Protoplanetary disks are strongly irradiated by a stellar FUV spectrum that is dominated by Lyα photons. We investigate the impact of stellar Lyα irradiation on the terrestrial planet region of disks (\(\leq 1\) AU) using an updated thermal-chemical model of a disk atmosphere irradiated by stellar FUV and X-rays. The radiative transfer of Lyα is implemented in a simple approach that includes scattering by H\(^+\) and absorption by molecules and dust. Because of their non-radial propagation path, scattered Lyα photons deposit their energy deeper in the disk atmosphere than the radially propagating FUV continuum photons. We find that Lyα has a significant impact on the thermal structure of the atmosphere. Photochemical heating produced by scattered Lyα photons interacting with water vapor and OH leads to a layer of hot (1500–2500 K) molecular gas. The temperature in the layer is high enough to thermally excite the H\(_2\) to vibrational levels from which they can be fluoresced by Lyα to produce UV fluorescent H\(_2\) emission. The resulting atmospheric structure may help explain the origin of UV fluorescent H\(_2\) that is commonly observed from classical T Tauri stars.

Key words: astrochemistry – protoplanetary disks – radiation mechanisms: thermal
emission, as in the model of Nomura et al. (2007). However, if there is a mechanism for heating the molecular gas to ~2500 K, then the excited vibrational levels of H$_2$ can be populated thermally.

Here we revisit the problem of the origin of hot H$_2$ emission from disks using an expanded thermal-chemical model of protoplanetary disk atmospheres that explores the role of Ly$\alpha$ in heating the atmosphere. The earlier version of our model implemented irradiation by stellar FUV continuum photons and a preliminary treatment of photochemical heating by H$_2$O and OH (Ádámkovics et al. 2014 hereafter AGN14). In the present study, we include irradiation by stellar Ly$\alpha$, self-shielding in the 900–1000 Å band, and an improved implementation of photochemical heating. The Ly$\alpha$ radiative transfer is treated in a schematic way.

We find that Ly$\alpha$ irradiation is an important heat source for disk atmospheres. Our model can account for the characteristic properties of the hot H$_2$: its characteristic temperature, column density, and emitting radii. Our model and the updates to it are described in Section 2. In Section 3 we demonstrate the role of Ly$\alpha$ heating in determining the thermal and chemical structure of the atmosphere. These results are discussed in Section 4, where we also summarize our findings.

### 2. THERMAL-CHEMICAL MODEL

We use a thermal-chemical model of an X-ray and FUV irradiated disk that was most recently described in AGN14. The model builds on the work presented in Glassgold et al. (2004, 2009) and Ádámkovics et al. (2011). As described in our previous work, the disk model atmosphere has a layered structure, with a hot (~5000 K) atomic layer overlying warm (~800 K) molecular and cool (~500 K) molecular layers. The resulting properties of the model atmosphere, such as warm columns of species and their radial extent, are in good agreement with the general molecular emission properties of Spitzer spectra of protoplanetary disks (Najita et al. 2011, AGN14).

The model adopts a static disk density and dust temperature structure from D’Alessio et al. (1999), with stellar and disk parameters listed in Table 1. As in AGN14, we assume dust properties (Table 1) that take into account that large grains settle to the midplane and leave a reduced population of small grains in the atmosphere. The grain size parameter $a_g$ corresponds to a decrease in grain surface area by a factor of 20 compared to interstellar conditions, and a dust surface area per hydrogen nucleus that is $S_d \approx 8 \times 10^{-23}$ cm$^2$. A set of thermal and chemical rate equations is used to determine the gas temperature and species abundances. The primary improvements to the model are in the treatment of FUV radiation and a more complete set of photodissociation pathways that use the stellar FUV field to heat the gas. Whereas we had previously included the photodissociation of water and OH (AGN14), here we also include the FUV photochemistry of additional abundant molecules and atoms and adopt the photochemical heating rates detailed in Glassgold & Najita (2015, hereafter GN15). Most notably, we now consider the radiative transfer and photochemistry of Ly$\alpha$ as separate from the FUV continuum.

In order to explore the effect of Ly$\alpha$ radiation on the disk atmosphere, we adopt a schematic treatment of its radiative transfer (scattering and absorption) that is based on detailed work in the literature, as described below. Scattering of FUV continuum photons (mostly forward) by grains is not considered. While we find that the propagation path of Ly$\alpha$ has a significant impact on the properties of the atmosphere (Section 3), our assumptions suggest that these results should be considered illustrative rather than quantitative. An improved FUV radiative transfer that includes scattering effects in a more realistic way is needed to understand the effect of Ly$\alpha$ on the detailed properties of the atmosphere.

The model presented here suffers from some additional shortcomings. Gas pressure balance is not enforced in that our calculation of the gas temperature does not alter the density structure of the atmosphere, as in the D’Alessio et al. (1999) model. We effectively assume that dust heating dominates in determining the density structure of the atmosphere. Because the gas temperature exceeds that of the dust in the atmosphere, we therefore tend to overestimate the density. We further assume that the dust abundance and size distribution are the same at all heights and radii in the atmosphere. Transport of material (radial or vertical) is also not considered, and we assume that the chemical timescales are rapid enough that abundances and thermal rates are determined by local conditions.

These effects are also likely to be more prominent at smaller disk radii. This is particularly relevant as the dust is important for attenuating the FUV, for H$_2$ formation, and for thermal accommodation of the gas at high densities. Detailed consideration of changes in the dust profile with height, radius, and time are all very interesting and will be the subject of future work. In particular, at radii within ~0.1 AU the dust structure of the inner rim may be important for determining the radiation environment in the terrestrial planet region. For now, however, we describe a simplified treatment below.

