The dynamics of light-induced interfacial charge transfer of different dyes in dye-sensitized solar cells studied by \textit{ab initio} molecular dynamics
The dynamics of light-induced interfacial charge transfer of different dyes in dye-sensitized solar cells studied by ab initio molecular dynamics†

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The charge-transport dynamics at the dye–TiO2 interface plays a vital role for the resulting power conversion efficiency (PCE) of dye sensitized solar cells (DSSCs). In this work, we have investigated the charge-exchange dynamics for a series of organic dyes, of different complexity, and a small model of the semiconductor substrate TiO2. The dyes studied involve L1, D35 and LEG4, all well-known organic dyes commonly used in DSSCs. The computational studies have been based on ab initio molecular dynamics (aiMD) simulations, from which structural snapshots have been collected. Estimates of the charge-transfer rate constants of the central exchange processes in the systems have been computed. All dyes show similar properties, and differences are mainly of quantitative character. The processes studied were the electron injection from the photoexcited dye, the hole transfer from TiO2 to the dye and the recombination loss from TiO2 to the dye. It is notable that the electronic coupling/transfer rates differ significantly between the snapshot configurations harvested from the aiMD simulations. The differences are significant and indicate that a single geometrically optimized conformation normally obtained from static quantum-chemistry calculations may provide arbitrary results. Both protonated and deprotonated dye systems were studied. The differences mainly appear in the rate constant of recombination loss between the protonated and the deprotonated dyes, where recombination losses take place at significantly higher rates. The inclusion of lithium ions close to the deprotonated dye carboxylate anchoring group mitigates recombination in a similar way as when protons are retained at the carboxylate group. This may give insight into the performance-enhancing effects of added salts of polarizing cations to the DSSC electrolyte. In addition, solvent effects can retard charge recombination by about two orders of magnitude, which demonstrates that the presence of a solvent will increase the lifetime of injected electrons and thus contribute to a higher PCE of DSSCs. It is also notable that no simple correlation can be identified between high/low transfer rate constants and specific structural arrangements in terms of atom–atom distances, angles or dihedral arrangements of dye sub-units.

Introduction

Since Grätzel's group presented fully operational dye-sensitized solar cells (DSSCs) in 1991,† many experimental and theoretical methods have been applied for the understanding and improvement of DSSCs in order to boost high cell performance, involve environmentally benign materials and offer low fabrication cost devices for photovoltaic conversion.2–32 The DSSC devices are conceptually simple, consisting of essentially two electrodes and an electrolyte, where (at least) one of the electrodes is made light-sensitive allowing the conversion of light into electric energy. The function is thus not too different from that of a battery, however with the light-conversion ability as an added feature. Therefore, also the role of the sensitizing dye molecules and their interaction with the electrode/semiconducting material will be a central component to study. Until now, power conversion efficiencies (PCEs) over 14% have been achieved by using a combination of two co-sensitizing organic dyes.33,34 However, there still exists a wide space to develop the PCE of DSSCs. The charge-transport processes in DSSCs are critical for high performance of the DSSCs. In this aspect, the effects of the dynamical behaviour of the sensitized dye adsorbed onto the TiO2 surface is yet not fully understood.

The central charge-transport processes (a–e) of DSSCs are outlined in Fig. 1. After the excitation of the dye molecule by sunlight in the visible to near-infrared (IR) range, which means
that the electron of the dye is typically excited from its highest occupied molecular orbital (HOMO) to its lowest unoccupied molecular orbital (LUMO) (a), the excited electron will be transferred, into the conduction band of the semiconductor substrate (b), typically mesoporous TiO\(_2\). Some of the injected electrons will recombine with the oxidized dye or oxidized components of the electrolyte (c). The extent of this type of recombination loss will depend on the rate of electron injection within TiO\(_2\) with respect to that of charge recombination. Among different charge-transfer processes, the charge-recombination process is one of the most important limiting processes in DSSCs. As indicated above, the injected and energy-rich electrons will transport to the back contact and outer circuit through diffusion. Eventually, the redox couple in electrolyte will carry the electron from the counter electrode (d) to the oxidized dye for regeneration (reduction) of the dye (e). In summary, light energy is converted to electric energy generating a photocurrent.

Numerous studies\(^{15-47}\) on the charge transfer at the dye–TiO\(_2\) interface have been made, since the processes of charge-transfer dynamics\(^{48-50}\) and charge recombination significantly affect the PCE of DSSCs. In 1995, Grätzel and his co-workers reported a picosecond electron injection from the Ru-based dye used into the conduction band of TiO\(_2\).\(^{35}\) Similarly, Koops et al.\(^{43}\) presented a detailed comparison of interfacial electron-transfer kinetics in dye-sensitized solar cells containing the coumarin-based organic dye (NKX2677) with respect to those observed for the ruthenium-based organometallic dye, N719. The transient photoluminescence measurements indicated a <60 ps injection halftime for NKX2677 as compared to ~350 ps injection halftime for N719, and the recombination rate was found to be on the microsecond and millisecond time scale. The organic sensitizers showed faster recombination rates, which was probably caused by a generally closer localization of the dye’s highest occupied molecular orbital (HOMO) to the semiconductor surface. Kopidakis et al. stated\(^{31}\) an electron-transport limited recombination with the redox electrolyte and indicated a causal link between electron transport and recombination by using photocurrent and photovoltage transient and spectroelectrochemical techniques. Listorti et al.\(^{44}\) reported a 100 ps electron injection rate from dyes to TiO\(_2\) and also a recombination rate on of microseconds and milliseconds. Several studies have also reported femtosecond injection kinetics for N719-sensitized TiO\(_2\).\(^{36-38}\) Ultrafast fluorescence dynamics demonstrated that the charge injection from the C343 dye to the conduction band of TiO\(_2\) occurred on the 200 fs time scale.\(^{39}\) Results from time-resolved laser techniques indicated an upper limit of 20 to 100 femtoseconds for the time needed to inject an electron from the dye into the semiconductor, which corresponded to the timescale for competing processes, such as charge redistribution.\(^{52}\)

Recently, nanosecond transient absorption spectroscopy\(^{53}\) showed that the rates of electron injection from the sensitized dye to the semiconductor TiO\(_2\), and charge recombination from TiO\(_2\) to the sensitized dye were >(10 ns)\(^{-1}\) and (6.7–8.3 ns)\(^{-1}\), respectively. Moreover, different experimental techniques gave different rates of electron injection. Using a two-component exponential model, the rates of (450 fs)\(^{-1}\) weighted at 47% and (32 ps)\(^{-1}\) weighted at 53% of the spectral response from an IR light probe were obtained, whereas a rate of (250 fs)\(^{-1}\) from a transient ultraviolet-visible (UV-vis) probe, as well as a charge-recombination rate of the magnitude (2–920 ps)\(^{-1}\). Fang et al.\(^{54}\) determined the adsorption of dye molecules on nanoparticle surfaces through second-harmonic light scattering techniques and electron injection through ultrafast transient mid-infrared absorption. They suggested that aprotic solvents with high polarity (such as acetonitrile) yielded more efficient solar cell devices. In addition, injection of photoexcited electrons from the para-ethyl red dye to TiO\(_2\) nanoparticles was characterized by transient absorption on ultrafast time scales.\(^{55}\) The electron injection lifetimes were in the range of 250–300 fs in different solvent environment, but displayed a trend in correlation with solvent polarity (the higher polarity, the faster electron injection): the electron injection lifetime was the shortest (257 fs) in acetonitrile followed by dichloromethane (271 fs) and chloroform (296 fs).

