Lifting from the Deep: Convolutional 3D Pose Estimation from a Single Image

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Abstract

We propose a unified formulation for the problem of 3D human pose estimation from a single raw RGB image that reasons jointly about 2D joint estimation and 3D pose reconstruction to improve both tasks. We take an integrated approach that fuses probabilistic knowledge of 3D human pose with a multi-stage CNN architecture and uses the knowledge of plausible 3D landmark locations to refine the search for better 2D locations. The entire process is trained end-to-end, is extremely efficient and obtains state-of-the-art results on Human3.6M outperforming previous approaches both on 2D and 3D errors.

1. Introduction

Estimating the full 3D pose of a human from a single RGB image is one of the most challenging problems in computer vision. It involves tackling two inherently ambiguous tasks. First, the 2D location of the human joints, or landmarks, must be found in the image, a problem plagued with ambiguities due to the large variations in visual appearance caused by different camera viewpoints, external and self occlusions or changes in clothing, body shape or illumination. Next, lifting the coordinates of the 2D landmarks into 3D from a single image is still an ill-posed problem – the space of possible 3D poses consistent with the 2D landmark locations of a human, is infinite. Finding the correct 3D pose that matches the image requires injecting additional information usually in the form of 3D geometric pose priors and temporal or structural constraints.

We propose a new joint approach to 2D landmark detection and full 3D pose estimation from a single RGB image that takes advantage of reasoning jointly about the estimation of 2D and 3D landmark locations to improve both tasks. We propose a novel CNN architecture that learns to combine the image appearance based predictions provided by convolutional-pose-machine style 2D landmark detectors [44], with the geometric 3D skeletal information encoded in a novel pretrained model of 3D human pose.

Information captured by the 3D human pose model is embedded in the CNN architecture as an additional layer that lifts 2D landmark coordinates into 3D while imposing that they lie on the space of physically plausible poses. The advantage of integrating the output proposed by the 2D landmark location predictors – based purely on image appearance – with the 3D pose predicted by a probabilistic model, is that the 2D landmark location estimates are improved by guaranteeing that they satisfy the anatomical 3D constraints encapsulated in the human 3D pose model. In this way, both tasks clearly benefit from each other.

A further advantage of our approach is that the 2D and 3D training data sources may be completely independent. The deep architecture only needs that images are annotated with 2D poses, not 3D poses. The human pose model is trained independently and exclusively from 3D mocap data. This decoupling between 2D and 3D training data presents a huge advantage since we can augment the training sets completely independently. For instance we can take advantage of extra 2D pose annotations without the need for 3D ground truth or extend the 3D training data to further mocap datasets without the need for synchronized 2D images.

Our contribution: In this work, we show how to integrate a prelearned 3D human pose model directly within a novel CNN architecture (illustrated in figure 1) for joint 2D landmark and 3D human pose estimation. In contrast to pre-existing methods, we do not take a pipeline approach that takes 2D landmarks as given. Instead, we show how such a model can be used as part of the CNN architecture itself, and how the architecture can learn to use physically plausible 3D reconstructions in its search for better 2D landmark locations. Our method achieves state-of-the-art results on the Human3.6M dataset both in terms of 2D and 3D errors.

2. Related Work

We first describe methods that assume that 2D joint locations are provided as input and focus on solving the 3D
lifting problem and follow with methods that learn to estimate the 3D pose directly from images.

**3D pose from known 2D joint positions:** A large body of work has focused on recovering the 3D pose of people given perfect 2D joint positions as input. Early approaches [19, 34, 25, 6] took advantage of anatomical knowledge of the human skeleton or joint angle limits to recover pose from a single image. More recent methods [13, 28, 3] have focused on learning a prior statistical model of the human body directly from 3D mocap data.

Non-rigid structure from motion approaches (NRSfM) also recover 3D articulated motion [8, 4, 14, 20] given known 2D correspondences for the joints in every frame of a monocular video. Their huge advantage, as unsupervised methods, is they do not need 3D training data, instead they can learn a linear basis for the 3D poses purely from 2D data. Their main drawback is their need for significant camera movement throughout the sequence to guarantee accurate 3D reconstruction. Recent work on NRSfM applied to human pose estimation has focused on escaping these limitations by the use of a linear model to represent shape variations of the human body. For instance, [10] defined a generative model based on the assumption that complex shape variations can be decomposed into a mixture of primitive shape variations and achieve competitive results.

