Establishing an Empirical Model for Surface Soil Moisture Retrieval at the U.S. Climate Reference Network Using Sentinel-1 Backscatter and Ancillary Data

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Abstract: Progress in sensor technologies has allowed real-time monitoring of soil water. It is a challenge to model soil water content based on remote sensing data. Here, we retrieved and modeled surface soil moisture (SSM) at the U.S. Climate Reference Network (USCRN) stations using Sentinel-1 backscatter data from 2016 to 2018 and ancillary data. Empirical machine learning models were established between soil water content measured at the USCRN stations with Sentinel-1 data from 2016 to 2017, the National Land Cover Dataset, terrain parameters, and Polaris soil data, and were evaluated in 2018 at the same USCRN stations. The Cubist model performed better than the multiple linear regression (MLR) and Random Forest (RF) model ($R^2 = 0.68$ and RMSE = 0.06 m$^3$ m$^{-3}$ for validation). The Cubist model performed best in Shrub/Scrub, followed by Herbaceous and Cultivated Crops but poorly in Hay/Pasture. The success of SSM retrieval was mostly attributed to soil properties, followed by Sentinel-1 backscatter data, terrain parameters, and land cover. The approach shows the potential for retrieving SSM using Sentinel-1 data in a combination of high-resolution ancillary data across the contiguous United States (CONUS). Future work is required to improve the model performance by including more SSM network measurements, assimilating Sentinel-1 data with other microwave, optical and thermal remote sensing products. There is also a need to improve the spatial resolution and accuracy of land surface parameter products (e.g., soil properties and terrain parameters) at the regional and global scales.

Keywords: remote sensing; soil moisture network; sensor synergy; data fusion; soil water conservation; ecological monitoring

1. Introduction

Soil moisture serves an important role in regulating water and energy transport [1–4]. It is considered as a key variable in agriculture, hydrology, atmospheric and climate sciences [5,6]. To improve understanding of the hydrological cycle and enhance water resources management, many studies have attempted to monitor and map soil moisture at different spatial and temporal scales [7].

Advances in sensor technologies have shown success in soil moisture monitoring across scales. These include several in-situ soil moisture monitoring stations in the USA [8] and international [9] monitoring networks. Real-time soil moisture monitoring enables validation of satellite soil moisture monitoring missions across the globe [10] and creating gridded soil moisture maps at the regional-scale [11]. However, both these studies often have a coarse spatial resolution, which does not apply to the field scale. Furthermore, soil hydrological processes are complexed by the
diverse effects of soil, climate, vegetation, and topography [12]. Characterizing soil moisture dynamics and distribution at large spatial and temporal scales is not easy, as it is affected by various physical processes (e.g., precipitation, evapotranspiration, runoff, drainage) and environmental controlling factors (e.g., meteorological forcing, soil texture, vegetation, topography) [7].

Satellite remote sensing measurements have provided soil moisture monitoring over large scales [13] compared to ground observations, which are mostly point-based [14]. Optical and thermal infrared sensors often suffer from cloud contamination, while microwave sensors are less affected by atmospheric conditions [15]. Passive microwave satellites measure the ground surface within a short time interval but at a coarse spatial resolution. Examples include the Soil Moisture Active Passive (SMAP) [16], Soil Moisture and Ocean Salinity [17] and Advanced Microwave Scanning Radiometer 2 (AMSR2) [18]. An active microwave system often has a fine spatial resolution but a long revisit time. For instance, Sentinel-1 satellites have been used to map relative soil moisture across Europe at a 1-km resolution every 1.5 and 4 days [19]. Metop Advanced SCATterometer is another active system [20].

Different models have been built for soil moisture retrieval with microwave remote sensing data. Physical models describe interactions of vegetation and ground roughness with radar signals to retrieve soil moisture [21]. Therefore, several parameters, such as emissivity and albedo, need to be estimated from soil properties and land cover characteristics, which is often difficult to quantify at a fine spatial resolution [16,21].

Compared to physical models, empirical models have also been used to retrieve soil moisture that capture relationships between soil moisture and geophysical variables measured by microwave sensors. The most widely used models include the Change Detection method (e.g., [22]) and machine learning algorithms (e.g., [23]). For example, Bauer-Marschallinger et al. reported that surface properties such as geometry, roughness, and vegetation structure are static parameters that affect the changes in backscatter data and need to be included in the model [19]. However, empirical models can be data-driven and location-specific and cannot estimate soil moisture in different soil types (e.g., sands, loamy soils) and land cover (e.g., Cultivated Crops, Pasture) conditions [24].

More recently, physical and empirical models have been developed to assimilate datasets from different remote sensing platforms (e.g., [25]). In terms of soil moisture mapping, Lievens et al. combined SMAP and Sentinel-1 to improve soil moisture estimates using a physical-based model [26] while Santi et al. used an empirical model (an artificial neural network) to merge SMAP, Sentinel-1, and AMSR2 satellite data [27]. Recently Bauer-Marschallinger et al. fused Sentinel-1 with ASCAT observations to improve the spatial and temporal resolution of SSM [28]. Das et al. applied a joint SMAP-Sentinel algorithm to retrieve SSM at 1-km and 3-km resolutions [29]. To the best of our knowledge, little research has been done to develop data fusion algorithms by combining remote sensing data with multiple ancillary data such as digital elevation model, land cover and soil properties.

