Dilepton production from SIS to LHC energies

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Abstract. We study $e^+e^-$ pair production in proton-proton and in nucleus-nucleus collisions from SIS to LHC energies within the parton-hadron-string dynamics (PHSD) approach which incorporates explicit partonic degrees-of-freedom in terms of strongly interacting quasiparticles (quarks and gluons) in line with an equation-of-state from lattice QCD as well as the dynamical hadronization and hadronic collision dynamics in the final reaction phase. We find a visible in-medium effect in the low mass dilepton sector from SIS to SPS energies whereas at RHIC and LHC energies such medium effects become more moderate. In the intermediate mass regime from 1.1 to 3 GeV pronounced traces of the partonic degrees of freedom are found at SPS and RHIC energies which superseed the hadronic (multi-meson) channels as well as the correlated and uncorrelated semi-leptonic $D$-meson decays. The dilepton production from the strongly interacting quark gluon plasma (sQGP) becomes already visible at top SPS energies and more pronounced at RHIC and LHC energies.

1. Introduction

Dileptons, i.e. correlated electron and positron pairs, are one of the key observables in ultra-relativistic nuclear collisions experiments since dileptons are emitted during the whole collision evolution and thus one may probe various aspects at different stages of a relativistic nuclear collision by measuring differential dilepton spectra. Another important feature is that the produced leptons interact only electromagnetically and thus interact only very weakly with the strongly interacting partonic or hadronic medium created in the collisions. In another words, e.g. an initial state Drell-Yan-pair from the early stages of the collision is expected to survive the subsequent evolution of the fireball.

An important dilepton observable is the invariant mass spectrum. The mass spectrum can be roughly divided in 3 different regions, in each of which different physics dominates the radiation. In the low mass region ($M_{e^+e^-} < 1$ GeV) the radiation is dominated by the decays of light mesons (consisting of $u$, $d$ and $s$ (anti)quarks) and especially gives information about in-medium properties of the $\rho^0$ meson. In the intermediate mass region ($1.1$ GeV $< M_{e^+e^-} < 3$ GeV) the dominant hadronic contribution to the invariant mass spectrum is obtained from the decays of open charm mesons, while above the $J/\psi$ peak, first open beauty decays and later on initial state Drell-Yan radiation are expected to dominate the dilepton spectrum. On top of the previously mentioned sources, especially in the intermediate mass region, also radiation from the strongly interacting Quark-Gluon-Plasma (sQGP) can give a significant signal [1] as well as some other
more exotic sources like simultaneous interactions of four pions \([2, 3,4, 5]\). These partonic
and hadronic channels have been studied in detail in Refs. \([6, 7]\) at the top Super-Proton-
Synchrotron (SPS) and Relativistic-Heavy-Ion-Collider (RHIC) energies and it has been found
that the partonic channels clearly dominate over multi-pion sources in the intermediate dilepton
mass regime. This contribution aims to summarize the perspectives of dilepton measurements
from low SIS to high LHC energies based on the Parton-Hadron-String Dynamics (PHSD)
transport model \([8]\).

