Characterizing the pulsations of the ZZ Ceti star KUV 02464+3239

Zs. Bognár,1⋆ M. Paparó,1 P. A. Bradley2 and A. Bischoff-Kim3

1Konkoly Observatory of the Hungarian Academy of Sciences, PO Box 67, H-1525 Budapest, Hungary
2X-4, MS T-087, Los Alamos National Laboratory, Los Alamos, NM 87545, USA
3Department of Chemistry, Physics and Astronomy, Georgia College & State University, CBX 82, Milledgeville, GA 31061, USA

Accepted 2009 July 21. Received 2009 July 21; in original form 2009 April 29

ABSTRACT
We present the results on period search and modelling of the cool DAV star KUV 02464+3239. Our observations resolved the multiperiodic pulsational behaviour of the star. In agreement with its position near the red edge of the DAV instability strip, it shows large amplitude, long-period pulsation modes, and has a strongly non-sinusoidal light curve. We determined six frequencies as normal modes and revealed remarkable short-term amplitude variations. A rigorous test was performed for the possible source of amplitude variation: beating of modes, effect of noise, unresolved frequencies or rotational triplets. Among the best-fitting models resulting from a grid search, we selected three that gave \( l = 1 \) solutions for the largest amplitude modes. These models had masses of 0.645, 0.650 and 0.680 \( M_\odot \). The three ‘favoured’ models have \( M_\text{eff} \) between \( 2.5 \times 10^{-3} \) and \( 6.3 \times 10^{-6} \) \( M_\odot \), and give 14.2–14.8 mas seismological parallax. The 0.645 \( M_\odot \) (11400 K) model also matches the spectroscopic log \( g \) and \( T_\text{eff} \) within 1σ. We investigated the possibility of mode trapping and concluded that while it can explain high amplitude modes, it is not required.

Key words: techniques: photometric – stars: individual: KUV 02464+3239 – stars: oscillations – white dwarfs.

1 INTRODUCTION
Since Arlo Landolt’s (1968) discovery of the first DAV (HL Tau 76) we have learned much about pulsating white dwarfs. They are otherwise normal white dwarf stars, and they represent the final stage of about 98 per cent of the stars (see the recent review of Winget & Kepler 2008 and references therein), so it is a key issue to gain insight into their interiors. While white dwarfs are relatively simple to model, some observed phenomena still challenge theory.

One unsolved mystery is the variability of the pulsational modes’ amplitudes and frequencies of Planetary Nebula Nucleus Variable (PNNV), cool DBV and cool DAV stars (Handler 2003a). While we can find very stable modes in certain white dwarfs which can be used to measure evolutionary effects (cooling and/or contraction; e.g. hot DAVs G117-B15A and R548 – ‘The Most Stable Optical Clocks Known’: Mukadam, Kepler & Winget 2001 and references therein), in some cases short-term variations make it difficult to determine even the pulsational modes. An example for this latter is the case of PG 1115+158 (DBV) with its remarkably unstable amplitude spectra (Handler 2003b).

In some cases, we encounter strange, sudden, short-term variations in the pulsational behaviours of stars: for example the ‘sfiorzando’ effect observed in the DBV star GD 358 in 1996, where the non-linear light curve of the star changed into a high amplitude, remarkably sinusoidal one for a short period of time (Kepler et al. 2003; Provencal et al. 2009). In the case of PG 1456+103 its luminosity variations almost disappeared just before the Whole Earth Telescope (WET; Nather et al. 1990) run started on the star (Handler 2003a). The frequency and amplitude variations of multiplet components (mostly for high \( k \) modes) observed in GD 358 (Provencal et al. 2009) are further examples for short-term variations.

Possible explanations for these observed phenomena could be non-linear mode coupling, convection/pulsation interactions, mode excitation and beating of different pulsation modes – such as unresolved rotational splitting. To find the right explanation(s) for a certain case is a great challenge. A crucial first step is to identify the periods of the true pulsation modes of a white dwarf.

One possible way of mode identification when strong amplitude variations occur is to observe the star in many seasons, determine all the observed periods from the different runs and search for the (nearly) equidistant period spacings among them, which can be consecutive overtones with the same horizontal degree (\( l \)) value. Kleinman et al. (1998) used this method for the first time for a DAV star (G29-38) where recurring sets of normal modes were identified.

