Improving constraints on gluon spin-momentum correlations in transversely polarized protons via midrapidity open-heavy-flavor electrons in $p + p$ collisions at $\sqrt{s} = 200$ GeV

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Polarized proton-proton collisions provide leading-order access to gluons, presenting an opportunity to constrain gluon spin-momentum correlations within transversely polarized protons and enhance our understanding of the three-dimensional structure of the proton. Midrapidity open-heavy-flavor production at $\sqrt{s} = 200$ GeV is dominated by gluon-gluon fusion, providing heightened sensitivity to gluon dynamics relative to other production channels. Transverse single-spin asymmetries in protons are experimentally accessible through the fine and hyperfine structure of atoms. These correlations in protons are experimentally accessible through observables known as transverse single-spin asymmetries (TSSAs). TSSAs quantify azimuthal modulations of particle production in collisions of transversely polarized nucleons with unpolarized particles, and have been measured to reach magnitudes up to 40% in hadron-hadron collisions [1–4]. Perturbative quantum chromodynamics (pQCD) calculations had predicted TSSAs of < 1% from purely perturbative contributions [5]; recent calculations suggest small additional perturbative contributions [6].

Two complementary theoretical frameworks exist for describing large TSSAs in which contributions arise from nonperturbative elements of the factorized cross section — transverse-momentum-dependent (TMD) factorization [7–9], and twist-3 factorization [10, 11] (see Ref. [12] for a recent review). The two frameworks are related, and phenomenological arguments indicate TSSAs in various reactions share a common origin in multiparton correlations [13]. The TMD framework has explicit dependence on transverse momentum $k_T$ of partons within hadrons in addition to the longitudinal momentum fraction $x$. In this approach, standard collinear parton distribution functions (PDFs) and fragmentation functions (FFs) are replaced with TMD functions. The twist-3 approach considers power-suppressed terms with respect to the hard-scattering energy scale $Q$ in the factorization expansion. Constraining TMD functions experimentally requires access to both a hard scale $Q$ and soft scale $k_T$ sensitive to partonic transverse momentum in the proton or the process of hadronization, with $Q \gg k_T$, while the higher-twist formalism only requires access to a hard scale that is represented by the transverse momentum of the produced particle ($p_T$). Twist-3 correlation functions can be written in terms of $k_T$ moments of corresponding TMDs [14]. Both frameworks have demonstrated success in modeling TSSAs in complementary regions of $p_T$ [14–16], and are relevant for constraining orbital angular momentum of quarks and gluons in protons [17–19]. At twist-3, quantum interference between standard $2 \to 2$ QCD processes and some processes involving an extra gluon must be considered, introducing additional terms to cross-section calculations depending on the number of colliding or produced hadrons. These terms encode quantum interference in twist-3 correlation functions convoluted with standard collinear PDFs and FFs. TSSAs are defined in Eq. (6), leading to the following proportionality at twist-3 [20, 21]:

$$A_N \propto \sum_{a,b,c} \phi^{(3)}_{a/A}(x_1, x_2, s_\perp) \otimes \phi_{b/B}(x') \otimes \hat{\sigma} \otimes D_{c\to C}(z) + \sum_{a,b,c} \delta\phi_{a/A}(x, s_\perp) \otimes \phi_{b/B}(x', x') \otimes \hat{\sigma}' \otimes D_{c\to C}(z) + \sum_{a,b,c} \delta\phi_{a/A}(x, s_\perp) \otimes \phi_{b/B}(x) \otimes \hat{\sigma}'' \otimes D_{c\to C}(z_1, z_2)$$

Each term with a superscript (3) corresponds to a twist-3 correlation function; the rest are at leading twist (twist-2), where $\otimes$ represents a convolution in longitudinal momentum fractions ($x$) of partons in parent protons and collinear momentum fractions ($z$) of produced hadrons with respect to their originating partons [21]. The primed variables originate from the unpolarized proton in the initial state, and the numbered variables appear in twist-3 correlators, where multiparton correlations must be considered. The $\phi$ and $D$ denote PDFs and FFs respectively, where the lowercase subscripts represent the parton type, and the uppercase subscripts represent the parent hadron. The term $\delta\phi_{a/X}(x, s_\perp)$ is the transversity distribution, a spin-spin correlation of transversely polarized quarks in transversely polarized hadrons [22].
Twist-3 correlators have more intuitive physical meaning through their relation to corresponding TMDs [7, 9, 14].

