On New Centroid Based Techniques for Solving Fuzzy Linear Programming Problems

Sudip Bhattacharyya and Pinaki Majumdar
Department of Mathematics, M.U.C Women’s College, Burdwan, West-Bengal, India

Abstract
In this paper we have proposed some new techniques based on the centroid of triangular and trapezoidal fuzzy numbers to solve a fuzzy linear programming problem. These proposed methods are easy to implement with less number of arithmetic operations required compared to the existing methods. To illustrate the proposed method, numerical examples are given. A comparative study between the proposed methods and existing methods are given at the end. The superiority of these centroid based methods over known ranking function method has also been shown with an example.

Keywords: Fuzzy linear programming problem (FLPP), Fully fuzzy linear programming problem (FFLPP), Triangular fuzzy number, Trapezoidal fuzzy numbers, Centroid

1. Introduction
The history of fuzzy operations research is nearly 40 years old now. It started with Beliman & Zadeh [1], although Zimmermann [2] first conceived the notion of fuzzy linear programming problem (FLPP). After that many authors have studied the notion of LPP in fuzzy settings. Fang et al. [3] introduced LPP with fuzzy constraints. Maleki and his colleagues [4, 5] considered LPP with fuzzy variables and computed the solution by considering the auxiliary problem. Fuzzy basic feasible solution for the fuzzy variable linear programming problem (FVLPP) [6, 7] and also the simplex algorithm along with the optimality conditions were studied by Mahdavi-Amiri and Nasseri [8]. Later Lotfi et al. [9] proposed a new method for finding the optimal solution of fully fuzzy linear programming problems. Allahviranloo et al. [10] proposed a new method to solve fully fuzzy linear programming problem (FFLPP) using ranking function. Kumar et al. [11] proposed FFLPP with inequality constraints by representing all the coefficients as triangular fuzzy numbers. Karpagam and Sumathi [13] proposed a new technique to solve FVLPP using ranking function. Although there are several techniques available for finding the solution of a FLP, but most of them requires a lot of rigorous calculations. Therefore our objective in this paper is to introduce some new techniques for solving FLPP which are easy to compute and gives better results. Here we have proposed a couple of centroid based methods to solve a FLPP. All these proposed methods are new and easy to implement as they require less number of arithmetic operations in comparison to other available methods. We have also shown the accuracy and compatibility of our techniques using numerical problems and established their superiority over other available methods.
The rest of the paper is organized as follows: in Section 2, some preliminary definitions related to fuzzy sets and FLPP are given. In Section 3, the brief algorithm and methods to solve a FLPP are discussed. In Section 4, a numerical example has been selected and solved by the proposed techniques discussed in the previous section. Section 5 contains results and discussions. Finally the last section concludes the article.

2. Preliminaries

In this section, we recall some definitions related to fuzzy sets, fuzzy numbers, LPP, FLPP, FFLPP, triangular fuzzy number, and trapezoidal fuzzy number, etc., which will be used for the rest of the paper.

Definition 2.1. If \( X \) is a collection of objects, then a fuzzy set \( \tilde{A} \) in \( X \) is a set of ordered pairs: \( \tilde{A} = \{(x, \mu_A(x)) \mid x \in X\} \), where \( \mu_A(x) \) is called the membership function or grade of membership (also degree of compatibility or degree of truth) of \( x \) in \( \tilde{A} \) that maps \( X \) to the membership space \( M \) i.e., \( \mu_A : X \to M = [0, 1] \).

Definition 2.2. The crisp LPP is formulated as follows:

Optimize \( \sum_{j=1}^{n} c_j x_j \) subject to \( \sum_{j=1}^{n} a_{ij} x_j (\leq \text{ or } = \text{ or } \geq) b_i \),

where \( x_j \geq 0, i = 1, 2, 3, ..., m \) and \( j = 1, 2, 3, ..., n \). Here \( x_j \)'s are the decision variables, \( c_j \)'s are the price parameters, \( a_{ij} \)'s are the activity parameters and \( b_i \)'s are the requirement parameters and all of them assume real number as their values.

