A New Job Shop Scheduling Method for Remanufacturing Systems Using Extended Artificial Bee Colony Algorithm

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1. INTRODUCTION

Remanufacturing is a process that end-of-life (EOL) products are disassembled into components, reprocessed through advanced technology, and reassembled to fabricate new products [4]. By means of innovative surface engineering technology and dedicated devices, the remanufactured products will have the same quality as the new ones, consequently realizing the objectives of green, circular, and low-carbon consumptions. Compared with new products, remanufactured products can be obtained for only 50% cost, 40% energy, 30% raw materials, and pollution discharge not exceeding 20% [23]. Thus, the remanufacturing industry is highly appreciated worldwide because of its considerable contribution to minimizing resource consumption and carbon emissions [23].

Remanufacturing can be considered as an industrial process covering a wide range of industries, such as those in the production of ballpoints, personal computers, and automotive clutch segments [30], [17], [3]. The remanufacturing system mainly includes three sub-systems: disassembly, reprocessing, and reassembly shops. Among them, the reprocessing shops serve as a link between disassembly and reassembly shops, through which the defective components of an
EOL product are reprocessed into high-quality components. The quality of the new and reprocessed components should essentially be the same in appearance, reliability, and performance. The components of an EOL product must be matched together when they are reprocessed and reassembled into the corresponding remanufactured product, hence the components of an EOL product constitutes a job family [36]. The job shop scheduling with job families (JSS-JF) has been widely recognized as a critical research issue. It aims to minimize the completion time of job families by allocating jobs to machines and sequencing the operations on corresponding machines for components reprocessing.

Although there are available literatures on the JSS-JF, most literatures only consider the time factor, such as total completion time of job families or total tardiness of job families on basis of due-dates [38], [16], [36], [37]. On the other hand, components obtained from disassembly shops in the remanufacturing environment are of different damaged conditions and the appropriate execution mode need to be selected for each component. Gharbi et al. [9] and Berthaut et al. [1] considered that remanufacturing operations can be implemented on different components with either replacement or repair mode. Thus, the execution mode selection can be integrated with remanufacturing scheduling to achieve a more optimal solution. However, few studies have focused on JSS-JF that considers different damaged conditions of components and selects the appropriate execution modes for reprocessing components.

In this study, a new JSS-JF model is proposed. In contrast to existing studies on JSS-JF, this study considers not only the total completion time of job families but also the two execution modes (i.e., replacement mode and repair mode) for reprocessing components. Gharbi et al. [9] mentioned that the remanufacturing process can be accelerated by replacing parts rather than repairing them. However, repairing a component usually costs less than replacement but takes more time. Thus, the appropriate execution mode should be selected for each component, depending on the comprehensive evaluation of the total completion time and total cost of job families. The scheduling problem in this study is decomposed into three sub-problems: (1) execution mode selection; (2) replacement job assignment and sequencing; and (3) repair machine assignment and operation sequencing. Once the execution modes are determined, the jobs with replacement mode are handled through replacement job assignment and sequencing, and the jobs with repair mode are handled through repair machine assignment and operation sequencing. The objective of the proposed JSS-JF model is to minimize the total completion time and total cost of job families.

The job shop scheduling problem is an NP-hard problem and has been widely solved using population-based algorithms, including genetic algorithm (GA) [27], [41] and particle swarm optimization (PSO) [40], [32]. An artificial bee colony (ABC) algorithm based on the intelligent foraging behavior of a honey bee swarm was first proposed by Karaboga [13] for solving numerical optimization problems and had been used to solve job shop scheduling problems successfully in recent years. Furthermore, Karaboga and Akay [14] compared the ABC algorithm with other population-based optimization algorithms and summarized its advantages, such as fewer control parameters, shorter search time, and better global optimization ability. In view of the successful application of the ABC algorithm in solving job shop scheduling problems, it is extended in the present study to solve the proposed JSS-JF model for remanufacturing systems.

Compared with the classical job shop scheduling problem, the presented JSS-JF problem in this study is a more complex multi-variable and multi-dimensional optimization problem. However, the one-dimensional encoding scheme of the basic ABC algorithm cannot be directly used to represent the complex structure of a JSS-JF solution. Therefore, a new three-dimensional encoding scheme is proposed to describe the JSS-JF solution. In addition, to improve the search ability and accelerate the convergence of the ABC algorithm, it is extended with crossover and mutation operators, local search, and elite replacement strategy. Finally, simulation experiments are performed for comparison with six baseline population-based algorithms. The experimental results confirm the practicability and effectiveness of the proposed extended ABC, i.e., EABC algorithm in solving the proposed JSS-JF model for remanufacturing systems.

