Interstellar absorptions towards the LMC: Small-scale density variations in Milky Way disc gas

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ABSTRACT

Observations show that the interstellar medium (ISM) contains sub-structure on scales less than 1 pc, detected in the form of spatial and temporal variations in column densities or optical depth. Despite the number of detections, the nature and ubiquity of the small-scale structure in the ISM is not yet fully understood. We use UV absorption data mainly from the Far Ultraviolet Spectroscopic Explorer (FUSE) and partly from the Space Telescope Imaging Spectrograph (STIS) of six Large Magellanic Cloud (LMC) stars (Sk-67°111, LH 54-425, Sk-67°107, Sk-67°106, Sk-67°104, and Sk-67°101) that are all located within 5° of each other, and analyse the physical properties of the Galactic disc gas in front of the LMC on sub-pc scales. We analyse absorption lines of a number of ions within the UV spectral range. Most importantly, interstellar molecular hydrogen, neutral oxygen, and fine-structure levels of neutral carbon have been used in order to study changes in the density and the physical properties of the Galactic disc gas over small angular scales. At an assumed distance of 1 kpc, the 5° separation between Sk-67°111 and Sk-67°101 implies a linear extent of 1.5 pc.

We report on column densities of H2, C I, N I, O I, Al II, Si II, P II, S III, Ar I, and Fe II in our six lines of sight, as well as C I*, C II*, Mg II, Si IV, S II, Mn II, and Ni II for four of them. While most species do not show any significant variation in their column densities, we find an enhancement of almost 2 dex for H2 from Sk-67°111 to Sk-67°101, accompanied by only a small variation in the O I column density. Based on the formation-dissociation equilibrium, we trace these variations to the actual density variations in the molecular gas. On the smallest spatial scale of < 0.08 pc, between Sk-67°107 and LH 54-425, we find a gas density variation of a factor of 1.8. The line of sight towards LH 54-425 does not follow the relatively smooth change seen from Sk-67°101 to Sk-67°111, suggesting that sub-structure might exist on a smaller spatial scale than the linear extent of our sight-lines.

The results show that we sample a mix of both neutral and ionised gas in our six lines of sight. Towards Sk-67°101 to Sk-67°107, we derive the temperature $T_{\text{exc}} \approx 70$ K for the inner self-shielded part of the gas based on the rotational excitation levels of H2, and an average density of $n(H) \approx 60$ cm$^{-3}$, typical of that for CNM. The gas towards LH 54-425 and Sk-67°111 shows different properties, and $T_{\text{exc}} \approx 200$ K. Our observations suggest that the detected H2 in these six lines of sight (with the extent of < 1.5 pc) is not necessarily physically connected, but that we are sampling molecular clouds with pathlengths < 0.1 – 1.8 pc and possibly different densities.

Key words. ISM: structure – ISM: molecules – Ultraviolet: ISM – Techniques: spectroscopic – Galaxy: disc

1 Introduction

Recent studies of the interstellar medium have shown a number of observed variations on scales smaller than 1 pc, indicating the existence of small-scale structure. These have been reported in the form of temporal variations and differences in column densities over small spatial scales.

Interferometric data of neutral hydrogen in 1976 showed variations in H I over small scales (Dieter et al. 1976). Since then a number of studies of small-scale structures in H I have been performed, by 21-cm absorption lines against pulsars with time variability (e.g., Clifton et al. 1988, Frail et al. 1994), sampling the gas on scales of tens to hundreds of AUs, or using interferometric observations with the Very Long Baseline Array (VLBA) (e.g., Faison & Goss 2001) finding optical depth variations on about the same scales.

Optical spectra at high spectral resolution have been taken of stars in globular clusters, providing a grid of very close sightlines (angular scales of only few arcsec) to detect structure in interstellar gas on scales down to 0.01 pc. In these studies column density variations have been found in mainly Ca II and Na I lines, and in differential reddening (e.g., Cohen 1978, Bates et al. 1990, 1991, 1995, Meyer & Lauroesch 1999, Andrews et al. 2001).

Using nearby binaries and multiple star systems with separations < 20 arcsec, the smallest projected scales have been probed (e.g., Meyer 1990, Watson & Meyer 1996, Lauroesch et al. 2000).

When measurements on small-scale structure were repeated, temporal variations have been found in several cases. Examples have been presented in the above cited investigations by, e.g., Lauroesch et al. 2000, and Lauroesch & Meyer 2003. In some other cases, where a proper motion star was the target, the repeated observations have revealed the spatial variations in the gas on scales smaller than the ones provided by multiple stars and binaries, as the lines of sight sample different parts of the same cloud at different times (Welty & Fitzpatrick 2001, Welty 2007).

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Fig. 1. Hα image of six background stars (star symbols) in their LMC environment with their Dec (in degrees) and RA (in hours) coordinates. Note that the luminous gas around the stars is warm ionised gas of the LMC, which is not relevant for our study. (This figure was adopted from Danforth et al. (2002).)

Table 1. Information about the FUSE data as retrieved from the MAST archive.

| Star   | RA\(^a\) (J2000) | Dec\(^a\) (J2000) | Spectral\(^a\) type | V [mag] | date       | programme | exp.time [ks] | aperture |
|--------|------------------|-------------------|---------------------|---------|------------|------------|--------------|----------|
| Sk-67°111 | 05 26 48.00    | -67 29 33.0       | O6 Iafpe            | 12.57   | 2002-03-20 | C155       | 7.98         | LWRS     |
|        |                  |                   |                     |         | 2002-03-20 | C155       | 5.58         | LWRS     |
|        |                  |                   |                     |         | 2002-03-19 | C155       | 7.91         | LWRS     |
|        |                  |                   |                     |         | 2002-03-19 | C155       | 6.83         | LWRS     |
|        |                  |                   |                     |         | 2002-03-20 | C155       | 4.52         | LWRS     |
|        |                  |                   |                     |         | 2002-03-19 | C155       | 4.35         | LWRS     |
| LH 54-425 | 05 26 24.25    | -67 30 17.2       | O3IIIf+O5           | 13.08   | 2008-05-07 | F321       | 9.42         | LWRS     |
|        |                  |                   |                     |         | 2008-05-07 | F321       | 23.20        | LWRS     |
|        |                  |                   |                     |         | 2008-05-07 | F321       | 17.01        | LWRS     |
|        |                  |                   |                     |         | 2008-05-07 | F321       | 19.79        | LWRS     |
|        |                  |                   |                     |         | 2008-05-07 | F321       | 19.79        | LWRS     |
| Sk-67°107 | 05 26 24.00    | -67 30 00.0       | B0                   | 12.50   | 2000-02-09 | A111       | 11.18        | MDRS     |
| Sk-67°106 | 05 26 13.76    | -67 30 15.1       | B0                   | 11.78   | 2000-02-09 | A111       | 11.27        | MDRS     |
| Sk-67°104 | 05 26 04.00    | -67 29 56.5       | O8 I                 | 11.44   | 1999-12-17 | P103       | 5.09         | LWRS     |
| Sk-67°101 | 05 25 56.36    | -67 30 28.7       | O8 II                | 12.63   | 1999-12-20 | P117       | 1.26         | LWRS     |
|        |                  |                   |                     |         | 2000-09-29 | P117       | 6.25         | LWRS     |

\(^{a}\) The coordinates and spectral types of the background LMC stars are from Danforth et al. (2002).
Despite the number of detections, the nature of these small-scale structures and their ubiquity is still a subject of study. It has not always been clear whether they reflect the variation in H\textsc{i} column density, or whether they are caused by changes in the physical conditions of the gas over small scales.

However, some explanations have been suggested for the ISM model consisting of fine scale structures, such as filamentary structures (Heiles 1997), fractal geometries driven by turbulence (Elmegreen 1997), or a separate population of cold self-gravitating clouds (Walker & Wardle 1998; Draine 1998; Wardle & Walker 1999).

