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Evidence for the $B^0 \rightarrow p\bar{p}K^{*0}$ and $B^+ \rightarrow \eta_cK^{+}$ decays and study of the decay dynamics of $B$ meson decays into $p\bar{p}h$ final states

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I. INTRODUCTION

This paper reports measurements of the branching fractions of the baryonic three-body decays $B \rightarrow p \bar{p}h$ where $h = \pi^+,$ $K_S^0,$ $K^{0\ast},$ or $K^{+\ast}$ and their resonant substructures. This work is a continuation of our study of the $B^+ \rightarrow p \bar{p} K^{+\ast}$ decay reported in Ref. [1].

These channels are interesting for the dynamical information in the distribution of the three final-state particles and for the possible presence of exotic intermediate states, such as a pentaquark candidate $\Theta^+ (1540)$ in the $m_{pK_S^0}$ spectrum [3] or an $f_j (2220)$ glueball candidate in the $m_{p\bar{p}}$ spectrum [4].

The quark diagrams of the three-body baryonic $B$ decays are described in detail in Ref. [5]; only the dominant contributions are described below. In particular, the $B^+ \rightarrow p \bar{p} \pi^+$ decay proceeds mainly through external and internal $W$-emission “tree” processes, while in the decay $B^0 \rightarrow p \bar{p} K^{0\ast}$ a virtual loop “penguin” process $b \rightarrow sg$ is expected to be dominant. The $B^+ \rightarrow p \bar{p} K^{+\ast}$ decay receives contributions from both the penguin and the doubly Cabibbo-Kobayashi-Maskawa-suppressed external $W$-emission tree processes.

An important feature of $B \rightarrow p \bar{p}h$ decays is an enhancement at low $p \bar{p}$ masses reported in Ref. [2], similar to that seen in several other baryonic decays of $B$ mesons [6] and $J/\psi$ [7]. This enhancement might reflect short-range correlations between $p$ and $\bar{p}$ in a fragmentation chain [5,8]. Alternatively, it could be a feature of a quasi-two-body decay in which the $p \bar{p}$ system is produced through an intermediate resonance [4], in particular, the $X (1835)$ state recently observed by BES [9]. Rosner [10] proposed distinguishing between the two mechanisms by studying the distribution of events in the Dalitz plot. As in the case of the resonance, $p$ and $\bar{p}$ are produced independent from a hadron, then the distributions $m_{p\bar{p}}$ and $m_{p\bar{h}}$ should be identical.

Ten experimental groups reported narrow enhancements near 1.54 GeV/$c^2$ in the invariant-mass spectra for $nK^+$ and $pK^0$ [11]. The minimal quark content of a state that decays strongly to $nK^+$ is $ddua\bar{s}$; therefore, these mass peaks were interpreted as a possible pentaquark state, called $\Theta (1540)^{+}$. On the other hand, a number of experiments that observe strange baryons with mass similar to that of the $\Theta (1540)^{+}$ [e.g., $\Lambda (1520) \rightarrow p K^-$] see no evidence for the $\Theta (1540)^{+}$ [12,13]. As suggested in Ref. [3] we search for a pentaquark baryon candidate $\Theta^+$ in the $m_{pK_S^0}$ mass distribution of $B^0 \rightarrow p \bar{p} K^0$ decays.

A narrow state $f_j (2220)$ with a width of 23 MeV was reported in the $K\bar{K}$ spectrum by the MARK III experiment [14] and later seen in $K^+ K^-,$ $K^0\bar{K}^0,$ $\pi^+\pi^-,$ and $p \bar{p}$ by the BES [15] experiment. However, its nonobservation in quite a few $p \bar{p}$ annihilation modes, in particular, in $p \bar{p} \rightarrow f_j (2220) \rightarrow K\bar{K}$ [16], has led to doubts about its existence [17]. One theoretical conjecture [4] suggests a possible presence of the $f_j (2220)$ resonance in baryonic $B$ decays.

Direct $CP$ violation is observable as an asymmetry in yields between a decay and its $CP$ conjugate when at least two contributing amplitudes carry different weak and strong phases. Following the observation of the direct $CP$ violation in $B^0 \rightarrow K^+ \pi^-$ [18] transitions and its nonobservation in $B^+ \rightarrow K^+ \pi^- [19]$, it is interesting to study the charge asymmetry in the $B \rightarrow p \bar{p} h$ system. Three-body baryonic $B$ decays $p \bar{p} h$ occur through two different mechanisms (penguin and tree), which carry different weak phases and, in general, different strong phases. Although negligible direct $CP$ violation asymmetry is measured in the $B^0 \rightarrow p \bar{p} K^\ast$ mode [1,2], recent theoretical calculations predict a significant asymmetry in the $B^0 \rightarrow p \bar{p} K^+\pi^-$ mode [20].

We use events with the same final-state particles to isolate the decay $B^0 \rightarrow \Lambda^+_c \bar{p}, \Lambda^+_c \rightarrow p K^{0\ast}(0)$ and decays $B \rightarrow X_{c\bar{c}} h,$ for $X_{c\bar{c}} = \eta, J/\psi,$ with a subsequent decay to $p \bar{p}$. Charge-conjugate reactions are included implicitly throughout the paper.

In Sec. II, we describe the BABAR detector. In Secs. III, IV, and V, we discuss the reconstruction of the $B$-meson candidates, the branching fraction (BF) extraction, and the systematic uncertainties, respectively. In Sec. VI, we present our results on the $B \rightarrow p \bar{p} h,$ $B \rightarrow X_{c\bar{c}} h,$ and $B^0 \rightarrow \Lambda^+_c \bar{p}$ branching fraction measurements, charge-asymmetry measurements, and searches for $\Theta (1540)^{+}$ pentaquark and $f_j (2220)$ glueball states. We discuss the $B \rightarrow p \bar{p} h$ decay dynamics and summarize in Secs. VII and VIII, respectively.
II. BABAR DETECTOR AND DATA SAMPLE

This measurement is performed with a data sample of 232 \( \times 10^6 \) \( Y(4S) \rightarrow BB \) decays corresponding to an integrated luminosity of 210 fb\(^{-1}\), collected at the \( Y(4S) \) resonance (“on-resonance”) with the BABAR detector at the PEP-II \( e^+ e^- \) storage ring. An additional 21 fb\(^{-1}\) of data (“off-resonance”), collected about 40 MeV below the resonance, is used to study the backgrounds from light-quark and \( c\bar{c} \) production. The BABAR detector is described in detail elsewhere [21]. Charged-particle trajectories are measured by a five-layer silicon vertex tracker and a 40-layer drift chamber, both operating in a 1.5-T solenoidal magnetic field. A Cherenkov radiation detector is used for charged-particle identification. The CsI(Tl) electromagnetic calorimeter detects photon and electron showers. The BABAR detector Monte Carlo simulation based on GEANT4 [22] is used to optimize selection criteria and to determine selection efficiencies.

III. B MESON RECONSTRUCTION

The \( B^+ \) and \( B^0 \) decays are reconstructed in the following modes: \( B^+ \rightarrow p\bar{p} \pi^+ \), \( B^0 \rightarrow p\bar{p}K^{*0} \), \( B^0 \rightarrow p\bar{p}K_S^0 \), and \( B^+ \rightarrow p\bar{p}K^{*+} \). Charged tracks not coming from \( K_S^0 \) must originate from the interaction point, have transverse momentum greater than 0.1 GeV/c, and at least 12 drift chamber hits. Charged pions, kaons, and protons are identified by the average energy loss \( (dE/dx) \) in the tracking devices and by the pattern of Cherenkov photons in the Cherenkov radiation detector. The \( K_S^0 \rightarrow \pi^+ \pi^- \) candidates are required to have a two-pion invariant mass within 8 MeV/c\(^2\) of the nominal \( K_S^0 \) mass [12] and a cosine of the angle between the line connecting the \( B \) and \( K_S^0 \) decay vertices and \( K_S^0 \) momentum greater than 0.999 in the laboratory frame. \( K^{*+} \) candidates are reconstructed in the \( K^{*+} \rightarrow K_S^0 \pi^+ \) decay channel, and \( K^{*0} \) candidates are reconstructed in the \( K^{*0} \rightarrow K^+ \pi^- \) mode. Candidates whose mass is within 80 MeV/c\(^2\) of the nominal \( K^* \) mass [12] are selected as \( K^* \) candidates, and the ones with mass 160–240 MeV/c\(^2\) away from the \( K^* \) mass are chosen as the \( K^* \) sideband sample. The three daughters in the \( B \) decay are fit constraining their paths to a common vertex.

