Stability SCAD: a powerful approach to detect interactions in large-scale genomic study

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Abstract

Background: Evidence suggests that common complex diseases may be partially due to SNP-SNP interactions, but such detection is yet to be fully established in a high-dimensional small-sample (small-n-large-p) study. A number of penalized regression techniques are gaining popularity within the statistical community, and are now being applied to detect interactions. These techniques tend to be over-fitting, and are prone to false positives. The recently developed stability least absolute shrinkage and selection operator (SLASSO) has been used to control family-wise error rate, but often at the expense of power (and thus false negative results).

Results: Here, we propose an alternative stability selection procedure known as stability smoothly clipped absolute deviation (SSCAD). Briefly, this method applies a smoothly clipped absolute deviation (SCAD) algorithm to multiple sub-samples, and then identifies cluster ensemble of interactions across the sub-samples. The proposed method was compared with SLASSO and two kinds of traditional penalized methods by intensive simulation. The simulation revealed higher power and lower false discovery rate (FDR) with SCAD. An analysis using the new method on the previously published GWAS of lung cancer confirmed all significant interactions identified with SLASSO, and identified two additional interactions not reported with SLASSO analysis.

Conclusions: Based on the results obtained in this study, SCAD presents to be a powerful procedure for the detection of SNP-SNP interactions in large-scale genomic data.

Keywords: Genome-wide association study (GWAS), Interaction, Least absolute shrinkage and selection operator (LASSO), Penalized logistic regression, Smoothly clipped absolute deviation (SCAD), Stability selection

Background

High-dimensional genomic data are becoming increasingly available to assist in the identification of genetic factors for complex diseases such as lung cancer. In particular, genome-wide association studies (GWAS) have implicated a variety of genetic variants in many diseases, while only a small fraction of phenotypic variation was explained by those. This suggests that multi-locus gene-gene or gene-environment interactions must be considered [1].

Gene-gene interactions could be detected using a variety of methods [2]. For example, multifactor dimensionality reduction (MDR, [3]) is a non-parametric and model-free method that does not require any assumption of genetic mode of inheritance. However, MDR is inefficient in handling large scale genetic datasets [4]. Penalized regression methods such as least absolute shrinkage and selection operator (LASSO) [5] and smoothly clipped absolute deviation (SCAD) [6] are also widely used for high-dimensional data. LASSO is a useful tool for detecting gene-gene interactions with a broad range of simulations [7]. SCAD penalty has an oracle property, and thus it is more consistent with the actual effects than LASSO [6]. The cross-validation is usually used for the choice of the amount of regularization in penalized regression methods (e.g., LASSO and SCAD), but it often includes too many noise variables. In an attempt to minimize such a problem, a modified LASSO penalized method, stability LASSO (sLASSO), has been proposed to unify optimal shrinkage and variable selection in GWAS ([8]). Stability selection controls false discovery rate and renders cross-validation practically unnecessary.
(2011) claimed that γLASSO could accurately identify the most important regions of GWAS, but in a simulation study γLASSO offers less power than the simpler and less computationally intensive methods of marginal association testing [8].

It has been shown that the LASSO penalty could produce a bias even in the simple regression setting due to its linear increase of penalty on regression coefficients. To remedy this bias issue, a non-concave penalty such as SCAD penalty was proposed. SCAD has the so-called oracle property, meaning that, in the asymptotic sense, it performs as effectively as if an analyst had known in advance which coefficients were zero and which ones were nonzero [6]. SCAD is capable of achieving the sparse variance which coefficients were zero and which ones were penalized as effectively as if an analyst had known in advance which coefficients were zero and which ones were nonzero [6]. SCAD is capable of achieving the sparse variance which coefficients were zero and which ones were nonzero [6].

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The following penalty functions are used in LASSO and SCAD, respectively:

\[
p_λ(θ_j) = λ |θ_j|,
\]

\[
\hat{p}_λ(θ) = λ \{1(|θ| ≤ λ) + \frac{a(λ - |θ|)}{(a - 1)λ} \mathbb{1}(λ > |θ|)\},
\]

where \(a\) is a fixed constant larger than 2, the notation \(\mathbb{1}\) stands for the positive part, and \(\mathbb{1}(\cdot)\) denotes the indicator function.

When the penalized logistic regression model is fitted, a predetermined number of the components of \(θ\) can be forced to zero by tuning \(λ\) to a certain value. For a specific variable, estimation of the coefficient is non-zero if the coefficient exceeds the threshold or equals to zero. Thus the selection of tuning parameter is a crucial step at the application of penalized likelihood. This is usually accomplished with cross validation. We used cross validation predictive area under the ROC curve to choose the appropriate tuning parameter.

LASSO and SCAD with cross-validated tuning parameter selection often lead to the inclusion of too many noise variables for high-dimensional data [9]. For variable selection in small-n-large-p genomic data, choosing the amount of regularization is more challenging than predicting where a cross-validation scheme can be used. A false variable in variable selection may lead to apparent association with a disease phenotype either through chance or correlation with the true variables. Studies using high-dimensional data often need to be validated due to false variables. Another practical issue here is reducing false variables while maintaining the power to detect relevant variables. To address this problem, Meinshausen and Büßmann [9] proposed a stability selection procedure that is relatively insensitive to the choice of tuning parameter [9].

In the current study, SCAD was used in variable selection in each sub-sample, and then stability selection was used to identify consensus ensemble of solutions.

