TaRh$_2$B$_2$ and NbRh$_2$B$_2$: Superconductors with a chiral noncentrosymmetric crystal structure

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It is a fundamental truth in solid compounds that the physical properties follow the symmetry of the crystal structure. Nowhere is the effect of symmetry more pronounced than in the electronic and magnetic properties of materials—even the projection of the bulk crystal symmetry onto different crystal faces is known to have a substantial impact on the surface electronic states. The effect of bulk crystal symmetry on the properties of superconductors is widely appreciated, although its study presents substantial challenges. The effect of a lack of a center of symmetry in a crystal structure, for example, has long been understood to necessitate that the wave function of the collective electron state that gives rise to superconductivity has to be more complex than usual. However, few nonhypothetical materials, if any, have actually been proven to display exotic superconducting properties as a result. We introduce two new superconductors that in addition to having noncentrosymmetric crystal structures also have chiral crystal structures. Because the wave function of electrons in solids is particularly sensitive to the host material’s symmetry, crystal structure chirality is expected to have a substantial effect on their superconducting wave functions. Our two experimentally obtained chiral noncentrosymmetric superconducting materials have transition temperatures to superconductivity that are easily experimentally accessible, and our basic property characterization suggests that their superconducting properties may be unusual. We propose that their study may allow for a more in-depth understanding of how chirality influences the properties of superconductors and devices that incorporate them.

INTRODUCTION

The discovery of superconductivity in CePt$_3$Si (1, 2) has sparked interest in superconductors with noncentrosymmetric crystal structures (3) and their anomalous character (4). By far, most superconductors reported to date have inversion symmetry, which many believe to be a favorable trait in a superconducting material. When a superconductor has an inversion center, it can be classified as having either spin singlet or spin triplet pairing because the resulting spin degeneracy is protected by the inversion (5, 6). However, for noncentrosymmetric crystal structures, conventional Cooper pairs can no longer form because the lack of inversion symmetry causes the Fermi surface to split (7). This splitting allows for mixed-parity pairing, which can result in complicated spin structures. The pairing can no longer be simply classified into even and odd parity, or as spin singlet or spin triplet (8). Such an admixture of spin states results in quasi-particle band structures (BSs) that are topologically nontrivial, which in turn results in a material with protected zero-energy states at the surface or edges, similar to topological insulators (9).

The violation of parity conservation can lead to various other exotic behaviors, such as magnetoelectric coupling (10) or anomalous upper critical field ($H_{c2}$) values, but does not guarantee such odd behavior (3). Some noncentrosymmetric superconductors have upper critical fields that exceed the Pauli limit ($H_{c2}$Pauli = $1.85T_C$) (11, 12), a limit that is based on the maximum magnetic field that will not break apart a singlet Cooper pair at low temperatures ($T_C$). The previously reported noncentrosymmetric superconductors such as Mg$_{10}$Ir$_{19}$B$_{16}$ (14, 15), Nb$_{0.18}$Re$_{0.82}$ (16), T$_2$Ga$_2$S$_3$ ($T$ = Rh, Ir) (17), Li$_2$TaB ($T$ = Pd, Pt) (18, 19), or other nonmagnetic analogs (20, 21) of CePt$_3$Si, such as LaPt$_3$Si (22), fit into categories based on whether they are both chiral and noncentrosymmetric or only noncentrosymmetric. Chiral crystal structures must also be noncentrosymmetric, but noncentrosymmetric crystal structures are not necessarily chiral. Although Mg$_{10}$Ir$_{19}$B$_{16}$ (14, 15), CePt$_3$Si (1, 2), and Nb$_{0.18}$Re$_{0.82}$ (16) are noncentrosymmetric, their crystal structures are nonchiral, that is, they are non-enantiomorphic, but of these, only CePt$_3$Si (1, 2) displays a higher than expected $H_{c2}$ value. On the other hand, Li$_2$TaB ($T$ = Pd, Pt) (18, 19) and Mo$_3$Al$_2$C (23) are both noncentrosymmetric and have chiral crystal structures, but these materials display upper critical fields below the Pauli limit. In addition, researchers did not note or explore the potential effect of their structural chirality on superconductivity. Sr$_2$RuO$_4$ (24, 25) and UPt$_3$ (26), which are both centrosymmetric and therefore structurally achiral, are, nonetheless, two of the main candidates believed to display chiral superconductivity (27). For a superconductor to be chiral, the phase of the superconducting gap function, $\Delta(k)$, must wind in either a counterclockwise or a clockwise direction as $k$ moves along the Fermi surface (27). Adopting a chiral structure type does not necessarily result in chiral superconductivity, but Li$_2$Pt$_3$B, which has a chiral crystal structure, has also been proposed (18) as a candidate for chiral superconductivity.

