Prospects for population synthesis in the H band: NeMo grids of stellar atmospheres compared to observations

J. Frémaux¹, F. Kupka², C. Boisson¹, M. Joly¹, and V. Tsymbal³,⁴

¹ LUTH, UMR 8102 du CNRS, associé à l’Université Denis Diderot, Observatoire de Paris, Section de Meudon, 92195 Meudon Cedex, France
e-mail: julien.fremaux@obspm.fr
² Max-Planck-Institute for Astrophysics, Karl-Schwarzschild Str. 1, 85741 Garching, Germany
³ Tavrian National University, Yaltinskaya 4, 330000 Simferopol, Crimea, Ukraine
⁴ Institute for Astronomy, University of Vienna, Türkenschanzstraße 17, 1180 Vienna, Austria

Received 27 June 2005 / Accepted 22 October 2005

ABSTRACT

Context. For applications in population synthesis, libraries of theoretical stellar spectra are often considered an alternative to template libraries of observed spectra, because they allow a complete sampling of stellar parameters. Most of the attention in published theoretical spectral libraries has been devoted to the visual wavelength range.

Aims. The goal of the present work is to explore the near-infrared range where few observed fully calibrated spectra and no theoretical libraries are available.

Methods. We make a detailed comparison of theoretical spectra in the range 1.57–1.67 µm for spectral types from A to early M and for giant and dwarf stars, with observed stellar spectra at resolutions around 3000, which would be sufficient to disentangle the different groups of late-type stars. We selected the NeMo grids of stellar atmospheres to perform this comparison.

Results. We first demonstrate that observed spectral flux distributions can be matched very well with theoretical ones for almost the entire parameter range covered by the NeMo grids at moderate resolution in the visual range. In the infrared range, although the overall shape of the observed flux distributions still matches reasonably well, the individual spectral features are reproduced by the theoretical spectra only for stars earlier than mid F type. For later spectral types the differences increase, and theoretical spectra of K type stars have systematically weaker line features than those found in observations. These discrepancies are traced back to stem primarily from incomplete data on neutral atomic lines, although some of them are also related to molecules.

Conclusions. Libraries of theoretical spectra for A to early M type stars can be successfully used in the visual regions for population synthesis, but their application in the infrared is restricted to early and intermediate type stars. Improving atomic data in the near infrared is a key element in making the construction of reliable libraries of stellar spectra feasible in the infrared.

Key words. stars: atmospheres – infrared: stars – galaxies: stellar content

1. Introduction

Due to the rapidly increasing spectral resolution of galaxy surveys (e.g. Sloan Digital Sky Survey), modelling any galaxy with spectral synthesis technique requires stellar library with a high spectral resolution.

In recent years, much progress has been made in synthesis models (e.g. Pelat 1997; Leitherer et al. 1999; Moulata & Pelat 2000; Bruzual & Charlot 2003; Le Borgne et al. 2004; Cid Fernandes et al. 2005). Moderate to high spectral resolution observations of stars in order to construct reliable template libraries have also been performed in the visible domain (e.g. STELIB of Le Borgne et al. 2003; UVES of Bagnulo et al. 2003; CoudeFed of Valdes et al. 2004) and in the IR (e.g. Dallier et al. 1996; Meyer et al. 1998; Ivanov et al. 2004).

However, the major limitation of all these libraries is the bad coverage in terms of stellar parameters such as metallicity.

One way to avoid such a difficulty is to build libraries of theoretical stellar spectra in order to choose the desired physical parameters. In this sense, some extensive libraries of synthetic spectra have appeared recently for the visible range.

Based on Kurucz’s ATLAS9 model atmospheres (1993a), Murphy & Meiksin (2004) have built a high resolution (λ/Δλ = 250 000) stellar library over an extended visible range (3000 to 10 000 Å). The convection zone is treated using the mixing length theory (MLT) with the overshooting treatment of Kurucz (cf. Castelli et al. 1997). This library provides spectra for 54 values of effective temperature from 5250 to 50 000 K, 11 values of log surface gravity from 0.0 to 5.0, and 19 metallicities from –5.0 to 1.0. They compared their synthetic library...
with observed spectra (STELIB library of Le Borgne et al. 2003) for the colours and the Lick indices and found generally good agreement.

Still based on Kurucz’s models, but with enhanced molecular line lists and the overshooting option switched off, Munari et al. (2005) also present a library of synthetic spectra for a similar wavelength range (2500 to 10 500 Å). They use a new grid of ATLAS9 model atmospheres (Castelli & Kurucz 2003). The effective temperature of these spectra is contained between 3500 and 47 500 K, with the log surface gravity between 0.0 and 5.0 and the metallicity between –2.5 and 0.5. These spectra are computed at a resolving power of \( \Delta / \Delta l = 500 000 \) and then Gaussian-convolved to lower resolution (\( \leq 20 000 \)). In contrast to Murphy & Meiksin (2004), the predicted energy level lines are not included in the line lists used to build this library, as Munari et al. (2005) favour the spectroscopic use rather than the photometric use of the synthetic spectra. The addition of these “predicted lines” permits a better statistical flux distribution, but individual wavelengths can be wrong by up to 5%.

Usually only the lower lying energy levels of atoms have been determined in the laboratory, particularly for complex spectra such as those from neutral or singly ionized iron. If only those transitions were taken into account, the atmospheric line blanketing computed from such data would be severely incomplete. A lot of weak lines that are possibly unidentified even in the solar spectrum, but are nevertheless present, would be missed. This would lead to overestimation of the ultraviolet flux, which in turn would be balanced out by a lack of flux in the visual (Kurucz 1992). To avoid this deficiency and to improve the temperature structure of the model atmospheres, the spectrophotometric flux distribution, and the photometric colours requires accounting for lines for which one or both energy levels have to be predicted from quantum mechanical calculations. This was one of the main goals of the ATLAS9 models of Kurucz (1992, 1993a). As the theoretical predictions are accurate to only a few percent, individual wavelengths can be wrong by up to a few 100 Å in the visual. Also the line oscillator strengths are sufficiently accurate merely in a statistical sense. This still permits improvement of the total flux within a wavelength band of a few dozen Å in the visual, but individual features do appear in the wrong part of the spectrum. For spectroscopy at higher resolutions, particularly if the spectrum is rectified or when working within small wavelength bands, adding the predicted energy level lines “pollutes” the theoretical spectrum with extra “noise”. This has to be avoided in libraries devoted to automatic fitting procedures or if particular line features are essential to identify a certain spectral type (lines predicted for the wrong wavelength will make this more difficult). Hence, with existing atomic data, either choice is only a compromise solution.