Since KUV 02464+3239 was found to be a luminosity variable DA star near the red edge of the DAV instability strip (Fontaine et al. 2001), we expect to find the short-term variations which characterize the pulsation of similar stars. Using a 2900-s-long light curve, Fontaine et al. (2001) determined a quasi-period of ~832 s for the star’s light variation. The long-period, large amplitude variations they found with strongly non-sinusoidal light curve along with the
presence of harmonic peaks in the frequency spectrum are consistent with the behaviour of a cool DAV star. However, up to now only the results of this short discovery run had been published about this target.

In this paper, we present the results of observational analysis of KUV 02464+3239. We describe our observations and data reduction process in Section 2. The results of Fourier analyses and frequency determination tests can be found in Section 3. Section 4 contains our tests on amplitude variations. We discuss the results of asteroseismological investigations (modelling, results for stellar parameters) in Section 5 and give a brief summary in Section 6.

2 OBSERVATIONS AND DATA REDUCTION

We observed KUV 02464+3239 on 20 nights between 2006 October and 2007 February. The observations were made with a Princeton Instruments VersArray:1300B back-illuminated CCD camera attached to the 1-m Ritchey-Chrétien-Coudé telescope at Piszkéstető mountain station of Konkoly Observatory. The log of observations is in Table 1. We did not use any filter (white light observations) to maximize the photon count from this relatively faint target ($m_v = 16.07\text{mag}$). The back-illuminated detector we used is more sensitive to bluer wavelengths than a front-illuminated one. Note that the amplitude values of the Fourier light curve solution corresponding to these white light measurements differ from filtered ones.

Standard IRAF\(^2\) routines were used during the reduction process; the frames were bias, dark and flat corrected before we performed aperture photometry with the IRAF DAOPHOT package. The observational times of every data point were calculated to Barycentric Julian Date (BJD).

Different apertures were used for every night. For a given night, we chose the aperture size that resulted in the lowest scatter for differential light curves of constant stars in the field.

We used 10 or 30 s exposure times depending on the weather conditions during the observing runs. For 10 s exposure we averaged the data into 30 s bins to keep all the data with the same bin, although we are aware of the fact that for multiperiodic pulsators with nearby pulsations it does introduce an extra uncertainty.

We performed aperture photometry on the same 22 stars for every night. Possible comparison stars were checked for variability and longer term trends (caused by the colour effects of stars with different spectral types) in an iterative way. This process resulted in our choosing the three brightest stars marked in Fig. 1 as a reference system for the differential photometry. The quality of this method is shown by the differential light curve of a check star (C3) compared to the average of the reference stars in Fig. 2.

Following the traditional method of photoelectric photometry, we obtained first-order extinction coefficients for the nights which were long enough. The values lay in the range of 0.07–0.39 in white light.

The colour term of extinction was checked. However, we could not precisely determine the second-order extinction coefficient for each night. In addition to the iterative process, we obtained $BVRI$ photometry to estimate the spectral types of the comparison stars selected in the iterative process. The relative colour indices were checked. The differences between the $B - V$ colour indices are higher than $~0.5$ which shows immediately that the comparison stars have much later spectral types than KUV 02464+3239. Naturally, this deficiency often resulted in trends in the differential light curves and accordingly significant signals in the low-frequency region of their Fourier transform (FT). Although the low-frequency

---

1\ http://www.princetoninstruments.com/products/imcam/versarray/dsheet.aspx

2\ IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.

