Black hole mass estimation with a relation between the BLR size and emission line luminosity of AGN

Xue-Bing Wu¹, R. Wang¹, M.Z. Kong², F.K. Liu¹, J.L. Han²

¹Department of Astronomy, Peking University, Beijing 100871, China
²National Astronomical Observatories of Chinese Academy of Sciences, Beijing 100012, China

Abstract. An empirical relation between the broad line region (BLR) size and optical continuum luminosity is often adopted to estimate the BLR size and then the black hole mass of AGNs. However, optical luminosity may not be a good indicator of photoionizing luminosity for extremely radio-loud AGNs because the jets usually contribute significantly to the optical continuum. Therefore, the black hole masses derived for blazar-type AGNs with this method are probably overestimated. Here we first derived a tight empirical relation between the BLR size and the Hβ emission line luminosity, \( R(\text{light} - \text{days}) = 24.05(L_{H\beta}/10^{42}\text{ergs s}^{-1})^{0.68} \), from a sample of 34 AGNs with the BLR size estimated with the reverberation mapping technique. Then we applied this relation to estimate the black hole masses of some nearby AGNs and found that for many extremely radio-loud AGNs the black hole masses obtained with the \( R - L_{H\beta} \) relation are systematically lower than those derived previously with the \( R - L_{5100 A} \) relation, while for radio-quiet and slightly radio-loud AGNs the results obtained with these two methods are almost the same. The difference of black hole masses estimated with these two relations increases with the radio-loudness for extremely radio-loud AGNs, which is consistent with the fact that their equivalent widths of Hβ emission line become smaller at higher radio-loudness. If the small Hβ equivalent widths of extremely radio-loud AGNs are indeed caused by the beaming effect, we argue that the optical emission line luminosity may be a better tracer of ionizing luminosity for blazar-type AGNs and the black hole mass derived with the \( R - L_{H\beta} \) relation are probably more accurate.

Key words: black hole physics – galaxies: active – galaxies: nuclei – quasars: general – quasars: emission lines

1. Introduction

Supermassive black hole is essential for AGNs activities (Lynden-Bell 1969; Rees 1984). The black hole masses of some nearby AGNs have been recently estimated by the reverberation mapping technique (Wandel, Peterson & Malkan 1999; Ho 1999; Kaspi et al. 2000), with which the size of the broad line region (BLR) can be measured from the time delay between the flux variations of the continuum and the emission lines of AGNs. The black hole mass is then estimated using the Virial theorem from the BLR size and the characteristic velocity (determined by the full width at half-maximum (FWHM) of emission line). So far, the reverberation studies have yielded the black hole masses of about 20 Seyfert 1 galaxies and 17 nearby bright quasars.

An empirical relation between the BLR size (\( R \)) and the optical continuum luminosity at 5100 Å (\( L_{5100 A} \)) has been derived by Kaspi et al. (2000) using the observed data of 34 nearby AGNs. Because the measurement of the BLR size with the reverberation mapping technique needs long-term monitoring of continuum and emission line fluxes, it is impractical for most AGNs. Therefore, the empirical relation has been frequently adopted to estimate the BLR size and then derive the black hole masses for AGNs in some samples of mostly radio-quiet objects (Laor 2000; McLure & Dunlop 2001; Wandel 2002), and of purely radio-loud objects (Lacy et al. 2001; Gu, Cao & Jiang 2001; Oshlack, Webster & Whiting 2002). However, the optical luminosity of some radio-loud AGNs (especially blazars), may not be a good indicator of ionizing luminosity, which is usually related to the UV/optical radiation from the accretion disk around the central black hole. The relativistic jets of blazar-type AGNs not only dominate the radio and high energy X-ray and \( \gamma \) ray radiations, but also significantly contribute to the optical luminosity in some cases (Scarpa & Urry 2002). For example, many optical jets have been discovered recently in AGNs by the HST (Scarpa et al. 1999; Jester 2003; Parma et al. 2003), which clearly suggests that the jets contribute significantly in the optical band. Furthermore, optical synchrotron radiation has been detected for many other radio-loud AGNs (Whiting, Webster & Francis 2001; Chiaberge, Capetti, & Celloti 2002; Cheung et al. 2003). Therefore, the measured optical continuum luminosity of some extremely radio-loud AGNs is significantly contributed by
the optical radiation from the jets and may be much larger than the ionizing luminosity required to produce broad emission lines. Using the empirical relation between the BLR size and optical luminosity at 5100Å, which was obtained based on the sample of mostly radio-quiet AGNs (Kaspi et al. 2000), one would significantly overestimate the actual BLR size and hence the black hole mass of these radio-loud AGNs. Oshlack et al. (2002) have shown that their estimated black hole masses would be lower if the synchrotron contribution to the optical flux is subtracted. However, it is not easy to make such a correction for a large sample of radio-loud AGNs. In addition, the contribution of the host galaxy to the optical continuum should also be taken into account especially when the host galaxy of AGNs can be resolved optically. Therefore, optical luminosity may not be a good indicator of photoionization luminosity of AGNs in some cases.

