Circumnuclear Dust in AP Librae and the Source of Its VHE Emission

Agniva Roychowdhury1, Eileen T. Meyer1, Markos Georganopoulos1,2, Peter Breiding3,4, and Maria Petropoulou5

Department of Physics, University of Maryland Baltimore County, 1000 Hilltop Circle, Baltimore, MD 21250, USA; agniva.physics@gmail.com
2 NASA Goddard Space Flight Center, Code 663, Greenbelt, MD 20771, USA
3 Department of Physics and Astronomy, West Virginia University, P.O. Box 6315, Morgantown, WV 26506, USA
4 Center for Gravitational Waves and Cosmology, West Virginia University, Chestnut Ridge Research Building, Morgantown, WV 26505, USA
5 Department of Physics, National and Kapodistrian University of Athens, University Campus Zografos, GR 15783, Greece

Abstract

The broad high-energy spectral component in blazars is usually attributed to various inverse Compton scattering processes in the relativistic jet, but has not been clearly identified in most cases due to degeneracies in physical models. AP Librae, a low-synchrotron-peak BL Lac object (LBL) detected in 2015 by H.E.S.S. at very high energies (VHE; $\gamma > 0.5 \text{TeV}$), has an extremely broad high-energy spectrum, covering $\sim$9 decades in energy. Standard synchrotron self-Compton models generally fail to reproduce the VHE emission, which has led to the suggestion that it might arise not from the blazar core, but from kiloparsec scales from inverse Compton (IC) scattering of cosmic microwave background (CMB) photons by a still-relativistic jet (IC/CMB). IC/CMB models for the TeV emission of AP Librae in prior works have implied a high level of infrared emission from the kiloparsec-scale jet. With newly obtained Hubble Space Telescope (HST) imaging, we obtain a deep upper limit on the kiloparsec-scale jet emission at 1.6 μm, well below the expected level. High-resolution Atacama Large Millimeter/submillimeter Array imaging in bands 3–9 reveals a residual dust-disk signature after core subtraction, with a clearly thermal spectrum, and an extent ($\sim 500 \text{ pc}$) that matches with a nonjet residual emission seen after point-spread function subtraction in our 1.6 μm HST imaging. We find that the unusually broad GeV and VHE emission in AP Librae can be reproduced through the combined IC scattering of photons from the CMB and the dust disk, respectively, by electrons in both the blazar core and subkiloparsec jet.

1. Introduction

Radio-loud active galactic nuclei (AGN) are characterized by relativistic jets of fully ionized plasma moving very near the speed of light (e.g., Urry & Padovani 1995; Blandford et al. 2019). High-resolution radio observations have revealed that these jets are highly collimated and originate near the central supermassive black hole (SMBH; e.g., Asada et al. 2009). In blazars, these jets are aligned within a few degrees of our line of sight. The emission from the fast-moving base of the jet (on parsec scales) is thus highly Doppler boosted, where the Doppler factors may range from a few to over a hundred (e.g., Ghisellini et al. 1993; Hovatta et al. 2009). This amplification of the emission from the base of the jet (or “core”) causes what is usually termed a jet-dominated blazar spectral energy distribution (SED) from radio to gamma-rays. In a plot of log $\nu F_\nu$ vs. log $\nu$, the typical spectrum appears as two broad components of nearly equal amplitude, the first peaking anywhere between $10^{12}$–$10^{17} \text{ Hz}$ and the second at GeV to TeV energies (e.g., von Montigny et al. 1995; Fossati et al. 1998; Meyer et al. 2011).

Although the cause of the lower-energy emission component in blazars is well established as synchrotron radiation from relativistic electrons (e.g., Urry & Mushotzky 1982), there is less certainty regarding the location and origin of the second (higher-energy) component in blazars. In most cases it is presumed that the emission originates either from the base of the jet or very near to it ($\sim$ few parsec scales). Most theoretical models assume a purely leptonic jet by default, where the same relativistic electrons responsible for synchrotron emission inverse Compton scatter either their own synchrotron photons (synchrotron self-Compton, SSC) or photons from an external field (external Compton or EC) to produce the GeV–TeV component of the SED (see, e.g., Böttcher 2007; Sikora et al. 2009).

Hadronic models are an alternative to the purely leptonic scenario. In these cases protons are accelerated to very high energies ($> \text{PeV}$) and can produce $\gamma$-rays directly via synchrotron radiation (e.g., Aharonian 2000; Mücke & Protheroe 2001; Petropoulou & Dimitrakoudis 2015) or indirectly via synchrotron plus Compton processes of secondary leptons produced in photodisproportionate interactions (e.g., Mannheim et al. 1991; Mannheim 1993; Aharonian 2000; Mücke et al. 2003; Petropoulou et al. 2015). The main objection to hadronic models is the necessarily high (often super-Eddington) power requirements (Sikora 2011; Zdziarski & Böttcher 2015).

The blazar population can be divided phenomenologically into low-synchrotron-peak (LSP; $\nu_{\text{peak}} < 10^{14} \text{ Hz}$), intermediate-synchrotron-peak (ISP; $10^{14} < \nu_{\text{peak}} < 10^{15} \text{ Hz}$) and high-synchrotron-peak (HSP; $\nu_{\text{peak}} > 10^{15} \text{ Hz}$) sources. Separately from the SED type, blazars with quasar-like broad emission lines (nearly all of which are LSP sources) are known as flat-spectrum radio quasars (FSRQs), suggestive of a strongly accreting system, and those with an optically featureless spectrum having equivalent line widths $\Delta \lambda < 5 \text{ Å}$ are known as BL Lacs, implying radiatively inefficient accretion. At VHE ($> 500 \text{ GeV}$), the dominant extragalactic source class is blazars.
and, in particular, HSP BL Lacs (HBLs). While HBLs comprise ~30% of all identified sources at VHE, only four LSP BL Lacs (LBLs) and eight FSRQs have been detected to date (Wakely & Horan 2008; Albert et al. 2007; Anderhub et al. 2009). In the leptonic scenario, the GeV–TeV emission is generally attributed to SSC in HBLs and EC in FSRQs and LBLs (e.g., Sikora et al. 2009; Meyer et al. 2012; Madejski & Sikora 2016), possibly reflecting weak accretion-disk emission in the former.

AP Librae is a well-known nearby LBL at $z = 0.049$ (3.8 kpc $/4''$, Jones et al. 2009) and one of the only four LBLs detected at VHE (HESS Collaboration et al. 2015). The X-ray to TeV component is unusually broad, extending over ~9 orders of magnitude in frequency. AP Librae also exhibits a resolved radio jet which has been detected in X-rays with the Chandra X-ray Observatory (Cassaro et al. 1999; Kaufmann et al. 2013), making it the only LBL source out of approximately 200 AGNs known to host an X-ray-emitting kiloparsec-scale jet$^6$.

The broadness of the high-energy component in AP Librae relative to the synchrotron peak makes it difficult to model using standard single-zone SSC or EC models. Even before the VHE detection of the source by H.E.S.S., Tavecchio et al. (2010) noted this difficulty when attempting to fit a one-zone SSC model to Fermi/LAT observations. Their model could not fit both the X-ray and the GeV bands simultaneously, underestimating the X-rays by ~an order of magnitude to fit the GeV or vice versa. They attributed this to the gross nonsimultaneity of the Fermi-LAT and X-ray observations ($\sim$9 yr) and the possible presence of an X-ray jet. However, Sanchez et al. (2015) confirmed these findings with quasi-simultaneous X-ray and Fermi/LAT observations (see also Zacharias & Wagner 2016).

Subsequently, several efforts were made to move beyond a simple SSC model for the VHE emission. Both Zacharias & Wagner (2016) and Sanchez et al. (2015) suggested that inverse Compton scattering off cosmic microwave background photons in the extended jet (the IC/CMB mechanism, first proposed by Tavecchio et al. 2000, for another source) could explain the high-energy Fermi/LAT and H.E.S.S. emission, although the synchrotron spectrum of the large-scale jet was severely unconstrained in these works. Rather than the kiloparsec-scale jet, Hervet et al. (2015) used a more complex blob-in-a-jet emission model and showed that electrons in the parsec-scale blob could reproduce the Fermi/LAT band and VHE spectra via inverse Compton scattering of broad-line region (BLR) photons and synchrotron photons from the parsec-scale jet, respectively. Petropoulou et al. (2017) favored the core as the origin of the high-energy emission, proposing a lepto-hadronic scenario with the TeV emission primarily arising from photodihadronic processes.

The very broad X-ray to VHE spectrum of AP Librae is unusual but not unique, and similar modeling difficulties as above have been encountered in other IBL/LBLs detected at VHE, namely BL Lacertae (Albert et al. 2007), S5 0716+714 (Anderhub et al. 2009), 3C 66A (Joshi & Böttcher 2007) and W Comae (Acciari et al. 2009). Although a single-zone SSC model has been able to explain the VHE emission in two nearby radio galaxies with a broad second component (M87; de Jong et al. 2015 and NGC 1275; Aleksic et al. 2014) it is inadequate for all the above blazars as well as the radio galaxy Centaurus A (Petropoulou et al. 2014; Tanada et al. 2019); in most cases, a combination of SSC and external Compton models is required.

For AP Librae, the potential physical scenarios and emission mechanisms laid out in previous works are considerably at variance and imply very different jet characteristics at a fundamental level, including jet composition, velocity, and total energy content. Our aim in this study is to explain the very broad second component in AP Librae and, in particular, to test the clear predictions of the models invoking IC/CMB in the kiloparsec-scale jet for TeV emission (e.g., Zacharias & Wagner 2016). These models predict a high level of infrared synchrotron emission from the jet, provided by the same electrons required to explain the TeV emission. In this paper, we present new observations of AP Librae with the Very Large Array (VLA), Atacama Large Millimeter/submillimeter Array (ALMA), the Hubble Space Telescope (HST), and the Fermi/LAT observatory designed to fully constrain the synchrotron spectrum of the kiloparsec-scale jet and deduce the origin of the VHE emission.

