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This article analyzes the process of image synthesis for a formation flying synthetic aperture radar (FF-SAR), which is a multistatic synthetic aperture radar (SAR) based on a cluster of receiving-only satellites flying in a close formation, in the framework of the array theory. Indeed, the imaging properties of different close receivers, when analyzed as isolated items, are very similar and form the so-called common array. Moreover, the relative positions among the receivers implicitly define a physical array, referred to as spatial diversity array. FF-SAR imaging can be verified as a result of the spatial diversity array weighting the common array. Hence, different approaches to beamforming can be applied to the spatial diversity array to provide the FF-SAR with distinctive capabilities, such as coherent resolution enhancement and high-resolution wide-swath imaging. Simulation examples are discussed which confirm that array theory is a powerful tool to quickly and easily characterize FF-SAR imaging performance.

I. INTRODUCTION

Spaceborne synthetic aperture radar (SAR) remote sensing missions have been delivering operational products and services since the early 1990s. In the last decade, SAR satellites have grown in number, capability, and complexity, culminating with the realization of multisatellite missions, such as COSMO-SkyMed [1] and Sentinel-1 [2] constellations and TanDEM-X formation [3], [4]. An important trend in satellite remote sensing technology is also toward system miniaturization. Spaceborne SAR missions have been successfully deployed relying on very compact platforms, i.e., the Israeli TecSAR (300-kg launch mass) [5], the Indian RISAT-2 (300-kg launch mass) [6], and the Finnish ICEYE-X1 (70-kg launch mass) [7]. Despite the rapid technological advances that have characterized satellite SAR missions, miniaturization has been only obtained at the expense of performance parameters, like mission lifetime, orbit duty cycle, image resolution, ground coverage, and interferometric revisit.

The term formation flying SAR (FF-SAR) is used in this article to indicate a cluster of receiving-only satellites flying in a close formation. Each satellite collects the echoed signal emitted by the transmitter and scattered from the area of interest. These collected echoes are then coherently combined to enhance the overall system performance and the quality of the delivered products.

Thanks to passive operations, an FF-SAR achieves high performance through a series of very compact, low weight, platforms. So, the FF-SAR mission concept is naturally coupled with the use of small space platforms. As a consequence, the system overall cost is lower, the replacement of a failed satellite is easier and faster, and it is possible to gradually update on board technologies by incrementally replacing elements of the formation, which is generally an issue for large monolithic space systems. Indeed, small satellite missions offer the opportunity to rapidly and flexibly inject new technology developments in spaceborne solutions. Concerning this, a CubeSat train was recently proposed [8] for high resolution radar sounding and imaging of Antarctica. The formation includes 50 CubeSats. Formation design and Earth rotation are used to synthesize a large cross-track array. The coherent combination of radar echoes collected by each platform is thus expected to guarantee high cross-track resolution, which is difficult to achieve by single satellite radar sounding.

An FF-SAR represents a generalization of the conventional SAR principle [9]–[10], and of standard interferometric SAR (InSAR) techniques [11], toward a highly flexible system able to implement a wide range of different working modes. When both cross-track/radial and along-track separations are available, the coherent processing approach can be adaptively modified to improve the desired imaging feature to the current scene and to the observation requirements. In addition, the separations among the receivers can be changed during the mission to further improve the system capabilities. According to multistatic SAR literature [12], various multistatic configurations can be defined, including: fully active systems, monomonostratic, and semiactive
systems. In this sense, the abovedefined FF-SAR, if realized as a companion satellite mission [13], i.e., collecting echoes from a preexisting monostatic SAR, can be also interpreted as a specific case of semiaactive multistatic SAR. Safe formation flying operations [3], [14], [15] and precise clock synchronization [12], [16], [17] among the receivers are prerequisites for FF-SAR implementation. Important capabilities in this ambit have already been successfully demonstrated by past bistatic SAR missions, like TanDEM-X mission [4], and more recently, in small satellite formation flying missions, like CanX-4&5 [18].

An FF-SAR can also operate as a multibaseline single-pass interferometer. Such a configuration has been proposed to implement advanced InSAR techniques [12] like single-pass tomography and ground moving target indication (GMTI) or to complement the processing architectures of differential SAR interferometry (DInSAR) through repeated multibaseline single-pass acquisitions. In this context, experimental results and methodologies are available [19]–[21].

The FF-SAR technique is analyzed in this article from a different perspective. Indeed, the working principle of the FF-SAR is not new. Its theoretical foundation can be dated back to [22]. Moreover, demonstrations have been performed in previous spaceborne [23] systems. The present work is mainly focused on FF-SAR imaging features, that is on the derivation of an analytical model to be used for evaluation of FF-SAR imaging performance. This FF-SAR image, thanks to the spatial diversity of the collection geometry and the redundancy of the measurements, is characterized by enhanced properties with respect to the image that a single receiver of the formation can generate when operating as an isolated item. Some studies have already investigated this topic [24]–[26]. An imaging model based on the k-space method was discussed in [24] able to represent the point spread function (PSF) for a system of cooperative monostatic SARs. The present article starts from this concept to introduce a model for representing the point target response of an FF-SAR and the key role played by the relative geometries between the transmitter and the available receivers. With specific reference to multiple formation flying receivers, most of the available results concern satellite formations with along-track-only separations to apply high-resolution wide-swath (HRWS) imaging, i.e., placing formation flying satellites as a multichannel antenna in the along-track direction. An imaging model, able to deal with both along-track and cross-track/vertical separations among the receivers, is that proposed in [27] and [28]. The model originally introduced the concept of sensor vector to characterize the added value of the spatial diversity among the receivers with respect to standard SAR coordinates of frequency and time. A key tool of the model is the array theory that effectively measures the relative contributions and the importance of frequency, time, and spatial diversity to determine image performance. The principle shows similarity with the k-space method [24], in which a k-set is introduced with the PSF of the system computed as the Fourier Transform of the k-set. However, the array theory is best suited for analyzing the effects of multistatic acquisitions on imaging performance. The model of [27] and [28] assumes that the transmitter and receivers fly at the same velocity, so it can be applied to the case in which the transmitter is flying in a very close formation with the receivers. The range of applicability of this model is thus limited. It cannot be used to study upcoming mission concepts like SESAME [29], STEREOID [30], Multistatic HRWS [31], and, more in general, is not valid when a formation of receivers is realized to complement an already existing monostatic SAR mission, i.e., for the case of companion satellites [13], [32], [33]. Indeed, performance enhancement made possible by FF-SAR is independent of the location of the transmitter, which can also be a mere illuminator, since FF-SAR does not need a monostatic SAR image to be exploited. This leads to even more exotic configurations, e.g., based on geostationary transmitters [34], [35] or digital video broadcasting terrestrial (DVB-T) opportunity illuminators [36].

The basic idea of this article is that the imaging properties of all receivers, when analyzed as isolated items, are very similar and can be represented by a so-called common array pattern, i.e., receivers are in close formation. Moreover, the relative positions among the receivers implicitly define a physical array, referred to as the spatial diversity array. The combination of the common and the spatial diversity arrays by suitable beamforming techniques lead to the resulting FF-SAR image. The introduced approach is of quite general validity meaning that it can be applied to 1) close satellite formations including both a monostatic SAR and a given number of receivers, as in [3] and [27]; 2) companion satellite-like configurations, i.e., large satellite formations with a transmitter that is relatively far from a cluster of receivers, as in [29]–[33]; 3) formations of close receivers working with transmitters operating at completely different ranges of altitude and velocity, as in [34]–[37].

The main output of the proposed model is the FF-SAR point target response, from which general performance parameters [38], like resolution, peak-side-lobe ratio (PSLR), integrated side-lobe ratio (ISLR), ambiguity levels, can be readily computed.

This article is organized as follows. Section II presents the FF-SAR signal model introducing the main relevant parameters and operators. The interpretation of FF-SAR image synthesis in the framework of array theory is illustrated in Section III, where the concepts of common and spatial diversity array are formulated. Then, Section IV discusses the most prominent FF-SAR beamforming techniques allowing the system to achieve coherent resolution enhancement (CRE), signal-to-noise ratio (SNR) improvement, and HRWS imaging. The application of the developed methodology to some examples of satellite formations is described in Section V.