**Penalized logistic regression for case-control GWAS**

Let \(y_i\) denote the disease status of the individual \(i\) (\(i = 1, \ldots, n\)): 1 for case and 0 for control. The SNP of individual \(i\), \(x_{ij}\), is formatted as the count of a particular allele (0, 1, or 2) where \(j = 1, \ldots, m\). The logistic model below includes SNP-SNP interaction terms:

\[
\log \frac{π_i}{1 - π_i} = β_0 + \sum_{j=1}^{m} β_j x_{ij} + \sum_{j<k} ξ_{jk} x_{ij} x_{ik}, i = 1, \ldots, n,
\]

where \(x_{ij}\) and \(x_{ij} x_{ik}\) are main effect and interaction features, respectively.

Penalized likelihood method makes the fitting of a logistic model with small-n-large-p computationally feasible. It also provides a mechanism for feature selection. \(L(θ)\) denotes the likelihood function of the above logistic model (1), where \(θ\) consists of those \(β\) and \(ξ\). The penalized log-likelihood function takes the form

\[
I_p(θ) = -2 \log L(θ) + \sum_j p_λ(θ_j),
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where \(p_λ(•)\) is the penalty function characterized by a tuning parameter \(λ\). The following penalty functions are used in LASSO and SCAD, respectively:

LASSO penalty: \(p_λ(θ_j) = λ |θ_j|\),

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**Methods**

**Ethics statement**

This collaborative study was approved by the institutional review boards of China Medical University, Tongji Medical College, Fudan University, Nanjing Medical University, and Guangzhou Medical College with written informed consent from all participants.

**Penalized logistic regression for case-control GWAS**

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**Stability selection procedure**

a) Meinshausen and Büßmann (MB) stability selection methodology

Stability selection seeks to identify the non-zero entries \(S = \{k: θ_k ≠ 0\}\) of a sparse parameter vector in above penalized logistic regression model (2). Assuming that the set \(I\) is a uniform random sub-sample of the index set \(\{1, \ldots, n\}\), the index set was used to subsample from the data to yield a subset \(Z(I)\). For the subset and a given regularization parameter \(λ \in Λ\), penalized regression procedure was used to yield an estimate of \(θ_λ\), i.e., \(\hat{θ}_λ(I)\). Selection variable set was denoted as

\[
\hat{S}(I) = \{ k : \hat{θ}_k = 0 \}.
\]
The conditional selection probability of the $k$-th covariate was defined as
\[
\hat{\Pi}_k^\lambda = P\{k \in \hat{S}_\lambda^\lambda(I) | X, y\}. \tag{3}
\]

The selection probabilities were naturally estimated by Monte Carlo method averaging over $B$ times independent sub-sampling. Variables with high selection probabilities were retained, while those with low selection probabilities were discarded. For a cut-off $\pi_{thr}$ with $0 < \pi_{thr} < 1$ and a set of regularization parameters $\Lambda$, the stable selection variables set was defined as
\[
\hat{S}_{\text{stable}} = \left\{ k : \max_{\lambda \in \Lambda} \hat{\Pi}_k^\lambda \geq \pi_{thr} \right\}. \tag{4}
\]

The basic idea of the stability selection is to repeat the feature selection process in many randomly perturbed subsamples (e.g., by bootstrapping the samples in the original data set), and to include features that are relevant to majority of the subsamples. The baseline of the stability selection procedure is explained below:

Given a cut-off, compute the stable selection variables set $\hat{S}_{\text{stable}} = \left\{ k : \max_{\lambda \in \Lambda} \hat{\Pi}_k^\lambda \geq \pi_{thr} \right\}$.

The threshold value $\pi_{thr}$ is a tuning parameter whose influence is very small. In principle, the tuning parameter of MB is based on the following theorem 1 of Meinshausen and Bühlmann.

**Theorem 1 (error control).** Assuming that the distribution of $\{1_{k \in \hat{S}_\lambda^\lambda(I)} : k \in \mathbb{N}\}$ is exchangeable for $\lambda \in \Lambda$, and the original procedure is not worse than random guessing. Let $q_\lambda$ be the average number of selected variables, $q_\Lambda = E\left(\bigcup_{k=1}^p \hat{S}_\lambda^\lambda(I)\right)$, the expected number $V$ of falsely selected variables is then bounded for $\pi_{thr} \in (1/2, 1]$ by
\[
E(V) \leq \frac{1}{2\pi_{thr} - 1} \frac{q_\lambda^2}{p}. \tag{5}
\]

b) Improvements of the MB stability selection
In the current study (where $p \gg n$), the primary goal was controlling the false discovery rate ($FDR$):

**Input:** Data set $(X, y)$, $B$ times independent sub-samples, a set of regularization parameters $\Lambda$

**Output:** Selection probabilities $(\hat{\Pi}_k^\lambda)_{k=1,...,p, \lambda \in \Lambda}$ and stable selection variables set $\hat{S}_{\text{stable}}$

for $i \in \{1, ..., B\}$ do
  Draw a subsample of $\{1, \cdots, n\}$ with a size $[n/2]$ without replacement, denoted it by $I$;
  for $\lambda \in \Lambda$ do
    Run a variable selection algorithm on $I$ with the regularization parameter $\lambda$;
    Save the active set $\hat{\Theta}_\lambda^I(I)$;
  end
end

for $k \in \{1, ..., p\}$ do
  for $\lambda \in \Lambda$ do
    Compute the selection probability $\hat{\Pi}_k^\lambda = P\{k \in \hat{S}_\lambda^\lambda(I) | X, y\}$;
  end
end
\[
\text{FDR} = E(V/|S_{\text{stable}}|) = E(V)/q_A \leq \frac{1}{2m_{\text{thr}}-1} \frac{q_A}{p}.
\]

(6)

An advantage of the stability selection is that the choice of the regularization parameters \( \Lambda \) does not have strong influence on the results, as long as \( \lambda \) is varied within a reasonable range [9]. To control FDR, we first chose a fixed regularization region \( \Lambda \), and then chose the selective probability threshold \( \pi_{\text{thr}} \) according to the above inequality (6).

