Guiding Monocular Depth Estimation Using Depth-Attention Volume

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Abstract. Recovering the scene depth from a single image is an ill-posed problem that requires additional priors, often referred to as monocular depth cues, to disambiguate different 3D interpretations. In recent works, those priors have been learned in an end-to-end manner from large datasets by using deep neural networks. In this paper, we propose guiding depth estimation to favor planar structures that are ubiquitous especially in indoor environments. This is achieved by incorporating a non-local coplanarity constraint to the network with a novel attention mechanism called depth-attention volume (DAV). Experiments on two popular indoor datasets, namely NYU-Depth-v2 and ScanNet, show that our method achieves state-of-the-art depth estimation results while using only a fraction of the number of parameters needed by the competing methods.

Keywords: Monocular depth · Attention mechanism · Depth estimation.

1 Introduction

Depth estimation is a fundamental problem in computer vision due to its wide variety of applications including 3D modeling, augmented reality and autonomous vehicles. Conventionally it has been tackled by using stereo and structure from motion techniques based on multiple view geometry. In recent years, the advances in deep learning have made monocular depth estimation a compelling alternative [5, 17, 22, 8, 24, 10, 18, 26, 41, 25, 12, 2, 37].

In monocular depth estimation, the basic idea is simply to train a model to predict a depth map for a given input image, and to hope that the model can learn those monocular cues that enable inferring the depth directly from the pixel values. This kind of a brute-force approach requires a huge amount of training data and leads to large network architectures. It has been a common practice to use a deep encoder such as VGG-16 [5], ResNet-50 [17, 24, 25], ResNet-101 [8], ResNext-101 [37], SeNet-154 [12, 2] followed by some upsampling and fusion strategy including the up-projection module [17], multi-scale feature fusion [12] or adaptive dense feature fusion [2] that all result in bulky networks with a large
number of parameters. Because high computational complexity and memory requirements limit the use of these networks in practical applications, also fast monocular depth estimation models such as FastDepth have been proposed, but their speed increase comes with the price of reduced accuracy. Moreover, despite of good results achieved with standard benchmark datasets such as NYU-Depth-v2, it still remains questionable if these networks are able to generalize well to unseen scenes and poses that are not present in the training data.

Instead of trying to learn all the monocular cues blindly from the data, in this paper, we investigate an approach where the learning is guided by exploiting a simple coplanarity constraint for scene points that are located on the same planar surfaces. Coplanarity is an important constraint especially in indoor environments that are composed of several non-parallel planar surfaces such as walls, floor, ceiling, tables, etc. We introduce a concept of depth-attention volume (DAV) to aggregate spatial information non-locally from those coplanar structures. We use both fronto-parallel and non-fronto-parallel constraints to learn the DAV in an end-to-end manner.

It should be noticed that plane approximations have already been used previously in monocular depth estimation, for example, in PlaneNet, where 3D planes were explicitly segmented and estimated from the images, but in contrast to these works, we embed the coplanarity constraint implicitly to the model by using the DAV, which is a building block inspired by the non-local neural networks. Unlike the convolutional operation, it operates non-locally and produces a weighted average of the features across the whole image paying attention on planar structures, and favoring depth values that are originating from those planes. By using the DAV we not only incorporate an efficient and important geometric constraint to the model, but also enable shrinking the size of the network considerably without sacrificing the accuracy. To summarize, our key contributions include:

- A novel attention mechanism called depth-attention volume that captures non-local depth dependencies between coplanar points.
- An end-to-end neural network architecture that implicitly learns to recognize planar structures from the scene and use them as priors in monocular depth estimation.
- State-of-the-art depth estimation results on NYU-Depth-v2 and ScanNet datasets with a model that uses considerably less parameters than previous methods achieving similar performance.

The source code and the model will be made publicly available upon publication of the paper.

2 Related work

Learning-based monocular depth estimation: Saxena et al. is one of the first studies using Markov Random Field (MRF) to predict depth from a single image. Later on Eigen et al. proposed method to estimate depth using
Fig. 1. Visualization of depth-attention maps. The input image with four query points is shown on the left. The corresponding ground-truth and predicted depth maps are in the middle. Because of the coplanarity prior the depth of the textureless white wall can be accurately recovered. The ground-truth and predicted depth-attention maps for the query points are on the right. Warm colour indicates strong depth prediction ability for the query point.

multi-scale deep network [6] and a multi-task learning model [5]. Since then, various studies using deep neural networks (DNNs) have been introduced. Laina et al. [17] employed a fully convolutional residual network (FCRN) as the encoder and four up-projection modules as the decoder to up-sample the depth map resolution. Fu et al. [8] successfully formulated monocular depth estimation as an ordinal regression problem. Qi et al. [24] proposed a network called GeoNet that investigate the duality between depth map and surface normal. The DNNs from Ren et al. [26] classified input images as indoor or outdoor before estimating the depth values. Lee et al. [18] suggested an idea of using a DNNs to estimate the relative depth between pairs of pixels. The proposed method from Jiao et al. [14] incorporated object segmentation into the training to increase depth estimation accuracy. Hu et al. [12] introduced an architecture that included an encoder, a decoder, a multi-scale feature fusion (MFF), and a new loss term for preserving edge structures. Inspired by [12], Chen et al. [2] used adaptive dense feature fusion (ADFF), and residual pyramid decoder in their network. The study by Facil et al. [7] proposed a DNNs that aims to learn calibration-aware patterns to improve the generalization capabilities of monocular depth prediction. Recently, Ramamonjisoa et al. [25] presented SharpNet that exploits occluding contours as an additional driving factor to optimize the depth estimation model besides the depth and the surface normal.

