1. Introduction

Nowadays, the problems of air pollution and the fossil fuel shortage have attracted public concern in many countries. As a potential solution to protect the environment and reduce the dependence on traditional fossil fuel, plug-in electric vehicles (PEVs) play an especially important role in the development of raising energy efficiency and alternative to traditional fuel-based automobiles [1–3]. When large-scale PEVs are connected to an electric distribution network simultaneously, some issues including the location of PEVs charging or discharging at a given time, the power fluctuation, active power loss, the state of charge (SOC) of PEVs, and the degree of PEV owners’ satisfactory should be concerned [4, 5]. Considering that PEVs can be regarded as both distributed energy source and load that can be scheduled, vehicle-to-grid (V2G) system was proposed by researchers. In V2G system, power can flow between the power grid system and PEVs. Meanwhile, PEVs can reduce the operation cost of power grid and relieve daily power curve. However, uncoordinated charging and discharging behaviors of PEVs may cause circuit damage, power congestion, electricity shortage, and other grid problems [6, 7]. Therefore, the optimization of PEVs charging and discharging is necessary.

There are many existing studies on the optimal scheduling of PEVs’ charging and discharging behaviors. A new mathematical model was established in the literature [5], to increase the degree of satisfaction of PEV owners and decrease the power grid’s operation cost. Based on the Monte Carlo simulation algorithm, the charging load curves of different types of PEVs were established in the literature [8, 9]. Considering the economic benefit of power grid and PEV owners, a bilayer system was designed in [9]. It verified that the electricity price can adjust the time and the location of PEVs charging and discharging. In [10, 11], an aggregator
was used to exchange information between power grid and PEV owners through VANWT, Wi-Fi, or cellular network. Several studies established optimization model aiming at minimizing the peak-to-valley difference and using the genetic algorithm to optimize the users’ charging time in valley electricity price period [12, 13]. The literature [14] introduced V2G robust energy-scheduling problems, and proposed an algorithm to adjust the trade-off between economic performance and reliable operation. In [15], an algorithm was proposed, which not only can efficiently shift the peak load and reduce the total operation cost, but also can provide great flexibility in adjusting the trade-off between economic performance and reliable operation. In [16], a combined control and communication approach considering distributed features and vehicle preferences was proposed. The literature [17] used the flexibility and schedulability of PEVs to relieve the power fluctuation in power distribution network. To solve the optimal dispatch problem of renewable generators and PEVs, Liu et al. [18] developed a novel algorithm to solve the optimal dispatch problem of renewable generators and PEVs. Most PEVs and power grid problems in V2G system are multiagent problem, and a novel method to solve the multiagent problems was used by [19].

Most of the current researches have focused solely on the management of the distribution grid or economic benefits. However, few researches so far put the two problems together and rarely the literature refers to the PEVs’ traveling purpose. This paper proposed a novel optimization method of PEVs charging and discharging based on the previous methods; meanwhile, the benefit of power grid and PEV users, the traveling purpose of PEV users, and the initial SOC of each PEV were taken into account. To reduce the impact of PEV-centralized charging on the branch in power grid, the main contribution of this paper is considering both the benefit of the power grid and PEV users to ensure the stable operation of the power grid and satisfy the traveling purpose of PEV users. We dominate this problem as the Max Power Grid and PEV Users Profit problem. Considering the initial SOC of PEVs arriving at charging stations, the traveling purpose of PEV users, and the load power without PEVs plugging in at this time, this paper proposed a novel charging and discharging model for PEV users to determine the PEV users’ charging and discharging status and time. Meanwhile, the charging and discharging power of PEVs at a given time is optimized to reduce the power fluctuation of distribution network. Daily basic load power curve is shown in Figure 1 [1].

The rest of the parts of this paper are organized as follows: In Section 2, considering about the current electricity price, the traveling purpose of PEV users, and the SOC of each PEV, the number of PEVs charging and discharging is defined. According to the Max Power Grid and PEV Users Profit problem and the number of PEVs charging and discharging that is obtained from Section 2, Section 3 builds a mathematical model to optimize PEVs’ charging and discharging power. This paper used genetic algorithm (GA) to calculate the optimal result. Section 4 gives the specific algorithm flow. Section 5 shows the simulation results of the mathematical model which is built in the Section 3. Finally, the conclusion of this paper and future work are given in the Section 6.

