Search for Excited and Exotic Muons in the $\mu\gamma$ Decay Channel in $p\bar{p}$ Collisions at $\sqrt{s}=1.96$ TeV

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We present a search for excited and exotic muon states $\mu^*$, conducted using an integrated luminosity of 371 pb$^{-1}$ of data collected in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV at the Tevatron with the CDF II detector. We search for associated production of $\mu\mu^*$ followed by the decay $\mu^* \rightarrow \mu\gamma$, resulting in the $\mu\mu\gamma$ final state. We compare the data to model predictions as a function of the mass of the excited muon $M_{\mu^*}$, the compositeness energy scale $\Lambda$, and the gauge coupling factor $f$. No signal above the standard model expectation is observed in the $\mu\gamma$ mass spectrum. In the contact interaction model, we exclude $10^7 < M_{\mu^*} < 853$ GeV/$c^2$ for $\Lambda = M_{\mu^*}$; in the gauge-mediated model, we exclude $100 < M_{\mu^*} < 410$ GeV/$c^2$ for $f/\Lambda = 10^{-2}$ GeV$^{-1}$. These 95% confidence level exclusions extend previous limits and are the first hadron collider results on $\mu^*$ production in the gauge-mediated model.

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In the standard model (SM) the quarks and leptons are treated as fundamental particles. Their generational structure and observed mass hierarchy motivate a model of composite quarks and leptons consisting of fewer elementary particles than contained in the SM. In this model, quarks and leptons are the lowest-energy bound...
states of these hypothetical particles, and additional excited states exist near the compositeness energy scale $\Lambda$. Exotic fermions are also predicted in the context of grand unified or string theories, in which the known forces are unified into a larger symmetry group $G$. In such models, additional fermions are predicted with properties similar to those of excited fermions.

At a $p\overline{p}$ collider, excited or exotic muon states could be observed through the reaction $q\overline{q} \rightarrow \mu^*\mu$. Excited muon production can be described using a contact interaction (CI) Lagrangian density $L$:

$$L = \frac{1}{2\Lambda} \bar{M}_R \gamma^\mu q_L \gamma^\mu \mu_L + h.c.,$$

where $M_L$ represents the left-handed $\mu^*$ field. For exotic muon production, the relevant gauge-mediated (GM) Lagrangian density is $L$:

$$L = \frac{1}{2\Lambda} \bar{M}_R \sigma^{\mu\nu} \left[ f g f' \cdot \bar{W}_{\mu\nu} + f' g Y \frac{2}{2} B_{\mu\nu} \right] \mu_L + h.c.,$$

where $W$ and $B$ are the $SU(2)_L$ and $U(1)_Y$ field strengths, $g$ and $g'$ are the respective electroweak couplings, and $f$ and $f'$ are phenomenological constants which are set equal to each other by convention to maximize the photonic decay branching ratio. For $f = f' (f = -f')$, the relative $\mu^*$ branching ratios are $BR(\mu^* \rightarrow \mu\gamma) = 0.3 \ (0)$, $BR(\mu^* \rightarrow eW) \approx 0.6 \ (0.6)$, and $BR(\mu^* \rightarrow \mu Z) \approx 0.1$ for $M_{\mu^*} > 200$ GeV/$c^2$. The $BR(\mu^* \rightarrow \mu\gamma)$ increases to 70% at $M_{\mu^*} = 100$ GeV/$c^2$ for $f = f'$. We use these branching ratios for both the GM and CI production models $R$.

In this Letter we describe a search for associated $\mu\mu^*$ production that extends existing $\mu^*$ mass limits. Prior searches for $\mu^*$ production have been performed by the LEP experiments, which have excluded $M_{\mu^*} < 200$ GeV/$c^2$ for $f/\Lambda > 10^{-2}$ GeV$^{-1}$ in the GM model $S$. The DØ experiment has excluded $M_{\mu^*} < 688$ GeV/$c^2$ for $\Lambda = M_{\mu^*}$ in a particular CI model $S$.

