High energy spin excitations in YBa$_2$Cu$_3$O$_{6.5}$

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Abstract

Inelastic neutron scattering has been used to obtain a comprehensive description of the absolute dynamical spin susceptibility $\chi''(\mathbf{q}, \omega)$ of the underdoped superconducting cuprate YBa$_2$Cu$_3$O$_{6.5}$ ($T_c = 52$K) over a wide range of energies and temperatures ($2$ meV $\leq \hbar \omega \leq 120$ meV and $5$K $\leq T \leq 200$K). Spin excitations of two distinct symmetries (even and odd under exchange of two adjacent CuO$_2$ layers) are observed which exhibit two different gap-like features (rather than a single “spin pseudogap”). The excitations show dispersive behavior at high energies.

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The magnetic excitation spectra of doped cuprates contain incisive and highly specific information about theories for high temperature superconductivity. Many models based on strong Coulomb correlations between charge carriers, for instance, predict that at high energies the spin dynamics should resemble those of the parent antiferromagnetic insulator. Until recently, neutron experiments on metallic and superconducting cuprates were confined to excitation energies below $\sim 50$ meV, larger than the superconducting energy gap but smaller than the intralayer nearest-neighbor superexchange $J_{||} \sim 100$ meV which sets the energy scale for spin excitations in the undoped antiferromagnetic precursor compounds. Recent pioneering studies of the single-layer superconductor La$_{1.85}$Sr$_{0.15}$CuO$_4$ extended these measurements to higher energies and established the presence of significant spectral weight at energies comparable to $J_{||}$ [1,2]. Analogous data for metallic and superconducting YBa$_2$Cu$_3$O$_{6+x}$ (YBCO) have thus far not been reported.

As YBCO is a bilayer system, such experiments can also answer questions about the nature and strength of the coupling between two directly adjacent CuO$_2$ layers, a problem of intense current research. As there are two Cu atoms per unit cell of YBCO, one generally expects the formation of bonding and antibonding electronic states. Conventional band theory predicts the formation of two Fermi surfaces in bands composed of bonding and antibonding states. However, theoretical [3] as well as experimental [4] evidence indicates that these predictions do not generally hold for low-dimensional systems in the presence of strong correlations. Here we report neutron scattering measurements that evidence a new magnon dispersion-like behavior at energies of the order of $J_{||}$. Moreover, the spin excitation spectrum is characterized by two different gap-like features. These features provide fundamental insights into the “spin pseudo-gap” phenomenon in metallic underdoped cuprates as well as essential new information about the interlayer interactions.

Transitions between states of the same type (bonding-to-bonding or antibonding-to-antibonding) and those of opposite types are characterized by even or odd symmetry, respectively, under exchange of two adjacent CuO$_2$ layers. In the cross section for inelastic magnetic neutron scattering, these transitions can be distinguished according to their distinct depen-
dences on the wavevector component $L$ perpendicular to the CuO$_2$ sheets: The odd component of the spin susceptibility displays a $\sin^2(\pi z_{Cu} L)$ dependence whereas the even component has the complementary $L$ dependence, $\cos^2(\pi z_{Cu} L)$. (Here, $z_{Cu} = 0.285$ is the reduced distance between nearest-neighbor Cu spins within one bilayer, and the wavevector $Q = (H, K, L)$ is measured in units of the reciprocal lattice vectors $2\pi/a \sim 2\pi/b \sim 1.63\text{Å}^{-1}$ and $2\pi/c \sim 0.53\text{Å}^{-1}$). In previous low energy neutron experiments in the metallic regime, only spin excitations of odd symmetry were found over the entire doping range. Does this reflect a fundamental selection rule, or is there a different (higher) energy scale associated with the first type of transition? In the latter case, a comparison between the energies and susceptibilities associated with the two excitation modes would yield quantitative information on the strength of the bilayer coupling, obviously an important parameter in models of high temperature superconductivity. This issue also bears directly on the interpretation of other experiments that are sensitive to this coupling. Our new measurements of high energy spin excitations in underdoped metallic YBa$_2$Cu$_3$O$_{6.5}$ have much better resolution and counting statistics than the initial studies on La$_{1.85}$Sr$_{0.15}$CuO$_4$. Excitations of both odd and even symmetries are observed; the even excitations are characterized by a $\sim 53$ meV energy gap, the odd excitations show a gap-like feature at $\sim 23$ meV. Both excitations exhibit large temperature dependences, and a dispersion-like behavior at high energies.