#### 2.1. FUV Radiative Transfer and Photochemistry

Previous work in the literature serves as a valuable guide to understanding the propagation of Ly$\alpha$ in disk atmospheres. Studies have found that Ly$\alpha$ emitted by the star can be

### Table 1

| Parameter | Symbol | Value |
|-----------|--------|-------|
| Stellar mass | $M_\ast$ | $0.5 \ M_\odot$ |
| Stellar radius | $R_\ast$ | $2 \ R_\odot$ |
| Stellar temperature | $T_\ast$ | 4000 K |
| Disk mass | $M_D$ | 0.005 $M_\ast$ |
| Dust to gas ratio | $\rho_d/\rho_g$ | 0.01 |
| Dust grain size | $a_g$ | 0.7 μm |
| Dust extinction | $Q_{ext}$ | 1.0 |
| X-ray temperature | $T_X$ | 1 keV |
| X-ray luminosity | $L_X$ | $2 \times 10^{39}$ erg s$^{-1}$ |
| FUV continuum luminosity$^a$ | $L_{\text{FUV}}$ | $1 \times 10^{33}$ erg s$^{-1}$ |
| Ly$\alpha$/FUV continuum$^b$ | $\eta$ | 3 |
| Accretion heating | $\alpha_a$ | 0.5 |

Notes.

$^a$ The FUV continuum luminosity is integrated from 1100 to 2000 Å and excludes Ly$\alpha$, so that it is smaller than the value used in AGN14.

$^b$ The ratio of the unattenuated downward Ly$\alpha$ photon number flux to the radially propagating FUV continuum number flux in 1200–1700 Å band.
scattered by intervening H I, e.g., in a wind, before it reaches the disk (Herczeg et al. 2004; Schindhelm et al. 2012). H I in the atomic layer at the disk surface will also scatter arriving Lyα photons so that they emerge roughly perpendicular to the disk surface (BB11). While a large fraction of the stellar Lyα photons may, in this way, be scattered away (reflected) from the disk, the fraction that passes through the atomic layer travels a path more directly downward into the disk, in contrast to the FUV continuum photons, which propagate at an oblique angle into the disk.

Quantitative results obtained in the earlier studies suggest a simple way to implement Lyα irradiation in our model. In their detailed Monte Carlo calculation of how Lyα photons interact with the gaseous disk, BB11 start out with a number flux of Lyα photons 6 times larger than the FUV continuum flux at the star. Upon leaving the star, Lyα photons are scattered away by intervening H I so that at the transition from atomic to molecular conditions in the disk atmosphere, the Lyα flux is roughly equal to flux of the (obliquely propagating) FUV continuum photons. A roughly similar ratio of Lyα to continuum photons is inferred observationally for the disk surface. In their analysis of the H2 fluorescence emission from CTTs, Schindhelm et al. (2012) found that the flux of Lyα incident on the fluorescing H2 layer (their $F_{ab}$) is 1.5–5 times larger than the continuum flux reaching the disk. Since some fraction of the stellar Lyα is absorbed or scattered away before reaching the fluorescing H2, the Lyα incident on the H2 is less than the stellar Lyα flux.

We therefore assume for our reference model that at the top of the atmosphere the ratio of the number flux of downward-propagating Lyα photons to the number flux of FUV continuum photons in the 1200–1700 Å band is $\eta = 3$, a value in the middle of the range reported by Schindhelm et al. (2012). We apply the methods described in AGN14 and assume a mean FUV continuum luminosity per 100 Å of $L_{\text{band}} = 1.1 \times 10^{30}$ erg s$^{-1}$. The FUV luminosities of CTTs can be an order of magnitude larger or smaller (Yang et al. 2012). The FUV continuum is absorbed by molecules and dust along the line of sight to the star. We improve on the treatment of the FUV continuum photoabsorption presented in AGN14 by treating a larger number of abundant molecules and atoms: H2, CO, N2, C, O2, NH3, HCN, CH4, C2H2, and SO2 in addition to H2O and OH.

Lyα photons are also attenuated by dust and molecules, and we incorporate, in an approximate way, scattering of Lyα by H I in the atmosphere. The scattering and absorption cross sections illustrate the relative roles of these processes for Lyα.

The UV dust absorption cross section is $8 \times 10^{-23}$ cm$^2$ per hydrogen, while the H2O absorption cross section at Lyα is $\sigma_{\text{H2O}}(\text{H}) \approx 10^{-17}$ cm$^2$ (van Dishoeck et al. 2006). For a typical water abundance of $x(\text{H2O}) \approx 10^{-4}$, $\frac{\sigma_{\text{dust}}}{x(\text{H2O})\sigma_{\text{H2O}}} \approx 0.08$. (1)

Thus, water will typically dominate the UV opacity in the molecular layer.

To compare the roles of H2O absorption and H I scattering for Lyα, we can consider a representative H I scattering cross-section. At ~80 Doppler widths (~300 km s$^{-1}$) from Lyα line center, where the Lyα line profile peaks in the spectrum of the CTTs TW Hya (Herczeg et al. 2004), the H I scattering cross section at that velocity is $\sigma_{\text{H}}(\text{H}) \approx 10^{-20}$ cm$^2$ (BB11). At the top of the molecular layer $x(\text{H})/x(\text{H2O})$ ranges from $3 \times 10^5$ to 10, so that the ratio of H I scattering to H2O absorption optical depths

$$\frac{x(\text{H})\sigma_{\text{H}}(\text{H})}{x(\text{H2O})\sigma_{\text{H2O}}} \approx 300 - 0.01. \quad \text{(2)}$$

The ratio in Equation (2) is a sensitive function of depth into the atmosphere, because $x(\text{H})$ and $x(\text{H2O})$ both depend strongly on vertical column. This comparison suggests that there may be regions where H I scattering can increase the path of Lyα photons through the absorbing medium, and can therefore increase the probability of absorption by H2O.

