Testing axial and electromagnetic nucleon form factors in
time-like regions in the processes $\bar{p} + n \rightarrow \pi^- + \ell^- + \ell^+$ and
$\bar{p} + p \rightarrow \pi^0 + \ell^- + \ell^+$, $\ell = e, \mu$

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(Dated: March 26, 2022)

Abstract

In frame of a phenomenological approach based on Compton-like Feynman amplitudes, we study the annihilation channel in antiproton nucleon collisions with production of a single charged or neutral pion and a lepton-antilepton pair. These reactions allow to access nucleon and axial electromagnetic form factors in time-like region and offer a unique possibility to study the kinematical region below two nucleon threshold. The differential cross section in an experimental set-up where the pion is fully detected is given with explicit dependence on the relevant nucleon form factors. The possibility to measure heavy charged pion in the annihilation channel is also discussed.

PACS numbers:
I. INTRODUCTION

In this paper we study the annihilation reaction $\bar{p} + n \rightarrow \pi^- + \ell^- + \ell^+$ and $\bar{p} + p \rightarrow \pi^0 + \ell^- + \ell^+$, $\ell = e, \mu$ which is the crossed process of pion electroproduction on a nucleon $N$: $e^- + N \rightarrow e^- + N + \pi$. It contains the same information on the nucleon from factors in a different kinematical region. This process is also related to the pion scattering process $\pi^+ + N \rightarrow N + \ell^- + \ell^+$ which was first studied in [1]. In this work it was already pointed out that the $\bar{p} + p$ annihilation process with pion production, under study here, renders possible the determination of the nucleon electromagnetic form factors in the unphysical region, which is otherwise unreachable in the annihilation reaction $\bar{p} + p \rightarrow e^+ + e^-$. In [2] a general expression for the cross section was derived and numerical estimations were given in the kinematical region near threshold. In this paper we extend the formalism in two directions. We take into account a larger set of diagrams which can contribute and give special emphasis to the possibility to access the axial nucleon form factors in the time-like region. For the annihilation process $\bar{p}N \rightarrow \ell^+ + \ell^- + \pi^{0,-}$, with $\ell = e$, or $\mu$, we will consider two reactions:

$$\bar{p}(p_1) + p(p_2) \rightarrow \pi^0(q_\pi) + \ell^+(p_+) + \ell^-(p_-), \quad (1)$$

and

$$\bar{p}(p_1) + n(p_2) \rightarrow \pi^-(q_\pi) + \ell^+(p_+) + \ell^-(-p_-), \quad (2)$$

where the notations of the particle four momenta are indicated in brackets. The interest of these processes lies in the possibility to access nucleon and axial form factors (FFs) in the time-like region. The expected values of the total cross sections at energies of a few GeV drop with the lepton pair invariant mass $q^2$, but are of the order of several nb and up to mb below threshold. Therefore these reactions are especially interesting as they will be measurable in next future at hadron colliders (or the crossed reactions at lepton colliders). The present work aims to evaluate the differential cross section for experimental conditions achievable at the future FAIR facility [3].

A. Electromagnetic (Vector) Form Factor

The structure of proton and nucleon is of great interest since it explores the quantum field theory of strong interaction, quantum chromodynamics (QCD), in a region where
the interaction between the constituents of quarks and gluons can not be treated as a perturbation. Its properties have been explored in many observables. For example, the electromagnetic form factors of proton and nucleon are measured in elastic electron-nucleon scattering with a space-like four momentum transfer $q^2 < 0$ via the process $e + p \rightarrow e + p$. For a momentum transfer of $-1 \text{ GeV}^2 < q^2 < 0 \text{ GeV}^2$, the electromagnetic form factors are well known for both neutron and proton.

The interest in the form factors of the nucleon for the region of $q^2 < -1 \text{ GeV}^2$ has recently been renewed by a measurement of the ratio of electric form factor over the magnetic form factor $\mu_p G_E/ G_M$ at TJNAF in a $q^2$-range up to $-5.8 \text{ GeV}^2$. The method of polarization transfer was employed for the first time at high values of $q^2$ using a longitudinally polarized electron beam and measuring the polarization of the recoil proton. The experiments gave the surprising new result that the ratio $\mu_p G_E/ G_M$ decreases from unity substantially for high $q^2$-values exhibiting eventually even a zero-crossing around $q^2 \approx -8 \text{ GeV}^2$. This new result is in contradiction with all data obtained from a Rosenbluth separation fit of unpolarized measurements giving a ratio of $\mu_p G_E/ G_M \approx 1$. The present understanding of this discrepancy is that the analysis of the unpolarized data lacks important corrections stemming from neglected higher order radiative corrections or electromagnetic processes like two-photon-exchange.

The situation of the experimental determination of the electromagnetic form factors in the time-like domain (i.e. $q^2 > 0$) is quite different. Existing data have explored the two basic processes: $e^- + e^+ \rightarrow p + \bar{p}$ and $p + \bar{p} \rightarrow e^- + e^+$. The precision of the cross section data in the time-like region is much lower and a determination of the individual electric and magnetic form factors has not been done with sufficient precision.

For both processes there is a threshold in $q^2$ for producing the two nucleons at rest or annihilation of the two nucleons at rest which amounts to $q^2 > (m_p + m_{\bar{p}})^2 = 4m_p^2$. In the region of $0 < q^2 < 4m_p^2$ (sometimes called the “unphysical region”) there are no data available. On the other hand this $q^2$-interval is of great interest since the intermediate virtual photon as well as the $\bar{p}p$-pair can couple to vector meson- and $\bar{p}p$-resonances respectively and thereby enhance the form factors substantially. This mechanism has been used to explain the large cross section in the time-like region above the threshold $q^2 > 4m_p^2$. Another possibility to explain this large cross section above threshold has been used recently by showing, that the large cross section in the annihilation process $\bar{p} + p \rightarrow e^+ + e^-$ can be
related to the $\bar{p}p$ scattering length [13].

