Research Article

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Experimental determination and modeling of flow curves of xanthan gum solutions over a large range of shear rates

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Abstract: The viscosities of solutions formulated with xanthan gum and xanthan gum with whey protein isolates are experimentally characterized and modeled over a wide range of shear rates \([10^{-3} \text{ to } 10^5 \text{ s}^{-1}]\). As shown by numerous studies \([1, 2]\), the generation of vortices in the cone-plate geometry is making viscosity measurements beyond a certain shear rate unreliable. In the present work, an innovative technique, based on microfluidics and developed by the company Formulaction, has been employed to extend to high shear rates, the viscosity flow curve obtained with a rotational rheometer. The main highlights of this study are firstly, to propose a scaling law for the inertial transition in the cone-plate geometry for different diameters and angles through the determination of the maximum shear rate at which one can expect a true viscosity value. Secondly, the high shear rate measurements allow the determination of the second Newtonian plateau for these solutions thanks to the Williams-Carreau model. An attempt for the second plateau modeling is proposed following the concept of an intrinsic viscosity in the high shear equilibrium. In the same way, other fitted parameters from the Williams-Carreau law are modeled as a function of the polymer concentration. This procedure allows to provide a predictive model for the rheological behavior of xanthan gum-based solutions used in high shear processes like high pressure homogenization, emulsification, foaming, microfluidics, etc in food, pharmaceutical or cosmetics applications.

Keywords: Polymer rheology, high shear rates, viscosity modeling, shear thinning, xanthan gum

1 Introduction

Xanthan gum is one of the hydrocolloids most extensively used in food and non-food applications mainly for viscosity enhancement, emulsion stabilization, temperature stability and pouring properties \([3, 4]\). Xanthan gum solutions present a marked shear thinning behavior \([5, 6]\) which is enhanced by the polymer concentration. Depending on the polysaccharide concentration, various concentration regimes can be encountered. In the “dilute regime” there is little or no steric effects and solutions tend to be slightly shear-thinning \([7]\). Beyond the critical concentration \((C^*)\), physical interaction between molecules takes place \([8]\) and the system goes into a “semi dilute regime” where the macromolecules start to interact, but internal forces are still dominated by polymer-solvent interactions \([9]\). Above a second critical concentration value \((C^{**})\), the system is in the “concentrated regime” where important entanglements occur and viscosity increases quickly with polymer concentration, leading to a pronounced shear-thinning behavior \([7]\).

Although \(C^*\) and \(C^{**}\) provide useful information to predict the dilution regime, there are no well-defined values, but rather a range of concentrations where systems gradually change from one concentration regime to another. The calculation of these critical values always implies a certain bias since they depend on the experimental technique employed \([8, 10]\). Additionally, in the case of xanthan, a natural polysaccharide, its source, composition and thermal history might as well affect the rheological behaviors of solutions prepared with this polymer \([11]\). As a matter of fact, for xanthan solutions, different values for \(C^*\) and \(C^{**}\) has been found in the literature. For instance, \(C^*\) is found to...
have values of 0.02% [12] 0.0126% [13] 0.007% [14] while reported values for C** include 0.078% [13] and 0.2% [14], among others.

Visualizing the transitions between the aforementioned regimes is possible by plotting log \( \eta_{sp} \) vs \( \log [\eta] \), where \( \eta_{sp} \) is the specific viscosity, \( \eta_{sp} = \eta_{rel} - 1 \), \( c \) is the concentration and [\( \eta \)] is the intrinsic viscosity. It is then possible to notice that the specific viscosity follows a power law as presented in equation 1 [15, 16], where \( k \) is a constant and \( p \) a parameter that represents the slope having values between 1 and 2 for the dilute regime, 2 to 3 for the semi dilute regime, and 3 to 5 for the concentrated regime [15]. The term \( c[\eta] \) known as the overlap parameter [17] provides information about the system concentration regime. Generally, at values of \( c[\eta] \) between 0.7 and 1.5 the transition from dilute to semi dilute regime is observed and at values of around 6-7 the systems change from semi dilute to a concentrated state [13].

\[
\eta_{sp} = k(c[\eta])^p
\]  

(1)

The intrinsic viscosity \( [\eta] \), which provides information on the hydrodynamic volume occupied by the individual isolated polymer molecules [18], depends mainly on the molecular weight and polymer conformation [15]. The models proposed by Huggins [19] (eqn. 2), Kraemer [20] (eqn. 3), Schulz & Blaschke [21] (eqn. 4) and Tanglerptaibul & Rao [22] (eqn. 5) are widely used to determine the value of the intrinsic viscosity.

\[
\frac{\eta_{sp}}{c} = [\eta] + k_1[\eta]^2c
\]  

(2)

\[
\frac{\ln \eta_{sp}}{c} = [\eta] + k_2[\eta]^2c
\]  

(3)

\[
\frac{\eta_{sp}}{c} = [\eta] + k_{SB}[\eta]^2\eta_{sp}
\]  

(4)

\[
1 - \frac{1}{\eta_{rel}} = [\eta]c
\]  

(5)

By extrapolation to a diluted state where \( c \) tends to zero, the second term of the Huggins equation can be neglected [23] and a simplified expression (eqn. 6) allows to easily determine [\( \eta \)] as the slope of the plot \( \eta_{rel} \) vs \( c \).

\[
\frac{\eta_{sp}}{c} = [\eta]
\]  

(6)

The marked shear-thinning behavior of xanthan solutions is of great technological interest as it allows tuning of the rheological properties when dissolved. Products with a high viscosity at rest can be obtained, ensuring a better stability. On the other hand, these solutions exhibit low viscosities when processed under high shear rates facilitating handling of fluid flows and minimizing energy consumption. Characterization of the viscosity profile of xanthan solutions is therefore crucial to design, understand and take advantage of their rheological behavior in industrial processing.