II. FF-SAR SIGNAL MODEL

A reference frame is defined in Fig. 1, with the origin of coordinates located at the center of the scene to be imaged, and x–y as the local plane. Transmitter and receivers fly
linear flight paths at constant velocity within the coherent processing interval. Transmitter position and velocity are indicated as \( \mathbf{P}_{Tx} \) and \( \mathbf{v}_{Tx} \), respectively, whereas the position vector of the \( i \)th receiver is \( \mathbf{P}_{Rx,i} \) and its velocity is \( \mathbf{v}_{Rx,i} \).

It worth noting that, differently from [27] and [28]

\[
\mathbf{v}_{Tx} \neq \mathbf{v}_{Rx,i}, \quad i = 1, \ldots, N
\]

where \( N \) is the number of receivers. So, the transmitter moves along a trajectory which is different from those of the receivers. Nonetheless, since coherent combination among the data collected by each receiver must be allowed, the receivers are assumed to fly as a satellite formation

\[
\frac{||\mathbf{v}_{Rx,i} - \mathbf{v}_{Rx,k}||}{||\mathbf{v}_{Rx,i}||} < < 1 \quad \forall i, k
\]

where \( || \) is the Euclidean norm. According to (2), velocity variations among the receivers within the coherent processing interval can be neglected, that is \( \mathbf{v}_{Rx,i} \equiv \mathbf{v}_{Rx} \), \( \forall \ i \).

Based on the start-stop approximation [38], [39], the raw bistatic signal at the \( i \)th receiver from a stationary point target located in \( \mathbf{P} \) can be formulated

\[
S_{Rx}(\mathbf{P}, u, t, i) = \gamma(\mathbf{P}) G_{Tx}(t, \mathbf{P}) \cdot G_{Rx}(t, \mathbf{P})
\]

\[
\exp \left\{ j \left[ \alpha \left[ u - \frac{R_{Tx}(t) + R_{Rx,i}(t)}{c} \right] \right]^2 \right\}
\]

\[
\exp \left\{ -j \frac{2\pi f_c}{c} \left[ R_{Tx}(t) + R_{Rx,i}(t) \right] \right\}
\]

\[
\operatorname{rect} \left( \frac{u - R_{Tx}(t) + R_{Rx,i}(t)}{\tau_p} \right) \quad i = 1, \ldots, N
\]

where \( u \) is the fast-time, \( t \) is the slow time, \( \gamma \) is the complex reflection coefficient of the target, \( G_{Tx} \) and \( G_{Rx} \) are, respectively, transmitting (Tx) and receiving (Rx) antenna gains in the direction of the targets, \( j \) is the imaginary unit, \( \alpha \) is the chirp rate, that is the ratio between signal bandwidth and the pulse length \( \tau_p \), \( c \) is the speed of light, and \( f_c \) is the carrier frequency. The model of (3) is the same as the standard one used for monostatic SAR [38], in which the monostatic range history is replaced by the bistatic one, i.e., \( R_{Tx}(t) = |\mathbf{P}_{Tx}(t) - \mathbf{P}| \) and \( R_{Rx,i}(t) = |\mathbf{P}_{Rx,i}(t) - \mathbf{P}| \). The fast-time Fourier transform of the raw bistatic signal can be computed as in [38] by the principle of stationary phase, thus yielding

\[
S_{Rx}(\mathbf{P}, f, t, i) = A_1 \gamma(\mathbf{P}) G_{Tx}(t, \mathbf{P}) \cdot G_{Rx}(t, \mathbf{P})
\]

\[
\cdot \operatorname{rect} \left( \frac{f}{\alpha \tau_p} \right)
\]

\[
\exp \left\{ -j \frac{2\pi f_c}{c} \left( R_{Tx}(t) + R_{Rx,i}(t) \right) \right\}
\]

\[
\exp \left\{ -j \frac{\pi f^2}{\alpha} \right\} \quad i = 1, \ldots, N
\]

where \( A_1 \) is a constant and \( f \) is the fast time frequency. A suitable approach to interpret FF-SAR imaging is by the basic array theory, that is analyzing the resulting radiation pattern [40] of the array represented (virtually) by the phase contributions of the signals collected by each receiver according to (4). No straightforward application of this idea can be performed as long as the phase model is not reformulated more conveniently. Required derivation is similar to the one discussed in [27] and [28] and it is herein presented.

Without loss of generality, one can assume the first receiver as the reference receiver. So, the baseline vector, \( \mathbf{B} \), can be introduced, representing the vector from the position of the reference receiver, \( \mathbf{P}_{Rx} \), to the generic one of the formation

\[
\mathbf{B} = \mathbf{P}_{Rx,i} - \mathbf{P}_{Rx} = \begin{bmatrix} B_x & B_y & B_z \end{bmatrix}^T
\]

and the superscript \( T \) indicates the transpose operation. According to (4) and (5), the phase is a function of five parameters which can be grouped in a single vector

\[
\mathbf{s} = \begin{bmatrix} B_x & B_y & B_z & f & t \end{bmatrix}^T
\]

referred to as sensor vector in [27] and [28]. Equations (4)–(6) states that each receiver observes the scene as a function of frequency (i.e., range or fast time) and slow time (i.e., azimuth) as in standard SAR, but those collections are performed from different relative positions \( \mathbf{B} \), which introduce a spatial diversity in the data, affecting the phase of collected signals too. Therefore, a useful representation of the phase can be obtained by two consecutive first-order Taylor series expansion, the first one as a function of the parameters, \( \mathbf{s} \), and the second one as a function of target location, \( \mathbf{P} \). The first series expansion is performed around

\[
\tilde{\mathbf{s}} = \begin{bmatrix} 0 & 0 & 0 & 0 \end{bmatrix}^T
\]

and yields

\[
\Psi(\mathbf{P}, \mathbf{s}) \approx \Psi(\mathbf{P}, \tilde{\mathbf{s}}) + (\nabla_\mathbf{s} \Psi|_{\tilde{\mathbf{s}}} )^T \Delta \mathbf{s}
\]

where \( \nabla_\mathbf{s} \) indicates the gradient operator with respect to sensor parameters. The phase derivative with respect to the frequency is proportional to the time delay

\[
\frac{\partial \Psi}{\partial f} |_{\tilde{\mathbf{s}}} = - \frac{2\pi}{c} \left[ |\mathbf{P}_{Tx}(0) - \mathbf{P}| + |\mathbf{P}_{Rx}(0) - \mathbf{P}| \right] = 2\pi \tau (\mathbf{P}, \tilde{\mathbf{s}})
\]
whereas the derivative with respect to time is related to the Doppler frequency
\[
\frac{\partial \Psi}{\partial t} \bigg|_{\bar{P}, \bar{s}} = -\frac{2\pi}{\lambda} \left[ \mathbf{v}_T^T \mathbf{i}_{T_2} (\bar{P}, \bar{s}) + \mathbf{v}_{R_1}^T \mathbf{i}_{R_2} (\bar{P}, \bar{s}) \right] = 2\pi f_D (\bar{P}, \bar{s})
\]
(10)
with \( \mathbf{i}_{T_2} \) and \( \mathbf{i}_{R_2} \) as the unit vectors from \( \mathbf{P} \) to the transmitter and to the reference receiver, respectively (see Fig. 1), and \( \lambda \) as the carrier wavelength. Finally, the derivatives with respect to baseline components are
\[
\frac{\partial \Psi}{\partial \mathbf{B}} \bigg|_{\bar{P}, \bar{s}} = -\frac{2\pi}{\lambda} \mathbf{i}_{R_2} (\bar{P}, \bar{s}).
\]
(11)

So, following the first Taylor series expansion and neglecting the constant phase term \( \Psi(\bar{P}, \bar{s}) \), the phase is
\[
\Psi(\bar{P}, \bar{s}) \approx -\frac{2\pi}{\lambda} \mathbf{i}_{R_2}^T (\bar{P}, \bar{s}) \mathbf{B} + 2\pi \tau (\bar{P}, \bar{s}) f + 2\pi f_D (\bar{P}, \bar{s}) t.
\]
(12)

Then, a second Taylor series expansion must be used to calculate the variation of phase gradients as a function of ground target location, that is
\[
\mathbf{i}_{R_2}^T (\bar{P}, \bar{s}) \approx \mathbf{i}_{R_2}^T (\bar{P}, \bar{s}) + \Delta \mathbf{P}_{xy} \nabla \mathbf{i}_{R_2} (\bar{P}, \bar{s}) |_{\bar{P}, \bar{s}}
\]
(13)
\[
\nabla \mathbf{P} = \left[ \frac{\partial \mathbf{P}_x}{\partial \mathbf{P}_x} \frac{\partial \mathbf{P}_y}{\partial \mathbf{P}_y} \right] = \left[ \frac{\partial \mathbf{P}_x}{\partial \mathbf{P}_y} \frac{\partial \mathbf{P}_y}{\partial \mathbf{P}_y} \right]
\]
and \( \nabla \mathbf{P} = \left[ \frac{\partial \mathbf{P}_x}{\partial \mathbf{P}_x} \frac{\partial \mathbf{P}_y}{\partial \mathbf{P}_y} \right] \) is the gradient operator with respect to ground coordinates.

