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Magnetic Monopole Search with the Full MoEDAL Trapping Detector in 13 TeV pp Collisions Interpreted in Photon-Fusion and Drell-Yan Production

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MoEDAL is designed to identify new physics in the form of stable or pseudostable highly ionizing particles produced in high-energy Large Hadron Collider (LHC) collisions. Here we update our previous search for magnetic monopoles in Run 2 using the full trapping detector with almost four times more material and almost twice more integrated luminosity. For the first time at the LHC, the data were interpreted in terms of photon-fusion monopole direct production in addition to the Drell-Yan-like mechanism. The MoEDAL trapping detector, consisting of 794 kg of aluminum samples installed in the forward and lateral regions, was exposed to 4.0 fb⁻¹ of 13 TeV proton-proton collisions at the LHCb interaction point and analyzed by searching for induced persistent currents after passage through a superconducting magnetometer. Magnetic charges equal to or above the Dirac charge are excluded in all samples. Monopole spins 0, ½, and 1 are considered and both velocity-independent and-dependent

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The existence of a magnetically charged particle would add symmetry to Maxwell’s equations and explain why electric charge is quantized in nature, as shown by Dirac in 1931 [1]. Dirac predicted the fundamental magnetic charge number (or Dirac charge) to be \( (e/2a_{em}) \approx 68.5 \) where \( e \) is the proton charge and \( a_{em} \) is the fine-structure constant. Consequently, in SI units, the magnetic charge can be written in terms of the dimensionless quantity \( g_D \) as \( q_m = n g_D e c \) where \( n \) is an integer number and \( c \) is the speed of light in vacuum. Because \( g_D \) is large, a fast monopole can induce ionization in matter thousands of times higher than a particle carrying the elementary electric charge.

It has subsequently been shown by ’t Hooft and Polyakov that the existence of the monopole as a topological soliton is a prediction of theories of the unification of forces [2–5]. For a unification scale of \( 10^{16} \) GeV such monopoles would have a mass \( M \) in the range \( 10^{17}–10^{18} \) GeV. In unification theories involving a number of symmetry-breaking scales [6–8], monopoles of much lower mass can arise, although still beyond the reach of the Large Hadron Collider (LHC). However, an electroweak monopole has been proposed [9–12] that is a hybrid of the Dirac and ’t Hooft–Polyakov monopoles [2,3] with a mass potentially accessible at the LHC and a minimum magnetic charge \( 2g_D \), underlining the importance of searching for large magnetic charges at the LHC.

There have been extensive searches for monopole relics from the early Universe in cosmic rays and in materials [13,14]. The LHC has a comprehensive monopole search program using various techniques devised to probe TeV-scale monopole masses for the first time [15–17]. The results obtained by MoEDAL using 8 TeV \( pp \) collisions allowed the previous LHC constraints on monopole pair production [18] to be improved to provide limits on monopoles with \( |g| \leq 3g_D \) and \( M \leq 3500 \) GeV [19], where \( g = q_m e c \). At 13 TeV LHC energies, MoEDAL extended the limits to \( |g| \leq 5g_D \) and masses up to 1790 GeV assuming Drell-Yan (DY) production [20,21].

