Non-equilibrium antineutrinos of primordial nucleosynthesis

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Abstract. During the era of primordial nucleosynthesis the background of non-equilibrium antineutrinos is being formed due to decays of neutrons and nuclei of tritium. The spectra of antineutrinos of this background were calculated taking into account the Coulomb interaction between electron and daughter nucleus in $\beta$-decay. The dependence of these spectra on the value of the baryon-to-photon ratio $\eta$ at the period of primordial nucleosynthesis is investigated. The observations of these antineutrinos will allow us to look directly at the very early Universe and nonequilibrium processes taken place before, during, and some time after primordial nucleosynthesis. In any case, this phenomenon is one more aspect in the picture of the standard cosmological model.
1 Introduction

The observations of the cosmic microwave background (CMB) allow us to see into our Universe when it was about 380 000 years old. Similarly primordial nucleosynthesis provides us with an indirect probe of the early Universe (about a few minutes old) based on the comparison of light element (D, $^4$He, $^7$Li) observations with corresponding theoretical calculations, which in turn is based on the well-established knowledge of nuclear and particle physics [1–4]. We cannot observe the Universe at that epoch directly using electromagnetic radiation due to the opacity of the Universe at early stages right up until primordial recombination. Nevertheless, the direct information about the first seconds of the Universe evolution principally can be obtained by the detection of relic neutrinos which were going out of equilibrium and beginning a free expansion without any interaction with the other primordial material when the age of the Universe was less then one second. These neutrinos as well known as the cosmic neutrino background $C_\nu$ (note that cosmic neutrino background consists of neutrino as well as antineutrino, so it is more correct to use the following abbreviation $C_\nu\bar{\nu}B$ but we use commonly accepted $C_\nu B$). Like the cosmic microwave background radiation, the $C_\nu B$ was formed with a thermal equilibrium spectrum which for neutrinos ($\nu$) and antineutrinos ($\bar{\nu}$) is given by the Fermi-Dirac distribution:

$$n_{\nu\bar{\nu}}(p)dp = \frac{1}{(2\pi \hbar)^3} \frac{4\pi p^2 dp}{\exp(p\epsilon/kT) + 1}. \quad (1.1)$$

This formula is expressed for the massless antineutrino case ($\epsilon_\nu = pc$). We can neglect the neutrino mass at the decoupling period ($T \sim 2$ MeV) because there is the upper limit of $\sum m\nu < 0.23$ eV [5, 6] and the ratio $m\nu c^2/kT$ is about $10^{-7}$ for this period. After neutrino decoupling the spectrum has kept the same form (due to the adiabatic expansion of the Universe) with a temperature decreasing like $T_\nu \propto (1 + z)$, where $z$ is the cosmological redshift. It is very important to note that this fact takes place for momentum distribution $n(p)$ whether or not neutrino possesses mass, while the form of energy distribution $n(\epsilon)$ depends on neutrino mass. Therefore despite the fact that $m_\nu \neq 0$, today ($z=0$) the momentum distribution $n(p)$ has the form to be the same as eq. (1.1) with the current temperature $T_{\gamma 0}$ whose value is related to the current temperature of the relic photons $T_{\gamma 0}$ (the CMB
temperature). The thermodynamics of the early Universe give us the relation between the relic neutrino and photon temperatures, $T_\nu = \left(\frac{4}{11}\right)^{1/3}T_\gamma$, arising from electron-positron annihilation. Given this relation and the current value of $T_\gamma^0 \approx 2.725 \pm 0.001$ K [7], we have the present temperature of relic neutrinos to be $T_\nu \approx 1.945$ K. However, small entropy transferring from electrons and positrons into neutrinos and antineutrinos during the epoch of $e^-e^+$–annihilation leads to the minor energy-dependent distortions of relic neutrinos energy spectrum [8–11], therefore, strictly speaking, the whole spectrum cannot be described by only a single parameter $T_{\nu 0}$.

The equilibrium part of relic neutrinos (CνB) carries only the information about thermal equilibrium between neutrinos and electron-nucleon-photon plasma before neutrino decoupling. In contrast distortions of relic neutrinos carry information about non-equilibrium processes with the participation of neutrinos after decoupling. Besides distortions due to $e^-e^+$–annihilation mentioned above there is one more significant non-equilibrium addition to CνB formed by antineutrinos which were being produced during the era of Big Bang nucleosynthesis (BBN) as a result of decays of $\beta^-$ unstable neutrons $n$ and nuclei of tritium (tritons) $t$ [12]. The spectra of these antineutrinos are non-equilibrium because the period of their formation take place rather after neutrino decoupling. These antineutrino spectra carry the information about the temporal evolution of abundances of these elements at that epoch.

