THE LACK OF DIFFUSE, NON-TERMAL HARD X-RAY EMISSION IN THE COMA CLUSTER: THE SWIFT BURST ALERT TELESCOPE’S EYE VIEW

Daniel R. Wik1,7, Craig L. Sarazin2, Alexis Finoguenov3,4, Wayne H. Baumgartner1, Richard F. Mushotzky5, Takashi Okajima1, Jack Tueller1, and Tracy E. Clarke6

1 Astrophysics Science Division, Laboratory for High Energy Astrophysics, Code 662, NASA/Goddard Space Flight Center, Greenbelt, MD 20771, USA; daniel.r.wik@nasa.gov
2 Department of Astronomy, University of Virginia, 530 McCormick Road Charlottesville, VA 22904, USA
3 Max-Planck-Institut für Extraterrestrische Physik, Giessenbachstr., 85748 Garching, Germany
4 University of Maryland, Baltimore County, 1000 Hilltop Cr., Baltimore, MD 21250, USA
5 Department of Astronomy, University of Maryland, College Park, MD 20742, USA
6 Naval Research Laboratory, 4555 Overlook Ave. SW, Code 7213, Washington, DC 20375, USA

Received 2010 September 24; accepted 2010 November 12; published 2011 January 12

ABSTRACT

The Coma Cluster of galaxies hosts the brightest radio halo known and has therefore been the target of numerous searches for associated inverse Compton (IC) emission, particularly at hard X-ray energies where the IC signal must eventually dominate over thermal emission. The most recent search with the Suzaku Hard X-ray Detector failed to confirm previous IC detections with RXTE and BeppoSAX, instead setting an upper limit 2.5 times below their non-thermal flux. However, this discrepancy can be resolved if the IC emission is very extended, beyond the scale of the cluster radio halo. Using reconstructed sky images from the 58-month Swift Burst Alert Telescope (BAT) all-sky survey, the feasibility of such a solution is investigated. Building on Renaud et al., we test and implement a method for extracting the fluxes of extended sources, assuming specified spatial distributions. BAT spectra are jointly fit with an XMM-Newton EPIC-pn spectrum derived from mosaic observations. We find no evidence for large-scale IC emission at the level expected from the previously detected non-thermal fluxes. For all non-thermal spatial distributions considered, which span the gamut of physically reasonable IC models, we determine upper limits for which the largest (most conservative) limit is $\lesssim 4.2 \times 10^{-12}$ erg s$^{-1}$ cm$^{-2}$ (20–80 keV), which corresponds to a lower limit on the magnetic field $B > 0.2 \mu$ G. A nominal flux upper limit of $\sim 2.7 \times 10^{-12}$ erg s$^{-1}$ cm$^{-2}$, with corresponding $B > 0.25 \mu$ G, is derived for the most probable IC distribution given the size of the radio halo and likely magnetic field radial profile.

Key words: galaxies: clusters: general – galaxies: clusters: individual (Coma) – intergalactic medium – magnetic fields – radiation mechanisms: non-thermal – X-rays: galaxies: clusters

Online-only material: color figures

1. INTRODUCTION

The X-ray emission from clusters of galaxies is primarily thermal in origin and is produced by a diffuse population of intergalactic electrons in the ionized intracluster medium (ICM). These electrons coexist with a non-thermal, relativistic electron population in at least some clusters—inferred from observations in the radio regime—which should also radiate at X-ray energies. While thermal emission clearly dominates in the kilo-electron volt (keV) energy range, it declines rapidly outside this range, allowing the detection of a non-thermal spectral signature as soft or hard excess emission. This possibility is especially promising at hard (>10 keV) energies, where the exponential decline of the thermal bremsstrahlung continuum is distinctly steeper than the expected non-thermal spectrum. Measurements of non-thermal X-ray emission are critical to the determination of the total amount of relativistic energy in the ICM, which is currently poorly constrained. While no more than $\sim 10\%$ of this energy is tied up in non-thermal components, amounts at or near this level will affect the dynamics and structure of the thermal gas (e.g., Vazza et al. 2009). Specifically, studies that attempt to infer the total masses of clusters from the hydrostatic state of the thermal gas will produce biased mass estimates if the pressure support of relativistic particles and fields is not accurately included. The mass functions built from these estimates can be used to constrain cosmological parameters; these studies are already underway using observables derived in both the X-ray (e.g., Mantz et al. 2008; Vikhlinin et al. 2009) and microwave (e.g., Vanderlinde et al. 2010, through the Sunyaev-Zel’dovich effect) regimes.

A measurement of the total energy in relativistic ICM components is possible when X-ray and radio non-thermal fluxes are combined. Diffuse, cluster-wide synchrotron radio emission, called radio halos or relics depending on their morphology, implies that both magnetic fields and relativistic electron populations are present on large scales. The total luminosity of a synchrotron-emitting electron is given by

$$L_R = \frac{4}{3} \sigma_T c \gamma^2 \epsilon_B,$$  

where $\sigma_T$ is the Thomson cross-section, $c$ is the speed of light, $\gamma$ is the Lorentz factor of the electron, and $\epsilon_B = B^2/8 \pi$ is the energy density of the magnetic field. For a collection of relativistic electrons, the value of $L_R$ depends both on the number of electrons and on $B$ and cannot independently determine either. However, these same electrons will up-scatter cosmic microwave background (CMB) photons through inverse Compton (IC) interactions, which have a luminosity $L_X$ equivalent in form
electrons, their ratio gives the volume-averaged magnetic field,
\[ \frac{L_R}{L_X} = \frac{B^2}{8\pi a T_{\text{CMB}}^4}, \]
where \( a \) is the radiation constant and \( T_{\text{CMB}} \) is the temperature of the CMB. The IC radiation should be observable at hard X-ray energies (Rephaeli 1977). Thus far, IC emission has only been detected at low significance (Nevalainen et al. 2004; Million & Allen 2009) or, in one case at higher significance, in the Ophiuchus cluster (Eckert et al. 2008; but see also Ajello et al. 2009 and Fujita et al. 2008), although the diffuse radio emission in this cluster is restricted to a smaller scale mini-halo (Murgia et al. 2010). The measurement of an IC flux from a synchrotron source directly leads to a simultaneous determination of the average value of \( B \) and the relativistic electron density (Harris & Romanishin 1974; Sarazin 1988). Therefore, searches for IC emission coincident with a radio halo or relic are an excellent way to constrain the contribution of relativistic materials in clusters.

The first, and brightest, radio halo was discovered by Willson (1970) in the Coma Cluster, and its radio properties have perhaps been the best studied (e.g., Giovannini et al. 1993; Deiss et al. 1997; Thiebach et al. 2003). Coma has been observed by all the major observatories with hard X-ray capabilities (Henriksen & Mushotzky 1986; Bazzano et al. 1990; Hughes et al. 1993; Rephaeli et al. 1994), and more recently non-thermal detections have been claimed by Rephaeli & Gruber (2002) with RXTE and by Fusco-Femiano et al. (1999, 2004) with BeppoSAX, though the latter detection is controversial (Rossetti & Molendi 2004; Fusco-Femiano et al. 2007). Due to the large field of view (FOV) of these non-imaging instruments and the simple characterization of the thermal gas, the source of this emission remains uncertain. Even more recently, long (~1 Ms) observations with INTEGRAL have imaged extended diffuse hard X-ray emission from Coma, though it was found to be completely consistent with thermal emission (Renaud et al. 2006a; Eckert et al. 2007; Lutovinov et al. 2008).

Most recently, Wik et al. (2009) performed a joint analysis of spectra from the XMM-Newton EPIC-pn and Suzaku HXD-PIN instruments—the most sensitive instruments at soft and hard energies to date—of the Coma Cluster and were unable to detect IC emission. Instead, they found an upper limit 2.5 times below the detections of Rephaeli & Gruber (2002) and Fusco-Femiano et al. (2004). However, the narrower FOV of the Hard X-ray Detector (HXD) relative to the collimators of the RXTE PCA/HEXTE and BeppoSAX PDS leaves open the possibility that the spatial distribution of IC photons is highly extended, and therefore much of the flux was missed by the HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30 HXD. The IC would have to be much broader than the size of the radio halo. A uniform IC surface brightness of at least 30

2. OBSERVATIONS

To achieve the necessary spatial coverage and spectral sensitivity, we take advantage of mosaics of the Coma Cluster constructed from observations by the XMM-Newton and Swift satellites. The high sensitivity and good spectral and spatial resolution of the XMM-Newton EPIC-pn data act as a check on the interpretation of the Swift BAT data, allowing the thermal and potentially non-thermal emission at hard energies to be accurately decoupled.

2.1. XMM-Newton EPIC-pn Mosaic Observations

The observations and processed XMM-Newton data used herein are identical to that presented in Wik et al. (2009), where a more detailed description can be found. The XMM-Newton EPIC-pn mosaic of Coma consists of 14 individual pointings, the first set (11 pointings) of which were discussed in Briel et al. (2001). The full 14 pointings considered here were first presented in Schuecker et al. (2004). For joint fitting with Swift BAT spectra, we extract events from a 65.5 x 65.5 box centered on the radio halo, which was originally chosen to match the Suzaku Hard X-ray Detector FOV; the region is shown as the outermost contour in Figure 3 of Wik et al. (2009) and also as the box in Figure 1 in the present paper. The only modification of our analysis procedure compared to that in Wik et al. (2009) is that the XMM-Newton spectra were not weighted by the spatial response of the Suzaku HXD, since they are not being fit simultaneously with that instrument. No similar weighting is needed for comparison to the Swift BAT data since the BAT
shown for clarity, and note that the FWHM of the BAT PSF is 19.14–20 keV survey image (square-root spacing: 0.0 pointings is corrected for during processing. The survey covers the entire sky and the vignetting of individual brightness image (Schuecker et al. 2004) with contours from the raw Figure 1.

