Abstract
This paper presents our approach to the problem of single sentence summarisation. We investigate the use of Singular Value Decomposition (SVD) to guide the generation of a summary towards the theme that is the focus of the document to be summarised. In doing so, the intuition is that the generated summary will more accurately reflect the content of the source document. Currently, we operate in the news domain and at present, our summaries are modelled on headlines. This paper presents SVD as an alternative method to determine if a word is a suitable candidate for inclusion in the headline. The results of a recall based evaluation comparing three different strategies to word selection, indicate that thematic information does help improve recall.

1 Introduction
In the midst of a plethora of archived electronic documents, the successful completion of a research task is affected by the ease with which users can quickly identify the relevant documents that satisfy their information needs. To do so, a researcher often relies on generated summaries that reflect the contents of the original document.

We explore the problem of generating a single sentence summary in the context of single document summarisation. Instead of identifying and extracting the most important sentence, we generate a new sentence from scratch. Thus, the resulting sentence summary may not occur verbatim in the source.

As a precursor to single sentence summarisation, we first explore the particular case of headline generation in the news domain, specifically English news. Our system re-uses words from the news article to generate a single sentence summary that resembles a headline. This is done by iteratively selecting a word from the source article and then appending it to previously selected words. This approach has been explored by a number of researchers (e.g., see Witbrock and Mittal, 1999; Jin and Hauptmann, 2002). In existing approaches, a word is selected on the basis of two criteria: how well it acts as a summary word, and how grammatical it will be given the preceding summary words that have already been chosen. Our approach uses Singular Value Decomposition (SVD) in the first criterion, as a means of determining if a word is a good candidate for inclusion in the headline.

In this paper, we present an overview of our basic summarisation algorithm in Section 2. Section 3 examines limitations of the basic algorithm, illustrating how words can be used out of context, resulting in factually incorrect statements. This is the motivation of our SVD extension which is introduced conceptually in Section 4. Section 5 describes how we generate sentence summaries using SVD. In Section 6, we present our experimental design in which we
evaluated our approach, along with the results and corresponding discussion. Section 7, provides an overview of related work. Finally, in Section 8, we present our conclusions and future work.

2 Searching for a Probable Headline

We re-implemented the work described in Witbrock and Mittal (1999) to provide a single sentence summarisation mechanism. For full details of their approach, we direct the reader to their paper (Witbrock and Mittal, 1999). For an overview of our implementation of their algorithm, see Wan et al. (2003). For convenience, a brief description is presented here.

In a search, \( n \) words are selected on the basis of the two criteria. Conceptually, the task is twofold. Witbrock and Mittal (1999) label these two tasks as Content Selection and Realisation. Each criterion is scored probabilistically, whereby the probability is estimated by prior collection of corpus statistics.

To estimate Content Selection probability for each word, we use the Maximum Likelihood Estimate (MLE). In an offline training stage, the system counts the number of times a word is used in a headline, with the condition that it occurs in the corresponding news article. To form the probability, this frequency data is normalised by the number of times the word is used in articles across the whole corpus. This particular strategy of content selection, we refer to this as the Conditional probability. The Realisation criterion is determined simply by the use of bigram statistics, which provides an approximation of grammatical correctness when ordering selected words.

3 The Veracity of Generated Summaries

Berger and Mittal (2000) describe limitations of headlines generated by recycling words from the article. Differences in word order (for example, if the subject and object are reversed) can drastically affect sentence meaning.

However, we believe that the veracity of the generated sentence, with respect to the original document, is affected by a more basic problem than variation in word order. Because words from any part of a source document can be combined probabilistically, there is a possibility that words can be used together out of context. We refer to this as Out-of-Context error. Figure 1 presents an example of a generated headline in which the verb wrongly reports stock price movement. It also presents the actual context in which that verb was used.

| Generated headline | Actual headline: |
|--------------------|-----------------|
| “singapore stocks shares rebound” | “Singapore shares fall, seen higher after holidays.” |

| Original context of use of ‘rebound’: |
| “Singapore shares closed down below the 2,200 level on Tuesday but were expected to rebound immediately after Chinese Lunar New Year and Muslim Eid Al-Fitr holidays, dealers said.” |

Figure 1. An error in the generated headline due to a word being re-used out of context.

Out-of-Context errors arise due to limitations in the two criteria (presented in Section 1) for selecting words. Word selection is based on the previous usage of a word in headlines, not on its relevance to the current document being summarised. In addition, word order is modelled probabilistically using ngrams of lexemes. However, the semantic relationship implied by probabilistically placing two words next to each other, for example an adjective and a noun, might be suspect. As the name “Out-of-Context” suggests, this is especially true if the words were originally used in non-contiguous and unrelated contexts. This limitation in the word selection criteria can be characterized as being due to a lack of long distance relationship information.

