SHELL MODEL DESCRIPTION OF \(^{102-108}\)Sn ISOTOPES

T. TRIVEDI
Tata Institute of Fundamental Research, Mumbai- 400005, India and
Department of Physics, University of Allahabad, Allahabad-211002, India

P.C. SRIVASTAVA
Instituto de Ciencias Nucleares, Universidad Nacional Autónoma de México, Apartado Postal
70-543, 04510 México, D.F., México

D. NEGI
Inter University Accelerator Centre, New Delhi- 116007, India

I. MEHROTRA
Department of Physics, University of Allahabad, Allahabad-211002, India

We have performed shell model calculations for neutron deficient even \(^{102-108}\)Sn and odd \(^{103-107}\)Sn isotopes in \(sdg_7/2h_{11/2}\) model space using two different interactions. The first set of interaction is due to Brown et al. and second is due to Hoska et al. The calculations have been performed using doubly magic \(^{100}\)Sn as core and valence neutrons are distributed over the single particle orbits \(1g_{7/2}, 2d_{5/2}, 2d_{3/2}, 3s_{1/2}\) and \(1h_{11/2}\). In more recent experimental work for \(^{101}\)Sn [Phys. Rev. Lett. 105 (2010) 162502], the g.s. is predicted as \(5/2^+\) with excited \(7/2^+\) at 172 keV. We have also performed another set of calculations by taking difference in single particle energies of \(2d_{5/2}\) and \(1g_{7/2}\) orbitals by 172 keV. The present state-of-the-art shell model calculations predict fair agreement with the experimental data. These calculations serve as a test of nuclear shell model in the region far from stability for unstable Sn isotopes near the doubly magic \(^{100}\)Sn core.

1. Introduction

The structure of neutron deficient nuclei far from \(\beta\)-stability is currently at the focus of nuclear structure due to development of the radioactive ion beam facilities, high efficiency gamma detector array and state-of-the-art shell model calculations using new effective interactions. Further, nuclei near the \(N\approx Z\), heaviest doubly magic core are more interesting because they exhibit many new structural phenomenon such as shell evolution\(^\text{1}\), change of collective properties\(^\text{2}\), band termination\(^\text{3}\) and magnetic rotation\(^\text{4}\) etc.

In recent years rich variety of experimental data is now available for neutron deficient Sn isotopes by various experimental studies. Faestermann et al. first time
measured the half-life, $\beta$- and $\gamma$-spectrum of $^{102}\text{Sn}$ at GSI\cite{5}. Exited states for $^{103}\text{Sn}$ using EUROBALL and ancillary detectors was reported in \cite{6}. Structure of high spin states in $^{104}\text{Sn}$ using reaction $^{58}\text{Ni}(^{50}\text{Cr},2\text{p}2\text{n})$ at 200 and 205 MeV beam energies were reported by Górska et al.\cite{7} Gadea et al.\cite{4} investigated structure of $^{105}\text{Sn}$ through $^{50}\text{Cr}(^{58}\text{Ni},2\text{pn})$ reaction at energies of 210 MeV, they also found dipole band similar to the Pb region. Coexistence of collective and quasiparticle structure in $^{106}\text{Sn}$ and $^{108}\text{Sn}$ have been reported by Juutinen et al.\cite{8} For $^{108}\text{Sn}$ smooth band termination is also reported in \cite{3}. In more recent experiment Banu et al.\cite{9} studied $^{108}\text{Sn}$ in inverse kinematics by intermediate-energy Coulomb excitation using the RISING setup at GSI. Vaman et al. studied even-mass $^{106-112}\text{Sn}$ at NSCL from intermediate-energy Coulomb excitations \cite{10}. Recently Ressler et al.\cite{11} reported $\beta$ decay studies of $^{107,109}\text{Sn}$ to establish low-lying states in $^{107,109}\text{Sn}$\cite{11}.

From theoretical point of view the Sn isotopes are interesting to study, as they are unique testing ground for nuclear structure calculation. Previously shell model calculation for neutron-deficient Sn isotopes have been performed by Engeland et al.\cite{12}, Covello et al.\cite{13} and Schubert et al.\cite{14} taking $^{100}\text{Sn}$ as core, almost more than one decade back. However, recently shell model calculations for $^{106-109}\text{Sn}$ isotopes using CD-Bonn and Nijmegen1 interactions are reported by Dikman\cite{15}.