By combining three different model atmospheres, the high-resolution stellar library of Martins et al. (2005) provides the largest coverage in effective temperature (from 3000 to 50 000 K) and log surface gravity (from –0.5 to 5.5). This library, which is still in the visible wavelength range (3000 to 7000 Å), uses the non-LTE model atmosphere TLUSTY (Hubeny 1988; Hubeny & Lanz 1995; Lanz & Hubeny 2003) for \( T_{\text{eff}} \geq 27 500 \) K, the Kurucz’s ATLAS9 model for 4750 \( \leq T_{\text{eff}} \leq 27 000 \) K, and Phoenix/NextGen models (Allard & Hauschildt 1995; Hauschildt et al. 1999) that use spherical symmetry for cooler stars with low surface gravity. A comparison with observed spectra (from the STELIB library of Le Borgne et al. 2003; and the Indo-US library of Valdes et al. 2004) shows the good agreement of this theoretical library with observations.

Thus, the visible range is now quite well covered by theoretical libraries, for photometric use, for spectroscopic use, and for a wide range of physical parameters. All the comparisons with observations show that these theoretical spectra can mimic real stars reasonably well, at least at the spectral resolution where the comparisons were made.

The goal of the present work is to go one step further to explore the near-infrared range where few observed and fully calibrated libraries and no theoretical ones at all are available. This research takes place in a more general framework that consists in the synthesis of the stellar population of galaxies hosting active galactic nuclei by an inverse method described in Pelat (1997) and Mouttaka & Pelat (2000). The \( H \)-band provides very good luminosity discriminators for stars later than K0 (cf. Dallier et al. 1996), and the particular region 1.57–1.64 \( \mu \)m of the \( H \)-band is clear of strong emission lines (except Brackett lines). It allows sampling the stellar content of the very nucleus of Seyfert 1 galaxies, in contrast to the visible range, where the strong broad emission lines of the active nucleus contaminate the spectra of the galactic inner part so much that there are too few absorption lines from the stellar component to synthesize this region.

The lack of stellar observations at medium resolution for the near-infrared range, especially for super-metallic stars, drove us to work with theoretical spectra. But the behaviour of model atmospheres and fluxes is not very well known in the infrared.

Decin et al. (2003) have compared several observed stars with theoretical spectra computed with the MARCS models (Gustafsson et al. 1975; Plez et al. 1992) in the range 2.38 to 12 \( \mu \)m for the ISO-SWS calibration at a resolving power \( R \geq 1000 \). Their study points out the difficulties of modelling because of strong molecular opacities and the lack of accuracy and completeness of the atomic data in these wavelength ranges.

In this paper, we compute theoretical spectra using the NeMo (Vienna New Model) grid of atmospheres (Heiter et al. 2002; Nendwich et al. 2004) based on the model atmosphere code ATLAS9 by Kurucz (1993a, 1998) and Castelli et al. (1997), combined with the list of absorption lines VALD (Vienna Atomic Line Database, Kupka et al. 1999), eventually completed by molecular data collected by one of us (VT). These models are described in Sect. 2. Synthetic stellar spectra are computed with the code SynthV (built by VT), as shown in Sect. 3, using the model atmospheres described in Sect. 2 as input. Several tests of the input parameters of the spectra are made in Sect. 4.

In the first step of applying our synthesis calculations (Sect. 5), we compare a set of observed stellar spectra with their corresponding models in the visible wavelength range (5000 to
9000 Å) to check the range of validity of the NeMo grid, exploring the whole range of physical parameters (effective temperature, surface gravity, and metallicity). In a second step, we generate synthetic spectra in the near-infrared range and compare them with observed ones. The results of this comparison are described in Sect. 6, as are tests which demonstrate that the particular choice of model atmospheres can be expected to be less important than the set of line lists used for the computation of spectra. Our conclusions are summarised in Sect. 7.

2. Description of the model atmospheres

The model grid NeMo differs from the original grids of model atmospheres based on ATLAS9 in the treatment of the convective energy transport. It also provides a higher vertical resolution of the atmospheres and a finer grid in effective temperature and surface gravity.

This model grid of stellar atmosphere uses convection treatment without overshooting. The overshooting prescription was introduced by Kurucz (1993a, 1998) and modified by Castelli et al. (1997). It was supposed to take into account the change in the temperature gradient of the stable atmosphere layers near a convective zone due to the overshooting of gas from that zone into the stellar atmosphere. But this prescription is ignored here, because, even if the properties of various numerical simulations are described well and agree with observations of the Sun, models with overshooting are worse than models without it for other stellar types (see Heiter et al. 2002, for a detailed discussion).

The NeMo grids offer a choice among different convection models. One of them is the MLT, with $\alpha = 0.5$. Parameter $\alpha$ represents the ratio between the characteristic length (distance traveled by an element of fluid before its dissolution) and the scale height of the local pressure. This parameter is subject to discussion: according to comparisons between observed and computed energy distributions for the Sun done by Castelli et al. (1997), $\alpha$ should be set at least to 1.25, but Van't Veer & Mégessier (1996), using the same codes and input data as Castelli et al. (1997) but different observations for the Sun, found that $\alpha = 0.5$ is required to fit both $H_{\alpha}$ and $H_{\beta}$ profiles. Fuhrmann et al. (1993) were the first to notice that a value of 0.5 for the parameter $\alpha$ is needed to reproduce the Balmer line profiles of cool dwarf stars. In addition, this parameter has to span a large domain (from 1 to 3) to reproduce the red giants (Stothers & Chin 1997). The alternative convective models available in the NeMo grids are of “Full Spectrum Turbulence” (FST) type. Introduced by Canuto & Mazzitelli (1991, 1992; thereafter CM model) and Canuto et al. (1996, thereafter CGM model), these models avoid the one-eddy approximation of the MLT. In addition, both models were recommended to be used with a different scale length from the usual multiple $\alpha$ of the local pressure scale height (see Heiter et al. 2002, for further details).

The last models were introduced in NeMo to allow a choice among different treatments of the internal structure of the stars, depending on the aim of the model computation and its underlying assumption of how to describe the convective energy transport within the limitations of a simple convection model (using only algebraic rather than differential equations).