4 Our Approach to “Encouraging Truth”

In response to this limitation, we explore the use of a matrix operation, Singular Value Decomposition (SVD) to guide the selection of words. Although our approach still does not guarantee factual correctness with respect to the source document, it has the potential to alleviate the Out-of-Context problem by improving the selection criteria for including words in the generated sentence, by considering the original contexts in which words were used. With this improved criteria, we hope to "encourage truth" by incorporating long distance relationships.
between words. Conceptually, SVD provides an analysis of the data which describes the relationship between the distribution of words and sentences. This analysis includes a grouping of sentences based on similar word distributions, which correspond to what we will refer to here as the main themes of the document. By incorporating this information into the word selection criteria, the generated sentence will "gravitate" towards a single theme. That is, it will tend to use words from that theme, reducing the chance that words are placed together out of context.

Figure 2 presents an example of headlines generated with and without using SVD. The headline grammar is still problematic, however, in this example, the SVD headline is closer in meaning to the original headline. In contrast, the non-SVD headline uses words which are contentful but used out of context to form a non-meaningful string of words.

| Actual Headline: | “China says conflict with U.S. unlikely.” |
|------------------|------------------------------------------|
| First Sentence:  | “Chinese Foreign Minister Qian Qichen said on Friday conflict between China and the United States was not possible unless Washington infringed on Beijing's sovereignty or territorial integrity.” |
| Generated Headline without SVD: | “taiwan premier china visit rebel world war” |
| Generated Headline with SVD: | “china taiwan foreign minister said improved ties” |

Figure 2. An example of headlines generated with and without SVD Content Selection.

By reflecting the content of the main theme, the summary may be informative (Borko, 1975). That is, the primary piece of information within the source document might be included within the summary. However, it would remiss of us to claim that this quality of the summary is guaranteed. In general, the generated summaries are at least useful to gauge what the source text is about, a characteristic described by Borko as being indicative.

5 Using Singular Value Decomposition for Content Selection

As an alternative to the Conditional probability, we examine the use of SVD in determining the Content Selection probability. Before we outline the procedure for basing this probability on SVD, we will first outline our interpretation of the SVD analysis, based on that of Gong and Liu (2001). Our description is not intended to be a comprehensive explanation of SVD, and we direct the reader to Manning and Schütze (2000) for a description of how SVD is used in information retrieval.

Conceptually, when used to analyse documents, SVD can discover relationships between word co-occurrences in a corpus of text. For example, in the context of information retrieval, this provides one way to retrieve additional documents that contain synonyms of query terms, where synonymy is defined by similarity of word co-occurrences. By discovering patterns in word co-occurrences, SVD also provides information that can be used to cluster documents based on similarity of themes.

In the context of single document summarisation, we require SVD to cluster sentences based on similarities of themes. The SVD analysis provides information about how words and sentences relate to these themes. One such piece of information is a matrix of scores, indicating how representative the sentence is of each theme. Thus, for a sentence extraction summary, Gong and Liu (2001) would pick the top n themes, and for each of these themes, use this matrix to choose the sentence that best represents it.

For single sentence summarisation, we assume that the theme of the generated headline should match the most important theme of the article. The SVD analysis provides an ordering of themes, beginning with the one that accounts for the largest number of sentences, which we take to be the most important. The SVD analysis provides a matrix which scores how well each word relates to each theme. Given a theme, scores for each word, contained in a

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2 Theme is a term that is used in many ways by many researchers, and generally without any kind of formal definition. Our use of the term here is akin to the notion that underlies work on text segmentation, where sentences naturally cluster in terms of their ‘aboutness’.
column vector of the matrix, can then be normalised to form a probability. The remainder of this section provides a more technical description of how this is done.

To begin with, we segment a text into sentences. Our sentence segmentation preprocessing is quite simple and based on the heuristics found in Manning and Schütze (2000). After removing stop words, we then form a terms (i.e. words) by sentences matrix, A. Each column of A represents a sentence. Each row represents the usage of a word in various sentences. Thus the frequency of word \( t \) in sentence \( s \) is stored in the cell \( A_{ts} \). This gives us a \( t \times s \) matrix, where \( t \geq s \). That is, we expect the lexicon size of a particular news article to exceed the number of sentences. For such a matrix, the SVD of A is a process that provides the right hand side of the following equation:

\[
A = U \Sigma V^{\text{transpose}}
\]

where \( U \) is a \( t \times r \) matrix, \( \Sigma \) is an \( r \times r \) matrix, and \( V \) is an \( s \times r \) matrix. The dimension size \( r \) is the rank of A, and is less than or equal to the number of columns of A, in this case, \( s \). A diagram of this is presented in Figure 3.

