Mercury-based cuprates HgBa$_2$CuO$_{4+\delta}$ with $0 < \delta < 0.2$ (Hg1201) are the superconductors with a single CuO$_2$ layer in unit cell and the optimally oxidized one has the highest $T_c = 88$ K among the ever reported single-CuO$_2$-layer superconductors. Double CuO$_2$ layered cuprates HgBa$_2$CaCu$_2$O$_{6+\delta}$ with $0.05 < \delta < 0.35$ (Hg1212) have the highest $T_c = 127$ K at the optimal oxygen concentration. This is the highest $T_c$ among the ever reported double-CuO$_2$-layer superconductors. The Hg1201 has the nearly perfect flat CuO$_2$ plane. The Hg1212 has the flattest CuO$_2$ plane among the other lower $T_c$ double-layer cuprates, which is associated with the mystery of the highest $T_c$. Both systems have a pseudo spin-gap in the magnetic excitation spectrum of the normal states. In this article, we present the microscopic studies of magnetic and electric properties of the Hg-based superconducting cuprates using nuclear magnetic resonance (NMR) and nuclear quadrupole resonance (NQR) techniques. NMR and NQR are powerful to detect local information through the nuclear sites in materials and have supplied us with information on low frequency magnetic response of electronic systems. Although the structure analysis indicates the flat CuO$_2$ planes, zero field $^{63,65}$Cu NQR spectra, which are sensitive to local electric charge distribution, show inhomogeneous broadening. The local electrostatic states are rather inhomogeneous. Although the $d$-wave superconductivity must be fragile to imperfection and non-magnetic impurities, the pure Hg-based superconducting cuprates show impure $^{63,65}$Cu NQR spectra but rather robust pseudo spin-gap in the $^{63}$Cu NMR Knight shift and nuclear-spin-lattice relaxation rate over the wide doping regions. There had been an issue whether the pseudo spin-gap results from a double-layer coupling or a single layer anomaly. The NMR results for Hg1201 served as the evidence for the existence of the single-layer pseudo spin-gap. The pseudo spin-gap is explained by a precursory phenomena of superconducting pairing fluctuations or spin singlet correlation. The different doping dependence of the pseudo spin-gap of Hg1201 and Hg1212 is associated with the different Fermi surface contour. The similar temperature dependence of the $^{199}$Hg and the $^{63}$Cu nuclear spin-lattice relaxation times indicates uniform interlayer coupling. The double-layer coupling effect is revisited through the comparison of Hg1201 and Hg1212.
The superconducting properties except the high-$T_c$ cuprate superconductors has renewed our interests of superconductivity. Low dimensionality on layered compounds, carrier doping effect, electron correlation effect, antiferromagnetic ordering and Mott transition play the key roles to understand the high-$T_c$ physics. Since the high-$T_c$ superconductivity emerges in close to antiferromagnetic instability, the significant role of magnetism is associated with the high-$T_c$ mechanism. Since Coulomb repulsion between electrons can produce spin and charge fluctuations, a close relation between magnetism and superconductivity is suggested. The superconducting properties except the high $T_c$ and vortex matter physics are conventional. The electronic and magnetic properties in the normal conducting state are unconventional. The high-$T_c$ cuprate superconductors have still attracted great interests. We may anticipate new development in understanding the solid state physics.

Mercury-based cuprates HgBa$_2$CuO$_{4+\delta}$ with $0 < \delta < 0.2$ (Hg1201) are the superconductors with a single CuO$_2$ layer in unit cell and the optimally oxidized one has the highest $T_c = 98$ K among the ever reported single-CuO$_2$-layer superconductors \[^{[1, 2]}\]. Mercury-based cuprates HgBa$_2$CaCu$_3$O$_{6+\delta}$ with $0.05 < \delta < 0.35$ (Hg1212) are the superconductors with double CuO$_2$ layers in unit cell and the optimally oxidized one has the highest $T_c = 127$ K among the ever reported double-CuO$_2$-layer superconductors \[^{[3]}\]. Hg1201 and Hg1212 are the layered compounds and contain one and two CuO$_2$ planes in unit cell, respectively \[^{[4]}\]. Triple-CuO$_2$-layer HgBa$_2$Ca$_2$Cu$_3$O$_{8+\delta}$ (Hg1223) is the highest $T_c = 134$ K at ambient pressure \[^{[2]}\] and $T_c = 164$ K at high pressure \[^{[3]}\]. Hg1234 is also known to be synthesized \[^{[6]}\]. But it has lower $T_c$ than Hg1223 \[^{[3]}\].

In this article, we present the Hg-based superconducting cuprates and the microscopic magnetic properties studied through nuclear magnetic resonance (NMR) and nuclear quadrupole resonance (NQR) techniques. Especially, we present the Cu NMR evidence of the existence of a pseudo spin-gap in the norma-state magnetic excitation spectrum of the single-layer cuprate superconductor. The discovery of a big pseudo spin-gap of the underdoped single-layer cuprate superconductor has turn our attention to the unconventional electronic state above $T_c$.

II. PSEUDO SPIN-GAP: SECONDARY OR INHERENT?

Conventional metallic states are well described by the Landau-Fermi liquid theory. Uniform magnetic susceptibility $\chi_s$ exhibits Pauli paramagnetism. Since the density of electron states is finite at the Fermi level, $\chi_s$ is finite at $T = 0$ K and nearly independent of temperature. Nuclear spin-lattice relaxation time $T_1$ satisfies Korringa relation with the spin Knight shift. Since the quasi-particle scattering through the finite density of states induces the nuclear spin relaxation, $1/T_1T$ is finite at $T = 0$ K.

Magnetic itinerant compounds involving the transition metal elements often exhibit Curie-Weiss magnetism, in spite of the absence of localized moments. Itinerant magnetism breaks down the Korringa relation. In antiferromagnetic compounds, the nuclear spin-lattice relaxation rate divided by temperature $1/T_1T$ is enhanced in a Curie-Weiss law, more than the uniform spin susceptibility $\chi_s$.

