SIMULTANEOUS MULTISLICE MAGNETIC RESONANCE FINGERPRINTING WITH LOW-RANK AND SUBSPACE MODELING

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Abstract

Magnetic resonance fingerprinting (MRF) is a new quantitative imaging paradigm that enables simultaneous acquisition of multiple magnetic resonance tissue parameters (e.g., $T_1$, $T_2$, and spin density). Recently, MRF has been integrated with simultaneous multislice (SMS) acquisitions to enable volumetric imaging with faster scan time. In this paper, we present a new image reconstruction method based on low-rank and subspace modeling for improved SMS-MRF. Here the low-rank model exploits strong spatiotemporal correlation among contrast-weighted images, while the subspace model captures the temporal evolution of magnetization dynamics. With the proposed model, the image reconstruction problem is formulated as a convex optimization problem, for which we develop an algorithm based on variable splitting and the alternating direction method of multipliers. The performance of the proposed method has been evaluated by numerical experiments, and the results demonstrate that the proposed method leads to improved accuracy over the conventional approach. Practically, the proposed method has a potential to allow for a 3x speedup with minimal reconstruction error, resulting in less than 5 sec imaging time per slice.

Index Terms
Low-rank model; subspace model; sparse sampling; simultaneous multislice (SMS); quantitative magnetic resonance imaging (qMRI)

1. INTRODUCTION

Most clinical magnetic resonance imaging (MRI) applications rely on contrast-weighted images, which are complex functions of intrinsic magnetic resonance (MR) tissue parameters (e.g., $T_1$, $T_2$, and spin density) and external scan settings (e.g., field inhomogeneity and coil geometry). These images are qualitative in nature, which provide limited capability for direct inter- and intra-patient comparisons across different institutions.
and/or across scanners. Quantitative MRI is a promising direction to overcome these limitations [1]; but it often results in prolonged data acquisition time. Magnetic resonance fingerprinting (MRF) [2] is a very recent breakthrough in quantitative MRI, which enables rapid acquisition of multiple MR tissue parameters. For example, with MRF, the acquisition time can be shortened to around 15 sec for acquiring a single imaging slice.

Although MRF provides an unprecedented imaging speed, it could still result in clinically unacceptable lengthy acquisitions of up to 20 minutes for volumetric coverage of e.g., the brain with a large number of imaging slices. Simultaneous multislice (SMS) imaging [3–6] is a powerful data acquisition methodology, which enables rapid volumetric imaging through acquiring data from multiple imaging slices simultaneously rather than sequentially. Recently, SMS techniques have been integrated with MRF to improve the imaging speed for volumetric quantitative MRI [7–9]. For data acquisition, additional gradient blips along slice direction are added, which generate phase modulation for simultaneously acquired slices. For image reconstruction, [7] integrates the conventional approach with slice sensitivity encoding (SENSE) method, while [8] combines generalized autocalibrating partially parallel acquisition (GRAPPA) with slice-GRAPPA. A more recent approach generalizes the above methods by using different acquisition parameters (e.g., flip angle and RF phases) for each slice [9], which is able to achieve a number of desired properties (e.g., reduced peak RF amplitude, and signals between slices being more orthogonal).

Extending our early work in [10], this work presents a new image reconstruction method for SMS-MRF. It utilizes the low-rank and subspace modeling to enable accurate reconstruction of MR tissue parameter maps from highly-undersampled data. Here the low-rank model exploits strong spatiotemporal correlation among MRF contrast-weighted images, while the subspace model captures the temporal evolution of magnetic dynamics. The proposed model results in a convex optimization problem, which is solved by a numerical algorithm based on variable splitting (VS) [11–13] and the alternating direction method of multipliers [12–14]. The effectiveness of the proposed method was evaluated with numerical experiments.

