Badge System Analysis and Design

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ABSTRACT
To incentivize users’ participations and steer their online activities, online social networks start to provide users with various kinds of rewards for their contributions to the sites. The most frequently distributed rewards include account levels, reputation scores, different kinds of badges, and even material awards like small gifts and cash back, etc. Attracted by these rewards, users will spend more time using the network services. In this paper, we will mainly focus on “badges reward systems” but the proposed models can be applied to other reward systems as well.

Badges are small icons attached to users’ homepages and profiles denoting their achievements. People like to accumulate badge for various reasons and different badges can have specific values for them. Meanwhile, to get badges, they also need to exert efforts to finish the required tasks, which can lead to certain costs. To understand and model users’ motivations in badge achievement activities, we will study an existing badge system launched inside a real-world online social network, Foursquare, in this paper.

At the same time, to maximize users’ contributions to online social networks, social network system designers need to determine the optimal badge system mechanism carefully. Badge system mechanism describes various detailed aspects of the system and can involve many parameters, e.g., categories of existing badges, number of badges available as well as the minimum contributions required to obtain the badges, which all need to be designed with meticulous investigations. Based on the model of users’ badges accumulating activities, in this paper, we will also study how to design the badge system that can incentivize the maximum users’ contributions to the social networks.

Categories and Subject Descriptors
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Keywords
Badge System, Social Network, Game Theory, Data Mining

1. INTRODUCTION TO BADGE SYSTEM

Social networks, e.g., Facebook, Twitter and Foursquare, have achieved remarkable success in recent years. These social networks are mostly driven by user-generated content, e.g., posts, photos and location checkins. To incentivize users’ participations and steer their online activities, many social networks start to offer users various rewards for their contributions to the networks. In this paper, we will mainly focus on “badge reward systems” but the proposed models can be applied to other reward systems as well. Badge systems have been adopted by a wide range of social networks: (1) Foursquare, a famous location-based social network (LBSN), is distributing different badges to users for their geo-location checkins; (2) Weibo, a social media in China, launches a badge system to give users badges for writing posts and replies; (3) Stack Over
a popular question and answer (Q&A) site for computer programming, adopts a system where users can get badges by answering questions in the site; and (4) In Khan Academy\footnote{https://www.khanacademy.org}, a popular massive open online course (MOOC) site, users are awarded badges for watching course videos and answering questions.

1.1 User Activity Observations

People like to accumulate badges for various reasons and different badges can have specific values for them. Extensive analyses have been done on a real-world badge system launched in Foursquare during the April of 2014. We collected 4,240 users together with all the 1,430 categories of badges achieved by them. These users are crawled with BFS search from several random seed users via the social connections in Foursquare, who are connected by follow links of number 81,291. To denote that a user has achieved certain badges, we add achieve links between users and badges, whose total number is 176,301 in the crawled dataset. On average, each user has achieved 42 badges in Foursquare. In addition, each category of badges can involve different badge levels, where badges of consequential levels can be connected by the level links. For example, badges of higher level, e.g., $l (l > 1)$, can have level links pointing to badge of level $l - 1$ and the number of level links among badges is 47,342. A more detailed information about the dataset is available in Table 1.

The statistical analyses results about the badge system dataset are available in Figure 1 and Table 2, from which many interesting phenomena can be observed:

1. Generally, users who are friends are more likely to share common badges. We randomly sample a certain number of user pairs who are (1) friends (i.e., connected by social links) and (2) not friends from Foursquare, and count the number of common badges shared by these user pairs respectively. The results are given in Figure 1(a) where the x axis is the number of randomly sampled user pairs and the y axis denotes the number of shared badges between these sampled pairs. From Figure 1(a) we can observe that online badge achievement in social networks is correlated with social connections among users and friends are more likely to have common badges.

2. In many cases, users are likely to obtain badges which have never been achieved by his friends. As shown in Figure 1(b) for each badge $b_j$ obtained by user $u_i$, we get the timestamp when $u_i$ get $b_j$ and the ratio of $u_i$’s friends who obtain $b_j$ before $u_i$. The distribution of the percentage of badges obtained at different ratios is given in Figure 1(b) from which we can observe that a large proportion of badges are obtained at small ratios, i.e., few of $u_i$’s friends have achieved the badge before $u_i$.

3. In some cases, users will follow their friends when most of their peers have obtained a certain badge. Still in Figure 1(b) when the ratio is close to 1.0, i.e., almost all the peers have obtained a certain badge, the fraction of badge obtained will increase to 0.1, representing that about 10% of the badges are obtained by users when all his friends have achieved the badge. As a result, users’ badge achievement activities in online social networks are highly related to those of their peers. These three observed effects of peers’ badges on users’ activities are called the peer leadership value of badges in Section 3.1.

4. Users are keen on getting badges that are to their interests. In Table 2 we extract top 10 popular badges achieved by the most users in Foursquare and each of these badges has 10 different levels. Numbers of users who have obtained certain levels of each kind of badge as well as the total number of badges achieved (i.e., summation of each row of the table) are provided. The corresponding icons of these badges are shown in Figure 3. Generally, higher-level badges require more efforts from the users, but from Table 2 we observe there are still a large number of users are willing to devote such high efforts to get the badges due to their personal interests. For example, among the 2,468 users who achieved the “Fresh Brew” badge of level 1, 22.5% of them will continue to get badge of level 5, which may denote these users like drinking coffee a lot. Similarly, for users who get different levels of “Mall Rat” badges, they should like shopping a lot; users who get the “JetSetter” badges are those who travel frequently. As a result, badges can reveal users personal interests, especially higher-level badges. Such a kind of effects

\begin{table}[h]
\centering
\caption{Properties of the Badge System Dataset}
\begin{tabular}{|c|c|}
\hline
property & number \\
\hline
nodes & 4,240 \\
badge & 1,431 \\
follow & 81,291 \\
achieved & 176,301 \\
level & 47,342 \\
\hline
\end{tabular}
\end{table}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure3.png}
\caption{Top 10 badges achieved by most users}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure4.png}
\caption{Tasks needed to unlock “JetSetter” badges.}
\end{figure}
Users in online social networks are enthusiastic in earning badges. As shown in Figure 4, the distribution of user fractions obtaining a certain number badges follows the power law \[5\] and the majority of the users in Foursquare have obtained more than 50 badges in Foursquare. In Table 2, we observe that over 2,000 have ever obtained the “Fresh Brew”, “Mall Rat”, “JetSetter”, “Hot Tamale”, “Great Outdoors” and “Pizzaiolo” badges. Considering that there are only 4,240 users in the dataset, we can observe that most users in Foursquare have achieved these badges. One potential explanation of the observation can be that: initially, people use social network services independently of the badges; meanwhile, after using the network for a while, users start to lose interesting, and the badges start to play their roles in keeping users within the network. Such a kind of effects of badges on users is defined as the network trend value of badges in Section 3.3.