In p+p collisions at $\sqrt{s} = 200$ GeV, open-heavy-flavor (OHF) production at midrapidity is dominated by gluon-gluon fusion, receiving only a small contribution from quark-antiquark annihilation [23]. In gluon-gluon fusion events, only the first term in Eq. (1) is relevant (as the gluon does not have a transversity distribution in spin 1/2 nucleons), providing sensitivity to the trigluon correlation functions in polarized protons. The relevant twist-3 correlators for quark-antiquark annihilation and gluon-gluon fusion are the Efremov-Teryaev-Qiu-Sterman (ggq) correlator [10, 24] and the trigluon (ggg) correlators [25–29] respectively. Note that the trigluon correlators were introduced in Ref. 25, and were subsequently clarified to be two independent functions [26–29]. The ggq correlator has been experimentally constrained from global fits, discussed in Ref. 13, while the ggg correlators have received less attention, with few measurements capable of providing indirect constraints [30–35] or direct constraints [36, 37].

The TSSA for open-charm production in p+p collisions at $\sqrt{s} = 200$ GeV was calculated in Refs. [38] and [39] within the twist-3 framework. The trigluon correlators in Ref. [39] are instead constrained to the gluon Sivers TMD PDF through constraints to the gluon Sivers TMD PDF through constraining the twist-3 trigluon correlators, which are related to $k_T$ moments of the gluon Sivers PDF [14].

II. DATA ANALYSIS

The asymmetry measurements presented here utilize data recorded in 2015 by the PHENIX experiment at RHIC with collisions of transversely polarized protons on transversely polarized protons at $\sqrt{s} = 200$ GeV, and approximately 23 pb$^{-1}$ of integrated luminosity. The polarization of each beam in RHIC in 2015 is measured to be $0.58 \pm 0.02$ for the clockwise beam and $0.60 \pm 0.02$ for the counterclockwise beam, with transverse polarization direction aligned vertically to the accelerator plane. The polarization direction is varied from bunch to bunch (a) to reduce systematics related to detector coverage and performance, and (b) to allow for the polarization of a single beam to be considered at a time by averaging over the polarization directions of the opposing beam. This yields two independent data sets from which the transverse single-spin asymmetries are extracted, validated for consistency, and averaged to obtain the final result.

The PHENIX detector is described in detail in Ref. [41]. Detector subsystems used for midrapidity charged-particle detection comprise two central-arm spectrometers oriented to the left and right of the beam axis, each with acceptance $|\eta| < 0.35$ and $\Delta \phi = 0.5\pi$, and a silicon vertex detector (VTX) [45, 46] with acceptance of $|\eta| < 1$ and $\Delta \phi \approx 0.8\pi$ per arm. The central arms contain drift and pad chambers for tracking [47], electromagnetic calorimeters (EMCal) to measure energy deposition of charged particles and photons [48], and a ring-imaging Čerenkov (RICH) detector for particle identification with $\epsilon/\pi$ separation up to 5 GeV/c [49].

