The Pale Green Dot: A Method to Characterize Proxima Centauri b Using Exo-Aurorae

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Abstract

We examine the feasibility of detecting auroral emission from the potentially habitable exoplanet Proxima Centauri b. Detection of aurorae would yield an independent confirmation of the planet’s existence, constrain the presence and composition of its atmosphere, and determine the planet’s eccentricity and inclination, thereby breaking the mass-inclination degeneracy. If Proxima Centauri b is a terrestrial world with an Earth-like atmosphere and magnetic field, we estimate that the power at the 5577 Å OI auroral line is on the order of 0.1 TW under steady-state stellar wind, or ~100× stronger than that on Earth. This corresponds to a planet–star contrast ratio of 10−6−10−7 in a narrow band about the 5577 Å line, though higher contrast (10−8−10−9) may be possible during periods of strong magnetospheric disturbance (auroral power 1–10 TW). We searched the Proxima Centauri b HARPS data for the 5577 Å line and for other prominent oxygen and nitrogen lines, but find no signal, indicating that the OI auroral line contrast must be lower than 2 × 10−2 (with power ≥3000 TW), consistent with our predictions. We find that observations of 0.1 TW auroral emission lines are likely infeasible with current and planned telescopes. However, future observations with a space-based coronagraphic telescope or a ground-based extremely large telescope (ELT) with a coronagraph could push sensitivity down to terawatt oxygen aurorae (contrast 7 × 10−6) with exposure times of ~1 day. If a coronagraph design contrast of 10−7 can be achieved with negligible instrumental noise, a future concept ELT could observe steady-state auroral emission in a few nights.

Key words: planets and satellites: atmospheres – planets and satellites: aurorae – planets and satellites: detection – planets and satellites: terrestrial planets

1. Introduction

The discovery of Proxima Centauri b (henceforth “Proxima Cen b”), with a distance of only 1.3 pc from the Sun (Anglada-Escudé et al. 2016), ushers in a new era of characterization of nearby potentially habitable exoplanets. Although Proxima Cen b is not known to transit—making transmission spectroscopy impossible—it is an ideal candidate for high-contrast direct spectroscopy using an extremely large coronagraph-equipped telescope. However, even with the enhancement in angular resolution provided by the proximity of its host star, Proxima Cen b’s close-in orbit (a = 0.0485 au; Anglada-Escudé et al. 2016) precludes imaging with current coronagraphs, such as the Gemini Planet Imager (GPI; Macintosh et al. 2014) and the Very Large Telescope’s Spectro-Polarimetric High-contrast Exoplanet REsearch facility (VLTI-SPHERE; Beuzit et al. 2008), which operate primarily in the near-infrared. This is in part due to the poorer Strehl ratios currently achievable at visible wavelengths with ground-based adaptive optics (AO) systems.5 Consequently, in advance of larger diameter ground- and space-based telescopes, and improvements in visible AO systems, we must initially consider observations that do not rely on transits or current coronagraphy to search for and characterize the atmosphere of Proxima Cen b.

Phase curves may offer one of the first means to study the atmosphere of Proxima Cen b (Kreidberg & Loeb 2016; Meadows et al. 2016; Turbet et al. 2016) by potentially showing the reduction in day–night thermal emission contrast associated with an atmosphere. Phase curves have proven to be a successful means to characterize the atmospheres of planets larger and hotter than Proxima Cen b (Cowan et al. 2007; Knutson et al. 2007, 2008; Crossfield et al. 2010; Brogi et al. 2012; Stevenson et al. 2014; Zellem et al. 2014), including ones that do not transit (Faigler & Mazeh 2011; Selis et al. 2011; Maurin et al. 2012; Brogi et al. 2014). However, the expected planet–star contrast ratio in the visible and NIR due to reflected stellar radiation is likely to be below the anticipated systematic noise floor for JWST/NIRSpec (Meadows et al. 2016), and although the planet–star contrast ratio becomes quite favorable beyond 10 μm, where the planetary thermal emission peaks, mid-IR phase curves will require JWST/MIRI.

To complement the anticipated JWST thermal phase curve measurements, in this work, we explore the possibility of directly detecting optical auroral emission from the atmosphere of Proxima Cen b using high-resolution optical spectroscopy. Numerous studies have investigated exoplanet aurorae in the radio due to cyclotron and synchrotron emission to constrain the planetary magnetic field (e.g., Bastian et al. 2000; Grießmeier et al. 2007; Zarka 2007; Driscoll & Olson 2011; Hess & Zarka 2011; Grießmeier 2015, pp. 213–237). Others have explored the detectability of optical and UV auroral emission from hot Jupiters, including France et al. (2010), who searched for far-UV auroral and dayglow H2 emission from the hot Jupiter HD 209458b and placed upper limits on its magnetic field strength, and Menager et al. (2013), who studied the detectability of Lyα auroral emission from HD 209458b and HD 189733b. Some studies have also

5 See, e.g., https://www.eso.org/sci/facilities/paranal/instruments/sphere/overview.html.
investigated auroral emission from terrestrial planets, including Smith et al. (2004), who modeled the role of aurorae in redistributing high energy incident stellar flux to the surface of rocky exoplanets, and Bernard et al. (2014), who investigated how the detection of the green oxygen airlow line could be used to infer the presence of planetary hydrogen coronae on CO2-dominated planets. Finally, Sparks & Ford (2002) suggested that exoplanet airlow and/or aurorae could be detected with a combination of high-contrast imaging and high dispersion spectroscopy. However, a detailed calculation of the expected auroral signal strength on a nearby terrestrial exoplanet and the feasibility of its detection has not yet been fully performed.

Detecting optical auroral emission from the possible atmosphere of Proxima Cen b is likely much more favorable for this system than for an Earth–Sun analog. This is due to both planetary and stellar characteristics that favor auroral production and improve detectability (see Table 1). In particular, Proxima Cen b’s intrinsic planetary properties may favor production of aurorae from oxygen atoms. If Proxima Cen b is Earth-like in composition, recent dynamical/planetary interior modeling results by Barnes et al. (2016) and Zuluaga & Bustamante (2016) suggest that the planet may have a magnetic field, potentially increasing the likelihood of atmospheric retention and of auroral emission. Atmospheres rich in oxygen-bearing molecules, including O2 and CO2, have been predicted for Proxima Cen b (Meadows et al. 2016) as a result of the evolutionary processes for terrestrial planets orbiting M dwarfs (Luger & Barnes 2015; Barnes et al. 2016). On Earth, the oxygen (O1) auroral line at 5577 Å provides the distinctive green glow observed in both the Aurora Borealis and the Aurora Australis, and is the brightest (i.e., highest photon emission rate) auroral feature (Chamberlain 1961; Dempsey et al. 2005). For emissions from the upper atmosphere, only the 1.27 μm O2 airlow and combined near-infrared OH night glow features are brighter (Hunten et al. 1967). The oxygen green line is seen in both the Earth’s O2-rich atmosphere (Chamberlain 1961) and Venus’ CO2-dominated atmosphere (Slanger et al. 2001), where it has been observed to increase in brightness after CME events (Gray et al. 2014).

Table 1
Proxima Centauri b Properties

| Property                          | Valuea  | 1σ Interval |
|----------------------------------|---------|-------------|
| Distance from Earth (pc)         | 1.295   | ...         |
| Host spectral type               | M5.5V   |             |
| Host mass, M_*(M⊙)              | 0.120   | [0.105–0.135]|
| Period, P (days)                 | 11.186  | [11.184–11.187]|
| Semimajor axis, a (au)           | 0.0485  | [0.0434–0.0526]|
| Minimum mass, m_p sin i (M⊙)    | 1.27    | [1.10–1.46] |
| Radius, R_p (R⊙)                 | Unknown | [0.94–1.40]b|
| Eccentricity, e                  | <0.35   |             |
| Mean longitude, λ (°)            | 110     | [102–118]   |
| Inclination, i (°)               | Unknown | [0–90]      |

Notes.

a Values from Anglada-Escudé et al. (2016) unless otherwise noted.

b Plausible range from Brugger et al. (2016), assuming m_p = 1.27M_E.

activity drives auroral emission for an Earth-like magnetosphere, such features may be much stronger on planets orbiting active M dwarfs. Additionally, with a close-in orbit of 0.0485 au, Proxima Cen b is about 20× closer to Proxima Centauri than the Earth is to the Sun (Anglada-Escudé et al. 2016). This proximity further increases particle fluxes incident on the planetary atmosphere that drive ionization and the subsequent recombination radiation.

In addition to increasing the likelihood and strength of the aurora, the characteristics of the Proxima Centauri system may also enhance its detectability. Since the Proxima system is only 1.3 pc away, it is perhaps the best-case scenario for the detection of the faint auroral signal from a terrestrial exoplanet. Even though the planet–star contrast ratio in reflected visible light is poor (≤10−7; see Kreidberg & Loeb 2016; Meadows et al. 2016; Turbet et al. 2016), if Proxima Cen b exhibits auroral emission, this will brighten the planet and potentially boost the planet–star contrast by one or more orders of magnitude at the wavelengths of the auroral emission features. The short wavelength of the oxygen green line also improves the contrast of the planet relative to the star due to the star’s cool temperature and TiO absorption, which strongly suppresses the brightness of the star in the visible. This improvement in contrast is significantly less for the near-infrared O2 1.27 μm and OH airlow lines. In addition to increasing the contrast, the small semimajor axis of Proxima Cen b results in an orbital velocity of ~50 km s−1, which will cause its auroral emission to be Doppler-shifted by as much as 1 Å over the course of its orbit, making it easier to disentangle it from stellar features via high-resolution spectroscopy. An additional advantage of the short wavelength of the O1 feature is the smaller inner working angle and point-spread function that may be achieved with a coronagraph at that wavelength (Agol 2007). These factors all improve the chance of detection with ground-based telescopes.

