Adsorption Studies of Aqueous Solutions of Methyl Green for Halloysite Nanotubes: Kinetics, Isotherms, and Thermodynamic Parameters

Y. M. Vargas-Rodríguez1,*, A. Obaya1, J. E. García-Petronilo1, G. I. Vargas-Rodríguez1, A. Gómez-Cortés2, G. Tavizón3, J. A. Chávez-Carvayar4

1Departamento de Ciencias Químicas, Facultad de Estudios Superiores Cuautitlán-Universidad Nacional Autónoma de México.
Camino No. 1. Av. 1 de mayo, Sta. María Las Torres, Cuautitlán Izcalli. Estado de México. México. C.P. 54740
2Instituto de Física, Universidad Nacional Autónoma de México. Ciudad Universitaria. Coyoacán. C.P. 04510. México, D. F. México
3Facultad de Química, Universidad Nacional Autónoma de México. Ciudad Universitaria. Coyoacán. C.P. 04510. México, D. F. México
4Instituto de Investigaciones en Materiales, Universidad Nacional Autónoma de México. Ciudad Universitaria. Coyoacán. C.P. 04510. México, D. F. México

*Corresponding author: ymvargas@unam.mx

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Abstract Halloysite nanotubes (HNTs) were used to successfully remove methyl green dye from water. The HNTs were also characterized by X-ray diffraction (XRD), scanning electron microscopy (SEM), transmission electron microscopy (TEM), 29Si and 27Al magic angle spinning nuclear magnetic resonance with magic angle spinning (MAS-NMR) and nitrogen adsorption at 77 K. SEM and TEM micrographs showed that HNTs have lengths of 0.2 to 1.5 μm, an outer diameter of 100 nm and lumen of 20 nm wide. X-ray diffraction patterns showed that the HNTs were totally dehydrated. HNTs may be regarded as a mesoporous material with a pore size distribution in the range of 1.5-150 Å and specific surface area of 34.49 m²⋅g⁻¹. The adsorption kinetics and equilibrium data of the dye, initial dye concentration, temperature, pH and contact time effect on removal efficiency were also investigated. Pseudo-first-order, pseudo-second-order, intraparticle diffusion and Eilrich models were evaluated in order to determine the rate parameters. Adsorption rate followed pseudo-second-order kinetic model. Adsorption revealed that methyl green was adsorbed as the Langmuir isotherm model describes and the maximum adsorption capacity of the HNTs was achieved (185 mg⋅g⁻¹), being an efficient adsorbent for methyl green adsorption.

Keywords: halloysite nanotubes, methyl green, adsorption, Kinetic, thermodynamic

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1. Introduction

Industries such as textile, leather, paper, plastics, and cosmetics use dyes in their processes, resulting in the generation of a considerable amount of colored wastewater [1]. It is estimated that there are more than 100,000 commercially available dyes with over 700,000 t of dyestuff produced annually and around 10% of the dyes are discharged into effluent from textile and related industries [2]. These effluents, that are often strongly colored, produce aesthetical and toxicological damages when they are disposed into water or soil [3].

Methyl green (MG) is used in medicine and biology [4,5] MG is, in a basic medium, a divalent cation, but into acidic conditions, it is a monovalent cation [6].

There are several methods used in the wastewaters treatment, both conventional (including biological) [7,8,9,10], advanced processes include chemical and photochemical oxidations, nanofiltration and adsorption [11,12,13]. Adsorption processes have been widely used for color and odor removal from water. Among the adsorbents used for wastewater dye treatment, activated carbon the oldest adsorbent known, is still effective for the most of common organic water pollutants [14,15,16,17]. On the other hand, inorganic adsorbents like zeolites [18,19,20,21], alumina [22,23,24], silica gel [25,26] and clay minerals [27,28,29,30] are effective and they can support oxidizing environments. Clay minerals are abundant, inexpensive, and generally safe for environmental applications. Due to their large specific
surface area, high porosity, surface charge and surface functional groups, clay minerals function as adsorbents, flocculants, and filtration media [31]. HNTs is an economically viable material for these water treatment goals. HNTs are chemically like kaolin and are lamina clay minerals composed of two layers, which are wound into a tubular morphology. The outer layer is composed of silicates (SiO₂) in a tetrahedral crystalline arrangement; the inner layer of the nanotube is formed by alumina (Al₂O₃) with an octahedral crystalline arrangement, arrangements that conforms a system known as halloysite nanotube (HNTs) [32]. The size of natural halloysite particles varies between 1-15 micrometers in length, with an inner diameter of 10-150 nm, depending on the deposits. The HNTs in their natural state can present traces of calcium oxide, magnesium, manganese, sodium, potassium and iron [33]. Since the active surfaces these HNTs have, they have been used as adsorbents to efficiently remove dyes, such as neutral red, methylene blue, malachite green, rhodamine and anionic chrome using Temkin, Freundlich, Langmuir and Dubinin-Radushkevich isotherms.

