SAL: Sign Agnostic Learning of Shapes from Raw Data

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Figure 1: We introduce SAL: Sign Agnostic Learning for learning shapes directly from raw data, such as triangle soups (left in each gray pair; back-faces are in red). Right in each gray pair - the surface reconstruction by SAL of test raw scans; in gold - SAL latent space interpolation between adjacent gray shapes. Raw scans are from the D-Faust dataset [7].

Abstract

Recently, neural networks have been used as implicit representations for surface reconstruction, modelling, learning, and generation. So far, training neural networks to be implicit representations of surfaces required training data sampled from a ground-truth signed implicit functions such as signed distance or occupancy functions, which are notoriously hard to compute.

In this paper we introduce Sign Agnostic Learning (SAL), a deep learning approach for learning implicit shape representations directly from raw, unsigned geometric data, such as point clouds and triangle soups.

We have tested SAL on the challenging problem of surface reconstruction from an un-oriented point cloud, as well as end-to-end human shape space learning directly from raw scans dataset, and achieved state of the art reconstructions compared to current approaches. We believe SAL opens the door to many geometric deep learning applications with real-world data, alleviating the usual painstaking, often manual pre-process.

1. Introduction

Recently, deep neural networks have been used to reconstruct, learn and generate 3D surfaces. There are two main approaches: parametric [19, 4, 40, 15] and implicit [12, 30, 28, 2, 14, 17]. In the parametric approach neural nets are used as parameterization mappings, while the implicit approach represents surfaces as zero level-sets of neural networks:

\[ S = \{ x \in \mathbb{R}^3 \mid f(x; \theta) = 0 \}, \]  

where \( f : \mathbb{R}^3 \times \mathbb{R}^m \rightarrow \mathbb{R} \) is a neural network, e.g., multilayer perceptron (MLP). The benefit in using neural networks as implicit representations to surfaces stems from their flexibility and approximation power (e.g., Theorem 1 in [2]) as well as their efficient optimization and generalization properties.

So far, neural implicit surface representations were mostly learned using a regression-type loss, requiring data samples from a ground-truth implicit representation of the surface, such as a signed distance function [30] or an occupancy function [12, 28]. Unfortunately, for the common raw form of acquired 3D data \( \mathcal{X} \subset \mathbb{R}^3 \), i.e., a point cloud or a triangle soup\(^1\), no such data is readily available and computing an implicit ground-truth representation for the underlying surface is a notoriously difficult task [5].

In this paper we advocate Sign Agnostic Learning (SAL), defined by a family of loss functions that can be used directly with raw (unsigned) geometric data \( \mathcal{X} \) and produce signed implicit representations of surfaces. An important application for SAL is in generative models such as variational auto-encoders [24], learning shape spaces directly.

\(^1\) A triangle soup is a collection of triangles in space, not necessarily consistently oriented or a manifold.
from the raw 3D data. Figure 1 depicts an example where collectively learning a dataset of raw human scans using SAL overcomes many imperfections and artifacts in the data (left in every gray pair) and provides high quality surface reconstructions (right in every gray pair) and shape space (interpolations of latent representations are in gold).

We have experimented with SAL for surface reconstruction from point clouds as well as learning a human shape space from the raw scans of the D-Faust dataset [7]. Comparing our results to current approaches and baselines we found SAL to be the method of choice for learning shapes from raw data, and believe SAL could facilitate many computer vision and computer graphics shape learning applications, allowing the user to avoid the tedious and unsolved problem of surface reconstruction in preprocess.

2. Previous work

2.1. Surface learning with neural networks

Neural parameteric surfaces. One approach to represent surfaces using neural networks is parametric, namely, as parameterization charts \( f : \mathbb{R}^2 \rightarrow \mathbb{R}^3 \), Groueix et al. [19] suggest to represent a surface using a collection of such parameterization charts (i.e., atlas); Williams et al. [40] optimize an atlas with proper transition functions between charts and concentrate on reconstructions of individual surfaces. Sinha et al. [32, 33] use geometry images as global parameterizations, while [27] use conformal global parameterizations to reduce the number of degrees of freedom of the map. Parametric representation are explicit but require handling of coverage, overlap and distortion of charts.