2. The PHSD approach
The dynamics of partons, hadrons and strings in relativistic nucleus-nucleus collisions is analyzed
here within the Parton-Hadron-String Dynamics approach \([8]\). In this transport approach the
partonic dynamics is based on Kadanoff-Baym equations for Green functions with self-energies
from the Dynamical QuasiParticle Model (DQPM) \([9]\) which describes QCD properties in terms
of ’resummed’ single-particle Green functions. In Ref. \([10]\), the actual three DQPM parameters
for the temperature-dependent effective coupling were fitted to the recent lattice QCD results of
Ref. \([11]\). The latter lead to a critical temperature \(T_c \approx 160\) MeV which corresponds to a critical
energy density of \(\epsilon_c \approx 0.5\) GeV/fm\(^3\). In PHSD the parton spectral functions \(\rho_j\) \((j = q, \bar{q}, g)\) are no
longer \(\delta\)– functions in the invariant mass squared as in conventional cascade or transport models
but depend on the parton mass and width parameters which were fixed by fitting the lattice
QCD results from Ref. \([11]\). We recall that the DQPM allows one to extract a potential energy
density \(V_p\) from the space-like part of the energy-momentum tensor as a function of the scalar
parton density \(\rho_s\). Derivatives of \(V_p\) w.r.t. \(\rho_s\) then define a scalar mean-field potential \(U_s(\rho_s)\)
which enters into the equation of motion for the dynamical partonic quasiparticles. Furthermore,
a two-body interaction strength can be extracted from the DQPM as well from the quasiparticle
width in line with Ref. \([12]\). The transition from partonic to hadronic d.o.f. (and vice versa) is
described by covariant transition rates for the fusion of quark-antiquark pairs or three quarks
(antiquarks), respectively, obeying flavor current-conservation, color neutrality as well as energy-
momentum conservation \([8, 10]\). Since the dynamical quarks and antiquarks become very massive
close to the phase transition, the formed resonant prehadronic color-dipole states \((gq\text{ or } qqq)\)
are of high invariant mass, too, and sequentially decay to the groundstate meson and baryon octets
increasing the total entropy.

On the hadronic side PHSD includes explicitly the baryon octet and decouplet, the \(0^-\) and
\(1^-\)-meson nonets as well as selected higher resonances as in the Hadron-String-Dynamics (HSD)
approach \([13, 14]\). Hadrons of higher masses \((> 1.5\) GeV in case of baryons and \(> 1.3\) GeV
for mesons) are treated as ’strings’ (color-dipoles) that decay to the known (low-mass) hadrons,
according to the JETSET algorithm \([15]\). Note that PHSD and HSD merge at low energy
density, in particular below the critical energy density \(\epsilon_c \approx 0.5\) GeV/fm\(^3\). For more detailed
descriptions of PHSD and its ingredients we refer the reader to Refs. \([9, 10, 16, 17]\).

The PHSD approach was applied to nucleus-nucleus collisions from \(s_{NN}^{1/2} \sim 5\) to 200 GeV
in Refs. \([8, 10]\) in order to explore the space-time regions of partonic matter. It was found
that even central collisions at the top-SPS energy of \(\sqrt{s_{NN}}=17.3\) GeV show a large fraction
of nonpartonic, i.e. hadronic or string-like matter, which can be viewed as a hadronic corona.
This finding implies that neither hadronic nor only partonic models can be employed to extract
physical conclusions in comparing model results with data.

3. Results for dilepton spectra in comparison to experimental data
We directly continue with the results from PHSD in comparison with the available experimental
data on dilepton production from SIS to RHIC energies.
3.1. SIS energies

The dileptons produced in low energy heavy-ion collisions have been measured first by the DLS Collaboration at Berkeley [18, 19, 20, 21]. The observed dilepton yield [21] in the mass range from 0.2 to 0.5 GeV in C+C and Ca+Ca collisions at 1 A GeV was about 5 times higher than the calculations by different transport models using the ‘conventional’ dilepton sources as bremsstrahlung, $\pi^0$, $\eta$, $\omega$ and $\Delta$ Dalitz decays and direct vector mesons ($\rho$, $\omega$, $\phi$) decays [22, 23, 24]. Even after including the different in-medium scenarios as collisional broadening and dropping mass for the $\rho$-meson spectral function did not solve the ‘DLS puzzle’ [25, 26, 27, 28].

The recent experimental data from the HADES Collaboration at GSI [29, 30, 31, 32, 33, 34], however, confirmed the measurement of the DLS Collaboration for C+C at 1.0 A GeV [30] as well as for the elementary reactions [35]. In the mean time also the theoretical transport approaches as well as effective models for the elementary NN reactions have been further developed.

A possible solution of the ‘DLS puzzle’ from the theoretical side has been suggested in Ref. [37] by incorporating stronger $pn$ and $pp$ bremsstrahlung contributions in line with the updated One-Boson-Exchange (OBE) model calculations from Ref. [36]. As shown in Ref. [37] the results of the HSD model (off-shell Hadron-String-Dynamics (HSD) transport approach) with ‘enhanced’ bremsstrahlung cross sections agree very well with the HADES data for C+C at 1 and 2 A GeV as well as with the DLS data for C + C and Ca + Ca at 1 A GeV, especially when including a collisional broadening in the vector-meson spectral functions. A similar finding has been obtained by other independent transport groups – IQMD [38] and Rossendorf BUU [39].

