The Magnetic Structure of the Subsolar MPB Current Layer From MAVEN Observations: Implications for the Hall Electric Force

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Abstract We report on the local structure of the Martian subsolar magnetic pileup boundary (MPB) from minimum variance analysis of the magnetic field measured by the Mars Atmosphere and Volatile EvolutionN (MAVEN) spacecraft for six orbits. In particular, we detect a well-defined current layer within the MPB and provide a local estimate of its current density which results in a sunward Hall electric force. This force accounts for the deflection of the solar wind ions and the acceleration of electrons which carry the interplanetary magnetic field through the MPB into the magnetic pileup region. We find that the thickness of the MPB current layer is of the order of both the upstream (magnetosheath) solar wind proton inertial length and convective gyroradius. This study provides a high-resolution view of one of the components of the current system around Mars reported in recent works.

Plain Language Summary We investigate the current layer associated with the outer boundary of the Martian induced magnetosphere in the subsolar sector from selected MAVEN magnetic field and solar wind plasma observations. We measure the variance of the magnetic field across the boundary to obtain its normal, which in turn is used to measure the strength of the current density. The current density we obtain is such that its derived Hall electric force is strong enough to stop the solar wind ions at the outer boundary of Mars magnetosphere. On the other hand, this force would push the solar wind electrons and the interplanetary magnetic field frozen into the electron plasma into the induced magnetosphere. We also find that the thickness of this current layer in terms of typical lengths of the solar wind ion plasma is similar to the thickness of the terrestrial magnetopause.

1. Introduction

Mars (1RM = 3,390 km) has either no or negligible present global magnetic field \((|M| < 2 \times 10^{11} \text{T} \cdot \text{m}^3)\) (Acuña et al., 1998). This makes the solar wind interact directly with its ionosphere and the charged particles from its exosphere. The Martian upper atmosphere (altitudes greater than 200 km), which is the region of interest for this work, is mostly composed of atomic oxygen, molecular oxygen, and hydrogen (Anderson 1974; Anderson & Hord, 1971; Mahaffy et al., 2015).

The interaction of the solar wind with Mars’ atmosphere produces the so-called induced magnetosphere, a region where the solar wind flow and field are disturbed by the presence of the planet. The supermagnetosonic nature of the solar wind needs a bow shock (BS) to form ahead of the obstacle to avoid it. Downstream from the BS, the solar wind plasma is mostly subsonic and significantly hotter. Also in this region—named magnetosheath—the magnetic field is highly variable due to the presence of turbulence (Ruhunusiri et al., 2017) and waves generated from electron and ion instabilities taking place both upstream and locally.

In areas where crustal magnetic fields can be ignored, the mass loading causes the frozen-in interplanetary magnetic field to increase in the subsolar region and to drape around the planet. On the dayside, the increase in the magnetic field strength has been found to be a permanent feature although single-spacecraft magnetic field time series suggest a variety of values for this gradient. Following the nomenclature of a
similar structure at active comets (Neubauer, 1987) the layer where the magnetic field strength gradient occurs received the name magnetic pileup boundary (MPB) (Acuña et al., 1998). Pre-MAVEN measurements (Bertucci et al., 2011; Dubinin et al., 2008) have shown that the MPB is located between the region dominated by the solar plasma—the magnetosheath—and that governed by the plasma of planetary origin—the magnetic pileup region (MPR), also called induced magnetosphere—which is characterized by a strong and organized magnetic field of solar origin as a result of pileup and draping (Bertucci et al., 2003). Once again these features apply for regions where crustal fields are not important. In the lower part of the magnetosheath, the solar plasma slows down further as it increasingly incorporates cold protons and heavier ions from Mars exosphere. These particles, being relatively slow, heavy and numerous compared to the solar wind, decrease the average speed of the solar wind (Szego et al., 2000) in areas where the influence of crustal magnetic fields is negligible (Connerney et al., 2001). This deceleration precedes a change in the composition of the plasma, from solar wind ions to heavy ions of planetary origin, at the ion composition boundary (ICB), which on the dayside is almost coincident with the MPB (Breus et al., 1991; Halekas et al., 2018; Holmberg et al., 2019; Matsunaga et al., 2017; Sauer et al., 1994).

