Optomechanical resonator-enhanced atom interferometry

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Matter-wave interferometry and spectroscopy of optomechanical resonators offer complementary advantages. Interferometry with cold atoms is employed for accurate and long-term stable measurements, yet it is challenged by its dynamic range and cyclic acquisition. Spectroscopy of optomechanical resonators features continuous signals with large dynamic range, however it is generally subject to drifts. In this work, we combine the advantages of both devices. Measuring the motion of a mirror and matter waves interferometrically with respect to a joint reference allows us to operate an atomic gravimeter in a seismically noisy environment otherwise inhibiting readout of its phase. Our method is applicable to a variety of quantum sensors and shows large potential for improvements of both elements by quantum engineering.
The ability to coherently manipulate massive particles by means of interaction with light has given rise to a variety of realisations of matter-wave interferometers. Today, these are widely employed in metrology and tests of fundamental physics\(^1\)–\(^{16}\). Especially the class of interferometers based on light pulses, first pioneered by Kasevich and Chu\(^{17,18}\), finds a broad range of applications in inertial sensing\(^{18,19}\)–\(^{28}\). In these measurements, the phase reference is usually realised by a mirror retroreflecting the light pulses towards the matter waves. Inertial effects acting on the matter waves and on the phase reference are indistinguishable. As a result, seismic noise contributes significantly to the instability of atomic inertial sensors, and is even the dominant noise source in state-of-the-art matter-wave gravimeters\(^{19,21}\). As such, the instability of atomic inertial sensors is a challenge of applications in inertial sensing\(^{18}\).

In recent years, developments in the quantum engineering of optomechanical resonators have yielded devices with exciting applications in fields such as quantum information, fundamental physics and, likewise, in inertial sensing\(^{38,39}\). To this end, optically reading out length variations of an optical cavity allows determination of acting accelerations with high bandwidth and resolution. In addition, interfaces between cold atoms and micromechanical cantilevers\(^{40}\) or nanomembranes\(^{41}\) have been demonstrated, showing the potential of these hybrid systems for fundamental physics.

Here, we combine a high-bandwidth optomechanical resonator with a long-term stable light-pulse atom interferometer, and measure the accelerations of the resonator’s test mass and a freely falling cloud of atoms relative to the atom interferometer’s inertial reference. Our atom interferometer measures gravity under strong seismic perturbations without loss of phase information. In contrast to previous approaches, our method merges two systems both benefiting from the large toolbox of methods usually exploited in optical spectroscopy and photonics into a highly customisable device for atom interferometry in rough environments.

**Results and discussion**

We operate a Kasevich–Chu interferometer\(^{17}\) combined with an optomechanical resonator attached to the mirror providing the phase reference for the interferometer as a graviometer (Fig. 1a, b and details in the “Methods” section). Ambient vibrational noise couples to the retroreflector at a weighted acceleration level of 3 mm s\(^{-2}\) per cycle. This leads to phase excursions exceeding a single fringe during one interferometric measurement with the readout appearing to be random due to the underlying 2\(\pi\) phase ambiguity (Fig. 1c). Accordingly, the atom interferometer signal, i.e., the relative population of the two ports, features a bimodal distribution visible in Fig. 2a. However, ambient vibrational noise also results in a displacement of the resonator test mass, which is recorded by the signal retroreflected from the optomechanical resonator (Fig. 1d). The records of the optomechanical resonator make it possible to reconstruct the atomic interference pattern (Fig. 2b). The signal from the optomechanical resonator is constrained to the band of interest. We apply high-pass filters at 0.8 Hz to suppress low-frequency drifts, as well as a digital low-pass filter at 50 Hz, the atom interferometer’s corner frequency (see “Methods” section). We subsequently sample it digitally over 60 ms centred around the central light pulse of each interferometer cycle. The phase correction is finally calculated from the signal utilising the acceleration sensitivity function describing the atom interferometer’s phase response\(^{42,43}\).

Residual systematic biases can be experimentally analysed as shown for commercial sensors in the ref. \(^{34}\).

Using our method, we measure the local gravitational acceleration \(g\) in an approximately 22 h-long, interruption-free, measurement series otherwise impossible when operating both sensors alone. By suppressing vibrational noise, our sensor fusion method improves the overall short-term stability by a factor 8 (Fig. 3). Figure 4 illustrates the present and projected features of the atom interferometer, the optomechanical resonator, and the combination of both.