To include Lyα absorption and scattering in a simple way, we can consider the scattering optical depth along a path length $\ell$ through a grid cell $\tau_s = n_s \sigma_s \ell = \ell/\ell_s$, where $n_s$ and $\sigma_s$ are the number density and cross section of scatterers, and $\ell_s$ is the scattering mean free path. To traverse a distance $\ell$ via a random walk, the Lyα photons will take approximately $\tau_s^2 \ell_s$ steps. That is, scattered photons will travel a distance $\ell_{\text{eff}} = \tau_s^2 \ell_s = \tau_s \ell$ through the absorbing medium. Because of the longer path length, the effective optical depth for absorption is

$$\tau_{\text{eff}} = n_s \sigma_s \ell_{\text{eff}} = (n_s \sigma_s \ell) \tau_s = \tau_s \tau_a \quad \text{(3)}$$

where $n_s$ and $\sigma_s$ are the number density and absorption cross section of absorbers (e.g., dust or molecules) and $\tau_a = n_a \sigma_a \ell$ is the usual absorption optical depth without scattering. As a result, for each grid step in the model, we calculate the scattering optical depth as

$$\tau_s = n(\text{H}) \sigma_{\text{H}}(\text{H}) \ell_s, \quad \text{(4)}$$

where $\ell_s$ is the vertical size of the grid cell, and approximate the increased probability of absorption in the presence of scattering by multiplying the normal absorption optical depth $\tau_a$ by a factor of $\tau_s$ when the scattering is large (i.e., $\tau_s > 1$). The increase in path length leads to increased Lyα absorption, which both attenuates the Lyα and increases the photochemical and photoelectric heating by Lyα. We also assume that fluorescent excitation of hot H2 does not attenuate the Lyα, consistent with detailed modeling of UV fluorescent H2 emission, which finds that only a small fraction of the incident Lyα is processed into H2 emission (2% for TW Hya; Herczeg et al. 2004).

The photodissociation rate for species X is given as the sum of the dissociation rates from FUV continuum and Lyα photons,

$$G(X) = G_{\text{cont}} + G_{\text{Lyα}}. \quad \text{(5)}$$

The continuum rate is

$$G_{\text{cont}} = \int_{\lambda_0}^{\lambda_h} F_{\text{cont}}(\lambda) \sigma(\lambda; X) d\lambda, \quad \text{(6)}$$

where $F_{\text{cont}}(\lambda)$ is the local FUV continuum photon number flux spectrum over wavelengths $\lambda$, which has been attenuated along the line of sight to the star and $\sigma(\lambda; X)$ is the photodissociation cross section spectrum for species X. Similarly, the photorate for dissociation by Lyα is

$$G_{\text{Lyα}} = F_{\text{Lyα}} \sigma(\text{Lyα}; X), \quad \text{(7)}$$

where $F_{\text{Lyα}}$ is the downward propagating Lyα number flux, and $\sigma(\text{Lyα}; X)$ is the photodissociation cross section for species X.
at Lyα. References for the cross sections used here are given in Table 2.

The opacity of the 911–1108 Å band is dominated by the abundant species H2, CO, N2, and C. Most importantly, H2, CO and N2 absorb via lines and thus self- and mutually shield one another, as well as all other species. They therefore require detailed treatment of their opacity. Being the most abundant, H2 is the most important absorber in the 911–1108 Å band. We use the H2 shielding function given by Draine \& Bertoldi (1996).

\[
J(H_2) = \frac{0.965}{1 + x/b_5^a} + \frac{0.035}{\sqrt{1 + x}} e^{-8.5 \times 10^{-4} / \sqrt{1 + x}},
\]

where \( x \equiv N(H_2) / 5 \times 10^{14} \text{ cm}^{-2} \), \( b_5 \equiv b / 10^5 \text{ cm s}^{-1} \), and the Doppler broadening parameter is \( b = 3 \text{ km s}^{-1} \). The original expression used \( \alpha = 2 \) and applied to temperatures up to 300 K. Wolcott-Green \text{ et al.} (2011) determined the shielding function in a 3D model and considered temperatures up to 10^3 K. They found that using \( \alpha = 1.1 \) gives a better parameterization of the shielding at high temperatures, which we use here in calculating \( J(H_2) \).

Tabulations of the shielding by CO as a function of \( N(H_2) \) and \( N(\text{CO}) \) are provided by Visser \text{ et al.} (2009) for a set of Doppler widths, excitations temperatures, and isotopologue ratios.\(^3\) We use the table for the conditions that most closely approximate the conditions in the molecular region of the disk, \( b(\text{CO}) = 0.3 \text{ km s}^{-1} \), \( T_{\text{ex}}(\text{CO}) = 100 \text{ K} \), and \( ^{12}\text{CO} / ^{13}\text{CO} = 69 \), to lookup the CO shielding function \( J(\text{CO}) \). Similarly, Li \text{ et al.} (2013) provide the shielding functions for N2, and we use the shielding functions \( J(N_2) \) tabulated for \( b(H_2) = 3.0 \text{ km s}^{-1} \), \( b(N_2) = 0.77 \text{ km s}^{-1} \), \( T_{\text{ex}}(N_2) = T_{\text{ex}}(H_2) = 1000 \text{ K} \), and \( N(\text{H}) = 10^{22} \text{ cm}^{-2} \).