In this paper we will first derive an empirical relation between the BLR size and the Hβ emission line luminosity for 34 AGNs in the sample of reverberation mapping studies. We then argue that the BLR size obtained from the Hβ luminosity is more reasonable at least for some extremely radio-loud AGNs. Finally we apply this new empirical relation to estimate the black hole masses of some quasars and compare them with previous results.

2. The relation between the BLR size and Hβ luminosity

Kaspi et al. (2000) have compiled the observational data of 17 Seyfert galaxies (Wandel, Peterson & Malkan 1999) and 17 nearby quasars with black hole masses estimated with the reverberation mapping technique. Using a linear fit to the available data with errors, they got an empirical relation between the BLR size and the optical continuum luminosity at 5100Å as:

\[ R_{BLR}(\text{light} - \text{days}) = (32.9 \pm 2.0) \times [L_{5100Å}^{\text{black}} / 10^{44} \text{ergs s}^{-1}]^{0.700 \pm 0.033} \]  \hspace{1cm} (1)

With an ordinary least square (OLS) bisector method (Isobe et al. 1990), we can obtain such a relation as \( R_{BLR}(\text{light} - \text{days}) = 31.1[L_{5100Å}^{\text{black}} / 10^{44} \text{ergs s}^{-1}]^{0.701} \), which is almost the same as that shown above. We should keep in mind that this \( R - L_{5100Å} \) relation was obtained with mostly radio-quiet AGNs. The optical continuum luminosity may not be a good indicator for photoionizing luminosity for some extremely radio-loud AGNs. Instead, the emission line luminosity may be a better indicator because it is free from the beaming effects of the jet.

Using the available data of BLR sizes and Hβ fluxes for 34 AGNs in the reverberation mapping studies, we can investigate the relation between the BLR size and the Hβ emission line luminosity (including both broad and narrow components). In Table 1 we listed the BLR size and the luminosity data of these 34 AGNs. The Hβ luminosity is calculated from the Hβ flux which is available for 16 PG quasars, 8 AGNs in Ohio sample, and other 9 Seyfert 1 galaxies (see references listed in Table 1). Because there is no available data of Hβ flux for PG 1351+640 (Kaspi et al. 2000), we exclude this object from our investigation. In addition, we add another Seyfert galaxy Mrk 279 in our sample because both the BLR size and the Hβ flux have been measured recently (Santos-Lleo et al. 2001). All Hβ luminosity data have been corrected for Galactic extinction using the values from NED\(^1\) (see also Burstein & Heiles 1982). The cosmology with Hubble constant \( H_0 = 75 \text{km s}^{-1} \text{Mpc}^{-1} \) and deceleration parameter \( q_0 = 0.5 \) were adopted throughout the paper.

