Real-space analysis of diffusion behavior and activation energy of individual monatomic ions in a liquid

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Investigation of the local dynamic behavior of atoms and molecules in liquids is crucial for revealing the origin of macroscopic liquid properties. Therefore, direct imaging of single atoms to understand their motions in liquids is desirable. Ionic liquids have been studied for various applications, in which they are used as electrolytes or solvents. However, atomic-scale diffusion and relaxation processes in ionic liquids have never been observed experimentally. We directly observe the motion of individual monatomic ions in an ionic liquid using scanning transmission electron microscopy (STEM) and reveal that the ions diffuse by a cage-jump mechanism. Moreover, we estimate the diffusion coefficient and activation energy for the diffusive jumps from the STEM images, which connect the atomic-scale dynamics to macroscopic liquid properties. Our method is the only available means to observe the motion, reactions, and energy barriers of atoms/molecules in liquids.

INTRODUCTION

Understanding atomic and molecular dynamics and reaction activities in liquids is crucial for developing higher-performance liquid systems because the macroscopic properties of a liquid, such as its viscosity and conductivity, are determined by the average local atomic and molecular dynamics and physical properties. However, gaining such an atomic- and molecular-scale understanding in liquids is highly challenging with conventional analytical methods, such as nuclear magnetic resonance and neutron scattering, which provide only averaged information on the whole liquid system. Thus, the development of a method for the high-resolution, real-space observation of the local dynamics and physical properties in liquids would provide important insight into the mechanisms that give rise to the macroscopic properties of liquids.

Among liquids, ionic liquids have unique properties, such as non-volatility, high ionic density, and designable hydrophilicity (1–3). Owing to these properties, ionic liquids have been applied in a variety of industrial fields (for example, as electrolytes and extraction or reaction solvents) (3–10). Because ionic liquids exhibit unique diffusion behavior, which deviates strongly from the Stokes-Einstein behavior, it is necessary to gain an understanding of the dynamics of atoms and molecules within ionic liquids.

Here, we directly observe the motion of individual monatomic ions in ionic liquids using atomic-resolution scanning transmission electron microscopy (STEM). To reveal the diffusion mechanism of monatomic ions, we analyze the dynamic motions of individual monatomic ions in an ionic liquid and furthermore, estimate local properties of the dynamics, such as diffusion coefficient and activation energy, by analyzing the STEM images.

RESULTS AND DISCUSSION

As schematically shown in Fig. 1, we observed gold (Au3+) and iodide (I−) dispersed in thin ionic liquid films using bright-field and annular dark-field (ADF) STEM. The simultaneously obtained bright-field and ADF images of the ionic liquid 1-ethyl-3-methylimidazolium bis(trifluoromethylsulfonyl)imide (C2mimTFSI) with gold ions at room temperature are shown in Fig. 2 (A and B). The thickness of the observed area measured using the electron energy-loss spectroscopy log-ratio method is ~4 nm (11, 12). Because the observation temperature (that is, room temperature) is higher than the melting point of C2mimTFSI, it is considered to be in a liquid state. The shape of the liquid films substantially changes when the films remain tilted for several hours inside the TEM, as shown in fig. S1. Although the monatomic ions are not identifiable in the bright-field image, the ADF image shows numerous bright spots. We speculate them to be gold ions because gold has much higher atomic number (Z) in this composition and should be observed with much higher intensity as described in section S2. To confirm that the bright spots correspond to “single” gold ions, we compared the experimental bright-spot image with the simulated image, as shown in Fig. 2 (B and C). The intensity profiles of the experimental and simulated images are shown in Fig. 2D; there is good agreement between the experimental and simulated profiles. Furthermore, we constructed a...
histogram of the areas of the bright spots, as shown in Fig. 2E, which is fitted with a Gaussian curve, indicating an average value of 0.0068 nm². This area corresponds to a circle with a diameter of 0.093 nm, which is identical to the full width at half maximum of the simulated bright spot. On the basis of these results, we conclude that most of the bright spots in Fig. 2B correspond to single gold atoms. Thus, individual gold atoms (monatomic gold ions) in liquid C₂₅mimTFSI were directly observed using ADF STEM.

A more detailed inspection reveals that some bright spots have distorted shapes, owing to atomic vibrations or small displacements. As described in section S2, the absolute intensity of a monatomic gold ion without the background is independent of the liquid thickness, and the depth resolution is <9 nm. The 42 atoms in Fig. 2B correspond to a concentration of 0.29 M. This matches the atomic concentration of gold that was prepared and thus indicates that all the gold ions within the observation area are imaged. Moreover, we also performed atomic-resolution ADF observations of gold and iodine in different ionic liquids (section S1). These observations demonstrated that not only gold, but also iodine can be observed in ionic liquids.

