Molecular spectroscopy for ground-state transfer of ultracold RbCs molecules

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We perform one- and two-photon high resolution spectroscopy on ultracold samples of RbCs Feshbach molecules with the aim to identify a suitable route for efficient ground-state transfer in the quantum-gas regime to produce quantum gases of dipolar RbCs ground-state molecules. One-photon loss spectroscopy allows us to probe deeply bound rovibrational levels of the mixed excited \((A^1\Sigma^+-b^3\Pi_0)\) 0\(^+\) molecular states. Two-photon dark state spectroscopy connects the initial Feshbach state to the rovibrionic ground state. We determine the binding energy of the lowest rovibrational level \(|\nu'=0,j''=0\rangle\) of the \(X^1\Sigma^+\) ground state to be \(D_0^*_0 = 3811.5755(16)\) cm\(^{-1}\), a 300-fold improvement in accuracy with respect to previous data. We are now in the position to perform stimulated two-photon Raman transfer to the rovibrionic ground state.

\section*{Introduction}

Ultracold and dense molecular samples promise myriad possibilities for new directions of research in fields such as ultracold chemistry, quantum information science, precision metrology, Bose-Einstein condensation, and quantum many-body physics. Recent overviews on the status of the field and on possible experiments can be found in Refs.\textsuperscript{1–3} Within our work on ultracold molecules we are primarily interested in dipolar many-body physics. Heteronuclear molecules such as KRb and RbCs in their rovibrionic ground state feature sizeable permanent electric dipole moments of about 1 Debye,\textsuperscript{4,5} giving rise to long range and anisotropic dipole-dipole interactions in the presence of external polarizing electric fields. As a consequence, at ultralow temperatures, few-body and many-body dynamics are expected to be governed by dipolar effects. In particular, a broad variety of novel quantum phases has been proposed for bosonic and fermionic dipolar gases that are confined to two- or three-dimensional lattice potentials.\textsuperscript{6–8}

Our goal is to produce a quantum gas of ground-state RbCs molecules. The molecule RbCs, in its lowest internal state, is stable under binary collisions,\textsuperscript{9} i.e. the exchange reaction \(2\text{RbCs} \rightarrow \text{Rb}_2 + \text{Cs}_2\) is not possible (this is e.g. not the case for the molecule KRb). Collisional stability is an important requirement for the formation of a molecular quantum gas in full thermal equilibrium. As molecular samples are not readily laser cooled, we intend to use a scheme in which the molecules are produced at high phase-space density out of an atomic Rb-Cs quantum-gas mixture\textsuperscript{10} by Feshbach association and coherent state-transfer techniques, similar to recent work on Cs\(_2\)\textsuperscript{20,21}, Rb\(_2\)\textsuperscript{22} and KRb.\textsuperscript{23} Experiments on KRb have reached a regime in which dipolar effects on reaction dynamics and thermalization processes have become very pronounced.\textsuperscript{24–26} For our experiments on RbCs an optical lattice will aid in the association and state-transfer process by preventing the molecules from undergoing collisional loss before they have reached the rovibrational ground state. Initially, RbCs Feshbach molecule\textsuperscript{27,28} will be formed out of two-atom Mott-insulator state in a generalized version of previous work on the efficient formation of homonuclear Rb\(_2\) and Cs\(_2\) molecules.\textsuperscript{29} The molecules will then be transferred to the lowest rovibrionic level of the \(X^1\Sigma^+\) absolute ground state on a two-photon transition using the STImulated Raman Adiabatic Passage (STIRAP) technique.\textsuperscript{30}

Here, we perform high-precision molecular spectroscopy on a dense sample of ultracold RbCs molecules to identify a suitable two-photon path to the rovibrionic \(X^1\Sigma^+\) ground state as depicted in Fig.\textsuperscript{1}(a). Starting from a Feshbach level \(|1\rangle\), we perform molecular loss spectroscopy to search for and identify a suitable level \(|2\rangle\) of the mixed \((A^1\Sigma^+-b^3\Pi_0)\) 0\(^+\) excited molecular potentials, hereafter named 0\(^+\) potentials. We probe levels that lie 6320 to 6420 cm\(^{-1}\) (1580 nm to 1557 nm) above the Rb(5\(^2\)S)+Cs(6\(^2\)S) limit and hence 10160 to 10260 cm\(^{-1}\) (980 nm to 970 nm) above the rovibrionic ground-state level \(|3\rangle\). The wavelength ranges above were chosen because they feature sufficiently strong transitions and because they can be covered by readily available diode laser sources. We then perform dark-state spectroscopy by simultaneous laser irradiation near 1570 nm and 980 nm, connecting the initial Feshbach level \(|1\rangle\) to the rovibrionic ground state \(|3\rangle\). We find several dark resonances, from which we derive normalized transition strengths and find that some of the two-photon transitions are candidates for ground-state transfer. The paper is organized as follows: In Section\textsuperscript{2} we describe the molecular structure relevant to identify a suitable route for the production of ultracold samples of RbCs molecules in their rovibrionic ground state. Section\textsuperscript{2} summarizes the sample preparation procedure. Section\textsuperscript{3} then presents the results of our one-photon loss spectroscopy measurements, while Section\textsuperscript{4} discusses the results of the two-photon dark state spectroscopy. We finally give an outlook on future work.
1 The route towards RbCs ground-state molecules

Our strategy to populate the rovibronic ground state is based on a STIRAP transfer scheme. This method is coherent, highly efficient, robust, fast, reversible, and allows control over all the intermolecular degrees of freedom including vibration, mechanical rotation, and nuclear spin. STIRAP typically involves three molecular levels that are coupled by a two-photon transition in a lambda-type configuration. To achieve highly efficient STIRAP transfer it is mandatory to determine a suitable three-level system. The initial state \( |1\rangle \) at threshold is a weakly bound Feshbach state. This state happens to be of almost pure triplet \( a^3\Sigma^+ \) character. We populate this state out of an ultracold Rb-Cs mixture via the Feshbach association technique as discussed below. The intermediate level \( |2\rangle \) is a level belonging to the electronically excited \( 0^+ \) potentials mixed by spin-orbit interaction. The final state \( |3\rangle \) is the lowest rovibronic level of the \( X^1\Sigma^+ \) ground state potential. Laser \( L_1 \) connects the initial Feshbach level \( |1\rangle \) to the intermediate level \( |2\rangle \), and laser \( L_2 \) couples the latter to \( |3\rangle \).

