Rubber friction on (apparently) smooth 

lubricated surfaces

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Abstract
We study rubber sliding friction on hard lubricated surfaces. We show that even if the hard 
surface appears smooth to the naked eye, it may exhibit short-wavelength roughness, which 
may make the dominant contribution to rubber friction. That is, the observed sliding friction is 
mainly due to the viscoelastic deformations of the rubber by the counterface surface asperities. 
The results presented are of great importance for rubber sealing and other rubber applications 
involving (apparently) smooth surfaces. 

(Some figures in this article are in colour only in the electronic version)

1. Introduction
Rubber friction on smooth surfaces is a topic of great practical 
importance, e.g., for rubber sealing, wiper blades or for the 
contact between a tire and the metal rim [1]. For perfectly 
smooth surfaces rubber friction is believed to be due to periodic 
cycles of pinning, elastic deformation, and rapid slip of rubber 
molecules [2–4] or, more likely, small patches [5] of the rubber 
at the sliding interface. In a recent publication, Vorvolakos and 
Chaudhury [6] (see also [7, 8]) have studied rubber friction 
for a silicone elastomer sliding on extremely smooth Si wafer, 
with the root-mean-square roughness ≈0.5 nm, covered by 
inert self-assembled monolayer films. The observed friction 
as a function of the sliding velocity exhibit a bell-like shape 
as expected from theory [2, 5]. However, a surface which 
appears smooth to the naked eye may exhibit strong surface 
roughness at short length scales, e.g., at the micrometer and 
nanometer length scale. This is true even for highly polished 
surfaces which may appear perfectly smooth to the naked 
eye. When a rubber block slides on a hard surface with 
surface roughness, a large contribution to the friction force 
may arise from the time-dependent, substrate asperity-induced 
deformations of the rubber surface. That is, during sliding the 
substrate asperities give rise to pulsating deformations of the 
rubber, which will result in energy dissipation because of the 
internal friction of the rubber. This is believed to be the major 
contribution to the tire-road friction [9, 10]. In this paper we 
will show that the roughness of a highly polished steel surface 
may also give the dominant contribution to the friction, even 
for lubricated surfaces. This result is very important for rubber 
sealing applications [11], in particular at low sliding velocities 
and low temperatures.

2. Rubber friction: experimental results
Friction tests have been carried out using a reciprocating 
tribometer where a steel cylinder (diameter \(D = 1.5\) cm and 
length \(L = 2.2\) cm) is squeezed against the substrate (rubber 
block, thickness 4 mm), see figure 1. The steel cylinder 
performs longitudinal oscillations against the rubber block 
with a stroke \(a = 1\) mm and frequency \(f = 50\) Hz. This gives 
the average slip velocity \(v \approx 0.1\) m s⁻¹. The rubber specimens 
(acronitrile butadiene rubber (NBR)) have been washed in 
industrial petroleum for 3 min by using an ultrasonic cleaner 
and then dried for 10 min. The rubber surface has the root-
mean-square roughness of \(\approx 0.4\) μm, and has parallel grooves 
caused during molding of elastomer sheets in steel mold. The 
steel cylinder has a root-mean-square roughness of \(\approx 0.1\) μm.

Figure 2 shows the power spectrum of the surface 
roughness of the steel surface. The power spectrum is defined 
by [12]

\[
C(q) = \int d^3x \langle h(x)h(0) \rangle e^{iq \cdot x} \tag{1}
\]

where \(\langle \cdot \rangle\) stands for ensemble averaging. Here \(h(x)\) is the 
surface height at the point \(x\), where we have assumed \(h(0) = 0\). The surface height was measured over different surface areas 
using atomic force microscopy and an optical method (3D 
optical surface profiler (Wyko NT 1100) in vertical scanning 
interferometry mode), and figure 2 was obtained from three
Figure 1. Test configuration for friction studies under reciprocating sliding conditions.

