Bandgap Correction and Spin-Orbit Coupling Induced Absorption Spectra of Dimethylammonium Lead Iodide for Solar Cell Absorber

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The search for stable and highly efficient solar cell absorbers has revealed interesting materials; however, the ideal solar cell absorber is yet to be discovered. This research aims to explore the potentials of dimethylammonium lead iodide (CH₃NH₂CH₃PbI₃) as an efficient solar cell absorber. (CH₃NH₂CH₃PbI₃) was modeled from the ideal organic–inorganic perovskite cubic crystal structure and optimized to its ground state. Considering the spin-orbit coupling (SOC) effects on heavy metals, the electronic band structure and bandgaps were calculated using the density functional theory (DFT). In contrast, bandgap correction was achieved by using the GW quasiparticle methods of the many-body perturbation theory. The optical absorption spectra were calculated from the real and imaginary dielectric tensors, which are determined by solving the Bethe–Salpeter equations of the many-body perturbation theory. Spin-orbit coupling induces band splitting and bandgap reduction in both DFT and GW methods, while the GW method improves the DFT bandgap. We report a DFT band gap of 1.55 eV, while the effect of spin-orbit coupling reduces the bandgap to 0.50 eV. Similarly, the self-consistent GW quasiparticle method recorded a bandgap of 2.27 eV, while the effect of spin-orbit coupling on the self-consistent GW quasiparticle method reported a bandgap of 1.20 eV. The projected density of states result reveals that (CH₃NH₂CH₃PbI₃) does not participate in bands around the gap, with the iodine (I) p orbital and the lead (Pb) p orbital showing most prominence in the valence band and the conduction band. The absorption coefficient reaches 10⁶ in the ultraviolet, visible, and near-infrared regions, which is higher than the absorption coefficient of CH₃NH₃PbI₃. The spectroscopic limited maximum efficiency predicts a high maximum efficiency of about 62% at room temperature and an absorber thickness of about 10⁻¹ to 10² μm, suggesting that (CH₃NH₂CH₃PbI₃) has an outstanding prospect as a solar cell absorber.

Keywords: spin-orbit coupling, GW quasiparticle method, absorption spectra, perovskites, solar cell
1 INTRODUCTION