\(^1\) http://nedwww.ipac.caltech.edu
With these data, we derive an empirical relation between the BLR size and $H_\beta$ luminosity. With the OLS bisector method we obtained:

$$\log R (\text{light} \,-\, \text{days}) = (1.381 \pm 0.080) + (0.684 \pm 0.106)\log (L_{H_\beta}/10^{42} \text{ergs s}^{-1}). \quad (2)$$

The slope of this relation is slightly flatter than that of $R - L_{5100} \alpha$ relation given in Kaspi et al. (2000), consistent with $L_{H_\beta} \propto L_{5100}^{0.93}$ obtained by Ho & Peng (2001) for PG quasars. The Spearman’s rank correlation coefficient of our $R - L_{H_\beta}$ relation is 0.91, slightly higher than 0.83 for the $R - L_{5100} \alpha$ relation (Kaspi et al. 2000), which implies that the $R - L_{H_\beta}$ relation is slightly tighter than the $R - L_{5100} \alpha$ relation. We also used the linear fit to the data with errors that was used by Kaspi et al. (2000) to derive the $R - L_{5100} \alpha$ relation. Applying this method to the $R - L_{H_\beta}$ relation yields the same result as the OLS bisector method.

In Fig. 1 we show the dependence of the BLR size on $L_{H_\beta}$ and $L_{5100} \alpha$. The two relations are similar and thus the $R - L_{H_\beta}$ relation can be an alternative of the $R - L_{5100} \alpha$ relation in estimating the BLR size for radio-quiet AGNs.

### 3. Comparison of black hole mass estimation of AGNs from two relations

Since the $R - L_{5100} \alpha$ relation obtained by Kaspi et al. (2000) has been frequently used to estimate the BLR size and the black hole mass of both radio-quiet and radio-loud AGNs, it is important to investigate the applicability of such an approach for radio-loud objects.

Brotherton (1996) studied the emission line properties of 59 radio-loud quasars. We adopted his published values of absolute $V$-band magnitude, equivalent width and FWHM of $H_\beta$ emission line. The continuum luminosity at $5100 \alpha$ and the $H_\beta$ luminosity (scaled to our cosmology parameters) were calculated after considering the Galactic extinction and K-correction (optical spectral index was assumed to be 0.3). We then estimated the BLR size using both $R - L_{H_\beta}$ and $R - L_{5100} \alpha$ relations and derived the black hole mass with the formula $M_{BH} = 3V_{FWHM}^{2}/G$ (here we assumed the BLR velocity $V \sim (\sqrt{3}/2)V_{FWHM}$ as in Kaspi et al. 2000). With these two relations, we also estimated the black hole masses of another 27 radio-loud quasars with available data of both the equivalent width and FWHM of $H_\beta$ emission line in the Parkes Half-Jansky flat-spectrum Sample (PHFS) (Drinkwater et al. 1997; Francis, Whiting & Webster 2000; Oshlack et al. 2001).

We compared the black hole masses obtained with the $R - L_{H_\beta}$ and $R - L_{5100} \alpha$ relations in Figure 2. Evidently the masses obtained with the $R - L_{H_\beta}$ relation are systematically lower than those obtained with the $R - L_{5100} \alpha$ relation for some extremely radio-loud quasars.

![Fig. 2. Upper panel: Comparison of the black hole masses of radio-loud quasars estimated with $R - L_{H_\beta}$ and $R - L_{5100} \alpha$ relations. The squares represent 59 quasars in Brotherton (1996) and the triangles represent 27 PHFS quasars in Oshlack et al. (2001). The diagonal line shows the relation where both masses are identical. Lower panel: The ratios of black hole masses estimated with two different relations are plotted against the radio-loudness of radio-loud quasars. The dashed line indicates the case where the two black hole mass estimates are identical. Evidently $M_{BH}[5100 \alpha]$ becomes systematically larger than $M_{BH}[H_\beta]$ at higher radio-loudness.](image-url)
of black hole masses and the radio-loudness. For some individual quasars with higher radio-loudness, the black hole mass estimated with the $R - L_{5100\AA}$ relation can be $3\sim 10$ times larger than that estimated with the $R - L_{H_\beta}$ relation. In Figure 3 we also plotted the equivalent width (EW) of $H_\beta$ emission line against the radio-loudness for objects in these two radio-loud AGN samples. We can see that the EW($H_\beta$) becomes smaller at higher radio-loudness. Such a relation, although with only a modest Spearman’s rank correlation coefficient of -0.33, indicates that the smaller EW($H_\beta$) of some extremely radio-loud AGNs could be at least partly due to the beaming effects.

