The EMBI in Latin America: Fractional Integration, Non-linearities and Breaks

Guglielmo Maria Caporale, Hector Carcel and Luis A. Gil-Alana
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Guglielmo Maria Caporale
Brunel University London, UK

Hector Carcel
University of Navarra, Faculty of Economics, Pamplona, Spain

Luis A. Gil-Alana
University of Navarra, Faculty of Economics and ICS, Pamplona, Spain

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Abstract

This paper analyses the main statistical properties of the Emerging Market Bond Index (EMBI), namely long-range dependence or persistence, non-linearities, and structural breaks, in four Latin American countries (Argentina, Brazil, Mexico, Venezuela). For this purpose it uses a fractional integration framework and both parametric and semi-parametric methods. The evidence based on the former is sensitive to the specification for the error terms, whilst the results from the latter are more conclusive in ruling out mean reversion. Further, non-linearities do not appear to be present. Both recursive and rolling window methods identify a number of breaks. Overall, the evidence of long-range dependence as well as breaks suggests that active policies might be necessary for achieving financial and economic stability in these countries.

Keywords: Emerging markets; EMBI; fractional integration; non-linearities

JEL Classification: C22, G12, F63

Corresponding author: Professor Guglielmo Maria Caporale, Research Professor at DIW Berlin. Department of Economics and Finance, Brunel University, London, UB8 3PH, UK. Tel.: +44 (0)1895 266713. Fax: +44 (0)1895 269770. Email: Guglielmo-Maria.Caporale@brunel.ac.uk

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1. **Introduction**

The EMBI (Emerging Market Bond Index) is an index constructed by JP Morgan for dollar-denominated sovereign bonds issued by a selection of emerging countries. In addition to being useful for measuring the performance of this asset class, it is the most widely used and comprehensive benchmark for emerging sovereign debt markets, and it also helps increase their visibility.

The EMBI is based on the interest differential between dollar-denominated bonds issued by developing countries and US Treasury bonds respectively, the latter traditionally being considered to be risk-free. This differential, also known as spread or swap, is expressed in basis points (bp). A spread of 100 bp means that the yield on bonds issued by the government in question is one percent (1%) higher than that on the risk-free US Treasury Bills: riskier bonds (with a higher default probability) pay higher interest. An increase in sovereign bond yields tends to drive up long-term interest rates in the rest of an economy, affecting both investment and consumption decisions. On the fiscal side, higher government bond yields imply higher debt-servicing costs and can significantly raise funding costs. This could also lead to an increase in rollover risk, as debt might have to be refinanced at unusually high cost or, in extreme cases, it might not be possible any longer to roll it over (Gómez-Puig and Mari del Cristo, 2014). Large increases in government funding costs can therefore have real effects in addition to the purely financial effects of higher interest rates (see Caceres et al., 2010).

This paper analyses the statistical properties of the EMBI in four Latin American countries, namely Argentina, Brazil, Mexico and Venezuela. Specifically, we examine long-range dependence or persistence, non-linearities and structural breaks.

The rest of the paper is structured as follows. Section 2 briefly reviews the existing literature on the EMBI in Latin America. Section 3 outlines the empirical
methodology used for the analysis. Section 4 describes the data and the main empirical results, while Section 5 offers some concluding remarks.

2. Literature Review

There are very few studies on the EMBI in Latin American countries. Fracasso (2007) examines the case of Brazil, and shows that foreign investors’ appetite for risk impacts substantially on EMBI spreads. Nogués and Grandes (2001) argue that in Argentina country risk is mainly determined by macroeconomic variables such as the external debt-to-exports ratio and growth expectations rather than the devaluation risk.

Vargas et al. (2012) provide evidence that in Colombia fiscal consolidation reduces the sovereign risk premium. López-Herrera et al. (2013) find long-run relationships between domestic macroeconomic variables and the Mexican EMBI. Délano and Selaive (2005) examine the behaviour of the Chilean EMBI and conclude that approximately 25% of the variability of the sovereign spread is due to global factors. Finally, the IMF (2010) calculates that a higher investment grade lowers Panamanian debt spreads by over 140 basis points.