In addition to the forward part used in previous analyses [20,21], the exposed Magnetic Monopole Trapper (MMT) volume analyzed here includes lateral components increasing the total aluminum mass to 794 kg; a schematic view is provided in the Supplemental Material [22]. All 2400 trapping detector samples were scanned in 2018 with a dc SQUID long-core magnetometer (2G Enterprises Model 755) installed at the Laboratory for Natural Magnetism at ETH Zurich. The measured magnetometer response is translated into a magnetic pole \( P \) in units of Dirac charge by multiplying by a calibration constant \( C \). Calibration was performed using two independent methods, described in more detail in Ref. [23]. The first method adds measurements performed at 1 mm intervals using a dipole sample of known magnetic moment \( \mu = 2.98 \times 10^{-6} \) A m² to obtain the response of a single magnetic pole of strength \( P = 9.03 \times 10^5 g_D \), based on the superposition principle. The second method measures directly the effect of a magnetic pole of known strength using a long thin solenoid providing \( P = 32.4 g_D/\mu A \) for various currents ranging from 0.01 to 10 \( \mu \)A. The results of the calibration measurements, with the calibration constant obtained from the first method, are shown in Fig. 1. The two methods agree within 10%, which can be considered as the calibration uncertainty in the pole strength. The magnetometer response is measured to be linear and charge symmetric in a range corresponding to 0.3–300\( g_D \). The plateau value of the calibration dipole sample was remeasured regularly during the campaign and was found to be stable to within less than 1%.

Samples were placed on a carbon-fiber movable conveyor tray for transport through the sensing region of the magnetometer, three at a time, separated by a distance of 46 cm. The transport speed was set to the minimum available of 2.54 cm/s, as it was found in previous studies that the frequency and magnitude of possible spurious offsets increased with speed [21]. The magnetic charge contained in a sample is measured as a persistent current in the superconducting coil surrounding the transport axis. This is defined as the difference between the currents measured after (\( I_2 \)) and before (\( I_1 \)) passage of a sample.
through the sensing coil, after adjustment for the corresponding contributions of the empty tray $I_{\text{tray}}^2$ and $I_{\text{tray}}^1$. Expressed in Dirac charges, the magnetic pole strength contained in a sample is thus calculated as $P = C\left(\langle I_2 \rangle - \langle I_1 \rangle\right) - \left(\langle I_{\text{tray}}^2 \rangle - \langle I_{\text{tray}}^1 \rangle\right)$, where $C$ is the calibration constant. All samples were scanned twice, with the resulting pole strengths shown in Fig. 2. The samples are not subject to any external magnetic field when passed through the superconducting loop that could possibly unbind a monopole from the material. The observed outliers may be due to spurious flux jumps occurring by ferromagnetic impurities in the sample, noise currents in the SQUID feedback loop, and other known instrumental and environmental factors [19]. Whenever the measured pole strength differed from zero by more than 0.4$g_D$ in either of the two measurements, the sample was considered a candidate. This procedure strongly reduces the possibility of false negatives. A total of 87 candidate samples were thus identified. A sample containing a genuine monopole would consistently yield the same nonzero value for repeated measurements, while values repeatedly consistent with zero would be measured when no monopole is present. The candidates were scanned repeatedly and it was found that the majority of the measured pole strengths for each candidate lay below the threshold of 0.4$g_D$, as shown in Fig. 3. Using the multiple candidate measurements to model the probability distribution of pole strength values, in the worst case in which one misses a monopole three times out of five measurements, an estimated false-negative probability of less than 0.2% is obtained for magnetic charges of $1g_D$. We are thus able to exclude the presence of a monopole with $|g| \geq g_D$.

The trapping detector acceptance, defined as the probability that a monopole of given mass, charge, energy, and direction would end its trajectory inside the trapping volume, is determined from the knowledge of the material traversed by the monopole [19,24] and the ionization energy loss of monopoles when they go through matter [25–28], implemented in a simulation based on GEANT4 [29]. For a given mass and charge, the pair-production model determines the kinematics and the overall trapping acceptance obtained. The uncertainty in the acceptance is dominated by uncertainties in the material description [19–21]. This contribution is estimated by performing simulations with hypothetical material conservatively added and removed from the nominal geometry model.

A DY mechanism (Fig. 4, left) is traditionally employed in searches as it provides a simple model of monopole pair production [17–21]. In the interpretation of the present search, photon fusion (γγ) (Fig. 4, right) [30] is considered in addition to DY for the first time at the LHC, having previously only been used in a collider search for direct monopole production at the H1 experiment at HERA [31].
An earlier D0 analysis of diphoton events at Tevatron used virtual-monopole production via photon fusion to set limits on the monopole mass [32].