In this study, the U.S. Climate Reference Network (USCRN, [30]) was used to develop an empirical soil moisture retrieval model by combining Sentinel-1 data with multiple ancillary datasets. The USCRN consists of soil moisture measurements across the entire USA, with distinct vegetation and soil conditions. The objectives of our study are two-fold:

1. To retrieve surface soil moisture (SSM) (at the depth of 0–0.05 m) at the USCRN stations using Sentinel-1 data collected from 2016 to 2017 combined with ancillary data (e.g., terrain, land cover, soil properties), and to evaluate the model performance in 2018 for different land cover types and with different algorithms.

2. To evaluate the contribution of different ancillary variables for predicting soil moisture dynamics for future SSM retrieval across larger spatial extents.

Two hypotheses will be tested in the study: (1) SSM can be empirically retrieved at the USCRN stations in different land cover by combining Sentinel-1 with other ancillary data, and; (2) Sentinel-1 backscatter and ancillary data have different influences on the SSM model performance.
2. Materials and Methods

In this study, SSM retrieval models were established between the in-situ soil sensor SSM measurements (used as the model response), Sentinel-1 data, and various ancillary data (used as covariates). We describe these in turn below. Note that the acronyms are listed in Table A1.

2.1. U.S. Climate Reference Network SSM Database

In total, 66 USCRN sites were included for building the SSM retrieval models (Figure 1). Soil moisture sensors at the USCRN sites measure soil volumetric water content (VWC) at five depths (i.e., 0–0.05, 0.05–0.10, 0.10–0.20, 0.20–0.50, 0.50–1.00 m) every 30 min. We used the daily average VWC measured at 0–0.05 m to generate models of SSM, as the C-band SAR signal cannot penetrate deeper into the surface of the soil except when there is a very dry soil surface [31].

![Figure 1. The U.S. Climate Reference Network (USCRN) stations used to retrieve surface soil moisture. The land cover map is obtained from the National Land Cover Database (https://www.mrlc.gov/data/type/land-cover). The red data points are the four USCRN stations of interest in this study.](image)

2.2. Sentinel-1 Data

The Sentinel-1 satellites are C-band dual-polarization Synthetic Aperture Radars (SAR). The Sentinel-1 mission comprises two identical spacecraft, Sentinel-1A (S-1A) and Sentinel-1B (S-1B) launched in 2014 and 2016, respectively. Depending on the number of satellites, the revisit time is every 6 (single satellite) or 12 (double satellites) days. The Sentinel-1 data used in this study were obtained from mid-March to mid-November across the USCRN from 2016 to 2018 to minimize the frozen ground period because of the insensitivity of radar backscatter data to soil moisture in frozen soil. Backscatter measurements were used that were available at two polarizations, VV (vertical transmit/vertical receive) and VV+VH (vertical transmit/horizontal receive). For brevity, we refer them to VV and VH modes. Both VV and VH data were used in the model because they have different sensitivity to SSM under different vegetation and land surface conditions [19].

The data used in this study were the Sentinel-1 Ground Range Detected (GRD) scenes in interferometric wide (IW) swath mode. The backscatter data were preprocessed using Google Earth Engine with thermal noise removal, radiometric calibration, and terrain correction [32]. Terrain depths (i.e., 0–0.05, 0.05–0.10, 0.10–0.20, 0.20–0.50, 0.50–1.00 m) every 30 min. We used the daily average VWC measured at 0–0.05 m to generate models of SSM, as the C-band SAR signal cannot penetrate deeper into the surface of the soil except when there is a very dry soil surface [31].
Engine with thermal noise removal, radiometric calibration, and terrain correction [32]. Terrain correction was done using a 30-m SRTM digital elevation model. The processed backscatter data were available at a 10-m scale.

To remove the speckle effect of the backscatter data, we used an aggregation approach following [19] to resample the 10-m backscatter images to the 30-m scale. We describe this briefly here: First, dynamic masks were applied to the raw images to exclude the backscatter values larger than –5 dB and smaller than –20 dB for the VV mode and to exclude the backscatter values larger than –10 dB and smaller than –30 dB for the VH mode. The upper limits of the masks were determined according to Bauer-Marschallinger et al. and represented urban features [19]; the lower limits of the masks were determined empirically based on the distribution of backscatter data over the three years and represented the sensor’s noises. Second, the processed images were passed through a Gaussian filter with a $3 \times 3$ kernel ($\frac{1}{16}$ $\begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix}$). Third, the filtered images at the 10-m scale were aggregated to the 30-m scale by the arithmetic mean. The aggregated backscatter will be used in this study for building the retrieval model for SSM across the USCRN stations.

We derived a number of indices from the aggregated backscatter data such as temporal mean and standard deviation (SD) of VV and VH backscatter and the ratios of the temporal SD to temporal mean. The VV and VH backscatter data were calculated pixel-wise at the 30-m sampling-scale from 2016 to 2018.