Two levels of vertical resolution are also offered, so we can either work with 72 or 288 layers. The MLT models are computed with 72 layers, CM models with 288, and CGM ones are computed for both values.

The metallicity of the model atmospheres covers a large range between $-2.0$ and $+1.0$ dex and has 13 different values. This range of metallicity is enough for our purpose. The super metal-rich stars, in particular, are represented with five different levels of metallicity ($+0.1, +0.2, +0.3, +0.5,$ and $+1.0$ dex) reaching the highest possible value for a real star.

Also, NeMo provides model atmospheres for effective temperatures between 4000 K and 10000 K, by successive steps of 200 K; for lowest temperatures, the model atmospheres computed with ATLAS9 become inadequate, mainly because of the molecular opacities that become very important for cool stars. The MARCS6 models (Gustafsson et al. 1975; Plez et al. 1992), more dedicated to the cool stars, handle this problem with a more complete treatment of molecular opacity.

The available values for the surface gravity (log $g$) of the stellar atmospheres in the NeMo grid span a range of 2.0 to 5.0 in steps of 0.2. It is bounded at 2.0 owing to the plane-parallel approximation used in ATLAS9; for lower values of log $g$, spherically symmetric geometry should be used instead (cf. Hauschildt et al. 1999, and Baraffe et al. 2002).

Other models that work with the appropriate geometry, like MARCS6 or Phoenix/NextGen (Allard & Hauschildt 1995; Hauschildt et al. 1999), are necessary for these small values. Indeed, MARCS6, whose main purpose is to model cool stars, also uses the approximation of spherically symmetric geometry to reproduce supergiants and the cool giant stars, which have low surface gravity (Plez et al. 1992). The NextGen models, like ATLAS9, assume LTE and plane-parallel geometry for dwarf stars, but a spherical symmetry is used for low-gravity giant and pre-main sequence stars (log $g < 3.5$, see Hauschildt et al. 1999).

In contrast to NeMo and MARCS6, NextGen can use a non-LTE model for high temperature stars. But using NLTE does not significantly improve the modelisation of our observed stars, as NLTE effects begin to occur only from 7000 K to higher effective temperatures (Hauschildt et al. 1999), but are still small to at least 10000 K. Moreover, NextGen does not reproduce the individual lines well enough owing to the treatment of atomic and molecular lines with a direct opacity sampling method. Indeed, working with opacity distribution functions, as in ATLAS9, would ask too much of computer resources when using NLTE calculations (Hauschildt et al. 1999). In addition to that, too few layers are used in the published models to describe the lower part of the photosphere.

However, NextGen could be an alternative to ATLAS9 type model atmospheres in a later step of our project, where generating spectra of stars with log $g$ below 2.0 (for which spherical symmetry is needed) and/or an effective temperature above 10000 K.

Bertone et al. (2004) compare both ATLAS9 and NextGen models to observations in the visible range along the whole spectral-type sequence. They conclude that both models
reproduce the spectral energy distribution of F type stars very well and do so for earlier type stars, but this good agreement decreases at lower temperature, especially for K stars, owing to the lack of molecular treatment in those models. Though ATLAS9 provides a better fit, in general, from B to K type stars, as said previously NextGen is more suitable for M stars, due to the use of spherical geometry for the giants and a more complete molecular line opacity. However, Martins et al. (2005) note that this comparison is made with a previous generation of NextGen models, using for example a mixing length parameter of 1 instead of the 2 preferred by hydrodynamic models. This is also true for the ATLAS9 models, as Bertone et al. (2004) did not use the latest versions of ATLAS9 that include new opacity distribution functions (Castelli & Kurucz 2003) and are computed with more up-to-date solar abundances and molecular contributions than the previous one.

Thus, a new comparison with observations in the visible range is not entirely useless. Moreover, an extensive comparison of spectra based on the NeMo grid of model atmospheres for the entire range of A to early M stars including both dwarfs and giants has not been done before. We thus begin our comparison with observations in the visual before proceeding to the infrared. The implications of changing abundances or the description of convection at spectral resolutions that are relevant to studies of galaxies are included as part of the discussion of our comparisons.

3. Obtaining a theoretical spectrum

First of all, we downloaded the model atmospheres corresponding to the needed stellar types from the NeMo website (http://ams.astro.univie.ac.at/nemo/). The models are classified according to the convection model (CM, CGM, or MLT) and to the number of layers representing the atmosphere. The model CGM with 72 layers is detailed enough for our purpose. Models with 288 layers are used only for specific applications like the calculation of the convective scale length in stellar interior models (Heiter et al. 2002). Reduced to the medium resolution of our observations, both computations of a model with 72 and 288 layers give similar spectra.

The next parameter to determine is the microturbulence velocity. For cool dwarf stars, this velocity is low at about 0–1 km s\(^{-1}\), but the value increases towards higher luminosities, reaching values as high as 5 km s\(^{-1}\) (Gray 1992). A few stars do not follow this rule: hot stars, like B and O type, have a negligible microturbulence velocity and some specific types of A stars can either have a null velocity (Ap type stars, for them magnetic field effects are important instead) or a velocity of 4 km s\(^{-1}\) (Am type stars). As the microturbulence velocity only has a small influence on the overall shape of the spectra and on the line profiles at our spectral resolution, we can use a common value of 2 km s\(^{-1}\) for comparison with all our stellar spectra, composed by A to early-M type dwarfs and F to K type giant stars, as 2 km s\(^{-1}\) is a good compromise for these stars (Gray 1992).

Then, the three main physical parameters of the star have to be chosen. The metallicity, the effective temperature, and the surface gravity of the theoretical stellar spectrum should correspond to the observed star to be compared as closely as possible. Therefore, once the stellar characteristics are determined, the nearest set of parameters (\(T_e\), \(\log g\), \(Z\)) in the NeMo grid is taken. The metallicity is taken from Nordström et al. (2004), Cayrel de Strobel et al. (2001), and Barbuy & Grenon (1990) when available for individual stars of the sample, otherwise assumed to be solar. Nordström et al. (2004) have determined the effective temperature of most of the dwarf stars in our sample; for other stars the effective temperature is assumed, as is the surface gravity, according to their spectral type from the corresponding values of temperature and gravity as given in Schmidt-Kaler (1982) and Gray (1992).