1.1 “Grand Unified Neutrino Spectrum”

In addition to relic neutrinos it should be mentioned that there are other neutrino backgrounds at higher energies which could be called “cosmological” as well: two narrow neutrino lines from $^7$Be decay [13] taken place after its recombination epoch, the diffuse supernova neutrino background [14], the active galactic nuclei (AGN) background and cosmogenic (GZK) neutrinos arising from interactions of ultraenergetic protons with the CMB photons (see e.g. [15] and references therein).

The spectra of CνB, energy-dependent admixture to these spectra due to $e^\pm$–annihilation and non-equilibrium spectra of “neutron” and “triton” antineutrino of primordial nucleosynthesis are shown in figure 1, which represent so called Grand Unified Neutrino Spectrum, among a number of neutrino/antineutrino spectra from other different natural sources. This can be seen that the spectra of relic neutrinos/antineutrinos occupy the area of the lowest energies in figure 1, because of the remoteness of the eras of their formation.

In this work we discuss the complementary ability to look at the early Universe and non-equilibrium processes occurred before, during and after primordial nucleosynthesis using spectrum calculations and future possible observations of antineutrinos having arisen from neutron and triton (nucleus of tritium) decays ($n \rightarrow p + e^- + \bar{\nu}_e$, $t \rightarrow ^3\text{he} + e^- + \bar{\nu}_e$).

2 Non-equilibrium antineutrino spectra

2.1 Free decaying nuclei at the BBN epoch

The number of antineutrinos produced in decays of neutrons and tritons per unit volume during a time interval $dt$ with momentum between $p$ and $p + dp$ is

$$dn_\nu(p) = \lambda n(t)f(p)dpdt,$$  \hspace{1cm} (2.1)

\footnote{The name “Grand Unified Neutrino Spectrum” was taken from [43].}
where λ is the decay rate of radioactive nuclear species in question, n(t) is its number density, f(p) is the momentum spectrum of antineutrino produced in β⁻ decay, it is normalized so that

$$\int_0^{p_{\text{max}}} f(p) dp = 1,$$

(2.2)

where p_{\text{max}} is the maximum antineutrino momentum in β⁻ decay. The number density n(t) of neutrons or tritons can be expressed as

$$n(z) = Y(z)n_b(z) = Y(z)n_b^0(1 + z)^3,$$

where Y(z) is the ratio of neutrons or tritons to all baryons n_b, and $n_b^0 = \eta n_\gamma^0 \approx 2.48 \times 10^{-7}$ cm⁻³ (see e.g.
Figure 2. The evolution of the mass fractions $A_i/n_i/n_b$ ($A_i$ is the mass number of species $i$) of the light nuclei produced during primordial nucleosynthesis as a function of the temperature. Red and crimson lines correspond to neutron and tritium mass fractions. The calculations have been done by using our own numerical code for primordial nucleosynthesis (see the text) [18].

The baryon number density at the present epoch ($z = 0$), $\eta$ is baryon-to-photon ratio at the present epoch and its value is $\eta = 6.1 \times 10^{-10}$ [17]. To obtain the dependencies $Y(t)$ we have updated our own previous numerical code for primordial nucleosynthesis [18] which is based on the historical Wagoner’s code [19] (results of our code are in good agreement with presented results of other known codes (e.g. [20–23]).

2.2 The antineutrino momentum spectrum in $\beta^-$ decay

The antineutrino momentum spectrum in $\beta^-$ decay is calculated using Fermi’s golden rule (see e.g. [24, 25]):

$$dW = w(p_{\nu})dp_{\nu} = \frac{2\pi}{\hbar}|\langle n|H_{\beta}|m\rangle|^2 d\rho(Q), \quad d\rho(Q) \equiv \frac{dn_e dn_{\nu}}{dQ} \bigg|_{Q=Q}. \quad (2.3)$$

