Depletion region surface effects in electron beam induced current measurements

Paul M. Haney¹, Heayoung P. Yoon², Benoit Gaury¹,³, Nikolai B. Zhitenev¹
¹. Center for Nanoscale Science and Technology, National Institute of Standards and Technology, Gaithersburg, MD 20899, USA
². Department of Electrical and Computer Engineering, University of Utah, Salt Lake City, UT 84112, USA
³. Maryland NanoCenter, University of Maryland, College Park, MD 20742, USA

Electron beam induced current (EBIC) is a powerful characterization technique which offers the high spatial resolution needed to study polycrystalline solar cells. Current models of EBIC assume that excitations in the p-n junction depletion region result in perfect charge collection efficiency. However we find that in CdTe and Si samples prepared by focused ion beam (FIB) milling, there is a reduced and nonuniform EBIC lineshape for excitations in the depletion region. Motivated by this, we present a model of the EBIC response for excitations in the depletion region which includes the effects of surface recombination from both charge-neutral and charged surfaces. For neutral surfaces we present a simple analytical formula which describes the numerical data well, while the charged surface response depends qualitatively on the location of the surface Fermi level relative to the bulk Fermi level. We find the experimental data on FIB-prepared Si solar cells is most consistent with a charged surface, and discuss the implications for EBIC experiments on polycrystalline materials.

I. INTRODUCTION

Polycrystalline photovoltaic materials such as CdTe exhibit high power conversion efficiency in spite of their high defect density [1]. Grain boundaries are a primary source of defects in these materials. Understanding the role of grain boundaries in the photovoltaic performance of these materials requires quantitative information about the electronic properties at the length scale of individual grains (typically 1 µm). A measurement technique which offers this spatial resolution is electron beam induced current (EBIC). Fig. 1 shows a schematic of an EBIC experiment: a beam of high energy electrons generates electron-hole pairs in proximity to an exposed surface. A fraction \( \eta \) of these electron-hole pairs are collected in the contacts and measured as electrical current [2], while the remaining fraction \( 1 - \eta \) undergoes recombination. We refer to \( \eta \) as the EBIC collection efficiency. EBIC has been used as a diagnostic tool for measuring material properties such as the minority carrier diffusion length and surface recombination velocity [3–5]. The small excitation volume associated with the electron beam is in close proximity to the exposed surface, so the high spatial resolution of EBIC is necessarily accompanied by strong surface effects on the measured signal.

Quantitative models of EBIC in single crystal materials are well established by Van Roosenbrook [4], Donolato [6] and Berz et al. [7], among others, who obtained solutions for the EBIC collection efficiency versus excitation position in the cross-sectional geometry, including the effects of surface recombination, while Ioannou et al. [8] and Luke [9] provide solutions and analysis for a planar contact geometry. All previous EBIC models apply for excitations in the neutral region, and enable the extraction of the minority carrier diffusion length, and the ratio of the surface recombination velocity to the minority carrier diffusivity. All of these models further assume that minority carriers in the p-n junction depletion region are collected with 100 % efficiency [10]. As we discuss next, this assumption is not always satisfied in EBIC experiments.

For CdTe, the EBIC response observed in several recent works deviates from the expected behavior based on previous EBIC models. For example, the depletion width of the p-n junction is on the order of 1 µm, and occupies a substantial fraction of the absorber thickness (which is typically on the order of 3 µm). Previous EBIC models assume 100 % collection from the depletion region, however experiments show a nonuniform EBIC response throughout the absorber which is well below 100 % [11–13]. In addition, the EBIC response near grain boundaries does not conform to existing models. These models relate the grain boundary recombination velocity to the reduction of EBIC collection efficiency at the grain boundary core [14]. However in CdTe the EBIC collection efficiency is maximized at the grain boundary core [11, 12].
Motivated by these observations, we present an extension of previous EBIC models to consider the response for excitations in the depletion region. We find analytical expressions and present numerical results for the EBIC collection efficiency which includes recombination from neutral and charged surfaces. To validate the relevance of the model, we also present experimental EBIC data on Si solar cells prepared by cleaving and focused ion beam (FIB) milling. We find that the FIB-prepared sample exhibits a suppressed maximum EBIC collection efficiency, and that the behavior is most consistent with the model of EBIC response in the presence of a charged surface.