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1.2 Badge System Analysis

To get badges, users in online social networks are required to finish certain tasks, which can be (1) finishing a certain number of check-ins at required locations in Foursquare, (2) answering a number of questions proposed by other users in Stack Overflow, and (3) publishing required numbers of posts in Weibo. These tasks of higher-level badges are usually more challenging. For instance, due to the following reasons: (i) finishing a certain number of contributions drawn by these badges will be low. On the other hand, if the threshold is set too high, very few people will devote their effort to getting the badge as these badges will be difficult to obtain and the total amount of users’ contributions will be low as well.

1.3 Badge System Modeling Challenges

The badge system analysis and design problem studied in this paper is a new research problem and it is very challenging to solve due to the following reasons:

- **Badge Value Definition**: The value of badges for users in online social networks is unclear. Formal definition, quantification and inference of the badge values for users can be the prerequisite for a comprehensive modeling users’ badge achievement activities.

- **User Utility Function**: Users can get reward from the achieved badges, i.e., the value of badges, but also needs devote their efforts, i.e., the cost. Formal definition of the payoff by achieving badges, i.e., the utility, is still an open problem.

### Table 2: Number of users achieving top 10 badges

| badge name           | obtain it by                             | # users achieving badges of different levels | total number |
|----------------------|------------------------------------------|---------------------------------------------|--------------|
| Fresh Brew           | Coffee Shops                             | 2468 1914 1235 817 555 374 255 144 78 38 | 7878         |
| Mall Rat             | Shopping Malls                           | 2545 1907 1076 624 366 224 130 81 46 29 | 7028         |
| JetSetter            | Airport Terminals                        | 2357 1703 972 564 339 210 147 102 63 11 | 6468         |
| Hot Tamale           | Mexican Restaurants                      | 2305 1733 989 583 336 191 105 58 37 18 | 6355         |
| Great Outdoors       | Parks and Outdoors                       | 2119 1535 801 468 295 200 132 95 53 30 | 5728         |
| Pizzaiolo            | Pizza Restaurants                        | 2192 1450 605 267 116 62 26 16 8 4    | 4746         |
| Swimmies             | Lake/Pond/Beach                          | 1888 1214 538 281 159 107 74 47 36 17 | 4361         |
| Bento                | Sushi Restaurants                        | 1741 1121 459 209 104 63 34 21 14 8   | 3774         |
| Zoetrope             | Movie Theaters                           | 1985 1106 309 103 34 16 12 6 5 4      | 3580         |
| Flame Broiled        | Burger Restaurants                       | 1944 1044 337 105 40 13 6 3 1 1       | 3494         |
• Game Among Users: Each user aims at maximizing his overall utility, which can be influenced by other users’ activities at the same time. As a result, users’ online badge achieving activities can lead to a game involving all users. Formulation and analysis of such a game among users in online social networks is very difficult.

• Optimal Badge Mechanism: Users’ utility in badge achievement is determined by the badge system mechanism set by the designer. Users aim at maximizing their overall utility with as few efforts as possible, while the designer aims at maximizing users’ overall contribution to the network. As a result, there also exists a game between users and the designer, which will make the problem more challenging.

The following parts of this paper are organized as follows. Section 2 is about the definitions of many important concepts. Various value functions of badges for users will be introduced and combined in the comprehensive value function in Section 3. Users’ utility function is given in Section 4. In Section 5, we study the game among users in online social network. In Section 6, we solve the badge system design problem by formulating it as a game between users and the designer and provide basic simulation analysis about various aspects in the badge system design problem. The related works are introduced in Section 7. Finally, we conclude the paper in Section 8.

2. TERMINOLOGY DEFINITION

Users in social networks can be gifted in different areas and they can satisfy the tasks required to get badges corresponding to their efforts. For instance, in Foursquare, sports enthusiasts can get Gym Rat badges easily as they do sports in gyms regularly, while travel lovers can obtain Jetsetter or Trainspotter badges by checking in at train stations and airports frequently. However, for users who want to get badges of areas that they are not good at, it would be very difficult to finish the required tasks. For example, a sports enthusiast may need to spend lots of time and money to get the Jetsetter or Trainspotter badges by travelling. Similarly, gourmets who seldom do sports may suffer a lot to get Gym Rat badges by visiting gyms. Let \( U = \{u_1, u_2, \ldots, u_n\} \) and \( B = \{b_1, b_2, \ldots, b_m\} \) be the sets containing users and badges respectively in the network. To depict such phenomena, we formally define the concepts of ability, effort and contribution of users in \( U \) as well as contribution threshold of badges in \( B \) as follows.

Definition 1. (Ability): User \( u_i \)'s talents or advantages in fields corresponding to badges in \( B \) can be represented as the ability vector \( a_i = [a_{i,1}, a_{i,2}, \ldots, a_{i,m}] \), where \( a_{i,j} \geq 0 \) denotes \( u_i \)'s ability in the field of badge \( b_j \) or simply \( u_i \)'s ability to get badge \( b_j \).

All people are assumed to be created equally talented. People can be talented at different aspects but the total intelligence each person have can be quite close. For simplicity, we assume the total abilities of different users are equal, i.e., \( |a_{1,j}| = |a_{2,j}| \), for \( \forall u_1, u_2 \in U \). Besides talents, to make achievements in certain areas, every people need to devote their efforts and passion, which can be either money, time, energy or knowledge. In this paper, the resources users will devote to the system is time and the formal definition of unit time effort is available as follows.

