Task Offloading with Multi-Tier Computing Resources in Next Generation Wireless Networks

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Abstract—With the development of next-generation wireless networks, the Internet of Things (IoT) is evolving towards the intelligent IoT (iIoT), where intelligent applications usually have stringent delay and jitter requirements. In order to provide low-latency services to heterogeneous users in the emerging iIoT, multi-tier computing was proposed by effectively combining edge computing and fog computing. More specifically, multi-tier computing systems compensate for cloud computing through task offloading and dispersing computing tasks to multi-tier nodes along the continuum from the cloud to things. In this paper, we investigate key techniques and directions for wireless communications and resource allocation approaches to enable task offloading in multi-tier computing systems. A multi-tier computing model, with its main functionality and optimization methods, is presented in details. We hope that this paper will serve as a valuable reference and guide to the theoretical, algorithmic, and systematic opportunities of multi-tier computing towards next-generation wireless networks.

Index Terms—intelligent IoT, task offloading, multi-tier computing, resource allocation.

I. INTRODUCTION

As the fifth generation wireless networks (5G) being commercially deployed, research efforts of the sixth generation wireless networks (6G) have begun to define 6G requirements and use cases. Four promising use cases have emerged. First, holographic telepresence allows realistic, full motion, three-dimensional (3D) images of people and objects to be projected as holograms into a meeting room to interact with each other in real time [1], [2]. Such remote holographic meeting, surgery, or distant learning will reduce the need for travel. The second key use case is digital twin, which creates a real-time, comprehensive, and detailed digital (virtual) copy of a physical object, or system [3]. Digital twins help push the boundaries of system reliability, used to support a wide range of capabilities such as diagnostics and fault prediction. The third one is connected industrial robots, tactile Internet and intelligent cars. In this use case, the components of a control system (e.g., controllers, sensors, and actuators) are distributed across a wide geographic region [3], and therefore need to be connected via a wide area mobile infrastructure. In addition, these intelligent applications usually require stringent delay and jitter performance, with typical maximum tolerable network latency below 1 milliseconds. The fourth use case is automated network operation empowered by distributed artificial intelligence (AI), intelligent IoT (iIoT), and big data technologies [4], [5].

Many current and future applications require low latency, high reliability, and high data security protection [6]. These cannot be adequately met by the traditional cloud computing model, which requires to upload massive data and computing tasks to the cloud through fronthaul links and hence is difficult to meet the requirements of low latency and high energy efficiency. To provide low-latency services, a new computing paradigm called multi-tier computing was proposed by effectively combining edge computing and fog computing [7], [8]. With multi-tier computing, a large number of smart devices with varying computational resources, located around the end user, can communicate and cooperate with each other to execute computational tasks. A comparison between multi-tier computing and the current 5G-based edge computing is illustrated in Fig. 1 Multi-tier computing complement cloud computing and edge computing by offloading and dispersing computational (and communication and caching) tasks and resources along the continuum from the cloud to things.

Multi-tier computing is expected to become an important part of 5G systems and beyond [9], [10], supporting computational-intensive applications that require low latency but high energy efficiency, high reliability and high security services. The effectiveness of multi-tier computing depends largely on resource scheduling among edge and cloud nodes to reduce service latency and ease network congestion [8], [11]–[13]. Because of the above characteristics, multi-tier computing plays a vital role in many industrial applications of iIoT, such as connected cars, smart grids, smart buildings, and smart cities etc. Along the development of next-generation wireless networks, all kinds of user equipments (UEs) will be online all the time, promoting the advancement of iIoT and bringing diversified applications. These novel intelligent applications typically require low latency and demand prompt computations
for real-time task processing and high data rates. However, mobile devices often have limited computation, storage, and energy resources. To overcome these limitations, the capability of offloading computational tasks from the end users to nodes in the multi-tier computing systems will be essential. Such task offloading enables distributed smart devices to share their idle computation and storage resources, which realizes the efficient utilization of multi-dimensional resources for low latency task processing. Additionally, multi-tier computing systems will provide new task offloading models with the development of B5G wireless communications system, even 6G wireless communication system, and the new generation of embedded AI. As computational capability moves from the cloud to edge and UEs, the computing capabilities will be integrated into the network. Computing and network will be deeply integrated. Cloud-to-things computing capabilities should also be coordinated, leading to a new stage of intelligent multi-tier computing systems.