The ability to explore materials for different technological applications allows us to improve the efficiency of various materials. Amongst these applications, materials are engineered to have a high figure of merits for viable thermoelectric generators (He et al., 2015; Ademabolo et al., 2021; Jouhara et al., 2021), which can efficiently convert heat energy to electricity. Similarly, material engineering has the potential of discovering catalysts (Zhao et al., 2021a; Wang et al., 2021b) with reduced activation barriers and improved reaction rates. For solar cell applications, materials could be engineered to scale up the power conversion efficiency. In all of these applications, the stability of these materials at varying temperatures, humidity, and other environmental conditions needs to be improved to withstand varying environmental conditions and enhance longevity (Aftab and Ahmad, 2021; Baranowska-Korcycz et al., 2021; Cha and Wu, 2021). For decades, a lot of success has been achieved from experimental and theoretical research in power generation from solar cells. Among these successes is the increased power conversion efficiency, from 4% to a maximum efficiency of 38.9% (Mancini et al., 2016; Akman et al., 2021; Zhao et al., 2021b; Zhang et al., 2021). A fascinating family of materials that plays a significant role in the increase of solar cell efficiency is the perovskite material (Park, 2016; Akman et al., 2021; Zhao et al., 2021a; Zhang et al., 2021). Alongside perovskites’ increased power conversion efficiency, inorganic and hybrid perovskites with a general formula, ABX₃, have hundreds of thousands of members as the A and B sites are filled with monovalent and divalent cations, while the X site is filled with either oxides or halides, allowing experimental and computational screening of potentials materials for solar cell absorbers and other technological applications. The success of perovskite materials is primarily attributed to the high carrier mobility, strong broadband absorption, long electron-hole diffusion length, design flexibility, and bandgap tunability of the absorbing materials (Kojima et al., 2009; Stoumpos et al., 2013; Snaith et al., 2014; Yin et al., 2014; Christians et al., 2015; Snaith and Hacke, 2018). Bandgap engineering is a well-demonstrated approach for modulating the power conversion efficiency of hybrid perovskites by substituting the X site element with other halides to form a mixed halide alloy (Hao et al., 2014; Ogomi et al., 2014; Mancini et al., 2015). Conversely, altering the A-site composition in a stoichiometric approach enhances the bandgap (Eperon et al., 2014). However, efforts to replace the A site in the ABX₃ perovskite compound (Im et al., 2012; Stoumpos et al., 2015) have served as a playground for further insights into the search for highly efficient perovskite materials. Lately, the quest for a stable and more efficient solar cell absorber has birthed the use of (CH₃)₂NH₂⁺ in the A site of ABX₃ perovskite compounds. At room temperature, CH₃NH₂CH₃PbI₃ crystallizes into a hexagonal crystal structure with space group P6₃/mmc. Furthermore, at 250K, it changes into the monoclinic crystal structure with space group P2₁/c due to first-order phase transition (García-Fernández et al., 2017). Similarly, previous experimental studies of dimethylammonium lead iodide (CH₃NH₂CH₃PbI₃) reported the room temperature phase with the hexagonal crystal structure having space group P6₃/mmc and lattice parameters a = 8.769 Å and b = 8.188 Å (Mancini et al., 2016). The hexagonal-structured (CH₃)₂NH₂PbI₃ reported an optical bandgap of 2.39 eV and 2.59, calculated by extrapolating the linear part of the Kubelka–Munk function (Mancini et al., 2016; García-Fernández et al., 2017). Percentage doping of the (CH₃)₂NH₂⁺ cation with cesium atoms (Cs) in the A site to form CsₓDMA1₋ₓPbI₃ thin-film yields a power conversion efficiency of up to 16.6% (Wang et al., 2019). Similarly, doping CsPbI₃ with up to 25% (CH₃)₂NH₂⁺ results in improved stability, although (CH₃NH₂CH₃)ₓ₋₁CsₓPbI₃ has a lower bandgap than the parent compound (CsPbI₃) (Marshall et al., 2021). Also, doping (CH₃NH₂CH₃)⁺ with Cs⁺ in the A site causes octahedra tilt, which induces bandgap increment and improves the resulting perovskite solar cell stability (Eperon et al., 2020). To improve stability and preserve power conversion efficiency, (CH₃)₂NH₂⁺ is partially substituted in the A site of CH₃NH₂PbI₃, changing the tetragonal crystal structure to a cubic structure when exposed to humidity, further exposure to humidity resulting in phase change into a hexagonal structure (Thomas et al., 2021). The spectroscopic limited maximum efficiency (SLME) is aimed at screening materials based on their intrinsic properties such as the bandgap, the absorption spectra, and the non-radiative combination loss (Yu and Zunger, 2012). Unlike the bandgap-dependent Shockley–Queisser efficiency limit (Shockley and Queisser, 1961), which predicted a maximum efficiency of 33.7% at the best bandgap of 1.34 eV, the spectroscopic limited maximum efficiency varies for materials with the same bandgap depending on the optical type of the bandgap (direct allowed, direct forbidden, and indirect allowed) and the absorption coefficient (Yu and Zunger, 2012). CuInSe₂, CuGaSe₂, and CuInS₂ with a high spectroscopic limited maximum efficiency of about 28% are found experimentally to be good absorbers, showing that the SLME is an excellent criterion to select good potential photovoltaic absorbers (Yu and Zunger, 2012). In this study, we present the electronic structure and the optical absorption spectra of the high-temperature cubic crystal structure of (CH₃NH₂CH₃PbI₃) with and without the effect of spin-orbit coupling. The density functional theory (Hohenberg and Kohn, 1964; Kohn and Sham, 1965) and the GW quasiparticle method (Marini et al., 2009; Sangalli et al., 2019; Rangel et al., 2020) were used to calculate the electronic structure, while the Bethe–Salpeter equation method of the many-body perturbation theory (Marini et al., 2009; Sangalli et al., 2019; Rangel et al., 2020) was used for the optical absorption spectra.

