Recent Timing Studies on RXTE Observations
of 4U 1538-52

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Abstract. The high mass X-ray binary pulsar 4U 1538-52 was observed between July 31 and August 7, 2003. Using these observations, we determined new orbital epochs for both circular and elliptical orbit models. The orbital epochs for both orbit solutions agreed with each other and yielded an orbital period derivative \( \dot{P}/P = (0.4 \pm 1.8) \times 10^{-6} \text{ yr}^{-1} \). This value is consistent with the earlier measurement of \( \dot{P}/P = (2.9 \pm 2.1) \times 10^{-6} \text{ yr}^{-1} \) at the 1σ level and gives only an upper limit to the orbital period decay. Our determination of the pulse frequency showed that the source spun up at an average rate of \( 2.76 \times 10^{-14} \text{ Hz sec}^{-1} \) between 1991 and 2003.

Key words. X-rays:binaries; Stars:neutron; pulsars:individual:4U 1538-52; accretion, accretion disks

1. Introduction

The source 4U 1538-52 was discovered using the Uhuru satellite (Giacconi et al. 1974). X-ray pulsations with a period of 529 seconds were detected from two independent satellite experiments: Ariel 5 (Davidson 1977) and OSO-8 (Becker et al., 1977). OSO-8 observations also revealed a clear orbital modulation at 3.7 days and evidence of an eclipse lasting \( \sim 0.51 \) days. The optical companion of 4U 1538-52 was identified to be the B0 I giant QV
Nor (Parkes, Murdin & Mason 1978). BATSE observations of this source permitted the
construction of long-term pulse frequency and intensity histories (Rubin, Finger, Scott
et al. 1997). In the pulse frequency history, Rubin et al. (1997) found short-term pulse
frequency changes of either sign, and a power density spectrum of fluctuations of the
pulse frequency derivative that is consistent with white torque noise on timescales from
16 to 1600 days.

From RXTE observations, Clark (2000) obtained new orbital parameters of the
source which provided marginal evidence of orbital decay, i.e., they found $P_{orb}/P_{orb} =
(−2.9 ± 2.1) \times 10^{-5}$ yr$^{-1}$. In this work, we present new orbital epoch and pulse frequency
measurements based on our analysis of archival RXTE observations of 4U 1538-52.

2. Observations

The observations of 4U 1538-52 took place between July 31 and August 7, 2003 (MJD
52851 - 52858) and accumulated a total nominal exposure of $\sim$ 75 ksec. The results pre-
sented here are based on data collected with the Proportional Counter Array (PCA,
Jahoda et al., 1996). The PCA instrument consists of an array of five collimated
xenon/methane multianode proportional counters. The total effective area is approxi-
mately 6250 cm$^2$ and the field of view is $\sim 1^\circ$ FWHM. The nominal energy range of the
PCA extends from 2 to 60 keV.

3. Determination of Orbital Epoch and Pulse Frequency

Background light curves and X-ray spectra were generated by using background estima-
tor models based on the rate of very large events (VLE), detector activation, and cosmic
X-ray background. The background light curves were subtracted from the source light
curve obtained from the binned Good Xenon data. For 4U 1538-52, X-ray emission
coming from the galactic ridge is only a few percent of the total X-ray emission which
should not affect our timing analysis (see Makishima et al. 1987),
so we did not include an estimation of the galactic ridge emission in our
analysis. In Figure 1, we present the background subtracted light curve. Although the
number of active PCUs varied from 1 to 4 during the observations, Figure 1 shows count
rates adjusted as if 5 PCUs had been active using the "correctlc" tool in HEASOFT
6. For the timing analysis, we corrected the light curve to the barycenter of the solar
system. We also corrected this barycentered light curve for binary orbital motion using
both circular and elliptical orbital models given in Table 1 (see also Clark (2000)). Then
a template pulse profile was created by folding the light curve into one master profile.
Pulse profiles were also made from each of the 12 independent RXTE observations seen
in Figure 1.
In order to find the pulse frequency and a new orbital epoch, we obtained 12 pulse arrival times through the \sim 2 binary orbits using a cross-correlation technique. In the pulse timing analysis, we used the method of harmonic representation of pulse profiles, which was proposed by Deeter & Boynton (1985). In this method, the pulse profiles for each orbit and the master profile are expressed in terms of harmonic series. We used 10-term unweighted harmonic series to cross-correlate the template pulse profile with the pulse profiles for each RXTE observation. The maximum value of the cross-correlation is analytically well-defined and does not depend on the phase binning of the pulses.

The source 4U 1538-52 has a variable pulse profile which affects the pulse timing. In order to estimate the errors in the arrival times, the light curve of each RXTE observation was divided into approximately 4-5 equal subsets and new arrival times were estimated. The standard deviation of the arrival times obtained from each subset of the observation was taken to be the uncertainty in the arrival time for that observation.

