Influence of Carbon Concentration on the Superconductivity in MgC$_2$Ni$_3$

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The influence of carbon concentration on the superconductivity (SC) in MgC$_2$Ni$_3$ has been investigated by measuring the low temperature specific heat combined with first principles electronic structure calculation. It is found that the specific heat coefficient $\gamma_n = C_{cn}/T$ of the superconducting sample ($x \approx 1$) in normal state is twice that of the non-superconducting one ($x \approx 0.85$). The comparison of measured $\gamma_n$ and the calculated electronic density of states (DOS) shows that the effective mass renormalization changes remarkably as the carbon concentration changes. The large mass renormalization for the superconducting sample and the low $T_c$ (7K) indicate that more than one kind of boson mediated electron-electron interactions exist in MgC$_2$Ni$_3$.

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The recently discovered superconductor MgCNi$_3$ with an anti-perovskite structure has attracted renewed attention, because it is a new intermetallic compound following the remarkable discovery of MgB$_2$ and is thought to be very close to ferromagnetism (FM) due to a large proportion of Ni in each unit cell. Experiments have shown that the superconductivity (SC) in MgC$_2$Ni$_3$ is very sensitive to the content of carbon and disappears below about $x = 0.88$. Moreover, Ni-site doping with Cu (electron doping) and Co (hole doping) have very different effects.

Many efforts have been focused on the origin of SC in MgC$_2$Ni$_3$. Some researchers explored the possibility of conventional phonon-coupled pairing. However, various experiments and theoretical calculations have not given a consistent coupling constant $\lambda$ in the frame of electron-phonon coupling (EPC) mechanism. For example, $\lambda \approx 1-1.6$ was estimated from the calculated plasma frequency ($\omega_p$) and measured resistivity, while the measured upper critical field $H_{c2}$ was suggested a much larger value of $\lambda \approx 2.5 - 3$. Furthermore, two discrepant values of $\lambda = 0.7$ and 2.2 were determined in the similar specific heat measurements by taking different approximations. Besides these confusing results, it has been proposed that EPC is possibly not the only contribution to the coupling mechanism in MgC$_2$Ni$_3$. Opposed to the conventional pairing mechanism, it was suggested that FM and SC may coexist due to the ferromagnetic instability caused by the high density of electronic states (DOS) at the Fermi energy ($E_F$). NMR experiment confirmed the presence of substantial ferromagnetic spin fluctuations in MgCNi$_3$, while it also exhibited a clear coherence peak of the nuclear spin-lattice relaxation rate just below $T_c$, which is typical for an isotropic s-wave superconductor. More recently, Voelker et al. proposed that MgCNi$_3$ could be a multiband superconductor with a conventional phonon mechanism similar to MgB$_2$. Thus, the origin of SC in MgCNi$_3$ is still controversial. One of the most illuminative methods is to study the influence of element-substitution on SC.

In this Letter, we compare the specific heat data of a superconducting MgC$_2$Ni$_3$ with $x \approx 1$ and that of a non-superconducting one with $x \approx 0.85$. Using the tight-binding linear muffin-tin orbital (TB-LMTO) band method and coherent potential approximation (CPA), we investigate the carbon concentration dependence of the electronic structure of MgC$_2$Ni$_3$. Combining the results of the specific heat and band calculations, we propose a self-consistent picture to understand the reduced SC in non-stoichiometric MgC$_2$Ni$_3$.

Poly-crystalline samples of MgC$_2$Ni$_3$ were prepared by powder metallurgy method. Details of the preparation were published previously. The superconducting transition of the stoichiometric sample (SC1) with $T_c = 7K$ is shown in Fig. 1. A non-superconducting sample (NSC08) was synthesized by continually reducing the carbon component until the diamagnetism was completely suppressed. X-ray diffraction (XRD) patterns show nearly single phase in both samples. The lattice parameters $a$ determined from XRD are 3.812A and 3.790A for SC1 and NSC08, respectively. By comparing these lattice parameters with the reported $a \sim x$ relation, we could estimate the carbon content as $x = 0.977$ and 0.850 for SC1 and NSC08, respectively. According to the $T_c \sim x$ relation presented in Ref., $x = 0.977$ corresponds to $T_c \approx 7K$ and $x = 0.850$ is very close to the critical stoichiometry of SC in MgC$_2$Ni$_3$, which is in good agreement with our experimental results. The temperature dependence of the normalized resistivity is shown in Fig. 1. The heat capacity data presented here were taken with the relaxation method based on an Oxford cryogenic system Maglab, in which the heat capacity is determined by a direct measurement of the thermal time constant, $\tau = (C_s + C_{add})/\kappa_w$, here $C_s$ and $C_{add}$ are the heat capacity of the sample and addenda, respectively, while
$\kappa_w$ is the thermal conductance between the chip and a thermal link. During the measurement the sample was cooled to the lowest temperature under a magnetic field (field-cooling) followed by data acquisition in the warming up process. The addenda includes a small sapphire chip, a tiny Cernox temperature sensor, small amount of Wakefield thermal conducting grease and gold leads ($\phi 25 \mu m$). All contributions to the heat capacity from the addenda have been measured separately and subtracted from the total specific heat before further analysis.