Here, we report our discovery and investigation of the superconductors TaRh$_2$B$_2$ and NbRh$_2$B$_2$, which have a chiral noncentrosymmetric crystal structure, reporting their characterization through single-crystal x-ray diffraction, temperature-dependent electrical resistivity, magnetic susceptibility, and specific-heat measurements. They are isostructural, both forming in the same chiral noncentrosymmetric space group $P3_1$ (no. 144). We show that many of their properties are consistent with normal conventional superconducting behavior, but we also find that both TaRh$_2$B$_2$ and NbRh$_2$B$_2$ display anomalous upper critical field [$H_{c2}(T)$] values that exceed the Pauli limit. We cannot rule out exotic pairing symmetries in the superconducting state for these materials.
RESULTS AND DISCUSSION

Chiral crystal structure

We used single-crystal diffraction to determine the crystal structure of the new superconductor TaRh$_2$B$_2$, which crystallizes in the chiral, noncentrosymmetric space group $P3_1$ (no. 144), where $a = 4.6980(7)$ Å and $c = 8.770(2)$ Å. The space group and lattice parameters from the single-crystal refinement were the starting point for the LeBail fits of the room temperature powder x-ray diffraction (pXRD) patterns in Fig. 1A for TaRh$_2$B$_2$ (top) and isostructural NbRh$_2$B$_2$ (bottom). Note that Schaak et al. (28) anticipated the potential existence of superconductivity in a material of nominal composition NbRh$_2$B$_2$-$x$ with an unknown crystal structure. Only standard solid-state synthesis methods resulted in making the nearly single-phase bulk samples whose powder patterns are shown in Fig. 1A. Table S1 gives summary of the single-crystal structure refinement for TaRh$_2$B$_2$, and table S2 gives selected interatomic bond distances. Table 1 shows atomic coordinates from the crystal structure refinement. The $3 \alpha$ screw axis in the structure, which results in its chirality and also its lack of inversion symmetry, can be seen in Fig. 1B (top) when the structure is viewed along the $a$ direction. The Ta, Rh spiral turns in either a right-handed or a left-handed direction within a superconducting domain, with B-B dimers interwoven throughout the spiral. Similar to other metal-rich boride superconductors such as NbRuB$_3$ (29), which has isolated boron atoms in addition to B-B dimers, the B-B dimers in TaRh$_2$B$_2$ are also critical for stabilizing the compound. B-B dimers are not rare in borides—W$_2$CoB$_2$ (30), for example, also has B-B dimers in its structure. A better understanding of the crystal structure of TaRh$_2$B$_2$ results by viewing the structure along the $c$ direction (Fig. 1B, bottom). The Ta atoms form isolated spirals (chains all turning in the same direction) that are surrounded by B-B dimers. The Ta spirals go through layers of Rh atoms arranged in a honeycomb lattice, where each honeycomb layer is slightly offset from the layer above and below, thus creating a spiral of Rh layers. The topology of the structure may host unique vortex states for the observed superconductivity. It may further help to understand the crystal structure to envision the Ta spirals as rods (31) penetrating the honeycomb layers of Rh that are themselves stacked in a spiral fashion. The B-B dimers stabilize the unusual structure through bonding to the metals.

