The power spectrum and bispectrum of SDSS DR11 BOSS galaxies – II. Cosmological interpretation

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ABSTRACT

We examine the cosmological implications of the measurements of the linear growth rate of cosmological structure obtained in a companion paper from the power spectrum and bispectrum monopoles of the Sloan Digital Sky Survey III Baryon Oscillation Spectroscopic Survey Data Release 11, CMASS galaxies. This measurement was of \( f^{0.43} \sigma_8 \), where \( \sigma_8 \) is the amplitude of dark matter density fluctuations, and \( f \) is the linear growth rate, at the effective redshift of the survey, \( z_{\text{eff}} = 0.57 \). In conjunction with cosmic microwave background (CMB) data, interesting constraints can be placed on models with non-standard neutrino properties and models where gravity deviates from General Relativity on cosmological scales. In particular, the sum of the masses of the three species of the neutrinos is constrained to \( m_\nu < 0.49 \text{ eV} \) (at 95 per cent confidence level) when the \( f^{0.43} \sigma_8 \) measurement is combined with state-of-the-art CMB measurements. Allowing the effective number of neutrinos to vary as a free parameter does not significantly change these results. When we combine the measurement of \( f^{0.43} \sigma_8 \) with the complementary measurement of \( f \sigma_8 \) from the monopole and quadrupole of the two-point correlation function, we are able to obtain an independent measurements of \( f \) and \( \sigma_8 \). We obtain \( f = 0.63 \pm 0.16 \) and \( \sigma_8 = 0.710 \pm 0.086 \) (68 per cent confidence level). This is the first time when these parameters have been able to be measured independently using the redshift-space power spectrum and bispectrum measurements from galaxy clustering data only.

Key words: galaxies: haloes – cosmological parameters – cosmology: theory – large-scale structure of Universe.

1 INTRODUCTION

Direct and model-independent constraints on the growth of cosmological structure are particularly important in cosmology. Measurements of the expansion history of the Universe (via standard candles or standard rulers) have clearly indicated an accelerated expansion since redshift \( z \sim 0.3 \), but are insufficient to identify the physics causing it; information on the growth of structure is key (for a review of the state of the field and general introduction to it, see e.g. Albrecht et al. 2006, Amendola et al. 2013, Feng et al. 2014 and references therein). In particular, while the cosmological constant remains at the core of the standard cosmological model, and is the most popular explanation for the accelerated expansion, it raises several problems from its smallness (the cosmological constant problem) to its fine-tuning (the coincidence problem). This situation has led many scientists to investigate alternatives to vacuum energy (dark energy) or to challenge one of the basic tenets of cosmology, namely General Relativity (GR). After all, precision tests of GR have been performed on Solar system scales, but more

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than 10 orders of magnitude extrapolation is required to apply it on cosmological scales. Should GR be modified on cosmological scales, it could still mimic the ΛCDM expansion history but the growth of structure would be affected.

Most of the information we can gather about clustering and large-scale structure, which on large scales would trace the linear growth of perturbations, come from galaxies. It is well known that different kinds of galaxies show different clustering properties, and thus not all objects can be faithful tracers of the underlying mass distribution; this feature is called galaxy bias. There are two notable observational techniques that avoid this limitation: gravitational lensing and redshift-space distortions. Gravitational lensing is an extremely promising approach which, however, at present reaches limited signal-to-noise ratio in the linear or mildly non-linear regime. The study of redshift-space distortions observed in galaxy redshift surveys uses galaxies as test particles in the velocity field, and thus this technique is relatively insensitive to galaxy bias.¹

A third approach is to use higher order correlations to disentangle the effects of gravity from those of galaxy bias (e.g. Fry 1994). This is the approach recently pursued in Gil-Marín et al. (2015) where, by performing a joint analysis of the monopole power spectrum and bispectrum of the CMASS sample of the Sloan Digital Sky Survey III Baryon Oscillation Spectroscopic Survey Data Release 11 (SDSSIII BOSS DR11) survey (Gunn et al. 1998, 2006; Eisenstein et al. 2011; Bolton et al. 2012; Dawson et al. 2013; Smee et al. 2013), constraints on both galaxy bias and growth of structures at the effective redshift of the survey \( z = 0.57 \) were obtained.

Here we investigate the cosmological implications of the measurement of the quantity \( f^{1.43} \sigma_8 \) at \( z = 0.57 \) (hereafter \( f^{1.43} \sigma_8 |_{=0.57} \)) obtained in Gil-Marín et al. (2015, hereafter Paper I). The parameter \( f \) quantifies the linear growth rate of structures: \( f = \text{dln} \delta / \text{dln} a \), where \( a \) is the scale factor and \( \delta \) the (linear) matter overdensity fluctuation; \( \sigma_8 \) is the rms of the (linear) matter overdensity field extrapolated at \( z = 0 \) and smoothed on scales of \( 8 h^{-1} \) Mpc. Paper I reported \( f^{1.43} \sigma_8 |_{=0.57} = 0.582 \pm 0.084 \) (0.584 \pm 0.051), where the first result corresponds to the conservative analysis and the second to the more optimistic analysis (see Paper I for details). Hereafter we report in parenthesis the results corresponding to the optimistic analysis. The difference in the central values is negligible at all effects; thus, we will only report the error bars corresponding to the optimistic analysis. This 14 per cent (9 per cent) error on the quantity \( f^{1.43} \sigma_8 |_{=0.57} \) is comparable to that obtained in the quantity \( f \sigma_8 \) from the study of redshift-space distortions of the power spectrum of the same survey (e.g. Beutler et al. 2014; Chuang et al. 2013; Samushia et al. 2014; Sánchez et al. 2014), which have error bars of typically 10 per cent. While not being statistically independent (the survey is the same), the method is complementary and the measurement relies on a different physical effect, harvesting the power of higher order correlations rather than the anisotropy of clustering induced by the redshift-space distortions. This paper is organized as follows: in Section 2, we present the data sets we use and the methodology and the consistency of the measurement with the ΛCDM model with GR. Section 3 presents tests constraining several extensions of this model which involve changes in the composition (i.e. neutrino properties) or background (i.e. dark energy models and geometry) or deviations from GR. We explore the potential of combining the bispectrum monopole with anisotropic clustering of the two-point function in Section 4 and conclude in Section 5.

