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Citation for the original published paper (version of record):
Ramezani, Z., Lidén Eddeland, J., Claessen, K. et al (2020). Multiple Objective Functions for Falsification of Cyber-Physical Systems. IFAC-PapersOnLine, 53(4): 417-422.
http://dx.doi.org/10.1016/j.ifacol.2021.04.040

N.B. When citing this work, cite the original published paper.
Multiple Objective Functions for Falsification of Cyber-Physical Systems

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Abstract:
Cyber-physical systems are typically safety-critical, thus it is crucial to guarantee that they conform to given specifications, that are the properties that the system must fulfill. Optimization-based falsification is a model-based testing method to find counterexamples of the specifications. The main idea is to measure how far away a specification is from being broken, and to use an optimization procedure to guide the testing towards falsification. The efficiency of the falsification is affected by the objective function used to evaluate the test results; different objective functions are differently efficient for different types of problems. However, the efficiency of various objective functions is not easily determined beforehand. This paper evaluates the efficiency of using multiple objective functions in the falsification process. The hypothesis is that this will, in general, be more efficient, meaning that it falsifies a system in fewer iterations, than just applying a single objective function to a specific problem. Two objective functions are evaluated, Max, Additive, on a set of benchmark problems. The evaluation shows that using multiple objective functions can reduce the number of iterations necessary to falsify a property.

Keywords: Testing, Falsification, Multiple Objective Functions, Cyber-Physical Systems.

1. INTRODUCTION

Cyber-Physical Systems (CPSs) consist of computational parts described by state models, communicating with a physical environment described by differential equations. Using high fidelity models is typical in model-based design of CPSs. Testing and verifying the correctness of all physical and cyber components of CPSs are important and a big challenge (Abbaspour Asadollah et al., 2015). An autonomous car is an example of a CPS where it is necessary with rigorous methods to assure the correctness of the system. Typically, formal verification and/or testing are used for this purpose.

For complex systems, testing is a necessary part of the design process since formal verification of systems with a combination of discrete and continuous dynamics is an undecidable problem (Henzinger et al., 1995). However, for both formal verification and testing, formal specifications of the properties that should be fulfilled are required in order to enable an automated approach. One approach, surveyed by Bartocci et al. (2018), that can be used is formal specification of properties that the closed-loop system should satisfy, combined with simulation of models and where the given specifications are monitored and it is evaluated whether they are satisfied or not. This can be combined with falsification techniques that search for counterexamples to given specifications of the closed-loop system.

The falsification process can be based on an optimization procedure where the optimization is performed over an input parametrization expressing possible input signals. The aim is to find counterexamples, if possible, to specifications of the system under test. This is done in an iterative manner where an objective function measures the distance to the specification being falsified. The objective function is determined by the definition of quantitative semantics for temporal logic formalisms (Fainekos and Pappas, 2009). Metric Interval Temporal Logic (MITL) (Koymans, 1990) and Signal Temporal Logic (STL) (Maler and Nickovic, 2004), are two variants of formalisms for which quantitative semantics can be defined. The main purpose of calculating an objective function value is to guide the testing process towards falsification by choosing the next set of parameters for the input signals to the system being simulated, such that the likelihood of falsifying the specification is increased.

For industrial systems typically only a black-box of the system under test is available, meaning that only input-output behavior of the system can be observed. In general, these systems are a mix of continuous dynamics, discrete event dynamics, and algorithms implemented using general-purpose programming languages. Parts of the system might also be implemented using physical hardware. Breach (Donzé, 2010) and S-TaLiRo (Annpreddy et al., 2011) are two Matlab/Simulink based toolboxes used for test monitoring and falsification. Both tools search for trajectories of minimal quantitative value to find counterexamples to MITL/STL specifications. Eddeland et al. (2020) show how STL specifications can be automatically de-
2. QUANTITATIVE SEMANTICS AND OBJECTIVE FUNCTIONS