Once the most suitable model atmosphere is determined, we can generate a theoretical flux calibrated spectrum with the code SynthV (by VT). This code requires several input parameters, such as the wavelength range for which the spectrum will be computed, as well as the wavelength step. This step has to be small enough compared to 2.5 Å, as the desired opacity in each wavelength point includes absorption from all nearest lines within 2.5 Å, so large wavelength steps would give wrong results. We take 0.1 Å in the visible and in the infrared range. Then, we can enter a rotation profile for the star, if needed, and indicate a list of absorption lines to be used. For our work, we take the Vienna Atomic Linelist Database (VALD), completed by several molecular line lists (C\(_2\), CN, CO, H\(_2\), CH, NH, OH, MgH, SiH, SiO, TiO, H\(_2\)O\(^1\)). The line profiles are approximated by a Voigt function. SynthV also provides the possibility to change individual abundances.

The final theoretical spectrum has to be reduced to the same resolution and the same sampling as the observed spectrum for further comparisons. As a result, the calculated spectrum is Gaussian smoothed and resampled by Fourier interpolation to the same step as the observed spectrum.

4. Testing parameters

The determination of the physical parameters of the observed stars is not as accurate as we would like, so it is necessary to investigate the nearest values of \(T_{\text{eff}}\) / \(\log g \)/ \(Z\) on the grid. The chemical abundances can also be changed; as these abundances are not very well-determined, it is crucial to notice how a variation of the abundance of one element modifies the spectrum.

The most important change is caused by the temperature. Indeed, the step of 200 K chosen for the grid computation is still quite large for our purpose and a deviation in this range can be dramatic for the slope of the spectrum. The coldest stars (M, K, and even G type) are the ones most affected by a change of 200 K.

Figures 1 and 2 show the evolution of the spectra with temperature in the visible range for the dwarfs and the giants, respectively, and Fig. 3 shows this evolution for dwarf stars in the infrared range. We can see that for intermediate temperature, there is mainly a difference in continuum. But for the extreme

---

1 File VColl_molec.lns built by VT from Kurucz’ CDROMs 15, 24, 25, and 26, see Kurucz (1993b, 1999); the file is available from V. Tsymbal upon request.
values, the modification of the spectrum is more dramatic, as it also affects the absorption line features.

A change in log $g$ causes a variation in the line profiles. This parameter is not very well known for observed stars, so it is important to test different values around a first guess. Even if the variation caused by a gap of 0.2 in log $g$ is not very large, it can improve the comparison.

The metallicity has an influence on the slope of the continuum: increasing the metallicity of a theoretical spectrum has a similar influence on the continuum as does decreasing the temperature (see e.g. Ramírez & Meléndez 2005, for a detailed discussion). A variation in metallicity also clearly influences the strength of the absorption lines.

The variation of individual abundances can also cause some changes in the spectra. By default SynthV uses the solar abundances of Anders & Grevesse (1989). But some more recent studies, like the ones by Kurucz (1993a) or Holweger (2001), give different values for various elements (like He, Fe, O, C, N, etc.). These changes can be quite large (up to 0.2 dex for Fe). A simple test to probe the influence of different abundances was made by comparing two spectra assuming the same physical parameters, except for the solar abundance of Holweger (2001)
in one case and the one used by Kurucz (1993a) in the other. The result shows only slight differences, and the comparison with our observations cannot determine whether one is better than the other. For our work, we chose the values given by Holweger (2001).

In order to fit metallic stars, it is also important to check the influence of the modification of an individual element abundance on the synthetic spectrum. A change in the individual abundances of O and C leads to a modification of OH and CO line strengths, respectively. Indeed, when the ratio \( \frac{C}{O} \) increases, more CO molecules will be formed; on the other hand, when it decreases, more oxygen will be left to form OH molecules (see Decin et al. 2000).

For the hottest stars, it is important to take rotational velocity into account. At the medium resolution of our observations, a convolution with a Gaussian profile is good enough to reproduce this effect, so we do not need to include a more accurate description of the change in the profile of the lines caused by the rotational velocity. Consequently, even though SynthV allows computing spectra with a rotational velocity profile for the lines, we compute the spectra without rotational velocity in order to save computation time and convolve them afterwards with a Gaussian profile.

Additional tests have been made with a different microturbulence velocity for a very cool star (4 km s\(^{-1}\) for a M0V-type spectrum in the visible range) and a different number of layers for the convection model (288 instead of 72 for the same CGM model and the same physical parameters). At the resolution of the observed samples, these modifications do not lead to any difference.

5. Results in the visible range

Although our goal is to explore spectra in the infrared wavelength range, a study of the behaviour of the NeMo model atmospheres and spectra in the visible range provides us a good indication of their reliability as a function of the physical parameters of the stars.

5.1. Observations in the visible

The 18 spectra of observed stars (A to M dwarfs and G to K giants) that correspond to the range of the parameters in the NeMo grid were compared to theoretical stellar spectra. This sample of observed spectra at a resolving power of \( R \approx 600 \) was taken from the stellar library used by Boisson et al. (2000). One part of these observations came from the stellar library of Silva & Cornell (1992) made at the KPNO with the MARK III spectrograph; they cover the wavelength range 3500–9000 Å. These spectra are, for the most part, a mean-value for several stars of close spectral type. The name of these stars and the mean associated spectral types as given by Silva & Cornell are listed in Table 1. The remainder of the library, mainly supermetallic stars, were observed by Serote Roos et al. (1996) at the CFHT with the Herzberg spectrograph and at OHP with the Aurelie spectrograph. The spectral range is limited to 5000–9000 Å. The name, spectral type (or associated mean-spectral type), and parameters of these stars are listed in Table 1, and the atmospheric bands were removed from the observed spectra to compare with the theoretical spectra.

5.2. Comparisons

When the physical parameters (see Table 1) were known, we took the model with the nearest values; otherwise we used the mean values according to the spectral type as starting points and investigated the nearby values to find the best agreement between the observed and the computed spectra. The theoretical spectra were computed with a wavelength step of 0.1 Å,
corresponding to a resolution of 60,000 at 6000 Å, then Gaussian smoothed to the resolution of the observed spectra. By Fourier interpolation, we reduced the computed spectra to a resolution of 60 000 at 6000 Å, then Gaussian smoothed to the resolution of the observed spectra.

The agreement between the observed and computed spectra is satisfactory for effective temperatures ranging 4600 to 9000 K, with 9000 K corresponding to the highest temperature for the stars composing our sample. For these spectra, the main discrepancies, which consist in differences in the slope of the continuum, can be explained by the difficulty of having a good flux calibration at the wavelength ends of the observational data (in particular at 5000 Å where strong MgI, MgH and FeI absorptions are present). Various examples of comparisons for these stars are shown in Fig. 4–7. The spectral type of the observed stars and the physical parameters used to compute the theoretical spectra are noticed for each figure.