Curating the electron candidate sample follows the same procedure as in Ref. [41]. The electron candidate sample is composed of tracks reconstructed from hits in the drift and pad chambers of the central arm spectrometers coincident with hits in the silicon vertex detector. Tracks within $1.0 < p_T$ (GeV/c) $< 5.0$ that fire at least one photomultiplier (PMT) tube in the RICH detector, and that have a maximum displacement of 5 cm between the track projection and center of the ring of Čerenkov light as measured by the PMTs in the RICH are considered. In order to increase the electron purity, track energy $E$ deposited in the EMCal and track momentum $p$ should have a ratio near unity, as electrons deposit most of their energy in the EMCal while charged hadrons do not. The $E/p$ distribution for electron candidates in Run-15 was fit with an exponential + Gaussian, where the mean $\mu_{E/p}$ and width $\sigma_{E/p}$ of the Gaussian portion...
were extracted and used to impose the following condition \(|E/p - \mu E/p|/\sigma E/p| < 2\). Spatial displacements \(\Delta z\) and \(\Delta \phi\) of track projections and corresponding electromagnetic showers in the EMCal are required to be separated by no more than 3 standard deviations of the corresponding \(\Delta z\) and \(\Delta \phi\) distributions, and the probability that an EMCal cluster originates from an electromagnetic shower (as calculated by the shower shape) is required to be above 0.01. Tracks reconstituted in the central arms are projected to the VTX detector and fit to coincidental VTX hits via the iterative algorithm described in Ref. [51] — the fit is required to satisfy \(\chi^2/ndf < 3\). A hit is required in both of the inner two layers of the VTX to veto conversion electrons created by photons interacting with detector material, and an additional hit is required in either of the outer layers of the VTX. The narrow opening angle between \(e^+e^-\) from photonic conversions is exploited to further reduce background from conversions in the beam pipe or inner two layers of the VTX; more details for this and the VTX detector can be found in Ref. [50]. An additional requirement was placed on the number of live trigger counts per bunch crossing because the asymmetry analysis is performed bunch-by-bunch.

TSSAs can be calculated as amplitudes of sinusoidal modulations of azimuthal particle production:

\[
A_N(\phi) = \frac{\sigma^+(\phi) - \sigma^-(\phi)}{\sigma^+(\phi) + \sigma^-(\phi)} = A_N \cos \phi, \quad (6)
\]

where \(\sigma^{\pm}(\phi)\) correspond to transversely polarized cross sections for different spin orientations. Due to the nature of the azimuthal angular acceptance of the PHENIX spectrometer arms, the measurements of midrapidity TSSAs are integrated in \(\phi\) for one arm at a time. This necessitates division by an azimuthal correction factor \(\langle |\cos \phi| \rangle\). Equation (6) must also be corrected for the polarization \(P\). All of these corrections are applied as seen in the "relative luminosity formula", a well-established PHENIX method used in Refs. [31, 36, 37, 52, 53] to extract TSSAs:

\[
A_N = \frac{1}{P\langle |\cos \phi| \rangle} \frac{N^\uparrow - RN^\downarrow}{N^\uparrow + RN^\downarrow}. \quad (7)
\]

In Eq. (7), \(N^{\uparrow, \downarrow}\) are the spin-dependent yields for collisions with \(\uparrow, \downarrow\) polarized bunch crossings respectively, and \(R = L^\uparrow/L^\downarrow\) is the relative luminosity, defined as the ratio of luminosities for collisions with oppositely oriented bunch crossing polarization. The azimuthal correction factor \(\langle |\cos \phi| \rangle\) is calculated in each transverse momentum \(p_T\) bin for the electron candidate sample to account for detector efficiency effects. To serve as a cross check to Eq. (7), the asymmetries are also calculated with the "square root formula," as shown in Eq. (3). The difference in asymmetries calculated with the separate methods is taken as a systematic uncertainty \(\sigma_{\text{diff}}^{\text{sys}}\).

\[
A_N = \frac{1}{P\langle |\cos \phi| \rangle} \sqrt{\frac{N^\uparrow_R N^\downarrow_L - N^\downarrow_R N^\uparrow_L}{N^\uparrow_L N^\downarrow_R + N^\downarrow_L N^\uparrow_R}}, \quad (8)
\]

The \(L, R\) subscripts represent the left and right spectrometer arm with respect to the polarized proton-going direction. The square root formula cannot be used independently on each spectrometer arm, leading to only two independent data sets for cross validation and averaging corresponding to the two beams, rather than four independent data sets as is the case for the relative luminosity formula, corresponding to the two beams and two spectrometer arms. As an additional cross check, \(A_N\) was calculated as shown in Eq. (9) via sinusoidal fits, with 3 \(\phi\) bins per spectrometer arm, yielding consistent results with that of Eqs. (7) and (8).

