Environment Assisted Quantum Transport in Organic Molecules

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One of the new discoveries in quantum biology is the role of Environment Assisted Quantum Transport (ENAQT) in excitonic transport processes. In disordered quantum systems transport is most efficient when the environment just destroys quantum interferences responsible for localization, but the coupling does not drive the system to fully classical thermal diffusion yet. This poised realm between the pure quantum and the semi-classical domains has not been considered in other biological transport processes, such as charge transport through organic molecules. Binding in receptor-ligand complexes is assumed to be static as electrons are assumed to be not able to cross the ligand molecule. We show that ENAQT makes cross ligand transport possible and efficient between certain atoms opening the way for the reorganization of the charge distribution on the receptor when the ligand molecule docks. This new effect can potentially change our understanding of how receptors work. We demonstrate room temperature ENAQT on the caffeine molecule.

1 Introduction

There is overwhelming evidence that quantum coherence plays an essential role in exciton transport in photosynthetic ligand molecules. One of the fundamental quantum effects there is the Environmentally Assisted Quantum Transport (ENAQT). It applies to partially coherent quantum transport in disordered systems. At low temperatures transport is dominated by quantum walk of excitons over the excitable sites forming a network. While a classical walker diffuses away from its initial position like $\sim \sqrt{t}$ in time via taking random turns, a quantum walker takes a quantum superposition of amplitudes of alternative paths. In a strongly disordered system the interference is destructive and the walker becomes stuck or 'localized'. At medium temperatures coupling to the environment partially destroys quantum interference and the walker is free to move and diffuse. Then at very high temperatures decoherence becomes very destructive and the exciton gets frozen due to the Zeno effect. As a result, transport is most efficient at medium temperatures or at medium level of decoherence and much less efficient at low or high temperatures. Transport efficiency is the highest and mean transport time is the shortest at medium temperatures. In photosynthetic systems parameters are such that this optimum is near room temperature (290K).

The conditions for ENAQT look quite generic and one can suspect that it can occur in a wide range quantum processes in biology. Yet, the presence of ENAQT has only been established in the exciton transport of light harvesting systems. In this paper we demonstrate that – indeed – ENAQT can play a major role in electron transport through organic molecules at ambient temperatures. Accordingly in certain cases our understanding of charge transport in biology needs revision.

Charge transport in biological molecules has been studied extensively with a wide range of quantum chemical methods. These methods cover fully quantum, mixed quantum-classical, semi-classical, and fully classical approaches. However, none of these cover the parameter range of the validity of ENAQT. In general, electronic levels are broadened due to the coupling to the environment. The width of the levels $\Gamma$ is proportional to the level of decoherence, which is then ultimately determined by the temperature of the environment $\Gamma \sim k_B T$. Quantum description is relevant, when the broadening is much smaller than the spacing between the consecutive energy levels $E_{n+1} - E_n \gg \Gamma$ and the mean level spac-
ing \( \Delta = \langle E_{n+1} - E_n \rangle \) is much greater than the temperature \( \Delta \gg k_B T \). The semiclassical and classical or mixed description is relevant in the opposite limit, when \( \Delta \ll k_B T \) and many energy levels are involved in the process. The most efficient ENAQT sets in when the environmental temperature is comparable with the main level spacing \( \Delta \approx k_B T \) or at least the level broadening is comparable\(^{10}\) with the spacings of some levels \( E_{n+1} - E_n \approx \Gamma \approx k_B T \). In small and medium sized (less than 500 Da) organic molecules the mean level spacing of electronic levels is on the electron volt scale, which is about two orders of magnitude larger than the room temperature (about 25 milli-electron volts). So, at first sight we would expect that EQNAT is relevant only at temperatures \( T = 1 eV / k_B \approx 12000 K \), which is twice of the temperature of the surface of Sun. However, there is a second possibility: In Fig. 1 we show the nearest neighbor spacings of the energy levels of caffeine. The mean level spacing is \( \Delta = 1.4 eV \), which is much larger than the energy scale of the decoherence \( k_B T = 0.025 eV \). However, there are several level spacings in the spectrum, which are close to 0.025 eV indicating that while global ENAQT extending for the entire molecule is not possible, there might be local pockets on the molecule, where it plays an important role. Next we continue with showing just that.

