Application of Digital Image Processing to Determine the Properties of Aggregates and Soil using MATLAB: A Case Study

M.C. Bathula1,*, S.V.H. Madiraju2

1Department of Civil Engineering, College of Engineering, Shiv Nadar University, Greater Noida – 201 314, Uttar Pradesh, India.
2Dept. of Civil Engineering, College of Engineering, VNR Vignana Jyothi Institute of Engineering and Technology, Hyderabad – 500 090, Telangana, India.

1. Introduction

A digital image is a numerical representation, normally binary, of a two-dimensional image. DIP is the process of performing image processing on digital images with the use of computer algorithms. It could be employed to determine and evaluate properties of aggregates, rocks with the help of images captured. These processes are advantageous as they are Non-Destructive Tests (NDT) and we can assess and access the materials which are inaccessible, or which are still in use. It also reduces the amount of time and energy necessary in carrying out these processes manually. DIP is easy to use and economical. Image processing is employed in this paper to obtain shrinkage of soil due to loss in moisture content by natural or artificial ways. The Wax-water method is a manual method used to find the shrinkage values of soil [1,2]. Soil shrinkage is, for the most part, kept to the upper layers of soil. Shrinkage splits are caused by the decrease in soil dampness content through dissipation from the soil surface in dry atmospheres, bringing down the groundwater table, and drying up of soil by trees amid transitory droughts in general muggy atmospheres. Shrinkage is influenced by properties of soil including moisture content, plasticity index, mineralogy, and to some extent permeability. Shrinkage and swelling lead to failure of soils due to change in stresses and lead to appearances of cracks in civil structures [3]. This study provides step by step procedure followed to evaluate the shrinkage in two different kinds of soil available in SNU with varying moisture content when changed from heating using image processing and compare the results with the Wax-water manual method of finding soil shrinkage volume [4]. The processing of data for storage and transmission using digital images is a DIP technique. It extracts information out of images [5]. There is a wide range of applications for image processing such as medical/biological fingerprints, space image processing, remote sensing applications etc. [6]. There are some basic functions to be performed that are imperative for producing the required result. These stepwise functions are pre-processing, image acquisition, recognition, interpretation, segmentation, representation, description, problem domain and result [7].

1.1 Aggregate Properties

a) Grading: Grading refers to the determination of the particle-size distribution for aggregate. Grading limits and maximum aggregate size affect the amount of aggregate used. Cement, water requirements, workability, pumpability, and durability of concrete are also affected by grading limits.

b) Angularity: Angularity is necessary to ensure adequate aggregate interlock and prevent excessive hot mix asphalt deformation under load. Angularity number is the measure of angularity. It is measured as the percentage of voids in the aggregate after compaction.

c) Elongation Index: The particles whose largest length is 1.8 times their mean dimension are elongated. To calculate the elongated index, the weight of elongated particles is expressed as a percentage of the total weight of the sample.

d) Flakiness Index: A flaky particle is the one whose least dimension is 0.6 times the mean size. Flakiness index is the percentage by weight of flaky particles in a sample.

e) Sphericity: It is a measure of the roundness of aggregates. Sphericity is usually defined as the ratio of the surface area of a sphere having the same volume as the particle to the actual surface area of the particle [8].

1.2 Soil Properties

a) Moisture Content: The percentage of moisture which is expressed as the ratio of the weight of water to the weight of the dry soil in each mass of soil after oven drying the sample by maintaining a temperature between 105 °C and 110 °C.

b) Specific Gravity: The ratio of the weight of soil sample in the air to the weight of distilled water of the same volume in the air at the same temperature. Specific Gravity is used to calculate other soil properties like void ratio, degree of saturation, and weight-volume relationship.

c) Permeability: The ability of the soil to transmit water and air through the soil. It is expressed as the coefficient of permeability. The rate of flow under laminar flow conditions through a unit cross-sectional area of the porous medium under the unit hydraulic gradient is defined as the coefficient of permeability. The knowledge

*Corresponding Author: maruti.bathula@outlook.com (Maruti Chowdary Bathula)
of this property is much useful in solving problems involving the yield of water-bearing strata, seepage through earthen dams, the stability of earthen dams, and embankments of canal banks affected by seepage, settlement et cetera.

d) Shrinkage-Limit: Every type of soil undergoes volumetric reduction when exposed to natural sunlight or by artificial heating. Shrinkage limit is the moisture content percentage limit of soil after which no volume change occurs even if the moisture content drops further [9].

