Radio Recombination Line Observations at 1.0 – 1.5 GHz with FAST

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Abstract H II regions made of gas ionized by radiations from young massive stars, are widely distributed in the Milky Way. They are tracers for star formation, and their distributions are correlated with the Galactic spiral structure. Radio recombination lines (RRLs) of hydrogen and other atoms allows for the precisest determination of physical parameters such as temperature and density. However, RRLs at around 1.4 GHz from H II regions are weak and their detections are difficult. As a result, only a limited number of detections have been obtained yet. The 19-beam receiver on board of the Five-hundred-meter Aperture Spherical radio Telescope (FAST) can simultaneously cover 23 RRLs for H\textsubscript{n}α, He\textsubscript{n}α, and C\textsubscript{n}α (n = 164 – 186), respectively. This, combined with its unparalleled collecting area, makes FAST the most powerful telescope to detect weak RRLs. In this pilot survey, we use FAST to observe nine H II regions at L band. We allocate 20 minutes pointing time for each source to achieve a sensitivity of around 9 mK in a velocity resolution of 2.0 km s\(^{-1}\). In total, 21 RRLs for H\textsubscript{n}α and C\textsubscript{n}α at 1.0 – 1.5 GHz have been simultaneously detected with strong emission signals. Overall, the detection rates for the H167α and C167α RRLs are 100%, while that for the He167α RRL is 33.3%. Using hydrogen and helium RRLs, we measure the electron density, electron temperature, and pressure for three H II regions. This pilot survey demonstrates the capability of FAST in RRL measurements, and a statistically meaningful sample with RRL detection, through which knowledge about Galactic spiral structure and evolution can be obtained, is expected in the future.

Key words: radio telescope: FAST — H II regions — RRLs — star formation

1 INTRODUCTION

Galactic H II regions are made of gas ionized young massive stars. They are tracers for star formation, their evolutions are interesting from an astrophysical point of view, and their distributions are correlated with the Galactic spiral structure (e.g., Churchwell et al., 2006, 2007; Beaumont & Williams, 2010; Hou & Han, 2014; Zhang et al., 2014, 2017). H II regions are ubiquitously distributed in the Milky Way. The Wide-Field Infrared Survey Explorer (WISE) catalog of H II regions (Anderson et al., 2014) is the largest sample of Galactic H II region candidates to date. The sample are distributed throughout the Milky Way disk, making them idea tracers for the Galactic spiral structure. Determining their distances and physical parameters is thus crucial.
Table 1 Sources and observational results.

| Source     | R.A.(J2000) | Dec.(J2000) | Velocity | $T_A$ (H167α) | FWHM | $T_A$ (C167α) | FWHM | $T_A$ (He167α) | FWHM |
|------------|-------------|-------------|----------|---------------|------|---------------|------|---------------|------|
|            | hh:mm:ss    | dd:mm:ss    | km s$^{-1}$ | K             | km s$^{-1}$ | K           | km s$^{-1}$ | K           | km s$^{-1}$ |
| G43.148+0.013 | 19:10:10.98 | +09:05:18.2 | 10.47    | 0.244         | 28.26 | 0.074         | 18.07 |
| G43.177−0.008 | 19:10:18.73 | +09:06:13.4 | 15.07    | 0.242         | 29.04 | 0.066         | 16.64 |
| G48.905−0.261 | 19:22:07.85 | +14:03:12.6 | 60.78    | 0.203         | 27.71 | 0.028         | 34.13 |
| G48.946−0.331 | 19:22:27.89 | +14:03:24.9 | 65.85    | 0.251         | 26.53 | 0.045         | 14.18 |
| G48.991−0.299 | 19:22:26.22 | +14:06:42.2 | 66.61    | 0.229         | 28.80 | 0.038         | 13.07 |
| G49.028−0.217 | 19:22:12.74 | +14:10:58.4 | 61.91    | 0.295         | 21.26 | 0.047         | 11.93 |
| G49.224−0.334 | 19:23:01.08 | +14:18:00.6 | 63.43    | 0.154         | 30.58 | 0.037         | 31.37 |
| G49.368−0.303 | 19:23:11.17 | +14:26:32.6 | 49.47    | 0.226         | 29.71 | 0.049         | 29.15 |
| G49.466−0.408 | 19:23:45.74 | +14:28:45.2 | 56.66    | 0.169         | 25.84 | 0.053         | 23.23 |

Notes. Only the $n=167$ data for H$\alpha$, He$\alpha$, and C$\alpha$ RRLs are listed above, because other transitions have a very close spectral information to the $n=167$.