Our goal is to identify a suitable intermediate level \( |2\rangle \) from the \( 0^+ \) potentials with sufficient oscillator strength with both levels \( |1\rangle \) and \( |3\rangle \). The STIRAP process takes advantage of the mixed singlet-triplet character of the \( 0^+ \) pair of states correlated to the Rb-Cs dissociation limit \( 5^2S_{1/2} + 6^2P_{3/2,1/2} \) (see also Table 2 below). Here \( \Omega' = 0 \) labels the projection of the total electronic angular momentum on the molecular axis, and the plus sign the parity of the state for the symmetry with respect to a plane containing the molecular axis. These two states result from the spin-orbit interaction between the lowest state of \( ^3\Pi \) symmetry and the second state of \( ^1\Sigma^+ \) symmetry in RbCs correlated to the Rb(5\( ^2S \)) + Cs(6\( ^2P \)) limit, hereafter referred to as the \( b^3\Pi \) and \( A^1\Sigma^+ \) states. Previous spectroscopic analysis of these states has resulted in two potential curves for the \( b^3\Pi \) and \( A^1\Sigma^+ \) states and molecular spin-orbit coupling functions varying with the internuclear distance \( R \). A potential curve for \( \Omega = 1 \) component of the fine structure manifold of the \( b^3\Pi \) state is also provided by Ref. We chose the \( X^1\Sigma^+ \) ground state potential curve determined in Ref. by the Inverted Perturbation Approach (IPA) of spectroscopic data. In principle, level \( |1\rangle \) is determined by the details of the hyperfine structure of the ground-state manifold. With its nearly pure triplet character it can be described as if it belonged to a single \( a^3\Sigma^+ \) potential curve for the purpose of our model. No experimental determination of this potential is available yet, although we are aware of ongoing work in the group of D. DeMille at Yale University. We use the \emph{ab initio} potential calculated in Ref. matched at 22 a.u. to the asymptotic potential derived from the spectroscopic analysis of the \( X^1\Sigma^+ \) ground state. We modify the \( C_6 \) van der Waals coefficient to the value \( C_6 = 5663 \) a.u. In addition we slightly moved the repulsive wall to reproduce the scattering length of 542 a.u. reported in Ref. This corresponds to a shift of the inner turning point at zero energy of about 0.2 a.u.

Using the Mapped Fourier Grid Hamiltonian (MFGH) method we compute the vibrational wave functions \( \psi_{\mathrm{X}(R)}, \psi_{\mathrm{a}(R)}, \) and \( \psi_{0^+}(R) \) of the \( X^1\Sigma^+, a^3\Sigma^+, \) and \( 0^+ \) molecular states, respectively, ignoring rotation in a first step. The upward STIRAP step relies on the \( a^3\Sigma^+ \rightarrow b^3\Pi \) electronic transition, and the downward step relies on the \( A^1\Sigma^+ \rightarrow X^1\Sigma^+ \) transition. The relevant \( R \)-dependent transition dipole moment functions are calculated following Ref. We plot them in Fig. (b). The resulting transition dipole moments (TDMs) \( \mu_{i\mu}^{a-0^+} = \langle \psi_{i\mu} | \mu_{a-0^+}(R) | \psi_{1\mu}^{0^+} \rangle \) and \( \mu_{i\mu}^{X-0^+} = \langle \psi_{i\mu}^{X} | \mu_{X-0^+}(R) | \psi_{1\mu}^{0^+} \rangle \) are displayed in Fig. 2 as functions of the \( 0^+ \) level energies. Here, \( v' \) and \( v'' \) are the vibrational quantum numbers of the initial, intermediate, and final levels, respectively. Note that \( v' \) labels the levels of the \( 0^+ \) coupled states corresponding to their numbering with increasing energy, which is not regular in contrast to the case of a single regular potential well. First, we find that the \( \mu_{i\mu}^{a-0^+} \) TDMs exhibit identical variations for \( v \) levels close to the dissociation limit apart from a \( v \)-dependent global scaling factor related to the amplitude of the wave function at the inner turning point of the \( a^3\Sigma^+ \) potential. This simply expresses the fact that the TDMs are mainly influenced by the inner part of the initial wave function where absorption occurs rather than by its multichannel character at large distances, and thus justifies the present model. Second, \( \mu_{i\mu}^{X-0^+} \) is much larger than \( \mu_{i\mu}^{a-0^+} \) above 6400 cm\(^{-1} \), reflecting the almost vanishing transition dipole moment around the \( a^3\Sigma^+ \) inner turning point. Below this energy the spatial overlaps of \( v' \) and \( v'' \) are much larger than \( 0 \) wave functions rapidly decrease as the bottoms of the \( X \) and \( A \) wells are shifted from each other.