For radio-quiet AGNs, however, both the optical continuum and emission line luminosities are probably free from the jet contributions and therefore both can be good tracers of photoionization luminosity. We check this by using the data of 70 low-redshift radio-quiet quasars in the Palomar-Green survey. The emission line properties of these quasars have been studied by Boroson & Green (1992). The continuum luminosity at 5100Å and the $H_\beta$ luminosity were estimated from the absolute V-band magnitude ($M_V$) and the equivalent width of $H_\beta$ emission line listed in their Table 1 and Table 2. Using the $R - L_{H_\beta}$ and $R - L_{5100\AA}$ relations we estimated the BLR sizes and black hole masses of these radio-quiet quasars. The results from the two relations are almost identical (see Figure 4). This is also indicated by the normalized $\chi^2$ value of the deviation of the points plotted in the upper panel of Figure 4, which is 0.94, much smaller than the value 2.58 for the points plotted in the upper panel of Figure 2 for radio-loud AGNs. From the lower panel of Figure 4, we can also see that the difference of the two black hole mass estimates does not correlate with the radio-loudness for radio-quiet quasars. The Spearman’s rank test gives a correlation coefficient of only 0.05, much smaller than that for radio-loud AGNs.

4. Discussions

Using the empirical relation between the BLR size and optical continuum luminosity possibly induces an overestimation of the BLR size and hence the black hole mass of some extremely radio-loud AGNs because of the jet contribution to the optical luminosity. We derived another empirical relation between the BLR size and the emission
line luminosity, and demonstrated that it can be used to estimate the BLR size and black hole mass of both radio-quiet and radio-loud AGNs. If the relativistic jets and host galaxy have significant contributions to the optical continuum, the emission line luminosity is probably a better tracer of ionizing luminosity. Comparisons of the estimated black hole masses with these two different empirical relations clearly indicate that the difference becomes significant if the radio-loudness of AGNs is larger. Using the $R - L_{H\beta}$ relation may result in more accurate estimations of black hole masses of some blazar-type AGNs.

In our study we focused on the possible effects of beaming on the optical continuum in radio-loud AGNs and ignored the difference in BLR physics between radio-loud and radio-quiet AGNs. The modest correlation between the EW($H\beta$) and the radio-loudness may indicate the presence of beaming effects, though some other effects such as a lower covering factor of the BLR of radio-loud AGNs can also lead to smaller EW ($H\beta$) values. Because currently we know little about the difference of BLR physics between radio-loud and radio-quiet AGNs, to prove the validity of our approach it is necessary to compare our estimated black hole mass with an independent estimate, for example, from the correlations of black hole mass with central velocity dispersion and host galaxy luminosity. Unfortunately, not many measured values of central velocity dispersion or host galaxy luminosity for extremely radio-loud AGNs are available. Although there are 8 objects in the sample of Brotherton (1996) with measured host magnitude (McLure & Dunlop 2001), the radio-loudness of these objects are mostly smaller than 1000 and thus the difference estimated with the $R - L_{H\beta}$ and $R - L_{5100}$ relations is rather small. The velocity dispersion measurements for radio-loud quasars are not available and the [OIII] profile in radio-loud AGNs may not be adopted to estimate the central velocity dispersion because of its complexity. Therefore, further imaging studies on the host galaxy and spectroscopic measurements of the central velocity dispersions of a large sample of extremely radio-loud quasars are still desired to confirm our results.

The advantage of using the $R - L_{H\beta}$ relation is that we can estimate the black hole mass of AGNs with only two observed parameters, namely the $H\beta$ line luminosity and its FWHM, and it can be applied to a larger sample of AGNs with redshift smaller than 0.8. In principle, one can analogously investigate the relation between the BLR size and the luminosity of some ultraviolet emission lines such as MgII and CIV, which may be used to estimate the black hole mass of some high redshift AGNs. Some recent studies have suggested to use the ultraviolet continuum luminosity and the FWHM of ultraviolet emission lines to estimate the black hole mass of high redshift AGNs (Vestergaard 2002; McLure & Jarvis 2002). However, the ultraviolet continuum luminosity can similarly suffer the serious contaminations from jet and Blamer continuum, therefore the luminosity of ultraviolet emission line again may be a better indicator of ionizing luminosity than the ultraviolet continuum luminosity.

