Response to the comments of Reviewer 1

This article provides what I consider an obvious first-order approach to modeling the effect of polarization of scattered sunlight over bare/desert regions. The advantages of the model are that it is simple and straightforward and physically intuitive. I consider this to be the first step in more complicated models. In addition, the model does not shy away from using advanced techniques. For instance, the authors select the agglomerated debris particles to represent their atmospheric aerosols. These particles have been demonstrated to be the most accurate at modeling the light-scattering properties of dust particles. In fact, they are the ONLY model particles that can accurately reproduce the light-scattering properties at multiple wavelengths (Zubko, 2013). As an introductory paper to this complicated topic, the paper leaves open several lines for future research and discussion. Not only does it provide the foundation for future, more advanced modeling approaches, but leaves some research questions unanswered:

Answer: The authors of this manuscript greatly thank this reviewer for the helpful and insightful comments.

1. When more complicated surface models are incorporated, how will this effect the results?

Answer: In the Conclusion, we add "When more complicated surface models such as that considering desert as semi-infinite particle layers are considered, it may improve the total reflectance modeling, but will have little effect on polarization degree and angle of polarization calculation, since polarization is mostly determined by single scattering at the top layer of the sand particles."

2. As with any model that is composed of several distinct physical parts, what are the predominate sources of error and what observations are necessary to test these parts independently, so that we know where it is best to focus our efforts to make improvements?

Answer: For a model composed of several distinct physical parts, the predominate sources of error is from each part. We must test each part and do sensitivity studies on the error effect of each part to determine the final error of the model. When we use observation data to check the error of each part, we must consider the sensitivity study of other parts, and use the representative parameters for other parts to model the final results, which are compared with the observational data.

3. Most significant in my mind are the surface parameters $f$ and sigma and their lack of dependence. What happens, for instance, when we consider extreme incident angles?
Answer: the surface parameters f and sigma are determined by the desert physical fact, which are fitted out by satellite data. They may have dependence on each other. But when they work together as a pair, they can produce results close to the satellite data. They are paired quantities and must be used as a pair. They should not be significantly affected by incident angles, but since they are derived from satellite data with limited incident angles, they may have small dependence on the incident angle due to sampling issue.

My only significant criticism is that I would prefer to see the figures discussed in more depth. The authors present several of these and make broad statements. In the text, they really should state what each figure shows and why it is being presented.

Answer: There are many figures with similar natures in the manuscript to better show the results for different wavelengths/viewing or incident geometries. Since we already have detailed description of each figure in the captions, we prefer to explain them in a summarized way in the text, to avoid redundant statements which make the paper lengthy. We tried our best to make the text concise under the condition that the meaning of each figure can be understood. Thanks for the reviewer’s recommendation, but we think we want to keep the summarized way to make the article concise.

There are some minor typographical considerations that I have transmitted to the authors.

Answer: Great thanks to the reviewer for the very detailed corrections of our errors in the text. A lot of careful corrections were made. The authors really appreciate the great help from this reviewer.

Response to the comments of Reviewer 2

This paper develops an algorithm for obtaining the spectral polarization state of solar light from desert with the PARASOL data. Through numerical experiments, concise but meaningful results are summarized. The reviewer recommends the publication to ACP, but the minor points below should be addressed before the publication.

Answer: The authors of this manuscript thank this reviewer for the helpful comments. The manuscript has been revised rigorously following these comments.
1) In Introduction, the importance of polarization correction should be emphasized quantitatively to let readers know the importance of this subject. How about adding some sentences around L15-17 in P8527.

Answer: This is done. We add "For example, the PARASOL data show that the degree of polarization (DOP) of reflected light from clear-sky desert can be ~30%. The broad-leaf trees also can reflect solar light with a DOP of ~70%. For a sensor with a sensitivity-to-polarization factor of only ~1%, its measurement for light with a DOP of ~30% and ~70% will have relative errors of ~0.3% and ~0.7%, respectively, solely due to the polarization (Sun and Lukashin, 2013)." in this section.

