Charm $CP$ violation and mixing at Belle

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Abstract. We present charm $CP$ violation and mixing measurements at Belle. They are the first observation of $D^0 - D^0$ mixing in $e^+e^-$ collisions from $D^0 \rightarrow K^+\pi^-$ decays, the most precise mixing and indirect $CP$ violation parameters from $D^0 \rightarrow K_S^0\pi^+\pi^-$ decays, and the time-integrated $CP$ asymmetries in $D^0 \rightarrow \pi^0n^0$ and $D^0 \rightarrow K_S^0\pi^0$ decays. Our mixing measurement in $D^0 \rightarrow K^+\pi^-$ decays excludes the no-mixing hypothesis at the 5.1 standard deviation level. The mixing parameters $x = (0.56 \pm 0.19^{+0.03+0.06}_{-0.09-0.06}) \%$, $y = (0.30 \pm 0.15^{+0.04+0.02}_{-0.05-0.06}) \%$, and indirect $CP$ violation parameters $|q/p| = (0.90^{+0.15+0.05}_{-0.15-0.05} \pm 0.06 \pm 0.06 \%$, $\arg(q/p) = (-6 \pm 11 \pm 3^{+3}_{-3})^\circ$, measured from $D^0 \rightarrow K_S^0\pi^+\pi^-$ decays, and the time-integrated $CP$ asymmetries $A_{CF}^{D^0 \rightarrow K^+\pi^-} = (-0.03 \pm 0.64 \pm 0.10) \%$ and $A_{CF}^{D^0 \rightarrow K^+\pi^-} = (-0.21 \pm 0.16 \pm 0.07) \%$ are the most precise measurements to date. Our measurements here are consistent with predictions of the standard model.

The magnitudes of $CP$ violation ($CPV$) and mixing rate in the charm system are very small in the standard model (SM) [1, 2]. Therefore, $D^0 - D^0$ mixing and $CPV$ measurements provide a unique probe to search for physics beyond the SM [3, 4]. $D^0 - D^0$ mixing occurs since the mass eigenstates $D_1$ and $D_2$ are different from the flavor eigenstates $D^0$ and $\bar{D}^0$. The mass eigenstates can be written in terms of the flavor eigenstates, namely, $|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$. The phenomenology of meson mixing is described by two parameters, $x = \Delta m/\Gamma$ and $y = \Delta \Gamma/2\Gamma$, where $\Delta m$ and $\Delta \Gamma$ are the mass and width differences between the two mass eigenstates, and $\Gamma$ is the average decay width of the mass eigenstates. Indirect $CPV$ parameters are $|q/p|$ and $\arg(q/p)$, where the former and the latter are responsible for $CPV$ in mixing and that in interference between the decays with and without mixing, respectively.

In this proceedings, we present charm $CPV$ and mixing measurements from the data recorded with the Belle detector [5] at the $e^+e^-$ asymmetric-energy collider KEKB [6].

1. Mixing in $D^0 \rightarrow K^+\pi^-$ decays

We present the first observation of $D^0 - D^0$ mixing from an $e^+e^-$ collision experiment by measuring the time-dependent ratio of the $D^0 \rightarrow K^+\pi^-$ (Wrong Sign) to $D^0 \rightarrow K^-\pi^+$ (Right Sign) decay rates [7]. Assuming $CP$ conservation and that the mixing parameters are small ($|x| \ll 1$ and $|y| \ll 1$), the time-dependent RS and WS decay rates are $\Gamma_{RS}(\hat{t}/\tau) \approx |A_{CF}|^2 e^{-\frac{\hat{t}}{\tau}}$ and $\Gamma_{WS}(\hat{t}/\tau) \approx |A_{CF}|^2 e^{-\frac{\hat{t}}{\tau}} \left( R_D + \sqrt{R_D y^2} \right) \left( \frac{\hat{t}}{\tau} \right)^2$, respectively, to second order in the mixing parameters, where $\hat{t}$ is the true proper decay time, $A_{CF}$ is the Cabibbo-Favored decay amplitude, $\tau$ is the $D^0$ lifetime, $R_D$ is the ratio of DCS (Doubly Cabibbo-Suppressed) to CF decay rates, $x' = x \cos \delta + y \sin \delta$, and $y' = y \cos \delta - x \sin \delta$, where $\delta$ is the strong phase difference.
between the DCS and CF decay amplitudes. The time-dependent ratio of WS to RS decay rates then

$$R(t/\tau) = \frac{\int_{-\infty}^{+\infty} \Gamma_{WS}(t/\tau)R(t/\tau - \tilde{\tau}/\tau)d(\tilde{\tau}/\tau)}{\int_{-\infty}^{+\infty} \Gamma_{RS}(t/\tau)R(t/\tau - \tilde{\tau}/\tau)d(\tilde{\tau}/\tau)},$$