Representing human 3D pose as a linear combination of a sparse set of 3D bases, pretrained using 3D mocap data, has also proved a popular approach for articulated human motion [28, 43, 49], while [49] propose a convex relaxation to jointly estimate the coefficients of the sparse representation and the camera viewpoint [28] and [43] enforce limb length constraints. Although these approaches can reconstruct 3D pose from a single image, their best results come from imposing temporal smoothness on the reconstructions of a video sequence.

Recently, Zhao et al. [47] achieved state-of-the-art results by training a simple neural network to recover 3D pose from known 2D joint positions. Although the results on perfect 2D input data are impressive, the inaccuracies in 2D joint estimation are not modeled and the performance of this approach combined with joint detectors is unknown.

**3D pose from images:** Most approaches to 3D pose inference directly from images fall into one of two categories: (i) models that learn to regress the 3D pose directly from image features and (ii) pipeline approaches where the 2D pose is first estimated, typically using discriminatively trained part models or joint predictors, and then lifted into 3D. While regression based methods suffer from the need to annotate all images with ground truth 3D poses – a technically complex and elaborate process – for pipeline approaches the challenge is how to account for uncertainty in the measurements. Crucial to both types of approaches is the question of how to incorporate the 3D dependencies between the different body joints or to leverage other useful 3D geometric information in the inference process.

Many earlier works on human pose estimation from a single image relied on discriminatively trained models to learn a direct mapping from image features such as silhouettes, HOG or SIFT, to 3D human poses without passing through 2D landmark estimation [1, 12, 11, 24, 32].

Recent direct approaches make use of deep learning [21, 22, 40, 41]. Regression-based approaches train an end-to-end network to predict 3D joint locations directly from the image [41, 21, 22, 48]. Li et al. [22] incorporate model joint dependencies in the CNN via a max-margin formalism, others [48] impose kinematic constraints by embedding a dif-
ferentiable kinematic model into the deep learning architecture. Tekin et al. [35] propose a deep regression architecture for structured prediction that combines traditional CNNs for supervised learning with an auto-encoder that implicitly encodes 3D dependencies between body parts.

As CNNs have become more prevalent, 2D joint estimation [44] has become increasingly reliable and many recent works have looked to exploit this using a pipeline approach. Papers such as [9, 16, 40, 26] first estimate 2D landmarks and later 3D spatial relationships are imposed between them using structured learning or graphical models.

Simo-Serra et al. [33] were one of the first to propose an approach that naturally copes with the noisy detections inherent to off-the-shelf body part detectors by modeling their uncertainty and propagating it through 3D shape space while satisfying geometric and kinematic 3D constraints. The work [31] also estimates the location of 2D joints before predicting 3D pose using appearance and the probable 3D pose of discovered parts using a non-parametric model. Another recent example is Bogo et al. [7], who fit a detailed statistical 3D body model [23] to 2D joint proposals.

Zhou et al. [50] tackles the problem of 3D pose estimation for a monocular image sequence integrating 2D, 3D and temporal information to account for uncertainties in the model and the measurements. Similar to our proposed approach, Zhou et al.’s method [50] does not need synchronized 2D-3D training data, i.e., it only needs 2D pose annotations to train the CNN joint regressor and a separate 3D mocap dataset to learn the 3D sparse basis. Unlike our approach, it relies on temporal smoothness for its best performance and performs poorly on a single image.

Finally, Wu et al. [45]’s 3D Interpreter Network, a recent approach to estimate the skeletal structure of common objects (chairs, sofas, …) bears similarities with our method. Although our approaches share common ground in the decoupling of 3D and 2D training data and the use of projection from 3D to improve 2D predictions the network architectures are very different and, unlike us, they do not carry out a quantitative evaluation on 3D human pose estimation.