Figure 2. The power spectrum of the surface roughness of the steel surface. The root-mean-square surface roughness is about 0.1 μm. The straight line has a slope corresponding to the fractal dimension $D_f \approx 2.66$.

different measurements involving different resolution. The straight (green) line has a slope corresponding to the fractal dimension $D_f \approx 2.66$. In the calculations of the friction presented below we have used the linear approximation and included the surface roughness power spectra over the full wavevector range shown in the figure. Thus the longest and the shortest wavelength roughness included in the analysis is $\lambda_0 = \frac{2\pi}{q_0} \approx 0.3$ mm and $\lambda_1 = \frac{2\pi}{q_1} \approx 6$ nm.

The experimental results presented in figures 5 and 6 were obtained for the load $F_N = 100$ N and with a test duration of 15 min. Since the oscillation stroke is very small (1 mm) one expects that most of the oil is squeezed out from the steel cylinder–rubber contact region.

The viscoelastic modulus $E(\omega)$ has been measured (using Ep lexor 150) using a rectangular rubber block $5 \times 2 \times 30$ mm$^3$. The measurements were done in tension with 8% of prestrain and 1.3% of dynamic strain amplitude. Figure 3 shows the logarithm of the real part of the viscoelastic modulus as a function of the logarithm of the frequency $\omega$ for the temperatures $T = 50$ and 80°C. For acronitrile butadiene rubber.

Figure 3. The logarithm of (a) the real part and (b) the imaginary part of the viscoelastic modulus as a function of the logarithm of the frequency $\omega$ for the temperatures $T = 50$ and 80°C. For acronitrile butadiene rubber.

Figure 4. Steel cylinder squeezed in contact to a rubber substrate.

For $F_N = 100$ N and for $T \approx 50$°C we have (see figure 3) $E* \approx 10$ MPa (where we have assumed the frequency $\omega \approx 10^{-3}$ s$^{-1}$, corresponding to the contact time $\sim 1000$ s) giving $d \approx 0.4$ cm and $\bar{p} \approx 1$ MPa.

Figure 5 shows the measured friction coefficients for the steel cylinder sliding against non-aged rubber in 11 different lubrication oils with very different viscosities. Thus, for example, the PAO1 and PAO2 oils have the viscosities (at $T = 40$°C) $4.4 \times 10^{-3}$ and $22.8 \times 10^{-3}$ Pa s, respectively. In spite of the large difference in viscosities, the rubber friction coefficients are nearly equal. This indicates that the rubber friction is not (mainly) due to shearing a thin viscous layer, but due to the internal friction of the rubber (see below).
Figure 5. Coefficient of friction of non-aged samples in different base oils. For the load $F_N = 100$ N.

Figure 6. Coefficient of friction of aged samples in different base oils. For the load $F_N = 100$ N.

Figure 6 shows the measured friction coefficients for aged rubber. The aged rubber samples were prepared by immersing them in different base fluids at $T = 125^\circ$C for one week. NBR rubber has polar nitrile groups and non-polar oils such as naphthenic have nearly no effect on the properties of NBR rubber, and this explained why rubber aged in naphthenic exhibits nearly the same friction as for non-aged NBR rubber (compare figure 5 with figure 6). However, oils with polar groups, e.g. polyol ester, will diffuse into the rubber which may reduce the internal friction of the rubber. In addition, when the rubber block is squeezed against the counterface, oil may be squeezed out from the rubber matrix, giving a thicker oil film at the interface and thus lower the friction (a similar effect is believed to contribute to the extremely low friction exhibited by human joints [16]). We believe that both effects may contribute to why NBR rubber aged in polyol ester exhibits much smaller friction than the non-aged rubber.

Figures 7–9 show the friction coefficient for different loads and temperatures. Here the temperature refers to the background temperature, which was varied by contacting the back-side of the rubber block to a metal block with the given temperature. (The temperature in the sliding contact is not known, but will be higher due to the frictional heating.) Note that as the temperature increases the friction decreases. This cannot result from the change in viscosity of the lubricant oil since we already know from above that the lubricant viscosity has a negligible influence on the friction, at least for the squeezing force $F_N = 100$ N, see figure 5. However, we will show in section 3 that the temperature dependence of the sliding friction can be understood from the temperature dependence of the internal friction of the rubber. Thus, when the temperature increases the rubber becomes more elastic (less viscous) and the internal friction decreases.
Figure 7. Friction coefficient as a function of load at the background temperature $T = 25^\circ C$.