Our sample was a high quality YBa$_2$Cu$_3$O$_{6.5}$ single crystal of volume $\sim 2.5$ cm$^3$ and superconducting transition temperature (midpoint) $T_c = 52$K. Its preparation and characterization have been described elsewhere; in particular, susceptibility measurements shown in Fig. 2 of Ref. indicate a sharp superconducting transition (full width 5K) which rules out significant inhomogeneities in oxygen content. The neutron experiments were performed on the triple axis spectrometers IN8 (installed on a thermal beam) and IN1 (installed on the hot neutron source) at the Institut Laue-Langevin (ILL). The incident beam was monochromated by the (111) reflection of a flat copper crystal on IN8, and by the (200) or (220) reflections of a vertically curved copper crystal on IN1. On both spectrometers, we used a graphite (002) analyzer with fixed vertical and adjustable horizontal
curvatures. On IN8, higher-order contamination was eliminated using a pyrolytic graphite (PG) filter on the scattered beam for different fixed final energies, $E_f = 14.7, 30.5$ and $35$ meV. On IN1, we worked with a fixed final energy of $E_f = 62.6$ meV, and a nuclear resonance Er filter was placed on the scattered beam to suppress contaminations from higher energy neutrons. In all the measurements we scanned the wavevector $Q$ while keeping the energy transfer constant. Two different scattering geometries were chosen in which wavevectors of the forms $Q = (H, H, L)$ or $Q = (3H, H, L)$, respectively, were accessible [12]. The results obtained on both instruments and in both geometries are in good agreement.

Previous experiments [5–15] have established that the low energy magnetic cross section is peaked around the in-plane wavevector $q_{2D} = (\pi/a, \pi/b)$, or $H = K = 1/2$ in reciprocal lattice units (r.l.u.). The cross section for odd spin excitations exhibits maxima at $L_{odd} \approx 1.7 + 3.5n$ ($n = \text{integer}$), and that for even excitations is maximum for $L_{even} \approx 3.5n$. We therefore performed constant-energy scans along $Q = (H, H, L_{odd})$ and $(H, H, L_{even})$, shown in Fig. 1. There are numerous optical phonon modes in the energy range covered by these data. However, scans in different diffraction zones as well as checks against phonon structure factor calculations [12] established the magnetic origin of the peaks. The strong temperature dependence of the peak intensities (see below) is also inconsistent with phonon scattering. This methodology has previously been applied to neutron data at lower energies [5–7, 9–12, 14], and the results were found to be consistent with polarized beam experiments wherever such checks proved feasible [8,12]. The temperature dependence of the uniform background presumably arises from multiphonon scattering.

The scans were fitted to Gaussian profiles convoluted with the instrumental resolution function, corrected for the Cu magnetic form factor [17], and converted to the dynamical spin susceptibility $\chi''$ [18] by adjusting for the thermal population factor. Fig. 2 shows $\chi''_{odd/even}(\omega) = \int dq_{2D} \chi''(q_{2D}, L_{odd/even}, \omega) / \int dq_{2D}$, the susceptibility averaged over the two-dimensional Brillouin zone in both odd and even channels. [We assume an isotropic $q$-dependence of the spin susceptibility around $(\pi, \pi)$. This assumption is consistent with the data along $(H,H)$ and a more limited data set along $(3H,H)$.] While odd excitations
are observed over the entire energy range probed by our experiments, an energy gap of \( \Delta_{\text{even}} \sim 53 \text{ meV} \) exists for even excitations. Both \( \chi''_{\text{odd}}(\omega) \) at low energies and the gap for \( \chi''_{\text{even}}(\omega) \) are consistent with previous measurements in this doping regime \([5,6,9]\) which established a lower bound on the gap. Further, previous studies had given the neutron cross section in arbitrary units, but many quantitative models now require an absolute unit scale for \( \chi'' \). We have therefore calibrated the magnetic intensity against the phonon spectrum, both against acoustic phonons at low energies and against an optical phonon at \( \hbar \omega = 42.5 \text{ meV} \) according to a procedure discussed elsewhere \([12]\). Both normalization procedures are in good agreement.

The temperature dependences of both \( \chi''_{\text{odd}} \) and \( \chi''_{\text{even}} \) are striking. At 200K, \( \chi''_{\text{odd}}(\omega) \) shows a broad peak around 30 meV which sharpens and shifts to lower energy with decreasing temperature. The \( \sim 50 \) meV dip in \( \chi''_{\text{odd}}(\omega) \) at low temperatures had not been observed before and may be related to the gap in \( \chi''_{\text{even}}(\omega) \). Much of the temperature evolution of \( \chi''_{\text{odd}}(\omega) \) takes place in the normal state; however, there is also an additional enhancement of the peak intensity at \( T_c \) \([13]\) which is presumably related to the magnetic resonance peak in the superconducting state dominating the magnetic spectra of more heavily doped samples \( (x > 0.9) \) \([3,13]\). While \( \chi''_{\text{odd}}(\omega) \) is little affected by temperature above \( \hbar \omega \sim 60 \) meV, at these energies \( \chi''_{\text{even}}(\omega) \) increases by almost a factor of two between 200K and 5K. In the same temperature interval \( \Delta_{\text{even}} \) softens from \( \sim 59 \) meV to \( \sim 53 \) meV. This parallels the enhancement and softening of the peak in \( \chi''_{\text{odd}}(\omega) \) at lower energies.

