The Influence of Magnetic Anisotropy on the Kondo Effect and Spin-Polarized Transport through Magnetic Molecules, Adatoms and Quantum Dots

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Transport properties in the Kondo regime of a nanosystem displaying uniaxial magnetic anisotropy (such as a magnetic molecule, magnetic adatom or quantum dot coupled to a localized magnetic moment) are analyzed theoretically. In particular, the influence of spin-polarized transport through a local orbital of the system and exchange coupling of conduction electrons to the system’s magnetic core on the Kondo effect is discussed. The numerical renormalization group method is applied to calculate the spectral functions and linear conductance in the case of the parallel and antiparallel configurations of the electrodes’ magnetic moments. It is shown that both the magnetic anisotropy as well as the exchange coupling between electrons tunneling through the conducting orbital and magnetic core play an important role in formation of the Kondo resonance, leading generally to its suppression. Specific transport properties of such system appear also as a nontrivial behavior of tunnel magnetoresistance. It is also shown that the Kondo effect can be restored by an external magnetic field in both the parallel and antiparallel magnetic configurations.

I. INTRODUCTION

Growing trend towards building ever more efficient and smaller electronic devices inevitably draws the researchers’ attention to nanoscopic hybrid systems. In this respect, single atoms or molecules seem to be promising prospects, as their incorporation into electronic nanodevices allows for developing novel systems capable of performing strictly imprinted functions among which information storage is of key interest. Consequently, due to recent advances in experimental techniques enabling to address transport through individual atoms and molecules, both natural as well as artificial (quantum dots) systems exhibiting magnetic anisotropy, such as magnetic atoms of spin $S > 1/2$ (i.e. Fe, Co or Mn)1–5 or single-molecule magnets (SMMs)6–9 have become the object of intensive studies.

It has been suggested, and in the case of magnetic adatoms also experimentally proven that magnetic state of such systems can be controlled by the use of spin-polarized currents or spin bias. This practically means that the system’s magnetic moment can be switched between two metastable states of minimal energy by only applying an electric/spin current pulse of a proper amplitude. Furthermore, if attached to two metallic nonmagnetic electrodes a SMM can act as a spin filter. If, however, coupled to electrodes characterized by unequal spin polarizations, the molecule can reveal transport characteristics typical of a spin diode. Most of these results have been obtained in the limit of weak coupling between a SMM and reservoirs of spin-polarized electrons. Nevertheless, in some situations, when mixing of localized electron states responsible for transport properties of the molecule and extended electron states in electrodes is significant, such an assumption not necessarily has to be correct.

In the strong coupling regime the electronic correlations can lead to an additional resonance in the density of states at the Fermi level of electrodes, known as the Kondo-Abrikosov-Suhl resonance. Since the end of the 1990s, the presence of the Kondo effect has been successively demonstrated in a large variety of nanoscopic objects like quantum dots magnetic adatoms, nanotubes and different types of molecules: Co(II)-based coordination complexes, di-vanadium molecules and $C_{60}$ molecules attached to gold or ferromagnetic nickel electrodes. However, in the case of nanosystems characterized by large spins the prominent role of the magnetic anisotropy in formation of the Kondo effect has been experimentally established only very recently. It turned out that the Kondo effect can be then tuned by changing both the orientation (e.g. by controlling the adatom’s local environment) and magnitude (e.g. by mechanical straining of the molecule) of the magnetic anisotropy. Moreover, Parks et al. were able to tune the anisotropy constant continuously and to modify accordingly the energy spectrum underlying the Kondo state. As a result, they managed to observe a crossover from the fully screened to underscreened Kondo effect. It is worthy of note that more recently electric field control of magnetic anisotropy has been experimentally established for a SMM embedded into a planar three-terminal device. Although a few theoretical works focused on transport related issues in SMMs in the Kondo regime have been already published, experimental evidence of the Kondo effect in transport through SMMs has been found only very recently.

The earlier works on the Kondo phenomenon in transport through SMMs have been primarily focused on the role of transversal magnetic anisotropy, and hence also on the role of quantum tunneling of the SMM’s spin in the
formation of the Kondo state. It has been shown that the interplay of quantum tunneling and spin exchange processes between the molecule and tunneling electrons may result in the pseudo-spin 1/2 Kondo effect. Furthermore, it was soon realized that when even a moderate transverse magnetic field is applied, any qualitative difference between the mechanisms of the Kondo effect for molecules with half- and full-integer spins cease to exist. Mapping of the Anderson-type Hamiltonian describing a SMM onto the spin-1/2 anisotropic Kondo Hamiltonian led to the conclusion that, depending on whether the molecule’s total spin is reduced or augmented in the singly charged state, the coupling in the Kondo Hamiltonian is antiferromagnetic or ferromagnetic, respectively. In the former case the Kondo effect is revealed, whereas in the latter one no resonance at the Fermi level is present due to renormalization of the transverse coupling to zero. In addition, the Kondo effect is expected to oscillate as a function of the magnitude of the transverse coupling to zero. In addition, the Kondo effect for molecules with half- and full-integer spins cease to exist. Therefore, it was soon realized that when even a moderate transverse magnetic field is applied, any qualitative difference between the mechanisms of the Kondo effect for molecules with half- and full-integer spins cease to exist. Mapping of the Anderson-type Hamiltonian describing a SMM onto the spin-1/2 anisotropic Kondo Hamiltonian led to the conclusion that, depending on whether the molecule’s total spin is reduced or augmented in the singly charged state, the coupling in the Kondo Hamiltonian is antiferromagnetic or ferromagnetic, respectively. In the former case the Kondo effect is revealed, whereas in the latter one no resonance at the Fermi level is present due to renormalization of the transverse coupling to zero. In addition, the Kondo effect is expected to oscillate as a function of the magnitude of the transverse field due to the Berry-phase periodical modulation of the tunnel splitting. Finally, the nonequilibrium spin dynamics of a SMM, triggered by a sudden change in the magnetic field amplitude has been studied, with the main emphasis on the time evolution of the Kondo screening.

Since physical mechanisms governing Kondo correlations in spin-polarized transport through nanoscopic systems exhibiting the magnetic anisotropy, such as magnetic adatoms or SMMs, are still at the early stage of research, the objective of the present paper is to provide further insight into the problem. In particular, we investigate how magnetic anisotropy affects the system’s transport characteristics such as conductance and tunnel magnetoresistance (TMR) in the linear response regime. To properly describe the transport properties in the strong coupling regime, we employ the Wilson’s numerical renormalization group (NRG) approach. This method is known as very powerful and essentially exact in solving quantum impurity problems.

The paper is organized as follows. In Sec. II we describe the model Hamiltonian used in calculations and provide a brief introduction to the NRG method. Numerical results and their discussion are given in Sec. III, where we analyze the spectral functions of the orbital level as well as the conductance and tunnel magnetoresistance (TMR) in the linear response regime. The above quantities are analyzed as functions of the orbital level position, strength and type of exchange coupling, and the anisotropy constant. In addition, we also discuss the effect of external magnetic field. Finally, the summary and conclusions are given in Sec. IV.

