1. Introduction

In recent years, low-mass stars have become the focus of the search for exoplanets via radial-velocity (RV) signals. The fact that the habitable zones of M dwarfs are much closer to the host star than those of solar analogs, combined with their low masses and radii, means that the detection of Earth-mass planets in a temperate environment is comparatively easy. There have been several exoplanet search campaigns targeting low-mass stars (e.g., Zechmeister et al. 2009; Bonfils et al. 2013; Berta et al. 2013), contributing to a total of 234 known exoplanets orbiting M dwarf hosts to date. Several stars in the immediate neighborhood of the Sun have recently been found to harbor Earth-sized exoplanets within their habitable zone, such as our closest neighbor Proxima Centauri (Anglada-Escudé et al. 2016) and the close-by Barnard’s Star (Ribas et al. 2018), Teegarden’s Star (Zechmeister et al. 2019), and Lalande 21185 (Stock et al. 2020b, and references therein).

2. Methods

We have assembled a catalog of 11 634 archival spectra of 186 M dwarfs acquired by seven different instruments covering the Ca\textsc{ii} H&K regime: ESPaDOnS, FEROS, HARPS, HIRES, NARVAL, TIGRE, and UVES. The relative chromospheric flux in these lines, \( R'_{\text{HK}} \), was directly extracted from the spectra by rectification with PHOENIX synthetic spectra via narrow passbands around the Ca\textsc{ii} H&K line cores.

3. Results

The combination of archival spectra from various instruments results in time series for 186 stars from the CARMENES GTO sample. As an example of the use of the catalog, we report the tentative discovery of three previously unknown activity cycles of M dwarfs.

4. Conclusions

We conclude that the method of extracting \( R'_{\text{HK}} \) with the use of model spectra yields consistent results for different instruments and that the compilation of this catalog will enable the analysis of long-term activity time series for a large number of M dwarfs.

Key words. stars: activity – planetary systems – techniques: radial velocities – stars: late-type.
One of the surveys dedicated to discovering planets orbiting M dwarfs is CARMENES (Quirrenbach et al. 2010; Reiners et al. 2018), an instrument built for the 3.5 m telescope at the Calar Alto Observatory. Being designed for high-precision RV measurements of cool stars, it comprises two spectrograph channels with wavelength ranges of 0.52–0.96 μm and 0.96–1.71 μm, respectively, with spectral resolutions of R ~ 80 000–96 000 (Quirrenbach et al. 2014) capable of providing an RV accuracy of ~1.2 m s$^{-1}$ (Bauer et al. 2020). More than 350 stars from the CARMENES guaranteed time observations (GTO) sample have been monitored since January 2016, resulting in 26 planet detections to date (e.g., Bluhm et al. 2020; Nowak et al. 2020, see Sabotta et al. 2021 for an exhaustive review), as well as several planet confirmations (Trifonov et al. 2018, 2020; Sarkis et al. 2018; Lalitha et al. 2019; Stock et al. 2020a).

The study of stellar magnetic activity plays a crucial role in the search for Earth-like planets around M dwarfs. These stars can be very active, resulting in a high level of irradiation in the UV and X-ray regimes for planets within their habitable zones (e.g., Shields et al. 2016; Vida et al. 2017; Youngblood et al. 2018). Some of these chromospheric indicators are the Ca II H&K triplet (IRT; Wilson & Merrill 1937; Shine & Linsky 1972; Mittag et al. 2017), and the Hα line (Fekel et al. 1986).

A common approach to deriving the chromospheric flux from spectroscopic data is the subtraction of appropriate model atmospheres, or comparison spectra of inactive stars with similar parameters, from measured spectra. Named the “spectral subtraction technique” by Montes et al. (1995), variations of it had been in use around a decade earlier (Barden 1985; Herbig 1985). Since then, it has been employed by various authors to measure the chromospheric flux excess in the Ca II H&K lines, for example, for FGK-type stars using PHOENIX model atmospheres by Mittag et al. (2013), or for M dwarfs using BT-Settl models (Allard 2014) by Scandariato et al. (2017). Other authors have employed different techniques to determine the chromospheric emission in Ca II H&K for M dwarfs, such as Suárez Mascareño et al. (2015, 2018) or Astudillo-Defru et al. (2017a), who calibrated and converted the S index (Wilson 1968) extracted from HARPS spectra.

