Achievement of Alternative Configurations of Vehicles on Multiple Lanes

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Heavy traffic congestion daily occurs at merging sections on highway. For releasing this congestion, possibility of alternative configuration of vehicles on multiple-lane road is discussed in this paper. This is the configuration where no vehicles move aside on the other lane. It has a merit in making smooth merging at an intersection or a junction due to so-called the "zipper effect". We show, by developing a cellular automaton model for multiple lanes, that this configuration is achieved by simple local interactions between vehicles neighboring each other. The degree of the alternative configuration in terms of the spatial increase of parallel driving length is studied by using both numerical simulations and mean field theory. We successfully construct a theoretical method for calculating this degree of the alternative configuration by using cluster approximation. It is shown that the theoretical results coincide with those of the simulations very well.

I. INTRODUCTION

In recent years, traffic dynamics has attracted much interest of physicists, and thus it has been studied more and more diligently [1, 2]. Researchers have mainly developed the analysis of the traffic flow on one-lane road by using continuous models [3] and cellular automaton (CA) models [4]. Recently, the analysis of the traffic flow on multiple lane road at an intersection or a junction is considered as one of the important study of traffic flow for releasing traffic congestion. Kita modeled merging interactions with one game theory [5]. Hidas investigated vehicle interactions in merging and weaving by using agent based simulations [6]. Davis introduced the cooperation in merging by adding interactions between pairs of vehicles in opposite lanes [7]. He showed that velocity of vehicles in cooperative merging was higher than that in no cooperation.

However, these previous works were qualitative and did not study the configuration of vehicles in detail on two lanes before an intersection or a junction which determines the efficiency of merging. Among various configurations, the alternative configuration is the best because it realizes the smooth "zipper" merging, which is the merging of vehicles by turns on one lane and on the opposite lane. Thus, the transformation of the configuration toward the alternative configuration is significant for the improvement of the congested flow at a junction.

The purpose of this paper is to propose a simple and natural method for achievement of the alternative configuration of vehicles on two lanes. Then we study the method by both computer simulations and a mean field theory. The communication of vehicles on two lanes is studied by the CA model which we call the multiple lanes stochastic optimal velocity (MLSOV) model. This is an extension of SOV model proposed in [8] by introducing the interactions between vehicles on the opposite lane.

This paper is organized as follows. In Sec. II we define MLSOV model, and results of simulations of two-lane flow before an intersection is presented in Sec. III. Then in Sec. IV we calculate the degree of alternative configuration by using cluster approximation and compare it with the results of the simulations. Sec. V is devoted to the concluding discussions.

II. A MULTIPLE LANES CA MODEL WITHOUT LANE CHANGE

We propose here the MLSOV model by introducing interactions between two lanes. We choose the SOV model as a basis of our extended model because it is one of the simplest model whose fundamental diagram, i.e. flow versus density plot, shows the metastable state observed in real traffic data [8]. MLSOV model represents the interactions of vehicles on two lanes by seeing the ones on the opposite lane each other. Note that we do not take into account of the lane change behaviour in this paper because we focus only on the achievement of the alternative configuration of vehicles before an intersection. In the model, the movement of all vehicles on both lane 1 and lane 2 is ruled as follows. \( i \)-th vehicle on each lane moves one cell in front in one time step with probability \( v_i^t \) at time \( t \) provided that the next cell is empty. Thus the movement is described as

\[
x_i^{t+1} = \begin{cases} x_i^t + 1, & \text{with probability } v_i^t \\ x_i^t, & \text{with probability } 1 - v_i^t \end{cases},
\]

where \( x_i^t \) is the position of \( i \)-th vehicle at time \( t \) as shown in figure [9]. \( v_i^t \) is called intension and normalized as \( 0 \leq v_i^t \leq 1 \). \( i+1 \)-th vehicle is located at the cell which is \( \Delta x_{i+1}^{t,i} \) cells ahead of \( i \)-th vehicle on the same lane as shown in figure [10]. The length of one cell is set as 7.5 m.
In the MLSOV model, the time evolution of \( v_i^t \) is determined not only by \( i \)-th and \( i + 1 \)-th vehicle but also \( j + 1 \)-th vehicle which is the closest vehicle to \( i \)-th vehicle on the neighboring lane, with the distance \( \Delta x_{2,i} \) cells ahead as shown in figure 1. \( v_i^t \) is given as

\[
v_i^{t+1} - v_i^t = a \left\{ V(\Delta x_{1,i}^t, \Delta x_{2,i}^t) - v_i^t \right\},
\]