In Section 2, we present the multi-wavelength data reduction procedure. In Section 3, we use multi-wavelength SED modeling to discuss the origin of TeV emission from the source. In Section 4, we conclude with a summary of the work and possible future directions this study can take.

2. Observations

We describe here the VLA, ALMA, HST, and Fermi/LAT data analyzed for this project, where we are primarily focused on new observations of the large-scale jet. Core fluxes (or total fluxes, presumed to be dominated by the core) were taken from the NASA Extragalactic Database$^7$ unless otherwise noted. In addition, we have utilized other observations reported previously in the literature for this source. These include Chandra X-ray fluxes of the large-scale jet which we obtained from Kaufmann et al. (2013), and the TeV spectrum and flux points from the H.E.S.S. observatory (HESS Collaboration et al. 2015).

2.1. Very Large Array

We reduced several historical VLA observations of AP Librae using the Common Astronomy Software Applications (CASA; McMullin et al. 2007). A summary of these observations with the relevant image properties including peak and total fluxes, final image rms in Jy, synthesized beam size in arcsec, and largest angular scale are listed in Table 1. We applied standard initial calibration to all the data sets. AP Librae is core-dominated and very bright in all radio imaging and thus phase and amplitude self-calibration were applied to improve the final imaging, where we used Briggs weighting with robustness $= 0.5$ (Briggs 1995).

Previous radio imaging shows AP Librae to host a $\sim 20''$ long radio jet (Cassaro et al. 1999). Our imaging deconvolution showed components in the large-scale jet within $1''$ from the peak core position. Accordingly, we produced core-subtracted images to more accurately measure the total jet flux. To do so we used the clean deconvolution task in CASA to create a point-source model for only the core and then subtracted it from the total visibility data using CASA...
This was followed by a final clean of the resulting core-subtracted visibility to produce a final image without the core. The total jet flux density for each of the VLA images was then given by the flux density of a large region containing all of the extended jet emission. The L-band (A-config) VLA image of AP Librae (core subtracted) is shown at left in Figure 1, with contours from the same observation overlaid. An ALMA band 3 image (also core subtracted) on the same scale and with the same L-band contours (further described below) is shown at right.

### Table 1: Radio and Submillimeter Observations

| Obs. | Band | Freq. (GHz) | Project Code | Date YYYY-MM-DD | Synthesized Beam (arcsec) | LAS (arcsec) | rms (Jy) | $F_{\text{core}}$ (Jy) | $F_{\text{tot}}$ (Jy) |
|------|------|-------------|--------------|-----------------|---------------------------|--------------|----------|----------------------|----------------------|
| VLA  | L    | 1.5         | AB700        | 1994-04-19      | 3.23 × 1.17              | 36           | 2.9 × 10^{-4} | 1.5000               | ...                  |
| VLA  | C    | 4.8         | AA099        | 1994-04-19      | 3.38 × 2.84              | 240          | 2.0 × 10^{-4} | 1.5240               | ...                  |
| VLA  | X    | 8.4         | AV0194       | 1992-04-27      | 4.86 × 2.26              | 145          | 5.3 × 10^{-4} | 1.6900               | ...                  |
| VLA  | U    | 15.0        | 20B-356      | 1992-04-27      | 0.24 × 0.11              | 36           | 1.7 × 10^{-5} | 2.1549               | ...                  |
| ALMA | 3    | 99          | 2017.1.01411.T | 2018-06-09    | 4.51 × 2.54              | 248          | 4.1 × 10^{-5} | 3.2468  | 3.2525               |
| ALMA | 5    | 198         | 2017.1.00568 | 2018-09-17     | 0.35 × 0.29              | 4.8          | 5.4 × 10^{-5} | 2.4037  | 2.4148               |
| ALMA | 6    | 232         | 2017.1.00995 | 2018-03-15     | 0.50 × 0.40              | 5.7          | 3.5 × 10^{-5} | 1.9375  | 1.9630               |
| ALMA | 7    | 337         | 2017.1.00258 | 2018-05-18     | 0.92 × 0.66              | 7.3          | 7.1 × 10^{-5} | 2.3496  | 2.3550               |
| ALMA | 7    | 341         | 2017.1.01583 | 2018-04-19     | 0.53 × 0.40              | 5.3          | 5.8 × 10^{-5} | 2.0052  | 2.0073               |
| ALMA | 7    | 348         | 2017.1.00963 | 2018-05-29     | 0.99 × 0.68              | 7.6          | 6.2 × 10^{-5} | 2.3919  | 2.3957               |
| ALMA | 8    | 405         | 2017.A.00047 | 2018-06-30     | 0.80 × 0.57              | 5.7          | 1.9 × 10^{-4} | 2.1090  | 2.1240               |
| ALMA | 8    | 426         | 2017.1.00239 | 2018-06-01     | 0.79 × 0.65              | 6.0          | 2.9 × 10^{-4} | 2.0920  | 2.0990               |
| ALMA | 8    | 464         | 2013.100244  | 2015-05-20     | 0.37 × 0.27              | 2.7          | 2.4 × 10^{-4} | 1.0390  | 1.0450               |
| ALMA | 9    | 654         | 2017.1.01555 | 2018-05-20     | 0.50 × 0.36              | 3.8          | 4.8 × 10^{-4} | 1.9420  | 1.9536               |
| ALMA | 9    | 671         | 2017.A.00047 | 2018-06-30     | 0.42 × 0.36              | 3.4          | 9.4 × 10^{-4} | 1.7510  | 1.7670               |
| ALMA | 9    | 679         | 2017.1.00337 | 2018-05-23     | 0.44 × 0.34              | 3.7          | 6.8 × 10^{-4} | 1.9240  | 1.9353               |
| ALMA | 9    | 692         | 2017.1.00023 | 2018-05-04     | 0.36 × 0.21              | 2.7          | 1.0 × 10^{-3} | 1.8453  | 1.8665               |
| ALMA | 9    | 699         | 2017.1.01555 | 2018-05-20     | 0.47 × 0.34              | 3.5          | 9.9 × 10^{-4} | 1.9070  | 1.9200               |

**Note.** LAS: largest angular scale; rms: root mean squared sensitivity.
imaging with clean. We used several rounds of (noncumulative) phase-only self-calibration and a final amplitude and phase self-calibration to greatly improve the dynamic range and sensitivity of the final images.

We show at right in Figure 1 a band 3 image with L-band radio contours overlaid. In all of the ALMA images, the point-source core is significantly (∼100 times) brighter than the jet. The residual images after core subtraction show both emission from the jet and residual flux around the core, which is increasingly dominant with increase in frequency. The residual emission region appears elongated in the NE–SW direction at position angle ∼50° with a maximum extent of ∼1″ (about 900 pc). This can be seen in the residual core-subtracted images shown with the same flux scale in Figure 2 where this emission clearly increases with increasing observing frequency. The dominance of this residual emission at higher frequencies and on similar scales to the inner jet made it difficult to accurately measure the flux from the jet alone. This was compounded by our incomplete knowledge of its structure, and the possibility of “oversubtracting” the core. To avoid the latter issue, we assume the peak flux is the total core emission and subtract this from the total source flux, measured using a large region around the full source and extended jet. The result is a combination of the jet and residual emission. This is given along with a 1σ error in Table 2. The associated uncertainties of the method have been described in more detail in Appendix A.

Summarizing, all the images in Figures 1 and 2 have been produced by subtracting the clean model for the core, but we followed the above method for calculating the jet + residual flux for the ALMA images only.

The residual emission in Figure 2 appears as a slightly asymmetric disk. Subtraction of the core in clean with lower iterations per cycle would show a more continuous disk emission such as in Appendix A. The disk has a larger NE–SW extent, while the SE harbors the blazar jet and the NW is faint. This fits with the expectation that the jet be roughly perpendicular to the disk. This has been found for FRI radio galaxies with circumnuclear dust (e.g., de Koff et al. 2000; Landt et al. 2010; Drouart et al. 2012), and thus may be expected for their possible beamed counterparts, which are BL Lac objects. The residual disk emission follows a quasi-Rayleigh–Jeans spectrum (Figure 6 and Section 3.2) and is therefore most likely dust emission. Since AP Librae is a blazar, the jet presumably forms a very close angle to the line...
Table 2
Radio and Submillimeter Fluxes for AP Librae after Core Subtraction

| Central Freq. (GHz) | $F_{\text{jet}}$ (Jy) | $F_{\text{jet-conv}}$ (Jy) | Std. Dev. |
|---------------------|------------------------|-----------------------------|-----------|
| 1.52$^a$            | 0.0940                 | ...                         | 0.0010    |
| 4.86$^a$            | 0.0450                 | ...                         | 0.0045    |
| 8.4$^a$             | 0.0300                 | ...                         | 0.0030    |
| 15$^a$              | 0.0187                 | ...                         | 0.0037    |
| 99                  | ...                    | 0.0057                      | 0.0006    |
| 198                 | ...                    | 0.0070                      | 0.0006    |
| 232                 | ...                    | 0.0055                      | 0.0004    |
| 337                 | ...                    | 0.0033                      | 0.0007    |
| 341                 | ...                    | 0.0027                      | 0.0005    |
| 348                 | ...                    | 0.0025                      | 0.0007    |
| 405                 | ...                    | 0.0082                      | 0.0013    |
| 426                 | ...                    | 0.0020                      | 0.0008    |
| 464                 | ...                    | 0.0036                      | 0.0026    |
| 654                 | ...                    | 0.0106                      | 0.0023    |
| 671                 | ...                    | 0.0160                      | 0.0032    |
| 679                 | ...                    | 0.0115                      | 0.0025    |
| 692                 | ...                    | 0.0212                      | 0.0065    |
| 699                 | ...                    | 0.0110                      | 0.0052    |

Note. For each of the four VLA/JVLA observations, the flux reported here is entirely due to the jet.

of sight. If the disk axis is perfectly aligned with that of the jet, we should see a more face-on view of the dusty disk as a circular halo after core subtraction. However, we see an absence of emission in the direction of the jet and the counterjet. It is possible that the dusty disk is slightly misaligned with the direction of the jet, resulting in the jet blowing away a fraction of the disk in the SE–NW direction, thereby resulting in a “gap” where the dust brightness is low. This is also consistent with X-ray observations of the core of AP Librae where Kaufmann et al. (2013) find a hydrogen column density $N_{\text{H}} \sim 10^{21}$ cm$^{-2}$, a value typical of ordinary galactic absorption instead of obscuring tori due to AGN or starburst heating (Hickox & Alexander 2018).