**Plane-based approaches:** Liu et al. [22] was the first study to consider using the planar constraint to predict depth maps from single images. Later the same authors published an incremental study to refine the quality of plane segmentation [21]. Yin et al. [37] formed a geometric constraint called virtual normal to predict the depth map as well as a point cloud and surface normals. Note that methods by Liu et al. focused explicitly on estimating a set of plane parameters and planar segmentation masks, while Yin et al. calculated a large virtual plane to train a DNNs that is robust to noise in the ground truth depth.

**Attention mechanism:** Attention was initially used in machine translation and it was brought to computer vision by Xu et al. [36]. Since then, attention mech-
anism has evolved and branched into channel-wise attention [11,30], spatial-wise attention [32,1] and mix attention [31] in order to tackle object detection and image classification problems. Some recent monocular depth estimation studies also followed this line of work. Xu et al. [35] proposed multi-scale spatial-wise attention to guide a Conditional Random Fields (CRFs) model. Li et al. [20] proposed a discriminative depth estimation model using channel-wise attention. Kong et al. [16] embedded a discrete binary mask, namely the pixel-wise attentional gating unit, into a residual block to modulate learned features.

In this paper, we propose using depth-attention volume (DAV) to encode non-local geometric dependencies. It can be seen as an attention mechanism that guides depth estimation to favor depth values originating from planar surfaces that are ubiquitous in man-made scenes. In contrast to previous plane-based approaches, we do not train the network to segment the planes explicitly, but instead, we let the network to learn the coplanarity constraint implicitly.

3 Proposed Method

This section describes the proposed depth estimation method. The first subsection defines the depth-attention volume and the following two subsections outline the network architecture and the loss functions. Further details are provided in the supplementary material.

3.1 Depth-attention volume

Given two image points \( P_0 = (x_0, y_0) \) and \( P_1 = (x_1, y_1) \) with corresponding depth values \( d_0 \) and \( d_1 \), we define that the depth-attention \( A(P_0, P_1) \) is the ability of \( P_1 \) to predict the depth of \( P_0 \). This ability is quantified as a confidence...
in the range \([0, 1]\) so that 0 means no ability and 1 represents maximum certainty of being a good predictor.

To estimate \(A\) we make the assumption that the scene contains multiple non-parallel planes, which is common particularly in indoor environments. The depth values of all points belonging to the same plane are linearly dependent. Hence, they are good depth predictors of each other. To exploit this property, we detect \(N\) prominent planes from the training images and parameterize each plane with \(S = (n_x, n_y, n_d, c)\), where \((n_x, n_y, n_d)\) is the plane normal and \(c\) is the orthogonal distance from the origin. We construct the first-order depth-attention volumes for all \(N\) planes:

\[
A_i(P_0, P_1) = 1 - \sigma(|S_i \cdot X_0| + |S_i \cdot X_1|), \quad i = 1, \ldots, N
\]  

where \(\sigma\) is the sigmoid function, \(X_0 = (x_0, y_0, d_0, 1)\) and \(X_1 = (x_1, y_1, d_1, 1)\). These volumes are represented as 4-D tensors of size \(H \times W \times H \times W\), where \(H\) and \(W\) are the vertical and horizontal sizes, respectively. In practice, one needs to subsample the volumes to keep the memory requirements reasonable. In all our experiments, we used a subsampling factor of 8.

In addition, we assume that all points located on the same fronto-parallel plane are good depth predictors of each other, because they share the same depth value. We use the ground-truth depths, and create a zero-order depth-attention volume (DAV) for every training image

\[
A_0(P_0, P_1) = 1 - \sigma(|d_0 - d_1|).
\]  

Finally, we combine these volumes by taking the maximum attention value of all volumes:

\[
A_D(P_0, P_1) = \max(A_i(P_0, P_1)), \quad i = 0, \ldots, N
\]

It is easy to observe that DAV is a symmetric function, i.e. \(A_D(P_0, P_1) = A_D(P_1, P_0)\).

If we consider \(P_0\) to be a query point in the image as illustrated in Figure 1\(^1\) (left), we can visualize the DAV as a two-dimensional attention map shown in Figure 1\(^1\) (right). Figure 2\(^1\) provides an example of a depth-attention volume generated from the ground truth depth map.

### 3.2 Network Architecture

Figure 3\(^2\) gives an overview of our model that includes three main modules: an encoder, a non-local depth-attention module, and a decoder.

We opt to use a simplified dilated residual networks (DRN) with 22 layers (DRN-D-22)\(^3,39\) as our encoder, which extracts high-resolution features and downsamples the input image only 8 times. The DRN-D-22 is a variation of DRN that completely removes max-pooling layers as well as smoothly distributes the dilation to minimize the gridding artifacts. This is crucial to our network, because to make training feasible, the non-local depth-attention module needs to
operate on a sub-sampled feature space. However, to capture meaningful spatial relationships this feature space also needs to be large enough.

