I. INTRODUCTION

The transport gaps measured experimentally in graphene nanoribbons (GNRs) exceed the theoretical electronic confinement gap.\textsuperscript{1,2} This discrepancy is attributed to localized states induced by edge disorder.\textsuperscript{1-4} Most theoretical studies of the electronic transport properties of GNRs assumed simplified edge topologies; see, e.g., Refs. 3–5. However, several experimental studies have characterized individual edge defects by means of Raman spectroscopy, scanning tunneling microscopy, or transmission electron microscopy.\textsuperscript{6–10} The high degree of chemical reactivity of graphene edges favors edge reconstruction with different topologies, some of which were examined in recent \textit{ab initio} calculations\textsuperscript{11–13} Dubois et al.\textsuperscript{14} showed that realistic edge topologies strongly affect electron transport in the armchair GNRs: The conductance can be suppressed by orders of magnitude for either electrons or holes, depending on the defect geometry.\textsuperscript{14} Heptagon defects were found to act as donors and to suppress the electron conductance much more strongly than the hole conductance whereas pentagon defects were found to act as acceptors and to suppress the hole conductance much more strongly than the electron conductance.\textsuperscript{14} This can be understood intuitively since a heptagon (pentagon) carbon ring introduces one more (less) $\pi$ electron into the graphene ribbon $\pi$ bands than does a hexagon ring resulting in donor (acceptor) character of the defect and electron-hole asymmetry in the electronic structure. More recently, a few defect topologies for armchair and zigzag GNRs were studied theoretically in Ref. 15. In contrast to Ref. 14, these authors\textsuperscript{15} reported pentagon and heptagon edge reconstructions to have little effect on the ribbon conductance near the Dirac point.\textsuperscript{16} The origin of this difference between the predictions of these two studies\textsuperscript{14,15} remains unclear. Furthermore, theoretical estimates of the transport gaps in GNRs are still not available for realistic models of edge reconstruction, and the implications for the interpretation of experimental data\textsuperscript{1,2} are yet to be explored. It has also been shown that electron-electron interactions modify electron conduction in GNRs substantially.\textsuperscript{17,18} Specifically, when the electron Fermi level is not at the charge neutrality point, electrons are predicted to accumulate along the edges of the ribbon and therefore any edge imperfection may be expected to play an important role in transport. However, the interplay between this charge redistribution effect and edge reconstruction in the context of transport is yet to be examined either theoretically or experimentally. Thus, the detailed understanding of electron transport in GNRs with realistic topological edge defects is still incomplete.

In this paper we report systematic studies of the electronic transport in realistic edge-disordered GNRs with both zigzag and armchair edges (zGNR and aGNR). Three different defect topologies are examined: pentagon, heptagon, and Stone-Wales. The Stone-Wales mechanism reconstructs zGNR edges into alternating pentagon-heptagon pairs (z57), while in aGNR it causes two separate “armrest” hexagons to merge into adjacent heptagons (a757). To describe realistic defect topologies we first relax the atomic geometries using density functional theory.\textsuperscript{19} We then obtain the tight-binding (TB) parameters for the relaxed geometries from the standard quantum chemical parametrization of the extended Hückel model.\textsuperscript{20,21}

We note that the previous theoretical studies of transport in GNRs with reconstructed topological defects\textsuperscript{14,15} employed TB parameters obtained by fitting tight-binding models to the results of density functional theory (DFT) based calculations in different ways. As we have already mentioned, those transport calculations\textsuperscript{14,15} yielded qualitatively different results. Also, the validity of DFT is limited to \textit{ground-state} properties.\textsuperscript{21} This is a fundamental limitation of DFT that often renders the results of DFT calculations of properties that involve excitations (such as electronic band structures and transport coefficients) unreliable.\textsuperscript{21} For example, DFT calculations
yield semiconductor band gaps that typically differ from the experimental values by factors of the order of 2. For these reasons we chose to base our TB parameters instead on the extended Hückel model whose parameters were derived from a large body of experimental molecular electronic structure data.\textsuperscript{20} We incorporate these TB parameters into the standard TB Hamiltonian of graphene. As will be discussed below, the transport results that we obtained using this TB model agree reasonably well with those in Ref. 14 for the systems that were studied in Ref. 14.

