Magnetovolume effects in manganese nitrides with antiperovskite structure

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Abstract
Magnetostuctural correlations in antiperovskite manganese nitrides were investigated systematically for stoichiometric and solid solution Mn₃Cu₁₋ₓAxN (A = Co, Ni, Zn, Ga, Ge, Rh, Pd, Ag, In, Sn or Sb). This class of nitrides is attracting great attention because of their giant negative thermal expansion, which is achieved by doping Ge or Sn into the A site as a relaxant of the sharp volume contraction on heating (spontaneous volume magnetostriction ωs) because of the magnetovolume effects. The physical background of large ωs and mechanism of how the volume contraction becomes gradual with temperature are central concerns for the physics and applications of these nitrides. An entire dataset of thermal expansion, crystal structure and magnetization demonstrates that the cubic triangular antiferromagnetic state is crucial for large ωs. The intimate relationship between ωs and the magnetic structure is discussed in terms of geometrical frustration related to the Mn₆N octahedron and magnetic stress concept. The results presented herein also show that ωs depends on the number of d electrons in the A atom, suggesting the important role of the d orbitals of the A atom. Not all the dopants in the A site, but the elements that disturb the cubic triangular antiferromagnetic state, are effective in broadening the volume change. This fact suggests that instability neighboring the phase boundary is related to the broadening. The relation between the gradual volume change and the local structure anomaly is suggested by recent microprobe studies.

Keywords: magnetovolume effect, magnetism, frustration, antiperovskite, negative thermal expansion

1. Introduction
An antiperovskite compound with the formula M₃AX (M, transitional metal; A, metal or semiconducting element and X, interstitial light element) is a treasury of functionalities. Various beneficial properties including magnetovolume effects [1, 2], magnetostriction [3, 4], magnetocaloric effects [5, 6], magnetoresistance [7, 8], low-temperature coefficient of resistance [9–11], superconductivity [12, 13] and functional mechanical properties [14, 15] have been obtained in antiperovskites. The wide diversity of physical properties of antiperovskites reflects an equally wide range of chemical-bonding interactions consisting of the d orbital in M and the p orbital in X. Intermetallic compounds containing ordered interstitial light elements, as typified by antiperovskites, form a major class of materials that have different physical backgrounds and different parameters from those of oxides. Their value as a reservoir of smart materials becomes still higher.

Among these compounds, antiperovskite manganese nitrides Mn₃AN characterized by their peculiar magnetovectorial correlations exhibit giant negative thermal expansion (NTE) [16–19]. The coefficient of linear thermal expansion α is over −30 ppm K⁻¹ for Mn₃AN, which is more...
than ten times as large as that of the NTE materials known before the discovery of this compound. This gigantic, isotropic and non-hysteretic NTE attracts great interest from practical and fundamental viewpoints. The NTE of the manganese antiperovskites was achieved by broadening the sharp volume contraction upon heating from low-temperature (low-T) large-lattice antiferromagnetic (AF) to high-T small-lattice paramagnetic (PM) phases using partial replacement of constituent elements. Such control of electronic phase change is now a key paradigm for the development of smart materials [20].

The gigantic NTE of Mn$_3$AN strongly affected NTE research, leading to the discovery of many NTE materials such as Cd(CN)$_2$CCl$_4$ [21], ReO$_3$ [22], ScF$_3$ [23], ZnF$_2$ [24], SrCu$_2$Fe$_2$O$_{12}$ [25], (Bi, La)NiO$_3$ [26] and La(Fe, Si, Co)$_{13}$ [27]. Particularly, NTE of SrCu$_2$Fe$_2$O$_{12}$, (Bi, La)NiO$_3$ and La(Fe, Si, Co)$_{13}$ is achieved using phase control similar to Mn$_3$AN. It is noteworthy that $\alpha$ reaches $-80$ ppm K$^{-1}$ in (Bi, La)NiO$_3$. In addition, Ca$_2$Ru$_{1-x}$Cr$_x$O$_4$ [28] was discovered as one NTE material realized by phase control, in which ordering of orbitals as well as spins is relevant to the NTE [29].

Unresolved problems related to the giant NTE in Mn$_3$AN are the origin of the large volume change associated with the magnetic phase transition, defined as spontaneous volume magnetostriction $\omega_s$, and the mechanism of how this volume change becomes gradual with $T$. They reflect the peculiar electronic states of Mn$_3$AN and the central issues to elucidate the physics of the magnetostructural correlations in this class of nitrides. Furthermore, they are dominant factors for the practical functionalities of NTE. Therefore, understanding them is desired as a scientific basis for improvement and control of NTE properties.