---

Table 1. Journal of observations of KUV 02464+3239. Subset No. refers to subsets in Section 3.2; $N$ denotes the number of points remained after averaging (see details in text) and $\delta T$ means the time span of the runs including gaps.

| Run No. | Subset No. | Date (UT) | Start time (BJD−2 450 000) | $N$   | $\delta T$ (h) |
|---------|------------|-----------|---------------------------|-------|---------------|
| 01   | 1       | 2006 Oct 06 | 4014.577               | 210   | 2.02          |
| 02   | 1       | 2006 Oct 07 | 4015.584               | 117   | 1.31          |
| 03   | 1       | 2006 Oct 09 | 4017.546               | 216   | 2.37          |
| 04   | 1       | 2006 Oct 11 | 4019.543               | 264   | 2.98          |
| 05   |          | 2006 Oct 25 | 4034.283               | 304   | 6.29          |
| 06   |          | 2006 Nov 26 | 4065.603               | 112   | 1.27          |
| 07   |          | 2006 Nov 27 | 4066.542               | 65    | 0.87          |
| 08   | 2       | 2006 Nov 28 | 4068.206               | 1163  | 11.17         |
| 09   |          | 2006 Dec 07 | 4077.299               | 278   | 4.11          |
| 10   |          | 2006 Dec 08 | 4078.474               | 182   | 1.89          |
| 11   | 3       | 2006 Dec 11 | 4081.169               | 732   | 8.72          |
| 12   |          | 2006 Dec 12 | 4082.435               | 81    | 0.75          |
| 13   |          | 2006 Dec 13 | 4083.176               | 477   | 9.92          |
| 14   | 4       | 2006 Dec 14 | 4084.170               | 1048  | 10.92         |
| 15   | 4       | 2006 Dec 15 | 4085.179               | 877   | 10.56         |
| 16   | 4       | 2006 Dec 16 | 4086.187               | 696   | 7.54          |
| 17   |          | 2006 Dec 17 | 4087.322               | 107   | 1.14          |
| 18   | 4       | 2006 Dec 19 | 4089.208               | 747   | 6.90          |
| 19   |          | 2007 Jan 29 | 4130.216               | 362   | 5.16          |
| 20   |          | 2007 Feb 19 | 4151.289               | 189   | 1.91          |
| Total |          |            |                          | 8227  | 97.80         |

---

Figure 1. Variable and comparison stars in the CCD field. The three brightest stars (C1, C2, C3) were selected as a reference system for the differential photometry.

Figure 2. Differential light curve of the check star (C3) to the average of the reference stars obtained on JD 2 454 086.
signals do not exceed 1–6 mmag, to get a homogeneous data set for the variable star, polynomial fits were performed in the last step of the reduction process. It is widely applied in white dwarf research using multichannel photometry. The light curves obtained for each run can be seen in Fig. 3.

3 FOURIER ANALYSIS

Since the star was not well studied before, our first aim was to find the frequency content. Analyses were made by the use of the MuFRAN (Multi-Frequency Analyzer) package (Kolláth 1990; Csubry & Kolláth 2004). MuFRAN provides efficient tools for frequency determination with its standard analyzer applications (Fast Fourier Transform, Discrete Fourier Transform, linear and non-linear fitting options) and graphic display routines. The program handles unequally spaced and gapped observational data. Frequency values are given in cycle per day (c d$^{-1}$) units.

We followed the standard steps of a pre-whitening process to get frequency, amplitude and phase values utilizing the light curve’s Fourier spectrum. In pre-whitening processes, the question is always when to stop iterating. In deciding whether a peak belongs to a real pulsation frequency, we used the widely accepted approximation: if a peak reaches the threshold of signal-to-noise ratio (S/N) of $\sim$4 it has a small probability of being due to noise (Breger et al. 1993).

The tools of the time string analysis program PERIOD04 (Lenz & Breger 2005) were used to calculate the S/N of the individual peaks. The program determines the signal (S) value as the amplitude of the peak after the least-squares fit. The noise (N) is given as an average amplitude calculated in a frequency range that encloses the peak in the residual spectrum. We determined S/N values from the ±25 c d$^{-1}$ frequency range of peaks after pre-whitening the original FT.

3.1 Investigation of individual nights

Because the pulsation periods are short compared to the typical run length, the one-night long observing runs provide a long enough time base to investigate the basic pulsational characteristic of the star, even in a case if not all the modes are resolved. In addition, a night-by-night analysis allows us to follow the changes in pulsation amplitudes.