1.3 Digital Image Process

DIP has changed the way the properties of aggregates are found. A lot of time and destruction are involved while finding out the properties [10]. DIP techniques are widely used to analyze the particle shape characteristics of aggregate due to reduced time and its NDT characteristics [11]. Properties of particles that are not accessible are easily found. Grading curves are either found by finding volume by 2-D image information or by combining two images to get 3-D information [12]. Angularity, sphericity, elongation index, and flakiness index are found hassle-free by introducing parameters to the information from the 2-D images [13].

2. Experimental Methods

Digital image processing could be used to find many physical properties of aggregates. It comes under NDT and consumes lesser time to derive results and hence this method is selected to find the volumetric shrinkage of soil due to loss of moisture content either by the natural or artificial method. This paper will also discuss the best algorithms that could be used to find aggregate properties such as angularity, sphericity, flakiness index, and elongation index using MATLAB. The shape factor is found by using digital image processing over a regular object with known dimensions. The bounding box of an irregular boulder is determined using DIP and to extract its maximum length, breadth, and center of gravity of the boulder. The properties of multiple aggregates such as length, breadth, area, volume, the center of gravity, elongation index, flakiness index, and sphericity using DIP are calculated and the results were compared with conventional results. A code was developed to extract the volumetric shrinkage of two different kinds of soil available in SNU for varying moisture content by oven drying the sample and compare the results to the conventional method of wax-water method of finding shrinkage is determined. All the raw materials such as aggregates and soil are collected from Shiv Nadar University. Different types of soil are collected from two points at the University for Comparison. One sample is taken from the lakeside of the university and another sample is taken from the Business Management block (BMS).

3. Results and Discussion

3.1 Extracting Information from a Regular Object

To familiarize readers with the code developed, the physical properties of a regular object are found with known data. The accuracy and ease of use are checked with this experiment and pixel to mm conversion is made by determining the scale factor [14]. The camera is placed at a fixed known height. A fixed height gives us the same scale factor. White chart paper is used as a background to get a clear view of the objects placed and avoid any sort of unwanted discrepancies during capture. Shadows were avoided by adjusting the light as much as possible [15].

The RGB image is read and converted into a greyscale image and global threshold level is found to convert the intensity image to a binary image

Using the level found, binary image is extracted

Holes and other disturbances are removed and object in the binary image is separated from its background

Code is written to find the maximum length of an irregular binary image and repeated to find maximum breadth of the aggregate using columns

Properties like area, centroid are found from the binary image

Fig. 2 Stepwise proceedings of the algorithm to find the aggregate properties

3.2 Extracting Information from an Irregular Boulder

After familiarizing with the code in MATLAB and establishing the scale factor using a regular object, the accuracy of length, breadth detection of an irregular object must be built as all the civil engineering materials used are irregular [16]. Therefore, an irregular boulder is used to find the accurate maximum length, maximum breadth, and centroid. A similar set-up is used as used to capture a regular object with white chart paper as a background. The height of the camera is the same as used for regular objects and care is taken to avoid major shadows. An irregular small boulder is captured using this set-up. MATLAB is used to extract the dimensions of the irregular boulder. A slightly modified version of the code is used to derive the maximum length and breadth of the irregular boulder. Maximum length and breadth were found and compared the results with manual length and breadth of the boulder. The centroid is also found and plotted concerning the origin. Figs. 3 and 4 represents stepwise proceedings of steps of an algorithm to extract information from irregular objects. The percentage of error when both DIP and conventional methods are compared is around 2-3% as per the results from Table 1. The lack of complete precision is due to some unavoidable shadows.

