Mitigation of Torsional Vibrations in a Modular Drivetrain with Interleaving Control

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Abstract: In order to meet requirements in machine design, modularity is often brought forward as a way to cope with load variations and adaptability of the architecture. The considered modular drivetrain consists of several identical induction motors, called motor modules, in cascade on the same shaft. However, implementing a modular drivetrain design evidently has an impact on the performance of the application. New opportunities may arise, such as improved motion dynamics and tolerance to failures. However, on other aspects, e.g., torsional vibrations and synchronization, performance can be negatively influenced. By adding multiple actuators in the drivetrain, additional sources of torque ripple are introduced. The aim of this article is first to investigate the impact of using a modular design on the torsional vibrations in the drivetrain, and second to mitigate these vibrations via an interleaving strategy of the PWM (pulse-width modulation) signals. Simulations and experimental data show that the modular setup requires a proper control strategy in order to ensure that the torsional vibrations in the system remain within the range of a traditional non-modular design. Interleaving of the PWM carrier waveforms in the different motor modules is proposed as a control method to mitigate the torsional vibrations identified in the modular drivetrain. This strategy results in a drivetrain setup that slightly outperforms the benchmark in terms of torsional vibrations.

Keywords: modular drivetrain; torsional vibration; interleaving control

1. Introduction

During the design of industrial machines, the objective and performance are often strictly defined [1]. In order to achieve optimal machine performance, process rates and load cases need to be kept tightly within that design range. Within those set boundaries, alterations to the process are usually difficult. Because industrial applications show a trend towards more customization [2], there is a need for more flexible drivetrain solutions. Flexibility means that such drivetrain solutions should enable the easy creation of different power or speed variants without the need to design a new motor each time.

Modularity seems a promising solution to handle the request for flexibility and to combat the constraints in traditional machine design [3,4]. While the design process could benefit from a modular approach, modularity impacts drivetrain performance.

Torsional vibrations are important factors in many mechatronic processes, impacting machine performance [5], and therefore design. The influence of torsional vibrations on the lifetime, cost, and performance of a drivetrain has been demonstrated in [6,7]. When using a modular setup, the behaviour of the system towards torsional vibrations is affected by this design. In [8], the negative effects of cascaded motors regarding torsional oscillations was explored. Through the use of a soft start mechanism, oscillations during start-up were suppressed. This paper investigates the effect on torsional vibrations of switching to a modular drivetrain.
1.1. Modularity

A modular drivetrain is often defined as a configuration of individual mechatronic function modules, where each part of the mechatronic application is expressed as a module. Power electronics, electrical machines, and mechanical systems are in this case seen as individual modules [1,9]. The overall drivetrain consists of a combination of several modules, as proposed by [4,10]. The use of this definition of modularity has already been widely implemented in many industrial applications, including weaving looms [11], crane applications [12], electric vehicles [13–15], and power electronics [16].

In these examples of modularity, the mechatronic system is built as a combination of several unique modules. However, [17] introduced the concept of defining an identical modular module that is repeated several times to form the drivetrain. The module consists of an electric motor, a power electronic converter to control the motor, and part of the mechanical drivetrain, which can interact with other modules and/or the load application. For larger load cases, several modules can be coupled to create the desired sizing of the drivetrain. The benefits of using this modular approach were researched by [18], and promising results regarding motion dynamics and tolerance to failures were found.

1.2. Torsional Vibrations

Torsional vibrations can have negative consequences on drivetrain performance. Efforts to mitigate these vibrations can be realized through either passive or active means [19]. Passive approaches use the inertial and/or damping properties of the drivetrain to dissipate the vibrations. This includes introducing series elasticity [20], viscous damping [21], flywheels [22], or centrifugal pendulum absorbers [23] in the drivetrain. Passive methods can, however, lead to increased energy consumption [7], reduce the system dynamics, or only work within a narrow frequency range [24].

Active methods, on the other hand, try to weaken the undesired vibrations through controller strategies. Control methods are usually based on state feedback or adaptive filters [25,26]. An active magnetic bearing was used in [27] to reduce vibrations with overhung rotors. In many cases, however, torsional displacement is not easily measured in the drivetrain. Torque sensors are expensive, and not easily mounted in a transmission. In [28], model-based estimators were used as a virtual sensor. Active vibration damping methods have already been implemented in hybrid electric powertrains [19] and electric vehicles [29,30]. The above-mentioned techniques, however, always consider a single source of vibrations, and therefore are not readily applicable in the modular approach.

In the modular drivetrain design, multiple identical motors are used. As electromechanical actuators are a source of torque ripple [31–33], the modular approach requires attention to torsional vibrations. Efforts to mitigate the resulting torsional vibrations in a modular drivetrain are investigated here. In [34], interleaving was proposed to reduce torque ripple in a multiphase motor. In this paper, the interleaving strategy is implemented to reduce torque ripple across several cascaded actuators in a modular drivetrain.

