DOUBLE HORIZONTAL BRANCHES IN NGC 6440 AND NGC 6569 UNVEILED BY THE VVV SURVEY∗

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ABSTRACT

We report the discovery of a peculiar horizontal branch (HB) in NGC 6440 and NGC 6569, two massive and metal-rich Galactic globular clusters (GGCs) located in the Galactic bulge, within 4 kpc from the Galactic center. In both clusters, two distinct clumps are detected at the level of the cluster HB, separated by only ~0.1 mag in the $K_s$ band. They were detected with IR photometric data collected with the “VISTA Variables in the Vía Láctea” Survey, and confirmed in independent IR catalogs available in the literature and Hubble Space Telescope optical photometry. Our analysis demonstrates that these clumps are real cluster features, not a product of field contamination or interstellar reddening. The observed split HBs could be a signature of two stellar sub-populations with different chemical composition and/or age, as recently found in Terzan 5, but it cannot be excluded that they are caused by evolutionary effects, in particular for NGC 6440. This interpretation, however, requires an anomalously high helium content ($\gamma > 0.30$). Our discovery suggests that such a peculiar HB morphology could be a common feature of massive, metal-rich bulge GGCs.

Key word: globular clusters; general

1. INTRODUCTION

Our understanding of the complexity of Galactic globular clusters (GGCs) has impressively expanded in the last decade, propelled by the discovery that they can host multiple populations of stars with a different chemical enrichment history (Piotto et al. 2005). The classical textbook definition of GGCs as prototypes of a simple stellar population, i.e., a chemically homogeneous aggregate of coeval stars, is now outdated. While a certain degree of inhomogeneity of light chemical elements is observed in nearly all GGCs (Carretta et al. 2009), a spread in iron content is a characteristic restricted to only a few very massive objects (Freeman & Rodgers 1975; Yong & Grundahl 2008; Cohen et al. 2010). Ferraro et al. (2009) discovered two horizontal branches (HBs) in the bulge GGC Terzan 5, separated by 0.3 mag in the $K_s$ band. The existence of multi-modality in the morphology of HBs has been known for nearly four decades (Harris 1975), and has been associated with the presence of multiple stellar populations since shortly thereafter (Rood & Crocker 1985). However, to date, Terzan 5 is the only globular cluster known to have two distinct HBs. The two features in Terzan 5 have a different spatial distribution, the brighter one being more centrally concentrated, more metal rich ($\Delta[Fe/H] \sim 0.5$ dex; Origlia et al. 2011), and possibly helium enhanced (D’Antona et al. 2010) and/or younger (Ferraro et al. 2009). Lanzoni et al. (2010) confirmed that Terzan 5 is more massive than previously thought, and it could be the relic of a bulge building block.

In this Letter, we show evidence that the bulge GGCs NGC 6440 and NGC 6569 host split HBs, similar to that of Terzan 5. NGC 6440 is a high-metallicity ([Fe/H] $\sim 0.5$; Origlia et al. 2008) cluster, located 8.5 kpc from the Sun and only 1.3 kpc from the Galactic center (Harris 1996, 2010 edition, hereafter H10). NGC 6569 is slightly less metal-rich ([Fe/H] $\approx -0.79$; Valenti et al. 2011) and is found at a distance of 10.9 kpc from the Sun and 3.1 kpc from the Galactic center (H10). Both NGC 6440 and NGC 6569 are among the 10 most luminous of the 64 GGCs located within 4 kpc from the Galactic center.

2. OBSERVATIONS AND REDUCTIONS

The “VISTA Variables in the Vía Láctea” (VVV) Survey (Minniti et al. 2010) is one of the six ESO Public Surveys operating on the 4 m Visible and Infrared Survey Telescope for Astronomy (VISTA). VVV is scanning the Galactic bulge and the adjacent part of the southern disk ($−65 \leq l \leq 10$, $−2 \leq b \leq +2$), in five near-IR bands ($Y^\prime Z^\prime J^\prime H^\prime K_s$) with the VIRCAM camera (Emerson & Sutherland 2010), an array of sixteen 2048 $\times$ 2048 pixel detectors with a pixel scale of 0.341 pixel$^{-1}$. VVV images extend four magnitudes deeper and exhibit increased spatial resolution (Saito et al. 2010) versus Two Micron All Sky Survey (2MASS; Skrutskie et al. 2006), which is particularly important for mitigating contaminated photometry in crowded regions near the Galactic center.