2. Materials and Methods

2.1. Raw Materials

HNTs and rade methyl green (analytical reagent g) were purchased from Sigma-Aldrich. Deionized water was obtained with a Millipore deionizer, with a conductivity of 5.1 mhos. MG stock solution was prepared with a concentration equal to 600 mg/L in deionized water. It was subsequently diluted to the required concentrations.

Table 1. Properties of the adsorbate

| Adsorbate                  | Methyl Green |
|----------------------------|--------------|
| Chemical formula          | ![Chemical formula image] |
| Linear formula            | C₂₇H₃₅ClBrN₃ZnCl₂ |
| CAS number                | 7114-03-6    |
| Molecular weight (g mol⁻¹) | 653.24       |

2.2. Methods

2.2.1. Characterization

Crystalline phase identification was carried out by XRD (Bruker AXS, D8 Advanced Plus X-ray diffractometer, with monochromatic CuKa1 radiation, λ = 1.54056 Å). Data collection was performed over the scan range 2 to 70° 2θ, with a step width of 0.02° and a count time per step of 1.8 sec. Normal operating conditions were 35 kV and 30 mA. SEM performed morphological characterization of samples, with a field emission JEOL JSM 7600F equipment, whose working conditions included a low accelerating voltage, 1 to 10 kV, and working distances from 4.7 to 7.6 mm. Micrographs were acquired with both backscattered and secondary electrons. This microscope was equipped with X-ray energy detector (X_ACT Oxford INCA) for chemical microanalyses (EDS or EDX). To complete the morphological characterization, studies were carried out by TEM (JEOL 1200 EX microscope, operating at 120 kV and 70 μA). ²⁷Al and ²⁹Si MAS NMR spectra were recorded with a 300 MHz spectrometer (Bruker, Billerica, MA). A 4.5 μs pulse (corresponding to 90°) was used with a repetition time of 5 s between pulses to avoid saturation effects; the spinning frequency was in the range of 4.0-4.5 kHz; the minimum number of scans per spectral data collection was 500. NMR measurements were carried out at room temperature. The specific surface area of the samples was determined by the Brunauer-Emmett-Teller (BET) method. The pore volume and pore-size distribution was estimated by the Barrett-Joyner-Halenda (BJH) method at 77 K (Autosorb 1 MP, Quantachrome Instrument). Prior to measurements, samples were degassed under vacuum at 573 K for 10 h.

2.2.2. Methyl Green Adsorption

A spectrophotometric calibration curve was performed to determine the concentration of MG in water. Measurement wavelength is 632 nm. The concentrations were between 10 and 300 mg·L⁻¹. A set of these solutions was called as system. Each system was kept under constant stirring at 600 rpm at different temperatures (297.15, 313.15 and 333.15 K). Then, 20 mg of HNTs were added to each of the systems at a different temperature. Then, the suspension was centrifuged at 2500 rpm for 3 minutes, to separate and recovers supernatant HNTs. The concentration of the dye before and after adsorption was determined using a spectrophotometer (Varian, Lambda 25). The amount of MG adsorbed by HNTs at any time was calculated from the mass balance equation, Eq. 1.

\[
q_t = \frac{V(C_0 - C_t)}{W},
\]

\(q_t\) is the amount of MG (mg·g⁻¹) adsorbed by NTHS; \(C_0\) and \(C_t\) (mg·L⁻¹) were the concentrations of MG before and after the contact time \(t\), respectively; \(V\) (L) was the volume of the solution of MG and \(W\) (mg) the mass of the HNTs. Experimental procedures under equilibrium were identical to the kinetic tests. The amount of dye adsorbed at equilibrium, \(q_e\) (mg·g⁻¹), was calculated from the following equation.
Where, \( C_0 \) and \( C_e \) (mg\( \cdot \)L\(^{-1} \)) were the liquid-phase concentrations of dye, initially and at equilibrium, respectively; \( V \) (L) is the volume of the solution and \( W \) (mg) is the mass of the adsorbent.