To minimize biases due to resolution, we calculate the true size of the excess emission by deconvoluting it from the beam. The dimensions could be determined from a simple Gaussian fit to the 652 GHz image inside CASA, for which the deconvolved major and minor axes are $1.30 \pm 0.05$ kpc and $0.20 \pm 0.02$ kpc. These translate to $R = 0.65 \pm 0.02$ kpc and $W = 0.20 \pm 0.02$ kpc where $R$ and $W$ are the NE–SW extent and the spread of the disk across the plane of the sky, respectively. However, the intrinsic scale height $H$ of the disk cannot be determined because of its face-on orientation. So we assume $H \sim R/5$ based on the ALMA observations of CO lines in radio-quiet AGNs (e.g., Hönig 2019).

2.3. Hubble Space Telescope

AP Librae has been imaged twice by HST since the SM1 optics correction. The initial observation was taken as part of a BL Lac snapshot program (6363) in 1997, consisting of three 100 s exposures with WFC2/PC in the F702W filter. The upper limit on the emission from the bright inner jet from this shallow observation is not constraining on the IC/CMB model predictions. We thus obtained a much deeper (two-orbit) observation with the fourth-generation Wide-field Camera 3 (WFC3) UVIS/IR imager on the HST. Observations totaling 5016 s were taken on 2018 February 15 with the F160W filter which peaks at 1.5 microns.

In order to more clearly observe any possible jet-related emission in our near-IR imaging, it was necessary to model and subtract both the host galaxy emission and the central point source due to the bright blazar core. For our point-spread function (PSF) model, we used an observation of a bright star made in the same instrument/filter setup and close-in detector coordinates to our observation of AP Librae. We chose the bright star V$^*$ AY Ori (05:36:08.3–06:48:36.36) observed in project 14695-ID7Z03010 on 2016 September 14 for 2.4 ks. The star has clear diffraction spikes of a similar strength to the central point source of AP Librae without adjacent contamination from other bright objects.

We used the publicly available GALFIT (GALaxy-FITting; Peng et al. 2002) routine to model the galaxy and central point source. GALFIT takes in the source image and PSF as FITS file inputs and fits a user-chosen model of one or more components. All fitting was done using nondistortion-corrected .flx images and the nondistortion-corrected PSF, where we used only a $300 \times 300$ pixel subset of the image centered on AP Librae. We used a simple model with a single Sérsic component, an exponential disk (to model the residual dust emission observed by ALMA) plus PSF to model the galaxy and point source in each of the four HST exposures. Addition of an exponential disk reduced the chi-square and subtracted residual emission which was otherwise visible with a simple Sérsic+PSF model (see Figure 3 where we illustrate this difference). We utilized a custom mask in the fitting to avoid biasing the fit from either the jet or extraneous background objects and other artifacts. We masked out the jet region (using radio maps as a guide) as well as any bright source in the $300 \times 300$ region. The average (over each raw image) best GALFIT parameters are given in Table 3.

After running GALFIT on each exposure to produce a galaxy/PSF-subtracted distorted image, we then used Astro-Drizzle and Tweakreg with standard settings to align the subtracted frames to produce a final subtracted and distortion-corrected image. To convert from count rate to flux units, we used the python PYSYNPHOT package. We adopted a flat spectral slope through the F160W band and an extinction magnitude $E(B–V)$ of 0.1177 (Schlafly & Finkbeiner 2011). A comparison of the resulting image stack using nonsubtracted frames and subtracted frames is shown in Figure 4, with L-band VLA radio contours overlaid.

There is no indication of any jet-related flux by eye in the HST imaging after subtraction. We confirmed this and derived an upper limit for the IR flux density. Due to imperfections in the galaxy subtraction, we carefully sampled areas of the subtracted image corresponding to the same radial distance from the core (corresponding to $\sim 5$ kpc, shown in Figure 4) to derive our 5$\sigma$ upper limit of 0.70 $\mu$Jy.

Further, using the value of the magnitude photometric zero-point for HST/WFC3 as 28.2 (see HST/WFC3 handbook in Equation (5) in Peng et al. (2002), we obtained the total integrated flux density of the exponential disk model, or the IR dust emission, as 1.27 mJy. The semimajor axis of this disk is $\sim 6$ pixels, and with a plate scale of $\sim 0.12^\prime$/pixel for WFC3, it turns out to be $\sim 0.7$ kpc, consistent with ALMA observations.

It is imperative to note that the flux of this model is $\lesssim 10^{-5} F_{\text{sersic}+\text{psf}}$ due to which the corresponding lower bound of this flux is poorly constrained. Observing the
worsening of the fit, we hence choose 50% and 20% lower and upper bounds, respectively, to the flux, implying \( F_{\gamma} \approx 1.27^{+0.25}_{-0.65} \text{ mJy} \). However, we note that this has little to no impact on our conclusions.

2.4. Fermi

AP Librae has been detected by the Fermi/LAT and is listed in the 4FGL-DR2 point-source catalog as 4FGL J1517.7-2422 with a detection significance of 95. We have analyzed over 12 yr of continuous Fermi/LAT observations to derive an average spectrum for this source, and have also derived the minimum flux state using the progressive-binning analysis method first presented in Meyer & Georganopoulos (2014). We briefly summarize the procedure here. Fermi/LAT event and spacecraft data were extracted using a 7° region of interest (ROI), an energy cut of 50 MeV–300 GeV, a zenith angle cut of 90°, and the recommended event class and type for point-source analysis (128 and 3, respectively). The time cuts included all available Fermi data at the time of analysis, with corresponding mission elapse time (MET) ranges of 239557417 to 626971271 (corresponding from 2008 August 4 to 2020 November 13).

Using a model file populated with known 4FGL sources, we first generated a light curve by dividing the data into three week on-source time bins and running the pre-likelihood analysis tools on each time bin separately. In the maximum likelihood analysis for each time bin we model AP Librae as a power law with a fixed photon index of 2.1; all other sources in the ROI similarly have their spectral shape fixed during the fit. We then used the combined-bin analysis procedure in order to determine the apparent minimum flux in each of the seven standard Fermi energy bands as used in the 4FGL catalog. The minimum and (12 yr) average fluxes are given in Table 4, along with the energy bin boundaries, central frequency, and the corresponding number of bins used to derive the minimum flux. The plot of flux versus number of bins combined for the seven energy bands is shown in Figure 5.

The time bins were defined in terms of good time interval (GTI) time, corresponding to roughly 8 weeks in real time.
3. Results and Discussion

3.1. Evaluating the IC/CMB Model

We present an updated spectral energy distribution (SED) for AP Librae in Figure 6, where all observations of the kiloparsec-scale jet below X-ray energies as well as the Fermi/LAT observations are newly presented in this paper. The historical total source fluxes (dominated by the blazar core) shown in gray are taken from Zacharias & Wagner (2016) (hereafter Z16) and/or NED. We have used red data points for the kiloparsec-scale jet fluxes and the IR upper limit, and orange triangles for the jet + dust fluxes measured by ALMA for the frequencies above 100 GHz (which are clearly dominated by the thermal component). An orange square point has been used for the estimated flux of the (presumed) dust-disk residual from our IR imaging. The X-ray spectrum for the kiloparsec-scale jet is also shown as red points (from Kaufmann et al. 2013). In the GeV–TeV band, we show the Fermi/LAT 12 yr average flux in dark gray and the minimum LAT fluxes in dark blue. Finally the H.E.S.S. TeV flux points are shown in magenta (from HESS Collaboration et al. 2015). In this section, we will primarily focus on the CMB seed photon field and the validity of the IC/CMB model for the TeV emission. In the following sections, we discuss the dust seed photon field in detail and its contribution to the broadband SED.

While we are able to separately resolve the core and the kiloparsec-scale jet at lower frequencies, in the GeV–TeV regime, the observations shown in Figure 6 are for the entire source and it is not clear which zone of emission dominates. The light gray and cyan model curves are taken from Z16. The thick cyan curve is their synchrotron model for the large-scale jet and the thin cyan curve is the corresponding IC/CMB emission proposed to explain the kiloparsec-scale X-ray and (total) TeV emission. The required synchrotron spectrum under this model is now clearly very discrepant considering the new data points. The radio spectrum is significantly harder than assumed in Z16, while our IR upper limit for the jet is far below the model curve. The light gray and cyan model curves are taken from Z16. The thick cyan curve is their synchrotron model for the large-scale jet and the thin cyan curve is the corresponding IC/CMB emission proposed to explain the kiloparsec-scale X-ray and (total) TeV emission. The required synchrotron spectrum under this model is now clearly very discrepant considering the new data points. The radio spectrum is significantly harder than assumed in Z16, while our IR upper limit for the jet is far below the model curve. The light gray and cyan model curves are taken from Z16. The thick cyan curve is their synchrotron model for the large-scale jet and the thin cyan curve is the corresponding IC/CMB emission proposed to explain the kiloparsec-scale X-ray and (total) TeV emission. The required synchrotron spectrum under this model is now clearly very discrepant considering the new data points. The radio spectrum is significantly harder than assumed in Z16, while our IR upper limit for the jet is far below the model curve. The light gray and cyan model curves are taken from Z16. The thick cyan curve is their synchrotron model for the large-scale jet and the thin cyan curve is the corresponding IC/CMB emission proposed to explain the kiloparsec-scale X-ray and (total) TeV emission. The required synchrotron spectrum under this model is now clearly very discrepant considering the new data points. The radio spectrum is significantly harder than assumed in Z16, while our IR upper limit for the jet is far below the model curve.
Instead, we have confined our measurements to the 4″ scale jet from which X-ray emission is detected.