The viscosity of solutions is commonly evaluated by using flow tests and is mainly based on the use of rotational rheometers (also known as shear rheometers). They are usually equipped with several tool geometries, the best suitable choice in each rheological study depending on the properties of fluids and on the desired range of shear stress. The cone-plate is the most common geometry for determining viscoelastic properties of polymeric fluids [24]. For low to medium shear rate ranges \( 10^{-3} \text{ to } 1000 \text{ s}^{-1} \), this geometry provides reliable data. However, secondary flows may occur beyond a certain shear rate [25], especially since the viscoelastic behavior is pronounced, so that the end of the flow curve does not reflect the viscosity but the inertial stress [26]. The “second Newtonian plateau” observed for the xanthan solutions may often be an artefact.

Mixing, mass transfer or dispersion of immiscible fluids are operations that are actually intensified through the implementation of high shear rates in many industrial units such as rotor-stators [27], extruders [25], spray dryers [28] and high pressure homogenizers. In this kind of processes, encountered shear rates can reach an order of magnitude of around \( 10^5 \text{ s}^{-1} \). Even higher shear rates can be reached in innovative applications using microfluidics [25, 29–32].

Ground-breaking techniques are being developed for measuring viscosity at high shear rates using microsystems in laminar straight flow conditions. In some apparatus, as in the Fluidicam\textsuperscript{TM} used here, the unknown viscosity of a fluid can be deduced from the observation of the coflowing of this fluid with a reference one, using image analysis [33, 34]. The fluid viscosity can also be deduced from a more classical way, based on the measurement of the pressure drop in the channel using pressure sensors [35]. However, due to the small scale of microchannels, these techniques are obviously less suitable and hence less accurate for viscosity measurements at low shear rates. Considering the two methods described above, the lower limit of shear rates available for measurement is about \( 10^2 \text{ s}^{-1} \).

For characterizations over a very large range of shear rates, \( i.e. \) from \( 10^{-2} \text{ s}^{-1} \) and up to \( 10^5 \text{ or } 10^6 \text{ s}^{-1} \), implementation of complementary characterization techniques is therefore usually needed; the literature is not profuse on this subject. Pipe & McKinley [36] provided an
in-depth study on the subject, but, from a technical point of view, their discussion does not cover all of the experimental tasks that experimenters might face. Some studies \([4, 35, 37–39]\) have reported values of the infinite-shear viscosity \((\eta_\infty)\) of xanthan gum solutions estimated at shear rates higher than \(10^3\ \text{s}^{-1}\). However, there is no discussion over these determinations at high shear rates and even in some cases, some important methodological information is missing. A couple of studies have investigated more exhaustively the characterization of viscosity at high shear rates for both Newtonian and non-Newtonian fluids using modifications of the known parallel plate geometry in conventional rotational rheometry \([2, 40–42]\).

This study aims at extending the knowledge in the field of viscosity characterization of polymeric fluids over a large range of shear rates by exploring two complementary techniques (rotational rheometry and microfluidic rheometry). The case of xanthan gum, a polymer encountered in numerous industrial applications, is selected for this purpose. Solutions from this polymer have been prepared in the concentration range \(0.08–0.5\%\ \text{w/w}\) relevant for food applications.

The main objective of this work is to propose a complete methodology to obtain relevant viscosity data in an extended range of shear rates \((10^{-3} \text{ to } 10^5\ \text{s}^{-1})\), in order to model the flow curves in the given range of concentrations. For a given solution, the deviation of the flow curves obtained using the two techniques provides a criterion for the appearance of the secondary flow in the cone-plate in terms of a critical value of the Reynolds number. The microfluidic rheometer employed is able to measure the viscosity at sufficiently high shear rates to enable the determination of the second Newtonian plateau by using the Williams-Carreau law. Finally, it is proposed to model the rheological parameters obtained from the Williams-Carreau fitting as a function of the polymer concentration. In addition, the same approach is applied to xanthan gum solutions with added whey protein isolates (WPI) in order to study the case of a mix of biopolymers that is also of industrial interest.

2 Materials and methods

2.1 Preparation of model solutions

2.1.1 Xanthan gum solutions

A commercial xanthan gum, XG, powder (Ketrol® AP from Kelco) and demineralized water were used for the preparation of the solutions. The powder was added gradually to the solvent at room temperature in a 2 L mixing vessel under agitation using an overhead stirrer (RZR 2020 from Heidolph instruments). The solutions were formulated at four concentrations (0.08, 0.2, 0.4 and 0.5% w/w) commonly encountered in food and non-food applications \([3]\). During the gradual addition of xanthan gum powder, speed agitation was manually monitored between 100 to 600 rpm in order to avoid air incorporation or formation of lumps. Then, the rotational speed was kept at 300 rpm for 4 hours to achieve complete dissolution and homogenization. No preservative agent was added, and solutions were then stocked at \(4\degree\ \text{C}\) until further characterization. Solutions are named according to the xanthan concentration: 0.08% (XG008), 0.2% (XG02), 0.4% (XG04) and 0.5% (XG05).