Our optomechanical resonator features a sensitivity comparable to commercial accelerometers, and we expect a large potential for improvements for both quantum-optical devices. The sensor fusion performance is nevertheless limited by low frequency noise (Fig. 4, solid blue trace). It displays a RMS white acceleration noise of \(1 \times 10^{-5} \text{ m s}^{-2} \text{ Hz}^{-1/2}\) between 10 and 50 Hz. Pink noise (\(\propto f^{-1}\)) dominates from 1 to 10 Hz. Below 1 Hz, Brownian noise (\(\propto f^{-2}\)) processes mainly caused by the optical fibre employed for interrogating the resonator prevail. Since the resonator’s sensitivity to accelerations increases quadratically with decreasing mechanical resonance frequency and linearly with optical finesse, there is room for improvements by trading sensitivity against larger bandwidth and dynamic range. We foresee an optimisation of the hybrid sensor (Fig. 4, solid orange trace) by tuning the resonance frequency to 1500 Hz to increase the bandwidth, improving the optical finesse to 1600 by high-reflectivity coating\(^{38}\), and the readout by an order of magnitude as compared to ref. \(^{38}\) by means of spectroscopy techniques developed for ultrastable resonators, e.g., Pound–Drever–Hall locking\(^{44,45}\). Millimetre-sized optomechanical resonators have already demonstrated sensitivities of \(1 \times 10^{-6} \text{ m s}^{-2} \text{ Hz}^{-1/2}\) over bandwidths up to 12 kHz.

Additionally, pathways exist for future atom interferometers customised for gravimetry, as discussed in ref. \(^{46}\). The sensitivity can be enhanced by operating the device with \(T = 35\) ms, a cycle rate of 1 Hz, higher-order Bragg processes transferring \(4 \cdot k_{\text{eff}}\) and a reduced phase noise of 3 mrad. By improving the atom interferometer and tuning the optomechanical resonator, it is plausible that the intrinsic noise can be lowered to \(6 \times 10^{-8} \text{ m s}^{-2} \text{ Hz}^{-1/2}\) under seismic noise as described in the ref. \(^{47}\). This target performance is comparable to the noise obtained in a quiet environment with an active vibration isolation\(^{19}\) and outperforms transportable, commercial devices\(^{23}\).

Many atomic gravimeters employ rubidium and generate the light for manipulating the atoms by second harmonic generation from fibre lasers in the telecom C-band\(^{48,49}\). The inclusion of the optomechanical resonator therefore requires only minor hardware changes and can be performed with an all-fibre setup. The resonator can be implemented directly into inertial reference mirrors under vacuum, thus improving the mechanical quality factor while supporting miniaturisation of the overall setup. It does not emit notable heat, and is nonmagnetic. Consequently, it does not induce systematic errors due to black body radiation\(^{50}\) or due to spurious magnetic fields coupling to the matter waves\(^{30,51}\), and neither do external magnetic fields couple to the resonator test mass. Moreover it can be easily merged with the retroreflection mirror of the atom interferometer. In addition, devices with different resonance frequencies or different orientations will grant access to larger bandwidth and multiple sensitive axes. Last but not least, the small volume of cubic millimetres offers great prospects for being integrated on atom chip sensors\(^{46}\) and, hence, a large potential for miniaturisation of the sensor head.

Our method shares analogies with atomic clocks by hybridisation of long-term and short-term references. Beyond this, our optical sensor might be used for compensating inertial
noise in the resonators of optical clocks, e.g., in transportable setups.

Conclusion. In conclusion, we have demonstrated an atom interferometer enhanced by an optomechanical resonator. We show operation of the atom interferometer under circumstances otherwise impeding phase measurements. Inertial forces on the atoms and on the resonator mirror are measured to the same reference permitting a direct comparison, and high common mode noise suppression in the differential signal. Our method is not restricted to atomic gravimeters and could be beneficial to nearly all atom interferometric sensors and even improve laser interferometers in environments with large inertial noise, thus replacing bulky vibration isolation and motion sensors. In particular, the achievable large dynamic range opens up great perspectives for the use of atomic sensors for inertial navigation and airborne gravimetry. Finally, a possible modification of our setup’s topology would ensure that the atom-optics light field is...
reflected directly off a micromechanical test mass. In future experiments, we envisage exciting research on coherent light-mediated coupling of matter waves and mechanical systems with pulsed instead of cw-interaction.

Methods

Atom interferometer. Our setup (Fig. 1a, b), which was employed as a differential gravimeter in the refs. 6,37, comprises a Kasevich–Chu interferometer.7 In a π/2 − π − π/2 pulse sequence, stimulated two-photon Raman transitions coherently split, redirect, and recombine matter waves of 87Rb. The interferometer phase is determined by measuring the number of atoms in output ports 1 and 2 with state-selective fluorescence detection. To leading order, a constant acceleration \( \vec{a} \) of the atoms induces a phase shift

\[
\Delta \phi = \vec{a}_{\text{eff}} \cdot \vec{a} \cdot T^2,
\]

where \( \vec{a}_{\text{eff}} \) is the photon recoil transferred to the atoms via a Raman process, and \( T \) denotes the time between two subsequent light pulses. A chirp of the relative frequency of the lasers cancels the phase induced by acceleration, and is a measure for the latter. The atom interferometer’s response to vibrational noise can be described using the sensitivity formalism.5,41 Notably, the response is flat in a band between DC and up to the corner frequency \( 1/(2T) \), above which it features a low-pass behaviour. Typically, the interferometer’s response is adjusted by varying \( T \) such that ambient noise induces phase shifts well within one fringe. At quiet conditions, i.e., with an operating vibration isolation system, the interferometer, which we operate at a cycle rate of 0.6 Hz, features a fringe contrast of \( \approx 30\% \) and a Raman phase locked-loop-limited phase noise of 3 mrad (orange dashed line).