The detection of the oxygen auroral line at 5577 Å would provide an important diagnostic for planetary properties. Its detection would not only confirm the existence of the planet, but would point to the presence of an atmosphere with abundant oxygen atoms, which is more likely to indicate a terrestrial body. Additionally, the detection of the line would yield a measurement of the radial velocity (RV) of the planet, which combined with the RV measurements of the star (Anglada-Escudé et al. 2016) would enable the measurement of the eccentricity and inclination of the orbit, ultimately yielding the mass of the planet (see, e.g., Lovis & Fischer 2010, pp. 27–53). Detection of the oxygen auroral line would therefore provide several key planetary parameters that could be used to constrain Proxima Cen b’s potential habitability (Barnes et al. 2016; Meadows et al. 2016).

This paper is organized as follows. In Section 2, we calculate the expected auroral emission strength of Proxima Cen b under different assumptions of stellar and planetary properties. In Section 3, we model the planet–star contrast ratio in a narrow band centered on the O1 5577 Å line and calculate the integration times required to detect the feature with different instruments. In Section 4, we conduct a preliminary search for auroral emission in the HARPS high-resolution, ground-based spectroscopy used by Anglada-Escudé et al. (2016) for the RV detection of Proxima Cen b. Finally, in Section 5, we discuss our results and present our conclusions.
2. Auroral Signal Strength

Below, we quantitatively estimate the auroral intensity for steady-state stellar input. We assume the planet to be terrestrial with the orbital characteristics of Proxima Cen b (see Table 1) and calculate the auroral emission via two different methods. Method 1 (Section 2.3) involves a simple estimation of the emitted electromagnetic auroral power driven by the stellar wind power delivered at the magnetopause of the planet. Method 2 (Section 2.4) uses the prediction of a magnetohydrodynamical (MHD) model that was tuned to calculate the auroral response at Earth, with modifications to the relevant inputs of the stellar wind of Proxima Centauri and assumed planetary parameters for Proxima Cen b (Anglada-Escudé et al. 2016).

The quantities we calculate include only the estimated, localized emissions caused by magnetospheric particle precipitation into a discrete auroral oval—not the diffuse, global phenomenon of airglow. On Earth, the 5577 Å airglow can be visible to the naked eye and could be significant on Proxima Cen b, but is commonly driven by different physical processes (e.g., nightside recombination due to dayside photoionization) that are outside the scope of this analysis. Similarly, the 5577 Å airglow has been observed at Venus (e.g., Slinger et al. 2001) and Mars (e.g., Seth et al. 2002)—both having no present-day global magnetic field. For these reasons, we cannot suggest basing the existence of or placing constraints on Proxima Cen b’s planetary magnetic field based on the detection of this auroral line (see, for instance, Grießmeier 2015). A search for radio emission from Proxima Cen b—which may be correlated with optical auroral emission, as it is on Earth and on Saturn (Kurth et al. 2005)—would likely be necessary to constrain the planetary magnetic field. However, it is worth noting that an Earth-like 1 kR (1 R = 1 Rayleigh = 10^9 photons s cm^-2) airglow across the entire planet would still emit ∼2 orders of magnitude less energy than the discrete polar aurora—see Section 2.6 below.

2.1. Stellar Winds at Proxima Cen b

M dwarf mass-loss rates, and therefore stellar winds, are not well constrained due to observational sparsity and difficulty (e.g., Wood et al. 2004). To model the M dwarf winds for Proxima Centauri, we adopt the predictions from the modeling efforts of Cohen et al. (2014), who generated an MHD stellar wind model for the M3.5 star EV Lacertae based on available observations. There are two primary differences between EV Lac and Proxima Centauri that we should take into account when considering the stellar wind at our planet’s location of interest: (1) the relative mass-loss rates and (2) the difference in rotation rates.

The first of these factors has been estimated by Wood et al. (2005), who find that the mass-loss per unit surface area for Proxima Centauri and EV Lacertae are quite similar. This suggests comparable wind conditions at equal distances in units of their respective stellar radii.

The second factor, the rotation rate, affects the morphology of the stellar wind magnetic field by changing the Alfvén radius. The Alfvén radius, $R_A$, is defined as the point where the Alfvén Mach number is equal to unity—i.e., $M_A \equiv \frac{u_{sw}}{v_A} = 1$, where $u_{sw}$ is the stellar wind speed and $v_A$ is the Alfvén speed. Interior to $R_A$ (the sub-Alfvénic wind), the magnetic field of the star is mostly radial, and corotates at the angular rate of the star; exterior to $R_A$ (the super-Alfvénic wind) the field begins to lag behind corotation as the magnetic tension is overcome by the flow of the wind. In the super-Alfvénic regime, the interplanetary magnetic field (IMF) exhibits the well-known Parker-spiral (Parker 1958). The Alfvén point is an important boundary that modifies the energy transfer between the stellar wind and the planetary magnetosphere.

To correctly estimate the interactions, it is important to consider Proxima Cen b’s orbital distance from its host star, for both the dynamic parameters (mass density, velocity) and the magnetic structure—i.e., we must consider where Proxima Cen b orbits relative to its Alfvén radius, $R_A$. We note that the rotational period of Proxima Centauri (82.6 days; Collins et al. 2016) is ∼19 times lower than EV Lacertae (4.376 days; Testa et al. 2004). For our purposes, we estimate an average $R_A$ for a simple stellar dipole moment:

$$R_A = \left(\frac{4\pi M_*^2}{M_A \omega_\star \mu_0}\right)^{1/3},$$

where $M_*$ is the magnetic dipole moment for the star, $M_A$ is the mass-loss rate, $\omega_\star$ is the angular frequency of stellar rotation, and $\mu_0$ is the vacuum permeability. For EV Lacertae and Proxima Centauri, $R_A$ are ∼65.4 R$_\star$ (0.075 au) and 115 R$_\star$ (0.192 au), respectively. This is the average value for a simple dipole moment because we are not including magnetic topology, but nonetheless the value obtained for EV Lac agrees well with the approximate average for the more complicated magnetic treatment simulated in Cohen et al. (2014). The relative orbit for Proxima Cen b is therefore ∼0.76 R$_\star$. Coincidentally, this corresponds well with the simulated Planet B at EV Lac in Cohen et al. (2014), which orbits at ∼0.79 $R_A$.

Recently, Garraffo et al. (2016) applied an MHD model of stellar winds based on the Zeeman–Doppler Imaging (ZDI) of GJ51, and scaled the magnitude of the surface field to match the anticipated value of 600 G for Proxima Centauri. Their results from the assumed magnetic environment are in line with the values we adopt from Table 2, and our value calculated for the magnetopause distance using Equation (3) below is within the range of their calculations for magnetopause distance for Proxima Cen b. However, the structure of the magnetic topology in the simulation of Garraffo et al. (2016) places Proxima Cen b primarily in the super-Alfvénic wind, contrary to both the simple method above and the bulk of the structure found by Cohen et al. (2014).

### Table 2

| Quantity | Sub-Alfvénic | Super-Alfvénic |
|----------|-------------|----------------|
| $n$ (cm$^{-3}$) | 433 | 12895 |
| $T$ (10$^5$ K) | 3.42 | 4.77 |
| $u$ (km s$^{-1}$) | (−630, −1, 30) | (−202, 102, 22) |
| $B$ (nT) | (−804, 173, 63) | (−57, 223, 92) |
| $M_A$ | 0.73 | 4.76 |

**Note.** Stellar wind conditions from Cohen et al. (2014), at EV Lacertae for $a = 51.98$ R$_\star$ (0.073 au). $n$ is the stellar wind number density, $T$ is the ion temperature, $u$ is the velocity, $B$ is the interplanetary magnetic field (IMF), and $M_A$ is the Alfvén mach number.
Our estimate of $R_A$ does not take into account the complicated magnetic topology of a realistic stellar magnetic field, which could indicate the planet likely orbits primarily through sub-Alfvénic conditions (e.g., Figure 1 of Cohen et al. 2014) or through primarily super-Alfvénic conditions (Figure 2 from Garraffo et al. 2016). Therefore, we consider both super- and sub-Alfvénic conditions for the steady-state stellar wind, using the reported parameters at Planet B from Cohen et al. (2014); see Table 2.

2.2. Magnetic Dipole Moment of Proxima Cen b

Tidal locking is likely for the expected orbital parameters of Proxima Cen b and the age of the system. We therefore expect a rotational period equal to the orbital period, 11.186 days, or 8.94% of the Earth’s rotational frequency. Following the magnetic moment scaling of Stevenson (1983) and Mizutani et al. (1992), we assume the upper limit of the rotationally driven planetary dynamo as $\mathcal{M} \propto \omega^{1/3} r_c^2$, where $\mathcal{M}$ is the magnetic moment, $\omega$ is the rotation rate of the planet, and $r_c$ is the core radius (which we assume to be proportional to the planetary radius). This suggests a magnetic moment for an Earth-radius Proxima Cen b of $\sim 0.3 \mathcal{M}_\oplus$. Taking the upper limit of the expected radius of Proxima Cen b, 1.4 $R_\oplus$, this gives a magnetic moment of $\sim 0.8 \mathcal{M}_\oplus$, which agrees with the upper limit of Zuluaga & Bustamante (2016). However, Driscoll & Barnes (2015) showed that for an Earth-like terrestrial planet orbiting a star of 0.1 $M_\odot$ with high initial eccentricity ($e \geq 0.1$) within 0.07 au, the planet will circularize before 1 Gyr. On this timescale, the orbital energy dissipated as tidal heating is sufficient to drive a strong convective flow in the planetary interior that could generate a magnetic moment in the range of $\sim 0.8-2.0 \mathcal{M}_\oplus$ during the process of circularization. Given the above, we consider the situation of an Earth magnitude magnetic field for Proxima Cen b, but discuss how each of the methods below can be scaled to various magnetic dipole moments.