2.3. Ancillary Data

Different ancillary data were used to retrieve SSM in combination with Sentinel-1 data. These include land cover, terrain parameters, and soil properties. These datasets are shown in Table 1 and described below. Precipitation data were not used as covariates as they did not directly affect the relationship between SSM and backscatter data. Conventionally, precipitation measurements are used as quality control flags for the retrieving algorithms [16].

Table 1. Remote sensing and environmental covariates used to retrieve soil moisture across the US.

| Datasets | Spatial Resolution | Temporal Resolution | Depth (m) | Comments |
|----------|--------------------|---------------------|-----------|----------|
| Soil water content measurements at the USCRN | N.A. | 1-day | 0-0.05 | Empirical model response |
| ESA – Sentinel-1 backscatter measured at two polarizations (VV and VH) and incidence angle | 10 m | 6–12 days | 0-0.05 | Empirical model covariates |
| Land cover map from National Land Cover Dataset | 30 m | N.A. | – | Empirical model covariate |
| Terrain parameters from the USGS | 10 m | N.A. | – | Empirical model covariates |
| Soil property maps of the US (Polaris) | 30 m | N.A. | 0-0.05 | Empirical model covariates |
| NASA-SMAP Level 3 radiometer-based surface soil moisture product | 36 km | 1-day | 0-0.05 | Independent validation dataset |

2.3.1. Land Cover

Land cover (LC) affects soil moisture [33]. The LC information was derived from the National Land Cover Database (https://www.mrlc.gov/data/type/land-cover) which provides 30-m land cover across the USA in the year of 2016 [34]. The land cover types include Developed, Water, Wetland, Shrub/Scrub, Herbaceous, Hay/Pasture, Forest and Cultivated Crops. We combined Shrub/Scrub and Dwarf scrub into Shrub/Scrub, and Deciduous Forest, Evergreen Forest, and Mixed Forest into Forest. We excluded Developed and Water, and Forest because the C-band Sentinel-1 data cannot penetrate the dense vegetation cover [35]. Wetland was also excluded. Four merged LC types were used as covariates: Cultivated Crops, Hay/Pasture, Herbaceous, and Shrub/Scrub. The final LC types are shown in Figure 1.
2.3.2. Terrain Parameters

The interaction between SSM and SAR backscatter measurements is affected by topography characteristics [36] and soil conditions such as ground roughness [16,21,37]. We used terrain parameters to model this relationship. The 10-m U.S. Geological Survey (USGS) National Digital Elevation Model (DEM) was used (www.nd.gov/gis). Slope, aspect, terrain ruggedness index (TRI), and topographic wetness index (TWI) were computed using the DEM data with the “terrain” function from the “raster” R package [38]. TRI and TWI are geo-morphometric parameters and have an impact on soil moisture distribution and dynamics [39,40]. Although these large-scale terrain parameters do not directly affect the backscattering behavior of the ground surface, we used them to model the spatial and temporal variations of soil VWC that were measured at the USCRN stations and were averaged daily assuming that surface soil water redistribution occurs due to topographic differences over this period.

2.3.3. Soil Properties

Soil properties influence soil moisture dynamics across the spatial and temporal scale. The Probabilistic Remapping of Soil Survey Geographic (POLARIS) dataset was used [41]. The POLARIS provides a 30-m probabilistic estimation of soil properties at six different depths across the USA, which are spatially continuous and internally consistent. The mean values of estimated properties at 0–0.05 m, including bulk density (BD), sand, silt and clay contents, and soil organic matter (SOM) content were used as covariates in the empirical models given their role in controlling of soil moisture storage [42].

To extract the Sentinel-1 and ancillary data to the USCRN stations for establishing SSM retrieval models and for mapping the SSM across the field, approximately 10 × 10 km regions of interest (ROIs) were selected for all USCRN stations with the USCRN sensors located in the center of the ROIs as they were large enough to observe the soil water variation in different vegetation, terrain, and soil conditions. We cannot choose an ROI that is too large because the Sentinel-1 sensor cannot capture the regions within one day and the composite Sentinel-1 image does not represent SSM within a specific day. Sentinel-1 data, LC types, terrain parameters, and soil properties were extracted within these ROIs onto 30 × 30 m grids. Sentinel-1 data were aggregated onto the 30-m using the method described earlier. LC types and soil properties data had 30-m resolutions and did not require further manipulation. Terrain parameters were extracted onto the 30-m grid using the bilinear interpolation algorithm. Along with the measured soil VWC from the USCRN sensors, these ancillary data were compiled, extracted onto the USCRN measuring stations and used for establishing empirical models to retrieve SSM at the USCRN stations over three years.

