Terahertz Transmission Characteristics of Free-Standing Fractal Jesus-Cross Structure

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We have fabricated a Jesus-cross structure on aluminum foil using the femtosecond laser technique. Using the terahertz time-domain spectroscopy (THz-TDS) system, the transmission properties of free-standing double-layer crossing fractal structure are tested. The parameters of the proposed structure were optimized using the finite element frequency domain technology of commercial software CST Microwave Studio package. The dimensions of the aluminum foil periodically patterned with crossing fractal structure are $1.5 \times 1.5 \text{ cm}^2$. The resonant frequencies of the proposed structure are 0.216 and 0.735 THz with 3-dB bandwidths of 62 and 15 GHz, respectively. The transmission ratio can reach to 0.89 and 0.57. It indicates the structure having dual-band filtering performance. This work has the potential to open a new avenue as a filter working for free-space terahertz radiation.

Keywords: terahertz transmission, transmission ratio, fractal, CST, THz-TDS

INTRODUCTION

Nowadays, terahertz (THz) wave has attracted widespread concern due to its unique applications such as wireless communication, imaging, security, etc. As an essential part of a terahertz wave system, terahertz wave manipulation is highly required. Different functional THz devices have been reported, such as modulator [1], filters [2, 3], switches [4–6], phase shifters [7], polarizers [8], absorbers [9, 10], and splitters [11–13]. We all know that terahertz wave filter is a kind of important signal processing device [14–16]. However, most of the reported terahertz filters are fabricated using photolithography processes, which results in high cost and is time consuming. Recently, various concepts of terahertz wave filters utilizing liquid crystal, frequency selective surface (FSS), graphene, photonic crystal, or metamaterial have been described [17–24]. To the best of our knowledge, relatively few studies on simple and efficient method to fabricate terahertz filter are reported. Therefore, terahertz filters are required for further research, and it is very valuable to find a simple method for fabricating terahertz filter.

In this article, we present a free-standing double-layer crossing fractal structure, which consists of symmetrical periodic metallic crossing fractal patterned on aluminum foil. We demonstrate a technique using femtosecond laser for aluminum foil fabrication to make a compact and free-standing terahertz band-pass filter. Theoretical simulation was carried out using the full-wave finite element frequency domain method of the commercial software CST Microwave Studio package. The measured terahertz transmission response spectrum shows a reasonable correspondence with simulation. The designed structure has simplicity, small size, high transmittance, and low loss.
In addition, the free-standing double-layer crossing fractal-based terahertz filters are suitable for application in terahertz systems due to their small size and fabrication using femtosecond laser high-precision micromachining technology. This work has the potential to open a new avenue as a dual-band filter working for free-space terahertz wave radiation.

**DEVICE STRUCTURE DESIGN AND PARAMETERS STUDY**

The structure of the present free-standing crossing fractal is depicted in Figure 1. The array of crossing fractal structures is fabricated on aluminum foil with a conductivity of $3.56 \times 10^7$ S/m. The geometrical parameters of the crossing fractal unit cell are $a$, $g$, $h$, and $t$. The structure is calculated using CST Microwave Studio. The unit cell is applied with periodic boundary conditions. Terahertz propagation vector is perpendicularly incident to the crossing fractal structure. The optimized dimensions of the crossing fractal structure are as follows: $a = 500 \mu$m, aluminum foil thickness of $10 \mu$m, $t = 45 \mu$m, $h = 480 \mu$m, $s = 135 \mu$m, and $g = 30 \mu$m. Here, we have simulated the frequency behavior of the power transmission based on the varied parameters such as lattice period $a$ and distance between two layer aluminum foils $t$. Figure 2 shows the frequency behavior of the crossing fractal-air-crossing fractal power transmission for different lattice periods of the crossing fractal geometrical parameter $a$ as the other parameters using their optimized values. From Figure 2, one sees that the lattice period $a$ mainly controls the first resonance frequency of the proposed structures. Particularly, it can be found that the first resonance frequency moves downward as the lattice period $a$ increases. For the crossing fractal-air-crossing fractal structure, one can see that the first resonant central frequency is 0.24 THz with transmittance of 0.96. At this time, the 3-dB bandwidth is 0.189–0.287 THz, covering the terahertz communication region, when $a$ equals $500 \mu$m. In addition, the second resonant central frequency is 0.64 THz. The 3-dB bandwidth is from 0.584 to 0.704 THz.
When the distance between two layer aluminum foils \( (t) \) changes from 35 to 55 \( \mu \)m, the other sizes of the proposed crossing fractal structure still adopt the optimized values. Figure 3 depicts the terahertz power transmission with different frequencies. It can be noted that the first and the second resonance central frequencies move downward as the distance between two layer aluminum foils of the parameter \( t \) is increased on the crossing fractal-air-crossing fractal structure. When \( t \) is equal to 45 \( \mu \)m, the two resonant peaks are of 0.24 and 0.64 THz, respectively. The 3-dB bandwidth of the first and second resonance peaks range from 0.189 to 0.287 THz and from 0.584 to 0.704 THz, respectively. To

