Numerical Study of Cosmic Ray Confinement through Dust Resonant Drag Instabilities

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\textbf{ABSTRACT}

We investigate the possibility of cosmic ray (CR) confinement by charged dust grains through resonant drag instabilities (RDIs). We perform magnetohydrodynamic particle-in-cell simulations of magnetized gas mixed with charged dust and cosmic rays, with the gyro-radii of dust and GeV CRs on $\sim$ AU scales fully resolved. As a first study, we focus on one type of RDI wherein charged grains drift super-Alfvénically, with Lorentz forces strongly dominating over drag forces. Dust grains are unstable to the RDIs and form concentrated columns and sheets, whose scale grows until saturating at the simulation box size. Initially perfectly-streaming CRs are strongly scattered by RDI-excited Alfvén waves, with the growth rate of the CR perpendicular velocity components equaling the growth rate of magnetic field perturbations. These rates are well-predicted by analytic linear theory. CRs finally become isotropized and drift at least at $v_A$ by unidirectional Alfvén waves excited by the RDIs, with a uniform distribution of the pitch angle cosine $\mu$ and a flat profile of the CR pitch angle diffusion coefficient $D_{\mu\mu}$ around $\mu = 0$, without the “90° pitch angle problem.” With CR feedback on the gas included, $D_{\mu\mu}$ decreases by a factor of a few, indicating a lower CR scattering rate, because the backreaction on the RDI from the CR pressure adds extra wave damping, leading to lower quasi-steady-state scattering rates. Our study demonstrates that the dust-induced CR confinement can be very important under certain conditions, e.g., the dusty circumgalactic medium around quasars or superluminous galaxies.

\textbf{Key words:} cosmic rays — plasmas — methods: numerical — MHD — galaxies: active — ISM: structure

\section{1 INTRODUCTION}

The transport physics of cosmic rays (CRs) has been a subject of active investigation since the 1960s (Kulsrud & Pearce 1969). As charged ultra-relativistic particles coupled to magnetic fields via Lorentz forces, CRs are fundamentally governed by particle-wave-interactions with magnetic fluctuations (e.g., Alfvén waves). Generally speaking, when Alfvén waves are excited with wavelengths broadly similar to the CR gyro radii, CRs are scattered toward ally speaking, when Alfvén waves are excited with wavelengths broadly similar to the CR gyro radii, CRs are scattered toward...

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indefinitely-large family of instabilities that appear in different forms, whenever dust grains move through a background fluid with some non-vanishing difference in the force acting on dust vs. fluid. The RDI can excite small-scale parallel Alfvén waves in magnetized gas (Hopkins & Squire 2018; Seligman et al. 2019), which can in turn scatter CRs and enhance their confinement. Which of these is the dominant process, or whether still different forms of the RDI can be excited, depend on the local plasma conditions, with scenario(s) being more likely in regions where the gas is relatively diffuse and external acceleration of dust grains is relatively strong (from e.g. absorbed photon momentum around a bright source). In any case, the co-existence of CRs and charged dust grains in the ISM is self-evident. Even in the CGM far from galaxies, where Squire et al. (2020) suggest scenario (2) would be more likely, the existence of significant dust populations is theoretically and observationally plausible: for instance, in the cool (\( \sim 10^4 - 10^5 \) K) or warm-hot (\( 10^5 - 10^6 \) K) phases of the CGM where the gas number density is low enough (\( \lesssim 10^{-3} \text{ cm}^{-2} \)), the hadronic and Coulomb losses of CRs are small (Guo & Oh 2008), and the temperature and density are low enough that the dust scattering time is long (Tielens et al. 1994). In fact, a significant amount of dust has already been observed in the CGM (Ménard et al. 2010; Peek et al. 2015). And around quasars or superluminous galaxies, dust grains could in principle easily be accelerated by radiation pressure and become unstable to the specific RDI which would source strong CR scattering on AU scales according to Squire et al. (2020). Dust clumping can scatter and re-emit photons from QSOs (e.g., Hennawi et al. 2010; Martin et al. 2010), and thus might produce observables in absorption lines of the CGM. Nevertheless, this scenario remains largely unexplored; even for the pure dust RDI without CRs, the only simulation study thus far, in Hopkins et al. (2020b), has simulated the CGM cases at a resolution of \( \sim 10 \) pc, far above AU scales on which CR-dust coupling occurs.

Motivated by the above, in this paper we present the very first numerical study of CR-dust-MHD coupling, with resolved CR and dust gyro-radii. In particular, here we focus on the proposed CR confinement scenario in which CRs are scattered by magnetic field irregularities caused by the specific forms the RDI described in Squire et al. (2020). The paper is organized as follows. In §2, we describe the numerical methods and setup of our simulations. §3 presents and analyzes the simulation results. Finally sumarize our findings in §4.

2 METHODS & SIMULATION SETUP

2.1 Numerical Methods

The numerical methods adopted here consist of three main components, each of which has been well-studied separately: the MHD solver in the code GIZMO (Hopkins 2015), dust grains evolved with a standard super-particle method (Hopkins & Squire 2018; Seligman et al. 2019), and CR particles evolved with a hybrid MHD particle-in-cell (MHD-PIC) method (Bai et al. 2015, 2019). Detailed implementations are described in the above-cited references, and we only briefly review them here.

The background plasma/liquid/gas and magnetic fields follow the equations of ideal MHD, solved in GIZMO with the well-tested constrained-gradient meshless finite-volume Lagrangian Godunov method (Hopkins & Raives 2016; Hopkins 2016). This has been shown to accurately reproduce a variety of detailed MHD phenomena including amplification, shocks, detailed structure of the magnetorotational and magnetothermal instabilities, and more (Hopkins 2017; Deng et al. 2019; Grudić et al. 2020). To this we add the “back-reaction” or feedback force of CRs and dust on gas, detailed below. Individual grains and CRs are integrated as PIC-like “super-particles” as is standard in the literature for both (Carballido et al. 2008; Johansen et al. 2009; Bai & Stone 2010; Pan et al. 2011; McKinnon et al. 2018; Bai et al. 2015, 2019; Holcomb & Spitkovsky 2019; v. Marle et al. 2019), sampling the distribution function statistically by taking each super-particle to represent an ensemble of identical micro-particles (individual grains or CRs). Dust grains obey the equation of motion

\[
\frac{d\mathbf{v}_{\text{dust}}}{dt} = \mathbf{a}_{\text{ext,dust}} + \mathbf{a}_{\text{gas,dust}},
\]