A. Task Offloading in Multi-Tier Computing-based Next-Generation Wireless Networks

Next-generation wireless communication networks present various novel technologies, including massive multiple-input multiple-output (MIMO), intelligent reflecting surface (IRS), space-air-ground integrated networks (SAGIN) and edge AI, etc. A multi-tier computing model integrates these radio technologies and AI to reduce task execution latency, allows large-scale user access, and enables efficient task offloading to realize efficient collaborative computing and multi-dimensional communication, caching, computation resource coordination. An example of multi-tier computing-based next-generation networks is illustrated in Fig. 2. Basically, it consisting of two types of nodes, i.e., task node (TN) and helper node (HN). In particular, multiple TNs are able to offload their tasks to multiple HNs. It remains a fundamental challenge to effectively map multiple tasks or TNs into multiple HNs to minimize the total cost, such as task offloading latency or energy consumption, in a distributed manner, known as the multi-task multi-helper (MTMH) problem [14], [15].

Massive MIMO can provide array gains, diversity gains, and multiplexing gains without increasing spectrum and power resources. It has been shown in [16] that massive MIMO schemes improve significantly the data rates at the cell edge and also increase exponentially the spectrum efficiency, resulting in an order of magnitude increasing of system capacity. The integration of multi-tier computing and massive MIMO has been proven to enhance task offloading performance in terms of ultra reliability and low latency [17]–[20]. In particular, Bursalioglu et al. [17] proposed and analyzed an architecture, so-called fog massive MIMO, where a large number of multi-antenna base stations (BSs) is densely deployed and serves the users using zero-forcing beamforming (ZFBF). Pirzadeh et al. [18] investigated the viability of supervised learning for user location estimation based on network signals transmitted by the users. In [19], Chen investigated a specific edge computing mechanism for fronthaul-constrained distributed Massive MIMO systems, aiming to minimize energy consumption on user devices. In [20], Mungara et al. considered a new architecture termed as dense fog massive MIMO, where the users establish high-throughput and low-latency data links in a seamless and opportunistic manner, as they travel through a dense fog with large number of multiple antennas remote radio heads (RRHs). Although the above research demonstrates the advantages of massive MIMO-based...
multi-tier computing, the influence of channel estimation error on resource allocation and task offloading is not studied, which is particularly important for time-varying multi-tier computing systems. On the other hand, to compensate for cloud computing, multi-tier computing systems provide computational capabilities both at the edge and center of the network. However, one of the major issues is how to manage task offloading and execution. More specifically, how to decide which tasks to perform at the end-user, fog/edge, or in the cloud. At a more granular level, the issue boils down to which node a particular task should be assigned to.

In B5G, the radio frequency may exceed 6 Gigahertz. Since higher-frequency signal is more sensitive to the blockage by obstacles, the coverage of each base station will be significantly reduced [21], [22]. Furthermore, devices at the cell edge or behind obstacles suffer from low task offloading rates, increasing both delay and energy consumption of task offloading in multi-tier computing systems [23]. IRS, regarded as an effective auxiliary wireless network technology for potentially achieving high spectrum and energy efficiency via low-cost reflecting elements, has attracted increasing attention to circumvent these restrictions and is listed as one of the candidate key technologies in 6G by academia and industry [24]–[30]. Due to the combination of array aperture gain (achieved by combining a direct transmission signal with an IRS reflection signal) and the reflection-assisted beamforming gain (achieved by controlling the phase shift of each IRS element), IRS is able to improve the success rate of task offloading and the potential of efficient resource scheduling of multi-tier computing systems. Therefore, IRS will be a key technology for task offloading in next-generation wireless networks. In [13], [31], the authors have studied the impact of IRS on computational performance in a multi-tier computing system, which have demonstrated the benefits of the IRS to improve the task offloading, in comparison to the benchmark schemes.

Meanwhile, by integrating satellite systems, aviation systems and ground communication systems, SAGIN is widely treated as a cornerstone of future 6G network. This new architecture supports seamless and near-instantaneous hyper-connectivity [32], aiming at global data acquisition with high temporal and spatial resolution, high-precision real-time navigation and positioning, and broadband wireless communications. Being an essential component of SAGIN, UAVs are deployed flexibly at the air-network layer, capable of assisting terrestrial network in task offloading and communications/computing/caching resources management due to their flexibility and proximity [33]. However, even with efficient task offloading, it is still not trivial to meet the quality of experience (QoE) requirements of heterogeneous users in the SAGIN.

Because of increasingly complex wireless networks, a typical 5G node is expected to have 2000 or more configurable parameters. Therefore, a recent new trend is to optimize task offloading and wireless resource allocation through AI technologies [34], [35], including applying AI at multiple protocol layers (e.g., physical layer resource allocation, data link layer resource allocation, and traffic control) [36]. Thanks to the rapid development of mobile chipsets, the computational capabilities of edge devices have been substantially improved. For example, smart devices nowadays have as much computational capability as computing servers a decade ago. In addition, edge servers could provide end users with low latency AI services that are not possible to achieve directly on the devices. Since the computational resources of edge servers are not as much as those of cloud centers, it is necessary to adopt
joint design principles across edge servers and edge devices to reduce task execution latency and enhance privacy for task offloading [34]. As a result, advances in multi-tier computing systems offer an opportunity to move the frontiers of AI from the cloud center to the edge of the network, inspiring a new field of research called edge AI, including both AI model training and inference procedures.