Three stars have a temperature below 4400 K, one dwarf and two giants. The M dwarf star (HD 36395) is particular as it has a very high metallicity. It is the most metallic star of Cayrel de Strobel’s catalog. Indeed, to correctly fit the observations, we need to set the metallicity of the theoretical star as high as possible (Fig. 8), but a metallicity of [M/H] = +1.0 dex is not realistic. However, recently Woolf & Wallerstein (2005) find a temperature of 3760 K (instead of 3850 K) and a metallicity of [Fe/H] = +0.2 dex for this star, so the discrepancies may be due simply to the difference in temperature, which is out of reach for NeMo.

The two others are K giant stars. First it is worth saying that at this low temperature, a difference of 200 K causes a greater variation in the slope of the continuum than for the highest temperatures. Thus, the continuum of the K3III observed star can not be correctly fitted by a computed spectrum whether with a temperature of 4400 K or with 4200 K, as the first one is too blue and the second is too red. Another difficulty comes from the Na line at 5894 Å and the MgH band being computed as too strong compared to the observations. These absorption features are very sensitive to a variation in temperature and too strong a value means that the temperature is too low, but increasing the temperature would lead to a continuum that is too blue. This is particularly clear for the K4III star, which lies on the boundaries of the NeMo grid for temperature and gravity (T = 4000 K, log g = 2.0), as we can see in Fig. 10. This star comes from the stellar library of Silva & Cornell (1992) whose original spectra extend down to 3500 Å. The agreement for the slope of the continuum is satisfactory, but the computed NaI line, the MgH band, as well as other lines and molecular bands such as e.g. CaII, CN, G band, are all too strong by far. If we set the temperature at 4200 K, which is still reasonable for this kind of star, the accordance for the lines and molecular bands would be better, but the slope of the observed continuum would be too red.

Table 1. List of observed stars in the visible, with the values of the parameters taken from the mean-values listed by Gray (1992) and Schmidt-Kaler (1982) or from (1) Nordström et al. (2004); (2) Cayrel de Strobel et al. (2001); and (3) Barbuy & Grenon (1990). In the last column, when no information is available on metallicity, a dash replaces it. The quantity (v sin i) is given in km s⁻¹.

| Name         | Spectral type | (v sin i) | T eff(K) | log g | [Fe/H] |
|--------------|---------------|----------|----------|-------|--------|
| HD 116608, HD 190785, HD 124320 & HD 221741 | A1–3 V     | 145      | 8900     | 4.2   | –      |
| HD 88815     | F2 V         | 90       | 7244     | 4.3   | −0.13  |
| HD 187691, HD 149890 | F8–9 V    | 7        | 6026, 5902 | 4.4   | 0.07, −0.44 |
| HD 121370    | rG0 IV       | 5        | 5957     | 4.4   | +0.27  |
| HD 38858     | G4 V         | 3        | 5636     | 4.5   | −0.26  |
| HD 161797    | rG5 IV       | 3        | 5700     | 4.5   | +0.23  |
| HD 149661, HD 151541, HD 33278, HD 23524, SAO 66004, SAO 84725 | G9K0 V    | 2        | 5176, 5236, 5300, 5200, 5300 | 4.5 | 0.01, −0.36, −0.49 |
| HD 93800     | rK0 V        | 2        | 5250     | 4.5   | +0.43  |
| HD 39715     | rK3 V        | 1        | 4850     | 4.6   | +0.33  |
| HD 36395     | rM1 V        | 1        | 3850     | 4.6   | +0.67  |
| HD 15866, HD 25894, HD 2506 | G0–4 III  | 10       | 5500     | 3.0   | –      |
| HD 163993    | wG8 III      | 3        | 4950     | 2.7   | −0.12  |
| HD 72324     | G9 III       | 3        | 4900     | 2.7   | –      |
| HD 33506, HD 112989 | rG9K2 III | 2        | 4700     | 2.6   | +0.14  |
| SAO 76803    | K2 III       | 2        | 4500     | 2.5   | –      |
| HD 181984    | rK2 III      | 2        | 4500     | 2.5   | +0.12  |
| HD 176670    | rK3 III      | 1        | 4300     | 2.2   | −0.03  |
| HD 154733, HD 21110 | K4 III  | 1        | 4000     | 2.0   | −0.14  |
The hypothesis of a plane-parallel geometry of the model begins to become unrealistic (low log gravity) and the molecular opacities, which are not taken sufficiently into account in ATLAS9, become significant for these cool stars.

6. Results in the infrared range

We can immediately say that there are, by far, more discrepancies between the computed and the observed spectra in the infrared than in the visible range, even at the medium resolution we have.

6.1. Observations in the infrared

The observed spectra for this wavelength range come from Meyer et al. (1998) and Boisson et al. (2002). Meyer’s are observations at a resolving power of $R \approx 3000$ at 1.6 $\mu$m with
the KPNO Mayall 4 m Fourier Transform Spectrometer; these spectra have to be calibrated in flux. The stars from Boisson et al. (2002) come from the ISAAC spectrograph mounted on the VLT telescope, at a resolving power of $R \approx 3300$ at $1.6 \mu m$. From these samples, we selected 23 stars matching the available parameters of NeMo (A to M dwarfs and F to K giants), listed in Table 2.

6.2. Comparisons

Around $1.6 \mu m$ hot stars are dominated by the Brackett lines, and a good determination of the rotational velocity of these stars, that broadens the lines is very important to have the best possible match between the computation and the observation. In our wavelength range, the Brackett lines at 1.588, 1.611, and...
1.641 μm are nearly the only features of the observed spectra. They are well fitted by the theoretical spectra.

When the temperature decreases, some atomic features appear and the comparison between observed and computed spectra deteriorates. Indeed, for the F6V, quite a large amount of metallic lines, visible in the observed spectra, are not present or are too weak in the computed spectra, and this trend continues with the F8.5V (Fig. 11). The continuum of these observed spectra is reproduced very well, but this is not the case for the lines: most of the metallic lines are computed as too weak.

