Electronic Structure of Cyanocobalamin: DFT+QMC Study

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Abstract We study the electronic structure and the magnetic correlations of cyanocobalamin (C63H88CoN14O14P) by using the framework of the multi-orbital single-impurity Haldane-Anderson model of a transition metal impurity in a semiconductor host. Here, we first determine the parameters of the Anderson Hamiltonian by performing density functional theory (DFT) calculations. Then, we use the quantum Monte Carlo (QMC) technique to obtain the electronic structure and the magnetic correlation functions for this effective model. We find that new electronic states, which correspond to impurity bound states, form above the lowest unoccupied level of the host semiconductor. These new states derive from the atomic orbitals at the cobalt site and the rest of the molecule. We observe that magnetic moments develop at the Co(3dν) orbitals and over the surrounding sites. We also observe that antiferromagnetic correlations exist between the Co(3dν) orbitals and the surrounding atoms. These antiferromagnetic correlations depend on the filling of the impurity bound states.

Keywords Vitamin B12 · Metalloenzymes · Anderson model · Transition-metal impurity in semiconductors

1 Introduction

Vitamin B12 is a very important organometallic molecule for biological systems [1–3]. In this paper, we study the electronic structure of cyanocobalamin (CNCbl) which is a form of vitamin B12. In Fig. 1, we illustrate the molecular structure of CNCbl. The cobalt atom neighbors five nitrogen atoms, of which four are located in the corrin ring. The CN ligand is also attached to Co, making the rare cobalt-carbon bonding. The charge neutral CNCbl molecule has 718 electrons. For this molecule, the HOMO (highest occupied molecular orbital) and the LUMO (lowest unoccupied molecular orbital) levels are separated by an energy gap of ≈ 2.2 eV [4]. The photoabsorption spectrum of CNCbl exhibits distinct peaks at ≈ 3.5 and 4.5 eV, of which origin remains elusive [4]. In addition, it is known that CNCbl has a weak diamagnetic response [5, 6].

Despite many years of research, there remains questions about the electronic structure and the functioning of vitamin B12 as well as the role of the transition-metal cobalt atom. In this paper, we study the electronic structure of CNCbl from the perspective of many body physics. In particular, we use the combined density functional theory (DFT) and quantum Monte Carlo (QMC) approach to study the electronic structure and magnetic correlations of this molecule within the framework of the Haldane-Anderson model [7]. This model was initially introduced to describe the electronic state of Au in a semiconductor Ge host. Here, we use the Haldane-Anderson model because CNCbl exhibits a semiconductor energy gap and contains the transition-metal cobalt atom.

In the combined DFT+QMC approach, we first determine the parameters of the Anderson Hamiltonian [8] by
We observe that magnetic moments develop at the Co(3d) to the discrete single-particle spectrum of the molecule. These antiferromagnetic correlations between these host magnetic moments develop above the LUMO level for CNCbl instead of in Section 3. Here, we find that impurity bound states electronic structure and the magnetic correlation functions can be expanded in terms of the NAO's in the Anderson Hamiltonian. We present the QMC data on the DFT calculations carried out with the Gaussian program [9]. Then, we study this effective Anderson Hamiltonian by performing QMC simulations with the Hirsch-Fye [10] algorithm. In our calculations, we use an orbital independent intra-orbital Coulomb interaction $U$ at the Co(3d$\nu$) orbitals and we neglect the inter-orbital Coulomb interactions along with the Hund’s coupling. We take the value of $U$ to be 4 eV. In addition, the Co(3d$\nu$) energy levels are shifted in order to prevent the double counting of the local Coulomb interactions by both DFT and QMC.

