GALEX colours of quasars and intergalactic medium opacity at low redshift

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ABSTRACT

Aims. The distribution of neutral hydrogen in the intergalactic medium (IGM) is currently explored at low redshift by means of UV spectroscopy of quasars. We propose here an alternative approach based on UV colours of quasars as observed from GALEX surveys. We built a NUV-selected sample of 9033 quasars with (FUV–NUV) colours. The imprint of HI absorption in the observed colours is suggested qualitatively by their distribution as a function of quasar redshift.

Methods. Because broad band fluxes lack spectral resolution and are sensitive to a large range of HI column densities a Monte Carlo simulation of IGM opacity is required for quantitative analysis. It was performed with absorbers randomly distributed along redshift and column density distributions. The column density distribution was assumed to be a broken power law with index β₁ (10¹⁵ cm⁻² < N_HI < 10¹⁷ cm⁻²) and β₂ (10¹⁷ cm⁻² < N_HI < 10²¹ cm⁻²). For convenience the redshift distribution is taken proportional to the redshift evolution law of the number density of Lyman limit systems (LLS) per unit redshift as determined by existing spectroscopic surveys. The simulation is run with different assumptions on the spectral index α, of the quasar ionising flux.

Results. The fits between the simulated and observed distribution of colours require an LLS redshift density larger than that derived from spectroscopic counting. This result is robust in spite of difficulties in determining the colour dispersion other than that due to neutral hydrogen absorption. This difference decreases with decreasing α, (softer ionising quasar spectrum) and would vanish only with values of α, which are not supported by existing observations.

Conclusions. We provide arguments to retain α = −2, a value already extreme with respect to those measured with HST/COS. Further fitting of power law index β₁ and β₂ leads to a higher density by a factor of 1.7 (β₁ = −1.7, β₂ = −1.5), possibly 1.5 (β₁ = −1.7, β₂ = −1.7). Beyond the result in terms of density the analysis of UV colours of quasars reveals a tension between the current description of IGM opacity at low z and the published average ionising spectrum of quasars.

Key words. intergalactic medium – ultraviolet: general – quasars: general

1. Introduction

Decades of quasar absorption line studies have provided a wealth of information on the column density and redshift distributions of the neutral hydrogen pockets surviving in the nearly completely ionised intergalactic medium (IGM). These distribution functions have become basic ingredients for the evaluation of the IGM opacity to ionising photons, a crucial link between the emissivity of the sources of ionising photons and the intensity of the ionising ultraviolet background radiation (e.g. Haardt & Madau 1996, 2012). At large redshifts (z ≥ 3), the sources contributing to the hydrogen ionisation at a given point in the IGM are essentially local and the transfer of ionising photons can be reduced to a mean free path term (e.g. Madau et al. 1999; Schirber & Bullock 2003; Faucher-Giguère et al. 2008; Becker & Bolton 2013). The mean free path depends on the properties of systems of optical depth near unity, usually referred as Lyman limit systems (LLSs). In addition, the mean free path to ionising photons can be now directly measured through composite quasar spectra (e.g. Prochaska et al. 2009; O’Meara et al. 2013; Fumagalli et al. 2013; Worseck et al. 2014).

The situation at low redshift (z < 2) deserves special attention for two reasons. For one, the mean free path to ionising radiation becomes very large (e.g. Fumagalli et al. 2013) and the simplification described above is no more valid. Second, the spectroscopic surveys of low-redshift LLSs, based on the identification of the Lyman break at 912 Å require space-based ultraviolet observations which have been scarce. This, in combination with the intrinsically low frequency of LLSs at low redshift, explains the limited size of available samples. Following the pioneering work of Tytler (1982) using IUE, Stengler-Larrea et al. (1995) have homogenised the early observations with those obtained from the first spectrographs of HST, ending with 11 LLSs in the redshift bin (0.36, 1.1). Songaila & Cowie (2010) have added nine LLSs in the redshift bin (0.58, 1.24) from the observations of 50 quasars with the GALEX grism spectrograph. Ribaudo et al. (2011) have performed an extensive analysis of archival HST quasar spectra (including from STIS), resulting in 31 LLSs (τ > 1) in their two lowest redshift bins (0.255, 1.060), (1.060, 1.423). More recently, O’Meara et al. (2013) have analysed the incidence of LLS in 71 quasars observed with the low dispersion modes of HST/ACS and HST/WFC3; they report 19 LLSs (τ > 1) at z < 2 but with an average redshift of about 1.8 and the bulk of statistical power at 2 < z < 2.5.

The Lyman break which can be identified in relatively noisy and low resolution spectra is also expected to leave a trace in the UV colours of quasars, opening the possibility to retrieve information on the distribution of LLSs and more generally HI in the low redshift IGM. Samples of UV colours of quasars, as obtained from GALEX surveys, can be much larger and less biased than
The GALEX instrument provides a (FUV − NUV) colour that might be caused by absorber Lyman break within the GALEX bands we have limited ourselves to $z < 1.9$. A more conservative limit will be adopted later in the analysis for the purpose of reducing selection effects. In order to avoid any risk of limitation in the astrometry or the photometry at the edge of the GALEX field of view, the useful field was limited to a radius of 0.55. More than one UV source may be obtained by cross-matching two first figures are best understood with the details of the spectroscopic samples described above. The paper is organised as follows. In the second section we describe how a sample of quasars with GALEX UV colours is built and how the presence of absorbers is contributing the dispersion observed in the colour distribution. In the third section we review the challenges for extracting quantitative information from the UV colour distribution. In the fourth section we propose a simple model, including a Monte Carlo calculation of the IGM opacity to ionising photons, to predict colour distribution from a limited set of parameters. In the fifth section we run the simulation in different redshift bins, forward modelling the input parameters by comparison with observations.