2. PROPOSED APPROACH

2.1. Problem Formulation

Assuming that \( N_s \) imaging slices are simultaneously excited at the \( n \)th time instant [or repetition time (TR)], the imaging equation for SMS-MRF can be written as

\[
d_{m,c} = F_m \sum_{q=1}^{N_s} S_{c,q} I_{m,q} + n_{m,c},
\]

for \( m = 1, \ldots, M \) and \( c = 1, \ldots, N_c \), where \( I_{m,q} \in \mathbb{C}^N \) denotes the contrast-weighted image associated with the \( n \)th TR and \( q \)th slice, \( S_{c,q} \in \mathbb{C}^{N_c \times N} \) a diagonal matrix whose diagonal entries contain the coil sensitivity profile for the \( c \)th coil and \( q \)th slice, \( F_m \in \mathbb{C}^{P_m \times N} \) the undersampled Fourier encoding matrix for the \( n \)th time instant, \( d_{m,c} \in \mathbb{C}^{P_m} \) the measured k-space data, and \( n_{m,c} \in \mathbb{C}^{P_m} \) the measurement noise.
For simplicity, we consider a discrete image model, in which the contrast-weighted images associated with each slice can be represented by the following Casorati matrix [15], i.e.,

\[
C_q = \begin{bmatrix}
I_{1,q}(x_1) & \cdots & I_{M,q}(x_1) \\
\vdots & \ddots & \vdots \\
I_{1,q}(x_N) & \cdots & I_{M,q}(x_N)
\end{bmatrix} \in \mathbb{C}^{N \times M}.
\]

With this notation, (1) can be rewritten as

\[
d_c = \Omega(F \sum_{q = 1}^{N_s} S_{c,q} C_q) + n_c,
\]

for \(c = 1, \ldots, N_c\), where \(d_c\) and \(n_c\) are both \(P \times 1\) complex vectors that respectively contain the measured data and measurement noise from all the time instants associated with the \(c\)th receiver coil, \(F \in \mathbb{C}^{N \times N}\) denotes the fully-sampled Fourier encoding matrix, and \(\Omega(\cdot) : \mathbb{C}^{N \times M} \rightarrow \mathbb{C}^P\) denotes the \((k, t)\)-space sparse sampling operator that acquires \(k\)-space data from each TR and then concatenates the data into \(d_c\).

Given that there is strong spatiotemporal correlation among the contrast-weighted images, \(C_q\) admits a low-rank approximation. Invoking a low-rank constraint, the image reconstruction problem can be formulated as follows:

\[
\{\widehat{C}_q\}_{q = 1}^{N_s} = \arg \min_{C_q} \sum_{c = 1}^{N_c} \left\| d_c - \Omega(F \sum_{q = 1}^{N_s} S_{c,q} C_q) \right\|_2^2 + \sum_{q = 1}^{N_s} R_{f}(C_q),
\]

where \(R_{f}(C_q)\) denotes a low-rank regularization functional. There are a number of ways of imposing a rank constraint. Here, we enforce an explicit low-rank constraint via matrix factorization [16–18], i.e., \(C_q = U_q V_q\), where \(U_q \in \mathbb{C}^{N \times r}\) and \(V_q \in \mathbb{C}^{r \times M}\) respectively span the spatial subspace and temporal subspace of \(C_q\).

Moreover, we can pre-estimate the temporal subspaces for the low-rank model prior to image reconstruction. Specifically, dictionaries can be generated via Bloch simulations that contain all possible magnetization evolutions, from which \(\{V_q\}\) can be estimated by the principled component analysis [15, 19]. As a consequence, the image reconstruction problem reduces to determining the spatial subspaces \(\{U_q\}\), i.e.,

\[
\{\widehat{U}_q\}_{q = 1}^{N_s} = \arg \min_{U_q} \sum_{c = 1}^{N_c} \left\| d_c - \Omega(F \sum_{q = 1}^{N_s} S_{c,q} U_q V_q) \right\|_2^2.
\]
where \( \{ \tilde{V}_q \} \) denote the pre-estimated temporal subspaces. After solving (2), the Casorati matrix associated with the contrast-weighted images can be formed, i.e., \( \tilde{\mathbf{C}}_q = \tilde{U}_q \tilde{V}_q \). Then we can estimate MR tissue parameters via dictionary based pattern matching as in the conventional approach.