Distributed AI and federated learning algorithms are performed on multi-tier computing servers at the access network, which is capable of realizing low-latency task processing and providing computing, storage, and networking services. Since the data is processed at the edge server in the close proximity of smart device by task offloading, there is no need to transfer a large amount of raw data to the back-end server. Thus, using edge AI on task offloading infrastructure not only saves network bandwidth on backhaul links, but also reduces greatly the task execution latency. Edge AI will be a significant step towards reducing task execution latency by intelligently enabling task offloading and local caching of popular file and content migration. In addition, intelligent task offloading for computational tasks will make it possible to further virtualize users’ handsets and improve battery lifetime. In all, edge AI provides a new paradigm of optimization algorithms design for efficient task offloading and service-driven resource allocation in multi-tier computing systems [10]. By seamlessly integrating sensing, communications, computing and intelligence, edge AI will empower multi-tier computing systems to support multiple intelligent applications, including industrial robots, intelligent robotic cars, and intelligent healthcare etc.

B. Main Contributions

In this paper, a vision of multi-tier computing with intelligent task offloading is presented. Furthermore, we summarize its interactions with various wireless techniques and resource allocations, as well as discuss future research directions and open problems, to embrace the era of multi-tier computing based next-generation wireless networks. Against the above backdrop, our contributions could be further detailed as follows:

- The vision, challenges and solutions for task offloading in multi-tier computing systems towards next-generation wireless networks.
- The task offloading in multi-tier computing systems is presented, including the massive MIMO-aided task offloading, the task offloading with IRS, the task offloading in Space-Air-Ground Integrated Networks (SAGIN), and edge AI-empowered task offloading.
- The resource allocation for task offloading is elaborated. Specifically, we introduce the main functionality and optimization methods as well as the algorithms for task offloading in multi-tier computing systems.
- We discuss the research directions and open problems of task offloading for multi-tier computing-based next-generation wireless networks.

C. Paper Organization

The rest of the paper is organized as follows. Section II introduces the enablement of multi-tier computing for next-generation wireless networks, while Section III presents the resource allocation for multi-tier computing systems. Section IV is focused on research directions and open problems for multi-tier computing. In Section V, we provide our conclusions.

II. ENABLEMENT OF TASK OFFLOADING FOR MULTI-TIER COMPUTING-BASED NEXT-GENERATION NETWORKS

In this section, we present the vision, challenges and solutions for task offloading in multi-tier computing systems, including the massive MIMO-aided task offloading, the task offloading with IRS, the task offloading in SAGIN, and edge AI-empowered task offloading.

A. Massive MIMO-Aided Task Offloading

With the advent of next-generation of wireless standards, new high-performance technologies are introduced. One of these key technologies is massive MIMO [37] that has been increasingly adopted in different networking and computing frameworks. However, the works of [8], [38]–[40] mainly considered single-antenna computation offloading systems, by taking joint resources allocation and task offloading into account, but failed to exploit the MIMO advantages in terms of task offloading efficiency. As we know that MIMO techniques have the potential of achieving high spectral efficiency (SE) [41]–[43], so as to improve the task offloading data rate. Therefore, new technologies have been introduced to improve the performance of edge users from current levels. In particular, equipping the base stations (BSs) with a large number of antennas, widely known as massive MIMO, has emerged as one of the most promising solutions [44], [45] to significantly improve systems SE and energy efficiency trade-off. More specifically, as the number of antennas increases, channels become more deterministic, known as channel hardening. Data rates and communication resource allocations are hence largely determined by large-scale fading. This implies that resource allocation does not need to be updated frequently, resulting in significant savings in signal transmission overhead.

In summary, massive MIMO schemes improve spectrum and energy efficiency and support an increased number of users, both of which are critical for multi-tier computing systems.

In addition, as the core technology of wireless communication, relay technique has been integrated into various wireless communication standards to improve network coverage and throughput [46]. In particular, massive MIMO-enabled relay networks can enhance spectral efficiency and achieve more reliable data transmission for spatially distributed user nodes through intermediate massive antenna relay nodes [47], [48]. Thus, a massive MIMO-aided fog access node (FAN) serving as a relay is capable of significantly improving the data rate of offloaded tasks and the task execution efficiency. The new computing model that combines massive MIMO with multi-tier computing will facilitate efficient task offloading of computation-intensive tasks to achieve efficient collaborative computing and multi-dimensional communication, caching, computation resource scheduling.
both for data transmission and for task offloading, so as to provide enhanced computational capability.