The study of long-term magnetic cycles and their possible relation to stellar rotation periods may provide further insight into the dynamo mechanism (Baliunas et al. 1996; Böhm-Vitense 2007; Shulyak et al. 2015). Several such cycles in M dwarfs have been detected using photometric and spectroscopic data (Savanov 2012; Robertson et al. 2013; Suárez Mascareño et al. 2016; Díez Alonso et al. 2019, and references therein). Chromospheric activity indices for the CARMENES sample of M dwarfs have been studied by various authors (Reiners et al. 2018; Schöfer et al. 2019). Besides, Jeffers et al. (2018) studied the sensitivity of, and correlations between, the indicators within the CARMENES spectral range with a larger sample, while Fühmeister et al. (2014) used time series of Hα, Na I D1, and Ca II H&K regime, Jeffer et al. (2018) used FEROS, CAFE (Aceituno et al. 2013) and HR3 (Tull 1998) spectra to obtain emission levels in these lines for a large number of targets from the CARMENES GTO sample.

The aim of this work is to use a variant of the spectral subtraction technique and assemble a database of archival spectra of the CARMENES GTO sample acquired with seven instruments, from which $R'_{\text{HK}}$, that is, the chromospheric emission in Ca II H&K relative to the bolometric flux, is extracted in a homogeneous fashion. The main purpose of this catalog of $R'_{\text{HK}}$ time series is to enable the determination of stellar rotation periods. Since the CARMENES spectrograph does not cover the Ca II H&K regime, Jeffers et al. (2018) used FEROS, CAFE (Aceituno et al. 2013) and HR3 (Tull 1998) spectra to obtain emission levels in these lines for a large number of targets from the CARMENES GTO sample.

Table 1. Source instruments for the database.

| Instrument   | $R'_{\text{HK}}$ | References | Archive links | # |
|--------------|-----------------|------------|---------------|---|
| ESPaDOnS    | 80              | 1, 2       | 10            | 577 |
| FEROS       | 48              | 3          | 12            | 345 |
| HARPS       | 115             | 4          | 12            | 4057 |
| HIERES      | 25–85           | 5, 6       | 12            | 4232 |
| NARVAL      | 65–75           | 2, 7       | 10            | 2283 |
| TIGRE       | 20              | 8          | 13            | 131  |
| UVES        | 22–78           | 9          | 11            | 68   |
| Total       |                 |            |               | 11634 |

References. (1) Donati et al. (2006); (2) Petit et al. (2014); (3) Kaufer et al. (1999); (4) Mayor et al. (2003); (5) Vogt et al. (1994); (6) Vogt (2002); (7) Donati et al. (1997); (8) Schmitt et al. (2014); (9) Dekker et al. (2000); (10) http://polarbase.irap.omp.eu/; (11) http://archive.eso.org/scienceportal/home/; (12) koa.ipac.caltech.edu/; (13) https://hsweb.hs.uni-hamburg.de/projects/TIGRE/EN/hrt_user/hrt_user_main_page.html.
Fig. 1. Schematic of the direct determination of \( R'_{\text{HK}} \) from a single HARPS spectrum of the M1.5 V star HD 36395 (Karmn J05314–036). Its tabulated astrophysical parameters are \( T_{\text{eff}} = 3891 \pm 51 \text{ K}, \log g = 4.64 \pm 0.07, [\text{Fe/H}] = 0.23 \pm 0.16 \) (Schweitzer et al. 2019) and an upper limit of \( v \sin i = 2 \text{ km s}^{-1} \) (Reiners et al. 2018). Top panel: a PHOENIX synthetic spectrum with parameters \( T_{\text{eff}} = 3900 \text{ K}, \log g = 4.5, [\text{Fe/H}] = 0.0 \). Middle panel: the measured HARPS spectrum. The six bands used for rectification of the spectrum and subtraction of the photospheric flux (\( H, K, h_1, h_2, k_1, \) and \( k_2 \)) are marked as shaded areas. Bottom panel: flux-calibrated spectrum (black line) after rectification of the measured spectrum with the gradient functions \( g_{\text{ms}}^k(\lambda) \) and, for comparison, the PHOENIX spectrum (gray line). The chromospheric fluxes \( F'_{\text{HK}} \) (gray areas in bottom panel) are derived by subtracting the theoretical photospheric fluxes \( F_{\text{HK,phot}} \) (gray areas in upper panel) from the surface fluxes \( F_{\text{HK}} \) (gray areas in middle panel).