The decoder part of our network contains a straightforward up-scaling scheme that increases the spatial dimension from $29 \times 38$ to $57 \times 76$ and then to $114 \times 152$. Upsampling consists of two bilinear interpolation layers followed by convolutional layers with a kernel size of $3 \times 3$. Two convolutional layers with a kernel size of $5 \times 5$ are then used to estimate the final depth map.

The non-local depth-attention module is located between the encoder and the decoder. It maps the input features $X$ to the output features $Y$ of the same size. The primary purpose of the module is to add the non-local information embedded in the depth-attention volume (DAV) to $Y$, but it is also used to predict and learn the DAV based on the ground-truth data. The structure of the module is presented in Figure 4.

We implement the DAV-predictor by first transforming $X$ into green and blue embeddings using $1 \times 1$ convolution. We exploit the symmetry of DAV, and maximize the correlation between these two spaces by applying cross-denormalization on both green and blue embeddings. Cross-denormalization is a conditional normalization technique [4] that is used to learn an affine transformation from the data. Specifically, the green embedding is first normalized to zero mean and unit standard deviation using batch-normalization (BN). Then, the blue embedding is convolved to create two tensors that are multiplied and added the normalized features from the green branch, and vice versa. The denormalized representations are then activated with ReLUs and transformed by another $1 \times 1$ convolution before multiplying with each other. Finally, the DAV is activated using the sigmoid function to ensure that the output values are in range $[0, 1]$. We empirically verified that applying cross-modulation in two embedding spaces is superior than using a single embedding with double the number of features.

Furthermore, $X$ is fed into the orange branch and multiplied with the estimated DAV to amplify the effect of the input features. Finally, we add a residual connection (red) to prevent the vanishing gradient problem when training our network.

![Diagram](image)

**Fig. 3.** The pipeline of our proposed network. An image is passed through the encoder, then the non-local depth-attention module, and finally the decoder to produce the estimated depth map. The model is trained using $L_{attention}$ and $L_{depth}$ losses, which are described in Subsection 3.3.
3.3 Loss Function

As illustrated in Figure 3, our loss function consists of two main components: attention loss and depth loss.

**Attention loss:** The primary goal of this term is to minimize the error between the estimated (output of the DAV-predictor in Figure 4) and the ground-truth DAV. The $L_{\text{mae}}$ is defined as the mean absolute error between the predicted and the ground truth depth-attention values:

$$L_{\text{mae}} = \frac{1}{(HW)^2} \sum_{i} \sum_{j} |\hat{A}_{i,j} - A_{i,j}|$$  \hspace{1cm} (4)

where $\hat{A}_{i,j} \equiv \hat{A}_{D}(P_i, P_j)$ and $A_{i,j} \equiv A_{D}(P_i, P_j)$ are the predicted and ground truth depth-attention volumes.

In addition, we minimize the angle between the predicted and the ground truth depth-attention maps for all query positions $i$ and $j$:

$$L_{\text{ang}} = \frac{1}{HW} \left( \sum_{i} \left| 1 - \frac{\sum_{j} \hat{A}_{i,j} A_{i,j}}{\sqrt{\sum_{j} \hat{A}_{i,j}^2 \sum_{j} A_{i,j}^2}} \right| + \sum_{j} \left| 1 - \frac{\sum_{i} \hat{A}_{i,j} A_{i,j}}{\sqrt{\sum_{i} \hat{A}_{i,j}^2 \sum_{i} A_{i,j}^2}} \right| \right)$$  \hspace{1cm} (5)

The full attention loss is defined by

$$L_{\text{attention}} = L_{\text{mae}} + \lambda L_{\text{ang}}$$  \hspace{1cm} (6)

where $\lambda \in \mathbb{R}^+$ is the weight loss coefficient.

**Depth loss:** Moreover, we define depth loss as a combination of three terms $L_{\text{log}}$, $L_{\text{grad}}$ and $L_{\text{norm}}$ that were originally introduced in [12]. The $L_{\text{log}}$ loss is a variation of the $L_1$ norm that is calculated in the logarithm space and defined as

$$L_{\text{log}} = \frac{1}{M} \sum_{i=1}^{M} F(|\hat{d}_i - d_i|)$$  \hspace{1cm} (7)
where \( M \) is the number of valid depth values, \( d_i \) is the ground truth depth, \( \hat{d}_i \) is the predicted depth, and \( F(x) = \log(x + \alpha) \) with \( \alpha \) set to 0.5 in our experiments.