where \( \mathbf{v}_{\text{dust}} \) is the grain velocity, \( \mathbf{a}_{\text{ext,dust}} \) and \( \mathbf{a}_{\text{gas,dust}} \) are grain accelerations from external forces (e.g. gravity, radiation) and background gas and magnetic fields respectively. The latter includes both drag and Lorentz forces:

\[
\mathbf{a}_{\text{gas,dust}} = -\frac{\mathbf{v}_{\text{dust}} - \mathbf{v}_{\text{gas}}}{t_s,\text{dust}} - \frac{\left(\mathbf{v}_{\text{dust}} - \mathbf{v}_{\text{gas}}\right) \times \mathbf{\hat{B}}}{t_L,\text{dust}},
\]

where \( \mathbf{\hat{B}} = B/|B| \) is the unit vector of the magnetic field \( B \), \( t_s,\text{dust} \) the dust drag drag or stopping time and \( t_L,\text{dust} \) the dust Larmor or gyro time. Since we are interested in regimes with super-sonic drift and microscopic dust grains (the Epstein drag limit), the drag and gyro timescales are given by:

\[
t_s,\text{dust} = \frac{\gamma}{\rho_{\text{gas}}} \frac{\epsilon_d^{\text{dust}}}{c_s} \left( 1 + \frac{9 \gamma}{28} \frac{\left| \mathbf{v}_{\text{dust}} - \mathbf{v}_{\text{gas}} \right|^2}{c_s^2} \right)^{-1/2},
\]

\[
t_L,\text{dust} = \frac{m_{\text{dust}}}{\rho_{\text{gas}} c_s} \frac{4 \pi e^2 \epsilon_d^{\text{dust}}}{3 \sqrt{2} |B|},
\]

where \( \gamma \) is the usual adiabatic index of the gas, and \( \gamma_d^{\text{dust}}, \epsilon_d^{\text{dust}}, m_{\text{dust}} \) and \( q^{\text{dust}} \) are the internal density, radius, mass and charge of dust grains respectively. Similarly, the equation of motion for CRs is:

\[
\frac{dc}{ct} \frac{da}{ct} = \mathbf{a}_{\text{ext,cr}} + \mathbf{a}_{\text{gas,cr}} = \mathbf{a}_{\text{ext,cr}} + \frac{\left(\mathbf{v}_{\text{cr}} - \mathbf{v}_{\text{gas}}\right) \times \mathbf{\hat{B}}}{t_L,0,\text{cr}},
\]

where \( c \) is the speed of light (and see below for \( \mathbf{c} \)), and \( \mathbf{v}_{\text{cr}} \) is the velocity of the CR particles, which is related to the CR four-velocity \( u_\alpha \) via the usual Lorentz factor \( \gamma_{\text{cr}} = (1 - \left| \mathbf{v}_{\text{cr}}^2/c^2 \right|)^{-1/2} \). The \( t_L,0,\text{cr} = 1/2\epsilon_{\text{cr}} \) is the usual non-relativistic CR gyro time and \( m_{\text{cr}}/q_{\text{cr}} \) are the CR mass and charge.

In the ideal MHD approximation, the “feedback” force from dust grains and CRs appears simply in the gas momentum equation as an equal-and-opposite force as from gas onto dust+CRs:

\[
\rho_{\text{gas}} \left( \frac{\partial}{\partial t} + \mathbf{v}_{\text{gas}} \cdot \nabla \right) \mathbf{v}_{\text{gas}} = -\nabla P - \frac{\mathbf{B} \times (\nabla \times \mathbf{B})}{4\pi} - \int d^3 \mathbf{v}_{\text{dust}} f_{\text{dust}}(x, \mathbf{v}_{\text{dust}}) \mathbf{a}_{\text{gas,dust}}(\mathbf{v}_{\text{dust}}, \ldots),
\]

\[
- \int d^3 \mathbf{v}_{\text{cr}} f_{\text{cr}}(x, \mathbf{v}_{\text{cr}}) \mathbf{a}_{\text{gas,cr}}(\mathbf{v}_{\text{cr}}, \ldots),
\]

where \( f_{\text{dust}}(x, \mathbf{v}_{\text{dust}}) \) and \( f_{\text{cr}}(x, \mathbf{v}_{\text{cr}}) \) are the phase-space density distributions of dust and CRs respectively. Non-Lorentz forces are integrated with a semi-implicit scheme and Lorentz forces using a Boris integrator, with the back-reaction terms implemented in a manner that ensures manifest machine-accurate total momentum conservation. These methods have been detailed and extensively tested in Hopkins & Lee (2016); Lee et al. (2017); Moseley et al. (2019); Seligman et al. (2019); Hopkins et al. (2020b).

Note that up to the detailed form of the gyro acceleration equation, the expressions for dust and gas evolution are functionally identical – indeed we can numerically think of the dust as a second, “heavy” (low charge-to-mass, non-relativistic) CR species which
also experiences drag, or think of the CRs as "relativistic, drag-free grains."

Finally, to avoid the Courant condition for the CR speed \( c \) leading to computationally impractical timesteps in our simulation, we adopt the reduced speed-of-light (RSOL) approximation by defining the RSOL \( \tilde{c} \) in Eq. (5) \( \tilde{c} < c \) (but still keeping \( \tilde{c} \) much larger than other velocities in our simulation). As shown in Li & Hopkins (2021), the particularly form of the RSOL implemented here, which simply modifies the CR acceleration by the power of \( \tilde{c}/c \) and defines the CR advection speed over the (non-relativistic) grid to be \( \vec{v}_{\text{CR}} \equiv \Delta x_{\text{g}} / \Delta t = (\tilde{c}/c) \vec{v}_{\text{CR}} \), ensures that all steady-state properties of the CR distribution function (number, momentum, energy density, pitch-angle distribution) are mathematically invariant to the choice of \( \tilde{c} \). With this new implementation, we are able to simultaneously match the CR energy density, mass density, and momentum density of any desired initial configuration, and account for the "correct" CR gyro-radius and back-reaction forces which are also independent of the choice of \( \tilde{c} \). This also means that throughout this paper when we refer to e.g. CR gyro-frequencies and other standard quantities, they have their usual meaning and values (i.e. unless otherwise specified, the RSOL \( \tilde{c} \) does not enter our expressions here).