Theoretical investigations have rarely been used to report the rate constants of electron injection from dyes to TiO\(_2\). Ronca et al.\(^{56}\) reported a joint theoretical and experimental investigation on the effect of TiO\(_2\) protonation on the interfacial electronic coupling and injection rate constants in organic dye-sensitized solar cells. Based on a simplified computational strategy of the organic sensitizer LUMO partial density of states (PDOS), they estimated the electron injection time about 3 and 6 fs. A density-functional theory approach (DFT) and time-dependent density-functional theory (TD-DFT) calculations were performed to study the solvent effects on the interfacial charge transfer in DSSC in three different solvents, including water, acetonitrile and carbon tetrachloride.\(^{57}\) The results suggested that acetonitrile was the best solvent for using in combination with an MZ-341 dye due to the electron and thermodynamic properties. Samanta et al.\(^{27}\) used DFT calculations to investigate the mechanism of electron injection and recombination at the dye–TiO\(_2\) interface, as well as the related structural properties. They estimated the rate constants of electron injection and charge recombination to be in the order of (10 ps)\(^{-1}\)–(10 ns)\(^{-1}\) and (10 ps)\(^{-1}\)–(100 ns)\(^{-1}\), respectively; thus highly competitive. Nevertheless, the use of a static structural model risks to overlook the effects of the intricate dynamical structural changes affecting the rate of charge transfer at the dye–TiO\(_2\) interface. Using experimental approaches to study the correlation between the dynamics of structure and charge transfer is extremely difficult in terms of the limited available techniques. However, a dynamical theoretical approach can offer valuable insights.
The main ambition of this work is to elucidate the effects of structural dynamics on the central processes of charge transfer at the dye–TiO₂ interface. *Ab initio* molecular dynamics (aMD) have been used to monitor the structural dynamics of protonated and deprotonated dyes in the L1–(TiO₂)₉, D35–(TiO₂)₉, and LEG4–(TiO₂)₉ model systems using the TeraChem code.²⁸ The structural dynamics obtained were subsequently used to estimate the electronic coupling of electron injection, hole transfer and charge recombination by using the Amsterdam Density Functional-2019 (ADF) software.⁵⁹ Using the Marcus–Hush theory,⁶⁰,⁶¹ electronic coupling and re-organization energies can be used to estimate the rate constant of charge transfer of these central processes in the DSSCs. It should be noted here that the present models for dye–TiO₂ interaction assumes that the main interactions take place between the dye–carboxylate group and the TiO₂ slab. This implicitly also assumes the dye molecules to be organized in a well-ordered, self-assembled monolayer, even though experimental evidence indicates that the interaction most likely is significantly more complex.⁶²–⁶⁴

The detailed analyses include the following section (1) The electronic coupling and rate constants of electron transfer, hole transfer and charge recombination of a dynamical process. (2) The relationship between electronic coupling and structural properties including specific atom–atom distances, angles and dihedral angles. (3) For comparison, also the electronic coupling, rate constants and structural properties of the optimized systems of the protonated and deprotonated L1–TiO₂, D35–TiO₂ and LEG4–TiO₂ systems have been estimated and are compared to the results obtained taking the structural dynamics into account.

**Computational details**

The model systems used in the current study are constructed from the D–π–A-type dye molecules L₁, D₃₅ and LEG₄, as well as their deprotonated versions combined with a model of the TiO₂ substrate, (TiO₂)₉, which has been validated to be sufficiently large to study the electron injection mechanism⁶⁵ and has previously successfully been used to model the charge-transfer characteristic of DSSCs by Samanta et al.²⁷ and Li et al.⁶⁶ see Fig. 2. The initial structures were structurally optimized using Gaussian 16, Revision C.01.⁶⁷ All dyes include the building blocks triphenylamine (TPA), thiophene and cyanoacrylic acid, which are typically denoted as the donor (D), π bridge and acceptor (A) parts, respectively. This paper aims to unveil the rate constant differences of charge transfer including the electron transfer from the LUMO of the dye to the LUMO of TiO₂, the hole transfer from the HOMO of TiO₂ to the HOMO of the dye, and the electron recombination reaction from the LUMO of TiO₂ to the HOMO of the dye. The computational strategy can be outlined as follows.

Firstly, the initial molecular conformations were obtained from geometric optimization employing the B3LYP hybrid functional and basis sets of 6-31g(d) quality for all atoms, except for the Ti atoms. The LANL2DZ basis set including an effective-core potential (ECP) was used for the Ti atoms. In the next step, *ab initio* molecular dynamics (aMD) was implemented using the TeraChem code, also at B3LYP level and with the same basis sets as in the initial calculations. Six simulation systems were constructed consisting of protonated-L1(TiO₂)₉, protonated-D35(TiO₂)₉, protonated-LEG4(TiO₂)₉, deprotonated-L1(TiO₂)₉, deprotonated-D35(TiO₂)₉, and deprotonated-LEG4(TiO₂)₉. The total simulation time for all systems was 100 ps and the time step 1 fs. The canonical ensemble NVT was utilized. A Langevin thermostat was adopted to retain the simulation temperature at 300 K.

After the aMD simulations, snapshots of the first 50 ps were selected for subsequent estimation of the charge-transfer rate constants at every 0.1 ps interval. In order to detect any faster correlations, all simulations were also analyzed every fs in a 0.5 ps section in the steady-state region of the simulations. No additional information could be extracted from these regions of higher temporal resolution. Following the Marcus–Hush theory, the electronic coupling and re-organization energy are essential for estimating the rate constants of charge transfer. As a popular computational chemistry software package, ADF has been successfully used to quantitatively predict the charge mobilities of π-stacked systems.⁵⁹ the charge transport in columnar stacked triphenylenes,⁶⁸ and absolute rate of hole transfer in DNA.⁶⁹ In this context, ADF was used to obtain the electronic coupling using the PW91 density functional at the generalized-gradient approximation level and basis sets of TZ2P quality.⁷⁰ In the electronic coupling calculations, the systems consisting of a dye and the TiO₂ model were separated into two fragments: the dye molecule and the TiO₂ model, respectively. Calculations on the separated fragments with full symmetry was carried out to generate the matrix elements of the molecular Kohn–Sham Hamiltonian in terms of fragment orbitals. In the charge-integral approach, a tight-binding approximation is employed, which treats the electron or the hole as a single orbital and assumes that only the nearest neighbouring fragments are involved in the coupling. Subsequently, the charge-transfer integrals and spatial overlap integrals of the HOMOs and LUMOs of the dyes and TiO₂, respectively, were calculated. This offers an estimation of the electronic coupling of electron transfer, hole transfer and charge recombination, modelled by the coupling between the LUMO of the dye and the LUMO of the TiO₂ fragment, the HOMO of the dye and the
HOMO of the TiO2 fragment, and finally the HOMO of the dye and the LUMO of the TiO2 fragment, respectively. To study the solvent effect, the electronic coupling calculations of both with and without considering implicit acetonitrile effect have been done for deprotonated L1–TiO2 system. The scalar level in the ZORA formalism and the MAPA potential were used for including relativistic effects. Dispersion correction using thegrimme4 model with \( s_b = 1.0 \) \( a_b = 0.7728 \) \( a_1 = 0.3958 \) \( a_2 = 4.9341 \) were used. The input files used for the calculations of electronic coupling can be found in ESL.† In order to obtain an accurate re-organization energy to be used in the estimates of charge-transfer rate constants, two different methods were used including optimized structures, as well as a statistical method. Both Gaussian 16 and ADF were used to calculate the re-organization energies of electron and aiMD simulation methods yielded by the Nelsen four-point method were carried out and the values obtained from aiMD simulations were ultimately adopted to estimate the rate constant of charge transfer.

