The thermonuclear rate for the $^{19}\text{F}(\alpha,p)^{22}\text{Ne}$ reaction at stellar temperatures

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Abstract

The $^{19}$F($\alpha$,p)$^{22}$Ne reaction is considered to be one of the main sources of fluorine depletion in AGB and Wolf-Rayet stars. The reaction rate still retains large uncertainties due to the lack of experimental studies available. In this work the yields for both exit channels to the ground state and first excited state of $^{22}$Ne have been measured and several previously unobserved resonances have been found in the energy range $E_{lab} = 792$-$1993$ keV. The level parameters have been determined through a detailed R-matrix analysis of the reaction data and a new reaction rate is provided on the basis of the available experimental information.

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FIG. 1: Energy level scheme for the $^{19}$F($\alpha$,p)$^{22}$Ne reaction. The entrance channel ($\alpha + ^{19}$F) has a threshold of 10.47 MeV with respect to the ground state of $^{23}$Na. The compound state can decay either via the $p_0$ channel to the ground state of $^{22}$Ne or by the $p_1$ channel to the first excited state of $^{22}$Ne. The subsequent emission of a 1.27 MeV photon from the decay of the first excited state ($2^+$) to the ground state ($0^+$) of $^{22}$Ne can also be observed. The dark rectangle above $^{23}$Na represents the energy region studied in this work. White regions above and below it correspond to energies where the cross sections were extrapolated.

I. INTRODUCTION

Fluorine is by far the least abundant of the elements with atomic mass between 11 and 32. While several nucleosynthesis scenarios have been proposed for the production of fluorine, a unique site for the origin of this element has not been identified yet.

Presently three different scenarios are being discussed for the origin of fluorine. One possible process is the neutrino dissociation of $^{20}$Ne in supernovae type II [1]. A second scenario is the pulsating He-burning stage in AGB stars [2] and the third possibility is the hydrostatic burning of helium in Wolf-Rayet stars [3]. It may be possible that all three sites contribute to the formation of fluorine in the universe [4]. So far, the only extra solar system objects in the galaxy where fluorine has been observed are AGB stars [5] and post-AGB star configurations [6].

Fluorine nucleosynthesis in AGB stars takes place in the hydrogen-helium intershell region where the $^{14}$N ashes from the preceding CNO burning are converted to $^{18}$F by $\alpha$-particle captures (a similar reaction path is followed by Wolf-Rayet stars). The unstable $^{18}$F isotope
decays with a half life of 109.8 minutes to \(^{18}\text{O}\). Both a proton or an \(\alpha\)-particle can be captured by \(^{18}\text{O}\). In the former case, \(^{4}\text{He}\) and \(^{15}\text{N}\) are being produced, while in the latter case \(^{22}\text{Ne}\) is formed. This second possibility does not produce fluorine. The alternative \(^{18}\text{O}(p,\alpha)^{15}\text{N}(\alpha,\gamma)^{19}\text{F}\) capture reaction is the main fluorine production link in this scenario. The abundance of \(^{15}\text{N}\) depends sensitively on the hydrogen abundance in the inter-shell region. Hydrogen has been depleted in the preceding CNO burning but can be regenerated through the \(^{14}\text{N}(n,p)^{14}\text{C}\) reaction, with the neutrons being produced by the \(^{13}\text{C}(\alpha,n)^{16}\text{O}\) reaction. Additional protons may be mixed into the region when the convective envelope penetrates the intershell region at the end of the third dredge up (TDU). \(^{14}\text{C}\) produced by this reaction provides a second link for the production of \(^{18}\text{O}\) via \(^{14}\text{C}(\alpha,\gamma)^{18}\text{O}\).

Fluorine is very fragile and three reactions may cause rapid fluorine destruction. Because of the high abundance of \(^{4}\text{He}\) in the intershell region, the \(^{19}\text{F}(\alpha,p)^{22}\text{Ne}\) is expected to be a dominant depletion link. Another depletion process corresponds to the \(^{19}\text{F}(n,\gamma)^{20}\text{F}\) reaction, caused by neutrons being produced by the \(^{13}\text{C}(\alpha,n)^{16}\text{O}\) or the \(^{22}\text{Ne}(\alpha,n)^{25}\text{Mg}\) reactions. If hydrogen is available in sufficient abundance, fluorine may also be depleted through the very strong \(^{19}\text{F}(p,\alpha)^{16}\text{O}\) reaction. All this, however, is strongly correlated with the existing proton and \(\alpha\)-particle abundance at the fluorine synthesis site.