Analytic formulas for the gradient of the time delay and of the Doppler frequency can be found in bistatic SAR literature [35], [41]–[43]
\[
\nabla \tau (\bar{P}, \bar{s}) |_{\bar{P}, \bar{s}} = \frac{1}{c} \left[ \mathbf{i}_{T_2} (\bar{P}, \bar{s}) + \mathbf{i}_{R_2} (\bar{P}, \bar{s}) \right]
\]
(14)
\[
\nabla f_D |_{\bar{P}, \bar{s}} = \frac{1}{\lambda} \left[ \left[ \mathbf{v}_{T_2} - \left( \mathbf{v}_{T_2}^T \mathbf{i}_{T_2} (\bar{P}, \bar{s}) \right) \right] \mathbf{i}_{T_2} (\bar{P}, \bar{s}) \right.
\]
\[
\left. - \frac{1}{\mathbf{P}_{R_t} (0) - \mathbf{P}} \left[ \mathbf{v}_{R_2} - \left( \mathbf{v}_{R_2}^T \mathbf{i}_{R_2} (\bar{P}, \bar{s}) \right) \mathbf{i}_{R_2} (\bar{P}, \bar{s}) \right] \right].
\]
(15)

Moreover, after proper algebra, one can verify that (16) shown at the bottom of this page.

As a result of the second Taylor expansion, the phase becomes
\[
\Psi(\bar{P}, \bar{s}) \approx -\frac{2\pi}{\lambda} \mathbf{i}_{R_2}^T (\bar{P}, \bar{s}) \mathbf{B} + 2\pi \tau (\bar{P}, \bar{s}) f
\]
\[
+ 2\pi f_D (\bar{P}, \bar{s}) t - \frac{2\pi}{\lambda} \Delta \mathbf{P}_{xy} \mathbf{v}_{R_2} (\bar{P}, \bar{s}) |_{\bar{P}, \bar{s}} \mathbf{B}
\]
\[
+ 2\pi \Delta \mathbf{P}_{xy} \nabla f_D (\bar{P}, \bar{s}) |_{\bar{P}, \bar{s}} f
\]
\[
+ 2\pi \Delta \mathbf{P}_{xy} \nabla f_D (\bar{P}, \bar{s}) |_{\bar{P}, \bar{s}} t
\]
(17)
and if one defines
\[
\Delta \mathbf{s} = \left[ B_x \ B_y \ B_z \ f \ \tau \right]^T
\]
\[
\mathbf{k}(\bar{P}, \bar{s}) = \left[ -\frac{2\pi}{\lambda} \mathbf{i}_{R_2}^T (\bar{P}, \bar{s}) \ 2\tau (\bar{P}, \bar{s}) \ 2\pi f_D (\bar{P}, \bar{s}) \right]^T
\]
(18)
the phase can be rewritten in a more compact form as
\[
\Psi(\bar{P}, \bar{s}) \approx \mathbf{k}^T (\bar{P}, \bar{s}) \Delta \mathbf{s} + \Delta \mathbf{P}_{xy}^T \Lambda_s \Delta \mathbf{s}.
\]
(19)

Equation (19) is of more general validity than the phase model of [27] and [28] since an analytic model for \( \Lambda_s \) has been derived here for a generic FF-SAR geometry and it represents its generalization to the case of \( N \) satellite receivers flying in a close formation and sharing the same transmitter which operates, in general, on a different and independent trajectory. In fact, equation (19) is the starting point to interpret FF-SAR imaging as an equivalent, distributed, array. Specifically, \( \mathbf{k}(\bar{P}, \bar{s}) \) is the wavenumber vector including array wavenumbers corresponding to the reference location \( \bar{P} \). Consequently, \( \Delta \mathbf{P}_{xy} \Lambda_s \) is a vector measuring the deviation from these wavenumbers resulting from a ground target displaced by \( \Delta \mathbf{P}_{xy} \) from \( \bar{P} \). Hence \( \Lambda_s \) is the sensor transformation matrix [27], [28] representing the virtual FF-SAR sensor or array, i.e., converting the location of a generic target into the relevant five-dimension wavenumber vector corresponding to that target.

III. FF-SAR IMAGE SYNTHESIS

According to the array theory basis, the radiation pattern of a generic array is defined as the coherent weighted sum of the signals collected by each element of the array [44]. Suitable weighting functions are adopted to provide the array with some desired features, such as pointing the array toward an assigned direction and filtering out noise or unwanted echoes from specific directions. In the following this approach is applied to the synthetic array defined in Section II. This virtual array includes various elements, represented by the possible values that the sensor vector \( \mathbf{s} \) can take. Those values depend on the available

\[
\nabla \mathbf{P}_{R_t}^T (\bar{P}, \bar{s}) |_{\bar{P}, \bar{s}} = \left[ \begin{array}{c}
- \frac{1}{\mathbf{P}_{R_t} (0) - \mathbf{P}} + \frac{\left( \mathbf{P}_{R_t} (0) - \mathbf{P}_0 \right)^2}{\left( \mathbf{P}_{R_t} (0) - \mathbf{P}_0 \right)^2 - \left( \mathbf{P}_{R_t} (0) - \mathbf{P} \right)^2} \frac{\left( \mathbf{P}_{R_t} (0) - \mathbf{P}_0 \right)^2}{\left( \mathbf{P}_{R_t} (0) - \mathbf{P}_0 \right)^2 - \left( \mathbf{P}_{R_t} (0) - \mathbf{P} \right)^2}
\end{array} \right].
\]
(16)

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range of frequency, time and baseline components. With specific reference to the available frequency samples, they range from the minimum to the maximum frequency of the transmitted signal, that is $f_m \in [-W/2; W/2]$ with $m = 1, \ldots M$, where $W$ is signal bandwidth, $M$ is the total number of frequency samples. The adopted sampling step in frequency, $\delta f$, is in inverse relation to the time length of the transmitted pulse. Concerning time, sampled time instants, $t_l$, $l = 1, \ldots L$, belong to the available coherent processing interval sampled at the selected pulse repetition frequency (PRF), which can be related to the Doppler bandwidth of the scene. Hence the radiation pattern corresponding to the virtual array derived in Section II can be evaluated as

$$E_{\text{FF-SAR}}(\mathbf{P}) = \sum_{i=1}^{N} \sum_{m=1}^{M} \sum_{l=1}^{L} w(s_{i,m,l}) \exp \left( j \Psi(\mathbf{P}, s_{i,m,l}) \right)$$

where $w$ is the selected weighting function. Defining target coordinates with reference to $\mathbf{P}$ and sensor parameters with respect to $s$, the radiation pattern turns out to be

$$E_{\text{FF-SAR}}(\Delta \mathbf{P}_{xy}) = \sum_{i=1}^{N} \sum_{m=1}^{M} \sum_{l=1}^{L} \exp \left( j \left( k^T (\mathbf{P}, s) \Delta s_{i,m,l} + \Delta \mathbf{P}_{xy} \right) \right)$$

(20)

As noted above, the applied weighting function depends on the number and the type of conditions that the array pattern must satisfy. The simplest condition one can set is that the peak of the pattern points in a specific direction, such as the reference location $\mathbf{P}$. This corresponds to

$$w(\Delta s_{i,m,l}) = \exp \left( -j \left[ k^T (\mathbf{P}, \tilde{s}) \Delta s_{i,m,l} \right] \right).$$

(21)

Equations (21) and (22) can be interpreted as the generalization of traditional SAR focusing to the case of a distributed SAR. Specifically, they state that the echoes from a specific target, separately collected by each receiver, must be coherently added, that is compensated for the phase difference generated by range frequencies ($m$-index) and azimuth time ($l$-index) but also for phase differences produced when the same target is observed by receivers embarked on different platforms ($i$-index) to get the final focused image of the target. The result is that the derived array pattern plays the same role as the point target response in traditional SAR literature, so it can be used to estimate system performance, such as image resolution, as shown in the next subsections. It is clear that a different determination of weights is required to point the array pattern to any ground target. Again, pointing the array is equivalent to defining the reference function for SAR focusing, e.g., when the reference function varies for different range and azimuth portions in the scene. FF-SAR characterization by the array radiation pattern of (21) and (22) implicitly assumes that problems related to focusing can be successfully solved. This includes range walk that, herein, is assumed not to be present or to be compensated for.