### 2.2. Solution Algorithm

In this subsection, we describe a solution algorithm based on variable splitting (VS) and the alternating direction method of multipliers (ADMM) to solve (2). First, we apply the following VS scheme:

\[
G_q = U_q \tilde{V}_q
\]

and

\[
H_c = \sum_{q=1}^{N_s} S_{c,q} G_q,
\]

and form an equivalent constrained optimization problem as follows:

\[
\min_{U_q, G_q, H_c} \sum_{c=1}^{N_c} \| d_c - \Omega(\mathbf{F} H_c) \|^2_2,
\]

s.t. 

\[ H_c = \sum_{q=1}^{N_s} S_{c,q} G_q \]

and 

\[ G_q = U_q \tilde{V}_q. \]

Second, the augmented Lagrangian function associated with (3) is formed as follows:

\[
L_{\mathcal{A}}(U_q, G_q, H_c) = \sum_{c=1}^{N_c} \| d_c - \Omega(\mathbf{F} H_c) \|^2_2 + \]

\[
\text{Re}( \langle X_c, H_c - \sum_{q=1}^{N_s} S_{c,q} G_q \rangle ) + \frac{\mu_h}{2} \left\| H_c - \sum_{q=1}^{N_s} S_{c,q} G_q \right\|_F^2 + \]

\[
+ \sum_{q=1}^{N_s} \left\{ \text{Re}( \langle Y_q, G_q - U_q \tilde{V}_q \rangle ) + \frac{\mu_g}{2} \left\| G_q - U_q \tilde{V}_q \right\|_F^2 \right\},
\]

where \( \{ X_c \} \) and \( \{ Y_q \} \) are the Lagrangian multipliers, \( \mu_g \) and \( \mu_h \) are the penalty parameters, and \( \text{Re}(\cdot) \) takes the real part of a complex number.

Third, we apply the ADMM algorithm to minimize \( L_{\mathcal{A}}(\cdot) \). Here the algorithm consists of solving the following optimization problems:

\[
\left\{ U_q^{(k+1)} \right\}_{q=1}^{N_s} = \arg \min_{U_q, G_q^{(k)}, H_c^{(k)}} L_{\mathcal{A}}(U_q, G_q^{(k)}, H_c^{(k)}), \quad (4)
\]

\[
\left\{ G_q^{(k+1)} \right\}_{q=1}^{N_s} = \arg \min_{G_q, H_c^{(k)}} L_{\mathcal{A}}(U_q^{(k+1)}, G_q, H_c^{(k)}), \quad (5)
\]
\[
\left\{ \mathbf{H}_c^{(k+1)} \right\}_{c=1}^{N_c} = \arg \min_{\mathbf{H}_c} \sum_{q=1}^{N_s} \mathcal{L}_{U_q} \left( \mathbf{u}_q^{(k+1)}, \mathbf{g}_q^{(k+1)}, \mathbf{h}_c \right),
\]

and updating the Lagrangian multipliers:

\[
\mathbf{x}_c^{(k+1)} = \mathbf{x}_c^{(k)} + \mu_h \left[ \mathbf{H}_c^{(k+1)} - \sum_{q=1}^{N_s} \mathbf{s}_{c,q} \mathbf{g}_q^{(k+1)} \right]
\]
\[
\mathbf{y}_q^{(k+1)} = \mathbf{y}_q^{(k)} + \mu_g \left[ \mathbf{g}_q^{(k+1)} - \mathbf{u}_q^{(k+1)} \right].
\]

Next we describe the solutions to (4)–(6).

The optimization problem in (4) is separable with respect to each \( \mathbf{u}_q \), and is equivalent to solving

\[
\mathbf{u}_q^{(k+1)} = \arg \min_{\mathbf{u}_q} \left\| \mathbf{u}_q \right\|_F^2 - \frac{1}{\mu_g} \mathbf{y}_q - \mathbf{G}_q - \mathbf{H}_c^{(k)} + \mathbf{x}_c^{(k)} \cdot \mu_h.
\]

for \( q = 1, \ldots, N_s \). Noting that \( \mathbf{V}_q^T \mathbf{V}_q = \mathbf{I} \), the solution to (7) is given by

\[
\mathbf{u}_q^{(k+1)} = \left( \mathbf{G}_q + \mathbf{y}_q / \mu_g \right) \mathbf{V}_q^H.
\]