This report describes systematic explorations of the magnetism and the crystal structure for stoichiometric and solid solution Mn$_3$Cu$_{1-x}$A$_x$N (A = Co, Ni, Zn, Ga, Ge, Rh, Pd, Ag, In, Sn or Sb), including typical NTE compositions. Here, we summarize the compositional requirements for large $\alpha_s$ and gradual volume change with $T$, and discuss their physical background.

### 2. Experimental procedures

All measurements were taken using sintered polycrystalline samples [30]. First we obtained Mn$_3$AN using a solid-state reaction. Powders of Mn$_3$N and pure element A (purity: 99.9% or higher), in total about 2 g, were mixed in a bag filled with nitrogen gas and then sealed in a quartz tube (9 mm diameter and 20 cm long) under vacuum ($<10^{-2}$ Torr). The sealed quartz tube was heated at 500–760°C for 40–70 h. To obtain the solid solution, we mixed powders of the stoichiometric antiperovskites in an appropriate molar ratio, pressed it into a pellet and sealed it in a quartz tube under vacuum. The final sintering was conducted at 800°C for 60 h. The crystal structure was investigated by powder x-ray diffraction (XRD). The nitrogen deficiency $\delta$ was confirmed by the method of thermal conductivity detection of the emitted gas. Here, we define $\delta$ as the general formula Mn$_3$AN$_{1-\delta}$. The results of $\delta$ measurements are presented in tables 1, 2, 4 and 5. In the text, we use the notation Mn$_3$AN for simplicity. The term ‘stoichiometric’ means in this paper that the A site is occupied by a single element, and does not mean $\delta = 0$.

Linear thermal expansion $\Delta L(T)/L$ was measured using a strain gage (types KFL and KFH; Kyowa Electronic Instruments Co. Ltd) at temperatures of 4–500 K. This method is simple but requires a material having a known degree of expansion. We used copper (purity: 99.99%) and the corresponding thermal expansion data of pure copper [31, 32]. Measurements of $\Delta L/L$ were partly conducted using a laser-interference dilatometer. The $T$ dependence of the lattice constant obtained from XRD data was reported for $A$ = Ni [33], Cu [9], Zn [34], Ga [35] and Ag [36]. Our $\Delta L/L$ data for stoichiometric Mn$_3$AN are in quantitative agreement with the previous XRD data presented above, thereby validating our thermal expansion measurements. Temperature-dependent magnetization $M(T)$ was measured at 5000 Oe using a superconducting quantum interference device magnetometer.

### 3. Results

#### 3.1. Stoichiometric Mn$_3$AN

Results for stoichiometric Mn$_3$AN are presented in tables 1 and 2. The previously reported crystal structure and lattice parameters of the stoichiometric Mn$_3$AX [2, 9, 33–51] are listed in table 3. The inset of figure 2(b) shows a crystal structure of an antiperovskite Mn$_3$AX.

Figure 1 displays $\Delta L/L$ measured for Mn$_3$Cu$_{1-x}$A$_x$N for eight dopants $A$ = Co, Ni, Zn, Ga, Rh, Pd, Ag and In. Each of the eight elements forms the stoichiometric Mn$_3$AN
Table 2. Physical properties of antiperovskite manganese nitrides Mn$_3$AN$_{1-x}$ without magnetovolume effects: C, cubic; T$_i$ and T$_t$, tetragonal and $a^*$ represents the cubic root of the pseudo-cubic-cell volume.

| Mn$_3$AN$_{1-x}$ | $1 - \delta$ | Temperature (K) | Lattice constant (Å) |
|-----------------|-------------|-----------------|---------------------|
| Cu              | 0.95        | PM, C           | $T_1^*$             |
| Ge              | 0.75        | PM, C           | $T_2^*$             |
| Sn              | 0.76        | PM, C           | $T_3^*$             |
| Sb              | 0.91        | PM, C           | $T_4^*$             |

Table 3. Literature review of lattice constants at ambient temperature for Mn$_3$AN. Data for carbide counterpart Mn$_3$AN$_{1-x}$ are also listed for comparison: C, cubic and T$_i$ and T$_t$, tetragonal.