In the present work, large-scale shell model calculation have been performed for neutron deficient even $^{102-108}\text{Sn}$ and odd $^{103-107}\text{Sn}$ isotopes for more recent accumulated experimental data. The calculation have been performed in $sdg_{7/2}h_{11/2}$ model space. The aim of present work is to test the effective interactions for these lighter Sn isotopes near the N$\simeq$Z line where pairing correlation are more important.

| orbital | sn100pn | snet | sn100pn(mod.) | snet(mod.) |
|---------|---------|------|---------------|------------|
| nlj     | Energy(MeV) |      |               |            |
| 2d$_5/2$ | -10.6089 | -10.10 | -10.6089 | -10.322 |
| 1g$_7/2$ | -10.2893 | -10.15 | -10.4369 | -10.15 |
| 3s$_1/2$ | -8.7167 | -8.40 | -8.7167 | -8.40 |
| 2d$_3/2$ | -8.6944 | -8.09 | -8.6944 | -8.09 |
| 1h$_{11/2}$ | -8.8152 | -7.85 | -8.8152 | -7.85 |

2. Details of Calculation

Shell model calculation of the low-lying states for mass A = 102-108, Sn isotopes have been performed in $sdg_{7/2}h_{11/2}$ valence space taking $^{100}\text{Sn}$ as core. Valence neutrons are distributed over the single particle orbits 1g$_7/2$, 2d$_5/2$, 2d$_3/2$, 3s$_1/2$ and 1h$_{11/2}$. In the present calculations, we have used two sets of interactions. The first set of interaction named sn100pn was obtained from a realistic interaction
developed by Brown et al., starting with G matrix derived from CD Bonn nucleon nucleon interaction. This interaction has three parts, proton-proton (pp), neutron-neutron (nn) and proton-neutron (pn). Apart from Coulomb interaction was added to the interaction between protons. The second set of interaction named snet was obtained from bare G matrix by Hoska et al. based on renormalized Paris potential for \( N = 82 \) nuclei. In more recent work for \( ^{101}\text{Sn} \), the g.s. is predicted as \( 5/2^+ \) with excited \( 7/2^+ \) at 172 keV. We have also performed another two set of calculations by taking difference in single particle energies of \( 2\,d_5/2 \) and \( 1\,g_7/2 \) orbitals by 172 keV. These two modified results are reported as sn100pn(mod.) and snet(mod.). The calculation have been performed using code Nushe II without any truncation except in case of \( ^{108}\text{Sn} \) where we have put maximum two particles in \( 1\,h_{11/2} \) orbital.

3. Results and Discussion

3.1. Excitation energies of even Sn isotopes

In Table 2, we have tabulated all the calculated and experimentally known levels for \( ^{102}\text{Sn} \) and corresponding levels are also shown in Fig. 1. Experimentally, only few excited states with \( J^\pi = 2^+ \), \( 4^+ \) and \( 6^+ \) are known. The ground state \( 0^+ \) is well predicted by both the interactions and it is found that calculated \( 2^+ \) state lies at 211 and 217 keV above the experimental values for sn100pn and snet interactions. However, with modified single particle energies in snet(mod.) interaction, the calculated \( 2^+ \) states is well reproduced with an energy difference of 146 keV, whereas, from sn100pn(mod.) interaction change is not much pronounced. The \( 4^+ \) state is well predicted by snet interaction but in case of sn100pn interaction it lies above the \( 6^+ \). The \( 6^+ \) is predicted at 2063 and 2089 keV by sn100pn and snet interaction, respectively.

The calculated and experimentally known energy levels for \( ^{104}\text{Sn} \) are tabulated.
Fig. 1. Experimental and calculated energy levels of $^{102}$Sn with sn100 and snet interactions.

Table 3. Experimental and theoretical low-lying states (up to 4.5 MeV) of $^{104}$Sn. Energies are in MeV.

| $J^\pi$ | Exp. | $J^\pi$ | sn100pn | $J^\pi$ | snet | $J^\pi$ | sn100pn(mod.) | $J^\pi$ | snet(mod.) |
|--------|------|--------|---------|--------|------|--------|----------------|--------|------------|
| $(0^+)$ | 0.000 | $0^+$  | 0.000   | $0^+$  | 0.000 | $0^+$  | 0.000          | $0^+$  | 0.000      |
| $(2^+)$ | 1.260 | $2^+$  | 1.494   | $2^+$  | 1.597 | $2^+$  | 1.467          | $2^+$  | 1.563      |
| $(4^+)$ | 1.943 | $4^+$  | 2.111   | $4^+$  | 2.098 | $4^+$  | 2.067          | $4^+$  | 2.070      |
| $(6^+)$ | 2.257 | $6^+$  | 2.282   | $6^+$  | 2.188 | $6^+$  | 2.246          | $6^+$  | 2.162      |
| $(8^+)$ | 3.140 | $0^+$  | 2.358   | $0^+$  | 2.337 | $0^+$  | 2.358          | $0^+$  | 2.201      |
| $(10^+)$ | 3.981 | $2^+$  | 2.537   | $2^+$  | 2.543 | $2^+$  | 2.476          | $4^+$  | 2.442      |

