The role of interference in unraveling the $ZZ$-couplings of the newly discovered boson at the LHC

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Abstract

We present a general procedure for measuring the tensor structure of the coupling of the scalar Higgs-like boson recently discovered at the LHC to two $Z$ bosons, including the effects of interference among different operators. To motivate our concern with this interference, we explore the parameter space of the couplings in the effective theory describing these interactions and illustrate the effects of interference on the differential dilepton mass distributions. Kinematic discriminants for performing coupling measurements that utilize the effects of interference are developed and described. We present projections for the sensitivity of coupling measurements that use these discriminants in future LHC operation in a variety of physics scenarios.

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I. INTRODUCTION

As the new particle discovered by the ATLAS [2] and CMS [3] collaborations appears to be similar to the Standard Model (SM) Higgs boson [4–9], it becomes very important to measure its properties as precisely as possible in order to find or constrain physics beyond the SM. The recent ATLAS and CMS results strongly suggest that the newly discovered boson has spin zero [10–14], which we take as the starting point in the studies presented in this report. There is a large body of literature [15–53] advocating the great potential of $X \rightarrow ZZ \rightarrow 4\ell$ decays for disentangling the spin-parity properties of resonances decaying to two Z bosons and for refining the methodology for doing such measurements. In this work we explore the sensitivity of future LHC analyses to interference between various operators in this channel. We follow the framework of Ref. [49], which is briefly reviewed below.

A. Review of Framework

We consider a spin zero state $X$, which in general is a linear combination of a $CP$-even state, $H$, and a $CP$-odd state, $A$:

$$X \equiv H \cos \alpha + A \sin \alpha. \quad (1)$$

The couplings of the arbitrary spin zero boson, $X$, to two $Z$ bosons can be described by the symmetry properties of the corresponding operators, which fall into the following three categories: (i) $CP$-even terms which clearly violate gauge invariance, (ii) $CP$-even terms which may preserve gauge invariance, (iii) $CP$-odd terms. For each category, the lowest dimensional operators in the effective theory, in terms of some new physics scale $\Lambda$, yield the Lagrangian

$$\mathcal{L} \supset - \left( \frac{g_1 M_Z^2}{v} \right) H Z_\mu Z^\mu - \left( \frac{g_2}{2 \Lambda} \right) H F_{\mu\nu} F^{\mu\nu} - \left( \frac{g_4}{2 \Lambda} \right) A F_{\mu\nu} \tilde{F}^{\mu\nu}, \quad (2)$$

where $\tilde{F}_{\mu\nu} = \frac{i}{2} \epsilon_{\mu\nu\rho\sigma} F^{\rho\sigma}$ and the $g_i$ are dimensionless coupling constants. Re-expressing the Lagrangian terms in Eq. (2) to involve the mass eigenstate $X$, we obtain

$$\mathcal{L} \supset - X \left[ \kappa_1 \frac{M_Z^2}{v} Z_\mu Z^\mu + \frac{\kappa_2}{2v} F_{\mu\nu} F^{\mu\nu} + \frac{\kappa_3}{2v} F_{\mu\nu} \tilde{F}^{\mu\nu} \right], \quad (3)$$

where

$$\kappa_1 = g_1 \cos \alpha, \quad \kappa_2 = g_2 \cos \alpha \left( v/\Lambda \right), \quad \kappa_3 = g_4 \sin \alpha \left( v/\Lambda \right). \quad (4)$$
TABLE I. Comparison of notations for the effective $XZZ$ couplings

| Ref.    | $\kappa_1$          | $\kappa_2$ | $\kappa_3$ |
|---------|---------------------|------------|------------|
| Refs. [27, 39] | $(i/2)g_1^{(0)}$ | $-ig_2^{(0)}$ | $-ig_4^{(0)}$ |
| Ref. [44] | $(g_{1z}/2)(v/M_Z^2)$ | $(g_{2z}/2)v$ | $(g_{4z}/2)v$ |
| Ref. [54] | $gv/(2MZ)$ | $g\lambda v/(2MZ)$ | $-g\lambda' v/(2MZ)$ |
| Ref. [55] | $-(g_{HZZ}k_{SM}v \cos \alpha)/(2M_Z^2)$ | $(k_{HZZ}v \cos \alpha)/(2\Lambda)$ | $(k_{ZZ}v \sin \alpha)/(2\Lambda)$ |

$^a$ We note that an overall phase in the amplitude, which can be seen in this table as an overall phase in the couplings, is irrelevant except in the likely-negligible case of interference between, e.g., the $gg \to X \to ZZ^* \to 4\ell$ signal, and the loop-induced $gg \to ZZ^* \to 4\ell$ background [56–59].

Each case where exactly one of the coefficients $\kappa_i$ is non-vanishing corresponds to a specific pure state: (i) $\kappa_1 \neq 0$ corresponds to a SM-like Higgs (in particular $\kappa_1 = 1$ is the tree-level SM coupling); (ii) $\kappa_2 \neq 0$ corresponds to the state which describes a SM singlet, usually denoted with $0^+_h$ [39]; (iii) $\kappa_3 \neq 0$ corresponds to a pure pseudoscalar ($J^{CP} = 0^-$).

The decay amplitude that one obtains from the Lagrangian in Eq. (3) is

$$A(X \to ZZ) = -\frac{2i}{v} \epsilon_1^{\mu} \epsilon_2^{*\nu} \left( (\kappa_1 M_Z^2 - \kappa_2 (p_1 \cdot p_2)) g_{\mu\nu} + \kappa_2 p_\mu p_\nu + \kappa_3 \epsilon_{\mu\alpha\beta} p_1^\alpha p_2^\beta \right).$$

(5)

Here $p_1(2)$ is the momentum of the intermediate Z boson labelled “1” (“2”), while $p = p_1 + p_2$ is the momentum of the X boson. We note, following, e.g., Refs. [27, 28, 39] (cf. especially Eq. (11) in Ref. [39]) that the three operators in Eq. (3) generate each of the three possible Lorentz structures in the general amplitude for the decay of $X$ to two bosons.

