Research Article

Investigating the Fatigue Characteristics of Large Stone Asphalt Mixtures Based on the Disturbed State Concept

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The mechanical response characteristics of large stone asphalt mixtures (LSAMs) are key factors in studying its fatigue characteristics during cyclic loading tests. Based on disturbed state concept (DSC) and viscoelastic continuum damage model (VECD), a series of tests using an overlay test (OT) were carried out to investigate the fatigue characteristics of LSAM. The results showed that disturbance and damage increased with decreasing frequency and increasing loading displacement and aging degree, while the asphalt content had no obvious adverse effect on the increase in damage. In addition, the disturbance and damage grew rapidly in the early stage of loading and reduced in the later stage of loading. On the contrary, based on DSC, the constitutive model modified with disturbance function \(D\) defined by external work could describe the mechanical properties, and the evolution process of disturbance function \(D\) could reflect the damage change in cyclic loading tests. The research conclusion can enrich the theoretical research on the fatigue failure response and mechanism of LSAM under cyclic loading and expand the application scope of DSC in the field of pavement.

1. Introduction

Semirigid materials are prone to fatigue cracking under repeated traffic loads and thermal gradients, which will destroy the pavement structure [1–4]. The inhomogeneity of the internal microstructure of asphalt mixtures will lead to differences in the damage location and mode [5, 6]. External environmental factors, such as test temperatures, aging, and loading, increase the complexity of describing fatigue characteristics of asphalt mixtures [2, 7]. To improve the fatigue resistance of asphalt mixtures, a variety of innovative products and technologies have been proposed in recent years. It is noteworthy that, with its nominal diameter of the largest dimension greater than 26.5 mm, LSAM has a good retarding effect on crack propagation because coarse aggregates can form a stable skeleton structure [8–11]. A great deal of attention has focus on fatigue behavior of conventional asphalt mixture. However, there are relatively few research studies on LSAM fatigue performance, especially on its constitutive model.

The applications of the viscoelastic continuum damage (VECD) model for predicting the fatigue performance of asphalt mixtures have been widely used in the past two decades [12–14]. Wang and Kim proposed a failure criterion by using the VECD model and considered that the attenuation of the pseudostiffness is a material constant that is independent of the loading mode, temperature, and stress/strain amplitude [15]. Babadopulos et al. studied the fatigue performance of aged asphalt mixtures using the VECD model [16]. Haddadi et al. used the VECD model to study the fatigue behavior of asphalt mixtures. The material constant \(a\) was inversely proportional to the slope of the central part of the relaxation modulus curve obtained by the bending dynamic test with a four-point bending beam device [17]. Sabouri and Kim proposed a new failure criterion using the VECD model and pointed out that the characteristic relationship between the average release rate of the pseudostrain energy and the final fatigue life during fatigue testing of recycled asphalt mixtures and nonrecycled asphalt.
mixtures was independent of the loading mode, strain amplitude, and temperature [18].

Furthermore, numerous studies have proposed quantitative methods for investigating damage and establishment of constitutive models [5, 7, 19–22], but these methods still have some shortcomings in reflecting the damage evolution and establishment of constitutive models of materials. From a macroscopic perspective, the influence of the change in the material structure on the mechanical properties has received increasing attention. The disturbed state concept (DSC) provides a unified modeling method for engineering materials [23–26], which can consider various responses such as elasticity, plasticity, creep, microcracking and fracture, softening, and healing within a unified coupling framework. However, due to the lack of test data for calibration and field measurement for validation, DSC has not been widely used in the field of pavement.

Although the literature shows wide application prospect of VECD in fatigue performance of conventional asphalt mixtures, few studies have applied VECD approach into the results of the OT fatigue test on LSAM. In this study, the OT test is employed to investigate the fatigue performance of LSAM, including assessment the effects on fatigue performance of frequency, loading displacement, asphalt-aggregate ratio, and aging degree. In addition, this paper establishes a constitutive model of LSAM under repeated loading-based DSC model. Disturbance $D$ was used to determine evolution of damage in materials. Meanwhile, the effects of frequency, loading displacement, asphalt-aggregate ratio, and aging degree on fatigue performance and change in disturbance were detected as well. The research conclusion not only enriches the theoretical research on the fatigue performance of LSAM under cyclic loading but also expands the application scope of DSC in the field of pavement.

