Modeling and Control PV-Wind Hybrid System Based On Fuzzy Logic Control Technique

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1. Introduction

Alternative energy sources such as solar and wind energies, has attracted many researchers and communities throughout the world since the “energy crisis” of the 1973 [1]. In addition, the increasing of energy demand, high energy prices, as well as the increasing concern on over environmental aspects, health and climate change implications of energy related to activities effecting the increasing concerns on alternative energy studies in communities [2-6]. The high costs of electricity might be due to centralize the energy systems which operate mostly on fossil fuels and require large investments for establish transmission and distribution grids which can penetrate remote regions [6]. Furthermore, the fossil fuel combustion results in the emission of obnoxious gases which rising concerns in climate change and other health hazards [7]. Conventional control algorithms require a mathematical model for the dynamic system to be controlled. The mathematical model then used to construct a controller. In many practical situations, however, it is not always feasible to obtain an accurate mathematical model of the controlled system. Artificial intelligent (AI) control offers a way dealing with modeling problems by implementing linguistic, non-formal expressed control laws derived from expert knowledge [8]. This paper presents a mathematical modeling of PV-wind hybrid system. Moreover, a control system using FLC controller is developed for achieving the coordination between the components of a PV-Wind hybrid system as well as control the energy flows between PV, wind and battery. This study is performed for an aquaculture system in remote area in Mersa Matruh, Egypt.
2. Modeling of Hybrid System Components

The goal of this work is to simulate the operation of PV-wind battery hybrid energy system as accurate as possible. To achieve this aim, one needs a set of relative detailed models. In this section, the individual mathematical model for each component is developed in MATLAB.

Various modeling techniques are developed by researchers to model components of hybrid renewable energy system (HRES). Performance of individual components is either modeled by deterministic or probabilistic approaches. General methodology for modeling HRES components like PV, wind and battery is described below.

2.1. PV Mathematical Model

A PV system consists of many cells which connected in series and parallel to provide the desired output terminal voltage and current, and exhibits a nonlinear $I$–$V$ characteristic [9-11]. The PV cell equivalent model represents the dynamic nonlinear $I$–$V$ characteristics of the PV system is described below [9-11]. The operating equation of current – voltage characteristics of solar cell under illumination effect is expressed by [12-14]

$$\begin{align*}
I_c &= N_p I_{oc} - N_n I_{ph} \left( \exp \left( \frac{V + IR_s}{V_t} \right) - 1 \right) \\
V_t &= a k T_p \frac{T_p}{q} \tag{1}
\end{align*}$$

Light generated current is given as:

$$I_g = \frac{G}{G_r} \left[ I_{sc} + m(T_c - T_r) \right] \tag{2}$$

Where reverse saturation current of PV cell is represented by

$$\begin{align*}
I_{ph} &= I_{ph} \left( \frac{T_c}{T_r} \right)^{\frac{c}{2}} \exp \left( -b \left[ \left( \frac{V}{V_t} \right) - \left( \frac{1}{V_t} \right) \right] \right) \\
I_{sc} &= \frac{I_{sc}}{\exp \left( \frac{V_{sc}}{V_t} \right) - 1} \tag{4}
\end{align*}$$

Cell temperature can be calculated by using the following equation [14]

$$T_c = T_r + \left[ \left( \frac{\alpha}{U_t} \right) \left( 1 - \frac{\eta}{\alpha} \right) \right] G \tag{6}$$

where,

- $I_{ph}$: Output current of PV array, (A).
- $V$: Output voltage of PV array, (V).
- $N_s$: Number of series modules.
- $N_p$: Number of parallel strings.
- $I_{ph}$: Light generated current, (A).
- $I_{sc}$: Reverse saturation current at operating temperature, (A).
- $I_{sc}$: Short circuit current at 28°C and 1000 W/m² (=2.52 A).
- $a, b$: Ideality factors (=1.92).
- $T_r$: Reference temperature (=301 K).
- $T_p$: Cell temperature (K).
- $T_c$: Cell temperature (°C).
- $k$: Boltzmann’s constant (=1.38×10^{-23} J/K).
- $G$: Cell illumination, W/m².
- $G_r$: Reference illumination (=1000 W/m²).
- $E_g$: Band gap for silicon (=1.11 ev).
- $m$: Short circuit current temperature coefficient (=0.0017 A/°C).
- $q$: Electron charge (=1.602×10^{-19} C).
2.2. Wind Turbine Generator

