Axial Error of Spindle Measurements Using a High-Frequency-Modulated Interferometer

Thanh-Trung Nguyen*, Thanh-Tung Vu*, Thanh-Dong Nguyen and Toan-Thang Vu*

School of Mechanical Engineering, Hanoi University of Science and Technology, Hanoi 100000, Vietnam; trung.nguyenthanh2@hust.edu.vn (T.-T.N.); dong.nguyenthanh@hust.edu.vn (T.-D.N.)
* Correspondence: tung.vuthanh@hust.edu.vn (T.-T.V.); thang.vutoan@hust.edu.vn (T.-T.V.)

Abstract: In this paper, a novel, compact, and high-precision axial error measurement using a frequency-modulated interferometer is developed. Normally, heterodyne interferometers are a powerful system for small displacement measurements due to their property of being less sensitive to temperature and pressure variations. However, the maximum measurement speed of the heterodyne interferometer is around 5 m/s because it is usually limited by the difference in frequency between the two components of the laser beam, which is no larger than 3 MHz or 20 MHz corresponding laser source based on the Zeeman effect and acousto-optic modulator, respectively. The proposed measuring system is realized by modulating the frequency of the laser diode source at a high modulation frequency and using lock-in amplifiers to extract the harmonics of the interference signal. The measurement speed is proportional to the modulation frequency. Thus, the higher the modulation frequency, the higher the measuring speed attains. The frequency-modulated interferometer is then applied to measure the axial error of an ultra-precision spindle. The proposed system can be a capable solution for noncontact and high-precision spindle error measurements in the machining process.

Keywords: axial error of spindle; displacement measurement; frequency modulation; interferometry; optical instruments

1. Introduction

The error motion of the machine tool spindle causes deviation for the workpieces such as roundness, straightness, and surface roughness [1,2]. Recently, the requirements for geometric parameters and finish surface quality of mechanical parts are increasingly tight. Therefore, the control of the spindle rotational error in ultra-fine machines is an urgent demand [3,4]. Error motions are small unwanted movements of the rotation axis relative to the stationary reference coordinate axes. There are five components of this error, the first three ones are translation in the three directions x, y, and z. The fourth component is a tilting relative to the x and y axes at a specified position along the z-axis and called the radial error motion. Axial error motion is error motion colinear with z-axis direction [5–7]. Spindle error measurements play an important role in the field of ultra-precision manufacturing. Normally, a cylindrical or spherical artifact combined with noncontact sensors to measure a machine tool spindle errors was used [8,9]. Capacitive sensor and eddy current sensor are most employed. Both types of sensors can achieve a nanometer level of resolution. However, these sensors are relatively low bandwidth, sensitivity to the environment, and short stand-off distance [10,11].

Laser interferometer has emerged as an effective tool for measuring the spindle error motion of machining machines with nanometer-scale measurement uncertainty because of their inherent accuracy and accordance with the definition of meter through the frequency of the laser source. Laser interference systems have been developed such as homodyne [12–16], heterodyne [17,18], and frequency modulation technique [19–21]. The heterodyne interferometer is not greatly affected by ambient temperature and refractive
index because its beat frequency is the carrier frequency of the information and is far from
DC components and low-frequency noise sources. Some available phase measurements
such pulse counting, two-phase lock-in amplifier (LIA), two phase-locked loops (PLLs) are
developed for the heterodyne system. The pulse counting method is fast enough to cover
high-speed measurements (up to 2.1 m/s), but the discrete nature of the counting operation
limits the system resolution [18]. This resolution can be improved using the LIA with
arc-tangent operations or the PLLs with feedback loop controls. However. The maximum
measuring speed of the heterodyne interferometer is limited by the heterodyne frequency.
In addition, the complicated and high-cost systems are also their drawbacks. Homodyne
interferometers are widely employed in measuring small motion with high resolution. T.
Keem eliminated the cyclic errors to achieve an accuracy of 10 pm [15] and J. Ahn reported
a nonlinear compensation method in a homodyne interferometer to obtain sub-picometer
resolution [16]. The homodyne interferometer signal is time-independent and therefore
it enables ultra-fast response because the phase change in the interferometer converts
instantaneously into the intensity variation. Hence, homodyne interferometers have the
potential to be used in high-speed applications. However, the homodyne interferometer
requires high stability of the laser source intensity during the whole measurement. This
means that the misalignment of the optical components, disturbance of the environment,
or the shift of a measuring point will have an extreme effect on measurement accuracy.
Additionally, the moving direction of the measurement target cannot be found if only one
interference signal is available. Normally, a pair of quadrature signals are employed to treat
such drawbacks. Among these techniques, sinusoidal frequency modulation (SFM) has
many advantages. The SFM interference signal, a continuous function of time, is a series of
harmonics of the modulation frequency. The phase-shift caused by the displacement of
the target mirror in the interferometer can be accurately extracted from the interference
signal using the synchronous detection method [22,23]. Furthermore, the measurement
speed of the SFM interferometer is only limited by the modulation frequency, which can be
obtained very high by modulating the injection current on a normal laser diode (LD).