The remainder of this paper is organized as follows. Section 2 reviews the related work on the job shop scheduling problem and ABC algorithm. Section 3 presents the proposed JSS-JF model in more detail with mathematical representation. Section 4 introduces the basic concept of the ABC algorithm and proposes the EABC algorithm to solve the proposed JSS-JF model. Section 5 presents the simulation experiments and discusses the experimental results to illustrate the superiority of the proposed EABC algorithm. Section 6 summarizes the main contributions of this study and directions for future work.

II. RELATED WORK

In this section, previous literatures that are closely related to this study including the job shop scheduling problem and ABC algorithm are reviewed.

A. JOB SHOP SCHEDULING PROBLEM

Various classical job shop scheduling problems and their extensions, such as job shop scheduling with alternative machines, flexible job shop scheduling, and stochastic job shop scheduling, have been studied. With the emergence of the remanufacturing industry, scheduling problems in remanufacturing systems have also drawn the interest of scholars. In the past decade, the JSS-JF in the remanufacturing system has been investigated as a variant of job shop scheduling.

In manufacturing systems, classical job shop scheduling problems, including machine assignment and operation sequencing, have been extensively studied [34], [42], [41]. In contrast to manufacturing, remanufacturing is more
complex because of its high uncertainty [44]. For example, the conditions of products obtained in remanufacturing facilities are highly variable [25]. Moreover, component matching requirements has to be considered in the remanufacturing system, i.e., the components for reassembling the product to be remanufactured must be matched [36].

The JSS-JF for remanufacturing systems has generally been solved from a local or systematic perspective. For example, Yu et al. [38] elaborated the job shop scheduling problem in which jobs are grouped into job families to minimize the total family flow time. Kim et al. [16] explored the job shop scheduling problem with job families to minimize the total family flow time with iterative greedy algorithms. Yu and Lee [26] focused on a scheduling problem with job families for remanufacturing systems with three sub-systems and separately solved the disassembly, reprocessing, and reassembly scheduling problems. Yu and Lee [37] considered a due-date-based objective to minimize the total family tardiness in the job shop scheduling problem with job families. Shi et al. [28] proposed an energy-aware remanufacturing scheduling method for the entire remanufacturing system with non-dedicated reprocessing lines. Fu et al. [5] focused on a stochastic multi-objective remanufacturing scheduling problem that integrates disassembly, reprocessing, and reassembly sub-systems.

In contrast, to leverage the advantages of different execution modes in various contexts, multiple execution modes have been studied in the domains of project scheduling [11], [24] and remanufacturing [22], [26], [2]. Linton and Jayaraman [22] indicated that the inherent full values of products cannot be fully exploited without recognizing their differences between the products, and proposed different modes of product life extension. Pellerin and Gharbi [26] and Berthaut et al. [2] considered two forms of execution modes: component repair and component replacement with new parts depending on the product to be remanufactured. In the domain of remanufacturing scheduling, Lin et al. [21] considered four execution modes (i.e., replacement, repair, refurbish, and recondition) and solved the multi-plant remanufacturing scheduling problem by exploring the relationship between execution mode and rework possibility.

Existing studies have explored the advantages of the execution mode in the remanufacturing industry; however, the trade-off among the execution modes and the impact of different execution mode selections on scheduling methods have not been considered. Accordingly, the current study proposes a new job shop scheduling method that integrates the execution mode selection, replacement job assignment and sequencing, and repair machine assignment and operation sequencing.

### B. ARTIFICIAL BEE COLONY ALGORITHM

The ABC algorithm was originally proposed by Karaboga [13] for solving continuous optimization problems. It is a population-based algorithm that simulates the intelligent foraging behavior of a honey bee swarm to optimize the objective function. Karaboga and Basturk [15] stated that the ABC algorithm outperformed many other intelligent algorithms and can be employed to solve complex optimization problems efficiently. Consequently, the ABC algorithm has been widely employed for practical applications, and its variations have also been developed. Singh [29] proposed an ABC algorithm for solving the leaf-constrained minimum spanning tree problem; their experiments demonstrated that the algorithm could yield improved solutions over a short period. Li et al. [18] presented a discrete ABC algorithm to solve the steelmaking scheduling problems with multiple constrained resources. Zhu et al. [45] proposed an ABC algorithm based on multiple improvement strategies to address the cloud manufacturing service composition. Zou et al. [46] utilized an effective discrete ABC algorithm to deal with the automatic guided vehicle scheduling problem in a linear manufacturing workshop. Gao et al. [6] surveyed the literatures that utilized ABC algorithm to solve the complicated discrete optimization problems in remanufacturing scheduling. In our previous work [43], an extended ABC algorithm was proposed to solve the networked correlation-aware manufacturing service composition. It was also demonstrated that the proposed algorithm outperformed other population-based algorithms.