(2)

where \( V(\Delta x_{1,i}^t, \Delta x_{2,i}^t) \) is the two-lanes Optimal Velocity (OV) function \([3]\), \( v_i^t \) tends to approach \( V(\Delta x_{1,i}^t, \Delta x_{2,i}^t) \) with the increase of the sensitivity parameter \( a \) (0 \( \leq a \leq 1 \)). We define for convenience \( \Delta v \) for communicating vehicles between lane 1 and lane 2 is taken into account for eliminating \( \Delta x_{1,i} \) cells ahead of \( i \)-th vehicle on the same lane. \( j + 1 \)-th vehicle is the closest vehicle to the \( i \)-th vehicle with the distance \( \Delta x_{2,i} \) cells ahead on the neighboring lane.

The part of two-lane road indicated in figure 2 (b) is partitioned into identical cells as shown in figure 2 (c). The cell size is fixed and one cell can accommodate at most one vehicle. The boundaries are open, and each vehicle is updated in parallel, and it enters in the leftmost cell on lane 1 or lane 2, and moves straight ahead without changing lanes, and goes out of the rightmost cell. Although the vehicles cannot change lanes, vehicles on one lane can interact with the ones on the opposite lane by looking at the behaviour of these vehicles.

All the parameters are defined in figure 2 (c). The length of this section is \( d \), and the leftmost cells are at \( x = 0 \) and the rightmost cells are at \( x = d - 1 \).

In the simulations we choose the worst injection condition for merging, i.e., a vehicle enters in \( x = 0 \) simultaneously on lane 1 and lane 2 with the probability \( \alpha \) as long as both leftmost cells are empty. This injection is considered to be the most severe configuration for attaining the alternative configuration at the end of the road where merging occurs. We will demonstrate in the following that the alternative configuration is surely achieved in all cases of the injection. The probability of going out of the rightmost cell of lane \( i \) is set as \( \beta_i \) (\( i = 1, 2 \)).

Next, we define two important quantities in the simulations. Firstly, we quantify the degree of the alternative configuration as shown below. Here we consider special two cases of the time evolution of \( v_i^t \) with the initial condition of \( v_i^0 = \nu \). In the case \( a = 0 \), MLSOV model corresponds to the single-lane Asymmetric Simple Exclusion Process (ASEP) \([9]\), since each vehicle moves irrespective of neighboring ones and \( v_i^t \) is given as

\[
v_i^t = \begin{cases} 
0, & \Delta x_{1,i}^t = 0 \\
\nu, & \Delta x_{1,i}^t \geq 1 \text{ and } \Delta x_{2,i}^t = 0 \\
q, & \Delta x_{1,i}^t \geq 1 \text{ and } \Delta x_{2,i}^t = 1 \\
p, & \Delta x_{1,i}^t \geq 1 \text{ and } \Delta x_{2,i}^t \geq 2,
\end{cases}
\]

(3)

which is simple enough to achieve the alternative configuration as shown below. Here we consider special two cases of the time evolution of \( v_i^t \) with the initial condition of \( v_i^0 = \nu \). In the case \( a = 0 \), MLSOV model corresponds to the single-lane Asymmetric Simple Exclusion Process (ASEP) \([9]\), since each vehicle moves irrespective of neighboring ones and \( v_i^t \) is given as

\[
v_i^t = \begin{cases} 
0, & \Delta x_{1,i}^t = 0 \\
\nu, & \Delta x_{1,i}^t \geq 1 \text{ and } \Delta x_{2,i}^t = 0 \\
q, & \Delta x_{1,i}^t \geq 1 \text{ and } \Delta x_{2,i}^t = 1 \\
p, & \Delta x_{1,i}^t \geq 1 \text{ and } \Delta x_{2,i}^t \geq 2.
\end{cases}
\]