In this paper, a new method to measure the axial error of a spindle was proposed. A
sinusoidal injection current of frequency 3 MHz was used to modulate the frequency of an
LD, and then the modulated LD was used as the light source of the Michelson interferometer.
The frequency-modulated interferometer was then used to measure the axial error of an
ultra-precision spindle. The axial error was determined from the interference signal of the
interferometer using the synchronous detection method. The system can operate accurately
even though the presence of vibration and environmental disturbance.

2. Methodology

The purpose of this paper is to determine the axial error of an ultra-precision spind
de that includes (1) longitudinal-motion error and (2) runout error of the spindle. The
longitudinal-motion error (1) is the error motion of the spindle collinear with the direction
of the laser beam. Moreover, the runout error (2) is caused by the misalignment of the
rotational spindle axis and the laser beam direction. A homodyne interferometer using the
frequency modulation of an LD is used to detect the axial error.

Figure 1 shows the diagram of the interferometer. The measurement mirror (MM) is
hardly glued to the end face of the spindle. A tunable laser diode (LD) is used as the laser
source, which is frequency-modulated with an MHz-order sinusoidal signal by a function
generator (FG). The angle frequency \( \omega(t) \) of the LD is expressed as

\[
\omega(t) = \omega_0 + \Delta \omega \sin(\omega_m t)
\]

(1)

where \( \omega_0 (=2\pi f_0) \), \( \omega_m (=2\pi f_m) \), and \( \Delta \omega \) are the initial angle frequency of LD, the angle
modulation frequency, and the magnitude of \( \omega_m \), respectively. A polarization beam splitter
(PBS1) divides the laser beam into two parts. One of the two parts (vertically polarized
beam) is directed to a half-wave plate (HWP) and reaches an interferometer (Agilent
10706A). Here, the polarization axis of HWP is oriented at 45\(^\circ\) to the polarization axis of
the incident beam. In the interferometer, another PBS splits the incident beam into two components (reflection and transmission components). The reflection component passes long the reference arm via a quarter-wave plate (QWP), a reference mirror (RM), the QWP again, and the PBS. Meanwhile, the transmission laser beam passes along the measurement arm via another QWP, MM, QWP, and PBS. It should be noted that the incident beams are reflected twice on the RM and MM in both arms and the measurement resolution of the interferometer is increased by double times.

At the PBS, the reflection and transmission beams combine and reach a photodetector (PD). Between the PBS and PD, a polarizer (P) is used. Since the polarization axis of P is oriented at 45° to the polarization axes of the overlapping two beams, they interfere with each other. At PD, the interference signal \( I(L,t) \) is thus generated and can be written as \([22,23]\)

\[
I(L,t) = I_0[1 + V \cos (\omega_m t + \omega_0 \frac{4 L n_{air}}{c})] \tag{2}
\]

where \( \omega_0 = 2\pi f_0 \), \( \omega_m \), \( n_{air} \), \( I_0 \), \( V \), \( L \), and \( c \) are the central angular frequency of LD, the angular modulation frequency, the refractive index of air, the average intensity, the contrast of a beat signal, the unbalance length of the interferometer, and the light velocity within vacuum, respectively. Here,

\[
m = \Delta \frac{\omega}{\omega_m} \sin \left( \frac{\omega_m \tau}{2} \right) \approx \frac{4 \pi \Delta f L n_{air}}{c} \tag{3}
\]

is the modulation index, where \( \tau \) and \( \Delta f \) are the time delay between the two arms of the interferometer and the frequency modulation amplitude, respectively. Using the Bessel function, Equation (2) is expanded as

\[
I(L,t) = I_0 \left\{ 1 + V \left\{ \cos \left( \omega_0 \frac{4 L n_{air}}{c} \right) \left[ I_0(m) + 2 \sum_{k=1}^{\infty} J_{2k}(m) \cos 2k\omega_m t \right] - \sin \left( \omega_0 \frac{4 L n_{air}}{c} \right) 2 \sum_{k=1}^{\infty} J_{2k-1}(m) \sin (2k-1)\omega_m t \right\} \right\} \tag{4}
\]