Once \(A_N\) is calculated for the electron candidate sample, background corrections allow for extraction of the asymmetry for OHF decay electrons. The relevant background sources are electrons from other parent particles (\(\pi^0, \eta, \text{direct photons } \gamma, J/\psi, K_0^0, K^\pm\)) and charged hadrons misidentified as electrons (primarily \(\pi^\pm\)). To calculate the background-corrected asymmetry, the fraction of each background source present in the data sample needs to be calculated and the background asymmetries need to be measured. Equation (9) shows the formula for extracting the \(\text{OHF} \rightarrow e\) asymmetry from the electron-candidate-sample asymmetry,

\[
A_N^{\text{OHF} \rightarrow e} = \frac{A_N - f_{h^\pm} A_N^{K^\pm} - f_{J/\psi} A_N^{J/\psi}}{1 - f_{h^\pm} - f_{J/\psi} - f_{\pi^0} - f_\eta - f_\gamma}, \quad (9)
\]

where \(f_i\) represent the background fractions, \(A_N\) is the asymmetry calculated on the electron candidate sample, and \(A_N^{K^\pm}\) are the background asymmetries. The procedure to calculate the background fractions and a more detailed description of background sources can be found in Ref. [50]. This procedure is repeated in this analysis with the relevant \(p_T\) bins, and uncertainties on calculated background fractions are propagated through Eq. (9) to obtain systematic uncertainties \(\sigma_{f_{\text{sys}}}^{\text{sys}}\). Figure 1 shows the resulting background fractions for electrons and positrons combined. The \(K^\pm\) background source, which consists of Dalitz decays of \(K^\pm\) and \(K_0^\pm\), is heavily suppressed over the measured \(p_T\) range. The transverse single-spin asymmetries for \(K^\pm\) or \(K_0^\pm\) have not been measured in \(\sqrt{s} = 200\text{ GeV}\) \(p_T\) collisions. However, given that the \(K^\pm\) background fraction is on the order of \(10^{-3}\), and is the smallest contributor, it is safely neglected in the background correction procedure. The relevant background fractions are calculated separately for positrons and electrons as shown in Table 1 with resulting background fractions shown in Figures 2 and 3.

TSSAs for each background source have been measured at PHENIX at midrapidity in \(p_T\) collisions at \(\sqrt{s} = 200\text{ GeV}\). The asymmetries for photonic background sources \(\pi^0, \eta, \text{and } \gamma\) were all measured by PHENIX to...
The TSSA for \( J/\psi \) was measured with previous PHENIX data sets. The uncertainty coming from propagating the previously measured \( A_N(p^+ + p \rightarrow J/\psi + X) \) could not be improved upon in the Run-15 data given the high degree of photonic electron background. The TSSA for midrapidity \( J/\psi \) production measured in Ref. \[52\] was recalculated as a function of decay lepton \( p_T \) using PYTHIA \[54\] decay simulations for the \( J/\psi \rightarrow e^+ e^- \) channel to apply Eq. \[9\].

