SPECTROSCOPY OF BROAD-LINE BLAZARS FROM 1LAC

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1. INTRODUCTION

The Fermi Gamma-Ray Space Telescope was launched on 2008 June 11. Its primary instrument is the Large Area Telescope (LAT; Atwood et al. 2009). Fermi generally operates in sky survey mode, observing the entire sky every 3 hr, and providing approximately uniform sky coverage on timescales of days to years.

The Fermi–LAT First Source Catalog (1FGL; Abdo et al. 2010b) catalogs the 1451 most significant sources detected in Fermi’s first year of operation. Based on the 1FGL catalog, the first catalog of active galactic nuclei (AGNs) detected by Fermi–LAT (1LAC; Abdo et al. 2010a) is the largest radio-γ-selected sample of blazars to date, associating 671 γ-ray sources to 709 AGNs (some may be unresolved composites) in the high-latitude sample.

Our quest is to optically characterize these sources, seeking maximum completeness in spectroscopic identifications and using the spectra to constrain the properties of these AGNs. Optically, the Fermi sources are evenly split between flat spectrum radio quasars (FSRQs) and BL Lac (BL Lac) objects. In this paper, we focus on the FSRQs. A companion paper (M. S. Shaw et al., in preparation) addresses the BL Lac objects.

In Section 2, we discuss the observational program and the data reduction pipeline. In Section 3, we describe the measurements and derived data products. In Section 4, we measure the continuum emission and non-thermal pollution. In Section 5, we estimate the black hole (BH) masses and Eddington ratio of the Fermi FSRQs. In Section 6, we discuss the orientation and shape of the broad-line regions (BLRs) in this population, and in Section 7, we relate this data set to ongoing radio monitoring of these AGNs.

In this paper, we assume an approximate concordance cosmology: \( \Omega_m = 0.3, \Omega_{Λ} = 0.7, \) and \( H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1} \).

2. OBSERVATIONS AND DATA REDUCTION

2.1. The FSRQ Sample

This paper reports on a multi-year observing campaign to follow-up the Fermi blazars. A principal aim is to achieve high-redshift completeness for the 1LAC sample (Abdo et al. 2010a).

In this paper, we discuss the spectra of FSRQs and other LAT blazar associations with strong emission lines. A major contribution is new spectroscopy of 165 of these blazars. To extend the analysis, we also measured archival spectra of 64 Sloan Digital Sky Survey (SDSS) blazars in the sample, for a total of 229 spectra.

This work takes the 1LAC high-latitude sample to 96% type completeness, with 316 FSRQs, 322 BL Lac objects, 33 other AGNs, 4 LINERs, and 4 galaxies. There are 30 remaining associated flat-spectrum radio sources of unknown type—generally these represent objects that are optically extremely faint (\( R > 23 \)) or show faint continuum-dominated spectra, where current spectroscopy does not have sufficient signal-to-noise ratio (S/N) to unambiguously confirm a BL Lac type ID.

The most important sub-set of this emission-line sample are the objects with traditional FSRQ properties—in addition to the flat-spectrum radio core emission which allows the LAT counterpart association, we require emission lines with kinematic FWHM \( > 1000 \text{ km s}^{-1} \) and bolometric luminosity \( > 10^{42} \text{ erg s}^{-1} \). We find that 188 FSRQs meet these criteria, including 10 low-latitude sources with 1LAC FSRQ associations. In addition, some 11 BL Lac objects show well-detected broad lines. For this paper, we adopt the traditional heuristic BL Lac definition: continuum-dominated objects with observed frame line equivalent width (EW) of \( < 5 \text{ Å} \) and, where measured, Balmer break strength of \( < 0.5 \) (Healey et al. 2008).

We classify an object as “BL Lac” if it meets these spectroscopic criteria at any epoch. For 6 of the 11 BL Lac objects our spectra include epochs in a “low” state where decreased continuum reveals broad emission lines with \( > 5 \text{ Å} \) EW. The other five objects satisfy the BL Lac criteria in all of our spectra, but nevertheless show highly significant, albeit low EW, broad lines.

The emission-line sample contains 29 other objects—spectroscopically these are 9 galaxies, 5 LINERs, and 15 other AGNs. These show only strong narrow lines. While the line strengths rule out BL Lac IDs for these objects, they are manifestly different from our typical FSRQs. They may be
misaligned radio galaxies, intrinsically weak AGNs, narrow-line Seyfert galaxies, and other less common types of γ-ray emitters (Abdo et al. 2010c).

Note that this sample of digital spectra does not include measurements for a number of bright, famous blazars, with historical spectroscopic classifications in the literature. Indeed, 137 of the 316 Fermi FSRQs fall into this category. Measured in $R$, the sources with archival spectra are brighter by 1.4 mag than our sample, so their omission may introduce systematic effects, discussed briefly in Section 5.3.

### 2.2. Observations

We have used medium and large telescopes in both hemispheres in a many-faceted assault on this sample. Observations were obtained from the Marcario Low Resolution Spectrograph (LRS) on the Hobby–Eberley Telescope (HET), the Large Cass Spectrometer (LCS) on the 2.7 m at McDonald Observatory, on the ESO Faint Object Spectrograph and Camera (EFOSC2; Buzzoni et al. 1984) and ESO Multi-Mode Instrument (EMMI; Dekker et al. 1986) at the New Technology Telescope at La Silla Observatory (NTT), on the Double Spectrograph (DBSP) on the 200″ Hale Telescope at Mt. Palomar, on the FOcal Reducer and low dispersion Spectrograph (FORS2; Appenzeller et al. 1998) on the Very Large Telescope (VLT) at Paranal Observatory, and on the Low Resolution Imaging Spectrograph (LRIS) at the W. M. Keck Observatory (WMKO). Observational configurations and objects observed are listed in Table 1.