Existing literature have also shown that ABC algorithms have been widely employed to solve job shop scheduling problems. For example, Yin et al. [35] proposed a discrete ABC algorithm to solve the job shop scheduling problem. Zhang and Wu [42] utilized the ABC algorithm to solve the stochastic job shop scheduling problem with the objective of minimizing the maximum lateness. Gao et al. [7] proposed a two-stage ABC algorithm for flexible job scheduling and re-scheduling with new job insertion. Gao et al. [8] proposed a two-stage ABC algorithm to solve the flexible job shop scheduling problem with fuzzy processing time.

Because of the good performance of ABC algorithm in solving optimization problems, it is extended for solving the proposed JSS-JF model in this study. The proposed JSS-JF model handles a multi-variable and multi-dimensional optimization problem. Accordingly, a new three-dimensional encoding scheme is proposed to describe the JSS-JF solution effectively. Moreover, three improvements, specifically the crossover and mutation operators, local search, and elite replacement strategy, are integrated in the EABC algorithm to solve the proposed model.

### III. PROBLEM DEFINITION AND MODELING

In remanufacturing, the job shop scheduling problem is defined through the proposed JSS-JF model. The illustrative example in Figure 1 shows that products 1 and 2 are disassembled on either one of the parallel disassembly workstations \((DW_1, DW_2, DW_3, \ldots)\) in the disassembly shop. Let \(C_p\) be the set of components of product \(p\); for example, \(C_1 = \{C_{11}, C_{12}, C_{13}\}\) and \(C_2 = \{C_{21}, C_{22}, C_{23}\}\) for products 1 and 2, respectively. The components of \(C_1\) and
C2 are individually reprocessed by selecting an appropriate execution mode (i.e., replacement mode or repair mode). Finally, the components are reassembled into corresponding remanufactured products 1 and 2 in either one of the parallel reassembly workstations (RW1, RW2, RW3, ...) in the reassembly shop.

As shown in the lower part of Figure 1, each component corresponds to a job in the reprocessing shop. The jobs are grouped into job families but are processed individually. Let JFm be the nth job family containing a set of jobs, e.g., JF1 = {J1, J2, J3} and JF2 = {J4, J5, J6} for the 1st and 2nd job families, respectively. In the current illustrative example, jobs J1, J2, J3, and J6 are executed with replacement mode, and human operators replace the defective components, i.e., C11, C12, C13, and C23, with new components, i.e., C′ 11, C′ 12, C′ 13, and C′ 23, respectively. By contrast, jobs J4 and J5, which reprocess components C21 and C22, are executed with repair mode and processed by the repair machines for sequential operations (O41, O42, ...) and (O51, O52, ...), respectively.

In the proposed JSS-JF model, the selection of different execution modes for jobs necessitates different scheduling methods, depending on the comprehensive evaluation of the total completion time and total cost of job families. If jobs are executed with replacement mode, the defective components are replaced with new components by human operators. If jobs are executed with repair mode, a set of jobs is processed by repair machines for sequential operations. Each repair job may involve multiple operations, and each of these is processed on one of the candidate repair machines.

For a more focused problem modeling, the following assumptions were made in this study: (1) the job description, such as the processing times of replacement jobs and repair operations, are determined and given in advance; (2) there is no priority relationship among job families or jobs; (3) replacement jobs and repair operations cannot be split and preempted; (4) setup and transportation times are negligible; (5) the human operators for processing replacement jobs are available; and (6) repair machine breakdowns are neglected.

**A. NOTATIONS**

To describe the proposed model explicitly, the following notations are introduced.

1) **INDICES AND SETS**

- **e** execution mode index; e = 1 and e = 2 indicate replacement and repair modes, respectively.
- **n** human operator index, n = 1, 2, ..., N.
- **Ji** the i th job, i = 1, 2, ..., I.
- **Oi** the l th operation of job Ji with repair mode, l = 1, 2, ..., Li.
- **JFm** the m th job family containing a set of jobs, m = 1, 2, ..., M.
- **MAk** the kth repair machine, k = 1, 2, ..., K.
- **MSil** set of candidate repair machines for performing Oili.

2) **PARAMETERS**

- **JCTi,e** completion time of Ji with the eth execution mode.
- **HSTi,n** starting time of Ji with replacement mode by the nth human operator.
- **HPTi,n** processing time of Ji with replacement mode by the nth human operator.
- **HCTi,n** completion time of Ji with replacement mode by the nth human operator.
- **HRCi,n** replacement cost of Ji with replacement mode by the nth human operator.
- **OSTi,l** starting time of Oili with repair mode on MAk.
- **OPTi,k** processing time of Oili with repair mode on MAk.
- **OCTi,k** completion time of Oili with repair mode on MAk.
- **ORCi,l,k** repair cost of Oili with repair mode on MAk.
- **TT** total completion time of all job families.
- **TC** total cost of all job families.
- **M** a large number.