2. The Model of PEVs Charging and Discharging

2.1. The Model of PEVs Connected to the Power Grid and Initial SOC. This paper analyzed the private PEV-centralized charging and discharging behaviors in the workdays mainly. According to the surveys, the annual average mileage of a vehicle in China is about 15,000~20,000 km and the average daily mileage is 40 km. The peak hours of private PEVs to go to work are from 7:00 to 8:00 and the charging time is during the working hours. The peak hours of private PEVs to come home from work are from 17:00 to 19:00 and the charging time is from 19:00 to 6:00 the next day. So, a PEV can connect to the power grid twice a day, and the initial SOC obeys the normal distribution $N(0.6, 0.01)$ [8]. Considering the traveling purpose of PEV users, the SOC after PEV charging or discharging must be higher than 0.6.

In this part, we assumed that each PEV’s charging power is constantly equal to 3.12 kW, the start time of charging obeys the normal distribution $N(9, 0.25)$, $N(19, 1.25)$, respectively, [5] and the corresponding probability of PEVs connected to the power grid is 0.5 and 0.7, respectively [8]. The Monte Carlo simulation method is used to extract the initial SOC, the charging start time, and the charging finish time of PEVs. Then, we can obtain the result of load calculation under the constraint conditions of meeting the charging time requirements [8]. The calculation model of PEVs charging load based on the Monte Carlo simulation method is shown in Figure 2. We assumed that the maximum capacity in each charging station is 10 PEVs.

2.2. The Cases of PEVs Charging and Discharging. To achieve the peak shaving of the power grid and to ensure the power transportation of each branch smooth, considering the bi-directional flow of energy between PEVs and power grid, the charging and discharging behaviors of PEVs can be coordinated to restrain the power fluctuation of power distribution network.

In this article, we improved the interests of PEV users to stimulate PEV users join in the optimal scheduling of power
distribution network. The electricity price at a given time interval is formulated thanks to Figure 1; the principle of formulation is that when the basic load power is higher, the electricity price is higher and when the basic load power is lower, the electricity price is lower, simulating the PEV users charging at the low-load time period and discharging at the high-load time period on the basis of satisfying the traveling purpose.

Due to the different electricity prices and to make calculation easier, 24 hours a day can be divided into 3 parts: low-price period, normal-price period, and high-price period, and the time interval is 24:00–10:00, 10:00–18:00, and 18:00–24:00, respectively. According to the initial SOC of PEV users and the different time period, the optimization system defines the charging or discharging status for each PEV user, which connected to the power grid. Just take one PEV as example, and all of the PEVs charging load could get satisfying the propose of PEVs traveling. /T_he behaviors of PEVs could be coordinated on the basis of satisfying the propose of PEVs traveling. The SOC of PEVs is updated after each time interval, and the number of PEVs charging and discharging is exported.

3. The Mathematical Model that Optimized PEVs’ Charging and Discharging Power

In this section, we established a mathematical model that the goal is to maximize the benefit of PEV users and minimize the fluctuation of the daily load curve in distribution network; meanwhile, the PEVs’ charging and discharging behaviors do not affect the normal work of basic loads and the power transmission constraints of each branch as the constraint conditions. The power fluctuation of distribution network is reduced, and the stable power transportation of branch is guaranteed through the optimization of charging and discharging power of PEVs.

3.1. The Objective Function. To raise the power grid companies’ profit, the power fluctuation needs to be reduced. Therefore, reducing the power fluctuation is an objective. So, the optimization objective function of power fluctuation \( g_1 \) is denoted as

\[
g_1 = \min \sum_{t=0}^{T} \left( P_{c,t} \times N_{c,t} + P_{load,t} - P_{d,t} \times N_{d,t} - \bar{P} \right)^2, \tag{1}
\]

where \( P_{c,t} \) and \( P_{d,t} \) represent the charging and discharging power of PEV users at time \( t \), respectively, \( N_{c,t} \) and \( N_{d,t} \) represent the number of PEV users’ charging and discharging at time \( t \), respectively, \( P_{load,t} \) represents the basic load power at time \( t \), and \( \bar{P} \) represents the average load power during a day without PEVs. \( P_{load,t} \) and \( \bar{P} \) can be got by gathering the historical data.
To raise the PEV users’ profit, the optimization objective function $g_2$ is denoted as

$$g_2 = \min \rho_{ct} \cdot N_{ct} \cdot \Delta t - \rho_{dt} \cdot N_{dt} \cdot \Delta t,$$

where $\rho_{ct}$ and $\rho_{dt}$ represent the charging and discharging electricity price at time $t$ and $\Delta t$ represents time interval (0.5 h).