Magnetic susceptibility

To characterize the superconductors TaRh$_2$B$_2$ and NbRh$_2$B$_2$, the field-dependent volume magnetization ($M_V$) was measured at 1.7 K (in the superconducting state) for both TaRh$_2$B$_2$ (Fig. 2A, inset) and NbRh$_2$B$_2$ (Fig. 2B, inset) and fitted to a line in the low-field region ($M_V = bH + a$). The fit lines $M_V$ were used to estimate the demagnetization factor $N$ (which is based on the sample shape and orientation with respect to the applied magnetic field) for both materials with the equation $b = \frac{a}{4\pi(1-N)}$, using the slope of the fitted line, $b$. These $N$ values were used to correct the magnetic susceptibility data in the main panels of Fig. 2 (A and B). We carried out further characterization through both zero-field–cooled (ZFC) and field-cooled (FC) temperature-dependent measurements.

![Fig. 1. Crystal structure characterization of TaRh$_2$B$_2$ and NbRh$_2$B$_2$. (A) Room temperature pXRD pattern showing a LeBail fit for the new superconducting phases TaRh$_2$B$_2$ (top) and NbRh$_2$B$_2$ (bottom). The experimentally observed data are shown with red circles, the calculated pattern is shown with a black line, and the green vertical marks indicate the expected Bragg reflections for space group $P3_1$ (no. 144). Impurity peaks are marked with asterisks. (B) The crystal structure of chiral and noncentrosymmetric TaRh$_2$B$_2$ and isostructural NbRh$_2$B$_2$ viewed along the $c$ direction, emphasizing the $3 \alpha$ screw axis (top) and along the $c$ direction (bottom), emphasizing the Ta spirals and a single Rh honeycomb layer. Tantalum/niobium is shown in blue, rhodium is shown in pink, and boron is shown in green. Arb. units, arbitrary units.](https://example.com/fig1.png)

Table 1. Atomic coordinates and equivalent isotropic displacement parameters of TaRh$_2$B$_2$ at 293(2) K. $U_{eq}$ is defined as one-third of the trace of the orthogonalized $U_{ij}$ tensor ($\AA^2$).

| Atom   | Wyckoff position | Occupancy | x     | y     | z     | $U_{eq}$ |
|--------|------------------|-----------|-------|-------|-------|----------|
| Ta     | 3α               | 1         | 0.8481(2) | 0.8481(2) | 0.3131(2) | 0.0041(2) |
| Rh1    | 3α               | 1         | 0.6638(4) | 0.4824(4) | 0.0447(3) | 0.0058(2) |
| Rh2    | 3α               | 1         | 0.3324(4) | 0.8190(4) | 0.1072(2) | 0.0058(3) |
| B1     | 3α               | 1         | 0.627(7)  | 0.550(8)  | 0.549(3)  | 0.012(5)  |
| B2     | 3α               | 1         | 0.288(9)  | 0.347(8)  | 0.215(3)  | 0.028(5)  |
Fig. 2. Superconducting characterization of TaRh$_2$B$_2$ and NbRh$_2$B$_2$. (A and B) ZFC and FC temperature-dependent magnetic susceptibility $\chi(T)$ for TaRh$_2$B$_2$ (A) and NbRh$_2$B$_2$ (B) measured in an applied magnetic field of 1 mT. The insets show field-dependent volume magnetization ($M_V$) measured at various temperatures below $T_c$. (C and D) Lower critical field $\mu_0 H_{cl}(T)$ versus temperature for TaRh$_2$B$_2$ (A) and NbRh$_2$B$_2$ (B). The data points were estimated from a difference between $M_V$ and $M_{fit}$ as is shown in the insets. (E) $C_p/T$ versus $T$ plotted from 0 to 9 K for TaRh$_2$B$_2$ (green open squares) and NbRh$_2$B$_2$ (blue open circles) measured in zero applied field where the solid black lines outline the equal area construction shown with gray shading. This construction is used for estimation of $T_c$ and the superconducting jump $\Delta C/T_c$. Inset: $C_p/T$ versus $T^2$ measured in 9-T field (in the normal state) fitted to $C_p/T = \gamma + \beta T^2$. (F) Temperature-dependent electronic specific heat $C_{el}$ for NbRh$_2$B$_2$ below 9 K. The solid curve through the data is a fit by a one-gap BCS model for superconductivity. Inset: $C_{el} - \gamma_0 T$ versus normalized temperature ($T_c/T$) for NbRh$_2$B$_2$ and TaRh$_2$B$_2$. (The lattice contribution was subtracted from the measured specific heat). emu, electromagnetic unit.
magnetic susceptibility measurements with a 1-mT applied field. We took the measurement from 1.7 to 10 K for TaRh$_2$B$_2$ (Fig. 2A, main panel), showing a superconducting critical temperature of 5.8(1) K. We determined the $T_c$ to be the intersection between the normal state of the magnetic susceptibility extrapolated to lower temperature with the line corresponding to the steepest slope of the diamagnetic signal (indicated by black solid lines) (32). We also performed ZFC and FC measurements on the Nb variant (Fig. 2B, main panel) from 1.7 K to 12 K, showing a $T_c = 7.6(1)$ K. Both the ZFC and FC measurements were corrected for $N = 0.504$ for the Ta variant and $N = 0.448$ for the Nb variant. The resulting diamagnetic signal is only slightly less than the ideal value of 4$\pi$N,(1 - N) = -1 for both TaRh$_2$B$_2$ and NbRh$_2$B$_2$. The observed critical temperatures in the susceptibility measurements are consistent with both the specific heat and resistivity measurements (discussed next) for each superconducting material. There is a very weak superconducting signal observed for the FC measurement for each material, as expected due to the polycrystalline nature of both samples.