C. Task Offloading in SAGIN

IoT seeks to connect billions of resource-constrained devices around us through heterogeneous networks. The SAGIN is viewed as a major candidate to support such IoT requirements, helping provision seamless and massive connectivity for smart services. In the past two years, 5G wireless networks have been commercialized and deployed around the world. Although 5G is still in its development, academia and industry have now shifted their attention to beyond 5G and 6G wireless networks, in order to meet the demands of ultra-low latency and high energy efficiency for IoT. Among the discussions about 6G, from the perspective of computing, communication, and caching, it is the trend to combine SAGIN with multi-tier computing technologies in the 6G networks.

Specifically, it is widely recognized that SAGIN will be the potential core architecture of the future 6G network to support seamless and near-instantaneous hyper-connectivity. Thus, multi-tier computing with SAGIN promotes the task offloading performance. As a key part of this, in the integrated air-ground branch, unmanned aerial vehicles (UAVs) are flexibly deployed at the aerial network layer, assisting in communication, computing and caching of ground networks due to their flexibility and proximity. However, in 6G networks, SAGIN still faces challenges such as the demands of temporal-spatial dynamic communication/computing/caching services, large-scale complex connection decisions and resource scheduling, and ubiquitous intelligence demands within the network. To sum up, it remains extremely challenging to realize these visions of 6G in SAGIN.

There have been heavy research efforts on the architecture of SAGIN and multi-tier computing in the existing literature. Cheng et al. proposed a novel air-ground integrated mobile edge network, by investigating the potential benefits and applications of drone cells, and UAV-assisted edge computing and caching. Support diverse vehicular services, Zhang et al. presented a software defined networking (SDN)-based space-air-ground integrated network architecture. Focusing on provisioning computing services by UAVs, Zhou et al. proposed an air-ground integrated MEC framework to cater for the urgent computing service demand from the IoTs. Furthermore, Kato et al. conducted a comprehensive study about how to deal with the challenges related to the space-air-ground integrated networks by AI techniques, including network control, spectrum management, energy management, routing and handover management, and security guarantee. In Cheng et al. demonstrated a SAGIN edge/cloud computing architecture for offloading the computation-intensive applications, considering remote energy and computation constraints, and developed a joint resource allocation and task scheduling approach to efficiently allocate the computing resources. In Shang et al. studied MEC in air-ground integrated wireless networks to minimize the total energy consumption by jointly optimizing users association for computation offloading, uplink transmit power,
allocated bandwidth, computation capacity, and UAV 3-D placement. However, how the air network layer allocate the communication/computing/caching resources intelligently for task offloading of the ground network layer in SAGIN has not been adequately addressed.

### D. Edge Intelligence-Empowered Task Offloading

With the continuing increase in the quantity and quality of rich multimedia services, the traffic and computational tasks of mobile users and smart devices have significantly increased in recent years, bringing huge workload to the already congested backbone and access networks. Even with the help of multi-tier computing systems, it is not trivial at all to satisfy the quality of experience (QoE) requirements of users. The main difficulty lies in the need of large amount of wireless data and task transmissions for task offloading, causing wireless channel congestion. Therefore, the optimization problem or decision making of the combined wireless communication resource allocation and multi-tier task offloading is the key. That is, how to share the communication resources and computing resources between edge nodes and the cloud. In response to the increasing complexity of wireless communication networks (for example, a typical 5G node is expected to have 2000 or more configurable parameters), a recent new research trend is to optimize wireless resource allocation through AI technologies [34], [35], including but not limited to applying AI algorithms to physical layer resource allocation, data link layer resource allocation, medium access control, and traffic and congestion control [36]. Especially, reinforcement learning is often applied to jointly manage communication, computing, and caching resources. With learning based multi-tier computing systems, we can optimize task offloading, communication resource allocation, and content caching at edge nodes. Further, federated learning [57], as a distributed learning framework, always brings the following benefits for task offloading: 1) great reduction of the amount of data that must be uploaded through wireless uplink channel, 2) cognitive response to the changing wireless network environments and conditions, and 3) strong adaptability to the heterogeneous nodes in the wireless networks, 4) better protection of personal data privacy.