With an areocentric distance of approximately 2 \( R_M \) for the bow shock and 1.3 \( R_M \) for the MPB (between 800 and 1,000 km), the magnetosphere of Mars is one of the smallest of the solar system (Moses et al., 1988). However, it is in this small portion of space that most of the solar wind’s energy and momentum are transferred to the planetary plasma. Recent estimates of atmospheric escape on Mars (Jakosky et al., 2015) suggest that the interaction with the solar wind has played a significant role in the removal of water from Mars for billions of years. In this context, the study of these electric fields is essential to understanding the processes of energy and momentum transfer from the solar wind to the plasma of planetary origin that lead to atmospheric escape.

The features that allow the detection of the MPB at Mars and other atmospheric bodies (Bertucci et al., 2011) are as follows: a marked increase in the magnitude of the magnetic field in the magnetosheath (by a factor of 2 or 3) followed by a decrease in the magnetic field fluctuations, a decrease in the temperature, velocity, and density of the solar wind ions and suprathermal electrons and an increase in the total plasma density as an increase in the number of charged particles of planetary origin. These features have allowed for statistical studies on its average location and shape (Edberg et al., 2008; Trotignon et al., 2006; Vignes et al., 2000). So far the sub-ion scale of the MPB has been studied from single-spacecraft observations (Bertucci et al., 2005) or multifluid simulations of high spatial resolution (Harnett & Winglee, 2007). Bertucci et al. (2005) applied minimum variance analysis (MVA) (Sonnerup & Scheible, 1998) to Mars Global Surveyor (MGS) magnetometer observations near the terminator and found that inside the MPB there is a current sheet, a layer of typically 100 km where the magnetic field vector rotates on a plane that is nearly perpendicular to the boundary normal obtained from the MPB static fit. The surface and volume current densities were 6.5 \( \times \) 10\(^6\) nA/m\(^2\) and 81 nA/m\(^2\), respectively, comparable to values obtained from multifluid simulations. Unfortunately, this work was limited to high solar zenith angles or SZA (i.e., larger than 30\(^\circ\)) because of the geometry of MGS premapping orbits. But also, the lack of ion measurements precluded any local estimate of relevant plasma length scales necessary to assess the origin of the detected currents.

In previous studies it has been shown that in the different regions of the Martian magnetosphere different terms of the electric field prevail (Dubinin et al., 2011). With the arrival of the Mars Atmosphere and Volatile Evolution (MAVEN) mission, reliable, high-resolution particle and magnetic field measurements have become available for a deeper analysis of the macroscopic current systems within Mars’ magnetosphere. Halekas et al. (2017) obtained averaged values of the current density and the derived Hall electric force (\( J \times B \)) around the MPB by estimating the curl of the magnetic field accumulated in static bins with a resolution of 500 km in the \( x_{MSE} - y_{MSE} \) Plane and 2,000 km in \( z_{MSE} \).

More recently Ramstad et al. (2020) have reported on a global, coupled current system at Mars by computing \( J = \frac{1}{\rho_i} (V \times B) \) as center-point differences for every location of two 3-D magnetic field map. This map was obtained averaging the magnetic field obtained over 9,814 orbits with a grid spacing of 0.1 \( R_M \) or 0.2 \( R_M \) depending on the altitude.

As we have access to high-resolution data we can determine more precisely where the current sheet is located inside the MPB and obtain its thickness in order to understand where this current is originated. We compare...
the MPB thickness with the solar wind proton inertial length and convective Larmor radius in the magnetosheath in order to see if a Hall-MHD model is enough or if there are kinetic effects that must be taken into account.

In the absence of collisions, local particle acceleration is produced by electric fields. Within the framework of a multifluid plasma, the equation of motion for each species $s$ is

$$m_s n_s \frac{dv_s}{dt} = q_s n_s (E + v_s \times B) - \nabla \cdot P_s$$

(1)

where $m_s$ and $q_s$ are the individual mass and electric charge of particles of species $s$, $n_s$ and $v_s$ are the particle density and velocity of the fluid formed of $s$ particles, and $P$ is the pressure tensor. If we assume a plasma made of electrons and a single ion species, quasi-neutrality dictates that $n_e = n_i = n$ and the current density is simply given by $J = en(v - v_e)$. If we further assume that the electron mass is negligibly small ($m_e \approx 0$), the equation for electrons reduces to a force equilibrium given by

$$E = -v \times B + \frac{1}{en} (J \times B - \nabla \times P_e)$$

(2)

This equation is also known as the generalized Ohm's law.