2.3. Auroral Stellar Wind Power Scaling

Desch & Kaiser (1984) suggested a correlation between incident stellar wind power and the power of planetary radio emissions in the solar system, a so-called “radiometric Bode’s law.” Zarka (2006). Zarka (2007) extended the work to modern solar system measurements as well as potential exoplanetary systems, and further suggested that a similar “auroral UV-magnetic Bode’s law” could exist, though the author notes such scaling would be less generally applicable than the radio case across planetary systems due to the complexities of UV auroral generation for differing planetary atmospheres and magnetospheric dynamics. The calculations in this section can be thought of similarly as a “visible-kinetic Bode’s law” for the specific case of exoplanets with an Earth-like atmosphere. A similar relation may also be derived for the magnetic stellar wind interaction (e.g., a “visible-magnetic Bode’s law”; details below).

The stellar wind kinetic power delivered to the magnetosphere of the planet can be expressed as

$$P_U = \rho \, v^3 \, \pi \, R_{MP}^2,$$  \hspace{1cm} (2)

where $\rho$ and $v$ are the stellar wind mass density and velocity relative to planetary motion ($\sim 48$ km s$^{-1}$), respectively, and $R_{MP}$ is the magnetopause distance along the line connecting the star and planet (sub-stellar point). The latter can be estimated through magnetospheric pressure balance with the stellar wind dynamic ram pressure (e.g., Schield 1969):

$$\frac{2 \, \mathcal{M}^2}{K_{SW} \, \mu_0 \, R_{MP}^2} = \rho_{ram},$$  \hspace{1cm} (3)

where $\mathcal{M}$ represents the magnitude of the magnetic dipole moment, $K_{SW}$ is related to particle reflection at the magnetopause (herein the interaction is assumed to consist of inelastic collisions, or $K_{SW} = 1$), and $R_{MP}$ is the distance from the planet at which the magnetic pressure of the planet balances the pressure of the stellar wind. The RHS of Equation (3) represents the dynamic ram ($\rho_{ram} = \rho^2$) pressure of the stellar wind, calculated from the values in Table 2.

We consider an Earth-strength magnetic dipole moment of $\mathcal{M} = 8.0 \times 10^{15}$ Tesla m$^3$. Solving for $R_{MP}$ in Equation (3) and inserting into Equation (2) provides an estimate of the stellar wind power incident on the planetary magnetopause. Externally driven planetary auroral systems are not typically 100% efficient at converting the incident stellar wind power into electromagnetic auroral emission, and range from $\sim 0.3\%$ at Neptune, $\sim 1\%$ at Earth, and up to almost 100% at Jupiter (e.g., Cheng 1990; Bhardwaj & Gladstone 2000). For reference, at Earth, this method gives us a reasonable estimate of the total emitted electromagnetic auroral power of $\sim 30$ GW for nominal solar wind conditions ($4 \, cm^{-3}, 400 \, km \, s^{-1}$), which is consistent with the anticipated power of 1–100 GW, depending on solar and magnetospheric activity. While the intensities of various emissions vary widely with activity and atmospheric conditions, we assume an averaged auroral emission. In order to estimate the emitted power of the O I 5577 Å line, we assume it represents 2% of all emitted electromagnetic power (Chamberlain 1961; Kivelson & Russell 1995, p. 586), as calculated by Equation (2). We note that this assumes an Earth-like atmosphere for the planet; we briefly discuss the effect of different atmospheric compositions in Section 5.

Figure 1 shows the predicted emitted power of the 5577 Å line based on Equation (2) and multiplied by the 2% factor mentioned above and by the conversion efficiency of 1%. For the Earth, this method predicts a power of $\phi_{5577} \sim 0.68$ GW in the 5577 Å line. Assuming a 5° latitudinal width starting at $\sim 18°$ co-latitude and extending equatorward, this corresponds to a photon flux of $\sim 13.7$ kR. This is in agreement with moderate auroral activity (IBC II$^6$, 10 kR 5577 Å emission; see Table 2.1 in Chamberlain 1961), and within a factor of 2–5 of observations during moderate geomagnetic disturbance (2.5–6 kR 5577 Å emission, e.g., Steele & McEwen 1990).

Power estimates for the 5577 Å line for a 0.05 au orbit around Proxima Centauri are shown in Table 3. The calculated power is $\sim 75.3$ (54.7) times $\phi_{5577}$ in the sub-(super-) Alfvénic stellar wind. These are the estimates for a steady-state stellar wind, for a terrestrial planet with an Earth-like magnetic dipole moment. Note that by inspection of Equations (2) and (3), one can see that the expected power scales as $\mathcal{M}^2/\gamma$, and so can easily be extended to different planetary dipole moments.

The method above has a weakness in that it completely ignores the incident Poynting flux from the IMF, and potential direct magnetic interactions between the stellar wind and

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$^6$ IBC—International Brightness Coefficients, a standardized scale for quantifying auroral intensities (see, e.g., Hunten 1955).
planetary magnetic field, e.g., flux merging or reconnection. These interactions can produce a significant amount of magnetospheric energy input, and so they are important to consider. Similar to Equation (2), a scaling relation between power emitted at the 5577 Å line and incident magnetic flux in the stellar wind, akin to a visible-magnetic Bode’s law, can be given as (e.g., Zarka 2006; Grießmeier et al. 2007; Zarka 2007)

\[ P_B = \epsilon K \left( \frac{v B_x^2}{\mu_0} \right) \pi R_{MP}^2, \]  

where \( \epsilon \) is the efficiency of reconnection (typically of the order of 0.1–0.2), \( K \) is related to the “openness” of the magnetosphere, and for an Earth-like dipole is \( K = \sin^4(\theta/2) \), where \( \theta \) is the angle between the perpendicular IMF and planetary dipole field, \( B_\perp \), the perpendicular IMF \( \left( \sqrt{B_1^2 + B_2^2} \right) \), \( \mu_0 \) is the vacuum permeability, and \( R_{MP} \) is the magnetopause sub-stellar point discussed above. We can estimate the magnetic interaction at Proxima Cen b using our stellar wind conditions by taking the ratio of Equations (4) and (2):

\[ \frac{P_B}{P_U} = \epsilon K \frac{B_x^2}{\mu_0 v^2}, \]  

which is essentially the ratio of the perpendicular IMF magnetic pressure to the ram pressure, modulated by magnetic field orientation and reconnection efficiency. In the best-case scenario, \( K \) is equal to 1 (indicating \( \theta = \pi \), driving strong reconnection at the magnetopause), and \( \epsilon \) is of the order of 0.2 or so. Assuming this best case, and inserting the values from Table 2 for the sub- and super-Alfvénic cases, one obtains a ratio of \( \sim 0.019 \) and 0.0084 for the sub- and super-Alfvénic cases, respectively. For the particular stellar wind parameters we have chosen, the kinetic power dominates the anticipated auroral output for Proxima Cen b. It is worth noting, however, that the magnetic environment (both planet and star) is largely unconstrained, and highly dynamic—particularly near active M dwarfs.

2.4. 3D MHD Empirical Energy Coupling

Equations (2) and (4) above are decent first approximations, but involve significant uncertainties concerning the energy dissipation in physical phenomena throughout the magnetosphere (i.e., auroral activity; Perreault & Akasofu 1978; Akasofu 1981). Wang et al. (2014) developed a global, 3D MHD model to obtain a fit for the energy coupling between the solar wind and Earth’s magnetosphere to estimate the energy transferred directly from the wind into the magnetosphere and auroral precipitation (see their Equation (13) and below). The simulations were performed over 240 iterations across their solar wind parameter space, and the resulting nonlinear fit for the energy transfer to the terrestrial magnetosphere was found to be

\[ P_{\text{trans}} = K_i n_{sw}^{0.24} v_{sw}^{1.47} B_T^{0.86} \left[ \sin^{2.5} \left( \theta/2 \right) + 0.25 \right], \]  

where \( K_i = 3.78 \times 10^7 \) is a coupling constant, \( n_{sw} \) and \( v_{sw} \) are the stellar wind number density (in \( \text{cm}^{-3} \)) and velocity relative to planetary motion (in \( \text{km} \text{s}^{-1} \)), respectively, \( B_T \) is the magnitude of the transverse component of the Sun’s IMF \( (B_T = \sqrt{B_1^2 + B_2^2}) \) in nT, and \( \theta \) is the so-called IMF clock angle (\( \tan \theta = B_1/B_2 \)). The coordinate system used is the geocentric solar magnetospheric (GSM) system, with \( \hat{X} \) pointing from the planet to the star, \( \hat{Y} \) aligned with the magnetic dipole axis of the planet (here assumed to be perpendicular to the ecliptic), and \( \hat{Z} \) completing a right-handed coordinate system.

Wang et al. (2014) were focused solely on the Earth’s magnetosphere, but one can scale to any dipole moment by noting that Equation (6) scales just as in Section 2.3: the dipole moment term is implicitly included in the coupling constant \( K_i \) above and scales with the planetary magnetic dipole magnitude as \( M_p^{1/3} \) (Vasyliunas et al. 1982, also Equations (2) and (3) above).

Equation (6) is the total power delivered by the stellar wind to the magnetosphere, which Wang et al. (2014) estimate is \( \sim 13\% \) of the total incident stellar wind energy. They further estimate that 12% of that energy is dissipated by particle precipitation into the auroral regions, yielding a total solar wind/auroral coupling efficiency of \( \sim 1.56\% \)—very similar to the efficiency value of 1% assumed for Earth and Proxima Cen b in Section 2.3. As simple validation for our purposes, we use this method to predict a maximum coupling of auroral particle precipitation (with IMF clock angle \( \theta = \pi \), driving reconnection and likely substorm activity) at Earth of \( \sim 0.17 \) TW. This is in agreement with terrestrial plasma observations during periods of geomagnetic disturbance (e.g., Hubert et al. 2002). This method is useful in that it provides a direct relationship between the power delivered as auroral particle precipitation and incident stellar wind conditions.