Results and discussion

1 Charge-transfer analysis

Light absorption in a DSSC device results in the excitation of an electron in the sensitizing dye used. In semiconductor-type of solar cells, this would have been described in terms of an exciton being formed. However, in a molecular device, such as a DSSC, the function can be focused on the excited electron, regarding the hole formed in the dye HOMO as stationary. Since modern dyes used in DSSCs are of push–pull type, charge separation is typically generated already upon electron excitation. In organic dyes, such as the ones studied in this work, the main first excitation is a singlet-to-singlet excitation mainly involving a transition from the HOMO to the LUMO of the dye. Injection to the TiO2 substrate typically takes place on the femtosecond scale, as reviewed above, providing that the dyes have been chosen properly and electrolyte additives not push the conduction band (LUMO) of the TiO2 substrate to too high energies. The dyes in this study have all been shown to work excellently as sensitizing dyes in DSSCs. Based on the Marcus–Hush formula,

\[
\lambda = \frac{E_b - E_a}{2} + \frac{\Delta G}{4k_B T}
\]

(1)

In eqn (1) \( J \) stands for the electronic coupling, between the dye and (TiO2)\( _N \). The electronic coupling of electron transfer, hole transfer and charge recombination in the model applied take place between the LUMO of the dye and the LUMO of TiO2, the HOMO of the dye and the HOMO of TiO2, and the HOMO of the dye and the LUMO of TiO2, respectively. \( \lambda \) represents re-organization energy and \( \Delta G \) symbolizes the Gibbs free energy difference between the initial and final states. \( k \) is the rate constant of charge transfer, \( h \) is plank quantum number, \( T \) is the temperature (absolute scale), and \( k_B \) is the Boltzmann constant. In this context, it should be noted that the essential calculational results are represented by the instantaneous coupling estimated from the many snapshots obtained from the aiMD simulations. The re-organization energies are required to transfer this information into terms of rate constants of charge transfer and can be regarded as a weighting function introducing one more level of uncertainty. Therefore, these results are handled in separate sections below.

1.1 Re-organization energy

The re-organization energy of a process carries information about the difference in energy between the initial and end states in a reaction and therefore implicitly also information about the barrier height of reaction expected according to eqn (1). Many theoretical studies routinely employ four-point geometric optimizations, as shown in eqn (2), to estimate the re-organization energies \( \lambda_e \) and \( \lambda_h \) for electron transfer and hole transfer, respectively. Table 1 gives the re-organization energies of electron and hole transfer in the deprotonated and protonated L1–TiO2, D35–TiO2 and LEG4–TiO2 systems as obtained from ADF and Gaussian 16. The data suggest that the re-organization energy of electron hopping in the protonated D35–TiO2 system obtained from Gaussian 16 is 1.21 eV larger than that obtained from ADF, which represents a significantly higher difference than expected. The re-organization energies obtained from the deprotonated systems derived using Gaussian 16 are clearly higher than those obtained from ADF, which suggests results from this kind of simple geometry optimization may be inflicted with very high uncertainties. Considering the calculational approach used in this study, where several snapshots from a dynamical simulation are used, the use of an optimized configuration representing just one of many possible configurations appears somewhat arbitrary. Therefore, alternative models to estimate the re-organization energies must be explored.

The formulas of optimization method27 for re-organization energies calculation are shown in eqn (2).

\[
\lambda_e = (E_b^e - E_a^e) + (E_b^0 - E_a^0)
\]

\[
\lambda_h = (E_b^h - E_a^h) + (E_b^0 - E_a^0)
\]

(2)

Instead, the use of the statistical method (Nelsen’s four-point method) to estimate the re-organization energy appears more

| Table 1 | The re-organization energies of the protonated and deprotonated L1–TiO2, D35–TiO2 and LEG4–TiO2 systems obtained from ADF and Gaussian |
|------|-----------------|---------------|---------------|---------------|---------------|
| Unit (eV) | L1–TiO2 | D35–TiO2 | LEG4–TiO2 |
| | p* | dep* | p* | dep* | p* | dep* |
| ADF | \( \lambda_e \) | 0.30 | 0.30 | 0.28 | 0.27 | 0.21 | 0.27 |
| | \( \lambda_h \) | 0.45 | 0.21 | 0.33 | 0.71 | 0.24 | 0.23 |
| Gaussian | \( \lambda_e \) | 0.62 | 1.03 | 1.49 | 1.00 | 0.46 | 0.48 |
| | \( \lambda_h \) | 0.28 | 0.78 | 0.43 | 1.10 | 0.29 | 0.83 |

\( a \) Represent the protonated system. \( b \) Represent the deprotonated system.
relevant in the current study. The formula of re-organization energies of electron transfer, hole transfer and charge recombination are shown in eqn (3). Based on eqn (3), re-organization energies obtained from static optimization and from 10 ps aiMD simulations, as listed in Tables S2 (ESI†) and Table 2, respectively, render very similar values. The 10 ps aiMD simulations were performed for each separate system including neutral dye(0), anionic dye(−), cationic dye(+), neutral TiO2(0), anionic TiO2(−) and cationic TiO2(+) employing the B3LYP hybrid functional and 6-31g(d) basis sets for C, H, O, N and S, as well as LANL2DZ for the Ti atoms. 100 steady-state snapshots from the aiMD simulations were selected to generate the single point energies of, $E_{\text{dye}(0)}$, $E_{\text{dye}(-)}$, $E_{\text{dye}(+)}$, $E_{\text{TiO2}(0)}$, $E_{\text{TiO2}(-)}$, $E_{\text{TiO2}(+)}$ and the same level of theory. The re-organization energies obtained from the aiMD simulations were ultimately used in this study.

\begin{align}
\lambda_c &= (E_{\text{dye}(+)} - E_{\text{dye}(0)}) + (E_{\text{TiO2}(0)} - E_{\text{TiO2}(-)}) \\
\lambda_h &= (E_{\text{dye}(+)} - E_{\text{dye}(0)}) + (E_{\text{TiO2}(0)} - E_{\text{TiO2}(+)}) \\
\lambda_{\text{rec}} &= (E_{\text{dye}(0)} - E_{\text{dye}(-)}) + (E_{\text{TiO2}(+)} - E_{\text{TiO2}(0)})
\end{align}

