Evidence for temporal evolution in the M33 disc as traced by its star clusters

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ABSTRACT
We present precision radial velocities and stellar population parameters for 77 star clusters in the Local Group galaxy M33. Our GTC and WHT observations sample both young, massive clusters and known/candidate globular clusters, spanning ages $\sim 10^5 - 10^{10}$ yr, and metallicities $[\text{M/H}] \sim -1.7$ to solar. The cluster system exhibits an age-metallicity relation; the youngest clusters are the most metal-rich. When compared to HI data, clusters with $[\text{M/H}] \sim -1.0$ and younger than $\sim 4$ Gyr are clearly identified as a disc population. The clusters show evidence for strong time evolution in the disc radial metallicity gradient ($\text{d[M/H]} \text{d}t / \text{d}R = 0.03 \text{dex/kpc/Gyr}$). The oldest clusters have stronger, more negative gradients than the youngest clusters in M33. The clusters also show a clear age-velocity dispersion relation. The line of sight velocity dispersions of the clusters increases with age similar to Milky Way open clusters and stars. The general shape of the relation is reproduced by disc heating simulations, and the similarity between the relations in M33 and the Milky Way suggests that heating by substructure, and cooling of the ISM both play a role in shaping this relation. We identify 12 “classical” GCs, six of which are newly identified GC candidates. The GCs are more metal-rich than Milky Way halo clusters, and show weak rotation. The inner ($R < 4.5$ kpc) GCs exhibit a steep radial metallicity gradient ($\text{d[M/H]} / \text{d}R = -0.29 \pm 0.11 \text{dex/kpc}) and an exponential-like surface density profile. We argue that these inner GCs are thick disc rather than halo objects.

Key words: galaxies: Local Group – galaxies: star clusters

1 INTRODUCTION
Observations suggest that the inner regions of relatively massive disc galaxies contain the oldest stars, and that their scalelengths increase with time (e.g. de Jong 1996). Such galaxies are thought to complete central star formation early, while their outer regions continue to grow as gas at large radii is converted into stars. Although this phenomenon has been known for two decades, it is now generally termed “inside-out” growth (e.g., MacArthur et al. 2004; Williams et al. 2009; Sánchez-Blázquez et al. 2014). The situation for lower-mass discs is less clear. The Large Magellanic Cloud (LMC; $M_\odot \sim 2 - 3 \times 10^9$ M$_\odot$; Kim et al. 1998; van der Marel 2004) - perhaps the best studied example - exhibits young stars that are found to be more centrally concentrated than older stars (e.g. Meschin et al. 2014). However, this may be in part due to its close proximity to the Milky Way, where interaction may act to shrink the star forming HI gas disc over time (Nidever 2014). The intermediate-mass Triangulum galaxy (M33; $M_\odot \sim 3 - 6 \times 10^9$ M$_\odot$; Corbelli 2003) appears to be an admixture of these two mass regimes (e.g., Barker et al. 2007; Williams et al. 2013; Robles-Valdez et al. 2013). The inner disc may form inside-out, and the outer (beyond the truncation radius) disc may form “outside-in”. Due to this dual nature, understanding intermediate-mass discs is of key importance for building a comprehensive understanding of disc formation (e.g. see Gogarten et al. 2010 for the case of NGC 300).

From the point of view of stellar population studies, important observational diagnostics of disc growth and evo-
lution include the age-metallicity relation (AMR) of the disc stellar population(s), their radial age gradients and metallicity gradients (e.g., Freeman & Bland-Hawthorn 2002; MacArthur et al. 2004). For example, one approach to understand disc formation is to study the radial metallicity gradients of disc stars and how these gradients evolve with time. The time evolution of metallicity gradients in discs is important because it is directly linked to disc growth: gradients encode the location and metallicity of gas accreted to the disc. The assumption that stars stay where they were born implicitly or explicitly form part of many chemical evolution models of galaxy discs (e.g. Tinsley et. al. 1974; Matteucci & Francois 1989; Boissier & Prantzos 1999). However, Roškar et al. (2008) have shown that subsequent dynamical evolution of disc stellar populations – such as radial mixing – may flatten out such gradients (but see also Grand, Kawata & Cropper 2013). In addition, radial mixing tends to flatten and create spread in the disc AMR (Roškar et al. 2008; Grand et al. 2014). The lesson here is that, as emphasised for example by Schoenrich & Binney (2009), disc chemistry and disc kinematics cannot be separated if a complete picture of disc formation is to be obtained (a good example of this approach is the CALIFA survey – see e.g., Sánchez-Blázquez et al. 2014).

In terms of kinematics, an important time-dependent diagnostic of disc formation is the age-velocity dispersion relation. The velocity dispersion of disc stars in the Milky Way increases with age (e.g. Holmberg et al. 2007; Soubirous et al. 2008; Aumer & Binney 2009) and recent work suggest this is also the case in M31 (Dorman et al. 2015). The origin of these relations is still unclear, but might arise due to either disc heating processes (e.g. Spitzer & Schwarzschild 1951; Wielen 1977; Mihos & Hernquist 1996; Minchev & Quillen 2006; Hänninen & Flynn 2002; Martig, Minchev & Flynn 2014), or the different kinematical properties of gas at the time of star formation (e.g. Brook et al. 2004; Bournaud, Elmegreen & Martig 2009; Bird et al. 2013), or some combination of the two mechanisms.

Observationally, one way of studying the time evolution of disc populations is to go to high redshift. For example, Yuan et al. (2011) studied the HII regions of a lensed disc galaxy at $z = 1.49$ and found a negative metallicity gradient more than ten times steeper than nearby systems - suggestive that metallicity gradients may flatten over time. However, major difficulties in this approach are that at $z > 1$ discs subtend only a few arcseconds. The information obtained from such studies is limited by the small spatial scales and faintness of these systems.

An alternative approach is to study nearby discs in detail, and compare the properties obtained from stellar populations that trace different epochs of star formation. Chemical abundances for massive (OB) stars are feasible for the nearest galaxies (e.g. Urbanajca et al. 2005; Esteban et al. 2009), while studies of more evolved populations have concentrated on bright emission lines from Planetary Nebula (e.g. Magrini et al. 2004), or on RGB stars for the very nearest systems (e.g., Kalirai et al. 2006; Leaman et al. 2009; Carrera et al 2011). While extremely useful, these tracer populations generally represent stellar populations with a limited range of (or poorly constrained) ages. For example, OB stars have lifetimes of $\sim$Myr and therefore reflect very recent star formation. In contrast PNe and RGB stars can span a wide range of ages, but their precise ages are hard to constrain - particularly for the oldest populations.

In contrast, star clusters in late-type galaxies exhibit a wide range of ages, from very young, massive clusters up to GC ages, present the opportunity to study disc evolution and kinematics over the whole lifetime of the galaxy (e.g., Huchra, Brodie & Kent 1991; Chandar et al. 2002; Schroder et al. 2002; Beasley et al. 2004; Bridges et al. 2007; Caldwell et al. 2011). In addition, star clusters can, in principle, have their ages and metallicities determined via studies of their resolved stars, or through integrated light techniques.

Here we present the first results of a spectroscopic campaign to characterise the star cluster system of M33. Due to its mass and proximity, M33 presents an important laboratory for understanding the formation of disc galaxies, and addressing some of the above issues. M33 is an intermediate mass ($M_* \sim 3 - 6 \times 10^9 M_\odot$; Corbelli 2003) disc system with a minimal bulge component (e.g. Regan & Vogel 1994). Its proximity (847±60 kpc; Galleti, Bellazzini & Ferraro 2004) and favourable inclination angle ($i = 56^\circ$; Faturel et al. 2003) make the galaxy an ideal target for understanding the disc ISM and its stellar populations. Star formation histories have been obtained for M33 based on both small-area, deep HST photometry (e.g. Barker et al. 2007; Williams et al. 2009) and on wider-field, but shallower studies (e.g., Davidge & Puzia 2011).

The star cluster system of M33 has been previously studied by a number of authors (see Hodge 2011 for a review). Notable imaging campaigns include those of Hiltner (1960), Christian & Schommer (1982), Chandar, Bianchi & Ford 1999, Sarajedini & Mancone (2007), Park & Lee (2007) and San Roman, Sarajedini & Aparicio (2010). In total, some ~600 cluster candidates have been identified. Spectroscopically, the M33 star clusters have been studied by Schommer et al. (1991), Chandar et al. (2002; hereafter CBFS02), Chandar et al. (2006) and Sharina et al. (2010). CBFS02 presented the most detailed kinematic study to date. They obtained velocities and estimated ages from a combination of integrated spectroscopy and integrated colours for 107 M33 star clusters and were able to separate the cluster system into two populations: a young population with disc kinematics and an older population with kinematics consistent with a halo cluster system. They also argued for an age spread of ~6 Gyr amongst the halo population. However, CBFS02 did not derive metallicities for their cluster sample and most ages came from integrated colours which are strongly affected by age-metallicity degeneracy.

In the following, we use the term star clusters to refer to stellar clusters as a general class (open, massive and globular), referring to globular clusters in the classical sense as the analogues of the Milky Way GCs. We assume a distance of 847 kpc to M33 (Galleti et al. 2004) for all conversions to physical distances and an optical disc scale of 9.2 arcminutes (Guidoni et al. 1981) which corresponds to 2.3 kpc at our adopted distance. In Section 2 we describe our observations and data reduction procedure. In Section 3 we show how cluster radial velocities and stellar population properties are derived. In Section 4 we discuss our results for the

1 http://www.mancone.net/m33_catalog/
stellar population properties and kinematics of the M33 star clusters. We summarise and discuss our findings in Section 5.