The typical low temperature specific heat at various magnetic fields up to 12 Tesla is presented in Fig. 2. For sample NSC08, all the data fall into an universal curve, indicating the independence of its specific heat on the magnetic field. For sample SC1, all the data above $T_c$ are independent on the field, and the normal state extends to the whole temperature region investigated here when $H \geq 10T$. The upper critical field $H_{c2}(T)$ can be determined from the position of the specific-heat jump, and $H_{c2}(0) \approx 117T$ is then derived by extrapolating $H_{c2}(T)$ to 0K. In order to describe the specific heat data of NSC08 and the normal state data of SC1, we use the following expression:

$$ C_n(T) = \gamma_n T + \beta T^3 + \delta T^5 $$  \hspace{1cm} (1)

where the linear-T term is the electronic contribution with $\gamma_n$ as Sommerfeld parameter, the second term represents the phonon contribution according to the Debye approximation, the last term is required to include deviations from the linear dispersion of the acoustic modes in extended temperature range. The fitting results are presented in Fig. 2 and the obtained parameters are shown in Table I. Besides the obvious difference between the Debye temperatures ($\Theta_D$) of SC1 and NSC08 (due to the larger elastic modulus of NSC08 than that of SC1), a more prominent difference is found between the Sommerfeld parameters $\gamma_n$ of these two samples, this is one of the main results in this work.

Before further analysis, we first investigate the specific heat data of the superconducting sample SC1 in zero field, as shown in the lower inset of Fig. 2. The solid curve represents the theoretical fits, the part above $T_c$ is the fitting result to the normal state data of SC1 as mentioned above, while the part below $T_c$ is an attempt to describe the data using the specific heat expression of conventional superconductor: $C_{cs} = A \exp(-\Delta(0)/k_B T)/T^3$, in which $A$ is a function of zero-temperature energy gap $\Delta(0)$ and the normal-state DOS $g(0)$. This equation is a low temperature approximation and is not adequate above $0.8T_c$ where $\Delta(T)$ has substantially deviated from $\Delta(0)$. This conventional expression can fit our data below $0.8T_c \approx 5K$ quite well, though the returned $\Delta(0)$ (1.46meV) leads to a large value of $2\Delta(0)/k_B T_c \approx 5$ comparing with the weak coupling value 3.5. This indicates that MgCNi$_3$ is a strong coupling superconductor, being consistent with the large value of $\Delta C/\gamma_n T_c \approx 1.7$ (the expected value for weak coupling is 1.43), where $\Delta C$ is the specific heat jump at $T_c$. As shown above, the specific heat coefficient $\gamma_n$ of SC1 is almost twice that of NSC08. In the frame of strong coupling mechanism, given the value of $\gamma_n$ and $N(E_F)$,

![FIG. 1: The temperature-dependent resistivity (normalized by the value at 300K) of the samples SC1 and NSC08. Inset: The enlarged view of the superconducting transition in AC susceptibility measurement.](image1)

![FIG. 2: A plot of $C/T$ vs $T^2$ for MgCNi$_3$ (SC1) and MgCa$_{0.85}$Ni$_3$ (NSC08) in various magnetic fields. The solid lines are fits to Eq. 1 as discussed in the text. The specific heat jump at the superconducting transition temperature is completely depressed by the field above 10T. Upper inset: The low-temperature specific heat for SC1 at various magnetic fields from 0T to 12T. Lower inset: Fitting for the zero-field specific heat data (open circles).](image2)