In absorption line spectroscopy most cases of temporal or spatial small-scale structures are observed in optical high-resolution spectra which, however, often provide little information on the physical conditions in the gas. Using UV spectra, valuable information can be gained about the physical properties of the gas. From fine structure levels of C\textsc{i}, N\textsc{i} (Netze 2007) discovered that the observed variations in Na and Ca lines towards the LMC sight-lines HD 219188 reflect the variation in the density and ionisation in the gas, and do not refer to high-density clumps. A different approach was used by Richter et al. (2003a, b) who found, using the many absorption lines of molecular hydrogen in the Lyman and Werner bands, that the molecular gas in their studied lines of sight resides in compact filaments, which correspond to the tiny-scale atomic structures in the diffuse ISM (Richter et al. 2003a).

The Large Magellanic Cloud (LMC) has many bright stars with small angular separation on the sky, and provides a good background for studying the gas in the disc and the halo of the Milky Way at small scales. Here we have chosen the six LMC sight-lines (see Table 1) which have in general lower S/N, while the data quality is significantly higher for all the FUSE detectors for the Sk -67\degree 101 sight-lines. Due to the different wavelength zero points in the calibrated data, the spectra of different stars and different cameras might shift within a few Ångström around the listed wavelength.

| Star | LiF:1A | 2A | 1B | 2B | SiC | STIS |
|------|--------|----|----|----|-----|------|
| Sk-67\degree 111 | 97 | 74 | 66 | 71 | 55 | - |
| LH 54-425 | 88 | 68 | 60 | 58 | 44 | - |
| Sk-67\degree 107 | 42 | 41 | 35 | 26 | 17 | 17 |
| Sk-67\degree 106 | 62 | 55 | 48 | 30 | 16 | 17 |
| Sk-67\degree 104 | 57 | 50 | 42 | 35 | 31 | 21 |
| Sk-67\degree 101 | 44 | 52 | 40 | 36 | 20 | 16 |

In the order of right ascension our target stars are: Sk-67\degree 111, LH 54-425, Sk-67\degree 107, Sk-67\degree 106, Sk-67\degree 104, and Sk-67\degree 101 (see Fig. 1). These are all bright stars of spectral types O and B, lying on an almost straight line at constant declination, and spread over 5\degree in RA. Because the stars are separated mainly in their RA, we have considered the projected separations in that coordinate. The smallest separation is however between LH 54-425 and Sk-67\degree 107, which has almost the same RA, which means that we have to take into account the true separation of 1\degree.2 (essentially in the declination), when comparing these two sight-lines.

We retrieved the already reduced data from the MAST archive and co-added them separately for each of the four co-aligned telescopes. For the information about the retrieved data as well as the properties of the stars, see Table 1. The data were all reduced with the CALFUSE v3.2.1, except for the LH 54-425 and Sk-67\degree 106, which were reduced with CALFUSE v3.2.2. The typical S/N of the data varies for different detector channels and sight-lines (see Table 2 for more information on the S/N of the FUSE and the STIS data). The data from the SiC channels have in general lower S/N, while the data quality is significantly higher for all the FUSE detectors for the Sk-67\degree 104 and LH 54-425 sight-lines. Due to the different wavelength zero points in the calibrated data, the spectra of different stars and different cameras might shift within ±20 km s\(^{-1}\). This shift however is steady for the whole spectral range and does not affect the line identification.

The STIS observations were part of a programme for studying the N 51 D superbubble (Wakker et al., in preparation). Only the stars Sk-67\degree 107, Sk-67\degree 106, Sk-67\degree 104, and Sk-67\degree 101 were observed in that programme. STIS provides a better resolution of 6.8 km s\(^{-1}\), and covers the wavelength range longward of the FUSE spectrum from about 1150 to 1730 Å.

### 3. Handling of spectral data

#### 3.1. LMC sight-line

The line of sight towards the LMC is rather complicated, because it contains several gas components. Knowing the absorption lines in the ISM with their transition wavelengths we are able to identify the different elements, and distinguish the different gas components through their radial velocities.

Savage & de Boer (1981): On a line of sight there is gas in the solar vicinity, normally seen around \( v_{\text{rad}} \approx 0 \) km s\(^{-1}\) (all velocities given are LSR velocities). Next is the intermediate velo-

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\(^{a}\) Multi-Mission Archive at Space Telescope: [http://archive.stsci.edu](http://archive.stsci.edu)
ity gas around \( \approx +60 \) km s\(^{-1}\) on essentially all LMC lines of sight; this gas likely is a foreground intermediate velocity cloud (IVC). Most lines of sight also show the presence of a high-velocity cloud (HVC) at \( v_{\text{rad}} \approx +110 \) km s\(^{-1}\). The properties of the IVC and HVC will be discussed in Nasoudi-Shoar et al. (in preparation). Finally, the LMC gas itself shows its presence in the velocity range between +180 and +300 km s\(^{-1}\). In this paper we analyse the Milky Way disc component at the velocity \( v_{\text{rad}} = 16 \pm 0.5 \) km s\(^{-1}\), where the various rotational levels of molecular hydrogen have relatively strong absorption and allow for a detailed study of the properties of the gas. The absolute wavelength calibration of the STIS data is much more reliable, therefore we base our radial velocities on these data. This reveals an additional weak component at \( v_{\text{rad}} = -23 \pm 1.8 \) km s\(^{-1}\), which we describe briefly, while we concentrate on the analysis of the strong disc component. We refer to the absorptions with similar radial velocity as parts of the same cloud.

**Fig. 2.** O\textsc{i} absorption at 936.63 (from FUSE:SiC), 1039.23 (from FUSE:LiF), and 1302.17 Å (from STIS) and the continuum fit is shown for all six stars (names given at right). The solid line is the continuum fit to which the spectrum has been normalised, the dashed lines show the upper and lower continuum choice. The bars at the top mark the known absorption component velocities for the O\textsc{i} lines (see Sect. 3.1).
3.2. Column-density measurements

The continua of the spectra consist of the spectral structures from the background stars with broad lines and P-Cygni profiles. Before measuring the equivalent widths we estimated a continuum level by eye, and normalized the spectra to unity with the programme SPECTRALYZOR (Marggraf 2004). In this way we eliminated the large scale variation of the continuum as well as the possible variations on scales less than 1Å. The absorption lines from those parts of the spectra where the continuum placement is highly uncertain were considered with special caution or were excluded from the final analysis.

For each velocity component the equivalent width of the absorption was measured either by integrating the pixel to pixel area up to the continuum level, or by Gaussian fits with MIDAS ALICE (only for unsaturated lines). Owing to the large number of spectral lines within the FUSE wavelength range and the wide velocity absorption range for each transition, there is considerable blending in the interstellar lines. For the absorption lines that needed deblending, a multi-Gaussian fit was used, except for the clearly saturated lines, where the former method was more suitable. For the final results we only took those lines into consideration where we found no blending or which could easily be decomposed by a multi-Gaussian fit. For the O I line at 1302Å however, which is heavily saturated and also blended with its also saturated component at $-23\text{ km s}^{-1}$, we used a different approach. We used profile fitting in addition to the curve-of-growth (CoG) technique, with the derived column density and $b$-value from the other O I lines (based on the CoG method) given as the initial guess, to separate the equivalent widths of the two components.

The dominant source of error in equivalent-width measurements is the placement of the continuum. We therefore estimated the errors based on the photon noise and the global shape of the continuum. The errors due to the continuum fit were measured by manually adopting a highest/lowest continuum within a stretch of few Ångström around each absorption line. The minimum errors in this way depend on the local S/N and correspond to the change of the continuum around $\pm 1\sigma$ noise level. Due to the complex shape of the stellar continuum, this way of choosing the continuum by eye is more reliable than an automatic continuum fitting. Examples are shown in Fig. 3 for some of the O I lines.