To suppress background, we impose a cut requiring a probability greater than 10\(^{-4}\) on the each of the \( K_S^0 \) and the \( B \) candidates’ vertices.

Two kinematic constraints of \( B \)-meson pair-production at the \( Y(4S) \) are used to characterize the \( B \) candidates: the beam-energy-substituted mass \( m_{ES} = [(E_{cm}^2/2 + p_0 \cdot p_B^2/E_0^2 - p_B^2)]^{1/2} \) and the energy difference \( \Delta E = E_B - E_{cm} \), where \( E_{cm} \) is the total center-of-mass energy, \( E_B \) is the center-of-mass energy of the \( B \) meson candidate (the asterisk denotes the center-of-mass frame throughout the paper), and \((E_0, p_0)\) is the four-momentum of the initial state, and \( p_B \) is the \( B \) momentum in the laboratory frame. For signal \( B \) decays the \( \Delta E \) distribution peaks near zero with a mode-dependent resolution of 11–17 MeV, while the \( m_{ES} \) distribution peaks near the \( B \) meson mass with a mode-dependent resolution of 2.5–3.0 MeV/c\(^2\), as determined in Monte Carlo simulation.

We select events with \( m_{ES} > 5.22 \text{ GeV}/c^2 \) (5.25 GeV/c\(^2\) for the \( B^+ \rightarrow p\bar{p} \pi^+ \) mode) and \( |\Delta E| < 0.10 \text{ GeV} \) (0.15 GeV for the \( B^0 \rightarrow p\bar{p}K_S^0 \) mode). We make these selections quite loose since these two variables are used in a maximum likelihood fit to extract the signal yield. Of the candidates passing that loose selection, only one candidate is chosen for each event, selecting the one with the highest \( B \) vertex probability, or, if a \( K_S^0 \) is present in the decay chain, the highest value of the product of the \( B \) and the \( K_S^0 \) vertex probabilities. To improve the resulting mass resolutions, after selecting the \( B \) candidates we perform a kinematic fit fixing the mass of each \( B \) candidate to its known value [12] and its energy to a half of the total center-of-mass energy.

The background is dominated by random combinations of tracks created in \( e^+ e^- \rightarrow q\bar{q} \) (where \( q \) is \( u, d, s, c \) quarks) continuum events. These events are collimated along the original quark directions and can be distinguished from more spherical \( B\bar{B} \) events. We construct a Fisher discriminant \( (F) \) [23] as a linear combination of the following four event-shape variables:

1. cos\( \theta_{\text{thr}} \), the cosine of the angle between the thrust axis of the reconstructed \( B \) and the beam axis;
2. cos\( \theta_{\text{mom}} \), the cosine of the angle between the momentum of the reconstructed \( B \) and the beam axis;
3. and 4. the zeroth and the second Legendre polynomial momentum moments, \( L_0 \) and \( L_2 \). They are defined as follows: \( L_0 = \sum_i |p_i^*| \) and \( L_2 = \sum_i |p_i^*||3\cos^2\theta_{\text{thr},i} - 1)/2 \), where \( p_i^* \) are the momenta of the tracks and neutral clusters not associated with the \( B \) candidate and \( \theta_{\text{thr},i} \) is the angle between \( p_i^* \) and the thrust axis of the \( B \) candidate.

The coefficients for the Fisher discriminant variables are determined for each of the modes separately by maximizing the separation between the means of the signal and background Fisher discriminant distributions obtained from the signal Monte Carlo samples and the off-resonance data events, respectively.

There is also a background for the three-body decays \( B \rightarrow p\bar{p}h \) from \( B \) mesons decaying into the same final states as the signal, such as \( B \rightarrow X_{c2}h \) decays, where \( X_{c2} = \eta_c, J/\psi, \psi', \chi_{c0}, \chi_{c1}, \chi_{c2} \) decaying to \( p\bar{p} \) and the \( B^0 \rightarrow X_{c1} \bar{p} \) decay. This background, which is of interest in its own right, is discussed in the next section. Other backgrounds from \( B \) decays are negligible.

IV. BRANCHING FRACTION EXTRACTION

We perform an unbinned extended maximum likelihood fit to extract the signal yields. The variables \( m_{ES}, \Delta E, \) and
$\mathcal{F}$ are used as discriminating variables to separate signal from background.

To estimate the contribution from $B$ decays that proceed through $b \to c$ transitions leading to the $p\bar{p}h$ final state, such as $\eta_c$, $J/\psi \to p\bar{p}$, and $\Lambda_c^+ \to pK_0^*/K^0$, the maximum likelihood fit is performed in three distinct regions:

1. The main “charmonium” region which includes the $\eta_c$ and $J/\psi$ resonances: $2.85 < m_{p\bar{p}} < 3.15$ GeV/$c^2$ (for $h = K^0/K^{\ast 0}/K^{\ast +}$).

2. The “charm” ($\Lambda_c^+$) region delimited by $|m_{p\bar{p}} - 2.3$ GeV/$c^2| < 0.1$ GeV/$c^2$ where $h = K_0^0/K^{\ast 0}$, and $|m_{p\bar{p}} - 3$ GeV/$c^2| > 0.15$ GeV/$c^2$ (this prevents overlap with the charmonium region). Note that for $h = K_0^0$ both $m_{p\bar{p}}$ and $m_{p\bar{p}}$ combinations are considered.

3. The “all-other” region. Significant background from slow pions in the $B^+ \to p\bar{p}\pi^+$ mode leads to a slight difference of the Fisher discriminant shape at low and high $m_{p\bar{p}}$. To reduce the sensitivity to that correlation we perform the fit for this mode in two regions: $m_{p\bar{p}} < 3.6$ GeV/$c^2$ and $m_{p\bar{p}} > 3.6$ GeV/$c^2$.

In the charmonium region, in addition to the three variables described above, the $m_{p\bar{p}}$ variable is used to distinguish between the nonresonant signal and contributions from $\eta_c$ and $J/\psi$. In the charm region the corresponding additional variable is $m_{p\bar{p}}$.

The data sample is assumed to consist of two components: signal events, including $B$ meson decays to $X_c h$ and $\Lambda_c^+ \bar{p}$, which have the same final-state particles as the signal, and combinatorial background events. The latter are due to random combinations of tracks from both continuum and $BB$ events. For the fit in the charmonium region, $\eta_c$ and $J/\psi$ signal-like components are included in the fit, a $\Lambda_c^+$ component corresponding to the overlap of charm and charmonium regions is not included here but its contribution is taken into account in Sec. VI.A. For the charm region, a $\Lambda_c^+$ component is included in the fit as both signal and background contributions. For the decay $B^+ \to p\bar{p}\pi^+$, an additional $B^+ \to p\bar{p}K^+$ component is considered, to account for the $B^+ \to p\bar{p}K^+$ events present in the fit region because of kaon/pion misidentification. The signal component is split into correctly reconstructed true events and misreconstructed events, so-called self-cross-feed (SCF). The SCF events are signal events in which one or more of the tracks from the signal side are lost and a track from the other $B$ decay is included in the reconstruction. The fraction of SCF events is determined with a $B \to p\bar{p}h$ Monte Carlo sample and varies from 0.5% for the $B^0 \to p\bar{p}K_0^0$ mode to 5.6% for the $B^+ \to p\bar{p}K^+$ mode. In the $B^0 \to p\bar{p}K_0^0$ mode, the SCF signal events are indistinguishable from the combinatorial background and no separate SCF signal component is used in the maximum likelihood fit.

In the maximum likelihood fit, each component is modeled by the product of probability density functions (PDFs) of the following variables, which are assumed to be uncorrelated for all components:

1. $m_{ES}, \Delta E, \mathcal{F}$, and $m_{p\bar{p}}$ in the charmonium region:

$$P_1 = P^x(m_{ES}, \Delta E, \mathcal{F}, m_{p\bar{p}})$$

2. $m_{ES}, \Delta E, \mathcal{F}$ and $m_{p\bar{p}}$ in the charm region:

$$P_2 = P^x(m_{ES}, \Delta E, \mathcal{F}, m_{p\bar{p}})$$

3. $m_{ES}, \Delta E, \mathcal{F}$ in the all-other region:

$$P_3 = P^x(m_{ES}, \Delta E, \mathcal{F})$$

where $x$ indicates the event source. In the all-other region there are two components: $x$ is either signal ($s$) or background ($b$). In the charmonium region there are four components $x = s, \eta_c, J/\psi$, and $b$; and in the charm region there are three components $x = s, \Lambda_c^+$, and $b$.