There are several existing models for the estimation of wind turbine power, such as the linear model, the model based on Weibull parameters and the quadratic model [15-19]. Choosing a suitable model is very important for wind turbine power simulation. There are three main factors that determine the output power of a wind turbine, i.e. the output power curve (determined by aerodynamic power efficiency, mechanical transmission and converting electricity efficiency) of a chosen wind turbine, the wind speed distribution of a selected site where the wind turbine is installed, and the tower height. The power curve of the machine reflects the aerodynamic, transmission and generation efficiencies of the system in an integrated form. Figure 1 shows the typical power curve of a generic wind turbine. The rated power of the turbine is 3 KW. The given curve is a theoretical one, and in practice we may observe the velocity power variation in a rather scattered pattern.

![Power curve of wind turbine](image_url)

Figure 1. Power curve of wind turbine.

The power curve of a wind turbine is non-linear. The data is available from the manufacturer and can be easily digitized and the resulting table can be used to simulate the wind turbine performance [20]. The outlet energy of a turbine could be calculated from its power-speed curve [21, 22]. The output power of each WG unit versus wind speed is, always, given by manufacturer and usually describes the real power transferred from WG to DC bus. In this study, Generic Wind turbine is considered. It has a rated capacity of 3 kW and provides 24 V DC at the output. The characteristic equation of wind generator is obtained by fitting the practical output characteristic curve using a least square minimization technique [23]. By using curve fitting to obtain a mathematical modeling of nonlinear region in power curve of wind turbine, the curve fitting equation of the output characteristic of wind generator can be expressed as [24]

\[
P = \begin{cases} 
0 & \text{if } V_c < V_i \\
V_i + \frac{b}{a} V_i^2 + c V_i^3 + d V_i + e & \text{if } V_i < V_r < V_c \\
V_r & \text{if } V_r < V_c < V_o
\end{cases} \tag{7}
\]

\[
p_w = A_v \eta p \tag{8}
\]

where,
- \(V_s\) Velocity (m/s).
- \(V_c\) Cut in velocity (m/s).
- \(V_r\) Rated velocity (m/s).
- \(V_o\) Cut out velocity (m/s).
\( P \)  
Output power density (W/m\(^2\)).

\( P_r \)  
Rated power density (W/m\(^2\)).

\( P_w \)  
Output power of wind turbine (W).

\( a, b, c, d, e \)  
Fitting parameters.

\( A_w \)  
Total swept area (m\(^2\)).

\( \eta \)  
Generator efficiency.

To express the exact model that represent the used of wind turbine power curve, the curve fitting using MATLAB toolbox has been used to extract the model. Linear model Poly4is used and the coefficient are (with 95% confidence bounds): \( a = 0.0005096 \), \( b = -0.02656 \), \( c = 0.4564 \), \( d = -2.747 \), \( e = 5.362 \), SSE: 0.03718, R-square: 0.998 and RMSE: 0.05566.

### 2.3. The Battery Storage Model

The battery model describes the relationship between the voltage, current and the state of charge is discussed. The equivalent electrical circuit of storage battery is adopted by Figure 6.4. The terminal voltage of a battery can be expressed in terms of its open circuit voltage and the voltage drop across the internal resistance of the battery [25]:

\[
V_s = V_r + I_s R_B
\]  
(9)

Where,

\( \zeta_B \)  
Battery terminal voltage (V).

\( I_B \)  
Battery current (A) (positive when charging and negative when discharging).

\( V_r \)  
Rest voltage (V).

\( R_B \)  
Internal resistance of the battery (ohms).