Radio recombination lines (RRLs) of hydrogen provide the simplest and precisest method of determining the electron temperature and density of H II regions. Unlike observations of optical emission lines, RRLs are unaffected by reddening from interstellar dust. Further, they can be accurately measured even in weak astronomical sources (Gordon & Sorochenko, 2002), allowing for accurate determination of the physical parameters. RRLs are distributed in a wide range of frequencies. Recent RRL surveys at different wavelengths were performed with highly sensitive facilities to study H II regions (e.g., Anderson et al., 2011, 2014; Liu et al., 2013; Alves et al., 2015; Chen et al., 2020). However, the RRLs at around 1.4 GHz from H II regions are relatively weak (Anderson et al., 2011), thus either large telescopes or long integration are needed to detect them. Before FAST, these observations are difficult, and only a small sample of H II regions were detected at $\sim$1.4 GHz.

FAST is located at geographic latitude of 25°39′10.6′′ and its observable maximum zenith angle is 40° (Nan et al., 2011; Jiang et al., 2019, 2020), thus FAST observation can cover all the H II regions distributed in the Galactic longitude range of around 21° to 223°. The 19-beam receiver of the FAST has a band width of 500 MHz with a frequency range of 1.0−1.5 GHz (Jiang et al., 2019, 2020), which can simultaneously cover 23 RRLs for H$\alpha$, C$\alpha$, and H$\alpha$ (principal quantum number $n = 164−186$), respectively. This makes FAST the most powerful telescope to detect weak RRLs at L band. Therefore, a larger population of H II regions deserve to be systematically studied with FAST. Using the RRLs and continuum emission at around 1.4 GHz, we could measure the pressure, evolutionary ages, distances, and relative abundance of elements in H II regions. With a reasonably-sized sample, we could determine the distribution of them in the Milky Way disk and correlate it with the physical parameters of the H II regions. This will deepen our understanding of the co-evolution between H II regions and the Milky Way.

In this work, as a pilot study, nine H II region candidates are selected from a 4−6 GHz RRL survey with Shanghai Tianma 65 m telescope by Chen et al. (2020), where RRLs such as H$\alpha$, H$\alpha$, and C$\alpha$ ($n = 98−113$) have been detected (see Table 1). We observe 1.0−1.5 GHz (see Table 2) RRLs using FAST to determine the physical parameters and to provide a first constraint on the expected detection rate.

2 OBSERVATIONS AND DATA REDUCTION

2.1 Observations with FAST

The FAST observations were conducted between Aug.28 and Sep.19, 2020. We used tracking mode to point to each target using the central beam (Beam-M01) of the 19-beam receiver on FAST. Other beams were used as off-source observations to calibrate the data in Beam-M01. This setup could save lots of observation time. The half-power beamwidth (HPBW) is $\sim$2.9′ at 1.4 GHz , and the pointing error
Fig. 1 Hα (n = 164 – 186) RRLs in a FAST spectrum for G43.148+0.013. The blue spectrum shows original and uncalibrated data with 500 MHz bandwidth and two minutes integration from FAST observations.

is ∼0.15′ (Jiang et al., 2019, 2020). For the backend, a high spectral resolution (1048576 channels), full bandwidth (500 MHz), and dual polarization mode were used to collect the observational signal, resulting in a frequency resolution of 476 Hz or a velocity resolution of ∼0.1 km s⁻¹ at 1.4 GHz. Each source was integrated for 20 minutes with a sampling rate of one second. For intensity calibration, noise signal with amplitude of 1 K was injected under a period of two seconds in only first two minutes at the beginning of each source observation. The relevant degrees per flux unit factor (DPFU) for Beam-M01 is DPFU ∼ 16.02 ± 0.26 Kelvin per Jy beam⁻¹ at 1400 MHz (Jiang et al., 2020).