The reaction rate for \(^{19}\text{F}(\alpha,p)^{22}\text{Ne}\) is highly uncertain at helium burning temperatures. Even recent nucleosynthesis simulations still rely on the very simplified rate expression of Caughlan and Fowler (CF88) based on an optical model approximation for estimating the cross section of compound nuclear reactions with overlapping resonances. This approach was originally developed and employed for cases where no experimental information was available. This reaction rate is in reasonable agreement with more recent Hauser-Feshbach estimates assuming a high density of unbound states in \(^{23}\text{Na}\). Other \(^{19}\text{F}\) nucleosynthesis simulations rely on the sparse experimental data available for \(^{19}\text{F}(\alpha,p)^{22}\text{Ne}\) for \(E_{\text{lab}}=1.3\text{ MeV}\) to \(3.0\text{ MeV}\), estimating also possible low energy resonant contributions from known \(\alpha\)-particle unbound states in \(^{23}\text{Na}\). For example, in their approach they approximated the reaction rate by only considering the resonance contributions of the various states neglecting possible interference effects and broad-resonance tail contributions. In this paper we describe a new measurement of \(^{19}\text{F}(\alpha,p)^{22}\text{Ne}\) at lower energies. In our study we explored the reaction for \(E_{\text{lab}}=792\) to \(1993\text{ keV}\) at different angles. The pronounced resonance structure was analyzed in terms of the multi-channel R-matrix model.
using the recently developed R-matrix code AZURE \[17\]. Energy regions not measured here were also included in the computation of the stellar reaction rate by using a combination of data available in the literature and our experimental results to extrapolate the reaction cross section. Possible low energy resonances were taken into account sampling characteristic $\alpha$-particle partial widths of the known $\alpha$-particle unbound states in $^{23}$Na, while deriving the corresponding proton partial width from the available elastic scattering data in the literature \[18\]. Interference terms were modelled with Monte Carlo simulations. In section 2 we describe the experimental setup and the experimental procedure. The R-matrix analysis of the experimental data and the determination of the nuclear parameters of resonances is described in section 3. Finally, the experimental and extrapolated reaction rates (with error bars) are presented and discussed in section 4.

II. EXPERIMENTAL METHOD

The destruction of $^{19}$F by an $\alpha$-particle capture occurs mainly by a resonant reaction process through the $^{23}$Na compound nucleus in an excitation range of high level density. The populated resonant levels will decay by proton emission to the ground state ($p_0$) or first excited state ($p_1$) of $^{22}$Ne. This study included the direct measurement of the $^{19}$F($\alpha$,p)$^{22}$Ne reaction by detecting both $p_0$ and $p_1$ protons (see \[19\] and \[20\]) as well as the additional measurement of the $p_1$ channel via the detection of the $\gamma$-ray transition \[21\] from the first excited state ($2^+$) to the ground state ($0^+$) of $^{22}$Ne (see figure II).

The experiment was performed at the Nuclear Science Laboratory of the University of Notre Dame using the 3.5 MV KN Van de Graaff accelerator. In a first run, the excitation curve of $^{19}$F($\alpha$,p)$^{22}$Ne was investigated between $E_{lab}=1224$ keV and 1993 keV. For this experiment two Si surface barrier detectors with a depletion depth of 300 $\mu$m were mounted at forward angles, while one 100 $\mu$m Si detector was positioned at a backward angle. These thicknesses were sufficient for stopping the reaction protons. The effective solid angle of the detectors at each position configuration was determined using a mixed $^{241}$Am and $^{148}$Gd $\alpha$-particle source with a known activity placed at the target position.

The energy range between $E_{lab}=1629$ keV to 1993 keV was mapped in 5 keV energy steps with the detectors mounted at 30°, 90° and 130°. This made it possible to use the two known resonances at $E_{lab}=1.67$ MeV and 1.89 MeV \[15\] as reference for calibrating and
matching the reaction yield to the previous results. At lower energies, the detector position was changed to 40°, 100° and 120° with respect to the beam direction. The excitation curve was mapped from $E_{lab}=1220$ to 1679 keV using the $E_{lab}=1.67$ MeV resonance as a reference. In total 483 proton spectra were acquired and for every energy, one elastic scattering $\alpha$-particle spectrum was taken. The stoichiometry of targets was constantly monitored with back-scattered $\alpha$-particles.

The $^{19}$F transmission targets were prepared by evaporating 10 $\mu$g/cm$^2$ of CaF$_2$ on 40 $\mu$g/cm$^2$ natural carbon substrates, mounted on aluminum frames. The target was placed with the evaporated material facing the beam on a ladder attached to a rotating rod at the center of the scattering chamber. The ladder held one target and a collimator that was used for centering the beam. The targets deteriorated significantly under beam bombardment, so their stability was monitored by measuring frequently the yield of the elastically scattered $\alpha$-particles at the $E_{lab}=1.89$ MeV resonance. Targets were constantly replaced with new and recently evaporated targets.

For any two detectors with the same absolute efficiency the relative count rate is independent of target stoichiometry and beam intensity, as expressed by

$$\frac{N_1(E, \theta)}{N_2(E, \theta)} = \left[ \frac{d\Omega_1}{d\Omega_2} \right]_{lab/cm}^{-1} \left( \frac{d\sigma(E, \theta)}{d\Omega} \right)_1^{-1} \left( \frac{d\sigma(E, \theta)}{d\Omega} \right)_2. \tag{1}$$

$N_1(E, \theta)$ and $N_2(E, \theta)$ corresponds to the number of events in detectors 1 and 2, respectively, $\left[ \frac{d\Omega_1}{d\Omega_2} \right]_{lab/cm}$ is the solid angle correcting for center of mass to the laboratory system, and $\frac{d\sigma(E, \theta)}{d\Omega}$ are the differential cross sections measured at detectors 1 and 2, respectively. The differential cross section of the $^{19}$F($\alpha$,p)$^{22}$Ne reaction was determined relative to the differential cross section for elastic scattering measured at 160°. It has been shown by Huang-sheng et al. and by Cseh et al. that below $E_{lab}=2.5$ MeV the elastic scattering of $^4$He on $^{19}$F follows the Rutherford law,

$$\frac{d\sigma(E, \theta)}{d\Omega}_{el} = \frac{d\sigma(E, \theta)}{d\Omega}_{Ruth} = \left( \frac{Z_1Z_2e^2}{4E} \right)^2 \sin^{-4} \frac{\theta}{2}. \tag{2}$$