2.4. Establishing Empirical SSM Retrieval Models

Once the SSM data were collected and Sentinel-1 and ancillary data were extracted onto the USCRN stations, three models were explored to establish SSM retrieval algorithms, including multiple linear regression, Cubist and the Random Forest models. The covariates of the models included the backscatter data (VV, VH, and angle) and temporal statistics (e.g., temporal mean and SD) of VV and VH, as well as other ancillary data such as terrain parameters, land cover, and soil properties (e.g., clay, silt, bulk density). We describe each of the models in turn. The overall flow chart of the methodology used in this study is shown in Figure 2.
2.4.1. MLR Model

A multiple linear regression (MLR) was built with data listed in Table 1. In brief, the model response was the SSM measured at the USCRN stations and the predictors included Sentinel-1 backscatter and incidence angle, soil properties (e.g., sand content), terrain parameters (e.g., slope), and land cover types. In this study, the Sentinel-1 data varied in space and time while soil properties, terrain parameters, and land cover types only varied in space. Here, we used backward elimination to select the predictors. Afterward, we fitted the model parameters using the ordinary least square algorithm.

2.4.2. Cubist Model

The cubist model is an M5 regression tree algorithm [43]. Regression tree algorithm yields rule-based models comprising one or more rules. For each rule there is a set of conditions related to a linear sub-model. It can explain the nonlinear relationship between target variables and independent variables [44,45]. Cubist models have been used previously for the estimation of soil moisture [46], precipitation [47], net ecosystem carbon exchange [48], percent land cover [45], and soil properties e.g., pH, organic carbon, total nitrogen and phosphorus, texture, depth, and clay content [49].

Similar to the MLR, a Cubist model was constructed to predict SSM measured at the USCRN using Sentinel-1 and other ancillary data as predictors (Table 1). We fitted 20 committee models for the optimal Cubist model to predict soil VWC. The mean values of the predictions from all the committee models were used to represent the final VWC. To fit the Cubist model, the “train” function from the R “caret” package was used to find the optimal model parameters [50].

2.4.3. Random Forest Model

Random Forest is a nonparametric algorithm based on similarities among observations to fit decision trees. To build a tree, a bootstrap sample (a random sample with replacement) is taken from observations. To determine a split at a node in a tree, a random subsample of predictor variables is taken to select the predictor that minimizes the regression error [51]. Nodes continue to be split until

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Figure 2. Block diagram of the method used in this study.
no further improvement in error is achieved. Omitted observations, termed the “out-of-bag” samples, are used to compute the regression errors for trees [51]. Random Forest has recently been widely applied to map various soil properties and water dynamics using remote sensing data (e.g., [52,53]).

Similar to MLR and Cubist, the Random Forest algorithm was used to fit SSM at the USCRN from a combination of Sentinel-1 data and other environmental covariates as predictors. The “train” function in the “caret” package in R software [50] was used to fit the Random Forest parameters. The number of resampling iterations, number of variables tried at each split, and number of trees were selected as 10, 11, and 500, respectively, for the optimum model selection after repeated 10-fold cross-validation.

2.4.4. Model Performance Analysis

To evaluate the model performance and the contribution of different controlling factors on SSM retrieval, we used the USCRN VWC measurements from 2016 to 2017 as the calibration dataset and VWC measurements in 2018 as the validation dataset. The coefficient of determination ($R^2$), mean error (ME), and root mean square error (RMSE) were calculated for both calibration and validation datasets using the measured VWC at the USCRN stations and predicted VWC from different empirical SSM models.

2.4.5. SMAP Soil Moisture Product

To validate and compare the performance of three empirical SSM models, the NASA SMAP L3 SSM product was used (accessed from https://nsidc.org/data/smap/spl3smp/data-fields). The dataset was developed using physical models and was available at 36 km every 2–3 days. SMAP SSM data were extracted onto four selected locations representing different LC types (Figure 1).

3. Results

3.1. Performance of Different Models

3.1.1. Multiple Linear Regression

As shown in Table 2, the covariates selected in the MLR model can be divided into four categories, including backscatter and their temporal statistics (VV, VH, Mean of VV, Mean of VH, SD/Mean of VV), terrain parameters (slope, aspect, TPI, TRI, TWI), soil properties (BD, clay, silt), and LC types. It can be interpreted from Table 2 that all the covariates listed were significant at the 5% level of significance ($p < 0.05$) except for the Shrub/Scrub LC type. The overall MLR model was significant at the 5% level of significance. The MLR was moderately accurate ($R^2 = 0.556$ and RMSE = 0.058 m$^3$ m$^{-3}$) for the calibration data (from 2016 to 2017). In terms of the validation datasets in 2018, the model had a moderate performance ($R^2 = 0.551$ and RMSE = 0.059 m$^3$ m$^{-3}$) (Figure 3).

In the MLR model, the importance of different covariates can be evaluated based on the P values. As shown in Table 2, VV was the most significant covariate, followed by soil properties such as silt, clay, and LC type. By comparison, terrain parameters (e.g., aspect, TPI) were less important and angle was the least important covariate in the MLR model.
was the least important covariate in the MLR model. As shown in Table 2, VV was the most significant covariate, followed by soil properties such as silt, clay, BD, TPI, aspect, Mean of VH, Mean of VV, angle, VV, and VH refer to the temporal mean values of VV and VH backscatter measurements during the 2016–2018; TPI, topographic position index; BD, bulk density; and LC, land cover.