The likelihood is given by

$$L_r = e^{r N_r} \prod_{i=1}^{N_r} \sum_x N_{xr}^{i} P_r^x,$$
TABLE I. The PDF parametrization of $B \to p\bar{p}h$ signal, SCF, $\eta_c$, $J/\psi$, $\Lambda_c^+$, and combinatorial background contributions. We use the following notation: “BifGauss” for a Bifurcated Gaussian, “G” for a Gaussian ($2 \times$ G are two Gaussian distributions with common mean), “Voigtian” for a convolution of a Breit-Wigner distribution and a sum of Gaussian distributions with common mean, “ARGUS” for a threshold function [24], “norm” for normalization, and “ratio” is a ratio of the normalizations of a linear to a Gaussian contributions. The parameters floated for each of the functions are specified in the brackets.

| Component | $m_{ES}$ | $\Delta E$ | $J$ | $m_{pp}$ | $m_{ph}$ |
|-----------|---------|------------|-----|---------|---------|
| $B^0 \to p\bar{p}K^0$ | BifGauss (mean) | $G + G$ (narrow mean) | $G + G$ | Constant (norm) | Constant (norm) |
| $J/\psi$ | Same as signal | Same as signal | Same as signal | $2 \times G$ (narrow $\sigma$) | $2 \times G$ |
| $\eta_c$ | Same as signal | Same as signal | Same as signal | $2 \times$ Voigtian | $2 \times G$ |
| $\Lambda_c^+$ | Same as signal | Same as signal | Same as signal | $2 \times$ Voigtian | $2 \times G$ |
| Combinatorial | ARGUS (slope) | Linear (all) | $G + G$ (means) | Linear | linear + $2 \times G$ (ratio) |

| $B^+ \to p\bar{p}K^+$ | BifGauss (mean) | $G + G$ (narrow mean) | $G + G$ | Constant (norm) | $2 \times G$ (narrow $\sigma$) |
| $J/\psi$ | Same as signal | Same as signal | Same as signal | $2 \times G$ (narrow $\sigma$) | $2 \times$ Voigtian |
| $\eta_c$ | Same as signal | Same as signal | Same as signal | $2 \times$ Voigtian | $2 \times G$ |
| SCF | ARGUS | Linear | $G + G$ | Constant | $2 \times G$ |
| Combinatorial | ARGUS (slope) | Linear (all) | $G$ (all) | Linear | linear + $2 \times G$ (ratio) |

| $B^0 \to p\bar{p}K^0$ | BifGauss (mean) | $G + G$ (narrow mean) | $G + G$ | Constant (norm) | constant (norm) |
| $J/\psi$ | Same as signal | Same as signal | Same as signal | $2 \times G$ (narrow $\sigma$) | $2 \times$ Voigtian |
| $\eta_c$ | Same as signal | Same as signal | Same as signal | $2 \times$ Voigtian | $2 \times G$ |
| $\Lambda_c^+$ | Same as signal | Same as signal | Same as signal | $2 \times G$ |
| SCF | ARGUS + G | Quadratic | $G + G$ | Constant | $2 \times G$ |
| Combinatorial | ARGUS (slope) | Linear (all) | $G$ (all) | Linear | linear + $2 \times G$ (ratio) |

| $B^+ \to p\bar{p}\pi^+$ | BifGauss (mean) | $G + G$ (narrow mean) | $G + G$ | $G + G$ |
| SCF | ARGUS | Linear | $G + G$ | $G + G$ |
| $p\bar{p}K^+$ | ARGUS | Linear | $G + G$ | $G + G$ |
| $p\bar{p}K^+$ SCF | ARGUS | Linear | $G + G$ | $G + G$ |
| Combinatorial | ARGUS (slope) | Linear (all) | $G + G$ (all) | $G + G$ |

The $m_{ES}$, $\Delta E$, and $J$ PDFs for the $\eta_c$, $J/\psi$, and $\Lambda_c^+$ contributions are taken to be the same as the corresponding PDFs for the $B \to p\bar{p}h$ signal. The known masses of the $J/\psi$ and $\Lambda_c^+$ and the known mass and width of the $\eta_c$ are used in the fits. All the other parameters that are not floated are fixed to the values obtained from the corresponding Monte Carlo simulation.

All the parameters for the $B^+ \to p\bar{p}K^+$ background events in the $B^+ \to p\bar{p}\pi^+$ mode are fixed in the fit to the values obtained from the $B^+ \to p\bar{p}K^+$ Monte Carlo events reweighted as described above as well as the expected amount of the charmonium events with $p\bar{p}K^+$ final states.

For the combinatorial background events all the parameters fixed in the fit are obtained from the on-Y(4S) resonance data $m_{ES}$ (4eV/c^2).

The parametrization of the signal and combinatorial background PDFs does not vary with the fit region.

The remaining floating parameters of the PDFs are determined by a maximum likelihood fit to the data. The fit uses the kinematic variables described above but is independent of the location of the event in the Dalitz plot. This fit not only determines the various parameters of the PDFs, but also the number of signal and background events, and the covariance matrix for these event numbers.

Once the maximum likelihood fit provides the best estimate of the PDF parameters, we use a weighting technique [25] to measure the branching fraction and reconstruct efficiency-corrected mass distributions. This method allows us to take into account the dependence of the efficiency on the position of a candidate in the Dalitz plot. We assume that distributions in the $m_{ES}$, $\Delta E$, and $J$ are uncorrelated with the location in the Dalitz plot.

The event-dependent weight to be signal, $W_s(x)$ (also known as the $sWeight$ in the $sPlots$ method [25]), is computed from the PDFs:

$$W_s(x) = \frac{\sum_i V_i(s, x) P_{r_i}^{s, j}}{\sum_i N_i P_{r_i}^{s, j}},$$

where $P_{r_i}^{s, j}$ is the value of the PDF for the component $x$ ($x = \text{signal signal, background, charmonium-signal}$, etc.)

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charmonium-$\eta_c$, etc.) in the event $j$ for the fit region $r$ [as defined in Eqs. (1)–(3)], and $V_r(s, x)$ is the covariance between the number of signal events $N^s_r$ and the number of events for the component $x$, $N^x_r$, in the fit region $r$ defined by

$$V_r(s, x) = \frac{\partial^2 \ln L}{\partial N^s_r \partial N^x_r} = \sum_{j=1}^{N^s_r} \sum_{j=1}^{N^x_r} \frac{P^s_{r,j} P^x_{r,j}}{P^s_{r,j} + P^x_{r,j}}. \tag{6}$$

The sum of $\mathcal{W}_j^s$ over all events $j$ is just $N^s = N^s_0 + N^s_2 + N^s_3$, while the sum of $\mathcal{W}_j^x$ over all events in a small area in phase space gives, in the limit of high statistics, the correct distribution of the signal in that area while preserving the total signal yield. These weights ($\mathcal{W}_j^x$) allow optimal discrimination between signal-like and background-like events [25] and serve as a tool to reconstruct the resulting signal distributions.

The resulting branching fraction is then calculated as follows:

$$B = \sum_{j=1}^{N} \frac{\mathcal{W}_j^s}{N_{BB} \cdot e_j \cdot B_{sub}}, \tag{7}$$

where the sum is over all events $j$, $N_{BB}$ is the total number of $BB$ pairs, $B_{sub}$ is the product of the branching fractions in the subdecays, and $e_j$ is the reconstruction efficiency of the event $j$. The reconstruction efficiency depends on the position of the candidate on the Dalitz plane and is obtained from the corresponding signal Monte Carlo simulations. The statistical error on the branching fraction is given by

$$\frac{\Delta B}{B} = \sqrt{\sum_{j=1}^{N} \frac{(\mathcal{W}_j^s)^2}{e_j^2}}. \tag{8}$$

V. SYSTEMATIC ERRORS

The contributions to the systematic errors on the measured branching fractions and charge asymmetries are summarized in Tables II and III.