Definition 2. (Unit Time Effort): Vector \( e_i = [e_{i,1}, e_{i,2}, \ldots, e_{i,m}] \) denotes user \( u_i \)'s efforts devoted to the field corresponding badges in \( B \) in unit time, where \( e_{i,j} \geq 0 \) represents \( u_i \)'s effort devoted in the area of badge \( b_j \), or simply \( u_i \)'s effort in getting badge \( b_j \).

Users’ unit time effort can vary with time and can be represented as a function on time, e.g., \( e_{i,j}(t) \). The total amount of unit time effort in different areas of all users are assumed to be equal, i.e., \( |e_{1,j}| = |e_{2,j}| \), for \( \forall u_1, u_2 \in U \). Meanwhile, the more time people devote to certain area, the more cumulative efforts he will devote to the area.

Definition 3. (Cumulative Effort): Term \( \hat{e}_{i,j} = \int_{0}^{T} e_{i,j}(t) \, dt \) is defined as the cumulative effort that user \( u_i \) devotes to badge \( b_j \) during time period \( [0, T] \). For both users and designer, cumulative effort is more meaningful as they only care about the total amount of effective efforts devoted to the system. Vector \( \hat{e}_i = [\hat{e}_{i,1}, \hat{e}_{i,2}, \ldots, \hat{e}_{i,m}] \) is defined as the cumulative efforts that user \( u_i \) pays to the network.

In this paper, active users are assumed to have more cumulative efforts as they spend more time using the social network. The achievements people obtain depend on not only their ability in a certain area but also the efforts the devoted to the area, which can be formally defined as their contributions to the network.

Definition 4. (User Contribution): The effectiveness of users’ cumulative efforts devoted to a social network is formally defined as their contributions. Vector \( c_i = [c_{i,1}, c_{i,2}, \ldots, c_{i,m}] \) is defined to be user \( u_i \)'s contributions to the whole system, where \( c_{i,j} \) is the contribution of user \( u_i \) devoted to the network in getting badge \( b_j \) during \([0, T]\):

\[
\forall i,j, \quad c_{i,j} = \int_{0}^{T} a_{i,j} e_{i,j}(t) \, dt = a_{i,j} \int_{0}^{T} e_{i,j}(t) \, dt = a_{i,j} \hat{e}_{i,j}.
\]

As a result, the more effort people devote to areas they are gifted at, the more remarkable achievements they can get in the areas. In social networks, whether a user can receive a badge depends on not only the contributions he/she make but also the contribution threshold of the badge.

Definition 5. (Badge Threshold): A badge’s threshold denotes the minimum required contributions required for users to get the badge. For badges in \( B \), their threshold can be represented as \( \theta = [\theta_1, \theta_2, \ldots, \theta_m] \).

For a given user \( u_i \), if his/her contribution to badge \( b_j \), i.e., \( c_{i,j} \), is greater than \( b_j \)’s threshold \( \theta_j \), then \( u_i \) will get \( b_j \), which can be represented with the following badge indicator function:

\[
I(c_{i,j} \geq \theta_j) = \begin{cases} 
1, & \text{if } c_{i,j} \geq \theta_j, \\
0, & \text{otherwise}.
\end{cases}
\]

Furthermore, the badges that user \( u_i \) have received can be represented as the badge indicator vector \( I_i = [I(c_{i,1} \geq \theta_1), I(c_{i,2} \geq \theta_2), \ldots, I(c_{i,m} \geq \theta_m)] \). Before the system starts to operate and players begin to invest their efforts, the badge system designer needs to specify the badge system settings in advance, which is formally defined as the badge system mechanism in this paper.

Definition 6. (Badges System Mechanism): Badge system mechanism describes various detailed aspects of the system. In addition to badge thresholds, the mechanism of badge system in online social networks can also involve the categories, number, names, IDs, levels of badges, as well as methods to get the badges, etc.
3. BADGE VALUE FUNCTIONS

The motivation of users being willing to devote efforts to get badges in online social networks is because these badges are valuable to them. Depending on the specific scenarios, the value of badges for users can be quite different. According to the observations in Section 1, the effects of badges on users’ social activities can be models as three different kinds of values of these badges. In this section, we will introduce three different value functions which can capture the badge values from different perspectives: (1) personal interest value function, (2) peer leadership value function, and (3) network trend value function.

3.1 Peer Leadership Value Function

In our daily life, on the one hand, people want to be different from the public, but, on the other hand, they may also want to follow the mainstream as well. We have similar observations about users badge achieving activities in online social networks. Users in online social networks want to be the first to win certain badges in their communities, which can show their uniqueness and make them stand out from his/her peers. Meanwhile, if most of the peers have obtained a certain badge, users will follow their friends to get the badge to extract themselves from the backward position. To depict the effectiveness of badges to make users be either more superior to his peers or closer to other leading peers, we formally define the peer leadership value badge in this part.

3.1.1 Peer Leadership Value Function Definition

Definition 7. (Peer Leadership Value): The peer leadership value of badge $b_j$ for a user $u_i$ is defined as a function of the ratio of $u_i$’s peers who have obtained badge $b_j$ already. Let $\Gamma(u_i)$ be the neighbor set of user $u_i \in U$, in which users who have achieved badge $b_j$ before $u_i$ can be represented as $\Psi(u_i, b_j) = \{ u_m \mid |u_m| \in \Gamma(u_i) \wedge (|u_m| (j) = 1) \}$. The peer leadership value function of badge $b_j$ for user $u_i$ can be represented as function

$$v^p(u_i, b_j|\Gamma(u_i)) = f\left(\frac{|\Psi(u_i, b_j)|}{|\Gamma(u_i)|}\right), \Psi(u_i, b_j) \subset \Gamma(u_i).$$

The concrete representation of the peer leadership value functions can be quite diverse depending on the selected function $f()$. In this paper, we try 4 different functions, and the corresponding peer leadership value functions are listed as follows:

- **linear peer leadership value function**
  $$v^p_l(u_i, b_j|\Gamma(u_i)) = a \left(\frac{|\Psi(u_i, b_j)|}{|\Gamma(u_i)|}\right) + b,$$

