DESIGN OF WASTE VEGETABLE OIL COLLECTION NETWORKS APPLYING VEHICLE ROUTING PROBLEM AND SIMULTANEOUS PICKUP AND DELIVERY

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Lisandra Quintana
Universidad Autónoma de Baja California, Instituto de Ingeniería, Calle de la Normal y Blvd. Benito Juárez S/N, 21280, Mexicali, B.C, Mexico, quintana.lisandra@uabc.edu.mx

Yalexia Herrera-Mena
Universidad Popular Autónoma del Estado de Puebla, Calle 17 Sur 711, 72410, Puebla, Mexico, yalexia.herrera@upaep.edu.mx

José L. Martínez-Flores
Universidad Popular Autónoma del Estado de Puebla, Calle 17 Sur 711, 72410, Puebla, Mexico, joseluis.martinez01@upaep.mx

Marcos A. Coronado
Universidad Autónoma de Baja California, Instituto de Ingeniería, Calle de la Normal y Blvd. Benito Juárez S/N, 21280, Mexicali, B.C, Mexico, marcos.coronado@uabc.edu.mx (corresponding author)

Gisela Montero
Universidad Autónoma de Baja California, Instituto de Ingeniería, Calle de la Normal y Blvd. Benito Juárez S/N, 21280, Mexicali, B.C, Mexico, gmontero@uabc.edu.mx

Patricia Cano-Olivos
Universidad Popular Autónoma del Estado de Puebla, Calle 17 Sur 711, 72410, Puebla, Mexico, patricia.cano@upaep.mx

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Abstract: The growth of industrialization in Mexico has caused an increase in the demand for materials to satisfy the consumption of goods and services of a growing population. Given this scenario, there is a rise of the residual generation with affectations on the ecosystem and population health. Hence, the objective of this research was to design a network for waste vegetable oil collection based on vehicle routing problem with simultaneous pickup and delivery, starting from a distribution centre to 49 restaurants, as the generation sources of waste vegetable oil. The Vehicle Routing Problem Simultaneous Pickup and Delivery with Time Windows was the variant used as a vehicle routing method to solve the problem. The free software VPRPD was the tool used to solve the vehicle routing problem with simultaneous pickup and delivery that allowed to specify time restrictions. This software uses the simulated annealing metaheuristics in its syntax. As a result, it was obtained a total of 8 networks, for a vehicle capacity utilization of 70 percent in the 6 t vehicle and 46 percent in the 8 t vehicle.

1 Introduction
The growth for industrialization in Mexico has caused an increase in the demand of materials to satisfy the consumption of goods and services of a growing population. Given this scenario, the increase in residual generation at the national level is evident, with affectations on the ecosystem and population health. Therefore, it is everyone's responsibility to find solutions that help mitigate these damages [1]. Scientific and technical advances have made it possible to identify that many of these wastes can be a potential feedstock in several production processes [2-5].

An example of this waste generation is the vegetable oil supply chain, where the last user generates waste vegetable oil (WVO), a residue obtained from frying food. This waste is recovered when it is subjected to a physical treatment process, becoming a good enough material that can be used in the production systems of the chemical industry for the production of biofuel as well as a food supplement for the livestock sector. The commercial value of the waste vegetable oil is evident, therefore, it is necessary to design logistic networks that transport the residual from the generation sources to a collection centre, where it can be treated and valorised. It would not only have a positive environmental and social impact; it would also open up new business opportunities with sustainable competitive advantages.

Residual management and products recovery are a complex problem that requires planning, management and, control of the flow of materials and products [6]. Hence, the recovery logistics process has a fundamental role,
which requires the design, development, and control of a system to collect the out-of-use product, and logistics management must be supported by strategic, tactical, and operational decisions [7].

This research is focused on the design of a waste vegetable oil pickup network from a residual recycling company located in the north of Mexico. Nowadays, the recycling company has 151 clients and wishes to expand by incorporating 49 new generation points (restaurants that generate waste vegetable oil). However, the company that outsources the pickup service is at the limit of its capacity and is not able to incorporate more clients. Therefore, the company must design a collection network to attend the demand of these new clients.

1.1 Importance of logistics in residual management

Since 2013, with the General Law for the Prevention and Integral Management of Residual, in Mexico, government actions have been carried out to mitigate the environmental and social damage generated by the indiscriminate dumping of waste into the environment. At the beginning of 2019, the Ministry of the Environment and Natural Resources began the Zero Waste Project, which seeks the modification of the current schedule for a new one following the principles of circular economy model [8].