In order to understand the STIRAP selection rules, levels \( |1\rangle \), \( |2\rangle \), and \( |3\rangle \) must be expressed in terms of a common quantum number \( J \), where \( J = \bar{L} + \bar{S} + \bar{\ell} \) is the total angular momentum of the molecule ignoring nuclear spin. Here, \( \bar{L} + \bar{S} \) is the total electronic angular momentum and \( \bar{\ell} \) is the pure rotation of the molecule. In the case of levels \( |2\rangle \) and \( |3\rangle \) the number \( J \) determines the rotational energy level structure of the molecule, while it is not well defined for the Feshbach level \( |1\rangle \). For details, see Section 3. Assuming that the radial wave function of a rovibrational level \( (v,J) \) is independent of \( J \) for the low \( J \) values involved, the transition dipole moments including rotation \( \mu_{i\mu,J}^{a-0^+} \) between the initial \( (v_i,J_i,M_i) \) and the final level \( (v_f,J_f,M_f) \) of the electronic states \( \Gamma_i \) and \( \Gamma_f \), respectively, are related to the purely vibrational dipole moments \( \mu_{v_i,v_f}^{\Gamma_i-\Gamma_f} \) using the usual H"{o}nl-London factors

\[
\mathcal{D}_{i,J_f,J_i,\Gamma_f,\Gamma_i}^{\pm,\pm} \equiv \sqrt{(2J_i+1)(2J_f+1)(1+q)} \times \left( \frac{J_f}{-M_f} \right)^{\pm,\pm} \times \left( \frac{J_f}{-q} \right)^{\pm,\pm} \times \mu_{v_i,v_f}^{\Gamma_i-\Gamma_f},
\]

where \( M_i \) (\( M_f \)) is the projection of \( J_i \) (\( J_f \)) onto the lab-frame quantization axis and \( \Lambda_i \) (\( \Lambda_f \)) is the projection onto the molecular axis. The index \( q \) labels \( \Sigma^+ \) (\( q = 0 \)) and \( \Sigma^- \) (\( q = \pm 1 \)) transitions, and \( \pm = 0 \) (= \( \pm 1 \)) defines the
laser polarization along (perpendicular to) the quantization axis. For the purpose of the next sections we present in Table [ ] the factors related to the possible values of the projection of the angular momentum of level $|1\rangle$, i.e. $M_J = 0, \pm 1, \pm 2$ for the two accessible rotational states $J' = 1, 3$ of the $|2\rangle$ levels.

### 2 Experimental setup and initial state preparation

The starting level $|1\rangle$ for optical spectroscopy and future STIRAP experiments is a Feshbach molecular level that we created directly from an $^{87}\text{Rb}$,$^{133}\text{Cs}$ atomic mixture by using the standard magneto-association technique using a Feshbach resonance.$^{28-30}$ We produce a pure sample of RbCs Feshbach molecules trapped in an optical dipole trap as follows. We first prepare an atomic mixture following an all-optical scheme similar to the one described in Ref.$^{19,27}$ In brief, Rb and Cs atoms are captured in a two-species magneto-optical trap (MOT) from a two-species Zeeman slower. After a stage of two-color degenerate Raman-sideband cooling.$^{22}$ a technique that simultaneously cools and polarizes the mixture in the absolute lowest hyperfine Zeeman level, the atoms are loaded into a magnetically levitated large-volume dipole trap. After 1 s of plain evaporation the dipole trap typically contains $1.7 \times 10^6$ Rb and Cs atoms at about 5 μK in the $|f_{\text{Rb}}=1, m_{f_{\text{Rb}}}=1\rangle$ and $|f_{\text{Cs}}=3, m_{f_{\text{Cs}}}=3\rangle$ Zeeman sublevels, respectively. As usual $f_{\text{Rb}}$ ($f_{\text{Cs}}$) is the total atomic angular momentum quantum number and $m_{f_{\text{Rb}}}$ ($m_{f_{\text{Cs}}}$) its projection onto the magnetic field axis. While a large volume trap is well suited for optimal loading of atoms from the MOT, a tightly focused dipole trap is desirable to increase the number density and to assure the high thermalization rate required for evaporative cooling towards Bose-Einstein condensation. However, Rb and Cs have a comparatively large interspecies background scattering length as a result of the presence of a near threshold $s$-wave state belonging to the open scattering channel.$^{28}$ The large scattering length is responsible for the large three-body Rb-Cs inelastic collisional rate observed in our recent experiments.$^{18}$ We follow the strategy of spatially separating the two species by loading Rb and Cs atoms into two different tightly focused dipole traps.$^{19,20}$ We then perform evaporative cooling on each species separately. At the onset of condensation, we stop the forced evaporation and we superimpose the Cs atomic cloud onto the Rb one by spatially shifting the Cs dipole trap. We end up with an atomic mixture of $1.5 \times 10^5$ Rb and $0.8 \times 10^5$ Cs atoms at a temperature of about 200 nK.

The near-degenerate atomic mixture is the starting point for Feshbach association.$^{28}$ In previous experiments we have found a large number of Feshbach resonances in the magnetic field range up to about 670 G.$^{27,28}$ In principle, each observed resonance can be used to convert atoms into molecules. For our one-photon spectroscopic measurements we have to match both the requirement of high conversion efficiency and large wave-function overlap between the starting molecular
Feshbach level and the final molecular state in the electronically excited mixed 0\(^+\) potentials. We identify two different Feshbach levels to be the most appropriate candidates for the initial state |1\> and the rotational states J’ = 1 and J’ = 3 of level |2\>. The labels “v” and “h” refer to the polarization \(\varepsilon = 0\) and ±1, respectively.