Definition 2.3. A fuzzy number is a generalization of real numbers, i.e., fuzzy number is a quantity whose value is not fixed. It can be considered as a function from the real number set to the set of real numbers between and including 0 and 1. Each number at the domain is assigned a specific membership grade, where 0 is the smallest possible membership grade where \( a \) is the largest possible membership grade.

Definition 2.4 [13]. A LPP is called FFLPP, if parameters and variables all are fuzzy numbers. General form of FFLPP is as follows:

Optimize \( \tilde{z} = \sum_{j=1}^{n} \tilde{c}_j \tilde{x}_j \) subject to \( \sum_{j=1}^{n} \tilde{a}_{ij} \tilde{x}_j (\leq \text{ or } = \text{ or } \geq) \tilde{b}_i \),

where \( \tilde{x}_j \geq 0, \tilde{c}_j \in (F(R))^m, \tilde{a}_{ij} \in (F(R))^{m \times n}, \tilde{b}_i \in (F(R))^m, \tilde{c}_j \in (F(R))^n, F(R) \) is the set of all fuzzy numbers.

In case of FLPP the variables are crisp, i.e., real valued. So a FFLPP is more general in nature than FLPP.
3. Solution Methods for Fuzzy LPP

In this section we shall discuss about the techniques to solve a FLPP.

**Method 1.** Solution using triangular fuzzy number and a ranking function:

This method is described in [11] and is based on certain ranking function of triangular fuzzy numbers. Here all the parameters are represented by triangular fuzzy numbers which was ultimately defuzzified using ranking function to reduce the FLPP to a crisp LPP.

**Algorithm 1.**

**Step 1:** First of all, we replace the crisp numbers \((c_j, a_{ij} \text{ and } b_i)\) of a LPP with the triangular fuzzy numbers to obtain a FLPP, i.e.,

\[
\max \tilde{z} = \tilde{c}_j \tilde{x}_j \text{ subject to } \tilde{a}_{ij} \tilde{x}_j \leq \tilde{b}_i, \quad \tilde{x}_j \geq 0.
\]

**Step 2:** Using the ranking function \(R(\tilde{c}, \tilde{A}) = \frac{b + 2a - \beta}{2}\) for a triangular fuzzy number \(\tilde{A} = (b, \alpha, \beta)\).

Let us take a triangular fuzzy number \((a, b, c)\), with peak as \(b\). Now calculate \(\alpha = b - a\) and \(\beta = c - b\). Then apply the ranking function to get a defuzzified form of that number. Apply this technique to all the triangular fuzzy numbers to get a defuzzified LPP.

**Step 3:** Solve the defuzzified LPP by simplex method. Before that, convert all the constraints into equations by adding slack variables with cost 0.

**Step 4:** Compute the value of \(\tilde{z}_j - \tilde{c}_j\) where \(\tilde{z}_j = \sum_{i=1}^{m} C_{ij} \tilde{y}_{ij}\) for \(j = 1, 2, ..., n\). If all those values are positive for all \(j\), then the optimality is satisfied. Otherwise go to Step 5.

**Step 5:** If at least one \(\tilde{z}_j - \tilde{c}_j < 0\), then the most minimum of all \(\tilde{z}_j - \tilde{c}_j\) is chosen. If \(\min(\tilde{z}_j - \tilde{c}_j) = \tilde{z}_k - \tilde{c}_k\) then the variable \(x_k\) is the entering variable and this column is called key column. Also compute \(\min \left\{ \frac{\tilde{y}_{ik}}{y_{rk}}, y_{rk} > 0 \right\}\). If this minimum is unique and occurs at \(i = r\), then the \(r\)-th variable of the basis is the departing variable and the row is called key row. The element at the intersection of the key row and key column, i.e., \(y_{rk}\) is called the pivot element.

**Step 6:** Perform the pivot operation and return to Step 4.

End of algorithm.

