Improved Iterative Parallel Interference Cancellation Receiver for Future Wireless DS-CDMA Systems

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We present a new turbo multiuser detector for turbo-coded direct sequence code division multiple access (DS-CDMA) systems. The proposed detector is based on the utilization of a parallel interference cancellation (PIC) and a bank of turbo decoders. The PIC is broken up in order to perform interference cancellation after each constituent decoder of the turbo decoding scheme. Moreover, in the paper we propose a new enhanced algorithm that provides a more accurate estimation of the signal-to-noise-plus-interference-ratio used in the tentative decision device and in the MAP decoding algorithm. The performance of the proposed receiver is evaluated by means of computer simulations for medium to very high system loads, in AWGN and multipath fading channel, and compared to recently proposed interference-cancellation-based iterative MUD, by taking into account the number of iterations and the complexity involved. We will see that the proposed receiver outperforms the others especially for highly loaded systems.

Keywords and phrases: code division multiple access, parallel interference cancellation, turbo multiuser detection, iterative detection and decoding, nonlinear MMSE soft decision.

1. INTRODUCTION

One of the main shortages of the code division multiple access (CDMA) communication systems can be identified in their vulnerability to multiple access interference (MAI): hence, during the 90s, great attention has been devoted to multiuser detection strategies that constitute the natural answer to this problem; the receivers based on this technique aim to exploit the interference as an additional information source but, generally, are characterized by a very high complexity. Firstly, multiuser detection researches have been focused on uncoded systems; however, practical CDMA communications rely on the utilization of error control coding and interleaving so that, recently, more and more attention has been addressed to coded systems. Optimal joint decoding/detection is an excellent solution to this problem, as shown in [1]. However, this scheme results in a prohibitive computational complexity for actual implementation. In contrast, suboptimal solutions, which separate the operations of symbol detection and channel decoding, appear more attractive for practical applications.

Particularly, the successful proposal of turbo codes [2] naturally leads to investigate the feasibility of iterative (turbo) processing techniques in the design of multiuser receivers. In the iterative multiuser detection, extrinsic information is determined in each detection and decoding stage and used as a priori information for the next iteration. This procedure is adopted at each iteration as in turbo codes: this detection philosophy is defined as turbo MUD and the advantages due to its introduction are remarkable, also for heavily loaded systems. In the last years, many iterative receivers that can achieve near-optimal performance [3, 4] have been investigated, but with the drawback of the complexity, that is still exponential in the number of users. This is the reason of the attention addressed to interference cancellation schemes [5, 6, 7, 8, 9].
The equivalent baseband received signal can be written as:

\[ b(t) + n(t) \]

where \( b(t) \) is the baseband signal and \( n(t) \) is the additive white Gaussian noise (AWGN) process with double-sided spectrum density \( \sigma^2 = N_0/2 \) (W/Hz).

In the receiver a bank of matched filters is used for despreading. Without loss of generality, we can assume that the first bit interval is observed: therefore, the index \( i \) in all the these variables is dropped. As a result, the output of the \( k \)th matched filter is given by

\[ y_k = \frac{1}{T_b} \int_0^{T_b} r(t) s_k(t) dt = \sqrt{E_b} c_k + \sum_{j=1}^N \sqrt{E_b} c_j \rho_{jk} + n_k, \] (2)

where \( \rho_{jk} \) is the normalized cross-correlation coefficient between the \( j \)th and \( k \)th users and \( n_k \) is the noise Gaussian sample of the \( k \)th user with distribution \( N(0, \sigma^2) \).