$Z_1$ and $Z_2$ are the atomic numbers of projectile and target, respectively, $e$ is the proton electric charge and $e^2=1440$ keV fm, $E$ is the relative energy of target and projectile in the center of mass system, and $\theta$ is the center of mass angle at which the elastically scattered particles are observed. Within the small thickness of the target ($27\pm5$ keV) the stopping cross section $\epsilon$ is assumed to be a constant. The variation of the elastic differential cross
section across the target thickness is also very small. Therefore the elastic yield can be expressed as

$$Y_{\text{elas}} = \left( \frac{d\sigma(E,\theta)}{d\Omega} \right)_{Ruth} \frac{\Delta}{\epsilon}. \quad (3)$$

Subsequently the target integrated proton yield $Y_p$ can be expressed relative to the elastic scattering cross sections as

$$Y_p = \frac{\Delta}{\epsilon} \left( \frac{d\sigma(E,\theta)}{d\Omega} \right)_{\text{prot}} \left( \frac{N_{\text{prot}}(E,\theta)}{N_{\text{elas}}(E,\theta)} \right) \left( \frac{d\Omega_{\text{prot}}}{d\Omega_{\text{elas}}} \right)_{\text{lab/cm}} \frac{\Delta}{\epsilon} \left( \frac{Z_1 Z_2 e^2}{4E} \right)^2 \sin^{-4} \frac{\theta}{2}. \quad (4)$$

The energy dependence of the stopping power $dE/dx$ of $^4\text{He}$ is well known for both calcium and fluorine [24]. The stopping power for fluorine was fitted to a quadratic polynomial function given by

$$\left( \frac{dE}{dx} \right)_F = \sum_{i=0}^{2} a_i E^i. \quad (5)$$

A similar relation was determined for the calcium stopping power. The partial stopping cross section $\epsilon$ for each of the nuclear species in the target is described by:

$$\epsilon = \frac{1}{n} \left( \frac{dE}{dx} \right), \quad (6)$$

where

$$n = \nu \rho N_A/A \quad (7)$$

with $\nu$ the number of atoms per molecule, $\rho$ the density of the target (again assuming the evaporated material has the same density as the powder used before target preparation), $N_A$ the Avogadro number, and $A$ the mass number. The total stopping cross section of the calcium fluoride target depends critically on the target stoichiometry

$$\epsilon = \epsilon_F + \frac{N_{Ca}}{N_F} \epsilon_{Ca}. \quad (8)$$

The ratio $\frac{N_{Ca}}{N_F}$ measured in the evaporated target layer does not necessarily reflect the stoichiometry of the material before being evaporated. It was reported in previous work [25] that evaporated CaF$_2$ shows a stoichiometric calcium to fluorine ratio of 1:1. The targets used in the present experiment were tested using well known resonances in the $^{19}\text{F}(p,\alpha\gamma)^{16}\text{O}$ reaction. The results indicated that the stoichiometry of the evaporated material is the same as that of the CaF$_2$ powder [26].
FIG. 2: Proton spectra for $^{19}$F($\alpha,p$)$^{22}$Ne at 135° for three beam energies (label at the right upper corner of each box). The upper spectrum shows both proton groups at the reference resonance. Both peaks appear clean of background and are easy to identify. The spectrum at $E_{lab}=1100$ keV shows two groups of protons, still well isolated from the background. Finally, a spectrum at $E_{lab}=792$ keV, where no proton groups were positively identified is shown. The integrated charges are (in $\mu$C) 1981, 180647, and 519252, respectively.

In a second set of experiments we measured the proton yield at lower energies. The experimental setup was designed to perform the measurements with higher beam currents and larger detector solid angles to compensate for the drop in reaction cross section.

The target chamber for this set of experiments allowed mounting of the target at two different angles with respect to the beam: at 45° and 90°. With the first option we measured scattering angles below 90°, while with the second other angles were measured at a smaller effective target thickness. We tested several $^{19}$F-implanted targets for stability. Substrates tested were Ta, Ni, Cr, Al, Fe, and Mo. The best stability against beam deterioration was obtained for the Fe substrate. Electron suppression was supplied through an aluminum plate at -400 volts, mounted 5 mm in front of the target. Carbon buildup on the target was minimized with a liquid nitrogen-cooled copper plate. The target itself was water cooled from the back and electrically isolated from the scattering chamber. Beam current was directly measured at the target holder.

Two Si detectors were mounted on the rotating plate with aluminum holders. Collimators were placed in front of the detectors and pin hole-free Al foils were used to stop the elastically
scattered α-particles, while allowing the protons to reach the surface of the detectors. Both detector holders and the rotating plate were electrically isolated from the rest of the chamber. The detectors had an effective detection area of 450 mm$^2$. The solid angles for both detectors were determined using a mixed $^{241}$Am+$^{148}$Gd α-particle source of known activity mounted at the target position. We measured them to be $0.130\pm0.026$ and $0.133\pm0.027$ steradians, respectively.