While it is clear that the specific IC/CMB model of Z16 is now ruled out, it is worthwhile to consider whether an IC/CMB model for the kiloparsec-scale X-ray emission could still be compatible with the GeV–TeV observations, if not fully explain them. In Figure 7 we show the same data as in the previous figure, and consider different possible IC/CMB scenarios given the constraints on the kiloparsec-scale synchrotron emission. In the “naive” scenario, we fit a
phenomenological power law with exponential cutoff model to the radio through IR data, shown as a thick blue line. The key parameters that govern the synchrotron and correspondingly the IC spectral shape are the Doppler factor $\delta$ ($=\Gamma(1 - \beta \cos \theta)^{-1}$ where $\beta$ is the jet bulk speed, $\Gamma$ is the bulk Lorentz factor, and $\theta$ is the angle between the jet and our line of sight) and the magnetic field $B$ (e.g., Georganopoulos et al. 2006), where the IC spectral shape can be derived from simple shifting of the synchrotron spectrum in frequency and luminosity. A $B/\delta$ value of $\sim 10^{-7.2}$ allows the corresponding IC/CMB component to match well the GeV maximum energy compared to that producing the radio.

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The only IC/CMB model that can satisfy the current observational constraints below $10^{15}$ Hz and explain the TeV emission without violating the Fermi/LAT minimum is a somewhat contrived two-component model, shown as a solid black line in Figure 7. Here we have simply added a second (phenomenological) synchrotron spectrum, peaking just below $10^{14}$ Hz to the previous dashed curve spectrum. Such a model does appear to match well the GeV–TeV spectrum of AP Librae, however, we have no direct evidence for the existence of the second synchrotron component, which would require a separate electron energy distribution with slightly higher maximum energy compared to that producing the radio.

### 3.2. Properties of the Dust Spectrum

Based on the core-subtracted imaging shown in Figure 2, the residual ALMA dust emission appears to arise from a disk possibly being viewed at a small inclination (or “face-on”). This is the first detection of large-scale dust emission in a BL Lac and is in marked contrast with studies that have otherwise failed to detect any dust emission from a parsec-scale torus in a large sample of BL Lacs (Plotkin et al. 2012). Detailed modeling of the dust structure and emission (e.g., Nenkova et al. 2002; Fritz et al. 2006; Stalevski et al. 2012) is beyond the scope of this paper. We employ a very simple cylindrical model (with thickness and height) to model its structure and thereby the emission spectrum as in Section 2.2, where we determined that the approximate radius $R$ of the disk is 0.65 kpc, and the inferred scale height using $H \approx R/5$ is 0.13 kpc. The inner radius $r_\mu$ of the disk must connect with the parsec-scale torus (if present) and for the purpose of modeling we neglect this as $r_\mu \ll R^2$. Assuming simplistically the disk thermally emits at a single temperature, the total luminosity of the disk would be given by $L = (2\pi R^2 H)^2 (14\pi R^2 / 5) F$, where $F$ is the total flux integrated over all frequencies emitted by the disk. If we use the blackbody flux $F = \sigma T^4$ and luminosity distance $D_L = 215$ Mpc, we find that the ALMA fluxes match a blackbody of temperature $T = 25$ K and $R = 0.10$ kpc. The fitted value of $R$ is shorter than an effective observed size ($\sqrt{RH} \approx 0.40$ kpc) as most of the flux comes from the central part of the dusty disk. While there are a range of blackbodies of different temperature and spatial size which are consistent with our data, we chose the above parameters since they are consistent with our imaging and SED modeling (Section 3.4) and slight differences do not affect our results. However, as a very conservative estimate, if $r_\mu$ is actually larger than assumed/observed, e.g., $r_\mu \sim 0.5R$, $L$ is only reduced by $\sim 15\%$. The fact that this is insensitive to the outcome of the paper is further exemplified in Appendices A and B.

From HST imaging, we only have one observation in the IR, which equals a flux value $F_\nu \approx 1.27$ mJy at $10^{14.30}$ Hz. The size of the dust disk, as inferred indirectly from model-fitting using GALFIT, was $R \approx 0.5$ kpc, consistent with that obtained from ALMA. The $25$ K blackbody that describes the ALMA observations grossly underestimates this IR flux (Figure 8), implying we require a better model to describe the total dust spectrum from submillimeter to the IR. Hence we represent the HST flux with a Heaviside spectral flux density centered at $10^{14.30}$ Hz with width equal to that of the F160W filter. We use both the above models of the dust seed photon fields in the upcoming subsections to explain the origin of TeV emission using inverse Compton scattering.

#### 3.3. Revisiting Inverse Compton Models

The discussion in Section 3.1 disproved a simple one-zone IC/CMB model for the origin of the VHE emission but did allow a double-synchrotron model to explain the broadband SED of AP Librae. Our objective in this section is to make indicative fits to the SED of AP Librae discussing the possibilities of different seed photon fields as a source of TeV emission through external Compton by hot electrons in the jet/core.

##### 3.3.1. Seed Photon Fields within the Kiloparsec-scale X-ray-emitting Jet

We consider the case of the kiloparsec-scale X-ray-emitting jet of AP Librae (Kaufman et al. 2013), which moves with bulk Lorentz factor $\Gamma$ (and speed $\beta$) and most emission occurs within $\sim 10$ kpc from the subkiloparsec core, with the bright knot(s) lying at $z_0 \lesssim 5$ kpc (Kaufman et al. 2013 and Figure 1). If we assume the average angle of the kiloparsec-scale jet to our line of sight ($\theta$) to lie between $5^\circ$ and $15^\circ$, following spectral modeling by Hervet et al. (2015) and Zacharias & Wagner (2016), this implies that the maximum deprojected jet length is 114 kpc, while the brightest knot lies at $z_0 = 0.40$ for $z_0 = 4$ kpc. In the following paragraphs, we discuss the importance of different seed photon fields for inverse Compton emission from the kiloparsec-scale jet.

**Radiation from the blazar core.** Let the blazar core be defined by a size $r_c = 1$ pc. Radiation from this core is relativistically beamed into an opening angle $\lesssim 1/\Gamma_{\text{core}}$, considering the subparsec jet to be moving with a bulk Lorentz factor $\Gamma_{\text{core}}$ (and a Doppler factor $\delta_c$). For an approximate value of the deprojected distance along the kiloparsec-scale jet (with $\theta \lesssim 10^\circ$) $z_{\text{deproj}} = 1$ kpc/$\sin 10^\circ = 5.75$ kpc ($\gg r_c$), it is safe to assume that radiation from the core illuminates the kiloparsec-scale jet directly from behind, implying the nuclear radiation is...
Figure 8. Data points are as in Figure 6. The orange fitted line is the blackbody fit to the ALMA fluxes for $T = 25$ K and size 100 pc. The radio-TeV SED of the extended jet is shown with the blue solid line. The gray line is the total SED of the core, including multi-order synchrotron self-Compton and IC/dust. It is clear that the total SED (maroon solid line) describes the GeV and most of the TeV emission, where the latter arises from IC/CMB and IC/dust in the extended jet.

Doppler de-boosted in the kiloparsec-scale jet frame. Following Stawarz et al. (2003), the observed energy density of the blazar radiation in the frame of the energetic electrons in the kiloparsec-scale jet can then be written as follows (primed coordinates refer to the kiloparsec-scale jet frame):

$$U'_{\text{core}} = \frac{L_{\text{core}}(\theta = 0)}{4\pi z^2c} \left| \frac{1}{4\Gamma_{\text{rel}}^2} \right|_{z=z_{\text{deproj}}},$$

where $L_{\text{core}}$ is the isotropic co-moving blazar luminosity, $z$ is the deprojected distance along the jet from the jet apex, and $\theta$ is the angle between the line of sight of an observer in the kiloparsec-scale jet frame and the blazar radiation. $\Gamma_{\text{rel}}$ is the relativistic bulk Lorentz factor between the jet and the core, $1/\Gamma_{\text{rel}}^2$ converges to 1 when $\Gamma_{\text{core}} \sim \Gamma$, while it deviates to $\ll 1$ when the core and jet speeds are very different. Since it is very unlikely they will have similar speeds, we can safely assume we will have deboosting of the core emission. While Stawarz et al. (2003) consider the blazar core to be stationary in the frame of the kiloparsec-scale jet ($\Gamma_{\text{rel}} = \Gamma$), we have relaxed the assumption here. Using conservative estimates of $\Gamma_{\text{core}} \simeq \delta_{\text{core}}$ and $L_{\text{core}} \simeq 10^{43}$ erg s$^{-1}$ ($\simeq L_{\gamma}$ from the SED) for the blazar core, we can evaluate $L_{\text{core}}(0)$ using Stawarz et al. (2003), $L_{\text{core}}(0) = L_{\text{core}}(2\Gamma_{\text{rel}}/\delta_{\text{core}})^3$, or $L_{\text{core}}(0) = 10^{44}$ erg s$^{-1}$. Therefore, the energy density of the blazar radiation in the frame of the kiloparsec-scale jet is $U'_{\text{core}} = 8.0 \times 10^{-14}/\Gamma_{\text{rel}}^2$ erg cm$^{-3}$.