Section 3.1.1. Spectra extracted within a 16 contiguous grid of regions of size 4.3 × 4.3 are fit to single-temperature APEC models over the energy range 0.5 keV < E < 14 keV. While energies of 9.5 keV < E < 14 keV are generally included during spectral fits, these data are primarily used to determine the background and are only included as a check of the background subtraction. Because of the low count rate at these energies, their inclusion does not significantly contribute to χ² or the resulting best-fit parameters.

While data from the Suzaku observation of Coma (OBSID 801097010) are not part of the current analysis, we do make use of the 2–7.5 keV spectrum from the 0 chip of the X-ray Imaging Spectrometer (XIS0) for calibration purposes, as described in Section A.1. We use the same spectrum that served to cross-calibrate the data in the previous XMM-Newton/Suzaku analysis (region 10 from Wik et al. 2009).

2.2. The Swift BAT 58-month Survey

The Swift mission is primarily to detect and localize gamma-ray bursts, which is accomplished with the very large FOV (∼1/8th of the sky), coded mask aperture BAT. As such, the nearly random pointing strategy culminates in an almost uniform coverage of the entire sky with an ∼8 Ms of exposure time, made from many ~5 minute individual observations. Images of the sky are reconstructed by cross-correlating the shadow pattern of the randomly coded mask in front of the detectors with a detector plane image via a fast Fourier transform. The detectors are sensitive to hard X-ray/soft gamma-ray photons from 14 to 195 keV in 80 native energy channels. As part of the default survey processing, the channels are combined into eight broader energy bands: 14–20 keV (E1), 20–24 keV (E2), 24–35 keV (E3), 35–50 keV (E4), 50–75 keV (E5), 75–100 keV (E6), 100–150 keV (E7), and 150–195 keV (E8). The final survey is built from the individual sky reconstructions, which are summed and resampled onto predetermined image planes of six facets, each in the Zenith Equal Area projection. The detailed processing methodology and survey properties for the 58-month BAT all-sky survey are nearly identical to those described in Tueller et al. (2010) for the 22-month survey. The only major difference is that for the 58-month survey, the gain of each detector pixel was individually calibrated with an onboard radioactive source, which had not been done previously. This better accounts for the sensitivity of low gain pixels, effectively increasing the overall sensitivity. Also, the sky images are more finely resampled so that the pixels near the center of the image projection scale 2.8 instead of 5° as with previous versions of the survey. The main advantage of this change is to improve the centroiding of sources.

Because the systematic uncertainties in the survey-averaged spectrum of the Crab Nebula are smaller than the uncertainties in the BAT survey response matrix, BAT survey fluxes are tied to the Crab fluxes in each band (see Tueller et al. 2010, Section 4.5). One drawback to this approach is that a source flux is only guaranteed to be correctly determined if its spectrum within the energy band is identical to the Crab’s (a power law with a photon index of Γ ~ 2.1), since the energy response within the band may not be uniform. Because we will fit the BAT spectrum jointly with the XMM-Newton spectrum, it is important that the cross-calibration between the Swift BAT and XMM-Newton be accurate. Since the flux calibration of the BAT survey is based on the Crab spectrum, we have made sure that the Swift BAT and XMM-Newton agree on the flux and spectrum of the Crab. The cross-calibration between Swift BAT and XMM-Newton is discussed in detail in Appendix A.

2.2.1. The Coma Cluster

The six facets of the BAT all-sky survey are oriented in Galactic coordinates with one facet centered on each of the Galactic poles and the other four centered uniformly around the Galactic plane. The Zenith Equal Area projection conserves surface brightness but not shapes, so objects far from the center of the projection can be somewhat distorted. However, the fortuitous location of the Coma Cluster near the North Galactic pole, and thus the center of its facet, means that any such distortions are negligible. Nevertheless, for all parts of the analysis image pixels are referred to in terms of their Galactic coordinates so that any image projection effects are completely eliminated.

Hard X-ray emission is clearly detected in the first four energy bands, up to 50 keV. In Figure 1, we present the wavelet-smoothed 2–7 keV XMM-Newton EPIC-pn image of the Coma Cluster mosaic overlaid with contours of the Crab-normalized BAT flux (see Tueller et al. 2010 for a description), which shows the hard X-ray emission to be elongated in the same east–west direction as the softer emission. As first noted by Ajello et al. (2009) in the BAT survey, the Coma Cluster is partially resolved by the BAT, which is explicitly shown in Figure 2. This figure compares the radial surface brightness profile of Coma with that of a nearby point source with a comparable flux. Coma is clearly extended. The points plotted are individual pixels. The greater
width of the distribution for Coma indicates that its surface brightness is not circularly symmetric. As shown in Figure 1, both the BAT and XMM-Newton X-ray emission is elongated in a ENE–WSW direction.

While coded mask instruments have some difficulty detecting extended emission, this is only true for emission extended on very large scales, when the shadow pattern of the mask on the detector plane becomes sufficiently blurred. Conceptually, as long as at least 1 detector pixel is always shadowed by the mask over the entire extent of emission, no flux can be mistaken for unmodulated background. The random placement of mask elements results in occasional, continuous clumps of over five elements across, which means that over a couple degrees all the unmodulated background. The random placement of mask elements results in occasional, continuous clumps of over five elements across, which means that over a couple degrees all the unmodulated background.

3. CHARACTERIZATION OF EXTENDED EMISSION IN BAT IMAGES

To extract fluxes for extended sources, we choose to test a priori model distributions, as opposed to using a method like the “CLEAN” algorithm (Högbohm 1974), which reconstructs fluxes from an unknown underlining distribution assuming the point-spread function (PSF) shape only. (See Appendix B.2 for details about this choice.) We represent a diffuse source as a collection of point sources, each of which is convolved by the PSF (Equation (B1)) and summed together. Throughout this work, image data are fit to these spatial models using the MPFIT algorithm (Markwardt 2009), which performs a Levenberg–Marquardt least-squares minimization to converge on best-fit parameter values.

3.1. Model Spatial Distributions of Hard X-ray Emission

Our goal is to detect IC emission from the same electrons producing the radio halo; however, the electron spatial distribution needs not follow the radio halo if B varies spatially within the ICM (e.g., Dolag et al. 2008). Indeed, there is evidence that the magnetic field in Coma declines with radius (Bonafede et al. 2010), which would allow for a more extended relativistic electron population visible through IC interactions with CMB photons. To accurately search for this potential signal, we need to both choose model distributions for this emission and to fully model the thermal emission also present in the BAT energy bands.

3.1.1. Thermal Models

Following the success of the XMM-Newton-derived temperature map for explaining the thermal origin of the Suzaku HXD-PIN spectrum (Wik et al. 2009), we use the same map to predict the spatial distribution of thermal emission at hard energies. For each region of the map, the flux of the best-fit APEC model is calculated in each BAT energy band and treated as a point source at that location. Note that because the APEC and MeKaL look-up tables are not defined above 50 keV in XSpec, we use MeKaL to derive the temperature map fluxes in the four highest energy bands. Then, for each band the 232 temperature map region “points” are taken together to serve as the diffuse model. To compare this or any of our diffuse models to the BAT image data, each point is assigned the PSF shape with its peak value equal to the point flux, and the overlapping PSFs are summed together and sampled at the location of the image pixels.

Thermal emission is detected in the first four BAT energy bands E1–E4. Since this emission is an extension of the X-ray emission which dominates the XMM-Newton image and its distribution is known, we fix the location of the thermal model to the best-fit position of the model for the E1 band data, where the signal-to-noise ratio (S/N) is the highest. Note that for the thermal model “fits” to the Swift BAT spatial distribution in various bands, only the normalization of the model in each band is allowed to vary. The spatial distribution within each of the bands is completely determined from the XMM-Newton data.

The XMM-Newton data will also contain any non-thermal emission within the XMM-Newton band. Is it reasonable to use the XMM-Newton temperature map and image to determine the spatial distribution of the hard X-ray thermal emission? The spectra in the temperature map were fit over the energy range 0.5 keV < E < 14 keV. While the upper limit of this

Figure 2. Radial profile of the Coma Cluster (crosses, black) compared to a point source of comparable brightness (squares, red; scaled slightly to match Coma’s central flux). Each point represents an individual pixel. The BAT emission from Coma is clearly extended and not axially symmetric, as shown by the larger spread in pixel count rates in its profile compared to the point source. (A color version of this figure is available in the online journal.)
band is fairly hard, the low energy limit guarantees that the spectra are dominated by softer photons. For any sensible non-thermal spectrum, the XMM-Newton spectra are dominated by thermal emission. In fact, if there is cool, dense gas along a given line of sight, the XMM-Newton-based model may actually underestimate the thermal hard X-ray emission. In any case, if there is strong non-thermal emission in the XMM-Newton spectrum, it will dominate the harder BAT energy bands and will be uncovered in the joint spectral fits to the XMM-Newton and BAT spectra (Section 4 below).

3.1.2. Non-thermal Spatial Models

The Suzaku HXD-PIN upper limit, which is 2.5 times below the RXTE and BeppoSAX detections, only excludes those measurements if the IC emission originates from a relatively compact region ($R \lesssim 20'$). More extended emission of roughly uniform surface brightness, however, would be consistent with both the detections and upper limit. In most physical models for the IC, it is likely that the surface brightness would decline with radius; one exception is the KW model discussed below. However, there is no single well-established model for this decline. Since our object is to test the possibility that the difference between our Suzaku HXD-PIN upper limit and the RXTE and BeppoSAX detections is due to the extent of the IC emission, we consider the extreme case of a uniform surface brightness disk. Thus, we assume any non-thermal emission to take the form of a uniform brightness, circular disk with a radius $R = 25'$ (R25), 30' (R30), 35' (R35), 40' (R40), 45' (R45), or 60' (R60).