4. Probabilistic 3D Model of Human Pose

One fundamental challenge in creating models of human poses lies in the lack of access to 3D data of sufficient variety to characterize the space of human poses. To compensate for this lack of data we identify and eliminate confounding factors such as rotation in the ground plane, limb length, and left-right symmetry that lead to conceptually similar poses being unrecognized in the training data.

Simple preprocessing eliminates some factors. Size variance is addressed by normalizing the data such that the sum of squared limb lengths on the human skeleton is one; while left-right symmetry is exploited by flipping each pose in the x-axis and re-annotating left as right and vice-versa.

4.1. Aligning 3D Human Poses in the Training Set

Allowing for rotational invariance in the ground-plane is more challenging and requires integration with the data model. We seek the optimal rotations for each pose such that after rotating the poses they are closely approximated by a low-rank compact Gaussian distribution.

We formulate this as a problem of optimization over a set of variables. Given a set of \( N \) training 3D poses, each represented as a \((3 \times L)\) matrix \( P_i \) of 3D landmark locations, where \( i \in \{1, 2, ..., N\} \) and \( L \) is the number of human joints/landmarks; we seek global estimates of an average 3D pose \( \mu \), a set of \( J \) orthonormal basis matrices\(^1\) \( e \) and noise variance \( \sigma \), alongside per sample rotations \( R_i \) and basis coefficients \( a_i \) to minimize the following estimate

\[
\arg \min_{R, \mu, a, e, \sigma } \sum_{i=1}^{N} \left( \| P_i - R_i (\mu + a_i \cdot e) \|_2^2 \right) + \sum_{j=1}^{J} (a_{i,j} \cdot \sigma_j)^2 + \ln \sum_{j=1}^{J} \sigma_j^2
\]

Where \( a_i \cdot e = \sum_j a_{i,j} e_j \) is the tensor analog of a multiplication between a vector and a matrix, and \( \| \cdot \|_2^2 \) is the squared Frobenius norm of the matrix. Here the \( y \)-axis is assumed to point up, and the rotation matrices \( R_i \) considered are ground plane rotations. With the large number of 3D pose samples considered (of the order of 1 million when training on the Human3.6M dataset [15]), and the complex inter-dependencies between samples for \( e \) and \( \sigma \), the memory requirements mean that it is not possible to solve directly as a joint optimization over all variables using a non-linear solver such as Ceres. Instead, we carefully initialize

\(^1\)When we say \( e \) is a set of orthonormal basis matrices we mean that each matrix, if unwrapped into a vector, is of unit norm and orthogonal to all other unwrapped matrices.
and alternate between performing closed-form PPCA \cite{38} to update \( \mu, \alpha, \beta, \sigma ; \) and updating \( R_t \) using Ceres \cite{2} to minimize the above error. As we do this, we steadily increase the size of the basis from 1 through to its target size \( J \). This stops apparent deformations that could be resolved through rotations from becoming locked into the basis at an early stage, and empirically leads to lower cost solutions.

To initialize we use a variant of the Tomasi-Kanade \cite{39} algorithm to estimate the mean 3D pose \( \mu \). As the \( y \) component is not altered by planar rotations, we take as our estimate of the \( y \) component of \( \mu \), the mean of each point in the \( y \) direction. For the \( x \) and \( z \) components, we interleave the \( x \) and \( z \) components of each sample and concatenate them into a large \( 2N \times L \) matrix \( M \), and find the rank two approximation of this such that \( M \approx \hat{A} \cdot B \). We then calculate \( \hat{A} \) by replacing each adjacent pair of rows of \( A \) with the closest orthonormal matrix of rank two, and take \( \hat{A}^\dagger M \) as our estimate\(^2\) of the \( x \) and \( z \) components of \( \mu \).

The end result of this optimization is a compact low-rank approximation of the data in which all reconstructed poses appear to have the same orientation (see Figure 2). In the next section we extend the model to be described as a multi-modal distribution to better capture the variations in the space of 3D human poses.