We retrieved from the VISTA Science Archive website the VVV images of the two GGCs, pre-reduced at the Cambridge Astronomical Survey Unit with the VIRCAM pipeline (Irwin et al. 2004). The selected data consist of four frames, sampling each point twice in an area of 17′′ $\times$ 22′′ around the GGCs, in each of the $Z^\prime J^\prime H^\prime K_s$ filters, plus 17 and 11 additional epochs in the $K_s$ frame (Saito et al. 2012) for NGC 6440 and NGC 6569, respectively. The VVV images of the two clusters, extracted from a single $K_s$ frame, are shown in Figure 1.

The point-spread function fitting photometry was obtained with the VVV-SkZ_pipeline (VSp; Mauro et al. 2012), code based on DAOPHOT and ALLFRAME (Stetson 1987, 1994) procedures, optimized for the VVV data. The photometry was

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* Based on observations gathered with ESO-VISTA telescope (proposal ID 172.B-2002).

http://horus.roe.ac.uk/vsa/

http://casu.ast.cam.ac.uk/
tied to 2MASS $JHK_s$ standards, as described in Moni Bidin et al. (2011) and Chen et al. (2012). Combining all the 36 and 24 $K_s$ measurements, the final photometric errors were 0.003 and 0.008 mag respectively at the brightness level of the cluster HB. The $K_s$ errors for NGC 6569 are constant with distance, while in NGC 6440 they increase up to 0.005 mag for $r<0.7$. The completeness of our photometry is heavily affected by crowding in the inner $0.7$ of both clusters, as can be appreciated in Figures 1 and 4. Due to incompleteness, ~80% of the detected HB stars stay outside this problematic inner region, where crowding is not a significant issue.

3. RESULTS

The $(J-K_s; K_s)$ Hess diagrams (HDs) for the stars detected within $1.83$ and $1.66$ from the cluster center, respectively, are shown in Figures 2 and 3. They were obtained calculating the number of stars in a bin of width 0.06 mag in $J-K_s$ (0.04 mag in the lower panels) and 0.04 mag in $K_s$, moved along the axis with steps of 0.015 mag in color (0.01 mag in the lower diagram) and 0.01 mag in magnitude. The HDs of both GGCs reveal a peculiar HB morphology, with two distinct clumps separated by ~0.1 mag. They will be referred to as HB-A and HB-B (lower panels of Figures 2 and 3) for the brighter and fainter one, respectively. The overdensity observed as a redder color is the red giant branch (RGB) bump: in fact, Valenti et al. (2005, hereafter V05) found $K_s$,bump = 14.08 in NGC 6569, and their $K_s$,bump–[Fe/H] relation predicts $K_s$,bump ≈ 14.1 in NGC 6440, in good agreement with our data.

To verify if both HBs are real and belong to their host cluster, we checked the data for stochastic fluctuations as a cause of the overdensity, and analyzed their spatial distribution as a function of the central distance. Furthermore, we compared our data with the IR photometry of Valenti et al. (2004, hereafter V04) and V05, and with the optical Hubble Space Telescope (HST) data from Piotto et al. (2002).

**Dereddening.** We used the maps from Gonzalez et al. (2011) to correct for reddening. They reveal that $E(J-K_s) ≈ 0.5–0.7$ in the $r = 1.8$ field of NGC 6440 under analysis. The case of NGC 6569 is much less extreme, with $E(J-K_s) = 0.20–0.24$. The HD of NGC 6440 shows a clear improvement (see Figure 2), with the two features less blurred and HB-B still presenting...
a slope. For NGC 6569 the dereddened HD is approximately similar to the raw one, as expected.

**Checking for stochastic variation.** We ran the procedure on four subsets of the original data, each one containing the ZY and JHKs data, but different Ke epochs: one subset included only the first epoch, while a unique set of three epochs were used in each of the three following subsets. The declared photometric errors in Ke passband vary from 0.007–0.009 mag to 0.003–0.005 mag at the level of the HB. Comparing the (J−Ke) HDs, obtained with the previous spacial selection and sampling procedure, both GGCs always exhibit a split HB, with only negligible differences in their morphology. As an additional test, we checked the HBs of other GGCs in the VVV, namely NGC 6380, NGC 6441, NGC 6528, and NGC 6553, finding no evidence of a split or peculiar HB.