In addition, for the F8.5V star, the Brackett lines at 1.611 and 1.641 μm, are computed to be too strong. Indeed, the Brackett lines have almost disappeared in the observed spectrum but are still strong in the computation. These Brackett lines are also present in all the theoretical G stars, which is not always the case for observed stars, as seen in Fig. 12.
The observed spectrum (in black) as the mean-value of two K4III type stars (HD 154733 and HD 21110). The theoretical one (in grey) is computed with the following parameters: $T = 4000$ K, $\log g = 2.0$, solar metallicity. The scale of this plot is not the same as for the previous figures.

Table 2. List of observed stars in the infrared, with the values of the parameters taken from the mean-values listed by Gray (1992) and Schmidt-Kaler (1982) or from (1) Nordström et al. (2004); (2) Cayrel de Strobel et al. (2001); and (3) Barbuy & Grenon (1990). In the last column, when no information on metallicity is available, a dash replaces it.

| Name     | Spectral type | $\langle v \sin i \rangle$ (km s$^{-1}$) | $T_{\text{eff}}$(K) | $\log g$ | [Fe/H] |
|----------|---------------|----------------------------------------|---------------------|----------|--------|
| HD 159217 | A0 V          | 150                                    | 9700                | 4.3      | –      |
| HD 27397  | F0 IV         | 120                                    | 7100                | 4.3      | –      |
| HD 48501  | F2 V          | 90                                     | 6850                | 4.3      | +0.01  |
| HD 26015  | F3 V          | 65                                     | 6776$^1$            | 4.3      | +0.11$^1$ |
| HD 30606  | F6 V          | 10                                     | 6152$^1$            | 4.4      | −0.01$^2$  |
| HD 98231  | F8.5 V        | 7                                      | 5794$^1$            | 4.4      | −0.35$^2$  |
| HD 112164 | G1.5 V        | 5                                      | 5768$^1$            | 4.4      | +0.24$^2$  |
| HD 10307  | G1.5 V        | 4                                      | 5781$^1$            | 4.4      | −0.04$^2$  |
| HD 98230  | G2 V          | 4                                      | 5794$^1$            | 4.5      | −0.34$^2$  |
| HD 106116 | G4 V          | 3                                      | 5572$^2$            | 4.5      | +0.15$^2$  |
| HD 20618  | G6 IV         | 2                                      | 5600                | 4.5      |        |
| HD 101501 | G8 V          | 2                                      | 5408$^1$            | 4.5      | +0.03$^2$  |
| HD 185144 | K0 V          | 2                                      | 5212$^1$            | 4.5      | −0.29$^1$  |
| HD 22049  | K2 V          | 2                                      | 5117$^2$            | 4.6      | −0.14$^2$  |
| HD 39715  | K3 V          | 1                                      | 4850                | 4.6      | +0.33$^3$  |
| HD 131977 | K4 V          | 1                                      | 4700                | 4.6      | +0.03$^2$  |
| HD 201902 | K7 V          | 1                                      | 4100                | 4.6      | −0.63$^2$  |
| GL 338    | M0 V          | 1                                      | 3900                | 4.6      | −        |
| HD 89025  | F0 III        | 80                                     | 7100                | 3.4      |        |
| HD 432    | F2 III        | 75                                     | 7278$^1$            | 3.2      | +0.18$^1$  |
| HD 107950 | G6 III        | 4                                      | 5050                | 2.8      | −0.16$^2$  |
| HD 197989 | K0 III        | 2                                      | 4800                | 2.7      | −0.19$^2$  |
| HD 3627   | K3 III        | 2                                      | 4300                | 2.0      | +0.04$^2$  |

The behaviour of the computed Brackett lines towards the temperature is shown on Fig. 3, while the Brackett lines are still present in theoretical spectra for temperatures as low as 5200 K.

Then, when the temperature decreases, as expected, the Brackett lines are fainter and atomic lines (FeI, SiI, MgI and CaI) become stronger and stronger for both the observed and theoretical spectra. But the agreement between the computed and the observed stars becomes worse. From Figs. 12 to 15, the residuals between observed and theoretical spectra show that several absorption lines are missing in the theoretical stars, iron lines for the most part. The model atmosphere cannot be...
the reason because the continuum shape is very good and several lines match perfectly, but the line list needs to be improved.

In the infrared range, the lack of several metallic and molecular lines causes the discrepancies, with enhanced differences at low temperature due to the greatest strength of the lines for the coolest star (Fig. 15). Figures 13 and 14 present two similar stars (K2V and K4V, respectively): the first one is from Meyer, the second a VLT observation at higher resolution. Both comparisons show this lack of absorption lines, with more details visible in Fig. 14.

The comparison for the coolest dwarf star in this sample, a M0V, is not so bad for such a low temperature, and the continuum is good in spite of the limitations of the model (Fig. 16). We notice, however, that in contrast to the previous spectra, the absorption lines computed as too strong for the theoretical spectrum, as seen thanks to the residual. This is probably due...
to the validity limit of the model atmospheres, as already seen in the visible range.

In order to further investigate which lines are missing in the computations, we compared (Fig. 18) the high-resolution spectrum of the well-known K1III star Arcturus (Hinkle et al. 1995) to a theoretical spectrum computed with the parameters of this star \( (T_{\text{eff}} = 4400 \text{ K}, \log g = 2.0, [\text{M/H}] = -0.2, v \sin i = 3.5 \text{ km s}^{-1}) \) and point out the discrepancies. Figure 19 shows a detail of this comparison, and Table 3 lists the missing lines in the whole range. In addition to the lines quoted in Table 3, several other features are computed as too weak, in particular OH and CO molecular bands, most certainly due to an inaccurate determination of the oscillator strengths, as discussed in Lyubchik et al. (2004).

This study, based on the NeMo grids of atmospheres, remains valid for the entire family of ATLAS models. As shown

Fig. 13. The observed spectrum (in black) from a K2V type star (HD 22049), and the theoretical one (in grey) computed with the following parameters: \( T = 4800 \text{ K}, \log g = 4.6, [\text{M/H}] = -0.1 \) dex.

Fig. 14. The observed spectrum (in black) from a K4V type star (HD 131977), and the theoretical one (in grey) computed with the following parameters: \( T = 4800 \text{ K}, \log g = 4.6, \) solar metallicity.
in Fig. 17, two theoretical spectra computed for the same physical parameters with the NeMo grid and the ATLAS9 models with the overshooting prescription (Kurucz 1993a, 1998; Castelli et al. 1997, respectively) are very similar at our spectral resolution. The discrepancies between the two different theoretical spectra are very faint compared to the discrepancies between the models and the observed spectra.