The $Y(4S)$ is assumed to decay equally to $B^0 \bar{B}^0$ and $B^+ B^-$ mesons. Incomplete knowledge of the luminosity and cross section leads to a 1.1% uncertainty in all branching fraction measurements. Charged-tracking, particle-identification (PID) and $K_S^0$ reconstruction studies of the data lead to small corrections applied to each track in these simulations. Limitations of statistics and purity in these data-Monte Carlo comparisons lead to residual systematic

| Error source | $p \bar{p} K^0$ | $p \bar{p} K^{*0}$ | $p \bar{p} K^{*+}$ | $\eta, K^0$ | $\eta, K^{*0}$ | $\eta, K^{*+}$ | $p \Lambda_c^+$ ($p K^0$) | $\bar{p} \Lambda_c^+$ ($p K^{*0}$) | \(\Theta^+\) |
|--------------|----------------|-----------------|-----------------|-------------|-------------|-------------|-----------------|-----------------|-------------|
| BB counting  | 1.1            | 1.1             | 1.1             | 1.1         | 1.1         | 1.1         | 1.1             | 1.1             | 1.1         |
| PID efficiency | 1.2         | 1.6             | 3.4             | 2.1         | 1.2         | 1.6         | 2.9             | 1.6             | 3.6         |
| Track reconstruction | 1.6 | 2.4             | 3.6             | 2.4         | 1.6         | 2.4         | 3.2             | 1.6             | 3.2         |
| $K_S^0$ reconstruction | 2.8 | 2.9             | 1.1             | 1.1         | 1.2         | 2.1         | 1.6             |                 |             |
| Monte Carlo statistics | 2.0 | -3.4/+/+4.4    | 2.5             | 2.6         | 0.3         | 1.3         | 0.8             | 1.2             | 1.0         |
| Dalitz plot binning | 2.1 | 3.5             | 1.4             | 2.0         |             |             |                 |                 |             |
| Preselection | 0.5            | 0.8             | 0.4             | 0.3         | 0.5         | 0.8         | 0.4             | 0.5             | 0.4         |
| Fit bias     | 5.0            | 3.0             | 3.6             | 1.1         | 3.4         | 3.4         | 1.5             | 20.0            | 11.0        |
| PDF parametrization | 3.0 | -3.7/+/+3.2    | -1.9/+/+2.2    | 6.2         | 1.1         | -3.3/+/+3.8 | 3.0             | 1.3             | 0.6         |
| Fit region   | 5.7            | 17.0            | 6.5             | 13.0        | 5.0         | 1.8         | 3.0             | 5.0             | 3.4         |
| $B$ background/BF | 1.0 | 0.8             | 2.9             | 0.8         |             |             |                 |                 |             |
| Nonresonant $K\pi$ | 15.4 | 25.2           |                 |             |             |             | -21.9/+/+22.7  | 15.5             | -42.7/+/+46.9 |
| Total (%)    | 9.5            | 24.4            | 27.1            | 15.2        | 6.7         | -22.8/+/+23.6 | 16.8            | 21.0            | -44.5/+/+48.6 |

Preselection correction | 0.976 | 0.967 | 0.968 | 0.983 | 0.976 | 0.967 | 0.968 | 0.969 | 0.968 | 0.976 |

| $K_S^0$ correction | 0.981 | 0.980 | 0.972 | 0.966 | 0.976 |         |         |         |         |         |

| Error | $p \bar{p} K^{*+}$ | $p \bar{p} K^0$ | $p \bar{p} \pi^+$ | $\eta, K^{*+}$ | $\eta, K^0$ | $J/\psi K^{*+}$ | $J/\psi K^{*0}$ |
|-------|-----------------|----------------|-----------------|-------------|-------------|-----------------|----------------|
| Track reconstruction | 0.002 | 0.004 | 0.002 | 0.002 | 0.004 | 0.002 | 0.004 |
| PID efficiency | 0.003 | 0.015 | 0.001 | 0.001 | 0.002 | 0.002 | 0.001 |
| Monte Carlo statistics | 0.012 | 0.057 | 0.021 | 0.017 | 0.004 | 0.002 | 0.016 |
| Fitting | 0.050 | 0.020 | 0.040 | 0.066 | 0.040 | 0.040 | 0.007 |
| Total | 0.05 | 0.05 | 0.05 | 0.07 | 0.04 | 0.04 | 0.02 |
uncertainties. Limitation of Monte Carlo statistics employed in each analysis contributes a small uncertainty. The effects of binning on the efficiency are estimated by studying the variation in the resulting signal yield due to changes in the chosen bin size.

A large control sample of $B \rightarrow J/\psi(e^+e^-\mu^+\mu^-)h$ is studied separately in data and Monte Carlo simulations to understand uncertainties arising from the choice of vertexing cuts and from the parametrization of the PDFs for $\Delta E, m_{\text{ES}}$, and $F$ (this uncertainty is labeled “Preselection” in Table II).

The uncertainty due to possible correlation between the fit variables is estimated by performing fits to a number of Monte Carlo experiments that consist of fully simulated signal events embedded in parametrized background simulations. This so-called “Fit bias” uncertainty in Table II is on the order of a few percent.

Where the Monte Carlo values are used to fix signal shape parameters in a fit, we obtain the uncertainty on the signal yield due to a change in each of the PDF parameters by doing a number of toy Monte Carlo experiments with parametrized signal and background distributions. In each a fit is performed with the original value of the PDF parameter and the value shifted by its uncertainty, which is obtained from the $B \rightarrow p\bar{p}h$ signal Monte Carlo simulation. The resulting uncertainties are added together in quadrature, taking into account the correlation between the PDF parameters, to obtain the total error for each PDF. The procedure is repeated using the correlation matrices between the variables to obtain the total error for each fit component, which is then added in quadrature to give the total error on PDF parametrization.

In a similar fashion, different fit ranges for charmonium and charm regions are employed and the resulting variation of the fit yields is taken as a systematic error.

The potential correlation of the fit variables with their location on the Dalitz plot would slightly violate the main principle of the sPlot method. To reduce the sensitivity to that correlation the fit is performed in one, two, and four $m_{p\bar{p}}$ regions for all the modes. The resulting variation of the branching fraction is taken as a systematic error. Note that we constrained the $B^+ \rightarrow p\bar{p}K^{*+}$ fit to make the signal component non-negative (in the charmonium region), which results in additional systematic error on the fit region. All the uncertainties above are summed in quadrature to give the “Fit region” error in Table II.

Branching fraction uncertainties [12] on $\mathcal{B}(B^+ \rightarrow Xh) \times \mathcal{B}(X \rightarrow p\bar{p})$, where $X = \chi_{c(0,1,2)}$, $\psi'$ and $h = K^0, K^*0$ or $K^{*+}$, and on the sub-branching fractions of $K^0$ and $K^*$, which affect the $B \rightarrow p\bar{p}h$ branching fraction measurements, are given in the “$B$ background/BF” line in Table II.

For modes that contain $K^*$ mesons, the nonresonant $K\pi$ background is obtained by performing a maximum likelihood fit and extracting the branching fraction in the $K^*$ sideband region. The nonresonant $K\pi$ contributions to the branching fraction values, based on the $K^*$ sideband data, for the $B^+ \rightarrow p\bar{p}K^{*+}$ and $B^0 \rightarrow p\bar{p}K^{*0}$ modes are $(0.34 \pm 0.74) \times 10^{-6}$ and $(0.23 \pm 0.30) \times 10^{-6}$, correspondingly. The $K^*$-sideband signal yields for $J/\psi K^{*0}$ and $J/\psi K^{*+}$ are $11.5^{+4.3}_{-3.5}$ and $1.2^{+1.7}_{-0.9}$ events; for $\eta K^{*0}$ and $\eta K^{*+}$ are $0 \pm 5.7$ and $1.8^{+2.9}_{-2.0}$ events; for the $B \rightarrow \Lambda_c^+ \bar{p}$ in the $B^0 \rightarrow p\bar{p}K^{*0}$ mode $4.5^{+2.7}_{-2.1}$ events. As no significant nonresonant $K\pi$ background is seen, we do not perform the sideband subtraction, but rather add these background contributions and their statistical uncertainties in quadrature to give the “Nonresonant $K\pi$” systematic uncertainties listed in Table II.

All the uncertainties described above are added in quadrature in the “Total” line in Table II. The final branching fraction value obtained from Eq. (7) is scaled by “Preselection” and “$K_0^*$” corrections.