Only a few time series studies have analysed the statistical properties of the EMBI. Espinosa et al. (2012) examined non-linearities in the EMBI index in six emerging Eastern European countries, applying the Hinich Portmanteau bi-correlation test, the BDS test, the Engle test and Wavelet theory; they find a non-linear structure at higher and medium frequencies moving towards lower frequencies, that is, from the short to the long term. Flores-Ortega and Villalba (2013) applied GARCH models to forecast the variance and return of several variables, including the Mexican EMBI, over the period from 2005 to 2011.
3. **Methodology**

The methods used here are based on the concept of fractional integration, which is more general than the standard approaches based on integer degrees of differentiation that simply consider the cases of stationarity I(0) and nonstationarity I(1).

For the present purposes, we define an I(0) process as a covariance-stationary one for which the infinite sum of the autocovariances is finite. This includes the white noise case, but also weakly dependent (stationary) ARMA-type processes. Instead a process is said to be fractionally integrated of order d (and denoted by I(d)) if it requires d-differences to make it stationary I(0). In other words, a process \{x_t, t = 0, \pm 1, \ldots\} is said to be I(d) if it can be represented as:

\[(1 - L)^d x_t = u_t, \quad t = 0, \pm 1, \ldots,\]  

with \(x_t = 0\) for \(t \leq 0\), and \(d > 0\), where \(L\) is the lag-operator \((Lx_t = x_{t-1})\) and \(u_t\) is I(0).

Note, however that \(x_t\) can be the errors in a regression model such as

\[y_t = f(z_t; \theta) + x_t, \quad t = 0, \pm 1, \ldots,\]  

where \(z_t\) is a set of deterministic terms that might include an intercept and/or a time trend, and \(f\) can also be of a non-linear form.

First we consider a linear model, where \(z_t\) contains an intercept and linear time trend, such that \(2\) and \(1\) become

\[y_t = \beta_0 + \beta_1 t + x_t, \quad (1 - L)^d x_t = u_t, \quad t = 1, 2, \ldots,\]  

under the assumptions of white noise and autocorrelated errors in turn. We estimate the differencing parameter \(d\) using a Whittle parametric function in the frequency domain (Dahlhaus, 1989); other maximum likelihood methods (Sowell, 1992; Beran, 1995) produced essentially the same results (not reported). We also apply semi-parametric methods; in particular, we use a “local” Whittle approach introduced by Robinson
(1995) and later developed by Abadir et al. (2007) and others. Further, the possibility of non-linear structures in the presence of fractional integration is examined taking the approach of Cuestas and Gil-Alana (2015), who use Chebyshev’s polynomials in time as an alternative to linear trends. Such polynomials, defined as

\[ P_{0,T}(t) = 1, \]
\[ P_{i,T}(t) = \sqrt{2} \cos \left( i \pi \left( t - 0.5 \right) / T \right), \quad t = 1, 2, \ldots, T; \quad i = 1, 2, \ldots \]  

(4)
offer various advantages. First, the fact that they are orthogonal means that one avoids the problem of near collinearity in the regressors matrix that typically occurs in the case of standard time polynomials; second, this specification makes it possible to approximate highly non-linear trends with rather low-degree polynomials (Bierens, 1997); third, their shape is ideally suited for modeling cyclical behaviour. We also investigate stability using recursive and rolling-window methods for the estimation of the fractional differencing parameter. Finally, a model combining fractional integration and structural breaks at unknown points in time (Gil-Alana, 2008) is estimated.

4. Data and Empirical Results

The EMBI series analysed are monthly and cover the period from January 1997 to June 2015. The data source in each case is the Central Bank of the corresponding country.