Table 2. Multiple linear regression (MLR) model for retrieving soil volumetric water content (VWC, m$^3$ m$^{-3}$) at 0–0.05 m depth. Note: coefficient of determination, $R^2$; VH, backscatter in vertical transmit/horizontal receive mode; VV, backscatter in vertical transmit/vertical receive mode; Mean of VV and VH refer to the temporal mean values of VV and VH backscatter measurements during the 2016–2018; TPI, topographic position index; BD, bulk density; and LC, land cover.

(1) Summary of fit

| Covariates | Estimate | Standard Error | t Ratio | Probability > |t| |
|------------|----------|----------------|---------|---------------|---|
| Intercept  | 0.156    | 0.022          | 7.07    | 2.0x10$^{-12}$| |
| VV         | 0.015    | 0.001          | 15.38   | 2.0x10$^{-51}$| |
| angle      | 0.001    | 0.000          | 2.62    | 8.8x10$^{-3}$ | |
| Mean of VV | −0.023   | 0.002          | −11.32  | 4.0x10$^{-20}$| |
| Mean of VH | 0.001    | 0.000          | 5.83    | 6.3x10$^{-9}$ | |
| aspect     | 0.000    | 0.010          | 8.32    | 1.0x10$^{-16}$| |
| TPI        | 0.054    | 0.014          | 3.96    | 7.6x10$^{-5}$ | |
| BD         | −0.063   | 0.010          | −5.99   | 2.4x10$^{-9}$ | |
| clay       | 0.004    | 0.000          | 13.45   | 5x10$^{-40}$  | |
| silt       | 0.002    | 0.000          | 14.01   | 4x10$^{-43}$  | |
| LC == Cultivated Crops | 0.049 | 0.004 | 12.33 | 4x10$^{-34}$ |
| LC == Herbaceous | −0.020 | 0.003 | −5.59 | 2.5x10$^{-8}$ |
| LC == Hay/Pasture | 0.030 | 0.003 | 8.95 | 6x10$^{-19}$ |
| LC == Shrub/Scrub | −0.061 | – | – | – |

(c) Analysis of variance

| Source | Degree of freedom | Sum of squares |
|--------|-------------------|----------------|
| Model  | 12                | 21.91          |
| Error  | 2,869             | 17.50          |
| Corrected total | 2,881 | 39.41          |
| F ratio | 299.40           |                |
| Probability > F | <0.0001 | |
3.1.2. Cubist

In the Cubist model, four categories of covariates were used, including backscatter and their temporal statistics (VV, VH, Mean of VV, Mean of VH, SD/Mean of VV), terrain parameters (slope, aspect, TPI, TRI, TWI), soil properties (BD, clay, silt), and LC types. In total, 20 committees were fitted for the optimal Cubist model and each of the committees had several rule-based sub-models. For example, the first, second, and third committee had 27, 10, and 21 number of rules that were chosen for optimum model building inside the “caret” package in R. Each rule fitted a regression equation between VWC and other covariates based on the mean, range, and estimated error of selected covariates (e.g., sand, SOM, VV, VH). The coefficients of the regression equations were selected based on the weightage decided by the optimum model build inside the “caret” package in R. The summary of the Cubist model formula is shown in Appendix A (Figure A1).

In the Cubist model, different conditions and predictors were determined and indicate the covariate usage in the model. As shown in Table 3, SOM (57% of usage), silt (39%), sand (34%), clay (26%), SD of VV (18%), aspect (18%), VV (18%), VH (17%) and other covariates were used as the conditions for selecting the rules of the Cubist model, whereas VV (90% of usage), silt (76%), sand (68%), VH (58%), SOM (55%) and others were used as the optimum model predictors. The weightages of the conditions and optimum model predictors were decided by the optimum model build inside the “caret” package in R. In terms of the model performance, it was improved compared to the MLR with $R^2 = 0.810$ and 0.682, and RMSE = 0.051 and 0.064 m$^3$m$^{-3}$ for the calibration and validation, respectively (Figure 3).

Table 3. Covariates usage in the Cubist model. Abbreviations: VH, backscatter measured in vertical transmit/horizontal receive mode; VV, backscatter measured in vertical transmit/vertical receive mode; Mean and SD of VV and VH refer to the temporal mean and temporal standard deviation values of VV and VH backscatter measurements during 2016–2018; TPI, topographic position index; TRI, terrain ruggedness index; TWI, topographic wetness index; BD, bulk density; SOM, soil organic matter; and LC, land cover.

| Covariates       | Conditions | Model  |
|------------------|------------|--------|
| SOM              | 57%        | 55%    |
| silt             | 39%        | 76%    |
| sand             | 34%        | 68%    |
| clay             | 26%        | 44%    |
| SD of VV         | 18%        | 47%    |
| aspect           | 18%        | 30%    |
| VV               | 18%        | 90%    |
| VH               | 17%        | 58%    |
| TPI              | 15%        | 25%    |
| TWI              | 11%        | 28%    |
| SD of VH         | 10%        | 45%    |
| SD/Mean (VV)     | 8%         | 51%    |
| Mean of VV       | 8%         | 39%    |
| angle            | 6%         | 32%    |
| slope            | 5%         | 38%    |
| TRI              | 3%         | 29%    |
| BD               | 3%         | 47%    |
| Mean of VH       | 3%         | 31%    |
| SD/Mean (VH)     | 3%         | 47%    |

3.1.3. Random Forest

The Random Forest was established with the same four categories of covariates as the MLR and Cubist model. The importance of the covariates is shown in Table 4. The most important covariates
were silt (%IncNodePurity = 9.3%) and sand (6.2%), followed by VV backscatter measurements (4.2%), SOM (3.5%), VH (3.4%), incidence angle (2.9%), and other covariates.