The optimization problem in (5) can be written as

\[
\min_{\mathbf{g}_q} \sum_{c=1}^{N_c} \frac{\mu_h}{2} \left\| \sum_{q=1}^{N_s} \mathbf{s}_{c,q} \mathbf{g}_q - \left( \mathbf{H}_c^{(k)} + \mathbf{x}_c^{(k)} / \mu_h \right) \right\|_F^2 + \sum_{q=1}^{N_s} \frac{\mu_g}{2} \left\| \mathbf{g}_q - \left( \mathbf{u}_q^{(k+1)} \mathbf{V}_q - \mathbf{y}_q^{(k)} / \mu_g \right) \right\|_F^2.
\]

(8)

for \( q = 1, \ldots, N_s \). Further, (8) can be written into the following compact form:

\[
\min_{\mathbf{g}} \frac{\mu_h}{2} \left\| \mathbf{S} \mathbf{g} - \mathbf{Q}^{(k)} \right\|_F^2 + \frac{\mu_g}{2} \left\| \mathbf{G} - \mathbf{W}^{(k)} \right\|_F^2.
\]

(9)

where
\[ G = \begin{bmatrix} G_1 \\ \vdots \\ G_{Ns} \end{bmatrix} \in \mathbb{C}^{NN_s \times M}. \]
\[ \tilde{S} = \begin{bmatrix} S_{1,1} & \cdots & S_{1,Ns} \\ \vdots & \ddots & \vdots \\ S_{Nc,1} & \cdots & S_{Nc,Ns} \end{bmatrix} \in \mathbb{C}^{NN_c \times NN_s}. \]
\[ Q^{(k)} = \begin{bmatrix} H_1^{(k)} + X_1^{(k)}/\mu_h \\ \vdots \\ H_{Nc}^{(k)} + X_{Nc}^{(k)}/\mu_h \end{bmatrix} \in \mathbb{C}^{NN_c \times M}. \]

and
\[ W^{(k)} = \begin{bmatrix} U_1^{(k+1)} - Y_1^{(k)}/\mu_g \\ \vdots \\ U_{Ns}^{(k+1)} - Y_{Ns}^{(k)}/\mu_g \end{bmatrix} \in \mathbb{C}^{NN_s \times M}. \]

Eq. (9) is equivalent to solving
\[
\left( \frac{\mu_h}{2} \tilde{S}^H \tilde{S} + \frac{\mu_g}{2} \right) G = \frac{\mu_h}{2} \tilde{S}^H Q^{(k)} + \frac{\mu_g}{2} W^{(k)},
\]
where \( I \) is the identity matrix. Noting that \( \left( \frac{\mu_h}{2} \tilde{S}^H \tilde{S} + \frac{\mu_g}{2} \right) \) is a sparse matrix, the above equation can be efficiently solved by iterative algorithms (e.g., pre-conditioned conjugate gradient algorithm).

The optimization problem in (6) is separable with respect to each coil and is equivalent to solving
\[
H_c^{(k+1)} = \arg \min_{H_c} \| \Omega(FH_c) - d_c \|^2_2 + \frac{\mu_h}{2} \left\| H_c - \sum_{q=1}^{N_s} S_{c,q} G_q^{(k+1)} + X_c^{(k)}/\mu_h \right\|^2_F,
\]
for \( c = 1, \ldots, N_c \). Note that (10) is further separable with respect to each time instant, and is equivalent to solving
\[
\left( F_m H_m + \frac{\mu_h}{2} I \right) h_{m,c}^{(k+1)} = \frac{\mu_h}{2} \sum_{q=1}^{N} s_{c,q} g_{m,q}^{(k+1)} - x_{m,c}^{(k)} + F_m H_m d_{m,c},
\]

for \( m = 1, \ldots, M \), where \( h_{m,c}, g_{m,q}, x_{m,c} \) are the \( m \)th columns of \( H_c, G_q, \) and \( X_c, \) respectively. Noting that the coefficient matrix \( \left( F_m H_m + \frac{\mu_h}{2} I \right) \) has a block Toeplitz structure, the above equation can be solved by a number of efficient numerical solvers (e.g., hierarchically semiseparable solver [20]).