2 COMPUTATIONAL PROCEDURE

The CH₃NH₂CH₃PbI₃ structure was modeled after the ideal cubic perovskite structure, where the lead (Pb) atom occupies the (0, 0, 0) position, the iodine (I) atoms occupy the (0.5, 0.0, 0.0), (0.0, 0.5, 0.0), and (0.0, 0.0, 0.5) positions in units of lattice vectors, while the dimethylammonium cation (CH₃NH₂CH₃)⁺ was placed in the middle of the cubic cage at (0.5, 0.5, 0.5).
The final structure is such that the NH$_2$ points toward the upper part of the cubic cage, while the two CH$_3$ arms point downward toward the sides of the cubic cage. In order to describe the dispersion forces, energy, and structure of the system accurately (Barone et al., 2009), the van der Waals interaction between the dimethylammonium molecule and the cubic cage was treated with the grimme-d2 semiempirical van der Waals correction (Grimme, 2006; Barone et al., 2009). The stable crystal structure of (CH$_3$)$_2$NH$_2$PbI$_3$ was achieved by optimizing the cut-off for the wavefunction to 115 Ry, and then kpoint optimization shows that the 16 $\times$ 16 $\times$ 16 Monkhorst–Pack kpoint mesh (Monkhorst and Pack, 1976) is sufficient to describe the system, while at minimum energy, a lattice parameter of 6.20 Å was achieved. The most stable pseudo-cubic structure is achieved using the Broyden–Fletcher–Goldfarb–Shannon quasirelativistic functional (Shanno, 1970), which relaxed the position of atoms and the size of the lattice. The density functional theory (Hohenberg and Kohn, 1964; Kohn and Sham, 1965) and the GW quasiparticle (Marini et al., 2009; Sangalli et al., 2019; Rangel et al., 2020) band structure were performed using the Perdew–Burke–Enzenhoff (Perdew et al., 1992; Perdew et al., 2008) exchange-correlation functional of the generalized gradient approximation (Perdew and Yue, 1986; Perdew et al., 1996) as implemented in the quantum espresso package (Scandolo et al., 2005; Giannozzi et al., 2009). The band structures are calculated along the Gamma (0.00, 0.00, 0.00); X (0.00, 0.50, 0.00); M (0.50, 0.50, 0.00); G (0.0, 0.0, 0.0); R (0.50, 0.50, 0.50); and X (0.00, 0.50, 0.00) high symmetry points, while the projected density of states was calculated using the tetrahedra method (Blochl et al., 1994). A denser Monkhorst–Pack kpoint mesh of 20 $\times$ 20 $\times$ 20 and 12 $\times$ 12 $\times$ 12 was used to calculate the density of states in the non-spin-orbit calculation and the spin-orbit calculations, respectively (Monkhorst and Pack, 1976). The non-spin-orbit and the spin-orbit coupling–based calculations (lattice optimizations, variable cell relaxation, electronic band structures, density of states, and optical absorption spectra) were carried out using the norm-conserving Troullier–Martins (Troullier and Martins, 1991a; Troullier and Martins, 1991b) scalar relativistic pseudopotentials (Pb.pbe-n-nc.UPF, I.pbe-n-nc.UPF, C.pbe-n-nc.UPF, H.pbe-n-nc.UPF, and N.pbe-n-nc.UPF) and the fully