Magnetic phase diagram of the $S = 1/2$ triangular layered compound NaNiO$_2$: a single crystal study

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Received 9 November 2009, in final form 10 January 2010
Published 8 March 2010
Online at stacks.iop.org/JPhysCM/22/126001

Abstract
Using magnetic torque measurements on a NaNiO$_2$ single crystal, we have established the magnetic phase diagram of this triangular compound. It presents five different phases depending on the temperature (4–300 K) and magnetic field (0–22 T) revealing several spin reorientations coupled to different magnetic anisotropies.

(Some figures in this article are in colour only in the electronic version)

1. Introduction
In magnetic systems with a two-dimensional triangular lattice, magnetic frustration may occur depending on the nature of the magnetic interactions and the orbitals involved. The case of LiNiO$_2$, where Ni$^{3+}$ has half filled e$_g$ orbitals, has long been studied both experimentally and theoretically [1]. Recent progress on the understanding of the orbital and magnetic properties of this compound has been achieved thanks to an appropriate control of the non-stoichiometry or doping effects, since no pure samples are available. Indeed magnetic Ni$^{2+}$ ions are substituted between the triangular planes on the Li sites, creating new magnetic exchange paths. It has been shown that Li$_{1-x}$Ni$_{1+x}$O$_2$ with $x = 0.01$ does not show long range magnetic order. Rather, a fluctuating state develops which is slowed down when Mg doping is introduced and no interplane Ni$^{2+}$ are present [2]. When Li is deintercalated, in Li$_{1-x}$Ni$_{1+x}$O$_2$, short range incommensurate antiferromagnetic order is observed for $x = 3/4$ and $2/3$ [3]. As for the orbital part, several experimental works are in favor of the $|3z^2-r^2\rangle$ orbital occupancy for the e$_g$ electrons with finite range order [4] or dynamical effects [2]. Such an occupancy is indeed observed unambiguously in the parent compound NaNiO$_2$, which seems to behave more classically. It orders ferro-orbitally below $\sim$480 K [5] and antiferromagnetically below 20 K [6]. Here, we present the first single crystal study of its magnetic phase diagram up to 20 T using torque measurements. We show that several spin reorientations with unusual magnetic anisotropy occur as a function of temperature or magnetic field.

2. State of the art on NaNiO$_2$
NaNiO$_2$ crystallizes in the $R\bar{3}m$ space group and, below the ferro-orbital ordering temperature, becomes monoclinic (C$2/m$) with $a = 5.3087$ Å, $b = 2.8413$ Å, $c = 5.5670$ Å, and $\beta = 110.45^\circ$ [7]. The two-dimensional triangular network of Ni$^{3+}$ then becomes distorted to accommodate the collective elongation of the oxygen octahedra surrounding the Ni ions (figure 1). At room temperature, the distorted triangles are described by two angles at 56.3$^\circ$ and 61.8$^\circ$ and two Ni–Ni distances at 2.84 and 3.01 Å. From one triangular plane to the other, the Ni–Ni distance is 5.47 Å. The antiferromagnetic ground state, observed below $T_N$, is of the A type with a ferromagnetic alignment of the Ni spins in the triangular plane and an antiferromagnetic alignment from one plane to the other. The magnetic moments point at 80$^\circ$ from the triangular planes. The Curie–Weiss behavior of the magnetic susceptibility above 100 K leads to ferromagnetic dominant interactions with a Curie-temperature $\theta = +36$ K. Below the ordering temperature ($T_N = 20$ K), application of a magnetic field reveals a spin flop transition at $\mu_0 H_{c1} = 1.8$ T [6] for $T = 4$ K and another transition at $\mu_0 H_{c2} = 8$ T [9, 10]. Spin wave measurements agree with an easy plane A type antiferromagnet model, although there are some discrepancies between the
3. Synthesis of NaNiO₂ single crystals

NaNiO₂ single crystals have been grown by the molten hydroxide flux method. The flux composition was NaOH and KOH, and a Ni crucible played the role of the Ni source. As a preliminary step, 61.6 g of a NaOH–KOH mixture (molar ratio 1:2) was melted in a separate Ni crucible at 400 °C. The molten mixture was then poured in another 40 ml Ni crucible and placed in a preheated open vertical furnace. The experiment was carried out at 650 °C. The evaporation of the NaOH–KOH mixture at the liquid surface induces a local saturation, then nucleation and crystal growth. Runs were stopped once an abundant 'crust' was observed covering the flux surface (typically after 12 h). The crystals were easily separated from the flux with water in an ultrasonic bath. They often take the shape of hexagonal small platelets (figure 2). The crystals were characterized using a scanning electron microscope equipped with the Ni planes. A small anisotropy in the easy plane is then responsible for the spin flop transition at $H_{c1}$.

