Excitation and emission spectra of rubidium in rare-gas thin-films
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To understand the optical properties of atoms in solid state matrices, the absorption, excitation and emission spectra of rubidium doped thin-films of argon, krypton and xenon were investigated in detail. A two-dimensional spectral analysis extends earlier reports on the excitation and emission properties of rubidium in rare-gas hosts. We found that the doped crystals of krypton and xenon exhibit a simple absorption-emission relation, whereas rubidium in argon showed more complicated spectral structures. Our sample preparation employed in the present work yielded different results for the Ar crystal, but our peak positions were consistent with the prediction based on the linear extrapolation of Xe and Kr data. We also observed a bleaching behavior in rubidium excitation spectra, which suggests a population transfer from one to another spectral feature due to hole-burning. The observed optical response implies that rubidium in rare-gas thin-films is detectable with extremely high sensitivity, possibly down to a single atom level, in low concentration samples.

I. INTRODUCTION

The strong \( S \rightarrow P \) transitions of alkali atoms have attracted a large interest in spectroscopy for a long time\(^1\). Gas phase experiments of these alkaline systems have led to outstanding findings in quantum optics and physics. Whereas gas phase spectra can be fully theoretically described, spectra of alkali atoms in solid states depend on environmental influences, which have not been understood well. Metal atoms embedded in rare-gas hosts were studied sparsely in the past decades\(^2-8\). These studies are useful for characterization of the guest atom, its local environments, and its transition properties. It further gives insight into the trapping sites. The Jahn-Teller effect can be characterized, since the electronic transition is modified by the highly sterical distorted lattice.

For quantum optics applications, a highly sensitive fluorescence detection of low-doping samples is desired. So far only a few studies characterize the emission properties of various metal species in different host systems. If the optical properties of alkali atoms are well understood, it might also give a better understanding of the optical desorption of atoms from surfaces\(^9\).

Atomic rubidium (Rb) in its vapor form is widely used in experimental quantum and atom optics. It is convenient because of its laser wavelengths and the spectral separation of the two \( D\)-line transitions. Comparatively little is known about optical properties of Rb embedded in solid state matrices. Early experiments on the absorption spectra of Rb in argon were performed in the 1960s by KUPFERMANN and coworkers\(^10\). But these comprehensive studies were limited to spectra in argon crystals. Only a short qualitative report exists on the luminescent properties of the sample\(^11\). Experimental studies of Rb in solid helium (He) observed weak emission properties\(^12,13\). In liquid He, Rb was reported to show strong laser induced fluorescence\(^14,15\). Further investigations of Rb doped He nanodroplets\(^16\) showed that laser induced fluorescence can be observed in this system, too. A sample produced by \( \beta^- \) decay of krypton, resulting in Rb dopant atoms was researched by MICKLITZ and LUCHER\(^17\). The spectral emission was found to depend strongly on their sample preparation method. In all the above studies, the reported optical characterizations focus on the \( D\)-line transitions in the near-infrared part of the optical spectrum. These transitions are often blue shifted from the corresponding gas phase transitions and are spectrally broader by several orders of magnitude.

In this paper we report on the absorption and emission properties of Rb in various rare-gas thin-films. We prepared ‘spray-on’ crystals of argon (Ar), krypton (Kr), and xenon (Xe) doped with rubidium from a thermal dispenser. The thermal dispenser has been commonly used in quantum optical experiments with atoms; we are not aware of any other paper which describes a similar sample-preparation method for doped thin-film measurements. Laser ablation or electronic discharge has been often used for sample preparation in matrix isolation studies of atoms. In this study, excitation-emission two-dimensional spectra were recorded in order to allow more insight on the properties of Rb in a solid state environment. We failed to acquire spectra with Rb in neon (Ne), although the cryogenic conditions allow for the growth of doped Ne crystals. Likewise, experiments with nitrogen (N\(_2\)) yielded a null result and were not pursued further.

II. EXPERIMENTAL DETAILS

The rare-gas thin films were grown on a 1 mm thick sapphire window thermally connected to the cold finger of a closed cycle GM refrigerator (Sumitomo, RDK-408). The base temperature of the cryostat was 4.1 K and its cooling power was 1 W. Rare gases were dosed from a nozzle (inner diameter=1.7 mm) mounted 33 mm in front of the window. A Rb-dispenser (Alvatec, AS-3-Rb-25-S) held on a thermal protective plastic holder (ULTEM)
was attached at the tip of the nozzle, and Rb vapo- 
ures generated by the dispenser were co-deposited on the sap-
pire window during the thin film growth. Earlier ex-
periments with a chromate based Rb dispenser (SAES 
Getters, 5G0120) showed broad spectral features due to 
impurities.