The bulk velocity of the plasma is $v = v_e$, since momentum is fully carried by ions in this approximation. The equation of motion for the ions, after replacing Equation 2 into Equation 1 and using the identity $\mathbf{j} \times \mathbf{B} = \frac{1}{\mu_0} (\mathbf{B} \cdot \nabla) \mathbf{B} - \nabla \times \left( \frac{\mathbf{B}^2}{2\mu_0} \right)$, reduces to

$$m_i n_i \frac{dv_i}{dt} = \frac{1}{\mu_0} (\mathbf{B} \cdot \nabla) \mathbf{B} - \nabla \times \left( \frac{\mathbf{B}^2}{2\mu_0} \right) - \nabla \times (P_e + P_i)$$

(3)

where the first term on the right-hand side (RHS) is the magnetic tension force, the second term is the magnetic pressure force, and the last term is the total thermodynamic pressure. The magnetic pressure gradient is directly proportional to the square of the magnetic field and inversely proportional to the thickness of the MPB. In contrast, the term of the tension, while also directly proportional to the square of the magnetic field, is inversely proportional to the curvature radius of the magnetic field lines.

In the present work we analyze MAVEN data to identify and characterize the local structure of the Martian subsolar MPB. Then we apply MVA to MAVEN magnetic field measurements to estimate the local current density flowing along the MPB and its associated Hall electric force in order to evaluate its importance in the plasma dynamics around the boundary. In section 2 we describe the data and methods used; the results are displayed in section 3 and are discussed in section 4.

2. Methods and Data

We analyzed six subsolar MPB crossings between October 2015 and November 2017. The magnetic field measured by the Magnetometer (MAG) (Connerney et al., 2015) has a 32 Hz sampling rate. The solar wind electron data from the Solar Wind Electron Analyzer (SWEA) (Mitchell et al., 2016) measures electrons in an energy range between 3 and 4,600 eV with a 2 s resolution. The Solar Wind Ion Analyzer (SWIA) (Halekas et al., 2015) provided the solar wind proton data in an energy range between 25 eV and 25 keV with a 4 s resolution.

2.1. Methodology

The MVA for a single spacecraft (Sonnerup & Scheible, 1998) is a technique widely used to find the normal vector for a one-dimensional discontinuity from magnetic field measurements obtained by the probe across the boundary (e.g., Knetter et al., 2004). The main purpose of the MVA is to estimate the normal to a one-dimensional current sheet in a plasma. This is achieved by determining the eigenvectors and eigenvalues of the covariance matrix defined as $M^B_{\mu \nu} = \langle B_\mu B_\nu \rangle - \langle B_\mu \rangle \langle B_\nu \rangle$ in terms of the magnetic field data and the coordinate system in which the data is presented, then finding its three eigenvalues $\lambda_i$ and their corresponding eigenvectors $\mathbf{x}_i$. The eigenvector corresponding to the smaller eigenvalue ($\mathbf{x}_3$ and $\lambda_3$) is the estimate for the direction of the normal vector to the current sheet, and $\lambda_3$ represents the variance of the magnetic field component in that direction. In general, for any set of vectors $\{\mathbf{R}^{(m)}\}$ across a transition layer, the set of $M^B_{\mu \nu}$ eigenvectors provides a convenient coordinate system to analyze the data. It must be noted that the variance matrix $M^B_{\mu \nu}$ is independent of the temporal order of the measured vectors.
Figure 1. Time series of the magnetic field and plasma data from MAVEN for the 16 March 2016 crossing. (from top to bottom) Magnetic field magnitude, magnetic field components, relative variation of the magnetic field, differential energy fluxes for solar wind electrons, and solar wind proton density. The MPB is shaded in green, the magnetosheath in red, and the MPR in blue.

In the present work MVA is applied to the MAG data in the MPB in order to obtain an estimate of the normal vector to this boundary and therefore to the associated current sheet.

In this first study we deliberately selected crossings that show an apparently sharp increase in the magnetic field amplitude and are located on the northern hemisphere, and all have solar zenith angle (SZA) < 30°. The crustal magnetic field according to the model by Cain et al. (2003) does not exceed 10% of the total field in the analyzed crossings. These crossings occurred in the span of more than one Martian year and have varied solar wind conditions and heliocentric distance.

2.2. MPB Identification in a Case Study

Figure 1 shows a time series of magnetic field and plasma data from MAVEN near the MPB for one of the orbits analyzed in this work. All vector magnitudes are represented in the Mars-centered Solar Orbital (MSO) coordinate system, in which the $\hat{x}$ axis points from Mars toward the Sun, the $\hat{y}$ axis points antiparallel to Mars’ orbital velocity, and $\hat{z}$ completes the right-handed coordinate system.