### 2.2 Simulation Parameters & Motivation

In what follows, we consider a system where dust grains are accelerated by some large \( a_{\text{ext}, \text{dust}} \), for example from radiation pressure from e.g. a quasar or luminous starburst in their host galaxy, in low-density magnetized gas representative of e.g. the CMB or ionized ISM bubbles. In these cases the fastest growing of the dust RDIs are generally the "aligned cosmic-ray-like" (so named because the eigenmode structure broadly resembles the Bell 2004 instability) or "dust gyro-resonant" RDIs, which lead to rapid growth of parallel ISM bubbles. In these cases the fastest growing of the dust RDIs correspond to more rapid RDI growth rates. Squire et al. (2020) considered super-sonic dust drift velocities \( v_{\text{drift}} \equiv \sqrt{\gamma_{\text{dust}} - 1} \), such that certain RDIs were excited, so we choose \( \tilde{a}_{\text{dust}} = 1.2 \times 10^{-3} \) such that the initial equilibrium dust drift velocity is \( v_{\text{drift}} = 10 \, c_{\text{dust}} \) (safely super-sonic).

As discussed in Hopkins & Squire (2018); Hopkins et al. (2020b) and Squire et al. (2020), while this is intentionally a somewhat extreme choice, it is plausible given the observed radiation fluxes in CGM environments around super-luminous sources such as quasars and starburst galaxies, e.g., at \( \sim 10 \) keV from a source with luminosity \( L_{\gamma} \sim 10^{42} \text{erg s}^{-1} \).

It is easy to verify that under these conditions, Lorentz forces on dust grains strongly dominate over drag forces (by a factor of \( \sim 10^{5} \)), as desired for our problem of interest, and that both CRs and dust have very similar gyro-radii, \( \sim 0.6 \, \text{AU} \) in the physical units above.

1 More precisely, we set \( L_{\text{box}} = \sqrt{N_{1D} \frac{c \Delta t}{\gamma_{\text{CR}}}} \), such that each Larmor wavelength is resolved with \( \sqrt{N_{1D}} \) elements and the box contains \( \sqrt{N_{1D}} \) Larmor wavelengths, which provides an optimal compromise for our purposes. For boxes with different resolution, we rescale the numerical parameters to correspond to fixed physical quantities (e.g. fixed gyro radius) while rescaling the box size to follow this relation. Here and throughout, we define the gyro-radius specifically as the gyro radius for an equivalent circular orbit, \( r_{\text{g}, \text{CR}} = \frac{v_{\text{CR}}}{\Omega_{\text{CR}}} \).

2 For our low-resolution \( N_{1D} = 64 \) boxes, the parameters which depend explicitly on \( L_{\text{box}} \) rescale to \( \tilde{a}_{\text{dust}} = 1.5 \times 10^{-5}, \tilde{c}_{\text{dust}} = 9 \times 10^{5}, \frac{\rho_{\text{dust}}}{\rho_{\text{gas}}} = 8.5 \times 10^{-4} \). We also set reduced speed of light to \( c \equiv 0.05 \, c \equiv 230 \, \text{cpc} \), ensuring it is larger than other speeds in the problem, but explicitly examine convergence with respect to this choice below.

3 As there is no particular reason to expect alignment between \( \vec{B} \) and \( \vec{a}_{\text{ext}, \text{dust}} \), we set \( \theta_{\text{dust}} = 45^\circ \), but this is largely a nuisance parameter.
2.3 On the Initial CR Pitch Angle Distribution

Note that our initial condition for the CRs corresponds to all CRs having pitch angle \( \mu = 1 \), i.e. free-streaming directly down magnetic field lines at drift velocity \( v^D \) with the maximum-possible anisotropy in the CR distribution function. This is almost certainly unrealistic, but our purpose is to study how CRs would be scattered away from this anisotropy by dust, hence the choice.\(^5\) However one consequence of this choice is that for the parameters above (with \( (\varepsilon_c, \varepsilon_B) / (\varepsilon_{B, cr}) > 1 \), where \( \varepsilon_B \) are the CR and magnetic energy densities), the non-resonant Bell instability would grow much faster than the CR resonant instability (Bell 1978; Haggerty & Ji et al. 2019) and much faster than the RDIs (by a factor \( \sim \mu_{cr}^{-1/2} (v^0_D/v^0_{dust}) (f_{L,Cr}/f^0_{L,dust})^{-1} \approx 1 \)). And indeed we have verified this directly in test simulations, which also allow us to confirm that, in code, both the non-resonant and resonant CR instabilities grow initially at their expected linear growth rates.

A more realistic initial condition would feature a close-to-isotropic CR distribution function, which would strongly suppress these instabilities relative to the RDIs, and we also consider this case below. However for a first simulation, in order to see how CRs would be scattered from an arbitrarily anisotropic distribution with \( \mu = 1 \) (which is particularly useful for understanding the scattering physics themselves), we consider the “ultra-low CR density” or “test-particle CR” limit. This amounts to the CR feedback on the gas (equivalently, taking the CR number or energy density to be negligibly small), i.e., dropping the last term on the right-hand side in Eq. (6). Thus, CR scattering via self-induced instabilities cannot occur and we can clearly isolate the effects of the RDIs. We study this as a test problem in §3.1 – §3.3. After the system reaches a saturation state and CRs become more isotropized with \( v^D \ll \varepsilon \) (a more realistic “initial condition” for the CRs), we turn on CR feedback and investigate its consequences in §3.4.