### Magnetization

The new superconductors TaRh$_2$B$_2$ and NbRh$_2$B$_2$ were further studied with field-dependent magnetization ($M_B$) measurements at different temperatures below the critical temperature, as seen in Fig. 2A (inset) for the Ta variant and in Fig. 2B (inset) for the Nb variant. The low-field linear fits to the magnetization data ($M_B$), as discussed previously, were used to construct the $M_B - M_{\text{fit}}$ plot in Fig. 2C (inset) for TaRh$_2$B$_2$ and NbRh$_2$B$_2$ (Fig. 2D, inset). The field at which the magnetization begins to deviate from a linear response (indicated by the black dashed line in each inset) is the uncorrected lower critical field, $\mu_0 H^c_1$ , for that temperature. All the $\mu_0 H^c_1$ values with the corresponding temperatures are plotted in Fig. 2C (main panel) for TaRh$_2$B$_2$ and in Fig. 2D (main panel) for NbRh$_2$B$_2$ and fitted to the following equation

$$\mu_0 H^c_1(T) = \mu_0 H^c_1(0) \left[1 - \left(\frac{T}{T_c}\right)^2\right]$$

where $\mu_0 H^c_1(0)$ is the lower critical field at 0 K and $T_c$ is the superconducting critical temperature. $\mu_0 H^c_1(0)$ was calculated to be 4.74(6) mT for TaRh$_2$B$_2$ and 7.45(4) mT for NbRh$_2$B$_2$. After correcting for the demagnetization factor for each sample, $\mu_0 H^c_1(0)$ was calculated to be 9.56(1) mT for the Ta variant and 13.50(2) mT for the Nb variant.

### Specific heat and observed superconducting parameters

The temperature-dependence of $C_p/T$ is plotted for both TaRh$_2$B$_2$ and NbRh$_2$B$_2$ in Fig. 2E (main panel) under zero applied magnetic field measured from 2 to 9 K, showing a large anomaly in the specific heat for each superconducting material. Using equal-entropy constructions of the idealized specific heat capacity jump (gray shading), the $T_c$ was determined to be 5.8 K for the Ta variant and 7.6 K for the Nb variant, consistent with the magnetic susceptibility and resistivity data.