## 2 Transport in ligand-receptor complexes

One of the most significant building blocks of biochemical processes in the cell is the docking of signaling molecules in receptors. A typical situation is shown in Fig. 2 where adenosine is docked in the A2A adenosine receptor. Besides hydrophobic interactions binding the ligand molecule to the receptor electrostatically, there are also hydrogen bonds connecting the two systems. The hydrogen bridge makes possible the exchange of electrons between the two systems. The receptor consists of amino acids and these can have very different charging situations. Arginine, histidine and lysine have positive side chains while glutamic acid and asparatic acid have negative side chains. The rest of the amino acids is neutral or hydrophobic. An electron from a negatively charged part of the receptor protein can jump via the hydrogen bridge to the neighboring atom of the ligand molecule. If the ligand molecule would be a good conductor the electron could walk trough the molecule and reach a positively charged part of the receptor trough and other hydrogen bridge. The ligand molecule would act as a molecular wire, a lightning rod. As a result, the charge distribution on the receptor protein would change suddenly upon the docking of the ligand molecule and could spark sudden motion of the parts of the protein, due to the change of the equilibrium of the electrostatic forces.

Our understanding before ENAQT ruled out such transport of electrons through the ligand molecule. Quantum calculations show that, unless tunneling plays a role in some special cases, ligand molecules act as insulators. Next, we show that ENAQT changes this picture and provides a mechanism for the easy and effective transport of electrons between certain atoms in the ligand molecule.

## 3 Transport model

We can develop a model for the description of the electron transfer process of the previous section. For the description of the molecule only the \( n \) electrons in the \( N \) atomic orbitals are considered. The molecular orbitals \( \psi_j \) are linear combinations of the atomic orbitals

\[
\psi_j = \sum_{i=1}^{N} C_{jr} \phi_i \quad \text{and} \quad j, r = 1, \ldots, N, \tag{1}
\]

where \( \phi_i \) are the valence atomic orbitals \( 2S, 2P_x, 2P_y, \) and \( 2P_z \) for carbon atoms and hetero atoms and \( 1S \) for hydrogen atoms. The molecular orbitals can be determined from the overlap matrix \( S_{rs} = \langle \phi_r | \phi_s \rangle \) and Hamiltonian \( H_{rs} = \langle \phi_r | H_{eff} | \phi_s \rangle \) matrices via the generalized eigenequation

\[
HC = ESC, \tag{2}
\]

where \( H, S \) and \( C \) are square matrices containing the elements of \( H_{rs}, S_{rs} \) and \( C_{jr} \) respectively. The raw molecular orbitals can be orthonormalized via the Löwdin transformation\(^{13}\). The
coefficients in the Löwdin basis can be introduced via \( C = S^{-1/2} C' \) and the transformed Hamiltonian \( H' = S^{-1/2} H S^{-1/2} \) satisfies the eigenequation
\[
H' C' = EC',
\]
where the eigenenergies \( E \) remain unchanged. Next, we will drop the prime signs and use this basis as default.

We assume that the electron is coming through the H-bridge or via other mechanisms and initially enters one of the atomic orbits of the molecule. Initially the \( n \) electrons are placed in pairs on the lowest molecular orbits with opposite spins and occupy about half of the orbitals. The incoming electron occupies one of the atomic orbitals. In a pure quantum description the initial wave function is a \( n + 1 \) dimensional Slater determinant of the \( n \) molecular orbitals and the single initial electron on the atomic orbital with wave function \( \Psi(t = 0) \). This wave function is localized on the atomic orbital and it is proportional with the initial atomic orbital \( \Psi(0) = \alpha \phi_i \), where \( \alpha \) is a normalization constant. The initial atomic orbital can be expanded in terms of all molecular orbitals \( \phi_i = \sum_j [C^{-1}]_{ij} \psi_j \), where \( C^{-1} \) is the inverse of the coefficient matrix. The function \( \phi_i \) is not orthogonal to the \( n \) occupied molecular orbitals and only the expansion coefficients corresponding to unoccupied molecular orbitals will contribute to the norm of the \( n + 1 \) electron wave function. We can split \( \Psi \) into two orthogonal parts
\[
\Psi = \Psi^o + \Psi^u,
\]
where \( \Psi^o \) is spanned over the occupied and \( \Psi^u \) over the unoccupied orbitals of the molecule with \( n \) electrons. The normalization condition of the Slater determinant then involves the unoccupied part only \( |\Psi^u|^2 = 1 \), which yields the following normalization condition
\[
\alpha^2 \sum_{j \in \text{unoccupied}} [C^{-1}]_{ij}^2 = 1.
\]
Consequently the norm
\[
|\Psi|^2 = \alpha^2 \frac{1}{\sum_{j \in \text{unoccupied}} [C^{-1}]_{ij}^2}
\]
is larger than unity. This reflects the fact that in this description the incoming electron creates both electronic states in the unoccupied sector and hole states in the occupied sector.

