Galaxies nurtured by mature black holes

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ABSTRACT
Supermassive black holes (SMBH) of size $10^6-10^9M_\odot$ are common in the Universe and they define the center of the galaxies. A galaxy and the SMBH are generally thought to have co-evolved. However, the SMBH cannot evolve so fast as commonly observed even at redshift $z > 6$. Therefore SMBH must form first before galaxy. Our goal is to clarify how this mature SMBH forms galaxy. Furthermore we clarify the mechanism how the SMBH designs variety of structures of galaxies. We explore a natural hypothesis that the SMBH have been formed mature at $z \approx 10$ before stars and galaxies. The SMBH forms energetic jets and outflows which trigger massive star formation in the ambient gas. They eventually construct globular clusters and classical bulge as well as the body of elliptical galaxies. We propose simple models which implement these processes along with the standard CDM-model. We point out that the globular clusters and classical bulges have a common origin but are in different phases. The same is true for the elliptical and spiral galaxies. Physics behind these phase division is the runaway star formation process with strong feedback to SMBH. This is similar to the forest-fire model that displays self-organized criticality. Finally we speculate several observational predictions that may help to test the present arguments.

Key words: circumstellar matter – infrared: stars.

1 INTRODUCTION
Almost all the galaxy harbors a supermassive black hole (SMBH) of mass $M_{BH} = 10^6-10^9M_\odot$ in its center (Kormendy & Richstone (1995)), where $M_\odot \approx 2 \times 10^{30}$kg is the solar mass. The mass of the SMBH is observed to have firm correlations with the basic components of the galaxy. For example in the case of classical bulge (CB), its mass $M_{CB}$ has the relation $M_{BH} \approx 10^{-3}M_{CB}$ (Gultekin et al. (2009)). In the case of globular clusters (GC), the number of them $N_{GC}$ in a galaxy has the relation $M_{BH} \approx 10^{5.5}N_{GC}M_\odot$ (Harris & Harris (2011)). Therefore it might be natural to think that the galaxy and its SMBH have co-evolved in their lives.

However, the standard coagulation of the stellar size black holes to form SMBH within a limited time scale turns out to be very difficult (Rees (1984)). This difficulty has become prominent by the recent observations (Marziani & Sulentic (2010); Wu et al. (2013)) that report many mature SMBH exist at around $z \approx 6$ (only 7.4 x 10^8 years after Big Bang). Various attempts to form these SMBH through the co-evolution with galaxies seem to be unnatural (Latif et al. (2014)), without assuming seed black holes of huge mass $10^9M_\odot$. Moreover there seems to be an evidence that the above black hole/bulge mass relation $M_{BH} \approx 10^{-3}M_{CB}$ has already been established or even the coefficient increases toward the past (Schulze & Wisotzki (2014)). All of these facts strongly suggest that the SMBH are primordial.

Therefore in this paper, we start from the hypothesis that mature SMBH have been formed at around $z \approx 10$ on top of the standard CDM model. Then the formation of all the structures, i.e. the stars, globular clusters, and bulges, should be attributed to this SMBH. These structures will quickly feed back to the SMBH. Thus the galaxy-SMBH co-evolution would have taken place in the very early stage and the several correlations above (Gultekin et al. (2009); Harris & Harris (2011)) would have already been established then.

The early formation of SMBH at around $z \approx 10$ has been studied in the model that the Bose-Einstein condensation of the self-interacting boson fields forms the dark energy (Nishiyama et al. (2004); Fuyuama & Morikawa (2006); Fuyuama et al. (2008); Fuyuama (2009)). In this model,
the unstable uniform condensation of the field can collapse to form SMBH everywhere in the Universe. This is possible because the coherent condensation does not have velocity dispersion which prevents the collapse. Furthermore in this model, the non-condensate component of the boson gas can contribute as the thermal dark matter around the SMBH.

The gravitational potential of this dark matter attracts baryon gas, and the SMBH will form a strong jet beyond the present size of the galaxy. This is plausible from the many observations at present although the jet ejection mechanism is not at all clear so far (Contopoulos et al. 2013). This jet will compress the surrounding gas and trigger massive star formation there especially in the dense gas environment (Reines & Deller 2012; Liu et al. 2013; Wagner et al. 2013; Gaibler et al. 2012). These first stars will build globular clusters (GC), the classical bulges (CB) in spiral galaxies (SG), and the main body of the elliptical galaxies (EG). This physics is closely related with the mechanism in (King 2003) which displays the correlation between the SMBH mass $M_{\text{BH}}$ and the velocity dispersion $\sigma$ of the stars in CB. This scenario is briefly explained in section 2.