Another loss term is \( L_{grad} \), which is used to penalize sudden changes of edge structures in both \( x \) and \( y \) directions. It is defined by

\[
L_{grad} = \frac{1}{M} \sum_{i=1}^{M} F(\Delta_x(|\hat{d}_i - d_i|)) + F(\Delta_y(|\hat{d}_i - d_i|))
\]

where \( \Delta_x \) and \( \Delta_y \) is the gradient of the error with respect to \( x \) and \( y \). Finally, we use \( L_{norm} \) to emphasize small details by minimizing the angle between the ground truth (\( n_i \)) and the predicted (\( \hat{n}_i \)) surface normals:

\[
L_{norm} = \frac{1}{M} \sum_{i=1}^{M} |1 - \hat{n}_i \cdot n_i|.
\]

Hence, the depth loss is defined by

\[
L_{depth} = L_{\log} + \mu L_{grad} + \theta L_{norm}
\]

where \( \mu, \theta \in \mathbb{R}^+ \) are weight loss coefficients. Our full loss is

\[
\mathcal{L} = \mathcal{L}_{attention} + \gamma \mathcal{L}_{depth}
\]

where \( \gamma \in \mathbb{R}^+ \) is a weight loss coefficient. Subsection 4.2 describes in detail how the network is trained using these loss functions.

4 Experiments

In this section, we evaluate the performance of the proposed method by comparing it against several baselines. We start by introducing datasets, evaluation metrics, and implementation details. The last three subsections contain the comparison to the state-of-the-art, ablation studies, and a cross-dataset evaluation. Further results are available in the supplementary material.

4.1 Datasets and evaluation metrics

Datasets: We assess the proposed method using NYU-Depth-v2 [28] and ScanNet [3] datasets. NYU-Depth-v2 contains \( \sim 120K \) RGB-D images obtained from 464 indoor scenes. From the entire dataset, we use 50K images for training and the official test set of 654 images for evaluation. ScanNet dataset comprises of 2.5 million RGB-D images acquired from 1517 scenes. For this dataset, we use the training subset of \( \sim 20K \) images provided by the Robust Vision Challenge 2018 [9] (ROB). Unfortunately, the ROB test set is not available, so we report the results on the Scannet official test set of 5310 images instead. SUN-RGBD is yet another indoor dataset consisting of \( \sim 10K \) images collected with four different sensors. We do not use it for training, but only for cross-evaluating the pre-trained models on the test set of 5050 images.
**Evaluation metrics:** The performance is assessed using the standard metrics provided for each dataset. That is, for NYU-Depth-v2 \cite{28} we calculate the mean absolute relative error (REL), root mean square error (RMSE), and thresholded accuracy ($\delta_1$). For the ScanNet and SUN-RGBD dataset, we provide the mean absolute relative error (REL), mean square relative error (sqREL), scale-invariant mean squared error (SI), mean absolute error (iMAE), and root mean square error (iRMSE) of the inverse depth values. Detailed definitions of the metrics are provided in the supplementary material.

### 4.2 Implementation Details

The proposed model is implemented with the Pytorch \cite{23} framework, and trained using a single Tesla-V100, batch size of 32 images, and Adam optimizer \cite{15} with $(\beta_1, \beta_2, \epsilon) = (0.9, 0.999, 10^{-8})$. The training process is split into three parts. During the first phase, we replace the DAV-predictor (Figure 4) with the DAVs computed from the ground truth depth maps. We train the model for 200 epochs using only the depth loss (Eq. 10) and the learning rate of $10^{-4}$. In the second phase, we add the DAV-predictor to the model, freeze the weights of other parts of the model, and train for 200 epochs with the learning rate of $7.0 \times 10^{-5}$. In the last phase, we train the entire model for 300 epochs using the learning rate of $7.0 \times 10^{-5}$ for the first 100 epochs and then reduce it at the rate of 5% per 25 epochs. The last two stages employ the full loss function defined in Equation (11). We set all the weight loss coefficients $\lambda, \mu, \theta,$ and $\gamma$ as 1.

We augment the training data using random scaling ([0.875, 1.25]), rotation([-5.0, +5.0] degrees), horizontal flip, rectangular window droppings, and colorization. Planes, required for training, are obtained by fitting a parametric model to the back-projected 3D point cloud using RANSAC with the inlier threshold of 1 cm.

![Accuracy & model size](image1)

![Absolute relative error & model size](image2)

**Fig. 5.** Analyzing the accuracy $\delta_1(\%)$ and mean absolute relative error (\%) with respect to the number of parameters (millions) for recent monocular depth estimation methods on NYU-Depth-v2. The left picture presents the thresholded accuracy where higher values are better, while the right picture shows the absolute relative error where lower values are better.
Table 1. Evaluation results on the NYU-Depth-v2 dataset. Metrics with ↓ mean lower is better and ↑ mean higher is better.

