Exotic magnetic field-induced spin-superstructures in a mixed honeycomb triangular lattice system

V. Ovidiu Garlea,1 Liurukara D. Sanjeewa,2,3 Michael A. McGuire,3 Cristian D. Batista,4,5 Anjana M. Samarakoon,1 David Graf,5 Barry Winn,1 Feng Ye,1 Christina Hoffmann,1 and Joseph W. Kolis2

1 Neutron Scattering Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA
2 Department of Chemistry and Center for Optical Materials Science and Engineering Technologies (COMSET), Clemson University, Clemson, South Carolina 29634-0973, USA
3 Materials Science and Technology Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA
4 Shull-Wollan Center, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA
5 Department of Physics and Astronomy, University of Tennessee, Knoxville, Tennessee 37996, USA
6 National High Magnetic Field Laboratory, Florida State University, Tallahassee, Florida 32310, USA

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The temperature-magnetic-field phase diagram of the mixed honeycomb triangular lattice system K2Mn3(VO4)2CO3 is investigated by means of magnetization, heat capacity and neutron scattering measurements. The results indicate that triangular and honeycomb magnetic layers undergo sequential magnetic orderings and act as nearly independent magnetic sublattices. The honeycomb sublattice orders at about 85 K in a Neél-type antiferromagnetic structure, while the triangular sublattice displays two consecutive ordered states at much lower temperatures, 3 K and 2.2 K. The ground state of the triangular sublattice consists of a planar “Y” magnetic structure that emerges from an intermediate collinear “up-up-down” state. Applied magnetic fields parallel or perpendicular to the e-axis induce exotic ordered phases characterized by various spin-stacking sequences of triangular layers that yield bilayer, three-layer or four-layer magnetic superstructures. The observed superstructures cannot be explained in the framework of quasi-classical theory based only on nearest-neighbor interlayer coupling and point towards the presence of effective second-nearest-neighbor interactions mediated by fluctuations of the magnetic moments in the honeycomb sublattice.

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I. INTRODUCTION

Field-induced magnetic states that occur in layered triangular lattice antiferromagnets (TLA) have been extensively studied and discussed in the context of broken discrete symmetries of the lattice and spin-rotation in the plane perpendicular to the applied field. It is widely recognized that thermal and quantum fluctuations lift the degeneracy of the classical spin configurations of the triangular antiferromagnetic Heisenberg model in a magnetic field. This well-known realization of order-by-disorder[1] leads to specific planar states: a “Y”-state or 120° spin configuration with two spins canting “up” and one pinned in a “down” direction, a collinear “up-up-down” (uud) state, and a canted “2:1” phase that is an oblique version of the uud state.[2][3] These planar spin configurations are sketched in Fig. 1. An easy-axis anisotropy can also remove the degeneracy and stabilize the same coplanar arrangements. The collinear uud state, which gives a one-third of the saturation magnetization plateau at intermediate fields (M=Ms/3), breaks the discrete Z3 symmetry of the lattice. The canted planar “Y” and “2:1” states that involve Sz - Sx spin components also break the continuous U(1) symmetry of spin rotations about the field axis. The latter spin states with broken mixed symmetries Z3 ⊗ U(1), can be viewed as magnetic supersolid phases that combine superfluid properties with long-range periodicity of solids, as proposed by Liu and Fisher.[4][5]

FIG. 1. Planar spin configurations of single-layer triangular lattice antiferromagnet at 0 K and finite magnetic fields.[3]

Most of existing theoretical studies on TLA assume negligible interplanar interactions. However, the presence of such coupling, as expected in real materials, can cause additional exotic field-induced phase transitions where the relative spin orientations change between adjacent planes to produce interesting magnetic superstructures. The spin-stacking pattern is expected to dramatically depend on the manner of stacking of neighboring layers which can be either eclipsed (adjacent layers related by a simple translation perpendicular to the layer...
plane) or staggered (shifted by certain in-plane lattice translation) near-neighbor planes, with the latter also enabling frustrated out-of-plane interactions. Possible magnetic structures of weakly-coupled eclipsed TLA were discussed by Gekht, Chubukov and Yamamoto. Yet, most theoretical predictions remained unconfirmed due to the limited number of good experimental realizations of equilateral TLA.

Some of the most explored series of TLA compounds are $AX_2$ and $ABX_3$, where $A = \text{Cs, Rb, } B = \text{Ni, Mn, Cu,}$ and $X = \text{Cl, Br, I};$ as well as $ACrO_2$, with $A = \text{Li, Cu, Ag, or Pd}.$ Unfortunately, these systems either have interplanar interactions that are larger than the intraplanar ones, or too strong intraplanar nearest-neighbor coupling that makes the field-induced transitions inaccessible to the currently available magnetic-fields at the neutron scattering facilities. Improvements in sample synthesis techniques allowed in the recent years the discovery of new triangular systems with transitions at accessible magnetic fields. Detailed temperature-magnetic-field ($T - H$) phase diagrams have been reported for several $S = 5/2$ TLA systems with planar (XY) anisotropy, $\text{RbFe(MoO}_4)_2$, $\text{RbAg}_2\text{Fe[VO}_4]_2$, or with weak easy-axis (Ising) anisotropy, $\text{Rb}_2\text{Mn(MoO}_4)_3$. Another exciting class of TLA that has recently emerged is that of $6H$-perovskites $\text{Ba}_3 M^+M''_1^O_3$ with $M^+ = \text{Ni, Co, Mn,}$ and $M'' = \text{Nb, Sb or Ta}.$ These compounds can possess either easy-plane or easy-axis anisotropies and adopt at low temperatures the expected planar $120^\circ$ magnetic structure. For all aforementioned systems experimental evidences for the three predicted field-induced states, the "Y", the one-third magnetization plateau $uuud$, and the "2:1" canted configuration, have been found. However, the lack of sufficiently large single crystal samples required for detailed neutron scattering studies has, in most of the cases, hindered the understanding of the impact of interlayer coupling in stabilization of field-induced ordered phases.

The vanadate - carbonate system $K_2\text{Mn}_3(\text{VO}_4)_2\text{CO}_3$ has been recently identified as a very promising prototype for studying magnetic frustration. Its structure, shown in Fig. 2, consists of alternately stacked triangular and honeycomb magnetic layers. Previous macroscopic measurements indicated complex physical properties with a presumed Jahn - Teller transformation at about 80 K and two successive magnetic phase transitions, at about 3 K and 2 K, into a weakly ferromagnetic ground state. It was inferred that divalent Mn is present in a high-spin state ($S = 5/2$) in the octahedral environment of the honeycomb layer and a low-spin state ($S = 1/2$) in the trigonal bipyramidal coordination of the Mn$^{2+}$ ions occupying the triangular layer. The low-temperature magnetic transitions were attributed to the ordering of the $S = 5/2$ ions of the honeycomb lattice, while the $S = 1/2$ triangular layers were thought to remain paramagnetic. Subsequent first-principles density functional theory-based analysis showed that, contrary to the previous suggestion, both inequivalent Mn ions occupying the two layers are in high-spin $S = 5/2$ state. The calculations predict that both layers exhibit antiferromagnetic orders with vastly different strengths of magnetic interactions. Intrigued by the richness of the magnetic phase diagram featured by this material we have undertaken a comprehensive magnetization and neutron scattering study using high-quality single crystal samples. Our study clarifies the magnetic ground-states of two magnetic layers, and establishes that $K_2\text{Mn}_3(\text{VO}_4)_2\text{CO}_3$ represents an excellent candidate TLA system for studying the effect of interplanar interactions in field-induced states. Applied magnetic fields induce new magnetic superstructures characterized by various spin-stacking sequences of triangular layers. Because the observed magnetic superstructures cannot be explained by any existing theories based only on nearest-neighbor interlayer coupling, they compel a closer look at effective second-nearest-neighbor interactions mediated by fluctuations of the magnetic moments in the honeycomb sublattice.

