State Feedback Control Based Networked Control System Design with Differential Evolution Algorithm

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Abstract This paper will propose the state feedback control based networked control system (NCS) design with the differential evolution algorithm. For designing a networked control system, one has to overcome the problems about the random latency and the data packet dropouts. Here, we will apply the state feedback control theory to design a controller to overcome the random latency and the data packet dropouts of NCS and guarantee the stability of the overall system. To improve the control performance, the differential evolution algorithm (DE) is applied to search the optimal control parameters. In this way, one can design NCS more effectively and without need to solve a complex Lyapunov-Krasovskii stability criterion. Finally, computer simulations are given to demonstrate the proposed control strategy and to illustrate its effectiveness.

Keywords Networked Control System, Differential Evolution Algorithm, Packet Dropouts, Time Delay, State Feedback Control

1. Introduction

The Internet of Things (IoT), the important technology of industry 4.0 [1-3], is emerging as the next technology mega-trend. Lots of researchers and research organization make studies about IoT [4-7]. An important issue of IoT is the networked control systems (NCSs) design [8-15], which is a spatially distributed system for which the connection between sensors, actuators, and controllers is supported by share communication networks. In NCS, data are transmitted in an atomic unit called data packets. It means that the system states and the output signals are sampled by the sensors and transmitted to the controllers by the data packets, and the controller signals are transmitted to the actuators by the data packets, and the actuators would control the controlled plants according to the receiving data packets.

Due to the introduction of the share communication network, two major challenges in NCSs still to be fully addressed are the effects of both “latency (caused by propagation, transmission, router, processing, computer … etc.)” and “packet dropout (caused by network congestion, multi-path fading, faulty network drivers… etc.)” on the system performance [14]. To treat the mentioned effects, several methods have been proposed. Seiler et al. adopted the $H_\infty$ control theory to stabilize NCS and analyzed the system robustness [9, 13]. Huang and Nguang applied the state feedback controller to treat the control problem of NCS [10]. Peng et al. applied T-S fuzzy control technique to guarantee the stability of NCS [11, 13]. Sahoo and Jagannathan applied stochastic control theory and event-driven technique to optimize the NCS design [15].

From the above-mentioned method, we can find out that designing NCS, one usually analyzes the stability of NCS based on Lyapunov stability theorem and solve the Lyapunov-Krasovskii stability criterion to obtain the control gain matrix [9-11, 14]. But, generally, the Lyapunov-Krasovskii stability criterion is difficultly calculated. So that, this paper adopted the differential evolution (DE [16-18]) is applied to search the optimal control gain matrix effectively.

Since in 1995 Storn and Price proposed the differential evolution (DE, [16]), which has attracted a lot of research interests. The advantage of DE is that their convergence rate is faster than many other acclaimed global optimization methods. Otherwise, it requires few control variables, is robust, easy to use, and lends itself very well to parallel computation. Hence it is very promising to solve lots of engineering optimization problems. Guney and Basbug adopted DE into antenna design [19]. Zheng et al. applied DE to estimate the state of hybrid power system [20]. Applied DE to microwave circuit designs [21].

In this paper, we adopt DE into NCSs design. First, we design the state feedback controller to overcome the latency and the packet dropout of NCS. Then, to optimize the control performance, DE is applied to search the optimal parameters of the controller and to guarantee the stability of the overall system. Finally, the computer simulations are given to demonstrate the effectiveness of the proposed results.

The main contributions of this paper are briefly as
follows: First, the controller design for NCS with transmission delay and data packet dropout is obtained and the stability of the overall system can be guaranteed. Also, by using DE, without solving the difficult Lyapunov-Krasovskii stability criterion, the optimal control parameters are searched to improve the control performance.

This paper is organized as follows: In section 2, we will describe the system description of NCS. Section 3 will present the design of differential evolution based networked control system. In section 4, computer simulation will be given to illustrate the control performance of the proposed control strategy. Section 5 will conclude this paper.

2. The System Description of NCS

This paper considers a class of the networked control system, where the framework shown in Figure 1 [9]. This system is composed of the following five parts: a sensor, a controller, a zero-order-holder (ZOH), applied as an actuator, a controller, a communication network channel, and a controlled plant.

Consider the controlled plant as following [14]:

\[ \dot{x}(t) = Ax(t) + \Delta Ax(t) + Bu(t) + wo(t) \] (1)

where \( x(t) = [x(t), \dot{x}(t), ..., \dot{x}^{(m)}(t)] \in \mathbb{R}^n \) is the state vector, \( u(t) \in \mathbb{R}^m \) is the control signal, \( wo(t) \in \mathbb{R}^n \) is the unknown external disturbance, \( A \in \mathbb{R}^{n \times n} \) and \( B \in \mathbb{R}^{m \times m} \) are known constant matrices, and \( \Delta A \in \mathbb{R}^{n \times n} \) is unknown uncertainty matrix. The initial condition of controlled plant is given as \( x(t_0) = x_0 \). Without loss of generality, we make the following assumption [9]:

**Assumption 1**: \( (A, B) \) is controllable pair.

**Assumption 2**: The external disturbance \( wo(t) \) is bounded. That is, \( wo(t) \in L_2[0, t_f], \forall t_f \in [0, \infty) \).