Between 17:40 and 18:40 UTC on 16 March 2016 MAVEN headed from the undisturbed solar wind to Mars, crossing the bow shock around 18:02 UTC and the MPB near the subsolar point around 18:13 UTC. Then, MAVEN continued within the induced magnetosphere and ionosphere and at 18:30 UTC entered the region of the magnetic tail.
For the identification of the MPB we rely on the criteria described by Bertucci et al. (2011): a sharp increase in the magnetic field strength by a factor of 2–3, a sharp decrease in the magnetic field fluctuations, a sharp enhancement of the magnetic field draping, a decrease in the temperature of electrons, and a decrease in the solar wind proton density with respect to the magnetosheath.

In order to determine the MPB apparent thickness, we selected by visual inspection four times which we called $t_1$, $t_2$, $t_3$, and $t_4$ so that outside the interval between $t_1$ and $t_4$ MAVEN would be unambiguously outside the MPB while in the interval between $t_2$ and $t_3$ MAVEN would be inside the MPB. In this interval we observe the defining characteristics of this boundary. The times thus determined were $t_1 = 18:13:00$ UTC, $t_2 = 18:13:13$ UTC, $t_3 = 18:14:06$ UTC, and $t_4 = 18:14:51$ UTC.

In this interval we observe the drastic changes in the plasma near the MPB: the magnetic field changes direction while its magnitude goes from 20 to 45 nT in less than 2 min. We also observe that the relative variations of $B$ (both parallel and perpendicular to the mean field) cease abruptly. This decrease is due to the diminishing amplitude of the fluctuations as well as the increase in magnetic field magnitude. The differential energy fluxes decrease in a range from 1 to 2 orders of magnitude in the MPB depending on the electron energy, which is consistent with the electron impact ionization described by Crider et al. (2000). The solar wind proton density decreases from 6 cm$^{-3}$ down to the instrumental noise for protons with energies above 25 eV.

3. Results

Once the times $t_1$, $t_2$, $t_3$, and $t_4$ delimiting the MPB were identified we applied MVA in the interval 18:13:33–18:14:06 UTC (shaded in yellow in Figure 2); the data consisted of 922 high-resolution measurements. We chose this interval in order to avoid the magnetic field oscillations around 18:13:20 while still providing a good $\lambda_2/\lambda_3$ ratio. Looking at the upper panel of Figure 2, where the magnetic field components are plotted, we can anticipate that the minimum variance direction will be approximately parallel to the $\hat{x}$ axis. We also see that the field points mainly in the $\hat{j}$ and $\hat{z}$ directions, so we can anticipate that $\mathbf{B}$ in the MPR will be mostly tangential.

The intermediate-to-minimum eigenvalue ratio for the analyzed crossing is $\lambda_2/\lambda_3 = 9.48$, which ensures that the minimum variance vector is well defined (Knetter et al., 2004).

The normal obtained with this method is $\mathbf{x}_3 = \hat{n}_{\text{MVA}} = (0.920, -0.302, 0.251)$ with angular error 5.4$^\circ$, that is, differing by 23$^\circ$ from the $\hat{x}$ axis. The error was obtained by applying MVA in intervals the size of the current sheet centered around every second within the interval [18:13:33, 18:14:06] and calculating the mean value of the angle between the normals thus obtained and $\hat{n}_{\text{MVA}}$. The mean magnetic field component along the normal is $\langle \mathbf{B}_n \rangle = -2.06 \pm 0.08$ nT and the mean magnetic field magnitude is $B_0 = |\langle \mathbf{B} \rangle| = 34.79$ nT, the quotient between both being $(\mathbf{B}_n)/B_0 = 0.06$ which is consistent with our assumption that the magnetic field in the MPR would be nearly tangential. The angle between the mean magnetic field vector ($\mathbf{B}$) and the normal is $\theta_\mu 4 = 93^\circ$, that is, the magnetic field is almost tangential and lies mostly in the $(\hat{\mathbf{x}}, \hat{\mathbf{z}})$ plane. The hodograms in Figure 2 show the magnetic field projection on the planes $(\hat{\mathbf{x}}, \hat{\mathbf{y}})$ and $(\hat{\mathbf{z}}, \hat{\mathbf{y}})$ in the interval where MVA was applied (between 18:13:37 and 18:14:06 UTC). The hodogram to the right (depicting the projection $\hat{\mathbf{x}}, \hat{\mathbf{y}}$) has an elongated shape, consistent with a good eigenvalue ratio and the plane containing the normal being well defined.

