Optimal design for the Josephson mixer

J.-D. Pillet,1,2 E. Flurin,1 F. Mallet,1 and B. Huard1
1) Laboratoire Pierre Aigrain, Ecole Normale Supérieure-PSL Research University, CNRS, Université Pierre et Marie Curie-Sorbonne Universités, Université Paris Diderot-Sorbonne Paris Cité, 24 rue Lhomond, 75231 Paris Cedex 05, France
2) Collège de France, 11 place Marcelin Berthelot, 75005 Paris, France

(Dated: 30 March 2015)

We present an optimal design in terms of gain, bandwidth and dynamical range for the Josephson mixer, the superconducting circuit performing three-wave mixing at microwave frequencies. In a compact all lumped-element based circuit with galvanically coupled ports, we demonstrate non degenerate amplification for microwave signals over a bandwidth up to 50 MHz for a power gain of 20 dB. The quantum efficiency of the mixer is shown to be about 70% and its dynamical range reaches 5 quanta per inverse dynamical bandwidth.

PACS numbers: 85.25.Cp, 84.30.Le, 84.40.Dc, 85.25.-j, 42.65.Hw, 42.50.Lc

Analog processing of microwave signals has recently entered the quantum regime owing to the developments of superconducting circuits. Quantum limited amplifiers that are based on the non-linearity provided by Josephson junctions have been developed in various designs.1–19 Non-degenerate three-wave mixing, a key operation, is realized by the Josephson ring modulator (JRM), which is a ring of four identical Josephson junctions20–22. This element is at the core of several tools able to generate and manipulate quantum microwave modes such as phase preserving amplifiers22–24, non-local entanglement generators25, frequency converters26, quantum memories27, or circulators28–29. In all previous implementations of the Josephson mixer, the JRM was embedded at the crossing of two distributed or lumped resonators, which puts a constraint on bandwidth and dynamical range that can be detrimental to quantum operations. In this letter, we discuss the origin of this constraint and how to optimize the figures of merit of the Josephson mixer. These ideas are put in practice on an experiment in which a phase preserving amplifier is solely built out of a JRM that is shunted with lumped plate capacitors. Compared to previous implementations, we report an order of magnitude increase of its dynamical bandwidth, up to 50 MHz at a power gain of 20 dB while keeping the dynamical range as high as 5 photons per inverse bandwidth.

In a Josephson mixer, the JRM couples three independent fluxes $\varphi_a$, $\varphi_b$, and $\varphi_p$ (Fig. 1), through the lowest order coupling term $H_{mix} = -E_J \sin(\Phi/4)\varphi_a \varphi_b \varphi_p$, where $E_J$ is the Josephson energy of each junction, $\varphi_0 = h/2e$ the reduced flux quantum and $\Phi$ the flux threading the ring.20–22 Three wave mixing occurs by embedding the ring in resonant circuits (Fig. 1) so that each flux can be expressed as $\varphi_k \propto (k + \tilde{k})$ where $k$ is the canonical annihilation operator of a microwave mode of characteristic impedance $Z_0$ and resonance frequency $f_k$. Although the Josephson mixer can be used in various ways,20–22,24,25, we will focus here on the amplification regime in order to describe the figures of merit on a concrete case. The signals sent towards $a$ and $b$ modes are amplified in reflection in a phase preserving manner by driving the mode $p$ out of resonance at the frequency $f_a + f_p$. Three main specifications matter in analog processing of quantum microwave signals. First, the power gain $G$ of the amplifier needs to be large enough so that the quantum noise at the input of the amplifier dominates all other noise sources on the detection setup. Typically 20 dB is enough if a cryogenic HEMT is used as a second stage of amplification.30 Second, the time correlations of the quantum signals should be dominated by the system of interest and not by the Josephson mixer. This requires to have as large a dynamical frequency bandwidth $\Gamma$ as possible. Finally, the maximum input power $P_{in}^{max}$ that does not affect the gain by more than 1 dB needs to be large enough to avoid any limitation on the amplitude of the quantum signals.