A use case for the modular design approach where torsional vibrations are of importance can be found in applications where a long shaft is used for power transfer, for example, a weaving loom. The driveshaft of a weaving loom is driven by one or more motors [11]. A common issue with these machines is torsional vibration across the shaft, resulting in desynchronization of the weaving process; [35,36] studied the shaft’s torsional dynamics regarding the shaft penetration factor and transient stability, while [37,38] have proposed reducing the vibrations across a shaft by modeling a predictive control and adjustable speed control. However, this research involves a single input–single output drivetrain, and thus is not directly applicable to a modular drivetrain. Synchronization of actuators was explored in [39,40], although focusing on speed and angular position synchronization, not on the induced torque ripple. Another use case for a modular approach is electric vehicles. While multi-motor drive systems have already been used in this context, the focus in the literature to date has mainly been on torque distribution [41] and energy management optimization [42].
1.3. Outline of This Paper

The aim of this article is, first, to investigate the impact of using a modular design on the torsional vibrations in the drivetrain, and second, to mitigate these vibrations using an interleaving strategy of the PWM signals. Weaving looms and electric vehicles have been introduced as excellent examples that could benefit from a modular approach; however, they are complicated drivetrains with many factors that influence the behaviour of the application. In order to demonstrate the use of modularity and the effect on torsional vibrations, a simplified drivetrain is presented. In Section 2, the mechanical modular drivetrain used in our research is explained. Section 3 elaborates on the motor model and shows simulation results regarding the performance with respect to the torsional vibrations of the modular drivetrain. The interleaving control strategy used to mitigate the assessed negative impact of using a modular drivetrain is explained in Section 4. In order to support the claimed simulation results, the results of validation measurements are provided in Section 5. Section 6 discusses the presented simulations and measurements, and Section 7 concludes with an overview of the findings.

2. Mechanical Driveline

Modularity was previously defined as a system that consists of modules that are repeated several times. In this case, the module, or component block, is composed of an electrical and a mechanical element. The electrical part consists of an asynchronous motor with a speed and current cascade controller and power electronic inverter to generate the PWM signals for motor control. The mechanical element is a shaft interconnected with couplings to link the modules together. The mechanical driveline, illustrated in Figure 1, is created with two modular modules and a load. A third induction motor is used to generate the load torque. The inertia of the motor represents the load inertia. The modelling was carried out in Matlab/Simscape. $J$, $k$, $b$ represent the component’s inertia, stiffness and damping, respectively; the subscripts $M_i$, $L_i$, $C_i$, and $S_i$ indicate the used component, i.e., the motor, load, coupling, or shaft, respectively; $T$ shows the torque; and $\theta$ shows the position of the motors and load.

![Figure 1. Dynamic model of the drivetrain.](image)

2.1. Dynamic Model

The dynamic behaviour of the mechanical components of the driveline was modelled by taking the inertia, stiffness, and damping of each element into account. The component flexibilities were implemented for each coupling and shaft as a two-inertia–spring–damper system. This method was chosen over more complex methods such as FEM because it provides an adequate representation and reduces calculation effort. The motor shaft inertias were modelled as well. The torsional flexibility of the motor shaft is not taken into account here, as torsional displacement is not expected at the motor shaft.

The model proposed in Figure 1 results in a seven-inertia system. While describing such a model is possible, it unnecessarily increases calculation time. Because the goal was to model the modular drivetrain, each module was simplified to an inertia–spring–damper system. The model can thus be rewritten as a three-inertia system, two modules, and a load, as illustrated in Figure 2. This simplification was carried out according to (1), and the approach is further validated in Section 2.2, where it is shown that the drivetrain indeed acts as a three-inertia system.
The simplified 3DOF (degrees of freedom) model can then be described with the equations of motion (2), similar to the 2DOF model presented by [43]. It is important to note that this model assumes linear system behaviour. High torsion amplitudes and torsion moments, where the behaviour becomes non-linear, are not taken into account.

\[
\begin{align*}
T_{M1} &= J_1 \ddot{\theta}_{M1} + b_1(\dot{\theta}_{M1} - \dot{\theta}_{M2}) + k_1(\theta_{M1} - \theta_{M2}) \\
T_{M2} &= J_2 \ddot{\theta}_{M2} - b_1(\dot{\theta}_{M1} - \dot{\theta}_{M2}) - k_1(\theta_{M1} - \theta_{M2}) + b_2(\dot{\theta}_{M2} - \dot{\theta}_L) + k_2(\theta_{M2} - \theta_L) \\
T_L &= J_3 \ddot{\theta}_L - b_2(\dot{\theta}_{M2} - \dot{\theta}_L) - k_2(\theta_{M2} - \theta_L)
\end{align*}
\]  