The normal-state pseudo spin-gap was first confirmed by NMR experiments \[^{[8-10, 11, 12, 13]}\]. The decrease of a static uniform spin susceptibility $\chi_s$ with cooling was observed in the NMR Knight shift measurements for the widely-studied double-layer YBa$_2$Cu$_3$O$_{7-\delta}$. The decrease of the nuclear spin-lattice relaxation rates divided by temperature $1/T_1T$ was also observed for the underdoped cuprates in the normal state. Thus, the existence of a pseudogap in the magnetic excitation spectrum was observed in the underdoped double-layer superconductors in the normal states. However, the existence of such a pseudogap in the magnetic excitation spectrum was not obvious for the single-layer superconductor La$_{2-x}$Sr$_x$CuO$_4$. Then, there had been an issue whether the pseudogap in the magnetic excitation spectrum is intrinsic in a CuO$_2$ plane or it is secondary due to spin singlet formation between adjacent CuO$_2$ planes in the double layer. The NMR studies of Hg1201 gave us an obvious evidence of the pseudo spin-gap in the single layer.

The review articles of the intensive NMR studies of the high-$T_c$ YBa$_2$Cu$_3$O$_{7-\delta}$ can be seen in \[^{[14, 15, 16, 17]}\]. Hence, we focus on the NMR studies of Hg1201 and Hg1212.

III. CRYSTAL STRUCTURE AND PHASE DIAGRAM

A. Record high $T_c$

Figure 1 shows the crystal structures of the Hg-based superconductors Hg1201 and Hg1212 \[^{[4]}\]. Strong covalent O-Hg-O bonds along the $c$-axis, which look like “dumbbell” shape, and dilute oxygen concentration in the HgO$_\delta$ layers are characteristics of the crystal structures. The change in oxygen concentration of the HgO$_\delta$ layers can yield a wide carrier doping region.

Figure 2 (a) shows the oxygen concentration dependences of $T_c$ of Hg1201, Hg1212, and Hg1223 \[^{[8]}\]. The typical “bell”-shaped dependences of $T_c$ are seen for Hg1201 and Hg1212. With changing only the oxygen concentration, the electronic states of Hg1201 and Hg1212 develop from the underdoped to the overdoped regions. Although no magnetic ordering states nor insulating states were confirmed for the deeply underdoped samples of Hg1201 and Hg1212, the existence of Hg-based cuprate insulators was observed for Hg$_2$Ba$_2$YCu$_3$O$_{8-\delta}$ (Hg2212)
which contains the double Hg layers \[19, 20, 21\].

Figure 2 (b) shows \(T_c\) plotted against the in-plane \(a\)-axis lattice parameter for Hg1201, Hg1212, and Hg1223 \[18, 22\]. The in-plane Cu-Cu distances of Hg1212 and Hg1223 are shorter than that of Hg1201. The shrunken CuO2 planes characterize the higher \(T_c\) cuprates.

Figure 2 (c) shows \(T_c\) plotted against the hole concentration \(P_{sh}\) defined by the ionic formal valence of Cu\(^{2+}\).\(^{P_{sh}}\) \[18\]. We estimated \(P_{sh} = 2\delta\) for Hg1201 and \(P_{sh} = \delta\) for Hg1212. The optimal hole concentration is nearly the same as the typical values of 0.18-0.20. Then, the mechanism of the record high \(T_c\) is not only due to the substantial hole concentration.

B. Flat CuO2 plane

Figure 2 illustrates a CuO2 plane and two key structure parameters. The two key parameters are the distance from the plane-site Cu ion to the apical oxygen and the bond angle between the plane-site Cu ions via the plane-site oxygen. Both parameters are associated with the flatness of the CuO2 planes. The large separation between Cu and the apical oxygen and the nearly 180 degree of the in-plane Cu-O-Cu bond angle are observed in Hg1201 and Hg1212 \[23, 24, 25, 26, 27, 28\].

The optimal \(T_c = 38\) K \(La_{2-x}Sr_xCuO_4\) with the single CuO2 layers and the optimal \(T_c = 93\) K \(YBa_2Cu_3O_{6.9}\) with the double CuO2 layers have the buckling structures in the CuO2 planes. The CuO2 planes of Hg1201 and Hg1212 are the flattest among the reported superconducting cuprates \[22, 24, 25, 26, 27, 28\].

Many researchers believe that the nearly perfect flat CuO2 plane is a significant factor to realize the higher \(T_c\). Actually, the double-Hg-layer (Hg, Tl)2212 has the relatively lower \(T_c\) and involves the bucking in the CuO2 planes \[21, 24\]. In the (Hg, Tl)2212, the in-plane Cu-O-Cu bond is bended and the bond angle is about 170 degree. The flatness of the CuO2 planes is associated with a higher \(T_c\) mechanism or at least an inevitable background of crystal structure.

IV. TWO DIMENSIONAL CONDUCTOR

Anisotropy of electrical resistivity has been measured for Hg1201 single crystals \[30\] and Hg1212 epitaxial thin films on vicinal substrates \[31, 32\]. Figure 4 shows the in-plane resistivity \(\rho_{ab}\) and the out-of-plane resistivity \(\rho_{c}\) for Hg1201 single crystal of \(T_c = 97\) K reproduced from \[30\] (a) and those of (Hg, Re)1212 of \(T_c = 117\) K.
reproduced from \[31, 32\] (b).

Dash lines are \(T\) linear functions for the in-plane resistivity \(\rho_{ab}\). The \(T\) linear resistivity is associated with the conduction electron scattering due to two dimensional antiferromagnetic spin fluctuations \[33, 34\]. The deviation from the \(T\)-linear behavior is associated with the scattering suppression due to the opening of a pseudo-spin-gap in the magnetic excitation spectrum. The onset temperatures of deviation from the \(T\) linear functions are denoted by \(T^*\).

At \(T^*\), the out-of-plane resistivity \(\rho_{cc}\) also takes the minimum value. The out-of-plane resistivity \(\rho_{cc}\) is two or three order higher than the in-plane resistivity \(\rho_{ab}\) and the temperature dependence is different from each other. The metallic in-plane resistivity \(\rho_{cc}\) and the semiconducting out-of-resistivity \(\rho_{cc}\) above \(T^*\) is an evidence of two dimensional electrical conduction in Hg1201 and Hg1212. This has been known for the other superconducting cuprates.