We selected primarily absorption lines of H$_2$ to study the fine structure of the gas. This allows us to derive the physical properties of the gas. Furthermore, H$_2$ exists in the coolest portions of the interstellar clouds and thus will produce the narrowest absorption lines. Moreover, in the FUV range many absorption lines from the same lower electronic level are available, thus allowing the easy determination of the respective CoG (see, e.g., de Boer et al. (1993), Richter et al. (1998), Richter (2000)). We also included available metal lines in the study, which are the lines of C I, N I, O I, Al II, Si II, P II, S III, Ar I, and Fe II. For the four sight-lines with available STIS observations, the lines of C I$^+$, C I$^+$, Mg II, Si IV, S II, Mn II, and Ni II were additionally detected.

A standard CoG method was used to estimate the column density $N$ and the Doppler parameter $b$ for each species. The theoretical CoGs were constructed for a range of $b$-values in the interval of $1\text{ km s}^{-1}$, based on the damping constant of the strongest measured transition in each species. The column densities were determined by finding the best representative CoG for the set of measured equivalent widths and their known log($f\lambda$). The $f$-values used are taken from the list of Abgrall et al. (1993a,b) for H$_2$, and Morton (2003) for other species. The final column densities were derived through a polynomial regression and are presented in Table 3 together with the $1\sigma$ errors. Thus the uncertainties in the column densities are based on the statistical errors in equivalent-width measurements and the uncertainties in the $b$-values.

4. Molecular hydrogen in Galactic disc gas

We determined the column densities of the molecular hydrogen for the different rotational states $J = 0 - 4$. These are given in logarithmic values in Table 4 together with the corresponding $b$-values. The $b$-values for various rotational states of molecular hydrogen are estimated separately in each CoG analysis and vary over the range of $2-6\text{ km s}^{-1}$ for the low $J$ for all sightlines. Thus, the various $J$-levels might differ slightly in their $b$-values, because they may sample different physical regions of the Galactic disc gas.

In our FUSE spectra we did not detect any level higher than $J = 4$ for any of our sight-lines. Moreover the $J = 4$ detection was not always certain. We therefore estimated a $1\sigma$ equivalent density from the corresponding CoG coefficient.
width \( EW_{1,1} \) based on the local noise fluctuation and the FUSE spectral resolution: \( EW_{1,1} = 1.06 \times FWHM_{\text{inst}} \times \sigma_{\text{noise}} \). For sight-lines with no measured absorption above the linear part of the C\(^\text{I}\) (Lockman et al. 1986), we have marked in that figure the projected separations between our sight-lines. The \( H_2 \) absorption shows a clear decline in column density towards Sk-67\(^\circ\)111, with a significant drop towards LH 54-425.

4.1. Note on the errors

There are different sources of errors contributing to our measured column densities. We included the statistical errors due mainly to the continuum placement and the local S/N in the equivalent-width measurements. However, the different detectors seem to have different responses, sometimes causing slightly lower or higher equivalent widths of the same absorption with a significant drop towards LH 54-425.

4.2. Physical properties of the gas from \( H_2 \)

The various rotational levels of molecular hydrogen reveal the physical state of the gas. While lower J-levels are mostly populated by collisional excitations, higher J-levels are excited by photons through UV-pumping (Spitzer & Zweibel 1974). The population of the lowest levels can be fitted to a Boltzmann distribution for the gas, the population of higher levels can be fitted in a similar way leading to an "equivalent UV-pumping temperature" \( T_{\text{UV-pumping}} \).

In Fig. 5 we plotted the column density of \( H_2 \) in level J, divided by the statistical weight, \( g_J \), against the rotational excitation energy, \( E_J \). For most of our sight-lines the rotational excitation can be represented by a two-component fit. A Boltzmann distribution can be fitted to the three lower levels \( J = 0, J = 1, \) and \( J = 2 \) to find the excitation temperature \( T_{0,2} \) of the gas. We get the equivalent UV-pumping temperature \( T_{3,4} \) through a fit to the \( J = 3 \) and \( J = 4 \) levels. The Boltzmann excitation temperature ranges from 65 K towards Sk-67\(^{0}\)101 and Sk-67\(^{0}\)104, to about 80 K in the directions of Sk-67\(^{0}\)106 and Sk-67\(^{0}\)107. This is in the typical temperatures range found for the cold neutral medium, CNM.

Towards LH 54-425 and Sk-67\(^{0}\)111, on the other hand, a fit to the \( J = 0 - 3 \) levels would give a \( T_{0,3} \) similar to \( T_{0,1} \) and \( T_{0,2} \), indicating that the \( J = 2 \) level is already excited by UV-pumping. Given that the derived column densities for \( J = 4 \) are upper limits, the gas in these two lines of sight may be fully thermalised, and a single Boltzmann fit through all points might be sufficient. In this case we have derived the excitation temperature \( T_{0,3} \sim 200 \) K.

Furthermore, the temperature plot confirms the estimated column densities, as the indicated errors by the COG-fit would lead to unrealistic ratios of the column densities and the statistical weight between the different J-levels. This steep drop of \( N(J) \) from \( J = 0 \) to \( J = 2 \) is also generally seen in the ISM for sight-lines with \( \log N(J = 0) > 17 \) (Spitzer & Cochran 1973).

Molecular hydrogen in the interstellar medium forms in cores of clouds where the gas is self-shielded from the ultraviolet radiation. The two-component fit to four of our sight-lines with low \( T_{\text{exc}} \) can be interpreted as a core-envelope structure of the partly molecular clouds, where the inner parts are self-shielded from the UV radiation. Detecting less H\(_2\) towards Sk-67\(^{0}\)111 and LH 54-425, together with the higher \( T_{\text{exc}} \) in these two directions, can be understood as looking towards the edge of the \( H_2 \) patch in those sight-lines, where the \( H_2 \) self-shielding is less efficient. However, Sk-67\(^{0}\)107, with a true separation of only 17.2\(^{\circ}\) from LH 54-425, shows a significantly higher column density of \( H_2 \) and a much lower temperature. Assuming that the disc gas exists at a distance between 100 pc to 1 kpc, the projected linear separation between LH 54-425 and Sk-67\(^{0}\)107 corresponds to a spatial scale of 0.01 to 0.08 pc (essentially only in declination). This suggests that the observed \( H_2 \) patch has a dense core and a steep transition to the edge.

5. Metal absorption and abundances

We determined the column densities for the species C\(^{1}\), N\(^{1}\), O\(^{1}\), Al\(^{1}\), Si\(^{1}\), P\(^{1}\), S\(^{1}\), Ar\(^{1}\), and Fe\(^{2}\) from the FUSE spectra. In addition, the column densities of C\(^{1}\), C\(^{1}\), Mg\(^{1}\), Si\(^{1}\), Si\(^{1}\), Mn\(^{1}\), and Ni\(^{1}\) were obtained for Sk-67\(^{0}\)101, Sk-67\(^{0}\)104, Sk-67\(^{0}\)106, and Sk-67\(^{0}\)107 using STIS data. These metal column densities are presented in Table 4. For a list of absorption lines used for the column density determination, see Table 4. Some of the species in the FUSE spectral range have additional transitions in STIS spectra, which made a more accurate determination of their column densities possible. This, together with the location of the data points on the COG, results in uncertainties in the column densities that are smaller along some sight-lines compared to others.

The better resolution of the STIS data allows us to separate the velocity component at \( \sim -20 \) km s\(^{-1}\) that otherwise appears as an unresolved substructure in, e.g., P\(^{1}\) and Ni\(^{1}\) absorption in the FUSE spectra. This component is strongest in the metal lines of O\(^{1}\), Mg\(^{1}\), and Si\(^{1}\). We do not consider this component any further, as it may be part of an infalling cloud, which is not connected to the disc gas for which we study the small-scale structure in this paper. Only for strong saturated lines does this component affect our measurements, as we mentioned in Sect. 4.