Optimizing these three parameters for a practical amplifier has been at the center of recent experimental works in various geometries.12–14,16 Recently Josephson Parametric Amplifiers have reached up to 20 dB gain over a 100 MHz bandwidth in an all lumped-element based design14,16 while 5 dB gain over 2 GHz bandwidth has been reported in a TiN traveling wave parametric amplifier.13 The constraints on the parameters of the Josephson mixer are similar in origin to those of its degenerate cousin, the Josephson Parametric Amplifier31, but with some differences.21 First, there is an upper bound on the energy that is stored in the $p$ pump mode, originating from the small flux $\varphi_p$ assumption in the three-wave mixing term $H_{mix}$. Therefore, in order to allow pump powers to reach the onset of parametric oscillations, at which large gain $G$ develops, one has to ensure that

$$p_a Q_a Q_b Q_k > \Xi,$$

where $\Xi$ is a number depending on the exact geometry of the mixer. $\Xi = 8$ will be used in the following.32 In this expression, $Q_k$ is the quality factor of mode $k$, defined as $Q_k = f_k/\Gamma_k$ where $\Gamma_k$ is the resonance bandwidth. The participation ratio $p_k$ of the JRM Josephson junctions in

---

a) corresponding author: francois.mallet@lpa.ens.fr
Indeed, neither the input signal power $P_{in}$ nor the vacuum noise should be amplified beyond a fraction of the Josephson energy $E_J$. For large gain, this condition can be approximated as

$$p_k G (P_{in}/(2\pi\Gamma_k) + h f) \Xi' < E_J,$$

where $\Xi'$ is a number of order 1 and $E_J$ is the Josephson energy $E_J = \phi_0^2/L_J$. The two above constraints (1) and (2) indicate that increasing both $P_{in}^{max}$ and $\Gamma$ for a given gain $G$ requires to increase the participation ratios $p_k$ and the Josephson junction energy $E_J$. However, these two figures are related since $p_k$ is a decreasing function of $E_J$. To minimize the detrimental influence of an increasing $E_J$ on $p_k$, it seems that the optimal design is when all the inductive parts of the resonators originate from the Josephson junctions themselves so that $L_{ex} = 0$ (Fig. 1c).

It is enlightening to represent graphically these constraints in the parameter phase spaces. In figure 1, shaded areas delimitate, for two different values of $L_{ex}$, the allowed values of the quality factor $Q$ and Josephson inductance $L_J$ for a typical quantum limited amplifier operating at a frequency $f = 7$ GHz with a 20 dB power gain, a saturating input power $P_{in}^{max} = -110$ dBm. Note that for the sake of clarity the two a and b modes have been set to identical parameters. As can be seen in the figure, lower $Q$ (larger bandwidth) can be obtained only by lowering $L_{ex}$. Conversely, Fig. 1 shows the maximal allowed extra inductance $L_{ex}^{max}$ as a function of saturating power $P_{in}^{max}$ for several desired quality factors $Q$. From these curves, one can deduce which maximal extra inductance $L_{ex}^{max}$ can be used for a given bandwidth. If $L_{ex}$ comes from the geometrical inductance of some wires, their length is of the order of $L_{ex}/\mu_0$, which is represented on the right axis of Fig. 1. From these considerations, one also determines the maximal spatial extension of a Josephson mixer to ensure a given bandwidth.

Our implementation of the optimal design (Fig. 1c) is presented in Fig. 2. The a and b mode resonators are composed of the JRM that is shunted by a cross of plate capacitors. The circuit is fabricated on a 500 µm thick Si chip covered with a 300 nm layer of SiO2 on top. In a first step, a Ti(5nm)/Al(30nm) common counter electrode for all the plate capacitors is fabricated using standard e-beam lithography (dark yellow in Fig. 2b). It spreads all over the surface underneath the rest of the circuit, except for a hole in the center and a thin stripe (brown in Fig. 2b) allowing to flux bias the circuit without the constraints imposed by the Meissner effect. The whole chip is then covered with 200 nm of amorphous dielectric silicon nitride by plasma-enhanced chemical vapor deposition. Finally, the second metallic plate of the capacitors (area 285 µm x 86 µm for the a resonator and 140 µm x 86 µm for the b resonator) and the Josephson junctions (area 4.2 µm x 1 µm) are fabricated by double angle deposition of 100 nm and 120 nm of aluminum with an intermediate oxydation step (Fig. 2c).