II. THEORETICAL DESCRIPTION

A. Model

We consider a generic theoretical model that allows for capturing essential features of quantum objects such as magnetic adatoms, quantum dots coupled to localized magnetic moments, and SMMs, see Fig. 1. It is assumed that electronic transport takes place via a single local orbital level (OL) of the system (conducting orbital of a SMM, adatom or quantum dot), which is coupled to electrodes. Moreover, the OL is also exchange-coupled to the corresponding magnetic core. Without loss of generality, we will henceforth refer to the systems under investigation as magnetic quantum dots (MQDs).

The total Hamiltonian of a MQD coupled to external leads can be written as

$$\mathcal{H} = \mathcal{H}_{\text{MQD}} + \mathcal{H}_{\text{leads}} + \mathcal{H}_{\text{tun}}. \quad (1)$$

The first term represents the MQD and has the form

$$\mathcal{H}_{\text{MQD}} = -DS_z^2 + \sum_{\sigma=\uparrow,\downarrow} \varepsilon n_{\sigma} + U n_{\uparrow} n_{\downarrow} - J_S \cdot \mathbf{S} + B_z (S_z + s_z), \quad (2)$$

where $D$ stands for the uniaxial anisotropy constant of the MQD, while $S_z$ denotes the $z$th component of the MQD’s internal spin operator $\mathbf{S}$. Since in the present paper we focus only on systems displaying magnetic bistability, the anisotropy constant is assumed to be positive ($D > 0$). Furthermore, $n_{\sigma} = c_{\sigma}^\dagger c_{\sigma}$ is the OL occupation operator, where $c_{\sigma}$ ($c_{\sigma}^\dagger$) creates (annihilates) a spin-\(\sigma\) electron of energy $\varepsilon$ in the OL. The Coulomb energy of two electrons of opposite spins occupying the OL is given by $U$. The penultimate term of Eq. (2) accounts...
for exchange coupling between the magnetic core of a MQD and the spin of an electron in the OL, represented by $s = \frac{1}{2} \sum_{\sigma} c_{\sigma}^\dagger c_{\sigma}$, where $\sigma = (\sigma^x, \sigma^y, \sigma^z)$ is the Pauli spin operator. The J-coupling can be either of ferromagnetic ($J > 0$) or antiferromagnetic ($J < 0$) type. Finally, the last term of Eq. (2) describes the Zeeman interaction of the MQD with an external magnetic field $B = (0,0,B_z)$ oriented along the easy axis of a MQD. Note that we put here $g\mu_B = 1$.

The ferromagnetic metallic electrodes, to which a MQD is coupled through the OL, are characterized by noninteracting itinerant electrons with the dispersion relation $\varepsilon_{k\sigma}$, where $q$ indicates either left ($q = L$) or right ($q = R$) electrode, $k$ denotes a wave vector and $\sigma$ is a spin index of an electron. Thus, the leads’ Hamiltonian is given by

$$\mathcal{H}_{\text{leads}} = \sum_{q=L,R} \sum_{k} \sum_{\sigma = \uparrow, \downarrow} \varepsilon_{k\sigma} c_{k\sigma}^\dagger a_{k\sigma} a_{k\sigma},$$

(3)

with $a_{k\sigma}^\dagger$ ($a_{k\sigma}$) being the relevant electron creation (annihilation) operator. At this point, it should also be mentioned that in the present paper we limit the discussion to collinear (parallel and antiparallel) configurations of electrodes’ magnetic moments. Furthermore, the MQD’s easy axis is assumed to be collinear with these moments as well. Finally, electron tunneling processes between the MQD and electrodes are included in the term $\mathcal{H}_{\text{tun}}$,

$$\mathcal{H}_{\text{tun}} = \sum_{q=L,R} \sum_{k} \sum_{\sigma = \uparrow, \downarrow} T_{q\sigma}^R c_{q\sigma}^\dagger a_{k\sigma} + \text{H.c.}$$

(4)

where $T_{q\sigma}^R$ denotes the tunnel matrix element between the OL and the $q$th lead.

In the linear response regime, it is numerically convenient to introduce the following canonical transformation $\sum_{\sigma = \uparrow, \downarrow}$

$$\begin{pmatrix} a_{k\sigma}^\dagger \\ a_{k\sigma} \end{pmatrix} = \frac{1}{\sqrt{\mathcal{V}_{k\sigma}}} \begin{pmatrix} T_{q\sigma}^L \\ T_{q\sigma}^R \end{pmatrix} \begin{pmatrix} a_{q\sigma}^\dagger \\ a_{q\sigma} \end{pmatrix},$$

(5)

where, $\mathcal{V}_{k\sigma} = \sqrt{|T_{q\sigma}^L|^2 + |T_{q\sigma}^R|^2}$, and the label $e$ ($o$) denotes the even (odd) combination of the leads operators. Such a rotation in the space of the left-right electron operators results in separation of the total Hamiltonian, Eq. (1), into two independent parts. The first one involves the OL coupled to a single electron reservoir described by the even linear combination of the leads’ electron operators, $a_{q\sigma}^\dagger$, while the other one is related with non-interacting electrons decoupled from MQD and described by the odd operators $a_{q\sigma}$. Consequently, the tunneling Hamiltonian can be written as

$$\mathcal{H}_{\text{tun}} = \sum_{q} \sum_{\sigma = \uparrow, \downarrow} \mathcal{V}_{q\sigma} \begin{pmatrix} a_{q\sigma}^\dagger c_{\sigma} + c_{\sigma}^\dagger a_{q\sigma} \end{pmatrix},$$

(6)

with $\mathcal{V}_{q\sigma}$ being effective OL-lead tunneling matrix elements. In the following we assume that the full spin-dependence is taken into account through the matrix elements $\mathcal{V}_{q\sigma}$ \cite{56}. For simplicity, we assume a flat conduction band in the interval $[-W,W]$, so that $\rho_\sigma(\omega) = \frac{\rho}{4\pi}$, with $W$ representing the cut-off energy of the system and $W = 1$ taken as the energy unit. Finally, the energy dependence of $\nu_{k\sigma}$ is neglected, $\nu_{k\sigma} \equiv \nu_n$ \cite{57}.

Under these circumstances, the overall effect of the ferromagnetic reservoir on the MQD is completely determined by the hybridization function $\Gamma_{\sigma}$,

$$\Gamma_{\sigma} = \pi \rho |\nu_{\sigma}|^2.$$ 

(7)

**B. Method of calculations**

In order to determine transport properties in the strong coupling regime, we use the Wilson’s numerical renormalization group method \cite{32,54,55}. The NRG technique consists of logarithmic discretization of the conduction band (with a discretization parameter $\Lambda > 1$) into intervals $[-\Lambda^{-n+1}W, \Lambda^{-n}W]$ and $[-\Lambda^{-n}W, -\Lambda^{-n+1}W]$ for $n = 0, 1, 2, 3, \ldots$, which allows for resolving transport properties on energy scales logarithmically approaching the Fermi level. After having discretized the conduction band, such a model is mapped onto a semi-infinite chain, whose first site is coupled to the impurity (in our case the MQD). The Hamiltonian then reads \cite{32,55,57}

$$\mathcal{H} = \mathcal{H}_{\text{MQD}} + \sum_{n=0}^{\infty} \sum_{\sigma = \uparrow, \downarrow} \sqrt{\rho} \left[ c_{f_n\sigma} f_{\sigma} + f_{\sigma}^\dagger c_{f_n\sigma} \right]$$

$$+ \sum_{n=0}^{\infty} \sum_{\sigma = \uparrow, \downarrow} t_n \left[ f_{n-1\sigma}^\dagger f_{n+1\sigma} + f_{n+1\sigma}^\dagger f_{n\sigma} \right].$$

(8)

The operators $f_{n\sigma} (f_{n\sigma}^\dagger)$ correspond to the $n$th site of the Wilson chain, with exponentially decaying hopping matrix elements $t_n$ between neighboring sites of the chain \cite{57}. As a consequence, by adding consecutive sites, one is able to access transport at lower and lower energy scales. In this way the method generally provides a non-perturbative description of the crossover from a free magnetic impurity at high temperatures to a screened spin at low temperatures. \cite{57} The Hamiltonian (8) can be solved iteratively by adding consecutive sites of the chain. This procedure allows for resolving static and dynamic properties of the system at energy scale $\Lambda^{-n/2}$, with $n$ being a given iteration.