With the chamber at the perpendicular target position and both detectors at 135°, a total of 540 spectra were acquired for laboratory energies between 792 and 1380 keV. Typical spectra are shown in figure 2; the last spectrum taken ($E_{lab}=792$ keV) does not show identifiable proton groups. Subsequently, the chamber was reoriented to the 45° target position. The detectors were mounted at 150° and 120° with respect to the beam direction and 178 spectra were taken. Finally, the detectors were mounted at 75° and 105° with respect to the beam direction and 69 spectra were measured.

In this experimental configuration the reaction yield could not be normalized to elastic scattering because of the thick target backing material. The yield was therefore measured relative to the accumulated charge on the target during each run. The reaction yield $Y_p(\theta)$ for the detector mounted at angle $\theta$ is derived from the number of registered proton events $N_p(\theta)$ in the detector is

$$Y_p(\theta) = \frac{N_p(\theta)}{N_\alpha \cdot \epsilon_p \cdot d\Omega_p}$$

where $N_\alpha$ is the accumulated charge, $\epsilon_p$ is the absolute detection efficiency (assumed to be 1 for charged particles and Si detectors at very low count rates), and $d\Omega_p$ is the solid angle subtended by the detector.

The differential cross section can be directly derived from the reaction yield normalized to the yield of the $E_{lab}=1.37$ MeV resonance as measured in the first experiment. This depends critically on the stability of the fluorine content in the target material. Since the amount of fluorine decreases with accumulated charge, the reaction yield needs to be corrected accordingly. During the experiment the yield of the $E_{lab}=1.37$ MeV resonance was monitored frequently to correct for target degradation. The on-resonance thick target yield $Y_{tt}$ as a function of accumulated charge $N_\alpha$ can be expressed by the linear relation:

$$Y_{tt} = a + bN_\alpha,$$
with $a$ and $b$ as constants. The measured yield of the observed protons $Y_\alpha(E)$ was corrected for target degradation in terms of the accumulated charge to

$$Y_p'(E) = \frac{a}{a + bN_\alpha} \cdot Y_p(E).$$

(11)

Data obtained from all the described experiments consist of 20 excitation functions, with eleven corresponding to $^{19}F(\alpha,p_0)^{22}\text{Ne}$ and nine to $^{19}F(\alpha,p_1)^{22}\text{Ne}$. Ten angles were measured in different energy regions. All add up to 1471 data points (See table II) which were analyzed in terms of the R-matrix theory.

III. MULTICHANNEL R-MATRIX ANALYSIS

For the analysis of the experimental data we used the A-matrix version of the computer code AZURE [17]. AZURE is a multichannel and multilevel code that implements the A- and R-matrix formalisms as presented by Lane and Thomas [27]. The code is capable of fitting experimental datasets by varying formal parameters (energies and width amplitudes) of compound-nucleus states. The integrated cross section can also be computed from angular distribution datasets. Error bars for both the parameters and cross section curves are treated with Monte Carlo techniques.

The input to the code consists of a set of initial nuclear parameters; each level is characterized by one energy eigenvalue and several formal reduced width amplitudes (one per channel per level). The code identifies open reaction channels and from the input it assigns an independent width amplitude for each $(s,l)$ combination allowed for the level. Theoretical differential cross section curves at different angles are computed and then compared to experimental yields after target integration corrections [28]. The maximum likelihood estimator is then minimized by varying all the parameters simultaneously. Each time a local minimum is found, the integrated value of the cross section is computed.

Overlapping of resonances complicated the simultaneous fitting of the yield curves. The code was by itself not able to find a set of formal parameters that would reasonably describe the yield curves. For this reason, an initial parameter set had to be found without the help of the minimization routines. By trial and error, the choice of initial nuclear parameters was done by adjusting the energy for each of the levels so as to describe the position of resonances as close as possible. The height and width of the resonances was, on the other
TABLE I: Yield curves measured in this work

