First-principles structural optimization and electronic structure of the superconductor picene for various potassium doping levels

Taichi Kosugi¹, Takashi Miyake¹,², Shoji Ishibashi¹, Ryotaro Arita²,³,⁴, and Hideo Aoki⁵
¹Nanosystem Research Institute “RICS”, AIST, Umezono, Tsukuba 305-8568, Japan
²Japan Science and Technology Agency (JST), CREST, Honcho, Kawaguchi, Saitama 332-0012, Japan
³Department of Applied Physics, University of Tokyo, Hongo, Tokyo 113-8656, Japan
⁴Japan Science and Technology Agency (JST), PRESTO, Kawaguchi, Saitama 332-0012, Japan
⁵Department of Physics, University of Tokyo, Hongo, Tokyo 113-0033, Japan

We theoretically explore the crystal structures of K₃picene, for which a new aromatic superconductivity has recently been discovered for x = 3, by systematically performing first-principles full structural optimization covering the concentration range x = 1-4. The crystal symmetry (space group) of the pristine picene is shown to be preserved in all the optimized structures despite significant deformations of each picene molecule and vast rearrangements of herringbone array of molecules. For Kₓpicene (x = 1-4) optimization indicates that (i) multiple structures exist in some cases, and (ii) dopants can enter in the intralayer region as well as in the interlayer region between the stack of herringbone structures. In the electronic structure obtained with the local density approximation for the optimized structures, the rigid-band approximation is invalidated for multifold reasons: the dopants affect the electronic properties not only through the rearrangement and distortion of molecules, but also through hybridizations between the molecules and metal atoms.

As a consequence the resultant Fermi surface exhibits a variety of multiband structures which take diverse topology for K₃picene and Kₓpicene.

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I. INTRODUCTION

The discovery of superconductivity in potassium-doped solid picene, K₃picene, with Tc = 7-18 K for a doping level x ≃ 3, recently reported by Mitsuhashi et al. [1], is seminal as the first aromatic superconductor. This is expected to open a new avenue in quest for organic superconductors. The occurrence of superconductivity in the doped picene should not be an exceptional case, since the discovery has been followed by a more recent report of superconductivity in another of aromatic compounds, coronene, by Kubozono et al. [2] with Tc up to 15 K for Kₓcoronene with x ≃ 3, and also in doped phenanthrene with Tc up to 5 K for x ≃ 3 by Wang et al. [3]. These aromatic compounds are now forming a new class in the family of carbon-based superconductors that include graphite-intercalation compounds (GICs) and doped fullerenes. For GIC, KₓC₆₀, the first carbon-based superconductor with Tc = 0.1 K [4], is followed by CaC₆₀ with the highest Tc = 11.6 K among GICs [5]. Doped fullerene KₓC₆₀, a superconductor with Tc = 20 K [6], is followed by Cs₂RbC₆₀ with Tc = 33 K [7], and Cs₃C₆₀ with Tc = 40 K under 15 kbar [8] or Tc = 38 K under 7 kbar [9].

The electronic structures of pristine and doped picene were first obtained by the present authors [10] as an initial step to elucidate the mechanism of superconductivity. It has been revealed that the conduction band group is derived from the lowest unoccupied molecular orbital (LUMO) and LUMO+1 of a picene molecule. The conduction-band structure of solid picene, where the molecules are arrayed in a herringbone structure with two molecules per unit cell, is indeed shown to be accurately reproduced by a four-orbital tight-binding model downfolded in terms of the maximally-localized Wannier functions [11]. We have also determined the dopant positions for Kₓpicene, where we have employed the experimental lattice parameters. Andres et al. [12], on the other hand, provided two, fully-optimized geometries of Kₓpicene, one with a herringbone structure and the other with a laminar structure. Giovannetti and Capone [13] performed an electronic structure calculations with different exchange-correlation functionals, and found that a hybrid functional leads to an antiferromagnetic state in Kₓpicene. Kim et al. [14] demonstrated that an antiferromagnetic state is stabilized in Kₓpicene when the volume is increased. They, as well as Giovannetti and Capone, suggested that a strong electron correlation exists in the system. This is reasonable in that the electronic correlation energy in solid picene is estimated to be U ≃ 0.85 eV with the momentum-dependent electron-energy-loss spectroscopy [15], which is actually greater than the width of the LUMO- and LUMO+1-derived conduction bands. This is also the case for potassium-doped picene, as will be demonstrated below.

