Decrease of heavy-hole exciton mass induced by uniaxial stress in GaAs/AlGaAs quantum well

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It is experimentally shown that the pressure applied along the twofold symmetry axis of a heterostructure with a wide GaAs/AlGaAs quantum well leads to considerable modification of the polariton reflectance spectra. This effect is treated as the stress-induced decrease of the heavy-hole exciton mass. Theoretical modeling of the effect supports this assumption. The 5%-decrease of the exciton mass is obtained at pressure $P = 0.23$ GPa.

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INTRODUCTION

In a number of structures like topological insulators,1,2 superconductors3,4 and graphen,5,6 the dispersion of the electron and hole energy near the $\Gamma$-point has a form of the Dirac cone that corresponds to the massless charged carriers. The time-reversal or spontaneous spatial symmetry breaking is capable, however, to make the charge carriers in these semiconductors massive (see, e.g., Refs. 1, 3, and 6). The generated carrier mass is described by the nondiagonal terms of the Dirac Hamiltonian which are independent of wave vector $k$ of the carrier. In Ref. 1, this mass is called as “Dirac” in order to distinguish it from the mass described by the matrix elements depending on $k^2$. The latter is called as “Newtonian” in the cited work.

Dirac mechanisms of the mass generation have been mainly discussed for the two-dimensional and one-dimensional semiconductors with the dominant linear over $k$ terms in the carrier Hamiltonian. At the same time, in the bulk semiconductors and heterostructures where the carriers are described by a Hamiltonian with the dominant quadratic over $k$ terms, the generation of additions to the effective mass is also possible due to mechanisms similar to the Dirac ones. For example, in the topological crystalline insulators, the carrier energy quadratically depends on wave vector $k$ though the band gap is close to zero.7,8 Any small change of crystal symmetry gives rise to the appearance of an energy gap and, as a consequence, to the change of carrier effective masses.

In a bulk GaAs crystal, the exciton energy dispersion law is quadratic in wave vector too. When an uniaxial stress is applied along axis $[100]$ to the GaAs crystal, the change (convergence) of masses of the heavy- and light-hole excitons should be observed as it was theoretically predicted in Ref. 9. A formal description of this effect is similar to the description of the Dirac mechanism of the carrier mass generation in topological insulators and superconductors because it is described by the nondiagonal Hamiltonian matrix elements independent of $k$.

Present work is devoted to the theoretical and experimental studies of the mass convergence effect in polariton reflectance spectra of a wide quantum well (QW) in the presence of a uniaxial stress applied along $[110]$ axis. From the experimental point of view, this direction is convenient because it is perpendicular to the cleavage plane of the sample, which coincides with the crystal plane $(110)$. Therefore, the pressure along this direction prevents unwanted breakup of the sample. Theoretical consideration of the pressure effect is similar to that performed in Ref. 9 for the pressure applied along the $[100]$ axis.

I. EXCITON HAMILTONIAN IN THE STRESS FIELD

We consider an exciton in a crystal with the zinc blende symmetry propagating along the $Z$ axis axis ($[001]$ crystal axis). This direction will be regarded as the axis of the carrier’s angular momentum quantization.

Exciton states observed in optical experiments with the GaAs semiconductors are formed by the states of the twofold-degenerate conduction band $\Gamma_6$ and fourfold-degenerate valence band $\Gamma_8$. Wave functions of electrons and holes in this approximation are represented by the two-component and four-component plane waves,10 respectively.

In the present work, we neglect the effects related to the corrugation of valence band10 since they are small and do not directly affect the discussed phenomenon. By the same reason we ignore small effects of the exchange coupling of exciton states, of the nonparabolicity of exciton dispersion and of the coupling of the ground and excited exciton states.11

The energy of an exciton moving in an unstrained crystal is:10

$$H_{X,h,l}^{(0)} = E_X + \frac{\hbar^2 K^2}{2M_{h,l}},$$

(1)
where $E_X = E_0 - R_X$ is the energy of the exciton ground state. Here $E_0$ is the band gap and $R_X$ is the exciton binding energy (Rydberg), $K = K_x$ is the exciton wave vector. Hereafter we assume that $K_x = K_y = 0$ that is the exciton propagates along the $z$-axis. The translational masses of the heavy-hole (denoted by index “$h$”) and light-hole (denoted by index “$l$”) excitons are defined by expressions:

$$M_h = m_e + m_h,$$

and

$$M_l = m_e + m_l.$$

Here $m_e$ is the electron effective mass, $m_{hl} = m_0(1/2\gamma_1 + 1/2\gamma_2)$ is the effective masses of a heavy (sign “$+$”) mass and light (sign “$-$”) holes, $\gamma_1$ and $\gamma_2$ are the Luttinger parameters, $m_0$ is a mass of a free electron.