According to the above scenario, the stars of GC and CB in the spiral galaxies, would have the same origin and are indistinguishable with each other. On the other hand, their clustering features are different; GC are extended in halo and CB forms the core of the galaxy. This divide may come from the two distinguished flows of gas in the primordial galaxy. We clarify these flows and the origin of distinct clustering features in section 3.

Furthermore an apparent similarity of CB (in SG) and EG suggests that the EG and SG have the common origin. The fact that SG is smaller than EG, in average, suggests that the strength of the jet from SMBH or the mass of SMBH will build globular clusters (GC), the classical bulges (CB) and the main body of the elliptical galaxies (EG). We will find much interesting parameter which clearly distinguish SG and EG in our model described in section 4.

We try to find the simplest model extracting the most relevant physics from very complicated galaxy formation processes. Limitations and prospects of our approach are described in the final section 5.

2 EARLY FORMATION OF SUPERMASSIVE BLACK HOLES

We briefly examine a possible origin of the primordial SMBH which was formed first before any other components of the galaxy. It is clear that the coagulation of the stellar size black holes to form SMBH takes too long time, more than the dynamical relaxation time scale $\tau_{\text{rel}}=\sigma^4/(G^2m\rho N)$, which turns out to be $2\times 10^{14}$ years, where $\sigma$, $m$, $\rho$, $N$, $G$ are the velocity dispersion, mass, mass density, number of the black holes, and the gravitational constant, respectively. To bring this time scale within the cosmic age $1.38 \times 10^{10}$ years, we need seed black holes of mass $10^5 M_\odot$ to start with. Furthermore dark matter gas is hopeless to collapse into SMBH because of its velocity dispersion and the angular momentum. The only possibility will be the collapse of the condensed field whose uniform component forms the dark energy (Nishiyama et al. 2004; Fukuyama & Morikawa 2006). This is possible if the dark energy is the Bose-Einstein condensation of fields (mass $m$) with an attractive self-interaction ($\lambda < 0$). The condensate is characterized by the classical scalar field $\Psi(t,r)$ in the metric, assuming spherical symmetry,

$$ds^2 = c^2 dt^2 - a^2 dr^2 - r^2 d\theta^2 - r^2 \sin^2 \theta d\phi^2$$

and obeys the equation of motion,

$$r \frac{d}{dr} \left(r^2 a^2 \frac{d\Psi}{dr} - 2\frac{\rho_0}{a^2} \Psi' - 2\alpha \frac{\rho_0}{a^2} \Psi' - 2 \frac{\rho_0}{a^2} \frac{\rho_0}{a^2} \frac{\Psi'}{r^2} \right) = 0,$$

This set of equations easily forms black hole even if mass-less non-interacting case, which was often used to analyze critical behavior in the black hole formation process (Choptuik 1993; Gundlach 2007). It was concluded that the resultant black hole mass shows scaling properties. On the other hand, more realistic bound for the black hole formation comes from the quantum fluctuations. However, it turns out that even the quantum fluctuations cannot prevent the collapse of the condensate to black hole if the mass of the boson field exceeds the Kaup limiting mass (Kaup 1968)

$$M_{\text{Kaup}} = 0.63 \frac{\hbar c}{G m} \approx \frac{m_{\text{pl}}^2}{m}$$

where $m_{\text{pl}}$ is the Planck mass. If the boson mass is the order of the present dark energy 0.01$eV$, then the limiting mass becomes $1.7 \times 10^{22}$kg, almost the planet Pluto mass.

After the adiabatic collapse of the dark energy, some portion of the condensation becomes a black hole (Choptuik 1993) and some other portion will melt to form thermal boson gas around the black hole (Nishiyama et al. 2004)). This latter melting process of the condensation depends on many complex conditions and has not yet been clarified. However it would be natural to suppose that it settles down to the thermal equilibrium of mass density $\rho(r) = \rho_0/(r/r_0)^2$ where $r$ is the distance from the central SMBH and $\rho_0$, $r_0$ are constants. Then this thermal uncondensed gas behaves as dark matter (Nishiyama et al. 2004; Fukuyama & Morikawa 2006) since it yields the commonly observed flat rotation curve.