relativistic pseudopotentials (Pb.rel-pbe-n-nc.UPF, I.rel-pbe-n-nc.UPF, C.rel-pbe-n-nc.UPF, H.rel-pbe-n-nc.UPF, and N.rel-pbe-n-nc.UPF) (Hamann et al., 1979; Kresse and Hafner, 1994; Dal Corso, 2014) (Hamann et al., 1979; Kresse and Hafner, 1994; Dal Corso, 2014), respectively. For both non-spin-orbit and spin-orbit coupling GW band structures, the ground state calculation was carried out using a 6 $\times$ 6 $\times$ 6 Monkhorst–Pack kpoint grid and a cut-off for a wavefunction of 30 Ry, and the number of Gvectors in the exchange term was optimized to 40 Ry and 30 Ry for non-spin-orbit coupling and spin-orbit coupling–based calculations, respectively. In comparison, the number of Gvector blocks in the dielectric constant was optimized to 5 Ry and 6 Ry for non-spin–orbit coupling and spin-orbit coupling–based calculations. The number of bands in the independent response function was optimized as 90 bands and 100 bands for non-spin–orbit coupling and spin-orbit coupling–based calculations. The GW band structures were calculated with six (6) empty and six (6) filled bands for non–spin-orbit coupling–based calculations, while seven (7) empty and seven (7) filled bands were used for the spin–orbit coupling–based calculations as implemented in the YAMBO code (Marini et al., 2009; Sangalli et al., 2019; Rangel et al., 2020). The Bethe–Salpeter equation optical properties were carried out with the 4 $\times$ 4 $\times$ 4 and 6 $\times$ 6 $\times$ 6 Monkhorst–Pack kpoint grid to determine the effect of kpoint optimization on the optical absorption spectra. The macroscopic dielectric matrix was calculated with eight (8) occupied and seventeen (17) unoccupied bands for the non–spin–orbit coupling calculation and fourteen (14) unoccupied and ten (10) occupied bands for spin-orbit coupling–based calculations as implemented in the YAMBO code (Marini et al., 2009; Sangalli et al., 2019; Rangel et al., 2020). Furthermore, the absorption and extinction coefficients, transmittance, reflectivity, refractive index, and absorbance were calculated from the real and imaginary parts of the dielectric tensor. We also determine the spectroscopy limited maximum efficiency, which could screen potential photovoltaic absorbers based on intrinsic properties such as absorption coefficient, temperature, direct and indirect allowed gap, and thickness of the absorber (Yu and Zunger, 2012).
At the same time, the dimethylammonium ion \((\text{CH}_3\text{NH}_2\text{CH}_3)^+\) is optimized such that the amino group \((\text{H-N-H})\) and the methyl group \((\text{H-C-H}_2)\) have a bond angle of 109.40 and 109.50, respectively. Thus, the H-N and H-C bond length is reported as 1.15 Å and 1.18 Å, similar to the experimental study of (Andrew E R and Canepa, 1969-1972), which reported the H-N and H-C bond length of 1.02 Å and 1.10 Å with a tetrahedra bond angle for the amino group \((\text{H-N-H})\) and the methyl group \((\text{H-C-H}_2)\).