2 THE DATA

2.1 The cluster sample and methodology

Our observing strategy consisted of using the WYFFOS/AF2 multifibre spectrograph (Watson 1995; Bridges 1998) on the William Herschel Telescope (WHT) to focus on the brightest M33 clusters, and OSIRIS (Cepa et al. 2000) in longslit mode on the Gran Telescopio de Canarias (GTC) to cover the fainter end of the luminosity function. Our star cluster sample was chosen from the updated version catalogue of Sarajedini & Mancone (2007) in addition to the newer catalogue of San Roman et al. (2010). The clusters were selected in order to cover as much of the optical disc as possible. All the targets possess accurate positions and integrated magnitudes based on HST and/or ground-based observations.

The GTC sample consists of confirmed clusters (from high resolution imaging or spectroscopy) with $g_t > 19$. The WHT observations prioritize the observations of bright confirmed clusters ($g_t < 19$), but to maximize the number of fibres used in each exposure, these requirements were relaxed and extra fibres were allocated for less certain, fainter candidate clusters. This potentially introduced some contamination into the sample (see Section 3.1).

We also included in the sample several objects to be used as radial velocity templates (but see Section 3.1). The M33 nucleus was observed as a template for young clusters while known GCs R12=SR1710−SM316 and R14=SR1765−SM275 (Sarajedini et al. 1998; Larsen et al. 2002) were observed as more appropriate templates for older objects. In addition, clusters M9=SR2075−SM402, U49=SR1458−SM178 and H38=SR1566−SM206 (from the same studies) were included as scientifically interesting cases based on their similarities to Milky Way GCs.

2.1.1 GTC data

Previously confirmed candidates (identified by radial velocities or high resolution imaging) were observed using OSIRIS on the Gran Telescopio de Canarias (GTC) in long-slit mode during semesters 2010B−2012A. A R2500V grism was used yielding an effective wavelength range of 4500–5600 Å. A slit-width of 1.0 arcsec was used in all cases yielding a final spectral resolution (FWHM) of 2.1 Å. In general, two objects were placed on each slit with the exception of one observing block where 3 objects were placed on the slit. Integration times were 900−5400s per object (depending upon the target magnitude) and we observed a total of 53 unique star clusters and obtained useable spectra for 48. A summary of the GTC observations is given in Table 1.

Basic reductions were performed using the OOPS OSIRIS data reduction pipeline written in PyRAF. These data were debiased, flat-fielded and wavelength solutions obtained using 20 to 30 Xenon, Neon and Argon arclines. Typical residuals to the wavelength solution were 0.08 Å. For some spectra we noticed that the 5577.34 Å skyline was shifted by up to 0.2 Å from the rest frame value, and in these cases we shifted the spectra in wavelength to the correct value. The final extraction of the 1-d spectra was performed using APALL in pyRAF. The spectra were flux-calibrated using the standards L1363-3 and BD28+4211 and with tasks STANDARD, SENSFUNC and RESPONSE also in pyRAF. The final, extracted spectra have a median S/N of 40 per Å.

2.1.2 WHT data

Previously identified star clusters, and star cluster candidates identified by San Roman et al. (2010) were observed using the WYFFOS/AF2 multifibre instrument on the William Herschel Telescope in La Palma. WYFFOS/AF2 allows for the allocation of up to 160 fibres over a 40 arcminute field of view. Two fibre configurations were observed over a total of five nights of observations, one configuration during the nights of 7−8 October and 8 November 2010, the second configuration during the nights of 23 and 24 October 2011. We used the 1200B grism which gave a useful spectral range of 4000−5500 Å and a spectral resolution of 2.1 Å (FWHM). A summary of the WHT observations is given in Table 1.

In order to maximise the number of clusters observed with the WHT, and taking into account fibre positioning limitations, we used different fibre configurations. Half of the fibres were allocated in both configurations to observe the faintest objects of the WHT sample; the remaining fibres were used for the brightest objects. Each WYFFOS/AF2 fibre has a 1.6 arcsecond diameter, similar to the size of the star clusters ($0.8 < r < 2.0$ arcseconds), thereby minimizing any loss of light. Few of these objects have previous velocity measurements.

Because the M33 disc provides a bright and variable background emission, estimations of the underlying galaxy light should be performed as locally as possible. For this reason, the observations were taken in a "beam-switching" mode, with three 15 minute off-source integrations (offset from the objects by 10 arcseconds to the north, west and east) interspersed within the 30 minute integrations on the clusters. Dedicated sky fibers were also placed across the field to check the background level. Comparison of the sky residuals indicated that the offset sky fibres gave better results (smaller sky residuals) than the dedicated sky fibres and therefore we used these to remove the sky contribution. The rms difference in the sky level across the sky fibres, after removing those fibres that fell on bright sources in the offset skies, was typically 10–15 percent. For the brightest targets, the sky background comprised $\sim 5$ percent of the total light down the fibre, rising to $\sim 25$ percent for the faintest objects. These data were reduced using the dedicated IDL WYFFOS/AF2 reduction pipeline (v1.02). The software performs bias subtraction, flat-field corrections using sky-flats and allows for the determination of the wavelength solution. For this we used Helium and Neon arc lines which gave typical residuals of 0.1 Å. Finally, a relative flux calibration was obtained using the standard BD+28 4211.

The final, extracted spectra have a median S/N of 20 per Å. A number of the spectra have significantly lower (typically a factor of 2 lower) S/N than expected based on the WYFFOS/AF2 ITC. We attribute this to problems with fibre positioning known to affect the instrument prior to the 2013 upgrade. After merging overlapping objects in the
Table 1. The instrumental setups for spectroscopy.

| Telescope       | GTC 10.4 m         |
|-----------------|--------------------|
| Instrument      | OSIRIS longslit    |
|                 | mode (1' slit)     |
| Dates           | queue mode        |
|                 | semesters 2010B−2012A |
| VPH grating     | 2500V              |
| Spectral range  | 4500–6000 Å       |
| Dispersion      | 0.80 Åpixel⁻¹     |
| Resolution (FWHM)| ~ 2.1 Å           |
| Detector        | 2 Marconi CCD42-82 |
|                 | (2048 × 4096 pixels) |
| Gain            | 0.95 e− ADU⁻¹     |
| Readout noise   | ~ 4.5 e−           |
| Seeing          | 0.8–1.2′          |

| Telescope       | WHT 4.2 m         |
|-----------------|--------------------|
| Instrument      | AF2 multifibre     |
|                 | spectrograph (1.6′ fibre) |
| Dates           | 7 – 8 Oct., 8 Nov. 2010, 23 – 24 Oct. 2011 |
| Grating         | 1200B              |
| Spectral range  | 4575–6000 Å       |
| Dispersion      | 0.43 Åpixel⁻¹     |
| Resolution (FWHM)| ~ 2.1 Å           |
| Detector        | 2 EGV-42-80        |
|                 | (4096 × 4096 pixels) |
| Gain            | 0.90 e− ADU⁻¹     |
| Readout noise   | ~ 4.2 e−           |
| Seeing          | 0.9–1.4′           |

WHT samples, we obtained a total of 61 spectra for which we could measure radial velocities of which 29 spectra have sufficient S/N for stellar population analysis.

3 ANALYSIS

3.1 Radial Velocities

Radial velocities for the star clusters and cluster candidates were determined by fourier cross-correlation using FXCOR in pyIRAF. For cross-correlation templates, we used a total of 350 MILES model SEDs (Vazdekis et al. 2010) in the age range 63 Myr to 17 Gyr and metallicity ([M/H]) range −2.3 to +0.2. The resolution of our data (~ 2.1 Å FWHM) is slightly higher than that of MILES (2.5 Å FWHM) and so we rebinned our spectra in order to match resolutions for cross-correlation. Despite the mild degradation in spectral resolution, tests showed that this turned out to be a better approach than using the template stars we observed at the native WHT and GTC resolutions. Even though, in principle, the slightly higher native spectral resolution should give higher velocity precision, in practice a lack of a wide range of adequate templates can prevent this precision from being achieved. This template mismatch problem is particularly acute for a cluster system such as M33 that has a very wide range of ages and metallicities (see Section 3.3). The best-fitting MILES templates provided significantly better (higher) normalised cross-correlation peaks than the best-fitting observed template stars. Therefore for each cluster we took the velocity returned for the best-fitting MILES SED as our final velocity. Heliocentric corrections were then applied to these velocities.

We assessed both the precision and accuracy of our velocities via run-to-run comparisons and through comparisons with literature values (Figure 1). For velocities with FXCOR Tonry & Davis (1979) $R$ values of $R \geq 15$ the agreement is good between different WHT runs with mean differences of 6.5 km/s (2.0 km/s) and rms 5.6 km/s (5.4 km/s) for the October/November 2010 (October 2011) observations and we take $R = 15$ (corresponding approximately to S/N ~ 10 per A in these data) as the lower limit for reliable velocities for these data. For the GTC observations there are unfortunately few (4) overlapping velocities with the WHT sample with which to check our velocities. However, we find 16 GTC velocities and 4 WHT velocities in common with those obtained by CBFS02. Comparisons between the combined GTC+WHT data with those of CBFS02 are shown in the bottom panels of Figure 1. Comparing all the clusters in common we find an offset of us - CBFS02 of +1.7 km/s.

Figure 1. Comparison of cluster velocities in common between different observing runs on the WHT (top panels) and for clusters in common with CBFS02 (bottom panels). Solid lines have unit slope in all cases.