Suppose that the SMBH thus formed at $z \approx 10$ is already surrounded by the thermal gas of dark matter with well developed gravitational potential. Then baryons are attracted within the free fall time scale about $5 \times 10^7$ years. At the same time the SMBH would yield energetic jets, which may trigger massive star formation along it through the ram pressure of the bow shock (Reines & Deller 2012; Liu et al. 2013). However the effect of the jet for star formation is not yet fully understood as well as the jet formation mechanism itself. We do not go deep into these problems in this paper. If the jet conveys the momentum to the ambient baryon gas, then the pressure compresses the gas to promote the star formation. On the other hand, if the jet conveys the energy to the gas, then the heat makes the gas expand to prevent the star formation. Among numerous arguments on the both directions, there seems to be a plausible direction (Wagner et al. 2013; Gaibler et al. 2012) that promotion
and prevention of star formation coexist depending on the parameters such as the gas density and inhomogeneity. In general the dense environment, such as in the early stage of the Universe or in the center of the gravitational potential, prefers the promotion of star formation. On the other hand the dilute environment prevents the prevention and disperses the gas clouds.

All the above arguments are for a steady jet with fixed direction. If the jet changes its direction rapidly less than the free fall time scale, as we will argue in the next section, then the trajectory envelope of the jet will form a superseded shock wave shells. A similar argument appears in (King (2003)) which displays the formation of the correlation between the mass $M_{BH}$ of the SMBH and the velocity dispersion $\sigma$ in galactic bulge. If the typical outflow radiation balances in momentum with the ambient gas of size $R$, then we have $GM_0M_{tot}/R^2 = L_{Edd}/c$, where $M_0 = fM_{tot}$ is the baryon mass of the galaxy, i.e. the fraction $f$ of the total mass $M_{tot}$. $L_{Edd} = 4\pi GM_0c/\kappa$ is the Eddington limiting luminosity where $\kappa$ is the electron scattering opacity. Then using the virial equilibrium relation $\sigma^2 = GM_{tot}/R$, we have (King (2003)),

$$M_{BH} = \frac{f\kappa\sigma^4}{4\pi G^2} \propto \sigma^4$$

This successfully describes the observations (Gultekin et al. (2009)). On the other hand if we supposed energy balance, we have an extra factor $(\sigma/c)$ on the right hand side of Eq. (4), and $M_{BH} \propto \sigma^5$. This predicts too small mass of SMBH and conflicts with observations. Thus the observed $M_{BH}$ vs relation is consistent with the momentum balance, which suggests the jet/outflow-induced star formation. As argued in the above, this star formation must have taken place in the early stage of the Universe. This burst-mode star formation induced by energetic jets should be distinguished from the spontaneous mild star formation later time when the jets generally expel and heat up the ambient gas to prevent the burst-model star formation.

3 SEPARATION INTO GLOBULAR CLUSTERS AND ELLIPSOIDS

Now we examine how SMBH triggers star formation and makes basic components of galaxy. The first stars, as well as their direct descendants formed after the first supernova explosions, are thought to be the main ingredients of the galaxy components: classical bulge (CB), globular clusters (GC) and the elliptical galaxies (EG). These components must be formed at the same time and same mechanism since observations indicate that all of them are composed from very old population-II stars. Then how these separations into components are processed?

We first consider the separation into GC and ellipsoids (i.e. the CB and the main body of EG). We consider that there had been two different kinds of gas velocity fields. One is caused by the local gravitational potential, and the other caused by the global cosmic turbulent flow (Nakamichi, & Morikawa (2010))

$$3\text{ This turbulence might be caused by the collapse of the condensation when SMBH are formed everywhere in the Universe.}$$

Figure 1. Velocity dispersion of ambient gas as a function of the distance $r$ from the central SMBH. There are two distinct velocity fields: The constant virial velocity field $v_{in} \equiv 200km/sec$ (broken blue, dominates inward) and the increasing turbulent velocity field $v_{out} \equiv (\epsilon r)^{1/2}$ (solid red, dominates outward). They are equal with each other at $r_\ast \approx 8.6kpc$. A star formed at $r < r_\ast$ falls down toward the SMBH and forms a bulge, while the star at $r > r_\ast$ stays far from the SMBH and forms globular clusters.
from the center possibly forming small clusters that we call globular clusters (GC).