in Table 3 and are also plotted in Fig. 2. Both the interactions predict very well the ordering of levels. In order to interpret the experimental results of $^{104}$Sn, Górska et al. [7] have also done similar calculations using snet interaction. Along with result of same interaction, we are also reporting results from sn100pn interaction for sys-
tematic study of this nucleus. The first excited $2^+$ state is overestimated by 234, 337 keV from sn100pn and snet interaction from the experimental value, which is reduced by 207 and 303 keV, respectively when single particle energies are adjusted in these interactions. The first $4^+$ is predicted at 2111 and 2098 keV by sn100pn and snet interaction while corresponding experimental value is 1943 keV. The first $6^+$ is predicted by both interactions within 70 keV difference from experimental observed data. The spacing between $4^+$ and $6^+$ gets compressed from snet interaction which remains almost unchanged with modified single particle energies too. The high-spin states $8^+$ and $10^+$ are calculated at 3623 and 3995 keV for sn100pn interaction whereas, from sn100pn (mod.) these states lie at 3562 and 3912 keV, which are closer to experimental data. With snet interaction, these states lie at 3505 and 3826 keV. The snet(mod.) interaction predicts $8^+$ and $10^+$ at 3702, 3878, keV respectively.

For $^{106}$Sn, the calculated and experimental states are listed in Table 4 and corresponding energy spectra are shown in Fig.3 More recently shell model calculation has been done by Dikmen\cite{15} for $^{106}$Sn using CD Bonn potential. The calculation reported in this paper using two different types of interactions have some what over estimated the experimentally observed ones, while our calculation using sn100pn and snet interactions are more close to the experimentally observed data. The position of $2^+$ level at 1.413 MeV from sn100pn interaction agrees with experimentally observed one at 1.208 MeV but it is over estimated by 350 keV in snet interaction. Again the $4^+$, $6^+$, $8^+$ and $10^+$ states are in good agreement with experimental data from both the interaction, even in much better agreement with snet interac-
Table 4. Experimental and theoretical low-lying states (up to 4.5 MeV) of $^{106}$Sn. Energies are in MeV.

| J$^\pi$ | Exp. J$^\pi$ | sn100pn J$^\pi$ | snet J$^\pi$ | sn100pn(mod.) J$^\pi$ | snet(mod.) J$^\pi$ |
|---------|-------------|----------------|-------------|------------------------|---------------------|
| (0$^+$) | 0.000 0$^+$  | 0.000 0$^+$    | 0.000 0$^+$ | 0.000 0$^+$            | 0.000 0$^+$         |
| (2$^+$) | 1.208 2$^+$  | 1.131 2$^+$    | 1.558 2$^+$ | 1.329 2$^+$            | 1.569 2$^+$         |
| (4$^+$) | 2.202 4$^+$  | 2.194 4$^+$    | 2.167 4$^+$ | 2.170 0$^+$            | 2.138 0$^+$         |
| (6$^+$) | 2.324 6$^+$  | 2.424 6$^+$    | 2.406 0$^+$ | 2.368 4$^+$            | 2.140 4$^+$         |
| (8$^+$) | 3.480 0$^+$  | 2.430 0$^+$    | 2.361 6$^+$ | 2.383 6$^+$            | 2.281 6$^+$         |
| (10$^+$)| 4.133 2$^+$  | 2.592 4$^+$    | 2.615 2$^+$ | 2.519 4$^+$            | 2.514 4$^+$         |
|        | - 4$^+$     | 2.676 4$^+$    | 2.625 4$^+$ | 2.592 2$^+$            | 2.573 2$^+$         |
|        | - 1$^+$     | 2.723 1$^+$    | 2.771 1$^+$ | 2.672 5$^+$            | 2.704 5$^+$         |
|        | - 5$^+$     | 2.762 3$^+$    | 2.799 5$^+$ | 2.703 3$^+$            | 2.709 3$^+$         |
|        | - 3$^+$     | 2.766 5$^+$    | 2.822 3$^+$ | 2.711 1$^+$            | 2.741 1$^+$         |
|        | - 6$^+$     | 2.985 6$^+$    | 2.932 6$^+$ | 2.967 6$^+$            | 2.897 6$^+$         |
|        | - 5$^+$     | 3.080 5$^+$    | 3.169 5$^+$ | 3.036 5$^+$            | 3.214 5$^+$         |
|        | - 1$^+$     | 3.481 3$^+$    | 3.293 3$^+$ | 3.111 3$^+$            | 3.298 3$^+$         |
|        | - 8$^+$     | 3.652 8$^+$    | 3.660 1$^+$ | 3.435 1$^+$            | 3.619 1$^+$         |
|        | - 7$^+$     | 4.020 7$^+$    | 3.692 8$^+$ | 3.586 8$^+$            | 3.660 8$^+$         |
|        | - 7$^+$     | 4.119 7$^+$    | 3.797 7$^+$ | 3.936 7$^+$            | 3.756 7$^+$         |
|        | - 10$^+$    | 4.362 10$^+$   | 4.125 10$^+$| 4.300 10$^+$           | 4.086 10$^+$        |