2. Hints for IGM opacity in UV colours

2.1. A sample of quasars with GALEX ultraviolet colours

The GALEX instrument provides a (FUV − NUV) colour from imaging in two ultraviolet bands, the FUV (1350–1750 Å) and NUV (1750–2750 Å), with 4′′2–5′′3 resolution and 1′25 field of view. The two bands are obtained simultaneously using a dichroic beam splitter. The observations are performed through three types of survey, the All-sky Imaging Survey (AIS) with typical exposure times of 100 s, the Medium Imaging Survey (MIS) with typical exposure times of 1500 s, the Deep Imaging Survey (DIS) with typical exposure times of 30 ks. A full description of the instrument and the mission is given by Martin et al. (2005), Morrissey et al. (2005, 2007).

A large sample of quasars with ultraviolet colours has been obtained by cross-correlating the SDSS Data Release 7 (DR7) quasar catalogue with the GALEX catalogue of UV sources, corresponding essentially to the data release GR4/GR5. The quasar catalogue (Schneider et al. 2010) contains 105 783 spectroscopically confirmed quasars. A maximum match radius of 2′′5 was adopted, slightly above the recommendation of Morrissey et al. (2007) based on the study of GALEX astrometry and similar to the value adopted by Trammell et al. (2007) in a previous study of the UV properties of SDSS-selected quasars. Larger match radii have been tested and discussed in the different context of GALEX FUV selection of high-redshift quasar by Syphers et al. (2009) and Worseck & Prochaska (2011). Our concern here is avoiding non quasar UV source rather than missing one line of sight since a miss, provided it is not related to neutral hydrogen absorption, is not expected to introduce any selection effect. As we are interested by the variations of the (FUV − NUV) colour that might be caused by absorber Lyman break within the GALEX bands we have limited ourselves to $z < 1.9$. A more conservative limit will be adopted later in the analysis for the purpose of reducing selection effects. In order to avoid any risk of limitation in the astrometry or the photometry at the edge of the GALEX field of view, the useful field was limited to a radius of 0.55. More than one UV source may be obtained within the 2′′5 match radius, most often in the case of quasars imaged in multiple GALEX exposures. Because of the poor astrometry at low signal to noise ratio, the closest source is not necessarily the one with the highest effective exposure time in the NUV. In order to overcome this issue and to retain significant NUV flux we have applied a threshold of 900 s to the NUV exposures. This results in a NUV-selected sample of 12 038 quasars with AB magnitudes ranging from 15.7 to 24.8. The (FUV−NUV) colours are calculated for the 9033 quasars also detected in the FUV. No correction for Galactic extinction is applied because, under current assumptions, the colour correction is only one third of the $E(B−V)$ colour excess (e.g. Wyder et al. 2005).

2.2. The effect of absorbers on the UV colour distribution

The (FUV−NUV) colours of the 9033 quasars detected in both GALEX bands are displayed in Fig. 1 as a function of the emission redshift. This plot is similar to one of those obtained by Trammell et al. (2007) in a previous study of the UV properties of SDSS-selected quasars. To deal with the 3005 quasars not detected in the FUV we have observed that the faintest FUV detections reach an (AB) magnitude of 24, rather flat from exposure times of 800 s to 5000 s and slowly increasing to 25 for longer exposures. As the exposure times longer than 5000 s make less than 5% of those with quasar undetected in the FUV we have adopted 24 as a limiting magnitude to display lower limit colours of the 3005 quasars not detected in the FUV in Fig. 2.

These two first figures are best understood with the details of the GALEX bands which are shown Fig. 3. When the emission redshift $z_e$ increases from 0.45 to 0.95 the probability of a Lyman break within the FUV band increases regularly as a function of the difference $z_e − 0.45$. The fraction of red quasars off the main locus of points follows a similar trend in Fig. 1. There is not yet any real FUV dropout in agreement with the relatively small number of lower limit colours in Fig. 2. Beyond $z_e = 0.95$ the
Fig. 3. Effective area (counts cm$^2$ photon$^{-1}$) of the FUV and NUV GALEX bandpasses (Morrissey et al. 2007). The vertical (red) tick marks indicate the position with respect to the bandpasses of the Lyman break at redshifts 0.45, 0.95 and 1.35.

Fig. 4. (FUV−NUV) GALEX colours as a function of emission redshift for the 50 quasars observed with GALEX grism spectrograph by Songaila & Cowie (2010). One lower limit colour (source GALEX J1712+6007) is indicated with a red triangle. All nine quasars circled in green colour (including the lower limit) have spectroscopically identified LLSs. Their LLS redshifts are all at $z < 0.95$ within the FUV band, except $z = 1.11$ for the reddest object GALEX J1418+5223 which does not appear as a FUV dropout.

Fig. 5. (FUV−NUV) GALEX colours (black dots) and lower limit colours (red triangles) as a function of emission redshift for the quasar sample used by Ribaudo et al. (2011) for studying LLS statistics. Quasars circled in green colour (including the lower limits) have spectroscopically identified LLSs. The vast majority of quasars with (FUV−NUV) > 2 have spectroscopically identified LLSs.

Second, we have used the analysis by Ribaudo et al. (2011) of the population of LLSs at low redshift from archival HST spectral observations with the Faint Object Spectrograph (FOS) and the Space Telescope Imaging Spectrograph (STIS). The GALEX UV colours have been searched for all the quasars with redshift $z < 1.85$ in their sample used for LLS statistics (their Table 3). They are displayed in Fig. 5 for 112 quasars along with 49 quasars with only lower limit colour (no detection in the FUV). The quasars with a spectroscopically identified LLSs (from their Table 4) are circled, except for four of them with a Lyman break at too low redshifts to be included in the FUV band. The vast majority of quasars with red colours, that is (FUV−NUV) larger than about two, and among them a significant number of lower limits, have spectroscopically identified LLSs while those bluer have none. Among the 13 quasars circled with (FUV−NUV) < 2 we have either objects classified as PLLSs (partial Lyman Limit System, $\tau < 1$) by Ribaudo et al. (2011) or an absorption redshift $z_{\text{LLS}} < 0.66$; both situations come with less absorption in the GALEX FUV band.