4. Magnetic torque measurements

A sample with a magnetic moment $\vec{m}$ placed in a magnetic field $\vec{H}$ will experience a torque $\Gamma = \vec{m} \times \vec{H}$ that can be measured using a cantilever (see figure 2). One of the larger crystals was selected (typically 1 mm × 1 mm × 0.2 mm) and glued on a copper–beryllium cantilever with a general electric varnish. Care was taken to avoid contact with air and moisture. The large face of the crystal containing the Ni planes was parallel to the cantilever (x, y) plane so that the z axis coincides with the crystal c' axis (see figure 2). The magnetic field $\vec{H}$ lies in the yz plane, making an angle $\theta$ with the z axis. The cantilever could rotate with regard to the magnetic field so that $\theta$ could be varied from 0° to 90°. The capacitive technique allows the measurement of the torque produced in the x direction: $\Gamma_x = m_x H_z - m_z H_y$, where $m$ is the sample magnetic moment. It is reduced to $\Gamma_x = \Delta \chi H^2 \sin(\theta - \theta_0) \cos(\theta - \theta_0)$ when the sample magnetic moment has a linear dependence on magnetic field. $\Delta \chi$ is the difference of the magnetic susceptibility parallel and perpendicular to the z axis; $\theta_0$ is the spin direction in the absence of torque. When the magnetization is saturated, the torque should vanish, except for g factor anisotropy effects, which should be negligible compared to $\Delta \chi$ effects in the ordered magnetic phase.

The expected torque for $\theta = 0^\circ$ using the easy plane model, with the small anisotropy described above, is given in figure 3(a), assuming that the z direction coincides with the spin direction. In the experiment, there is a 10° difference. Because of the crystal twinning, the x and y directions are not crystallographically well defined. This means that the measurement gives the average of $\Gamma_x$ and $\Gamma_y$. In these calculations, the torque has a quadratic dependence on the magnetic field, with a change of sign and magnitude at the spin flop field ($\mu_0 H_{c1} = 1.8$ T), and vanishes at either $H_{c2}$ or $H_E$. We, therefore, expect to observe three different regimes labeled (a), (b) and (c) in figure 3(a). The measured data are reproduced in figure 3(b). Four different regimes are observed with no saturation. Regime (1) has the expected quadratic field dependence and can be identified as regime (a). It disappears at $H_{c1}$ to enter regime (2) with a change of slope, both in sign and magnitude, as expected for regime (b). This transition is widened, probably due to thermal effects. Regime (b) is in fact divided in two parts, (2) and (3), with similar magnetic field dependencies. Note that the quadratic field dependence for these regimes does not extrapolate to zero, as calculated in regime (b), but rather there is an internal torque which has different values for regimes (2) and (3). This unexpected zero field torque can exist if the extrapolated zero
Figure 3. Magnetic field dependence of the torque on a NaNiO$_2$ crystal: (a) calculation within the easy plane model, (b) measurements and second order polynomial fits. Insets: derivative of the torque.

Field magnetization is not zero (in a canted antiferromagnet for instance), or there exist local fields that are not collinear with the sample magnetization (dipolar fields due to twinning or other anisotropic fields, due to crystal field effects for instance). The presence of two regimes, instead of one, suggests that there is a change in the anisotropy fields, i.e. a spin reorientation.

The highest field regime observed, regime (4), does not saturate at all, contrary to what has been calculated for regime (c).

The presence of an incommensurate magnetic phase is ruled out, since neutron diffraction data at zero field are unambiguously fitted within a commensurate magnetic structure. On the other hand, 110$^\circ$ is exactly the monoclinic (a, c) angle of the crystal structure. Macroscopic effects linked to twinning are then probably responsible, but difficult to evaluate due to the low symmetry of the system. Note that the critical field at which this regime disappears has the following angular dependence:

$$H_{c1}(\theta) = \frac{H_{c1}}{\cos(\theta - \theta_{01})}$$

with $\theta_{01} = -10^\circ$, in agreement with previous measurements [1, 6]. The free spin direction is at $\theta_{01} = -10^\circ$, in agreement with the neutron diffraction data [7].

Regime (3) has the correct angular dependence:

$$H_{c3}(\theta) = \frac{H_{c3}}{\cos((\theta - \theta_{02})/2)}$$

with $\theta_{02} = -10^\circ$ and $\theta_{03} = +30^\circ$. This confirms the spin reorientation process from regime (2) to (3).

Finally, regime (4) follows the $\sin(\theta - \theta_0)\cos(\theta - \theta_0)$ law, with $\theta_0$ close to 0$^\circ$. We have checked that the field dependence remains the same for all angles, with a constant value for $\mu_0H_{c4}$ around 20 T.