Based on these comparisons we conclude that there is good velocity consistency both within our dataset, and between our dataset and that of CBFS02. The mean velocity uncertainty of our dataset is 9.0 km/s with a standard deviation of 5.4 km/s.

3.2 Star Cluster Identification

All the GTC targets are genuine star clusters in M33, identified either in high-resolution ground-based imaging, from HST observations, or spectroscopically. The WHT targets contain a mix of known and candidate star clusters and in these data we expected some level of contamination from foreground stars. Clusters in the M33 disc are expected to follow the HI rotation (e.g., Schommer et al. 1992; CBFS02) and therefore are kinematically separable from Milky Way halo stars based on their well-defined velocity distribution and similarity to the disc rotation solution. However, any
clusters in M33 belonging to kinematically hotter populations (e.g., thick disc, halo) are expected to have a broader distribution of radial velocities.

Therefore, we visually inspected all the candidate WHT spectra to look for interloping foreground stars. A number of objects were unambiguously identified as foreground stars based on either the presence of very strong molecular features (e.g., CN, CH, TiO), or on atomic lines (e.g. NaD) much stronger than expected for star clusters. All these objects have $v_{\text{helio}} > -100$ km/s, and we classify them as stars and do not consider them further in this analysis. Five cluster candidates (WHT-72, WHT-84, WHT-286, WHT-318 and WHT-402) have spectra resembling old GCs and velocities which are consistent with kinematically hot M33 stellar population or low velocity foreground stars. Based on the above and their non-stellar appearance on ground based imaging we tentatively classify these as GCs. An additional candidate (WHT-323) has $v_{\text{helio}} = -160 \pm 4$ and we also consider this a good GC candidate.

The velocity histograms of the GTC and cleaned WHT samples are shown in Figure 2. For comparison, we show the cluster velocities from the sample of CBFS02. The GTC+WHT velocities occupy a velocity range similar to that of CBFS02, but it is possible that we are missing some of the lowest velocity clusters. Whether this is real or a result of our candidate selection is unclear. The GTC velocities show a wide range consistent with a disc population.

In total, we identify 77 clusters suitable for stellar population analysis and their basic properties are listed in Table 2.

3.3 Stellar population analysis

To estimate the ages and metallicities of the star clusters we primarily used the Vazdekis et al. (2010) stellar population models based on the MILES empirical stellar library of Sánchez Blázquez (2006) (hereafter the MILES model[1]). The youngest age predicted by the MILES models (version 9.0), based on the Padova isochrones (Girardi et al. 2000), is 63 Myr. We expected clusters younger than this in our sample and in order to model these younger clusters we extended the MILES parameter space with the models of González Delgado (2005; hereafter GD05). The GD05 models extend to 1 Myr ages through the use of theoretical libraries and allowed us to probe the full expected age range of the M33 cluster system. The GD05 models also extend to older ages, but for ages greater than 63 Myr we prefer to use models based upon empirical rather than theoretical libraries.

Stellar population parameters were estimated using the ULySS (Koleva et al. 2009) IDL code which performs full spectrum fitting in pixel space to the observed spectrum using model templates. The code minimises the $\chi^2$ between object and template represented by a linear combination of non-linear model components. We adopted a full spectral fitting approach instead of using index-index plots in order to make full use of the spectral information at hand. In comparison with indices, full spectral fitting can maximize the information available in the spectrum, at the potential expense of complicating the interpretation of the results and estimation of uncertainties. This approach proved particularly useful for the younger clusters in our sample. For ages < 100 Myr by far the most prominent feature in our optical spectra is the balmer H$\beta$ absorption line (and H$\alpha$ lines for very young clusters). Metal lines (iron, magnesium etc) are quite weak in integrated spectra at these young ages meaning that individual measurements of these lines can have large uncertainties even for relatively high S/N spectra.

For each cluster we allowed ULySS to search through a grid of MILES + GD05 SSP models, calculate and locate the minimum $\chi^2$ as a function of age and metallicity. Prior to these fits, we determined the "line spread function" of the GTC and WHT using several stellar templates observed as radial velocity standards (see Koleva et al. 2009). We did not attempt to fit for $\alpha$/Fe abundances because the majority of star clusters are at young ages where spectral differences attributable to varying $[\alpha$/Fe] are minimal (Vazdekis et al. 2015). In addition, we did not explore in detail the possibility that some of the star clusters may have multiple stellar populations with different ages (e.g. Milone et al. 2015). We plan to explore this issue in future work. For each best-fit solution, we visually examined the spectrum, the residuals between the observed and model template spectrum, and the 2-dimensional $\chi^2$ maps produced by the code. In most cases, ULySS correctly identified the best-fit template and the residuals were of order of a few percent around most spectral features. Examples of a $\chi^2$ map and the best solutions for the GTC spectrum of GC U49 are given in Figures 3 and 4. ULySS correctly selects the true minimum based on the $\chi^2$ contours.

However, in some situations the H$\beta$ line was clearly over/under fit and checking the $\chi^2$ maps showed that ULySS had settled either on a “false minimum”, or had selected the true minimum but favoured a lower metallicity and a higher age than otherwise suggested by inspection of the H$\beta$ line (a manifestation of the age-metallicity degeneracy). In the case...
Table 2. Basic and derived data for M33 cluster sample. Full table available online. IDs are from San Roman et al. (2010).

| ID   | RA (J2000) | Dec (J2000) | Age  | [M/H] | $V_{\text{helio}}$ | $V_{\text{HI}}$ | PA   | notes       |
|------|------------|-------------|------|-------|-------------------|-----------------|------|-------------|
|      | (hh mm ss) | (dd mm ss)  | (Gyr)| (dex) | (km/s)            | (km/s)         | (degrees) |             |
| 856  | 1 32 55.39 | +30 38 38.57| 3.845 ± 0.924 | −1.21 ± 0.19 | −130 ± 12        | −148           | 266.0 |             |
| 902  | 1 32 59.90 | +30 27 19.92| 0.281 ± 0.105 | −0.03 ± 0.25  | −62 ± 24         | −108           | 226.1 |             |
| 941  | 1 33 6.88  | +30 41 3.46 | 1.165 ± 0.457 | −0.45 ± 0.26  | −171 ± 11        | −164           | 277.5 |             |
| 1066 | 1 33 16.06 | +30 20 56.66| 0.19 ± 0.032  | −0.1 ± 0.17   | −70 ± 7          | −101           | 205.1 |             |
| 1115 | 1 33 20.53 | +30 49 1.52 | 9.967 ± 1.528 | −1.13 ± 0.17  | −160 ± 4         | −221           | 321.0 | GC candidate|
| 1133 | 1 33 22.13 | +30 40 25.80| 0.019 ± 0.003 | −0.16 ± 0.16  | −160 ± 8         | −165           | 276.5 | young, HeI   |

Figure 3. Top panel: comparison of the observed spectrum of cluster S2916 (U49) (black line) compared to the best model SED (blue line). The cyan curve represents the flux ratio between the models and observation. Bottom panel: Residuals from division of the GTC spectrum of the cluster by the best fitting SED. In this example of a good fit, residuals are of order ~ 2 percent. The green lines represent the mean and standard deviation of the residuals.

of poor fits, we re-ran ULySS restricting the age-metallicity parameter space to what we considered best described the cluster under consideration based on spectral features such as the width of Hβ, the presence (or lack of) HeI lines and the continuum shape of the cluster. Examples of our spectra with a range of ages are shown in Figure 5. In most cases, ages of < 100 Myr were indicated by the presence of HeI lines ($\lambda\lambda 4712$ Å and 4920 Å) originating in hot stars ($T \geq 15,000$ K), and very blue continua with a few weak metal-lines (we identified no clusters with HeII lines indicative of ~ 10 Myr ages). Older (100 Myr–1 Gyr) clusters also show broad Hβ lines and blue continua, but with increasingly strong metal lines (e.g., Mg at $\lambda 5170$ Å) and no HeI lines present. For clusters older than ~ 1 Gyr, metal-lines strengthen further, the Hβ line becomes increasingly narrow and the continuum reddens (to an extent dependent upon the metallicity of the cluster). These considerations highlight the need for manual supervision while applying this type of full spectrum fitting techniques to star cluster spectra.

Uncertainties in ages and metallicities were determined from Monte Carlo simulations implemented in ULySS. For

Figure 4. Map of $\chi^2$ values for the range of ages and metallicities in the MILES models as determined by ULySS. The best solution lies at ~ 10 Gyr ages and [M/H] = −1.3. However, another ("false minimum") solution lies at similar metallicities but ~ 100 Myr ages. In this case ULySS has correctly identified the true minimum. Metal-rich solutions at all ages are rejected.

Figure 5. Example spectra of M33 clusters spanning a range of ages, from ~20 Myr to 12 Gyr. The spectra have been offset by a constant in flux for display purposes. Very blue continua, strong and broad Hβ lines and HeI lines are evident in the youngest clusters. Older clusters show redder continua and more prominent metal lines.
each spectrum, ULySS produces 100 synthetic spectra with S/N corresponding to the input spectrum generated using Poisson statistics and a random seed. ULySS was then run to find the best fit age and metallicity for each spectrum, and the uncertainties in age and metallicity were taken to be the standard deviation on the mean of the distributions of these parameters. Typical uncertainties are \(\sim 30\) percent in age and \(\sim 0.2\) dex in metallicity for a median S/N of \(\sim 30\) per Å, characteristic of this sort of analysis (see e.g., Wolf et al. 2007, As’ad et al. 2013). Note that the uncertainties given here account for the statistical errors based on the S/N of the spectra, and do not include systematic errors due to our choice of stellar population models.