**Field contamination and spatial distribution.** We checked the field contribution to the HDs, selecting an annular region with near-zero levels at large distances from the cluster centers.

The behavior of the stellar densities (SDs) with distance r from the center is shown in Figure 4 for the two features highlighted in the lower panels of Figures 2 and 3. The SDs (stars arcmin⁻²) were calculated with a bin width of 10'' moved at steps of 2'' for NGC 6440, while for NGC 6569 we used the values of 15'' and 6'', respectively. The SDs of the two groups steeply decay at increasing radii, in both GGCs, and their members are distributed on the CCD with circular symmetry. The radial profile of the two features in NGC 6569 is identical. The HB-B group in NGC 6440 is more populated than the brighter HB-A by a factor of two, but a Kolmogorov–Smirnov test reveals that their radial behavior coincides also in this case. The stellar counts in the inner 0.7′ ≃ Sr is the core radius from H10) are incomplete because of crowding. The photometry of NGC 6569 is also incomplete for r < 0.7′ ≃ 2rc.

The radial profile of NGC 6569 was fit with a King (1962) profile of the form:

\[
f(r) = k \left[ \left( 1 + \left( \frac{r}{r_c} \right)^2 \right)^{-1/2} - \left( 1 + \left( \frac{r}{r_t} \right)^2 \right)^{-1/2} \right]^2 + F,
\]

where \(k\) is a scale parameter, \(r_c\) is the tidal radius, and \(F\) the field contribution. For NGC 6440, we used the approximation for \(r >> r_c\):

\[
f(r) = k r_c^2 \left( \frac{1}{r} - \frac{1}{r_t} \right)^2 + F.
\]

For NGC 6440, the fit leads to \(r_A = 5.1 ± 0.7\) and \(r_B = 5.2 ± 0.5\), consistent with \(r_c = 5.84\) quoted by H10. The core radius and the scale parameter cannot be separated and estimated individually. The SDs of the two features in NGC 6569 are compatible with \(r_c = 0.35\) and \(r_c = 7.15\) (H10).

**Comparison with previous photometry.** We matched our VVV photometry of NGC 6440 and NGC 6569 with the catalogs of V04 and V05, respectively. The photometry of V04 is based on observations with the near-IR camera IRAC2@ESO/MPI 2.2 m, covering a 250'' × 250'' field centered on the cluster. Similarly, the photometry of V05 was performed on data collected with the near-IR camera SOFI@ESO/NTT, covering a 300'' × 300'' field centered on the cluster. The estimated internal photometric errors are lower than 0.03 mag. Both photometries were calibrated onto the 2MASS photometric system and astrometrically corrected by using the 2MASS catalog.

For both GGCs, the luminosity distributions in the Ke magnitudes of the V04 and V05 catalogs for the matched stars do not show a clear bimodal distribution. However, when the stars belonging to the HB-A and HB-B groups are identified, their luminosity distributions are different, as shown in Figure 5. For NGC 6440, the Gaussian fits of the two distributions are centered at \(K_{s,V04} = 13.55\) and \(K_{s,V05} = 13.66\) for HB-A and HB-B, respectively, with a dispersion of \(\sigma = 0.12\). While in our VVV photometry, the values are \(K_{s,VVV} = 13.55\) and 13.67, respectively, with a dispersion of \(\sigma = 0.03\). Analogously, we find \(K_{s,V05} = 14.26\) and \(K_{s,V05} = 14.36\), respectively, for the HB-A and HB-B clumps in NGC 6569, with a dispersion of \(\sigma = 0.07\), and \(K_{s,VVV} = 14.26\) and 14.35 for the same features in our photometry, with a dispersion of \(\sigma = 0.02\). Thus, the mean magnitude of the clumps of both GGCs is identical in VVV and Valenti et al.'s catalogs, but the separation is four times more statistically significant in the VVV data. This result proves that the HBs of both GGCs are intrinsically split in magnitude, with a brighter and a fainter part that remain separated even in V04 and V05 photometry, respectively, once the stars are identified.