Since the report of the superconductivity in potassium-doped picene, a few theoretical studies aiming at clarifying its mechanism of superconductivity has been reported. These include phonon studies such as Kato et al. [16], who have estimated the phonon frequencies and the electron-phonon coupling for various hydrocarbon molecules. For picene they found that the electron-phonon coupling is large enough to attain Tc ≃ 10 K. Subedi and Boeri [17] calculated the electron-phonon interaction in doped picene within the rigid-band approximation, and obtained coupling constants large enough to
explain the experimental $T_c \simeq 18$ K in K$_3$picene. Casula et al. \cite{18} performed a more elaborate calculation, and obtained the electron-phonon coupling large enough to explain the experimental $T_c \simeq 7$ K, to which they found the dopant and intermolecular phonon modes contribute significantly.

However, one essential question is: what is so special about K$_3$picene as opposed to other values of $x$? The question is important, since it should be intimately related to another question: to what extent the aromatic superconductivity is general. We can for instance remember that the problem of why $A_3$ fullerene ($A$: alkali metal elements) is special played an important role in elucidating its electronic properties. One experimentally unresolved situation is that, in the doped picene, both its atomic structure and even the number of dopant atoms actually accommodated in the samples have yet to be experimentally determined, although there are some estimates as discussed in Ref.\cite{2}. Given the circumstance, a theoretical prediction for the geometry of doped picene is thus desirable, especially for systematically varied doping levels. This will also give a starting point to discuss whether the superconductivity is driven by a phonon mechanism, or by an electronic mechanism as in some classes of organic superconductors\cite{11}.

This is exactly the purpose of the present work. For organic materials, not only the atomic positions but also the unit cell should be relaxed for a reliable optimization of the geometry. Hence we have performed here the full structural optimization of K$_x$picene, covering the concentration range $x = 1-4$.

II. METHOD

For the electronic structure calculation and the structural optimization in the present work, we adopt the density-functional theory with the projector augmented-wave (PAW) method\cite{20} with the Quantum MAterials Simulator (QMAS) package\cite{21} in the local density approximation (LDA)\cite{22}. The Bloch pseudofunctions are expanded in plane waves, with an energy cutoff of 40 Ry throughout the present work. All the self-consistent field calculations are performed with $4 \times 4 \times 4$ $k$ points. The structural optimization allows the atomic coordinates and the cell parameters to be relaxed with no constraint imposed on them. In each iteration of the self-consistent field calculation, the forces and stress\cite{23} felt by the system are calculated. The optimization is regarded as converged when the largest force and stress are smaller than $5 \times 10^{-5}$ $\text{Ry/}a_{B}$ and $5 \times 10^{-7}$ $\text{Ry/}a_{B}^3$, respectively. We employ the maximally-localized Wannier function technique\cite{11}, which has been recognized to be a standard method for describing electronic orbitals in solid. There, Wannier functions are constructed from the Bloch wave functions belonging to the specified electronic bands. In the present work we extract the transfer integrals between the localized Wannier functions constructed for the solid picene.

III. RESULTS

Pristine solid picene comprises molecular layers stacked in the $c$ direction, as depicted in Fig. 1. In each layer, picene molecules are in a herringbone arrangement, which means a unit cell contains two molecules. The crystal lattice is monoclinic with space group $P2_1$. Its lattice parameters are reported to be $a = 8.480, b = 6.154, c = 13.515$ in $\text{Å}$, and the angle $\beta = 90.46^\circ$ between $a$ and $c$ axes from a single-crystal X-ray diffraction experiment.\cite{23} The samples used by Mitsuihashi et al.\cite{1} had the same lattice parameters.

Let us first classify the candidate positions into which dopants can be accommodated. A conventional organic insulator, solid pentacene, where each molecule has the same chemical formula C$_{22}$H$_{14}$ as picene but five benzene rings are connected on a straight line with zigzag edges, is known to accommodate dopants in its interlayer region when doped with alkali elements,\cite{24} with its $c$ axis significantly expanded. By contrast, the $c$ axis of picene is reported to shrink when potassium-doped with $x = 2.9$.\cite{1} This suggests that the dopants have intruded into the intralayer region of solid picene. To determine whether intralayer insertion of potassium atoms is energetically more favorable than interlayer insertion, we performed in our previous work\cite{10} a structural optimization by locating a potassium atom on different positions on the $ab$ plane of the pristine picene as initial geometries, and found that the intralayer insertion is in fact energetically favorable. In the present work, we hence explore optimized geometries of the dopants with intralayer insertion.