1. Comparison of Conventions

Various conventions have been used in writing Lagrangians and amplitudes for the study of the $X \to ZZ$ interaction. For the convenience of the reader, Table I contains a dictionary of the couplings used in Refs. [27, 39, 44, 49, 54, 55].

2. Sensitivity to Loop-Induced Couplings

The coefficients $\kappa_i$ in Eq. (3) are real, since they originate from the tree-level Lagrangian in Eq. (3). By the optical theorem, the amplitude may obtain contributions from loops with
light particles (lighter than $M_X/2 \approx 63$ GeV) such that the expression for the amplitude including loop effects is analogous to that in Eq. (5), where the effective couplings $\kappa'_i$ are complex:

$$A(X \to ZZ) = -\frac{2i}{v} \epsilon_1^{\mu} \epsilon_2^{\nu} \left( (\kappa'_1 M_Z^2 - \kappa'_2 (p_1 \cdot p_2)) g_{\mu\nu} + \kappa'_2 p_{\mu} p_{\nu} + \kappa'_3 \epsilon_{\mu\alpha\beta} p_{1\alpha}^{\alpha} p_{2\beta}^{\beta} \right).$$

(6)

However, at least one of the $\kappa_i$ must not be predominantly loop-induced, or else one runs into a contradiction with the experimental constrains. For example, consider a generic loop with some invisible new particle whose coupling to the $X(Z)$ boson is $g_{X(Z)}$. Then, naively,

$$\delta \kappa'_i = \frac{g X g_2^Z}{16\pi^2} \times O(1).$$

(7)

In this scenario the invisible width of the $X$ boson is

$$\Gamma_{X,\text{inv}} = \frac{g_X^2 M_X}{16\pi} \times O(1),$$

(8)

hence taking $\Gamma_{X,\text{inv}} \lesssim \Gamma_{X,\text{total}} \lesssim 7$ GeV [60], we obtain $g_X \lesssim 2$. Since the gauge coupling to the $Z$, $g_Z$, should be $\lesssim 1$, we get

$$\delta \kappa'_i \lesssim 1 \times 10^{-2}.$$  

(9)

This is about two orders of magnitude smaller than the magnitude of couplings needed to give the SM rate [49]. More stringent constraints on the $\delta \kappa'_i$ (with some caveats) may be obtained from more stringent limits on the invisible width of the Higgs [13, 51, 61–64] or the invisible width of the $Z$ [65]. It is therefore well-motivated to treat the relevant couplings, $\kappa'_i$, (namely, the ones which are large enough to measure at present) as predominantly real.

### B. Experimental Situation

The hypothesis of the new boson being a 100% pure pseudoscalar, $0^-$, has been excluded by CMS [11] [66] and ATLAS [10] [14]. The possibility of a 100% pure $0^+_u$ is also disfavored at 92% C.L. [11]. Hence, in this study we assume a non-zero value of coupling, $\kappa_1$, and address the question of the experimental sensitivity to the presence of $\kappa_2$ and $\kappa_3$ terms in the $XZZL$ Lagrangian.

The current limit, set by CMS [11], on the presence of a pseudoscalar contribution expressed in terms of a fractional cross section is $f_{a3} = \sigma_3 / (\sigma_1 + \sigma_3) < 0.58$. Here the cross

$\footnote{We note that increasing the number of particles running in the loop alleviates the constraints on the $\delta \kappa'_i$.}$
sections $\sigma_1$ and $\sigma_3$ are taken for the $4e$, $4\mu$, and $2e2\mu$ final states together\footnote{For given values of couplings $\kappa_i$ and $\kappa_j$, the ratios of cross sections $\sigma_i/\sigma_j$ ($i \neq j$) for same-fermion and different-fermion final states are different. This is due to the interference effects associated with permutations of identical fermions in the final state. Hence, one should specify which final states are used in the definition of $f_{a3}$.} and correspond to 100% pure $0^+$ and $0^-$ states, respectively. This result translates into a limit on the ratio of couplings $|\kappa_3/\kappa_1| < 6.1$. The corresponding CMS analysis was set up in such a way that it was not sensitive to the interference between the $\kappa_3$- and $\kappa_1$-induced amplitudes.

C. Objective

In this paper, we show that by explicitly exploiting the interference between amplitudes which involve the $0^+$, $0^+_h$, and $0^-$ states (corresponding to the $\kappa_1$, $\kappa_2$, and $\kappa_3$ terms in the Lagrangian in Eq. (3), respectively) one can boost the experimental sensitivities to the presence of an $0^-$ (and $0^+_h$) admixture. We show that the gains become particularly large at high integrated luminosities, allowing one to probe smaller values of the $\kappa_2$ and $\kappa_3$ couplings. We also address the question of establishing the presence of the interference and evaluating its sign, should decay amplitudes associated with spin zero higher dimensional operators be detected. Recently, the importance of a proper treatment of interference was discussed in the context of a somewhat different aspect of the $H \to ZZ \to 4\ell$ channel [44]; there it was the interference associated with permutations of identical leptons in the $4e$ and $4\mu$ final states that was considered. This interference is always included in the studies presented in this report.

II. THE PHYSICAL IMPORTANCE OF INTERFERENCE

In general, interference effects can manifest themselves in two different ways: either at the level of total cross sections (reflected in the production rate, as discussed in Sec. II A below), or at the level of differential distributions (as discussed in Sec. II B below).
A. The impact of interference effects on the production rate

The overall rate for $X \to ZZ \to 4\ell$ events is proportional to the partial width for $X \to ZZ$ \[49\]

$$\Gamma(X \to ZZ) = \Gamma_{SM} \sum_{i,j} \gamma_{ij} \kappa_i \kappa_j,$$

(10)

where the partial $H \to ZZ$ width predicted in the SM, $\Gamma_{SM}$, is factored out in order to define constant dimensionless coefficients $\gamma_{ij}$ (with $\gamma_{ij} = \gamma_{ji}$) \[3\]

$$\gamma_{11} = 1, \quad \gamma_{22} = 0.090, \quad \gamma_{33} = 0.038, \quad \gamma_{12} = -0.250, \quad \gamma_{13} = \gamma_{23} = 0.$$  \(11\)