The observing runs jointly targeted emission-line objects discussed in this paper and BL Lac objects to be discussed in a companion paper (M. S. Shaw et al., in preparation). All objects discussed in this work have highly significant emission lines and confirmed spectroscopic redshifts.

All spectra are taken at the parallactic angle, except for LRIS spectra using the atmospheric dispersion corrector, where we observed in a north–south configuration. In a few cases, we rotated the slit angle to minimize contamination from a nearby star. At least two exposures are taken of every target for cosmic-ray cleaning. Typical exposure times are $2 \times 600$ s.

With the variety of telescope configurations and varying observing conditions, the quality of the spectra are not uniform: resolutions vary from 4 to 15 Å, exposure times from 360 s to 2400 s, and telescope diameters from 2.7 m to 10 m. During this campaign, we generally used the minimum exposure required for a reliable redshift, rather than exposure to a uniform S/N. This may introduce selection effects into the sample, discussed briefly in Section 4.

### 2.3. Data Reduction Pipeline

Data reduction was performed with the IRAF package (Tody 1986; Valdes 1986) using standard techniques. Data were overscan subtracted and bias subtracted. Dome flats were taken at the beginning of each night, the spectral response was removed, and all data frames were flat-fielded. Wavelength calibration employed arc lamp spectra and was confirmed with checks of night sky lines. For these relatively faint objects, we employed an optimal extraction algorithm (Valdes 1992) to maximize the final S/N. For HET spectra, care was taken to use sky windows very near the long-slit target position so as to minimize spectroscopic residuals caused by fringing in the red, whose removal is precluded by the rapidly varying HET pupil. Spectra were visually cleaned of residual cosmic-ray contamination affecting only individual exposures.

We performed spectrophotometric calibration using standard stars from Oke (1990) and Bohlin (2007). In most cases standard exposures were available from the data night. Since the HET is queue scheduled, standards from subsequent nights were sometimes used. At all other telescopes, multiple standard stars were observed per night under varying atmospheric conditions and different air masses. The sensitivity function was interpolated between standard star observations when the solution was found to vary significantly with time.

For blue objects, broad-coverage spectrographs can suffer significant second-order contamination. In particular, the standard HET configuration using a Schott GG385 long-pass filter permitted second-order effects redward of 7700 Å. The effects on object spectra were small, but for blue WD spectrophotometric standards, second-order corrections were needed for accurate determination of the sensitivity function. This correction term was constructed following Szokoly et al. (2004). In addition, since BL Lac spectra are generally simple power laws, we used BL Lac objects observed during these runs (M. S. Shaw et al., in preparation) to monitor second-order contamination and residual errors in the sensitivity function. This resulted in excellent, stable response functions for the major data sets.

### Table 1

| Telescope  | Instrument | Resolution ($\lambda$) | Slit Width (arcsec) | Objects | Filter | $\lambda_{\text{min}}$ ($\lambda$) | $\lambda_{\text{max}}$ ($\lambda$) |
|------------|------------|------------------------|---------------------|---------|--------|-------------------------------|-------------------------------|
| HET        | LRS        | 15                     | 2                   | 77      | GG385  | 4150                          | 10500                         |
| HET        | LRS        | 8                      | 1                   | 1       | GG385  | 4150                          | 10500                         |
| McDonald 2.7 m | LCS     | 15                     | 2                   | 1       | ...    | 4200                          | 8200                          |
| NTT        | EFOSC2     | 16                     | 1                   | 14      | ...    | 3400                          | 7400                          |
| NTT        | EMMI       | 12                     | 1                   | 8       | ...    | 4000                          | 9300                          |
| Palomar 200′ | DBSP      | 5/15                   | 1                   | 3       | ...    | 3100                          | 8100                          |
| Palomar 200′ | DBSP      | 5/15                   | 1.5                 | 1       | ...    | 3100                          | 8100                          |
| Palomar 200′ | DBSP      | 5/9                    | 1.5                 | 2       | ...    | 3100                          | 8100                          |
| VLT        | FORS2      | 11                     | 1                   | 22      | ...    | 3400                          | 9600                          |
| VLT        | FORS2      | 17                     | 1.6                 | 2       | ...    | 3400                          | 9600                          |
| WMKO       | LRIS       | 4/7                    | 1                   | 11      | ...    | 3100                          | 10500                         |
| WMKO       | LRIS       | 4/9                    | 1                   | 22      | ...    | 3100                          | 10500                         |

Note. For DBSP and LRIS the blue and red channels are split by a dichroic at 5600 Å; the listed resolutions are for blue and red sides, respectively.
Spectra were corrected for atmospheric extinction using standard values. We followed Krisciunas et al. (1987) for WMKO LRIS spectra, and used the mean KPNO extinction table from IRAF for P200 DBSP spectra. Our NTT, VLT, and HET spectra do not extend into the UV and so suffer only minor atmospheric extinction. These spectra were also corrected using the KPNO extinction tables. We removed Galactic extinction using IRAF’s de-reddening function and the Schlegel maps (Schlegel et al. 1998). We made no attempt to remove intrinsic reddening (i.e., from the host galaxy).

Telluric templates were generated from the standard star observations in each night, with separate templates for the oxygen and water line complexes. We corrected separately for the telluric absorptions of these two species. We found that most telluric features divided out well, with significant residuals only apparent in spectra with very high S/N. On the HET spectra, residual second-order contamination prevented complete removal of the strong water band redward of 9000 Å.

When we had multiple epochs of these final cleaned, flux-calibrated spectra with the same instrumental configuration, we checked for strong continuum variation. Spectra with comparable fluxes were then combined into a single best spectrum, with individual epochs weighted by S/N.

Due to variable slit losses and changing conditions between object and standard star exposures, we estimated that the accuracy of our absolute spectrophotometry is ∼30% (Healey et al. 2008), although the relative spectrophotometry is considerably better.

