A MODEL FOR MAGNETICALLY COUPLED SYMPATHETIC ERUPTIONS

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ABSTRACT

Sympathetic eruptions on the Sun have been observed for several decades, but the mechanisms by which one eruption can trigger another remain poorly understood. We present a three-dimensional MHD simulation that suggests two possible magnetic trigger mechanisms for sympathetic eruptions. We consider a configuration that contains two coronal flux ropes located within a pseudo-streamer and one rope located next to it. A sequence of eruptions is initiated by triggering the eruption of the flux rope next to the streamer. The expansion of the rope leads to two consecutive reconnection events, each of which triggers the eruption of a flux rope by removing a sufficient amount of overlying flux. The simulation qualitatively reproduces important aspects of the global sympathetic event on 2010 August 1 and provides a scenario for the so-called twin filament eruptions. The suggested mechanisms are also applicable for sympathetic eruptions occurring in other magnetic configurations.

Key words: methods: numerical – Sun: corona – Sun: coronal mass ejections (CMEs) – Sun: filaments, prominences – Sun: flares – Sun: magnetic topology

Online-only material: animations, color figures

1. INTRODUCTION

Solar eruptions are observed as filament (or prominence) eruptions, flares, and coronal mass ejections (CMEs). It is now well established that these three phenomena are different observational manifestations of a single eruption, which is caused by the destabilization of a localized volume of the coronal magnetic field. The detailed mechanisms that trigger and drive eruptions are still under debate, and a large number of theoretical models have been developed (e.g., Forbes 2010).

Virtually all existing models consider single eruptions. The Sun, however, also produces sympathetic eruptions, which occur within a relatively short period of time—either in one, typically complex, active region (e.g., Liu et al. 2009) or in different source regions, which occasionally cover a full hemisphere (the so-called global eruptions; Zhukov & Veselovsky 2007). It has been debated whether the close temporal correlation between sympathetic eruptions is purely coincidental, or whether they are causally linked (e.g., Biesecker & Thompson 2000). Both statistical investigations (e.g., Moon et al. 2002; Wheatland & Craig 2006) and detailed case studies (e.g., Wang et al. 2001) indicate that physical connections between them exist.6

The exact nature of these connections has yet to be established. They have been attributed, for instance, to convective motions or destabilization by large-scale waves (e.g., Ramsey & Smith 1966; Bumba & Klvana 1993). At present, it seems most likely that the mechanisms by which one eruption can trigger another act in the corona and are of a magnetic nature. Perturbations traveling along field lines that connect source regions of eruptions (e.g., Ji et al. 2010) and changes in the background field due to reconnection (e.g., Ding et al. 2006; Zuccarello et al. 2009) have been considered. In an analysis of a global sympathetic event (see Section 2), Schrijver & Title (2011) found evidence for connections between all involved source regions via structural features like separators and quasi-separatrix layers (QLs; Priest & Forbes 1992; Démoûlin et al. 1996), suggesting the importance of the structural properties of the large-scale coronal field in the genesis of sympathetic eruptions.

A magnetic configuration that appears to be prone to producing sympathetic eruptions is a unipolar streamer or pseudo-streamer (PS; e.g., Hundhausen 1972; Wang et al. 2007). A PS is morphologically similar to a helmet streamer, but divides open fields of like polarity and contains an even number (typically two) of closed flux lobes below its cusp. PSs are quite common in the corona (e.g., Eselevich et al. 1999; Riley & Lührmann 2011) and occasionally harbor two filaments. It seems that if one of these erupts, the other one follows shortly thereafter (the so-called twin filament eruptions; Panasenco & Velli 2010).

Here, we present a numerical simulation that suggests two possible magnetic trigger mechanisms for sympathetic eruptions. It was inspired by the global sympathetic event on 2010 August 1, which involved a twin filament eruption in a PS.

2. THE SYMPATHETIC ERUPTIONS ON 2010 AUGUST 1

A detailed account of the individual eruptions that occurred in this global event can be found in Schrijver & Title (2011). Here we focus on a subset of three consecutive filament eruptions, all of which evolved into a separate CME. Figures 1(a), (b), and (c) show, respectively, the eruptions as seen by STEREO/EUVI (Howard et al. 2008), the pre-eruptive filaments, and a synoptic magnetogram obtained from the Solar and Heliospheric Observatory/Michelson Doppler Imager (SOHO/MDI; Scherrer et al. 1995) data. The large filaments 2 and 3 were located along the inversion lines dividing an elongated positive polarity and two bracketing negative polarities; the small filament 1 was located at the edge of the southern negative polarity. A potential field source surface extrapolation

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6 We do not distinguish here between sympathetic flares and sympathetic CMEs, since both are part of the same eruption process.
(PFSS; e.g., Schatten et al. 1969) for Carrington rotation 2099 reveals that filaments 2 and 3 were located in the lobes of a PS (Figure 1(d); see also Panasenco & Velli 2010).