The different direct production mechanisms, DY and $\gamma\gamma$, imply different kinematical distributions, as shown in the Supplemental Material [22]. However, due to the considerably higher cross section for $\gamma\gamma$ over most of the spin and mass range [30], the $\gamma\gamma$ mechanism is dominant for setting mass bounds. For both processes the cross sections are computed using the Feynman-like diagrams shown in Fig. 4, although the large monopole coupling to the photon places such calculations in the nonperturbative regime. A proposal involving the thermal Schwinger production of monopoles in heavy-ion collisions [33], which does not rely on perturbation theory, overcomes these limitations [34,35]. Here the subsequent combination of the production processes implies merely summing the total cross sections computed from these leading-order diagrams, respecting at the same time the different kinematics. No interference terms are considered.

As in the previous MoEDAL MMT analysis [21], monopoles of spins 0, $\frac{1}{2}$, and 1 are considered, with the

![Graphs showing production cross-section upper limits at 95% C.L. for the combined DY and $\gamma\gamma$ monopole pair production model with $\beta$-independent (left) and $\beta$-dependent (right) couplings in 13 TeV $pp$ collisions as a function of mass for spin-0 (top), spin-$\frac{1}{2}$ (middle), and spin-1 monopoles (bottom). The colors correspond to different monopole charges. The solid lines are cross-section calculations at leading order.](image)
values of the monopole magnetic moment assumed to be zero for spin $\frac{1}{2}$ and one for spin 1, i.e., equal to the Standard Model values for particles with these spins. Models were generated in MadGraph5 [36] using the Universal FeynRules Output described in Ref. [30]. We used tree-level diagrams and the parton distribution functions NNPDF23 [37] and LUXqed [38] for the DY and $\gamma\gamma$ production processes, respectively. LUXqed is determined in a model-independent manner using $e^+p$ scattering data and is the most accurate photon PDF available to date. In addition to a pointlike quantum electrodynamics coupling, we have also considered a modified photon-monopole coupling in which $g$ is substituted by $\beta g$ with $\beta = \sqrt{1 - (4M^2/s)}$ (where $M$ is the mass of the monopole and $\sqrt{s}$ is the invariant mass of the monopole-antimonopole pair), as in the previous MoEDAL analysis [21]. This “$\beta$-dependent coupling” illustrates the range of theoretical uncertainties in monopole dynamics close to threshold. Moreover, in the case of spin-$\frac{1}{2}$ and spin-1 monopoles, together with the introduction of a magnetic-moment phenomenological parameter $\kappa$, the $\beta$-dependent coupling may lead to a perturbative treatment of the cross-section calculation [30].

The behavior of the acceptance as a function of mass has two contributions: the mass dependence of the kinematic distributions, and the energy loss, which decreases as the monopole slows down. For monopoles with $|g| = g_D$, acceptance losses predominantly come from punching through the trapping volume, resulting in the acceptance reaching a maximum of 3.8% at low masses (high energy loss) and at high masses (low initial kinetic energy), having a minimum at around 3 TeV. The reverse is true for monopoles with $|g| > g_D$ that predominantly stop in the upstream material and for which the acceptance is highest (up to 4.5% for $|g| = 2g_D$, 4% for $|g| = 3g_D$, and 4% for $|g| = 4g_D$) for intermediate masses (around 2 TeV). The acceptance remains below 0.1% over the whole mass range for monopoles carrying a charge of $6g_D$ or higher because they cannot be produced with sufficient energy to traverse the material upstream of the trapping volume. In this case, the systematic uncertainties become too large and the interpretation ceases to be meaningful. The dominant source of systematic uncertainties comes from the estimated amount of material in the GEANT4 geometry description, yielding a relative uncertainty of $\sim 10\%$ for $1g_D$ monopoles [19]. This uncertainty increases with the magnetic charge reaching a point (at $6g_D$) where it is too large for the analysis to be meaningful. The spin dependence is solely due to the different event kinematics. The reader is referred to the Supplemental Material for more details on kinematic distributions and acceptances [22].