There are some specific features of the above scenario which may be significant in comparison with observations:

(a) All the stars in GC and CB have the same age and chemical components because they are formed by the same gas triggered by the common jet at the same time. (b) Each GC has almost no local angular momentum. This is because each GC is formed in the finite region where the relative gas speed is small and coherent according to the relation $v_{\text{out}} \equiv (cr)^{1/3}$ (Fig. 1). Reflecting this small velocity dispersion at small scale, each GC becomes compact with the typical size $r_{\text{GC}} \approx (GM)^{2/3}c^{-2/3} \approx 2.5\,\text{pc}$ for $M = 10^9\,M_\odot$. (c) GC are loosely bounded to the galaxy since they tend to have higher velocities $v_{\text{out}}$ than the virial equilibrium $v_{\text{in}}$. Therefore there may be significant number of stray GC in between galaxies. This point should be considered in wider viewpoint including the dwarf spheroidal galaxies (Bershady 2007). In summary, CB and GC are the same species but separated into two phases by two distinct velocity fields.

4 SEPARATION INTO SPIRAL AND ELLIPTICAL GALAXIES

Next we consider the separation into the spiral (SG) and elliptical (EG) galaxies in our scenario of mature SMBH. Apart from the disk, the classical bulge (CB) in SG, and EG are composed from the old population-II stars as globular clusters (GC). Therefore it would be natural to think that CB and EG are the same species but in different phases.

In order to demonstrate this process of separation, we introduce a simple model for the massive star formation by jets. We concentrate on the very basic Physics behind first in order to explore the plausible mechanism for galaxy formation at present. Therefore our model is simply a representative one among many possible models. Suppose the energetic jet from SMBH hits the ambient gas that is isotropically distributed around the SMBH. We assumed that the jet triggers the gas to form stars. Then those stars formed in the near region $r < r_*$ fall down toward he center. Some of them will give torque on the SMBH through the deformation of the accretion disk. Then the jet from SMBH changes its direction since the jet direction is thought to be parallel to the SMBH rotation axes. In the new direction of the jet, there will be plenty of fresh gas ready to form stars. Thus the jet will trigger new star formation in this rich gas environment. This yields further torque on the SMBH. This feedback dynamics will be simply represented by the following model:

$$
\dot{g}_i(t) = -\mu |\vec{T}(t)|
\begin{cases}
\hat{s}_i, & |\vec{t}| \leq s_i,
\hat{t}, & \text{else}
\end{cases}
\dot{\vec{T}}(t) = -\lambda |\vec{T}(t)| \sum_i [\hat{s}_i \hat{g}_i (t)]_n \sum_i \hat{g}_i (t) - \kappa \vec{T},
$$

where the vector $\vec{T}(t)$ represents the jet (direction=axes of the jet, amplitude=strength of the jet). The scalar $g_i (t)$ represents the amount of gas in the $i$-th direction $\hat{s}_i$, where $\{\hat{s}_i\}_{1 \leq i \leq N}$ covers the whole solid angle. The parameter $\alpha$ simply controls the beam widths and the symbol $[\hat{s}]_n$ represents the unit vector with the same direction $\hat{s}$. The directions $\{\hat{s}_i\}_{1 \leq i \leq N}$ are designed based on the Fibonacci-Himawari coordinate system using the golden angle $\beta = 137.5^\circ \ldots$ so that it covers the whole solid angle with uniform density:

$$
\vec{r}_i = (s \sin \gamma, s \cos \gamma, c) \text{ with } c = 1 - 2(i/\text{total}), s = \sqrt{1 - \gamma^2}, \gamma = \beta i.
$$

The first line of Eq. (6) represents the gas reduction process by the star formation triggered by the jet. This is proportional to the star formation rate $\mu$, the strength of the jet toward the direction $i$ with the jet collimation parameter $\alpha$, and the amount of gas at that direction $g_i(t)$. The second line represents the time change rate of the jet. This is proportional to the feeding efficiency $\lambda$ of the formed star to the SMBH, and the torque exerted by the falling stars just formed. A natural fade-out term parametrized by $\kappa$ is added.

There are two typical cases in this model (Figs. 2, 3).