The Feshbach molecular states near threshold are typically described using the atomic basis. The full set of good quantum numbers is given by \(|\tilde{v}; f_{Rb}, m_{f_{Rb}}; f_{Cs}, m_{f_{Cs}}; \ell, m_{\ell}; M_F\rangle\), where \(m_{f_{Rb}} = m_{f_{Cs}}\) is the quantum number for the mechanical rotation of the molecule, and \(m_{\ell}\) is its projection on the laboratory axis. We use the symbol \(\tilde{v}\) to label the vibrational level, numbered downwards from the Rb(5\(^2\)S\(_{1/2}\)) + Cs(6\(^2\)S\(_{1/2}\); f\(_{Cs}\) = 3) atomic threshold at a magnetic field strength B of about 217 G and 182 G, referred to in the following as |1a\> and |1b\>, respectively. We populate these levels by the usual magnetic field ramping technique.\(^{28,40}\) To avoid undesired atom-molecule collisions we remove the Rb and Cs atoms by Stern-Gerlach separation.\(^{28}\) We finally obtain an optically trapped sample of up to 4000 RbCs Feshbach molecules at a temperature of about 200 nK. To image the molecules and to determine their number we ramp back across the Feshbach resonance to dissociate the molecules and take separate absorption pictures of the Rb and Cs atomic samples.\(^{19}\)

### Table 1 Hön-London factors for the transitions between the rotational state \(J = 2, M_J\) of level \(|1\rangle\) and the rotational states \(J’ = 1\) and \(J’ = 3\) of level \(|2\rangle\).

| \(M_J\) | \(J’ = 1\) | \(J’ = 3\) |
|---|---|---|
| \(v\) | \(\sigma_-\) | \(\sigma_+\) | \(v\) | \(\sigma_-\) | \(\sigma_+\) |
| 0 | \(\sqrt{\frac{1}{15}}\) | \(\sqrt{\frac{1}{15}}\) | \(\sqrt{\frac{2}{15}}\) | \(\sqrt{\frac{2}{15}}\) | \(\sqrt{\frac{4}{15}}\) | \(\sqrt{\frac{4}{15}}\) |
| 1 | \(\sqrt{\frac{1}{10}}\) | \(\sqrt{\frac{1}{10}}\) | 0 | \(\sqrt{\frac{2}{10}}\) | \(\sqrt{\frac{2}{10}}\) | \(\sqrt{\frac{4}{10}}\) | \(\sqrt{\frac{4}{10}}\) |
| 2 | 0 | \(\sqrt{\frac{1}{10}}\) | 0 | \(\sqrt{\frac{2}{10}}\) | \(\sqrt{\frac{2}{10}}\) | \(\sqrt{\frac{4}{10}}\) | \(\sqrt{\frac{4}{10}}\) |
| 3 | 0 | 0 | \(\sqrt{\frac{1}{10}}\) | \(\sqrt{\frac{2}{10}}\) | \(\sqrt{\frac{2}{10}}\) | \(\sqrt{\frac{4}{10}}\) | \(\sqrt{\frac{4}{10}}\) |

The light for driving the lambda-type three-level system is derived from two lasers, \(L_1\) and \(L_2\). These are widely tunable diode laser systems with linewidths of about 10 kHz. For short term stability the optical resonators are referenced to a \(^{133}\)Cs-vapor saturation spectroscopy signal using transfer diode lasers and the beat locking technique. We determine the laser wavelengths by using two independent wavemeters, whose accuracies we estimate to be about 0.0016 cm\(^{-1}\) and 0.0003 cm\(^{-1}\). The beams of lasers \(L_1\) and \(L_2\) have 1/\(e^2\)-intensity radii of 39(1) \(\mu\)m and 20(1) \(\mu\)m at the location of the molecular sample, respectively. The laser beams lie in the horizontal plane and propagate almost collinearly. The magnetic field defining the quantization axis is oriented along the vertical direction. The light is polarized either in the horizontal plane (“h”, \(\varepsilon = ±1\)) or in the vertical (“v”, \(\varepsilon = 0\)) direction. The light can thus induce either \(\sigma^+ / \sigma^-\) or \(\pi\) transitions.

### 3 The intermediate state: the electronically excited states of \(\Omega' = 0^+\) and \(\Omega' = 1^+\) symmetry

For ground-state transfer we are primarily interested in transitions from |1\> to rovibronic levels \(|\nu', J'\rangle\) of the electronically excited mixed states \(0^+\). But also transitions to the state with \(\Omega' = 1\) could be of interest. With our current laser setup we address different vibrational levels ranging from \(\nu' = 33\) to \(\nu' = 38\) for \(0^+\). For each vibrational level we record the excitation spectrum and we measure the single-photon excitation rate.

#### 3.1 Loss resonances and excitation rates to \(\Omega' = 0^+\) levels

In a first set of experiments we perform optical spectroscopy using state |1a\>. The molecules are irradiated by laser \(L_1\) for a certain irradiation time \(t_{\text{irr}}\), typically ranging from 10 \(\mu\)s to 10 ms, and we record the number of remaining molecules in |1a\>. For each data point in the spectrum, a new sample is prepared and the laser frequency \(f_1\) is stepped to a new value. Since prior to our experiments the precise energies of the excited state levels had poorly been known, we first performed our search over a broad range of frequencies \(f_1\) using a comparatively high laser intensity.