We put all the objective functions together, so the method can be regarded as a multiobjective optimization problem. Because coupling does not exist between the objective functions in this paper, the problem can be translated into a single-objective optimization problem by weighted linear combination in the following equation:

$$\min f = \alpha_1 \cdot g_1 + \alpha_2 \cdot g_2,$$

where $\alpha_1$ and $\alpha_2$ is the weight of $g_1$ and $g_2$, respectively, $g_2$ represents the benefit of PEV owners and $g_1$ represents the benefit of power grid where it is more important than $g_2$ because of the demand of reality. Therefore, we set $\alpha_1 = 0.6$, $\alpha_2 = 0.4$.

### 3.2. Constraints.

The following constrains in the mathematical model must be met at each time interval $\Delta t$, and the definitions of corresponding parameters are shown in Table 1.

![Figure 3: The flowchart of the number of PEVs charging and discharging.](image)

| Symbol          | Definition                                                                 |
|-----------------|----------------------------------------------------------------------------|
| $SOC_{ini,h,t}$ | Initial SOC of PEV $h$ when it arriving at the charging station at time $t$ |
| $SOC_{fin,h,t}$ | Final SOC of PEV $h$ when it leaving the charging station at time $t$       |
| $C_{max}$       | The maximum capacity of PEV’s battery                                      |
| $E_{total,t}$   | Total energy in distribution network at time $t$                           |
| $E_{load,t}$    | Total energy used by basic load at time $t$                               |
| $P_{l,\text{max}}$ | Maximum active power transmission of line $l$                           |
| $N_{S_{p},t}$   | Maximum accommodation capacity of the station $S$                         |
| $P_{c,\text{min}}$ | Minimum charging power of PEV                                              |
| $P_{c,\text{max}}$ | Maximum charging power of PEV                                              |
| $P_{d,\text{min}}$ | Minimum discharging power of PEV                                           |
| $P_{d,\text{max}}$ | Maximum discharging power of PEV                                           |
| $N_{p,t}$       | The number of PEVs neither charging or discharging at the charging station $S$ at time $t$ |
| $N_{c,t}$       | The number of PEVs charging at the charging station $S$ at time $t$        |
| $N_{d,t}$       | The number of PEVs discharging at the charging station $S$ at time $t$     |

$$\left(\frac{SOC_{fin,h,t} - SOC_{ini,h,t}}{C_{max}}\right) \cdot N_{c,t} \leq E_{total,t} - E_{load,t},$$

$$P_{Load,t} + P_{c,t} \cdot N_{c,t} + P_{d,t} \cdot N_{d,t} \leq P_{l,\text{max}},$$

### Table 1: The parameters of constraints.
\begin{align*}
P_{c,\text{min}} & \leq P_{c,t} \leq P_{c,\text{max}}, \quad (6) \\
P_{d,\text{min}} & \leq P_{d,t} \leq P_{d,\text{max}}, \quad (7) \\
0 & \leq N_{c,t} \leq N_{c,\text{max}}^{S}, \quad (8) \\
0 & \leq N_{d,t} \leq N_{d,\text{max}}^{S}, \quad (9) \\
0 & \leq N_{\text{p,t}} \leq N_{\text{p,\text{max}}}^{S}, \quad (10) \\
0 & \leq N_{c,t}^{S} + N_{d,t}^{S} + N_{\text{p,t}}^{S} \leq N_{\text{max}}^{S}. \quad (11)
\end{align*}