For H2, CO, and N2, the first (continuum) term in the expression for \( G(X) \) is decreased according to the shielding factors described above, as well as by all other continuum absorbers including dust grains. The absorption spectrum of C in the 911–1108 Å band is essentially continuum absorption, and for large \( N_\text{H} \), the molecular hydrogen shielding occurs in the far line wing, which covers a significant fraction of continuum. Therefore, H2 may shield the ionization of atomic carbon, and so we estimate the attenuation of \( G(C) \) by a factor of \( J(H_2) \), defined in Equation (8).

2.2. X-Rays with Compton Scattering

The theory for X-ray ionization presented in Ádámkovics \text{ et al.} (2011) and implemented in AGN14, uses a single temperature X-ray spectrum, and considers only the absorption of X-rays. Studies by Ercolano \& Glassgold (2013), using a 3D radiative transfer and photoionization code with Compton scattering together with a more realistic two-temperature X-ray spectrum, show that ionization rates can be factors of several larger at low densities (and smaller at high densities) in the disk atmosphere than in our earlier calculations. Ercolano \& Glassgold (2013) tabulate ionization rates calculated with depleted ISM elemental abundances for X-ray spectra that match the observations of the Chandra Orion Ultradeep Project (COUP). Since we consider the same disk density structure, we scale total ionization rates in Ádámkovics \text{ et al.} (2011) to match Ercolano \& Glassgold (2013) at each altitude in the model, and we use this scaling to calculate the shell-specific ionization rates.

2.3. Thermal Processes: Photochemical Heating by Lyα

Our thermal model includes the heating processes described in Glassgold \text{ et al.} (2004) and AGN14: X-ray heating, accretion-related mechanical heating, thermal accommodation between gas and dust, grain photoelectric heating, photochemical heating by H2O and OH, and H2 formation heating. In addition we include photochemical heating for C, H2, CO, H2O, and OH following GN15, as well as O2, which is described in the Appendix. We do not calculate the photochemical heating for NH3, HCN, CH4, C2H2, and SO2 due to their small abundances. We include photochemical heating for H2O and OH by Lyα photons, because these two molecules dominate the molecular opacity at Lyα. The photochemical heating from other species, which do not contribute significantly to the Lyα opacity, are ignored. Line cooling is essentially the same as in our earlier work and includes H1 recombination lines, Lyα, H2, vibrational and rotational transitions, CO rovibrational and pure rotational transitions, H2O vibrational and rotational transitions, and O1 forbidden and fine structure transitions. Above the atomic to molecular transition, Lyα cooling dominates and is supplemented at the transition by CO rovibrational, dust-gas and O1 forbidden-line cooling.

In the prescription given in AGN14 for the chemical heating associated with the photodissociation of water and OH, roughly half of the photon energy in excess of the dissociation energy was converted to heating, primarily through collisions of the dissociation products. GN15 provide a more detailed description of the energetics of the dissociation products of these and other molecules and the thermal energy that could potentially be produced in their subsequent chemical reactions. The total heating due to the photodissociation of species X, \( Q(X) \), is the sum of the direct heating component, \( Q_{\text{dir}}(X) \), which arises from the translational energy of the dissociation products, and the chemical heating component, \( Q_{\text{chem}}(X) \), which arises from the excitation of the products and their subsequent chemical reactions. The heating rate per photodissociation of each species is the sum of the heating by FUV continuum photons, \( Q_{\text{cont}}(X) \), and by Lyα photons, \( Q_{\text{Lyα}}(X) \),

\[
\Gamma_{\text{phchem}} = Q_{\text{cont}} n Q_{\text{cont}} + Q_{\text{Lyα}} n Q_{\text{Lyα}},
\]

where \( n \) is the volumetric number density of a particular species, having dropped the X from the notation.

Water and OH are the dominant sources of opacity for Lyα in the molecular layer as well as the dominant sources of photochemical heating. The photodissociation of H2O by Lyα has three possible product channels (Harich \text{ et al.} 2000), which were used in GN15 to calculate FUV continuum dissociation at wavelengths below 1450 Å (their Band 2). In this band, GN15 obtained direct and chemical heating energies of \( Q_{\text{dir}} = 0.24 \text{ eV} \) and \( Q_{\text{chem}} = 0.86 \text{ eV} \), respectively, for very high densities. We can apply the continuum results of GN15 that were based on experiments for Lyα photodissociation by simply raising the mean energy used in the GN15 treatment (9.67 eV), to the Lyα photon energy of 10.2 eV. For Lyα dissociation of H2O, \( Q_{\text{dir}} \) becomes 0.8 eV and the total photochemical heating is \( Q_{\text{Lyα}}(\text{H}_2\text{O}) = Q_{\text{dir}} + Q_{\text{chem}} = 1.6 \text{ eV} \). Similarly, we can recalculate the heating per OH dissociation in GN15 using the 10.2 eV Lyα photon instead of the mean FUV continuum photon energy. Taking...
3. RESULTS

We calculate the vertical (altitude) structure of abundances \( x \), and gas temperature \( T_g \), at radial distances of 0.24, 0.48, and 0.95 AU, which are characteristic of the emitting regions inferred from \( \text{H}_2 \) line widths in CTTS (France et al. 2012, Table 4). Although many thermal processes are considered here, in general only a few play major roles in the disk atmosphere. For example, in the low density layer just above the atomic to molecular transition, accretion heating is balanced by Ly\( \alpha \) cooling, but cooling by CO rovibrational emission and \( \text{H}_2 \) formation heating are also important. The dominant heating mechanisms are plotted as a function of the vertical column density of hydrogen from the top of the disk atmosphere \( N_H \) in Figure 1, along with the Ly\( \alpha \) and FUV continuum fluxes, for a radial distance of \( r = 0.24 \) AU.