## 2 Methods and Data Sets

In Paper I, we have analysed the anisotropic clustering of the BOSS CMASS DR 11 sample, composed of 690 827 galaxies in the redshift range of \( 0.43 < z < 0.70 \). This survey covers an angular area of \( 8498 \text{ deg}^2 \), which corresponds to an effective volume of \( \sim 6 \text{ Gpc}^3 \).

We have measured the corresponding redshift-space galaxy power spectrum and bispectrum monopoles, providing a measurement of the linear growth rate, \( f \), in combination with the amplitude of matter density fluctuations, \( \sigma_8 \), obtained from the survey, \( z_{\text{eff}} = 0.57 \). The optimistic estimate is obtained by pushing slightly more into the mildly non-linear regime and thus including significantly more modes. For this particular combination of \( f \) and \( \sigma_8 \), close to the maximum likelihood solution the likelihood surface is much closer to that of Gaussian distribution than in the individual parameters. In addition, this measurement is insensitive to the fiducial cosmology assumed in the analysis. Our measurements are supported by a series of tests performed on dark matter N-body simulations, halo catalogues (obtained both from \( \text{PHALOS} \) and N-body simulation) and mock galaxy catalogues (see section 5 in Paper I for an extensive list of tests to check for systematic errors and to assess the performance of the different approximations adopted). These tests are used to identify the regime of validity of the adopted modelling, which occurs when all the k-modes of the bispectrum triangles are larger than 0.03 h Mpc\(^{-1}\) and less than 0.17 h Mpc\(^{-1}\) (with the conservative analysis) or less than 0.20 h Mpc\(^{-1}\) being more optimistic. We have also accounted for real-world effects such as the survey window and systematic weighting of objects. We have opted to add in quadrature the statistical error and half of the systematic shift in order to account for the uncertainty in the systems correction. Because the bispectrum calculation is computationally intensive, we have only considered a subset of all possible bispectrum shapes: \( k_2/k_1 = 1 \) and \( k_2/k_1 = 2 \).

The statistical error on \( f^{1.43} \sigma_8 |_{=0.57} \) has been obtained from the scatter among 600 mockcatalogues. Our cosmologically interesting parameters are the linear matter clustering amplitude \( \sigma_8 \) and the growth rate of fluctuations \( f = \text{dln} \delta / \text{dln} a \). In Paper I, we showed that even jointly, the power spectrum and bispectrum monopole cannot measure these two parameters separately, but do constrain on the \( f^{1.43} \sigma_8 |_{=0.57} \). In this variable, the distribution of the best-fitting parameters for the galaxy mock catalogues is much closer to a Gaussian distribution than in the separate \( \sigma_8 \) and \( f \) parameters.

We combine the \( f^{1.43} \sigma_8 |_{=0.57} \) measurement with the constraints from cosmic microwave background (CMB) observations acquired by the \textit{Planck} satellite (Planck Collaboration 2011; Planck Collaboration I 2014a, XVI 2014b). In many cases, we use the outputs of their Monte Carlo Markov Chains for importance sampling; when specified we run new Markov chains. We use either the \textit{Planck} + WP data (\textit{Planck} primary temperature data with the \textit{Wilkinson Microwave Anisotropy Probe} (WAMP); Bennett et al. 2003) polarization data (Bennett et al. 2013; Hinshaw et al. 2013) at low multipoles or \textit{Planck} + WP + high-L – the above data with the addition of high multipoles temperature observations from the Atacama Cosmology Telescope (Das et al. 2014) and the South Pole telescope (Reichart et al. 2012). The \textit{Planck} maps have also been analysed to extract the weak gravitational lensing signal arising from intervening large-scale structure (Planck Collaboration XVII 2014c). This task is done through the four-point function of the temperature maps; when including this information we refer to it as \textit{lensing}. In some cases, the

¹ This technique would be sensitive, of course, to a velocity bias if tracers did not to statistically represent the distribution of velocities of dark matter. Such a velocity bias is not expected on large scales.

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The bispectrum of BOSS galaxies II 1915

2 METHODS AND DATA SETS

In Paper I, we have analysed the anisotropic clustering of the BOSS CMASS DR 11 sample, composed of 690 827 galaxies in the redshift range of 0.43 < z < 0.70. This survey covers an angular area of 8498 deg², which corresponds to an effective volume of ~6 Gpc³. We have measured the corresponding redshift-space galaxy power spectrum and bispectrum monopoles, providing a measurement of the linear growth rate, f, in combination with the amplitude of matter density fluctuations, σ₈, from the above data with the addition of high multipoles temperature observations from the Atacama Cosmology Telescope (Das et al. 2014) and the South Pole telescope (Reichart et al. 2012). The Planck maps have also been analysed to extract the weak gravitational lensing signal arising from intervening large-scale structure (Planck Collaboration XVII 2014c). This task is done through the four-point function of the temperature maps; when including this information we refer to it as lensing. In some cases, the
3 RESULTS

In this section, we present the constraints that the $f^{0.43} \sigma_8 |_{z=0.57}$ measurement provides on different extensions of $\Lambda$CDM+GR such as (i) neutrino mass properties, (ii) changes in the dark energy equation of state and (iii) deviations from GR.