Fig. 3. Same as figure 1 for $^{106}$Sn.

Table 5. Contains experimentally observed and theoretically calculated states up to 4.5 MeV for $^{108}$Sn. These states are also shown in Fig. 4. In both set of shell model
Table 5. Experimental and theoretical low-lying (up to 4.5 MeV) states of $^{108}$Sn. Energies are in MeV.

| $J^\pi$ | Exp. $E$ (MeV) | $J^\pi$ | sn100pn $E$ (MeV) | $J^\pi$ | snet $E$ (MeV) | $J^\pi$ | sn100pn(mod.) $E$ (MeV) | $J^\pi$ | snet(mod.) $E$ (MeV) |
|---------|----------------|---------|-----------------|---------|----------------|---------|------------------------|---------|------------------------|
| $0^+$   | 0.000          | 0$^+$   | 0.000           | 0$^+$   | 0.000          | 0$^+$   | 0.000                  | 0$^+$   | 0.000                  |
| $2^+$   | 1.207          | 2$^+$   | 1.186           | 2$^+$   | 1.498          | 2$^+$   | 1.201                  | 2$^+$   | 1.540                  |
| $4^+$   | 2.111          | 4$^+$   | 2.142           | 4$^+$   | 2.177          | 4$^+$   | 2.146                  | 4$^+$   | 2.146                  |
| $6^+$   | 2.365          | 6$^+$   | 2.264           | 6$^+$   | 2.315          | 0$^+$   | 2.247                  | 0$^+$   | 2.163                  |
| $8^+$   | 3.561          | 6$^+$   | 2.297           | 0$^+$   | 2.326          | 2$^+$   | 2.248                  | 6$^+$   | 2.299                  |
| $10^+$  | 4.256          | 0$^+$   | 2.315           | 2$^+$   | 2.606          | 6$^+$   | 2.283                  | 2$^+$   | 2.526                  |
|         | -              | 4$^+$   | 2.338           | 4$^+$   | 2.607          | 4$^+$   | 2.316                  | 4$^+$   | 2.589                  |
|         | -              | 1$^+$   | 2.575           | 5$^+$   | 2.767          | 5$^+$   | 2.521                  | 5$^+$   | 2.674                  |
|         | -              | 5$^+$   | 2.588           | 1$^+$   | 2.771          | 3$^+$   | 2.560                  | 3$^+$   | 2.726                  |
|         | -              | 3$^+$   | 2.607           | 3$^+$   | 2.797          | 1$^+$   | 2.582                  | 1$^+$   | 2.756                  |
|         | -              | 6$^+$   | 2.985           | 6$^+$   | 2.859          | 5$^+$   | 2.794                  | 6$^+$   | 2.762                  |
|         | -              | 5$^+$   | 2.759           | 5$^+$   | 3.115          | 6$^+$   | 2.816                  | 1$^+$   | 3.165                  |
|         | -              | 6$^+$   | 2.840           | 3$^+$   | 3.338          | 3$^+$   | 2.909                  | 5$^+$   | 3.208                  |
|         | -              | 3$^+$   | 2.886           | 7$^+$   | 3.666          | 1$^+$   | 2.951                  | 3$^+$   | 3.312                  |
|         | -              | 1$^+$   | 3.006           | 8$^+$   | 3.693          | 8$^+$   | 3.500                  | 8$^+$   | 3.672                  |
|         | -              | 8$^+$   | 3.502           | 8$^+$   | 4.054          | 7$^+$   | 3.608                  | 7$^+$   | 3.689                  |
|         | -              | 7$^+$   | 3.612           | 7$^+$   | 4.137          | 8$^+$   | 3.889                  | 8$^+$   | 4.023                  |
|         | -              | 10$^+$  | 4.051           | 10$^+$  | 4.235          | 10$^+$  | 4.199                  | 10$^+$  | 4.211                  |