Since the NRG calculations may in general pose a serious numerical challenge, it becomes essential to take advantage of as many available symmetries of the system’s Hamiltonian as possible. To efficiently address the present problem, we have employed the flexible density-matrix numerical renormalization group (DM-NRG) code \cite{58} which can exploit an arbitrary number of both Abelian and non-Abelian symmetries. \cite{In the case under discussion, the $U_{\text{charge}}(1) \times U_{\text{spin}}(1)$ symmetry of the model has been used, so that the $z$th component of the total spin,

$$S_z = S_z^{\dagger} + \frac{1}{2} \sum_{n=0}^{\infty} \left( f_{n\uparrow}^\dagger f_{n\downarrow} - f_{n\downarrow}^\dagger f_{n\uparrow} \right),$$

(9)
where \( S'_z = S_z + s_z \), as well as the total charge
\[
\tilde{Q}^{\uparrow} = \sum_{\sigma} c^\dagger_{\sigma} c_{\sigma} - 1 + \sum_{n=0}^{\infty} \left( \sum_{\sigma} f^\dagger_{n\sigma} f_{n\sigma} - 1 \right).
\]

served as quantum numbers according to which the states of the Hamiltonian were classified during computation. Finally, the discretization parameter \( \Lambda = 1.8 \) has been taken in calculations, and we have kept 2000 states after each step of the iteration.

The central quantity of interest is the OL spin-dependent spectral function\(^{55,65}\)
\[
A_\sigma(\omega) = -\frac{1}{\pi} \text{Im} \langle \langle c_\sigma | c^\dagger_\sigma \rangle \rangle_\omega,
\]

where \( \langle \langle c_\sigma | c^\dagger_\sigma \rangle \rangle_\omega \) denotes the Fourier transform of the retarded Green's function \( \langle \langle c_\sigma | c^\dagger_\sigma \rangle \rangle_\omega = -i\theta(t) \langle \langle c_\sigma(t), c^\dagger_\sigma(0) \rangle \rangle \) of the orbital level. Some technical details concerning calculation of the spectral function can be found in Appendix A.

Having found the spectral function, one can determine the linear response conductance \( g \) from the Landauer-Wingreen-Meir formula\(^{66-69}\) which at \( T = 0 \) yields
\[
g = \pi \sum_\sigma 2\Gamma^L_\sigma \Gamma^R_\sigma \cdot A_\sigma(\omega = 0) \quad \text{(in units of } 2e^2/\pi),
\]

with \( \Gamma^L_\sigma(\pm) = \frac{\Gamma}{2}(1 \pm P) \) and \( \Gamma^R_\sigma(\pm) = \frac{\Gamma}{2}(1 \pm P) \) for the parallel magnetic configuration of electrodes, while \( \Gamma^L_\sigma(\mp) = \frac{\Gamma}{2}(1 \pm P) \) and \( \Gamma^R_\sigma(\mp) = \frac{\Gamma}{2}(1 \mp P) \) for the antiparallel one. We assumed that both electrodes are made of the same material and \( P \) denotes their spin polarization. The effective coupling between the MQD and the reservoir for the parallel magnetic configuration is \( \Gamma^P_\sigma(\mp) = \Gamma(\pm P) \), while for the antiparallel one \( \Gamma^{AP}_\sigma(\mp) = \Gamma \), with \( \Gamma = (\Gamma^L_\sigma + \Gamma^R_\sigma)/2 \). Note that in the case of left-right symmetric systems, \( \Gamma^{AP}_\sigma(\mp) \) is independent of \( \sigma \) in the antiparallel configuration, and hence the system behaves effectively as coupled to nonmagnetic leads. As a result, the linear spin-resolved conductance (in units of \( 2e^2/\pi \)) in the two magnetic configurations is given by
\[
\begin{align*}
g^P_{\mp}(\omega) &= \frac{\pi}{2}(1 \pm P) \Gamma_{\mp}^P(\omega = 0), \\
g^{AP}_{\mp}(\omega) &= \frac{\pi}{2}(1 - P^2) \Gamma_{\mp}^{AP}(\omega = 0),
\end{align*}
\]

with \( A^{AP}_\sigma \) being the spectral function in the respective magnetic configuration.

### III. Numerical Results and Discussion

Transport characteristics of the system, such as the linear-response conductance \( g \) and tunnel magnetoresistance (TMR), have been numerically calculated for a hypothetical MQD characterized by the spin number \( S = 2 \).

Since the key feature of the transport regime under discussion is the presence of the Kondo resonance, it is convenient to introduce the Kondo temperature \( T_K \) as the most relevant energy scale for the system, to which other energy parameters will be related, if necessary. In the present work, the Kondo temperature \( T_K \) is estimated from the half-width at half-maximum of the Kondo resonance in spectral function at \( T = 0 \) for \( J = 0 \) and \( P = 0.22 \). We note here that, for the sake of simplicity, we assume \( k_B = 1 \), i.e. temperatures are also given in units of energy. As a result, for the parameters used in Fig. 2 we get \( T_K/W \approx 5 \times 10^{-4} \) \( (T_K/G \approx 0.022) \).

Before presenting and discussing numerical results, it is worth recalling that the Kondo effect appears as a result of spin exchange processes in the OL due to its strong coupling to electrodes. This coupling is described here by the effective hybridization parameter \( \Gamma \), which introduces the Kondo temperature \( T_K \) as the relevant energy scale. However, the model considered provides also another independent physical mechanism (channel) through which the Kondo effect can be modified, i.e. the exchange interaction \( J \) between an electron in the OL and the MQD's magnetic core. Therefore, one can expect the ratio of the \( J \)-coupling and the Kondo temperature \( T_K \) to be the key parameter controlling whether the Kondo resonance will appear or not. Indeed, we show below that the electronic correlations between the OL and electrodes effectively result in formation of the Kondo resonance only if \( |J| \lesssim T_K \).

In order to see how the parameters of the system, especially the \( J \)-coupling and the magnetic anisotropy \( D \), influence the transport properties, we first calculate and discuss the relevant spectral functions.