The work presented here is focused on a possibility of extracting the electromagnetic form factors of the nucleon in the “unphysical region” and above using the process $\bar{p} + p \rightarrow \pi + e^+ + e^-$, as it has been proposed earlier [1, 2]. The measurement of the cross section of this reaction will be accessible at the future FAIR facility at GSI.

**B. Axial Form Factor**

In addition, we explore here also the new idea of accessing the axial vector current of the nucleon. The axial form factors in the space-like region are measured in nuclear $\beta$-decay, in neutrino scattering, in muon capture and in pion-electroproduction ($e + p \rightarrow e + n + \pi^+$). A review on the present status of the axial structure of the nucleon in the space-like region is given in Ref. [14]. The first methods represent a rather direct measurement in the sense that the axial coupling of the weak charged currents is used to measure the axial form factor. The extraction of the axial form factor from pion-electroproduction in the space-like region is possible due to the application of a chiral Ward identity referred to as the Adler-Gilman relation [15]. A recent review on the theoretical development can be found in Ref. [16]. Corrections to order $O(p^4)$ have been calculated in the framework of chiral perturbation theory in Ref. [17]. There are no data available on the axial form factor in the time-like region. A direct measurement would be possible by studying the weak neutral or charged current in the annihilation of $\bar{p}p$. Such a measurement is not accessible with present day experimental techniques. On the other hand an application of the Adler-Gilman relation to the matrix element of the crossed channel of pion-electroproduction, namely $\bar{p} + n \rightarrow \pi^- + e^+ + e^-$, renders the possibility of accessing the axial current also in the time-like region around and below threshold. Despite the theoretical uncertainties, namely on one hand the applicability range of the Adler-Gilman relation which is strict only at the $\pi$-threshold and on the other hand the treatment of the off-shell nucleon between the $\pi$-vertex and the virtual photon vertex, the measurement of the cross section in $\bar{p} + n \rightarrow \pi^- + e^+ + e^-$ at low energies would render the first estimation of the axial form factor in the time-like region. Also here, the measurement of the cross section of this reaction will be accessible at the future FAIR facility at GSI.
C. Approach

Our approach is based on Compton-type annihilation Feynman amplitudes and aims to establish the matrix element of the processes (1) and (2). The main uncertainty in our description in terms of Green functions of mesons and nucleons (and their expected partners) is related to the model dependent description of hadron FFs and to the modeling of excited hadronic states.

The paper is organized as follows: the formalism is developed in Section II and some of the kinematical constraints for the considered reactions are discussed in Section III. Section IV contains a discussion on nucleon FFs and of our choices of parametrization, for electromagnetic as well as for axial FFs. In Section V the numerical results for the differential cross section of the considered processes will be presented. In Conclusions we discuss the results and summarize the perspectives opened by the experimental study of these reactions, including possible manifestation of heavy (radial) excited \( \pi \) states.

II. FORMALISM

Let us consider the reactions (1) and (2) and calculate the corresponding matrix elements in the framework of a phenomenological approach based on Compton-like Feynman amplitudes. The Feynman diagrams for the reaction (1), are shown in Fig. 1a and 1b, for pair emission from the proton and from the antiproton, respectively. For the reaction (2), the corresponding Feynman diagrams are shown in Figs. 2a, 2b and 2c: for pair emission from the charged pion, from the antiproton and from the neutron, respectively.

As previously discussed in Ref. [2], no free nucleons are involved in the electromagnetic vertexes of pions and nucleons, as one of the hadrons is virtual, and rigorously speaking, the form factors involved should be modified taking into account off mass shell effects. However we will use the expression for electromagnetic current involving on mass shell hadrons. A discussion of the errors and the consequences of such approximation is given below.

The vertexes \( \gamma^* \bar{N}N^* \rightarrow \gamma^* \bar{N}N \) and \( \gamma^* \pi \pi \rightarrow \gamma^* \pi \pi^* \) contain the information on the electromagnetic form factors (FFs) of proton, neutron and pion (FFs of antiproton differ by sign from proton FF, due to charge symmetry requirements). Nucleon FFs can be expressed in terms of Dirac and Pauli FFs \( F_{1,2}^{p,n}(q^2) \), which enter in the expression of the electromagnetic
current:

\[
<N(p')|\Gamma_\mu(q)N|N(p)> = \bar{u}(p') \left[ F_1^N(q^2)\gamma_\mu + \frac{F_2^N(q^2)}{4M}(\hat{q}\gamma_\mu - \gamma_\mu\hat{q}) \right] u(p), \quad N = n, p, \tag{3}
\]

where \( M \) is the nucleon mass and \( q \) is the four-momentum of the virtual photon. The nucleon FFs in the kinematical region of interest for the present work are largely unexplored. The assumptions and the parametrizations used for FFs in the numerical applications are detailed below.