The paper is organized as follows: in Sec. II we present experimental results of the cross-sectional EBIC response of Si solar cells where the sample surfaces are prepared with cleaving and FIB milling. In Sec. III we present 2-d numerical simulation results and corresponding analytical expressions for the EBIC efficiency in the depletion region which includes recombination at a neutral surface. In Sec. IV we extend the model to consider surfaces with charged defect levels. We end with a comparison of the model predictions to the experimental data, which shows that the charged surface model is most consistent with the experimental observations.

II. EXPERIMENT

We start with the experimental data which demonstrates the need for a model of EBIC response in the depletion region. Two sets of EBIC data were obtained from a commercially available, single crystalline Si solar panel (power conversion efficiency of 20 %). The absorber thickness is approximately 300 µm. A conventional capacitance-voltage measurement yields a doping density of $10^{13}$ cm$^{-3}$ in the Si absorber layer. We use the native contacts on the $p$-type and $n$-type layers of the solar cell for the EBIC measurement. Following the cleaving process, we carried out an additional ion milling process for one of the samples. A focused Ga ion beam at 30 keV (beam current of 2.5 nA) was irradiated on top of the sample, and the exposed area was etched away. This type of FIB process is often used to create smooth sections of photovoltaic devices prior to their local electrical and optical characterizations. The cross-sections of the cleaved and the FIB prepared Si samples were very smooth, minimizing the artifacts arising from the surface roughness. A series of EBIC data was obtained at different electron beam energies to examine the depth dependence of the EBIC response inside the depletion region and away from the $p$-$n$ junction.

To determine the absolute EBIC collection efficiency $\eta$, we estimate the generation rate of electron-hole pairs $G_{\text{tot}}$ using the empirical relation \[ G_{\text{tot}} = (1 - b) \frac{(I_{\text{beam}}/q) \times (E_{\text{beam}}/E_0)}{2.59 \times (E_g/E_0) + 0.71}, \] (1)

where $I_{\text{beam}}$ is the electron beam current, $q$ is the electron charge, $E_{\text{beam}}$ is the beam energy, $E_g$ is the material bandgap, $E_0 = 1$ eV, and $b$ is the backscattering coefficient, corresponding to the fraction of reflected energy. $b$ is determined by Monte Carlo calculations \[19\]; we find $b$ is approximately 0.15 and varies slightly with beam energy. The electron beam current varies with the beam energy, and is in the range of 200 pA to 500 pA. The EBIC collection efficiency is the ratio of the measured current to $G_{\text{tot}}$.

We estimate 10 % uncertainty in the measured EBIC efficiency $\eta$ (all uncertainties are reported as one standard deviation). The dominant sources of uncertainty are from the beam current, the backscattering coefficient, which is computed for pure, uncontaminated Si, and the reliability of the empirical relation we use Eq. (1) to estimate the rate of electron-hole pair generation.

EBIC collection efficiency maps are shown in Fig. 2(a) and (b) for the cleaved and FIB-prepared samples, respectively, for an electron beam energy of 15 keV. For the FIB-prepared sample, the maximum EBIC efficiency is reduced and the collection efficiency decays much more rapidly as compared to the cleaved sample. Plots of the EBIC collection efficiency versus excitation position for several electron beam energies are shown in Fig. 2(c) for the FIB-prepared sample. The maximum collection efficiency is much less than 100 % and only recovers to 0.85 for a beam energy of 20 keV (see Fig. 2(d)). In contrast, for cleaved samples we find that the maximum EBIC collection efficiency is 100 % (within the experimental uncertainty) for all electron beam energies. The

![EBIC collection efficiency maps](image-url)
reduced EBIC collection efficiency for FIB-prepared samples is therefore due to the sample surface preparation, indicating the importance of including surface effects in EBIC models.