3) **DECISION VARIABLES**

- **αi,e** binary variable; if Ji is processed with the eth execution mode, then, αi,e = 1; otherwise, αi,e = 0.
- **χi,n** binary variable; if Ji with replacement mode is processed by the nth human operator, then, χi,n = 1; otherwise, χi,n = 0.
- **βi,l,k** binary variable; if Oili with repair mode is processed on MAk, then, βi,l,k = 1; otherwise, βi,l,k = 0.
- **ξi,i′,l,n′** binary variable; if Ji with replacement mode is immediately followed by Ji′ with replacement mode by the nth human operator, then, ξi,i′,l,n′ = 1; otherwise, ξi,i′,l,n′ = 0.
- **yi,l,i′,e** binary variable; if Oili with repair mode is immediately followed by Oil,i′ with repair mode on MAk, then, yi,l,i′,e = 1; otherwise, yi,l,i′,e = 0.

**B. OBJECTIVES**

This study aims to minimize TT and TC to obtain the optimal schedule.

TT is an important indicator of production efficiency. It can be calculated as the maximal completion time using Equation (1) which is obtained by comparing the completion time of each job family.

\[
TT = \max_{1 \leq m \leq M} \left\{ \max_{Ji \in JFm} \left\{ \sum_{e=1}^{2} \alpha_{i,e} \cdot JCT_{i,e} \right\} \right\} \tag{1}
\]

The total job cost, TC, which includes the replacement and repair costs for replacement jobs and repair operations, can be calculated using Equation (2). If the job is executed with
FIGURE 1. An example: system configuration of the proposed JSS-JF model for remanufacturing systems.

replacement mode, the human operator replaces the defective component with a new part, incurring replacement cost. If the job is executed with the repair mode, the operations of the job are processed on repair machines, incurring repair cost.

\[ TC = \sum_{i=1}^{N} \sum_{n=1}^{I} \alpha_1^i \chi_n^i HRC_n^i + \sum_{i=1}^{L_i} \sum_{k \in MS} \alpha_2^i \beta_i^k ORC_k^i \] (2)

The comprehensive evaluation measure of schedule \( f \) is calculated by setting appropriate weights to \( TT \) and \( TC \). Accordingly, the objective of the proposed JSS-JF model is formulated using Equation (3).

\[ \max f = \omega_1 \frac{TT_{\text{max}} - TT_{\text{min}}}{TT_{\text{max}} - TT_{\text{min}}} + \omega_2 \frac{TC_{\text{max}} - TC_{\text{min}}}{TC_{\text{max}} - TC_{\text{min}}} \] (3)

where \( TT_{\text{max}} \) and \( TC_{\text{max}} \) denote the maximal \( TT \) and \( TC \), respectively; \( TT_{\text{min}} \) and \( TC_{\text{min}} \) denote the minimal \( TT \) and \( TC \), respectively; and \( \omega_1 \) and \( \omega_2 \) that add up to 1 represent the weights of \( TT \) and \( TC \), respectively.

C. TOTAL COMPLETION TIME OF JOB FAMILIES

In the proposed JSS-JF model, the total completion time of job families is calculated according to the completion time of the jobs; \( JCT_e^i \) is calculated using Equation (4). If the job is executed with replacement mode, then, its completion time is equal to that of the last operation of the job.

\[ JCT_e^i = \begin{cases} \sum_{n=1}^{N} \chi_n^i HCT_n^i & e = 1 \\ \sum_{k \in MS} \beta_i^k \cdot OCT_k^i & e = 2 \end{cases} \] (4)

The starting and completion times of processed jobs with replacement mode (i.e., \( HST_n^i \) and \( HCT_n^i \)) are calculated using Equations (5) and (6), respectively.

\[ HST_n^i = EAH_n \] (5)

\[ HCT_n^i = HST_n^i + HPT_n^i \] (6)

where \( EAH_n \) represents the earliest available time of the \( n \)th human operator.

The starting and completion times of processed operations with repair mode (i.e., \( OST_{il}^k \) and \( OCT_{il}^k \)) are obtained by Equations (7) and (8), respectively.

\[ OST_{il}^k = \max \left \{ EAM_k, OCT_{il}^{k'} \right \} \] (7)

\[ OCT_{il}^k = OST_{il}^k + OPT_{il}^k \] (8)

where \( EAM_k \) represents the earliest available time of \( MA_k \), and \( k' \) is the index of repair machine that processes the previous operation of \( O_{il} \) (i.e., \( O_{il(l-1)} \)).
D. CONSTRAINTS OF THE PROPOSED MODEL

The given objective of the JSS-JF model is subject to the constraints expressed by Equations (9) – (17).