3. Interplay between UV colours and IGM opacity

Although the distributions of GALEX UV colours displayed in the previous sub-sections illustrate beyond doubt the impact of LLSs (and more generally neutral hydrogen absorption) on these colours, there are many difficulties for extracting quantitative information.

First of all, other factors contribute to the dispersion/reddening of UV quasar colours. In addition to photometric uncertainties, there is a natural dispersion of intrinsic quasar colours. Although the spectral energy distribution of quasars display a relatively consistent mean successfully approximated by power laws, a significant dispersion is still present. We need to examine how the spectral energy distributions of quasars can be described in the rest-frame spectral range relevant to the GALEX colours and redshift range of interest here and whether it is possible to disentangle information on the absorbers from the uncertainties in the flux distribution.

A related aspect is the large number of lower limit colours coming with the quasar undetected in the FUV band. In the absence of any absorption the quasars are already red, at a typical (FUV−NUV) colour of about one. With a median NUV trend flattens since an increasing fraction of quasars may have a Lyman break longward of the FUV band and go undetected, as seen in Fig. 2.

2.3. Comparison with samples of spectroscopically identified LLSs

In order to support our view that the red colours of quasars may indicate the presence of neutral hydrogen absorption we have looked at the distribution of GALEX UV colour vs. emission redshift in existing samples with spectroscopically identified LLSs at low redshift.

We have first used the GALEX grism spectrograph observations of 50 quasars with $0.8 < z < 1.3$ by Songaila & Cowie (2010). The UV colours have been found from MAST (Mikulski Archive for Space Telescopes) and are displayed in Fig. 4. Of the nine quasars with a LLS spectroscopically identified by Songaila & Cowie (2010), eight have colours significantly redder than the quasars without LLS, including the one with a lower limit colour which is not a FUV dropout (LLS at $z = 0.82$).

Second, we have used the analysis by Ribaudo et al. (2011) of the population of LLSs at low redshift from archival HST spectral observations with the Faint Object Spectrograph (FOS) and the Space Telescope Imaging Spectrograph (STIS). The GALEX UV colours have been searched for all the quasars with redshift $z < 1.85$ in their sample used for LLS statistics (their Table 3). They are displayed in Fig. 5 for 112 quasars along with 49 quasars with only lower limit colour (no detection in the FUV). The quasars with a spectroscopically identified LLSs (from their Table 4) are circled, except for four of them with a Lyman break at too low redshifts to be included in the FUV band. The vast majority of quasars with red colours, that is (FUV−NUV) larger than about two, and among them a significant number of lower limits, have spectroscopically identified LLSs while those bluer have none. Among the 13 quasars circled with (FUV−NUV) < 2 we have either objects classified as PLLSs (partial Lyman Limit System, $\tau < 1$) by Ribaudo et al. (2011) or an absorption redshift $z_{\text{LLS}} < 0.66$; both situations come with less absorption in the GALEX FUV band.
magnitude of 22.4 over the full sample, a number of quasars go undetected in the FUV with only a modest reddening (typically 1.6 mag associated to a FUV limiting magnitude of 25). In these conditions many lower limit colours are not indicative of true FUV dropouts.

Another obvious difficulty in the interpretation of photometric data is the lack of spectral resolution which prevents determination of any absorption redshift and results in a degeneracy between absorption redshift and column density. Any colour significantly redder than the average trend in Fig. 1 and potentially revealing neutral hydrogen absorption may be caused by different combinations of absorption redshift and absorption strength. This is a basic difference with a spectroscopic approach which provides a list of well defined absorbers at specific redshifts and with a uniform optical depth limit (e.g. larger than 1 or 2) that can be translated into a distribution law of LLSs (i.e. number of LLS per unit redshift as a function of z). Here, the UV colour is influenced not only by the absorbers that are usually identified as LLSs (optical depth larger than 1 or HI column density $N_{\text{HI}} \geq 10^{17.2} \text{cm}^{-2}$) but also by an increasing number of absorbers with $N_{\text{HI}} < 10^{17.2} \text{cm}^{-2}$. In contrast to counting a few well identified optically thick clouds, we are challenged here by an opacity problem caused by a large population of absorbers. This bears resemblance to the direct evaluation of mean free path to ionisation radiation through the analysis of stacked spectra by O’Meara et al. (2013) and Worseck et al. (2014).

In the same vein as the redshift vs. absorption strength degeneracy due to the lack of spectral resolution, the photometric approach is unable to distinguish absorbers lying close to the quasars which are usually excluded in spectroscopic surveys (e.g. Proximate LLSs in Prochaska et al. 2010).

Beyond $z_e = 0.95$, LLSs may appear in the NUV band and be responsible for a decrease of the quasars NUV flux depending on the HI column density of the LLS and its position in the band. The resulting sample bias increases rapidly with redshift and requires a cut in the redshift $z_e$ for any quantitative analysis. Some average numbers may be derived from the average redshift density of 0.82 LLS reported in the range (1.060, 1.423) by Ribaudo et al. (2011). For a sample of about 600 quasars as in our observations, we get about 144 LLSs in the NUV band up to $z_e < 1.3$, with an absorption of as much as 0.27 of the NUV flux of the quasars. Up to $z_e < 1.4$ we get about 192 LLSs with an absorption of as much as 0.4 of the NUV flux. A redshift cut at $z_e < 1.35$ would therefore keep sample bias within acceptable limits for quantitative analysis.