Redshifts were generally confirmed by multiple emission lines and derived by cross-correlation analysis using the rvsao package (Kurtz & Mink 1998). For a few objects only single emission lines were measured with high S/N. In general we could use the lack of otherwise expected features to identify the species and the redshift with high confidence. Nevertheless, single-line redshifts are marked (Tables 3 and 4) with a colon (:) and discussed in Section 2.4. Velocities are not corrected to heliocentric or LSR frames.

Reduced spectra of the newly measured objects are presented in Figure 1 (full figure available in the online journal).

2.4. Individual Objects

A few observations require individual comment.

J0023+4456. This spectrum had low S/N (∼2) and, while C iv, C iii, and Mg ii lines were tentatively identified, we mark the final solution as uncertain.

J0654+5042. This blazar, 0.5′ from a bright star, was observed using DBSP with the slit along the blazar-star axis. We were able to isolate the stellar light by extraction from the wings of the convolved object. This spectrum was scaled and subtracted from the blazar spectrum to remove the stellar rest wavelength absorption features, giving a relatively clean blazar spectrum. While the emission line and redshift measurements are unambiguous, the continuum spectrophotometry should be treated with caution.

J0949+1752, J1001+2911, J1043+2408, and J1058+0133. These blazars show only a single broad emission line; good spectral coverage gives high confidence of identification as Mg ii.

J1330+5202. This blazar shows only strong [O iii] in emission at 3727 Å, with associated host Ca H/K absorptions. No broad emission lines are observed.

J1357+7643. Only one broad line is detected with high significance. A weaker corroborating feature implies C iv, Mg ii at z = 1.585. However, a z = 0.431 solution cannot be ruled out so we mark this solution as tentative.

J2250–2806. With a single strong narrow line (assigned to [O i] 3727 Å), this blazar has an uncertain redshift. No broad emission lines are observed.

3. MEASURED PROPERTIES

3.1. Primary Spectra and Multiple Epochs

For some objects, multiple exposures at different epochs show significant spectral variability. In general, follow-up epochs have higher resolution or S/N or targeted the blazar in a lower flux state. In a few cases SDSS spectra were published after we had obtained independent data. We adopt the spectrum showing the highest S/N for broad-line detection as the primary spectrum used in this analysis. In general, this is the spectrum used to solve for the source redshift. As noted above, for particularly faint objects we can make S/N-weighted combinations of spectra (for which no strong flux variation is seen) to obtain the best primary spectrum. This is particularly valuable for the HET data, as limited track time requires short observations, but queue scheduling with very stable configurations allows easy combination of multiple epochs.

As noted above, in six cases, sources in this sample transitioned from a bright (continuum-dominated) state to a lower state. For these the “Primary” spectrum is from the low state, allowing better line measurements, during which the source is a nominal FSRQ (broad-line EW > 5 Å). We nevertheless retain the original BL Lac typing (see Section 3.7). Clearly a more physical separation between the classes, and attention to duty cycles in the various “states” is needed.

3.2. Continuum Properties

We have fit power-law continua to all our spectra, using the scipy.optimize.leastsq routine4 based on Levenberg–Marquardt fitting to estimate parameter values and statistical errors. For these fits we first excise regions around the strongest emission lines in the blazar rest frame: \( \lambda \lambda 1200–1270, 1380–1420, 1520–1580, 1830–1970, 2700–2900, 3700–3750, 4070–4130, 4300–4380, 4800–5050, 6500–6800 \) Å. We then fit simple power-law flux spectra to the entire spectral range, excluding regions at the blue or red end with uncharacteristically large noise. We do not here attempt to separate the thermal disk contribution. The results are presented as power-law indices, \( \alpha \), and continuum fluxes at \( 10^{44.7} \) Hz (\( \sim 5980 \) Å), the center of our spectral range, as measured in the observer frame. These data may be combined with multi wavelength data to study the spectral energy distribution (SED) of the blazars in our sample.

The statistical errors on \( F_\lambda \) (Tables 3 and 4) are generally small, but should be convolved with the overall fluxing errors, estimated at 30%. We estimate errors on the spectral index by independently fitting the red and blue halves of the measured spectrum. We then sum the differences in quadrature for an estimated error:

\[
\alpha_{err} = \left( (\alpha_{red} - \alpha)^2 + (\alpha_{blue} - \alpha)^2 \right)^{1/2}.
\]

Note that large error bars generally indicate deviation from power-law continua rather than poor statistics. We find that extreme values of \( \alpha \) seem to correlate with large Galactic AV, suggesting errors in the assumed extinction and residual curvature in the corrected spectrum.

4 http://www.scipy.org
3.3. Line Properties

All line measurements are conducted in the object’s rest frame. The local continuum and line parameters are measured with the scipy.optimize.leastsq routines. We first isolate the local continua surrounding the line, as in Section 3.2 (including an additional pseudocontinuum for Mg II from the Fe II/Fe III line complex). Then, the line is fit to the continuum-subtracted data. Reported errors are purely statistical.

We follow Shen et al. (2011) in their line measurement techniques to facilitate comparison of our results with measurements in the extensive SDSS quasar catalog. We focus on lines used for BH mass estimates: Hβ at 4861 Å, Mg II at 2800 Å, and C IV at 1550 Å.

Before reporting kinematic widths, we subtract in quadrature the observational resolution, to eliminate bias between objects measured by different telescopes, and to improve estimates of narrower lines. In higher redshift sources, emission lines are sometimes contaminated by intervening or associated absorption line systems. We visually check all emission lines.

