Simulation of Electrical Characteristics of Switching Nanostructures "Pt – TiO – Pt" and "Pt – NiO – Pt" with Memory

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Submitted January 1, 2019 / Accepted September 26, 2019

Abstract. The nanostructures “Pt – TiO – Pt” and “Pt – NiO – Pt” with weak switching properties and memory were studied within the framework of semi-empirical Hückel method. The calculation was implemented in the program Atomistix ToolKit with Virtual NanoLab. The transmission spectra, current-voltage characteristics and differential conductivity of nanostructures are calculated. It was revealed that in the range of voltages –1.3 V÷1.3 V, a hysteresis appears in the form of eight shaped figure on the current-voltage characteristic of Pt – TiO – Pt nanostructure, and in Pt – NiO – Pt nanostructure, the hysteresis appears in the voltage intervals –1.8 V÷0.8 V and 0.9 V÷1.8 V in the form of two oval-shaped figures connected to a segment. The manifestation of the hysteresis characteristic of these nanocontacts shows that they have memory. It was found that a negative differential resistance is observed in the voltage range, where the hysteresis of the current-voltage characteristic is appeared. It is shown that the investigating nanostructures have weak switching properties. The results of the paper can be useful for the calculation of memristic elements of nanoelectronics.

Keywords

Memristor, nanostructure, electron transport, current-voltage characteristic, differential conductivity, transmission function (spectrum)

1. Introduction

At the end of 2008, the discovery of the effect of memrisivity in systems Pt – TiO2 – Ti2O3 – Pt, predicted back in 1971 by L. Chua, became a turning point in microelectronics [1–3]. It became clear that the effect of memrisivity arises in metal-dielectric nanocomposites due to the displacement of charges in a superthin dielectric layer when an electric field is applied. Increased interest in such nanostructures is associated with their use to create a new passive element of the electrical circuit – a memristor – a resistor with controlled resistance. Currently, the creation of switches, memory elements, constituent logic elements, oscillators, as well as modules of neural computers is being considered on the basis of memorial constructions [4–8]. In this regard, there is an intensive search for new metal-dielectric materials with memristic properties, as well as new models, describing their electrical characteristics [9], [10]. Various methods and modeling tools, such as SPICE (LTspice, Multisim and others), FEKO, Matlab, Verilog-A and others [11–15] have been developed to describe the memorial properties of various metal-dielectric materials.

In this paper, an attempt has been made to determine the main electrical characteristics of nanostructures of the type “Pt – TiO – Pt” and “Pt – NiO – Pt” using the extended Hückel method [16].

2. Description of the Object and Methods of Research

The geometry of the studied nanocontacts is shown in Fig. 1, 2 (a), (b). The nanosystems under consideration consist of 306 atoms and have three regions with a total size ~50 Å: central region, left and right electrode areas. In the central region of Pt – TiO – Pt the active part of the nanodevice in the form of an oxide fragment of titanium consisting of 90 atoms is located, and in Pt – NiO – Pt there is nickel oxide consisting of 54 atoms, where the scattering of quasiparticles occurs in a region with a length of ~8.78 Å and ~3.98 Å, respectively. Electrodes are obtained by expanding the central region along the C axis by ~5.732 Å and ~8.6 Å. The distances between electrodes are ~33.24 Å (Pt – TiO – Pt) and ~34.6 Å (Pt – NiO – Pt), where the central region of the nanosystem is located.

Usually, optimization of such structures is well implemented using the ReaxFF potential (ReaxFF is Reactive Force Field), which is used to describe reactive processes [17]. In our case, the optimization of the nanostructures Pt – TiO – Pt is realized using the potential ReaxFF.CHONSiPtZrYBaTi.2013 [18], and of the nano-
structures Pt – NiO – Pt by ReaxFF_CHONSFPt-CNi_2010 [19]. At optimization of Pt – TiO – Pt structure the distance between atoms takes the following values: Pt – Pt – ~2.482 Å; Ti – Ti – ~2.866 Å; Pt – O – ~2.2 Å; Ti – O – ~2.195 Å; Pt – Ti – ~2.99 Å. In the optimized structure of Pt – NiO – Pt nanocontact, the interatomic distances take the following values: Pt – Pt – ~2.58 Å; Ni – Ni – ~2.85 Å; O – O – ~2.81 Å; Pt – O – ~1.758 Å; Ni – O – ~2.02 Å; Pt – Ni – ~2.72 Å. (The distance and angles between atoms were determined using the VESTA program (Visualization for Electronic and ST ructural Analysis) [20]).