3 RESULTS

3.1 Time Evolution & Saturated States

Fig. 1 and 2 shows plots of the dust grain projections, gas density fluctuations, gas velocity perturbations superposed with velocity streamlines, magnetic field strength superposed with field lines, and cosmic ray particle projections, viewed along the \( z \)-axis (the direction of the initial magnetic fields) and \( x \)-axis respectively. We choose the snapshots at \( t = 9.781 f_{L,dust}, 10.22 f_{L,dust}, 10.65 f_{L,dust} \) and \( 13.04 f_{L,dust} \), which are representative samples spanning between the end of the linear stage, the nonlinear stage and the saturation stage. Dust grains are unstable to the RDIs and non-linearly evolve into highly-concentrated columns along the \( z \)-axis, which merge and form into fewer but thicker columns or sheets with time. At the saturation stage, all dust grains form into one single column in our simulation box. This is expected since all wavelengths are unstable to RDIs, and the RDI growth rates decrease with increasing wavelengths. Therefore, we see the merging of structures until the box-scale mode saturates. Compared to collisionless dust grains which are strongly clumped, gas is only weakly compressible, with density and velocity fluctuations at levels of \( \sim 1\% \) and \( 10\% \) respectively. As shown in Fig. 1 and 2, since field lines are strongly stretched by dust grains, magnetic fields are amplified by up to one order of magnitude from their initial values, and the regions of field amplification tightly trace the location of clustered dust. At the saturation stage, field lines become significantly distorted and wrap around columns of dust grains, with the magnetic tension force \( B \times (\nabla \times \delta B) / 4\pi \) balancing the driving force from the dust on the gas \( \sim \rho_{dust} a_{ext, dust} \) (Seligman et al. 2019). As illustrated in Fig. 3, the morphology of the gas density, dust distribution and magnetic field are tightly correlated, and the system reaches approximately dynamical equilibrium between the gas pressure \( P_{gas} \), the magnetic pressure \( \sim |\mathbf{B}|^2 / 8\pi \) and the dust ram pressure \( \rho_{dust} v^2 \) (estimated as the dust momentum flux across the surface of the dust filament \( \rho_{dust} v_{z,dust} v_{x,y,dust} \)). Starting from a random distribution initially, CRs strongly react to RDI-induced magnetic field perturbations, being scattered and transiently highly clustered together with the dust before scattering leads to their returning to a nearly random spatial distribution again at the saturation stage (but now with a nearly-isotropic pitch angle distribution, as we shall show below). Initially the CRs react coherently small-scale modes (which have \( \lambda \ll f_{L, CR} \)) because CRs initially have a perfectly coherent (\( \delta \) function) distribution function and magnetic fields are distorted by the RDIs; but as the CRs scatter, these local “concentrations” disperse.

Fig. 4 shows the probability density functions (PDFs) of densities (top) and velocities / Lorentz factor (bottom) for gas (left), dust (middle) and CRs (right). Density PDFs are obtained by mapping particle mass onto grids, and velocity / Lorentz factor PDFs are weighted directly by particle masses. Compared with gas densities which only vary by \( \sim 20\% \), the PDF of gas densities spans over two orders of magnitude and become highly non-Gaussian at the non-linear and saturation stages, with a flat tail extending to \( \rho_{dust} (|v|_D) > 10 \) (similar to other pure-RDI simulations in, e.g., Seligman et al. 2019; Hopkins et al. 2020b). The relatively uniform PDF is qualitatively maintained in the high-resolution run, indicating that if there is a characteristic lumpiness, it’s not yet being recovered by the simulation. The CR density PDFs are qualitatively similar to the dust density PDFs at the nonlinear stage, as the initially coherent CRs are “dragged” by the RDIs, while at the saturation stage when CRs become fully scattered, the CR density PDF recovers its initial Gaussian shape (for the reasons above). The gas velocity PDFs suggest that gas is significantly accelerated by dust feedback up to rms velocities \( \sqrt{\langle v^2_{gas} \rangle} / c_s \sim 10^{-2} - 10^{-1} \). Dust grains are gently decelerated with time, and the velocity PDFs do not reach an equilibrium state by the end of the simulation. The CR Lorentz factor PDFs gradually broaden out with time, indicating CRs are mildly accelerated or decelerated by \( \sim 3\% \) during their interaction with local magnetic fields (i.e., some “diffusive re-acceleration” effects with a non-zero CR momentum diffusion coefficient \( D_{pp} \), as will be discussed in §3.3).

3.2 Growth Rates vs. Linear Theory

We next examine the amplification of magnetic fields \( |\mathbf{B}_x|, |\mathbf{B}_y| \) and \( |\mathbf{B}_z| \), and the growth of the CR velocity component perpendicular to local magnetic fields \( v_{L, CR} \) (normalized to the magnitude of total CR velocity \( |v_{CR}| \). By defining the pitch angle \( \theta \) as the angle between CR velocity and local magnetic field vectors, we see \( v_{L, CR} / |v|_{CR} = \mu \) and \( v_{L, CR} / |v|_{CR} = (1 - \mu^2)^{1/2} \), where \( \mu = \cos \theta \) is the pitch angle cosine and \( v_{L, CR} \) the CR velocity component parallel with local magnetic fields. As shown in the top and middle panels of Fig. 5, \( |\mathbf{B}_x|, |\mathbf{B}_y| \) and \( |\mathbf{B}_z| \) grow exponentially at almost the same growth rate until they reach saturation at \( t \sim 10 f_{L,dust} \). This indicates that, starting from highly anisotropic initial conditions with \( v_{L, CR} / |v_{CR}| = 0 \), CRs are strongly scattered by increasingly distorted magnetic fields due to the development of the dust RDI.

To estimate the magnitude of CR bulk drift velocity, we measure the arithmetic mean values of the CR velocity components (the net drift velocity) over all CR particles at the saturation stage. We find that \( \langle v_{x,y,z, CR} \rangle \sim \alpha c \) with \( \alpha \) fluctuating between \( \sim 10^{-4} - 10^{-2} \) with time, which is thus highly isotropic compared with the CR.
Figure 1. Plots of (from top to bottom) dust grain projections, gas density fluctuations, gas velocity perturbations superposed with velocity streamlines, magnetic field strengths superposed with field lines, and CR particle projections, at (from left to right) $t = 9.78 t_{\text{dust}}, 10.22 t_{\text{dust}}, 10.65 t_{\text{dust}}$ and $13.04 t_{\text{dust}}$, viewed along the $z$-axis (parallel with the direction of initial magnetic fields). Dust grains are unstable to the RDI and modes grow and merge until they saturate in a large box-scale sheet mode, which significantly distorts and amplifies magnetic fields. CRs strongly respond to and are scattered by dust-induced magnetic field irregularities.
Figure 2. Plots as Fig. 1, but viewed along the x-axis (perpendicular to the direction of initial magnetic fields).
Figure 3. Slice plots of (from left to right) gas thermal pressure \(P_{\text{gas}}\), magnetic pressure \(P_{\text{mag}}\), the sum of gas thermal pressure and magnetic pressure \(P_{\text{gas}} + P_{\text{mag}}\), dust ram pressure \(P_{\text{dust}}\) estimated as dust momentum flux across the surface of the dust filament \(\rho_{\text{dust}} v_{\text{dust}} v_{\text{y},\text{dust}}\), and the sum of all pressure terms \(P_{\text{gas}} + P_{\text{mag}} + P_{\text{dust}}\) in code units of \(\rho_{\text{gas}}^0 (c_s^0)^2\) at the saturation stage when \(t = 13.04 t_{\text{L},\text{dust}}\). The sum of pressure terms is nearly a constant spatially, indicating the system is roughly in pressure balance.

