Phase-dependent dielectric properties and proton conduction of neopentyl glycol

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Phase-dependent dielectric properties and proton conduction of neopentyl glycol (NPG), which is an organic molecular plastic crystal, were studied via variable-temperature broadband dielectric spectroscopy (BDS). Permittivity and conductivity data show the phase transformations of NPG from the crystalline state to the plastic crystalline state at 315 K and then to the molten state at 402 K across the temperature range of 293–413 K. The Vogel temperatures (T_v) fitted from the Vogel–Fulcher–Tammann (VFT) equation agree well with the values extrapolated by the Stickel plot (linearized Vogel plot). Impedance and modulus data display a separation of the –Z” (the imaginary part of the complex impedance) and M” (the imaginary part of the complex electric modulus) peaks in the crystalline phase. However, they overlap in both the plastic crystalline phase and the molten phase, indicating long-range proton conduction. In both the molten phase and the plastic crystalline phase, the temperature dependence of direct current conductivity (σ_ac) obeys the VFT equation very well. While the vehicle mechanism (translational diffusion) is an intrinsic mechanism for ionic or protonic conduction in the molten phase, it is speculated that the Grotthuss mechanism also works due to the self-dissociation of NPG molecules, which are similar to water molecules. In the plastic crystalline phase, the proton hopping mechanism is most likely the underlying ion-conducting mechanism because of the rotational disorder and intrinsic defects (vacancies) of the NPG molecules. In the ordered crystalline phase, the proton conduction is presumed to follow the proton hopping mechanism as determined from the localized relaxation and the temperature dependence of σ_ac (Arrhenius behavior).

Introduction

Molecular substances composed of globular or pseudo-globular molecules often lead to the formation of mesophases (mesostates) between the ordered crystalline state and isotropic liquid. This mesophase is usually referred to as the plastic crystalline state, and the molecular substances are known as plastic crystals. Plastic crystals have the long-range center-of-mass crystalline order (positional order) and short-range dynamic disorder of molecular orientations, and thus are also known as the orientationally disordered crystals or rotator phases. Normally, they have a very low entropy of fusion and a relatively large entropy of solid–solid phase transition thus enabling high ionic conductivities, which makes them promising candidates for applications as protonic or ionic conductors in fuel cells, batteries, and supercapacitors.

Neopentylglycol (NPG) or 2,2-dimethyl-1,3-propanediol, an important representative of molecular plastic crystals, has been widely studied in various aspects. Many studies focused on phase transitions and/or crystal structures. It can be concluded that within the investigated temperature range (e.g. from 150 K to 423 K), NPG undergoes one solid–solid phase transition and one solid–liquid phase transition successively. Specifically, NPG exhibits its solid–solid phase transition from the ordered crystalline state to the plastic crystalline state at around 314 K (the low temperature monoclinic α phase transforms into the high temperature cubic γ phase), and then the melting transition at around 403 K between the plastic crystalline state and the molten state. Scheme 1 shows the crystal structure (monoclinic α phase) of NPG at 295 K based on the results from Chandra et al.

Scheme 1 Crystal structure (monoclinic phase) of NPG at 295 K.
Notes: left, view along (1 1 1) crystal plane; right, view along (0 1 0) crystal plane.
There were also some studies on dielectric properties and dielectric relaxations of NPG. Chandra et al. reported the AC conductivities of NPG in a powder form in a narrow temperature range between 295 K and 356 K and both the z and γ phases are thermally activated. They also reported the AC impedance spectroscopic results and the frequency and temperature effects on the conductivities, relaxation times, and diffusional parameters. In addition, Tamarit et al. studied dielectric relaxation behaviors of NPG in the plastic crystalline phase and its supercooled plastic crystalline phase, which was interpreted in terms of the Dissado–Hill theory by means of the Jonscher and Havriliak-Negami equations. They also reported that the z phase is thermally activated. But they revised this conclusion in another paper, which revealed that the temperature dependence of the relaxation time showed a non-Arrhenius behavior. This different conclusion may be largely due to the narrow temperature range. Previous reports seem to be doubtful, which prompted the present new investigation on this compound. In addition, dielectric properties of NPG in liquid state are scarce and the possible conduction mechanisms of protons need further elucidation.