(4)

In the case \( a = 1 \), MLSOV model corresponds to a two-lane version of the Zero Range Process (ZRP) \([10]\), and \( v_i^t \) is given as

\[
v_i^t = \begin{cases} 
0, & \Delta x_{1,i}^t = 0 \\
\nu, & \Delta x_{1,i}^t \geq 1 \text{ and } \Delta x_{2,i}^t = 0 \\
q, & \Delta x_{1,i}^t \geq 1 \text{ and } \Delta x_{2,i}^t = 1 \\
p, & \Delta x_{1,i}^t \geq 1 \text{ and } \Delta x_{2,i}^t \geq 2.
\end{cases}
\]

(5)

Note that in the case \( a = 0 \), the model is exactly solvable and we can theoretically calculate the stationary state and hence the fundamental diagram. In the case \( a = 1 \), if we neglect the effect of the other lane, then we can also solve the model exactly.

III. SIMULATIONS

Our idea for making the traffic flow smooth is to draw the compartment line between the lanes as shown in figure 2. The line prohibits vehicles from changing lanes, and this will be used for communicating vehicles between lanes and expected to induce the zipper effect at the end of the line. Then, the disordered lane change at the merging area will be smooth and becomes safe.
We obtained $Ge(x)$ versus $x$ and $\bar{v}$ versus $x$ by using numerical simulations. The conditions of the simulations are as follows. Three sets of parameters in the OV function are chosen as $p = 1$ and $(q, r) = \{(0.99, 0.99), (0.8, 0.8), (0.5, 0.5)\}$. Moreover, five kinds of the value of the sensitivity parameter are chosen as $a = \{0, 0.001, 0.01, 0.1, 1\}$. The length of the road is set as $d = 100$. The probability of simultaneous injection on both lanes is given as $\alpha = 0.05$. Vehicles enter in the leftmost cells with the initial injection $p$ which appears in $\beta_i$. $\beta_i$ $(i = 1, 2)$ is given as each vehicle’s intension $v$ on the cell at $x = d - 1$. We see that traffic flow is always in a free flow under this $\alpha$ and $\beta$. The number of iterations of the simulations is $M = 10$, and the period for measurement is between $T_1 = 100000$ and $T_2 = 200000$.

The results of the simulations are shown in figure 6. From figure 6 we see that $Ge(x)$ increases monotonically from 0 to 1 as $x$ become larger in the cases of $a = \{0.001, 0.01, 0.1, 1\}$, and stays constant at 0 regardless of $x$ in the cases of $a = 0$. The sharpness of the increase of $Ge(x)$ becomes larger as $a$ becomes larger, and as $q(= r)$ becomes smaller from figure 6(a)-(c). $\bar{v}(x)$ has one minimum value in the case of $a = \{0.001, 0.01, 0.1, 1\}$, and stays constant at $\bar{v}(x) = 1$ in the case of $a = 0$ from figure 6(d)-(f). The position $x$ which gives the minimum value of $\bar{v}$ becomes smaller as $a$ becomes larger, and as $q(= r)$ becomes smaller. The minimum value of $\bar{v}(x)$ becomes smaller as $a$ becomes larger, and as $q(= r)$ becomes smaller.

Figure 6 (a)-(c) clearly show the achievement of the alternative configuration toward the spatial axis. These figures suggest us how we realize the smooth merging at an intersection or a junction. The sufficient length of compartment line for communicating is significant for
the achievement of the alternative configurations. For instance, if we set the target $Ge$ as $Ge_{tar} = 0.9$ in the case of $a = 0.1, p = 1$, and $q = 0.5$, which are typical values of real traffic, then we achieve this value of $Ge$ by drawing the line of 22 cell length which is equal to 165 m. Note that this alternative configuration is formed only by the local interaction within the range of $\Delta x_2 \leq 1$ of each vehicle. The relationships between $a$ and the sharpness of the increase of $Ge(x)$ suggest that the length of line necessary for realizing the complete alternative configuration becomes shorter if vehicles respond to the ones on the opposite lane more quickly. The relationships between $q$ and the sharpness of the increase of $Ge(x)$ suggest that this length of line becomes shorter if vehicles decelerate more strongly in the case of $\Delta x_2 \leq 1$.