The circular economy is a system designed to be restored and regenerative [9]. The circular economy is an "alternative growth discourse" and not an "alternative to the growth discourse". It is a model that follows a continuous development cycle, preserves and increases natural capital, optimizes resource returns, and minimizes system risks, managing finite stock and renewable flows [10]. This philosophy assumes that the life cycle of a product ranges from its production to its recovery or reduction after it is used [11].

The adoption of a circular economy program implies that the company has to work seeking to optimize resources.

Given the need for production systems of the industrial sector to be more sustainable, with cleaner processes and a closed life cycle; it is important to design logistic systems that enable the recovery of material and feedstock with a high added value. It is a challenge since the business sector considers that residual recovery processes are not very profitable. Therefore, the continuous improvement of the logistic processes and fundamentally, the optimization of the collection networks is one of the elements is necessary to work seeking to optimize resources.

1.2 Vehicle Routing Problem

Given the need for production systems of the industrial sector to be more sustainable, with cleaner processes and a closed life cycle; it is important to design logistic systems that enable the recovery of material and feedstock with a high added value. It is a challenge since the business sector considers that residual recovery processes are not very profitable. Therefore, the continuous improvement of the logistic processes and fundamentally, the optimization of the collection networks is one of the elements is necessary to work seeking to optimize resources.
Different variants of the VRPPPD were developed between 1999 and 2016, in which two situations were considered: a static environment [17], which occurs when all the input data of the problem is known before the construction or design of the routes and the planning horizon is limited, and a dynamic environment [18], where some input data are known or updated during the period in which the delivery and pickup operations of the products takes place. However, most of the delivery and pickup problems have been focused on the static scenario and few authors have worked on the dynamic part of the problem.

The VRP problem with simultaneous deliveries and pickup (VRPSPD) is one of the variants of VRPPPD and was first addressed by Hokey Min in 1989 [19], who recognizes that it can exist simultaneously delivered and pickup in the same node. The objective of the VRPSPD is to find a series of routes for a set of vehicles at a minimum cost, in order to serve customers in the most appropriate way, which fulfills the restriction that the vehicles have sufficient transport capacity for the products (or persons) that must be collected and/or delivered and pickup to each customer (node). It must start from a depot and arrive at the same depot. The aim is to find the optimum solution or quality sub-optimal solutions. This is a combinatorial optimization problem and most of its versions are of the NP-Hard class, meaning that the solution cannot be found in polynomial time [20].

Unlike the classic vehicle routing problem, in VRPSPD the feasibility of routes is determined not only by the subset of clients that makes up the route but also, the order in which they are visited. The first condition requires that the total of transported products does not exceed the capacity of the vehicle. The element of order is added because, at all times, the load is a mixture between the product previously collected from the customers visited and those yet to be delivered. Due to the fluctuation in the load, even when the total demand does not exceed the capacity of the vehicles, there may be intermediate points on the route where this does happen [15].

The VRPSPD, like the rest of the problems derived from the VRP, has among its variants the following [21]:

- VRPSPD + heterogeneous fleet, considering capacity, costs, availability, and speed of loading/unloading, and travel.

This last variant is known in the Vehicle Routing Problem Simultaneous Pickup and Delivery with Time Windows (VRPSDPPTW) and aims to minimize the difference between routing costs and incomes associated with pickups [20].

VRPSDP is the least studied or applied in the literature and most of the authors consulted assume elements that facilitate the search of a solution, which in some are theoretical solutions that are far away from what happens in real life. Some authors [22] have found optimal solutions using exact methods but have had to make assumptions such unlimited number of vehicles and number of nodes or clients to visit less than 30, this makes it an NP-hard problem.

VRPSPD is one of the least addressed types of VRP in the literature because of its complexity, since the search for optimal solutions can increase exponentially depending on the number of customers or nodes that are part of the problem. Therefore, the computational resources that work with exact algorithms could not be used in scenarios with more than 40 clients. Consequently, the heuristic or metaheuristic algorithms are the most used to find a solution that, even if is not optimal can be feasible.

2 Methodology

The objective of this research was to design a waste vegetable oil collection network to attend the demand of 49 generation sources. Based on the VRPSPD, a mathematical model is designed considering the restrictions of the studied network. Finally, a simulated annealing metaheuristic algorithm was used to obtain a feasible solution.

2.1 Problem Statement

The company increases its client portfolio each year as the capacity to treat residual raises, as well as the awareness of the production chains to have cleaner, more sustainable, and environmentally friendly processes.