### 3. Results and Discussion

#### 3.1. Characterization

X-ray diffraction results are shown in Figure 1. Peaks at \( 2\theta \) values of 12.2°, 20.1°, 24.5°, 35.1°, 38.1°, 54.6° and 62.6°, indicate the presence of a HNTs. This identification can be remarked by two important results for the \( d_{001} \) reflection near to the 12.2° peak, which were observed in the pattern: this peak corresponds to a \( d \)-spacing around 7.2 Å a characteristic result for a dehydrated HNTs (7 Å) and the intensity of this peak is the half of that of the peak located at 20.1°, in \( 2\theta \) scale [43]. Similar XRD results have been observed for samples from New Zealand [33,44,45].

#### 3.2. \(^{27}\text{Al} \) and \(^{29}\text{Si} \) MAS-NMR

The spectrum for \(^{29}\text{Si} \), Figure 1b, showed a signal at -93.027 ppm. This signal is typical of a \( Q^3(0\text{Al}) \) basic silicate structure, a layered-clays like kaolinite and a variable degree of ordering in the Si O Si subunits. \(^{27}\text{Al} \) MAS-NMR spectrum for HNTs shows a signal at 0.312 ppm, characteristic for an octahedral symmetry for Al, Figure 1c [46].

![Figure 1](image1.png)

**Figure 1.** a) XRD pattern for halloysite nanotubes (HNTs)

![Figure 2](image2.png)

**Figure 2.** SEM micrographs of halloysite nanotubes at different magnifications
3.3. SEM, TEM and EDS

The chemical composition of the HNTs in mass percentage were SiO$_2$, 53.10; Al$_2$O$_3$, 39.05; CaO, 2.11; MgO, 0.02; K$_2$O, 2.74; 0.45, 0.02; MnO$_2$, 2.50. The SiO$_2$:Al$_2$O$_3$ ratio is similar to that which was found in the Algerian HNTs [47,48] and that from Camerun [49]. SEM micrographs of the HNTs, Figure 2, showed nanotubes agglomerates unevenly with lengths from 0.2 to 1.5 $\mu$m. The transmission electron micrograph, Figure 2d, showed an outer diameter of 100 nm and lumen of 20 nm. These dimensions agree with reported data [50]. The chemical composition of the HNTs shows a SiO$_2$:Al$_2$O$_3$ theoretical ratio like that of kaolinite with high water content [51].

3.4. N$_2$ Adsorption-desorption

Analyses of adsorption and desorption of nitrogen were carried out to investigate the surface area and pore volume of HNTs, Figure 4a. The adsorption-desorption isotherm showed a tiny hysteresis cycle, H3 type, which closes to a relative pressure of approximately 0.42. The formation of this hysteresis cycle is characteristic of mesoporous materials (2-50 nm), which form agglomerates of particles with pores or slit-laminar shaped, and / or non-uniform size [52]; the closing of the hysteresis loop is generated by the presence of particles with pore radius in the micropore and mesopore border (1.7-2.0 nm), which means that the Kelvin equation may not apply for that size of small pores i.e. $< 2$ nm which are equivalent to these relative pressures. Similar hysteresis loops were obtained for HNTs of New Zealand and Western Australia [53] and for a HNTs purchased from Sigma-Aldrich [54].

Figure 4b shows the pore size distribution of HNTs, obtained by the Barrett-Joyner-Halenda (BJH) method. The sample shows mesopores and macropores. The distribution of pore size has two maximum pore size, with mesopore diameters of 3.7 and 9.3 nm, respectively. The concentration of fine pores, which has been observed for halloysite, has been attributed to the tubular shape of halloysite particles. The tubes provide the characteristic small pores directly, due to their hollow interiors, and also indirectly, due to the voids, which are created when they pack together [55].