One sanity check of our age determinations is to compare the ages from ULySS with those of the single-index model predictions for H\(\beta\). This comparison is shown in Figure 4. Both the models and spectra have been smoothed to a common dispersion of 5 Å in this case - the resolution for star cluster comparisons suggested in Vazdekis et al. (2010). The strength of the balmer lines in young stellar populations increase as a function of increasing age until \(\sim 400\) Myr as A stars come to dominate the integrated spectrum (e.g. GD05). At older ages, the balmer lines then decline in strength as the main-sequence turn-off moves to lower temperatures. The models and data clearly show this behaviour Figure 4. The cluster data follows the overall behaviour of the models as a function of age. Clearly the two measurements are not independent - the ages come from full spectrum fitting which include H\(\beta\) which is often the strongest line in the integrated spectrum - but the agreement is reassuring. In terms of the model predictions, there is a discontinuity at \(63\) Myr. This is the age representing the lower age limit of the Padova-based MILES models and where we use the GD05 models to predict ages and metallicities for the youngest clusters. A rescaling of the GD05 ages in this region (for example) by \(\sim 15\) Myr to older ages would bring better agreement with the MILES models in terms of the H\(\beta\) index, although we have not done this here since the origin of this offset is not clear.

Our final age and metallicity estimates with their associated uncertainties are given in Table 2.

4 PROPERTIES OF THE M33 CLUSTER SYSTEM

We first broadly characterised the M33 cluster sample based on their stellar population properties. The distributions in age and metallicity of the cluster samples, determined from our stellar population analysis, are shown in Figures 7 and 8. The clusters exhibit a range of ages, from very young \(\sim 10\) Myr objects to \(\sim 13\) Gyr old globular cluster-like ages. Some 61 percent (47/77) of the sample is younger than 1 Gyr. Based on the present data, M33 seems to have produced clusters throughout its lifetime. The relative lack of clusters between 3-9 Gyr may be due to a decrease in cluster formation at this epoch, or increase in cluster destruction. A more complete spectroscopic sample will be required to explore the reality of this age gap.

In terms of metallicity (Figure 8), the clusters show a wide distribution \((-1.74 < [M/H] < 0.18)\) with clusters younger than 1 Gyr being more metal-rich ([M/H] > –1.0). This suggests a distinct age-metallicity relation for the clusters which we discuss in more detail in Section 5.1. The metallicities of the youngest clusters are very similar to those found by Urbaneja et al. (2005) for a sample of 11 B-type supergiants determined from spectral synthesis ([M/H] = –0.14, \(\sigma_{[M/H]} = 0.17\)). These massive stars with main-sequence lifetimes of \(\sim\)Myr constitute a metal-
rich disc population in M33. For very young clusters (< 100 Myr), metallicities from integrated spectra are least well constrained since metallic features are weak compared to the Balmer series (this reduced metallicity sensitivity is indicated by the convergence of the lines of metallicity in the AMR of stellar population is an important observational constraint on chemical evolution models. Age-metallicity relations in the M33 disc

4.1 Age-metallicity relations in the M33 disc

The AMR of stellar population is an important observational constraint on chemical evolution models. Age-metallicity plots of the M33 clusters are shown in Figures 11 and 12. Mean ages and metallicities for the young, intermediate-young, intermediate and old subgroups are listed in Table 3. The uncertainties in age and metallicity are the standard deviations on the mean values.

Figures 11 and 12 show that there is a clear AMR in the cluster sample in the sense that older clusters are, on average, more metal-poor than younger clusters. Clusters younger than ~300 Myr show an approximately constant
Figure 10. The projected spatial distributions of the sample of 77 star clusters in M33 compared to a FUV GALEX image of the galaxy. The clusters have been separated into four subgroups based upon their ages: red circles: $t < 150$ Myr, green triangles: 150 Myr – 1 Gyr, blue squares: 1–4 Gyr, yellow stars: $> 4$ Gyr. Our sample is clearly confined (in projection) to the UV/optical disc of M33.

Metallicity of $\sim [\text{M}/\text{H}] = -0.2 \pm 0.17$ This is consistent with the metallicities found for OB stars in the M33 disc (Urbaneja et al. 2005) as mentioned previously. Older clusters become progressively more metal-poor until the oldest clusters seem to either depart from the AMR, or show a larger scatter in metallicity ($\sigma_{\text{M/H}} = 0.31$ for a given age) than the younger clusters. As we show in Section 4.4 this seems to coincide with a transition from rotation-dominated kinematics to more dispersion-dominated kinematics. Monte Carlo simulations indicate that the typical (statistical) uncertainty in our metallicities is $\sim 0.22$ dex for both the MILES and GD05 stellar population models. We calculated the dispersions in metallicity of the age subgroups (by first fitting and subtracting a 3rd order polynomial fit to the AMR) and find dispersions of 0.17 dex (young subgroup), 0.19 dex (intermediate-young), 0.31 dex (intermediate age) and 0.31 dex (oldest clusters). Subtracting our observational errors in quadrature from these dispersions we find that the intrinsic metallicity spread in the clusters cannot be more than $\sim 0.25$ dex at most, and for the two youngest cluster bins is equal to or less than our 0.2 dex metallicity uncertainties.

4 It is not clear whether the apparent age gap at $\sim 50$ Myr is real, or rather reflects the difference in apparent age zero-points between the MILES and GD05 models.

Also shown in Figure 11 are chemical evolution models from Barker & Sarajedini (2007) which were explicitly
modeled for the M33 disc. Qualitatively the agreement between the model and cluster AMRs is reasonable, although it is clear that for ages younger than 5 Gyr the modeled AMR is flatter than the cluster AMR. However, it should be noted that this comparison is not entirely appropriate since the Barker & Sarajedini (2007) modeled an observed CMD ~9 kpc from the galaxy centre, whereas the majority of our clusters lie within 6 kpc from the centre of M33.

4.2 Spatial distributions of the M33 clusters

The deprojected radii of the clusters are shown as a function of their ages and metallicities in Figure 13. No clusters younger than ~ 100 Myr are found beyond a projected radius of 4 kpc in our sample. More generally, the spatial distributions of youngest clusters show a mild tendency to be more centrally concentrated than the older clusters. The mean radius of each of the cluster age groups is given in Table 4 illustrating this trend.

Deprojected surface density profiles of the cluster subgroups are shown in Figure 14. These density profiles are compared to an exponential profile \( N(R) \propto e^{-R} \), which might be expected for disc stellar populations, and a power-law relation \( N(R) \propto R^{-1} \) the expectation for an isothermal sphere. The clusters, in general, exhibit profiles which are more similar to exponential distributions than power-law distributions, i.e. the clusters have spatial distributions more consistent with that expected of disc rather than spheroidal populations. Interestingly, and although limited by small numbers, the profiles for the two oldest cluster groups are suggestive of exponential profiles within \( R \sim 4.5 \) kpc (i.e., within approximately two optical disc scale-lengths) but then appear to flatten beyond this radius. The hint of an exponential surface density profile for the oldest clusters in our sample within \( R \sim 4.5 \) kpc is both intriguing and unexpected. We return to this issue shortly.

4.3 Metallicity gradients in the M33 disc

The disc radial metallicity gradient, and any evolution (or lack thereof) of this gradient places important constraints on disc formation models (e.g., Chiosi 1980; Boissier & Prantzos 1999; Cioni 2009; Marcon-Uchida, Matteucci & Costa 2010; Gibson et al. 2013). We explored the M33 disc metallicity gradient as traced by its star clusters in our data. Since the inclination and position angle of the semi-major axis of M33 is known, we can explore the behaviour of the cluster metallicities as a function of deprojected radius. To deproject the clusters into the plane of the galaxy we assumed an inclination angle to the line of sight of \( i = 56 \) degrees.
(Paturel et al. 2003) and a position angle for the major axis of $\phi = 22$ degrees (Warner, Wright & Baldwin 1973). The metallicities of the three youngest cluster groups are plotted as a function of deprojected radius in Figure 15.

For each cluster subgroup we performed weighted linear least-squares fits with radius as the explanatory variable. The results of these fits (gradient, intercept) are given in Table 3. We estimated confidence intervals (10 and 90 percentiles of the distributions) and uncertainties on the gradients by running 1,000 Monte Carlo (bootstrap with replacement) simulations. Our fits and confidence intervals are shown in the lower panel of Figure 15. For the two youngest cluster subgroups we identify mildly positive radial metallicity gradients. The youngest subgroup has formally a steeper positive gradient (d[M/H]/dR = $0.045 \pm 0.033$ dex/kpc) than the 150 Myr–1 Gyr group (+0.024 ± 0.035). However, within our confidence intervals the two distributions are quite similar. For clusters in the 1 – 4 Gyr age group, we find a negative radial gradient ($-0.054 \pm 0.046$ dex/kpc). I.e., the gradients of the cluster populations show a tendency to become less negative with time. Combining the three youngest cluster groups, we find a gradient of ($-0.026 \pm 0.038$ dex/kpc) in the disc clusters. By comparison, Frinchaboy et al. (2013) find a gradient of $-0.09 \pm 0.03$ dex/kpc for open clusters within a galactocentric radius of 10 kpc in the Milky Way. Steeper gradients have been found by Urbaneja et al. (2005) for supergiant stars in M33 (our fits to the Urbaneja et al. data : $-0.057 \pm 0.025$). These gradients are also similar to the median [O/H] gradient measured for nearby isolated late-type spirals ($-0.041 \pm 0.009$ dex/kpc; Rupke, Kewley & Chien 2010) and are consistent with our data.