Considering the threshold of S/N $\sim$ 4 for the peaks, our results show that the pulsation frequencies of KUV 02464+3239 are at $\sim$87, 97, 104, 111 and 139 c d$^{-1}$. In one case we also find a very significant (S/N = 5.4) signal at $\sim$70 c d$^{-1}$. During the pre-whitening process we did not take into account peaks under 60 c d$^{-1}$ in the FTs. This limit is an overestimation of the frequency range filtered by polynomial fitting, and this means that any possible pulsation frequency below this level remained undiscovered.

Our analysis revealed that remarkable amplitude variations can happen from one night to another as in many cases of PNNV, cool DBV and cool DAV stars (Handler 2003a).

3.2 Analysis of reference intervals

The data set can be grouped into four subsets of selected nights. The longer time base means better spectral resolution and with the
proper selection of nights, the time base still remains short enough not to obscure the possible short-term variabilities.

The first four nights (JD 2 454 014–2 454 019) were selected from October (subset 1). We got the longest time string during the eighth run (JD 2 454 068) so we used this run as a reference for November (subset 2). In December, we had the chance to observe KUV 02464+3239 in two consecutive weeks. In view of the results of individual nights’ Fourier analyses we selected two intervals: the first is the run on JD 2 454 081 (subset 3), the second consists of four nights (subset 4; JD 2 454 084–2 454 089, except the short run on JD 2 454 087). The latter runs have similar FTs but the run on JD 2 454 081 has a different FT.

Fig. 4 shows the FTs of our subsets. The variations in amplitudes of peaks in the FTs are obvious. Frequency values determined after pre-whitening are given in Table 2. S/N values of peaks were also calculated. Noise levels change from lower to higher frequencies between 2.6 and 2.5 mmag (subset 1), 3.3 and 1.9 mmag (subset 2), 2.7 and 2.5 mmag (subset 3), and 1.7 and 1 mmag (subset 4). Standard deviations of frequency values are determined by Monte Carlo (MC) simulations, getting solutions for each frequency in each subset. We generated synthetic light curves (by adding Gaussian random noise) using the frequencies listed in Table 2. After the non-linear least-squares fitting of 100 synthetic data sets of each subset we determined the standard deviations of the frequencies.

3.2.1 Frequency determination test

To support our final frequency determination we performed a robustness test. Synthetic light curves were generated using frequencies, amplitudes and phases of the light curve solutions with Gaussian random noise added. The applied noise levels were scaled from one to four times the residual scatters (σ) of the light curve solutions. Independent frequency analyses were carried out for each data set (1) to check how accurately we can get back the input frequencies from the noisy data sets and (2) whether we can identify the same frequencies that were found to be significant in the original data sets.

Testing our first subset we faced a ±1–2 c d⁻¹ alias problem as we raised the noise level, especially in the case of frequencies with lower amplitudes. Frequencies were found rather far from the input values. At the 4σ level we could identify two frequencies (99.25 and 103.79 c d⁻¹) out of the four found to be significant earlier. In the case of our second and third subsets, the amplitudes were rather high and we found all four of the frequencies identified before. Adding noise to the fourth subset caused alias problems from the 2.5σ level upward and the lowest amplitude peaks disappeared. We could find only four frequencies (86.99, 90.10, 98.79 and 104.03 c d⁻¹) within the most noisy time string.

Table 3 shows the results of our robustness test with the finally accepted frequencies. Peaks at ∼104 and 99 c d⁻¹ were found in all subsets. Other four frequencies (at ∼69, 87, 111 and 139 c d⁻¹) were rather high amplitude peaks in one or two segments. These six frequencies were determined unambiguously by the analyses of subsets and perhaps characterize the pulsation of KUV 02464+3239 within some amplitude limit.

As can be seen in Fig. 4 and in Table 3, remarkable amplitude variations occur from one subset to another. A signal at ∼87 c d⁻¹ became dominant in December while the amplitude of the peak at 104 c d⁻¹ decreased by 66 per cent. The peak at 99 c d⁻¹