4.2. A Multi-Modal Model of 3D Human Pose

Although the learned Gaussian model of section 4.1 can be directly used to estimate the 3D (see Table 1), inspection of figure 2 shows that the data is not Gaussian distributed and is better described using a multiple modal distribution. In doing this, we are heavily inspired both by approaches such as \cite{27} which characterize the space of human poses as a mixture of PCA bases, and by related works such as \cite{42,8} that represent poses as an interpolation between exemplars. These approaches are extremely good at modeling tightly distributed poses (e.g. walking) where samples in the testing data are likely to be close to poses seen in training. This is emphatically not the case in much of the Human3.6M dataset, which we use for evaluation. Zooming in on the edges of Figure 2 reveals many isolated paths where motions occur once and are never revisited again.

 Nonetheless, it is precisely these regions of low-density that we are interested in modeling. As such, we seek a coarse representation of the pose space that says something about the regions of low density but also characterizes the multi-modal nature of the pose space. We represent the data as a mixture of probabilistic PCA models using few clusters, and trained using the EM-algorithm \cite{38}. When using a small number of clusters, it is important to initialize the algorithm correctly, as accidentally initializing with multiple clusters about a single mode, can lead to poor density estimates. To initialize we make use of a simple heuristic.

We first subsample the aligned poses (which we refer to as \( P \)), and then compute the Euclidean distance \( d \) among pairs. We seek a set of \( k \) samples \( S \) such that the distance between points and their nearest sample is minimized

\[
\arg\min_S \sum_{p \in P} \min_{s \in S} d(s, p) \tag{2}
\]

We find \( S \) using greedy selection, holding our previous estimate of \( S \) constant, and iteratively selecting the next candidate \( s \) such that \( \{s\} \cup S \) minimizes the above cost. A selection of 3D pose samples found using this procedure can be seen in the rendered poses of Figure 2. In practice, we stop proposing candidates when they occur too close to the existing candidates, as shown by samples (a–d), and only choose one candidate from the dominant mode.

Given these candidates for cluster centers, we assign each aligned point to a cluster representing its nearest candidate and then run the EM algorithm of \cite{38}, building a mixture of probabilistic PCA bases.

5. A New Convolutional Architecture for 2D and 3D Pose Inference

Our 3D pose inference from a single RGB image makes use of a multistage deep convolutional architecture, trained end-to-end, that repeatedly fuses and refines 2D and 3D poses, and a second module which takes the final predicted 2D landmarks and lifts them one last time into 3D space for the final estimate (see Figure 1).

At its heart, the architecture is a novel refinement of the Convolutional Pose Machine of Wei et al. \cite{44}, who reasoned exclusively in 2D, and proposed an architecture that
iteratively refined 2D pose estimations of landmarks using a mixture of knowledge of the image and of the estimates of landmark locations of the previous stage. We modify this architecture by generating, at each stage, projected 3D pose belief maps which are fused in a learned manner with the standard maps. From an implementation point of view this is done by introducing two distinct layers, the probabilistic 3D pose layer and the fusion layer (see Figure 1).

Figure 3 shows how the 2D uncertainty in the belief maps is reduced at each stage of the architecture and how the accuracy of the 3D poses increases with each stage.

5.1. Architecture of each stage

The sequential architecture consists of 6 stages. Each stage consists of 4 distinct components (see Figure 1):

Predicting CNN-based belief-maps: we use a set of convolutional and pooling layers, equivalent to those used in the original CPM architecture [44], that combine evidence obtained from image learned features with the belief maps obtained from the previous stage \((t-1)\) to predict an updated set of belief maps for the 2D human joint positions.

Lifting 2D belief-maps into 3D: the output of the CNN-based belief maps is taken as input to a new layer that uses new pretrained probabilistic 3D human pose model to lift the proposed 2D poses into 3D.

Projected 2D pose belief maps: The 3D pose estimated by the previous layer is projected back onto the image plane to produce a new set of projected pose belief maps. These maps encapsulate 3D dependencies between the body parts.

2D Fusion layer: The final layer in each stage (described in section 5.5) learns the weights to fuse the two sets of belief maps into a single estimate passed to the next stage.