\[
\sum_{i=1}^{n} \alpha_{il} = 1, \quad \forall i
\]

\[
HCT_{il} \leq HST_{il} + (1 - x_{il}^{n}) \cdot M, \quad (9)
\]

\[
\alpha_{il}^{2} = 1, \quad \alpha_{il}^{1} = 1, \quad i \neq i', \quad \forall n
\]

\[
\sum_{i=1}^{n} \alpha_{il}^{2}x_{il}^{n} \leq 1, \quad \alpha_{il}^{1} = 1, \quad \forall n
\]

\[
\sum_{i=1,i \neq i'}^{n} \alpha_{il}^{2}x_{il}^{n} \leq 1, \quad \alpha_{il}^{1} = 1, \quad \forall n
\]

\[
\sum_{i=1}^{n} \alpha_{il}^{2} = 1, \quad \alpha_{il}^{1} = 1, \quad \forall i
\]

\[
OCT_{il}^{k} \leq OST_{il}^{k} + \left(1 - y_{il}^{k}\right) \cdot M, \quad (13)
\]

\[
\alpha_{il}^{2} = 1, \quad \alpha_{il}^{1} = 1, \quad l \in [1, L_{l}], \quad l' \in [1, L_{l'}], \quad i \neq i', \quad l \neq l', \quad \forall k
\]

\[
\sum_{i=1}^{n} \alpha_{il}^{2}y_{il}^{k} \leq 1, \quad \alpha_{il}^{1} = 1, \quad l \in [1, L_{l}], \quad \forall k
\]

\[
\sum_{i=1,i \neq i'}^{n} \alpha_{il}^{2}y_{il}^{k} \leq 1, \quad \alpha_{il}^{1} = 1, \quad l \in [1, L_{l'}], \quad \forall k
\]

\[
\sum_{il \in MS_{il}} \beta_{il}^{k} = 1, \quad \alpha_{il}^{2} = 1, \quad l \in [1, L_{l}]
\]

Constraint (9) guarantees that each job is executed with one execution mode. Constraints (10) – (13) are related to the replacement jobs. Constraint (10) specifies that no two jobs can be simultaneously processed by one human operator. Constraint (11) ensures that at most one another job is selected to be processed following \( J_{i} \) by each human operator. Constraint (12) ensures that at most one another job is selected to be processed preceding \( J_{l} \) by each human operator. Constraint (13) guarantees that each repair operation is processed by one human operator.

Constraints (14) – (17) are related to the repair operations. Constraint (14) ensures that no two repair operations can be simultaneously processed on one repair machine. Constraint (15) ensures that at most one another repair operation is selected to be processed following \( O_{il} \) on each repair machine. Constraint (16) ensures that at most one another repair operation is selected to be processed preceding \( O_{il'} \) on each repair machine. Constraint (17) guarantees that each repair operation is processed on one of the candidate repair machines.

IV. EXTENDED ARTIFICIAL BEE COLONY ALGORITHM FOR SOLVING PROPOSED MODEL

In this section, the basic ABC algorithm is briefly introduced. Then, the EABC algorithm is presented to solve the proposed JSS-JF model. Two improvements are also introduced: (1) using a new three-dimensional encoding scheme to represent the JSS-JF solution and (2) integrating the crossover and mutation operators, local search, and elite replacement strategy to enhance the exploration and convergence abilities of the ABC algorithm.

A. INTRODUCTION OF THE BASIC ARTIFICIAL BEE COLONY ALGORITHM

The main steps of the basic ABC algorithm [13], which is inspired by the intelligent foraging behavior of a honey bee swarm, are summarized as follows. The numbers of employed bees and onlooker bees are both equal to the number of the solutions.

1) Initialization phase: A solution with multiple decision variables is analogized as a food source. The initial solutions are generated in this phase.

2) Employed bee phase: Each employed bee explores a new solution from an existing solution, and the greedy selection is used to retain the better solution. When the employed bees complete new solutions, they share important solution information with other bees.

3) Onlooker bee phase: Each onlooker bee selects an existing solution depending on the solution’s probability and explores a better solution.

4) Scout bee phase: If a solution fails to improve after limit trials, the solution is abandoned. The employed bee becomes a scouter and randomly generates a new solution through initialization to replace the abandoned solution.

Phases (2) – (4) are repeated until the termination condition is satisfied, and the near-optimal solution is returned.

B. EXTENDED ARTIFICIAL BEE COLONY ALGORITHM

The EABC algorithm is proposed in this study to effectively solve the JSS-JF model. First, a new three-dimensional encoding scheme is proposed to describe the complex structure of the JSS-JF solution. This is because the traditional one-dimensional encoding scheme of the basic ABC algorithm cannot be used to represent the JSS-JF solution. Then, the crossover and mutation operators, local search, and elite replacement strategy are integrated into the EABC algorithm to enhance its search ability and accelerate convergence. The framework of the EABC algorithm is shown in Figure 2.