2) In Method of L17 in P8530, how is the sensitivity of the assumption for 0.02 of the refractive index?

Answer: We add "This assumption of sand’s imaginary refractive index could have a small effect on the modeled total reflectance from the desert, but has little effect on the DOP and AOLP calculations." in the text.

3) For typographical point, L11 in P8535, ‘Figures 20 to 15’, 15 should be 25.

Answer: This is corrected.
Deriving Polarization Properties of Desert-Reflected Solar Spectra with PARASOL Data

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**Highlights**

1. Spectral polarization state of reflected solar radiation is needed in correcting satellite data.

2. An algorithm for deriving spectral polarization state of solar light from desert is reported.

3. PARASOL data at 3 polarized channels are used in deriving polarization of whole solar spectra.

4. Desert-reflected solar light’s polarization state at any wavelength can be obtained.
Abstract. One of the major objectives of the Climate Absolute Radiance and Refractivity Observatory (CLARREO) is to conduct highly accurate spectral observations to provide an on-orbit inter-calibration standard for relevant Earth-observing sensors with various channels. To calibrate an Earth-observing sensor’s measurements with the highly accurate data from the CLARREO, errors in the measurements caused by the sensor’s sensitivity to the polarization state of light must be corrected. For correction of the measurement errors due to the light’s polarization, both the instrument’s dependence on the incident light’s polarization state and the on-orbit knowledge of the polarization state of light as a function of observed scene type, viewing geometry, and solar wavelength, are required. In this study, an algorithm for deriving the spectral polarization state of solar light from desert is reported. The desert/bare land surface is assumed to be composed of two types of areas: Fine sand grains with diffuse reflection (Lambertian non-polarizer) and quartz-rich sand particles with facets of various orientations (specular-reflection polarizer). The adding-doubling radiative transfer model (ADRTM) is applied to integrate the atmospheric absorption and scattering in the system. Empirical models are adopted in obtaining the diffuse spectral reflectance of sands and the optical depth of the dust aerosols over the desert. The ratio of non-polarizer area to polarizer area and the angular distribution of the facet orientations are determined by fitting the modeled polarization states of light to the measurements at 3 polarized channels (490, 670, and 865 nm) by the Polarization and Anisotropy of Reflectances for Atmospheric Science instrument coupled with Observations from a Lidar (PARASOL). Based on this physical model of the surface, the desert-reflected solar light’s polarization state at any wavelength in the whole solar spectra can be calculated with the ADRTM.
Introduction