We set a fixed regularization region as \( \Lambda = [\lambda_{\text{min}}, \lambda_{\text{max}}] \), which was decided by the number of selected variables \( q \) as follow: \( \lambda_{\text{max}} \) corresponded to the variable that first entered the regularization path and \( \lambda_{\text{min}} \) was chosen such that the first \( q \) variables that appeared in the regularization path, mathematically, \( \lambda_{\text{min}} \) was chosen such that \( \{ |\lambda_{\text{lim}} \leq \lambda \leq \lambda_{\text{lim}}^\dagger| \} \leq q \). The value of \( q \) was chosen a priori to yield a non-trivial bound (see discussion on the paper by Meinshausen and Bühlmann [9]), i.e. \( q = O(\sqrt{2m_{\text{thr}}-1}/p) \). The choice of \( q \) in stability selection does not have a strong impact on the FDR [9]. We used a conservative estimate of \( q \) (the square root of the number of predictors) in the discovery stage.

For the fixed regularization region, we applied the SCAD procedure to every subsample, \( \pi_{\text{thr}} = \left( 1 + \frac{q_A}{pa} \right) / 2 \), if \( q_A \leq pa \).

(7)

Unfortunately, given the nature of genetic data, the exact hypotheses required by the theorem of Meinshausen and Bühlmann are unlikely to hold [9]. In particular, the exchangeability assumption of Theorem 1 about the indicator random variables \( \{ 1_{\{ k \in S^i \}} \} \) is questionable due to the correlations among the markers induced by linkage disequilibrium. We worried that the false positives of stability selection might be grossly wrong in our genetic data. So we adopted the method described in Alexander and Lange [8] to make a rough check on the false discovery rate of stability selection. We randomly permuted the phenotype vector \( y \) for all participants, firstly. We then performed the stability selection procedure on the permutation sample and obtained the selection probability of the variable corresponding to the maximum test statistic in the association analysis, and finally compared the selection probability with the cut-off calculated from the theorem of Meinshausen and Bühlmann.

**Data simulation**

\( \$ \)SCAD selection procedure was compared with LASSO, SCAD, and \( \$ \)LASSO under a variety of interaction models.

**Genotype simulation**

HAPGEN (v2.2.0) program [10] was used to simulate genotype information. The simulation parameters for SNP frequencies and variance structure were extracted from HapMap3 JPT + CHB that includes SNPs located within \( \pm 20 \)-kb of \( ABCC4 \) (ATP-binding cassette subfamily C member 4) at 13q31. The legend file for the SNP markers, and the fine scale recombination rate were downloaded from the HapMap website (http://hapmap.ncbi.nlm.nih.gov/downloads/index.html.en). After quality control, 327 common SNPs remained (with the exclusion criteria: missing data of SNPs > 5%, minor allele frequency < 5%, Hardy-Weinberg \( p \)-value < \( 10^{-4} \)). The linkage disequilibrium (LD) pattern is shown in Figure 1.

**Phenotype simulations**

Genetic interaction model was applied for case/control phenotypes simulations. During the phenotype simulation, we took \( m = 327 \) (\( C_m^2 = 53301 \) two-way interactions) and randomly selected causal SNPs from different haplotype blocks. The blocks were computed through Haploview v4.2 by standard expectation-maximization algorithm [11], which partitioned the region into segments of strong linkage disequilibrium (LD). A total of 26 blocks were generated with a minimum size of 2 markers and a maximum size of 64 markers. All the causal SNPs and SNP-SNP interactions were assumed to improve the risk (\( OR = 1.3, 1.4, \) and 1.5, respectively); wherein we let \( y_i \) denote the phenotype value of subject \( i \), which is obtained according to the logistic regression model (1).

We conducted simulations to evaluate selection performance of the LASSO, SCAD, \( \$ \)LASSO and \( \$ \)SCAD procedures under the following scenarios:

(A). The interactive SNPs have no main effects:
\[ \beta_j = 0 \text{ for all } j, \] and \( \xi_{jk} = 0 \) for some randomly chosen \( j, k \).

(B). Only one SNP in the SNP-SNP interaction pair has a main effect:
\[ \xi_{jk} = 0 \text{ and } \beta_j \neq 0 \text{ for some randomly chosen } j, k. \]

(C). Both interactive SNPs have main effects:
\[ \xi_{jk} \neq 0, \beta_j \neq 0 \text{ and } \beta_k \neq 0 \text{ for some randomly chosen } j, k. \]

The odds ratio parameters are shown in Table 1. Since there are only a few etiological loci - only a few of the
coefficients in the model are nonzero - the phenomenon is referred to as being sparse.