The compact notation of (21) and the introduced quantities $w$, $k$, and $\Lambda_s$ are very useful to characterize the overall FF-SAR imaging performance. Some metrics were introduced in [27] based on singular value decomposition (SVD) of $\Lambda_s$ and under the assumption that $w$ is a Gaussian function with width and orientation described by the relevant covariance matrix. In the next sections, instead, a different approach is applied making the quantities explicit. This is useful to highlight FF-SAR features, that is the role played by both multiple measurements and spatial diversity.

A. Common and Spatial Diversity Array Patterns

Based on (22), and without loss of generality, the weighting function is

$$w(\Delta s_{i,m,l}) = p(B_i) q(f_m) r(t_l) = p_i q_m r_i.$$  

(23)

According to (17), (21)–(22), one can write

$$E_{\text{FF-SAR}}(\Delta \mathbf{P}_{xy}) = E_C(\Delta \mathbf{P}_{xy}) E_{SD}(\Delta \mathbf{P}_{xy})$$

with

$$E_C(\Delta \mathbf{P}_{xy}) = \sum_{m=1}^{M} \left[ q_m \exp \left( j \left( 2 \pi \tau \left( \tilde{\mathbf{P}}, \tilde{s} \right) f_m \right) \right) \right]$$

$$\times \left[ \sum_{l=1}^{L} \left[ r_l \exp \left( j \left( 2 \pi f_{\tau} \left( \tilde{\mathbf{P}}, \tilde{s} \right) t_l \right) \right) \right] \exp \left( j \left( 2 \pi f_{\tau} \left( \tilde{\mathbf{P}}, \tilde{s} \right) t_l \right) \right) \right]$$

$$\times \exp \left( -j \left( \frac{2 \pi}{\lambda} v_{\tau} \left( \tilde{\mathbf{P}}, \tilde{s} \right) B_i \right) \right).$$

$$E_{SD}(\Delta \mathbf{P}_{xy}) = \sum_{i=1}^{N} \left[ p_i \exp \left( -j \left( \frac{2 \pi}{\lambda} v_{\tau} \left( \tilde{\mathbf{P}}, \tilde{s} \right) B_i \right) \right) \right].$$

(24)

Hence FF-SAR array pattern is the product of two main contributions.

1) The common array pattern $E_C$, depending on the time delay and the Doppler frequency of the target with respect to the reference receiver. It measures the contribution of a single receiver in the formation as an isolated element.

2) The spatial diversity array pattern, $E_{SD}$, depending on the baselines, i.e., on the spatial separations among the receivers. It characterizes the added value of the FF-SAR in which more receivers are available.

The interpretation of (24) is as follows. Since we deal with receivers in close formation ($|\mathbf{B}| << |\mathbf{P}_{\tau}B_i|$), the bistatic SAR images generated by all receivers are very similar. If one considers the amplitudes of their point target response, they are so similar that differences can be neglected in practice. This behavior is modeled by the common array. However, since receivers work from different locations, the phases of the bistatic images are different ($|\mathbf{B}| >> \lambda$) and can be used to synthesize one further array called the spatial diversity array. This is the physical array realized by the relative positions among the receivers in the cluster, properly weighted by beamforming to obtain the desired FF-SAR performance enhancement (see the
Section IV). The model of (23)–(25) covers a wide range of different SAR schemes. Specifically, FF-SAR can be properly characterized by this model, but even the main properties of simpler realizations, that is more traditional monostatic and bistatic SAR, can be derived. Concerning this, the introduced methodology based on the array theory can easily measure the imaging performance improvement of an FF-SAR with respect to either monostatic or bistatic SARs as it will be pointed out in the remainder of this article.

Error sources exist affecting FF-SAR imaging: They include synchronization errors and positioning errors. Different forms of synchronization must be applied to enable FF-SAR operations. They can be organized in three main classes [12]. 1) Spatial synchronization, i.e., receiving antennas are requested to cover the ground area illuminated by the transmitter; 2) echo window or time synchronization, i.e., each receiver must know with sufficient precision the time instants in which echoes from the scene are expected to reach Rx antenna; 3) clock synchronization, i.e., all the receivers must be coherent for the period of time required to get useful data from the scene. A standard assumption is that the transmitter and the receivers are indirectly synchronized at platform level using GPS time, which guarantees an accuracy of 1–2 μs. This is typically enough to support spatial synchronization and, completed by the leap PRF technique [3], guarantees also adequate echo window synchronization. Clock synchronization, instead, is the robust and accurate matching of transmitter and receiver clock phases, with random mean errors smaller than a fraction of a wavelength. Lacking clock synchronization influences both the time (either fast or slow) and the phase of the collected bistatic signals. Clock error is dominated by the frequency offset between the oscillator frequencies of the transmitter and of each receiver. This can be computed accurately using dedicated intersatellite links, as in [4]. An alternative solution for platform with limited resources—e.g., small and micro satellites, or when an illuminator of opportunity is used—is a rough estimation of the offset from the GPS time which is then refined by suitable postprocessing of the collected raw bistatic data [45]. As for positioning errors, it is important to remark that tight orbit control is not required for FF-SAR operation [46], which sets instead tight requirements on the knowledge of the relative positions. Specifically, different requirements are posed by bistatic SAR processing and FF-SAR beamforming. The former involves the knowledge of the relative positions between the Tx and each Rx with an accuracy ruled by the ratio between platform velocities and the Doppler bandwidth, i.e., typically below one meter. Beamforming instead requires subwavelength, i.e., up to mm-scale in X-band, accuracy on the knowledge of the baselines among the receivers, which can be achieved by postprocessing carrier-phase differential GPS (CDGPS) techniques [47]. The following derivations and the simulation results of Section V do not consider error sources. Nonetheless the proposed imaging model based on common and spatial diversity arrays is of quite general validity and simulations could be run to evaluate the effect of either positioning or synchronization errors as outlined in Section VI.

B. Bistatic SAR

If a bistatic SAR is considered, a single receiver is available. In this case no spatial diversity can be exploited

\[ E_{SD}(\Delta P_{xy}) = 1 \Rightarrow E_{bist}(\Delta P_{xy}) = E_C(\Delta P_{xy}) \]  

with \( E_{bist} \) as the representative array pattern of a bistatic SAR, which can be derived assuming

\[ q_m = \exp\left(-j\left(2\pi\tau(\tilde{P}, s)f_m\right)\right) \]

\[ r_l = \exp\left(-j\left(2\pi f_D(\tilde{P}, s)t_l\right)\right) \]

that is performing bistatic SAR focusing

\[ E_{bist}(\Delta P_{xy}) = \sum_{m=1}^{M} \left[ \exp\left(j\left(\Delta P_{xy}^T 2\pi \nabla_P \tau(\tilde{P}, s)|_{\tilde{P}, s}f_m\right)\right) \right] \]

\[ \times \sum_{l=1}^{L} \left[ \exp\left(j\left(\Delta P_{xy}^T 2\pi f_D(\tilde{P}, s)|_{\tilde{P}, s}t_l\right)\right)\right]. \]