\begin{table}[h]
\centering
\begin{tabular}{|l|l|l|}
\hline
\textbf{Table 1} & \textbf{Comparison of properties of the single irregular small boulder by DIP and conventional methods} \\
\hline
\textbf{Length} & \textbf{DIP (cm)} & \textbf{Conventional (cm)} \\
\hline
8.80 & 9.2 \\
\hline
\textbf{Breadth} & 6.34 & 6.5 \\
\hline
\end{tabular}
\end{table}

Fig. 1 Chronological order of steps to extract information from the regular object image

Fig. 3 Chronological order of steps to extract information from an image of an irregular boulder

The computing programming language used in this paper to compute the necessary information of various civil engineering materials is MATLAB. Figs. 1 and 2 represent logical steps in chronological order carried out to extract information from the regular objects. The regular objects captured for the purpose are a cap and a disk with known dimensions. Minor percentage error of under 2% in the length and area from DIP when compared to the real length and surface area of the objects due to the placement of objects and due to unavoidable specs of shadows.

Fig. 1 Chronological order of steps to extract information from the regular object image

https://doi.org/10.30799/jacs.234.21070104

Cite this Article as: M.C. Bathula, S.V.H. Madiraju, Application of digital image processing to determine the properties of aggregates and soil using MATLAB: A case study, J. Adv. Chem. Sci. 7(1) (2021) 711–716.
Extracting Information from Multiple Coarse Aggregates

Extract information from a bulk of coarse aggregates at the same time in one image is timesaving and DIP gives accurate results of aggregate properties [17]. MATLAB codes on both regular and irregular single aggregates are tested. Improving and extending the code can achieve good results of multiple coarse aggregate properties such as maximum length, maximum breadth, area, volume, centroid, elongation ratio, flakiness ratio, and sphericity of the coarse aggregates [18]. Volume from 2D imaging is tedious and proved methods are used to find volume, sphericity, flakiness ratio, and elongation ratio using 2D imaging as per Mora et al. 2000. Thickness and volume are estimated by an assumption that aggregates from the same source have more or else the same characteristics.

This mean thickness can be estimated from the breadth of the aggregates.

mean thickness = \( \lambda \times \) breadth

\( \lambda \) depends on the flakiness of aggregates and it is expressed as

\[ \lambda = \frac{M_p}{\sqrt{\text{area} \times \text{breadth}}} \]

volume = \( \lambda \times \) breadth \times area

The flakiness ratio is expressed as \( \lambda \) determined as it represents the mean thickness/breadth ratio of the aggregate sample. Elongation ratio is expressed as length to breadth ratio.

Sphericity = \( \sqrt{\text{thickness} \times \text{breadth} / \text{length}^2} \)

Most of the results are compared to the results from manual conventional methods to determine the accuracy and compute the percentage of error. Coarse aggregate is collected from the lab and sieved analysis was performed on the sample. Sample for capturing is chosen by taking aggregates from every sieve to have the right mix of samples of different sizes. A white chart paper is spread, and aggregates are placed over it. Care is taken such that there is no overlap of aggregates. Fixed height is used as used for the previous two pictures to get the same scale factor. Shadows are avoided as much as possible and pictures are to have a good definition.

Tests performed on the aggregates. Sieve analysis is performed to get the right sample for DIP. Flakiness and Elongation index and specific gravity tests are performed on the coarse aggregates from which the sample is collected. Table 2 shows the results of the tests on coarse aggregates. Stepwise proceedings of the algorithm to find the properties of multiple coarse aggregates are represented in Fig. 5. The chronological order of steps to extract information from an image of multiple aggregates is represented in Fig. 6. From Table 2, Flakiness index and elongation index are found.