The outline of this paper is as follows. In Section 2, we obtain the one-electron parameters of the effective Anderson Hamiltonian. We present the QMC data on the electronic structure and the magnetic correlation functions in Section 3. Here, we find that impurity bound states develop above the LUMO level for CNCbl instead of being inside the semiconducting energy gap. This is due to the discrete single-particle spectrum of the molecule. We observe that magnetic moments develop at the Co(3d$\nu$) orbitals and at the host states which have the strongest hybridization. We also observe that there are antiferromagnetic correlations between these host magnetic moments and the Co(3d$\nu$) moments. These antiferromagnetic correlations disappear when the impurity bound states are filled. We note that in Ref. [11], we combined the Hartree-Fock (HF) approximation with the QMC technique to study CNCbl. In the HF+QMC calculations, we used only the smaller imidazole part of the CNCbl instead of the whole molecule. In Section 4, we compare the HF+QMC results on Im-[Co$^{3+}$H$_{68}$CoN$_{14}$O$_{12}$P], with the DFT+QMC results on CNCbl. Section 5 gives the summary and conclusions of the paper.

The multi-orbital single-impurity Anderson Hamiltonian [8] is given by

$$H = \sum_{m,\sigma}(\epsilon_m - \mu)c_{m\sigma}c_{m\sigma}^\dagger + \sum_{\nu,\sigma}(\epsilon_{\nu\sigma} - \mu)d_{\nu\sigma}^\dagger d_{\nu\sigma}^\dagger + \sum_{m,\nu,\sigma}(V_{mn\nu}c_{m\sigma}^\dagger d_{\nu\sigma} + V_{mn\nu}^* c_{m\sigma} d_{\nu\sigma}^\dagger)$$

(1)

where $c_{m\sigma}$ ($c_{m\sigma}^\dagger$) creates (annihilates) an electron in host state $m$ with spin $\sigma$, $d_{\nu\sigma}^\dagger$ ($d_{\nu\sigma}^\dagger$) is the creation (annihilation) operator for a localized electron with spin $\sigma$ at the Co(3d$\nu$) orbital, and $n_{\nu\sigma} = d_{\nu\sigma}^\dagger d_{\nu\sigma}$. Here, $\epsilon_m$ and $\epsilon_{\nu\sigma}$ are the energies of the host and the Co(3d$\nu$) impurity states, respectively. The hybridization matrix element between these states is $V_{mn\nu}$. The intra-orbital Coulomb repulsion is $U_{\nu\nu}$. Finally, a chemical potential $\mu$ is introduced since the QMC calculations are performed in the grand canonical ensemble.

We obtain the one-electron parameters $\epsilon_m$, $\epsilon_{\nu\sigma}$ and $V_{mn\nu}$ as explained below. Within DFT, the one-electron wave function $\psi_n(r)$ are determined from

$$F(r)\psi_n(r) = E_n \psi_n(r),$$

(2)

where the Kohn-Sham operator [12] is

$$F(r) = \left(-\frac{\hbar^2}{2m_e} \nabla^2 + V_{ext}(r) + \int d^3r' \frac{\rho(r')}{|r-r'|} + V_{xc}(r)\right)$$

(3)

and the molecular orbital energy is $E_n$. The molecular orbitals $|\psi_n\rangle$ can be expanded in terms of the $N$ atomic orbitals $|\phi_i\rangle$,

$$|\psi_n\rangle = \sum_i C_{ni} |\phi_i\rangle,$$

(4)

where $C_{ni}$ are the elements of the coefficient matrix $C$. Substituting (4) in (2), the Roothan equation, $\mathbf{CF} = E\mathbf{CS}$, is obtained. Here, the elements of the Kohn-Sham matrix $\mathbf{F}$ are defined as

$$F_{ij} = \int d^3r \phi_i^*(r) F(r) \phi_j(r)$$

(5)