We now turn to the wavevector dependence of the spin susceptibility. At low energies (below \( \sim 30 \) meV), the scans are peaked around \( \mathbf{q}_{2D} \) with an intrinsic width of \( \Delta \mathbf{q}_{2D} \sim 0.2 \text{ Å}^{-1} \) (FWHM). (Previous measurements with better \( \mathbf{q} \)-resolution had indicated a flat-topped shape of these profiles \([19]\)). Fig. 1 shows that at high energies the peak broadens to \( \Delta \mathbf{q}_{2D} \sim 0.3 \text{ Å}^{-1} \) and disperses away from \( \mathbf{q}_{2D} = (\frac{1}{2}, \frac{1}{2}) \), so that a double peak structure emerges. For the sake of simplicity, we have fitted the \( \mathbf{q} \)-scans to the sum of two displaced peaks only when a single peak did not give a satisfactory fit. The positions and intrinsic widths of the peaks in \( \chi''_{\text{odd}}(\mathbf{q}_{2D}, \omega) \) and \( \chi''_{\text{even}}(\mathbf{q}_{2D}, \omega) \) resulting from this procedure are shown
It is instructive to compare these data to previous high energy measurements on the bilayer antiferromagnetic parent compound YBa$_2$Cu$_3$O$_{6.2}$ and on the single-layer, optimally doped compound La$_{1.86}$Sr$_{0.14}$CuO$_4$. Clearly, the basic structure of the spin excitation spectrum of YBa$_2$Cu$_3$O$_{6.5}$ bears some resemblance to the spin wave spectrum of the YBa$_2$Cu$_3$O$_{6.2}$ \cite{17,20,22}, with the ungapped odd (gapped even) excitations corresponding to acoustic (optical) spin waves, that is, in-phase (antiphase) precessions of localized spins in adjacent layers. The dynamical susceptibility of the acoustic spin wave mode is

$$
\chi''(Q,\omega) = 4S\pi Z_{\chi} Z_{c} \mu_B^2 \frac{1 + \gamma(q_{2D})}{\sqrt{1 - \gamma^2(q_{2D})}} \sin^2(\pi z_{Cu} L) \delta[h\omega - 4SZ_{c}J||\sqrt{1 - \gamma^2(q_{2D})}] \quad (1)
$$

where $\gamma(q_{2D}) = \frac{1}{2} [\cos(q_x a) + \cos(q_y b)]$, and the quantum corrections for the spin wave velocity and the spin susceptibility are taken into account respectively as $Z_{c} = 1.18$ and $Z_{\chi} = 0.51$ following theoretical predictions \cite{23} in agreement with experiment \cite{12}. An analogous equation holds for even excitations, with $\cos^2(\pi z_{Cu} L)$ instead of the $\sin^2$ factor and a dispersion with a gap of 67 meV \cite{21}. The average of (1) over the 2D Brillouin zone is finite, $4SZ_{\chi}/J||\mu_B^2$, and approximately independent of energy in the energy range probed by our experiment. For comparison this quantity is shown as the dashed line in Fig. 2 (as 10 $\mu_B^2/eV$ with $J|| = 102$ meV after quantum corrections \cite{17}). Clearly, the spectral weights of spin excitations in antiferromagnetic YBa$_2$Cu$_3$O$_{6.2}$ and superconducting YBa$_2$Cu$_3$O$_{6.5}$ are comparable. Finally, the spin wave dispersions of YBa$_2$Cu$_3$O$_{6.2}$ are superimposed on the data of Fig. 3. Heuristically, the odd excitation spectrum of YBa$_2$Cu$_3$O$_{6.5}$ can be fitted to a dispersive mode with a pseudo-gap of 23 meV \cite{16} and a dispersion of $\sim 420$ meVÅ, smaller than the antiferromagnetic spin wave velocity of 650 meVÅ \cite{17,22}. However, this analysis requires a very large damping parameter comparable to the gap. This pseudo-gap is characteristic of the normal state; at this doping level, the dynamical susceptibility is only weakly modified by superconductivity. Other features of the spin excitations of YBa$_2$Cu$_3$O$_{6.5}$ such as the strong temperature dependence, the pronounced peak-dip structure at low temperatures and the energy-dependent broadening of the $q$-width are also very
different from spin waves in YBa$_2$Cu$_3$O$_{6.2}$. An explanation of these features presents a challenge to theories of the spin dynamics in the cuprates [24].