Fig. 4. Same as figure 1 for $^{108}$Sn.

calculations for $^{108}$Sn, the calculations have been performed by imposing restriction of maximum two particles in $h_{11/2}$ orbital to tackle dimension of matrices. For the sn100pn interaction, the calculated $2^+$, $4^+$, $6^+$, $8^+$ and $10^+$ states are predicted at 1186, 2142, 2297, 3502 and 4051 keV corresponding to experimental value of 1207,
Table 6. Experimental and theoretical low-lying states (up to 2.5 MeV) of $^{103}$Sn. Energies are in MeV.

| $J^\pi$ | Exp. | $J^\pi$ sn100pn | $J^\pi$ | $J^\pi$ snet | $J^\pi$ sn100pn(mod.) | $J^\pi$ | $J^\pi$ snet(mod.) |
|---------|------|-----------------|---------|-------------|-----------------------|---------|-----------------|
| (5/2$^+$) | 0.000 | 5/2$^+$ | 0.000 | 5/2$^+$ | 0.000 | 5/2$^+$ | 0.000 |
| (7/2$^+$) | 0.168 | 7/2$^+$ | 0.026 | 7/2$^+$ | 0.077 | 7/2$^+$ | 0.107 | 7/2$^+$ | 0.254 |
| (11/2$^+$) | 1.486 | 5/2$^+$ | 1.124 | 3/2$^+$ | 1.068 | 1/2$^+$ | 1.267 | 3/2$^+$ | 0.920 |
| (13/2$^+$) | 1.785 | 1/2$^+$ | 1.186 | 5/2$^+$ | 1.241 | 5/2$^+$ | 1.268 | 5/2$^+$ | 1.351 |
| - | 7/2$^+$ | 1.307 | 9/2$^+$ | 1.399 | 3/2$^+$ | 1.325 | 3/2$^+$ | 1.420 |
| - | 3/2$^+$ | 1.355 | 1/2$^+$ | 1.512 | 9/2$^+$ | 1.430 | 1/2$^+$ | 1.550 |
| - | 9/2$^+$ | 1.395 | 7/2$^+$ | 1.521 | 3/2$^+$ | 1.435 | 9/2$^+$ | 1.587 |
| - | 11/2$^+$ | 1.635 | 11/2$^+$ | 1.601 | 11/2$^+$ | 1.647 | 11/2$^+$ | 1.668 |
| - | 9/2$^+$ | 1.717 | 9/2$^+$ | 1.612 | 9/2$^+$ | 1.663 | 1/2$^+$ | 1.865 |
| - | 1/2$^+$ | 1.749 | 1/2$^+$ | 1.660 | 1/2$^+$ | 1.784 | 15/2$^+$ | 1.885 |
| - | 11/2$^+$ | 1.763 | 11/2$^+$ | 1.751 | 11/2$^+$ | 1.799 | 13/2$^+$ | 1.904 |
| - | 13/2$^+$ | 1.798 | 17/2$^+$ | 1.925 | 15/2$^+$ | 1.839 | 11/2$^+$ | 1.925 |
| - | 17/2$^+$ | 1.876 | 13/2$^+$ | 1.931 | 13/2$^+$ | 1.840 | 13/2$^+$ | 1.982 |
| - | 15/2$^+$ | 1.924 | 15/2$^+$ | 1.938 | 17/2$^+$ | 1.918 | 17/2$^+$ | 2.085 |
| - | 15/2$^+$ | 2.066 | 15/2$^+$ | 2.010 | 13/2$^+$ | 2.079 | 15/2$^+$ | 2.252 |

2111, 2365, 3561 and 4256 keV. It has been observed that experimental levels are in much better agreement from sn100pn as well as snet interactions as compared to the previous work done by Dikmen\cite{15}. In general, the calculations performed with new single particle energies\cite{18}, significantly improve the predictive power of calculations as compared to the calculations performed with previously taken single particle energies.

3.2. Excitation energies of odd Sn isotopes

The calculated energy spectra for odd $^{103-107}$Sn isotopes are shown in Figs. 5-6. In the present calculations the energy spectra are plotted up to 2.5 MeV excitation energy whereas previous calculations were reported up to 2 MeV. Here, we have extended the calculations with better agreement from experimental data for odd A Sn isotopes. Some characteristic features have been reported ahead.