| Frequency Period Ampl. S/N |
|-----------------------------|
| (c d⁻¹) | (s) | (mmag) |   |
|--------------------------------|
| Subset 1 | 90.660±0.004 | 953.01 | 12.8 | 4.9 |
| 99.251±0.003 | 870.52 | 17.4 | 6.6 |
| 103.790±0.002 | 832.45 | 30.6 | 11.9 |
| 114.103±0.004 | 757.21 | 10.0 | 4.0 |
| Subset 2 | 99.567±0.028 | 867.76 | 23.6 | 7.1 |
| 104.880±0.036 | 823.80 | 20.2 | 6.5 |
| 111.452±0.045 | 775.22 | 15.1 | 5.6 |
| 139.227±0.063 | 620.57 | 11.6 | 6.0 |
| Subset 3 | 69.475±0.047 | 1243.61 | 14.7 | 5.4 |
| 87.264±0.044 | 990.09 | 16.3 | 6.0 |
| 98.025±0.053 | 881.41 | 16.1 | 6.0 |
| 104.358±0.047 | 827.92 | 18.0 | 7.3 |
| Subset 4 | 86.579±0.004 | 997.93 | 9.5 | 5.5 |
| 86.996±0.002 | 993.15 | 18.4 | 10.6 |
| 89.142±0.003 | 969.24 | 10.7 | 6.2 |
| 90.100±0.001 | 958.94 | 15.2 | 8.8 |
| 98.797±0.002 | 874.52 | 9.1 | 5.5 |
| 104.036±0.002 | 830.48 | 10.2 | 6.5 |
| 139.954±0.005 | 617.35 | 3.8 | 4.7 |
| 173.960±0.004 | 496.66 | 4.7 | 4.3 |

1 Closely spaced frequencies to the dominant peak. Signals at 89.14 and 90.10 c d⁻¹ are close to the 1 c d⁻¹ aliases of each others. The peak at 90.1 c d⁻¹ has an unreliable high amplitude solution only when we fit at least the first six frequencies of this subset.
Table 3. Frequency and amplitude values of the six accepted pulsation frequencies for each subset. Amplitudes were determined by fitting these frequency components only. Subset No. refers to subsets of Section 3.2

| Subset No. | Frequency (c d\(^{-1}\)) | Amplitude (mmag) |
|------------|--------------------------|-----------------|
| 1          | 99.25 103.79             | 17.28 29.56     |
| 2          | 99.57 104.88             | 23.61 20.24     |
| 3          | 69.48 87.26 98.02 104.36 | 14.74 16.25 16.07 17.96 |
| 4          | 86.99 98.80 104.04       | 20.83 8.83 10.14 |

Figure 5. Frequencies out of the six accepted ones found at least in two subsets. The plotted error bars correspond to the frequency range within which the peaks were found during our robustness test (see Section 3.2.1 for details).

first increased its amplitude by 37 per cent, and then decreased by 63 per cent.

We represent the frequencies which were found at least in two subsets together in Fig. 5. The groups of frequencies are well separated, and there is no problem with overlapping sidelobes. The error bars give the uncertainty of our findings on a certain value in a subset. Since they overlap, it is clear that the two peaks around 87 c d\(^{-1}\) can have different values because of the uncertainties. The error bars also overlap in the case of peaks at \(\sim 104\) c d\(^{-1}\). The four peaks around 99 c d\(^{-1}\) represent an interesting case. Since the three well-determined peaks are more widely separated than the error bars, we can say that they are distinct. The reasons could be a frequency change on a short time-scale (from one subset to the other – within one month). Another explanation is that they are independent modes that are always excited and their amplitudes change from subset to subset. Alternatively, they might be components of an unresolved rotationally split mode. A comparative analysis on a longer time base could clear up the real situation (if it is a regular behaviour).

At this early stage of the interpretation of KUV 02464+3239, we mention this behaviour but we give a general solution based on the whole data set.

3.3 Analysis of the whole data set

The long time base of the whole data set gives more precise frequency values if we assume the frequencies are stable over the time base. In this case, the short-term variations in amplitudes are obscured but the frequencies are well determined.

The successive pre-whitening steps of the whole data set can be seen in the panels of Fig. 6. Table 4 shows the values of frequencies determined from the whole data set. Standard deviations are calculated by MC simulations. Peaks at \(f_1 \rightarrow f_6\) are marked in the first and second panels of Fig. 6 (upper segment of Table 4). They represent the six frequencies that come out of the final analysis. The residual spectrum in the third panel is definitely not white noise. With further analysis, we found seven other frequencies \((f_7 \rightarrow f_{13})\) in the residual spectrum and present them in the lower segment of Table 4. The last panel of Fig. 6 shows the FT after pre-whitening with 13 frequencies.