Constraint (4) ensures that the total PEV users’ charging energy cannot exceed the surplus energy of the distribution network, where the maximum capacity of PEV’s battery \( (C_{\text{max}}) \) is identically equal to 24 kWh. Constraint (5) indicates that the limit of active power transportation of each branch, which ensures the branch safety at power distribution network would not be influenced by PEVs’ charging and discharging behaviors. The constraints (6) and (7) represent the scope of charging and discharging power of PEV’s, respectively. The PEVs would be broken if charging or discharging power exceeds the maximum power of PEVs; meanwhile, the excessive charging and discharging power would increase the fluctuation of the power grid. However, if the PEVs’ charging and discharging power is lower than \( P_{c,\text{min}} \) and \( P_{d,\text{min}} \), the waiting time would become so long that the owners’ degree of satisfaction would decrease. Constraints (8)–(11) represent that the total number of PEVs cannot exceed the maximum accommodation capacity of charging stations, which is to reduce the PEV owner’s waiting time.

### 4. Power Optimization Algorithm

The key of the power optimization algorithm for PEVs charging and discharging is how to deal with the optimal power flow model, which is a nonlinear, nonconvex, large-scale, static optimization problem with both continuous and discrete control variables. Genetic algorithm is applied to find optimal result, the algorithm considered the parameter \((P_{c,t}, P_{d,t})\) as optimal variables. The optimal charging and discharging power of PEVs and the daily power curve of distribution network can be obtained under the PEV users’ responsiveness \( \delta \).

We can obtain the number of PEVs charging and discharging in each charging station at the given time from Section 3. The total PEVs charging power in a charging station equals the sum of charging power of each PEV in the charging station, which is denoted as Equation (12). Similarly, the total PEVs discharging power is denoted as Equation (13). According to the optimization objective functions in the Section 3, choose the excellent parameter \((P_{c,t}, P_{d,t})\).

\[
P_{c,\text{total}} = P_{c,t} \times N_{c,t}, \quad (12)
\]

\[
P_{d,\text{total}} = P_{d,t} \times N_{d,t}. \quad (13)
\]

The main process of algorithm is as follows:

1. Initialize grid load parameters and PEVs load parameters, which include PEV users’ responsiveness, basic load power without PEVs connecting to the power grid in each time interval, average load power during one day without PEVs, the maximum battery capacity of PEVs, initial SOC, arriving time, leaving time, and average energy consumption.

2. Calculate the number of PEVs charging and discharging at the current time interval.

3. Generate 100 initial populations of EV charging power and discharging power \((P_{c,t}, P_{d,t})\) randomly.

4. Calculate the constraint value of populations, which include equality constraints and inequality constraints, and eliminate the populations that unsatisfied the constrains of the mathematical model. Then, calculate the interests of PEV users charging and discharging and the PEVs charging and discharging power at the current time interval according to the initial populations that satisfied constrains. Based on the basic load power at the current time, PEVs charging and discharging power after coordinating and the average basic load power during one day, the power fluctuation of distribution network can be calculated.

5. According to the power fluctuation of distribution network and the charging and discharging interests of PEV users, calculate and sort the fitness value. Select and retain excellent individuals through the roulette rule to ensure that the superior genes are retained.

6. The surviving genes were crossed and mutated to generate offspring populations, where the probability of crossover and mutation is 0.7 and 0.2, respectively.

7. Repeat the iterative optimization, until reaching the maximum genetic algebra, and then output the optimal result \((P_{c,t}, P_{d,t})\).

8. Calculate PEVs charging and discharging power in each charging station \((P_{c,\text{total}}, P_{d,\text{total}})\).

9. Output the daily load power curve that before and after optimization of distribution network.

The optimization algorithm flowchart of charging and discharging power is shown in Figure 4.

### 5. Simulation Results

According to the optimization strategy that proposed in this paper, simulation results can be shown by MATLAB.

Just consider the charging behavior of PEVs and without any coordination, a branch of daily load power curve shown in Figure 5. As can be seen from the figure, the peak-to-valley difference of a branch increased due to the behavior of PEVs uncoordinated charging, especially between 19:00 and 21:00 hours, the load power become too high, which might impact on the power transportation or even damage the branch.
The load power curve after price optimized coordination is shown in Figure 6. Compared with the load power curve of distribution power grid that uncoordinated charging, peak and off-peak difference of the load power curve is decreased thanks to the optimization strategy of electricity price and thus ensure the stable operation of each branch. However, as shown, the power fluctuation is large and PEVs’ charging and discharging power needs to be optimized for each time period in a day.