2.1.2 Whey protein isolates-xanthan gum solutions

Addition of proteins into a xanthan gum solution is interesting for the tensioactive effect as investigated in a previous study carried out in our laboratory for the manufacturing of food foams using an innovative microfluidic technology \([31]\). Therefore, solutions containing whey protein isolates (WPI) and xanthan gum (XG) are considered in this study to account for the presence of proteins. The WPI (Pronativ® 95 from Lactalis France) was mixed with xanthan gum (Ketrol® AP from Kelco) and then added to demineralized water under agitation following a similar protocol as for the xanthan gum solutions described above. The WPI concentration was set at 3% w/w while four concentrations were employed for the xanthan gum: 0.2, 0.35, 0.4 and 0.5% w/w. Solutions are named according to the concentrations of XG and WPI (WPI3XG02, WPI3XG035, WPI3XG04 and WPI3XG05).

2.2 Solution viscosity characterization

Two different rheometric techniques were employed in this study to characterize the viscosity of the solutions over a wide range of shear rates. A rotational rheometer was used to measure the viscosity at low and medium shear rates whereas a microfluidic rheometer from the company Formulaction (France) was used for the viscosity measurements at high shear rates.
2.2.1 Rotational rheometer

A rotational rheometer (AR 1000, TA Instruments) was used with stress-imposed procedures in the range of $10^{-3}$ – 40 Pa during 5 min to characterize viscosity in the shear rate range $10^{-3}$ to $10^{3}$ s$^{-1}$. The considered duration was beforehand tested to provide time independent results. Two cone-plate geometries were used for the viscosity determination of XG solutions; one having a diameter of 60 mm with an angle of $2^\circ$ (60-2) and another one having a diameter of 40 mm and an angle of $4^\circ$ (40-4). WPIXG solutions are only characterized with the geometry 40-4. All samples were tested at 20$^\circ$C and measurements were made in triplicate.

2.2.2 Microfluidic rheometer

A microfluidic rheometer (FLUIDICAM Rheo™ from Formulation, France) was used for viscosity determinations at high shear rates ($>10^3$ s$^{-1}$). The principle of this device is based on establishing a cocurrent fully developed laminar flow (Figure 1) between the studied fluid (sample fluid) and a Newtonian reference fluid whose viscosity is known. The relative section occupied by the fluids is proportional to the product of the viscosity ratio and the flowrate ratio (eqn. 7) [33, 34].

$$ \frac{W}{W_R} = \frac{\eta_{app}}{\eta_R} \frac{Q}{Q_R} $$

In order to determine the true viscosity ($\eta_{true}$) from the apparent viscosity ($\eta_{app}$) obtained from equation 7, equation 8 is used.

$$ \tau = \eta_{app} \dot{\gamma}_{app} = \eta_{true} \dot{\gamma}_{true} $$

As the channel height is small compared to channel width, as well as to the respective widths occupied by the two fluids, the apparent shear rates in laminar flows can be estimated as in a 2D flow (eqn. 9):

$$ \dot{\gamma}_{app} = \frac{6 (Q)}{(w h^2)} $$

where $Q$ is the volume flow rate of the concerned fluid, $h$ the height of the channel and $w$ the width occupied by the fluid [43].

The shear stress ($\tau$) was determined using the apparent viscosity and apparent shear rates measured during experimentation. The true shear rate ($\dot{\gamma}_{true}$) in a rectangular duct was then calculated from the Weissenberg-Rabinowitsch-Mooney equation [44]. The term $\frac{d \ln \dot{\gamma}_{app}}{d \ln \tau}$ corresponds to the slope of the plot $\ln \dot{\gamma}_{app}$ vs $\ln \tau$. Finally, the true viscosity was obtained from equation (10):

$$ \dot{\gamma}_{true} = \frac{\dot{\gamma}_{app}}{3} \left[ 2 + \frac{d \ln \dot{\gamma}_{app}}{d \ln \tau} \right] $$
2.3 Modeling the solutions viscosity and correlation with polymer concentration

2.3.1 Determination of a critical Reynolds number $Re_c$ using a cone-plate geometry

It is well known that due to centrifugal forces, flow recirculations (namely secondary flow or Taylor vortices) may take place when using a cone-plate geometry. The concern is to have a quantitative criterion for the onset of these instabilities that supports the validity of the measurements. Several authors have discussed this problem either using empirical means or by developing analytic or numerical calculations [1, 45–47]. However, there is still no universal simple way to predict the onset of instabilities for any fluid and any cone-plate geometry as easily as is in the Couette flow. Therefore, in the present study, we have developed a simple semi-empirical methodology to identify the region of shear rates where instabilities are likely to appear when using the cone-plate geometry. To give more weight to this approach, by analogy with the Taylor number for Couette flow, a rotational Reynolds number is computed to characterize the limit of the onset of instabilities for the different combinations of geometries and solutions.

This conventional Reynolds number is defined for rotational devices used in process engineering [48], like stirred vessels; it is designated as ‘rotational Reynolds number’ in the following:

$$Re = \frac{\rho N D^2}{\eta} \quad (11)$$

Here $\rho$ is the solution density, $D$ the diameter of the cone geometry, and $N$ the rotational speed, all variables are in International System of Units (SI). In rotational flows, the Reynolds number is an internal measure of the ratio between centrifugal and viscous forces. One can notice that it is very similar to the Taylor number and can be considered as that for a given geometry. Reynolds numbers based on centrifugal forces were previously used by several authors like Turian [1] who developed analytical solutions for Newtonian and non-Newtonian flows in cone-plate systems and Fewel and Helluns [45] who characterized secondary flows of Newtonian fluids in cone-plate viscosimeters.