We use 371 pb$^{-1}$ of data collected with the CDF II detector at the Fermilab Tevatron. The detector has been described in detail elsewhere $R$. Its magnetic spectrometer consists of silicon microstrip and drift chamber $T$, tracking detectors. Surrounding this are central $R$ ($|\eta| < 1$) and forward $T$ ($|\eta| > 1.1$) electromagnetic (EM) and hadronic calorimeters. Embedded in the central EM calorimeter are wire and strip chambers $R$ (used to measure the transverse shower profiles of photons) and a central preshower detector $R$ (used for detecting photon conversions). Outside the calorimeters are CMUP ($|\eta| < 0.6$) and CMX (0.6 < $|\eta| < 1$) muon detectors $T$. The momentum resolution of beam-constrained drift-chamber tracks is $\Delta p_T/p_T \approx 0.05\%$/GeV/$c$. The electromagnetic energy resolution for the high-energy photons typical of $\mu^*$ decays is approximately 2.5%.

We analyze events passing the readout trigger requirement of one drift-chamber track with $p_T > 18$ GeV/$c$ $R$, matched to a reconstructed track segment in the muon chambers. In the offline analysis, we require two muon candidates identified by drift-chamber tracks with $p_T > 20$ GeV/$c$ and $|\eta| < 1$, which pass requirements on impact parameter and number of hits, have minimum-ionizing particle properties, and at least one of which has a matching muon chamber segment $T$. Both tracks must pass the calorimeter isolation requirement $I < 0.1$, where $I$ is the ratio of the combined EM and hadronic calorimeter $E_T$ surrounding the track in a cone of radius $R = \sqrt{(\Delta\eta)^2 + (\Delta\phi)^2} < 0.4$ $R$ to the track $p_T$. In addition, both tracks must also pass the tracking isolation requirement $T < 0.1$, where $T$ is the ratio of the summed $p_T$ of tracks to the muon $p_T$, where the sum is taken over tracks in a cone of radius $R < 0.4$ around the muon direction. Finally, we reject cosmic rays based on tracking and track-timing information $S$.

We select dimuon events that have a central or forward photon candidate with $E_T > 25$ GeV, $|\eta| < 2.8$, and $I < 0.1$, where calorimeter isolation is now defined relative to the photon. The photon energy is defined as the EM calorimeter energy in a 0.2 × 0.25 $\eta$ -- $\phi$ region, and its transverse component is determined by the vertex of the highest momentum muon with a matching muon chamber segment. Photon candidates are identified on the basis of their longitudinal and transverse calorimeter shower profiles. Central photon candidates require the sum $p_T$ of charged particles within a cone of radius $R < 0.4$ around the photon direction to be less than 5 GeV + 0.005 × $E_T^\gamma$, where $E_T^\gamma$ is the $E_T$ of the photon, and no single charged particle within $R < 0.4$ to have $p_T > 10$ GeV/$c$. To suppress the initial-state radiation (ISR) $Z(\rightarrow \mu\mu)\gamma$ background, we reject events with dimuon invariant mass $m_{\mu\mu}$ in the range 81 -- 101 GeV/$c^2$.

A $Z \rightarrow \mu\mu$ sample is used to measure the efficiencies of the muon identification criteria and trigger. The efficiency of the calorimeter and tracking identification requirements is measured to be (92.6 ± 0.3stat)$\%$. We measure the combined trigger and muon chamber matching efficiency to be (79.3 ± 1.0stat)$\%$ for the CMUP and (95.0 ± 0.6stat)$\%$ for the CMX.

The photon identification efficiency is extracted from a GEANT-based detector simulation $T$. Since the electromagnetic showers of electrons are similar to those of photons, we validate the simulated photon efficiency using a control sample of electrons from $Z \rightarrow ee$ events. The events are triggered and identified using one electron; the second electron is used to emulate the photon to determine the cut efficiencies for photons. In the central calorimeter, the emulated photon efficiency is (79.0 ± 0.5stat)$\%$ in the data and (77.0 ± 0.6stat)$\%$ in the simulation. The corresponding values in the forward calorimeter are (89.0 ± 0.6stat)$\%$ in the data and (89.6 ± 0.6stat)$\%$ in the simulation. These comparisons show that photon detection is well-modeled by the simul-
lation; the statistically significant differences are included in the systematic uncertainty.

