Measurement of the Excited Energies Identified in $^{42}$Ca using the ROSPHERE Gamma-ray Arrays

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Abstract

Excited energy states totalling 11 in number identified to be associated with the $^{42}$Ca were detected via the ROSPHERE gamma-ray array detectors of IFIN-HH Bucharest from a $^{28}$Si($^{18}$O, 2p2n), where a multi-particle of 2 protons and 2 neutrons were evaporated in a fusion reaction. The excited energies were identified using $\gamma$-ray coincidences. All detected gamma energies ($\gamma$) recorded were compared with various literatures from NNDC and this shows an excellent agreement with each and the results are presented together with their calculated relative intensities.

Keywords: Absolute relative error, accuracy, comparative study, stability.

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1. Introduction

Calcium-42 is one of the isotopic-nucleus of calcium with 22 neutrons and 20 protons. The two excess neutrons present in the nucleons distinguish it from the first stable nucleus of $^{40}$Ca with either protons or neutrons being magic. The heaviest of the isotopes is $^{48}$Ca with 8-neutrons higher than $^{40}$Ca [1]. The measured gamma energies of the nucleus have been reported in several articles with some of them showing the relative intensities of the measured gamma transitions. In this, the relative intensities of these gamma energies have been measured after they were identified to be associated with $^{42}$Ca through the instrumentalities of Coincidence analysis [2].

2. Experimental Details

In the Coulomb unsafe reaction of $^{192}$Os target with the $^{18}$O beam at 80 $MeV$ using the 9 $MV$ tandem accelerator of the Horia Hulubei National Institute of Physics and Nuclear Engineering (known as IFIN-HH) in Bucharest [3], a fusion multi-particle of 2n2p was evaporated from the fusion of $^{28}$Si target with $^{18}$O – beam. $^{28}$Si was found to be one of the impurities in the $^{192}$Os target foil material bought from the Trace company in USA. This contaminated percentage of $^{42}$Ca and other chemical impurities from the target were observed to have reacted during the experiment when the $^{18}$O beam delivered the laboratory energy of 80 $MeV$ on the $^{192}$Os target in the chamber of the accelerator. Details of the purity composition of the $^{192}$Os are as shown in Table 1.

This nuclear fusion evaporation reaction produced $^{42}$Ca as
the product of the reaction after evaporating \(2n2p\) particles from the compound with the beam current of 20 \( pnA \) with a hardware trigger condition of either \( \text{LaBr}_3(\text{Ce}) - \text{LaBr}_3(\text{Ce}) \) or \( \text{HPGe} - \text{HPGe} \) [4, 5]. The predicted fusion-evaporation cross-section for the observed channels (that is, from 60 \( \text{MeV} \) to 100 \( \text{MeV} \)) have \(42\text{Ca}\) nucleus dominating the entire laboratory energy region as chosen in this work. The relative cross-section measured for the \(42\text{Ca}\) nucleus is \(\leq 100 \text{ mb} \) [4, 5].

The experiment for the \(18\text{O}\) beam on \(192\text{Os}\) target was conducted for a period of 9 consecutive days at IFIN-HH Bucharest within which an approximate count of 1,200,000.00 was recorded using the ROmanian SPectroscopy in HEavy REactions, ROSPHERE gamma-ray array of 14 High Purity Germanium, HPGe and 11 Lathanum-Bromide doped Cerium, \(\text{LaBr}_3(\text{Ce})\) detectors [4, 5, 6].

Table 1. The \(^{192}\text{Os}\) Target with the Observed Chemical Impurities [5]

| Element      | Symbol | Impurity Measurement (ppm) |
|--------------|--------|----------------------------|
| Aluminium    | Al     | 500                        |
| Calcium      | Ca     | 100                        |
| Copper       | Cu     | 70                         |
| Iron         | Fe     | 500                        |
| Magnesium    | Mg     | 50                         |
| Manganese    | Mn     | 50                         |
| Nickel       | Ni     | 100                        |
| Lead         | Pb     | 50                         |
| Platinum     | Pt     | 50                         |
| Silicon      | Si     | 500                        |
| Tungsten     | W      | 100                        |

3. Data Analysis

Coincidence analysis was performed on the detected gamma energies from the ROSPHERE gamma-ray array detectors of the IFIN-HH Bucharest and these were identified to be associated with \(^{42}\text{Ca}\). Doing this, a gating condition was used where a particular gamma transition was selected as a reference energy and all other energies that were seen to be in coincidence, that is, appearing with the selected gate at the same time were recorded. This was to further confirm that the measured gamma transitions were indeed associated with \(^{42}\text{Ca}\) [1, 7, 8]. Table 2 shows all the measured gamma transitions in the current work. The partial energy level scheme of \(^{42}\text{Ca}\) was obtained as shown in Figure 1 using RADware.