Here, \( L \) in Equation (4) can be expressed as

\[
L = L_0 + \Delta L \tag{5}
\]

where \( L_0 \) and \( \Delta L \) are the initial unbalanced length between the two arms and the displacement of the measurement mirror (MM) that is ruled as the axial error of the spindle when the spindle performs a high-velocity rotation. Substituting Equation (5) into (4) and using \( 2 \pi f_0 \), we can obtain

\[
I(\Delta L,t) = I_0 \left\{ 1 + V \left\{ \cos \left( \frac{8 \pi n}{\lambda_0} \Delta L \right) \left[ I_0(m) + 2 \sum_{k=1}^{\infty} J_{2k}(m) \cos 2k\omega_m t \right] - \sin \left( \frac{8 \pi n}{\lambda_0} \Delta L \right) 2 \sum_{k=1}^{\infty} J_{2k-1}(m) \sin (2k-1)\omega_m t \right\} \right\} \tag{6}
\]

As a result, Equation (6) shows that the interference signal \( I(\Delta L,t) \) contains many frequency components with a fundamental modulation frequency \( \omega_m \) and its harmonics of \( (2k-1)\omega_m \) and \( 2k\omega_m \). Using two lock-in amplifiers (LIAs), we can extract any pair of consecutive harmonics, \( (2k-1)\omega_m \) and \( 2k\omega_m \), where \( k \) is an integer \( \geq 1 \) \([22]\).

The \( (2k-1)\omega_m \) and \( 2k\omega_m \) harmonics are given by

\[
I_{2\omega_m} = I_0 V J_2(m) \cos \left( \frac{8 \pi n}{\lambda_0} \Delta L \right) \tag{7}
\]

\[
I_{3\omega_m} = -I_0 V J_3(m) \sin \left( \frac{8 \pi n}{\lambda_0} \Delta L \right) \tag{8}
\]
In Equations (7) and (8), the gains of the two LIAs are assumed to be the same. A Lissajous diagram is a representation of $I_3/ω_m/I_2/ω_m$. The phase of the Lissajous diagram is obtained, and $ΔL$ can be calculated as

$$ΔL = \frac{λ_0}{8πn} \left\{ \arctan \left( \frac{I_2(m)/I_3/ω_m}{I_2(m)/I_3/ω_m} \right) \right\}$$  

(9)

In the frequency-modulated interferometer, two successive harmonics are detected using LIAs. When the target moves, the Doppler frequency shortens the gap between these harmonics. The maximum measurement speed is limited when the bandwidth of two successive harmonics is overlapped. The maximum velocity of the target can be expressed as the following

$$V_{max} ≤ \frac{λ_0}{4f_m}$$

(10)

where $V_{max}$ is the maximum velocity.

Figure 1. Measurement of the axial error of spindle using the frequency-modulated interferometer. HWP: half-wave plate; QWP: quarter-wave plate; PBS: polarization beam splitter; RM and MM: reference and measurement mirrors; HSS: high-speed spindle; M: mirror; P: polarizer; PD: photodetector; LIA: lock-in amplifier; ADC: analog-to-digital converter.

In Figure 1, we set up the two incident beams directing to the MM such that they are symmetrical to the axis of the spindle rotation. It leads that the axial error only contains the longitudinal-motion error of the spindle. This interferometer can obtain the longitudinal error vibration of the spindle.