Figure 1 displays the plots of the four series. It can be seen that in the case of Argentina there is an upward shift around 2002 and a downward one after three and a half years, in July 2005. The Brazilian series exhibits two peaks, in January 1999 and August 2002 respectively, before a sharp decline. In the case of Mexico there is a peak in September 1998, followed by a downward trend. Finally, the Venezuelan series peaks in September 1998 (the same date as in Mexico), December 2008 and June 2015.
As a first step we consider the linear model given by equation (3) and estimate the fractional differencing parameter for the three standard cases found in the literature, i.e., those of no deterministic terms, \((\beta_0 = \beta_1 = 0\) in (3)), an intercept \((\beta_0\) unknown and \(\beta_1 = 0\)) and an intercept with a linear time trend \((\beta_0 \text{ and } \beta_1 \text{ unknown})\). The results are displayed in Table 1 for uncorrelated (white noise) and autocorrelated errors (as in Bloomfield, 1973) respectively, the latter being a non-parametric approach that produces errors decaying exponentially as in the ARMA case.

[Insert Table 1 about here]

It can be seen that under the white noise specification the unit root null hypothesis is rejected in favour of orders of integration higher than 1 in the case of Argentina, Brazil and Mexico. For Venezuela the estimated value of \(d\) is also above 1 but the unit root null (i.e. \(d = 1\)) cannot be rejected. When using the exponential model of Bloomfield (1973), all the estimated parameters are below 1, and the unit root cannot be rejected for Brazil and Venezuela, but it is rejected in favour of mean reversion (i.e., \(d < 1\)) in the case of Argentina and Mexico.

[Insert Table 2 and Figure 2 about here]

Because of the differences in the results depending on the specification of the error term, we also apply a semi-parametric method that does not require modelling assumptions about the error term. The results reported in Table 2 are for selected bandwidth parameters, while Figure 2 displays the estimated values of \(d\) for the whole range of values \((m = 1, \ldots, T/2)\); only for Brazil, and in some cases Mexico, is there any evidence of mean reversion.

The possibility of non-linear behaviour is then examined using the approach developed by Cuestas and Gil-Alana (2015). The model specification is the following:
\[ y_t = \sum_{i=0}^{m} \theta_i P_i T(t) + x_t, \quad (1 - L)^d x_t = u_t, \quad t = 1, 2, \ldots, \]  \hspace{1cm} (5)

where \( m = 2 \) to allow for a certain degree of non-linearity. Table 3 displays the results for white noise \( u_t \); similar values were obtained with autocorrelated errors.

[Insert Table 3 about here]

Consistently with Table 1, the estimated values of \( d \) are above 1 and the unit root null hypothesis is rejected in favour of \( d > 1 \) for Argentina, Brazil and Mexico, while it cannot be rejected in the case of Venezuela. However, the coefficients of the Chebyshev’s polynomials are all statistically insignificant, which means that there is no evidence of non-linear trends.

Next we investigate if the fractional differencing parameter changes over time. The stability analysis is based on the results displayed in the lower panel of Table 1, i.e. those for the Bloomfield specification with an intercept, which is chosen using a battery of diagnostics tests on the residuals. Two different approaches are taken: a recursive one, starting with a sample of 60 observations corresponding to the first five years (1997 – 2001), and then adding six more observations at a time, and a rolling one with a window of 60 observations.

Figure 3 displays the estimates of \( d \) using the recursive method. In the case of Argentina, the estimate of \( d \) is initially very low but increases when adding the observations for the following year, and then remains relatively stable. The results for Brazil are rather similar, with an increase in the estimated value of \( d \) around 2002. For Mexico and Venezuela the values are relatively stable, though in the latter case there is a slight increase over time.