We have checked that the electron-hole pair excitation rate is low enough to avoid “high-injection” nonlinearities in the EBIC response [20]. The excitation bulb size at energies less than 10 keV is less than the depletion width of the p-n junction (which is approximately 1 µm), so that the reduced efficiency is not the result of an extended excitation profile [21]. As discussed in the introduction, the observation of less than 100 % collection efficiency for excitations in the depletion region violates assumptions of previous EBIC models, motivating the models we present in the next sections.

III. RECOMBINATION FROM NEUTRAL SURFACES

We consider the collection efficiency for an excitation in the depletion region for a 2-d model, which includes recombination from the exposed surface. In this section the surface is assumed to be uncharged.

Fig. 1 shows our geometry and coordinate system. For the 2-d finite difference simulations, we solve the electron and hole continuity equations together with the Poisson equation. The depth of the system away from the surface \(L_z\) is large enough to ensure that the lower boundary does not affect the results. We use a highly non-uniform mesh, with grid spacing as small as 1 nm near the surface in order to properly resolve the generation profile and density gradients there.

We assume selective contacts, such that the contact surface recombination is infinite (zero) for majority (minority) carriers. The exposed surface recombination is included by adding an extra recombination term at the surface,

\[ R_{surf} = \delta(z) \times S \frac{nk_n - n^2}{n_e + p_s + n_{surf} + p_{surf}}, \] (2)

where the surface recombination velocity \(S\) parametrizes the magnitude of the surface recombination. \(n_s (p_s)\) is the electron (hole) density evaluated at the surface, and \(n_{surf}, p_{surf}\) are

\[ n_{surf} = N_C \exp \left( \frac{E_{surf} - E_C}{k_B T} \right) \] (3)

\[ p_{surf} = N_V \exp \left( \frac{E_V - E_{surf}}{k_B T} \right), \] (4)

where \(E_{surf}\) is the surface defect energy level, \(E_V (E_C)\) is the valence (conduction) band edge energy, \(N_C (N_V)\) is the conduction and valence effective band density of states, \(k_B\) is the Boltzmann constant, and \(T\) is the temperature. For the neutral surface we take \(E_{surf}\) to be at midgap.

| Parameter       | Value       |
|-----------------|-------------|
| \(N_C = N_V\)   | \(10^{19}\) cm\(^{-3}\) |
| \(E_g\)         | 1.1 eV      |
| \(N_A\)         | \(10^{14}\) cm\(^{-3}\) to \(10^{15}\) cm\(^{-3}\) |
| \(N_D\)         | \(10^{18}\) cm\(^{-3}\) |
| \(\mu_e = \mu_h\) | 10 cm\(^2\)/(V⋅s) |
| \(\epsilon\)    | 11          |
| \(\tau_{bulk}\) | \(10^{-6}\) s |
| \(L_x\)         | \(30\) µm    |
| \(L_z\)         | \(56\) µm    |
| \(I_{beam}\)    | 1 pA        |
| \(S\)           | \(10^6\) cm/s |
| \(N_{surf}\)    | \(10^{11}\) cm\(^{-2}\) |

TABLE I: List of default parameters for numerical simulations.

The generation profile for a beam positioned at \(x_B\) is taken to be Gaussian:

\[ G(x,z) = \frac{A}{2\pi\sigma^2} \exp \left[ -\frac{(x-x_B)^2 + (z-z_B)^2}{2\sigma^2} \right], \] (5)

where \(z_B = 0.3 R_B, \sigma = R_B/\sqrt{15}\) [5], and the excitation bulb size \(R_B\) is given in the following empirical relation [22]:

\[ R_B = \frac{0.043 \times R_0}{(\rho/\rho_0)} \left( \frac{E_{beam}/E_0'}{1.75} \right), \] (6)

where \(\rho\) is the material mass density, \(\rho_0 = 1\) g/cm\(^3\), \(E_0' = 1\) keV, and \(R_0 = 1\) µm.

The units of the total generation in the 2-d model are \(s^{-1}\) m\(^{-1}\). To convert the experimental generation rate \(G_{tot}\) (which has units \(s^{-1}\)) into a 2-dimensional generation rate, we divide \(G_{tot}\) by the diffusion length \(L_D\). In Eq. (5), \(A\) is chosen such that the spatial integral of \(G(x,z)\) in the sample is equal to \(G_{tot}/L_D\). Table I gives a list of the parameters used in the numerical calculations.

