Detection of Ventricular Fibrillation Using the Image from Time-Frequency Representation and Combined Classifiers without Feature Extraction

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Abstract: Due to the fact that the required therapy to treat Ventricular Fibrillation (VF) is aggressive (electric shock), the lack of a proper detection and recovering therapy could cause serious injuries to the patient or trigger a ventricular fibrillation, or even death. This work describes the development of an automatic diagnostic system for the detection of the occurrence of VF in real time by means of the time-frequency representation (TFR) image of the ECG. The main novelties are the use of the TFR image as input for a classification process, as well as the use of combined classifiers. The feature extraction stage is eliminated and, together with the use of specialized binary classifiers, this method improves the results of the classification. To verify the validity of the method, four different classifiers in different combinations are used: Regression Logistic with L2 Regularization (L2RLR), adaptive neural network (ANN), Bagging (BAGG), and K-nearest neighbor (KNN). The Hierarchical Method (HM) and Voting Majority Method (VMM) combinations are used. ECG signals used for evaluation were obtained from the standard MIT-BIH and AHA databases. When the classifiers were combined, it was observed that the combination of BAGG, KNN, and ANN using the Hierarchical Method (HM) gave the best results, with a sensitivity of 95.58 ± 0.41%, a 99.31 ± 0.08% specificity, a 98.6 ± 0.04% of overall accuracy, and a precision of 98.25 ± 0.29% for VF. Whereas a sensitivity of 94.02 ± 0.58%, a specificity of 99.31 ± 0.08%, an overall accuracy of 99.14 ± 0.43%, and a precision of 98.59 ± 0.09% was obtained for VT with a run time between 0.07 s and 0.12 s. Results show that the use of TFR image data to feed the combined classifiers yields a reduction in execution time with performance values above to those obtained by individual classifiers. This is of special utility for VF detection in real time.

Keywords: biomedical systems; ECG electrocardiogram signals; time-frequency representation; non-stationary signals; image analysis; combined classification algorithms; hierarchical classifiers; voting majority method classifiers

1. Introduction

The most common causes of sudden death are cardiovascular diseases, which are among the leading causes of death worldwide. One of the cardiovascular diseases with the highest mortality is Ventricular Fibrillation (VF), which is a cardiac arrhythmia condition produced by a disorganized electrical activity in the ventricles. During VF, the ventricles contract with an absence of an effective...
beat causing a pumping failure which could lead to a sudden death if the patient is not adequately treated within a few minutes. Defibrillation is the only definitive treatment for VF. It consists of applying a high voltage electric shock on the patient’s chest, facilitating the restart of a normal electrical cardiac activity [1–3]. However, the success of defibrillation is inversely proportional to the interval of time lapsed from the beginning of the episode to the application of the discharge.

There are many difficulties in diagnosing VF: On the one hand, the intrinsic characteristics of the VF signal (lack of organization, irregularity, etc.) and, on the other hand, the great similarity between VF and other cardiac pathologies such as ventricular tachycardia (VT) [4], especially in early stages of VF. The differentiation between VT and VF is quite complex: The wrongful diagnosis of VF for a patient that really suffers of VT can cause serious complications at the time of applying the therapy corresponding toVF (high voltage electrical discharge), as it may cause VF to the patient. On the contrary, if VF is incorrectly interpreted as VT or any other cardiac rhythm, the result can also be dangerous for the patient's life since the treatment would imply receiving less voltage than the appropriate level. Thus, an effective detection method for distinguishing VF from VT is critical in clinical research.

The electrocardiogram (ECG) is a non-invasive, low-cost examination tool that has been used as the basic method of diagnosing cardiac conduction disorders by studying the heart rate and morphology of different waves that constitute the cardiac cycle. ECG analysis is a good source of information from which different types of heart disease can be detected. Due to the fact that the ECG signal is a non-stationary random signal, the time domain analysis does not prove to be sufficiently sensitive to the distortions of the ECG waveforms. However, these methods do not always show all the information that can be extracted from the ECG signals [5,6], thus losing information on the frequency domain which shows additional information on the signal.

Diagnosis in the frequency domain [7] uses methods such as the Fourier transform. Therefore, the analysis in the frequency domain allows to determine the frequencies of the signal. On the other hand, the temporary-type information of the signal is lost, which is a very limited method and is not useful for the analysis of non-stationary signals. Several studies have used mathematical models that combine temporal and spectral information in the same representation. This technique of Time-Frequency Representation (TFR) is very important in the treatment of non-stationary signals such as the ECG signal, as it distributes the energy of the signal in a two-dimensional time-frequency space [8,9]. In addition, multiple factors might alter the acquisition and recording of the ECG signal: The influence of the environment, 50–60 Hz mains interference, variations of the base line of low-frequency interference in the range of 0 Hz to 0.5 Hz [10,11]. On the other hand, there are disturbances of physiological origin such as those of electromyography (EMG). ECG noise reduction has been one of the main fields of research in the last decades since an adequate noise reduction allows a good pre-processing of the signal, extracting the maximum amount of information possible and eliminating ECG signal contamination from other sources.

Usually, after the initial processing of the signal, several algorithms are applied to obtain characteristics, features, or parameters which are supposed to offer a difference in value depending on the pathology. Typically, these parameters can be redundant or remove relevant information, being necessary to apply different techniques to select the most adequate. After optimisation, selected parameters are intended to serve as input to a classifier responsible for separating classes (associated to a pathology or type of rhythm, in this case), i.e. identified signal types.

In order to improve the performance of individual classifiers, the combination of classifiers (multiclassifiers) can improve the performance in separating classes. It is based on constructing a global classifier built from a set of classifiers that can provide interesting information on the representation of data compared to the results achieved using individual classifiers. There are many examples in the literature that have used the combination of classifiers focused towards the field of bioinformatics and biomedical research, geophysical analysis and remote sensing, among others. Out of the most frequently used multi classifiers, Random Forests [12], Bagging [8], Boosting [13], or Random Subspaces
are the most commonly employed multiclassifiers. In the case of Random Subspaces, different subsets of attributes are used to train each individual classifier. The Bagging type variety comes from using different subsets of instances to train each individual classifier. Random Forests is a substantial modification of bagging that uses Random Trees as individual classifiers. The Boosting type iteratively trains the individual classifiers, therefore, it modifies the weights of the instances that will use the next individual classifier. There are other methods such as cascading [14], Stacking [15], and Grading [16].

Other examples using a combination of classifiers for ECG signal analysis can be found in the literature as a multiple classifier system [17], a genetic ensembles of classifiers [18], or a classification approach that uses majority voting optimized by the taguchi method [19]. In some cases, a majority voting [20,21], or a combined stacking technique [22]. Other combinations are also applied, e.g., an application of the decision tree to integrate the results of a set of individual neural classifiers (MLP, TSK, and the SVM) working in parallel [23] or a majority voter determining the P-wave absence over seven beats [24].

This work proposes a new strategy for the detection of VF whose steps are the initial processing of the signal and obtaining its time-frequency representation (TFR) with its equivalent image (TFRI). The TFR or TFRI (both cases will be analysed) is directly entered into an individual classifier or combined, without calculating parameters or extracting features since time-frequency representation contains both temporal and spectral information from the ECG signal, allowing the classifier to have enough information for the detection of different types of cardiac pathologies in real time. Since the ECG is a temporal signal, it is not common to find works converting the temporal signal into an image and further analyse the image, some works used some geometrical features from the ECG in combination with other features entering the classification stage. Other works also extract features from a time-frequency or discrete wavelet transform, but they do not use it as an image.