The time evolution in this model is very simple. The molecular orbitals are eigenfunctions of the Hamiltonian and remain unchanged except the stationary phase factors \( e^{-iE_j t} / \hbar \). The time evolution of the incoming electron is governed by the Schrödinger equation
\[
\frac{i\hbar}{\partial t} \Psi = H \Psi.
\]
The reduced density matrix is given by this density matrix according to (8). The physically relevant and contains both occupied and unoccupied states. We evolve our model: the details of the molecule and the value of $\kappa$ from the entrance to the exit. This depends on two factors in $\tau$ next quantity is the average time an electron needs to get from the entrance to the exit. This depends on two factors in our model: the details of the molecule and the value of $\kappa$. It is hard to set the value of $\kappa$ without detailed models or measurements of the system, therefore we have to find its value from other considerations. Since the typical energy range in the system is the mean level spacing we can expect that the rate of leaking is in the order of the time $\kappa \sim \Delta / h$. Once the scale of the escape rate is set we determine the average time needed from an initial atom to reach the destination $\tau_{FI}$ and also the time an electron would need to leave the system if it would be placed immediately to the final site $\tau_{FF}$. The difference $\tau_{FI} - \tau_{FF}$ is a better characteristics of the transport as the pure pure pumping time is transformed out and mainly the inter-atomic travel time enters.

The average transit time can be calculated from the evolution of the reduced density matrix. The outflowing probability current at the exit site $F$ at time $t$ is given by $dP(t)/dt = 2d\kappa \langle \psi_F | \rho (t) | \psi_F \rangle$ and the average transit time is the average

$$\tau = 2 \kappa \hbar \int_0^\infty t \langle \psi_F | \rho (t) | \psi_F \rangle \, dt.$$  

This integral can be calculated analytically using the solution of the evolution equation. Equation (8) can be cast into the form

$$\frac{\partial \rho_{rs}}{\partial t} = -i \frac{\hbar}{\kappa} \sum_{pq} R_{rs pq} \rho_{pq}.$$  

We can re-index this equation and introduce a new index replacing the pairs of indexes $J = (r,s)$ and $J' = (p,q)$. With the new indexing (10) reads

$$\frac{\partial \rho_{J}}{\partial t} = -i \frac{\hbar}{\kappa} \sum_{J'} R_{JJ'} \rho_{J' \bar{J}}.$$  

The solution of this is

$$\rho(t) = \exp \left( -i R \tfrac{t}{\hbar} \right) \rho(0).$$  

Since the initial density matrix has only one nonzero element $J_I = (I,I)$ the integral in (9) yields the matrix element

$$\tau = -2 \kappa \hbar^2 \left[ R^{-2} \right]_{J_F J_I},$$  

where $J_F = (F,F)$. Next, we show the results of the calculation for a molecule with biological relevance.

5 Caffeine

In order to show ENAQ in organic molecules we should pick a biologically relevant example which is also computationally feasible. Our choice is caffeine as it is a sufficiently small molecule with 24 atoms (see in Table 1). Using the Extended Hückel method implemented in the YaeHMO software package. There are $N = 66$ valence atomic orbitals. The computational task involves the repeated calculation of the inverse of $R$, which is an $(N \times N) \times (N \times N) = N^2 \times N^2$ matrix, or $4356 \times 4356$ in case of caffeine. The rapid growth of the computation time with $N^2$ is the strongest numerical limitation in the problem. In the calculation the escape rate $\kappa = \hbar / 1eV$ has been used. There are 2145 possible pairs of initial and final atomic orbitals. In Figure 3 we collected the most interesting results. These are the transit times of electrons ending on the 2S orbital of oxygen no. 6 in Table 1. The blue line shows the transit time between this orbital and itself. This is the minimum time $\tau_{FF}$ needed for an electron to leak out from this site. This value is constant for low dephasing and starts increasing.
Fig. 3 Transit times between atomic orbitals in the caffeine molecule at escape rate \( \kappa = \hbar / 1eV \). Dephasing rate \( \Gamma \) in units of eV is shown on the horizontal axis. Curves show transition times between the \( N = 66 \) atomic orbitals and the \( 2S \) orbital of oxygen atom no. 6 in Table I. The blue curve corresponds to the transit time between \( 2S \) orbital of oxygen no. 6 and itself. The green curves show the transit time between the \( 2S \) orbital of oxygen no. 6 and the \( 2P_x, 2P_y \) and \( 2P_z \) of oxygen no. 6. The red curve shows the transition time between the \( 2S \) orbital of oxygen no. 11 and \( 2S \) of oxygen no. 6. The black curves show the rest of the transit time curves.