(2)

The eigenvalues \(\lambda_1, \lambda_2,\) and \(\lambda_3\) can be calculated with the free vibration system of (2) according to (3) [44]:

\[
det [J^{-1} K - \lambda I] = 0
\]  

(3)

\(J, K,\) and the inertia and stiffness matrices are described in (4), and \([I]\) is an identity matrix.

\[
J = \begin{bmatrix} J_1 & 0 & 0 \\ 0 & J_2 & 0 \\ 0 & 0 & J_3 \end{bmatrix}, \quad K = \begin{bmatrix} k_1 & -k_1 & 0 \\ -k_1 & k_1 + k_2 & -k_2 \\ 0 & -k_2 & k_2 \end{bmatrix}
\]  

(4)

From the eigenvalues, the undamped natural frequencies \((f_1, f_2, f_3)\) of the system can be found with (5). For this system, the undamped natural frequencies, calculated with the values from Table 1, are found at 0, 74, and 161 Hz:

\[
f_i = \sqrt{\frac{\lambda_i}{2\pi}}
\]  

(5)

In order to use the dynamical model, the parameters from (1) must be specified. Inertia and stiffness values are easily calculated or found in datasheet information. The damping parameters can be calculated according to (6). However, implementing the correct damping ratio \(\xi\) is difficult. Therefore, in order to properly implement damping into the dynamical behaviour of the mechanical model, a test setup was used to identify the parameters of the dynamic system through frequency response analysis, converting (2) to a transfer function model. After Laplace transformation and implementing Cramer’s rule, the relations between torques and angular speeds are provided in (7), with \(s\) the complex variable in...
the complex frequency domain. The transfer functions \((G_{ij})\) are described in Appendix A Equation (A1):

\[
b_i = \frac{\xi k_i}{\pi f_i}
\]

\[
\begin{align*}
\dot{\theta}_{M1}(s) &= G_{11}(s)T_{M1}(s) + G_{12}(s)T_{M2}(s) + G_{13}(s)T_L(s) \\
\dot{\theta}_{M2}(s) &= G_{21}(s)T_{M1}(s) + G_{22}(s)T_{M2}(s) + G_{23}(s)T_L(s) \\
\dot{\theta}_L(s) &= G_{31}(s)T_{M1}(s) + G_{32}(s)T_{M2}(s) + G_{33}(s)T_L(s)
\end{align*}
\]

2.2. Dynamical Behaviour Validation

To obtain proper damping characteristics, frequency response measurements were performed with the setup shown in Figure 3, built up in the same manner as the schematic model from Figure 1. The first module has a steel shaft with a diameter of 18 mm and a length of 108 mm. The second module uses a torque sensor (Lorenz DR-2112) as a shaft. All components are connected with backlash-free servo couplings (KTR Radex-NC). The motor in the first module is equipped with an encoder to measure angular position.

The system transfer function, represented by a Bode plot, was identified using the Matlab Signal processing toolbox. A random uniformly-distributed torque signal at motor M1 was used as the input signal, while the encoder speed was used as the output. This makes it possible to estimate the system transfer function, \(G_{11}(s)\), in (7). During this measurement, motor M2 and the load motor are not energized, and remain connected. In this way, the mechanical system stays identical. Performing this experiment to identify one transfer function provides enough information to estimate all functions. While different excitations propagate differently, the identification is unchanged.

![Figure 3. Test setup used for experimental validation: left, the mechanical drivetrain; right, the inverters and data acquisition system.](image)

A random torque signal with a magnitude of 20% of the nominal motor torque was applied on motor M1 through field-oriented control. A uniformly distributed random offset of \(\pm 3.5\%\) was used. A 1 ms sampling time was used. By fitting the damping ratio, \(\xi\), in (6), the damping behaviour of the model can be closely matched to the real setup. Small alterations to the parameters found in the component datasheets were made to fine-tune the model further. The final model parameters used after fitting are listed in Table 1.

In Figure 4, the Bode plots from physical measurement and the theoretical model are compared with each other. It is clear that the measured and estimated transfer functions have a similar characterization, with the system resonance modes at 74 and 161 Hz. Note that the measured frequencies above 200 Hz show high oscillations. This is caused by the limitations of the measurement method, and does not properly represent the actual behaviour.
Table 1. Mechanical model parameters after identification.

| Parameter | Value  |
|-----------|--------|
| $J_1$ [kgm$^2$] | 0.0121 |
| $J_2$ [kgm$^2$] | 0.0123 |
| $J_3$ [kgm$^2$] | 0.0495 |
| $k_1$ [Nm/rad] | 4350 |
| $k_2$ [Nm/rad] | 5144 |
| $b_1$ [Nms/rad] | 0.116 |
| $b_2$ [Nms/rad] | 0.134 |

Figure 4. System identification Bode measurement and simulation with random torque input at motor M1 and measured speed output at M1. Measurement with a sample time of 1 ms; resonance modes of the system at 74 and 161 Hz.