The company specializes in the maintenance and cleaning of grease traps, as well as hoods, adding a service of waste vegetable grease collection, which they use for biodiesel production. The grease collection service is outsourced to a company dedicated to the transportation and distribution of products. Currently, that company cannot assume the commitment to include the 49 generation points that the recycling company wishes to add in its client portfolio. Therefore, the recycling company needs to conduct a study to determine if it has the capacity to execute the collection process for new clients. The locations of existing customers and the new ones to be incorporated are showed in Figure 1.
The objective of the collection process is to deliver empty containers to the points of generation for the collection of residual and to collect containers with WVO. In this process, it is necessary to consider that:

- The generation point will be visited only once; and the opening, closing, and resting times of each point.
- The collection center has two vans, 6 t and 8 t dedicated exclusively to the delivery of empty containers and the collection of full containers at each generation point.
- Deliveries of empty containers and collections of full containers would be made simultaneously.
- 20 L containers will be delivered so that the residual is collected at each generation point.

2.2 Method of solution

Knowing the characteristics of the collection process, it is a VRPSPD with elements of a VRPTW, being then a VRPSPDTW. Both models belong to the family of vehicle routing problems with capacity restrictions. Both consider that all routes start and end at the collection centre. At no point of the route can the load exceed the capacity of the vehicle, the vehicles have different capacities and can make at most one trip. For the solution of the problem, it is estimated that the load of the vehicle is a mixture of the products collected from the clients already visited and the one that remains to be visited. Also, it was considered that each establishment has time to attend the vehicle that makes the delivery and collection of the product.

A route is an ordered sequence of customers associated with a specific vehicle. In short, it is a problem where the starting point is a collection centre with a heterogeneous fleet of vehicles and a set of generation points are visited. At each point, there is a demand for 20 L containers, known as delivery demand and 20 L containers containing WVO are for pickup, known as the pickup demand. Both, the collection centre and the generation points have time restrictions to attend the delivery and pickup process. Therefore, a network is designed to satisfy the demand of all customers, optimizing the distance and travel time.

2.2.1 Design of the mathematical model of the Vehicle Routing Problem Simultaneous Pickup and Delivery with Time Windows

The objective of the VRPSPDTW is to determine the set of routes that satisfies the demand of all the clients by optimizing the distance, fulfill the demand of the clients, and attending to their time restrictions. The parameters and variables that define the model are shown in Table 1.
The mathematical model presented is based on the models defined by [20,21,23]. The problem is modelled on a graph, being the vertices the clients and the deposit, so the set I* and the arcs are the paths between these vertices.

**Objective function:**

\[ \text{min} \sum_{i=1}^{m} \sum_{i \in I^*} C_{ij} \times x_{ij}^k \]  

(1)

**Restrictions:**

1. \[ \sum_{i=1}^{m} \sum_{i \in I^*} x_{ij}^k = 1 \quad \forall i \in I \]  
2. \[ \sum_{j \in I^*} x_{kj}^k - \sum_{j \in I^*} x_{ij}^k = 0 \quad \forall s \in I^*, \forall k \in K \]  
3. \[ \sum_{j \in I^*} x_{ij}^k \leq m^k \quad \forall k \in K \]  
4. \[ \sum_{i \in I^*} D_{ij} = \sum_{i \in I^*} d_i \]  
5. \[ \sum_{i \in I^*} P_{ij} = \sum_{i \in I^*} p_i \]  
6. \[ \sum_{j \in I^*} D_{ij} - \sum_{j \in I^*} D_{ij} = d_i \quad \forall i \in I \]  
7. \[ \sum_{j \in I^*} P_{ij} - \sum_{j \in I^*} P_{ij} = p_i \quad \forall i \in I \]  
8. \[ P_{ij} + D_{ij} \leq \sum_{k=1}^{m} x_{ij}^k \times Q^k \quad \forall i, j \in I^* \]  
9. \[ t_{ij}^k = 0 \quad \forall k \in K \]  
10. \[ x_{ij}^k (t_{ij}^k + s_{ij}^k + t_{ij}^k - t_{ij}^k) \leq 0 \quad \forall i, j \in I^*, \forall k \in K \]  
11. \[ t_{ij}^k \geq 0 \quad \forall i \in I, \forall k \in K \]  
12. \[ x_{ij} \in \{0,1\} \quad \forall i, j \in I^* \]  
13. \[ D_{ij} \geq 0 \quad \forall i, j \in I^* \]  
14. \[ P_{ij} \geq 0 \quad \forall i, j \in I^* \]  

The objective function (1) minimizes the travel distance. The restriction (2) ensures that all customers are visited once. The continuity of the distance travelled from one point is guaranteed by the restriction (3). It (4) ensures that each vehicle is used only once and taking into account that the vehicle fleet is heterogeneous. Restrictions (5) and (6) ensure that everything that is collected is taken to the depot and that everything that is to be delivered is in the depot (7) and (8) ensure that the demands of pickup and delivery at each customer are attended. In the case of (9), it indicates that the product can only be distributed through the arch included in the solution. With (10) it is guaranteed that all vehicles leave the warehouse at the initial moment. The relationship between the arrival times of consecutive customers on a route is defined in the restriction (11), (12) makes the arrival time a non-negative value. Finally, (13) is associated with the domain, and (14), (15) are the non-negative conditions.