The rotational critical Reynolds number ($Re_c$) (eqn. 13) and the critical rotational speed defined by equation 12 were determined by the shear rate $\dot{\gamma}_{\text{max}}$ where the rheometer and the Fluidicam flow curve diverged. Equation 12 derives from the calculation of the uniform shear rate in the cone-plate flow.

$$N_c = \frac{\dot{\gamma}_{\text{max}} \theta}{2\pi} \quad (12)$$

The two datasets (rotational rheometer and microfluidic rheometer) were plotted on a same graph of viscosity vs shear rate and each one fitted by the Williams-Carrreau law given in equation 14, where $\eta$ stands for the fluid viscosity at the current shear rate $\dot{\gamma}$, $\eta_0$ is the zero-shear viscosity (first plateau), $\eta_\infty$ the infinite shear viscosity (second plateau), $m$ is a constant related to the flow index, and $\lambda$ is a time constant representing the shear rate where the rheological behavior changes from the 1st Newtonian plateau to the shear-thinning range.

$$\frac{\eta - \eta_0}{\eta_0 - \eta_\infty} = \frac{1}{1 + (\lambda \dot{\gamma})^2}^m \quad (14)$$

The diverging region between the two flow curves determines the maximum shear rate $\dot{\gamma}_{\text{max}}$ beyond which flow instabilities are likely to appear due to the centrifugal forces. The maximum shear rate was estimated at the point where the two models diverged by more than 10%. An example of this approach is given in Figure 2, for 0.08% w/w xanthan gum solution and the 60-2 cone-plate geometry.

![Figure 2: Determination of the onset of inertial effects for xanthan gum solution 0.08% w/w using the cone-plate geometry 60-2 (60mm diameter and 2° angle). In legend: viscosity measurements from rotational rheometer (Rot rheo), viscosity measurements obtained with microfluidic rheometer (Micro rheo), model fit for data from rotational rheometer (fit Rot), model fit for data from microfluidic rheometer (fit Rot+Micro), calculated rotational Reynolds numbers (Rot Re), shear rate where instabilities begin to appear (max shear) and calculated critical Reynolds number ($Re_c$).](image-url)
2.3.2 Determination of the fitting rheological parameters of the Williams-Carreau law

In a first step, rheological parameters were determined from the rotational rheometer flow curve. Then, viscosity values above the calculated \( Re_c \) were replaced by the Fluidicam\textsuperscript{TM} data so as to determine a model for the whole range of shear rates: in this approach, \( \eta_0 \), \( \lambda \), \( m \), were kept constant from the first step, and only the second plateau \( \eta_\infty \) was fitted in the second step.

2.3.3 Modeling the fitted rheological parameters of the Williams-Carreau law with polymer concentration

The fitted parameters from the Williams-Carreau model (\( \eta_0 \), \( \lambda \), \( m \), and \( \eta_\infty \)) determined as explained in section 2.3.2 were then correlated with the polymer concentration. For the first Newtonian plateau the viscosity \( \eta_0 \) was fitted to a power-law model (eqn. 15) as presented in [15, 16]. From the literature, the intrinsic viscosity \([\eta]\) for xanthan gum solutions in water is approximately 15.5 m\(^3\)kg\(^{-1}\) [18]. In equation 15, the specific viscosity \( \eta_{sp0} \) is built on the first plateau viscosity.

\[
\eta_{sp0} = k (c [\eta]_0)^p
\]  
(15)

For the second Newtonian plateau \( \eta_\infty \), a linear trend as a function of concentration was observed (eqn. 16). Therefore, an attempt was made to determine an intrinsic viscosity \([\eta]_\infty \) corresponding to the conformation equilibrium at the second plateau. The specific viscosity in this case is built on the infinite-shear viscosity. The model proposed by Huggins [19] when concentration tends to zero reads:

\[
\frac{\eta_{sp\infty}}{c} = [\eta]_\infty
\]  
(16)

For the parameters \( \lambda \) and \( m \), no theoretical groundings were used and these values were fitted with empirical models to evaluate their variation as function of the polymer concentration.

### 3 Results and Discussion

#### 3.1 Determination of the critical Reynolds number

The rotational critical Reynolds number (\( Re_c \)) is estimated at the onset of flow instabilities due to centrifugal forces in the rotational rheometer. As explained in the methodology, the shear rate \( \dot{\gamma}_{\text{max}} \) determining the onset of these instabilities is estimated experimentally where the two model fits (Figure 2) deviate by more than 10%. Then, a critical Reynolds number \( Re_c \) can be computed using equations 12 and 13. This procedure is carried out for all solutions and geometries tested. It is important to recall that the viscosity at high shear rates is characterized with the same microfluidic geometry described in the methodology while two different cone-plate geometries (60-2 and 40-4) are used for the characterization at low to medium shear rates.

Table 1 summarizes the values of \( \dot{\gamma}_{\text{max}} \) and \( Re_c \) found in this study for all the experiments. The \( Re_c \) is dependent on the cone-plate geometry used, with higher values (33-36) for the XG solutions using the geometry 60-2, compared to those obtained with the geometry 40-4 (4-10) for the same solutions. The higher value of \( Re_c \) obtained with the г-
Figure 3: Critical Reynolds numbers for the two cone-plate geometries.

