MURA Dataset: Towards Radiologist-Level Abnormality Detection in Musculoskeletal Radiographs

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Abstract

We introduce MURA, a large dataset of musculoskeletal radiographs containing 40,895 images from 14,982 studies, where each study is manually labeled by radiologists as either normal or abnormal. On this dataset, we train a 169-layer densely connected convolutional network to detect and localize abnormalities. To evaluate our model robustly and to get an estimate of radiologist performance, we collect additional labels from board-certified Stanford radiologists on the test set, consisting of 209 musculoskeletal studies. We compared our model and radiologists on the Cohen’s kappa statistic, which expresses the agreement of our model and of each radiologist with the gold standard, defined as the majority vote of a disjoint group of radiologists. We find that our model achieves performance comparable to that of radiologists. Model performance is higher than the best radiologist performance in detecting abnormalities on finger studies and equivalent on wrist studies. However, model performance is lower than best radiologist performance in detecting abnormalities on elbow, forearm, hand, humerus, and shoulder studies, indicating that the task is a good challenge for future research. To encourage advances, we have made our dataset freely available at https://stanfordmlgroup.github.io/projects/mura.

1. Introduction

Large, high-quality datasets have played a critical role in driving progress of fields with deep learning methods (Deng et al., 2009). To this end, we introduce MURA, a large dataset of radiographs, containing 14,982 musculoskeletal studies of the upper extremity. Each study contains one or more views (images) and is manually labeled by radiologists as either normal or abnormal.

The abnormality detection task, or in other words determining whether a radiographic study is normal or

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abnormal, is a critical radiological task: a study interpreted as normal rules out disease and can eliminate the need for patients to undergo further diagnostic procedures or interventions. Musculoskeletal conditions affect more than 1.7 billion people worldwide (BMU, 2017), and are the most common cause of severe, long-term pain and disability (Woolf & Pfleger, 2003), with 30 million emergency department visits annually and increasing. Our dataset, MURA, contains 9,067 normal and 5,915 abnormal musculoskeletal radiographic studies of the upper extremity including the shoulder, humerus, elbow, forearm, wrist, hand, and finger. MURA is one of the largest public radiographic image datasets.

On MURA, we developed a competitive abnormality detection model. The model takes as input one or more views for a study. On each view, our 169-layer convolutional neural network predicts the probability of abnormality; the per-view probabilities are then averaged to output the probability of abnormality for the study.

To evaluate models robustly and to get an estimate of radiologist performance, we collected six additional labels from board-certified radiologists on a holdout test set of 209 studies. We compare the performance of our model and radiologists, and find that our model achieves performance comparable to that of radiologists. Model performance is higher than the best radiologist’s performance in detecting abnormalities on finger studies, and equivalent in wrist studies. However, model performance is lower than best radiologist’s performance in detecting abnormalities on elbow, forearm, hand, humerus, and shoulder studies. We have made our dataset freely available to encourage advances in medical imaging models.

2. MURA

The MURA abnormality detection task is a binary classification task, where the input is an upper extremity radiograph study — with each study containing one or more views (images) — and the expected output is a binary label $y \in \{0, 1\}$ indicating whether the study is normal or abnormal, respectively.

2.1. Data Collection

Our institutional review board approved study collected de-identified, HIPAA-compliant images from the Picture Archive and Communication System (PACS) of Stanford Hospital. We assembled a dataset of musculoskeletal radiographs consisting of 14,982 studies from 12,251 patients, with a total of 40,895 multi-view radiographic images. Each belongs to one of seven standard upper extremity radiographic study types: elbow, finger, forearm, hand, humerus, shoulder, and wrist. Table 1 summarizes the distribution of normal and abnormal studies.

Each study was manually labeled as normal or abnormal by board-certified radiologists from the Stanford Hospital at the time of clinical radiographic interpretation in the diagnostic radiology environment between 2001 and 2012. The labeling was performed during interpretation on DICOM images presented on at least 3 megapixel PACS medical grade display with max
To evaluate models and get a robust estimate of radiologist performance, we collected additional labels from board-certified Stanford radiologists on the test set, consisting of 209 musculoskeletal studies. The radiologists individually retrospectively reviewed and labeled each study in the test set as a DICOM file as normal or abnormal in the clinical reading room environment using the PACS system. The radiologists have 8.83 years of experience on average ranging from 2 to 25 years. The radiologists did not have access to any clinical information. Labels were entered into a standardized data entry program.