To verify the proposed method, an axial error measurement of an ultra-precision spindle that the maximum speed of the spindle was less than 5000 pps (600 rpm) was performed. Following the ANSI/ASME B89.3.4M, Axes of Rotation: Methods for Specifying and Testing Standard, the motion error is described by its radial (x- and y-directions at a specified location), axial (along the z-axis), and tilt components (rotation about the x- and y-axes) [7]. It is noteworthy that both the radial and axial errors can be determined using the displacement-measuring interferometer. For the radial error measurements, the measurement speed must be much higher than the axial error measurement. From Equation (5), the measurement speed of the frequency modulation interferometer can be improved using a high-frequency modulation frequency. Therefore, a modulation frequency of 3 MHz (according to Equation (10), the measurable speed ~0.48 m/s with $λ = 635$ nm) was applied.
to the laser to measure the axial errors of the spindle. Moreover, a primary experiment using a modulation frequency of 20 MHz (~3.16 m/s) that can be used to measure the radial errors was performed and validated.

3. Results and Discussion

The experimental conditions used in the axial error measurement of an ultra-precision spindle are shown in Table 1. An LD (Thorlabs, HL6312G wavelength $\lambda = 635$ nm) is used as the laser source of the interferometer. The MM mounted on the end face of the spindle was driven by an ultra-precision spindle (HDR50/M, Thorlabs Inc.) at 4200 pps (4200 \times 0.72^\circ/360^\circ \times 60 = 504$ rpm, 8.4 Hz). The modulation frequency of LD $f_m = 3$ MHz generated from the digital FG (Moku: labs) is used for the LD. The interference signal $I(\Delta L, t)$ is recorded by a PD (Thorlabs, DET08CFC/M) and then is transmitted to two LIAs. We employ two Moku: labs, whose sampling rate is up to 500 Ms/s, as two digital LIAs to extract the $2f_m (=6$ MHz) and $3f_m (=9$ MHz) harmonics. The LIAs must be synchronized with each other. In the experiment, the cutoff frequency of the LIAs was set at 50 kHz. In the experiment, the MM was located at $L = \sim0.9$ m. Therefore, $m = 3.77$ from Equation (3) with $\Delta f = 100$ MHz, $n_{air} \approx 1$, and $c \approx 3.10^8$ m/s.

Figures 2 and 3 show experimental results of the axial error measurement. Two LIAs were used to detect second and harmonics and to remove anything unsynchronized with the reference signals. Hence, a Lissajous diagram using the harmonics was generated accurately even though the presence of environmental disturbance, as shown in Figure 2. Figure 3 shows the axial error of the spindle. An axial error of the spindle with a peak-to-peak value of 0.8 $\mu$m was successfully detected. The effect of vibration can be seen clearly at the peaks of the axial error measurement graph caused by the air gap of the ball bearings of the spindle. The length noise floor analyzed using FFT are shown in Figure 3b. The result shows that a primary peak of 8.4 Hz, which is the same as the rotary frequency of the spindle axis, and its harmonics are found. The obtained noise level reaches less than 10 nm/$\sqrt{Hz}$ from 1 Hz to 1000 Hz and downs to 0.01 nm/$\sqrt{Hz}$ and lower at frequencies above 10 kHz instead of those unwanted peaks. Moreover, other redundant peaks found may be caused by this air gap of the ball bearings of the spindle above.

Table 1. Experimental conditions.

| Spindle Speed | 4200 pps (~504 rpm or 8.4 Hz) |
|---------------|-----------------------------|
| Laser Source  | (Thorlabs, HL6312G)          |
| Modulation Frequency Amplitude $\Delta f$ | ~100 MHz |
| Modulation Frequency for LD | 3 MHz |
| Lock-in Amplifier | Moku:labs |
| Cut Off Frequency of Low Pass Filters | 50 kHz |
| Output Sampling Frequency | 100 kS/s |
| Sampling Time | 2 s |
| ADC | (Contect, AD16-16(PCl(EV)) |
| Resolution of ADC | 16 bits |

