The origin of redshift asymmetries: how ΛCDM explains anomalous redshift

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ABSTRACT

Aims. Several authors have found a statistically significant excess of galaxies with higher redshifts relative to the group centre, so-called discordant redshifts, in particular in groups where the brightest galaxy, identified in apparent magnitudes, is a spiral. Our aim is to explain the observed redshift excess.

Methods. We use a semi-analytical galaxy catalogue constructed from the Millennium Simulation to study redshift asymmetries in spiral-dominated groups in the cold dark matter (ΛCDM) cosmology. We create two mock catalogues of galaxy groups with the Friends-of-Friends percolation algorithm to carry out this study.

Results. We show that discordant redshifts in small galaxy groups arise when these groups are gravitationally unbound and the dominant galaxy of the group is misidentified. About one quarter of all groups in our mock catalogues belong to this category. The redshift excess is especially significant when the apparently brightest galaxy can be identified as a spiral, in full agreement with observations. On the other hand, the groups that are gravitationally bound do not show a significant redshift asymmetry. When the dominant members of groups in mock catalogues are identified by using the absolute B-band magnitudes, our results show a small blueshift excess. This result is due to the magnitude limited observations that miss the faint background galaxies in groups.

Conclusions. When the group centre is not correctly identified it may cause the major part of the observed redshift excess. If the group is also gravitationally unbound, the level of the redshift excess becomes as high as in observations. There is no need to introduce any “anomalous” redshift mechanism to explain the observed redshift excess. Further, as the Friends-of-Friends percolation algorithm picks out the expanding parts of groups, in addition to the gravitationally bound group cores, group catalogues constructed in this way cannot be used as if the groups are purely bound systems.

Key words. galaxies: clusters: general – galaxies: distances and redshifts – methods: N-body simulations – methods: numerical – cosmology: large-scale structure of Universe

1. Introduction

Groups of galaxies contain a large fraction of all galaxies in the Universe (Hollmerb 1950; Humason et al. 1956; Huchra & Geller 1982; Geller & Huchra 1983; Nothenius & White 1987; Ramella et al. 2002). These density enhancements in the sky and in the redshift space are important cosmological indicators of the distribution of matter in the Universe, and may provide important clues for galaxy formation. Groups of galaxies are, in general, divided into a large number of different classes, for example, loose groups (e.g. Ramella et al. 1995; Tucker et al. 2000; Einasto et al. 2003), poor groups (e.g. Zabludoff & Mulchaey 1998; Mahdavi et al. 1999), compact groups (e.g. Shakhbazyan 1973; Hickson 1982; Hickson et al. 1989; Focardi & Kelm 2002) and fossil groups (e.g. Ponman et al. 1994; Jones et al. 2003; D'Onghia et al. 2005; Santos et al. 2007). However, from the observational point of view, groups of galaxies and their member galaxies are not extremely well defined.

In recent years a number of grouping algorithms have been developed and applied (e.g. Turner & Gott 1976; Materné 1978; Huchra & Geller 1982; Botzler et al. 2004; Goto et al. 2002; Kim et al. 2002; Bahcall et al. 2003; Koester et al. 2007; Yang et al. 2007) to identify real groups. Despite the vast number of grouping algorithms, the Friends-of-Friends (FoF; Huchra & Geller 1982, hereafter HG82) percolation algorithm remains the most frequently applied. The FoF algorithm or slightly modified versions of it are widely used even for modern day galaxy surveys. Several authors have presented group and cluster catalogues that applied the FoF algorithm based on the SDSS (Sloan digital sky survey) data (e.g. Merchan & Zandivarez 2005; Berlind et al. 2006; Tago et al. 2008) and on the 2dF (the two degree field) data (e.g. Eke et al. 2004; Tago et al. 2006).

Few studies (see Niemi et al. 2007, and references therein) have argued that grouping algorithms may not always return true groups; a significant number of groups can be spurious and contain interlopers. Niemi et al. (2007, hereafter Paper I) have shown that the FoF algorithm produces a significant fraction of groupings which are not gravitationally bound systems, but merely groups in a visual sense. This can introduce various errors when these groups are studied in detail and treated as gravitationally bound structures.

This may even be true for compact groups of galaxies. In this case, and also in general, extended X-ray emission can be used to distinguish real, gravitationally bound groups from spurious ones. The analysis of X-ray data suggests that errors are rather common (Ostriker et al. 1995, and references therein). Unfortunately, groups with low mass and a spiral-dominated main galaxy in general do not show any extended X-ray emission. Therefore this method is not useful for small and loose groups of galaxies.
An excess of higher redshift galaxies was discovered by Arp (1970, 1982) and it was studied in detail by Jaakkola (1971). Since then many authors have found a statistically significant excess of high redshift companions relative to the group centre. Bottinelli & Gouguenheim (1973) extended the study of Arp (1970) to nearby groups of galaxies in which the magnitude difference between the companion and the main galaxy was greater than 0.4 mag. Sulentic (1984) found a statistically significant excess of positive redshifts while studying spiral-dominated (i.e. the central galaxy is a spiral galaxy) groups in the catalogue of galaxy groups by HG82. The two mock catalogues differ in the values of free parameters of the FoF grouping algorithm.

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If the group as a whole is not virialized, there is no need for the redshift symmetry explanation of Valtonen & Byrd (1986) to work; whether it works quantitatively is a question to be answered in this paper.

In this paper we study redshift asymmetries theoretically in small groups of galaxies by taking advantage of the largest cosmological N-body simulation conducted so far: the Millennium Run (Springel et al. 2005). We create two “mock” catalogues of groups of galaxies from the semi-analytical galaxy catalogue (Licia & Blaizot 2007) of the Millennium Simulation by mimicking observational methods. For the creation of mock catalogues we apply the Friends-of-Friends percolation algorithm developed by HG82. The two mock catalogues differ in the values of parameters of the FoF grouping algorithm.