In learning-based multi-tier computing systems, task offloading decision and communication resource allocation vectors generally are binary variables, turning out it is challenging to find the optimal solution of resource allocations. Moreover, the feasible set and the objective function of the optimization problem are generally not convex, making the problem NP hard. In addition, in time-variant systems, channel conditions and computational cost are dynamic. Instead of solving the NP hard optimization problem by utilizing conventional optimization methods, the task offloading and communication resource allocation problem in multi-tier computing systems could be possibly solved using online learning algorithms. During the online learning process, the deep reinforcement learning methods might be applied to jointly optimize the subcarrier allocation and task offloading in each time episode. Online federated learning framework is recently utilized to learn in a distributed way, in order to solve the task offloading and communication resource allocation problem. Based on the communication, computational resource allocation, the multi-tier task offloading decisions can then be optimized.

Furthermore, edge learning methods have been investigated in some edge/fog computing systems to simplify the optimization algorithm or fulfill online implementations [11], [58]–[64]. In [59], Huang et al. designed a deep learning-based task offloading strategy to minimize weighted energy consumption and latency. In [63], Wang et al. leveraged deep reinforcement learning method for smart resource allocation in a software defined network (SDN)-enabled edge computing architecture. In [62], Huang et al. proposed a deep learning-based task offloading strategy for offloading decisions and resource allocation of a wireless powered edge computing system. In [65], Yang et al. also used deep reinforcement learning method in IRS-aided edge computing systems to enhance system security and maximize the sum rate of the down-link task offloading. In [66], a convolutional neural network was constructed for channel estimation of a large IRS-aided massive MIMO communication system to estimate the direct and the cascaded channels, used for multi-tier task offloading.

### III. Resource Allocation for Task Offloading

In this section, we characterize the multi-tier computing resources allocation in next generation wireless networks. Effective optimization methods are then presented to achieve efficient task offloading with multi-tier resources.

#### A. Main Functionality

In this subsection, the computational and communication resources allocation, service placement, and security requirement are characterized for designing multi-tier computing systems, which is illustrated in Fig. 4.

1) **Computation**: Multi-tier computing architectures were envisioned to achieve rapid and affordable scalability by developing computation capabilities flexibly along the entire cloud-to-things continuum [67]. In essence, multi-tier computing systems distribute computing capability anywhere between the cloud and the things to take full advantage of the computational resource available along this continuum, thus extending...
the traditional cloud computing architecture to the edge of the network. Thanks to multi-tier computing, some application components can be performed at the network’s edge, like delay-sensitive components. While other components, such as time-tolerant and computation-intensive ones, are performed in the cloud. Satisfying diverse user requirements will require both cloud computing with enormous resources and distributed fog/edge computing with resources and simple algorithms closer to the users to support time-sensitive tasks. With heterogeneous computing resources and the collaborative service architecture, the proposed multi-tier computing systems are able to effectively support a full range of services in different environments. On this basis, multi-tier computing provides the advantage of low-latency task offloading since it allows task to be processed at the network edge, close to the end devices. However, cloud computing alone is not adequate for supporting all IoT applications, while a multi-tier computing system can be complementary.

For smart devices with abundant computing resources, multi-tier computing seeks to achieve seamless integration of edge and cloud systems. This vision goes beyond treating the network edge and smart devices as separate computing platforms. Seamlessly integrating fleets and swarms of mobile IoT entities into a dense multi-tier enclave is a new distributed computing paradigm that improves the scalability, extensibility and assemblability of cloud services through edge of computing systems. Smart devices (cars, drones and robots) have spare computational resource, allowing the multi-tier computing platform to reduce energy consumption and task processing latency compared to the traditional edge computing scenarios relying on static and low-power edge servers.

2) Communication: Multi-tier computing systems distribute communication functions anywhere between the cloud and things to take full advantage of the communication resource available along this continuum. In massive MIMO-aided multi-tier computing systems, the achievable data rates are mostly determined by large-scale fading, and so is the communication resource allocation. This means that there is no need to frequently update communication resource allocations, hence reducing signaling overhead. IRS is capable of improving the success rate of the task offloading. Given the potential gains, if the line-of-sight (LoS) link between the task offloading nodes and computing nodes is blocked by obstacles, the task could be offloaded via the IRS reflected link. In this manner, we attempt to optimize the link selection and wireless communication resource allocation.

It is important to maintain the required data rates for task offloading. Take the task offloading from a car as an example. Given that a connected car produces tens of megabytes of data per second, an autonomous vehicle may generate up to a gigabyte per second [7]. Here, dense moving edge nodes can support accelerated data communication by largely utilizing directional high-rate communication in the massive MIMO, IRS or the SAGIN. Edge nodes at the same time provide novel strategies for smart devices to combine the benefits of centralized and ad-hoc topology into a unified solution by using multi-hop, multi-connection mechanisms to communicate with adjacent network infrastructure when facing the intermittent connectivity.

