TRANSIENT SIMULATION STUDY OF FLOOR HEATING SYSTEMS

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This case study is aimed at transient simulation of floor heating systems. There is comparison of surface floor temperatures and heat fluxes changes of different systems over time. The first studied system is a dry floor heating system which consists of system boards made from insulation material, spreader plates, and it is covered by cement fiber boards. The second examined system is heavy wet concrete floor heating system whose heating power is set identically as heating power of dry floor heating system. Mean temperature of heating water is investigated. All simulations, both time steady-state and transient, are performed in software CalA. Reduction of duration and computational performance of simulation is achieved by creation of a surrogate model. The surrogate model evinces identical surface temperatures and heat fluxes. Total number of computational grid is reduced and therefore lower number of equations is solved. Results show that dry floor heating system has faster response than concreate floor heating system. It is caused by lower weight and lower thermal capacity of this system.

Keywords: floor heating, software CalA, numerical simulation, surrogate model, steady-state simulation, transient simulation

1. Introduction

Three different floor heating systems are examined. The first studied system (Model 1) is dry floor heating system which consists of system boards made from insulation material, spreader plates, and it is covered by cement fiber boards. The second examined system (Model 2) is wet anhydrite floor heating system and the third one (Model 3) is heavy wet concrete floor heating system. Dry floor heating system is mostly used for floor reconstructions and for a floor heating system for wooden houses. This solution is used in these light-weight buildings because cement screed or anhydrite layer are wet processes and increase the load of ceiling construction.

A lot of publications are aimed at problematics of floor heating systems [1] also examining different compositions and constructions. Simulations and measurements are most frequently methods to study temperature field or heat power of floor heating [2–4]. Dry floor heating systems are very often used in the United States of America where many different patents of these systems are held [5–6]. It is possible to use numerical simulation to solve both steady and transient states of thermal activated constructions [7–9].

2. Materials and calculation methods

2.1. Calculation method

The simulations were carried out in software CalA, which is developed at Brno University of Technology. It is based on numerical solution of 2D heat conduction Eq. (1) by finite volume method, see [10].

$$\frac{\partial}{\partial x} \left( \lambda \frac{\partial T}{\partial x} \right) + \frac{\partial}{\partial y} \left( \lambda \frac{\partial T}{\partial y} \right) + Q = \rho c \frac{\partial T}{\partial t} \quad (1)$$

where \( T \) [°C] is temperature, \( \lambda \) [W·m⁻¹K⁻¹] thermal conductivity, \( \rho \) [kg·m⁻³] density, \( c \) [J·kg⁻¹K⁻¹] specific thermal capacity, \( t \) [s] time, \( Q \) [W] volumetric heat source.

The detailed calculation of linear thermal transmittance in case of contact external peripheral wall and plastic window frame [11] or the impact of freezer room operation on changes of temperature field in subsoil within both steady-state and transient boundary conditions [12] were performed in software CalA. The comparison of results of software CalA and ANSYS Fluent is also performed [13].

Keywords: floor heating, software CalA, numerical simulation, surrogate model, steady-state simulation, transient simulation

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2.2. Geometry

The calculation models represent typical section of heating systems and the adjacent floor construction. Axes of symmetry are used for creation of these models. The width of models is determined as a half of axial distance of heating pipes. Axial distance of heating pipes is 150 mm therefore the width of model is 75 mm, see Fig. 1.

2.3. Material characteristics

Material characteristics of used materials are listed in Table 1. Compositions of examined floor heating systems and thickness of individual layers are shown in Fig. 1.

2.4. Boundary conditions

Model boundary conditions are set both steady-state and transient. The boundary condition I – Indoor cli-

![Fig. 1. Compositions of examined floor heating systems and thickness of layers](image)

Table 1. Material characteristics

| Material                  | Thermal conductivity $\lambda$ [W·m⁻¹K⁻¹] | Density $\rho$ [kg·m⁻³] | Thermal capacity $c$ [J·kg⁻¹K⁻¹] |
|---------------------------|--------------------------------------------|------------------------|---------------------------------|
| PVC                       | 0.16                                       | 1400                   | 1100                            |
| Fermacell boards          | 0.35                                       | 1150                   | 1100                            |
| Extruded polystyrene      | 0.034                                      | 30                     | 2060                            |
| Reinforced concrete       | 1.43                                       | 2300                   | 1020                            |
| Plaster                   | 0.88                                       | 2000                   | 790                             |
| Polyethylene              | 0.35                                       | 930                    | 1470                            |
| Air                       | 0.07                                       | 1                      | 1010                            |
| Spreader plate (steel)    | 20                                         | 7850                   | 440                             |
| Cement screed             | 1.1                                        | 2100                   | 1570                            |
| Anhydrite                 | 1.8                                        | 2100                   | 1550                            |
The temperature of indoor climate is designed indoor air temperature during the winter season and is unchangeable. The boundary condition II – Heating water is also Newton boundary condition. The temperature of heating water presents average of inlet and outlet heating water. Transient models simulate starting-up the floor heating systems. The boundary condition of symmetry axes is the adiabatic boundary condition. Parameters of boundary conditions are shown in Fig. 2.

Heating water temperature of Models 2 and 3 is parametrically changed so that useful heat flux of both models is same as useful heat flux of Model 1.

### 2.5. Simplified models

Geometry of simplified models of examined floor heating systems is adjusted. Thickness of concrete layer is reduced to one quarter of the original thickness, see Fig. 3. Number of solved equations are reduced 2.6 times (from 1 460 526 to 560 526 equations).

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**Fig. 2.** Boundary conditions of examined models

**Fig. 3.** Comparison of full scale model and simplified model
Material characteristics of concrete are transformed so that the thermal conductivity and thermal accumulation of concrete layer are identical in both models, see Fig. 2. The reason is that there is no possibility to transform discretization of part of model mesh in software CalA.