Geometry 60-2 would be the result of a greater diameter leading to more intense centrifugal forces. It is also noticeable how the \( Re_c \) for WPIXG solutions with geometry 40-4 are very close to the values found for XG solutions with the same geometry. This is demonstrating that the rotational Reynolds number, with the meaning of a Taylor number, provides a relevant universal parameter through its critical value \( Re_c \) to predict the inertial transition for a given geometry. Figure 3 presents the rotational critical Reynolds numbers identified for the appearance of secondary flows for the experimental conditions used in this study. The critical Reynolds numbers identified at rather low shear rates (under 150 s\(^{-1}\)) are in fair agreement with the literature\[26\]. The works of Heuser & Krause and that of Sdougos \textit{et al.} \[49, 50\] have studied the local flow structure in a cone-plane geometry and have found that secondary flows might appear at Reynolds numbers as low as 4. With regard to polymer fluids, Kulicke & Porter \[51\] have reported that these flow instabilities might appear from shear rates as low as 5 s\(^{-1}\). Similarly, Davies & stokes \[2\] have reported a Reynolds number of 100 as the limit where the effects of secondary flows are significant. For Newtonian fluids, it has been reported that the inertial disturbances caused by these secondary flows might appear at Reynolds numbers 800 \[46\] for cone angle between 1\(^\circ\) and 4\(^\circ\), which is higher than other results, but it is clear that the viscoelastic behavior plays an important part in this transition.

### 3.2 Determination of the fitting rheological parameters of the Williams-Carreau law

#### 3.2.1 General considerations about flow curves

After elimination of the data from the rotational rheometer that are above of the rotational critical Reynolds number, the viscosities of the solutions are modeled over approximately eight decades (10\(^{-3}\) to 10\(^{6}\) s\(^{-1}\)). The Figure 4 presents the flow curves (markers) and corresponding models (solid lines) for the XG solutions for both cone-plate geometries, 60-2 (Figure 4a) and 40-4 (Figure 4b) as well as for WPIXG solutions with the geometry 40-4 (Figure 4c). The model fitting parameters for all experimental conditions are summarized in Table 2. Figure 4a displays the flow curves for XG solutions at four different concentrations (0.08%, 0.2%, 0.4%, and 0.5% w/w). The marked shear-thinning behavior of the xanthan solutions \[39, 52\] is clear for the four cases, around four orders of magnitude for the viscosity loss. For the most concentrated so-

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### Table 2: Williams-Carreau fitted rheological parameters for all solutions. MADP is the mean absolute percent deviation between experimental data and model.

| Solution  | Geometry | \( \eta_0 \) Pa·s | \( \eta_\infty \times 10^{-3} \) Pa·s | \( \lambda \) s | \( m \) | MAPD % |
|-----------|----------|-----------------|-----------------|--------|------|------|
| XG008     | 60-2     | 0.8             | 1.1             | 9.48   | 0.60 | 11.5 |
| XG02      | 60-2     | 11.5            | 1.5             | 15.4   | 0.79 | 8.46 |
| XG04      | 60-2     | 84.2            | 2.2             | 29.4   | 0.87 | 12.1 |
| XG05      | 60-2     | 146             | 2.3             | 34.8   | 0.87 | 12.7 |
| XG008     | 40-4     | 1.2             | 1.1             | 14     | 0.63 | 8.3  |
| XG04      | 40-4     | 110             | 2.0             | 32     | 0.86 | 17   |
| XG05      | 40-4     | 182             | 2.5             | 42.1   | 0.87 | 14.7 |
| WPI3XG02  | 40-4     | 20.4            | 1.3             | 20.7   | 0.78 | 4.7  |
| WPI3XG035 | 40-4     | 95              | 2.0             | 32.6   | 0.84 | 4.7  |
| WPI3XG04  | 40-4     | 125             | 2.0             | 35.3   | 0.82 | 6.4  |
| WPI3XG05  | 40-4     | 201             | 2.1             | 41.7   | 0.85 | 6.4  |
Modeling viscosity of xanthan gum solutions

3.2.2 Discussion on the second plateau viscosity values

The most delicate point in this study is the relevant determination of the second Newtonian plateau as it is the base of a fair prediction of the viscosity at high shear rates. Some comparisons of our results and previous literature studies are worth to be discussed here, despite the fact that the polymer origin may have an impact on the viscosity values. It is commonly admitted that the viscosity of this second plateau is close to that of the solvent (here water at 20°C being $10^{-3}$ Pa·s). Our actual values allow to qualify this feature more precisely.

Comba et al. [37] have reported a value of $\eta_\infty$ of 0.0020 Pa·s for a XG solution having a concentration of 3 g·L$^{-1}$ (~ 0.3% wt.). This value seems to fit quite well the values found in this study for XG02 (0.2% wt.) and XG04 (0.4%...
wt.) which were in the range (0.0015 – 0.0022) Pa·s. These authors also used two techniques to model the viscosity over a wide range of shear rates. For the evaluations at high shear rates, they succeeded in evaluating viscosity with the parallel plate geometry with small gaps for the solution with concentration 3 g·L$^{-1}$, but this might not be possible for more diluted solutions. Xu et al. [38] also modeled the viscosity of XG solutions at three different concentrations (0.1, 0.25 and 0.5% wt.). For the concentration 0.5%, the authors obtained a $\eta_{\infty}$ of 0.004 Pa·s which is almost two times more than the one found in this study (0.0023 Pa·s) for the same concentration. They used only a rotational rheometer and the characterizations were done at 20$^\circ$C, over a shear rate range from 0.001 to 1000 s$^{-1}$. However, they do not specify the type of geometry used. Another interesting example of the determination of the second Newtonian plateau found in the literature is the study from Mrkowska & Krztoń-Maziopa [39]. In this case, the authors used coaxial cylinders, at 21$^\circ$C and a shear rate range between $10^2$ and $10^3$ s$^{-1}$ for the generation of flow curves of XG solutions having concentrations in the range (0.25 – 1.4) g·L$^{-1}$ (~0.025 – 0.14 % wt.). The infinite shear viscosity (0.00413 Pa·s) of their solution at 0.075% is two times higher when compared with the one (0.023 Pa·s) reported here for the solution XG008 (0.08%). Similarly, for a 0.4% XG solution, Wyatt & Liberatore [14] found a $\eta_{\infty}$ of 0.0051 Pa·s which is much higher than the value, 0.0022 Pa·s, found here for a XG solution at the same concentration (XG04). In this case, the authors used two geometries (cone-plate 60 mm – 1$^\circ$ and concentric cylinders) for the rheological characterizations of their solutions without specifying which one is used for each solution. The fitting parameters were calculated using a shorter shear rate range $10^3$ to $10^5$ s$^{-1}$ which might explain the higher values of $\eta_{\infty}$ predicted in their study.