Within our spectral range Fe\(^{2}\) appears in a number of transitions with a wide range in \( f \)-values, making an accurate fit to the COG possible. Some of the other species, on the other

\(^{c}\) The fit has been including all possible \( b > 2 \) km s\(^{-1}\).
Fig. 4. Sample of H$_2$ absorption lines from different excited levels shown for the different sight-lines. The sight-lines are labelled on the right, from top to bottom: Sk-67°111, LH 54-425, Sk-67°107, Sk-67°106, Sk-67°104, and Sk-67°101. The spectra are normalised to unity in all cases. The corresponding transitions are labelled on the upper plots of Sk-67°111, the same portion of the spectrum is plotted in each panel for the other sight-lines. 1 Å corresponds to 270 km s$^{-1}$.

hand, have only few transitions in our spectra within a small log$f_{\lambda}$ range, and therefore can be fit to a wide range of $b$-values. Owing to the lack of more information about the Doppler widths of these species, we adopted the $b$-value of Fe II for each line of sight, and we determined the column densities of other ions from the Fe II-CoG. There are some exceptions discussed below for O I, N I, and Ar I (and C I, discussed in the next section).

For O I we find a number of transitions within the FUSE spectral range, and two additional lines within the STIS spectral range (see Table 4). The derived Doppler parameters of O I are very similar to those of Fe II. This can be expected because turbulent broadening dominates thermal broadening in the LISM. We have derived them separately however. With both saturated and very weak O I lines, we are able to make a relatively accurate fit to the CoG (see Fig. 5) and do not need to rely on the accuracy of the Fe II-CoG. Adopting the Fe II-CoG would furthermore lead to unsatisfying fits in most cases. We plotted in Fig. 5 the measured O I column densities together with those...
of $\text{H}_2$. The $N(\text{O} \, \text{I})$ stays constant within the errors between the lines of sight, except for the decrease towards LH 54-425.

$\text{N} \, \text{I}$ is also detected in a number of transitions. These lines also yield $b = 7 \, \text{km s}^{-1}$, even though they are mainly on the flat part of the COG, which makes the determination of the COG less certain. $\text{N} \, \text{I}$ probably originates from the same physical region of the neutral gas as $\text{O} \, \text{I}$. We therefore adopted the $\text{O} \, \text{I}$-COG to determine the column densities of $\text{N} \, \text{I}$. Assuming that also $\text{Ar} \, \text{I}$ mainly exists with the $\text{O} \, \text{I}$ in the neutral gas, we fitted the two detected $\text{Ar} \, \text{I}$ absorptions to the $\text{O} \, \text{I}$-COG as well.

$\text{Si} \, \text{II}$ has only one moderately strong line in the FUSE spectra (see Table 4) and some very strong absorptions in STIS. The absorption at 1020.7 Å is kind of an outlier though when adopting the $\text{Fe} \, \text{II}$-COG, because it appears too low on the COG. Hence the reduction of the $N(\text{Si} \, \text{II})$ towards $\text{Sk-67}^\circ \, 111$ and LH 54-425, compared to the rest of the sight-lines, is mainly due to the lack of further available data, rather than reflecting the differences in the equivalent width of the 1020.7 line. We therefore represent the $N(\text{Si} \, \text{II})$ towards $\text{Sk-67}^\circ \, 111$ and LH 54-425 as lower limits in Table 4. It is possible that this problem occurs because of the sampling of different gas components. This would appear more strongly in the stronger absorptions compared to the weaker ones, which would explain why the 1020.7 line appears too low on the COG, compared to the much stronger lines of the STIS spectra.

The metal column densities show mostly insignificant variations between our lines of sight, but are generally the lowest to LH 54-425. Below we investigate the variations in form of abundance ratios. Due to the lack of information about $\text{H} \, \text{I}$ column densities with a spatial resolution that corresponds to our particular sight-lines, we derive the abundances as the ratio $[X/O] = \log(X/O) - \log(X/O)_0$, with the solar abundances taken from Asplund et al. (2005), and the assumption that the detected $X^+$ is the dominant ion of the element $X$. $\text{O} \, \text{I}$ is an ideal tracer for $\text{H} \, \text{I}$ since, unlike iron and silicon, only small fractions are depleted into dust grains, it has the same ionisation potential as hydrogen, and both atoms are coupled by a strong charge-exchange reaction in the neutral ISM. Some of the derived metal abundances are plotted in Fig. 7 against the angular separation of the sight-lines.

$\text{N} \, \text{I}$, with an ionisation potential of 14.1 eV, acts as another tracer for the neutral gas. Our derived [N I]/[O I] abundances are in general close to solar, except towards $\text{Sk-67}^\circ \, 106$ and $\text{Sk-67}^\circ \, 104$, where they are somewhat lower. The ionisation balance of $\text{N} \, \text{I}$ is more sensitive to local conditions of the ISM, as $\text{N} \, \text{I}$ is not as strongly coupled to $\text{H} \, \text{I}$ as $\text{O} \, \text{I}$ (Jenkins et al. 2000; Moos et al. 2002). We therefore can expect the [N I]/[H I] to vary within a spatial scale, while [O I]/[H I] remains constant. Thus, the variation of [N I]/[O I] could suggest a lower shielding towards the sight-lines with observed lower [N I]/[O I]. Jenkins et al. (2000) have modelled the deficiency of local $\text{N} \, \text{I}$ with decreased $\text{H} \, \text{I}$ column density. It is thus possible that the variation of [N I]/[O I] between our sight-lines are caused by the actual variations in the density. The $\text{N} \, \text{I}$ absorptions are, however, not easily measured due to the multiplicity of the transition, which can lead to high uncertainties in the $\text{N} \, \text{I}$ column densities.

$\text{Fe}$, Mn, and Ni are generally depleted into dust grains in the Galactic disc, which can explain their low relative abundances (Fig. 7). The underabundance of Ar can, however, be explained by the large photo-ionisation cross section of Ar I (Sofia & Jenkins 1998). The slightly higher [Ar/O] towards LH 54-425 and $\text{Sk-67}^\circ \, 111$ would then suggest a higher shielding in these sight-lines, compared to the others, given that the derived column densities are precise. [Si II]/[O I], on the other hand, is close to solar in the lines of sight $\text{Sk-67}^\circ \, 107$ to $\text{Sk-67}^\circ \, 101$ (with available weak and strong absorption lines). As $\text{Si} \, \text{II}$ is the dominant ion in both warm neutral medium (WNM), and warm ionised medium (WIM), these ratios might indicate that part of the $\text{Si} \, \text{II}$ absorption originates from the ionised gas. If silicon is partly depleted into dust grains, these ratios could be even higher. Furthermore, the detection of $\text{Si} \, \text{III}$ (not included in Table 4 due to heavy saturation), and $\text{Si} \, \text{IV}$ strongly suggests the presence of gas that is partially or predominantly ionised.
Fig. 6. Sample of COGs of O I for the six sight-lines (the star name on top of each figure). Each plot shows COGs for $b = 1, 3, 6, 7, 8 \text{ km s}^{-1}$. The solid line is the resulting COG from the best fit ($b = 7 \text{ km s}^{-1}$), and the dotted lines ($b = 6$ and $b = 8 \text{ km s}^{-1}$) correspond to approximately $1 \sigma$ errors.

While the metal absorption shows no change in the ionisation structure in the gas on the lines of sight Sk -67°107 to Sk -67°101, the lines of sight to Sk -67°111 and LH 54-425 distinguish themselves from the other sight-lines. Every line of sight samples a mix of CNM, WNM, and WIM, of which the fraction of ionised gas appears to be higher in the lines of sight Sk -67°107 to Sk -67°101.