In order to reach the objectives sought, the present work is structured as follows: Section 2 describes the materials and methods, followed by Section 3 which details the initial processing applied to the ECG signal. Section 4 shows the extraction of information. Section 5 presents the individual and combined classification algorithms. Section 6 shows the standard statistical indexes, and finally, Section 7 shows obtained results for individual and combined classifiers, and Sections 8 and 9 give a comparison of results with other authors and conclusions, respectively.

2. Materials and Methods

Records of the ECG signals have been taken from the standard MIT-BIH Malignant Ventricular Arrhythmia Database [25,26] and AHA (2000 series) [27], generating both the training and the test sets from them. In total, 24 continuous monitoring records (22 MIT-BIH records plus two additional AHA records) were used, with a sampling frequency of 125 Hz. All records have cardiac events already labeled. The additional AHA records aim to increase the number of Ventricular Tachycardia (VT) episodes to improve the balance between recorded time of VT and VF episodes. With the episodes labeled, four groups (classes) of signals were created: Ventricular Fibrillation (VF) corresponds to the class VF represents all the sections of registers in which there has been ventricular fibrillation and ventricular flutter. ECG signals with the presence of ventricular tachycardia were assigned to the class VT, which, in many cases, appear as a prior stage to ventricular fibrillation (sometimes, VT sections have VF-like morphologies). Normal rhythms were assigned to the Normal class that constitutes the segments labeled with sinus rhythm. Finally, the rest of signal types not labelled as the previous classes (other arrhythmias, noise, etc.) have also been considered and assigned to the class Others. In total, 20,040 s were generated for all ECG signal registers, 3600 s corresponded to the class VF, 1380 s to VT, 10,860 s to Normal, and 4200 s to Others.

3. ECG Signal Processing

If we look for a classifier that can obtain a satisfactory result of detecting VF and its differentiation from VT, it is necessary that the data provided as input to this classifier are properly treated. For this
reason, different stages of data conditioning are performed to both the temporal signal of ECG and its time-frequency representation TFR. Figure 1 shows the general scheme of the followed methodology, from the reading of the records of the database to the results obtained by the classifier.

Figure 1. General diagram of the processing steps performed for the detection of Ventricular Fibrillation. After the reduction of the baseline oscillation and the calculation of the reference marks, the Hilbert transform (Ht) and the time-frequency representation (TFR) for a time window (tw) is obtained. Optionally, the possibility of obtaining the equivalent image from the TFR (TFRI) is used to serve as input to the combined classifier using three cascaded classifiers (Cla, Clb, Clc) where all of them are the same type (Cla = Clb = Clc) or combined Cla_Clb_Clc in case at least one classifier among them (Cla, Clb, Clc) is different.

The developed methodology is composed of three fundamental phases.

- First phase: Data filtering in order to reduce the baseline that affects the ECG. Once filtered, obtain the Window Reference Mark (WRM) of the ECG signal. Each WRM indicates the beginning of a time window (tw) of the ECG signal.
- Second phase: Extraction of information through the implementation of the Hilbert transform to each window tw obtained in the first phase, then, assessment of the TFR matrix using the Pseudo Wigner-Ville, and the Time-Frequency Representation Image (TFRI).
- Third phase: The classification phase is carried out considering both the individual and combined classifiers used. In this phase, the previously obtained TFRI matrices are used as input. The success in the detection of VF depends on the processing of the signal and the structure of the classifiers used. In order to better adapt to the data, we must adjust the parameters of the classifier to obtain the best performance.

3.1. Reduction of Baseline Oscillations

The first step in the processing of the ECG signal is to use a baseline filter, reducing the variation of the baseline and thus obtaining a better quality and definition of the temporal signal that will result in better characteristics provided by the TFR. This processing consists of the implementation of an 8th order infinite impulse response filter (IIR) with a Butterworth bandpass type ranging from 1 Hz to 45 Hz [28,29]. Figure 2 represents the effect of applying this bandpass filter, showing a reduction of the baseline. Thus, all signal contribution not located in the mentioned frequency range, which corresponds to non-ECG source, are eliminated.
3.2. Reference Marks

Next, it is necessary to obtain a Window Reference Mark (WRM) to indicate the beginning of the $t_w$ ECG time window. Following [30], a value from 50 to 120 beats per minute (bpm) can be considered as a normal heart rate range, and thus, the minimum ($WRM_{\text{min}}$) and the maximum ($WRM_{\text{max}}$) distances between two consecutive WRM is 0.5 s and 1.2 s, respectively. Accordingly, these values were used in our analysis. The calculation of WRM reference marks was obtained by an already developed algorithm [8], where $N_{\text{LMC}}$ is the number of local maxima LM marks existing in the signal. From each previously generated WRM reference mark, a time window $t_w$ of 1.2 s in length ($150$ samples) was generated, starting at the corresponding WRM mark, $t_w = [WRM, WRM+1.2\text{ s}]$ as shown in (Equation (1)).

$$t_w = [WRM_j, WRM_j + 1.2\text{ s}]; \ j = 1, ..., N_{\text{LMC}}$$ (1)

4. Extraction of Information

For each window $t_w$, the Hilbert transform (Ht) is calculated first and then TFR of the PWV (Pseudo Wigner-Ville) type is calculated. Once the TFR is obtained, the contributions of frequency over 45 Hz are canceled, thereby eliminating both the network interference (50 Hz or 60 Hz) as well as the electromyogram (EMG). After this process, a Data Matrix ($DM'$) obtained from the TFR, being $45 \times 150$ in size is obtained. This is useful since the signal of interest is found in values below 45 Hz (see Figure 3a,b).

Once $DM'$ is obtained from the TFR for each $t_w$ window, this data matrix TFR is converted into an image $TFRI_{L_f \times L_t}$ with size $L_f \times L_t$ pixels being $L_f = 45$ and $L_t = 150$ converting the energy levels of the signal into a pixel intensity range from 0 to 255. These values correspond to different levels of grey in an image as they are shown in Figure 3c,d. Each $TFRI$ image is then stored in a Data Matrix ($DM''$) of size $45 \times 150$.

Once $DM''$ data matrix is obtained, the data matrix is directly fed into the classifier. By doing this, all ECG signal information in the temporal and spectral domains is contained in the data matrix, providing the classifier with maximal data information. Note that this method requires a large number of inputs to the classifiers ($45 \times 150 = 6750$) since each $DM''_{ij}$ data in a matrix coordinate corresponds to an input. It is important to note that there is no feature extraction from the data matrix $DM''$ as it contains the temporal and spectral information from the ECG signal.
Figure 3. From top to bottom: (a,b) correspond to the original signal window and TFR; (c,d) show the TFRI being 45 × 150 in size, for Normal (c) and VF (d) types.

5. Classification Algorithms

In this work, several classifiers are used to evaluate the efficiency of the VF detection algorithm. All DM′′ data were separated into two subsets: one for training and one for test. The training subset is used so that the algorithms learn to discriminate among the various types of defined classes (VF, VT, Normal, and Others). As soon as each classifier concludes its training, it generates a prediction function that is later used to evaluate new data. Each of the classifiers used in this work have parameters that must be optimized for the purpose of obtaining the maximum yield. The tuning of the classifiers is done on the basis of final classification performance.

Some algorithms propose the use of four classes [8,31]. However, we can combine different binary algorithms for two-class separation so that they can provide important complementary information about the representation of the data.