The same ATLAS9 models, but without overshooting (NOVER models, Castelli et al. 1997), present even less differences with the NeMo spectra, in particular the slight discrepancy found for the Brackett lines disappear. They are more sensitive than other lines to the fact that the Kurucz overshooting prescription changes the temperatures at Rosseland optical depths of 0.1 to 0.5.

Fig. 15. The observed spectrum (in black) from a K3III type star (HD 3627), as above the theoretical one (in grey) computed with the following parameters: $T = 4400$ K, log $g = 2.0$, solar metallicity.

Fig. 16. The observed spectrum (in black) from a M0V type star (GL 338), as above the theoretical one (in grey) computed with the following parameters: $T = 4000$ K, log $g = 4.6$, solar metallicity.
7. Conclusions

In spite of some discrepancies, the comparisons between observed and theoretical spectra in the visible range suggests a reasonable agreement, even at the limits of the parameter range of NeMo. However, we have to be careful when we compute a model near the lower limit in temperature.

The spectra modeled with NeMo can be used to build a theoretical spectral library for A to K dwarf and giant stars in the visible range, but this is not the case for the near-infrared range. Indeed, in the range 1.57 to 1.67 μm, the computed spectra do not reproduce the observations very well. Despite good agreement for the overall flux distribution shape, we can see that there are many differences in the line features when focusing on the details of the spectra. The strength of the infrared absorption lines is usually underestimated in calculations, and some lines are simply missing (Fe, OH, and CO lines are the most problematic). As pointed out by Decin et al. (2003) for the MARCS6 models and Lyubchik et al. (2004) for NextGen models of ultracool dwarfs and a Kurucz model for Arcturus, it was not possible to generate synthetic spectra that can reproduce observed spectra in the infrared with the line lists that have been used in constructing the model atmospheres, even at
Table 3. List of the missing lines, according to the comparison between Arcturus and a computed spectrum. The Ni line is not missing, as such, but shifted by 2 Å in the atomic database.

| Wavelength (µm) | Element | Wavelength (µm) | Element |
|-----------------|---------|-----------------|---------|
| 1.5764          | Fe      | 1.6208          | Fe      |
| 1.5893          | Fe      | 1.6214          | Fe      |
| 1.5895          | Fe      | 1.6231          | Fe      |
| 1.5913          | Fe      | 1.6285          | Fe      |
| 1.5939          | Fe      | 1.6316          | Fe      |
| 1.5954          | Fe      | 1.6319          | Fe      |
| 1.5968          | Fe      | 1.6362          | Ni      |
| 1.6007          | Fe      | 1.6394          | Fe      |
| 1.6008          | Fe      | 1.6440          | Fe      |
| 1.6041          | Fe      | 1.6450          | OH      |
| 1.6071          | Fe      | 1.6517          | Fe      |
| 1.6076          | Fe      | 1.6524          | Fe      |
| 1.6088          | Fe      | 1.6532          | Fe      |
| 1.6116          | Fe      | 1.6569          | Fe      |
| 1.6126          | Fe      |                 |         |
| 1.6175          | Fe      |                 |         |
| 1.6195          | Fe      |                 |         |

a medium resolution. In particular, the oscillator strengths are still not known well enough.

We also compared spectra that include the lines from iron peak elements with predicted energy levels, as published by Kurucz (1998), along with the observations of Arcturus discussed above. As expected, such spectra contain more lines, but the inaccuracy of their energy levels frequently places them at the wrong wavelengths, and the overall match hardly improves. The total flux distribution over all wavelength ranges, particularly in the ultraviolet, is closer to observations when including this set of lines; but for the limited wavelength range around the H band, the effects are small and sufficiently compensated for when setting the zero point of the flux distribution. For the case of Arcturus we also made a comparison with spectra computed with PHOENIX in LTE (P. Hauschildt, priv. comm. 2005). The resulting spectra for the 1.57 to 1.67 µm range were found to be fairly similar to those from NeMo/VALD/SynthV when including the predicted level lines. One important reason for this must be that the atomic line lists for PHOENIX are essentially those of Kurucz (1998). Because the flux distribution of the PHOENIX spectra is similar to the observations, as well, at least for the K giants the detailed choice of the model atmosphere code appears to be clearly less important than the choice of atomic line lists (note that PHOENIX uses its own collection of molecular line lists, different from the one we have used here). Considering how uniform the deterioration of the match of spectra in the 1.57 to 1.67 µm range is when looking at the sequence from F to K stars, we conclude that the insufficient line lists and, in particular, lists of atomic lines are the main obstacles to a more satisfactory match of the observed spectra of these groups of stars. The modelling in the infrared range needs some further improvements, in particular in the absorption lines database, before building a theoretical spectral library that can be used with greater benefit than a library of observed stars.

The lack of M stars in the spectral library would definitely hinder the study of stellar populations, as the variations in their strong atomic lines and molecular bands during their evolution from dwarf to supergiant to giant provides very good age discriminators (from 10⁶ to 10¹⁰ yr). The M stars peak in a wavelength range that is not absorbed much even in heavily reddened regions, such as young stellar clusters, making them easily detected. Moreover, they are known to be very big contributors to the stellar populations of galaxies, as much for their
mass as for the luminosity. All this makes a good theoretical library of M stars very critical in order to extend incompletely observed libraries.

The prospects of constructing such a library from the upcoming generation of model atmospheres (MARCS, PHOENIX, perhaps future versions of ATLAS) are indeed improving because of the enormous efforts being made to extend the molecular line data and equation of state. To match the spectra of the hot end of M stars in the H band will nevertheless require more complete atomic data, although this is less crucial that for K stars. Efforts in this direction are currently being made.

Acknowledgements. F.K. gratefully acknowledges the hospitality of the Observatoire de Paris-Meudon during his stays as an invited visitor. J.F. also thanks the kind people of the AMS group at the Vienna Observatory for their hospitality and help during part of this work. V.T. acknowledges the support by the Austrian Fonds zur Förderung der wissenschaftlichen Forschung FwF (P17580) and by the BM:BWK (project COROT). This research made use of the model atmosphere grid NeMo, provided by the Department of Astronomy of the University of Vienna, Austria, and funded by the Austrian FwF (P14984). We are thankful to Peter Hauschildt who computed the comparison spectra for Arcturus for us, which helped to demonstrate the importance of the line lists used relative to the particular choice of model atmosphere codes.

