From superradiance to subradiance: exploring the many-body Dicke ladder

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We report a time-resolved study of collective emission in dense ensembles of two-level atoms. We compare, on the same sample, the build-up of superradiance and subradiance from the ensemble when driven by a strong laser. This allows us to measure the dynamics of the population of superradiant and subradiant states as a function of time. In particular we demonstrate the build up in time of subradiant states through the superradiant dynamics. This illustrates the dynamics of the many-body density matrix of superradiant ensembles of two-level atoms when departing from the ideal conditions of Dicke superradiance in which symmetry forbids the population of subradiant states.

Collective spontaneous emission of light by atomic ensembles has seen a renewed interest lately in the context of quantum technologies. Superradiance, i.e. the emission of light at a rate enhanced with respect to the single atom case, was observed in many experiments [1, 2]. Recently, it was studied with cold atoms [3, 4], both in dilute clouds [5–7] and dense ensembles [8], also with atoms in cavity [9] or trapped near waveguides and fibers [10–12]. Its counterpart, subradiance, associated to a slow collective emission, has proven more challenging to observe [13, 14]. It has been demonstrated only in a handful of experiments using dilute [7, 15, 16] and dense [17, 18] clouds of randomly distributed cold atoms. Here we address the question as to how superradiant and subradiant collective states are populated and evolve in laser-driven ensembles of two-level atoms.

In Dicke’s original proposal [19], superradiance originates from an ensemble of $N$ two-level atoms (states $|g\rangle$ and $|e\rangle$), placed in a volume small with respect to the transition wavelength and all initially inverted [20]. In this scenario, only permutationally-symmetric superradiant states are populated during the decay. Contrarily, anti-symmetric subradiant states are never populated. Moreover, these subradiant states are strictly uncoupled even to an external drive, preventing the observation of subradiance. Experimental samples, however, depart from the symmetric conditions of the Dicke proposal, due to (i) the finite (or large) sample size and (ii) the random positions of the atoms that leads to spatially varying dipole-dipole interactions (the so-called van der Waals dephasing in [20]). When sorted by the number $n$ of atoms in $|e\rangle$, the full set of states realizes a ladder, with the resonant dipole-dipole interaction coupling the bare states inside a manifold corresponding to a given $n$ (see Fig. 1a). Further, this breaking of symmetry makes it possible for symmetric states that, in the Dicke case, would lead only to a superradiant cascade to now decay towards subradiant ones. When all these $2^n$ states have to be considered, calculating the dynamics of the population of superradiant and subradiant states, following a population inversion or when driving the transition, is extremely challenging for large systems [8, 16].

To understand the conditions for the appearance of super- and subradiance and how the corresponding states are populated, we here perform experiments observing both phenomena on the same sample. This is a dense, cigar-shaped cloud of two-level atoms with radial size smaller than the wavelength of their transition and axial size of a few wavelengths, as in [8, 17]. By applying a global resonant excitation laser on the $g - e$ transition, and performing time-resolved fluorescence measurements during and after the excitation, we characterize both the superradiant and subradiant states in the same sample: we either nearly completely invert the system, or resolve the full dynamics during a long excitation pulse. We show that direct driving does populate subradiant states due to symmetry breaking, and that a long excitation pulse populates slowly the subradiant manifold, in a process akin to optical pumping [16], while superradiance is weakened.

Our setup, described in [21, 22], operates an optical tweezers containing $N \simeq 4500 ^{87}$Rb at a temperature of 650µK. The cloud’s dimensions are $\sigma_{ax} = 15\lambda_0$ and $\sigma_{rad} = 0.5\lambda_0$, where $\lambda_0 = 780.2$ nm is the wavelength of the D2 line ($\Gamma_0 \simeq 2\pi \times 6$ MHz, $I_{sat} = 1.67$mW/cm$^2$). We isolate two Zeeman sub-levels with a 50G magnetic field perpendicular to the cloud’s axis [8]. The atoms are optically pumped in $|g\rangle = |S_{1/2}, F = 2, m_F = -2\rangle$ and are then excited perpendicularly to the cloud’s axis (along the direction of the magnetic field), after being released from the trap, [23], by a $\sigma$-polarized light resonant with $|e\rangle = |P_{3/2}, F = 3, m'_F = -3\rangle$. The excitation beam size is much larger than the atomic cloud. The intensity is $s = I/I_{sat} \simeq 75$ (Rabi frequency $\Omega \simeq 6.5\Gamma_0$), with $\sim 10\%$ shot-to-shot fluctuations. The temporal shape of the excitation is controlled with a fibered electro-optical modulator with rising and falling times shorter than 1 ns, combined with two acousto-optical modulators to suppress residual light. The fluorescence emitted by the atoms along the cloud’s axis is fiber-coupled to an avalanche photodiode operating in the single photon counting mode.