At low temperature, the specific heat data can be described by the equation

$$\frac{C_p}{T} = \gamma + \beta T^2$$

where $\gamma T$ is the electronic contribution and $\beta T^2$ is the phonon contribution to the specific heat. This linear relationship can be seen in the $C_p/T$ versus $T^2$ plot in the inset of Fig. 2E for TaRh$_2$B$_2$ and NbRh$_2$B$_2$. By fitting our data to the above equation (using data from the 9-T measurement taken from the normal state), the Sommerfeld parameter $\gamma$ was calculated to be 5.8(1) mJ mol$^{-1}$ K$^{-2}$ for the Ta analog and 8.8(2) mJ mol$^{-1}$ K$^{-2}$ for the Nb analog. On the basis of the slope of the each fitted line, $\beta$ was calculated to be 0.178(5) mJ mol$^{-1}$ K$^{-4}$ for TaRh$_2$B$_2$ and $\beta = 0.203(3)$ mJ mol$^{-1}$ K$^{-4}$ for NbRh$_2$B$_2$. The Debye model was then used with the $\beta$ value in the equation

$$\Theta_D = \left(\frac{12\pi^4}{5\beta} nR\right)^{1/3}$$

to calculate the Debye temperature $\Theta_D$, where $n = 5$ (TaRh$_2$B$_2$ or NbRh$_2$B$_2$) and $R$ is the gas constant 8.314 J mol$^{-1}$ K$^{-1}$. The Debye temperatures were calculated to be $\Theta_D = 379(4)$ K for the Ta and Nb variants, respectively. With $\Theta_D$ and $T_c$, the electron-phonon coupling constant $\lambda_{ep}$ can then be calculated using the inverted McMillan (33) equation

$$\lambda_{ep} = \frac{1.04 + \mu^* \ln\left(\frac{\Theta_D}{1.45T_c}\right)}{(1 - 0.62\mu^*) \ln\left(\frac{\Theta_D}{1.45T_c}\right) - 1.04}$$

where $\mu^*$ = 0.13 and $T_c$ = 5.8 and 7.6 K, respectively. The superconducting parameter $\lambda_{ep}$ = 0.624(5) and 0.688(4) for TaRh$_2$B$_2$ and NbRh$_2$B$_2$, suggesting that both materials are weak-moderate coupling superconductors. Using $\lambda_{ep}$, $\gamma$, and the Boltzmann constant $k_B$, the density of electronic states at the Fermi energy $N(E_F)$ can be calculated from the equation

$$N(E_F) = \frac{3\gamma}{\pi^2 k_B^2 (1 + \lambda_{ep})^2}$$

$N(E_F)$ was estimated to be 1.52(3) states eV$^{-1}$ per formula unit (fu) of TaRh$_2$B$_2$ and 2.21(5) states eV$^{-1}$ per fu of NbRh$_2$B$_2$, respectively. In addition, the normalized specific heat jump, $\Delta C/\gamma T_c$, was found to be 1.56(4) and 1.60(3) for the Ta and Nb analogs, both of which are larger than the expected value of 1.43 (34), which suggests that both materials are moderately coupled superconductors.

Figure 2F (main panel) shows low-temperature (superconducting state) electronic specific heat $C_el$ versus $T$ for NbRh$_2$B$_2$ in zero applied field and fitted to the equation

$$C_{el} = \gamma_0 T + \alpha T e^{-\Delta_0/k_B T}$$

where $k_B$ is the Boltzmann constant, $\gamma_0 T$ is the electronic contribution to the specific heat coming from the sample impurities, and $\Delta_0$ is the magnitude of the superconducting gap. $C_{el} - \gamma_0 T$ plotted as a function of the normalized $T_c/T$ for both TaRh$_2$B$_2$ and NbRh$_2$B$_2$ is shown in the inset of Fig. 2F. For a weak coupling superconductor (34)

$$2\Delta_0 = 3.5k_B T_c$$

For TaRh$_2$B$_2$, the obtained value $\Delta_0 = 0.98(2)$ meV (for which $2\Delta_0 = 1.96$ meV) is larger than the theoretical value of $2\Delta_0 = 1.75$ meV (for $T_c = 5.8$ K). Likewise for NbRh$_2$B$_2$, the calculated value of $\Delta_0 = 1.4$ (1) meV ($2\Delta_0 = 2.8$ meV) is larger than the expected value of $2\Delta_0 = 2.29$ meV (for
$T_c = 7.6$ K), which is consistent with what we proposed previously that TaRh$_2$B$_2$ and NbRh$_2$B$_2$ are moderately coupled superconductors.