One of the major objectives of the Climate Absolute Radiance and Refractivity Observatory (CLARREO) (Wielicki et al., 2013) is to conduct highly accurate spectral observations to provide an on-orbit inter-calibration standard for relevant Earth-observing sensors with various channels. To calibrate an Earth-observing sensor’s measurements with the highly accurate data from the CLARREO, errors in the measurements caused by the sensor’s sensitivity to the polarization state of light must be corrected (Lukashin et al., 2013; Sun and Lukashin, 2013; Sun et al., 2015). For correction of the measurement errors due to light’s polarization, both the instrument’s dependence on the incident light’s polarization state and the on-orbit knowledge of the polarization state of light as a function of observed scene type, viewing geometry, and solar wavelength, are required. Empirical polarization distribution models (PDMs) (Nadal and Breon, 1999; Maignan et al., 2009) based on data from the Polarization and Anisotropy of Reflectances for Atmospheric Science instrument coupled with Observations from a Lidar (PARASOL) (Deschamps et al., 1994) may be used to correct radiometric bias (Lukashin et al., 2013). But these can only be done at 3 or 4 solar wavelengths (i.e. 490, 670, and 865 nm) at which the PARASOL has reliable polarization measurements. Since the CLARREO is designed to measure solar spectra from 320 to 2300 nm with a spectral sampling of 4 nm (Wielicki et al., 2013), which has potential to inter-calibrate space-borne sensors at nearly all of the solar wavelengths (Sun and Lukashin, 2013), the PDMs for the inter-calibration applications should be made as functions of every sampling wavelength of the CLARREO. Due to strong dependence of solar
light’s polarization on wavelength (Sun and Lukashin, 2013), the applicability of empirical
PDMs based on only 3 or 4 channels of PARASOL polarization measurements will be very
limited. In our previous studies (Sun and Lukashin, 2013; Sun et al., 2015), polarized solar
radiation from the ocean-atmosphere system is accurately modeled. Because the refractive index
of water at solar spectra is well known (Thormählen et al., 1985), Sun and Lukashin (2013)
actually can produce the PDMs for ocean-atmosphere system at any solar wavelength. However,
it is still a difficult problem to obtain spectral PDMs for other scene types. For scene types other
than water bodies, although many studies have been conducted (Coulson et al., 1964; Egan,
1968; Egan 1969; Wolff, 1975; Egan, 1970; Vanderbilt and Grant, 1985; Tamalge and Curran,
1986; Grant, 1987), no reliable surface reflection matrix such as that based on the Cox and Munk
(1954; 1956) wave slope distribution models for oceans is available. For scene types dominated
by diffuse reflection, like fresh snow, grass lands or needle-leaf trees/bushes, this may not be a
serious problem. But for scene types like desert, snow crust/ice surfaces, or even broad-leaf trees,
specular reflection is still significant (like what happens at the ocean surface), polarization of the
reflected light can be very strong, thus needs to be accurately accounted for. For example, the
PARASOL data show that the degree of polarization (DOP) of reflected light from clear-sky
desert can be ~30%. The broad-leaf trees also can reflect solar light with a DOP of ~70%. For a
sensor with a sensitivity-to-polarization factor of only ~1%, its measurement for light with a
DOP of ~30% and ~70% will have relative errors of ~0.3% and ~0.7%, respectively, solely due
to the polarization (Sun and Lukashin, 2013).

For bare soils and vegetation, Breon et al. (1995) developed some simple methods to calculate
the polarized reflectance from the surface. But these methods can only model the polarized
reflectance, which are not suitable for deriving the full elements of the surface reflection matrix
for coupling with the radiative transfer model to simulate all Stokes parameters of the reflected light at the top of the atmosphere (TOA). Our objective for this study is to model the PDMs, which are the degree of polarization (DOP) and angle of linear polarization (AOLP) (Sun and Lukashin, 2013) of the reflected light at any solar wavelength. Polarized reflectance solely is insufficient for deriving the DOP and not usable for deriving the AOLP.

In this study, an algorithm for obtaining the spectral polarization state of solar light from desert with the PARASOL data is developed. The method of deriving the polarization state of solar light from desert-atmosphere system at any wavelength with the PARASOL-measured polarized radiances at 490, 670, and 865 nm is reported in Section 2. Numerical results and discussions are presented in Section 3. Summary and conclusions are given in Section 4.

2 Method

The polarization of reflected light is related to the surface roughness (Wolff, 1975) and to the size of reflecting elements (Egan, 1970). In this study, the desert/bare land surface is assumed to be composed of two types of areas: Fine sand grains with diffuse reflection (Lambertian non-polarizer) and quartz-rich sand particles with facets of various orientations (specular-reflection polarizers). The desert surface light reflection matrix is obtained based on mixed effects of the two types of areas. Similar to the treatment for rough-ocean surfaces (e.g. Sun and Lukashin, 2013), the desert surface reflection matrix with 4x4 elements is calculated as

\[
\mathbf{R}_0(\theta_s, \theta_v, \varphi) = f\mathbf{R}_L + (1 - f) \frac{\pi \mathbf{M}(\theta_s, \theta_v, \varphi)}{4 \cos^4 \beta \cos \theta_s \cos \theta_v} P(Z_s, Z_v),
\]