- **quadratic peer leadership value function**
  $$v^p_q(u_i, b_j|\Gamma(u_i)) = a \left(\frac{|\Psi(u_i, b_j)|}{|\Gamma(u_i)|}\right)^2 + b \left(\frac{|\Psi(u_i, b_j)|}{|\Gamma(u_i)|}\right) + c,$$

- **cubic peer leadership value function**
  $$v^p_c(u_i, b_j|\Gamma(u_i)) = a \left(\frac{|\Psi(u_i, b_j)|}{|\Gamma(u_i)|}\right)^3 + b \left(\frac{|\Psi(u_i, b_j)|}{|\Gamma(u_i)|}\right)^2 + c \left(\frac{|\Psi(u_i, b_j)|}{|\Gamma(u_i)|}\right) + d,$$

- **exponential peer leadership value function**
  $$v^p_e(u_i, b_j|\Gamma(u_i)) = a \times e^{-b \left(\frac{|\Psi(u_i, b_j)|}{|\Gamma(u_i)|}\right)} + c,$$

where $a$, $b$, $c$, and $d$ are the coefficients in the functions which can be learnt from the historical data.

Given the real **peer leadership value function** of badges in the social network, $f(x)$, the optimal parameters can be learnt by minimizing the following objective function:

$$\hat{\omega} = \arg\min_{\omega} \int_0^1 |f(x) - v^p(x)| \, dx$$

where $\omega$ is the vector of coefficients (e.g., $\omega = [a, b]$ in the linear peer leadership value function) and $x = \frac{|\Psi(u_i, b_j)|}{|\Gamma(u_i)|} \in [0, 1]$. To resolve the function, we propose to learn the coefficients by fitting the 11 discrete points shown in Figure 1(b) and can get different estimated peer leadership value functions in Figures 5(a) - 5(d) respectively.

3.1.2 Peer Leadership Value Function Evaluation

**Experiment Settings**

The higher **peer leadership value** a badge has, the more likely a user will try to obtain it. To test the effectiveness of the above introduced peer leadership value functions, we conduct an experiments on the Foursquare badge system dataset introduced in Section 7?. In the experiment, badges achieved by less than 100 users are removed and the remaining badges achieved by users are organized in a sequence of (user, badge) pairs according to their achieving timestamps. These (user, badge) pairs are divided into two subsequences according to their relative timestamps: the training set and testing set, the proportion of whose sizes is $9 : 1$. In addition, a set of non-existing (user, badge) pairs which is of the same size as the positive test set are randomly sampled from the network as the negative test set, which together with the positive test set are used to form the final testing set. Pairs in the training set are regarded as the historical data, based on which we calculate the values of pairs in the testing set and output them as the confidence scores of these pairs.

The evaluation metrics applied in the experiment is AUC. In statistics, a receiver operating characteristic (ROC), or ROC curve, is a graphical plot that illustrates the performance of a binary classifier system as its discrimination threshold is varied. The curve is created by plotting the true positive rate (TPR) against the false positive rate (FPR) at various threshold settings. The area under
the ROC curve is usually quantified as the AUC score. When using normalized units, the area under the curve (i.e., AUC) is equal to the probability that a classifier will rank a randomly chosen positive instance higher than a randomly chosen negative one (assuming “positive” ranks higher than “negative”). Generally speaking, larger AUC score corresponds to better performance of the prediction model.

**Experiment Results**

We learn the coefficients of different value functions with the training set and apply the learnt function to calculate the peer leadership values of pairs in the testing set. The results are available in Figure 6. From the results, we observe that AUC achieved by the quadratic peer leadership function is 0.65, which is slightly better than other value functions, and the AUC scores obtained by the linear, cubic and exponential peer leadership functions are 0.58, 0.63, and 0.62 respectively. Here, quadratic function can outperform cubic and exponential functions because of the reason that cubic function may suffer from the overfitting problems a lot. Next, we will use the quadratic peer leadership function as the only peer leadership function, which will be compared with other value functions in Figure 7.

### 3.2 Network Trend Value Function

Besides the effects of personal interests and peer pressure, there exists some global trend about the network steering users badge achievement activities in the whole network. In online social network, users achieve badges in a sequential time order. For example, badges achieved by user $u_i$ can be organized into a sequential transaction $\langle b_1, b_2, \ldots, b_I \rangle$ according to the achieving timestamps, where $u_i$ got badge $b_i$ before $b_j$ if $p < q$. For all users in $\mathcal{U}$, we can represent the badge achievement sequential transactions as $\{ u_1 : \langle b_1, b_2, \ldots, b_I \rangle, u_2 : \langle b'_1, b'_2, \ldots, b'_I \rangle, \ldots, u_n : \langle b_n, b'_2, \ldots, b'_n \rangle \}$.

The network influence can be captured by extracting the frequent badge achieving sequential patterns from the transactions and many different pattern extraction methods have been proposed so far. In this paper, PrefixSpan proposed by Pei et al. [15] is applied. Consider, for example, we extract two frequent sequence patterns: pattern 1: $\langle b_1, b_2, \ldots, b_p \rangle$ and pattern 2: $\langle b_1, b_2, \ldots, b_p, b_h \rangle$ with supports $support(pattern \ 1)$ and $support(pattern \ 2)$ respectively from the network. Rule $r$ can be generated based on pattern 1 and pattern 2 representing that for users who have obtained badges in $\langle b_1, b_2, \ldots, b_p \rangle$ has a chance of $conf$ to get badge $b_h$:

$$r : \langle b_1, b_2, \ldots, b_p \rangle \rightarrow \langle b_h \rangle, \ \text{conf} = \frac{support(pattern \ 2)}{support(pattern \ 1)},$$

where $\langle b_1, b_2, \ldots, b_p \rangle$ is called the antecedent of rule $r$ (i.e., $\text{ant.}(r)$) and $\langle b_h \rangle$ is named as the consequent of $r$ (i.e., $\text{con.}(r)$). Score $\text{conf}(r) = \frac{support(pattern \ 2)}{support(pattern \ 1)}$ is called the confidence of rule $r$. Various rules together with their confidence scores can be generated based on the frequent sequence pattern mining results, which can be represented as set $\mathcal{R}$, based on which we can define the network trend value function as follow.