The rare-gases were supplied through a flow-controller 
(Horiba STEC 7320) with a flow rate of 50 ccm (cubic 
centimetre per minutes). The gas was expanded from am-
bitious conditions and both the nozzle and the dispenser 
holder were kept at ambient temperatures. After the 
deposition, the nozzle/ dispenser arrangement was re-
tracted ≈ 300 mm away from the crystal window, and 
obsured by an opaque matte block to prevent the resid-
ral fluorescence of the high-temperature plastic holder from reaching our detector. Prior to each experiment, 
the residual fluorescence of the cleaned sapphire window 
was verified to be at the noise-level for acquisition times 
of 60 secs.

For optical absorption measurements, a retractable 
mirror was installed next to the crystal window to steer the optical beam through the sample. Optical absorp-
tion spectra were acquired with a tungsten lamp and a 
double-grating monochromator (Spex). The instrumen-
tal linewidth was measured to be below 1.3 nm. The 
light dispersed by the monochromer was detected by a 
photon counting photomultiplier (Hamamatsu) through an optical multimode fiber.

A continuous wave (cw) titanium-sapphire (TiSa) ring 
aser was used (Coherent, 899-21, SW optics) for excita-
tion and emission measurements of Rb / rare-gas sam-
les. The optical etalon unit of the ring laser was re-
moved to achieve a wide continuous tuning range be-
tween 690 and 790 nm. The laser line width was nar-
rrower than 0.3 nm without the etalon. The light from 
the ring laser was directed to the cryostat via an opti-
tical single mode fiber. The incident light was linearly 
polarized and its maximal intensity was measured to be 
≈ 200 mW over a Gaussian beam profile with 2 mm 
diameter. A calibrated photo diode was used to mon-
itor the incident power throughout the experiment. A 
combination of three short-pass filters (one SP785 ‘Ra-
zorEdge’, Semrock, NY and two FES0800, Thorlabs, NJ) 
removed any incident radiation longer than 785 nm from 
the laser or the optical setup. The excitation light was 
reflected into the cryostat by a dichroic mirror (FF801-
Di02, Semrock). Emission from the sample longer than 
800 nm passed through the same dichroic mirror, fol-
lowed by two long pass filters (LP780 and LP785, Sem-
rock), and was collected into a 50 µm multimode fiber 
(Thorlabs). The long pass optical filters did not exhibit 
strong distortions to the acquired emission spectra above 
λ=810 nm. To further reduce the amount of reflected and 
scattered light going into the detection path, the sample 
sapphire window was tilted by a few degrees from the 
optical axis. Emission spectra were spectrally analyzed 
by a spectrometer with a 300 lpi grating (Acton SP-2356 
Imaging Spectrograph), and detected by a sensitive CCD 
camera (Roper Scientific, PI Acton PIXIS:100B).

Special attention was given to ensure reliable and re-
producible sample preparation. The following proce-
dure was programmed and computer-controlled: (1) Af-

ter achieving the base temperature of 4.2 K for more than 
20 minutes, pure rare-gas films were first grown on the sapphire window for 300 s with 50 ccm gas flow, (2) then 
the doped crystal of rare-gas and rubidium was grown for 
1500 s with the rare-gas flow held constant, and (3) 
finally pure rare-gas films were coated on the mixed crys-
tal by dosing pure rare-gas for another 300 s. The films 
were grown at 7.8 K, which gave better crystallinity. The 
sample holder temperature did not rise during the crystal 
growing process. Annealing of the films for several hours at T≈T_{melt}/3 was also attempted, but did not produce 
any qualitative change in the acquired spectra in any ma-
trices. All the spectral observation was made at 4.2 K.

In order to achieve a high concentration of isolated 
atoms and not clusters, the dispenser was tuned to a high 
current (8 A) during the growing process. This cor-
responds to a measured temperature of the dispenser of 
250-300°C. The dispenser had a small and narrow 
opening (0.5×4 mm²), and was positioned 40 mm from the 
sapphire window. The concentration of dopant atoms 
inside the crystals was estimated to be on the order of 
1:1000. We found that an initial heating of the dispenser 
was required to achieve a reproducible and homogeneous 
rubidium sample. We annealed the dispenser far away 
from the sapphire window for 20 min prior to each crys-
tal growth.