![Figure 3: Terahertz power transmission with different frequencies.](image1)

![Figure 4: Electric field distribution.](image2)

![Figure 5: Photography of the fabricated structure.](image3)
cover the terahertz communication frequency band, we set the gap between two layer aluminum foils ($t$) as 45 $\mu$m. To clarify the transmission mechanism of the proposed structure, we simulated the electric field and surface current of the double-layer crossing fractal structure. From Figures 4A,B, we can find that the resonance of 0.24 THz is generated by the electric dipole response of two perpendicular crossing arms. The surface current mainly flows on the perpendicular metal arms of the crossing fractal pattern (see Figure 4B). For the resonance frequency of 0.64 THz, as shown in Figures 4C,D, the resonance is stimulated by the electric dipole response of the horizontal arm. The surface free charge accumulated at the left and right areas of the horizontal arm forms the external electric field (see Figure 4D). It is pretty obvious that the first and the second transmission peaks are associated with the resonances of the crossing fractal structure.

**FABRICATION AND MEASUREMENT**

According to the optimized physical dimensions, the proposed free-standing crossing fractal structure is fabricated on a 10-$\mu$m aluminum foil with a conductivity of $3.56 \times 10^7$ S/m using an ultrafast high-intensity laser technique. The femtosecond laser has 45 fs pulse width, 800 nm wavelength, and 1 kHz repetition rate. In addition, the laser with 50 $\mu$J pulse energy, 10 $\mu$m spot size, and 1 mm/s moving speed is employed to fabricate the crossing fractal structure. The aluminum foil is placed on a precise computer-controlled platform. An objective lens is used to focus the femtosecond laser on the aluminum foil surface. Figure 5 shows the photography of the fabricated structure and a local enlarged microscopic image. A Z2 THz-TDS system from Zomega Co. Ltd. is employed to test the terahertz power transmission of the present crossing fractal-air-crossing fractal structure at room temperature of 25$^\circ$C. To achieve a high signal/noise ratio in the frequency range from 0.2 to 0.8 THz, each spectrum was obtained by averaging three scans. Thus, the results provided here are repeatable and credible. Figure 6 shows the measured and simulated transmittance spectra of the proposed crossing fractal structure. The transmittance of the single-layer structure can be given by $S = |S_{21}|^2$, where $S_{21}$ is the transmission coefficient. Similarly, the power transmittance of the two-layer structure is expressed as $T = |S|^2$. The measured results show that the crossing fractal-air-crossing fractal structure has a 3-dB bandwidth of 62 GHz from 0.216 to 0.278 THz with center frequency located at 0.245 THz, and 15 GHz from 0.66 to 0.81 THz with center frequency located at 0.735 THz. The first and the second transmission peaks of the crossing fractal-air-crossing fractal structure are 0.89 and 0.57, respectively. The experimental result has some striking discrepancy with the simulation due to the limitation of its mechanical tolerance, which has been neglected in our simulation.

**CONCLUSION**

In summary, we proposed a dual-band terahertz band-pass filter based on the free-standing crossing fractal structure working for free-space terahertz radiation. We analyzed the filtering spectrum performance with various geometrical parameters of the double-layer crossing fractal structure. Using the femtosecond laser technique, we have fabricated double-layer Jesus-cross structure on aluminum foil. The frequency response of the filter is tested using THz-TDS. The resonant peaks of the filter are at 0.245 THz with the transmittance of 0.89 and 0.735 THz with the transmittance of 0.57, respectively. The experimental result has some discrepancies with those of our simulation. Owing to the symmetrical characteristic of the free-standing crossing fractal structure, the proposed filter is polarization insensitive. Our design will have great potential applications in terahertz communications, imaging, and terahertz sensor systems due to its simple structure and ease of manufacturing.

**DATA AVAILABILITY STATEMENT**

All datasets generated for this study are included in the article/supplementary material.

**AUTHOR CONTRIBUTIONS**

R-HX carried out the whole experiment. JL wrote the paper. All authors discussed the results and contributed to the paper.

**FUNDING**

This work was supported by the National Natural Science Foundation of China (Grant Nos. 61871355 and 61831012).
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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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