Due to the large contribution of statistical uncertainty coming from propagating the previously measured \( A_N(p^+ + p \rightarrow J/\psi + X) \) from Ref. \[52\] through the background correction formula (Eq. \[9\]), we report nonphotonic electron and positron asymmetries in addition to the open-heavy-flavor-decay electron and positron asymmetries. This allows the statistical precision of the open-heavy-flavor result to be improved upon given a more statistically precise measurement of \( A_N(p^+ + p \rightarrow J/\psi + X) \). Figures 4 and 5 do not show the nonphotonic electron asymmetries because they are not the focus of this paper. However, these asymmetries are shown and discussed below. The formula for extracting the nonphotonic electron (NPe) asymmetry from the electron candidate sample asymmetry is

\[
A_N^{\text{NPe}} = \frac{A_N - f_h A_N^{\text{D}}} {1 - f_{h^0} - f_{\eta} - f_{\gamma}}.
\]

Note that Eq. \[10\] only differs from Eq. \[9\] by the omission of the terms including \( J/\psi \) background fractions and asymmetries.

The TSSAs for midrapidity open charm production (\( A_N^{D} \)) predicted in Refs. \[38\] and \[39\] were also recalculated as a function of decay lepton \( p_T \) for all possible semileptonic decay channels, with decay kinematics simulated in PYTHIA \[54\] to obtain correlations between \( p_T \) and \( \phi \) of the decay lepton and \( D \) meson. The \( \phi \) distribution was then weighted in accordance with \( w(\phi^e) = 1 + A_N^{D}(p_T^D) \cos \phi^D \) in each \( p_T \) bin and then fit with \( f(\phi) = N_0(1 + A_N^{D} \cos \phi) \) to extract the decay lepton asymmetry. \( D^0 \) and \( \bar{D}^0 \) production was considered for comparisons to results from Refs. \[38\] and \[39\].

### Table I. Fractions of background \( f_i \) present in each \( p_T \) bin for the open-heavy-flavor positrons and electrons, used as inputs to the background correction procedure, and shown in Figs. 2 and 3 respectively.

| \( e^+ \) \( p_T \) range (GeV/c) | \( (p_T) \) (GeV/c) | \( f_{\eta} \)\( \pm \) | \( f_{h^0} \)\( \pm \) | \( f_{\gamma} \)\( \pm \) | \( f_{J/\psi \rightarrow e^+ e^-} \) \( f_{J/\psi \rightarrow \pi^0} \) |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 1.0 – 1.3       | 1.161           | 0.458           | 0.0738          | 0.00274         | 0.09916         | 0.0140          |
| 1.3 – 1.5       | 1.398           | 0.318           | 0.0592          | 0.00336         | 0.0195          | 0.00924         |
| 1.5 – 1.8       | 1.639           | 0.264           | 0.0582          | 0.00339         | 0.0344          | 0.0120          |
| 1.8 – 2.1       | 1.936           | 0.215           | 0.0458          | 0.00399         | 0.0520          | 0.0134          |
| 2.1 – 2.7       | 2.349           | 0.173           | 0.0394          | 0.00481         | 0.0823          | 0.0179          |
| 2.7 – 5.0       | 3.290           | 0.111           | 0.0297          | 0.00480         | 0.122           | 0.0300          |

\( e^- \) \( p_T \) range (GeV/c) | \( (p_T) \) (GeV/c) | \( f_{\eta} \)\( \pm \) | \( f_{h^0} \)\( \pm \) | \( f_{\gamma} \)\( \pm \) | \( f_{J/\psi \rightarrow e^+ e^-} \) \( f_{J/\psi \rightarrow \pi^0} \) |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 1.0 – 1.3       | 1.161           | 0.439           | 0.0704          | 0.00335         | 0.09000         | 0.0261          |
| 1.3 – 1.5       | 1.398           | 0.347           | 0.0692          | 0.00364         | 0.0206          | 0.0198          |
| 1.5 – 1.8       | 1.639           | 0.299           | 0.0665          | 0.00394         | 0.0375          | 0.0230          |
| 1.8 – 2.1       | 1.936           | 0.252           | 0.0478          | 0.00535         | 0.0577          | 0.0205          |
| 2.1 – 2.7       | 2.349           | 0.208           | 0.0429          | 0.00490         | 0.0872          | 0.0245          |
| 2.7 – 5.0       | 3.290           | 0.143           | 0.0296          | 0.00572         | 0.127           | 0.0279          |
FIG. 2. Fractions of measured positron candidates attributed to each background source ($f_i$); results are shown in Table I and used as inputs to the background correction procedure – charge (+).