For Proxima Cen b, subjected to the stellar winds from Table 2, this method predicts a total power of auroral particle precipitation of \( \sim 10.7 \) (5.8) TW for the sub-(super-)Alfvénic
stellar wind. The stellar wind parameters in Table 2, however, are a snapshot and not indicative of the highly variable conditions likely experienced at Proxima Cen b.

Magnetospheric substorms, related to transient populations of energized particles driven by magnetic reconnection in the magnetotail, can drive strong increases in auroral particle precipitation. Though not a one-to-one indicator, substorm activity can be associated with periods of strong reconnection at the magnetopause—correlated with a significant negative $B_Z$ component in the IMF. In the present work, we assume $\theta = \pi$, or $B_Y = 0$, to obtain an upper limit to substorm influence under our model. Although this is not a strict definition, Wang et al. (2014) calibrated the model used here to include periods of substorm activity and high hemispheric energy input. Assuming with this strong negative $B_Z$ that a substorm is driven at Proxima Cen b, we predict an energy input of $\sim$28.3 (15.9) TW for the sub-(super-)Alfvénic wind. To compare directly to the 5577 Å line auroral power output such as that calculated in Section 2.3, we must link these values to the aurora by including the efficiency of precipitating charged particles in the production of auroral emission for the 5577 Å line, which will be done below.

To calculate the auroral 5577 Å photon flux, we use the precipitating auroral particle powers above obtained from Equation (6), and combine with the anticipated size of the auroral oval and an observed conversion efficiency for electron precipitation to 5577 Å emission. This gives the photon flux in kR, $\phi_{5577}$:

$$\phi_{5577} = P_{in} A_{mag}^{-1} \epsilon_e,$$

where $P_{in}$ is 12% (discussed above) of $P_{trans}$ from Equation (6), $A_{mag}$ is the summed area of both the northern and southern auroral ovals (we assume N–S symmetry), and $\epsilon_e$ is the efficiency with which magnetospheric electrons are converted to auroral emission of the 5577 Å oxygen line. We use the reported values from Steele & McEwen (1990; noted below), who used ground-based observations of auroral line intensities and the related satellite observations of energetic electron flux to draw a relation between electron precipitation and auroral photon flux. We then integrate the resulting flux over a nominal 5° auroral oval (for each hemisphere), the co-latitude of which is dependent on the sub-stellar magnetopause distance (discussed below).

Steele & McEwen (1990) reported the conversion efficiency for the 5577 Å O I line as $1.73 \pm 0.51$ (1.23 ± 0.44) kR/erg cm$^{-2}$ s$^{-1}$ for a magnetospheric Maxwellian electron population of characteristic temperature $1.8$ (3.1) keV. In the present work, we take the average values for these populations, $\sim 1.48$ kR/erg cm$^{-2}$ s$^{-1}$. We assume the fraction of total hemispheric power ($P_{in}$) delivered by electrons to be 0.8 (Hubert et al. 2002), so this factor is included in the $P_{in}$ factor.

The magnetopause distance we calculate via Equation (3) for the Earth-like magnetic dipole moment is $\sim$4.2 (3.3) $R_P$ for the (sub-)super-Alfvénic conditions. From these values, we can provide a simple estimate of the total auroral oval coverage. The magnetic co-latitude of the boundary between open and closed flux for our assumed ideal planetary dipole geometry (i.e., the co-latitude where the field structure no longer intersects the planetary surface) is $\sin^{-1}(1/\sqrt{R_{mp}})$ (Kivelson & Russell 1995). Discrete auroral activity occurs primarily due to energized plasma originating from closed field structure stretched out behind the planet in the stellar wind, i.e., the magnetotail. This field structure intersects the planet equatorward of the open/closed boundary co-latitude. If we assume a nominal 5° auroral oval width beginning at the co-latitude obtained, and extending equatorward, we calculate a single-hemisphere coverage of $\sim 1.17 \times 10^{17}$ cm$^2$ for the auroral oval under sub-Alfvénic conditions, and $\sim 1.30 \times 10^{17}$ cm$^2$ under super-Alfvénic conditions.

Following the above, we obtain a photon flux value of $\phi_{5577} \sim 2.26$ (1.16) MR for the sub-(super-)Alfvénic wind conditions. This corresponds to our predicted emission power in Table 3, method 2 (quiet) of $\sim 0.090$ (0.049) TW under steady-state sub-(super-)Alfvénic conditions. For the maximum emission during a magnetospheric substorm, we obtain values of $\sim 0.24$ (0.14) TW for sub-(super-)Alfvénic winds.

There is another case of interactions that we should consider that involves stellar activity—flaring and coronal mass ejections (CME). During these events, stellar wind densities could increase by a factor of $\sim 10$, velocities by a factor of $\sim 3$, and IMF magnitude by a factor of $\sim 10$–20 (Khodachenko et al. 2007; Gopalswamy et al. 2009). Inserting such ratios in the 3D MHD-fit predicted power in from Equation (6), we predict transient maximum 5577 Å emissions of $\sim 8.10$ (4.40) TW for the sub-(super-)Alfvénic CME conditions. For the maximum emission during a magnetospheric substorm under CME conditions, we obtain values of $\sim 21.42$ (12.10) TW for sub-(super-)Alfvénic winds. These transient CME conditions can have timescales of $\sim 10$–10$^3$ minutes per event, with multiple, consecutive events possible. Given that Davenport et al. (2016) report such high stellar activity for Proxima Centauri, Proxima Cen b could experience CME impacts for a large percentage of its orbital phase (e.g., Khodachenko et al. 2007).

### 2.5. Unmagnetized Planet

The above results all assume a large, Earth-like planetary magnetic dipole moment for Proxima Cen b. If, in fact, the

| Case          | Method 1 (TW) | Method 2 (quiet) (TW) | Method 2 (SS) (TW) | Method 2 (CME) (TW) | Method 2 (CME+SS) (TW) |
|---------------|--------------|-----------------------|--------------------|---------------------|------------------------|
| Prox Cen b (Sub) | 0.051        | 0.09                  | 0.24               | 8.103               | 21.42                  |
| Prox Cen b (Sup) | 0.038        | 0.049                 | 0.14               | 4.41                | 12.10                  |
| Earth/Sun     | $6.7 \times 10^{-4}$ | $7.5 \times 10^{-4}$   | $1.5 \times 10^{-3}$ | 0.068               | 0.1317                 |

**Note.** Power emitted for the O 5577 Å line in terrawatts (TW) for an Earth-strength magnetic dipole on Proxima Cen b in the sub-Alfvénic (Sub) and super-Alfvénic (Sup) stellar winds. For method 2: column 2 assumes no significant stellar activity and a quiet magnetosphere; column 3 assumes geomagnetic substorm (SS) activity; column 4 assumes CME conditions in the stellar winds, but no magnetospheric disturbance; column 5 assumes both CME conditions and substorm activity.
planet does not sustain a global dynamo, it will only be protected by a relatively thin spherical shell (~1000 km) of plasma in the upper atmosphere—similar to Earth’s ionosphere.

For the sub-Alfvénic case, the interaction is a unipolar interaction similar to the Jupiter–Io interaction (Zarka 2007). In this case, the power dissipated by the wind is similar to the form of Equation (4), where $c$ and $K$ are replaced by a single parameter indicating the fraction of magnetic flux convected onto the “obstacle” (the ionosphere), and $R_{\text{Io}p}$ becomes the size of the “obstacle”—for an Earth-like ionosphere, ~1.16 planetary radii. While there is no dipolar focusing mechanism for the particle precipitation in this case, it is worth considering the energized particles flowing on the flux tube connecting the unmagnetized planet with the star, producing maxima on the unmagnetized body in the plane perpendicular to the IMF (see, e.g., Saur et al. 2000, 2004).

Assuming 100% of incident magnetic energy flux is convected onto the planet and ionosphere, the expected 5577 Å auroral power becomes $5.9 \times 10^{-4} \text{ TW}$ for the sub-Alfvénic stellar wind conditions in Table 2. This interaction is likely insignificant in the context of remote sensing.

For the super-Alfvénic flow, this could be considered as analogous to Venus’ situation, which sustains no global magnetic field. In this case, the discrete aurora would obviously not be expected due to a lack of magnetic structure, though induced airglow is still a consideration. Lacking a planetary magnetosphere, the magnetic structure fails to focus precipitating particles into the upper atmosphere of such a planet, though there is still magnetic interaction at the planet. The ionosphere is a spherical, conducting shell, and so interacts with the magnetic flux from the IMF as it drapes over and around the planet. Energized particles in the impacting stellar wind magnetic flux could still dip down into the upper atmosphere, depositing sufficient energy to produce airglow—this is especially true for the strong flows from CME activity, or fast stellar wind flow.

A study of the intensity of 5577 Å oxygen emission at Venus, relative to Earth, for CME/flare events from the Sun was performed by Gray et al. (2014). The results indicated that the airglow was relatively on par with that of Earth’s upper atmosphere, varying between 10 and a few hundred Rayleigh, which, if integrated over an entire hemisphere of an Earth-like planet, gives a value less than 1% of the discrete values given in Table 3. For the super-Alfvénic flow in Table 2, the number density is ~1500 times greater than the average at Venus, and the velocity is a factor of ~0.5 that at Venus or Earth. Given the power scales as $\rho v^3$, this is a factor of ~200 greater power delivered to the planet. Assuming that airglow at an unmagnetized Proxima Cen b scales linearly with the incident power, this would give a brightness of ~2–60 kR, which is at most a factor of ~5 times the value for Earth using Method 1 and 2 in Table 3, or on the order of $10^{-3} \text{ TW}$. Given our discussion of auroral detectability below (Section 3), we do not expect that this signal could be observed with either current or upcoming missions.