In this study, the \(\text{CH}_3\text{NH}_2\text{CH}_3\text{PbI}_3\) crystal displayed in Figure 1 is optimized such that the lattice size and the atomic positions are at the ground state. The variation in the lattice parameter reported in this study and in the work of Kim et al. (Kim et al., 2017), shown in Table 1, is within about 5% agreement with the theoretical study of Kim et al. (2017); this slight variation could be a result of lattice size and atomic position being in a local minimum and the difference in the Perdew–Burke–Enzenhoff exchange-correlation functional used in this study and the refitted Perdew–Wang 86 exchange-correlation functional used by Kim et al. (2017) and Shastri and Pandey (2018). However, the slight difference in the lattice parameter tends to affect the bandgap, magnetic properties, and other superconducting properties (Bagayoko and Callaway, 1983; Wang et al., 1996; Kim et al., 2017).

### 3.2 Electronic Structure

The density functional theory band structure has its maximum valence band and its minimum conduction band at the R high symmetry point, resulting in a direct bandgap of 1.55 eV as shown in Figure 2. The DFT band structure calculated without spin-orbit coupling shows a dense band around 2 eV along the \(\Gamma\)-\(X\)-\(M\)-\(\Gamma\)-\(R\)-\(X\) high symmetry point in the valence band, but less dense bands were noticed along the \(\Gamma\)-\(X\)-\(M\)-\(\Gamma\)-\(R\)-\(X\) high symmetry point in the conduction band, as shown in Figure 2. The density of states calculated without spin-orbit coupling shows a similar amount of available states, which results in sharp peaks around the 2 eV of the valence band, while smaller peaks that result from fewer states and relate to fewer bands in the band structure are reported in the total density of states. The projected density of states indicates that the iodine (I) p orbital is most responsible in the valence band, while the lead (Pb) p orbital shows dominance in the conduction band, which is in agreement with previous studies (Crespo, 2019; Agbaoye et al., 2020; Agbaoye et al., 2021). Hybridization of other orbitals accounts for the other available states as reported for the non-spin-orbit coupling- and the spin-orbit coupling–based density of states. The dimethylammonium cation does not

### Table 1 | Lattice parameters of pseudo-cubic \(\text{CH}_3\text{NH}_2\text{CH}_3\text{PbI}_3\).

|          | \(a(\text{Å})\) | \(b(\text{Å})\) | \(c(\text{Å})\) | \(\alpha(°)\) | \(\beta(°)\) | \(\gamma(°)\) |
|----------|----------------|----------------|----------------|--------------|-------------|-------------|
| This work| 6.26           | 6.25           | 6.52           | 95.7         | 97.1        | 85.7        |
| Kim et al. (2017) | 6.61           | 6.57           | 6.55           | 88.1         | 85.8        | 80.5        |
| Kim et al. (2017) | 6.59           | 6.60           | 6.57           | 82.7         | 98.0        | 94.6        |
| Kim et al. (2017) | 6.59           | 6.58           | 6.56           | 86.2         | 86.4        | 96.6        |
| Kim et al. (2017) | 6.79           | 6.47           | 6.46           | 88.2         | 93.9        | 95.0        |

### Figure 2 | DFT band structure and density of states of pseudo-cubic \(\text{CH}_3\text{NH}_2\text{CH}_3\text{PbI}_3\).

- (A) DFT band structure of \(\text{CH}_3\text{NH}_2\text{CH}_3\text{PbI}_3\).
- (B) DFT density of states of \(\text{CH}_3\text{NH}_2\text{CH}_3\text{PbI}_3\).
- (C) DFT + SOC band structure of \(\text{CH}_3\text{NH}_2\text{CH}_3\text{PbI}_3\).
- (D) DFT + SOC density of states of \(\text{CH}_3\text{NH}_2\text{CH}_3\text{PbI}_3\).
contribute significantly to the band edges at the maximum valence band and the minimum conduction bands as shown in the available state of the projected density of states in agreement with previous studies (Filip and Giustino, 2014; Im et al., 2015; Crespo, 2019). The spin-orbit coupling–based DFT band structure recorded a lower bandgap of 0.50 eV at R high symmetry; band splitting inherent to spin-orbit coupling is noticed in the spin-orbit–based DFT band structure. The spin-orbit coupling effect creates a gap between the first and the second band in the conduction region at R and M high symmetry points for both DFT-soc and GW-soc band structure calculations.

The DFT method underestimates the bandgap of semiconductors and insulators as a result of self-interaction error (Einollahzadeh et al., 2016; Morales-García et al., 2017; Crespo, 2019), while materials with d and f orbitals require more advanced formalism like DFT + U for accurate bandgaps (Morales-García et al., 2017). Although DFT + U improves semiconductors’ bandgaps, they sometimes fail due to the parameterization of the Hubbard parameter (U) and the fact that U is sometimes fitted to the experimental bandgaps (Morales-García et al., 2017). Furthermore, hybrid functionals which mix a portion of the Fock exchange with DFT functionals are often used to improve the bandgaps of semiconductors, but the material dependence of hybrid functionals and the associated high computation cost count as its demerit (Morales-García et al., 2017). This study also performs the self-consistent GW calculations on the system’s eigenvalues for both G and W. This method is known to reproduce the experimental bandgap of materials accurately (Morales-García et al., 2017). Although self-consistent GW calculations can be calculated on both the eigenvalues and the wavefunctions, the eigenvalue-based self-consistent GW calculations give results that are comparable to those of experimental studies since DFT calculations produce good wavefunctions. The GW and GW-soc band structures shown in Figure 3 also show identical bands, comparable with the DFT band structures. The \( G_0 W_0 \) and the spin-based \( G_0 W_0\)-soc band structure reported a bandgap of 2.25 and 1.10 eV, respectively, while self-consistent GW and GW-soc calculations reported a direct gap of 2.27 eV for \( G_1 W_1 \), 1.18 eV for \( G_1 W_1\)-soc, and 1.20 eV for \( G_2 W_2\)-soc at the R high symmetry point as shown in Table 2. The self-consistent GW and GW-soc calculations reported bands at a similar energy range in the valence band region, while the effect of the GW self-consistency was noticed in the conduction band, as shown in Figure 3.