In the framework of approximations introduced above, the Hamiltonian of the exciton moving in the unstrained crystal, according to Ref. 10, may be written as the $8 \times 8$ matrix, consisting of two identical diagonal blocks of the size $4 \times 4$, which nonzero elements has form (1). The first of these blocks describes optically active exciton states with projections of the exciton spin $J_z = \pm 1$, whereas the second one represents optically inactive states with projections $\pm 2$ and 0 for heavy and light excitons, respectively.

Basis wave functions of such Hamiltonian taking into account the spin moment of exciton are written as:

$$|j, s\rangle_K = \nu_{j, s}\Psi(K),$$

where $\nu_{j, s}$ is the eight-component spinor with one non-zero component equal unity: $j = \pm 3/2, \pm 1/2$ and $s = \pm 1/2$ are the projections of the spin moments of the hole and the electron, respectively, to the selected axis; $\Psi(K)$ is the coordinate part of the wave function.

Let us now consider the impact of the uniaxial stress $P$ applied along axis [110] on the exciton states. Components of the strain tensor are described by following expressions:

$$\varepsilon_{xx} = \varepsilon_{yy} = -(S_{11} + S_{12})\frac{1}{2} P, \ \varepsilon_{zz} = -S_{12} P,$$

$$\varepsilon_{xy} = -S_{44}\frac{1}{2} P, \ \varepsilon_{xz} = \varepsilon_{yz} = 0,$$

where $S_{11}$, $S_{12}$, $S_{44}$ are components of the elastic compliance tensor. Such strain, particularly, leads to the effect, which is described by the linear over the wave vector additive terms in the electron-hole Hamiltonians. In the case under consideration, these additive terms lead to coupling of the exciton 1s- and np-states and, as a consequence, to the change of the exciton binding energy. Nevertheless, this change is small compared to the effects discussed hereafter. Therefore, we do not consider it in present work.

The most remarkable effect of crystal strain is the alteration of valence band $\Gamma_8$, which is described by the Bir-Pikus Hamiltonian. This Hamiltonian does not couple optically active states, $|j, s\rangle = |\pm 3/2, \mp 1/2\rangle, |\pm 1/2, \pm 1/2\rangle$, with optically inactive states, $|j, s\rangle = |\pm 3/2, \pm 1/2\rangle, | \pm 1/2, \mp 1/2\rangle$. To simplify our analysis, we turn from exciton basis (2) to a new representation using following formulas:

$$|j\alpha\rangle = \frac{1}{\sqrt{2}}[3/2, -1/2] \pm \frac{i}{\sqrt{2}}|3/2, 1/2\rangle,$$

$$|l\alpha\rangle = \frac{1}{\sqrt{2}}[1/2, 1/2] \pm \frac{i}{\sqrt{2}}|1/2, -1/2\rangle.$$  

Here the upper and lower signs correspond to indexes $\alpha = x' \pm y'$, respectively. These states can be excited by the light polarized along axes [110] and [110], which are the axes of optical anisotropy in the presence of the uniaxial stress.

A matrix of the total exciton Hamiltonian constructed using these wave functions is composed of two blocks:

$$\hat{H}_X = \begin{pmatrix} H_{h\alpha} & V \\ V^* & H_{l\alpha} \end{pmatrix},$$

where $\alpha = x', y'$. (5)

Here

$$H_{h\alpha} = H_{h\alpha} = H_{h\alpha} = H_{h\alpha} = H_{h\alpha} = H_{h\alpha} = H_{h\alpha} = H_{h\alpha},$$

$$H_{l\alpha} = H_{l\alpha} = H_{l\alpha} = H_{l\alpha} = H_{l\alpha} = H_{l\alpha} = H_{l\alpha} = H_{l\alpha},$$

$$V = iqS_{44}\frac{P}{4},$$

where $a, b,$ and $d$ are the strain potentials. Since the states corresponding to $\alpha = x'$ and $\alpha = y'$ are decoupled, the problem for each such block can be solved independently.