We found strong absorption lines (associated and self-absorption systems) in a number of objects and edited these out before fitting the emission lines. Associated Mg II absorbers were found in J0043+3426 (Δν ∼ −2400 km s⁻¹), J0252−2219 (Δν ∼ −3500 km s⁻¹ and Δν ∼ −2800 km s⁻¹), J1120+0704 (Δν ∼ −1600 km s⁻¹), J1639+4705 (Δν ∼ −600 km s⁻¹), and J2212+2355 (Δν ∼ −2400 km s⁻¹). In J0325+2224 we find self-absorbed C IV absorption. In J2321+3204, we find two
systems ($\Delta v \sim -400$ km s$^{-1}$ and $\Delta v \sim 100$ km s$^{-1}$) and remove the absorptions from both Mg $\Pi$ and C IV before fitting. Finally, in J2139−6732, we edit out an intervening ($z = 0.923$) Fe II absorption system coincident with the C IV emission line. We next summarize particular issues for the three major species fit.

3.4. Fitting H$\beta$

For H$\beta$, it is essential to include narrow components in the line fit. After power-law continuum removal, we simultaneously fit broad and narrow H$\beta$, narrow [O III]$_{4959}$ Å, and narrow [O III]$_{5007}$ Å (McLure & Dunlop 2004). We fix the rest wavelengths of narrow H$\beta$ and the [O III] lines at the laboratory values and fix widths at the spectral resolution, as measured from sky lines; the broad H$\beta$ center and width are free to vary. All lines are modeled with single Gaussian profiles. The continuum is measured at 5100 Å.

3.5. Fitting Mg $\Pi$

For Mg $\Pi$, we fit the pseudocontinuum from broad Fe $\Pi$/Fe III along with a power law. For the former, we use a template (Vestergaard & Wilkes 2001) convolved with the observational resolution. The power law is fit using the $\lambda\lambda$2200−2700 and 2900−3100, portions of the spectrum; both continuum component fluxes and the power-law index vary freely. After continuum subtraction, we fit the Mg $\Pi$ line with broad and narrow Gaussian components. For this line, the continuum measurement is made at 3000 Å to minimize residual Fe contamination (McLure & Dunlop 2004).

3.6. Fitting C IV

Here, we fit the power-law continuum over 1445−1464 Å and 1700−1705 Å. After subtraction, we fit the C IV line with three Gaussians, following Shen et al. (2011), and report the full FWHM of the line. Any narrow self-absorption components are visually identified and removed prior to the fit, as with the intervening absorbers described above.

3.7. Objects with Special Type Classifications

Several blazars were classified as BL Lac objects in initial epoch observations. At the “primary” spectrum epoch, with low continuum, each was a nominal FSRQ. The objects which changed (and continuum decrease) were: J0058+3311 (8 ×), J0923+4125 (4 ×), J1001+2911 (6 ×), J1607+1551 (5 ×), J2031+1219 (4 ×), and J2244+4057 (10 ×).

With very high S/N observations, we were able to detect broad lines at high significance at EW levels <5 Å in several objects. These were thus “BL Lac objects” at all of our epochs, but can be analyzed along with the FSRQ. The BL Lac objects (and strongest broad-line EWs) were: J0430−2507 (Mg $\Pi$ at EW = 0.9 Å), J0516−6207 (C IV at EW = 1.6 Å; C III, Mg $\Pi$ also present), J1058+0133 (Mg $\Pi$ at EW = 2.2 Å), J2236+2828 (Mg $\Pi$ at EW = 4.9 Å), and J2315−5018 (Mg $\Pi$ at EW = 3.8 Å). These EW measurements are in observed frame. Clearly these sources are transitional between our standard FSRQs and BL Lac types.

3.8. Calibrating Our Measurements

For 53 of the 64 SDSS spectra in our sample Shen et al. (2011) tabulate standard measurements of the continuum and emission-line properties. This allows us to check the consistency of our measurements techniques. We find that our measurements of continuum and line luminosities are consistent with those of Shen et al. (2011), although some scattered differences in line luminosity are seen, as the luminosity is sensitive to the fitting details. In particular, for Mg $\Pi$ and H$\beta$, the variations in the narrow-line component flux can change the measured broad-line luminosity. Nevertheless, we see no systematic offset between our results and those of Shen et al. (2011).

However, we do note that our fitted kinematic FWHM values are systematically ~10% lower (for the same sources) than those of Shen et al. (2011). For Mg $\Pi$ and H$\beta$, we attribute this to small differences in the fit to the narrow component. For C IV, three Gaussians are used and we suspect that our central (narrowest) Gaussian is systematically weaker than that found in the SDSS fits. As we shall see, interesting differences from the SDSS quasars include narrower lines, on average, so we conservatively chose not to bias our fitter to force agreement. Nevertheless FWHM effects may be suspect at the 10% scale.

3.9. Comparison to SDSS Non-blazars

To place our Fermi sample in the context of the broader QSO population, we compare our measurements to those of the largely (>90%) radio-quiet SDSS Data Release 7 (DR7) quasar sample (Shen et al. 2011). We find significant offsets in the mean values of the continuum luminosities, line luminosities, and line FWHMs of the two classes as plotted in Figure 2. Since our sample extends fainter than the SDSS QSOs, we also plot the distributions for a magnitude cut $i < 19.1$ sample (Schneider et al. 2010).

To quantify these differences, we compute the medians as well as the semi-interquartile range (SIQR) for each distribution. We can use these values to estimate statistical errors on the median as $\sigma = \text{SIQR}/\sqrt{n}$, where $n$ is the number of points in the sample. In Figure 2, we report both the median offset, $\Delta$, and its estimated significance, $\Delta/\sigma$, for each parameter. The corresponding medians and errors for the magnitude-cut sample are given in parentheses.