The pion electromagnetic FF, \( F_\pi(q^2) \) is also introduced in the standard way. The corresponding current has the form:

\[
J_\mu^\pi = (q_1 + q_2)_\mu F_\pi(q^2) \tag{4}
\]

with \( q_1 \) and \( q_2 \) ingoing and outgoing charged pion momenta, and \( q_\pi = q_1 - q_2 \). Special attention must be devoted to the pion nucleon interaction, in the vertexes \( \pi NN \) that are parametrized as:

\[
\bar{v}(p_1)\gamma_5 u(p_2)g_{\pi NN}(s), \quad \text{and} \quad \bar{v}(p_1 - q)\gamma_5 u(p_2)g_{\pi NN}(m_\pi^2). \tag{5}
\]

with \( s = (p_1 + p_2)^2 \). The vertex of \( \pi NN \) interaction is related to the general axial vector current matrix element:

\[
<N(p')|A_j^A(0)|N(p)> = \bar{u}(p') \left[ G_A(q^2)\gamma_\mu + \frac{q_\mu}{2M}G_P^2(q^2) + i\frac{\sigma^{\mu\nu}}{2M}G_T(q^2) \right] \gamma_5 \frac{\tau_j}{2} u(p), \tag{6}
\]

where \( q_\mu = p'_\mu - p_\mu \), \( G_A(q^2) \) is the axial nucleon FF, \( G_P(q^2) \) the induced pseudoscalar FF, and \( G_T(q^2) \) the induced pseudotensor FF. In the chiral limit, the requirement of conservation

FIG. 1: Feynman diagrams for the reaction \( \bar{p} + p \rightarrow \pi^0 + \ell^+ + \ell^- \).
of the axial current leads to the relation:

\[ 4MG_A(q^2) + q^2 G_P(q^2) = 0, \]  

(7)

which shows that \( G_P(q^2) \) has a pole at small \( q^2 \). Indeed, assuming that the axial current interacts with the nucleon through the conversion to pion interaction, one obtains:

\[ G_P(q^2) = -\frac{4Mf_{\pi}g_{\pi NN}(q^2)}{q^2}, \]  

(8)

Comparing Eqs. (7) and (8) one obtains the Golberger-Treiman relation:

\[ \frac{G_A}{f_{\pi}} = \frac{g_{\pi NN}}{M}. \]  

(9)

We suggest a generalization of this relation in the form:

\[ g(s) = g_{\pi NN}(s) = \frac{MG_A(s)}{f_{\pi}}, \quad G_A(0) = 1.2673 \pm 0.0035. \]  

(10)

where \( g(s), g(m_{\pi}^2) \) are the pion-nucleon coupling constants for pion off and on mass shell. This assumption can be justified by the fact that \( f_{\pi} \) is weakly depending on \( q^2 \) and it is
in agreement with the ChPT expansion at small \( q^2 \) \cite{[16]}. Therefore measuring the \( g_{\pi NN}(s) \) coupling constant gives information on the axial and induced pseudoscalar FFs of the nucleon in the chiral limit (neglecting the pion mass).

The matrix element is expressed in terms of the hadronic \( H \) and leptonic \( J \) currents:

\[
M^i = \frac{4\pi\alpha}{q^2} H^\mu_J(q), \quad H^\mu = \bar{v}(p_1)O^\mu_u(p_2), \quad J^\mu(q) = \bar{v}(p_+)^\gamma_{\mu}u(p_-),
\]

where the index \( i = 0, - \) refers to \( \pi^0 \) and \( \pi^- \) respectively. The cross section for the case of unpolarized particles has a standard form (we imply that the nucleon target (proton or neutron) is at rest in the Laboratory frame):

\[
d\sigma^i = \frac{1}{16PM} \sum |M^i|^2 d\Gamma, \quad P^2 = E^2 - M^2,
\]

where \( E \) (\( P \)) is the energy (the modulus of the momentum), and \( d\Gamma \) is the phase space volume:

\[
d\Gamma = \frac{1}{d^3q_\pi \beta} \frac{d^4q}{2\epsilon_+2\epsilon_-2E_\pi} \delta^4(p_1 + p_2 - p_+ - p_- - q_\pi).
\]

The phase space volume can be written as:

\[
d\Gamma = \frac{d^3q_\pi}{2E_\pi} d\Gamma_q \frac{d^4q}{(2\pi)^5} \delta^4(p_1 + p_2 - q - q_\pi),
\]

with

\[
d\Gamma_q = \frac{d^3p_+}{2\epsilon_+} \frac{d^3p_-}{2\epsilon_-} \delta^4(q - p_+ - p_-).
\]

Considering an experimental set-up where the pion four-momentum is fully measured, we can perform the integration on the phase space volume of the lepton pair:

\[
\int d\Gamma_q \sum J_\mu(q)J^*_\nu(q) = -\frac{2\pi}{3}(q^2 + 2\mu^2)\beta\Theta(q^2 - 4\mu^2) \left( g_{\mu\nu} - \frac{q_\mu q_\nu}{q^2} \right) ,
\]

where \( \Theta \) is the usual step function, \( \mu \) is the lepton mass and \( \beta = \sqrt{1 - (4\mu^2/q^2)} \).

The cross section can be expressed in the form:

\[
d\sigma^i = \frac{\alpha^2}{6s\pi r} \beta(s^2 + 2\mu^2) \mathcal{D}^i \frac{d^3q_\pi}{2\pi E_\pi},
\]

with

\[
s = (q_\pi + q)^2 = 2M(M + E), \quad r = \sqrt{1 - (4M^2/s)}
\]

and

\[
\mathcal{D}^i = \left( g_{\mu\nu} - \frac{q_\mu q_\nu}{q^2} \right) \frac{1}{4} Tr(\hat{p}_1 - M)O^i_\mu(\hat{p}_2 + M)(O^i_\nu)^*, \quad i = 0, -.
\]
Using Feynman rules we can write (see Figs. 1, 2):

\[ O^- \mu = \Gamma^\mu_n(p) \frac{\hat{p}_1 - \hat{q} - M}{(p_1 - q)^2 - M^2} \gamma_5 g(m_\pi^2) - \gamma_5 \frac{\hat{p}_2 - \hat{q} + M}{(p_2 - q)^2 - M^2} \Gamma^\mu_n(p) g(m_\pi^2) + \frac{(2q_\pi + q)_\mu}{s - m_\pi^2} g(s) F_\pi(q^2) \gamma_5, \]

\[ O^0 \mu = \Gamma^\mu_n(p) \frac{\hat{p}_1 - \hat{q} - M}{(p_1 - q)^2 - M^2} \gamma_5 g(m_\pi^2) - \gamma_5 \frac{\hat{p}_2 - \hat{q} + M}{(p_2 - q)^2 - M^2} \Gamma^\mu_p(q) g(m_\pi^2)^2; \]