5. Discussion

These torque measurements on a twinned crystal reveal that the NaNiO$_2$ system presents several spin reorientations and very unusual magnetic anisotropies depending on magnetic
field. The modeling is quite complex due to the low crystal symmetry of the compound (monoclinic unit cell) and the presence of three types of twins. Nevertheless, we can establish a magnetic phase diagram using these torque measurements at different temperatures (see figure 5). As the ordering temperature is approached, regime (1) disappears altogether, while regimes (2) and (3) merge into another regime. Note that the torque diminishes as the temperature increases but has still a non-vanishing field dependence. We checked that it behaves as \( \Gamma_1 = \Delta \chi H^2 \sin(\theta - \theta_0) \cos(\theta - \theta_0) \) and noticed that \( \Delta \chi \) decreases exponentially with an activation energy exactly equal to the Curie–Weiss temperature +36 K (see the inset of figure 5). One concludes that there is a magnetic anisotropy induced by the exchange energy. It is responsible for the high field torque observed at low temperature, which tends to vanish only above \( H_{c4} \).

We can now establish the magnetic phase diagram. We have plotted, in figure 6, the critical fields obtained in this work, as well as in previous studies mainly on powder samples [9, 11], except for the first magnetization measurements, which were taken on a twinned crystal up to 3 T [6]. At low temperature, five phases are present: phase (1) where the spin lies at 10° from the Ni plane, phases (2) and (3) with different spin orientations, and finally phases (4) and (5), which are close to full saturation. Phases (1)–(3) disappear at \( T_N = 20 \) K, but a crossover line persists above. This phase diagram was obtained when the magnetic field was at 10° from the z axis. All the boundary lines correspond to a good approximation, to the phase diagram when the magnetic field lies in the free spin direction i.e. \(-10°\) for phase (1), \(+30°\) for phase (3), except for the transition between phase (4) and (0) where the border line shifts to lower temperatures when \( \theta \) is changed, in agreement with the specific heat data on a powdered sample [9], where a quasi-vertical line is observed. While most of the phase diagram was already established, we have shown, using torque measurements on a crystal, that two additional phases are present at low temperature, phases (3) and (5). The transition line to phase (5), \( H_{c4}(T) \), is obtained from the fit of the torque field variations. Since it is not a direct experimental measurement, its uncertainty is wider than for \( H_{c1}, H_{c2} \) and \( H_{c3} \). Note that \( H_{c4} \approx 20 \) T corresponds to an energy for the \( S = 1/2 \) Ni\(^{2+}\) spin of the order of 20 K, the same order of magnitude as the observed anisotropy activation energy and Curie–Weiss temperature of 36 K. As for the transition lines \( H_{c2}(T) \) and \( H_{c3}(T) \), which are quite close, it is tempting to identify them with the two zero field modes at 6.5 and 9.0 cm\(^{-1}\) observed in the electron spin resonance measurements on a powdered sample at 4 K [10]. The associated magnetic fields can be matched to \( H_{c2} \) and \( H_{c3} \) assuming a gyromagnetic factor \( g \approx 2.6 \), in reasonable agreement with the observed \( g \) value at 200 K: \( g_\parallel = 2.03 \) and \( g_\perp = 2.28 \). This suggests that both \( H_{c2} \) and \( H_{c3} \) are associated with the same crystallographic plane as \( g_\perp \) (perpendicular to the elongation axis of the oxygen octahedra). Note also that the presence of these two modes at 6.5 and 9.0 cm\(^{-1}\) cannot be explained in an easy plane A type antiferromagnetic model with only two magnetization sublattices [10]. The inadequacy of this model is confirmed by our torque measurements in

![Figure 5](image1.png)

**Figure 5.** Magnetic field dependence of the torque at different temperatures. Inset: torque parameter \( \Delta \chi \) as a function of temperature, the red line is an exponential fit.

![Figure 6](image2.png)

**Figure 6.** Magnetic phase diagram of NaNiO\(_2\) from crystal torque measurements obtained at \( \theta = 10° \), heat capacity [9] and magnetization [6, 11] measurements.
regimes (2) and (3), where an internal torque has to be added to the model.

6. Conclusion

The magnetic study of a millimeter size NaNiO$_2$ crystal was achieved successfully using torque measurements. We have established the presence of five different ordered phases with different spin orientations and magnetic anisotropies. The corresponding critical magnetic fields are 1.8, 5.1, 7.4 and \( \sim 20 \) T at 4 K. These reflect the presence of several characteristic energies in the system at around 2.5, 7.5, 11 and 30 K. A more complex behavior is observed than a simple easy plane A type antiferromagnet, with probably different possible magnetic ground states quite close in energy.

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