Figure 4. The density (top) and velocity / Lorentz factor (bottom) PDFs of gas (left), dust (middle) and CRs (right). Most PDFs feature a strong asymmetry. The density PDFs of dust and CRs span up to two orders of magnitude, while gas is only weakly compressible. Gas and dust grains are accelerated and decelerated respectively due to their momentum exchange, and the PDFs of CR Lorentz factor slightly broaden with time.

Initial conditions of \((v_x, v_y, v_z) = (0, 0, c)\). Although the magnitude of the “residual” drift velocity \(\sqrt{2 \gamma_x \gamma_z \langle v_{\text{dust}} \rangle^2}\) is of the same order of magnitude with \(\langle v_{\text{dust}} \rangle\), given that we sample the CR distribution function with \(\sim 10^6\) particles in our default simulations, we caution that this range of \(\alpha\) is precisely what we would expect from Monte Carlo sampling noise for an intrinsically uniform pitch-angle distribution. This sampling noise (which unfortunately converges slowly, as \(N_{\text{part}}^{-1/2}\)) dominates the “residual” drift velocity here, thus we cannot draw a firm conclusion on the CR drift speed from direct measurement. However, there is still a way to investigate the CR drifting by Alfvén waves. As shown in the bottom panel of Fig. 5, the (negative) magnitude of the gas cross helicity \(-\nabla \times \mathbf{v}_{\text{gas}}\cdot \mathbf{B}\), which is related to the asymmetry of Alfvén waves, remains a single sign and grows exponentially with a squared RDI growth rate before saturating. This indicates that the propagation of the Alfvén waves excited by the RDIs is increasing unidirectional (antiparallel to the large-scale magnetic fields in this case when the cross helicity is negative); therefore, the CRs must at least drift at \(\sim v_A\) by the Alfvén waves all propagating in one direction.

In Fig. 6, we plot the analytically predicted growth rates for our simulation parameters as a function of the wave number \(|k|\), for a specific mode angle of \(\hat{k} \cdot \hat{r}_{\text{dust}} = 0.6\). We find that the growth rate measured from our simulation in Fig. 5 replicates the analytical solution well, with the growth rates peaking at wave numbers around \(kL_{\text{box}} \sim 10 \sim 40\). This corresponds to a fastest growing wavelength of \(2\pi/k \sim 0.16 \sim 0.6L_{\text{box}}\), which is somewhat consistent with the structures seen in Fig. 1 and 2.
Figure 5. Time evolutions of averaged magnetic fields (top), the perpendicular component of CR velocity (middle) and the averaged negative gas cross helicity (bottom). Both the magnetic fields and the CR perpendicular velocity component follow almost the same analytically-predicted growth rate (and the squared growth rate for the cross helicity since it is the dot product of velocities and magnetic fields), indicating a strong correlation between magnetic field fluctuations, Alfvén wave propagation and CR scattering.

3.3 Pitch Angle Scattering & Transport/Scattering Coefficients

Fig. 7 shows the time evolution of CR pitch angle PDFs (top) and the pitch angle diffusion coefficients $D_{\mu\mu}$ (bottom), which is defined as:

$$D_{\mu\mu}(\mu_0, t_0) = \frac{1}{(\Delta t)^3} \int_{\mu_0}^{\mu(t_0)} \int_{t_0}^{t+\Delta t} \frac{(\mu - \mu_0)^2}{2(t - t_0)} dt_1 dt_2,$$

where $\mu_0(t_0)$ and $\mu(t)$ are initial and final pitch angle cosine (time) respectively, $\Delta t$ is the integration time, and we trace the change of pitch angles for all CR particles over a short time interval to keep $(\mu - \mu_0)$ small, following e.g., Beresnyak et al. (2011); Xu

We explicitly verified that the mode angle of $\mathbf{k} \cdot \mathbf{v}_{\text{dust}} = 0$, i.e., the wave vector and dust velocities are aligned or anti-aligned, gives the fastest growth rate, which is consistent with the findings in Seligman et al. (2019). Therefore, we only show the growth rates for this specific mode angle here. For a detailed description of calculating these growth rates, see Hopkins & Squire (2018).

Figure 6. Analytical growth rates of RDI as a function of wave number $|k|$, which perfectly predicts the growth rate measured directly from the simulation as shown in Fig. 5.

Figure 7. Time evolution of PDFs of the CR pitch angle cosine $\mu$ (top), and the CR pitch angle diffusion coefficient $D_{\mu\mu}$ (normalized by the initial CR gyro-frequency $\Omega^\mu_0$) as a function of the CR pitch angle cosine (bottom). At the saturation stage, CRs are fully isotropized with a uniform distribution of the pitch angle cosine, and the CR pitch angle diffusion coefficient features a flat profile around $\mu = 0$, without encountering the 90° pitch angle problem predicted by quasi-linear theories.
& Yan (2013). Here \( \bar{\mu} \equiv (\bar{\xi}/c) t_{\text{code}} \) denotes the in-code time multiplied by the factor \( \bar{\mu}/c \) to correct for the reduced speed of light (RSOL) approximation.\(^7\) As shown in the top panel of Fig. 7, the distribution of CR pitch angles becomes uniform at the saturation stage, indicating that CRs are nearly isotropized, with typical \( D_{\mu\mu} \approx 0.001 \) \( \sim 0.01 \Omega_0 \) (where \( \Omega_0 \equiv q_{\text{cr}} |B|/\gamma_{\text{LH},\text{cr}}c \) is the usual relativistic CR gyro-frequency).

For comparison, if we assume isotropic/grey scattering with the usual quasi-linear theory slab scattering expressions (Schlickeiser 1998), then we would expect the average value of \( D_{\mu\mu} \) to be given by \( D_{\mu\mu} \sim (3\pi/16 \Omega_0) |\delta B|^2/|\delta B|^2 \) (Zweibel 2013), where \( \delta B \) represents the magnitude of magnetic fluctuations on gyro-resonant scales. We see in Fig. 7 that our typical \( D_{\mu\mu} \) values correspond to \( |\delta B| \sim 0.1 |\delta B| \), which is roughly what we see in Figs. 1-3 (in fact we see slightly larger overall magnetic fluctuations, but what matters here is the gyro-resonant, parallel component, so the effective \( |\delta B|^2 \) entering the scattering-rate expressions we would expect to be reduced by a factor of \( \sim 2 \) or \( \sim 3 \)). Thus, at least to order of magnitude or better, the typical scattering rate we see is consistent with quasi-linear theory expectations.