Production cross-section upper limits at 95% confidence level (C.L.) for combined Drell-Yan and photon-fusion monopole production with the two coupling hypotheses ($\beta$-independent, $\beta$-dependent) and three spin hypotheses (0, $\frac{1}{2}$, 1) are shown in Fig. 5. They are extracted from the knowledge of the acceptance estimates and their uncertainties, the delivered integrated luminosity 4.0 fb$^{-1}$, measured at a precision of 4% [39], corresponding to the 2015–2017 exposure to 13 TeV $pp$ collisions, the expectation of strong binding to aluminum nuclei [40] of monopoles with velocity $\beta \leq 10^{-3}$, and the nonobservation of magnetic charge $\geq 9g_D$ inside the trapping detector samples. Acceptance loss is dominated by monopoles punching through the trapping volume for $|g| = g_D$ while it is dominated by stopping in upstream material for higher charges, explaining the shape difference. Analogous limits considering DY production only are given in the Supplemental Material [22] to facilitate comparison with previous MoEDAL [19–21] and ATLAS [17,18] results.

Production cross sections computed at leading order are shown as solid lines in Fig. 5. Using these cross sections and the limits set by the search, indicative mass limits are extracted and reported in Table I for magnetic charges up to 5$g_D$. No mass limit is given for the spin-0 and spin-$\frac{1}{2}$ 5$g_D$ monopole with standard pointlike coupling, because in this case the low acceptance at small mass does not allow MoEDAL to exclude the full range down to the mass limit set at the Tevatron of around 400 GeV for DY models [41]. We note that these mass limits are only indicative, since they rely upon cross sections computed (at leading order) using perturbative field theory when the monopole-photon coupling is too large to justify such an approach.

In summary, the aluminum elements of the MoEDAL trapping detector exposed to 13 TeV LHC collisions during the period 2015–2017 were scanned using a SQUID-based magnetometer to search for the presence of trapped magnetic charge. No candidates survived our

| Process/coupling | Spin | 95% C.L. mass limits (GeV) |
|------------------|-----|---------------------------|
| $DY$             | 0   | 790 1150 1210 1130        |
|                  | $\frac{1}{2}$ | 1320 1730 1770 1640  |
|                  | 1   | 1400 1840 1950 1910 1800  |
| $DY$ $\beta$ dep. | 0   | 670 1010 1080 1040 900  |
|                  | $\frac{1}{2}$ | 1050 1450 1530 1450  |
|                  | 1   | 1220 1680 1790 1780 1710  |
| $DY + \gamma\gamma$ | 0   | 2190 2930 3120 3090  |
|                  | $\frac{1}{2}$ | 2420 3180 3360 3340  |
|                  | 1   | 2920 3620 3750 3740  |
| $DY + \gamma\gamma$ $\beta$ dep. | 0   | 1500 2300 2590 2640  |
|                  | $\frac{1}{2}$ | 1760 2610 2870 2940 2900  |
| $DY + \gamma\gamma$ $\beta$ dep. | 1   | 2120 3010 3270 3300 3270  |
scanning procedure and cross-section upper limits as low as 11 fb were set, improving previous limits of 40 fb also set by MoEDAL [21]. We considered the combined photon-fusion and Drell-Yan monopole-pair direct production mechanisms, the former process for the first time at the LHC. Consequently, mass limits in the range 1500–3750 GeV were set for magnetic charges up to $5 g_D$ for monopoles of spins 0, $\frac{1}{2}$, and 1—the strongest to date at a collider experiment [42] for charges ranging from two to five times the Dirac charge. For a comparison, previous DY mass limits set by MoEDAL at 13 TeV ranged from 450 to 1790 GeV [21].

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\section*{Acknowledgments}

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