### 2. SYSTEM MODEL

We consider an uplink DS-CDMA communication system with \( K \) synchronous turbo-coded users. Timing, amplitudes, carrier phases, and spreading sequences of all the users are assumed to be perfectly known at the receiving end in the base station. Each user encodes blocks of information bits \( n_{k,i} \) with a parallel concatenated convolutional code (PCCC) and transmits the resulting codewords composed of \( I \) coded bits over a common AWGN channel with BPSK modulation. The equivalent baseband received signal can be written as

\[ r(t) = \sum_{k=1}^K \sqrt{E_b} \sum_{i=0}^{I-1} c_k, p(t - iT_b) s_k(t - iT_b) + n(t), \] (1)

where

(i) \( T_b \) is the bit interval;

(ii) \( E_b \) is the \( k \)th user received energy;

(iii) \( c_k \in \{ +1, -1 \} \) is the bit transmitted by \( k \)th user during the \( i \)th bit period;

(iv) \( p(t) \) is the unit-power rectangular pulse shape with duration \( T_b \);

(v) \( s_k(t) \) is the \( k \)th user unit-power spreading sequence;

(vi) \( n(t) \) is an additive white gaussian noise (AWGN) process with double-sided spectrum density \( \sigma^2 = N_0/2 \) (W/Hz).

In this paper, we propose a new iterative multiuser detector based on the utilization of a parallel interference cancellation (PIC) and a bank of turbo decoders. In the proposed structure the PIC detector is broken up so that it is possible to perform interference cancellation after each constituent convolutional decoder. Due to the tight relationship between the proposed receiver and the MAP decoders, we defined it as MAP decoder aided PIC (MPIC): this solution aims to profit by IC introduction from the first iterations. Moreover, in the paper the variance of the noise-plus-(residual-)interference is determined by a new algorithm: particularly, only the most reliable symbols are used in variance determination, neglecting all the others. This solution affords performance improvement for all the considered systems.

### 3. A NEW IC ITERATIVE RECEIVER

An iterative cancellator consists of an interference-cancellation (IC)-based multiuser detector (MUD) followed by \( K \) single-user turbo decoders. Each constituent block iteratively provides soft information to the others, as shown in Figure 1. In the first multiuser detection iteration, the a priori information of the coded bits is not available, that is, \( \hat{L}_{ap}(c_k) = 0, \ k = 1, 2, \ldots, K \). The IC stage delivers interference-cancelled soft outputs \( \hat{y}_k \) to the input of the turbo decoders. After a fixed number of turbo decoder iterations, the extrinsic information of the coded bits at the output of turbo decoders are fed back to the input of the IC detector as the a priori information for the next receiver iteration.

The considered turbo codes are composed of two recursive systematic convolutional codes (RSC) which are connected by an interleaver and a MAP-based algorithm is used for iterative decoding [10]. Since the IC receiver requires soft information about the reliability of both the systematic and the parity bits, the decoding algorithm is properly modified.
to produce also extrinsic information about the latter [11]. At each new iteration, the iterative structure permits the multiuser receiver to have a more reliable a priori information and the decoders to operate on the soft inputs, in which a greater amount of interference has been cancelled.

### 3.1. The conventional iterative PIC receiver

In the conventional iterative parallel interference cancellation (PIC) receiver [12], at each IC stage, MAI is to be removed simultaneously from each user. Therefore, at the $m$th receiver iteration, the PIC soft output, that is, the turbo decoders input, can be expressed as

$$
\hat{y}_k(m) = y_k - \sum_{j=1}^{N} E_b \rho_k \hat{c}_j(m)
$$

$$= \sqrt{E_b} c_k + \sum_{j=1}^{N} E_b \rho_{kj} (c_j - \hat{c}_j(m)) + n_k,
$$

(3)

where $\hat{c}_j(m)$ is the estimate at the $m$th iteration of the bit $c_j$ transmitted by $j$th user. Note that the second summation represents the residual MAI after cancellation.

The data estimates $\hat{c}_k(m)$ have been chosen in [12] as the expectation of coded bits, that is equal to

$$
\hat{c}_k(m) = E [c_k(m)] = \tanh \left( \frac{1}{2} L_{ap}(c_k(m)) \right),
$$

(4)

in order to take advantage of the turbo decoders output. The term $L_{ap}(c_k(m))$ is the a priori log-likelihood ratio of bit $c_k$ at the $m$th iteration, which is defined as

$$
L_{ap}(c_k(m)) \triangleq \log \frac{P(c_k(m) = +1)}{P(c_k(m) = -1)}.
$$

(5)

In the first receiver iteration no a priori information is available from the decoder output. Hence, as an initializing condition, it is assumed that $L_{ap}(c_k(0)) = 0$, $k = 1, 2, \ldots, K$.