There were some studies of NPG in terms of calorimetric properties, solid–liquid interfacial energy, and colloidal barocaloric effects. In addition, orientationally disordered molecular mixed crystals relating to NPG were also studied. The related studies includes the packing, thermodynamic analysis, relaxation dynamics, calorimetric investigation and structural recovery. Forming a solid solution by mixing another similar molecule is to some extent an effective way to form a supercooled plastic crystal, which would be simple to study the glass transition phenomenon as only one degree of freedom is involved. Interestingly, it was found that admixing a related molecular species of larger size can considerably enhance the ionic conductivity and the stability range of the plastic phase. NPG and its derivatives have many applications including water based coatings, magnetic coatings, and powder coatings. In addition, it is used as an intermediate for the synthesis of lubricants, plasticizers, adhesives, photographic materials, pharmaceuticals, pesticides, fragrances, fabric softeners and vibration dampeners. It also has potential applications in the intumescent flame retardants, refrigeration, and air-conditioning.

Broadband dielectric spectroscopy (BDS) has the advantage of probing electrical properties, (dielectric) relaxation phenomena and thermal phase transitions over a wide range of temperatures and frequencies. In the present work, NPG was studied across a wide range of temperatures (from 293 K to 413 K) and frequencies via the BDS. Dielectric properties of NPG in three phases (the ordered crystalline, plastic crystalline and liquid phases) were studied. In addition, the possible proton conduction mechanisms were also explored.

### Experimental

#### Materials

NPG ([CH3]2C(CH2OH)2) was purchased from Sigma-Aldrich with purity of 99% and used as received.

### Dielectric measurements

Dielectric properties were measured by means of a Novocontrol BDS spectrometer based on a high resolution impedance analyzer (Alpha A) in the 10⁻¹ to 10⁶ Hz frequency range. A Novocontrol Quatro Cryosystem was used to control the temperatures (from 293 K to 413 K) via a dry nitrogen gas flow derived from liquid nitrogen. NPG was placed in a stainless-steel liquid cell and then heated from ambient temperature to 413 K to ensure complete filling of the cell. The system was then cooled down to 293 K. Afterwards, the sample was heated up again to 413 K with temperature interval of 1 K. The detailed operation process can be found in ref. 41.

### Results and discussion

#### Three representations of dielectric properties

In general, dielectric spectra can be shown in three complex quantities – permittivity ($\varepsilon^*$), conductivity ($\sigma^*$) and complex electric modulus ($M^*$), which are related to each other based on eqn (1).

$$M^*(f) = \frac{1}{\varepsilon^*}(f) = \frac{2\pi f \varepsilon_0 \sigma^*(f)}{\varepsilon^*(f)}$$ (1)
Specifically, Fig. 1a displays the frequency dependence of $\varepsilon'$ (the real part of $\varepsilon^*$), $\varepsilon''$ (the imaginary part of $\varepsilon^*$), $\sigma'$ (the real part of $\sigma^*$), $M'$ (the real part of $M^*$) and $M''$ (the imaginary part of $M^*$) recorded at 353 K (in the plastic crystalline state). Clearly, it shows that there are no obvious relaxation phenomena of NPG recorded at 353 K in the frequency range of $10^{-1}$ to $10^{6}$ Hz based on the frequency dependence of $\varepsilon'$. The dc conductivity ($\sigma_{dc}$) is characterized by a plateau of the frequency dependence of $\sigma'$ (in-phase part of conductivity). In addition, the frequency dependence of $M'$ takes the form of a well-pronounced peak, a so-called conductivity relaxation peak, which directly yields the relaxation time $\tau_M$ (e.g. $\tau_M = 1.04 \times 10^{-5}$ s at 353 K). Fig. 1b depicts the temperature-dependent dielectric properties of NPG at 133 Hz in the temperature range of 293–413 K. As the temperature increases, $\varepsilon'$, $\varepsilon''$ and $\sigma'$ show an increasing tendency, while $M'$ and $M''$ present a decreasing tendency. In addition, the two jumps at around 315 K and 402 K indicate two phase transitions clearly, which are in accord with the previous results.\textsuperscript{11,12,14,18} Thus, the three phases (phase II, phase I and melt phase) can be distinguished according to these two phase transition temperatures.