Combination Topologies

The parallel topology method is the most frequent in combination of classifiers. All the classifiers are run in parallel using the same input data, and the results achieved by all the classifiers (classifier1-Cla, classifier2-Clb, classifier3-Clc) generate a multiclassifier result (Cla_Clbd_Clce) that are combined with the objective of obtaining an appropriate decision using a combination rule, e.g., the voting method [32], as shown in Figure 4 which is called Voting Majority Method (VMM). For real time execution, this methodology has a high execution time since all classification algorithms must be executed to make the final decision. The voting method works in the same way as the humans when voting in political elections. In other words, depending on the number of votes reached in favor of each class, it is assigned to the one that obtains the majority.
Figure 4. Parallel classifier combination and final voting. All classifiers receive all data and must obtain a four-class decision through a majority voting among results generated by each classifier.

In a hierarchical topology, parallel and cascaded topologies are combined (Figure 5). By joining these two approaches, better results than those achieved by using individual classifiers can be obtained. The first classifier (Cla) generates a binary output for signal to be VFVT or NormalOthers. Then, two specific classifiers Clb and Clc generate a new binary classification VF, VT for the signal classified as VFVT by Cla, and Others, Normal for the signal classified as NormalOthers, respectively. By joining the classifiers, a multi-class cascaded algorithm is generated.

Figure 5. Hierarchical topology classifier. Multi-class classification is obtained by joining several binary classifiers.

6. Performance Assessment

To evaluate the performance of the classifier, we use standard statistical indexes such as Sensitivity (Sens), Specificity (Spe), Accuracy (Acc), and Precision (Pre), as shown by Equations (2)–(5), where TP are the True Positives, FN the False Negatives, TN the True Negatives, and FP the False Positives [33].

\[
\text{Sensitivity(\%)} = \frac{TP}{TP + FN} \times 100
\]

\[
\text{Specificity(\%)} = \frac{TN}{TN + FP} \times 100
\]

\[
\text{Accuracy(\%)} = \frac{TP + TN}{TP + FN + TN + FP} \times 100
\]

\[
\text{Precision(\%)} = \frac{TP}{TP + FP} \times 100
\]

The calculation of the value of the global specificity, accuracy and Precision of one of the types (VF, VT, Normal, Others) is obtained by using the specificity, accuracy, and Precision of this type of pathology before the sum of the remaining pathology types. The execution time of each of the tests performed was measured using a Fujitsu AH544 (Tokyo, Japan) laptop computer with an Intel (R) Core (TM) i7-3612QM@2.10 GHz processor with 8GB RAM, 64-bit operating system using Matlab (R).

For completion, the Receiver Operating Characteristic (ROC) curve and Area Under the Curve (AUC) values are also calculated.
7. Results

In total, 28,507 windows were generated for all MD obtained from the corresponding TFRI: 5309 corresponded to the class VF, 1987 to VT, 15,160 to Normal, and 6051 to Others. For each class, 67% of the data were used for training, and the rest for testing. This approach is repeated by making a 5-fold cross validation: Individual and combined classifier algorithms are assessed by taking the average of these 5 iterations. A 5-fold validation was chosen amongst different z-fold possibilities after some trials, with 5-fold cross validation obtaining the lowest generalization error, thus minimizing the structural risk of classifiers. For 5-fold cross validation, each class was divided into five datasets, equal in size; four dataset were used for training and one for testing. After five iterations, all datasets served for training and testing, obtaining a more balanced result.

Different analyses were done, the first test is based on different types of individual classification algorithms, the second uses combined classification algorithms.

7.1. Results for Individual Classifiers

In this first test, individual classifiers are used. The results are obtained using four different classification algorithms: L2RLR, ANNC, BAGG, and KNN [8,31]. After several trials, the parameters for the classifiers were the following:

- **L2RLR**: With regularization parameter $\lambda = 10^{-9}$. In this case, the $\lambda$ value is very small to account for high values in regression coefficients.
- **ANNC**: Two hidden layers, 20 neurons in each hidden layer. Two layers allow better classification in case of a high number of inputs, as in this case. In case of a single layer, a higher number of neurons should be used.
- **BAGG**: 600 decision trees. This was an experimental value. A higher number of trees did not produce better results.
- **KNN**: Euclidean distance showed a good performance, together with K = 1.

Tables 1 and 2 summarize the results achieved by making comparisons between the values of sensitivity, specificity, accuracy, and precision. When analyzing the values shown in the tables, it is observed that the KNN classifier obtained the best result, with a sensitivity of 94.97 $\pm$ 0.70%, a global specificity of 99.27 $\pm$ 0.05%, accuracy of 98.47 $\pm$ 0.01%, and an overall precision of 97.09 $\pm$ 0.14% achieved for VF. For VT, a sensitivity of 93.47 $\pm$ 0.19%, specificity of 99.39 $\pm$ 0.15%, accuracy 98.97 $\pm$ 0.08%, and an overall precision of 92.11 $\pm$ 0.7% was obtained.

For a complete analysis, the confusion matrices for the classes and the used algorithms were calculated (Tables 3 and 4). These tables show that the main conflicts exist in pairs: VF and VT, Normal and Others. Actually, since the number of segments is lower for VF and VT compared to normal and Others, the proportion of confusion mainly resides in VF and VTS, which was expected according to other algorithm results and clinical practice.
Table 1. Results for the different algorithms adaptive neural network (ANNC), Bagging (BAGG), L2 Regularization (L2RLR), and K-nearest neighbor (KNN) using as input the time-frequency representation image (TFRI) used to characterize and detect VF and VT classes.

| Classification Algorithms | VF       | VT       |
|---------------------------|----------|----------|
|                           | Sens %   | Spe %    | Acc %   | Pre %   | Sens %   | Spe %    | Acc %   | Pre %   |
| **L2RLR**                 |          |          |         |         |          |          |         |         |
| Test                      | 91.54 ± 0.46 | 98.45 ± 0.06 | 97.15 ± 0.09 | 94.74 ± 1.27 | 88.15 ± 0.59 | 98.81 ± 0.04 | 98.07 ± 0.07 | 89.67 ± 1.77 |
| **ANNC**                  |          |          |         |         |          |          |         |         |
| Test                      | 95.56 ± 0.33 | 98.80 ± 0.13 | 98.19 ± 0.15 | 95.26 ± 0.45 | 88.80 ± 1.13 | 99.52 ± 0.06 | 98.87 ± 0.03 | 94.05 ± 0.80 |
| **BAGG**                  |          |          |         |         |          |          |         |         |
| Test                      | 98.46 ± 0.26 | 98.43 ± 0.12 | 98.44 ± 0.14 | 97.09 ± 0.14 | 84.8 ± 1.70 | 99.86 ± 0.04 | 98.82 ± 0.12 | 97.81 ± 0.82 |
| **KNN**                   |          |          |         |         |          |          |         |         |
| Test                      | 94.97 ± 0.70 | 99.27 ± 0.05 | 98.47 ± 0.01 | 97.09 ± 0.14 | 93.47 ± 0.19 | 99.39 ± 0.15 | 99.97 ± 0.08 | 92.11 ± 0.70 |

Table 2. Results for individual algorithms ANNC, BAGG, L2RLR, and KNN using as input the TFRI used to characterize and detect Others and Normal classes.

