EXTRINSIC RADIO VARIABILITY OF JVAS/CLASS GRAVITATIONAL LENSES

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ABSTRACT

We present flux ratio curves of the fold and cusp (i.e., close multiple) images of six Jodrell Bank VLA Astrometric Survey and Cosmic Lens All-Sky Survey (JVAS/CLASS) gravitational lens systems. The data were obtained over a period of 8.5 months in 2001 with the Multi Element Radio-Linked Interferometer Network (MERLIN) at 5 GHz with 50 mas resolution, as part of a MERLIN Key Project. Even though the time delays between the fold and cusp images are small (≤ 1 day) compared to the timescale of intrinsic source variability, all six lens systems show evidence that suggests the presence of extrinsic variability. In particular, the cusp images of B2045+265—regarded as the strongest case of the violation of the cusp relation (i.e., the sum of the magnifications of the three cusp images add to zero)—show extrinsic variations in their flux ratios up to ~40% peak to peak on timescales of several months. Its low Galactic latitude of b ≈ −10° and a line of sight toward the Cygnus superbubble region suggest that Galactic scintillation is the most likely cause. The cusp images of B1422+231 at b ≈ +69° do not show strong extrinsic variability. Galactic scintillation can therefore cause significant scatter in the cusp and fold relations of some radio lens systems (up to 10% rms), even though these relations remain violated when averaged over a ≤ 1 yr time baseline.

Subject headings: gravitational lensing — ISM: general — scattering

1. INTRODUCTION

Cosmological cold dark matter (CDM) simulations predict the existence of condensed structures in the halos around massive galaxies (Klypin et al. 1999; Moore et al. 1999) if the initial power spectrum does not cut off at small scales and dark matter is cold and not self-interacting. However, we see at most, the high-mass tail of these structures in the form of dwarf galaxies. This raises the question of where most of their less massive (∼10^6–10^9 M_☉) counterparts are located. Either these CDM structures have not formed, in conflict with CDM predictions, or they consist predominantly of dark matter and baryons have been blown out (preventing star formation altogether), or baryons are present but have not condensed inside their potential well to form visible stars. If either one of the latter two is the case, the only way to detect them is through their gravitational effect, in particular, through dynamics and lensing.

The initial suggestion by Mao & Schneider (1998) that anomalous flux ratios in the lens system B1422+231 can be caused by small-scale mass substructure in the lens galaxy was recently extended to a larger, although still limited, sample of gravitational lens systems with fold and cusp images (Metcalf & Madau 2001; Keeton 2001; Chiba 2002; Metcalf & Zhao 2002; Dalal & Kochanek 2002; Bradač et al. 2002; Keeton et al. 2003). In particular, analyses have focused on the so-called normalized cusp relation, which says that R_cusp ≡ Σ_m/Σ_m → 0 for the magnifications μ_i of the three merging images of a source well inside the cusp (Blandford 1990; Schneider & Weiss 1992). A similar relation holds for the two fold images. These relations are only two of many (in fact, infinite) scaling laws (Blandford 1990). Because globular clusters and dwarf galaxies are too few in number to explain the rate of anomalous flux ratios and cusp relations, this could be used as an argument in favor of CDM substructure as the dominant cause of these apparent anomalies (Kochanek & Dalal 2003).

If the observed violations of the cusp relation (i.e., R_cusp ≠ 0), as discussed above, are due to substructure on mass scales of 10^6–10^9 M_☉, the effect should be the same for radio and optical flux ratios (if the latter are available), and it should be constant in time. However, another possible explanation is microscoping of stellar mass objects in combination with a smoothly distributed (dark) matter component (Schechter & Wambsganss 2002). This one does not require the optical and radio flux ratios to behave in the same way, and, in particular, it predicts the optical flux ratios to change over timescales of years. Finally, there is...
also the possibility that the flux density and surface brightness distribution of lensed radio images are affected by the ionized interstellar medium (ISM) in the lens galaxy and/or our Galaxy, also leading to changes in the apparent value of the cusp relation.