We identify the defect bands in the electronic band structures of the GNRs with reconstructed edge defects and relate strong electron backscattering in these GNRs to the structures of the GNRs with reconstructed edge defects and multiple heptagon defects in aGNRs. Consistent with previous for a representative class of systems with single and multiple heptagon defects in aGNRs. Consistent with previous studies,\textsuperscript{17,18} we find that the electron-electron interactions to give rise to charge redistribution towards the edges of the ribbons when gating shifts the ribbon Fermi energy away from the Dirac point. This results in enhanced concentrations of the charge carriers on the defects at the edges of the ribbon. Naively, one might expect this to result in increased backscattering of the charge carriers by the edge defects and therefore a decrease of the ribbon conductance due to electron-electron interactions. However, surprisingly, we find the opposite. Namely, we find the conductances of ribbons with these edge defects to increase for most values of the Fermi energy when electron-electron interactions are introduced into the model. We explain this counterintuitive behavior as arising from spatial rearrangement of the electronic eigenstates of the ribbons and screening of local density of states fluctuations, both of which result from electron-electron interactions. This weakening of the effects of edge disorder on transport due to electron-electron interactions is a novel effect that appears to be unique to graphene devices. It may have played a role in the conductance quantization that has been observed in recent experiments\textsuperscript{22–24} on graphene nanostructures despite the presence of edge imperfections.

\section*{II. MODEL}

We consider suspended graphene nanoribbons, adopting a similar approach to that in Ref. 18. The GNR is separated from the back gate by dielectric and air layers and is attached at its two ends to semi-infinite leads represented by ideal ribbons having the same width $W$. The system is described by the Hamiltonian

$$H = \sum_i (E_i + V_i^H) a_i^\dagger a_i - \sum_{i,j} t_{ij}(a_i^\dagger a_j + \text{H.c.}),$$

where $E_i$ is the bare atomic orbital energy on atom $i$, $t_{ij}$ is the matrix element between nearest-neighbor atoms; in pristine graphene $t_{ij} = t = 2.7$ eV. $V_i^H$ is the Hartree potential at atom $i$ which results from the Coulomb interaction with the uncompensated charge density $-en$ in the system (including the image charges). In coordinate space the Hartree potential can be written as

$$V_i^H(r) = \frac{e^2}{4\pi\varepsilon_0}\int \frac{dr'}{4\pi\varepsilon_0} \sum_{\kappa} \frac{e^{-i(k-r') \cdot r}}{\sqrt{|r-r'|^2 + b_k^2}}.$$

where $-en_i(r')$ is the $k$th electron or image charge placed at distance $b_k$ from the graphene layer. The integration in (2) was performed over the whole device including the seminfinite leads. For details of our model we refer the reader to Ref. 18. Note that spin effects are outside of the scope of present study.

The edge reconstruction is introduced as randomly located defects at the edges of the hexagonal graphene lattice. We suppose low concentrations of defects that do not cluster though later we shall comment on such a case. We performed geometry relaxations for the edge reconstruction in GNRs using the GAUSSIAN 09 software package.\textsuperscript{19} The structures studied were graphene half disks of several tens of carbon atoms passivated at the edges with hydrogen, the defects being near the center of the straight edge. The carbon atoms belonging to the defect core as well as several nearest atoms at the edge were allowed to relax freely, the other carbon atoms being held fixed in the standard hexagonal graphene geometry with the C-C distance of 1.42 Å. The whole structure was kept planar. The relaxed structures obtained in this way are shown in the insets in Figs. 1 and 2. The matrix elements in the Hamiltonian Eq. (1) were modified to account for reconstructed topology by calculating the relevant matrix elements within the extended Hückel model.\textsuperscript{20,21}

