Hydrogen atoms can be located accurately and precisely by x-ray crystallography

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Precise and accurate structural information on hydrogen atoms is crucial to the study of energies of interactions important for crystal engineering, materials science, medicine, and pharmacy, and to the estimation of physical and chemical properties in solids. However, hydrogen atoms only scatter x-radiation weakly, so x-rays have not been used routinely to locate them accurately. Textbooks and teaching classes still emphasize that hydrogen atoms cannot be located with x-rays close to heavy elements; instead, neutron diffraction is needed. We show that, contrary to widespread expectation, hydrogen atoms can be located very accurately using x-ray diffraction, yielding bond lengths involving hydrogen atoms (A–H) that are in agreement with results from neutron diffraction mostly within a single standard deviation. The precision of the determination is also comparable between x-ray and neutron diffraction results. This has been achieved at resolutions as low as 0.8 Å using Hirshfeld atom refinement (HAR). We have applied HAR to 81 crystal structures of organic molecules and compared the A–H bond lengths with those from neutron measurements for A–H bonds sorted into bonds of the same class. We further show in a selection of inorganic compounds that hydrogen atoms can be located in bridging positions and close to heavy transition metals accurately and precisely. We anticipate that, in the future, conventional x-radiation sources at in-house diffractometers can be used routinely for locating hydrogen atoms in small molecules accurately instead of large-scale facilities such as spallation sources or nuclear reactors.

INTRODUCTION

The role of hydrogen in chemistry cannot be understated. The hydrogen atom commonly terminates the valences of other atoms and thus is a major constituent of the molecular surface. The hydrogen ion concentration (pH) is a control variable for chemical reactions, and H atoms play a key role in biology and medicine (1–3), with increased interest in determining their positions with x-radiation (4). In materials science, some argue that, to mitigate the consequences of human-induced climate change, hydrogen storage materials must play a key role (5).

Unfortunately, the very reason that makes H atoms so central in chemistry—the fact that they have only one electron—makes them very hard to detect with x-rays accurately because x-rays scatter from the electron density (6, 7). On the other hand, thermal neutrons diffract strongly from the nuclei of H atoms, which makes them detectable by using nuclear reactors or spallation facilities as radiation sources. However, the cost of a neutron diffraction facility is immense, the perceived risk of operating a nuclear reactor is not negligible, and the accessibility for researchers is limited. In contrast, operating an x-ray diffractometer is routine, and far more than a million structures solved by x-ray diffraction have been published.

It has been known for some time that H atoms in small molecules can, in principle, be located by x-rays (that is, refined freely without constraints or restraints), provided that high-quality and high-resolution low-temperature data are available (8, 9). This requires a change in the standard molecular and atomic model away from the 100-year-old independent atom model (IAM) (10)—a superposition of spherical atomic electron densities—that has implemented the Stewart-Davidson-Simpson (SDS) scattering factor for the hydrogen atom (11). Instead, fixed bonded-atom polarized scattering factors for the hydrogen atom were introduced by Stewart et al. (12, 13) but only seldomly applied (14, 15). An extension of this idea is based on aspherical atomic electron densities in the Hansen-Coppens pseudoatom formalism [multipole modeling (16)] using databases (17–19). However, these database methods are regarded as specialist techniques. A new technique called Hirshfeld atom refinement (HAR) (20, 21) is available and can be applied as easily as the IAM. It provides improved tailor-made aspherical atomic electron densities, which are extracted from a crystal-field–embedded quantum-chemical electron density using Hirshfeld’s scheme (22) (see Fig. 1). In preliminary work, it was indeed possible for two organic molecules to freely refine H atom positions and the corresponding anisotropic displacement parameters (ADPs) using x-ray diffraction and the HAR technique (21, 23), but neither accuracy and precision nor general applicability had been investigated.

The recent work and a strong interest in H atoms alluded to the question: Is it possible to obtain H atom positions and associated bond lengths accurately and precisely from routine x-ray diffraction data?