The presence of interference is then implied by nonzero values of the “off-diagonal” coefficients $\gamma_{ij}$ with $i \neq j$. Eq. (11) shows that the overall rate is affected by interference between $0^+$ and $0^+_h$, which is destructive (constructive) when $\kappa_1$ and $\kappa_2$ have the same (opposite) signs. Eq. (11) also implies that at the level of total cross sections there is no interference between $0^+$ and $0^-$ or between $0^+_h$ and $0^-$.\[5\]

The magnitude of interference depends on the values of the couplings $\kappa_1$ and $\kappa_2$. Obviously, for a pure $0^+$ state ($\kappa_1 \neq 0$, $\kappa_2 = 0$) and for a pure $0^+_h$ state ($\kappa_2 \neq 0$, $\kappa_1 = 0$) the interference is absent. Given the values in Eq. (11), one could expect the interference effect to be maximal for

$$\frac{\kappa_2}{\kappa_1} = \frac{1}{2} \tan^{-1} \left( \frac{2\gamma_{12}}{\gamma_{11} - \gamma_{22}} \right) \approx 3.89.$$  \(12\)

In practice, the signal rate for $X \to ZZ \to 4\ell$ production is measured from data, thus imposing one constraint through Eq. (10) on the $\{\kappa_1, \kappa_2, \kappa_3\}$ parameter space \[49\] (provided the production rate for the $X$ is fixed). The constraint may be solved explicitly by a suitable change of variables, reducing the relevant $\{\kappa_i\}$ parameter space to a two-dimensional surface which can be taken to be effectively the surface of a sphere \[49\]. For this reason, we shall not discuss the overall rate further. Instead, we will assume in our analyses that the rate measurement has already been performed and the couplings $\kappa_i$ have been chosen so that they satisfy the constraint of Eq. (10).

\[3\] The values quoted in Eq. (11) correspond to the $2e2\mu$ channel before cuts. For the $4e$ or $4\mu$ channels (or with cuts) the numerical values are similar but not identical \[49\].
B. The impact of interference effects on differential distributions

Even if the overall rate is kept fixed, the interference effects are still present at the level of differential distributions (the size of this effect will be quantified in Sec. IV below). In general, the kinematics of $X \rightarrow ZZ \rightarrow 4\ell$ events is described in the $X$ rest frame by 7 independent degrees of freedom, and interference will impact the differential distribution in this 7-dimensional signature space. For simplicity, in this subsection we will focus only on the $M_{Z_1}$ and $M_{Z_2}$ invariant mass distributions and use them to illustrate the effects of interference. In order to provide an intuitive understanding of some of the results to follow in Sec. IV, we shall derive analytical formulas for the $M_{Z_1}$ and $M_{Z_2}$ distributions, which explicitly demonstrate the interference effects.

The doubly differential decay width with respect to $M_{Z_1}$ and $M_{Z_2}$ can be written as

$$\frac{d^2\Gamma}{dM_{Z_1}dM_{Z_2}} = \frac{1}{v} \sum_{i,j} \kappa_i \kappa_j F_{ij}(M_{Z_1}, M_{Z_2}; M_X),$$

where the dimensionless functions $F_{ij}$ are symmetric with respect to their indices: $F_{ij} = F_{ji}$. In the absence of any selection criteria, the functions $F_{ij}$ are

$$F_{11}(M_{Z_1}, M_{Z_2}) = \frac{M^4_Z}{M^2_{Z_1} M^2_{Z_2}} (x + 3) \xi(M_{Z_1}, M_{Z_2}; M_X),$$

$$F_{12}(M_{Z_1}, M_{Z_2}) = \frac{M^2_Z}{M_{Z_1} M_{Z_2}} 3\sqrt{x + 1} \xi(M_{Z_1}, M_{Z_2}; M_X),$$

$$F_{22}(M_{Z_1}, M_{Z_2}) = (2x + 3) \xi(M_{Z_1}, M_{Z_2}; M_X),$$

$$F_{13}(M_{Z_1}, M_{Z_2}) = 0,$$

$$F_{23}(M_{Z_1}, M_{Z_2}) = 0,$$

$$F_{33}(M_{Z_1}, M_{Z_2}) = 2x \xi(M_{Z_1}, M_{Z_2}; M_X),$$

where the dimensionless common factor $\xi$ is given by

$$\xi(M_{Z_1}, M_{Z_2}; M_X) \equiv \left(\frac{g_a^2 (g^2_a + g^2_v)}{2 \cos^2 \theta^2_W} \right)^2 \frac{M^6_{Z_1} M^6_{Z_2} \sqrt{x}}{9(2\pi)^5 v M^3_X P_1 P_2}.$$

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4 Note the webpage http://yichen.me/project/GoldenChannel/ created by the authors of Ref. [46], may be used to make plots of interesting differential distributions for different values of the couplings $\kappa_i$. 
5 Since $\kappa_i$ are already dimensionless, in the right-hand side of Eq. 13 we factor out $1/v$ to make $F_{ij}$ dimensionless as well.
Here $g_2$ is the $SU(2)_W$ gauge coupling constant, $g_v = -\frac{1}{2} + 2\sin\theta_W^2$, $g_a = -\frac{1}{2}$, $\theta_W$ is the Weinberg angle,

$$x \equiv \left( \frac{M_X^2 - M_{Z_1}^2 - M_{Z_2}^2}{2M_{Z_1}M_{Z_2}} \right)^2 - 1$$

(21)

is a dimensionless parameter introduced in Ref. [39], and

$$P_i \equiv (M_{Z_i}^2 - M_{Z}^2)^2 + \Gamma_Z^2 M_Z^2$$

(22)

are the $Z$ propagator functions which depend on the mass, $M_Z$, and width, $\Gamma_Z$, of the $Z$-boson.