2. Materials and Methods

2.1. Materials and Specimen Preparation. In the test, the binder is AH-70 heavy traffic paving asphalt, the aggregates are limestone aggregates, and the filler is limestone ore powder. The aggregate gradation design for LSAM-30 is shown in Table 1. The LSAM-30 test results and the technical specifications obtained from the Marshall test are shown in Table 2. Therefore, the optimum asphalt-aggregate ratio is 3.38%. Referring to the method of T0703-2011, which is stipulated in JTGE20-2011 [27], test specimens are trimmed into prismatic specimens with dimensions of 150 mm $\times$ 100 mm $\times$ 60 mm originating from a rutting plate with dimensions of 300 mm $\times$ 300 mm $\times$ 100 mm. In the short-term aging test, the rutting plates were made. In the study, test temperature was set at 25°C, and specific test conditions are shown in Table 3. The loading displacement waveform is shown in Figure 1. The output data from the OT test are shown in Figure 2. Peak load, number of cycles, and temperature are automatically recorded. An example of measured load and number of cycles is shown in Figure 2(a), and the peak load against number of cycles is shown in Figure 2(b). As shown in Figure 2, with the increase in the number of cycles, the peak load gradually decreases until fracture. During the test, three parallel tests were carried out for each group of specimens, and the average value of the test results was obtained. The specimen gluing process was performed as follows: (1) ensure that the bonding surface of the specimen and base plate was clean; (2) apply Vaseline on the spacer bar and inserted the spacer bar between the base plates; (3) place a piece of tape to cover the gap; (4) glue the specimens to the base plates with epoxy; and (5) add a 2.5 kg weight on top of the specimen for no less than 24 hours at room temperature. In each group, three specimens were placed in the environment box for no less than 4 hours, and the temperature was set at the test temperature $\pm 0.5^\circ$C. Displacement control was applied during the test.

3. VECD Model and DSC Model

3.1. VECD Model. The mathematical expression of the pseudostrain is shown in (1a), where $e = D/d$, in which $D$ and $d$ are the tension displacement and steel plate spacing, respectively (shown in Figure 1), and $E(t − τ)$ is relaxation modulus which can be obtained by a Prony series in the first load stage from OT, as shown in (1b):

$$\varepsilon^R(t) = \frac{1}{E^R} \int_0^t E(t − τ) \frac{\partial e}{\partial τ} dτ,$$  \hspace{1cm} (1a)$$

$$E(t) = E_{∞} + \sum_{i=1}^{N} E_i e^{−(t/\tau_i)},$$  \hspace{1cm} (1b)
where $E(t)$ is the relaxation modulus, $E_\infty$ is the long-term equilibrium modulus, $E_i$ is the components of relaxation modulus, $\rho_i$ is the relaxation time, and $N$ is the number of elements in Prony series.

Based on the concept of the pseudostrain and continuous damage theory, the pseudostiffness $C$ is the ratio of the peak stress to the corresponding pseudostrain [17]:

$$C = \frac{\sigma}{I \times \varepsilon^R}.$$  \hspace{1cm} (2)

where $I = \sigma_i/\varepsilon_i^R$ is the variable used to normalize pseudostiffness $C$ and $\sigma_i$ and $\varepsilon_i^R$ are the stress and pseudodisplacement at the end of the first cycle, respectively.

The $C$-$S$ curve under the uniaxial tension test is different from that under the uniaxial compression test. Likewise, the $C$-$S$ curve under the tension-compression test is different from that under the uniaxial tension test. Researchers believe that damage only accumulates in the tensile portion of each cycle [33, 34]. Park et al. [35] calculated the damage parameter $S$ in asphalt mixtures by using the following equation:

$$dS \over dt = -I \varepsilon^R \frac{dC}{dt} \frac{\alpha}{1 + \alpha}, \hspace{1cm} (3)$$

where $W^R$ is the pseudostrain energy density function, $\alpha$ is a constant related to the rate of damage growth, and $t$ is the time. $\alpha = 1 + (1/m)$ for strain-controlled tests, while $\alpha = 1/m$ for stress-controlled tests, where $m$ represents the maximum slope of the relaxation modulus vs. the time graph in log-log scale. For asphalt mixtures, the functions of the stress and pseudostrain energy density under uniaxial loading are expressed as follows:

$$\sigma = \frac{\partial W^R}{\partial \varepsilon^R} = I C(S)\varepsilon^R, \hspace{1cm} (4)$$

$$W^R = \frac{I}{2} C(S)\varepsilon^R. \hspace{1cm} (5)$$

Damage parameters $S$ are obtained from formulas (3) and (5):

$$dS \over dt = -I \varepsilon^R \frac{dC}{dt} \frac{\alpha}{2} \frac{dN}{dt} \left(\frac{\alpha + 1}{\alpha} \right). \hspace{1cm} (6)$$

In repeated load tests, the following relationships are established:

$$N = ft \rightarrow \frac{dN}{dt} = f \rightarrow dt = \frac{dN}{f}, \hspace{1cm} (7)$$

where $N$ is the number of cycles and $t$ is the time. In consideration of $(\partial C/\partial t) = (\partial C/\partial N)(\partial N/\partial t)$ and $(\partial S/\partial t) = (\partial S/\partial N)(\partial N/\partial t)$, the following equation is derived from (6):

$$dS \over dN \frac{f}{f} = -I \varepsilon^R \frac{\partial C}{\partial N} \frac{1}{2} \frac{dN}{dt} \left(\frac{\alpha + 1}{\alpha} \right). \hspace{1cm} (8)$$

$$S_M = \sum_{i=1}^{M} \left( I \varepsilon_i^R \frac{C_{i+1} - C_i}{f} \right)^{\alpha} \left( N_t - N_{i-1} \right) \frac{f}{1 + \alpha}, \hspace{1cm} (9)$$
3.2. Constitutive Model Based on the DSC. In the DSC model, the forces (mechanical force and thermal and environmental forces) cause a disturbance of the material microstructure, resulting in material changes in the internal microstructure from a relatively intact state (RI) after an automatic adjustment process to a fully adjusted state (FA). This self-adjusting process may involve the relative movement of particles that produce microcracks and damage. It can cause obvious disturbance. This disturbance is defined by a disturbance function $D$, which represents the relationship between the observation response and initial response and describes the evolution of the disturbance with the macroscopic mechanical response to simulate the constitutive relationship of the materials:

$$d\sigma_{ij} = (1 - D)d\sigma_{ij}^r + Dd\sigma_{ij}^d + dD\left(\sigma_{ij}^r - \sigma_{ij}^d\right), \quad (10a)$$

$$d\sigma_{ij}^n = (1 - D)C_{ijkl}d\epsilon_{kl} + DC_{ijkl}d\epsilon_{kl}^d + dD\left(\sigma_{ij}^n - \sigma_{ij}^d\right), \quad (10b)$$

where $\sigma_{ij}$ and $\epsilon_{ij}$ are the stress and strain, respectively; $C_{ijkl}$ is the elastic coefficient; and $a$, $i$, and $c$ represent the observation state, RI, and FA, respectively.

The relative intact (RI) state is defined by an ideal elastic-plastic model, and for the uniaxial stress state, the elastic coefficient tensor $C^e = E$ ($E$ is the elasticity modulus). The fully adjusted (FA) state under uniaxial tension is defined based on the approximation of the ultimate asymptotic response of the material, and the ultimate tensile stress $\sigma^c$ is defined by the stress during material failure.

Figure 3 shows a schematic diagram of the mechanical response of a material in a DSC model and the first cycle hysteretic loop curve in the low cycle fatigue test. For the loading section of the first period, as shown in Figure 3, the linear relationship between the load and displacement is obvious. It shows that the material maintains an elastic deformation in the first period of loading, and it is considered that there is no damage in the material at this stage. Therefore, the first loading period is considered as the RI; thus, the work of the external force during the first loading process is $W_0$.