| Classification Algorithms | Others   | Normal  |
|---------------------------|----------|---------|
|                           | Sens %   | Spe %    | Acc %   | Pre %   | Sens %   | Spe %    | Acc %   | Pre %   |
| **L2RLR**                 |          |          |         |         |          |          |         |         |
| Test                      | 94.80 ± 0.55 | 98.79 ± 0.03 | 97.91 ± 0.12 | 96.29 ± 0.98 | 97.63 ± 0.12 | 96.61 ± 0.4 | 97.17 ± 0.27 | 97.56 ± 0.68 |
| **ANNC**                  |          |          |         |         |          |          |         |         |
| Test                      | 96.87 ± 1.06 | 99.55 ± 0.08 | 98.96 ± 0.21 | 98.45 ± 0.39 | 98.98 ± 0.13 | 97.72 ± 0.56 | 98.40 ± 0.27 | 98.39 ± 0.22 |
| **BAGG**                  |          |          |         |         |          |          |         |         |
| Test                      | 95.66 ± 0.31 | 99.87 ± 0.02 | 98.95 ± 0.07 | 99.60 ± 0.10 | 99.39 ± 0.19 | 97.61 ± 0.09 | 98.57 ± 1.31 | 97.71 ± 0.04 |
| **KNN**                   |          |          |         |         |          |          |         |         |
| Test                      | 97.69 ± 0.21 | 99.40 ± 0.04 | 99.03 ± 0.05 | 97.92 ± 0.16 | 99.07 ± 0.08 | 98.29 ± 0.10 | 98.71 ± 0.06 | 98.66 ± 0.06 |
Table 3. Confusion matrix for classification of VF, VT, Others, and Normal using the L2RLR and ANNC algorithms.

| Algorithms | L2RLR | ANNC |
|------------|-------|-------|
|            | VF    | VT    | Others | Normal | VF    | VT    | Others | Normal |
| VF         | 1627  | 64    | 13     | 48     | 1689  | 34    | 3      | 26     |
| VT         | 59    | 583   | 2      | 12     | 55    | 589   | 0      | 12     |
| Others     | 9     | 0     | 1909   | 79     | 11    | 1     | 1941   | 44     |
| Normal     | 32    | 8     | 68     | 4895   | 18    | 3     | 27     | 4955   |

Table 4. Confusion matrix for classification of VF, VT, Others, and Normal using the BAGG and KNN algorithms.

| Algorithms | BAGG | KNN |
|------------|------|-----|
|            | VF   | VT  | Others | Normal | VF   | VT  | Others | Normal |
| VF         | 1721 | 9   | 2      | 20     | 1666 | 52  | 13     | 21     |
| VT         | 85   | 564 | 0      | 7      | 27   | 618 | 0      | 11     |
| Others     | 4    | 1   | 1902   | 90     | 8    | 0   | 1954   | 35     |
| Normal     | 16   | 3   | 6      | 4978   | 14   | 1   | 29     | 4949   |

Comparing the results offered by the different algorithms, there is an important variation in the results for the sensitivities of VF and VT depending on the algorithm. For instance, if the sensitivity level for VF is high, the sensitivity for VT decreases. It can be observed that the KNN classifier achieves the best performance for the proposed methodology due to the adequate detection and discrimination capacity of VF when compared against the rest of classes. However, it has a high execution time because the KNN algorithm requires many iterations to calculate the closest distances. For the ANNC algorithm, the classes are separated by means of a surface that maximizes the margin among them, with the least number of training errors, having a computational cost much lower than that obtained with KNN. The L2RLR algorithm has less time of execution because it is based on probabilities. The Bagging creates its individual classifiers by training a system of classification on different bootstrap samples of the training set, thus retrieving a higher run time than the rest of the classifiers (except for KNN).

7.2. Comparative Study for the Method of Combined Classifiers

In this section, the results obtained by the combination methods are described: Voting Majority Method (VMM) and Hierarchical Method (HM) described above. In the classification tests performed, we show how the combination of classification algorithms behaves in relation to the results obtained in the previous test using individual classifiers. For proper comparison, the same DM" data used for individual classifiers, and the same classifier parameters were used in these analyses.

In the first analysis, the Voting Majority Method (VMM) is applied using different combinations of three individual classification algorithms in parallel, the results obtained are shown in Tables 5–8. When analyzing the results from the tables, it can be seen, in both cases, that the detection of VF has significantly improved when compared with individual classifiers. However, the detection of VT has decreased when compared with what those obtained by the KNN algorithm, which was the best individual classifier. It is concluded that the combination of classifiers do not exceed the results obtained in case of KNN.
Table 5. Results for the voting majority method (VMM) combination method using TFRI as data input. Results correspond to detection of VF and VT pathologies.

| Class | Combined Classification Algorithms (Cla, Clb, Clc) | VF | VT |
|-------|--------------------------------------------------|----|----|
|       | Sens % | Spe % | Acc % | Pre % | Sens % | Spe % | Acc % | Pre % |
| ANNC_KNN_L2RLR Test | 97.47 ± 0.13 | 99.09 ± 0.10 | 98.71 ± 0.06 | 96.12 ± 0.23 | 91.31 ± 0.88 | 99.97 ± 0.08 | 99.18 ± 0.01 | 96.26 ± 0.90 |
| ANNC_KNN_BAGG Test | 98.46 ± 0.06 | 98.98 ± 0.02 | 98.89 ± 0.01 | 96.04 ± 0.60 | 89.63 ± 0.30 | 99.86 ± 0.01 | 99.14 ± 0.02 | 97.64 ± 0.15 |
| BAGG_KNN_L2RLR Test | 98.43 ± 0.16 | 98.98 ± 0.08 | 98.87 ± 0.04 | 95.79 ± 0.50 | 91.01 ± 0.68 | 99.83 ± 0.03 | 99.16 ± 0.02 | 97.51 ± 0.18 |
| BAGG_ANNC_L2RLR Test | 97.89 ± 0.08 | 98.84 ± 0.05 | 98.66 ± 0.04 | 95.33 ± 0.31 | 87.80 ± 1.21 | 99.88 ± 0.03 | 99.98 ± 0.06 | 97.61 ± 0.50 |

Table 6. Results for the VMM combination method using TFRI as data input. Results correspond to detection of Other and Normal classes.

| Class | Combined Classification Algorithms (Cla, Clb, Clc) | Others | Normal |
|-------|--------------------------------------------------|--------|--------|
|       | Sens % | Spe % | Acc % | Pre % | Sens % | Spe % | Acc % | Pre % | Sens % | Spe % | Acc % | Pre % |
| ANNC_KNN_L2RLR Test | 97.35 ± 0.15 | 99.67 ± 0.02 | 99.16 ± 0.03 | 98.57 ± 0.05 | 99.22 ± 0.05 | 98.41 ± 0.09 | 98.84 ± 0.03 | 98.63 ± 0.02 |
| ANNC_KNN_BAGG Test | 97.20 ± 0.11 | 99.84 ± 0.04 | 99.27 ± 0.01 | 99.21 ± 0.14 | 99.52 ± 0.06 | 98.29 ± 0.05 | 98.95 ± 0.01 | 98.64 ± 0.04 |
| BAGG_KNN_L2RLR Test | 96.95 ± 0.11 | 99.77 ± 0.04 | 99.16 ± 0.01 | 99.25 ± 0.18 | 99.4 ± 0.05 | 98.30 ± 0.03 | 98.89 ± 0.01 | 98.51 ± 0.02 |
| BAGG_ANNC_L2RLR Test | 96.54 ± 0.09 | 99.74 ± 0.05 | 99.05 ± 0.02 | 99.12 ± 0.17 | 99.38 ± 0.09 | 97.68 ± 0.23 | 98.59 ± 0.09 | 98.26 ± 0.17 |
Table 7. Confusion matrix for classification of \textit{VF}, \textit{VT}, \textit{Others}, and \textit{Normal} classes using the ANNC\textsubscript{KNN}\textsubscript{L2RLR} and ANNC\textsubscript{KNN}BAGG VMM combined classifier.