The reports on La$_{1.85}$Sr$_{0.15}$CuO$_4$ [1,2] did not contain information about the temperature evolution of $\chi''(\omega)$, and the measurements did not have sufficient resolution to establish the presence or absence of a dip feature in the spectrum. However, the general shape of 2D $\mathbf{q}$-integrated $\chi''(\omega)$ in deeply underdoped YBa$_2$Cu$_3$O$_{6+x}$ and optimally doped La$_{2-x}$Sr$_x$CuO$_4$ are substantially similar. Despite the different $\mathbf{q}$-dependences of $\chi''(\mathbf{q}, \omega)$ at low energies (four sharp incommensurate peaks in La$_{1.85}$Sr$_{0.15}$CuO$_4$, one broad commensurate peak in YBa$_2$Cu$_3$O$_{6.5}$), both spectra are peaked near 25 meV. However, the maximum of $\chi''$ per CuO$_2$ layer is almost twice as large in absolute units in YBa$_2$Cu$_3$O$_{6.5}$ (If given per formula unit, as in Fig. 2, the susceptibility of the bilayer compound exceeds the one of the single-layer compound by about a factor of 4). By contrast, fully oxygenated YBa$_2$Cu$_3$O$_7$ has a much smaller normal state susceptibility and a sharp resonance peak in the superconducting state [8,12].

In summary, we have reported the first observation of the even part of the dynamical spin susceptibility of the bilayer superconductor YBa$_2$Cu$_3$O$_{6.5}$, an important part of the experimental description of spin fluctuations in the cuprates. Both the odd and the even components are characterized by strong and unusual temperature dependences and by a dispersive behavior at high energies. Our observation of two different gap-like features in the dynamical spin susceptibility demonstrates that the spin-gap phenomenon, a hallmark of the underdoped cuprates, is more complex than previously thought. Our measurements of the spin correlations in absolute units over a wide range of energies, wavevectors and temperatures provide an excellent basis for theories of this phenomenon.

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Figure Captions

1. Constant energy scans of (a) $\chi''_{\text{odd}}(Q, \omega)$ through $Q = (\frac{1}{2}, \frac{1}{2}, L_{\text{odd}})$ and (b) $\chi''_{\text{even}}(Q, \omega)$ through $Q = (\frac{1}{2}, \frac{1}{2}, L_{\text{even}})$, measured at 5 K (closed circles) and 200 K (open squares). Data have been obtained mostly on IN8 with a final energy of $E_f=35$ meV except at the energy transfer of $\hbar\omega =15$ meV where $E_f=14.7$ meV. The scan for $\hbar\omega = 80$ meV has been obtained on IN1 by rocking the sample around $Q=(0.5,0.5,5.4)$ with $E_f=62.6$ meV. Data obtained on IN8 in different counting times have been rescaled to the the same monitor (monitor=2000, $\approx 6$ mn/point). Lines are the results of fits to a single Gaussian on top of a linear background, except at 80 meV where the line corresponds to two identical Gaussian lines displaced symmetrically on each side of $H = 0.5$.

2. Odd (a) and even (b) spin susceptibilities at $T=5$ K, $T=60$ K (just above $T_C$) and $T=200$ K in absolute units (see text). Measurements using different final neutron energies $E_f$ obtained on the two different spectrometers have been rescaled to the same units. The error bars do not include a $\sim 30\%$ normalization error.

3. Spin excitation spectrum for odd (open symbols) and even (closed circles) excitations at 5 K. The open square indicates the energy of the maximum of the odd susceptibility. The horizontal bars represent the full width at half maximum after a Gaussian deconvolution from the spectrometer resolution. The dotted lines correspond to the spin-wave dispersion relation in the insulating antiferromagnetic state with $J_{||} = 120$ meV and $J_{\perp}/J_{||} = 0.08$ (without quantum corrections) \[21\,22\].
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with the antiferromagnetic undoped compound are *not* due to inhomogeneities in oxygen content. Apart from the sharp superconducting transition, The spectra of Fig. 2 themselves are inconsistent with an energy independent admixture due to spin waves in undoped regions of the sample. Further, the low energy excitations, $\sim 2$ meV, are sharply suppressed below the superconducting $T_C$. (H.F. Fong *et al*, to be published).
FIGURES

![Graph showing intensity vs. field for different temperatures and energies](Image)

- **Odd**
  - 80meV IN1
  - 65meV
  - 15meV

Intensity (Counts/2000 monitor)

H (r.l.u.)
\[ \chi''_{\text{odd}}(\omega) \left( \mu_B^2 / eV \right) \]

\[ \chi''_{\text{even}}(\omega) \left( \mu_B^2 / eV \right) \]

Energy (meV)

YBa$_2$Cu$_3$O$_6.5$  \( T_c = 52 \text{ K} \)

\( T = 5 \text{ K} \)

\( T = 60 \text{ K} \)

\( T = 200 \text{ K} \)