**Assumption 3**: There exists a bounding matrix \( E_\alpha^\top E_\alpha \) such that \( \Delta A^\top \Delta A \leq E_\alpha^\top E_\alpha \).

For NCS, since the controller is connected with the sensor or ZOH via a share communication network channel, propagation, transmission, router, processing, computer, storage delays … etc. would cause latency. Also, network congestion, multi-path fading, faulty network drivers would cause packet dropout. Figure 2 show latency and packet dropout of NCS. Because of latency and packet dropout, packets are transmitted from the sensor to the controller spend \( \tau_{sck} \), and from the controller to the actuator spend \( \tau_{cak} \). Define the total latency as \( \tau_k = \tau_{sck} + \tau_{cak} \) at every sampling instant \( t_k \) and make the following assumptions:

**Assumption 4** [14]: The total latency \( \tau_k \) is bounded.

Also, for the packet dropout, we make the following assumption:

**Assumption 5** [14]: The packet dropout number \( \eta_k \) is bounded as \( 0 \leq \eta_k \leq \eta_{\text{max}} \) where \( \eta_{\text{max}} \) is upper bound of \( \eta_k \).

The objective of this paper is design a control strategy to inhibit the effect of latency and packet dropout such that the system state vector \( x(t) \) of NCS would converge to zero.
To treat the objective, we adopt state feedback control and design the control law as follows:

\[ u(t) = Kx(t) \]  \hspace{1cm} (2)

where \( K \) is the control gain matrix. Usually, the control gain matrix \( K \) is obtained by solving the Lyapunov-Krasovskii stability criterion. But, solving the stability criterion usually has to calculate the difficult LMI problem or an eigenvalue problem. In order to obtain the control gain matrix \( K \) more efficiently, this paper applied the differential evolution. The detail algorithm will be provided in Section 3.

3. The Design of Differential Evolution Based Networked Control System

In this section, we will propose the design of differential evolution based networked control system. Based on the above-mentioned discussion, we will apply DE to search the optimal control gain matrix for NCS. The detail algorithm can be described as follows:

**Initiation:** At first, let the mutation scale factor as \( F \), the crossover rate as \( C_c \), the population size as \( N_p \), and the maximum generation number as \( G_{\text{max}} \). Since \( K \in \mathbb{R}^{m \times n} \), we randomly generate

\[ K_{i,j} \in \mathbb{R}^{m \times n} \quad \text{for} \quad i = 1,\ldots,N_p \]  \hspace{1cm} (3)

as a population for the 1st generation. Define the fitness function as

\[ f(K_{i,G}) = \frac{1}{1 + \sum \|s\|}, \]  \hspace{1cm} (4)

and calculate the fitness value for all \( K_{i,G} \) \((i = 1,\ldots,N_p)\).

**Mutation:** Then, randomly select \( K_{1,G}, K_{2,G}, \ldots, K_{N_p,G} \) and get the mutant vector by the following equation:

\[ K_{i,G+1,U} = K_{i,G} + F \cdot (K_{j,G} - K_{j,G}) \]  \hspace{1cm} (5)

**Crossover:** After that, to increase the diversity of the perturbed parameter vectors, crossover is introduced. Each element of the trial vector, \( K_{i,G+1,U} \), can be get by

\[ k_{j,G+1,U} = \begin{cases} k_{j,G+1,U} \quad \text{if} \quad \text{rand}(0,1) \leq C_c \\ k_{j,G+1,U} \quad \text{otherwise} \end{cases} \]  \hspace{1cm} (6)

**Selection:** To decide whether or not it should become a member of generation \( G + 1 \), the trial vector \( K_{i,G+1,U} \) is compared to the target vector \( K_{i,G} \) using the greedy criterion. If vector \( K_{i,G+1,U} \) yields a smaller cost function value than \( K_{i,G} \), then \( K_{i,G+1} \) is set to \( K_{i,G+1,U} \); otherwise, the old value \( K_{i,G} \) is retained.