3. Motor Control

To model the asynchronous motors, we used an available motor model according to (8) in Matlab/Simscape Electrical [45]. The standard two level inverter was modelled as depicted in Figure 5. The inverter had a switching frequency of 4 kHz. A field-oriented control was used for each motor. Current control was individual for each module. A PI cascade controller was used for speed regulation. Both modules share the same speed feedback from the encoder positioned at motor M1, as shown in Figure 3.

\[
\begin{align*}
    v_{ds} &= \frac{1}{\omega_{base}} \frac{d\psi_{ds}}{dt} - \omega \psi_{qs} + R_s i_{ds} \\
    v_{qs} &= \frac{1}{\omega_{base}} \frac{d\psi_{qs}}{dt} - \omega \psi_{ds} + R_s i_{qs} \\
    v_{bs} &= \frac{1}{\omega_{base}} \frac{d\psi_{bs}}{dt} + R_s i_{qs} \\
    v_{dr} &= \frac{1}{\omega_{base}} \frac{d\psi_{dr}}{dt} - (\omega - \omega_r) \psi_{qr} + R_r i_{dr} = 0 \\
    v_{qr} &= \frac{1}{\omega_{base}} \frac{d\psi_{qr}}{dt} - (\omega - \omega_r) \psi_{dr} + R_r i_{qr} = 0 \\
    \psi_{ds} &= L_{ss} i_{ds} + L_m i_{dr} \\
    \psi_{qs} &= L_{ss} i_{qs} + L_m i_{qr} \\
    \psi_{bs} &= L_{ss} i_{qs} \\
    \psi_{dr} &= L_{rr} i_{dr} + L_m i_{ds} \\
    \psi_{qr} &= L_{rr} i_{qr} + L_m i_{qs} \\
    T &= \psi_{ds} i_{qs} - \psi_{qs} i_{ds}
\end{align*}
\]

With $v_{ds}$, $v_{qs}$, and $v_{bs}$ the d-axis, q-axis, and zero-sequence stator voltages, $v_{dr}$ and $v_{qr}$ the d-axis and q-axis rotor voltages, $\psi_{ds}$, $\psi_{qs}$, and $\psi_{bs}$ the d-axis, q-axis and zero-sequence
stator flux linkages, $\psi_{dr}$ and $\psi_{qr}$ the d-axis and q-axis rotor flux linkages, $i_{ds}$, $i_{qs}$, and $i_{0s}$ the d-axis, q-axis, and zero-sequence stator currents, $i_{dr}$ and $i_{qr}$ the d-axis and q-axis rotor currents, $R_s$ and $R_r$ the stator and rotor resistance, $L_{ss}$ and $L_{rr}$ the stator and rotor inductances, $L_m$ the magnetizing inductance, and $T$ the rotor torque. An overview of the parameters can be found in Table 2.

![Power electronics model in Simscape](image)

**Figure 5.** Power electronics model in Simscape.

| Parameter | Value |
|-----------|-------|
| $R_s$ [$\Omega$] | 0.625 |
| $R_r$ [$\Omega$] | 0.469 |
| $L_{ss}$ [mH] | 57.0 |
| $L_{rr}$ [mH] | 55.4 |
| $L_m$ [mH] | 54.1 |

**Table 2.** Motor model parameters.

The motor model does not take any efficiency losses or slot harmonics into account. However, a power electronic inverter with sinusoidal PWM introduces an electromagnetic torque ripple that causes an exciting force on the mechanical drivetrain.

To showcase this, simulations with the model were carried out. Steady state behaviour at a constant speed of 500 rpm was studied. A 5 Nm load was set at the load motor. In the modular scenario, both motors M1 and M2 are used and share the load. In Figure 6, the frequency spectrum of the torque input from motor M2 during the modular scenario is shown. A torque ripple at the PWM switching frequency of 4 kHz is visible. An excitation of the first mechanical resonance, at 74 Hz, is visible as well. For motor M1, similar behaviour is observed.