VI. RESULTS

A. $B \rightarrow p\bar{p}h$ branching fraction measurements

The event yields from the maximum likelihood fit are presented in Table IV, while Fig. 1 shows projections of the corresponding three-dimensional PDFs on the $\Delta E$ and $m_{\text{ES}}$ axes. The measured branching fractions calculated from Eq. (7) (scaled by Preselection and $K_0^*$ corrections) are summarized in Table V, where the effective efficiency for

| Region | Charmonium | Charm | All-other | Total |
|--------|------------|-------|-----------|-------|
| Component | $B^0 \rightarrow p\bar{p}K_0^*$ mode | $B^0 \rightarrow p\bar{p}K_0^*$ mode |
| Signal | $17^{+9}_{-8}$ | $3^{+4}_{-3}$ | $70^{+12}_{-11}$ | $90^{+16}_{-14}$ |
| $\eta_c$ | $23^{+8}_{-7}$ | $53^{+8}_{-7}$ |
| $J/\psi$ | $6.8^{+3.6}_{-2.8}$ |
| $\Lambda_c^+$ | $1152 \pm 34$ | $1096 \pm 33$ |
| Background | $766 \pm 28$ |
| $B^0 \rightarrow p\bar{p}K^{*+}$ mode |
| Signal | $0 \pm 9$ | $52^{+11}_{-10}$ | $52 \pm 14$ |
| $\eta_c$ | $12.3^{+3.4}_{-3.6}$ | $12.3^{+3.4}_{-3.6}$ |
| $J/\psi$ | $34 \pm 6$ | $34 \pm 6$ |
| Background | $2207 \pm 47$ | $1971 \pm 45$ |
| $B^0 \rightarrow p\bar{p}K^0$ mode |
| Signal | $8^{+10}_{-8}$ | $4^{+6}_{-4}$ | $50^{+15}_{-15}$ | $63^{+18}_{-16}$ |
| $\eta_c$ | $37^{+10}_{-10}$ | $37^{+10}_{-10}$ |
| $J/\psi$ | $106 \pm 11$ |
| $\Lambda_c^+$ | $12.3^{+4.9}_{-4.8}$ | $12.3^{+4.9}_{-4.8}$ |
| Background | $2207 \pm 47$ |
| $B^0 \rightarrow p\bar{p}\pi^+$ mode |
| Signal | $185 \pm 28$ | $185 \pm 28$ |
| $p\bar{p}K^*$ | $157 \pm 30$ | $157 \pm 30$ |
| Background | $90438 \pm 30590438 \pm 305$ |
FIG. 1 (color online). Distributions (points with error bars) of $\Delta E$ and $m_{ES}$ for data candidates in all-observer region passing loose selection in the $B^0 \rightarrow p\bar{p}K^0$ (a)–(b), $B^+ \rightarrow p\bar{p}K^{*+}$ (c)–(d), $B^0 \rightarrow p\bar{p}K^{*0}$ (e)–(f), $B^+ \rightarrow p\bar{p}\pi^+$ (g)–(h) modes. The superimposed solid curves represent the projections on the three-dimensional-fit PDFs on the respective axis, and the dashed line is the fitted signal contribution. Because these are projections of multiparameter fits, the statistical significance of signal cannot be added directly and is generally greater than it appears in the figure. Note that the excess of events on the left of the signal peak in (g) corresponds to the $B^+ \rightarrow p\bar{p}K^+$ final states, where $K^+$ is misidentified as $\pi^+$. The following loose selection is applied: (a) $m_{ES} > 5.275$ GeV/$c^2$ and $\mathcal{F} > 0.2$; (b) $|\Delta E| < 0.02$ GeV/$c^2$ and $\mathcal{F} > 0.2$; (c) $m_{ES} > 5.275$ GeV/$c^2$ and $\mathcal{F} > 0.2$; (d) $|\Delta E| < 0.02$ GeV/$c^2$ and $\mathcal{F} > 0.2$; (e) $m_{ES} > 5.275$ GeV/$c^2$ and $\mathcal{F} > 0.6$; (f) $|\Delta E| < 0.015$ GeV/$c^2$ and $\mathcal{F} > 0.6$; (g) $m_{ES} > 5.275$ GeV/$c^2$ and $\mathcal{F} > 1.5$; (h) $|\Delta E| < 0.015$ GeV/$c^2$ and $\mathcal{F} > 1.5$.

The remaining unknown background comes from the $B \rightarrow \chi_{c0}\phi \pi$ events. It is possible to estimate the $B^0 \rightarrow \chi_{c0}K^0$ branching fraction using the corresponding $B^+ \rightarrow \chi_{c0}K^+$ branching fraction measurement. Because of isospin symmetry one would expect ratios of the charged and neutral B mesons decaying into $\chi_{c0}$ and $\chi_{c1}$ to be equal. Thus we estimate [12]: $\mathcal{B}(B^0 \rightarrow \chi_{c0}K^0) \approx \mathcal{B}(B^+ \rightarrow \chi_{c0}K^+) \approx \mathcal{B}(B^0 \rightarrow \chi_{c0}K^0) / 2 \approx (1.6^{+0.5}_{-0.3}) \times 10^{-4} \times 0.12 \pm 0.04) \times 10^{-3}$. This number needs to be multiplied by the $\mathcal{B}(\chi_{c0} \rightarrow p\bar{p}) = (0.22 \pm 0.03) \times 10^{-3}$ and results in the expected contributions to the branching fraction from this

the modes observed is calculated accounting for the correct event distribution in the Dalitz plot.

Our fitting method removes all $B \rightarrow \eta, J/\psi h$ and $B \rightarrow J/\psi h$ (except in the $B^+ \rightarrow p\bar{p}\pi^+$ mode) contributions and most of the $B^0 \rightarrow \Lambda_c^+\bar{p}$ contributions. There is still some remaining $B^0 \rightarrow \Lambda_c^+\bar{p}$ background contribution from the $B^0 \rightarrow \Lambda_c^+\bar{p}$ events in the charmonium region. Knowing the relative efficiencies of $B^0 \rightarrow \Lambda_c^+\bar{p}$ Monte Carlo events inside and outside the charmonium region allows us to calculate the remaining $B^0 \rightarrow \Lambda_c^+\bar{p}$ background contribution to be $(0.04 \pm 0.02) \times 10^{-6}$ and $(0.06 \pm 0.03) \times 10^{-6}$ for the $B^0 \rightarrow p\bar{p}K^0$ and the $B^0 \rightarrow p\bar{p}K^{*0}$ modes, respectively.

TABLE V. Summary of the noncharm, noncharmonium $B \rightarrow p\bar{p}h$ branching fraction calculation including $B$ background subtraction. Note that effective efficiency includes the subdecay branching fractions as well as the correct event distribution in the Dalitz plot.

|                | $p\bar{p}K^0$ | $p\bar{p}K^{*+}$ | $p\bar{p}K^{*0}$ | $p\bar{p}\pi^+$ |
|----------------|---------------|-------------------|-------------------|-----------------|
| Sum of signal weights | 181 ± 29      | 52 ± 14           | 63 ± 17           | 185 ± 28        |
| Effective efficiency, % | 24.5          | 4.1               | 16.0              | 44.6            |
| BF from Eq. (7) (10^{-6}) | 3.17 ± 0.53   | 5.45 ± 1.49       | 1.70 ± 0.45       | 1.79 ± 0.29     |
| $B$ background BF (10^{-6}) | 0.22 ± 0.03   | 0.17 ± 0.04       | 0.23 ± 0.05       | 0.10 ± 0.01     |
| Final BF (10^{-6}) | 3.0 ± 0.5 ± 0.3 | 5.3 ± 1.5 ± 1.3   | 1.47 ± 0.45 ± 0.40 | 1.69 ± 0.29 ± 0.26 |
mode of $(0.026 \pm 0.009) \times 10^{-6}$. The resulting contribution to the absolute systematic error on the $B$ background is $0.009 \times 10^{-6}$. The contribution from the $B \to \chi_{c0}h$ events is ignored for other modes [26].

From Ref. [12] we estimate the contribution of $B^+ \to J/\psi \pi^+$ to the $B^+ \to p \bar{p} \pi^+$ mode and the remaining charmonium contributions ($B \to \chi_{c1}h$ and $B \to \psi(2S)h$) for all the other modes. Since only an upper limit exists for the branching fraction of the $B \to \chi_{c0}h$ mode, it is not subtracted but taken as a one sided contribution to the systematic uncertainty. The total expected $B$ background contribution is quoted in the line “$B$ background BF.”

