Diverse Properties of Carbon-Substituted Silicenes

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The theoretical framework, which is built from the first-principles results, is successfully developed for investigating emergent two-dimensional materials, as it is clearly illustrated by carbon substitution in silicene. By the delicate VASP calculations and analyses, the multi-orbital hybridizations are thoroughly identified from the optimal honeycomb lattices, the atom-dominated energy spectra, the spatial charge density distributions, and the atom and orbital-decomposed van Hove singularities, being very sensitive to the concentration and arrangements of guest atoms. All the binary two-dimensional silicon-carbon compounds belong to the finite- or zero-gap semiconductors, corresponding to the thoroughly/strongly/slightly modified Dirac-cone structures near the Fermi level. Additionally, there are frequent $\pi$ and $\sigma$ band crossings, but less anti-crossing behaviors. Apparently, our results indicate the well-defined $\pi$ and $\sigma$ bondings.

Keywords: buckled structure, silicene, substitution, geometric structure, electronic properties

1. INTRODUCTION

Chemical substitutions on layered materials are capable of band structure tailoring which could lead to significant modifications of the properties of pristine lattices through very strong host-guest multi-orbital hybridizations. With the use of modern experimental growth techniques, ternary and binary compounds, which are characterized by $B_xC_yN_z$, have been successfully synthesized for three-dimensional (3D) bulk systems [1, 2], two-dimensional (2D) layers [3], one-dimensional (1D) cylindrical nanotubes [4], 1D nanoribbons [5], and zero-dimensional (0D) quantum dots [6]. Their geometric structures vary from three to zero dimensions, as observed in carbon-related systems [7, 8]. This clearly indicates that each atom possesses at least three half-filled orbitals. Similar syntheses have been performed for the high-potential C-Si compounds [9]. In general, it would be routine to produce the above-mentioned compounds, whereas the opposite might be true for specific components. For example, using high-performance experimental techniques, it may be difficult to manipulate the ratio between the C/Si atoms. Such non-monoelement condensed-matter systems have been predicted or found to exhibit the observable energy gaps or belong to specific semiconductors. The main reason lies in the distinct ionization energies of their components, being consistent with the tight-binding model for non-vanishing diagonal Hamiltonian matrix elements (the sublattice-dependent site energies). Gap engineering could be achieved by transforming the strengthful relations in the $\pi$, $\sigma$, and $sp^3$ bondings of the $[p_z, (s, p_x, p_y), (s, p_x, p_y, p_z)]$-orbital hybridizations.

Chemisorption and substitution of carbon atoms on silicene are two very interesting procedures, since first-principles predictions are available for understanding the important differences between these two types of chemical modification [10, 11], and providing additional information regarding another approach for the formation of silicon-carbide compounds [12] or induce magnetism based...
on transition-metals are embedded in silicene [13]. Based on the viewpoint of a silicon-created honeycomb lattice, carbon atoms are regarded as adatoms and guest ones, respectively. Both silicon and carbon atoms have rather active dangling bonds, leading to significant multi-orbital hybridizations in Si-C [Si-Si and C-C] bonds. Most importantly, the planar bondings between Si and C atoms are expected to be stronger and complicated, compared with the perpendicular configuration. That is to say, the $\pi$ and $\sigma$ bondings of silicene will be significantly modified by C-substitutions. This is directly reflected in the diversified properties, the spatial charge distributions, atom-dominated energy bands, and atom-as well as orbital-projected density-of-states.

The present work is focused on the diverse geometric, and electronic properties of C-substituted silicene. A theoretical framework, which is based on multi-orbital hybridizations, is further developed to clearly analyze the concentration- and configuration-dependent phenomena. For example, the zero- and finite-gap behaviors, the main features of $\pi$, $\sigma$, and sp$^3$ chemical bondings. On the experimental side, a controllable synthesis way, using MTMS/hexane as precursors, is proposed to generate the large-area graphene-based Si-C binary 2D compounds [14]. Furthermore, the silicon-carbide nanosheets are successfully synthesized by a catalyst-free carbothermal method and post-sonication process [15], in which the AFM measurements show the average thickness of $\sim$2–3 nm and size of $\sim$2 μm.