Neural implicit surfaces. Another approach to represent surfaces using neural networks, which is also the approach taken in this paper, is using an implicit representation, namely \( f : \mathbb{R}^3 \rightarrow \mathbb{R} \) and the surface is defined as its zero level-set, equation 1. Some works encode \( f \) on a volumetric grid such as voxel grid [41] or an octree [36]. More flexibility and potentially more efficient use of the degrees of freedom of the model are achieved when the implicit function \( f \) is represented as a neural network [12, 30, 28, 2, 17]. In these works the implicit is trained using a regression loss of the signed distance function [30], an occupancy function [12, 28] or via particle methods to directly control the neural level-sets [2]. Excluding the latter that requires sampling the zero level-set, all regression-based methods require ground-truth inside/outside information to train the implicit \( f \). In this paper we present a sign agnostic training method, namely training method that can work directly with the raw (unsigned) data.

Shape representation learning. Learning collections of shapes is done using Generative Adversarial Networks (GANs) [18], auto-encoders and variational auto-encoders [24], and auto-decoders [8]. Wu et al. [41] use GAN on a voxel grid encoding of the shape, while Ben-Hamu et al. [4] apply GAN on a collection of conformal charts. Dai et al. [13] use encoder-decoder architecture to learn a signed distance function to a complete shape from a partial input on a volumetric grid. Stutz et al. [34] use variational auto-encoder to learn an implicit surface representations of cars using a volumetric grid. Baqutdinov et al. [3] use variational auto-encoder with a constant mesh to learn parametrizations of faces shape space. Litany et al. [25] use variational auto-encoder to learn body shape embeddings of a template mesh. Park et al. [30] use auto-decoder to learn implicit neural representations of shapes, namely directly learns a latent vector for every shape in the dataset. In our work we also make use of a variational auto-encoder but differently from previous work, learning is done directly from raw 3D data.

2.2. Surface reconstruction.

Signed surface reconstruction. Many surface reconstruction methods require normal or inside/outside information. Carr et al. [9] were among the first to suggest using a parametric model to reconstruct a surface by computing its implicit representation; they use radial basis functions (RBFs) and regress at inside and outside points computed using oriented normal information. Kazhdan et al. [22, 23] solve a Poisson equation on a volumetric discretization to extend points and normals information to an occupancy indicator function. Walder et al. [38] use radial basis functions and solve a variational hermite problem (i.e., fitting gradients of the implicit to the normal data) to avoid trivial solution. In general our method works with a non-linear parametric model (MLP) and therefore does not require a-priori space discretization nor works with a fixed linear basis such as RBFs.

Unsigned surface reconstruction. More related to this paper are surface reconstruction methods that work with unsigned data such as point clouds and triangle soups. Zhao et al. [43] use the level-set method to fit an implicit surface to an unoriented point cloud by minimizing a loss penalizing distance of the surface to the point cloud achieving a sort of minimal area surface interpolating the points. Walder et al. [37] formulates a variational problem fitting an implicit RBF to an unoriented point cloud data while minimizing a regularization term and maximizing the norm of the gradients; solving the variational problem is equivalent to an eigenvector problem. Mullen et al. [29] suggests to sign an unsigned distance function to a point cloud by a multi-stage algorithm first dividing the problem to near and far
3. Sign agnostic learning

Given a raw input geometric data, $\mathcal{X} \subset \mathbb{R}^3$, e.g., a point cloud or a triangle soup, we are looking to optimize the weights $\theta \in \mathbb{R}^m$ of a network $f(x; \theta)$, where $f : \mathbb{R}^3 \times \mathbb{R}^m \to \mathbb{R}$, so that its zero level-set, equation 1, is a surface approximating $\mathcal{X}$.