The in-plane and the out-of-plane electrical conduction is correlated with each other with respect to the \(T^*\). The two dimensional electrical resistivity is understood in terms of a hot spot and a cold spot on the two dimensional Fermi surface \[34\].

![Diagram of CuO\(_2\) plane and HgB\(_2\)CuCu\(_6\)O\(_{6\delta}\)]

**FIG. 3:** A CuO\(_2\) plane (left) and two key structure parameters (right) are illustrated. The two key structure parameters (right) are the distance from the plane-site Cu to the apical oxygen and the bond angle between the Cu ions via the oxygen ion in the CuO\(_2\) plane. The flatness of the CuO\(_2\) plane is believed to be a significant factor to the higher \(T_c\).

V. CU NQR, NMR AND MAGNETIC FLUCTUATIONS

Nuclear magnetic resonance (NMR) and nuclear quadrupole resonance (NQR) are powerful techniques to characterize microscopically magnetic insulators, metals, superconductors, alloys and compounds \[35\]. Microscopic studies using the NMR and NQR techniques have provided us with rich information inside unit cell through the nuclear sites in a site-selective way. Using the NMR and NQR techniques, one can obtain static and dynamic information of the electronic systems.

A. Inhomogeneous Cu NQR spectrum of pure Hg-based cuprate

\(^{63,65}\)Cu nuclei have spin \(I = 3/2\) and then quadrupole moments \(Q_m\). In a non-cubic crystalline symmetry, they interact with the electric field gradient \(V_{\alpha\beta}\) \((\alpha, \beta = x, y, z)\) of electric static crystalline potential \(V\) \[36\]. Nuclear quadrupole Hamiltonian is given by

\[
H_Q = \frac{\varepsilon^2 q Q_m}{4I(2I-1)}[(3I_z^2 - I^2) + \frac{\eta}{2}(I_+^2 - I_-^2)]
\]

where \(q\) is the maximum component of the electric field gradient

\[
eq \frac{\partial^2 V}{\partial z^2}
\]

and \(\eta\) is called the asymmetry parameter

\[
\eta \equiv \frac{V_{xx} - V_{yy}}{V_{zz}}.
\]

\(^{63,65}\)Cu nuclear quadrupole resonance frequency \(\nu_{NQR}\) is given by

\[
\nu_{NQR} = \nu_Q \sqrt{1 + \frac{\eta^2}{3}}.
\]
where \( \nu_Q = e^2 q Q_m / 2 \). The ratio of the natural abundance of \(^{63}\text{Cu}\) and \(^{65}\text{Cu}\) atoms is about 69.1 to 30.9. The ratio of the nuclear quadrupole moments \( Q_m \) is about 0.211 to 0.195. For one crysallographic Cu site, a pair of single-CuO\(_n\) NQR frequency spectra for various optimally doped panels (a) and double-CuO\(_2\)-layer superconducting cuprates (right panels) (b) at \( T = 4.2 \) K.

![Figure 5: Zero-field plane-site \(^{63,65}\text{Cu}\) NQR frequency spectra for single-CuO\(_2\)_layer superconducting cuprates (left panels) (a) and double-CuO\(_2\)-layer superconducting cuprates (right panels) (b) at \( T = 4.2 \) K.](image)

Non-stoichiometry in compounds gives rise to inhomogeneous broadening in NMR and NQR spectra, because magnetic shift and quadrupole frequency are distributed. YBa\(_2\)Cu\(_4\)O\(_8\) with double CuO\(_2\) planes and double CuO chains in unit cell has \( T_c = 82 \) K. In Fig. 5 this stoichiometric and naturally underdoped compound shows sharp Cu NQR spectra. YBa\(_2\)Cu\(_4\)O\(_6\) with double CuO\(_2\) planes and a single CuO chain in unit cell has \( T_c = 93 \) K. In Fig. 5 this stoichiometric and slightly overdoped compound shows sharp Cu NQR spectra. Although the CuO\(_2\) planes of these compounds have the buckling structures, the Cu NQR spectra are rather sharp.

The superconducting Hg1201 and Hg1212 at any doping level, however, show the inhomogeneously broad Cu NQR spectra \([44, 45, 46]\). In general, crystalline imperfection is the origin of the inhomogeneous broadening of an NQR spectrum. In Fig. 5 Bi\(_{2}\text{Sr}_{1.9}\text{Ca}_{0.9}\text{Cu}_2\text{O}_{8+\delta}\) (Bi2212) also shows a broad Cu NQR spectrum. This is attributed to a wide range structural modulation of the BiO layers. In spite of the dilute oxygen concentration in the HgO layers of Hg1201 and Hg1212, most of the Cu nuclei feel inhomogeneous electric field gradients. Thus, the effect of dilute oxygen ions on the crystalline potential may be long ranged. Long-range Friedel oscillations from the excess oxygen ions may yield such a broad NQR spectrum. The inhomogeneously broad Cu NQR spectrum is observed in the nearly perfect flat CuO\(_2\) plane. This is instructive for us to understand the relation between NQR and the crystal structure. The broad Cu NQR spectrum results from the nonstoichiometry but not from the buckling of the CuO\(_2\) planes.

In Fig. 5 one should note that the value of Cu \( \nu_Q \) of Hg1201 is similar to that of Bi\(_2\)Ba\(_2\)CuO\(_6+\delta\) and about a half of those of YBa\(_2\)Cu\(_4\)O\(_7\) and YBa\(_2\)Cu\(_4\)O\(_8\). The local density approximation calculations of the NQR frequencies account for these experimental similarity and difference \([47]\).