Final lifting: The belief maps produced as the output of the final stage \((t = 6)\) are then lifted into 3D to give the final estimate for the pose (see Figure 1) using our algorithm to lift 2D poses into 3D.

5.2. Predicting CNN-based belief-maps

Convolutional Pose Machines [44] can be understood as an updating of the earlier work of Ramakrishna et al. [29] to use a deep convolutional architecture. In both approaches, at each stage \(t\) and for each landmark \(p\), the algorithm returns dense per pixel belief maps \(b_p[u,v]\), which show how confident it is that a joint center or landmark occurs in any given pixel \((u,v)\). For stages \(t \in \{2, \ldots, T\}\) the belief maps are a function of not just the information contained in the image but also the information computed by the previous stage.

In the case of convolutional pose machines, and in our work which uses the same architecture, a summary of the convolution widths and architecture design is shown in Figure 1, with more details of training given in [44].

Both [29, 44] predict the locations of different landmarks to those captured in the Human3.6M dataset. As such the input and output layers in each stage of the architecture are replaced with a larger set to account for the greater number of landmarks. The new architecture is then initialized by using the weights with those found in CPM’s model for all preexisting layers, with the new layers randomly initialized.

After retraining, CPMs return per-pixel estimates of landmark locations, while the techniques for 3D estimation (described in the next section) make use of 2D locations. To transform these belief maps into locations, we select the most confident pixel as the location of each landmark

\[
Y_p = \arg \max_{(u,v)} b_p[u,v]
\]

5.3. Lifting 2D belief-maps into 3D

We follow [50] in assuming a weak perspective model, and first describe the simplest case of estimating the 3D pose of a single frame using a unimodal Gaussian 3D pose model as described in section 4. This model is composed of a mean shape \(\mu\), a set of basis matrices \(e\) and variances \(\sigma^2\), and from this we can compute the most probable sample
Rather than attempting to solve this optimization problem allows it to be parameterized in terms of a single angle \( \theta \). The resulting \( \Phi \) leads to a significantly worse 3D reconstructions.

frame scale. Although, given fixed choices of rotation the terms \( \Pi E R_{\mu} \) and \( \Pi E R_{e} \) can be precomputed and finding the optimal \( \alpha \) becomes a simple linear least square problem.

This process is highly efficient and by oversampling the rotations and exhaustively checking in 10, 000 locations we can guarantee that a solution extremely close to the global optima is found. In practice, using 20 samples and refining the rotations and basis coefficients of the best found solution using a non-linear least squares solver obtains the same reconstruction, and we make use of the faster option of checking 80 locations and using the best found solution as our 3D estimate. This puts us close to the global optima and has the same average accuracy as finding the global optima. Moreover, it allows us to upgrade from sparse landmark locations to 3D using a single Gaussian at around 3,000 frames a second using python code on a standard laptop.

To handle models consisting of a mixture of Gaussians, we follow [27] and simply solve for each Gaussian independently and select the most probably solution.

5.4. Projecting 3D poses onto 2D belief maps

The projected pose model is interleaved throughout the architecture (see Figure 1). The goal is to correct the beliefs regarding landmark locations at each stage, by fusing extra information about 3D physical plausibility. Given the solution \( R, s, \) and \( a \) from the previous component, we estimate a physically plausible projected 3D pose as

\[
\hat{Y} = s\Pi E R(\mu + a \cdot e)
\]
5.5. 2D Fusion of belief maps

The 2D belief maps predicted by the probabilistic 3D pose model are fused with the CNN-based belief maps $b^p$ according to the following equation

$$f_t^p = w_t \cdot b^p_t + (1 - w_t) \cdot \hat{b}_t^p$$  \hspace{1cm} (7)

where $w_t \in [0,1]$ is a weight trained as part of the end-to-end learning. This set of fused belief maps $f_t$ is then passed to the next stage and used as an input to guide the 2D re-estimation of joint locations, instead of the belief maps $b_t$ used by convolutional pose machines.