**Cosmic microwave background.** The CMB is isotropic and it is preferentially boosted in the direction of the fast-moving kiloparsec-scale jet. At a redshift of $z = 0.048$, the CMB energy density is given by (see e.g., Tavecchio et al. 2000; Georganopoulos et al. 2006)

$$U'_{\text{CMB}} = aT_{\text{CMB}}^4 (1+z)^4 \Gamma^2 \simeq 4.8 \times 10^{-13}\Gamma^2\text{ergs cm}^{-3},$$

where $a = 7.53 \times 10^{-26}$ cgs units is the radiation constant and $T_{\text{CMB}} = 2.73$ K is the temperature of the CMB at $z = 0$. Therefore, it directly follows that $U'_{\text{core}}/U'_{\text{CMB}} \simeq 0.1/\Gamma_{\text{rel}}^2$, or the energy density of the nuclear radiation $U'_{\text{core}} \ll U'_{\text{CMB}}$ can be neglected in the frame of the kiloparsec-scale jet. We also do not consider synchrotron radiation from the kiloparsec-scale jet as a dominant source of seed photons since the corresponding energy density is orders of magnitude lower than the CMB.

**Large-scale dust emission (ALMA).** The radiation from a possible (currently undetermined) parsec-scale dusty torus, if present in AP Librae, will have a minimal energy density as it reaches the kiloparsec-scale jet since it will be Doppler de-boosted and hence will lose relevance. Therefore, in this section, we will only consider the “outskirts” of the molecular torus, or the 500 parsec-scale photon field imaged using ALMA and HST.

The minimum temperature blackbody that the ALMA data points describe has a temperature of 25 K and is $\sim 100$ pc in size. Generally, for the case of the parsec-scale torus, the dust photons are preferentially de-boosted in the frame of the kiloparsec-scale jet since they are very far away and hence only illuminate the jet electrons from behind. In this case, however, if one uses the observed size $R \sim 0.65$ kpc from ALMA imaging, one needs to derive the exact energy density as a function of distance along the jet. Simplistically assuming the dusty disk has spherical symmetry for calculating the isotropic luminosity and that the jet is dominantly illuminated by the surface of the disk facing it, we derived the energy density of the kiloparsec-scale dusty disk in the co-moving jet frame in Appendix B. It shows the dependence of the energy density with increase in distance along the jet, from the jet apex. It naturally gives rise to beaming at very low distances compared to the size of the disk and de-beaming at distances $z \gg R$ along the jet.
Large-scale dust emission (HST). This emission is centered at the observing frequency, i.e., $\nu_0 = 10^{14.30} \text{Hz}$ and would constitute a source of a seed photon field for the kiloparsec-scale jet. The width of the F160W filter for WFC3 is $\Delta \lambda \sim 0.4 \mu \text{m}$, which transforms to $\Delta \nu = 10^{13.72} \text{Hz}$. The flux density $F_\nu = 1.27 \text{ mJy}$, which implies the total integrated flux, would simply be given by

$$F = \int_{\nu_0}^{\nu_\infty} F_\nu \Theta(\nu - \nu_0 + \Delta \nu) \Theta(\nu_0 + \Delta \nu - \nu) d\nu = F_\nu (2 \Delta \nu),$$

where $\Theta$ is the Heaviside step function assuming equal transmission through the entire filter. At most, this assumption underestimates the total flux as we are using a monochromatic spectrum. Therefore, the luminosity of the dusty disk at the source would simply be given by $L_\nu = F (4\pi D_L^2)$ where $D_L = 215 \text{ Mpc}$ is the luminosity distance to the source. Using the given values, we obtain $L_\nu \approx 6.0 \times 10^{42} \text{ erg s}^{-1}$. The expression for the energy density due to the infrared-emitting region is the same as in Appendix B. In the upcoming sections, we will discuss this further.

For all our calculations in the Appendix, we use a spherically symmetric assumption for the dusty disk to calculate the isotropic luminosity. Assumption of spherical symmetry of the dusty disk at the deprojected kiloparsec-scale jet is at variance with works that follow better approximations; see, for example, Stalevri et al. (2012), Fritz et al. (2006), and Nenkova et al. (2002) for a discussion on parsec-scale tori emission models and Drouart et al. (2012) for a thorough observational study of parsec-scale torus–jet alignment in radio galaxies. In this case, our ALMA imaging confirms that our dusty disk is very likely being viewed at a low inclination. While the jet may be aligned at a different angle which implies that a part of the disk preferentially illuminates the nearer side of the jet, this mis-alignment between the jet and the disk/jet requires meticulous treatment and is out of the scope of this paper.

3.3.2. Dust Photon Fields in the Frame of the Parsec-scale Core

The parsec and subparsec core/jet receives most of the radiation from the inner part of the dusty disk and can be assumed to be approximately isotropically illuminated for this work. We will find that this assumption will not change our final conclusions.

3.4. Evaluating the IC-dust Model

We here use a simple one-zone homogeneous leptonic model to understand the SED of AP Librae. Our code models both the synchrotron and inverse Compton (IC) emission, where we have also implemented Klein–Nishina effects at higher energies. We consider a region of size $R$ containing a homogeneous magnetic field $B$ moving relativistically with a bulk Lorentz factor $\Gamma$. Radiation from the region is beamed with Doppler factor $\delta$. Electrons with relativistic energies following a power law $Q(\gamma) = N(\gamma)^{-p}$ are injected into the region at timescales much shorter than the light-crossing time. The electron energy distribution $n(\gamma, t)$ is self-consistently evaluated at later times using the Fokker–Planck equation:

$$\frac{\partial n(\gamma, t)}{\partial t} + \frac{n(\gamma, t)}{\tau_{\text{esc}}} = \frac{\partial}{\partial \gamma} \left[ \gamma n(\gamma, t) + Q(\gamma) \right],$$

where $\tau_{\text{esc}}$ is the average time an electron spends in the emission region and the first and second terms on the right-hand side represent cooling and injection, respectively. For our purpose, we use the total energy density of the CMB and the dust (submillimeter and IR) for simultaneous inverse Compton scattering by electrons in the same emission region. Although we use energy densities strictly following the results in Appendix B, we boost the frequency (by $\Gamma$) for simplicity. We will shortly find that this choice is immaterial. The set of parameters of the broad dust spectrum required to produce the VHE emission has been tabulated in Table 5, with $U_{\text{cmb}} = 4.2(1 + z) \times 10^{-13} \text{erg cm}^{-3}$ and $h\nu_{\text{cmb}}/m_e c^2 = (1 + z) \times 10^{-9}$.

The final SED has been shown in Figure 8. The orange data points describe the ALMA and the HST dust fluxes and the orange dashed line represents the 25 K blackbody fit with 100 pc size, as discussed earlier. The gray line is the spectrum of the blazar core and the total (core+jet) SED is given in brown. We find that the total inverse Compton spectrum due to IC/CMB, IC/submillimeter (inverse Compton scattering of submillimeter dust photons) and IC/IR (inverse Compton scattering of IR dust photons), shown by a solid blue line, produces the entire GeV–TeV spectrum. The IC/CMB majorly produces the low-energy end of the VHE spectrum (like Figure 7) while the submillimeter dust photons are IC-scattered to produce the TeV emission. Since we used a very conservative estimate of the luminosity for the infrared photons, the IC spectrum is poorly sensitive to the IC/IR photons. Hence, in the coming sections, we will mainly discuss the submillimeter photon field. However, since we expect the dust emission to be bright through a range in IR frequencies, a complete observation in

| Table 5 | Physical Parameters of the SED Model for the Core and the Extended Jet Emission |
|---------|-------------------------------------------------------------|
| Parameter | Core | Extended Jet |
| $\delta$ (Doppler factor) | 15 | 8.5 |
| $\Gamma$ (Bulk Lorentz factor) | 10 | 5 |
| $\theta$ | 5$^\circ$2 | 4$^\circ$7 |
| $R_{\text{core}}$ (pc) | 0.003 | 13 |
| $t_{\text{m}}$/$R_{\text{core}}$/$c$ | 0.45 | 8.0 |
| $p$ | 1.40 | 2.45 |
| $\gamma_{\text{min}}$ | 10 | 20 |
| $\gamma_{\text{max}}$ | $6.5 \times 10^3$ | $8 \times 10^9$ |
| $B$ (G) | 0.08 | 2.3 $\times 10^{-6}$ |
| $L_\nu$ (erg s$^{-1}$) | $10^{43}$ | 3.65 $\times 10^{44}$ |
| $U_{\text{cmb}}$ (erg cm$^{-3}$) | $4.41 \times 10^{-11}$ | $2.1 \times 10^{-10}$ |
| $U_{\text{dust}}$ (erg cm$^{-3}$) | $1.05 \times 10^{-7}$ | $1.2 \times 10^{-7}$ |
| $U_{\text{obs}}$ (erg cm$^{-3}$) | $2.0 \times 10^{-7}$ | 2.1 $\times 10^{-7}$ |
| $U_{\text{dust}}$ (erg cm$^{-3}$) | $1.6 \times 10^{-9}$ | $1.6 \times 10^{-9}$ |

Note. $R_{\text{core}}$ refers to the size of the emission region and $\nu_0$ is the injected electron power. The energy densities $U$ have additionally been defined in Equation (B3). The parameter $t_{\text{esc}}$ refers to the deprojected distance from the jet apex where external Compton emission is dominant. It has been determined using the corresponding energy density in Figure 9. The corresponding parameters for the core have considerable freedom and the dissipation locations are typically $\lesssim 10$ pc, occurring in the parsec-scale jet, which we have shown in Figure 10 but not in an energy density plot.
the IR may allow us to constrain the VHE better. In addition, the total inverse Compton spectrum clearly underproduces the X-rays by $\sim 30\%$. It is not clear if the X-rays are due to IC/CMB+IC/dust or they are produced due to synchrotron emission in a different emitting zone in the extended jet. In fact, the origin of X-rays in extragalactic jets is a long-debated question (e.g., Harris & Krawczynski 2006; Georganopoulos et al. 2006; Meyer et al. 2015; Breiding et al. 2017) and also remains open in AP Librae. The GeV spectrum is only approximately described by our model. The detection of small flares in the Fermi band over the last decade may indicate some contamination from the core. However, since we are only using an indicative fit to constrain the TeV emission rather than a simultaneous fitting of all data, such discrepancies are considered only minor. It is possible that an additional parsec-scale jet model similar to Hervet et al. (2015) may be better able to fit the observations, although at the cost of significant parameter degeneracies.