We also show metallicity as a function of radius for the oldest clusters (>4 Gyr) in Figure 15. A linear least-squares fit yields a gradient of d[M/H]/dR = $0.04 \pm 0.06$ dex/kpc for these clusters (for clarity we do not show the confidence limits on this fit in Figure 15). However, inspection of Figure 15 shows curious behaviour; the inner clusters ($R < 4.5$ kpc) exhibit a steep negative gradient, while clusters beyond this show a flatter relation (with significant scatter). The gradient for the $R < 4.5$ kpc clusters is $-0.29 \pm 0.11$ dex/kpc. That is, there appears to be a break in the metallicity gradient of the oldest clusters at about $R \sim 4.5$ kpc. Interestingly, this is also the location where the oldest clusters, and the 1–4 Gyr cluster group, show a hint of a transition from an exponential distribution to a flatter (power-law like) distribution (see Figure 15). One possibility is that we are seeing a superposition of two old cluster populations in M33, a disc-like inner population and a more spherically distributed outer population. We return to this issue in more detail in Section 4.6.1.

Returning to the M33 cluster sample as a whole, while larger samples would be desirable to confirm the trends, our data does suggest an evolution of the M33 metallicity gradient in the sense that the gradient has flattened (or rather, become less negative) with time. This is in qualitative agreement with higher redshift systems. Not only are discs expected to undergo significant size evolution with time (in the sense that discs are smaller at higher redshifts; e.g. Brooks et al. 2010), also radial metallicity gradients of higher redshift systems seem to be steeper than those observed locally. For example Yuan et al. (2011) claim a measurement of a metallicity gradient for a lensed grand-design spiral at $z = 1.49$ ($\sim 9.3$ Gyr for $H_0 = 70$, $\Omega_M = 0.3$, $\Omega_z = 0.7$) based on HII regions. These authors obtain an extremely steep gradient in [O/H] ($-0.16 \pm 0.02$ dex/kpc) in a system with a dynamical mass of $1.3 \pm 0.2 \times 10^{10} M_\odot$ (within 2.5 kpc). Interestingly, Jones et al. (2010) claim an even steeper metallicity gradient in a lensed galaxy at $z = 2$ (the so-called “Clone arc”) finding $-0.27 \pm 0.05$ dex/kpc in an even more massive system ($\sim 2.4 \times 10^{10} M_\odot$, within 2.9 kpc).

We compare the measured evolution of the M33 metallicity gradient for our star cluster sample with data from other tracers of gradients in M33 and also high redshift systems in Figure 15. For M33, data for OB stars comes from Urbaneja et al. (2005), HII and PNe from Bresolin et al. (2010) and Magrini, Stanghellini and Villaver (2009) and CMD-based estimates of metallicity from Tiede, Sarajedini and Clark (1998). Data for high-redshift discs comes from Yuan et al. (2011) and Jones et al. (2013) (see above). Note that the emission-line data (for HII, PNe and the high redshift systems) measure [O/H] rather than [Fe/H] (or total metallicity [M/H]). We make the assumption that, in terms of gradients, these quantities track each other to first order.

In terms of the M33 data there is some disagreement as

5 Caveats include that these high-redshift systems will presumably evolve to be significantly more massive than M33. In addition, the high-redshift observations measure gas abundances whereas our gradients are derived from the metals already locked up in stars.
Figure 15. Radial metallicity gradients of the M33 clusters. Top panel: metallicities of the clusters as a function of deprojected galactocentric radius. The clusters are binned as a function of age: red circles: t < 150 Myr, green triangles: 150 Myr − 1 Gyr, blue squares: 1−4 Gyr, black diamonds: >4 Gyr. Lower panel: Gradients of the cluster subpopulations from linear least-squares fits. The shaded regions represent the 10- and 90- percent confidence limits obtained from bootstrap resampling. For the oldest clusters, only the slope and confidence limits for the inner (R < 4.5 kpc) clusters are shown (see text).

to whether or not the gradient evolves with time. Our data suggests that it does - and quite strongly. The dashed line in Figure 15 shows a fit to the M33 cluster data yielding an evolution in the metallicity gradient, d[M/H]/dt / dR = 0.03 dex/kpc/Gyr. This strong evolution is consistent with observations of some high-redshift systems (Jones et al. 2013; Yuan et al. 2011). However, the RGB stars and PNe suggest a much weaker evolution, which is also consistent with some high redshift observations (e.g., see the redshift ~ 2.2 system in the data of Jones et al. 2013; Figure 15). This uncertainty is reflected in the simulations. The results of two simulations for L* discs (i.e., a factor of ~ 10 more massive than M33) with differing feedback prescriptions are shown in Figure 15. The realisations come from the “McMaster Unbiased Galaxy Simulations” (MUGS; Stinson et al. 2010) and “Making galaxies in a Cosmological Context” (MaGICC; Brook et al. 2012; Stinson et al. 2013).

The MUGS simulations reflect the M33 data (and high-redshift systems) quite well, consistent with a strong evolution in the metallicity gradient. However, the MaGICC simulations - which show little evolution - better reflect the RGB and (possibly) the PNe data. The principal differences between the two simulations are that MUGS-g15784 uses a thermal feedback scheme that injects approximately 40 percent less energy into the ISM from supernovae than MaGICC (see Gibson et al. 2013 for more details).

The principal observational problem in constraining the time-evolution of metallicity gradients in local discs is age-dating older (> 2 Gyr) stellar populations. This is indicated by the lower limits on the RGB star and PNe data in Figure 15 and reflects the poorly constrained ages of these evolved populations. This is less of an issue for the youngest populations (e.g., HII, OB stars, young clusters) where the metallicity gradients agree quite well (c.f., Figure 15). Spectroscopic metallicities of RGB stars and more data on the intermediate-age to old clusters should help to better constrain this regime.

In summary, we find a flattening of the M33 metallicity gradient with time from the star cluster data. This is in agreement with high redshift observations of more massive discs, but in some tension with observations of RGB stars and PNe in M33. Our results are consistent with the picture that the inner galaxy regions of the M33 disc is more chemically evolved than the outer regions. I.e., consistent with an “inside-out” disc formation scenario (e.g. MacArthur et al., 2004; Jones et al. 2010).

4.4 Kinematics

Previous studies (Schommer et al. 1992; CBFS02) have shown that the young M33 clusters rotate in a similar sense to the HI disc, and that the average velocity dispersion of M33 cluster populations increases with the age of the population. However, these studies were only able to place upper limits on the velocity dispersions of the young clusters due to uncertainties on the individual cluster velocities of 25-30 km/s, of order or larger than the HI disc dispersion (~ 18.5 km/s; Putman et al. 2009). In addition, age infor-
Table 3. Stellar population properties measured for cluster subgroups.

| Subsample      | mean age (Gyr) | mean [M/H] (dex) | σ[M/H] (dex) | [M/H] gradient (dex/kpc) | intercept (dex) | N  |
|----------------|----------------|------------------|--------------|--------------------------|----------------|----|
| young          | 0.033 ± 0.007  | -0.19 ± 0.04     | 0.17         | 0.045 ± 0.033            | -0.377 ± 0.019 | 22 |
| young-intermediate | 0.46 ± 0.05    | -0.23 ± 0.04     | 0.21         | 0.024 ± 0.035            | -0.300 ± 0.020 | 24 |
| old-intermediate | 1.75 ± 0.16    | -0.74 ± 0.08     | 0.33         | -0.054 ± 0.046           | -0.582 ± 0.022 | 19 |
| old            | 10.35±0.71     | -1.12 ± 0.09     | 0.32         | 0.041 ± 0.050 (-0.290 ± 0.110)$^a$ | -1.282 ± 0.010 (-0.530 ± 0.048)$^a$ | 12 |

$^a$ R < 4.5 kpc.

Figure 16. Time evolution of the metallicity gradient in M33. The top panel shows gradients as a function of population age, lower panel as a function of redshift. The M33 clusters (red circles) are compared to the gradients determined from OB stars (Urbanek et al. 2005), HII regions and PNe (Bresolin et al. 2010; Margini et al. 2009), RGB star photometry (Teide et al. 2004). Also shown are gradients determined for high-redshift systems (Jones et al. 2013; Yuan et al. 2010). Predictions are also shown for two different simulations of L* disc galaxies (Brook et al. 2012; Stinson et al. 2010). The black dashed line shows a fit to the M33 data giving an evolution of the metallicity gradient of 0.03 dex/kpc/Gyr. In the top panel we have fixed the ages of the OB stars from Urbanek et al. (2005) and HII and “young” PNe from Bresolin et al. (2010) to 10$^7$ yr for display purposes.

We show the radial velocities of our sample plotted as a function of position angle with respect to that of the M33 major axis in Figure 17. Position angles were calculated following the common convention E through N, adopting the NED value for the centre of M33 (RA(2000) = 01$^h$ 33$^m$ 50$^s$ 89, Dec. (2000) = 30$^\circ$ 39$'$ 36$''$ 8). The clusters have been separated into the previously defined age bins. Rotation is clearly present in the three youngest cluster subgroups (Figure 17), with the dispersion about the rotation solution increasing with the mean age of the subgroup. The oldest clusters also show some evidence for rotation, but with a rotation axis misaligned with that of the younger clusters. However, both the amplitude and position angle of this rotation is poorly constrained due to the small number of clusters in the oldest bin (see below).