Finally, the specific surface area was determined by the Brunauer-Emmett-Teller ($S_{BET}$) method [56]. The $S_{BET}$ for HNTs was 34.49 m$^2$·g$^{-1}$. A low value if compared to those obtained for natural HNTs from Algeria, New Zealand, Australia and Hunan (China), with 64, 58, 56 and 50.4 m$^2$·g$^{-1}$, respectively [47,50,53]. However, the HNTs from Sigma-Aldrich had a similar $S_{BET}$ value, 32.76 m$^2$·g$^{-1}$ [54,57].

3.5. Removal of Methyl Green by HNTs: Adsorption Studies

3.5.1. Effects of Contact Time and Initial Dye Concentration

The kinetic profiles for adsorption of methyl green on HNTs were studied to determine the effect of initial concentrations of methyl green. Initial concentrations of the dye were 20, 40, 100 and 200 mg·L$^{-1}$, as shown in Figure 5. It is observed that the rate of adsorption increased proportionally to the initial concentration. In addition, the adsorption of MG was faster along the first minutes and then reached a maximum, because the system approached to equilibrium conditions on adsorption.
It was observed that the maximum amount of MG adsorbed per gram of HNTs increased depending on the initial concentration of MG, from 4.95 to 77 mg, for the conditions of pH 6, 120 minutes and 24°C. Then, the percentage of adsorption for each system was determined, using Eq. 3:

\[
\text{Adsorption (\%)} = \frac{C_o - C_f}{C_o}
\]

Where \(C_o\) is the initial concentration and \(C_f\) is the final concentration (after 120 min) of MG. In Figure 5, there is the plot of adsorption percentage as a function of initial concentration; it indicates that when the concentrations of methyl green in aqueous solution on HNTs are very low, i.e., almost 100% of the initial concentration is adsorbed, most of the active sites of the particles of adsorbent are available, on the other hand if the MG concentration increases the adsorption is reduced because most of the active sites are saturated. It is important to observe that, in the concentration range studied, the results of adsorption vs \(C_o\) fitted a straight line, which intercepts with the 100 % point and has a slope = -0.1186 and \(r^2 = 0.9926\) (Figure 5).

3.5.2. Effect of pH

The effect of pH on the adsorption was studied in the pH range 2 and 10. There were evaluated 3 initial concentrations of MG: 20, 28 and 41 ppm, as presented also in Figure 5. With the results of initial and final concentrations the adsorption was determined, for each initial concentration. Two different tendencies were observed; at acidic conditions, the adsorption was increased proportionally with pH, up to 6; at basic environments (pH from 6 to 10), the adsorption of MG on HNTs remained constant. It might be explained because that, in this pH range, methyl green has carbinol, but has not dicatonic species. These findings are like those reported for the VM adsorption in montmorillonite, where it has been shown that the carbinol is adsorbed in greater amounts than dicatonic species of methyl green [37]. Furthermore, with an increase in pH, the surfaces of HNTs have greater negative charge, increasing the electrostatic attraction between the cationic species of methyl green and the adsorption sites negatively charged, which increases the dye adsorption [33].

3.5.3. Effect of Temperature

The effect of temperature, on the adsorption of methyl green, was performed at 297.15, 313.15 and 333.15 K; the adsorbed amount of methyl green (MG) on the adsorbent mass vs time of adsorption was plotted. Results, shown in Figure 5, indicated that the dye adsorption process was favored at higher temperatures.

3.6. Adsorption Kinetics

To interpret the experimental data on the rate of the adsorption of methyl green on HNTs, pseudo-first order, pseudo-second order, intraparticle diffusion and Elrich kinetic models were carried out.

3.6.1. Pseudo-first Order Kinetic Model

Pseudo-first order model is defined by Eq. 4 [58]:

\[
\ln(q_e - q_t) = \ln q_e - k_1 t,
\]
where \( q_e \) and \( q_t \) are the values of the MG mass absorbed per unit mass (mg⋅g\(^{-1}\)) at equilibrium and at time \( t \), respectively, and \( k_1 \) (min\(^{-1}\)) is the pseudo-first-order adsorption rate constant. Then, \( \ln(q_e - q_t) \) vs time was plotted, and data were fitted into a linear regression (Figure 6). With the values of the slope, the value of \(-k_1\) was obtained and, from intercepts with vertical axis, it was calculated the value of \( \ln q_e \) (for each temperature); these data are presented in Table 2.