Note that the hadronic current $J^\mu_\mu = \bar{v}(p_1)O^- \mu u(p_2)$ is conserved, $J^\mu_\mu = \bar{v}(p_1)O^- \mu u(p_2)$ is not conserved:

\[ q_\mu J^\mu = \left[ (-F^\mu_1(q^2) + F^\mu_1(q^2))^2 g(m_\pi^2) + g(s) F_\pi(q^2) \right] \bar{v}(p_1) \gamma_5 u(p_2) = C \bar{v}(p_1) \gamma_5 u(p_2). \]

Therefore, to provide gauge invariance, it is necessary to add to $O^- \mu$ a contact term with the appropriate structure (20). The explicit expressions for $D^0$ and $D^-$ are given in the Appendix.

Selecting the coefficients which depend on pion energy in $D_1$, Eq. (17), an analytical integration on the pion energy can be performed. In the limit of small lepton pair invariant mass, $q^2$, after integration on pion energy, the differential cross section with respect to $q^2$ becomes:

\[ (q^2)^2 \left. \frac{d\sigma}{dq^2} \right|_{q^2 \ll M^2} \approx \frac{\alpha^2 [g(s) - g(m_\pi^2)]^2}{24\pi r}, \]

Eq. (21) contains one of the most important results of this work, as it shows that the measurement of the cross section at small $q^2$ allows to determine experimentally the off mass shell pion nucleon coupling constant.

Writing the differential cross section in the form:

\[ \frac{d\sigma}{dq^2} = \frac{(q^2 + 2\mu^2)^2}{(q^2)^2} \left[ \frac{c}{q^2} + R(q^2) \right], \]

with $c$ and $R(0)$ finite functions of $s$. After integration of lepton invariant mass, we find:

\[ \sigma_{\text{tot}} = \int_{4\mu^2}^s \frac{d\sigma}{dq^2} dq^2 = \frac{c(s)}{5\mu^2} + R(0, s) \left( \log \frac{s}{\mu^2} - \frac{5}{3} \right) + \int_0^s \frac{dq^2}{q^2} [R(q^2, s) - R(0, s)]. \]

The first term in the right hand side of Eq. (23) is divergent for massless leptons, and induces a rise of the cross section (especially in the case of electron positron pair). However it is very hard to achieve experimentally such kinematics, $q^2 \to 4\mu^2$. The total cross section can be integrated within the experimental limits of detection of the particles. Such (partial) total cross section will be calculated below.
### III. KINEMATICS

In the Laboratory system, useful relations can be derived between the kinematical variables, which characterize the reaction. The allowed kinematical region, at a fixed incident total energy \( s \), can be illustrated as a function of different useful variables.

One can find the following relation between \( q^2 \), the invariant mass of the lepton pair and the pion energy:

\[
q^2 = (p_1 + p_2 - q_\pi)^2 = 2M^2 + m_\pi^2 + 2M(E - E_\pi) - 2p_1q_\pi = s + m_\pi^2 - 2E_\pi M - 2p_1 q_\pi, \tag{24}
\]

with

\[
2p_1 q_\pi = 2E_\pi E - 2\sqrt{E_\pi^2 - m_\pi^2} P \cos \theta_\pi, \tag{25}
\]

where \( \theta_\pi = \hat{p}_1 q_\pi \) is the angle between the antiproton and the pion momenta (in the Laboratory frame).

The limit \(-1 \leq \cos \theta_\pi \leq 1\) translates into a maximal and a minimal value for the pion energy. The allowed kinematical region is shown in Fig. 3 left, for three values of the beam energy: \( E = 2, 7, 15 \) GeV. To this constraint, one should add the minimal thresholds \( q^2 \geq 4m_\pi^2 \) and \( E_\pi \geq m_\pi \). For the minimal value of \( q^2 \simeq m_\pi^2 \), one can plot the dependence of the pion energy on \( \theta_\pi \) (Fig. 3 right), for different values of the beam energy. As the energy increases the kinematically allowed region becomes wider. At backward angles the maximum pion energy becomes larger at small \( s \) values. For larger values of \( q^2 \), \( E_\pi \) is smaller.

For fixed values of the lepton pair invariant mass, the pion energy can take values in the region:

\[
\frac{E_{\pi\text{min}}}{M} = \frac{s - q^2}{s(1 + r)} \leq \frac{E_\pi}{M} \leq \frac{s - q^2}{s(1 - r)} = \frac{E_{\pi\text{max}}}{M}, \tag{26}
\]

neglecting the pion mass.

The phase space volume of the produced pion can be written (neglecting terms \( \simeq m_\pi^2/m_N^2 \)) in three (equivalent) forms:

\[
\frac{d^3 q_\pi}{2\pi E_\pi} = dq_\pi^2 \delta[q^2 - 2E_\pi(E + M - P \cos \theta_\pi)]E_\pi dE_\pi d\cos \theta_\pi =
\]

\[
=E_\pi dE_\pi d\cos \theta_\pi \tag{27a}
\]

\[
=M \frac{dq_\pi^2}{sr} dE_\pi \tag{27b}
\]

\[
=q^2 M^2 dq_\pi^2 d\cos \theta_\pi \frac{1}{s^2(1 - r \cos \theta_\pi)^2} \tag{27c}
\]
FIG. 3: (Color online) Left: The kinematical limit for $q^2$ is shown for $\cos \theta_\pi = -1$ and for $\cos \theta_\pi = 1$ in the Lab system as function of the pion energy for different values of the beam energy: $E=2$ GeV$^2$ (dotted line), $E=7$ GeV$^2$ (dashed line), $E=15$ GeV$^2$ (solid line). The allowed kinematical region lies below the curves.