In order to obtain the MPB spatial thickness, $h$, we calculated the angle $\theta_\nu$ between the average spacecraft velocity $\langle \mathbf{v}_\nu \rangle$ in the MPB and the normal; the calculation yielded $\theta_\nu = 117^\circ$. This means that MAVEN motion was almost parallel to the MPB.

Once we have the normal we can estimate $h$ assuming that the boundary is one-dimensional and static, although there is no evidence of that being the case. Even though we do not know the MPB velocity, recent studies by Madanian et al. (2020) estimated the BS velocity at 5 km/s; this suggests that the MPB could be expanding at a similar speed. As in these crossings the angle $\theta_\nu$ is high, MAVEN speed inside the MPB is comparable with the estimated MPB velocity. This would lead to errors between 10% and 50% in the estimated thickness for this crossing.

We then approximate $h = |\mathbf{r}_{\text{in}} - \mathbf{r}_{\text{out}}| \cdot \hat{n}$, where $\mathbf{r}_{\text{in}}$ is the position of the spacecraft when entering the MPB and $\mathbf{r}_{\text{out}}$ is the position when leaving; being that it is not uniquely defined, we actually approximate a
Figure 2. Magnetic field components in MVA coordinates and amplitude (top). The upstream and downstream intervals from the MPB and the interval where MVA was applied are shaded. Magnetic hodograms \(N = 922, \lambda_2/\lambda_3 = 9.8\) depicting the magnetic field projection on the planes \((\hat{e}_1, \hat{e}_2)\) and \((\hat{e}_1, \hat{e}_3)\) in the interval where MVA was applied (bottom). The start point is marked with a circle and the end point with a cross.

minimum thickness corresponding to the interval between \(t_2 - t_1\) and a maximum thickness in the interval \(t_1 - t_4\). In this way, we obtained \(h_{23} = 82\text{km}\) and \(h_{14} = 174\text{km}\). These values are comparable to both the magnetosheath solar wind proton inertial length \((\lambda = c/\omega_{pi} = 97.9\text{km})\) and the magnetosheath convective proton gyroradius \((r_g = \lambda v_{\perp}/|q|B = 68.4\text{km})\). The solar wind proton inertial length was calculated from SWIA data, as \(\omega_{pi}\) is the proton plasma frequency obtained using the mean proton density in the upstream region (shown shaded in purple in Figure 2). On the other hand, for obtaining the magnetosheath convective proton gyroradius we considered \(B\) as the average magnetic field and \(v_{\perp}\) as the velocity perpendicular to \(B\) in the upstream region.

Another estimate of the normal vector to the MPB can be obtained from the conic section fit representing its average position (e.g., Vignes et al., 2000). We used the parameters \(x_0 = 0.78R_M\) and \(\epsilon = 0.9\) given by Vignes et al. (2000). We estimated the semilatus rectum \(L = 0.87R_M\) by requiring that the ellipsoid contains the point through which the spacecraft passes at \(t = 18:13:49\). We chose this point as it corresponds to half the interval which delimits the current sheet.

The normal thus obtained is \(\hat{n}_{\text{fit}} = (0.856, -0.066, 0.512)\), a value that differs by 21° from that of the normal obtained by applying MVA and by 31° from the \(\hat{x}\) axis. The mean value of the magnetic field along this normal is \(\langle B_3 \rangle = -1.72\text{nT}\), which when comparing it to \(B_0\) yields \(\langle B_3 \rangle/B_0 = 0.05\). The angle \(\theta_B\) between the mean magnetic field vector and this normal is \(\theta_B = 92.8°\). We observe again that the magnetic field is almost tangential to the boundary.
In the Successive Columns, the Following Data of the Six MPB Crossings Are Displayed: Date, Time, Minimum and Maximum MPB Thickness, Ion Inertial Length, Larmor Radius, Volume Current Density, Hall Electric Force per Unit Volume, Solar Wind Dynamic Pressure Upstream From the Shock, and Magnetic Pressure Downstream From the MPB.