We introduce the Sign Agnostic Learning (SAL) defined by a loss of the form

$$\text{loss}(\theta) = \mathbb{E}_{x \sim D_{\mathcal{X}}} \tau\big(f(x; \theta), h_{\mathcal{X}}(x)\big),$$

where $D_{\mathcal{X}}$ is a probability distribution defined by the input data $\mathcal{X}$; $h_{\mathcal{X}}(x)$ is some unsigned distance measure to $\mathcal{X}$; and $\tau : \mathbb{R} \times \mathbb{R}_+ \to \mathbb{R}$ is a differentiable unsigned similarity function defined by the following properties:

(i) **Sign agnostic:** $\tau(-a, b) = \tau(a, b)$, $\forall a \in \mathbb{R}$, $b \in \mathbb{R}_+$.

(ii) **Monotonic:** $\frac{\partial \tau}{\partial a}(a, b) = \rho(a - b)$, $\forall a, b \in \mathbb{R}_+$,

where $\rho : \mathbb{R} \to \mathbb{R}$ is a monotonically increasing function with $\rho(0) = 0$. An example of an unsigned similarity is $\tau(a, b) = ||a| - b|$.

To understand the idea behind the definition of the SAL loss, consider first a standard regression loss using $\tau(a, b) = |a - b|$ in equation 2. This would encourage $f$ to resemble the unsigned distance $h_{\mathcal{X}}$ as much as possible. On the other hand, using the unsigned similarity $\tau$ in equation 2 introduces a new local minimum of loss where $f$ is a signed function such that $|f|$ approximates $h_{\mathcal{X}}$. To get this desirable local minimum we later design a network weights’ initialization $\theta^0$ that favors the signed local minima.

As an illustrative example, the inset depicts the one dimensional case ($d = 1$) where $\mathcal{X} = \{x_0\}$, $h_{\mathcal{X}}(x) = |x - x_0|$, and $\tau(a, b) = ||a| - b|$, which satisfies properties (i) and (ii), as discussed below; the loss therefore strives to minimize the area of the yellow set. When initializing the network parameters $\theta = \theta^0$ properly, the minimizer $\theta^*$ of loss defines an implicit $f(x; \theta^*)$ that realizes a signed version of $h_{\mathcal{X}}$ in this case $f(x; \theta^*) = x - x_0$. In the three dimensional case the zero level-set $S$ of $f(x; \theta^*)$ will represent a surface approximating $\mathcal{X}$.

To theoretically motivate the loss family in equation 2 we will prove that it possesses a **plane reproduction** property. That is, if the data $\mathcal{X}$ is contained in a plane, there is a critical weight $\theta^*$ reconstructing this plane as the zero level-set of $f(x; \theta^*)$. Plane reproduction is important for surface approximation since surfaces, by definition, have an approximate tangent plane almost everywhere [16].

We will explore instantiations of SAL based on different choices of unsigned distance functions $h_{\mathcal{X}}$, as follows.
Unsigned distance functions. We consider two \( p\)-distance functions: For \( p = 2 \) we have the standard \( L^2 \) (Euclidean) distance

\[
h_2(z) = \min_{x \in \mathcal{X}} \| z - x \|_2,
\]

and for \( p = 0 \) the \( L^0 \) distance

\[
h_0(z) = \begin{cases} 
0 & z \in \mathcal{X} \\
1 & z \notin \mathcal{X}.
\end{cases}
\]

Unsigned similarity function. Although many choices exist for the unsigned similarity function, in this paper we take

\[
\tau_\ell(a, b) = ||a| - b|^{\ell},
\]

where \( \ell \geq 1 \). The function \( \tau_\ell \) is indeed an unsigned similarity: it satisfies (i) due to the symmetry of \( |\cdot| \); and since

\[
\frac{\partial \tau_\ell}{\partial a} = \ell |a| - b|^{\ell-1} \text{sign}(a - b \text{sign}(a))
\]

it satisfies (ii) as well.