Because individual gold ions in ionic liquids could be visualized, we investigated their dynamic behavior in C₂₅mimTFSI. First, we considered the atomic movement during the single-image observation in Fig. 2B. In this image, most of the bright spots have near-spherical shapes, and they are imaged within 15 scanning lines, which correspond to 0.114 nm (0.0076 nm per line). The acquisition time for a single, whole bright spot was approximately 0.25 s (section S3); that is, each of the ions is trapped in a very small space (or “cage”), which is accompanied by unidentifiable vibration for at least 0.25 s. It can be assumed that the monatomic gold ions are strongly solvated by the counterionic solvent molecules (13). By contrast, a few spots, such as spot B in Fig. 2B, show distinctly strained shapes, which are thought to originate from “jumping” from one cage to form a new cage or displacement accompanying the whole cage during imaging of the single gold ion. As shown in section S2, we simulated how a gold ion is imaged when it is displaced during imaging; a displacement >0.08 nm was found to be identifiable. In Fig. 2B, ~10% of the ions exhibit identifiable displacements. This behavior of the gold ions (that is, remaining in a cage and jumping from the cage) is supported by previously reported simulations of the diffusion of small ions in a similar ionic liquid (13).

Continuously acquired images of C₂₅mimTFSI with gold ions are shown in Fig. 3A. The liquid thickness is ~7 nm, and the frame rate is 4.2 s per frame. We confirmed that the damage caused by electron irradiation was not appreciable by imaging an area for several minutes (discussed in section S6). Labeled as A, B, and C in Fig. 3A, the ions were tracked, although spot B disappears in the image taken at 25.2 s as a result of jumping across the scanning line, and ion C appears to split into two spots (that is, C1 and C2) in the image taken at 29.4 s as a result of jumping from C1 to C2 during scanning.
The trajectories of all the ions are shown in Fig. 3B, in which it can be seen that the dynamics of the monatomic ions in the liquid phase are spatially and temporally heterogeneous in their displacement distances, directions, and times. As an example, we take the trajectory of ion C in Fig. 3C. The numbers in the figure correspond to the atomic positions in the respective frames. This trajectory shows that ion C often underwent large displacements within the 4.2-s scan (between frames 1 to 5, 6 and 7, and 8 and 9), as well as small jumps or displacements (between frames 5 and 6, 7 and 8, and 9 and 10). We consider this heterogeneity in the atomic dynamics to reflect the differences in the local solvation environment and temperature at each position. Small jumps or displacements (namely, between frames 5 and 6, 7 and 8, and 9 and 10) indicate that the monatomic gold ion was strongly caged by the surrounding solvent molecules or had low kinetic energy; by contrast, the ions moved under weakly constraining environments. We found that, contrary to the spatial and temporal heterogeneity, the displacements are completely isotropic on average as shown in section S4.

A histogram of the interframe displacements (within 4.2 s) of all ions is shown in Fig. 3D. The average displacement of the gold ions in the liquid is 0.19 nm per frame, and the number of gold ions remaining in the same positions (that is, displacement \( \leq 0.08 \) nm) is 35%, indicating that 65% of the ions underwent several jumps or displacements within 4.2 s. In addition, most ions (94%) exhibit almost round shapes in all frames and thus remain in their original positions for longer than 0.06 s (which is the scanning time of each round bright spot in these images). This result indicates that the transition of the relaxation behavior from
remaining in a cage to jumping between cages occurs on a time scale between 0.06 and 4.2 s in this system. We then estimated the physical properties related to the diffusion of the monatomic gold ions in the liquid phase. The two-dimensional diffusion coefficient of the monatomic ions, $D_{2D,obs}$, was estimated to be $2.5 \times 10^{-21} \text{m}^2 \text{s}^{-1}$ by measuring the mean square displacement (Fig. 3E). Furthermore, the activation energy for the diffusive jump of the monatomic ions was estimated using an approach with the diffusion coefficient, which gave a value of $\sim 0.9$ eV. This energy is reasonable, considering the small ionic size and high charge ($14^+$), and it leads to the slow motion of small ions. The details of the estimation method are described in section S5. Knowing these physical properties, such as the diffusion coefficient and the activation energy, enables a quantitative understanding of the atomic-scale local dynamics and environment, which determine the macroscopic properties.

In summary, we achieved direct imaging of monatomic gold ions in ionic liquids using STEM. Moreover, we observed the diffusion of the ions via a cage-jump mechanism, in which ions jump to form new cages. The diffusion behavior was spatially and temporally heterogeneous. Furthermore, the diffusion coefficient was estimated from the trajectory of the ions, and the activation energy for diffusion was estimated with an approach using the ionic diffusion coefficient.

Our observation and analysis method has the potential to reveal not only the diffusion and relaxation behavior of atoms and molecules, but also chemical reactions, such as atomic adsorption to and dissociation from catalytic molecules and nanoparticles, respectively, on the basis of the atomic-scale dynamics and activation energies. In addition, the liquid sample enables the investigation of liquid behavior in confined films by observing the dependence on the film thickness. We believe that our method will enhance the comprehensive understanding of phenomena occurring in liquids.

**MATERIALS AND METHODS**

Heavy-element ions were dispersed into the ionic liquids because they can be observed with Z-dependent contrast using ADF STEM (15, 16).