| Date       | $t_2 - t_1$ (UTC) | $h_{23}$ | $h_{14}$ | $c/\omega_{pi}$ | $r_g$ | $|\mathbf{j}_v|$ | $|\mathbf{F}|$ | $P_{dyn}$ | $P_{mag}$ |
|------------|-------------------|----------|----------|-----------------|-------|-----------------|---------|-----------|----------|
| 2015-Oct-10| 12:41:58          | 39       | 97       | 159             | 203   | 403             | $4.37 \times 10^{-14}$ | 0.55 ± 0.14a | 0.64 ± 0.06a |
| 2015-Oct-12| 19:19:09          | 19       | 73       | 133             | 62    | 255             | $3.80 \times 10^{-14}$ | 0.37 ± 0.10 | 0.56 ± 0.04 |
| 2016-Mar-16| 18:14:40          | 82       | 174      | 98              | 68    | 282             | $1.20 \times 10^{-14}$ | 0.88 ± 0.04 | 0.86 ± 0.03 |
| 2016-Mar-31| 13:04:25          | 39       | 122      | 101             | 76    | 401             | $1.34 \times 10^{-14}$ | 0.56 ± 0.03 | 0.52 ± 0.09 |
| 2016-Apr-05| 05:16:22          | 44       | 175      | 130             | 168   | 363             | $0.92 \times 10^{-14}$ | 0.21 ± 0.19 | 0.32 ± 0.02 |
| 2017-Nov-24| 12:15:06          | 115      | 447      | 120             | 46    | 92              | $2.04 \times 10^{-14}$ | 0.03 ± 0.11 | 0.28 ± 0.03 |

Note. Dates are formatted as yyyy-Mmm-dd.

These values were obtained using SWICS data as there are no SWICA data available for the selected crossing.

We obtained $\theta_0 = 101^\circ$, which is consistent with the motion of the spacecraft being almost parallel to the surface of the MPB.

In the same way as before, we estimated $h$ in the intervals $t_1 - t_2$ and $t_3 - t_4$. In this case, the obtained values are smaller, which is to be expected given that the angle $\theta_0$ is smaller, yielding $h_{23} = 34$ km and $h_{14} = 71$ km.

In general, we consider the results derived from MVA to be more representative of reality, since this method is based on the local properties of the magnetic field at the time of the crossing. Nonetheless, results show a good agreement between the local (MVA) and the macroscopic (fit) normals, and in both cases we observe that the normal points mostly along $+\hat{x}$, which is consistent with a SZA close to $25^\circ$.

In Table 1 are displayed the thickness of the MPB obtained from MVA, the solar wind convective proton inertial length, and the convective Larmor radius for six subsolar MPB crossings (SZA < 30°). In all cases the normal is well defined ($\lambda_2/\lambda_1 > 9$) and points mainly along the $x$ axis. A case for the MPB thickness being of the order of the ion inertial length as well as the Larmor radius could be made for all crossings.

### 3.1. Current Density and the Hall Electric Force at the MPB

We estimated the current density along the boundary from Ampère’s Law in a discontinuity, assuming that the MPB is a planar surface of negligible thickness. If $\hat{n}$ is the surface normal and $\mathbf{B}_n$, $\mathbf{B}_d$ are the magnetic field measurements upstream in the magnetosheath and downstream in the MPR, respectively, the surface current density $\mathbf{j}_s$ will be given by

$$\mathbf{j}_s = \frac{1}{\mu_0} \hat{n} \times (\mathbf{B}_n - \mathbf{B}_d)$$

We calculated $\mathbf{B}_n$ by taking the average value of $\mathbf{B}$ between 18:12:06 and 18:13:00 UTC and $\mathbf{B}_d$ between 18:14:51 and 18:15:45 UTC; these intervals are shaded in Figure 2. The values thus obtained were $\mathbf{B}_n = (4.58,19.24, -6.2)$ nT and $\mathbf{B}_d = (18.64,31.9, -28.59)$ nT. The intervals were selected because they were outside the MPB but without large variations in the magnetic field, in order to be representative of what happens at the boundary.

The surface current density obtained based on the MVA normal yields $\mathbf{j}_{MVA}^{\text{MVA}} = (-2.9, -19.2, -12.6)$ mA/m and its magnitude $|\mathbf{j}_{MVA}^{\text{MVA}}| = 23.2$ mA/m; whereas when the fit normal is used, $\mathbf{j}_{\text{fit}}^{\text{fit}} = (4.0, -21.0, -9.4)$ mA/m, $|\mathbf{j}_{\text{fit}}^{\text{fit}}| = 23.3$ mA/m.