We show that the excess of positive redshifts is mainly due to wrong identification of the dominant galaxy in a group and, at the same time, the group being gravitationally unbound. We also show that groups that show a large excess of positive redshifts are more often gravitationally unbound than groups that do not show any significant excess. These errors in the identification of the dominant galaxy result from our current inability to measure the relative distances inside groups of galaxies, except for a few of the nearest ones (Karachentsev et al. 1997; Jerjen et al. 2001; Rekola et al. 2005a,b; Teerikorpi et al. 2008). Due to peculiar motions of group members we cannot transform the apparent magnitudes of galaxies in group catalogues into absolute magnitudes precisely.

The sample of galaxy groups

The two mock catalogues of groups of galaxies from Millennium Simulation data were constructed so that they would be comparable to the real observational group catalogues HG82 and UZC-SSRS2 (Ramella et al. 2002) as much as possible. Both of these catalogues are produced with the FoF algorithm. However, slightly different values for the free parameters of the algorithm have been used. We show in Sect. 3.1 that our groups from the Millennium Simulation are comparable to observed groups in a statistical sense. We also discuss briefly how our results compare to works of other authors.

2.1. Millennium simulation data

The Millennium simulation (MS; Springel et al. 2005) is a cosmological N-body simulation of the ΛCDM model performed by the Virgo Consortium. The MS was carried out with a customized version of the GADGET2 code developed by Springel et al. (2001b). The MS follows the evolution of 21603 particles from redshift $z = 127$ in a box of 500 h$^{-1}$ Mpc on a side. The cosmological parameters of the MS simulation are: $\Omega_m = \Omega_{m0} + \Omega_b = 0.25$, $\Omega_b = 0.045$, $h = 0.73$, $\Omega_{\Lambda} = 0.75$, $n = 1$, and $\sigma_8 = 0.9$ (for a detailed description of the MS see Springel et al. 2005).

The galaxy formation modeling of the MS data is based on merger trees built from 64 individual snapshots. Properties of
galaxies in MS data are obtained by using semi-analytical galaxy formation models, where the star formation and its regulation by feedback processes is parametrized in terms of analytical physical models. A detailed description of the creation of the MS galaxy catalogue can be found in Lucia & Blaizot (2007), see also Croton et al. (2006).

The MS galaxy database does not directly give a morphology for galaxies. We have used a method which takes an advantage of bulge-to-disc ratios to assign a morphology to every galaxy. Simien & de Vaucouleurs (1986) found a correlation between the bulge magnitude and $T$ magnitude of galaxies. We have used a method which takes an advantage of the total magnitude and $T$ magnitude to assign a morphology to every galaxy. We have used a method which takes an advantage of the total magnitude and $T$ magnitude to assign a morphology to every galaxy.

We produce two mock catalogues with different choices of free parameters. Both group catalogues are generated from five independent volumes of the Millennium Simulation galaxy catalogue. Each of the cubes used have a side length of 250 $h^{-1}$ Mpc, and they do not overlap. The observation point inside each volume was chosen to be in the centre of the particular cube. No additional criteria were applied for the selection of observation points. Reasonable statistical agreement, as shown in the next section between mock catalogues and observed group catalogues shows that our method of choosing the origin without any further criteria is strict enough in a statistical study of galaxy groups. Both of our catalogues from simulations, Mock1 and Mock2, contain groups of galaxies whose lower limit on the number of members, $n$, is 3. All groups containing $n > 2$ members are considered when group properties are studied in Sect. 3.1. In Sect. 3.2 we limit the number of group members to $2 < n < 11$, comparable to S84.

Our first mock catalogue, named Mock1, is generated with the same values ($m_{\text{lim}} = 13.2$, in the Zwicky or de Vaucouleurs B(0) magnitude system, $D_0 = 0.60$ $h^{-1}$ Mpc and $V_{0} = 400$ km s$^{-1}$) of the free parameters as the original HG82 catalogue. This choice guarantees that we can compare results found in S84 directly to our simulated catalogue and we can be sure that different choices of parameter values do not effect the results. Even though the Mock1 catalogue uses the same values of parameters as HG82 it contains over 10 times more groups than the original HG82 catalogue. Thus it provides significantly better statistics.

Our Mock2 catalogue has an apparent $B$-band magnitude limit of $m_{\text{lim}} = 14.0$, while $V_{0}$ = 200 km s$^{-1}$ and $D_0 = 0.37$ $h^{-1}$ Mpc were adopted for the free parameters of the FoF algorithm, corresponding to the space density enhancement of $\sim 68$. Despite the use of more strict parameters, Mock2 contains almost 10 times more groups than Mock1 due to the fainter apparent $B$-band magnitude limit adopted. Because of the greater number of groups, Mock2 is used for comparison and for better statistics. It should also contain groups which are more often gravitationally bound due to the higher density enhancement of groups.

Table 1 shows the values of free parameters used in creating our mock catalogues. It also shows parameter values of various group catalogues based on modern redshift surveys. All catalogues shown in Table 1 have been generated with the FoF algorithm. However, catalogues based on the SDSS and the 2dF data

### Table 1. Values of free parameters used for creating mock and observed group catalogues.

| Authors          | Sample | $m_{\text{lim}}$ | $D_0$ | $V_0$ | $\delta_{\text{F}}$ | $\alpha$ | $M^*$ | $\phi^*$ |
|------------------|--------|------------------|-------|-------|----------------------|----------|-------|---------|
| This paper       | Mock1  | 13.2             | 0.64  | 400   | 19.8                 | $-1.02$  | $-19.06$ | 0.0277  |
| This paper       | Mock2  | 14.0             | 0.37  | 200   | 68.0                 | $-1.15$  | $-19.84$ | 0.0172  |
| Huchra & Geller  | HG82   | 13.2             | 0.64  | 400   | 20                  | $-1.02$  | $-19.06$ | 0.0277  |
| Ramella et al.   | UZC-SSRS2 | 15.5             | 0.25  | 350   | 80                  | $-1.1 (-1.2)$ | $-19.1 (-19.73)$ | 0.04 (0.013) |
| Eke et al. (2004)| 2dFGRS | 19.45            | 0.13  | 143   | --                  | --       | --    | --      |
| Goto (2005)      | SDSS-DR2 | 17.77            | 1.5   | 1000  | --                  | --       | --    | --      |
| Mercán & Zandivadev (2005) | SDSS-DR3 | 17.77          | --  | 200   | 80                  | $-1.05$  | $-20.44$ | --      |
| Berlind et al. (2006) | SDSS-DR5 | 17.5            | 0.14  | 75    | --                  | --       | --    | --      |
| Tago et al. (2006)| 2dFGRS | 19.45            | 0.25  | 200   | --                  | $-1.21$  | $-19.66$ | --      |
| Tago et al. (2008)| SDSS-DR5 | 17.77            | 0.25  | 250   | --                  | --       | --    | --      |