Computer simulation of the nanocontact was carried out within the framework of the extended Hückel method using the method of nonequilibrium Green's functions (NEGF – Non-Equilibrium Green's Functions) [16]. The calculation of electrotransport properties of the nanocontact consists of two stages. In the first stage, a self-consistent calculation is performed for platinum electrodes in the direction of the flow of electric current. In the second stage, the density matrices are determined, the density of real space is estimated, and the Hartree potential is calculated. A detailed description of this method can be found in [21–23].

To calculate the density matrix of the central region, firstly, a self-consistent calculation of the nanocontact left and right electrodes is performed and the corresponding Fermi levels are estimated: \( \mu_L \) and \( \mu_R \). Taking into account the bias voltage between two platinum electrodes, we determine the left and right chemical potentials:

\[ \mu_L = \delta_L - eV_{bias} \quad \text{and} \quad \mu_R = \delta_R. \]

The applied bias voltage moves the quasiparticles from the left electrode to the right, thereby causing an electric current from left to right. The density matrix of the considered nonequilibrium system is represented as the sum of the density matrices of the left and right electrodes:

\[ \mathbf{D} = \mathbf{D}^L + \mathbf{D}^R \]  

where \( \mathbf{D}^L \) and \( \mathbf{D}^R \) is density matrix of the left and right electrodes, respectively.

\[ \mathbf{D}^L = \int \rho^L(\varepsilon) f\left(\varepsilon - \frac{\mu_L}{k_B T_L}\right) \, d\varepsilon \]  

where \( \varepsilon \) is energy, \( \rho^L(\varepsilon) \) is spectral matrix, \( f(\varepsilon) \) is Fermi energy distribution function of quasiparticles, \( k_B \) is Boltzmann constant, \( \mu_L \) is electrochemical potential, \( T_L \) is current temperature of the left electrode. Density matrix for the right electrode \( \mathbf{D}^R \) is found in a similar way. The spectral matrix is defined using the Green functions:

\[ \rho^L(\varepsilon) = \frac{1}{2\pi} G(\varepsilon) \Gamma^L(\varepsilon) G^L(\varepsilon) \]  

where \( \Gamma^L(\varepsilon) \) is broadening matrix (broadening function), \( G(\varepsilon) \) is retarded and advanced Green’s functions. The broadening matrix of the left electrode is described by the following equation:

\[ \Gamma^L(\varepsilon) = \frac{1}{i} \left[ \Sigma^L - (\Sigma^L)^\dagger \right] \]  

where \( i \) is imaginary unit, \( \Sigma^L \) is self-energy of the left electrode. A similar equation exists for the density matrix of
the right electrode. Green’s retarded function is represented as

$$G(\varepsilon) = \left( (\varepsilon + i \delta) \mathbf{S} - \mathbf{H} - \sum_{k} \mathbf{t}_{k} \delta(\varepsilon - \varepsilon_{k}) \right)^{-1}$$  \hspace{1cm} (5)

where $\delta$ is an infinitely small positive number, $\mathbf{S}$ is overlap integral matrix, $\mathbf{H}$ is Hamiltonian matrix.