### 2. COMPUTATIONAL DETAILS

Our investigation of the diverse properties of carbon-substituted silicene is based on density functional theory using VASP codes [16, 17]. The exchange and correlation energies due to many-particle Coulomb interactions were calculated with the use of the Perdew-Burke-Ernzerhof (PBE) functional under the generalized gradient approximation [18], whereas the electron-ion interactions can be characterized by the projector augmented wave (PAW) pseudopotentials [19]. A plane-wave basis set with a maximum kinetic energy cutoff of 500 eV was chosen to expand the wave function. In a direction perpendicular to the silicene plane, a vacuum layer with a thickness of 15 Å was added to avoid interactions between adjacent unit cells. The k-point mesh was set as 9 × 9 × 1 in geometry optimization, 100 × 100 × 1 for further calculations on electronic properties via the Monkhorst-Pack scheme. During the ionic relaxations, the maximum Hellmann-Feynman force acting on each atom is less than 0.01 eV/Å whereas the convergent energy scale was chosen as $10^{-5}$ eV between two consecutive steps.

### 3. RESULTS AND DISCUSSIONS

#### 3.1. Geometric Structures

Carbon-substituted silicon systems are capable of possessing unusual geometries, as it is clearly indicated in Table 1 and Figures 1A–L. Four types of typical C-substitution

| Number atoms/unit cell | Pristine | 100% | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta |
|------------------------|----------|------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| Number of C atoms      | 1        | 2    | 3        | 4        | 5        | 6        | 7        | 8        | 9        | 10       | 11       | 12       | 13       | 14       |
| C-Si bond length (Å)   | X        | 2.250| 2.260| 2.270| 2.280| 2.290| 2.300| 2.310| 2.320| 2.330| 2.340| 2.350| 2.360| 2.370|
| C-C bond length (Å)    | X        | 1.785| 1.805| 1.825| 1.845| 1.865| 1.885| 1.905| 1.925| 1.945| 1.965| 1.985| 2.005| 2.025|
| Nearest Si-Si (Å)      | X        | 2.252| 2.262| 2.272| 2.282| 2.292| 2.302| 2.312| 2.322| 2.332| 2.342| 2.352| 2.362| 2.372|
| Second nearest Si-Si (Å) | X    | 2.560| 2.570| 2.580| 2.590| 2.600| 2.610| 2.620| 2.630| 2.640| 2.650| 2.660| 2.670| 2.680|

#### 3.2. Electronic Properties

The band gaps, ground state energies per unit cell, together with the height differences between A and B sublattices.

| Number of C atoms | 100% | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta | 2:1 meta |
|-------------------|------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| C-Si bond length (Å) | 2.250| 2.260| 2.270| 2.280| 2.290| 2.300| 2.310| 2.320| 2.330| 2.340| 2.350| 2.360| 2.370| 2.380|
| C-C bond length (Å) | 1.785| 1.805| 1.825| 1.845| 1.865| 1.885| 1.905| 1.925| 1.945| 1.965| 1.985| 2.005| 2.025| 2.045|
| Nearest Si-Si (Å) | 2.252| 2.262| 2.272| 2.282| 2.292| 2.302| 2.312| 2.322| 2.332| 2.342| 2.352| 2.362| 2.372| 2.382|
| Second nearest Si-Si (Å) | 2.560| 2.570| 2.580| 2.590| 2.600| 2.610| 2.620| 2.630| 2.640| 2.650| 2.660| 2.670| 2.680| 2.690|

#### 3.3. Spatial Charge Distributions

The spatial charge distributions are calculated using the atom-dominated energy bands and atom-as well as orbital-projected density-of-states.
con configurations, which cover meta, ortho, para, and single cases, are chosen for a model investigation. In general, the third and fourth types, respectively, possess the lowest and highest ground state energies, i.e., the para-configuration is the most stable among them, or it is expected to be relatively easily synthesized in experimental growths. Moreover, the percentage is considered as a measure of the concentration of the ratio between the guest and host atoms are determined by the following formula:

$$n_C / (n_{tot} - n_C)$$

where $n_C$, $n_Si$, and $n_{tot} = n_C + n_{Si}$ are the numbers of carbon, silicon, and total atom, respectively, in the unit cell.