**B. Bulk magnetic susceptibility**

A static magnetic field \( H \) is applied to a material along the \( z \)-axis and then a magnetization \( M_z \) is measured by a magnetometer. The bulk magnetization \( M_z \) is the sum of respective electron spins \( S_{iz} \)

\[
M_z = \sum_i \langle S_{iz} \rangle, \quad (5)
\]

where \( \langle S_{iz} \rangle \) is a thermal average of the electron spin along the \( \alpha \)-axis. Then the bulk magnetic susceptibility \( \chi \) is defined by

\[
\chi = \frac{\sum_i \langle S_{iz} \rangle}{H_{\text{ext}}}. \quad (6)
\]

The paramagnetism of 3d transition metal oxides results from the unpaired \( d \) electron spins and the orbital momentums. The bulk magnetic susceptibility is expressed by the sum of the spin susceptibility \( \chi_{\text{spin}} \), the Van Vleck orbital susceptibility \( \chi_{\text{VV}} \), and the diamagnetic susceptibility \( \chi_{\text{dia}} \) of inner core electrons

\[
\chi = \chi_{\text{spin}}(T) + \chi_{\text{VV}} + \chi_{\text{dia}}. \quad (7)
\]
In the 3d transition metal oxides, the Knight shift $K$ is decomposed into the spin shift $K_s$ due to unpaired electron spins and the orbital shift $K_{orb}$ due to the Van Vleck orbital susceptibility

$$K = K_s(T) + K_{orb}. \tag{10}$$

The spin Knight shift $K_s$ is given by

$$K_s = A(q = 0) \frac{\chi_s'(q = 0, \omega = 0)}{N_A \mu_B} \tag{11}$$

where $A(q = 0)$ is the uniform Fourier component of the hyperfine coupling constant and $\chi_s'(q = 0, \omega = 0)$ is the static ($\omega = 0$) uniform ($q = 0$) electron spin susceptibility. $\mu_B$ is the Bohr magneton. $N_A$ is the Avogadro number. $\chi_{s'}$ is the measured bulk susceptibility in emu/mole-atom.

The hyperfine coupling constant reflects the characters of the wave functions of the electron orbitals. Measurement of the Knight shift at each nuclear enables us to obtain the site-specific information. The temperature dependence of the Knight shift reveals that of the intrinsic uniform spin susceptibility $\chi_{spin}$ at each site.

In covalent bonded compounds, the transferred and supertransferred hyperfine coupling constants play important roles. In the high-$T_c$ cuprate superconductors, the Fourier transformed hyperfine coupling constants at the plane-site Cu and the oxygen are expressed by

$$A^{C_{Cu}}_\alpha(q) = A_\alpha + 2B \{ \cos(q_x) + \cos(q_y) \} \tag{12}$$

and

$$A^{O}_{\alpha}(q) = 2C \cos(q_z/2), \tag{13}$$

where $A_\alpha$ ($\alpha = ab$ and cc) is an on-site anisotropic hyperfine coupling constant, $B(>0)$ is a supertransferred isotropic hyperfine coupling constant from a Cu to a Cu through an oxygen, and $C(>0)$ is a transferred hyperfine coupling constant from a Cu to an oxygen \cite{16, 49}.

For the optimally doped Hg1201, we estimate $A^{C_{Cu}}_{\alpha}(q = 0) = 145$ kOe/mole-Cu-$\mu_B$ from the $K - \chi$ plot, where the Knight shift $K_{ab}$ \cite{48, 49} is plotted against the bulk magnetic susceptibility $\chi$ in Fig. 6 with temperature as an implicit parameter.

## C. Knight shift

Nuclear spins of constituent ions in a crystal interact with electron spins through an electron-nuclear hyperfine coupling. When a static uniform magnetic field $H_{ext}$ is applied to the system along the $z$-axis, the electron medium is polarized along the $z$-axis. The magnetic polarization produces an additional magnetic field at the nuclear sites through the hyperfine coupling and then leads to a shift of the resonance field (frequency) of the nuclear spins. This is Knight shift $K$.

The static nuclear spin Hamiltonian of a Zeeman coupling and the electron-nuclear hyperfine coupling is given by

$$H_{int} = -\gamma_n I \cdot \sum_i (H_{ext} + A_{iz} \langle S_{iz} \rangle) \tag{8}$$

where $\gamma_n$ is the nuclear gyromagnetic ratio and $A_{iz}$ is a hyperfine coupling constant along the $z$-axis with the $i$-site electron spin.

The experimental Knight shift is defined by a shift of the observed resonance frequency $\omega_{res}$ from the reference frequency $\omega_{ref}$

$$\omega_{res} = \gamma_n H_{ext}(1 + K) = \omega_{ref}(1 + K). \tag{9}$$

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## D. Nuclear spin-lattice relaxation

Nuclear spins are coupled by the fluctuating hyperfine fields of electron spins through a time-dependent hyperfine coupling Hamiltonian

$$H_{int}(t) = \frac{1}{2} \sum_i (I \cdot A_i \delta S_{i-}(t) + I_+ A_i \delta S_{i-}(t)). \tag{14}$$

In a spin-echo recovery technique, the nuclear moments excited by inversion $rf$-pulse are in a thermal nonequilibrium state. The energy dissipation from the nuclear moments to a lattice takes place through the fluctuating hyperfine fields. The recovery time of the nuclear
moments to a thermal equilibrium state is the nuclear spin-lattice relaxation time \( T_1 \).

Moriya derived a general expression of \( T_1 \) [51],
\[
\frac{1}{T_1} = \frac{\gamma^2}{2} \sum_i A_i^2 \int_{-\infty}^{\infty} (\{\delta S_i+(t)\delta S_i-(0)\}) e^{-i\omega_n t} dt
\]
\[
= \frac{2\gamma^2}{g^2\mu_B^2} \sum_i \int d^D q A(q)^2 \chi_{\text{ab}}''(q,\omega_n). \tag{15}
\]

\( D \) is the dimension of space on which the electronic system lies. \( 1/T_1T \) is the square of the hyperfine coupling constant \( A(q)^2 \) times the wave vector averaged low frequency dynamical spin susceptibility \( \chi''(q,\omega) \) [59]. Thus, from measurements of the Knight shift and the nuclear spin-lattice relaxation time, one can infer the \( \delta \) dependence of the dynamical spin susceptibility \( \chi''(q,\omega) \). The modified Korringa ratio can give us a criterion which the electronic system is, ferromagnetic or antiferromagnetic and where \( \chi''(q,\omega) \) is enhanced in the \( q \) space.