The strong differential reddening affecting the region of NGC 6440 causes the HB to be strongly tilted at optical wavelengths, hence a simple luminosity distribution does not show a bimodal behavior. For this reason, we analyzed the HST...
optical data of Piotto et al. (2002), projecting the position of each HB star along the HB slope, according to the equation:

\[
F_{555W_{nr}} = F_{555W_{nr}} - a(F_{439W_{nr}} - F_{555W_{nr}} - (F_{439W_{nr}} - F_{555W_{nr}}) - 2.2)
\]

where \(a = 3.7\) is the slope of the HB and \((F_{439W_{nr}} - F_{555W_{nr}}) = 2.2\) is the HB mean color. As advised by the authors, the magnitudes adopted were those not corrected for reddening \((nr)\). To avoid contamination from RGB stars, we selected only the sources with \(18.2 \leq F_{555W_{nr}} \leq 19.1\) and \(2 \leq (F_{439W_{nr}} - F_{555W_{nr}}) \leq 2.4\). The distribution of \(F_{555W_{nr}}\), calculated with bin width of 0.08 mag and step of 0.04 mag (see Figure 5), reveals a clear double peak separated by \(~0.23\) mag, with the fainter peak 1.6–1.7 times more populated. A similar procedure was performed for NGC 6569 also, but we were not able to disentangle any bimodality.

4. DISCUSSIONS AND CONCLUSIONS

The analysis of VVV data reveals that the HB of the GGCs NGC 6440 and NGC 6569 is split into two distinct clumps. This behavior is not introduced by stochastic fluctuations of the density in the color–magnitude diagram (CMD), or induced by photometric errors, as it is found to be identical in four independent subsets of data. Field contamination is not the cause either, because the members of both HBs are distributed with spherical symmetry with respect to the cluster center, and their density steeply decays with distance. The separation in NGC 6440 is even cleaner after applying a differential reddening correction, while in NGC 6569 it remains similar, presenting lower differential reddening. This HB split is, however, not found in the same VVV data of four less massive bulge GGCs.

The magnitude difference between the two HB clumps is only \(~0.08–0.1\) mag in \(K_s\), smaller than in Terzan 5 by a factor of three. It is thus not surprising that this HB split...
NGC 6440 is more populated than the brighter one by about a factor of two, slightly higher than what was found in the central regions of Terzan 5 (~1.6; Ferraro et al. 2009). However, these results are not directly comparable because our photometry is incomplete in the inner 0.7 of NGC 6440. HST data suggest that in the central region this ratio could be lower (~1.6), as expected if, analogously to Terzan 5, the brighter HB was more centrally concentrated. On the other hand, we did not detect any difference in the radial density profile of the two clumps, so the issue remains unresolved.

The two HBs of Terzan 5 are associated with two sub-populations of different metallicity, with the brighter HB being richer in iron by ~0.5 dex (Ferraro et al. 2009; Origlia et al. 2011). According to Salaris & Girardi (2002), a difference of ~0.3 dex would be expected if the observed HB splits are interpreted only in terms of metallicity. Nevertheless, this is only a rough upper limit, because differences in helium content and age also can contribute to cause the same split. Origlia et al. (2008) measured the metallicity of 10 stars in NGC 6440, finding a dispersion of only 0.06 dex, compatible with observational errors. However, their targets are mainly located within 0.7 of the center, where the HB-A members could be few if the population ratio is constant at all radial distances. Hence, Origlia et al.’s sample likely contains only a small quantity of HB-A stars, and their results are insufficient to exclude a metallicity spread in this cluster.

Contrary to the case of NGC 6440 and Terzan 5, the two groups identified in the HB of NGC 6569 have approximately the same color and the same radial distribution, the fainter HB-B being 1.3 times more populated than the other clump. Valenti et al. (2011) measured the metallicity of six stars in this cluster, finding a bimodal distribution with two groups separated by ~0.08 dex.