Carbon and silicon atoms, respectively, possess four outer orbitals of $[2p_x, 2p_y, 2p_z, 2s]$ and $[3p_x, 3p_y, 3p_z, 3s]$. Besides the pristine ones, the substitutions of carbon on silicene, as clearly illustrated in Figures 3A–L, will create the hybridized $\pi$ and $\sigma$ bondings $[2p_x-3p_x]$ and $(2s, 2p_x, 2p_y-3s, 3p_x, 3p_y]$ in silicene honeycomb lattice (the standard orbital hybridizations in Figures 2A). This seems to be responsible for the extremely non-uniform chemical/physical environments in an enlarged unit cell. Consequently, the Si-Si/Si-C bond lengths and the height difference between A and B sublattices might lie in specific ranges (Table 1). Specifically, the full C-substitution case, with the only uniform environment, is clearly different from the pristine one, since they, respectively, have the planar and buckled honeycomb lattices [Figures 1A,B; $\Delta = 0-0.48\,\AA$]. When the C-concentration is sufficiently low, the buckled structures will recover, such as the C:Si ratio lower than 15%. For the other conditions, the existence of buckling strongly depends on the concentration and configuration of the substitution.

In addition, the spin-dependent interactions are included in the numerical evaluations to see whether the magnetic configurations play an important role in the essential properties. However, the C- and Si-dependent spin configurations/interactions are fully suppressed by the very strong and complicated chemical bondings. That is to say, the spin-induced magnetic configuration is absent in any C-substituted silicene.

### 3.2. Band Structure Tailoring of Carbon-Substituted Silicene Systems

Apparently, the concentrations and configurations of carbon guest atoms play a crucial role in the diverse electronic configurations, which cover meta, ortho, para, and single cases, are chosen for a model investigation. In general, the third and fourth types, respectively, possess the lowest and highest ground state energies, i.e., the para-configuration is the most stable among them, or it is expected to be relatively easily synthesized in experimental growths. Moreover, the percentage is considered as a measure of the concentration of the ratio between the guest and host atoms are determined by the following formula:

$$n_C / (n_{tot} - n_C)$$

where $n_C$, $n_Si$, and $n_{tot} = n_C + n_{Si}$ are the numbers of carbon, silicon, and total atom, respectively, in the unit cell.

Carbon and silicon atoms, respectively, possess four outer orbitals of $[2p_x, 2p_y, 2p_z, 2s]$ and $[3p_x, 3p_y, 3p_z, 3s]$. Besides the pristine ones, the substitutions of carbon on silicene, as clearly illustrated in Figures 3A–L, will create the hybridized $\pi$ and $\sigma$ bondings $[2p_x-3p_x]$ and $(2s, 2p_x, 2p_y-3s, 3p_x, 3p_y]$ in silicene honeycomb lattice (the standard orbital hybridizations in Figures 2A). This seems to be responsible for the extremely non-uniform chemical/physical environments in an enlarged unit cell. Consequently, the Si-Si/Si-C bond lengths and the height difference between A and B sublattices might lie in specific ranges (Table 1). Specifically, the full C-substitution case, with the only uniform environment, is clearly different from the pristine one, since they, respectively, have the planar and buckled honeycomb lattices [Figures 1A,B; $\Delta = 0-0.48\,\AA$]. When the C-concentration is sufficiently low, the buckled structures will recover, such as the C:Si ratio lower than 15%. For the other conditions, the existence of buckling strongly depends on the concentration and configuration of the substitution.