Recently, Kushnir & Waxman (2010) proposed another model for the IC emission of the Coma Cluster which is consistent with both the Suzaku HXD-PIN upper limit and the RXTE and BeppoSAX detections. In this model, the IC hard X-ray emission comes from a separate population of electrons from those in the radio halo. This new population of electrons is accelerated at the virial accretion shock of the cluster at a very large radius. These virial shock accelerated electrons lose energy quickly and form a shell of hard X-ray emission, which projects on the sky as a ring with nearly uniform surface brightness emission in its interior. We will refer to this as the KW model. While most of the flux resides in a ring at the cluster virial radius, the amount of flux detected by an instrument pointed at the cluster center will depend sensitively on its FOV. We take all the model parameter values for Coma directly from Kushnir & Waxman (2010) when comparing their expected flux to the constraints imposed by the BAT data, though the only relevant parameter for the spatial distribution is the accretion shock radius $\theta_{200} = 82'$. The radial distribution of flux is simply geometrical in form, assuming an infinitely thin shell at this radius; the expression is given in Kushnir & Waxman (2010, Equation (9)).

In reality, it is unlikely the spatial distribution of emission would be as regular and axisymmetric as portrayed by these models. However, for the spatial extent we consider relative to the resolution of the BAT, deviations from the idealized models will not particularly impact our results.

We do not assume that the center of the non-thermal emission distribution from Coma is the same as the center of the thermal emission. Instead, for each of the non-thermal models, the model center is placed at 81 different positions on a $9 \times 9$ grid with 2.5 spacings around the centroid of the large-scale thermal emission. The center of the non-thermal emission is taken as one of the parameters to be varied in the fits of the spatial and spectral distributions below.

3.2. Spatial Fits to the BAT Data

The spatial models for the thermal emission alone, or for the thermal emission plus non-thermal emission, were fit to the pixel values in the BAT images in each of the eight BAT bands. As noted above (Section 3.1.1), the center of the thermal model was determined by fitting the center in the E1 band. For the thermal model, only the overall normalization was allowed to vary. For the non-thermal models, the center was varied for a grid of positions (but fixed in each individual fit, see Section 3.1.2). The model normalization (i.e., flux) in each of the eight BAT bands was fit independently for the thermal and non-thermal models. That is, the spatial fits made no assumptions about the spectrum of either type of emission.

In Figure 3, we present the Swift BAT images of Coma in all eight energy bands (first and third columns) along with the thermal-model-subtracted residuals for bands E1–E4 (center column). The spatial distribution of the thermal models is represented with the contours in the first column. Note that only positively valued pixels appear in the gray scale, which has a square-root scaling, and that for each band pure black corresponds to a slightly different value. Each panel covers an identical 27' x 1'5 region of the sky. Residuals from the fits are consistent with background fluctuations, as can also be seen in the radial profiles shown in Figure 4.

As noted above (Section 3.1.1), these thermal models are solely based on the XMM-Newton temperature map. That is, the spatial distribution is completely determined from the XMM-Newton data, fit over the energy range 0.5 keV $< E < 14$ keV, and only the total normalization, independently measured in each band, is allowed to vary. Ideally, we would use a harder bandpass to derive the temperature map, especially since it is known that such broadband single-temperature fits, when performed on a truly multi-temperature spectrum, produce biased results (Nevalainen et al. 2010). In practice, however, the lower count rate at energies above 2 keV means that temperatures cannot be determined in regions with lower temperature gas or lower flux. We also extract such a temperature map, using the 2–12 keV band, and find systematically higher temperatures, $\lesssim$10 % larger than the temperatures in the map we use here. Taking this map to represent the input spatial distribution, we obtain statistically worse fits to the data, especially in the E1 band. Because cooler, less bright gas in Coma’s outskirts is not included in this temperature map, though it is present in the BAT data, the emission at larger radii cannot be properly fit. In any case, the fluxes we derive in each BAT band do not significantly depend on the absolute temperatures in the map, since only relative temperature differences across the cluster matter, as the total normalization is independently fit for in each band. Because all the temperatures in the map are increased when a higher energy bandpass is used, the flux in each BAT band remains essentially the same regardless of which temperature map is adopted. We therefore use the map determined from the 0.5 keV $< E < 14$ keV band in order to include the cooler gas at larger radius. Regardless, this thermal model provides an adequate description of both the spatial and spectral (discussed in Section 4 below) properties of the detected emission in the BAT data. This success justifies our approach and confirms that extended emission is detected with the same efficiency as that from the cluster center.

The good fit of the XMM-Newton-based thermal model for the emission in BAT bands E1–E4 and the lack of obvious excess emission in the harder E5–E8 bands suggest that non-thermal emission is not very strong or extended.
The Astrophysical Journal, 727:119 (17pp), 2011 February 1

Wik et al.

Figure 3. Images from the eight energy bands of the Swift BAT survey (first and third columns). The gray scale follows a square-root scaling from 0 counts s\(^{-1}\) (white) to \(>10^{-6}\) counts s\(^{-1}\) pixel\(^{-1}\) (black). The contours in the images in the first column show the best-fit thermal model for each band, following a square-root spacing. For E1, the contours range from 0 to \(4.2 \times 10^{-5}\) counts s\(^{-1}\) pixel\(^{-1}\) and for E2 and E3, the contours range from 0 to \(1.7 \times 10^{-5}\) counts s\(^{-1}\) pixel\(^{-1}\), spanning five contours in each case. For E4, the three contours represent the model surface brightness at 0, \(2.5 \times 10^{-5}\), and \(10^{-6}\) counts s\(^{-1}\) pixel\(^{-1}\). The E1 contours occur at the same levels as shown in Figure 1. The middle column shows the thermal model-subtracted residual images for E1–E4, with the same for gray scale as the data on the left. The residuals show that the thermal spatial models are generally well mapped to the actual data. Note that the local background is also fit for and subtracted from the data in the residual images, so the outer fluctuations are not identical to those in the left column. Emission is clearly not detected in the four highest energy bands (E5–E8), which are shown in the third column.

The non-thermal model with the most extended emission is the KW model (Kushnir & Waxman 2010), in which the IC hard X-ray emission comes from a thin shell at a very large radius. Following the methodology in Section B.2, we simulate the expected combined thermal and non-thermal flux distribution for this model and compare to the actual data. The results for the E1 BAT band are shown in the upper panel of Figure 5. Clearly, we do not detect the non-thermal emission expected by the KW model. The lower panel shows the thermal plus KW model compared to a simulation of the BAT data assuming the distribution actually followed this model. It is clear that the statistics in the BAT data would allow us to detect the non-thermal emission from the KW model, were it present. A more quantitative limit is derived in Section 5.

4. SPECTRAL FITS

To search for a non-thermal component in the X-ray spectrum of the Coma Cluster, spectral models are fit to the data. The fits were done for the Swift BAT spectrum alone or simultaneously with the XMM-Newton spectrum of the cluster. The BAT spectra were binned into eight spectral channels, given by the eight standard BAT bands E1–E8. To determine the spectrum in each channel, the total measured raw photon fluxes in each band were converted into “true” photon fluxes using the calibration determined from the BAT Crab spectrum; we also create a generic redistribution matrix to better represent models with spectral shapes that differ from the Crab (see Section A.1). The uncertainties in each channel were determined from the flux uncertainty for a point source \(\sigma_{\text{bgd}}\) (see Section C.1) and
Figure 4. Radial profiles of the data and thermal model fits shown in the first column images of Figure 3. BAT pixels are averaged in annuli of 1′ width (crosses), as are the model values for each pixel position (histogram); the residuals are plotted below each fit, on the same scale as the fit. The structure in the E1 and E3 residuals could be due to a slightly larger PSF FWHM and/or a true spatial distribution of emission that differs slightly from our models; in either case, the effect on the extracted flux would be less than its 1σ error.

then corrected for the effects of source extent as described in Section C.2, Equation (C3), and Table 3. The final uncertainty is given by σ_{diffuse} in Equation (C3). Additionally, a problem with the implementation of the APEC, which we use as our thermal description for spectral fitting, and MeKαL models in XSpec is that the look-up tables are undefined above 50 keV. Therefore, for the four energy channels above 50 keV, we substitute MeKα for APEC. This should have no significant effect given the small thermal flux at these energies relative to the errors.

For the BAT-only spectra, in which only the non-thermal component of the spatial fit is used to build the spectra, a single power-law model is sufficient to measure the non-thermal flux. We also do joint fits of the Swift BAT (containing both the thermal and non-thermal spatial components) and XMM-Newton spectra. In these fits, the excellent statistics at low energies in the XMM-Newton spectra very strongly constrains the thermal emission. However, the XMM-Newton mosaic covers a smaller area compared to either the Swift BAT or most of the non-thermal spatial models. (The XMM-Newton extraction region used for this spectral analysis is indicated by the square in Figure 1.) Thus, in these fits the models applied to the XMM-Newton spectra are reduced by the fraction of the emission in our XMM-Newton spectral extraction region.

4.1. Joint XMM-Newton EPIC-pn–Swift BAT Thermal Emission Fit

We first consider a purely thermal model for the X-ray emission in Coma and fit the Swift BAT and XMM-Newton spectra simultaneously. The spatial distribution of the emission was assumed to follow the thermal model (Section 3.1.1) as determined from the XMM-Newton data. For these and all following fits, we restrict ourselves to energies above 2 keV. This choice ensures that the thermal component is not strongly biased to lower temperatures by cooler gas in these global, multi-phase spectra (e.g., Nevalainen et al. 2010). The resulting single-temperature fit is presented in Figure 6, and the parameters are given in the first row of Table 1. The quality of the fit is quite good, indicating that a single component description for the temperature structure is sufficient and that the spectra have been reasonably well cross-calibrated. A slight ascending trend in the E1–E3 residuals exists, however, which is primarily due to a slightly lower than expected E1 flux. While not particularly
Figure 5. Top panel shows the BAT E1 profile and spatial fit for a model with both thermal emission and non-thermal emission following the KW model (histogram, red). The best-fitted value of the normalization of the KW component is actually negative. The dash-dotted line represents the background level and the dashed line (blue) shows the predicted spatial distribution of flux for the KW model (Kushnir & Waxman 2010) from 14 to 20 keV. The inset expands the scale of the y-axis above it to highlight the difference between the data and the expected flux. In the bottom panel, we perform the same fit to simulated BAT data based on the thermal plus KW model, including shot and systematic noise comparable to that present in the actual data. This shows that the BAT would have easily detected a non-thermal component with the spatial distribution given by the KW model and the predicted flux.