It would have been favourable if the HI column densities would have been known from 21 cm data. Such high spatial resolution data do not exist. The Galactic All Sky Survey, GASS (McClure-Griffiths et al. 2009), has a resolution of only 16′, which does not help for our investigation. ATCA interferometric 21 cm data on the other hand are only available for velocities $v > 30 \text{ km s}^{-1}$. Yet, the GASS 21 cm profiles show over 30′ a slight trend. The high velocity resolution of the GASS 21 cm data reveals a two-component profile at velocities of $+4$ and $-4 \text{ km s}^{-1}$. The intensity of the two components increases/decreases to opposite east/west directions overall in favour of a stronger HI emission to lower RA. These velocity components are not resolved in our FUSE, or STIS spectra. Considering the changes in the N(O I), however, it is likely that our pencil beam spectra could be going through the cloud boundary, where the column density summed over the two components is less to e.g., LH 54-425, compared to the other sight-lines.
| Species | Sk-67/111 (FUSE) | LH54-425 (FUSE) | Sk-67/107 (FUSE+STIS) | Sk-67/106 (FUSE+STIS) | Sk-67/104 (FUSE+STIS) | Sk-67/101 (FUSE+STIS) |
|---------|-----------------|----------------|----------------------|----------------------|----------------------|----------------------|
|         | b               | log N          | b                   | log N                | b                   | log N                |
| H₂       | 4±1             | 15.3±1.6       | 2±1                 | 15.4±1.1            | 3±1                 | 17.3±0.1c           |
| J = 0    |                 |                 | 3±1                 | 17.3±0.1c           | 3±1                 | 17.8±0.1           |
| J = 1    | 6±1             | 15.6±1.8       | 4±1                 | 15.6±1.3            | 3±1                 | 17.5±0.1           |
| J = 2    | 4±1             | 15.0±1.9       | 4±1                 | 15.0±1.3            | 4±1                 | 15.5±0.3           |
| J = 3    | 8±2             | 14.5±0.1       | 6±3                 | 14.3±0.1            | 5±3                 | 14.5±0.1           |
| J = 4    | > 2             | < 13.6         | > 2                 | < 13.9               | 5±3                 | 14.1±0.1           |
| Total    | 15.9±1.7        | 15.8±1.2       | 17.6±0.3            | 18.0±0.6            | 18.1±0.2            | 18.1±0.6           |
| C II     | 3±1             | 14.0±0.1       | 3±1                 | 13.8±0.1            | 3±1                 | 13.9±0.3           |
| FS       |                 |                 | 3±1                 | 13.9±0.3           | 3±1                 | 14.0±0.1           |
| C IV     | < 13.8          | < 13.8         | < 13.8              | < 13.8              | < 13.8              | < 13.8              |
| C IV FS  | < 13.8          | < 12.9         | < 12.8              | < 12.9              | < 12.8              | < 12.8              |
| O I      | 7±1             | 17.3±0.4       | 7±1                 | 16.9±0.2            | 7±1                 | 17.6±0.1           |
| FS       |                 |                 | 7±1                 | 17.6±0.1           | 7±1                 | 17.7±0.5           |
| N II     | 16.4±0.1        | 16.2±0.4       | 16.8±0.3            | 16.4±0.3            | 16.8±0.5            | 16.8±0.5           |
| Ar I     | 14.8±0.1        | 14.3±0.1       | 14.8±0.3            | 14.8±0.3            | 14.8±0.3            | 14.8±0.3           |
| Fe II    | 8±1             | 14.8±0.1       | 7±1                 | 14.6±0.1            | 8±1                 | 14.8±0.1           |
| FS       |                 |                 | 8±1                 | 14.8±0.1           | 9±1                 | 14.8±0.1           |
| Mg II    | 15.7±0.1        | 15.7±0.1       | 15.7±0.1            | 15.8±0.1            | 15.8±0.1            | 15.8±0.1           |
| Al II    | < 14.5          | < 14.8         | < 14.8              | < 14.8              | < 14.8              | < 14.8              |
| Si II FS | > 15.1b         | > 14.9b        | > 15.1b             | > 14.9b             | > 15.1b             | > 15.1b             |
| Si IV    | 16.5±0.3c       | 16.5±0.3c      | 16.5±0.3c           | 16.3±0.9            | 16.3±0.9            | 16.4±0.7           |
| P II     | 13.0±0.1        | 13.0±0.1       | 13.0±0.1            | 13.1±0.1            | 13.1±0.1            | 13.3±0.1           |
| S II     | 13.8±0.2        | 13.8±0.2       | 13.8±0.2            | 13.6±0.2            | 13.6±0.2            | 13.7±0.3           |
| Si III FS| 14.4±0.2b       | 14.4±0.2b      | 14.4±0.2b           | 14.5±0.2b           | 14.5±0.2b           | 14.5±0.2b           |
| Mn II    | 13.0±0.1b       | 13.0±0.1b      | 13.0±0.1b           | 13.0±0.1b           | 13.0±0.1b           | 13.1±0.1b           |
| Ni II    | 13.5±0.1        | 13.5±0.1       | 13.5±0.1            | 13.5±0.1            | 13.5±0.1            | 13.7±0.1           |

Most of the metal column densities are based on the adopted b from Fe II in each line of sight. N I and Ar I are derived from the CoG of O I, and the fine-structure levels of carbon from the CoG of C I.

Based on one absorption line

The best fit includes outliers (less than 32% of the data points). For the H₂ data, these outliers are all the absorptions from FUSE:SiC (see Sect. 4.1). For the Si II data, the outlier is the weak line at 1020.7 Å (see Sect. 5).

Based on FUSE data only

Based on both FUSE and STIS for Sk-67°107 to Sk-67°101
The abundances are expressed as the ratio $[X/\text{O}] = \log(X/\text{O}) - \log(X/\text{O})_{\odot}$, assuming that the $X^+$ is the dominant ion of $X$. $X^+$ is given on the right side of the figure.

### 6. Gas densities

The available data allow us to derive the gas density in two ways. One possibility is based on the $H_2$/O abundance and models for the self-shielding of the gas. The other uses the level of collisional excitation of $C$ as derived from the absorption lines. In the latter case the result is not only limited by the accuracy of column densities of the fine-structure levels of neutral carbon, but also by the derived $T_{\text{exc}}$ from $H_2$.

#### 6.1. Density variations derived from $H_2$

The observed column density variations along our sight-lines observed for the various ions and $H_2$ suggest a change in the physical conditions in the foreground gas at relatively small spatial scales. For the metal ions, the observed column densities depend on three physical parameters: the volume density of the respective element in the gas, the fractional abundance of the observed ionisation state of that element (reflecting the ionisation conditions in the gas), and the thickness of the absorbing gas layer. These three quantities may vary between adjacent sight-lines, so that the ion column densities and their variations alone tells us very little about the actual (total) particle-density variations $\Delta n_{\text{H}}$ in the gas. Yet it is these density variations that we wish to know in order to study the density structure of the ISM at small scales.

As we show below, it is possible to reconstruct the particle density distribution in the gas by combining our ion column-density measurements with the $H_2$ measurements in our data sample, and assuming that the molecular abundance is governed by an $H_2$ formation-dissociation equilibrium (FDE). In FDE, the neutral to molecular hydrogen column density ratio is given by

$$\frac{N(H_1)}{N(H_2)} = \frac{(k)}{\beta} R \xi,$$

where $(k) \approx 0.11$ is the probability that the molecule is dissociated after photo absorption, $\beta$ is the photo-absorption rate per second within the cloud, and $R$ is the $H_2$ formation coefficient on dust grains in units cm$^3$ s$^{-1}$.

Unfortunately, the local $H_1$ column density cannot be obtained directly from our absorption measurements because the damped $H_1$ Ly $\beta$ absorption in our FUSE data represents a blended composite of all absorption components in the Milky Way and LMC along the line of sight. However, as mentioned in the previous section, neutral oxygen has the same ionisation potential as neutral hydrogen, and both atoms are coupled by a strong charge-exchange reaction in the neutral ISM, so that $O_1$ serves as an ideal tracer for $H_1$. If we now solve the previous equation for $n_{\text{H}}$ and assume that $N(H_1) = z_o N(\text{O})$ with $z_o$ as the local hydrogen-to-oxygen ratio, we obtain

$$n_{\text{H}} = \frac{N(H_2)}{N(\text{O})} \frac{(k)}{\beta} R,$$

For interstellar clouds that are optically thick in $H_2$ (i.e., $\log N(H_2) > 14$) $H_2$ line self-shielding has to be taken into account. The self-shielding reduces the photo absorption rate in the cloud interior and depends on the total $H_2$ column density in the cloud. Draine & Bertoldi (1996) find that the $H_2$ self-shielding can be characterised by the relation $\beta = S \beta_0$, where $S = (N_H/10^{14} \text{ cm}^{-2})^{-0.75} < 1$ is the self-shielding factor and $\beta_0$ is the photo absorption rate at the edge of the cloud (which is directly related to the intensity of the ambient UV radiation field).