After obtaining a self-consistent one-electron Hamiltonian, the transmission function of the nanostructures under consideration is determined, which is then used to determine its current-voltage characteristic (CVC) and differential conductivity. The fraction of the scattering state $k$, propagating through the structure, is determined by the transmission amplitude $t_{k}$, then the transmission coefficient at energy $\varepsilon_{i}$ is determined by summing the transmission amplitude $t_{k}$ from all states at this energy:

$$T(\varepsilon) = \sum_{k} t_{k}^{*} \delta(\varepsilon - \varepsilon_{k})$$  \hspace{1cm} (6)

where $\varepsilon$ is energy, $t_{k}$ is transmission amplitude, $\delta(\varepsilon)$ is delta function. Using (4)–(6), the transmission spectrum can be calculated by the expression:

$$T(\varepsilon) = \text{tr}[\Gamma_{L}^{\dagger} \mathbf{G} \Gamma_{R}^{\dagger}] = \text{tr}[\Gamma_{R}^{\dagger} \mathbf{G} \mathbf{G}^{\dagger}]$$  \hspace{1cm} (7)

The current flowing through the nanocontact is determined on the basis of the well-known Landauer equation, which indicates the fundamental connection of the electric current with the transmission spectrum:

$$I = \frac{2e}{h} \int_{-\infty}^{\infty} T(\varepsilon) \left[ f\left(\frac{\varepsilon - \mu_{R}}{k_{B}T_{R}}\right) - f\left(\frac{\varepsilon - \mu_{L}}{k_{B}T_{L}}\right) \right] d\varepsilon$$  \hspace{1cm} (8)

where $e$ is electron charge, $h$ is Planck’s constant, $T_{R}$, $T_{L}$ are current temperatures and $\mu_{R}$, $\mu_{L}$ are chemical potentials of the right and left electrode.

The transconductance estimate is obtained by calculating a self-consistent current at a number of applied bias voltages $V_{\text{bias}}^{1}, V_{\text{bias}}^{2}, \ldots$, and performing numerical differentiation according to the formula

$$\sigma(V_{\text{bias}}, T_{L}, T_{R}) = \frac{I(V_{\text{bias}}^{1}, T_{L}, T_{R}) - I(V_{\text{bias}}^{2}, T_{L}, T_{R})}{V_{\text{bias}}^{1} - V_{\text{bias}}^{2}}$$  \hspace{1cm} (9)

### 3. Description and Analysis of Results

The results of computer simulations of the transmission spectra, CVC, and differential conductivity of “Pt – TiO – Pt” and “Pt – NiO – Pt” nanostructures are shown in Fig. 3, 4.

The features of the transmission spectrum of Pt – TiO – Pt nanocontact are observed in the energy interval $–3.6\pm 6$ eV (Fig. 3a). The transmission spectrum maxima in the absence of a bias voltage are observed at energies $-3.6$ eV, $-3.12$ eV, $-1.8$ eV, $-1.44$ eV, $-1.08$ eV, $-0.48$ eV, $0.12$ eV, $0.6$ eV, $1.08$ eV, $2.28$ eV, $2.64$ eV, $3.0$ eV, $3.48$ eV, $3.72$ eV, $4.44$ eV and $5.52$ eV.

The deviation from the constant value of the transmission spectrum of Pt – NiO – Pt nanocontact is observed in the energy range $–4.2$ eV÷$0$ eV (Fig. 3 b). The maxima of the transmission spectrum of a nanocontact in the absence of a bias voltage are observed at energies $-3.72$ eV, $-3.36$ eV, $-2.4$ eV, $-2.04$ eV, $-1.68$ eV, $-1.2$ eV, $-0.96$ eV, $-0.36$ eV, $-0.12$ eV.

The transmission spectra of the being examined system with distinct maxima resemble the spectrum of resonant tunnel structures [24]. This may be due to the low dimension of the central region of the nanosystem consisting of a fragment of titanium and nickel oxides with sizes $\sim 8.78$ Å and $\sim 3.98$ Å, respectively (Fig. 1, 2).

Figure 4 shows the dependence of the transmission spectrum of Pt – TiO – Pt nanocontact on $k$ at various energy values. At energy $–1.32$ eV, the spectrum has minima with the following combinations of $k_{A}, k_{B}$: $(0.012; 0.0012)$; $(–0.0012; –0.0011)$; $(–0.0012; –0.2)$ and $(0.2; –0.0011)$.