### Table 4. Covariates importance in the Random Forest model. Abbreviations: %IncNodePurity means a total decrease in node impurities from splitting on the variable, averaged over all trees; VH, backscatter measured in vertical transmit/horizontal receive mode; VV, backscatter measured in vertical transmit/vertical receive mode; Mean and SD of VV and VH refer to the temporal mean and temporal standard deviation values of VV and VH backscatter measurements during 2016–2018; TPI, topographic position index; TRI, terrain ruggedness index; TWI, topographic wetness index; BD, bulk density; SOM, soil organic matter; and LC, land cover.

| Covariates     | %IncNodePurity |
|---------------|----------------|
| silt          | 9.3            |
| sand          | 6.2            |
| VV            | 4.2            |
| SOM           | 3.5            |
| VH            | 3.4            |
| angle         | 2.9            |
| LC            | 1.6            |
| clay          | 1.0            |
| aspect        | 0.8            |
| SD/Mean (VH)  | 0.7            |
| TPI           | 0.7            |
| BD            | 0.5            |
| Mean of VV    | 0.4            |
| SD of VV      | 0.4            |
| SD of VH      | 0.4            |
| SD/Mean (VV)  | 0.4            |
| slope         | 0.4            |
| Mean of VH    | 0.3            |
| TRI           | 0.3            |
| TWI           | 0.3            |

In terms of the model performance, the Random Forest model had the largest $R^2$ (0.941) and the smallest RMSE (0.029 m$^3$ m$^{-3}$) for the calibration data as compared to the MLR and Cubist model. In terms of the validation data, the model was not good compared to the Cubist ($R^2 = 0.676$ and RMSE = 0.065 m$^3$ m$^{-3}$) (Figure 3). In this study, the optimal numbers of trees and other hyperparameters were chosen by the “train” function in the R “caret” package and the final optimal model had 500 trees. This suggested that the Random Forest model was over-fitted to the calibration data compared to the Cubist model.

### 3.2. Model Performance within Different LC Types

The SSM retrieval models had different performance within different LC types (Table 5). In terms of the MLR model, the coefficient of determination ($R^2$) calculated between measured VWC and predicted VWC for calibration datasets was largest in Herbaceous areas (0.503), followed by Shrub/Scrub (0.351), Cultivated Crops (0.264), and Hay/Pasture (0.230). In terms of the validation dataset, the patterns were slightly different, whereby Cultivated Crops had the largest $R^2$ (0.451), followed by Herbaceous (0.351), Shrub/Scrub (0.314), and Hay/Pasture (0.104). Note that Cultivated Crops and Herbaceous land cover types always outperformed the Shrub/Scrub and Hay/Pasture.
Table 5. Model performance for different methods within different land cover types calculated for calibration and validation datasets. Abbreviations: N, number of samples; $R^2$, coefficient of determination; RMSE, root mean square error (m$^3$ m$^{-3}$); ME, mean error (m$^3$ m$^{-3}$); RF, Random Forest.

|                | Cultivated Crops | Hay/Pasture | Herbaceous | Shrub/Scrub | Cultivated Crops | Hay/Pasture | Herbaceous | Shrub/Scrub |
|----------------|------------------|-------------|------------|-------------|------------------|-------------|------------|-------------|
| **Calibration**|                  |             |            |             |                  |             |            |             |
| N              | 303              | 730         | 934        | 986         | 210              | 502         | 550        | 842         |
| $R^2$          |                  |             |            |             |                  |             |            |             |
| MLR            | 0.264            | 0.230       | 0.503      | 0.351       | 0.451            | 0.104       | 0.351      | 0.314       |
| Cubist         | 0.567            | 0.671       | 0.809      | 0.723       | 0.512            | 0.457       | 0.513      | 0.522       |
| RF             | 0.895            | 0.903       | 0.943      | 0.916       | 0.509            | 0.398       | 0.523      | 0.543       |
| **Validation** |                  |             |            |             |                  |             |            |             |
| R$^2$          |                  |             |            |             |                  |             |            |             |
| MLR            | 0.084            | 0.092       | 0.080      | 0.059       | 0.071            | 0.098       | 0.079      | 0.057       |
| Cubist         | 0.062            | 0.061       | 0.049      | 0.039       | 0.067            | 0.076       | 0.072      | 0.048       |
| RF             | 0.034            | 0.036       | 0.028      | 0.023       | 0.068            | 0.080       | 0.073      | 0.046       |
| RMSE           |                  |             |            |             |                  |             |            |             |
| MLR            | 0.000            | 0.000       | 0.000      | 0.000       | 0.005            | −0.008      | 0.005      | −0.000      |
| Cubist         | −0.001           | 0.001       | −0.003     | −0.003      | −0.000           | −0.001      | 0.003      | −0.004      |
| RF             | 0.000            | 0.045       | −0.000     | −0.000      | 0.002            | −0.001      | 0.005      | 0.000       |

This was not the case for Cubist and Random Forest models. When these two models were used, the model performance was best within the Herbaceous, followed by Shrub/Scrub, Hay/Pasture, and Cultivated Crops, for calibration datasets and within Shrub/Scrub, followed by Herbaceous, Cultivated Crops, and Hay/Pasture for validation datasets.