Several distributions show large offsets from the SDSS population. Our C IV and Mg $\Pi$ lines are significantly less luminous than those of the SDSS QSOs. Comparing the values for the flux-cut sample, we see that a significant difference persists. We conclude that we are sampling a population with intrinsically weaker lines or that fainter, weaker-line objects are lifted into our samples by the addition of extra non-thermal continuum flux. It seems that the local continua around Mg $\Pi$ and C IV are similar for our objects; we do notice that our H$\beta$ continua seem substantially brighter than those of the QSO population. We suspect that a lower redshift distribution and larger host-light contribution (see below) may explain this effect.

For all species (and for the sub-sample) we find that our measured lines are significantly narrower than those of the SDSS QSOs. We attribute this to preferential alignment, further discussed in Section 6.

4. EXCESS CONTINUUM

We expect our radio-γ-selected population to have significant continuum contribution from non-thermal jet emission. At low redshift, there may also be additional galaxy light, especially around the H$\beta$ line, to the red of the Balmer break.

4.1. Estimated Continua from Lines

In order to characterize the non-thermal emission in our spectra, we estimate a predicted continuum luminosity from the emission-line fluxes, scaling to a non-blazar sample. Shen...
et al. (2011) report line and continuum luminosities for the DR7 quasars. These are highly correlated ($r_{xy} = 0.85, 0.91, \text{and } 0.68$ for H$\beta$, Mg $\text{II}$, and C $\text{IV}$ respectively), and they fit continuum luminosities to line luminosities for Mg $\text{II}$ and C $\text{IV}$, finding

$$\log L_{3000} = 1.016 \pm 0.003 \cdot \log L_{\text{Mg II}} + 1.22 \pm 0.11$$  \hspace{1cm} (2)

$$\log L_{1350} = 0.863 \pm 0.009 \cdot \log L_{\text{C IV}} + 7.66 \pm 0.41.$$ \hspace{1cm} (3)

We extend this treatment by fitting the SDSS QSO results for the H$\beta$ line:

$$\log L_{5100} = 0.802 \pm 0.049 \cdot \log L_{\text{H} \beta} + 1.574 \pm 0.060.$$ \hspace{1cm} (4)

Since the line flux continuum predictions are calibrated to a non-blazar sample, they should be independent of the non-thermal jet activity. Of course for both samples, at low redshift, there may still be galaxy light contaminating the H$\beta$ region, increasing the scatter. We compare the predicted to observed continuum levels for our Fermi FSRQs, finding that the lines predict (on average) 44%, 40%, and 32% of observed continuum luminosities for H$\beta$, Mg $\text{II}$, and C $\text{IV}$ respectively. We attribute the excess to non-thermal “jet” emission.

It is of interest to inspect the non-thermal dominance ($\text{NTD} \equiv L_{\text{obs}} / L_{\text{pred}}$) for individual objects in our sample. While most objects have NTD $\sim 1$ (i.e., mostly thermal continua), for
correlation in same-object NTD measured from the three species based on measurements of at least one line. We find significant must account for this dominant non-thermal emission. Spectra are BL Lac-like and analysis of the optical properties contaminating galaxy light. Thus for 10% of our sample, the $H_{\alpha}$ color version of this figure is available in the online journal.

We thin error bars for NTD non-thermal dominance is weakly correlated to low spectral indices in circles. Squares indicate BL Lac designations from a previous spectrum. Large by galaxy luminosity as well. BL Lac objects in the primary spectrum are continuum emission near each of the lines. The $H_{\alpha}$ (A color version of this figure is available in the online journal.) observations. We thin error bars for NTD $< 0.8$ for readability.

57 blazars we have NTD $> 2$ and 18 spectra show NTD $> 10$ based on measurements of at least one line. We find significant correlation in same-object NTD measured from the three species ($r_{xy} = 0.51$ for Mg II and C IV; $r_{xy} = 0.73$ for $H_{\beta}$ and Mg II) $H_{\beta}$ generally measures larger NTD, which we attribute to contaminating galaxy light. Thus for 10% of our sample, the spectra are BL Lac-like and analysis of the optical properties must account for this dominant non-thermal emission.

4.2. Non-thermal Continuum Pollution

In Figure 3, we report on the NTD of our sample. An optically selected population, such as that of Shen et al. (2011), peaks at log NTD $= 0$, the line-predicted thermal flux is comparable to the measured flux. Unsurprisingly the $Fermi$ blazars extend to much larger NTD levels. This plays an important role in continuum-calibrated estimates of hole mass in Section 5.

Further we find a weak, but interesting correlation between NTD and $Fermi$ $\gamma$-ray spectral index. The $Fermi$ FSRQ population has $\langle \gamma \rangle = 2.44$, whereas the BL Lac population has $\langle \gamma \rangle = 2.04$. Thus the $\gamma$-ray hardness is a good predictor of the continuum strength in the broadband SED. Indeed, we find that the objects in our sample with the largest NTD show relatively hard $Fermi$ spectra. It will be of interest to trace this trend deeper into the BL Lac population, although NTD estimates will be more difficult for this sample. Note that while actual BL Lac objects (circles), unsurprisingly, are mostly in the high NTD regime, a number of nominal FSRQs are found in this region, as well.

5. THE CENTRAL ENGINE

5.1. Traditional Virial Mass Estimates

As in Shen et al. (2011), we estimate traditional virial BH masses from a relation of the form

$$\log \left( \frac{M_{BH}}{M_\odot} \right) = a + b \log (\lambda L_\lambda) + 2 \log (\text{FWHM}),$$

where $a$ and $b$ are calibrated from reverberation mapping for each line species (McLure & Dunlop 2004). The broad-line FWHM, in km s$^{-1}$, and the continuum luminosity $\lambda L_\lambda$, in units of $10^{44}$ erg s$^{-1}$, are measured as described in Sections 3.4–3.6. Values of $a$ and $b$ are tabulated in Table 2 from Vestergaard & Peterson (2006; hereafter VP06) for $H_{\beta}$ and C IV and Vestergaard & Osmer (2009; hereafter, VO09) for Mg II. A scatter of $\sim 0.4$ dex has been inferred for virial masses in optically selected samples (Shen et al. 2011).