Distribution \( D_X \). The choice of \( D_X \) is depending on the particular choice of \( h_X \). For \( L^2 \) distance, it is enough to make the simple choice of splatting an isotropic Gaussian, \( \mathcal{N}(x, \sigma^2 I) \), at every point (uniformly randomized) \( x \in \mathcal{X} \); we denote this probability \( \mathcal{N}_\sigma(\mathcal{X}) \); note that \( \sigma \) can be taken to be a function of \( x \in \mathcal{X} \) to reflect local density in \( \mathcal{X} \). In this case, the loss takes the form

\[
\text{loss}(\theta) = \mathbb{E}_{z \sim \mathcal{N}_\sigma(\mathcal{X})} | | f(z; \theta) | | - h_2(z)^\ell.
\]

For the \( L^0 \) distance however, \( h_X(x) \neq 1 \) only for \( x \in \mathcal{X} \) and therefore a non-continuous density should be used; we opt for \( \mathcal{N}(x, \sigma^2 I) + \delta_x \), where \( \delta_x \) is the delta distribution measure concentrated at \( x \). The loss takes the form

\[
\text{loss}(\theta) = \mathbb{E}_{z \sim \mathcal{N}_\sigma(\mathcal{X})} | | f(z; \theta) | | - 1 | | + \mathbb{E}_{x \sim \mathcal{X}} | | f(x; \theta) | | ^\ell.
\]

Remarkably, the latter loss requires only randomizing points \( z \) near the data samples without any further computations involving \( \mathcal{X} \). This allows processing of large and/or complex geometric data.

Neural architecture. Although SAL can work with different parametric models, in this paper we consider a multilayer perceptron (MLP) defined by

\[
f(x; \theta) = \varphi(w^T f_k \circ f_{k-1} \circ \cdots \circ f_1(x) + b),
\]

and

\[
f_i(y) = \nu(W_i y + b_i), W \in \mathbb{R}^{d_{i+1} \times d_i}, b_i \in \mathbb{R}^{d_{i+1}},
\]

where \( \nu(a) = (a)_+ \) is the ReLU activation, and \( \theta = (w, b, W_1, b_1, \ldots, W_l, b_l) \); \( \varphi \) is a strong non-linearity, as defined next:

2D example. The two examples in Figure 2 show case the SAL for a 2D point cloud, \( \mathcal{X} = \{ x_i \}_{i=1}^8 \subset \mathbb{R}^2 \), (shown in gray) as input. These examples were computed by optimizing equation 6 (right column) and equation 7 (left column) with \( \ell = 1 \) using the \( L^2 \) and \( L^0 \) distances (resp.). The architecture used is an 8-layer MLP; all hidden layers are 100 neurons wide, with a skip connection to the middle layer.

Notice that both \( h_X(x) \) and its signed version are local minima of the loss in equation 2. These local minima are stable in the sense that there is an energy barrier when moving from one to the other. For example, to get to a solution as in Figure 2(b) from the solution in Figure 2(d) one needs to flip the sign in the interior or exterior of the region defined by the black line. Changing the sign continuously will result in a considerable increase to the SAL loss value.

We elaborate on our initialization method, \( \theta = \theta^0 \), that in practice favors the signed version of \( h_X \) in the next section.
4. Geometric network initialization

A key aspect of our method is a proper, geometrically motivated initialization of the network’s parameters. For MLPs, equations 8-9, we develop an initialization of its parameters, \( \theta = \theta^0 \), so that \( f(x; \theta^0) \approx \varphi(\|x\| - r) \), where \( \|x\| - r \) is the signed distance function to an \( r \)-radius sphere. The following theorem specify how to pick \( \theta^0 \) to achieve this:

**Theorem 1.** Let \( f \) be an MLP (see equations 8-9). Set, for \( 1 \leq i \leq \ell, b_i = 0 \) and \( W_i \) i.i.d. from a normal distribution \( \mathcal{N}(0, \sqrt{2}/\sqrt{d_{\text{out}}}) \); further set \( w = \frac{\sqrt{\pi}}{\sqrt{d_{\text{out}}}^2} \mathbf{1}, c = -r \). Then, \( f(x) \approx \varphi(\|x\| - r) \).