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properties. Figure 2 shows the Brillouin zone scheme for many unit cells in which all the electronic states are plotted along Γ-K-M-Γ paths. In pristine monolayer silicene, the specific relations among the $\pi$, $\sigma$, and sp$^3$ bondings account for the main features of the band structure. The electron-hole symmetry around the Fermi level is only weakly modified at low energy, as illustrated in Figure 3A. The first pair of valence and conduction bands, being nearest to $E_F = 0$, are initiated from the stable K/K' valley. A very narrow band gap of $E_F \sim 0.01$ meV comes to exist between slightly separated Dirac cones, mainly due to the weak spin-orbital coupling (a single-particle interaction). This result is consistent with that obtained using the tight-binding model [20]. Additionally, they show the valence/conduction saddle M-point structure at $-1.02/0.59$ eV. Finally, the $\pi$ band is ended at the stable Γ valley, in which the $\pi$-band energy width for valence states, the energy spacing between the $\pi$-bands (three-band) widths could be well determined for $\Gamma$-K and $\Gamma$-M directions since there exists a weak, comparable in the [C,Si]-co-dominated energy bands. The higher/lower ionization energy of 2p$_z$/3p$_z$ orbitals further leads to the creation of a band gap for the honeycomb lattice, and the C-/Si-dominance of the $\pi/\pi^*$ bands (the red and blue circles). The first pair of energy bands are highly anisotropic. For example, the valence/conduction $\pi/\pi^*$ states, which are initiated from the K valley, show different group velocities along the KM and Kr directions, especially for the saddle point/the partially flat dispersion related to the M point. Furthermore, the $\pi$-band energy width is ($E_w = 3.71$ eV) according to the difference between the K- and $\Gamma$-point energies ($-1.50$ and $-5.20$ eV). Compared with a pristine 3p$_z$/3p$_z$ case ($E_w \sim 3.20$ eV in Figure 3A), the larger bandwidth might indicate the stronger 2p$_z$/3p$_z$ bonding. The two $\sigma$ bands, which arise from [3p$_x$, 3p$_y$]-[2p$_x$, 2p$_y$] hybridizations, appear at $E_F \sim -2.60$ eV initiated from the $\Gamma$ point, but remain fourfold degenerate electronic states there. Furthermore, the contributions from the different orbitals are comparable in the [C,Si]-co-dominated energy bands. The concave-downward parabolic valley near the $\Gamma$ point is dramatically transformed into concave-upward ones/the saddle-point forms along the K/M direction. Consequently, the first $\sigma$-bandwidth is approximately 4.30 eV. There exist direct crossings of the $\pi$ and $\sigma$ valence bands along any direction, e.g., Mr and Kr. This result clearly reveals no evidence of sp$^3$ bonding [25]. As a result, the fundamental properties of the [1:1] Si-C compound are dominated by the well-behaved $\pi$ and $\sigma$ bondings in the absence of sp$^3$ ones.

Electronic energy spectra are greatly enriched through the modulations of concentration and distribution configuration. The [2:4]-meta and [2:4]-ortho/para cases, as clearly displayed in Figures 3C,D, present finite- and zero-gap behaviors, respectively, corresponding to the highest occupied state and lowest one at the $\Gamma$ point ($E_g \sim 0.90$ eV) and the gapless Dirac-cone structure along the rK or rM direction. That the low-lying valence and conduction bands are initiated from the stable K and r valleys are associated with the zone-folding effect. According to the pristine and full-substitution configurations (Figures 3A,B), the valence and conduction bands in the energy range of $|E^{*\,\pi}| < 1.30$ eV, including the first pair, mainly arise from the [2p$_x$, 3p$_z$]-orbital hybridizations. Such bondings are responsible for the low-energy physical properties. This result is also confirmed by the orbital-projected density-of-states (discussed later in Figure 5B). It should be noted that the latter (Figure 5D) belongs to a zero-gap semiconductor because of the vanishing density of states at the Fermi level. The low-lying energy bands are dominated by the 3p$_z$ orbitals of silicon-host atoms because of the higher weight. More energy subbands come to exist under the enlarged unit cells. Therefore, the band crossings and anti-crossings would happen
FIGURE 3 | Electronic structures, with the dominance of silicon and carbon atoms (the blue circles and red triangle ones), for the C-substituted silicene systems; the (A) pristine, (B) [1:1]-, (C) [2:4]-meta-, (D) [2:4]-ortho-/para-, (E) [2:6]-meta-, (F) [2:6]-ortho-, (G) [2:16]-para-, (H) [2:16]-ortho-, (I) [2:16]-para-, (K) [1:7]-single-, (L) [1:17]-single substitution configurations.
frequently. In addition, it might be able to define the $n$-band energy widths through the $rK \rightarrow KM \rightarrow Mr$ direction (examinations from the 3p$_z$-projected density-of-states in Figures 5C,D), respectively, corresponding to 4.01 and 4.70 eV for the meta- and ortho-configurations. It would be very difficult or even meaningless, in characterizing bandwidths with a further
decrease of guest-atom concentration, as a result of more complicated valence subbands. Concerning the first π valence bands, they are roughly identified from the initial r-states at $E \sim -1.80 \text{ eV}$ for the meta-case (Figure 3C), while the very strong zone-folding effects forbid their characterizations under the ortho-condition (Figure 3D).