Examining \( D_{\mu\mu}(\mu) \), we see that the CR pitch angle diffusion coefficients saturate at a smooth distribution as a function of \( \mu \) (nearly \( \mu \)-independent), which contradicts the usual prediction of \( D_{\mu\mu}(\mu = 0) \sim 0 \) from quasi-linear theory (e.g., Skilling 1971; Yan & Lazarian 2002). This prediction from quasi-linear theory is known as the 90° pitch angle problem, since \( \mu = 0 \) corresponds to an extremely short resonance wave length which contains insufficient energy to scatter CRs away from the 90° pitch angle, and thus CRs might be naively expected to become “trapped” at \( \theta = 90^\circ \) without being fully isotropized (e.g., Giacalone & Jokipii 1999; Felice & Kulsrud 2001). However, in our simulation, since the RDI-induced magnetic field perturbation \( \delta B/B \) can grow up to a few \( 10^{-1} \), CRs can be scattered across the 90° pitch angle and become isotropic without any difficulty; suggesting the dust RDI is efficient in exciting small-scale parallel Alfvén waves and confine CRs on \( \sim \) AU scales. Previous studies have suggested that resonance broadening due to non-linear wave-particle interactions (e.g., Yan & Lazarian 2008; Bai et al. 2019) or mirror scattering (e.g., Felice & Kulsrud 2001) might help to avoid the 90° pitch angle problem, which may be occurring in our simulations as well.

With this, we can further estimate the CR parallel diffusion coefficient \( \kappa_\parallel \) from our simulation in standard fashion (Earl 1974):

\[
\kappa_\parallel \approx \frac{1}{8} \int d\mu \frac{\mu^2 (1-\mu^2)^2}{D_{\mu\mu}(\mu)}. 
\]

Calculating this numerically in the saturation stage, we obtain \( \kappa_\parallel \sim 1.7 \times 10^{25} \Omega_0^5 L_{\text{box}} \sim 700 \Omega_0 c L_{\text{box}} \sim 0.7 \times 10^{27} \text{cm}^2 \text{s}^{-1}, \) i.e., a factor of \( \sim 1000 \) larger than the Bohm limit. This value is significantly lower than typical values of \( \kappa \sim 10^{29-30} \text{cm}^2 \text{s}^{-1} \) inferred from Solar system measurements or

\[
\tilde{\mu} \equiv (\tilde{\xi}/c) t_{\text{code}} \text{multiplied by the factor } \tilde{\mu}/c \text{ to correct for the reduced speed of light (RSOL) approximation.}^7\]
factor ~ 4 higher parallel diffusion coefficients. This is still more than sufficient to keep the CRs isolated and strongly-confined (and the 90° pitch-angle problem still does not appear), but it is not a negligible difference.

Physically, we showed in § 3.3 that the scattering rates followed approximately the quasi-linear theory expectation, \( D_{\mu\nu} \propto |\mathbf{B}|^2 / |\mathbf{B}|^2 \). Thus a factor ~ 4 suppression of \( D_{\mu\nu} \) by CR back-reaction corresponds to a factor of ~ 2 suppression of \( \delta B \) on gyro-scales. Indeed, we can directly verify that after we turn on the CR feedback the fluctuations in the magnetic field are damped by roughly this factor. If the fluctuations are predominately driven by the RDIs, then this change in their saturation amplitudes is not surprising: recall from § 2.2, when we turn on back-reaction (i.e. account for finite CR pressure effects on gas), we assume a fairly large CR pressure relative to thermal pressure, \( P_{\text{cr}} \sim 5 P_{\text{thermal}} \) (with both \( P_{\text{cr}} \) and \( P_{\text{thermal}} \) much larger than magnetic pressure). Thus if we saturate as described in § 3.1 with the perturbations driven by the RDIs (ultimately powered by the dust “ram pressure” or acceleration force per unit area \( P_{\text{dust}} \)) compensated by gas thermal plus CR pressure, then we expect \( |\delta B|^2 \) to be a factor of a few lower in saturation (from the increase in the total thermal+magnetic+CR background pressure). Effectively, the background medium becomes “stiffer” against perturbation by the dust.

From the view point of the standard quasi-linear theory wherein one assumes linear growth of scattering modes compensated by wave damping setting the quasi-steady-state scattering rates, with the CR feedback turned on, the backreaction on the RDI from the CR pressure plus the magnetic tension leads to stronger damping, and thus less CR confinement as found in the simulations. Quasi-linear theories also predict that the CR feedback can generate small-scale Alfvén waves via the CR gyro-resonant and non-resonant instabilities, i.e. the CR “self-confinement” modes which add linearly with the RDI driven perturbations and thus increase the CR confinement. However, this is in opposite to the decrease of the CR confinement in our simulations, because CRs are highly isotropic in the saturation stage, thus the CR-excited Alfvén waves and their resulting CR confinement are negligible. But admittedly, it is plausible to imagine that if there is a continuous driving of the background CR gradients, the growth rates of Alfvén waves from dust and CRs do add linearly when they both have drifts and small densities, and we might see the enhancement of the CR confinement, as quasi-linear self-confinement theories predicted.

3.5 Convergence Tests

Although previous studies have investigated how simulations of just the RDIs (Moseley et al. 2019; Seligman et al. 2019; Hopkins et al. 2020b) or just CRs depend on resolution, those simulations did not combine these physics nor investigate the same range of scales and parameters as we do here. Therefore, we consider a “high-resolution” simulation with \( N_{\text{gas}} = N_{\text{dust}} = N_{\text{ICW}} = N_{\text{ICW}}^1 = 128^3 \). Note that since we enforce \( c_{\perp,\text{dust}} / L_{\text{box}} = \sqrt{N_{\text{ICW}}} \), the high-resolution run with doubled 1D resolution fits a factor-of-\( \sqrt{2} \) larger number of Larmor wavelengths along each side of the simulation domain, and resolves each Larmor wavelength with \( \sqrt{2} \) times more elements.