Here $dW$ is the probability per unit time of the $\beta^-$ transition from the state in which there is a $\beta^-$ unstable system to a state in which there are an antineutrino of momentum in the interval between $p_{\nu}$ and $p_{\nu} + dp_{\nu}$ and an electron of momentum in the interval between $p_e$ and $p_e + dp_e$; $\langle n|H_{\beta}|m\rangle$ is the matrix element of the Hamiltonian operator of the weak interaction between the initial state $|m\rangle$ and the final state $|n\rangle$, $d\rho(Q)$ is the number of the possible
final states (for the given antineutrino momentum) per unit energy range around the energy released $Q$ in $\beta^-$ decay, where the product of infinitesimal phase spaces of the electron and the antineutrino is

$$dn_e dn_\nu = \frac{V d^3 p_e V d^3 p_\nu}{(2\pi \hbar)^3 (2\pi \hbar)^3}. \quad (2.4)$$

As (i) the matrix element $\langle n | H_\beta | m \rangle$ weakly depends on energy, (ii) the recoil energy of the daughter nucleus is negligible compared with the energy taken by the electron and the antineutrino in the form of their kinetic energy (that gives $\varepsilon_e + \varepsilon_\nu = Q$), and (iii) $p_e = \frac{1}{c} \sqrt{\varepsilon_e (\varepsilon_e + 2m_e c^2)}$ for the emitted electron and $p_\nu = \varepsilon_\nu/c$ for the emitted antineutrino, then collecting all constant factors into the only constant $C'$ we obtain the shape of the probability of finding the antineutrino with the momentum $p$:

$$w(p) = C' F(p), \quad (2.5)$$

with

$$F(p) = \frac{1}{c^3} \sqrt{(Q - pc)(Q - pc + 2m_e c^2)(Q - pc + m_e c^2)p^2}. \quad (2.6)$$

This expression is analogous to well-known result for the transition probability for an electron emitted in $\beta^-$ decay with momentum $p_e$:

$$F(p_e) = \frac{1}{c^3} (Q - \sqrt{p_e^2 c^2 + m_e^2 c^4})^2 p_e^2. \quad (2.7)$$

Dependencies (2.6) and (2.7) are shown in Figure 4.

The transition probability (2.3) integrated over all possible values of the antineutrino momentum gives the total probability of $\beta^-$ decay per unit time and it is equal to the decay rate $\lambda$ or the inverse mean lifetime $\tau$ of decaying nucleus:

$$\mathcal{W} = \int_0^{Q/c} w(p) dp = \int_0^{Q/c} C' F(p) dp = \lambda = \frac{1}{\tau}. \quad (2.8)$$

It is seen from the normalization conditions (2.2) and (2.8), that the relation between the momentum spectrum $f(p)$ of antineutrino emitted in $\beta^-$ decay (2.1) and the function $F(p)$ is the following:

$$f(p) = \tau C' F(p). \quad (2.9)$$

It is convenient to take (2.9) in the dimensionless form using dimensionless parameters: $\tilde{p} = pc/Q$, which takes values from 0 to 1, $\tilde{m}_e = m_e c^2/Q$, $C = \tau C' Q^4/c^5$, that gives

$$f(\tilde{p}) = C \sqrt{(1 - \tilde{p})(1 - \tilde{p} + 2\tilde{m}_e)(1 - \tilde{p} + \tilde{m}_e)} \tilde{p}^2. \quad (2.10)$$

### 2.3 The evolution of the antineutrino spectrum in the expanding Universe

The momentum of particles propagating freely through the Universe obeys the following relation (see e.g. [2, 3]):

$$p(t)a(t) = p^i a^i, \quad (2.11)$$

where $a(t)$ is the scale factor of the Universe related to the cosmological redshift $z(t)$ through the definition $1 + z(t) = 1/a(t)$ (and $a = 1$ at the present epoch). The superscript $i$ stands for “initial” values.
It is seen from the relation (2.11) that in the expanding Universe the momentum of antineutrinos decreases as time passes. Due to the above fact antineutrinos become non-relativistic at some moment, and the relation between its momentum and kinetic energy $\varepsilon$ takes the form

$$p^0 c = \sqrt{\varepsilon (\varepsilon + 2m_\nu c^2)}, \quad (2.12)$$

where $m_\nu$ is the antineutrino mass. The superscript 0 stands for values taken at the present epoch ($z = 0$, $t_0 = 13.8$ Gyr). It can be put in the following dimensionless form:

$$\tilde{p}^0 = \sqrt{\tilde{\varepsilon} (\tilde{\varepsilon} + 2 \tilde{m}_\nu)}, \quad (2.13)$$