II. EXPERIMENTAL DETAILS

Single crystals of $K_2\text{Mn}_3(\text{VO}_4)_2\text{CO}_3$ were grown using a high-temperature hydrothermal technique. The chemicals used in this synthesis were used as received, without further purification: $\text{Mn}_2\text{O}_3$ (Alfa Aesar, 98%), $\text{V}_2\text{O}_5$ (Alfa Aesar, 99.6%) and $K_2\text{CO}_3$ (Alfa Aesar, 99.997%). In a typical reaction, $\text{Mn}_2\text{O}_3$ and $\text{V}_2\text{O}_5$ were mixed in a 3:2 molar ratio with 0.8 mL of 5 M $K_2\text{CO}_3$ mineralizer, giving approximately 0.4 g of reactants. Reactions were performed in silver ampules with a diameter of 9.5
mm, with approximately a 70% fill of free volume. After loading the reactants and the mineralizer, the ampoules were welded and loaded in a Tuttle cold-seal style autoclave and filled with distilled water at 80% of free volume to provide suitable counter pressure. The autoclave was heated to 580 °C for two weeks at a typical pressure of 1.5 kbar. Brown hexagonal crystals were isolated using suction filtration. The single crystal specimens used for physical properties characterization and neutron scattering experiments were physically examined and selected under an optical microscope equipped with a polarizing light attachment. The powder sample used for the powder neutron diffraction measurements was generated by grinding crystals produces in the reaction described above.

Temperature and field-dependent magnetic measurements were carried out using a Quantum Design Magnetic Property Measurement System (MPMS). The measurements were carried out on a single crystal specimen with the crystallographic c-axis aligned either parallel or perpendicular to the applied magnetic field. The temperature dependence of static susceptibility \((M/H(T))\) was measured over a temperature range of 2 to 700 K for applied fields \(\mu_0 H = 0.01 \text{ T} \text{ and } 1 \text{ T}\). The isothermal magnetization measurements were performed for fields up to 8 T. Additional isothermal magnetization curves were recorded using a vibrating sample magnetometer (VSM) in magnetic fields up to 16 T, applied along c-axis. Heat-capacity measurements were performed with a Physical Property Measurement System (PPMS, Quantum Design) in zero and magnetic fields up to 6 T applied either parallel and perpendicular to the crystal c-axis.

Neutron powder diffraction measurements were carried out using the HB2A high-resolution diffractometer at the High Flux Isotope Reactor (HFIR), using the 2.41 Å wavelength neutron beam. A powder sample with a total mass of approximately 5 grams was compacted in pellets, loaded into a cylindrical aluminium can, and placed inside a cryostat with ³He insert. Data were collected at temperatures from 150 K to 0.3 K. Single-crystal neutron diffraction measurements were performed at \(T = 150 \text{ K}\) using the TOPAZ time-of-flight diffractometer at the Spallation Neutron Source (SNS). The integrated Bragg intensities were obtained using the 3-D ellipsoidal Q-space integration method and were corrected for background using the MANTID software. Data reduction including, Lorentz and absorption corrections as well as spectrum, detector efficiency, data scaling and normalization was carried out with the ANVRED3 program.

Elastic neutron scattering measurements at temperatures down to 1.6 K were performed at the fixed incident energy (14.6 meV) HB1A triple-axis spectrometer at the HFIR, and at CORELLI and HYSPEC spectrometers at the SNS. Two separate crystals with the approximated dimensions 1 x 1 x 4 mm³ and 4 x 3 x 1 mm³ were used for collecting data under magnetic fields applied parallel and perpendicular to the c-axis, respectively. At CORELLI, white-beam Laue diffraction measurements were taken at 1.6 K and selected magnetic fields up to 5 T, applied along c axis or [1, 1, 0]. For each field configuration the sample was rotated in steps of 3° over ranges of 60°. MANTID software was utilized to carry out the Lorentz and spectrum corrections, as well as to merge the full volume of the scattering data.

At HYSPEC, the elastic measurements were performed in applied magnetic fields up to 8 Tesla, using a fixed incident energy \(E_i = 15 \text{ meV}\) and a Fermi chopper frequency of 120 Hz. Measurements were concentrated over narrow range reciprocal lattice volumes, centered around the relevant magnetic reflections.

Inelastic neutron-scattering (INS) measurements were performed at the HYSPEC spectrometer, operated with the incident energies \(E_i = 25 \text{ meV}\) and 3.8 meV, and the Fermi chopper frequency of 360 Hz. For these measurements, multiple single crystals where coaligned along the c-axis, while the in-plane directions were distributed in a quasi-random manner to provide a total mass of about 0.3 g.

Structural and magnetic data refinements were carried out with the FullProf Suite program. Possible magnetic structures models have been explored by representation analysis using the program SARAh and by the magnetic symmetry approach using the tools available at the Bilbao Crystallographic Server. The INS data reduction and visualization was done with the MANTID and DAVE software packages. Spin-wave calculation were performed using the linear spin wave theory with the program SpinW.

To reproduce experimental data, we have performed classical Monte Carlo simulations using a standard metropolis sampling algorithm on the triangular lattice subsystem. The simulations were performed on finite lattice of 12 x 12 x 4 unit-cells (containing 1152 spins) with periodic boundary conditions. Starting from a completely random and disordered configuration, a spin system was annealed down to a finite temperature in finite number of intermediate temperature steps. Then, the magnetic field was increased up to 22 T with 300 intermediate field points. At each temperature/field step, the magnetization (M) and heat capacity (C) were calculated by taking the ensemble average over the 2000 samples followed by thermalization sampling with adaptive step size, while the static spin structure factor S(Q) was calculated by Fourier Transforming captured spin configurations with the frequency of 500 samples. For better statistics, all the measurements were averaged over 120 independent simulations.