Hence, before one can confidently accept the detection CDM substructure, rigorous testing is required to see whether observed flux ratios correspond to magnification ratios or whether they can be affected by propagation effects (or microlensing). Here we make the first coordinated attempt to test the effects of propagation on the observed radio fluxes of lensed images.

In § 2 and 3, we present the first results of our MERLIN Key Project (A. Biggs et al. 2003, in preparation) to search for extrinsic variability between fold and cusp images (i.e., close multiple images) on the basis of their flux density curves. A discussion and conclusions are given in § 4.

2. MERLIN 5 GHz DATA

MERLIN 5 GHz data were obtained between 2001 February 21 and November 7. A total of 41 epochs of 24 hr each was obtained, on average, once per week. Eight lens systems were observed (Table 1 plus B1608+656 and B1600+434), of which seven are four-image systems and one is a double. The data acquisition and reduction is described in A. Biggs et al. (2003, in preparation), which also presents the flux density curves of all the lensed images.

In this paper, we focus on the flux ratio curves. This approach has several advantages when looking for extrinsic variability. The dominant errors on flux density curves in the radio are those resulting from residual noise in the maps and from multiplicative errors as a result of erroneous flux calibration. Because multiplicative errors are equal for each of the lensed images, they disappear in the flux ratio curves (not corrected for the time delays), which should therefore be flat and dominated by noise in the absence of variability.

All presented lens systems also have small time delays between fold/cusp images (≤ 1 day) compared to the time between observations and the timescale of intrinsic variability as seen in the flux density curves (A. Biggs et al. 2003, in preparation). Hence, intrinsic flux density variations should effectively occur simultaneously in fold and cusp images and, thus, disappear in the flux ratio curves. Throughout this paper, we therefore assume that (1) due to the small time delays between fold/cusp images, intrinsic variability does not affect the flux ratio curves, (2) systematic flux density errors are multiplicative and also do not affect the flux ratio curves, and (3) extrinsic variability does not correlate between lensed images. We exclude the double B1600+434 and the quad B1608+656 from our analysis: both have nonnegligible time delays (i.e., several weeks to months; see Fassnacht et al. 1999a, 2002; Koopmans et al. 2000; Burud et al. 2000).

3. RESULTS

3.1. Normalized Flux Ratio Curves

In Figure 1, the resulting flux ratio curves of all images are shown with respect to image A, which is often the brightest image. We follow the labeling of these images as published in the literature (A. Biggs et al. 2003, in preparation). Each flux ratio curve has been normalized to unity by dividing them through the average flux ratio of all 41 epochs. The errors are the square root of the sum of the two fractional (noise) errors on the flux-densities squared. The flux density errors are determined from the rms in the residual maps (i.e., the radio maps with the lensed images subtracted).

In Table 1, we list the average flux ratios and the rms scatter for each image pair, the reduced $\chi^2$ values (assuming that each normalized flux ratio should be unity in the case of no extrinsic variability and under the assumptions mentioned in § 2), and the values of $R_{\text{cusp}}$ (Mao & Schneider 1998; Keeton et al. 2003), which we discuss further in § 4.

3.2. Evidence for Extrinsic Variability

To test for extrinsic variability in the lensed images on timescales less than the monitoring period of 8.5 months, we introduce the following method. Let us designate the normalized light curves of the individual cusp/fold images as $a_i \equiv A_i / A$, $b_i \equiv B_i / B$, and $c_i \equiv C_i / C$, where their average flux densities over the 41 epochs are $\langle A \rangle$, $\langle B \rangle$, and $\langle C \rangle$, respectively. First, the points $(a_n, b_n, c_n)$ are plotted in a three-dimensional Cartesian space, so that multiplicative errors and intrinsic flux density variations (the latter because of the negligible time delays) move points parallel to the vector $(1, 1, 1)$. Second, each point $(a_n, b_n, c_n)$ is projected on to a two-dimensional plane that is normal to the vector $(1, 1, 1)$. Hence, the projected points will not move on that plane, because of either intrinsic flux density varia-