3. Results

3.1. Heating water temperatures

Results of steady-state parametrical simulation of Model 2 and Model 3 are listed below in Table 2. Corresponding heating water temperatures are determined by using the functional approximation, see Figs 4 and 5. The resulting heating water temperatures for all models are listed below in Table 3, these temperatures are used in the following transient simulations.

### 3.2. Comparison of full scale model and simplified model

Floor and ceiling (bottom of the model) surface temperatures of dry floor heating system of both full scale and simplified models are compared in Figs 6 and 7.

| Anhydrite floor heating system | Cement screed floor heating system |
|-------------------------------|-----------------------------------|
| Temperature of heating water  | Temperature of heating water       |
| [°C]                          | [°C]                              |
| 25                            | 25                                |
| 30                            | 25                                |
| 35                            | 35                                |
| Average of floor temperature  | Average of floor temperature       |
| [°C]                          | [°C]                              |
| 22.63                         | 22.24                             |
| 25.25                         | 24.48                             |
| 27.87                         | 26.73                             |
| Average of useful heat flux density | Average of useful heat flux density |
| [W·m⁻²]                       | [W·m⁻²]                           |
| 21.00                         | 35.80                             |
| 42.01                         | 53.87                             |
| 63.00                         |                                    |

| Anhydrite floor heating system | Cement screed floor heating system |
|-------------------------------|-----------------------------------|
| Temperature of heating water  | Temperature of heating water       |
| [°C]                          | [°C]                              |
| 25                            | 25                                |
| 30                            | 30                                |
| 35                            | 35                                |
| Average of floor temperature  | Average of floor temperature       |
| [°C]                          | [°C]                              |
| 22.63                         | 22.24                             |
| 25.25                         | 24.48                             |
| 27.87                         | 26.73                             |
| Average of useful heat flux density | Average of useful heat flux density |
| [W·m⁻²]                       | [W·m⁻²]                           |
| 21.00                         | 35.80                             |
| 42.01                         | 53.87                             |
| 63.00                         |                                    |

![Fig. 4. Investigation of heating water temperature of anhydrite floor heating system](image)

![Fig. 5. Investigation of heating water temperature of cement screed floor heating system](image)
Average value of surface temperatures and heat fluxes including differences between models are listed below in Tables 4 and 6. Upper parts of temperature fields of models are shown in Fig. 8.

| Model                              | Temperature of heating water [°C] | Average of floor surface temperature [°C] | Average of useful heat flux density [W·m⁻²] |
|------------------------------------|-----------------------------------|------------------------------------------|---------------------------------------------|
| Model 1 Dry floor heating system   | 35                                | 24.803                                   | 38.423                                      |
| Model 2 Anhydrite floor heating system | 29.15                             | 24.804                                   | 38.433                                      |
| Model 3 Cement screed floor heating system | 30.71                             | 24.802                                   | 38.413                                      |

Fig. 6. Comparison of floor surface temperature of full scale model and simplified model

Fig. 7. Comparison of ceiling surface temperature of full scale model and simplified model

Fig. 8. Comparison of temperature field of full scale model and simplified model
3.3. Transient simulations

Simplified models of floor heating systems are used for transient simulations. Floor surface temperature and useful heat fluxes over time are shown in Figs 9 and 10. First time step length is 1 second, next time step is always twice of previous step. Time step length starts to be constant when it reaches 10 minutes.

4. Discussion

The thermal conductivity of concrete of simplified model is set as isotropic although geometry of concrete layer is modified only in the vertical direction. The results show that this simplification has negligible impact on floor surface temperature and useful heat flux. Anisotropic thermal conductivity is also examined but it does not reach reduction of duration of simulation.

Heating water temperature of dry floor heating system is approximately 5°C higher than anhydrite and concrete floor heating system with identical useful heat flux. It is caused by thermal conductivity of fermacell boards located over the heating pipes. On the other hand, thickness of fermacell board layer is lower than anhydrite and cement layer. Thermal capacity of

| Table 4. Average surface temperature |
|-------------------------------------|
| **Full scale model** | **Simplified model** | **Difference** | **Difference [%]** |
| Floor | 24.814 °C | 24.803 °C | 0.011 °C | 0.04 |
| Ceiling | 21.476 °C | 21.452 °C | 0.024 °C | 0.11 |

| Table 5. Average heat flux |
|---------------------------|
| **Full scale model** | **Simplified model** | **Difference** | **Difference [%]** |
| Useful heat | 38.509 W·m⁻² | 38.423 W·m⁻² | 0.086 W·m⁻² | 0.22 |
| Heat losses | 11.808 W·m⁻² | 11.613 W·m⁻² | 0.195 W·m⁻² | 1.65 |

![Fig. 9. Floor surface temperature over time](image)

![Fig. 10. Useful heat flux over time](image)
fermacell layer is also lower and it has impact on faster response of dry floor heating system.

5. Conclusion

The main goal of this study is the assessment of the use of geometric simplified models of floor heating systems and the use of these models for transient simulations. Difference of average floor surface temperature of full scale model and simplified model is lower than 0.05% and difference of average ceiling surface temperature is lower than 0.2%. Difference of average heat fluxes is slightly higher because heat fluxes are calculated from temperature field. The difference of useful heat flux is lower than 0.3% and the difference of heat losses is lower than 1.7%. These results show good similarity between both models. Number of solved equations is reduced 2.6 times and duration of simulation is also reduced. Results of transient simulations show that dry floor heating system has faster response than concrete floor heating system. It is caused by lower weight and lower thermal capacity of this system.

Acknowledgements

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