Next we propose the following three methods which involve the centroid of triangular and trapezoidal fuzzy numbers instead of any arbitrary ranking functions. This is used because the techniques of finding the centroid of triangular or trapezoidal fuzzy numbers are well known and easy to determine. Also the centroid preserves the characteristics of the original fuzzy number.

**Method 2.** Solution using centroid of a triangular fuzzy number:

The algorithm is almost same with Method 1 except that in Step 2 of Algorithm 1, we replace the ranking function by the centroid of the triangle [9] with vertices \(a, b\) and \(c\) as \(G(a, b, c) = \frac{a + b + c}{3}\) and then perform all the steps of the above algorithm to solve the FLPP.

**Method 3.** Solution using centroid of a trapezoidal fuzzy number:

The algorithm is almost same with Method 1 except that in Step 1 of Algorithm 1, we use the trapezoidal fuzzy numbers instead of triangular fuzzy numbers.

In Step 2, we defuzzify the trapezoidal fuzzy numbers using the centroid formula of Trapezoidal numbers given in [9] as follows:

\[
C(\alpha, \beta, \gamma, \delta) = \frac{2ac + a^2 + bc + ab + b^2}{3(a + b)},
\]

where \(a = \gamma - \beta; b = \delta - \alpha; c = \beta - \alpha m\) and \(\alpha, \beta, \gamma, \delta\) are the abcissa of the vertices of the trapezium. Then follow the similar steps to solve the FLPP.

**Method 4.** Solution using trapezoidal fuzzy numbers and the centroid of centroids formula.

In Step 2, of the above algorithm, we defuzzify the trapezoidal fuzzy numbers using the centroid of centroids formula [9].

Here ABCD is the trapezoidal representation of the trapezoidal fuzzy number \((\alpha, \beta, \gamma, \delta)\). Now, join BF. So, here we get three triangles \(\triangle ABF, \triangle BCF\) and \(\triangle CDF\). We compute the centroids of the triangles and let \(G_1, G_2\) and \(G_3\), respectively be the centroids of them.

So as discussed in Method 3, we have:

\[
G_1 = \frac{\alpha + \beta + \gamma}{3}, \quad G_2 = \frac{\beta + \gamma + \delta}{3} \quad \text{and} \quad G_3 = \frac{\gamma + \delta}{3}.
\]

Now we get a triangle made by those centroids, viz \(G_1G_2G_3\). If \(G\) is the centroid of this triangle, then \(G = \frac{G_1 + G_2 + G_3}{3}\) and we can consider this centroid \(G\) is the centroid of the trapezium ABCD.

Now, to solve the FLPP, we have to follow the similar steps.
4. A Numerical Example to Show the Application of the Proposed Methods

The normal or crisp LPP model the cases when there are no uncertainties associated with the parameters related to the problem. But if there are uncertainties in price, activity or requirement parameters associated to any problem then FLPP is used to model such cases. To illustrate such a case consider the following problem: Suppose a petrol pump sells two types of petrol, namely ‘normal’ and ‘speed’. But the price of each type of petrol may change slightly on day to day basis. Let the selling price of them is approximately 3 and 4 units, respectively. The storage capacities of normal and speed are approximately in the ratio of 3 : 4 with total capacity of 24 units. Again the cost price of each kind of petrol is more or less 1 and 3 units respectively. And the owner of the petrol pump can spend nearly 15 units of money each day for buying petrol. Now what are the amount of each kind of petrol is more or less ratio of 3 : 4 units. Again the cost price of them is approximately

\[ 3x_1 + x_2 + x_3 = 15, \]
\[ 3x_1 + 4x_2 + x_4 = 24, \quad x_i \geq 0, \quad i = 1, 2, 3, 4. \]

So, optimality satisfied and the solution is: \( x_1 = 4, x_2 = 3 \) and \( max \ z = 25 \).