4. Modelling the distribution of quasar UV colours

To recover quantitative information from the observed dispersion of the UV colour distribution, we have generated Monte Carlo quasar spectra randomly imprinted with IGM absorption from the observed statistical properties of redshift and column density distributions of neutral hydrogen. Folded through the GALEX bandpasses, these spectra provide a large set of colours to be compared with the observed UV colour distribution. We review in the following sub-sections the physical quantities entering the calculations and expected to be constrained in this comparison.

4.1. Quasar spectral energy distribution

The first step of the simulation is to adopt a representative quasar spectral energy distribution over the rest frame wavelength range 550 Å–2800 Å that is shifted over the GALEX bandpasses for quasars with $z_e < 1.35$. The rest-frame continuum of quasars is usually described by power laws $F_\nu \propto \nu^{\alpha}$ or $F_\nu \propto \lambda^{\alpha_2}$ with $\alpha_2 = -(\alpha_1 + 2)$ (e.g. Shull et al. 2012).

At wavelengths longer than about 1100 Å, there is a consensus on the spectral index which consequently will not be retained as a parameter to be optimised through the simulation. In addition as emission lines may play a role in the quasar colours, we have not chosen an average index but preferred to adopt the composite spectrum of Vanden Berk et al. (2001). Incidentally, this composite spectrum can be approximated by a power law index of $-0.44$ above 1200 Å (Vanden Berk et al. 2001). In contrast, the $\alpha_r$ index in the EUV domain (<912 Å) should be an essential parameter of the simulation since it is in this wavelength range that the interplay between the quasar ionising flux continuum and the continuum absorption by neutral hydrogen clouds is expected to change the most the GALEX broadband fluxes. A number of $\alpha_r$ index values have already been reported from UV spectroscopic observations of bright, low-z targets. Zheng et al. (1997) obtain $\alpha_r = -1.8$ (radio-quiet sample only) from HST/FOS and Telfer et al. (2002) $\alpha_r = -1.57\pm0.17$ (radio-quiet), $-1.96\pm0.12$ (radio-loud) from HST/FOS/GHRS/STIS. These values are challenged by $\alpha_r = -0.56$ from FUSE observations (Scott et al. 2004) but from GALEX spectroscopy Barger & Cowie (2010) find values of $-1.76$ and $-2.01$ in good agreement with the earlier HST determinations of Zheng et al. (1997) and Telfer et al. (2002). More recent results have not clarified the situation. Shull et al. (2012) and Stevans et al. (2014) report $\alpha_r = -1.41\pm0.15$ from HST/COS observations. The first quasar stacked spectrum at $z \sim 2.4$ from HST/WFC3 (Lusso et al. 2015) has confirmed the most negative values but a value $\alpha_r = -0.72\pm0.26$, in line with that from FUSE, has been recently given from new HST/COS observations and analysis (Tilton et al. 2016). The $\alpha_r$ index (<912 Å) is clearly a parameter to be optimised in our simulation.

One area of difficulty, especially for our purpose of integration into the GALEX bandpasses, is the transition zone between the composite spectrum of Vanden Berk et al. (2001) and the softening expected in the EUV domain according to most of the
values in the references above. A comparison with the compositespectrum of Shull et al. (2012) suggests to stop the composite spectrum of Vanden Berk et al. (2001) below 1190 Å once theLyα line has been fully covered and to start the powerlaw continuum only below about 1000 Å. Between, we have used anintermediate power law continuum (Fig. 6). By folding theresulting complete spectral energy distribution into the GALEXbandpasses, we have determined an index $\sim -1.4$ as best matchingthe observed colour distribution of Fig. 1 in the domain of $z_c < 0.6$ where the dispersion of colours is not yet affected byIGM opacity effects. This is shown in Fig. 7. This figure illustrates how the powerlaw index of the ionising spectrum starts to affect the quasar colours above a redshift of 0.7 and is the most sensitive in the range 0.9–1.3.

4.2. IGM absorption

The second step of the simulation follows the standard practice of Monte Carlo evaluation of the intergalactic hydrogen attenuation due to photoelectric absorption and resonant scattering by Lyman transitions (e.g. Möller & Jakobsen 1990; Madau 1995; Bershady et al. 1999; Meiksin 2006; Inoue & Iwata 2008; Haardt & Madau 2012; Inoue et al. 2014). At low redshift we can concentrate on the photoelectric absorption mechanism and we have not extended the simulation to the resonant scattering by Lyman transitions. To account for this latter mechanism we have used instead the observed average transmission $1 - 0.013(1 + z_c)^{1.54}$ (observed wavelength frame) reported at low redshift by Kirkman et al. (2007). We have calculated that this factor has an impact of less than 0.05 mag on the colour in nominal conditions.

We now turn to the parameters used in the Monte Carlo evaluation of the Lyman continuum absorption and, among them, the necessary limited number of those we plan to vary and constrain by fitting the output of the simulation with the observed quasar colour distribution. We adopt the current notation (e.g. O’Meara et al. 2007; Prochaska et al. 2010) for the column density distribution function $f(N_{\text{HI}}, X)$ giving the number of absorbers with column density $N_{\text{HI}}$ per $dN_{\text{HI}}$ interval and per absorption pathlength $dX$ (for the moment we ignore X and the relation with the redshift). The $N_{\text{HI}}$ dependency of this function is usually approximated by broken power laws (e.g. Prochaska et al. 2010; Ribando et al. 2011; O’Meara et al. 2013) of the form $\Lambda_i N_{\text{HI}}^{\beta_i}$ with the $\Lambda_i$ and $\beta_i$ independent of redshift and linked by continuity equations at the breaking points between the different classes of absorbers.