It is possible that the peculiar HB morphology discovered in NGC 6440 is a pure evolutionary effect, and not a signature of the presence of sub-populations. In fact, wedge-shaped HBs are predicted under special circumstances, as depicted in Figure 4 of Catelan & de Freitas Pacheco (1996) and Figure 1 of Dorman et al. (1989), and statistical effects could lead to the actual bimodal distribution of HB magnitudes. These features are found in the luminosity–temperature plane, but the simulated optical CMDs reveal only a clump at the bluer (and brighter) end of the sloped HB, at variance with what is observed in HST data, while the behavior of these features in the IR bands has not been simulated. Hence, this interpretation seems unlikely, but it cannot be excluded and represents an intriguing possibility. In fact, the high metallicity alone cannot explain the formation of a wedge-like HB, and a very high helium abundance (~Y > 0.30) is required. Such an He-enriched field population has been recently interpreted only in terms of metallicity. Nevertheless, this is.

The interpretation of these features as an evolutionary effect implies that the helium content of this cluster must be anomalously high, actually higher than what is predicted at [Fe/H] = −0.5 by the models of bulge chemical enrichment (e.g., Catelan & de Freitas Pacheco 1996). The split HB observed in NGC 6569, whose components are well separated and with a narrow color spread, is very different to the simulated HBs of Catelan & de Freitas Pacheco (1996) and Dorman et al. (1989). The interpretation of these features as an evolutionary effect induced by a high helium content is unlikely.

The fainter HB of NGC 6440 (HB-B) is tilted, the brightness of its stars increasing at bluer colors. This is clearly visible in Figure 2, where we indicate the direction of the reddening

passed unnoticed in previous investigations, considering also the strong differential reddening affecting the NGC 6440 field (ΔE(J − Ks) = 0.2; Gonzalez et al. 2011). We find that the dichotomy is blurred by observational errors in the IR photometry of V04 and V05, but the two features are clearly separated even in their data once their members are identified in their catalog. The HST optical data of NGC 6440 from Piotto et al. (2002) show two peaks separated by 0.23 mag in the corrected magnitude F555Wnr defined in Equation (3).

The fainter HB of NGC 6440 is bluer than the brighter one. This resembles what was previously found in Terzan 5 (Ferraro et al. 2009; Lanzoni et al. 2010). In addition, the fainter HB of

Figure 5. Luminosity distribution in $K_{s,V04}$ and $K_{s,V05}$ passband (in upper and middle frames for NGC 6440 and NGC 6569, respectively) for the matched stars belonging to the two features HB-A and HB-B of the respective GGCs. Luminosity distribution of the values $F555W_{nr}$ for NGC 6440 in the lower frame. The center and the sigma resulting from the Gaussian fits are also shown.
in the IR bands from Catelan et al. (2011) for comparison. Dereddening the photometry, the slope is still present, but the map resolution of 1′ does not permit strong claims. The tilt is more pronounced in the optical HST photometry of Piotto et al. (2002), where we measured a slope $\Delta(B) / \Delta(B-V) \approx 3.7$, which is higher than the standard reddening law $R_V = A_V / E(B-V) \approx 3.1$. Moreover, the optical extinction is non-standard toward the Galactic bulge, and $R_V$ can be as low as $\sim 2.5$ (Nataf et al. 2012). In conclusion, the slope of the HB in NGC 6440 is directed approximately aligned with the reddening vector, but it is steeper than the expectations of interstellar reddening. This behavior was already observed in NGC 6388 and NGC 6441 (Sweigart & Catelan 1998; Busso et al. 2007), two other massive, metal-rich bulge GGCs, and it was attributed to an anomalously high helium content (Catol & D’Antona 2007). Very interestingly, the HB stars of NGC 6388 could show the same peculiar properties observed in $\omega$ Centauri (Moehler & Sweigart 2006; Moni Bidin et al. 2011), the most famous cluster hosting a complex mix of sub-populations with different chemical enrichment histories.

Our results indicate that Terzan 5 is not a unique object. A complex HB morphology could be a relatively common feature among metal-rich, massive bulge GGCs. This is not detected in less massive objects (e.g., NGC 6528, NGC 6553), or in equally massive but metal-poor bulge GGCs, such as M 22 and M 28, whose HB is very extended toward the blue. The large metallicity spread observed in Terzan 5 (Origlia et al. 2011) is also present in M22 (Marino et al. 2009). Further investigations are needed to unveil if the HB splits reflect the presence of two stellar populations with different chemical composition and/or age.