In order to investigate the influence of the initial atomic states on the collective decay, we tune the duration of the driving pulse, exploiting the Rabi oscillations induced by the driving. If the pulse duration is small with respect to the spontaneous emission decay (occurring on a timescale $1/\Gamma_0$) the system is approximatively prepared in a coherent superposition $(\cos(\Omega t)|g_n\rangle + i e^{i\Delta \Omega t} R_{k_{bias}} \sin(\Omega t)|e_n\rangle)^{\otimes n}$. In the Dicke limit, $R_{k_{bias}} R_{\sigma} \approx 0$, and this initial state is coupled only to superradiant states since it is invariant under the exchange of two
FIG. 1. **Dynamics of super- and subradiant many-body states.** a) Representation of the “Dicke ladder” for our two-level ensembles. The superradiant states (highlighted in red) drive the cascade. The departure from ideal Dicke symmetries induces (i) a possibility for direct laser driving of the subradiant states (green) and (ii) a decay from superradiant states towards subradiant ones. c) and d) [resp. e) and f)] show the dynamics under driving of the superradiant (resp. subradiant) lifetime and photon count, extracted from the early (resp. late) decay with timescales shown in b), see main text for details.

atoms. Conversely, for pulse durations long with respect to the decay and \( \Omega \gg \Gamma_0 \), the population reaches steady-state and the resulting density matrix is \( \hat{\rho}_n = (|e_n\rangle \langle e_n| + |g_n\rangle \langle g_n|)^{\otimes n}/2^n \) in which super and subradiant states are equally populated [16, 24]. As we have recently shown [8], the axial emission during Rabi oscillations is enhanced by superradiance. However the evolution of the population of the excited state for the large Rabi frequency used here is only weakly modified and follows well the single atom behavior described by the optical Bloch equations (OBEs). By collecting the fluorescence emitted perpendicularly to the cloud’s axis (not enhanced by superradiance) we are able to measure the evolution of the excited state fraction \( n_e \) [8]. This evolution is also recovered when measuring the axial fluorescence at very low atom number where superradiance does not take place.

To investigate the super and subradiant decay of our sample, we record the photon counts during a 1 ns time bin, detected after having switched the excitation light off (at \( t_0 \)) and separate the analysis in different time windows [see Fig. 1 b)]. At short time, superradiance dominates and we extract the associated decay time \( \tau_{\text{super}} \) by an exponential fit in the first \( 1/\Gamma_0 \approx 26 \text{ ns}. \) We exclude the first 5 ns from the fit to start it after the superradiant pulse occurring shortly after \( t_0 \), when close to the total population inversion [8]. We also record the total number of photons \( N_{\text{super}} \) during the first 26 ns. This count provides an indication of the population stored in superradiant states, which emit faster than the single atom lifetime. The results for \( \tau_{\text{super}} \) and \( N_{\text{super}} \) are reported in Fig. 1c),d) as a function of the duration of the excitation pulse. Both quantities oscillate at the same frequency, given by the Rabi frequency \( \Omega = \sqrt{\sigma} \). The excited state fraction \( n_e \), measured for low atom number, is reported as a reference in each panel of Fig. 1. The population of superradiant states oscillates in phase with respect to \( n_e(t) \), as expected, while \( \tau_{\text{super}} \) oscillates in quadrature (i.e. the emission rate \( \Gamma_{\text{super}} = 1/\tau_{\text{super}} \) oscillates in phase as expected).