Fig. 1 shows a comparison of the HSD results to the HADES mass-differential dilepton spectra for C + C at 1.0 A GeV (left) and 2.0 A GeV (right) [40, 29] for the ‘free’ (upper...
Figure 2. Results of the HSD transport calculation for the mass differential dilepton spectra for central Au+Au collisions from 2 to 14 A GeV calculated for different in-medium scenarios - collisional broadening and combined scenario (dropping mass + collisional broadening).

part) and the in-medium scenario (lower part). At the higher bombarding energy the $\eta$ Dalitz decay provides the dominant contribution in the mass region from 0.2 to 0.5 GeV followed by $\Delta$ Dalitz decays and the combined bremsstrahlung channels. The mass region around 0.75 GeV is overestimated in the 'free' scenario, whereas including in-medium spectral functions for the vector mesons the description of the data is improved due to shifting of the strength from the vector-meson pole mass regime to lower invariant mass. However, the in-medium effects for the light C + C system are only very moderate. In order to observe a strong broadening of the $\rho$-meson spectral function one has to investigate a larger size system such as Au + Au. A corresponding measurement has been performed recently by the HADES Collaboration and the upcoming data will provide more accurate information on the in-medium effects.

In Fig. 2 we show the HSD predictions for the dilepton yields from central Au + Au collisions calculated for different energies from 2 to 14 A GeV applying the different in-medium scenarios: collisional broadening and combined approach (dropping mass + collisional broadening). One can see that both scenarios lead to an enhancement of the dilepton yield in the mass region $M = 0.3 - 0.8$ GeV by a factor of about 2. The largest in-medium effect is, however, attributed to the reduction of the dilepton yield between the $\omega$ and $\phi$ peaks due to the downward shift of the poles of the $\rho$ and $\omega$ spectral functions. However, the latest scenario is not consistent with existing experimental data at higher energies, so one has to rely most likely on the relatively modest in-medium effects due to collisional broadening.

3.2. SPS energies

We step up in energy and compare our model results with experimental data for dileptons from In+In collisions at 160 A GeV measured by the NA60 Collaboration.

In Fig. 3 we present PHSD results for the dilepton excess over the known hadronic sources as produced in In+In reactions at 158 A GeV compared to the acceptance corrected data. We find here that the spectrum at invariant masses in the vicinity of the $\rho$ peak is well reproduced by the $\rho$ meson yield, if a broadening of the meson spectral function in the medium is assumed, while the partonic sources account for the yield at high masses. Our analysis shows that the
**Figure 3.** Left: Acceptance corrected mass spectra of excess dimuons from In+In at 158 A GeV integrated over $p_T$ in $0.2 < p_T < 2.4$ GeV from PHSD compared to the data of NA60 [41]. The dash-dotted line shows the dilepton yield from the in-medium $\rho$ with a broadened spectral function, the dashed line presents the yield from the $q + \bar{q}$ annihilation, the dash-dot-dot line gives the contribution of the gluon Bremsstrahlung process ($q\bar{q} \rightarrow g l^+ l^-$), while the solid line is the sum of all contributions. For the description of the other lines, which correspond to the non-dominant channels, we refer to the figure legend. Right: The inverse slope parameter $T_{eff}$ of the dimuon yield from In+In at 158 A GeV as a function of the dimuon invariant mass in PHSD compared to the data of the NA60 Collaboration [42, 41].

The contributions of the ‘4π’ processes (shown by the lines with symbols), first noted by the authors of Ref. [2], are very much suppressed.