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REFERENCES

Busso, G., Cassisi, S., Piotto, G., et al. 2007, A&A, 474, 105
Caloi, V., & D’Antona, F. 2007, A&A, 463, 949
Carretta, E., Bragaglia, A., Gratton, R. G., et al. 2009, A&A, 505, 117
Catelan, M., & de Freitas Pacheco, J. A. 1996, PASP, 108, 166
Catelan, M., Minniti, D., Lucas, P. W., et al. 2011, in RR Lyrae Stars, Metal-Poor Stars, and the Galaxy, ed. A. McWilliam (Pasadena: CA: The Observatories of the Carnegie Institute of Washington), 145
Chené, A.-N., Borissova, J., Clarke, J. R. A., et al. 2012, A&A, 545A, 54
Cohen, J. G., Kirby, E. N., Simon, J. D., & Geha, M. 2010, ApJ, 725, 288
D’Antona, F., Ventura, P., Caloi, V., et al. 2010, ApJ, 715, L63
Dorman, B., VandenBerg, D. A., & Laskarides, P. G. 1989, ApJ, 343, 750
Emerson, J., & Sutherland, W. 2010, The Messenger, 139, 2
Ferraro, F. R., Dalessandro, E., Mucciarelli, A., et al. 2009, Nature, 462, 483
Freeman, K. C., & Rodgers, A. W. 1975, ApJ, 201, L71
Gonzalez, O. A., Rejkuba, M., Zoccali, M., Valenti, E., & Minniti, D. 2011, A&A, 534, A3
Harris, W. E. 1975, ApJS, 29, 397
Harris, W. E. 1996, AJ, 112, 1487
Irwin, M. J., Lewis, J., Hodgkin, S., et al. 2004, Proc. SPIE, 5493, 411
King, I. 1962, AJ, 67, 471
Lanzoni, B., Ferraro, F. R., Dalessandro, E., et al. 2010, ApJ, 717, 653
Marino, A. F., Milone, A. P., Piotto, G., et al. 2009, A&A, 505, 1099
Mauro, F., Moni Bidin, C., Chené, A. N., et al. 2011, RMxAA, submitted
Minniti, D., Lucas, P. W., Emerson, J. P., et al. 2010, New Astron., 15, 433
Moehler, S., & Sweigart, A. V. 2006, A&A, 455, 943
Minniti, C., Mauro, F., Geisler, D., et al. 2011, A&A, 535, A33
Moni Bidin, C., Villanova, S., Piotto, G., Moehler, S., & D’Antona, F. 2011, ApJ, 738, L10
Nataf, D. M., & Gould, A. 2012, ApJ, 751, L39
Nataf, D. M., Gould, A., Fouqué, P., et al. 2012, ApJ, submitted (arXiv:1208.1263)
Origlia, L., Rich, R. M., Ferraro, F. R., et al. 2011, ApJ, 726, L20
Origlia, L., Valenti, E., & Rich, R. M. 2008, MNRAS, 388, 1419
Piotto, G., King, I. R., Djorgovski, S. G., et al. 2002, A&A, 391, 945
Valenti, E., Ferraro, F. R., & Origlia, L. 2004, MNRAS, 351, 1204
Valenti, E., Ferraro, F. R., & Origlia, L. 2005, MNRAS, 361, 272
Rood, R. T., & Crocker, D. A. 1985, Horizontal-branch and UV-bright Stars (Schenectady: L Davis Press), 99
Saito, R., Hempel, M., Alonso-García, J., et al. 2010, The Messenger, 141, 24
Saito, R. K., Hempel, M., Minniti, D., et al. 2012, A&A, 537, A107
Salaris, M., & Girardi, L. 2002, MNRAS, 337, 332
Skrutskie, M. F., Cutri, R. M., Stiening, R., et al. 2006, AJ, 131, 1163
Stetson, P. B. 1987, PASP, 99, 191
Stetson, P. B. 1994, PASP, 106, 250
Sweigart, A. V., & Catelan, M. 1998, ApJ, 501, L63
Valenti, E., Ferraro, F. R., & Origlia, L. 2004, MNRAS, 351, 1204
Valenti, E., Ferraro, F. R., & Origlia, L. 2005, MNRAS, 361, 272
Valenti, E., Origlia, L., & Rich, R. M. 2011, MNRAS, 414, 2690
Yong, D., & Grundahl, F. 2008, ApJ, 672, L29