Method 4.1. Solution using triangular fuzzy number and a ranking function \[ \text{[13]:} \]

Now let us convert the crisp LPP into a FFLPP using Triangular fuzzy numbers as follows:

\[
\begin{align*}
\max \ & \tilde{z} = (1.5, 4, 5.3)\tilde{x}_1 + (1.9, 3, 3.7)\tilde{x}_2 \quad \text{subject to} \\
& (1.7, 3, 4.2)\tilde{x}_1 + (0.7, 1, 1.1)\tilde{x}_2 \leq (5, 15, 20.3), \\
& (1.6, 3, 4.5)\tilde{x}_1 + (1.8, 4, 6.4)\tilde{x}_2 \leq (11.8, 24, 26.2), \\
& \tilde{x}_i \geq 0, \quad i = 1, 2.
\end{align*}
\]

Let us apply the ranking function as defined above to defuzzify the Triangular fuzzy numbers and also introduce the slack variables as follows:

\[
\max \tilde{z} = 3.85\tilde{x}_1 + 2.25\tilde{x}_2 + 0.\tilde{x}_3 + 0.\tilde{x}_4 \quad \text{subject to} \\
2.2\tilde{x}_1 + 0.75\tilde{x}_2 + \tilde{x}_3 = 14.85, \\
2.15\tilde{x}_1 + 3\tilde{x}_2 + \tilde{x}_4 = 23.1,
\]

Table 1. Simplex table of Method 4.0

| \( C_B \) | \( x_B \) | \( c_j \) | 4 | 3 | 0 | 0 | \( \text{Min ratio} \) |
|-----------|---------|--------|---|---|---|---|-------------------|
| 0         | \( x_3^* \) | 15     | 3* | 1 | 1 | 0 | \( \frac{15}{3} = 5^* \) |
| 0         | \( x_4 \) | 24     | 3  | 4 | 0 | 1 | \( \frac{24}{3} = 8 \) |

\( z_j - c_j \)

| 4 | \( x_1 \) | 5 | 1 | \( \frac{1}{3} \) | \( \frac{1}{3} \) | 0 | 15 |
| 0 | \( x_4^* \) | 9 | 0 | 3* | -1 | 1 | 3* |

\( z_j - c_j \)

| 20 | 0 | \( -\frac{5}{3}^* \) | \( \frac{1}{3} \) | 0 |
| 4  | \( x_1 \) | 4 | 1 | 0 | \( \frac{4}{3} \) | \( -\frac{1}{3} \) |
| 3  | \( x_2 \) | 3 | 0 | 1 | \( \frac{1}{3} \) | \( \frac{5}{3} \) |

\( z_j - c_j \)

| 25 | 0 | 0 | \( \frac{7}{3} \) | \( \frac{5}{3} \) |
As shown in Table 2, optimality satisfied and the solution is:
\( \tilde{x}_1 = 5.42, \tilde{x}_2 = 3.873, \max \tilde{z} = 29.581 \).

**Method 4.2.** Solution using triangular fuzzy numbers and the centroid formula:

Now we defuzzify the triangular fuzzy numbers using the centroid formula, i.e.,
\[ G(a, b, c) = \frac{a + b + c}{3}, \]
where \( a, b \) and \( c \) are the vertices of the triangle.

So, the above FLPP is defuzzified as follows:
\[
\begin{align*}
\max \tilde{z} & = 3.6\tilde{x}_1 + 2.867\tilde{x}_2 + 0.\tilde{x}_3 + 0.\tilde{x}_4 \\
& \quad \text{subject to} \\
2.967\tilde{x}_1 + 0.933\tilde{x}_2 + \tilde{x}_3 & = 13.43, \\
3.033\tilde{x}_1 + 4.067\tilde{x}_2 + \tilde{x}_4 & = 20.66, \\
\tilde{x}_i & \geq 0, \; i = 1, 2, 3, 4.
\end{align*}
\]

As shown in Table 3, optimality satisfied and the solution is:
\( \tilde{x}_1 = 3.824, \tilde{x}_2 = 2.233, \max \tilde{z} = 20.168 \).