Table 2. Details of the Observed Transitions in the Current Work as Detected from the \(^{28}\text{Si}(^{18}\text{O},2n2p)^{42}\text{Ca}\)

| \(E_\gamma(\text{keV})\) | \(E_i \rightarrow E_f\) | \(I_\gamma\) | Transition       |
|------------------------|-----------------------|------------|------------------|
| 146                    | 6555 \(\rightarrow\) 6409 | 23         | \(9^- \rightarrow 8^-\)   |
| 264                    | 6409 \(\rightarrow\) 6146 | 7          | \(8^- \rightarrow 7^-\)   |
| 437                    | 3190 \(\rightarrow\) 2752 | 50         | \(6^+ \rightarrow 4^+\)   |
| 810                    | 6555 \(\rightarrow\) 5747 | 28         | \(9^- \rightarrow 7^-\)   |
| 815                    | 7369 \(\rightarrow\) 6555 | 20         | \(10^- \rightarrow 9^-\)  |
| 910                    | 4099 \(\rightarrow\) 3190 | 36         | \(5^- \rightarrow 6^+\)   |
| 917                    | 6409 \(\rightarrow\) 5492 | 18         | \(8^- \rightarrow 6^-\)   |
| 1227                   | 2752 \(\rightarrow\) 1525 | 78         | \(4^+ \rightarrow 2^+\)   |
| 1347                   | 4099 \(\rightarrow\) 2752 | 7          | \(5^- \rightarrow 4^+\)   |
| 1525                   | 1525 \(\rightarrow\) 0   | 100        | \(2^+ \rightarrow 0^+\)   |
| 1645                   | 5745 \(\rightarrow\) 4099 | 28         | \(7^- \rightarrow 5^-\)   |

Figure 1. Symmetrical HPGe \(\gamma - \gamma\) matrix showing gates on 1227 keV and 1525 keV (left panel). The right panel of the figure shows the same gates on 1227 keV and 1525 keV gamma energies but with a different folding coincidence condition of \(\gamma - \gamma - \gamma\) (triple) trigger in HPGe detectors using RADware and GASpware softwares.

4. The Measured Energy Levels Associated with \(^{42}\text{Ca}\) in the Current Work

The 1525-keV Level. The 1525 keV level is fed with a 1227 keV transition from the yrast \(I^\pi = 4^+\) state to the \(I^\pi = 2^+\). This energy level is assigned a spin of 2 with a positive parity. It decays to the ground state 0+ with the gamma energy of 1525 keV. The relative intensities of the gamma transitions have been determined in this current work as shown in Table 2.

The 2752-keV Level. This energy level is populated by 437 keV gamma transition which is a decay from the 3190 keV level to a spin and positive parity of 4+. The relative intensity is calculated to be 50 (even though the directional correlations from
oriented states DCO’s calculation is not shown here). The multipolarity is dominantly an E2, but can possibly be an M3 transition using the expression in equation (1):

\[ |I_i - I_f| \leq \Delta L \leq |I_i + I_f|, \]  

(1)

where the largest possible value of \( \Delta L \) is \( I_i + I_f \) and the lowest possible value \( I_i - I_f \). The parity change in the transition is given by the selection rules [9].

The 3190-keV Level. As shown in Figure 2 of the current work, more than two gamma transitions populated this energy level but with different experimental branching ratios, B(M1)/B(M2) (not determined here). Apart from 910 keV transition energy populating this state, both 2956 keV and 2302 keV gamma transitions are not observed in this current work. This also forms the basis for which the gamma transitions are shown as broken lines and under brackets. The observed multipolarity is M1 which is the likely dominant one. This is so because there is a strong dependence of the transition rate on multipolarity where the lowest multiplicities are most likely to occur [9]. The relative intensity of the 910 keV gamma transition is calculated as 18 and this is shown in Table 2.

5. Discussion and Conclusion

The coincidence spectra on selected gamma transition energies in the left panel of Figure 1 is a double fold: that is, \( \gamma - \gamma \) matrix sorting condition in the master trigger of ROSPHERE. In this sorting, the gamma energy generally has more counts as recorded for same gates in triple fold gating condition. On the 1227 keV gate, gamma transitions of 145-, 264-, 382-, 437-, 810-, 815-, 910-, 917-, 1347-, 1525-, and 1645-keV were observed to be in coincidence with one another with 437-keV having the highest counts of approximately 2000 counts/keV. Looking at both Figures 1.0 and 2.0, 1227 keV and 1525 keV are coincident with each other. This implies that, a gate on either one should produce the other one in coincidence. On 1525 keV gate, gamma transitions found to be in coincidence are the 145-, 437-, 507-, 810-, 910-, 1227-, and 1645-keV [7, 8, 5, 10]. The coincidence analysis performed in Figure 1 further affirms the assigned nucleus of \( ^{42}\text{Ca} \) in the current work where the gamma transitions have already been reported by other researchers [1].

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