The geometric acceptance and detector response are calculated with the GEANT detector simulation separately for the CI and GM models. We use the PYTHIA [15] generator for the CI model and the LAMHEP [16] and COMHEP [17] programs to generate GM model events. The total signal acceptance (including identification efficiencies) for the CI model increases from 13% at $M_{\mu^{+}\mu^{-}} = 100 \text{ GeV}/c^2$ to an asymptotic value of 21% for $M_{\mu^{+}\mu^{-}} > 400 \text{ GeV}/c^2$. The acceptance for the GM model increases from 12% at $M_{\mu^{+}\mu^{-}} = 100 \text{ GeV}/c^2$ to an asymptotic value of 23% for $M_{\mu^{+}\mu^{-}} > 300 \text{ GeV}/c^2$. The relative systematic uncertainty on the acceptance is 3.1%, which is dominated by the uncertainty in the identification efficiency (2.2%) and simulation statistics (2.0%).

We compute the expected background contributions from the following sources: (1) $Z/\gamma^{*}(\rightarrow\mu\mu\gamma)$, (2) $Z/\gamma^{*}(\rightarrow\tau\tau\gamma)$, where the $\tau$'s decay to muons, (3) $Z/\gamma^{*}(\rightarrow\mu\mu)+\text{jet}$, where the jet is misidentified as a photon, (4) $t(\rightarrow\mu b)+\bar{t}(\rightarrow\mu b)$, where a fermion radiates a photon, (5) $W(\rightarrow\mu\nu)+Z(\rightarrow\mu\mu)$, where the electron is misidentified as a photon, and (6) $Z(\rightarrow\mu\mu)+Z(\rightarrow\mu\mu)$, where one of the electrons is misidentified as a photon. Other backgrounds ($\geq 3$ jets, $W+\geq 2$ jets, and $W\gamma+\geq 1$ jet) were found to be negligible.

The $Z\gamma$, $t\bar{t}$, $WZ$, and $ZZ$ backgrounds are estimated using simulated events, with the ZGAMMA [18] generator for the $Z(\rightarrow\mu\mu)\gamma$ background and PYTHIA for the others. Systematic uncertainties on these background predictions arise due to integrated luminosity (6%) [19], parton distribution functions (PDFs) (5%), higher-order QCD corrections (5%) [20], acceptance (1%), and identification efficiencies (2%).

The $Z+\text{jet}$ background is estimated by weighting $Z+\text{jet}$ events from the data by an $E_{T}$-dependent jet $\rightarrow \gamma$ misidentification rate. The latter is measured using a jet-triggered data sample, correcting for the fraction of true prompt photons in the jet sample [21]. The prompt photon fraction is estimated using $\gamma \rightarrow ee$ conversions identified with the calorimeter preshower detector [21]. The jet $\rightarrow \gamma$ misidentification rate is applied as a function of $E_{T}$ in the central calorimeter and as a function of $E_{T}$ and $\eta$ in the forward calorimeter.

We observe 17 signal candidates with a background prediction of $8.3 \pm 0.9$, of which $8.1 \pm 0.8$ are expected from $Z\gamma$ production. The Poisson probability for the background to fluctuate up to the observation, or higher, is 0.8%. Investigating further, we find that 11 candidate events have a 3-body mass $m_{\mu\mu\gamma}$ in the 81-101 GeV/$c^2$ range, consistent with being final-state radiation (FSR) $Z \rightarrow \mu\mu\gamma$ events, to be compared to the FSR $Z \rightarrow \mu\gamma\gamma$ prediction of $5.5 \pm 0.5$ events. Figure 1 and Table 1 show the $m_{\mu\gamma}$ and $m_{\mu\mu\gamma}$ distributions for the data and background.

To test our background prediction, we lower the minimum photon $E_{T}$ to 15 GeV and observe 43 events with a prediction of $38.5 \pm 4.0$ events. The data show good agreement with expectation in this higher statistics sample, as shown in Figure 2. Additionally, we find consistency in the ISR $Z\gamma$ control region of $81 < m_{\mu\mu} < 101 \text{ GeV}/c^2$ and $25 < E_{T}^{Z} < 50 \text{ GeV}$, where we observe 5 events with a prediction of $7.2^{+1.2}_{-0.8}$ events. We conclude that our signal sample has an upward statistical fluctuation, dominantly in the number of FSR $Z \rightarrow \mu\gamma\gamma$ events.