(a) The jet is active and wildly changing its direction until finally all the ambient gas is exhausted to form stars (Fig. 2). (b) The jet is less active and the direction is not wildly changed. There are finite remaining gas that failed to form stars and distributed almost perpendicular to the final jet direction. The gas will eventually settle to form a disk and a spiral galaxy is left.

If the settled jet-pair happens to point toward the gas remaining regions, then the small scale star formation activity may be still triggered which further induce density wave arm structure emanating from there.

Figure 2. The galaxy formation history in case (a), high accretion rate $\lambda = 1$. These are the snapshots of the gas distribution (small balls), jet (arrows), and the bulge (central pink ball) derived by the numerical calculations of Eq. (6). The time flows from left to right ($t = 0, 150, 300$). The gas was isotropically distributed at $t = 0$. Accreted objects keep exerting torque on SMBH and the jet wildly changes its direction rapidly. This rampaging jet triggers star formation in the whole solid angle. Eventually all the gas is exhausted and an elliptical galaxy is left. The parameters are $\mu = 1, n = 10, \kappa = 0.01, N = 256$.

Figure 3. The galaxy formation history in case (b), low accretion rate $\lambda = 0.1$. The same as Fig. 2 but with low accretion rate. The jet is inactive and its direction does not change much. Therefore the gas is left in a torus form almost perpendicular to the final jet direction. The gas will eventually settle to form a disk and a spiral galaxy is left.
This case. (center) The case the star formation rate changed. The remaining gas fraction has a sharp bend only in not exist at all (\(j\)). (right) The initial jet strength \(j\) is changed. If the jet activity does not exist at all (\(j = 0\)), it may yield a bulge-less spiral galaxy. The other parameters are the same as in Fig. 2.

Some portion of this gas located inward would eventually relaxed to form regular disk structure, in which new stars are going to be formed spontaneously. The remaining gas outward would be scattered and lost by the turbulence. This is the typical spiral galaxy. Thus the elliptical and spiral galaxies born at the same time by the same mechanism. Only the degree of jet activity separates them into the two phases SG and EG. The jet direction trajectories in both cases are compared in Fig. 4.

The distinction of the two phases seems to be sharp if parametrized by the accretion rate \(\lambda\), but not by the other parameters, as shown in Fig. 5. If \(\lambda\) is large, then the torque exerted from the falling stars strongly changes the jet direction so that more star formation takes place in the fresh ambient gas. This further exert strong torque and this runaway continues until all the gas is exhausted. On the other hand if \(\lambda\) is small, then the falling stars exert only weak torque to change the jet direction. Then the jet cannot hit the sufficient amount of fresh gas to yield torque and eventually the jet direction is settled, leaving the torus shape gas distribution around the central bulge. The positive feedback eventually stops, and no runaway takes place.

This galaxy formation process has similar physics to the forest-fire model in complex systems (Henley 1985; Bald 1990). This model is composed of many trees on a two-dimensional lattice. Each tree on a lattice site has a finite probability \(p\) to ignite spontaneously. If ignite, the fire spreads to the neighboring trees with some probability. On the site of the burnt tree, a new tree has a chance to grow with some probability. The main feature is that the fire-fire correlation length \(\xi(p)\), depends on \(p\), determines the asymptotic two distinct states: (a) The fire dies out if \(\xi(p)\) exceed the system size \(L\). (b) The fire is sustained if \(\xi(p) < L\). Percolation caused by the positive feedback or runaway process is the common feature in our galaxy model and the forest-fire model although the former is deterministic, as Eq. (3), and the latter is probabilistic.

In our model, the parameter of accretion rate \(\lambda\) may particularly be important to divide the galaxies into the elliptical and spiral (Fig. 5 left). The special value \(\lambda_* \approx 0.1\) divides the EG (\(\lambda > \lambda_*\)) and SG (\(\lambda < \lambda_*\)). This parameter corresponds to the relevant parameter \(p\) in the above forest-fire model.