Right: Kinematical limit for the pion energy $E_\pi$ as a function of the pion angle (Lab system), for $E=2$ GeV$^2$ (dotted line), $E=7$ GeV$^2$ (dashed line), $E=15$ GeV$^2$ (solid line), for the minimum value of $q^2 \simeq m_\pi^2$.

IV. AXIAL AND ELECTROMAGNETIC FORM FACTORS

Experimental measurements on FFs are object of ongoing programs in several world facilities. Hadron FFs are measured in space-like (SL) region through elastic electron hadron scattering, and in time-like (TL) region through annihilation reactions. It has been only recently possible to use polarization techniques. The availability of high intensity, high energy polarized beams allows to extend these measurements to large $q^2$ regions and to achieve very high precision.

The theoretical effort for a complete description of the nucleon structure should be extended to a unified picture which applies to the full kinematical region (SL and TL) [18]. Few phenomenological models, developed for the SL region can be successfully extended to the TL region [19]. A tentative extrapolation of a TL model to SL region has also been
done, and constraints have been found from the few available data [12].

In TL region, data for EM FFs exist over the NN threshold, up to 18 GeV$^2$ [20] but a precise separation of the electric and magnetic contributions has not yet been possible, due to the low statistics. Moreover, FFs are complex quantities, and polarization experiments are necessary to determine their relative phase. Presently only the modulus of FFs is available, under the hypothesis $|G_E^N|^2 = |G_M^N|^2$ or $G_E^N = 0$. These data have been obtained in the reactions $e^+ + e^- \leftrightarrow \bar{p} + p$ (see Ref. [21] and references therein) and, more recently by the radiative return method [22], in the region over the kinematical threshold $s > 3.52 \text{ GeV}^2$. The possible existence of an $N\bar{N}$ resonance under threshold has also been predicted as an explanation of the fact that TL FFs are larger than SL ones, at corresponding $|q^2|$ values. In order to give quantitative predictions, for the cross section of the processes (1) and (2), it is necessary to know the value of FFs in the unphysical region. As data are not available, such estimation can be only done in the framework of models, based, for example, on VMD or on dispersion relations, which predict several discontinuities due to meson resonances. Not all nucleon models give expressions for FFs which can be extended to time-like region, and not all nucleon models give a satisfactory description of all four nucleon FFs.

Following [19], in the present calculation we use two models for electromagnetic FFs: a model based on Ref. [23], which firstly predicted the behavior of the proton electric FF as found from recent polarization experiments [7], recently extended to TL region. This model, as all VMD inspired models, has poles in the unphysical region, in correspondence with the meson resonances which are taken into account. In order to have a smooth parametrization, we considered also a perturbative QCD (pQCD) inspired model prescription (corrected by dispersion relations [24]) which reproduces the experimental data in TL region, does not show discontinuities and can be considered an ‘average’ expectation:

$$|G_E^N| = |G_M^N| = \frac{A(N)}{q^4 \left( \ln^2 \frac{q^2}{\Lambda^2} + \pi^2 \right)}, \quad q^2 > \Lambda^2,$$  \tag{27}

where $\Lambda = 0.3 \text{ GeV}$ is the QCD scale parameter and $A$ is fitted to the data. This parametrization is taken to be the same for proton and neutron. The best fit is obtained with a parameter $A(p) = 98 \text{ GeV}^4$ for the proton and $A(n) = 134 \text{ GeV}^4$ for the neutron, which reflects the fact that in the TL region, neutron FFs are systematically larger than for the proton. In principle, this parametrization holds only for very large $q^2$ values, but, in practice, it reproduces
the existing data quite well in the whole physical region. Evidently it is meaningless at small
$q^2$, $(q^2 < \Lambda^2)$, and it has not the good normalization properties for $q^2 \to 0$.

Usually the data are shown in terms of the Sachs FFs, electric $G^N_E$, and magnetic $G^N_M$, which are related to the Pauli and Dirac FFs by the following relations:

$$G^N_E = F^N_1 + F^N_2, \quad G^N_M = F^N_1 + \tau F^N_2, \quad \tau = q^2/(4M^2).$$

. They correspond in a nonrelativistic limit (or in the Breit frame) to the Fourier transform
of the charge density (electric form factor $G_E$) and magnetization distribution (magnetic
form factor $G_M$) of the proton.

The behavior of these FFs is shown in Fig. 4, compared with the existing experimental
data. For the neutron, the first and still unique measurement in TL region was done at
Frascati, by the collaboration FENICE [25].

Concerning the pion FF, a reasonable description exists in the kinematical region of
interest here, for a recent discussion see Ref. [26]. For the sake of simplicity, we use here a
$\rho$ meson saturated monopole-like parametrization, which takes a Breit Wigner form in TL
region:

$$F^\pi_n(q^2) = \frac{m^2}{m^2 - q^2 - im \Gamma_{\rho}}.$$  \hspace{1cm} (28)

Data on axial FFs in TL region do not exist, and they suffer in SL region from a model
dependent derivation. In SL region, the nucleon axial FF, $G_A(q^2)$, for the transition $W^* + p \to n$ ($W^*$ is the virtual $W$-boson), can be described by the following simple formula [27]:

$$G_A(q^2) = G_A(0)(1 - q^2/m^2)^{-n}$$  \hspace{1cm} (29)

with $m_A = 1.06$ GeV, if $n = 2$. A simple analytical continuation of this prescription to
the TL region, presents a pole in the unphysical region. Therefore we used a 'mirror'
parametrization from SL region:

$$FF^{(TL)}(|q^2|) = FF^{(SL)}(|q^2|).$$

Such a prescription is, in principle, valid only at very large $q^2$, since it obeys to asymptotic
analytical properties of FFs [18].