(A color version of this figure is available in the online journal.)

significant, it is worth mentioning several potential causes for the trend. The most straightforward explanation is that the calibration is slightly wrong. We presume the true Crab spectrum to be a simple power law across the entire 2–200 keV interval, but if the spectrum actually steepens around $E \sim 10$ keV as is likely the case (Kirsch et al. 2005), the higher energy bands will be assigned progressively higher flux conversion factors (Column 3 in Table 3); basically, the flux in an energy band will be more and more overestimated for bands at higher and higher energies. Also, because emission is more significantly detected in the lower energy bands, a small change in the overall value of the XMM-Newton and Swift cross-normalization factors—such that the Swift flux would be raised—could reduce the spread in residuals. From a more physical perspective, a single-temperature model is not entirely appropriate; in multi-temperature model fits, the trend in residuals is not as strong. In any case, an adjustment to the cross-calibration of 3%–5% is sufficient to account for the trend, which is well within our assumed 90% confidence interval uncertainty of 10%.

The best-fit temperature is $kT = 8.24 \pm 0.12 \, \text{(stat)} \pm 0.15 \, \text{(sys)}$ keV. The systematic term in the error is based on varying the cross-normalization factor by 10%; the origin of this percentage is discussed in Section 5 below. This global temperature matches extremely well with previous measurements. For example, Hughes et al. (1993) found $kT = 8.21$ keV with a spectrum spanning $\sim 2$ keV $< E < 11$ keV from the Ginga satellite.

Figure 6. Single-temperature (APEC, red histogram) fit to the XMM-Newton EPIC-pn and Swift BAT spectra. The BAT spectra shown are reduced to the fraction which occurs in the XMM-Newton spectral extraction region. The BAT spectra were constructed assuming the spatial distribution predicted by the XMM-Newton temperature map. The origin of the low E1 (14–20 keV) flux is discussed in the text. A single-temperature model ($kT = 8.24$ keV) is sufficient to describe the 2–200 keV emission from the central square degree region of the Coma Cluster.

(A color version of this figure is available in the online journal.)
which had a similar FOV (collimator with $1^\circ -2^\circ$ FWHM) to our aperture, and Arnaud et al. (2001) found $kT = 8.25$ keV over a smaller FOV and lower energy range ($0.3$ keV $< E < 10$ keV) with the XMM-Newton EPIC-MOS instruments. Including lower energy photons tends to lower single-temperature fits to multi-component spectra (Cavagnolo et al. 2008), and having a smaller FOV tends to emphasize the hotter central temperature of $kT \sim 9$ keV in Coma, which explains both why the Ginga and XMM-Newton temperatures agree and why the XMM-Newton–Suzaku analysis of Wik et al. (2009) found a slightly higher $kT = 8.45$ keV. While we find good agreement with other measurements, note that our temperature, along with other temperatures derived with XMM-Newton, could be systematically cooler by a few tenths of a keV than temperatures obtained with other observatories, given the steeper XMM-Newton Crab spectrum and the implications for its instrumental response (see Section A.1).

We also tried a two-temperature thermal model for the XMM-Newton and BAT data. However, the two temperatures and normalizations could not be individually constrained by the data (Table 1); the temperatures/normalizations listed in the table result when the two-temperature model is fit for with initial temperatures of $kT_1 = 6$ keV and $kT_2 = 10$ keV. The two-temperature fit is not a significant improvement on a single-temperature fit.

While the average spectrum in the square degree region around Coma is adequately described with one or two temperatures for the gas, in fact the temperature distribution is quite non-isothermal. We account for temperature variations in the spatial models used to extract fluxes from the BAT images by extrapolating the XMM-Newton temperature map from Wik et al. (2009) to higher energies. This map can also be converted into a spectral model (labeled “T$_{map}$” in Table 1) and compared to the joint spectrum. By including the spatial information of the XMM-Newton data in the spectral model, we can better account for the thermal contribution in the BAT energy bands. The quality of this fit (allowing the normalization, but not the shape, of the model to vary) is reported in Table 1. In principle, the “T$_{map}$” spectral model should perfectly represent the total XMM-Newton spectrum, but due to incomplete coverage of the temperature map with the total XMM-Newton region and the imperfect determination of the individual temperatures, the $\chi^2$ value—which is primarily driven by the higher quality XMM-Newton data—is larger than for the other fits, in which the model shape is free to vary and can account for these minor differences. Even so, the BAT data are slightly better described by this model than by any of the other spectral models presented. Although this result is perhaps unexpected, given that the “T$_{map}$” spatial distribution is used to measure the BAT fluxes, it does indicate that the method is self-consistent.

In all of the thermal models investigated, no evidence for a strong high-temperature component is hinted at by the BAT data.

### 4.2. Non-thermal Spectra

#### 4.2.1. Non-thermal Emission from the Cluster Center

To search for evidence of more centrally located non-thermal emission, an IC component was first fit to purely thermally derived spectra—i.e., spectra created from fits to the BAT data using only the thermal spatial model—which are reported in rows 4 and 5 of Table 1. As in Section 4.1, all fits are to the joint XMM-Newton–Swift spectrum extracted from the square region in Figure 1. Not surprisingly, the thermal model parameters are almost identical to the fits without the IC component, and no significant IC emission is present. The good single-temperature fit to the Swift BAT and XMM-Newton data already suggests that the non-thermal contribution is not very significant. If the photon spectral index $\Gamma$ of the non-thermal component is allowed to vary, it is unconstrained and the best-fitted value is unphysically steep, and in any case, only an upper limit can be placed on the non-thermal flux (Table 1). If we assume a photon index of 2.0 for the non-thermal component based on the radio data (Section 5 below), the 90% upper limit on the 20–80 keV flux

---

**Table 1**

Joint Fits to XMM-Newton and Swift Spectra

| Spatial Model | Spectral Model | $kT$ (keV) | Norm. | $\Gamma$ or $kT$ | $\chi^2$/dof |
|---------------|---------------|------------|-------|-----------------|--------------|
| Thermal Region | Single T | 8.28 ± 0.13 | 0.373 ± 0.002 | ... | ... | 1576.79/1544 |
| Thermal Region | 2T | 7.8 | 0.25 | 0.4 | 0.12 | 1575.77/1542 |
| Thermal Region | $T_{map}$ | ... | ... | ... | ... | 1590.01/1545 |
| Thermal Region | T+IC$^c$ | 8.27 ± 0.13 | 0.373 ± 0.003 | 7.2 | $<0.51$ | 1576.79/1543 |
| Thermal Region | T+IC$^d$ | 8.27 ± 0.13 | 0.373 ± 0.003 | 2.0 | $<0.00148$ | 1577.21/1543 |
| Thermal and KW | Single T | 8.30 ± 0.13 | 0.373 ± 0.002 | ... | ... | 1570.32/1544 |
| Thermal and KW | 2T | 7.8 | 0.25 | 0.12 | ... | 1568.63/1542 |
| Thermal and KW | $T_{map}$ | ... | ... | ... | ... | 1584.59/1545 |
| Thermal and KW | T+IC$^c$ | 8.30 ± 0.14 | 0.372 ± 0.002 | −1.5 | $<1.9 \times 10^{-9}$ | 1570.23/1543 |
| Thermal and KW | T+IC$^d$ | 8.30 ± 0.14 | 0.373 ± 0.003 | 2.0 | $<0.00082$ | 1570.62/1543 |

Notes:

- $^a$ Normalization of the APEC thermal spectrum, which is given by $(10^{-14}/[4\pi(1+z)^2D_A^2]) \int n_e n_H dV$, where $z$ is the redshift, $D_A$ is the angular diameter distance, $n_e$ is the electron density, $n_H$ is the ionized hydrogen density, and $V$ is the volume of the cluster.
- $^b$ Value is $\Gamma$ for the T+ IC model and $kT$ (in keV) for the 2T model.
- $^c$ Value is the normalization of the power-law component for the T+ IC model, which is the photon flux at a photon energy of 1 keV in units of photons cm$^{-2}$ s$^{-1}$ keV$^{-1}$. For the 2T model, the value is the normalization of the second APEC thermal model in units of cm$^{-2}$.
- $^d$ Parameters unconstrained.
- $^e$ Value of $\Gamma$ is fixed when deriving errors.
- $^f$ Value of $\Gamma$ fixed based on radio spectrum.
is 1.24 × 10^{-12} \text{ erg s}^{-1} \text{ cm}^{-2}, which corresponds to <0.8\% of the total flux in the range 2 \text{ keV} < E < 200 \text{ keV}.