In general, the \( q \) dependence of the hyperfine coupling constant \( A(q) \) is slower than that of \( \chi(q) \). But, the form factor of the plane-site oxygen \( A_{O}^2(q)^2 \) of Eq. (13) acts as a filter for a finite \( q \) correlation. The antiferromagnetic correlation of \( Q = [\pi, \pi] \) and \( Q^* = [\pi(1+\delta), \pi(1+\delta)] \) is cancelled at the plane-site oxygen through the form factor of Eq. (13). The plane-site Cu nuclei can probe the antiferromagnetic correlation through Eq. (12).

### E. Gaussian Cu nuclear spin-spin relaxation

Strong indirect Cu nuclear spin-spin interaction was first found in \( \text{YBa}_2\text{Cu}_3\text{O}_7 \) [51, 52]. Gaussian decay in the transverse relaxation of the plane-site Cu nuclear moments is predominantly induced by the indirect nuclear spin-spin interaction through the in-plane antiferromagnetic electron spin susceptibility. Strong antiferromagnetic fluctuations persist in all the high-\( T_c \) cuprate superconductors. Thus, the Gaussian decay rate of the plane-site Cu nuclear spin-spin relaxation provides us fruitful information on the antiferromagnetic electron spin susceptibility [53, 54].

The indirect nuclear spin-spin interaction is given by
\[
H_{II} = \sum_{i,j} \Phi(r_{ij}) I_j \cdot I_j \tag{16}
\]

where a range function \( \Phi(r_{ij}) \) is given by
\[
\Phi(r_{ij}) = \int d^D q A(q)^2 \chi(q). \tag{17}
\]

The Gaussian decay rate \( 1/T_{2g} \) of the nuclear spin-spin relaxation is given by
\[
\left( \frac{1}{T_{2g}} \right)^2 \propto \sum_j \Phi(r_{ij})^2
\]
\[
\approx \int d^D q A(q)^4 \chi'(q)^2. \tag{18}
\]

The Kramers-Kronig relation is
\[
\chi'(q) = \frac{2}{\pi} \int_0^\infty d\omega \frac{\chi''(q,\omega)}{\omega}. \tag{19}
\]

The Gaussian decay rate \( 1/T_{2g} \) reflects the full range frequency integration of the dynamical spin susceptibility \( \chi''(q,\omega) \).

The cross section of inelastic neutron scattering is expressed by
\[
\frac{\partial^2 \sigma}{\partial \Omega \partial q} \propto \frac{1}{1-e^{-\beta \omega}} \chi''(q,\omega), \tag{20}
\]
where \( q \) is a momentum transfer of the neutron, \( \omega \) the energy transfer, and \( \beta = 1/k_BT \) [58]. In the high-\( T_c \) cuprate superconductors, the enhancement of \( \chi''(q,\omega) \) was observed over a finite range of \( \omega \) and at around \( q = Q \) or \( Q^* \) [59]. In general, it is hard to see \( \chi''(q,\omega) \) over the full range.

From measurements of the nuclear spin-lattice relaxation and the Gaussian decay rate of nuclear spin-spin relaxation, one can infer the dynamical spin susceptibility at low and high frequency regions.

### F. Two dimensional nearly antiferromagnetic spin fluctuation model

The electronic state of a \( \text{CuO}_2 \) plane of the high-\( T_c \) cuprate superconductor is described by a single band picture. The anisotropy of Knight shift and nuclear spin-lattice relaxation and the site differentiations are explained by anisotropic hyperfine coupling and different \( q \) dependence of the coupling constant due to transferred and supertransferred hyperfine couplings. That is Mila-Rice-Shastry hyperfine coupling Hamiltonian [60, 61]. Two dimensional antiferromagnetic spin fluctuations through the Mila-Rice-Shastry hyperfine coupling yield the anisotropy and the site difference [13, 62, 63]. The two dimensional spin fluctuation models were successfully applied to account for NMR, neutron scattering and conductivity results [33, 64, 65].

We employ the two dimensional nearly antiferromagnetic spin fluctuation model in [33]. The dynamical spin susceptibility is expressed by a relaxation mode
\[
\chi(q,\omega) = \frac{\chi(q)}{1-i\omega/\Gamma(q)}. \tag{21}
\]

The leading terms of \( \chi(q) \) and \( \Gamma(q) \) in a random phase approximation (RPA) are expressed using a long wave length expansion around a specific mode \( q = Q \) by
\[
\chi(q) \approx \frac{\chi_0(Q)}{\kappa^2 + (q-Q)^2} \tag{22}
\]
and
\[
\Gamma(q) \approx \Gamma_0(Q)/(\kappa^2 + (q-Q)^2). \tag{23}
\]
\( \kappa \) is the inverse of a magnetic correlation length \( \xi \) defined around \( q = Q \),

\[
\xi^2 = -\frac{1}{\chi(Q)} \frac{\partial^2 \chi(q)}{\partial q^2} \bigg|_{q=Q}.
\]

\( \chi_0(Q) \) is the spin fluctuation amplitude at \( q = Q \) and \( \Gamma_0(Q) \) is the characteristic spin fluctuation energy. The staggered spin susceptibility \( \chi(Q) \) is then

\[
\chi(Q) = \chi_0(Q) \xi^2. \tag{25}
\]

We obtain the plane-site Cu nuclear spin-lattice relaxation rate expressed by the leading term of \( \xi \)

\[
\frac{1}{T_1 T} \approx A(Q)^2 \int d^D q \frac{\chi(q)}{\Gamma(q)}
\]

\[
\approx \chi_0(Q) \frac{\Gamma_0(Q)}{\xi q} \int \frac{d^D q}{\{ \xi^2 + (q - Q)^2 \}^2}
\]

\[
\propto \xi^4-D \chi_0(Q) \frac{\Gamma_0(Q)}{\xi q} \int \frac{d^D q}{\{ 1 + (\xi q)^2 \}^2}
\]

\[
\propto \xi^{4-D} \chi(Q)^2 \propto \chi(Q)^2-D/2, \tag{26}
\]

where \( q_B \) is the spherical radius of the same volume as the first Brillouin zone and \( \xi q_B \gg 1 \). We also obtain the Gaussian Cu nuclear spin-spin relaxation rate expressed by the leading term of \( \xi \)

\[
\left( \frac{1}{T_2 g} \right)^2 \approx A(Q)^4 \int d^D q \chi(q)^2
\]

\[
\propto \chi_0(Q)^2 \frac{\Gamma_0(Q)}{\xi q^2} \int \frac{d^D q}{\{ \xi^2 + (q - Q)^2 \}^2}
\]

\[
\propto \xi^{4-D} \chi_0(Q)^2 \frac{\Gamma_0(Q)}{\xi q^2} \int \frac{d^D q}{\{ 1 + (\xi q)^2 \}^2}
\]

\[
\propto \xi^{4-D} \chi(Q)^2-D/2. \tag{27}
\]