To answer this question, we refined a total of 81 crystal structures of small organic molecules from the literature using HAR and compared the obtained A–H bond lengths with averaged results obtained with neutron diffraction (24). According to Allen and Bruno (24), the A–H bonds occurring in the 81 selected crystal structures can be categorized into four different classes, comprising various types of C–H, O–H, and N–H bonds, plus O–H in crystal water that we considered additionally. The main selection criteria used to source the x-ray data were that they could, in principle, be obtained in a normally equipped x-ray diffraction laboratory; that the temperature was below 140 K, and that the resolution was at least 0.6 Å. Full details can be found in Materials and Methods as well as in the Supplementary Materials.
RESULTS

In Fig. 2, we present statistical analyses of the comparisons of A–H bond lengths between x-ray diffraction (HAR and IAM) and neutron diffraction derived values. All HAR results come from a fully anisotropic model for all atomic displacements, including hydrogen atom ADPs, which is impossible in the IAM. Details of the statistics applied are described in Materials and Methods. There is remarkably good agreement between the averaged bond lengths from HAR and neutron refinements in Fig. 2. The differences between the means are always less than two HAR sample SDs, and smaller than one HAR sample SD for all bond types with at least 30 representatives in the x-ray sample (see the right-hand column in Fig. 2 for the sample number). This agreement represents a fundamental improvement in the results obtained from the routinely used IAM (also shown in Fig. 2). Mean bond lengths from IAM deviate significantly from the accurate HAR and neutron results.

Despite these encouraging results, the two-sided Welch test (27) shows that, for most bond types, the mean bond lengths from HAR and neutron diffraction are not equal within a 95% confidence interval. In almost all cases, the HAR values are systematically smaller, and the difference between the individual means is, on average, between 0.01 and 0.02 Å. Therefore, the one-sided Welch test (27) was applied to further investigate the cases in which the hypothesis of equality of neutron and HAR means was rejected. At a 5% significance level, the differences between neutron and HAR means exceed the confidence interval by 0.001 to 0.020 Å; however, this deviation is within a single SD for each bond type and refinement strategy. This means that, if the averaged bond lengths agree within 0.020 Å, then statistical equivalence would be achieved. Hence, the actual achieved agreement of 0.01 to 0.02 Å is within the value for strict statistical agreement. This level of agreement can be understood as a measure of the accuracy of the HAR procedure if the results from neutron diffraction are considered as the...
classes resolution (those obtained from x-ray diffraction (HAR and IAM models) at restricted sample standard deviations (SDs) obtained from neutron diffraction versus comparisons between HAR and multipole modeling in a forthcoming study.

A total number of 0.01 to 0.02 Å was not reached. We will present more detailed comparisons between HAR and IAM-derived bond lengths, but an agreement on some selected examples agree more closely derived bond lengths on some selected examples agree more closely with the neutron results than IAM-derived bond lengths, but an agreement of 0.01 to 0.02 Å was not reached. We will present more detailed comparisons between HAR and multipole modeling in a forthcoming study.

Sample standard deviations (SDs) (error bars in Fig. 2) can be used as a measure of the precision of determining the A–H bond lengths within each bond class. Again, this is an approximation to precision because the spread of the values can be influenced by actual chemical effects, such as intermolecular interactions, or physical effects caused by, for example, difference in the temperature of measurements. Nevertheless, Fig. 2 shows in this context that the results from neutron diffraction are only slightly more precise than the HAR results, with the SDs always being in the same order of magnitude. This finding is contrary to the intuition that neutron diffraction experiments provide significantly more precise H atom parameters. The results from IAM treatment are clearly less precise as well as less accurate. The case of the O–H bonds in cocrystallized water is exceptional (last row in Fig. 2): The spread of values can be reduced drastically for water, which is prone to be involved in hydrogen bonds, by using a different refinement method, namely, HAR applied to x-ray data and not neutron diffraction. Therefore, only part of the spread can be caused by chemical features, and the difference in the SD shows that HAR is notably more precise than neutron diffraction for water.

To test the effect of resolution on the A–H bond lengths, we performed refinements at the respective maximum resolution of each data set and at resolutions of 0.6, 0.7, and 0.8 Å. Figure 2 summarizes the results for the highest (max) and lowest (0.8 Å) resolutions. The accuracy and precision of hydrogen atom positions obtained for the lowest resolution are as good as those obtained for the maximum resolution. Although the fact that all evaluated compounds scattered to at least 0.6 Å in the measurement means that our selection does not represent the average routine data set for structure determination that might only be resolved to a maximum of 0.8 Å, successful reflation of every data set pruned to 0.8 Å is a significant result. It renders it possible, in the future, to routinely apply HAR to data sets for standard small-molecule structure elucidation.