Under the previous approximations one can think of $\mathbf{j}_v$ being constant throughout the MPB. In that case, a volume current density can simply be estimated as $\mathbf{j}_v/h = \mathbf{j}_s$; we considered for this the minimum thickness $h_{23}$ yielded by both the MVA and the fit. Using the MVA normal, we obtained $\mathbf{j}_{MVA}^{\text{MVA}} = (-35, -233, -154)$ nA/m² and its magnitude $|\mathbf{j}_{MVA}^{\text{MVA}}| = 282$ nA/m². On the other hand, using the fit normal we obtained $\mathbf{j}_{\text{fit}}^{\text{fit}} = (48, -255, -113)$ nA/m² with modulus $|\mathbf{j}_{\text{fit}}^{\text{fit}}| = 284$ nA/m².

The values of $\mathbf{j}_v$ and $\mathbf{j}_s$ obtained with both methods are consistent not only between them but with the values we obtained for different MPB crossings (shown in Table 1) and those given by Bertucci et al. (2005) for an MPB crossing with SZA = 63° from MGS data where they obtained $|\mathbf{j}_s| = 6.5$ mA/m, $|\mathbf{j}_v| = 81$ nA/m².
Next, we calculate the Hall electric force per unit volume as \( F = \mathbf{j}_H \times \mathbf{B} \). From \( \mathbf{j}_H^{MVA} \) we obtained the force \( \mathbf{F}^{MVA} = (10.0, -3.3, 2.3) \times 10^{-15} \text{N/m}^3 \) and from \( \mathbf{j}_H^{fit} \) the force \( \mathbf{F}^{fit} = (9.4, -0.7, 5.6) \times 10^{-15} \text{N/m}^3 \).

The Hall electric force is associated with the Hall term \( \mathbf{E}_H = \frac{1}{c} \mathbf{j} \times \mathbf{B} \) in the generalized Ohm’s Law (Equation 2). The force (and therefore, the Hall electric field) points mainly along the +\( \hat{x} \) axis, opposing the motion of the solar wind ions, which travel in –\( \hat{x} \), and accelerating the planetary ions. The Hall electric field calculated from the values obtained through the MVA is \( \mathbf{E}_H^{MVA} = (26.37, -8.44, 6.85) \text{mV/m} \), while the field calculated from the values obtained from the fit is \( \mathbf{E}_H^{fit} = (24.42, -1.85, 14.52) \text{mV/m} \).

Below, we show that the magnetic pressure at the MPR is indeed sufficient to stop the solar wind ions. If steady state is assumed and if the magnetic tension force is neglected, a total pressure conservation (\( P_{total} = \text{constant} \)) along a streamline antiparallel to the \( \hat{x} \) axis can be obtained from 3:

\[
P_{total} = P_{dyn} + P_{in} + P_{mag}
\]

where \( P_{dyn} = mnv^2 \), \( P_{in} = P_{e} + P_{i} \), and \( P_{mag} = B^2/2\mu_0 \). As explained in Spreiter and Stahara (1992) the dynamic pressure is dominant in the supersonic solar wind while the magnetic pressure is dominant in the MPR. Therefore, to stop the solar wind ions in the subsolar sector, the magnetic pressure in the MPR should be approximately equal to the solar wind pressure upstream from the shock. In the upstream interval 17:30–17:40 UTC, the dynamic pressure obtained from SWIA fine archive data is \( P_{dyn} = 0.88 \pm 0.04 \text{nPa} \), while the average magnetic pressure downstream from the MPR (shaded area in Figure 2) yields \( P_{mag} = 0.86 \pm 0.03 \text{nPa} \). The values obtained for the solar wind \( P_{dyn} \) and MPR \( P_{mag} \) for the other crossings are listed in Table 1.

4. Discussion and Conclusions

In this work we report on the properties of the Hall electric force associated with the current layer detected at the Martian MPB in the subsolar region from high-resolution data. The current is detected from the change in the tangential component of the magnetic field at the MPB. The intensities of the surface current density for the six analyzed crossings range from 10.7 to 39.2 mA/m. This represents a factor 2 increase with respect to the values derived from MGS data by Bertucci et al. (2005) closer to the terminator (6.5 mA/m at SZA = 63°). Although the sample is too small to deduce any general trend with SZA, the higher \( j_b \) values in the subsolar sector would be consistent with a stronger pileup (Dubinin et al., 2011) and/or a narrower MPB around the subsolar sector. The volume current density ranges from 92 to 400 nA/m², up to 20 times greater than the values obtained by Ramstad et al. (2020). Nonetheless, this discrepancy is to be expected as our study is centered on the sub-ion scale of the MPB whereas theirs do not resolve structures smaller than 339 km. It too must be noted that as our selection consisted in crossings with a sharp increase in the magnetic field it may be biased toward greater values of \( j_b \).

