Optical polarization and intervalley
scattering in single layers of MoS$_2$
and MoSe$_2$

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Single layers of MoS$_2$ and MoSe$_2$ were optically pumped with circularly polarized light and an
appreciable polarization was initialized as the pump energy was varied. The circular polarization of
the emitted photoluminescence was monitored as a function of the difference between the excitation
energy and the A-exciton emission at the K-point of the Brillouin zone. Our results show a threshold
of twice the LA phonon energy, specific to the material, above which phonon-assisted intervalley
scattering causes depolarization. In both materials this leads to almost complete depolarization within
~100 meV above the threshold energy. We identify the extra kinetic energy of the exciton (independent
of whether it is neutral or charged) as the key parameter for presenting a unifying picture of the
depolarization process.

Materials often exhibit fundamentally new phenomena in reduced dimensions, and the new properties that
emerge can lead to novel applications. Like graphite, the molybdenum-based transition metal dichalcogenides,
MoX$_2$ (X = S, Se) are a class of materials that readily lend themselves to dimensional manipulation. These layered
structures have strong intralayer bonding and weak interlayer van der Waals coupling, enabling one to isolate
individual layers. In bulk form, MoX$_2$ are indirect gap semiconductors. However, because of their reduced dimen-
sionality, single layers are direct-gap with a range of bandgaps in the visible regime. This makes them ideal candi-
dates for a host of optoelectronic applications ranging from light-emitting diodes to light harvesting to sensors$^1$–$^3$.

Besides the obvious light-based applications, these materials are also good candidates for the emerging field of
valleytronics$^6$–$^{12}$. The reduced-dimensional, hexagonal lattice leads to non-degenerate K-points in the Brillouin
zone making the inequivalent K and K’ valley populations potential new state-variables of these systems.

A single layer of MoX$_2$, schematically shown in Fig. 1(a), consists of a plane of transition metal atoms sand-
wiched by layers of chalcogen atoms. The Brillouin zone of this system is shown in Fig. 1(b). In single layer
form, the direct gap occurs at the K-point, and the optical properties of these materials are governed by strong
excitonic transitions, both neutral and charged. These excitons are strongly bound, with the neutral exciton hav-
ing binding energies on the order of 0.5–0.8 eV$^{15,17}$ and the charged exciton (trion) having a binding energy of
20–30 meV$^{18}$. In addition to being optically active with strong photoluminescence (PL), they also have unique
optical selection rules (Fig. 1(c)). Time reversal symmetry and strong orbital–hybridization couples the valley and
spin indices. This enables access to a single valley using polarized light, since the angular momentum of incident
circularly-polarized light interacts with carriers to produce specific spin states$^8$–$^{11,15,20}$. In other words, the sym-
metry properties of the two inequivalent valleys lead to a difference in the absorption of circularly polarized light,
either positive ($\sigma^+$) or negative ($\sigma^-$) helicity, resulting in a strong chiral selectivity.

Polarization-resolved photoluminescence of single layer MoS$_2$ has been extensively studied, and a high
initial circular polarization was reported with a circularly polarized pump$^8$–$^{19}$. In contrast, there are few
polarization-dependent studies for MoSe$_2$ at zero magnetic field. One recent study$^{21}$ reported very low initial
circular polarization in the PL. This result is surprising since one expects members of the MoX$_2$ family to behave
similarly. Several other recent studies$^{22,23}$, demonstrated generation of valley polarization in MoSe$_2$ by applying
external magnetic fields up to 10 T perpendicular to the sample. In particular, MacNeil et al.$^{22}$ observed a maxi-
mum polarization of 14% for the charged and 9% for the neutral exciton at 4.2 K and 6.7 T attributed to the mag-
netic field breaking the K/K’ valley-degeneracy.

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The width of the emission from MoS2 at the K-point of the Brillouin zone (see Fig. 1(c)). At low temperature, we measure the A-exciton at 1.89 eV for (532 nm). The dominant emission peak is the A-exciton, a feature that originates from the lowest energy transition.