Columns: The group catalogue used, $m_{\text{lim}}$ is the apparent magnitude limit of the search ($B$-band for mock catalogues, $r$-band for the SDSS and $b_J$ for the 2dF; note however that different redshift limits have been applied in individual papers), $D_0$ is the projected separation in $h^{-1}$ Mpc chosen at some fiducial redshift, $V_0$ is the velocity difference in km s$^{-1}$, $\delta_{\text{F}}$ is the density enhancement and $\alpha$, $M^*$, and $\phi^*$ parametrize the Schechter (1976) function. The Schechter parameters for the Mock2 sample are derived from the Millennium Galaxy Catalogue by Driver et al. (2007). The Schechter parameters for Ramella et al. (2002) refer to the CfA (SSRS2) groups.
have taken advantage of modified versions of the original FoF. The most noticeable modifications include the use of dark matter mock catalogues and group re-centering.

There are large differences between the Mock1 and Mock2 catalogues. The most obvious difference is in the total number of groups. Mock1 contains 1601 groups in total while Mock2 contains 13 786 groups. Note that five different “observation” points inside the MS are used, and none of these observation points overlap each other. The difference in the number of groups is due to the difference in the adopted apparent B-band magnitude limit. If we compare the fraction of gravitationally bound groups between the two catalogues, (i.e. $T_{	ext{vir}}/U < 1$, where $T_{	ext{vir}}$ is the kinetic energy and $U$ is the absolute value of the potential energy of the group; for a detailed description see Paper I) the differences are not great. The fraction of gravitationally bound groups is surprisingly low in both mock catalogues. In the Mock1 catalogue the fraction of bound groups is 52.64 ± 9.21% while in Mock2 it is only 50.19 ± 1.15%. The error limits are standard deviation errors between the five observation points.

It is an indication of the reliability of the group-finding algorithm that the same relative number of bound groups are found in spite of the fact that the Mock2 catalogue has about three times higher density enhancement than Mock1. In Paper I we found that the Mock2 catalogue contains a significant fraction of groups that are not gravitationally bound systems. Based on the FoF algorithm contain a significant fraction of groups that are not gravitationally bound systems.

### 3. Analysis of groups

#### 3.1. Comparison with observations

In this subsection we briefly show that our mock catalogues are comparable to real observational group catalogues. We compare our simulated mock catalogues to UZC-SSRS2 and to HG82 catalogues. We only show comparisons in velocity dispersion and in the “observable” mass of groups. Even though our mock catalogues are comparable to observations, we find some differences. We also find differences between the two mock catalogues. Before discussing these differences we briefly review the comparison catalogues and parameters.

The HG82 group catalogue was derived from a whole sky catalogue of 1312 galaxies brighter than $m_B = 13.2$ (in Zwicky or de Vaucouleurs B(0) magnitude system) with complete redshift information. The velocity of each galaxy has been corrected for a dipole Virgo-centric flow. The catalogue of groups was obtained with $D_h = 0.60$ h$^{-1}$ Mpc (corresponding to a density enhancement of ~20) and with $V_{0} = 400$ km s$^{-1}$. Only groups containing more than two members have been included in the final catalogue.

The UZC-SSRS2 group catalogue was derived from a magnitude-limited redshift sample of galaxies. A compilation of 6846 galaxies with the apparent magnitude limit of $m_{	ext{lim}} \leq 15.5$ was used for the creation of the UZC-SSRS2 catalogue, which contains, in total, 1168 groups. The group catalogue covers 4.69 sr, and the parameter values of $V_0 = 350$ km s$^{-1}$ and $D_0 = 0.25$ h$^{-1}$ Mpc have been adopted for the creation of the UZC-SSRS2 catalogue. These values correspond to a density contrast threshold ~80. Only groups containing more than two members have been included in the final catalogue.

Our mock catalogues were discussed in the previous section. However, we would like to point out that our Mock1 (Mock2) catalogue is comparable to HG82 (UZC-SSRS2) in the choice of parameters. The Mock2 catalogue does not adopt exactly the same parameters as the UZC-SSRS2, even though the density enhancement is comparable. The reason for not adopting exactly the same values is that volumes inside the MS are not large enough. Adopting $m_{	ext{lim}} = 15.5$ would have introduced errors in groups and their properties due to edge effects and missing group members. We wish to avoid this, as our purpose is to study distribution of group members and possible redshift asymmetries.

We have shown in Paper I that cosmological N-body simulations can produce groups of galaxies which are comparable to observations. However, in Paper I, we were greatly limited by the volume of our simulation boxes, causing comparisons to be less conclusive. Moreover, in Paper I we compared properties of dark matter haloes to real observed galaxies. As Millennium Simulation offers a larger volume and the properties of the galaxy data are derived with semi-analytical models, the comparison between mock catalogues and observational catalogues (UZC-SSRS2 and HG82) is now more robust. We use the same definitions and equations for velocity dispersion and “observable” mass of a group as in Paper I.