It may be interesting to examine a possible galaxy classification further in our model, focusing on the representative parameters \(\mu\) and \(\lambda\) (Fig. 6). Large star formation rate \(\lambda\) is provided, for example, by the dense ambient gas such as in the bottom of the gravitational potential produced by the huge dark matter halo. On the other hand large feeding efficiency \(\lambda\) is provided, for example, by small angular momentum of the whole gas cluster. Therefore the galaxies produced in dense ambient gas with small angular momentum correspond to large \(\mu\) and large \(\lambda\). This set of parameter provides strong and violent jet and leaves a big cluster of stars without remaining gas. This may yield elliptical galaxies. Contrary the galaxies produced in dilute ambient gas with large angular momentum correspond to small \(\mu\) and small \(\lambda\). This set of parameter provides weak and steady jet and leaves small cluster of stars with plenty of gas remaining. This may yield spiral galaxies. The intermediate case that the galaxies produced in dense ambient gas with large angular momentum correspond to large \(\mu\) and small \(\lambda\). This set of parameter provides strong jet and leaves a big cluster of stars with some amount of remaining gas. This may yield lenticular galaxies. The remaining case of small \(\mu\) and large \(\lambda\) would not yield any prominent regular structures. Smallest values of \(\mu\) and \(\lambda\) may yield apparently tiny galaxies. These tiny galaxies would be clearly distinguished from GC by the existence of their central SMBH and dark matter, which are absent in GC (Satyapal et al. 2014).

According to our scenario, these galaxy species are intrinsic and do not change in time. However the ratio of galaxy species may be slightly altered by later merger processes, which may not dominate nor are relevant in our scenario though. Moreover we can speculate the apparent evolution of the galaxy species. The produced EG has no gas and therefore no further prominent star formation process, except some AGN in which the jet is re-activated for any reason. Thus the population of EG species will not largely change in time. On the other hand the SG has plenty of gas remaining around the central bulge and the spontaneous star formation actively continues. This spontaneous-mode of star formation is contrasted with the burst-mode of them due to the jets. The former stars mainly form the population I and the latter the population II. In SG, the ambient gas was initially irregular and inhomogeneous just after the formation because of the random jets. This primordial SG will eventually form regular disk around the central bulge by consuming their locally excess kinetic energy to trigger new star formation through the shocks. Therefore the apparent irregular
We proposed a scenario that the primordial supermassive black hole (SMBH) made the galaxy. Energetic jets from the SMBH give ram pressure to trigger the massive star formation in the primordial dense gas environment. We focused on the following two aspects of this scenario.

The first aspect is the comparison of a globular cluster (GC) and a classical bulge (CB). According to our scenario, they are the same species but in distinct phases. We proposed that the difference comes from the existence/absence of the runaway separates the same species into two phases. This process has the common physics to the forest-fire model in complex systems.

Thus a SMBH defines the center of a galaxy and various star clusters in the galaxy (GC, CB, EG) are nurtured by the SMBH through the energetic jet emanating from the SMBH. According to this scenario, the hypothesis of the population-III stars that formed spontaneously may not be necessary.

Our simple analysis may be a useful supplement to the solid simulations of galaxy formation including all physical processes. We have ignored many detail dynamics such as the star formation process, back reaction to the jet, jet formation and collimation, and transfer of the angular momentum, etc. We wanted to extract the most relevant physics in the complex galaxy formation process and to construct a natural model based on them. We would like to report how the elaboration of our model including the above fundamental processes can be possible in our future study.

Several final remarks are in order. The jet activity may leave its trace in the faint structures in a spiral galaxy. The final stage of the jet would be gentle and the jet will generally have small precession. This jet may form a double-cone shape region in which the stars are massively formed. Subsequent supernova explosions of those stars may leave high energy electrons and protons there captured and stored in the magnetic fields. This relic ionized region will be observed in the early galaxies. However this relic structure may be contaminated with the relatively recent jet activity which often observed (Dobler et al. (2010)).

In our scenario, a SMBH always defines the center of the galaxy. Therefore even the expelled SMBH, after multiple merger of galaxies, if any, will form a new galaxy independently around it. In any case, galaxy merger is not a dominant process in our scenario. Rather, we expect a cluster of SMBH which will be formed by the instability of the huge condensed field. In this case, multiple SMBH are expected to form on a plane after the collapse of the condensation in the form of pancake. This process does not destroy any of the ΛCDM model in which the dark matter forms individual gravitational potential. Actually we simply need a tiny fraction of those dark matter cluster becomes condensed and collapse to form SMBH.

We hope we will soon be able to report these considerations by checking the fundamental processes theoretically and observationally.
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