**Arrival time delays** may arise from the change of the pulse frequency during the observation (or intrinsic pulse frequency derivative) and from the **differences between the assumed and actual orbital and pulse parameters** (Deeter, Boynton and Pravdo 1981),

\[
\delta \phi = \phi_o + \delta \nu (t - t_o) + \frac{1}{2} \nu(t - t_o)^2 - \delta \nu \frac{2 \pi \delta T_{\pi/2}}{P_{\text{orbit}}} \frac{a \sin \iota}{c \cos \iota},
\]

where \(\phi_o\) is the initial phase, \(\nu\) is the spin frequency, \(T_{\pi/2}\) is the time to half the pulse period, \(P_{\text{orbit}}\) is the orbital period, \(a\) is the semi-major axis, \(\iota\) is the orbital inclination, and \(c\) is the velocity of light.
where $\delta \phi$ is the pulse phase offset deduced from the pulse timing analysis, $t_o$ is the mid-time of the observation, $\phi_o$ is the residual phase offset at $t_o$, $\nu$ is the pulse frequency at time $t_o$, $\dot{\nu}$ is the pulse frequency derivative of the source, $T_{\pi/2}$ is the orbital epoch when the mean orbital longitude is equal to 90 degrees, $P_{\text{orb}}$ is the orbital period and $l_n = 2\pi(t_n - T_{\pi/2})/P_{\text{orb}} + \pi/2$ is the mean orbital longitude at $t_n$. Corrected values of orbital and pulse parameters $\delta \nu$, $\delta T_{\pi/2}$ and $\dot{\nu}$ were estimated from the fits of above expression to pulse phase residuals.

Table 1 presents the result of fits for both orbital and pulse parameters. We also reestimated the orbital epochs by varying the projected orbital radius $(a_x/c)\sin i$ in the range of its uncertainty ($\pm 1\sigma$) and found that the resulting orbital epochs are consistent with the best fit value at the $1\sigma$ level. The error in the orbital epoch due to an error in $(a_x/c)\sin i$ may also be expressed (Deeter, Boynton and Pravdo 1981) as

$$\sigma_{T_{\pi/2}} = \frac{P_{\text{orb}}\sigma_{(a_x/c)\sin i}}{2\pi a_x/c\sin i} \sim 0.0073 \text{ days}$$

where $\sigma_{(a_x/c)\sin i}$ is the uncertainty in the projected orbital radius. This value is small relative to our error estimate for the orbital epoch (see Table 1). In Figure 2, we present the arrival time delay, the best fit elliptical orbit model, and arrival time residuals.

As seen from Table 1, the orbital epochs for circular and elliptical orbital models agree with each other at the $1\sigma$ level. In order to check our technique, we extracted observations of 4U 1538-52 done in 1997 (MJD 50449.93-50453.69) and estimated orbital epochs for those observations. The results agreed with the orbital epochs given by Clark (2000).

In Table 2, we present the orbital epoch measurements from different observatories and orbital cycle number ($n$). In Figure 3, we present observed minus calculated values of orbital epochs ($T_{\pi/2} - n < P_{\text{orb}}$ $> - T_{\pi/2} - n < P_{\text{orb}}$ $>>$) relative to the constant orbital period ($< P_{\text{orb}} > = 3.7228366$ days). A quadratic fit to the epochs from all experiments yielded an estimate of the rate of period change $\dot{P}_{\text{orb}}/P_{\text{orb}} = (0.4 \pm 1.8) \times 10^{-6}$ yr$^{-1}$. In Figure 4, we display the long-term pulse frequency history of the source.

4. Discussion

Before CGRO observations, 4U 1538-52 had been found to have a long-term spin down trend. A linear fit to pre-CGRO pulse frequency history gives $\dot{\nu}/\nu \sim -8 \times 10^{-12}$ s$^{-1}$ and a linear fit to CGRO and our RXTE result yields $\dot{\nu}/\nu \sim 1.45 \times 10^{-11}$ s$^{-1}$. Rubin et al (1997) constructed the power spectrum of pulse frequency derivative fluctuations. Their analysis showed that the pulse frequency derivative fluctuations can be explained on timescales from 16 to 1600 days with an average white noise strength of $(7.6 \pm 1.6) \times 10^{-21}$ Hz$^{-1/2}$ Hz$^{-1}$. A random walk in pulse frequency (or white noise in pulse frequency derivative) can be explained as a sequence of steps in pulse frequency with an RMS value of $< (\delta \nu^2) >$ which occur at a constant rate $R$. Then the RMS variation
of the pulse frequency scales with elapsed time $\tau$ as $\langle (\Delta \nu)^2 \rangle = R < (\delta \nu)^2 > \tau$ (Hz), where $S = R < \delta \nu^2 >$ is defined as noise strength. Then, RMS scaling for the pulse

Table 1. Orbital Parameters of 4U 1538-52

| Parameter               | Elliptical Orbit | Circular Orbit |
|-------------------------|------------------|----------------|
| $T_{s/2}$ Orbital Epoch (MJD) | 52855.0421±0.025  | 52855.0441±0.025 |
| $a_x \sin i$ (lt-s)$^a$ | 56.6±0.7         | 54.3±0.6       |
| $e^a$                    | 0.174±0.015      |                |
| $\omega^a$(deg)         | 64±9             |                |
| $P_{\text{orbit}}^a$    | 3.7228366±0.000032 | 3.7228366±0.000032 |
| Epoch (MJD)              | 52855.0585±0.025  | 52855.0585±0.025 |
| $P_{\text{pulse}}$ (s)  | 526.8551±0.016    | 526.8535±0.013  |
| $\dot{\nu}$ (Hz s$^{-1}$) | (2.838±4.124)$\times 10^{-13}$ | (2.241±2.764)$\times 10^{-13}$ |
| reduced $\chi^2$        | 1.44             | 1.0            |