and the overlap matrix $\mathbf{S}$ has the matrix elements $S_{ij} = \langle \phi_i | \phi_j \rangle$. Because the atomic orbitals do not form an orthogonal basis, we use the natural atomic orbitals (NAO’s) [13] which form an orthogonal basis. The NAO’s form a maximally localized basis set. Next, we express the Kohn-Sham matrix in the NAO basis. We take the Co(3d$\nu$) NAO’s as the impurity orbitals and their energy levels as $\epsilon_{d\nu}$’s in the Anderson Hamiltonian. Diagonalizing the remaining part of...
the Kohn-Sham matrix, we obtain the host eigenstates $|\mu_m\rangle$ and their energy levels $\tilde{\varepsilon}_m$ in addition to the hybridization matrix elements $V_{m\nu}$. This procedure is explained in more detail in Ref. [11]. We use the Gaussian program [9] with the BP86 energy functional [14, 15] and the 6-31G basis set with $N = 1035$ basis functions to obtain the DFT solutions.

In the QMC calculations, we use $U = 4$ eV. In various Co compounds, the intra-orbital Coulomb interaction at the Co(3$d$) orbitals is estimated to be between 4 eV and 5 eV [16]. It is important to note that, in the DFT+QMC approach, the on-site Coulomb interaction $U$ is taken into account both by the DFT and the QMC calculations. Therefore, in order to prevent this double counting, an orbital-dependent double-counting term $\mu_{\nu}^{DC}$, which is defined as

$$\mu_{\nu}^{DC} = \frac{U \langle n_{d\nu}^{DFT}\rangle}{2}$$

is subtracted from the bare Co(3$d$) levels, $\varepsilon_{d\nu} \rightarrow \tilde{\varepsilon}_{d\nu} = \varepsilon_{d\nu} - \mu_{\nu}^{DC}$ [17–20]. In the Anderson Hamiltonian, $\tilde{\varepsilon}_{d\nu}$ is used instead of $\varepsilon_{d\nu}$. Here, $\langle n_{d\nu}^{DFT}\rangle$ is the electron number in the Co(3$d$) NAO's obtained by the DFT calculations.

We begin presenting data by showing the density of states $D(\varepsilon) = \sum_{\nu=1}^{N} \delta(\varepsilon - E_{\nu})$ in Fig. 2a. In this figure, the highest occupied molecular orbital (HOMO) is located at $-4.9$ eV, and the lowest unoccupied molecular orbital (LUMO) is located at $-3.2$ eV, which means that the energy gap is $1.7$ eV. In Fig. 2b, the host density of states $D_h(\varepsilon) = \sum_{m=1}^{N} \delta(\varepsilon - \varepsilon_m)$ is shown as a function of energy $\varepsilon$. In this figure, vertical lines indicate the shifted Co(3$d$) NAO energy levels $\tilde{\varepsilon}_{d\nu}$. For these parameters, while the $\nu = x^2 - y^2$ NAO is located at $\varepsilon \approx -9.5$ eV, the $\nu = yz$, $xz$ and $3z^2 - r^2$ NAO's are located at $\varepsilon \approx -8.5$ eV and the $\nu = xy$ NAO is located at $\varepsilon \approx -7.5$ eV. We note that here, we choose a coordinate system in which the $x$- and $y$-axis are located at 45 degrees to the Co-N bond direction instead of being parallel.

The DFT data on the square of the hybridization matrix elements $|V_{m\nu}|^2$ between the $m$'th host eigenstate $|\mu_m\rangle$ and the Co(3$d$) NAO's are shown as a function of $\varepsilon_m$ in Fig. 3. Here, we observe that the $m = 336, 337$ and 340 host states have the largest hybridization matrix elements. The $m = 336$ and 337 host states hybridize most strongly with the Co(3$d_{xy}$) NAO, while, the $m = 340$ host state has the strongest hybridization with the Co(3$d_{3z^2-r^2}$) and Co(3$d_{xz}$) NAO’s. In the QMC data, we will see that these host states are strongly influenced by the local Coulomb interaction.