Because all our sight-lines are passing with small separation through the same local interstellar gas cloud, the respective parameters $\beta_0$, $R$, and $z_o$ should be identical along these sight-lines. The observed quantities $N(H_1)$ and $N(O_1)$ instead vary from sight-line to sight-line due to the local density variations $\Delta n_{\text{H}}$ and different self-shielding factors in the gas. If we now consider Eq. (2) and assume $\beta = S(N(H_2)) \beta_0$, for two adjacent lines of sight (LOS1 and LOS2) through the same cloud, we obtain for the local density ratio $\xi$ between LOS1 and LOS2

$$\xi = n_{\text{H,LOS1}} / n_{\text{H,LOS2}} = \frac{N(O_1)_{\text{LOS2}}}{N(O_1)_{\text{LOS1}}} \left( \frac{N(H_2)_{\text{LOS1}}}{N(H_2)_{\text{LOS2}}} \right)^{0.25},$$

A small rise in $n_{\text{H}}$ only slightly increases the $H_2$ grain formation rate $n_{\text{H}}$, but it substantially reduces the photo dissociation rate $(k)\beta_0 S$ due to the increased $H_2$ self-shielding, so that in the end $\Delta N(H_2) \propto \Delta n_{\text{H}}^{1/4}$ while $\Delta N(O_1) \propto n_{\text{H}}$. Therefore, the $H_2/O_1$ column density ratio represents a very sensitive tracer for density variations in the gas.

We now use Eq. (3) to study the density variations in the local gas towards our six lines of sight. In Fig. 8 we plot the relative density to Sk-67°111 together with the derived $T_{\text{exc}}$ versus the separations in RA coordinates. While the excitation temperature suggests a cold core in the sight-lines Sk-67°101, Sk-67°104, Sk-67°106, and Sk-67°107, the total mean density appears to be lower by a factor of almost 2 compared to LH 54-425.

While the column density variations of different excitational levels of $H_2$ suggest that we are observing a high density core of the $H_2$ between the sight-lines Sk-67°101 to Sk-67°106, the result from the relative abundances together with the derived total density variation point to a higher mean density to LH 54-425.

This might be due to a smaller total absorber pathlength in the direction of LH 54-425, which can include a slightly more confined region, for which the mean density averaged over the pathlength is higher compared to the other sight-lines, or due to
the higher fraction of neutral gas towards LH 54-425, on which we base $\xi$.

If we analyse the density $n_{\text{HI}}$ directly from Eq. (3) by using the typical values observed for $R = 3 \times 10^{-19}$ cm$^3$ s$^{-1}$ and $\beta_0 = 5 \times 10^{-10}$ s$^{-1}$ (Spitzer 1978), and the total neutral hydrogen column density $N$(H$^1$) derived from $N$(O$^1$) assuming solar oxygen abundance, we obtain $n_{\text{HI}} \approx 2$ cm$^{-3}$ on average. This represents the lower limit required for the H$^2$ to exist in the FDE. The observed $N$(O$^1$) represents the indirect measure of the total $N$(H$^1$) along a line of sight. It is likely that only a fraction of this H$^1$ is available for the H$^2$ formation, and that the H$^2$ self-shielding is less efficient than assumed because of a complex geometry of the H$^2$ structures.

6.2. Density from C$^1$ excitation

The ground electronic state of C$^1$ is split into three fine-structure levels. The two upper levels C$^1*$ and C$^1**$ are populated through collisional excitation and some UV-pumping (de Boer & Morton 1974). We can therefore use the fine-structure levels of neutral carbon together with the excitation temperature derived from H$^2$, to derive the density $n_{\text{HI}}$ of the gas.

Using the population of the fine-structure levels as a function of $n_{\text{HI}}$ and $T$, calculated by de Boer & Morton (1974), we find the densities in the range of $\sim 40 - 60$ cm$^{-3}$ on the lines of sight Sk$^{}$-67$^1$101 to Sk$^{}$-67$^5$106, and a higher density of $\sim 80$ cm$^{-3}$ towards Sk$^{}$-67$^4$107 (see Table5). The densities derived in this way are dependent on the accuracy in the temperature, as well as the C$^1$ column densities. For LH 54-425 and Sk$^{}$-67$^5$101 we are only able to derive an upper limit for C$^1*$, and hence upper limits of $< 126$ and $< 65$ cm$^{-3}$, respectively for $n_{\text{HI}}$ in these sight-lines. Note that these upper limits are not comparable. While the upper limit of C$^1*$ towards LH 54-425 was based on an absorption with $f$-value similar to the ones used towards Sk$^{}$-67$^5$107 to Sk$^{}$-67$^5$101, the C$^1*$ upper limit for the Sk$^{}$-67$^5$111 sight-line was based on a weaker line, since the same spectral region was occupied by an absorption of a different velocity component.

The column densities of C$^1$ also allow us to calculate the ionisation balance, assuming that the abundance ratio of C to O is solar. One thus has

$$\frac{N(C^1)}{N(C)} = \frac{\Gamma}{\alpha(T) n_e},$$

and with $N(C) = (C/O)_{\odot} \cdot N(O)$ one obtains

$$\frac{N(C^1)}{N(O)} = \frac{(C/O)_{\odot} \alpha(T) n_e}{\Gamma}.$$  

Using $(C/O)_{\odot} \approx 0.6$ (Asplund et al. 2005), $\alpha(T) \sim 70$ K $\approx 12 \cdot 10^{-12}$ cm$^3$ s$^{-1}$ (Pequignot & Aldrovandi 1986) and $\Gamma(C) = 310 \cdot 10^{-12}$ s$^{-1}$ (de Boer et al. 1973), one arrives at

$$\frac{N(C^1)}{N(O)} = 0.025 n_e.$$  

Note that for $T \approx 210$ K $\alpha$ would be a factor 1.7 smaller. And for strong shielding of UV radiation, $\Gamma$ would be up to a factor of 2 smaller (see de Boer et al. 1973). The column density ratios of C$^1$ to O$^1$ lead to values of $n_{\text{HI}}$ as given in Table5. We used the value of $\alpha$ for $T = 70$ K for the sight-lines Sk$^{}$-67$^5$107 to Sk$^{}$-67$^5$101 and for the other two sight-lines the 1.7 smaller $\alpha$.

These values, in combination with $\alpha(C^1)$, indicate a larger ionisation fraction towards Sk$^{}$-67$^5$111 and LH 54-425.

7. Conclusions

We have presented UV absorption line measurements of Galactic H$_2$, C$^1$, N$^1$, O$^1$, AI$^1$, Si$^1$II, P$^1$I, S$^1$III, Ar$^1$, and Fe$^2$I towards the six LMC stars Sk$^{}$-67$^5$111, LH 54-425, Sk$^{}$-67$^5$107, Sk$^{}$-67$^5$106, Sk$^{}$-67$^5$104, and Sk$^{}$-67$^5$101, and analysed the properties of the Galactic disc gas in these lines of sight. Our sight-lines were chosen within 5' in RA, with an almost constant Dec, to allow us to investigate the small-scale structures of the interstellar gas within $< 1.5$ pc (assuming that the foreground gas exists at a distance of $< 1$ kpc), with the smallest separation corresponding to $< 0.08$ pc. For four of the sight-lines, Sk$^{}$-67$^5$101, Sk$^{}$-67$^5$104, Sk$^{}$-67$^5$106, and Sk$^{}$-67$^5$107, we also analysed STIS spectral data, from which we have further determined the column densities of C$^1*$, C$^1**$, Mg$^2$I, Si$^4$IV, S$^2$II, Mn$^2$I, and Ni$^2$I. The STIS data provide additional absorption lines for some of the species already available in the FUSE spectra, allowing us to have a more reliable determination of the column densities.