III. EXPERIMENTAL RESULTS AND DISCUSSION

A. Crystal structure

The structural model of \(\text{K}_2\text{Mn}_3(\text{VO}_4)_2\text{CO}_3\) proposed by Yakubovich et al. has been confirmed by the re-
TABLE I. Refined structural parameters and selected bond distances of K$_2$Mn$_3$(VO$_4$)$_2$CO$_3$ from single-crystal neutron diffraction data collected at T = 150 K.

| Atom     | Wyck. | x    | y    | z    | U$_{eq}$ |
|----------|-------|------|------|------|---------|
| K        | 4f    | 1/3  | 2/3  | 0.6578(1) | 0.0144(4) |
| Mn1      | 4f    | 1/3  | 2/3  | 0.0646(1) | 0.0081(3) |
| Mn2      | 2a    | 0    | 0    | 1/4  | 0.0092(5) |
| V        | 4c    | 0    | 0    | 0.0800(4) | 0.0057   |
| C        | 2c    | 1/3  | 2/3  | 1/4  | 0.0070(3) |
| O1       | 12i   | 0.3210(1) | 0.3098(1) | 0.0550(1) | 0.0080(1) |
| O2       | 4c    | 0    | 0    | 0.1552(1) | 0.0138(3) |
| O3       | 6h    | 0.0682(1) | 0.6255(1) | 1/4    | 0.0113(3) |

Space group: $P6_3/m$, a=b=5.1959(3)Å, c = 22.405(2)Å  
$R_f = 0.051$, $\chi^2 = 2.04$

The temperature dependence of magnetic susceptibility ($\chi = M/H$) measured with a magnetic field applied along and perpendicular to the $c$-axis is shown in Fig. 3. In this figure we choose to plot the temperature axis in a logarithmic scale to increase the visibility of the magnetic phase transitions that occur over a large temperature interval. A first magnetic transition near $T_{N1} \approx 85$ K is revealed by a subtle drop in the susceptibility curve measured with field applied along $c$ direction. A second magnetic order transition is discernible as a rise of the $\tilde{H} || c$ susceptibility at $T_{N2} \approx 3$ K. This is immediately followed by a third transition, which appears as a kink in the susceptibility curve at $T_{N3} \approx 2.2$ K. The large difference between the $T_{N1}$ and $T_{N2}$ ordering temperatures denotes that the honeycomb and triangular magnetic layers possess magnetic interactions of completely different energy scales and act as nearly independent magnetic sublattices.

The low-temperature region of the zero-field heat capacity data, together with magnetic susceptibility data corresponding to two different magnetic field orientations, $\tilde{H} || c$ and $\tilde{H} \perp c$, are displayed in Fig. 4. The two successive magnetic transitions at approximately 3 K and 2.2 K can be clearly seen in heat capacity data ($c_P$) as two distinguishable lambda-shaped peaks. One can also notice in Fig. 4 that the magnetic susceptibility exhibits significant anisotropic behavior. When the field is applied parallel to the $c$-axis the susceptibility undergoes changes at both $T_{N2}$ and $T_{N3}$ transitions. However, when the field is applied perpendicular to the $c$-axis, only the lower transition near 2.5 K ($T_{N3}$) is visible. This behaviour is indicative of a spin-canting taking place at the lowest temperature.
FIG. 3. (a) Evolution of the magnetic susceptibility \((M/H)\) as a function of temperature, measured in a field of 1 T applied parallel (open symbol) and perpendicular (solid symbol) to the \(c\)-axis. The temperature axis is given in a logarithmic scale to increase the visibility of the magnetic phase transitions. The inset shows the inverse susceptibility that features two linear regimes at 200 K and 700 K. The Curie-Weiss fits are shown as red lines. (b) Expanded view of magnetization curves around the \(T_{N1}\) transition temperature. The magnetic order is revealed by a subtle drop in the magnetization curve measured with field applied along the \(c\) direction.

The inverse magnetic susceptibility is shown in the inset of Fig. 3 along with fits using the Curie-Weiss model \((\chi = \chi_0 + C/(T - \Theta_{CW}))\). The \(1/\chi\) data shows two linear regimes: one for the temperature range 200 to 700 K where all spins are paramagnetic, and a second at lower temperatures ranging from 10 to 50 K. For the high temperature range, the Curie-Weiss fit yields a Curie constant \(C = 4.44 \text{ cm}^3/\text{mol-Mn} \cdot \text{K}\), a Weiss temperature of -215 K, and a temperature-independent term \(\chi_0 = -0.00027 \text{ cm}^3/\text{mol-Mn}\). The negative experimental value of \(\chi_0\) can be attributed to the diamagnetic background from the sample holder, as the core diamagnetism correction is estimated to be about an order of magnitude smaller that the obtained value. The negative Weiss temperatures indicates dominant antiferromagnetic interactions. The obtained effective moment 5.95 \(\mu_B/\text{Mn}\) is very close to that expected for \(S = 5/2 \text{ Mn}^{2+}\), \(g\sqrt{S(S+1)}\)

\[ = 5.91 \mu_B/\text{Mn}, \] suggesting that Mn ions have the same spin state in both honeycomb and the triangular planes. A Curie-Weiss fit performed using a constrained \(\chi_0 = 0\), yields a slightly lower effective moment 5.72 \(\mu_B/\text{Mn}\) and \(\Theta_{CW} = -188\) K. Note that previous study reported much smaller values for both the effective moment (2.75 \(\mu_B/\text{Mn}\)) and the Curie-Weiss temperature (114 K), which were likely caused by an overestimation of the temperature-independent susceptibility term. Although the temperature interval of the second Curie-Weiss regime, 10 K < \(T\) < 50 K, is too narrow for extracting definite information, the Curie-Weiss fit yields a Weiss temperature of about -19 K and Curie constant 1.62 \(\text{ cm}^3/\text{mol-Mn} \cdot \text{K}\). One could remark that this Curie constant represents about 36% of the value obtained for the high temperatures and it correlates reasonably well with the 1/3 fraction of spins located in the triangular layer. This suggests that the honeycomb and triangular layers act as nearly independent magnetic sublattices.

The isothermal magnetization curves measured at selected temperatures ranging from 2 K to 300 K are shown in Fig. 3. Magnetization data was taken for magnetic fields up to 16 T applied along \(c\)-axis, and up to 8 T for fields applied perpendicular to the \(c\)-axis. In agreement with the previous report, the magnetization curve measured with \(H\parallel c\) at \(T = 2\) K exhibits a plateau at about 4.5 Tesla, followed by a sharp upturn at approximately 7 T. Another step-like transition is observed near 11 T, and then a tendency towards saturation as the field approaches 16 T. The magnetization value of the plateau state \((\approx 0.55 \mu_B/\text{Mn})\) appears to correspond to about 1/9 of total saturation value of \(\text{Mn}^{2+}\) moments \((M_S = gS = 5 \mu_B)\), or 1/3 of saturation value of \(\text{Mn}^{2+}\)
moments located in the triangular layers. The magnetization plateau value, labeled as $1/3 M_{ST}$, is marked by a dashed line in Fig. 5. We note that the saturation of magnetization of the triangular layers, $M_{ST} = 1.66 \mu_B/Mn$, is found to be reached at a magnetic field of about 14.3 Tesla. At $T = 4$ K, the plateau-like state in the $\mu_0 H || c$ magnetization curve is no longer present, suggesting that this is related to the low-temperature ordering states observed below 3 K ($T_{N2}$). On the other hand, the 11 T step-like transition persists up to 50 K, appearing to be related to the higher-temperature ordered state that emerges at $T_{N1} \approx 85$ K. There is no apparent rational number correlation between the magnetization value corresponding to this transition and the total saturation value $M_S$. In contrast to the magnetization curve measured with $\overrightarrow{H} || c$, the curve measured with $\overrightarrow{H} \perp c$ shows a smooth increase with increasing the magnetic field up to the highest measured value of 8 T.