Only for organic compounds are there enough available equivalent neutron and x-ray data sets to perform meaningful statistical analyses. For A–H bonds in inorganic compounds, only a proof of principle for selected compounds of interest can be presented herein, including bridging H atoms and H atoms bonded to heavy transition metals (Table 1). A significant elongation of all A–H bonds between HAR and IAM treatments is observed, which means improved accuracy relative to the reference values accompanied by significant improvement in precision. For elements up to argon, HAR is as easy as for organic compounds, whereas HAR treatments with heavier elements can fail because they are technically not simple and beyond routine applicability at present. This includes problems with the availability of suitable all-electron basis sets for atoms beyond period 4 and related issues with obtaining a robust electron density for these systems, as well as problems with the availability of good-quality x-ray data sets that provide starting positions for hydrogen atoms bonded to heavy elements. However, Table 1 and Fig. 1D show that the method is, in principle, able to locate H atoms accurately and precisely next to transition metals as heavy as ruthenium and platinum, which are both known to be potent catalysts for hydrogen activation (28).

The total number of individual hydrogen ADPs in all the structures subjected to HAR amounted to 1001, and 94 to 99% of them (depending on the applied resolution cutoff) belonged to successfully refined data sets. Therefore, hydrogen ADPs can generally be refined to convergence. The A–H bond lengths determined from anisotropic refinements are in slightly better agreement with the neutron-derived A–H results than those from isotropic refinements for the resolution 0.8 Å (by 0.003 Å), whereas for all the other resolution ranges, there is no difference (see tables S1 to S66 in the extended supplementary document "Raw refinement and
 statistical data”). This is true even if the quality of the hydrogen ADPs (judged by visual inspection) is poor in some cases. Obliqueness and oblateness of hydrogen ADPs occur much more frequently after anisotropic HAR than, for example, after modeling via transfer from neutron-based data as implemented in the SHADE method (30). However, contrary to all other methods (31, 32), in HAR the ADPs are obtained only from information derived from the x-ray data for the particular compound.

For an independent check and a quantification of the quality of the hydrogen ADPs, we used the checkCIF service normally used for quality control when submitting crystal structures for publication (http://checkcif.iucr.org), which emits “alerts” (labeled A, B, and C) of successively decreasing severity. The specific meaning of the alerts in terms of ellipsoid dimensions and the detailed analysis of the hydrogen ADPs for each structure can be found in the extended supplementary document “Raw refinement and statistical data” (tables S67 to S70). For example, nonpositive definite ADPs are reported as alert A if found in the main molecule. The percentage of hydrogen ADPs causing the most serious alert A is at 4% for the maximum and 0.6-Å resolutions and grows with further decreasing resolution, attaining 5% at 0.7 Å and 9% at 0.8 Å. The fraction of alert B and alert C ADPs, which are unlikely to signify major refinement problems, remains constant for different resolutions and amounts to approximately 1 to 2% and 5 to 6%, respectively.

**DISCUSSION**

HAR is carried out with the free software Tonto (33) [HARt (HAR terminal) subprogram, http://github.com/dylan-jayatilaka/tonto], which has recently been incorporated into the free crystallographic program Olex2 (34) (www.olexsys.org). HAR treatments amount to several hours for small organic compounds to several days for bigger molecules on current single-processor desktop workstations. We do not expect this to be a serious problem in the near future because the availability of many-processor computing is becoming ubiquitous. Here, a refinement was considered successful if the least-squares procedure was convergent and the molecular structure was conserved. Among all performed refinements (different resolution, different hydrogen atom treatment), 97% of the refinements were successful. Ultimately, 75 of 81 data sets (93%) could be refined successfully. Ultimately, 75 of 81 data sets (93%) could be refined successfully. Additionally, 97% of the refinements were successful. Ultimately, 75 of 81 data sets (93%) could be refined successfully.