Now that the SED model has the energy densities of the seed photon fields required to produce the VHE emission, it is imperative to determine the corresponding distance along the jet where the required submillimeter energy density would hold, allowing us to determine the location of VHE emission using results from Appendix B and check if it is physically feasible. From Figure 9 we find that the dust photons (and the CMB) are inverse Compton scattered to GeV–TeV majorly at $r_{\text{diss}} \sim 740$ pc along the jet, which translates to $\sim 0.07$ kpc in projected scale, at the HST/ALMA resolution limit. In addition, we adopt $\Gamma = 5$ for the jet and we have beamed the frequency of the seed photons. Incorporation of the beaming pattern of the dust from Appendix B would at most reduce it by $(1 - \delta_{\text{diss}}^2/\sqrt{(R^2 + r_{\text{diss}}^2)}) \approx 0.4$, or $\nu_{\text{seed}}$ would effectively be boosted by $\Gamma = 2$ instead of 5, which would reduce the maximum IC-scattered frequency. This discrepancy can be resolved by noting the fact that the peak of the submillimeter blackbody is essentially unconstrained, therefore allowing us to increase the temperature and thereby the frequency of the seed photon field, although that may reduce the fitted size of the disk. Moreover, it is also not clear if there is only one blackbody since we also observe the residual emission in the mid-IR, which implies that the true peak frequency is underestimated. This might result in underestimated of the emitting size (compared to the observed) when a single blackbody is used for the fit, as we saw in Section 3.2. Without filling the gap in the submillimeter to mid-IR observations, none of the above can be constrained and hence, for the broader implications of this work, the assumption of boosting the seed photon frequency is plausible.

In Figure 10 we show an illustration of the structure of the source, the different emission mechanisms, and their locations. It shows a basic cylindrical model of the dusty disk covering a parsec-scale core, aligned perpendicular to the extended jet. The GeV–TeV emitting region is mostly in the projected $< 0.1$ kpc (or deprojected $\lesssim 0.8$ kpc) portion of the jet, as expected from the beaming pattern of the dust seed photons in the frame of the jet. The radio-emitting region is spread through $\sim 0.01$ kpc, corresponding to the size of the emission region, but the fluxes in the radio SED are dominated by different parts of the extended jet. The figure is broadly consistent with the results of our work.

The location of the VHE emitting region in the jet is not unexpected. At a large distance along the jet away from the dusty disk, the seed photons will be Doppler de-boosted, thereby making IC/dust irrelevant. Hence the above estimates of locations $r_{\text{diss}} < 1$ kpc are intuitively expected. However, it is imperative to reconcile these findings with the location of a synchrotron-emitting region. The radio and the X-rays mainly arise from the kiloparsec-scale jet. The same set of electrons that produce the radio synchrotron inverse Compton scatter dust and CMB photons to produce the GeV–TeV emission. Although the projected location along the jet where this dissipation occurs is $r_{\text{diss}} \sin \theta < 0.1$ kpc and is at variance with the observed radio emission location observed using VLA 1.4 GHz, which is in the projected kiloparsec-scale jet, the dominating radio emission region changes observed location with change in frequency. Hence, a subkiloparsec location of emission from radio to TeV using a one-zone emission model is plausible for the broader implications of this work. We do not claim a precise determination of the location of the emission region since it is model-dependent, but we can say the dissipation region must not be $> 1$ kpc away in projected distance from the central engine, or the seed photon energy density would be too low to produce the VHE emission. Accurate determination of the emission location requires other diagnostic tests (e.g., Harvey et al. 2020) and we assume for this work it lies within the 0.1 kpc projected jet and is at the resolution limit for the HST/ALMA. In addition, the size of the emission region from the modeling is $R_{\text{em}} \sim 10$ parsecs. This is consistent with a sphere that fits inside a jet which has a cross sectional dimension $r_{\text{diss}}/\Gamma \approx 150$ pc $> R_{\text{em}}$. Using $\delta = 8.5$ (Table 5), a model-dependent predicted variability timescale would be $r_{\text{var}} \sim 3.5$ yr. Ideally, since the CMB is static, one would not expect a variability signature. However, since we have multiple seed photon fields, variability may be complex. Future monitoring of the extended jet from this source will

Figure 9. The external photon (dust) energy density (in a solid green line) as a function of deprojected distance $z$ along the jet. Using the energy density from the SED model ($U_{\text{diss}}$ in a dashed yellow line), we calculate the $z$ at which the ALMA seed photons are inverse Compton scattered to produce the TeV emission.
allow a strong constraint on the true size of the dominant emission region, if it is variable.

Emission from the blazar core, in contrast, was unperturbed by the presence of the seed photon fields. This is expected because the magnetic energy density is orders of magnitude larger than the maximum seed photon energy densities \((U_\gamma \approx 5 \times 10^{-4} \text{ erg cm}^{-3} > U_{\text{ext}} \approx 10^{-7} \text{ erg cm}^{-3}\), extrapolating \(U_{\text{ext}}\) in Figure 14 to \(\sim 100\) pc, or \(10\) pc in projected scale) and \(\gamma^2 \nu_{\text{thr}} \approx 10^{23} \text{ Hz} \ll \nu_{\text{GeV}} \gtrsim 10^{23} \text{ Hz}\).

With a large-scale dusty structure as observed, it is also imperative to consider \(\gamma - \gamma\) pair production on the dust photon fields as a possible disruption of the \(>\text{GeV}\) radiation within the inner jet. Since even the “highly beamed” jet may encounter this large disk because it is on the \(\sim \text{kpc}\) scale, one cannot rule out the \(\gamma - \gamma\) opacity using relativistic beaming arguments. The threshold energy of the seed photon required for pair production by a \(E_{\text{ext}} = 1\) TeV photon is \(E_{\text{thr}} = 2(m_e c^2)^2[E_{\text{ext}}(1 - \mu)]^{-1} \gtrsim 0.25 \text{ eV}\), or \(\nu_{\text{thr}} = 10^{13.8} \text{ Hz}\) for a head-on collision \(\mu = -1\), which is \(\sim\text{IR}\).

However, the energy density of the observed IR photons is too low to be considered relevant in this case. Even if we conservatively assume the IR photon field is a blackbody spread through the size of the ALMA imaged structure (0.5 kpc), the corresponding “compactness” parameter is \(l \approx U_{\sigma T} R / m_e c^2 \) (\(R\) is the size of the absorption region and \(U\) is the IR energy density; e.g., Roustazadeh & Böttcher 2011; Böttcher & Els 2016), or \(l \approx 2.5 \times 10^{-6} R_{\text{pc}} \ll 1\) using a rough estimate of \(U(z < 50\) pc \(\approx 10^{-6} \text{ erg cm}^{-3}\) from Appendix B. This implies that the large-scale dust is essentially optically thin to the TeV radiation from the parsec-scale core to the kiloparsec-scale jet.

Finally, we note that the \(\sim 10\) TeV emission is underproduced by our model. It is possible the high-energy TeV emission is unphysical and an artifact of inaccurate EBL corrections. However, since we do not have enough multilateral observations, we cannot rule out a high-IR energy density spread through mid- to near-IR, inverse Compton scattering of which may produce the high TeV. Note that Klein–Nishina effects will begin to appear at these seed photon energies.

### 3.5. Jet Energetics and Composition

The question of jet composition, and the total power thus carried, is still not fully settled. A purely leptonic jet contains light electron–positron pairs, as produced purely in a black hole spin-powered jet built in the black hole magnetosphere (Blandford & Znajek 1977), while a purely hadronic jet is produced from the accretion disk and contains electron–proton pairs (Blandford & Payne 1982). In FSRQs, due to the presence of very strong photon fields in the vicinity of the parsec-scale jet, the jet must have a minimum proton content to prevent significant deceleration due to Compton drag on the \(e^- - e^+\) pairs and minimize heavy annihilation signatures which are otherwise not observed. For HBLs, since external photon fields are either not observed due to beaming or are intrinsically weak, the proton content is difficult to constrain (Madejski et al. 2016). However, AP Librae is a low-synchrotron peaking BL Lac (LBL) that has a subkiloparsec-scale dusty disk, suggesting the possibility that it is a so-called “fake” BL Lac (e.g., Keenan et al. 2021) with strong accretion and therefore parsec-scale seed photon fields. Photons from the large-scale dust can be important for both the parsec-scale and the kiloparsec-scale jet. However, none of these can be used to constrain the proton content using present observations so we will dedicate this subsection to making rough estimates of the minimum power demanded by our model and its general plausibility.