The rest voltage, \( V_r \), is expressed in terms of cell temperature as

\[
V_r = 2.04 \left[ 1 - 0.001 \left( T_r - T_c \right) \right]
\]  
(10)

The battery resistance during charge and discharge process is given by:

\[
R_{sc} = \frac{1}{BC} \left[ R + \frac{0.189}{(1.142 - SOC)} \right] + (SOC - 0.9) \ln \left( 300 \frac{I_s}{BC} + 1 \right)
\]  
(11)

\[
R_{sd} = -\frac{1}{BC} \left( \frac{0.189}{SOC} + R \right)
\]  
(12)

\[
R_v = 0.15 \left[ 1 - 0.02 \left( T_r - T_c \right) \right]
\]  
(13)

The battery state of charge is the instantaneous ratio of the actual amount of charge stored in the battery and the total charge capacity of the battery at a certain battery current. In the model, it is estimated as [26-28]:

\[
SOC = SOC_0 + \frac{Q}{BC}
\]  
(14)

where,

\( BC \)  
Battery capacity.

\( SOC \)  
Battery state of charge.

\( T_r \)  
Reference temperature.

\( T_c \)  
Cell temperature.

\( SOC_0 \)  
Previous SOC.

\( Q \)  
Amount of exchanged charge from the previous time to the time of interest (C).

\( BC \)  
Battery capacity (Ah).

\( I_B \)  
Battery current (A).
3. The Fuzzy Logic Concept

Fuzzy logic arose from a desire to incorporate logical reasoning and the intuitive decision making of an expert operator into an automated system [8]. The aim is to make decision based on a number of learned or predefined rules, rather than numerical calculations. Fuzzy logic incorporates rule-base structure in attempting to make decisions [8, 27]. However, before the rule-base can be used, the input data should be represented in such a way as to retain meaning, while, still allowing for manipulation. Fuzzy logic is an aggregation of rules based on the input state variables condition with a corresponding desired output. A mechanism must exist to decide on which output or combination of the different outputs will be used since each rule could conceivably result in a different output action. Fuzzy logic can be viewed as an alternative form of input-output mapping.

The fuzzy rule representation is based on linguistic [8, 27]. Thus, the input is a linguistic variable that corresponds to the state variable under consideration. In fuzzy logic control, the term “linguistic variable” refers to whatever state variables the system designer is interested in [8]. The fuzzy variable is perhaps better described as a fuzzy linguistic qualifier. Once, the linguistic and fuzzy variables have been specified, the complete inference system can be defined as developing a FIS and applying it to a control problem involves several steps:

a. Fuzzification.
b. Fuzzy rule evaluation (fuzzy inference engine).
c. Defuzzification.

4. Electrical System Control

The aim of PV wind battery hybrid system controller is to ensure the management of the power, which is delivered by the hybrid system to satisfy the load and to charge the lead acid battery during the period of excess generated energy. The power management strategy flowchart is adopted in Figure 2. The block diagram of controlling the PV wind battery hybrid system using FLC is shown in Figure 3.
The reference load is compared with the generated power to produce the error signal which used as input signal to FLC. Membership function values are assigned to the linguistic variables, using seven fuzzy subsets: NB (negative big), NM (negative medium), NS (negative small), ZE (zero), PS (positive small), PM (positive medium), and PB (positive big). The value of input error (e) and change of error (ce) are normalized by an input scaling factor. The triangular shape of the membership function of this arrangement presumes that for any particular input there is only one dominant fuzzy subset. The composition operation is the method by which the controlled output is generated. The Max–Min method is used. The output membership function of each rule is given by the Minimum. Table 1 shows the rule base of the FLC. As a system usually requires a non fuzzy value of control, a defuzzification stage is needed. Defuzzification for this system is the center of gravity method which is simple and fast. The overall system SIMULINK block diagram is presented in Figure 4. The block diagram of FLC unit built in MATLAB SIMULINK is shown in Figure 5. The triangular membership function used in this control design summarized in Figure 6.

Table 1. Rule base of fuzzy logic controller.

| Error (e) | CHANGE OF ERROR (CE) | NL | NM | NS | ZE | PS | PM | PL |
|----------|----------------------|----|----|----|----|----|----|----|
| NL       | NL                   | NL | NL | NL | NL | NS | NS | ZE |
| NM       | NL                   | NL | NL | NM | NS | ZE | PS | PL |
| NS       | NL                   | NL | NL | NS | ZE | PS | PM | PL |
| ZE       | NL                   | NM | NS | ZE | PS | PM | PL | PL |
| PS       | NS                   | NS | ZE | PS | PL | PL | PL | PL |
| PM       | NS                   | ZE | PS | PM | PL | PL | PL | PL |
| PL       | ZE                   | PS | PL | PL | PL | PL | PL | PL |

Figure 5. SIMULINK block diagram of FLC.