4.2.2. Extended Non-thermal Emission

Our goal is to search for extended non-thermal emission, which is measured with spatial model fits to the unlimited FOV BAT survey images (Section 3.2). Because the thermal and non-thermal spatial model normalizations are individually and simultaneously allowed to vary to best match the total flux in the BAT images, spectra can be created from the sum of both components or separately, and also within any aperture. For each of the 81 grid positions relative to the center of the cluster at which each non-thermal model was fitted for, two spectra are produced. One consists of the total, unvignetted flux of the non-thermal component only, and the other includes the sum of both the thermal and non-thermal emission inside the \textit{XMM-Newton} extraction region. The second type of spectrum has the advantage that it can be jointly fit with the EPIC-pn spectrum, which in the case of a non-detection provides a tighter constraint on the flux of non-thermal emission than the first type, since the non-thermal component must be consistent with the higher quality, lower energy \textit{XMM-Newton} data as well. In none of these cases, for either type of spectrum, is a non-thermal component detected with \( 2\sigma \) confidence. We therefore conclude that, while the \textit{Swift} BAT instrument is certainly sensitive to extended emission, none of a non-thermal origin is observed in the current version of the survey. As an example, the fit parameters for various spectral models are shown in Table 1 for the KW spatial model nominally positioned (i.e., centered on the large-scale \textit{XMM-Newton} emission).

In Figure 7, the non-thermal model with the most significant IC component is shown, assuming a fixed photon index \( \Gamma = 2 \) for the spectral fits of each non-thermal spatial distribution tried. Note that the model in this figure represents the upper limit for a non-thermal component, not its best-fit value, and that the cross-normalization has been adjusted by 10\% in the direction that favors a non-thermal signal. The BAT spectra in Figures 6 and 7 are quite similar, indicating that even in the most favorable case the data reject a significant IC contribution to the spectrum of the Coma Cluster, extended or otherwise.

5. UPPER LIMITS TO DIFFUSE, NON-TEMPERAL EMISSION

To ensure that appropriate upper limits are derived, we must determine and include any important systematic uncertainties in our results. Typically, instrumental and/or cosmic backgrounds can be a serious concern and must be carefully treated. At lower energies where the thermal emission is bright, the background is not comparable to cluster emission until an energy of \( \sim 7 \) keV, so even a background uncertainty of a few percent does not significantly impact the \textit{XMM-Newton} EPIC-pn spectrum. This background includes both the non-X-ray and cosmic backgrounds. Given the size of the mosaic, the uncertainty in the overall EPIC-pn background used here (\( \sim 2\% \)–12 keV) is 2.4\% (Read & Ponman 2003). Increasing the \textit{XMM-Newton} background favors larger non-thermal fluxes since this reduces the temperature slightly, so the \textit{XMM-Newton} background is raised by 2.4\% during upper limit derivations. Point sources in the \textit{XMM-Newton} mosaic account for only \( \sim 1\% \) of the emission and have a spectrum that as a whole does not vary significantly from a \( \Gamma \sim 2 \) power law (Wik et al. 2009), so we do not model their contribution to the \textit{XMM-Newton} spectrum. While their flux may artificially enhance a non-thermal signal, ignoring them will only result in slightly more conservative upper limits. For the BAT survey data, the background is automatically removed as part of the image reconstruction procedure, and systematic variations are encoded as fluctuations in empty sky regions, which is already included in the error budget.

The more significant systematic uncertainty is in the determination of the cross-calibration between \textit{Swift} and \textit{XMM-Newton}. Ideally, there should be no uncertainty since we basel the BAT calibration on the \textit{XMM-Newton} data and the \textit{Suzaku} XIS0 Crab spectrum. However, the slope of the calibration (i.e., the assumed photon index of the Crab) is less certain. The total error, statistical and systematic, of the photon index in \textit{XMM-Newton} EPIC Crab fits is \( \pm 0.05 \) (Kirsch et al. 2005), so we adjust our calibration to make the canonical Crab spectrum flatter by 0.05, which acts to increase the BAT fluxes (\( \sim 10\% \) for E1, \( \sim 20\% \) for E8) and flatten the BAT spectra, thus enhancing non-thermal fluxes. This approach to the systematic uncertainty is also conservative, as it is known that the Crab spectrum steepens above 10 keV (e.g., Kirsch et al. 2005).

Since we have no clear detection of non-thermal emission, we must decide on its photon index from other arguments. The natural choice is to use the spectral index of the radio halo, or \( \Gamma = 1.5\text{--}2.5 \) (Giovannini et al. 1993), though the lower range of the X-ray regime explored here corresponds to lower energy electrons where the emission may have a flatter spectrum. Also, both previous detections using \textit{RXTE} and \textit{BeppoSAX} data found \( \Gamma \sim 2 \), and the model of Kushnir & Waxman (2010) predicts this photon index. Therefore, we fix the non-thermal power-law index to \( \Gamma = 2 \), primarily because we are most interested in directly comparing our upper limits with these previous detections and model predictions. If the spectrum of non-thermal emission is in fact flatter, our upper limits will be low by some amount since the BAT errors are large and the \textit{XMM-Newton} data will have less leverage on the fits. However, the high energy flux will not increase dramatically; as illustrated...
Figure 8. Upper limits (small arrows) for each non-thermal spatial model relative to the RXTE (Rephaeli & Gruber 2002, upper cross, green), BeppoSAX (Fusco-Femiano et al. 2004, lower cross, red), and Suzaku (Wik et al. 2009, long arrow, blue) detections/upper limit. The previous flux detections \((1.5 \pm 0.5) \times 10^{-11} \text{ erg cm}^{-2} \text{s}^{-1}\) and upper limit \((6 \times 10^{-12} \text{ erg cm}^{-2} \text{s}^{-1})\) are corrected to account for the fraction of emission missed due to vignetting by the collimator response functions (see the text). In the top panel, upper limits are calculated from the simultaneous joint fits to the XMM-Newton and Swift spectra, and all non-thermal fluxes reported are from inside the XMM-Newton extraction region (the square in Figure 1). In the bottom panel, upper limits are derived from BAT spectra created from the non-thermal component of spatial fits only, and the fluxes represent the total emission of the spatial model. Based on the results presented in the top panel, we conclude that extended IC emission cannot reconcile the discrepancy between the Suzaku and RXTE/BeppoSAX observations.

In Table 3 of Wik et al. (2009), the 20–80 keV flux rises by a factor of two from \( \Gamma = 2 \) to \( \Gamma = 1.5 \), and trials show the same behavior for the non-thermal component in this work.

For the above systematic uncertainties, we find the 90% confidence upper limits to non-thermal emission for both the non-thermal-only BAT and for the joint EPIC-pn/BAT spectra. The thermal component in the latter case is simultaneously fit with the normalization of the non-thermal component. We present each individual limit in Figure 8 along with the vignetting corrected fluxes/upper limit from RXTE (Rephaeli & Gruber 2002, upper cross, green), BeppoSAX (Fusco-Femiano et al. 2004, lower cross, red), and Suzaku (Wik et al. 2009, upper limit, blue). The collimator responses for these instruments are convolved with the model flux distributions to give these values or limits. The Suzaku HXD-PIN instrument is a square collimator with spatial sensitivity of the form given in Equation (3) of Wik et al. (2009), and the RXTE PCA/HEXTE and BeppoSAX PDS instruments are hexagonal collimators with triangular approximation full width half-maximum (FWHM) of \(1^\circ\) and \(1.3^\circ\), respectively. We approximate the nearly axisymmetric response with a fourth-order polynomial of the form

\[
R_{\text{hex}}(\theta) = 1.00 - 1.36 \left( \frac{\theta}{\theta_{\text{max}}} \right) + 0.46 \left( \frac{\theta}{\theta_{\text{max}}} \right)^2 - 0.58 \left( \frac{\theta}{\theta_{\text{max}}} \right)^3 + 0.48 \left( \frac{\theta}{\theta_{\text{max}}} \right)^4 ,
\]

where \(R_{\text{hex}}(\theta)\) is the fraction of emission visible to the instru-

| Model | Joint BAT limit \((10^{-12} \text{ cgs})\) | RXTE \((10^{-12} \text{ cgs})\) | BeppoSAX \((10^{-12} \text{ cgs})\) | Suzaku \((10^{-12} \text{ cgs})\) |
|-------|---------------------------------|-----------------|-----------------|-----------------|
| KW    | -3.86                          | 16.8 ± 5.6      | 8.3 ± 2.8       | <24.8           |
| R80   | -2.16                          | 19.3 ± 6.4      | 13.4 ± 4.5      | <25.7           |
| R45   | -2.34                          | 23.0 ± 7.7      | 18.4 ± 6.1      | <25.4           |
| R40   | -2.53                          | 25.3 ± 8.4      | 21.0 ± 7.0      | <24.7           |
| R35   | -2.95                          | 26.1 ± 8.7      | 22.4 ± 7.5      | <21.7           |
| R30   | -3.22                          | 23.7 ± 7.9      | 21.0 ± 7.0      | <16.8           |
| R25   | -3.48                          | 21.7 ± 7.2      | 19.7 ± 6.6      | <13.3           |

Note. a Units for flux are \(10^{-12} \text{ erg cm}^{-2} \text{s}^{-1}\).

ment at off-axis angle \(\theta\) and \(\theta_{\text{max}}\) is where emission is no longer detected. For each spatial model, our upper limits are ordered in Galactic coordinates from the lowest values of \(l\) and \(b\) in our grid, incrementing \(l\) for all positions with that latitude before incrementing \(b\), with \(l\) reset to the minimum value. It is this ordering that produces the pattern evident in the limits. The limits for the joint spectral fits are given in the top panel, while the non-thermal-only spectral limits are provided in the bottom panel.

Surprisingly, the upper limits derived from extended spatial models and the BAT data alone (bottom panel) are comparable in sensitivity to the previous detections/limit. Larger models are generally less constrained, due to the greater uncertainty in their estimated flux (Equation (C3)), though local fluctuations have a greater impact on smaller models, increasing the spread with position. Stronger constraints are obtained when lower energy emission is simultaneously considered (top panel), and a similar range in upper limits is found for each spatial model distribution. This result is not surprising, as each model contributes roughly the same amount of flux inside the XMM-Newton extraction region, since most of them are extended beyond this region. Interestingly, the KW model provides the limits most consistent with the BeppoSAX detection, which follows from the large PDS FOV—it would observe a higher proportion of the brighter ring otherwise—from the Coma Cluster. We find no evidence for any of the spatial models when one fully accounts for the differences in spatial sensitivity between instruments. Our upper limits, for the nominal case where the non-thermal distribution is centered on the large-scale thermal emission, are compared to these previous measurements in Table 2. However, note that for the KW model we tested only the nominal case model parameter values; because some of these parameters are not well-determined, it is not unreasonable that another choice of values could be consistent with the BAT data.