For every simulation scenario of phenotype in Table 1, the phenotype $y_i$ was generated based on the simulated SNPs by HAPGEN 2 using the above-mentioned logistic regression model (1). We simulated the population with an equal number of cases and controls ($n/2 = 10,000$) with 200 replicate data sets, and then 1,000 cases and 1,000 controls were randomly sampled from the population to form one sample set. Next, we performed different variable selection methods for each sample set.

Simulated data analysis

R software (version 2.14.0, The R Foundation for Statistical Computing) was used to perform the simulation. The package “glmnet” and modified package “ncvreg” were used for LASSO and SCAD analysis, respectively. For stability selection, we chose $B = 500$ times independent sub-samples with a size of 500 cases and 500 controls from each 1000-1000 cases-controls sample set.

Application

The study subjects were from an ongoing two-center (Nanjing and Beijing, China) GWAS of lung cancer in China. At recruitment, written informed consent was obtained from each subject. The study was approved by the institutional review boards of each participating institution. The details of population and other related information were described previously [12]. A systematic quality control procedure was applied for both SNPs and individuals. SNPs were excluded if they did not map on autosomal chromosomes, with minor allele frequency < 0.05, with call rate < 95%, with $p < 1 \times 10^{-5}$ for Hardy-Weinberg equilibrium in combined samples of two studies or $p < 1 \times 10^{-4}$ in either the Nanjing or Beijing study samples. We removed samples with a call rate of < 95%, ambiguous gender, familial relationships, extreme heterozygosity rate, and outliers. Briefly, there were 1,473 cases and 1,962 controls in the Nanjing center, 858 cases and 1,115 controls in the Beijing center after quality control.

A multi-stage strategy is often used for detecting interactions on a genome-wide scale. The method proposed in the current study could not be directly applied to such high dimensional data.

| Feature of simulated set | Scenario | Number of nonzero main effects | Number of nonzero interactions | Locations of causal variants | Designed OR |
|--------------------------|----------|-------------------------------|-------------------------------|-----------------------------|-------------|
| ABC4 (327 SNPs, 53301 two-way interactions) | A1/A2/A3 | 0 | 1 | SNP33 × SNP197 | 1.5/1.4/1.3 |
| | B1/B2/B3 | 1 | 1 | SNP18 + SNP18 × SNP134 | 1.5/1.4/1.3 |
| | C1/C2/C3 | 2 | 1 | SNP33 + SNP134 + SNP33 × SNP134 | 1.5/1.4/1.3 |

Abbreviations: ABC4 ATP-binding cassette sub-family C member 4, OR odds ratio, SNP single nucleotide polymorphisms.
applied to genome-wide scale SNPs data since it is too computationally intensive to exhaustively search for all SNP pairs. A filtering method could be helpful, as explained below using the achPathway pathway (a role of nicotinic acetylcholine receptors in the regulation of apoptosis). This pathway is one of the top pathways associated with lung cancer risk in the Han Chinese population. Several studies have shown that the nicotinic acetylcholine receptors in the regulation of cell proliferation. Several studies have shown that the nicotinic acetylcholine receptors can induce cell proliferation as well as angiogenesis [13]. The achPathway pathway includes the genes PIK3R1, PTK2B, PTK2, AKT1, PIK3CG, FASLG, MUSK, CHRNG, RAPSN, BAD, FOXO3, TERT, CHRNB1, PIK3CA, SRC and YWHAH. All SNPs are mapped into genes within 20 kb downstream or upstream. All together, there are 344 common SNPs. We conducted an exhaustive search (\(C_{344}^2 = 58996\)) of two-way interaction in the pathway. Covariates including age, gender, pack-year of smoking, and the first two principal components, which have been proposed to sufficiently adjust for population stratification derived from EIGENSTRAT 3.0 [14], were adjusted in the stability selection procedure [12].

To increase confidence in the selection of significant interactions from tens of thousands of SNP pairs, interactions findings often need to be replicated in independent studies. We adopted a two-stage strategy in the current study. In the initial discovery stage, we used SLASSO and \(\ell\)SCAD to select significant SNP-SNP interactions using the data from the Nanjing center. In the replication stage, the findings in the initial step were validated using the data from the Beijing center with SLASSO and \(\ell\)SCAD. A slight variation was made to calibrate the significant threshold for the replication phase (i.e., we set the initial fixed number of variables in Beijing study as the number of selected variables in the discovery stage).

The SNP pairs were selected using the following criteria: (i) the interaction had the selection probability \(p_I \geq \pi_{thr1}\) in the Nanjing study, while in the Beijing study the selection probability was \(p_I \geq \pi_{thr2}\) (\(\pi_{thr1}\) and \(\pi_{thr2}\) are the significant thresholds of the Nanjing and Beijing studies, corresponding to the control of the FDR under 0.1); (ii) the Nanjing and Beijing centers both demonstrated identical direction of odds ratios for the two SNPs, with their interaction derived from penalized logistic regression.