Thus, for \( D = 2 \) we have

\[
\frac{T_1 T}{T_2 g} \propto \Gamma_0(Q) \xi^{-1}, \tag{28}
\]

and

\[
\frac{T_1 T}{T_2 g} \propto \Gamma_0(Q) \chi_0(Q). \tag{29}
\]

In the self-consistent renormalization (SCR) theory for two dimensional antiferromagnetic spin fluctuations, the Curie-Weiss behavior of the square of the antiferromagnetic correlation length \( \xi^2 \) (\( \propto \) the staggered spin susceptibility \( \chi(Q) \)) is reproduced as a function of the distance from the quantum critical point and the spin fluctuation energy \( \Gamma_0(Q) \). Using \( \chi_0(Q) = 1/2 \alpha_s T_A \) (\( \alpha = U \chi_0(Q) \)), \( \Gamma_0(Q) = 2 \pi T_0 \) and \( t = T/T_0 \), we obtain

\[
\frac{T_1 T}{T_2 g} \propto T_0 \xi(t)^{-1}, \tag{30}
\]

which represents the inverse of the antiferromagnetic correlation length with a unique parameter \( T_0 \), and

\[
\frac{T_1 T}{T_2 g} \propto \frac{T_0}{T_A}, \tag{31}
\]

which represents the integrated spin fluctuation weight. Using Eqs. (30) and (31), the NMR relaxation data for \( \text{Tl}_2\text{Ba}_2\text{CuO}_6 \text{Cu}_{0.1} \), \( \text{YBa}_2\text{Cu}_2\text{O}_7 \), and \( \text{YBa}_2\text{Cu}_4\text{O}_8 \) were analyzed.

VI. NORMAL-STATE PSEUDO SPIN-GAP

A. Single-layer pseudo spin-gap: Hg1201

The left panels of Fig. 7 show \( ^{63}\text{Cu} \) NMR results of the underdoped Hg1201 of \( T_c = 50 \) K. The NMR experiments were performed for the powdered polycrys-
talline sample. All the powder samples were magnetically aligned along the c axis. In general the mercury compounds cannot be easily aligned by a magnetic field. Then, the NMR experiments were performed for partially oriented powder samples. This does not indicate that the NMR data are the partially powder-averaged ones. The sharply aligned NMR lines can be separated in the powder pattern, so that the selected signals surely come from the aligned grains.

The plane-site $^{63}$Cu Knight shift $K_{ab}$, nuclear spin-lattice relaxation rate $(1/T_1T)_{cc}$, and Gaussian nuclear spin-echo decay rate $(1/T_{2g})_{cc}$ are shown as functions of temperature. Temperature dependences of the plane-site $^{63}$Cu Knight shifts $K_{ab}$ (top panels), nuclear spin-lattice relaxation rates $(1/T_1T)_{cc}$ (middle panels), and Gaussian decay rates $(1/T_{2g})_{cc}$ of nuclear spin-spin relaxation (bottom panels) are shown for the underdoped (left), the optimally doped (center) and the overdoped samples (right). Dash lines denote the respective $T_c$'s. The data are reproduced from [41].

**B. Double-layer pseudo spin-gap: Hg1212**

The middle panels of Fig. 8 show $^{63}$Cu NMR results of the optimally doped Hg1212 of $T_c = 127$ K [41], which is the maximum $T_c$ among the ever reported single and double layers. The plane-site $^{63}$Cu Knight shift $K_{ab}$, nuclear spin-lattice relaxation rate $(1/T_1T)_{cc}$, and Gaussian nuclear spin-echo decay rate $1/T_{2g}$ are shown as functions of temperature. The decrease of the $^{63}$Cu Knight shift $K_{ab}$ with cooling down is obvious even at the optimal Hg1212. Above $T_s = 200$ K, $1/T_1T$ shows a Curie-Weiss behavior, because of the development of the antiferromagnetic correlation length. The decrease of $1/\chi(T)$ starts below $T_s = 200$ K. This $T_s = 200$ K of Hg1212 is larger than $T_c = 140$ K of the optimally doped Bi2212 with $T_c = 86$ K in [74]. The record optimal $T_c$ of Bi2212 is about 96 K [72]. For the double layer systems of Hg1212 and Bi2212, the ratio ($\sim 1.4$) of the optimal $T_s$'s is nearly the same as that of $T_c$. The slight decrease of $1/T_{2g}$ is also seen, because of the large pseudo spin-gap effect on the
frequency integrated \( \chi(q, \omega) \). The finite \( 1/T_{2g} \) below \( T_c \) indicates the \( d_{x^2-y^2} \) wave pairing symmetry [70, 71, 72].

Figure 5 shows the hole doping dependence of \( ^{63}\text{Cu} \) NMR results of Hg1212 [41]. Temperature dependences of the plane-site \( ^{63}\text{Cu} \) Knight shifts \( K_{ab} \) (top panels), nuclear spin-lattice relaxation rates \( (1/T_1)_{cc} \) (middle panels), and Gaussian decay rates \( (1/T_{2g})_{cc} \) of nuclear spin-relaxation (bottom panels) are shown for the underdoped (left), the optimally doped (center) and the overdoped samples (right). The pseudo spin-gap temperature \( T_s \) decreases from the underdoped to the overdoped samples. The values of \( T_s \) of Hg1212 are higher than those of Bi2212 [74]. The temperature region of the Curie-Weiss behavior in \( (1/T_1)_{cc} \) above \( T_s \) is broadened with the hole doping. It should be noted that the overdoped sample shows the Curie-Weiss behavior in \( (1/T_1)_{cc} \) but not Korringa behavior above \( T_s \) [42].