#### A. Spectral functions

In the following will we analyze dependence of the spectral functions of the OL on some essential parameters of the system. Figure 2 shows the normalized spin-resolved spectral functions \( \pi \Gamma_\sigma A_\sigma(\omega) \) as a function of the OL energy \( \omega \) in the antiparallel and parallel magnetic configurations for \( |J|/T_K \approx 2 \). In the antiparallel configuration the spectral functions for both spin components are equal. In the parallel configuration, on the other hand, the main contribution comes from the spin-up electrons which are the majority ones. In both configurations and for both types of exchange coupling, the spectral functions show clear resonances associated with degeneracy of the neighboring charge states – compare the boundaries between regions corresponding to different \( Q \), where \( Q \) denotes the average number of electrons occupying the OL. In the singly-occupied regime, \( Q = 1 \), the Kondo effect due to hybridization of the OL spin with the conduction electrons of the leads should be present. However, there are two ingredients that may generally suppress the Kondo resonance: the exchange coupling \( J \) and the exchange field due to the presence of ferromagnetic leads. Since the results in Fig. 2 are shown for \( |J|/T_K \approx 2 \), only the remi-
Figure 2. (Color online) Normalized spin-resolved orbital level (OL) spectral functions, $\pi \Gamma_{\sigma} A_{\sigma}(\omega)$, shown as a function of the OL energy $\varepsilon$ in the antiparallel (a)-(b) and parallel (c)-(f) magnetic configurations. Top panel corresponds to the case of ferromagnetic ($J > 0$) coupling between electrons in the OL and MQD’s magnetic core, while the bottom one presents results for the antiferromagnetic coupling. The variable $Q$ denotes the average number of electrons occupying the OL. The parameters are: $U/W = 0.3$, $D/U \approx 1.7 \cdot 10^{-4}$ ($D/T_K = 0.1$), $\Gamma/U \approx 0.075$, $|J|/\Gamma \approx 0.044$ ($|J|/T_K \approx 2$), $B_z = 0$, and $P = 0.5$. Note that the spectral functions are presented in a logarithmic scale.

In the antiparallel configuration, the resultant coupling is the same for the spin up and spin down when the system is left-right symmetric. Consequently, there is no exchange field and we observe a well-pronounced peak in the spectral function at the Fermi level also outside the particle-hole symmetric point.

The height of the Kondo peak becomes reduced with the increase of $|J|$, and for $|J| \gg T_K$ the peak almost completely vanishes. We note that the disappearance of the resonance is faster in the case of the antiferromagnetic coupling ($J < 0$), see Figs. (b,d,f). Furthermore, as the $J$-coupling grows, some additional features in the spectral functions emerge. Apart from the Hubbard peak originating from the Coulomb repulsion of two electrons in the OL level, there are two additional resonances for $J > 0$, marked as dashed lines A and B in Fig. (a), and one resonance for $J < 0$, line C in Fig. (b). Interestingly, position of one of the two resonances for $J > 0$ remains roughly independent of energy (line A), whereas the other resonance moves towards larger energies as $J$ increases (line B), see Fig. (a).

Some insight into physical origin of the resonances A, B and C can be gained by considering the lowest energy states of a free-standing MQD with one extra electron in the OL, see Figs. (g,h). First, we note that the consequence of exchange interaction between an electron in OL and magnetic core is a decomposition of the molecular magnetic states into two spin-doublets, corresponding

Let us now analyze how the shape of spectral functions in the Kondo regime evolves when the exchange interaction between electrons in the OL and the MQD’s core is turned on gradually, see Figs. (a)-(f). Note that whenever we consider behavior of the system in the particle-hole symmetric point, i.e. for $\varepsilon = -U/2$, only the range of positive energies is presented. As one might expect, the behavior of the system for small values of $|J|$, i.e. $|J| \ll T_K$, resembles that of a single-level quantum dot, and a well defined and pronounced Kondo peak in the antiparallel configuration of the electrodes’ magnetic moments is observed for $\omega \leq T_K$, see Figs. (a)-(b). In the parallel configuration, on the other hand, spin-dependent coupling to the electrodes acts as an effective exchange field leading to spin splitting of the OL. This in turn results in suppression of the Kondo effect, except for the particle-hole symmetric point, $\varepsilon = -U/2$, as shown in Figs. (c)-(f), where the effective exchange field vanishes.

niscent of the Kondo effect can be observed. The suppression of the Kondo resonance is especially visible for the antiferromagnetic coupling ($J < 0$). Moreover, while in the case of ferromagnetic coupling ($J > 0$) some residual Kondo resonance can still be visible for the energy corresponding to the particle-hole symmetry ($\varepsilon = -U/2$), the resonance is practically absent for the antiferromagnetic coupling, though some side resonances appear. The origin of these additional features will be discussed further in the text.
to $S + 1/2$ and $S - 1/2$. In addition, the sign of the coupling parameter $J$ determines which of the two multiplets has lower energy. Since we focus exclusively on the case of $T = 0$, it is justified to take into account only the relevant low energy states in both spin-multiplets. These are presented in Figs. 3g,h, where the zero-field ($B_z = 0$) energy of states $|\pm \frac{3}{2}\rangle^\pm$, and $|\pm \frac{3}{2}\rangle^\pm$ is presented as a function of the coupling parameter $J$. The superscript $\pm$ at the states $|\pm \frac{3}{2}\rangle^\pm$ is used to distinguish between states of higher $(+)$ and lower $(-)$ energy. We note that the state $|\pm \frac{3}{2}\rangle^-$ belongs to the spin-multiplet corresponding to $S+1/2$, while for $J > 0$ the state $|\pm \frac{3}{2}\rangle^-\ldots$ belongs to the multiplet $S+1/2$ and the state $|\pm \frac{3}{2}\rangle^+$ to the multiplet $S-1/2$ (note we assumed $S = 2$). For $J < 0$, the situation is opposite, i.e. $|\pm \frac{3}{2}\rangle^-$ belongs to the multiplet $S-1/2$ whereas the state $|\pm \frac{3}{2}\rangle^+$ to the multiplet $S+1/2$. In the absence of external magnetic field the MQD’s states of interest take the form

$$
\begin{align*}
\left|S_z^J = \pm \frac{5}{2}\right> &= |\uparrow(\downarrow)\rangle^\text{OL} \otimes |\pm 2\rangle^\text{core}, \\
\left|S_z^J = -\frac{3}{2}\right> &= \pm A^\pm_{\pm^{3/2}} \downarrow \text{OL} \otimes |\pm 2\rangle^\text{core} \\
&\quad + B^\pm_{\pm^{3/2}} \uparrow \text{OL} \otimes |\mp 2\rangle^\text{core}, \\
\left|S_z^J = +\frac{3}{2}\right> &= \pm A^\pm_{\pm^{1/2}} \uparrow \text{OL} \otimes |\pm 2\rangle^\text{core} \\
&\quad + B^\pm_{\pm^{1/2}} \downarrow \text{OL} \otimes |\mp 2\rangle^\text{core},
\end{align*}
$$

with $|\bullet\rangle^\text{OL}(\text{core})$ denoting the spin state of OL (magnetic core). The coefficients $A^\pm_m = A^\pm \exp[\iota \phi^\pm_m]$ and $B^\pm_m = B^\pm \exp[\iota \gamma^\pm_m]$ can be regarded as effective Clebsch-Gordan coefficients, which are nontrivial functions of the system’s parameters $J$ and $D$. Here, $\phi^\pm_m$ and $\gamma^\pm_m$ are relevant phase factors. As above, the superscript $\pm$ is used to distinguish between states of higher $(+)$ and lower $(-)$ energy. It is worth emphasizing that, to some extent, the situation under consideration is similar to the case of a quantum dot subjected to an external magnetic field which leads to splitting of the Kondo resonance. However, in the case of a simple quantum dot in a magnetic field there are two energy levels, whereas the energy structure of a MQD is much more complex, even in zero field. Moreover, except for the states $|\pm \frac{3}{2}\rangle$, all MQD’s states for $Q = 1$ correspond to an electron in the OL being in the superposition of spin-up and spin-down states.