| Algorithms | ANNC\textsubscript{KNN}L2RLR | ANNC\textsubscript{KNN}BAGG |
|------------|-------------------------------|-------------------------------|
|            | VF   | VT   | Others | Normal | VF   | VT   | Others | Normal |
| VF         | 1706 | 23   | 5      | 18     | 1720 | 17   | 2      | 13     |
| VT         | 45   | 600  | 1      | 10     | 53   | 595  | 0      | 8      |
| Others     | 8    | 0    | 1948   | 41     | 1943 | 47   |
| Normal     | 14   | 0    | 23     | 4985   | 14   | 1    | 15     | 4973   |

Table 8. Confusion matrix for classification of \textit{VF}, \textit{VT}, \textit{Others}, and \textit{Normal} classes using the BAGG\textsubscript{KNN}L2RLR and BAGG\textsubscript{ANNC}L2RLR VMM combined classifier.

| Algorithms | BAGG\textsubscript{KNN}L2RLR | BAGG\textsubscript{ANNC}L2RLR |
|------------|-----------------------------|-----------------------------|
|            | VF   | VT   | Others | Normal | VF   | VT   | Others | Normal |
| VF         | 1724 | 14   | 0      | 14     | 1717 | 13   | 2      | 2      |
| VT         | 55   | 595  | 0      | 6      | 62   | 586  | 0      | 8      |
| Others     | 6    | 1    | 1935   | 55     | 7    | 0    | 1930   | 60     |
| Normal     | 14   | 1    | 14     | 4974   | 15   | 1    | 16     | 4971   |

In the second analysis, the Hierarchical Method (HM) is applied to three individual algorithms (\textit{Cla}, \textit{Clb}, \textit{Clc}) getting the \textit{Cla Clb Clc} multiclassifier where \textit{Clb} and \textit{Clc} are in parallel and both cascaded after \textit{Cla} (Figure 5). The obtained results are shown in Tables 9 and 10 with confusion matrices in Tables 11–13.

Since \textit{KNN} was the best individual algorithm in the detection and discrimination between \textit{VF} and \textit{VT}, it was chosen as \textit{Clb}. The \textit{ANNC}, \textit{BAGG}, \textit{L2RLR} algorithms are taken as \textit{Cla} for the discrimination between the classes \textit{VFVT} and \textit{NormalOthers} and the \textit{ANNC} and \textit{L2RLR} algorithms are used as \textit{Clc} for \textit{Normal} and \textit{Others} discrimination. Analyzing the results, it can be concluded that the combinational algorithms have a similar or better behavior than the individual \textit{KNN} in the detection of \textit{VF} in very large datasets and high dimensionality, with a reduced execution time.

With all the results obtained, the use of combined algorithms can be recommended as the best method of classification. In addition, results obtained using the combination \textit{BAGG\textsubscript{KNN}ANNC} using HM showed better classification ratio when compared to those obtained using the algorithms individually, and other multi classifiers.

The \textit{BAGG\textsubscript{KNN}ANNC} HM obtained a good behavior in the discrimination between the classes \textit{VF}, \textit{VT}, \textit{Normal}, and \textit{Others}, with a sensitivity of 95.58 \pm 0.4%, a global specificity of 99.31 \pm 0.08%, an accuracy of 98.6 \pm 0.04%, and an overall precision of 98.25 \pm 0.29% for \textit{VF}. For \textit{VT}, a sensitivity of 94.02 \pm 0.58%, a specificity of 99.31 \pm 0.08%, an accuracy of 99.14 \pm 0.43%, and a precision of 98.59 \pm 0.09% was obtained.

It is interesting to note that the \textit{ANNC} classifier obtained a good behavior in the discrimination between the classes \textit{Normal} and \textit{Others}, and the \textit{BAGG} classifier had a good behavior in the discrimination between the classes \textit{NormalOthers} and \textit{VFVT} with a fast execution time in comparison with the individual \textit{KNN} algorithm.
Table 9. Results for different hierarchical method (HM) combined classifier methods to detectVF and VT pathologies.

| Class                  | Combined Classification Algorithms (Cla, Clb, Clc) | Sens % | Spe % | Acc % | Pre % | Sens % | Spe % | Acc % | Pre % |
|------------------------|---------------------------------------------------|--------|-------|-------|-------|--------|-------|-------|-------|
|                        | VF                                                 |        |       |       |       | VT                                              |       |       |       |
| ANNC_KNN_ANNC          | Test                                               | 95.13 ± 0.06 | 99.10 ± 0.04 | 98.41 ± 0.04 | 96.38 ± 0.19 | 92.32 ± 0.66 | 99.33 ± 0.07 | 98.91 ± 0.02 | 91.38 ± 0.84 |
| ANNC_KNN_L2RLR         | Test                                               | 94.89 ± 0.56 | 99.08 ± 0.20 | 98.32 ± 0.27 | 96.02 ± 0.87 | 92.37 ± 2.46 | 99.27 ± 0.10 | 98.78 ± 0.23 | 90.71 ± 1.38 |
| BAGG_KNN_ANNC          | Test                                               | 95.58 ± 0.40 | 99.31 ± 0.08 | 98.6 ± 0.04 | 98.25 ± 0.29 | 94.02 ± 0.58 | 99.31 ± 0.08 | 99.14 ± 0.43 | 98.59 ± 0.09 |
| BAGG_KNN_L2RLR         | Test                                               | 95.58 ± 0.42 | 99.31 ± 0.04 | 98.6 ± 0.05 | 96.93 ± 0.19 | 94.02 ± 0.58 | 99.31 ± 0.08 | 99.14 ± 0.43 | 91.25 ± 0.91 |
| L2RLR_KNN_ANNC         | Test                                               | 93.33 ± 0.31 | 98.93 ± 0.07 | 97.88 ± 0.12 | 95.30 ± 0.96 | 92.01 ± 0.58 | 99.22 ± 0.09 | 98.71 ± 0.03 | 90.06 ± 1.37 |
| L2RLR_KNN_L2RLR        | Test                                               | 93.54 ± 0.31 | 98.01 ± 0.07 | 97.98 ± 0.12 | 95.65 ± 0.35 | 92.95 ± 0.58 | 99.26 ± 0.08 | 98.82 ± 0.03 | 90.70 ± 0.98 |

Table 10. Results for different HM combined classifier methods to detect Normal and Others classes.