3) Storage: Because the edge nodes often have limited storage resources, distributing the data among edge and cloud nodes is vital for optimizing task offloading latency or energy consumption at a given QoS requirement. On top of it, multi-tier computing also brings a large amount of cloud-like services closer to the end users. Caching computational data or services at edge nodes is hence crucial, which relieves the burden of backhaul transmission with transporting all the data to the clouds.

Accordingly, elastic storage capacity of edge nodes might be used to support applications running on resource constrained IoT devices. Due to the inherent flexibility of multi-tier computing systems, it is possible to integrate a large number of densely distributed devices. Caching capacity of edge servers is usually accessed by both smart devices and edge access points. For example, user nodes are possibly consolidated into special capacity areas. Then, multiple interconnected edge infrastructures that coexist in space and time can pool the storage resources of adjacent edge networks together for sharing by smart devices and end users.

4) Security: In cloud computing systems, massive data needs to be uploaded to the cloud data center through a front-haul link, where data security cannot be guaranteed. However, multi-tier computing systems presents unique security challenges and opportunities. Dense edge nodes with established dynamic trust chains are acting as a trusted authority for other smart devices and systems. In particular, multi-tier computing systems with edge and cloud can handle responsibilities such as trusted computing platforms, and secure storage of short-term sensitive information. Multi-tier computing systems also use edge systems to facilitate local threat monitoring, detection, and protection for users and provide powerful proximity-based authentication services for better authentication through proxy smart devices.

However, the multi-tier computing systems meanwhile incur new security vulnerabilities, mainly from multiple heterogeneous nodes. For example, in a multi-node environment, when multiple potentially competing service providers and consumers share resources distributed across a set of hardware platforms, advanced authorization and authentication mechanisms need to be created to effectively leverage this heterogeneous medium and devices between edge and cloud entities. Fortunately, a trusted execution environment supported by a public key infrastructure may be a suitable solution to the above problems. Nevertheless, the intelligent integration of hardware assistance and software security mechanisms in multi-tier computing systems remains an open research challenge.

Additionally, multi-tier computing systems will have to cope with changing environments compared to existing edge computing systems that operate mainly under known conditions. In this case, the security mechanism for multi-tier computing systems is supposed to constantly adapt to the changing operating conditions. To address this challenge, multi-tier computing systems must dynamically adjust their overall security posture. It requires the design of new security protocols, which is able to respond to any security threat without causing service
disruptions and to achieve secured and uninterrupted operation of the task offloading.

B. Optimization Algorithms

In this subsection, the effective optimization methods are presented to achieve efficient task offloading with multi-tier resources.

1) Nonconvex Optimization: During task offloading process, most of the resource allocation problems in multi-tier computing systems need to solve a series of nonconvex optimization problems. For example, for IRS-aided multi-tier computing systems, there are four blocks of optimization variables, namely, the task offloading ratio, power allocation at the relay node, and IRS phase shifts of two hops task transmission. The optimization of the task offloading ratio is related to the computing setting, while the optimization of power allocation and phase-shift matrices affects the communication design. However, the resource allocation problem in IRS-enabled multi-tier computing systems is difficult to solve due to two aspects. The first one is the coupling effect between the power allocation vector and the IRS phase-shift vector. The second one is the objective function (OF) is non-convex with respect to the phase shifts. Obviously, it is an open challenge to obtain a globally optimal solution directly. In fact, alternating optimization technique is a widely applicable and efficient approach for solving optimization problems involving coupled optimization variables, which has been successfully applied to several communication resource allocation problems such as hybrid precoding [68], power allocation [69], and IRS phase shift optimization [24], [70]. In this case, a locally optimal solution is usually provided. To be specific, the resource allocation optimization problem can be transformed into a phase shift optimization problem, a power allocation problem, and a task allocation problem, respectively, by using the popular alternate optimization technique to decouple communication and computational design.

Remarkably, in contrast to the alternate optimization technique, distributed optimization algorithms for non-convex optimization have appeared in the literature [71]. In [72], [73], Tatarenko et al. and Zeng et al. studied distributed gradient descent methods for unconstrained non-convex optimization problems, respectively. Distributed optimization algorithms are generally divided into two categories: discrete time algorithms and continuous time algorithms. The existing work mainly focuses on discrete time algorithms, while continuous time problem has attracted extensive attention in recent years, mainly because of the wide application of continuous time setting in practical systems and the development of continuous time control technology. In addition, discrete time and continuous time algorithms are closely related to each other due to the time scale transformation. Specifically, when the time step size approaches zero, the optimization algorithm for discrete time system is similar to the continuous time system. Note that coupled non-linear constraints are also an important constraint in distributed optimization problems. However, distributed algorithms dealing with coupled non-linear constraints are basically convex problems, namely, both the objective function and the constraint are convex. In [74], Wang et al. studied distributed augmented Lagrangian based algorithms for non-convex optimization problems of multi-tier computing systems subject to local constraints and coupled non-linear equality constraints, and investigated the joint design of the task offloading, service caching and power allocation to minimize the total task scheduling delay.