Let us now discuss cotunneling processes leading to the resonances for ferromagnetic (FM) exchange coupling $(J > 0)$, the top panel of Fig. 3. We emphasize that now we consider the regime of large $J$ (i.e. $J > T_K$ and $J < \Gamma$), where the zero-energy resonance is absent and only side resonances (lines A and B) appear. Assume that initially the molecule occupies the state $|\pm \frac{3}{2}\rangle$. Due to spin-flip cotunneling processes, the MQD can be excited to one of the two states: $|\pm \frac{3}{2}\rangle^-\ldots$ (resonance A) and $|\pm \frac{3}{2}\rangle^+\ldots$ (resonance B), see Fig. 3g. Taking into account the energy spectrum, one can estimate the corresponding energy gaps for $|J| > D$ as (exact formulas in Appendix B)

$$
\begin{align*}
\Delta_1^\text{FM} &\approx 2SD \left[ 1 - \frac{2(|J| - D)}{(2S + 1)(|J| - 2D)} \right], \\
\Delta_2^\text{FM} &\approx \frac{2S + 1}{2} |J|.
\end{align*}
$$

Thus, the resonance corresponding to the line A in Fig. 3a is related to transitions characterized by the energy gap $\Delta_1^\text{FM}$, while the resonance indicated by the line B is associated with the gap $\Delta_2^\text{FM}$. Moreover, one can note that $\Delta_2^\text{FM}$ depends linearly on $J$, whereas $\Delta_1^\text{FM}$ only slightly changes with $J$.

The picture presented above for $J > 0$ alters only slightly when the exchange coupling changes to the antiferromagnetic (AFM) one $(J < 0)$, see Figs. 3b,d.f.
Spin-flip cotunneling processes can excite the MQD to one transition on the uniaxial anisotropy constant $D$. Variation of the OL spectral functions with $D$ is shown in Fig. 4 for a specific value of $|J|/T_K \approx 2$. Since $|J| > T_K$, the zero-energy Kondo resonance is practically absent, and only side resonances are visible. These resonances – marked in Figs. 4(a)-(b) by letters A, B and C – correspond to the relevant resonances in Figs. 3(a)-(b).

Especially interesting seems to be the case of $J > 0$, where two resonances (A and B) emerge at $D \approx T_K$. By a closer inspection of Fig. 4(g) one finds that this takes place when the condition $D > J/2$ is satisfied. However, it should be noted that according to our definition of the Kondo temperature, the relation $D > J/2 \approx T_K$ is only coincidental, and thus valid just for the current set of parameters. Moreover, in the limit $D \gg |J|$ the energy gaps introduced above can be estimated as

$$
\Delta_{1}^{\text{AFM}} \approx \Delta_{2}^{\text{AFM}} \approx \frac{2S+1}{2}|J|.
$$

As a consequence, only the resonance denoted by the line C is then visible in Fig. 4(b). Physical origin of the resonances in the parallel magnetic configuration, Figs. 4(c)-(e) and (d)-(f), can be accounted for in a qualitatively similar way. Finally, weak vertical lines visible in Fig. 3 for $\omega = U$, correspond to the resonance between singly occupied and empty OL.

As shown above, the exchange coupling of electrons in the OL and magnetic core modifies the energy spectrum of a MQD, and hence affects the Kondo effect. However, it has been demonstrated experimentally that the energy spectrum can also be modified by changing the anisotropy constant $D$. Variation of the OL spectral functions with $D$ is shown in Fig. 4 for a specific value of $|J|/T_K \approx 2$. Since $|J| > T_K$, the zero-energy Kondo resonance is practically absent, and only side resonances are visible. These resonances – marked in Figs. 4(a)-(b) by letters A, B and C – correspond to the relevant resonances in Figs. 3(a)-(b).

Especially interesting seems to be the case of $J > 0$, where two resonances (A and B) emerge at $D \approx T_K$. By a closer inspection of Fig. 4(g) one finds that this takes place when the condition $D > J/2$ is satisfied. However, it should be noted that according to our definition of the Kondo temperature, the relation $D > J/2 \approx T_K$ is only coincidental, and thus valid just for the current set of parameters. Moreover, in the limit $D \gg |J|$ the energy gaps introduced above can be estimated as

$$
\Delta_{1}^{\text{AFM}} \approx \frac{2S+1}{2}|J|,
$$

$$
\Delta_{2}^{\text{AFM}} \approx \frac{(2S+1)^2J^2}{16(2S-1)D}.
$$

so that $\Delta_{1}^{\text{AFM}}$ is nearly constant with respect to $D$, whereas $\Delta_{2}^{\text{AFM}}$ depends almost linearly on $D$. At first glance, the latter result appears to contradict the shape of the resonance B seen in Fig. 4(a), so that consideration of the energy spectrum becomes apparently insufficient. In order to account for this disparity, we must also take into account the explicit form of the MQD’s states contributing to the resonances, see Eq. (14). For $D > |J|/2$, we have $|B^-\rangle^2 > |A^-\rangle^2$ and $|A^+\rangle^2 > |B^+\rangle^2$, and as the magnetic anisotropy $D$ increases, at some point we get $|B^-\rangle^2 = |A^+\rangle^2 \approx 1$ and $|A^-\rangle^2 = |B^+\rangle^2 \approx 0$, Fig. 4(g), which basically means that $|A^-\rangle \approx |\downarrow\rangle_{\text{OL}} \otimes |2\rangle_{\text{core}}$ and $|B^+\rangle \approx |\downarrow\rangle_{\text{OL}} \otimes |0\rangle_{\text{core}}$. In other words, when $D \gtrsim |J|$, the cotunneling processes associated with transitions between the states $|-\frac{S}{2}\rangle$ and $|-\frac{S}{2}\rangle$ are allowed, while those between the states $|\frac{S}{2}\rangle$ and $|\frac{S}{2}\rangle$ are forbidden. Consequently, the resonance marked with a vertical dashed line in Fig. 4(b) actually represents two independent resonances: B for $D \lesssim |J|$ and A for $D \gtrsim |J|$.