We observe a number of resonant loss features caused by excitation to the electronically excited \(0^+\) states. Typical molecular excitation spectra are displayed in Fig. 3(a) and (b). The comparison with the calculated energy positions and rotational constants from Ref.\(^{32}\) results in an assignment to the levels \(\nu' = 33\) to \(\nu' = 38\). As expected, the vibrational levels are not evenly spaced. For each \(0^+\) vibrational level \(\nu'\) we detect a two-peak structure, which we ascribe to the \(J' = 1\) and \(J' = 3\) rotational levels. Fig. 4 presents high resolution
Fig. 3 Typical loss resonances for excitation from the Feshbach level $|1a\rangle$ to (a) the $v' = 37$ and (b) to the $v' = 38$ levels of the $0^+$ potentials. The Feshbach molecules are irradiated for 10 ms with laser light at an intensity of $I = 5 \times 10^5$ mW/cm$^2$ and we plot the number of remaining Feshbach molecules as a function of the laser frequency $f_1$ of laser $L_1$. For each vibrational level we identify two resonances corresponding to $|J' = 1\rangle$ and $|J' = 3\rangle$. The half right of panel (b) shows additional loss peaks corresponding to transitions that we attribute to the excited $\Omega' = 1$ state. Here we observe a more complex structure that includes rotational and hyperfine levels, as discussed in Sec. 3.2. The lines are not fits but are guides to the eye and simply connect the data points.

Fig. 4 High resolution spectroscopy of deeply bound excited levels of RbCs: Typical loss resonances corresponding to various levels of the $0^+$ states for weak excitation from the initial Feshbach level $|1a\rangle$. (a) $|v' = 38, J' = 1\rangle$, (b) $|v' = 35, J' = 1\rangle$, and (c) to the $|v' = 35, J' = 3\rangle$. For comparison, panel (b) also shows a loss feature for excitation from the level $|1b\rangle$ using vertically polarized light (red squares). All measurements are performed with an irradiation time of $t_{irr} = 10\mu s$. The solid lines are fits according to the model discussed in the text. Zero detuning is defined by the minimum of the single exponential fit according to Eq. 1.
scans of selected resonances. Except for the level \( \nu' = 35 \), we do not observe any additional substructure, i.e. substructure caused by Zeeman or hyperfine interaction, in agreement with the expectation of a small hyperfine splitting of the 0\(^{+}\) lines. Table 2 summarizes the transition energies, rotational constants, and further parameters to be discussed below for the relevant vibrational levels of the 0\(^{+}\) potential. We obtain a difference of about \( h \times 7.5 \text{ GHz} \) between calculated and observed transition energies. This discrepancy results from insufficient knowledge of the \( X^1\Sigma^+ \) well depth. Since we measure that energy as described below by two-photon spectroscopy (see Section 4), we provide adjusted values for the calculated transition energies.

Only two rotational lines are observed for each of the 0\(^{+}\) vibrational transitions shown above. This observation gives us information about \( J \) for |1\> as well as about the parity selection rules. The Feshbach level |1\> has \( \ell = 2 \) and has almost full triplet character.\(^{23}\) With \( S = 1 \) and \( L = 0 \) the total angular momentum number can take values \( J = 1, 2, 3 \). For level |2\>, \( J' \) is a good quantum number and rotational states \( J' = 0, 1, 2, 3, 4 \) could be populated in principle. However, as no \( J' = 0, 2, 4 \) lines are observed, we conclude that level |1\> has mostly \( J = 2 \) character (the same observation holds for level |1b\>). From the two-photon spectroscopy below we conclude that \( M_J = +1 \) for level |1a\>. Further, the parity \( P_{\text{tot}} = P_{\text{elec}}P_{\text{rot}} \) of the total wave function is a product of the electronic wave function parity (\( P_{\text{elec}} = +1 \) for both 0\(^{+}\) and \( \nu^4\Sigma^+ \) states) and the rotational wave function parity (\( P_{\text{rot}} = (-1)^J \)).\(^{24}\) As is well known, dipole transitions obey the \(+1 \rightarrow -1 \) selection rule for the total parity. Hence, we have \( P(|1\>) = +1 \), so that only transitions to level |2\> with negative parity are allowed, namely to \( J' = 1, 3 \).

We get an estimate for the natural linewidth \( \Gamma \) of the excited levels from the high resolution scans shown in Fig. 4. These are taken with a much smaller frequency step size for higher spectral resolution and a much lower laser intensity to avoid artificial line broadening due to depletion of the initial state. In a first approximation, we extract \( \Gamma \) by using a simple two-level model. In the limit of \( \Omega_1 \ll \Gamma \) the number of Feshbach molecules \( N \) decays according to the following equation

\[
N(t_{\text{irr}}) = N_0 \exp(-t_{\text{irr}}\Omega_1^2\Gamma/(\Gamma^2 + 4\Delta_1^2)),
\]  

(1)

where \( N_0 \) is the initial molecule number, \( t_{\text{irr}} \) as before is the irradiation time, \( \Omega_1 \) is the Rabi frequency of \( L_1 \), and \( \Delta_1 \) is the laser detuning. For fixed \( t_{\text{irr}}\Omega_1^2 \) we fit Eq. (1) to the spectroscopic data as a function of \( \Delta_1 \) and we extract \( \Gamma \). As an example, Fig. 4(a) shows the loss feature for excitation from \( |1a\> \) to \( |\nu' = 37, J' = 1\> \) together with the fit. The excitation spectra for the \( |\nu' = 35, J' = 1\> \) and \( |\nu' = 35, J' = 3\> \) levels are special cases, exhibiting double loss features as shown in Fig. 4(b) and (c). We fit these resonances using Eq. (1) generalized to the case of two exponential functions. The presence of two closely spaced loss features is probably the result of hyperfine splitting of \( |\nu' = 35, J' = 1\> \) and \( |\nu' = 35, J' = 3\> \). It is unlikely that a level of the \( \Omega' = 1 \) state accidentally overlaps with either the \( |\nu' = 35, J' = 1\> \) or the \( |\nu' = 35, J' = 3\> \) level, as we think that we have identified all the relevant \( \Omega' = 1 \) levels in the wavelength region of interest (see the discussion below in Section 3.2). Nevertheless, a further investigation is needed to clarify this issue.