The self-consistent GW method improves the GW bandgaps by increasing the \( G_0 W_0 \) bandgap by up to 0.5 eV (Filip and Giustino, 2014). In this work, the results suggest that the self-consistency in the GW method improves the \( G_0 W_0 \) bandgap without spin-orbit by 0.02 eV, while the bandgap with spin-orbit coupling improves by 0.1 eV in agreement with Filip and Giustini’s findings (Filip and Giustino, 2014; Katan et al., 2015). Alongside the band splitting, the spin-orbit coupling also reduces the bandgap gap by pushing the valence bands upward in the DFT band structure as shown in Figure 2, but both the valence band and the conduction band are pushed downward in the GW band structure calculation as shown in Figure 3. In the DFT band structure, the spin-orbit effect reduces the bandgap of \( \text{CH}_3\text{NH}_2\text{CH}_3\text{PbI}_3 \) by 0.94 eV (65%), in agreement with previous studies (Filip and Giustino, 2014; Agbaoye et al., 2020; Agbaoye et al., 2021). Similarly, the effect of spin-orbit reduces the bandgap of the GW band structure by 1.15 eV (51%), similar to the bandgap difference of 1.18 eV reported by Filip and Giustino (Filip and Giustino, 2014). Hence, the accurate bandgap

![Figure 3](https://example.com/figure3.png)
TABLE 2 | DFT and self-consistent GW bandgaps of pseudo-cubic CH$_3$NH$_2$CH$_3$PbI$_3$.

| Method         | DFT (eV) | DFT + soc (eV) | G$_0$W$_2$ (eV) | G$_1$W$_1$ (eV) | G$_0$W$_2$+soc (eV) | G$_1$W$_1$+soc (eV) | G$_2$W$_2$+soc (eV) |
|----------------|----------|----------------|----------------|----------------|-------------------|-------------------|------------------|
| This work (PBE) | 1.55     | 0.50           | 2.25           | 2.27           | 1.10              | 1.18              | 1.20             |
| Crespo (2019) (PBE) | 1.60     |                |                |                |                   |                   |                  |
| Kim et al. (2017) (GGA-PAW) | 1.61     |                |                |                |                   |                   |                  |
| Kim et al. (2017) (GGA-PAW) | 1.81     |                |                |                |                   |                   |                  |
| Kim et al. (2017) (GGA-PAW) | 1.78     |                |                |                |                   |                   |                  |
| Kim et al. (2017) (GGA-PAW) | 1.80     |                |                |                |                   |                   |                  |

of perovskites requires fully relativistic spin-orbit correction coupled with the GW quasiparticle method (Filip and Giustino, 2014). The DFT, DFT-soc, GW, and GW-soc band structures recorded similar band curvature, which indicates that although the DFT band structure underestimates the bandgap, it gives accurate band curvature. The DFT bandgap reported in this study is lower than the bandgaps reported by Crespo (2019) and Kim et al. (2017), as shown in table 2. The difference in the bandgaps reported in this study and the work of Crespo (2019) could be a result of the difference in lattice parameters and lattice coordinates, which is known to produce variation in the value of bandgaps (Bagayoko and Callaway, 1983; Wang et al., 1996; Kim et al., 2017). Alternatively, the difference in the bandgaps reported in this study and the study of Kim et al. (2017) may be associated with the difference in the Perdew–Burke–Enzenhoff exchange-correlation functional treated with the Grimme-d2 dispersion correction used in this study and the projected augmented wavefunction (PAW) formalism of the generalized gradient approximation method and the refitted Perdew–Wang 86 exchange-correlation functional used by Kim et al. (2017).