Table 4. Frequency, period and amplitude values of 13 frequencies derived by the whole data set. Frequencies at \(f_1 \rightarrow f_6\) are accepted as normal modes by the analyses and test of subsets. Frequency and amplitude values of \(f_1 \rightarrow f_6\) were determined by fitting with these components only. Frequencies and amplitudes of \(f_7 \rightarrow f_{13}\) were calculated by fitting with all the 13 frequencies.

| Frequency (cd\(^{-1}\)) | Amplitude (mmag) |
|--------------------------|-----------------|
| \(f_1\) 69.1060 ± 0.0003 | 799.838 1250.253 4.4 (4.4) |
| \(f_2\) 86.9879 ± 0.0001 | 1006.804 993.242 13.2 (14.4) |
| \(f_3\) 99.7516 ± 0.0001 | 1154.532 866.151 9.5 (11.5) |
| \(f_4\) 104.2617 ± 0.0001 | 1206.733 828.684 11.6 (11.4) |
| \(f_5\) 111.1095 ± 0.0002 | 1285.989 777.611 5.5 (8.0) |
| \(f_6\) 139.5157 ± 0.0003 | 1614.765 619.285 4.0 (3.9) |
| \(f_7\) 88.1611 | 1020.383 980.024 8.4 |
| \(f_8\) 89.7100 | 1038.311 963.103 7.3 |
| \(f_9\) 98.8533 | 1144.136 874.024 6.5 |
| \(f_{10}\) 104.3915 | 1208.235 827.654 10.2 |
| \(f_{11}\) 111.0865 | 1285.724 777.772 5.8 |
| \(f_{12}\) 139.0162 | 1608.983 621.510 3.7 |
| \(f_{13}\) 173.9642 | 2013.474 496.654 3.2 |
Amongst $f_7$, $f_8$ and $f_9$, additional pulsation modes could be present, but we cannot say which ones are real modes. $f_2$ is near to the $+1$ c d$^{-1}$ alias of the $f_2$ peak obtained in subset 3. There is no sign of $f_8$ in any subsets. $f_9$ can be a remainder of the group of four peaks near $f_1$ obtained by the subsets. The two higher frequencies in Table 3 (99.25 and 99.57 c d$^{-1}$) appear as $f_9$ and the two lower frequencies (98.02 and 98.80 c d$^{-1}$) can produce $f_9$ in the whole data set. The double structure around 139 c d$^{-1}$ might be a sign of rotational splitting: $\delta f = 0.5$ c d$^{-1} = 5.79$ µHz. Assuming that these peaks belong to high-overtone ($k \gg 1$) $l = 1$, $m = -1$, 0 or $m = 0$, 1 modes the rotation period of the star would be $\sim 1$ d. Considering the peaks at 104 c d$^{-1}$, their frequency separation is only $\delta f = 0.13$ c d$^{-1} = 1.5$ µHz which corresponds to a $\sim 3.8$ d rotation period under the assumptions above. However, regarding the large amplitude of the closely spaced peak, $f_{10}$ could also be an independently excited mode with another $l$ value. Determination of the frequency at 111.09 c d$^{-1}$ ($f_{11}$) was ambiguous because of aliasing. The peak at 173.96 c d$^{-1}$ is consistent with being the first harmonic of the dominant mode.

For asteroseismological investigations, we use only the six-frequency solution supported by the analyses of subsets. We consider these frequencies as a set of normal modes. A data set with better coverage and higher S/N would enable us to determine additional real pulsation modes.

4 TESTS ON AMPLITUDE VARIATIONS

The Fourier analysis method presumes stationary amplitude and frequency values while the behaviour of KUV 02464+3239 seems to be different. We do not know why the observed amplitudes of the star vary so much. To provide constraints for possible explanations, we performed tests for the amplitude variability.