2.6. Signal Summary

The preceding estimates are mostly conservative. It is possible that all the auroral numbers reported for the sub-Alfvénic cases above could be a factor of four to five (or more) larger. We are assuming a simple dipolar interaction with the stellar wind, which is not specifically the case for a planetary dipole in the sub-Alfvénic stellar wind; these interactions are more akin to the interactions of Ganymede and Io with the corotating magnetosphere of Jupiter, with the formation of Alfvén wings. Modeling efforts by Preusse et al. (2007) showed that for a giant planet with a dipole magnetic moment, field-aligned currents (which are associated with auroral activity) are significantly stronger for planets orbiting inside the Alfvén radius of their stellar host. Our estimates, therefore, could be viewed as lower limits. It is also worth noting that Cohen et al. (2014) suggested that a transition between the sub- and super-Alfvénic conditions would likely produce enhanced magnetospheric activity and therefore could lead to a periodicity in the auroral activity depending on combined planetary orbital and stellar rotational phases.

For planets in the solar system, only Mars and Earth exhibit observed, significant 5577 Å emission for both diffuse airglow and discrete aurora. Mars does not presently have a global magnetic field, but there are crustal regions containing the remnants of previous magnetization that exist and focus particles into the upper atmosphere to produce a relatively weak (inferred ~30 $R_{\text{5577A}}$) discrete aurora that is ~10 times the strength of the nominal airglow (e.g., Acuña et al. 2001; Bertaux et al. 2005; Lilensten et al. 2015). On Earth, the airglow and aurora are typically in the range of 0.01–1 kR and 1–1000 kR, respectively. During transient periods of minimal auroral activity and maximum airglow emission, emissions can be roughly equivalent, but the average ratio of airglow emission to auroral emission is ≤1% (e.g., Chamberlain 1961; Greer et al. 1986). Even for a constant, planet-wide 1 kR airglow on an Earth-sized planet at Proxima Cen b ($R_{\text{P}} \sim 6371 \text{ km}$), the total signal from the observer-facing hemisphere would be ~$4.54 \times 10^8 \text{W}$, which is ~1% of the lowest signal from Table 3 and would not be detectable.

Nevertheless, it is important to note that the FUV flux from Proxima Centauri is nearly two orders of magnitude higher than that of the Sun (Meadows et al. 2016). Airglow stemming from recombination of photodissociated O$_2$ and CO$_2$ could thus be significantly stronger on Proxima Cen b than on Earth. Barthelemy & Cessateur (2014) stress the importance of stellar UV/FUV emissions on the production of UV and visible aurorae, and note that, e.g., Lyα flux can contribute up to 25% to the production of the O(1D) red-line. However, even if Proxima Cen b had a sustained 100 kR airglow—one hundred times the maximum Earth airglow—its emission would be comparable to the lowest estimate of auroral emission in Table 3, which is still unlikely to be detectable (see Section 3). We therefore ignore this potential contribution in the present work, noting that a detailed photochemical treatment would be required to pin down the expected airglow emission at Proxima Cen b.

In summary, we predict a steady-state auroral emission at 5577 Å from Proxima Cen b that is of the order of 100 times stronger than seen on Earth for a quiet magnetosphere, corresponding to an emitted auroral power for the O I line on the order of ~0.090 (0.049) TW for the sub-(super-)Alfvénic winds using method 2 (Section 2.4). We believe that this method yields more realistic results than the purely kinetic power estimate in method 1 (Section 2.3), due to the inclusion of magnetic interactions in method 2—though the magnitudes are similar to within a factor of two. Assuming Proxima Cen b is an Earth-like terrestrial planet, our maximum transient power estimate for the 5577 Å line for CME conditions that drive a
magnetospheric substorm is $\sim21.42$ TW, or $\sim30,000$ times stronger than on Earth under nominal solar wind conditions. The actual values for Proxima Cen b will naturally change based on planetary parameters (e.g., magnetic dipole moment, magnetospheric particle energy distributions, substorm onset, atmospheric Joule heating) and stellar activity. By our analysis, a $\sim10^3$ (or higher) enhancement compared to Earth as suggested by O’Malley-James & Kaltenegger (2016) is only possible due to one or more of the following: transient magnetospheric conditions driven by either CME or substorm activity, a magnetic dipole significantly stronger than Earth’s, or higher stellar mass-loss than predicted (Wood et al. 2005; Cohen et al. 2014).

3. Auroral Detectability

In this section, we assess the detectability of the 5577 Å OI auroral emission line from the atmosphere of Proxima Cen b. Below, we investigate the line profile shape and then calculate planet–star contrast ratios and integration times required for auroral detection.

3.1. OI Auroral Line Profile

To estimate the signal-to-noise as a function of spectral resolution, we need to estimate the auroral spectral line width. The OI 5577 Å green line has no hyperfine structure and because it is a forbidden line, it has negligible ($\lesssim10^{-15}$ Å) natural width (Hunten et al. 1967). Spectroscopic observations of the O I airglow by Keck/HIRES (Slanger et al. 2001) and by HARPS (Anglada-Escudé et al. 2016, see Section 4) are unresolved, revealing the resolution element width of the instrument used for the observation at the wavelength of the line ($\sim0.1$ Å Keck/HIRES; $\sim0.05$ Å HARPS) rather than the full width at half maximum (FWHM) of the line.

To determine the width of the line, we examine several line broadening mechanisms that play a key role in terrestrial atmospheres. The planet’s rotation will broaden the O I line, but calculations by Barnes et al. (2016) and Ribas et al. (2016) show that Proxima Cen b is likely tidally locked with a rotation period of 11.2 days, resulting in negligible instantaneous rotational broadening (FWHM $=0.002$ Å). Pressure broadening can also be safely neglected since O I auroral emission occurs in terrestrial atmospheres at an elevation of $\sim100$ km where the atmosphere is thin (Slanger et al. 2001). Similarly, broadening due to atmospheric turbulence can also safely be neglected due to the stratospheric origin of the line. Thermal Doppler broadening should therefore be the dominant line broadening mechanism, resulting in a Gaussian line profile. For the 5577 Å OI line, Doppler broadening gives the following scaling relation:

$$\text{FWHM} = 2\Delta \lambda = 0.014 \left( \frac{T}{200 \text{ K}} \right)^{1/2} \text{ Å},$$

where $T$ is the temperature of the emitting layer, for which we adopt the value of 200 K (see Slanger et al. 2001). An FWHM of 0.014 Å is in good agreement with the Fabry–Perot interferometric line width measurements of Wark (1960).

Given the relatively short period of Proxima Cen b and the long exposure times expected for high-resolution spectroscopy, we must also consider the possibility of broadening due to the orbital motion of the planet over the course of an observation. One could take a series of shorter exposures, but this strategy will introduce significant instrumental noise, which is likely to overwhelm any planetary signals. In Figure 2, we plot the orbital broadening of the 5577 Å O I line as a function of the exposure time for observations made at different orbital phases: 90° (quadrature), 100°, 135°, and 180° (full phase). The FWHM given by Equation (8) (0.014 Å) is indicated by a horizontal red line; the intersection of this line with the black curves corresponds to the integration time for which the FWHM doubles. At quadrature, exposures up to $\sim6$ hr long have a negligible effect ($\Delta \lambda \lesssim 10^{-3}$ Å) on the width of the line. At all other phases, the broadening is larger and can cause a significant increase in the FWHM in $\sim1$ hr.

Figure 2. Orbital broadening of the 5577 Å O I line as a function of the exposure time for observations made at different orbital phases: 90° (quadrature), 100°, 135°, and 180° (full phase). The FWHM given by Equation (8) (0.014 Å) is indicated by a horizontal red line; the intersection of this line with the black curves corresponds to the integration time for which the FWHM doubles. At quadrature, exposures up to $\sim6$ hr long have a negligible effect ($\Delta \lambda \lesssim 10^{-3}$ Å) on the width of the line. At all other phases, the broadening is larger and can cause a significant increase in the FWHM in $\sim1$ hr.

3.2. Contrast Ratios and Telescope Integration Times

To unambiguously detect a narrow emission feature, such as the example shown in Figure 3, the telescope resolving power ($R = \lambda / \Delta \lambda$) needs to be taken into account. The typical resolving power being considered for future space-based coronagraph mission concepts is $R \approx 100$, which is

![Figure 2](image-url)
appropriate for the detection of molecular absorption bands in the optical and NIR given the relatively low planet-star contrast ratio (Robinson et al. 2016). However, at 5577 Å an R = 100 spectrograph has a spectral element width of Δλ ≈ 56 Å, over ~10^3 times broader than the O I green line width. Future space-based high-contrast exoplanet imaging missions would need to fly with higher resolution spectrographs to detect the O I 5577 Å line.

Figure 4 shows planet-star contrast ratios in a spectral element centered on the 5577 Å O I auroral line as a function of spectrograph resolving power and auroral power, assuming an FWHM of 0.014 Å (i.e., negligible orbital broadening). The FWHM of the auroral line and equivalent width (W_e) as a function of auroral power are represented as "resolving powers," where R_{FWHM} = λ_{O I}/FWHM and R_W = λ_{O I}/W_e, respectively. In Figure 4, the dashed-white line gives the resolving power such that the spectral element width matches the equivalent width of the line at a given auroral power. The dashed-orange line gives the resolving power such that the spectral element width matches the FWHM of the line. That is, a fixed FWHM = 0.014 Å yields R_{FWHM} = 4 × 10^5. Optimal observations occur when the planet-star contrast (indicated by the contours) is highest. An increase in the contrast of the emission line is only achieved when the width of a spectral element is smaller than the equivalent width of the line. For resolving powers greater than R_{FWHM}, multiple spectral elements are needed to span the emission line, which may introduce additional unwanted read noise and dark current. Therefore, observations should be made in the wedge between the FWHM resolving power and the equivalent width resolving power. Our predicted steady-state auroral emission (~0.1 TW) requires that spectrographs achieve R \gtrsim 10^5.