In this paper, Breach is used for falsification, hence STL is used to model the specifications. The syntax of STL is defined as follows (Raman et al., 2014)

\[ \varphi := \mu \mid \neg \varphi \mid \varphi \land \psi \mid \varphi \lor \psi \mid \mathrm{C}_{[a,b]}[\varphi] \mid \mathrm{O}_{[a,b]}[\varphi] \]

where the predicate \( \mu \) is \( \mu(s) > 0 \) and \( s \) is a signal; \( \varphi \) and \( \psi \) are STL formulas; \( \mathrm{C}_{[a,b]}[\varphi] \) denotes the globally operator between times \( a \) and \( b \) (with \( a < b \)); \( \mathrm{O}_{[a,b]}[\varphi] \) denotes the finally operator between \( a \) and \( b \).

The satisfaction of the formula \( \varphi \) with respect to the discrete signal \( s \) at the discrete time instant \( k \) is defined as:

\[ (s, k) \models \mu \iff \mu(s[k]) \]

\[ (s, k) \models \neg \mu \iff \neg \mu(s[k]) \]

\[ (s, k) \models \varphi \land \psi \iff (s, k) \models \varphi \land (s, k) \models \psi \]

\[ (s, k) \models \varphi \lor \psi \iff (s, k) \models \varphi \lor (s, k) \models \psi \]

\[ (s, k) \models \mathrm{C}_{[a,b]}[\varphi] \iff \forall k' \in [k + a, k + b] (s, k') \models \varphi \]

\[ (s, k) \models \mathrm{O}_{[a,b]}[\varphi] \iff \exists k' \in [k + a, k + b], (s, k') \models \varphi \]

Instead of only checking the boolean satisfaction of an STL formula, the notion of a quantitative value, i.e. an objective value, will be defined in order to measure how far a specification is from being falsified. A Valued Boolean (VBool) (Claessen et al., 2018) \( (v, x) \) is a combination of a Boolean value \( v \) (true, \( T \), or false, \( F \)) together with a real number \( x \) that is a measure of how true or false the specification is. This value will be used as a measure of how convincingly a test passed, or how severely it failed, respectively. In the original VBool definition, \( x \) is defined to always be non-negative. However, in this paper we use the convention that \( x \) is negative when \( v \) is false, and positive otherwise.

2.1 Quantitative Semantics

Using VBools, we define three quantitative semantics: Max, which is essentially the same as standard STL quantitative semantics; Additive; For these semantics we define the respective and, or, always, and eventually operators.

For conjunction, the semantics differ only in the two cases where the truth values are the same:

\[
\begin{array}{c|c|c}
(T, x) \land (T, y) = & (T, \min(x,y)) & (T, \frac{1}{1+y}) \\
(T, x) \land (F, y) = & (F, y) & (F, 0) \\
(F, x) \land (T, y) = & (F, y) & (F, 0) \\
(F, x) \land (F, y) = & (F, y) & (F, 0) \\
\end{array}
\]

Using the de Morgan laws, the or operator can be defined in terms of and, as \( (v_1, x) \lor (v_2, y) = \neg(\neg v_1(x) \land \neg v_2(y)) \), where VBool negation is defined as \( \neg v(x) = (\neg v, -x) \).

For the Max semantics, the always operator over an interval \( [a, b] \) is straightforwardly defined in terms of and, as \( \Box_{[a,b]}[\varphi] = \bigwedge_{k=a}^b \varphi[k] \), where \( \varphi \) is a finite sequence of VBools defined for all the discrete time instants in \( [a, b] \).

For the Additive semantics, though, always is a bit more elaborate: \( \Box_{[a,b]}[\varphi] = \bigwedge_{k=a}^b \varphi[k] \# \delta t \), where \( \delta t \) is the simulation step size.
that makes the quantitative value independent of the simulation time, and $\#$ is $(\sum, x) \# \delta t = (\sum, x \cdot \delta t)$ and $(T, x) \# \delta t = (T, x/\delta t)$. Furthermore, the eventually operator is for all three semantics defined over an interval $[a, b]$ in terms of always, as $\dot{\varphi} = -\langle \square_{[a,b]} \varphi \rangle$.