![Simulated torque output from motor M2 during the synchronized control modular scenario](image)

**Figure 6.** Simulated torque output from motor M2 during the synchronized control modular scenario.
To evaluate the performance of the modular setup, a benchmark scenario was chosen. Here, only motor M1 is energized and carries the load. Motor M2 remains mechanically connected in order to maintain the same mechanical drivetrain, and is not used. In Figure 7a the torque at the load during the benchmark is shown. The high-frequency torque ripple at 4 kHz is dampened by the mechanical system, and only a vibration at the resonance frequency remains. The torque ripple has an amplitude of 0.24 Nm. When observing the same signal during the modular scenario, as depicted in Figure 7b, the ripple increases by 91% to 0.46 Nm. Furthermore, a harmonic of the resonance frequency (2·\(f_N\)) emerges. It can thus be concluded that the use of a modular setup has a negative effect on the torsional vibration behaviour of the drivetrain. An effort to reduce this torque ripple is necessary in order to keep the modular drivetrain design competitive with traditional machine performance.

![Figure 7. Simulated torque ripple amplitude monitored at the load in (a) the benchmark scenario, 0.24 Nm at the resonance mode; (b) the modular scenario, 0.46 Nm; (c) the modular scenario with interleaving control, 0.20 Nm.](attachment:image.png)

4. Interleaving for Mechanical Resonance Reduction

The proposed technique to mitigate the negative impact on the electromagnetic torque produced by the current ripple due to the PWM modulation involves interleaving of the PWM carrier waveforms in the different motor modules. Interleaving has previously been used to control the torque ripple at the PWM frequency of a multiphase motor in [33,34]; by taking a two-segmented motor system and implementing a phase-shift in the PWM generation of one of the segments, the torque ripple was reduced. The impact on the driven mechanics was not analysed.

In the present paper, however, two standard three-phase induction motors were used. A phase-shift between the PWM generation of both motors is proposed, as shown in Figure 8. The torque ripple of each motor is thus not altered, and the impact on the mechanical system level can be investigated. The idea here was to delay the PWM carrier of motor M2 relative to motor M1, thereby offsetting the torque oscillation with respect to motor M1 and bringing both ripples into counter-phase.
4.1. Theoretical Impact of Interleaving on Mechanical Resonances

To investigate the functionality of interleaving, a transfer function model of the mechanical drivetrain was created according to (9) in order to describe the relationship between the input torques of the motors and the output torque at the load. The model consisted of two transfer functions; $G_1(s)$ describes the behaviour of a torque input at motor M1 to the load output, while $G_2(s)$ describes the same for a torque input at motor M2. For a linear system, adding both outputs provides the total torque output of the system. The Bode characteristics of both transfer functions are shown in Figure 9; the transfer functions are described in Appendix A Equation (A3).

$$T_{out} = G_1(s) * T_{M1} + G_2(s) * T_{M2}$$ (9)

The goal of using an interleaving strategy is to impact the behaviour at the mechanical resonance frequencies. For the first mode, at 74 Hz, both signals are equally amplified and in phase; thus, if the phase of one of the signals is shifted 180 degrees, both signals at 74 Hz will counteract one another. However, for the second mode, at 161 Hz, both signals are already in counter-phase. The shift will therefore cause the signals to amplify each other. Because the impact at the lower frequency has been shown to be more common, this possible benefit is more advantageous than the drawback at the second resonance mode. At the PWM frequency of 4 kHz, both transfer functions weaken the input signal significantly, and show little impact on the output.
To confirm this approach, the interleaving strategy was first used on a simple sinusoidal input. Both motor inputs received a sinusoidal input according to (10) with a frequency of 4 kHz and amplitude of 10 Nm, while the torque at the load was monitored. The torque input signal of motor M2 was shifted by an angle $\phi$, and the impact of this shift was observed.

\[
\begin{align*}
T_{M1} &= A \sin(\omega t) \\
T_{M2} &= A \sin(\omega t + \phi)
\end{align*}
\]  

(10)

In Figure 10, the result when $\phi = 0$ is shown. Both signals are synchronized. It can be seen that this results in a transient oscillation at the mechanical resonance frequencies of the system; the 4 kHz is weakened by the mechanics. After the transient period, a small oscillation at 4 kHz remains, and no effect is visible at the mechanical resonance frequency.

The interleaving strategy, with $\phi = \pi$, is shown in Figure 11. Here, similar behaviour is visible. After the transient phase, the resonance oscillations die out. Only the weakened sinusoidal input remains. Again, in the steady state of the simulation no effect of the interleaving strategy is visible, as the high frequency is significantly weakened by the mechanical structure. The benefit of the interleaving strategy is visible in the transient phase of this simulation. Using this technique, the oscillation is much smaller in amplitude at the first resonance mode and slightly increased at the second mode, as would be expected by observing the bode characteristics in Figure 9. It can therefore be concluded that the interleaving strategy only has a beneficial impact on the mechanical resonance of the system during transient behaviour.