**Resistivity**

The temperature-dependent electrical resistivity measured from 300 to 1.7 K for polycrystalline TaRh$_2$B$_2$ is shown in Fig. 3A (main panel) and for polycrystalline NbRh$_2$B$_2$ in Fig. 3B (main panel). The resistivity drops to zero at 5.8 K for the Ta variant and at 7.7 K for the Nb variant. These new materials are both poor metals, and the resistivity is essentially temperature-independent for the temperature range above $T_c$. The dependence of $T_c$, taken as 50% of the resistivity transition (black dashed line), on the applied magnetic field is shown in the inset of Fig. 3A for TaRh$_2$B$_2$ and Fig. 3B for NbRh$_2$B$_2$, where the field is increased from 0 to 12 T in 0.5-T increments for the Ta variant and from 0 to 14 T for the Nb variant. Even with an 11-T applied magnetic field, the critical temperature was only suppressed to ~1.9 K for the Ta variant and to ~3 K for the Nb variant in a 14-T applied magnetic field.

Figure 3C shows the upper critical fields $\mu_0 H_{c2}(0)$ plotted as a function of the estimated $T_c$ values at different applied fields. The dependence of the superconducting transition on applied magnetic field measured (A) from 1.7 to 7 K for the Ta variant in applied fields from 0 to 12 T and (B) from 1.7 to 9 K for the Nb variant in applied magnetic fields from 0 to 14 T in 0.5-T increments. The dashed black line shows 50% of the superconducting transition. (C) $T_c$ values at different applied fields were used to calculate $\mu_0 H_{c2}(0)$ to be 11.7(4) T for TaRh$_2$B$_2$ and 18.0(4) T for NbRh$_2$B$_2$.

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limit. Likewise, for TaRh$_2$B$_2$, the last measurable $T_c$ value was 1.9 K at 11 T, which is already above the Pauli limit for this material. A higher than expected $\mu_0H_{c2}(0)$ value has also been seen in the noncentrosymmetric superconductor CePt$_3$Si (1, 2), as discussed previously, which suggests that the superconductors reported here are potentially anomalous. In addition, it would be of future interest to perform measurements with the magnetic field applied along each axis direction of a single crystal to see whether the $H_{c2}$ value displays anisotropy for each superconducting material.

The determined $\mu_0H_{c2}(0)$ and $\mu_0H_{c1}(0)$ values can be used to calculate several other superconducting parameters. Using the equation

$$\mu_0H_{c2}(0) = \frac{\Phi_0}{2\pi^2 GL},$$

where $\Phi_0$ is the quantum flux $\hbar/2e$, the Ginzburg-Landau coherence length $\xi_{GL}$ was calculated to be 53(1) Å for TaRh$_2$B$_2$ and 43(1) Å for NbRh$_2$B$_2$. We used the dirty limit (discussed previously) to determine $\mu_0H_{c2}(0)$ because the obtained ratio of the coherence length $\xi_{GL}$ and the mean free path ($l$) is close to 1 and therefore on the boundary between the dirty and clean limits. We determined the mean free path using the following equation [derived in the study of Singh et al. (36)]

$$l = 2.372 \times 10^{-14} \left(\frac{m_e}{m_0}\right)^2 \frac{V_F^2}{N(E_F)^2 \rho^3}$$

where $V_M$ is the molar volume, $\rho$ is the resistivity, and $N(E_F)$ is the density of states (DOS) at the Fermi level. For TaRh$_2$B$_2$, $V_M = 33.6$ cm$^3$ mol$^{-1}$, $\rho = 2$ milliohm·cm, $N(E_F) = 1.52(3)$ states eV$^{-1}$ per fu, and assuming that $m_e/m_0 = 1$, we obtain $l = 58$ Å. Similarly, for NbRh$_2$B$_2$, $V_M = 39.0$ cm$^3$ mol$^{-1}$, $\rho = 2.2$ milliohm·cm, and $N(E_F) = 2.21(5)$ states eV$^{-1}$ per fu, which gives $l = 34$ Å. The resulting ratios of $\xi_{GL}/l$ are 0.9 and 1.3 for the Ta and Nb variants, respectively, which show that both TaRh$_2$B$_2$ and NbRh$_2$B$_2$ are on the border of the dirty limit and clean limit; we chose to use the dirty limit for the upper critical field calculations.