3.1 Neutrino mass constraints

Among possible $\Lambda$CDM model extensions, which still assume GR, we expect the $f^{0.43} \sigma_8 |_{z=0.57}$ measurement to provide significant improvement over CMB data alone for the cases of where significant evolution in the growth rate to low redshift is expected. This is the case for massive neutrinos and for models where dark energy deviates from a cosmological constant and where more than one evolution-affecting parameter is added to the ‘base’ $\Lambda$CDM model. In other model extensions, the addition of the growth constraints only reduces the CMB error bars by few per cent. In these cases, therefore, this combination offers a test of consistency rather than a technique of reducing parameter degeneracies and improving cosmological constraints.

Massive neutrinos affect the growth of cosmological structure by suppressing clustering below their free streaming length; as a result in models with massive neutrinos the power spectrum amplitude at large-scale structure scales is lower than that at CMB scales. If we allow the three standard-model neutrinos to have a non-zero mass and the sum of the masses $m_\nu$ to be the parameter to be constrained, the Planck+WP data constraints are $m_\nu < 1.31$ eV at 95 per cent confidence, which become $m_\nu < 0.66$ eV when the highL data are considered. Including the $f^{0.43} \sigma_8 |_{z=0.57}$ measurement produces $m_\nu < 0.68(0.47)$ eV and $m_\nu < 0.49(0.38)$ eV, respectively, always at 95 per cent confidence, which represent a factor 2 (2.8) and 1.3 (1.7) improvement, respectively. When the information about lensing is included (through the four-point function of the CMB temperature) in the CMB analysis, the constraint on neutrino masses relaxes to, $m_\nu < 0.85$ eV (95 per cent confidence).\footnote{This point is discussed at length in the literature and in Planck Collaboration XVI (2014b) and is possibly due to a mild tension between the CMB damping tail and the four-point function constraints on the magnitude of the lensing signal.} Including the $f^{0.43} \sigma_8 |_{z=0.57}$ measurement brings back the upper limit to $m_\nu < 0.67(0.50)$ eV. Fig. 2 presents the constraints in the $\sigma_8$--$m_\nu$ plane and illustrates the above features. Basically, the $f^{0.43} \sigma_8 |_{z=0.57}$ measurement, by effectively constraining $\sigma_8$, breaks the $m_\nu$--$\sigma_8$ degeneracy.

A slightly more general extension of the $\Lambda$CDM model is the case where both the number of effective neutrino species $N_{eff}$ and the neutrino mass $m_\nu$ are treated as free parameters. Also in this case the $f^{0.43} \sigma_8 |_{z=0.57}$ measurement improves the constraints, especially on the sum of neutrino masses. This behaviour is illustrated in Fig. 3, where the blue, dashed contours are for Planck+WP and the solid, thick purple (thin, black) contours are in combination with the $f^{0.43} \sigma_8 |_{z=0.57}$ measurement. For $m_\nu$ (marginalized over $N_{eff}$), the CMB constraint $m_\nu < 0.85$ eV (95 per cent confidence) becomes $m_\nu < 0.63(0.46)$ eV (95 per cent confidence).

Qualitatively similar results are also obtained for the massive sterile neutrino case, where the extra sterile neutrinos are made massive constraints on the expansion history and therefore on the growth of structure.

Fig. 1 presents the constraints on the $f$--$\sigma_8$ plane, at $z = 0.57$, obtained from the Planck+WP CMB observations extrapolated assuming GR and a flat $\Lambda$CDM model, from the direct measurement of Paper I and, for completeness, from the BOSS CMASS galaxies anisotropic clustering (Samushia et al. 2014): $f\sigma_8 = 0.441 \pm 0.044$, at $z = 0.57$. The galaxy clustering measurements are individually in agreement with the standard $\Lambda$CDM cosmological paradigm within $\sim$1$\sigma$.

As the two measurements constrain different combinations of $f$ and $\sigma_8$, they can be measured separately from a combined analysis. We explore this prospect in Section 4.

Although there is no evidence for significant tensions between the CMB and the lower redshift measurements (in particular the $f^{0.43} \sigma_8 |_{z=0.57}$ measurement of Paper I), we consider standard $\Lambda$CDM model extensions, where one or more extra cosmological parameters are allowed to vary. We then consider direct constraints on modifications of GR.