The sub-DLAs ($10^{17.2} \text{cm}^{-2} < N_{\text{HI}} < 10^{20.3} \text{cm}^{-2}$) and DLAs ($N_{\text{HI}} \geq 10^{20.3} \text{cm}^{-2}$) do not contribute much to the opacity because of their small numbers. As the column density distribution is also measured in these categories of absorbers from the damping profiles, we have therefore adopted the values (respectively $\beta_1 = -0.8$ and $\beta_2 = -1.4$) reported by Ribando et al. (2011) for the most comparable redshift range. This leaves $\beta_2$ for the LLSs ($10^{17.2} \text{cm}^{-2} < N_{\text{HI}} < 10^{19} \text{cm}^{-2}$), $\beta_1$ for the PLLSs (partial LLS, $N_{\text{HI}} < 10^{17.2} \text{cm}^{-2}$). The column density lower limit will be determined later) and the values $A_1$ (or $A_2$) as parameters to optimise in our simulation.

For the purpose of comparison with previous observations and in order to explore realistic values for matching the observed quasar colour distribution, it is highly desirable to establish the relation between our set of parameters and the density of LLSs observed from previous spectroscopic surveys. In these surveys the observable quantity is the redshift density of LLSs $l(z)$, obtained as the ratio of the number of LLSs ($\tau > 1$) detected in a redshift interval to the total survey path contained in that redshift interval. The redshift evolution law is often parameterised as $l(z) = l_0(1 + z)^\gamma$. We will refer to those of Ribando et al. (2011), $l(z) = 0.286(1 + z)^{1.19}$ ($\tau > 1$) and Songail & Cowie (2010), $l(z) = 0.151(1 + z)^{1.94}$ displayed in Fig. 8 along with the density measurements from which they have been obtained.

The quantity $l(z)$ is related to $l(X)$, the density of LLSs per unit pathlength $X$, by (e.g. Ribando et al. 2011; O’Meara et al. 2013)

$$l(X) dX = l(z) dz$$

where

$$dX = \frac{H_0}{H(z)} (1 + z)^2 dz$$

\[ F(NUV) - GALEX \]
and
\[ H(z) = H_0 (\Omega_M + \Omega_{\Lambda}) (1 + z)^{\gamma} \]

is the zeroth moment of the column density function
\[ f(N_{\text{HI}}, X) \] and with the broken power laws approximating this function, we have
\[ l(X)_{\text{min}} \times 10^{17.2} \text{ cm}^{-2} = A_2 \int_{10^{17.2}}^{\infty} N_{\text{HI}}^{0.8} dN_{\text{HI}} + A_1 \int_{10^{17.2}}^{10^{19}} N_{\text{HI}}^{-1.4} dN_{\text{HI}}. \]

With the relations above and \( l(X) \) almost constant at low redshift, we may calculate the average number of LLS absorbers \( N_{\text{HI}} > 10^{17.2} \text{ cm}^{-2} \) along a line of sight up to a redshift \( z_e \), as
\[ N_{\text{HI}} > 10^{17.2} \text{ cm}^{-2} = \int_{0}^{z_e} A_2 \int_{10^{17.2}}^{\infty} N_{\text{HI}}^{0.8} \left( \frac{1 + z}{0.7 + 0.3(1 + z)} \right)^{1/2} \text{d}z. \]

Substituting the value of \( l(X)_{\text{min}} > 10^{17.2} \text{ cm}^{-2} \) from the integration on the power laws into the last equation and comparing with the other calculation of the number of LLSs by
\[ N_{\text{min}} > 10^{17.2} \text{ cm}^{-2} = \int_{0}^{z_e} A_0 (1 + z)^{\gamma} \text{d}z \]
provides a link between the set of parameters to optimise and the LLS density measured by Songaila & Cowie (2010) and Ribaudo et al. (2011). This allows us to compare the constraints from our photometric approach with the data from previous spectroscopic surveys.

If we assume that the shape of the redshift evolution as a function of \( z \) used for LLSs may be extended in the domain of PLLSSs, the above equations may be extended down to lower column density with the parameters \( A_1 \) and \( \beta_1 \). They may be used to determine the lowest column density \( N_{\text{HI,lim}} \) with a significant role in the IGM Lyman continuum absorption.

\[ l(X)_{\text{min}} > N_{\text{min}} = l(X)_{\text{HI}} > 10^{17.2} \text{ cm}^{-2} + A_1 \int_{N_{\text{min}}}^{10^{17.2}} N_{\text{HI}}^{\beta_1} dN_{\text{HI}} \]

and
\[ N_{\text{HI}} > N_{\text{min}} = l(X)_{\text{HI}} > N_{\text{min}} \int_{0}^{z_e} \left( \frac{1 + z}{0.7 + 0.3(1 + z)} \right)^{1/2} \text{d}z. \]

We have used column density limits of \( 10^{14} \text{ cm}^{-2} \) to \( 10^{15} \text{ cm}^{-2} \) (domain of transition between the Ly-\( \alpha \) forest and the PLLSSs) and current values of \( \beta_1 \) and \( \beta_2 \) in the two equations above to run the opacity calculation described in the following subsection. Moving the limit from \( 10^{15} \text{ cm}^{-2} \) to \( 10^{14} \text{ cm}^{-2} \) would increase the total number of absorbers by a factor of about 4.9 but only decrease the average transmitted FUV to NUV flux ratio by less than 0.002. For all practical purposes the range of column densities above the limit of \( 10^{15} \text{ cm}^{-2} \) is responsible for the totality of neutral hydrogen absorption and will be used in the following Monte Carlo opacity evaluation.

### 4.3. Monte Carlo opacity calculation

For each quasar line of sight used in our Monte Carlo opacity calculation, a number of absorbers has been pseudo-randomly generated from a Poisson distribution with, for mean parameter, the number \( N_{\text{min}} > 10^{17.2} \text{ cm}^{-2} \) obtained above for the emission redshift \( z_e \).