This observation is a confirmation that population inversion is the main drive for Dicke superradiance. But to deepen the analysis, we plot in Fig. 2 the measured superradiant decay time and photon count, now as a function of the measured excited state population \( n_e \). Strikingly, the data do not collapse on a single curve: for a given excited state fraction \( n_e \), very different decay times and photon counts are observed. This stems from the fact that superradiance arises not only from population inversion, but also from the emergence of in-phase correlations between atoms, of the form \( e^{i\hat{k}_n(R_n-R_0)}\langle \hat{a}_m^+\hat{a}_n^- \rangle(t) \) where and \( \hat{a}_n^+(-) \) is the raising (lowering) operator for the state of atom \( n \) with position \( R_n \), and \( \hat{k}_n \) is the wavevector of the light emitted along the cloud axis.
The superradiant states in our system are the ones for which these correlations are sizeable [8]. When the population is inverted, these correlations first grow in time before decaying via a superradiant cascade [8]. Thus depending at which stage of the collective Rabi cascade one measures the decay, a different dynamics unfolds. When we stop at $t_0$ the driving early in a Rabi cycle (say $\pi/2$ time for which $n_e = 1/2$), the correlations have not had time to grow before $t_0$ and we observe a low photoemission rate and relatively slow final decay for $t \geq t_0$. On the other hand when we stop the driving at the end of a Rabi flop ($3\pi/2$, again with $n_e = 1/2$) these correlations have had time to grow before $t_0$, so that a higher photoemission and faster decay is observed after $t_0$. This explains why at the same excited state fraction ($n_e = 1/2$), different decay times and superradiant population can be observed.

Having probed the dynamics of superradiant states, we now move to the study of the subradiant decay occurring at later times after switching off the drive. For the same experimental data as above, we measure the decay time $\tau_{\text{sub}}$ using an exponential fit for $t \geq t_0 + 4/\Gamma$ [see Fig. 1b)]. We now sum the photons recorded after $t_0 + 4/\Gamma$. This count $N_{\text{sub}}$ is related to the population of the long-lived states. The results are reported in Fig. 1e,f). This decay time $\tau_{\text{sub}}$ is nearly independent of the duration of the driving as the late decay mostly involve subradiant states with similar decay times [17]. Next, contrarily to superradiance, we observe that the number of photons in the subradiant tail increases nearly monotonically with time during the Rabi oscillations, saturating when the system reaches steady state. Importantly, after a single Rabi cycle (at $t = 25$ ns), the population of the subradiant states has already grown. This shows that, going through one cycle of Rabi oscillations (including through superradiant states) does lead to the population of subradiant states, due both to the decay towards subradiant states [25] and a direct driving from the ground state. This reveals the existence of a finite coupling between super and subradiant states due to the fact that, in our regime, the symmetry hypotheses on which Dicke’s model is based are not satisfied. However, the subradiant population has not reached its maximum value in a single cycle. Several such cycles are necessary to reach the maximum population of subradiant states. These measurements thus amount to a time-resolved observation of an effective optical pumping mechanism towards subradiant states through cycles in superradiant ones as suggested in [16] for dilute clouds.

To gain intuition on the observations reported above, we have solved the master equation [26] for $N = 2$ interacting dipoles placed at an interatomic distance $\lambda/3$, that is the mean nearest neighbour distance in our experiment. The dipole-dipole interaction in the numerics is thus similar to the one of the experiment. For different times during the driving, we evaluate the excited state fraction $n_e$, and that of the subradiant state $\langle |−| \rho(t) − \rangle \langle −| = \frac{1}{\sqrt{2}} (\langle ee \rangle ± \langle ge \rangle )$. To partially account for the randomness of the atomic spatial distribution, the simulations averaged over 1000 realizations, each obtained by changing the angle between the interatomic axis and the quantization axis, at a fixed interatomic distance.

We report in Fig. 3a) the results of the simulation for an excitation pulse of 150 ns. They reproduce remarkably well the qualitative behavior observed in the experiment: while the excited state fraction $n_e$ oscillates, the population of the subradiant state is built through a different dynamics that involve both direct excitation and decay from the doubly excited state $|ee\rangle$. To highlight this, we report in Fig. 3b) the results of the simulations with a $\pi$-pulse where the population of $|ee\rangle$ is maximized: after the end of the driving, the population of subradiant state increases indicating that the symmetric state $|ee\rangle$ decays in part towards $|−\rangle$. Depending on the relative orientation between the laser propagation axis and the interatomic axis, a direct excitation of $|−\rangle$ from the ground state is also possible, leading to a different dynamics for different orientations. Our observations above indicate that both mechanisms take place in our many-body experiments.