Figure 1(e) shows a cut through the coronal distribution of the squashing factor \( Q \) (Titov et al. 2002) above filaments 2 and 3. The dark lines of high \( Q \) outline structural features and exhibit here a shape characteristic for a PS (compare with Figure 3(b) below). The photospheric distribution shows slog \( Q \) (Titov et al. 2011), depicting the footprints of (quasi-) separatrix surfaces. The structural skeleton of a PS consists of two separatrix surfaces, one vertical and one dome-like, which are both surrounded by a thin QSL (Masson et al. 2009) and intersect at a separator (Titov et al. 2011). It has been demonstrated that current sheet formation and reconnection occur preferably at such separators (e.g., Baum & Brantnaeh 1980; Lau & Finn 1990).

The presence of the PS above filaments 2 and 3 suggests that the CME associated with filament eruption 1 may have triggered the subsequent eruptions by destabilizing the PS, presumably by inducing reconnection at its separator. We now describe an MHD simulation that enabled us to test this scenario using an idealized model.

3. NUMERICAL SIMULATION

The basic simulation setup is as in Török et al. (2011), where two instances of the coronal flux rope model by Titov & Démoulin (1999, hereafter TD) were used to simulate the interaction of two flux ropes in a PS. Here we add a TD configuration on each side of the PS (Figure 2(a)). The new configuration on the left is used to model the CME associated with filament eruption 1, while the new one on the right is merely used to obtain a (line-)symmetric initial configuration, which facilitates the construction of a numerical equilibrium. It does not significantly participate in the dynamic evolution described below. The flux ropes FR1-3 are intended to model filaments 1–3.

We integrate the zero \( \beta \) compressible ideal MHD equations, neglecting thermal pressure and gravity. The equations are normalized by the initial TD torus axis apex height, \( R−d \) (see TD), the maximum initial magnetic field strength and Alfvén velocity, \( B_{0\text{max}} \) and \( v_{0\text{max}} \), and derived quantities. The Alfvén time is \( \tau_a = (R−d)/v_{0\text{max}} \). We use a nonuniform Cartesian grid of size \([-25, 25] \times [-25, 25] \times [0, 50]\) with resolution \( \approx 0.04 \) in the flux rope area. The initial density distribution is \( \rho_0(x) = |\mathbf{B}_0(x)|^{3/2} \), such that \( v_{0}(x) \) decreases slowly with distance from the flux concentrations. For further numerical details we refer to Török & Kliem (2003).

The model parameters are chosen such that all flux ropes are initially stable with respect to the helical kink (Török et al. 2004) and torus instabilities (TI; Kliem & Török 2006). The ropes are placed along the \( y \)-direction, at \( x = \pm 1.5\) and \( \pm 5.5 \), and have identical parameters \( (R = 2.75, a = 0.8, d = 1.75, L = 0.5, q = 4.64; \text{see TD}) \). The signs of the sub-photospheric point charges, \( \pm q \), are set according to the signs of the polarities surrounding filaments 1–3 (Figure 1(c)). The half-distance between the charges, \( L \), is such that the TI can be triggered by a relatively weak perturbation (Schrijver et al. 2008). To obtain a numerically stable initial configuration that contains (semi-)open field above the PS lobes, the two charges associated with each flux rope are adjusted to \(-0.55 q/0.65 q\) for FR1 and FR4 and to \(-0.34 q/0.24 q\) for FR2 and FR3. The twist is chosen to be left-handed for all ropes to account for the observed dextral chirality of filaments 2 and 3 (Panasenco & Velli 2010).

We first relax the system for 85 \( \tau_a \) and reset the time to zero. Then we trigger the eruption of FR1 by imposing localized converging flows at the bottom plane (as in Török et al. 2011), which slowly drive the polarities surrounding FR1 toward the local inversion line, yielding a quasi-static expansion of the rope’s ambient field. The flows are imposed for 25 \( \tau_a \) (including phases of linear increase (decrease) to a maximum velocity of 0.02 \( v_{0\text{max}} \) (to zero), each lasting 5 \( \tau_a \).
Though we solve the ideal MHD equations, extra diffusion is introduced by numerical differencing (as in every MHD code that models solar magnetic fields). This numerical diffusion is localized in regions where the current density is largest and leads to reconnection of magnetic field lines. Although it is much larger than the diffusion expected on the Sun, experience has shown that simulations produce solutions with physically expected behavior, as long as the numerical diffusion is sufficiently small. We therefore expect that our simulation indicates the true evolution of the system, but that the reconnection rates might differ from those present on the Sun.