The beam current used in the simulation is less than the experimental value. We find that using the experimental value in a 2-d simulation results in high injection effects and screening of the p-n junction. However, the experiment is not in the high injection regime, as evidenced by the lack of beam current dependence, the undistorted EBIC lineshapes [23], and the estimate for the critical beam current for high injection given in Ref. [20]. The reason for this discrepancy is that the onset of high injection effects depends strongly on system dimensionality [24]. We therefore reduce the electron beam current of the model to prevent high injection effects.

Fig. 3(a) shows the computed EBIC efficiency as a function of beam position for a fixed beam energy of 1 keV and three values of \(S\). The maximum efficiency
is strongly reduced for increasing $S$. We propose the following expression to describe the EBIC efficiency when the excitation is localized near the surface:

$$\eta(E_{\text{beam}} \to 0) = \frac{\mu E}{\mu E + S/2},$$

where $\mu$ is the smaller of the electron and hole mobility, and $E$ is the (position-dependent) electric field. Eq. (7) has a simple physical interpretation. The collection efficiency is determined from the competition between drift current and surface recombination. The total collection rate from drift current is $A_x \times (n \mu E)$, where $n$ is the carrier density at the excitation point, and $A_x$ is the area of the excitation normal to the direction of the drift current. The total recombination rate is $A_z \times (n S/2)$, where $A_z$ is the area of the excitation normal to the surface. The factor of $1/2$ multiplying $S$ follows from the assumption that $n \approx p$ near the excitation, which reduces the recombination rate at the surface by $1/2$ (see Eq. (2)). This assumption is easily satisfied for excitations in the depletion region. For the small, symmetrical excitations considered here, $A_x \approx A_z$. Forming the ratio of the collection rate to the sum of the collection and recombination rates leads to Eq. (7).

Larger beam energies generate electron-hole pairs further from the surface, reducing its effect on the EBIC collection efficiency. This is demonstrated in the simulation data shown in Fig. 3(b), where the maximum EBIC efficiency increases with increasing beam energy. We find that the following expression accounts for the dependence of the surface recombination on the excitation depth $z_B$:

$$\eta = 1 - \left( \frac{S/2}{\mu E + S/2} \right) \left( \frac{D/z_B}{\mu E + D/z_B} \right).$$

In the above, the first factor in parentheses is the recombination probability for a charge located at the surface. This is given by the ratio of the recombination velocity to the sum of drift and recombination velocities (see discussion below Eq. (7)). The second factor in Eq. (8) represents the probability a charge located at $z_B$ below the surface will diffuse to the surface.

The solid lines of Fig. 4 show the estimated EBIC collection efficiency given by Eq. (8), using the standard form of the p-n junction electric field $E(x)$. We observe good agreement deep within the depletion region (for beam positions between 0.3 and 0.7 $\mu$m) between the analytical and numerical models. In this region the assumption $n \approx p$ is satisfied. For beam positions outside of this interval, a disparity between the numerical and analytical models is due to a violation of the $n \approx p$ assumption. The maximum EBIC signal occurs deep within the junction so that Eq. (5) reliably predicts the maximum EBIC collection efficiency.

The predicted maximum EBIC efficiency versus electron beam energy is shown in Fig. 4 as a solid red line. The surface recombination has a minor impact on EBIC efficiency for electron beam energies greater than 5 keV, corresponding to excitation bulb sizes greater than 300 nm. This can be understood from Eq. (8), which shows that surface recombination becomes negligible for $z_B \gg D/(\mu E)$. For relevant material parameters, this corresponds to $z_B \approx 10$ nm.

The experimental data also shown in Fig. 4 indicate that surface effects are present at much larger electron beam energies than those predicted by the neutral surface model. While our numerical and analytical work provide a full picture of the neutral surface model, the experimental data are at odds with these results, indicating that other factors not included in this model play a key role in the experiment. In the next section, we consider electric fields at the surface induced by charged surface defects.