The radiation pattern includes two independent contributions given by the inner product between the ground separation \( \Delta P_{xy} \) from the reference position and, respectively, the gradient of the time delay and of the Doppler frequency. This result matches well-known bistatic SAR analyses [34], [35], [41]–[43], [48]–[50]. A bistatic SAR is able to detect changes of time delay and Doppler frequency and this capability acts along the directions of the gradients of the time delay and of the Doppler frequency, respectively. These directions are, in general, not perpendicular leading to ground pixel skewing. Moreover, the representative array of a bistatic SAR includes time and frequency samples that are regularly spaced and sufficient in number to apply the sinc approximation to the relevant pattern. This means that the point target response is a two-dimensional sinc function with axes aligned to the directions of ground range and Doppler gradients. Corresponding image resolutions can be computed by the so-called gradient method [42]. Nonetheless the same result can be obtained using (28) and applying the array theory to the derived radiation pattern. Indeed, the resolution of an array along a generic direction can be estimated as the projection of the half-power beamwidth of the array along that direction, where, as expected the 3-dB aperture is in direct relation to the wavelength-to-array size ratio [44]. Based on this well-known result, one can formulate ground range and Doppler resolutions as

\[ \delta R_g = \chi_f \frac{\lambda}{\Delta R_g} R_b \]

\[ \delta a = \chi_t \frac{\lambda}{\Delta a} R_b \]

where \( R_b \) is the bistatic range

\[ R_b = |P_{Tx}(0) - \tilde{P}| + |P_{Rx}(0) - \tilde{P}| \]
\( \Delta R_g \) and \( \Delta a \) are the array sizes, along the ground range and Doppler directions, respectively, and \( \chi_f \) and \( \chi_t \) are the coefficients of the applied windowing function in frequency and time, e.g., \( \chi_f = \chi_t \equiv 0.886 \) for rectangular windowing. The bistatic radiation pattern of (28) is used to calculate the array sizes. Namely, the latter are determined considering the total phase angles in (28) as a function of \( m \) and \( l \), respectively, and interpreting those angles as the product of ground range and Doppler wavenumbers with array sizes. Hence
\[
\Delta \Psi_f = k_f \Delta R_g = 2\pi W [\nabla_{P_{xy},\tau}] \Delta P_{xy}^T i_t
\]
\[
\Delta \Psi_t = k_t \Delta a = 2\pi CPI [\nabla_{P_{xy},f_D}] \Delta P_{xy}^T i_{f_0} \tag{31}
\]
where \( CPI \) is the coherent processing interval, \( \nabla_{P_{xy},\tau} \) is the ground projection of \( \nabla_P (P, \bar{s})|_{P_{xy}} \), \( i_t \) is the unit vector in the direction of \( \nabla_{P_{xy},\tau} \), \( \nabla_{P_{xy},f_D} \) is the ground projection of \( \nabla_P f_D (P, \bar{s})|_{P_{xy}} \) and \( i_{f_0} \) is the unit vector in the direction of \( \nabla_{P_{xy},f_D} \). Based on (31) one can write
\[
k_f = \frac{2\pi \Delta P_{xy}^T i_t}{\lambda R_b} \Delta R_g = \lambda R_b W [\nabla_{P_{xy},\tau}]
\]
\[
k_t = \frac{2\pi \Delta P_{xy}^T i_{f_0}}{\lambda R_b} \Delta a = \lambda R_b CPI [\nabla_{P_{xy},f_D}] . \tag{32}
\]
Hence, bistatic ground range and Doppler resolutions are
\[
\delta R_g = \frac{\chi_f}{W [\nabla_{P_{xy},\tau}]}
\]
\[
\delta a = \frac{\chi_t}{CPI [\nabla_{P_{xy},f_D}] . \tag{33}
\]
and the amount of pixel skewing is measured as the angle between \( i_t \) and \( i_f \), which agrees with equations derived by the gradient method [34], [41], [42].

C. Monostatic SAR

When considering a monostatic SAR, a single receiver exists and it is colocated with the transmitter. Therefore, the reference frame of Fig. 1 can be defined with the \( y \)-axis parallel to platform velocity and \( x-z \) plane as the range elevation plane, such that
\[
P_{Rx} (0) = P_{Rx} (0) = R \begin{bmatrix} -\sin \theta \\ 0 \\ \cos \theta \end{bmatrix}
\]
\[
v_{Rx} = v_{Rx} = v 
\]
\[
P = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \tag{34}
\]
where \( v \) is platform velocity, \( R \) is the slant range of the reference target and \( \theta \) is the incidence angle. Based on (15) one derives
\[
\nabla_{P_{xy},\tau} = \frac{2}{c} \begin{bmatrix} -\sin \theta \\ 0 \\ 1 \end{bmatrix} i_t = \begin{bmatrix} -1 \\ 0 \end{bmatrix} \tag{35}
\]
\[
\nabla_{P_{xy},f_D} = \frac{2}{\lambda R} \begin{bmatrix} 0 \\ v \end{bmatrix} i_{f_0} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \tag{36}
\]
Using (34)–(36) the resulting array size along ground range and azimuth directions are
\[
\Delta R_g = \frac{4\lambda RW}{c} \sin \theta \tag{37}
\]
\[
\Delta a = 4v CPI .
\]
Replacing (37) in (29), the well-known formulas of monostatic SAR resolutions are obtained.

IV. BEAMFORMING OF FF-SAR DATA

According to Section III-A, the spatial diversity array is peaked around the reference location \( \bar{P} \) as an effect of the introduced weighting functions. The representative radiation pattern of an FF-SAR is thus the result of the spatial diversity array weighting the common array. Since the latter models the image of a generic, isolated, either bistatic or monostatic, receiver of the formation, (23)–(25) also represent an example of beamforming applied to the spatial diversity array to provide the FF-SAR with additional properties with respect to the single receiver case.

A. Coherent Resolution Enhancement

Coherent resolution enhancement is achieved by FF-SAR when beamforming is applied as in (23)–(25) and the peak of the spatial diversity array is significantly narrower than the main lobe of the common array. As expected, this sets constraints on the size of the spatial diversity array and so on the baseline among the receivers.

As an example, an FF-SAR can be considered including a monostatic side-looking SAR as both the transmitter and the reference receiver of the formation. Depending on the available baselines among the receivers, the spatial diversity array can be wider than the common, i.e., the monostatic, one thus significantly contributing to the overall FF-SAR array size and to its resolution. Equation (29) can be still used to quantify the achievable resolution in this case, but differently from the Sections III-B and III-C, \( E_{SD} (\Delta P_{xy}) \neq 1 \). The spatial diversity array is defined by the spatial gradient of the unit vector from the reference location to the reference receiver. Based on (16) and (34), one derives
\[
\nabla_P P_{Rx} (P, \bar{s})|_{P_{xy}} = \begin{bmatrix} -\cos^2 \theta \\ 0 \\ -\frac{\sin \theta \cos \theta}{R} \end{bmatrix} \tag{38}
\]
where the same reference frame as in Section III-C is used. The resulting FF-SAR array size along ground range and azimuth directions are
\[
\Delta R_g,FF-SAR = \frac{4\lambda RW}{c} \sin \theta + \Delta B_\perp \cos \theta
\]
\[
\Delta a_{FF-SAR} = 4v CPI + \Delta B_y \tag{39}
\]
where \( \Delta B_\perp \) is the maximum baseline component normal to the line of sight and \( \Delta B_y \) is the maximum along-track baseline component. According to (29), FF-SAR ground range resolution can be computed as
\[
\delta R_g,FF-SAR = \frac{\chi_f 4\lambda RW}{c} \sin \theta + \frac{2\lambda R}{c} \sin \theta + \Delta B_\perp \cos \theta
\]
\[ \Delta W = \frac{c \Delta B_\perp}{2\nu CPI} \]  
\[ \delta a_{\text{mono}} = \frac{2\nu CPI}{2\nu CPI} \]  

where \( \Delta B_\perp \) is the null-to-null width and \( \delta a_{\text{mono}} \) is the monostatic SAR azimuth resolution.

The right term in (47) is the so-called critical orthogonal baseline [12]. Hence requiring the spatial diversity array to show grating lobes outside the main lobe of the monostatic point target response means setting the orthogonal baseline shorter than the critical value. Moreover, it is worth noting that (47) corresponds to \( \Delta W \leq W \) in (41), that is, the ground range resolution improvement is limited to a factor of 2. The result can be extended to the case of an FF-SAR working with more receivers. Grating lobes for an array of \( N \) uniformly displaced elements occur at angles that are still ruled by (43) if \( \Delta B_s \) is interpreted as the distance between adjacent elements. Therefore, if the latter is shorter than the critical value, no grating lobes of the spatial diversity array fall into the main lobe of the monostatic response. This result seems to suggest that by using a formation of \( N \) uniformly displaced receivers one can enhance the ground range resolution by a factor of \( N \). However, care must be taken in combining data collected from baselines close to the critical value, which are, no doubt, subject to baseline decorrelation effects. The same approach can be applied to the azimuth direction leading to the same conditions as in [54] for coherent resolution enhancement in azimuth.