Here, $\lambda_c$, $\lambda_h$ and $\lambda_{\text{rec}}$ represent the re-organization energies of electron transfer, hole transfer and charge recombination, respectively. Each energy is obtained from the average of 100 structural simulation snapshots. $E_{\text{dye}(−)}$ and $E_{\text{TiO2}(−)}$ are the energies of the anionic state of the dye molecule and the TiO2 substrate. $E_{\text{dye}(0)}$ and $E_{\text{TiO2}(0)}$ represent the energies of the neutral dye and the neutral TiO2 model in their neutral state. $E_{\text{dye}(+)}$ and $E_{\text{TiO2}(+)}$ symbolize the energies of the neutral dye obtained from cationic and anionic snapshot structures, respectively. $E_{\text{dye}(0)}$ and $E_{\text{TiO2}(0)}$ express the energies of the anions of the dye molecule and the TiO2 substrate from their neutral structures. $E_{\text{TiO2}(0)}$ and $E_{\text{TiO2}(+)}$ symbolize the energies of the cations from neutral TiO2 snapshot structures and cationic snapshot structures, respectively. $E_{\text{TiO2}(−)}$ represent the energy of the neutral TiO2 model generated from the anionic snapshot structures.

### 1.2 Gibbs free energy difference

The current model systems of charge transfer are best regarded as two-state systems, and thus a suitable method for the estimation of changes in the Gibbs free energy difference, $\Delta G$, must be identified. Some charge-transfer states are poorly described by standard density functional due to long-range, self-interaction errors.71-73 Thus, extended investigation into the identification of appropriate density functionals to model the charge-transfer state was performed. It was noted that the commonly used B3LYP hybrid functional in fact provides reasonable $\Delta G$ estimates, which has been reported by Liu et al.74 Therefore, all our $\Delta G$ estimates were performed at the level of B3LYP/6-31g(d), with the exception for LANL2DZ applied to Ti atoms.

A charge-transfer state should ideally be modelled by the optimized-excited state structure. However, because of severe convergence problems of excited-state structures for quite large systems, it is infeasible to obtain the optimized electronic structure and energy of the excited state. Cornil et al.75 obtained the Gibbs free energy difference by computing the energies of the isolated neutral and charged donor/acceptor systems ($E_{D}/E_{A}$ and $E_{D^+}/E_{A^−}$), as well as the energy of the excited donor ($E_{D^*}$) and the energy of Coulombic interaction between the donor and the acceptor $\Delta E_{\text{coul}}$. The Gibbs free energy difference of charge recombination ($\Delta G_{\text{rec}}$) and electron transfer ($\Delta G_{e}$) were analogously calculated by $E_{D} + E_{A} - E_{D^*} - E_{A^*} + \Delta E_{\text{coul}}$ and $E_{D} + E_{A} - E_{D^*} - E_{A^*} + \Delta E_{\text{coul}}$, respectively. This approximation is suitable if the main interaction term between the donor and the acceptor is the Coulombic one.

Liu et al.74 also reported an approach to evaluate the Gibbs free energy difference of the charge recombination ($\Delta G_{\text{rec}}$) and electron transfer ($\Delta G_{e}$). They suggested that the $\Delta G_{\text{rec}}$ can be obtained from the energy difference between the sum of $E_{D}$ and $E_{A}$ and the energy of the charge-separated state $E_{\text{cs}}$. $\Delta G_{e}$ can be computed by the energy difference between the energy $E_{\text{cs}}$ and the sum of the excited state donor energies $E_{D^*}$ and $E_{A}$. Liu and co-workers noted that the energy difference between the donor/acceptor dimer and the sum of the energy of the separate donor/acceptor typically is quite small (0.02 eV) because of the small Coulombic interaction energy. Therefore, it is reasonable to assume that the energy of the complex of the donor excited state and acceptor ground state properly can be represented by the sum of the separate molecular component in the excited state $E_{D^*}$ and the ground state $E_{A}$ generating only small errors. However, the authors pointed out that the charge-separated state energy cannot simply be replaced by the sum of the separate entity charge energy, $E_{D^*}$ and $E_{A^*}$, because the interaction between the charged fragments, $D^*$ and $A^*$, is large.

Based on the above methods to estimate the Gibbs free energy difference, we employed the above computational strategy to obtain the Gibbs free energy difference for the protonated and the deprotonated L1–TiO2, D35–TiO2, LEG4–TiO2 systems. In conclusion, a vertical excited-state calculation of the dye–TiO2 system in the structure of the ground state is used as an approximation to acquire the energy of the charge-separated state $E_{\text{cs}}$. Furthermore, all the interaction energies between the dye and the TiO2 substrate before and after electron transfer, hole transfer and charge recombination were considered. The formula used to
estimate the Gibbs free energy differences of electron transfer, hole transfer and charge recombination are shown in eqn (4). For the deprotonated L1–TiO2 system including implicit solvent effect, the energy of the charge-separated state $E_{\text{cs}}$ could be obtained by geometric optimization of the excited state (feasible computational effort).

$$
\Delta G_e = E_{\text{cs}} - \left( E_{\text{TIO2}} + E_{\text{TiO2}} + E_{\text{inter}}(\text{dye}/\text{TiO2}(0)) \right)
$$

$$
\Delta G_h = \left( E_{\text{dye}} + E_{\text{TiO2}}^{+} + E_{\text{inter}}(\text{dye}(0)/\text{TiO2}(1)) \right)
$$

$$
\Delta G_{\text{rec}} = E_{\text{dye}(0)/\text{TiO2}(0)} - E_{\text{cs}}
$$

(4)

Here, $\Delta G_e$, $\Delta G_h$ and $\Delta G_{\text{rec}}$ are the Gibbs free energy difference of electron transfer, hole transfer and charge recombination, respectively. $E_{\text{dye}(0)/\text{TiO2}(0)}$ is the energy of the complex consisting of the dye and TiO2 model before charge separation, also including basis set superposition error (BSSE) correction. $E_{\text{cs}}$ represents the vertical triplet excited state energy of dye–TiO2 entity, which approximately models the energy of the charge-separated state. $E_{\text{dye}}$ is the energy of the vertical triplet excited state of the dye. $E_{\text{TIO2}}$ and $E_{\text{TiO2}}^{+}$ are the energies of the neutral TiO2 model and the dye, respectively. $E_{\text{TiO2}}^{+}$ and $E_{\text{dye}}^{+}$ represent the energies of the cationic TiO2 model and the dye, respectively. $E_{\text{inter}}(\text{dye}/\text{TiO2}(0))$ represents the interaction energy between the excited-state dye and the neutral TiO2 model, which here is regarded to model the interaction between the ground-state dye and the ground-state TiO2 fragment. $E_{\text{inter}}(\text{dye}(0)/\text{TiO2}(1))$ is the interaction energy between the neutral dye and the cationic TiO2. Finally, $E_{\text{inter}}(\text{dye}^{+}/\text{TiO2}(0))$ is the interaction energy between the cationic dye and the neutral TiO2 substrate. The interaction energies include BSSE corrections. The changes in Gibbs free energy of electron transfer, hole transfer and charge recombination for the protonated and the deprotonated L1–TiO2, D35–TiO2 and LEG4–TiO2 systems are listed in Table 3.