The selected number was in turn distributed pseudo-randomly on redshift and column density according to the distribution laws
\[ l(z) = l_0 (1 + z)^{\gamma} \] and \( A_0 N_{\text{HI}}^{\beta_1} \) in their respective \( N_{\text{HI}} \) domains.

An absorber of column density \( N_{\text{HI}} \) at an absorption redshift \( z_a \) has an optical depth at rest wavelength \( \tau = l_0 / (1 + z_a) \) given by
\[ \tau = 6.3 \times 10^{-18} l_0 / (1 + z_a) / 912^3 N_{\text{HI}} \] or
\[ \tau = 0 \text{ if } l_0 / (1 + z_a) > 912 \text{ Å}. \]

The total optical depth at \( l_0 \) is obtained by adding all individual absorber optical depths. The resulting transmission as a function of wavelength is then multiplied with the quasar spectral energy distribution (defined above with the spectral index \( \alpha_v \)) and provides a quasar spectrum with randomly imprinted IGM absorption. Finally an integration in the GALEX bandpasses gives the distribution of quasar UV colours resulting from our Monte Carlo opacity evaluation.

### 5. The optimisation process

The previous section has identified the four input parameters of our Monte Carlo simulation of the distribution of GALEX UV colours of quasars at low redshift. They are the quasar continuum spectral index \( \alpha_v \) in the UV spectral range, the power law index of the HI column density distribution \( \beta_2 \) in the range \( 10^{15} \text{ cm}^{-2} < N_{\text{HI}} < 10^{17.2} \text{ cm}^{-2} \) and \( \beta_1 \) in the range \( 10^{17.2} \text{ cm}^{-2} < N_{\text{HI}} < 10^{19} \text{ cm}^{-2} \) and the density factor \( A_1 \).

Given the factor larger than two between the LLS redshift densities determined so far by spectroscopy in the FUV range (see Fig. 8) we started the optimisation with the density factor \( A_1 \) and \( \alpha_v \) expected to affect most the simulated colour histograms. The density factor \( A_1 \) is calculated with the equations in Sect. 4.2 and the redshift evolution law used for the density of LLSs. After a normalisation by the density factor obtained with the evolution law adopted, it is possible to work in terms of a relative number density \( 1 + k \) in each redshift bin. Adopting the evolution law of Ribaudo et al. (2011) this means that when \( k = 0.5 \) we have 1.5 times more LLSs than implied by their distribution law.

The parameters \( \beta_1 \) and \( \beta_2 \) are first set to a central value \( -1.5 \) and are expected to provide a possible fine tuning on the density factor \( A_1 \) once determined. They correspond to a range of \( N_{\text{HI}} \) where most of the opacity to hydrogen-ionising photons takes place and where the column density distribution function may be difficult to establish. In the range \( 10^{15} \text{ cm}^{-2} < N_{\text{HI}} < 10^{17.2} \text{ cm}^{-2} \) (index \( \beta_1 \)) the absorbers are saturated in Ly-\( \alpha \) and, unless the Lyman break is measurable, the determination of \( N_{\text{HI}} \) requires the use of high-order Lyman series transitions (e.g. Kim et al. 2002, 2013). Although of relatively low opacity individually, the absorbers contribute to the overall opacity through their number (e.g. Rudie et al. 2013). In the range \( 10^{17.2} \text{ cm}^{-2} < N_{\text{HI}} < 10^{19} \text{ cm}^{-2} \) (index \( \beta_2 \)) the HI column densities can be distinguished on the basis of the Lyman breaks only at the low range extremity and the LLS density resulting from spectroscopic survey is in fact an integral on a column density function.

The emission redshift \( z_e \) is a crucial quantity since the quasar intrinsic colour depends on the redshift and the number of absorbers is related to the redshift pathlength within the GALEX bandpasses whatever the random distribution of absorbers adopted. The comparison will therefore be divided into redshift intervals. Ten emission redshift bins from \( z_e = 0.4 \) to 1.3, with size \( z_e \pm 0.05 \) and containing from 500 to 800 observed quasars are used. In each of these bins, \( 10^4 \) model lines of sight are usually run for each set of parameters. The distribution obtained from the simulation is scaled to the number of quasars observed within the same redshift bin (including those with only lower limit
We have a number of reasons for extending up to $z_e = 1.35$ our calibration $\sigma = 0.05$ at low redshift. First, the NUV magnitude distribution is not changing very much among the 10 redshift bins (average magnitude per bin between 19.76 and 20.19) and consequently an increase of photometric uncertainty with redshift due to UV flux getting fainter is unlikely. Second, we have plotted the observed GALEX (FUV–NUV) colours as a function of their NUV magnitude in Fig. 10. Even in the case of the redshift bins 1.0–1.3 which exhibit the largest skewness as seen Fig. 1 there is no relation between the reddest and the faintest quasars. Last, the possibility that the reddest colours may be associated to objects in high galactic extinction regions has been examined. Of the 2537 quasars in Fig. 10 only 56 objects have $u$ band Galactic extinction $A_u > 0.5$ (Schlegel et al. 1998) with a maximum $A_u = 1.04$. Among these latter 56 objects only seven have (FUV–NUV) $> 2$ while the seven with the largest $A_u$ have (FUV–NUV) $< 2$. There is no relation between the reddest colour and high galactic extinction regions. Incidentally, the extinction $A_u = 0.5$ would correspond to a shift of $-0.05$ and 0.842 in the (FUV–NUV) and NUV magnitude respectively with the corrections of Wyder et al. (2005), $A_{\text{FUV}} = 1.584 \times A_u$ and $A_{\text{NUV}} = 1.684 \times A_u$.