| Class                  | Combined Classification Algorithms (Cla, Clb, Clc) | Others | Sens % | Spe % | Acc % | Pre % | Normal | Sens % | Spe % | Acc % | Pre % |
|------------------------|---------------------------------------------------|--------|-------|-------|-------|-------|--------|-------|-------|-------|-------|
|                        |                                                   |         |        |       |       |       |         |        |       |       |       |
|                        | VF                                                 |         |        |       |       |       | VT                                              |       |       |       |       |
| ANNC_KNN_ANNC          | Test                                               | 97.22 ± 0.14 | 99.57 ± 0.11 | 99.06 ± 0.10 | 98.45 ± 0.39 | 99.04 ± 0.15 | 98.10 ± 0.26 | 98.61 ± 0.15 | 98.39 ± 0.22 |
| ANNC_KNN_L2RLR         | Test                                               | 96.11 ± 0.67 | 99.18 ± 0.33 | 98.45 ± 0.38 | 96.70 ± 1.16 | 98.42 ± 0.43 | 97.67 ± 0.26 | 98.17 ± 0.30 | 98.01 ± 0.22 |
| BAGG_KNN_ANNC          | Test                                               | 97.42 ± 0.12 | 99.52 ± 0.07 | 99.07 ± 0.08 | 98.25 ± 0.29 | 99.02 ± 0.14 | 98.36 ± 0.10 | 98.72 ± 0.11 | 98.59 ± 0.09 |
| BAGG_KNN_L2RLR         | Test                                               | 96.92 ± 0.38 | 98.92 ± 0.05 | 98.28 ± 0.04 | 96.10 ± 0.17 | 98.22 ± 0.07 | 97.73 ± 0.19 | 97.99 ± 0.05 | 98.06 ± 0.16 |
| L2RLR_KNN_ANNC         | Test                                               | 97.22 ± 0.11 | 99.50 ± 0.06 | 99.01 ± 0.07 | 98.20 ± 0.24 | 98.61 ± 0.14 | 97.39 ± 0.27 | 98.05 ± 0.18 | 97.79 ± 0.23 |
| L2RLR_KNN_L2RLR        | Test                                               | 95.71 ± 0.30 | 98.84 ± 0.02 | 98.16 ± 0.04 | 95.83 ± 0.07 | 97.81 ± 0.08 | 96.89 ± 0.32 | 97.38 ± 0.10 | 97.34 ± 0.27 |

VF: Ventricular Fibrillation; VT: Ventricular Tachycardia; ANNC: Artificial Neural Network Classifier; KNN: K-Nearest Neighbors; L2RLR: L2 Regularized Logistic Regression; BAGG: Bagging; Pre: Predictive; Acc: Accuracy; Sens: Sensitivity; Spe: Specificity; Cla, Clb, Clc: Different combinations of classifiers.
Table 11. Confusion matrix for classification of \(VF\), \(VT\), \(Others\), and \(Normal\) using the \(ANNC\_KNN\_ANNC\) and \(ANNC\_KNN\_L2RLR\) combined classifiers in HM topology.

| Algorithms | \(ANNC\_KNN\_ANNC\) | \(ANNC\_KNN\_L2RLR\) |
|------------|-----------------|-----------------|
| \(VF\)     | 1667 56 3 26    | 1662 60 7 23    |
| \(VT\)     | 33 612 0 11    | 38 606 1 11    |
| \(Others\) | 12 0 1941 44 | 12 0 1919 66 |
| \(Normal\)| 19 2 27 4955 | 18 2 59 4924 |

Table 12. Confusion matrix for classification of \(VF\), \(VT\), \(Others\), and \(Normal\) using the \(BAGG\_KNN\_ANNC\) and \(BAGG\_KNN\_L2RLR\) combined classifiers in HM topology.

| Algorithms | \(BAGG\_KNN\_ANNC\) | \(BAGG\_KNN\_L2RLR\) |
|------------|-----------------|-----------------|
| \(VF\)     | 1674 56 5 17    | 1674 56 7 15    |
| \(VT\)     | 32 617 0 7     | 32 617 1 6     |
| \(Others\) | 5 0 1945 47    | 5 0 1916 76    |
| \(Normal\)| 16 3 30 4954 | 16 3 70 4914 |

Table 13. Confusion matrix for classification of \(VF\), \(VT\), \(Others\), and \(Normal\) using the \(L2RLR\_KNN\_ANNC\) and \(L2RLR\_KNN\_L2RLR\) combined classifiers in HM topology.

| Algorithms | \(L2RLR\_KNN\_ANNC\) | \(L2RLR\_KNN\_L2RLR\) |
|------------|-----------------|-----------------|
| \(VF\)     | 1635 60 6 51    | 1639 56 12 45    |
| \(VT\)     | 38 604 0 14    | 32 610 1 13    |
| \(Others\) | 9 0 1941 47    | 9 1 1911 76    |
| \(Normal\)| 32 7 30 4934 | 33 7 69 4894 |

Table 14 shows the average execution time of all the classification algorithms analyzed in this work. The execution time corresponds to the elapsed time between the input of a \(tw\) window from the ECG signal to the generation of a classification result of the algorithm. Concerning individual classifiers, it can be appreciated that \(L2RLR\) and \(ANNC\) have a lower computational cost than other individual algorithms, with a run time of \(t = 7 \times 10^{-5}\) s and \(t = 5 \times 10^{-4}\) s, respectively. For \(KNN\) and \(BAGG\), \(t = 0.17\) s and \(t = 0.05\) s was attained, respectively. In case of the VMM combination methods, they are the slowest among HM and individual, ranging from \(t = 190\) ms to \(t = 290\) ms. This is normal since all three classifiers (\(Cla\), \(Clb\), \(Clc\)) must be computed, increasing the total computation time. Actually, any VMM combination method required more computation time than the slowest individual algorithm (\(KNN\)). In case of HM classification methods, we obtained different computation time depending on the executed classifier (\(Clb\) or \(Clc\)) depending on the results given by the first classifier (\(Cla\)). For this reason we obtained a minimum and maximum computation time, ranging from \(t = 50\) ms to \(t = 130\) ms. Thus HM combined methods provide a high classification, together with a reduced computation time, showing their feasibility for real-time classification systems.
8. Discussion

Table 15 and Figure 6 show the AUC values and ROC curves, respectively, Figure 6a for VF and Figure 6b for VT in case of the analyzed individual algorithms. Table 16 and Figure 7 show the AUC values and ROC curves, respectively, for VF (Figure 6a) and VT (Figure 6b) classification results for the VMM combination of classifiers. Table 17 and Figure 8 show the AUC values and ROC curves, respectively, for VF (Figure 6a) and VT (Figure 6b) classification results for the HM combination of classifiers. As shown, ROC curves are more adjusted in case of combined classifiers, especially in case of the VMM method.

![ROC curves for VF detection algorithms](image1.png)

![ROC curves for VT detection algorithms](image2.png)

**Figure 6.** ROC curve for VF (a) and VT (b) in L2 Regularization (L2RLR), adaptive neural network (ANNC), Bagging (BAGG), and K-nearest neighbor (KNN) individual algorithms.
Figure 7. Receiver operating characteristic (ROC) curve for voting majority method (VMM) combination methods in detection of VF (a) and VT (b).

Figure 8. ROC curve for hierarchical method (HM) classification combination methods in detection of VF (a) and VT (b).

Table 15. Area under the curve (AUC) values for VF and VT in L2RLR, ANNC, BAGG, and KNN individual algorithms.

| Algorithm | L2RLR (%) | ANNC (%) | BAGG (%) | KNN (%) |
|-----------|-----------|----------|----------|---------|
| AUC(VF)   | 95.02     | 97.18    | 98.44    | 97.12   |
| AUC(VT)   | 93.48     | 94.16    | 92.33    | 96.43   |

Table 16. AUC for VMM combination methods in detection of VF and VT.

| Algorithm | ANNC_KNN_L2RLR (%) | ANNC_KNN_BAGG (%) | BAGG_KNN_L2RLR (%) | ANNC_ANNC_L2RLR (%) |
|-----------|--------------------|--------------------|--------------------|---------------------|
| AUC(VF)   | 98.28              | 98.72              | 98.70              | 98.36               |
| AUC(VT)   | 95.03              | 97.18              | 98.44              | 97.12               |

Table 17. AUC for HM classification combination methods in detection of VF and VT.

| Algorithm | ANNC_KNN_ANNC (%) | ANNC_KNN_L2RLR (%) | ANNC_KNN_L2RLR (%) | ANNC_KNN_L2RLR (%) | ANNC_KNN_L2RLR (%) | ANNC_KNN_L2RLR (%) | BAGG_KNN_ANNC (%) |
|-----------|-------------------|--------------------|--------------------|--------------------|--------------------|--------------------|-------------------|
| AUC(VF)   | 97.11             | 96.98              | 97.44              | 97.44              | 97.44              | 96.13              | 95.77             |
| AUC(VT)   | 95.03             | 97.18              | 99.44              | 97.12              | 97.12              | 97.12              | 98.44             |
Additionally, the structural risk of the classifier is important in order to determine the training robustness. A risk test is proposed by the A-test where multiple z-fold cross-validation are performed in order to assess how classification error evolves. In this case, we have also tested 9-fold cross validation for comparison purposes with 5-fold. Figure 9 shows that very similar results are obtained for the same classifier. Specially in case of HM combined classifiers, z-5 provides a slightly higher classification ratio. In any case, differences between z-5 and z-9 in the same classifier do not exceed 1% in classification value.