Temperature dependent PL emission from MoS2 and MoSe2 are shown in Fig. 3(a,b), respectively (full experimental details are described elsewhere)\(^1\). In these spectra, the samples were excited with a laser at 2.33 eV (532 nm). The dominant emission peak is the A-exciton, a feature that originates from the lowest energy transition at the K-point of the Brillouin zone (see Fig. 1(c)). At low temperature, we measure the A-exciton at 1.89 eV for MoS2, and at 1.625 eV for MoSe2, reflective of the smaller bandgap of MoSe2. The width of the emission from MoS2 is very broad (FWHM = 0.09 eV) so it is not possible to distinguish features within the spectra and we assign this feature to the neutral exciton, X\(^0\). However, the emission from MoSe2 is much narrower (FWHM = 0.01 eV), and it is possible to distinguish two clear peaks separated by 0.03 eV that become apparent as the sample is heated (Fig. 3(b)). These peaks have been identified as a neutral exciton (X\(^0\)) and a charged exciton (T)\(^0\). It is not possible to determine whether the lower energy peak is a positive or negative charged exciton based solely on the emission energy, because the effective mass of electrons and holes in this material is similar.

As the temperature is increased the relative luminescence of charged vs. neutral exciton changes, with the neutral exciton eventually becoming the dominant feature. Note that the charged exciton is still visible at temperatures much higher than is seen in other quasi-2D systems such as GaAs QWs\(^2\). The temperature dependence of the exciton emission channels for both systems shows a typical semiconductor behavior (Fig. 3(c,d), solid...
symbols) and the data can be fit using a standard hyperbolic cotangent relation as defined by O’Donnell and Chen\(^3\). The solid lines are the fits to the data with the function \( E(T) = E(0) - S \langle \hbar \omega \rangle \left[ \coth \left( \langle \hbar \omega \rangle / 2 kT \right) - 1 \right] \) where \( E(0) \) is the energy position of a given feature at zero temperature, \( S \) is a dimensionless coupling constant, and \( \langle \hbar \omega \rangle \) is an average phonon energy. The fitting parameters obtained here are \( S = 1.16 \) (2.18) and \( \langle \hbar \omega \rangle = 19 \) meV (14.5 meV) for MoS\(_2\) (MoSe\(_2\)).

To examine the valley spin dynamics, we measure the helicity dependent PL from these monolayers. Because of the optical selection rules (Fig. 1(c)), when pumped with light of positive (\( \sigma^+ \)) or negative (\( \sigma^- \)) helicity, either the K or K’ valley will be selectively populated\(^6\). Information on the depolarization process comes from analyzing the polarization of the subsequent PL. Figure 4(a,b) show representative PL spectra analyzed for \( \sigma^+ \) (solid red line) and \( \sigma^- \) (dashed blue line) at \( T = 5 \) K for MoS\(_2\) and MoSe\(_2\), respectively, at selected \( \sigma^+ \) excitation energies. By using a combination of sharp, long-pass filters, stray light was suppressed at the spectrometer entrance. In addition, as the excitation energy approached the PL emission energy, the excited Raman modes were cut-off from entering the detection system. This experimental setup limited our lowest excitation energies to 1.984 eV (625 nm) for MoS\(_2\) and 1.722 eV (720 nm) for MoSe\(_2\). It is clear from Fig. 4 that, for both materials, the higher the excitation energy, the lower the polarization of the emission\(^3\).