From the above discussion it is clear that important methodological information is missing for the characterization of viscosity of xanthan gum solutions at high shear rates. In addition, it is noteworthy that reported values for $\eta_{\infty}$ using only traditional rotational rheometric techniques (irrespective of the geometry), are generally twice as large as those found in this study. Therefore, the determinations of the infinite-shear viscosity presented above, done exclusively with data obtained from a rotational rheometer without explicitly considering inertial instabilities, might not be accurately characterizing $\eta_{\infty}$. Nonetheless, recent works [2, 40] are investigating the possibility of extending the range of measurable shear rates using a modified rotational rheometer. This can lead to improvements in the accuracy of high shear rates viscosity determinations for polymer fluids using traditional rheometric techniques. The emerging field of microfluidics is offering an interesting alternative for rheological characterizations at high shear rates. A previous study that explored viscosity characterizations at high shear rates by microfluidic rheometry has been undertaken by Pipe et al. [36]. In their research, these authors were able to model the viscosity of a 0.3% XG solution over the shear rate range $10^{-3}$ – $10^{4}$ s$^{-1}$ at 22$^\circ$C using two conventional geometries (40 mm parallel plates and 60 mm cone-plate) and a microfluidic capillary viscometer. The infinite shear viscosity for this solution was around 0.002 Pa·s which is also in agreement with the range of $\eta_{\infty}$ found in our study between solutions at similar concentrations XG02 (0.0015 Pa·s) and XG04 (0.0022 Pa·s).

### 3.2.3 Effect of WPI protein addition

A comparison between XG and WPIXG solutions can be proposed thanks to the measurements performed with the geometry 40-4 (Figure 4b and 4c). It is noticeable that the addition of another polymer, in this case WPI, significantly increases the value of $\eta_0$ while differences are less for $\eta_{\infty}$. The increase of the solutions zero-shear viscosity when adding WPI stems from a more important phenomenon of steric hindrance between the two polymers. No interaction between the polymers is presumed since no interaction have been identified at WPI concentrations ≤ 4% wt. and XG ≤ 0.5% wt. [56]. Additionally, it has been reported a low interaction of native WPI with other molecules in solution unless they undergo conformational changes, for instance due to heating [57, 58].

### 3.2.4 Effect of the cone-plate geometry

Our data allow to compare the results for the same solutions XG008, XG04 and XG05 for the two cone-plate systems, (see Figures 4a, 4b, 4d and Table 2). Overall, there are no significant discrepancies except for the values of $\eta_0$. The zero-shear viscosity values are systematically lower for the geometry 60-2. This viscosity reduction with a small gap has already been observed in other studies for parallel plate geometry [2]. According to Kamykowski [59], the low shear rates measurement are less affected by the torque limit with the 60-2 system than the 40-4 system, and we consider that the measurements obtained with the greater diameter and smaller angle are more reliable for the final modeling. Nevertheless, the 40-4 measurements are treated in the next section of the study for comparison purposes.
Table 3: Model equations and fitted parameters for the correlations of the rheological parameters with polymer concentration. Adjustment of models in terms of MAPD (mean absolute percent deviation).

| Rheological parameters | Equation | Fitted parameters and model error |
|------------------------|----------|----------------------------------|
|                        |          | XG-60-2° | XG-40-4° | WPIXG-40-4° |
| $\eta_0$               | $\eta_0 = (k[c[\eta]]^p + 1)\eta_{solvent}$ | k = 0.61  | k = 1.19  | k = 2.54  |
|                        |          | p = 2.86  | p = 2.74  | p = 2.62  |
|                        |          | MAPD = 2.76 | MAPD = 3.37 | MAPD = 4.74 |
| $\eta_\infty$          | $\eta_\infty = (c[\eta] + 1)\eta_{solvent}$ | [\eta] = 0.26 | [\eta] = 0.26 | [\eta] = 0.22 |
|                        |          | MAPD = 5.36 | MAPD = 5.63 | MAPD = 8.11 |
| m                      | $m = ac^b$ | a = 0.64  | a = 0.66  | a = 0.73  |
|                        |          | b = 0.21  | b = 0.18  | b = 0.09  |
|                        |          | MAPD = 3.13 | MAPD = 1.09 | MAPD = 1.02 |
| $\lambda$              | $\lambda = ac + b$ | a = 6.20  | a = 6.45  | a = 7.02  |
|                        |          | b = 3.96  | b = 8.34  | b = 7.13  |
|                        |          | MAPD = 3.74 | MAPD = 4.58 | MAPD = 1.65 |

Figure 5: Correlation of the rheological parameters of the Williams-Carreau model with polymer concentration a) zero-shear viscosity ($\eta_0$) b) infinite-shear viscosity ($\eta_\infty$) c) constant related to flow index (m) d) time constant ($\lambda$).
3.3 Correlating the fitted rheological parameters with polymer concentration

The rheological fitted parameters found for each solution presented in the previous section are now modeled as a function of concentration. Figure 5 presents the modeling of $\eta_0$, $\eta_\infty$, $m$ and $\lambda$ for all experimental conditions, and the equation values are recapitulated in Table 3. Model adjustment is evaluated in terms of the mean absolute deviation (MAPD) given in percent.