The circuit is then placed in a copper box enclosed in a Cryoperm magnetic shielding box anchored at base temperature of a dilution refrigerator ($T_{ref} \simeq 50$ mK). Two 180° hybrid couplers address separately the differential a and b modes through their $\Delta$ ports as well as the pump

---

**FIG. 1.** (a) Flux quadratures of the eigenmodes of the Josephson Ring Modulator. (b) Original mixer design where the JRM is placed at the crossing of two resonators of different frequencies. Two lines represent the spatial profiles of the voltage in the $\lambda/2$ resonators. (c) Ideal design where every inductive parts originate from the Josephson junctions. (d) Equivalent circuit of the differential modes $a$ and $b$ when the pump is turned off. A parasitic inductance $L_{ex}$ in series with the JRM is considered. (e) The two shaded regions, corresponding to $L_{ex} = 1$ nH and $L_{ex} = 50$ pH, indicate the combinations of quality factor $Q$ and Josephson junction inductance $L_J$ that verify the inequalities (1) and (2) for a power gain $G = 20$ dB, a saturating input power $P_{in}^{max} = -110$ dBm and operating frequency $f = 7$ GHz. For a given extra inductance $L_{ex}$ and saturating power $P_{in}^{max}$, there is a minimum quality factor which limits the bandwidth of the Josephson mixer and a maximum inductance for the Josephson junction. (f) Maximal allowed value of the resonator extra inductance $L_{ex}^{max}$ within the constraints (1) and (2) as a function of saturating power $P_{in}^{max}$ plotted for various quality factors $Q$. 

---

the $k$ mode quantifies the ratio of the total energy in this mode that is actually stored across the JRM junctions. For a serial coupling, it is given by $p_k = L_J/(L_J + L_{ex}^{k})$ where $L_{ex}^{k}$ is the effective extra inductance of the resonator defining the $k$ mode and $L_J = \phi_0^2/E_J$ is the inductance of a single junction of the JRM (Fig. 1d). Second, there is an upper bound on the power spectral density of the amplified signals coming from the small flux $\phi_{a,b}$ assumption in the three-wave mixing term $H_{mix}$. Indeed, neither the input signal power $P_{in}$, nor the vacuum noise should be amplified beyond a fraction of the Josephson energy $E_J$. For large gain, this condition can
mode $c$ through one of the $\Sigma$ ports. The resonators have characteristic impedances smaller than 10 $\Omega$ and are galvanically connected to the 50 $\Omega$ ports of the device so as to maximize bandwidth, only limited by impedance mismatch. Owing to the large coupling between the differential modes and the input/output ports, the gain is sensitive to the frequency dependence of the impedance. In order to probe the characteristics of the Josephson mixer alone without carefully engineering the impedance of the environment, we connect a 6 dB attenuator at the $\Delta$ ports of the hybrid couplers. A coil allows to control the flux threading the JRM loop to tune the mixing term in $H_{\text{mix}}$ via its current $I_{\text{coll}}$.

The effect of the flux bias can also be seen (Fig. 3a) on the resonance frequencies $f_a$ and $f_b$ which depend in an hysteretic manner of the flux with a period $4\phi_0$. This hysteretic behavior could be removed by inserting additional inductances in the JRM in order to extend the static bandwidth of the amplifier. However, this comes at the expense of lowering participation ratios, which we aim at maximizing, and becomes less useful with a large dynamical bandwidth. In this device, we observe a frequency dependence on $I_{\text{coll}}$, which is not perfectly periodic. This observed non-linear dependence of $\Phi_{\text{ext}}$ on $I_{\text{coll}}$ may originate form vortex dynamics in the large superconducting capacitor plate that is buried under the silicon nitride. For each resonance frequency, it was possible to measure the quality factor (inset of Fig. 3a). This dependence can lead to a quantitative model describing the Josephson mixer. In this detailed model, based on Fig. 1d, a stray inductance $L_{\text{stray}}$ is considered in series with the capacitor $C_{\text{res}}$. Using first full 3D microwave simulations of the whole device, it was possible to estimate the geometrical electrical parameters of $C_{\text{res}} = 3$ pF, $L_a = 130$ pH and $C_{\text{res}} = 6$ pF, $L_{\text{stray}}$ + $L_{\text{stray}}^b$ = 85 pH. Then, by fitting $L_I$ = 90 pH, one gets $f_p^{(\text{fit})}$ = 6.95 GHz and $f_b^{(\text{fit})}$ = 5.74 GHz, which are close to the measured resonance frequencies at $\Phi_{\text{ext}}$ = 0 (Fig. 3a). From there, one can estimate the participation ratios to be $p_a$ = 25% and $p_b$ = 35%. Note that similar values for the participation ratios can be obtained by fitting directly the flux dependence of the resonance frequency (see supplementary material of Ref. 23). Finally, one can fit the stray inductances to best recover the curve $Q(f)$ and find $L_{\text{stray}}^a$ = 75 pH, $L_{\text{stray}}^b$ = 51 pH.