| Mn$_3$AN      | Structure | Lattice constant (Å) | References |
|---------------|-----------|----------------------|------------|
| Al            | C         | $a = 3.8545$         | [48]       |
| Mn            | C         | $a = 3.872$          | [39]       |
| Ni            | C         | $a = 3.886$          | [33]       |
| Cu            | C         | $a = 3.906$          | [37]       |
| Zn            | C         | $a = 3.902$          | [42]       |
| Ga            | C         | $a = 3.8951$         | [34]       |
| Ge            | $T_1^*$   | $a = 3.9008$         | [49]       |
| As            | $T_4^*$   | $a = 5.782$, $c = 8.370$ | [41]       |
| Rh            | C         | $a = 3.9280$         | [38]       |
| Pd            | C         | $a = 3.9796$         | [38]       |
| Ag            | C         | $a = 4.0195$         | [37]       |
| In            | C         | $a = 4.0291$         | [38]       |
| Sn            | C         | $a = 4.0585$         | [43]       |
| Sb            | $T_1^*$   | $a = 4.181$, $c = 4.280$ | [41]       |
| Pt            | C         | $a = 3.9685$         | [38]       |
| Au            | C         | $a = 3.972$          | [44]       |
| Hg            | C         | $a = 4.0235$         | [38]       |
| Mn$_3$ZnC     | C         | $a = 3.930$          | [2]        |
| Mn$_3$GaC     | C         | $a = 3.896$          | [39]       |
| Mn$_3$SnC     | C         | $a = 3.894$          | [2]        |

The eight stoichiometric cubic Mn$_3$AN compounds presented in figure 1, respectively, exhibit anomalies in $\Delta L/L$ at $T^*$ and contract upon heating. For quantitative evaluation of the magnetovolume effects, we estimate the magnetic contribution to the volume, i.e. spontaneous volume magnetostriction $\omega_s$, defined as the difference between the hypothetical phononic thermal expansion ($\Delta L/L)_{pb}$ and the measured thermal expansion. As presented in figure 1, $\Delta L/L$ of Mn$_3$Cu$_{1-x}$A$_x$N at the PM phase is apparently universal irrespective of $x$. Consequently, the hypothetical phononic expansion is determined by extrapolating this envelope using the following equation of the lattice constant $a$ at $T$ due to the anharmonic phonon [52]:

$$a(T) = a_0 \left[ 1 + \frac{k_B r}{V_0} T \varphi(\theta_B/T) \right]$$  \hspace{1cm} (1)$$

(\varphi, Thacher's approximate function [53]; $a_0$, the lattice constant at absolute zero temperature; $V_0$, the volume of the unit cell at absolute zero temperature; $r$, the number of atoms in the unit cell; $K$, the bulk modulus; $\theta_B$, the Debye temperature; $\gamma$, the Grüneisen parameter and $k_B$, the Boltzmann constant). Because the cubic crystal structure is maintained over the $T$ range, we assume that $V = a^3$. Based on the previous results on the Young modulus of that exhibits magnetovolume effects in the cubic AF ground state. Cadmium, which is also categorized in the same group, is omitted from the present study. Figure 2 displays $\Delta L/L$ of typical NTE compounds Mn$_3$Cu$_{1-x}$A$_x$N with A = Ge and Sn. A comparison with the magnetization $M(T)$ depicted in figure 3 shows that the anomaly temperature in $\Delta L/L$, $T^*$, corresponds to the magnetic transition temperature (the Curie temperature $T_C$ for the ferromagnetic (FM) transition; the Neel temperature $T_N$ for the AF transition).
Figure 1. Linear thermal expansion $\Delta(T)/L$ of Mn$_3$Cu$_{1-x}$A$_x$N for $x = 0$ (black), 0.1 (red), 0.15 (orange), 0.3 (green), 0.5 (light blue), 0.7 (blue) and 1 (magenta): A = Co (a), Ni (b), Zn (c), Ga (d), Rh (e), Pd (f), Ag (g) and In (h).

Figure 2. Linear thermal expansion $\Delta(T)/L$ of Mn$_3$Cu$_{1-x}$A$_x$N: A = Ge (a) and Sn (b). The inset in (a) shows the (111) peak of XRD for $x = 0.5$. The inset in (b) shows the crystal structure of an antiperovskite M$_3$AX.