The degree of circular polarization is shown in Fig. 5 as a function of the excess energy, \( \Delta E = E_{\text{pump}} - E_{\text{PL}} \), the difference between the excitation energy \( E_{\text{exc}} \) and PL emission energy, \( E_{\text{PL}} \) (the inset of Fig. 5 is a graphical representation). Data are plotted for MoSe\(_2\) (solid red circles) and MoS\(_2\) (solid blue circles) and are derived from spectra where the temperature was held constant and the laser energy was varied, or the laser energy was fixed.
and the emission energy was varied via a change in temperature\textsuperscript{8,11,19}. Since this plot incorporates the energy difference between excitation and PL emission rather than the specific energy of the neutral and charged excitons, the behavior observed for both materials can be shown. Data for MoS\textsubscript{2} from the literature are also plotted in Fig. 5. The open circle, open square with a cross, and open triangle are data from Refs 8,10 and 20, respectively. These data were taken at 5 K with circularly polarized excitation from a HeNe laser (1.96 eV). The open squares with a slash are data from Ref 19 obtained at fixed excitation energy of 1.96 eV but at temperatures ranging from 5 to 300 K. To the best of our knowledge, these data represent the trends seen in the literature for MoS\textsubscript{2}. All data follow the same depolarization trend line when plotted as a function of excess energy. Using this methodology, all of the data collapse onto a single curve for each material, independent of whether the polarization of the trion or neutral exciton is considered. The data clearly demonstrate that as the excess energy increases the emitted circular polarization decreases.

Discussion
To explain this behavior, we begin by noting that due to the optical selection rules\textsuperscript{6} intra-valley scattering cannot result in a reduction in the observed polarization even if the pump energy exceeds the spin-orbit splitting (160 meV for MoS\textsubscript{2}, 180 meV for MoSe\textsubscript{2})\textsuperscript{8}. Therefore, inter-valley scattering is required to account for the reduced polarization observed, and the change in momentum necessary for such scattering implicates a phonon-mediated process\textsuperscript{8,11}. Close to resonance the emitted circular polarization is expected to be essentially 100\%, since there is not enough energy in the system to facilitate intervalley scattering. As the laser excitation energy increases or as the temperature changes for a fixed pumping energy, the available excess energy $\Delta E$ increases and phonon-assisted scattering is enabled above some material-dependent energy threshold. For MoS\textsubscript{2}, the combined data set clearly interpolate to 100\% polarization at $\Delta E = 60$ meV, corresponding to twice the LA phonon energy\textsuperscript{11}.

Intervalley scattering requires participation from in-plane longitudinal phonons. From the phonon-dispersion curves for single layers of MoS\textsubscript{2} and MoSe\textsubscript{2} the lowest energy phonon available for scattering are longitudinal.
Figure 4. Polarization of photoluminescence spectra. PL spectra at T = 5 K analyzed for $\sigma^+$ and $\sigma^-$ at selected photo-excitation energies for (a) MoS$_2$ and (b) MoSe$_2$. The pumping is $\sigma^+$ in both cases. A dramatic decrease in the emitted circular polarization is observed as the excitation energy increases. The peaks were normalized and vertically shifted for clarity. For the MoSe$_2$ spectra, the inset is an enlargement of the area indicated by a rectangular box and shows the neutral exciton emission.

Figure 5. Polarization dependence on excess energy. Degree of circular polarization of the emitted PL as function of excess energy, $\Delta E$. Data are derived from spectra where the temperature was held constant and the laser energy was varied, or the laser energy was fixed and the emission energy was varied via a change in temperature. Solid symbols (MoSe$_2$ is red and MoS$_2$ is blue) are our data, and open symbols are data from references 8,10,19,20. A graphical definition of excess energy is presented in the inset. Except where noted, error bars are not in excess of the symbol size.
acoustic phonons with energies of 30 meV for MoS$_2$ and 19 meV for MoSe$_2$. Intervalley scattering becomes accessible when the excitation energy exceeds a threshold value that is the sum of the exciton Coulombic formation energy (PL emission energy) and twice the lowest acoustic-phonon energy available in the system (essentially a phonon for each the electron and hole). That is 60 meV for MoS$_2$ and 38 meV for MoSe$_2$. There are two mechanisms that could be responsible for the electron or hole spin-flip during this phonon mediated intervalley scattering event. One is that the spin-flip is mediated by short range scattering from impurities. The presence of a background carrier population could enhance the probability of such a process. The other mechanism is that intervalley scattering proceeds through the nearly spin-degenerate Γ valley of the Brillouin zone.