The velocity dispersion $\sigma_v$ of a group is defined as:

$$\sigma_v = \sqrt{\frac{1}{N_G - 1} \sum_{i=1}^{N_G} (v_i - \langle v_i \rangle)^2}, \quad (3)$$

where $N_G$ is the number of galaxies in a group, $v_i$ is the radial velocity of the $i$th galaxy and $\langle v_i \rangle$ is the mean group radial velocity. In observations, the group masses can be estimated by various methods. In the HG82 and in the UZC-SSRS2 catalogues the total mass of a group is estimated with a simple relation:

$$M_{\text{obs}} = 6.96 \times 10^8 \sigma_v^2 R_{\text{H}} M_\odot, \quad (4)$$

where $\sigma_v$ is the velocity dispersion, and $R_{\text{H}}$ is the mean harmonic radius:

$$R_{\text{H}} = \frac{\pi \langle v_g \rangle}{H_0} \sin \left( \frac{1}{2} \left[ \frac{N_G(N_G-1)}{2} \sum_{i=1}^{N_G} \sum_{j=i+1}^{N_G} \theta_{ij} \right]^{-1} \right), \quad (5)$$

where $\theta_{ij}$ is the angular separation of the $i$th and $j$th group members.

To compare abundances of groups in magnitude-limited samples we weight each group according to its distance (Moore et al. 1993; Diaferio et al. 1999). This weighting is necessary as there is no “total” volume of a galaxy sample in magnitude-limited group catalogues. After weighting each group individually we can scale abundances of groups in Figs. 1 and 2 to the comoving volume of the sample. We include all galaxies with $cz > 500$ km s$^{-1}$. This lower cut-off avoids including faint objects that are close to the observation point as these groups could contain galaxies fainter than in real magnitude-limited surveys. Therefore we consider only groups with mean radial velocity, $\langle cz \rangle$, greater than 500 km s$^{-1}$ in Mock1, Mock2, HG82 and UZC-SSRS2 catalogues.

Figures 1 and 2 show that cosmological N-body simulations can produce groups of galaxies whose statistical properties are similar to observed ones. The agreement is, in general, within $2\sigma$ error bars. However, there are clear differences visible between all catalogues in both figures. These differences are discussed below in greater detail. We use a statistical Kolmogorov-Smirnov (K-S) test to prove or disprove the null hypothesis, $H_{\text{null}}$, that the two distributions are alike and are drawn from the same population distribution function. Results of the K-S tests are presented.
Fig. 1. The cumulative number density of velocity dispersion $\sigma_v$ for galaxy groups. Simulation data are averaged over the ensemble of 5 observation points. The error bars are $1\sigma$ errors and are only shown for Mock2 for clarity. The error bars for other data have similar or slightly greater size due to poorer statistics.

Fig. 2. Group abundance by “observable” mass of the groups. Simulation data are averaged over the ensemble of 5 observation points. The error bars are $1\sigma$ errors and are only shown for Mock2 for clarity. The error bars for other data have similar or slightly greater size due to poorer statistics.

as significance levels (value of the $Q$ function) for the null hypothesis and are listed in Table 2.

Both figures show that the total density of the Mock1 and HG82 catalogue is lower than of Mock2 and UZC-SSRS2. This result is due to the lower apparent magnitude limit of these catalogues, even when weighting is applied. Mock1 and the HG82 are missing more faint galaxies than Mock2 and UZC-SSRS2 due to the lower magnitude limit. Because of this, these catalogues are missing groups that are built only from relatively faint galaxies i.e. these catalogues miss small groups with small velocity dispersions in comparison to Mock2 and UZC-SSRS2.

Figure 1 shows that groups of galaxies in our mock catalogues are similar to observed ones in a statistical sense when velocity dispersions are studied. However, both mock catalogues show an excess of high velocity dispersion groups in comparison to observations. Despite these differences the K-S test is approved (at level of 0.01) for Mock1 when the comparison is to HG82 and for Mock2 when the comparison is to the UZC-SSRS2 catalogue. It is also noteworthy that the Mock1 catalogue shows a small excess of groups around $\sim 500$ km s$^{-1}$ in comparison to Mock2. This difference is probably due to the larger value of $V_0$ in Mock1 that allows a greater difference between group members in redshift space.

Qualitatively better agreement in velocity dispersion is observed when mock catalogues are compared to the UZC-SSRS2 catalogue. There are also some differences between the HG82 and UZC-SSRS2 catalogue, especially when the abundance of high velocity dispersion groups are considered. The discrepancy between the mock catalogues and the HG82 group catalogue is relatively large when large velocity dispersions are considered. This difference is due to the low number of groups (92) in HG82. Also the volume of the HG82 catalogue is relatively small. Thus, the HG82 catalogue lacks high velocity dispersion groups and clusters as the Virgo cluster is the only big cluster within the visible volume of the catalogue.

The quartile values of velocity dispersion of the Mock1 (Mock2) catalogue groups are $131.0/213.4/347.4$ km s$^{-1}$ (80.5/131.0/213.4 km s$^{-1}$). The values of the Mock2 catalogue groups are closer to the observed ones than the values of mock catalogue groups of Paper I. The large values of Mock1 groups can be explained with larger number of interlopers due to the lower density enhancement and the relatively large value of $V_0$. The above differences show that the selection of $V_0$ is important, especially for velocity dispersions of groups.

From Fig. 2 it is clear that our mock catalogues show an excess in the abundance of heavier groups. Despite the differences the K-S test supports the null hypothesis for the Mock2 catalogue (for numerical details see Table 2). Because of the strong connection between group mass and the velocity dispersion (see Eq. (4)) the Mock1 catalogue shows (qualitatively) similar behavior in both Figs. 1 and 2. There is also a significant difference between HG82 and UZC-SSRS2 catalogue when the abundance of massive groups is studied. However, the most striking difference is between mock catalogues and HG82 when massive groups and clusters are considered. These differences can be explained with the small volume and the low number of large groups in HG82. In total, HG82 has only two groups with more than 30 members while the UZC-SSRS2 catalogue has 14 groups. The Mock1 (Mock2) catalogue has 45 (276) groups that have more than 30 members. It is obvious that the most massive groups are the ones that have highest velocity dispersion and that are the most expanded ones, meaning simply the ones having most members.