2) Mixed-Combinatorial Optimization: Combinatorial optimization problems have been analyzed in many works (e.g., [75]–[78]). Under the framework of combinatorial optimization, an important trend is analyzing combinatorial optimization problem within the framework of Euclidean combinatorial optimization, whose optimization is carried out in a Euclidean space. In [77], [78], Barbolina et al. and Yemets et al. studied the Euclidean combinatorial optimization problems, and investigated the properties of its convex hull and methods of solving separate classes of Euclidean problems of combinatorial optimization problems. Additionally, the general permutation set problem is an important Euclidean combinatorial optimization problem.

As previously mentioned, the resource allocation problems in multi-tier computing systems involve optimizing computation, communication and caching. In general, task offloading, task data caching and communication resource allocations are binary variables. Specifically, in multi-tier computing for next-generation wireless networks, we need to jointly optimize the subcarrier and bandwidth allocation [79]–[81], transmit power and receive beamforming [12], [60], passive beamforming at IRS [13], device selection [8], [13], location updates task offloading [11], and computational frequency control [8], so as to reduce the latency and energy consumption in the task offloading procedure. Therefore, these resource allocation schemes can be formulated as a mixed combinatorial optimization problem that requires joint optimization of continuous value variables (e.g., beamforming, power control) and discrete value variables (e.g., task allocation, service placement, subcarrier allocation).

It should be noted that the existing optimization methods for mixed combinatorial optimization problems are mainly based on traditional iterative optimization approaches [13], [82]–[85], or adopt a direct end-to-end online learning approaches [11], [86]. However, they may not achieve good trade-off between algorithm complexity and resource allocation performance. Additionally, reinforcement learning (RL)-based approaches are often involved to solve combinatorial optimization problems that are unconstrained or have few constraints due to feasibility issues [60], [87]. Deep RL requires a Markov process to achieve satisfactory resource allocation performance [88]. However, Markov process may not exist in practical combinatorial optimization problems, as they have many non-convex constraints with memory. This results in difficult design of reward features for Markov optimization process, unfeasible solutions, and potential degradation of overall performance.

3) Stochastic Optimization: In multi-tier computing systems, stochastic optimization approach only relies on the probabilistic description of the uncertainty of the computation capacity and radio channel condition, and is able to provide
a trade-off between conservatism and probabilistic assurance for the achievable task offloading performance. Stochastic programming has been widely studied in the past decade due to its wide application in machine learning and resource allocation. In a stochastic optimization problem, the objective function or constraints are the expectation of some function of random variables (such as estimated computation capacity and channel condition in learning approach) \[89\]. The challenge of stochastic optimization is that the distribution of the random variables is often unknown. Most existing literature on stochastic programming assumes that the basic distribution of random variables is fixed and that independent samples are sequentially drawn from this common distribution. However, the basic distribution of random variables involved in stochastic optimization may change slowly over time in many practical applications.

Stochastic optimization in state-based systems with discrete or continuous time are often modeled with Markov chains. Their effective optimization method is an important research topic. The Markov model has a wide range of applications, especially in the area of task offloading in multi-tier computing systems. Specifically, some work modeled the task offloading problem as a stochastic programming problem, and jointly optimized the task allocation and the communication resources allocation \[90\]. However, in all these works, system parameters need to be acquired offline, which is impossible for a time-varying system \[91\]. It should be noted that there are multiple dynamic parameters in multi-tier computing systems. Therein, user mobility and channel condition are intrinsic features of wireless networks when nodes are usually in a mobility state. Then, due to changes in network topology, these parameters are time-varying, and the stochastic task offloading framework is considered as a method of online learning where users can learn time-varying system parameters.

In many multi-tier computing applications, optimization criteria are trade-offs between several competing goals, such as computational cost minimization and profit maximization. In general, in this tradeoff model, it is important to establish an optimal strategy that may often not be intuitive. However, there are also optimization problems with no tradeoff characteristics, leading to counterintuitive optimal strategies. Therefore, the use of Markov decision process (MDP) to optimize stochastic systems should not be ignored. It should be noted that there exists extensive literature in online learning task offloading for stochastic optimization, such as deep RL (DRL) \[92\]–\[95\], which generally target at a broader set of learning problems in MDPs. However, as far as we know, high-dimensional action spaces are still an urgent and challenging problem in DRL. To make the problem tractable, the general optimization problem is reduced into an MDP that only considers a meaningful parameter. Furthermore, the Multi-Armed Bandit (MAB) problem is a special case of MDP problems for which regret learning frameworks are generally considered to be more efficient in terms of computational complexity. Additionally, the use of the MAB model is appropriate and recognizable, taking advantage of the fact that the resources of edge node are limited. Based on the above analysis, MDP promises an online learning framework for learning computing resources and available resources information for stochastic optimization, aiming to minimize task offloading cost.