In Table 2 we list the measured linewidths that we determine by the single exponential function fits. We note that the values given are only approximate as unresolved hyperfine and Zeeman substructure might lead to apparent line broadening. The computed linewidths are derived from the MFGH wave functions and the \( R \)-dependent TDMs (Section 1) neglecting hyperfine structure. The singlet-dominated 0\(^{+}\) levels, i.e. the levels \( \nu' = 33, 36, 38 \), have linewidths of about \( \Gamma_{\text{calc}} \approx 2\pi \times 5 \text{ MHz} \) and the triplet-dominated levels have linewidths of about \( \Gamma_{\text{calc}} \approx 2\pi \times 2 \text{ MHz} \). The measured linewidths are approximately 1 MHz larger than the calculated values.

In a second experiment we measure the single photon excitation rates to obtain an estimate for the Rabi frequency \( \Omega_1 \) and hence for the transition strength for the various transitions. Again we record the time evolution of the Feshbach-molecule number \( N \) as a function of \( t_{\text{irr}} \). This time we keep \( L_1 \) on resonance. In this case Eq. (1) reduces to \( N(t_{\text{irr}}) = N_0 \exp(-t_{\text{irr}}\Omega_1^2\Gamma/\Gamma) \). Typical decay curves of the molecule number in levels |1a\> and |1b\> are shown in Fig. 5. From the fit to the data we determine the decay constant \( t_{\text{irr}} = \Gamma/\Omega_1 \) to obtain the Rabi frequency \( \Omega_1 = (\Gamma/\tau_{\text{irr}})^{1/2} \). The linewidth \( \Gamma \) is taken from the loss resonance data as described above.

In Table 2 we list the normalized Rabi frequencies determined as described above for the transitions from level |1a\>. We have factored out the dependence on laser intensity \( I \). We translate the values into experimental TDMs, which we display in Fig. 6. For reference, also computed TDMs are displayed. These come with an arbitrary scaling factor, as discussed in the previous section. For the transitions to |2\> = |\nu', J' = 3\> the TDMs are essentially independent of polarization. This agrees with the expectation as the calculated TDMs in this case differ by only a factor 1.1 in view of the H"onl-London factors (see Table 1 for \( M_J = +1 \) of level |1a\>). However, for the transitions to |2\> = |\nu', J' = 1\> we find reduced values for the TDMs when we switch from horizontal to vertical polarization. This is in contrast to the expectation, which gives an increase by a factor \( \sqrt{2} \). The discrepancy is even more striking for transitions from the Feshbach level |1b\> to |\nu', J' = 1\>. When we switch from vertical to horizontal polarization the TDM is reduced by more than a factor of 5. Here, one would again expect an increase by a factor of \( \sqrt{2} \). The reduction for the excitation rate by more than a factor of 25 can clearly be seen in the decay measurements (see Fig. 5(c)). It is most probable that the mismatch between experiment and theory cannot be explained within a two-level model, and we speculate that mixing with additional excited levels could be responsible for the unusual behavior. In future, we plan to investigate this issue in detail as it is important for a full understanding of the molecular structure relevant to the ground-state transfer.

3.2 Single photon spectroscopy of the \( \Omega' = 1 \) excited state

In principle, excitation to levels of the electronically excited \( \Omega' = 1 \) and \( \Omega' = 2 \) potentials is possible starting from our Fes-
Some levels of the electronically excited \( \Omega' = 0 \) and \( \Omega' = 1 \) potentials are quite close to each other and could even accidentally overlap. It is thus very important for the future STIRAP transfer scheme to be able to distinguish between these two classes of levels. In the course of our spectroscopic measurements we have detected a number of levels belonging to the \( \Omega' = 1 \) potential. In Fig. 3(b) we clearly see additional loss features on the high-frequency side of the \( v' = 38 \) resonances. These peaks cannot be attributed to any level of either the \( \Omega' = 0 \) or the \( \Omega' = 2 \) potential and hence must be caused by excitations to levels of the \( \Omega' = 1 \) potential.\(^{22}\)

Based on the energy and rotational splittings we identify this level to be the vibrational level with \( v' = 29 \). The loss peaks exhibit a much richer and a more complex substructure than the \( \Omega' = 0 \) features (the substructure is not clearly resolved in the coarse scan shown in Fig. 3(b)). This behavior is to be expected as a result of the excited state Zeeman and hyperfine splitting. Note that the rotational structure is a multiplet of \( J' = 1 \), \( J' = 2 \), \( J' = 3 \) lines. Excitation to \( J' = 2 \) is allowed by the parity selection rules discussed above, because the \( \Omega' = 1 \) potential is doubly degenerate with two individual components of \( +1 \) and \( -1 \) parity.

4 Two-photon dark state resonance spectroscopy

The next step towards coherent optical transfer into the rovibronic ground state is the search for a suitable dark state resonance. It is well known that an essential property of a lambda-type three-level system is the existence of a dark state as an eigenstate of the system.\(^{20}\) This state is dark in the sense that it is decoupled from the excited state \( |2\rangle \). It is thus not directly influenced by the excited state’s radiative decay. The existence of such a loss-free state lies at the heart of the STIRAP technique. It is thus of prime importance to find an appropriate dark state resonance. Here we consider the three-level system involving one of the initial Feshbach states, i.e. either \( |1a\rangle \) or \( |1b\rangle \), an intermediate level \( |2\rangle = |v', J' = 1\rangle \) belonging to the \( 0^+ \) coupled potentials, and the rovibronic ground-state level \( |3\rangle = |v'' = 0, J'' = 0\rangle \) as the final state. Alternatively, we take \( |3\rangle = |v'' = 0, J'' = 2\rangle \) as the third level and compare the data to the data involving the rovibronic ground-state level.