**Method 4.3** Solution using centroid of trapezoidal fuzzy numbers:

Now let us convert the crisp LPP into a FLPP using Trapezoidal fuzzy numbers as follows:
\[
\begin{align*}
\max \tilde{z} & = (0.8, 2.5, 4.8, 6.2)\tilde{x}_1 + (0.2, 1.8, 4.6, 5.8)\tilde{x}_2 \\
& \quad \text{subject to} \\
(0.5, 1.6, 4.8, 5.5)\tilde{x}_1 + (0.1, 0.6, 1.2, 1.7)\tilde{x}_2 & \leq (1.5, 12.2, 19.6, 30.8), \\
(0.1, 1.2, 4.2, 6.5)\tilde{x}_1 + (0.6, 2.3, 4.9, 7.1)\tilde{x}_2 & \leq (2.6, 21.3, 30.8, 50.8), \\
\tilde{x}_i & \geq 0, \; i = 1, 2.
\end{align*}
\]

Now we defuzzify the trapezoidal fuzzy numbers using the
Table 4. Simplex table of Method 4.3

| C_B  | x_B   | c_j | 3.5  | 2.88 | 0   | 0   | Min ratio |
|------|-------|-----|------|------|-----|-----|-----------|
| 0    | x_3^* | 14.54 | 2.5^* | 0.8  | 1   | 0   | 3.144^*   |
| 0    | x_4   | 23.48 | 2.93  | 3.14 | 0   | 1   | 3.894     |

| z_j - c_j | 0       | -3.5^* | -2.88 | 0   | 0   |

| 3.5 | x_1   | 5.816 | 1     | 0.32 | 0.337 | 0   | 18.175   |
| 0   | x_4^* | 6.739 | 0     | 2.202* | -1.172 | 1   | 3.060^* |

| z_j - c_j | 20.356 | 0    | -1.76 | 1.4  | 0   |

| 3.5 | x_1   | 4.837 | 1     | 0    | 0.570 | -0.145 |
| 2.88 | x_2   | 3.060 | 0     | 1    | -0.532 | 0.454 |

| z_j - c_j | 25.742 | 0    | 0     | 0.463 | 0.8 |

Table 5. Simplex table of Method 4.4

| C_B  | x_B   | c_j | 4    | 3.622 | 0   | 0   | Min ratio |
|------|-------|-----|------|------|-----|-----|-----------|
| 0    | x_3^* | 17.189 | 3.689^* | 1    | 1   | 0   | 4.659^*   |
| 0    | x_4   | 27.778 | 3.333  | 4.089 | 0   | 1   | 8.33      |

| z_j - c_j | 0       | -4^*  | -3.622 | 0   | 0   |

| 4    | x_1   | 4.659 | 1    | 0.271 | 0.271 | 0    | 17.19     |
| 0    | x_4   | 11.471 | 0     | 3.186 | -0.903 | 1    | 3.6^*     |

| z_j - c_j | 18.636 | 0    | -2.538 | 1.262 | 0   |

| 4    | x_1   | 3.683 | 1     | 0    | 0.348 | -0.085 |
| 3.622 | x_2   | 3.6   | 0     | 1    | -0.283 | 0.314 |

| z_j - c_j | 27.771 | 0    | 0     | 0.367 | 0.797 |

centroid formula, i.e.,

\[ C(\alpha, \beta, \gamma, \delta) = \frac{2ac + a^2 + bc + ab + b^2}{3(a + b)}, \]

where \( a = \gamma - \beta; b = \delta - \alpha; c = \beta - \alpha \) and \( \alpha, \beta, \gamma, \delta \) are the abscissa of the vertices of the trapezium.