Figure 6. Membership functions.
5. System Simulation

The electrical subsystem consists of several units, PV array and wind generator units as primary sources of energy, battery bank unit as auxiliary source of energy, load unit and control unit. By applying FLC as control technique which is developed to control the power management between different sources and the load, The PV-wind-battery hybrid system SIMULINK block diagram using FLC is given by Figure 7. The PV unit implementation using MATLAB SIMULINK is depicted in Figure 8. The PV unit has two input parameters affected PV generator performance; the solar irradiance and the air temperature while the outputs are PV current ($I_{PV}$), PV voltage ($V_{PV}$) and PV power ($P_{PV}$). The wind turbine unit has the wind speed as input signal and the wind current ($I_{W}$) and the power ($P_{W}$) as output signals.

The battery bank SIMULINK model implementation is illustrated in Figure 9. The battery has the air temperature and the charge current as input variables, and gives the battery voltage during charge ($V_{BC}$) and discharge ($V_{BD}$) process, the power ($P_{B}$), the state of charge (SOC) and the depth of discharge (DOD).

The control unit implemented by FLC is designed to control the battery current according to the supplement of the load with the required power. FLC has two inputs and one output. The inverter unit is used to convert the DC generated power from renewable energy sources to feed the load with the required AC power.
6. Results

In this section the simulation results of the electrical subsystem are introduced and analyzed. The results are given in a typical day in summer and winter to verify the different environmental condition variation over the year. Each unit has its inputs and outputs, the control results of using FLC techniques are obtained to evaluate the control performance.

The solar irradiance and air temperature are used as the input parameters for the PV operation. The outputs are the PV current and the PV power. The PV power in summer and winter is presented in Figure 10. The value of PV power in summer is higher than in winter due to high solar irradiance and medium air temperature. The PV power takes the same shape of the solar irradiance due to the direct proportional relationship between them. PV and wind unit have been used to supply the load with the required power. The wind power is cleared in Figure 11. The wind power in winter is higher than in summer which has the inverse operation of PV unit so that the PV and the wind unit have compensated each other to feed the load over the year. The battery has the following operation; it is used to store excess energy during the day hours and to feed load with the required energy when there is no solar irradiance and wind speed. FLC is used to control the battery operation during charge and discharge process. The battery power variation over the day of simulation using FLC is given by Figure 12.

The battery feeds the load during the night hours and begins to charge with increasing the solar irradiance and the wind speed. The battery charges to higher current values in summer rather than in winter due to the high power generation of renewable energy resources in summer season.
Applying the proposed control technique on the desired application, Figure 13 shows the generated current using FLC with reference load in summer and winter. It is obvious that, the generated current tracked the reference load over the simulation period. The error signal is depicted in Figure 14. The error signal ensures that the two signals (load current and generated current) have the same shape so the error signal has zero amplitude.

Figure 11. Wind generator power (a) summer (b) winter.

Figure 12. The battery power over the simulation period using FLC (a) summer (b) winter.

Figure 13. The generated current over the simulation period using FLC (a) summer (b) winter.
7. Conclusion

The investigated PV-wind hybrid system is designed to be totally self-satisfy the load during the operation period. The system is simulated to predict its performance under different environmental conditions before implemented in remote areas. Design via simulation allows studying different options, considering various influence parameters and effectively fulfills the system/user requirements. Mathematical models of the system components are interconnected to form a general representation of the whole system, through a central supervisory controller that defines the way in which components interact to simulate the operation of the entire system. The power management between PV array, wind generator, battery bank, and the load was controlled using FLC. The system performance using FLC had high applicability of FLC technique for this application. The simulation results using MATLAB SIMULINK showed the high performance of the proposed system. The results showed that the PV and wind generator were capable of feeding the load with the required energy and charge the battery with its demands during night hours. FLC has two input signals which are error and change of error. 49 rule bases, the COG and Max-Min method were used.

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