In the spectral range of FUSE we are able to gain information from the different excitation levels of H$_2$, which provides us with valuable information about the fine structure of the gas, because H$_2$ arises in the coolest regions of the interstellar clouds, and enables us to derive the physical properties of the gas. The H$_2$ absorptions show considerable variation between our sight-lines. The lines of sight to Sk$^{}$-67$^5$101 and Sk$^{}$-67$^5$104 contain a significantly higher amount of H$_2$, about 2 dex in their column densities, compared to Sk$^{}$-67$^5$111. The rotational excitation of H$_2$ towards Sk$^{}$-67$^5$101 to Sk$^{}$-67$^5$107 agrees with a core-envelope structure of the H$_2$ gas with an average temperature...
of $T_{\text{exc}} \sim 70$ K, typical for CNM. This, and the low Doppler parameter of the lower $J$-levels, indicates that the molecular hydrogen probably arises in confined dense regions in these sightlines, where it is self-shielded from UV-radiation. The gas to LH 54-425 and Sk-67°111, on the other hand, appears to be fully thermalised, with $T_{\text{exc}} \sim 200$ K. This could suggest that within the $<5'$, we sample a core of a molecular hydrogen cloud, and reach the edge between Sk-67°107 and Sk-67°111. After including the LH 54-425 sight-line in our study, however, the spatial variation is not a smooth change from Sk-67°101 to Sk-67°111 (Fig. 8), and density fluctuation on scales smaller than the extent of $5'$ cannot be excluded.

In order to trace these variations back to the actual density variations and changes in the physical properties of the gas we have derived the densities partly based on the formation-dissociation equilibrium of molecular hydrogen using the measured $H_2$ and $O1$ column densities, and partly based on the excitation of the fine-structure levels of neutral carbon. For the latter we have also used the derived $T_{\text{exc}}(H_2)$, assuming that $C1$ and $H_2$ exist in the same physical region. The density derived in this way is $n_{\text{HI}} \approx 40 - 80 \text{ cm}^{-3}$ towards Sk-67°101 to Sk-67°107, for which we have relatively accurate measurements for column densities of $C1$ and $C18$, as well as $T_{\text{exc}}$. This is well above the value $n_{\text{H}} \approx 2 \text{ cm}^{-3}$ derived based on the formation-dissociation equilibrium of $H_2$. This is most likely because the available hydrogen for molecular formation is less than the total Galactic $N(H_1)$ derived from $N(O1)$ along a line of sight. Moreover, the $H_2$ self-shielding could be overestimated (and thus $n_{\text{HI}}$ underestimated) because of a complex absorber geometry. Thus that for $n_{\text{HI}}$ gives a minimum density required for the existence of the $H_2$.

On all sight-lines $N(H_2) \ll N(H1)$. If we assume that $[N/H]_{\text{tot}}$ is proportional to $n_{\text{HI}}$ (from $C1$) in the same way as for the inner region of a molecular cloud (meaning $[N/H]_{\text{tot}} = [n_{\text{HI}}/N(H_1)]_{\text{mol}}$), we can derive from Eq. (2) the column density of $H_1$ that coexists with $H_2$ in FDE. We so find that this is 18% of the total $N(H_1)$ (averaged over the sight-lines Sk-67°101 to Sk-67°107). It is of course likely that the partly molecular core is more dense because it is confined, and $n_{\text{HI}}$ not linearly related to the $N(H_1)$ as assumed above. Furthermore, $[N/H]_{\text{tot}}$ as derived from $C1$ is the averaged density of the molecular part of the gas, where $C1$ exists, and again not related to all the $H_1$ gas along a line of sight as assumed above. Thus, the $N(H_1)_{\text{tot}}$ together with the $n_{\text{HI}} = 40 - 80 \text{ cm}^{-3}$ give only an upper limit for the pathlength of the partly molecular cloud to be $D_{\text{mol}} = 0.5 \text{ - } 1.8 \text{ pc}$ (included in Table 5). These derived pathlengths are of the same size as (or smaller than) our lateral extent of the sight-lines ($<1.5\text{ pc}$). This derived upper limit for $D_{\text{mol}}$ also agrees with the higher density ratio for the LH 54-425 sight-line, derived in Sect. 4.1, which otherwise is difficult to explain if we consider this sight-line to sample the edge of the same cloud with the core on the Sk-67°101 to Sk-67°107 sightlines. Based on $\xi$ and an average density of $n_{\text{HI}} = 60 \text{ cm}^{-3}$, $D_{\text{mol}}$ in the direction of LH 54-425 and Sk-67°111 is estimated to be 0.1 and 0.6 pc, respectively. Given these small sizes, the $H_2$ patches observed on these six lines of sight are not necessarily connected. The small pathlength is further important for the shielding of the molecular gas, given the small amount of $H_1$ that is possible available in FDE with $H_2$.

We thus conclude that the $H_2$ observed along these six lines of sight exists in rather small clumps with an upper size $D_{\text{mol}} = 0.5 \text{ - } 1.8$, and possibly even less, < 0.1 pc, as implied by the LH54-425 sight-line. Part of the absorbing gas is possibly located at a distance closer than the 1 kpc assumed thus far, resulting in an even smaller spatial scale. This agrees with the sub-pc structure of molecular clouds previously detected by e.g. [Pan et al. (2001), Lauroesch et al. (2000, Richter et al. (2003-04), and Margraf et al. (2004). On a smaller scale of 5 to 104 AU however, [Boissé et al. (2009) found no variation in the column density of the $H_2$, observed over a period of almost five years towards the Galactic high-velocity star HD 34078. This despite the variations in the CH column densities found over the same period. They concluded that while the variation in CH and CH$^+$ is due to the chemical structure of a gas that is in interaction with the star, the $H_2$, located in a quiescent gas unaffected by the star, remains homogeneously distributed. Hence no small-scale density structure was proposed in the quiescent gas within this scale. Our spatial resolution limits us to the smallest separation of 14. We have therefore no further information about the AU-scale structure of the molecular gas in these lines of sight.

The absorber pathlength through the disc has previously been found to be divided into smaller cloudlets of $H_1$-absorbers ([Welty et al. (1999)], which are not necessarily physically connected to the cloud with the observed $H_2$. While the clumpy nature of $H_2$ is verified by different studies, the Galactic $H_1$ gas, when sampled over a line of sight, normally does not show variations on small scales, since such effects statistically cancel out and smooth the total observed $H_1$ (or $O1$ in our case). If such cloudlets exist in the Galactic disc component, their LSR velocity should be similar, and therefore would not be resolved in our spectra. Our derived density ratio $\xi$, as well as the relative abundances, suggest that the number of these absorbers might differ along the sight-lines, being less towards LH 54-425 and Sk-67°111. This interpretation also agrees with the higher electron density derived for these lines of sight.

We summarised in Sect. 4.1 the detection of small-scale structure by different independent methods. This paper presents yet another approach to identify the structure of the gas on small scales. FUV and UV spectral data, with the large range of transitions particularly of $H_2$ and $O1$ together with the fine-structure of $C1$, provide a sensitive approach to study the physical properties of the gas on small scales. However, our spatial resolution is limited to the separation of our background sources, and does not allow us to directly detect the fine structure that might exist on even smaller scales. Our findings are consistent with the small-scale structure found earlier in the interstellar medium, and suggest inhomogeneity in the interstellar Galactic gas down to, and possibly below, scales of 0.1 pc.