So, the above FLPP is defuzzified as follows:

\[ \text{max } \tilde{z} = 3.5\tilde{x}_1 + 2.88\tilde{x}_2 + 0.\tilde{x}_3 + 0.\tilde{x}_4 \text{ subject to} \]

\[ 2.5\tilde{x}_1 + 0.8\tilde{x}_2 + \tilde{x}_3 = 14.54, \]

\[ 2.93\tilde{x}_1 + 3.14\tilde{x}_2 + \tilde{x}_4 = 23.78, \]

\[ \tilde{x}_i \geq 0, i = 1, 2, 3, 4. \]

As shown in Table 4, optimality satisfied and the solution is:
\( \tilde{x}_1 = 4.837, \tilde{x}_2 = 3.060, \text{max } \tilde{z} = 25.742. \)

Method 4.4. Solution using trapezoidal fuzzy numbers and the centroid of centroids formula:

\[ \text{Using this technique, the above trapezoidal FLPP is reduced to a crisp LPP as follows:} \]

\[ \text{max } \tilde{z} = 4\tilde{x}_1 + 3.622\tilde{x}_2 + 0.\tilde{x}_3 + 0.\tilde{x}_4 \text{ subject to} \]

\[ 3.689\tilde{x}_1 + \tilde{x}_2 + \tilde{x}_3 = 17.189, \]

\[ 3.333\tilde{x}_1 + 4.089\tilde{x}_2 + \tilde{x}_4 = 27.778, \]

\[ \tilde{x}_i \geq 0, i = 1, 2, 3, 4. \]

As shown in Table 5, \( \tilde{x}_1\tilde{x}_2\text{max } \tilde{z}\tilde{x}_1\tilde{x}_2\text{max } \tilde{z}\text{Optimality satisfied and the solution is: } \tilde{x}_1 = 3.683, \tilde{x}_2 = 3.6, \text{max } \tilde{z} = 27.771. \)

5. Results and Discussion

In the above section we have considered a practical problem and represented it in terms of a FLPP where the constants...
Table 6. Comparison of results

|       | Crisp | Ranking function | Centroid using triangular fuzzy numbers | Centroid using trapezoidal fuzzy numbers | Centroid of trapezoidal fuzzy numbers |
|-------|-------|------------------|-----------------------------------------|------------------------------------------|---------------------------------------|
| \( \hat{x}_1 \) | 4     | 5.42             | 3.824                                   | 4.837                                    | 3.683                                 |
| \( \hat{x}_2 \) | 3     | 3.873            | 2.233                                   | 3.060                                    | 3.6                                    |
| \( \max \hat{z} \) | 25    | 29.581           | 20.168                                  | 25.742                                   | 27.771                                 |

are fuzzy numbers. Also it can be considered as a normal LPP if we neglect the uncertainty factors described there. We have first solved this FLPP by a known method using ranking function. Also for crisp case we have used well known ‘simplex method’ to solve it. Then we have applied our new centroid based methods (3 in number) to solve the FLPP. The results obtained by all these five method are represented in tabular form (Table 6).

Here we see that the results obtained by our proposed methods are different from the results obtained using the known ranking function method [13]. Also our results are comparatively closer with the results obtained by solving crisp LPP. But in all cases the results of FLPP are not equal with crisp LPP results, which is natural due to the presence of uncertainty in FLPP. On the other hand centroid of triangular and trapezoidal fuzzy numbers retains the properties of the original fuzzy number to a large extent. This shows the superiority of our proposed centroid based techniques instead of taking ranking functions. Also it can be said undoubtedly that our proposed methods involves only the calculation of centroid of triangular and trapezoidal fuzzy numbers, which is very elementary, and then the use of simplex method.

6. Conclusion

In this paper some new methods to solve a FLPP based on centroid of triangular and trapezoidal fuzzy numbers has been proposed. Also a method based on the centroid of centroids of a trapezoidal fuzzy number has been introduced. In these methods a FLPP is defuzzified into a crisp LPP using the proposed methods and solving it using simplex method. Since centroids are well equipped to express the features of the triangular or trapezoidal fuzzy numbers, so these methods are more realistic than the existing methods based on the ranking function. Also the calculation for finding the centroid of a triangular and a trapezoidal number is very simple. The numerical example also clearly proves the superiority of our proposed methods.

Conflict of Interest

No potential conflict of interest relevant to this article was reported.