**Definition 8. (Network Trend Value Function):** For a given user $u_i$, who has achieved a sequence of badges $H = \langle b_1, b_2, \ldots, b_H \rangle$, already, the network trend value function of badge $b_j$ for $u_i$ is defined as the maximal confidence score of rules that can be applied to badges in $H$ and badge $b_j$, i.e.,

$$v^T(u_i, b_j | H) = \max \{ \text{conf}(r) | r \in \mathcal{R}, \text{ant.}(r) \subset H, \text{con.}(r) = b_j \}.$$  

We evaluate the effectiveness of the introduced network trend value of badges based on the same experiment setting introduced in Section 3.1.2. As shown in Figure 7, network trend value based badge predictor along can achieve an AUC score of 0.68 in inferring potential badge achievement activities.

### 3.3 Personal Interest Value Function

Users can have their personal interests, which can steer their social activities in online social networks. For example, sport enthusiasts may visit gyms and outdoor places frequently, while gourmets tend to go to good restaurants on the other hand. Users’ personal interests can be revealed from the badges obtained in the past. For example, for a given user $u_i$ who has already achieved the “Gym Rat” badges of levels from 1 to 4, it can show that $u_i$ can like doing sports a lot and “Gym Rat” of level 5 can meet his interest and can be of great value to him. Viewed in this way, the value of badges can be evaluated with the badges that users obtained in the past.

**Definition 9. (Personal Interest Value):** For a given user $u_i$ and the set of badges obtained by $u_i$ in the past, i.e., $H$, the personal interest value of badge $b_j$ for user $u_i$ is defined to be

$$v^P(u_i, b_j | H) = \sum_{b_k \in H} s(b_j, b_k) v^P(u_i, b_k),$$

where $s(b_j, b_k)$ denotes the similarity score between badge $b_j$ and $b_k$ and $v^P(u_i, b_k)$ represents the personal interest value of badge $b_k$ for user $u_i$.

For badge $b_k \in H$ that $u_i$ has obtained in the past, we define the personal interest value of $u_i$ to badge $b_j$ as 1.0 (i.e., $v^P(u_i, b_k) = 1.0$, for $\forall b_k \in H$). The similarity score between any two badges, e.g., $b_j$ and $b_k$, is defined as the Jaccard’s Coefficient score [14] of user sets who have achieved $b_j$ and $b_k$ (i.e., $\Gamma(b_j)$ and $\Gamma(b_k)$) respectively in the network:

$$s(b_j, b_k) = \frac{\left| \Gamma(b_j) \cap \Gamma(b_k) \right|}{\left| \Gamma(b_j) \cup \Gamma(b_k) \right|}.$$

Based on the above descriptions, the personal interest value of badge $b_j$ for user $u_i$ can be represented as

$$v^P(u_i, b_j | H) = \sum_{b_k \in H} \frac{\left| \Gamma(b_j) \cap \Gamma(b_k) \right|}{\left| \Gamma(b_j) \cup \Gamma(b_k) \right|}.$$

The effectiveness of the personal interest value of badge is evaluated with a similar experiment setting, whose result is available in Figure 7. We can observe that ranking badges according to their personal interest values for each user can achieve an AUC score of 0.66.

### 3.4 Comprehensive Value Function Definition and Evaluation

To capture the information from all the three aspects in calculating badge values, we define the comprehensive value function as a combination of the personal interest value, peer leadership value and network trend value functions:

$$v^C(u_i, b_j) = \alpha \cdot v^P(u_i, b_j) + \beta \cdot v^T(u_i, b_j) + (1 - \alpha - \beta)v^P(u_i, b_j),$$

where parameters $\alpha$, $\beta$ are assigned with value $\frac{1}{3}$ for simplicity in this paper.

To show the effectiveness of the above defined badge value functions in modeling users’ badge obtaining activities, we also compare their performance in inferring users’ badge achieving probabilities in the Foursquare badge system dataset. For the peer leadership value function, the quadratic function is used as it can achieve
the best performance in Figure 6. Experiment setting here is identical to that introduced in Section 3.1.2 and the result is available in Figure 7. From the result we observe that network trend value function performs better than personal interest and peer leadership value functions, which can achieve AUC scores about 0.68, 0.66, and 0.65 respectively. Meanwhile, the comprehensive value function that merge the isolated value functions together can improve the performance greatly and can obtain AUC score is 0.77, which is 13.2%, 16.7%, and 18.5% higher than the AUC scores achieved by personal interest, peer leadership and network trend value functions.

4. USER UTILITY FUNCTION

Value of badges is the reward that users can receive from the system. Meanwhile, to get the reward, they also need to afford certain costs introduced when finishing the required tasks. Generally, if the reward is greater than the cost, the badge will deserve the efforts. For example, if user $u$ get a reward for finishing the required tasks. Generally, if the reward is greater than the cost, the badge will deserve the efforts.

4.1 User Utility Function Definition

Definition 10. (Reward Function): The reward function of user $u_i$ in achieving badge $b_j$ is defined as

$$reward(u_i, b_j) = I(c_{i,j} \geq \theta_j)v^*(u_i, b_j).$$

If $u_i$ can obtain $b_j$, then the reward $u_i$ can achieve will be the comprehensive value of badge $b_j$ for $u_i$; otherwise, the reward will be 0.

Definition 11. (Cost Function): To achieve a certain badge, e.g., $b_j$, the cost that $u_i$ needs to pay is defined as the cumulative effort that $u_i$ invests on $b_j$:

$$cost(u_i, b_j) = \hat{e}_{i,j}.$$ 

The minimum efforts $\hat{e}_{i,j}$ required for user $u_i$ to get badge $b_j$ is determined by $u_i$'s ability in achieving $b_j$ as well as the badge threshold of $b_j$, which can be represented as

$$\hat{e}_{i,j} = \arg \min_{\hat{e}} (a_{i,j} \hat{e}_{i,j} \geq \theta_j) = \frac{\theta_j}{a_{i,j}}.$$ 

4.2 User Utility Function Evaluation

To demonstrate the effectiveness of the utility in modeling users' badge achieving activities, we conduct the experiments to show the performance of user utility function in inferring users badge achieving activities. Experiment settings here is identical to those introduced before but, to calculate the utilities of different badges for users, we need to know users' total cumulative efforts, ability distributions, and badge thresholds in advance.