The spatial change of $\tilde{v}(x)$ is caused by the interactions between the vehicles neighboring each other in two steps. Firstly, $i$-th vehicle enters into $x = 0$ with $\Delta x_{2,i} = 0$ and slows down due to the OV function $V < 1$ to apart from the ones on the neighboring lane. It keeps slowing down until $\Delta x_{2,i} \geq 2$. Then, $\Delta x_{2,i} = 2$ is attained, and it starts to accelerate with $V = 1$. These interactions generate the minimum value of $\tilde{v}(x)$ at the point where $\Delta x_2$ of the most vehicle becomes 2. Vehicles slow down more quickly as the response parameter $a$ becomes larger, and $q (= r)$ becomes smaller. Thus, $x$ which give the minimum value of $\tilde{v}(x)$ becomes smaller as $a$ becomes larger, and as $q$ becomes smaller.

IV. ANALYSIS OF ALTERNATIVE CONFIGURATIONS WITH CLUSTER APPROXIMATION

In this section, we theoretically study the achievement of alternative configurations by using cluster approximation. In the approximation, the two-lane road as shown in figure [2] is divided into the four cells at $x = \{k, k + 1\}$ ($k = 0, 1, \ldots, d - 2$) which is denoted by $C_k$. Then, the stationary state on $C_k$ is calculated in the order of $k = 0, 1, \ldots, d - 2$. The state vector of $C_k$ at time $t$ is defined as $\Pi_k^t = \{\Pi(1)_{k}^t, \Pi(2)_{k}^t, \ldots, \Pi(10)_{k}^t\}$, where $\Pi(n)_{k}^t (1 \leq n \leq 10)$ is the probability of $C_k$ having the state $S_n$ at time $t$ as shown in figure [3]. The state transition of $C_k$ from $\Pi_k^t$ to $\Pi_k^{t+1}$ is defined by using the state transition matrix $P_k$ whose size is $10 \times 10$. This state transition is given as

$$\Pi_k^{t+1} = P_k \Pi_k^t. \hspace{1cm} (8)$$

The stationary state $\Pi_k^\infty$ is given as the solution of

$$\Pi_k^\infty = P_k \Pi_k^\infty \hspace{1cm} (9)$$

with the normalized condition $\sum_{n=1}^{10} \Pi(n)_{k}^\infty = 1$. We construct $P_k$ to solve [3] in the order of $k = 0, 1, 2, \ldots, d - 2$. $P_k$ is given in the following by the boundary conditions (B.C.), and by the dynamics of vehicles.

The B.C. of each $P_k (k = 0, 1, 2, \ldots, d - 2)$ are given as shown in figure [5]. The left B.C. of $P_0$ is given strictly as vehicles entering in the leftmost cells simultaneously with probability $\alpha$ provided that both leftmost cells are empty. The right B.C. of $P_0$ needs approximations because the stationary state of $C_k (1 \leq k \leq d - 2)$ is not yet calculated. The right B.C. of $P_0$ is approximated as a pair of vehicles existing on both cells at $x = 2$ with probability $\bar{\alpha}$. $\bar{\alpha}$ is approximated as $\bar{\alpha} = \alpha/(1 + \alpha)$ which is the expected density of the loss system. The left B.C. of $P_k (1 \leq k \leq d - 3)$ is the stationary state of $C_k$ which is given strictly by $\Pi_k^{\infty}$. The right B.C. of $P_k (1 \leq k \leq d - 3)$ is the stationary state of $C_k$ which is not yet calculated. This stationary state is approximated by $\Pi_k^{\infty}$, i.e., the stationary state at $x = \{k + 1, k + 2\}$ is approximated as that at $x = \{k - 1, k\}$. This approximation represents well the spatial change of the configurations if the flow is in free state. The left B.C. of $P_{d-2}$ is the stationary state of $C_{d-2}$ which is given strictly by $\Pi_{d-2}^{\infty}$. The right B.C. of $P_{d-2}$ is given strictly as vehicles go out of the rightmost cell on lane $i$ ($i = 1, 2$) with probability $\bar{\beta}_i$.