(1)

where \(\theta_s, \theta_v,\) and \(\varphi\) denote solar zenith angle, viewing zenith angle, and relative azimuth angle of the reflected light, respectively. The fraction of Lambertian area is denoted as \(f\). \(\mathbf{R}_L\) is the reflection matrix of Lambertian reflector, with the reflectance as the only nonzero element.
4x4 elements of $M(\theta_x, \theta_v, \varphi)$ for each quartz-rich sand particle facet orientation are calculated in the same way as in Mishchenko and Travis (1997) based on the Fresnel Laws. $P(Z_x, Z_y)$ is the quartz-rich sand facet orientation probability distribution as a function of the surface roughness. Assuming desert is a stationary sand “ocean” with quartz-rich sand particle facets as specular reflection “waves” and Lambertian reflection sand grains as “foams”, we can adopt the formula given in Cox and Munk (1956) for $P(Z_x, Z_y)$ as

$$P(Z_x, Z_y) = \frac{1}{\pi \sigma^2} \exp\left(-\frac{Z_x^2 + Z_y^2}{\sigma^2}\right), \quad (2)$$

where $\sigma$ denotes the roughness parameter of the desert surface, and

$$Z_x = \frac{\partial Z}{\partial x} = \frac{\sin \theta_v \cos \varphi - \sin \theta_t}{\cos \theta_v + \cos \theta_s}, \quad (3)$$

$$Z_y = \frac{\partial Z}{\partial y} = \frac{\sin \theta_v \sin \varphi}{\cos \theta_v + \cos \theta_s}. \quad (4)$$

In Eqs. (2) to (4), $Z$ denotes the height of the surface. In Eq. (1), $\beta$ is the tilting angle of a sand facet, and $\tan \beta = \sqrt{Z_x^2 + Z_y^2}$.

The polarization of reflected solar radiation from the Earth-atmosphere system is the result of both the surface reflection and the scattering by molecules and particles in the atmosphere. In this study, the adding-doubling radiative transfer model (ADRTM) (Sun and Lukashin, 2013) is applied to integrate the atmospheric absorption and scattering with the desert surface reflection.

To get the reflection matrix elements of desert with Eq. (1), we must obtain 4 unknown quantities in advance: $f$, $\sigma$, $R_L$, and the refractive index of quartz-rich sand. In this study, the refractive index of quartz-rich sand is assumed to be that of fused silica as a function of solar wavelength (Malitson, 1965):
\[ n^2 - 1 = \frac{0.6961663\lambda^2}{\lambda^2 - (0.0684043)^2} + \frac{0.4079426\lambda^2}{\lambda^2 - (0.1162414)^2} + \frac{0.8974794\lambda^2}{\lambda^2 - (9.896161)^2}, \]  

where \( n \) is the real refractive index of the silica and \( \lambda \) denotes the solar wavelength in \( \mu \)m. In this study, to account for the impurity absorption in the quartz-rich sands, we assume the imaginary part of the sand refractive index to be 0.02. This assumption of sand’s imaginary refractive index could have a small effect on the modeled total reflectance from the desert, but has little effect on the DOP and AOLP calculations.

However, \( f \), \( \sigma \), and \( R_L \) must be obtained from observations for desert. In this study, the spectral structure of the Lambertian reflectance of desert \( R_L^0(\lambda) \) for wavelength longer than 800 nm is based on the analysis of data in Aoki et al. (2002) and Sadiq and Howari (2009) for desert reflectance in Taklimakan Desert and the southeast of Qatar, respectively. For wavelengths shorter than 800 nm, the spectral structure of \( R_L^0(\lambda) \) is determined by an analysis of data in Aoki et al. (2002), Sadiq and Howari (2009), Bowker et al. (1985), and Koelemeijer et al. (2003). This spectral reflectance structure multiplied with a scale factor \( \alpha \) is then entered in the ADRTM, and on the condition of \( f = 1.0 \) and at a solar zenith angle of 28.77° the solar reflectances at the wavelength of 490, 670, and 865 nm from the ADRTM and those from the 24-day mean of the PARASOL measurements are compared. By varying the scale factor \( \alpha \), we can make the reflectances at the wavelengths of 490, 670, and 865 nm from the ADRTM close to those from the PARASOL data. The resultant \( \alpha R_L^0(\lambda) \) is the reflectance of the Lambertian desert area, which as the first element of the \( R_L \), is linearly extrapolated to the CLARREO solar wavelength limit of 320 nm. The empirical spectral reflectance of desert from this process is displayed in Fig. 1.