The doubly differential distribution in Eq. (13) is an interesting object to study experimentally and CMS and ATLAS have published plots of the Higgs candidate events in the $(M_{Z_1}, M_{Z_2})$ plane. Events are expected to be clustered around $M_{Z_1} = M_Z$, while the $M_{Z_2}$ dependence is non-trivial and contains interesting information [44]. Therefore we integrate the expression in Eq. (13) over $M_{Z_1}$ and consider instead the corresponding one dimensional distribution

$$\frac{d\Gamma}{dM_{Z_2}} \equiv \int dM_{Z_1} \left( \frac{d^2\Gamma}{dM_{Z_1}dM_{Z_2}} \right) \equiv \sum_{i,j} \kappa_i \kappa_j f_{ij} (M_{Z_2}; M_X),$$

(23)

with newly defined dimensionless functions

$$f_{ij}(M_{Z_2}; M_X) \equiv \frac{1}{v} \int dM_{Z_1} F_{ij}(M_{Z_1}, M_{Z_2}; M_X)$$

(24)

in place of Eqs. (14-19). Comparison of Eq. (10) and Eq. (13) shows that the normalization of the functions $F_{ij}$ and $f_{ij}$ is given by the values of the coefficients $\gamma_{ij}$ in Eq. (11)

$$\gamma_{ij} = \frac{1}{v \Gamma_{SM}} \int dM_{Z_1} \int dM_{Z_2} F_{ij}(M_{Z_1}, M_{Z_2}; M_X)$$

(25)

$$= \frac{1}{\Gamma_{SM}} \int dM_{Z_2} f_{ij}(M_{Z_2}; M_X).$$

(26)

Fig. 1 shows the four non-vanishing functions $f_{11}$ (blue), $f_{12}$ (green), $f_{22}$ (red) and $f_{33}$ (magenta) as a function of $M_{Z_2}$ for the nominal value of $M_X = 125$ GeV. The two functions $f_{13}$ and $f_{23}$ vanish due to the $CP$ properties of the operators considered in the Lagrangian in Eq. (3). All functions in panel (a) are normalized to unity, which makes it easier to study the differences in their shapes. In panel (b) the functions are properly normalized in accordance with Eq. (26).
FIG. 1. The four non-vanishing functions \( f_{ij} \) defined in Eq. (24) as a function of \( M_{Z_2} \), with \( M_X = 125 \) GeV and (a) unit normalization or (b) properly normalized as in Eq. (26).

Fig. 1(a) shows that all four functions exhibit similar dependence on \( M_{Z_2} \). At first, they all monotonically increase from 0 at \( M_{Z_2} = 0 \), reaching a peak somewhere in the neighborhood of \( M_{Z_2} \sim 25 - 30 \) GeV, followed by a sudden drop at around \( M_{Z_2} \sim 34 \) GeV, and a long tail until \( M_{Z_2} = 62.5 \) GeV. This behavior can be understood purely in terms of kinematics. The majority of the events contain an on-shell \( Z \)-boson with \( M_{Z_1} \approx M_Z \), which leaves only up to \( M_X - M_Z \sim 34 \) GeV available to \( M_{Z_2} \), which explains the kinematic endpoint at \( M_{Z_2} \sim 34 \) GeV. The tail results from events where both \( Z \)-bosons are off-shell, and extends to half the \( X \) mass, \( M_X/2 = 62.5 \) GeV. Finally, the distributions peak relatively close to the \( M_{Z_2} \sim 34 \) GeV endpoint, since the propagator functions in Eq. (22) prefer \( M_{Z_2} \) to be as close as possible to the mass \( M_Z \) of the \( Z \)-boson.

Fig. 1(b) compares the relative size of the different \( f_{ij} \) functions. We see that the overall magnitude is largest for \( f_{11} \) and smallest for \( f_{33} \). Note that the interference contribution from \( f_{12} \) has the second largest magnitude and an opposite sign compared to the other three functions shown in the plot — these two facts will be important in the discussion to follow.

The observable \( M_{Z_2} \) distribution is obtained by a suitable superposition of the individual contributions seen in Fig. 1(b), properly weighted by products of \( \kappa_i \) couplings as specified in Eq. (23). Fig. 1 allows us to understand the resulting \( M_{Z_2} \) shapes. First, we concentrate on the location of the peak of the total \( M_{Z_2} \) distribution, which has been suggested as an

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6 Contrast this to the case of the SM background, where there is a contribution from a virtual photon which dominates and causes the \( M_{Z_2} \) distribution to peak at much lower values [39, 44].
FIG. 2. The location of the peak in the $M_{Z_2}$ distribution as a function of (a) the ratio $\kappa_2/\kappa_1$, with $\kappa_3 = 0$ and (b) the ratio $\kappa_3/\kappa_1$, with $\kappa_2 = 0$. The shaded region denotes the lower cut on $M_{Z_2}$ used in our analysis. The blue circle corresponds to the case of the tree-level SM ($\kappa_1 = 1$, $\kappa_2 = 0$, $\kappa_3 = 0$).

An easily measurable global observable characterizing any invariant mass distribution [67]. The peak location is plotted in Fig. 2 for two scenarios: (a) $\kappa_3 = 0$ and varying the ratio $\kappa_2/\kappa_1$, keeping the total $X \to ZZ \to 4\ell$ partial width fixed to $\Gamma_{SM}$; and (b) $\kappa_2 = 0$ and similarly varying the ratio $\kappa_3/\kappa_1$.

Let us first focus on the interplay between the $\kappa_1$ and $\kappa_3$ terms in the Lagrangian [3]. In this case, the behavior of the peak shown in Fig. 2(b) is relatively simple, due to the absence of an interference contribution ($f_{13} = 0$). The case of the SM (denoted by the blue circle) corresponds to $\kappa_1 = 1$ and $\kappa_3 = 0$, in which case the $M_{Z_2}$ distribution is made up entirely of the $f_{11}$ contribution, which peaks around 28 GeV. As the value of $\kappa_3$ is gradually increased, one introduces a larger fraction of the $f_{33}$ component from Fig. 1, which peaks at a lower value of $M_{Z_2}$, around 25 GeV. As a result, the peak location in Fig. 2(b) is initially a decreasing function of the ratio $\kappa_3/\kappa_1$. Eventually, we reach the case of a pure $0^-$ state with $\kappa_2 \neq 0$ and $\kappa_1 = 0$, when the $M_{Z_2}$ distribution is composed entirely of the $f_{33}$ component and the $M_{Z_2}$ peak is located at $M_{Z_2} \sim 25$ GeV. The right half of Fig. 2(b), where the $\kappa_1$ and $\kappa_3$ couplings are taken with a relative minus sign, is a mirror image of the left and can be understood in the same way.