One further case to consider is an FF-SAR working with \( N \) receivers that are not regularly displaced. In this case, as long as separations show no periodicity [40], [44], no real grating lobes (i.e., as strong as the main lobe) appear, although high spurious lobes may be present, which occur outside the main lobe of the monostatic response.

The above derivation can be further generalized to the case in which an FF-SAR is used, exploiting a transmitter working on an independent trajectory, i.e., an illuminator of opportunity. In this case the common array corresponds to the bistatic array of the reference satellite. So, equation (29) is still valid to represent FF-SAR image resolution if the total array size is considered along both range and Doppler directions. According to (25), FF-SAR total phase angles along \( \tau_1 \) and \( \tau_{f_0} \) are, respectively

\[ \Delta \Psi_{f,\text{FF-SAR}} = \frac{2\pi}{\lambda} \left[ \frac{\Delta P_{xy}^T \tau_1}{R_b} \right] \]  
\[ \Delta \Psi_{f,\text{FF-SAR}} = \frac{2\pi}{\lambda} \left[ \frac{\Delta P_{xy}^T \tau_{f_0}}{R_b} \right] \]  

with \( k \) integer number. As noted above, to ensure good FF-SAR performance it is desired that grating lobes fall outside the main lobe of the monostatic point target response in ground range. If \( \Delta \theta_{NTN} \) is the null-to-null width corresponding to the monostatic point target response, that is

\[ \Delta \theta_{NTN} = \frac{2 \nu CPI \cos \theta}{R} \]
where $\Delta \mathbf{B}$ is the vector of the maximum baseline components. Hence, FF-SAR resolutions become

$$\delta R_{g, \text{FF-SAR}} = \chi_f \left| \Psi_{P, xy}^f \right| + \frac{1}{\lambda} \mathbb{E} \left[ \mathbb{E}^T \Psi_{P, xy}^f \mathbb{E} \left( \mathbb{E}^T \Phi_{P, xy}^f \right) \right]$$

$$\delta \alpha_{\text{FF-SAR}} = \chi_f \left| CPI \left| \Phi_{P, xy}^f \right| \right| + \frac{1}{\lambda} \mathbb{E} \left[ \mathbb{E}^T \Phi_{P, xy}^f \mathbb{E} \left( \mathbb{E}^T \Phi_{P, xy}^f \right) \right]$$

(49)

It is worth noting that, equations (40), (42), and (49) represent an approximate estimate of FF-SAR resolution. This is because they implicitly assume the spatial diversity array to include regularly spaced elements, in a number sufficient to model peak sections along ground range and Doppler directions as sinc functions. When the number of adopted receivers is low, and receivers are irregularly displaced, the resulting spatial diversity pattern can notably deviate from a sinc-like shape. In this case a viable solution for estimating FF-SAR resolution is the numerical simulation of the radiation patterns (see Section V).

Concluding this section on coherent resolution enhancement it is important to clarify that both the common and the spatial diversity arrays are representative of FF-SAR performance when the effect of perturbing phenomena like topography is negligible or it can be compensated for [12], [52].

B. SNR Improvement

Interpreting coherent resolution enhancement as just the improvement of nominal resolutions of the reference bistatic SAR means limiting FF-SAR capabilities. Indeed, not only $\delta R_g$ and $\delta \alpha$ can be improved, but bistatic response can be drastically modified. As an example, pixel skewing achieved in either squinted monostatic or bistatic SAR geometries can be attenuated. Moreover, even when the sizes of the spatial diversity array are small, thus not allowing for resolution enhancement, additional features can be achieved. This is the case of coherent signal-to-noise ratio (SNR) improvement and high-resolution wide-swath (HRWS) imaging. The latter is fully analyzed in Section IV-C whereas the former is briefly presented herein. Specifically, working with $N$ receivers, as an effect of the coherent combination of (24), the SNR achieved by an FF-SAR is the sum of the SNR of each bistatic receiver. Moreover, if the spatial diversity array is small, so that short baselines are established, no resolution enhancement is achieved, but range variations among the receivers can be neglected, thus making it possible to assume that the SNR is the same for all receivers. So, SNR can be improved up to a factor given by the number of adopted receivers. Finally, for those, short baseline, formations, even though the spatial diversity array is still sparse, the relevant grating lobes are not a matter of concern for the FF-SAR, since they are strongly attenuated by the common array.

C. Null-Steering and HRWS Imaging

Null-steering can be applied to the spatial diversity array for providing FF-SAR array pattern with additional features. Indeed, even when the condition of (22) is set, that is both common and spatial diversity array patterns are steered toward a specific target, further degrees of freedom are available. This is evident from the definition of $E_{SD}(\Delta \mathbf{P}_{xy})$ in (25). Specifically, this represents a single scalar condition affecting the $N$ available $p_i(\mathbf{B}_i)$ weights. Hence, the effects of the spatial diversity array are still able to satisfy an additional $N - 1$ conditions, i.e., a more general beamforming problem can be formulated for the spatial diversity array including both beam and null steering. Following (25), a steering function can be defined

$$\phi (\mathbf{B}_i, \Delta \mathbf{P}_{xy}) = \exp \left[ -j \left( \frac{2\pi}{\lambda} \mathbb{E} \left( \mathbb{E}^T \Phi_{P, xy}^f \right) \mathbb{E} \right) + \Delta \mathbf{P}_{xy} \mathbb{E} \left( \mathbb{E}^T \Phi_{P, xy}^f \right) \right]$$

(50)

and adding null-steering constraints to the spatial diversity array leads to the following problem:

$$\begin{bmatrix}
p (\mathbf{B}_i, \phi (\mathbf{B}_i, 0)) = 1 
p (\mathbf{B}_i, \phi (\mathbf{B}_i, \Delta \mathbf{P}_{null, g})) = 0
\end{bmatrix}
\begin{bmatrix}
i = 1, \ldots, N \quad g = 1, \ldots, G - 1
\end{bmatrix}

(51)

where $\Delta \mathbf{P}_{null, g}$ is the $g$th ground location toward which a null of the spatial diversity array must be set. The problem of (51) can be recast in a standard linear form

$$A_{\mathbf{P}_{SD}} = \mathbf{e}_1$$

(52)

where $\mathbf{p}_{SD}$ is the unknown vector

$$\mathbf{p}_{SD} \in \mathbb{R}^{N \times 1} \Rightarrow \mathbf{p}_{SD} = [p (\mathbf{B}_1) \ldots p (\mathbf{B}_N)]^T.$$  

$A$ is the steering matrix

$$A \in \mathbb{R}^{G \times N} \Rightarrow A = \begin{bmatrix}
\phi^T (0) 
\phi^T (\Delta \mathbf{P}_{null, 1}) 
\vdots 
\phi^T (\Delta \mathbf{P}_{null, G-1})
\end{bmatrix}$$

(54)

with

$$\phi (\Delta \mathbf{P}_{null}) \in \mathbb{R}^{N \times 1} \Rightarrow \phi (\Delta \mathbf{P}_{null}) = [\phi (\mathbf{B}_1, \Delta \mathbf{P}_{null}) \ldots \phi (\mathbf{B}_N, \Delta \mathbf{P}_{null})]^T$$

(55)

and

$$\mathbf{e}_1 \in \mathbb{R}^{G \times 1} \Rightarrow \mathbf{e}_1 = [1 \ 0 \ldots 0]^T.$$  

(56)

If $G \leq N$, it is well known that one solution of (52) is

$$\mathbf{p}_{SD} = A^H (A A^H)^{-1} \mathbf{e}_1$$

(57)

where $A^H (A A^H)^{-1}$ is the pseudoinverse matrix of $A$.