In the experiment we prepare the Feshbach molecules either in state \( |1a\rangle \) or in state \( |1b\rangle \) and simultaneously irradiate the sample with rectangular light pulses from \( L_1 \) and \( L_2 \). Typical irradiation times range between 10 \( \mu \)s to 100 \( \mu \)s. The laser light intensities are chosen such that the Rabi frequency \( \Omega_2 \) for \( L_2 \) is much greater than \( \Omega_1 \), the Rabi frequency for \( L_1 \). Immediately after irradiation we probe the molecule number. We repeat this procedure as we vary the detuning \( \Delta_2 \) of laser \( L_1 \), whereas \( L_2 \) is kept in resonance (\( \Delta_2 = 0 \)). In this way we have explored all the dark state resonances that involve the various excited levels \( |2\rangle = |v', J' = 1\rangle \) found in the one-photon spectroscopy measurements discussed above. We find that the excited level \( |2\rangle = |v' = 35, J' = 1\rangle \) so far gives us the best results as it has the highest two-photon transition.
Table 2: Vibrational quantum numbers $\nu'$ (with the percentage of $b^3\Pi$ and $A^1\Sigma^+$ character in parentheses), experimental and calculated rotational constants $B_{\nu'}$ (in units cm$^{-1}$), experimental and calculated transition energies $E_{[1a],[2]}^\text{exp}$ (in units cm$^{-1}$), experimental and calculated transition dipole moments (TDMs) $D_{[1a],[2]}^\text{exp}$ (in units 10$^{-4}$ a.u.), normalized Rabi frequencies $\Omega_0^\text{calc}$ (in units kHz $\times (1/$(mW/cm$^2$)$)^{1/2}$, where $I$ is the laser intensity), and experimental and calculated natural linewidths $\Gamma$ (in units MHz) for the transition from level $|1a\rangle$ to the 0$^+$ levels in the wavelength range from about 1581 nm to 1557 nm for $J'=1,3$ and for vertical ($v=0$) and horizontal ($h=\pm 1$) polarization $\mathcal{P}$. The calculated transition energies are extracted from Ref. 22 and corrected using our new determination of the $X^1\Sigma^+$ ground-state energy, see Section 5 below. The experimental transition energies are extracted for the Zeeman shift by extrapolation to zero magnetic field. The 1σ-statistical errors are 0.0002cm$^{-1}$ for $B_{\nu'}^\text{exp}, 0.002$cm$^{-1}$ for $E_{[1a],[2]}^\text{exp}$, and 15% for $D_{[1a],[2]}^\text{exp}, \Omega_0^\text{calc}$, and $\Gamma^\text{exp}$.

| $\nu'$ | $B_{\nu'}^\text{calc}$ | $B_{\nu'}^\text{exp}$ | $J'$ | $E_{[1a],[2]}^\text{calc}$ | $E_{[1a],[2]}^\text{exp}$ | $\mathcal{P}$ | $D_{[1a],[2]}^\text{calc}$ | $D_{[1a],[2]}^\text{exp}$ | $\Omega_0^\text{exp}$ | $\Gamma^\text{calc}/2\pi$ | $\Gamma^\text{exp}/2\pi$ |
|-------|-------------------|-------------------|-----|-------------------|-------------------|-------|-------------------|-------------------|-------------------|-------------------|-------------------|
| 33    | 0.0127            | 1                 | 6321.84 | 6321.850          | 11.48             | 3.2   | 0.36              | 5.7               | 6.5               |
| (14.1,85.9) |                      |                   | 34    | 0.0149            | 0.0150            | 1     | 6329.36           | 6329.357          | 1.77              | 0.9               | 0.10              | 1.9               |
| (65.2,34.8) |                      |                   | 3      | 6329.51           | 6329.507          | 3.09  | 2.2               | 0.24              | 1.9               | 2.9               |
| (59.9,40.1) |                      |                   | 35    | 0.0147            | 0.0148            | 1     | 6364.04           | 6364.031          | 2.94              | 2.9               | 0.33              | 2.2               |
| (20.3,79.7) |                      |                   | 36    | 0.0130            | 1                 | 6372.30 | 6372.314          | 11.54             | 4.0               | 0.44              | 5.3               |
| (60.0,40.0) |                      |                   | 37    | 0.0147            | 0.0148            | 1     | 6398.67           | 6398.663          | 4.46              | 2.7               | 0.30              | 2.0               |
| (21.3,78.7) |                      |                   | 38    | 0.0130            | 1                 | 6422.97 | 6422.986          | 8.29              | 1.0               | 0.11              | 5.3               |

strength. Typical dark state spectra for coupling to either the $|\nu'=0,J''=0\rangle$ level or to the $|\nu'=0,J''=2\rangle$ level are shown in Fig. 7(a) and (b). The strong suppression of loss at zero detuning is caused by the appearance of the dark state. In the limit of $\Omega_1 \ll \Omega_2$ there is an analytic solution for the lambda-type three-level system that allows us to perform a simple fit of the w-shaped spectrum in the form of

$$N = N_0 \exp \left(-t_{\text{int}} \Omega_1^2 \left(\frac{4\Gamma^2 + \Gamma_{\text{eff}}(\Omega_2^2 + \Gamma_{\text{eff}}\Gamma)}{\Omega_2^2 + (\Gamma + 2\Delta I)(\Gamma_{\text{eff}} + 2i\Delta)^2}\right)\right).$$