For a cubic system, $\omega_s$ is defined as $3[\Delta L/L - (\Delta L/L)_ph]$. The obtained $\omega_s$ values are presented in figure 5 and table 1. For Mn$_3$GeN and Mn$_3$SnN, we do not obtain finite values of $\omega_s$. We infer that they are zero. Furthermore, for Mn$_3$CuN (figure 4), $\omega_s$ is negligibly small ($\omega_s$ is less than $0.44 \times 10^{-3}$). However, slight dopants, typically $x \sim 0.1$, produce large $\omega_s$. Therefore, we plot in figure 5 the value for A = Cu$_{0.85}$Ge$_{0.15}$ and $\omega_s = 12.59 \times 10^{-3}$, as a potential $\omega_s$ of Mn$_3$CuN (see table 4). The presented result clearly exhibits a good agreement between $\omega_s$ and the number of d electrons in the A atom. $\omega_s$ is larger for the 3d series than for the 4d series. It increases concomitantly with increasing atomic number in the same series. For Mn$_3$ZnN and Mn$_3$GaN, $\omega_s$ becomes prominently large, more than twice the size of the second

the antiperovskites [54], we fixed $K$ at 130 GPa. For an antiperovskite structure, $r$ is five. Consequently, the fitting parameters were reduced to three in the present analysis:

$\alpha_0$, $\gamma$ and $\theta_D$. The obtained parameters are listed in table 1. The result for Mn$_3$CuN is portrayed in figure 4. These fitting parameters are physically reasonable because they are comparable to those of typical transition metal-based intermetallic compounds [55–57]. For $A = Ni$, it might be difficult to define the envelope because $\Delta L/L$ in the PM phase varies according to $x$. If we estimate $\Delta L/L_{ph}$ by extrapolating the measured $\Delta L/L$ at the PM phase of Mn$_3$NiN, then we would obtain an unphysically large Debye temperature ($\alpha_0 = 3.883 \text{Å}$, $\gamma = 3.23$ and $\theta_D = 1441 \text{K}$). However, $\Delta L/L$ at the PM phase is apparently universal for $x = 0.1–0.5$. We estimated $\Delta L/L_{ph}$ for Mn$_3$NiN using this common part of $\Delta L/L$ for $x = 0.1–0.5$, instead of the measured Mn$_3$NiN data. In this analysis, the fitting parameters are in the reasonable range ($\alpha_0 = 3.875 \text{Å}$, $\gamma = 2.11$ and $\theta_D = 525.9 \text{K}$). Assuming this $\Delta L/L_{ph}$, $\omega_s$ does not disappear even at the PM phase for Mn$_3$NiN. Empirically, the finite $\omega_s$ originates from the rather weak $T$ dependent $\Delta L/L$ of Mn$_3$NiN at the PM phase. This flat $\Delta L/L$ is also the origin of an unphysically large $\theta_D$ in the fitting analysis of $\Delta L/L_{ph}$. The finite $\omega_s$ suggests spin fluctuations at the PM phase [58].
Figure 3. Temperature-dependent magnetization $M(T)$ of stoichiometric Mn$_3$AN measured during a cooling process in an applied field of 5 kOe: (a) A = Ni, Zn, Ga, Pd and Ag; (b) A = Co, Rh, Ag and In and (c) A = Cu, Ge, Sn and Sb. The inset in (c) shows magnified magnetization for A = Ge and Sn at the high-temperature region of $T = 300$–700 K.

Figure 4. Linear thermal expansion $\Delta L/L$ of Mn$_3$CuN (open circle) and the ideal lattice thermal expansion determined by fitting analysis using equation (1) (red line). The fitting parameters are $a_0 = 3.891$ Å, $T_0 = 320.3$ K and $\gamma = 2.33$.

Figure 5. Spontaneous volume magnetostriction $\omega_s$ for stoichiometric Mn$_3$AN at 10 K. For A = Cu, the value of Mn$_3$Cu$_{0.85}$Ge$_{0.15}$N is shown as a representative value of potential $\omega_s$ because Mn$_3$Cu$_{0.85}$N-based antiperovskites exhibit pronounced $\omega_s$ when the cubic triangular AF state is recovered by slight dopants on the A site.

3.2. Solid solution Mn$_3$Cu$_{1-x}$A$_x$N

The results are presented in tables 4 ($x = 0.15$) and 5 ($x = 0.5$). The giant NTE of the antiperovskites was first discovered in the Mn$_3$Cu$_{1-x}$Ge$_x$N solid solution. Surprisingly, neither end material Mn$_3$CuN nor Mn$_3$GeN exhibits magnetovolume effects or NTE. The drastic change in physical properties of Mn$_3$Cu$_{1-x}$Ge$_x$N exemplifies the diverse physical properties of Mn$_3$AN.