### 2.2.2 The Vehicle Routing Problem Simultaneous Pickup and Delivery with Time Windows solution

Previously knowing the amount of data to process and the complexity of the mathematical model of the problem to be solved, a metaheuristic algorithm was used, to get a feasible solution in less time. Using a metaheuristic algorithm prevents the solution from falling into optimum locations as there are intelligent and high-level procedures. The free software VPRPD was used to solve the problem. This software uses the simulated annealing metaheuristic in its syntax. These metaheuristics has an algorithm that selects candidates randomly and allows degraded solutions, but always with an acceptable probability that will depend on two factors: the control parameters and the difference in values that the objective function takes.

Input data that were used:

- Travel distance matrix between each of the generation points and the collection centre, considering vehicle traffic restrictions.
- Travel time matrix between each of the generation points and the collection centre, taking into account vehicle traffic restrictions.
- Vehicle capacity.
- Workday at the collection centre.
- Number of 20 L containers with waste vegetable oil to collect at each generation point.
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3 Results and discussion
The solution is shown in Figure 2, taking into account the geographical location of the generation points and the collection centre.

Table 2 shows a summary of the long times of each route, the distance travelled to execute them, as well as the load transported and advantage of the vehicle’s capacity on each trip.

| Routes with 6 t van | Time (min) | Distance (km) | Load (20 L containers) | Capacity use |
|---------------------|------------|---------------|------------------------|--------------|
| 1 CR-P33-P34-P35-P45-P26-CR | 199.51 | 20.80 | 61 | 90% |
| 2 CR-P14-P9-P37-P49-CR | 140.35 | 14.15 | 23 | 34% |
| 3 CR-P32-P25-P18-P10-P41-P12-P11-P16-CR | 176.68 | 19.40 | 57 | 84% |
| 4 CR-P21-P48-P17-P36-P43-P42-P28-CR | 189.51 | 22.42 | 41 | 60% |
| 5 CR-P13-P47-CR | 148.22 | 16.90 | 56 | 82% |
| TOTAL | 854.27 | 93.67 | 238 | |

Figure 2 Collection networks for new customers
It will not be possible to make all the visits on a working day, because the time it takes to make all the visits exceeds the workday established of the collection centre. Therefore, it should be considered when scheduling the delivery and collection process.

The allocation of the load in the vehicles is acceptable, however, the capacity use of the 8 t Van is only 46 percent, while the utilization of the 6 t Van capacity is 70 percent. Finally, the use of the dynamic capacity of the vehicle is low, which could impact badly in the efficiency of the distribution process.

4 Conclusions

It is appropriate to carry out a strategy to prevent pollution that allows the creation of an environmental training supported by strategic, tactical and operational decisions, that are the bases for the design of a recovery logistic system, permitting the evaluation of the waste generated in the current supply chain.

The collection is a fundamental process of the recovery logistic system, which consist of collecting the waste and deliver the container for its later collection, this task is only possible by connecting all the waste generators with the collection centre throughout the design of a collection and distribution network. Therefore, the waste vegetable oil collection is a vehicle routing problem with simultaneous deliveries and collection, considering time restrictions and a heterogeneous vehicle fleet.

The VRDSPTW is a complex problem, due to the process’s restrictions and the number of nodes that form part of the network, therefore, it was necessary for the current problem the utilization of simulated recursive metaheuristic, which made possible to reach a feasible solution in less time, obtaining 49 WVO generation points. Finally, the analysis of the previous results obtained by the free VPRPD software, showed 8 routes for a vehicle capacity utilization of 70 percent in the 6 t vehicle and 46 percent in the 8 t vehicle, highlighting lower exploitation of the dynamic capacity.

The results presented in this investigation are the beginning of a project to design a logistic system for the recovery of waste vegetable oil. Therefore, in future studies the following elements should be considered:

- Analysis of the collection centre’s capacity to deal with an increase in the volume of residual to be collected.
- Include transport indicators as restrictive elements of the model.
- Combine the collection of waste vegetable oil generated by the restaurant and the domestic sector.
- Make an assignment of the clients that would be attended by the collection centre itself and by the contracted company, seeking better use of vehicular capacity and resource optimization.

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