### Table 1. A–H bond lengths in inorganic compounds (terminal and bridging)

| Compound                  | Bond Type  | IAM      | HAR     | Reference |
|---------------------------|------------|----------|---------|-----------|
| Diborane (25) (see Fig. 1)| B–H bridging | 1.229(5) and 1.248(5) | 1.296(6) and 1.296(6) | [1.339(6) and 1.339(6)] |
|                           | B–H terminal | 1.052(6) and 1.053(6) | 1.170(7) and 1.168(6) | [1.196(8) and 1.196(8)] |
| BHPCU12 (26) (see Fig. 1) | B–H bridging | 1.186(18) | 1.264(7) | N/A       |
|                           | B–H terminal | 1.093(17) | 1.209(7) | N/A       |
|                           | Cu–H bridging | 1.802(18) | 1.809(7) | N/A       |
| Pentaphenyldisiloxane     | Si–H       | 1.391(12) | 1.482(9) | [1.481(5), 1.506(2)] |
| QOSZON                   | Fe–H       | 1.421(21) | 1.414(8) | 1.521(2)  |
| AGOZEC                   | Fe–H       | 1.442(22) | 1.531(9) | 1.529(2)  |
| METRAF                   | Ru–H       | 1.589(15) | 1.707(18) | [1.694(71)] |
|                           | Pt–H       | 1.601(43) | 1.686(4) | [1.610]**  |

The main molecule. The percentage of hydrogen ADPs causing the most serious alert A is at 4% for the maximum and 0.6-Å resolutions and grows with further decreasing resolution, attaining 5% at 0.7 Å and 9% at 0.8 Å. The fraction of alert B and alert C ADPs, which are unlikely to signify major refinement problems, remains constant for different resolutions and amounts to approximately 1 to 2% and 5 to 6%, respectively.

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Application of HAR to network structures, disordered compounds, or molecular biology is not yet possible. Moreover, apart from code optimizations within HAR, improvements in measurement techniques and better accuracy of data collection and reduction are necessary. However, this study shows that HAR is easily accessible and successful. It can be performed from now on as the last step of most small-molecule crystal structure determinations, which is of huge interest for every scientist using x-ray crystallography as an analytical tool because it will yield H atom positions that are as accurate and precise as those derived from neutron diffraction experiments. Accurately and precisely locating all the atomic positions, but especially those of hydrogen atoms, is more crucial as a starting point for electron density or x-ray wave-
function refinements that give access to properties that cannot be generally obtained from traditional crystallographic refinements, such as energies of interactions. We therefore believe that HAR is one of the central milestones in the evolving field of quantum crystallography.

**MATERIALS AND METHODS**

**Experimental design**

Eighty-one data sets of organic compounds were selected from various sources and subjected to HAR. The selection was restricted by the following conditions:

1. Only published data sets. Details, CCDC REFCODES, and assignment to references ([14, 21, 23, 32, 46–92]) are given in table S1.
2. Only x-ray data sets of at least $d = 0.6 \, \text{Å}$, to test the effect of resolution.
3. Temperature of experiment not higher than 140 K.
4. Purely organic compounds with no metal ions.
5. Absence of disorder (except water molecules with fractional occupancy in the structures).
6. No anharmonic motion reported.
7. Only data available in *Acta Crystallographica* journals.

With the above restrictions 1–7, we found 60 data sets. The earliest data were from 1988. Because the location of H atoms is particularly important for biology, we selected some additional data (not always in *Acta Crystallographica*): four amino acids, one dipeptide, six tripeptides, benzene, sucrose, and urea. Because they were used in a recent detailed study of HAR, we also included data for the dipeptide Gly-L-Ala with a slightly lower resolution of 0.657 Å.

Some crystal structures appeared multiple times. For those, the bond lengths used in the analysis were the weighted averages with corresponding weighted SDs. Three of them contained two molecules of the main compound per asymmetric unit (so-called $Z = 2$ structures). In further 23 structures, a solvent molecule (mostly water) was also present. The only atoms appearing other than C, N, O, and H were S (six compounds), P (two compounds), F (one compound), and Cl (four compounds). No H atoms bonded to S or P were present.