3. RESULTS

Representative results from numerical experiments are shown to illustrate the performance of the proposed method. A numerical phantom based on the BrainWeb database [21] was built, in which three imaging slices (containing \( T_1, T_2, \) and spin density maps) were taken with a distance of 35 mm apart. We simulated the MRF experiments using an inversion recovery fast imaging with steady state free precession (IR-FISP) pulse sequence with the same acquisition parameters as in [22], and synthesized the contrast-weighted images with the extended phase graph formalism [23]. We generated coil sensitivity maps associated with a 32 channel receiver head coil using a Biot-Savart calculator. A multiband RF pulse was used to excite three imaging slices (i.e., \( MB = 3 \)), and the t-blipped SMS-MRF was simulated by adding 120° phase difference between the three slices, with an increment of 120° phase across all three slices from one TR to the next. We used the same set of spiral trajectories as in [22], which consists of 48 spiral interleaves. A single spiral interleave was acquired for each TR such that the in-plane acceleration is \( AF = 48 \). The \( k \)-space data were synthesized with the nonuniform fast Fourier transform [24], and the length of the MRF acquisition was set as \( M = 500 \).

We perform image reconstruction using the conventional approach in [7] and the proposed method. Figs. 1, 2, and 3 respectively show the reconstructed \( T_1, T_2 \) and spin density maps, along with the voxelwise normalized error maps. Here we also calculate the overall normalized root-mean-square error (NRMSE) for the reconstructed parameter maps, defined as \( \text{NRMSE} = \frac{\| \theta - \hat{\theta} \|_2}{\| \theta \|_2} \). Here \( \theta \) and \( \hat{\theta} \) respectively denote the true parameter and reconstructed parameter. As can be seen, the proposed method yields more accurate \( T_1, T_2, \) and spin density maps than the conventional approach, although the improvement is more pronounced for the \( T_2 \) and spin density maps. Qualitatively, the proposed method reduces the ringing and shading-like artifacts appearing in the \( T_2 \) and spin maps from the conventional approach. Clearly, due to the high slice acceleration (i.e., \( MB = 3 \)) and in-plane acceleration (i.e., \( AF = 48 \)), the conventional approach that simply combines the slice SENSE with dictionary matching could not fully resolve aliasing artifacts. In contrast, the proposed method, which integrates the advanced low-dimensional image model with parallel imaging, leads to substantial performance improvement.
4. CONCLUSION

In this paper, we present a new image reconstruction method based on low-rank and subspace modeling for SMS-MRF. With the proposed model, the image reconstruction problem is formulated as a convex optimization problem, for which a numerical algorithm based on variable splitting and the alternating direction method of multipliers is described. The performance of the proposed method is evaluated by numerical experiments, and the results demonstrate the improved accuracy provided by the proposed method.

In the future work, it is worth evaluating the performance of the proposed method with in vivo experiments. Moreover, note that the proposed method provides a general image reconstruction framework for SMS-MRF, for which a number of extensions can be performed. For example, the proposed method can incorporate with some specialized blipped spiral trajectory [25], and/or more flexible signal excitation scheme [9] for SMS-MRF data acquisitions. Additionally, we can integrate the proposed low-rank and subspace model with sparsity constraint [26], which could potentially lead to improved performance, although this will increase the computational cost.

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Fig. 1.
Reconstructed $T_1$ maps and associated error maps for SMS-MRF with SMS = 3 using the conventional approach and the proposed method. Note that the overall error is labeled at lower right corner of each error map, and that the skull and scalp were removed from each error map.
Fig. 2.
Reconstructed $T_2$ maps and associated error maps for SMS-MRF with SMS = 3 using the conventional approach and the proposed method. Note that the overall error is labeled at lower right corner of each error map, and that the skull and scalp were removed from each error map.
Fig. 3.
Reconstructed spin density maps and associated error maps for SMS-MRF with SMS = 3 using the conventional approach and the proposed method. Note that the overall error is labeled at lower right corner of each error map, and that the skull and scalp were removed from each error map.