The quartile values of “observable” mass of the Mock1 (Mock2) catalogue groups are $0.7/3.5/7.9 \times 10^{13}$ $M_\odot$ $(1.4/3.1/15.8 \times 10^{13}$ $M_\odot$). The values of Mock2 are close to the observed values (see Table 4 in Paper I for numerical details) even if there is an excess in the abundance of massive groups in comparison to observations. The good agreement in quartile

Table 2. The significance levels of the K-S tests.

| Sample | Property | HG82 | UZC-SSRS2 | HG82 vs. UZC-SSRS2 |
|--------|----------|------|-----------|---------------------|
| Mock1  | $\sigma_v$ | 0.013 | 0.08      |
| Mock2  | $\sigma_v$ | 0.015 | 0.05      |
| Mock2  | $M_0$   | 0.042 | 0.05      |

Note: Significance levels of the K-S test for the null hypothesis that observations and the simulations are alike and are drawn from the same parent population (HG82 and UZC-SSRS2 columns). Significance level of the K-S test for the null hypothesis that the HG82 and the UZC-SSRS2 group catalogue are alike and are drawn from the same parent population (HG82 vs. UZC-SSRS2 column).
values suggests that simulated groups are similar in a statistical sense, as the greatest differences in Fig. 2 are observed at very low densities.

Despite the differences discussed above, our mock catalogues are comparable to observational catalogues in a statistical sense (see Table 2). This conclusion is supported by the K-S tests, by the good agreement on quartile values and by the fact that the properties of simulated groups are, in general, within 2σ error limits. We do not compare other properties of groups in this paper, as the focus of the paper is to study and explain the observed redshift asymmetries. However, before explaining these asymmetries we briefly compare our results to the findings of other authors.

Eke et al. (2004, 2006) have previously applied the same method to galaxy groups identified in the 2dFGR Survey. These groups are typically much further away than our groups, as the median redshift of their groups is 0.11. Despite this difference we make an attempt to compare their results to ours. Eke et al. (2004) found the median velocity dispersion of 227 km s\(^{-1}\) for groups with at least three members. This is rather close to our Mock1 catalogue value (\(\sim 213\) km s\(^{-1}\)) implying that our mock groups are similar to their groups in a statistical sense. The median velocity dispersion of the Mock2 catalogue is only \(\sim 131\) km s\(^{-1}\), and differs significantly from the value of Eke et al. (2004). This result is somewhat expected, as our mock groups are all found at very close distances. The median value of dynamical mass in our Mock1 catalogue is close to the value of Eke et al. (2004); even though their definition of dynamical mass is different to ours.

Eke et al. (2004) found that as much as \(\sim 40\) per cent of groups can contain interlopers. This fraction is close to the fraction of groups we find to be gravitationally unbound. Eke et al. (2006) found that dynamical group masses give higher abundances to the mass function. It is possible that the reason for this discrepancy lies in the large fraction of unbound groups. If the (dynamical) mass of a group is calculated by adopting the virial theorem, one has to assume that the group is a bound structure. However, if one applies the virial theorem to a group that is gravitationally unbound, the dynamical mass of the group can be overestimated significantly. Even if the virial theorem is not used while calculating the dynamical mass, one can easily overestimate the mass, as unbound groups can have significantly higher velocity dispersion and size, leading to the higher abundance noticed by Eke et al. (2006).

As groups observed by Eke et al. (2004, 2006) are typically much further away, these groups are not expected to show significant redshift asymmetry. In our groups the distance ratio of the far side of the group relative to the front side of the group can be rather large, and this causes the interesting effects that are discussed next.

3.2. Redshift asymmetries in groups

In this subsection we use our mock catalogues to study and explain the observed redshift asymmetries. However, before that, we discuss the suitability of our mock catalogues and quantify the methods of calculating the redshift asymmetries.

The Mock1 catalogue has been generated with the same parameters as the original HG82 catalogue, from which S84 found positive redshift excess. Because of this it is most suitable for this study and for the comparison of redshift excesses found in S84. Mock1 is also favoured because a redshift excess is most noticeable for nearby groups for which there is a larger distance ratio between the background and the foreground galaxies. Mock2 is used to provide better statistics and for comparison. Note, however, that Mock2 probes groups deeper in redshift space than Mock1, and therefore the total effect of nearby groups is not as strong. It is also noteworthy that in this subsection we study small groups, therefore we limit the number of group members to less than 11 (i.e. \(2 < n < 10\)).

Both mock catalogues have been generated from the Millennium Simulation. Even though the Millennium run provides reliable statistics its mass resolution is only \(\sim 10^9 M_\odot\). This complicates the matter of identifying low mass groups with at least three members inside. The low mass resolution might have a large effect on studies of the abundance or space density of individual objects. An even greater effect would be noticed if one was interested in subhalo properties or abundances. However, as our purpose is to study the relative location and distribution of galaxies inside groups, we do not consider the low mass resolution as a significant problem. Further, Sect. 3.1 showed that the abundance of low mass groups in the Millennium Simulation is comparable to observational catalogues. This ensures that the mass resolution is good enough for a statistical study like ours, especially as in a statistical sense missing dwarf galaxies could reside anywhere inside the dark matter halo.

We calculate redshift asymmetries both on a group and on a galaxy level. On a group level we use groups from five different observation points and calculate the sum of groups with redshift/blueshift excess in each point. The redshift or the blueshift excess percentage shown is the mean value of the excesses from the five observation points when ties have been removed. The error limits are standard deviation errors between five observation points. When the redshift asymmetries are studied on a member galaxy level, we quantify the redshift excess as in Byrd & Valtonen (1985):

\[
Z = \frac{N_B - N_R}{N_B + N_R},
\]

where \(N_B\) is the number of galaxies having a redshift lower than the apparently brightest group member and \(N_R\) is the number of galaxies having a redshift higher than the apparently brightest group member.

Table 3 shows a general comparison of the mock catalogues and samples from S84 when the asymmetries have been calculated on a group level. Mock catalogues show a (weak) positive redshift excess when spiral-dominated (i.e. the central galaxy is a spiral galaxy) groups are studied. However, the excess is not significant for elliptical (E or S0) dominated groups. These groups actually show a small blueshift excess, similar to S84. By conventional theory, this suggests that these groups could be mostly gravitationally bound. However, we find that \(\sim 35.0 \pm 10.0 (27.4 \pm 1.3)\) per cent of E/S0-dominated groups in Mock1 (Mock2) are gravitationally unbound. This suggests that the absence of redshift asymmetry does not alone guarantee that these groups are gravitationally bound systems.