3.3.1 The first Newtonian plateau viscosity

For the modeling of the first Newtonian plateau $\eta_0$, the equation 15 presented in section 2.3.3 is employed; the purpose here is to use a well-known equation type to model the zero-shear viscosity $\eta_0$ in the range of concentration of our interest and see if errors are acceptable to use this model as a predictive tool for future studies. Equation 15 is handled with the solvent viscosity (water) of $10^{-3}$ Pa·s, and the intrinsic viscosity $[\eta]_0$ of xanthan gum in water taken at $15.5 \text{ m}^3\text{kg}^{-1}$ [18]. The values of the constants $k$ and $p$ are fitted with a solver, leading to a deviation less than 5% (MAPD $\leq 5\%$). The results are presented in Table 3 and displayed in Figure 5a.

The $k$ value is increasing with addition of WPI, while for the constant $p$, similar values are obtained in the range $2.6 - 2.9$ (percent differences $< 10\%$) denoting the end of the semi entangled regime and the beginning of the concentrated regime as stated by Roy [15]. To better visualize the dilution regime of our solutions, we overlay our $\eta_0$ values over the data proposed by Wyatt & Liberatore [14], where the $\eta_0$ is plotted against a wide range of concentrations for salt-free xanthan gum solutions (Figure 6). For concentrations ($c$) $\leq c^*$ the system is in the dilute regime. The region between $c^*$ and $c_e$ corresponds to the semi dilute unentangled regime and concentrations between $c_e$ and $c_d$ belong to the semi dilute entangled regime. Finally, when concentrations are higher than $c_d$, the system attains the concentrated regime. The superposition of our data over this graph clearly suggests that firstly, our data are very close in value and trend with respect to the curve of Wyatt & Liberatore [14], and secondly that most of our solutions are in the concentrated regime.

3.3.2 The second Newtonian plateau viscosity

As stated before, the second Newtonian plateau has not received too much attention despite its interest in numerous industrial processes. In this study we proposed the use of the Huggins model [19], that is, when the system is highly diluted (equation 16). This could be the case in the high shear rate equilibrium since the molecules have completely different conformations and interactions, probably due to a much less hydrodynamic volume compared to the molecules at rest. To our knowledge, no research study has really addressed the study of the hydrodynamic volume of xanthan gum molecules in the second Newtonian plateau. The parameter $[\eta]_\infty$ is fitted to the data that follow a unique linear curve for XG solutions independently of the geometry used (Figure 5b), and the resulting value of $[\eta]_\infty = 0.26$ confirms the former assumption. The global deviation is under 10% (MAPD $\leq 10\%$).

In Figure 5b, it is observed that the presence of proteins is almost negligible at the second Newtonian plateau and a single model could be proposed for the three sets of data. This would indicate that the intrinsic viscosity of the xanthan gum molecules determines the viscosity at high shear rates to a greater extent than in the case of the viscosity at rest ($\eta_0$). An additional study involving more concentrations would be necessary to support this view.

3.3.3 The relaxation time and flow index

The rheological parameters $m$ and $\lambda$ (Figure 5c and 5d) are fitted empirically using adapted models. A power law model provides a good adjustment to $m$ values (MAPD $\leq 5\%$) whereas an affine model gives a better fit for $\lambda$ values (MAPD $\leq 5\%$). The model fitting parameters for these cases can be found in Table 3. For the variable $m$, the two models

![Figure 6: Superposition of zero-shear viscosity values over the $\eta_0$ vs concentration graph developed by Wyatt & Liberatore [14] for several concentrations of salt-free xanthan gum solutions in water.](image-url)
for XG solutions (60-2 and 40-4) are almost the same as expected. The model for the $m$ values for the WPIXG solutions presented the lowest error (MAPD = 1.02%). This was probably due to the fact that these solutions were only characterized with the microdevice having a channel height of 50 µm and not with the one with channel height of 150 µm. The latter is precisely the device providing data in the region where the two flow curves built in section 3.1 diverge ($10^1$ to $10^3$ s$^{-1}$). Therefore, not having data points in this diverging region is what might be accounting for lower error in the case of WPIXG solutions for the parameter $m$.

Concerning the higher errors for $\lambda$ for XG solutions when compared to WPIXG solutions, low-torque limit effects might be at the origin of this. According to the manufacturer the rotational rheometer used in this study has a minimum torque of 0.1 µN·m. As a result, for the less viscous solutions (XG008), data under a shear rate of 0.1 s$^{-1}$ might be less precise. Since $\lambda$ is determined by the transition between the 1st Newtonian plateau and the shear-thinning region (occurring precisely at around 0.1 s$^{-1}$), less precise $\lambda$ values for XG008 solutions might be contributing to the higher error identified for XG solutions.