In order to gain insight into these host states, in Fig. 4, we illustrate the $m = 336, 337$ and 340 host states in terms of the NAO's. These host states contain contributions from NAO's around the Co site. In particular, the $m = 340$'th host state contains significant amount of weight from the CN ligand.

### 3 Quantum Monte Carlo Results

In this section, QMC data on the effective Haldane-Anderson model for CNCbl are presented. For this model, QMC calculations were performed by using the Hirsch-Fye QMC algorithm [10]. In the QMC calculations, a discrete Matsubara time step of $\Delta \tau = 0.13$ eV$^{-1}$ is used. The results are presented for temperature $T = 700$ K in the grand canonical ensemble.

Figure 5a shows the electron occupation number $\langle n_{\nu}\rangle = \sum_{\nu} \langle d_{\nu}\rangle$ for the Co(3$d$) NAO states as a function of the chemical potential $\mu$. In Fig. 5a, we see that $\langle n_{\nu}\rangle$ becomes finite at $\mu \approx -12$ eV, and the Co(3$d$) NAO's...
Fig. 3  (Color online) DFT results on the square of the hybridization matrix elements $|V_{m\nu}|^2$ between the Co(3d$_\nu$) natural atomic orbitals and the $m$'th host states versus the host energy $\varepsilon_m$. In a, results are shown for the 3$d_{3z^2-r^2}$ and 3$d_{xy}$ natural atomic orbitals, and in b for the 3$d_{xz}$, 3$d_{x^2-y^2}$, and 3$d_{yz}$ natural atomic orbitals. Here, the vertical solid and dashed lines denote the values of the HOMO and LUMO levels, respectively. We observe that $m = 336, 337$, and 340th host states have the strongest hybridization matrix elements

become singly occupied at $\mu \approx -6.5$ eV. At $\mu \approx -5.5$ eV, the Co(3$d_{3z^2-r^2}$) NAO becomes doubly occupied. At the HOMO level, the Co(3$d_{xy}$) NAO is singly occupied, while the remaining orbitals have occupation number near 1.4. Between the HOMO and LUMO levels, the Co(3$d_{\nu}$) occupations do not change. The occupation of the Co(3$d_{xy}$) NAO exhibits a sudden increase at $\mu \approx -2.5$ eV by about 0.3 electrons. We think that this sudden increase corresponds to an impurity bound state located at this energy. When $\mu$ reaches $-1.0$ eV, all of the Co(3$d_{\nu}$) orbitals become doubly occupied.

An interesting observation in Fig. 5a is that the impurity bound states are not induced in the semiconducting energy gap between the HOMO and LUMO levels. They are located above the LUMO level between $-3.0$ and $-2.0$ eV. Now, as seen in Fig. 2, the main features of the host density of states $D_h(\varepsilon)$ consist of a continuous conduction band located below $\approx -5$ eV, two discrete states located at $-3.3$ and $-2.6$ eV, and a continuum of valence band states above $-2.0$ eV. In Fig. 5a, we observe that the new impurity bound states are induced right below the continuum of valence band states located above $-2.0$ eV. The impurity bound states are located above the LUMO level because the spectrum of the host states is discrete around the LUMO level.

Figure 5b shows the square of the magnetic moment at the Co(3$d_{\nu}$) NAO’s, $\langle (M^{z\nu}_\beta)^2 \rangle$, where $M^{z\nu}_\beta = d_{\beta\uparrow}^\dagger d_{\nu\uparrow} - d_{\beta\downarrow}^\dagger d_{\nu\downarrow}$, as a function of $\mu$. We observe that the magnetic moments of the Co(3$d_{\nu}$) NAO’s increase continuously, as $\mu$ is increased up to $\mu \approx -6.5$ eV. The magnetic moment of the Co(3$d_{3z^2-r^2}$) NAO decreases rapidly at $\mu \approx -5.5$ eV due to double occupancy. For $\nu = 3z^2 - r^2, xz$ and
Electron occupation number $\langle n_{\nu} \rangle$ of the Co(3d$_{\nu}$) natural atomic orbitals versus the chemical potential $\mu$.