Although these series of arguments support our calibration of a dispersion factor at low redshift we acknowledge that we are missing an evaluation of photometric uncertainties. This is a consequence of using colours instead of fluxes in our simulation, in order to stay away from uncertainties associated to UV luminosity functions of quasars. In the following we will therefore control on purely empirical basis how each optimization may be dependent on variations around the nominal dispersion factor of $\sigma = 0.05$.

5.2. The bin by bin optimisation

We have explored the fit between predicted and observed cumulative histograms up to the bin $z_e = 1.3$ with steps of 0.1 in $\alpha_k$ and $k$, in the ranges $-2.6 < \alpha_k < -1.2$ and 0 $< k < 2$. The steps correspond to a reasonable change that can be detected in the histogram comparison. We have proceeded quantitatively searching the minimum of the absolute sum of the differences in each colour histogram bin up to a colour of 3. Fits are not considered satisfactory if this minimum is larger than about 350.

No satisfactory fit between predicted and observed cumulative histograms is found over the redshift bins 0.6–0.9 as if the number of absorbers was not yet large enough nor the EUV spectral range sufficiently well shifted in the GALEX bandpasses for the optimal sensitivity of the method to be reached. It is also possible that the spectral index adopted to represent the typical quasar spectrum has significant dispersion in the transition zone between 1190 Å and 1000 Å. In addition we have checked that this situation is not due to slight variations of the dispersion factor $\sigma$.

Beyond redshift 0.9 where the neutral hydrogen absorption becomes prevalent satisfactory fits may be obtained when the number density increases (example in Fig. 9). This happens over a significant range of $\alpha_k$ values. The combinations of index $\alpha_k$ and number density $(1+k)$ leading to these fits are collected and displayed in Fig. 11. Error bars corresponding to the precision on the determination of the fits are of the order of 0.05 and are shown (they were obtained by running 50,000 model lines of sight and using a step of 0.05 in $k$). These fits are obtained with the nominal value $\sigma = 0.05$. In some instances a better fit may be found with different values of $\sigma$. If the value of $k$ is different we have extended accordingly the error bar on $k$ as a sign of added uncertainty due to photometric dispersion. Beyond the range of...
β in all cases. the sample size of 30 bins translates into a 95% significance level
between the cumulative distributions is found to vary from
the redshift range of interest would lead to larger overdensi-
shows densities lower than those of Ribaudo et al. (2011) in
Adopting the evolution law of Songaila & Cowie (2010) which
of Ribaudo et al. (2011) integrated to the appropriate redshift.
values (see Sect. 4.1). This range of values excludes the lowest
scattered points are along the short-dashed line. Using an arbitrary evolution law is beyond the scope of our
the number density in ordinate
density of LLSs than found from previous spectroscopic deter-
in a 95% significance level in all cases.
For each set of index αν and number density values in
Fig. 11, we have applied the Kolmogorov–Smirnov test to the
two distribution functions involved in each fit and attached to
observations and simulation respectively. The maximum difference
between the cumulative distributions is found to vary from
0.035 to 0.105, which according to the statistical test tables and
the sample size of 30 bins translates into a 95% significance level
in all cases.
We have finally examined how variations of the parameters
β1 and β2 affect the main trend in Fig. 11. Densities can be
obtained below the main trend and are plotted as open symbols
with indications of the relevant β1 and β2 values. The nominal
value of dispersion σ = 0.05 has been used and error bars similar
to those in the main trend are not displayed for clarity.

5.3. Results
A major result in Fig. 11 is that the simulation requires larger
density of LLSs than found from previous spectroscopic deter-
minations. We emphasise that the number density in ordinate
is the fraction of absorbers in the range 10^{17.2} cm^{-2} < N_{HI} <
10^{19} cm^{-2} normalised by the density of LLSs over the same
range of HI column density obtained from the evolution law
of Ribaudo et al. (2011) integrated to the appropriate redshift.
Adopting the evolution law of Songaila & Cowie (2010) which
shows densities lower than those of Ribaudo et al. (2011) in
the redshift range of interest would lead to larger overdensi-
ities. Using an arbitrary evolution law is beyond the scope of our
method.
The required overdensity is dependent on the spectral index
αν of the quasar ionising spectrum and decreases when the index
decreases and gets softer than the range of usually reported val-
ues (see Sect. 4.1). This effect is stronger than the uncertainties
on the dispersion σ. The dependence on the spectral index does
not come as a surprise since the evaluation of colours has to use
an intrinsic quasar spectrum for reference; less ionising flux from
quasar should require less neutral hydrogen absorption to pro-
duce the same colour dispersion. This is illustrated by the two
options of αν plotted in Fig. 7. At αν > −2 we are faced to an
unwanted situation with k values changing significantly with the
redshift bin. This will be discussed in light of all the constraints
on αν and the number density.
Figure 11 shows also the lower overdensities values reached
after optimisation of the β1 and β2 parameters, about 1.7 (αν =
−2) or 1.4 (αν = −2.4) with β1 decreased to about −1.7. This value of β1 is in agreement with the value −1.65 reported by
Kim et al. (2002, 2013), and Rudie et al. (2013). Lower overdensi-
ities at about 1.5 (αν = −2) or 1.2 (αν = −2.4) may be obtained
with β2 decreased also to about −1.7. However, the latter value
is not consistent with a flattening of the column density distribu-
tion at N_{HI} > 10^{17.2} cm^{-2} reported by most of the observations
(e.g. Prochaska et al. 2010) and simulations (Altay et al. 2011).

6. Discussion
The optimisation of the power law indices β1 and β2 of the HI
column density distribution has eased but not solved the ten-
sion between the results of our approach and existing density
evaluations based on spectroscopy. In order to determine which
combination of values to adopt from our approach we need to
examine the existing constraints on the ionising quasar spectrum
(αν, index) and the density of LLSs.