Since desert reflectance varies significantly with desert types (Otterman, 1981; Bowker et al., 1985; Dobber et al., 1998; Aoki et al., 2002; Koelemeijer et al., 2003), our empirical desert \( R_L \)
model may not be very representative. However, with the other two free parameters \( f \) and \( \sigma \) in the model, we may still approach the accurate PDMs (i.e. DOP and AOLP) even when \( R_L \) has some difference from true values in practice.

In this study, the adding-doubling radiative transfer model (ADRTM) (Sun and Lukashin, 2013) is applied for calculation of the Stokes parameters of the reflected light from the desert-atmosphere system. The U. S. Standard Atmosphere (1976) is applied in the calculations. Gas absorption coefficients from the \( k \)-distribution treatment (Kato et al., 1999) of the spectral data from the line-by-line radiative transfer model (LBLRTM) (Clough et al., 1992; 1995) using the MODTRAN 3 dataset (Kneizys et al., 1988) is used. Ozone absorption coefficients are taken from the ozone cross-section table provided by the World Meteorological Organization (1985) for wavelengths smaller than 700 nm. Molecular scattering optical thickness is from Hansen and Travis (1974). The scattering phase-matrix elements of molecular atmosphere are based on the Rayleigh scattering solution with a depolarization factor of 0.03 (Hansen and Travis, 1974). Single-scattering properties of sand--dust aerosols are calculated using agglomerated debris particles with the discrete-dipole approximation (DDA) light scattering model (Zubko et al., 2006; 2009; 2013). Two-mode lognormal size distributions (Davies, 1974; Whitby, 1978; Reist, 1984; Ott, 1990; Porter and Clarke, 1997) are applied in calculation of the single-scattering properties of aerosols. A dust aerosol refractive index of \( 1.5 + 0.0i \) is assumed in the modeling. An average aerosol optical depth (AOD) of the dust over the Morocco desert (Toledano et al., 2008) is adopted in this study:

\[
AOD = 0.2374 \lambda^{-0.2291},
\]

where \( \lambda \) is the solar wavelength in \( \mu \text{m} \). Dust AOD decreases with the increase of wavelength.

In this study, the ratio of the non-polarizer area to polarizer area of the desert and the angular
distribution of the quartz-rich sand–particle facet orientations are determined by fitting the modeled polarization states of reflected light to the measurements at 3 polarized channels (490, 670, and 865 nm) by the PARASOL. By varying the two free parameters $f$ and $\sigma$ in the model, we calculated a lookup table of spectral DOP and AOLP as functions of $f$ and $\sigma$ for desert. We then compared the modeled DOP and AOLP with those from the PARASOL data. The pair of $f$ and $\sigma$ that simultaneously produce similar DOP and AOLP to the PARASOL data at a solar zenith angle of 28.77° and 3 polarized channels (490, 670, and 865 nm) of the PARASOL are the retrieved values for the physical model of desert surface. In this retrieval, the PARASOL data are from the mean of 24-day measurements for global desert. The 24 days of PARASOL data are taken from the first two days of each month across 2006. The retrieved $f$ and $\sigma$ values are then used to calculate the DOP and AOLP at any solar wavelengths and any solar zenith angles. This can produce the PDMs for clear-sky desert. For desert with clouds, it is straightforward to do the calculation by simply adding cloud layers in the ADRTM.