[Insert Figures 3 and 4 about here]
The rolling window estimates are reported in Figure 4. They suggest a higher degree of instability and the possible presence of structural breaks. For this reason we employ the Bai and Perron’s (2003) tests for multiple breaks (see also Table 4). Two breaks are detected for Argentina, one in 2001M12, which coincides with the Corralito measures taken by the Argentine government in response to a massive bank run, and the other one in 2005M7, when, buoyed by a strong recovery in the Argentine economy, former president Kirchner obtained an overwhelming triumph in the legislative elections. A break is found in Brazil in 2004M8, at which time the country was experiencing 5% growth in GDP. Two breaks are found in Mexico (1999M12 and 2003M4) and three in Venezuela (2003M12, 2008M9 and 2012M10), possibly reflecting political instability in the latter case.

[Insert Table 4 about here]

Finally, we test for breaks in the context of an I(d) model as in Gil-Alana (2008). The detected breaks coincide with those identified with the Bai and Perron (2003) method in the case of Argentina (2001M12 and 2005M7). For Brazil the break date is found to be two months before (2004M6); for Mexico, the dates coincide for the first break (1999M12) but not for the second one, now estimated to occur in 2008M3; finally for Venezuela a single break is now found in 2008M9.

Table 5 and 6 display the estimated coefficients for each country and each subsample under the assumption of white noise and autocorrelated (Bloomfield) disturbances respectively. It can be seen that for Argentina the unit root null hypothesis cannot be rejected in the first two subsamples, but is rejected in favour of $d > 1$ after 2005M7. For Brazil, the two orders of integration are significantly higher than 1. For Mexico, the unit root null cannot be rejected in any of the three subsamples, while for
Venezuelan unit root is found in the first subsample, and an order of integration significantly higher than 1 after the break at 2008M9.

[Insert Tables 5 and 6 about here]

When allowing for autocorrelated errors, the break dates coincide with those identified with white noise disturbances, but the estimates of $d$ are much lower and the confident bands wider. For Argentina, the estimated values of $d$ are 0.53, 0.23 and 0.82 respectively for the first, second and third subsample, although the confidence bands imply that mean reversion only takes place in the second subsample. For Brazil, the two estimates of $d$ are smaller than 1 but the unit root null hypothesis cannot be rejected in either of the two subsamples. For Mexico the estimated value of $d$ increases from 0.15 in the first subsample to 0.49 in the second one and to 0.66 in the third one, and mean reversion occurs in the first two cases. For Venezuela, the estimated value of $d$ also increases from 0.63 to 0.96 and mean reversion is found only in the first subsample.

5. Conclusions

The EMBI is a key benchmark for emerging sovereign debt markets. However, very limited empirical evidence is available concerning its behaviour in Latin America. The present study fills this gap by examining it in four countries belonging to this region (Argentina, Brazil, Chile and Mexico), and investigating in particular long-range dependence or persistence, as well as possible non-linearities and structural breaks. Moreover, it uses a fractional integration framework which is more general than the standard approach based on the I(0)/I(1) dichotomy.

Both parametric and semi-parametric methods are applied. The evidence based on the former is sensitive to the specification for the error terms, whilst the results from the latter are more conclusive in ruling out mean reversion. Further, non-linearities do
not appear to be present. Both recursive and rolling window methods identify a number of breaks, which can be plausibly be interpreted in terms of some well-known political and economic developments in the countries of interest. Overall, the evidence of long-range dependence as well as breaks suggests that active policies might be necessary for achieving financial and economic stability in these countries.
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Figure 1: EMBI

|            | ARGENTINA | BRAZIL |
|------------|-----------|--------|
| MEXICO     |           |        |
| VENEZUELA  |           |        |