Heat capacity measurements in applied magnetic fields have been carried out to construct the $T - H$ phase diagram around the two low-temperature magnetic transitions. The results are summarized in Fig. 6. For the field oriented along the $c$-axis direction, the $T_{N3}$ magnetic transition shifts quickly towards lower temperatures with increasing the magnetic field, while the intermediate transition $T_{N2}$ extends first to higher temperatures and then diminishes to define a dome-like shape with the tip at approximately $\mu_0 H = 4$ T and 3.75 K. The transition points for $\overrightarrow{H} \perp c$ are represented by filled symbols in Fig. 6(c). It is also interesting that the heat capacity peak corresponding to the intermediate transition displays a dramatic increase in intensity as the field increases to 4 T, after which it remains relatively flat. This $\overrightarrow{H} \parallel c$ phase diagram is reminiscent of that of a triangular lattice antiferromagnet with weak easy-axis anisotropy, and it is strikingly similar to that observed for Rb$_4$Mn(MoO$_4$)$_3$ [17] and Ba$_3$MnNb$_2$O$_9$ [24].

Upon applying the magnetic field perpendicular to $c$-axis the heat capacity peak corresponding to the $T_{N2}$ transition shifts only slightly to higher temperatures, whereas the peak denoting the $T_{N3}$ transition splits into two components that display dome-shaped profiles as a function of magnetic field. The higher-temperature component that emerges from the zero-field heat capacity peak, labeled as $T'_{N3}$ in Fig. 6 is much broader and reduced in amplitude. The phase diagram for this field direction is unexpectedly more complicated than that observed in other triangular lattice antiferromagnets.
C. Zero-field magnetic order

1. Magnetic order of the honeycomb sublattice

Powder and single crystal neutron diffraction data collected below \( T_{N1} \) reveal additional scattering at low angles reflections, of the type \((1, 0, L=2n)\) corresponding to the long-range magnetic ordering of the Mn1 ions occupying the honeycomb layers.

The magnetic moment orientation for each atomic position curve is observed near 2.2 K, that matches the position of the second peak at \( T \lesssim 85 \) K, described by \( k=(0, 0, 0) \) and the magnetic space group \( P6_3/m \).

A new set of magnetic reflections with propagation vector \( \mathbf{k} = (1/3, 1/3, 0) \) appear upon cooling below approximately 3.2 K. The temperature evolution of the \((1/3, 1/3, 1)\) peak intensity is shown in Fig. 9. The observed transition point agrees well with \( T_{N2} \) obtained from macroscopic measurements. Furthermore, a kink in the order parameter curve is observed near 2.2 K, that matches the position of the second peak at \( T_{N3} \) in the heat capacity data.

No change in intensity of the \((1/2, 1/3, 0)\) and \((1/2, 1/3, 1)\) peaks associated with the ordering of Mn1 honeycomb sublattice was observed to occur at these low temperatures. The spin reorientation suggested by the static susceptibility data to take place at \( T_{N3} \) is best captured by following the temperature dependence of the ratio between \((1/4, 1/3, 1)\) and \((1/4, 1/3, 3)\) peak intensities, shown in the insert of Fig. 9. It is noticeable that the \((1/3, 1/3, 3)\) ex-
hibits a larger gain in intensity below 2.2 K. Considering that only the moment component perpendicular to the momentum transfer $Q$ contributes to the magnetic intensities, the abrupt change in the relative intensity gain indicates that some magnetic moments are rotating away from the c-axis. A rough estimate of the canting angle $\Theta = 54(5)\degree$ is obtained from the intensities ratio at $T = 1.7$ K.

The new satellite peaks associated with the wavevector $\mathbf{k} = (\frac{1}{3}, \frac{1}{3}, 0)$ that developed below 3 K have been attributed to the long-range magnetic ordering of the manganese atoms (Mn2) in the triangular layer. The neutron scattering data is well described by a magnetic structure with the static magnetic moments pointing along the c-axis, and amplitudes which follow the $k$-wavevector modulation such as: $m_i = m_0 R[\cos(2\pi \mathbf{k} \cdot \mathbf{r}_i + \phi)]^{[46]}$. Here, $m_0$ represents the amplitude of the ordered moment in the zeroth cell, and $\phi$ is a phase factor. The moment distribution for a phase $\phi = 0$ along the a axis is $m_0$, $-m_0/2$, $-m_0$, while for a choice of $\phi = \pi/2$ the sequence becomes $0$, $-\sqrt{3}/2m_0$, $\sqrt{3}/2m_0$. The moments are thus fully compensated inside the plane. Furthermore, the selection rule $L=2n+1$ indicates that successive triangular layers are stacked antiferromagnetically along the $c$ direction. It is important to realize that we are discussing the ordering of the static moment. Other possible disordered or strongly-fluctuating magnetic components that may exist do not contribute to the Bragg intensities. The only possibility to obtain a uniform amplitude across all Mn2 magnetic sites is if an additional $\mathbf{k} = (0, 0, 0)$ component would be present. This is important to understand, since most publications refer to this intermediate state, which is specific to the triangular lattice systems with weak easy-axis anisotropy, as the $udd$ phase, without any further description of its single-$\mathbf{k}$ or double-$\mathbf{k}$ character. In our case, the lack of $\mathbf{k} = (0, 0, 0)$ contribution (and thus of net magnetization) is obvious from the magnetization measurements. Furthermore, a careful measurement of the temperature evolution of the $(1,0,1)$ reflection across the two low-temperature transitions, shown in Fig. [9] indicates no additional magnetic scattering as one.

FIG. 9. (Color online) Temperature dependence of $(\frac{1}{3}, \frac{1}{3}, 1)$ magnetic peak intensity revealing the long-range magnetic order of Mn2 ions on the triangular layer at $T_{N2} \approx 3.2$ K, followed by a spin reorientation at $T_{N3} \approx 2.2$ K. The absence of magnetic scattering contribution to the $(1,0,1)$ reflection across the two low-temperature transitions suggests that the intermediate magnetic order consists of a collinear $up- up- down$ structure with modulated-amplitude (see text for details). The insert displays the temperature dependence of the ratio of the intensities $(\frac{1}{3}, \frac{1}{3}, 1)$ and $(\frac{1}{3}, \frac{1}{3}, 3)$. The larger gain in intensity of $(\frac{1}{3}, \frac{1}{3}, 3)$ below $T_{N3}$ demonstrates that magnetic moments are rotating away from the c-axis to produce a “Y”-type spin structure.