Square of magnetic moment $\langle (M_{z\nu})^2 \rangle$ for Co(3d$_{\nu}$) natural atomic orbitals versus the chemical potential $\mu$. Here, the vertical solid and dashed lines denote the values of the HOMO and LUMO levels, respectively. These results are for $U = 4$ eV.

Square of magnetic moment $\langle (M_{z\nu})^2 \rangle$ versus the chemical potential $\mu$. Here, the vertical solid and dashed lines denote the values of the HOMO and LUMO levels, respectively. These results are for $U = 4$ eV.

In Fig. 6a, we present QMC data on the total electron occupation of the Co(3d$_{\nu}$) NAO’s $\langle n_{d} \rangle = \sum_{\nu=1}^{5} \sum_{\sigma} \langle d_{\nu\sigma}^{\dagger} d_{\nu\sigma} \rangle$ as a function of $\mu$. We see that $\langle n_{d} \rangle$ increases up to HOMO level, it equals 7.2 at $\mu \approx -4.8$ eV. We observe that $\langle n_{d} \rangle$ does not change between the HOMO and LUMO levels. The total number of the host electrons $\langle n_{h} \rangle = \sum_{m=1}^{N_{h}=336} \sum_{\sigma} \langle c_{m\sigma}^{\dagger} c_{m\sigma} \rangle$ is shown in Fig. 6b. Figure 6c shows the total electron number for CNCbl $\langle n_{T} \rangle = \langle n_{d} \rangle + \langle n_{h} \rangle$ versus $\mu$. Here, we clearly see that between the HOMO and LUMO levels the total electron number $\langle n_{T} \rangle = 718$ corresponding to the neutral CNCbl molecule.

In Fig. 7a, we present QMC data on the host electron number $\langle n_{m} \rangle = \sum_{\sigma} \langle c_{m\sigma}^{\dagger} c_{m\sigma} \rangle$ versus $\mu$ for the $m = 336, 337, 340$ host eigenstates. The bare energy levels $\epsilon_{m}$ of these states are located at $-6.48, -6.43$, and $-6.16$ eV for $m = 336, 337, 340$, respectively. Here, we observe that these host states do not become doubly occupied as $\mu$ passes through the $\epsilon_{m}$ s. For example, at the HOMO level, $\langle n_{m} \rangle = 1.72, 1.67, and 1.52$ for $m = 336, 337, and 340$, respectively, even though they are located deep below the HOMO level. Consequently, these host states have finite magnetic moments when $\mu$ is at the HOMO level as seen in Fig. 7b. The magnetic moments...
vanish after these host states become doubly occupied for \( \mu \gtrsim -1 \text{ eV} \).

Next, in Fig. 8a–c, we present QMC data on the magnetic correlation function \( \langle M^z_\nu M^z_m \rangle \) between the magnetic moments at the Co(3d\_\nu) NAO's and the \( m \)'th host states for \( m = 336, 337, \) and 340. These figures show that the host states with the strongest hybridization have antiferromagnetic correlations with the moments at the Co(3d\_\nu) NAO's. These antiferromagnetic correlations vanish as the host states become doubly occupied.

### 4 Comparison of the HF+QMC and the DFT+QMC Results

In Ref. [11], numerical results were presented from previous HF+QMC calculations on Im-[Co\textsuperscript{III}(corrin)]-CN\textsuperscript{+}, which is a smaller piece of the CNCbl molecule. Here, we compare those results with the current DFT+QMC data obtained for the whole CNCbl molecule.