### 3.3.4 Synthesis of the rheological parameters

In this section, the elements involved in the correlations of the four rheological parameters are recapitulated. In general, the models proposed described quite accurately the experimental data (MAPD < 10%). The most delicate case was the infinite-shear viscosity presenting the higher errors. However, acceptable values were obtained (MAPD in the range of 5 to 9%). Renewed scientific interest and new technological advancements (such as microfluidic rheometry) will certainly help improve precision in measurements and fundamental understanding of molecular behavior at high shear rates.

### 3.4 Evaluation of the quality of the correlations

The correlations proposed in section 3.3 are now evaluated by using them to find the values of the different rheological parameters ($\eta_0$, $\eta_\infty$, $m$ and $\lambda$) and then building a flow curve from these parameters (model fitting). Figure 7 presents the adjustment of these model fits (solid lines) to the experimental data (markers) for the XG solutions with the geometry 60-2 and for the WPIXG solutions with the geometry 40-4. The model fits adjust well the experimental data. However, some data around a shear rate range between 100 and 1000 s$^{-1}$ slightly deviate from the model fits. These points correspond to measurements performed with the microfluidic device having a greater depth of 150 µm. The slight deviations are probably due to the minimal flow rate generated by the syringe pumps used with the microfluidic rheometer. To insure a very stable and a constant laminar flow of the fluids in the channel, with no mixing, no diffusion or turbulences during the co-flow even with miscible products, a minimum flow rate is set and by that the minimum shear rate provided is defined at 100 s$^{-1}$. This technical limitation might lead to less precise determinations at low shear rates when using a microfluidic rheometer, thereby resulting in higher error in the model fits. A similar situation has been discussed Pipe

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**Figure 7**: Experimental data and model fits (solid lines) built from the correlations as a function of concentration. a) XG solutions. b) WPIXG solutions
Table 4: rheological variables of the model fits used in Figure 6 and mean absolute percent deviation between experimental data and model fit (MAPD)

| Solution | Geometry | $\eta_0$ Pa·s | $\eta_{\infty}$ $\times 10^{-3}$ Pa·s | $\lambda$ s | $m$ | MAPD % |
|----------|----------|---------------|--------------------------------------|------------|------|--------|
| XG008    | 60-2     | 0.8           | 1.2                                  | 8.92       | 0.61 | 11.3   |
| XG02     | 60-2     | 11.3          | 1.5                                  | 16.4       | 0.74 | 17.1   |
| XG04     | 60-2     | 81.9          | 2.0                                  | 28.7       | 0.86 | 14.1   |
| XG05     | 60-2     | 155           | 2.3                                  | 35         | 0.90 | 14.5   |
| WPI3XG02 | 40-4     | 20.5          | 1.4                                  | 21.2       | 0.78 | 4.9    |
| WPI3XG035| 40-4     | 88.9          | 1.8                                  | 31.7       | 0.82 | 6.9    |
| WPI3XG04 | 40-4     | 126           | 1.9                                  | 35.2       | 0.83 | 6.5    |
| WPI3XG05 | 40-4     | 226           | 2.1                                  | 42.2       | 0.84 | 13     |

e t al. [36] for a xanthan gum solution with concentration 0.3% wt. Table 4 presents the rheological parameters calculated from the correlations proposed in section 3.3 that were used to plot the model fits presented in Figure 7. The adjustment of the models to the experimental data is also presented in this table in terms of MAPD. The higher MAPD for the XG solutions is due precisely to the less precise fit at shear rates around 100-1000 s$^{-1}$ discussed previously. For the case of WPIXG solutions, since they were only characterized with the microdevice having a minor depth of 50 µm, the values of MAPD tended to be lower.

4 Conclusion

The purpose of this study is to investigate a methodology to model the viscosity of xanthan gum-based solutions as a function of their concentration, over a large range of shear rates ($10^{-3}$ – $10^6$ s$^{-1}$). More specifically, xanthan gum is a biopolymer widely encountered in industrial applications, so that many works have dealt with its rheology but few information concerning high shear rates is presented in the literature. This is why this work describes a complete methodology which is based on the analysis of experimental data obtained by combining two rheological techniques, rotational rheometry and microfluidic rheometry. In a first step, raw data obtained from the two techniques were analyzed and compared. The microfluidic data extend the rheometer data and the establishment of flow instabilities is determined at the shear rate where the two curves diverge. This point leads to the determination of a critical Reynolds number. Its value is linked to the cone-plate geometry and is found to be lower when using a larger cone angle which is consistent with conclusions of previous works in the literature. A first limit in this subject is that no generalized Reynolds or Taylor number definition has been found to give a unique critical value for the different cone-plate geometries.

At the lowest shear rates attained by the microfluidic rheometer, a slight discrepancy with the rotational rheometer is observed which is due to the difficulty of getting an accurate and stable fluid flow. By merging the results from the two rheometers, a relevant flow curve can be established over the whole shear rate range by using a Williams-Carreau equation. The four parameters from the Williams-Carreau law are modeled as a function of polymer concentration. The first Newtonian plateau is in good agreement with literature data in the considered dilution regime. The second Newtonian plateau, which is the most sensitive parameter for our purpose of viscosity model implementation in high shear processes, is also the most difficult to determine accurately. Thanks to the Fluidican™ device, it is now possible to have a realistic model for the concentration range of interest, with a sufficient accuracy for the needs of process engineering. The findings from this research might benefit applications in fields of food, cosmetics, coatings and other related sectors. Additionally, this study contributes to the understanding of rheology at high shear rates for a polymer mixture (xanthan gum with whey protein isolates) of industrial relevance for food applications.

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