| Architecture | #params | REL ↓ | RMSE ↓ | δ1 ↑ | δ2 ↑ | δ3 ↑ |
|--------------|---------|-------|--------|------|------|------|
| Eigen’15 [5] ** | 141.1M | 0.215 | 0.907 | 0.611 | 0.887 | 0.971 |
| Laina’16 [17] ** | 63.4M | 0.127 | 0.573 | 0.811 | 0.953 | 0.988 |
| Liu’18 [22] † | 47.5M | 0.142 | 0.514 | 0.812 | 0.957 | 0.989 |
| Fu’18 [8] ** | 110.0M | 0.115 | 0.509 | 0.828 | 0.965 | 0.992 |
| Qi’18 [24] | 67.2M | 0.128 | 0.569 | 0.834 | 0.960 | 0.990 |
| Hao’18 [10] | 60.0M | 0.127 | 0.555 | 0.841 | 0.966 | 0.991 |
| Lee’19 [18] | 118.6M | 0.131 | 0.538 | 0.837 | 0.971 | 0.994 |
| Ren’19 [26] ** | 49.8M | 0.113 | 0.501 | 0.833 | 0.968 | 0.993 |
| Zhang’19 [41] | 95.4M | 0.121 | 0.497 | 0.846 | 0.968 | 0.994 |
| Ramamonjisoa’19 [25] † | 80.4M | 0.139 | 0.502 | 0.836 | 0.966 | 0.993 |
| Hu’19 [12] | 157.0M | 0.115 | 0.530 | 0.866 | 0.975 | 0.993 |
| Chen’19 [2] | 210.3M | 0.111 | 0.514 | 0.878 | 0.977 | 0.994 |
| Yin’19 [37] | 114.2M | 0.108 | 0.416 | 0.875 | 0.976 | 0.994 |
| Ours | 25.1M | 0.108 | 0.412 | 0.882 | 0.980 | 0.996 |

4.3 Comparison with the state-of-the-art

In this section, we compare the proposed approach with the current state-of-the-art monocular depth estimation methods.

NYU-Depth-v2: Table 1 contains the performance metrics on the official NYU-Depth-v2 test set for our method and for [5,17,22,10,24,18,26,41,25,12,2,37]. In addition, the table shows the number of model parameters for each method. The performance figures for the baselines are obtained using the pre-trained models provided by the authors [22,8,25,12,2,37] or from the original papers if the model was not available [5,17,24,10,18,26,41]. Methods indicated with ** and † are trained using the entire training set of 120K images or with external data, respectively. For instance, Ramamonjisoa et al. [25] trained the method using synthetic dataset PBRS [40] before fine-tuning on NYU-Depth-v2. The best performance is achieved by the proposed model that also contains the least amount of parameters. The best performing baselines, Yin et al. [37], Hu et al. [12], and Chen et al. [2], have 4.5, 6.2, and 8.3 times more parameters compared to ours, respectively. Figure 5 provides an additional illustration of the model parameters with respect to the performance.

Figure 6 shows qualitative examples of the obtained depth maps. In this case, the maps for the baseline methods are produced using the pre-trained models provided by the authors. The method by Eigen and Fergus [5] performs well on uniform regions, but has difficulties in detailed structures. Laina et al. [17] produces overly smoothed depth maps losing many small details. In contrast, Fu et al. [8] returns many details, but with the expense of discontinuities inside objects or smooth areas. The depth images by Ramamonjisoa et al. [25] contain noise and are prone to miss fine details. Yin et al. [37], Hu et al. [12], and Chen et al.
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Fig. 6. Qualitative results on the official NYU-Depth-v2 [28] test set from different methods. The color indicates the distance where red is far and blue is close. Our estimated depth maps are closer to the ground truth depth when comparing with state-of-art methods.

[2] provide the best results among the baselines. However, they have difficulties e.g. on the third (near the desk and table) and the fourth examples from the left (wall area). We provide further qualitative examples in the supplementary material.

ScanNet: Table [2] contains the performance figures on the official ScanNet test set for our method, Ren et al. [26] (taken from the original paper), Hu et al. [12] and Chen et al. [2]. We use the public code from [12][2] to train their models. Unfortunately, the other baselines do not provide the results for ScanNet official test set. Moreover, the test set used in the Robust Vision Challenge (ROB) is not available at the moment and we are unable to report our performance on that. Nevertheless, we have included the best methods from the ROB challenge.
Table 2. Evaluation results on ScanNet [3].

| Architecture | #params | REL  | sqREL | SI  | iMAE | iRMSE | Test set |
|--------------|---------|------|-------|-----|------|-------|----------|
| CSWS.E.ROB   | 65.8M   | 0.150| 0.060 | 0.020| 0.100| 0.130 | ROB      |
| DORN.ROB     | 110.0M  | 0.140| 0.060 | 0.020| 0.100| 0.130 | ROB      |
| DABC.ROB     | 56.6M   | 0.140| 0.060 | 0.020| 0.100| 0.130 | ROB      |
| Hu’19        | 157.0M  | 0.139| 0.081 | 0.016| 0.100| 0.105 | Official |
| Chen’19      | 210.3M  | 0.134| 0.077 | 0.015| 0.093| 0.100 |         |
| Ren’19       | 49.8M   | 0.138| 0.057 | -    | -    | -     |          |
| Ours         | 25.1M   | 0.118| 0.057 | 0.015| 0.089| 0.097 |          |

in Table 2 to provide indicative comparison. Note that all methods are trained with the same ROB training split. The proposed model outperforms [26] with a clear margin in terms of REL. The results are also substantially better compared to ROB challenge methods, although the comparison is not strictly fair due to different test splits. Figure 7 provides qualitative comparison between our method and [12,2,20], using the sample images provided in [20]. The geometric structures and details are clearly better extracted by our method.

4.4 Ablation studies

Firstly, we assess how the number of prominent planes, used to estimate the ground truth DAVs in the training phase, affects the performance (see Sec. 3.1). To this end, we train our model using the fronto-parallel planes (see Eq. 2).