In Section 4, we also consider the measurement of the combination $f\sigma_8$ from Samushia et al. (2014). This references the same data set as Paper I but exploits the fact that redshift-space distortions causing an isotropic two-point correlation function become anisotropic. The magnitude of the large-scale velocity field traced by galaxies depends on the nature of gravitational interactions; thus, the angular dependence of the two-point function can be used to measure the combination $f\sigma_8$. For more details, see Reid et al. (2012), Samushia et al. (2014) and references therein.
Constraints in the total neutrino mass in (light) blue, dashed lines indicating 68 and 95 per cent confidence and with the addition of the $f^{0.43} \sigma_{8}\left|z=0.57\right|$ constraints in solid thick purple (solid thin black) contours. As above the tighter constraints are obtained with the optimistic measurement. For $m_\nu$ (marginalized over $N_{\text{eff}}$), we obtain that the CMB constraint $m_\nu < 0.85 \text{ eV}$ at 95 per cent confidence becomes $m_\nu < 0.63(0.46) \text{ eV}$ at 95 per cent confidence.

lower value for $\sigma_8(z = 0)$ than that inferred from the CMB assuming a standard $\Lambda$CDM model with near massless neutrinos. This mismatch has been interpreted as an evidence of non-zero neutrino mass with $m_\nu \sim 0.45 \text{ eV}$. In particular, the joint analysis of Planck temperature data with the cluster abundance from the Planck Sunyaev–Zeldovich clusters (Planck Collaboration XX 2014d) yields a tentative detection of neutrino masses $m_\nu = 0.45 - 0.58 \pm 0.21 \text{ eV}$ depending on assumptions about the calibration of the mass-observable relation. The $f^{0.43} \sigma_{8}\left|z=0.57\right|$ measurement seems to disfavour the new physics in the neutrino sector interpretation of the $\sigma_8$ mismatch. These results are summarized in Table 1.

### 3.2 Dark energy equation of state constraints

In the case of a non-flat model where the dark energy equation of state parameter $w$ is constant, but not necessarily equal to $-1$ –ovCDM-, the combination of Planck+WP and $f^{0.43} \sigma_{8}\left|z=0.57\right|$ measurements constrain $w$ to be $-2.10 < w < -0.33$ ($-1.94 < w < -0.62$) at 95 per cent confidence and the curvature to be $-0.093 < \Omega_k < +0.008$ ($-0.076 < \Omega_k < +0.007$), also at 95 per cent confidence. The joint constraints in the $\Omega_k$–$w$ plane are displayed in the left-hand panel of Fig. 4.

Conversely, if we assume flat geometry, but allow the dark energy equation of state to change with the scale factor $a$ rather than having the mass being equally distributed among all neutrino families: $m_\nu < 0.51(0.42) \text{ eV}$ at 95 per cent confidence when we impose a limit to the physical thermal mass for the sterile neutrino $< 10 \text{ eV}$, for which the particles are distinct from cold or warm dark matter (see Table 1 for details). Some large-scale structure data sets, including the cluster abundance from the Planck Sunyaev–Zeldovich clusters (Planck Collaboration XX 2014d), yield a much

### Table 1. Constraints (95 per cent limits) on the sum of neutrino masses for several models and data set combinations. The $m_\nu$–$\Lambda$CDM model is a spatially flat power-law $\Lambda$CDM model where the sum of neutrino masses is an extra parameter. The $N_{\text{eff}}$–$m_\nu$–$\Lambda$CDM model is a spatially flat power-law $\Lambda$CDM model where both the effective number of neutrino species and the total neutrino mass are extra parameters. The $N_{\text{eff}}$–$m_\nu$–$\Lambda$CDM model is similar to $N_{\text{eff}}$–$m_\nu$–$\Lambda$CDM, but where the massive neutrinos are only the sterile ones. To calculate the constraints, we have imposed a physical thermal mass for the sterile neutrino $< 10 \text{ eV}$, which defines the region in the CMB where the particles are distinct from cold or warm dark matter.

| Model | Planck+WP | Planck+WP+highL | Planck+WP+highL+lensing | Planck+WP | Planck+WP+highL |
|-------|-----------|-----------------|-------------------------|-----------|----------------|
| $m_\nu < 1.31 \text{ eV}$ | $m_\nu < 0.66 \text{ eV}$ | $m_\nu < 0.85 \text{ eV}$ | $m_\nu < 0.67 \text{ eV}$ | $m_\nu < 0.59 \text{ eV}$ | $m_\nu < 0.51 \text{ eV}$ |
| $+f^{0.43} \sigma_{8}\left|z=0.57\right|$ | $+f^{0.43} \sigma_{8}\left|z=0.57\right|$ | $+f^{0.43} \sigma_{8}\left|z=0.57\right|$ | $+f^{0.43} \sigma_{8}\left|z=0.57\right|$ | $+f^{0.43} \sigma_{8}\left|z=0.57\right|$ | $+f^{0.43} \sigma_{8}\left|z=0.57\right|$ |
| Conserv. | $m_\nu < 0.68 \text{ eV}$ | $m_\nu < 0.49 \text{ eV}$ | $m_\nu < 0.67 \text{ eV}$ | $m_\nu < 0.63 \text{ eV}$ | $m_\nu < 0.51 \text{ eV}$ |
| Optim. | $m_\nu < 0.46 \text{ eV}$ | $m_\nu < 0.38 \text{ eV}$ | $m_\nu < 0.50 \text{ eV}$ | $m_\nu < 0.46 \text{ eV}$ | $m_\nu < 0.42 \text{ eV}$ |
Figure 4. Constraints obtained from Planck+WP in combination with the $f^{0.43}\sigma_8|_{\Omega_m=0.57}$ measurement for the following models. In the left-hand panel, constraints in the $\Omega_k$--$w$ plane for a non-flat Universe where the dark energy equation of state is constant but not necessarily $-1$; in the middle panel, constraints in the $w$--$\omega_\gamma$ plane for a flat model where the dark energy equation of state parameter changes with the scale factor $a$ as $w(a) = w_0(1 - a)$. The right-hand panel is the same as the middle panel but where the spatial flatness assumption is relaxed. In this case, $-0.076 < \Omega_k < 0.009$ (95 per cent confidence), respectively. The contour lines represent the 68 and the 95 per cent confidence regions. The saturation of the colour is proportional to the posterior likelihood.