3. FALSIFICATION USING MULTIPLE OBJECTIVE FUNCTIONS

This section presents the multiple objective functions for falsification of CPSs. Different combinations of objective functions and different strategies for switching between objective functions is discussed in this paper. The main optimization algorithm considered in this paper is an implementation of Nelder-Mead which is also included in Breach. This algorithm is implemented as finnsearch (Lagarias et al., 1998) in Matlab. We propose a modified optimization algorithm based on Nelder-Mead, that exploits multiple objective functions. The new algorithm is presented in Algorithm 1 and works in the following way. The presentation of the algorithms is based on two objective functions, in this case using the Max and Additive semantics, however the approach is generic and can be applied to an arbitrary number of objective functions.

1. The algorithms starts with $p$ sample points. For each example, $p$ is different and it refers to the number of inputs of each example multiple by 10. All these points are sorted from lowest to highest according to the values of different objective functions. Note, that objective values will be different for each used quantitative semantic, thus there will be one ordering for each semantic. By using a heuristic algorithm to choose which quantitative semantic, the minimum point is considered and it will generate $n$ new points around the first point before starting the optimization.

2. The first $n + 1$ points in the parameter space are needed by the NM style optimization algorithm to start the optimization process. Again, all these points must be sorted from lowest to highest according to the values of the different objective functions.

3. For each ordering of the objective values, the algorithm will suggest a new point in the parameter space for evaluation. For each quantitative semantic there will be an ordering of the points in the parameter space that is based on the objective value used for the specific semantic. By using a heuristic algorithm to choose which quantitative semantic, one new point will be selected for further evaluation, i.e. being simulated.

4. Now, one iteration in the optimization can execute, i.e. the execution of Step 4 to 7 in Algorithm 1.

5. When reaching to Step 8, once again calculate the objective values for all of the considered quantitative semantics and saved points, and create one ordering for each of the considered quantitative semantic. Choose $n + 1$ points with lowest objective value function of the semantic that wins the heuristic strategy.

Note, a new quantitative semantic can be selected in each iteration of the algorithm. In this paper, we have implemented two heuristic algorithms that are based on the variance of the $n + 1$ lowest objective values and the distance of largest and lowest objective functions.

Strategy 1 (Variance). For each ordering of objective values, i.e. one ordering for each quantitative semantic, consider the $n + 1$ points with lowest objective value, i.e. the points that according to the semantics that are closest to falsifying the specification. For these points, calculate the variance among the $n + 1$ points using $\sigma^2 = \frac{1}{n+1} \sum_{i=1}^{n+1} (\mu - \varphi_i)^2$, where $\mu$ refers to the objective function value of each $n + 1$ points that have lowest value for each semantic. $\mu$ is the mean of $n + 1$ points.

Strategy 2 (Distance). The distance can be calculated using $Dist = \frac{\sum_{i=1}^{n+1} (\mu - \varphi_i)}{\sum_{i=1}^{n+1} x_i}$, where $\mu_{max}$ and $\mu_{min}$ refer to the maximum and minimum objective function values of the $n + 1$ points that have the lowest objective value of each semantic. $x_{max}$ and $x_{min}$ refers to their points, respectively.

The heuristic will choose the point given by the quantitative semantic that corresponds to the largest variance in strategy 1; largest distance in strategy 2. These heuristics are thus selecting the quantitative semantic that has a clear sense of direction and avoids using semantic that has close to constant objective values resulting in small variance and distance. However, other heuristics could be used as well, but a more thorough evaluation of possible heuristics is future research.

4. BENCHMARK PROBLEMS

Three examples are considered here to show the performance of the multiple objective functions approach, that are also used in Eddeland et al. (2020), below is a brief description of the examples.