According to Equation (10), the measurement speed of the interferometer is limited by $f_m$. To obtain measurements of the radial error of the spindle with a speed of up to several m/s, $f_m \sim$ tens of MHz should be achieved. In our previous works, it was difficult to restore an interferometric signal modulated with $f_m \sim$ tens of MHz owing to the hardware limitation caused by the low bandwidth of LIAs [22,23]. In the following experimental step, we attempt to enhance the modulation frequency of LD up to 20 MHz using the new digital LIAs of the Moku: labs with a large bandwidth of 200 MHz for improving high-speed measurements. A digital oscilloscope (Moku: labs, San Diego, CA, USA) is employed to examine the modulated signal for one cycle period of ~30 $\mu$s at a sampling frequency of 500 Ms/s. Figure 4 shows the measurement result. An $f_m$ sine-wave modulation signal with a peak-to-peak amplitude of ~6.5 mV is graphed for 1 $\mu$s (one portion of 30 $\mu$s), as shown in Figure 4a. Figure 4b,c show the RMS amplitude of the signal in the frequency domain a bandwidth of 250 MHz and a frequency resolution of approximately 30.5 kHz.
using the FFT. A peak of $10^{-2} \text{ mV/} \sqrt{\text{Hz}}$ at $f_m = 20 \text{ MHz}$ is attained. Additionally, the 2nd and 3rd harmonics of $f_m = 20 \text{ MHz}$ were found, and the sine wave in Figure 4a can be distorted. Unfortunately, since the spindle speed is limited, we have not acquired the high-speed measurement of both the axial and radial errors using $f_m = 20 \text{ MHz}$. We are planning to execute this problem using high-speed spindle.

Figure 2. Lissajous diagram using second and third harmonics.

Figure 3. Axial error measurement result using the frequency-modulated interferometer. (a) axial error; (b) noise level.

Figure 4. Modulation signal of the interferometer at $f_m = 20 \text{ MHz}$. (a) Sine waveform of the signal versus time, (b) and (c) FFT analysis of graph (a) with linear and logarithmic frequency axes, respectively.
4. Conclusions

A new method to measure the axial error of a spindle using a high-frequency-modulated interferometer was proposed and validated. The frequency modulation of 3 MHz was applied to an LD and the axial error of an ultra-precision spindle at 504 rpm was determined using two consecutive harmonics. There was some deformation in the Lissajous diagram because of environmental disturbance and vibration. The measurement resolution with the order of approximately 10 nm can be achieved. Moreover, the primary experimental result has proved that the modulation frequency up to 20 MHz for the LD was possible. Some harmonics can be seen clearly by the FFT analysis. It was a significant condition to extend the measurement speed of the proposed system. The measuring system is compact, low-cost, and stable. For future work, the proposed interferometer should be compared with a heterodyne interferometer to clarify the measurement accuracy of the system.

Author Contributions: Conceptualization, T.-T.V. (Toan-Thang Vu) and T.-T.V. (Thanh-Tung Vu); methodology, T.-T.V. (Toan-Thang Vu) and T.-D.N.; software, T.-T.N.; validation, T.-T.V. (Thanh-Tung Vu); formal analysis, T.-T.N.; investigation, T.-T.N.; resources, T.-T.V. (Toan-Thang Vu); data curation, T.-D.N.; writing—original draft preparation, T.-T.N.; writing—review and editing, T.-T.V. (Thanh-Tung Vu); supervision, T.-T.V. (Toan-Thang Vu); funding acquisition, T.-T.V. (Toan-Thang Vu). All authors have read and agreed to the published version of the manuscript.

Funding: This research was funded by Hanoi University of Science and Technology, grant number T2020-PC-204.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Data sharing not applicable.

Conflicts of Interest: The authors declare no conflict of interest.