C. Interlayer coupling via Hg NMR

The Hg site is located just halfway between the CuO\(_2\) planes and between the respective Cu ions. The Hg nuclei can serve as a probe of the interplane coupling. If the interplane coupling is antiferromagnetic, the in-plane antiferromagnetic correlation is also cancelled out at the Hg site. If the interplane coupling is uniform and ferromagnetic, the in-plane antiferromagnetic correlation is also seen at the Hg site.

Figure 9 shows \(^{63}\text{Cu} \) and \(^{199}\text{Hg} \) nuclear spin-lattice relaxation rates \( 1/T_1 T \) for the optimally doped Hg1201 (a) and for the overdoped Hg1201 (b) [57]. Temperature dependence of \(^{199}(1/T_1 T)\) is nearly the same as that of \(^{63}(1/T_1 T)\), for both samples.

D. Pseudo spin-gap phase diagram

Figure 10 shows the magnetic phase diagrams of Hg1201(a) and Hg1212 [37, 41, 73]. Pseudo spin-gap temperatures \( T_s \) and superconducting transition temperatures \( T_c \) are plotted against the hole concentration \( P_{sh} \) per plane-site Cu. The value \( P_{sh} \) of Cu\(^{2+}\) is estimated from the excess oxygen concentration \( \delta \) and the charge neutrality condition. Solid and dash curves are guides to the eyes.

The hatched region of the overdoped Hg1201 indicates a pseudo Korringa behavior below \( T_s \) [42]. It should be noted that the pseudo spin-gap persists at the optimally doped regions for Hg1201 and H1212. The doping dependence of \( T_s \) of Hg1212 is different from that of Hg1201 even in the underdoped region. The \( T_s \) as a function of \( P_{sh} \) does
not seem to be universal.

We present two theoretical explanations for the doping dependence of $T_c$. In the two dimensional $t$-$J$ model with spinon-holon decomposition technique, the pseudo spin-gap temperature $T_{RGVB}$ is regarded as the onset temperature of a spin singlet RVB (resonating valence bond) state \cite{73, 80, 81}. The real transition temperature $T_c$ is given by a Bose-Einstein condensation temperature $T_{BEC}$ of holons, leading to the underdoped regime. With an existing approximation, $T_{RGVB}$ is a second order phase transition temperature. Figure 11 (a) shows a numerical $T_{RGVB}$ as a function of doped hole concentration \cite{81}. The doping dependence of $T_{RGVB}$ depends on the contour of a basal Fermi surface. For each high-$T_c$ family with different Fermi surface, $T_{RGVB}$ exhibits the different doping dependence.

In the two dimensional superconducting fluctuation theory with the strong coupling, the pseudo spin-gap temperature $T_s$ is regarded as the onset of enhancement of $d_{x^2-y^2}$-wave superconducting fluctuations and a mean-field $T_c$. The actual $T_c$ is reduced by the strong superconducting fluctuations so that the underdoped regime appears. Thus, the mean-field $T_c$ is a crossover temperature. Figure 11 (b) shows the mean-field $T^{MF}_c$ and the suppressed $T_{c}^{MF}$. The doping dependence of $T^{MF}_c$ depends on the shape of the Fermi surface.

From the above two theories, one may conclude that the difference in the hole doping dependence of $T_c$ of Hg1201 from Hg1212 can be attributed to the different shape in the basal Fermi surface of Hg1201 and Hg1212.

The band structure calculations have been performed by the full potential linear muffin-tin orbital method for Hg1201, Hg1212 and Hg1223 \cite{82}. The band calculations indicate the different electronic structures and Fermi surfaces between Hg1201 and the others \cite{82}. The Fermi surface of a single crystal Hg1201 was observed by angle-resolved photoemission measurement \cite{82}.

VII. SPIN FLUCTUATION SPECTRUM

A. Scaling

The ratios of $T_1 T$ and $T_{2g}$ tell us the spin fluctuation parameters through Eqs. (28), (29), (30) and (31). In Figs. 12 and 13 $T_1 T / T_{2g}$ (a) and $T_1 T / (T_{2g})^2$ (b) for Hg1201 and Hg1212 are plotted against temperatures from the underdoped to the overdoped samples \cite{36, 37, 41, 73}. The pseudo scaling of $T_1 T / T_{2g} = \text{constant}$ is observed in the limited temperature region for Hg1212. The pseudo scaling temperature region
underdoped T hole doping [84], that is inconsistent with the experimental energy 

tation energy 

doped samples. In the overdoped regime, the decrease of 

The decrease of the spin fluctuation amplitude and the spin fluctuation 

t holds. The value of \( \xi \) decreases from the underdoped to the overdoped regimes of Hg1201 and Hg1212.

Equation (28) indicates that \( T_1T/T_{2g} \) is proportional to the inverse of the antiferromagnetic correlation length \( \xi \) and has a unique scale parameter \( T_0 \). In Figs. 12 and 13 \( T_1T/T_{2g} \) decreases from the underdoped to the overdoped samples of Hg1201 and Hg1212. This is inconsistent with the theoretical doping dependence of the magnetic correlation length near the two dimensional quantum critical point. The \( \xi^{-1} \) in the SCR theory increases from the weakly antiferromagnetic to the nearly antiferromagnetic regimes and away from the quantum critical point [33]. The decrease of \( T_1T/T_{2g} \) suggests the decrease of the spin fluctuation energy \( T_0 \) from the underdoped to the overdoped samples. In the overdoped regime, the decrease of \( T_c \) can be associated with the decrease of the spin fluctuation energy \( T_0 \).

In the RPA for the two dimensional t-J model, both \( T_1T/T_{2g} \) (a) and \( T_1T/(T_{2g})^2 \) (b) depend on temperature more or less [84]. The value of \( T_1T/T_{2g} \) increases with the hole doping [84], that is inconsistent with the experimen-
tal doping dependence. But the decreases of \( T_1T/(T_{2g})^2 \) with doping is reproduced within the RPA calculations.