We find various differences between the outcomes of the HF and DFT calculations. In the HF method, non-interacting electrons are described under the influence of a mean field potential which consists of the classical Coulomb potential and a non-local exchange potential. On the other hand, in the DFT calculations, a local exchange potential is used [21]. Furthermore, in the HF+QMC approach, the intra-orbital Coulomb interaction was assumed to be unscreened and the bare Coulomb matrix elements were used. For cobalt, the intra-orbital \( U \) was taken to be about 36 eV. On the other hand, in the DFT+QMC approach, the intra-orbital Coulomb interaction is assumed to be renormalized due to long-range screening effects. Here, \( U \) was taken to be 4 eV.
In the HF calculations, the locations of the Co(3d\_xy) NAO’s separate into two groups corresponding to the e_g and t_2g symmetries. In the HF+QMC calculations, we have used a constant energy shift \( \mu^{DC} \) to compensate for the double counting of \( U \). The resultant QMC data reflect this ordering of the Co(3d\_xy) NAO’s. However, the DFT calculations yield nearly degenerate Co(3d\_xy) NAO’s. In the DFT+QMC approach, we have used an orbital-dependent \( \mu^{\nu}_{DC} \) which led to the ordering of the Co(3d\_xy) NAO’s seen in Fig. 2b. We find that there are some differences in the locations of the shifted Co(3d\_xy) NAO’s where we compare the HF and DFT results. These differences clearly influence the outcome of the QMC calculations. Nevertheless, we observe that impurity bound states involving the Co(3d\_xy) and Co(3d\_z^2\_r^2) NAO’s are found in both the HF+QMC and DFT+QMC calculations. In both cases, the impurity bound state for the Co(3d\_z^2\_r^2) NAO is located higher in energy compared to that of the Co(3d\_xy).

5 Summary and Conclusions

In summary, we have studied the electronic structure and magnetic correlations of cyanocobalamin. For this purpose, we have used the multi-orbital single-impurity Haldane-Anderson model of a transition metal impurity embedded in a semiconductor host. First, we have constructed an effective Haldane-Anderson model by using DFT calculations. We have obtained the one-electron parameters of this model from the Kohn-Sham matrix written in the basis of the natural atomic orbitals. We have taken \( U = 4 \text{ eV} \) and have shifted the Co(3d\_xy) levels by \( \mu^{\nu}_{DC} \) to prevent the double-counting of the intra-orbital Coulomb interaction by both DFT and QMC.

The QMC results clearly show how the single-electron spectral weight is distributed in energy. In our calculations, we see that as the chemical potential increases, the Co(3d\_xy) NAO’s become occupied. When the chemical potential reaches the HOMO level, the total electron number equals 718. This corresponds to the neutral CNCbl molecule. In this case, the Co(3d\_xy) NAO’s are less than doubly occupied, and they have finite magnetic moments. Between the HOMO and LUMO levels, there is no single-particle spectral weight. We observe that above the LUMO level and between \(-3.0 \text{ and } -2.0 \text{ eV}\), there are new states induced by the Coulomb interaction \( U \). We identify these new states as impurity bound states because of the filling dependence of the antiferromagnetic correlations between the Co(3d\_xy) NAO’s and the host magnetic moments. This identification is similar to that done previously in the analysis of the HF+QMC results presented in Ref. [11]. The impurity bound state is most clearly seen for the Co(3d\_xy) NAO. Surprisingly according to the DFT+QMC result, the impurity bound states are located above the LUMO level instead of being in the semiconducting energy gap. We think that this is because of the discrete energy spectrum of the CNCbl molecule.

It remains to be seen whether the impurity bound states found in the DFT+QMC calculations are related to the peaks observed in the photoabsorption spectrum of CNCbl. For a more direct comparison with the experimental data, it would be necessary to include the inter-orbital Coulomb interactions along with the Hund’s coupling. We note that we have performed similar DFT+QMC calculations for hemoglobin, where we also find impurity bound states. Hence, these correlated electronic states appear to be a common feature of metalloproteins and metalloenzymes. We think that it will be interesting to figure out whether the impurity bound states have a general role in the functioning of metalloproteins and metalloenzymes.

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