2.3. Abnormality Analysis
To investigate the types of abnormalities present in the dataset, we reviewed the radiologist reports to manually label 100 abnormal studies with the abnormality finding: 53 studies were labeled with fractures, 48 with hardware, 35 with degenerative joint diseases, and 29 with other miscellaneous abnormalities, including lesions and subluxations.

2.2. Test Set Collection
To evaluate models and get a robust estimate of radiologist performance, we collected additional labels from board-certified Stanford radiologists on the test set, consisting of 209 musculoskeletal studies. The radiologists individually retrospectively reviewed and labeled each study in the test set as a DICOM file as normal or abnormal in the clinical reading room environment using the PACS system. The radiologists have 8.83 years of experience on average ranging from 2 to 25 years. The radiologists did not have access to any clinical information. Labels were entered into a standardized data entry program.

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| Radiologist 1 | Radiologist 2 | Radiologist 3 | Model |
|---------------|---------------|---------------|-------|
| Elbow         | 0.795 (0.770, 0.819) | 0.733 (0.703, 0.764) | 0.738 (0.709, 0.767) | 0.733 (0.703, 0.764) |
| Finger        | 0.304 (0.249, 0.358) | 0.403 (0.339, 0.467) | 0.410 (0.358, 0.463) | 0.525 (0.476, 0.573) |
| Forearm       | 0.796 (0.772, 0.821) | 0.802 (0.779, 0.825) | 0.798 (0.774, 0.822) | 0.670 (0.634, 0.705) |
| Hand          | 0.661 (0.623, 0.698) | 0.927 (0.917, 0.937) | 0.789 (0.762, 0.815) | 0.780 (0.752, 0.809) |
| Humerus       | 0.867 (0.850, 0.883) | 0.733 (0.703, 0.764) | 0.933 (0.925, 0.942) | 0.800 (0.776, 0.824) |
| Shoulder      | 0.864 (0.847, 0.881) | 0.791 (0.765, 0.816) | 0.864 (0.847, 0.881) | 0.795 (0.770, 0.819) |
| Wrist         | 0.791 (0.766, 0.817) | 0.931 (0.922, 0.940) | 0.931 (0.922, 0.940) | 0.931 (0.922, 0.940) |
| Overall       | 0.724 (0.719, 0.728) | 0.766 (0.762, 0.770) | 0.780 (0.777, 0.784) | 0.749 (0.744, 0.753) |

Table 2. We compare radiologists and our model on the Cohen’s kappa statistic, which expresses the agreement of each radiologist/model with the gold standard, defined as the majority vote of a disjoint group of radiologists. We highlight the best (green) and worst (red) performances on each of the study types and in aggregate. On finger studies, model performance is significantly higher than the best radiologist performance. On wrist studies, model performance is equivalent to the best radiologist performance. On hand, humerus, and shoulder studies, model performance is higher than the worst radiologist performance but lower than the best radiologist performance. On elbow and shoulder studies, model performance is comparable to the worst radiologist performance. On forearm studies, model performance is significantly worse than the worst radiologist performance.

3. Model
The model takes as input one or more views for a study of an upper extremity. On each view, our 169-layer convolutional neural network predicts the probability of abnormality. We compute the overall probability of abnormality for the study by taking the arithmetic mean of the abnormality probabilities output by the network for each image. The model makes the binary prediction of abnormal if the probability of abnormality for the study is greater than 0.5. Figure 2 illustrates the model’s prediction pipeline.

3.1. Network Architecture and Training
We used a 169-layer convolutional neural network to predict the probability of abnormality for each image in a study. The network uses a Dense Convolutional Network architecture – detailed in Huang et al. (2016) – which connects each layer to every other layer in a feed-forward fashion to make the optimization of deep networks tractable. We replaced the final fully connected layer with one that has a single output, after which we applied a sigmoid nonlinearity.