5.6. The Objective and Training

Following [44], the objective or cost function $c_t$ minimized at each stage is the squared distance between the generated fusion maps of the layer $f_t^p$, and ground-truth belief maps $b_c^p$ generated by Gaussian blurring the sparse ground-truth locations of each landmark $p$

$$c_t = \sum_{p=1}^{L+1} \sum_{z \in Z} ||f_t^p - b_c^p||_2^2$$ \hspace{1cm} (8)

For end-to-end training the total loss is the sum over all layers $\sum_{t \leq 6} c_t$. The novel layers were implemented as an extension of the published code of Convolutional Pose Machines [44] inside the Caffe framework [17] as Python layers, with weights updated using Stochastic Gradient Descent with momentum. Details of the novel gradient updates used lifting estimates through 3d pose space are given in the supplementary materials.

6. Experimental evaluation

Human3.6M dataset: The model was trained and tested on the Human3.6M dataset consisting of 3.6 million accurate 3D human poses [15]. This is a video and mocap dataset of 5 female and 6 male subjects, captured from 4 different viewpoints, that show them performing typical activities (talking on the phone, walking, greeting, eating, etc.).

2D Evaluation: Figure 5 shows how the 2D predictions are improved by the projected pose model, reducing the overall mean error per landmark. The 2D error reduction using our full approach over the estimates of [44] is comparable in magnitude to the improvement due to the change of architecture moving from the work Zhou et al. [50] to the state-of-the-art 2d architecture [44] (i.e. a reduction of 0.59 pixels vs. 0.81 pixels). See Table 2 for details.

3D Evaluation: Several evaluation protocols have been followed by different authors to measure the performance of their 3D pose estimation methods on the Human3.6M dataset. Tables 1 and 2 show comparisons of the 3D pose estimation results of our approach on the Human3.6M dataset against competitors that follow Protocol #1 for evaluation (3D errors are given in mm). We substantially outperform all other methods in terms of average error showing a 4.7mm average improvement over our closest competitor. Note that some approaches [37, 50] use video as input instead of a single frame.
Table 2: Further evaluation on the Human3.6M dataset. Top two tables compare our 3D pose estimation errors against competitors on Protocols #2 or #3. Bottom table compares our 2D pose estimation error against competitors. Our approach, which lifts the 2D landmark predictions into a plausible 3D model and then projects them back into the image, substantially reduces the error. Note that [50] use video as input and knowledge of the action label, estimation with previous works, where we take care to evaluate using the appropriate protocol.

**Protocol #1**, the most standard evaluation protocol on Human3.6M, was followed by [15, 22, 37, 35, 36, 50, 31]. The training set consists of 5 subjects (S1, S5, S6, S7, S8), while the test set includes 2 subjects (S9, S11). The original frame rate of 50 FPS is down-sampled to 10 FPS and the evaluation is on sequences coming from all 4 cameras and all trials. The reported error metric is the 3D error i.e. the Euclidean distance from the estimated 3D joints to the ground truth, averaged over all 17 joints of the Human3.6M skeletal model. Table 1 shows a comparison between our approach and competing approaches using Protocol #1. Our baseline method using a single unimodal probabilistic PCA model outperforms almost every method in most action types, with the exception of Sanzari et al. [31], which it still outperforms on average across the entire dataset. The mixture model improves on this again, offering a 4.76mm improvement over Sanzari et al., our closest competitor.

**Protocol #2**, followed by [46, 30], selects 6 subjects (S1, S5, S6, S7, S8 and S9) for training and subject S11 for testing. The original video is down-sampled to every 64th frame and evaluation is performed on sequences from all 4 cameras and all trials. The error metric reported in this case is the 3D pose error equivalent to the per-joint 3D error up to a similarity transformation (i.e. each estimated 3D pose is aligned with the ground truth pose, on a per-frame basis, using Procrustes analysis). The error is averaged over 14 joints. Table 2 shows a comparison between our approach and other approaches that use Protocol #2. Although, our model was trained using only the 5 subjects used for training in Protocol #1 (one fewer subject), it still outperforms the other methods [30, 46].