In Table 6, we have listed all experimentally known and calculated low-lying states for $^{103}$Sn. Experimentally, only three excited states $7/2^+$, $11/2^+$ and $13/2^+$ are known above the ground state $5/2^+$. From Fig. 5 we can see that in both sets of calculations, the splitting of two low-lying states $5/2^+$ and $7/2^+$, which are essentially single particle in nature, is underestimated by $\sim 140$ and $\sim 90$ keV from sn100pn and snet interactions whereas, from recently observed single particle energies\cite{18}, this improves with the difference of $\sim 60$ keV and $\sim 85$ keV, respectively from both interactions. Above $7/2^+$, experimentally their is large pronounced gap of about 1.3 MeV from the first $11/2^+$ state. This is well reproduced by both the interactions. Our calculations predict many more levels as compared to the levels observed experimentally.

Fig. 6 compares the experimental and theoretical low lying states of $^{105}$Sn and corresponding excitation energies are tabulated in Table 7. Experimentally, the first
Shell model description of $^{102-108}$Sn isotopes

Fig. 5. Experimental and calculated energy levels of $^{103}$Sn with sn100pn and snet interactions.

Fig. 6. Same as figure 1 for $^{105}$Sn.

$7/2^+$ state lies at 200 keV above the $5/2^+$ ground state, which is reproduced very well with the modified single particle energies in both the interactions. The levels observed above the $7/2^+$ are reproduced by both interactions within reasonable
Trivedi, Srivastava, Negi and Mehrotra

Table 7. Experimental and theoretical low-lying states (up to 2.5 MeV) of $^{105}\text{Sn}$. Energies are in MeV.

| $J^\pi$ | Exp. $^\text{a}$ | $^\text{b}$ | sn100pn | $^\text{c}$ | snet | $^\text{d}$ | sn100pn(mod.) | $^\text{e}$ | snet(mod.) |
|---------|-----------------|-----------|----------|-----------|-------|----------|----------------|-----------|------------|
| $(5/2^+)$ | 0.000 | 5/2$^+$ | 0.000 | 5/2$^+$ | 0.000 | 5/2$^+$ | 0.000 | 5/2$^+$ | 0.000 |
| $(7/2^+)$ | 0.200 | 7/2$^+$ | 0.130 | 7/2$^+$ | 0.141 | 7/2$^+$ | 0.193 | 7/2$^+$ | 0.223 |
| $(9/2^+)$ | 1.195 | 3/2$^+$ | 0.887 | 3/2$^+$ | 1.027 | 3/2$^+$ | 0.840 | 3/2$^+$ | 1.023 |
| $(11/2^+)$ | 1.394 | 5/2$^+$ | 0.942 | 5/2$^+$ | 1.144 | 5/2$^+$ | 0.998 | 5/2$^+$ | 1.172 |
| $(13/2^+)$ | 1.849 | 1/2$^+$ | 1.016 | 5/2$^+$ | 1.199 | 1/2$^+$ | 1.105 | 5/2$^+$ | 1.253 |
| $(15/2^+)$ | 1.916 | 3/2$^+$ | 1.177 | 1/2$^+$ | 1.254 | 3/2$^+$ | 1.210 | 1/2$^+$ | 1.302 |
| $(17/2^+)$ | 2.031 | 9/2$^+$ | 1.385 | 1/2$^+$ | 1.450 | 9/2$^+$ | 1.353 | 7/2$^+$ | 1.506 |
| $(19/2^+)$ | 2.168 | 11/2$^+$ | 1.449 | 9/2$^+$ | 1.473 | 11/2$^+$ | 1.475 | 9/2$^+$ | 1.520 |
| $(21/2^+)$ | 2.204 | 1/2$^+$ | 1.501 | 7/2$^+$ | 1.500 | 1/2$^+$ | 1.536 | 11/2$^+$ | 1.592 |
| $(23/2^+)$ | - | 7/2$^+$ | 1.553 | 9/2$^+$ | 1.579 | 7/2$^+$ | 1.558 | 9/2$^+$ | 1.598 |
| $(25/2^+)$ | - | 9/2$^+$ | 1.692 | 11/2$^+$ | 1.589 | 9/2$^+$ | 1.708 | 1/2$^+$ | 1.628 |
| $(27/2^+)$ | - | 15/2$^+$ | 1.976 | 13/2$^+$ | 1.878 | 15/2$^+$ | 1.970 | 13/2$^+$ | 1.869 |
| $(29/2^+)$ | - | 13/2$^+$ | 2.000 | 13/2$^+$ | 1.962 | 13/2$^+$ | 1.974 | 13/2$^+$ | 2.004 |
| $(31/2^+)$ | - | 11/2$^+$ | 2.066 | 11/2$^+$ | 2.017 | 11/2$^+$ | 2.070 | 15/2$^+$ | 2.017 |
| $(33/2^+)$ | - | 13/2$^+$ | 2.147 | 15/2$^+$ | 2.043 | 13/2$^+$ | 2.155 | 15/2$^+$ | 2.050 |
| $(35/2^+)$ | - | 17/2$^+$ | 2.267 | 15/2$^+$ | 2.143 | 15/2$^+$ | 2.262 | 15/2$^+$ | 2.219 |
| $(37/2^+)$ | - | 15/2$^+$ | 2.271 | 17/2$^+$ | 2.147 | 17/2$^+$ | 2.276 | 17/2$^+$ | 2.219 |