Here, $\Delta = \Delta_1 - \Delta_2$ is the two-photon detuning and the parameter $\Gamma_{\text{eff}}$ phenomenologically accounts for loss and decoherence between levels $|1\rangle$ and $|3\rangle$. From the fit we find for the transition from $|1a\rangle$ to $|\nu'=0,J''=0\rangle$ that $\Omega_1 = 2\pi \times 0.4(3)$MHz and $\Omega_2 = 2\pi \times 0.8(6)$MHz, resulting in $\Omega_1 = 2\pi \times 0.6(4)$kHz(I/(mW/cm$^2$)$)^{1/2}$ and $\Omega_2 = 2\pi \times 7.4(7)$kHz(I/(mW/cm$^2$)$)^{1/2}$. For the transition from $|1b\rangle$ to $|\nu'=0,J''=2\rangle$ we find that $\Omega_1 = 2\pi \times 0.16(2)$MHz and $\Omega_2 = 2\pi \times 5.7(3)$MHz, resulting in $\Omega_1 = 2\pi \times 0.54(8)$kHz(I/(mW/cm$^2$)$)^{1/2}$ and $\Omega_2 = 2\pi \times 6.7(3)$kHz(I/(mW/cm$^2$)$)^{1/2}$. These values, given sufficient laser coherence, should be good enough for performing STIRAP transfer to the vibrational ground state. We note that we measure a comparatively short lifetime for the dark state when we couple to the $|\nu'=0,J''=0\rangle$ level. Fig. 7(a) shows that the dark state involving $|\nu'=0,J''=0\rangle$ decays on the timescale of 10μs. A non-zero $\Gamma_{\text{eff}}$ is responsible for this behavior. In principle, the dark state would show decay if there were not enough laser coherence. However, our data involving the ground-state level $|\nu'=0,J''=2\rangle$ (see Fig. 7(b)) shows essentially no decay on the timescale of 100μs. This fact thus excludes the possibility of insufficient laser coherence. In principle, the short lifetime could limit the efficiency of the STIRAP transfer to $|\nu'=0,J''=0\rangle$ level. We expect that we have to go beyond the simple three-level approximation to understand the reduced lifetime. Additional investigations are needed to shine light on this crucial issue.

From the dark state data we determine the binding energy of the lowest rovibrionic level $|\nu'=0,J''=0\rangle$ of the ground state as follows. The difference of laser frequencies at 217 G (laser $L_1$ at 6364.0439cm$^{-1}$ and laser $L_2$ at 10175.2913 cm$^{-1}$ to populate the $|\nu'=0,J''=0\rangle$ level) measured with respect to the Rb(5$^2$S$^1/2$f,Rb = 1) + Cs(6$^2$S$^1/2$f,Cs = 3) asymptote yields 3811.2477 cm$^{-1}$. The binding energy at zero field, with respect to the center of gravity of the hyperfine manifold, 3811.5755(16) cm$^{-1}$, is obtained by adding the Zeeman shift (0.0131cm$^{-1}$, or 0.394 GHz) and the relevant energy spacing (0.3150cm$^{-1}$, or 9.443 GHz). The error estimates our wavemeter precision. This result represents a 300-fold improvement in accuracy with respect to the previous value of 3811.3(5) cm$^{-1}$ from Ref. 32. Note that in Table 2, the computed 0$^+$ level energies have been corrected by 0.24cm$^{-1}$, as the extraction of potential curves from Ref. 32 relies on the latter value. Our measurement is entirely limited by the precision of our wavemeters and could be greatly improved by e.g. referencing the lasers to a frequency comb. The new
value will allow more accurate coupled-channel calculations to determine the complete ground-state structure of the RbCs system.

5 Conclusions and outlook

We have performed high resolution one- and two-photon laser spectroscopy on ultracold samples of RbCs molecules with the aim to identify a suitable two-photon transition for stimulated ground-state transfer. In particular, we have identified the rovibronic ground state \( |\nu' = 0, J'' = 0 \rangle \) by creating a dark state involving the initial Feshbach level and \( |\nu' = 0, J'' = 0 \rangle \) of the \( X^1\Sigma^+ \) state. We plot the relative number of remaining Feshbach molecules as a function of the detuning \( \Delta \) of laser \( L_1 \). Laser \( L_2 \) is on resonance. The strong suppression of loss at zero detuning reflects the creation of the dark state. The solid lines are fits to the data using a three-level model that includes loss processes. For details see text. (a) The dark resonances involve the initial Feshbach level \( |\nu' = 0 \rangle \), the intermediate level \( |\nu' = 35, J' = 1 \rangle \), and the final level \( |\nu'' = 0, J'' = 0 \rangle \). The polarizations of lasers \( L_1 \) and \( L_2 \) are chosen to be \( v \) and \( h \), respectively. Lasers \( L_1 \) and \( L_2 \) simultaneously irradiate the sample for 20 \( \mu \)s (circles) and 40 \( \mu \)s (squares). (b) Here, the initial Feshbach level is \( |\nu' \rangle \), the intermediate level is \( |\nu' = 35, J' = 1 \rangle \), and the final level is \( |\nu'' = 0, J'' = 2 \rangle \). Lasers \( L_1 \) and \( L_2 \) have \( v \) and \( h \) polarization and are directed onto the molecular sample for 100 \( \mu \)s. Zero detuning is defined by the center of the one-photon resonance derived from a single exponential fit according to Eq. 1.

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Fig. 6 Transition dipole moments measured for different vibrational levels $|\nu', J' = 1\rangle$ of the $0^+$ state with horizontally polarized (filled circles) and vertically polarized light (empty circles) in comparison to the computed values for both horizontally polarized light (filled squares) and vertically polarized light (empty squares). The experimental data refer to the initial Feshbach level $|1a\rangle$. In the model, we chose the $\nu = -3$ level of the $a_3^+ \Sigma^+$ potential to match the overall magnitude of the experimental TDMs, which is equivalent to choosing the $\nu = -6$ level scaled by a factor 2.42 (see Fig. 5).

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