Finally, one should be cautious to the uncertainties in estimating the black hole mass of AGNs using the $R - L_{H\beta}$ relation. Firstly, the variations of $H\beta$ emission line flux and its FWHM are common in AGNs. Estimating the black hole mass with the values of these two parameters in a single spectrum may lead to large errors. Secondly, the different inclination of the BLR may also significantly affect the results (McLure & Dunlop 2001; Wu & Han 2001). If the BLR has a flatten geometry and the inclination of BLR is rather small, our derived values of black hole mass may significantly underestimated. However, the ratio of black hole masses estimated with two empirical relations does not depend on the inclination. Better understandings of BLR geometry and dynamics are absolutely needed to diminish the uncertainties in deriving the black hole mass of AGNs (Krolik 2001).

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References

Boroson, T.A., Green, R.F. 1992, ApJs, 80, 109
Brotherton, M.S. 1996, ApJs, 102, 1
Burstein, D., Heiles, C. 1982, AJ, 87, 1165
Chiaberge, M., Capetti, A., Celotti, A. 2002, New Astronomy Review, 46, 335
Cheung, C.C., Wardle, J.F.C., Chen, T., Hariton, S.P. 2003, New Astronomy Review, 47, 423
Collier, S.J., Horne, K., Kaspi, S., Netzer, H., et al. 1998, ApJ, 500, 162
Dietrich, M., Peterson, B. M., Albrecht, P., Altmann, M., et al. 1998, ApJs, 115, 185
Drinkwater, M.J., Webster, R.L., Francis, P.J., Condon, J.J., Ellison, S.L., Jauncey, D.L., Lovell, J., Peterson, B.A., Savage, A. 1997, MNRAS, 284, 85
Francis, P.J., Whiting, M.T., Webster, R.L. 2000, PASA, 17, 56
Gu, M., Cao, X., Jiang, D.R. 2001, MNRAS, 327, 1111
Ho, L.C. 1999, in Observational Evidence for Black Holes in the Universe, ed. S.K. Chakrabarti (Dordrecht: Kluwer), 157
Ho, L.C. & Peng, C.Y. 2001, ApJ, 555, 650
Isobe, T., Feigelson, E.D., Akritas, M.G., Babu, G.J. 1990, ApJ, 364, 104
Jester, S. 2003, New Astronomy Review, 47, 427
Kaspi, S., Maoz, D., Netzer, H., Peterson, B.M., et al. 1996, ApJ, 470, 336
Kaspi, S., Smith, P.S., Netzer, H., Maoz, D., Jannuzi, B.T., & Giveon, U. 2000, ApJ, 533, 631
Lacy, M., Laurent-Muehleisen, S. A., Ridgway, S.E., Becker, R.H., White, R.L. 2001, ApJ, 511, L17
Laor, A. ApJ, 543, L111
Krolik, J.H. 2001, ApJ, 551, 72
Lyden-Bell, D. 1969, Nature, 223,690
McLure, R.J, Dunlop, J.S. 2001, MNRAS, 327, 199
McLure, R.J., Jarvis, M.J. 2002, MNRAS, 337, 109
Oshlack, A. Y. K. N., Webster, R. L., Whiting, M. T. 2002, ApJ, 576, 81
Parma, P. de Ruiter, H.R., Capetti, A., Fanti, R., Morganti, R., Bondi, M., Laing, R.A., Canvin, J.R. 2003, A&A, 397, 127
Peterson, B.M., Berlind, P., Bertram, R., Bischoff, K. 2002, ApJ, 581, 197
Peterson, B.M., McHardy, I.M., Wilkes, B.J., Berlind, P. et al. 2000, ApJ, 542, 161
Peterson, B.M., Wanders, I., Bertram, R., Hunley, J.F., Pogge, R.W., Wagner, R.M. 1998, ApJ, 501, 82
Rees, M.J. 1984, ARA&A, 22 471
Santos-Lleo, M., Chatzichristou, E., Mendes de Oliveira, C., Winge, C., et al. 1997, ApJs, 112, 271
Santos-Lleo, M., Clavel, J., Schulz, B., Altieri, B., et al. 2001, A& A, 369, 57
Scarpa, R., Urry, C. M. 2002, New Astronomy Review, 46, 405
Scarpa, R., Urry, C. M., Falomo, R., Treves, A. 1999, ApJ, 526,643
Stirpe, G.M., Winge, C., Altieri, B., Alloin, D., et al. 1994, AJ, 425, 609
Vestergaard, M. 2002, ApJ, 571, 733
Wandel, A. 2002, ApJ, 565, 762
Wandel, A., Peterson, B.M., & Malkan, M.A. 1999, ApJ, 526, 579
Whiting, M.T., Webster, R.L., Francis, P.J. 2001, MNRAS, 323, 718
Winge, C., Peterson, B.M., Horne, K., Pogge, R.W., Pastoriza, M.G., Storchi-Bergmann, T. 1995, ApJ, 445, 680
Wu, X.-B., Han, J.L. 2001, ApJ, 561, L59
Table 1. The BLR size and luminosity data of 34 AGNs in the reverberation mapping studies