Fig. 7. Same as figure 1 for $^{107}\text{Sn}$.

accuracy. In comparison to the previous work by Schubert et al.\[14\], our calculations predict much better spectra.

In Table 8, we have listed experimental and theoretical low lying states of $^{107}\text{Sn}$ and corresponding levels are drawn in Fig. 7. We have extended the calculations performed by Dikmen\[15\] to higher spin states. Dikmen has performed the shell
Table 8. Experimental and theoretical low-lying states (up to 2.5 MeV) of $^{107}$Sn. Energies are in MeV.

| $J^p$ | Exp. $J^p$ | sn100pn $J^p$ | snet $J^p$ | sn100pn(mod.) $J^p$ | snet(mod.) $J^p$ |
|-------|------------|----------------|-------------|---------------------|--------------------|
| (5/2$^+$) | 0.000 5/2$^+$ | 0.000 5/2$^+$ | 0.000 5/2$^+$ | 0.000 5/2$^+$ | 0.000 5/2$^+$ |
| (7/2$^+$) | 0.151 7/2$^+$ | 0.186 7/2$^+$ | 0.116 7/2$^+$ | 0.116 7/2$^+$ | 0.210 7/2$^+$ |
| (3/2$^+$) | 0.704 3/2$^+$ | 0.761 3/2$^+$ | 1.002 3/2$^+$ | 1.002 3/2$^+$ | 0.775 3/2$^+$ |
| (5/2$^+$) | 0.818 5/2$^+$ | 0.905 5/2$^+$ | 1.047 5/2$^+$ | 1.047 5/2$^+$ | 0.210 5/2$^+$ |
| (3/2$^+$) | 1.221 3/2$^+$ | 1.133 3/2$^+$ | 1.148 3/2$^+$ | 1.148 3/2$^+$ | 1.012 3/2$^+$ |
| (5/2$^+$) | 1.280 5/2$^+$ | 1.284 5/2$^+$ | 1.453 5/2$^+$ | 1.453 5/2$^+$ | 1.155 5/2$^+$ |
| (11/2$^+$) | 1.470 11/2$^+$ | 1.377 9/2$^+$ | 1.477 7/2$^+$ | 1.477 7/2$^+$ | 1.450 9/2$^+$ |
| (3/2$^+$) | 1.454 3/2$^+$ | 1.445 3/2$^+$ | 1.578 11/2$^+$ | 1.578 11/2$^+$ | 1.476 11/2$^+$ |
| (13/2$^+$) | 2.009 13/2$^+$ | 1.683 9/2$^+$ | 1.709 9/2$^+$ | 1.709 9/2$^+$ | 1.647 9/2$^+$ |
| (15/2$^+$) | 2.065 3/2$^+$ | 1.780 3/2$^+$ | 1.740 11/2$^+$ | 1.740 11/2$^+$ | 1.630 11/2$^+$ |
| (15/2$^+$) | 2.142 11/2$^+$ | 2.189 13/2$^+$ | 2.007 15/2$^+$ | 2.007 15/2$^+$ | 2.200 13/2$^+$ |
| (17/2$^+$) | 2.206 15/2$^+$ | 2.232 13/2$^+$ | 2.080 13/2$^+$ | 2.080 13/2$^+$ | 2.056 13/2$^+$ |
| - - | - - | - - | - - | - - | - - |
| - - | - - | - - | - - | - - | - - |
| - - | - - | - - | - - | - - | - - |
| - - | - - | - - | - - | - - | - - |

model calculation for low lying levels using CD Bonn potential and Nijmegen11 interactions. In our calculations, using sn100pn interaction we have better agreement for low-lying states, whereas for levels above 11/2$^+$, ordering is well reproduced but values are slightly over predicted. However, calculations performed using snet interaction are able to explain low-lying states as well as higher-lying levels with better accuracy. Hence it is required to retune the TBME or readjust the single particle energies in sn100pn interaction.