Figure 8. Friction coefficient as a function of load at the background temperature $T = 40^\circ C$.

Figure 9. Friction coefficient as a function of load at the background temperature $T = 80^\circ C$.

Figure 10 shows the friction coefficients (for the load $F_N = 100$ N) at $T = 40$ and $80^\circ C$ for the same base oil but with different additives. As expected, there is negligible dependence of the friction on the additives. The reason for this is the same as before: the observed friction is mainly due to the internal friction of the rubber which does not change between the different experiments. That is, although the additives in the base oil may adsorb on the solid surfaces and act as boundary lubricants, the result of the study above indicates that such (mono) layers have negligible influence on the friction.

3. Rubber friction: theory

We have calculated the dependence of the rubber friction on the sliding velocity and the temperature using the theory presented in [9]. The theory assumes that the friction is entirely due to the viscoelastic deformation of the rubber, which results from the pulsating deformations from the substrate asperities. The only inputs in the calculations are the counterface roughness power spectrum (see figure 2) and the rubber viscoelastic modulus. We have measured the viscoelastic modulus $E(\omega)$ of the rubber as a function of frequency (and temperature). In the calculations we do not take into account the lubrication oil directly (but it influences the friction indirectly by reducing (or removing) the adhesion between the solid walls [15]). We have assumed the nominal contact pressure of 1 MPa.

Neglecting the flash temperature, the friction coefficient is given by [9]

$$\mu = \frac{1}{2} \int dq \ g^3 C(q) P(q) \int_0^{2\pi} d\phi \ \cos\phi \ \text{Im} \left( \frac{E(q v \cos\phi)}{(1 - \nu^2)\sigma} \right)$$

where

$$P(q) = \frac{2}{\pi} \int_0^\infty dx \ \frac{\sin x}{x} \exp \left[ -x^2 G(q) \right] = \text{erf} \left( \frac{1}{2}\sqrt{G} \right)$$

with

$$G(q) = \frac{1}{8} \int_0^q dq \ g^3 C(q) \int_0^{2\pi} d\phi \ \left| \frac{E(q v \cos\phi)}{(1 - \nu^2)\sigma} \right|^2$$

where $\sigma$ is the perpendicular pressure (the load divided by the nominal contact area).
Figure 10. Friction coefficient for one base oil with several different additives and for $T = 40$ and $80 \degree C$. For the load $F_N = 100$ N.

Figure 11. The steady state kinetic friction coefficient calculated using the measured surface roughness power spectrum (from figure 2) and the measured viscoelastic modulus of the rubber. For the background temperatures 50 and 80\degree C, and the nominal squeezing pressure $p = 1$ MPa.

Figure 11 shows the steady state kinetic friction coefficient calculated using the measured surface roughness power spectrum (from figure 2) and the measured viscoelastic modulus of the rubber. Results are presented for the background temperatures 50 and 80\degree C. Note that the magnitude of the calculated friction coefficient at the sliding velocity $\sim 0.1$–1 m s$^{-1}$ is similar to what is observed experimentally, and also the temperature dependence is in good agreement with the measurements (see section 2).

In figure 12 we show (a) the friction coefficient $\mu_k$, and (b) the logarithm of the (normalized) contact area $A/A_0$ (where $A$ is the contact area observed at the highest magnification, and $A_0$ is the nominal or apparent contact area), as a function of the logarithm of the large-wavevector cut-off $q_1$ (in units of the low-wavevector cut-off $q_0$). In the calculations we only include surface roughness with wavevectors $q_0 < q < q_1$.

Results are presented for two different temperatures $T = 50$ and 80\degree C and for the sliding velocity $v = 1$ m s$^{-1}$.