Using the auroral power estimates from Section 2, we explore the feasibility of detecting the 5577 Å O I auroral emission line with five different ground-based telescope configurations: the 3.6 m High Accuracy Radial velocity Planet Searcher (HARPS), the 8.2 m Very Large Telescope (VLT) with and without a coronagraph, and a Thirty Meter Telescope (TMT) concept with and without a coronagraph (Johns et al. 2012; Udry et al. 2014; Skidmore et al. 2015). We also model the detection using two future space-based coronagraph concepts: the 16 m Large UV/Optical/IR Surveyor (LUVOIR; Kouveliotou et al. 2014; Dalcanton et al. 2015) and the 6.5 m Habitable Exoplanet Imaging Mission (HabEx; Mennesson et al. 2016).

High spectral resolution coronagraphy with the VLT will require an update to the SPHERE high-contrast imager and a coupling with the ESPRESSO spectrograph, as described in Lovis et al. (2016). Note that given the VLT’s 8.2 m diameter, the SPHERE coronagraph must achieve an inner working angle no more than \theta_{IWA} = 2.7\lambda/D to observe at wavelengths as long as 5577 Å given the maximal planet-star angular separation of 37 mas for Proxima Cen b. Our HARPS, TMT, LUVOIR, and HabEx telescope models use R = 115,000, while for VLT we use R = 120,000. All models assume a total telescope and instrument throughput of 5% and a quantum efficiency of 90%. Coronagraph noise estimates use the model presented in Robinson et al. (2016) with updated parameters from Meadows et al. (2016), and consider noise due to speckles, dark counts, read noise, telescope thermal emission, and zodi and exozodi light. Ground-based coronagraphy assumes a conservative design contrast of 10^{-5} (Dou et al. 2010; Guyon et al. 2012), while space-based assumes 10^{-10} (Meadows et al. 2016) unless stated otherwise. Typically, telescope detectors have a maximum exposure time to mitigate the damaging effect of cosmic ray strikes (see Robinson et al. 2016). Therefore, integration times longer than one hour require multiple readouts, introducing more detector noise. Non-coronagraph telescope calculations assume only stellar noise at the photon limit; their values are therefore lower limits, and may increase significantly due to stellar activity (see Section 4). To prevent significant orbital broadening, we
assumed that observations are made for one hour at a time at or close to quadrature; longer exposure times are achieved by stacking multiple observations. For exposure times much longer than an hour, stacking will appreciably increase the read noise and dark current for coronagraph observations, where the star is nulled, but not for the non-coronagraph observations, where the stellar photons dominate the noise budget.

Our integration time calculations follow those described in Robinson et al. (2016). For the stellar spectrum, we adopt the steady-state Proxima Centauri spectrum of Meadows et al. (2016) and neglect the impact of flares on the stellar continuum. We assume that the quoted auroral power emitted via the 5577 Å OI line is constant throughout the entire observation.

For observations without a coronagraph, both the stellar flux and reflected stellar flux define the continuum from which we wish to resolve the auroral emission feature. Observations with a coronagraph need only resolve the auroral emission above the coronagraph noise and reflected stellar continuum. With these considerations in mind, we simulate the net planetary emission as a combination of reflected stellar continuum and auroral emission. We compute the flux from the reflected stellar continuum by assuming that the planet is a Lambertian scatterer at quadrature with a planetary geometric albedo of 0.3 and a planetary radius of 1.07R⊕ following Barnes et al. (2016). We then inject the expected flux from the auroral line at its wavelength. We integrate over all spectral elements that contain the auroral line flux, taking the auroral photon count rate as our signal and all other sources as noise as in Robinson et al. (2016). For the oxygen 5577 Å line width of ~0.014 Å (Section 3.1) and our nominal resolving power, this corresponds to one spectral element.

Table 4 shows the integration times required to achieve a signal-to-noise ratio of six on the 5577 Å OI auroral emission line above the stellar and reflected planetary continuum as a function of auroral power. We simulated contrast ratios and integration times for emitted auroral powers at the O I 5577 Å line ranging from 10−3 to 103 TW to bracket all potential auroral fluxes. The 10−3 TW lower limit corresponds to a strong 5577 Å emission from Earth (Earth total electromagnetic auroral power is of the order of 10−2 TW with 5577 Å typically ~2% of this value). The upper limit of 103 TW is an extreme case that is an order of magnitude stronger than the largest value predicted in Section 2. Values in between correspond to the different cases considered in Table 3, which depend on the planetary dipole moment, magnetospheric substorm activity, and whether CME conditions are present. For reference, the estimated steady-state Proxima Cen b value calculated in Section 2 is ~0.1 TW.

For a SPHERE-ESPESSO coupling (Lovis et al. 2016), the integration times required to detect an O I auroral line are slightly more favorable over a wide range of possible auroral powers, but still prohibitively long under most plausible circumstances. If Proxima Cen b has a Neptune-strength magnetic dipole moment, and observations were made during substorm conditions (when the power in the O I 5577 Å line reaches ~1 TW with a contrast ratio of 7 x 10−4), a coronagraph-equipped VLT would have to integrate for ~400 hr. However, if observations coincided with periods of more vigorous stellar activity such as during a concurrent CME and substorm, the auroral output could reach ~100 TW and contrast ratios of 7 x 10−4. An upgraded SPHERE (denoted by VLT+C in Table 4) may be able to detect this signal in under one hour. Since CMEs and fast stellar wind streams can have timescales of ~10 hr, and substorms up to several days (Gonzalez et al. 1994, 1999), the high level of transient activity may be observable. Under near constant CME activity, storm conditions could potentially last for weeks or longer, improving the chances of detecting auroral emission (Khodachenko et al. 2007).

Even future observations with TMT, HabEx, and LUVOIR outfitted with instruments optimized for high-resolution, high-contrast coronagraphy will be unable to detect a steady-state 0.1 TW O I aurora on Proxima Cen b. However, a coronagraph-equipped TMT could detect a substorm strength aurora

Table 4

| Power (TW) | Contrast | HARPS | VLT | VLT + C | TMT | TMT + C | HabEx | LUVOIR | TMT + C |
|-----------|----------|-------|-----|--------|-----|---------|-------|--------|---------|
| 0.001     | 9 x 10−8 | 2 x 10−5 | 4 x 10−12 | 4 x 108 | 3 x 1011 | 1 x 107 | 6 x 108 | 2 x 107 | 1 x 108 |
| 0.01      | 2 x 10−7 | 2 x 10−11 | 4 x 10−10 | 4 x 108 | 3 x 109 | 1 x 106 | 6 x 108 | 2 x 108 | 2 x 107 |
| 0.1       | 8 x 10−7 | 2 x 10−5 | 4 x 108 | 4 x 104 | 3 x 107 | 1 x 106 | 6 x 108 | 6 x 109 | 40 |
| 1         | 7 x 10−6 | 2 x 10−5 | 4 x 108 | 4 x 102 | 3 x 105 | 10 | 7 x 105 | 30 | 3 |
| 10        | 7 x 10−5 | 2 x 10−5 | 4 x 108 | 4 x 10 | 3 x 103 | 4 x 10−1 | 10 | 1 | 3 x 10−1 |
| 100       | 7 x 10−4 | 2 x 10−5 | 4 x 107 | 4 x 10−1 | 30 | 3 x 10−1 | 6 x 10−1 | 9 x 10−2 | 3 x 10−2 |
| 1000      | 7 x 10−3 | 20 | 4 | 3 x 10−2 | 3 x 10−1 | 3 x 10−3 | 6 x 10−2 | 9 x 10−3 | 3 x 10−3 |

Note: Integration times refer to the time required to achieve a signal-to-noise ratio of six on the auroral emission above the continuum assuming a telescope throughput of 5%, a spectrograph with resolution Δ/λ = 115,000 for HARPS, TMT, HabEx, and LUVOIR and Δ/λ = 120,000 for VLT. “+ C” indicates the use of a coronagraph and associated noise sources discussed in Robinson et al. (2016). Auroral power of the order of 0.1 TW (boldface) corresponds to the predicted steady-state value in Section 2, while ~1–100 TW corresponds to our predicted auroral power arising from a combination of substorm event and CMEs. TMT + C” denotes a coronagraph-equipped TMT concept with a design contrast of C = 10−7 and negligible instrumental noise.
of \sim 10 \text{ TW} in about 10 \text{ hr}, while LUVOIR could make the predicted substorm auroral observation in about 30 \text{ hr}. Only auroral powers \gtrsim 10 \text{ TW} would be detectable with HabEx. Auroral powers of the order of 100 \text{ TW} arising from a concurrent CME and substorm could be observed by the TMT, HabEx, and LUVOIR in well under an hour.

Finally, we consider how improvements in ground-based instrumentation might expand the ability to detect exo-aurorae. In the top panel of Figure 5, we model a coronagraph-equipped TMT concept that achieves a design contrast of $C = 10^{-7}$ and has negligible instrumental noise (e.g., no dark current and read noise). Low-resolution observations with a resolving power smaller than the equivalent width resolving power, $R < \lambda/W_{\lambda}$, yield longer integration times at fixed auroral power as the auroral signal is diluted by additional stellar continuum photons from larger spectral elements, which increases the noise. For high resolutions that exceed the equivalent width resolving power, $R > \lambda/W_{\lambda}$, the auroral signal dominates the planetary continuum as the spectral element more tightly bounds the narrow emission feature, yielding little additional improvement in integration times.