FIG. 10. (Color online) (a) Three-sublattice static magnetic order of Mn2 atoms (inside the triangular layer) in the intermediate temperature $2.2$ K $\lesssim T \lesssim 3$ K. The magnetic moments are aligned parallel to the c-axis in an $up- up- down$ configuration. The moment amplitude follows the $k=(\frac{1}{3}, \frac{1}{3}, 0)$ modulation, $m_i = m_0 R[\cos(2\pi \mathbf{k} \cdot \mathbf{r}_i)]$, resulting in a fully compensated magnetization inside the plane. Successive triangular layers are stacked in an antiparallel manner. The honeycomb layers maintain the AFM structure shown in Fig. [5] but are omitted for clarity. A view along the c-axis of a three-sublattice collinear magnetic order is shown in the right panel. (b) Three-sublattice magnetic structure below 2.2 K. Two of Mn2 atoms develop in-plane $(ab$ ordered spin components to form a planar canted $Y$-type structure, where moments are rotated by about $120\degree$ between neighboring sites. The structure remains bilayer with the moments of adjacent layers being antiparallel to each other. The right panel of the figure displays the projection of the spin structure on the $ab$ basal plane.
would expect from an uncompensated magnetic component. Our amplitude modulated \textit{udd} (single-\textbf{k}) magnetic structure can be described by the magnetic space group \textit{P6\textsubscript{3}}/m in a 3 x 3 x 1 magnetic supercell. Within this expanded unit cell, there are three non-equivalent magnetic sites (Mn\textsubscript{2+}, i=1,2,3) that follow the modulation imposed by the \textbf{k} wavevector. Note that the same magnetic space group can be used to describe a uniform \textit{udd} double-\textbf{k} structure. The proposed magnetic structure model for Mn2 site in the temperature range 2.2 K \(\leq T \leq 3\) K is shown in Fig. 10(a), and the site-specific orientation of magnetic moments is given in Table III. In Fig. 10 we omitted the Mn1 honeycomb layers that preserve the same spin arrangement as shown in Fig. 8.

As evidenced by the order parameter curve in Fig. 8 an in-plane spin component develops below 2.2 K resulting in a canting of the ordered moment away from the \(c\) direction. The in-plane spin component exhibits a modulation in amplitude in accord to \(\textbf{k} = (\frac{1}{3}, \frac{1}{3}, 0)\). The natural tendency toward an uniform static moment magnitude for all sites is fulfilled by the development of in-plane components only on the two sites with reduced \(m_c\) static moments. This can be realized by considering an offset between phase factors \(\phi\) of the two moment components, \(m_a\) and \(m_{ab}\) of \(\pi/2\). Ideally, this produces a 120° spin configuration in the plane containing the \(c\)-axis, and is known in literature as the planar “Y” canted structure. Similar to the intermediate phase, the successive Mn2 triangular layers remain aligned antiparallel with respect to each other. This low-temperature ordered state inherits the broken lattice symmetry while also breaking the spin-rotational symmetry within the \(ab\) plane and thus can be viewed as an magnetic analogue to a supersolid state.[9, 10] The magnetic structure can be described using the monoclinic magnetic subgroup \(P2\textsubscript{1}'\) (#4.9) operating on a 3 x 3 x 1 magnetic supercell. We note that the in-plane spin component can align along any direction and, experimentally, this cannot be uniquely determined. For fitting the single-crystal neutron data we selected a model where the spins form an ideal 120° structure in the \((1,1,0)\) plane. The refined magnitude of the static moment is 3.7(2)\(\mu_B\), significantly smaller than that expected for spin \(S = 5/2\). Similar reduced ordered moment of about 3.9(5)\(\mu_B\) was reported for the \(S = 5/2\) TLA system RbFe(MoO\textsubscript{4})\textsubscript{2}.[12] One possibility is that the static moment does not reach full saturation at the measured temperature of 1.7 K, but it could also be that the geometrical frustration are causing strong quantum fluctuations. The magnetic moments arrangement in this canted structural model for the temperatures below 2.2 K is summarized in Table III and illustrated in Fig. 10(b).

### D. Spin-wave excitations

1. **Magnetic excitation spectrum of the honeycomb sublattice**

Inelastic neutron-scattering measurements performed with the incident energy \(E_i = 25\) meV revealed a well defined spin-wave branch emerging from the \((1,0,0)\) magnetic peak and extending to an energy transfer of approximately 22 meV (see Fig. 11(a)). There is no discernable dispersion along the \(c\)-axis indicating very weak coupling between magnetic layers. As visible in Fig. 11(b), the two-dimensional correlations is evidenced by rods of scattering along \([0,0,L]\) direction in the contour plot of the reciprocal lattice plane corresponding to the energy transfer range 6 - 10 meV. The scattering intensity along \(Q\) follows the decay expected for the magnetic form factor of \(\text{Mn}^{2+}\) magnetic ion. As described in Section II the sample used for these measurements was relatively small (0.3 g) and consisted of coaligned crystals only along \(c\)-axis direction with random in-plane orientation. This has negatively impacted the data quality and the amount of information that can be extracted from it. Thus, certain assumptions which simplified the analysis had to be
made. Excitations from a honeycomb lattice are typically described by using a Heisenberg model that includes first-, second-, and third-neighbor in-plane exchange interactions \(J_1, J_2, J_3\), an exchange interaction between planes \(J_c\), and an anisotropy term \(D_h\). Based on our experimental resolution we can estimate that the interplane coupling \(J_c\) and the anisotropy are two orders of magnitude smaller than the in-plane exchange interactions. The \(J_3\) is not expected to have a significant contribution, and is beyond our ability to determine with the available data. The strength of nearest-neighbor exchange interaction can be estimated from the Curie-Weiss temperature \(\Theta_{CW} = -215 \text{ K}\), \(J_1 = 3k_B\frac{\Theta_{CW}}{\zeta} S(S+1)\). Considering the number of nearest-neighbor \(\zeta = 3\) and the spin value the \(S = 5/2\), one obtains \(J_1 = 2.1(3)\) meV. Fixing the \(J_1\) value, the measured inelastic spectrum can be well reproduced by using an additional second-neighbor exchange \(J_2 = -0.3(1)\) meV. The ratio between the \(J_1\) and \(J_2\) is consistent with that expected for a Néel-type magnetic ground state in a honeycomb lattice. \[48\, 49\]

In the absence of measurable spin-wave excitation gap, the magnitude of the axial anisotropy term \(D_h\), responsible for the spins alignment along c-axis, can be obtained from the value of the field-induced transition observed near 11 T. For a honeycomb lattice ordered in a Néel-type AFM magnetic structure a spin-flip transition is expected to occur at a field \(H_{sf} = 2S\sqrt{D_h(3J_1-D_h)/g\mu_B}\). This yields an anisotropy \(D_h\) of approximately 0.010(2) meV. The calculated spin-wave excitation spectrum using the aforementioned exchange parameters over an averaged in-plane momentum transfer is shown in Fig. 11(c).

Our estimates show that the dipole-dipole interaction can present an important contribution to the uniaxial anisotropy of Mn\(^{2+}\) (\(S = 5/2\)) ions in the honeycomb layer. The intralayer and interlayer distances, 3.01 Å and 5.5 Å, yield an anisotropy comparable in magnitude (\(10^{-2}\) meV) to those observed and calculated for the classical antiferromagnets MnO \[51, 52\] and MnF\(_2\) \[53, 54\], where the nearest-neighbors distances are about 3.1 Å and 3.3 Å, respectively.