Notice that the $f_{11}$ and $f_{33}$ contributions always enter with positive weights, $\kappa_1^2$ and $\kappa_3^2$,
respectively. Thus the shape of the combined $M_{Z_2}$ distribution is a weighted average between the $f_{11}$ and $f_{33}$ shapes seen in Fig. 1(a), which are already very similar. As a result, the peak location stays relatively constant over the whole range of the couplings ratio $\kappa_3/\kappa_1$.

In contrast, when we consider the interplay between $\kappa_1$ and $\kappa_2$, the situation changes completely, as demonstrated by Fig. 2(a). Now the $M_{Z_2}$ distribution is built up from three components: $f_{11}$, which peaks near 28 GeV, $f_{22}$, which peaks around 30 GeV, and $f_{12}$, whose magnitude peaks near 29 GeV. Given that the peaks of all these three components are very close, one might expect that the peak of the total $M_{Z_2}$ distribution would also fall in the vicinity of 28 to 30 GeV. However, Fig. 2(a) reveals that this naive expectation is false and that in the range where the couplings $\kappa_1$ and $\kappa_2$ have the same sign, the peak location can vary from as low as 15 GeV to as high as 31 GeV. The reason for this wild behavior can be traced to the fact that the interference term, $f_{12}$, is significant and opposite in sign from $f_{11}$ and $f_{22}$, so that when the couplings $\kappa_1$ and $\kappa_2$ have equal signs, it destructively interferes with the sum of the $f_{11}$ and $f_{22}$ terms. Even more surprisingly, as the value of $\kappa_2$ is increased relative to $\kappa_1$, at a certain point the $M_{Z_2}$ distribution undergoes a type of “first order phase transition”, where the location of the peak “jumps” suddenly and discontinuously from around 18 GeV to near 30 GeV, signaling the presence of at least two local maxima in the $M_{Z_2}$ distribution.

The peculiarities exhibited in Fig. 2(a) prompt further detailed investigations. In Fig. 3 we plot the $M_{Z_2}$ distribution (shown with a red solid line) for a series of interesting ratios $\kappa_2/\kappa_1$. In each frame, we also show the three individual contributions, appropriately weighted with products of $\kappa_i$ factors: $f_{11}$ (dashed blue), $f_{22}$ (dot-dashed orange) and the interference term $f_{12}$ (dotted green). The top left frame represents the case of the SM with $\kappa_1 = 1$ and $\kappa_2 = 0$. The $M_{Z_2}$ distribution is comprised entirely of the $f_{11}$ component and peaks rather sharply around 28 GeV. As we start increasing the value of $\kappa_2$, the (negative) interference term $f_{12}$ begins to partially offset the $f_{11}$ piece and shifts the peak towards lower $M_{Z_2}$ values. At the same time, the shape of the $M_{Z_2}$ distribution becomes deformed, while the $M_{Z_2}$ peak becomes rather broad.

A very interesting situation occurs in the $\kappa_i$ parameter region illustrated by the plots in the second row of Fig. 3. Here the cancellation between the (negative) interference term $f_{12}$ and the (positive) $f_{11}$ and $f_{22}$ is near maximal (see Eq. (12)). More importantly, the resulting $M_{Z_2}$ distribution begins to develop a second local peak at high values of $M_{Z_2} \sim 30$ GeV. As
FIG. 3. $M_{Z_2}$ distributions for $\kappa_3 = 0$ and different choices of $\kappa_1$ and $\kappa_2$. The net total (shown in solid red) is comprised of three contributions: from $f_{11}$ (dashed blue), from $f_{22}$ (dot-dashed orange), and from the interference term $f_{12}$ (dotted green). More plots like these are available in movie form at http://www.phys.ufl.edu/~gainer/k1k2-movie.mov.

As the value of $\kappa_2$ is increased beyond the region of the “first order phase transition” shown in Fig. 4, the $M_{Z_2}$ distribution starts to be dominated by the $f_{22}$ contribution and eventually we get to the pure $0^+_h$ state (the second to last panel in Fig. 3).
FIG. 4. Unit-normalized differential $M_{Z_2}$ distributions for $\kappa_3 = 0$ and several choices of $\kappa_1$ and $\kappa_2$ near the point of the “first order phase transition”, where the impact of interference on the shape of the distribution is maximal (see Fig. 3).

in Fig. 3 shows a representative point with opposite signs for the couplings $\kappa_1$ and $\kappa_2$. In that case, the sign of the interference term $f_{12}$ is flipped and it adds constructively with $f_{11}$ and $f_{22}$, causing the peak of the $M_{Z_2}$ distribution to stay in the vicinity of 28 – 30 GeV.

III. METHODOLOGY

A. Optimized Analyses

To obtain the greatest sensitivity to a signal in a model which is characterized by a modest number of parameters, it is customary to use analyses with criteria specifically optimized for each point in the parameter space of the underlying model. This procedure
is used in all searches for Higgs bosons, whether SM or otherwise. The approach has also been advocated for SUSY searches where the signal model may have a greater number of parameters \[68, 69\]. In line with this idea, we introduce the kinematic discriminants that are automatically optimized for each point in the $XZZ$ coupling parameter space.

In this report we assume that the cross section has been well-measured and that variations in the overall rate may be absorbed into the $ggX$ couplings (provided we consider only the $pp \rightarrow X \rightarrow ZZ \rightarrow 4\ell$ channel). For this reason, the parameters we aim to measure are not the $XZZ$ couplings, $\kappa_i$, but their ratios $\kappa_2/\kappa_1$ and $\kappa_3/\kappa_1$. These quantities can be easily re-expressed in any desired convention, such as “geolocating” angles as in Ref. \[49\] or $f_a$-like fractions as in Ref. \[11\]. In this study we assume that the couplings are real numbers, as already explained in Sec. \[1A2\].