3 Results

In this study, the retrieved values of $f$ and $\sigma$ for desert are 0.95 and 0.164, respectively. These values are applied to the ADRTM to calculate the polarization properties of reflected solar spectra from desert. Figures 2 to 4 show the modeled reflectance, DOP, and AOLP of reflected solar light from desert at a wavelength of 490 nm and a solar zenith angle (SZA) of 28.77° with those from the PARASOL data at a SZA bin of 27-30°. We can see that the model results are very close to the PARASOL data at nearly all viewing directions. The modeled DOP agrees very well with that from the PARASOL data, with differences smaller than 5%. The AOLPs from the ADRTM and the PARASOL are also very similar, with only minor differences at viewing angles.
close to the backscattering direction. The reflectance from the ADRTM with \( f = 0.95 \) and \( \sigma = 0.164 \) is also very close to that from the PARASOL, which is nearly Lambertian but a little larger at backward-reflecting directions. At a larger SZA of 56.94°, Figures 5 to 7 show that the modeled reflectance, DOP, and AOLP are also very close to those from the PARASOL data, demonstrating that the retrieved desert physical property \( f = 0.95 \) and \( \sigma = 0.164 \) work well for solar angles other than the SZA of 28.77°, at which they are derived from the PARASOL measurements. From Figs. 2-7, we also can see that at the wavelength of 490 nm desert has a strong polarization effect in the forward-reflecting direction. At a viewing zenith angle (VZA) of 60°, the DOP of desert at 490 nm can reach ~30%, which means that for a satellite sensor with only ~1% polarization dependence, the desert polarization to sunlight can cause ~0.3% error in spectral radiance measurement (Sun and Lukashin, 2013).

For a longer wavelength of 670 nm, Figures 8 to 13 show that the modeled DOP is very similar to the PARASOL data for different solar and viewing angles. The AOLP from the ADRTM shows some difference from that of the PARASOL at backward-reflecting directions. Particularly, Figure 10 shows that the AOLP from the ADRTM has a pattern in the neighborhood of backward-reflecting angle that is very similar to those for clouds reported in Sun and Lukashin (2013), Sun et al. (2014), and Sun et al. (2015). This likely is because the refractive index for dust aerosols in our modeling is assumed to be 1.5 and the imaginary part is zero. Under this condition, the dust particles are nonabsorbing crystals which have similar scattering properties to water droplets or ice crystals in clouds at the wavelength of 670 nm. However, it is worth noting here that the errors in the AOLP from the ADRTM due to our assumptions for dust refractive index will only have a minor effect on the polarization correction accuracy. This is due to the fact that the DOPs at these observation angles are very small, and
also that the AOLP errors in these observation angles actually will not result in any significant difference in polarization correction, i.e. AOLP = −0° and AOLP = −180° means the same to the satellite sensor. However, at 670 nm, the PARASOL data for desert show stronger reflectance in the backward-reflecting directions than in the forward-reflecting directions. This is significantly different from the ocean cases. Desert’s reflection of solar radiation is a complicated phenomenon which is neither Lambertian nor specular-reflection. Thus, our simple approach here shows some difference in reflectance from the data. However, our objective for this study is to accurately model the desert DOP accurately, and to accurately model the desert AOLP accurately when the DOP is not trivial. Such modeling errors in the total reflectance are to be expected and not the concern of this study. Errors in modeling the reflectance is ignorable for this purpose.

For an even longer wavelength of 865 nm, Figures 14 to 19 show that, similar to the cases for the wavelength of 670 nm, the modeled DOP and AOLP are very similar close to the PARASOL data. The PARASOL reflectance at 865 nm also shows significantly stronger reflectance in the backward-reflecting directions than in the forward-reflecting directions. Without knowing the proper reason for the desert reflectance angular feature, our modeling cannot capture this angular distribution of reflected light well. This is a topic deserving further study, probably by researchers concerned with this. This is worthy of being studied by people working for the radiation energy budget studies.

Note here that it is not a surprise that we can get accurate modeling far-off the DOP and AOLP of reflected solar spectra from desert as shown in Figs. 2-4, 8-10, and 14-16, for a solar zenith angle of 28.77°, since the parameters $f = 0.95$ and $\sigma = 0.164$ used in the modeling are retrieved from the PARASOL data at this solar zenith angle. To examine whether or not the desert surface physical
parameters \((f \text{ and } \sigma)\) from a specific solar zenith angle can be accurately applied to any other solar zenith angles, we modeled the polarized radiation from the desert-atmosphere system at a solar zenith angle of 56.94° with the \(f\) and \(\sigma\) obtained at a solar zenith angle of 28.77°. These modeling results are compared with the PARASOL data in Figs. 5-7, 11-13, and 17-19. It is demonstrated that at all the 3 wavelengths of 490, 670, and 865 nm, the DOP and AOLP from the ADRTM agree well with the PARASOL data in every case. These results show that the method can be applied to any other solar zenith angles once the desert surface physical parameters \((f \text{ and } \sigma)\) are obtained at a specific solar zenith angle.