For our $Fermi$ sample we estimate mass from $H_{\beta}$ for 50 objects, from Mg II for 176 objects, and from C IV for 68 objects. For 39 and 50 objects respectively, we measure mass from both $H_{\beta}$ and Mg II, and from Mg II and C IV. Masses are reported in Tables 3 and 4.

We urge caution in a naive interpretation of these masses, as applied to blazars. Due to the significant NTD of our sample, we expect continuum luminosity to not scale as in the reverberation mapping sample, as discussed below in Section 5.2. Further, preferential alignment and a non-spherical BLR yields systematically narrower lines, as discussed in Section 6.

5.2. Mass Estimates from Lines Alone

Bearing in mind the substantial NTD of much of our $Fermi$ sample, we wish to make mass estimates from the line luminosity and line kinematic width alone. Greene & Ho (2005) and Kong et al. (2006) calibrate such estimators from reverberation mapping samples. Shen et al. (2011) calibrate estimators for Mg II and C IV from the SDSS sample. We have augmented this, using the SDSS mass estimators and developed our own coefficients for $H_{\beta}$ with values consistent with the predicted continuum luminosity and mass estimates of Section 5.1. The coefficients for these estimators are listed in Table 2 for a formula of the form of Equation (5), replacing $\lambda L_\lambda$, with line luminosity in units of $10^{44}$ erg s$^{-1}$.

In Figure 4, we compare the line-estimated masses for our radio-$\gamma$-selected sample with estimates from the traditional continuum virial mass equations. We find that the line masses are smaller than the traditional virial masses by 0.14 dex on average. This is a small, but significant effect. More interesting is the comparison for different species and different epochs. For example the nearby, low-mass, low-luminosity $H_{\beta}$ mass sample shows a larger average line-mass decrease than the powerful C IV FSRQ. We attribute this primarily to host-light pollution in the former and thermal disk domination in the latter.

For those objects where we have multiple epochs of observation (see Section 3.1 for details), we calculate the mass in both spectra. Due to the statistical uncertainty in measuring the line kinematic width, and the large role that plays in mass calculations, in all but three cases, the measurement in the multiple spectra are not significantly different from that in the primary spectrum. In the right panel of Figure 4, we also plot estimated mass changes from continuum luminosity fluctuations in spectra too poorly measured to estimate line properties. The general trend is for variations to extend above the line-determined values, which show smaller fluctuation (i.e., continuum variations dominate and bias mass estimates, as expected).

5.3. Comparison to Optically Selected Quasars

Using the less biased masses derived using line strengths, we compare in Figure 5 our radio-$\gamma$ sample to the optically selected
Figure 4. On the left, masses from the lines are plotted against traditional virial masses for Fermi FSRQs. Most objects lie to the right of the 1:1 (solid) line, indicating larger traditional (continuum) masses. The dashed line shows the effect of a 3× NTD. Closed symbols indicate objects with error <0.4 dex in both masses. In the right panel, objects with multiple observations are plotted. For the three objects with significant (>2σ) mass offset, we connect the two masses with a solid line, and plot the error ellipse around the primary observation. For others, we measure the continuum luminosity in both spectra, and mark the mass offset from continuum change by a dotted line.

(A color version of this figure is available in the online journal.)

Table 2

| Source        | Hβ  | Mg ii | C iv  | Reference          |
|---------------|-----|-------|-------|--------------------|
| Mass from continuum | a   | b     | a     | b                  | MD04 (Hβ, C iv), VO09 (Mg ii) |
| Mass from lines   | 1.63 ± 0.04 | 0.61 | 1.70 ± 0.07 | 0.62 | 0.660 ± 0.53 | This work (Hβ), Shen et al. (2011) (Mg ii, C iv) |

Notes. Coefficients for the virial fitting relation in Equation (5). Coefficients derived from this work, McLure & Dunlop (2004, MD04), Vestergaard & Osmer (2009, VO09), and Shen et al. (2011).
Table 3
Line Properties for \( z < 1 \) Broad-line 1LAC AGNs