The Eddington luminosity for AP Librae is \(L_{\text{edd}} \approx 3 \times 10^{46} \text{ erg s}^{-1}\). The injected electron power (or power in “hot”
electrons), from Table 5, is simply \( P_e = 3.65 \times 10^{44} \text{ erg/s} \). A crude estimate of the radiative power \( P_e \) (which is the power spent by the electrons to produce the observed luminosity), due to the anisotropic nature of inverse Compton scattering, can be obtained from Ghisellini & Tavecchio (2010) as \( P_e \approx 31 \times 10^{43} L_c \approx 10^{46} \text{ erg s}^{-1} \) where \( L_c \approx 10^{42} \text{ erg s}^{-1} \) is a proxy for the total luminosity. \( P_e \) is therefore an observational limit. Additionally, the magnetic field power \( P_B \approx \pi R^2 B^2 U_{\text{B}} \approx 10^{39} \text{ erg s}^{-1} \) \( \ll P_e \), implying the jet is most likely matter dominated. The most important questions, however, are regarding the fraction of the “cold” electrons, number of electron–positron pairs and number of protons per pair. We will employ the simplest approach of power estimates by measuring that for a purely leptonic (pairs only) and for a purely hadronic (e-p) jet. For a hadronic jet, if we assume an acceleration mechanism only energizes a fraction \( \eta_e \) of the electrons, the total power in the leptons would then be \( P_e = P_{\text{cold}} + P_{\text{hot}} = \frac{1}{\gamma_p} P_\gamma + P_e \approx 5.2 \times 10^{44} \text{ erg s}^{-1} \) for \( \eta_e = 10\% \) and \( \langle \gamma \rangle \approx \gamma_{\text{min}} \), where the latter provides an upper bound to the power as ideally \( \langle \gamma \rangle \approx (p - 1)/(p - 2) \gamma_{\text{min}} \) for \( p > 2 \). Therefore, the total jet power in the purely leptonic case would be \( P_e = P_{\text{cold}} + P_{\text{hot}} = \frac{1}{\gamma_p} P_\gamma + P_e \approx 4.1 \times 10^{45} \text{ erg s}^{-1} \) for \( \eta_e \approx 10\% \), or the total jet power \( P_h \approx 4.2 \times 10^{45} \text{ erg s}^{-1} \approx 0.14 \eta_{\text{min}} \). However, in addition to \( \gamma_{\text{min}} \), the above estimates are sensitive to \( \eta_e \) and \( \eta_p \), which are unconstrained in general. For a more conservative estimate of \( \eta_e \approx 1\% \), \( P_\gamma \approx 2 \times 10^{45} \text{ erg s}^{-1} \approx 0.07 \eta_{\text{cold}} \) and \( P_e \approx 5.6 \times 10^{45} \text{ erg s}^{-1} \approx 0.2 P_{\text{cold}} \). The extended jet power must interpolate between \( P_{\text{cold}} \) and \( P_e \) and is sub-Eddington at all times in contrast to the previous literature on AP Librae (Hervet et al. 2015; Petropleou et al. 2017). We also note that the power estimates for the core are likely to be similar to or lower than that for the extended jet since the hot electron power \( L_{\gamma, \text{core}} \approx 10 L_{\gamma, \text{jet}} \), \( \gamma_{\text{min}} \) is half that of the jet, the magnetic power \( P_B \approx \gamma_1 \approx 10^{45} \text{ erg s}^{-1} \) (Table 5), and \( P_{\gamma, \text{core}} \approx \gamma_{\text{min}}^3 L_c \approx 10^{47} \text{ erg s}^{-1} \approx 10 P_{\gamma, \text{jet}} \) (the SSC emission is isotropic in the co-moving frame). Therefore, the total (core+jet) power may at most be double that of the jet and hence will still be sub-Eddington. However, it is not clear to what extent \( \eta_e \) and \( \eta_p \) depend on the type of acceleration and if it will stay the same for a purely leptonic and a purely hadronic jet. For the case of AP Librae, further constraints on the cold particle fraction can be obtained through future studies of faint diffuse emission in the jet, where particles are not energetic enough and bulk Compton signatures may prevail (e.g., see Georganopoulos et al. 2005; Mehta et al. 2009 for the case of PKS 0637-752).

In light of the above discussion, we also note that the maximum apparent speed observed for the parsec-scale jet is \( \beta_{\text{app}} \approx 6 \) (Lister et al. 2019), which implies \( \theta_{\text{max}} \approx 19^\circ \), consistent with Table 5. Assuming the “pattern” speed represents the actual bulk flow, \( \Gamma_{\min} \approx 6 \) for the parsec-scale core, consistent with \( \Gamma_{\gamma} > 10 \Gamma_{\min} \) obtained fromSED modeling. For the larger-scale jet, proper motion studies do not yet exist. However, as ALMA observations suggest, a large gas reservoir must exist within the few kiloparsec of the galactic nucleus and may cause sufficient mass loading (see, e.g., Perucho et al. 2014 and next section) and/or Compton drag (e.g., Sikora et al. 1996) if the jet is light. Hence a deceleration from \( \Gamma_c = 10 \) to \( \Gamma_{\text{jet}} = 5 \) appears reasonable.

**Figure 11.** HST-WFC3 image of AP Librae showing it in an interacting pair of galaxies, confirmation of what was first observed by Stickel et al. (1993) and Pesce et al. (1994). The large object is AP Librae and its host galaxy, while approximately ∼65” to the NE, lies a lenticular galaxy 2MASX J15174385-2421212. The outermost contours of AP Librae show distinct elongation in the direction of the secondary galaxy, suggestive of a tidal interaction.

### 3.6. Possible Origin of the Dust Emission

The maximum extent of a torus such that it is bright in the mid-IR due to AGN-heating and is under the influence of the black hole will be given by \( r < r_{\text{max}} = GM_{\text{BH}}/\sigma^2 \), where \( M_{\text{BH}} \) is the mass of the black hole and \( \sigma^2 \) is the velocity dispersion of stars in the spherical bulge of the galaxy (Alexander & Hickox 2012). Using \( M_{\text{BH}} = 2.5 \times 10^8 M_\odot \) in the classic \( M - \sigma \) relation from Gebhardt et al. (2000), we obtain \( \sigma^2 \approx 240 \text{ km/s} \). This gives us \( r_{\text{max}} \approx 20 \text{ pc} \), which is more than 10 times smaller than the structure detected in our ALMA imaging. This larger-scale dust is cold and clearly outside the influence of the AGN, but may plausibly indicate hot dust on parsec scales (i.e., a classical molecular torus).

The elliptical host of AP Librae has a close companion galaxy, 2MASX J15174385-2421212, located 65” (62 kpc) to the NE and at the same redshift (Pesce et al. 1994). Figure 11 shows the closely interacting pair in our 1.6 \( \mu \)m image, with visible tidal distortions in the outer NE contours/isophotes of the AP Librae host. It is a long-standing claim that AGN activity is a result of major mergers (e.g., Hopkins & Quataert 2010, but see also Lambresides et al. 2021), and this appears to be an even stronger claim for radio-loud AGNs (Chiaberge & Marconi 2011). The environment of radio-loud AGNs has been observed to more likely have a close companion instead of normal gas-rich galaxies (e.g., Ellison et al. 2011; Tadhunter 2016), with FRIs more likely than FRIs to be associated with an interacting pair. The AP Librae host is considerably brighter (by 1.5–2 orders of magnitude) than the companion and is presumably far more massive. This is consistent with the findings of Ellison et al. (2011), where they find in the case of unequal-mass interacting pairs, the highermass primary galaxy is more likely than the lower-mass secondary to host an AGN.
AGN lifetime. For dust in a radio-loud AGN with a relativistic jet. Only a detailed study of the inner torus would reveal vital details regarding the dynamics of outflow/inflow from kiloparsec to parsec scales.

The confirmation of a major interaction triggering AGN activity should be visible in other observations of this system, like evidence of enhanced star formation and molecular inflow. Indeed, detailed photometric observations of AP Librae reveal its host galaxy to be much bluer than average (Baxter et al. 1987) in its nuclear regions (<10 kpc, observed during low AGN activity) and redder at larger radii, in apparent contrast with both typical ellipticals and early-type spirals. Thus, it appears plausible that the subkiloparsec dust (we see in the far and mid-IR) is heated by the nuclear starburst launched by the galaxy interaction rather than the AGN.

It appears that this is the first time a torus or circumnuclear dusty disk has been observed in a BL Lac object, though dusty disks have been observed in several FR I radio galaxies (Sparks et al. 2000). Plotkin et al. (2012), using ~100 WISE-selected weakly beamed BL Lacs, failed to detect the presence of a parsec-scale torus in the entire sample. This may be due to the fact that low-power BL Lacs are poor accretors (e.g., Hardcastle & Croston 2020) and hence dust is poorly heated, in contrast to FSRQs where there has been observational confirmation of dust tori (Castignani & De Zotti 2015). If there is a parsec-scale molecular torus in AP Librae, we also expect a strong accretion signature. An accretion disk “big blue bump” (BBB) is not clearly visible in the SED, though Hervet et al. (2015) and Zacharias & Wagner (2016) assign the apparent flattening of the core spectra in the optical–UV to a BBB. The emission-line spectra of AP Librae (e.g., Disney et al. 1974; Peterson et al. 1976; Rodgers & Peterson 1977) show variable emission-line intensities with equivalent widths \( \lesssim 2 \) A. It is unclear if this reflects a change in the gas supply near the core or if it is simply due to inherent variability in the competing beamed nonthermal radiation.

4. Conclusions

AP Librae is an unusual BL Lac object with a high-energy spectral component spanning 9 decades in energy. As previously noted by Sanchez et al. (2015), Hervet et al. (2015), and Zacharias & Wagner (2016), simple one-zone leptonic SSC models for the blazar core (both first-order and second-order) fail to reproduce any TeV and most of the GeV emission from AP Librae. In this work, we have detected circumnuclear dust of <1 kpc extent around the core of AP Librae, which we find to be a plausible source of seed photons that can be upscattered to higher energies by energetic electrons in the kiloparsec-scale jet. In contrast, based on our improved sampling of the synchrotron-emitting jet spectrum, the VHE emission cannot be produced by a simple kiloparsec-scale IC/CMB model as previously suggested (Zacharias & Wagner 2016). Our preferred explanation for the origin of VHE emission is a combination of inverse Compton scattering of the CMB and dust photons by a single population of electrons in the subkiloparsec jet. The jet power required in this scenario is significantly sub-Eddington, in contrast to most alternative models.

At VHE, a kiloparsec-scale origin could be ruled out if high-amplitude fast variability is detected (e.g., by the Cerenkov Telescope Array). Because of the scale of the resolved jet and the steadiness of the CMB and possibly of the dust on timescales of hundreds of years, the VHE emission resulting from IC processes in the extended jet should be nonvariable. Although a few small-scale flares have been observed with Fermi, it is quite possible that these are due to variability in the core which likely contributes to the flux at GeV energies.