As mentioned previously, the CLARREO is designed to measure solar spectra from 320 to 2300 nm with a spectral sampling of 4 nm. To calibrate space-borne sensors with the CLARREO measurements in the solar spectra, the PDMs to correct polarization-induced errors in radiation measurement for the inter-calibration applications should be made as a function of every sampling wavelength of the CLARREO. Therefore, the modeling of the reflected solar radiation’s polarization must be done over the range of any solar wavelengths. Figures 20 to 25 show exemplary results for the modeling method to be applied to the wavelength limits (320 nm and 2300 nm) of the CLARREO solar measurements at different solar zenith angles. It is shown that at short wavelengths, the region’s desert’s polarization from desert regions to solar radiation is can be very strong, can be ~50%. However, at long wavelengths, the polarization degree is only ~10%. However, even a ~10% degree of polarization degree could cause significant errors in radianc if the sensor’s dependence on polarization is significant.

4 Conclusions
In this study, an algorithm for deriving the spectral polarization state of solar light reflected from desert is reported. The desert/bare land surface is assumed to be composed of two types of areas: Fine sand grains with diffuse reflection (Lambertian non-polarizer) and quartz-rich sand particles with facets of various orientations (specular-reflection polarizer). The adding-doubling radiative transfer model (ADRTM) is applied to integrate the atmospheric absorption and scattering in the system. Empirical models are adopted in obtaining the diffuse spectral reflectance of sands and the optical depth of the dust aerosols over the desert. The ratio of non-polarizer area to polarizer area and the angular distribution of the facet orientations are determined by fitting the modeled polarization states of light to the measurements at 3 polarized channels (490, 670, and 865 nm) by the Polarization and Anisotropy of Reflectances for Atmospheric Science instrument coupled with Observations from a Lidar (PARASOL). Based on this simple physical model of the surface, the polarization state of the desert-reflected solar light’s polarization state at any wavelength in the whole solar spectra can be calculated with the ADRTM. When more complicated surface models such as that considering desert as semi-infinite particle layers are considered, it may improve the total reflectance modeling, but will have little effect on polarization degree and angle of polarization calculation, since polarization is mostly determined by single scattering at the top layer of the sand particles.