The optimized lattice parameters and the internal coordinates of potassium atoms are summarized in Table I. The crystal symmetry of pristine picene was found to be preserved in all the optimized doped structures, despite significant deformations of each molecule from the planar shape along with significant rearrangements of molecules upon doping. The preserved symmetry contrasts with the situation in K$_3$coronene, for which we have shown that doping lowers the symmetry.\cite{25} The geometries, the electronic band structures, the densities of states, and the Fermi surfaces for the optimized structures are shown for K$_x$picene in Fig. 2 for K$_2$picene in Fig. 3 and for K$_3$picene in Fig. 4. In each case, the conduction band group comprises four bands, which have main characters of LUMO and LUMO+1 of an isolated picene molecule. Since the herringbone structure has two molecules per unit cell, we have constructed four maximally-localized wave functions (WFs) from the four bands around the Fermi level of the individual. For each of them, two WFs, $\psi_3$ and $\psi_4$, localized at each molecule with higher and lower orbital energies were obtained as shown in Fig. 3.
to each other.

K layers stacked in the picene (drawn with VESTA[24]), which comprises molecular layers in the intralayer region and another in the interlayer region as the initial positions of the optimization, while K is 0.36 eV per molecule, the picene molecules have metallic electronic band structures. The width of the band group consisting of four around their Fermi level is 0.36 for K1(A), and 0.52 eV for K1(B).

A. K1picene

Let us start with K1picene. Two structures, K1(A) and K1(B), have been obtained. K1(A) appears when we put one potassium atom per molecule in the intralayer region as the initial position of the optimization, while K1(B) appears when we put the dopant in interlayer. In both structures, the dopants end up with intralayer positions after the optimization. The insertion of the dopants into the intralayer region supports the result of our previous work[10]. In K1(B), with a total energy higher than in K1(A) by 0.316 eV per molecule, the picene molecules are more strongly twisted than in K1(A). Both systems have metallic electronic band structures. The width of the band group consisting of four around their Fermi level is 0.36 for K1(A), and 0.52 eV for K1(B).

B. K2picene

K2picene structure was obtained by putting one potassium atom in the intralayer region and another in the interlayer region as the initial positions of the optimization, where we confirmed that an additional atom doped into K1picene again prefers the intralayer region by moving to an intralayer position after the optimization. The obtained K2picene is an insulator, with a band gap of 0.638 eV at X. The widths of the highest occupied and the lowest unoccupied band groups are 0.21 and 0.29 eV, respectively. By analyzing the projected density of states for the WFs, we find that each of the two bands has comparable weights for the two types of the Wannier functions w_h and w_l.

C. K3picene

For K3picene we first obtain K3picene(A) structure by putting three potassium atoms in the intralayer region as the initial positions for the optimization. Andres et al. [12] obtained the monoclinic K3picene structure with a = 7.359, b = 7.361, c = 14.018 in Å and β = 105.71°, in which the potassium atoms are all in the intralayer region. We have also tried a structural optimization start-

![Figure 1](image-url)
FIG. 2: (Color online) Geometries (large spheres: K atoms), electronic band structures, densities of states, and Fermi surfaces of the K$_1$ structures. The origins of energy are set to the respective Fermi level.

Then the geometry resulted in another structure, which we call K$_2$picene(B) here. Although the lattice parameters of K$_3$(A) and K$_3$(B) are close to each other with the difference in the total energy being only 1 meV per molecule, they are distinct in the positions of dopants, as seen in Table I and in Fig. 4. K$_3$picene(B) has the lattice parameters and the dopant positions close to those of the K$_3$picene structure obtained by Andres et al. [12], and we therefore consider the two structures to be the same. K$_3$(A) and K$_3$(B) have metallic electronic band structures with the same width 0.6 eV of the band group consisting of four around their Fermi level.