### 3.6.2. Pseudo-second Order Kinetic Model

Pseudo-second order kinetic model [59] is expressed by Eq. 5:

\[
t/q_t = 1/k_2 q_e^2 + (1/q_e) t
\]

where \( q_e \) is the mass absorbed per unit mass (mg⋅g\(^{-1}\)) at equilibrium, \( q_t \) is the amount of MG adsorbed per unit mass (mg⋅g\(^{-1}\)) at any time and \( k_2 \) (g⋅mg\(^{-1}\)⋅min\(^{-1}\)) is the pseudo-second order rate constant. To evaluate \( k_2 \) in this model, \( t/q_t \) was plotted as a function of time, Figure 6. After a linear regression, \( q_e \) was determined from the inverse value of the slope and \( k_2 \), from the intercept of the graph, Eq. (6). Results, which are presented in Table 2, indicate that the adsorption is faster as temperature increases.

\[
k_2 = \frac{1}{aq_e}
\]  

### 3.6.3. Intraparticle Diffusion Kinetic Model

This model [60] is described by Eq. 7:

\[
q_t = k_i t^{1/2} + C
\]

where \( q_t \) is the amount of the MG mass adsorbed per mass unit (mg⋅g\(^{-1}\)) at time \( t \), and \( k_i \) (min\(^{-1/2}\)) and \( C \) are constants. From a graph of the mass absorbed \( (q_t) \) vs \( t^{1/2} \), Figure 6, data were fitted into a linear regression. From the slope, the intra-particle diffusion constants \( k_i \) were obtained and, from intercepts with the vertical axis, the \( C \) values were determined. Results, which are presented in Table 2, show that the correlation parameters \( r^2 \) ranged between 0.8 and 0.9; thus, data did not fit the model of intra-particle diffusion.

### 3.6.4. Elovich Kinetic Model

Roginsky and Zeldovich proposed an equation [61] known as the Elovich model, Eq. (8), which considers that the rate-controlling step factor, parameter is the diffusion of the dye molecules and chemisorption kinetics [62], this model has been successfully applied to systems in which the adsorption surface is heterogeneous.

\[
q_t = (1/\beta) \ln \alpha + (1/\beta) \ln t,
\]

where \( q_t \) is the adsorbed amount of MG per unit mass of adsorbent (mg⋅g\(^{-1}\)) at any time \( t \) (min), \( \alpha \) is the initial adsorption rate and \( \beta \) is the Elovich coefficient related to the extent of surface coverage and activation energy. A graph \( q_t \) vs \( \ln t \) was plotted, Figure 6, and then it was fitted by a linear regression. The parameter \( \alpha \) was obtained from the intercept \( (a) \) and slope \( (b) \) of Eq. (9) and the term \( \beta \), from the inverse value of the slope.

\[
\alpha = b \cdot e^{a/b}
\]

Results, that are plotted in Figure 6 and summarized in Table 2, indicate that the correlation coefficients, for the three systems at different temperatures, were lower than 0.972, which indicates that the adsorption of methyl green on HNTs is not a chemisorption process.

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**Figure 6.** Model for kinetics adsorption of MG on HNTs: a) Pseudo-first order (pH = 6.0 and Co= 200 ppm); b) Elovich (pH = 6.0 and Co = 200 ppm); c) Intra-particle (pH = 6.0 and Co = 200 ppm), and d) Pseudo-second order (pH = 6.0 and T = 297.15 K).
The best correlation for these results was for the pseudo-second order model and it indicates that the rate of adsorption of methyl green on HNTs increased with temperature.