Further, at $–0.96$ eV, the indicated spectrum minima remain, however, its maximum at $8.4$ arbitrary units is observed at $k_{A} = 0.0012$ and $k_{B} = –0.0011$ (Fig. 4b). At zero energy, four minima disappear, the maximum remains at the center of dependence $T(k)$.

Further, the peak of the function $T(k)$ begins to shift from the center to the edge and at $3.48$ eV the minimum value of the transmission spectrum appears at $k_{A} = 0.0012$.
and $k_B = -0.0011$. As can be seen, the transmission spectrum of the structure is an oscillating function.

Figure 5 shows the evolution of the transmission spectrum of Pt – NiO – Pt nanocontact from $k$ with a change in energy. As can be seen from Fig. 3(b) the oscillation of the transmission spectrum occurs in the energy interval $-4.2$ eV÷0 eV; therefore, we consider the dependence $T(k)$ in this energy interval. At $-4.2$ eV, four localized maxima of the spectrum are observed (Fig. 5a). With increasing energy up to $-2.4$ eV, the peak values of the spectrum accumulate at the center of the dependence $T(k) = 14$ arb. units at $k_A = k_B = 0$. Further, the maxima of $T(k)$ function begin to shift from the center to the edge and at $-1.2$ eV the minimum value of the spectrum is observed at $k_A = k_B = 0$.

The results of simulation of current-voltage characteristics (CVC) and differential conductivity are shown in Fig. 6. (The solid curve describes the characteristics of the direct connection of nanocontacts to the power source, and the dotted one – on the reverse inclusion.)

In the voltage range of $-1.3$ V÷1.3 V, when directly connected and changing the polarity, the CVC characteristic of Pt – TiO – Pt nanocontact acquires a shape of eight number (inherent in memristic elements). However, with further voltage variation, no hysteresis of the current-voltage characteristic is observed (Fig. 6a).

The differential conductivity of such nanosystem has a peak structure, and when directly turned on, its maxima of 260 µS, 60 µS, 120 µS are observed at values of a bias voltage of 0 V, ± 1.4 V, ± 2.6 V, respectively. The minima of the $dI/dV$ spectrum of the nanosystem $-30$ µS and 20 µS occur as “dips” at bias voltages of ±1 V, ±1.8 V, respectively. When the nanocontact is switched back on, the “large peak” of conductivity splits into two 222 µS and 250 µS at voltages of $-1.1$ V and 1.2 V, respectively (Fig. 6a).

The hysteresis of the CVC of Pt – NiO – Pt nanocontact is observed in the voltage range of $-1.8$ V÷0.8 V and 0.9 V÷1.8 V in the form of an oval shape (Fig. 6b). Outside the specified voltage range, the amount of current flowing through the contact is the same in both direct and reverse connection.

At direct and reverse switching of the nanocontact, the maxima of the differential conductivity of 300 µS and 270 µS appear at a bias voltage of $-2$ V and 2.1 V, respectively, also “secondary” peaks 110 µS and 125 µS occur at ±1.05 V.

Differential conductivity dips are observed at $-2.6$ V ($-12$ µS), $-1.6$ V ($-70$ µS), $1.6$ V ($-30$ µS), 2.4 V (36 µS). At reverse switching, a shift in dips of $-1.4$ V ($-50$ µS), 1.45 V ($-20$ µS) is observed.

As can be seen from Fig. 6(a), (b), on the characteristics of both nanocontacts, a negative differential resistance
is observed in the voltage range, where the hysteresis of the
CVC is appeared.

Observation of the hysteresis characteristics of these
nanocontacts shows that they have memory. Also, from the
current-voltage characteristics of the structures, it can be
seen that the investigated objects have weak switching
properties (Fig. 6). For example, at reverse connection
of Pt – TiO – Pt nanocontact in the voltage range of
–0.86 V–1 V, a rapid linear change in the current value
from −42 μA to 42 μA is observed, and in the case of
Pt – NiO – Pt nanocontact, switching from ON mode to
OFF occurs at voltages of −0.88 V and 0.85 V.