| System            | $\langle r(B/A) \rangle$ | $\langle r(C/A) \rangle$ | $\langle r(D/A) \rangle$ | $\chi^2$/dof | $R_{\text{cusp}}$ |
|-------------------|--------------------------|--------------------------|--------------------------|-------------|------------------|
| B0128+437 .......... | 0.584(0.029)              | 0.520(0.029)              | 0.506(0.032)              | 1.8/1.9/2.4 | 0.445 (0.015)    |
| B0712+472 .......... | 0.843(0.061)              | 0.418(0.037)              | 0.082(0.035)              | 4.8/3.2/8.0 | 0.255 (0.030)    |
| B1359+154 .......... | 0.580(0.039)              | 0.782(0.031)              | 0.193(0.031)              | 1.9/0.9/1.2 | 0.510 (0.024)    |
| B1422+231 .......... | 1.062(0.029)              | 0.551(0.007)              | 0.024(0.006)              | 1.8/2.0/1.5 | 0.187 (0.004)    |
| B1555+375 .......... | 0.620(0.039)              | 0.507(0.030)              | 0.086(0.024)              | 3.4/2.1/2.4 | 0.417 (0.024)    |
| B2045+265 .......... | 0.578(0.059)              | 0.739(0.073)              | 0.102(0.025)              | 8.2/10.9/2.9 | 0.501 (0.035)    |

Note.—Flux ratios of each image pair. The rms scatter in the flux ratio is indicated between parentheses, calculated from the 41 epochs. The reduced $\chi^2$ values are listed as well, calculated on the basis that each normalized flux ratio curve should be unity and that there is no variability. In addition, the values of $R_{\text{cusp}}$ (see § 3) and its rms (between parentheses) are listed (Mao & Schneider 1998; Keeton et al. 2003).
Fig. 1.—Normalized flux ratio curves of the three independent image pairs for all six quadruple lens systems. The scale on the $y$-axis is set to $\pm 5$ times the rms scatter of the flux ratio curves. The errors on the flux ratio curves are determined from the errors on the individual flux density curves.
tions or multiplicative errors. Both of these are movements perpendicular to the plane and, thus, translate to the same projected point.

Third, if one defines the \( x \)-axis, \( \hat{x} \), of this two-dimensional plane to be the projected \( a \)-axis, \( \hat{a} \), of the three-dimensional space, and \( y \) to be perpendicular to \( \hat{x} \) in the same normal plane, one finds the following simple mapping:

\[
x = \frac{(2a_n - b_n - c_n)}{\sqrt{6}} ,
\]
\[
y = \frac{(b_n - c_n)}{\sqrt{2}} ,
\]

or, in polar coordinates,

\[
\rho^2 = x^2 + y^2 ,
\]
\[
\theta = \arctan(x, y) .
\]

Because \( \hat{a} \) projects onto \( \hat{x} \), any uncorrelated extrinsic variations in image A will only result in a movement of a point along \( \hat{a} \) and, thus, only along the \( \hat{x} \) axis.