Since correct detection and classification of VF and VT is of pivotal importance for an automatic external defibrillation and patient monitoring, they should be able to distinguish VF and VT accurately. If VT was misinterpreted as VF, a high-energy defibrillation would be delivered, which could damage the heart. If VT is misinterpreted as VF, the low-energy cardioversion may not return the heart to its normal sinus rhythm, which could be fatal [34]. However, clear distinction between ventricular arrhythmia rhythms and normal or other arrhythmias is required, preventing the patient to be unnecessarily exposed to an electrical cardioversion.

As previous results show, the proposed methods obtain a high accuracy, not only in VF and VT separation but also in Normal and Others. This fact leads to further separate the Others class into other sub-classes where different heart pathologies could also be detected: Premature Ventricular Complex (PVC) in bigeminy or trigeminy, hypertrophy, idioventricular Rhythms, asystoles, etc. Thus, using a new classifier level, all rhythms detected as Others could enter into a new classification process in order to discern among other cardiac pathologies.

Table 18 compares results with different studies in the bibliography to check to what extent the obtained data support our hypothesis. Although different works are roughly comparable, we set two different groups for better comparison: those works aiming to distinguish between VF and VT, and those works classifying multiple rhythms.

Table 18

| Classification Values (%) using z-5 Fold and z-9 Fold Cross Validation |
|---------------------------------------------------------------|
| Class            | z-5_VF | z-9_VF | z-5_VT | z-9_VT | z-5_Others | z-9_Others | z-5_Normal | z-9_Normal |
|------------------|---------|--------|--------|--------|------------|------------|------------|------------|
| %                | 84      | 86     | 88     | 90     | 92         | 94         | 96         | 98         |

**Figure 9.** Classification rate for sensibility to each class, for the test dataset using z-5 and z-9 cross validation. Individual and combined VMM and HM classifiers are shown.
Table 18. Performance evaluation of VF detection algorithms for comparison with the four analyzed classifiers in this work.

| Types | VF       | VT       | Other | Normal |
|-------|----------|----------|-------|--------|
|       | Sens %   | Spe %    | Acc % | Sens % | Spe % | Acc % | Sens % | Spe % | Acc % | Data Base |
| This work, ANNC(t-f) | 95.56 | 98.80 | 98.19 | 88.80 | 99.52 | 98.87 | 96.86 | 99.55 | 98.98 | AHA & MIT-BIH |
| This work, BAGG(t-f) | 98.46 | 98.43 | 98.44 | 84.58 | 99.86 | 98.82 | 95.66 | 99.87 | 98.95 | AHA & MIT-BIH |
| This work, KNN(t-f) | 94.97 | 99.27 | 98.47 | 93.47 | 99.39 | 98.97 | 97.69 | 99.40 | 99.07 | AHA & MIT-BIH |
| This work, BAGG_KNN_ANNC(t-f) | 95.58 | 99.31 | 98.6 | 94.02 | 99.31 | 99.14 | 97.42 | 99.52 | 99.07 | AHA & MIT-BIH |
| [35], using Boltzmann | 92.52 | 93.80 | 94.7 | 96.20 | 96.20 | 96.3 | 96.20 | 96.20 | 96.3 | AHA & MIT-BIH |
| [1], using Discriminant Analysis | 94.40 | 95.90 | 94.7 | 96.20 | 96.20 | 96.3 | AHA & MIT-BIH |
| [36], using Filter and Counts | 94.40 | 95.90 | 94.7 | 96.20 | 96.20 | 96.3 | AHA & MIT-BIH |
| [37], using SVM | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | 96.20 | 96.3 | AHA & MIT-BIH |
| [38], using Lempel-Ziv and EMD | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | 96.20 | 96.3 | AHA & MIT-BIH |
| [39], using Fuzzy Simil App Entropy | 97.98 | 97.03 | 97.5 | 94.40 | 95.90 | 94.7 | 96.20 | 96.20 | 96.3 | AHA & MIT-BIH |
| [39], using Approximate Entropy | 91.84 | 90.2 | 91.0 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | AHA & MIT-BIH |
| [40], using EMD & App Entropy | 90.47 | 91.66 | 91.2 | 98.10 | 93.80 | 96.20 | 96.20 | 96.3 | AHA & MIT-BIH |
| [41], using KNN | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | 96.20 | 96.3 | AHA & MIT-BIH |
| [41], using RBF | 91.53 | 90.91 | 91.3 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | AHA & MIT-BIH |
| [42], using Type 2 fuzzy | 90.9 | 84.0 | 91.3 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | AHA & MIT-BIH |
| [42], using Neural SOM | 90.9 | 84.0 | 91.3 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | AHA & MIT-BIH |
| [43], using Type 2 TSK Fuzzy | 93.3 | 92.0 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | 96.3 | AHA & MIT-BIH |
| [43], using Type 2 Mamdani Fuzzy | 93.3 | 92.0 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | 96.3 | AHA & MIT-BIH |
| [44], using Random Forest Classifier | 95.04 | 94.78 | 94.7 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | AHA & MIT-BIH |
| [45], using SVM | 95 | 99 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | 96.3 | AHA & MIT-BIH |
| [45], using SVM | 95 | 99 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | 96.3 | AHA & MIT-BIH |
| [46], using SVM | 95 | 99 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | 96.3 | AHA & MIT-BIH |
| [47], using SVM | 95 | 99 | 98.15 | 96.01 | 97.1 | 94.10 | 93.80 | 96.20 | 96.3 | AHA & MIT-BIH |
For the first group, Xie et al. [39] used approximate entropy to distinguish between VF and VT with performance ratios of Sens = 91.84% to VF, Spe = 90.2%, Acc = 91.0%, using similar signal sources than our work. In addition, they also proposed a modified version using fuzzy similarity-based approximate entropy that, in turn, got high performance ratios (Sens = 97.98% to VF, Spe = 97.03%, Acc = 97.5%). Although we obtained higher values, to make a fair comparison between both analysis, it has to be taken into account that Xie used representative and clean episodes of VT and VF as input data, in front of our work that used a multiclass scheme, classifying four types of rhythms and considering complete patient’s registers as the input signal. The same happens for other studies distinguishing between VF and VT rhythms; Kaur and Singh [40] used approximate entropy with Empirical Mode Decomposition (EMD) and a more reduced dataset than Xie, having good performance values (Sens = 90.47 to VF, Spe = 91.66%, Acc = 91.2%). Later, Xia et al. [38] also used, in the same line, Lempel-Ziv Complexity and EMD in the same conditions that Xie did before, using a representative number of clean episodes of each pathology, and they also got high performance ratios (Sens = 98.15% to VF, Spe = 96.01%, Acc = 97.1%). The same occurred to Li et al. [37] using SVM where Sens = 96.20% to VF, Spe = 96.20%, and Acc = 96.3%, for a 2 s window, was obtained; in this case, a sensitive different set of source signals was used. Other works provides good performance ratios distinguishing between VF and VT when applied to compressed ECG signals [41]. In all cases, our performance results are slightly or sensitive better.