Flakiness index = \( \frac{W_2}{W_1} \times 100 \times 0.526 \times 4.955 \times 100\% = 10.879\% \)

Elongation index = \( \frac{W_2}{W_1} \times 100 \times 0.564 \times 4.955 \times 100\% = 11.7\% \)

A comparison of parameters of coarse aggregates using both DIP and conventional methods is provided in Table 3. Negligible error is noticed in volume. But elongation and flakiness indices are noticed to have significant errors as the sample size is very small. It can further be improved with the quality of pictures and the removal of complete shadows.
3.4 Extracting Information on Volumetric Soil Shrinkage

Soil shrinkage occurs in expansive soil when the soil dries when heating occurs naturally or through oven drying. Failure occurs in the form of cracks due to volumetric changes in the soil. Therefore, it is important to find a change in the volume of shrinkage to study the damage caused by the soil. Shrinkage depends on the changing moisture content of the soil, mineralogy, plasticity index, pore water pressure, and so forth. DIP can be used to calculate the volumetric changes in soil due to shrinkage as it gives accurate results [19]. DIP shrinkage results are compared with conventional results. The conventional method used to find the shrinkage is the wax-water method which works on the Archimedes principle. The soil sample is collected from two points in SNU (Shiv Nadar University). The first point is right next to the lake and the second point is near BMS (Business management school). The soil was collected from a depth of about 50cms. To reduce the basic soil properties and compare the differences between both the soils laboratory tests are performed. They are, (i) grain size analysis (sieve analysis), (ii) moisture content, (iii) specific gravity, iv) consistency limits (plastic limit, liquid limit, and plasticity index) and v) permeability test. The laboratory tests are performed as per conventional methods as followed by Indian Standard (IS) procedures.

3.4.1 Grain Size Analysis of the Sample Soils (Sieve Analysis)

This section provides the results of the grain size analysis for lake soil and BMS soil (Tables 4 and 5 respectively), the trend of grain size (mm) and (% finer of both lake and BMS soils (Fig. 7), D60, D30, D15 of the lake, and BMS soil (Table 6).

| Table 4 | Grain sieve analysis observations (lake soil) |
|----------|---------------------------------------------|
| LS. Sieve | Wt. retained in each sieve (g) | % retained on each sieve | Cumulative % retained on each sieve | % Finer |
| Number or size in mm | | | | |
| 4.25 | 26 | 5.39 | 5.39 | 94.61 |
| 2 | 46 | 9.54 | 14.93 | 85.07 |
| 1.18 | 46 | 9.54 | 24.47 | 75.53 |
| 0.6 | 50 | 10.37 | 34.84 | 65.16 |
| 0.425 | 36 | 7.46 | 42.3 | 57.7 |
| 0.3 | 6 | 1.24 | 43.54 | 56.46 |
| 0.15 | 40 | 8.29 | 51.8 | 48.17 |
| 0.075 | 172 | 35.68 | 87.51 | 12.49 |
| Pan | 60 | 12.45 | 100 | 0 |

| Table 5 | Grain sieve analysis observations (BMS soil) |
|----------|---------------------------------------------|
| LS. Sieve | Wt. retained in each sieve (g) | % retained on each sieve | Cumulative % retained on each sieve | % Finer |
| Number or size in mm | | | | |
| 4.25 | 26 | 5.33 | 5.33 | 94.67 |
| 2 | 36 | 7.38 | 12.7 | 87.29 |
| 1.18 | 40 | 8.20 | 20.1 | 79.10 |
| 0.6 | 36 | 7.38 | 28.28 | 71.72 |
| 0.425 | 32 | 6.56 | 34.83 | 65.16 |
| 0.3 | 6 | 1.23 | 36.06 | 63.93 |
| 0.15 | 32 | 6.56 | 42.62 | 57.38 |
| 0.075 | 190 | 38.93 | 81.56 | 18.44 |
| Pan | 90 | 18.44 | 100 | 0 |