Very interestingly, two kinds of band properties are also revealed in the [2:6] cases, as clearly indicated in Figures 3E–G. The meta-, ortho- and para-configurations, respectively, exhibit the small-, narrow- and zero-gap behaviors (the finite- and zero-gap semiconductors) according to the first pair of energy bands nearest to the Fermi level. The first case has an indirect band gap of $E_\Gamma \approx 0.31 \text{ eV}$, which is determined by the specific energy spacing between the highest occupied state at the K point and the lowest unoccupied state at the r point (Figure 3E). Furthermore, the first valence band has an oscillatory energy dispersion. As a result, two stable valleys revealed in the [2:6] cases, as clearly indicated in Figures 3F and 3G. There are zero-gap semiconductors (the vanishing density-of-states at $E_F$) according to the zone-folding effects forbid their characterizations under the other deeper-/higher-energy electronic states might be closely related to the [2p$_x$, 2p$_y$, 2s, 3p$_x$, 3p$_y$, 3s] or eight orbitals in Si and C atoms. The carbon substitutions in silicene can only induce the modified Dirac cone structures, but not free carriers (the n- or p-type dopings).

3.3. Spatial Charge Density Distributions

The spatial charge density distributions are able to provide certain observable evidences regarding the existence of the impure/pure π and σ chemical bondings as well as their non-orthogonality or orthogonality. 

Pristine 2D silicene, as clearly displayed in Figure 4A with the $[x,z]$- and $[x,y]$-plane projections, shows the well-defined $3p_z$-$3p_x$ and $[3s, 3p]$-$[3s, 3p, 3p]$ orbital hybridizations, especially for the latter. In our notation, π is a symmetric distribution around the Si-Si bond center. Most of the charge density is accumulated between two silicon atoms (the red region), corresponding to the very strong σ bonding of three orbitals. The neighboring Si-atoms are also attracted together through the parallel $3p_z$ orbitals perpendicular to the $[x,y]$ plane, in which the π bonding appears in the outer region shown by the light green/blue color.

As a result of buckling, they have the weak, but significant $sp^3$ hybridizations under the non-orthogonality of π and σ chemical bondings. When the Si-Si bonds become Si-C ones under full substitution, π presents a dramatic transformation, is clearly illustrated in Figure 4B. The charge density is highly asymmetric with respect to the C-Si bond center, mainly owing to the different electron affinities of the guest and host atoms. There exist more carriers around the guest C-atoms (the red region); that is, electrons are transferred from silicon to carbon atoms. The whole C-Si bonds consist of a planar honeycomb lattice with a stronger σ bonding, compared with those of a pristine one (Figure 4A). The σ and π bondings could be roughly defined under the impure $2p_x$-$3p_y$ and $[2s, 2p_y, 2p_x]$-$[3s, 3p_y, 3p_x]$ orbital hybridizations, respectively. They are directly reflected in the π- and σ-electronic valence subbands, with direct crossings (Figure 3B). Most importantly, two kinds of chemical bondings are orthogonal to each other. Therefore, the $sp^3$ orbital hybridizations are negligible in the [1:1] case. Each Si-C bond has an identical chemical environment, i.e., only one chemical bond in a unit cell. This clearly illustrates that it is relatively easy to simulate the first-principles band structure using the tight-binding model [24].

When the carbon concentrations are decreased (Figures 4C–H), the existence of π and σ chemical bondings is relatively easily examined from the spatial charge densities. There exist C-Si, Si-Si, and even C-C bonds, for which the last ones are stable under the specific ortho cases (Table 1). The almost symmetric carrier distributions are clearly revealed between two silicon atoms for any concentration and configuration, in which they possess the lowest charge density among three kinds of chemical bonds. Similar phenomena appear for C-C bonds with the highest carrier densities, e.g., π values in Figures 4D,F at [2:4] and [2:6]
ortho conditions, respectively. Roughly speaking, the spatial charge densities in different chemical bonds are not sensitive to changes in various carbon substitutions. These further illustrates that the $\sigma$ and $\pi$ chemical bondings might be well separated from each other. Therefore, they could be roughly defined in the carbon-substituted silicene systems. As a result, the fundamental low-energy properties are expected to be dominated by the $\pi$-electronic states due to the modified Dirac cone structures. On the other hand, the different chemical bonds lead to complex orbital hybridizations and thus contribute to the difficulties in obtaining suitable phenomenological models. When the first principles electronic energy spectra along the high-symmetry paths are successfully simulated by the tight-binding model with the non-uniform and multi-/single-orbital hopping integrals [25], the diversified essential properties could be fully explored in the near future, e.g., the rich and unique magnetic quantization phenomena [23], as predicted/observed in layered graphene systems [26].