As a second group of comparable works we can find those aiming to distinguish normal sinus (N) apart from VT or VF. Within this group, Tan et al. [42] obtained good accuracy ratios (Acc(VF) = 90.9%, Acc(VT) = 84.0%, Acc(N) = 100%) using a type-2 fuzzy logic-based classifier for a three class multiclass classification (VF, VT and Normal). Tan also described the results of using a SOM neural network with poor VT accuracy. Later, Phong et al. [43] followed the same line implementing another multiclass classifier using a type-2 TSK fuzzy system, with the same three classes than Tan used; in this case, with better accuracy ratios (Acc(VF) = 93.3%, Acc(VT) = 92.0%, Acc(N) = 100%). They also tried a a type-2 Mandami fuzzy system with lower values.

Other works analyse a binary distinction between VF and non-VF rhythms. Verma et al. [44] used 17 features: Morphological, spectral, and complexity. Here, the random forest classifier has been used for discrimination between VF category and non-VF category, with Acc = 94.79%, Sens = 95.04%, Spe = 94.78%. In [45], they used 13 parameters accounting for temporal (morphological), spectral, and complexity features of the ECG signal, using an SVM to distinguish between VF and non-VF categories with Sens = 95%, Spe = 99%. In another attempt [46], different heart rhythms were detected and classified into the VF and non-VF types using six features, four are derived from image-based phase plot analysis, one is derived in the frequency domain, and the last reflects the nonlinear characteristics of a data segment, values of (Acc = 95.3%, Sens = 94.5%, Spe = 94.2%) and (Acc = 90.4%, Sens = 91.6%, Spe = 89.3%) using binary decision tree (BDT) and the SVM, respectively. The algorithm proposed by Tripathy et al. [47], using digital Taylor-Fourier transform (DTFT) features of ECG signals and least square support vector machine (LS-SVM) with linear and radial basis function (RBF) kernels for detection of VF and non-VF arrhythmia episodes, obtained performance values of Acc = 83.75%, Sens = 85.20%, Spe = 82.46%.

Other authors have classified the ECG signal segments into VFVT and non-VFVT. These results are not directly comparable with those in the previous table since they provide a binary output. However, we include them since they are interesting to see how simpler two-class classification still provides similar results to those obtained in this work. Zhou et al. [48] classified the ECG signal segments into the normal sinus rhythm (NSR) or arrhythmic shockable classes VFVT. The classification is based on Time-Delay Transform (TDT) of the signals and a neural network with Weight Fuzzy Membership Functions (NEWFM). They obtained Acc = 89.5%, Sens = 73.6%, and Spe = 93.5%. Xu et al. [49] detected VFVT using boosted classification and regression tree (Boosted-CART) obtaining Acc = 98.29%, Sens = 97.32%, and Spe = 98.95%. Other studies that have also used the class VFVT [1] have evaluated both time domain (e.g., energy, permutation entropy) and frequency domain (e.g., renyi
entropy) features. The classification is done by using a Random Forest (RF) classifier aiming to identify shockable and non-shockable ventricular arrhythmia with CUDB and MITDB databases with results of $\text{Acc} = 97.23\%$, $\text{Sens} = 96.54\%$, $\text{Spe} = 97.97\%$ [50]. Thirteen time-frequency and statistical features were extracted and applied to the C4.5 classifier [51], resulting in $\text{Acc} = 97.02\%$, $\text{Sens} = 90.97\%$, $\text{Spe} = 97.86\%$ for VFVT detection (including ventricular flutter). In Kimmo et al. [52], gaussian processes were used to detect VT, VFL, and VF episodes (all three considered in the same class) extracting 15 metrics obtaining $\text{Acc} = 91\%$, $\text{Sens} = 89\%$, $\text{Spe} = 88\%$.

9. Conclusions

As mentioned above, one of the main causes of sudden death is caused by the VF arrhythmia [3,53]. The rapid and correct detection of VF and VT is of fundamental importance both for the use of an automatic external defibrillator and for monitoring the patient. In order to obtain a reliable algorithm to discriminate between the different arrhythmias, an attempt was made to perform this detection task using the lowest computational load. The methodology uses the ECG to monitor biomedical signals that have different morphological and spectral characteristics.

We propose the analysis of the ECG signal for the real-time detection of the onset of ventricular fibrillation using a time-frequency method [7,54]. Reduction of network interference and other noises, which correspond to high frequency noises in these signals was carried out. After performing the steps above, the data matrix of each TFR is converted to an image (TFRI) corresponding to the different cardiac pathologies of the processed ECG signal, allowing to obtain an appropriate representation capable of providing useful information about the problem to be solved and allowing practical applications to the diagnosis in real time. The novelty of this work lies in the fact of using a reference mark WRM to establish a time-frequency window $t_w$, obtaining a time-frequency representation and its associated image (TFR and TFRI matrices, respectively) which are used as input to a combined classification algorithm without calculation of additional parameters for the classifier. This fact avoids the extraction of characteristics and thus, the loss of relevant information to discriminate between the different classes. Additionally, we propose the use of combined specialized classifiers to improve classification. An analysis of several combination methodologies, and a comparative study between the individual performance of the KNN, ANN, L2RLR, and BAGG algorithms was done. All of these individual and combined classifier algorithms were trained with the cross-validation method and evaluated based on sensitivity, specificity, accuracy, precision, and execution time.

Using the TFRI strategy, we concluded that, using z-5 cross validation, the individual KNN classifier achieves good results retrieving a sensitivity of $94.97 \pm 0.70\%$, a specificity of $99.27 \pm 0.05\%$, an accuracy of $98.47 \pm 0.01\%$, and a precision of $97.09 \pm 0.14\%$ for VF. In case of VT, a sensitivity of $93.47 \pm 0.19\%$, specificity of $99.39 \pm 0.15\%$, accuracy of $98.97 \pm 0.08\%$, and precision of $92.11 \pm 0.7\%$, with a running time $t = 0.17$ s. Using the TFRI strategy with combined classifiers in hierarchical form (HM) achieved a sensitivity of $95.58 \pm 0.40\%$, specificity of $99.31 \pm 0.08\%$, $98.6 \pm 0.04\%$ accuracy, and a precision of $98.25 \pm 0.29\%$ for VF, with a sensitivity of $94.02 \pm 0.58\%$, specificity of $99.31 \pm 0.08\%$, accuracy of $99.14 \pm 0.43\%$, and a precision of $98.59 \pm 0.09\%$ for VT, with execution time between $0.07$ s and $0.12$ s.

Different classifier robustness and classification analysis are performed to validate results: Sensibility, specificity, accuracy, precision, confusion matrices, ROC, AUC, and A-test. All these analyses show that the used methodology is adequate and congruent results are obtained.

Taking into consideration the performed study, we have concluded that the use of combined classifiers is the best way to integrate the information since they provide stronger and efficient estimates than a single classifier. The proposed methodology provides useful information for the detection of VF in real time with a low computational time, discriminating VF from the rest of the cardiac pathologies satisfactorily. This fact significantly improves the possibilities of correct diagnosis of the patient when presenting an episode with any of these arrhythmias.
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