![FIG. 5: The B.C. of each $P_k (k = 0, 1, 2, \ldots, d - 2)$](image)

The dynamics of vehicles in this cluster approximation is given as follows. We update the intensity of vehicles spatially to represent the spatial change of the mean intensity $\tilde{v}$ observed in the simulation results (figure [9] (d)-(f)). To realize the spatial change of the intensity, we define $u_{ik} (0 \leq k \leq d - 2)$ as the intensity of $i$-th vehicle on $C_k$. To give the specific form of $u_{ik}$, we use $\tilde{v}_k$ defined as the intensity common to the vehicles on $C_k$, and $V_k (0 \leq k \leq d - 2)$ defined as the stationary mean OV function of $C_k$. $\tilde{v}_k$ is calculated by using $\Pi_k^{\infty}$ as

$$\tilde{v}_k = (p\Pi(3)_{k}^{\infty} + q\Pi(6)_{k}^{\infty} + 2r\Pi(7)_{k}^{\infty} + r\Pi(9)_{k}^{\infty})/ (\Pi(3)_{k}^{\infty} + \Pi(5)_{k}^{\infty} + \Pi(6)_{k}^{\infty} + 2\Pi(7)_{k}^{\infty} + \Pi(8)_{k}^{\infty} + 2\Pi(9)_{k}^{\infty} + 2\Pi(10)_{k}^{\infty}), \hspace{1cm} (10)$$

and $\tilde{v}_k$ is updated spatially as

$$\tilde{v}_{k+1} = (1 - a)\tilde{v}_k + a\tilde{V}_k. \hspace{1cm} (11)$$
\( u_{i,k} \) is given by using \( \tilde{v}_k \), and by the configuration on \( C_k \) as

\[
\begin{align*}
  u_{i,k} &= (1 - a) \tilde{v}_k + a V (\Delta x_{1i}, \Delta x_{2i}) \\
  &= \begin{cases} 
  (1 - a) \tilde{v}_k, & \Delta x_{1i} = 0 \\
  (1 - a) \tilde{v}_k + ar, & \Delta x_{1i} \geq 1 \text{ and } \Delta x_{2i} = 0 \\
  (1 - a) \tilde{v}_k + aq, & \Delta x_{1i} \geq 1 \text{ and } \Delta x_{2i} = 1 \\
  (1 - a) \tilde{v}_k + ap, & \Delta x_{1i} \geq 1 \text{ and } \Delta x_{2i} \geq 2.
  \end{cases}
\end{align*}
\]

(12)

Now the concrete form of \( P_k \) is given as follows. We define \( P_k \) \((i, j) (1 \leq i, j \leq 10)\) as the element of \( P_k \) at \( i \)-th row, and \( j \)-th column. \( P_k \) \((i, j)\) is the probability of the transition of the state from \( S(j) \) to \( S(i) \). For instance, \( P_k \) \((1, 1) = 1 - a \), and \( P_k \) \((7, 1) = a \). The other elements of \( P_0 \), and \( P_k \) \((1 \leq k \leq d - 3)\), and \( P_{d-2} \) obeying the B.C. of the cells at \( x = d - 1 \), such that \( \beta_j = u_{i,d-1} (j = 1, 2) \) for \( i \)-th vehicle, are straightforward and shown in [11].