In terms of the importance of the covariates, the temporal Mean of VV and VH backscatter data (Mean of VV, Mean of VH), soil texture, and aspect were important in all three models (Tables 2–4). This indicated that these factors had strong influences on SSM. The land cover type was only important in the MLR and Random Forest model. This was possible because the Cubist model used other continuous covariates (e.g. SOM, sand, silt, clay content, SD of VV, aspect) to define the conditions that performed better than the land cover type (Table 3).

The temporal variations of measured and predicted SSM using the Cubist model are plotted for different LC types at four USCRN stations over 2016–2018 (Figure 4). The measured SSM was collected from the ground soil moisture probes at the measuring stations. The predicted SSM values were extracted from the Cubist model on to the measuring stations. This type of comparison was similarly used by Bauer-Marschallinger et al. [19] and Das et al. [29] to evaluate the performance of the SSM retrieval models. The performance of the SSM retrieval models varied with the stations. In general, soil VWC was well predicted in 2018 using historical (2016–2017) Sentinel-1 data with ancillary data in stations with Shrub/Scrub (MS_Newton), Herbaceous (SD_Pierre), and Cultivated Crops (MO_Chillicothe). Soil VWC was poorly retrieved in Hay/Pasture (KY_Versailles).

To compare the empirical model with the SMAP products, SMAP L3 Radiometer SSM estimates were also extracted on to the USCRN stations assuming the 36-km pixel values represent SSM measured at the stations (Figure 4). In general, the SMAP products have a larger model error compared to the empirical model established using Sentinel-1 data at these four locations.
eral, the SMAP products have a larger model error (Figure 4). This was most likely due to the use of fine-resolution environmental covariates as compared to the SMAP model [16].

4. Discussion

4.1. Importance of Covariates on SSM Retrieval at USCRN Stations

Compared with other “black-box” models such as artificial neural networks used to retrieve SSM (e.g., [27]), the use of MLR, Cubist and Random Forest algorithms makes the empirical models relatively easy to interpret. They also illustrate the relative importance of the covariates for retrieving SSM. As shown in Tables 2–4, the SSM dynamics at the USCRN stations are influenced by backscatter data and environmental variables, including soil properties, LC, terrain parameters. Among the three models, backscatter data and soil properties are most important in retrieving SSM, followed by several terrain parameters, and then LC types.

This highlights the need for measurement of high-resolution backscatter data from SAR sensors, as well as the development of high-resolution maps of soil properties for the future improvement of SSM empirical or physical retrieval models. Besides, high-resolution digital elevation models are also important as aspect, TPI, and TRI were used in the conditions and model of the Cubist model and found to be significant in the MLR and Random Forest model.

4.2. Implications of the Empirical SSM Retrieval Models

The empirical models established in this study have several advantages. First, the Cubist model is more accurate than the SMAP Level 3 radiometer-based SSM product (a resolution of 36 km) at the selected USCRN stations, particularly within Shrub/Scrub, Herbaceous, and Cultivated Crops (Figure 4). This was most likely due to the use of fine-resolution environmental covariates as compared to the SMAP model [16].

Second, the MLR model was worse than the Cubist and Random Forest models because the simplicity of the MLR model cannot account for the complex relationship between VWC and microwave...
data. This suggests that non-linear models should be used to retrieve SSM using Sentinel-1 data and is consistent with the previous studies that use non-linear models for predicting SSM (e.g., [54–56]). The Random Forest model over-fits the calibration dataset, so it should be used with caution for the future development of SSM retrieval models.

Third, the Cubist model is simple as no detailed information such as the ground roughness, emissivity, and opacity of the vegetation are required unlike those used in the physical models (e.g., [16,21]). Instead, we only used environmental covariates (soil properties, land cover, terrain parameters) that have become available across large spatial extents from various sources of remote sensing and ancillary data. When historical SSM measurements are available from the ground monitoring networks, SSM dynamics can be retrieved using a combination of Sentinel-1 and ancillary data in the future under similar land surface conditions. Because these environmental covariates are widely available across the US and the world [57–59], it is worth further exploring this approach to a large spatial extent (across the US or globally) by including more SSM network measurements [9].

4.3. Limitations of the Empirical SSM Retrieval Models

There are a few limitations of the empirical models. First, the empirical model established in this study can only retrieve SSM well in three LC types (Shrub/Scrub, Herbaceous, and Cultivated Crops). Future work is required to establish SSM retrieval models in other LC types, such as Hay/Pasture and Forest. The effective measuring depth of C-band SAR is around 0.05 m, so it is possible to combine Sentinel-1 data with other microwave data, such as the radiometer of the SMAP mission [29] and AMSR2. In a similar study, Alexakis et al. showed that Sentinel-1 backscatter data can be combined with vegetation indices (e.g., NDVI) to estimate SSM using a non-linear approach such as an artificial neural network (ANN) [56].