As shown in Figure 1, heating by \( \text{H}_2 \), \( \text{OH} \), and \( \text{H}_2 \) formation dominates other heating mechanisms at the top of molecular layer (\( \log N_H = 21.5 - 21.7 \) \( \text{cm}^{-2} \)) and raises the temperature of the molecular gas above 1500 K. These heating processes can each exceed mechanical and photoelectric heating. The \( \text{H}_2 \) formation heating in the warm molecular layer is actually photochemical in origin, as discussed in GN15. Deeper into the molecular layer the FUV radiation (both continuum and Ly\( \alpha \)) is shielded by both dust and molecules and neither mechanism has an important role in heating the atmosphere.

Figure 2 shows the vertical profiles of key molecular abundances and temperatures plotted for the reference model (solid curves), and for comparison we also show the results for a model without Ly\( \alpha \) (dotted curves), which are essentially the same as our earlier reference model (i.e., the top left panel of Figure 5 in AGN14). In the absence of Ly\( \alpha \), there is a steep transition to peak \( x(\text{H}_2) \) and peak \( x(\text{H}_2\text{O}) \) near \( \log N_H = 21.4 \) \( \text{cm}^{-2} \) and after the transition there is a steady decline in gas temperature and \( x(\text{OH}) \) with increasing \( N_H \). Thus
as in earlier models, the disk atmosphere is characterized by a hot (∼5000 K) atomic layer that overlies a cooler (∼1000 K) molecular layer. The region between these two layers is where the role of FUV radiation and photochemistry is most important, with the strength of the radiation field determining whether there is a sharp or a gradual transition from atomic to molecular conditions (AGN14).

As illustrated by our reference model with Lyα (solid curves in Figure 2), Lyα radiation is important for both heating the gas and photodissociating molecules near the transition. With Lyα included, the transition occurs deeper than with FUV continuum radiation alone, and e.g., the abundance of molecules such as H₂ and H₂O are reduced near log N_H ≈ 21.6 cm⁻². This is similar to the effect of increasing the FUV continuum luminosity when Lyα is absent (Figure 4 in AGN14). Since the vertical optical depth of the atmosphere is roughly an order of magnitude less than the line of sight optical depth, the downward propagating Lyα penetrates deeper into regions of higher density than the FUV continuum, which travels along an oblique line of sight from the star. In contrast to our models without Lyα, the gas temperature T_g in our reference model increases with vertical column N_H after the transition, from log N_H = 21.5 through 21.7 cm⁻² as a result of photochemical heating by Lyα. The red shaded region in Figure 2 highlights the layer of hot molecular gas, where T_g is 1500–2500 K. The total column of H₂ in this region is 4.9 × 10¹⁹ cm⁻². In the absence of Lyα, the gas temperature is much lower, and there is no region of the atmosphere where H₂ is both abundant and hot.

The depth to which the FUV penetrates determines where hot molecular gas is present. As a result, the total column of hot molecular gas is sensitive to the magnitude of the FUV. Since we assume that the downward Lyα number flux is a factor of η = 3 larger than the FUV continuum number flux at the top of the atmosphere (see Section 2.1), an order of magnitude increase in the FUV continuum leads to an order of magnitude more Lyα and produces a factor of ∼4 times more hot H₂ (Table 3) at 0.24 AU. Increasing Lyα also leads to higher temperatures at larger radii. While there is no significant column of hot H₂ in the reference model at r = 0.48 AU (with L_{FUV} = 10³¹ erg s⁻¹), and order of magnitude increase in F_{Lyα} leads to significant columns (>10¹⁹ cm⁻²) of hot gas out to 0.48 AU in the disk.

On the other hand, a reduction in the FUV radiation has an even more dramatic effect on the column of hot molecular gas. We varied the radiation by decreasing both the FUV continuum and Lyα; we also removed Lyα entirely by setting F_{Lyα} = 0. In either case, the column of hot H₂ drops significantly. In models with either L_{FUV} = 10³⁰ erg s⁻¹ or no Lyα, the maximum temperature in the irradiated molecular layer is below 1500 K, and the column of hot H₂ is four decades smaller (Table 3). In these cases, the only region of the atmosphere where T_g > 1500 K is in the hot atomic layer, where x(H₂) ≲ 10⁻⁵. As a result of the small abundance of H₂, the total column of hot H₂ in the atomic layer is only ∼10¹⁵ cm⁻². This is the characteristic minimum value in Table 3 that indicates the lack of a hot molecular region. While both FUV continuum and Lyα are important for heating, the absence of a hot molecular region when Lyα is removed—while the FUV continuum is maintained—suggests that Lyα plays a more important role than the continuum in producing hot molecular gas. Again, this is because the downward propagating Lyα photons penetrate deeper than the continuum.

### Table 2

| Species | σ_{Lyα}^2 | Q_{opt} | References |
|---------|-----------|---------|------------|
| H₂O     | 2.1       | 1.6     | 1          |
| OH      | 5.5       | 6.4     | 2          |
| O₂      | 6.3       | ...     | 3          |
| H₂      | 12.5      | ...     | 4          |
| CO      | 8.7       | ...     | 5          |
| C       | 8.0       | ...     | 6          |
| N₂      | ...       | ...     | 7          |

**Notes.**

a Units for photochemical heating energies are eV per photodissociation and cross sections are in 10⁻¹⁸ cm².

b The species that contribute to FUV continuum photochemical heating have numerical values in second column, Q_{FUV}, and those considered for Lyα photochemical heating have values listed in the third column for Q_{Lyα}.

c Lyα cross sections from van Dishoeck et al. (2006). The molecules that cannot be dissociated from their ground state by Lyα do not have cross sections listed.

d References for FUV continuum cross sections: (1) Lee & Suto (1986), Parkinson & Yoshino (2003), Mota et al. (2005), (2) van Dishoeck & Dalgarno (1984), (3) Yoshino et al. (1992, 2005). References for line shielding: (4) Draine & Bertoldi (1996), (5) Visser et al. (2009), (6) McGuire (1968), (7) Li et al. (2013).