4.1 Automatic Transmission (AT) Benchmark

The inputs to the model are the throttle and brake of a vehicle. The outputs of the model are the vehicle speed $v$, the engine speed $\omega$, and the gear, see Hoxha et al. (2014) for details.

4.2 Third Order $\Delta - \Sigma$ Modulator

The third order $\Delta - \Sigma$ modulator is a model of a technique for analog to digital conversion. It has one input $U$, three states $x_1, x_2, x_3$, and three initial conditions $x_{init}^1, x_{init}^2, x_{init}^3$, see Dang et al. (2004) for details.

4.3 Static Switched (SS) System

The static switched system is a model without any dynamics that is included as a simple case make falsification worse than only using single boolean objective function. The model has been inspired by Dokhanchi et al. (2015).

5. EXPERIMENTAL SETUP AND RESULTS

The experimental setup is described in more detail in Eddeland et al. (2020). The implementation starts by evaluating 100 random points for the AT example, 40 for third order $\Delta - \Sigma$ modulator example and 20 for the SS example before starting the optimization. After doing that if the falsified point is not found, the optimization solver starts from the point with lowest objective value. In Table 1, the STL specifications that should be falsified for all the models, and the benchmark models are presented.

The results of running Algorithm 1 on the benchmark problems are shown in Tables 2, 3, and 4, and the aggregated results are
Algorithm 1 Modified Nelder-Mead Algorithm Using Multiple Objective Functions

1. Choose \( p \) random points. Start with \( p \) random points and order and re-label the vertices from lowest function value to highest function value:
   \[
   f_{\max}(x_1^i) \leq f_{\max}(x_1^j) \leq \cdots \leq f_{\max}(x_1^n),
   \]
   \[
   f_{\delta \max}(x_1^i) \leq f_{\delta \max}(x_1^j) \leq \cdots \leq f_{\delta \max}(x_1^n),
   \]
   Use a heuristic algorithm to choose which quantitative semantic to follow in this iteration of the optimization. Take the minimum point of semantic that wins the heuristic algorithm.

2. Let \( x_i \) denote the list of vertices in the current simplex, \( i = 1, \ldots, n + 1 \). These points are generated from the minimum point of Step 1.

3. Order. For each objective function \( i = 1, \ldots, p \), order and re-label the \( n \) vertices from lowest function value to highest function value:
   \[
   f_{\max}(x_1^i) \leq f_{\max}(x_1^j) \leq \cdots \leq f_{\max}(x_1^n),
   \]
   \[
   f_{\delta \max}(x_1^i) \leq f_{\delta \max}(x_1^j) \leq \cdots \leq f_{\delta \max}(x_1^n),
   \]
   Use a heuristic algorithm to choose which quantitative semantic to follow in this iteration of the optimization, see Strategy 1 and 2 for examples.

4. Reflection. Compute the reflected point \( x_r \) by \( x_r = \bar{x} + \rho(x - x_{n+1}) \), where \( \bar{x} \) is the centroid of the \( n \) points with lowest objective function values, \( \bar{x} = \sum_{i=1}^{n} x_i \), \( i = 1, \ldots, n \). The rest of the optimization will be executed with the chosen semantic, then \( f \) refers to the objective function value of that semantic.

   if \( f(x_l) < f(x_r) < f(x_u) \)
   Replace \( x_{n+1} \) with the point \( x_r \) and go to Step 8.
   end if

5. Expansion. If \( f(x_r) < f(x_u) \)
   Compute the expanded point \( x_e \) by \( x_e = \bar{x} + \chi (x_r - \bar{x}) \).
   if \( f(x_r) < f(x_u) \)
   Replace \( x_{n+1} \) with \( x_r \) and go to Step 8.
   else
   Replace \( x_{n+1} \) with \( x_e \) and go to Step 8.
   end if