The extended Hückel model employs a small basis set of Slater-type atomic orbitals $\{|\phi_i\rangle\}$, their overlaps $S_{ij} = \langle \phi_i | \phi_j \rangle$, and a Hamiltonian matrix $H_{ij} = \langle \phi_i | H | \phi_j \rangle$. The diagonal Hamiltonian elements $H_i = E_i$ are the experimentally determined (negative) atomic orbital ionization energies $E_i$. We approximate the nondiagonal elements as in Ref. 20 by $H_{ij} = (1.75 + \Delta_i^2 - 0.75\Delta_j^2)S_{ij}(E_i + E_j)/2$, where $\Delta_i = (E_i - E_j)/(E_i + E_j)$, a form chosen\textsuperscript{20} for consistency with experimental molecular electronic structure data. In the standard tight-binding Hamiltonian of pristine graphene with one atomic p orbital per carbon atom, the energy scale is chosen so that the carbon 2p$_z$ orbital energy is zero whereas in extended Hückel theory\textsuperscript{20} the carbon 2p$_z$ orbital energy is the ionization energy $E_C = -11.4$ eV. Accordingly, for consistency, in our extended Hückel Hamiltonian matrix we make the replacement $H_{ii} \rightarrow H_{ii} - E_C = E_i$ in Eq. (1). Because the extended Hückel basis states on different atoms are not in general mutually orthogonal the nondiagonal extended Hückel Hamiltonian matrix elements are then also adjusted according to $H_{ij} \rightarrow H_{ij} - S_{ij}E_C$, as is discussed in Ref. 25. $t_{ij}$ in Eq. (1) is then obtained from $H_{ij}$ that depends formally on the geometry of the reconstructed graphene ribbon through the atomic orbital overlaps $S_{ij}$. For further details and comparison with tight-binding parametrizations estimated
FIG. 1. (Color online) The conductances (a)–(c) and defect band structures (d)–(f) for armchair graphene nanoribbons with heptagon, pentagon, and Stone-Wales edge reconstruction defects, respectively. The respective single-defect geometries along with the tight-binding parameters are illustrated in the insets of (a)–(c). The conductances are presented for the ideal ribbon (dotted line), the ribbon with a single defect (dashed line), and 30 randomly distributed defects (solid gray line). The solid black line in (a)–(c) corresponds to the averaged conductance over 100 configurations. The band structures in (d)–(f) are calculated for the defect periodically repeated along both edges of the ribbon. The bands due to defects [shown in red in (d) and (e)] are clearly distinct from the standard dispersion of the armchair ribbon and correspond to the Fermi energies where strong electron or hole backscattering occurs. The top plots (g)–(j) show the square modulus of the wave function for the energies marked by the arrows in (d)–(f). All ribbons are 4.2 nm wide and 500 nm long, which corresponds to 33 carbon atoms in the cross section and 1173 unit cells along the device.

from density functional theory we refer the reader to our earlier study of adsorbed atoms and molecules on graphene.26 The modified matrix elements are given in the insets in Figs. 1 and 2.

Having calculated the reconstructed geometries and corresponding Hamiltonian matrix elements we find the conductance

$$G = -\frac{2e^2}{h} \int dE \sum_{ij} T_{ij}(E) \frac{\partial f(E - E_F)}{\partial E}$$

(3)

as a function of the Fermi energy $E_F$. Here $T_{ij}(E)$ is the transmission coefficient from subband $j$ in the left lead to

FIG. 2. The same as Figs. 1(a)–1(f) but for zigzag graphene ribbons. The ribbon dimensions $W = 4.2$ nm and $L = 500$ nm correspond to 20 carbon atoms in the cross section and 2033 unit cells along the device.
subband $i$ in the right lead, at energy $E$ and $f$ is the Fermi function. $T_{ij}(E)$ is calculated by the recursive Green’s-function method\cite{27} and includes the effect of electron interactions via Eq. (2).

III. RESULTS

We investigate the transport properties of edge reconstructed GNRs of realistic sizes, similar to those investigated experimentally.\cite{1,2} Two host/edge graphene orientations are studied in the following; armchair and zigzag. The edges are assumed to be randomly decorated by either heptagon, pentagon, or joint heptagon-pentagon (Stone-Wales) defects. The graphene ribbons with edge reconstruction defects that we study are assumed to be passivated with hydrogen; they can be realized experimentally by introducing hydrogen into the system after the reconstruction defects are formed.

Before we proceed with these edge reconstructions we shall comment on the effect of edge relaxations that preserve the benzenoid topology of pristine armchair and zigzag graphene edges. In this case, the outermost carbon atoms, when relaxed, move toward the graphene host which in turn leads to incremental changes of the hopping energies between the outermost carbon atoms. In the armchair configuration, we find the Hamiltonian matrix elements $t_{ij}$ between the two outer atoms of the armrest to increase by 9% while the hopping matrix elements between these atoms and their other nearest neighbors are enhanced by 3%. In the zigzag configuration, the two nearest-neighbor hopping energies $t_{ij}$ to/from the outermost carbon atoms increase by 3%. With these marginal changes incorporated, the transport properties stay qualitatively unchanged although the electronic subband bottoms shift by a few percent.