Using the result of $\xi_{GL}$, with $\mu_0H_{c1}$ (determined previously), the superconducting penetration depth $\lambda_{GL} = 2580(60)$ Å for the Ta analog and 2190(70) Å for the Nb analog were estimated using the lower critical field equation

$$\mu_0H_{c1} = \frac{\Phi_0}{4\pi \lambda_{GL}} \ln \frac{\lambda_{GL}}{\xi_{GL}}$$

The value $\kappa_{GL} = \lambda_{GL}/\xi_{GL}$ was calculated to be $\kappa_{GL} = 48(2)$ for TaRh$_2$B$_2$ and $\kappa_{GL} = 51(3)$ for NbRh$_2$B$_2$, confirming the type II superconducting behavior in both new materials. Combining the results of $H_{c1}$, $H_{c2}$, and $\kappa_{GL}$, the thermodynamic critical field can be estimated from the equation

$$H_{c2}H_{c1} = H^2 \ln \kappa_{GL}$$

This calculation yields $\mu_0H_c = 169(3)$ mT for the Ta variant and 248(4) mT for the Nb variant. Table 2 gives a summary of all the observed superconducting parameters for TaRh$_2$B$_2$ and NbRh$_2$B$_2$, with a chiral noncentrosymmetric crystal structure.

### Electronic structure

To gain an intrinsic insight into the relationship between the superconductivity observed and the electronic states of TaRh$_2$B$_2$ and NbRh$_2$B$_2$, we investigated the electronic DOS and BS for both superconducting materials without and with spin-orbit coupling (SOC) (Fig. 4). The total and partial DOS for TaRh$_2$B$_2$ and NbRh$_2$B$_2$ are illustrated in Fig. 4 (C and F). The DOS in the energy below $-2.0$ eV mainly consists of Ta/Nb and Rh $s$ and $d$ orbitals. The DOS in the energy range from $-2.0$ to $+2.0$ eV contains mixed Ta/Nb and Rh $s$ and $d$ orbitals in addition to $s$ and $p$ orbitals from B, in particular, around the Fermi level. Note that the calculated DOS($E_F$) values are 1.3 states eV$^{-1}$ per fu of TaRh$_2$B$_2$ and 1.5 states eV$^{-1}$ per fu of NbRh$_2$B$_2$; these obey the same qualitative behavior as the observed values presented in Table 2. A sharp peak in the DOS is often an indication of a nearby structural, electronic, or magnetic instability such as superconductivity. To investigate further, we calculated the BS both with/without SOC for TaRh$_2$B$_2$ (Fig. 4, A and B) and for NbRh$_2$B$_2$ (Fig. 4, D and E). The broad peak in the DOS at $E_F$ is due to the presence of saddle points in the electronic structure at the M and L points in the Brillouin zone. Researchers have often proposed that Saddle points near $E_F$ are important for yielding superconductivity (37) and they may also be significant in the current materials.

In summary, we report two new noncentrosymmetric superconductors, TaRh$_2$B$_2$ and NbRh$_2$B$_2$, which both have a new crystal structure belonging to the chiral space group $P\overline{3}1$. Temperature-dependent electrical resistivity, magnetic susceptibility, and specific heat data confirmed bulk superconductivity with $T_c = 5.8$ K for the Ta analog and $T_c = 7.6$ K for the Nb analog. The derived superconducting parameters show that TaRh$_2$B$_2$ and NbRh$_2$B$_2$ are basically type II Bardeen, Cooper, Schrieffer (BCS) moderately coupled superconductors. However, their
behavior under applied magnetic fields shows that $\mu_0 H_c(0)$ exceeds the Pauli limit for both superconducting materials. Although many of the superconducting properties are conventional, we cannot rule out more complicated spin states in the superconducting state. Future work on these materials to determine whether their chiral noncentrosymmetric crystal structure has an effect on their normal state and superconducting properties, and on their use in advanced devices, particularly those with chirality junctions, will be of interest.