For comparison, another parametrization is also used [28], inspired from [23]:

$$G^{SL}_A(q^2) = d(q^2)G_A(0) \left[ 1 - \alpha + \alpha \frac{m_A^2}{m^2_A - q^2} \right],$$  \hspace{1cm} (30)
FIG. 4: (Color online) Nucleon electromagnetic FFs in time-like region: proton electric FF (a), proton magnetic FF (b), neutron electric FF (c), neutron magnetic FF (d). Data are from [22] and predictions from model [23] (solid line), and from pQCD (dashed line).

The parameter $\alpha = 1.893 \pm 0.02$ has been fitted on the available data, in the SL region, averaging the dispersion due to the model dependent extraction of the data themselves, $m_A \simeq 1.235$ GeV is the mass of a light axial meson, and $d(q^2) = (1 - \gamma q^2)^{-2}$ is the function describing the internal core of the nucleon. We take $\gamma$ as a fixed parameter, from the fit of nucleon electromagnetic form factors: $\gamma \simeq 0.25$ GeV$^{-2}$. Let us note however that this value is not good from a $t$ channel point of view, because it gives a pole in the physical region, $t_0 = \frac{4}{\gamma} = 4$ GeV$^{-2}$. In order to extend the expression (30) to TL region, following [23], a phase is added to the dipole term. Moreover the complex nature of the axial FF is insured by adding a width to the axial meson, and we replace the propagator as in Eq. [28].

The expression for the TL axial FF is therefore:

$$G_A(q^2) = d(q^2)G_A(0) \left[ 1 - \alpha + \alpha \frac{m_A^2}{m_A^2 - q^2 - i m_A \Gamma_A} \right], \quad (31)$$
FIG. 5: (Color online) Proton axial FF from VMD inspired model (solid line) and from a dipole extrapolation (dashed line).

with $d(q^2) = (1 - \gamma e^{i\delta} q^2)^{-2}$, where $\Gamma_A=0.140$ GeV, and $\delta=0.925$.

The two models for $G_A$ used in the calculation of the cross section are shown in Fig. 5 and differ by one order of magnitude. Moreover, an enhancement is expected from Eq. (31), in correspondence to the mass of the axial meson.

V. RESULTS

The differential and integrated cross sections were calculated for several values of the antiproton energy and different choices of FFs described above.

The differential cross sections, Eq. (15), as a function of $E_{\pi}$ and $q^2$, Eq. (27a), are shown in Figs. 6 and 7 for the reactions $\bar{p} + p \rightarrow \pi^0 + \ell^+ + \ell^-$ and $\bar{p} + n \rightarrow \pi^- + \ell^+ + \ell^-$ and at $E= 7$ GeV$^2$. As one can see from the figures, the differential cross sections are large and measurable in a wide range of the considered variables. It is reasonable to assume that the region up to $q^2 = 7$ GeV$^2$, at least, will be accessible by the experiments at FAIR.

The discontinuities in the small $q^2$ regions are smoothed out by the steps chosen to histogram the variables. However, depending on the resolution and the reconstruction efficiency, it will be experimentally possible to identify the meson and nucleon resonances.
FIG. 6: (Color online) Left: Double differential cross section for the reaction $\bar{p} + p \rightarrow \pi^0 + \ell^+ + \ell^-$ as a function of $q^2$ and $E_\pi$, using FFs from [25] for nucleon and [30] for axial FF. Right: Same quantity as in the left plot for the reaction $\bar{p} + n \rightarrow \pi^- + \ell^+ + \ell^-$. The kinematical constraints in the $(E_\pi, q^2)$-plane shown in Fig. 8 are visible here.

FIG. 7: (Color online) Left: Double differential cross section for the reaction $\bar{p} + p \rightarrow \pi^0 + \ell^+ + \ell^-$ as a function of $q^2$ and $E_\pi$, using pQCD inspired nucleon FFs and dipole axial FFs. Right: Same quantity as in the left plot for the reaction $\bar{p} + n \rightarrow \pi^- + \ell^+ + \ell^-$. 

16
The differential cross section as a function of $q^2$ can be obtained after integrating on the pion energy, Eq. (15), with the help of Eq. (27b):

$$\frac{d\sigma_i}{dq^2} = \frac{\alpha^2}{6s\pi r} \frac{\beta(q^2 + 2\mu^2)}{(q^2)^2} \frac{M}{sr} \int_{E_{\pi}^{min}}^{E_{\pi}^{max}} \mathcal{D}^i dE_\pi,$$

where the integration on the hadronic term is detailed in the Appendix. The result of the calculation is shown in Fig. 8. For charged pion production, the presence of the axial FF is the reason of a larger cross section as compared to the neutral pion case. For both reactions, again, the present calculation gives an integrated cross section of the order of several $\mu b$ in the unphysical region, for both choices of FFs.

The $q^2$ dependence is driven by the choice of FFs. In case of pQCD-like FFs, the behavior is smooth and similar for proton and neutron. In case of FFs from [23], the resonant behavior due to $\rho$, $\omega$ and $\phi$ poles appears in the figures. The partial total cross section, integrated over $q^2$, Eq. (23), is shown in Fig. 9 as a function of $q_{min} \gg 4\mu^2$ for two different values of $s$, $s=2$ and 5 GeV$^2$. Evidently the calculations for the VMD FFs [23] have been done beyond the resonance region, due to the divergence of the integrals at the meson poles.