Fig. 9 shows projections of dust grains, slices of magnetic field strength superposed with field lines and projections of CR particles along the z-axis for the high-resolution simulation. The high-resolution run is qualitatively similar to the low-resolution run shown in Fig. 1, but contains smaller-scale structures as expected. At the saturation stage, the high-resolution run contains two large-scale coherent structures of dust columns and magnetic vortices, in contrast to the single sheet-like structure in the low-resolution run. This is likely because the high-resolution run contains more Larmor wavelengths and thus it simulates a larger domain in real physical units. The time evolution of the magnetic fields and the perpendicular CR velocity in the high-resolution run are shown in Fig. 10, where the growth rate is almost identical to the low-resolution run. Thus the linear growth rates of the relevant modes are not measurably dependent on resolution, and they agree well with analytic theory: moreover the final properties (widths) of the PDFs are similar in both cases. Of greatest interest, the values of \( D_{\mu\nu} \) and (correspondingly) \( k_{\perp} \) and \( D_{\perp \perp} \) differ by less than 5% in the high resolution run. Thus it appears that the key results here are not sensitive to resolution. However, we caution that it is only possible to numerically resolve a tiny fraction of the interesting dynamic range (let alone effects like turbulent cascades or field-line wandering from large-scale dynamics, which operate on orders-of-magnitude larger scales), so this should be taken with some caution.

We also examine the numerical convergence with respect to the RSOl by varying \( \epsilon \) over a factor of \~ 5. For standard-resolution runs with \( \epsilon = (0.02, 0.05, 0.1, c) \), we find qualitatively identical behavior in all properties studied here, with the numerically-estimated in-saturation parallel diffusion coefficients \( k_{\perp} \sim (700, 700, 600) c_{\perp,\text{Lyr}} \), respectively – i.e. nearly invariant to \( \epsilon \). Note there is a (very weak) hint that \( k_{\perp} \) may decrease with increasing \( \epsilon \) here, perhaps owing to slightly stronger confinement at higher \( \epsilon \) perhaps because with lower \( \epsilon \) the CRs response may slightly artificially lag the RDI growth rates; but if we extrapolate to \( \epsilon = c \) by fitting our results, the resulting inferred \( k_{\perp} \) is only decreased by \~ 40%, a rather small correction compared to other theoretical uncertainties here (e.g. the effect of back-reaction discussed below).

3.6 Discussion: Damping & Saturation Scalings

Owing to our limited numerical resolution and MHD-PIC assumptions (where the plasma is treated as an MHD fluid), our simulations do not include certain plasma processes that can also damp Alfvén waves, such as ion-neutral or Landau damping. Ion-neutral damping is not likely relevant under conditions of interest for our problem here (e.g. diffuse, warm, highly-illuminated CGM), as the expected neutral fractions are vanishingly small. But Landau damping could be non-negligible, in principle. If we consider e.g. the usual non-linear Landau damping rate with \( \Gamma \sim \left(\sqrt{\pi} / 4\right) \epsilon_j (k_\perp^2 / k_\parallel^2) \sim \left(\sqrt{\pi} / 8\right) \epsilon_j \left(\| \mathbf{B} \|^2 / |\mathbf{B}|^2 \right) \), then at the scale where the RDI growth rate is maximized \( \sim c_{\perp,\text{Lyr}} \) the implied Landau damping rate (given \( |\delta B| \sim 0.1 |B| \) we see) is generally \~ 10% of the RDI growth rate in Fig. 6. That suggests it may not be negligible, but it is also unlikely to qualitatively change the behaviors here, if included. However, the simulations do, given the finite resolution, have non-zero numerical dissipation which happens (coincidently) to be similar in magnitude to Landau damping: given a standard numerical MHD dissipation rate in GIZMO which scales as \~ \Delta x \epsilon_j k_\perp^2 \sim \epsilon_j k (k \Delta x) \) (where \( \Delta x \) is the effective grid resolution for the MHD, and the prefactor depends on the specific numerical problem and details of the method, see Hopkins & Raives 2016), then for \( k \sim 1 / c_{\perp,\text{Lyr}} \sim 1 / (10 \Delta x) \) this is roughly similar in magnitude to the physical Landau damping. Of course, other mechanisms could in principle contribute to damping including interactions with extrinsic turbulence (Farmer & Goldreich 2004), which we cannot capture owing to our limited range of scales. Dust itself could act as a damping mechanism in some circumstances (Squire et al. 2021) but the conditions where this would occur are dramatically different from those here.

These limitations in physics, finite resolution, and simulation box size preclude making detailed statements regarding the saturation mechanisms of the RDI across a broader parameter space. However, the fact that we see roughly isotropic \( D_{\mu\nu} \) following approximately the expected quasi-linear scaling with \( |\delta B| / |B| \) gives us some confidence that the CR scattering rates induced by the RDI should
indeed scale with the saturation amplitude of $\delta B$. And even if the saturation mechanism is uncertain, some broad conclusions are robust. For example, based on their idealized RDI-only simulations, Hopkins et al. (2020b) discuss two possible saturation mechanisms, the first being balance between magnetic tension and dust ram pressure as discussed in § 3.1, the second being a scenario where the crossing time of the RDI-generated modes ($\sim \delta v_{\text{gas}}/\lambda$) becomes faster than the RDI growth time, producing non-linear dissipation. Non-linear Landau damping is another potential saturation mechanism, limiting $\delta B$ when the damping becomes faster than linear RDI growth rates. Squire et al. (2021) consider yet another saturation scenario, assuming a Kraichnan (1965)-like damping via self-interactions (which gives a damping rate akin to non-linear Landau but with $c_s$ replaced by the Alfvén speed). Crucially, the “driving” in all of these scenarios scales with the dust-to-gas ratio $f_{\text{dust-gas}}$ and force/acceleration/drift velocity on the grains (which appear in both the dust ram pressure and RDI growth rates). This is proportional to the incident radiation flux $F_{\text{rad}}$. Combining these estimates for the saturation $\delta B$ with the usual scalings for gyro radii and scattering rates we obtain, for any of the saturation scenarios above, a scattering rate which scales dimensionally as $D_{\mu\nu} \propto f_{\text{dust-gas}} F_{\text{rad}}^{0.7 - 1.5} |B|^{(0.8 - 3)}$ (with a weaker residual dependence on gas density and/or temperature, and the exact power-law scaling depending on the saturation model). In other words, there is a qualitatively robust prediction that with lower-dust-to-gas-ratios and/or incident radiative fluxes and/or stronger magnetic fields, the confinement of CRs by dust become weaker. All else equal, in order for the scattering rate from the dust RDIs to drop to below that inferred for Milky Way ISM gas (and thus become relatively unimportant), the factor $f_{\text{dust-gas}} F_{\text{rad}}$ would need to be $\sim 1000$ times smaller than the value we assume to motivate our tests. So for there to be “too little dust,” the metallicity or dust-to-metals ratio would need to be 1000 times lower than ISM values (which seems unlikely at least at low cosmological redshifts, even in the CGM), given the observations reviewed in § 1, which suggest this factor is perhaps something like $\sim 10$ times lower than in the ISM). But more plausibly, the incident flux could easily be 1000 times smaller, if for example the galaxy is a typical Milky Way-like or smaller dwarf galaxy with a star formation rate of $\sim 10 M_\odot$ yr$^{-1}$ and has negligible AGN luminosity (i.e. galaxy luminosity $\lesssim 10^{10} L_\odot$) or the dust is at $\sim 100$ kpc from the host. The magnetic field dependence is also interesting: it suggests these instabilities and ensuing confinement would be easier to excite in the distant CGM or IGM (where nano-Gauss fields are expected), but may be suppressed in denser, more highly-ionized super-bubbles near to galaxies.