Because the 1 \( \sigma \) errors on the normalized flux densities \( a_n, b_n, \) and \( c_n \) are known from the observations, one can calculate the corresponding expected 1 \( \sigma \) errors on \( x \) and \( y \),

\[
\sigma_\rho = \frac{\sqrt{2}}{\sqrt{6}} \sigma_x + \frac{1}{\sqrt{6}} \sigma_y + \frac{1}{\sqrt{2}} \sigma_z ,
\]
\[
\sigma_\theta = \frac{1}{\sqrt{2}} \sigma_x + \frac{1}{\sqrt{6}} \sigma_y - \frac{1}{\sqrt{6}} \sigma_z ,
\]

and, similarly,

\[
\sigma_\rho^2 = \left( \frac{(2a_n - b_n - c_n)^2 \sigma_x^2 + (2b_n - c_n - a_n)^2 \sigma_y^2 + (2c_n - a_n - b_n)^2 \sigma_z^2}{9 \rho^4} \right)
\]
\[
\sigma_\theta^2 = \left( \frac{2 \sigma_x^2}{\rho^2} \right)
\]

Notice that the scatter in \( x \) will be a combination of the scatter in \( a_n, b_n, \) and \( c_n \), if each image behaves independently.

On the other hand,

\[
\chi^2 = \frac{1}{\text{dof}} \sum_i (r_i / \sigma_{r,i})^2
\]

is a direct estimator of the significance of the presence of extrinsic variability on timescales of less than 8.5 month, irrespective of the image(s) it occurs in. In other words, it does not tell us which image or images exhibit extrinsic variability, only that extrinsic variability is present if \( \chi^2 > 1 \) is significantly larger than unity.

The significance of extrinsic variability in individual image is far more difficult to assess. However, we can estimate the level of extrinsic variability in image A, for example, by knowing that the expected variance in that image due to noise and in the absence of extrinsic variability, should be

\[
E(\sigma_{\rho}^2) \approx \frac{1}{2} \text{Var}(x) - \frac{1}{2} \text{Var}(y) .
\]

If the observed value of \( \langle \sigma_{\rho}^2 \rangle = (\sum_i^N \sigma_{r,i}^2) / N \) is smaller than \( E(\sigma_{\rho}^2) \), the difference is due to extrinsic variability, with an estimated variance of

\[
\text{Var}(a_{\text{ext}}) \approx E(\sigma_{\rho}^2) - \langle \sigma_{\rho}^2 \rangle .
\]

The same procedure can be repeated for each of the other images. In Table 2, we have listed the values of \( \chi^2 \) and the values of \( \text{Var}(a_{\text{ext}}, b_{\text{ext}}, c_{\text{ext}}) \) if larger than zero. (Note that \( E(\sigma_{\rho}^2) \) is an estimate and could therefore be smaller than \( \langle \sigma_{\rho}^2 \rangle \) when measured from a finite set of observations.)

Finally, we further discuss whether correlations between the flux measurements of the merging images could potentially occur. We note, however, that \( \sigma_{a/b/c} \) are noise errors as determined from residual maps, i.e., the original maps, after we subtract the best-fit model of the lensed images. The residual radio maps are consistent with noise maps. Since the images are separated by many beam sizes (i.e., resolution elements), the flux measurements of images A, B, and C, even though measured from the same map, are independent, except for the multiplicative errors, as explained previously. Hence, there should be no effect of measurement correlations in equations (3) or (4) that could skew our results.

The technique discussed above is explicitly designed to separate the effects of multiplicative errors, extrinsic variability, and noise and should also be free of measurement correlations. For example, if one were to cross-correlate (e.g., using the Spearmann rank correlation) the flux ratio curves (Fig. 1) of a single-lens system with each other, one would find that they correlate strongly, even in the absence of extrinsic variability, the reason being that the same noise variations in image A would be introduced in both \( B/A \) and \( C/A \). A Spearmann rank correlation on flux ratio curves without extrinsic variability but with similar noise properties and number of epochs confirms this. However, one notices from equations (3) and (4) that any multiplicative error does not affect \( \sigma_{r,i}^2 \) or \( \sigma^2 _{\rho} \) (where it cancels out) or the projection on the plane that we defined in equations (1) and (2), as previously discussed. In addition, one finds from equations (1), (2), and (4) that if there is no extrinsic variability, \( \chi^2 \rightarrow 1 \), whereas the presence of extrinsic variability implies \( \chi^2 > 1 \). Hence, \( \chi^2 \) is indeed independent from multiplicative errors and, therefore, the correct estimator of the significance of the presence of extrinsic variability in the (shown) absence of measurement correlations.