### B. Preparation of Monte Carlo Samples

The analyses are performed using simulated $gg \rightarrow X \rightarrow ZZ \rightarrow 4\ell$ events, generated using FeynRules \[70\] and MadGraph \[71\] according to the MEKD framework \[44\]. This approach ensures that we include all interference effects: those arising from the presence of multiple terms in the Lagrangian as well as those associated with permutations of identical leptons in the $4e$ and $4\mu$ final states. Following the ATLAS and CMS results \[10, 11\] the mass of the scalar Higgs-like boson mass is taken to be 125 GeV. We use MadGraph to simulate the $q\bar{q} \rightarrow ZZ$ backgrounds. Our simulation is performed entirely at the leading order and at the parton level. In order to compensate somewhat, we consider events with the four-lepton invariant mass in a very conservative 10 GeV mass window centered at the Higgs mass of 125 GeV (in contrast, the LHC detectors have $1 - 2\%$ mass resolution). Consequently, the larger mass window results in the acceptance of more background events.

We use lepton kinematic selection criteria very similar to those used in the $H \rightarrow ZZ \rightarrow 4\ell$ analyses of ATLAS and CMS experiments \[10, 11\]. Leptons are required to have transverse momenta $p_T > 5$ GeV and pseudorapidity $|\eta| < 2.5$. At least one same-flavor opposite-sign lepton pair must have an invariant mass greater than 40 GeV, while the other lepton pair must have an invariant mass greater than 12 GeV. We use events with all three final-state combinations ($4e$, $4\mu$, and $2e2\mu + 2\mu2e$) in all of our analyses.
C. Projected Event Yields

In order to obtain the analysis results as a function of the integrated luminosity of the LHC runs at 14 TeV, we estimate experimental reconstruction efficiencies and contribution of the background at the 14 TeV LHC using the average of the expected signal and background event yields reported by ATLAS and CMS (Table II). The number of events expected in the 14 TeV LHC runs with \( L \) fb\(^{-1}\) of integrated luminosity, \( N(L) \), is computed as:

\[
N(L) = \frac{N_{\text{ATLAS}} + N_{\text{CMS}}}{2} \times \frac{\sigma(14 \text{ TeV})}{\sigma(8 \text{ TeV})} \times \frac{L}{(25 \text{ fb}^{-1})},
\]  

(27)

The ratios of cross sections for the SM Higgs boson signal and the dominant \( q\bar{q} \rightarrow ZZ \) background used in Eq. (27) are \( \sigma_H(14 \text{ TeV})/\sigma_H(8 \text{ TeV}) = 2.6 \) [72] and \( \sigma_{ZZ}(14 \text{ TeV})/\sigma_{ZZ}(8 \text{TeV}) = 1.9 \) (computed with MCFM [73]). With these assumptions, the average expected event rates per experiment per fb\(^{-1}\) of integrated luminosity at the 14 TeV LHC are 1.9 (signal) and 0.76 (background, in the 10 GeV mass window described above).

TABLE II. The expected event yields for the SM Higgs boson signal with mass \( m_H = 125 \text{ GeV} \) and background, as reported by the ATLAS and CMS collaborations for 7+8 TeV LHC Run I.

| Experiment | Process | Event yield | Integrated luminosity at 7 + 8 TeV | Source |
|------------|---------|-------------|-----------------------------------|--------|
| ATLAS      | Signal  | 18.2        | 4.6 + 20.7 = 25.3 fb\(^{-1}\)     | Tab. 7 in Ref. [10] |
|            | Bkgd    | \( \sim 1 \text{ event/GeV} \) |                                    | Fig. 4 in Ref. [10] |
| CMS        | Signal  | 19.2        | 5.1 + 19.6 = 24.7 fb\(^{-1}\)     | Tab. 2 in Ref. [11] |
|            | Bkgd    | \( \sim 1 \text{ event/GeV} \) |                                    | Fig. 2 in Ref. [11] |

D. Kinematic Discriminants

Kinematic discriminants for separation between the two types of four-lepton processes, A and B, may be constructed by calculating the ratio of the squared matrix elements for these two hypotheses, as described in Ref. [44]. For each four-lepton event with kinematic information \( \mathbf{x} \), one can compute:

\[
D(A,B; \mathbf{x}) = \frac{|\mathcal{M}(A; \mathbf{x})|^2}{|\mathcal{M}(B; \mathbf{x})|^2},
\]  

(28)
In our analysis, we compute the kinematic discriminants following this approach. We first consider the kinematic discriminant \( D(X; 0^+) \). Here, the hypothesis “\( X \)” is the hypothesis that the scalar Higgs-like boson couples to \( Zs \) via both the \( \kappa_1 \) and \( \kappa_3 \) operators. We will further refer symbolically to this state as \( X = \kappa_1 [0^+] + \kappa_3 [0^-] \). The hypothesis “\( 0^+ \)” assumes that the scalar Higgs-like boson has only the tree-level SM coupling to \( Z \) bosons. Therefore, for \( D(X; 0^+) \) we obtain:

\[
D(X; 0^+) = \frac{|M(X)|^2}{|M(0^+)|^2} = \kappa_1^2 + \kappa_3^2 \frac{|M(0^-)|^2}{|M(0^+)|^2} + \kappa_1 \kappa_3 \frac{\text{(interference)}}{|M(0^+)|^2}.
\]

By construction, this discriminant takes into account all aspects in which kinematic distributions differ between the two hypotheses, including in particular those associated with the interference between the \( \kappa_1 \) and \( \kappa_3 \) operators in hypothesis “\( X \)”.

Alternatively, one can choose to use the kinematic discriminant \( D(0^-; 0^+) \) [11], where the two hypotheses, “\( 0^- \)” and “\( 0^+ \)”, correspond to the cases where only the \( \kappa_3 \) term or only the \( \kappa_1 \) term are non-vanishing, respectively:

\[
D(0^-; 0^+) = \frac{|M(0^-)|^2}{|M(0^+)|^2}.
\]

Since the two hypotheses from which the discriminant is calculated correspond to two pure states, discriminant \( D(0^-; 0^+) \) is explicitly insensitive to the potential effects on kinematic distributions associated with the interference (unlike discriminant \( D(X; 0^+) \)). The \( D(0^-; 0^+) \) discriminant is optimal for comparing the two pure states or for testing for the presence of an additional pseudoscalar state nearly degenerate with the scalar Higgs-like boson (but with a sufficiently different mass that there is no significant interference in the scalar and pseudoscalar production and decays). However, as it ignores interference effects, it is not optimal for measuring the state \( X \) which couples with \( ZZ \) via both \( \kappa_1 \)- and \( \kappa_3 \)- terms. Discriminant \( D(X; 0^+) \) described above is ideal for this purpose.