1.3 Dynamic electronic coupling between different dyes and TiO2. It should be noted that the dyes L1, D35 and LEG4, all relying on anchoring via the cyanoacrylic end-group, are expected to lose their protons upon coordination with the TiO2 surface, based on existing literature, and are thus most properly be represented by the deprotonated model in our study. However, the comparison between protonated and deprotonated coordination modes may give some insights into the charge-transfer dynamics in the systems and therefore also the protonated models are investigated.

The electronic coupling of charge transfer reflects the strength of the orbital interaction between the selected dye and the TiO2 fragment orbitals and therefore gives information regarding the probability of charge transfer. The electronic coupling of electron transfer, hole transfer and charge recombination of the protonated and deprotonated L1–TiO2, D35–TiO2 and LEG4–TiO2 systems during a 50 ps aMD simulation are depicted in Fig. 3(a–i) and 4(a–i), respectively. Fig. 3(a–c, d–f and g–i) show the electronic coupling of electron transfer, hole transfer and charge recombination for the protonated L1–TiO2, D35–TiO2 and LEG4–TiO2 systems, respectively. The electronic couplings of electron transfer, hole transfer and charge recombination vary significantly in the systems: $1.0 \times 10^{-5}$–$0.14$, $1.0 \times 10^{-5}$–$0.012$ and $1.0 \times 10^{-5}$–$0.168$ eV for the protonated L1–TiO2 system; $0.003$–$0.347$, $1.0 \times 10^{-5}$–$0.004$ and $1.3 \times 10^{-6}$–$0.192$ eV for the protonated D35–TiO2 system; and $1.0 \times 10^{-5}$–$0.194$, $1.0 \times 10^{-5}$–$0.016$ and $1.8 \times 10^{-4}$–$0.126$ eV for the protonated LEG4–TiO2 system, respectively. The average electronic coupling of electron transfer, hole transfer and charge recombination are 0.056, 0.002 and 0.045 eV for the protonated L1–TiO2 system; 0.179, 0.001 and 0.095 eV for the protonated D35–TiO2 system, and 0.069, 0.002 and 0.040 eV for the protonated LEG4–TiO2 system, respectively. The electronic coupling of hole transfer for all the three systems are extremely low, which suggests the interaction between the HOMOs of protonated L1, D35 and LEG4 and the HOMO of the TiO2 model are quite weak. The shapes and the number of the peaks of electronic coupling of electron transfer and charge recombination are extraordinary similar, while the electronic couplings of charge recombination are about half that of the electron transfer. This indicates that there exists some kind of relationship between electron transfer and charge recombination, which is consistent with the results reported by Kopidakis et al.51

| Table 3 | The Gibbs free energies differences of electron transfer, hole transfer and charge recombination of the protonated and the deprotonated L1–TiO2, D35–TiO2 and LEG4–TiO2 systems, as well as the deprotonated L1–TiO2 including implicit solvent effect |
|--------|--------|--------|--------|--------|
|        | L1–TiO2 | D35–TiO2 | LEG4–TiO2 |
| Unit (eV) | p¹ | dep/dep² | p¹ | dep | p¹ | dep |
| −ΔG_e | 0.30 | 0.66/0.91 | 1.18 | 0.54 | 0.89 | 0.94 |
| −ΔG_h | 0.94 | 0.72 | 0.93 | 0.43 | 0.94 | 0.71 |
| −ΔG_{rec} | 1.15 | 0.13/0.56 | 0.97 | 1.39 | 0.84 | 1.29 |

¹ Represent the protonated system. ² Represent the deprotonated system. ³ Represents implicit solvent effect.
As noted above, the deprotonated dye systems described below will represent models closest to the systems studied experimentally. The electronic coupling of electron transfer, hole transfer and charge recombination vary from $7.2 \times 10^{-4}$–$0.381$, $5.0 \times 10^{-5}$–$0.047$ and $0.369$–$1.695$ eV for the deprotonated L1–TiO$_2$ system, $2.5 \times 10^{-4}$–$0.381$, $1.0 \times 10^{-5}$–$0.026$ and $0.001$–$1.569$ eV for the deprotonated D35–TiO$_2$ system, and $4.6 \times 10^{-4}$–$0.282$, $1.0 \times 10^{-5}$–$0.042$ and $0.389$–$0.619$ eV for the deprotonated LEG4–TiO$_2$ system, respectively. The average electronic coupling of electron transfer, hole transfer and charge recombination are $0.255$, $0.011$ and $1.135$ eV for the deprotonated L1–TiO$_2$ system; $0.131$, $0.007$ and $1.100$ eV for the deprotonated D35–TiO$_2$ system; and $0.146$, $0.008$ and $1.154$ eV for the deprotonated LEG4–TiO$_2$ system, respectively. The electronic coupling of electron transfer of deprotonated L1–TiO$_2$, D35–TiO$_2$ and LEG4–TiO$_2$ systems are all of same order of magnitude and slightly larger than those of the protonated systems. This suggests that the electron transfer of the deprotonated systems show slightly higher probability. Electronic coupling of hole transfer for all the three deprotonated systems are apparently lower than those of electron transfer by about one order of magnitude, which suggests that the interaction between the LUMOs of the deprotonated L1, D35 and LEG4 dyes and the LUMO of TiO$_2$ are stronger than those between the HOMO of the deprotonated L1, D35 and LEG4 dyes and the HOMO of TiO$_2$. To our surprise, the electronic coupling of charge recombination in the deprotonated L1–TiO$_2$, D35–TiO$_2$ and LEG4–TiO$_2$ systems are significantly higher than those of electron transfer and hole transfer, as well as higher than the corresponding coupling in the protonated systems. The shapes and the number of peaks of the electronic coupling dynamics of electron transfer and charge recombination are quite similar, also compared to those of the protonated systems. The electronic coupling of electron transfer seems to be correlated with charge recombination, which again is in good agreement with the results reported by Kopidakis et al.$^{51}$