6. IMPLICATIONS AND DISCUSSION

By taking advantage of the crude imaging capabilities of the Swift BAT instrument and the impressive sensitivity of the 58-month all-sky survey, we are able to constrain the amount of non-thermal, hard X-ray emission—extended or otherwise—from the Coma Cluster. We find no evidence for an extended, hard excess that could reconcile recent detections from RXTE (Rephaeli & Gruber 2002) and BeppoSAX (Fusco-Femiano et al. 2004) with the upper limit from Suzaku (Wik et al. 2009); note, however, that these detections would still be in conflict with the upper limit of Rossetti & Molendi
Generic, uniform surface brightness disks, along with a recently proposed IC model (Kushnir & Waxman 2010), were fit to BAT survey images, converted to spectra, and investigated for signs of a non-thermal component. For each spatial model, we compute upper limits on a grid of positions and compare them to previous measurements, being careful to convert detected fluxes into intrinsic source fluxes, given a particular spatial distribution, by accounting for the collimator vignetting functions. These are direct comparisons, in the sense that the instrumental response of all detectors involved has been fully considered, and as such we, like Rossetti & Molendi (2004), cannot confirm the claimed detections of Rephaeli & Gruber (2002) and Fusco-Femiano et al. (2004).

Their observed hard excesses could have had other reasonable sources, if not diffuse IC emission from the non-thermal phase of the ICM. A common difficulty is an accurate determination of both the cosmic and non-X-ray background, the treatment of which is the primary difference between Fusco-Femiano et al. (2004) and Rossetti & Molendi (2004). Another possibility is the variable nature of nearby point sources, most notably the AGN W Comae, which was once quite bright but has been fading for many years. The concurrence of the RXTE and BeppoSAX observations could have simply been unlucky and caught W Comae (or another source) in a bright state. A somewhat more subtle, and perhaps more likely, explanation concerns the multi-temperature nature of Coma’s ICM. Small amounts of hot gas could dominate the high energy emission, so the extrapolation of an average temperature determined from lower energy data may not be an adequate description of the thermal contribution to the high energy flux. The effect of the multi-temperature gas on Coma is evident in the southwest extension at high energies observed by INTEGRAL (Renaud et al. 2006b; Eckert et al. 2007) and confirmed here; higher temperatures seen at this location in the temperature map (Wik et al. 2009) are sufficient to explain the change in morphology, which points to the increased significance of this gas at higher energies. Even so, single-temperature spectral fits do not produce IC detections in this study or in Wik et al. (2009). The explanation may simply rest in a slight mischaracterization of the hard energy emission weighted temperature; in Fusco-Femiano et al. (2004), the FOV of the lower energy HPSPC instrument does not quite match the higher energy PDS, and the temperature of 7.67 ± 0.1 keV found in Rephaeli & Gruber (2002) is significantly below that allowed by the XMM-Newton data.

Given radio synchrotron emission and an upper limit on the X-ray IC flux, a lower limit on the average ICM magnetic field can be estimated, as described by Equation 13) in Winter et al. (2009) and the accompanying text. A diffuse radio flux of 640 mJy at 1.4 GHz is detected out to a radius of ~40′ in Deiss et al. (1997). For comparison, we will use the upper limit of 2.7 × 10\(^{-12}\) erg s\(^{-1}\) cm\(^{-2}\) (20 < E < 80 keV) from the R = 40′ disk model. These values imply B > 0.25 μ G, an increase from Winter et al. (2009) but still well below the equipartition value of B\(_{eq}\) = 0.5 μ G for the Coma radio halo (Giovaninni et al. 1993). A slightly lower limit of B > 0.2 μ G results if a more conservative IC upper limit of 4.2 × 10\(^{-12}\) erg s\(^{-1}\) cm\(^{-2}\) is used, which considers the limits from all spatial models tested. Regardless, these limits on B fall well below line-of-sight estimates of several μ G from Faraday rotation measure (RM) observations (Feretti et al. 1995), though due to geometric effects these measurements may not represent the average cluster magnetic field (Petrosian 2001).

However, the global field may be recovered by combining many RM measurements along different lines of sight through the ICM with numerical simulations (Murgia et al. 2004). Bonafede et al. (2010) have applied this method to the Coma Cluster, deriving a radial profile where the energy density of the magnetic field falls roughly in proportion with the energy density of thermal gas and with a central field strength of B\(_0\) ~ 4.7 μ G. Combining this model of B(r) with an approximate representation of the radial density profile of synchrotron emission, implied by a rough β-model fit to the point-source-subtracted image of Deiss et al. (1997) (r\(_c\) = 18′, β = 1, and l\(_0\) = 1.23 mJy arcmin\(^{-2}\)), directly leads to a prediction of the expected IC surface brightness as a function of radius. Our illustrative—due to the large uncertainties in all parameters assumed in this exercise—IC surface brightness distribution is flat out to ~30′ with a 20–80 keV flux of ~8 × 10\(^{-17}\) erg s\(^{-1}\) cm\(^{-2}\) arcmin\(^{-2}\), at which point it nearly linearly drops toward zero, though not reaching it, around a radius of 90′. This surface brightness is about an order of magnitude below that implied by our upper limits, providing a possible explanation for why we are unable to detect an IC signature. An order of magnitude lower hard X-ray flux for Coma is also predicted by Brunetti & Lazarian (2010, see their Figure 5), who have developed the most comprehensive picture yet of radio halo generation by MHD turbulence. On the other hand, larger IC fluxes would be expected if the radio synchrotron emission falls off more gradually than modeled here, since a flatter radial profile would suggest a higher relativistic electron density given the falling magnetic field with cluster radius. More accurate maps of Coma’s radio halo, preferably at lower frequencies where the radio electrons correspond more closely to the IC-emitting electrons, will clarify this issue.

Ultimately, a true detection of IC emission from Coma will have to wait for upcoming missions with focusing hard X-ray telescopes, namely NuSTAR\(^8\) and Astro-H.\(^9\) For NuSTAR to achieve a sensitivity comparable to our upper limits, a single pointed observation of at least 100 ks will be required (Madsen et al. 2009). However, the much finer spatial resolution will remove the uncertainty associated with bright background active galactic nuclei (AGNs) and allow multiple spatially resolved joint fits. Assuming the hottest gas, which produces the largest amount of thermal emission at high energies, is localized, then these regions can be identified and avoided in order to detect a lower surface brightness, but more uniform, IC component. Similarly, if the IC emission is more localized, it will be easier to identify with spatially resolved joint fits between XMM-Newton and NuSTAR or Astro-H spectra, as has been done with Chandra data alone (Million & Allen 2009). The unambiguous detection of IC emission associated with radio halos and relics is crucial to determining the energy content in the relativistic phase of the ICM and how significant of an influence this phase has on the dynamics and structure of the thermal gas in clusters.

We thank W. Reich who kindly provided us with the Deiss et al. (1997) radio image, C. B. Markwardt who explained to us (and wrote) many of the BAT software analysis routines used in this work, D. Kushnir and E. Waxman for helpful comments and pointing out a small error, and the referee D. Eckert for helpful comments that particularly improved the clarity of the paper. D.R.W. was supported by a University of Virginia GSAS Dissertation Year Fellowship and a Virginia Space Grant Consortium Fellowship. D.R.W. and C.L.S. were supported in part by

\(^{8}\) http://www.nustar.caltech.edu/
\(^{9}\) http://astro-h.isas.jaxa.jp/
NASA through Suzaku grants NNX08AZ99G, NNX09AH25G, and NNX09AH74G, and XMM-Newton grants NNX08AZ34G and NNX08AW83G. Basic research in radio astronomy at the NRL is supported by 6.1 Base funding.

APPENDIX A

XMM-NEWTON EPIC-PN–SWIFT BAT CROSS-CALIBRATION

Because the systematic uncertainties in the survey-averaged spectrum of the Crab Nebula are smaller than the uncertainties in the BAT survey response matrix, BAT survey fluxes are tied to the Crab fluxes in each band since the systematic uncertainties in the survey-averaged spectrum of the Crab Nebula are smaller than the uncertainties in the BAT survey response matrix (see Tueller et al. 2010, Section 4.5). This method also requires that the intrinsic Crab spectrum be defined since its exact spectrum remains somewhat uncertain (see Section A.2 below), particularly at higher X-ray energies. In practice, though, we are less concerned with an accurate absolute calibration for the BAT than we are with, in this case, an accurate calibration relative to our XMM-Newton EPIC-pn spectrum. Therefore, instead of prescribing a canonical Crab spectrum as close to the true spectrum as it has been measured thus far, we need to set it to the Crab spectrum as measured by the XMM-Newton EPIC-pn instrument over the energy range we consider. Otherwise, systematic calibration errors between the instruments could significantly affect our result, since our goal is to detect excess radiation at hard energies due to non-thermal emission. Errors leading to steeper (flatter) XMM-Newton spectra and flatter (steeper) Swift spectra, for example, will reduce (increase) the thermal contribution at higher energies and similarly enhance (suppress) a non-thermal signal. In other words, any systematic miscalibrations are mimicked in the BAT calibration so that thermal and non-thermal models can be simply applied during joint fits of the data.