Figure 3 depicts level-sets (zero level-sets in bold) using the initialization of Theorem 1 with the same 8-layer MLP (using \( \varphi(a) = a \)) and increasing width of 100, 200, and 2000 neurons in the hidden layers. Note how the approximation \( f(x; \theta^0) \approx \|x\| - r \) improves as the layers’ width increase, while the sphere-like (in this case circle-like) zero level-set remains topologically correct at all approximation levels.

The proof to Theorem 1 is provided in the supplementary material; it is a corollary of the following theorem, showing how to chose the initial weights for a single hidden layer network:

**Theorem 2.** Let \( f : \mathbb{R}^d \rightarrow \mathbb{R} \) be an MLP with ReLU activation, \( \nu \), and a single hidden layer. That is, \( f(x) = w^T \nu(Wx + b) + c \), where \( W \in \mathbb{R}^{d_{\text{out}} \times d}, b \in \mathbb{R}^{d_{\text{out}}}, w \in \mathbb{R}^{d_{\text{out}}}, c \in \mathbb{R} \) are the learnable parameters. If \( b = 0 \), \( w = \frac{\sqrt{\pi}}{\sqrt{\sigma^2}^{d_{\text{out}}} \mathbf{1}, c = -r, r > 0 \), and all entries of \( W \) are i.i.d. normal \( \mathcal{N}(0, \sigma^2) \) then \( f(x) \approx \|x\| - r \). That is, \( f \) is approximately the signed distance function to a \( d-1 \) sphere of radius \( r \) in \( \mathbb{R}^d \), centered at the origin.

5. Properties

5.1. Plane reproduction

Plane reproduction is a key property to surface approximation methods since, in essence, surfaces are locally planar, i.e., have an approximating tangent plane almost everywhere [16]. In this section we provide a theoretical justification to SAL by proving a plane reproduction property. We first show this property for a linear model (i.e., a single layer MLP) and then show how this implies local plane reproduction for general MLPs.

The setup is as follows: Assume the input data \( X \subset \mathbb{R}^d \) lies on a hyperplane \( \mathcal{X} \subset \mathcal{P} \), where \( \mathcal{P} = \{ x \in \mathbb{R}^d | n^T x + c = 0 \}, n \in \mathbb{R}^d, \|n\| = 1 \), is the normal to the plane, and consider a linear model \( f(x; w, b) = \varphi(w^T x + b) \). Furthermore, we make the assumption that the distribution \( D_X \) and the distance \( h_X \) are invariant to rigid transformations, which is common and holds in all cases considered in this paper. We prove existence of critical weights \( (w^*, b^*) \) of the loss in equation 2, and for which the zero level-set of \( f, f(x; w^*, b^*) = 0 \), reproduces \( \mathcal{P} \):

**Theorem 3.** Consider a linear model \( f(x; \theta) = \varphi(w^T x + b), \theta = (w, b) \), with a strong non-linearity \( \varphi : \mathbb{R} \rightarrow \mathbb{R} \). Assume the data \( X \) lies on a plane \( \mathcal{P} = \{ x | n^T x + c = 0 \} \), i.e., \( X \subset \mathcal{P} \). Then, there exists \( \alpha \in \mathbb{R}_+ \) so that \( (w^*, b^*) = (\alpha n, \alpha c) \) is a critical point of the loss in equation 2.

This theorem can be applied locally when optimizing a general MLP (equation 8) with SAL to prove local plane reproduction. See supplementary for more details.