(according to Chevallier & Polarski 2001 and Linder 2003) as $w(a) = w + w_0(1 - a) - \omega_\gamma\Omega_{\Lambda\text{CDM}}$, we obtain the constraints presented in the middle panel of Fig. 4. The single parameter constraints are $-2.03 < w < -0.06 (-1.80 < w < -0.16)$ and $w_0 < 1.27(1.08)$ (at 95 per cent confidence). These constraints do not degrade significantly if flatness is relaxed $-\omega_\gamma\Omega_{\Lambda\text{CDM}}$, as shown in the right-hand panel of Fig. 4. In this case, the constraint on the geometry becomes $-0.083 < \Omega_k < 0.007 (-0.074 < \Omega_k < 0.007)$ at 95 per cent confidence and for the dark energy parameters $-2.38 < w < 0.39 (-2.20 < w < -0.01)$ and $w_0 < 1.64(1.60)$ (95 per cent confidence). For all these cases, we ran new Markov Chains rather than importance sampling existing ones. We conclude that a dark energy component is needed and is dominant even in non-flat models where the dark energy equation of state parameter is not necessarily constant. The density of dark energy in units of the critical density $\Omega_{\text{dark\;energy}}$ at 68 per cent confidence is $0.61 \pm 0.13 (0.637 \pm 0.090)$ in the $\omega\text{CDM}$ model, $0.742 \pm 0.071 (0.728 \pm 0.055)$ in the $\omega\omega\text{CDM}$ model and $0.62 \pm 0.12 (0.639 \pm 0.086)$ in the $\omega\omega\text{CDM}$ model. These constraints are obtained using only data at $z \geq 0.57$ (i.e. $f^{0.43}\sigma_8|_{\Omega_m=0.57}$ and CMB). Any more ‘local’ explanation for dark energy is therefore disfavoured.

### 3.3 Modifications of GR

In modern cosmology, the rationale behind introducing modifications of GR is to explain the late-time cosmological acceleration. Therefore, the most popular modifications of GR mimic the effects of the cosmological constant on the expansion history and become important only at low redshifts. If we allow gravity to deviate from GR, the CMB offers only weak constraints on the late-time growth of structures, via the Integrated Sachs–Wolfe effect and lensing. A popular parametrization for deviations from GR growth is given by

$$f(z) = \Omega_m(z)^{\epsilon}.$$  

(1)

For $\Lambda\text{CDM}$+GR, $\gamma|_{\Lambda\text{CDM}} \approx 0.56$; for dark energy models with an equation of state parameter different from $w = -1$, $\gamma$ acquires a weak redshift dependence and its value does not deviate significantly from $\gamma|_{\Lambda\text{CDM}}$. Since we have a measurement at a given redshift, we consider $\gamma$ to be constant. We also assume that this modification affects the late-time Universe and not the CMB. This assumption is reasonable as in this parametrization, as $\Omega_m(z) \rightarrow 1$ (i.e. for most cosmologies at $z \gg 1$), the growth becomes that of an Einstein–De Sitter Universe for any value of $\gamma$.

For this extension to the base model, we assume that the background expansion history is given by that of the $\Lambda\text{CDM}$ model as constrained by Planck+WP (using Planck+WP+ highL + BAO does not change the results significantly). The constraints on the growth rate reduce to $\gamma = 0.40^{+0.50}_{-0.28}$ at 68 per cent confidence and $\gamma < 0.87 (0.80)$ at 95 per cent confidence.

For coupled dark energy–dark matter models, the growth can be parametrized as (e.g. di Porto & Amendola 2008, and references therein),

$$f(z) = \Omega_m(z)^{\epsilon} (1 + \eta).$$  

(2)

Using this equation, we obtain $\eta = 0.055 \pm 0.145 \pm 0.090$ at 68 per cent confidence. For the coupled dark energy–dark matter models, $\eta$ is related to the coupling constant $\beta_c$. These models have a non-negligible amount of dark energy at early times, so they can be constrained by the CMB. Nevertheless, the $\eta$ constraint can be reinterpreted as a limit on the coupling constant $\beta_c < 0.34 (<0.28)$ at 95 per cent confidence at the effective survey redshift $z = 0.57$; as expected this constraint is much weaker than that obtained from the CMB by Pettorino et al. (2012) assuming a constant coupling.

Inspired by Acquaviva et al. (2008), who introduced the quantity $\epsilon = f/f|_{\Lambda\text{CDM}} - 1$, we can define

$$\epsilon' = \frac{f^{0.43}\sigma_8|_{\Lambda\text{CDM}}}{f^{0.43}\sigma_8} - 1,$$  