Table 4 further divides the mock catalogues to subsamples on the basis of whether the groups are gravitationally bound or not. The unbound groups are important, since about one half of all groups in both of our mock catalogues belong to this category. A further division in Table 4 is made on the basis of whether the dominant galaxy is correctly identified, i.e. whether the brightest, in apparent magnitudes group member is also the most massive galaxy in the group. A large and statistically highly significant redshift excess appears only in those subsamples where the groups are gravitationally unbound, and in addition, their dominant galaxies have been misidentified. These comprise approximately one quarter of all groups. The excess appears both among
Table 3. A general comparison of the mock catalogues and samples from S84.

| Sample                        | n_G | n_{Δz} | n_{−Δz} | Δz (%) | −Δz (%) | ±Δz (%) |
|-------------------------------|-----|---------|----------|--------|---------|---------|
| S84, all groups (n ≤ 10)      | 85  | 42      | 32       | 11     | 57.0    | 43.0    | 12.9    |
| S84, E/S0 dominant groups     | 60  | 33      | 18       | 9      | 65.0    | 35.0    | 15.0    |
| S84, E/S0 dominant groups     | 21  | 9       | 10       | 2      | 47.0    | 53.0    | 9.5     |
| Mock1, all groups (n ≤ 10)    | 1384| 622     | 505      | 257    | 55.2 ± 5.1| 44.8 ± 5.1| 18.6 ± 1.9|
| Mock1, spiral (T ≥ 0.92)      | 1153| 528     | 408      | 217    | 56.4 ± 5.6| 43.6 ± 5.6| 18.8 ± 2.4|
| Mock1, E/S0 (T < 0.92)        | 231 | 94      | 97       | 40     | 49.2 ± 6.9| 50.8 ± 6.9| 17.3 ± 4.2|
| Mock2, all groups (n ≤ 10)    | 12100| 5087   | 4658     | 2355   | 52.2 ± 1.3| 47.8 ± 1.3| 19.5 ± 0.6|
| Mock2, spiral (T ≥ 0.92)      | 9086| 3854    | 3466     | 1748   | 52.5 ± 1.8| 47.3 ± 1.6| 19.2 ± 0.8|
| Mock2, E/S0 (T < 0.92)        | 3013| 1179    | 1227     | 607    | 49.0 ± 1.8| 51.0 ± 1.8| 20.1 ± 2.0|

Note: Sample refers either to S84, Mock1 or Mock2 catalogues, n_G is the number of groups, n_{Δz} is the number of groups with positive redshift excess, n_{−Δz} is the number of groups with no excess, Δz (%) is the number of groups with no excess, ±Δz (%) is the percentage of groups with positive redshift excess when ties have been removed, −Δz (%) is the percentage of groups with negative redshift excess when ties have been removed and ±Δz is the percentage of groups having equal number of negative and positive redshifts. Errors for mock catalogues are standard deviation errors between five different observation points.

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galaxy level, we see similar results as in Tables 3 and 4. No
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erred, the redshift excess is only 0
When only bound groups from Mock1 (Mock2) are consid-
erned, the redshift excess is only 0.03 depending on the parameters adopted, while the most probable value was 0.2. The good agreement between observations, analytical models and simulations is reasonable. This points to the possibility that E/S0 galaxies do mark the position of the group centre correctly.

Table 4 also shows that groups that are gravitationally bound show larger error limits for redshift asymmetries than groups which are unbound, suggesting that there are large differences in the fraction of bound groups between our five observation points. This result shows that projection effects can play a significant role when the FoF percolation algorithm is applied, and that it can produce groups which are spurious because of these projection effects. It also shows that the choice of free parameters can affect the results, as the Mock2 catalogue does not show larger errors for bound groups in comparison to unbound ones.

When redshift asymmetries are studied at a member galaxy level, the results stay similar. If we consider only spiral-dominated groups which are unbound and whose centre is wrongly identified, we find a redshift excess of Z = 0.22 and Z = 0.10 for the Mock1 and Mock2 catalogues, respectively. When only bound groups from Mock1 (Mock2) are considered, the redshift excess is only 0.07 (0.04). The former values are similar to observed ones, as S84 found a redshift excess of Z = 0.21 for spiral-dominated (i.e. the apparently brightest galaxy is a spiral galaxy) groups. Byrd & Valtonen (1985) and Valtonen & Byrd (1986) derived values of the redshift excess from an analytical model that ranges from Z = 0.1 to Z = 0.5 depending on the parameters adopted, while the most probable value was 0.2. The good agreement between observations, analytical models and simulations (unbound and wrongly identified groups) suggests that most of the membership of H82’s spiral-dominated groups is unbound and that the centre has been misidentified for these groups. Simulations further show that to obtain as high a redshift excess as observed, we have to select groups that are gravitationally unbound and whose centre has been misidentified.

If we concentrate on E/S0-dominant groups at a member galaxy level, we see similar results as in Tables 3 and 4. Now Mock1 (Mock2) shows a blueshift excess of Z = −0.05 (Z = −0.01) for gravitationally unbound groups, whose central galaxies are correctly identified. This is a slightly weaker blueshift excess than S84 found (−0.13), but comparable. These values are in agreement with the analytical calculations of Byrd & Valtonen (1985) and Valtonen & Byrd (1986) that showed the blueshift excess of correctly identified, but unbound E-dominated groups ranging from Z = −0.13 to Z = 0.03 depending on the values of free parameters. Here the agreement between observations, analytical models and simulations is reasonable. This points to the possibility that E/S0 galaxies also mark the position of the group centre correctly.