References

[1] R. E. Bellman and L. A. Zadeh, “Decision-making in a fuzzy environment,” Management Science, vol. 17, no. 4, pp. B141-B273, 1970. [https://doi.org/10.1287/mnsc.17.4.B141]

[2] H. J. Zimmermann, “Fuzzy programming and linear programming with several objective functions,” Fuzzy Sets and Systems, vol. 1, no. 1, pp. 45-55, 1978. [https://doi.org/10.1016/0165-0114(78)90031-3]

[3] S. C. Fang, C. F. Hu, H. F. Wang, and S. Y. Wu, “Linear programming with fuzzy coefficients in constraints,” Computers & Mathematics with Applications, vol. 37, no. 10, pp. 63-76, 1999. [https://doi.org/10.1016/S0898-1221(99)00126-1]

[4] H. R. Maleki, M. Tata, and M. Mashinchi, “Linear programming with fuzzy variables,” Fuzzy Sets and Systems, vol. 109, no. 1, pp. 21-33, 2000. [https://doi.org/10.1016/S0165-0114(98)00066-9]

[5] H. R. Maleki, “Ranking functions and their applications to fuzzy linear programming,” Far East Journal of Mathematical Sciences, vol. 4, no. 3, pp. 283-301, 2002.

[6] Kolman and Hill, “Fuzzy variable linear programming problem by use of a certain linear ranking function,” Applied Mathematics, vol. 18, 1984.

[7] S. H. Nasseri, E. Ardil, A. Yazdani, and R. Zaefarian, “Simplex method for fuzzy variable linear programming.
problems,” International Journal of Mathematical, Computational, Physical, Electrical and Computer Engineering, vol. 3, no. 10, pp. 884-888, 2005.

[8] N. Mahdavi-Amiri and S. H. Nasseri, “Duality in fuzzy variable linear programming,” in Proceedings of the 4th World Enformatika Conference (WEC), Istanbul, Turkey, 2005, pp. 24-26.

[9] F. H. Lotfi, T. Allahviranloo, M. A. Jondabeh, and L. Alizadeh, “Solving a full fuzzy linear programming using lexicography method and fuzzy approximate solution,” Applied Mathematical Modelling, vol. 33, no. 7, pp. 3151-3156, 2009. https://doi.org/10.1016/j.apm.2008.10.020

[10] T. Allahviranloo, F. L. Lotfi, M. K. Kiasary, N. A. Kiani, and L. Alizadeh, “Solving fully fuzzy linear programming problem by the ranking function,” Applied Mathematical Sciences, vol. 2, no. 1, pp. 19-32, 2008.

[11] 564426024A. Kumar, J. Kaur, and P. Singh, “Fuzzy optimal solution of fully fuzzy linear programming problems with inequality constraints,” International Journal of Mathematical and Computer Science, vol. 6, no. 3, pp. 37-40, 2010.

[12] Y. M. Wang, J. B. Yang, D. L. Xu, and K. S. Chin, “On the centroids of fuzzy numbers,” Fuzzy Sets and Systems, vol. 157, no. 7, pp. 919-926, 2006. https://doi.org/10.1016/j.fss.2005.11.006

[13] A. Karpagam and P. Sumathi, “New approach to solve fuzzy linear programming problems by the ranking function,” Bonfring International Journal of Data Mining, vol. 4, no. 4, pp. 22-25, 2014.

Sudip Bhattacharyya is a Ph.D. scholar under Dr. Pinaki Majumdar. He has done his M.Sc. in Pure Mathematics from the University of Burdwan in 2013. His area of research includes neutrosophic sets, fuzzy operations research, fuzzy multisets etc. He has already published a couple of research papers in international journals.

Pinaki Majumdar is an assistant professor of Mathematics at M.U.C Women’s College, University of Burdwan, India. He has completed his M.Sc. and Ph.D. in Mathematics from Visva-Bharati University, India in 2002 and 2013, respectively. Main area of his research includes fuzzy functional analysis, soft set theory and applications, neutrosophic set theory, etc. He has published more than 40 research papers and contributed a few chapters in research monographs in reputed international journals.

E-mail: pmajumdar2@rediffmail.com