The line “Final BF” in Table V summarizes the values of the charmless and charmoniumless $B \to p \bar{p}h$ branching fractions after $B$ background subtraction.

We report the first evidence for the $B^0 \to p \bar{p}K^{*0}$ decay with a significance of $3.2 \sigma$ (including systematic uncertainties). The statistical significance $\sigma$ throughout the paper is taken as $\sqrt{-2 \ln \left( \frac{\mathcal{L}(0)}{\mathcal{L}_{\text{max}}} \right)}$, where $\mathcal{L}(0)$ is the likelihood of the fit assuming zero signal events and $\mathcal{L}_{\text{max}}$ is the likelihood obtained in the full fit. For the $B^0 \to p \bar{p}K^{*0}$ decay the $\mathcal{L}(0)$ is taken to be at zero signal events, but at the expected number of the $B$ background events as discussed above. To obtain the total significance in the $B^0 \to p \bar{p}K^{*0}$ mode the significances in each of the three regions are added in quadrature. To obtain the value of significance including the systematic uncertainties the likelihood function is smeared with a Gaussian distribution which has a width of the corresponding systematic uncertainty.

The measurements of branching fractions for the $B \to p \bar{p}h$ modes from Ref. [2] and this work are summarized in Table VI and compared to those of the two-body mesonic modes from Refs. [12,27,28].

The branching fraction is approximately two times smaller for the $B^+ \to p \bar{p}K^{*+}$ mode, when compared to the Belle measurement [2], bringing it below that of the $B^+ \to p \bar{p}K^+$ mode and more in line with theoretical predictions [5]. However, the two experiments are in agreement within their errors.

Since the virtual loop penguin process $b \to s g$ preserves isospin we would naively expect the ratio of the rates for $B^+ \to p \bar{p}K^+$ and $B^0 \to p \bar{p}K^0$ to be unity as it is in two-body mesonic modes $B \to J/\psi h$ and $B \to \rho^0 h$, but it is closer to two (see Table VI). This could be explained by absence of the external W-emission Feynman tree diagram for the neutral $B$ mode. However, if this tree diagram were important, we would expect a much larger rate for $B^+ \to p \bar{p}\pi^+$ than for $B^+ \to p \bar{p}K^+$, in contradiction with the data. The $B^+ \to p \bar{p}K^{*+}$ branching fraction is also larger (by a factor of three) than that of $B^0 \to p \bar{p}K^{*0}$ similar to the pattern suggested by the data for decays to $\rho^0 K^+$ and $\pi^0 K^*$. The $B \to p \bar{p}K^*$ modes are consistently smaller than the $B \to p \bar{p}K$ modes in both the charged and neutral cases. This seems to be the case for the $B \to J/\psi h$ modes as well, but not for the $B \to \rho^0 h$ modes. The $B^+ \to p \bar{p}\pi^+$

### Table VI

Summary of the experimental values for the branching fractions $(\times 10^{-6})$ of $B \to p \bar{p}h$ and their comparison to two-body mesonic modes. The values for the two-body mesonic modes are taken from Ref. [12] unless otherwise noted. The values in **bold** are those presented in the current work.

| $h$     | **Belle** $B \to p \bar{p}h$ [2] | **BABAR** $B \to p \bar{p}h$ | $B \to \rho^0 h$ | $B \to \pi^0 h$ |
|---------|---------------------------------|-------------------------------|------------------|------------------|
| $K^+$   | $6.0 \pm 0.3 \pm 0.4$          | $6.7 \pm 0.5 \pm 0.4$ [1]     | $12.1 \pm 0.8$   | $5.0_{-0.8}^{+0.9}$ |
| $K^0$   | $2.40_{-0.44}^{+0.64} \pm 0.28$| $3.0 \pm 0.5 \pm 0.3$         | $11.5 \pm 1.0$   | $5.4_{-1.0}^{+0.9}$ |
| $K^{*+}$| $10.3^{+3.6}_{-5.0}+1.3$       | $5.3 \pm 1.5 \pm 1.3$         | $6.9 \pm 2.4$    | $11.0 \pm 4.0$ |
| $K^{*0}$| $<7.6, 90\%$ C.L.             | $1.47 \pm 0.45 \pm 0.40$      | $<3.5, 90\%$ C.L.| $5.6 \pm 1.6$ [28] |
| $\pi^+$ | $1.68_{-0.17}^{+0.19} \pm 0.12$| $1.69 \pm 0.29 \pm 0.26$      | $5.5 \pm 0.6$    | $8.7 \pm 1.1$ |

### Table VII

Summary of the resulting branching fractions for the $\eta_c$ and $J/\psi$ modes (the order of the uncertainties is as follows: statistical, systematic, due to partial branching fraction correction where appropriate). The following values of branching fractions are used $\mathcal{B}(\eta_c \to p \bar{p}) = (1.3 \pm 0.4) \times 10^{-3}$ and $\mathcal{B}(J/\psi \to p \bar{p}) = (2.12 \pm 0.10) \times 10^{-3}$ [12].

| $p \bar{p}X$ | Efficiency | $\mathcal{B}(B \to \eta_c(p \bar{p})X)(10^{-6})$ | $\mathcal{B}(B \to \eta_c X)(10^{-3})$ |
|------------|------------|-----------------------------------------------|---------------------------------|
| Mode       | %          | Measured                                      | Measured                       |
| $p \bar{p}K^0$ | 36.3       | $0.83_{-0.26}^{+0.28} \pm 0.05$               | $0.64_{-0.20}^{+0.22} \pm 0.04_{-0.13}^{+0.28}$ | $1.2 \pm 0.4$ |
| $p \bar{p}K^{*0}$ | 23.7       | $1.03_{-0.30}^{+0.27} \pm 0.17$               | $0.80_{-0.13}^{+0.21} \pm 0.35_{-0.32}^{+0.19}$ | $1.6 \pm 0.7$ |
| $p \bar{p}K^{*+}$ | 15.7       | $1.57_{-0.46}^{+0.56} \pm 0.45$               | $1.21_{-0.35}^{+0.43} \pm 0.34_{-0.28}^{+0.54}$ | $\ldots$ |

| Mode       | Efficiency | $\mathcal{B}(B \to J/\psi(p \bar{p})X)(10^{-6})$ | $\mathcal{B}(B \to J/\psi X)(10^{-3})$ |
|------------|------------|-----------------------------------------------|---------------------------------|
| $p \bar{p}K^0$ | 37.1       | $1.87_{-0.28}^{+0.26} \pm 0.07$               | $0.88_{-0.13}^{+0.14} \pm 0.03 \pm 0.04$ | $0.85 \pm 0.04$ |
| $p \bar{p}K^{*0}$ | 25.0       | $2.82_{-0.38}^{+0.30} \pm 0.36$               | $1.33_{-0.28}^{+0.30} \pm 0.28_{-0.13}^{+0.14}$ | $1.31 \pm 0.07$ |
| $p \bar{p}K^{*+}$ | 17.8       | $3.78_{-0.64}^{+0.72} \pm 0.28$               | $1.78_{-0.30}^{+0.34} \pm 0.09_{-0.08}^{+0.13}$ | $1.35 \pm 0.10$ |
branching fraction is lower than that of the \( B^+ \to p\bar{p}K^+ \) mode as expected because the \( b \to u \) transition at tree level is suppressed compared to the \( b \to s \) penguin. This is similar to what is observed in the \( B \to \pi^0h \) modes but contrary to what is observed in \( B \to \rho^0h \).

Overall, the theoretical calculations of the baryonic \( B \) decays are not very certain and the current measurements of the branching fractions of all four \( B \to p\bar{p}K \) modes are a further challenge to our understanding.

### B. \( B \to (J/\psi, \eta_c)h \) branching fraction measurements

Using the \( \eta_c \) and \( J/\psi \) yields from Table IV we obtain the branching fractions shown in Table VII. The values obtained are consistent with current world averages [12]. We also report the first evidence for the \( B^+ \to \eta_cK^{*-} \) decay, with a significance of 3.2\( \sigma \) (including systematic uncertainties). A sample of the maximum likelihood fit result for the charmonium region is shown in Fig. 2.