| curve | channel | angle | $E_{\text{min}}$ (keV) | $E_{\text{max}}$ (keV) | $\Delta$ (keV) |
|-------|---------|-------|------------------------|------------------------|----------------|
| 1     | $^{19}F(\alpha,p_0)^{22}Ne$ | 130   | 1641                   | 1993                   | 15             |
| 2     | $^{19}F(\alpha,p_0)^{22}Ne$ | 90    | 1641                   | 1993                   | 15             |
| 3     | $^{19}F(\alpha,p_0)^{22}Ne$ | 30    | 1641                   | 1993                   | 15             |
| 4     | $^{19}F(\alpha,p_0)^{22}Ne$ | 120   | 1224                   | 1679                   | 15             |
| 5     | $^{19}F(\alpha,p_0)^{22}Ne$ | 100   | 1224                   | 1679                   | 15             |
| 6     | $^{19}F(\alpha,p_0)^{22}Ne$ | 40    | 1224                   | 1679                   | 15             |
| 7     | $^{19}F(\alpha,p_0)^{22}Ne$ | 105   | 1027                   | 1367                   | 25             |
| 8     | $^{19}F(\alpha,p_0)^{22}Ne$ | 120   | 929                    | 1359                   | 35             |
| 9     | $^{19}F(\alpha,p_0)^{22}Ne$ | 135   | 792                    | 1363                   | 25             |
| 10    | $^{19}F(\alpha,p_0)^{22}Ne$ | 150   | 929                    | 1359                   | 35             |
| 11    | $^{19}F(\alpha,p_0)^{22}Ne$ | 75    | 1027                   | 1367                   | 35             |
| 12    | $^{19}F(\alpha,p_1)^{22}Ne$ | 130   | 1629                   | 1981                   | 15             |
| 13    | $^{19}F(\alpha,p_1)^{22}Ne$ | 90    | 1629                   | 1981                   | 15             |
| 14    | $^{19}F(\alpha,p_1)^{22}Ne$ | 30    | 1629                   | 1981                   | 15             |
| 15    | $^{19}F(\alpha,p_1)^{22}Ne$ | 120   | 1224                   | 1679                   | 15             |
| 16    | $^{19}F(\alpha,p_1)^{22}Ne$ | 100   | 1224                   | 1679                   | 15             |
| 17    | $^{19}F(\alpha,p_1)^{22}Ne$ | 40    | 1224                   | 1679                   | 15             |
| 18    | $^{19}F(\alpha,p_1)^{22}Ne$ | 120   | 929                    | 1359                   | 35             |
| 19    | $^{19}F(\alpha,p_1)^{22}Ne$ | 135   | 792                    | 1363                   | 25             |
| 20    | $^{19}F(\alpha,p_1)^{22}Ne$ | 150   | 929                    | 1359                   | 35             |

hand, approximated by varying the width amplitudes.

Interference patterns between the various resonances were determined by iteratively probing the contribution to yield curves of levels within groups of the same $J^\pi$. The sign of the width amplitudes was flipped one by one for all the (s,l) channels. These steps were repeated iteratively several times until the theoretical curves resembled the dataset. The resulting set of parameters was then used as input to the R-matrix code coupled to the $\chi^2$ minimization routines. Every time a calculation was performed all 20 excitation curves were examined. The target thickness $\Delta$ used for each of the yield curves is shown in table [I].
The resulting R-matrix fits to the experimental yield data $Y_p$ are shown in figures 3 and 4 for the ground state and the excited state transitions, respectively. Both the energies $E_\lambda$ and reduced width amplitudes $\gamma_i$ were determined with a single channel radius ($a_c=5.5$ fm). The boundary condition was set to $S_c$, the shift function, at the level in each $J^\pi$ group with the lowest energy. Background states were included for each of the $J^\pi$ groups. (The set of 201 R-matrix parameters and the experimental dataset can be obtained by contacting the author.)

Parameter error bars were determined with a bootstrap method [29] and correspond to a confidence interval of 95% (see figure 5). From the set of 1,471 experimental data points we generated 40,000 subsets, with each subset containing 1,471 data points as well. The selection of points was performed with a Monte Carlo method and as a result, each set contains a random number of points repeated more than once. Using the set of formal parameters obtained with the R-matrix analysis described above, a $\chi^2$ was computed for each of the subsets sampled by bootstrapping. The distribution of $\chi^2$ values is shown in figure 5(a). The 0.95 cumulative value of the distribution corresponds to $\chi^2 \equiv \chi^2_{95}=22,774$. Finally, with a Monte Carlo technique, we generated $\chi^2$ curves by varying each parameter independently while fixing all others. The error bar corresponds to the largest parameter value such that $\chi^2 \leq \chi^2_{95}$ (see figure 5(b)). Total cross sections for both channels were computed as well and are discussed in the next section and shown in figure 6.

IV. THE REACTION RATE

The thermonuclear reaction rate has contributions from three energy regimes: a) the region measured experimentally in this work, spanning from $E_{lab}=792$ keV to 1993 keV, b) the region below $E_{lab}=792$ keV (not measured), and c) the region above $E_{lab}=1993$ keV (not measured here as well).

The contribution to the rate from our experimental dataset was calculated by integrating numerically the total cross section $\sigma(E)$ over the Maxwell-Boltzmann distribution of stellar gas at temperature $T$

$$N_A \langle \sigma v \rangle = N_A \left( \frac{8}{\pi \mu} \right)^{1/2} (kT)^{-3/2} \int \sigma(E)E \exp \left( \frac{-E}{kT} \right) dE.$$  \hspace{1cm} (12)
FIG. 3: Experimental yield curves for the $^{19}$F($\alpha$,p$^0$)$^{22}$Ne channel and the R-matrix fits (solid lines). Different curves are offset by a factor of 100. Vertical axis units are relative yields. The labels to the right of each curve are described in table I.
FIG. 4: Experimental yield curves for the $^{19}$F($\alpha,p$)$_1^{22}$Ne channel and the R-matrix fits (solid lines). Different curves are offset by a factor of 100. Vertical axis units are relative yields. The labels to the right of each curve are described in table II.
FIG. 5: Calculation of error bars. (a) Bootstrap histogram used to compute the error bars with a 95% confidence level. The horizontal axis corresponds to the raw $\chi^2$ value associated to the set of central-value parameters. Each bin contains intervals $\Delta \chi^2 = 20$. A total of 40,000 subsets were sampled from the experimental set with a Monte Carlo method. Note that the curve does not correspond to a normal distribution. However, the centroid corresponds to the raw value of $\chi^2$ associated to the best R-matrix fit ($\chi^2_{\text{min}} = 20,535$). An area corresponding to 95% of the total integral is below $\chi^2_{95} = 22,774$ (vertical line). (b) Sample $\chi^2$ vs. parameter value ($\gamma$) curve. The horizontal line represents $\chi^2_{95}$, while the dotted vertical lines are, from left to right, the lower limit, central value, and upper limit of the parameter, respectively. An equivalent curve was generated for each of the formal parameters.
FIG. 6: R-matrix calculated total cross sections for $^{19}F(\alpha, p)^{22}\text{Ne}$. Both $^{19}F(\alpha, p_0)^{22}\text{Ne}$ (upper panel) and $^{19}F(\alpha, p_1)^{22}\text{Ne}$ (lower panel) curves are shown with uncertainty bands, as computed by sampling the 95% confidence interval nuclear parameter space with a Monte Carlo method. The strong oscillations in the upper and lower limits of the bands are an artifact of the finite number of samples (10,000) taken with the Monte Carlo method.