In this implementation of interleaving, a delay of half the signal frequency was chosen. To determine whether or not this was the optimal choice, different delay lengths were compared. In Figure 12, the amplitude of the first resonance mode is compared for various values of $\phi$ from 0 to $2\pi$. By shifting the second motor signal with a varying offset, a clear minimum was found at half the signal frequency.
4.2. Implementation of Interleaving Control on a Modular Drivetrain

In the modular drivetrain under consideration, the PWM generation for the power electronic inverters is the source of the torque ripple; a ripple in the motor current is thereby produced, which in turn results in a ripple in the torque generation. This creates a mechanical resonance oscillation in the drivetrain, even in steady state speed conditions. Therefore, the interleaving strategy could improve the behaviour of the drivetrain and counteract these oscillations.

Figure 7c shows the load torque output during the simulation of the modular drivetrain when the interleaving control strategy is used. Here, the torque ripple is reduced to 0.20 Nm, which is 17% lower than during the benchmark scenario. With this simulation, it can be concluded that the interleaving control strategy has a similar impact on the modular drivetrain, as outlined in Section 4.1. The oscillations from both motor inputs
are brought into counterphase through the interleaving control, and the overall impact at the first resonance mode is thus reduced. However, it should be noted that when using the interleaving control strategy, a harmonic of this resonance frequency \((2^*f_N)\) becomes more pronounced. The harmonic \((2^*f_N)\) oscillation is increased because this frequency is close to the second resonance mode, and therefore the two oscillations are brought back into phase with each other by interleaving, as illustrated in Figure 9. The impact on the system is therefore increased. Based on these simulation results, it can be concluded that the interleaving control strategy improves the torsional vibration behaviour of a modular design, and makes it competitive with a traditional machine design regarding this performance indicator.

The previous simulations were carried out with a controller PWM switching frequency of 4 kHz. This was chosen to match the operating conditions of the setup used in Section 5. However, modern power electronics make it possible to run a motor controller at higher PWM switching frequencies. In order to evaluate the impact of the PWM switching frequency on the torsional vibrations in a modular drivetrain, the simulations showcased in Figure 7 were repeated with a switching frequency of 10 kHz.

In these simulations, it was observed that the overall torque ripple introduced by the motors had a smaller amplitude. As the PWM switching frequency increases, the resulting motor current ripple decreases. Therefore, the resulting torque ripple can be expected to be smaller. Figure 13 shows the frequency spectrum of the torque input from motor M2. The 10 kHz switching frequency is clearly present, though with a 60% smaller amplitude when compared to the simulations at 4 kHz in Figure 6.

![Figure 13. Simulated torque output from motor M2 during the synchronized control modular scenario with a switching frequency of 10 kHz.](image)

The comparison between the benchmark and modular drivetrains at 10 kHz is illustrated in Figure 14. Similar to the previous simulations shown in the modular scenario without any form of torque ripple control, there was a 36% increase in torsional vibrations at the first resonance. When implementing the interleaving control strategy, these vibrations were reduced by 81% compared with the benchmark, a much better result than the 17% reduction simulated at 4 kHz. This indicates that a modular drivetrain design could have a significant beneficial effect on torsional vibrations over traditional designs.
Figure 14. Simulated torque ripple amplitude at 10 kHz PWM switching frequency in (a) the benchmark scenario, 0.11 Nm at the resonance mode; (b) the synchronized control modular scenario, 0.15 Nm; (c) the interleaving control modular scenario, 0.02 Nm.

5. Experimental Validation
5.1. Setup
The simulation results comparing the modular drivetrain design against the benchmark were experimentally validated using the setup shown in Figure 3. Two 3 kW induction motors were used as the motor modules, while the third, a 5.5 kW induction motor, functioned as the load. The load motor was driven through a Siemens Sinamics industrial drive, while the modular motors were driven through two Semikron Semiteach inverters. A dSPACE Microlabbox was used to operate the setup. Field-oriented motor control, including speed and current feedback and PWM generation for the two modular motors, was implemented on the Microlabbox. In this manner, interleaving was implemented in the setup. The motor currents of the two modular motors were measured through six current sensors. An incremental encoder at the first motor was used for speed feedback. A load torque setpoint was communicated over CAN to the Siemens Sinamics S120 drive. The experiment was performed at 500 rpm with a load of 5 Nm. Steady state behaviour was analysed through a torque sensor (Lorenz DR-2112).

5.2. Measurements
In Figure 15a, the frequency spectrum of the measured load torque during the benchmark testing is shown. Here, only motor 1 was used to drive the load; while motor two was mechanically connected, it was not energized. The first mechanical resonance is clearly triggered with an amplitude of 0.21 Nm. The second resonance is not significantly influenced. Other frequencies, at 55 Hz and 60 Hz, are present; however, as these change at different speeds, it can be concluded that this was caused by noise and/or imbalances in the mechanical setup. The focus is therefore on the resonance frequencies.