5.2. Convergence to the limit signed function

The SAL loss pushes the neural implicit function \( f \) towards a signed version of the unsigned distance function \( h_X \). In the \( L^0 \) case it is the inside/outside indicator function of the surface, while for \( L^2 \) it is a signed version of the Euclidean distance to the data \( X \). Figure 4 shows advanced epochs of the 2D experiment in Figure 2; note that the \( f \) in these advanced epochs is indeed closer to the signed version of the respective \( h_X \), since the indicator function and the signed Euclidean distance are discontinuous across the surface, they potentially impose quantization errors when using standard contouring algorithms, such as Marching Cubes [26], to extract their zero level-set. In practice, this phenomenon is avoided with a standard choice of stopping criteria (learning rate and number of iterations). Another potential solution is to add a regularization term to the SAL loss; we mark this as future work.

6. Experiments

6.1. Surface reconstruction

The most basic experiment for SAL is reconstructing a surface from a single input raw point cloud (without using any normal information). Figure 5 shows surface reconstructions based on four raw point clouds provided in [21] with three methods: ball-pivoting [6], variation-implicit reconstruction [21], and SAL based on the \( L^0 \) distance, i.e.,
optimizing the loss described in equation 7 with \( \ell = 1 \). The only parameter in this loss is \( \sigma \) which we set for every point in \( \mathbf{x} \in \mathcal{X} \) to be the distance to the 50-th nearest point in the point cloud \( \mathcal{X} \). We used an 8-layer MLP, \( f : \mathbb{R}^{3} \times \mathbb{R}^{m} \rightarrow \mathbb{R} \), with 512 wide hidden layers and a single skip connection to the middle layer (see supplementary material for more implementation details). As can be visually inspected from the figure, SAL provides high fidelity surfaces, approximating the input point cloud even for challenging cases of sparse and irregular input point clouds.

### 6.2. Learning shape space from raw scans

In the main experiment of this paper we trained on the D-Faust scan dataset [7], consisting of approximately 41k raw scans of 10 humans in multiple poses\(^2\). Each scan is a triangle soup, \( \mathcal{X}_i \), where common defects include holes, ghost geometry, and noise, see Figure 1 for examples.

**Architecture.** To learn the shape representations we used a modified variational encoder-decoder [24], where the encoder \( (\mu, \eta) = g(X; \theta_1) \) is taken to be PointNet [31] (specific architecture detailed in supplementary material), \( X \in \mathbb{R}^n \times 3 \) is an input point cloud (we used \( n = 128^2 \)), \( \mu \in \mathbb{R}^{256} \) is the latent vector, and \( \eta \in \mathbb{R}^{256} \) represents a diagonal covariance matrix by \( \Sigma = \text{diag} \exp \eta \). That is, the encoder takes in a point cloud \( X \) and outputs a probability measure \( \mathcal{N}(\mu, \Sigma) \). The point cloud is drawn uniformly at random from the scans, i.e., \( X \sim \mathcal{X}_i \). The decoder is the implicit representation \( f(x; w, \theta_2) \) with the addition of a latent vector \( w \in \mathbb{R}^{256} \). The architecture of \( f \) is taken to be the 8-layer MLP, as in Subsection 6.1.

**Loss.** We use SAL loss with \( L^2 \) distance, i.e., \( h_2(z) = \min_{x \in \mathcal{X}_i} \| z - x \|_2 \) the unsigned distance to the triangle soup \( \mathcal{X}_i \), and combine it with a variational auto-encoder type loss [24]:

\[
\text{Loss}(\theta) = \sum_{i} \mathbb{E}_{X \sim \mathcal{X}_i} \left[ \text{loss}_R(\theta) + \lambda \| \mu \|_1 + \| \eta + 1 \|_1 \right]
\]

\[
\text{loss}_R(\theta) = \mathbb{E}_{z \sim \mathcal{N}_\theta(x_i), \omega \sim \mathcal{N}(\mu, \Sigma)} \left[ \| f(z; w, \theta_2) - h_2(z) \|_1 \right],
\]

where \( \theta = (\theta_1, \theta_2) \), \( \| \cdot \|_1 \) is the 1-norm. \( \| \mu \|_1 \) encourages the latent prediction \( \mu \) to be close to the origin, while \( \| \eta + 1 \|_1 \) encourages the variances \( \Sigma \) to be constant \( \exp(-1) \); together, these enforce a regularization on the latent space. \( \lambda \) is a balancing weight chosen to be \( 10^{-3} \).