(3)

which is a more model-independent approach than the $\gamma$-parametrization of equation (1) or the $\eta$-parametrization of equation (2). Equation (3) also enables one to quantify possibly early times deviations from GR. Note that since $\sigma_8(z)/\sigma_8(z)|_{\Lambda\text{CDM}} = D(z)/D(z)|_{\Lambda\text{CDM}}$, where $D(z)$ is the linear growth factor, equation (3) parametrizes deviations on the $f^{0.43}\sigma_8|_{\Omega_m=0.57}$ (or on the $f^{0.43}D|_{\Omega_m=0.57}$ produced by changes in the theory of gravity on $f$ and $D$, whereas equation (2) only accounts for changes on $f$. This quantity, which is identical to zero for $\Lambda\text{CDM}$ and exceedingly close to zero for minimally coupled quintessence-type models, is redshift dependent and can, in principle, be also scale dependent when departures from GR

\[ \text{In the } \gamma\text{-parametrization, the standard growth is recovered for all values of } \gamma \text{ at } z > 0.5; \text{ when } \Omega_m \rightarrow 1. \]
are present. Here we assume $\epsilon'$ is scale independent over the scales probed and we compute its value at the effective survey redshift. For $f^{0.43}\sigma_8|_\Lambda CDM$, we take the range predicted by the Planck+WP combination and obtain, at 68 per cent confidence,

$$\epsilon'(z = 0.57) = 0.04 \pm 0.15(\pm 0.10),$$

in agreement with the GR value of zero.

4 BREAKING THE $f$-$\sigma_8$ DEGENERACY

As displayed in Fig. 1, the constraints in the $f$-$\sigma_8$ plane produced by the redshift-space distortions of the anisotropic redshift-space correlation function and those produced by the monopole of the power spectrum and bispectrum are highly complementary.

A joint analysis combining the two-point anisotropic clustering and the bispectrum monopole is able to break the degeneracy between $f$ and $\sigma_8$, enabling the measurement of both quantities separately. Here we do not attempt a full, combined analysis of the power spectrum monopole, quadrupole and the bispectrum monopole, which would yield the combined constraint of multiple parameters, including bias if a single consistent bias model were adopted. We will consider such analysis in a future work.

Instead, we perform a combined, a posteriori, analysis between the measurements of $f\sigma_8|_{z=0.57}$ obtained by Samushia et al. (2014), when the background expansion is fixed to the one predicted by Planck, and of $f^{0.43}\sigma_8|_{z=0.57}$ obtained in Paper I. Although the measurements were carried out independently, and one is performed in configuration space while the other in Fourier space, they share the information related to the monopole of the two-point statistics, and therefore they are expected to be moderately correlated. Using measurements based on the same set of mocks (Manera et al. 2013), we compute the correlation and errors from their dispersion (see section 3.9 in Paper I for details of the method). We consider the measurement of $|f\sigma_8|$ and $|f^{0.43}\sigma_8|$, for each single $i$-mock, and combining them we extract the corresponding values:

$$|f| = \left\{ |f\sigma_8|/|f^{0.43}\sigma_8| \right\}^{1/0.57},$$

(5)

$$|\sigma_8| = |f\sigma_8|/|f|. $$

(6)

The errors on $f$ and $\sigma_8$ are estimated from the dispersion of $|f|$, and $|\sigma_8|$, among all the mocks, respectively. This result is illustrated in Fig. 5, where the blue dots represent the obtained values of $|f|$, and $|\sigma_8|$, for the 600 realizations of the galaxy mocks: $i = 1, 2, \ldots, 600$.

The combined constraints in the $f$-$\sigma_8$ plane are displayed in Fig. 5, which illustrates the constraints on $f\sigma_8$ and $f^{0.43}\sigma_8$ from Samushia et al. (2014) and Paper I, respectively, using the same line notation as in Fig. 1. Blue dots represent the best-fitting values for the mocks and the red cross shows the best-fitting value for the DR11 CMASS data set. The green dashed ellipses represent the Planck CMB-inferred constraints (68 and 95 per cent confidence) when assuming GR and a $\Lambda$CDM model. The red contours correspond to the (joint) 68 per cent (solid lines) and 95 per cent (dashed lines) confidence levels extracted from the mocks and centred on the data, where the mild prior $0 < f < 2$ has been used.

Originally, the constraints on $f\sigma_8$ and $f^{0.43}\sigma_8$ were $f\sigma_8|_{z=0.57}=0.447\pm0.028$ and $f^{0.43}\sigma_8|_{z=0.57}=0.582\pm0.084 (0.051)$. After combining the measurements, the degeneracy between $f$ and $\sigma_8$ is broken, although the two parameters remain significantly (anti)correlated, with a correlation coefficient of $\sim-0.9$. From the joint distribution, we can now obtain marginalized constraints on each of the parameters: $f(z_{eff}) = 0.63 \pm 0.16 (0.13)$ (marginalized over $\sigma_8$), $\sigma_8(z_{eff}) = 0.710 \pm 0.086 (0.069)$ (marginalized over $f$), where all the reported errors are at the 68 per cent confidence level. These values represent a 12(10) per cent and 25(20) per cent relative error for $\sigma_8(z_{eff})$ and $f(z_{eff})$, respectively.

Previous works in the literature have used bispectrum alone or in combination with the power spectrum of galaxies to break degeneracies present in the power spectrum analysis. Scoccimarro et al. (2001), Verde et al. (2002), Nishimichi et al. (2007), McBride et al. (2011) and Chiang et al. (2015) constrain the bias parameters $b_1$ and $b_2$ with the bispectrum (or equivalent observables), the derived $b_1$ parameter can then be used in combination with the power spectrum-derived $\beta \sim f/b_1$ to constrain $f$. Marin et al. (2013) use the bispectrum to constrain the amplitude of primordial fluctuations $\sigma_8$ when other cosmological parameters (such as $f$) were fixed to fiducial ($\Lambda$CDM, GR) values. However, this is the first time that these two quantities $f$ and $\sigma_8$ have been separately determined from galaxy clustering using the power spectrum and bispectrum measurements.