2. Magnetic excitation spectrum of the triangular sublattice

The \(T = 1.7\) K inelastic data contains additional low-energy magnetic excitations that are due to cooperative

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FIG. 11. (color online) (a) Energy-momentum slice of the inelastic neutron scattering data measured with \(E_i = 25\) meV at the HYSPEC spectrometer. A spin-wave branch emerges from the (1,0,0) magnetic peak and extends to an energy transfer of approximately 22 meV. (b) Contour plot of the \((H,0,L)\) reciprocal plane for energy transfer integrated between 6 and 10 meV. The rod of scattering along \([0,0,L]\) direction indicates very weak coupling between magnetic layers. (c) Calculated spin-wave spectrum using a Heisenberg model that includes first- and second-neighbor in-plane exchange interactions \((J_1 = 1.55\) meV, \(J_2 = -0.45(3)\) meV) in the \(S = 5/2\) honeycomb lattice. (d) Low-energy magnetic excitations that develop around the magnetic peaks at \((1/3, 1/3, 1)\) and \((2/3, 2/3, 1)\). (e) 2D slice of momentum space corresponding to energy transfer range 0.2 - 0.3 meV revealing the quasi-two-dimensional character of the excitations. (f) The calculated spin-wave spectrum of \(S = 5/2\) triangular lattice Heisenberg antiferromagnet characterized by nearest-neighbor exchange interactions \((J = 0.08\) meV) and a easy-axis anisotropy \((D_t = 0.03\) meV). The spectrum is averaged over all in-plane \(Q\) directions to reproduce the experimental conditions.
fluctuations of magnetically ordered spins in the triangular layer. As shown in Fig. 11(d) spin-wave excitations develop around the magnetic Bragg peak positions ($\frac{1}{3}$, $\frac{1}{3}$, 1) and ($\frac{2}{3}$, $\frac{2}{3}$, 1) and have a bandwidth of approximately 0.8 meV. The quasi-two-dimensional character of the excitations is revealed by the rod-like scattering along [0,0,L] direction in the 2D slice plot of momentum space corresponding to energy transfer range 0.2 - 0.3 meV, displayed in Fig. 11(e). Keeping in mind that only one-third of magnetic ions occupy the triangular layer, it is not surprising that the INS data quality for these low-energy excitation is even more affected by the small sample mass and its random in-plane orientation. In addition, a diffusive quasielastic component seems to overlap with the spin-waves, accounting for some of the missing ordered moment. Such diffuse scattering was previously observed in other triangular systems and was attributed to uncorrelated trimers that could survive well below the ordering temperature. Nonetheless, from the bandwidth of the spin-wave spectrum one can estimate the value of a nearest-neighbor exchange interaction (J) as approximately 0.08(1) meV. As pointed out in the previous sections, the magnetic behaviour observed from the triangular layer suggests the existence of a weak easy-axis anisotropy (D$_t$). The energy gap expected from such anisotropy could not be resolved in our INS data. However, one can determine the value of D$_t$ from its relationship to the two-step transition temperatures $T_0(\approx J(T_N^2-T_N))/T_N$, or from the saturation magnetic field of the triangular magnetic sublattice $H_S = \frac{(9J-2D_t)}{g\mu_B} = 14.3$ T. The estimated value of the axial anisotropy is $D_t \approx 0.028(2)$ meV, which is nearly twice as large than that in the honeycomb layer $D_h \approx 0.010(2)$ meV. Considering that the interatomic distance for Mn ions located in the triangular layer are much larger, ~ 5.2 Å, a much smaller dipolar contribution of the order of 10$^{-3}$ meV is estimated for this site. It therefore appears that the $D_t$ magnetic anisotropy is mainly due to higher-order terms in the interplay between crystalline-field and spin-orbit couplings and covalency effects, as demonstrated for other 3$d^5$ systems. For instance, spin-orbit coupling effects were shown to produce an anisotropy of about 0.06 meV in Mn$_2$WO$_4$. The observed strength of the trigonal bipyramidal coordination of Mn$^{2+}$ in the triangular layer is anticipated to induce a stronger spin-orbit-induced anisotropy than the more-regular octahedral environment of the magnetic ions in the honeycomb layer. The calculated in-plane averaged spin-wave spectrum using the estimated $J$ and $D_t$ parameters is shown in Fig. 11(f). The inelastic magnetic spectrum of the intermediate ordered state $uuu$ has also been measured at 2.8 K and it shows no discernible change with respect to that observed at the base temperature.

**E. Field-induced magnetic phases in triangular sublattice**

The effect of applied magnetic fields on the magnetic order of $K_2Mn_3(VO_4)_2CO_3$ has been studied using the CORELLI and HYSPEC instruments for fields up to 8 T. For such magnetic fields, only the triangular magnetic layer shows a notable magnetic response. Figure 12 shows the evolution of the elastic scattering in the $(H, H, L)$ reciprocal plane for the magnetic fields of 0, 0.5 T and 5 T, applied along the c-axis direction. The data reveal changes in intensity of satellite magnetic peaks associated with the propagation vector $k=(\frac{1}{3}, \frac{1}{3}, 0)$, as well as the development of strong diffuse scattering intensity along the L-direction. The diffuse scattering becomes progressively stronger with increasing field, and has a well-structured profile. A cut along the L direction of the diffuse scattering with prominent peaks at $H$=0, ±0.5, ±1 and ±5 is displayed in Fig. 12(d). A more thorough survey of the field effect on the intensities of $(\frac{1}{3}, \frac{1}{3}, 0)$ and $(\frac{2}{3}, \frac{2}{3}, 1)$ magnetic Bragg peaks has been carried out using HYSPEC instrument and is shown in Fig. 13. One can observe an immediate increase in intensity of $(\frac{1}{3}, \frac{1}{3}, 0)$ peak as the field is raised above zero. Furthermore, the $(\frac{2}{3}, \frac{2}{3}, 1)$ peak intensity undergoes a slight decrease with a minimum near 1.5 T, followed by a recovery with a local maximum at about 5.5 T, and then a strong decrease to a nearly complete disappearance at the highest measured field $\mu_0H = 8$ T. The profile of the field dependence reveals the existence of at least four different spin configurations before reaching the saturation.

When the magnetic field is applied along the [1,1,0] direction, the evolution of magnetic peaks is strikingly different. Representative slices of $(H, H, L)$ reciprocal plane obtained at fields of 0, 1.5 T, 3.5 T and 5 T are presented in Figure 14. The 1.5 T data reveals the appearance of well-defined $(\frac{1}{3}, \frac{1}{3}, 0)$ and $(\frac{2}{3}, \frac{2}{3}, 0)$ magnetic peaks and no diffuse scattering along the L-direction. At 3.5 T the magnetic peaks appear to relocate along L-direction to a slightly incommensurate lattice vector $\xi = 0.654(1)$. As the magnetic field is ramped up to 5 T, the magnetic phase recovers its commensurate state with $k = (\frac{1}{3}, \frac{1}{3}, 0)$. The order-parameter profiles of the commensurate and incommensurate magnetic states as a function of the field at 1.7 K, are shown in Fig. 15. One can see that the incommensurate phase forms at about 2 T and disappears near 4.5 T. There is no detectable change in the incommensurability for this field range. Above 4.5 T, the commensurate $(\frac{1}{3}, \frac{1}{3}, 1)$ peak reappears but does not recover all its intensity, and exhibits a slow decrease with increasing the field. The phase-diagram revealed by neutron scattering measurement sheds light on the origin of the split into two components of the heat capacity low-temperature peak, presented in Fig. 6. It is plausible that the heat capacity peak at $T_N^*$ is related to the commensurate-incommensurate phase transition. The intermediate-field incommensurate state appears to be stable only over a finite temperature range, which sug-
suggests that thermal fluctuations play a key role in its formation.