The transition time between the two oxygen atoms is just 10 times as large as the minimum leaking time set by the scale of \( \kappa \). This should be contrasted with the quantum limit, where the transition times are 1000 to 100000 times larger than the minimum leaking time. A pure quantum calculation would find the caffeine molecule strongly insulating between the atoms and electron transport would be practically impossible.

in the classical limit of large dephasing. The green curves show the leaking time from the same atom but the electron is initially placed on the three \( 2P \) orbitals of the atom. In this case we can observe a shallow minimum in the \( \Gamma = 1 - 10eV \) range. The black curves represent the transitions between all the atomic orbitals and the \( 2S \) orbital of oxygen no. 6, except \( 2S \) of oxygen no. 11, which is shown in red. The black and the green curves show the sign of ENAQT and are large both for small and large \( \Gamma \) with a minimum in the middle. The minimum corresponds again to about \( 1 - 10eV \) in accordance with the expectation based on the mean level spacing \( 1.4eV \), which is 2-3 orders of magnitude larger than room temperature. The red curve also has a minimum in this range. However, a second shallow minimum is also developed around \( 0.01eV \) and at room temperature \( 0.025eV \) the transition time is still close to this minimum. This second optimum of ENAQT signals fast transport between the \( 2S \) orbits of the two oxygen atoms.

Table 1 Index and position of atoms in the caffeine molecule

| Index | Atom | x     | y     | z     |
|-------|------|-------|-------|-------|
| 1     | N    | 1.047000 | -0.000000 | -1.312000 |
| 2     | C    | -0.208000 | -0.000000 | -1.790000 |
| 3     | C    | 2.176000  | 0.000000  | -2.246000 |
| 4     | C    | 1.285000  | -0.001000 | 0.016000  |
| 5     | N    | -1.276000 | -0.000000 | -0.971000 |
| 6     | O    | -0.384000 | 0.000000  | -2.993000 |
| 7     | C    | -2.629000 | -0.000000 | -1.533000 |
| 8     | C    | -1.098000 | -0.000000 | 0.402000  |
| 9     | C    | 0.193000  | 0.005000  | 0.911000  |
| 10    | N    | -1.934000 | -0.000000 | 1.444000  |
| 11    | O    | 2.428000  | -0.000000 | 0.437000  |
| 12    | N    | 0.068000  | -0.000000 | 2.286000  |
| 13    | C    | -1.251000 | -0.000000 | 2.560000  |
| 14    | C    | 1.161000  | -0.000000 | 3.261000  |
| 15    | H    | 1.800000  | 0.001000  | -3.269000 |
| 16    | H    | 2.783000  | 0.890000  | -2.082000 |
| 17    | H    | 2.783000  | -0.889000 | -2.083000 |
| 18    | H    | -2.570000 | 0.000000  | -2.622000 |
| 19    | H    | -3.162000 | -0.890000 | -1.198000 |
| 20    | H    | -3.162000 | 0.889000  | -1.198000 |
| 21    | H    | -1.679000 | 0.000000  | 3.552000  |
| 22    | H    | 1.432000  | -1.028000 | 3.503000  |
| 23    | H    | 2.024000  | 0.513000  | 2.839000  |
| 24    | H    | 0.839000  | 0.513000  | 4.167000  |

6 Conclusions

We investigated the possibility of ENAQT in organic molecules at room temperature. We worked out a framework which makes it possible to treat this problem in first approximation. We showed that global ENAQT is not present in these molecules in general as the optimal temperature is several orders of magnitude higher than the room temperature. However, room temperature ENAQT can be observed in the electron transport between certain atoms in the caffeine molecule. This indicates that in ligand-receptor systems the ligand molecule can act as a molecular wire connecting differently charged areas of the receptor protein and can contribute to their response for the docking. This can have a significant importance in understanding signaling and drug action in cells.

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