Data analysis. In order to suppress systematic shifts independent of the direction of momentum transfer we use the \( k \)-reversal method.38,39 The interferometer measures ten times in each direction of momentum transfer over a period of 18 s. For each scattering direction, we create histograms out of the normalised output population of the interferometer. Hereby each individual histogram comprises data accumulated over a 9000 s period. From each histogram, we extract the interferometer response’s amplitude and offset as shown in Fig. 2. We subsequently estimate the ambient noise in Fig. 3 from the phase corrections made during postcorrection. Accordingly, the data resembles the underlying ambient acceleration noise after weighting it with the atom interferometer’s transfer function. The first uncorrected value of \( \approx 3 \) mm s\(^{-2}\) per cycle also manifests in the 1/6 width of the Gaussian-shaped spread in Fig. 2c.

Optomechanical sensor. Mirrors forming the optomechanical resonator, which has a volume on the order of a few hundred mm\(^3\), are made from the vibration frequency at tip of a fused silica test mass supported by a stiff u-shaped flexible mount, the cantilever (Fig. 1a), following the design of ref. 81. Our sensor features an optical finesse of about two, a resonance frequency of \( \omega_0 = 2 \times 678.5 \text{ Hz} \) and a mechanical quality factor of \( Q = 630 \). Due to its stiffness the optomechanical resonator can be described as an ideal harmonic oscillator. Below the resonance frequency, displacement of the test mass \( X \) as a function of vibration frequency \( \omega \) linearly depends on the acting acceleration \( A \).

\[
X(\omega) = \frac{1}{\omega_0^2 - \omega^2 + i \frac{\omega}{Q}},
\]

and is therefore flat. By means of more advanced data analysis, the upper limit of the usable bandwidth can be extended beyond the mechanical resonance. Using adhesive bonding, the resonator is attached to a two-inch square mirror retroreflecting the light pulses driving the atom interferometer. The resonator’s acceleration-sensitive axis is aligned collinearly with the retroreflector’s normal vector (Fig. 1a) by orienting the outer edges of both devices parallel. The motion of the test mass is read out with a fibre-based optical setup based on telecom components comprising a tunable laser operating at a wavelength near 1560 nm protected by an optical isolator (Fig. 5). The sensor has a quarter wave plate incorporated in its lead fibre thereby enabling us to separate the signal reflected off the resonator using a polarising beam splitter. Additionally, a small fraction of the laser light is split off before the resonator using a 90:10 splitter. Making use of differential data acquisition of photo detectors PD 1 and 2 we can therefore cancel the test mass readout with a 90:10 splitter. Making use of differential data acquisition of photo detectors PD 1 and 2 we can therefore cancel the test mass readout with a 90:10 splitter. Making use of differential data acquisition of photo detectors PD 1 and 2 we can therefore cancel the test mass readout with a 90:10 splitter. Making use of differential data acquisition of photo detectors PD 1 and 2 we can therefore cancel the test mass readout with a 90:10 splitter.

Data availability. The data used in this manuscript are available from the corresponding author upon reasonable request.

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Fig. 5 Displacement readout system for the optomechanical resonator. Laser light split off for intensity noise correction and light reflected back from the optomechanical resonator (OMR) are detected on photo diodes (PD 1 & 2). Both signals are passed to current-to-voltage converters (I/V) followed by high-pass filters (HPF) at 0.8 Hz and are subsequently enhanced by amplifiers (Amp). Finally, the difference signal is digitally low-pass filtered (LPF) at 50 Hz.
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Author contributions
W.E., E.M.R., C.S., and D.S. designed the atom interferometer and its laser system. L.L.R., H.A., D.N., and D.S. contributed to the design of the atom interferometer and its laser system and realised the overall setup. A.R., M.M., L.K., L.C., R.S., C.B., and F.G. designed, built, and tested the optomechanical resonator and designed the readout laser system. A.R., C.M., D.T., and E.W. built and characterised the laser system for readout. L.L.R., F.G., L.K., and A.R. implemented the optomechanical resonator in the atom interferometer setup. L.L.R., H.A., D.N., and A.R. operated the final experimental setup. Sv.A., M.G., and C.S. contributed to the data acquisition system utilised for post correction. A.R., D.N., C.S., and L.L.R. performed the analysis of the data presented in this manuscript. L.L.R., D.S., and F.G. drafted the initial manuscript. A.R., M.M., C.S., D.T., E.W., E.M.R., and L.K. provided major input to the manuscript and all authors critically reviewed and approved of the final version.

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Competing interests
Related to the patent Optomechanical Inertial Reference for Atom Interferometers (WO 2020/168314 A1) filed by the University of Arizona (UA), L.L.R. (UA affiliate), F.G. (UA affiliate and inventor), E.M.R. (inventor), and D.S. (inventor) declare competing financial interests. The patent covers the use of opto-mechanical systems as inertial references for atom interferometry. All other authors declare no competing interests.

Additional information
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