Based on the recorded integrated intensities, models of the magnetic structures corresponding to each stage of the $\mathbf{H} \parallel c$ or $\mathbf{H} \perp c$ phase-diagrams have been constructed. The available models were further scrutinized by considering the results of Monte-Carlo simulations performed on a spin Hamiltonian of a TLA described using the determined nearest-neighbor exchange coupling ($J = 0.08$ meV) and easy-axis anisotropy ($D_z = 0.028$ meV), as well as an approximate weak inter-layer coupling $J_{z1} = 0.005$ meV. The calculated magnetization curves for $T = 0$ K and 1.7 K, along with the predicted magnetic configurations at 0 K are presented in Fig. 17. The zero-field heat-capacity curve, shown in the inset of Fig. 17 reproduces the two successive magnetic transitions at low-temperatures, while the calculated isothermal magnetization curve captures the experimental data very well.

The appearance of $L = \text{even}$ reflections in neutron data suggests the change in the spin-stacking sequence between triangular layers, with part of the spins tending to align parallel to each other. Therefore, in the low-field regime of $\mu_0 \mathbf{H} \parallel c$, the “Y” magnetic configurations of the adjacent triangular layers are no longer compensating each other as in the zero-field structure but follow the field direction to produce a net magnetization along the $c$-axis. The determined low-field magnetic structure is shown in Figs. 17(a) and 17(b). It consists of two triangular layers, as the chemical crystal structure, with the stacked spins rotated by approximately $2\pi/3$ relative to each other. Upon further increasing the magnetic field, the spins in each layer are continuously rotating to arrange parallel to the $c$-axis into a 1/3 $M_{ST}$ plateau state $\text{uud}$. This collinear configuration is displayed in Fig. 17(ii). Note that such ordered state has a double-$\mathbf{k}$ nature, as $\mathbf{k} = (0, 0, 0)$ contribution adds to the zero-field $\mathbf{k} = (\frac{1}{3}, \frac{1}{3}, 0)$. Due to the geometrical degeneracy, there are three possible magnetic configurations for each triangular layer: $\text{uud}$, $\text{udu}$ or $\text{duu}$, that we will refer to in the following as $A$, $B$ and $C$ magnetic layers. These magnetic configurations are presented in Fig. 16. The existence of stacking disorder of neighboring layers is apparent in the presence of the structured diffuse scattering along the $L$-direction. The relative intensities at $(\frac{1}{3}, \frac{1}{3}, L)$ peaks positions for $L = 0$, 1 and 0.5 can be explained by an admixture of two magnetic polytypes: the bilayer $AB - AB$ and a four-layer superstructure.
$\text{AABB} - \text{AABB}$. The phase ratio of the two observed polytypes at $T = 1.7$ K is found to be nearly 4:1. Figure 18 displays only the dominant $AB - AB$ bilayer magnetic polytype. While the spin-stacking disorder could be explained by the presence of small structural imperfections in the crystal, the four-layer polytype is indicative of the presence of second-nearest-neighbor inter-layer interactions. This is very surprising since the separation between second-nearest-neighbor triangular layers is very large ($\approx 22.4$ Å), while each Mn atom is located in a zero-molecular-field of the adjacent honeycomb sublattice. As presented in Fig. 10, a bilayer structure is expected for AFM nearest-neighbor interlayer coupling ($J_{z1}$) and FM second-nearest-neighbor interlayer interaction ($J_{z2}$). In contrast, a four-layer superstructure $\text{AABB} - \text{AABB}$ is only possible for FM nearest-neighbor interlayer interaction ($J_{z1}$) weaker than twice the second-nearest-neighbor interlayer interaction ($2|J_{z2}| > |J_{z1}|$). The experimental restraints prevented from carrying out measurement below 1.7 K to determine if the disorder and polytypes mixing ratio exhibits any temperature dependence. This might be expected if thermal and quantum fluctuations are involved in the effective interlayer coupling via order from disorder mechanism (effective interaction mediated by fluctuations of the magnetic moments in the honey-
At magnetic fields above 5.5 T the collinear state starts to evolve towards an oblique “2:1” structure, as shown in Fig. 18(iii). As the field increases the magnetic moment that is pointing opposite to the field direction is continuously rotating to align with the field. In the absence of neutron data for fields larger than 8 T, we used classical Monte Carlo simulations to define the magnetic state. The calculations indicate that the moments are pass through a canted “V” spin configuration before the full saturation (Ms), as shown in Fig. 18(iv). The field-induced magnetic configurations within the layer are consistent with the theoretical predictions and with those observed in similar triangular systems. The dominant bilayer magnetic polytypes (i), (ii) and (iii) found at low and intermediate fields are consistent with the configurations predicted by Gekht and Bondarenko for weakly-coupled triangular antiferromagnets. However, the presence of multiple magnetic polytypes including the four-layer superstructure is indicative of more complicated interlayer coupling and calls for more thorough theoretical investigations.

In the case of the field applied perpendicular to c-axis, along the [1,1,0] direction, the low-field magnetic structure can be looked as a distorted of the zero-field “Y” structure where the two canted spins are rotating towards the field direction. This reorientation does not alter the lattice periodicity along the c-direction and the magnetic structure remains bilayer up to about 2 T. The low-field magnetic structure that describes well the low-field (0 < µ0H ≤ 2 T) neutron data is shown in Fig. 18(i). The rotation of the spins continues until they reach a nearly-orthogonal arrangement, at about 2 T, with one spin pointing along the in-plane field direction and the other two aligned nearly parallel to c-axis (i.e. up-right-down or urd magnetic structure). Similarly to the plateau case described by A, B, C configurations (Fig. 16), any permutation of the three spin orientations is possible for such an orthogonal model. Our diffraction data clearly indicates that a three-layer superstructure is stabilized at intermediate fields between approximately 2 T and 4.5 T. This superstructure is shown in Fig. 18(ii). The stacked spins are alternating their orientations across the three layers as, urd, rud and dru, equivalent to a ABC – ABC configuration that becomes stable when both nearest-neighbor and second-nearest-neighbor are antiferromagnetic. There is, however, a small incommensurability of the modulation along c-axis (k=(1/3, 1/3, 0.654)), and therefore the spin orientations undergo slight undulations around the ideal directions. This could arise from a competition between nearest-neighbor and second-nearest-neighbor inter-layer interactions. It is interesting to point out that the c-axis modulation of the magnetic order appears to be locked-in to a constant value for the entire range (2 < µ0H < 4.5 T), despite the fact that the magnetization curve shows a uniform increase suggesting a continuum rotation of the spins towards the field direction. It is also important to note that no stacking disorder is observed, which indicates that this intermediate-field incommensurate magnetic phase is well stabilized. Our classical Monte Carlo simulation, which only accounts for a weak nearest-neighbor interlayer exchange, predicts for this intermediate-field range only a bilayer spin arrangement in the form of urd – rud (see Fig. 17(b)). Considering the stability of the three-
FIG. 18. (Color online) Models of the static magnetic orders induced by magnetic fields applied parallel to $c$ (i-iv) and along [1,1,0] (i'-iv') as determined from neutron diffraction data. The figure only presents the dominant bilayer structure but the (i-iii) states are susceptible to spin-stacking disorder and four-layer superstructure formation as described in the text. A three-layer stacking sequence (ii') was found for the in-plane field orientation where the moments form a nearly orthogonal configuration and are permuting orientations across the three layers.