![FIG. 3: (a) Simulated EBIC linescans for a series of surface recombination velocities, with fixed beam energy of 1 keV. (b) Simulated EBIC linescans for a series of electron beam energies, with a fixed $S = 10^6$ cm/s. For both plots, circles indicate numerical results, while solid lines show the prediction of Eq. (5).](image)

![FIG. 4: Maximum EBIC efficiency versus beam energy for the neutral and charged surface 2-d models, and the experimental data. In the models, $S = 10^6$ cm/s. For the charged surface model, $E_{\text{surf}} = 0$. $N_{\text{surf}} = 10^{14}$ cm$^{-2}$, and the results for two doping densities are shown.](image)
IV. RECOMBINATION FROM CHARGED SURFACES

We next consider charged surface defect states. The surface charge density \( \rho_{\text{surf}} \) is determined by the occupancy \( f_{\text{surf}} \) of defect energy level [23]:

\[
\rho_{\text{surf}} = q \frac{N_{\text{surf}}}{2} (1 - 2f_{\text{surf}}),
\]

where \( N_{\text{surf}} \) is the 2-d density of surface defect states and \( f_{\text{surf}} \) is given by

\[
f_{\text{surf}} = \frac{n_s + \rho_{\text{surf}}}{n_s + p_s + n_{\text{surf}} + \rho_{\text{surf}}.}
\]

We add Eq. (9) to the drift-diffusion-Poisson numerical model. Fig. 5 shows the computed equilibrium electrostatic potential for a surface defect energy level at the midgap and \( \rho_{\text{surf}} = 10^{11} \text{ cm}^{-2} \). As expected, the Fermi level is pinned to the defect energy level at the surface, which leads to dramatic changes in the electrostatic potential of the \( p-n \) junction.

An important transition occurs where the bulk \( p-n \) junction electrochemical potential is equal to the surface defect energy level - this is shown as a red arrow in Fig. 5 and we denote this position \( x_0 \). For positions greater than \( x_0 \), the surface electrostatic field is directed away from the surface, while for positions less than \( x_0 \), the surface field is directed toward the surface. The surface field generally changes directions within the \( p-n \) junction for any surface defect level which is positioned between the Fermi levels of the \( n \) and \( p \) type semiconductors. The surface field drives electrons towards the surface for \( x > x_0 \), and drives holes to the surface for \( x < x_0 \). We emphasize that the position of \( x_0 \) depends strongly on the surface defect energy level.

\[ \text{FIG. 6: Depiction of band diagrams versus position away from the surface } z \text{ at a position } x > x_0 \text{ (upper row) where the bulk is } p \text{-type, and at a position } x < x_0 \text{ (lower row) where the bulk is } n \text{-type. The surface may be } n \text{-type, intrinsic, or } p \text{-type. Depending on the combination of surface and bulk properties, recombination is enhanced or suppressed at the surface, as shown in the various cases. Electrons (holes) are represented with red (blue) dots, and arrows indicate the drift direction of each carrier type due to the surface electric field.} \]

We start with a qualitative discussion of the system behavior. Far enough from the surface, there is drift along the bulk \( p-n \) junction. Holes (electrons) drift parallel (anti-parallel) to the field lines of Fig. 5. Closer to the surface, carriers drift towards/away from the surface, which is the dominant recombination center. The minority carrier type at the surface depends on the surface defect energy level. If the carriers driven to the surface by the surface electric field are minority carriers there, then recombination occurs and the EBIC signal is decreased (this corresponds to Figs. 6(c) and (d)). On the other hand, if the carriers driven to the surface are majority carriers there, then recombination does not take place (this corresponds to Figs. 6(a) and (f)). Due to Fermi level pinning at the surface, there is no potential gradient along it so that majority carriers undergo simple diffusion to the contacts along the surface, and the EBIC collection efficiency is \( \approx 100 \% \). The various cases of surface and bulk types and the resultant surface recombination \( R_{\text{surf}} \) are shown in Fig. 6.