Another key point is the thickness of the MPB. We find a strong variability in our estimates (from 18 to 450 km) which is likely a result of the MPB moving with respect to the planet at speeds comparable to the spacecraft velocity during the crossing (Bertucci et al., 2005). Unfortunately this effect cannot be corrected due to the nature of single-spacecraft observations. Nevertheless, most cases display thicknesses that are loosely compatible with both the magnetosheath solar wind proton inertial length and with their gyroradius (see Table 1). If the MPB thickness is somehow determined by \( c/\omega_{pi} \), a two-fluid MHD description should be able to theoretically capture this feature. On the other hand, if the thickness is determined by the Larmor radius, kinetic effects would need to be considered. The fact that these two length scales are not too dissimilar, makes it more difficult to discriminate between these two scenarios. A similar discussion takes place with the Earth magnetopause, as reported by Haaland et al. (2020) using Magnetospheric Multiscale (MMS) data for a large number of crossings.

The magnetic pressure term in the Hall electric force is roughly inversely proportional to the MPB thickness while the magnetic tension is inversely proportional to the curvature radius of the magnetic field lines. As the MPB thickness is of the order of the hundred kilometers, while the typical radius of curvature of the draped magnetic field in the subsolar region is roughly 4,000 km (Vignes et al., 2000), the first term will be at least 1 order of magnitude greater than the second. In the induced magnetotail, however, the magnetic tension dominates (Dubinin et al., 1993).
In the six subsolar passes, the Hall electric force points in a direction not far from \( \hat{x} \) (i.e., sunward) and its strength varies between \( 2.4 \times 10^{-15} \) and \( 4.37 \times 10^{-14} \) N/m\(^3\). These values are 1 or 2 orders of magnitude stronger than the magnetic pressure gradients obtained by Halekas et al. (2017). However, they report that their Hall electric force (which in that paper is called Lorentz force) estimations might be underestimated as their values were averaged over large spatial intervals. As shown in Table 1, the magnetic pressure measured in the MPR is comparable to or higher than the dynamic pressure in the solar wind. This means that the derived Hall electric force is strong enough to eventually stop the solar wind ions from going through the MPB.

A net force in the sunward direction contributes to the deceleration of the solar wind ions near the MPB while pushing the solar wind electrons inward into the MPR. This would favor a decoupling between the solar wind protons and electrons (due to the Hall effect) as they struggle to enter the induced magnetosphere, while the solar wind electrons push the IMF through the MPB thus contributing to the magnetic barrier buildup (Dubinin et al., 2011). In such a scenario the IMF would be frozen in to the electron plasma, not the ion plasma; quantifying this from direct measurements is a major challenge even for multisatellites missions such as MMS (Lundin et al., 2005). In the meantime, quasi-neutrality across the MPB would be ensured by planetary ions which would be accelerated upward by the sunward force. Some of these planetary ions would be able even to get out of the MPR although once in the magnetosheath they could be reaccelerated either by the electron pressure gradient (back into the MPR) or by the convective electric field into the plume (Dong et al., 2015).

In summary, our results are consistent with a thickness for the Martian MPB of the order of an ion inertial length. However, we cannot rule out the possibility that the MPB thickness is determined by the convective Larmor radius of solar wind protons, since (1) these two length scales are not too dissimilar, and (2) we are bound by the limitations of single-spacecraft observations.

**Data Availability Statement**

All data used are publicly available on the NASA Planetary Data System (https://pds.nasa.gov). In particular, MAG data are available in https://pds-ppi.igpp.ucla.edu/search/view/?f=yes&id=pds://PPI/maven.mag.calibrated/data/ss/highres/ selecting the appropriate date. SWIA data are available in https://pds-ppi.igpp.ucla.edu/search/view/?f=yes&id=pds://PPI/maven.swia.calibrated/data selecting coarse or fine in archive or survey mode depending on the use of SWICA/S or SWIFA/S. SWEA data are available in https://pds-ppi.igpp.ucla.edu/search/view/?f=yes&id=pds://PPI/maven.swea.calibrated/data/ss/highres/ selecting the appropriate date.

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