![Graphs](image-url)
Table 1: Estimates of $d$ based on a parametric method

| Country   | No regressors | An intercept | A linear time trend |
|-----------|---------------|--------------|---------------------|
| ARGENTINA | 1.24 (1.11, 1.42) | 1.24 (1.11, 1.43) | 1.24 (1.11, 1.43) |
| BRAZIL    | 1.24 (1.11, 1.41) | 1.30 (1.15, 1.48) | 1.30 (1.15, 1.48) |
| MEXICO    | 1.10 (0.98, 1.25) | 1.19 (1.04, 1.39) | 1.19 (1.04, 1.39) |
| VENEZUELA | 1.11 (1.00, 1.26) | 1.10 (0.98, 1.25) | 1.10 (0.98, 1.25) |

i) White noise errors

| Country   | No regressors | An intercept | A linear time trend |
|-----------|---------------|--------------|---------------------|
| ARGENTINA | 0.82* (0.71, 0.95) | 0.80* (0.69, 0.95) | 0.80* (0.69, 0.95) |
| BRAZIL    | 0.87 (0.73, 1.08) | 0.80 (0.65, 1.04) | 0.80 (0.63, 1.04) |
| MEXICO    | 0.83* (0.70, 0.98) | 0.63* (0.52, 0.79) | 0.61* (0.47, 0.77) |
| VENEZUELA | 0.84 (0.68, 1.01) | 0.80 (0.64, 1.01) | 0.81 (0.66, 1.01) |

ii) Autocorrelated errors

*: Evidence of mean reversion at the 5% level.

Table 2: Estimates of $d$ based on a semiparametric method

|          | ARGENTINA | BRAZIL | MEXICO | VENEZUELA | Conf. Intv. |
|----------|-----------|--------|--------|-----------|-------------|
| 10       | 1.038     | 0.688* | 0.687* | 0.936     | (0.739, 1.260) |
| 11       | 1.127     | 0.711* | 0.736* | 0.864     | (0.752, 1.247) |
| 12       | 1.201     | 0.728* | 0.801  | 0.835     | (0.762, 1.237) |
| 13       | 1.143     | 0.755* | 0.862  | 0.872     | (0.771, 1.228) |
| 14       | 1.071     | 0.724* | 0.875  | 0.920     | (0.780, 1.219) |
| 15       | 1.071     | 0.701* | 0.917  | 0.908     | (0.787, 1.212) |
| 16       | 1.089     | 0.739* | 0.935  | 0.848     | (0.794, 1.205) |
| 17       | 1.091     | 0.773* | 0.991  | 0.834     | (0.800, 1.199) |
| 18       | 1.079     | 0.749* | 0.887  | 0.825     | (0.806, 1.193) |
| 19       | 1.102     | 0.717* | 0.890  | 0.852     | (0.811, 1.188) |
| 20       | 1.120     | 0.688* | 0.819  | 0.861     | (0.816, 1.183) |

*: Evidence of mean reversion at the 5% level.
Figure 2: Estimates of $d$ based on the semiparametric method

|           | ARGENTINA | BRAZIL |
|-----------|-----------|--------|
|           |           |        |
| $d$       | 1.22      | 1.29   |
|           | (1.08, 1.35) | (1.14, 1.37) |
| $\theta_1$ | 3399.78  | 212.60 |
|           | (0.41)    | (0.09) |
| $\theta_2$ | 88.39    | 273.69 |
|           | (0.01)    | (0.18) |
| $\theta_3$ | -769.29  | 2.701  |
|           | (-1.08)   | (0.005) |
| $\theta_4$ | -1337.32 | -74.542 |
|           | (-1.08)   | (-0.23)|

The thick lines refer to the 95% confidence intervals of the I(1) case.

Table 3: Estimated coefficients in a model with non-linear deterministic trends

|           |           |        |        |        |        |
|-----------|-----------|--------|--------|--------|--------|
|           | $d$       | $\theta_1$ | $\theta_2$ | $\theta_3$ | $\theta_4$ |
| ARGENTINA | 1.22      | 3399.78  | 88.39   | -769.29 | -1337.32 |
|           | (1.08, 1.35) | (0.41)  | (0.01)  | (-1.08) | (-1.08)  |
| BRAZIL    | 1.29      | 212.60   | 273.69  | 2.701   | -74.542 |
|           | (1.14, 1.37) | (0.09)  | (0.18)  | (0.005) | (-0.23) |
| MEXICO    | 1.17      | 34.89    | 170.54  | 87.33   | 45.82   |
|           | (1.02, 1.35) | (0.04)  | (0.32)  | (0.40)  | (0.34)  |
| VENEZUELA | 1.10      | 162.89   | 37.00   | 200.60  | -58.35  |
|           | (0.98, 1.25) | (0.08)  | (0.03)  | (0.36)  | (-0.16) |