2.2 Data Reduction

Our selected sources have extremely strong continuum emission (≥10 Jy), this leads to that the total fluxes with noise diode at switch-on and switch-off states have no obvious discrepancy. Thus, our observational data could not be calibrated directly by noise diode. This issue could be solved by using the simultaneously observed data in other beams to calibrate our target data from the central beam, assuming that all data from each beam have the same rms. We could firstly calibrate data from the FAST Beam-M16 receiver (Jiang et al., 2020) to get the antenna temperature (T_A) using:

\[ T_A = T_{\text{noise}} \times \frac{\text{Power}_{\text{caloff}}}{\text{Power}_{\text{calon}} - \text{Power}_{\text{caloff}}}, \]

where T_{\text{noise}} is the injected noise temperature of known, Power_{\text{calon}} and Power_{\text{caloff}} are, respectively, the observed total power for noise diode with switch-on and switch-off. Assuming that the FAST Beam-M01 data have the same rms as the Beam-M16, we then could calibrate the observed data in the Beam-M01 using the Beam-M16¹. Such calibration method may introduce an uncertainty of 30% into the derived antenna temperature. Finally, we smoothed the spectral data into a resolution (channel width) of 10 KHz, corresponding to a spectral resolution of around 2.0 km s⁻¹ at 1.4 GHz. The sensitivity achieves to around 9 mK at such conditions.

3 ANALYSIS AND DISCUSSION

3.1 RRLs in FAST spectral observations

Figure 1 presents one FAST spectrum including the whole 500 MHz bandwidth and using two minutes integration toward H II region G43.148+0.013. Hα (n = 164 – 186) RRLs are indicated in the spectrum. Additional bonus are the carbon and helium RRLs, which could be simultaneously covered together with the hydrogen RRLs. This means that the FAST observation could simultaneously cover 23 hydrogen,
Fig. 2 Detected RRLs toward G43.148+0.013. The positions of Hα, Hβ, and Cα RRLs with n = 164 – 186 (except n = 177, 180, which are polluted by RFIs.) have been indicated in each panel.

carbon and helium RRLs, respectively. However, some frequencies are often polluted by RFI. For example at around 1175 MHz, H177α RRL is always seriously polluted by communication satellites. This will lead to that one often cannot see the seriously polluted emission lines, for example H177α RRL.
3.2 Hydrogen, Carbon and Helium RRLs

Figure 2 presents the detected RRLs toward the H II region G43.148+0.013. The positions of H\textalpha, H\textbeta, and C\textalpha RRLs with $n = 164 - 186$ (except $n = 177, 180$) have been indicated in each panel. For the RRLs with $n = 177$ and $n = 180$, they have been seriously polluted by RFL, so they are not given here. The rest frequencies of H\textalpha, H\textbeta, and C\textalpha ($n = 164 - 186$) lines are listed in Table 2. Figure 3 shows the detected H167\textalpha, He167\textalpha, and C167\textalpha RRLs in nine sources (see Table 1) and their Gaussian fitting results. We can see that the He167\textalpha RRL was detected in only three sources (G48.946–0.331, G48.991–0.299, and G49.028–0.217), while H167\textalpha and C167\textalpha RRLs were detected in all the nine sources. The detection rates are respectively 33.3\% for He167\textalpha RRL, and 100\% for H167\textalpha and C167\textalpha RRLs in our selected nine sample.

Information obtained from hydrogen RRLs enables us to determine the basic physical conditions of H II regions as well as distribution of ionized hydrogen in Galaxy (Brown et al., 1978; Zhang et al., 2014; Oonk et al., 2017; Xu et al., 2020). Helium, the second-most abundance element of the ISM, is also ionized in the majority of H II regions. The ratio of the integrated intensities of hydrogen and helium RRLs enables us to accurately determine the relative abundance of helium, which has great significance not only for understanding the physics of the ISM, but also for understanding how the Universe formed. In three sources, we simultaneously detected and then measured their line ratios (listed in Table 3), which are respectively around 0.0154, 0.0168, and 0.0137 in G48.946–0.331, G48.991–0.299, and G49.028–0.217. This means that in such H II regions there is $N(\text{He}^+)/N(\text{H}^+)$ ~ 1.5\%, which is consistent with the investigations for other giant H II regions in Galactic center (Churchwell et al., 1974).