The Josephson mixer can be used as an amplifier by setting the flux $\phi_1$ slightly lower than $2\phi_0 = h/e$ and driving the $c$ pump mode at the frequency $f_p$ = 12.26 GHz, which is close to $f_a + f_b^{(20)}$. The gain was measured in reflection on both amplifier ports as a function of frequency (Fig. 3b) for various values of the pump power $P_p$ at the fixed flux $\phi_1$. As the pump power rises towards...
the parametric oscillation threshold, the gain increases on both ports up to 30 dB. Conversely, the operating bandwidth decreases. This curve demonstrates a bandwidth of 50 MHz at 20 dB, which is an order of magnitude higher than using previous implementations of the Josephson mixer.

The amplifier added noise is evaluated by amplification of zero point fluctuations in a and b modes. A spectrum analyzer measures the spectral power density coming from a\textsubscript{out} and b\textsubscript{out} as a function of P\textsubscript{p}. No signal is sent into a\textsubscript{in} and b\textsubscript{in}. The difference between spectral densities while the amplifier is ON and OFF is given by

\[ S\text{ON} - S\text{OFF} = G_{LNA} \times hG(S_{add} + 1), \]

where \( G \) is the gain of the amplifier and \( G_{LNA} \) is the total gain of the output lines. Here the modes are assumed to be in the vacuum state and \( G \gg 1 \). In this case the added noise \( S_{add} \) can be related to the quantum efficiency \( \eta \) of the mixer by \( S_{add} = (1 - \eta)/2\eta \). Determination of \( \eta \) requires thus separate measurements of the amplifier gain \( G \), as those of Fig. 3 and fine calibrations of the attenuations and gains of the input and output lines connecting the mixer to the detectors. We obtain this calibration by measuring the shift in frequency as a function of power sent into a\textsubscript{in} and b\textsubscript{in}. It provides, by comparison with numerical calculations of the circuit shown in Fig. 1(d), a precise calibration of the attenuation of the input line between a\textsubscript{in} and the mixer. The gain \( G_{LNA} \) between the Josephson mixer and a\textsubscript{out} is then deduced from the total transmission between a\textsubscript{in} and a\textsubscript{out}, the pump being turned off. Note that we also observe a clear frequency shift in the gain measurements of Fig. 4(b) while changing pump power due to higher order cross-Kerr terms that are proportional to \( P_p a^\dagger a \) and \( P_p b^\dagger b \). Figure 4(a) presents the measured \( \eta \) as a function \( G \). It indicates an efficiency of 0.7, up to 33 dB of gain above which the amplifier enters the parametric oscillation regime where \( \eta \) is near 0.2.

The last important specification of an amplifier is its dynamical range. It is characterized by the 1 dB compression point \( P_{in}^{\text{max}} \) of the amplifier. In Josephson parametric devices, such as the Josephson mixer, this saturation can be caused either by depletion of the pump (i.e., the gain is so large that the pump cannot refill quickly enough to feed the amplifier), or by reaching a large enough number of photons such that higher order non-linearities cannot be neglected. Using the calibration of the input power \( P_{in} \) on port b above, we used a vector network analyzer to measure the output power \( P_{out} \) as a function of input power \( P_{in} \) (Fig. 4b) at 6.76 GHz (center frequency when \( G = 20 \) dB) for various pump powers following Ref. \( [31] \). At low input powers \( P_{in} < -120 \) dBm, the gain goes from 0 to 25 dB for increasing pump power \( P_p \) without depending on \( P_{in} \). For the pump power corresponding to \( G = 20 \) dB at low input power, the amplifier behaves linearly for low power until it reaches the 1 dB compression point at -112 dBm at the JRM input. At 6.76 GHz and for a bandwidth of 50 MHz, this power corresponds to 4.5 photons per bandwidth. Above this threshold the gain drops and finally saturates. This dynamical range is large enough not only for performing qubit readout [23] but also for amplifying vacuum squeezed states [25].