First, we examine the doping effects of two representative dopants: Ge and Sn. The linear thermal expansion and the magnetization are shown, respectively, in figures 2 and 6. Doping effects of Ge and Sn are fundamentally the same. The sequence starting from the low-doping level is the following: deformation, possesses different magnetic structure and does not exhibit magnetovolume effects (table 2). The structural deformation is interpreted as a consequence of the band Jahn–Teller effects. The band filling varies according to $n_v$. At both ends of small and large $n_v$, its condition is satisfied, i.e. the Fermi level approaches singularity in the density of states.

largest group. A = In, Ni or Ag. In previous arguments, the number of valence (outer s and p) electrons in A, $n_v$, was regarded as the dominant factor for the electronic states, based on the clear relationship between $T^*$ and $n_v$ [1]. However, $\omega_s$ is unrelated to $T^*$. Therefore, it is unrelated to $n_v$ in the presented results. In terms of the electronic structure, this fact implies that $\omega_s$ increases as the $d$ level of the A atom moves away from the Fermi level, suggesting an important role of the $d$ level of the A atom, although it has been disregarded to date.

From the viewpoint of $n_v$, the cubic AF phase showing the magnetovolume effects appears for $n_v = 2$ and 3. When $n_v$ becomes smaller ($n_v = 1$: A = Cu) or larger ($n_v = 4$: A = Ge, Sn; $n_v = 5$: A = As, Sb), the system undergoes structural
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Temperature-dependent XRD measurements were conducted
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similar to that of the Ge- or Sn-doped compounds, except

Ni and Pd) states. The XRD patterns are portrayed in figure 7 for A = Ge (a), Ga (b), Ag (c) and Ni (d) as representatives. Here, the contribution from the \( K_\omega \) was subtracted. For A = Ge, the (200) peak keeps a single component down to the lowest temperature, implying the cubic structure over a whole T range. For A = Ga, the (200) peak is a single component at 300 K, but it splits into two parts at 10 K. The intensity ratio of the lower-angle peak to that of the higher-angle one is 2:1. Therefore, the lower and higher peaks are assigned, respectively, to (200) and (002) in the tetragonal notation. The cubic unit cell is deformed into the tetragonal one with the shorter c-axis, namely \( T_1^- \), which is the same as Mn

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Figure 6. Inverse susceptibility $\chi^{-1}(T)$ of Mn$_3$Cu$_{1-x}$A$_x$N measured during a cooling process in an applied field of 5 kOe. A = Ge (a) and Sn (b).

including phase-separated ones, although it is at its largest $2.66 \times 10^{-3}$ for A = Zn and becomes much smaller for A = Ga and Ag, where the lattice is tetragonally distorted. For A = Ag, however, $\omega_s$ becomes large ($10.51 \times 10^{-3}$) in the cubic intermediate state ($70 < T < 145$ K), although it is small ($1.88 \times 10^{-3}$) in the $T_{\text{c}}$ ground state. The presented result on A = Ga is in agreement with the previous result [43].

Even though 15% doping is small for magnetovolume effects, such as A = Ga or Zn, further doping achieves the cubic AF state showing magnetovolume effects. This is nicely presented in the series of Mn$_3$Cu$_{0.85}$A$_{0.15}$N (table 5). The experiments here reveal that all the systems listed in table 5 maintain a cubic structure over the whole $T$ range and possess the AF ordered state. $\omega_s$ is ($7.82-14.90) \times 10^{-3}$. An important difference is not the magnitude of volume change $\omega_s$, but the temperature window $\Delta T$ in which the volume gradually contracts on heating. The broadening of the volume change that causes NTE at room temperature does not appear for all dopants. In this study, broadening is remarkable in the order of A = Ge ($\Delta T = 85$ K), Co (46 K), Sn (36 K) and Pd (30 K). For the other dopants, broadening is limited and the volume change remains sharp. Particularly, $\Delta T$ is less than 1 K for A = Zn and Ga. Such a sharp volume change is a characteristic feature of the end materials Mn$_3$ZnN and Mn$_3$GaN. The difference in atomic size between Cu and the dopant A is unrelated to the broadening.

Figure 7. Temperature dependence of XRD profiles of Mn$_3$Cu$_{0.85}$A$_{0.15}$N: A = Ge (a), Ga (b), Ag (c) and Ni (d).
4. Discussion

4.1. Physical background of magnetovolume effects

4.1.1. Requisites for large $\omega_s$. From the results, we might conclude that the cubic crystal structure is a requisite for large $\omega_s$ in Mn$_3$NiN. In addition, the AF state, particularly, the triangular ($\Gamma^5s$ and $\Gamma^4s$) magnetic structure, is apparently required for large $\omega_s$. Although the dc magnetization measurements do not provide us with information related to the magnetic structure, this study shows that large $\omega_s$ is incompatible with FM states. A comparison between the previous neutron diffraction study and the presented results offers direct evidence for the relation between the triangular AF structure and the large $\omega_s$.