The resulting values for $f$ and $\sigma_8$ are in broad agreement with the CMB-inferred values. This can be appreciated in Fig. 5, where the green dashed ellipses are in general agreement with the red contours of the data. We have also computed the tension $T$ as introduced in Verde, Protopapas, & Jimenez (2013), which quantifies whether multidimensional cosmological parameters constraints from two different experiments are in agreement or not. We find that the tension is not significant, $\ln T < 1$, i.e. the two measurements are in agreement.

We have repeated the analysis of Sections 3.1 and 3.2 using these new constraints, but we find that the constraints on the cosmological parameters do not change in any significant way. At the current size of the error bars of $f^{0.43}\sigma_8|_{z=0.57}$, the $f\sigma_8$ degeneracy is being cut for
high values of $\sigma_8$, but has a tail for low values of $\sigma_8$, as it is shown in Fig. 5. Therefore, breaking the $f\sigma_8$ degeneracy in this way (in combination with Planck data) does not improve significantly the error bars in the studied parameters. We expect that this will improve with the forthcoming analysis of DR12, where a joint analysis of power spectrum monopole, quadrupole and bispectrum monopole will be performed.

When the measurements obtained on $f$ are applied to the parameters of equation (1), the constraints on $\sigma_8$ increase $\gamma = 0.40 \pm 0.43(0.35)$ (68 per cent confidence). We can now consider the variable $\epsilon$ introduced by Acquaviva et al. (2008), obtaining $\epsilon = -0.21 \pm 0.56(0.45)$, also at 68 per cent confidence. Both measurements should be considered at $z_{\rm eff} = 0.57$ at scales of $k \approx 0.1 \, {\text{h Mpc}}^{-1}$. In order to be able to use these measurements to distinguish between GR and popular and viable modifications of gravity that match the $\Lambda$CDM model expansion history, error bars would have to be reduced by a factor of few.

In this paper, we only have considered to combine the results obtained from the power spectrum and bispectrum monopole analysis, with those from the anisotropic two-point correlation function (Samushia et al. 2014). Moreover, we only consider constraints on the parameters describing the growth of perturbations and not the expansion history. The expansion history can be probed with the power spectrum (both monopole and quadrupole) via the parameters $D_\Lambda/r_\Lambda$ and $F$ as it has been done by the same collaboration (Samushia et al. 2014). But exploring the effect of adding the bispectrum information to e.g. break the degeneracy between $F$ and $f\sigma_8$ goes beyond the scope of this paper.

It may seem disappointing at first sight that the time consuming and challenging analysis of the galaxy bispectrum does not seem to improve dramatically the cosmological constraints on parameters such as $\gamma$. However, it is important to keep in mind that the bispectrum is a different statistic from the monopole and quadrupole of the power spectrum, which relies on different modelling, different physical effects and is affected by different systematics. It adds some additional information to the power spectrum analysis which goes beyond the size of the error bars on some cosmological parameters. It offers a consistency check. It gives insights on the behaviour and amplitude of the galaxy bias, and serves as a test of our modelling of mild non-linearities and non-linear redshift-space distortions.

We have shown for example that adding our bispectrum result on $f^{0.45}\sigma_8$ to Planck data, constrains neutrino mass as much as adding the ‘highL’ and ‘highL’ combined with Planck lensing.

Moreover, it has been proposed that the bispectrum in combination with the power spectrum could be used to constrain not just gravity and bias, but also the nature of the initial conditions (primordial non-Gaussianity) from future surveys. It is important to start exploring the challenges and opportunities that a combined power spectrum and bispectrum analysis offer.

5 CONCLUSIONS

We have examined the cosmological implications of the constraints on the quantity $f^{0.45}\sigma_8$ at $z_{\rm eff} = 0.57$, which offers a direct cosmological and model-independent probe of the growth of structure. This constraint has been obtained from the measurement of the power spectrum and bispectrum monopoles of the SDSSIII BOSS DR11 CMASS galaxies and has been recently presented in a companion paper (Paper 1).

We have combined this result with recent state-of-the art CMB constraints for several underlying cosmological models. We find agreement in the standard $\Lambda$CDM cosmological paradigm between the growth of structure predicted by CMB observations and the direct measurement from galaxy clustering.

When considering popular $\Lambda$CDM model extensions, which still rely on GR, we find that this new measurement is useful to improve the CMB constraints on cosmological parameters only for model extensions that involve massive neutrinos or for models where dark energy deviates from a cosmological constant and where more than one parameter is added. The $f^{0.43}\sigma_8|_{z=0.57}$ measurement improves CMB neutrino mass constraints by at least 30 per cent and in some cases by as much as factor 2.2–2.8. (see Table 1 for details). There is no evidence for non-standard neutrino properties when considering CMB and $f^{0.43}\sigma_8|_{z=0.57}$ measurements.

For dark energy models where the equation of state parameter of dark energy is not constant, or for models where it is constant but not equal to $-1$ and the geometry of the Universe is not constrained to be flat, we can obtain interesting constraints. Curvature is constrained at the 8 per cent level (95 per cent confidence). We find no evidence for any deviations from a cosmological constant, but dark energy is needed as a dominant component of the Universe, even for non-flat, non-$\Lambda$CDM cosmologies. This conclusion is reached using only data at $z \geq 0.57$, thus disfavouring ‘local’ explanations of dark energy.