Because any topological edge defect causes much more dramatic changes in the electron transport properties we shall in what follows neglect the above hexagon relaxation except in the vicinity of the topological defects. For the sake of clarity we shall begin by considering electron transport within the noninteracting approach, setting $V_H = 0$ in Eq. (1).

A. Armchair ribbons

Figure 1(a) shows the conductances of aGNRs with heptagon edge defect(s). The relaxed defect geometry along with the estimated hopping energies between neighboring carbon atoms are given in the inset. The conductance for a single relaxed heptagon [the dashed line in Fig. 1(a)] develops stronger backscattering for higher electron subbands. As the defect concentration grows, the conductance becomes suppressed more strongly with pronounced oscillations due to quantum wave interference. After averaging over different defect configurations, conductance dips due to enhanced backscattering near subband bottoms become apparent, as has been discussed previously in the context of simple atomic lattice defects.\cite{2} This property appears to be generic for any edge reconstruction defect. For sufficiently large defect concentrations the electron transport mechanism undergoes a transition from ballistic transport to Anderson localization in these 500-nm-long GNRs.

The strong electron-hole conductance asymmetry in Fig. 1(a) for heptagon defects randomly distributed along the edges of the ribbon (solid grey and solid black lines) is qualitatively similar to that predicted by Dubois et al.\cite{14} for armchair ribbons with heptagon defects. They found heptagon defects to act as donors and quasibound states associated with them to result in strong electron scattering and depressed conductances at positive energies.\cite{14} We also find that if the heptagon defect is repeated periodically along the edges of the ribbon an additional electron subband appears in the GNR spectrum mainly at positive energies; this is the subband shown in red in Fig. 1(d). The associated Bloch states are exponentially\cite{28} localized at the edges of the ribbon as is shown in Fig. 1(g). We note that this additional subband is poorly matched to the Bloch states propagating in the pristine GNR leads and therefore results in strong electron backscattering in the positive energy range. For heptagon defects randomly distributed along the GNR’s edges this additional electron subband breaks up into electron defect states that also mediate electron backscattering, giving rise to the much stronger suppression of electron conductance than hole conductance in Fig. 1(a). [Note that the band structure in Fig. 1(d) is an idealized one presented only for the purpose of the present discussion since it is computed using the tight-binding parameters of the core of the isolated defect; for extended or clustered defects some of the tight-binding parameters will differ.]

By contrast, pentagon edge defects [see the inset in Fig. 1(b)] in armchair ribbons have been predicted to behave as acceptors.\cite{14} Consistent with this we find them to introduce hole states, or in the case of pentagons periodically repeated along the edges, an additional hole subband shown in red in Fig. 1(e). The result is strong hole backscattering and therefore much stronger suppression of the hole conductance than of the electron conductance, see Fig. 1(b), as in Ref. 14.

The effect of the Stone-Wales defect [Fig. 1(c)] is more subtle because it does not change the number of carbon atoms at the ribbon’s edge. For periodically repeated Stone-Wales defects the aGNR unit cell is doubled and the band structure exhibits both electron and hole bands associated with the defect; see Figs. 1(f), 1(i), and 1(j). The Bloch states are localized on different graphene sublattices [Figs. 1(i) and 1(j)] and cause differing backscattering. We found somewhat stronger backscattering for holes than for electrons for this 757 defect, see Fig. 1(c), whereas Ref. 14 predicted similar scattering for electrons and holes, and slightly stronger for the electrons.