4 CONCLUSIONS

In this paper, we investigate the impact of the dust RDIs on cosmic ray scattering, by performing the first numerical simulations of

Figure 9. Plots of dust grain projections (top), magnetic field strengths superposed with field lines (middle) and CR particle projections (bottom), as Fig. 1, but from the high-resolution simulation. The morphology of dust grains, magnetic fields and CRs in the high-resolution run is qualitatively similar with those in the fiducial run, but exhibits more detailed small-scale structures and contains more large-scale coherent structures (since the domain size of the high-resolution run is effectively larger – see the text for a full explanation).
solutions. Initially perfectly streaming CRs are strongly scattered by magnetic field fluctuations, with the growth rate of the perpendicular CR velocity component (to local magnetic fields, $v_{\perp,cr}/|v_{cr}|$, or $\sqrt{1 - u^2}$) equaling the growth rate of magnetic fields. At the saturation stage, the CRs are isotropized with a near-uniform distribution of the pitch angle cosine $\mu$, and the CR pitch angle diffusion coefficient $D_{\mu}(\mu)$ is nearly independent of pitch-angle $\mu$ (in particular around $\mu = 0$). There is no $90^\circ$ pitch-angle problem in our simulations. The scattering rate is in order-of-magnitude agreement with the usual quasi-linear theory expectation $D_{\mu}(\mu) \sim \Omega_{cr} \langle \delta B \rangle^2 / |B|^2$, with the large $\langle \delta B \rangle^2 / |B|^2 \sim 10^{-3} - 10^{-2}$ on gyro-resonant scales driven by the dust RDIs (in part because the dust has broadly similar gyro-radii to the CRs, under these types of conditions). The numerically-calculated CR parallel diffusion coefficient is $\sim 500 - 1000$ times the Bohm value: sufficient for strong confinement of the CRs.

When the system reaches saturation and CRs become close to isotropic (with the CR drift velocity $v_{pd} \ll c_0$), we turn on CR feedback to the gas and study its consequences. We find that with CR feedback, the CR pitch angle diffusion coefficient $D_{\mu}(\mu)$ decreases by a factor of $\sim 4$ (and thus this slightly reduces CR confinement). This owes to the fact that the large assumed CR pressure (several times larger than thermal+electric+nonlinear) suppresses the saturation amplitude of the magnetic field fluctuations $\delta B$ induced by the RDIs by a modest factor $\sim 2$, and the scattering modes are thus damped more by backreaction on the RDIs from the CR pressure, in addition to the magnetic tension. Since CRs in the saturation stage are highly isotropic, the quasi-linear self-confinement theory which predicts higher scattering rates due to CR-excited Alfven waves is not applicable here, unless there exists a continuous driving of CR gradients.

We finally stress that several caveats apply to our study. (1) As a first experiment, we picked one particular initial condition to investigate an interesting case, which is plausible for some conditions as noted above but should not be considered typical everywhere. There exist a variety of RDIs which can have totally different behaviors in different circumstances (Hopkins et al. 2020b) and indeed, under some conditions dust might even have the opposite effect, acting as a wave-damping mechanism and reducing the confinement of CRs (Squire et al. 2020). (2) Although we perform a small resolution study, our simulations are still limited in resolution and dynamical range. Even for a single grain size, the RDIs are unstable at all spatial wavelengths, so it is impossible to encompass their complete dynamic range (let alone global scales of structure or extrinsic turbulence, which are vastly larger than our box sizes). (3) We do not include any explicit wave-damping processes. While we do not expect appreciable ion-neutral damping in environments of interest (as the neutral fractions are negligible), Landau damping could be important, as could damping from a turbulent cascade, and these could reduce the efficacy of confinement. However at least for the extreme parameters considered here, it is unlikely these would significantly reduce the scattering rates. (4) Our periodic boxes neglect large-scale ($\gtrsim L_{box}$) CR pressure gradients $(\nabla P_{cr})$ which act as a source/driving term for super-Alfvenic CR drift. (5) For simplicity, we consider only one grain size+charge and one CR energy+species, rather than a full spectrum of grain sizes and CR energies. In future work it will be particularly interesting to see how a full spectrum of both modifies the dynamics here, as a broad range of gyro-radii overlap and different gyro-resonant modes can interact non-linearly and even linearly (when CRs+dust+gas are all combined), via their back-reaction on the gas.

With these limitations in mind, we consider this study to be a proof of concept, showing that CR dust-gas interactions might indeed be very important in some astrophysical conditions. For instance, this mechanism might be able to resolve some of the incompatibility be-
between CR confinement models and observations by preventing CR “runaway” (Hopkins et al. 2021a), at least under certain conditions investigated in this study. Considerable work remains to map out the parameter space, include additional physics, and understand the macroscopic consequences of confining CR-dust interactions (for either CRs themselves or for galaxy/CGM evolution). Nevertheless, the simulations here clearly argue that these effects are worth studying in detail.

DATA AVAILABILITY

The data supporting the plots within this article are available on reasonable request to the corresponding author. A public version of the GIZMO code is available at http://www.tapir.caltech.edu/~phopkins/Site/GIZMO.html.

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