Fig. 7. Predicted depth maps from our model with baselines on the official ScanNet [3] test set.
Fig. 8. The benefit of applying the planar constraint to calculate the depth-attention volume. The above images show the error maps in planar areas. Error maps have the same scale, and warm color indicates high values.

Table 3. Performance of our model using different types of depth-attention volume.

| DAV-types   | REL ↓ | RMSE ↓ | δ1 ↑ | δ2 ↑ | δ3 ↑ |
|-------------|-------|--------|------|------|------|
| 0-Plane-DAV | 0.116 | 0.442  | 0.867| 0.976| 0.995|
| 3-Plane-DAV | 0.110 | 0.421  | 0.879| 0.978| 0.995|
| 5-Plane-DAV | 0.108 | 0.412  | 0.882| 0.980| 0.996|
| 7-Plane-DAV | 0.111 | 0.447  | 0.851| 0.970| 0.993|

Table 4. Ablation studies of models without and with the attention loss on the NYU-Depth-v2. This shows the importance of the DAV in guiding the monocular depth model.

| Training                | REL ↓ | RMSE ↓ | δ1 ↑ | δ2 ↑ | δ3 ↑ |
|-------------------------|-------|--------|------|------|------|
| w/o Lattention          | 0.126 | 0.540  | 0.841| 0.967| 0.992|
| w/ full loss            | 0.108 | 0.412  | 0.882| 0.980| 0.996|
| continue w/o Lattention | 0.109 | 0.415  | 0.882| 0.979| 0.995|

plus zero, three, five, and seven non-fronto-parallel planes (N in Eq. 1). The corresponding results for the NYU-Depth-v2 test set are provided in Table 3. One can observe that the results improve by increasing the number of planes up to five and decrease after that. Possible explanation for this could be that the images used in the experiments do not typically contain more than five significant planes that can predict the depth values reliably. Figure 8 illustrates errors in depth estimation for planar areas for five- and zero-plane versions. The five-plane version has clearly smaller errors and they are more evenly distributed.

Secondly, we study the impact of the attention loss term (Eq. 6). For this purpose, we first train our model with and without the attention loss, and then continue training by dropping the attention loss after convergence. We report the results in Table 4. The model without the attention loss has clearly inferior performance indicating the importance of this loss term. Furthermore, continuing training by dropping the attention loss also degrades the performance.
4.5 Cross-dataset evaluation

To assess the generalisation properties of the model, we perform a cross-dataset evaluation, where we train the network using NYU-Depth-v2 and test with SUN-RGBD \cite{29,13,34} without any fine-tuning. We also evaluate the baseline methods from \cite{12,2} and report the results in Table 5. As can be seen our model performs favourably compared to the other methods. Figure 9 contains a few examples of the results with the SUN-RGBD dataset. One can observe that our model is able to well estimate the geometric structures and details of the scene despite the differences in data distributions between the training and testing sets.

5 Conclusions

This paper proposed a novel monocular depth estimation method that incorporates a non-local coplanarity constraint with a novel attention mechanism called depth-attention volume (DAV). The proposed attention mechanism encourages depth estimation to favor planar structures, which are common especially in indoor environments. The DAV enables more efficient learning of the necessary priors, which results in considerable reduction in the number of model parameters. The performance of the proposed solution is state-of-the-art on two popular benchmark datasets while using 2-8 times less parameters than competing methods. Finally, the generalisation ability of the method was further demonstrated in cross dataset experiments.
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In this document, we present additional qualitative results on NYU-Depth-v2 and SUN-RGBD datasets in Section A and B respectively. In addition, details of the network architecture are described in Section C while Section D gives the definitions of the evaluation metrics.

A Additional qualitative results on NYU-Depth-v2

This section provides further results and analysis on NYU-Depth-v2 dataset.

A.1 Depth map with and without $L_{attention}$

As shown in Figure 1 and 2, the model with full loss significantly improves depth map quality at boundaries and detailed areas.

Fig. 1. Predicted depth maps from our model train with and without the $L_{attention}$ term.
Fig. 2. Predicted depth maps from our model train with and without the $L_{attention}$ term.
A.2 Point cloud reconstructions

We further examine the accuracy of the predicted depth maps by reconstructing the point clouds of three arbitrary views in the NYU-Depth-v2 test set. The back-projected 3D points are shown in Figure 3. The results near the walls, floors and ceilings are virtually linear and close to the ground truths.

Fig. 3. Reconstructed point clouds for a set of randomly selected examples from NYU-Depth-v2. The images from the point clouds are captured in different camera poses to provide an overview of the 3D scenes.
B  Additional qualitative results of cross-dataset evaluation on SUN-RGBD

In this section, we use our pretrained model on NYU-Depth-v2 [53] to estimate depth values from SUN-RGBD images [54, 49, 55]. Dissecting the predicted depth maps, reconstruction point clouds and attention maps demonstrates the generalization ability of our proposed method.

B.1  Predicted depth maps

As shown in Figure 4, our model provides reasonable depth maps for SUN-RGBD examples although it has not been trained on this dataset. The geometry layout of the scene is retained, even in difficult scenarios (e.g. images in row (5) and (6) in Figure 4).