We should note here that the uniaxial stress also leads to a coupling of the light-hole states and states of the split-off valence band, which is resulted in an alteration of the light-hole mass. We have found, however, that respective energy shifts of the exciton states caused by this coupling are small in comparison to those due to the heavy-hole and light-hole coupling. Therefore, we do not consider this effect in what follows.

The nondiagonal elements $V$ in Hamiltonian (5) describes the effect of the mass convergence stipulated by coupling of the heavy-hole and light-hole excitons. The effect is observed in optical spectra of a heterostructure with the wide QWs. To model these spectra one needs to take into account the impact of the mass convergence effect on the dielectric properties of medium.

II. PERMITTIVITY IN THE PRESENCE OF UNIAXIAL STRESS

For analysis of the reflectance spectra with taking the pressure-induced effects into account, we employ a model of the polariton wave interference in a wide QW described, e.g., in Refs. 15–17. It is supposed that the incident light is directed along the normal to the sample surface and linearly polarized along one of the optical anisotropy axes.
The exciton-photon interaction is described by the perturbation operator (see, e.g., Ref. 18):

\[ V_d = -(d_h + d_l)E^{(a)}, \quad (a = x', y') \]  

where \( E^{(a)} \) is the electric field of a light wave and \( d_{h,l} \) is the matrix elements of a dipole moment for the heavy-hole and light-hole exciton. The square of the matrix elements can be expressed as: \( d_h^2 = 3d_l^2 = \hbar \omega_{LT} \epsilon_0 \Omega \), where \( \hbar \omega_{LT} \) is the energy of the longitudinal-transverse splitting, \( \epsilon_0 \) is the background permittivity and \( \Omega \) is the crystal volume.

The wave function of a polariton is a linear combination of the “pure” exciton wave functions (4):

\[ \Psi_\alpha(K) = C_{vac}|vac\rangle + \sum_{\beta=h,l} C_{\beta\alpha}|\beta\rangle \]  

where \( C_{\beta\alpha} \) are the expansion coefficients and \( |vac\rangle \) is the crystal vacuum state.

Dispersion relations, wave functions and permittivity in the case of exciton-photon interaction can be obtained using the method proposed in Refs. 9 and 18. To this end, one should first solve a system of equations for energies of the heavy-hole and light-hole excitons taking into account interaction (6):

\[ (\mathbb{H} - \hbar \omega) \cdot C = \begin{pmatrix} H_{h\alpha} - \hbar \omega & V & -d_h E^{(a)} \\ V^* & H_{l\alpha} - \hbar \omega & -d_l E^{(a)} \\ -d_h E^{(a)} & -d_l E^{(a)} & H_{vac} - \hbar \omega \end{pmatrix} \cdot \begin{pmatrix} C_{h\alpha} \\ C_{l\alpha} \\ C_{vac} \end{pmatrix} = 0. \]  

Here \( H_{vac} = 0 \) is the energy of the vacuum state and \( \hbar \omega \) is the photon energy. The expansion coefficients \( C_{\alpha} \) are easily found from the first two lines of this matrix equation if one assumes that the optical excitation is very weak, therefore, \( C_{vac} \approx 1 \).

The exciton-photon interaction leads also to a resonant polarization of medium, which depends on the exciton wave vector. This polarization is described by the expression: \( \epsilon_\alpha(x', y') = \epsilon_0 + 4\pi \chi_\alpha(x', y') \).

Here \( 4\pi \chi_\alpha \) are contributions to the optical susceptibility at the heavy-hole and light-hole exciton resonances, respectively. From formulae (8) and (9) one can come to relations for \( \chi_{h,l} \): \( 4\pi \chi_{h\alpha} = \frac{\tilde{H}_{l\alpha} \hbar \omega_{LT}}{\tilde{H}_{l\alpha} \hbar_{l\alpha} - |V|^2} \pm \frac{1}{\sqrt{3}} \frac{V \hbar \omega_{LT}}{\tilde{H}_{l\alpha} H_{l\alpha} - |V|^2} \) \( 4\pi \chi_{l\alpha} = \frac{1}{3} \frac{\tilde{H}_{l\alpha} \hbar \omega_{LT}}{\tilde{H}_{l\alpha} \hbar_{l\alpha} - |V|^2} \pm \frac{1}{\sqrt{3}} \frac{V \hbar \omega_{LT}}{\tilde{H}_{l\alpha} H_{l\alpha} - |V|^2} \).