**Baseline.** We compared versus three baseline methods. First, AtlasNet [19], one of the only existing algorithms for learning a shape collection from raw point clouds. AtlasNet uses a parametric representation of surfaces, which is straightforward to sample. On the down side, it uses a collection of patches that tend to not overlap perfectly, and their loss requires computation of closest points between the generated and input point clouds which poses a challenge for learning large point clouds. Second, we approximate a signed distance function, \( h_2 \), to the data \( \mathcal{X}_i \) in two different ways, and regress them using an MLP as in DeepSDF [30]; we call these methods SignReg. Note that Occupancy Networks [28] and [12] regress a different signed distance function and perform similarly.

To approximate the signed distance function, \( \tilde{h}_2 \), we first tried using a state of the art surface reconstruction algorithm [23] to produce watertight manifold surfaces. However, only 28684 shapes were successfully reconstructed (\( 69\% \) of the dataset), making this option infeasible to compute \( h_2 \). We have opted to approximate the signed distance function similar to [20] with \( \tilde{h}_2(z) = n_\mathcal{X}^T(z - x_\mathcal{X}) \), where \( x_\mathcal{X} = \arg \min_{x \in \mathcal{X}} \| z - x \|_2 \) is the closest point to \( z \) in \( \mathcal{X} \); and \( n_\mathcal{X} \) is the normal at \( x_\mathcal{X} \in \mathcal{X} \). To approximate the normal \( n_\mathcal{X} \), we tested two options: (i) taking \( n^* \) directly from the original scan \( \mathcal{X}_i \) with its original orientation; and (ii) using local normal estimation using Jets [10] followed by consistent orientation procedure based on minimal spanning tree using the CGAL library [1].

Table 1 and Figure 6 show the result on a random 75%-25% train-test split on the D-Faust raw scans. We report the 5%, 50% (median), and 95% percentiles of the Chamfer distances between the surface reconstructions and the
Table 1: Reconstruction of the test set from D-Faust scans. We log the Chamfer distances of the reconstructed surfaces to the raw scans (one-sided), and ground-truth registrations; we report the 5-th, 50-th, and 95-th percentile. Numbers are reported $\times 10^3$.

| Method          | Registrations | Scans       |
|-----------------|---------------|-------------|
|                 | 5%  | Median   | 95%  | 5%  | Median   | 95%  |
| Train           |     |          |      |     |          |      |
| AtlasNet [19]   | 0.09 | 0.15     | 0.27 | 0.05 | 0.09     | 0.18 |
| Scan normals    | 2.53 | 43.99    | 292.59| 2.63 | 44.86    | 257.37|
| Jet normals     | 1.72 | 30.46    | 513.34| 1.65 | 31.11    | 453.43|
| SAL (ours)      | 0.05 | 0.09     | 0.2  | 0.05 | 0.06     | 0.09 |
| Test            |     |          |      |     |          |      |
| AtlasNet [19]   | 0.1  | 0.17     | 0.37 | 0.05 | 0.1      | 0.22 |
| Scan normals    | 3.45 | 45.03    | 294.15| 3.21 | 277.36   | 45.03 |
| Jet normals     | 1.88 | 31.05    | 489.35| 1.76 | 30.89    | 462.85|
| SAL (ours)      | 0.07 | 0.12     | 0.35 | 0.05 | 0.08     | 0.16 |

Figure 6: Reconstruction of the test set from D-Faust scans. Left to right in each column: input test scan, SAL (our) reconstruction, AtlasNet [19] reconstruction, and SignReg - signed regression with approximate Jet normals.