FIG. 1. Experimental setup used in the present study. (a) 
Side-view inside the cryostat. A nozzle, fed from a compart-
ment at ambient temperature resides inside the vacuum jacket 
of the cryostat. The thermal rubidium dispenser attached on 
a thermal protective holder is held below the nozzle. The 
etire nozzle-dispenser arrangement can be mechanically re-
tracted inside the vacuum chamber and replaced with a black 
beam block for excitation/emission measurements. (b) Top-
view of the optical setup. An optical short-pass filter (SP) 
reduces unwanted higher order contributions from the laser 
and background fluorescence of the optical fiber leading to 
the experiment. Two long-pass filters (LP) allow a highly 
sensitive detection of Stokes-shifted emission from the doped 
thin-films. The sapphire window is slightly tilted to reduce the 
scattering and reflection of laser light to the detection channel.
III. RESULTS

A. Film Thickness

An interferometric measurement was used for the measurement of the thickness of thin-films. Single-frequency HeNe-Laser radiation (632.8 nm) was focused to a small point (≈10 µm), centered on the sapphire window, and the optical fringes after the thin-films was recorded during crystal growth. The spacing of the observed oscillations depended linearly on growing time. Since the thickness measurement was checked against substantial thicker samples, the bulk refractive indices taken from literature \(^{18-20}\) were used for the thickness calculation. The typical thicknesses for the doped fraction of the Ar, Kr, and Xe films, were 2.7, 3.2, and 4.1 µm respectively. The simultaneous doping of Rubidium did not affect the final thickness of the film; the observed optical interference fringes showed the same spacing with and without current flow in the dispenser. With the above mentioned flow rates and times, we found that ≈0.1% of the sprayed on gas adsorbs on the window. This value was consistent for Ar, Kr and Xe. The low yield indicates a continuous ablation from the film while growing, and explains the lack of differences between annealed and unannealed films.

B. Absorption Spectra

Optical absorption spectra of Ar, Kr and Xe thin-films doped with rubidium are shown in Fig. 2. A good qualitative agreement with previously reported spectra \(^{10}\) was obtained for the Rb/Ar system. This reconfirms the existence of two distinct triplets, originating from the removal of the threefold orbital degeneracy of the \(P\) configuration due to the Jahn-Teller crystal field effect. The triplets for the Rb/Kr and the Rb/Xe systems were observed as small dents in the acquired spectra.

C. 2D Spectrum in Ar

Since the emission properties of Rb in rare-gas hosts are not well characterized in the literature \(^{11}\), excitation-emission two dimensional spectra were recorded for the full characterisation. The emission spectra were recorded at a low irradiance on the order of 5 kW/m². The two dimensional spectra of Rb in Ar are shown in the left panel of Fig. 3. A number of emission-excitation peaks were observed. The same complicated 2D spectrum was observed even after the purity of the used argon was carefully checked. After additional annealing for several hours, neither the qualitative nature, the peak positions, nor their relative intensity of the spectrum did change. Argon crystals were prepared with several different conditions, but the observed spectra were consistent over a large range of preparation conditions.

In the excitation spectrum, we found peaks around 705 nm and 755 nm, which are also seen in Fig. 2. The separation of these two peaks in our spectrum is smaller than that reported earlier (700 nm and 775 nm \(^{10,11}\)). The peak in emission due to the excitation of the red-triplet occurred at around 877 nm, which is higher than the reported value of 830 nm \(^{11}\). Generally, the observed emission in Ar was weaker than in other rare-gas hosts. The difference between our results and the previous reports may be attributed to the difference in crystal growth conditions. Due to the lattice mismatch between Ar and Rb, the emission spectrum must be very sensitive to local lattice structures.

Fig. 4 shows excitation and emission spectra, which were obtained by integrating 2D spectra shown in Fig. 3. Direct comparison with the absorption spectrum in Ar (see the top trace of Fig. 2, note that the absorption peaks are downwards) and the excitation spectra (see the upper right panel of Fig. 4, note that the excitation peaks are upwards) tells us that the emission in the Rb/Ar system is mostly due to the very efficient absorption around 755 nm.