**1.4 Dynamic rate constants of charge transfer.** As noted above, the results of electronic coupling can here be translated into rate constants of charge transfer using eqn (1). Already from the dynamics of electronic coupling, it is clear that the temporal dye–TiO$_2$ structure will differ enormously. This must have consequences for the average charge-transfer rates observed experimentally, which by necessity must represent average values over time and space. The charge transport at the dye–TiO$_2$ interface is highly central for the ultimate PCE recorded for DSSCs. According to the Marcus–Hush theory, the rate constants of electron transfer, hole transfer and charge recombination for the protonated and deprotonated L1–TiO$_2$, D35–TiO$_2$ and LEG4–TiO$_2$ systems are shown in Fig. 5(a–i) and 6(a–i), respectively, and these by necessity represent weighted consequences of the corresponding orbital electronic coupling highlighted in the preceding section. The maximum rate constants of electron transfer, hole transfer and charge recombination are $(81.2 \text{ fs})^{-1}$, $(920.0 \text{ fs})^{-1}$ and $(3.4 \text{ fs})^{-1}$ for the protonated L1–TiO$_2$ system, $(0.7 \text{ fs})^{-1}$, $(487.3 \text{ fs})^{-1}$, $(2.9 \text{ fs})^{-1}$ for the protonated D35–TiO$_2$ system, and $(2.2 \text{ fs})^{-1}$, $(405.5 \text{ fs})^{-1}$ and $(10.5 \text{ fs})^{-1}$ for the protonated LEG4–TiO$_2$ system, respectively.
The average rate constants of electron transfer, hole transfer and charge recombination are \( (479.9 \text{ fs}^{-1}, (141.8 \text{ ps}^{-1}) \) and \( (28.8 \text{ fs}^{-1}) \) for the protonated L1–TiO\(_2\) system; \( (2.3 \text{ fs}^{-1}, (131.6 \text{ ps}^{-1}) \) and \( (9.8 \text{ fs}^{-1}) \) for the protonated D35–TiO\(_2\) system, and \( (11.9 \text{ fs}^{-1}, (7.9 \text{ ps}^{-1}) \) and \( (64.7 \text{ fs}^{-1}) \) for the protonated LEG4–TiO\(_2\) system, respectively. The maximum and average values of the rate constants of electron transfer and charge recombination are on a femtosecond time scale. The maximum and average values of rate constants of hole transfer are on a femtosecond and pico-second time scale, respectively. Our results are close to those experimental results.\(^{36,40,76-78}\) The dynamics of charge recombination is as mentioned above correlated to those of electron transfer.

Fig. 6(a–i) shows the rate constants of charge transfer for the deprotonated L1–TiO\(_2\), D35–TiO\(_2\) and LEG4–TiO\(_2\) systems. The fastest rate constants of electron transfer, hole transfer and charge recombination are \( (0.3 \text{ fs}^{-1}, (127.5 \text{ fs}^{-1}) \) and \( (0.007 \text{ fs}^{-1}) \) for protonated L1–TiO\(_2\) system; \( (1.4 \text{ fs}^{-1}, (7.3 \text{ ps}^{-1}) \) and \( (0.3 \text{ fs}^{-1}) \) for deprotonated D35–TiO\(_2\) system; and \( (0.8 \text{ fs}^{-1}, (9.3 \text{ fs}^{-1}) \) and \( (0.03 \text{ fs}^{-1}) \) for deprotonated LEG4–TiO\(_2\) system. The corresponding average value of electron transfer, hole transfer and charge recombination are \( (0.9 \text{ fs}^{-1}, (1.4 \text{ ps}^{-1}) \) and \( (0.1 \text{ fs}^{-1}) \) for deprotonated L1–TiO\(_2\) system; \( (19.7 \text{ fs}^{-1}, (79.6 \text{ ps}^{-1}) \) and \( (0.5 \text{ fs}^{-1}) \) for deprotonated D35–TiO\(_2\) system; and \( (2.3 \text{ fs}^{-1}, (1.2 \text{ ps}^{-1}) \) and \( (0.05 \text{ fs}^{-1}) \) for deprotonated LEG4–TiO\(_2\) system.

In contrast to the corresponding protonated systems, the rate constants of charge recombination of the deprotonated systems are about two or three orders of magnitude faster. These results demonstrate that when an electron is transferred from a deprotonated dye to TiO\(_2\) there is a high probability (risk) that it will transfer back to the dye increasing losses of injected, energy-rich electrons from the TiO\(_2\) substrate. In this context, it is notable that DSSCs based on liquid electrolytes normally include electrolyte additives in terms of salts of small, polarizable cations, such as Li\(^{+}\) or Mg\(^{2+}\). The polarizing cations are thought to assemble at the dye–TiO\(_2\) interface, where they can both affect the charge-transfer balance and the energy levels of both the adsorbed dyes and the TiO\(_2\) substrate. It can be anticipated that added Li\(^{+}\) ions to the electrolyte may have a similar effect as the protons of the cyanoacrylic acid groups of the dyes in retarding recombination loss rate constants. This will be investigated in the following section.

### 1.5 The effects of lithium ions.

In order to get some insights into the effects of lithium ions in the deprotonated dye–TiO\(_2\) systems, in particular regarding the rate constants of recombination loss reactions from TiO\(_2\) to the dyes, two different structural models were studied using aiMD for the deprotonated L1–TiO\(_2\) system. A lithium ion was placed at two different positions in close proximity to the cyanoacrylic acid group of the system. The initial and corresponding optimized structures are outlined in Fig. 7(a and b). The electronic coupling and rate constants of electron transfer, hole transfer and charge recombination of the Li1–L1–TiO\(_2\) and Li2–L1–TiO\(_2\) systems are depicted in Fig. S1(a–f) (ESI†) and Fig. 8(a–f). The electronic coupling of electron transfer, hole transfer and charge recombination range from \( 3.20 \times 10^{-4} \) to \( 0.2376 \) and \( 8.0 \times 10^{-5} \) to \( 0.0453 \) and \( 8.38 \times 10^{-7} \) to \( 0.0677 \) eV for the Li1–L1–TiO\(_2\) system; and \( 1.50 \times 10^{-7} \) to \( 0.1026 \), \( 2.0 \times 10^{-5} \) to \( 0.0301 \) and \( 9.3 \times 10^{-4} \) to \( 0.4100 \) eV for Li2–L1–TiO\(_2\) system. These results show that an Li\(^+\) ion located close to the position of the proton in a protonated cyanoacrylic acid group of the dye, as expected, promotes electron transfer. The rate constants of electron transfer, hole transfer and charge recombination range from \( 1.3 \text{ fs}^{-1} \) to \( 0.7 \text{ ns}^{-1} \), \( 138.5 \text{ fs}^{-1} \) to \( 23.3 \text{ ns}^{-1} \) and \( 0.3 \text{ fs}^{-1} \) to \( 10.9 \text{ ps}^{-1} \) for the Li1–L1–TiO\(_2\) system, and \( 6.9 \text{ fs}^{-1} \) to \( 3.2 \text{ ns}^{-1} \), \( 503.2 \text{ fs}^{-1} \) to \( 58.5 \text{ ns}^{-1} \) and \( 1.1 \text{ fs}^{-1} \) to \( 0.2 \text{ ns}^{-1} \) for the Li2–L1–TiO\(_2\) system. This suggests that the electron transfer in the Li1–L1–TiO\(_2\) system is faster than that in the Li2–L1–TiO\(_2\) system, which in turn indicates that the position of an Li\(^+\) ion plays a significant role. Moreover, compared with the deprotonated L1–TiO\(_2\) system, the electronic coupling and rate constant of charge recombination are stronger/faster than those of observed for the Li1–L1–TiO\(_2\) and Li2–L1–TiO\(_2\) systems. In addition, the electronic coupling and rate constant of electron transfer and charge recombination for the Li1–L1–TiO\(_2\) and Li2–L1–TiO\(_2\) systems are close to those of observed in the protonated L1–TiO\(_2\) system. These results strongly indicate that added Li\(^+\) ions can show similar results as protons regarding the charge-transfer dynamics at the dye–TiO\(_2\) interface in DSSCs. In this context, it can be noted that lithium salts are typically added with concentrations of about 0.1 M, which should be sufficient for extensive interaction at the dye–TiO\(_2\) interface.