### 3.4. Density of States

There are four/five categories of van Hove singularities in carbon-substituted silicene systems or pristine one, as clearly illustrated in Figures 5A–F. The orbital- and atom-decomposed density-of-states are very useful in fully understanding the bonding-induced special structures. The critical points, i.e., the band-edge states, in the energy-wave vector space include the linear Dirac cone structure, local minima or maxima of parabolic energy dispersion, saddle points, constant energy loops, which are

![Figure 4](image_url)
closely related to band anticrossings, and partially flat bands (Figures 3A–L). Their densities-of-states generate the V-shape form, discontinuous shoulders, logarithmic divergent peaks, asymmetric peaks in the square root divergence, and delta-function-like peaks, respectively. A pure monolayer silicene in Figure 5A displays an almost linear $E$-dependence across the Fermi energy with a vanishing density-of-states (a quasi-V shape in the range $-0.5 \leq E \leq 0.5$ eV; the purple curve of $3p_z$ orbitals), a logarithmic symmetric $\pi$-peak/$\pi^*$-peak at $-1.02$/$0.59$ eV, the $[\pi, \sigma]$-mixing created square root asymmetric peaks at ($-2.20, -2.65, -3.15$ eV). The red, green and blue curves of $(3p_x, 3p_y, 3p_z)$ orbitals, the $\Gamma$-valley $\pi$ shoulder at $-3.20$ eV, the initial $\sigma$-[$3p_x, 3p_y$] shoulder at $-1.03$ eV at the $\Gamma$ point, their M saddle point symmetric peak at $-2.47$ eV and the K valley shoulder at $-4.40$ eV. Consequently, the $\pi$ and $\sigma$ bandwidths are $-3.15$ and $3.36$ eV, respectively. It should be noted that the $3s$ orbitals (the red curve) are frequently accompanied by $[3p_x, 3p_y]$ ones, but their contributions become significant at the deeper/higher energies, e.g., density-of-states within $E < -3.0$ eV. The above mentioned features of van Hove singularities further illustrate the well behaved $\pi$ and $\sigma$ chemical bondings and their weak, but important hybridization. The structural features, energy and number of van Hove singularities exhibit a dramatic transformation under full carbon substitution, as indicated in Figure 5B. The special structures cover vanishing density-of-states within a band gap of $E_g \sim 2.56$ eV at the K/K' valley, the initial $\pi$ shoulder/delta function-like $\pi$ peak at $-1.26/1.26$ eV (also shows the low-lying $\pi$ and $\sigma^*$ bands in Figure 3B), the $-1.95$ eV symmetric $\pi$ peak in the logarithmic divergence, the final $\pi$ shoulder at $-5.00$ eV, the first $\sigma$ shoulder at $-2.75$ eV, the $-4.10$ eV logarithmic peak, and the second discontinuous structure at $-7.01$ eV. We also, observe that the first valence/conduction structure is dominated by the C-2p$_z$ orbitals/Si-3p$_z$ ones due to an obvious difference of ionization energy. The widths of the $\pi$ and first $\sigma$ bands are $-3.74$ and $4.26$ eV, respectively. Additionally, there is no evidence of $\pi$-$\sigma$ band mixing. This is mainly due to the absence of the simultaneous four-orbital structures. The fact that the sp$^3$ bonding is absent agrees with the direct $\pi$-$\sigma$ subband crossings (Figure 3B).
Within the whole energy range, the van Hove singularities become more complex during the decrease of guest-C-atom concentration, as a result of zone-folding effects as well as the significant $[3s, 3p_x, 3p_y, 3p_z] - [2s, 2p_x, 2p_y, 2p_z]$ multi-orbital hybridizations. For example, the $[2s]$-meta and $[2s]$-ortho configurations, as clearly illustrated in Figures 5C,D, exhibit diverse low-energy van Hove singularities arising from the dominant $3p_z-2p_z$ chemical bonding. The former has a $\pi$-electronic zero density-of-states in the 0.90 eV-gap region (the $\Gamma$ valley in Figure 3C), a threshold valence shoulder at $-0.45$ eV (the first composite conduction state structure due to the discontinuous shoulder and delta function-like peak at $0.45$ eV), a strong logarithmic peak at $-1.41$ eV, as well as the second and third step structures at $-1.69$ and $-2.71$ eV, respectively. Regarding the latter, the $3p_z-2p_z$-diversified van Hove singularities show a gapless V-shape (a Dirac cone energy spectrum in Figure 3D), the first valence shoulder at $-0.5$ eV (the initial conduction shoulder at $0.30$ eV), the logarithm-step composite structure at $-1.01$ eV, the symmetric peak arising from two opposite shoulders at $-1.32$ eV, a similar one at $-2.10$ eV, and the $-2.65$ eV asymmetric peak in the square root form. The widths of the $\pi$-band in the former and latter cases are estimated to be $-4.05$ and $4.70$ eV, respectively. Furthermore, the first $\sigma$-bands are wider than $4.5$ eV. Obviously, the low-energy physical phenomena are dominated by the $3p_z$ orbitals of Si-host atoms.