Here $E$ is the energy of the particles in the center of mass system, $N_A$ is Avogadro’s number, $k$ is Boltzmann’s constant, $\mu$ the reduced mass, and $T$ the temperature of the gas. The total cross section $\sigma$ was derived from the R-matrix calculation with the recommended values of formal parameters. Both $p_0$ and $p_1$ components are shown in figure 6. Upper and lower limits of the total cross section and the reaction rate in this energy regime were
computed by sampling the parameter space defined by the upper and lower values of the fitting parameters with a Monte Carlo technique. All parameters were varied simultaneously and a total of 10,000 parameter sets were produced. The reaction rate for each parameter set was calculated with equation 12 and all resulting rates were compared with each other. The highest (lowest) value obtained corresponds to the upper (lower) limit of the reaction rate.

The contribution to the reaction rate from resonances below \( E_{\text{lab}} = 792 \) keV, which were not measured in the present experiment, was considered as well. Previous studies through other reaction channels do indicate several unbound states in \(^{23}\text{Na}\) in this energy range near the \( \alpha \)-particle threshold \[16\], which may contribute significantly to the \(^{19}\text{F}(\alpha,p)^{22}\text{Ne}\) reaction. Most notably, detailed elastic proton scattering measurements were performed for this energy range in \(^{23}\text{Na}\) \[18\], and provide important information necessary for estimating the contributions of these lower energy states to the reaction rate. Resonances observed in the \(^{22}\text{Ne}(p,p)^{22}\text{Ne}\) and \(^{22}\text{Ne}(p,p')^{22}\text{Ne}\) channels were used to define the spins, parities, energies, and both proton \( p_0 \) and \( p_1 \) partial widths of contributing states. On the other hand, \( \alpha \)-particle partial widths \( \Gamma_\alpha \) were obtained by adopting the experimentally known \( \alpha \)-particle reduced widths \( \gamma^2_\alpha \) determined in the high energy range.

Energies and reduced widths obtained with the R-matrix analysis were used to calculate the logarithmic average \( < \log(\gamma^2_\alpha) > \) for each \( J^\pi \) group (see figure 7). The extrapolated reduced \( \alpha \)-particle width amplitude for a state with parameters \( (J,\pi) \) was chosen to be

\[
\gamma^2_\alpha(J,\pi) = 10 < \log(\gamma^2_\alpha) > . \tag{13}
\]

Extrapolated upper (lower) limit values of the reduced \( \alpha \)-particle widths were set equal to the highest (lowest) \( \gamma^2_\alpha \) value determined from the experimental data of the corresponding \( J^\pi \) group. The set of extrapolated \( \gamma^2_\alpha \) values, together with the reduced proton widths \( \gamma^2_p \) calculated from \(^{22}\text{Ne}(p,p)^{22}\text{Ne}\) and \(^{22}\text{Ne}(p,p')^{22}\text{Ne}\) experiments by \( \Gamma_p = 2P\gamma^2_p \) (where \( P \) is the penetrability through the Coulomb barrier) is shown in table II.