The stoichiometric compounds, Mn$_3$NiN, Mn$_3$ZnN and Mn$_3$GaN, which were confirmed to have the triangular AF configuration by neutron diffraction study [1], exhibit a large $\omega_s$ in this study, $8.18 \times 10^{-3}$, $20.44 \times 10^{-3}$ and $19.10 \times 10^{-3}$, respectively. However, for Mn$_3$RhN, which is confirmed to have a different AF configuration by the neutron study [1], $\omega_s$ is small ($2.07 \times 10^{-3}$). The neutron study [1] also indicates that the $\Gamma^5s$ AF structure is realized just below $T_s$ in Mn$_3$AgN, but the $\Gamma^4s$ FM component is developed as $T$ decreases. The small $\omega_s$ of Mn$_3$AgN at 10 K ($5.79 \times 10^{-3}$) might be partly explained by this mixing of the FM components.

A recent neutron study [60] revealed good agreement between the $\Gamma^5s$ AF structure and the appearance of $\omega_s$ for the solid solution Mn$_{1-x}$Cu$_{1-x}$Ge$_x$N. In addition, the $\Gamma^4s$ AF state with large $\omega_s$ of Mn$_3$GaN is found to be unstable against slight Fe dopants on the Mn site. Moreover, the FM state is induced at lower temperatures [61]. Impressively, the $\omega_s$ disappears at the impurity-induced FM state. The detailed magnetic structure is yet to be confirmed.

An exception is Mn$_3$SnN. An earlier neutron study [1] revealed that it possesses the cubic $\Gamma^5s$ AF state at $237<T<357$ K, although no magnetovolume effects are confirmed in previous [46] studies or the present study. It must be considered that Mn$_3$SnN easily loses nitrogen ($1-\delta=0.76$ in this study). The nitrogen deficiency drastically alters the physical properties of this class of nitrides [62]. Indeed, the physical properties of Mn$_3$SnN studied here differs from those of the previous one [1]: the former undergoes two successive transitions at 550 and 45 K (figure 3(c)), whereas the latter undergoes four transitions at 475, 357, 237 and 186 K.

These arguments enable us to predict the low-$T$ crystal structure of Mn$_3$Cu$_{0.85}$Rh$_{0.15}$N and Mn$_3$Cu$_{0.85}$In$_{0.15}$N, which were not measured in this study. Rather, the large $\omega_s$, estimated as $7.89 \times 10^{-3}$ and $10.99 \times 10^{-3}$ for the Rh- and In-doped compounds, respectively, predicts the cubic crystal structure for these solid solutions.

4.1.2. Frustration. An intimate relation between the triangular AF structure and the large $\omega_s$ suggests that geometrical frustration plays a role in the magnetovolume effects. An Mn$_4$N octahedron has three-dimensional geometrical frustration because the nearest-neighbor (Mn–Mn) magnetic interaction $J_1$ is AF [63]. As a result, non-collinear long-range order such as $\Gamma^5s$ or $\Gamma^4s$ AF structure is stabilized, keeping the cubic structure only by a very narrow margin of energy with the assistance of the strong FM next-nearest-neighbor interaction $J_2$ [40]. The pronounced magnetovolume effects in the cubic triangular AF phase imply that lattice expansion with cubic symmetry brings larger energy gain than removal of degeneracy by lattice deformation. An idea incorporating the frustration into the magnetovolume effects is that the strong frustration might assist lattice contraction at the PM state because the volume contraction increases the bandwidth and hence reduces the electronic energy. This is energetically favorable, although the amplitude of a magnetic moment is decreased, when the short-range magnetic ordering, or spin fluctuation, is suppressed by the strong frustration.

This study produces a result supporting the idea presented above. Figure 8 displays the $x$ dependence of the lattice parameter deduced from XRD and thermal expansion measurements. As presented in figure 8(a), Vegard’s law is not fulfilled for Mn$_3$Cu$_{1-x}$Ge$_x$N. The deviation from Vegard’s law at 10 K is reasonably ascribed to the large $\omega_s$. At this temperature, the lattice parameter is fairly scaled to $\Delta L/L$. That is, it increases suddenly at $x \sim 0.1$ and possesses a broad peak around $x = 0.5$. Then, it decreases slowly with increasing $x$. What is important is the deviation from Vegard’s law at 500 K, at which the magnetovolume effects cannot be confirmed. Figure 8(b) shows the lattice constant at 500 K, 400 K, and 295 K for Mn$_3$Cu$_{1-x}$In$_x$N. The short-range magnetic ordering, or spin fluctuation, is suppressed by the strong frustration.