To quantify the rotation amplitude and position angle in the cluster subgroups we assumed that the clusters are confined to a thin plane of inclination i to the line of sight, and performed non-linear least-squares fits to the cluster bins using the functional form:

$$V(\theta) = V_{sys} + V_{rot} \times \sin(\phi - \phi_0) \sin(i)$$  

where $V(\theta)$ is the observed cluster velocity at position angle $\theta$, $V_{sys}$ is the systemic velocity of the clusters, $V_{rot}$ the rotation amplitude and $\phi$ the position angle of the line of nodes of the best-fit rotation solution with respect to that of the M33 major axis ($\phi_0$). We left $V_{sys}$, $V_{rot}$ and $\phi$ as free parameters to be determined by the fits. Uncertainties were determine by Monte Carlo simulations (1,000 bootstrap resamples with replacement for each age bin). We also tested our rotation solutions by fixing the position angle of the line of nodes to that of the youngest cluster bin (81±9 degrees) which is coincident with the M33 minor axis. The rotation amplitudes do not change significantly when fixing the position angle.

Our fits are shown graphically in Figure 17 and listed in Table 4. We calculated the line of sight velocity dispersion of the cluster subgroups by subtracting the best-fit rotation curve and then measuring the velocity dispersion of each group. These values are also given in Table 4. In addition, we include a small correction for our intrinsic velocity uncertainties which are subtracted in quadrature from the velocity dispersion estimates (a correction of $\sim$ 2 km/s). It is evident that there is a trend for the rotation amplitude to decrease and velocity dispersion to increase with increasing cluster...
age (as quantified by $V/\sigma$ in Table 4). A similar effect was identified by CBFS02.

We interpret the decrease in the rotation amplitude as a function of group age as a manifestation of asymmetric drift; the increasing tendency of older populations to “hide” their rotation in randomized motions. Therefore, we corrected the rotation velocities of our cluster groups for asymmetric drift by assuming a flat rotation curve and that the star clusters follow an exponential surface density profile (Figure 14) (see Hinz et al. 2001) leading to the expression (from Leaman et al. 2012):

$$V_{\text{cor}}^2 = V_{\text{rot}}^2 + \sigma_{\text{los}}^2 (\frac{R}{R_d} - 1)$$

where $V_{\text{cor}}$ and $V_{\text{rot}}$ are the asymmetric-drift corrected and observed, inclination-corrected velocities of the cluster subgroups respectively, $\sigma_{\text{los}}$ the velocity dispersion of the clusters, $R$ the mean radius of the cluster group and $R_d$ the disc scalelength.

These corrected rotation velocities are listed in Table 4. Once corrected for asymmetric drift, the rotation amplitudes for all four cluster subgroups are similar ($\sim 100$ km/s). This is also true for the oldest cluster subgroup (although note that the uncertainties here are of order $\sim 70$ percent of the rotation amplitude). The rotation of all the clusters is consistent with the rotation curve of M33 (Corbelli & Salucci 1999) at the mean radii of the cluster subgroups.

Another approach to quantify the $V/\sigma$ of the clusters is to compare the cluster kinematics to the HI rotation curve. CBFS02 did this by creating a disc model from the rotation curve of Warner et al. (1973). Here, we take advantage of the available two dimensional data by measuring the HI velocity directly at the location of each cluster from the VLA HI 21cm velocity moment maps of Gratier et al. (2010). These data are available at spatial resolutions of 25, 17 and 12 arcseconds respectively. We chose to use the 25 arcsecond maps due to their more complete spatial coverage over the M33 disc, although the use of different resolution maps does not significantly affect our results.

The quantity $V_{\text{HI}} - V_{\text{cluster}}$, a measure of the deviation of the cluster velocity from the mean HI gas velocity at the position of the cluster, is plotted against cluster age in Figure 18. The velocity dispersions about the HI gas disc for the four (youngest to oldest) subgroups are: 23.7$\pm$5.0, 29.1$\pm$6.0, 31.1$\pm$8.0 and 98.2$\pm$25.0 km/s respectively. These values are consistent with our previous results from our simple disc model. The three youngest cluster groupings clearly constitute disc populations and the clusters show an increasing velocity dispersion with age. The youngest population has dispersion 23.7 km/s which is close to the mean HI disc dispersion (18.5 km/s; Putman et al. 2009). Creating an additional bin with clusters younger than 50 Myr (N=18), yields a mean value for $V_{\text{HI}} - V_{\text{cluster}}$ of 19$\pm$5 km/s.

### 4.5 The age-velocity dispersion relation

The age-velocity dispersion relation (AVR) for the M33 clusters (with dispersions taken adopting the thin-disc model) is shown in Figure 19. In the figure we also compare the M33 cluster data with the total LOS velocity dispersions of solar neighbourhood stars (Holmberg et al. 2007) and
those of Milky Way open clusters (OCs) compiled by Hayes & Friel (2014). In the case of the Hayes & Friel (2014) data, we have multiplied their velocity dispersions by a scalefactor of $\sqrt{3}$ assuming isotropic velocity distributions. This is an estimate of the true scalefactor, since the Hayes & Friel (2014) velocities contain both components of $\sigma_U$ and $\sigma_V$. However, the good agreement between the Holmberg et al. (2007) and Hayes & Friel (2014) LOS dispersions for disc populations at a given age (after applying our scalefactor) suggests that this scaling is reasonable.

It is evident that the M33 clusters in Figure 18 show an increasing velocity dispersion with age. This behaviour is similar to that of the Milky Way OCs. This is also observed in Milky Way disc stars, where the youngest stars in the solar neighbourhood have velocity dispersions of $\sim 10$ km/s (again assuming isotropic velocity ellipsoids; Aumer & Binney 2009), rising to $\sim 60$ km/s at 10 Gyr ages (e.g., Holmberg et al. 2007).

A number of workers have interpreted the AVR of the stellar disc with time as a result of disc heating processes (e.g. Spitzer & Schwarzschild 1951; Wielen 1977). Candidate mechanisms for this heating may be secular - such as stellar interactions with giant molecular clouds (Spitzer & Schwarzschild 1951 - but see Lacey (1984)) and spiral arms (Minchev & Quillen 2006), or related to substructure infall including black holes from the Galactic halo passing through the disc (Hänninen & Flynn 2002) and the infall of satellites in the form of minor mergers within the context of the hierarchical clustering paradigm (e.g. Mihos & Hernquist 1996; Benson et al. 2004; Villalobos & Helmi 2008; House et al. 2011).

An alternative (and not mutually exclusive) interpretation of the AVR is that stars and star clusters of a given age may have been formed in gas with intrinsically different kinematical properties (e.g. Brook et al. 2004; Bournaud, Elmegreen & Martig 2009; Bird et al. 2013). Specifically, the average (molecular) gas velocity dispersion in discs may have been higher at early times (e.g., Förster Schreiber et al. 2009; Wisnioski et al. 2014), thereby leading to stellar populations formed at these epochs with characteristically higher velocity dispersions. In some sense, this may be regarded as a “cooling” of the disc ISM over time.

Both heating and cooling might be expected to occur in discs, but teasing out the relative importance of these processes is difficult with these data. Indeed, even with full phase-space information and detailed chemical abundances this is a challenging task (e.g., Bovy et al. 2012). However, the fact that we see similar AVRs in both the Milky Way and M33 discs does place constraints on the underlying cause of this relation (see also Leaman et al. 2013).

Simulations that take into account both secular heating and merging processes make a fair job of reproducing the observations. In Figure 14, we show the region of age-velocity dispersion space produced by the simulations of Martig, Minchev & Flynn (2014). These authors re-simulated at high resolution 7 disc galaxies taken from cosmological simulations (Martig et al. 2012) with a range of formation histories (quiescent to 1:4 mergers) and stellar masses ($3.3 \times 10^{10} M_{\odot}$). Although the stellar mass of the M33 disc is ($3 \times 10^9 M_{\odot}$; Corbelli 2003), which is a factor of 10 less massive than Martig et al’s least massive galaxy, the normalisation and trend of the simulations are broadly consistent with the M33 and Milky Way cluster data at all ages (the simulations show a wide range in velocity dispersion since we have taken the minimum and maximum values of all 7 galaxies as the range in model predictions). In detail, the slope of the AVR in the simulations is somewhat flatter than the observations. In addition, the youngest Milky Way OCs have velocity dispersions that lie below the models. The latter discrepancy may reflect the resolution limits in the simulations resulting in stars being born too hot (Martig et al. 2014).

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**Table 4.** Kinematical solutions obtained for cluster subgroups. $V_{\text{rot}}$ indicates the rotation amplitude of the cluster subgroups corrected for inclination. $V_{\text{cor}}$ indicates $V_{\text{rot}}$ corrected for asymmetric drift.

| Subsample     | $V \sin i$ (km/s) | $V_{\text{rot}}$ (km/s) | $V_{\text{cor}}$ (km/s) | Position angle (degrees) | $V_{\text{sys}}$ (km/s) | $\sigma_{\text{los}}$ (km/s) | $V_{\text{rot}} / \sigma_{\text{los}}$ | Mean radius (kpc) |
|---------------|-------------------|--------------------------|-------------------------|--------------------------|--------------------------|-----------------------------|-------------------------------|------------------|
| young         | 77 ± 11           | 95 ± 14                  | 100.4 ± 29.1            | 81 ± 9                   | −167 ± 8                 | 20.0 ± 5.0                  | 4.8 ± 1.4                    | 2.38              |
| young-intermediate | 67 ± 9          | 83 ± 11                  | 103.6 ± 25.0            | 59 ± 9                   | −147 ± 7                 | 29.5 ± 6.0                  | 2.8 ± 0.7                    | 2.74              |
| old-intermediate | 47 ± 18        | 58 ± 22                  | 85.9 ± 38.0             | 86 ± 20                  | −159 ± 15                | 38.9 ± 8.9                  | 1.5 ± 0.7                    | 2.85              |
| old           | 65 ± 40           | 80 ± 49                  | 158.5 ± 107.2           | 229 ± 44                 | −173 ± 35                | 67.3 ± 19.4                 | 1.2 ± 0.8                    | 3.96              |

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Figure 18. $V_{\text{HI}} - V_{\text{cluster}}$ versus age for the M33 clusters. The horizontal shaded region represents the mean velocity dispersion ($\sim 18.5$ km/s) of the HI in the star forming disc (Putman et al. 2009).
Figure 19. Age-velocity dispersion relation of M33 clusters. Velocity dispersion of M33 clusters versus age compared to Milky Way open clusters (134 clusters; Hayes & Friel 2014). Also shown are estimates of the inter-cloud molecular gas velocity dispersion for the Milky Way from Stark (1984) and for M33 from Druard et al. (2014). The shaded region indicates the predictions from the simulations of Martig et al. (2014). The AVR for the Milky Way and M33 clusters look very similar.