Inference of Cumulative Effort: Active users in online social networks are assumed to have more cumulative efforts. In our dataset, the activeness measure can be defined as the number of badges users achieved. And the cumulative effort of user, e.g., $u_i$, can be obtained by normalizing the badge numbers to the range of $[0, 1]$ with equation $\frac{\#(u_i) - \#_{min}}{\#_{max} - \#_{min}}$, where $\#(u_i)$ is the number of badges achieved by $u_i$ and $\#_{max}$ and $\#_{min}$ are the maximal and minimal number of badges achieved by users in $U$ respectively.

Inference of User Ability Vector: In the training set, user $u_i$'s inferred ability vector is defined to be $a_i^{inf} = (a_{i,1}, a_{i,2}, \ldots, a_{i,m})$ of length $m = |B|$, where $a_{i,j}$ is the number of times that $u_i$ obtained badge of category $b_j$ in the training set. Each user is assumed to have the same amount of ability but can be distributed differently. Vector $a_i^{inf}$ is normalized by the total number of achieved badges to ensure $\|a_i^{inf}\|_1 = 1$. Considering that users can have
their hidden abilities, a random ability vector $a^{\text{random}}$ of length $m$ is generated whose cells contain random numbers in $[0, 1]$ and $a = a^{\text{initial}} + (1.0 - a) \cdot a^{\text{random}}$ is used as the final ability vector of user $u_i$. In this paper, we set parameter $\alpha = 0.85$.

**Inference of Badge Threshold:** Badges which are hard to achieve will be obtained later. For each badge $b_j \in B$, we get all the users who have achieved $b_j$ from the training set: $\{u'_1, u'_2, \ldots, u'_k\}$. For user $u'_{i} \in \{u'_1, u'_2, \ldots, u'_k\}$, we organize all the badges obtained by $u'_{i}$ from the training set in a sequence according to their achieving timestamps, the index of $b_j$ in $u'_{i}$’s achieved badge list is extracted to calculate $b_j$’s threshold. For example, if $u_i$ have achieved $p$ badges in all and the index of $b_j$ in the list is $q$, then the threshold of $b_j$ for $u_i$ is estimated as $\theta_{i,q} = \frac{q}{p}$. The threshold of badge $b_j$ is defined as the average of thresholds calculated for all these users: $\theta_j = \frac{\sum_{k=1}^{m} \theta_{i,k}}{m}$ where $\theta_j$ is a scaling parameter. Value $\theta_j$ is selected as large as possible but, at the same time, $\theta_j$ needs to ensure that for all users who have obtained badge $b_j$ in the training set (i.e., $u'_i \in \{u'_1, u'_2, \ldots, u'_k\}$). When $u'_{i}$ devotes all his cumulative effort to get $b_j$, $u'_i$’s contribution can obtain $b_j$ in our model and, in other words, his contribution can exceed $\theta_j$.

Based on the above inferred cumulative efforts, ability of users as well as badge thresholds, we show the results achieved by the user utility function in Figure 8 and also compare it with the comprehensive value function introduced before. From the results, we can observe that the introduced user utility function can perform very well in modeling users badge achieving activities. The AUC score achieved by the user utility function is 0.83, which is 7.8% larger than the AUC score achieved by comprehensive value function (i.e., 0.77). As a result, user utility function can provide a more comprehensive modeling about users’ badge achievement activities.

## 5. GAME AMONG USERS

In social networks, every user wants to maximize his/her utility in achieving badges and the value of different badges for certain user may depend on other users social activities. As a result, the badge achieving activities in online social networks can form a game among users. In traditional game theory, all the agents (e.g., users in social networks) are all assumed to be self-interested, which means that they have their own description about the states of world they like the most and they will act in an attempt to bring about these states of the world. “Self-interested” doesn’t necessarily mean that users tend to harm other users to maximize their payoff, as it can also include good things happening to other users as well. Meanwhile, what users can do in the game is to determine the distribution of their cumulative efforts, which is formally defined as the strategy as follows.

**Definition 13.** (Strategy): A user’s strategy refers to the options that he chooses in a setting where the outcome depends not only on his own actions but also on the actions of other users. A user’s strategy can determine the actions the user will take at any stage of the game.

In badge systems, users strategy can cover various aspects of their social activities but, in this paper, we refer to the strategy of users as the way how they distribute their cumulative efforts for simplicity. In game theory, strategy can be divided into two categories: (1) pure strategy, and (2) mixed strategy. The strategy which is to select one single action in the game is referred to as the pure strategy. In the given badge set $B$, a user $u_i$ can choose to get one badge only, e.g., $b_j \in B$, and devote all his/her efforts to obtaining that badge, the strategy of which is a pure strategy.

Meanwhile, let $\Pi(X)$ be the set of all possible distributions over set $X$. Then the set of mixed strategies for user $u_i$ is $\Pi(u_i) = \Pi(A_i)$, where $A_i$ is the set of all possible actions that $u_i$ can take. The set of all possible mixed strategy that $u_i$ can apply is represented as set $S_i$. For simplicity, we can just regard the cumulative effort distribution vector $\hat{e}_i = [\hat{e}_{i,1}, \hat{e}_{i,2}, \ldots, \hat{e}_{i,m}]$ as the action distribution $\Pi(A_i)$, i.e., user $u_i$’s strategy $s_i = \hat{e}_i$.

Given the set $U$, we can represent the strategies of all users in $U$ except $u_i$ as $s_{-i} = (s_1, s_2, \ldots, s_{i-1}, s_{i+1}, \ldots, s_n)$. Thus we can write the strategies of all users in $U$ as $s = (s_i, s_{-i})$, where $s_k = \hat{e}_k, k \in \{1, 2, \ldots, n\}$. Meanwhile, depending on users’ various mixed strategies, different kinds of social activities will be exerted in achieving badges, which can lead to different utilities.