The short-wavelength roughness is important in the present case is the large fractal dimension ($D_f \approx 2.7$) of the steel surface, which implies that the ratio between the amplitude and the wavelength of the surface roughness strongly increases as the wavelength decreases$^4$, and this makes the short-wavelength

$^4$ For a self affine fractal surface the ratio between the height $h(\lambda)$ and wavelength $\lambda$ of the surface roughness component with wavevector $q = 2\pi/\lambda$ is $h/\lambda \sim \lambda^{D_f-2}$. Thus the larger the fractal dimension $D_f > 2$, the faster the ratio $h/\lambda$ and will increase as the wavelength decreases, and this will tend to increase the importance of the short-wavelength roughness.
roughness much more important than the long-wavelength roughness.

4. Squeeze-out

We have argued above that the observed rubber friction can be explained as resulting from the viscoelastic deformations of the rubber by the countersurface asperities. In this section we briefly address the role of the lubrication oil. We first note that the oil will effectively eliminate the adhesive interaction between the rubber and the countersurface [15]. Most of the oil will be squeezed out from the steel–rubber contact area, but a molecular thin layer may remain even after long squeezing time.

Consider first a flat rigid rectangular block squeezed against a flat hard countersurface with the nominal (or average) pressure \( p \) in a lubrication fluid with the viscosity \( \eta \). The separation between the surfaces after the time \( t \) is (see figure 13) [16]

\[
h(t) \approx (\eta/2pt)^{1/2} d.
\]

Here \( d \) is the thickness of the bottom surface of the block and we assume that \( d \ll L \), where \( L \) is the length of the bottom surface of the block. With \( d \approx 0.4 \text{ cm} \), \( p \approx 1 \text{ MPa} \) and with \( t = 1000 \text{ s} \) we get with the typical viscosity \( \eta \approx 0.01 \text{ Pa s} \), \( h(t) \approx 4 \text{ nm} \). For surfaces with roughness the squeeze-out from asperity contact regions is even faster, but in this case some liquid may get 'trapped' in sealed off regions [17]. For non-aged rubber the trapped islands may disappear because of diffusion of lubricant oil into the rubber matrix, see figure 14. The shear stress developed in a fluid film with thickness \( h \) is \( \sigma = \eta v/h \). In the present case, if \( v = 0.1 \text{ m s}^{-1} \) and \( h = 10 \text{ nm} \) we get \( \sigma = 0.1 \text{ MPa} \) which would give a contribution to the friction coefficient of order \( \sigma/p \approx 0.1 \). However, the thickness of the oil film will be very non-uniform, and in many regions (cavity regions) at the interface the film may be much thicker than 10 nm (see below), and shearing the lubricant film in these regions will give a negligible contribution to the friction. In other regions, where the steel asperities make direct contact with the rubber, the local squeezing pressure is much higher than the average pressure, and in these regions at most a few monolayers of oil film will remain trapped. Nevertheless, since the region of direct wall–wall contact is only a small fraction of the nominal contact area, the contribution to the friction from shearing the confined thin layers appears to be negligible (see section 2).

Figure 15 shows the probability distribution \( P_u \) of surface separations \( u \).

Figure 15. The calculated probability distribution \( P_u \) of surface separations \( u \).

The calculated probability distribution \( P_u \) of surface separations \( u \). This function has been calculated as outlined in [18]. In the calculation we have assumed a rubber elastic modulus \( E = 100 \text{ MPa} \) which correspond to the temperature \( T = 40^\circ \text{C} \) and the perturbing frequencies \( \omega \approx 10^8 \text{ s}^{-1} \) (see figure 2), which is a typical perturbing frequency \( (\omega = qv) \) from surface roughness with wavevector \( q = 10^7 \text{ m}^{-1} \) and sliding velocity \( v = 0.1 \text{ m s}^{-1} \). In the calculation we have neglected the direct influence of the lubrication oil, but it is accounted for indirectly by neglecting the adhesive interaction between the rubber and the steel surface. Using \( P_u \) we can give a more accurate estimate of the contribution from the oil film to the shear stress. We get the viscous shear stress

\[
\sigma \approx \eta v \int_{u_c}^\infty \frac{du}{u} \tilde{P}_u
\]