### C. \( B^0 \to \Lambda_c^+ \bar{p} \) branching fraction measurement

From the \( B^0 \to \Lambda_c^+ \bar{p} \) fit yields in the \( B^0 \to p\bar{p}K_0^0 \) and \( B^+ \to p\bar{p}K^{*-} \) modes given in Table IV we obtain the branching fractions shown in Table VIII. Averaging results for both modes and adding the errors in quadrature (except the systematic error on \( B \)-counting), we obtain the branching fraction 

\[
\mathcal{B}(B^0 \to \Lambda_c^+ \bar{p}) = (21.0^{+5.6}_{-6.2}(\text{stat})^{+6.7}_{-4.4}(\text{syst})^{+2.6}_{-1.3}(\text{BF})^{+2.4}_{-3.9}(B(\Lambda_c^+ \to pK\pi)) \times 10^{-6}
\]

This measurement is consistent with the current value of 

\[
\mathcal{B}(B^0 \to \Lambda_c^+ \bar{p}) = (21.9^{+5.6}_{-4.9} \pm 3.2 \pm 5.7) \times 10^{-6}
\]

based on a single measurement by Belle [29].

### D. \( B \to p\bar{p}h \) charge-asymmetry measurements

The CP-violating charge asymmetry is defined as \( A_{ch} = (N_p - N_{\bar{p}})/(N_p + N_{\bar{p}}) \), where \( N_p \) and \( N_{\bar{p}} \) are the event yields in each of the categories of interest. The event yields are obtained from the maximum likelihood fit described in the Sec. IV, by integrating over the resulting signal event weights for each of the two charge categories separately. The resulting yields for all the modes (except \( B^0 \to p\bar{p}K^0 \), which does not have information on the flavor of \( B \) meson) are summarized in Table IX. The measurements for the current modes are consistent with zero within less than three standard deviations.

### E. \( B(B^0 \to \Theta(1540)^+ \bar{p}) \) upper limit calculation

As suggested in Ref. [3], we search for a pentaquark baryon candidate, \( \Theta^+ \), in the \( m_{pK_0^0} \) mass distribution of \( B^0 \to p\bar{p}K^0 \) decays. If \( \Theta^+ \) decays strongly, there are only two possible decay modes: \( nK^+ \) and \( pK^0 \). For this measurement we assume \( \mathcal{B}(\Theta \to pK_0^0) = 25\% \). From dedicated signal Monte Carlo we determine that the \( \Theta^+ \) invariant-mass resolution is represented by a sum of two Gaussian functions with a common mean. The resolution of the main (secondary) Gaussian is 0.95(2.32) MeV/c^2 and the wider Gaussian contributes 19% of the total. The overall resolution, defined as the full width at half maximum of the resolution function divided by 2.4, is 1 MeV/c^2 at the \( \Theta^+ \) mass of 1.54 GeV/c^2. The \( \Theta^+ \) pentaquark signal efficiency is 30.8 ± 0.1%. No events are observed in the \( \Theta^+ \) region of \( 1.52 < m_{pK_0^0} < 1.55 \) GeV/c^2 (see Ref. [30] for details). A Bayesian approach is used to calculate the upper limit of \( 0.20 \times 10^{-6} \) at 90% confidence level, assuming Poisson-distributed events in the absence of background, including a multiplicative systematic error of 7.1%. This value is consistent with and improves on the upper limit from the Belle Collaboration \( \mathcal{B}(B^0 \to \Theta(1540)^+ \bar{p}) < 0.92 \times 10^{-6} \) [2].

### Table VIII. Summary of the resulting branching fractions for \( B^0 \to \Lambda_c^+ \bar{p} \) [the order of the uncertainties is as follows: statistical, systematic, the uncertainty in the ratio of the \( \mathcal{B}(\Lambda_c^+ \to pK^0/\mathcal{B}(\Lambda_c^+ \to pK\pi) \)[12] and the uncertainty in the \( \mathcal{B}(\Lambda_c^+ \to pK\pi) \) value [12]]. Note that efficiency does not include the subdecay branching fractions.

| \( \Lambda_c^+ \) decay | Efficiency, % | \( \mathcal{B}(\Lambda_c^+ \to pX)(10^{-3}) \)[12] | \( \mathcal{B}(B^0 \to \Lambda_c^+ \bar{p})(10^{-6}) \) | Statistical significance |
|-------------------------|--------------|---------------------------------|---------------------------------|-------------------------|
| pK^0 | 25.4 | 23 ± 6 | 15.1^{+8.0}_{-4.3}^{+1.4+5.3}_{-1.2-3.2} | 3.4 |
| pK^0 | 19.7 | 16 ± 5 | 26.9^{+10.7+13.0+4.0}_{-9.0-12.0-3.1-5.5} | 4.3 |
TABLE IX. Summary of the asymmetry study: event yields for each of the categories of interest and the charge asymmetry. We observe no statistically significant CP asymmetries.

| Events type | $N_{\beta}$       | $N_{\bar{\beta}}$ | $A_{ch}$   |
|-------------|-------------------|--------------------|------------|
| **Signal**  | 35 ± 6            | 28 ± 5             | 0.11 ± 0.13 ± 0.06 |
| $\eta_c$    | 23 ± 5            | 13 ± 4             | 0.28 ± 0.16 ± 0.04 |
| $J/\psi$    | 63 ± 8            | 43 ± 7             | 0.19 ± 0.10 ± 0.02 |
| **Background** | 15 050 ± 123 | 15 443 ± 125 | −0.013 ± 0.006 |

**$B^0 \rightarrow p \bar{p} K^{*0}$ mode**

| Events type | $N_{\beta}$       | $N_{\bar{\beta}}$ | $A_{ch}$   |
|-------------|-------------------|--------------------|------------|
| **Signal**  | 34 ± 6            | 18 ± 4             | 0.32 ± 0.13 ± 0.05 |
| $\eta_c$    | 7 ± 3             | 5 ± 2              | 0.20 ± 0.28 ± 0.07 |
| $J/\psi$    | 18 ± 4            | 16 ± 4             | 0.07 ± 0.17 ± 0.02 |
| **Background** | 5453 ± 74 | 5377 ± 73 | 0.007 ± 0.010 |

**$B^+ \rightarrow p \bar{p} \pi^+$ mode**

| Events type | $N_{\beta}$       | $N_{\bar{\beta}}$ | $A_{ch}$   |
|-------------|-------------------|--------------------|------------|
| **Signal**  | 97 ± 10           | 89 ± 9             | 0.04 ± 0.07 ± 0.04 |
| **Background** | 45 434 ± 213 | 44 968 ± 212 | 0.005 ± 0.003 |

FIG. 3. Dalitz plots for signal in the (a) $B^0 \rightarrow p \bar{p} K^{*0}$, (b) $B^+ \rightarrow p \bar{p} \pi^+$, (c) $B^0 \rightarrow p \bar{p} K^{*0}$, and (d) $B^+ \rightarrow p \bar{p} K^{*+}$ modes obtained using the weighting technique described in Ref. [25]. The positions of the following resonances are shown: $\eta_c$ in solid, $J/\psi$ in dashed, and $\Lambda_c$ in dot-dashed lines. Note, that because of fluctuations and uncertainties, the signal rate in many bins is negative. The white areas correspond to regions with no entries.
F. Search for glueball $f_{J}(2220)$ in $B \rightarrow p\bar{p}h$ decays

We search for the narrow state $f_{J}(2220)$ by scanning through the $2.2 < m_{p\bar{p}} < 2.4$ GeV/$c^2$ region with a 30 MeV/$c^2$ mass window in the final states $p\bar{p}K^0$ and $p\bar{p}K^*$. This procedure is described in detail in Ref. [25]. The largest upper limits at 90% confidence level, obtained using the weighting technique described in Ref. [25]. The expected positions of the following resonances are shown:

VII. STUDY OF THE $B \rightarrow p\bar{p}h$ DECAY DYNAMICS

For decay dynamics studies, the maximum likelihood fit is performed using three variables ($m_{ES}$, $\Delta E$, and the Fisher discriminant) simultaneously over the whole Dalitz plot, with the exception of the $p\bar{p}\pi^+$ mode where we perform the fit in two regions: $m_{p\bar{p}} < 3.6$ GeV/$c^2$ and $m_{p\bar{p}} > 3.6$ GeV/$c^2$.

The resulting background-subtracted efficiency-corrected Dalitz plots for all the modes are shown in Fig. 3. The main features of the Dalitz plots are expected to be the charmonium resonances (with $J/\psi \rightarrow p\bar{p}$ and $\eta_c \rightarrow p\bar{p}$ bands most prominent), potential $\Lambda_c^+$ bands in $B^0 \rightarrow p\bar{p}K^0$ and $B^0 \rightarrow p\bar{p}K^{*0}$ modes, as well as the low $p\bar{p}$ mass enhancements. Figure 4 shows the corresponding background Dalitz distributions. The combinatorial background events favor the edges of the Dalitz plot, as they are dominated by the inclusion of random low-momentum tracks.