**Results**

**Result of simulation**

We evaluated the performance of different variable selection procedures using four established statistical indexes, including the true positive rate (TPR):

\[
TPR = \frac{TP}{TP + FN},
\]

the Matthews correlation coefficient (MCC) [15]:

\[
MCC = \frac{TP \times TN - FP \times FN}{\sqrt{(TP + FP)(TP + FN)(TN + FP)(TN + FN)}},
\]

the estimated area under the ROC curves (AUC) [16]:

\[
AUC = \frac{1}{t_0(p - t_0)} \sum_{u = 1}^{p} \sum_{v = t_0 + 1}^{t_0} \left[ l(\hat{p}_u > \hat{p}_v) + \frac{1}{2} I(\hat{p}_u = \hat{p}_v) \right],
\]

and the estimated false discovery rate (FDR, [17]):

\[
FDR = \frac{FP}{TP + FN},
\]

where \(TP\) and \(TN\) stand for true positives and true negatives, \(FP\) and \(FN\) stand for false positives and false negatives, respectively. \(\hat{p}_u\) is the selection probability of the \(u\)-th predictor and the first \(t_0\) variables are assumed to be true signals. The index TPR is known as sensitivity, whereas MCC is generally regarded as a balanced measure for both sensitivity and specificity, AUC summarizes overall prediction performance, and FDR is a criterion to measure and control the number of false positives for the class-skewed high-throughput data [18]. The indexes TPR, MCC and AUC are used to measure the power of detecting interactions, while FDR is primarily used to assess false positives of detection.

The simulation results of different procedures for the three kinds of scenarios are summarized in Tables 2, 3 and 4. All indexes are presented as average and standard

| Table 2 Selection performance of different methods in different scenarios (OR = 1.5) |
|---|
| Method | Scenario | A1 | B1 | C1 |
|---|---|---|---|---|
| TPR | LASSO | 0.768(0.027) | 0.775(0.020) | 0.857(0.018) |
| SCAD | 0.801(0.025) | 0.775(0.021) | 0.603(0.016) |
| \(\ell\)LASSO | 0.750(0.018) | 0.780(0.009) | 0.990(0.005) |
| \(\ell\)SCAD | 0.933(0.013) | 0.897(0.002) | 0.968(0.003) |
| MCC | LASSO | 0.292(0.014) | 0.384(0.012) | 0.356(0.021) |
| SCAD | 0.350(0.013) | 0.435(0.013) | 0.373(0.016) |
| \(\ell\)LASSO | 0.776(0.011) | 0.706(0.012) | 0.875(0.011) |
| \(\ell\)SCAD | 0.826(0.008) | 0.843(0.016) | 0.837(0.015) |
| AUC | LASSO | 0.593(0.018) | 0.601(0.002) | 0.632(0.002) |
| SCAD | 0.596(0.018) | 0.606(0.002) | 0.632(0.002) |
| \(\ell\)LASSO | 0.612(0.001) | 0.616(0.002) | 0.638(0.005) |
| \(\ell\)SCAD | 0.631(0.001) | 0.615(0.001) | 0.630(0.002) |
| FDR | LASSO | 0.859(0.013) | 0.827(0.007) | 0.789(0.026) |
| SCAD | 0.837(0.009) | 0.813(0.008) | 0.742(0.018) |
| \(\ell\)LASSO | 0.186(0.006) | 0.160(0.009) | 0.107(0.017) |
| \(\ell\)SCAD | 0.167(0.003) | 0.147(0.007) | 0.166(0.014) |

**Abbreviations**: TPR true positive rate, MCC Matthews correlation coefficient, AUC area under the ROC curve, FDR false discovery rate.

Numbers in each cell represent mean (standard error) by 200 times simulation.
Table 3 Selection performance of different methods in different scenarios (OR = 1.4)

| Method | Scenario |
|--------|----------|
|        | A2       | B2       | C2       |
| TPR    | LASSO    | 0.726(0.028) | 0.726(0.021) | 0.797(0.020) |
|        | SCAD     | 0.750(0.026) | 0.740(0.021) | 0.734(0.022) |
|        | sLASSO   | 0.706(0.019) | 0.720(0.012) | 0.942(0.010) |
|        | sSCAD    | 0.861(0.016) | 0.890(0.004) | 0.953(0.002) |
| MCC    | LASSO    | 0.240(0.015) | 0.334(0.013) | 0.309(0.013) |
|        | SCAD     | 0.295(0.014) | 0.380(0.015) | 0.333(0.014) |
|        | sLASSO   | 0.716(0.012) | 0.636(0.015) | 0.826(0.013) |
|        | sSCAD    | 0.787(0.009) | 0.800(0.018) | 0.817(0.018) |
| AUC    | LASSO    | 0.537(0.018) | 0.542(0.002) | 0.577(0.003) |
|        | SCAD     | 0.538(0.019) | 0.529(0.003) | 0.570(0.004) |
|        | sLASSO   | 0.557(0.002) | 0.569(0.003) | 0.590(0.003) |
|        | sSCAD    | 0.557(0.003) | 0.561(0.003) | 0.560(0.001) |
| FDR    | LASSO    | 0.868(0.014) | 0.829(0.010) | 0.797(0.008) |
|        | SCAD     | 0.838(0.009) | 0.817(0.010) | 0.754(0.009) |
|        | sLASSO   | 0.198(0.007) | 0.146(0.009) | 0.122(0.010) |
|        | sSCAD    | 0.166(0.004) | 0.149(0.007) | 0.180(0.007) |

Abbreviations: TPR true positive rate, MCC Matthews correlation coefficient, AUC area under the ROC curve, FDR false discovery rate.
Numbers in each cell represent mean (standard error) by 200 times simulation.