The MoSe$_2$ data (solid red symbols) exhibit a similar behavior – the measured polarization rapidly increases as the excess energy $\Delta E$ decreases. The narrow linewidths in MoSe$_2$ allow us to distinguish the particular emission channels $X^0$ and $T$. Therefore, for MoSe$_2$, we can plot the polarization of both the neutral and charged exciton. Note that due to the low intensity of the $X^0$ data, it is difficult to see the polarization on the same scale as the trion emission, therefore a typical set of $X^0$ emission spectra are shown in the inset of Fig. 4(b). As with MoS$_2$, all the data coalesce onto the same depolarization curve as a function of excess energy. The solid red line is a model fit described below, and intercepts 100% polarization at $\Delta E = 38$ meV, corresponding to twice the MoSe$_2$ LA phonon energy of 19 meV from the literature. These data make it clear that depolarization and intervalley scattering are governed by the excess energy, $\Delta E$, imparted to the photoexcited carriers through optical pumping.

To model this behavior, we begin with a familiar rate equation model in which the emitted circular polarization can be expressed as $P_{\text{circ}} = 1/(1 + 2C)$, where $\tau_1$ is the exciton lifetime and $\tau_2$ the intervalley scattering time. Both $\tau_1$ and $\tau_2$ depend on temperature, or more specifically on the thermal energy given to the exciton during optical excitation. We associate this additional thermal energy with the exciton, $\Delta E$. It has been shown that $\tau_2$ depends linearly on temperature, therefore we expect it to have a linear dependence with $\Delta E$. In addition, the increase in the excess energy leads to an increase of the phonon population. We assign the intervalley scattering rate $\tau_2^{-1}$ to be proportional to the phonon population $\langle n \rangle = 1/(e^{\hbar \omega_q/kT} - 1)$ and substitute $kT$ with $(\Delta E - \hbar \omega_q)$. Taking into account these dependencies on $\Delta E$ we can fit the data using the relation $P = 1/(1 + C\Delta E/(e^{\hbar \omega_q/(\Delta E - \hbar \omega_q)} - 1)).$ Here $\hbar \omega_q$ is the LA phonon energy, the minimum energy necessary for the exciton (electron and hole) to scatter from one valley to the other and reduce the optical polarization, and $C$ is a scaling constant. These two values, $C$ and $\hbar \omega_q$, are the only fitting parameters. Note that this fitting relation is valid only for $\Delta E > \hbar \omega_q$. The solid lines in Fig. 5 are fits to the data and yield values for 2LA of 54 meV for MoS$_2$ and $\pm 4$ meV for MoSe$_2$, in good agreement with the respective literature values of 60 and 38 meV.

The data for MoS$_2$ diverge systematically from the fitted line above 150 meV. The main reason for this discrepancy may be that our simple rate equation model does not take into account the spin-orbit interaction (150 meV for MoS$_2$) and the corresponding material. The exciton kinetic energy greater than this is the key parameter for the depolarization.

Even though the optical response of 2-dimensional crystals is dominated by the formation of excitons, we used the phonon-assisted intervalley scattering model, which is based on a single particle picture. This is a straightforward way to describe the sharp depolarization of the emitted PL as a function of the excess energy that includes a threshold energy. However, the thermally activated relaxation of the carriers may not represent all aspects of physics that could describe the spin relaxation in this system. Recently, alternative interpretations based on the excitonic picture explain the PL depolarization as valley-decoherence due to long-range exciton exchange, i.e., direct intervalley electron-hole exchange. Both of these mechanisms may be at play with different relative contributions that varies across different material systems. Our observation of a threshold depolarization energy, however, is more easily explained with the phonon model we have presented.