6.1. Ionising quasar spectrum (αν index)
There is a large spread in the average power law spectral index
reported for the ionising spectrum of quasars from about −2 to
−0.56 (see Sect. 4.1). This range of values excludes the lowest
overdensities obtained for αν < −2. Constraining the overdensi-
tries within reasonable values and avoiding the unwanted disper-
sion with redshift observed at large αν in Fig. 11 would require
to stay close to this limit αν > −2. This is in contrast with the
distribution in spectral index obtained from 159 HST/COS AGN
by Stevans et al. (2014) with few objects with αν < −2.
A possible explanation has perhaps to do with the duality of the average spectral index $\alpha_\nu$. On one hand, especially in the case of simulation, the index is for the total ionising flux. On the other hand the index refers only to the UV continuum in which case the spectral resolution is crucial for continuum placement in presence of EUV absorption and emission lines (e.g. Stevans et al. 2014). In these conditions an $\alpha_\nu$ index of about $-2$, close to determinations earlier than those taking advantage of the high spectral resolution of HST/COS, might be appropriate.

6.2. LLSs density

While the spectroscopic determination of the density of LLSs does not include those too close to the quasar (usually within 3000 km s$^{-1}$), our approach coupled with opacity model does not distinguish between the ambient IGM and the proximity from quasars. This may cause an overdensity in our approach. Prochaska et al. (2010) have discussed the incidence of these so-called Proximate LLSs at high redshift but we will refer to the samples of Songaila & Cowie (2010) and Ribaudo et al. (2011) for a comparable redshift range. Of the nine LLSs (seven only samples of Songaila & Cowie (2010) and Ribaudo et al. (2011) have discussed the incidence of these so-called Proximate LLSs at high redshift but we will refer to the samples of Songaila & Cowie (2010) and Ribaudo et al. (2011) for a comparable redshift range. Of the nine LLSs (seven only samples of Songaila & Cowie (2010) and Ribaudo et al. (2011) have discussed the incidence of these so-called Proximate LLSs at high redshift but we will refer to the samples of Songaila & Cowie (2010) and Ribaudo et al. (2011) for a comparable redshift, of which 652 quasars with a redshift interval of about 0.7 each in the redshift bin $z_{\text{e}} = 1.2$. The volume is large but the simulation includes all types of absorbers without any specific redshift. The spectroscopic counting results also in a well defined accuracy in contrast to our approach with a precision based on the fitting process of histograms and an average uncertainty on the overdensity curves estimated to about 0.07. Last, the sample of quasar colours is probably more homogeneous than the archival sample of Ribaudo et al. (2011). It is not clear that this may provide an explanation for the overdensities since an opposite effect is seen in Fig. 12 by the measurements of Songaila & Cowie (2010) with their GALEX spectroscopic sample.

7. Conclusion

We have built a sample of 9033 quasars with GALEX (FUV–NUV) colours to put constraints on the IGM neutral hydrogen absorption at low redshift (0.5 < $z$ < 1.3) from the observed dispersion of their colours as a function of redshift. The degeneracy between the redshift and the strength of absorption inherent to broad band fluxes requires a Monte Carlo simulation of the IGM opacity. Parameters based on existing determinations of redshift and neutral hydrogen column density distribution have been used and a limited set of crucial parameters have been kept for the purpose of forward modelling with the observed quasar colours. They are the density of LLSs ($10^{17.2} \text{ cm}^{-2} < N_{\text{HI}} < 10^{19} \text{ cm}^{-2}$), the power law index $\beta_\nu$ of the distribution of N(HI) column density in the same range as well as the similar index $\beta_1$ in the range $10^{15} \text{ cm}^{-2} < N_{\text{HI}} < 10^{17.2} \text{ cm}^{-2}$. It was convenient to normalise the LLS density in the simulation with the redshift density obtained by Ribaudo et al. (2011) from spectroscopic counting of LLSs and to adopt their redshift evolution law for running the simulation in different redshift bins. A standard quasar spectral energy distribution is also required for the evaluation of quasar colour in the simulation. We have used existing determinations but kept the power law index of the ionising spectrum $\alpha_\nu$ (<1000 Å) as a parameter for the optimisation.

The fraction of the colour dispersion not caused by neutral hydrogen absorption is calibrated at low redshift. In spite of uncertainties due to the extrapolation of this calibration at higher redshifts and the limited accuracy of the fitting process, the simulation shows a link between the derived relative LLS number density and the power law index assumed for the ionising spectrum $\alpha_\nu$. Such a link is expected in the sense the more ionising photons, the more neutral hydrogen required for a given set of quasar colours. However, the numerical values show a tension with the existing determinations based on spectroscopic methods. A number density as those obtained from these methods...
would come with $\alpha_\nu \sim -2.4$, out of the range of existing determinations of the ionising spectrum slope. At the opposite end a slope $\alpha_\nu \sim -1.4$, as in the last determinations from HST/COS by Shull et al. (2012), Stevans et al. (2014) but see Tilton et al. (2016), would come with an overdensity larger than 2 and too large a dispersion between redshift bins.

We argue that a combination $\alpha_\nu = -2$ at the edge of the range of existing values of the ionising spectrum slope and an overdensity of 1.7 over the evolution law of redshift density of LLSs of Ribaudo et al. (2011) could make sense. This latter value would reduce to about 1.5 with the power law index $\beta_2$ of the distribution of HI column density set to $-1.7$ instead of $-1.5$ and finally to 1.35 with the correction for proximate LLSs included. Beyond the specific and modest overdensity values obtained here, this paper illustrates the potential of large and deep sample of quasar UV colours for exploring the link between the distribution of neutral hydrogen in the IGM and the existence of a consistent mean ionising spectrum for quasars.

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