(1)

where $t$ is the reconstructed proper decay time and $R(t/\tau - \tilde{\tau}/\tau)$ is the resolution function of the real decay time, $\tilde{\tau}$. Figure 1 shows the time-dependent ratios of WS to RS decays together with the two hypothesis tests, with (line) and without mixing (dots). The $\chi^2$ difference between the “no-mixing” and “mixing” hypotheses, $\Delta \chi^2 = \chi^2_{\text{no-mixing}} - \chi^2_{\text{mixing}}$, is 29.3 for two degrees of freedom, corresponding to a probability of $4.3 \times 10^{-7}$; this implies the no-mixing hypothesis is excluded at the 5.1 standard deviation level. Thus, we observe $D^0 - D^0$ mixing for the first time in an $e^+e^-$ collision experiment. We also show this in Figure 2 with the $1\sigma$, $3\sigma$, and $5\sigma$ contours around the best fit point in the $(x'^2, y')$ plane.

![Figure 1](image1.png)

**Figure 1.** The time-dependent ratios of WS to RS decay rates. Points with error bars reflect the data and their total uncertainties. The lines show the fit with (solid) and without (dashed) the mixing hypothesis.

![Figure 2](image2.png)

**Figure 2.** Best-fit point and contours in the $(x'^2, y')$ plane. The solid, dashed, and dotted lines, respectively, correspond to 1, 3, and 5 standard Gaussian deviations from the best fit. The cross is the no-mixing point.

2. **Mixing and indirect CPV in $D^0 \to K_S^0\pi^+\pi^-$ decays**

We present the most precise mixing and indirect CPV violation parameters from $D^0 \to K_S^0\pi^+\pi^-$ decays [8] using the time-dependent Dalitz fit analysis [9]. The time-dependent decay matrix elements of $D^0 \to K_S^0\pi^+\pi^-$ and $\bar{D}^0 \to K_S^0\pi^+\pi^-$ are

$$\mathcal{M}(m_+^2, m_-^2, t) = g_+(t)A(m_+^2, m_-^2) + \frac{q}{p}g_-(t)\bar{A}(m_+^2, m_-^2)$$

and

$$\mathcal{M}(m_+^2, m_-^2, t) = g_+(t)\bar{A}(m_+^2, m_-^2) + \frac{q}{p}g_-(t)A(m_+^2, m_-^2),$$

(2)

where $m_+^2 = m_{K_S^0\pi^+}^2$, $A(m_+^2, m_-^2) = \sum a_je^{i\delta_j}A_j(m_+^2, m_-^2)$, $\bar{A}(m_+^2, m_-^2) = \sum \bar{a}_je^{i\delta_j}A_j(m_+^2, m_-^2)$, $g_+(t) = (e^{-i\lambda_1t} \pm e^{-i\lambda_2t})/2$, and $\lambda_i = m_i - i\Gamma_i/2$, where $a_j$, $\delta_j$, and $A_j(m_+^2, m_-^2)$ are amplitude, phase, and resonance matrix element, respectively. The decay matrix element squared $\mathcal{M}^2$ then contains the mixing parameters $x$ and $y$ as well as $q/p$ of which magnitude and argument are indirect CPV parameters. Two separate time-integrated Dalitz fits to $D^0$ and $\bar{D}^0$ samples show no direct CPV resulting in $a_j \approx \bar{a}_j$ and $\delta \approx \delta$. Hence, we search for indirect CPV assuming...
no direct CPV, namely, $A(m_+^2, m_-^2) = A(m_+^2, m_-^2)$. The best fit model for $A(m_+^2, m_-^2)$ is found to be a sum of twelve Breit-Wigner for $P$- and $D$-wave resonances, $K$-matrix [10] and LASS [11] models for $\pi\pi$ and $K\pi$ S-wave states, respectively, without non-resonant decay. Figure 3 shows the proper-time distribution superimposing the fit under both direct and indirect CP conservation and the fit results are $x = (0.56 \pm 0.19^{+0.03+0.06}_{-0.09-0.09})\%$ and $y = (0.30 \pm 0.15^{+0.04+0.03}_{-0.05-0.06})\%$. With allowing indirect CPV, the fit returns $x = (0.56 \pm 0.19^{+0.04+0.06}_{-0.08-0.08})\%$, $y = (0.30 \pm 0.15^{+0.05+0.07}_{-0.15-0.04})\%$, $|q/p| = (0.90^{+0.16+0.05}_{-0.15-0.05})$, and $\arg(q/p) = (-6 \pm 11 \pm 3^{+3}_{-4})^\circ$. Our measurements of indirect CPV parameters are the most accurate to date, but consistent with no CPV. Figure 4 show the two-dimensional $(x, y)$ confidence-level (C.L.) contours for the CP-conserved and CPV-allowed fits, where the no-mixing point $(x = 0, y = 0)$ is excluded with 2.5 standard deviations.