### 3.3 Optical Absorption

Similar optical spectra were reported by the 6×6×6 and the 4×4×4 Monkhorst–Pack kpoint scheme based Bethe–Salpeter equation method (BSE) without spin-orbit coupling. Furthermore, the 4×4×4 and 6×6×6 Monkhorst–Pack kpoint mesh optical spectra also show similar spectra in the spin-orbit coupling–based calculation. However, the optical spectra calculated using the 6×6×6 Monkhorst–Pack kpoint grid do not agree completely with the 4×4×4 Monkhorst–Pack kpoint grid; this could be a result of the kpoint convergence dependence in the Bethe–Salpeter equation method. The spin–orbit coupling–based optical spectra calculated with the 6×6×6 and 4×4×4 kpoint mesh record a redshift compared to the non–spin–orbit coupling–based optical spectra.

The 4×4×4 based optical spectra have sharper and more prominent absorption peaks compared to the results of the 6×6×6 optical spectra in both spin-orbit coupling and non–spin-orbit coupling calculation. The non–spin–orbit coupling–based optical spectra show higher and sharper absorption peaks in the 6×6×6 and 4×4×4 Monkhorst–Pack mesh than the spin–orbit coupling–based optical spectra. The optical absorption onsets in the real dielectric tensor and refractive index were noticed from the 6×6×6 and 4×4×4 kpoint mesh–based BSE calculation without spin–orbit coupling at 423 nm, 386 nm, 355 nm and 435 nm, 372 nm, and 349 nm, respectively. Alternatively, for non–spin–orbit coupling–based BSE calculation of the imaginary dielectric tensor, extinction coefficient, reflectivity, and absorbance, we report absorption peaks at 412 nm, 375 nm, 338 nm, 306 nm and 420 nm, 359 nm, 333 nm, and 306 nm for 6×6×6 and 4×4×4 kpoint mesh calculations, respectively. In the spin–orbit coupling–based BSE calculations, the real dielectric tensor and reflectivity have optical absorption peaks at 711 and 458 nm for the 4×4×4 kpoint mesh–based calculations and 793 nm, 567 nm, and 410 nm for the 6×6×6 kpoint mesh–based calculations. Similarly, the imaginary dielectric tensor, extinction coefficient, reflectivity, and absorbance have absorption peaks at 658 nm, 600 nm, and 448 nm for 4×4×4 kpoint mesh–based calculations and 687 nm, 538 nm, and 394 nm for 6×6×6 kpoint mesh–based calculation. The 4×4×4 (color red) and 6×6×6 (color blue) kpoint mesh–based spin–orbit coupling absorption coefficient of CH$_3$NH$_2$CH$_3$PbI$_3$ increases from 10$^3$ to 10$^6$ within the ultraviolet region. In contrast, the absorption coefficient remains steady at 10$^6$ along the visible spectrum toward the near-infrared region. The 4×4×4 (color black) and 6×6×6 (color green) kpoint mesh–based non–spin–orbit coupling reported its absorption coefficient in the order of 10$^6$ cm$^{-1}$ along the ultraviolet region and toward the visible spectrum. The absorption coefficient attenuates to 10$^3$ cm$^{-1}$ along the visible and toward the near-infrared region. Similar attenuation was reported in our previous study (Agbaoye et al., 2020) and the result of silicon (Green and Keveers, 1995), shown in Figure 4F. The absorption coefficient of CH$_3$NH$_2$CH$_3$PbI$_3$ calculated with and without spin–orbit coupling recorded lower values at the ultraviolet region than silicon’s absorption coefficient (Green and Keveers, 1995).