![Figure 4](image)

**Fig. 4.** Randomly examples from the SUN-RGBD test set. Areas in the white boxes show missing or incorrect depth values from the ground truth data.
B.2 Analyzing the predicted attention maps

As depicted in Figure 5, the proposed network learns to pay attention on planar-areas. At the green query point in the first image, the network concentrates on table surfaces as indicated by the warm color in its attention map. At the magenta query point, the model shifts its attention to the wall in the background.

Fig. 5. Estimated attention and depth maps of our model train on NYU-Depth-v2 and test on SUN-RGBD. Left column presents predicted attention maps at indicated query points, while right column shows the predicted and ground truth depth maps. The input images are displayed in the middle.
B.3 Point cloud reconstruction

Figure [6] illustrates re-projected point clouds for SUN-RGBD examples produced by a model that is trained on NYU-Depth-v2. The produced point clouds are relatively close to the ground truth despite the fact that the model was trained on a different dataset.

Fig. 6. Reconstructed point clouds for randomly selected samples from the SUN-RGBD test set. The images of the point clouds are captured from different camera poses to provide an overview of the 3D scenes. The estimated depth maps are obtained from the model trained with NYU-Depth-v2.
C  Network architecture

This section gives complementary details regarding the network architecture and training process. The general structure of our network encompasses an encoder, a non-local depth attention module and a decoder. We construct the encoder by removing the average pooling and fully connected layer from the DRN-D-22 variation of the dilated residual networks [57, 58]. Table 1 shows the detailed structure of our encoder where \texttt{conv} represents 2D convolutional layer with specific kernel-size ($k$), stride ($s$), and dilation ($d$). \texttt{bn} stands for batch normalization. \texttt{CH} is the number of output channels and \texttt{RES} is the spatial resolution of the output feature maps. \texttt{basic-block} represents the basic residual block with corresponding dilation.

As explained in the manuscript, we split the training scheme into three parts. It is worth to mention that during the first training phase, we initialize the encoder with pre-trained weights on the ImageNet [44]. Our experiments confirm that using the pretraining model improves accuracy and speed of convergence. The second and third training stages follow the procedure described in the main paper.

| Input  | Operations  | $k$ | $s$ | $d$ | CH   | RES         | Output |
|--------|-------------|-----|-----|-----|------|-------------|--------|
| image  | conv+bn+relu| 7   | 1   | 1   | 16   | 228×304     | layer0 |
| layer0 | conv+bn+relu| 3   | 1   | 1   | 16   | 228×304     | layer1 |
| layer1 | conv+bn+relu| 3   | 2   | 1   | 32   | 114×152     | layer2 |
| layer2 | basic-block | -   | -   | -   | 1    | 64         | d-res-1a|
| d-res-1a| conv+bn     | 1   | 2   | 1   | 64   | 57×76       | d-res-1b|
| d-res-1b| basic-block | -   | -   | -   | 1    | 64         | layer3 |
| layer3 | basic-block | -   | -   | -   | 1    | 128        | d-res-2a|
| d-res-2a| conv+bn     | 1   | 2   | 1   | 128  | 29×38       | d-res-2b|
| d-res-2b| basic-block | -   | -   | -   | 1    | 128        | layer4 |
| layer4 | basic-block | -   | -   | -   | 2    | 256        | d-res-3a|
| d-res-3a| conv+bn     | 1   | 1   | 1   | 256  | 29×38       | d-res-3b|
| d-res-3b| basic-block | -   | -   | -   | 2    | 256        | layer5 |
| layer5 | basic-block | -   | -   | -   | 4    | 512        | d-res-4a|
| d-res-4a| conv+bn     | 1   | 1   | 1   | 512  | 29×38       | d-res-4b|
| d-res-4b| basic-block | -   | -   | -   | 4    | 512        | layer6 |
| layer6 | conv+bn+relu| 3   | 1   | 2   | 512  | 29×38       | layer7 |
| layer7 | conv+bn+relu| 3   | 1   | 1   | 512  | 29×38       | layer8-X|

The non-local depth attention module is the central component of our network with the detailed structure provided in Table 2. In that, \texttt{green}, \texttt{blue}, \texttt{orange} indicate the green, blue, and orange embedding spaces mentioned in the
manuscript. “⨀” denotes element-wise multiplication, “⨁” indicates element-wise sum, and “⨂” is the outer product. Layers denoted with ‡‡ imply reshaping and permuting the tensor to match the required shape for operation. Note that green-1bn, green-1γ, green-1β and blue-1bn, blue-1γ, blue-1β are generated at the same time as indicated by the dashed line.