It is important to note that the \( U \) matrix of the analysis provides information about how well words correspond to a particular theme. We examine the first column of the \( U \) matrix, sum the elements and then normalize each element by the sum to form a probability. This probability, which we refer to as the SVD probability, is then used as the Content Selection probability in the Viterbi search algorithm (Forney, 1973).

As an alternative to using the SVD probability and the Conditional Probability in isolation, a Combined Probability is calculated using the harmonic mean of the two. The harmonic mean was used in case the two component probabilities differed consistently in their respective orders of magnitude. Intuitively, when calculating a combined probability, this evens the importance of each component probability.

6 Experiments

6.1 Data

In our experiments, we attempted to match the experimental conditions of Witbrock and Mittal (1999). We used news articles from the first six months of the Reuters 1997 corpus (Jan 1997 to June 1997). Specifically, we only examined news articles from the general Reuters category (GCAT) which covers primarily politics, sport and economics. This category was chosen not because of any particular domain coverage but because other categories exhibited frequent use of tabular presentation. The GCAT category contains in excess of 65,000 articles. Following Witbrock and Mittal (1999), we randomly selected 25,000 articles for training and a further 1000 articles for testing, ensuring that there was no overlap between the two data sets. During the training stage, we collected bigrams from the headline data, and the frequency of words occurring in headlines.

6.2 Experiment Design

We conducted an evaluation experiment to compare the performance of the three Content Selection strategies that we identified in Section 5: the Conditional probability, the SVD probability, and the Combined probability. We
measure performance in terms of recall, i.e. how many of the words in the actual headline match words in the generated headline. The recall metric is normalised to form a percentage by dividing the word overlap by the number of words in the actual headline.

For each test article, we generated headlines using each of the three strategies. For each strategy, we generated headlines of varying lengths, ranging from length 1 to 13, where the latter is the length of the longest headline found in the test set. We then compared the different strategies for generated headlines of equal length.

To determine if differences in recall scores were significant, we used the Wilcoxon Matched Pairs Signed Ranks (WMPSR) test (Siegel and Castellan, 1988). In our case, for a particular pair of Content Selection strategies, the alternate hypothesis was that the choice of Content Selection strategy affects recall performance. The null hypothesis held that there was no difference between the two content selection strategies. Our use of the non-parametric test was motivated by the observation that recall scores were not normally distributed. In fact, our results showed a positive skew for recall scores. Since the Conditional strategy was found to perform better, we then compared this with the Combined strategy, as shown in Table 2. From Table 1, it is clear that, for all sentence lengths, there is a significant difference between the SVD strategy and the Conditional strategy, and so we reject the null hypothesis. Similarly, Table 2 shows that there is a significant difference between the Conditional strategy and the Combined strategy, and again we reject the null hypothesis. We conclude that SVD probability alone is outperformed by the Conditional probability; however, using both probabilities together leads to a better performance.

6.3 Results

6.3.1 Recall Comparison
The results for the comparison of recall scores are presented in Table 1 and Table 2. Table 1 shows results of the WMPSR test when comparing the SVD strategy with the Conditional strategy. Since the Conditional strategy was found to perform better, we then compared this with the Combined strategy, as shown in Table 2. From Table 1, it is clear that, for all sentence lengths, there is a significant difference between the SVD strategy and the Conditional strategy, and so we reject the null hypothesis. Similarly, Table 2 shows that there is a significant difference between the Conditional strategy and the Combined strategy, and again we reject the null hypothesis. We conclude that SVD probability alone is outperformed by the Conditional probability; however, using both probabilities together leads to a better performance.

6.3.2 Agreement between Strategies
The agreement between strategies is presented in Table 3. Interestingly, of the words recalled, the majority have only been selected by one content selection strategy. That is, the set of words recalled by one content selection strategy do not necessarily subsume the set recalled by the other. This supports the results obtained in the recall comparison in which a combined strategy leads to higher recall. Interestingly, the last column in the table shows that the potential combined recall is greater than the recall achieved by the combined strategy; we will return to this point in Section 6.4.

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3 Word overlap, whilst the easiest way to evaluate the summaries quantitatively, is an imprecise measure and must be interpreted with the knowledge that non-recall words in the generated headline might still indicate clearly what the source document is about.

4 The performance of our Conditional strategy is roughly comparable to the results obtained by Banko, Mittal and Witbrock (2000), in which they report recall scores between 20% to 25%, depending on the length of the generated headline.
1. Whilst using the Combined probability did lead to a significantly improved result, this increase in recall was only small. Indeed, the analysis of the agreement between the Conditional strategy and the SVD strategy indicates that the current method of combining the two probabilities is not optimal and that there is still considerable margin for improvement.