For each image $X$ of study type $T$ in the training set, we optimized the weighted binary cross entropy loss

$$L(X, y) = -w_{T,1} \cdot y \log p(Y = 1 | X) - w_{T,0} \cdot (1 - y) \log p(Y = 0 | X),$$

where $y$ is the label of the study, $p(Y = i | X)$ is the probability that the network assigns to the label $i$, $w_{T,1} = |N_T|/(|A_T| + |N_T|)$, and $w_{T,0} = |A_T|/(|A_T| + |N_T|)$.
| Dataset                  | Study Type                          | Label          | Images |
|-------------------------|-------------------------------------|----------------|--------|
| MURA                    | Musculoskeletal (Upper Extremity)    | Abnormality    | 41,299 |
| Pediatric Bone Age (AIMI)| Musculoskeletal (Hand)              | Bone Age       | 14,236 |
| 0.E.1 (OAI)             | Musculoskeletal (Knee)              | K&L Grade      | 8,892  |
| Digital Hand Atlas      | Musculoskeletal (Left Hand)         | Bone Age       | 1,390  |
| ChestX-ray14 (Wang et al., 2017) | Chest                  | Multiple Pathologies | 112,120 |
| OpenI (Denner-Fushman et al., 2015) | Chest                  | Multiple Pathologies | 7,470  |
| MC (Jaeger et al., 2014) | Chest                              | Abnormality    | 138    |
| Shenzhen (Jaeger et al., 2014) | Chest                              | Tuberculosis   | 662    |
| JSRT (Shiraishi et al., 2000) | Chest                              | Pulmonary Nodule | 247    |
| DDSM (Heath et al., 2000) | Mammogram                          | Breast Cancer  | 10,239 |

Table 3. Overview of publicly available medical radiographic image datasets.

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|N_T| where |A_T| and |N_T| are the number of abnormal images and normal images of study type \( T \) in the training set, respectively.

Before feeding images into the network, we normalized each image to have the same mean and standard deviation of images in the ImageNet training set. We then scaled the variable-sized images to 224 \( \times \) 224. We augmented the data during training by applying random lateral inversions and rotations.

The weights of the network were initialized with weights from a model pretrained on ImageNet (Deng et al., 2009). The network was trained end-to-end using Adam with default parameters \( \beta_1 = 0.9 \) and \( \beta_2 = 0.999 \) (Kingma & Ba, 2014). We trained the model using minibatches of size 8. We used an initial learning rate of 0.0001 that is decayed by a factor of 10 each time the validation loss plateaus after an epoch, and chose the model with the lowest validation loss.

4. Radiologist vs. Model Performance

We assessed the performance of both radiologists and our model on the test set. Recall that for each study in the test set, we collected additional normal/abnormal labels from 6 board-certified radiologists. We randomly chose 3 of these radiologists to create a gold standard, defined as the majority vote of labels of the radiologists. We used the other 3 radiologists to get estimates of radiologist performance on the task.

We compared radiologists and our model on the Cohen’s kappa statistic (\( \kappa \)), which expresses the agreement of each radiologist/model with the gold standard. We also reported the 95% confidence interval using the standard error of kappa (McHugh, 2012). Table 2 summarizes the performance of both radiologists and the model on the different study types and in aggregate. The radiologists achieved their highest performance on either wrist studies (radiologist 2) or humerus studies (radiologists 1 and 3), and their lowest performance on finger studies. The model also achieved its highest performance on wrist studies and its lowest performance on finger studies.

We compared the best radiologist performance on each of the study types against model performance. On finger studies, the model performance of 0.525 (95% CI 0.476, 0.573) was significantly higher than the best radiologist performance of 0.410 (95% CI 0.358, 0.463). On wrist studies, the model performance of 0.931 (95% CI 0.922, 0.940) was equivalent to the best radiologist’s performance. On all other study types, and overall, model performance was significantly lower than best radiologist’s performance.

We also compared the worst radiologist performance on each of the study types against model performance.
On forearm studies, the model performance of 0.670 (95% CI 0.634, 0.705) was significantly lower than the worst radiologist’s performance of 0.796 (95% CI 0.772, 0.821). On elbow studies, the model performance of 0.733 (95% CI 0.703, 0.764) was not significantly different than the worst radiologist’s performance of 0.733 (95% CI 0.703, 0.764). On all other study types, and overall, model performance was higher than the worst radiologist performance, and significantly so except on shoulder studies.