the approach. We denote \( R_{\text{HK}}' \) as the ratio between \( \text{Ca} \, \text{II} \) H\&K emission and the stellar bolometric flux (Linsky \\& Ayres 1978; Linsky et al. 1979):

\[
R_{\text{HK}}' = \frac{F_{\text{HK}}'}{F_{\text{bol}}} = \frac{F_{\text{H}}' + F_{\text{K}}'}{\sigma T_{\text{eff}}^4},
\]

where \( T_{\text{eff}} \) is the stellar effective temperature, \( \sigma \) is the Stefan-Boltzmann constant, and \( F_{\text{H}}' \) and \( F_{\text{K}}' \) are the chromospheric fluxes:

\[
F_{\text{H}}' = F_{\text{H}} - F_{\text{H,phot}},
F_{\text{K}}' = F_{\text{K}} - F_{\text{K,phot}},
\]

that is, the difference between the surface fluxes \( F_{\text{H}} \) and \( F_{\text{K}} \) and the photospheric fluxes \( F_{\text{H,phot}} \) and \( F_{\text{K,phot}} \).

The oldest approach to derive \( R_{\text{HK}}' \) has been to determine the Mount Wilson \( S \) index (Wilson 1968; Duncan et al. 1991) and subsequently transform it via color-dependent conversion factors (Middelkoop 1982; Noyes et al. 1984):

\[
R_{\text{HK}}' = C_{\text{cf}} \frac{S}{R_{\text{bol}}},
\]

in which the conversion factor \( C_{\text{cf}} \) and the ratio between photometric and bolometric flux \( R_{\text{phot}} = (F_{\text{H,phot}} + F_{\text{K,phot}})/F_{\text{bol}} \) are color-dependent (e.g., Astudillo-Defru et al. 2017a).
Since our database contains archival spectra from seven different instruments with spectral resolutions $R$ ranging from $\approx 2 \times 10^4$ to $\approx 10^5$ and we wanted to avoid any transformation via the S index, we chose to determine the relative flux excess with a variant of the spectral subtraction technique using a set of narrow wavelength bands around the H and K lines to rectify the spectra with PHOENIX synthetic spectra (Husser et al. 2013).2

The approach can be summarized in the following steps:

- Each spectrum in the grid of PHOENIX synthetic spectra is rotationally broadened using the PYAstromony package (Czesla et al. 2019) with rotational velocities in the range of $v \sin i = [0, 100]$ km s$^{-1}$ in increments of 1 km s$^{-1}$ with a linear limb-darkening law and coefficients from Claret & Bloemen (2011) for the Johnson U filter.
- Each spectrum from this extended grid is then instrumentally broadened with the appropriate spectral resolution.
- Mean fluxes in six bands are extracted from each model spectrum, one of width 1.2 Å around the center of each of the H&K lines, and in two narrow bands of width 0.5 Å situated around each line. The passbands, which are listed in Table 2 (shaded red and blue areas in Fig. 1) and, from this theoretical spectrum, we only required $H$ and $K$ line cores. In order to avoid the extraction of the resulting set.
- The gradients $g_{\text{th/hs}}(\lambda)$, $g_{\text{th/ms}}(\lambda)$, and $g_{\text{th/k2}}(\lambda)$ between the sets of passbands $h_1, h_2$ and $k_1, k_2$ are calculated for the theoretical (“th”) and measured (“ms”) spectrum via:

$$g_{\text{th/hs}}(\lambda) = \frac{F_{\text{th/hs}}(\lambda_{h1}) - F_{\text{th/hs}}(\lambda_{h2})}{\lambda_{h1} - \lambda_{h2}} .$$

$$g_{\text{th/ms}}(\lambda) = \frac{F_{\text{th/ms}}(\lambda_{h1}) - F_{\text{th/ms}}(\lambda_{h2})}{\lambda_{h1} - \lambda_{h2}} .$$

$$g_{\text{th/k2}}(\lambda) = \frac{F_{\text{th/k2}}(\lambda_{h1}) - F_{\text{th/k2}}(\lambda_{h2})}{\lambda_{h1} - \lambda_{h2}} .$$