### Table I: Fits to Eq. 1 for samples SC1 and NSC08.

| sample | $\gamma_n$ (mJ/molNiK$^2$) | $\beta$ (mJ/molNiK$^4$) | $\delta$ (mJ/molNiK$^6$) | $\Theta_D$ (K) |
|--------|----------------|-------------------|----------------|-------------|
| SC1    | 11.3           | 0.075             | 0.00049       | 351         |
| NSC08  | 5.8            | 0.040             | 0              | 434         |
In order to obtain \( N(E_F) \), we have calculated the electronic structures using a TB-LMTO method based on Green function formalism \(^{17}\) within the atomic sphere approximation (ASA). The parameterized exchange-correlation potential of Ref. \(^{24}\) and the scalar-relativistic Dirac equation \(^{23}\) were employed. The coherent potential approximation (CPA) used in our calculation allowed us to study the electronic structure of MgC\(_x\)Ni\(_3\) for any carbon concentration. In the crystal structure of cubic antiperovskite-type MgCNi\(_3\), the atoms occupy the positions Mg (0,0,0), C (0.5,0.5,0.5), and Ni (0.5,0.5,0), (0.5,0.5,0.5), (0.0,0.5,0.5). Self-consistency was reached using 1000 k-points within the irreducible wedge of the simple cubic Brillouin zone. In the calculations, we adopted the experimental determined \(^4\) relation between the lattice parameter \( a \) and the carbon concentration \( x \). A fixed radii proportion as 2.078 : 1 : 1.617 (Mg:C:Ni) was taken for the stoichiometric situation \( x = 1 \), and only the radii of carbon-site was reduced with decreasing \( x \).

The DOS of MgC\(_x\)Ni\(_3\) for \( x = 1 \) are presented in the upper inset of Fig. 3, which is consistent with the reports of other groups \(^6\)\(^8\)\(^9\)\(^10\). The \( \pi^* \) antibonding states of Ni-3d and C-2p are located just below \( E_F \), yielding a high DOS peak whose height is proved to be sensitive to the exact method. Fortunately, the obtained value of \( N(E_F) = 4.53 \, \text{eV}^{-1} \text{cell}^{-1} \) is not far away from the result of general potential linearized augmented plane wave method \((4.99 \, \text{eV}^{-1} \text{cell}^{-1})^3\) and that of full-potential LMTO method \((4.57 \, \text{eV}^{-1} \text{cell}^{-1})^2\), which is a good starting point for the following consideration of the doping effect.

Fig. 3 shows the evolution of the DOS around Fermi level with the change of carbon concentration \( x \) in MgC\(_x\)Ni\(_3\). It is found that the Fermi level slightly shifts towards low energy with the decreasing \( x \), while the Ni3d-C2p antibonding peak is depressed remarkably. In the nearest-neighbor approximation, the degeneration of this DOS peak indicate that the carbon-site vacancies locally break the hybridization between Ni-3d and C-2p orbitals and hence lead to a redistribution of the electronic states. Atom-resolved DOS shows that the near-\( E_F \) DOS peak of Ni-3d component and that of C-2p component do not depart from each other with decreasing \( x \), indicating that carbon-site vacancies does not destroy the Ni3d-C2p bond for all carbon concentrations investigated here. Therefore, the decrease of the peak possibly means the enhanced itinerancy of electrons. As shown in Fig. 3, the depressed DOS peak just below \( E_F \) results in a notable reduction of \( N(E_F) \). The dependence of \( N(E_F) \) on the carbon concentration is presented in Fig. 4. We can see a obvious decrease of \( N(E_F) \) from 4.26\,eV\(^{-1} \) at \( x = 0.977 \) to 3.14\,eV\(^{-1} \) at \( x = 0.85 \). Moreover, the doping dependence of \( N(E_F) \) is linear above a critical doping \( x_c \approx 0.88 \) which is very close to the carbon content in NSC08 and also the lower limit of the carbon concentration for SC in MgC\(_x\)Ni\(_3\). Below \( x_c \), the doping dependence of \( N(E_F) \) becomes much weaker than that above \( x_c \).