Table 4 Selection performance of different methods in different scenarios (OR = 1.3)

| Method | Scenario |
|--------|----------|
|        | A3       | B3       | C3       |
| TPR    | LASSO    | 0.681(0.032) | 0.664(0.023) | 0.777(0.021) |
|        | SCAD     | 0.715(0.028) | 0.678(0.023) | 0.785(0.022) |
|        | sLASSO   | 0.651(0.019) | 0.692(0.012) | 0.874(0.012) |
|        | sSCAD    | 0.835(0.014) | 0.808(0.005) | 0.878(0.005) |
| MCC    | LASSO    | 0.173(0.018) | 0.298(0.018) | 0.303(0.016) |
|        | SCAD     | 0.253(0.016) | 0.350(0.017) | 0.312(0.014) |
|        | sLASSO   | 0.676(0.012) | 0.600(0.015) | 0.768(0.013) |
|        | sSCAD    | 0.736(0.012) | 0.737(0.014) | 0.778(0.019) |
| AUC    | LASSO    | 0.506(0.018) | 0.524(0.003) | 0.536(0.006) |
|        | SCAD     | 0.517(0.021) | 0.514(0.006) | 0.536(0.006) |
|        | sLASSO   | 0.518(0.002) | 0.545(0.005) | 0.535(0.005) |
|        | sSCAD    | 0.537(0.005) | 0.541(0.002) | 0.551(0.002) |
| FDR    | LASSO    | 0.869(0.015) | 0.838(0.011) | 0.798(0.010) |
|        | SCAD     | 0.832(0.013) | 0.819(0.008) | 0.726(0.009) |
|        | sLASSO   | 0.188(0.007) | 0.164(0.006) | 0.182(0.010) |
|        | sSCAD    | 0.169(0.006) | 0.163(0.007) | 0.174(0.008) |

Abbreviations: TPR true positive rate, MCC Matthews correlation coefficient, AUC area under the ROC curve, FDR false discovery rate.
Numbers in each cell represent mean (standard error) by 200 times simulation.
Table 5 Empirical selection probability of significant SNP pairs by \textit{\texttt{LASSO}} and \textit{\texttt{SCAD}} under subsampling

| SNP1(rs) | Gene1 | SNP2(rs) | Gene2 | \(\pi\)_{\text{LASSO}} | \(\pi\)_{\text{SCAD}} | Marginal | \(\pi\)_{\text{LASSO}} | \(\pi\)_{\text{SCAD}} | Marginal | \(\pi\)_{\text{LASSO}} | \(\pi\)_{\text{SCAD}} | Marginal |
|----------|-------|----------|-------|-----------------|-----------------|---------|-----------------|-----------------|---------|-----------------|-----------------|---------|
| rs7839119 | PTK2  | rs12544802 | PTK2  | 0.724*          | 0.702*          | 1.04 \times 10^{-6} | 0.628*          | 0.940*          | 6.34 \times 10^{-7} | 0.668*          | 0.801*          | 3.10 \times 10^{-6} |
| rs3781626 | RAPSN | rs6018348  | SRC   | 0.734*          | 0.680*          | 3.25 \times 10^{-3} | 0.514*          | 0.654*          | 2.88 \times 10^{-3} | 0.617*          | 0.824*          | 1.40 \times 10^{-4} |
| rs7839119 | PTK2  | rs4524871  | MUSK  | 0.746*          | 0.734*          | 7.19 \times 10^{-4} | 0.478           | 0.518*          | 4.98 \times 10^{-2} | 0.600*          | 0.980*          | 5.02 \times 10^{-4} |
| rs2736100 | TERT  | rs40318    | PIK3R1| 0.586           | 0.830*          | 9.87 \times 10^{-6} | 0.390           | 0.582*          | 2.22 \times 10^{-2} | 0.696*          | 0.977*          | 2.51 \times 10^{-6} |

\(\pi\) represents the empirical selection probability of SNP pairs under subsampling.

without marginal effects do exist [19], \textit{\texttt{SCAD}} is a valuable tool for discovering interactions without main effects and complement \textit{\texttt{LASSO}} in GWAS.

Result of application

Two SNP-SNP interactions were significant in both the discovery and replication phases by \textit{\texttt{LASSO}} (Table 5), and four SNP-SNP interactions were significant in both phases of \textit{\texttt{SCAD}} selection. \textit{\texttt{SCAD}} contained all significant interactions identified by \textit{\texttt{LASSO}}. When using \textit{\texttt{SCAD}}, the two pairs (rs7839119-rs4524871 and rs2736100-rs40318) were shown to have significant interactions in both the discovery and replication populations. In contrast, neither of two pairs was validated as significant in the replication phase with \textit{\texttt{LASSO}}.

For the \textit{\texttt{LASSO}} procedure, there were ten significant (\(l \geq \pi_{\text{thr}}\), \textit{FDR} < 0.1) two-way SNP-SNP interactions in the Nanjing discovery study (Table 6). Among these ten SNP pairs, two were selected (\(l \geq \pi_{\text{thr}},\textit{FDR} < 0.1\)) in the replication phase (Table 7). Both SNP-SNP interactions (rs7839119-rs12544802 and rs3781626-rs6018348) were verified in the replication phase. In an overall analysis that included discovery and replication datasets (5,408 subjects; 2,331 cases and 3,077 controls), the empirical selection probabilities of rs7839119-rs12544802 and rs3781626-rs6018348 interactions were 0.668 and 0.617, respectively; thus, indicating little statistical significance (\(\pi_{\text{LASSO}} \geq \pi_{\text{thr}},\textit{FDR} < 0.1\)).