Table 2. Kinetic parameters for adsorption of methyl green on HNTs

| Temperature (K) | \( T \) |
|----------------|-------|
| 297.15         |       |
| 313.15         |       |
| 313.15         |       |

Pseudo-first-order model
\[
\ln(q_e - q_t) = \ln q_e - k_t t
\]
\[
q_t, \text{ mg g}^{-1}
\]
\[
q_e, \text{ mg g}^{-1}
\]
\[
R^2
\]

Pseudo-second-order model
\[
t / q_t = 1 / k_t q_e^2 + 1 / q_e t
\]
\[
q_e, \text{ ppm min}^{-1}
\]
\[
q_t, \text{ ppm min}
\]
\[
k_t, \text{ g mg}^{-1} \text{ min}^{-1/2}
\]
\[
R^2
\]

Intraparticle diffusion model
\[
q_t = k_i t^{1/2} + C
\]
\[
k_i, \text{ mg g}^{-1} \text{ min}^{-1/2}
\]
\[
C
\]
\[
R^2
\]

Ehrlich model
\[
q_e = A \ln q_t + B \ln C_e
\]
\[
q_e, \text{ mg g}^{-1}
\]
\[
A
\]
\[
B \left( \text{mg g}^{-1} \right)
\]

3.6.5. Activation Energy

To determine the activation energy for the adsorption of methyl green on HNTs, between 297.15 and 333.15 K, it was used the linear form of Arrhenius equation (Eq. 10):
\[
\ln k = \ln A - \frac{E_a}{R} \left( \frac{1}{T} \right)
\]
where \( k \) is the constant of pseudo-second order rate (min\(^{-1}\)-mg\(^{-1}\)-g), \( A \) is the frequency factor (min\(^{-1}\)-mg\(^{-1}\)-g-min), \( E_a \) is the activation energy (J/mol), \( R \) is the universal gas constant (8.314 J mol\(^{-1}\) K\(^{-1}\)) and \( T \) is the temperature (K). Thus, from the graph \( \ln k \) as a function of reciprocal temperature, a straight line with slope equal to \( (E_a/R) \) and intercept (\( \ln A \)) was obtained, Figure 7a. With the slope value, \( E_a \) resulted to be 31 547 J mol\(^{-1}\).

3.7. Adsorption Equilibrium Isotherms

To describe the behavior of equilibrium adsorption of methyl green on HNTs, data of the adsorbed amount of methyl green per gram of adsorbent, at equilibrium, were obtained at 297.15, 303.15 and 313.15 K, Figure 7b. An increase of the adsorbed amount of methyl green on HNTs, according to the equilibrium concentration, was observed. It is because at higher concentrations of the dye, it is greater the shift of the adsorption-desorption equilibrium towards the adsorption process until reaching the highest concentrations, which shows a saturation of the active sites of the adsorbent. Therefore, the values \( R^2 \) of \( q_e \) increased as the methyl green equilibrium concentrations increased. Results, at equilibrium, were assessed by fitting data into Temkin, Freundlich, Langmuir and Dubinin-Radushkevich (DRK) adsorption isotherms.

3.7.1. Temkin Isotherm

The Temkin model [62] is linearly represented by equations (11) and (12). There \( q_e \) is the amount of adsorbed methyl green (mg·g\(^{-1}\)) at equilibrium, \( A_t \) is Temkin isotherm equilibrium binding constant (L·g\(^{-1}\)) and \( B \) is a constant related to heat of sorption (J mol\(^{-1}\)) and \( C_e \) is the concentration of the dissolution of methyl green (mg·L\(^{-1}\)) at equilibrium, \( b_T \) is the Temkin isotherm constant (dimensionless) and \( R \) the universal gas constant (8.314 J mol\(^{-1}\)·K\(^{-1}\)).

\[
q_e = B \ln A_T + B \ln C_e \tag{11}
\]
\[
b_T = \frac{RT}{B} \tag{12}
\]

Then, a plot of \( q_e \) as a function of \( \ln C_e \) (Figure 8a) allows, by fitting these data into a linear regression, to determine \( B \) from the slope and \( A_t \) from the intercept (a), using Eq. 13.

\[
A_T = e^a/B \tag{13}
\]
The linear regression parameters $r^2$ for the three operating temperatures are above 0.99 indicating that these results fitted well the Temkin model, probably because this model is valid for solute concentrations that are not close to zero, or at high concentrations, like some of the experiments carried out in this work (Table 2). According to the model, the adsorption of methyl green on HNTs is characterized by a uniform distribution of the binding energy and heat of adsorption (as a function of temperature) of all the molecules in the layer, which decreases linearly with coverage [63].