6. Contraction. If \( f(x_c) > f(x_u) \)
   Perform a contraction between \( x_r \) and the best among \( x_{n+1} \) and \( x_e \).
   if \( f(x_u) \leq f(x_l) < f(x_{n+1}) \)
   Calculate \( x_c = \bar{x} + \tau(x_r - \bar{x}) \) Outside contract.
   if \( f(x_u) \leq f(x_l) \)
   Replace \( x_{n+1} \) with \( x_c \) and go to Step 8.
   else
   Go to Step 7.
   end if

7. Shrink. Evaluate the \( n \) new vertices \( x' = x_1 + \phi(x_i - x_1), i = 2, \ldots, n + 1 \).
   Replace the vertices \( x_2, \ldots, x_{n+1} \) with the new vertices \( x_2', \ldots, x_{n+1}' \).

8. Re-Order. Calculate the objective values for the new point for all the quantitative semantics and for each quantitative semantic and save it or them (If “Shrink” happens). Order and re-label the \( \delta \) vertices from lowest function value to highest function value:
   \[
   f_{\max}(x_1^i) \leq f_{\max}(x_1^j) \leq \cdots \leq f_{\max}(x_1^n),
   \]
   \[
   f_{\delta \max}(x_1^i) \leq f_{\delta \max}(x_1^j) \leq \cdots \leq f_{\delta \max}(x_1^n),
   \]
   where \( \delta \) refers to the number of \( n + 1 \) of Step 2 and plus the number of points that are reached at each iterations (Steps 4-7).

9. Selecting semantics. Take \( n + 1 \) of each semantic that has lowest objective function values from Step 8. Select the semantic according to the heuristic algorithm and continue with the chosen semantic, \( f \) refers to the objective function value of the chosen semantic. While the stopping condition is not reached go to Step 4, thus
   if \( f(x_{n+1}) - f(x_l) < \epsilon \)
   Stop, where \( \epsilon > 0 \) is a small predetermined tolerance.
   else
   Go to Step 4.
   end if

Note: \( \rho, \chi, \tau \) are constant parameters.

Table 1. Specifications to falsify for the three benchmark models AT, (\( \Lambda - \Sigma \)), and SS.

| Spec. | Formula |
|-------|---------|
| \( \varphi_1^T \) | \( \varphi_{\Lambda,1}(\omega \geq 2000) \) |
| \( \varphi_2^T \) | \( \varphi_{\Lambda,2}(\omega \leq 3500 \land \omega \geq 4500) \) |
| \( \varphi_3^T \) | \( \varphi_{\Lambda,3}(\text{gear} == 3) \) |
| \( \varphi_4^T \) | \( \land i \in 1,4 \omega(\text{gear} == i) \land \varphi_{\Lambda,6}(\text{gear} == i) \Rightarrow \varphi_{\Lambda,7}(\text{gear} == i)) \) |
| \( \varphi_5^T \) | \( \varphi_{\Lambda,6}(\omega \leq 850) \land \delta(\omega \geq 4500) \) |
| \( \varphi_6^T \) | \( \varphi_{\Lambda,6}((\varphi_{\Lambda,1}\text{gear} == 1) \land \varphi_{\Lambda,2}\text{gear} == 2) \) |
| \( \varphi_7^T \) | \( \varphi_{\Lambda,6}((\varphi_{\Lambda,1}\text{gear} == 3) \land \varphi_{\Lambda,2}\text{gear} == 3) \land \varphi_{\Lambda,2}\text{gear} == 2) \) |
| \( \varphi_8^T \) | \( \varphi_{\Lambda,6}(\text{gear} == 4 \land \text{throttle} > 45 \land \text{throttle} < 50) \Rightarrow \omega > \omega_0 \) |
| \( \varphi_9^T \) | \( \varphi_{\Lambda,6}(\omega > 3500) \) |

shown in Fig. 1. The tables are formatted as follows. The first column denotes the specification falsified. Each specification has one to three parameter values, these parameter values are shown in the second columns. The remaining columns show the different semantics including the Max, Additive, and their combination with two difference strategies. For each parameter value and semantic, two values are presented. The first value is the relative success rate of falsification, in percent. There are a total of 20 falsification run for each parameter value and objective functions, meaning that the success rate will be a multiple of 5%. The second value, inside parentheses, is the average number of needed simulations per successful falsification. Each falsification is set to have a maximum of 1000 simulations performed.