### Table 3

| Calculation | Parameters^b |
|-------------|--------------|
|             | α_{Lyα} a_{Lyα} a_{Lyα} L_{FUV} |
|             | 0.24 0.48 0.95 |
| Reference   | 3.6(15) 3.1(15) 3.8(15) 0.50 0.71 |
| Reduced     | 1.9(20) 3.6(19) 4.5(15) 0.50 0.71 |
| Larger      | 7.3(19) 6.0(15) 8.0(15) 0.50 0.71 |
| Reduced     | 1.2(15) 2.2(15) 1.6(15) 0.50 0.70 |
| Larger      | 1.4(15) 1.6(15) 2.0(15) 0.50 0.70 |
| Reduced     | 3.4(20) 9.9(18) 2.4(15) 0.50 0.70 |
| Larger      | 3.9(19) 5.8(19) 2.5(16) 0.50 0.70 |
| No Lyα      | 9.5(19) 3.8(19) 3.3(19) 0.50 0.70 |

**Notes.**

a Column densities for gas temperatures T > 1500 K in units of cm⁻², with values above 10¹⁵ cm⁻², which indicate a hot H₂ region, highlighted in bold.

b Parameter units: a_{Lyα} is the dimensionless accretion-related mechanical heating parameter; a_{Lyα} is the grain size parameter in μm; and L_{FUV} is the FUV continuum luminosity in erg s⁻¹.

c The reference model that is plotted for r = 0.24 AU in the figures.
The depth to which Ly\(\alpha\) photons penetrate depends on scattering in the hot molecular region. To illustrate the role of scattering we considered a case of pure absorption, i.e., only dust and molecular absorption and no H\(_2\) scattering, which leads to the deepest penetration of radiation (black dotted curve in the bottom panel of Figure 1) and nearly an order of magnitude increase in the columns of hot H\(_2\) than when scattering is included (Table 3). The column of hot H\(_2\) is also sensitive (obviously) to \(\eta = F_{\text{Ly}\alpha}/F_{\text{cont}}\) at the top of the atmosphere (Figure 3). When Ly\(\alpha\) is reduced by a factor of 3 relative to our reference model (setting \(\eta = 1\)) the gas is heated to barely above 1500 K. An increased value of \(\eta = 5\) results in a higher peak temperature for the hot H\(_2\) and deeper penetration of the radiation into the disk.

Two other parameters in the model that are generally important for heating are the accretion-related mechanical heating parameter \(\alpha_h\), defined in Glassgold et al. (2004), and the dust grain size parameter, \(a_g\). Mechanical heating is the dominant heating term deep in the disk and in the hot atomic region, while dust-gas thermalization is the dominant cooling mechanism at large column densities. Table 3, which shows the hot H\(_2\) columns for cases with reduced \(\alpha_h\), larger \(a_g\), or a combination of the two, illustrates the sensitivity of our results to these parameters. Effectively eliminating mechanical heating by reducing \(\alpha_h = 0.01\) does not reduce the column of hot H\(_2\) (Table 3). This is because mechanical heating is subdominant to photochemical heating and H\(_2\) formation heating in the region of hot H\(_2\) (Figure 1). Indeed, reducing \(\alpha_h\) decreases the heating of the atomic layer, so that the transition from atomic to molecular conditions occurs at a higher altitude in the disk atmosphere (Figure 4). Models with smaller \(\alpha_h\) therefore have columns of hot H\(_2\) that are somewhat larger than the reference model, by a factor of \(\sim 50\%\) (Table 3).

The dust in the atmosphere plays competing roles as an important opacity source for the FUV, as the catalyst for H\(_2\) formation and therefore H\(_2\) formation heating, and as an important coolant via thermal accommodation in regions of high density. Increasing the grain size parameter, \(a_g\), reduces the surface area and opacity of the dust, reduces H\(_2\) formation heating, and allows the FUV to penetrate deeper into the disk. With larger dust grains, the transition from atomic to molecular conditions occurs at a lower altitude in the disk atmosphere, where the densities are higher (AGN14). For the reference FUV continuum luminosity \((L_{\text{FUV}} = 10^{31} \text{erg s}^{-1})\) and large grains...
(a_g = 7.07 μm), the transition is from hot atomic conditions to cool, fully molecular conditions, and there is no region of hot H_2. However, models with increased radiation as well as with large grains produce the largest columns of hot H_2 (Table 3), as the irradiated molecular layer occurs deeper into the disk (Figure 4). The details of the dominant thermal and chemical changes due to variations in α_h, a_g, and L_{FUV} are complex. However, as these parameter variations illustrate, hot H_2 columns \( \sim 10^{19} \text{ cm}^{-2} \) are a common outcome for a range of \( a_g \) and \( \alpha_h \) values.