### 3.3. Individual Lens Systems

Here we discuss each case on the basis of its reduced \( \chi^2 \) values. Image D is not considered because of its faintness and larger inferred time delay compared with the other images.

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Table 2: Significance and Estimates of Extrinsic Variability

| Systems | \( \sigma_{a_{\text{ext}}} \) | \( \sigma_{b_{\text{ext}}} \) | \( \sigma_{c_{\text{ext}}} \) | \( \chi^2 / \text{dof} \) |
|---------|-----------------|-----------------|-----------------|-----------------|
| B0128+437 | 2.9 | 1.9 | 2.5 | 3.3 |
| B0712+472 | 4.8 | 4.2 | 4.8 | 6.2 |
| B1359+154 | 1.0 | 4.6 | 1.0 | 2.8 |
| B1422+231 | ... | 0.6 | 0.9 | 3.7 |
| B1555+375 | 3.3 | 4.2 | 3.0 | 5.3 |
| B2045+265 | 6.1 | 7.0 | 7.2 | 17.1 |

Note.—Estimated rms levels of extrinsic variability in images A, B, and C. The reduced values of \( \chi^2 \) are given to indicate the significance of the presence of extrinsic variability in the combined set of images. Ellipses: Estimated variance was smaller than zero (see § 3.2 for more details).
3.3.1. All Systems Except B2045+265

On the basis of the relatively low values of $\chi^2$ and the estimated levels of extrinsic variability (Table 2) for the images of B0128+437, B1359+154, B1422+231, and B1555+375 and the remaining possibility that some minor undetected additive errors could be present, the evidence for extrinsic variability in these four systems is not totally convincing. We exclude these from further discussion.

In the case of B0712+472, the reduced $\chi^2$ values of the $(B/A)_n$ flux ratio curves and also $\chi^2$ seem more significant. In Figure 1, we see that a large number of epochs are deviant over the entire observing season. Deviations of the $(C/A)_n$ flux ratio curve from unity are less significant, probably because image C has a larger fractional error than images A and B. Even though there is some evidence in this system for extrinsic variability between the two fold images, we conservatively regard it also as weak, and we will concentrate our discussion on B2045+265. In § 4, however, we further discuss possible reasons for some of the higher values of $\chi^2$ and extrinsic variability.

3.3.2. B2045+265

In Tables 1 and 2, we see that both the $(B/A)_n$ and $(C/A)_n$ flux ratio curves have very high values of the reduced $\chi^2$ (reflected also in large rms values), the estimated rms values of extrinsic variability and the value of $\chi^2$ are very large, and a visual inspection of the $(B/A)_n$ and $(C/A)_n$ flux ratio curves shows changes of up to $\sim 40\%$ on timescales of several months. Because the time delays between the cusp images are only a fraction of a day (Fassnacht et al. 1999b), residual intrinsic source variability cannot cause these variations.

A more quantitative analysis based on the structure function (Simonetti, Cordes, & Heeschen 1985) of the flux ratio curves [indicated by $R(t)$] is shown in Figure 2. The structure function $\langle D^1(\tau) \rangle = \langle [R(t + \tau) - R(t)]^2 \rangle$ quantifies the average rms fluctuations (squared) between two points on the same flux ratio curve, separated by a time lag $\tau$. A lower value of $\langle D^1(\tau) \rangle$ means a stronger correlation (assuming no errors). Figure 2 shows that even though $\langle D^1(\tau) \rangle$ fluctuates considerably, it continues to increase toward longer lags. Around $\tau \sim 150$ days, the rms suddenly decreases considerably, suggesting possible long-term correlated variations in the flux ratios on that timescale. If $\langle D^1(\tau) \rangle$ increases beyond $\tau \gtrsim 200$ days, flux density variations of several tens of percent on a timescale of $\gtrsim 1$ yr could be present as well. However, we note that the overlap of the flux ratio curves becomes smaller for longer lags and, consequently, the errors become larger. Longer observations are required to make stronger statements about the longer time lags. Even so, similar fluctuations of the structure function are seen in some scintillating sources (Dennett-Thorpe & de Bruyn 2003).