We generated synthetic light curves corresponding to the whole data set using the frequency, amplitude and phase values of either the six accepted frequencies or with the additional closely spaced frequencies around the 87 c d$^{-1}$ dominant mode. In every case, we analysed the four subsets by non-linear least-squares fitting using the original frequency values as initial parameters. As our first test (a) we generated a synthetic light curve using only six frequencies, and we did not add noise to the data set. The analyses of subsets did not show noticeable amplitude variations from one subset to another. This result shows that beating of the six modes cannot explain the apparent amplitude variations.

In our second test (b) we added Gaussian random noise to the synthetic light curve using the residual scatter of the whole light curve’s 13-frequency solution. Our analysis showed that noise had a slight influence on the amplitudes (mainly for the lower amplitude modes) and cannot be responsible for the large observed variability. In our subsequent tests (c–h) we generated the synthetic light curves using 6+2 frequencies where the two additional frequencies were close to the dominant mode ($\delta f = \pm 0.185$ c d$^{-1} = 2.14$ µHz). This separation was selected to be close to the resolution limit of the smallest subset (subset 4), and this could be a reasonable value for rotational splitting. We set the amplitudes of the triplet’s side components to be the half (c–e) and one-tenth (f–h) of the 87 c d$^{-1}$ mode’s amplitude. The phase differences were $\pm 22.5°$, $\pm 45°$, $\pm 90°$ and $\pm 120°$ with respect to the central peak’s phase at the initial epoch (JD 2454014). With these tests we simulated the effects on amplitudes of closely spaced frequencies which might remain unresolved in the subsets. Such peaks could be detected by the analysis of the whole light curve if they had large enough amplitudes so as not to vanish in the other peaks and the noise.

Table 5 summarizes the test results on the amplitude variations of the dominant peak. In some cases we got large amplitude variations: disappearance and almost-disappearance of the peak in subset 3 (tests c and d). In test c we fitted a peak at 86.3 c d$^{-1}$ (the input value was 86.99 c d$^{-1}$) with 1.5 mmag amplitude. This means an amplitude decrease by 87 per cent if we accept the 86.3 c d$^{-1}$ peak as the representative of the original one. In test d we got a 64 per cent decrease in amplitude. Triplet side components with smaller amplitudes caused smaller, but noticeable variations. The maximum was a 28 per cent decrease in the amplitude of the dominant peak (test g).

Amplitude variations were detected for other modes as well. The presence of noise and beating with triplet components can be the explanation since we generated the synthetic light curves using constant amplitude values. The average of the variations of the five modes is 15 per cent. We conclude that the observed large amplitude variability can be simulated with a triplet assuming certain phase relations and relatively high amplitudes for the side components. However, these special phase relations and high amplitudes of side lobes to the main peak are rather improbable. A real amplitude variation seems to be plausible.

5 ASTEROSEISMOLOGY OF KUV 02464+3239

Our main goal in asteroseismology is to find stellar models that match the observed properties of the star with the highest precision. The most important observed values are the periods of light curves. At first, we are looking for models which produce pulsation periods with the lowest differences to the observed ones. We used the White Dwarf Evolution Code (WDEC) originally written by Martin Schwarzschild and modified by Kutter & Savedoff (1969), Lamb & van Horn (1975), Winget (1981), Kawaler (1986), Wood (1990), Bradley (1993), Montgomery (1998) and Bischoff-Kim, Montgomery & Winget (2008a) to generate equilibrium white dwarf models each with a given set of input parameters. For each model, we computed a set of periods based on the adiabatic equations of non-radial stellar oscillations (Unno et al. 1989). We computed grids of such models, varying the input parameters.

In WDEC, we start with a hot (~100,000 K) polytropic model. The code evolves it down to the requested temperature and the model we finally get is thermally relaxed solution to the stellar structure equations. To get pulsation periods of a model we used the integrated form of the WDEC given by Metcalfe (2001), which includes a pulsation code.