4. RESULTS

Figures 2 and 3 summarize the main dynamics and reconnection occurring in the simulation. Figure 3(a) shows the initial configuration and Figures 2(a) and 3(b) show the system after relaxation, during which weak current layers form at the PS separatrices surfaces, but no noticeable reconnection occurs. Note the correspondence between the current layer pattern and the Q-distribution shown in Figure 1(e).

As the converging flows are applied, FR1 starts to rise slowly, in response to the quasi-static expansion of its ambient field. In contrast to other simulations, where such flows have been used to create a flux rope from a sheared arcade (e.g., Amari et al. 2000), here they do not lead to noticeable reconnection. The slow rise lasts until the rope reaches the critical height for TI onset at \( t \approx 40 \tau_a \), after which it rapidly accelerates upward driven by the instability (Török & Kliem 2007; Fan & Gibson 2007; Schrijver et al. 2008; Aulanier et al. 2010). FR1 attains a maximum velocity of \( \approx 0.45 v_{0\text{max}} \) at \( t \approx 90 \tau_a \) before it slowly decelerates. Figure 2(b) shows the system in the course of this eruption. The rise of the rope is slightly inclined, due to the asymmetry of its ambient field (e.g., Filipov et al. 2001). The rope rotates counterclockwise about its rise direction (as seen from above), due to the conversion of its twist into a writhe (e.g., Green et al. 2007).

The expansion of FR1’s ambient field compresses the field between FR1 and the PS, particularly at larger heights where it is weak (see online animations). As a result, a tilted arc-shaped current layer forms around the PS separator (Figures 3(c) and 4). Further compression by the eruption steepens the current densities until reconnection (R1) between the open flux to the left of the PS and the closed flux in the right PS lobe sets in. The lobe flux then starts to open up, while the open flux starts to close down above the left PS lobe (Figures 2(b) and 3(c)). This successively decreases (increases) the magnetic tension above FR2 (FR3), so that FR2 rises slowly, while FR3 is slowly pushed downward. At \( t \approx 95 \tau_a \), FR2 reaches the critical height for TI onset and erupts, attaining a maximum velocity of \( \approx 0.60 v_{0\text{max}} \) at \( t \approx 120 \tau_a \). Figure 2(c) shows that FR2 also rises non-radially, but rotates less than FR1. The apparently smaller rotation of FR2 is due to the faster decay of its overlying field with height, which leads to a distribution of the total rotation over a larger height range than for FR1 (Török et al. 2010). By the time shown, FR1 has fully erupted, an elongated vertical current layer has formed in its wake (Figure 3(d)), and reconnection therein has produced cusp-shaped field lines below it. As FR2 erupts, it rapidly pushes the arc-shaped current layer to large heights (Figure 3(d)). While R1 still commences for some time, it does not anymore play a significant role in the following evolution.

A vertical current layer also forms below FR2. The subsequent reconnection (R2) initially involves the very same flux systems that took part in R1. The flux previously closed down by R1 opens up again, and the flux previously opened up by R1—and by the expansion of FR2—closes down to form cusp-shaped field lines below the current layer (Figure 3(e)). After these fluxes are exhausted, R2 continues, now involving the left PS lobe and the open flux to the right of the PS. While the former opens up, the latter closes down as part of the growing cusp (Figure 3(f)). Thus, R2 continuously removes closed flux above FR3. As before, this progressive weakening of magnetic tension leads to a slow rise of the rope, followed by its erup-
Figure 3. Illustration of the two reconnection phases that trigger the successive flux rope eruptions in the pseudo-streamer. Field lines are colored the same as in Figure 2. The transparent inverted gray scale in the central plane, \( y = 0 \), shows the logarithmic distribution of \( |\mathbf{j}|/|\mathbf{B}| \), where \( \mathbf{j} \) is the electric current density, outlining flux rope currents and thin current layers. Fainter field line segments are located behind the transparent layer. Panel (a) shows the initial configuration, panel (b) the system after relaxation, and panels (c)–(f) show the dynamic evolution, at \( t = 85, 126, 142, \) and \( 158 \tau_a \), respectively. Panels (a) and (b) and (c)–(f) use a different scaling of \( |\mathbf{j}|/|\mathbf{B}| \), respectively. Panel (c) shows reconnection R1, which triggers the eruption of FR2, and panels (e) and (f) show reconnection R2, which triggers the eruption of FR3. Panel (d) shows a state between the two reconnection phases.

(An animation and a color version of this figure are available in the online journal.)

Figure 4. Volume rendering of \( |\mathbf{j}|/|\mathbf{B}| \) in the pseudo-streamer area at the same time as in Figures 2(b) and 3(c), outlining the tilted arc-shaped current layer that forms around the separator.