Gordon & Sorochenko (2002) found that the centroids of the carbon line emission are offset from that of the hydrogen line emission, the radial velocities were often different from the hydrogen RRLs, and the line widths were always much narrower. Although the carbon lines were spatially associated, they probably did not come from the region of the H II gas itself. For these reasons, Zuckerman & Palmer (1968) suggested that the carbon lines originated from the outer parts of a dense HI region bounding the discrete H II regions. Comparing the centroids and line widths of the carbon and hydrogen 167\textalpha RRLs for all sample, we found that there exist velocity offsets within ±10 km s$^{-1}$ between them, and that the carbon line widths were indeed narrower than those for the hydrogen RRLs. This indicates that

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{fig3.png}
\caption{Detected H167\textalpha, He167\textalpha, and C167\textalpha RRLs in nine sources and their Gaussian fitting results. The velocity at 0 km s$^{-1}$ corresponds to 1399.368 MHz, which is the rest frequency of H167\textalpha.}
\end{figure}
Table 2: The rest frequencies for H$\alpha$, He$\alpha$, and C$\alpha$ RRLs.

| Transition $n$ | $\nu_{H\alpha}$ (MHz) | $\nu_{He\alpha}$ (MHz) | $\nu_{C\alpha}$ (MHz) |
|---------------|------------------------|------------------------|------------------------|
| 164           | 1477.335               | 1477.937               | 1478.072               |
| 165           | 1450.716               | 1451.307               | 1451.440               |
| 166           | 1424.734               | 1425.314               | 1425.444               |
| 167           | 1399.368               | 1399.938               | 1400.066               |
| 168           | 1374.600               | 1375.161               | 1375.286               |
| 169           | 1350.414               | 1350.964               | 1351.088               |
| 170           | 1326.792               | 1327.333               | 1327.454               |
| 171           | 1303.718               | 1304.249               | 1304.368               |
| 172           | 1281.175               | 1281.697               | 1281.815               |
| 173           | 1259.150               | 1259.663               | 1259.778               |
| 174           | 1237.626               | 1238.130               | 1238.243               |
| 175           | 1216.590               | 1217.086               | 1217.197               |
| 176           | 1196.028               | 1196.515               | 1196.625               |
| 177           | 1175.927               | 1176.406               | 1176.514               |
| 178           | 1156.274               | 1156.745               | 1156.851               |
| 179           | 1137.056               | 1137.520               | 1137.624               |
| 180           | 1118.262               | 1118.718               | 1118.820               |
| 181           | 1099.880               | 1100.328               | 1100.429               |
| 182           | 1081.898               | 1082.339               | 1082.438               |
| 183           | 1064.307               | 1064.740               | 1064.838               |
| 184           | 1047.094               | 1047.521               | 1047.617               |
| 185           | 1030.251               | 1030.671               | 1030.765               |
| 186           | 1013.767               | 1014.180               | 1014.273               |

References: Müller et al. (2005)

the C II and H II regions are formed in different layers of molecular clouds. For example, (Alves et al., 2015) suggested the C II regions may be formed in the outer and cooler layers of molecular clouds at the boundaries with H II regions. The helium and hydrogen 167$\alpha$ RRLs have a close line-center velocity, indicating that they may be originated from the same region.

3.3 Electron density, electron temperature, and pressure

Interstellar bubbles (H II regions in nature) surrounding OB stars are the result of the combined effects of radiation pressure and stellar winds (Zhang et al., 2013, 2016, 2019). The expansion of bubbles will lead to changes in the dust-to-gas ratio, due to movement of the grains from one zone to another, as well as because of grain destruction (Draine, 2011). In the outer part of bubbles, Draine (2011) and Zhang & Wang (2013) detected the drift speeds become small as being away from the bubble. Radiation pressure acting on gas and dust causes H II regions to have central densities that are lower than the density near the ionized boundary (Draine, 2011; Dutta et al., 2018). Since the effects of radiation pressure are not negligible, the observed cavity must be the result of the combined effects of radiation pressure and a stellar wind.

For optically thin ionized gas and local thermodynamic equilibrium (LTE) condition, one could derive the electron temperature $T_e$ based on the ratio between 1.4 GHz continuum flux density and H167$\alpha$ line intensity (Gordon & Sorochenko, 2002; Zhang et al., 2014) with

$$T_e = \left[ \frac{6985}{\alpha(\nu, T_e)} \left( \frac{\Delta V_{H167\alpha}}{\text{km s}^{-1}} \right)^{-1} \left( \frac{T_{1.4\text{GHz}}}{T_{H167\alpha}} \right)^{0.11} \left( \frac{\nu}{\text{GHz}} \right)^{1.1} \left( \frac{N(\text{He}^+)}{N(H^+)} \right)^{-1} \right]^{0.87}$$