Under the \textit{\texttt{SCAD}} procedure, all four significant SNP-SNP interactions (rs7839119-rs12544802, rs3781626-rs6018348, rs7839119-rs4524871 and rs2736100-rs40318) were successfully replicated (Tables 5, 8, and 9). The empirical selection probabilities of rs7839119-rs12544802, rs3781626-rs6018348, rs7839119-rs4524871 and rs2736100-rs40318 interactions in the overall analysis, which included all 5,408 subjects, were 0.801, 0.824, 0.980 and 0.977, respectively. In turn, these results indicate statistical significance (\(\pi_{\text{LASSO}} \geq \pi_{\text{thr}},\textit{FDR} < 0.1\)).

We also included the result of one permuted data set from the total 5,408 subjects combined. The selection probabilities of the \textit{\texttt{LASSO}} and \textit{\texttt{SCAD}} were 0.402 and 0.306, respectively. This corresponds to the maximum value of the test statistic for the permutation set. The cutoffs obtained from above inequality (6) for \textit{\texttt{LASSO}} and \textit{\texttt{SCAD}} with the significance (\(\textit{FDR} < 0.1\)) were 0.593 and 0.560, respectively; thus, suggesting that the \textit{FDR} calculated from the Meinshausen and Bülmann theorem is conservative. There appears to be little danger of selecting grossly inaccurate \textit{FDR} when applying the Meinshausen and Bülmann theory.

Discussion

Identifying interactions among multiple SNPs is both statistically and computationally challenging in large-scale association studies. The challenges include high-dimensional problems, computational capability, multiple testing problems, and genetic heterogeneity [20]. Many stochastic and heuristic detecting epistasis methods [21] could be used to analyze GWAS dataset. Wang \textit{et al.} used AntEpiSeeker, a two-stage ant colony optimization algorithm (ACO), to identify epistasis [22]. Wan \textit{et al.} proposed SNPRuler [23].
Table 7 Empirical selection probability of significant SNP pairs in Beijing study by the $\hat{\text{LASSO}}$

| SNP1(rs) | Gene1 | SNP2(rs) | Gene2 | */$\Pi$ |
|---------|-------|---------|-------|--------|
| rs3779632 | PTK2 | rs9644448 | PTK2 | 1.000 |
| rs2736100 | TERT | rs11994882 | PTK2 | 0.904 |
| rs10109684 | PTK2 | rs11231753 | BAD | 0.904 |
| rs11994882 | PTK2 | rs4983387 | AKT1 | 0.840 |
| rs6969923 | PKCG | rs11997161 | PTK2 | 0.788 |
| rs2677764 | PKCA | rs2821124 | MUSK | 0.784 |
| rs4551415 | PTK2 | rs1359711 | MUSK | 0.740 |
| rs1550099 | CHRNA5 | rs10817088 | MUSK | 0.706 |
| rs12466358 | CHRNA5 | rs2566062 | PTK2 | 0.708 |
| rs3791723 | CHRNA5 | rs7839119 | PTK2 | 0.684 |
| rs7839119 | PTK2 | rs12544802 | PTK2 | 0.628 |
| rs9773817 | PTK2 | rs6018088 | SRC | 0.610 |
| rs479744 | FOXO3 | rs752435 | BAD | 0.612 |
| rs2736122 | TERT | rs12945577 | CHRNA5 | 0.598 |
| rs10817082 | MUSK | rs5994451 | YWHAH | 0.596 |
| rs251398 | PKCRI | rs10733579 | MUSK | 0.530 |
| rs3781626 | RAPSN | rs6018348 | SRC | 0.514 |
| rs4727666 | PKCG | rs7856889 | MUSK | 0.506 |

*/$\Pi$* represents a predictor's empirical probability of model inclusion under 500 times subsampling.

Table 8 Empirical selection probability of significant SNP pairs in Nanjing study by the $\hat{\text{SCAD}}$

| SNP1(rs) | Gene1 | SNP2(rs) | Gene2 | */$\Pi$ |
|---------|-------|---------|-------|--------|
| rs929087 | FASLG | rs12544802 | PTK2 | 0.904 |
| rs2853462 | CHRNA5 | rs7856889 | MUSK | 0.876 |
| rs2736100 | TERT | rs40318 | PKCRI | 0.830 |
| rs7446640 | TERT | rs10733579 | MUSK | 0.786 |
| rs411751 | PKCRI | rs939269 | PTK2 | 0.756 |
| rs7839119 | PTK2 | rs4524871 | MUSK | 0.734 |
| rs7839119 | PTK2 | rs12544802 | PTK2 | 0.702 |
| rs725787 | PTK2 | rs5998196 | YWHAH | 0.692 |
| rs3781626 | RAPSN | rs6018348 | SRC | 0.680 |
| rs4946933 | FOXO3 | rs11231740 | BAD | 0.640 |
| rs6578141 | PTK2 | rs1904245 | MUSK | 0.604 |

*/$\Pi$* represents a predictor's empirical probability of model inclusion under 500 times subsampling.