References

Allard, F., & Hauschildt, P. H. 1995, ApJ, 445, 433
Anders, E., & Grevesse, N. 1989, Geochem. Cosmochim. Acta, 53, 197
Baguhl, S., Jehin, E., Ledoux, C., et al. 2003, The Messenger, 114, 10
Baraffe, I., Chabrier, G., Allard, F., & Hauschildt, P. H. 2002, A&A, 382, 563
Barbey, B., & Giro, M. 1990, in ESO/CTIO Workshop on Bulges of Galaxies, 83
Barone, E., Buzzoni, A., Chavez, M., & Rodriguez-Merino, L. H. 2004, AJ, 128, 829
Boisson, C., Joly, M., Moulata, J., Pelat, D., & Serro Roos, M. 2000, A&A, 357, 850
Boisson, C., Coupé, S., Cuby, J. G., Joly, M., & Ward, M. J. 2002, A&A, 396, 489
Bruijza, G., & Charlot, S. 2003, MNRAS, 344, 1000
Canuto, V. M., & Mazzitelli, I. 1991, ApJ, 370, 295
Canuto, V. M., & Mazzitelli, I. 1992, ApJ, 389, 724
Canuto, V. M., Goldman, I., & Mazzitelli, I. 1996, ApJ, 473, 550
Castelli, F., & Kurucz, R. L. 2003, in Modelling of Stellar Atmospheres, ed. N. E. Piskunov, W. W. Weiss, & D. F. Gray, IAU Symp., 210, A20C
Castelli, F., Gratton, R., & Kurucz, R. L. 1997, A&A, 318, 841, erratum: 1997, A&A, 324, 432
Cayrel de Strobl, G., Soubran, C., & Raile, N. 2001, A&A, 373, 159
Cid Fernandes, R., Mateus, A., Sodré, L., Stasińska, G., & Gomes, J. M. 2005, MNRAS, 358, 363
Dallier, R., Boisson, C., & Joly, M. 1996, A&AS, 116, 239
Decin, L., Vandenbussche, B., Waelkens, C., et al. 2003, A&A, 400, 679
Decin, L., Waelkens, C., Eriksson, K., et al. 2000, A&A, 364, 137
Fuhrmann, K., Axer, M., & Ghebren, T. 1993, A&A, 271, 451
Gray, D. F. 1992, The observation and analysis of stellar photospheres (Cambridge University Press)
Gustafsson, B., Bell, R.A., Eriksson, K., & Nordlund, Å. 1975, A&A, 42, 407
Hauschildt, P. H., Allard, F., Ferguson, J., Baron, E., & Alexander, D. R. 1999, ApJ, 525, 871
Heiter, U., Kupka, F., van’t Veer-Menneret, C., et al. 2002, A&A, 392, 619
Hinkle, K., Wallace, L., & Livingston, W. 1995, PASP, 107, 1042
Holweger, H. 2001, in SOHO/ACE Workshop Solar and Galactic Composition, ed. R. F. Wimmer-Schweingruber (Springer, New York), AIP Conf. Ser., 598, 23
Hubeny, I. 1988, Computer Physics Comm., 52, 103
Hubeny, I., & Lanz, T. 1995, ApJ, 439, 875
Ivanov, V. D., Rieke, M. J., Engelbracht, C. W., et al. 2004, ApJS, 151, 387
Kupka, F., Piskunov, N. E., Ryabchikova, T. A., Stempels, H. C., & Weiss, W. W. 1999, A&AS, 138, 119
Kurucz, R. L. 1992, in The Stellar Population of Galaxies, ed. B. Barbuy, & A. Renzini (Dordrecht: Kluwer), IAU Symp., 149, 225
Kurucz, R. L. 1993a, ATLAS9 Stellar atmospheres programs and 2 km s−1 grid, CD-ROM 13, SAO
Kurucz, R. L. 1993b, Atomic data for molecules, CD-ROM 15, SAO
Kurucz, R. L. 1998, http://kurucz.harvard.edu/, http://cfaku5.cfa.harvard.edu/
Kurucz, R. L. 1999, Atomic data for TiO and H2O, CD-ROMs 24, 25 and 26, SAO
Lanz, T., & Hubeny, I. 2003, ApJS, 146, 417
Le Borgne, D., Rocca-Volmerange, B., Prugniel, P., et al. 2004, A&A, 425, 881
Le Borgne, J.-F., Bruzual, G., Pelló, R., et al. 2003, A&A, 402, 433
Leitherer, C., Schaerer, D., Goldader, J. D., et al. 1999, ApJS, 123, 3
Lyubchik, Y., Jones, H. R. A., Pavlenko, Y. V., et al. 2004, A&A, 416, 655
Martins, L., P. González Delgado, R. M., Leitherer, C., Cerviño, M., & Hauschildt, P. 2005, MNRAS, 358, 49
Meyer, M. R., Edwards, S., Hinkle, K. H., & Strom, S. E. 1998, ApJ, 508, 397
Moulata, J., & Pelat, D. 2000, MNRAS, 314, 409
Munari, U., Sordo, R., Castelli, F., & Zwitter, T. 2005, A&A, 442, 1127
Murphy, T., & Meiksin, A. 2004, MNRAS, 351, 1430
NeMo website, 2003, http://amsastro.univie.ac.at/nemo/
Nendwich, J., Heiter, U., Kupka, F., Nesvadl, N., & Weiss, W. W. 2004, Comm. Asteroseism., 144, 43
Nordström, B., Mayor, M., Andersen, J., et al. 2004, A&A, 418, 989
Pelat, D. 1999, ApJ, 522, 789
Plez, B., Brett, J. M., & Nordlund, Å. 1992, A&A, 256, 551
Ramírez, I., & Meléndez, J. 2005, ApJ, 626, 446
Schmidt-Kaler, Th. 1982, in Landolt-Börnstein; Stars and star clusters. Numerical data and functional relationships in science and technology, ed. K. Schaifers, & H. H. Vöight, Group IV, V ol. 2b
Serro Roos, M., Boisson, C., & Joly, M. 1996, A&AS, 117, 93
Silva, D., & Cornell, M. 1992, ApJS, 81, 865
Stothers, R. B., & Chin, C. 1997, ApJ, 478, L103
Valdes, F., Gupta, R., Rose, J. A., Singh, H. P., & Bell, D. J. 2004, ApJS, 152, 251
van’t Veer-Menneret, C., & Mégessier, C. 1996, A&A, 309, 879
Woolf, V. M., & Wallerstein, G. 2005, MNRAS, 356, 963