where \( u_c \) is a cut-off length of order \( \sim 1 \text{ nm} \) since molecular thin lubrication films cannot be described by the continuum theory of fluid mechanics [17]. We note that \( P_u \) has a delta function at the origin \( u = 0 \), but in the present case this carries the weight \( A(\zeta_1)/A_0 \approx 0.01 \) and the contribution from the area of real contact to the friction force can be neglected. Using the calculated \( P_u \) (see figure 15), and assuming \( \eta = 0.01 \text{ Pa s} \) and \( v = 0.1 \text{ m s}^{-1} \), equation (5) gives \( \sigma \approx 0.06 \text{ MPa} \) so the contribution to the friction from the lubricant film is very small, of order 0.06 (where we have assumed the normal stress \( p = 1 \text{ MPa} \)). We note that this is likely to be an overestimation.
of the contribution of the oil film to the friction coefficient, as the oil film may tend to slightly increase the separation between the walls, and also because we have not accounted for the roughness on the rubber surface in the analysis.

5. Discussion

When a block of a viscoelastic solid, such as rubber, is sliding on a hard rough countersurface, the largest contribution to the sliding friction is usually derived from the time-dependent deformations of the rubber by the countersurface asperities. This is the case, for example, for the tire-road contact. Here we have shown that even a highly polished countersurface, which may appear mirror-smooth to the naked eye, may have enough surface roughness at short length scale to give a large contribution to rubber friction. This result has many important applications, e.g., in the context of rubber sealing.

In many rubber sealing applications the rubber surface and the (lubricated) countersurface are squeezed together for a long time before the slip events. Furthermore, during the onset and stop of sliding the slip velocities will be very small. This may result in nearly complete squeeze-out of the lubricant film. Thus, at some point in time slip will occur between what is effectively un lubricated surfaces. This may result in high friction and large wear, and perhaps failure of the seal with potentially serious consequences.

Note that with respect to sliding friction there is an asymmetry between roughness on the countersurface and on the rubber block. Thus, only roughness on the hard countersurface will contribute to the friction force. Roughness on the rubber surface may in fact lower the sliding friction by trapping lubrication fluid. On the other hand, with respect to stationary contact mechanics, roughness on the two surfaces plays a similar role [13, 19].

There is an important difference between rubber friction on very rough surfaces, such as a road surface, and rubber friction on smoother surfaces with only short-wavelength roughness. On very rough surfaces, as the magnification increases we observe smaller and smaller rubber-countersurfaceasperity contact regions, and the local stress and temperature will rapidly increase until the limit of strength of the rubber has been reached. For tread rubber in contact with road surfaces this limit is reached at the length scale (or resolution) \( \lambda_c \approx 1-10 \mu \text{m} \), and at this length scale during slip strong wear processes occur. The rubber friction on road surfaces can be explained by including the viscoelastic deformations of the rubber from road surface roughness with wavelength down to \( \lambda_c \). On the other hand, for surfaces with mainly short-wavelength roughness, such as the steel surface used in the present study, it may be necessary to include roughness with wavelength down to the molecular length scale, e.g., the distance between cross links in the rubber which typically is of order a few nanometers. This may result in different wear mechanisms and wear rates than on surfaces with large long-wavelength roughness.

The results presented in this paper may also be relevant for the adhesion and locomotion of some animals on rough substrates. Thus, some animals, such as grasshoppers and tree frogs, have smooth attachment pads built from a (non-compact) material which is highly viscoelastic (like rubber) [20]. Furthermore, the toe pad–substrate contact region is wet (lubricated) with a liquid injected into the contact area by the animal. The liquid viscosity, the nominal squeezing pressure, and the size and shape of the contact area differ from the lubricated rubber–counterface contact problem studied above, but some of the results presented above may nevertheless be relevant for the animal toe pad–substrate interaction problem [21, 22].

6. Summary and conclusion

We have presented a combined experimental–theoretical study of rubber sliding friction against hard lubricated surfaces. We have shown that even if the hard surface appears smooth to the naked eye, it may exhibit short-wavelength roughness, which may give the dominant contribution to rubber friction. The presented results may be of great importance for rubber sealing and other rubber applications involving (apparently) smooth surfaces.

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