Fig. 7 The trend of grain size (mm) and % finer of both lake and BMS soils

3.4.2 Determining Moisture Content of the Soils

Initial moisture content is determined by oven drying the samples for one day and taking the weights of normal soil and oven-dried soil. Two samples for each type of soil are used for the test. The average moisture content for lake soil is 5.48% and the average moisture content of BMS soil is 2.61% (Table 7).

| Table 7 | Observations derived from moisture content experiment |
|----------|---------------------------------------------|
| S.No. | Sample | Lake (g) | BMS (g) |
| 1 | Weight of container with lid | 14 | 16 |
| 2 | Weight of container with lid + wet soil | 44 | 45.6 |
| 3 | Weight of container with lid + dry soil | 42.8 | 42.2 |
| 4 | Water/Moisture content | 4.17% | 6.78% |

3.4.3 Determining Specific Gravity of the Soils

Soil passing through a 4.75 mm IS sieve is used for the test. Specific gravity is necessary to calculate soil properties like void ratio, degree of saturation. Two samples of each type of soil are used to determine specific gravity. The average specific gravity of lake soil is 2.430 and the average specific gravity of BMS soil is 2.399 (Table 8).

| Table 8 | Observations of specific gravity experiment |
|----------|---------------------------------------------|
| S. No. | Observation Number | Lake (g) | BMS (g) |
| 1 | Weight of density bottle (Wg) | 74.62 | 56.27 |
| 2 | Weight of density bottle + dry soil (Wg) | 91.11 | 72.32 |
| 3 | Weight of bottle + dry soil + water at the temperature T°C (Wg) | 182.66 | 165.27 |
| 4 | Weight of bottle + water at the temperature T°C (Wg) | 172.9 | 156.07 |
| 5 | Specific Gravity G at T°C | 2.44 | 2.34 |

3.4.4 Determining Consistency Limits of the Soils

3.4.4.1 Liquid Limit

Table 9 provides the observations derived from the liquid limit experiment of both soils. Semi-log plot of moisture content (%) and number of blows in the liquid limit gives the moisture content of lake soil at 25 blows (Fig. 8).

Table 9 Observations from the Liquid limit experiment of both the soils

| Determination Number | Lake | BMS |
|----------------------|------|-----|
| Weight of container (g) | 206 | 202 |
| Weight of container + wet soil (g) | 356 | 360 |
| Weight of container + dry soil (g) | 326 | 330 |
| Weight of water (g) | 30 | 32 |
| Weight of dry soil (g) | 120 | 128 |
| Moisture content (%) | 25 | 25.35 |
| No. of blows | 17 | 25 |

Fig. 8 Semi-log graph plot between moisture content (%) and the number of blows in the liquid limit

The liquid limit is majorly used to know the stress history and general properties of soil. Two samples of each soil type are taken. The moisture content at which the groove formed by a standard tool into the sample of soil taken in the standard cup, closes for 10 mm on being given 25 blows is the Liquid limit. The liquid limit of lake soil is 23.71% and the liquid limit of BMS soil is 23.43%.
3.4.4.2 Plastic Limit

The plastic limit is the moisture content of the soil at which you can make long thin 3 mm diameter rolled soil. The soil is well kneaded and rolled until the thread crumbles. Two samples of each soil are used to determine the plastic limit. By the observations in Table 10, the plastic limit of lake soil is 26.51% and for BMS soil it is 13.69%.

### Table 10 Observations from the plastic limit experiment of both the soils

| Determination Number | Lake (g) | BMS (g) |
|----------------------|---------|---------|
|                      | 1       | 2       | 1      | 2      |
| Weight of container + lid, \(W_1\) | 202     | 202     | 202    | 204    |
| Weight of container + lid + wet sample, \(W_2\) | 285     | 233     | 233    | 232    |
| Weight of container + lid + dry sample, \(W_2\) | 268     | 224     | 230    | 228    |
| Weight of dry sample = \(W_2 - W_1\) | 66      | 22      | 28     | 24     |
| Weight of water in the soil = \(W_1 - W_2\) | 17      | 6       | 3      | 4      |
| Water content (%) = \((W_2 - W_1) / (W_2 - W_1)\) x 100 | 25.75%  | 27.27%  | 10.71% | 16.67% |