To complete the discussion of spectral functions, we note that the presence and behavior of the resonance C for the antiferromagnetic $J$-coupling ($J < 0$), Fig. 4(b), can be explained in a way similar to that for $J > 0$, with the relevant energy gaps for $D \gg |J|$ estimated as

$$
\Delta_{1}^{\text{AFM}} \approx |J| + \frac{(2S+1)^2J^2}{16(2S-1)D},
$$

$$
\Delta_{2}^{\text{AFM}} \approx (2S-1)D + \frac{(2S+1)^2J^2}{8(2S-1)D}.
$$

However, only virtual spin-flip transitions between the states $|-\frac{S}{2}\rangle$ and $|\frac{S}{2}\rangle$, represented by the energy gap $\Delta_{1}^{\text{AFM}}$ [see Eq. (16)], are then possible. On the other hand, in the opposite limit, $D \ll |J|$, both types of
spin-flip cotunneling processes characteristic for the antiferromagnetic $J$-coupling (as discussed earlier) can in principle operate. Both these transitions are associated with the same energy gap given by Eq. (16), which, unlike in the case of $J > 0$, results in formation of one resonance only, Fig. 4(b).

B. Conductance in the linear response regime

From the spectral function discussed above one can determine the spin-resolved as well as total linear conductance, shown in Figs. 5(a)-(g). For $|J| \ll T_K$, the results well known for Kondo effect in a single-level quantum dot are recovered. In particular, for the antiparallel magnetic configuration an enhanced conductance occurs in the blockade regime (single electron in the OL, $Q = 1$), whereas in the parallel configuration only a sharp peak in the particle-hole symmetry point, $\varepsilon = -U/2$, appears. More precisely, in the antiparallel configuration the linear conductance (measured in the units of $2e^2/h$) is given by $g_{\uparrow\uparrow} = 1 - P^2$, while in the parallel configuration the conductance reaches unity for $\varepsilon = -U/2$, $g_{\downarrow\downarrow} = 1$, with $P_{\uparrow\downarrow\uparrow\downarrow} = \sum_{\sigma} g_{\sigma\uparrow\downarrow\downarrow}$ representing the total linear conductance. Suppression of the Kondo effect for other values of $\varepsilon$ in the latter case is a consequence of spin splitting of the OL due to an effective exchange field created by ferromagnetic electrodes, as it has already been mentioned in the previous section.

When strength of the $J$-coupling increases, the Kondo effect becomes gradually suppressed and the linear conductance in the blockade ($Q = 1$) region decreases. In order to explain this dependence, we note that in the situation under discussion electrons are transmitted through OL that is exchange-coupled to magnetic core, see Eqs. (10). As a result, cotunneling processes responsible for the Kondo state are more complex than in the case of $J = 0$. First, the amplitude of the cotunneling processes becomes reduced as now the electron occupying the OL is in a superposition of the spin-up and spin-down states. Second, the $J$-coupling creates an energy gap between the relevant states, which effectively suppresses the Kondo effect.

Looking more carefully at the conductance curves in Fig. 5 one finds some difference between the cases with $J > 0$ and $J < 0$. While for $J < 0$ the Kondo peak vanishes rapidly after $|J| > T_K$, some remanent Kondo peak is still visible for $J > 0$. This disparity stems from different properties of quantum states taking part in the formation of the Kondo state for $J > 0$ and $J < 0$. First, when $|J| > T_K$, the ground state energy of a singly-occupied MQD is lower for $J > 0$ than for $J < 0$ [compare Figs. 5(g) and (h)]. Second, the ground state for $J < 0$ is a superposition of spin-up and spin-down states, which is not the case when $J > 0$. As a result, the cotunneling processes driving the Kondo effect are more effective for $J > 0$ than for $J < 0$, which leads to lower conductance for $J < 0$ as compared to $J > 0$.

From the previous subsection we know that the uniaxial magnetic anisotropy modifies electron states of a MQD, affecting thus the Kondo effect. This is shown explicitly in Figs. 4(c)-(d), As one can note in Fig. 4 conductance in the parallel magnetic configuration is rather insensitive to the anisotropy constant $D$ – regardless of the type of exchange coupling $J$, see the filled points in Fig. 4(c)-(d), and certain weak dependence on the

Figure 5. (Color online) Total linear conductance $g = \sum_{\sigma} g_{\sigma\sigma}$ in the antiparallel (a,b) and parallel (c,d) magnetic configurations, and the spin-resolved linear conductance $g_{\sigma\sigma}$ in the parallel configuration (e)-(h), presented as a function of the OL energy $\varepsilon$ for indicated values of the parameter $J$ in the case of the ferromagnetic ($J > 0$ – top panel) and antiferromagnetic ($J < 0$ – bottom panel) exchange interaction between electrons in the OL and magnetic core. All other parameters are as in Fig. 2.
Figure 6. (Color online) Influence of the uniaxial magnetic anisotropy constant $D$ on the total linear conductance $g = \sum_\sigma g_\sigma$ for $|J|/T_K \approx 2$ and the exchange $J$-coupling of either (a,c) ferromagnetic ($J > 0$) or (b,d) antiferromagnetic ($J < 0$) type. Other parameters are the same as in Fig. 4.

Anisotropy constant $D$ appears then in the particle-hole symmetry point $\varepsilon = -U/2$ (Kondo peak), see Figs. 4(a)-(b). This dependence, however, becomes weaker when the magnitude of exchange coupling increases. On the other hand, the role of anisotropy is more important in the case of antiparallel magnetic configuration (also for $\varepsilon \neq -U/2$), especially for $|J| > T_K$, see the hollow points in Fig. 4(c)-(d).

Variation of the conductance with the anisotropy constant $D$ depends on the sign of exchange parameter $J$. The conductance curves for $J > 0$ and $J < 0$ differ significantly only for $D \ll |J|/2$, while when $D$ exceeds $|J|/2$, the difference becomes insignificant. Moreover, it should be noted that in the parallel configuration the conductance for $J > 0$ decreases with growing $D$, whereas for $J < 0$, one observes the opposite tendency, see Fig. 4. Such an overlap of the conductance curves for ferromagnetic and antiferromagnetic $J$-coupling in the limit of large anisotropy constant $D$ can be explained in a similar way as above. One has to take into account that in the present situation the difference in energy gaps between ground states for $J > 0$ and $J < 0$ diminishes, and so do the energies of these states as $D$ increases.

C. Tunnel magnetoresistance (TMR)

A quantity that describes difference between transport properties in the parallel (P) and antiparallel (AP) magnetic configurations is the tunnel magnetoresistance (TMR), defined here as

$$\text{TMR} = \frac{g^P - g^\text{AP}}{g^\text{AP}}. \quad (19)$$

Figure 7. (Color online) Total linear conductance $g = \sum_\sigma g_\sigma$ in the parallel (P – filled points) and antiparallel (AP – hollow points) magnetic configuration shown as a function of the uniaxial anisotropy constant $D$ for indicated values of the $J$-coupling and two representative OL energies: (a)-(b) $\varepsilon = -U/2$ and (c)-(d) $\varepsilon = -U/4$. Left panel corresponds to the ferromagnetic $J$-coupling ($J > 0$), while right panel to the antiferromagnetic one ($J < 0$). Other parameters as in Fig. 4.

Using the conductance data analyzed in the previous subsection, we consider now how TMR depends on the key parameters of the model, i.e. on the $J$-coupling, Figs. 5(a)-(b) and the magnetic anisotropy $D$, Figs. 5(c)-(d).