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Table 4. List of absorption lines, used for the column density determination in one or more sight-lines.  

| Species | $\lambda_0$ [Å] | $f \times 10^{-3}$ | Instrument | detector |
|---------|------------------|--------------------|------------|----------|
| C I     | 945.19           | 152.223            | FUSE       | SiC      |
|         | 1139.79          | 12.3               | FUSE       | LiF      |
|         | 1157.91          | 21.2               | FUSE       | LiF      |
|         | 1158.32          | 6.55               | FUSE       | LiF      |
|         | 1276.48          | 5.89               | STIS       |          |
|         | 1280.14          | 26.3               | STIS       |          |
|         | 1328.83          | 75.7756            | STIS       |          |
|         | 1560.31          | 77.4086            | STIS       |          |
|         | 1656.93          | 149.0              | STIS       |          |
| C I*    | 1279.89          | 14.3               | STIS       |          |
|         | 1560.68          | 58.1               | STIS       |          |
|         | 1656.27          | 62.1               | STIS       |          |
|         | 1657.38          | 37.1               | STIS       |          |
|         | 1657.91          | 49.4               | STIS       |          |
| C I**   | 1139.76          | 9.54               | FUSE       | LiF      |
|         | 1329.34          | 75.8               | STIS       |          |
|         | 1657.18          | 149.0              | STIS       |          |
| N I     | 952.30           | 2.29000            | FUSE       | SiC      |
|         | 952.42           | 1.97000            | FUSE       | SiC      |
|         | 952.52           | 0.518              | FUSE       | SiC      |
|         | 953.42           | 12.9300            | FUSE       | SiC      |
|         | 953.66           | 24.6900            | FUSE       | SiC      |
|         | 953.97           | 33.0700            | FUSE       | SiC      |
|         | 954.10           | 4.00000            | FUSE       | SiC      |
|         | 963.99           | 12.4100            | FUSE       | SiC      |
|         | 1134.17          | 14.6000            | FUSE       | LiF      |
|         | 1134.41          | 28.6500            | FUSE       | LiF      |
|         | 1134.98          | 41.5900            | FUSE       | LiF      |
|         | 1199.55          | 131.820            | STIS       |          |
| O I     | 922.20           | 0.245              | FUSE       | SiC      |
|         | 924.95           | 1.54500            | FUSE       | SiC      |
|         | 925.45           | 0.354              | FUSE       | SiC      |
|         | 930.26           | 0.537              | FUSE       | SiC      |
|         | 936.63           | 3.650              | FUSE       | SiC      |
|         | 971.74           | 11.6               | FUSE       | SiC      |
|         | 974.07           | 0.0156             | FUSE       | SiC      |
|         | 976.45           | 3.306              | FUSE       | SiC      |
|         | 1039.23          | 9.060              | FUSE       | LiF      |
|         | 1302.17          | 48.0100            | STIS       |          |
|         | 1355.60          | 0.00116            | STIS       |          |
| Mg II   | 1239.93          | 0.6320             | STIS       |          |
|         | 1240.39          | 0.3560             | STIS       |          |
| Al II   | 935.27           | 2.51803            | FUSE       | SiC      |
|         | 1670.79          | 1738.12            | STIS       |          |
| Si II   | 1020.70          | 16.7920            | FUSE       | LiF      |
|         | 1190.42          | 291.945            | STIS       |          |
|         | 1193.29          | 582.444            | STIS       |          |
|         | 1304.37          | 86.4170            | STIS       |          |
|         | 1526.71          | 132.814            | STIS       |          |
| Si IV   | 1393.76          | 513.0              | STIS       |          |
|         | 1402.77          | 254.0              | STIS       |          |
Table 4. continued.

| Species | $\lambda_0$ (Å)$^a$ | $f(\times 10^{-4})$ $^b$ | Instrument$^c$ | detector |
|---------|------------------|-----------------|----------------|----------|
| P II    | 961.04           | 348.54          | FUSE           | SiC      |
|         | 963.80           | 1458.86         | FUSE           | SiC      |
|         | 1152.82          | 2.4504          | FUSE           | LiF      |
| S II    | 1250.58          | 5.4311          | STIS           |          |
|         | 1253.81          | 10.9086         | STIS           |          |
|         | 1259.52          | 16.5881         | STIS           |          |
| S III   | 1012.49          | 43.8134         | FUSE           | LiF      |
|         | 1190.20          | 23.6254         | STIS           |          |
| Ar I    | 1048.22          | 262.753         | FUSE           | LiF      |
|         | 1066.66          | 67.4488         | FUSE           | LiF      |
| Mn II   | 1197.18          | 217.0           | STIS           |          |
| Fe II   | 1055.26          | 7.500           | FUSE           | LiF      |
|         | 1062.15          | 3.802           | FUSE           | LiF      |
|         | 1063.18          | 54.7513         | FUSE           | LiF      |
|         | 1081.87          | 12.5841         | FUSE           | LiF      |
|         | 1096.88          | 32.6469         | FUSE           | LiF      |
|         | 1112.05          | 4.46            | FUSE           | LiF      |
|         | 1121.97          | 28.9746         | FUSE           | LiF      |
|         | 1125.45          | 15.5838         | FUSE           | LiF      |
|         | 1127.10          | 2.8             | FUSE           | LiF      |
|         | 1133.67          | 4.72            | FUSE           | LiF      |
|         | 1142.37          | 4.01            | FUSE           | LiF      |
|         | 1143.23          | 19.2251         | FUSE           | LiF      |
|         | 1144.94          | 83.0268         | FUSE           | LiF      |
|         | 1608.45          | 57.7553         | STIS           |          |
| Ni II   | 1370.13          | 76.9551         | STIS           |          |
|         | 1454.84          | 32.2986         | STIS           |          |

$^a$ Due to the varying S/N for different data and the differences in the shape of the continua, a few of the listed absorptions are not used in all six sight-lines.

$^b$ The rest wavelength $\lambda_0$, and $f$-values are from Morton (2003).

$^c$ No STIS data are available for Sk -67$^\circ$ 111 and LH 54-425.
Table 5. Physical conditions in the Milky Way foreground gas as derived from the data.

| star          | Sk -67° 111 | LH 54–425 | Sk -67° 107 | Sk -67° 106 | Sk -67° 104 | Sk -67° 101 | comments |
|---------------|-------------|------------|-------------|-------------|-------------|-------------|----------|
| log \(N(\text{H}_1)\) | 20.6 | 20.2 | 20.9 | 21.0 | 20.9 | 21.0 | Sect. 6.1* |
| log \(N(\text{H}_2)\) | 15.9 | 15.8 | 17.6 | 18.0 | 18.1 | 18.1 | Sect. 4 |
| \(T_{\text{exc}}(\text{H}_2)\) [K] | 220 | 190 | 75 | 80 | 65 | 65 | Sect. 4.2 |
| \(\xi\) | 1.0 | 2.4 | 1.3 | 1.3 | 1.8 | 1.4 | Sect. 6.1 |
| \(n_{\text{H}}(\text{C}_1)\) [cm\(^{-3}\)] | <65 | <125 | 80 | 55 | 65 | 40 | Sect. 6.2 |
| \(n_e\) [cm\(^{-3}\)] | 0.045 | 0.072 | 0.007 | 0.007 | 0.005 | 0.014 | Sect. 6.2 |
| \(D_{\text{tot}}\) [pc] | 3.5 | 6.5 | 4.5 | 9 | | | Sect. 7 |
| \(D_{\text{mol}}\) [pc] | 0.6\(^b\) | 0.1\(^b\) | 0.5 | 1.1 | 0.8 | 1.8 | Sect. 7 |

Shielding as derived from \(\text{H}_2\):

|                | low | low | high | high | high | high | high | Sect. 4.2 |
|----------------|-----|-----|------|------|------|------|------|----------|

Depletion

| Fe,Mn,Ni | high | high | high | Sect. 5 |
|----------|------|------|------|---------|

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* Derived from O\(i\) and \((\text{O/H})_\odot = -3.34\) (Asplund et al. 2005).

\(^b\) Based on \(\xi\) and a reference LOS averaged over the values for Sk -67° 101 to Sk -67° 107.