When comparing this benchmark result to the synchronized modular setup, as depicted in Figure 15b, it can be clearly seem that the mechanism is triggered more significantly. The first resonance frequency now has an amplitude of 0.34 Nm, an increase of 62% compared to the benchmark measurement. Furthermore, the second resonance is clearly visible. This results in a less desirable drivetrain, similar to the simulations.

When implementing the interleaving strategy, the mechanical resonances are reduced, as shown in Figure 15c. The first resonance is reduced to 0.19 Nm, 10% below the original benchmark result. The second resonance, however, is not significantly impacted by the
interleaving control when compared to the synchronized modular setup. The negative impact from interleaving in simulations at the second resonance mode is thus not observed.

Figure 15. Measured torque ripple amplitude at 4 kHz PWM switching frequency in (a) the benchmark scenario, 0.21 Nm at the resonance mode; (b) the synchronized control modular scenario, 0.34 Nm; (c) the interleaving control modular scenario, 0.19 Nm.

As stated in Section 4.1, an interleaving control strategy provides an improvement in the functionality of the modular drivetrain regarding torsional vibrations. The best result was found with a delay of half the switching frequency, as shown in Figure 12. In order to validate that the optimum is indeed found when using a delay of half the switching frequency of the drive, the interleaving control was repeated with different delays. In Figure 16, the results with various delays are shown. Experimentally, the minimum was again found when using half the switching time.

Figure 16. Torque amplitude measured at the first resonance mode with different delay times of the interleaving control.
6. Discussion

The goal of this paper is to investigate the impact of a modular design on the torsional vibrations in the drivetrain. A negative impact is observed in the modular design when no control measures were used. Interleaving is proposed as a control strategy to mitigate this negative impact. Table 3 summarizes the most important findings of this paper with respect to interleaving in modular drivetrains. The measured drivetrain performance is in line with the simulated behaviour. Overall torsional vibrations at the resonance frequency are slightly lower than in the simulations, e.g., 0.21 Nm measured vs. 0.24 Nm simulated in the benchmark scenario. The behaviour of the modular drivetrain with synchronized control did not impact the performance as negatively as was expected from simulation. Nevertheless, an increase in vibrations of 62% was observed, which is unacceptable. Interleaving proved an effective method to mitigate this negative impact, and reduced the vibrations by 10% compared to the benchmark.

Validation of the simulations using a PWM switching frequency of 10 kHz was not possible due to the limitations of the setup. However, because simulations with a PWM switching frequency of 4 kHz can properly represent the measured behaviour, it is assumed that the simulations with a PWM switching frequency of 10 kHz conducted with the same model represent a decent portrayal of the expected behaviour, thus demonstrating that if a higher switching frequency is used, the interleaving strategy can act as an active method to dampen torsional vibrations in the mechanical drivetrain.

The performed simulations and measurements were focused on the available setup. The results, however, are not limited to this particular drivetrain, and are more widely applicable in modular systems. The above-mentioned examples, such as weaving looms and electric vehicles, likewise face challenges with torsional vibrations. For each drivetrain that can be modelled with the presented model in Figure 2, the technique of interleaving can be implemented in these applications and should result in similar improvements in drivetrain performance concerning torsional vibrations.

Table 3. Torque ripple amplitude at the resonance mode comparing simulations with a PWM switching frequency of 4 and 10 kHz with measurements at a PWM switching frequency of 4 kHz.

|                  | Simulated 4 kHz | Measured | Simulated 10 kHz |
|------------------|----------------|----------|-----------------|
| Benchmark        | 0.24 Nm        | 0.21 Nm  | 0.11 Nm         |
| Modular, synchronized | 0.46 Nm (+91%) | 0.34 Nm (+62%) | 0.15 Nm (+36%) |
| Modular, interleaving  | 0.20 Nm (−17%) | 0.19 Nm (−10%) | 0.02 Nm (−81%) |

The presented results used steady-state conditions, i.e., constant speed and constant load torque, to evaluate the performance of a modular drivetrain. In subsequent research, more dynamic load cases might be investigated. Implementing a variable load that changes with angular position and/or using varying speed conditions could further highlight the benefits of a modular drivetrain over traditional machine designs in more industry-relevant operational conditions.

7. Conclusions

Modularity is presented in the literature as a novel approach to machine drivetrain design. It shows promising results in creating machines that are more easily adapted to varying load cases. However, using a modular setup has an impact on the performance of the drivetrain. This paper presented the torsional vibrations behaviour of a simplified modular setup. A model of a mechanical drivetrain and electric drives was used to simulate drivetrain behaviour in order to investigate this issue. It was determined that a modular
system introduces a negative impact on the drivetrain’s torsional vibrations if the control of the modular drivetrain is not properly implemented.