E. Statistical analysis

We obtain distributions for the kinematic discriminants described above using simulation. Distributions are obtained for events that correspond to the signal hypothesis “\( X \)”, to the signal hypothesis “\( 0^+ \)” (both described above) and to the background hypothesis. Examples of the distributions, \( pdf(D \mid X + bkg) \) and \( pdf(D \mid 0^+ + bkg) \) are shown in Fig. 5(a).
These kinematic discriminant distributions are then used to construct the test statistic $q$ as follows:

$$q = -2 \ln \frac{\mathcal{L}(\text{"data"} \mid X + \text{bkg})}{\mathcal{L}(\text{"data"} \mid 0^+ + \text{bkg})} = -2 \ln \prod_i \frac{\text{pdf}(D_i \mid X + \text{bkg})}{\text{pdf}(D_i \mid 0^+ + \text{bkg})},$$

where $i$ runs over all the events in a pseudoexperiment. An example of the test statistic distributions obtained with 50000 pseudoexperiments for a particular choice of the integrated luminosity $L$ and $\kappa_3/\kappa_1$ ratio is shown in Fig. 5(b).

To quantify the expected separation power between alternative signal hypotheses, we find a “mid-point” value, $\tilde{q}$, of the test statistic $q$ between the medians of the two test statistic distributions (those generated using each signal hypothesis). We use point $\tilde{q}$ to define two “tail probabilities”, $P(q \geq \tilde{q} \mid X)$ and $P(q \leq \tilde{q} \mid 0^+)$, in such a way that $P(q \geq \tilde{q} \mid X) = P(q \leq \tilde{q} \mid 0^+)$. This tail probability is then converted into significance $\tilde{Z}$ (in $\sigma$) using the one-sided Gaussian tail convention:

$$P = \int_{\tilde{Z}}^{+\infty} \frac{1}{\sqrt{2\pi}} \exp(-x^2/2) \, dx.$$  

(32)

Finally, for the separation power between alternative signal hypotheses we quote $Z = 2\tilde{Z}$, where the extra factor of 2 arises from the fact that the $\tilde{q}$ point is half-way between the
medians of the two distributions. With such a definition, we treat two alternative hypotheses symmetrically and we do not need to generate billions of pseudoexperiments to assess tail probabilities corresponding to $5\sigma$-separations.

The presence of a non-zero value of $\kappa_3$ could be established, albeit with different significances, in searches performed using either $D(X;0^+)\text{ or } D(0^-;0^+)$. The difference in the sensitivity between the two searches is manifested in case the interference between the $\kappa_1$ and $\kappa_3$ operators is present. This is not unlike the actual discovery of the Higgs boson candidate, which gave rise to the $\sim 5\sigma$ signal in the SM Higgs search \cite{2,3} and at the same time was also seen as $\sim 3\sigma$ excesses in the Higgs boson searches performed in the context of the fermiophobic and SM4 scenarios \cite{74}. In case the presence of a non-zero value of $\kappa_3$ is established, the next two questions to answer are:

- whether there is one state $X = \kappa_1[0^+] + \kappa_3[0^-]$ with interference or there are two non-interfering states, scalar $S = \kappa_1[0^+]$ and pseudoscalar $P = \kappa_3[0^-]$;

- if there is interference, how well we can tell apart the relative signs of $\kappa_3$ and $\kappa_1$ couplings.

Both of these questions can be addressed by repeating the statistical analysis with properly adjusted kinematic discriminants. To demonstrate the ability of an experiment to establish the presence or absence of interference, as well as to determine the relative sign of couplings, we plot the per event log likelihood for two particular benchmark points in Figures 6 and 7.

The benchmark point used for Figure 6 (Figure 7) has non-zero values for $\kappa_1$ and $\kappa_2$ ($\kappa_1$ and $\kappa_3$), while the log likelihood is evaluated for various values of the $\kappa_2/\kappa_1(\kappa_3/\kappa_1)$ ratio.

In the absence of interference, the likelihood functions are symmetric under $\kappa_{2,3} \rightarrow -\kappa_{2,3}$. The presence of interference breaks this symmetry and gives one sensitivity to the sign of the couplings. We note that interference between contributions to the amplitude from the $\kappa_1$ and the $\kappa_2$ terms is relatively straightforward to detect, as one would expect from the behavior of the $M_{Z^2}$ distribution discussed above. On the other side, interference involving the $\kappa_1$ and $\kappa_3$ terms will be more challenging to detect. Interestingly, it is significantly easier to determine the correct sign of $\kappa_3$ assuming interference, than it is to determine whether that interference is present.
FIG. 6. The log likelihood per event for various values of $\kappa_2/\kappa_1$ for a particular benchmark point with $(\kappa_1, \kappa_2) \approx (1.77, 4.26)$ (vertical line), which is the point with the same cross section as SM for which $x_1 = x_2$ in the language of Ref. [49]. The quantity on the horizontal axis represents the angle along a circle of constant cross section in $(\kappa_1, \kappa_2)$ space in the absence of interference.

IV. RESULTS

Figure 8(a) presents the expected upper limits on the ratio of couplings $\kappa_3/\kappa_1$ versus the integrated luminosity. Similarly, Fig. 8(b) shows a plot for the expected $5\sigma$-observation sensitivity. Results with both the optimal $D(X; 0^+)$ and the interference-blind $D(0^-; 0^+)$ discriminants are shown. The expected exclusion and observation sensitivities are identical for positive and negative signs of the $\kappa_3/\kappa_1$ ratio. Of course, for a given pseudoexperiment and in the actual LHC running one sign or the other will be preferred by the data.