4. Electromagnetic transition strengths

The reduced transition probabilities $B(E2; 0^+_g \rightarrow 2^+_1)$, obtained from calculation with the experimental value [9,10], are shown in Table 9. The neutron effective charge used in the present calculation is 1.0e, same as used in Refs. [9,10]. The results obtained from both the interactions have almost similar pattern and increase in $B(E2)$ values have been observed with increasing neutron number, which is a signature for enhancement in collectivity.

5. Conclusion

The shell model calculations for Sn isotopes with $A = 102-108$, have been performed in $sd_{5/2}g_{9/2}$ valence space with two different types of interactions. Theoretical calculations show better agreement for even Sn isotopes with experimental data as compared to odd Sn isotopes. In general, the present calculations are in better agreement with experimental data with sn100pn interactions as compared to the snet interaction. However, the results of sn100pn interaction with modified single particle energies improves the calculations significantly. It is observed that overall
Table 9. Comparison of the $B(E2; 0^+_g \rightarrow 2^+_1)$ values, obtained from the shell model calculations with the experimental values in $e^2b^2$ for even Sn isotopes. The experimental values have been taken from [11,12].

| Isotope | Exp. | sn100pn | snet |
|---------|------|---------|------|
| $^{102}$Sn | - | 0.039 | 0.041 |
| $^{104}$Sn | - | 0.090 | 0.083 |
| $^{106}$Sn | 0.240 | 0.138 | 0.116 |
| $^{108}$Sn | 0.230 | 0.176 | - |

Agreement between theory and experimental data are quite satisfactory. Further, more experimental data is needed for lighter Sn isotopes for making more complete assessment of the calculations.

Acknowledgements

Discussions with Dr. Sandeep Ghugre, UGC-DAE-CSR, Kolkata, India, is gratefully acknowledged. P.C.S. acknowledges support from Conacyt, Mexico, and by DGAPA, UNAM project IN103212.

References

1. T. Otsuka et al., Phys. Rev. Lett. 104 (2010) 012501; A. Gade and T. Glasmacher, Prog. Part. Nucl. Phys. 60 (2008) 161; O. Sorlin and M.-G. Porquet, Prog. Part. Nucl. Phys. 61 (2008) 602.
2. P. Federman and S. Pittel, Phys. Rev. C20 (1979) 0820.
3. R. Wadsworth et al., Phys. Rev. C53 (1996) 2763.
4. A. Gadea et al., Phys. Rev. C55 (1997) 1(R).
5. T. Faestermann et al., Eur. Phys. J. A15 (2002) 185.
6. C. Fahlander et al., Phys. Rev. C63 (1996) 021307(R).
7. M. Görskia et al., Phys. Rev. C58 (1998) 108.
8. S. Juutinen et al., Nucl. Phys. A617 (1997) 74.
9. A. Banu et al., Phys. Rev. C72 (2005) 061305(R).
10. C. Vaman et al., Phys. Rev. Lett. 99 (2007) 162501.
11. J. J. Ressler et al., Phys. Rev. C65 (2002) 044330.
12. T. Engeland et al., Phys. Scr. T56 58 (1995).
13. A. Covello et al., Prog. Part. Nucl. Phys, Vol 38 (1997) 162.
14. R. Schubart et al., Z. Phys. A352 (1995) 373.
15. E. Dikmen Commun. Theor. Phys. 51 (2009) 899.
16. B. A Brown et al., Phys. Rev. C71 (2005) 044317.
17. R. Machleidt, F. Sammarruca, and Y. Song, Phys. Rev. C53 (1996) R1483.
18. I.G. Darby et al., Phys. Rev. Lett. 105 (2010) 162502.
19. A. Hosaka et al., Nucl. Phys. A444 (1985) 76.
20. B. A Brown et al., Phys. Rev. C50 (1994) 2270(R).
21. B. A Brown and W. D. M. Rae, Nushell@MSU, MSU-NSCL report (2007).
22. M. Lipoglavsek et al., Phys. Lett. B440 (1998) 246.
23. T. Ishii et al., Z. Phys. A347 (1993) 41.