1) SOLUTION REPRESENTATION

The representation of a reasonable JSS-JF solution is crucial to enable the EABC algorithm to adapt to the proposed JSS-JF model. To describe the complex structure of the JSS-JF solution accurately, a new three-dimensional encoding scheme for the EABC algorithm is proposed. It is composed of three rows, representing jobs, execution modes, and human operators/repair machines. The first row represents the sorted permutation of the reprocessed jobs. The second row denotes the execution modes of the corresponding jobs. The third row indicates the human operators or repair machines depending on the corresponding execution modes for processing the jobs. If the job is processed with the
replacement mode, the value in the third row denotes the human operator. If the job is processed with the repair mode, the value in the third row denotes the repair machine.

A simple example of the solution (involving five jobs, three human operators, and three repair machines) is shown in Figure 3. It can be seen from Figure 3 that jobs $J_1$, $J_3$, and $J_4$ are executed with replacement mode, while jobs $J_2$ and $J_5$ are executed with repair mode. Each repair job may consist of multiple operations, and the occurrence times of the repair job indicate its operation index. The first element “5” in the first row indicates the first operation ($O_{51}$) of repair job $J_5$, and the second occurrence of “5” indicates the second operation ($O_{52}$) of repair job $J_5$. The first column indicates that the first operation ($O_{51}$) of repair job $J_5$ is processed on repair machine $MA_3$. The fourth column indicates that replacement job $J_4$ is processed by the 3rd human operator.

The solution in Figure 3 can be decoded from left to right. First, each job and the corresponding execution mode must be identified. Then, the human operator or repair machine for the job is determined according to the corresponding execution mode. Finally, the sequence of reprocessed jobs depends on the left-to-right positions of the encoding scheme. Based on the decoding scheme, a schedule can be determined.

2) EMPLOYED BEE PHASE

In the employed bee phase, each employed bee seeks a new solution from an existing solution. In the EABC algorithm, the crossover and mutation operators are utilized to enhance the diversity of solutions. Based on the three-dimensional encoding scheme, crossover and mutation operators are designed to evolve the population. The details of the crossover and mutation operators are as follows.

1) Crossover operator

The precedence operation crossover [39] is employed to seek a new solution. It is implemented through the illustrative example shown in Figure 4, according to the following steps.

Step 1: Randomly select two parent solutions $P_1$ and $P_2$. Randomly divide the jobs into two sets of jobs $JS_1$ and $JS_2$.

Step 2: Copy the columns of $P_1$ with the jobs in $JS_1$ to the offspring solution $O_1$ in the same positions, and copy the columns of $P_2$ with the jobs in $JS_2$ to the offspring solution $O_1$ in the same order.

Step 3: Copy the columns of $P_2$ with the jobs in $JS_1$ to the offspring solution $O_2$ in the same positions, and copy the columns of $P_1$ with the jobs in $JS_2$ to the offspring solution $O_2$ in the same order.

2) Mutation operator

The mutation operator selects several positions in the third row and replaces the existing human operators or repair machines with candidate ones.

The crossover and mutation operators are executed under certain probabilities including crossover rate and mutation rate respectively. Then, new solutions are generated, and the greedy selection is used to retain the solution with a higher fitness value, i.e., the objective function that is calculated by Equation (3).

When all employed bees complete the exploration of new solutions, they return to the hive and share important solution information with the onlooker and scout bees.

3) ONLOOKER BEE PHASE

In the onlooker bee phase, each onlooker bee explores the solutions found by the employed bees. The local search is used to enhance the search ability. Based on the three-dimensional encoding scheme, four local search operators are utilized (one-swap, one-insert, two-swap, and two-insert operators), as illustrated in Figure 5.

1) The one-swap operator is shown in Figure 5 (a), which randomly selects two columns in different positions and swaps them.
(2) The one-insert operator is shown in Figure 5 (b), which randomly selects two columns in different positions, and inserts the latter column in front of the former column.

(3) The main procedure of the two-swap operator is the implementation of the one-swap process twice.

(4) The main procedure of the two-insert operator is the execution of the one-insert process twice.

Each onlooker bee randomly selects an existing solution under a certain probability and explores the neighborhood of this solution using one local search operator with a random selection. Then, new solutions are generated, and the greedy selection retains the solution with higher fitness value.

4) SCOUT BEE PHASE

The scout bee phase is used to escape from the local optima of the ABC algorithm. If a solution fails to improve after limit trials, the solution is abandoned. The corresponding employed bee becomes a scouter and randomly explores a new solution through initialization to replace the abandoned solution. However, it is hard to generate a new solution better than the previous solution based on single exploration in the ABC algorithm. Thus, each scout bee makes 10 explorations to increase the probability of obtaining the best solution with the highest fitness value to replace the abandoned solution.