A.1. The Spectrum of the Crab According to XMM-Newton

Because of its high X-ray flux, simple spectrum, and lack of significant variability, the pulsar wind nebula of the Crab supernova remnant has been proposed as an X-ray standard flux calibrator (Kirsch et al. 2005). Observations over a large range of energies and with many diverse instruments reveal an intrinsic spectrum nearly consistent with a single power law; however, the photon index and normalization determined by each detector exhibit small but not insignificant differences (Kirsch et al. 2005; Weisskopf et al. 2010). XMM-Newton EPIC-pn measurements, which require that observations are made in burst mode due to XMM-Newton’s large collecting area, are best fit with a steeper than average photon index ($\Gamma = 2.13$ versus $\Gamma = 2.08$ for simultaneous fits to many instrument observations; Kirsch et al. 2005) that is driven by the shape of the spectrum from 0.5–2 keV. However, the residuals to this fit in their Figure 7 suggest that for energies above 2 keV, the XMM-Newton photon index is more in line with the average, and since we only consider energies above 2.3 keV, we need to determine what the Crab spectrum is measured to be in this range.

Instead of fitting the Crab spectrum directly, we choose to compare the XMM-Newton data to Suzaku XIS0 data, which has been well calibrated and consistently fit over its energy range using observations of the Crab. Spectra from each instrument are extracted from identical spatial regions at the center of the Coma Cluster (specifically, Region 10 from Wik et al. 2009), where both the gas temperature and surface brightness are roughly constant. Fitting each spectrum from 2.3 to 12 keV with a single-temperature APEC model, we find the XMM-Newton-derived temperature to be slightly, though not insignificantly, lower than the Suzaku temperature: 8.32 keV versus 8.90 keV. The lower EPIC-pn temperature is consistent with an increasingly larger effective area at higher energies relative to Suzaku’s high energy effective area; positing that XMM-Newton’s calibration is correct, the relative Suzaku effective area at larger energies should be increased as a function of energy, which would lower the flux and therefore the temperature. We model this effect as a multiplicative power-law component to the Suzaku APEC fit, which simultaneously accounts for both the gradient and the overall cross-normalization between the two instruments. Fixing the APEC model parameters to those found with the fit to the XMM-Newton spectrum, we find this modification to the Suzaku calibration: $f(A_{\text{eff}}) = 0.923 (E/1\text{keV})^{0.045}$. In other words, Suzaku spectra are flatter than XMM-Newton spectra and have similar hard band fluxes; however, note that the XMM-Newton effective area had previously been reduced by 15%, as per the analysis in Wik et al. (2009), in order to match the 2–10 keV EPIC-pn and XIS0 fluxes. Dividing the XIS0 best-fit Crab spectrum of Ishida et al. ($F_{\text{Crab, XIS0}}(E) = 9.51 (E/1\text{keV})^{-2.05}$, given in Suzaku Memo 2007–110) by $f(A_{\text{eff}})$ finally yields the correct parameters for the XMM-Newton fit to the Crab spectrum in the energy range of interest ($E > 2\text{ keV}$):

$$F_{\text{Crab}}(E) = 10.30 \left( \frac{E}{1\text{keV}} \right)^{-2.05} \text{photons cm}^{-2} \text{s}^{-1}. \quad (A1)$$

We take this equation as our canonical Crab spectrum. Then, the true flux of a source in each of the eight bands is given by the BAT source count rate in that band divided by the observed Crab BAT count rate in that band and multiplied by the spectrum in Equation (A1) integrated over the band (see Tueller et al. 2010, Equations (2)–(4)). This conversion factor is reported in Table 3 as the “Flux Calib.” Note that this photon index differs significantly from that assumed in Tueller et al. (2010), $\Gamma = 2.15$. Our goal here is to choose a photon index that agrees with the XMM-Newton data and best matches the Crab spectrum at the lowest BAT energies, where it is flatter than at harder energies (see the discussion in Section A.2).

While this method is the standard way to create spectra from BAT survey data, it is technically only valid for source spectra that have a shape similar to the Crab. Unfortunately, the BAT survey redistribution matrix, which could properly account for arbitrary spectral shapes, is more uncertain than the observed Crab fluxes (Tueller et al. 2010). Thermal emission above ~10 keV is typically much steeper than the spectral index in Equation (A1), so we would prefer to include an approximate redistribution matrix that will handle other such spectral models correctly. To do this, we take a standard response matrix for an on-axis source from a single observation and multiply the input energies by a smooth function so that the flux-converted Crab spectrum matches Equation (A1) to <1 % in all energy bands. The addition of this redistribution matrix has a minor effect on spectral fits generally, but it does improve the quality of fits using a thermal model, so we employ it throughout.

10 http://www.astro.isas.ac.jp/suzaku/doc/suzakumemo/suzakumemo-2007-11.pdf
The Astrophysical Journal

...amounts of thermal versus non-thermal emission in the joint quoted hereafter may differ from their true fluxes, the relative rates to true fluxes are not guaranteed. The goal instead is to... canonical Crab spectrum is at some level arbitrary. Calibration method relies on using the Crab as a flux standard, shape—are carefully conserved. Ultimately, because our BAT... 20.14-195 75.19 3.84 1.31 1.24 1.42 1.45 1.26 1.29 1.23 1.65 1.56 1.93

Notes.

a “Flux Calibration,” defined such that the incidence photon flux at the Earth (photons cm\(^{-2}\) s\(^{-1}\)) is given by the BAT source count rate multiplied by Flux Calib.
b Units are \(10^{-5}\) photons s\(^{-1}\) cm\(^{-2}\).

A.2. The Hard X-ray Spectrum of the Crab

With this approach, accurate conversions from BAT count rates to true fluxes are not guaranteed. The goal instead is to match the BAT calibration with the EPIC-pn calibration, which ensures that spectral models can be applied seamlessly between the *XMM-Newton* and *Swift* spectra in joint fits. While fluxes quoted hereafter may differ from their true fluxes, the relative amounts of thermal versus non-thermal emission in the joint spectra—considering both their cross-normalization factor and shape—are carefully conserved. Ultimately, because our BAT calibration method relies on using the Crab as a flux standard, and since the true Crab spectrum is not known, the choice of a canonical Crab spectrum is at some level arbitrary.

Even so, the hard band fluxes derived herein should be consistent with fluxes derived from other missions. Using the same power-law form as for Equation (A1), Kirsch et al. (2005) found a range of normalizations and photon indices for several instruments that overlap with the BAT energy bands: *BeppoSAX* PDS: 8.84 \(E^{-2.126}\), *RXTE* PCA: 11.02 \(E^{-2.025}\), *RXTE HEXT*: 9.9 \(E^{-2.090}\), INTEGRAL ISGRI: 15.47 \(E^{-2.225}\), and INTEGRAL SPI: 15.9 \(E^{-2.203}\). These photon indices agree well with the shape of the total Crab spectrum determined by an earlier, detailed balloon-borne study, which found \(\Gamma = 2.12\) (Bartlett 1994). Also, the *Suzaku* PIN fit of 10.93 \(E^{-2.090}\) is consistent with both the scatter in the above results and our adopted spectrum. Ignoring the photon indices derived from *XMM-Newton* data, there seems to be a steepening in the Crab spectrum at higher energies, which means that our relatively flat photon index may overpredict harder band fluxes and thus enhance a potential non-thermal signal. Our Crab spectrum also has a slightly higher overall flux (in the 20–80 keV band), so that fluxes and upper limits may be biased high, though any such biasing would be well within the absolute calibration uncertainties of all the above missions.

Assuming that the INTEGRAL SPI observations are the most accurate, due to its extensive ground calibration, we can compare our adopted model with the results of Jourdain & Roques (2009), which show a clear steepening of the Crab spectrum above 100 keV. Below 100 keV, they find a photon index of 2.07, consistent with our value of 2.095. Their best-fit photon index above 100 keV is 2.24, which would lead our flux calibration to overestimate fluxes in our two highest energy bands. However, since we detect no flux in these bands, extended or otherwise, even a large erroneous calibration—which is not the case here—would not bias or otherwise affect our results. Jourdain & Roques (2009) also fit a smoothly varying power law to their Crab spectrum. Not surprisingly, this model is sufficiently similar to our adopted Crab spectrum, particularly below 50 keV where the flux calibration is more important, that using it instead of our simple power-law model would not lead to quantitatively different results.

APPENDIX B

EXTRACTING BAT FLUXES FROM EXTENDED SOURCES

Very extended, diffuse emission is difficult to detect with coded mask instruments, since the shadow pattern of the mask on the detectors gets smeared out and the signal becomes indiscernible from the background. However, small-scale-extended emission is detectable, as long as its size is less than the minimum scale necessary to dilute the distinguishability of the mask pattern. In the following, we show that, by simulating extended sources as collections of point sources, this minimum scale is larger than our region-of-interest and that essentially 100% of the diffuse emission can be detected.

B.1. BAT Point-spread Function

For on-axis sources in the BAT FOV, the point-spread function (PSF) has a full width half-maximum (FWHM) of \(~22^\prime\). Because the sky image is basically the cross-correlation function of the coded mask with the count rates in the individual detectors, it does not represent the intensity per solid angle (i.e., within a pixel). Instead, a pixel value is proportional to the flux of a point source at that location. The width of the PSF is actually due to oversampling the sky plane, not the scattering of photons inside the instrument, and it depends on the size of individual mask element shadows on the detector relative to the size of detector pixels.

As such, the PSF should not be summed in order to derive the source flux—this is provided by the central peak value—and its FWHM depends on the off-axis angle of the source. The distance between the mask and detector increases as the off-axis angle increases, so an angular separation at large off-axis angles produces a more dramatic shift in the shadow pattern across the detector pixels than more on-axis positions, which effectively...
reduces the oversampling factor and leads to narrower FWHM. Since survey images are created from many “random” individual pointings, each with a given source located at a different off-axis angle, the survey PSF will have an average FWHM and uniform shape, which is roughly Gaussian. Simple Gaussian fits to all the > 10σ sources in all eight bands yield an average FWHM of 19.47, irrespective of signal-to-noise ratio (S/N) or energy band, essentially identical to the value determined in the 22-month survey (Tueller et al. 2010).