Let us estimate the uncertainties inherent to our model assumptions. The off mass-shell effects were previously discussed for these particular reactions in [2]. Large theoretical effort has been devoted to this problem in the past (Ref. 29 and ref. therein), where it was...
shown that indeed off-mass shell effects can be large and have the effect to increase FFs. In the region of virtuality $p^2 \leq 0.5$ GeV$^2$ it was calculated that off mass shell effects modify FFs at the level of 3%. The $Q^2$-dependence of FFs is not changed significantly, when one of the particles goes off shell. It is interesting to note that the ratio of electric and magnetic nucleon FF is rather insensitive to off shell effects. Moreover ChPT arguments support a smooth behavior of FFs as a function of the degree of nucleon virtuality $\delta \sim \frac{\nu^2 - M^2}{M} \leq 2$, which does not exceed 10%. For the present kinematics the virtuality involved varies in the interval, $2m_\pi/M < \delta < 2 - 2m_\pi/M$. In the case of detection of soft pions in laboratory frame, errors arising from off shell effects will decrease to $3 \div 5\%$.

In the intermediate state, in principle, resonances can be excited. The estimation of contribution of the $\Delta$ resonance, compared to nucleon intermediate state, is of the order of $M_\Delta g_{\Delta N \pi}/g_{NN \pi} \simeq 0.07$. Higher resonances have smaller contribution.

These considerations support an estimation on the precision of our model at the level of 10%.
VI. CONCLUSION AND PERSPECTIVES

The differential cross section for the processes $\bar{p} + n \rightarrow \pi^- + \ell^- + \ell^+$ and $\bar{p} + p \rightarrow \pi^0 + \ell^- + \ell^+$ has been calculated in the kinematical range which will be accessible in next future at FAIR. The main interest of these reactions is related to the possibility of measuring nucleon electromagnetic and axial FFs in the time-like and in the unphysical regions. As previously pointed out [1, 2], varying the momentum of the emitted pion allows to scan the $q^2$ region of interest, keeping the beam energy fixed.

In Ref. [2] it was also noticed that in the lepton invariant mass squared distribution, a divergent term was present:

$$
\frac{d\sigma}{dq^2} \simeq \left[ 2F_1^\pi(q^2) + F_\pi(q^2) \right]^2 \frac{1}{(q^2)^2}, \quad q^2 \rightarrow 0,
$$

(33)

(in our notation the right hand side of Eq. (33) corresponds to $C^2/(q^2)^2$). It was argued that the singularity at $q^2 \rightarrow 0$ cancels due to $2F_1^\pi(0) = 1$ and $2F_\pi(0) = -1$. This compensation takes place if the following equality $g_{\pi NN}(s) = g_{\pi NN}(m_{\pi^0}^2)$ holds, which is verified for annihilation at rest. In the present work, one can not rely on such assumption and the validity of this relation has to be verified experimentally.

The detailed measurement of the double differential cross section, as a function of $q^2$ and $E_{\pi}$ allows in principle to extract all nucleon FFs which are involved in the considered reactions. A precise simulation of different processes involving the production of a pion will be necessary with a study of the best kinematical conditions in order to minimize background contribution. In particular the reaction $\bar{p} + p \rightarrow \pi^0 + \pi^0$ has been identified as a potential source of background in the $e^+e^-$-spectrum due to its Dalitz decay $\pi^0 \rightarrow e^+e^-\gamma$.

The assumption about the validity of a generalized form of the Golberger-Treiman relation, which allows to relate the pseudoscalar $g_{\pi NN}$ coupling constant to the axial nucleon FF can be experimentally verified in case of small invariant mass of the lepton pair. The possibility of measurement of heavy negatively charged pions ($\pi^-'$-radial excitation of pion, $M' = 1300$ MeV) in the process of $\pi^-$ production can be taken into account in the following way. The matrix element for the excitation of a resonant state for the virtual charged pion in the intermediate state, $M_{res}$, can be written as follows:

$$
M_{res} = \frac{4\pi\alpha}{q^2} \frac{g_{\pi NN}}{s - M^2 + iM\Gamma} \bar{v}(p_1)\gamma_5 u(p_2) \lambda(q^2) \left( q_{\mu} - \frac{q^2}{qq_{\pi}} q_{\pi\mu} \right) J_\mu
$$

(34)
The corresponding cross section is:

\[
d\sigma_{\text{res}} = \frac{\alpha^2}{12r\pi} \frac{|\lambda(q^2)g_{\pi N\bar{N}}|^2}{(s - M'^2)^2 + M'^2\Gamma'^2} \frac{d^3q_\pi}{2\pi E_\pi}.
\]  

(35)

where \(\lambda(q^2)\) is the transition from factors for the vertex \(\pi'\gamma^*\). We do not consider processes involving vector mesons, \(\Delta\) resonances and higher excited nucleon states, estimating that their contribution does not exceed 10%.

In case of multi-pion production, the quantity \(s_1 = (p_1 + p_2 - q)^2 - m_\pi^2\) becomes positive. Varying \(s_1\) at fixed beam energy, by changing \(q^2\) and \(\theta_\pi\), it is in principle possible to identify and study other mechanisms, as the excitation of heavy pion resonances, \(\pi'\), or the possible presence of a \(N\bar{N}\) 'quasi-deuteron' state under the kinematical threshold for \(p\bar{p}\) annihilation in two leptons. The study of multipion production will be the subject of a forthcoming publication.

VII. ACKNOWLEDGMENTS

The authors are thankful to L. Lipatov for critical remarks on the manuscript and interesting discussions. Useful discussion with S. Scherer, H. W. Hammer and G. I. Gakh are acknowledged. Two of us (E. A. K. and C. A.) are grateful to DAPNIA/SPhN, Saclay, where this work was done. The Slovak Grant Agency for Sciences VEGA is acknowledged by C.A. for support under Grant N. 2/4099/26.

VIII. APPENDIX

In this appendix we give the explicit expression of the coefficients entering in the calculation of the cross section, as well as useful integrals.