**Protocol #3**, followed by [7], selects the same subjects for training and testing as Protocol #1. However, evaluation is only on sequences captured from the frontal camera (“cam 3”) from trial 1 and the original video is not subsampled. The error metric used in this case is the 3D pose error as described in Protocol #2. The error is averaged over a subset of 14 joints. Table 2 shows a comparison between our approach and [7]. Our method outperforms Bogo et al. [7] by almost 3mm on average, even though Bogo et al. exploits a high-quality detailed statistical 3D body model [23] trained on thousands of 3D body scans, that captures both the variation of human body shape and its deformation through pose.

**MPII and Leeds datasets**: The proposed approach trained exclusively on the Human3.6M dataset can be used to identify 2D and 3D landmarks of images contained in different datasets. Figure 4 shows some qualitative results on the MPII dataset [5] and on the Leeds dataset [18], including failure cases. Notice how the probabilistic 3D pose model generates anatomically plausible poses even though the 2D landmark estimations are not all correct. However, as shown in bottom row, even small errors in 2D pose can lead to drastically different 3D poses. These inaccuracies could be mitigated without further 3D data by annotating additional RGB images for training from different datasets.

7. Conclusion
We have presented a novel approach to human 3D pose estimation from a single image that outperforms previous solutions. We approach this as a problem of iterative refinement in which 3D proposals help refine and improve upon the 2D estimates. Our approach shows the importance of thinking in 3D even for 2D pose estimation within a single image, with our method demonstrating better 2D accuracy than [44], the 2D approach it is based upon. Our novel approach for upgrading from 2D to 3D is extremely efficient. When using 3 models, as in Tables 1 and 2, the upgrade for each stage in CPU-based Python code runs at approximately 1,000 frames a second, while a GPU-based real-time approach for Convolutional Pose Machines has been announced. Integrating these systems to provide a reliable real-time 3D pose estimator is a natural future direction, as is integrating this work with a simpler 2D approach for real-time pose estimation on lower power devices.

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Supplementary Material

1. Computing derivatives for back-propagation through our lifted model

As discussed by the Convolution Pose Machine paper [1] recurrent like architectures such as ours have problems with vanishing gradients and for effective training they require an additional loss function to be defined for each layer, that independently drives each individual layer to return correct predictions regardless of how this information is used in subsequent layers.

Before we give the derivation of the gradients it should be emphasized that it is entirely possible to train the network without using them – in fact similar results can be obtained by only using the 3D lifting for the forward pass, and not back-propagating the lifting derivatives through the rest of the network. As the additional layers make use of custom Python-based derivatives rather than an efficient implementation, for computational reasons it might preferable to avoid this step. Nonetheless for completeness we include the derivatives.

There are two reasons the gradients are unneeded: Our lifting 3D model we use makes its best predictions when the 2D predictions of the same layer are closest to ground truth, and this is a constraint naturally enforced by the objective of equation (8) of the main paper. Further, as with Convolutional Pose Machines [1] our architecture suffers from problems with vanishing gradients. To overcome this Wei et al. [1] defined an objective at each layer, which acted to locally strengthen the gradients. However, a side effect of this multi-stage objective is that most of the effects of back-propagation happen locally and gradients back-propagated from other layers have little effect on the learning. This makes subtle interactions between layers less influential, and forces the learning process to concentrate on simply making accurate 2D predictions in each layer.

We first give the results for computing the gradients of sparse predicted locations \( \hat{Y} \) from \( Y \) (see section 5 of the main paper), before discussing the gradients induced on the confidence maps by these sparse locations.

1.1. Landmark Gradients

In the interests of readability we neglect the use of indices to indicate stages, the reader should assume that all variables are taken from the same stage. Similarly, when dealing with a mixture of Gaussians, as we are only interested in computing a sub-gradient, the reader should assume that the best model has already been selected in the forward pass and we are computing gradients using only this model.