Although Martig et al. (2014) could not identify the exact mechanism(s) responsible for disc heating in their simulations, they conclude that for quiescent systems disc heating produces a smoothly increasing velocity dispersion up to ∼9 Gyr. A general result is that stars older than this are born kinematically hot in turbulent gas at early times (Brook et al. 2004; Bournard, Elmegreen & Martig 2009; Bird et al. 2013).

The M33 data seems consistent with the picture of a smoothly heated disc cluster population, perhaps with the oldest population formed in a kinematically hotter environment. However, the similarity between the AVRs of the Milky Way OCs and the M33 clusters suggests that something other than just secular heating is controlling the overall shape of the AVR. Analytic models (Leaman et al. 2015) that account for both substructure heating and ISM evolution as a function of host galaxy mass suggest that the ISM defines a characteristic “pressure floor”, with additional heating via substructure playing an increasingly important role for systems with masses similar to, or greater than, that of M33.

Finally, we highlight that comparisons between the AVRs of stars and star clusters in a given disc should place constraints on heating processes within stellar discs. We expect that the efficiency of mechanisms that heat a population via scattering will be a function of the mass ratio of the scatterer and “scatteree” (e.g. Spitzer & Schwarzschild 1951). For example, in scenarios where stars and star clusters are heated via scattering off GMCs in the plane of the disc, we would expect stars of a given age and position in the disc to be more efficiently scattered than star clusters, yielding a higher line of sight velocity dispersion.

4.6 The globular clusters

We identify 12 clusters in our sample that have age, metallicity and kinematical properties consistent with globular clusters in M33. Six of these GCs in our sample (R12, R14, M9, U49, H38, U77) have HST CMDs (in F555W and F814W filters) that extend to ∼ 1.5 magnitudes below the horizontal branch (Sarajedini et al. 2000). The remaining six clusters we identify as good GC candidates, having radial velocities and stellar population properties consistent with this interpretation (Section 3.2).

4.6.1 Globular cluster ages

A number of previous studies have concluded that there may be a significant age spread amongst the M33 GCs based on integrated broadband photometry (Cohen, Persson & Searle 1984; CBFS02), integrated spectra (Christian & Schommer 1983; Chandar et al. 2006) or arguments based on the horizontal branch morphology (Sarajedini et al. 2000). Sarajedini et al. (2000) found that the clusters R12, U49 and H38 have exclusively red horizontal branches (red clumps), despite their relatively low metallicities. Based on this fact, Sarajedini et al. concluded that these clusters exhibit the so-called second-parameter effect, and argued that under the assumption that the second parameter is age then R12, U49 and H38 may be as young as ∼ 7 Gyr. We find old ages for these three clusters (∼ 10 Gyr). Given the uncertainties in the modelling of integrated stellar populations and the continued controversy over what drives the second parameter effect (e.g. Milone et al. 2014) we do not consider that our
ages are in serious disagreement with the Sarajedini et al. (2000) study.

Sarajedini et al. also identified the clusters M9 and U77 as being genuinely old (\( \sim 12 \) Gyr) clusters. For M9 we obtain an age of \( \sim 12 \) Gyr in good agreement with Sarajedini. However, for U77 we obtain an age of \( \sim 6 \) Gyr even though our derived metallicities are identical within the uncertainties with Sarajedini et al. (see below). The HST CMD of U77 clearly shows stars blueward of the HB instability strip suggesting that this is indeed an old cluster even though we find younger age solutions from ULYSS. Previous studies indicate that blue HB stars can affect integrated spectra to the extent that old stellar populations can look young if the HB is not properly accounted for in SSP models (e.g. Beasley et al. 2002; Schiavon et al. 2004; Yoon, Yi & Lee 2006; Cenarro et al. 2008). The MILES models model a canonical blue HB at low metallicities, but an excess of hot blue stars may be artificially lowering the spectroscopic age of this cluster. We indentify two further GC candidates with ages similar to U77. CMDs will be very valuable for investigating whether these are genuinely younger objects, or exhibit blue HBs. For example, Chandar et al. (2006) conclude, based on MMT integrated spectra and HST photometry of the horizontal branch, that the M33 cluster C38 (not in our sample) has ages \( \sim 2 - 5 \) Gyr. The observed lack of a blue HB in C38 supports this claim.

CBFS02 also give ages for five clusters in common with our sample (R12, R14, M9, U49-2916 and H38) which were based on integrated colours (CBFS99). CBFS02 determined ages : R12 (2.5 - 10 Gyr), R14 (10 - 25 Gyr), M9 (1.25 - 2 Gyr), U49 (1.25 - 2 Gyr) and H38 (1.25 - 2.5 Gyr) (where the age ranges come from the error bars given by CBFS02). From our analysis we find that all of these clusters are old with an age range between 9.5 - 12.4 Gyr, this is consistent with the CBFS02 findings for R12 and R14, but inconsistent with M9, U49 and H38. Due to the difficulties of breaking the age-metallicity degeneracy with broadband colours, we prefer our age estimates over those of CBFS02.

To summarise our age results, we find no compelling evidence, based on the present data, for a significant age spread in the GCs of M33 as claimed by previous authors. However, our sample is small, and ages from integrated spectra lack fidelity at old ages and can also be affected by non-canonical hot stellar populations. Only deep CMDs reaching to below the main sequence turnoff in these clusters will provide secure ages for these objects.

\subsection{4.6.2 Globular cluster metallicities}

Our spectroscopic metallicities for five clusters compared to those derived by Sarajedini et al. (2000), based on the slope of the red giant branch, are shown in Figure 20 (R14 is not included due to high differential reddening in this cluster). We find reasonable agreement between the spectroscopic and CMD-derived metallicities in the range \(-1.8 < \text{[M/H]} < -0.8\).

The metallicity distributions of the M33 GCs are compared to those derived for the Milky Way, M31, LMC and Fornax dwarf GCs in Figure 21. These metallicities come from a variety of techniques; the majority of the Milky Way clusters have high dispersion spectroscopic measurements of individual stars (see Harris et al. 2006). Metallicities for M33 and M31 come from integrated spectra (this paper and Caldwell et al. 2011 respectively), the LMC clusters have metallicities predominantly from Calcium Triplet spectroscopy of individual stars (Olszewski et al. 1991) and the Fornax dwarf spheroidal GC metallicities come from high resolution (Larsen, Brodie & Strader 2012) and low resolution (Strader et al. 2003) integrated spectroscopy. The metallicities from these varied approaches are consistent at the 0.2 - 0.3 dex level (e.g., Beasley et al. 2002; Puzia et al. 2002; González Delgado & Cid Fernandes 2010; Colucci et al. 2013).
Figure 24 shows that the metallicities of the M33 GCs are quite metal-rich ($\langle [M/H] \rangle = -1.12 \pm 0.09$). This metallicity is entirely consistent with the expected location of M33 ($M_V \sim -18.9$) on the “zero-age” luminosity–metallicity relation derived by Côté, Marzke & West (1998). The mean M33 GC metallicities are also similar to the the mean metallicity of the M31 clusters ($\langle [M/H] \rangle = -1.00 \pm 0.02$), but more metal-rich than the Milky Way ($\langle [M/H] \rangle = -1.27 \pm 0.05$), and significantly more metal-rich than the LMC ($\langle [M/H] \rangle = -1.87 \pm 0.08$) and Fornax dwarf spheroidal ($\langle [M/H] \rangle = -2.08 \pm 0.17$) cluster systems. Restricting the Milky Way clusters to the metal-poor halo population ($\langle [M/H] \rangle = -1.53 \pm 0.04$) makes the apparent disparity with M33 more acute. A similar separation cannot easily be performed for the M31 cluster system since the metallicity distribution of its cluster system is not clearly bimodal, although Caldwell et al. (2011) do identify a possible metal-poor peak at $\langle [M/H] \rangle \sim -1.4$.

We investigated further the differences between the Milky Way and M33 clusters by determining, via Monte Carlo simulation, the likelihood that the M33 GCs could be drawn from a parent population resembling the Milky Way halo clusters. We cut both samples at $[M/H] < -0.7$ (i.e. restricting ourselves to the halo clusters) giving 11 M33 clusters and 118 Milky Way clusters. We then ran 10,000 trials where we randomly selected 11 clusters from the Milky Way distribution and calculated their mean metallicities. Only 0.24 percent of these samples had mean metallicities equal to or greater than the mean of the M33 clusters. Therefore, based solely on metallicity, the M33 clusters are unlikely to have been drawn from a parent population resembling the Milky Way halo clusters at $\sim 99.8$ per cent confidence.