References
1. Murakami, H.; Katsuki, A.; Sajima, T. Simple and simultaneous measurement of five-degrees-of-freedom error motions of high-speed microspindle: Error analysis. Precis. Eng. 2014, 38, 249–256. [CrossRef]
2. Jin, A.; Chen, J.; Yang, W.; Lin, J.; Wang, L.; Jin, P. Measurement of spindle radial error based on target trajectory tracking. Measurement 2019, 146, 179–185. [CrossRef]
3. Lei, W.; Hsu, Y. Accuracy test of five-axis CNC machine tool with 3D probe–ball. Part I: Design and modeling. Int. J. Mach. Tools Manuf. 2002, 42, 1153–1162. [CrossRef]
4. Cao, H.; Li, B.; Li, Y.; Kang, T.; Chen, X. Model-based error motion prediction and fit clearance optimization for machine tool spindles. Mech. Syst. Signal Process. 2019, 133, 106252. [CrossRef]
5. Conte, J.; Santolaria, J.; Majarena, A.; Acero, R.; Conte, J.; Santolaria, J.; Majarena, A.; Acero, R. Modelling, kinematic parameter identification and sensitivity analysis of a Laser Tracker having the beam source in the rotating head. Measurement 2016, 89, 261–272. [CrossRef]
6. ANSI/ASME B89.3.4M. Axes of Rotation–Methods for Specifying and Testing; The American Society of Mechanical Engineers: New York, NY, USA, 1985.
7. ISO 230-7:2006. Test Code for Machine Tools–Part 7: Geometry Accuracy of Axes of Rotation; International Standardisation Organisation: Geneva, Switzerland, 2006.
8. Cui, H.; Lei, D.; Zhang, X.; Lan, H.; Jiang, Z.; Kong, L. Measurement and analysis of the radial motion error of aerostatic ultra-precision spindle. Measurement 2019, 137, 624–635. [CrossRef]
9. Chrzanowski, J.; Salaciński, T.; Skiba, P. Spindle Error Movements and Their Measurement. Appl. Sci. 2021, 11, 4571. [CrossRef]
10. Peng, K.; Yu, Z.; Liu, X.; Chen, Z.; Pu, H. Features of capacitive displacement sensing that provide high-accuracy measurements with reduced manufacturing precision. IEEE Trans. Ind. Electron. 2017, 64, 7377–7386. [CrossRef]
11. Ye, Y.; Zhang, C.; He, C.; Wang, X.; Huang, J.; Deng, J. A Review on Applications of Capacitive Displacement Sensing for Capacitive Proximity Sensor. IEEE Access 2020, 8, 45325–45342. [CrossRef]
12. Castro, H. A method for evaluating spindle rotation errors of machine tools using a laser interferometer. Measurement 2008, 41, 526–537. [CrossRef]
13. Gregorič, P.; Požar, T.; Možina, J. Quadrature phase-shift error analysis using a homodyne laser interferometer. Opt. Express 2009, 17, 16322–16331. [CrossRef]
14. Petrů, F.; Číp, O. Problems regarding linearity of data of a laser interferometer with a single-frequency laser. *Precis. Eng.* 1999, 23, 39–50. [CrossRef]
15. Keem, T.; Gonda, S.; Misumi, I.; Huang, Q.; Kurosawa, T. Simple, real-time method for removing the cyclic error of a homodyne interferometer with a quadrature detector system. *Appl. Opt.* 2005, 44, 3492–3498. [CrossRef]
16. Ahn, J.; Kim, J.-A.; Kang, C.-S.; Kim, J.W.; Kim, S. A passive method to compensate nonlinearity in a homodyne interferometer. *Opt. Express* 2009, 17, 23299–23308. [CrossRef] [PubMed]
17. Wu, C.-C.; Hsu, C.-C.; Lee, J.-Y.; Chen, H.-Y.; Dai, C.-L. Optical heterodyne laser encoder with sub-nanometer resolution. *Meas. Sci. Technol.* 2008, 19, 045305. [CrossRef]
18. Demarest, F.C. High-resolution, high-speed, low data age uncertainty, heterodyne displacement measuring interferometer electronics. *Meas. Sci. Technol.* 1998, 9, 1024–1030. [CrossRef]
19. Sasaki, O.; Okazaki, H. Sinusoidal phase modulating interferometry for surface profile measurement. *Appl. Opt.* 1986, 25, 3137–3140. [CrossRef] [PubMed]
20. Suzuki, T.; Sasaki, O.; Higuchi, K.; Maruyama, T. Real time displacement measurement in sinusoidal phase modulating interferometry. *Appl. Opt.* 1989, 28, 5270–5274. [CrossRef] [PubMed]
21. Sasaki, O.; Yoshida, T.; Suzuki, T. Double sinusoidal phase-modulating laser diode interferometer for distance measurement. *Appl. Opt.* 1991, 30, 3617–3621. [CrossRef]
22. Vu, T.-T.; Higuchi, M.; Aketagawa, M. Accurate displacement-measuring interferometer with wide range using an I2 frequency-stabilized laser diode based on sinusoidal frequency modulation. *Meas. Sci. Technol.* 2016, 27, 105201. [CrossRef]
23. Duong, Q.A.; Vu, T.T.; Higuchi, M.; Wei, D.; Aketagawa, M. Iodine-frequency-stabilized laser diode and displacement-measuring interferometer based on sinusoidal phase modulation. *Meas. Sci. Technol.* 2018, 29, 065204. [CrossRef]