### 1.6 Solvation effect.

Here, we take the system of deprotonated L1–TiO\(_2\) as an example to demonstrate solvent effect on...
structural properties, electronic coupling and the rate constants of charge transfer. A Polarizable Continuum Model (PCM) was used to account for the solvent effects. The detailed analyses for solvent effect on structural properties are given in ESI.†

1.6.1 Solvent effects on electronic couplings of charge transfer. The electronic couplings of charge transfer reflect the strength of the frontier molecular orbital interaction between the donor L1 and the acceptor TiO2, and therefore provide information regarding the probability of charge transfer. The electronic couplings of electron transfer, hole transfer and charge recombination of the deprotonated L1–TiO2 model are outlined in Fig. 9(a–c) for both solvent and non-solvent conditions, which are represented by black and red curves, respectively. The electronic couplings of electron and hole hopping in acetonitrile are slightly smaller than those in gas phase. The electronic couplings of electron transfer for non-solvent and solvent conditions range from 0.0018–0.4880 and 0.0015–0.2975 eV, respectively, and the corresponding average values are 0.2515 and 0.1372 eV. The electronic couplings of hole transfer for non-solvent and solvent systems range from $10^{-5}$–0.0301 and $10^{-5}$–0.0058 eV, respectively, and the corresponding average values are 0.0107 and 0.0015 eV. However, the electronic couplings of charge recombination in acetonitrile presents dramatic decrease as compared with those in gas phase. The electronic couplings for non-solvent- and solvent-containing systems range from 0.4736–1.6985 and 0.0011–0.3895 eV, respectively. The corresponding average values are 1.152 and 0.1110 eV, respectively. The electronic couplings of charge recombination in non-solvent conditions are 10 times higher than those in solvent condition. This suggests that the presence of a reasonably dielectric solvent, such as acetonitrile, significantly can reduce charge recombination from TiO2 to deprotonated L1.

1.6.2 Solvent effects on the rate of charge transfer reactions. A higher DSSC PCE can be achieved by combining an ultrafast electron injection and a much slower charge-recombination process. Some papers report that acetonitrile is the best solvent for promoting the PCE of DSSCs.55,57 Thus, it is of special interest to investigate how the rate constant of charge transfer is affected by the presence of acetonitrile. The dynamics rate constants of electron transfer and charge recombination in the gas phase and implicit acetonitrile of the deprotonated L1–TiO2 model system are exhibited in Fig. 10(a–d). The ranges and averages of the rate constants are listed in Table 4. In gas phase, the rate constants of electron transfer and charge recombination for the deprotonated L1–TiO2 model system are ranging from $(0.1 \text{ ns})^{-1}$–$(0.3 \text{ fs})^{-1}$ and $(1.4 \text{ fs})^{-1}$–$(0.07 \text{ fs})^{-1}$, respectively. Inclusion of acetonitrile implicitly using the PCM model gives the rate constants of electron transfer and charge recombination for the deprotonated L1–TiO2 model system ranging from $(32.4 \text{ fs})^{-1}$–$(0.8 \text{ fs})^{-1}$ and $(30.3 \text{ ns})^{-1}$–$(1.3 \text{ fs})^{-1}$, respectively.

The average of the rate constants of electron transfer and charge recombination in gas phase are $(0.9 \text{ fs})^{-1}$, and $(0.1 \text{ fs})^{-1}$ respectively. While the average of the rate constants of electron transfer and charge recombination for the deprotonated L1–TiO2 model system range from $(2.4 \text{ fs})^{-1}$ and $(21.9 \text{ fs})^{-1}$, respectively in acetonitrile. From the above data, we can deduce that the rate constants of electron transfer are in the femtosecond time scale, irrespective if the system is in acetonitrile or in gas phase. The rate constants of charge recombination in gas phase are still in the femtosecond time scale. However, the rate constants of charge recombination are approximately two orders of magnitude lower in acetonitrile than in gas phase, which suggests that the solvent acetonitrile plays an important role in retarding the charge recombination loss rates. This indicates that a solvent such as acetonitrile promotes higher PCEs of DSSCs, which is in accord with the results of Fang et al.54,55

Table 4 The rate constants of electron transfer and charge recombination for the deprotonated L1–TiO2 model system with and without considering PCM solvent (acetonitrile) effects

| Rate constants | Non-solvent (a) | Solvent (b) |
|----------------|----------------|-------------|
| $et$           | $(0.1 \text{ ns})^{-1}$–$(0.3 \text{ fs})^{-1}$ | $(32.4 \text{ fs})^{-1}$–$(0.8 \text{ fs})^{-1}$ |
| Average        | $(0.9 \text{ fs})^{-1}$              | $(2.4 \text{ fs})^{-1}$              |
| $rec$          | $(1.4 \text{ fs})^{-1}$–$(0.07 \text{ fs})^{-1}$ | $(30.3 \text{ ns})^{-1}$–$(1.3 \text{ fs})^{-1}$ |
| Average        | $(0.6 \text{ fs})^{-1}$              | $(21.9 \text{ fs})^{-1}$              |

*a Denote the rate constants of electron transfer and recombination, respectively.
2 Analysis of the correlation between dye configuration and electronic coupling

The current dynamical study also allows a study of the correlation between specific dye configurations and the rate constants of charge-transfer obtained. Fig. 11 shows the analyzed structures. The effects specifically studied involve hydrogen bonding between one oxygen atom of TiO$_2$ and the O–H of the cyanoacrylic acid group of the dyes, the Ti–O bond lengths, the O–O distances, the O–Ti–O angle distributions and C–O–Ti–O dihedral angles, Φ S–C–C–C and Ψ C–C–C–C. The structural analyses for the aiMD simulation using 1.0 fs time steps are given in the ESI†. If the relation between structural properties and electronic coupling/transfer rate constant is qualitative, we will not be able to identify a cause-effect correlation between the snapshot structures and the electronic coupling from the correlation with a resolution of 0.1 ps in the aiMD simulation. In addition, the aiMD simulation of the protonated L1–TiO$_2$ system was also evaluated in a 0.5 ps steady-state region and 100 snapshots were extracted to render a higher time resolution for comparison, as shown in Fig. S11(a–c) and S12(a–g) (ESI†). The correlation between dye conformation and electronic coupling/charge-transfer rate constants were explored for 20 continuous snapshots, listed in Table S4 (ESI†). However, we cannot identify any clear correlation. Consequently, there are no simple structural-rate constant correlation to be extracted from the dynamical results. Instead, the high/low rate constants of charge transfer detected seem to result from complex concerted structures of the dyes studied. We had expected to note a correlation with the dye–TiO$_2$ distance, but taking the full dye structure dynamics into account any such correlation downs in the structural overall effects. For this reason, the correlations linked to the dye–TiO$_2$ distance is studied explicitly below.