Recall (section 5 of main body of paper) that the mapping from the initial landmarks \( Y \) to the projected 3D proposals \( \hat{Y} \) is given by

\[
\hat{Y} = \Pi R (\mu + a \cdot e) \tag{1}
\]

where

\[
R, a = \arg \min_{\{R^* \in R, a^* \in R^J\}} ||Y - \Pi R^*(\mu + a^* \cdot e)||_2^2 + (\sigma \cdot a^*)^2 \tag{2}
\]

where \( R \) is a discrete set of rotations we exhaustively minimize over, and \( J \) is the number of bases in \( e \). Owing to the use of discrete rotations, this mapping from \( Y \) to \( \hat{Y} \) is a piecewise smooth approximation of the smooth function defined over a continuous \( R \), and sub-gradients can be induced by fixing \( R \) to its current state. Hence:

\[
\frac{d\hat{Y}}{da} = \Pi Re \tag{3}
\]

For the remainder of the section, and to compact notation we will write \( E \) for the matrix of size \( 2L \times J \) (\( L \) the number of landmark points and \( J \) being the number of bases in \( e \) ) formed by unwrapping tensor \( \Pi Re \). Similarly, we will unwrap the \( 2 \times L \) matrices \( Y \) and \( \hat{Y} \) and write them as \( y \) and \( \hat{y} \). We also write \( p \) for the vector representing the unwrapped set of 2D landmark positions \( \Pi R \mu \).
We will use \([y,0]\) for the vector formed by vector \(y\) followed by \(J\) zeros, and \(\bar{E}\) for the matrix of size \((2L + J) \times J\) formed by concatenating \(E\) with the matrix that has values \(\sigma\) along the diagonals and zero everywhere else. We can rewrite equation (3) in its new notation as:

\[
\frac{d\hat{y}}{da} = E
\] (4)

and given \(R\), we can rewrite equation (2) as

\[
a = \arg \min_{a \in \mathbb{R}^J} ||[y,0] - [p,0] - a^* \bar{E}||_2^2
\] (5)

or

\[
a = [(y - p), 0] E^\dagger
\] (6)

with \(E^\dagger\) continuing to represent the pseudo-inverse of \(E\). Hence

\[
\frac{da}{d[y,0]} = E^\dagger
\] (7)

and

\[
\frac{d\hat{y}}{dy} = \frac{d\hat{y}}{da} \frac{da}{dy} = E E^\dagger
\] (8)

where \(E^\dagger\) is the truncation of \(E^\dagger\).

1.2. Mapping belief gradients to coordinate transform

The coordinates of each predicted landmark \(\hat{Y}_p\) induce a Gaussian in the belief map \(\hat{b}_p\). So a change in the \(x\) component of \(\hat{Y}_p\) induces an update which is equivalent to a difference of Gaussians.

\[
\frac{db_p}{dY_p^x} \approx \frac{G(Y_p^x(\cdot + \delta_x)) - G(Y_p^x(\cdot - \delta_x))}{2\delta_x}
\] (9)

and the same for the \(y\) component as well. For computational purposes we take \(\delta_x\) as one pixel. As such, an induced gradient on the projected belief map near the predicted location \(\hat{Y}\) \(\hat{b}_p\) induces an updating of \(\hat{Y}\) that is propagated through to \(Y\) using the sub-gradients described in equation (8).

Updating \(B\) Writing \(B\) for the the set of all \(b_p\), and assuming \(Y_p\) is not in the right location, i.e. given updates \(\Delta \hat{B}\) on \(\hat{B}\) such that

\[
\Delta \hat{B}, \frac{d\hat{B}}{dY} \frac{dY_p}{dY_p} \neq 0,
\]

any update of \(b\) in which we decrease the belief at \(b_p\) and increase anywhere else is a valid sub-gradient. We choose as a sensible update a negative step at \(b_p\) of magnitude \(m = k ||\Delta \hat{B}, \frac{d\hat{b}}{dY} \frac{dY_p}{dY_p}||\) and a positive update for each element \(Y\) of \(B_p\) of the magnitude \(m \cdot N(Y, \sigma^2)\) in the quadrant of a Gaussian of the same width used to generate \(\hat{b}\) (i.e. \(\sigma = 1\) see section 5.6 of main paper) and with the same direction as \(\Delta \hat{B}, \frac{d\hat{B}}{dY} \frac{dY_p}{dY_p}\) in each \(x\) and \(y\) coordinate.

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