In addition, for each parameter value, the semantic with the highest (or tied highest) success rate has the success rate displayed in bold characters. For each parameter value where there are semantics with same success rate, the semantic with the lowest average number of simulations per successful simulation has that number displayed in bold characters (inside the parentheses).

5.1 Results

As can be seen from Fig 1, the top two approaches are Multiple semantics. All two strategies of the multiple objective functions, perform better than when we only have a single objective function. They are more successful in falsifying with fewer simulations.

By looking at three tables of results, it can be seen that for automatic transmission, \( \varphi_1^T (T = 20) \), \( \varphi_3^T (T = 5) \), \( \varphi_4^T (T = 2) \), \( \varphi_6^T (T = 12) \), \( \varphi_8^T (\omega = 3000) \), the Multi-Max-Add using variance strategy works better. While, for \( \varphi_1^T (T = 30) \), \( \varphi_2^T \), \( \varphi_4^T \), \( \varphi_6^T (T = 1) \), \( \varphi_8^T (\omega = 3000) \), the Multi-Max-Add using distance works better. Only, for \( \varphi_8^T (T = 4.5) \), Max is better. Additive works for \( \varphi_1^T (T = 40) \), \( \varphi_8^T (\omega = 3500) \).

For \( \varphi^{\delta - \Sigma} \) Benchmark, except \( U \in [-0.45, 0.45] \) that Max performs better for that, multiple objective function using variance perform well. For all specifications of the Static Switched
Parameters

System, multiple objective function using variance give better results.

One conclusion that can be given here is that the Max-Additive multiple objective function using both strategies work better than others, and for only a few of specifications, the single semantics works better. Only for the specifications $\varphi^{AT}_{\bar{\omega}}$, $\varphi^{AT}_{\bar{\omega}}$, and $\varphi^{AT}_\omega$ of the automatic transmission example, the Additive was successful in finding more falsification. For other semantics that the Max or Additive work better still the single and multiple objective functions have same success ratio of falsification, only the number of simulations is different. As a result, the multiple objective functions using both strategies can guide the testing process towards falsification better than only single semantic is used, on the given benchmark set.

6. CONCLUSION

In this paper, the use of multiple objective functions for falsification of CPSs was proposed. With a single objective function, the optimization may get the wrong or even no information for it to be able to guide the falsification process towards falsifying the specification. Since for CPSs, the simulation time is the most limiting factor, not the evaluation of the simulation results, multiple objective functions were suggested. Combinations of two different semantics Max and Additive were evaluated. A variance and distance based strategy were used to switch between the objective functions, such that the objective function with highest variance (distance) was picked for each iteration of the falsification. Three benchmark CPSs examples were considered to show the performance of the multiple objective functions.

The main conclusion drawn from the data gathered is that the proposed optimization algorithm perform better than when only a single objective function is used on the used benchmark examples. Also multiple objective functions are more successful in finding counterexamples in less number of simulation runs. This so, since multiple objective functions can better guide the optimization algorithm towards falsification, increasing the chance of falsifying the specification.

For future work, it would be interesting to explore different heuristics for choosing between multiple objective functions as well as extending the number of benchmark problems to further evaluate the performance of the proposed approach.
Fig. 1. A cactus plot showing performance of using optimization based on multiple objective functions compared to using a single objective function. The plotted values tell how many successful falsifications (x-axis) were completed in less than a specific number of simulations (y-axis). The maximum number of simulations per falsification is 1000. Note that we also include the cactus plot for Uniform Random sampling, as a baseline approach.

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