layer phase over a finite temperature interval, one may infer that the second-nearest-neighbor interlayer coupling are strengthened by quantum-mechanical coupling via order-by-disorder mechanism. [1, 61, 62]. Upon increasing the magnetic field above 4.5 T the magnetic structure recovers its original bilayer form, with a tilted variant of $udr - rud$ configuration, labeled as “W”, illustrated in Fig. 18(iii'). Our Monte Carlo calculation predicts that before saturation the spins may experience an additional change in the stacking pattern as drawn in Figs. 17(b) and 18(iv').

IV. SUMMARY

The structural and magnetic properties of the vanadate carbonate $K_2Mn_3(VO_4)_2CO_3$ have been studied by means of magnetization, specific-heat and neutron scattering measurements. The structure consists of an alternate stacking of honeycomb and triangular layers made of edge sharing $\text{MnO}_6$ octahedra and $\text{MnO}_5$ trigonal-bipyramids, respectively. Contrary to what was previously reported in Ref. 33, and in agreement with the first-principles calculations of Ref. 34, we found that both layers consists of $\text{Mn}^{2+}$ in high-spin state. The two magnetic layers act as nearly independent magnetic sublattices with magnetic interactions of completely different energy scales. The honeycomb magnetic sublattice orders at about 85 K in a Neél-type AFM magnetic structure, with the Mn moments oriented parallel to the $c$-axis. This AFM state produces a zero-molecular-field on Mn atoms located in the triangular sublattice, which order magnetically in two steps at much lower temperatures. Analysis of neutron diffraction data show that the first transition, at $\approx 3$ K, is to an amplitude-modulated AFM collinear $udd$ magnetic structure described by a propagation vector $k = (\frac{1}{2}, \frac{1}{2}, 0)$. The second magnetic transition, at 2.2 K, corresponds to the development of in-plane spin components that leads to the formation of a canted “Y” magnetic structure in a plane containing the $c$-axis. Successive triangular layers are aligned antiferromagnetically along the $c$-direction. Magnetization measurements performed under applied magnetic fields revealed a 1/3 magnetization plateau and a saturation near 14.3 T of the triangular sublattice, and a spin-flop reorientation of the honeycomb sublattice at about 11 T. On the basis of these field-induced transitions, the axial magnetic anisotropy of the octahedrally coordinated Mn ions in the honeycomb lattice was estimated to be 0.010(2) meV, while the anisotropy in the pentagonal-bipyramidal en-
vironment of the triangular lattice was found to be appreciably larger, about 0.028(2) meV. Inelastic scattering measurements revealed spin-wave excitations with a strong two-dimensional character. The excitation branch associated to the honeycomb ordered state was described by using a Heisenberg model that includes first-neighbor $J_1 = 2.1(3)$ meV, and second-neighbor $J_2 = -0.3(1)$ meV in-plane exchange interactions. On the other hand, the spin-wave spectrum of the triangular sublattice yielded an estimate of the nearest-neighbor exchange interaction value of 0.08(1) meV. The determined exchange interactions were used for Monte Carlo simulations to obtain the temperature – magnetic field phase diagram. A systematic neutron diffraction study for applied magnetic-field along the $c$-axis revealed that the triangular magnetic lattice undergoes at least four intermediate magnetic phases before reaching the saturation. These phases are generally consistent with the previous theoretical predictions for TLA and with our Monte Carlo simulations and include the canted “V”, collinear $ud$, canted “2:1” and “V” in-layer spin configurations. Nevertheless, some discrepancies have been identified with regard to the spin-stacking sequence of neighboring layers. A stacking disorder and a mixture of bilayer and four-layer magnetic polytypes were revealed by the presence of highly structured magnetic diffuse scattering along the $L$-direction. An applied magnetic field perpendicular to $c$-axis is also found to produce at intermediate fields a novel magnetic state that exhibits a three-layer periodicity along the $c$-direction. In the three-layer structure the spins are alternating orientations in a quasi-orthogonal arrangement with two perpendicular and one parallel to the field direction. The appearance of such magnetic superstructures indicate that at finite temperature and intermediate fields the second nearest-neighbor interlayer interactions cannot be ignored, and may become instrumental in generating new magnetic orderings. This raises the possibility that subtle thermal and quantum fluctuations may generate effective interlayer tunneling between the triangular layers separated by honeycomb lattices. Furthermore, the formation of multiple spin-stacking sequences in a single material is very remarkable since each superstructure requires different types (AFM or FM) and different relative strengths of the interlayer nearest-neighbor and second-nearest-neighbor interactions. We hope that our findings will stimulate further theoretical studies and launch new considerations of field-induced magnetic phase diagrams in weakly-coupled triangular lattices.

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[1] C. L. Henley, Phys. Rev. Lett. 62, 2056 (1989).
[2] H. Kawamura and S. Miyashita, J. Phys. Soc. Japan 54, 4530 (1985).
[3] S. Miyashita, J. Phys. Soc. Jpn. 55, 3605 (1986).
[4] A. V. Chubukov and D. I. Golosov, J. Phys.: Condens. Matter 3, 69 (1991).
[5] R. S. Gekht and I. N. Bondarenko, Zh. Eksp. Teor. Fiz. 111, 627643 (1997).
[6] L. Seabra, T. Momoi, P. Sindzingre, and N. Shannon, Phys. Rev. B 84, 214418 (2011).
[7] O. A. Starykh, Rep. Prog. Phys. 78, 052502 (2015).
[8] D. Yamamoto, G. Marmorini, and I. Danshita, Phys. Rev. Lett. 114, 027201 (2015).
[9] L. Seabra and N. Shannon, Phys. Rev. Lett. 104, 237205 (2010).
[10] K. S. Liu and M. E. Fisher, J. Low Temp. Phys. 10, 655 (1973).
[11] M. F. Collins and O. A. Petrenko, Can. J. Phys. 75, 605 (1997), and refs therein.
[12] M. Kenzelmann, G. Lawes, A. B. Harris, G. Gasparovic, C. Broholm, A. P. Ramirez, G. A. Jorg, M. Jaime, S. Park, Q. Huang, A. Y. Shapiro and L. A. Omenets, Phys. Rev. Lett. 98, 267205 (2007).
[63] H. Kadowaki, H. Takei and K. Motoya, J. Phys.: Cond. Matter 7, 6869 (1995).