Figure 7 shows the hysteresis of the CVC and the
change in the resistance of the channels of nanocontacts
depending on the bias voltage. As can be seen, at the be-
eginning of the formation of hysteresis, the CVC of the
nanocontacts of the channel resistances for direct and re-
verse connection are ($R_{d.c.0} \approx R_{r.c.0}$).

At the case of nanocontact Pt – TiO – Pt:
$R_{d.c.0} \approx R_{r.c.0} \approx 12.9 \Omega$. At direct switching of nanocontact
Pt – TiO – Pt in the interval of $V_{bias}$ from −1.3 V to 0 V
channel resistance decreases exponentially to several ohms,
then in the interval $V_{bias}$ from 0 V to 1.3 V its value is re-
stored (Fig. 7 a). At reverse switching of nanocontact in the
interval of $V_{\text{bias}}$ from $-1.3$ V to 0.1 V resistance increases to $95.24$ k$\Omega$. Then there is a sharp decrease in channel resistance and at the same time the completion of the first loop of the CVC. A similar inverse process of resistance behavior during reverse switching occurs in the interval of $V_{\text{bias}}$ from 0 V to $-1.3$ V, forming the second loop of CVC.

At the beginning of the formation of hysteresis of the CVC of the nanocontact Pt – NiO – Pt the resistances $R_{\text{d.c.0}} \approx R_{\text{r.c.0}} \approx 23.74$ k$\Omega$–$24$ k$\Omega$. At direct switching of the nanocontact to $V_{\text{bias}} \approx 1.8$ V the final resistances at direct and reverse switching are equal to $R_{\text{d.c.1}} \approx R_{\text{r.c.1}} \approx 23.2$ k$\Omega$. At the reverse switching of nanocontact to $V_{\text{bias}} \approx 1.3$ V the channel resistance increases sharply, forming the maximum value of the first hysteresis loop of the CVC due to the significant difference in the channel resistance. Then the channel resistance decreases to 17 k$\Omega$ at a near-zero bias voltage value. At $V_{\text{bias}} \approx 0.7$ V, the formation of the first hysteresis loop of the CVC is completed. Then, in the range of $V_{\text{bias}}$ from $-0.1$ V to $-1.35$ V, an increase in channel resistance is observed. At $V_{\text{bias}} \approx -0.8$ V, the resistances $R_{\text{d.c.0}} \approx R_{\text{r.c.0}} \approx 25$ k$\Omega$ and the second CVC loop is formed. The growth of the channel resistance stops after reaching the maximum value of $65.7$ k$\Omega$ at $V_{\text{bias}} \approx -1.35$ V. In this case, the value $\Delta R \approx 51.43$ k$\Omega$ assumes the maximum value, which is reflected in the hysteresis of the CVC.

4. Conclusion

Thus, in this work, the basic electric transport characteristics (transmission spectra, CVC, differential conductivity) of Pt – TiO – Pt and Pt – NiO – Pt nanocontacts were investigated within the framework of the semi-empirical extended Hückel method. It was shown that in the voltage range $-1.3$ V÷$1.3$ V, the CVC of Pt – TiO – Pt nanostructure has a number eight shape hysteresis, and the hysteresis of the CVC of Pt – NiO – Pt nanostructure manifests itself in voltage intervals $-1.8$ V÷$0.8$ V and $0.9$ V÷$1.8$ V in the form of two oval-shaped figures, connected to a segment. Observation of the hysteresis characteristics of these nanocontacts shows that they have memory. It was found that the “large peak” of the differential conductivity of Pt – TiO – Pt nanocontact at the reverse switching of the conductivity splits into two $222 \mu$S and $250 \mu$S at voltages of $-1.1$ V and $1.2$ V. It is shown that negative differential resistance is observed in the voltage range, where the hysteresis of the current-voltage characteristic is appeared. The evolution of the transmission spectrum of the nanostructure with an increase in the bias voltage (from $-3$ V to 3 V) is presented. It is shown that an increase in the difference in the resistance of the channels of nanocontacts increases the hysteresis of their CVC. The results of the paper may be useful for the calculation of new promising memorial elements of nanoelectronics.

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