Figure 8. Deviation from Vegard’s law in the lattice constant of solid solutions Mn$_3$Cu$_{1-x}$A$_x$N: A = Ge (a) and Sn (b).
500 K (figure 8(b)), although it is less clear because the atomic size of Sn is much greater than that of Cu. The large \( \omega_s \) might be partly attributable to the small volume at the PM state because of the frustration. A similar effect might play an important role also for the huge \( \omega_s \) up to 5% in YMn\(_2\) [64], in which strong frustration is regarded as suppressing spin fluctuations and hence the volume immediately above \( T_N \). We refer to an important difference: \( T_N \) of NTE manganese nitrides (\( \sim 300 \) K or higher) is much higher than that of YMn\(_2\) (\( \sim 100 \) K).

### 4.1.3. Magnetic structure.

The magnetovolume effect is a change in volume attributable to a variation in the amplitude of the magnetic moment \( m \) in a magnetic metal. It was first discovered in Ni–Fe Invar, showing low thermal expansion of \( \alpha = 0.5 - 1 \) ppm K\(^{-1} \) below \( T_C = 500 \) K [65]. It appears as a huge volume change up to 5% in YMn\(_2\) [64] as described above. A general explanation of NTE caused by the magnetovolume effect is that a larger volume favors the appearance of a magnetic moment in a metal. The electronic theory of solids provides a microscopic picture: an increase in volume suppresses the overlap of electronic orbitals and therefore reduces the electronic bandwidth. Narrowing of the bandwidth can increase the density of states \( \rho(\varepsilon) \) at Fermi energy \( \varepsilon_F \), which favors magnetism. The magnetovolume effect is related directly to a longstanding problem, the origin of magnetism in a metal, and has long been regarded as a fundamental topic of physics\(^3\) [66, 67].

Magnetovolume effects are formulated in terms of itinerant-electron magnetism, or the Stoner–Edwards–Wohlfarth concept [68], ascribed to singularity in \( \rho(\varepsilon) \). In this framework, \( \omega_s \) is related to the amplitude of the magnetic moment \( m \) in a manner: \( \omega_s = C_{mv} m^2 / K \). Here, \( C_{mv} \) is the magnetovolume coupling constant. In the spin fluctuation theory [69], this relationship is modified as \( \omega_s = C_{mv} \varepsilon_F^2 \) (\( \varepsilon_F \): the amplitude of spin fluctuations). In these frameworks, the physics related to the magnetic structure would be incorporated via the coupling constant \( C_{mv} \). However, magnetovolume effects related to the magnetic structure are apparently not fully discussed in the framework explained above.

In an itinerant-electron magnet, the magnetic and electronic structures are intimately related. Therefore, \( \omega_s \) is naively related to the magnetic structure. However, the physics of the electronic structure is too rich to incorporate only through the unique constant \( C_{mv} \) or singularity in \( \varepsilon_F \). One attempt to take the physics omitted from the arguments presented above into consideration is the concept of magnetic stress [70]. Magnetic stress is related to the strain tensor derivative of the energy exchange interaction parameter \( J \), which determines the magnetic structure. In fact, \( J \) and its strain tensor derivative depend strongly on the origin of the magnetic interactions, and consequently on the distance between the sites. They provide us with information related to the anisotropy or strains. We can also examine volume effects by considering the trace of the stress tensor.

For CrN [70], the nearest-neighbor AF Cr–Cr coupling \( J_1 \) is mediated by direct \( t_{2g} \) orbital interactions. The shorter atomic distance enhances overlapping of the orbitals. Therefore, the magnitude of \( J_1 \) becomes larger. In that case, the AF nearest-neighbor Cr–Cr bonds tend to decrease, although the FM nearest-neighbor Cr–Cr bonds tend to increase. This scheme explains the observed AF ordering and lattice distortion in CrN at \( T_N \) to an excellent degree. Consequently, the magnetostuctural correlations of the antiperovskites also might be discussed comprehensively using the magnetic-stress concept.

### 4.2. Mechanism of broadening in volume change

Chemical disorder is not a primary cause for broadening of the volume change. The XRD measurement of typical broadened composition Mn\(_3\)Cu\(_0\)Ge\(_3\)Sn\(_3\)N (the inset of figure 2(a)) clearly contra-indicates compositional inhomogeneity: the width of the (111) peak does not widen in the operating temperature window of NTE, compared with that above and below it. Moreover, the neutron and NMR measurements [71] reveal that the volume expands as the \( \Gamma^5 \) AF ordered moment gradually develops. Instead, the broadening seems to result from dopants that disturb the cubic triangular AF state because Mn\(_3\)Ge\(_3\)N and Mn\(_3\)Sn\(_3\)N have different electronic states from it [72].