According to the power optimization in Section 3, the simulation results of one branch and the whole power are

**Figure 4:** The optimization algorithm flowchart of charging and discharging power.
shown in Figures 7 and 8. As can be seen from Figure 7, the peak and off-peak difference in power curve of one branch would increase if PEVs are connected to the power grid while without charging coordination, especially during the 18:00–22:00 hours, which might lead to the electricity shortage of basic load or even damage the circuit. Considering V2G system, the peak and off-peak difference in power curve of one branch can be reduced through the electricity price control and the optimization of charging and discharging power, which ensures the normal operation of branch.

This paper used an IEEE 33-bus distribution network to simulate the whole distribution network, and the specific data can be obtained by [20]. Figure 8 shows the load curve comparison chart of three kinds of cases: basic load without considering the PEVs, uncoordinated PEVs charging and discharging behaviors, PEVs joined in the optimal dispatch of distribution network. As can be seen from Figure 8, the optimization strategy of charging and discharging behaviors of PEVs has a better property on the peak and off-peak difference; meanwhile, daily load power curve is smoother compared with uncoordinated charging and no PEVs.

6. Conclusions

In this paper, we have relieved the intensifying power fluctuation of power grid caused by a large-scale PEVs connecting to the power grid simultaneously. To this aim, we have investigated optimization of the PEVs charging and
discharging behaviors to balance the profit of power grid and PEV owners. A novel two-phase optimization method is proposed for PEVs charging and discharging. The first phase is about optimization of electricity price. According to the historical daily power curve, the status of electricity price is defined based on the principle of high load and high price. This phase ensures the maximum profit of both the power grid and PEV owners, and the PEV owners’ traveling purpose is taken into account at the same time. The second phase is about optimization of PEVs’ charging and discharging power. This phase aims to reduce the fluctuation and ensures the power transmission safety of distribution network. Compared with the power curve of uncoordinated charging and non-PEVs, simulation results have shown that the optimization strategy proposed in this paper can reduce the peak and off-peak difference of distribution network and protect each branch of power transportation which is not damaged obviously.

Data Availability

Daily basic load power data were used to support this study and are available in Reference [4]. These prior studies (and datasets) are cited at relevant places within the text as Reference [4]. Electricity price data were used to support this study and are available in Reference [5]. These prior studies (and datasets) are cited at relevant places within the text as Reference [5]. Specific data of IEEE 33-bus distribution network were used to support this study and are available in Reference [20]. These prior studies (and datasets) are cited at relevant places within the text as Reference [20].

Conflicts of Interest

The authors declare that there are no conflicts of interest exist.

Acknowledgments

This work was supported by National Key Research and Development Program of China (2016YFB0901900), Natural Science Foundation of Hebei Province of China (F2017501107), Open Research Fund from the State Key Laboratory of Rolling and Automation, Northeastern University (2017RALKFKT003), and Technology Support Foundation of Northeastern University at Qinhuangdao (no. XNK201603).

References

[1] R. Yu, W. Zhong, S. Xie, C. Yuen, S. Gjessing, and Y. Zhang, “Balancing power demand through EV mobility in vehicle-to-grid mobile energy networks,” IEEE Transactions on Industrial Informatics, vol. 12, no. 1, pp. 79–90, 2016.

[2] Z. Xia, X. Wang, X. Sun, and Q. Wang, “A secure and dynamic multi-keyword ranked search scheme over encrypted cloud data,” IEEE Transactions on Parallel & Distributed Systems, vol. 27, no. 2, pp. 340–352, 2016.

[3] P. Yi, T. Zhu, B. Jiang, R. Jin, and B. Wang, “Deploying energy router in an energy internet based electric vehicles,” IEEE Transactions on Vehicular Technology, vol. 65, no. 6, pp. 4714–4725, 2016.

[4] J. Yang, L. He, and S. Fu, “An improved PSO-based charging strategy of electric vehicles in electrical distribution grid,” Applied Energy, vol. 128, no. 3, pp. 82–92, 2014.