In conclusion, we have discussed an optimal and compact design for the Josephson mixer and applied these principles to demonstrate phase preserving quantum limited amplification. The resulting device operates with gains reaching 30 dB within 0.4 photons of the quantum limit of noise and a saturation power of -112 dBm, which is promising for analog information processing of quantum signals, directional amplification and on-chip circulators [25]. These specifications do not hinder the dynamical bandwidth of the mixer, which reaches 50 MHz at \( G = 20 \) dB. Such device is suited for fast operation on superconducting qubit, which are necessary to the improvement of the efficiency of quantum feedback [32,37], multiplexing several qubit [35] or more generally quantum error correction schemes.
ACKNOWLEDGMENTS

We thank Michel Devoret for enlightening discussions. Nanofabrication has been made within the consortium Salle Blanche Paris Centre. This work was supported by the program ANR-12-JCJC-TIQS of Agence Nationale pour la Recherche. JDP acknowledges financial support from Michel Devoret.

1. M. A. Castellanos-Beltran and K. Lehnert, Appl. Phys. Lett., 91, 083509 (2007).
2. E. Tholén, A. Ergül, E. Doherty, F. Weber, F. Grégis, and D. Haviland, Appl. Phys. Lett. 90, 253509 (2007).
3. T. Yamamoto, K. Inomata, M. Watanabe, K. Matsuba, T. Miyazaki, W. D. Oliver, Y. Nakamura, and J. S. Tsai, Appl. Phys. Lett. 93, 042510 (2008).
4. D. Kinion, J. Clarke, Appl. Phys. Lett. 92, 172503 (2008).
5. M. A. Castellanos-Beltran, K. D. Irwin, G. C. Hilton, R. L. Vale, and K. W. Lehnert, Nat. Phys. 4, 929 (2008).
6. A. Kamal, A. Marblestone, and M.H. Devoret, Phys. Rev. B 79, 184301 (2009).
7. L. Spitz, K. Irwin, M. Lee, and J. Aumentado, Appl. Phys. Lett. 97, 142502 (2010).
8. C. Eichler, D. Bozyigit, C. Lang, M. Baur, L. Steffen, J. M. Fink, S. Filipp, and A. Wallraff, Phys. Rev. Lett. 107, 113601 (2011).
9. R. Vijay, D.H. Slichter, and I. Siddiqi, Phys. Rev. Lett. 106, 110502 (2011).
10. M. Hatridge, R. Vijay, D.H. Slichter, J. Clarke, and I. Siddiqi, Phys. Rev. B 83, 143501 (2011).
11. I. Gao, L. R. Vale, J. A. B. Mates, D. R. Schmidt, G. C. Hilton, K. D. Irwin, F. Mallet, M. A. Castellanos-Beltran, K. W. Lehnert, J. Zmuidzinas, and H. G. Leduc, Appl. Phys. Lett. 98, 232508 (2011).
12. D. Hover, Y.-F. Chen, G. J. Ribeil, S. Zhu, S. Sendelbach, and R. McDermott, Appl. Phys. Lett. 100, 063503 (2012).
13. B. H. Zom, P. K. Day, H. G. LeDuc, and J. Zmuidzinas, Nat. Phys. 8, 623 (2012).
14. J. Y. Mutus, T. C. White, E. Jeffrey, D. Sank, R. Barends, J. Bochmann, Yu Chen, Z. Chen, B. Chiaro, A. Dunsworth, J. Kelly, A. Megrant, C. Neill, P. J. J. O’Malley, P. Roushan, A. Vainsencher, J. Wenner, A. N. Cleland, and J. M. Martinis, Appl. Phys. Lett. 103, 122602 (2013).
15. L. Zhong, E. P. Menzel, R. Di Candia, F. Eder, M. Ihig, A. Baust, M. Haeberlein, E. Hoffmann, K. Inomata, T. Yamamoto, Y. Nakamura, E. Solano, F. Deppe, A. Marx, and R. Gross, New J. Phys. 15, 125013 (2013).