Table 2. Internal structure of the non-local depth attention module.

| Input            | Operations          | k | s | d | CH | RES | Output          |
|------------------|---------------------|---|---|---|----|-----|-----------------|
| layer8-X         | conv                | 1 | 1 | 1 | 256 | 29 × 38 | orange         |
| layer8-X         | conv                | 1 | 1 | 1 | 1024 | 29 × 38 | green-1        |
| green-1          | bn                  | - | - | - | 1024 | 29 × 38 | green-1bn      |
| green-1          | conv                | 1 | 1 | 1 | 1024 | 29 × 38 | green-1γ       |
| green-1          | conv                | 1 | 1 | 1 | 1024 | 29 × 38 | green-1β       |
| green-1bn-γ, blue-1γ | ⊙                   | - | - | - | 1024 | 29 × 38 | green-1bn-γ    |
| green-1bn-γ, blue-1β | ⊕                   | - | - | - | 1024 | 29 × 38 | green-1-denorm |
| green-1-denorm   | relu+conv           | 1 | 1 | 1 | 1024 | 29 × 38 | green-2        |
| layer8-X         | conv                | 1 | 1 | 1 | 1024 | 29 × 38 | blue-1         |
| blue-1           | bn                  | - | - | - | 1024 | 29 × 38 | blue-1bn       |
| blue-1           | conv                | 1 | 1 | 1 | 1024 | 29 × 38 | blue-1γ        |
| blue-1           | conv                | 1 | 1 | 1 | 1024 | 29 × 38 | blue-1β        |
| blue-1bn-γ, blue-1γ | ⊙                   | - | - | - | 1024 | 29 × 38 | blue-1bn-γ     |
| blue-1bn-γ, blue-1β | ⊕                   | - | - | - | 1024 | 29 × 38 | blue-1-denorm  |
| blue-1-denorm    | relu+conv           | 1 | 1 | 1 | 1024 | 29 × 38 | blue-2         |
| green-2‡‡, blue-2‡‡ | ⊙                   | - | - | - | 1102 × 1102 | dav-1 |
| dav-1            | sigmoid             | - | - | - | 1102 × 1102 | dav-2 |
| dav-2, orange    | ⊙                   | - | - | - | 256 | 29 × 38 | dav-3‡‡        |
| dav-3            | conv+bn             | 1 | 1 | 1 | 512 | 29 × 38 | dav-4          |
| dav-4, layer8-X  | ⊕                   | - | - | - | 512 | 29 × 38 | layer8-Y       |

Unlike previous studies [45, 50, 47, 52, 59, 51, 48, 42, 56], we implement a straightforward decoder with two bilinear upsamplings follow by 2D convolutional layers and batch-normalizations. Finally, the upsampled feature maps are refined to produce the final depth map using two 2D convolutional layers. Table 3 provides a detailed structure of our decoder.

Table 3. Internal structure of the decoder where bilinear represents bilinear upsampling layers.

| Input            | Operations          | k | s | d | CH | RES | Output          |
|------------------|---------------------|---|---|---|----|-----|-----------------|
| layer8-Y         | bilinear+conv+bn    | 3 | 1 | 1 | 256 | 57 × 76 | up-conv-1      |
| up-conv-1        | bilinear+conv+bn    | 3 | 1 | 1 | 128 | 114 × 152 | up-conv-2     |
| up-conv-2        | conv+bn+relu        | 5 | 1 | 1 | 64  | 114 × 152 | refine-1       |
| refine-1         | conv                | 5 | 1 | 1 |    | 114 × 152 | depth          |
D Definitions of the evaluation metrics

All pixels in the predicted and ground truth depth maps with depth values in the range [0.0, 10.0] are considered valid and used to calculate the errors. We evaluate the performance for our model and for baselines on the NYU-Depth-v2 [53] using the following metrics:

– Mean absolute relative error (REL):

$$\frac{1}{T} \sum_{i=1}^{T} \frac{\lvert \hat{d}_i - d_i \rvert}{d_i}$$  \hspace{1cm} (1)

– Root mean square error (RMSE):

$$\sqrt{\frac{1}{T} \sum_{i=1}^{T} (\hat{d}_i - d_i)^2}$$  \hspace{1cm} (2)

– Thresholded accuracy (δi):

$$\max(\frac{\hat{d}_i}{d_i}, \frac{d_i}{\hat{d}_i}) = \delta_i < 1.25^i \quad (i = 1, 2, 3)$$  \hspace{1cm} (3)

where $T$ is the number of valid pixel, $\hat{d}_i$ indicates the predicted depth value at pixel $i$, and $d_i$ is the ground truth depth at pixel $i$. Lower REL and RMSE values indicate better results, while the higher $\delta_1$, $\delta_2$ and $\delta_3$, the better. In addition to the mean absolute relative error (REL), we assess model performance on ScanNet [43] and SUN-RGBD [54, 49, 55] using:

– Mean relative square error (sqREL):

$$\frac{1}{T} \sum_{i=1}^{T} (\hat{d}_i - d_i)^2$$  \hspace{1cm} (4)

– Mean absolute error of the inverse depth (iMAE):

$$\frac{1}{T} \sum_{i=1}^{T} \lvert \hat{p}_i - p_i \rvert$$  \hspace{1cm} (5)

– Root mean square error of the inverse depth (iRMSE):

$$\sqrt{\frac{1}{T} \sum_{i=1}^{T} (\hat{p}_i - p_i)^2}$$  \hspace{1cm} (6)

– Scale-invariant mean square error (SI) [46]:

$$\frac{1}{2T} \sum_{i=1}^{T} \left[ \log \hat{d}_i - \log d_i + \frac{1}{T} \sum_{j=1}^{T} (\log d_j - \log \hat{d}_j) \right]^2$$  \hspace{1cm} (7)

where $\hat{p}_i$ and $p_i$ are the inverse value of the predicted and ground truth depth at pixel $i$, respectively.
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