Background-subtracted efficiency-corrected $m_{p\bar{p}}$ distributions are shown in Fig. 5 and are summarized in Table X. Although the $m_{p\bar{p}}$ enhancement at low mass is quite prominent in the $B^0 \rightarrow p\bar{p}K^0$ and $B^+ \rightarrow p\bar{p}\pi^+$ modes, in the case of the $B^0 \rightarrow p\bar{p}K^{*0}$ and $B^+ \rightarrow p\bar{p}K^{*+}$ modes the statistics are too limited to draw a definite conclusion.

[Graphs and figures are not provided in the text.]

FIG. 4. Dalitz plots for background in the (a) $B^0 \rightarrow p\bar{p}K^0$, (b) $B^+ \rightarrow p\bar{p}\pi^+$, (c) $B^0 \rightarrow p\bar{p}K^{*0}$, and (d) $B^+ \rightarrow p\bar{p}K^{*+}$ modes obtained using the weighting technique described in Ref. [25]. The expected positions of the following resonances are shown: $\eta_c$ in solid, $J/\psi$ in dashed, and $\Lambda_c$ in dot-dashed lines. The white areas correspond to regions with no entries.
The histograms correspond to the relevant three-body phase-space signal Monte Carlo distributions. The dashed line shows zero. The bin size is varying and is specified in Table X. Note that the contribution from the $B$ decays to charmonium is removed.

TABLE X. Summary of efficiency-corrected, background-subtracted number of events in $m_{pp}$ bins for $B^0 \to p\bar{p}K^0$, $B^+ \to p\bar{p}\pi^+$, $B^0 \to p\bar{p}K^{*0}$ and $B^+ \to p\bar{p}K^{*+}$. Note that contributions from the $B$ decays to charmonium are removed.

| $m_{pp}$ range (GeV/c²) | $B^0 \to p\bar{p}K^0$ | $B^+ \to p\bar{p}\pi^+$ | $B^0 \to p\bar{p}K^{*0}$ | $B^+ \to p\bar{p}K^{*+}$ |
|---|---|---|---|---|
| 1.876–2.100 | 160 ± 50 ± 14 | 96 ± 30 ± 9 | 30 ± 37 ± 17 | 280 ± 109 ± 39 |
| 2.100–2.350 | 151 ± 50 ± 13 | 74 ± 25 ± 9 | 7 ± 34 ± 16 | 53 ± 90 ± 22 |
| 2.350–2.600 | 80 ± 40 ± 7 | 64 ± 24 ± 5 | 3 ± 26 ± 5 | 213 ± 95 ± 18 |
| 2.600–2.850 | 60 ± 31 ± 6 | 83 ± 27 ± 8 | 30 ± 26 ± 12 | 189 ± 86 ± 22 |
| 2.850–3.150 | 48 ± 23 ± 8 | 22 ± 21 ± 3 | 32 ± 38 ± 5 | 0 ± 39 ± 37 |
| 3.150–3.400 | −2 ± 13 ± 5 | 37 ± 18 ± 3 | 32 ± 21 ± 6 | 112 ± 66 ± 33 |
| 3.400–3.600 | 3 ± 22 ± 8 | −1 ± 11 ± 1 | 64 ± 27 ± 8 | 129 ± 75 ± 14 |
| 3.600–3.900 | 13 ± 27 ± 5 | 35 ± 19 ± 9 | 47 ± 31 ± 7 | 84 ± 80 ± 17 |
| 3.900–4.150 | 41 ± 25 ± 10 | 11 ± 9 ± 1 | 58 ± 30 ± 12 | 30 ± 65 ± 9 |
| 4.150–4.387 | 24 ± 25 ± 9 | −2 ± 7 ± 1 | 49 ± 30 ± 5 | 105 ± 88 ± 17 |
| 4.387–4.580 | 49 ± 29 ± 10 | −11 ± 4 ± 3 | −1 ± 6 ± 1 | 0 ± 11 ± 3 |
| 4.580–4.782 | 25 ± 34 ± 6 | 0 ± 12 ± 17 | Not applicable | Not applicable |
| 4.782–5.139 | Not applicable | 12 ± 18 ± 19 | Not applicable | Not applicable |
Note that the shapes of the enhancement in $B^{0} \to p\bar{p}K^{0}$ and $B^{+} \to p\bar{p}\pi^{+}$ [1] are similar within the statistics of the measurements, in agreement with the theoretical predictions [5].

To shed light on the nature of this enhancement [10], its uniformity on the Dalitz plot has been tested. The Dalitz plot is divided along the diagonal $m_{ph} = m_{\bar{p}h}$ line and each of the two halves is projected onto the nearer axis. If the Dalitz plot is symmetric we expect the number of events in both projections to be the same. The corresponding background-subtracted efficiency-corrected distributions for the signal events in all the modes are shown in Fig. 6. No asymmetry is expected to be introduced from variations in $m_{\bar{p}h}$, which is charge symmetric and slowly varying with $m_{ph}$.

In the case of $B^{0} \to p\bar{p}K^{0}$, there is no information on the flavor of the $B$ meson and thus this study cannot be performed. For the $B^{+} \to p\bar{p}K^{+}$ mode there seems to be no difference between the two halves within the available statistics. In the $B^{0} \to p\bar{p}K^{*0}$ mode there might be a marginal excess at low $m_{ph}$, which could be caused by the presence of the standard baryon resonances (such as $\Lambda_{c}^{+}$), while in the $B^{+} \to p\bar{p}\pi^{+}$ mode there is a marginal excess of events at high $m_{ph}$ around 3.8 GeV/c² in the $m_{\bar{p}h}$ half of the Dalitz plot, contrary to the result observed in the $B^{+} \to p\bar{p}K^{+}$ mode [1]. No quantitative theoretical description of this correlation is available at present.

Although the asymmetry in the low $m_{\bar{p}h}$ band shown in [1] disfavors the possibility of the low mass $p\bar{p}$ enhancement originating only from the presence of a resonance below threshold (such as the baryonium candidate at 1835 MeV/c² recently seen by BES [9]) the low statistics of the current modes do not allow one to derive a definite conclusion.

VIII. CONCLUSIONS

In summary, with 210 fb⁻¹ of data, we report evidence for the $B^{0} \to p\bar{p}K^{*0}$ decay with a branching fraction $(1.47 \pm 0.45(stat) \pm 0.40(syst)) \times 10^{-6}$, and provide improved measurements of branching fractions of the other $B \to p\bar{p}h$ modes, where $h = \pi^{+}, K^{0},$ and $K^{*+}$. One key observation is that the pattern of decays for $B \to p\bar{p}h$...
differs from that found for $B \rightarrow \pi^0 h$ and $B \rightarrow p^0 h$. We also identify decays of the type $B \rightarrow X_c \ell^+ h \rightarrow p \bar{p} h$, where $h = K_S^0, K^0$, and $K^{*+}$, and $X_c = \eta_c$ and $J/\psi$. In particular, we report evidence for the $B^+ \rightarrow \eta_c K^{*+}$ decay with the branching fraction of $B(B^+ \rightarrow \eta_c K^{*+}) \times B(\eta_c \rightarrow p\bar{p}) = (1.57^{+0.56}_{-0.46} \text{stat})^{+0.46}_{-0.36} \text{syst}) \times 10^{-6}$. We confirm the earlier observation of the $B^0 \rightarrow \Lambda_c^+ \rho$ decay \cite{29} and report measurements of the charge asymmetry consistent with zero in the $B^+ \rightarrow p\bar{p} \pi^+$, $B^0 \rightarrow p\bar{p} K^0$, and $B^+ \rightarrow p\bar{p} K^{*+}$ modes. No evidence is found for the pentaquark candidate $\Theta^+$ in the mass range 1.52 to 1.55 GeV/c$^2$, decaying into $p K_0^0$, or the glueball candidate $f_4(2220)$ in the mass range $2.2 < m_{p\bar{p}} < 2.4$ GeV/c$^2$, and branching fraction limits are established at the 10$^{-7}$ level.

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$-0.86 \pm 0.70$ events in the $\chi_{c0}$ region for each of the modes shown in Table \textbf{V} respectively.

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