4. DISCUSSION

We find that including Lyα in our earlier model of a disk atmosphere irradiated by FUV continuum and X-rays (AGN14) produces a new component of the inner disk atmosphere: a region of hot molecular gas (1500–2500 K; Figure 2). The reason for the difference is related to the distinctive radiative transfer and propagation path of the Lyα photons more than to their luminosity. Although the Lyα component is much more luminous than the FUV continuum in the present case, the total FUV luminosity (continuum + Lyα) is similar to that assumed in AGN14. More significantly, the Lyα fraction of the FUV luminosity propagates more directly downward through the disk compared to the FUV the continuum, which propagates along an oblique line of sight into the disk. As shown in Table 3, a hot molecular component occurs under a wide range of conditions. The column density of hot H_2 is insensitive to the value of the mechanical heating parameter \( \alpha_h \). Column densities of hot H_2 > \( 10^{19} \text{ cm}^{-2} \) are obtained for a range of FUV luminosities, i.e., FUV continuum luminosities 0.0025–0.025 \( L_\odot \). Large column densities are also found when both the grain size parameter and mechanical heating are reduced.

The FUV continuum luminosities we considered span the middle to upper range among TTS (Yang et al. 2012) and are consistent with the properties of sources with well-studied hot H_2 (France et al. 2012; Schindhelm et al. 2012). The properties of the hot H_2 found in the models (temperature, column density, radial distance) are similar to those inferred for the UV fluorescent molecular hydrogen emission from TTS. For example, in their study of H_2 emission from TW Hya, Herczeg et al. (2004) inferred an excitation temperature of \( T_{\text{ex}} = 2500 (+700/-500) \text{ K} \), an H_2 column density of \( \log N(\text{H}_2) = 18.5(+1.2/-0.8) \text{ cm}^{-2} \), and constrained the source of the emission to radial distances within 2 AU. Schindhelm et al. (2012) reported similar conditions for the UV fluorescent H_2 emission from a larger sample of TTS (\( T(\text{H}_2) = 2500 \pm 1000 \text{ K} \), \( \log N(\text{H}_2) = 19 \pm 1 \text{ cm}^{-2} \)). The H_2 line profiles reported in France et al. (2012) for single, normal (non-transition) TTS suggest that the emission arises typically from radii \( \sim 0.1-1 \text{ AU} \).

In the above studies, the TTS that show fluorescent H_2 emission include sources that have experienced significant grain settling relative to ISM values. The Taurus sources in Schindhelm et al. (2012) span a range of 10 μm silicate emission equivalent widths (0.22–1.0) and MIR colors (\( n_{1-25} = -0.4-0.2 \); Furlan et al. 2006), which are consistent with grain area reduction by a factor \( \sim 100 \). The best fits in the Herczeg et al. (2004) modeling of the fluorescent H_2 emission from TW Hya have the H_2 mixed with little dust compared to an ISM grain abundance (they assumed no dust). These conditions are similar to the reduced grain area adopted in our models.

The hot H_2 occurs in a region that is primarily atomic, \( x(\text{H}_2)/x(\text{H}) < 0.1 \), and mixed with a high abundance of water, \( x(\text{H}_2\text{O}) \sim 10^{-5} \). Thus, both scattering and photochemical heating are important in this region of the atmosphere. Interestingly, Lyα reconstruction studies typically assume that the UV fluorescent H_2 occurs in a region with little H_1 (Herczeg et al.; Schindhelm et al.). Our results suggest that H_1 scattering could play a larger role, potentially increasing the likelihood of Lyα excitation of hot H_2, similar to the increased probability of Lyα absorption by dust or water when H_1 scattering occurs.

As noted in France et al. (2012), the UV fluorescent H_2 emission profiles indicate that the emission arises from similar disk radii as the CO rovibrational emission from disks (Salyk et al. 2011, e.g.). Our model also produces an enhanced column density of hot (\( T > 900 \text{ K} \)) CO, with columns in the \( 10^{17}-10^{18} \text{ cm}^{-2} \) range, generally from within 1 AU. For models with large grain sizes (\( a_g = 7.07 \mu m \)) in the upper range of UV luminosity (\( L_{\text{FUV}} = 0.025 L_\odot \)), a significant fraction of radiation penetrates deep into the disk and we see columns of up to \( \sim 2 \times 10^{18} - 8 \times 10^{18} \text{ cm}^{-2} \) of hot CO within 0.5 AU (Figure 4). These values compare favorably to the CO rovibrational emission properties of T Tauri disks (e.g., Najita et al. 2003). Salyk et al. (2011) reported line of sight CO emission columns of \( 10^{18}-10^{19} \text{ cm}^{-2} \) and excitation temperatures of 900–1600 K for a sample of Taurus disks; the small CO emitting areas and the width of the emission lines are consistent with much of the emission arising from \( <0.4 \text{ AU} \).

Thus, the enhanced hot H_2 and CO that we find in the hot atomic and warm irradiated layers of our model may help to explain the UV fluorescent H_2 and CO rovibrational emission that is commonly observed from T Tauri disks.

The study by Nomura et al. (2007) provides an interesting counterpoint to the current study. In their pioneering work on the excitation of H_2 in disks, Nomura et al. (2007) illustrated how protoplanetary disks that are irradiated by stellar UV and X-rays could produce detectable H_2 emission at UV and IR wavelengths. There are many differences between the two models, e.g., the chemical model used here is more detailed and molecular shielding is included, but hydrostatic equilibrium is not enforced and the H_2 level populations are not calculated. However, one of the most interesting differences between the two models is the way in which the stellar UV heats the gas. In Nomura et al. (2007), the gas is heated by UV photons through grain photoelectric heating. As grains settle out of the disk atmosphere, grain photoelectric heating is reduced, the temperature of the gaseous atmosphere drops, and the H_2 emission declines in strength. These results led Nomura et al. to conclude that H_2 emission will be strongest from disks with an abundant small grain population, i.e., disks that have experienced little grain growth and settling. In contrast, H_2 emission is detected commonly from TTS, the majority of which have experienced significant grain settling.