4.6.3 On the origin of the globular cluster population

The high metallicity of the M33 GCs presents something of a problem if we wish to identify the majority of these objects solely with an accreted halo population (e.g. Searle & Zinn 1978; Côté, Marzke & West 1998). The mean metallicities of LMC and Fornax clusters suggest that no combination of the GC systems of these (present day) galaxies could have contributed to the build up the metallicity distribution of M33 GCs in our present sample, save perhaps for the very metal-poor tail of the distribution. Since Fornax ($M_* \sim 10^8 M_\odot$; Mateo 1998) and the LMC ($M_* \sim 10^9 M_\odot$) bracket the lower and higher mass ends of Local Group “dwarfs” with GC systems, this constrains the nature of the origin of the M33 GCs.

Assuming a Fornax dwarf or Small Magellanic Cloud (SMC)-like field star AMR, we can ask what age a GC accreted from such a galaxy need have in order to attain a metallicity of $[M/H] \sim -1.1$, the mean metallicity of the M33 GC system. The AMR for the SMC field stars suggests that an age of $\sim 5$ Gyr or younger would be required to achieve the necessary enrichment levels (Dobbie et al. 2004; Carrera et al. 2008; Leaman et al. 2013). Such young ages for the GCs in our sample are generally ruled out based on our stellar population analysis and previous observations (see below). This age constraint can be relaxed to $\sim 10$ Gyr if we assume that a more massive, LMC-like system were accreted. However, given that the LMC stellar disc is similar in mass to the M33 stellar disc ($\sim 3 \times 10^9 M_\odot$), such an equal-mass merger would likely disrupt the entire M33 disc. A system intermediate in mass between the SMC and LMC could possibly accommodate both the metallicities and ages seen in the M33 GCs, but some fine-tuning would be required (since the bulk on the inner M33 GC system would have to be built up of such systems).

Interestingly, the simulations of Cooper et al. (2010) suggest that the typical satellite that went to form a Milky Way-like halo had a mass similar to that of the brightest Local Group dwarf spheroidal (dSphs) (e.g. Fornax-like systems). However, differences observed between the stellar populations of halo stars and those seen in Local Group dSphs (Venn et al. 2004; Helmi et al. 2006; Fiorentino et al. 2014) suggest that these systems played at most a minor role in building up the Milky Way halo. If the M33 clusters truly represent the remnants of an accreted population then these clusters must have come from systems more massive than presently observable dSphs.

An alternative origin for some or all of these GCs is a formation during an early collapse phase, perhaps leading to the formation of a bulge or disc component (e.g. Brook et al. 2004). The question of whether or not M33 has a bulge remains controversial (e.g. Hodżê 2012). However, Regan & Vogel (1994) placed an upper limit on any putative bulge of $M_V > -16 (L_V < 2 \times 10^7 L_\odot)$. Assuming a relatively generous $V$-band specific frequency of 1 (Harris et al. 1991), this suggests that at most 3 GCs may be associated with this component. An alternative is to associate the GCs with the M33 disc. This association is not unreasonable: our GC sample is confined to within $\sim 6$ kpc of the galaxy centre and are seen in projection against the optical disc (Figure 10). The inner ($R < 4.5$ kpc) GCs show a hint of an exponential-like surface density profile and also a steep and negative radial gradient consistent with the evolution of the gradient seen for the younger disc clusters. As discussed above, the M33 clusters in our sample are more metal-rich than Milky Way halo clusters, and also appear to be more metal-rich than expected for true halo clusters in M33 (e.g. Stokkutė et al. (2008) find $[M/H] \leq -1.4$ for an extended star cluster lying 12.5 kpc in projection from the centre of M33). In addition, the kinematics of the clusters are consistent with a continuous heating of the disc cluster population (or a cooling of the ISM from which they formed - see Section 4.5) over the disc lifetime (Section 4.4).

Finally, clues to the origin of the inner M33 GCs comes from analysis of their structural parameters. Mackey & van den Bergh (2005) have shown that the “young halo” (YH) GCs in the Milky Way tend to have larger half-light and tidal radii than the inner “old halo” (OH) clusters, which in turn are more extended than the more metal-rich bulge/disc (BD) globular clusters. Ma (2015) has presented structural parameters for 10 M33 globular clusters (from Sarajedini et al. 1998), five of which are in our spectroscopic sample. All these clusters (R12, R14, M9, U49 and H39) appear quite compact for their luminosities, with mean half-light radii of $\sim 3.5$ pc (King model) and a maximum $R_h = 5.8$ pc (U49). This is similar to the BD clusters in Mackey & van den Bergh (2005) which all have $R_h < 7$ pc. The distribution of

7 If we consider only the M33 GCs identified by HST CMDs, the mean GC metallicity still remains high, $[M/H] = -1.25 \pm 0.14$
half-light radii for the OH and YH clusters extends to \( \sim 17 \) and 25 pc respectively.

Similarly, the mean tidal radii of the M33 clusters is \( \sim 31 \) pc with R14 having the largest \( (R_t \sim 40 \) pc). The BD clusters in Mackey & van den Bergh (2005) all have \( R_t < 60 \) pc, with mean radii of \( \sim 30 \) pc, consistent with the M33 sample. Such small tidal radii are expected of clusters that spend a significant fraction of their time in a deep potential (i.e. near the galaxy centre), suggesting that these are truly central clusters and not simply halo clusters seen in projection. By comparison, the OH and YH GCs in the Milky Way have distributions of tidal radii that extend out to \( \sim 200 \) and 150 pc respectively.

To summarise, while our sample size is small, based on their stellar populations, spatial locations, kinematics and structural parameters, we suggest that the inner M33 GCs are better associated with the M33 disc rather than its halo or minimal bulge.

5 CONCLUSIONS

We have obtained precision velocities (to \( \sim 10 \) km/s) and stellar population parameters (age, metallicity) for a sample of 77 star clusters in M33. Our principal findings are:

- The M33 disc clusters show a clear age-metallicity relation in the sense that younger clusters are more metal-rich than the older clusters. The youngest clusters in our sample have \( \sim 10 \) Myr ages and near solar metallicities, very similar to the M33 OB star populations.
- We find evidence for evolution in the disc metallicity gradient in M33. The metallicity gradient becomes less negative with time. The evolution in the the metallicity gradient is strong with \( \sim 0.03 \) dex/kpc/Gyr. The inner globular clusters \((R < 4.5 \) kpc) show a steep, negative radial metallicity gradient.
- We find little evidence for radial age gradients in the disc clusters. Clusters have continued to form throughout the star forming disc (within 6 kpc) throughout the disc lifetime.
- Clusters younger than \( \sim 4 \) Gyr all exhibit rotation consistent with the disc of M33. The rotation amplitude decreases and velocity dispersion increases with increasing cluster age. We find a smoothly increasing age-velocity dispersion relation very similar to that seen in the Milky Way open cluster system. We interpret this as a combination of secular heating processes and cooling of the ISM with time.
- We identify six new globular cluster candidates that have kinematics and stellar populations consistent with genuine globular clusters. Follow-up high resolution imaging is required to unambiguously determine their nature.
- We find no strong evidence for a significant age spread in the M33 globular clusters. The majority of globular clusters in our sample are old (\( \sim 10 \) Gyr). Three clusters have spectroscopic ages of \( \sim 6 \) Gyr. However, one of these is clearly older than this based on the presence of a well-developed blue HB in its \( HST \) CMD (Sarajedini et al. 2000). The remaining two clusters may be genuinely intermediate aged clusters in M33.
- The mean metallicity of the M33 globulars is relatively metal-rich \(([M/H]=-1.12\pm0.09)\). This is significantly more metal-rich than the halo GCs in the Milky Way, and GCs in the LMC and the Fornax dSph. Based on their high metallicities, spatial distributions, kinematics and structural parameters we argue that the inner GCs are better associated with the M33 disc than halo.

We believe that this contribution reinforces the utility of star clusters in studying the disc components of galaxies. Since clusters typically span a large range of ages, they can be used to probe disc properties over the whole disc lifetime, while at the same time consistent analysis methods can be applied. This contrasts with complementary approaches that use stellar population tracers that are confined to narrow age ranges (e.g. OB stars; Urbanč et al. 2005) or age ranges that are not well constrained (e.g., PNe; Magrini et al. 2004; Ciardullo et al 2004) and require intrinsically different analysis methods.

The stellar population analysis used here, consisting of full spectral fitting (e.g., Koleva et al. 2009) to the latest generation of model SEDs (Vazdekis et al. 2010), is a powerful technique for estimating ages and metallicities of star clusters. However, it does have its limitations. Most apparent is its lack of age resolution at old ages. Given the uncertainties in stellar population modelling, particularly in understanding non-canonical hot populations and the incorporation of non-solar abundance ratios, our ability to differentiate age amongst the oldest populations is limited. This is most apparent in our discussion of the putative age-spread amongst the M33 globular clusters (Section 4.4). Only deep CMDs reaching to below the turnoff in these clusters will provide secure ages for these objects.

Future improvements to this work should include increasing the sample size and spectral range covered for the cluster populations. In particular, going to bluer wavelengths will give additional leverage in constraining the ages of the younger clusters. In addition, providing that the systematics are adequately characterised (Sakari et al. 2014), new techniques that obtain heavy- and light-element abundances via integrated spectroscopy (e.g., McWilliam & Bernstein 2008; Colucci et al. 2012, 2013; Larsen et al. 2012; Sakari et al 2013) could usefully be applied to M33 star clusters and other nearby disc cluster systems.

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