(2)

where $\alpha(\nu, T_e) \sim 1$ is a slowly varying function tabulated by Mezger & Henderson (1967), $\frac{N(\text{He}^+)}{N(H^+)} \sim 0.015$ (see Section 3.2), $\Delta V_{H167\alpha}$ is the FWHM of H167$\alpha$ RRL, and the ratio $\frac{T_{1.4\text{GHz}}}{T_{H167\alpha}}$ could be directly measured.
continuum. Finally we get the electron temperature from the observations, where we ignore the relatively weak background contribution into the 1.4 GHz telescope beam. For the H167\textalpha line, the peak line intensity is $S_{\lambda}$, thus we could assume $\theta_e = 1.5^{\circ}$ for estimation. The corresponding volume electron density is estimated by $n_e$ from

$$EM = 7.1 \text{pc cm}^{-6} \left( \frac{S_{\lambda}}{\text{Jy}} \right) \left( \frac{\lambda}{\text{mm}} \right) \left( \frac{T_e}{\text{K}} \right)^{1.5} \left( \frac{\Delta V}{\text{km s}^{-1}} \right) \left( \frac{\theta_e}{\text{arcsec}} \right)^{-2}.$$  

For the H167\textalpha line, the peak line intensity is $S_{\lambda}$ and the line width $\Delta V$ are listed in Table 1. The observing wavelength is $\lambda = 21$ cm. Based on the parameters above, we could obtain an EM. The intrinsic size $\theta_e$ could be derived from the radius of an H II region. Our selected H II regions have larger size than the telescope beam (3'), thus we could assume $\theta_e = 1.5^{\circ}$ for estimation. The corresponding volume electron density is estimated by $n_e$ from

$$EM = n_e^2 L f_v,$$

where we could assume the path length as $L = D \times \tan(\theta_e)$ ($D$ is the source distance listed in Table 3) and volume filling factor as $f_v = 1$.

The pressure $P_e$ from the ionized gas can be estimated following:

$$P_e = 2n_e k_b T_e,$$

where electron density $n_e$ and electron temperature $T_e$ have been derived and listed in Table 3. If not measured, $T_e$ can be inferred from the Galactocentric distance of a source using $R_{\text{gal}}$: $T_e = 278 \text{K} \times (R_{\text{gal}}/\text{kpc}) + 6080 \text{K}$ (Tremblin et al., 2014). Comparing the two methods, the derived electron temperatures in our work are consistent with that. Given a larger sample, we could estimate the mid-plane pressure as a function of Galactocentric distance (Wolfire et al., 2003) and test the fitting formula in Tremblin et al. (2014). This will also help us to further understand the distribution of $n_e$ and $T_e$ in the Milky Way.

### 4 SUMMARY

The FAST telescope has a large collecting area and enables high-sensitivity observations for extended sources. The 19-beam receiver has a wide bandwidth (500 MHz) and it can simultaneously cover 23 H\textalpha, H\textbeta, and C\textalpha (n = 164 – 186) RRLs, respectively. This combination is idea for the systematic study of RRLs from Galactic H II regions. In this pilot study, we observe nine H II regions using hydrogen, carbon and helium RRLs. Using 20 minutes pointing time for each source, a sensitivity of around 9 mK with a spectral resolution of around 2.0 km s$^{-1}$ can be achieved. In total, 21 RRLs for H\textalpha and C\textalpha at 1.0 – 1.5 GHz have been simultaneously detected in strong emission except two lines ($n = 177$ and $n = 180$), which are seriously polluted by RFI. Overall, the detection rates for the He167\alpha and C167\alpha RRLs are 100%, while that for the He167\alpha RRL is 33.3% in our selected sample.

Comparing the centroids and line widths of the carbon and hydrogen 167\alpha RRLs for all sample, we found that there exist velocity offsets between −10 and +10 km s$^{-1}$. This indicates that the C II and H II regions are formed in different layers of molecular clouds. Using the hydrogen and helium RRLs,
we have measured electron density, electron temperature, and pressure (listed in Table 3) in three H II regions. This pilot study proves that the survey for a large sample of statistical measurement is feasible in the future.

In a future FAST work, we plan to observe a statistically significant sample of H II regions to measure electron density, electron temperature, pressure, evolutionary stages, and the relative abundance of elements. The sample would allow us to study the distribution of these physical parameters (including line widths, line ratios, electron temperatures and densities) in various parameter spaces, as well as the relation between the physical properties of H II and their locations measured in terms of, for example, the Galactocentric distance, to understand the co-evolution between the H II regions and the Galactic disk.

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