Table 4 shows that E/S0 galaxies mark the position of the centre correctly more often than spiral galaxies. If we calculate the percentage of groups whose dominant member has been correctly identified it is clear that ~73.9 per cent of E/S0-dominated groups are correctly identified while as much as ~60.0 per cent of spiral-dominant groups are incorrectly identified. The incorrect identification of the central galaxy is important as it may lead to a redshift excess, since it is more likely that the apparently brightest galaxy is in the front part of the cluster than in the back part of it. The galaxies in the front part of the group appear brighter, and in the back part of the group fainter than what their absolute magnitudes would lead us to expect, i.e. compared with the situation when they all are at the same distance from us. This greater apparent brightness of the group members in the front makes it also more likely that the actually brightest member is picked from the front volume of the group. Statistically this applies to groups of all sizes. In a gravitationally bound group this would not in itself cause a redshift excess, but if the whole group or a substantial part of it is in Hubble flow, then the galaxies in front are typically blueshifted while the galaxies in the back are redshifted relative to the apparently brightest galaxy.

To further test the cause of redshift asymmetries we use absolute B-band magnitudes rather than apparent ones to identify the dominant group member and calculate the redshift asymmetries in this case. The use of absolute magnitudes leads to a small blueshift excess for all groups. The blueshift excess is highest for unbound, spiral-dominated and misidentified groups, being ~56 ± 1.5 per cent (Z ~ −0.06). For all gravitationally bound groups we find a small blueshift excess of ~52.5 ± 2.5 (Z ~ −0.02). This small and hardly significant blueshift excess is expected and is due to the fact that magnitude limited observations will miss faint members from the back part of the group with higher probability than from the front part. Additionally, if the group is expanding (unbound) it can further lead to a case where the group is missing redshifted members. A small blueshift excess is also present if we consider only groups that are correctly identified.

Although the redshift excess disappears when using absolute B-band magnitudes, it does not lead to a significantly smaller number of misidentifications as the fraction remains roughly the same as in the case of apparent magnitudes. The percentage of
misidentifications for all galaxies in the case of apparent magnitudes for Mock2 is $\pm 5.6 \pm 1.7\%$ while it is $\pm 5.1 \pm 1.8\%$ in the case of absolute magnitudes. This result is due to the fact that both B-band magnitudes are a poor indicator of the most massive galaxy as they tend to favour spiral galaxies over elliptical ones.

### 4. Summary and conclusions

In this paper we have compared cosmological N-body simulations to observations. We have studied fractions of unbound groups, redshift asymmetries and their connection. We have found an explanation for the positive redshift excess found by many authors from different observational group catalogues.

Our mock catalogues of groups of galaxies are in reasonable agreement (in general, within 2\(\sigma\)) with observational catalogues when dynamical properties of groups are studied. Both mock catalogues show a significant fraction of gravitationally unbound groups, independent of the choices of free parameter values in the Friends-of-Friends algorithm. Even though the density enhancement of the Mock2 catalogue is more than three times higher than the density enhancement of Mock1, we found that both mock catalogues contain roughly 50% gravitationally unbound groups. Even though the density enhancement does not have a significant effect on the fraction of gravitationally bound groups, the values of free parameters of the FoF algorithm have an effect on group properties. Our results show that the value of \(V_0\) has an effect on the abundance of high velocity groups. This is an expected result as a higher \(V_0\) value gives the percolation algorithm more room in redshift space leading to a higher number of high velocity dispersion groups.

Mock catalogues produce similar redshift asymmetries as found in observations. The Mock1 catalogue produces higher redshift asymmetries than Mock2 in all cases, because the redshift asymmetries are most noticeable for nearby groups for which there is a larger distance ratio between the background and the foreground galaxies. The redshift excess is similar to observations for groups that are gravitationally unbound and in which, at the same time, the apparently brightest galaxy is in the front part of the cluster than in the back part of it. The galaxies in the front part of the group appear brighter, and in the back part of the