[5] L. He, J. Yang, J. Yan, Y. Tang, and H. He, “A bi-layer optimization based temporal and spatial scheduling for large-scale electric vehicles,” Applied Energy, vol. 168, pp. 179–192, 2016.

[6] K. Ma, L. Xie, and P. R. Kumar, “A layered architecture for EV charging stations based on time scale decomposition,” in Proceedings of IEEE International Conference on Smart Grid Communications, pp. 674–679, IEEE, Piscataway, NJ, USA, November 2014.

[7] S. V. Chakraborty, S. K. Shukla, and J. Thorp, “A hierarchical networked micro-simulator to study grid-integration of renewables and electric vehicles,” in Proceedings of Modeling and Simulation of Cyber-Physical Energy Systems, pp. 1–6, IEEE, Piscataway, NJ, USA, 2013.

[8] L. Bedogni, L. Bononi, A. D’Elia, M. Di Felice, M. Di Nicola, and T. S. Cinotti, “Driving without anxiety: a route planner service with range prediction for the electric vehicles,” in Proceedings of International Conference on Connected Vehicles and Expo, pp. 199–206, IEEE, Piscataway, NJ, USA, November 2014.

[9] S. Shrestha and T. M. Hansen, “Spatial-temporal stochasticity of electric vehicles in an integrated traffic and power system,” in Proceedings of IEEE International Conference on Electro Information Technology, pp. 0227–0232, IEEE, Piscataway, NJ, USA, May 2016.

[10] J. C. Mukherjee and A. Gupta, “Distributed charge scheduling of plug-in electric vehicles using inter-aggregator collaboration,” IEEE Transactions on Smart Grid, vol. 8, no. 1, pp. 331–341, 2017.

[11] L. Bedogni, L. Bononi, M. D. Felice et al., "An integrated simulation framework to model electric vehicle operations and services," IEEE Transactions on Vehicular Technology, vol. 65, no. 8, pp. 5900–5917, 2016.

[12] S. Y. Ge, L. Huang, and H. Liu, “Optimization of peak-valley TOU power price time-period in ordered charging mode of electric vehicle,” Power System Protection & Control, vol. 40, no. 10, pp. 1–5, 2012.

[13] W. Wei, F. Liu, and S. Mei, “Charging strategies of EV aggregator under renewable generation and congestion: a normalized Nash equilibrium approach,” IEEE Transactions on Smart Grid, vol. 7, no. 3, pp. 1630–1641, 2016.

[14] Z. Zhou, C. Sun, R. Shi, Z. Chang, S. Zhou, and Y. Li, “Robust energy scheduling in vehicle-to-grid networks,” IEEE Network the Magazine of Global Internetworking, vol. 31, no. 2, pp. 30–37, 2017.

[15] K. Wang, L. Gu, X. He et al., “Distributed energy management for vehicle-to-grid networks,” IEEE Network, vol. 31, no. 2, pp. 22–28, 2017.

[16] L. Wang, S. Sherkh, and A. J. Chipperfield, "Optimal decentralized coordination of electric vehicles and renewable generators in a distribution network using A+ search," International Journal of Electrical Power & Energy Systems, vol. 98, pp. 474–487, 2018.

[17] A. Dutta and S. Debbarma, "Frequency regulation in deregulated market Using Vehicle-to-Grid Services in Residential Distribution Network," IEEE Systems Journal, vol. 99, pp. 1–9, 2017.

[18] D. Liu, Y. Wang, and Y. Shen, "Electric vehicle charging and discharging coordination on distribution network using
multi-objective particle swarm optimization and fuzzy decision making,” *Energies*, vol. 9, no. 3, p. 186, 2016.

[19] H. N. D. Melo, J. P. F. Trovao, P. G. Pereirinha et al., “A controllable bidirectional battery charger for electric vehicles with vehicle to grid capability,” *IEEE Transactions on Vehicular Technology*, vol. 67, no. 1, pp. 114–123, 2018.

[20] M. E. Baran and F. F. Wu, “Network reconfiguration in distribution systems for loss reduction and load balancing,” *IEEE Transactions on Power Delivery*, vol. 4, no. 2, pp. 1401–1407, 1989.