Let us first discuss the behavior of TMR as a function of the exchange coupling constant $J$, Figs. 5(a)-(b). Since for $|J| \ll T_K$ the conductance in the Kondo regime is generally larger in the antiparallel magnetic configuration than in the parallel one, regardless of the type of the $J$-coupling, the corresponding TMR is negative in almost the entire Coulomb blockade region. The only exception occurs around the particle-hole symmetry point $\varepsilon = -U/2$. This behavior follows from the suppression of the Kondo effect in the parallel configuration due to the exchange field, except for the particle-hole symmetric point. However, as $|J|$ becomes larger than $T_K$, the Kondo peak becomes suppressed also in the antiparallel configuration and positive TMR may be observed in the blockade regime as well. Moreover, suppression of the conductance $g^\text{AP}$ for the antiparallel alignment is more evident in the case of antiferromagnetic ($J < 0$) coupling, Fig. 5(b), and the corresponding TMR is therefore significantly larger than for the ferromagnetic coupling ($J > 0$). Another observation for $J < 0$ is that when $|J| \geq T_K$, two distinctive local maxima develop in the Coulomb blockade regime. Their positions depend on $J$ and are symmetric with respect to $\varepsilon = -U/2$. In addition, for $J < 0$, the TMR considerably surpasses the relevant Julliere’s value,
Consider now variation of TMR with the magnetic anisotropy $D$, Figs. 8(c)-(d). First of all, when the OL is either empty or occupied by two electrons, TMR remains insensitive to any changes in the anisotropy constant $D$. The same cannot be said about the region of $\varepsilon$ corresponding to single occupation of the OL, where large variation of TMR appears especially for $J < 0$, see Fig. 8(d). From Fig. 8(d) follows that the smaller the magnetic anisotropy, the larger TMR. Positions of the two local maxima in TMR, however, are now rather independent of $D$. Furthermore, for $D \ll |J|/2$, TMR stays positive. On the contrary, for the ferromagnetic $J$-coupling ($J > 0$), Fig. 8(c), the TMR is negative in the considered range of $\varepsilon$ and is only weakly modified upon changing $D$.

### D. The restoring effect of magnetic field

In the light of the foregoing discussion, we know that the Kondo effect is suppressed by exchange field generated by ferromagnetic electrodes as well as by the exchange coupling of the OL to magnetic core. Very recently, it was shown both experimentally and theoretically that one can compensate for the exchange-induced splitting of the orbital level by fine-tuning an external magnetic field, restoring thus the universal features of the Kondo effect. Now we will thus consider the possibility of restoring the Kondo effect by applying a compensating external magnetic field, $B_z$, oriented along the MQD’s easy axis, Fig. 9. The interesting observation worth mentioning is that the restoration can take place not only for the parallel magnetic configuration, Figs. 9(c)-(d), but also for the antiparallel one, Figs. 9(a)-(b). Furthermore, we would like to emphasize that the considered effect occurs only for the antiferromagnetic ($J < 0$) coupling between an electron in the OL and the MQD’s magnetic core. From Figs. 9(c)-(d) follows that for the parallel magnetic configuration the full unitary Kondo resonance (with the maximum value of conductance $g = 1$) is restored, whereas in the antiparallel configuration the peak of height $1 - P^2$ is retrieved owing to the magnetic field.

From the experimental point of view, it would be useful to know, at least roughly, how the magnitude of the compensating field $B_z$ depends on the system’s parameters. For this purpose, it is essential to know physical mechanism responsible for the restoration of the Kondo effect. Thus, in order to gain some deeper understanding of the problem once again we employ the model of a free-standing MQD. It appears that the restoration of the Kondo effect becomes possible always when the magnetic field $B_z$ brings the ground state of the spin multiplet $S_z = S - 1/2$ into resonance with the ground state of the multiplet $S_z = S + 1/2$. Depending on the direction of the field, the resonance takes place either between the states
\[ |-\frac{S}{2}\rangle \leftrightarrow |\frac{S}{2}\rangle \text{ or } |\pm \frac{S}{2}\rangle \leftrightarrow |\mp \frac{S}{2}\rangle. \]

Moreover, the possibility of such degeneracy is straightforwardly granted by the fact that these states are characterized by different numbers \( S^i \) (different \( z \) component of the MQD's total spin). Accordingly, the Zeeman contributions to these states are different. Because the \( J \)-coupling is of the antiferromagnetic type, the state with greater \( |S^i| \) has then larger energy in the absence of magnetic field \((B_z = 0)\). Thus, if \( B_z > 0 \), the energy of the state \( |-\frac{S}{2}\rangle \) decreases faster with increasing the field than the energy of \( |\frac{S}{2}\rangle \), so the degeneracy of these states occurs at a certain value of magnetic field, \( B = B_c \), which can be then determined from the condition \( \Delta_{\text{AFM}}(B_c) = 0 \), Fig. 10(a).

Taking into account the resonance condition introduced in the previous paragraph, we find the general expression describing dependence of the compensating field \( B_c \) on the \( J \)-coupling and magnetic anisotropy \( D \) in the form

\[
B_c = \frac{2S + 1}{4} |J| - \frac{2S - 1}{2} D + \sqrt{\frac{(2S + 1)^2}{16} J^2 + \frac{(2S - 1)^2}{4} D(D + |J|)}.
\]

The comparison between the analytical solution and numerically derived values of the compensating field \( B_c \) for different magnetic configurations of the system is presented in Fig. 10(b). It is clearly visible that the numerical values of \( B_c \) generally follow the trend of the approximate analytical curve, Eq. (20), and substantial discrepancies arise only for small values of \( |J| \), as one might expect. The slightly smaller value of the compensating field in the situation of a MQD attached to magnetic electrodes can be attributed to renormalization of MQD's energy levels due to the strong OL-electrodes coupling, which results in diminishing energy gaps between the states participating in formation of the Kondo effect. It should be here emphasized that this difference can be seen only due to specific normalization of the compensating field \( B_c \) with respect to \( |J| \). Otherwise, when presented in the logarithmic scale, the curves corresponding to numerical and analytical solutions follow the same trend, see the inset in Fig. 10(b).

Finally, since the form of Eq. (20) is exactly the same as for \( \Delta_{\text{AFM}} \), Eq. (15), the asympotic values of \( B_c \) are immediately obtained as: \( B_c \approx (2S+1)|J|/2 \) for \( |J| \gg D \), and \( B_c \approx S|J| \) for \( |J| \ll D \). Additionally, it might be helpful to know how the change of magnetic anisotropy \( D \) influences the analytical solution \( B_c(|J|) \), bold line in Fig. 10(b). For this purpose, we calculate the inflexion point position (IPP) of the compensating magnetic field curve \( B_c(|J|) \),

\[
\text{IPP} = \frac{2(2S-1)}{(2S+1)^2} \left[ 1 - \left(\frac{2S}{2S+1}\right)^{2/3} \right] \left[ 1 + \left(\frac{2S}{2S+1}\right)^{1/3} \right] D.
\]

It turns out that IPP depends linearly on \( D \), with the proportionality constant being a complex function of the MQD's core spin number \( S \). Consequently, modification of the magnetic anisotropy constant \( D \) does not affect the general shape of the compensating field curve \( B_c(|J|) \), but it only leads to shifting of the curve's inflexion point.