Instead, in the successive iterations the extrinsic information coming from the decoders can be used, leading to $L_{ap}(c_k(m)) = L_{ap}(c_k(m - 1))$.

### 3.2. The proposed iterative MPIC receiver

As it is known, as the number of decoding iterations increases, the coding gain offered by a turbo decoder becomes larger. However, the performance improvement obtained by the turbo codes is remarkable in the first iterations, and more and more negligible in the successive ones. This remark suggests to concentrate the significant part of interference cancellation in the first iterations: for this reason many IC-based iterative receivers with a first linear stage have been proposed [7, 8, 13]. Nevertheless, a linear MUD has the drawback of extremely high computational complexity.

In this paper we present an iterative PIC receiver, which exploits most interference-cancellation in the first iterations: a conventional iterative receiver tries to cancel the MAI from all the parity and the systematic bits only once at the end of each decoding iteration. Note that in turbo decoding iteration, the first MAP decoder provides extrinsic information about all the systematic and half of the parity bits while the second decoder gives the extrinsic information about the interleaved systematic bits and the second half of the parity bits; as a consequence, in the proposed receiver the interference-cancellation is performed after each decoding iteration and the systematic bits are cancelled twice. Because of the tight connection between the proposed receiver and the MAP decoders, we have named it as MAP decoder aided PIC (MPIC).

The structure of this receiver is shown in Figure 2. Note that the subscripts $s, p_1,$ and $p$ have been added in this figure to describe thoroughly the performance cancellation operation.

Assuming that $R_c$ is the turbo encoder code rate and that only the parity bits are punctured at the transmitter end, the computational complexity needed by the MPIC to perform interference cancellation at each iteration is $(1 + R_c)$ greater than the conventional PIC. However it will be shown by simulation that the proposed iterative receiver performance...
is better than the conventional one even with equal complexity. This goal has been reached by removing from the last iterations so many cancellation stages equal to the ones added in the first iterations.

3.3. An improved nonlinear MMSE estimator

The tentative decision device (4), which is used to estimate the data bits and to reconstruct and cancel the MAI, exploits only the extrinsic information from the decoders but not channel outputs; hence, only a fraction of available information sources is used in the decision. An improved data estimator can be obtained by exploiting jointly decoders and channel outputs, as in [6], where an ML estimator is used, producing tentative hard decisions [14]. Unlike [6], we derive a nonlinear MMSE estimator, that can also provide the reliability value of each estimated bit. The decision \( \hat{c}_k(m) \), for \( k \)-th user at the \( m \)-th receiver iteration, is taken as the expectation of \( c_k \), given the channel output, that is,

\[
\hat{c}_k(m) = E[c_k(m) \mid \tilde{y}_k(m)].
\]

(6)

Under the assumption that the interference can be modelled as a Gaussian process, it can be demonstrated that

\[
\hat{c}_k(m) = \text{tanh} \left[ \frac{1}{2} \left( 2 \frac{\sqrt{E_b} \tilde{y}_k(m)}{\sigma_k^2} + L_\text{ap} (c_k(m)) \right) \right],
\]

(7)

where \( \sigma_k^2 \) is the thermal noise-plus-interference variance, given by \( \sigma_k^2 = \sigma^2 + \sigma_{k,\text{MAI}}^2 \). The proof of (7) can be found in the appendix. As it is shown in [15], the combination of the channel output and the extrinsic information in the decision statistic yields a biased residual interference term which tends to cancel the useful signal. However, the computer simulations confirm that a better performance is achieved by using all the information sources and that the mitigation of the bias effect is obtained after few iterations.