In a number of experiments we realized that the amount of laser induced fluorescence was highest for previously-unexposed samples. Further investigations on the Rb/Ar system indicated a bleaching behavior at very high laser irradiation \((I \approx 10 \text{ MW/m}^2)\). Specifically, the irradiation of intense laser radiation at 710 nm depleted...
FIG. 3. Two-dimensional normalized excitation-emission spectra of rubidium in argon, krypton and xenon, observed at T=4.2 K. The argon spectrum shows two main contributions, at the excitation wavelength around 705 nm and 755 nm. These values correspond roughly to the earlier reported values for the red and blue triplet\(^{10}\). The commonly observed simple triplet structure for alkali atoms in rare-gas hosts is seen in Kr and Xe systems. Emission from Rb/Kr was around one order of magnitude stronger than that for the Rb/Xe system.

The excitation peak at 705 nm with the increase of excitation between 730 nm and 770 nm; meanwhile the irradiation at 760 nm weakened the excitation signal at 755 nm with the increase of excitation between 700 nm and 750 nm. These behavior suggested that the bleaching is associated with the population transfer between different sites. Further study is needed to identify site specific behaviors in the bleaching.

The bleaching behaviour is described by the equation \(a \exp(-I/\tau)\), where \(a\) is a constant scaling factor, \(I\) is the irradiance in Wm\(^{-2}\) and \(\tau\) is a characteristic time constant. The associated time-constant for the Rb/Ar system was \(\tau = 1.2\) Wsm\(^{-2}\). Such bleaching only occurred at high laser intensity and was not observed during the low-intensity spectroscopic measurements.

D. 2D Spectrum in Kr

The two dimensional spectrum of rubidium in krypton (Fig. 3, middle), exhibits a simple triplet of excitation-emission peaks. The three peaks are of comparable size and approximately equally spaced in energy. They are centered around 722, 731, and 743 nm respectively, and can be assigned to the so-called “blue-triplet”\(^{10}\). The corresponding red-triplet was not detectable within our detection wavelength range. The corresponding emission spectrum is centered around 923 nm with 37 nm full-width at half-maximum (FWHM).

No spectral difference between annealed and non-annealed samples were detected for Rb in Kr. The photo-depletion, however, of Rb in Kr was observed. After illuminating the samples with an irradiance of \(I=10\) MW/m\(^2\), we found about 95\% of the signal had disappeared. The remaining signal was very stable for further illumination. Although we did not observe any peaks increase in height after the photo-illumination, we tentatively attribute this depletion to a hole-burning process as in the case of the Rb/Ar system. The associated time-constant was \(\tau = 1.1\) Wsm\(^{-2}\).

E. 2D Spectrum in Xe

The rubidium spectrum in xenon (Fig. 3, right) shows a typical triplet structure as for Rb in Kr. The three peaks were close to the edge of our excitation range and the two peaks at longer wavelength were weakly resolved.
| Observed system         | Contribution | Excitation wavelength | Emission wavelength | FWHM | FWHM |
|------------------------|--------------|-----------------------|---------------------|------|------|
| Rb/Ar, red triplet     |              | 755                   | 877                 | 15   | 53   |
| Rb/Ar, blue triplet    |              | 705                   | 989                 | 15   | 53   |
| Rb/Kr, blue triplet    |              | 722, 731, 743         | 923                 | 29   | 37   |
| Rb/Xe, blue triplet    |              | 760, 771, 782         | 969                 | 30   | 39   |

TABLE I. Wavelengths of the excitation and emission of each peak, and their linewidths.

The excitation wavelengths of these peaks were measured at 700, 771, and 782 nm respectively. In addition, weak peaks were observed near 810 nm in the emission wavelength. These weak peaks were not studied in further detail, since the clipping of spectra was severe due to the limited detection range. Generally, the quantum yield of the xenon emission was about one order of magnitude less than that of the krypton samples. We found an increase of scattering of white light for thicker Xe films. This indicates that the Xe films are not as homogeneous as other Ar and Kr films. Xenon’s higher melting point explains this different crystallization behavior.

Table I summarizes the observed peak wavelengths in all crystals.

F. Spectra in Ne

We have attempted to observe Rb spectra in Ne films, but we did not detect any signal. We also tried a different sample preparation method, in which the system was subject to 1000 repeated growing-cooling cycles (1 sec of deposition and 3 sec of cooling). This method also failed to produce spectra. We attribute the failure in Ne samples to the close proximity of the nozzle and dispenser to the sapphire window under our experimental setup. Precooling the Ne gas may improve the growth of doped Ne thin-films.