Further clarity on the dynamics of the dust, and thereafter the source of VHE emission from AP Librae would be gained with new, deep IR and submillimeter observations to better constrain the synchrotron emission of the jet (current observations up to ~100 GHz do not probe the peak). It is also unclear if the ALMA-detected dust and the IR-detected residual are intrinsically connected, which can only be verified with deep far and mid-IR observations. Spectroscopic observations with ALMA and JWST will also provide insights into the inflow/outflow dynamics or molecular and ionized gas, which can help us to understand triggering of AGN activity. In principle, deep observations in the far-IR with JWST could strengthen or rule out the extended jet as being the source of the TeV emission.

This paper is based on observations made with the NASA/ESA Hubble Space Telescope obtained from the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS 5-26555. This work was supported by the HST-GO grant No. 15175.

This paper makes use of the following ALMA data: ADS/JAO.ALMA#2017.1.01411.T, 2017.1.00568, 2017.1.00995, 2017.1.00258, 2017.1.01583, 2017.1.00963, 2017.A.00047, 2017.1.00239, 2013.1.00244, 2017.1.01555, 2017.A.00047, 2017.1.00337, 2017.1.00023, 2017.1.01555. ALMA is a partnership of ESO (representing its member states), NSF (USA) and NINS (Japan), together with NRC (Canada), MOST and ASIAA (Taiwan), and KASI (Republic of Korea), in cooperation with the Republic of Chile. The Joint ALMA Observatory is operated by ESO, AUI/NRAO and NAOJ. The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc.

Facility: VLA, ALMA, HST, Chandra, Fermi, H.E.S.S.

Software: CASA (Petry & CASA Development Team 2012), SAO DS9 (Smithsonian Astrophysical Observatory 2000), GIMP (The GIMP Development Team 2019).
Appendix A
ALMA Imaging of the Dust Emission

The suggestion that the dust emission is continuous is not directly clear from or proven in Figure 2. It is a priori unclear if the best source structure is a point source atop a uniform disk or if the disk has a large inner radius. In this section, we demonstrate the validity of the assumptions used in the paper.

Generally in radio interferometry, in cases where the source is not observed long enough or multiple antennas have dropped out, large gaps in $u-v$ coverage can create false symmetric structures (or “side-lobes”), which must then be handled carefully (e.g., ignored during self-calibration). In all of the ALMA data used in the work, the total observing times were $\gtrsim 20$ minutes and the $u-v$ coverage was dense (example visibility amplitude versus $u-v$ distance shown in Figure 12). Even if we assume the symmetric structures are due to only gaps in the $u-v$ coverage (or even amplitude errors), their brightness/strength must follow the brightness of the core. However, from Tables 1 and 5, the radio core spectrum is mainly flat ($\alpha \sim 0.2$) while the brightness of the extended structure increases sharply with frequency following a quasi-blackbody spectrum. This further rules out any false positives regarding association of $u-v$ coverage issues with our detection. Furthermore, amplitude errors can manifest as symmetric structures, but they only follow the radio array pattern and are distinctly different from side-lobes and our detected emission pattern.

The above discussion therefore implies that even if the symmetric structure in our detection is not continuous and does not join with the core, it is still real. However, using a lower gain and number of iterations per clean cycle may allow us to demonstrate or verify the uniformity of emission of the dusty disk. We used a lower gain value of 0.05, which implies that at every step of a minor clean cycle, 5% of the core flux is subtracted from the entire image. Reducing the number of minor cycles per iteration therefore allows more control on the imaging procedure.

Figure 13 shows the core as well as the core-subtracted model residuals of four of the higher frequency ALMA bands using a lower gain. Note that these are residuals, and hence are not byproducts of any “user-dependent” prescription. In all the images, we see a continuous diffuse structure across the location of the core. This demonstrates the uniformity of the disk emission. However, in the 654 GHz image, a “gap” between two symmetric structures may be due to a difference in intrinsic fluxes between the two halves of the dusty disk. A slight oversubtraction of the core was needed to “decouple” it from the disk emission, but that resulted in oversubtraction of the half with a slightly lower flux than the other. In spite of the gap, the core is very close to the brighter half of the disk. Hence this is expected even from a continuous emission. The uncertainties in fluxes are large ($\gtrsim 30\%$, Table 2) and can also be affected by amplitude flux calibration errors $\lesssim 20\%$ at higher frequencies. Hence these differences may be artificial, which can only be constrained by deeper spectroscopic follow-up. Even with a large $\sim 20\%$ error, the $T^4$ temperature dependence results in little effect on $T$. Furthermore, a gap in the disk emission, if it really exists, would increase $r_{in}$ to $\sim 0.5R$ at most. This has no effect on the outcome of the paper since photons from the inner disk are strongly Doppler de-boosted compared to photons from the outer disk, in the co-moving frame of the jet. This has been mentioned in Section 3.2 and Appendix B. Another important consideration in this respect is the significant scatter in the values of the ALMA jet+dust fluxes as in Figure 7. If the dust emission is indeed continuous, the peak flux may be contaminated with flux from the dust.

Figure 12. Visibility amplitude vs. UV radius for the ALMA 232 GHz observation. The $u-v$ plane is visibly well sampled. The amplitude is almost constant, demonstrating that the source is very core-dominated. The scatter is due to antenna gain errors.
emission. Therefore if one simply subtracts the peak flux from the total for obtaining the jet+dust flux, considerable scatter may be expected since the radio core is variable. The only way to remedy all of the above problems perfectly is by using a $u-v$ plane fitting, which likely requires deeper imaging and a specialized analysis, which is out of the scope of this paper.

Given the above, a disk is the simplest model we can choose, and submillimeter photons with energy density anything similar to Equation (B3) can produce the TeV photons, whether or not they are coming from an actual disk.

**Appendix B**

**Calculation of the Energy Density of Dust Photons in the Co-moving Frame of the Extended Jet**

Assuming the dusty disk is stationary, we intend to transform the radiation energy density in the frame of the disk to the co-moving jet frame, which is moving at a bulk speed $\beta$ with respect to the disk. Any variable with primed coordinates shall refer to that in the co-moving jet frame. Therefore the external photon energy density in the jet frame (primed variables) can be written as (see, e.g., Stawarz et al. 2003)

$$U_{\text{ext}}' = \frac{1}{c} \int_{\Omega'} I_{\text{ext}}' d\Omega' = \frac{1}{c} \int_{\Omega} I_{\text{ext}} d\Omega \delta^{-2}$$

$$= \frac{1}{c} \int_{\Omega} I_{\text{ext}} \delta^2 d\Omega,$$

(B1)

where $I_{\text{ext}}$ is the intensity of the seed photon field at distance $z$ along the jet axis ($I_{\text{ext}} = \delta^4 F_{\text{ext}}'/\Omega'$) and $\delta = [\Gamma(1 + \beta \cos(\theta)] = [\Gamma(1 - \beta \cos(\theta'))^{-1}$. We assume $I_{\text{ext}}$ is isotropic in the frame of the dusty disk, arising from a spherically symmetric emission region, which is a simplistic approximation. Therefore, $I_{\text{ext}} = L_{\text{ext}}/4\pi z^2$.

Using the above equation for the dusty disk and a point on the jet axis at distance $z$ from the jet apex, it is straightforward to show that

$$U_{\text{ext}}' = \frac{I_{\text{ext}}}{c} \int_{\pi}^{z} \sin^2(\theta) d\theta \times \int_{\Omega} d\phi,$$

(B2)

where $R$ is the radial extent of the dusty structure defined in the main text. Note we cannot assume $\tan^{-1}(R/z) \approx R/z \ll 1$ since both the disk and the jet extend through kiloparsec scales. Hence we require a rigorous treatment. The complete integral, when expanded without approximations, reads

$$U_{\text{ext}}'(z) = \frac{L_{\text{ext}}}{2cz^2} \left[ (1 - \mu) - \beta(1 - \mu^2) + \frac{\beta^2}{3}(1 - \mu^2) \right],$$

(B3)

where $\mu = 1/\sqrt{R^2/z^2 + 1}$. If we, however, use the small angle approximation by ignoring terms $O(R^3/z^3)$, we obtain an expected result where the radiation is de-boosted in the co-moving jet frame:

$$U_{\text{ext}}'(z) \bigg|_{R/z \ll 1} \approx \frac{L_{\text{ext}}R^2}{4cz^2(1 + \beta)^2},$$

(B4)

In contrast, in the limit of large $R/z$, the expression assumes simple beaming, as intuitively expected. Using $R = 0.65$ kpc, we plot Equation (B3) in Figure 14 for different values of $\Gamma$. 

Figure 13. All the panels from (a) to (d) show the core ALMA images and the core-subtracted model residuals for the frequency bands in Figure 2. The beam size being large, the extended emission (jet+dust) is barely visible in (a) and (b). The core-subtracted images show almost continuous emission in all the observations. The core/peak flux is marked with a white/black cross.
versus $z$, the distance along the jet from the jet apex. It is interesting to note that if the inner radius of the disk is chosen much larger than assumed, for example, $r_{in} \approx 0.5 R$ and if that is included in the above calculation, the resulting energy density is still unchanged since the major contribution is from the $>200$ pc part of the disk.

A major assumption in the above derivation is that of uniform emissivity across the disk in the $x/y$ or the polar radial direction. An approximation is provided by the GALFIT model in Table 3, where the fitted extent of the disk $R$ in the expdisk model essentially represents the e-folding scale for the emissivity $\propto \exp(-r/R)$ where $r$ may represent the distance from the disk center to a shell at a larger distance along the radial direction. Emissivity-weighted seed photon energy density will enhance the brightness of dust regions near the jet while they will reduce that for regions far away from the jet. However, photons from dust regions closer to the jet are more likely to be Doppler de-boosted and vice versa, implying the emissivity weighting will hardly change the energy density we have obtained. Hence, we have omitted this for simplicity.