The PSF shape is described by a Gaussian to first order, which is not surprising given the non-repeating, randomly filled mask and the many pointings that contribute to the flux at each position. However, as is clear from the residuals to a Gaussian fit to the 14–20 keV band Crab data and another source (Cyg X-2) in Figure 9, deviations on the order of 1% of the flux exist (and are significantly larger than the root mean square (rms) of the background in this case). While this deviation does not strongly impact the flux of point sources, since only the maximum, central value maps to the flux, a diffuse source is composed of overlapping PSFs, where differences in the wings could affect the overall flux. The residual structure in the wings of the PSF is mainly eliminated by the addition of the two-part function:

\[
f(r) = p_0 \left[ e^{-r^2/2\sigma_{psf}^2} + \frac{1}{120} \begin{cases} \cos \pi x & x < 3 \\ -e^{-\pi(x-3)/1.19} & x > 3 \end{cases} \right] + p_1,
\]

where \( p_0 \) is the distance from the center in arcminutes, \( p_0 \) and \( p_1 \) are the fit parameters (the normalization and background, respectively), \( x = 2r/(1.19\text{FWHM})+1 \) (\( x \) has units of radians), and \( \sigma_{\text{psf}} = \text{FWHM}/(2\sqrt{\ln 2}) \). The improved fit for the Crab is illustrated in the very bottom left panel of Figure 9; while in this case the fit is still not perfect, for other sources the fit is typically better (bottom right panel of Figure 9). We take \( p_0 \) to be our measurement of the flux. While the maximum of the PSF may not exactly correspond to \( p_0 \), since all fluxes are determined this way and are also related to the Crab fluxes, any such bias will cancel out during the conversion from BAT count rates to fluxes. Note that most the additional terms to \( f(r) \) could affect a flux, assuming they, for some reason, poorly represented the true PSF shape, is at the \( <1\% \) level.

B.2. Tests of the Detection of Extended Sources

As discussed in Section 3, we extract fluxes for extended sources by fitting a priori model distributions, as opposed to using a method like the “CLEAN” algorithm (Högbohm 1974), which reconstructs fluxes from an unknown underlying distribution assuming the PSF shape only. The “CLEAN” method requires some fine-tuning, such as the region of extraction (for clearly detected sources, expanding the region-of-interest even a little beyond the wings of the source can significantly bias the derived flux), “loop gain,” and completion threshold. In our case, since there are only a few likely spatial distributions for the thermal and any potential non-thermal emission, we are less likely to produce biased fluxes by first assuming a spatial distribution than by using a method like “CLEAN.” We represent a diffuse source as a collection of point sources, each of which is convolved by the PSF (Equation (B1)) and summed together.

We now test whether diffuse sources are detectable over our scales of interest can be evaluated. In general, we treat extended emission as a collection of closely spaced point sources, since existing software is built with these sources in mind. Point sources at any position in the BAT FOV are straightforward to simulate with the HEASOFT Swift batmasking task with the following options set: coord_type=taxxyz; distance=1e7; corrections=forward,unbalanced,flatfield; and rebalance=no. This task outputs the fraction of each detector pixel which is illuminated by the source given its position relative to the detector axis; a value of 0.45 means that 55% of the detector area is shadowed by the mask. At this stage, the detector image can be multiplied by the counts or count rate of the source, and several such detector images representing different sources in the FOV can be added together along with a background—all including Poisson statistics. The background can then be fit and subtracted with the task batclean, and finally a reconstructed sky image can be produced via the task batfftimage. For now, to isolate the detectability of diffuse emission by the BAT, we simply add uniformly bright, perfectly known point source masks without background or source Poisson noise, to create circular, extended disks of various radii \( R \). Images of the sky are constructed with batfftimage for each disk detector image, and the “observed” disk surface brightness profile is fit for as a function of radius. While even large disks (\( R > 10' \)) are visibly noticeable, sky images produced in this way include significant systematic effects induced by the large spatial extent of the emission, leading to high rms noise that eventually destroys the disks’ detectability. The recovered surface brightness, relative to the input level, of simulated diffuse disks of radius \( R \) is presented in Figure 10. Error bars represent the simple error of the mean (\( \sigma_{\text{rms}}/\sqrt{N} \), where \( N \) is the number of pixels used to determine \( \sigma_{\text{rms}} \), and the smooth as opposed to random variation around the input surface brightness results from their systematic nature. For sources in the size range of interest to us, \( R < 1\% \), the intrinsic uncertainty due to the telescope design is \( <3\% \).
The Astrophysical Journal, 727:119 (17pp), 2011 February 1

C.2. Flux Uncertainties for Extended Sources

The error for a point source, or more correctly the error in the value of a given pixel, presented in Section C.1 does not directly apply to extended sources. Also, we cannot take the standard error from spatial \( \chi^2 \) fits, using the point source error as the error for the flux in each pixel, because nearby pixels are correlated. Helpfully, the expected error for diffuse sources has already been derived by Renaud et al. (2006b) for the IBIS coded mask instrument onboard INTEGRAL. In their appendices, they derive source fluxes and errors in reconstructed sky images from detector images and find the straightforward result that the error in a flux measurement from an extended source is proportional to its spatial area normalized by the area of the PSF function (Renaud et al. 2006b, Equation (B3)). Specifically,

\[
\sigma_{\text{ext}} = \sigma_{\text{bgd}} \sqrt{N_{\text{PSF}}}. \tag{C1}
\]

where \( N_{\text{PSF}} \) is the area of the source normalized by the PSF area. If \( I_X(\Omega) \) is the surface brightness of the source convolved with the PSF, \( I_X^{\text{max}} \) is its maximum value, \( \Omega \) is the solid angle, and \( f(\Omega) \) is the PSF, then

\[
N_{\text{PSF}} = \frac{\int I_X(\Omega) d\Omega}{I_X^{\text{max}} \int f(\Omega) d\Omega}. \tag{C2}
\]

Before we generally apply Equation (C1) to Swift BAT data, we test whether this prescription does in fact apply to extended sources in the Swift BAT. For each of the diffuse thermal (Section 3.1.1) or non-thermal (Section 3.1.2) spatial models described above, we created 121 simulations of the extended source and a number of other point sources in the FOV, each with detector counts for the source fluxes and background randomly assigned (taken from a Poisson distribution). Each simulated observation is made from a unique position on an \( 11 \times 11 \) grid, with the relative positions of all the sources kept intact. Both the variation of position relative to the telescope axis and the inclusion of point sources are necessary to fully recreate the systematic contribution to the error. The simulated detector images are then background subtracted and converted into sky images via the procedure outlined in Section B.2. The total flux of the diffuse sources is chosen so that the S/N is \( \sim 20–50 \). To check Equation (C1), fluxes of all the sources are measured in each simulated sky image, and the average standard deviation of the point source fluxes is compared to the standard deviation of the diffuse source flux. We find that the estimated errors for the diffuse models (Thermal band E1, Disks R25–R60, and KW) generally fall below the expected trend with \( N_{\text{PSF}} \) in Figure 11. This discrepancy may be due to the number of simulations we were computationally limited to performing—the distribution of fluxes is only roughly Gaussian—or it may represent a true deviation from the results of Renaud et al. (2006b). However, to be safe we use Equation (C3) to calculate the error of fluxes extracted with the corresponding model.

There is one additional modification to errors on fluxes extracted with our methodology. Because we fit a spatial model, convolved by the PSF, to the BAT image data, the error in the flux is not just the standard deviation of nearby background pixels, but it depends on how the model is fit to all the pixels. For example, the distribution of normalizations from many fits of a Gaussian function to random data of mean zero and standard deviation \( \sigma_{\text{bgd}} \) will not equal \( \sigma_{\text{bgd}} \) but some value \( < \sigma_{\text{bgd}} \) depending on the pixel scale. A delta function, or Gaussian of
width zero, will produce a distribution consistent with $\sigma_{\text{bgd}}$, since this is identical to measuring the standard deviation, but anything wider finds an average over several pixels, and therefore the distribution of normalizations will tend to be closer to the mean of the random pixels. For our purpose, where the normalization is related to the source flux, the correct error of a flux should come from the distribution of model fits to background (empty) regions of the survey, which may not be equivalent to $\sigma_{\text{bgd}}$. Unlike in the above example, neighboring pixels in the survey are correlated due to oversampling—this is essentially the origin of the PSF—and so the standard deviation of model normalizations will be affected by this correlation. Generally, the distribution of normalizations will be larger than $\sigma_{\text{bgd}}$ in this case, as $\chi^2$ minimization will be more influenced by the larger fluctuations near the flux extraction region. The net effect does not significantly change the error distribution shape, but simply inflates the effective standard deviation by some factor, $f_m$, which is both model dependent (varying from 1.4 $\sigma_{\text{bgd}}$ for a point source to 2.24 $\sigma_{\text{bgd}}$ for the KW model) and energy dependent since the noise properties vary slightly from band-to-band. The total flux uncertainty for a diffuse source in the BAT survey is adjusted from Equation (C1) to become

$$\sigma_{\text{diffuse}} = f_m \sigma_{\text{ext}} = f_m \sigma_{\text{bgd}} \sqrt{N_{\text{PSF}}}.$$  

(C3)

The precise value of $f_m$ is determined from the standard deviation of fits to 100 blank sky regions, in which we avoid obvious ($>5\sigma$) sources and the Galactic plane ($b > 20^\circ$). These factors are reported for each band in Table 3. Not including this factor in the flux error estimate results in spectral fits with unacceptably high $\chi^2$ values.