| Name            | \( z \) | \( F_{\nu, 10^{28}} \) (10\(^{-28}\) erg cm\(^{-2}\) s\(^{-1}\) Hz\(^{-1}\)) | \( \alpha \) | \( L_{\lambda 5100} \) (erg s\(^{-1}\)) | \( L_{\lambda H\beta} \) (erg s\(^{-1}\)) | FWHM (km s\(^{-1}\)) | Mass \( \log(M/M_\odot) \) | \( L_{\lambda 3000} \) (erg s\(^{-1}\)) | \( L_{\lambda Mg\, ii} \) (erg s\(^{-1}\)) | FWHM (km s\(^{-1}\)) | Mass \( \log(M/M_\odot) \) | Telescope |
|-----------------|--------|--------------------------------|---------|-------------------|-------------------|-----------------|-----------------|-------------------|-------------------|-----------------|-----------------|-----------|
| J0004−4736      | 0.880  | 11.4 ± 0.0                      | −0.99 ± 0.08     | ...                | ...                | ...              | ...              | 45.339 ± 0.011 | 42.896 ± 0.151 | 2700 ± 500    | 7.85 ± 0.36     | NTT       |
| J0008+1450      | 0.045  | 73.8 ± 0.1                      | −1.79 ± 0.23     | 43.216 ± 0.002    | 40.921 ± 0.120    | 10800 ± 2600    | 8.19 ± 0.48     | ...                | ...                | ...              | ...              | SDSS      |
| J0017−0512      | 0.226  | 30.4 ± 0.1                      | −0.46 ± 0.36     | 44.353 ± 0.004    | 42.388 ± 0.107    | 2300 ± 500      | 7.55 ± 0.45     | ...                | ...                | ...              | ...              | HET       |
| J0024+0349      | 0.545  | 27.1 ± 0.0                      | −1.88 ± 0.08     | ...                | ...                | ...              | ...              | 45.110 ± 0.001 | 42.585 ± 0.057 | 3000 ± 200    | 7.76 ± 0.14     | WMKO      |
| J0043+3426      | 0.966  | 6.6 ± 0.0                       | −1.24 ± 0.03     | ...                | ...                | ...              | ...              | 45.201 ± 0.006 | 42.807 ± 0.072 | 3400 ± 300    | 8.01 ± 0.16     | WMKO      |
| J0050−0452      | 0.922  | 7.7 ± 0.1                       | −0.92 ± 0.19     | ...                | ...                | ...              | ...              | 45.198 ± 0.013 | 43.140 ± 0.141 | 3300 ± 600    | 8.20 ± 0.34     | HET       |
| J0102+4214      | 0.874  | 30.1 ± 0.1                      | −1.63 ± 0.86     | 46.001 ± 0.004    | 43.460 ± 0.038    | 1900 ± 200      | 7.92 ± 0.16     | 45.409 ± 0.007 | 43.593 ± 0.072 | 3300 ± 300    | 8.49 ± 0.17     | WMKO      |
| J0102+5824      | 0.644  | 167.0 ± 0.3                     | −1.25 ± 0.36     | ...                | ...                | ...              | ...              | 46.093 ± 0.076 | 43.449 ± 0.256 | 4100 ± 1200   | 8.57 ± 0.61     | HET       |
| J0112+2244      | 0.265  | 18.6 ± 0.2                      | −2.71 ± 0.79     | ...                | ...                | ...              | ...              | ...                | ...                | ...              | ...              | HET       |
| J0113+1324      | 0.685  | 15.2 ± 0.0                      | −0.01 ± 0.26     | 45.063 ± 0.006    | 43.094 ± 0.062    | 3800 ± 500      | 8.35 ± 0.25     | 45.263 ± 0.006 | 43.389 ± 0.082 | 4300 ± 400    | 8.57 ± 0.19     | SDSS      |

Note. The J4+4 names represent radio positions of the objects, as found in Abdo et al. (2010a).

(This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)
Table 4
Line Properties for \(z > 1\) Broad-line 1LAC AGNs

| Name         | \(z\)  | \(F_{\nu, 10^{14.7}}\) (\(10^{-28}\) erg cm\(^{-2}\) s\(^{-1}\) Hz\(^{-1}\)) | \(L_{3000}\) (erg s\(^{-1}\)) | \(L_{\text{Mg}\, II}\) (erg s\(^{-1}\)) | FWHM (km s\(^{-1}\)) | Mass \((M/M_\odot)\) | \(L_{1350}\) (erg s\(^{-1}\)) | \(L_{\text{C}\, IV}\) (erg s\(^{-1}\)) | FWHM (km s\(^{-1}\)) | Mass \((M/M_\odot)\) | Telescope |
|--------------|--------|------------------------------------------------------------------|----------------------------|--------------------------------|------------------|------------------|----------------------------|--------------------------|------------------|------------------|------------|
| J0011+0057   | 1.493  | 5.2 ± 0.1                                                         | 45.486 ± 0.021             | 43.541 ± 0.081             | 4900 ± 500       | 8.80 ± 0.19     | 45.800 ± 0.069  | 43.493 ± 0.435       | 2500 ± 1300      | 8.09 ± 1.02       | SDSS       |
| J0015+1700   | 1.709  | 8.0 ± 0.0                                                          | 46.070 ± 0.004             | 44.178 ± 0.043             | 5900 ± 300       | 9.56 ± 0.10     | 45.818 ± 0.016  | 44.180 ± 0.068       | 5900 ± 500       | 9.15 ± 0.17       | WMKO       |
| J0023+4456   | 2.023  | 1.3 ± 0.1                                                          | ...                        | ...                        | ...              | ...              | 45.213 ± 1.000  | 43.336 ± 0.875       | 1900 ± 2200      | 7.78 ± 2.29       | HET        |
| J0042+2320   | 1.426  | 5.1 ± 0.1                                                          | 45.533 ± 0.017             | 43.412 ± 0.137             | 6900 ± 1100      | 9.01 ± 0.32     | ...                        | ...                        | ...              | ...              | HET        |
| J0044–8422   | 1.032  | 9.7 ± 0.0                                                          | 45.401 ± 0.007             | 43.667 ± 0.113             | 3900 ± 500       | 8.68 ± 0.26     | ...                        | ...                        | ...              | ...              | VLT        |
| J0048+2235   | 1.161  | 11.5 ± 0.0                                                         | 45.639 ± 0.002             | 43.143 ± 0.049             | 4300 ± 200       | 8.43 ± 0.11     | 45.916 ± 0.027  | 43.272 ± 0.115       | 3400 ± 500       | 8.25 ± 0.28       | WMKO       |
| J0058+3311   | 1.369  | 3.1 ± 0.1                                                          | 45.331 ± 0.003             | 42.805 ± 0.054             | 3400 ± 200       | 8.01 ± 0.13     | 45.177 ± 0.035  | 43.451 ± 0.076       | 2200 ± 200       | 7.97 ± 0.19       | WMKO       |
| J0104–2416   | 1.747  | 8.8 ± 0.0                                                          | 45.817 ± 0.010             | 43.613 ± 0.111             | 5000 ± 600       | 8.85 ± 0.26     | 45.989 ± 0.025  | 44.121 ± 0.292       | 4900 ± 1700      | 8.97 ± 0.69       | NTT        |
| J0157–4614   | 2.287  | 1.9 ± 0.0                                                          | 45.632 ± 0.030             | 43.216 ± 0.171             | 2500 ± 500       | 7.98 ± 0.40     | 45.522 ± 1.000  | 44.083 ± 7.015       | 3000 ± 24900     | 8.52 ± 20.15      | VLT        |
| J0226+0937   | 2.605  | 16.9 ± 0.0                                                         | ...                        | ...                        | ...              | ...              | ...                        | ...                        | ...              | ...              | P200       |

Note. The 1J4+4 names represent radio positions of the objects, as found in Abdo et al. (2010a).