Substituting the relation (2.11), taken in the form $p_i = p^0 / a_i = p^0 (1 + z^i)$, into the expression (2.10) one obtains the fraction of antineutrinos of momentum in a given interval, which were produced at fixed value of $z = z^i$:

$$f(\tilde{p}^0) d\tilde{p}^0 = f(\tilde{p}^0 (1 + z^i)) (1 + z^i) d\tilde{p}^0 = f^0(\tilde{p}^0) d\tilde{p}^0. \quad (2.14)$$

It corresponds to the fraction of antineutrinos, which at present have kinetic energy in the interval from $Q \cdot \tilde{\varepsilon}$ to $Q \cdot (\tilde{\varepsilon} + d\tilde{\varepsilon})$:

$$f^0(\tilde{\varepsilon}) d\tilde{\varepsilon} = f^0(\tilde{p}^0(\tilde{\varepsilon})) d\tilde{p}^0(\tilde{\varepsilon}) d\tilde{\varepsilon}. \quad (2.15)$$

### 2.4 Non-equilibrium antineutrino spectral characteristics

The total number density of non-equilibrium antineutrinos of energy in the interval between $\tilde{\varepsilon}$ and $\tilde{\varepsilon} + d\tilde{\varepsilon}$ is calculated as the integral of quantity (2.1) diluted due to the expansion of the Universe (where $p$ is expressed through the kinetic energy at the present epoch) over all redshifts:

$$dn^0_\nu(\tilde{\varepsilon}, \varepsilon) = \int_0^{z^i(\tilde{\varepsilon})} \frac{dn_\nu(\tilde{\varepsilon}, z)}{(1 + z)^3} dz = -\frac{1}{\tau} \int_0^{z^i(\tilde{\varepsilon})} \frac{n(z)}{(1 + z)^3} f^0(\tilde{\varepsilon}) \frac{dt}{dz} dz d\tilde{\varepsilon}. \quad (2.16)$$

The lower limit on the integral corresponds to the redshift of the present time ($z = 0$) and the upper limit $z^i(\tilde{\varepsilon})$ equals to $(1 / \sqrt{\tilde{\varepsilon} (\tilde{\varepsilon} + 2 \tilde{m}_\nu)} - 1)$ for every fixed value of $\tilde{\varepsilon}$, what is derived from the condition $p^0 c \cdot (1 + z) \leq Q$. The factor $(1 + z)^{-3}$ arises in (2.16) because of dilution of the number density $dn_\nu(\tilde{\varepsilon}, z)$ due to the expansion of the Universe. The function $dt/dz$ can be obtained from the relation between time $t$ and temperature $T_\gamma(z) = T_\gamma^0 (1 + z)$ during the radiation-dominated era (see e.g. [1]):

$$t = 1.78 \text{ s} \cdot \left( \frac{T_\gamma^0 (1 + z)}{10^{10} \text{ K}} \right)^{-2} + \text{ Const}, \quad (2.17)$$

from which it is seen that $dt/dz < 0$, that explains the minus sign in the front of the integral (2.16). Thus, the energy spectrum of non-equilibrium antineutrinos at present epoch is

$$n^0_\nu(\varepsilon) = -\frac{1}{Q \tau} \int_0^{z^i(\tilde{\varepsilon})} \frac{n(z)}{(1 + z)^3} f^0(\tilde{\varepsilon}) \frac{dt}{dz} dz. \quad (2.18)$$
Figure 3. The calculated fluxes of non-equilibrium antineutrinos due to decays of neutrons (red curvatures) and tritons (crimson curvatures) during primordial nucleosynthesis [12] and fluxes of neutrinos and antineutrinos from various natural sources: relic neutrinos and antineutrinos \( (C\nu B) \) with temperature \( T_\nu = 1.945 \) K (see e.g. [1]); a non-thermal addition to relic neutrinos and antineutrinos due to \( e^+e^- \)-annihilation at the beginning of primordial nucleosynthesis [8–11]; solar neutrinos from reactions of thermonuclear synthesis [42]; the doublet of the narrow cosmological neutrino lines from \(^7\)Be decay [13]; antineutrinos produced geologically (geoneutrinos) in decays of radioactive isotopes [44, 45]. The fluxes in the case of massless neutrinos are represented by dashed lines and in the case of \( m_\nu = 0.01 \) eV with solid lines.

