,15,16 and methods beyond DFT.17–23

The emerging field of single-atom catalysis (SAC)24–30 is a case in point. Although, there are reports of highly-active single-atom catalysts,31–37 the field remains controversial38 because such systems are difficult to characterize experimentally. Moreover, the catalytic mechanism is often proposed on the basis of theoretical calculations,31,36,39–41 which utilize an idealized catalyst support with metal adatoms adsorbed at high-symmetry sites on a low index facet. Thus, the 1 : 1 equivalence of experimental and theoretical data is difficult to establish.

Fe3O4 nanocrystallites have been observed as a support material that can anchor single adatoms, with both Pt and Ir adatoms exhibiting catalytic activity.31,33 These two studies utilized the same coprecipitation method to generate the nanocrystallites and, in the work of Lin et al.,33 were observed by X-ray diffraction to be primarily magnetite crystallites. Recently we discovered that the (001) surface of a magnetite single crystal can stabilize ordered arrays of metal adatoms (e.g. Au,44 Pd,45 and Pt46).47 These adatoms were found to be homogenously distributed up to a comparatively high coverage and with high thermal stability, and is therefore a promising model system to provide insight into single atom catalysts supported on Fe3O4 nanocrystallites. It is this remarkable density, stability, and homogeneity of adatom arrays that offers the opportunity to perform a precise structural determination, and test the ability of DFT-based calculations to accurately model these dispersed lone adatoms. To that end, we report a normal incidence X-ray standing waves (NIXSW48) study of two members of this family: Ag1 and Cu1 adatoms on Fe3O4(001). These adatoms were chosen for their nobility, in order to avoid undesired adsorption of the residual gases found in ultra-high vacuum, and thus are used as a comparatively simple benchmark with which to test the performance of theoretical calculations. Both metals were determined to adsorb in a surface tetrahedral cation site, with significantly different adsorption heights (0.96 ± 0.03 Å for Ag and 0.43 ± 0.03 Å for Cu). DFT calculations using the Heyd–Scuseria–Ernzerhof (HSE) functional39 reproduce the geometry well, but the more common Perdew–Burke–Ernzerhof + U (PBE + U) and PBEsol + U approaches perform poorly. Although improved structural...
agreement can be achieved by constraining the lattice parameter to the experimental value, the failure to meet this experimental benchmark raises concern over this widely used functional in the field of adatoms on metal oxide surfaces.

Full experimental details can be found in the ESL.† The as-prepared surface exhibits a sharp (2√2)R45° low energy electron diffraction (LEED) pattern (not shown), and scanning tunneling microscopy (STM) images reveal rows of surface Fe₂oct atoms running in the [110] directions (see Fig. 1A and B). Here, Fe₂oct refers to atoms with octahedral coordination to oxygen in bulk Fe₃O₄. The surface Fe₂oct rows exhibit a characteristic distortion due to an ordered array of subsurface cation vacancies and interstitials,⁴⁷ the so-called subsurface cation vacancy (SCV) reconstruction.

Fig. 1 shows STM images of the surface following the deposition of 0.27 ML Ag (a) and 0.41 ML Cu (b). Isolated adatoms appear as bright protrusions between the surface Fe₂oct rows, with apparent heights relative to the surface Fe₂oct rows of 1.1 ± 0.3 Å and 0.6 ± 0.2 Å for Ag₁ and Cu₁ respectively. As observed previously,⁴⁹ adatom adsorption occurs almost exclusively at the site marked by an × in Fig. 1A, i.e., where the separation of the Fe₂oct rows appears narrowest with a sample bias of 1–1.5 V.⁴⁷ Approximately 10% of the Cu adatoms occupy an alternative adsorption site, Cu₁*, after room temperature deposition. This site is metastable, and can be converted into regular Cu₁ by annealing at 550 K. For Ag, small clusters begin to form at a coverage of ≤ 0.5 ML.⁵¹ This aggregation is irreversible, but does not affect the position of the majority adatom species measured by the NIXSW method.

The calculations predict that the Ag₁ adatom protrudes further than the Cu₁ adatom. An analysis of the NIXSW profile yields two parameters: the coherent position (Phkl) and coherent fraction (f coherence). The results are overlaid with a ball-and-stick model representing an idealized Fe₂oct-O₂ bulk termination. The adsorption site can be clearly identified at the center and corners of the map, corresponding to an oxygen bridge site.

Fig. 1C and D show the minimum-energy configuration for Cu₁ and Ag₁ adatoms on the Fe₃O₄(001) surface, as determined by HSE-based calculations. The favoured adsorption site for both adatoms is twofold coordinated to surface oxygen atoms between the surface Fe₂oct rows. Specifically, the adatoms bind to the two oxygen atoms without a subsurface Fe₄tet (i.e. tetrahedrally coordinated Fe) neighbour, where the next Fe₄tet atom would reside if the bulk structure were continued outward. The calculations predict that the Ag₁ adatom protrudes further from the surface than the Cu₁ (Δz = 1.12 Å and Δz = 0.59 Å, respectively), which corresponds remarkably well to the STM apparent heights in the bias range V sample = 1–1.5 V.