**MATERIALS AND METHODS**

**Experimental design**

The starting materials for the synthesis of TaRh$_2$B$_2$ and NbRh$_2$B$_2$ bulk materials were elemental tantalum (>99.9%, 100 mesh; Alfa), niobium (>99.9%, 200 mesh; Sigma-Aldrich), rhodium (>99.9%, 325 mesh; Alfa), and boron (submicron particles, Callery Chemical). Powders of the starting materials Ta/Nb, Rh, and B were weighed out in a 1:1.9:2.1 ratio, ground using a mortar and pestle, and pressed into a pellet. The samples were then wrapped in Ta foil, placed in an alumina crucible, and heated in a high vacuum furnace to 1200°C for 6 hours. Variation from the above loading compositions or heating temperature led to the presence of secondary phases in larger amounts. Attempts to arc-melt TaRh$_2$B$_2$ followed by annealing at 1100°C for 1 week in an evacuated silica tube did not result in a single-phase sample. Samples of TaRh$_2$B$_2$ and NbRh$_2$B$_2$ are stable in air and do not decompose over time.

**Crystal structure characterization**

The purity of the samples studied was checked using room temperature pXRD using a Bruker D8 Advance Eco Cu K$_\alpha$ radiation ($\lambda = 1.5406$ Å) diffractometer with a LynxEye-XE detector. Single crystals from an arc-melted and annealed sample of TaRh$_2$B$_2$ were mounted on the tips of Kapton loops. A Bruker Apex II x-ray diffractometer with Mo K$_\alpha$ radiation ($\lambda = 0.71073$ Å) was used to collect room temperature intensity data. The data were collected over a full sphere of reciprocal space with

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**Fig. 4. Electronic calculations for TaRh$_2$B$_2$ and NbRh$_2$B$_2$.** Calculated BS for (A and B) TaRh$_2$B$_2$ and (D and E) NbRh$_2$B$_2$ both with (middle) and without (left) SOC plotted in the energy range from $-2.0$ to $2.0$ eV. The total DOS calculated using the Wien2K with LDA-type pseudopotentials with SOC included (blue line) and without SOC (red line) for (C) TaRh$_2$B$_2$ and (F) NbRh$_2$B$_2$. 

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The crystal structure of TaRh$_2$B$_2$ was solved using direct methods and refined by full-matrix least-squares on $F^2$ with the SHELXTL package. A total of 25 space groups were tested according to the observed Laue symmetry, and the space group was determined to be P$\bar{3}$$_1$. The best of our knowledge, TaRh$_2$B$_2$ has a unique structure type. The crystal structure images were created in the program VESTA.

Superconducting property measurements

A Quantum Design Physical Property Measurement System (PPMS) Dynacool was used to measure the temperature- and field-dependent magnetization and temperature-dependent electrical resistivity of TaRh$_2$B$_2$ and NbRh$_2$B$_2$ using a vibrating sample magnetometer and resistivity option. Both ZFC and FC magnetic susceptibility measurements were collected on a Quantum Design PPMS Evercool II with applied magnetic fields of 0 to 9 T.

Electronic structure calculations

The BS and DOS of TaRh$_2$B$_2$ and NbRh$_2$B$_2$ were calculated using Wien2K with LDA-type (local density approximation) pseudopotentials. The structural lattice parameters obtained from single-crystal diffraction measurements for TaRh$_2$B$_2$ were used for the calculation. SOC was included for all atoms. Reciprocal space integrations were completed over an 8 $\times$ 8 $\times$ 4 Monkhorst-Pack $k$-points mesh. The convergence criterion for a self-consistent calculation was taken as $1.0 \times 10^{-6}$ eV.

SUPPLEMENTARY MATERIALS

SUPPLEMENTARY material for this article is available at http://advances.sciencemag.org/cgi/content/full/4/eear7969/DC1 table S1. Single-crystal crystallographic data for TaRh$_2$B$_2$.

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