In the bottom panel of Figure 5, we vary coronagraph design contrasts for observations with and without instrumental noise. We find that a TMT with coronagraphic starlight suppression, negligible instrumental noise, a design contrast of $C = 10^{-7}$ and $R > 10^5$ allows for a detection of our predicted steady-state OI auroral emission (auroral power of \sim 0.1 \text{ TW}) over about 40 \text{ hr} (see also Table 4). The discontinuities that occur at high resolving powers are due to the need for additional spectral elements to span the width of the OI auroral line.

Despite the likely increased strength of aurorae on Proxima Cen b compared to Earth, observing a steady-state 0.1 \text{ TW} aurora requires sufficiently long integration times, which is not currently feasible, nor will it be feasible with the next generation of instruments, unless ideal instrumental performance is achieved. OI auroral detection may only be possible if observations coincide with magnetospheric substorms or periods of vigorous stellar activity, such as CMEs, which can induce much stronger aurorae ranging from 1–10 \text{ TW} (and up to \sim 100 \text{ TW} if Proxima Cen b has a stronger magnetic dipole than Earth). These transient events are frequent on Proxima Centauri (Davenport et al. 2016) and may persist on timescales comparable to the integration times needed to detect strong aurorae.

4. Search in the HARPS Data

The ESO Archive\footnote{http://archive.eso.org/} hosts 319 HARPS spectra of Proxima Centauri taken between 2004 and 2016 and totaling about 70 \text{ hr} of exposure time. The spectra were taken in the wavelength range of 3782–6913 \text{ Å} with a resolving power of $R = 115,000$, yielding a wavelength resolution of $\Delta \lambda \approx 0.05 \text{ Å}$ at 5577 \text{ Å}. Each wavelength bin was oversampled by a factor of about five. Given the estimates in Table 4, if Proxima Cen b’s auroral power were on the order of 10 \text{ TW} (however unlikely), the OI line could be detectable in this data set. We therefore downloaded all spectra to conduct a search for the OI emission feature of Proxima Cen b. The method we outline below is similar to so-called “spectral deconvolution” techniques used to detect molecular absorption in exoplanet atmospheres (e.g., Sparks & Ford 2002; Riaud & Schneider 2007; Kawahara et al. 2014; Snellen et al. 2015).

We first shifted all spectra to the stellar rest frame by cross-correlating them against each other and calibrating the wavelength array to the stellar Na D I and II lines. Next, we removed stellar lines by performing weighted principal component analysis (WPCA; Delchambre 2015) on a 250 \text{ Å} window centered at 5577 \text{ Å}. Each spectrum was then fit with a linear combination of the first 10 principal components, a number that we obtained by optimizing the recovery efficiency of injected planetary signals (see below); the fit was then subtracted, reducing the noise in the vicinity of 5577 \text{ Å} by a
factor of $\sim 7$. In order to obtain the principal components, we weighted each spectrum by the square root of its exposure time and assigned weights of zero to the individual telluric 5577 Å airglow features because these are among the strongest features in any individual spectrum and may incorrectly bias the principal components in the stellar frame. We remove Earth airglow separately below.

Next, we Doppler-shifted all spectra into the frame of Proxima Cen b. Since the orbital inclination $i$ is unconstrained, we performed a grid search, varying $i$ in one degree increments from 30° to 90°. We did not consider inclinations lower than 30° due to the difficulty of deconvolving stellar and planetary signals in near-face-on orbits. We further varied the planet period $P$ and planet mean longitude $\lambda$ across a range spanning $\pm 3\sigma$ about the best-fit values reported in Table 1 of Anglada-Escudé et al. (2016), in increments of 0.25$\sigma$; in total, we considered 37,440 different orbital configurations for the planet. For simplicity, the eccentricity was assumed to be zero, the planet mass was set to $1.27 M_\oplus / \sin i$, and the stellar mass was held fixed at 0.12$M_\odot$. The latter parameter is considerably uncertain; however, changing the stellar mass changes the amplitude of the planetary RV signal, making the stellar mass degenerate with the inclination of Proxima Cen b’s orbit. A grid search over the stellar mass is therefore redundant as long as we treat the inclination above as an “effective” inclination for $M_\star = 0.12 M_\odot$.

After Doppler-shifting each spectrum, we translated them back to the original wavelength grid by linear interpolation. Once in the planet frame, we identified and interpolated over $>10\sigma$ outliers in each wavelength bin of the normalized spectra outside the 0.2 Å window centered on the O I line. We found that this successfully removed telluric airglow and prevented outlier features in individual spectra from contributing to the stacked spectrum. We purposefully did not perform this outlier removal step in the vicinity of the O I line; the 5577 Å feature is one of only two with $S/FAP \sim 0.12$ and is in no way a detection of planetary 5577 Å emission. To avoid contamination from O I emission by those sources. For orbits close to edge-on, this reduced the total exposure time from 70 to about 50 hr, and less for lower inclination orbits. In order to remove correlated stellar noise, we then applied a high pass median filter of window size 1 Å.

Finally, we binned the stacked spectra to 0.05 Å-wide bins, with the central bin centered at 5577.345 Å, the empirical wavelength of the O I green line (Cabannes & Dufay 1955; Chamberlain 1961). Our bin size is the HARPS resolution at that wavelength, and closely matches the FWHM of the telluric O I lines in the data set. As we argued in Section 3, a higher resolution spectrograph (with less instrumental broadening) would allow for smaller bin sizes and higher contrast in the O I line. We then measured the amplitude of the 5577.345 Å bin relative to the spectrum mean.

The results of our grid search are shown in the triangle plot in Figure 6. Along the main diagonal, we plot the maximum fractional strength of the 5577 Å signal as a function of each of the orbital parameters (the inclination $i$, the period $P$, and the mean longitude $\lambda$). Below those plots, we show the two-parameter joint distributions of the maximum signal strength, where darker colors correspond to higher values. A peak is visible at an (effective) inclination of 52°, a period of 11.1845 days, and a mean longitude of 126°. In Figure 7, we show the spectra Doppler-shifted into the planet frame according to these orbital parameters. Each of the processed spectra are normalized and distributed vertically along the main subplot according to the planetary phase at the time the observation was made. The location of the expected O I planetary feature is indicated in blue; we show the same window in the frame of Proxima Centauri (red) and Earth (green), where residual telluric emission is clearly visible. As mentioned above, spectra in which Proxima Centauri is one of only two features visible at an inclination $\sim 0.12$ and is entirely consistent with noise.

The stacked flux in the planetary frame is shown below the main plot, where the peak at 5577 Å is visible. Below it, we show the stacked flux binned to 0.05 Å bins; the feature also stands out here. The inset at the bottom left of the main subplot shows a histogram of the S/N of all the bins in a 250 Å window centered on the O I line; the 5577 Å feature (indicated by a dashed red line) is one of only two with $S/N \sim 4$. However, this signal is consistent with correlated stellar noise and is in no way a detection of planetary 5577 Å emission. To show this, we performed the same grid search used to generate Figure 6 in each of 2250 wavelength bins on either side of 5577 Å (where we do not expect significant planetary emission) and computed the strongest recovered signal in each
wavelength bin. The results are shown in Figure 8, where the 5577 Å bin is indicated by a red circle. The dashed red line indicates the fractional strength of the signal in that bin, ~0.006, which roughly corresponds to a planet–star contrast of the same magnitude if the signal were real. However, it is clear from the figure that over 20% of the bins in the range of 5465–5670 Å have a stronger peak signal than that in the 5577 Å bin, from which we estimate a detection significance of ~0.7σ and a false alarm probability (FAP) for our recovered peak of ~0.2. These data are also shown as a histogram in Figure 9, where the number of signals are plotted as a function of their fractional strength. It is evident from these figures that the peak shown in Figure 7 is fully consistent with noise.

A striking feature of Figure 8 is the correlated nature of the noise; for instance, no bins in the range of 5500–5575 Å have particularly strong signals, while the 5577 Å peak is one of many in its immediate vicinity. This is likely a sign of correlated stellar noise that was improperly removed by PCA, either due to high temporal stellar variability or nonlinear correlations across the spectrum that cannot be captured by PCA. At present, this noise is the limiting factor in our ability to recover auroral emission by Proxima Cen b. Future coronographic observations of Proxima Centauri (Section 3) should greatly reduce this noise by nulling most of the starlight.

In order to quantify the constraints our non-detection imposes on the properties of Proxima Cen b, we inject Gaussian O I emission signals with FWHM 0.05 Å and of varying contrast into each of the raw spectra and attempt to recover them via the procedure described above. We find that an O I auroral signal with planet–star contrast 1.8 × 10⁻² yields a detection with S/N ~ 8 (Figure 10). By performing the same wavelength search as before (Figures 8 and 9), we estimate the significance of this detection to be 8σ, which we conservatively choose to be our nominal detection threshold for the HARPS data set. From Table 4, this contrast is equivalent to an O I auroral power of ~3 × 10³ TW, our empirical upper limit on the strength of Proxima Cen b’s 5577 Å emission. Note that by scaling the estimates in that table, it should take only a few hours (versus the 50 hr used in the injection/recovery step) to detect such a signal with HARPS. This order-of-magnitude difference is likely related to the correlated stellar noise discussed above. Integration times for telescopes without coronagraphs may therefore be significantly longer than the estimates quoted in that table.
consistent with the calculations in Section 2.}

expected non-detection in Figure 7 therefore constrains the auroral power on Proxima Cen b to be ~ \(10^{-3}\) TW. Consistent with this, Figure 7 also shows that the auroral power is significantly lower for other exoplanets with similar properties, as evidenced by the lower signal-to-noise ratio (SNR). The non-detection in Figure 7 is consistent with the model calculations in Section 2.

Finally, we also performed similar searches for the red oxygen lines (6300.308 and 6363.790 Å) and the 3914.4 Å UV nitrogen line, which are prominent in Earth’s aurora, but find no significant peaks. Given the lower power in the red lines relative to the green line, and the low transmissivity of Earth’s atmosphere and lower detector efficiencies in the UV, this non-detection is consistent with the non-detection of the 5577 Å feature.