### Permittivity analysis

Fig. 2a and b presents $\varepsilon'$ and $\varepsilon''$, respectively, as a function of frequency ($10^{-1}$ to $10^{6}$ Hz) and temperature (293–413 K). With the decrease of frequency, $\varepsilon'$ and $\varepsilon''$ both show an increasing tendency in the lower frequency region, which is attributed to the electrode polarization. Clearly, both graphs show the two same jumps at 315 K and 402 K during the heating process and the former jump is significantly larger than the latter, which is a characteristic of plastic crystals. In addition, there are no obvious relaxation phenomena over the frequency range of $10^{-1}$ to $10^{6}$ Hz. Detailed analysis of relaxation phenomena (e.g. molecular tumbling) can be found in previous research.\textsuperscript{21,22}

### Conductivity analysis

Fig. 3 depicts the three dimensional (3D) graph of the real part of complex conductivity ($\sigma'$), the in-phase component of conductivity, as a function of frequency and temperature. Similar to permittivity results (Fig. 1 and 2), two apparent jumps take place at the sample temperatures of 315 K and 402 K. In addition, the dc conductivity ($\sigma_{dc}$) is characterized by a plateau of the frequency dependence of $\sigma'$ and thus it can be determined by fitting the plateau of the temperature dependence of $\sigma'$ curves.

The temperature dependence of $\sigma_{dc}$ for NPG is shown in Fig. 4. With the increase of the temperatures from 293 K to 413 K, $\sigma_{dc}$ presents an upward tendency. The two apparent jumps at 315 K and 402 K in $\sigma_{dc}$ are in good agreement with the two endothermic peaks at 316 K and 403 K in DSC trace (Fig. 4). These two jumps can also be found in Fig. 1b, 2 and 3. The value of $\sigma_{dc}$ increases about 1.5 orders of magnitude after it undergoes the solid–solid phase transition at 315 K, while it increases more rapidly in phase II than in phase I.

To study the temperature dependence of $\sigma_{dc}$, a simple test (eqn (2)) to check whether $\sigma_{dc}$ obeys a Vogel–Fulcher–Tammann (VFT) relation or an Arrhenius equation was introduced by Turnhout and Wübbenhorst.\textsuperscript{42}
\[
\left(\frac{\ln \sigma}{dT}\right)^{-1/2} = \left(\frac{R}{E_v}\right)^{1/2} (T - T_v) \tag{2}
\]

where \(\sigma\) represents the conductivity, \(T\) the temperature, \(R\) the universal gas constant, \(T_v\) the Vogel temperature and \(E_v\) the activation energy at \(T_v\). This equation combines both a VFT \((T_v \neq 0\) K\) and an Arrhenius equation \((T_v = 0\) K\) and thus allows an evaluation of \(E_v\) and \(T_v\) from the slope and the intersection of the extrapolated, linearized curves with the abscissa.\(^{42}\)

Fig. 5 shows linearized Vogel plots of NPG with the corresponding correlation coefficient \((R^2)\) in the temperature range of 293–413 K. Overall, \(\sigma_{dc}\) of these three phases (phase II, phase I and the melt phase) can be fitted by three equations with high \(R^2\), respectively. Specifically, \(T_v\) values of phase II, phase I and the melt phase are 0 K, 153.1 K and 391.7 K, respectively. Because \(T_v\) is equal to 0 K in phase II, the temperature dependence of \(\sigma_{dc}\) most likely obeys the Arrhenius law. In addition, the temperature dependence of \(\sigma_{dc}\) most likely obeys the VFT equation for both phase I and the melt phase due to \(T_v \neq 0\) K.