They are plotted in the upper and middle panels of Fig. 1 with dashed lines.
- The measured spectrum can then be rectified in the two wavelength regions around the H&K lines through:

$$f_{\text{rec}}(\lambda) = \frac{F_{\text{ms}}(\lambda)}{g_{\text{th}}(\lambda)} .$$

resulting in normalized, flux-calibrated spectra in the two wavelength regimes, as displayed as a solid black line in the bottom panel of Fig. 1. Assuming that the theoretical model is adequate, this approach will also correct for imperfect blaze normalization of the measured spectra.

$R_{\text{H/K}}$ is then extracted directly from the rectified spectrum:

$$R_{\text{H/K}} = R_{\text{HK}} - R_{\text{phot}} = \frac{\mathcal{F}_{\text{H}} + \mathcal{F}_{\text{K}}}{\sigma T_{\text{eff}}^4} - \frac{\mathcal{F}_{\text{H}\text{ph}} + \mathcal{F}_{\text{K}\text{ph}}}{\sigma T_{\text{eff}}^4} .$$

$$= \left( \int_{\lambda_{h1}+0.6 \text{Å}}^{\lambda_{h1}+0.6 \text{Å}} f_{\text{rec}}(\lambda) \lambda \lambda \right) \left( \int_{\lambda_{k2}+0.6 \text{Å}}^{\lambda_{k2}+0.6 \text{Å}} f_{\text{rec}}(\lambda) \lambda \lambda \right).$$

The error estimation is performed with a Monte Carlo approach. In each trial, the flux in each bin of the measured spectrum is randomly displaced within a gaussian distribution with width of the flux error, and all stellar parameters are displaced in the same manner according to the error values given by Carmencita. $R_{\text{H/K}}'$ is then evaluated for each trial, and the error $\Delta R_{\text{H/K}}'$ is taken to be the standard deviation of the resulting set.

Figure 1 shows a schematic of the direct determination of $R_{\text{H/K}}'$ for a single HARPS spectrum the M1.5 V star HD 36395. The upper panel displays a PHOENIX synthetic spectrum with similar astrophysical parameters broadened with $v \sin i = 2$ km s$^{-1}$ and the spectral resolution of HARPS ($R = 115000$). From this theoretical spectrum and the measured HARPS spectrum (middle panel), we extracted fluxes in the six different bands listed in Table 2 (shaded red and blue areas in Fig. 1) and, from them, determined the gradient functions $g_{\text{th/hs}}(\lambda)$ (dashed lines in upper and middle panel). The bottom panel of Fig 1 shows the rectified HARPS spectrum, which is in good agreement with the photospheric PHOENIX synthetic spectrum in the areas around the H&K line cores. In order to avoid the extraction of $R_{\text{H/K}}'$ from spectra with insufficient flux in the H&K regime, we required the integrated signal-to-noise ratio of the spectra in the four rectification bands $h_1, h_2, k_1, k_2$ to be $S/N \geq 1.5$. This restriction resulted in a total of 11 634 $R_{\text{H/K}}'$ measurements for 186 targets from the CARMENES GTO sample. Table 2 shows the first 5 rows of the catalog of 11 634 $R_{\text{H/K}}'$ measurements of 186 M dwarfs.