Figure 3. The proper-time distribution for events in the signal region (points) and fit projection for the CP conserved fit (curve). The shaded region shows the combinatorial components. The residuals are shown below the plot.

Figure 4. Central value (point) and C.L. contours for $(x, y)$ : dotted (dashed) corresponds to 68.3\% (95\%) C.L. contour for CP-conserved Dalitz fit, and solid corresponds to 95\% C.L. contour for CPV-allowed fit with statistical, experimental and model uncertainties included.

3. **Time-integrated CPV in $D^0 \rightarrow \pi^0\pi^0$ and $D^0 \rightarrow K^0_S\pi^0$ decays**

We present the time-integrated CPV asymmetry in $D^0 \rightarrow f$, $A_{CP}^{D^0-f}$, where $f$ is the final state $\pi^0\pi^0$ or $K^0_S\pi^0$ [12]. It is measured through the reconstruction asymmetry

$$A_{rec} \approx A_{CP}^{D^0-f} + A_{FB}^{D^0+,D^0-} + A_{FB}^{D^0+,D^0-},$$

where $N_{rec}$ is the number of reconstructed signal events, $A_{FB}$ is the forward-backward asymmetry, $A_{FB}^{D^0+,D^0-}$ is the detection asymmetry between positively and negatively charged soft pions, and $A_{FB}^{D^0+,D^0-}$ is the asymmetry due to different nuclear interactions between $K^0$ and $K^0$ [13], thus included to the decay $D^0 \rightarrow K^0_S\pi^0$. Once we remove $A_{FB}^{D^0+,D^0-}$ with the correction in Ref. [14]
and $A_{K^0}$ with the value in Ref. [15], then $A_{rec}$ becomes to have $A_{CP}^{D^0 \rightarrow f}$ and $A_{FB}^{D^{*+}}$ only, where the latter is an odd function of the cosine of the polar angle of the $D^{*+}$ momentum in the center-of-mass system ($\cos \theta_{D^{*+}}$). Using the antisymmetry of $A_{FB}^{D^{*+}}$ in $\cos \theta_{D^{*+}}$, we obtain $A_{CP}$ as a function of $|\cos \theta_{D^{*+}}|$ as shown in Figure 5. The central $A_{CP}$ values obtained from a least-square minimization are $A_{CP}^{D^0 \rightarrow \pi^0 \pi^0} = (-0.03 \pm 0.64 \pm 0.10)\%$ and $A_{CP}^{D^0 \rightarrow K^0_S \pi^0} = (-0.21 \pm 0.16 \pm 0.07)\%$ which are the most precise measurements to date revealing no CPV, thus consistent with the SM.

**Figure 5.** The $A_{CP}$ values in the decays $D^0 \rightarrow \pi^0 \pi^0$ (left) and $D^0 \rightarrow K^0_S \pi^0$ (right) as a function of $|\cos \theta^*|$. The solid lines and shaded regions represent the central value and 1$\sigma$ interval of the $A_{CP}$.

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