### Table 4. A detailed view of the redshift asymmetries in mock catalogues.

| Sample | \(n_G\) | \(n_{\Delta z}\) | \(n_{\Delta z}\) | \(n_{\Delta z}\) | \(\Delta z\) (%) | \(-\Delta z\) (%) | \(\pm \Delta z\) (%) |
|--------|--------|----------------|----------------|----------------|----------------|----------------|----------------|
| Mock1, gravitationally bound groups | | | | | | | |
| all groups (n ≤ 10) | 675 | 282 | 259 | 134 | 50.5 ± 10.1 | 49.5 ± 10.1 | 19.9 ± 2.5 |
| spiral (T ≥ 0.92) dominant groups | 537 | 231 | 199 | 107 | 52.4 ± 10.6 | 47.6 ± 10.6 | 19.9 ± 2.7 |
| E/S0 (T < 0.92) dominant groups | 138 | 51 | 60 | 27 | 46.0 ± 16.0 | 54.1 ± 16.0 | 19.6 ± 4.4 |
| Mock1, gravitationally unbound groups | | | | | | | |
| all groups (n ≤ 10) | 709 | 340 | 246 | 123 | 58.3 ± 2.9 | 41.7 ± 2.9 | 17.3 ± 2.2 |
| spiral (T ≥ 0.92) dominant groups | 616 | 297 | 209 | 110 | 59.0 ± 3.2 | 41.0 ± 3.2 | 17.9 ± 2.8 |
| E/S0 (T < 0.92) dominant groups | 93 | 43 | 37 | 13 | 54.1 ± 7.1 | 45.9 ± 7.1 | 14.0 ± 8.5 |
| Mock1, bound, wrongly identified | | | | | | | |
| all groups (n ≤ 10) | 289 | 142 | 110 | 37 | 56.3 ± 12.9 | 43.7 ± 12.9 | 12.8 ± 4.2 |
| spiral (T ≥ 0.92) dominant groups | 257 | 129 | 95 | 33 | 57.6 ± 12.8 | 42.4 ± 12.8 | 12.8 ± 3.7 |
| E/S0 (T < 0.92) dominant groups | 32 | 13 | 15 | 4 | 46.4 ± 18.2 | 53.6 ± 18.2 | 12.5 ± 12.0 |
| Mock1, gravitationally unbound groups | | | | | | | |
| all groups (n ≤ 10) | 338 | 193 | 96 | 49 | 66.8 ± 3.8 | 33.2 ± 3.8 | 14.5 ± 4.6 |
| spiral (T ≥ 0.92) dominant groups | 297 | 171 | 83 | 43 | 67.6 ± 3.5 | 32.4 ± 3.5 | 14.5 ± 4.8 |
| E/S0 (T < 0.92) dominant groups | 41 | 22 | 13 | 6 | 62.9 ± 9.7 | 37.1 ± 9.7 | 14.6 ± 9.9 |
| Mock2, gravitationally bound groups | | | | | | | |
| all groups (n ≤ 10) | 5175 | 2327 | 2124 | 1174 | 51.3 ± 1.7 | 48.7 ± 1.7 | 20.5 ± 0.7 |
| spiral (T ≥ 0.92) dominant groups | 3649 | 1515 | 1386 | 748 | 52.3 ± 2.9 | 47.7 ± 2.9 | 20.5 ± 1.2 |
| E/S0 (T < 0.92) dominant groups | 2066 | 801 | 839 | 426 | 48.8 ± 2.2 | 51.2 ± 2.2 | 20.6 ± 2.5 |
| Mock2, gravitationally unbound groups | | | | | | | |
| all groups (n ≤ 10) | 6385 | 2760 | 2444 | 1181 | 52.9 ± 1.6 | 47.1 ± 1.6 | 18.5 ± 0.9 |
| spiral (T ≥ 0.92) dominant groups | 5437 | 2357 | 2080 | 1000 | 53.0 ± 1.7 | 47.0 ± 1.7 | 18.4 ± 1.1 |
| E/S0 (T < 0.92) dominant groups | 947 | 402 | 364 | 181 | 52.4 ± 2.8 | 47.6 ± 2.8 | 19.1 ± 1.7 |
| Mock2, bound, wrongly identified | | | | | | | |
| all groups (n ≤ 10) | 2618 | 1193 | 1028 | 397 | 53.7 ± 2.2 | 46.3 ± 2.2 | 15.2 ± 0.7 |
| spiral (T ≥ 0.92) dominant groups | 2151 | 980 | 840 | 331 | 53.8 ± 2.7 | 46.2 ± 2.7 | 15.4 ± 1.0 |
| E/S0 (T < 0.92) dominant groups | 467 | 213 | 188 | 66 | 53.1 ± 1.7 | 46.9 ± 1.7 | 14.1 ± 3.4 |
| Mock2, unbound, wrongly identified | | | | | | | |
| all groups (n ≤ 10) | 3591 | 1661 | 1379 | 551 | 54.6 ± 1.9 | 45.4 ± 1.9 | 15.3 ± 1.3 |
| spiral (T ≥ 0.92) dominant groups | 3291 | 1535 | 1260 | 496 | 54.8 ± 2.0 | 45.2 ± 2.0 | 15.1 ± 1.4 |
| E/S0 (T < 0.92) dominant groups | 300 | 126 | 119 | 55 | 51.4 ± 5.6 | 48.6 ± 5.6 | 18.3 ± 4.1 |

Note: Sample is the subsample of the mock catalogue, \(n_G\) is the number of groups, \(n_{\Delta z}\) is the number of groups with positive redshift excess, \(n_{\Delta z}\) is the number of groups with negative redshift excess, \(n_{\Delta z}\) is the number of groups with no excess, \(+\Delta z\) is the percentage of groups with positive redshift excess when ties have been removed, \(-\Delta z\) is the percentage of groups with negative redshift excess when ties have been removed, \(\pm \Delta z\) is the percentage of groups having equal number of negative and positive redshifts. Errors for mock catalogues are standard deviation errors between five different observation points.
group fainter than what their absolute magnitudes would lead us to expect, i.e. compared with the situation when they all are at the same distance vector.

The use of absolute $B$-band magnitudes does not lead to a redshift excess; however, a small blueshift excess is present. This is due to the fact that magnitude limited observations miss faint group members from the back rather than from the front part of the group. Despite the lack of redshift excess, the fraction of groups in which the dominant group member has been incorrectly identified remains as we observe roughly the same number of misidentified groups (∼52 per cent) as in the case of apparent magnitudes when all groups from Mock2 are considered. Thus, absolute and apparent $B$-band magnitude is a poor indicator of the dominant member in a group. Our results also show that the E/S0 galaxies tend to mark the group centre correctly, as ∼75 per cent of E/S0-dominated groups have been correctly identified. These groups do not show significant redshift excess in any case.

Gravitationally bound groups do not show any significant redshift excess. This is in agreement with conventional theory, where it is expected that distribution of redshift differentials should be evenly distributed. The subsample of the Mock1 catalogue that includes only gravitationally bound groups has an equal number of galaxies relative to the brightest member within any case.

We conclude that when the group centre is not correctly identified, it may cause the major part of the observed redshift excess. If the group is also gravitationally unbound, the level of the redshift excess becomes as high as in S84. Thus the explanation of the group is also gravitationally unbound, the level of the redshift excess is verified. It further means that there is no need to introduce any “anomalous” redshift mechanism to explain the redshift excess of Arp (1970).

This paper shows that the Friends-of-Friends percolation algorithm picks out the expanding parts of the groups, in addition to the gravitationally bound group cores. Thus the group catalogues constructed in this way cannot be used as if the groups are purely bound systems. For example, the use of the virial theorem to estimate group masses easily leads to wrong answers. As about 50 per cent of groups in our mock catalogues are bound, in principle one could apply the virial theorem only to this subclass of groups, but then it is difficult to identify this subclass in observations. The redshift excess in a sample of groups would tell us readily that there must be many unbound groups in the sample. However, the absence of redshift excess alone does not guarantee that these groups are gravitationally bound systems.

To overcome the difficulty of finding gravitationally bound groups, one can, for example, use stellar mass rather than luminosity for identifying the central galaxy. Even then dark matter and the lack of knowledge of relative distances inside observed groups complicates matters. If the grouping algorithm concentrates on finding satellite galaxies that belong to the same dark matter halo (see Yang et al. 2007), it could return groupings that are mainly gravitationally bound. Detection of extended X-ray radiation can also indicate gravitationally bound groups.

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