B. Zigzag ribbons

The conductances and band structures for GNRs of nominally the same sizes and having the same numbers of reconstructed topological defects as in Fig. 1 but for the zigzag edge configuration are shown in Fig. 2. Some significant differences between the zigzag and armchair cases are as follows. First, the pristine zGNR supports a zero-energy mode whose wave function is localized along the edges. This mode hybridizes with the defect states and (unlike for armchair ribbons) no distinct defect bands occur in the band structures. This can be seen by comparing Figs. 1(d) and 1(e) and
Figs. 2(d) and 2(e). Also, unlike in the case of aGNRs, for zGNRs this hybridized band, whose wave function occupies edge carbon atoms, matches well with the bands of the pristine zGNR and supports enhanced conduction at positive (negative) Fermi energies for the heptagon (pentagon) defect. Second, the scattering of the carriers by the defects is generally weaker for the zigzag case. Third, the z575 defect causes especially strong conductance suppression near the flat band of the structure with periodically repeated defects; see Figs. 2(c) and 2(f). Fourth, the flat band of the pristine zGNR is strongly affected and no longer present near the graphene Dirac point for heptagon and pentagon defects but not so for the z575 defect. The strong modification of the subband structure in the first two cases results from the topological properties of the zigzag edge because it supports charge localization at the edges where defects form. The much weaker perturbation of the flat band for the z575 defect may be explained by effective narrowing of the ribbon such that the zigzag edge moves effectively into the ribbon interior.

C. Transport gaps

The GNRs studied above in Figs. 1 and 2 were only 4.2 nm wide and 500 nm long, but the analysis presented applies equally well to other geometries including realistic sizes fabricated experimentally. An important property of disordered ribbons measured in the experiments is the transport gap \( E_g \). This quantifies the energy (or gate voltage) window where the conductance is suppressed below some threshold value. Figure 3 shows the calculated \( E_g \) as a function of the ribbon width. The length of ribbon is fixed at \( L = 1 \mu m \) and the number of defects is 440. The threshold value was chosen to be half of the conductance quantum. We found that, for the reconstructed GNRs with randomly located defects, \( E_g \) scales inversely with the ribbon width. This agrees qualitatively with experimental data. We find the magnitudes of \( E_g \) to be ordered as follows: \( a^{757} > a^7 \gtrsim a^5 > z^{57} > z5 \gtrsim z^7 \), according to the type of defect and ribbon edge. The heptagon and pentagon defects cause approximately the same gap to develop. Note that this width dependence of \( E_g \) is very different than that for bulk defects where \( E_g \) was found to be independent of \( W \).

D. Electron-electron interactions

Having studied the effects due to edge reconstruction within the noninteracting electron model, we are in a position to consider the effects of electron interactions. However, an approach that accounts for Coulomb interactions as formulated in Sec. II demands huge computational resources that prohibit the study of GNRs of realistic sizes. Therefore we will restrict further study to a representative aGNR of \( W = 10 \) nm and \( L = 100 \) nm with heptagon defects only and will focus on the new physics introduced by the electron interactions. Figure 4 shows the conductance and charge densities on individual carbon atoms as a function of the Fermi energy. Previous theoretical work has shown electron-electron interactions to result in redistribution of charge towards the ribbon edges when the ribbon is gated away from the charge neutrality point. This effect is responsible for the nonlinear growth of the calculated charge densities on the atoms of the heptagon edge defect in the Hartree approximation as the Fermi energy moves away from the Dirac point in Fig. 4(b). The stronger charge accumulation at positive than negative energies in the Hartree approximation in Fig. 4(b) is due to the donor character of the heptagon edge defect. In stark contrast, the noninteracting model for the same single defect location predicts linear charge

![FIG. 3. (Color online) The transport gap \( E_g \) of GNRs with 440 randomly placed edge reconstruction defects as a function of ribbon width. The length is fixed at \( L = 1 \mu m \). The widths of the aGNRs are chosen so that conduction at the Dirac point is metallic for the defect-free ribbons. The effect of edge reconstruction defects on the transport gap is similar for aGNRs that are semiconducting when they are defect free.](image)

![FIG. 4. (Color online) (a) The conductances of aGNRs with heptagon defects calculated in the noninteracting and Hartree approaches. Forty-eight heptagon defects corresponds to 10% of the hexagon rings being replaced. (b) The charge densities on individual carbon atoms of the heptagon defect as numbered in the inset. \( L = 100 \) nm, \( W \sim 10 \) nm (82 carbon atoms in cross section), temperature \( T = 10 \) K.](image)
accumulation on the defect in Fig. 4(b) and slightly larger hole
densities than electron densities.

Thus electron-electron interactions result in the redistribution of charge towards the ribbon edges where the edge
defects are located. However, surprisingly, we find that this does not result in stronger electron backscattering by the
defects in the Hartree approximation than in the noninteracting electron model. To the contrary, we find the net effect of the electron-electron interactions to be, in most cases, to weaken electron backscattering by the edge defects and therefore to increase the ribbon conductance.