Based on these parameters, the resonant contribution to the cross section was calculated using the R-matrix formalism. Nevertheless, the interference pattern between resonances cannot be predicted in this scheme. Therefore, we simulated its effect with a Monte Carlo sampling of possible width amplitude sign combinations. Figure 8 shows the resulting S-factor for three sample assumptions for interference between resonances. Upper and lower
| $J$ | $\pi$ | $E_{cm}$ (MeV) | $\gamma_\alpha^2$ (MeV) $^a$ | $\gamma_\alpha^2$ (MeV) $^a$ | $\gamma_\alpha^2$ (MeV) $^a$ |
|---|---|---|---|---|---|
| 1.5 | 1 | 0.010 | 3.72E-4 | 5.29E-4 | 2.61E-4 |
| 1.5 | -1 | 0.031 | 8.89E-5 | 1.51E-4 | 5.37E-5 |
| 0.5 | 1 | 0.037 | 9.60E-6 | 2.44E-4 | 1.48E-6 |
| 2.5 | 1 | 0.049 | 1.04E-4 | 4.04E-4 | 2.75E-5 |
| 2.5 | 1 | 0.078 | 1.04E-4 | 4.04E-4 | 2.75E-5 |
| 1.5 | -1 | 0.106 | 8.89E-5 | 1.51E-4 | 5.37E-5 |
| 1.5 | 1 | 0.147 | 3.72E-4 | 5.29E-4 | 2.61E-4 |
| 2.5 | 1 | 0.147 | 1.04E-4 | 4.04E-4 | 2.75E-5 |
| 1.5 | -1 | 0.207 | 8.89E-5 | 1.51E-4 | 5.37E-5 |
| 1.5 | -1 | 0.237 | 8.89E-5 | 1.51E-4 | 5.37E-5 |
| 1.5 | 1 | 0.354 | 3.72E-4 | 5.29E-4 | 2.61E-4 |
| 1.5 | -1 | 0.355 | 8.89E-5 | 1.51E-4 | 5.37E-5 |
| 1.5 | 1 | 0.369 | 3.72E-4 | 5.29E-4 | 2.75E-5 |
| 2.5 | 1 | 0.369 | 1.04E-4 | 4.04E-4 | 2.61E-4 |
| 1.5 | -1 | 0.405 | 8.89E-5 | 1.51E-4 | 5.37E-5 |
| 0.5 | -1 | 0.438 | 1.07E-5 | 3.00E-4 | 4.76E-8 |
| 2.5 | 1 | 0.438 | 1.04E-4 | 4.04E-4 | 2.75E-5 |
| 0.5 | 1 | 0.448 | 9.60E-6 | 2.44E-4 | 1.48E-6 |
| 1.5 | 1 | 0.461 | 3.72E-4 | 5.29E-4 | 2.61E-4 |
| 0.5 | 1 | 0.481 | 9.60E-6 | 2.44E-4 | 1.48E-6 |
| 2.5 | 1 | 0.503 | 1.04E-4 | 4.04E-4 | 2.75E-5 |
| 1.5 | 1 | 0.503 | 3.72E-4 | 5.29E-4 | 2.61E-4 |
| 1.5 | 1 | 0.506 | 3.72E-4 | 5.29E-4 | 2.61E-4 |
| 1.5 | -1 | 0.511 | 8.89E-5 | 1.51E-4 | 5.37E-5 |
| 0.5 | 1 | 0.524 | 9.60E-6 | 2.44E-4 | 1.48E-6 |
| 1.5 | 1 | 0.525 | 3.72E-4 | 5.29E-4 | 2.61E-4 |
| 0.5 | 1 | 0.569 | 9.60E-6 | 2.44E-4 | 1.48E-6 |
| 0.5 | -1 | 0.618 | 1.07E-5 | 3.00E-4 | 4.76E-8 |
| 2.5 | 1 | 0.640 | 1.04E-4 | 4.04E-4 | 2.75E-5 |
| 1.5 | 1 | 0.642 | 3.72E-4 | 5.29E-4 | 2.61E-4 |
values of the reaction rate were calculated with equation 12 from different combinations of signs and widths sampled within the parameter space, as before. The recommended value corresponds to the logarithmic average of the upper and lower limits of the reaction rate.

Finally, the contribution to the reaction rate from resonances above $E_{lab}=1993$ keV was computed by extrapolating our experimental rate to higher temperatures by following the energy dependence of the Hauser-Feshbach rate MOST \cite{30}. We did not perform an R-matrix analysis due to the current uncertainty of spins and parities of excited states in $^{23}$Na in this energy region, for which several experimental works have been published (for example see \cite{15, 23, 31, 32}). Over one hundred resonances have been identified for $2.0 \leq E_{lab} \text{ (MeV)} \leq 4.7$, but the data has not been able to constrain the spins and parities of most of the states. The average level density is $0.04 \text{ keV}^{-1}$, high enough to apply the Hauser-Feshbach formalism for calculating the reaction rate \cite{33}. At the upper limit of the Gamow window corresponding to our experimental data ($T=1\times10^9$ K), the agreement between the Hauser-Feshbach and our R-matrix calculated rate is very good. We used the experimentally determined reaction rate here to renormalize the MOST values above this temperature.

The total reaction rate consists, for temperatures below $T=1\times10^9$ K, of the sum of the rate from the R-matrix analysis of our experimental data and the rate calculated from extrapolated Monte Carlo cross sections at the lowest energies, and of the Hauser-Feshbach renormalized rate above $T=1\times10^9$ K. The resulting reaction rate is shown in table III.
### TABLE III: Reaction rate for $^{19}F(\alpha, p)^{22}Ne$