(This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)
ratios for this FSRQ support this picture, we do not find any inverse correlation between Eddington ratio and NTD as might be expected if high values indicate a transition to a BL Lac type state.

6. ORIENTATION OF THE BLR

The virial BH mass estimates require that the BLR has an isotropic velocity distribution (Salviander et al. 2007). In practice, there is a lack of consensus as to the shape of the BLR (McLure & Dunlop 2004). With a more disk-like BLR, objects observed perpendicular to the disk will have lower kinematic FWHMs, and thus, lower inferred BH masses. Following Decarli et al. (2011), we can interpret the FWHM offset of Section 3.9 as a geometric effect and estimate the f-value, as a measure of the shape of the BLR.

If we assume that the underlying broad-line shape distribution is the same as that of the SDSS QSOs, and use our $i < 19.1$ flux-cut sample, we find that our MgII and CIV lines are 0.14 dex narrower. Recalling that our line widths seem to be systematically slightly lower than the SDSS line estimates by 0.04 dex, the true offset may be as high as 0.18 dex.

We assume that we are probing a population with the same mass distribution as SDSS. Then, for a 0.14 dex offset our f-value is 1.38 $f_{\text{SDSS}}$, which is inconsistent with both a spherical BLR and a geometrically thin disk. In fact f can be related to the typical disk thickness ratio $H/R$:

$$\langle f \rangle = 0.5 \left[ \left( \frac{H}{R} \right)^2 + \sin^2 \theta \right]^{-1/2},$$  

where the average is taken over the observer inclination angle $\theta$. Since there is good evidence that the Fermi FSRQs are highly aligned (within $5^\circ$; Ajello et al. 2011) by assuming that the SDSS QSOs are viewed uniformly (in $\sin \theta$) away from the obscuring equatorial torus (at $\theta > 60^\circ$), we obtain an estimate for $H/R \sim 0.4$. Since the function is very flat at low $\theta$, the result is insensitive to the precise degree of Fermi FSRQs alignment. In fact, the required axis ratio only increases to 0.44 if the Fermi FSRQs are aligned within $2^\circ$. The decreased line width and hence the decreased inferred hole mass are fully consistent with the preferred alignment of these blazars as expected in the standard model. Thus while we do not exclude underlying masses differences, our measurements are best explained by similar optically selected and radio-\$\gamma\$-selected BH mass distributions, but with viewing angles strongly aligned to the disk (and jet) axis for the latter. As noted in Section 5.4, we do however find that the FSRQs show a higher Eddington ratio than the typical QSO, so some difference in accretion activity is indicated.

7. COMPARISON WITH RADIO ACTIVITY

Since the Fermi FSRQ associations are largely selected from a sample of radio bright, flat-spectrum sources, it may be useful to compare the optical spectroscopic properties with radio measurements indicating strong non-thermal activity. One good measure of this activity is the radio variability. Much of the Dec $> -20$ blazar sample has been monitored at 15 GHz at Owens Valley Radio Observatory since before the launch of Fermi. These data have been used to measure the intrinsic modulation index, a measure of the activity:

$$m = \frac{S_0}{\sigma_0},$$  

where $S_0$ and $\sigma_0$ are the intrinsic mean flux density and its standard deviation of the radio light curve, estimated from the data using a maximum-likelihood method (Richards et al. 2011). It has, for example, been found that this index is smaller for high-redshift FSRQs than lower redshift BL Lac objects.

We might, therefore, expect this modulation to correlate with either the BH mass (Figure 7) or the NTD (Figure 8). The lowest intrinsic modulations do appear among the highest mass holes, but there does not seem to be any increase in modulation for FSRQs with the higher NTD. Thus, jet variability does not
seem directly correlated with BH and broad-line properties. It is possible that more significant differences may be traced to the radio variability timescale, but this requires longer radio monitoring and a more complete analysis of the flaring activity.

8. CONCLUSIONS

We have used the optical spectral properties of our measured Fermi FSRQ sample to characterize the state of the central engine. We find that the optical continuum is significantly augmented by non-thermal (synchrotron) emission, presumably associated with the jet. In fact, such emission dominates the optical continuum for a third of our measured FSRQs. Unsurprisingly the degree of NTD correlates with the γ-ray spectral index and the likelihood of BL Lac classification.

To avoid bias from the additional continuum, we have developed estimates of the BH mass and the Eddington luminosity ratio which only use the line properties. These measurements show that the Fermi FSRQs are more active accretors than the bulk QSO population (at a given mass). We also find evidence for a significantly lower mean measured BH mass, even for a sample with a similar flux limit. Intriguingly, we find that the redshift evolution of the mass tracks that of the full QSO population. Thus, although non-thermal flux can pull less luminous, lower mass AGNs into the sample, we speculate that the primary effect is due to the high expected degree of alignment for the FSRQ sample. If alignment is indeed the explanation, the data suggest a modest degree ($H/R \sim 0.4$) of flattening in the BLR and that we probe a similar mean mass population (and evolution) as the bulk QSO distribution.

While the present sample shows no strong correlation with the bulk radio variability, we expect that a broader look at the Fermi blazar sample, including comparison with the BL Lac properties and study of the BL Lac state-duty cycle and timescales for radio and optical modulation, will reveal additional correlations with the properties of the central BH and its surrounding BLR. This extension to the BL Lac portion of the sample is under way.

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