Based on the introduced beamforming problem, HRWS imaging can be formulated as an application of FF-SAR, which aims at overcoming the close relationship existing between the azimuth resolution and the width of the unambiguous swath [9]. For either a monostatic or a bistatic SAR, high resolution in the Doppler direction requires a wide Doppler bandwidth, which, in turn, implies a high PRF for proper sampling. On the other hand, high operating PRF values lead to strong limitations on the unambiguous
swath intervals in range, due to range ambiguities. Hence, a high azimuth resolution implies a small unambiguous swath width and vice versa. An FF-SAR system is able to break this inverse relationship by jointly exploiting samples gathered by several platforms [25], [26]. In this concern, the array theory is, again, a very powerful tool to represent FF-SAR application to HRWS. Namely, if the PRF required to achieve an assigned large swath width is too low, proper sampling of the Doppler bandwidth cannot be performed. Consequently, the common array $E_C(\Delta P_{xy})$ shows grating lobes which are referred to as azimuth, or Doppler, ambiguities [9], [55]. Those gratings are placed in locations $P_\delta$ corresponding to Doppler frequencies that are offset by integer multiples of the PRF from the Doppler frequency of $\tilde{P}$. According to (10)

$$\frac{1}{\lambda} v_T^T \begin{bmatrix} P_{Tx}(0) - P_{A,d} \end{bmatrix} - \frac{1}{\lambda} v_R^T \begin{bmatrix} P_{Rx}(0) - P_{A,d} \end{bmatrix} = f_P \begin{bmatrix} \tilde{P}, \delta \end{bmatrix} + d \text{ PRF} \quad d = \pm 1, \pm 2, \ldots$$

Nonetheless, if null steering of the spatial diversity array is applied, with nulls corresponding to the locations of the ambiguities, grating lobes of the common array are suppressed in the resulting FF-SAR array pattern.

V. SIMULATION RESULTS

The concepts of radiation pattern and array synthesis are first applied to a monostatic-bistatic SAR configuration. This is the case of STEREOID mission [30] conceived as a companion satellite augmenting Sentinel-1D capability. The space segment of the mission consists of two identical sub-500-kg class spacecraft carrying a receive-only radar instrument as the main payload and flying in a re-configurable formation with Sentinel-1D. Both monostatic and bistatic images are thus available for the observed areas. The augmentations are based on the use of several azimuth lines of sight to support precise measurements of small-scale motion and deformation fields of the ocean surface, glaciers and ice sheets, and solid earth. Table I lists the main parameters of Sentinel-1D that are used for the simulation of the monostatic radiation pattern.

For the sake of simplicity, computation is performed introducing a reference frame with origin in the simulated point target, z-axis as the local vertical direction, (x, y) as the local ground plane, with y-axis along Sentinel-1D platform velocity. The simulated radiation pattern is depicted in Fig. 2. The expected behavior of the point target response of a monostatic SAR is correctly reconstructed [Fig. 2(a)] as a 2-D sinc function with orthogonal axis aligned with ground range and azimuth directions according to monostatic iso-range and iso-Doppler lines [Fig. 2(b)]. The analysis of ground range and azimuth cuts [Fig. 2(c) and (d)] of the radiation pattern confirms that the introduced model methods the point target response in a proper way leading to 3.0-m ground range and 6.2-m azimuth resolution, respectively. Performance parameters like PSLR and ISLR are also in line with image focusing by rectangular weighting functions.

| Parameter                        | Value               |
|----------------------------------|---------------------|
| Wavelength                       | 0.055 m             |
| Satellite Altitude               | 693 km              |
| Tx Signal Bandwidth              | 80 MHz              |
| Incidence Angle                  | 33.7°               |
| Tx Antenna Size                  | 12.3 m x 0.82 m     |
| Tx Pulse Length                  | 30 μs               |
| Monostatic CPI                   | 0.42 s              |
| PRF                              | 1.49 kHz            |
| Rx Antenna Size                  | 1.3 m x 0.8 m       |
| Rx Along-track Baseline          | 345 km              |
| Bistatic CPI                     | 0.56 s              |
| Tx Position                      | [-452 km, -0.03 km, 678 km] |
| Tx Velocity                      | [0 km/s, 7.59 km/s, 0 km/s] |
| Rx Position                      | [-451 km, -344 km, 670 km] |
| Rx Velocity                      | [-0.02 km/s, 7.58 km/s, 0.4 km/s] |

TABLE I Simulation Parameters for Sentinel 1D and STEREOID Monostatic-Bistatic System [30].

Bistatic SAR imaging performance can be also analyzed by the relevant radiation pattern. Fig. 3 shows the results considering one bistatic receiver of STEREOID placed along the same orbit of Sentinel-1D with a mean anomaly difference realizing an along-track separation of more than 340 km (see Table I). As expected, the 2-D radiation pattern [Fig. 3(a)] is still a 2-D sinc function but the relevant axes are no longer orthogonal, being characterized by a skew angle of about 105° which is confirmed by the analysis of iso-range and iso-Doppler curves [Fig. 3(b)]. Cuts of the 2-D radiation pattern are also analyzed along both iso-Doppler [Fig. 3(c)] and iso-range [Fig. 3(d)] lines, where the natural sinc-like shape can be recognized. The estimated point target response widths are, respectively, 2.9-m along the iso-Doppler line and 5.2-m along the iso-range one. The results agree with (33) and with the gradient method.

In detail, the latter computes the distance between two iso-range (iso-Doppler) curves separated by a time delay (Doppler frequency) of $\chi / W$ ($\chi / CPI$). This distance is shorter than the distance between the same iso-range (iso-Doppler) lines computed along the iso-Doppler (iso-range) curve by a factor depending on the skew angle as shown in Fig. 4. So, one can retrieve the above reported values of 2.9 and 5.2 m by (33) and then multiplying the estimated ground range and Doppler resolution by the sine of the skew angle.

As an example of a multistatic FF-SAR mission, a satellite formation including six microsatellites is simulated. One platform is a Tx/Rx one whereas the other five satellites are Rx-only. The system has been preliminarily designed to operate from an altitude of 500 km and to guarantee −25-dB noise equivalent sigma zero (NESZ) within a swath width of 30 km by just 1-kW peak power and 2-m² antenna area. The main system parameters are listed in Table II.

The formation is characterized by a dominant along-track baseline component but residual vertical and cross-track baselines are present, which are used to partially decouple the collision risk from the along-track design [56].
Fig. 2. Simulated monostatic SAR radiation pattern for Sentinel-1D. (a) Point target response. (b) Iso-range (thick) and iso-Doppler (thin) curves. (c) Ground range cut of the 2-D radiation pattern along the thin dotted line of (b). (d) Azimuth cut of the 2-D radiation pattern along the thick dotted line depicted of (b). Bold line in (a) indicates the $-3$-dB curve.

TABLE II
Simulation Parameters for HRWS Through a Formation of Microsatellites

| Parameter                | Value                                      |
|--------------------------|--------------------------------------------|
| Wavelength               | 0.031 m                                    |
| Satellite Altitude       | 500 km                                     |
| Incidence Angle          | 25.5°                                      |
| Tx Antenna Size          | 2 m x 1 m                                  |
| CPI                      | 0.98 s                                     |
| PRF                      | 4.139 kHz                                  |
| Rx Antenna Size          | 2 m x 1 m                                  |
| Tx Position              | [-25 km, -0.01 km, 495 km]                 |
| Tx Velocity              | [0 km/s, 7.69 km/s, 0 km/s]                 |
| Number of Receivers      | 6                                          |
| Along-track Baselines    | [-313 m, -209 m, -103 m, 0 m, 92 m, 195 m] |
| Vertical Baselines       | [35 m, 24 m, 17 m, 9 m, -18 m, -40 m]       |
| Cross-track Baselines    | [21 m, -2 m, 22 m, 0 m, -3 m, 44 m]        |

The working principle is based on the application of beamforming on the signal collected by the six receivers to obtain HRWS imaging and to exploit the residual redundancy to work with low Tx power. Indeed, the assigned antenna area and swath width set timing requirements that cannot be easily fulfilled by a single-platform, single-channel system. Nominal operations of an FF-SAR system implementing the principle of HRWS imaging involves data collection from receivers working with pure along-track separations without any orthogonal baseline component. Such an assumption can be made for HRWS systems operating from a single-platform using multichannel antennas as receivers, e.g., [31], but it is unrealistic for an FF-SAR. Cross-track and vertical baseline components generate additional phase contributions depending on surface topography too. Therefore, beamforming to be applied on the received signals must include a correction accounting for the topographic phase [23].

Fig. 5(a) shows the simulated common radiation pattern, i.e., the radiation pattern representing the point target response of the Tx/Rx satellite, along an iso-range line. Since the Doppler bandwidth is undersampled, azimuth ambiguities arise. Nonetheless, according to Section IV-C
Fig. 3. Simulated bistatic SAR radiation pattern for one receiver of STEREOID mission with large along-track baseline. (a) Point target response. (b) Iso-range (thick) and iso-Doppler (thin) curves. (c) Ground range cut of the 2-D radiation pattern along the thin dotted line of (b). (d) Azimuth cut of the 2-D radiation pattern along the thick dotted line depicted of (b). Bold line in (a) indicates the −3-dB curve.