3.4. Variance estimation

The tentative decision device needs to know the noise-plus-(residual-)interference variance, such as the channel reliability value used in the MAP decoding [2]; hence, an appropriate estimation method has to be used. In [5, 16] a simple algorithm based on the data samples has been proposed; particularly, therein the variance is calculated as

\[
\hat{\sigma}_k^2(m) = \frac{1}{I_1} \sum_{i=0}^{I_1-1} (\tilde{y}_{k,i}(m))^2 - \overline{y}_{k,i}(m)^2,
\]

(8)

where the mean \( \overline{y}_{k,i}(m) \) has been either derived by the samples [16] or assumed equal to the square root of the received energy \( \sqrt{E_b} \) [5]. As it will be confirmed by the simulation results, this algorithm leads to the underestimation the variance in the case of a low signal-to-interference-plus-noise ratio (SINR). The motivation of this behaviour is the following: assuming that the (residual-)interference is Gaussian, the conditional probability density functions (pdf) of the variable \( \tilde{y}_{k,i}(m) \), that is, \( p(\tilde{y}_{k,i}(m) \mid c_k = \pm 1) \), are also Gaussian. As a consequence, the unconditional pdf of \( \tilde{y}_{k,i}(m) \) is given by

\[
p(\tilde{y}_{k,i}(m)) = P(c_k = +1)p(\tilde{y}_{k,i}(m) \mid c_k = +1) + P(c_k = -1)p(\tilde{y}_{k,i}(m) \mid c_k = -1)
\]

where the last equality follows from the assumption that the transmitted bits are independent and identically distributed (i.i.d.). As it can be seen from Figure 3, the values \( \tilde{y}_{k,i}(m) \), satisfying the inequality \( |\tilde{y}_{k,i}(m)| < \sqrt{E_b} \), are ambiguous, in the sense that they belong to the region of maximum superposition of the conditional pdfs. For this reason we have chosen to evaluate the variance only by the values satisfying \( |\tilde{y}_{k,i}(m)| \geq \sqrt{E_b} \). This original variance definition can be used to improve the variance estimation through the formula

\[
\hat{\sigma}_{k,m}^2 = \frac{1}{I_1} \sum_{i=0}^{I_1-1} \left( |\tilde{y}_{k,i}(m)| - \sqrt{E_b} \right)^2,
\]

(10)

where \( I_1 \leq I \) indicates the number of such values in a codeword.

4. ITERATIVE MPIC FOR MULTIPATH SLOWLY FADING CHANNELS

Wireless CDMA systems usually have to cope with multipath fading environments. The multipath fading channel is often assumed to be wide-sense stationary with uncorrelated scattering [17]. Based on this assumption, the received baseband DS-CDMA signal can be written as

\[
r(t) = \sum_{k=1}^{K} \sum_{i=0}^{L-1} \sum_{l=1}^{L} \sqrt{E_b} c_k \alpha_k^i(t) s_k(t - iT_b - \tau_k^l) + n(t),
\]

(11)

where \( L \) is the number of propagation paths and \( \alpha_k^i(t) \) and \( \tau_k^l \) are, respectively, the time-varying complex attenuation factor and the relative delay of the \( l \)-th path of the \( k \)-th user.

![Figure 3: Decision variable probability density function.](image-url)
signal. Besides, we assume that $E\{\sum_{l=1}^{L} ||\alpha_{k}^{l}(t)||^2\} = 1/T_b$, so that $E_{b_k}$ is the received averaged energy of the $k$th user, and that the channel fading is so slow that $\alpha_{k}^{l}(t)$ does not change in a chip interval and thus can be denoted as $\alpha_{k}^{l}(h)$, where $h$ refers to chip position in the codeword. The chip matched filter output for the $l$th path of the $k$th user is then given by

$$y_{k,l,h}^{(l)} = \frac{1}{T_c} \int_{(h-1)T_c + \tau_{l}^{k}}^{hT_c + \tau_{l}^{k} - \lfloor \frac{h}{G} \rfloor T_b} r(t) s_h(t - \tau_{l}^{k} - \lfloor \frac{h}{G} \rfloor T_b) dt,$$

where $T_c$ is the chip interval that is tied to the bit interval through the processing gain $G = T_b/T_c$.