Several reliability checks of the extrinsic variations of the cusp images of B2045+265 are called for: first, we note that the lensed images are of roughly equal brightness and, within a factor of $\sim 2$, as bright as the images in B0128+437, B1359+154, B0712+472, and B1555+375. Hence, there is no indication that the observed flux ratio variations are related to the faintness or brightness of the lensed images. Second, there are no problems with the closeness between the cusp images ($\lesssim 0.7\arcsec$) and the separation of their flux densities because of the high resolution of the MERLIN radio maps ($\sim 50$ mas). Hence, the fluxes of the three images are fully independent. Third, we have calculated the Spearman rank correlation coefficients $(r_S)$ between each of its images A, B, and C and those of the other five lens systems. This leads to 45 independent values of $r_S$ (i.e., noise does not introduce correlation in this case), which, on average, should tend to zero. We find $(r_S) = 0.0024$ and an rms of 0.153 (Keeping 1962). The theoretical expectation value of the rms value is $1/(N - 1)^{1/2} = 0.151$, where $N = 45$ in our case. Hence, we recover the expectation values of both the average and rms. This shows that any correlation between the images cannot be the result of obvious systematic errors in the data reduction process, in the creation of the flux ratio curves, or in our analysis. Hence, we confidently conclude that the cusp images of B2045+265 show strong evidence for the presence of extrinsic variability.

4. DISCUSSION AND CONCLUSIONS

We have presented the flux ratio curves of six gravitational lens systems, each composed of 41 epochs taken over a period of 8.5 months in 2001 with MERLIN at 5 GHz, as part of a MERLIN Key Project. The systems were chosen to have merging cusp or fold images, such that the time delays between these images are negligible ($\lesssim 1$ days) compared to the timescale of intrinsic variability and the rate at which the light curves are sampled. The flux ratio curves should therefore be void of intrinsic variability and multiplicative errors. The main goal of our program was to find additional cases of extrinsic variability other than radio microlensing in B1600+434 (Koopmans & de Bruyn 2000; L. Koopmans & A. de Bruyn 2003, in preparation).

We find some statistical evidence for extrinsic variability in all six lens systems on the basis of reduced $\chi^2$ values larger than unity (§ 3.2; Tables 1 and 2). Residual intrinsic
variations due to the finite time delays or small additive error are unlikely to be the cause of this but cannot fully be excluded yet. The high resolution of MERLIN also ensures negligible correlations between the fluxes of the merging images. The evidence for B0128+437, B1359+154, B1422+231, and B1555+375 is fairly marginal. The case for B0712 is stronger, however, and this object clearly deserves further study. The best case is B2045+265, which we discuss further below.

Even though radio microlensing cannot be excluded, we think at this point that Galactic scintillation is the more likely cause of some of the higher values of $\chi^2$ (Tables 1 and 2). Indeed, all compact extragalactic radio sources should show refractive scintillation at some level. At wavelengths of 5 GHz and for image sizes $\sim 1$ mas, the expected rms fluctuations due to scintillation in a typical line of sight out of the Galactic plane, are a few percent (Walker 1998, 2001), which are comparable to the observed flux density errors.

One gravitational lens systems, B2045+265, shows unambiguous evidence for extrinsic variability on the basis of the reduced $\chi^2$ values significantly larger than unity (Tables 1 and 2) and visually apparent long-term variations in its flux ratio curves (Fig. 1). One possible explanation for the variations is radio microlensing similar to B1600+434 (Koopmans & de Bruyn 2000; L. Koopmans & A. de Bruyn 2003, in preparation). However, because B2045+265 has a Galactic latitude $b \approx -10^\circ$ and is the lowest Galactic latitude system in our sample, Galactic refractive scintillation is the more likely explanation.