**IV. SUMMARY AND CONCLUSIONS**

In this paper we have investigated transport properties in the Kondo regime of a class of systems exhibiting uniaxial magnetic anisotropy. The model assumed includes one orbital level through which electrons can tunnel and which is additionally exchange-coupled to a magnetic moment. The model can describe a single-level quantum dot in which electrons are exchange-coupled to an embedded magnetic impurity. It can also be used to describe transport through magnetic atoms and molecules.

Using the numerical renormalization group method we have calculated spectral density of the OL level and linear conductance of the system. The key new feature of transport characteristics is the suppression of the Kondo effect by exchange coupling to magnetic core. Independently of the sign of the coupling parameter \( J \), suppression takes place for both ferromagnetic as well as antiferromagnetic coupling. In the limit of small \( J \), \( |J| \ll T_K \), we find the Kondo resonance characteristic of single-level dots. This resonance is suppressed with increasing \( J \) but then some side resonances appear in the spectral density. It is worthy of note that the suppression of the Kondo peak in the case considered appears gradually with increasing \( J \), contrary to the case of a dot exchange-coupled to electron reservoir of continuous density of states, where the suppression is associated with a quantum phase transition.

We have also shown that the suppressed Kondo reso-
nance in spectral function and in transport characteristics can be restored by application of an external magnetic field. This restoration is however complete only in the case of antiferromagnetic exchange coupling ($J < 0$) for both the parallel and antiparallel magnetic configurations.

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Appendix A: Calculation of the spectral function

During the course of NRG iterative calculation, the spectral function $A_\sigma(\omega)$ is obtained as a set of the Dirac delta functions $\delta(\omega - \omega_n)$ at frequencies $\omega_n$, which next have to be broaden in order to acquire a continuous spectrum. Because of logarithmic discretization of conduction band, it is convenient to collect the delta peaks in logarithmic bins and broaden them using a logarithmic Gaussian distribution, with the broadening parameter typically given by $\log(\Lambda)$. It turns out, however, that due to logarithmic discretization of the band and truncation during the NRG run, the broadened spectral function may exhibit some artifacts, such as an oscillatory behavior for energies smaller than the Kondo temperature. One of the tricks to overcome these problems is the so-called self-energy trick.

The essential idea of the self-energy trick relies on finding the spectral function by constructing the full self-energy $\Sigma_\sigma(\omega)$ of the system. The self-energy can be expressed as a ratio of two spectral functions. Although each spectral function displays similar problems related with discretization, by calculating their ratio one obtains a smooth function where most of the artifacts are suppressed. Having found the self-energy, one can then calculate the retarded Green’s function $\langle c_\sigma^{|c_\sigma^\dagger}\rangle_\omega$ of the OL, Eq. (A1), using the equation of motion method,

$$\langle c_\sigma^{|c_\sigma^\dagger}\rangle_\omega = \frac{1}{\omega - \varepsilon_\sigma - \Sigma_\sigma(\omega)},$$  \hspace{1cm} (A1)

where $\varepsilon_\sigma = \varepsilon + \frac{1}{2} B_2(\delta_{\sigma\uparrow} - \delta_{\sigma\downarrow})$. The total self-energy consists of three terms,

$$\Sigma_\sigma(\omega) = \Sigma_{\sigma}^{\text{Coul}}(\omega) + \Sigma_{\sigma}^{\text{ex}}(\omega) + \Delta_\sigma^f(\omega),$$  \hspace{1cm} (A2)

which represent contributions stemming from: the Coulomb interaction, $\Sigma_{\sigma}^{\text{Coul}}(\omega)$, the exchange interaction between an electron spin in the OL and the core spin of the MQD, $\Sigma_{\sigma}^{\text{ex}}(\omega)$, and the tunneling coupling of the OL to electrodes, $\Delta_\sigma^f(\omega)$. The explicit forms of the above self-energy contributions are given by

$$\Sigma_\sigma^{\text{Coul}}(\omega) = \frac{U}{\omega - \varepsilon_\sigma - \Sigma_{\sigma}^{\text{Coul}}(\omega)} + \frac{U}{\omega + \varepsilon_\sigma - \Sigma_{\sigma}^{\text{Coul}}(\omega)},$$  \hspace{1cm} (A3)

$$\Sigma_\sigma^{\text{ex}}(\omega) = \frac{J}{2} \left[ \delta_{\sigma\uparrow} \langle c_\sigma S_z^+ | c_\sigma^\dagger \rangle_\omega + \delta_{\sigma\downarrow} \langle c_\sigma S_z^- | c_\sigma^\dagger \rangle_\omega + (\delta_{\sigma\uparrow} - \delta_{\sigma\downarrow}) \langle c_\sigma S_z | c_\sigma^\dagger \rangle_\omega \right],$$  \hspace{1cm} (A4)

$$\Delta_\sigma^f(\omega) = \frac{G_\sigma}{\pi} \left[ \ln \frac{|W + \omega|}{|W - \omega|} - i\pi \right].$$  \hspace{1cm} (A5)

Finally, the improved spectral function of the orbital level is given by

$$A_\sigma(\omega) = -\frac{1}{\pi} \frac{\text{Im} \Sigma_\sigma(\omega)}{[\omega - \varepsilon_\sigma - \text{Re} \Sigma_\sigma(\omega)]^2 + [\text{Im} \Sigma_\sigma(\omega)]^2}.$$  \hspace{1cm} (A6)

Appendix B: Energy gaps

In the case of the ferromagnetic (FM) $J$-coupling ($J > 0$), exact analytical expressions for the energy gaps $\Delta_1^{FM}$ and $\Delta_2^{FM}$ can be derived as the energy difference between appropriate MQD’s states: $|\pm \frac{3}{2}\rangle$ and $|\pm \frac{1}{2}\rangle$ for $\Delta_1^{FM}$, and $|\pm \frac{3}{2}\rangle$ and $|\pm \frac{3}{2}\rangle$ for $\Delta_2^{FM}$ so that

$$\Delta_1^{FM} = \frac{2S + 1}{4} |J| + \frac{2S - 1}{2} D + \sqrt{\left(\frac{(2S + 1)^2}{16}\right) J^2 + \left(\frac{(2S - 1)^2}{4}\right) D(D - |J|)}.$$  \hspace{1cm} (B1)

The energy gaps for antiferromagnetic (AFM) $J$-coupling ($J < 0$) can be found in a similar way. The energy difference between the MQD’s states $|\pm \frac{3}{2}\rangle$ and $|\pm \frac{3}{2}\rangle$ is then given by

$$\Delta_1^{AFM} = \frac{2S + 1}{4} |J| - \frac{2S - 1}{2} D + \sqrt{\left(\frac{(2S + 1)^2}{16}\right) J^2 + \left(\frac{(2S - 1)^2}{4}\right) D(D + |J|)},$$  \hspace{1cm} (B2)

whereas the formula for the gap between the states $|\pm \frac{3}{2}\rangle$ and $|\pm \frac{3}{2}\rangle$ takes the form

$$\Delta_2^{AFM} = 2 \sqrt{\left(\frac{(2S + 1)^2}{16}\right) J^2 + \left(\frac{(2S - 1)^2}{4}\right) D(D + |J|)}.$$  \hspace{1cm} (B3)
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