Here

\[ \tilde{H}_{l,h\alpha} = H_{l,h\alpha} - \hbar \omega + i \Gamma_{h,l}, \]

where \( \Gamma_{h,l} \) is a phenomenological parameter introduced to describe processes of energy dissipation. The upper and lower signs in relation (10) correspond to the light polarization along the \( x' \) and \( y' \) axes.

One should also keep in mind that, even in the absence of exciton resonances, the uniaxial stress leads to an optical anisotropy of crystal due to the piezo-optic effect. This effect leads to an additional background permittivity, which, in the basis of light waves polarized along \( x' \) and \( y' \) axes, is described as:\( 20,21 \)

\[ -\delta \epsilon_{x'} = \delta \epsilon_{y'} = \pi_{44} P \equiv \delta \epsilon, \]  

where \( \pi_{44} \) is the component of the piezo-optic tensor.

The total permittivity of medium with account of contributions (10) and (11) has the form:

\[ \epsilon_\alpha(x', K) = \epsilon_0 \pm \delta \epsilon + 4\pi \chi_{h\alpha} + 4\pi \chi_{l\alpha}, \quad (\alpha = x', y'). \]  

In order to obtain dispersion relations for polariton eigenmodes, one should solve the following dispersion equation:\( 22 \)

\[ \epsilon_\alpha(x', K) = \frac{\epsilon_0^2 K^2}{\omega^2}, \]  

where \( c \) is the light velocity and \( \epsilon_\alpha(x', K) \) is described by expression (12). Equation (13) has independent solutions for \( \alpha = x' \) and \( \alpha = y' \), which correspond to two linear polarizations of the incident light. For each polarization, the equation is a polynomial of the third order over \( K^2 \). Its solutions are the eigenmodes, which differ from each other by the primary contribution of either the light component (photon-like, \( p \)-type dispersion branch) or states of the heavy-hole or light-hole exciton (\( h \)- or \( l \)-type exciton branch, respectively).

Figure 1 shows the dispersion curves for polariton eigenmodes calculated for strained and unstrained GaAs crystal. The following material parameters were used: \( \hbar \omega_{LT} = 0.08 \text{ meV}, \epsilon_0 = 12.56, m_0 = 0.067 m_0, \gamma_1 = 6.8, \gamma_2 = 2.3, E_g = 1520 \text{ meV}, S_{11} = 1.172 \cdot 10^{-2} \text{ cm}^2/\text{dyn}, S_{12} = -0.365 \cdot 10^{-2} \text{ cm}^2/\text{dyn}, S_{44} = 1.68 \cdot 10^{-2} \text{ cm}^2/\text{dyn}, \) \( \pi_{44} = 1.5 \text{ GPa} \) and \( d = -4.55 \text{ eV}, a = -6.7 \text{ eV}, b = -1.7 \text{ eV}. \)  

The deformation leads to reduction of the GaAs crystal symmetry from \( T_d \) to \( D_{2d} \). Therefore, the dispersion
curves of the exciton-like modes of $h$- and $l$-types are shifted to higher energies due to the diagonal terms of Hamiltonian (8). The $l$-type mode is shifted stronger so it becomes higher than the $h$-type mode.

The dispersion curves are additionally splitted due to their coupling described by the nondiagonal matrix elements $V$ of Hamiltonian (8). As it is seen in Fig. 1, the dispersion branch for the $h$-type polaritons becomes steeper at pressure $P = 0.23$ GPa. This behavior is equivalent to the mass reduction of the $h$-type polaritons. At the same time, the dispersion curve of $l$-type becomes flatter, which is equivalent to an increase of polariton mass. In the first approximation, this effect can be described as the convergence of effective masses of the $h$- and $l$-types polaritons.