As the guest-atom concentration is declined, there appear additional van Hove singularities. Overall, in this way, one is able to characterize the width of the $\pi$-band from the effective distributions of the $[3p_z, 2p_z]$ orbitals for any concentration and configuration (Figures 5A–L). However, the opposite is true for the first $\sigma$-band width except for full substitution and the pristine cases (Figures 5A,B). Certain van Hove singularities, close to the Fermi level, are very useful to comprehend the band-edge states in the first pair of the valence and conduction bands. The main features cover the vanishing density-of-states at/ across the Fermi level (Figures 5C through E)/(Figures 5D through G), the electron-hole asymmetry near the first pair of clearly identifiable shoulders, the prominent $\pi$ peak in logarithmic form, the second and third shoulders and so on. Finally, the dip structure at $E_F$ with a very small gap comparable to the broadening factor, will come to exist for a sufficiently low concentration, e.g., the almost gapless behavior in the $[1:17]$ case (Figure 5L). We also noticed that the single-particle interactions of spin-orbital couplings cannot create any significant effects on the electronic properties and thus the other essential properties.

4. CONCLUDING REMARKS

The geometric and electronic properties of carbon-substituted silicene are investigated using DFT calculations. The systems present unusual geometric properties, which are directly reflected in the spatial charge distributions. At high carbon-concentrations, the planar structure clearly indicates a very small variation in the sigma bonding of C-$[2s, 2p_x, 2p_y]$ orbitals. Therefore, they hardly take part in Si-C bonds and lead the C-C bond lengths in substitution cases to remain almost unchanged. The above mentioned important results directly reveal critical mechanisms, i.e., the multi-orbital hybridizations of $sp^3$-in Si-C bonds, $sp^3$-$sp^3$ in Si-Si bonds, and $sp^3$-$sp^2$ in C-C bonds.

All substitution results in semiconducting behavior with a finite or zero band gap in which the Dirac cone structure presents a deviation from the $\Gamma$ point, a strong distortion, or even destruction. The number of valence and conduction energy subbands remains the same after chemical substitutions. Furthermore, they are co-dominated by the C-guest and Si-host atoms. High-resolution ARPES measurements are very useful in verifying the low-lying valence bands near/crossing the Fermi level along $\Gamma K$ and $\Gamma M$ path and the rigid sigma bands initiated from the $\Gamma$ valley.

Several unusual van Hove singularities in the atom and orbital decomposed density-of-states are created under the C-guest-atom chemical substitution. The strong bonding evidence is totally destroyed by substitutions except for the very diluted Si-adatoms. They are replaced by a finite density of states at $E_F = 0$, many shoulders, and peak structures. Furthermore, they are co-dominated by the four Si-$[3s, 3p_x, 3p_y, 3p_z]$ orbitals and the single C-$2p_z$ orbital, since their contributions are merged together. The above-mentioned significant features further support and illustrate the $sp^3$-$sp^3$ and $sp^3$-$sp^2$ multi-orbital hybridizations in Si-C bonds and C-C bonds, respectively. The predicted van Hove singularities could be verified by the high-resolution STS experiments [27].

DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

AUTHOR CONTRIBUTIONS

HP: collected the data, performed the analysis, wrote the paper. SL: contributed data or analysis tools. GG: performed the analysis, wrote the paper (checking English grammar). NK: contributed data or analysis tools. ML: methodology, checked and evaluated results, wrote the paper.

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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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