In summary, the proposed control strategy can be expressed as the following procedures:

**Design Procedures:**

- Generate \( N_p \) individuals of the initial population randomly.
- For \( G = 1 : G_{\text{max}} \)
- For \( i = 1 : N_p \)
  - calculate the fitness value \( f(K_{i,G}) \)
- End for
- For \( i = 1 : N_p \)
  - //Mutation randomly select \( K_{1,G}, K_{2,G}, \ldots, K_{N_p,G} \), compute \( K_{i,G+1,U} = K_{i,G} + F \cdot (K_{j,G} - K_{j,G}) \)
  - //Crossover
  - For \( j = 1 : (m \times nL) \)
    - generate \( \text{rand}(0,1) \)
- End for
4. Simulation

In this section, an inverted pendulum system simulated as the controlled plant to demonstrate the performance of the proposed control strategy. Let $x_i(t)$ be the angular of the pendulum with respect to the vertical line and $u(t)$ be the applied the control signal. Define $x(t) = [x_1(t), \dot{x}_1(t)]^T$, $\dot{x}(t) = [\dot{x}_1(t), \dot{x}_2(t)]^T = [x_1(t), x_2(t)]^T$, the dynamic equations of the inverted pendulum system can be described as follows:

$$
\begin{align*}
\dot{x}_1(t) &= x_2(t) \\
\dot{x}_2(t) &= \frac{g \sin(x_1) - a m_p l x_2^2 \sin(x_1) \cos(x_1)}{(4l/3) - a m_p l \cos^2(x_1)} + \frac{a \cos(x_1) u}{(4l/3) - a m_p l \cos^2(x_1)} + \omega(t)
\end{align*}
$$

where $a = m_c + m_p$, $g = 9.8 m/s^2$ is the acceleration due to gravity, $m_c$ is the mass of the cart, $m_p$ is the mass of the pole and $l$ is the half length of the pole. In this simulation, we set $m_c = 1 kg$, $m_p = 0.1 kg$, $l = 0.5 m$ and the sampling period as 0.001 sec.

The Jacobian linearized model around the equilibrium $x(0) = [0,0]^T$ can be obtained directly from $x(t) = [x_1(t), x_2(t)]^T$, the dynamic equations (Eq. 8), which yields

$$
\begin{align*}
\begin{bmatrix}
\dot{x}_1(t) \\
\dot{x}_2(t)
\end{bmatrix} &= \begin{bmatrix}
0 \\
\frac{g}{(4l/3) - a m_p l}
\end{bmatrix} \begin{bmatrix}
x_1(t) \\
x_2(t)
\end{bmatrix} + \begin{bmatrix}
1 \\
0
\end{bmatrix} \begin{bmatrix}
\dot{x}_1(t) \\
\dot{x}_2(t)
\end{bmatrix} + \Delta A \begin{bmatrix}
x_1(t) \\
x_2(t)
\end{bmatrix} + \begin{bmatrix}
0 \\
\frac{a}{(4l/3) - a m_p l}
\end{bmatrix} u + \begin{bmatrix}
0 \\
\omega(t)
\end{bmatrix}
\end{align*}
$$

where $\Delta A$ is be regarded as the uncertainty terms due to latency, packet dropout and linearization error.

To demonstrate the proposed method, we simulation the following cases:

**Case 1**: This case is the ideal condition. It means the total latency $\tau_k = 0$, and the packet dropout number $\eta_k = 0$. Set the initial condition is as $x(0) = [0.2,0]^T$.

**Case 2**: The total latency is set as the random number generated from a Gaussian distribution with zero mean and the standard deviation as 0.06 sec. The packet dropout number is set as the random number generated from uniform Gaussian distribution with zero mean and the standard deviation as 1. The bound of $\eta_k$ is set as 15. The initial condition is set as $x(0) = [-0.2,0]^T$.

Here we set the mutation scale factor $F = 0.9$, the crossover rate $C_r = 0.3$, the population size $N_p = 50$, and the maximum generation number $G_{max} = 100$ for all cases. Besides, in the simulations, all the programs coded by Matlab version R2015a were executed by a personal computer with Intel(R) Core(TM) i7-4600U CPU @ 1.6 GHz processor, 16GB RAM and 64-bit Windows 7 operating system with service pack 1.
Figure 3. The trajectory of $x_1(t)$ for Case 1

Figure 4. The trajectory of $x_2(t)$ for Case 1

Figure 5. The control signal $u(t)$ for Case 1

Figure 6. The trajectory of $x_1(t)$ for Case 2

Figure 7. The trajectory of $x_2(t)$ for Case 2

Figure 8. The control signal $u(t)$ for Case 2
5. Conclusions

This paper has presented the state feedback control based networked control system design with DE algorithm. The state feedback controller is designed to compensate the latency, and packet dropout and to guarantee the stability of the overall system. Applying DE, the optimal control parameters are searched to improve the control performance.

The main contributions of this paper are briefed as follows: First, the controller design for NCS with transmission delay and data packet dropout is obtained and the stability of the overall system can be guaranteed. Also, by using DE, the optimal control parameters are obtained without solving the difficult Lyapunov-Krasovskii stability criterion, one can obtain the optimal control parameters. The simulation results show that the proposed control strategy can successfully stability the NCS and has good performance. Currently, the proposed control strategy is being studied for the practice systems, although still exist various challenging issues.

Acknowledgements

This work was supported in part by Ministry of Science and Technology, Taiwan, R.O.C. under Grant MOST 105-2221-E-262-016 –

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