To conclude, we have explored the dynamics of super and subradiant modes hosted in the same atomic cloud of two-levels emitters close to the Dicke limit. By changing the duration of the excitation pulse, we prepare the system in different many-body density matrices, studying how super and subradiant states are populated during the driving and their interplay during the decay. We find that although superradiance is mainly governed by the excited state fraction, different correlations, that grow during the drive lead to very different superradiant decays. We resolved in time how subradiant modes are
FIG. 3. Simulation of the driving and decay of two atoms. a) Excited state fraction (red) and population (green) of the subradiant state $|\rangle$ during driving, for many different interatomic axis orientations (thin lines), and average (solid line). b) Same, but with driving switched-off at the $\pi$-pulse time. This allows to see initial direct driving of the population in $|\rangle$ and then an increase in population due to decay from the doubly excited state $|ee\rangle$. The four states of the 2-atom system are shown as an inset in b).

populated via both a direct coupling and an optical-pumping-like mechanism through the Dicke ladder. Elucidating the correlation growth dynamics will be key to exploring the phase diagram of ordered superradiant ensembles [27–30]. Furthermore, future experimental studies should aim at measuring the predicted growth of entanglement associated to subradiance, e.g. by measuring intensity correlation of the fluorescence [24].

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[1] N. Skribanowitz, I. P. Herman, J. C. MacGillivray, and M. S. Feld, Observation of dicke superradiance in optically pumped hf gas, Phys. Rev. Lett. 30, 309 (1973).
[2] M. Gross, C. Fabre, P. Pillet, and S. Haroche, Observation of near-infrared dicke superradiance on cascading transitions in atomic sodium, Phys. Rev. Lett. 36, 1035 (1976).
[3] T. Wang, S. F. Yelin, R. Côté, E. E. Eyler, S. M. Farooqi, P. L. Gould, M. Koštun, D. Tong, and D. Vinceaux, Superradiance in ultracold rydberg gases, Phys. Rev. A 75, 033802 (2007).
[4] E. Paradis, B. Barrett, A. Kumarakrishnan, R. Zhang, and G. Raithel, Observation of superfluorescent emissions from laser-cooled atoms, Phys. Rev. A 77, 043419 (2008).
[5] M. O. Araújo, I. Krešić, R. Kaiser, and W. Guerin, Superradiance in a large and dilute cloud of cold atoms in the linear-optics regime, Phys. Rev. Lett. 117, 073002 (2016).
[6] S. J. Roof, K. J. Kemp, M. D. Havey, and I. M. Sokolov, Observation of single-photon superradiance and the cooperative lamb shift in an extended sample of cold atoms, Phys. Rev. Lett. 117, 073003 (2016).
[7] D. Das, B. Lemberger, and D. D. Yavuz, Subradiance and superradiance-to-subradiance transition in dilute atomic clouds, Phys. Rev. A 102, 043708 (2020).
[8] G. Ferioli, A. Glicenstein, F. Robicheaux, R. T. Sutherland, A. Browaeys, and I. Ferrier-Barbut, Laser-driven superradiant ensembles of two-level atoms near dicke regime, Phys. Rev. Lett. 127, 243602 (2021).
[9] M. A. Norcia, M. N. Winchester, J. R. K. Cline, and J. K. Thompson, Superradiance on the millihertz linewidth strontium clock transition, Science Advances 2, 10.1126/sciadv.1601231 (2016), https://advances.sciencemag.org/content/2/10/e1601231.full.pdf.
[10] A. Goban, C.-L. Hung, J. D. Hood, S.-P. Yu, J. A. Muniz, O. Painter, and H. J. Kimble, Superradiance for atoms trapped along a photonic crystal waveguide, Phys. Rev. Lett. 115, 063601 (2015).
[11] P. Solano, P. Barberis-Blostein, F. K. Fatemi, L. A. Orozco, and S. L. Rolston, Super-radiance reveals infinite-range dipole interactions through a nanofiber, Nature Communications 8, 1857 (2017).