16. Y. Mutus, T. C. White, R. Barends, Y. Chen, Z. Chen, B. Chiaro, A. Dunsworth, E. Jeffrey, J. Kelly, A. Megrant, C. Neill, P. J. J. O’Malley, P. Roushan, D. Sank, A. Vainsencher, J. Wenner, K. M. Sadowski, A. N. C. Cleland, and J. M. Martinis, Appl. Phys. Lett. 104, 263513 (2014).
17. C. Eichler, Y. Salathe, J. Mylnik, S. Schmidt, and A. Wallraff, Phys. Rev. Lett. 113, 110502 (2014).
18. A. Narla, K.M. Sliwa, M. Hatridge, S. Shankar, L. Fruzio, R. J. Schoelkopf, and M.H. Devoret, Appl. Phys. Lett. 104, 232605 (2014).
19. X. Zhou, V. Schmitt, P. Bertet, D. Vion, W. Wustmann, V. Shumeiko, and D. Esteve, Phys. Rev. B 89, 214517 (2014).
20. N. Bergeal, R. Vijay, V. E. Manucharyan, I. Siddiqi, R. J. Schoelkopf, S. M. Girvin, and M. H. Devoret, Nat. Phys. 6, 296 (2010).
21. B. Abdo, A. Kamal, and M. Devoret, Phys. Rev. B 87, 014508 (2013).
22. N. Bergeal, F. Schackert, M. Metcalfe, R. Vijay, V. E. Manucharyan, L. Fruzio, D. E. Prober, R. J. Schoelkopf, S. M. Girvin, and M. H. Devoret, Nature 465, 64 (2010).
23. B. Abdo, F. Schackert, M. Hatridge, C. Rigetti, and M. Devoret, Appl. Phys. Lett. 99, 162506 (2011).
24. N. Roch, E. Flurin, F. Nguyen, P. Morfin, P. Campagne-Ibarcq, M. H. Devoret, and B. Huard, Phys. Rev. Lett. 108, 147701 (2012).
25. E. Flurin, N. Roch, F. Mallet, M. H. Devoret, and B. Huard, Phys. Rev. Lett. 109, 183901 (2012).
26. B. Abdo, K. Sliwa, F. Schackert, N. Bergeal, M. Hatridge, L. Fruzio, A. D. Stone, and M. Devoret, Phys. Rev. Lett. 110, 173902 (2013).
27. E. Flurin, N. Roch, J.D. Fillet, F. Mallet, and B. Huard, Phys. Rev. Lett. 114, 090503 (2015).
28. B. Abdo, K. Sliwa, L. Fruzio, and M. Devoret, Phys. Rev. X 3, 031001 (2013).
29. K. M. Sliwa, M. Hatridge, A. Narla, S. Shankar, L. Fruzio, R. J. Schoelkopf, and M. H. Devoret, e-print [arXiv:1503.00269].
30. S. Wernrehb, M.W. Pospieszalski, and R. Norrod, in IEEE MTT-S International Microwave Symposium Digest, New York, USA, 25-27 May 1988, edited by IEEE, 945.
31. C. Eichler, and A. Wallraff, EPJ Quantum Technology 1, 2 (2014).
32. E. Flurin, Ph. D. thesis, Ecole Normale Supérieure, Paris, 2014.
33. I. Hoi, A. F. Kockum, T. Palomaki, T. M. Stace, B. Fan, L. Torber, S. R. Sathyamoorthy, G. Johansson, P. Delsing, and C. M. Wilson, Phys. Rev. Lett. 111, 053601 (2013).
34. C. M. Caves, Phys. Rev. D 26, 1817 (1982).
35. Y. Chen, D. Sank, P. O’Malley, T. White, R. Barends, B. Chiaro, J. Kelly, E. Lucero, M. Mariantoni, A. Megrant, C. Neill, A. Vainsencher, J. Wenner, Y. Yin, A. N. Cleland, and J. M. Martinis, Appl. Phys. Lett. 101, 182601 (2012).
36. R. Vijay, C. Macklin, D. H. Slichter, S. J. Weber, K. W. Murch, R. Naik, A. N. Korotkov, and I. Siddiqi, Nature 490, 77 (2012).
37. P. Campagne-Ibarcq, E. Flurin, N. Roch, D. Darso, P. Morfin, M. Mirrahimi, M. H. Devoret, F. Mallet, and B. Huard, Phys. Rev. X 3, 021008 (2013).