The degree of the alternative configurations at \( x = k (0 \leq k \leq d - 2) \) in the stationary state is defined as \( Ge^\infty_k \) which is given by using \( \Pi_k^\infty \) as

\[
Ge^\infty_k = \Pi(3)^k + \Pi(3)^k + \Pi(5)^k + \Pi(6)^k + \Pi(7)^k + \Pi(8)^k + \Pi(9)^k + \Pi(10)^k.
\]

(13)

We measure \( Ge^\infty_x \) versus \( x \), and \( \tilde{v}_x \) versus \( x \), and compare them with the simulation results. The conditions of the cluster approximation are given similarly to the simulations. \( d, p, q, r, a, \) and \( \alpha \) are the same to those of the simulations. \( \beta_j \) \((j = 1, 2)\) is given as the \( u_{i,d-1} \) for each \( i \)-th vehicle.

The results of the four cluster approximation are shown in figure 6, together with the simulation results to compare the theoretical results with the simulations. Both \( Ge^\infty_x \) and \( \tilde{v}_x \) coincide with \( Ge(x) \), and \( \tilde{v}(x) \) respectively. The difference \( |Ge^\infty_x - Ge(x)| \) is smaller in the case of \( a = 0 \) and \( a = 1 \) than that of \( a = 0.1 \).

The coincidence between \( Ge^\infty_x \) and \( Ge(x) \) with various \( a \) and \( q \) suggests that our four cluster approximation is a good theoretical approximation for obtaining the alternative formation. We can obtain the length of the communication line necessary for the target of \( Ge \) by the theoretical calculation as well as by the simulations. Various \( Ge^\infty_x \) are generated by the spatial update of the intention as shown in [10]-[12]. \( |Ge^\infty_x - Ge(x)| \) in the case of \( a = 0 \) and \( a = 1 \) are smaller than that of \( a = 0.1 \) because the calculation of \( u_{i,k} \) does not contain the approximation of the spatial update of \( \tilde{v}_x \) in the case of \( a = 0 \) and \( a = 1 \): \( u_{i,k} \) in the case of \( a = 0 \) is given as

\[
u_{i,k} = \tilde{v}_0
\]

(14)

and \( u_{i,k} \) in the case of \( a = 1 \) is given as

\[
\begin{align*}
  u_{i,k} &= \begin{cases} 0, & \Delta x_{1i} = 0 \\
r, & \Delta x_{1i} \geq 1 \text{ and } \Delta x_{2i} = 0 \\
q, & \Delta x_{1i} \geq 1 \text{ and } \Delta x_{2i} = 1 \\
p, & \Delta x_{1i} \geq 1 \text{ and } \Delta x_{2i} \geq 2.
  \end{cases}
\end{align*}
\]

(15)

The coincidence of \( \tilde{v}_x \) and \( \tilde{v}(x) \) suggests that this spatial update of the intention is a good approximation for expressing the spatial change of the mean intension.

V. CONCLUDING DISCUSSIONS

In this paper we have proposed a simple method for the achievement of alternative configurations of vehicles by using MLSOV model. We obtain for the first time the achievement of alternative configurations of vehicles by emergent behaviour of drivers. This alternative configurations is achieved along a compartment line which is drawn between two lanes, and prohibits vehicles from changing lanes, and permits them to interact with the ones on the opposite lane. This achievement is significant for traffic engineering in realizing the smooth "zipper merging", and is supported by the four cluster approximation. Moreover, drawing compartment lines for realizing this alternative configuration costs less than other methods for easing traffic congestion at an intersection, e.g., construction of a cubic interchange. Further improvement of the flow at an intersection or a junction by the alternative configuration will be published elsewhere [12].
FIG. 6: Ge(x) versus x and \( \bar{v}(x) \) versus x obtained by the simulations, together with \( Ge_x^\infty \) versus x and \( \bar{v}_x \) versus x calculated by the four cluster approximation. Ge(x) and \( Ge_x^\infty \) increase monotonically as x increases, and the sharpness of the increase of Ge(x) and \( Ge_x^\infty \) becomes larger as \( a \) becomes larger, and as \( q(=r) \) becomes smaller. \( v(x) \) and \( \bar{v}_x \) have one minimum value.
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