If a maximal ratio combiner (MRC) RAKE receiver is used, the decision statistic can be expressed as

$$y_{k,i} = \sum_{l=1}^{L} \sum_{h=iG}^{(i+1)G-1} (\alpha_{k}^{l}(h))^* y_{k,l}^{(l)}(h), \quad i = 0, 1, \ldots, I - 1. \quad (13)$$

In the $m$th iteration of the iterative PIC receiver, the $k$th received signal after the MAI subtraction is given by

$$r_{k}^{(m)}(t) = r(t) - \sum_{j=1}^{E_b} \sum_{i=0}^{I-1} \sum_{l=1}^{L} \sum_{h=iG}^{(i+1)G-1} \sqrt{E_{b_{j}}\xi_{j}(m)} \alpha_{k}^{l}(h) s_j(t - iT_b - \tau_{l}^{j}), \quad (14)$$

Figure 4: Histograms and Gaussian approximations of matched filters and PIC output for different iterations: $E_{b_0}/N_0 = 10$ dB. (b) One iteration. (c) Two iterations. (d) Six iterations.
where the bit tentative decision $\hat{c}_{j,i}(m)$ is given by (7), while
the variance estimation formula has to be modified to take
into account the fading attenuation. The conditional pdfs
$p(\hat{y}_{k,i}(m) \mid c_{k,i} = \pm 1, \alpha_{k}^{l})$ are Gaussian and (10) can be
rewritten as

$$\hat{\alpha}_{k}^{2}(m) = \frac{1}{I_{i}} \sum_{l=0}^{I_{i}-1} \left( \frac{|\hat{y}_{k,i}(m)| - \overline{c_{k}(l)} \sqrt{E_{b,k}}}{\alpha_{k}^{l}} \right)^{2},$$

where $\overline{c_{k}(l)}$ is the bit-averaged fading attenuation after re-
combination and it is computed as

$$\overline{c_{k}(l)} = \frac{1}{G} \sum_{h=1}^{G} \sum_{l=1}^{L} \left| c_{k}^{l}(iG + h) \right|^{2}. \quad (16)$$

## 5. SIMULATION RESULTS

In this section we investigate the effectiveness of the proposed
receiver through computer simulations. In order to mitigate
the complexity burden due to the implementation of a non-
linear decision device, the tanh(·) function has been approxi-
mated by an eight-value look-up table. For all simulations we
use a rate $R_{k} = 1/2$ turbo code, composed of two 8-state RSC
codes with generator polynomials $G_{0} = (13)_{h}, G_{1} = (15)_{h},$
and the block interleaver recommended by the UMTS stan-
dard [18]. We compare the proposed iterative MPIC receiver
with the conventional PIC [6] and the iterative partial PIC
(PPIC) receiver proposed in [6] and derived from [14].

First, we analyze the performance in a synchronous
AWGN channel. The system has 10 equal-power users with
pseudo-noise short codes, processing gain $G=16$, and frame
length 800. The quantized log-MAP algorithm is used for
the decoding [10]. Figure 4 shows the decision variables his-
togram at the output of the MF bank and of the PIC re-
ceiver after 1, 2, 3, and 6 iterations for a signal-to-noise-ratio
$E_{b}/N_{0} = 10$ dB, compared with the Gaussian distribution
with variance calculated through (10). We can remark the
interference reduction through iterations and the accuracy
of enhanced variance estimation, while a bias is evident just
in the first iteration. In Figure 5 the performance improve-
ment obtained using the enhanced variance estimator in com-
parison with the basic one, derived from (8), is shown. Figure 6 shows the performance gain achieved by the pro-
posed receiver by increasing the number of iterations. At a
BER of $10^{-4}$ and with 16 iterations the loss from the single-
user bound is about 0.8 dB. A comparison of performance
versus iterations between the iterative PIC, MPIC, and PPIC
is made in Figure 7 at $E_{b}/N_{0} = 3$ dB. The cancellation weights
for PPIC have been found by a trial-and-error searching
method, as $p_{0} = 0.55$, $p_{1} = 0.65$, $p_{2} = 0.75$, $p_{3} = 0.85,$
$p_{4} = 0.92$, $p_{5} = 0.97$, $P_{DOCS} = 1.0$.