One concludes from Fig. 3 that the measured spectrum for $M > 1$ GeV is dominated by the partonic sources. Indeed, the domination of the radiation from the QGP over the hadronic sources in PHSD is related to a rather long – of the order or 3 fm/c – evolution in the partonic phase (in co-existence with the space-time separated hadronic phase) on one hand (cf. Fig. 10 of Ref. [43]) and the rather high initial energy densities created in the collision on the other hand (cf. Fig. 6 of Ref. [44]). In addition, we find from Fig. 3 that in PHSD the partonic sources also have a considerable contribution to the dilepton yield for $M < 0.6$ GeV. The yield from the two-to-two process $q + \bar{q} \rightarrow g l^+ l^-$ is especially important close to the threshold ($\approx 0.211$ GeV). This conclusion from the microscopic calculation is in qualitative agreement with the findings of an early (more schematic) investigation in Ref.[45].

The comparison of the mass dependence of the slope parameter evolution in PHSD and the data is shown explicitly in the right part of Fig. 3. Including partonic dilepton sources allows us to reproduce in PHSD the $m_T$-spectra as well as the finding of the NA60 Collaboration [41, 42] that the effective temperature of the dileptons (slope parameters) in the intermediate mass range is lower than that of the dileptons in the mass bin $0.6 < M < 1$ GeV, which is dominated by hadronic sources (cf. Fig. 3, right). The softening of the transverse mass spectrum with growing invariant mass implies that the partonic channels occur dominantly before the collective radial flow has developed. Also, the fact that the slope in the lowest mass bin and the highest one are approximately equal – both in the data and in PHSD – can be traced back to the two
3.3. RHIC energies

Now we are coming to the top RHIC energy of $\sqrt{s_{NN}} = 200$ GeV and present the most important findings from the PHSD study in Ref. [6]. In the left part of Fig. 4 we show our results for the invariant mass spectra of inclusive dileptons in Au+Au collisions for the acceptance cuts on single electron transverse momenta $p_{eT} > 0.2$ GeV, $|\eta_e| < 0.35$, $-3\pi/16 < \phi_e < 5\pi/16$, $11\pi/16 < \phi_e < 19\pi/16$, $|y| < 0.35$.

In the low mass region $M = 0 - 1.2$ GeV, the dilepton yield in the PHSD is dominated by hadronic sources and essentially coincides with the earlier HSD result [48]. Note that the collisional broadening scenario for the modification of the $\rho$-meson was used in the calculations presented in Fig. 4 that underestimates the PHENIX data from 0.2 to 0.7 GeV substantially. In contrast, the partonic radiation as well as the yield from correlated $D$-meson decays are dominant in the mass region $M = 1 - 3$ GeV as seen in Fig. 4 (left), i.e. in the mass region between the $\phi$ and $J/\Psi$ peaks. The dileptons generated by the quark-antiquark annihilation in the sQGP constitute about half of the observed yield in this intermediate-mass range. For $M > 2.5$ GeV the partonic yield even dominates over the D-meson contribution. Thus, the inclusion of the partonic radiation in the PHSD fills up the gap between the hadronic model results [48, 49] and the data of the PHENIX Collaboration for $M > 1$ GeV, however, the early expectation of a partonic signal in the low mass dilepton spectrum is not verified by the microscopic PHSD calculations.

In order to investigate the momentum dependance of the "missing low mass yield", we have calculated the $p_T$-spectra of dileptons in different bins of invariant mass $M$. In the right part of Fig. 4 we show the measured transverse momentum spectra of dileptons for minimum bias Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV (symbols) in comparison with the spectra from the PHSD (lines) for six mass bins as indicated in the figure. Whereas the PHSD can well describe the dilepton spectra in the mass intervals [0,100 MeV] and [810 MeV, 990 MeV], it underestimates the low $p_T$ dileptons in the other mass bins, particularly in the mass bins [300 MeV, 500 MeV].
Figure 5. The PHSD results for the invariant mass spectra of dileptons in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV for $M = 0 - 1.2$ GeV (left part) and for $M = 0 - 4$ GeV (right part) and 0 - 10 % centrality within the cuts of the STAR experiment. The preliminary data from the STAR Collaboration are adopted from Ref. [50].