We have also examined the constraints that the measurement of $f^{0.43}\sigma_8|_{z=0.57}$, in combination with data on the Universe’s geometry and expansion history, provides on modifications of GR. We have examined different phenomenological parametrizations of how the growth of structure is modified when we relax the assumption of GR. We do not observe any significant tension between these measurements and GR predictions; in particular, we find that $\gamma = 0.40^{+0.35}_{-0.22}(0.25)$ (68 per cent confidence), where $f(z) = \Omega_m(z)^\gamma$.

Finally, we have presented the measurement of $f^{0.43}\sigma_8|_{z=0.57}$ can be combined with the measurement of $f\sigma_8|_{z=0.57}$ from the same galaxy sample to break the degeneracy between $f$ and $\sigma_8$. This is the first time that a separate measurement of $f$ and $\sigma_8$ has been obtained using power spectrum and bispectrum measurements from galaxy clustering: $f = 0.63 \pm 0.16$ and $\sigma_8 = 0.710 \pm 0.086$, both at $z = 0.57$. The size of errors already provides an insight on how powerful a fully and optimal joint analysis can be. We find that $f$ can be measured with a relative precision of $\sim 25$ per cent, and $\sigma_8$ with $\sim 10$ per cent at 68 per cent confidence level. We expect that the size of these error bars can be reduced if the power spectrum multipoles and bispectrum monopole are combined prior to obtain the $f$ and $\sigma_8$ best-fitting values. Further testing for potential systematics would also be of benefit for such novel analysis.

While the $f-\sigma_8$ degeneracy could also be broken using measurements at several different redshifts, or resorting to weak lensing data or cross-correlation with the weak lensing signal of the CMB, the approach described in this paper provides a complementary and self-contained approach to achieve the same goal relying on galaxy redshift surveys alone, without the need of wide redshift coverage.

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REFERENCES

Acquaviva V., Hajian A., Spergel D. N., Das S., 2008, Phys. Rev. D, 78, 043514
Albrecht A. et al., 2006, Astrophyics, preprint (arXiv: e-prints)
Amendola L. et al., 2013, Living Rev. Relativ., 16, 6
Anderson L. et al., 2013, MNRAS, 427, 3435
Bennett C. L. et al., 2003, ApJS, 148, 1
Bennett C. et al., 2013, ApJS, 208, 20
Beutler F. et al., 2011, MNRAS, 416, 3017
Beutler F. et al., 2014, MNRAS, 443, 1065
Blake C. et al., 2011, MNRAS, 418, 1707
Bolton A. S. et al., 2012, AJ, 144, 144
Chevalier M., Polarski D., 2001, Int. J. Mod. Phys. D, 10, 213
Chiang C.-T., Wagner C., Sánchez A. G., Schmidt F., Komatsu E., 2015, preprint (arXiv: e-prints)
Chuang C.-H. et al., 2013, MNRAS, 433, 3559
Das S. et al., 2014, JCAP, 04, 014
Dawson K. S. et al., 2013, AJ, 145, 10
di Porto C., Amendola L., 2008, Phys. Rev. D, 77, 083508
Eisenstein D. J. et al., 2011, AJ, 142, 72
Feng J. L. et al., 2014, preprint (arXiv: e-prints)
Fry J. N., 1994, Phys. Rev. Lett., 73, 215
Gil-Marín H., Noreña J., Verde L., Percival W. J., Wagner C., Manera M., Schneider D. P., 2015, MNRAS, 451, 5058
Gunn J. F. et al., 1998, AJ, 116, 3040
Gunn J. E. et al., 2006, AJ, 131, 2332
Hinshaw G. et al., 2013, ApJS, 208, 19
Linder E. V., 2003, Phys. Rev. Lett., 90, 091301
McBride C. K., Connolly A. J., Gardner J. P., Scranton R., Scocccimarro R., Berlind A. A., Marín F., Schneider D. P., 2011, ApJ, 739, 85
Manera M. et al., 2013, MNRAS, 428, 1036
Marín F. A. et al., 2013, MNRAS, 432, 2654
Nishimichi T., Kayo I., Hikage C., Yahata K., Taruya A., Jing Y. P., Sheth R. K., Suto Y., 2007, PASJ, 59, 93
Padmanabhan N., Xu X., Eisenstein D. J., Sculzo R., Cuesta A. J., Mehta K. T., Kazin E., 2012, MNRAS, 427, 2132
Percival W. J. et al., 2010, MNRAS, 401, 2148
Petrorino V., Amendola L., Baccigalupi C., Quercellini C., 2012, Phys. Rev. D, 86, 103507
Planck Collaboration I, 2011, A&A, 536, A1
Planck Collaboration I, 2014a, A&A, 571A, 1
Planck Collaboration XVI, 2014b, A&A, 571A, 16
Planck Collaboration XVII, 2014c, A&A, 571A, 17
Planck Collaboration XX, 2014d, A&A, 571A, 20
Reichardt C., Shaw L., Zahn O., Aird K., Benson B. et al., 2012, ApJ, 755, 70
Reid B. A. et al., 2012, MNRAS, 426, 2719
Samushia L. et al., 2014, MNRAS, 439, 3504
Sanchez A. G. et al., 2014, MNRAS, 440, 2692
Scocccimarro R., Feldman H. A., Fry J. N., Frieman J. A., 2001, ApJ, 546, 652
Smee S. A. et al., 2013, AJ, 146, 32
Verde L. et al., 2002, MNRAS, 335, 432
Verde L., Protopapas P., Jimenez R., 2013, Phys. Dark Universe, 2, 166

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