During the loading process, the work done by the external force per cycle is $W_j$, and the work done by the external force in the last cyclic loading cycle is $W_C$. Thus, the disturbance $D$ is defined as
According to the fatigue test on the asphalt mixture, the cumulative disturbance is nonlinear. The evolution equation of the disturbance can be expressed as follows:

\[ D = 1 - \left[ 1 - \left( \frac{N}{N_f} \right)^r \right]^a, \quad (12) \]

where \( r \) and \( a \) are fitting parameters and \( N \) and \( N_f \) are the number of loading cycles and fatigue life, respectively. Based on the RI and FA states and once disturbance is defined, the DSC equations under repeated loading can be derived as

\[ \sigma_{ij}^F = (1 - D)\sigma_{ij}^F + D\sigma_{ij}^F. \quad (13) \]

After normalizing the peak load of each cycle, (13) can be expressed as follows:

\[ \frac{\sigma_{ij}^F}{\sigma_{ij}^{(1)}} = (1 - D)\frac{\sigma_{ij}^F}{\sigma_{ij}^{(1)}} + D\frac{\sigma_{ij}^F}{\sigma_{ij}^{(1)}}. \quad (14) \]

where \( \sigma_{ij}^F \) is the observed stress in the fatigue test, \( \sigma_{ij}^F \) is the stress in the RA, \( \sigma_{ij}^{(1)} \) is the stress in the FA, \( \sigma_{ij}^{(1)} \) is the maximum stress in the first loading cycle, and \( D = \frac{N}{N_f} \) is the disturbance corresponding to each loading cycle.

4. Results and Discussion

In the C-S curve (in Figure 4), \( S \) represents the damage in the specimens during the test, and \( C \) represents the normalized pseudostiffness. The slower the C-S curve descends, the longer the curve is, the better the performance of the asphalt mixture will be. It can be seen from Figure 4 that the pseudostiffness decreases with increasing damage, and the rate of decrease in the pseudostiffness in the early stage is faster than that in the later stage. The C-S curves of 5 Hz and 10 Hz are higher than that obtained for 1 Hz, which indicates that increasing the frequency can slow down the damage development rate and prolong the service life. The decline rate of the C-S curve of 0.1 mm is slower than that of 0.2 mm and 0.3 mm, but the curve of 0.3 mm decreases faster. This indicated that increasing the loading displacement will accelerate the damage and failure of the specimens. The C-S curve of the asphalt-aggregate ratio of 3.6% is shorter and lower than that of the other two asphalt-aggregate ratios. The two curves of 3.38% and 3.9% indicate that increasing the asphalt content does not substantially improve the tensile strength, but increasing the asphalt content can prolong the fatigue life of the specimens. The C-S curve becomes shorter after aging, and the rate of decrease gradually increases with the aging degree, which indicates that aging has an effect on the fatigue life. The brittleness of the aged asphalt mixtures increases, the damage increases rapidly with increasing aging degree, and the fatigue life of the aged asphalt mixtures decreases.

It can be seen from Figure 5 that the disturbance increases rapidly in the early stage of loading displacement; when the fatigue life ratio is approximately 0.2, the disturbance increases slowly. This indicates that the integrity of the materials decreases substantially, and the damage increases rapidly during early loading. However, the damage increases slowly, and the rate of cumulative damage slows down during later loading. The disturbance decreases with the increase in the frequency until the fatigue life ratio is approximately 0.8, which indicates that increasing the loading frequency can prolong the fatigue life. The disturbance increases with the increase in the loading displacement, which indicates that the damage caused by a loading displacement of 0.1 mm is smaller than that with a larger loading displacement. The disturbance curves of the loading displacements of the 0.2 mm and 0.3 mm almost overlap, which indicates that the damage in the specimens under these two conditions does not change substantially. The disturbance curve of the asphalt-aggregate ratio of 3.6% is higher than that of the other two asphalt-aggregate ratios, which indicates that the damage develops faster when the asphalt-aggregate ratio is 3.6%. Aging will increase the modulus of the asphalt mixture and weaken its tensile strain, so aging will accelerate the development of damage in the specimens. That is, the disturbance increases with the increase in the aging degree.