5) ELITE REPLACEMENT STRATEGY

The elite replacement strategy [12], [13] is implemented to preserve the elite solution with the highest fitness value and replace the worst solution in the next generation. This strategy can prevent the elite solution from being lost and accelerate the convergence of the EABC algorithm.

V. SIMULATION EXPERIMENTS

This section presents the three sets of simulation experiments that are conducted to demonstrate the practicality and effectiveness of the presented EABC algorithm in solving the proposed JSS-JF model by comparing with the other six population-based algorithms, such as basic GA, basic PSO algorithm, basic ABC algorithm, hybrid genetic algorithm (HGA) [33], hybrid particle swarm optimization (HPSO) [20], and hybrid artificial bee colony algorithm (HABC) [10]. Each simulation experiment was executed 10 times to improve the robustness of the results, and the average results were used for evaluation. All experimental data of this study have been uploaded in the Figshare (https://doi.org/10.6084/m9.figshare.13530941). The simulation experiments were implemented using Python programming language on a personal computer with Windows 10 64-bits, AMD Ryzen 7 3700X 8-Core processor at 3.60 GHz and 40 GB RAM.

A. EXPERIMENTAL SETUP

In this study, instances with three scales were used to simulate the real environment of remanufacturing systems, specifically small-scale, medium-scale, and large-scale instances. The configurations for each instance are summarized in Table 1.

The processing time and replacement cost of each replacement job, and the processing time and repair cost of each repair operation were randomly generated within certain ranges as shown in Table 2.

B. PARAMETER DESIGN

The parameters of each algorithm are summarized in Table 3. The first set of simulation experiments was applied on a medium-scale instance M03 to determine the maximum number of the function evaluations for the seven population-based algorithms being compared. For each algorithm, the initial population size, weights of total completion time, and total cost were set as 45, 0.7, and 0.3, respectively. The evolutionary curves of the average fitness values obtained from the seven algorithms are presented in Figure 6. It can be observed that the EABC algorithm and GA are found to converge in 3020 function evaluations, and exhibit a better convergence ability than the other five baseline algorithms. The figure shows that the fitness value obtained from the EABC algorithm is better than those obtained from the six baseline algorithms when all evolutionary curves tend to be stable. It means that the EABC algorithm has a better search ability.
than other algorithms. Furthermore, the HGA algorithm and HPSO algorithm converge slowly, and the PSO algorithm and ABC algorithm fall into local optima. The average fitness value obtained from the HABC algorithm is increased slowly, and tends to be stable in 15000 function evaluations. Based on the performances of the seven algorithms, the maximum number of the function evaluations is selected as 15000 in the subsequent experiments to ensure fair comparisons.

The second set of simulation experiments was applied on the medium-scale instance M03 to select the reasonable initial population size of the seven population-based algorithms; the weights of the total completion time and total cost were set as 0.7 and 0.3, respectively. The experimental results of the average fitness values obtained from the seven algorithms when the initial population size increases from 20 to 60 with an increment of five are shown in Figure 7. The average fitness values obtained from the EABC algorithm obviously exceed those from other algorithms, regardless of the initial population size. The average fitness values obtained from the EABC algorithm and HPSO algorithm have a slight upward trend when the initial population size increases from 20 to 45 and tend to be stable when the initial population size exceeds 45. When the initial population size increases from 20 to 60, the average fitness values obtained from GA have an upward trend. The average fitness values obtained from HGA algorithm tend to be fluctuant when the initial population size increases from 20 to 45 and tend to be stable when the initial population size exceeds 45.

The performances of the seven algorithms are comprehensively evaluated in Table 3. The average fitness values obtained from the HABC algorithm are increased slowly, and the tendency is stable in 15000 function evaluations. Based on the performances of the seven algorithms, the maximum number of the function evaluations is selected as 15000 in the subsequent experiments to ensure fair comparisons.