Then, we illustrate the performance of the proposed re-
ceiver in an asynchronous 3-path fading channel with per-
fected power control: the replica amplitudes are assumed to
be Rayleigh distributed, with relative attenuations equal to
0, $-1$, $-9$ dB. Processing gain is $G = 15$ and the spread-
ing operation is performed by a set of pseudonoise short
codes. The frame length is 500, a MRC-RAKE receiver is used
as path-combiner and the max-log-MAP algorithm is used
for the decoding. The channel has a normalized frequency
Doppler $f_{d}T_{h} = 0.0002$ and just 2 receiver iterations are
performed. The other transmission parameters are the same as
the AWGN case. In Figure 8 it can be seen that in a system
with 20 active users, that is, with a system load $\beta = N/G$.
greater than one ($\beta = 1.33$), the MPIC outperforms the conventional PIC: a gain of $3.5$ dB for the MPIC versus the PIC receiver at a BER of $10^{-3}$ is observed. In this figure, the great benefit obtained for both the receivers is shown by using a correct estimate of the noise-plus-(residual-)interference variance rather than approximating it by the ambient noise, assumed perfectly known, as in [6]. Figure 9 shows that the iterative MPIC receiver can support heavily loaded DS-CDMA systems. This behaviour can be exalted with the assistance of low cross-correlations spreading sequences, as shown in Figure 10 where the MPIC receiver reaches single-user performance in a fully loaded DS-CDMA system, with normalized Doppler frequency $f_d T_b = 0.0004$, processing gain 31, and 31 equal-power users using Gold31 codes.
6. CONCLUSION

In this paper, a new turbo multiuser detector for turbo-coded DS-CDMA systems has been presented. In the proposed detector a parallel interference cancellation (PIC) has been divided in order to perform interference cancellation after each MAP constituent decoder. Moreover, an improved algorithm to estimate the variance of the noise-plus-residual-interference has been derived. Performance results of computer simulations for different system loads, in AWGN and multipath fading channel, confirm the excellent behaviour of the proposed receiver. It is shown that it outperforms recently proposed alternative IC-based turbo MUD with the same complexity.

By invoking Bayes theorem, the decision variable is equal to

\[ p(\hat{c}_k(m) | c_k(m)) = \frac{1}{\sqrt{2\pi\sigma_k^2}} \exp \left( \frac{(\hat{y}_k(m) - E_{b_k}c_k(m))^2}{2\sigma_k^2} \right) = \frac{1}{\sqrt{2\pi\sigma_k^2}} \exp \left( \frac{(\hat{y}_k(m))^2 + E_{b_k}}{2\sigma_k^2} \right) \exp \left( \frac{E_{b_k}c_k(m)}{\sigma_k^2} \right). \]  

(A.3)

and, that

\[ \exp \left( 2\left( E_{b_k}c_k(m)/\sigma_k^2 \right) + L_{ap}(c_k(m)) \right) - \exp \left( -2\left( E_{b_k}c_k(m)/\sigma_k^2 \right) - L_{ap}(c_k(m)) \right) \]  

\[ \exp \left( 2\left( E_{b_k}c_k(m)/\sigma_k^2 \right) + L_{ap}(c_k(m)) \right) + \exp \left( -2\left( E_{b_k}c_k(m)/\sigma_k^2 \right) - L_{ap}(c_k(m)) \right). \]  

(A.5)

\[ \exp (c_kL_{ap}(c_k(m))/2) = \exp (-c_kL_{ap}(c_k(m))/2 + \exp (c_kL_{ap}(c_k(m))/2), \]  

(A.4)

By taking into account that

\[ p(\hat{y}_k(m) | c_k(m)) = \frac{1}{\sqrt{2\pi\sigma_k^2}} \exp \left( \frac{(\hat{y}_k(m) - E_{b_k}c_k(m))^2}{2\sigma_k^2} \right) \]  

(A.2)

\[ \sum_{c_k \in \{+1,-1\}} c_k \exp (c_kL_{ap}(c_k(m)) \right) \]  

(A.1)

\[ \exp (c_kL_{ap}(c_k(m))/2) \right) + \exp (c_kL_{ap}(c_k(m))/2), \]  

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