As usual, what is observable is not the number density of particles, but the flux. The flux of antineutrinos \( F(\varepsilon) \) can be calculated by integrating (2.18) multiplied by antineutrino velocity \( v(\varepsilon) \) over hemisphere \( \Omega/2 \):

\[
F(\varepsilon) = \frac{v(\varepsilon)}{4\pi} \int_\Omega n_\nu^0(\varepsilon) \cos \Theta d\Omega = -\frac{v(\varepsilon)}{4Q\tau} \int_0^{z(\varepsilon)} \frac{\tilde{n}(z)f^0(\tilde{\varepsilon})}{(1+z)^3} \frac{dt}{dz} dz, \tag{2.19}
\]

and antineutrino velocity can be found from the relations \( v = dE/dp \) and \( \tilde{E} = \sqrt{(pc)^2 + (m_\nu c^2)^2} \):

\[
\frac{dE}{dp} = \frac{pc}{\tilde{E}} c = \frac{\tilde{p}}{\tilde{E} + \tilde{m}_\nu c}. \tag{2.20}
\]

The calculated fluxes of non-equilibrium antineutrinos are shown in figure 3. In the calculations we used the following values of lifetimes and released energies: triton’s lifetime...
Figure 4. The upper panels: the energy spectra of an electron and antineutrino emitted in $\beta^-$ decay of triton. Solid lines represent the spectra calculated taking into account Coulomb interaction and dashed lines represent the spectra calculated ignoring Coulomb interaction. Dash-dotted lines are the non-relativistic approximation (2.22) for the Fermi function $F(Z = 2, \varepsilon_e)$ for triton’s $\beta^-$ decay. Red circles are the values of the Fermi function calculated relativistically in [30]. In left figure all the spectra are normalized to unity in accordance with (2.2), and on right one the spectra differ from each other by the factor of the Fermi function. Note that left panel demonstrates that taking Coulomb interaction into account leads to an increase in the fraction of antineutrinos with higher energies, and the right panel demonstrates that Coulomb interaction effectively leads a lifetime of decaying nuclei to decrease. The bottom panel: the ratio of antineutrino fluxes from decays of tritons calculated taking into account and ignoring Coulomb interaction.

$\tau_t \simeq 17.656$ years [26], neutron’s lifetime is $\tau_n \simeq 880.2$ seconds [27, 28], triton decay energy released is $Q_t \simeq 18.592$ keV [29]; neutron decay energy released is $Q_n \simeq 782.346$ keV [29].

2.5 Coulomb interaction

Because of the Coulomb interaction between emitted in $\beta^-$ decay electron and the daughter nucleus, the asymptotic momentum of the electron is lower than its momentum at the time of its creation. By this reason the expression (2.3) gives an underestimated value of the transition probability at every momentum. To correct this discrepancy the Fermi function $F(Z, \varepsilon_e)$ is used. It is defined as the ratio of squared moduli of the electron wave functions at the site of the nucleus calculated taking Coulomb interaction into account and ignoring it

$^{2}$Authors in [26] give triton’s half life $\tau_{1/2}$, which is related to its lifetime as $\tau \ln 2$. 

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Figure 5. Left panel: the evolution of the mass fractions $A_i n_i/n_b$ of neutrons and tritons as a function of the temperature under various values of $\eta_{BBN}$. Left panel: the fluxes of non-equilibrium antineutrinos calculated using the mass fractions of neutrons and tritons which correspond to various values of $\eta_{BBN}$.

(see e.g. [24, 25]):

$$F(Z, \varepsilon_e) = \frac{|\psi^{Coul}(0)|^2}{|\psi(0)|^2}.$$ (2.21)

In calculations of the transition probability the right hand side of equality (2.3) is multiplied by the Fermi function. The Fermi function actually should be calculated relativistically, but there is the following non-relativistic approximation for the Fermi function which works very good in the case of triton decay (because of relatively small electric charge of triton):

$$F(Z, \varepsilon_e) = \frac{x}{1 - e^{-x}}, \quad x = \frac{2\pi Z \alpha}{\beta},$$ (2.22)

where $Z$ is a charge of the daughter nucleus, $\alpha$ is the fine structure constant, $\beta$ is the velocity of electron in units of the speed of light. The non-relativistic approximation for the Fermi function $F(Z=2, \varepsilon_e)$ for decay of triton is shown in figure 4. In addition, values of the Fermi function $F(Z=2, \varepsilon_e)$ which were calculated relativistically in [30] are put in this figure by red circles to demonstrate the good agreement between the non-relativistic approximation for the Fermi function and the relativistic numerical calculations of the Fermi function.