The second set of simulation experiments was applied on the medium-scale instance M03 to select the reasonable initial population size of the seven population-based algorithms; the weights of the total completion time and total cost were set as 0.7 and 0.3, respectively. The experimental results of the average fitness values obtained from the seven algorithms when the initial population size increases from 20 to 60 with an increment of five are shown in Figure 7. The average fitness values obtained from the EABC algorithm obviously exceed those from other algorithms, regardless of the initial population size. The average fitness values obtained from the EABC algorithm and HPSO algorithm have a slight upward trend when the initial population size increases from 20 to 45 and tend to be stable when the initial population size exceeds 45. When the initial population size increases from 20 to 60, the average fitness values obtained from GA have an upward trend. The average fitness values obtained from HGA algorithm tend to be fluctuant when the initial population size increases from 20 to 45 and tend to be stable when the initial population size exceeds 45. When the initial population size increases from 20 to 60, the average fitness values obtained from GA have an upward trend. The average fitness values obtained from HGA algorithm tend to be fluctuant when the initial population size increases from 20 to 45 and tend to be stable when the initial population size exceeds 45. When the initial population size increases from 20 to 60, the average fitness values obtained from GA have an upward trend. The average fitness values obtained from HGA algorithm tend to be fluctuant.
population size is around 30, but have an uptrend in general. Moreover, the average fitness values obtained from GA and HGA algorithms have small changes when the initial population size exceeds 50. The tendencies of the average fitness values obtained from the HABC and ABC algorithms are both stable. The tendency of the average fitness values obtained from PSO is fluctuant when the initial population size increases. On the other hand, if the initial population size is extremely large, the computational time of the algorithms increases significantly [19]. Therefore, for a fair and efficient comparison in the subsequent experiments, the initial population sizes of the algorithms are all set as 50.

### C. EXTENDED ARTIFICIAL BEE COLONY ALGORITHM PERFORMANCE IN SOLVING PROPOSED MODEL

To evaluate the performance of the EABC algorithm in solving the proposed JSS-JF model, the third set of simulation experiments was performed on instances with different scales and various weight combinations of total completion time and total cost. In this experiment, the weight combinations were set as 0.7 and 0.3, 0.5 and 0.5, 0.3 and 0.7 respectively. \( \text{Max} \), \( \text{Ave} \), and \( \text{SD} \) denote the best fitness value, average fitness value, and standard deviation of fitness values of the 10 runs. The indicator is marked in bold if the EABC algorithm outperforms the three baseline algorithms in this indicator.
By comparing with the basic algorithms and the improved algorithms proposed by other scholars, the superiority of the proposed algorithm is verified. Tables 4 – 6 summarize the experimental results of the four algorithms with various weight combinations, including EABC, GA, PSO, and ABC algorithms. It is observed that the EABC algorithm has a competitive performance over the basic algorithms. In terms of Max and Ave, the EABC algorithm outperforms the other algorithms in most instances whatever the weight combination is set. In terms of SD, the EABC algorithm also outperforms them in 9 out of 12 instances when the weight combination is 0.7 and 0.3; in 8 out of 12 instances when the weight combination is 0.5 and 0.5; and in 9 out of 12 instances when the weight combination is 0.3 and 0.7.

Tables 7 – 9 show the experimental results of the four algorithms with various weight combinations, including EABC, HGA, HPSO, and HABC algorithms. By observing the values of Max, Ave and SD in various weight combinations, it can be concluded that the EABC algorithm outperforms the other improved algorithms in at least 9 out of 12 instances in terms of Max; in at least 11 out of 12 instances in terms of Ave; and in at least 8 out of 12 instances in terms of SD.

Tables 4 – 9 show that the times of EABC algorithm outperforming the other algorithms are slightly fluctuant under various weight combinations.
the various weight combinations, but the EABC algorithm has generally a better performance over other algorithms in solving the proposed JSS-JF model. Therefore, it demonstrates that the various weight combinations have a minimal effect on the EABC algorithm in solving the proposed JSS-JF model. In summary, the EABC algorithm outperforms the six baseline algorithms in terms of practicality and effectiveness.

VI. CONCLUSION

JSS-JF is a critical issue in remanufacturing scheduling. In view of the various damage conditions of components encountered in the remanufacturing process, this study proposed a new JSS-JF model for remanufacturing systems that can be solved well by the EABC algorithm presented above. The main contributions of this study are summarized as follows.

(1) The proposed JSS-JF model for remanufacturing systems was presented, which decomposed the scheduling problem into three sub-problems: execution mode selection, replacement job assignment and sequencing, and repair machine assignment and operation sequencing.

(2) The EABC algorithm, which has extended the basic ABC algorithm in four aspects, including the three-dimensional encoding scheme, crossover and mutation operators, local search and elite replacement strategy, was proposed to solve the proposed JSS-JF model effectively.

Furthermore, simulation experiments based on instances with different scales were designed to illustrate the practicability and effectiveness of the proposed EABC algorithm by comparing with the six baseline algorithms. The comparative experimental results demonstrated that the EABC algorithm outperformed the other baseline algorithms in solving the proposed JSS-JF model.

With regard to future work, this study will be extended in several directions. First, more execution modes will be considered in remanufacturing systems by analyzing the characteristics of execution modes. Second, more practical factors, including non-zero ready time and machine breakdowns, will be explored. The future study will also consider the availability of the human operators to make the model more practical. Finally, the performance of the proposed EABC algorithm will be further enhanced by the integration of heuristic rules.

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