| $T_9$ | $N_A < \sigma v >$ | $N_A < \sigma v >$ | $N_A < \sigma v >$ |
|------|------------------|------------------|------------------|
|      | recomm [cm$^3$/s mol] | low [cm$^3$/s mol] | up [cm$^3$/s mol] |
| 0.10 | 2.402E-22        | 1.049E-23        | 5.500E-21        |
| 0.11 | 5.072E-21        | 4.173E-22        | 6.166E-20        |
| 0.12 | 6.322E-20        | 8.649E-21        | 4.621E-19        |
| 0.13 | 5.625E-19        | 1.158E-19        | 2.732E-18        |
| 0.14 | 3.943E-18        | 1.117E-18        | 1.392E-17        |
| 0.15 | 2.477E-17        | 8.120E-18        | 7.555E-17        |
| 0.16 | 1.399E-16        | 4.807E-17        | 4.070E-16        |
| 0.18 | 2.758E-15        | 1.073E-15        | 7.091E-15        |
| 0.20 | 3.310E-14        | 1.455E-14        | 7.556E-14        |
| 0.25 | 3.680E-12        | 2.047E-12        | 7.088E-12        |
| 0.30 | 1.272E-10        | 7.709E-11        | 2.759E-10        |
| 0.35 | 2.431E-09        | 1.484E-09        | 6.038E-09        |
| 0.40 | 3.340E-08        | 1.939E-08        | 7.961E-08        |
| 0.45 | 3.631E-07        | 2.064E-07        | 7.438E-07        |
| 0.50 | 3.072E-06        | 1.796E-06        | 5.475E-06        |
| 0.60 | 1.020E-04        | 6.176E-05        | 1.601E-04        |
| 0.70 | 1.445E-03        | 8.658E-04        | 2.151E-03        |
| 0.80 | 1.115E-02        | 6.630E-03        | 1.624E-02        |
| 0.90 | 5.615E-02        | 3.346E-02        | 8.186E-02        |
| 1.00 | 4.173E-01        | 2.483E-01        | 6.068E-01        |
| 1.25 | 5.748E+00        | 3.398E+00        | 8.746E+00        |
| 1.50 | 3.946E+01        | 2.278E+01        | 6.111E+01        |
| 1.75 | 1.770E+02        | 1.007E+02        | 2.738E+02        |
| 2.00 | 5.944E+02        | 3.381E+02        | 9.115E+02        |
| 2.50 | 3.773E+03        | 2.169E+03        | 5.674E+03        |
| 3.00 | 1.456E+04        | 8.458E+03        | 2.160E+04        |
| 3.50 | 4.089E+04        | 2.394E+04        | 6.023E+04        |
| 4.00 | 9.261E+04        | 5.448E+04        | 1.359E+05        |
| 5.00 | 3.123E+05        | 1.846E+05        | 4.563E+05        |
| 6.00 | 7.420E+05        | 4.398E+05        | 1.082E+06        |
FIG. 8: Monte Carlo simulated low energy S-factor for $^{19}\text{F}(\alpha, p)^{22}\text{Ne}$ for three different sample resonance interference assumptions.

Figure 9 shows the total reaction rate relative to the phenomenological rate estimate of CF88. Shown are the Hauser-Feshbach model predictions using the codes MOST and NON-SMOKER relative to the CF88 predictions. Also compared is the rate estimate of Lugaro et al. [13], which is based on a single non-interfering resonance approximation.

The new rate is significantly higher (about one order of magnitude in the stellar temperature regime) than the rate based on the assumption of single non-interfering resonance levels of Lugaro et al. [13]. This can be attributed to the fact that the new rate is calculated from non-narrow resonance contributions, as given by the R-matrix analysis. Also, the CF88 rate is very similar to the new rate, except for the astrophysically relevant temperature $T = 3 \times 10^8$ K, where it is close to a factor of 10 smaller. However, the statistical model predictions overestimate the reaction rate and can be rejected at a 95% confidence level for $2.5 < T (10^8 \text{ K}) < 5.5$. For the highest temperatures, the new recommended rate differs from the statistical model predictions by a renormalization factor (0.62).

The main source of uncertainty in the new rate at AGB star temperatures comes from the uncertainty in the extrapolation of the reaction cross section. Experimental work below $E_{lab}=800$ keV is required to constrain the partial $\alpha$-particle widths and the interference patterns in the $^{19}\text{F}(\alpha, p)^{22}\text{Ne}$ reaction. We have shown the importance of the interference effects between resonances. Therefore, a direct measurement towards lower energies is probably the only plausible solution to the problem of the uncertainty of this reaction rate at AGB star
FIG. 9: (Color figure) The new rate for the $^{19}\text{F}(\alpha,p)^{22}\text{Ne}$ reaction compared to the phenomenological rate listed in the literature (CF88) [8], the Hauser-Feshbach predictions, and Lugaro et al.’s [13] rate.

For explosive stellar scenarios ($T > 1 \times 10^9$ K) the situation is still more delicate as spins and parities of resonances contributing to the rate are uncertain. Both direct and indirect measurements of the $^{19}\text{F}(\alpha,p)^{22}\text{Ne}$ reaction above $E_{lab}=2$ MeV can help improving the quality of the rate for explosive scenarios.
V. SUMMARY AND CONCLUSIONS

We have measured the $^{19}$F($\alpha$,p)$^{22}$Ne reaction in the energy range $E_{lab}$=792-1993 keV. Stable fluorine targets were developed and several resonances were found in the 20 experimental yield curves. Ten different angles ranging from 30° to 150° were measured and two reaction channels ($p_0$ and $p_1$) observed. An R-matrix analysis of the data was performed to determine the differential and total reaction cross sections in the investigated excitation energy range. The cross section is characterized by many broad resonances tailing into the low energy range. Possible additional resonance contributions in that excitation range were predicted in a Monte Carlo cross section analysis on the basis of available data on the nuclear level structure of the $^{23}$Na compound nucleus. The predicted contributions were included in the final reaction rate analysis. A full analysis of the impact of this new rate on the fluorine production in AGB stars will be presented in a subsequent paper.

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