Fig. 4. Illustration of the skewing effect in bistatic SAR imaging.

FF-SAR array pattern is shown in Fig. 5(c). Efficient suppression of azimuth ambiguities is obtained. With reference to Fig. 5(b), it is worth noting that the spatial diversity array is affected by strong grating lobes. However, as discussed in Section IV-C, those grating lobes fall outside the main beam of the common radiation pattern (see Fig. 6). Hence their effect on the quality of the resulting FF-SAR image is negligible.

The above-presented example dealt with a multistatic system in which FF-SAR is used to improve the performance of a monostatic, single-channel SAR in terms of swath width and SNR. Nominal resolutions of the Tx/Rx monostatic satellite are unaltered (Fig. 6). However, FF-SAR features can be exploited to realize a multistatic system able to bypass bistatic SAR imaging limitations, e.g., coarse resolution and pixel skewing, but also, depending on system parameters, narrow unambiguous swath. Array theory, once again, is a valuable tool for assessing FF-SAR capabilities in this ambit.

Another case considered is the Passive SAR satellite constellation (PASSAT) concept [36], in which transmitters of opportunity are ground-based broadcasting stations, in
Fig. 5. Simulated radiation pattern for a formation of microsatellites. 
(a) Common radiation pattern. (b) Spatial diversity radiation pattern. (c) FF-SAR point target response. System parameters listed in Table II.

Fig. 6. Zoomed view, around target location of the radiation pattern for a formation of microsatellites.

TABLE III
Simulation Parameters for an FF-SAR Based on DVB-T Signal Transmission (Tx Signal Parameters Adapted From [36])

| Parameter                     | Value                         |
|-------------------------------|-------------------------------|
| Wavelength                    | 0.46 m                        |
| Tx Signal Bandwidth           | 7.7 MHz                       |
| Symbol Length                 | 896 μs                        |
| Tx Position                   | [-7.78 km, -7.78 km, 0.23 km] |
| Rx Position                   | [0, 0, 400 km]                |
| Rx Velocity                   | [0 km/s, 7.67 km/s, 0 km/s]   |
| Rx Antenna Aperture           | 5°                            |
| CPI                           | 4.54 s                        |
| Number of Receivers           | 7                             |
| Along-track Baselines         | [-300 m, -200 m, -100 m, 0 m, 100 m, 200 m, 300 m] |
| Cross-track Baselines         | [-5700 m, -5130 m, -3420 m, 0, 1140 m, 2850 m, 3990 m] |

form of DVB-T signals and receivers are onboard low earth orbit (LEO) satellites. Receivers are assumed to be arranged into a satellite constellation to achieve the desired temporal and spatial coverage.

The imaging performance of the bistatic system including a single DVB-T station and a single LEO receiver is analyzed in [36]. Indeed, DVB-T signals show a complex structure able to transmit compressed digital audio, video, and other data using coded orthogonal frequency division multiplexing (COFDM): Data are delivered in a series of discrete blocks or symbols at the so-called symbol rate. Nonetheless suitable processing can be applied [36] allowing one to interpret single symbols as radar pulses characterized by about 8-MHz bandwidth. Symbol duration, useful for radar imaging is about 896 μs which leads to a maximum equivalent PRF of about 1.1 kHz. As an example of bistatic geometry for PASSAT, a generic DVB-T broadcasting station is assumed as a 230-m high tower illuminating a target which is about 11-km distant. A nadir looking satellite receiver is also simulated orbiting at about 400-km altitude. Further system parameters are listed in Table III. Fig. 7(a) and (b) show, respectively, the bistatic array radiation pattern and iso-range and iso-Doppler lines. The origin of the reference frame is target location and receiver velocity is along the y-axis, with, again, (x, y) as the ground plane. According to the gradient method the resolution along the x-axis is 48.8 m, whereas the resolution along y-axis is 4.7 m, and a significant skew angle of 135° arises. Those values agree with the simulated array radiation pattern of Fig. 7(a).

Furthermore, owing to the limited equivalent PRF, azimuth undersampling occurs. The Doppler bandwidth is about 1.45 Hz, so azimuth or Doppler ambiguities dominate the radiation pattern [see Fig. 7(c)].

Imaging performance is notably improved when each receiver of PASSAT constellation is replaced by an FF-SAR. In detail, provided that a sufficient number of properly separated formation flying receivers can be deployed, the resolution along the x-axis can be enhanced and the first azimuth ambiguities can be suppressed. According to Table III, a
formation of seven satellites is simulated, characterized by a dominant separation along the $x$-axis and residual baseline components along $y$-axis. Based on this geometric arrangement, the FF-SAR array radiation pattern can be computed, steering the beam of the spatial diversity array towards target location and forcing nulls in the direction of the first azimuth ambiguities.

Fig. 8 shows the estimated radiation patterns around target location. According to the simulated baseline components the spatial diversity array pattern [Fig. 8(b)] features a
narrow peak along the x-axis but very limited discrimination capabilities along y-axis.

As a result, the realized FF-SAR achieves much better resolution [Fig. 8(a)] compared to the case of a single bistatic receiver [Fig. 7(a)]. Fig. 8(c) shows the cut of the radiation pattern along x-axis. FF-SAR point target response width is about 10 m, together with $-9$-dB PSLR. Concerning the latter value, it is worth noticing that, because of the limited number of receivers, the spatial diversity array pattern is far from showing a sinc-like behavior. Hence the cost to pay for a significant improvement of the point target response width by using several receivers is a degradation of the side-lobe level.

Fig. 9 illustrates the ambiguity rejection capabilities of the simulated FF-SAR. Differently from the former example of short formation (Fig. 5), the capability of null steering to reduce the ambiguous power is weakened. This is because setting a null in the radiation pattern of a longer array naturally affects a smaller image portion [see Fig. 9(d)]. Nonetheless ambiguities in the FF-SAR image are more than 26-dB lower than the relevant target which can be acceptable for imaging purposes.

VI. CONCLUSION

Imaging properties of monostatic, bistatic, and multistatic SAR can be recast into a single theoretical framework by the array theory. Indeed, when a single receiver is considered, the introduced common array pattern models time delays and Doppler frequencies of the observed targets. Moreover, for a multistatic SAR the effect of the physical separation among the receivers is described by the spatial diversity array. This article focuses on a specific realization of a multistatic SAR, referred to as FF-SAR. This is based on a cluster of satellite receivers flying in coordinated motion with separations in both along-track and cross-track/vertical directions. The introduced methodology allows the measurements of the performance improvement of an FF-SAR with respect to more traditional systems like monostatic and bistatic SAR. Both proper selection of baselines among the receivers and beamforming of the spatial diversity array contribute to FF-SAR imaging. However, presented simulations confirmed that, even though the spatial diversity array is, by definition, a sparse array, receiving platforms must not be evenly or regularly spaced, hence tight control of relative positions is not required. Baselines among the
receivers can drift. This does not degrade imaging capabilities significantly if suitable solutions for beamforming can be applied. The theoretical and simulation analyses of this article have some limits depending on the relevant assumptions. Straight path and constant velocities were assumed for both the transmitter and the receivers within the coherent processing interval. This is a good approximation to characterize imaging performance, but it is inadequate for some bistatic and multistatic focusing steps, like motion compensation, in which the curvature of the orbits must be accounted for. Hence, FF-SAR performance estimated in the present work is valid if suitable solutions are applied for bistatic SAR focusing and beamforming, which are already available in the literature. The proposed signal model was derived considering a flat scene, so, if orthogonal baselines are involved, the model can be applied when topography can be neglected or reduced, locally, to a constant slope. No time and clock synchronization errors were included in the analysis. However, their effects on FF-SAR performance could be simulated by the derived FF-SAR signal model by injecting the terms of the common and the spatial diversity arrays with various realizations of these errors. Similarly, even though presented results did not take into account errors in the knowledge of the relative positions among the receivers, one could compute beamforming weights using baseline vectors that are different from the simulated ones to model the accuracy of the relative positioning system. Future activities are planned toward the generalization of the signal model and of the way simulations are carried out for representing error sources which may limit true FF-SAR imaging.

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