**Sample fabrication**

We selected ionic liquid C$_2$ mimTFSI (purity, 99.5%; Kanto Chemical Co., Inc.) as a solvent, the viscosity of which is 32 centipoise (at 298 K) (17). The vapor pressure at 298 K is approximately estimated to be $10^{-8}$ ~ $10^{-10}$ Pa (18). The melting point was measured to be $-17.2$°C by differential scanning calorimetry, which is consistent with previously reported values (19). Gold, a heavy element ($Z_{Au} = 79$), was dispersed into the solvent by blending with sodium tetrachloroaurate(III) dihydrate (NaAuCl$_4$·2H$_2$O) (purity, 99.99%; Wako Pure Chemical Co.) at a concentration of $0.1$ M. Gold is present as Au$^{3+}$ ions in these solutions. Liquid film samples for TEM observation were fabricated as follows (11, 20). The ionic liquid solution was blended into ethanol at a ratio of 1:10. Next, $\sim 2$ µl of the solution was dropped onto a Quantifoil R1.2/1.3 holey carbon film (Quantifoil GmbH) with a thickness of $\sim 40$ to 50 nm (11); the ethanol was then evaporated by vacuum drying ($\sim 1$ Pa, 100°C) for 20 min. The residual liquid, which is the heavy element-doped ionic liquid, forms thin films in the holes owing to surface tension.

**STEM observations**

We used an aberration-corrected STEM (JEM-ARM200CF, JEOL Ltd.) equipped with a cold-type field-emission gun operating at an accelerating voltage of 200 kV. The beam current was 9.5 pA ($5.9 \times 10^7$ electrons s$^{-1}$) and the probe diameter was $\sim 0.08$ nm. The probe-forming aperture half-angle was $24.5$ mrad; the detection angle was $0$ to $9$ mrad for bright-field imaging and $110$ to $440$ mrad for ADF imaging, which allows heavy atoms to be observed with high contrast to the background atoms ($\sim Z^2$). The imaging conditions for the experiments presented in Fig. 2 (A and B) were an image size of $1024 \times 1024$ pixels, a pixel size of 0.0076 nm per pixel, and a dwell time of 16 µs per pixel (the total acquisition time for one image was 16.8 s). The sequential images in Fig. 3A were observed with an image size of $512 \times 512$ pixels, a pixel size of 0.0152 nm per pixel, and a dwell time of 16 µs per pixel (acquisition time for one image of 4.2 s). Total dose for an image and dose per area were $2.5 \times 10^8$ electrons and $9.8 \times 10^{23}$ electrons s$^{-1}$ m$^{-2}$, respectively. The thickness of the observation area was measured by electron energy-loss spectroscopy using the log-ratio method (12). The image in Fig. 2B was processed by convoluting the averaging filter of 5 × 5 pixels with a value of 0.04. The room temperature was $23$°C. The pressure in the STEM chamber was $2 \times 10^{-5}$ Pa.

**Molecular dynamics simulation**

Molecular dynamics simulations were performed to construct liquid models for the ADF-STEM image simulation. In the C$_2$ mimTFSI simulation, the charge of each atom was estimated via a first-principles numerical-basis molecular orbital calculation based on density-functional theory using the Dmol$^3$ code for an isolated C$_2$ mimTFSI molecule in a 1.5-nm cubic supercell. Next, 64 C$_2$ mimTFSI molecules were set in a 3.015-nm cubic supercell (the density coincided with the experimental value of 1.518 g cm$^{-3}$ at $25$°C and 1 atm). A molecular dynamics simulation was then performed with the Forcite code under the conditions of the COMPASS II force field, an NVT ensemble, a time step of 1 fs, and a total time of 500 ps. The temperature was set to 1773 K to make an amorphous liquid structure in the short time.

**Multislice image simulation**

ADF image simulation was performed using the multislice method (21) with Dr. Pro1 high-resolution(STEM) TEM image simulation software. The C$_2$ mimTFSI liquid structure with a thickness of $3$ nm was prepared on the basis of the aforementioned structure determined by molecular dynamics simulations, and a gold atom was placed in the middle of the structure. The image was simulated from a 1-nm square of $64 \times 64$ pixels ($0.0156$ nm per pixel) centered on the gold atom, which satisfies the Nyquist sampling criterion. The image simulations were carried out under the same conditions as in the experiment. A Gaussian source profile with a full width at half maximum of 0.08 nm was convoluted on the simulated image. The frozen lattice model was applied to approximate the thermal atomic vibrations at each point.

**Differential scanning calorimetry**

Differential scanning calorimetry was performed using a DSC-60 Plus (Shimadzu Co.) instrument to know the melting point of the sample. The sample liquids were sealed in aluminum pans. The masses of the samples were 13 mg. The temperature range was $-120$ to $100$°C, and the cooling and heating rate was set to $5$°C min$^{-1}$.

**SUPPLEMENTARY MATERIALS**

Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/3/12/e1701546/DC1

section S1. ADF observation of different compositions (C$_2$ mimCl-Au, C$_2$ mimTFSI, and C$_2$ mimCH$_4$) section S2. Multislice image simulation for thickness, defocus, and composition dependence section S3. Splitting spot analysis
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