**IV. RESEARCH DIRECTIONS AND OPEN PROBLEMS**

In this section, we present the research directions and open problems for task offloading in next generation wireless networks, supported by the wireless network infrastructures in Section II.

**A. Multi-Dimensional Resource Management**

Compared to cloud computing, the edge nodes and end users in multi-tier computing systems may have limited resources. Therefore, communication, computing and caching resource allocation is a very important research issue in multi-tier computing systems. Specifically, next-generation wireless communication networks present various technologies, including massive MIMO, IRS, SAGIN, and AI etc. The new computing model by combining them with multi-tier computing will reduce task offloading delay, grant large-scale user access and promote rapid development of the intelligent services, as well as enable efficient task offloading to realize efficient collaborative computing and multi-dimensional communication, caching, computation resource sharing.

However, the computation power of multi-tier servers is typically limited. The wireless physical layer resource allocation and user access techniques are the key challenges that hinder the success of multi-tier computing for 5G and beyond in executing compute-intensive and latency-critical applications. The optimization of resource allocation may be multi-objective in different situations, e.g., diverse nature of applications, heterogeneous server capabilities, user demands and characteristics, and channel connection qualities.

**B. Multi-Tier Task Allocation**

Since multi-tier computing systems provide extra computing capability at the network edge, one of the core problems is how to manage task allocation. More specifically, how to decide which tasks should be performed on end-user devices, at fog/edge systems, or in the cloud. At a more granular level, the challenge is to which computing nodes should a task be assigned. To achieve low latency and high energy efficiency task offloading, computing tasks need to be scheduled to computing nodes with different capabilities according to different task computing models, communication bandwidths and channel qualities. Therefore, heterogeneity becomes an important factor in multi-tier computing architectural design. Dealing with different task computation and various communication protocols to manage task offloading becomes a major problem.

**C. Heterogeneous QoS Management**

With the development of various novel technologies, intelligent services are increasingly applied in many fields of human life, including business, manufacturing, health-care, entertainment, etc. On one hand, the number of smart services deployed around edge and cloud servers is growing rapidly. On the other hand, different service providers provision services...
with similar functions, and different edge servers may possess different service performance. Then, the smart devices will require services with different QoS requirements. In light of these descriptions, intelligent services are migrating to the network, i.e., to edge servers residing near end users.

Note that the QoS requirements in multi-tier computing systems include task response time, throughput, reliability and availability, typically different for different users. However, user mobility and different server capabilities turn the applicability of traditional QoS management inapplicable. Therefore, how to monitor and manage QoS attributes, and schedule multi-dimensional resources timely and effectively to fulfill specific QoS requirement for each user becomes the main issue in multi-tier computing systems.

D. Data Privacy

In multi-tier computing systems, data and computation task need to be collected close to the physically distributed edge devices, and there exists a large number of devices in the systems. When analyzing sensitive information from distributed nodes, data privacy requirements must be satisfied. We should select computing nodes in a way that best protect the data privacy, considering the computing nodes in different parts of the network may have different privacy protection capabilities. The tasks collected, transmitted, and processed at the edge or in the cloud needs to be anonymized [96]. Then, multi-tier data analysis and processing is achieved securely in multi-tier computing systems. Note that distributed systems are in general more vulnerable to be attacked than centralized systems, and both the devices and edge nodes in multi-tier computing systems are generally less powerful than the cloud. Therefore, these nodes may not have as adequate resources as the cloud to protect themselves. In addition, the devices and edge systems may not have enough intelligence and capability needed to detect threats due to limited resources. In all, data privacy of multi-tier computing from things to the cloud will be the focus of future research in multi-tier computing systems.

V. CONCLUSIONS

In this paper, we investigated the key wireless communication techniques, effective resource allocation approaches and research directions to embrace the era of task offloading for multi-tier computing-based next-generation wireless networks. In particular, the multi-tier computing system model, multi-tier computing resources and optimization methods were presented for better serving the task offloading. We hope that this paper will serve as a valuable reference and guide to further promote the theoretical, algorithmic, and systematic development and advancement of the task offloading with multi-tier computing resources in next generation wireless networks.

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