Table 2. Wavelength bands used for rectification and flux extraction.

| Band | Wavelength range $[\lambda_{\text{min}}, \lambda_{\text{max}}]$ |
|------|----------------------------------|
| K    | $[\lambda_K - 0.6 \text{Å}, \lambda_K + 0.6 \text{Å}]$ |
| H    | $[\lambda_H - 0.6 \text{Å}, \lambda_H + 0.6 \text{Å}]$ |
| $k_1$ | $[\lambda_K - 2.5 \text{Å}, \lambda_K - 2.0 \text{Å}]$ |
| $k_2$ | $[\lambda_K + 2.5 \text{Å}, \lambda_K + 3.0 \text{Å}]$ |
| $h_1$ | $[\lambda_H - 1.75 \text{Å}, \lambda_H - 1.25 \text{Å}]$ |
| $h_2$ | $[\lambda_H + 2.0 \text{Å}, \lambda_H + 2.5 \text{Å}]$ |

Notes. Relative to the central wavelengths: $\lambda_K = 3933.66$ Å, $\lambda_H = 3968.47$ Å.
2.2. Sensitivity to uncorrected RV shifts and spectral resolution, and comparison between instruments

Since our algorithm shifts the archival spectra to the stellar rest frame based on the mean radial velocity value listed by Car mencita, and does not account for RV modulations caused by planetary companions or induced by stellar magnetic activity, we tested the stability of the approach with regard to uncorrected RV shifts. Single spectra of three early M dwarfs (V2689 Ori/Karm J05365+113, HO Lib/J15194–077, and Wolf 636/J17052–050) of different activity levels (active, semi-active, quiescent) of similar S/N were shifted by a set of radial velocities $\pm j \times 10^i$ km s$^{-1}$ with $j = 1.9$ and $i = –3.2$ from their catalog rest frame velocity, after which we extracted $R'_{\text{HK}}$. Figure 2 shows the resulting $R'_{\text{HK}}$ normalized by the rest frame index $R'_{\text{HK},0}$ as a function of the velocity offset, $\Delta v$. Since the measurement errors are larger than the deviation caused by velocity offsets $\Delta v \leq 10$ km s$^{-1}$, we concluded that the influence of smaller velocity offsets was negligible and that we did not need to correct for the RV of single spectra.

In a similar manner, we tested whether the artificial broadening with regard to spectral resolution applied in our approach leads to systematic offsets in $R'_{\text{HK}}$, since the model spectra are broadened according to $\mathcal{R}$ and not using the actual line spread function. Figure 3 shows $R'_{\text{HK}}$ as a function of the spectral resolution of the model spectra for two spectra of HD 119850 acquired by the instrument with the lowest resolution in our sample (TIGRE, $\mathcal{R} \approx 20000$) and the highest resolution (HARPS, $\mathcal{R} \approx 115 000$), both normalized by the $R'_{\text{HK},0}$ determined with the respective nominal resolution of the instruments. Both lines converge toward unity around a resolution of 20 000, leading us to conclude that, while the influence of the spectral resolution is negligible for the instruments in this work, the use of spectra with a lower resolution would result in systematic errors.

We checked the validity of the approach by comparing the time-averaged results from different instruments to each other. In order to do this, we evaluated the average $R'_{\text{HK}}$ for each target and for single instruments. Figure A.1 shows the resulting correlations between the subsamples. Apart from a few outliers, all comparisons show a good agreement between data derived from
different instruments. We studied the influence of the deviation from equality between values derived from different instruments, and found that it can stem from activity modulation in the form of cycles and/or flares. However, in order to rule out systematic errors, we study the influence of instrumental effects on the accuracy of our method in the next section.

2.3. Sensitivity to instrumental effects

The spectra from different instruments may be subject to systematic errors caused by effects such as the wavelength-dependent throughput, the spectral energy distribution of the flat-fielding source, and the blaze function correction, all of which can cause fluctuations in the normalization. We therefore checked the stability of our approach with regard to variations in the spectral normalization by multiplying a single HARPS spectrum of Gl 526 (displayed in Fig. 4) with a polynomial of shape

\[ p(\lambda) = a_1 \left( \frac{\lambda - \lambda_0}{\lambda_{\text{char}}} \right) + a_2 \left( \frac{\lambda - \lambda_0}{\lambda_{\text{char}}} \right)^2 + a_3 \left( \frac{\lambda - \lambda_0}{\lambda_{\text{char}}} \right)^3 + a_4 \left( \frac{\lambda - \lambda_0}{\lambda_{\text{char}}} \right)^4 \]  