Full details of the compounds with relevant information (source for the list of measured reflection data, structure, literature references, HAR details, and previous high-resolution refinement details) are presented in table S1 and in the extended supplementary document “Raw refinement and statistical data” (including representations of the HAR-refined geometries with anisotropic atomic displacement ellipsoids), which has been deposited at www.figshare.com and can be obtained under https://dx.doi.org/10.6084/m9.figshare.3205588.v1.

The inorganic compounds were selected to include hydrogen atoms in quite different environments: bonded to second- to sixth-row elements, in bridging and terminal positions. The data for diborane stemming from a charge-density study (25) were made available by C. B. Hübschle (University of Bayreuth). We measured data for pentaphenyldisiloxane at beamline D3 of storage ring DORIS III at the HASYLAB (Hamburger Synchrotronstrahlungslabor) of DESY (Deutsches Elektronen-Synchrotron) in Hamburg [triclinic $P\bar{T}$, $Z = 2$, $a = 9.110(2) \, \text{Å}$, $b = 10.543(2) \, \text{Å}$, $c = 13.597(3) \, \text{Å}$, $\alpha = 94.30(3)^\circ$, $\beta = 106.90(3)^\circ$, $\gamma = 92.96(3)^\circ$, $V = 1242.3(5) \, \text{Å}^3$; $T = (8+1) \, \text{K}$, $\lambda = 0.5166(2) \, \text{Å}$, $d_{\text{max}} = 0.45 \, \text{Å}$; number of collected reflections = 273,011; number of unique reflections = 25,392; completeness of data = 89.2%; $R_{\text{int}} = 0.063$]. More details will be reported in a forthcoming study. Data for further inorganic compounds were retrieved from *Acta Crystallographica* publications (unless otherwise stated) and subjected to HAR: (tetrahydroborato)bis(triphenylphosphine) copper(I) (REFCODE: BHPTCU12) (26), [1,1-bis(diphenylphosphino)ferrocene]-carbonyl[dihydroboros(pyrazol-1-yl)-borato]hydridoruthenium(II) acetone solvate (REFCODE: AGOZEC) (35), dicarbonyl-cis-dihydrodiborato trans-bis(triphenylphosphine-O)-iron(II) (REFCODE: QOSZON; data made available by V. Arion, University of Vienna) (36), and trans-bromohydridobis(triphenylphosphine)-platinum(II) (REFCODE: METRAF) (37).

**Hirshfeld atom refinement**

The HAR method of crystallographic structural refinement uses aspherical atomic scattering factors obtained from the quantum-mechanical electron density of a molecule in a simulated crystal environment. This requires only single-molecule calculations. Full details have been published elsewhere (20, 21). For most of the structures, refinement was performed starting from the initial geometry obtained from the literature. For calculations of molecular wave functions in HAR, the central moiety was embedded in a cluster of charges and dipoles on all atoms on all surrounding molecules with at least one atom within the radius of 8 Å. The wave function was calculated using density functional theory (38) with the Becke-Lee-Yang-Parr functional (39, 40). The correlation-consistent polarized valence double-$\zeta$ (cc-pVDZ) basis set (41) was chosen for the unconstrained refinement of hydrogen positions in crystals because it was previously shown to be sufficient (21). The refinement was performed on structure factor magnitudes ($F$) using only the reflections with $F > 4\sigma(F)$. Coordinates of all the atoms, including hydrogen atoms, were freely refined. ADPs of all nonhydrogen atoms were always refined, whereas, as far as hydrogen atoms are concerned, two versions of each refinement were carried out—with anisotropic and isotropic treatment of hydrogen displacement parameters. In contrast to other programs for structure refinement, in the program HArT, the unique $U_{\text{iso}}$ value is not explicitly refined as a separate parameter but obtained by removing linear combinations of redundant parameters in the least-squares matrix. Therefore, in nonorthogonal crystal systems, the isotropic displacement parameter is not diagonal; compare Eq. 44 in Trueblood et al. (42). Furthermore, for each organic compound, the refinement was performed on four sets of reflections: for the maximum resolution (different for various structures) and for three resolution cutoffs: 0.6, 0.7, and 0.8 Å. For the inorganic compounds, only the maximum resolution was used. Instead of the cc-pVDZ basis set, DZP according to Barros (43) was used for Ru and DZP according to de Berredo and Jorge (44) was used for Pt. Crystallographic information files (CIFs) for all refinements are deposited with this article as supplementary information. The isotropic refinement at maximum resolution for each compound has been submitted as CIF to the CSD (see table S1 for the deposition numbers) and can be obtained free of charge at www.ccdc.cam.ac.uk. A CIF including the anisotropic refinement of diborane was deposited with the Inorganic Crystal Structure Database (deposition no. CSD-430202) and can be obtained at http://icsd.fiz-karlsruhe.de.