In our model, UV photons heat the gas primarily through photodissociation of OH and H_2O. While photoelectric heating is included in our calculation, it plays a limited role because of the reduced abundance of small grains in the atmosphere. In this way, heating by UV remains strong even as grains settle out of the atmosphere. Indeed, as the grains settle, the FUV...
radiation penetrates deeper, and larger columns of hot H$_2$ and CO are produced.

Our models complement the disk model of Du & Bergin (2014) in both the methods employed and the astrophysical issues that are addressed. In Du & Bergin (2014), Ly$\alpha$ propagation is treated in a much more sophisticated way and photochemical heating is included in a simplified way compared to the methods used here. As in AGN14, Du & Bergin (2014) focussed on the distribution of warm water and primarily on the region $>1$ AU in contrast to the smaller radii considered here. While Du & Bergin (2014) did not address in their work the origin of fluorescent H$_2$, the methods used in their work could be used to investigate this question in greater detail.

In summary, we find that the Ly$\alpha$ component of the FUV radiation field of young stars has a significant impact on the thermal structure of disk atmospheres. Ly$\alpha$ photons scattered by H$_2$ at the top of the disk atmosphere deposit their energy deeper in the disk atmosphere than radially propagating FUV continuum photons. In addition, scattering by H$_2$ throughout the upper disk atmosphere can cause much of the Ly$\alpha$ energy to be deposited over a restricted range in column density, which leads to a surface layer of hot H$_2$. The temperature in the layer is high enough ($\sim$2000 K) to thermally excite the H$_2$ to vibrational levels from which they can be fluoresced by Ly$\alpha$ to produce the UV fluorescent H$_2$ emission that is characteristic of accreting young stars. Ly$\alpha$ irradiation also leads to a layer of warm CO ($>900$ K) in the inner disk atmosphere that has a column density similar to that inferred for 4.7 $\mu$m rovibrational CO emission from young stars. The high H$_2$ and CO temperatures are primarily the result of photochemical heating (by H$_2$O, OH and H$_2$ formation), a process that offers an efficient way to tap energy of the stellar UV field when grains have settled out of disk atmospheres and photoelectric heating is diminished.

We have investigated the impact of Ly$\alpha$ heating on a particular disk atmosphere model. Given the significant impact of Ly$\alpha$ irradiation on the thermal structure of the disk atmosphere, it is important to examine its role relative to other processes over a range of disk radii. More generally, we have investigated the impact of Ly$\alpha$ heating in the context of one particular disk atmosphere model. Further studies of the impact of Ly$\alpha$ heating under a wider range of disk conditions would be useful to understand the general nature of this process.

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APPENDIX

FUV PHOTOCHEMICAL HEATING OF O$_2$

The photochemical heating discussed in Section 2 is based on GN15. However, the examples treated there do not include O$_2$ which can play a significant role in the FUV heating of the molecular layer. The photochemical heating defined in Equation (1) is composed of a direct and a chemical part,

$$Q_{\text{phchem}} = Q_{\text{dir}} + Q_{\text{chem}} \tag{10}$$

where $Q_{\text{dir}}$ comes from the kinetic energy of the dissociation fragments (two O atoms in this case), and $Q_{\text{chem}}$ from their chemical energies. As emphasized by GN15, photochemical heating is dependent on the density because some of it arises from excitation of the products and only leads to heating if the density is high enough for collisional de-excitation of the excited levels to occur. In the present application to the molecular layer, the densities are high enough ($>10^{10}$ cm$^{-3}$) that it is a good approximation to assume that essentially all excitation goes into heating.

The UV absorption cross section of O$_2$ is well known. It is dominated by the Schumann–Runge continuum from 1300-1800 Å, well measured by Yoshino et al. (2005). Over much of this band, one of the atoms is produced in the $^2$D$_2$ level (Lee & Nee 2000, 2001). Following GN15, we assume that all of the excitation energy, $E(D_2^2) = 1.98$ eV, is available for heating. Below 1400 Å, the branching ratio $b$ for the $^2$D$_2$ level is less than one, but this only reduces the mean heating from its collisional de-excitation by $\sim10\%$. The $^1$S$_0$ level at 4.19 eV is also produced below 1100 Å, but it quickly decays to the $^2$D$_2$ level. In any case, these wavelengths are heavily blocked by H$_2$ and CO self-shielding, and we ignore O$_2$ heating in the 900-1100 Å band.

The direct heating has been obtained by calculating the mean value of the quantity,

$$\Delta E_{\text{dir}} = h\nu - D(O_2) - b E(D_2^2), \tag{11}$$

in each of ten 100 Å bands from 1100 to 2400 Å; the dissociation energy of O$_2$ has been set to $D(O_2^2) = 5.12$ eV, and the mean value of $b$ is $b = 0.90$. The result is $Q_{\text{dir}} = 1.6$ eV. The chemical energy is obtained from the reactions, initiated by each O atom,

$$O + H_2 \rightarrow OH + H, \tag{12}$$

and,

$$OH + H_2 \rightarrow H_2O + H, \tag{13}$$

which are equivalent to,

$$O + 2H_2 \rightarrow H_2O + 2H, \tag{14}$$

with a net energy yield of 0.57 eV. Thus the net chemical energy is $Q_{\text{chem}} = 2(0.57 + b \times 1.98)$ eV or 4.7 eV, and the total photochemical heating is $Q_{\text{phchem}}(O_2) = 6.3$ eV. For the same conditions, the photochemical heating of H$_2$O and OH are 2.1 and 5.5 eV, respectively. The heating rates in Figure 1 reflect these values together with the abundances of the oxygen molecules.

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