However, the absorption coefficient of CH$_3$NH$_2$CH$_3$PbI$_3$ recorded higher values along the visible and the near-infrared region, in agreement with the result of previous studies (Agbaoye et al., 2020; Agbaoye et al., 2021), and this compensates for the lower value of the absorption coefficient along the ultraviolet region, which suggests that CH$_3$NH$_2$CH$_3$PbI$_3$ could have comparable solar cell efficiency with silicon. The absorption onset at 418 nm from the absorption coefficient of the 6×6×6 kpoint mesh–based BSE calculation agrees with the absorption onset at 3 eV in the absorption coefficient reported by Crespo (2019). The spin–orbit coupling–based transmittance calculated with 6×6×6 (color blue) and 4×4×4 (color red) kpoint mesh reports a blue shift of the non–spin–orbit coupling–based transmittance and suggests that
CH$_3$NH$_2$CH$_3$PbI$_3$ will transmit only the short wavelength of the ultraviolet region due to the transmittance result up to 100% from 150 to 200 nm. Alternatively, the non–spin-orbit coupling–based transmittance can only transmit in the visible and the near-infrared region due to the exponential increase in the transmission value from 0 to 80% within 450–800 nm. The spectroscopic limited maximum efficiency predicted a maximum efficiency of 30% at a thickness of 10$^{-2}$ μm, which increases linearly to 62.7% at a thickness of 10$^{-1}$ μm, and then remains constant as the thickness increases, as shown in Figure 5. These interesting maximum efficiency limits are calculated at room temperature (293.15 K), a direct allowed bandgap of 1 eV, an indirect allowed bandgap of 1.97 eV, and the BSE-soc absorption coefficient reported in Figure 4.
4 CONCLUSION

This study reveals the electronic structure and the optical absorption spectra of CH$_3$NH$_2$CH$_3$PbI$_3$, the lattice parameters, and the DFT bandgap of the pseudo-cubic ground state structure were reported in agreement with previous studies (Kim et al., 2017; Crespo, 2019). The spin-orbit coupling effect was introduced to both the electronic structure and optical spectra to cater for the presence of heavy metals such as lead (Pb); the spin-orbit coupling effect causes band splitting and bandgap reduction in agreement with the previous studies (Filip and Giustino, 2014; Agbaoye et al., 2020; Agbaoye et al., 2021). The projected density of states reveals that the dimethylammonium cation does not contribute to the bands around the maximum valence band and the minimum conduction band, while the lead (Pb) p orbital and the iodine (I) p orbital play the most significant roles in the conduction and the valence band, respectively. The spin-orbit coupling–based self-consistent GW bandgaps were calculated to correct the deficiency of DFT bandgaps, giving a more accurate bandgap of 1.20 eV, which is within the highest Schockly–Queisser maximum efficiency limit of about 33% (Queisser, 2009; Sha et al., 2015). The spin-orbit coupling–based optical spectra show a redshift of the non–spin–orbit coupling spectra, while the size of the k-point mesh plays a significant role in the size and position of the absorption peaks. The absorption coefficients were reported in the order of 10$^8$ along the ultraviolet region, lower than silicon, but increased absorption coefficients in the order of 10$^6$ higher than silicon were recorded along the visible spectrum. The spectroscopic limited maximum efficiency predicts an attractive maximum efficiency of about 62.7% within 10$^{-1}$ to 10$^2$ μm thickness, which affirms that CH$_3$NH$_2$CH$_3$PbI$_3$ will be a highly efficient solar cell absorber.

DATA AVAILABILITY STATEMENT

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

AUTHOR CONTRIBUTIONS

RA, SB, PA, SK, and GA contributed to conception and design of the study. AK, A-OA, HM, and BM prepared the input files and literatures. RA, SB, AK, A-OA, HM, and BM wrote sections and the first draft of the manuscript. RA, PA, SK, and GA performed review and editing. RA, SK, and GA performed supervision, validation, and resources. All authors contributed to manuscript revision and read and approved the submitted version.

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