IV. DISCUSSION

The spectral shift of the $S \rightarrow P$ transition in a solid state system depends on the host environment. In rare-gas films, it is expected that the atomic polarizability contributes most of the spectral shift. In Fig. 5 the spectral positions of the blue and red triplet are shown referenced to the gas phase $D_2$ line. The close linear relation between excitation wavelength and the polarizability allowed assignment of the red and blue bands, partially through extrapolation. The relation between emission wavelength and the polarizability was also found to be linear, and has been reported earlier.

By extrapolating the blue triplets of Kr and Xe linearly, we estimate the excitation wavelength in Ar to be around 708 nm as seen in Fig. 5. If we assume a linear relation for the emission wavenumbers as well, we estimate the emission in Ar to be around 890 nm extrapolating from the values of 923 and 989 nm in Kr and Xe, respectively. These predicted excitation and emission peak wavelengths are closer to our detected peaks (705 nm for excitation and 877 nm for emission) than those reported previously (700 nm for excitation and 830 nm for emission)\textsuperscript{7,10,11}. Experiments on sodium in rare-gas hosts\textsuperscript{7} showed a similar spectral deviation for the Ar system.

By assuming the same separation between the blue and red triplets for each gas, we can estimate the positions of red triplet peaks in Kr and Xe. As shown in Fig. 5, the predicted excitation wavelengths are out of the range of our laser coverage. This explains why we did not observe peaks corresponding to the red triplet in Kr and Xe.

Complicated excitation-emission 2D spectrum in Ar compared to Kr and Xe may result from size differences between the host and matrix atoms. Since there is no report on the one-to-one pair bond length between Rb and rare gas atoms, we employ the reported van der Waals (vdW) radii of 188 pm (Ar), 202 pm (Kr), 216 pm (Xe)\textsuperscript{21,22}, and 303 pm (Rb)\textsuperscript{22} for the size of each atom as a simple approximation. The rare-gas lattice must be distorted by the presence of Rb occupying a single substitutional site. The greater mismatch in radius for Rb/Ar leads us to expect a larger lattice distortion than that from Rb/Kr and Rb/Xe, which may explain the complicated excitation-emission 2D spectrum in Ar. More quantitative discussion on the spectral impact of crystal defects was reported previously\textsuperscript{17}.

The spectral splitting between the three peaks of the observed triplets in Kr and Xe characterizes the Jahn-Teller splitting due to interactions with the host lattice. We do not find any difference between the two Jahn-Teller splittings in Kr and Xe within our measurement accuracy. The interaction that induces the Jahn-Teller splitting must be similar in both gases.

V. CONCLUSION

We have presented absorption, excitation and emission spectra of rubidium in rare-gas hosts. For the excitation and emission, we used two-dimensional spectroscopy to characterize the spectra in more detail. Certain slices through the two-dimensional Rb/Ar spectra agree with earlier reports; however, we find the emission wavelength for the Rb/Ar system red-shifted by $\approx 40$ nm. The spectra of Rb in Kr and Xe have a much simpler structure; the Rb/Kr system showing the strongest emission. Therefore, for very low concentration samples approaching to the single atom level, we propose the use of the Rb/Kr system. For such experiments we would need to increase the collection efficiency of the cryogenic confocal microscope.
FIG. 5. A plot of excitation wavelength vs the polarizability of the rare-gas hosts. The y-axis is linearly scaled in energy. The left-axis shows the wavelengths relative to the gas phase D$_2$ transition. The black points indicates the observed wavelengths obtained in the present study, and the grey points are those reported earlier$^{10}$. The dashed circles indicate extrapolated wavelength to predict the positions of undetected peaks. The extrapolation assumed the same spacing between each pair of blue and red triplets as in Ar (denoted by s).

Our results will be extended to lower Rb concentrations and open a way to better understand the optical properties of thin films of Rb in rare-gases. Further experiments with magnetic fields are under preparation$^{24}$. The undesirable adsorption of Rb and other atoms on surfaces of the vacuum chambers is observed in a number of atom-optics experiments. The optical desorption of Rb from surfaces has been observed$^{9}$ and stands as a potentially useful mechanism. Our experiments might allow a more efficient desorption, since the optical spectrum is better understood.

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