To quantitatively benchmark the adatom geometry, we performed NIXSW experiments⁴⁶,⁴⁹ at beamline I09, Diamond Light Source. NIXSW exploits the standing wavefield generated by the interference between incident and reflected photon beams at a specific Bragg condition of the substrate. As the incident photon energy is varied near such a condition, the standing wavefield moves relative to the Bragg planes.

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shown in Fig. 1E), occurring at \( h\nu = 2960, 2450 \) and 4180 eV respectively. Note that at exact normal incidence, the wavelength of the light will be twice the spacing between the planes. Atomic density maps (e.g. Fig. 1F), reconstructed from three reflections using a Fourier expansion described in the ESI,† directly (and unambiguously) identify the three dimensional adsorption site as the surface oxygen bridge site, confirming the site inferred from the STM/calculated data. Here we focus primarily on the (004) data, which specifically probes the vertical positions of the adatoms. Details of the complete NIXSW analysis are included in the ESI†.

Fig. 2 shows the fitted (004) NIXSW profiles following the deposition of 0.4 ML of Cu and Ag at room temperature. The photon energy scale is plotted relative to the Bragg energy, defined by the X-ray reflectivity curve shown in the lower curve. Clearly, the maximum photoemission intensity occurs at significantly different energies for the Ag 3d/2 and Cu 2p3/2 data, indicating a significant difference in their position with respect to the Fe3O4(004) planes. Specifically, \( F_{004} \) values of 0.71 ± 0.02 (Cu1) and 0.96 ± 0.01 (Ag1) were obtained, which corresponds to heights of \( H_{\text{Cu}} = 0.43 ± 0.03 \) Å (Cu1) and \( H_{\text{Ag}} = 0.96 ± 0.03 \) Å (Ag1) above an idealized FeoctO2 bulk termination. The corresponding \( f_{004} \) values are 0.71 ± 0.03 (Cu1) and 0.66 ± 0.03 (Ag1). Annealing the Fe3O4(001)/Cu surface to 550 K resulted in a dramatic increase in the coherent fraction to 0.93 ± 0.03, consistent with the conversion of metastable Cu1* species (Fig. 1B) into regular Cu1 adatoms. The relatively low coherent fraction of Ag1 is attributable to clustering.50 Since the clusters are likely three dimensional, and thus have an equal occupation of all sites within the projected layer spacings, their contribution to the NIXSW simply lowers the coherent fraction without altering \( F_{004} \).

Table 1 shows a selection of the computational results for the Fe3O4(001)/Cu1 and Fe3O4(001)/Ag1 systems. Full details of the various calculations are contained within the ESI,† but briefly, we utilized the Vienna \textit{ab initio} Simulation Package (VASP)51,52 with the following functionals: PBE,9 PBE + U,9,53,54 PBEsol + U,11 and HSE.23 The surface calculations utilized an asymmetric surface slab with 5 fixed and 2 relaxed layers FeoctO2 layers including the SCV reconstruction.47 Initially we followed the standard procedure for calculating Fe3O4 surfaces, using a theoretical lattice parameter obtained by relaxing the bulk unit cell with the relevant functional. PBE + U and HSE overestimate the lattice by 0.75% and 0.18%, respectively, whereas PBE and PBEsol + U underestimate it by 0.01% and 0.61%, respectively. All calculations except the PBE find that the addition of the metal adatom reduces the total magnetic moment from 60\( \mu_\text{B} \) to 59\( \mu_\text{B} \) in both cases, indicating a charge state of +1 for the adatoms.

\begin{table}
| Method | HSE | PBE + U | PBE | PBE | PBEsol + U | NIXSW |
|--------|-----|--------|-----|-----|------------|-------|
| Lattice param. 〈Å〉 | 8.411 | 8.459 | 8.396 | 8.390 | 8.345 | 8.396 |
| \( \alpha \)-oct (%) | +0.18 | +0.75 | 0 | -0.01 | -0.61 | 0 |
| \( \Delta z_{\text{ad}} \) (Å) | 1.12 | 1.00 | 1.05 | 0.96 | 0.85 | — |
| Ag-O bond length (Å) | 2.11 | 2.09 | 2.09 | 2.06 | 2.02 | — |
| \( E_{\text{ad}} \) (eV) | -1.99 | -2.19 | -1.93 | -2.30 | -2.63 | — |
| \( H_{\text{Cu}} \) (Å) | 0.37 | 0.33 | 0.41 | 0.38 | 0.31 | 0.43 ± 0.03 |
| \( \Delta z_{\text{Cu}} \) (Å) | 0.59 | 0.53 | 0.55 | 0.56 | 0.50 | — |
| Cu-O bond length (Å) | 1.86 | 1.85 | 1.84 | 1.84 | 1.84 | — |
| \( E_{\text{ad}} \) (eV) | -3.46 | -3.76 | -3.60 | -3.85 | -4.17 | — |
\end{table}
To directly compare the theoretical geometry to the NIXSW results, the adatom height must be calculated with respect to the bulk lattice. Thus we must convert the theoretical adatom height with respect to the bottom fixed Fe\textsubscript{oct}O\textsubscript{2} layer in the DFT slab, \(z_{ad}\), to \(H_{ad}\) (ad = Ag, Cu) by:

\[
H_{ad} = z_{ad} - n \cdot d_{004}.
\]

where \(n = 6\) is the number of Fe\textsubscript{oct}O\textsubscript{2} inter-layer spacings in the DFT slab, and \(d_{004} = 2.099\) Å is the bulk (004) layer spacing. Clearly, the HSE results (Table 1) best model the experiment, yielding \(H_{ad}\) values just below the experimental range. Moreover, the Ag binding energies of 2.0 eV compares well to a recent adsorption calorimetry experiment for Ag on Fe\textsubscript{3}O\textsubscript{4}(111) (2.3 eV).\(^{55}\)

Interestingly, the predicted charge state (+1 − supported by X-ray photoelectron spectroscopy, see ESI†) and Cu−O and Ag−O bond lengths (1.86 Å and 2.11 Å, respectively) are similar to the bulk compounds Cu\textsubscript{2}O and Ag\textsubscript{2}O (1.8481 ± 0.0004 Å and 2.043 ± 0.002 Å, respectively),\(^{56}\) where the cations bind linearly to \(\text{O}^{2−}\) anions. Thus, the adatom geometry can be understood as the metal adopting its favored bond length to oxygen, with the constraint that the surrounding Fe\textsubscript{oct}O lattice precludes the ideal linear geometry. It is then straightforward to understand why the \(H_{ad}\) predicted by PBE + U is too low (\(H_{Ag} = 0.78\) Å, \(H_{Cu} = 0.33\) Å). Although the Cu−O and Ag−O bond lengths are similar to HSE, the overestimation of the lattice parameter leads to a widening of the relevant O−O distance, and the adatoms sink towards the substrate. Simply rescaling the calculation to the experimental lattice makes matters worse, because this also reduces the Ag−O/Cu−O bondlengths, and thus the adatom height. If instead, utilising the PBE + U functional, the substrate lattice parameter is constrained to the experimental value (8.396 Å) at the outset of the calculation, the Ag−O and Cu−O bondlengths are unaffected, and \(H_{ad}\) values closer to the experiment are obtained. The local structure of the adatoms provides a very good approximation to the HSE results, though it must be noted that constraining the lattice in this way leads to a small expansion in the \(z\) direction in the relaxed layers. Altering the \(U_{eff}\) parameter did not provide a more accurate modelling of the geometric structure (see ESI/Fig. S5†). Given the importance of the lattice parameter and metal−oxygen bonding in general, one might expect that PBE\textsubscript{sol} + U, specifically designed to correct for the disfavor of density overlapping of PBE, should perform well. Such calculations do indeed yield a lattice parameter closer to experiment than PBE + U, but the Ag adatom height is dramatically underestimated because the Ag−O bond length is also significantly reduced, therefore constraining the lattice constant to the experimental value resulted in a greater disagreement with experiment. This concomitant overbinding of adsorbates by PBE\textsubscript{sol} has been observed previously.\(^{31}\) A similar overbinding is observed in the PBE calculations (without \(U\)), due to highly reduced degree of localization of the Fe 3d electrons. Thus PBE and PBE\textsubscript{sol} are clearly not a suitable choice for SAC studies.

**Conclusions**

In summary, we demonstrate via direct NIXSW imaging, that Cu and Ag adatoms occupy a bulk-continuation cation site on the Fe\textsubscript{3}O\textsubscript{4}(001) surface. Furthermore the NIXSW data indicates their height above the surface differs significantly by 0.52 ± 0.04 Å. Successful theoretical modelling of this quantitative experimental result was found to be dependent not only on the choice of functional, but also on the bulk lattice parameter.

Large deviations from the lattice parameter are known to affect calculations of phonon and magnetic properties, but the values obtained here would not normally be considered problematic, especially for adsorption studies. However, the PBE + U functional only obtains quantitative agreement with experiment when the lattice parameter is within 0.2% of the experimental value (8.396 Å). Despite this ability to “shoe-horn” the PBE + U calculations into more accurately modelling the experimental results, it is clear that, by predicting an underbinding of the atoms in the substrate and a relative overbinding between the substrate and the adatom, PBE + U fails at this experimental benchmark. Thus the use of the popular PBE + U functional must be questioned, certainly in its application to metal adatoms supported on magnetite, potentially to single metal adatoms supported on other metal oxides surfaces as well, and possibly even to metal nanoclusters supported on metal oxides in general.

**Conflicts of interest**

The authors have no conflicts to declare.

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