Table 9 Empirical selection probability of significant SNP pairs in Beijing study by the $\hat{\text{SCAD}}$

| SNP1(rs) | Gene1 | SNP2(rs) | Gene2 | */$\Pi$ |
|---------|-------|---------|-------|--------|
| rs7839119 | PTK2 | rs12544802 | PTK2 | 0.940 |
| rs3779632 | PTK2 | rs9644448 | PTK2 | 0.828 |
| rs10515077 | PKCRI | rs10817088 | MUSK | 0.658 |
| rs3781626 | RAPSN | rs6018348 | SRC | 0.654 |
| rs2736122 | TERT | rs12945577 | CHRNA5 | 0.610 |
| rs3639 | PTK2 | rs3781626 | RAPSN | 0.602 |
| rs3791723 | CHRNA5 | rs7859119 | PTK2 | 0.594 |
| rs2736100 | TERT | rs40318 | PKCRI | 0.582 |
| rs9773817 | PTK2 | rs6018088 | SRC | 0.574 |
| rs3800230 | FOXO3 | rs7856889 | MUSK | 0.568 |
| rs10980510 | MUSK | rs3829603 | CHRNA5 | 0.560 |
| rs2677764 | PKCIII | rs2853668 | TERT | 0.556 |
| rs411751 | PKCRI | rs9609396 | YWHAH | 0.526 |
| rs9480867 | FOXO3 | rs11231741 | BAD | 0.522 |
| rs7839119 | PTK2 | rs4524871 | MUSK | 0.518 |
| rs4524871 | MUSK | rs10980564 | MUSK | 0.502 |

*/$\Pi$* represents a predictor's empirical probability of model inclusion under 500 times subsampling.

Based on both predictive rule inference, and two-stage design. Boolean operation-based screening and testing (BOOST) [24] involves only Boolean values, and allows the use of fast logic operations to obtain contingency tables. TEAM [25] exploits properties of test statistics to mitigate multiple testing problems. To date, there appears to be no one method free from model sensitivity.

In addition to non-parametric and model-free methods, many LASSO-based penalized parametric methods provide the estimation of parameter as the dimensionality increases, even if the number of variables is greater than the sample size. The coefficients of those non-disease- associated SNPs will be zero in the penalized multivariate regression model. Thus, detecting interactions is equivalent with the variable selection problem under the framework of regression analysis. A broad range of simulations has demonstrated that the penalized regression method is a useful tool for detecting gene-gene interactions. However, the regularization choice in penalized regression is usually made by cross-validation that maximizes predictive accuracy in finite samples; although it does not necessarily induce the correct sparseness pattern for variable selection [26]. In our simulations, cross-validation often leads to the inclusion of too many noise variables, and induces instability of variable selection for the ordinary penalized regression method, such as LASSO or SCAD. A major hurdle for studying interactions in GWAS is the lack of efficient algorithms that can map different forms of interactions while keeping FDR under control [27]. $\hat{\text{LASSO}}$ introduces stability selection into traditional LASSO. The stability selection procedure combines selection algorithms for high dimensional problems by sub-sampling. $\hat{\text{LASSO}}$ dramatically reduces the number of false discovery rate, and could...
accurately identify crucial regions of GWAS; however, it is overly conservative, and may miss some important regions.

\( \mathcal{S}_{\text{SCAD}} \) procedure increases the power of detecting the interactions while controlling FDR. It attempts to provide more true interactions, but less noise terms than \( \mathcal{S}_{\text{LASSO}} \). The above advantage could be attributed to the fact that running the LASSO-penalized procedure within stability selection results in more false positives than SCAD for each random sub-sample. Thus, the interactions causing noise as well as true interactions in the region both satisfy the threshold condition \( \pi_{\text{thr}} \) for selection. To control the number of falsely selected variables, the threshold must be very stringent. As a result, the \( \mathcal{S}_{\text{LASSO}} \) selection suffers a loss of power.

We analyzed a previously reported lung cancer data-set in Han Chinese, and confirmed significant interactions in the achPathway pathway, which supported the appropriate use of the proposed method. The observation of interactions between two closely located SNP pairs supports the hypothesis that some genetic variation in complex traits may hide in interactions between linked SNPs [28].

Application of the proposed procedure to GWAS data may ensure that the power of detection is reduced when over-stringent threshold \( \pi_{\text{thr}} \) conditions exist for the much increased ratio of SNPs to samples. A good alternative to derive genome-wide significant threshold is permutation. Unfortunately, genome-wide permutation in real GWAS of interactions is computationally prohibitive for the \( \mathcal{S}_{\text{SCAD}} \) selection. Partial search strategies based on biological knowledge [29] or the filtering of unimportant SNPs prior to analysis [30] could be adopted to reduce excessive computing burdens in early stage of genome-wide scale. These strategies are also necessary for the proposed method.

Under our current approach, high-dimensional data were primarily managed with sparse models. High correlations (individual SNPs that have a variance inflation factor (VIF) > 2 with other markers) were excluded. The chip data were pruned, and then analyzed with regression model method using a sparse constraint. Many common diseases may be associated with many SNPs with small to moderate effects. In this situation, we are considering group penalized methods in another paper.

Conclusions

We developed a variable selection procedure (referred to as \( \mathcal{S}_{\text{SCAD}} \) selection). This procedure could control the FDR while maintaining the power to detect SNP-SNP interactions in association studies. In the pure interaction model, this procedure seems to overcome the conservativeness of \( \mathcal{S}_{\text{LASSO}} \). The end result is that \( \mathcal{S}_{\text{SCAD}} \), as a new technique in detecting interactions, can benefit the selection of \( \mathcal{S}_{\text{LASSO}} \).

Competing interests

The authors declare that they have no competing interests.

Authors’ contributions

JC performed the simulations, participated in the data analysis, and prepared for the manuscript. YZ participated in the design of simulations, and helped to draft the manuscript. YW helped to perform the simulations. RZ, YQ and PZ participated in the data analysis. CW, TWDY, WT, ZH, DL and HS acquired the data. FC conceptualized the study. All authors read and approved the final manuscript.

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