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Figure 1. Empirical spectral reflectance of desert from analysis of data in Aoki et al. (2002), Sadiq and Howari (2009), Bowker et al. (1985), and Koelemeijer et al. (2003), and is scaled by the PARASOL measurements.
Figure 2. Comparison of the modeled DOP and reflectance of desert-reflected solar light at relative azimuth angles (RAZ) of 0° and 180° with those from the PARASOL data at the wavelength of 490 nm. The solar zenith angle (SZA) is 28.77° in the modeling. The SZA is in the bin of 27-30° for the PARASOL data.
Figure 3. Same as in Fig. 2, but at relative azimuth angles (RAZ) of 90° and 270°.
Figure 4. Comparison of the modeled AOLP of desert-reflected solar light with those from the PARASOL data at the wavelength of 490 nm. The solar zenith angle (SZA) is 28.77° in the modeling. The SZA is in the bin of 27-30° for the PARASOL data.
Figure 5. Comparison of the modeled DOP and reflectance of desert-reflected solar light at relative azimuth angles (RAZ) of 0° and 180° with those from the PARASOL data at the wavelength of 490 nm. The solar zenith angle (SZA) is 56.94° in the modeling. The SZA is in the bin of 54-57° for the PARASOL data.
Figure 6. Same as in Fig. 5, but at relative azimuth angles (RAZ) of 90° and 270°.
Figure 7. Comparison of the modeled AOLP of desert-reflected solar light with those from the PARASOL data at the wavelength of 490 nm. The solar zenith angle (SZA) is 56.94° in the modeling. The SZA is in the bin of 54-57° for the PARASOL data.
Figure 8. Comparison of the modeled DOP and reflectance of desert-reflected solar light at relative azimuth angles (RAZ) of 0° and 180° with those from the PARASOL data at the wavelength of 670 nm. The solar zenith angle (SZA) is 28.77° in the modeling. The SZA is in the bin of 27-30° for the PARASOL data.
Figure 9. Same as in Fig. 8, but at relative azimuth angles (RAZ) of 90° and 270°.
Figure 10. Comparison of the modeled AOLP of desert-reflected solar light with those from the PARASOL data at the wavelength of 670 nm. The solar zenith angle (SZA) is 28.77° in the modeling. The SZA is in the bin of 27-30° for the PARASOL data.
Figure 11. Comparison of the modeled DOP and reflectance of desert-reflected solar light at relative azimuth angles (RAZ) of 0° and 180° with those from the PARASOL data at the wavelength of 670 nm. The solar zenith angle (SZA) is 56.94° in the modeling. The SZA is in the bin of 54-57° for the PARASOL data.
Figure 12. Same as in Fig. 11, but at relative azimuth angles (RAZ) of 90° and 270°.
Figure 13. Comparison of the modeled AOLP of desert-reflected solar light with those from the PARASOL data at the wavelength of 670 nm. The solar zenith angle (SZA) is 56.94° in the modeling. The SZA is in the bin of 54-57° for the PARASOL data.
Figure 14. Comparison of the modeled DOP and reflectance of desert-reflected solar light at relative azimuth angles (RAZ) of 0° and 180° with those from the PARASOL data at the wavelength of 865 nm. The solar zenith angle (SZA) is 28.77° in the modeling. The SZA is in the bin of 27-30° for the PARASOL data.
Figure 15. Same as in Fig. 14, but at relative azimuth angles (RAZ) of 90° and 270°.
Figure 16. Comparison of the modeled AOLP of desert-reflected solar light with those from the PARASOL data at the wavelength of 865 nm. The solar zenith angle (SZA) is 28.77° in the modeling. The SZA is in the bin of 27-30° for the PARASOL data.
Figure 17. Comparison of the modeled DOP and reflectance of desert-reflected solar light at relative azimuth angles (RAZ) of 0° and 180° with those from the PARASOL data at the wavelength of 865 nm. The solar zenith angle (SZA) is 56.94° in the modeling. The SZA is in the bin of 54-57° for the PARASOL data.
Figure 18. Same as in Fig. 17, but at relative azimuth angles (RAZ) of 90° and 270°.
Figure 19. Comparison of the modeled AOLP of desert-reflected solar light with those from the PARASOL data at the wavelength of 865 nm. The solar zenith angle (SZA) is 56.94° in the modeling. The SZA is in the bin of 54-57° for the PARASOL data.
Figure 20. The modeled DOP and reflectance of desert-reflected solar light at relative azimuth angles (RAZ) of 0° and 180° at the wavelength of 320 nm. The solar zenith angle (SZA) is 28.77° and 56.94°, respectively, in the modeling.
Figure 21. Same as in Fig. 20, but at relative azimuth angles (RAZ) of 90° and 270°.
Figure 22. The modeled AOLP of desert-reflected solar light at the wavelength of 320 nm.
The solar zenith angle (SZA) is 28.77° and 56.94°, respectively, in the modeling.
Figure 23. The modeled DOP and reflectance of desert-reflected solar light at relative azimuth angles (RAZ) of 0° and 180° at the wavelength of 2300 nm. The solar zenith angle (SZA) is 28.77° and 56.94°, respectively, in the modeling.
Figure 24. Same as in Fig. 23, but at relative azimuth angles (RAZ) of 90° and 270°.
Figure 25. The modeled AOLP of desert-reflected solar light at the wavelength of 2300 nm. The solar zenith angle (SZA) is 28.77° and 56.94°, respectively, in the modeling.