3.4.5 Determination of Coefficient of Permeability of Soils

The falling head method is used to determine the coefficient of permeability. Permeability is used to determine groundwater flow, seepage through dams, settlement of structures et cetera. The permeability of each soil sample is determined by letting water flow through the soil cylinder using a permeameter. The coefficient of permeability of lake soil is \(1.1769 \times 10^{-5}\) and that of BMS soil is \(7.705 \times 10^{-6}\) from the observations made in Table 11.

After testing the basic soil properties of the two soils collected from the campus, the soil samples are mixed with different quantities of water for permeability of lake soil is \(1.1769 \times 10^{-5}\) and for BMS soil it is \(7.705 \times 10^{-6}\) from the observations made in Table 11.

### Table 11 Observations from the permeability test of both the soils

| Failing head permeability test | Lake | BMS |
|-------------------------------|------|-----|
| Areas of standpipe (5 cm diameter) | a (cm) | 0.1963 | 0.1963 |
| Cross-sectional area of soil specimen | A (cm²) | 78539 | 78539 |
| Length of soil specimen | L (cm) | 12.8 | 12.8 |
| Initial reading of standpipe | h (cm) | 80 | 80 |
| Final reading of standpipe | h (cm) | 40 | 40 |
| Time | T (sec) | 195 | 187 |
| Coefficient of permeability at T (cm/sec) | k | 1.359 x 10⁻⁴ | 1.1845 x 10⁻⁴ |

3.4.6 Manual Method of Determining Volumetric Soil Shrinkage and Shrinkage Limit

By oven drying or by natural environment soil loses moisture and it changes from liquid state to plastic state, from plastic state to semi-solid state and then to solid-state. Volumetric changes also occur with varying moisture content. Shrinkage limit is the limit of moisture content at which any moisture change does not cause any more volume change [20]. Dicks of the fixed volume are used for the test. The formula used for shrinkage limit is

\[
\text{Shrinkage limit} = W - (V - V_0) \times (\gamma W_0) \times 100
\]

where, \(W = \text{Moisture content of wet soil pat (g)}\), \(V = \text{Volume of wet soil pat in cm}^3\), \(V_0 = \text{Volume of dry soil pat in cm}^3\), \(W_0 = \text{Weight of oven-dry soil pat in g}\).

The volume shrunk is calculated from \((V - V_0)\). The volume of dry pat is determined by the principle of Archimedes.

![Fig 10 Shrinkage volume with varying moisture content using both DIP and manual methods of BMS soil](image)

### Fig. 10 Shrinkage volume with varying moisture content using both DIP and manual methods of BMS soil

### Fig. 11 Shrinkage volume with varying moisture content using both DIP and manual methods of lake soil

![Fig 12 The chronological order of pictures of lake soil leading to soil shrinkage](image)

![Fig 9 Stepwise proceedings of the algorithm to find the shrinkage of soil](image)

The RGB image is read and converted into a greyscale image and global threshold level is found to convert the intensity image to a binary image. Using the level found, binary image is extracted. Holes and other disturbances are removed and object in the binary image is separated from its background. Scale is found automatically as the disk used for soil sample is the same for all with fixed diameter (45 mm). The shrunk part is detected and the area of it is derived in pixels and this is converted to mm² using the found scale factor.
varying moisture content for both soils. An error of more than 10% is observed and a trend of increasing soil shrinkage with increasing moisture content is observed. This process is more accurate at finding properties of multiple aggregates over soil shrinkage. The properties found by Digital Image Processing (DIP) method are reasonably agreeable for multiple aggregates and minor percentage differences in the soil shrinkage results. It could be concluded that DIP is a non-destructive, economical, easy to use reliable method to compute the properties of civil engineering materials.

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