In the numerical calculations for the small size t-J model using the Lanczos diagonalization method, the doping dependence of \( T_1T/T_{2g} \) below \( T = 1390 \) K agrees with the experimental tendency. Above \( T = 2320 \) K, the doping dependence of \( T_1T/T_{2g} \) above \( T = 2320 \) K reproduces those of the SCR and the RPA calculations [85].

**B. Spin fluctuation parameters**

Within the framework of Eliashberg-Nambu strong coupling superconductivity theory, the actual \( T_c \) is determined by competition between the pairing effect and the depairing effect [84, 87, 88]. In the spin-fluctuation-mediated superconductors, the depairing effect due to low frequency spin fluctuations competes the paring effect due to high frequency ones. For the \( d_{x^2-y^2} \) superconductivity on a square lattice, the numerical calculation and theoretical consideration tell us that \( T_c \) is proportional to the characteristic energy scale of antiferromagnetic spin fluctuations [80],

\[
T_c \propto T_0.
\]  

(32)

The spin-fluctuation-induced superconductivity theories are studied for the two and three dimensional Hubbard models [90, 91]. As a general tendency, two dimensional systems have higher \( T_c \) than three dimensional ones [89, 92, 93]. Then, the mystery of the high \( T_c \) of the layered compounds is traced back to the two dimensionality and the large scale of the antiferromagnetic spin fluctuation energy.
Figure 14 shows \( T_c \) plotted against \( T_1 T/(T_2 g)^2 \) of Hg1201, Hg1212, and TI2212 reproduced from [94]. If one assumes \( T_1 T/(T_2 g)^2 \sim T_0 / T_A \) of Eq. (29), the linear relation between \( T_c \) and the spin fluctuation energy does not seem to hold. The spin fluctuation product \( \chi(Q) \Gamma(Q) \) decreases monotonically with the hole doping as in Figs. [12] and [13]. This has been recognized in the other systems [52]. Thus, \( T_1 T/(T_2 g)^2 \) is a monotonic function of the doped hole concentration and then the indicator. At some threshold value of \( T_1 T/(T_2 g)^2 \) in the overdoped regime, \( T_c \) starts to increase toward the optimally doping level. Beyond the optimally doping level, \( T_c \) decreases and \( T_s \) increases as the hole concentration is reduced. The antiferromagnetic spin fluctuation spectrum is different between the underdoped and the overdoped samples. Thus, the overdoped part of the \( T_s \)-vs-\( T_1 T/(T_2 g)^2 \) curves indicates some correlation between \( T_c \) and the spin fluctuation parameters, but the underdoped part indicates the suppression of \( T_c \) due to the grown of the large pseudo spin-gap.

C. Double-layer coupling: revisited

From the fact that the uniform spin susceptibility \( \chi_s \) is suppressed at low temperatures in YBa\(_2\)Cu\(_3\)O\(_{6.6}\) and YBa\(_2\)Cu\(_4\)O\(_8\) more than La\(_2\)-\( x \)Sr\(_x\)CuO\(_4\), the bilayer (double-layer) coupling effect had been proposed to be the primary origin of the pseudo spin-gap [95, 96, 97, 98]. The double-layer exchange scattering effect was proposed to account for the different behavior of \( 1/T_1 T \) and \( 1/T_2 g \) below \( T_s \) [99, 100]. Now the single CuO\(_2\) layer Hg1201 is found to possess the pseudo spin-gap in the low-lying excitation spectrum. However, the existence of the double-layer coupling was actually confirmed by the neutron scattering [59] and NMR [101] experiments for low doped YBa\(_2\)Cu\(_3\)O\(_{6.6}\). Spin-echo double resonance techniques have been applied to estimate the double-layer coupling constant in Y\(_2\)Ba\(_4\)Cu\(_7\)O\(_{15-\delta}\) [102, 103] and in Bi\(_2\)Sr\(_2\)Ca\(_2\)Cu\(_3\)O\(_{10}\) [104]. The angle dependence of the Gaussian decay rate \( 1/T_2 g \) was measured to estimate the like-spin interlayer coupling for Hg1223 [105].

Figure 15 shows \( K_{ab} \), \( (1/T_1 T)_{cc} \), and \( (1/T_2 g)_{cc} \) for Hg1201 (black symbols) and Hg1212 (red symbols) from Figs. 7 and 8 to compare two systems [36, 57, 41, 73]. The NMR results of Hg1212 is quantitatively different from those of Hg1201.

As to the underdoped Hg1201 and Hg1212 samples, \( (1/T_1 T)_{cc} \) of Hg1201 is nearly the same as that of Hg1212 but the \( T_c \) is about twice higher than Hg1212. The different point is the underdoped \( (1/T_2 g)_{cc} \) of Hg1212 higher than that of Hg1201. Thus, not the low frequency spin fluctuations but the high frequency ones contribute the higher \( T_c \).

As to the optimally doped Hg1201 and Hg1212 samples, the spin part of the Cu Knight shift of Hg1212 and \( (1/T_1 T)_{cc} \) are smaller than those of Hg1201, whereas the \( (1/T_2 g)_{cc} \) is higher than that of Hg1201. The electron spin-spin correlation function \( \chi_{\text{inter}} \) due to the double-layer coupling is competitive in the in-plane correlation function \( \chi_{\text{intra}} \) of \( K_{ab} \) and \( (1/T_1 T)_{cc} \) but is additive in \( (1/T_2 g)_{cc} \) [100]. Although the double-layer coupling is not a primary origin of the pseudo spin-gap, it surely affects the microscopic magnetic properties.

VIII. CONCLUSION

The flat CuO\(_2\) plane and the large pseudo spin-gap are the characteristics of the mercury-based high-\( T_c \) superconducting cuprates Hg1201 and Hg1212. The role of the pseudo spin-gap in the higher \( T_c \) is still unclear. Is the pseudo spin-gap a consequence of the enhanced superconducting fluctuations to suppress the mean field \( T_c^{MF} \) ? Then, we should explore the layered compounds with higher energy spin fluctuations and any method to suppress the superconducting fluctuations to get higher \( T_c \).
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