Since the superconductivity in potassium-doped picene was observed for $x \simeq 3$, [1, 2] more elaborate exploration of geometries is required than for other concentrations. We have in fact found another structure, which we call K$_2$K$_1$picene, by putting two potassium atoms in the intralayer region and one in the interlayer region as the initial positions for the optimization. This structure is higher in the total energy than the K$_3$(A) structure by 0.465 eV per molecule. However, the lattice parameters are closer to the experimental results [1] of $a = 8.707$, $b = 5.912$, $c = 12.97$ in Å, and $\beta = 92.77^\circ$ for K$_2$picene. The electronic band structure is again
metallic for the $K_2K_1$ structure. The four bands around the Fermi level, whose width is 0.51 eV, are close to the higher bands as compared with those in the $K_3(A)$ and $K_3(B)$ structures.

Each of $K_3(A)$ and $K_3(B)$ has multiple Fermi surfaces comprising a pocket and complicated, connected surfaces. The existence of a Fermi pocket implies three-dimensional electron transfer integrals despite the layered structure. On the other hand, $K_2K_1$ has one-dimensional (a pair of planar) Fermi surfaces along with connected surfaces. We can also note that, while the Fermi surface of $K_3$coronene also consists of multiple surfaces, the topology of the Fermi surfaces for $K_3$coronene (consisting of a pair of quasi-one-dimensional, planar surfaces and another pocket) differs from those found here for $K_3$picene(A) and $K_3$picene(B) (consisting of multiple surfaces of two- or higher dimensional characters), and for $K_2K_1$picene (consisting of a pair of quasi-one-dimensional, planar surfaces and another, multiply-connected one).

The largest interlayer transfer integral of the WFs in $K_3(A)$ ($K_2K_1$) is 13.6 (19.6) meV, while that in undoped picene is 14.6 meV. The larger interlayer transfer integrals in $K_2K_1$ than in $K_3(A)$ originate in the presence of dopants in the interlayer region. The widths of the bands around the Fermi level in these doped structures are larger than in undoped picene (0.39 eV), though $K_3(A)$ has the smaller interlayer transfer integrals. It implies that their larger band widths come from the enhanced intralayer transfers of electrons due to the hybridization of the wave functions of potassium atoms and the molecular orbitals. In fact, the largest interlayer transfer integral in $K_3(A)$ ($K_2K_1$) is 82.7 (70.6) meV, which is much larger than that in undoped picene, 57.9 meV. The intermolecular transfer integrals between the WFs of $K_3(A)$picene and $K_2K_1$picene are shown in Fig. 7. It is seen that $K_3(A)$ allows for the transfers between more distant WFs in the $a$ direction, which leads to its more two-dimensional and wider band dispersion than $K_2K_1$.

D. $K_4$picene

We have obtained the $K_4$picene structure by putting three potassium atoms in the intralayer region and one in the interlayer region as the initial positions of the optimization, because the three dopants sitting on every other benzene rings out of five rings in each picene molecule may tend to push the fourth dopant to the interlayer region. In the optimized structure, all the four dopants end up with sitting in the intralayer region, but two of them are rather close to the interlayer region due to the crowded space. The system is an insulator with a band gap of 0.36 eV. The highest occupied band group consists of two bands, separated from the second highest group of two bands by 0.01 eV. The widths of the higher and lower band groups are 0.17 and 0.20 eV, respectively. By analyzing the projected density of states for the WFs, we found that the higher and lower occupied band groups consist mainly of $w_3$ and $w_1$, respectively. This contrasts with the situation in another insulator, $K_2$picene.

E. Discussions

For each concentration $x$, the lowest-energy structure shown above contains the dopants in the intralayer region. This behavior is consistent with the observed tendency of the $c$ axis of $K_4$picene, in which the $c$ axis shrinks monotonically with increasing $x$, implying that the dopants move into the intralayer region regardless of the concentration. This is to be contrasted with $Rb_2$picene, whose $c$ axis was observed to expand up to $x = 2$ and shrink afterwards.

In Fig. 6 we have displayed the maximally-localized Wannier functions ($w_3$ and $w_1$ with higher and lower orbital energies, respectively) in the optimized structures for all the cases of $K_4$picene to $K_4$picene. We can see that the WFs have basically the same features for all the structures in that all the WFs have LUMO and LUMO+1 orbital characters, although small but significant amplitudes found around the potassium atoms whose magnitudes depend on the doping level $x$. More precisely, we can show that $w_3$ and $w_1$ have characters of the linear combinations of LUMO and LUMO+1: $w_{3,1} = \phi_{LUMO} \pm \phi_{LUMO+1}$, as in the undoped picene.