Fig. 7 shows that the impact of the surface field on the EBIC efficiency depends on the surface type (\( n \), \( p \), or intrinsic). We first consider a \( p \)-type surface. The collection efficiency is maximized for excitation positions less than \( x_0 \) (i.e. where the field is directed toward the surface). In this case the surface field drives holes toward the surface, where they are majority carriers and therefore undergo no recombination. On the other hand, for excitation positions greater than \( x_0 \) (i.e. where the
field is directed away from the surface) the surface field drives electrons to the p-type surface. Because electrons are minority carriers there, they undergo recombination and the the EBIC collection efficiency is reduced.

For an n-type surface, the situation is reversed; for excitation positions less than \(x_0\), the surface field drives holes to the n-type surface, where they recombine, while for excitations positioned beyond \(x_0\), the surface field drives electrons to the n-type surface, where they avoid recombination. This results in an “inverted” EBIC signal in which the collection efficiency is maximized away from the p-n junction. This type of EBIC signal has been previously observed \([25, 26]\) and attributed to surface passivation via the electrostatic surface field, as described here.

Finally, for an intrinsic surface, there is no clearly defined majority/minority carrier and both electrons and holes undergo recombination at the surface. In this case, the collection efficiency is maximized at the excitation position \(x = x_0\); at this position the magnitude of the surface field is minimized, so carriers aren’t driven to the surface here. In this case, the maximum EBIC efficiency is significantly less than 1, consistent with the experimental observations.

The length scale in the \(z\)-direction over which the surface influences the EBIC collection efficiency is set by the depletion width of the surface, which depends on the surface defect level and bulk doping. This length scale is generally much larger than that of the neutral surface recombination. For example, a midgap surface defect level and p-type doping of \(10^{14} \text{ cm}^{-3}\) results in a surface depletion width of \(1.5 \mu\text{m}\).

Fig. 7(a) shows the simulated EBIC lineshape for several electron beam energies for a \(p\) doping level of \(N_A = 10^{14} \text{ cm}^{-3}\) and midgap surface defect level. As expected, the surface effect is diminished for larger beam energies (larger excitation bulb sizes). The dotted vertical line in Fig. 7(b) indicates the surface depletion width, and the maximum EBIC efficiency begins to saturate for excitation bulb sizes which exceed this. Fig. 7(c) and (d) show the same data for an increased doping level \((N_A = 5 \times 10^{14} \text{ cm}^{-3})\) and smaller associated surface depletion width. As expected, the surface influence is diminished at lower electron beam energies in this case.

Fig. 8 shows the maximum EBIC efficiency versus electron beam energy observed experimentally, together with the predictions of the neutral and charge surface models. It is clear that the charged surface model is more consistent with the data. For a doping density of \(10^{15} \text{ cm}^{-3}\), the EBIC collection efficiency increases with electron beam energy more rapidly than observed experimentally. However, the value of EBIC efficiency at high electron beam energies remains well below 1. We consider this to be a signature of surface recombination from charged surfaces. Reducing the doping density to \(10^{14} \text{ cm}^{-3}\) in the model yields a better fit to experimental data. We also find that to obtain the best fit to experimental data, the value of the mobility \(\mu\) must be substantially lower than the expected Si mobility (we use \(\mu = 10 \text{ cm}^2/(\text{V} \cdot \text{s})\), see Table 1). Since most of the carrier transport occurs near the sample surface, it is plausible that for the FIB-prepared sample the mobility of carriers near the surface is substantially less than the bulk mobility, due to disor-
V. CONCLUSION

In summary, we’ve developed a model of the EBIC response to excitations in the depletion region which includes surface recombination from neutral and charged surfaces. This model is motivated by observations that, under certain experimental conditions, the maximum EBIC collection efficiency is substantially less than 100% and varies throughout the depletion region. A comparison between the model and Si samples offers clear indication of the role of surface effects in EBIC experiments, and how they depend on sample preparation methods. A particularly useful and common application of low energy, high resolution EBIC is probing the characteristics of polycrystalline photovoltaics. However the interpretation of the EBIC response in these materials is complicated by the presence of grain boundaries. Using a simpler material such as Si offers a cleaner interpretation of surface effects and development of surface models. Ultimately these surface models can be applied to more complex materials, enabling a determination of properties of grain boundary and subsurface interfaces. Moreover, models of the EBIC response at the sample surface can be readily applied to internal surfaces (e.g. grain boundaries), so that the formulas and qualitative descriptions given here may be applied to studies of grain boundaries as well.