For a single edge defect, the weakening of electron backscattering due to electron-electron interactions manifests itself most clearly at positive energies in Fig. 4(a) where it results in weakening or complete suppression (in the Hartree approximation) of the conductance dips at subband edges that are a prominent feature of the noninteracting model. For 48 heptagon defects distributed randomly along the edges of the ribbon, as can be seen in Fig. 4(a), the calculated conductance in the Hartree approximation is substantially higher than that for the noninteracting electron model for most values of the Fermi energy. To understand this effect it is helpful to examine the wave functions and transmission probabilities for the different electronic eigenstates of the ribbon. These are shown for the noninteracting and Hartree models in Figs. 5 and 6, respectively, for the states at the Fermi energy $E_F = 0.14t$ indicated by the arrow in Fig. 4(a).

We attribute the counterintuitive enhancement of the ribbon conductance that arises from electron-electron interactions to a combination of two physical mechanisms, namely, (i) spatial rearrangement of both the low- and high-energy electronic eigenstates due to the formation of triangular electrostatic potential wells at the edges of the sample and (ii) screening of local density of states features associated with electron backscattering. Mechanism (i) is as follows: If electron-electron interactions are included in the model, the excess electronic charge on the ribbon gives rise to triangular electrostatic potential wells at the edges of the ribbon. If the structure of the ribbon does not have mirror symmetry about the ribbon centerline, then its eigenstates do not have a definite parity and each low-energy electron eigenstate localizes primarily in one of the triangular potential wells or the other. This can be seen in Figs. 6(b) and 6(c) where $\Psi_1 (\Psi_2)$ localizes primarily along the lower (upper) edge of the ribbon; whereas no pronounced effect of this kind is visible in Fig. 5. (Unlike the armchair structures in Fig. 1, the structures in Fig. 4 do not have mirror symmetry due to their different widths.) Thus, for the ribbon considered here in the presence of electron-electron interactions, electrons in the low-energy eigenstates backscatter mainly from defects on one edge of the ribbon; defects at the other edge have relatively little effect on them. Thus the low-energy electrons interact primarily with approximately half of the defects in the sample in the model with electron-electron interactions, although they interact with each of these defects somewhat more strongly than in the absence of the electron-electron interactions. Of these two competing effects, the reduction in the number of defects with which the electron interacts strongly has a larger effect on the conductance than does the stronger coupling. Thus the transmission probabilities for modes 1 and 2 are somewhat larger in Fig. 6(a) (the Hartree case) than in Fig. 5(a) (the noninteracting case). The higher-energy states also undergo a spatial re-arrangement due to electron-electron interactions in the Hartree approximation and this gives rise to an even larger enhancement of the ribbon conductance: The charge associated with the low-energy electronic states that localize in the triangular wells at the edges of the ribbon repels the carriers in the higher-energy states. Thus in the Hartree approximation the wave functions of the higher-energy electronic eigenstates have less weight at the ribbon edges where the edge defects are located. Therefore the transmission probabilities through the ribbon for the higher-energy electronic states are enhanced, as can be seen by comparing the transmission probabilities
for $\Psi_1$ and $\Psi_4$ in Fig. 6(a) (the Hartree case) with those in Fig. 5(a) (the noninteracting case). Thus the re-arrangement of the electronic states that occurs when electron-electron interactions are turned on results in an enhancement of the ribbon’s conductance. The screening mechanism (ii) is more subtle. Local charge fluctuations associated with electronic scattering resonances are screened or antiscreened due to electron-electron interactions. The effect of this on electron backscattering is strongly energy dependent: At energies near subband edges the screening tends to strongly suppress charge fluctuations and the associated electron backscattering is also suppressed. At other energies screening weakly enhances the charge fluctuations, however, the conductance is also enhanced. Thus mechanism (i) appears to have a larger effect on the conductance than does mechanism (ii) at those energies.

IV. DISCUSSION

Heptagon and pentagon edge reconstruction has been observed directly in experimental studies of armchair and zigzag graphene edges.9,10 Our results demonstrate strong observed directly in experimental studies of armchair and other types of the defects.