It was found that the Coulomb interaction increases the fraction of non-equilibrium “tritium” antineutrinos of higher energies (see the bottom panel of figure 4). In contrast the Coulomb interaction rather slightly modifies the distribution function of antineutrino in $\beta$– decay of neutron, it is explained by relatively high energy released ($Q_n = 782.346$ keV in comparison with $Q_t = 18.592$ keV).

2.6 Non-equilibrium antineutrinos as a “baryometer”

The only free parameter of primordial nucleosynthesis is the baryon-to-photon ratio of the Universe. Its value $\eta_{BBN} = (6.2 \pm 0.4) \cdot 10^{-10}$ [31] is now deduced from the comparison of light element observations and results of BBN numerical calculations. One more independent way to determine $\eta$ comes from the analysis of the CMB anisotropies and it gives the value of the baryon density $\Omega_b h^2 = 0.0224 \pm 0.0001$ [17] which is related to $\eta_{CMB}$ by $\Omega_b h^2 \approx \eta_{CMB} \cdot 10^{10}/274$ and this gives $\eta_{CMB} = (6.13 \pm 0.03) \cdot 10^{-10}$. This analysis deals with to the era of primordial recombination ($\approx 380,000$ years after the Big Bang) and strictly speaking, $\eta_{CMB}$
is not necessarily equals to $\eta^{\text{BBN}}$. Primordial nucleosynthesis and recombination are different cosmological epochs and there is the possibility of a change in $\eta$ on cosmological time scales due to some non-standard processes referred to as physics beyond the Standard Model, such as the decays (or annihilation) of dark matter particles (see e.g. [32] and references therein). The existence of such processes is suggested, among other things, by the discrepancy between theoretical predictions and observational data for primordial $^7\text{Li}$ (see e.g. [33]).

Hence, independent measurements of $\eta^{\text{BBN}}$ and $\eta^{\text{CMB}}$ are powerful tool for exploring physics beyond the Standard Model. The dependence of non-equilibrium antineutrino spectra on $\eta^{\text{BBN}}$ was studied in this regard. The number density of the decaying nuclei depends on $\eta^{\text{BBN}}$ both explicitly through the factor $\eta$ and implicitly through the function $X_i(z)$, with the latter sentence being demonstrated in the left panel of figure 5. The calculations of antineutrino spectra at various values of $\eta^{\text{BBN}} = (2, 6, 10) \times 10^{-10}$ show that smaller fluxes correspond to higher values of $\eta$ (see the right panel of figure 5). It is explained by the fact that the more dense matter (higher values of $\eta$) the bigger part of neutrons and tritons tends to transform into $^4\text{He}$ through nuclear reactions (see the left panel of figure 5).

## 3 Conclusions

The non-equilibrium spectra of antineutrinos of primordial nucleosynthesis have been calculated taking into account the Coulomb interaction between electron and daughter nucleus in $\beta^-$ decay. It was found that the Coulomb interaction increases prominently the number of “tritium” antineutrinos of higher energies. Namely at the energies $\varepsilon > 10^{-7}$ MeV the ratio of antineutrino fluxes calculated, taking into account and ignoring the Coulomb interaction, amounts to several tens of percents.

Independent measurements of $\eta^{\text{BBN}}$ and $\eta^{\text{CMB}}$ serves as a powerful tool for studying the physics beyond the Standard Model. Non-equilibrium antineutrinos may potentially serve as the baryometer, which indicates the value of $\eta^{\text{BBN}}$. In this context, the dependence of non-equilibrium antineutrino spectra on value of $\eta^{\text{BBN}}$ is studied. Calculation of antineutrino fluxes at various values of $\eta^{\text{BBN}}$ showed that smaller fluxes correspond to higher values of $\eta^{\text{BBN}}$.

The direct detection of the non-equilibrium antineutrino background is an observational challenge. However various possibilities of the direct detection of relic neutrinos are discussed in the literature. The promising proposals among them are relic neutrino capture on radioactive $\beta$ decaying nuclei [34] and relic antineutrinos capture on radioactive nuclei decaying via electron capture [35, 36]. There is also the PTOLEMY project which aims to develop a design for a $\nu$B detector [37]. For descriptions of other ways and current perspectives of the direct detection of the relic neutrinos/antineutrinos see, for instance, the following detailed works [38–40] as well as [41] and references therein.

Distortions in the spectrum of relic neutrinos can provide very useful observational information about cosmological epochs which immediately follow neutrino decoupling. This information could be used to extract values of a number of cosmological parameters and set constraints on various cosmological scenarios.

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