On the other hand, high $p_T$ dileptons are reproduced quite well by the PHSD calculations. We conclude that the missing dilepton yield for masses from 0.15 to 0.6 GeV is essentially due to a severe underestimation of the data at low $p_T$ by up to an order of magnitude. We recall that at top SPS energies the low $p_T$ dilepton yield could be attributed to $\pi\pi$ annihilation channels, i.e. to the soft hadronic reactions in the expansion phase of the system. These channels are, however, insufficient to describe the very low slope of the $p_T$ spectra at the top RHIC energy.

In order to shed some light on the ‘PHENIX puzzle’ we step to a comparison of the PHSD predictions with the preliminary STAR data measured for Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV with the acceptance cuts on single electron transverse momenta $p_{eT}$, single electron pseudorapidities $\eta_e$ and the dilepton pair rapidity $y$, i.e. $0.2 < p_{eT} < 5$ GeV, $|\eta_e| < 1$, $|y| < 1$. Our predictions for the dilepton yield within these cuts are shown in Fig. 5 for 0-80% centrality. One can observe generally a good agreement with the preliminary data from the STAR Collaboration [50] in the whole mass regime. Surprisingly, our calculations are also roughly in line with the low mass dilepton spectrum from STAR in case of central collisions whereas the PHSD results severely underestimate the PHENIX data for central collisions. The observed dilepton yield from STAR at masses below 1.2 GeV can be accounted for by the known hadronic sources, i.e. the decays of the $\pi_0$, $\eta$, $\eta'$, $\omega$, $\rho$, $\phi$ and $a_1$ mesons, of the $\Delta$ particle and the semileptonic decays of the $D$ and $\bar{D}$ mesons, where the collisional broadening of the $\rho$ meson is taken into account.

The discrepancy between the PHENIX and STAR data will have to be investigated closer by the experimental collaborations. Furthermore, the upgrade of the PHENIX experiment with a hadron blind detector should provide decisive information on the origin of the low mass dileptons produced in the heavy-ion collisions at $\sqrt{s_{NN}} = 200$ GeV.

4. Conclusions
We close this contribution by noting that the dileptons are an interesting probe of the dynamical processes in heavy-ion collisions at all energy regimes. The low-mass dileptons provide information on the vector meson spectral function in the medium whereas the high mass part from 1.1 to 3 GeV can be attributed dominantly to the partonic annihilation in the QGP phase. At the higher RHIC and LHC energies the modifications of the low-mass sector are less pronounced than at SIS and SPS energies, however, the dilepton emissivity from the sQGP...
becomes substantial or even dominant relative to the background from $D$-meson decays.