where \( \lambda \) is the spectral wavelength, \( a_1, a_2, a_3, \) and \( a_4 \) are polynomial coefficients, \( \lambda_0 \) is the central wavelength and \( \lambda_{\text{char}} \) is the characteristic scale of the variability. We repeated the process 10^6 times, randomly selecting polynomial coefficients \( a_{1,2,3,4} \) between \([-1, 1]\), central wavelengths \( \lambda_0 \) between the cores of the \( \text{Ca}\,\text{ii}\) H and K lines and \( \lambda_{\text{char}} \) between 0.5 and 2 times the average length of the single blaze orders of 51 Å (HARPS has an effective wavelength range of 3100 Å and 61 orders). During each try, the relative changes in \( R'_{\text{HK}} \) and the classical \( S \) index (e.g., Mittag et al. 2013; Astudillo-Defru et al. 2017b) were evaluated. As an example, Fig. 4 shows, aside from the original spectrum, three polynomials and the resulting spectra for coefficients \( a_1 = [-1, 0.5, 1], \ a_2 = [1, 0.5, -1], \ a_3 = [0, 1, -1], \ a_4 = [0, -1, 1], \ \lambda_0 = [3951.065 \, \text{Å}, 3968.47 \, \text{Å}, 3933.66 \, \text{Å}] \) and \( \lambda_{\text{char}} = [51 \, \text{Å}, 26 \, \text{Å}, 102 \, \text{Å}] \).

Figure 5 shows the resulting distribution of the relative changes \( \Delta R'_{\text{HK}} \) and \( \Delta S \) of the 10^6 trials, where \( R'_{\text{HK}} \) and \( S \) are the indices extracted from the unperturbed spectrum, and \( \Delta R'_{\text{HK}} \) and \( \Delta S \) are the changes relative to them. The peaks of the distributions are separated by more than two orders of magnitude, indicating that our approach is significantly more accurate. We concluded that this is due to the proximity of the reference bands \( h_1, h_2, k_1, \) and \( k_2 \) to the \( \text{Ca}\,\text{ii}\) H&K line cores. Furthermore, the relative errors caused by normalization systems in our approach are typically of order 10^{-7}, which is far lower than the typical measurement errors caused by photon noise.

3. Results and discussion

3.1. Comparison to previous results

Several authors have published catalogs of chromospheric \( \text{Ca}\,\text{ii}\) H&K emission of M dwarfs with a sufficiently large overlap with our sample to allow for comparison. For example, Astudillo-Defru et al. (2017a) derived \( R'_{\text{HK}} \) of all M dwarfs in the HARPS sample via extraction and conversion of the \( S \) index. Boro Saikia et al. (2018) compiled a catalog of \( R'_{\text{HK}} \) of 4454 late-type stars from published data. Their measurements were based on the same HARPS spectra as Astudillo-Defru et al. (2017a), which are in turn also included in our database.

Figure 6 shows the comparison between our data and those of Boro Saikia et al. (2018) and Astudillo-Defru et al. (2017a). While our average values are in good agreement with Boro Saikia et al. (2018), who also used PHOENIX.
In order to investigate the origin of this discrepancy, we tested the reliability of the flux determination for M dwarfs based on PHOENIX synthetic spectra. In a similar manner as done for the calibration bands in Sect. 2.1, we extracted flux predictions in four filter bands (Johnson B and V and Gaia G_BP, G_RP) from the theoretical spectra. Since the magnitudes in these bands have been measured for the majority of the CARMENES GTO sample (Cifuentes et al. 2020), we were then able to compare the measured colors G_BP − G_RP and B − V to the theoretical predictions, as displayed in Fig. 7. As evident in both colors, the PHOENIX synthetic spectra seem to overestimate the flux in the blue end of the spectrum for the latest M dwarfs.

If true, it explains why we obtained a good agreement with the \( R'_{\text{HK}} \) values published by Boro Saikia et al. (2018) and a systematic offset compared to those determined by Astudillo-Defru et al. (2017a). It also means that any comparison between the activity levels of stars with different parameters will be prone to systematic errors, which is why we did not include the analysis of averaged activity levels of the single targets, for instance, for the derivation of rotation-activity relations, in this publication. However, this overestimation does not affect the ability of our method to determine activity time series for individual stars based on data from multiple instruments.