The values in the parenthesis are in the second column, the 95% confident intervals, and in the remaining columns they are their corresponding t-values.
Figure 3: Recursive estimates of $d$ adding six observations at a time

The dotted lines refer to the 95% confidence bands for the values of $d$. 
Figure 4: Recursive estimates of $d$ with rolling-windows of 60 observations

The dotted lines refer to the 95% confidence bands for the values of $d$. 
### Table 4: Estimated break dates using Bai and Perron’s (2003) method

| Series      | Number of breaks | Break dates          |
|-------------|------------------|----------------------|
| ARGENTINA   | 2                | 2001M12, 2005M7      |
| BRAZIL      | 1                | 2004M8               |
| MEXICO      | 2                | 1999M12, 2003M4      |
| VENEZUELA   | 3                | 2003M12, 2008M9, 2012M10 |

### Table 5: Estimated coefficients with breaks and I(d) behaviour and uncorrelated errors

| Series      | Breaks      | Date breaks          | 1st subsample | 2nd subsample | 3rd subsample |
|-------------|-------------|----------------------|---------------|---------------|---------------|
| ARGENTINA   | 2           | 2001M12, 2005M7      | 1.16          | (0.81, 1.69)  | 0.75          | (0.49, 1.50)  | 1.24          | (1.08, 1.46)  |
| BRAZIL      | 1           | 2004M8               | 1.30          | (1.09, 1.60)  | 1.21          | (1.07, 1.41)  | ---           |               |
| MEXICO      | 2           | 1999M12, 2003M4      | 1.24          | (0.90, 1.82)  | 1.03          | (0.81, 1.34)  | 1.17          | (0.99, 1.43)  |
| VENEZUELA   | 1           | 2008M9               | 1.01          | (0.86, 1.22)  | 1.19          | (1.02, 1.44)  | ---           |               |

### Table 6: Estimated coefficients with breaks and I(d) behaviour and autocorrelated errors

| Series      | Breaks      | Date breaks          | 1st subsample | 2nd subsample | 3rd subsample |
|-------------|-------------|----------------------|---------------|---------------|---------------|
| ARGENTINA   | 2           | 2001M12, 2005M7      | 0.53          | (-0.02, 1.14) | 0.23*         | (0.62, 1.13)  |
| BRAZIL      | 1           | 2004M8               | 0.75          | (0.43, 1.14)  | 0.89          | (0.59, 1.20)  | ---           |               |
| MEXICO      | 2           | 1999M12, 2003M4      | 0.15*         | (-0.43, 0.84) | 0.49*         | (0.28, 0.85)  | 0.66          | (0.33, 1.12)  |
| VENEZUELA   | 1           | 2008M9               | 0.63*         | (0.46, 0.86)  | 0.96          | (0.71, 1.31)  | ---           |               |

*: Evidence of mean reversion at the 5% level.
Figure 3: Estimated trends in the model based on white noise errors

| ARGENTINA | BRAZIL |
|-----------|--------|
| ![Graph](image1.png) | ![Graph](image2.png) |

| MEXICO | VENEZUELA |
|--------|-----------|
| ![Graph](image3.png) | ![Graph](image4.png) |
Figure 4: Estimated trends in the model based on autocorrelated errors

| ARGENTINA          | BRAZIL          |
|--------------------|-----------------|
| ![Graph for Argentina](image) | ![Graph for Brazil](image) |

| MEXICO            | VENEZUELA       |
|-------------------|-----------------|
| ![Graph for Mexico](image) | ![Graph for Venezuela](image) |