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References

[1] Shuryak E V 1978 Phys. Lett. B 78 150; 1978 Sov. J. Nucl. Phys. 28 408; 1978 Yad. Fiz. 28 796.
[2] Song C, Ko C M and Gale C 1994 Phys. Rev. D 50 1827
[3] Li G Q and Gale C 1998 Phys. Rev. C 58 2914 [arXiv:nucl-th/9807005].
[4] van Hees H and Rapp R 2006 Phys. Rev. Lett. 97 102301
[5] van Hees H and Rapp R 2008 Nucl. Phys. A 806 339
[6] Linnyk O, Cassing W, Manninen J, Bratkovskaya E L and Ko C M 2012 Phys. Rev. C 85 024910
[7] Linnyk O, Bratkovskaya E L, Ozvenchuk V, Cassing W and Ko C M 2011 Phys. Rev. C 84 054917
[8] Cassing W and Bratkovskaya E L 2009 Nucl. Phys. A 831 215
[9] Cassing W 2007 Nucl. Phys. A 795 70
[10] Bratkovskaya E L, Cassing W, Konchakovski V P and Linnyk O 2011 Nucl. Phys. A 856 162
[11] Aoki Y et al. 2009 JHEP 0906 088
[12] Peshier A and Cassing W 2005 Phys. Rev. Lett. 94 172301
[13] Ehehalt W and Cassing W 1996 Nucl. Phys. A 602 449
[14] Cassing W and Bratkovskaya E L 1999 Phys. Rep. 308 65
[15] Bengtsson H U and Sjöstrand T 1987 Comp. Phys. Commun. 46 43
[16] Cassing W 2007 Nucl. Phys. A 791 365
[17] Cassing W 2009 Eur. J. Phys. 30 3
[18] Mattis H S et al., DLS Collaboration 1995 Nucl. Phys. A 583 617C
[19] Wilson K et al. DLS Collaboration 1998 Phys. Rev. C 57 1865
[20] Wilson K et al. DLS Collaboration 1993 Phys. Lett. B 316 245
[21] Porter R J et al. DLS Collaboration 1997 Phys. Rev. Lett. 79 1229
[22] Wolf G, Cassing W and Mosel U 1993 Prog. Part. Nucl. Phys. 30 273
[23] Bratkovskaya E L, Cassing W and Mosel U 1996 Phys. Lett. B 376 12
[24] Xiong L, Wu Z G, Ko C M and Wu J Q 1990 Nucl. Phys. A 512 772
[25] Ernst C, Bass S A, Belkacem M, Stoecker H and Greiner W 1998 Phys. Rev. C 58 447
[26] Bratkovskaya E L, Cassing W, Rapp R, and Wambach J 1998 Nucl. Phys. A 634 168
[27] Bratkovskaya E L and Ko C M Phys. Lett. B 445 265
[28] Fuchs C, Faessler A, Cozma D, Martemyanov B V and Krivoruchenko M I 2005 Nucl. Phys. A 755 499
[29] Agakishiev G et al., HADES Collaboration 2008 Phys. Lett. B 663 43
[30] Pachmayer Y C et al., HADES Collaboration 2008 J. Phys. G 35 104159
[31] Sudol M et al., HADES Collaboration 2009 Eur. Phys. J. C 62 81
[32] Agakishiev G et al., HADES Collaboration 2010 Phys. Lett. B 690 118
[33] Lapidus K et al., HADES Collaboration arXiv:0904.1128 [nucl-ex].
[34] Agakishiev G et al., HADES Collaboration 2011 Phys. Rev. C 84 014902
[35] Agakishiev G et al., HADES Collaboration 2012 Phys. Rev. C, in press, arXiv1203.2549 [nucl-ex]
[36] Kaptari L P and Kämpfer B 2006 Nucl. Phys. A 764 338
[37] Bratkovskaya E L and Cassing W, 2008 Nucl. Phys. A 807 214
[38] Thomere M, Hartnack C, Wolf G and Aichelin J 2007 Phys. Rev. C 75 064902
[39] Barz H W., Kämpfer B, Wolf G and Zetenyi M arXiv:0910.1541 [nucl-th].
[40] Agakishiev G et al., HADES Collaboration 2007 Phys. Rev. Lett. 98 052302
[41] Arnaldi R et al., NA60 Collaboration 2009 Eur. Phys. C 59 607
[42] Arnaldi R et al., NA60 Collaboration 2006 Phys. Rev. Lett. 96 162302; Seixas J et al., 2007 J. Phys. G 34 034015; Damjanovic S et al., 2007 Nucl. Phys. A 783, 237c; Arnaldi R et al., 2009 Eur. Phys. J. C 61 71
[43] Cassing W and Bratkovskaya E L 2009 Nucl. Phys. A 831 215
[44] Linnyk O, Bratkovskaya E L, and Cassing W 2008 Int. J. Mod. Phys. E 17 1367
[45] Alam J, Hirano T, Nayak J K, and Sinha B arXiv:0902.0446.
[46] Toia A, et al., PHENIX Collaboration, 2006 Nucl. Phys. A 774 743
[47] Adare A et al., PHENIX Collaboration 2010 Phys. Rev. C 81 034911
[48] Bratkovskaya E L., Cassing W and Linnyk O 2009 Phys. Lett. B 670 428
[49] Manninen J, Bratkovskaya E L, Cassing W and Linnyk O 2011 Eur. Phys. J. C 71 1615
[50] Zhao J et al., STAR Collaboration arXiv:1106.6146[nucl-ex].