5. Model Interpretation

We visualize the parts of the radiograph which contribute most to the model’s prediction of abnormality by using class activation mappings (CAMs) (Zhou et al., 2016). We input the radiograph X into the fully trained network to obtain the feature maps output by the final convolutional layer. To compute the CAM $M(X)$, we take a weighted average of the feature maps using the weights of the final fully connected layer. Denote the $k$th feature map output by the network on image $X$ by $f_k(X)$ and the $k$th fully connected weight by $w_k$. Formally,

$$M(X) = \sum_k w_k f_k(X).$$

To highlight the salient features in the original radiograph which contribute the most to the network predictions, we upscale the CAM $M(X)$ to the dimensions of the image and overlay the image. We provide several examples of CAMs along with radiologist commentary in Figure 3.

6. Related Work

Large datasets have led to deep learning algorithms achieving or approaching human-level performance on tasks such as image recognition (Deng et al., 2009), speech recognition (Hannun et al., 2014), and question answering (Rajpurkar et al., 2016). Large medical datasets have led to expert-level performance on detection of diabetic retinopathy (Gulshan et al., 2016), skin cancer (Esteva et al., 2017), heart arrhythmias (Rajpurkar et al., 2017a), brain hemorrhage (Grewal et al., 2017), pneumonia (Rajpurkar et al., 2017b), and hip fractures (Gale et al., 2017).

There has been a growing effort to make repositories of medical radiographs openly available. Table 3 provides a summary of the publicly available datasets of medical radiographic images. Previous datasets are smaller than MURA in size, with the exception of the recently released ChestX-ray14 (Wang et al., 2017), which contains 112,120 frontal-view chest radiographs with up...
to 14 thoracic pathology labels. However, their labels were not provided directly from a radiologist, but instead automatically generated from radiologists’ text reports.

There are few openly available musculoskeletal radiograph databases. The Stanford Program for Artificial Intelligence in Medicine and Imaging hosts a dataset containing pediatric hand radiographs annotated with skeletal age (AIMI). The Digital Hand Atlas consists of left hand radiographs from children of various ages labeled with radiologist readings of bone age (Gertych et al., 2007). The OsteoArthritis Initiative hosts the O.E.1 dataset which contains knee radiographs labeled with the K&L grade of osteoarthritis (OAI). Each of these datasets contain less than 15,000 images.

7. Discussion

Abnormality detection in musculoskeletal radiographs has important clinical applications. First, an abnormality detection model could be utilized for worklist prioritization. In this scenario, the studies detected as abnormal could be moved ahead in the image interpretation workflow, allowing the sickest patients to receive quicker diagnoses and treatment. Furthermore, the examinations identified as normal could be automatically assigned a preliminary reading of "normal"; this could mean (1) normal examinations can be properly triaged as lower priority on a worklist (2) more rapid results can be conveyed to the ordering provider (and patient) which could improve disposition in other areas of the healthcare system (i.e., discharged from the ED more quickly) (3) a radiology report template for the normal study could be served to the interpreting radiologist for more rapid review and approval.

Second, automated abnormality localization could help combat radiologist fatigue. Radiologists all over the world are reading an increasing number of cases with more images per case. Physician shortages exacerbate the problem, especially for radiologists in medically underserved areas (Nakajima et al., 2008). While physician fatigue is a common problem that affects all healthcare professionals, radiologists are particularly susceptible, and there is evidence that workloads are so demanding that fatigue may impact diagnostic accuracy. (Bhargavan & Sunshine, 2005; Lu et al., 2008; Berlin, 2000; Fitzgerald, 2001). A study examining radiologist fatigue in the interpretation of musculoskeletal radiographs found a statistically significant decrease in fracture detection at the end of the work day compared to beginning of work day (Krupinski et al., 2010). Thus, a model which can perform automatic abnormality localization could highlight the portion of the image that is recognized as abnormal by the model, drawing the attention of the clinician. If effective, this could lead to more efficient interpretation of the imaging examination, reduce errors, and help standardize quality. More studies are necessary to evaluate the optimal integration of this model and other deep learning models in the clinical setting.

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