By inserting the experimental value of \( \gamma_n \) and the calculated \( N(E_F) \) into Eq. (2), we can determine the coupling constant as \( \lambda = 2.37 \) and 1.35 for the samples SC1 and NSC08, respectively. The former is close to that reported by Wälte et al. \(^{11}\) while the remarkable difference in the coupling strength between a superconducting sample and a carbon-deficient non-superconducting one is for the first time found in the MgC\(_x\)Ni\(_3\) system. However, applying \( \lambda = 2.37 \) to the McMillan’s \( T_c \) formula \(^{27}\).
$T_c = \frac{\Theta}{1.45} e^{-\frac{1+\lambda}{\lambda_{\text{spin}}}}$ gives rise to $T_c > 30K$, which seems to be too large as compared to experimental value $T_c = 7K$. In other words, $T_c = 7K$ corresponds to $\lambda = 0.42$, which is much smaller than the value determined here. This contradiction can be resolved if we adopt the picture that there are two kinds of boson-mediated electron-electron interactions, for example, electron-phonon coupling (EPC) and spin fluctuation (SF). Due to the different effect of the spin fluctuations on mass renormalization and superconducting properties, it should add in the mass renormalization term and subtract in the pairing term for SC. So in the frame of strong coupling, the specific heat determined $\lambda$ has two contributions: $\lambda = \lambda_{\text{ph}} + \lambda_{\text{spin}}$. Similarly, the simplified McMillan’s $T_c$ formula should be modified as

$$T_c = \frac{\Theta}{1.45} e^{-\frac{1+\lambda_{\text{ph}} + \lambda_{\text{spin}}}{\lambda_{\text{ph}} - \lambda_{\text{spin}}}}$$

Using the determined parameters for sample SC1 (namely, $\lambda = 2.2$, $T_c = 7K$ and $\Theta = 351K$), one obtains $\lambda_{\text{ph}} - \lambda_{\text{spin}} = 0.95$ from Eq. (8). Combining this result with $\lambda_{\text{ph}} + \lambda_{\text{spin}} = 2.37$, we determine the strength of both EPC and electron-paramagnon coupling as $\lambda_{\text{ph}} = 1.66$ and $\lambda_{\text{spin}} = 0.71$. Firstly, by assuming that $\lambda_{\text{spin}}$ is invariable with the decreasing carbon concentration, we could obtain $\lambda_{\text{ph}} = 0.64$ for sample NSCo8. This suggests a strong dependence of the EPC strength on the carbon concentration in MgC$_2$Ni$_3$. For NSCo8, $\lambda_{\text{ph}} = 0.64$ has become smaller than $\lambda_{\text{spin}} = 0.71$, which is closely associated with the disappearance of SC. Secondly, on the assumption that $x = 0.85$ is the critical stoichiometry for SC, i.e., $\lambda_{\text{ph}} = \lambda_{\text{spin}} = 0.665$. This indicates a 6% decrease of $\lambda_{\text{spin}}$ from $x = 0.977$ to $x = 0.85$. However, $\lambda_{\text{ph}}$ is lost near 60% in the same system, which seems to be responsible for the suppression of SC in MgC$_2$Ni$_3$.

We have been aware of some recent calculations suggesting that both Co doping and Cu doping in MgCNi$_3$ lead to a reduction of $N(E_F)$, which seems to be critical in depressing SC in this system (MgCNi$_{1-x}$Y$_x$ [Y=Co or Cu]). However, these investigations were based on the ordered substitutions, i.e., $x=1$, 2 or 3, which is somewhat away from the key problem because the solubility of Cu is limited to 3% ($x = 0.1$) in technology and the bulk SC disappears for only 1% Co doping ($x = 0.03$). Our further calculations did not show obvious reduction of $N(E_F)$ in this doping range. Therefore, some necessary investigations on the variation of the EPC in this system must be supplemented.

In summary, we have investigated the specific heat data in MgC$_2$Ni$_3$ system and found a remarkable difference between the Sommerfeld parameters of a superconducting sample ($x \approx 1$) and a non-superconducting one ($x \approx 0.85$). Band calculations reveal a distinct decrease of the density of the electronic states at Fermi level with the decreasing carbon concentration. Further analysis indicate that there is more than one kind of boson-mediated electron-electron interactions existing in MgC$_2$Ni$_3$ system. In the frame of strong coupling theory, a substantial depression of the electron-phonon coupling caused by the decrease of carbon concentration is for the first time found in this system and seems to be responsible for the impairment of its superconductivity.

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