| Name      | z   | $A_B$ | $R_{BLR}$ (light-days) | $L_{\text{H}\beta}^{5100\AA}$ ($10^{42}$ erg/s) | $L_{\text{H}\alpha}$ ($10^{42}$ erg/s) | Ref |
|-----------|-----|-------|------------------------|-----------------------------------------------|--------------------------------------|-----|
| 3C 120    | 0.333 | 0.570 | 42.0 ± 0.142           | 73.00 ± 13.00                                | 1.222 ± 0.120                       | 1   |
| 3C 390.3  | 0.056 | 0.170 | 22.9 ± 0.130           | 64.00 ± 11.00                                | 1.433 ± 0.171                       | 3   |
| Akn 120   | 0.033 | 0.400 | 37.4 ± 0.333           | 139.00 ± 26.00                               | 2.496 ± 0.463                       | 1   |
| F 9       | 0.046 | 0.000 | 16.3 ± 0.76            | 137.00 ± 15.00                               | 2.056 ± 0.174                       | 4   |
| IC 4329A  | 0.016 | 0.000 | 1.4 ± 0.29             | 16.40 ± 2.10                                 | 0.183 ± 0.014                       | 5   |
| Mrk 110   | 0.035 | 0.000 | 18.8 ± 0.63            | 38.00 ± 13.00                                | 0.811 ± 0.203                       | 1   |
| Mrk 279   | 0.030 | 0.000 | 16.2 ± 0.51            | 66.00 ± 6.30                                 | 1.023 ± 0.071                       | 12  |
| Mrk 335   | 0.026 | 0.100 | 16.4 ± 0.53            | 62.20 ± 5.70                                 | 1.160 ± 0.073                       | 1   |
| Mrk 509   | 0.034 | 0.180 | 76.7 ± 6.00            | 147.00 ± 15.00                               | 3.070 ± 0.332                       | 1   |
| Mrk 509   | 0.026 | 0.050 | 20.0 ± 0.49            | 51.00 ± 9.60                                 | 0.498 ± 0.143                       | 1   |
| Mrk 79    | 0.022 | 0.230 | 17.7 ± 4.8             | 42.30 ± 5.60                                 | 0.619 ± 0.041                       | 1   |
| Mrk 817   | 0.031 | 0.000 | 15.0 ± 3.4             | 52.60 ± 7.70                                 | 0.740 ± 0.123                       | 1   |
| NGC 3227  | 0.004 | 0.020 | 10.9 ± 5.6             | 2.02 ± 0.11                                  | 0.017 ± 0.002                       | 6   |
| NGC 3783  | 0.010 | 0.470 | 4.5 ± 3.4              | 17.70 ± 1.50                                 | 0.292 ± 0.021                       | 7   |
| NGC 4051  | 0.002 | 0.000 | 6.5 ± 6.6              | 0.525 ± 0.03                                 | 0.0048 ± 0.0005                     | 8   |
| NGC 4151  | 0.003 | 0.000 | 3.0 ± 1.8              | 7.20 ± 0.42                                  | 0.152 ± 0.010                       | 9   |
| NGC 5548  | 0.017 | 0.000 | 21.2 ± 2.4             | 27.00 ± 5.30                                 | 0.421 ± 0.092                       | 10  |
| NGC 7469  | 0.016 | 0.120 | 4.9 ± 0.6              | 55.30 ± 1.60                                 | 0.423 ± 0.019                       | 11  |