It should be pointed out that perturbation $V$ acts similar to a perturbation in the Hamiltonians of an electron and a hole in the topological insulators, superconducting condensate and topological crystalline insulators describing the Dirac mass generation mechanism for massless particles.
heavy-hole exciton are compared. For more precise comparison with experiment we have used different damping parameters for the non-stressed and stressed QW: $\Gamma_k = 0.07 \text{ meV}$, $\Gamma_l = 0.35 \text{ meV}$ for $P = 0$ and $\Gamma_l = 0.27 \text{ meV}$, $\Gamma_l = 0.55 \text{ meV}$ for $P = 0.23 \text{ GPa}$. The possible reason for the increase of peak broadening with pressure is some inhomogeneity of the pressure. It should be also noted, that the damping parameter for the light-hole exciton is larger than that for the heavy-hole one, that is typically observed in experiment (see, Fig. 2(a) and Ref. 17).

There is noticeable difference in general behavior of experimental and simulated spectra. We attribute this difference to the complex layer structure of the sample under study containing many technological layers. It is well known (see, e.g., Ref. 15) that the interference of light waves reflected from different layers may result in slow spectral modulation of reflectance. We ignore this effect in the simulation for simplicity and consider here the behavior of the spectral oscillations, which contains valuable information on the polariton dispersion. The calculations show that the observed spectral oscillations are mainly caused by the contribution from the $h$-type modes. The contribution of the $l$-type modes for $K \gg q$ is negligibly small due to the smaller oscillator strength as well as the significantly larger inhomogeneous broadening.

The calculated spectra well reproduce overall behavior of the spectral oscillations observed experimentally (see Fig. 3). In particular, the enlargement of energy distance between the oscillations in the stressed QW is reproduced. The increase of the oscillation quasiperiod indicates a decrease of the effective mass $M_h$ of the heavy-hole exciton. This decrease at $P = 0.23 \text{ GPa}$ is not small:

$\Delta M_h = 0.026 \times m_0$ which is of about 5% of initial exciton mass.

IV. CONCLUSIONS

We have theoretically and experimentally studied the impact of uniaxial mechanic stress applied along the second order symmetry axis on the polariton reflectance spectra of the heterostructure with a wide GaAs/AlGaAs QW. It was shown that the applied stress leads to the decrease of effective mass of the heavy-hole exciton. In the reflectance spectra, this effect manifests itself in the increase of relative energy distance between the spectral oscillations caused by the interference of photon-like and exciton-like polariton waves in the QW. The observed phenomenon is due to the stress-induced coupling of the heavy-hole and light-hole exciton states. The coupling is described by the Bir-Pikus Hamiltonian and has some
similarity with the Dirac mass generation mechanism for massless carriers in topological insulators and superconducting condensate. The analysis of spectral oscillations shows a good agreement of the theory with the experiment.