Figure 6 shows evolution of pseudostiffness with the increasing number of cycles, and it suggests that an exponential function can capture the trend of pseudostiffness with the increasing number of cycles. Equation (15) is an example of fitted exponential function:

\[ y = 17.74x + 0.087 \]

\[ R^2 = 0.98 \]
\[ C = 1 - \exp\left(-A \left(\frac{N}{N_f}\right)^Z\right), \] (15)

where \( A \) and \( Z \) are fitting coefficients. It can be seen from Figure 6 that the curve can be fitted well by an exponential function, and the pseudostiffness develops rapidly in the early stage but slows down in the later stage, which is consistent with the variation trend of the disturbance curve. This indicates that the DSC model proposed in this paper can effectively reflect the evolution of damage.

The calculation results of the parameters in (12) and (15) are shown in Table 4. It can be seen from Table 4 that parameters \( r \) and \( a \) increase with increasing frequency. An increasing loading displacement will increase parameter \( a \), while parameter \( r \) shows a trend of decreasing first and then increasing. The increase in the asphalt content and aging will decrease parameter \( a \). Both parameters \( A \) and \( Z \) decrease with increasing displacement. \( Z \) decreases with increasing frequency. Increasing the asphalt content will increase parameter \( Z \), while aging will decrease parameter \( Z \).

Figure 7 shows the test results and theoretical calculation results of the peak load varying with the loading cycle. The relationship between the peak load obtained from the test and the number of cycles is in good agreement with the calculated results, which indicates that the proposed constitutive model under repeated loading can reflect the variation in its mechanical properties. The increase in the frequency and loading displacement can substantially increase the peak load. The influence of aging and increasing the asphalt content on the peak load is not obvious, but increasing the asphalt content can delay the load attenuation.
Figure 5: Disturbance $D$ characteristic curves corresponding to the (a) frequency, (b) loading displacement, (c) asphalt-aggregate ratio, and (d) aging degree.

Figure 6: $C - N/N_f$ curve (10 Hz).

$y = 1 - \exp(-0.096x^{-0.46})$

$R^2 = 0.97$
Table 4: The calculation parameters.

| Test conditions | $r$  | $a$  | $A$  | $Z$  |
|-----------------|------|------|------|------|
| Standard        | 0.4  | 1.93 | 0.159| -0.422|
| Group 1 1 Hz   | 0.053| 0.82 | 0.154| -0.285|
| 5 Hz           | 0.25 | 1.8  | 0.125| -0.379|
| Group 2 0.1 mm | 0.28 | 0.85 | 0.598| -0.173|
| 3.6%           | 0.22 | 1.93 | 0.131| -0.321|
| Group 3 3.9%   | 0.25 | 1.34 | 0.194| -0.253|
| Group 4 Short aging | 0.26 | 1.96 | 0.113| -0.375|
| Long aging     | 0.24 | 1.18 | 0.151| -0.435|

Note. The standards in Table 4 are as follows: the asphalt-aggregate ratio is 3.38%, the temperature is 25°C, the loading frequency is 10 Hz, the displacement amplitude is 0.3 mm, and nonaging.

Figure 7: Test and theoretical curves corresponding to the (a) frequency, (b) loading displacement, (c) asphalt-aggregate ratio, and (d) aging degree.
speed, which is conducive to delaying the development of cracks, while aging can accelerate the load attenuation speed and crack expansion.

5. Conclusions

In this paper, a constitutive model of the LSAM under repeated loading is proposed based on the DSC theory. Through the analysis of the fatigue characteristics of the LSAM under different conditions, it is shown that the model proposed in this paper can reflect its mechanical properties, and the disturbance can reflect the damage evolution during the fatigue process. The conclusions are summarized as follows:

(1) Damage develops rapidly in the early stage of loading and slows down in the later stage of loading. Damage increases with the decrease in the frequency, the increase in the loading displacement, and the increase in aging degree. The asphalt content has no obvious adverse effect on the increase in damage.

(2) The magnitude of the disturbance reflects the damage degree. The results show that the disturbance increases with decreasing frequency and increasing loading displacement and aging degree. The pseudo-stiffness evolution model in this study can reflect the relationship between the pseudo-stiffness and the number of loading cycles.

(3) The VECD model can effectively reflect the fatigue characteristics of the LSAM. Increasing the loading displacement, decreasing the frequency, and increasing the aging degree will increase the decline rate of the C-S curve. That is, the fatigue life will be shortened.

Data Availability

The data used to support the findings of this study are available from the corresponding author upon request.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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