[12] R. Pennetta, M. Blaha, A. Johnson, D. Lechner, P. Schneeweiss, J. Volz, and A. Rauschenbeutel, Collective radiative dynamics of an ensemble of cold atoms coupled to an optical waveguide (2021), arXiv:2109.00860 [quant-ph].
[13] R. G. DeVoe and R. G. Brewer, Observation of superradiant and subradiant spontaneous emission of two trapped ions, Phys. Rev. Lett. 76, 2049 (1996).
[14] B. H. McGuyer, M. McDonald, G. Z. Iwata, M. G. Tarallo, W. Skomorowski, R. Moszynski, and T. Zelevinsky, Precise study of asymptotic physics with subradiant ultracold molecules, Nature Physics 11, 32 (2015).
[15] W. Guerin, M. O. Araújo, and R. Kaiser, Subradiance in a large cloud of cold atoms, Phys. Rev. Lett. 116, 083601 (2016).
[16] A. Cipris, N. A. Moreira, T. S. do Espirito Santo, P. Weiss, C. J. Villas-Boas, R. Kaiser, W. Guerin, and R. Bachelard, Subradiance with saturated atoms: Population enhancement of the long-lived states, Phys. Rev. Lett. 126, 103604 (2021).
[17] G. Ferioli, A. Glicenstein, L. Henriet, I. Ferrier-Barbut, and A. Browaeys, Storage and release of subradiant excitations in a dense atomic cloud, Phys. Rev. X 11, 021031 (2021).
[18] N. Stiesdal, H. Busche, J. Kumlin, K. Kleinbeck, H. P. Büchler, and S. Hofferberth, Observation of collective decay dynamics of a single rydberg superatom, Phys. Rev. Research 2, 043339.
[19] R. H. Dicke, Coherence in spontaneous radiation processes, Phys. Rev. 93, 99 (1954).
[20] M. Gross and S. Haroche, Superradiance: An essay on the theory of collective spontaneous emission, Physics Reports 93, 301 (1982).
[21] A. Glicenstein, G. Ferioli, L. Brossard, Y. R. P. Sortais, D. Barredo, F. Nogrette, I. Ferrier-Barbut, and A. Browaeys, Preparation of one-dimensional chains and dense cold atomic clouds with a high numerical aperture four-lens system, Physical Review A 103, 43301 (2021).
[22] A. Glicenstein, G. Ferioli, N. Šibalić, L. Brossard, I. Ferrier-Barbut, and A. Browaeys, Collective shift in resonant light scattering by a one-dimensional atomic chain, Phys. Rev. Lett. 124, 253602 (2020).
[23] The largest duration of the pulse we used is 150ns and the typical thermal velocity is \( v_{th} \approx 0.25 \text{m/s} \). The thermal expansion during the driving is \( \approx 0.05 \lambda_0 \) and thus the atoms can be considered as frozen.
[24] A. C. Santos, A. Cidrim, C. J. Villas-Boas, R. Kaiser, and R. Bachelard, Generating long-lived entangled states with free-space collective spontaneous emission (2021), arXiv:2110.15033 [quant-ph].
[25] S. J. Masson, I. Ferrier-Barbut, L. A. Orozco, A. Browaeys, and A. Asenjo-Garcia, Many-body signatures of collective decay in atomic chains, Phys. Rev. Lett. 125, 263601 (2020).
[26] A. Asenjo-Garcia, M. Moreno-Cardoner, A. Albrecht, H. J. Kimble, and D. E. Chang, Exponential improvement in photon storage fidelities using subradiance and “selective radiance” in atomic arrays, Phys. Rev. X 7, 031024 (2017).
[27] B. Olmos, D. Yu, and I. Lesanovsky, Steady-state properties of a driven atomic ensemble with nonlocal dissipation, Phys. Rev. A 89, 023616 (2014).
[28] C. D. Parmee and N. R. Cooper, Phases of driven two-level systems with nonlocal dissipation, Phys. Rev. A 97, 053616 (2018).
[29] C. D. Parmee and J. Ruostekoski, Signatures of optical phase transitions in superradiant and subradiant atomic arrays, Communications Physics 3, 205 (2020), 2007.03473.
[30] R. J. Lewis-Swan, S. R. Muleady, D. Barberena, J. J. Bollinger, and A. M. Rey, Characterizing the dynamical phase diagram of the dicke model via classical and quantum probes, Phys. Rev. Research 3, L022020 (2021).