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1. X.-L. Qi and S.-C. Zhang, Topological insulators and superconductors, Rev. Mod. Phys. 83, 1057 (2011).
2. J. C. Budich, B. Trauzettel and P. Michetti, Time reversal symmetric topological exciton condensate in bilayer HgTe quantum wells, Phys. Rev. Lett 112, 146405 (2014).
3. A. Pashkin, A. Leitenstorfer, Particle physics in a superconductor, Science 345, 1121 (2014).
4. Ryusuke Matsunaga, Naoto Tsuji, Hiroyuki Fujita, Arata Sugio, Kazumasa Makise, Yoshinori Uzawa, Hirokazu Terai, Zhen Wang, Hideo Aoki, Ryo Shimano, Light-induced collective pseudospin precession resonating with Higgs mode in a superconductor, Science 345, 1145 (2014).
5. K. S. Novoselov, A. K. Geim, S. V. Morozov, D. Jiang, M. I. Katsnelson, I. V. Grigorieva, S. V. Dubonos, A. A. Firsov, Two-dimensional gas of massless Dirac fermions in graphene, Nature 438, 197 (2005).
6. M. Zarenia, A. Perali, D. Neilson, F.M. Peeters, Enhancement of electron-hole superfluidity in double few-layer graphene, Scientific Reports 4, 7319 (2014).
7. Liang Fu, Topological crystalline insulators, Phys. Rev. B 106, 106802 (2011).
8. Kai Sun, Topology and structural distortions, Nature mater. 14, 262 (2015).
9. D. K. Loginov, A. V. Trifonov, I. V. Ignatiev, Effect of uniaxial stress on the interference of polaritonic waves in wide quantum wells, Phys. Rev. B 90, 075306 (2014).
10. Evan O. Kane, Exciton dispersion in degenerate bands, Phys. Rev. B 11, 3850 (1975).
11. A. Siarkos, E. Runge, and R. Zimmermann, Center-of-mass properties of the exciton in quantum wells, Phys. Rev. B 61, 10854 (2000).
12. G. L. Bir and G. E. Pikus, Symmetry and strain induced effects in semiconductors (Wiley, New York, 1972).
13. G. Pikus, V. Maruschkak, and A. Titkov, Spin splitting and carrier spin relaxation in cubic crystals $\text{A}^{111}\text{B}^{11V}$, Fiz. Tekh. Poluprovodn. 22, 185 (1988) [Sov. Phys. Semicond. 22, 115 (1988)].
14. L. C. Lew Yan Voon, M. Willatzen, The $k \cdot p$ Method (Springer-Verlag, Berlin, 2009), ch. 7.
15. A. V. Kavokin, J. J. Baumberg, G. Malpuech, and F. P. Laussy, Microcavities (Oxford University, New York, 2007).
16. S. A. Markov, R. P. Seisyan, and V. A. Kosobukin, Exciton-polariton spectroscopy of strained semiconductor structures $\text{A}^{11V}\text{B}^{11V}$ with wide quantum wells, Fiz. Tekh. Poluprovodn. 38, 230 (2004). [Semiconductors 38, 225 (2004)].
17. D. K. Loginov, E. V. Ubyivovk, Yu. P. Efimov, V. V. Petrov, S. A. Eliseev, Yu. K. Dolgikh, I. V. Ignatiev, V. P. Kochereshko and A.V. Sel’kin, Interference of polariton waves in structures with wide GaAs/AlGaAs quantum wells, Fiz. Tverd. Tela 48, 1979 (2006) [Phys. Solid State 48, 2100 (2006)].
18. Yasuo Nozue, Manabu Itoh and Kikuo Cho, Excitonic polariton dispersion in ZnSe determined by the resonant Raman scattering under two-photon excitation of excitonic molecules, J. Phys. Soc. Jpn. 50, 889 (1981).
19. E. L. Ivchenko, Optical Spectroscopy of Semiconductor Nanostructures (Alpha Science, Harrow, 2005).
20. P. Etchegoin, J. Kircher, M. Cardona, C. Grein and E. Bustarret, Piezo-optics of GaAs, Phys. Rev. B 46, 15139 (1992).
21. P. Etchegoin, J. Kircher, M. Cardona and C. Grein, Piezo-optical response of Ge in the visible-uv range, Phys. Rev. B 45, 11721 (1992).
22. V. M. Agranovich and V. L. Ginzburg, Crystal optics with spatial dispersion and the exciton theory, 2nd ed. (Nauka, Moscow, 1979; Springer, New York, 1984).
23. R. Sooryakumar and P. E. Simmonds, High-resolution resonant Brillouin scattering and the effect of stress on GaAs, Phys. Rev. B 27, 4978 (1983).
24. G. E. Stillman, D. M. Larsen, C. M. Wolfe, R. C. Brandt, Precision verification of effective mass theory for shallow donors in GaAs, Solid State Comm. 9, 2245 (1971).
25. Landolt-Bornstein, Band 17a, Halbleiter (Springer, Berlin, Heidelberg, 1982).
26. F. Cerdeira, C.J. Buchenauer, Fred H. Pollak, Manuel Cordona, Stress-induced shifts of first-order Raman frequencies of diamond-and zinc-blende-type semiconductors, Phys. Rev. B 5, 580 (1972).
27. E. L. Ivchenko and G. Pikus, Superlattices and other microstructures (Springer-Verlag, Berlin, 1995).
28. E. V. Ubyivovk, D. K. Loginov, I. Ya. Gerlovin, Yu. K. Dolgikh, Yu. P. Efimov, S. A. Eliseev, V. V. Petrov, O. F. Vyvenko, A. A. Sitnikova and D. A. Kirilenko, Experimental determination of dead layer thickness for excitons in a wide GaAs/AlGaAs quantum well, Fiz. Tverd. Tela 51, 1818 (2009). [Phys. Solid State 51, 1929 (2009)].
29. D. Schiunmarini, N. Tomassini, L. Pilozzi, and A. D’Andrea, Polariton propagation in weak-confinement quantum wells, Phys. Rev. B 82, 075303 (2010).