FIG. 3. Fractions of measured electron candidates attributed to each background source ($f_i$); results are shown in Table I and used as inputs to the background correction procedure – charge (−).

FIG. 4. $A_N(OHF \rightarrow e^\pm)$ (red) circles and (blue) squares for positrons and electrons, respectively. Also plotted are predictions of $A_N(D^0/\bar{D}^0 \rightarrow e^\pm)$ from Ref. [38], $A_N(D^0/\bar{D}^0 + D^+/− \rightarrow e^\pm)$ from Ref. [39] for best-fit trigluon-correlator-normalization parameters, with the red/blue solid, dashed, and dotted lines corresponding to central values of the 1σ confidence intervals shown in the legend.

while $D^+$ and $D^−$ production was additionally considered when comparing to results of Ref. [39]. OHF production is dominated by open charm at the relevant kinematics, for which $D^0, \bar{D}^0, D^+, \text{ and } D^−$ cover a significant fraction. The effect of including $D^+$ and $D^−$ in comparing to Ref. [39] makes very little difference as supported by our simulations, implying that comparing to $D^0$ and $\bar{D}^0$ for Ref. [38] is sufficient. A scan over ($\lambda_f, \lambda_d$) parameter...
space and independent scans over $K_G$ and $K'_G$ were performed to generate a set of theory curves for comparison, allowing for best-fit parameters and confidence intervals to be determined from data.

III. RESULTS

The $\text{OHF} \rightarrow e^\pm$ TSSAs are plotted in Fig. 3 alongside theoretical predictions of $A_X(p^+ + p \rightarrow (D^0/D^0 \rightarrow e^\pm) + X)$ from Ref. 38 in (red/blue) solid lines, and $A_N(p^+ + p \rightarrow (D/D \rightarrow e^\pm) + X)$ from Ref. 39 in (red/blue) dashed and dotted lines, with $\lambda_f$, $\lambda_d$, $K_G$ and $K'_G$ chosen to best fit the data for the separate charges simultaneously. The measurements are consistent with zero, and are statistically more precise than previous heavy-flavor measurements. The total systematic uncertainties come from combining those associated with the background fractions, background asymmetries, and the difference in calculating $A_N$ with Eqs. (7) and (8); there is no dominant source of systematic uncertainty across charges and $p_T$ bins. The systematic uncertainty reaches at most 37% of the corresponding statistical uncertainty (see Table III), while it is typically suppressed by an order of magnitude or more. The placement of the theoretical curves in Fig. 4 differs for $e^+$ vs $e^-$ due to the contribution of the symmetric trigluon correlator having opposing signs in charm vs anticharm production, leading to constructive vs destructive interference with the antisymmetric trigluon correlator contribution for the separate charges. This allows for constraining power on all parameters. Summaries for final asymmetries with statistical and systematic uncertainties are given in Table III for OHF positrons $A_N^{\text{OHF-}e^+}$ and electrons $A_N^{\text{OHF-}e^-}$ and in Table IV for nonphotonic (NP) positrons $A_N^{\text{NP}e^+}$ and electrons $A_N^{\text{NP}e^-}$.

To determine theoretical parameters that fit the data best, $\chi^2(\lambda_f, \lambda_d)$, $\chi^2(K_G)$, and $\chi^2(K'_G)$ were calculated for the separate charges and summed to extract minimum values. The results along with 1σ confidence intervals are $\lambda_f = -0.01\pm0.03$ GeV and $\lambda_d = 0.11\pm0.09$ GeV for parameters introduced Ref. 38, and $K_G = 0.0006^{+0.0014}_{-0.0017}$, and $K'_G = 0.00025\pm0.00022$ for parameters introduced in Ref. 39. This corresponds to the first constraints on $(\lambda_f, \lambda_d)$, and is in agreement with previous constraints on $K_G$ and $K'_G$ derived in Ref. 39. Figure 3 summarizes the results of the statistical analysis performed to extract best-fit parameters $\lambda_f$ and $\lambda_d$, where the theoretical asymmetries depend on both parameters. Nicely illustrated are the constraining power of the individual charges and the necessity of combining the charges in the statistical analysis. Both charges predict that contributions from trigluon correlations are small, indicating that $\lambda_f$ and $\lambda_d$ values that result in cancellation of their contributions to the asymmetry calculation are preferred.