3.7.2. Freundlich Isotherm

The Freundlich [64] adsorption isotherm is commonly used to describe the adsorption processes on heterogeneous surfaces, and it is mathematically expressed by Eq. 14.

$$\log q_e = \log k + \frac{1}{n} \log C_e$$

where $C_e$ (mg L$^{-1}$) is the equilibrium concentration of methyl green, $q_e$ (mg g$^{-1}$) is the equilibrium amount of adsorbed methyl green, $k$ (mg g$^{-1}$) and $n$ are constants for a given adsorbate and adsorbent, per mass unit of adsorbent, at equilibrium. High values of $k$ indicate an easy uptake of the adsorbate. The slope $1/n$ of Freundlich equation indicates the heterogeneity of the surface of the adsorbent, where values of $1/n$ close to zero imply higher heterogeneity whilst values of $1/n$ closer to unity imply a lower heterogeneity.

To evaluate the results by the Freundlich isotherm, a graph $\log q_e$ vs $\log C_e$ was plotted at 297.15, 313.15 and 333.15 K, Figure 8b. Data were fitted into linear regressions; with the inverse value of the slope the value of $n$ was obtained and $K$ with the intercept. These results are presented in Table 3.

3.7.3. Langmuir Isotherm

The Langmuir isotherm [65], mathematically shown in Eq. 15, assumes a monolayer adsorption.

$$\frac{C_e}{q_e} = \frac{1}{q_0 K_L} + \frac{1}{q_0} C_e$$

where $C_e$ (mg L$^{-1}$) is the equilibrium concentration, $q_e$ (mg g$^{-1}$) is the amount of adsorbate, which was adsorbed per unit mass of adsorbent and $q_0$ and $K_L$ are the Langmuir constants related to the adsorption capacity and the rate of adsorption, respectively. From a graph of $C_e/q_e$ vs $C_e$, $q$ is obtained from the slope and $K_L$ from the intercept, Figure 8c. Results are presented in Table 3.

3.7.4. Dubinin-Radushkevich Isotherms

Data were fitted into the Dubinin-Radushkevich (D-R) adsorption isotherm, in its linear form. This model is generally applied to express the adsorption mechanism with a Gaussian energy distribution on a heterogeneous surface [66].

$$\ln q_e = \ln q_s - K_{ad} \varepsilon^2$$

where $q_s$ is amount of adsorbate in the adsorbent (mg g$^{-1}$) at equilibrium, $q_s$ the theoretical isotherm saturation capacity (mg g$^{-1}$), $K_{ad}$ the Dubinin-Radushkevich isotherm constant (mol$^2$ K$^{-1}$ J$^{-2}$) and $\varepsilon$ the Rubinin-Radushkevich isotherm constant and is calculated using Eq. 17.

$$\varepsilon = RT \ln \left( 1 + \frac{1}{C_e} \right)$$

where $R$ is the gas constant, 8.314 J mol$^{-1}$ K$^{-1}$, and $T$ the absolute temperature (K). The graph $\ln q_e$ vs $\varepsilon^2$ is shown in Figure 8d. The results are presented in Table 2, it is observed that for the three temperatures R2.
Table 3 shows that the obtained results, for the three experimental temperatures, fitted Temkin and Langmuir equations, with \( r^2 \) of 0.9962, 0.9967 and 0.9994 for the Temkin equation and \( r^2 \) of 0.9982, 0.9986 and 0.9994 for Langmuir equation. The results fitted to Temkin equation possibly due to the concentration range studied (neither very close to zero nor high concentrations). However, the correlation to the Langmuir equation is slightly higher.