Interleaving was proposed as a control method to mitigate the negative impact created by the additional source of torque ripple in modular drivetrains. Simulations and experimental validation demonstrated that a modular drivetrain with interleaving control is able to match and even outperform the set benchmark scenario. Therefore, it is concluded that modular drivetrains show competitive potential compared to traditional designs with respect to the issue of torsional vibration.

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Appendix A. Transfer Functions

The system transfer functions used in (7):

\[
\begin{align*}
G_{11}(s) &= \frac{\theta_{M1}(s)}{\omega_{M1}(s)} = \frac{J_2 J_3 s^4 + (J_2 b_2 + J_1 (1 + b_2)) s^3 + (J_2 k_2 + b_1 b_2 + J_3 (k_1 + k_2)) s^2 + (b_1 k_2 + b_2 k_1) s + k_1 k_2}{\Delta_1} \\
G_{12}(s) &= \frac{\theta_{M2}(s)}{\omega_{M2}(s)} = \frac{J_2 b_1 s^3 + (J_2 k_1 + b_1 b_2) s^2 + (b_1 k_2 + b_2 k_1) s + k_1 k_2}{\Delta_1} \\
G_{13}(s) &= \frac{\theta_{M3}(s)}{\omega_{M3}(s)} = \frac{b_1 b_2 s^2 + (b_1 k_2 + b_2 k_1) s + k_1 k_2}{\Delta_1} \\
G_{21}(s) &= \frac{\theta_{M2}(s)}{\omega_{M1}(s)} = G_{12}(s) \\
G_{22}(s) &= \frac{\theta_{M2}(s)}{\omega_{M2}(s)} = \frac{J_1 J_3 s^4 + (J_2 b_2 + J_1 (1 + b_2)) s^3 + (J_2 k_2 + J_3 (1 + b_2)) s^2 + (b_1 k_2 + b_2 k_1) s + k_1 k_2}{\Delta_1} \\
G_{23}(s) &= \frac{\theta_{M3}(s)}{\omega_{M2}(s)} = \frac{J_1 b_2 s^3 + (J_2 k_2 + J_3 (1 + b_2)) s^2 + (b_1 k_2 + b_2 k_1) s + k_1 k_2}{\Delta_1} \\
G_{31}(s) &= \frac{\theta_{M1}(s)}{\omega_{M3}(s)} = G_{13}(s) \\
G_{32}(s) &= \frac{\theta_{M2}(s)}{\omega_{M3}(s)} = G_{23}(s) \\
G_{33}(s) &= \frac{\theta_{M3}(s)}{\omega_{M3}(s)} = \frac{J_1 J_2 s^4 + (J_2 b_2 + J_1 (1 + b_2)) s^3 + (J_2 k_1 + J_3 (1 + b_2)) s^2 + (b_1 k_2 + b_2 k_1) s + k_1 k_2}{\Delta_1}
\end{align*}
\]

With \( \Delta_1 \):

\[
\Delta_1 = J_1 J_2 J_3 s^5 + (J_3 b_1 (1 + J_1) + J_1 b_2 (J_2 + J_3)) s^4 + (J_3 k_1 (J_1 + J_2) + J_1 k_2 (J_2 + J_3) + b_1 b_2 (J_1 + J_2 + J_3)) s^3 + (b_1 k_2 + b_2 k_1) (J_1 + J_2 + J_3) s^2 + k_1 k_2 (J_1 + J_2 + J_3) s
\]

The transfer functions used in (9):

\[
\begin{align*}
G_1(s) &= \frac{\omega_{out}(s)}{\omega_{M1}(s)} = \frac{J_1 b_1 b_2 s^2 + f_1 (b_1 k_1 + b_2 k_2) s + J_1 k_1 k_2}{\Delta_2} \\
G_2(s) &= \frac{\omega_{out}(s)}{\omega_{M2}(s)} = \frac{J_1 J_3 b_2 s^3 + (J_1 J_3 k_1 + J_3 b_1 b_2) s^2 + f_1 (b_1 k_2 + b_2 k_1) s + J_3 k_1 k_2}{\Delta_2}
\end{align*}
\]

With \( \Delta_2 \):

\[
\Delta_2 = J_1 J_2 J_3 s^4 + (b_2 (J_1 J_2 + J_1 J_3) + b_1 (J_1 J_3 + J_2 J_3)) s^3 + (k_2 (J_1 J_2 + J_1 J_3) + k_1 (J_1 J_3 + J_2 J_3) + b_1 b_2 (J_1 + J_2 + J_3)) s^2 + (b_1 k_2 + b_2 k_1) (J_1 + J_2 + J_3) s + k_1 k_2 (J_1 + J_2 + J_3)
\]
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