Fitting the above formula to our band gaps in Fig. 3 yields the extent of the disorder-induced localized surface-type states.3

The defects in a zGNR and found tight-binding parameters close as asymmetries at the energies of interest in this work (those closer to the Dirac point) are introduced by the heptagon and pentagon edge defects that we consider here. It is also worth pointing out that, in realistic devices, the edge reconstruction regions are not infinitely long but rather are sandwiched between electron reservoirs. This is equivalent to the transport problem we formulated and studied here whereas the band gaps obtained for infinitely long periodic defect structures.15,34 do not straightforwardly correspond to the transport gaps in such devices.

In the case where ribbon edges contain several different defects the combined effect on transport appears to be roughly additive.14 For aGNRs, the Clar representation depends on ribbon width, being either fully benzenoid, Kekulé, or incomplete Clar structures. Upon the introduction of any edge reconstruction defects, the bonding can be considered as the superposition of two mirroring Kekulé structures that partially destroy the benzenoid character of GNRs. By increasing the localization of $\pi$ electrons in carbon-carbon double bonds, such defects destroy the local aromaticity at the ribbon edge and are thus expected to have large impact on $\pi-\pi^*$ conduction channels.14

We studied isolated edge reconstruction defects that are assumed to be surrounded by the pristine hexagonal graphene lattice. This picture is valid for low defect concentrations when neighboring defects do not merge. However, the model that we have presented might be further extended to clustered groups of defects that were, for example, observed in some experiments.31 In this case, neighboring defects will affect the geometry of the relaxed structure and the tight-binding parameters $t_{ij}$ in the Hamiltonian Eq. (1) will be different. We have performed a test calculation for periodic Stone-Wales defects in a zGNR and found tight-binding parameters close to those reported in the literature.15,32 For those parameters the band structure, that is similar to Fig. 2(f), reveals downward bending of the flat band, i.e., the flat band occurs below the graphene Dirac point, in agreement with ab initio band structures in the literature.11,12,33,34

It is worth noting that the present formulation of the model does not include next-neighbor hopping in the Hamiltonian (1). We estimate that hopping to be $0.27t$ for pristine graphene. Next-neighbor hopping is known to introduce electron-hole asymmetry into the graphene band structure that becomes significant at energies well away from the Dirac point. While inclusion of this parameter will substantially complicate the calculation we expect that it would not change the results presented above qualitatively; much stronger electron-hole asymmetries at the energies of interest in this work (those closer to the Dirac point) are introduced by the heptagon and pentagon edge defects that we consider here. It is also worth noting that, in realistic devices, the edge reconstruction regions are not infinitely long but rather are sandwiched between electron reservoirs. This is equivalent to the transport problem we formulated and studied here whereas the band gaps obtained for infinitely long periodic defect structures.15,34 do not straightforwardly correspond to the transport gaps in such devices.

In the case where ribbon edges contain several different defects the combined effect on transport appears to be roughly additive.14 For example, equal concentrations of heptagon and pentagon defects restore electron-hole conductance symmetry and act in concert to increase the transport gap value.

Based on our findings, electron-electron interactions play a significant role in transport in graphene ribbons. Although they result in redistribution of charge to the edges of the ribbon where the edge defects are located, their net effect on transport is to reduce the backscattering of charge carriers by edge defects and thus to increase the ribbon conductance. While electron-electron interactions affect the conductance quantitatively, at the Hartree level of approximation they do not change the transport properties of the ribbon considered in
the present study qualitatively. For example, the electron-hole asymmetry of the conductance in Fig. 4 is maintained.

V. CONCLUSION

Our quantum transport calculations have shown edge reconstruction to cause strong electron/hole scattering and transport gaps to occur in GNRs in agreement with the experiments of Han et al. and Molitor et al. Strong scattering is a manifestation of mismatch between propagating states in the pristine ribbon and the states due to the defect. It is accompanied by electron-hole conductance asymmetry for defects that behave as donors or acceptors. We show that electron-electron interactions at the Hartree level of approximation result in charge accumulation at edge defects when the Fermi energy (or the gate voltage) varies but predict weaker electron backscattering by the defects in comparison to the noninteracting approach. Our results suggest that edge reconstruction may affect electron transport strongly in many experimentally realized graphene based devices. Work is in progress to address this issue in the context of the 0.7 anomaly in graphene nanoconstrictions observed recently by Tombros et al.