Table 2 demonstrates that the latent optimization method further improves predictions quality, compared to a single forward pass. In 7 and 8, we demonstrate few representative examples, where we plot left to right in each column: input test scan, SAL reconstruction with forward pass alone, and SAL reconstruction with latent optimization. Failure cases are shown in the bottom-right. Despite the little variability of humans in the training dataset (only 8 humans), 7 shows that SAL can usually fit a pretty good human shape to the unseen human scan using a single forward pass reconstruction; using latent optimization further improves the approximation as can be inspected in the different examples in this figure.

Figure 8 shows how a single forward reconstruction is able to predict the pose correctly, where latent optimization improves the prediction in terms of shape and pose.

Generalization to unseen data. In this experiment we test our method on two different scenarios: (i) generating shapes of unseen humans; and (ii) generating shapes of unseen poses. For the unseen humans experiment we trained on 8 humans (4 females and 4 males), leaving out 2 humans for test (one female and one male). For the unseen poses experiment, we randomly chose two poses of each human as a test set. To further improve test-time shape representations, we also further optimized the latent $\mu$ to better approximate the input test scan $X_i$. That is, for each test scan $X_i$, after the forward pass $(\mu, \eta) = g(X; \theta_2)$ with $X \subset X_i$, we further optimized $\text{loss}_{r_{\text{reg}}}$ as a function of $\mu$ for 800 further iterations. We refer to this method as latent optimization.
Figure 7: Reconstruction of unseen humans scans. Each column from left to right: unseen human scan, SAL reconstruction with a single forward pass, SAL reconstruction with latent optimization. Bottom-right shows failure.

Figure 8: Reconstruction of unseen pose scans. Each column from left to right: unseen pose scan, SAL reconstruction with a single forward pass, SAL reconstruction with latent optimization. Bottom-right shows failure.

Figure 9: Failure in capturing thin structures. In each pair: ground truth model (left), and SAL reconstruction (right).

Table 2: Reconstruction of the unseen human and pose from D-Faust scans. We log the Chamfer distances of the reconstructed surfaces to the raw scans (one-sided), and ground-truth registrations; we report the 5-th, 50-th, and 95-th percentile. Numbers are reported $\times 10^3$.

| Method                      | Registrations | Scans          |
|-----------------------------|---------------|----------------|
|                             | 5%  | Median | 95%  | 5%  | Median | 95%  |
| Train SAL (Pose)            | 0.08 | 0.12   | 0.25  | 0.05 | 0.07   | 0.1  |
| SAL (Human)                 | 0.06 | 0.09   | 0.18  | 0.04 | 0.06   | 0.09 |
| Test SAL (Pose)             | 0.11 | 0.37   | 2.26  | 0.07 | 0.18   | 0.93 |
| SAL + latent opt. (Pose)    | 0.08 | 0.16   | 1.12  | 0.05 | 0.09   | 0.19 |
| SAL (Human)                 | 0.26 | 0.75   | 4.99  | 0.14 | 0.34   | 1.53 |
| SAL + latent opt. (Human)   | 0.12 | 0.3    | 3.05  | 0.07 | 0.14   | 0.49 |

Limitations. SAL's limitation is mainly in capturing thin structures. Figure 9 shows reconstructions (obtained similarly to 6.1) of a chair and a plane from the ShapeNet [11] dataset; note that some parts in the chair back and the plane wheel structure are missing.

7. Conclusions

We introduced SAL: Sign Agnostic Learning, a deep learning approach for processing raw data without any preprocess or need for ground truth normal data or inside/outside labeling. We have developed a geometric initialization formula for MLPs to approximate the signed distance function to a sphere, and a theoretical justification proving planar reproduction for SAL. Lastly, we demonstrated the ability of SAL to reconstruct high fidelity surfaces from raw point clouds, and that SAL easily integrates into standard generative models to learn shape spaces from raw geometric data. One limitation of SAL was mentioned in Section 5, namely the stopping criteria for the optimization.

Using SAL in other generative models such as generative adversarial networks could be an interesting follow-up. Another future direction is global reconstruction from partial data. Combining SAL with image data also has potentially interesting applications. We think SAL has many exciting future work directions, progressing geometric deep learning to work with unorganized, raw data.

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