3.2. Time series

We give below an example of the advantage of activity catalogs derived from multiple instruments. The Mount Wilson Observatory HK project (e.g., Baliunas et al. 1995), which provides archival \( S \) index time series for thousands of stars covering decades, did not include the M dwarf range. However, the rise of projects searching for substellar companions to cool dwarfs has resulted in long time series of spectra for M dwarfs, provided the individual data sets are combined.

We present the time series and periodograms of three stars with previously unknown long-term variations in \( R'_{\text{HK}} \), suggesting the presence of an activity cycle, in Fig. 8. To estimate the period of this long-term variability, we used the common generalized Lomb-Scargle (GLS) method described by Zechmeister & Kürster (2009), along with their approach to estimate the false alarm probability (FAP). Table 4 lists the resulting periodicities and names of the three stars. Since the peaks of all cycles exhibit an FAP smaller than 0.1 % and are, thus, significant, we used a sinusoidal model with amplitude \( A \), cycle period \( P_{\text{cycle}} \), offset \( R_{\text{HK,0}} \), and a jitter term \( \sigma_{\text{Jitter}} \) to evaluate the statistical significance of the cyclic variability of the shape. The fitted periods, listed in Table 4, agree well with those derived via GLS. We computed the log-likelihood \( \mathcal{L} \) via:

\[
\ln \mathcal{L} = -\frac{1}{2} \sum_{i} \ln \left( 2\pi \sigma_i^2 + \sigma_{\text{Jitter}}^2 \right) + \frac{\left( R'_{\text{HK,obs},i} - R'_{\text{HK,mod},i} \right)^2}{\sigma_i^2 + \sigma_{\text{Jitter}}^2}.
\]

The best-fit parameters are listed in the bottom panel of Table 4.

We also implemented a second model that included time-correlated noise following the approach of Haywood et al. (2014), thus testing whether the fit quality improves when accounting for rotational variability. While the derived cycle periods agreed with the GLS analysis and the sinusoidal model, and the log-likelihood difference \( \Delta \ln \mathcal{L} \) increased only slightly compared to the model without red noise, the error estimates did increase significantly, which led us to conclude that such an approach did not constitute a better model.

Two of the three stars had a previous determination of the rotation period, \( P_{\text{rot}} \) (see Table 4), which are much shorter than the \( P_{\text{cycle}} \) that we derive. Astudillo-Defru et al. (2017b) reported a possible \( \sim 2000\text{d} \) activity cycle of Luyten’s Star/Karmn J07274+052, which we identified as an alias of the cycle period in Table 4.

4. Summary

We compiled a library of archival spectra of 186 M dwarfs from the CARMENES GTO sample with sufficiently high S/N acquired by seven high-resolution spectrographs covering the \( \text{Ca}^{+} \)H&K lines. By applying a variant of the spectral subtraction technique and using a set of narrow spectral bands around the doublt line, we rectified the observed spectra and normalized them based on theoretical PHOENIX model spectra, which enabled us to extract the fluxes in the H&K lines and, thus, \( R'_{\text{HK}} \) in a uniform manner. This method was shown to be stable.
with regard to small deviations in radial velocity, and to produce consistent results for data from different instruments. We also determined that our method is stable with regard to instrumental effects by randomly varying a spectrum with a polynomial. A comparison to the classical $S$ index revealed that our approach is significantly more accurate with respect to instrumental variability.

The aim of this catalog is to provide the basis for further analysis of the $R'_{HK}$ time series of single targets. We demonstrate that the use of a variety of instruments can yield long time series allowing for the discovery of activity cycles. The detailed derivation of rotation periods and activity cycles of all individual targets is beyond the scope of this paper.

We compared our results to the $R'_{HK}$ values published by Boro Saikia et al. (2018), who used a similar technique to that employed here, and those derived by Astudillo-Defru et al. (2017b), who converted the “classical” $S$ index into $R'_{HK}$. The latter comparison revealed a systematic offset toward low activity levels, the origin of which we determined to be the systematic underestimation of flux in PHOENIX spectra toward the blue end of the spectrum. While this underestimation prevented us from carrying out a comparison of activity levels of stars with different effective temperatures, it did not influence the purpose of the catalog, namely the creation of long time series of $R'_{HK}$ for the CARMENES GTO M dwarfs for the determination of rotation periods and other variability.