**Statistical analysis**

A–H bonds (C–H, O–H, and N–H bonds) present in the refined crystal structures of the organic compounds were grouped into bond types...
identified in the course of a similar analysis performed for neutron A–H bonds by Allen and Bruno (24). Their work gives access only to the values of the averaged neutron bond lengths, their sample SDs, and the numbers of observations in the sample, without revealing the values of individual observations. For this reason and also because of the very limited number of crystalline structures for which both neutron and x-ray experimental data are available, only a comparison between averaged neutron and averaged x-ray A–H bond lengths can be done, if the condition of a statistically meaningful number of bonds representing each bond type is to be fulfilled. In the article by Allen and Bruno (24), two different classes of bond types were defined—a class containing only eight general bond types detailed in table 4 of the cited article [Z\^2–Csp^\circ\circ–H, Z^2–Csp^\circ\circ\circ–H\circ\circ\circ, Z–Csp^\circ\circ–H^\circ\circ, Csp^\circ\circ^\circ–H, Z–O–H, Z–N–H, and N^\circ–H], where Z stands for any element except H and C(ar) denotes aromatic carbon; otherwise, hybridization of carbon is given in italics] and a class containing more specific bond types collected in their table 2, 24 of which were identified in the analyzed data sets. In the case of table 4, the values from columns containing averages based on experimental results from the temperature ranges T ≤ 60 K and 60 ≤ T ≤ 140 K were merged for comparison with the corresponding x-ray HAR averages. For each bond type, a statistically significant number of observations higher than 50 was achieved for the x-ray data, enabling a reliable comparison between x-ray and neutron bond lengths. This was not the case for the 24 bond types identified according to table 2, for half of which the number of representatives in the x-ray HAR statistic was smaller than 30 and for which four types were substantially underrepresented in the neutron results. For those bond types, only a rough comparison can be made, allowing, however, to gain certain insight into the performance of HAR for H atoms in more specific chemical groups. Additionally, the O–H bond in cocrystallized water molecules is included in the study. In this case, a suitable statistic was performed on the basis of water-containing molecular neutron structures deposited with the CSD, according to the guidelines described in the work of Allen and Bruno (24).

The comparison of the neutron and x-ray HAR A–H bond lengths was based on the averaged values obtained for the defined bond types and their sample SDs. For the HAR bond lengths, the performed Shapiro-Wilk test (45) proved that, in many cases, the assumption of normality is not fulfilled. For the neutron bond lengths, only averaged values and SDs were available; thus, neither testing of the data for normality nor performance of nonparametric statistical tests was possible. Therefore, the final choice for testing the equality of neutron and x-ray HAR mean bond lengths was Welch’s t test (27); it is used to compare two samples with unequal variances and is suitable if the means of the samples are approximately normally distributed. According to the central limit theorem, the means of a sample with finite variance converge to the normal distribution, with the sample size approaching infinity, irrespective of the actual distribution of the population. It is customary to assume that, for sufficiently large samples (that is, at least 30 observations), the distribution of their means is approximately normal. This assumption is valid for all the bond types in fig. S1 (C and D) and for half of the bond types in Fig. 1 as well as fig. S1 (A and B). For the remaining bond types, the results of the Welch test are only approximations and are presented here to give a general view of the performance of the method in more scarcely encountered bond types. The two-sided Welch test (assumed significance level of 5%) was used to decide on the equality of the neutron and x-ray HAR means. In those cases in which the hypothesis on equality was rejected, the biggest possible difference between x-ray and neutron means was calculated (from the one-sided Welch test) so that the two means would agree at the same significance level. The results can be found in the extended supplementary document “Raw refinement and statistical data” (tables S1 to S66).

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