Alternatively, active and passive remote sensing data could be used to retrieve soil moisture coupled with statistical, empirical, and backscattering models [60]. It is also possible to assimilate these microwave data with other remote sensing satellite products, including optical and thermal bands, such as LANDSAT and Sentinel-2 (e.g., [61]) and ECOSTRESS [62] satellites to better account for the differences in leaf area and land surface radiance due to the spatial-temporal variations in SSM. Alternatively, a physical model such as Water Cloud Model could be effectively used for SSM retrieval from Synthetic Aperture Radar (SAR) imagery [63]. It is also feasible to combine multi-sensor satellite data from microwave and optical sensors to retrieve SSM using a hybrid approach [64].

Second, to implement this SSM model for irrigation scheduling whereby SSM measurements from sparse soil moisture measurements are available in the field (e.g., [65]), process models are required to forecast soil water storage and movement within the root-zone (e.g., [66,67]). This can be achieved by assimilating VWC measurements at multiple depths from soil moisture probes with mechanistic models using ensemble Kalman filtering (e.g., [68,69]). Alternatively, empirical and mechanistic models may be used to obtain deeper-layer soil water content from the satellite-derived SSM measurements [70–72].

Lastly, the small-scale roughness element is often used to model the backscatter signal from microwave radar [21,37,73]. Because most DEM data has a limited resolution (10 m), it is also possible to include high-resolution tomography radar imaging for improved terrain delineation under certain regions [74]. To apply the SSM model across a larger spatial extent, it is worth exploring how to downscale the roughness parameters from coarse-resolution DEM for developing the soil water retrieval model.

5. Conclusions

Empirical models are established for predicting surface soil moisture (SSM, 0–0.05 m) in 2018 based on historical (2016–2017) Sentinel-1 and ancillary data at the U.S. Climate Reference Network soil moisture. Multiple linear regression (MLR), Cubist, and Random Forest models are compared to fit the models using 30-m Sentinel-1 data, a 10-m digital elevation model, 30-m Polaris soil property maps, and 30-m land cover maps of the USA.
The Cubist model is better than the MLR and Random Forest (R² = 0.68 and RMSE = 0.06 m³ m⁻³ for validation). The Cubist model performs best in Shrub/Scrub, followed by Herbaceous and Cultivated Crops but poorly in Hay/Pasture and shows better performance than the SSM retrieved by SMAP Radiometer at the 36-km resolution at several USCRN stations due to the use of fine-resolution environmental covariates. The SSM model performance is mostly affected by backscatter data, soil properties and terrain parameters, followed by land cover types. This indicates the need to improve the spatial resolution and accuracy of these land surface parameter products at the regional and global scales.

Future work is required to improve the model performance by including more SSM measurements, assimilating Sentinel-1 data with other remote sensing products such as microwave (SMAP, AMSR2), optical and thermal (LANDSAT, Sentinel-2, ECOSTRESS) satellites as well as developing high-resolution topography maps.

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Appendix A

Table A1. List of acronyms used in the paper.

| Acronyms  | Full Form                                      |
|-----------|------------------------------------------------|
| USCRN     | U.S. Climate Reference Network                |
| S-1       | Sentinel-1                                     |
| SAR       | Synthetic Aperture Radar                      |
| VV        | Vertical transmit/vertical receive            |
| VH        | Vertical transmit/horizontal receive          |
| SMAP      | Soil Moisture Active Passive                  |
| AMSR2     | Advanced Microwave Scanning Radiometer 2     |
| SSM       | Surface Soil Moisture                         |
| VWC       | Volumetric Water Content                      |
| LC        | Land Cover                                    |
| ROI       | Region of Interest                            |
| GRD       | Ground Range Detected                        |
| SRTM      | Shuttle Radar Topography Mission              |
| DEM       | Digital Elevation Model                       |
| USGS      | U.S. Geological Survey                        |
| TRI       | Terrain Ruggedness Index                     |
| TWI       | Topographic Wetness Index                    |
| TPI       | Topographic Position Index                   |
| NDVI      | Normalized Difference Vegetation Index        |
| POLARIS   | Probabilistic Remapping of Soil Survey Geographic |
| SOM       | Soil Organic Matter                           |
| BD        | Bulk Density                                  |
| MLR       | Multiple Linear Regression                    |
| RF        | Random Forest                                 |
| ANN       | Artificial Neural Network                     |
| SD        | Standard Deviation                            |
| ME        | Mean Error                                    |
| RMSE      | Root Mean Square Error                        |
| R²        | Coefficient of Determination                  |
SOM Soil Organic Matter 
BD Bulk Density 
MLR Multiple Linear Regression 
RF Random Forest 
ANN Artificial Neural Network 
SD Standard Deviation 
ME Mean Error 
RMSE Root Mean Square Error 
R^2 Coefficient of Determination 

Figure A1. Summary of Cubist rules.

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