In summary, at zero magnetic field, we initialized circular polarization in MoS$_2$ and MoSe$_2$ using energy-dependent circularly-polarized optical pumping and measured the valley polarization process as a function of the excess energy absorbed by the carriers. Independent of the emission channel or the material studied (MoS$_2$ or MoSe$_2$), all the data can be modeled by a single depolarization mechanism, intervalley scattering mediated by LA phonons. The threshold needed for depolarization is found to be twice the LA phonon energy of the corresponding material, and the exciton kinetic energy greater than this is the key parameter for the depolarization. Generating high chirality photoluminescence in Mo-based two-dimensional structures enables applications in valley-photonic.

**Methods**

**Sample preparation and characterization.** All samples used in this study were mechanically exfoliated from bulk crystals. The MoS$_2$ was deposited onto a 285-nm SiO$_2$ layer on a Si substrate, while the MoSe$_2$ flakes were deposited on a 90-nm SiO$_2$ layer on a Si substrate. The typical size of monolayer regions is 5–10 μm across for MoS$_2$ and 1–2 μm for MoSe$_2$, and were identified with an optical microscope and confirmed with Raman spectroscopy at room temperature and 488 nm excitation. Raman spectroscopy has been established as a reliable tool for determining the specific number of layers in transition metal dichalcogenides. In MoS$_2$, the 18 cm$^{-1}$ energy difference between the two main vibrational modes, E'$_{2g}$ at 384 cm$^{-1}$ and A$_g$ at 402 cm$^{-1}$, is the fingerprint for the accurate determination of the single layer. In MoSe$_2$, the in-plane E'$_{2g}$ (287 cm$^{-1}$) and the out-of-plane A$_g$ (242 cm$^{-1}$) modes are much lower in energy than in MoS$_2$ because of the larger mass of the Se atom. Also, the in-plane and out-of-plane modes switch positions relative to the MoS$_2$, i.e., the out-of-plane mode is softer than the in-plane one. This can be verified by measuring thicker layers of MoSe$_2$ and observing a Davydov splitting in the A$_g$ mode for multi-layer flakes. The single layer is identified by the absence of the B$_2g$ mode at 353 cm$^{-1}$.

**Optical measurements.** The photoluminescence data were taken in a backscattering geometry using a micro-PL setup (spatial resolution of 1 μm) with a 50 x objective and incorporating a continuous-flow He-cryostat. The MoS$_2$ samples were excited with either a continuous-wave 2.33 eV (532 nm) solid-state laser or
a tunable pulsed laser while the MoSe₂ flakes were excited by a continuous-wave Ti:Sapphire laser. The pulsed source was an optical parametric amplifier (pumped by a Ti:Sapphire laser) tunable from 1.77–2.48 eV (700–500 nm) at a 250-kHz repetition rate with a double-pass grating (500 g/mm) geometry to reduce the spectral bandwidth to < 5 meV (1 nm). The photoluminescence emission was collected, passed though a polarization analyzer, and dispersed by a single monochromator equipped with a multichannel charge coupled device (CCD) detector.

References

1. Mak, K. F., Lee, C., Hone, J., Shan, J. & Heinz, T. F. Atomically Thin MoSe₂: A New Direct-Gap Semiconductor. Phys. Rev. Lett. 105, 136805 (2010).
2. Splendiani, A. et al. Emerging Photoluminescence in Monolayer MoS₂. Nano Lett. 10, 1271–1275 (2010).
3. Korn, T., Heydrich, S., Hirmer, M., Schmutzler, J. & Schiller, C. Low-temperature photocarrier dynamics in monolayer MoS₂. Appl. Phys. Lett. 99, 102109 (2011).
4. Bernardi, M., Palummo, M. & Grossman, J. C. Extraordinary Sunlight Absorption and One Nanometer Thick Photovoltaics Using Two-Dimensional Monolayer Materials. Nano Letters 13, 3664–3670 (2013).
5. Perkins, F. K. et al. Chemical Vapor Sensing with Monolayer MoSe₂, Nano Letters 13, 668–673 (2013).
Author Contributions
G.K., A.H. and M.C. performed the experiments. G.K., A.H. and M.C. analyzed the data. A.F. fabricated the samples. All authors discussed the results and A.H., G.K., M.C. and B.J. wrote the manuscript.

Additional Information
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