Let us define \(q^2\)-dependent terms, which contain FFs and the necessary constants:

\[
f_a(s) = F_\pi(q^2)G_{\pi N\bar{N}}(s), \quad f_{iN}(q^2) = g(m_\pi^2)F_i^N(q^2), \quad i = 1, 2; \quad N = n, p,
\]

\[
C(s) = f_a(s) - f_{1p}(q^2) + f_{1n}(q^2),
\]

and the quantity:

\[
X = \frac{p_1q_\pi}{p_2q_\pi} = \frac{(s - q^2)}{(2ME_\pi)} - 1.
\]  

(36)
Let us write the expressions for the hadronic part of the matrix element (17):

- for the process $p + \bar{p} \to \ell^+ + \ell^− + \pi^0$

$$D^0 = |f_{2p}|^2 \left[ \frac{E - M}{M} - \frac{1}{2} \left( 1 - \frac{q^2}{4M^2} \right) \frac{(1 - X)^2}{X} \right] + |f_{1p} - f_{2p}|^2 \frac{(X + 1)^2}{X}, \quad (37)$$

- for the process $n + \bar{p} \to \ell^+ + \ell^− + \pi^−$

$$D^- = \frac{1}{4} \left[ \sum_i C_{i,i} |f_i|^2 + 2 \sum_{j,k; j < k} C_{j,k} Re(f_j f_k^*) + \frac{2|C|^2 s}{q^2} \right], \quad i, j, k = 1p, 2p, 1n, 2n, a. \quad (38)$$

The explicit form of the coefficients is:

$$C_{1p,1p} = 4X, \quad C_{2p,2p} = \frac{s}{M^2} \left( 1 + \frac{q^2}{2s} X \right), \quad C_{1p,2p} = -3 \left( 1 + X \right), \quad C_{a,a} = \frac{2q^2}{s} - 4,$$

$$C_{1n,1n} = 4 \frac{1}{X}, \quad C_{2n,2n} = \frac{s}{M^2} \left( 1 + \frac{q^2}{2sX} \right), \quad C_{1n,2n} = -3 \left( 1 + \frac{1}{X} \right),$$

$$C_{a,1p} = 2, \quad C_{a,2p} = \left( 1 - \frac{q^2}{s} \right) \left( 1 + X \right), \quad C_{1p,1n} = 4, \quad C_{1p,2n} = \left( \frac{1}{X} - 2X - 1 \right),$$

$$C_{2p,2n} = \left( 2 + \frac{2}{X} - \frac{q^2}{2M^2} + X \right), \quad C_{2p,1n} = \left( X - \frac{2}{X} - 1 \right),$$

$$C_{a,1n} = -2, \quad C_{a,2n} = - \left( 1 - \frac{q^2}{s} \right) \left( 1 + \frac{1}{X} \right). \quad (39)$$

The structure of $D_\ell$ allows to select the terms which depend on the pion energy. It is straightforward to perform an analytical integration on the pion energy, using the following integrals:

$$\int_{E_{\pi}^{\text{min}}}^{E_{\pi}^{\text{max}}} \frac{dE_{\pi}}{M} = \frac{r(s - q^2)}{2M^2} = rb; \quad b = \frac{s - q^2}{2M^2}, \quad (40)$$

$$\int_{E_{\pi}^{\text{min}}}^{E_{\pi}^{\text{max}}} \frac{dE_{\pi}}{M} X = \int_{E_{\pi}^{\text{min}}}^{E_{\pi}^{\text{max}}} \frac{dE_{\pi}}{M} \frac{1}{X} = \frac{s - q^2}{2M^2} \left[ \ln \frac{1 + r}{1 - r} - r \right] = b(\ell - r); \quad (41)$$

with $r$ given in (16) and $\ell = \ln[(1 + r)/(1 - r)]$. The result of the integration on the pion energy is:

- for the process $p + \bar{p} \to \ell^+ + \ell^− + \pi^0$

$$\int_{E_{\pi}^{\text{min}}}^{E_{\pi}^{\text{max}}} D^0 \frac{dE_{\pi}}{M} = b \left\{ 2|f_{1p} - f_{2p}|^2 \ell + |f_{2p}|^2 \left[ \frac{E - M}{M} r + \left( 1 - \frac{q^2}{4M^2} \right) (2r - \ell) \right] \right\} \quad (42)$$

- for the process $p + \bar{p} \to \ell^+ + \ell^− + \pi^0$

$$\int_{E_{\pi}^{\text{min}}}^{E_{\pi}^{\text{max}}} D^- \frac{dE_{\pi}}{M} = \frac{b}{4} \left[ \sum_i K_{i,i} |f_i|^2 + 2 \sum_{j,k; j < k} K_{j,k} Re(f_j f_k^*) + |C|^2 \frac{2rs}{q^2} \right], \quad (43)$$
where

\[ K_{1p,1p} = 4(\ell - r), \quad K_{2p,2p} = \frac{s}{M^2} \left( r + \frac{q^2}{2s} (\ell - r) \right), \]

\[ K_{1p,2p} = -3\ell, \quad K_{a,a} = \left( \frac{2q^2}{s} - 4 \right) r, \]

\[ K_{1n,1n} = 4(\ell - r), \quad K_{2n,2n} = \frac{s}{M^2} \left( r + \frac{q^2}{2s} (\ell - r) \right), \quad K_{1n,2n} = -3\ell, \]

\[ K_{a,1p} = 2r, \quad K_{a,2p} = \left( 1 - \frac{q^2}{s} \right) \ell, \quad K_{1p,1n} = 4r, \quad K_{1p,2n} = -\ell, \]

\[ K_{2p,2n} = \left[ 3\ell - \left( 1 + \frac{q^2}{2M^2} \right) r \right], \quad K_{2p,1n} = -\ell, \]

\[ K_{a,1n} = -2r, \quad K_{a,2n} = -\left( 1 - \frac{q^2}{s} \right) \ell, \]  \hspace{1cm} (44)

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