The catalog is continuously updated when new data become available. Since the approach of using a set of theoretical spectra in conjunction with narrow passbands to rectify and normalize the measured spectrum was proven to be stable, it may be worthwhile to apply it to other chromospheric activity indicators.

Acknowledgements. We thank the anonymous referee for the valuable input. We acknowledge financial support from the Agencia Estatal de Investigación of the Ministerio de Ciencia, Innovación y Universidades and the ERDF through projects PID2019-109522GB-C21 (AEI/10.13039/501100011033) and the Centre of Excellence “Severo Ochoa” and “María de Maeztu” awards to the Instituto de Astrofísica de Canarias (CEX2019-000920-S), Instituto de Astrofísica de Andalucía (SEV-2017-0737), and the Generalitat de Catalunya/CERCA programme. Based on observations obtained at the Canada-France-Hawaii Telescope (CFHT), which is operated by the National Research Council of Canada, the Institut National des Sciences de l’Univers of the Centre National de la Recherche Scientifique of France, and the University of Hawaii. Based on observations made with ESO Telescopes at the La Silla Paranal Observatory under programme IDs 0100.C-0097(A), 0101.C-0516(A), 0101.D-0494(A), 0102.C-0558(A), 0102.D-0483(A), 0103.A-9009(A), 072.C-9006(A), 072.C-0488(E), 072.D-0621(A), 073.D-0038(B), 074.B-0639(A), 074.C-0364(A), 074.D-0016(A), 075.D-0614(A), 076.A-9005(A), 076.A-9013(A), 076.C-0155(A), 076.D-0560(A), 077.A-9005(A), 077.C-0364(E), 078.A-9058(A), 078.A-9059(A), 078.C-0044(A), 078.C-0333(A), 078.D-0071(D), 079.A-9007(A), 079.A-9013(B), 079.C-0255(A), 080.D-0086(C), 080.D-0086(D), 080.D-0140(A), 081.A-9055(A), 081.A-9024(A), 081.C-0218(A), 082.C-0718(A), 082.C-0718(B), 082.D-0953(A), 084.C-0403(A), 085.A-9027(A), 085.C-0019(A), 086.A-9014(A), 087.C-0831(A), 087.C-0991(A), 087.D-0069(A), 088.A-9032(A), 088.C-0662(B), 089.A-9007(D), 089.A-9008(A), 089.C-0440(A), 089.C-0497(A), 089.C-0732(A), 090.A-9003(A), 090.A-9010(A), 090.A-9029(A), 090.C-0200(A), 090.C-0395(A), 091.A-9004(A), 091.A-9012(A), 091.A-9032(A), 091.C-0034(A), 091.C-0216(A), 091.D-0296(A), 092.A-9009(A), 092.C-0203(A), 093.A-9001(A), 093.C-9029(A), 093.C-0343(A), 093.C-0409(A), 094.A-9029(A), 094.D-0596(A), 095.C-0551(A), 095.C-0718(A), 095.D-0658(A), 096.C-0499(A), 097.C-0561(A), 097.C-0561(B), 097.C-0624(A), 097.C-0864(B), 098.C-0518(A), 098.C-0739(A), 099.C-0205(A), 099.C-0880(A), 1102.C-0323(A), 180.C-0886(A), 183.C-0437(A), 183.C-0972(A), 191.C-0505(A), 191.C-0873(A), 191.C-0873(B), 191.C-0873(D), 191.C-0873(E), 191.C-0873(F), 192.C-0224(A), 192.C-0224(C), 192.C-0224(G), 192.C-0852(A), 192.C-0852(M), 198.C-0838(A), 276.C-0354(A), 60.A-9036(A), 60.A-9709(G), 69.D-0092(A), and 69.D-0478(A). This research has made use of the Keck Observatory Archive (KOA), which is operated by the W. M.
Appendix A: Comparison of $R'_{HK}$ values from different instruments

**Fig. A.1.** Comparison of mean $R'_{HK}$ derived from individual instruments. The x-axis shows the $R'_{HK}$ of the instruments denoted by the labels under each subplot, while the y-axis is the fraction between $R'_{HK}$ of the instruments denoted on the y-axis and those denoted on the x-axis.