No data presented here contradict the assumption that disturbance to the cubic triangular AF state is relevant to the broadening of the volume change. Because we know the detailed magnetic structure of seven stoichiometric Mn\(_3\)AN (\( A = \) Ni, Zn, Ga, Ge, Rh, Ag and Sn) [1], we first examine these seven dopants. The ground state of Mn\(_3\)AN (\( A = \) Ni, Zn, Ga or Ag) was confirmed to be the cubic triangular AF state, showing remarkable magnetovolume effects. Actually, Mn\(_3\)AgN is weak FM at low temperatures, but it clearly shows a peak in the \( M(T) \) curve (figure 3(a)) and \( T_N \) is definable. This weak FM behavior is ascribed to the mixing of the \( \Gamma^4 \) FM component. However, the ground state of Mn\(_3\)AN (\( A = \) Ge, Rh or Sn) has different magnetic structures from the triangular AF. This study demonstrates that the former four dopants do not induce remarkable broadening of the volume change, although the latter three dopants induce broadening.

Indium also does not induce broadening. For Mn\(_3\)InN, we have no information related to the magnetic structure, but this study confirmed that the crystal structure is cubic and the magnetic state is suggested to be weak FM, similar to Mn\(_3\)AgN, which are consistent with a recent report [50]. Therefore, Mn\(_3\)InN might have the ground state of the triangular AF structure. However, Co and Pd induce broadening of the volume change. Results of this study confirmed that Mn\(_3\)CoN and Mn\(_3\)PdN have a cubic structure and AF magnetic properties. Although the magnetic structures

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\(^3\) For a review see [66].

\(^4\) Of course, also in the antiperovskites, chemical inhomogeneity can induce the coexistence of larger-volume and smaller-volume regions and be the origin of broadened volume change, which is realized in the case of a huge NTE material (Bi, La)\(_2\)NO\(_3\) [26]. Nevertheless, what is important is that even without such inhomogeneity, the volume change becomes broadened in the antiperovskites.
of Mn$_2$CoN and Mn$_2$PdN are yet to be confirmed, this study predicts that they have no triangular AF structure.

For Mn$_2$Cu$_{1-x}$Ge$_x$N and Mn$_2$Cu$_{1-x}$Sn$_x$N, the cubic triangular AF states spread over a large area up to $x \sim 0.9$. The volume change is gradual as $T$ from $x \sim 0.4$ to this boundary. The broadening of volume change near the phase boundary suggests that a kind of phase instability plays an important role in this broadening. It is interesting and suggestive that Ni–Fe Invar showing anomaly in thermal expansion lies near the fcc–bce boundary in the Ni–Fe phase diagram [66]. Microscopic probes such as pair-distribution-function analysis of the neutron diffraction [73], x-ray absorption fine structure [74] and electron microscope observation [75] indicate that local structure anomaly is relevant to the broadening of the volume change in the antiperovskites. The relation to phase instability is yet to be explored.

5. Concluding remarks

We performed systematic explorations of the crystal structure and magnetism of stoichiometric and solid-solution Mn$_2$Cu$_{1-x}$A$_x$N (A = Co, Ni, Zn, Ga, Ge, Rh, Pd, Ag, In, Sn or Sb), particularly addressing the origin of pronounced spontaneous volume magnetostriction $\omega_s$ and the mechanism of broadening of the volume change.

An entire set of linear thermal expansion data enables us to evaluate the magnetic contribution to the thermal expansion, $\omega_s$. The results demonstrate that $\omega_s$ depends highly on crystal and magnetic structures. Particularly, the cubic triangular AF state is apparently a prerequisite for large $\omega_s$. In addition, $\omega_s$ was found to depend on the number of $d$ electrons in A, suggesting an important role of the $d$ orbitals of the A atom. Based on these results, we discussed the effects of the geometrical frustration related to the Mn$_n$N octahedron and a concept of magnetic stress.

Not all dopants in the A site, but the elements that disturb the cubic triangular AF state, are effective in broadening the volume change. The results suggest that chemical disorder is not a primary cause for the broadening, but that a kind of instability in structural and/or magnetic states is related to the broadening. As an important issue for future study, we refer to the relation between local structure anomaly and broadening of the volume change.

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