In order to quantitatively verify the above conclusion (Fig. 5), the \(\sigma_{dc}\) values in the three phases are fitted by the VFT equation (eqn (3)) and the Arrhenius equation (eqn (4)), respectively.\(^{43,45}\)

\[
E_a = RT^2(\frac{d\ln \sigma}{dT}) \tag{5}
\]

\[
E_a = RBT^2(T - T_v)^2 - RT/2 \tag{6}
\]

Obviously, activation energies are in function of temperatures because \(R\) and \(B\) are constants in eqn (6). The temperature dependence of \(E_a\) is also shown in Fig. 6. It is shown that \(E_a\) in the low temperature region (phase II) is a constant, which indicates the thermally activated conductivity. In phase I and the melt phase, as the temperature increases, \(E_a\) decreases rapidly (especially in the melt phase), which indicates the non-thermally activated conductivity agreeing well with the analysis of relaxation time.\(^{22}\)

**Impedance and modulus analysis**

Fig. 7 illustrates the temperature dependence of \(M'\) and \(-Z''\) for NPG at selected temperatures. One or two temperatures are chosen as
representatives for each phase. Clearly, both the impedance and electric modulus data show a single relaxation response in the frequency range of $10^1$ to $10^6$ Hz. The separation of the $Z''$ and $M''$ peaks (phase II: Fig. 7a) results from localized relaxation while the overlapping of the $Z''$ and $M''$ peaks (phase I: Fig. 7b and c; melt: Fig. 7d) in the spectra reflects long-range migration of protons.\(^{48,49}\)

While the vehicle mechanism (translational diffusion) is an intrinsic mechanism for proton conduction in the melt phase, it is speculated that the Grotthuss mechanism should also function due to the self-dissociation of hydrogen-bonded NPG molecules (eqn (7)), which are similar to water molecules. Therefore, in the melt phase, the proton conduction results from both the vehicle and Grotthuss mechanisms.

$$\text{(CH}_3\text{)}_2\text{C(CH}_2\text{OH)}_2 \leftrightarrow \text{[(CH}_3\text{)}_2\text{C(CH}_2\text{OH)}(\text{CH}_2\text{O})]^+ + \text{H}^+ \leftrightarrow \text{[(CH}_3\text{)}_2\text{C(CH}_2\text{O)}_2]^2++ 2\text{H}^+$$

(7)

In the plastic crystalline phase (phase I), the proton hopping mechanism is most likely the underlying ion-conducting mechanism because of the rotational disorder in the cubic phase and intrinsic defects (vacancies) of the NPG molecules featured by the hydrogen bond network,\(^{26}\) and the long-range migration of protons indicated by the overlapping of the $Z''$ and $M''$ peaks.

In the ordered crystalline state (Fig. 7a), the proton conduction is presumed to follow the proton-hopping mechanism via the hydrogen bond network due to the localized relaxation and the temperature dependence of $\sigma_{dc}$ (Arrhenius behavior).

### Conclusions

Phase dependent dielectric properties and proton conduction of the molecular plastic crystal neopentyl glycol (NPG) were studied via the variable-temperature broadband dielectric spectroscopy. Permittivity and conductivity data show that NPG undergoes phase transitions from crystalline phase to plastic crystalline phase at 315 K and then to the molten state at 402 K successively from 293 K to 413 K. The Vogel temperatures obtained by the Vogel–Fulcher–Tammann (VFT) fits agree well
with the values extrapolated by the Stickel plots (linearized Vogel plots). Impedance and elastic modulus data display the separation of the $-Z'$ and $M'$ peaks in the crystalline phase, and the overlaps of the $-Z'$ and $M'$ peaks in the plastic crystalline phase and the molten phase; the latter case indicates the long-range migration of protons. In both the molten phase and the plastic crystalline phase, the temperature dependence of direct current conductivity ($\sigma_{dc}$) obeys the VFT equation well. In the molten phase, the proton conduction results from both the vehicle and Grotthuss mechanisms. In the plastic crystalline molten phase, the proton conduction results from both the ion-conducting mechanism due to the rotational disorder and intrinsic defects (vacancies) of the hydrogen-bonded NPG molecules. In the ordered crystalline phase, the proton conduction is speculated to be intermolecular proton transport via proton hopping as determined from the localized relaxation and the temperature dependence of $\sigma_{dc}$ (Arrhenius behavior).

**Conflicts of interest**

The authors declare no conflict of interest.

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