However, a key message in the present band structure results is that, although the orbital characters of the WFs are common to all the optimized geometries, their band structures very much differ. This is not surprising, since the molecular shape as well as the herringbone arrangement of molecules distort significantly with doping. More importantly, the lobes of molecular WFs extend outward the molecule via the potassium atoms, with significant hybridizations of WFs around the potassium atoms. Specifically, we find that the small contributions from the potassium wave functions have a $p$ orbital character, as seen in Fig. 6.

In other words, the rigid-band picture is invalidated for multifold reasons, i.e., through the rearrangement and distortion of molecules, but also via hybridization of the potassium $p$ orbitals with the molecular orbitals of picene. Indeed, for all the optimized geometries we have also calculated their band structures (not shown) with potassium atoms removed but the doping level is fixed by shifting the chemical potential to find that the band structures are drastically changed from those of the doped systems. As a consequence the resultant Fermi surface exhibits a variety of multiband structures which take diverse topology for $K_1$picene and $K_3$picene. This obviously provides an intriguing starting point for exploring mechanisms of superconductivity as a future work.

Final point of interest, about the molecular species dependence, is the following: we can note that the calculated band structures for all $x$ (including $x = 0$)
FIG. 4: (Color online) Geometries (large spheres: K atoms), electronic band structures, densities of states, and Fermi surfaces of the K₃picene. The origins of energy are set to the respective Fermi level.

have significant dispersion along the c direction as well as along the a and b directions, which indicates isotropic components in the electron transfers. If we compare this with the situation in K₃coronene, we find that the band dispersion is more anisotropic in both undoped coronene and K₃coronene²⁷, which reflects the differences between the intermolecular distances in each direction.
IV. SUMMARY

We have systematically performed a full structural optimization for $K_4$picene, covering the doping level $x = 1$-4. The crystal symmetry of pristine picene of $P2_1$ was found to be preserved in all the optimized structures despite the deformation and rearrangements of the molecules upon doping. The optimized systems for $K_1$picene and $K_3$picene have metallic band structures, while band gaps open around their Fermi levels for $K_2$picene and $K_4$picene. In each of the optimized systems, the electronic bands in the vicinity of the Fermi level are derived from LUMO and LUMO+1 of the aromatic molecule as in the undoped picene. We found that the presence of dopants affects the electronic properties of all the doped structures. The electronic structures obtained with the local density approximation for the optimized structures reveal that the rigid-band approximation is invalidated due to the rearrangement and deformation of molecules and the accompanied charge redistribution between the molecules and dopants. The resultant Fermi surface exhibits a variety of multiband structures which take diverse topology for $K_4$picene and $K_5$picene.

In all the optimized systems, the widths of the LUMO- and LUMO+1-derived bands do not exceed 0.6 eV, which are much smaller than the experimental electronic correlation energy $U \approx 0.85$ eV, indicating that the material may be a strongly correlated electronic system. Further investigations for clarifying the material properties and the mechanism of superconductivity in doped picene should thus take into account the magnetic instability and the strong Coulomb interaction, as pointed out by Giovanetti and Capone and Kim et al.

$Rb_{3.1}$picene and $Ca_{1.5}$picene have also been reported to become superconducting with $T_c \approx 7$ K, which indicates that the transfer of three electrons from the alkali atoms to a picene molecule can lead to superconductivity in alkali-doped picene. Theoretical exploration of their possible geometries is needed, where $Rb_2$picene is expected to accommodate dopants in the interlayer region due to a larger atomic radius of $Rb$ than in $K_2$picene.

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FIG. 6: (Color online) Maximally-localized Wannier functions in the optimized structures for K\textsubscript{1}picene (a), K\textsubscript{2}picene (b), K\textsubscript{3}picene(A) (c), K\textsubscript{2}K\textsubscript{1}picene (d), and K\textsubscript{4}picene (e). \(w_h\) and \(w_l\) stand for the higher- and lower-energy states, respectively.

FIG. 7: (Color online) Significant \(|t| > 30\text{ meV}\) transfer integrals \(t\) between Wannier functions, two at each molecule, are depicted with arrows for K\textsubscript{3}picene(A) (a), and K\textsubscript{2}K\textsubscript{1}picene (b).

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