IV. SUMMARY

In summary, the PHENIX experiment has measured the transverse single-spin asymmetry of midrapidity open-heavy-flavor decay electrons and positrons as a function of $p_T$ in $p^+ + p$ collisions at $\sqrt{s} = 200$ GeV. Open-heavy-flavor production at RHIC is an ideal channel for probing trigluon correlations in polarized protons because initial-state $qgq$ correlations in the proton and final-state twist-3 correlations in hadronization contribute negligibly. This measurement provides constraints for the antisymmetric and symmetric trigluon correlation functions in transversely polarized protons, including the first constraints on $\lambda_f$ and $\lambda_d$ as $\lambda_f = -0.01\pm0.03$ GeV and $\lambda_d = 0.11\pm0.09$ GeV — a necessary step forward in our understanding of proton structure through correlations between proton spin and gluon momentum.

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TABLE II. Summary of final asymmetries $A_N^{OHF\rightarrow e^\pm}$ for open-heavy-flavor positrons and electrons with statistical $\sigma_{tot}^{A_N^{OHF\rightarrow e^\pm}}$ and systematic uncertainties, shown in Fig. [4]

| $e^\pm$ | $p_T$ range (GeV/c) | $<p_T>$ (GeV/c) | $A_N^{OHF\rightarrow e^\pm}$ | $A_N^{OHF\rightarrow e^\pm}$ | $A_N^{OHF\rightarrow e^\pm}$ | $A_N^{OHF\rightarrow e^\pm}$ | $A_N^{OHF\rightarrow e^\pm}$ | $A_N^{OHF\rightarrow e^\pm}$ | $A_N^{OHF\rightarrow e^\pm}$ |
|---------|---------------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| $e^+$   | 1.0–1.3             | 1.161          | -0.00256        | 0.0212          | 0.00193         | 0.00855         | 0.00264         | 0.000435        | 0.00330         | 0.00281         |
|         |                     |                |                 |                 |                 |                 |                 |                 |                 |                 |
| $e^-$   | 1.0–1.3             | 1.161          | -0.00113        | 0.0186          | 0.00273         | 0.00364         | 0.000474        | 0.00342         | 0.00688         | 0.00501         |

TABLE III. Summary of final asymmetries $A_N^{NP\rightarrow e}$ for nonphotonic positrons and electrons with statistical $\sigma_{tot}^{A_N^{NP\rightarrow e}}$ and systematic uncertainties.

| $e^\pm$ | $p_T$ range (GeV/c) | $<p_T>$ (GeV/c) | $A_N^{NP\rightarrow e}$ | $A_N^{NP\rightarrow e}$ | $A_N^{NP\rightarrow e}$ | $A_N^{NP\rightarrow e}$ | $A_N^{NP\rightarrow e}$ | $A_N^{NP\rightarrow e}$ | $A_N^{NP\rightarrow e}$ |
|---------|---------------------|----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| $e^+$   | 1.0–1.3             | 1.161          | -0.00202        | 0.0207          | 0.00115         | 0.006531        | 0.00259         | 0.006435        | 0.00286         | 0.00268         |
|         |                     |                |                 |                 |                 |                 |                 |                 |                 |                 |
| $e^-$   | 1.0–1.3             | 1.161          | -0.0106         | 0.0182          | 0.00338         | 0.00203         | 0.00242         | 0.000120        | 0.00474         | 0.00343         |

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