**Definition 14.** (Strategy Utility Function): Given user $u_i$’s and other users’ strategies: $s_i$ and $s_{-i}$, the utility that $u_i$ can get based on $s_i$ and $s_{-i}$ can be represented as:

$$
    u(s_i, s_{-i}) = \text{utility}(u_i|s_i, s_{-i}) = \sum_{j=1}^{m} \text{utility}(u_i, b_j|s_i, s_{-i}).
$$

**Definition 15.** (Strategy Domination): Let $s_i$ and $s'_i$ be two mixed strategies of user $u_i$ and $s_{-i}$ be the strategies of all other users in $U$ except $u_i$. Then,

- **Strict Domination:** for $u_i, s_i$ strictly dominates $s'_i$ iff $u(s_i, s_{-i}) > u(s'_i, s_{-i})$ for all $s_{-i} \in S_{-i}$, where $S_{-i}$ represents the set of all potential strategies of other users except $u_i$;
- **Weak Domination:** for $u_i, s_i$ weakly dominates $s'_i$ iff $u(s_i, s_{-i}) \geq u(s'_i, s_{-i})$ for all $s_{-i} \in S_{-i}$ and $\exists s_{-i} \in S_{-i}$, such that $u(s_i, s_{-i}) > u(s'_i, s_{-i})$;
- **Very Weak Domination:** for $u_i, s_i$ very weakly dominates $s'_i$ iff $u(s_i, s_{-i}) \geq u(s'_i, s_{-i})$ for all $s_{-i} \in S_{-i}$.

**Definition 16.** (Dominant Strategy): Let $s_i$ be a mixed strategy of user $u_i$, $s_i$ is a (strictly, weakly, very weakly) dominant strategy iff $s_i$ can (strictly, weakly, very weakly) dominate $s'_i$ for $s'_i \in S_i, s'_i \neq s_i$, regardless of other users’ strategies (i.e., $s_{-i}$).

The optimal distribution of $u_i$’s cumulative efforts is identical to the dominant strategy of $u_i$, which can be obtained by solving the following maximization objective function:

$$
    \delta_i = \arg \max_{s_i} u(s_i, s_{-i}),
$$
where $\tilde{s}_i$ is the dominant strategy of $u_i$ and other users strategies $s_{-i} \not\in S_{-i}$ can take any potential value.

The above objective function is very hard to solve mathematically, as we may need to enumerate all potential strategies of all the users (including both $u_i$ and other users) in the network to obtain the global optimal strategy of $u_i$. Based on the assumption that all users are “self-interested”, in this paper, we propose to calculate the equilibrium state of all users strategy selection process instead as follows:

We let the users to decide their optimal strategies in a random order iteratively until convergence. At first, in the 1st round, we let users to decide their optimal strategies in a random order. For example, if we let $u_1$ be the first one to choose his “optimal strategy” when other users are not involved in the system (i.e., $s_{-1} = 0$), we can represent strategy selected by $u_i$’s as:

$$\tilde{s}_i = \arg\max_{s_i} u(s_i, 0).$$

Based on $u_i$’s “optimal strategy”, other users in $I - \{u_i\}$ (e.g., $u_j$) will take turns to decide their own “optimal” strategies by utilizing the selected strategies of other users. For example, let $u_j$ be the 2nd user to decide his/her strategy right after $u_i$. The “optimal strategy” of $u_j$ can be represented as

$$\tilde{s}_j = \arg\max_{s_j} u(s_j, \{\tilde{s}_i\} \cup 0).$$

And let $u_k$ be the last user to select the “optimal strategy” in the 1st round. Based on the known strategies selected by all the other users, the “optimal strategy” of $u_k$ can be represented as

$$\tilde{s}_k = \arg\max_{s_k} u(s_k, \{\tilde{s}_1, \tilde{s}_2, \cdots, \tilde{s}_{k-1}, \tilde{s}_{k+1}, \cdots, \tilde{s}_I\}).$$

After finishing the 1st round, we will start the 2nd round and all users will decide their strategies in a random order. Such a process will continue until all users’ “optimal strategies” selected in round $k$ is identical to those in round $k - 1$ (i.e., the stationary state), which will be outputted as the final optimal strategies of all users.

### 6. BADGE SYSTEM DESIGN

In addition to the game among users, there also exists a game between users and badge system designer. Users in online social networks want to maximize their utilities with as few efforts as possible. Meanwhile, badge system designer who decides the badge system mechanism aims at maximizing all users contributions to the network on the other hand. In this section, we will study how to determine the optimal badge system mechanism, and provide detailed simulation analysis about the designed badge system based on the model of user badge achievement activities learnt from the previous sections.

#### Table 3: Contributions of top 10 badges

| badge name     | total # | total contributions |
|----------------|---------|---------------------|
| Fresh Brew     | 7878    | 27.6                |
| Mall Rat       | 7028    | 26.2                |
| JetSetter      | 6468    | 24.5                |
| Hot Tamale     | 6355    | 23.2                |
| Great Outdoors | 5728    | 21.8                |
| Pizzaiolo      | 4746    | 17.8                |
| Swimmies       | 4361    | 16.4                |
| Bento          | 3774    | 13.7                |
| Zoetrope       | 3580    | 12.9                |
| Flame Broiled  | 3494    | 12.6                |

For simplicity, we define the amount of contribution attracted by a badge as the contribution of the badge as follows:

**Definition 17. (Badge Contribution):** For a given badge mechanism $M$, where the placed badge set is $B$, the contribution of badge $b_j \in B$ is defined as the total amount of contributions that users devoted to getting $b_j$. Based on the optimal strategy $\tilde{s}_i$ of user $u_i$ obtained from the game objective function proposed in the previous section, badge $b_j$’s contribution can be represented as

$$c(b_j | M) = \sum_{u_i \in U} a_{i,j} \tilde{s}_{i,j},$$

where $\tilde{s}_{i,j}$ is the optimal strategy of $u_i$ selected to get badge $b_j$.

Furthermore, for a given badge mechanism $M$, where the badge set is $B$, the contribution of badge set $B' \subseteq B$ selected in badge mechanism $M$ can be represented as

$$c(B' | M) = \sum_{b_j \in B'} \sum_{u_i \in U} a_{i,j} \tilde{s}_{i,j}.$$

Different badge system mechanisms can lead to different amounts of contributions from users and the optimal one that can attract the maximum contribution is defined as the dominant badge mechanism.