For the $\mu^{*}$ resonance search, we scan the $m_{\mu\gamma}$ spectrum with a sliding window of width $3\sigma$, where $\sigma$ is the mass width predicted by the simulation. Over almost the
TABLE I: Comparison of data and integrated background predictions above a given cut on the invariant mass of all $\mu\gamma$ combinations (left) and on the $\mu\mu\gamma$ invariant mass (right).

| $m_{\mu\gamma}$ (GeV/$c^2$) | Events | $m_{\mu\mu\gamma}$ (GeV/$c^2$) | Background |
|-----------------------------|--------|-------------------------------|------------|
| $> 0$ | 34 | $> 0$ | 17 | 16.6 ± 1.8 | 8.3 ± 0.9 |
| $> 50$ | 22 | $> 50$ | 6 | 10.4 ± 1.1 | 2.7 ± 0.3 |
| $> 100$ | 4 | $> 100$ | 2 | 2.1 ± 0.3 | 1.5 ± 0.2 |
| $> 150$ | 2 | $> 150$ | 2 | 0.89 ± 0.14 | 0.9 ± 0.1 |
| $> 200$ | 0 | $> 200$ | 1 | 0.37 ± 0.07 | 0.51 ± 0.09 |
| $> 300$ | 0 | $> 300$ | 0 | 0.29 ± 0.06 | |

entire model parameter space, $\sigma$ is dominated by detector resolution. The tracker momentum scale and resolution, and the calorimeter energy scale and resolution, are tuned on the well-known $Z \rightarrow \mu\mu$ and $Z \rightarrow ee$ mass peaks, respectively. For $M_{\mu^*} = \Lambda$, the reconstructed $\mu^*$ mass resolution ranges from 9-90 GeV/$c^2$ for masses ranging from 200-800 GeV/$c^2$.

We use a Bayesian approach, with a flat prior on the signal cross section and gamma priors on acceptance and backgrounds, to set limits on the $\mu^*$ production cross section as a function of $M_{\mu^*}$. The cross section limits are converted to $M_{\mu^*}$ limits by comparing them to the next-to-next-to-leading-order (NNLO) theoretical cross sections, computed using the MRST set of PDFs. We use the CTEQ prescription to calculate the cross section uncertainty due to PDFs, which varies from 5% ($M_{\mu^*} = 100$ GeV/$c^2$) to 20% ($M_{\mu^*} = 1$ TeV/$c^2$). Uncertainties on higher-order QCD corrections (7-13%) depend on $M_{\mu^*}$ and the production model.

Figure 3 shows the 95% confidence level (CL) upper limits on the experimental cross section $\times$ branching ratio and the theoretical curves for $M_{\mu^*} = \Lambda/f$ ($M_{\mu^*} = \Lambda$) for the GM (CI) model. Masses below 221 GeV/$c^2$ (853 GeV/$c^2$) are excluded for the GM (CI) model for the case $M_{\mu^*} = \Lambda/f$ ($M_{\mu^*} = \Lambda$). Figure 3 shows the limits in the parameter space of $f/\Lambda$ ($M_{\mu^*}/\Lambda$) versus $M_{\mu^*}$ for the GM (CI) model. For both models, we lose sensitivity for $M_{\mu^*} < 100$ GeV/$c^2$ due to large backgrounds and loss of signal acceptance in this range. We note that our CI limit of $M_{\mu^*} > 853$ GeV/$c^2$ reduces to $M_{\mu^*} > 696$ GeV/$c^2$ if we use $\mu^*$ branching ratios that account for hypothetical CI decays, as assumed by the DO collaboration.

In conclusion, we have presented a search for excited and exotic muons. In the GM model, we exclude $100 < M_{\mu^*} < 410$ GeV/$c^2$ for $f/\Lambda = 10^{-2}$ GeV$^{-1}$ at the 95% C.L., which is the first GM result at a hadron collider and is substantially beyond previous limits. We have also presented $\mu^*$ limits in the CI model as a function of $M_{\mu^*}$ and $\Lambda$, excluding $107 < M_{\mu^*} < 853$ GeV/$c^2$ for $\Lambda = M_{\mu^*}$. These limits complement our recent results of a search for excited and exotic electrons.

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