(A color version of this figure is available in the online journal.)

The eruptions of FR2 and FR3 are initiated by the removal of a sufficient amount of stabilizing flux above the flux ropes via reconnection. R1 is similar to quadrupolar “breakthrough” or “breakout” reconnection (Syrovatskii 1982; Antiochos et al. 1999). Here it is driven by a nearby CME rather than by an expanding arcade and, in contrast to the breakout model, a flux rope is present prior to eruption. R2, on the other hand, corresponds to standard flare reconnection in the wake of a CME. Here it removes flux from the adjacent PS lobe, thereby triggering the eruption of FR3. A similar mechanism for the initiation of a second eruption in a PS was suggested by Cheng et al. (2005), who, however, attributed it to reconnection inflows rather than to flux removal. We emphasize that R1 and R2 merely trigger the eruptions, which are driven by the TI and supported by the associated flare reconnection (e.g., Vršnak 2008). Thus, in the system studied here, both PS eruptions require the presence of a pre-eruptive flux rope. We further note that the reconnections do not have to commence for the whole time period until the TI sets in. It is sufficient if they remove enough flux for the subsequently slowly rising flux ropes to reach the critical height for TI onset.

R1 is driven by a perturbation of limited duration—the lateral expansion of a nearby CME—and is slow since it involves only weak fields, around a separator at a significant height in the corona. Therefore, its success in triggering an eruption depends on parameters like the distance of the CME from the PS and the amount of pre-eruptive flux within the PS lobes. Indeed, if we sufficiently increase these parameters in the simulation we find that R1 still commences, but does not last long enough to trigger an eruption. In contrast, R2 is driven by the rise of FR2 and involves strong fields. It is therefore faster and more efficient, which supports the finding by Panasenco & Velli (2010) that an eruption in one lobe of a PS is often followed by an eruption in the neighboring lobe.

Figure 2 shows that the simulation correctly reproduces the order of the eruptions shown in Figure 1(a) and yields a good match of their inclinations and rotations. Assuming that the first eruption indeed triggered the subsequent ones, it is surprising
that the filament located further away from it went off first. While filament 2 may simply have been closer to its stability limit than filament 3 (as indicated by its larger height; see Figure 1(a)), the simulation provides an alternative explanation: the perturbation of the separator yields an orientation of the current layer that leads to a removal of closed flux only in the right PS lobe (Figure 3(c)), thus enforcing the eruption of FR2. Hence, although we could not find observational signatures of R1 (presumably because the involved fields were too weak), the observed eruption sequence supports its occurrence. The time intervals between the simulated eruptions exhibit a ratio different to the observed ones. Matching the observed ratio requires a search for the appropriate model parameters and a more realistic modeling of reconnection, which are beyond the scope of this work.

FR2 reaches a velocity about 35% larger than that of FR1, which is in line with Liu (2007) and Fainshtein & Ivanov (2010), who found that CMEs associated with PSs are, on average, faster than those associated with helmet streamers. Liu (2007) suggested that this difference is due to the typically smaller amount of closed flux the former have to overcome. Indeed, FR1 has to pass through flux that is closed at all heights above it, while FR2 faces much less closed flux, a significant fraction of which is, moreover, removed by R1. FR3 remains significantly slower than FR2, most likely because it encounters more closed flux at eruption onset, and only partially opened flux later on (Figures 3(e) and (f)).

6. CONCLUSIONS

We present an MHD simulation of two successive flux rope eruptions in a PS, and we demonstrate how they can be triggered by a preceding nearby eruption. The simulation suggests a mechanism for twin filament eruptions and provides a scenario for a subset of the sympathetic eruptions on 2010 August 1. More realistic initial configurations and a more sophisticated treatment of reconnection are needed for a quantitative comparison with observations.

Our results support the conjecture that the trigger mechanisms of sympathetic eruptions can be related to the structural properties of the large-scale coronal field. However, while structural features are present in our model configuration, they do not connect the source region of the first eruption with the source regions of the subsequent ones. Moreover, the mere presence of such features in a source region is not a sufficient criterion for the occurrence of a sympathetic event, even if reconnection at structural features is triggered by a distant eruption. The conditions in the source region must be such that the resulting perturbation forces the region to cross the stability boundary.

The two trigger mechanisms presented here are independent and applicable also to other magnetic configurations. Triggering a sympathetic eruption by R1 requires the presence of a separator (or null point) above closed flux that stabilizes a pre-eruptive flux rope, which can be realized, in the simplest case, in a so-called fan-spine configuration (e.g., Antiochos 1998; Pariat et al. 2009; Török et al. 2009). Triggering a sympathetic eruption by R2 requires the presence of an adjacent closed flux system overlying a flux rope, which can exist, for example, in quadrupolar configurations.

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