**Definition 18. (Dominant Badge Mechanism):** Given a badge mechanism $M$, in which the placed badge set is $B$, if $M$ can lead to more user contributions to the system than all the other badge mechanisms, then $M$ is defined as the dominant badge mechanism:

$$\hat{M} = \arg\max_{M} c(M) = \arg\max_{M} c(B | M).$$

**Badge Mechanism** can cover lots of different aspects, e.g., badge categories, the total number of badges, tasks required to get these badges, etc. In the following parts, we will analyze these aspects one by one.

**Definition 19. (Dominant Badge Category)** For the given badge mechanism $M$ (in which the badge set is $B$), the dominant badge category is defined as the badge category that can lead to the maximum contribution to the social network,

$$b_j = \arg\max_{b_j \in B} c(b_j | M).$$

According to the experiment settings introduced in Section 4, users decide their optimal strategies with methods proposed in the previous section. Based on users’ optimal strategies, the top 10 most badge categories that can lead to the maximum contribution are available in Table 3. In the table, we show the badge names, number of times that users have obtain certain kind of badges and
the contributions of each badge. Generally, popular badges (i.e., badges achieved by many users) can attract more contributions from users according to the results.

\textbf{Definition 20.} (Dominant Badge Category Set) For the given badge mechanism $\mathcal{M}$ and badge set $\mathcal{B}$, the \textit{dominant badge category set} of size $K\in\{1, 2, \cdots, 5, 10, 20, \cdots, 50, 100, 200, \cdots, 500]\}$ categories of badges from the network and calculate the contribution of these badges. The simulation results are given in Figure 9, where the total contribution of all these top 3 badges will increase as $K$ increases, but the speed of the growth will slow down when $K$ is large enough (e.g., $K \geq 100$).

To analyze the effects of badge numbers on the global contributions of badge system, we select the top $K$, $K\in\{1, 2, \cdots, 5, 10, 20, \cdots, 50, 100, 200, \cdots, 500\}$ categories of badges from the network and calculate the contribution of these badges. The simulation results are given in Figure 9, where the total contribution of all these top $K$ badges will increase as $K$ increases, but the speed of the growth will slow down when $K$ is large enough (e.g., $K \geq 100$).

Another key factor in badge system design is the badge thresholds and the optimal badge thresholds is formally defined as the dominant badge threshold as follows.

\textbf{Definition 21.} (Dominant Badge Threshold) For the given badge mechanism $\mathcal{M}$ and badge set $\mathcal{B}$, the \textit{dominant badge threshold} $\hat{\theta}$ is defined as

$$\hat{\theta} = \arg \max_{\theta} c(\mathcal{B}, \mathcal{M}, \theta).$$

We also study the effects of badge thresholds on the overall contributions of these badges to the network and the simulation analysis results are given in Figure 10. To simplify the experiment setting, we set the thresholds of all badges with the same value in $\{0.0, 0.1, \cdots, 0.9, 1.0\}$ and get the contributions obtained by the badges. As shown in Figure 10 the contribution of all these badges is 0 when the threshold is 0 and 1.0, where threshold 0 denotes that users can get badges without paying any efforts; threshold 1.0 means that users need to devote all their efforts on getting the badge corresponding to the area that all their ability lies in (i.e., ability in this area is 1.0). Contributions made to the network will increases fast as badge threshold increase at the beginning and can achieve the maximal contribution when threshold is 0.3 and 0.4 and then it will decreases.

7. RELATED WORK

Reward systems, e.g., badge system, have been widely employed in online social networks, like Foursquare [3][4]. Antin et. al. study the badges in online social networks from a psychological perspective and give some basic introduction of badges in Foursquare [3]. Large amount of badges are placed in Foursquare and a complete list of Foursquare badges is available [1]. To obtain badges in Foursquare, users need to reveal their locations by checking in at certain locations. Carburn et. al. study the problem between privacy preservation and badge achievement in Foursquare [4].

Users are all assumed to be “selfish” and want to maximize their payoff, which will form a game among users in online social networks to compete with each other. There has been a growing literature on analyzing the game among users in online social networks. Ghosh et. al. [10][7][9] provide a game-theoretic model within which to study the problem of incentivizing high quality user generated content, in which contributors are strategic and motivated by exposure. Jain et. al. [13] present a simple game-theoretic model of the ESP game and characterize the equilibrium behavior in their model. Their equilibrium analysis supports the fact that users appear to be coordinating on low effort words.

To achieve the maximal contribution to the sites, many works have been done on designing the badge system for online social networks. Jain et. al. [12] study the problem of incentive design for online question and answer sites. Anderson et. al. [2] study how badges can influence and steer users behavior on social networks, which can lead both to increased participation and to changes in the mix of activities a user pursues in the network. Ghosh et. al. [6] study the problem of implementing a mechanism which can lead to optimal outcomes in social computing based on a game-theoretic approach. Immorlica et. al. [11] study the badge system design whose goal is to maximize contributions. Easley et. al. [8] take a game-theoretic approach to badge design, analyzing the incentives created by badges and potential contributors as well as their contribution to the sites.

The \textit{badge system analysis and design} problem studied in this paper is a novel problem and different from existing works on reward system analysis: (1) “steering user behavior with badges” [2], which studies the incentives of badges in guiding users online activities without considering the effects of social connections among users; (2) “social status and the design of optimal badges” [11], which provides theoretical derivations of the optimal badge system design problem but fails to consider the game among users and the game between users and badge system designer; and (3) “implementing optimal outcomes in social computing: a game-theoretic approach” [8], which tries to use a game theory based method to analyze the motivations of users in getting badges but doesn’t consider the “badge system design” problem.

8. CONCLUSION

In this paper, we study the badge system analysis and design problem, which covers (1) badge system analysis and (2) badge system design problem. We introduce the three different categories of badges value functions for users in online social networks. To depict users’ payoff by achieving badges in online social networks, we formally define the utility function for users. We solve the “badge system analysis” problem as a game among users in social network and address the “badge system design” problem as a game between badge system designer and the users. Experiments conducted on real-world badge system dataset demonstrate that our model can capture users’ motivations in achieving badges online very well and design badge system mechanism that can lead to maximal contributions.
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