| PG 0026   | 0.142 | 0.130 | 113.0 ± 18.0           | 700.00 ± 100.00                              | 5.693 ± 0.493                       | 2   |
| PG 0052   | 0.155 | 0.120 | 134.0 ± 31.0           | 650.00 ± 110.00                              | 9.505 ± 1.119                       | 2   |
| PG 0804   | 0.100 | 0.110 | 156.0 ± 15.0           | 660.00 ± 120.00                              | 13.95 ± 0.908                       | 2   |
| PG 0844   | 0.064 | 0.080 | 24.2 ± 9.1             | 172.00 ± 17.00                               | 2.585 ± 0.257                       | 2   |
| PG 0953   | 0.239 | 0.000 | 151.0 ± 22.0           | 1190.00 ± 160.00                             | 19.39 ± 1.129                       | 2   |
| PG 1211   | 0.085 | 0.130 | 101.0 ± 23.0           | 493.00 ± 80.00                               | 8.588 ± 1.056                       | 2   |
| PG 1226   | 0.158 | 0.000 | 387.0 ± 50.0           | 6440.00 ± 770.00                             | 88.37 ± 7.192                       | 2   |
| PG 1229   | 0.064 | 0.000 | 50.0 ± 29.0            | 94.00 ± 10.0                                 | 1.601 ± 0.202                       | 2   |
| PG 1307   | 0.155 | 0.020 | 124.0 ± 46.0           | 527.00 ± 52.00                               | 9.603 ± 1.301                       | 2   |
| PG 1411   | 0.089 | 0.000 | 102.0 ± 38.0           | 325.00 ± 28.00                               | 5.268 ± 0.285                       | 2   |
| PG 1426   | 0.086 | 0.120 | 95.0 ± 31.0            | 409.00 ± 63.00                               | 4.952 ± 0.465                       | 2   |
| PG 1613   | 0.129 | 0.040 | 39.0 ± 20.0            | 696.00 ± 87.00                               | 7.014 ± 0.451                       | 2   |
| PG 1617   | 0.114 | 0.150 | 85.0 ± 19.0            | 237.00 ± 41.00                               | 4.060 ± 0.493                       | 2   |
| PG 1700   | 0.292 | 0.020 | 88.0 ± 126.0           | 2710.00 ± 190.00                             | 35.29 ± 1.851                       | 2   |
| PG 1704   | 0.371 | 0.000 | 319.0 ± 184.0          | 3560.00 ± 520.00                             | 9.752 ± 1.257                       | 2   |
| PG 2130   | 0.061 | 0.170 | 200.0 ± 18.0           | 216.00 ± 20.00                               | 4.241 ± 0.381                       | 2   |

Notes: The Galactic extinction values are adopted from NED. Data of $R_{BLR}$ and $L_{\text{H}\beta}^{5100\AA}$ are taken from Kaspi et al. (2000). The $H\beta$ luminosity is calculated from the flux given in the literature (see the column "ref"). References: (1) Peterson et al. 1998; (2) Kaspi et al. 2000; (3) Dietrich et al. 1998; (4) Santos-Lleo et al. 1997; (5) Winge et al. 1996; (6) Winge et al. 1995; (7) Strirpe et al. 1994; (8) Peterson et al. 2000; (9) Kaspi et al. 1996; (10) Peterson et al. 2002; (11) Collier et al. 1996; (12) Santos-Lleo et al. 2001.