$^a$ Taken from Clark (2000)
Fig. 3 – The phase residuals of orbital epoch for 4U 1538-52. The orbital phases are estimated relative the constant orbital period \( (T_{\pi/2} - n < P_{\text{orbit}} > - < T_{\pi/2} - n < P_{\text{orbit}} >>) \), where \( n \) is the orbital cycle number (see Table 2). The rightmost point corresponds to the most recent RXTE observation of ID 80016.

Frequency derivatives can be obtained as \( < (\Delta \dot{\nu})^2 >^{1/2} = (S/\tau)^{1/2} \text{Hz.s}^{-1} \). As seen from Table 1, in our fits, upper limits on intrinsic pulse frequency derivatives are 7-10 times higher than the long-term spin up rates. If white noise in the pulse frequency derivative can be interpolated to a few days, then the upper limit on the change of frequency derivative obtained from a ~ 1 week observation should typically have a magnitude

**Table 2. Orbital epochs by pulse timing analysis**

| Experiment | Orbit Number | Orbital Epoch (MJD) | Reference                     |
|------------|--------------|---------------------|-------------------------------|
| OSO 8      | -1128        | 43015.800± 0.1      | Becker et al., 1977           |
| Tenma      | -457         | 45517.660± 0.050    | Makishima et al., 1987        |
| Ginga      | 0            | 47221.474± 0.020    | Corbet et al., 1993           |
| BATSE 370  | 48600.979± 0.027 | Rubin et al., 1997 |                               |
| BATSE 478  | 49003.629± 0.022 | Rubin et al., 1997 |                               |
| BATSE 584  | 49398.855± 0.029 | Rubin et al., 1997 |                               |
| BATSE 691  | 49797.781± 0.022 | Rubin et al., 1997 |                               |
| RXTE 866   | 50450.206± 0.014 | Clark 2000         |                               |
| RXTE 1511  | 52855.0421± 0.025 | present work       |                               |
that can be estimated from $< (\Delta \dot{\nu})^2 _{week} > = < (\Delta \dot{\nu})^2 _{1600 days} > \times 15^2$. This value is $15/7 - 15/10$ times higher than the measured upper limit values. Therefore the measured upper limits on the intrinsic pulse frequency derivatives for 1 week are consistent with the values from the extrapolation of the power spectrum within a factor of a few.

Previous marginal measurement of change in the orbital period, was $(-2.9 \pm 2.1) \times 10^{-6}$ yr$^{-1}$ (Clark 2000), and our new value for the orbital period change, $\dot{P}/P = (0.4 \pm 1.8) \times 10^{-6}$ yr$^{-1}$, are consistent with zero. These two measurements are consistent with each other in $1\sigma$ level.

In most of the X-ray binaries with accretion powered pulsars, the evolution of the orbital period seems to be too slow to be detectable. Yet there are still some such systems in which this evolution was measured and $\dot{P}/P$ were reported. These systems include Cen X-3 with $(-1.8 \pm 0.1) \times 10^{-6}$ yr$^{-1}$ (Kelley et al. 1983; Nagase et al. 1992), Her X-1 with $(-1.32 \pm 0.16) \times 10^{-8}$ yr$^{-1}$ (Deeter et al. 1991), SMC X-1 with $(-3.36 \pm 0.02) \times 10^{-6}$ yr$^{-1}$ (Levine et al. 1993), Cyg X-3 with $(1.17 \pm 0.44) \times 10^{-6}$ yr$^{-1}$ (Kitamoto et al. 1995), 4U 1700-37 with $(3.3 \pm 0.6) \times 10^{-6}$ yr$^{-1}$ (Rubin et al. 1996), and LMC X-4 with $(-9.8 \pm 0.7) \times 10^{-7}$ yr$^{-1}$ (Levine et al. 2000). Change in the orbital period of Cyg X-3 was associated with the mass loss rate from the Wolf-Rayet companion star. For 4U 1700-37, the major cause of orbital period change was also thought to be mass loss from the
companion star. For Her X-1, mass loss and mass transfer from the companion were proposed to be the reasons of the change in the orbital period of the system.

On the other hand, for the high mass X-ray binary systems Cen X-3, LMC X-4 and SMC X-1, the major cause of change in the orbital period is likely to be tidal interactions (Kelley et al. 1983; Levine et al. 2000; Levine et al. 1993). For these three systems, orbital period decreases (i.e. derivative of the orbital period is negative). Our new measurement of orbital period change ($\dot{P}/P$) gives the value of about $-10^{-6}$ yr$^{-1}$ which is similar to the observed values of SMC X-1 and Cen X-3. Further observations can give further information about the orbital period change of this source.

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