To examine this, first we naively use the revised electron-density model of our Galaxy by Cordes & Lazio (2003). This model gives a scattering measure of $8 \times 10^{-4}$ kpc m$^{-2/3}$, an angular broadening at 5 GHz of 50 $\mu$as, and a transition frequency of 22 GHz between the weak and strong scattering regimes. If we chose the source size to be 250 $\mu$as, we find a modulation index of 7% (Walker 1998, 2001) or an rms scatter of $\sim 10\%$ in the flux ratio curves (as observed; Table 1), and a typical variability timescale of $\sim 1$ week for an effective transverse velocity $v_{\|}$ of $50$ km s$^{-1}$. Note, however, that the timescale of variability might vary with the time of year due to the Earth’s motion (Dennett-Thorpe & de Bruyn 2000, 2002).

Refractive scintillation could therefore explain the observed extrinsic variations up to a timescale of possibly several weeks in B2045+265 for reasonable lensed images sizes. However, the structure function shows correlated variations on timescales that are much longer. These could indicate either modification(s) of the Kolmogorov spectrum of density fluctuations that was assumed in the above calculation or a very low transverse velocity of the medium, i.e., $10$ km s$^{-1}$. If there is more power in the spectrum on larger scales, or a cutoff on smaller scales, fluctuations will become stronger on longer timescales (Blandford, Narayan, & Romani 1986; Romani, Narayan, & Blandford 1986; Goodman et al. 1987). Such large-scale electron density waves might also explain the apparent fluctuations in the observed structure function (Fig. 2).

On further examination, however, we find that B2045+265 is very close, if not seen through, the Cygnus superbubble region (see Fig. 6 in Fey, Spangler, & Mutel 1989), making our analysis based on the model in Cordes & Lazio (2003) rather uncertain. This region has considerably enhanced scattering measures, and if this is the case for B2045+265 as well, it would strongly support Galactic scintillation as the cause of the observed flux density variations. The complexity of such regions, where turbulence in the ionized ISM presumably originates, could be the reason we see large-amplitude fluctuations in the flux ratios with timescales that are not expected from simple Kolmogorov turbulence models (see also J1819+3845; Dennett-Thorpe & de Bruyn 2000, 2002).

Finally, it is interesting to note that B2045+265 has the strongest and most significant violation of the cusp relation of all known lens systems (Keeton et al. 2003). Even so, the values of $R_{\text{cusp}}$ of the systems discussed in this paper (see Table 1) agree with those in Keeton et al. (2003). However, the strong observed variations in the flux ratio curves should caution against the use of both flux ratios and values of $R_{\text{cusp}}$ ($\S$ 1) derived from single-epoch observations, even if the inferred time delays are only a few hours!

Whether the violation of the cusp relation in B2045+265 averaged over 8.5 months (Table 1) and Galactic refractive scintillation and/or scattering is completely coincidental is not clear at this point. At any instant in time, however, large-scale electron-density fluctuations in the Galactic ISM can focus or defocus the images with long timescales of variability, as is apparent from our observations, probably even more so toward regions of enhanced turbulence (i.e., the Cygnus region). CDM substructure mostly focuses the images. It is interesting to note that B0712+472, probably the system with second-best evidence for extrinsic variability in our sample, also has a low Galactic latitude, $b = +23^\circ$.

While the observations reported in this paper do not contradict the exciting conclusion that CDM substructure might have been detected within the central regions of lens galaxies, they do suggest that extrinsic, refractive effects are also of importance and that it is imperative to carry out further multifrequency monitoring to distinguish them from achronatic, gravitational effects.

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