The maximum amount of methyl green that the HNTs adsorb, at 273.15 K, is 187.18 mg on g of HNTs. Table 4 shows the results of maximum adsorption of methyl green on different adsorbents, the studies were carried out both in the Batch system and in Fixed bed adsorption. It is observed that the adsorbents with the highest adsorption capacity for methyl green are sepiolite phyllosilicates and HNTs with 65.32 and 187.18 mg g\(^{-1}\) respectively. The result of this study is due to the fact that the structure of the nanotubes has a lumen in addition to an external surface, so the methyl green was mainly encapsulated in the lumen and was partially charged on the surface, so that the HNTs functioned as carriers of the dye, in addition to being adsorbent, as has happened with other compounds such as ibuprofen [67], and dyes such as methylene blue [33], red neutral [32], Malachite green [34] and Methyl violet [68]. These results indicate that HNTS are an efficient adsorbent for methyl green.

### 3.7.5. Thermodynamic Parameters

The constant adsorption for Langmuir isotherms (\( K_L \)) at 297.15, 313.15 and 333.15 K was used to determine thermodynamic parameters: the variation in the standard enthalpy (\( \Delta H^\circ \)) and standard entropy (\( \Delta S^\circ \)), by using Eq. 18.

\[
\ln K_L = \frac{\Delta S^\circ}{R} - \frac{\Delta H^\circ}{RT}
\]

where \( K_L \) is Langmuir constant when concentration terms are expressed in L mol\(^{-1}\), R is the universal gas constant (8.314 J mol\(^{-1}\) K\(^{-1}\)) and T (K) is the temperature. The \( \Delta H^\circ \) and \( \Delta S^\circ \) values can be calculated from the slope and intercept of the plot of \( \ln K_L \) vs 1/T (Figure 9). The standard Gibbs free energy changes (\( \Delta G^\circ \)) at temperatures of 297.15, 313.15 and 333.15 K, was determined using Eq. 19.

\[
\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ
\]

The changes in the activation energy (\( E_a \)) that are presented in Table 5 can be interpreted as follows: if they are low (5 to 40 kJ mol\(^{-1}\)), the main process is a physisorption and, if they are high (40-800 kJ mol\(^{-1}\)), main process is chemisorption [65]. The activation energy for MG adsorption on HNTs resulted to be 31.45 kJ mol\(^{-1}\), showing that physisorption is the principal process. The Gibbs free energy values were negative, which indicates that the adsorption is spontaneous. The decrease in the value standard free energy with increasing temperature reveals that the adsorption of MG in HNTs becomes more favorable at higher temperature. The positive value of \( \Delta H^\circ \) also confirms that the adsorption is endothermic. The positive value of \( \Delta S^\circ \) inferred increased randomness MG during adsorption in active sites of HNTs [37].

### 4. Conclusions

A kinetic and thermodynamic study of the adsorption-adsorption of methyl green on HNTs was carried out, finding that the nanotubes used have lengths from 0.2 to
1.5 μm, an outer diameter of 100 nm and lumen of 20 nm. The effect of time and concentration on the adsorption of MG was studied, after 10 minutes the adsorption is practically independent of time, the % of adsorption is inversely proportional to the initial concentration. The optimal adsorption pH for MG is between 6 and 7. It was found that the adsorption kinetics of methyl green on HNTs fitted properly to a pseudo- second order kinetics model.

The adsorption isotherms were adjusted to the Langmuir equation, indicating that the adsorption is localized, only at defined (active) sites on the surface, that the surface of the HNTs is homogeneous and a methyl green monolayer is formed, if each adsorption site can adhere only one adsorbate molecule, and that there is no interaction between the adsorbed molecules, and the maximum amount that 1 g of HNTs can adsorb is 187.7 mg L−1, a result much higher than those reported in other studies on the adsorption of methyl green with other adsorbents.

The increase in temperature in the adsorption induces a slight increase in the adsorption of MG and considering that the adsorption isotherms conform to the Langmuir equation, this energy is the same for all active adsorption sites. The value small the activation energy 31.45 (kJmol−1), indicated that the adsorption of methyl green was a physisorption process, and the negative values of ΔG° (kJmol−1), indicate that the process is spontaneous. Because of HNTs occur naturally, they are inexpensive and can be used as mined without further treatment, under the mild adsorption conditions of methyl green (room temperature and pH: 6-7), because the process is spontaneous, because the adsorption is physical, since the methyl green was encapsulated in the lumen and was partially charged on the surface, so that the HNTs function as carriers of the methyl green. Finally, the HNTs are an efficient adsorbent for the adsorption and recovery of methyl green in aqueous medium.

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