3 Scanning of Ti–O(dye) distance and charge-transfer rates

In order to study the effect of the Ti–O(dye) distance on the electronic coupling and rate constant of charge transfer, a fixed scan of Ti–O(dye) distance from 1.67 to 3.67 Å for the deprotonated L1–TiO$_2$ system was performed. The corresponding electronic coupling and rate constant of charge transfer are depicted in Fig. 12(a–f). The electronic coupling and rate constants of electron transfer, hole transfer and charge recombination present a steep decrease with increasing Ti–O(dye) distance from 1.67 to 2.47 Å. For Ti–O(dye) distances longer than 2.50 Å, the curves of the electronic coupling and rate constant of charge transfer flatten out. This suggests, as expected that when the Ti–O(dye) distance increases, the frontier orbital interactions get weaker. Thus, the corresponding electronic coupling of charge transfer gets weaker and the corresponding rate constants of charge transfer decrease. An exponential relation is found for the relationship between Ti–O(dye) distance and electronic coupling or rate constants of electron transfer and charge recombination. This indicated that straightforward orbital overlap may be involved. There also exists an exponential relation between Ti–O distance from 1.67 to 2.27 Å and the electronic coupling/rate constant of hole transfer. However, when the Ti–O distance is longer than 2.30 Å, the curves of electronic coupling and rate constant of hole transfer reach the plateau region, which suggests that the overlap of the HOMO of deprotonated L1 and LUMO of the TiO$_2$ are very small. All the relations are shown in Fig. S13(a–f) (ESI†). The current results are in contrast to the results in the preceding section, where it seems that full structural flexibility will dominate both changes in energetics as well as in simple correlations.

4 Statically optimized structures and charge-transfer rates

For sake of comparison, an analysis of the electronic coupling and charge-transfer rate constants were also performed for systems statically optimized in the protonated and deprotonated L1–TiO$_2$, D35–TiO$_2$, and LEG4–TiO$_2$, as listed in Table 5. All electronic couplings are in the range of the corresponding electronic coupling as obtained from the aiMD simulation snapshots. Most of the rate constants of electron transfer and
charge recombination are on femtosecond time scale and few of them are on picosecond and nanosecond time scale, which all are within the range of the rates of electron transfer and charge recombination yielded by aiMD snapshots. Moreover, the rate constant of electron transfer of the protonated D35–TiO2 system is higher than those of the protonated L1–TiO2 and LEG4–TiO2 systems anchored to a TiO2 surface significantly affects the orbital features. The current study has employed aiMD simulations for the study of the interaction between three organic dyes, L1, D35 and LEG4, with a model of a TiO2 semiconductor substrate. Instead of a static approach, where the systems are geometrically optimized followed by an analysis of electronic coupling, the systems have been dynamically traced and structural snapshots have been extracted for the subsequent analysis of electronic coupling and rate constants of charge transfer when compared to the snapshots generated from aiMD simulations. It is difficult to identify the arguments for why the geometrically optimized structures should provide unique and reliable results.

Conclusions

The current study has employed aiMD simulations for the study of the interaction between three organic dyes, L1, D35 and LEG4, with a model of a TiO2 semiconductor substrate. Instead of a static approach, where the systems are geometrically optimized followed by an analysis of electronic coupling, the systems have been dynamically traced and structural snapshots have been extracted for the subsequent analysis of electronic coupling and rate constants of charge transfer. This dynamic approach has allowed us to identify several previously unknown features.

Generally, the structural dynamics of a dye adsorbed/anchored to a TiO2 surface significantly affects the orbital overlap and all resulting properties in the systems. More specifically, electron coupling and rate constants of charge transfer for central processes in DSSC devices cover a huge range. The most relevant data to compare with experiment will be averages sampled over a relevantly large time of simulation. A comparison with a static evaluation of the same parameters indicate that the values obtained from such an analysis risk to be arbitrarily placed in the window of rate constants defined by a dynamic approach. Our results indicate that a proper analysis of electronic coupling and rate constants of transfer need to invoke the structural dynamics in order to offer statistical results that can be compared with experiment, where the results by necessity represent averages over time and space.

More specifically, the results of the dynamic analysis of electronic coupling and rate constants of charge transfer also offer some new and unexpected insights. First, recombination loss rate constants of deprotonated dyes attached to the TiO2 model are one or two order of magnitude higher than those of electron injection. This shows that high photocurrents will need to rely on fast transport rates away from the dye interface in the TiO2 substrate. Second, it is clear that this potential problem at least partly can be mitigated by salts of polarizing cations added to the electrolyte. Finally, a dielectric solvent, such as acetonitrile, can favour higher PCEs of DSSCs by retarding recombination loss rates. All the charge-transfer processes studied are quite fast and in accordance with experiment.

There is no simple correlation identified between high or low transfer rate constants and specific structural arrangements in terms of atom–atom distances, angles or dihedral arrangements of the dye sub-units. However, a scan of the Ti–O(dye) distance alone suggests that an exponential relation exists between the Ti–O(dye) distance and the electronic coupling/rate constants of charge transfer, which suggests that the Ti–O(dye) distance does play a significant role for the electronic coupling between the dye and the substrate, although its overall effect drowns in the concerted structural dynamics of the system as a whole.

Conflicts of interest

There are no conflicts to declare.

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Table 5 The rate constants (lifetime) and electronic couplings of the optimized protonated and deprotonated L1–TiO2, D35–TiO2 and LEG4–TiO2 systems

|        | L1–TiO2 | D35–TiO2 | LEG4–TiO2 |
|--------|---------|----------|-----------|
| **ec** | p       | dep      | p         | dep      |
| **et** | 0.0103  | 0.0339   | 0.2768    | 0.1456   |
| **ht** | 0.0004  | 0.0001   | 0.0003    | 0.0034   |
| **cr** | 0.0109  | 1.4260   | 0.1370    | 1.0185   |
| **Rate constants** |         |          |           |          |
| **et** | 1.9 ps  | 51.4 fs  | 6.4 fs    | 4.1 fs   |
| **ht** | 380.4 ps| 100 ns   | 775.8 ps  | 615.4 ps |
| **cr** | 0.5 ps  | 0.1 fs   | 4.2 fs    | 1.3 fs   |

Table 5 cont.

|        | L1–TiO2 | D35–TiO2 | LEG4–TiO2 |
|--------|---------|----------|-----------|
| **ec** | p       | dep      | p         | dep      |
| **et** | 0.0103  | 0.0339   | 0.2768    | 0.1456   |
| **ht** | 0.0004  | 0.0001   | 0.0003    | 0.0034   |
| **cr** | 0.0109  | 1.4260   | 0.1370    | 1.0185   |
| **Rate constants** |         |          |           |          |
| **et** | 1.9 ps  | 51.4 fs  | 6.4 fs    | 4.1 fs   |
| **ht** | 380.4 ps| 100 ns   | 775.8 ps  | 615.4 ps |
| **cr** | 0.5 ps  | 0.1 fs   | 4.2 fs    | 1.3 fs   |

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