Acknowledgment

B. Gaur acknowledges support under the Cooperative Research Agreement between the University of Maryland and the National Institute of Standards and Technology Center for Nanoscale Science and Technology, Award 70NANB10H193, through the University of Maryland. H. Yoon also acknowledges the support by the NSF MRSEC program at the University of Utah under grant # DMR 1121252.

[1] S. G. Kumar, K. S. R. K. Rao, Energy and Environmental Science 7, 45 (2014).
[2] J.I. Hanoka, R.O. Bell, Annu. Rev. Mater. Sci. 11, 353 (1981).
[3] C. J. Wu and D. B. Wittry, J. Appl. Phys., 49, 2827, (1978).
[4] W. can Roosbroeck, J Appl. Phys. 26, 380 (1955).
[5] C. Donolato, Solid-State Elect. 25, 1077 (1982).
[6] C. Donolato, App. Phys. Lett. 43, 120 (1983).
[7] F. Berz and H. K. Kuiken, Sol. St. Elect. 19 437 (1976).
[8] D. E. Ioannou and C. A. Dimitriadis, IEEE Trans. on Elect. Dev. 29, 445 (1982).
[9] K. L. Luke, J. App. Phys. 80, 5775 (1996).
[10] The assumption that all carriers within the depletion region are collected is contained in the boundary condition that the minority carrier density vanishes at the depletion region edge.
[11] C. Li, Y. Wu, J. Poplewsky, T. J. Pennycook, N. Paudel, W. Yin, S. J. Haigh, M. P. Oxley, A. R. Lupini, M. Al-Jassim, S. J. Pennycook, and Y. Yan, Phys. Rev. Lett. 112, 156103 (2014).
[12] H. P. Yoon, P. M. Haney, D. Ruzmetov, H. Xua, M. S. Leite, B. H. Hamadani, A. Talin, and N. B. Zhitenev, Sol. Energy Mat. and Solar Cells 117, 499, (2013).
[13] O. Zywitzki, T. Modes, H. Morger, C. Metzner, B. Siepchen, B. Späth, C. Drost, V. Krishnakumar, and S. Frauenstein, J. App. Phys. 114, 163518 (2013).
[14] C. Donolato, J. Appl. Phys. 54, 1314 (1983).
[15] C. Donolato, Mat. Sc. and Eng. B24, 61 (1994).
[16] R. Corkish, T. Puzzer, A. B. Sproul, and K. L. Luke, J.
[17] J. Chen, T. Sekiguchi, D. Yang, F. Yin, K. Kido and S. Tsurekawa, J. App. Phys 96, 5490 (2004).

[18] H. Yoon, P. M. Haney, J. Schumacher, K. Siebein, Y. Yoon, N. B. Zhitenev, Microscopy and Microanalysis, 20, 544 (2014).

[19] J. F. Ziegler, M. D. Ziegler, and J. P. Biersack, Nucl. Inst. and Methods in Phys. Res. Sec. B: Beam Int. with Mat. and Atoms 268, 1818 (2010).

[20] P. M. Haney, H. P. Yoon, P. Koirala, R. W. Collins, N. B. Zhitenev, Nanotech. 26, 295401 (2015).

[21] K. L. Luke, O. v. Roos, and L.-j. Cheng, J. App. Phys. 57, 1978 (1985).

[22] A. E. Grün, Zeitschrift für Naturforschung, 12a (1957) 89.

[23] M. Nichterwitz and T. Unold, J. App. Phys. 144, 134504 (2013).

[24] K. Taretto and U. Rau, J. App. Phys. 103, 094523 (2008).

[25] R. Hakimzadeh and S. G. Bailey, J. Appl. Phys. 74, 1118 (1993).

[26] G. A. Hungerford and D. B. Holt, Institute of Physics Conference Series 87, 721 (1987).

[27] S. Saraf and Y. Rosenwaks, Surf. Sci. 574, L35 (2005).