2. Even though the recall of the SVD strategy was poorer by only a few percent, the lack of improvement in recall is perplexing, given that we expected the thematic information to ensure words were used in correct contexts. There are several possible explanations, each warranting further investigation. It may be the case that the themes identified by the SVD analysis were quite narrow, each encompassing only a small number of sentences. If so, certain words occurring in sentences outside the theme would be given a lower probability even if they were good headline word candidates. Further investigation is necessary to determine if this is a shortcoming of our SVD strategy or an artefact of the domain. For example, it might be the case that the sentences of news articles are already thematically quite dissimilar.

3. One might also question our experimental design. Perhaps the kind of improvement brought about when using the SVD probability cannot be measured by simply counting recall. Instead, it may be the case that an evaluation involving a panel of judges is required to determine if the generated text is qualitatively better in terms of how faithful the summary is to the information in the source document. For example, a summary that is more accurate may not necessarily result in better recall. Finally, it is conceivable that the SVD strategy might be more sensitive to preprocessing stages such as sentence delimitation and stopword lists, which are not necessary when using the Conditional strategy.
Despite these outstanding questions, there are pragmatic benefits when using SVD. The conditional strategy requires a paired training set of summaries and source documents. In our case, this was easily obtained by using headlines in lieu of single sentence summaries. However, in cases where a paired corpus is not available for training, the SVD strategy might be more appropriate, given that the performance does not differ considerably. In such a situation, a collection of documents is only necessary for collecting bigram statistics.

7 Related Work

As the focus of this paper is on statistical single-sentence summarisation we will not focus on preceding work which generates summaries greater in length than a sentence. We direct the reader to Paice (1990) for an overview of summarisation based on sentence extraction. Examples of recent systems include Kupiec et al. (1995) and Brandow et al. (1995). For examples of work in producing abstract-like summaries, see Radev and McKeown (1998), which combines work in information extraction and natural language processing. Hybrid methods for abstract-like summarisation, which combine statistical and symbolic approaches, have also been explored; see, for example, McKeown et al. (1999), Jing and McKeown (1999), and Hovy and Lin (1997).

Statistical single sentence summarisation has been explored by a number of researchers (see for example, Witbrock and Mittal, 1999; Zajic et al., 2002). Interestingly, in the work of Witbrock and Mittal (1999), the selection of words for inclusion in the headline is decided solely on the basis of corpus statistics and does not use statistical information about the distribution of words in the document itself. Our work differs in that we utilise an SVD analysis to provide information about the document to be summarized, specifically its main theme.

Discourse segmentation for sentence extraction summarisation has been studied in work such as Boguraev and Neff (2000) and Gong and Liu (2001). The motivation behind discovering segments in a text is that a sentence extraction summary should choose the most representative sentence for each segment, resulting in a comprehensive summary. In the view of Gong and Liu (2001), segments form the main themes of a document. They present a theme interpretation of the SVD analysis, as it is used for discourse segmentation, upon which our use of the technique is based. However, Gong and Liu use SVD for creating sentence extraction summaries, not for generating a single sentence summary by re-using words.

In subsequent work to Witbrock and Mittal (1999), Banko et al. (2000) describe the use of information about the position of words within four quarters of the source document. The headline candidacy score of a word is weighted by its position in one of the quarters. We interpret this use of position information as a means of guiding the generation of a headline towards the central theme of the document, which for news articles typically occurs in the first quarter. SVD potentially offers a more general mechanism for handling the discovery of the central themes and their positions within the document.

Jin et al. (2002) have also examined a statistical model for headlines in the context of an information retrieval application. Jin and Hauptmann (2001) provide a comparison of a variety of learning approaches used by researchers for modelling the content of headlines including the Iterative Expectation-Maximisation approach, the K-Nearest neighbours approach, a term vector approach and the approach of Witbrock and Mittal (1999). In this comparison, the approach of Witbrock and Mittal (1999) fares favourably, ranking second after the term vector approach to title word retrieval (see Jin and Hauptmann, 2001, for details). However, while it performs well, the term vector approach Jin et al. (2002) advocate doesn't explicitly try to model the way a headline will usually discuss the main theme and may thus be subject to the Out-of-Context problem.

8 Conclusion

Combining both the SVD probability and Conditional probability marginally improves recall; lending support to the intuition that thematic information may help generate better single sentence summaries by avoiding out-of-
context errors. However, there are still many unanswered questions. In future work, we intend to investigate these techniques in a domain other than news text so that we can draw conclusions as to how well these strategies generalise to other genres. We also intend to conduct user evaluations to gauge the quality of the generated summaries for both the Conditional and the SVD strategies. Finally, we are interested in how well this approach works with other languages. Preliminary results with Chinese headline generation are promising.

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