In Fig. 8(a) and Fig. 8(b) one can see that the sensitivities obtained with the two discriminants scale very differently with integrated luminosity $L$. This is because the $D(0^-; 0^+)$ discriminant does not change when one wishes to probe smaller or larger values of the $\kappa_3/\kappa_1$ ratio. In this case, the sensitivity to $|\kappa_3/\kappa_1|^2$ which is related to the ratio of cross sections...
FIG. 7. The log likelihood per event for various values of $\kappa_3/\kappa_1$ for a particular benchmark point with $(\kappa_1, \kappa_3) = (1/\sqrt{2}, 1/\sqrt{2\gamma_{33}})$ (vertical line), which is the point with the same cross section as the standard model and an angle of $\pi/4$ with respect to the SM axis, along a circle of constant cross section in $(\kappa_1, \kappa_3)$ space.

$\sigma_3/\sigma_1 = \gamma_{33} \kappa_3^2/\kappa_1^2$ scales approximately as $1/\sqrt{L}$. On the other hand, the $D(X; 0^+)$ discriminant is automatically optimized for any given $\kappa_3/\kappa_1$-value probed. For this reason analyses with $D(X; 0^+)$ which probe different fractions of the $0^-$ state can be thought of as separate analyses, and their respective sensitivities to $|\kappa_3/\kappa_1|^2$ at different luminosities do not have to be connected via a simple $1/\sqrt{L}$ relationship.

The difference between the sensitivities obtained with the two discriminants can be quantified in terms of a ratio of integrated luminosities required to achieve the same sensitivity. Figures 8(a) and 8(b) show that this difference grows very large for smaller values of $\kappa_3/\kappa_1$. For example, to probe $\kappa_3/\kappa_1 = 1$, the integrated luminosities needed for a $2\sigma$-separation differ by a factor of 4: $\sim 700$ fb$^{-1}$ with the interference-sensitive $D(X; 0^+)$ discriminant versus $\sim 3000$ fb$^{-1}$ with the interference-blind discriminant $D(0^-; 0^+)$. With $L = 3000$ fb$^{-1}$, the interference-sensitive discriminant $D(X; 0^+)$ allows for reaching a $5\sigma$-sensitivity for
FIG. 8. (a) The integrated luminosity required for an expected 2σ-exclusion of the ratio of couplings \( \kappa_3/\kappa_1 \), provided the data is described by the SM hypothesis. (b) The integrated luminosity required for 5σ-observation sensitivity for the ratio of couplings \( \kappa_3/\kappa_1 \), in the presence of non-zero \( \kappa_3 \). Results with interference-sensitive \( D(X; 0^+) \) and interference-blind \( D(0^-; 0^+) \) discriminants are shown with blue and green curves, respectively.

\[ |\kappa_3/\kappa_1| \sim 1. \] However, at an integrated luminosity of 10 fb\(^{-1}\) which approximately corresponds to 25 fb\(^{-1}\) at 8 TeV, the difference in sensitivities to \( \kappa_3/\kappa_1 \) achievable with the two discriminants is rather modest, \( \mathcal{O}(10\%) \).

Figure 9 shows the expected 2σ-exclusion and 5σ-observation sensitivities for the ratio of couplings \( \kappa_2/\kappa_1 \) vs. the integrated luminosity. In these figures we focus on the \( \kappa_2/\kappa_1 > 0 \) region for which destructive interference is present, as the prospects for early detection are more favorable with this choice of the relative sign of the two couplings. Results with both the optimal \( D(X; 0^+) \), where \( X = \kappa_1 [0^+] + \kappa_2 [0^+_h] \), and interference-blind \( D(0^+_h; 0^+) \) discriminants are shown. As suggested in Eq. (12) above, there is substantial destructive interference in the range of \( \kappa_2/\kappa_1 \approx 2 - 4 \) that leads to dramatic changes in the \( M_{Z_2} \) invariant mass distribution shown in Fig. 3. The kinematic discriminants are automatically sensitive to such changes in the \( M_{Z_2} \) distributions, as well as to changes in other kinematic variables. As a result, it would be relatively easy to differentiate the case where \( \kappa_2/\kappa_1 \) is in this range from the pure SM Higgs-like boson. In fact, since the \( \sim 25 \) fb\(^{-1}\) of 8 TeV data already recorded on tape translates into the \( \sim 10 \) fb\(^{-1}\) of 14 TeV data, we find that the LHC
FIG. 9. (a) The integrated luminosity required for a 95% CL exclusion of the ratio of couplings $\kappa_2/\kappa_1$, provided the data is described by the SM hypothesis. Results with both $D(X; 0^\pm)$, $X = \kappa_1 [0^+] + \kappa_2 [0_h^+]$, and interference-blind $D(0_h^+; 0^\pm)$ discriminants are shown. (b) Luminosity required for a $5\sigma$-observation of a presence of a $J^{CP} = 0_h^-$ state versus assumed ratio of couplings $\kappa_2/\kappa_1$.

experiments should already be able to discover or exclude the $2 < \kappa_2/\kappa_1 < 4$ range. We note also that with existing data there should be a borderline sensitivity for exclusion of the $\kappa_2/\kappa_1 > 4$ range, which includes the case of a pure $0_h^+$ state. This result is well in agreement with the expected sensitivity of $1.8\sigma$ for a 100% pure $0_h^+$ state reported by CMS [11]. The observed limit reported by CMS is 92% CL.

V. SUMMARY

We have considered the important question of how to measure the couplings of the scalar Higgs-like boson, $X$, to two $Z$ bosons. In particular, we have studied the effects of the interference between various $XZZ$ operators, presented the kinematic discriminants that take into account these interference effects, and provided projections for the coupling measurements using these discriminants at the 14 TeV LHC.

We have also compared the sensitivity of these kinematic discriminants with the kinematic discriminants that do not include interference terms and found that incorporating interference effects allows one to significantly improve the sensitivity to states where more
than one operator is present in the $XZZ$ coupling. Depending on the value of the couplings being probed, using analyses that take interference into account may reduce the integrated luminosity required to reach a given sensitivity by as much as a factor of four, as compared with analyses that neglect this interference. Thus using analyses such as those presented may allow one to reach given sensitivity benchmarks at the LHC years earlier than otherwise.

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