5. Discussion and Conclusions

Our calculations above assume that Proxima Cen b is a terrestrial planet with an Earth-like atmosphere. Although its radius is not known—making an estimate of its density impossible—the planet is statistically likely to be rocky. The a priori probability distribution for the inclination of an exoplanet is \(P(i)di = \sin(i)di\). With 68% confidence, the inclination of Proxima Cen b is greater than 47°, and with 95% confidence it is greater than 18°. Given \(m_p \sin i = 1.27 M_\oplus\), this corresponds to true planet masses smaller than 1.7 \(M_\oplus\) (68% confidence) and 4.1 \(M_\oplus\) (95% confidence). Recent exoplanet population studies suggest that the transition between rocky and gaseous exoplanets occurs at a radius of about ~1.6 \(R_\oplus\) (Rogers 2015; Wolfgang & Lopez 2015). However, a corresponding value for the transition mass is still uncertain, and since the radius of Proxima Cen b has not been measured, we cannot argue for its terrestrial nature based on its mass alone. Nevertheless, we can obtain predictions for its radius under certain assumptions. Assuming it is a rocky planet with Earth-like composition, we may use the scaling law from Fortney et al. (2007) to obtain radii of 1.16 \(R_\oplus\) \((m_p = 1.7 M_\oplus)\) and 1.45 \(R_\oplus\) \((m_p = 4.1 M_\oplus)\). Using the mass–radius grids of Lopez et al. (2012) and assuming instead that Proxima Cen b is a super-Earth-mini-Neptune with a thin H/He envelope with mass equal to 1% the planet mass, the radii jump to 1.7 \(R_\oplus\) \((m_p = 1.7 M_\oplus)\) and 2.1 \(R_\oplus\) \((m_p = 4.1 M_\oplus)\). Planet occurrence rate calculations for cool M dwarfs (Dressing & Charbonneau 2013) suggest that there is a steep drop in the number of short-period planets per star with radii above 1.4 \(R_\oplus\) \((0.19^{+0.07}_{-0.05})\), compared to those with radii below 1.4 \(R_\oplus\), which are more than twice as common \((0.46^{+0.09}_{-0.06})\). This suggests that Proxima Cen b is more likely to be terrestrial than Neptune-like. A thin \((<1\%)\) by mass H/He veneer is still possible, but given the extended pre-main-sequence phase of the host star, past hydrodynamic escape is likely to have blown it off (Luger et al. 2015; Barnes et al. 2016).

Nevertheless, we cannot definitively rule out the possibility that Proxima Cen b has an atmosphere dominated by H/He, in which case we would not expect O I auroral emission. A search for Lyman–Werner H2 emission in the UV would be more appropriate in this case. Although broader than the lines we consider here, this emission is likely stronger, and is unlikely to be confused with stellar emission, given that it is molecular in origin. However, perhaps more importantly, a robust non-detection of this and other H/He features could rule out a large gaseous envelope and confirm the terrestrial nature of the planet. That said, we are currently unable to efficiently probe near-face-on orbits due to the much smaller Doppler shift of the planetary lines. Observations made exclusively at quadrature, when the planet RV is highest, may help with this in the future.

Alternatively, Proxima Cen b could be terrestrial but be significantly larger than the Earth, with mass as high as ~4 \(M_\oplus\) and radius ~1.5 \(R_\oplus\). Since the scaling methods used in Section 2 implicitly assume Proxima Centauri b is similar to Earth in size, the auroral strength could be different than what we estimate. Assuming a global field, a larger planetary radius (and therefore core radius) could increase the magnetospheric cross-section to the stellar wind, leading to an increase in the emitted power. Furthermore, assuming an Earth-like atmospheric composition, the higher surface gravity would decrease the ionospheric scale height, which could lead to larger magnetic field parallel potential drops in auroral acceleration regions. This would increase the upward flowing current and therefore the downward accelerated electron beams into the upper atmosphere, which could also enhance the auroral signal. Moreover, an increased atmospheric density at the depth where precipitating electrons deposit their energy could also change recombination rates and alter the energy level distribution of the O atoms, which would in turn affect the auroral strength in different lines. A quantitative estimate of these effects is beyond the scope of this study, as it would require both modeling the changes to the atmospheric structure and solving the Boltzmann kinetic transport equation.

Assuming Proxima Cen b is terrestrial, our HARPS search constrains its auroral power to be \(<3 \times 10^3\) TW. This is consistent with the calculations in Section 2, which suggest that the O I auroral power on Proxima Cen b is likely ~0.1 TW, or \(\sim 100 \times\) that of the Earth during steady-state solar wind conditions. Those calculations, however, ignore transient increases in stellar magnetic activity, which can enhance the auroral signal and the diffuse airglow emission of the planet. As discussed in Section 2, transient magnetospheric activity could result in auroral power for the 5577 Å line up to 10–100 TW, lasting from 10–10^2 minutes (Section 2.4). In addition, for
a planet that is under near constant CME activity, it is possible
that the storm conditions last for weeks or longer (Gonzalez et al. 1994, 1999). Spectra taken during periods of vigorous
stellar activity could thus enhance the chances of detecting
auroral emission.

Even if Proxima Cen b is terrestrial, an auroral signal is not
guaranteed to be present. The existence of an atmosphere is still
an open question, owing to vigorous past hydrodynamic escape
(Luger & Barnes 2015; Barnes et al. 2016), observed persistent
stellar activity (Davenport et al. 2016), and an observationally
unconstrained planetary magnetic field. If an atmosphere is in
fact present, it may not be Earth-like; instead, it could be
dominated by CO2 (e.g., Meadows et al. 2016). Airglow and
auroral 5577 Å emission are still expected for such an
atmosphere, since atomic oxygen is produced by photodisso-
ciation of CO2; in fact, O I 5577 Å emission has been observed at
both Mars and Venus, both of which are CO2-dominated
(e.g., Slanger et al. 2001; Bertaux et al. 2005). In particular,
Slanger et al. (2001) and Slanger et al. (2006) found that the
Venusian airglow strength is comparable to that of Earth.
Given that Venus receives about twice the solar flux Earth
receives, airglow and/or auroral emission from a CO2-rich
Proxima Cen b could be a factor of ~2 weaker than the values
we predict in this paper, though detailed photochemical
modeling is required to accurately model this scenario.

In the case in which the atmosphere is oxygen-rich, nitrogen
may need to be present to enhance the auroral signal. On Earth,
the O I green line emission results primarily from O2 dissociative recombination, as well as collisions with excited
N2 and direct electron impact (Strickland et al. 2000). It is
unclear whether or not other molecular species could play a
similar role if N2 is not the bulk atmospheric constituent.
However, the detection of the 3914 Å N2 band could be a good
diagnostic in the UV, where the star is even fainter. If we
assume that the power of the 3914 Å nitrogen band is
comparable to that of the O I line (which is typical for higher
energy magnetospheric particle populations), then the planet–
star contrast in the N2 band would be an order of magnitude
greater than at 5577 Å. Since the strength of the N2 band scales
with magnetospheric parameters, stellar activity could cause
strong transient features in the UV, which may be observable.
Note, however, that limitations in UV detector efficiencies may
complicate the detection of nitrogen and other UV aurorae.

Our integration times for the predicted steady-state 5577 Å
O I auroral line render its detection infeasible for current
facilities. However, if key design goals are met for future
coronagraphs, steady-state aurorae may be more easily
detected. As shown in Figure 4, achieving the optimal star–
planet contrast ratio at the emission line requires that the width
of a spectral element (resolving power) is smaller (greater) than
the line’s equivalent width. For our predicted steady-state
auroral emission (~0.1 TW), this requires future spectrographs
to achieve $R \gtrsim 10^3$. High-resolution spectroscopy is also
needed to resolve the Doppler shift of the planetary auroral
emission (~1 Å) and place strong constraints on the eccentricity and mass/inclination of the planet. Such constraints
would lead to greater confidence in the terrestrial nature of
Proxima Cen b. Furthermore, since read noise and dark current dominate the coronagraph instrumental noise budget,
the development of low-noise detectors, e.g., MKIDS (Mazin et al. 2012, 2015), would significantly help the detection
sensitivity and would allow such high-resolution spectroscopy
infrared auroral characterization difficult. Moreover, the earlier type host emits a larger fraction of its light in the optical, resulting in
a poorer auroral contrast ratio.
Finally, exoplanets orbiting nearby brown dwarfs may be prime targets for exoaурoral searches. Early-type brown dwarfs display significant magnetic activity (West et al. 2008) and are significantly fainter than M dwarfs in the optical, potentially enhancing the detectability of the 5577 Å signal from planets in orbit around them. Although no short-period exoplanets are currently known to orbit nearby brown dwarfs (He et al. 2017), the methods described in this paper may be used as a means of exoplanet detection, as suggested by Sparks & Ford (2002). Since the stack-and-search method described in Section 4 does not require previous RV observations of a system, a long baseline of spectroscopic observations of nearby M dwarfs and brown dwarfs could be used to search for Doppler-shifted 5577 Å OI emission. Our method is particularly sensitive to short-period terrestrial planets, whose auroral power (if an atmosphere is present) is large and whose large RV will Doppler shift the signal by one or more Å. However, since the stack-and-search method is best suited to detect steady-state emission, exoaурoral searches will likely have to wait for a future generation of space-based telescopes or noiseless ground-based ELTs capable of detecting sub-TW aurorae. These searches may someday reveal the presence of unknown nearby terrestrial exoplanets, including ones in the habitable zone.

The code used to generate the tables and figures in this paper is open source and available at https://github.com/rodluger/exoaуrora. A static version of the code is archived at https://doi.org/10.5281/zenodo.192459.

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