We used the equation-of-state (EOS) tables of Lamb (1974) in the core and the EOS tables of Saumon, Chabrier & van Horn (1995) in

| Subset | a | b | c | Test cases | d | e | f | g | h |
|--------|---|---|---|-----------|---|---|---|---|---|
| 1      | 0 | +4| +28| +9        | −12| −3| +10| −3|
| 2      | 0 | −6| +60| +37       | −32| +11| +1 | −9|
| 3      | 0 | +15| −87| −64       | −17| −7 | −28| +6|
| 4      | 0 | −5| +22| +11       | −35| +7 | +14| −4|

Table 5. Results of tests on amplitude variability of the 87 c d$^{-1}$ mode. At test cases a–h we give relative amplitude differences with respect to the synthetic light curves’ input value. See details in Section 4.
the envelope of the star. We used OPAL opacities updated by Iglesias 
& Rogers (1996). The convection was treated within the mixing 
length theory (MLT) according to Böhm & Cassinelli (1971) and 
with the $\alpha = 0.6$ parametrization suggested by model atmosphere 
calculations of Bergeron et al. (1995b). Precise value of $\alpha$ has 
very little effect on the pulsation periods of models (Bischoff-Kim, 
Montgomery & Winget 2008b). Treatment of the hydrogen/helium 
transition zone was done by equilibrium diffusion calculations contrary 
to the treatment of the helium/carbon transition layer which was 
parametrized.

5.1 The model grid

As we discussed in Section 3.3, we used the six-frequency light 
curve solution for the seismological analysis of KUV 02464+3239. 
Table 4 shows that we found modes only in the long-period regime 
(between 619 s and 1250 s). Bischoff-Kim et al. (2008b) show that 
low-order modes are especially sensitive to the mass of the hydrogen 
layer.

The best-fitting models have to fulfil two criteria: (1) to give back 
the period values closest to our observed values and (2) to provide 
physically acceptable solutions for effective temperature and log $g$.

Finding solutions according to the first criterion we used the FITTER 
tool developed by Kim (2007). The program calculates the rms values using the following equation:

$$\sigma_{\text{rms}} = \sqrt{\frac{\sum_{i=1}^{N} (p_i^{\text{calc}} - p_i^{\text{obs}})^2}{N}},$$

where $N$ denotes the number of observed periods.

We built our model grid varying five input parameters of the WDEC: $T_{\text{eff}}$, $M_*$, $M_{\text{H}}, X_0$ (central oxygen abundance) and $X_{\text{fm}}$ (the fractional mass point where the oxygen abundance starts dropping). For our first scan we fixed the mass of the helium layer at $M_{\text{He}} = 10^{-2} M_\odot$. We built our grid and searched for acceptable solutions in the parameter space determined by spectroscopic results on the star. Fontaine et al. (2001) derived $T_{\text{eff}}=11\,290$ K and log $g=8.08$ values for KUV 02464+3239 with the estimated flux calibration uncertainties of $\pm 200$ K and $0.05$ dex in log $g$ (Fontaine et al. 2003). However, this uncertainty estimate does not include contributions from different spectra, modelling uncertainties and different fitting procedures. We make some allowance for this by covering a range of $\pm 500$ K in $T_{\text{eff}}$ and $\pm 0.1$ dex in log $g$. According to this effective temperature value, our grid covers the range 10 800–11 800 K ($\sim 11\,290$ K $\pm 2.5\sigma$). Estimating the mass range we have to cover, we used the seismological masses determined for DAs by Bradley (1996). According to his results, the mass of a DA white dwarf with log $g = 8.08$ is about 0.65 $M_\odot$. Our grid covers the $M_*$ = 0.525–0.74 $M_\odot$ mass range (log $g = \sim 7.9$–8.2) which means that we investigated model solutions at log $g = 8.08 \pm 2\sigma$. We varied the mass of the hydrogen layer between $10^{-4}$ and $10^{-8} M_\odot$. The core parameters were changed between $X_\text{c} = 0.5$–0.9 and $X_{\text{fm}} = 0.1$–0.5, taking into account the carbon–oxygen profiles described by Salaris et al. (1997). Step sizes were 200 K ($T_{\text{eff}}$), 0.005 $M_\odot(M_*)$, $10^{-0.2} M_*(M_{\text{H}})$ and 0.1 ($X_0$ and $X_{\text{fm}}$).

5.2 Best-fitting models

While running the WDEC we allowed the modes to be $l = 1$ or 2. Since there are no previous asteroseismological analyses on this star or other constraints on the $l$ values of modes, we let all six modes be $l = 1$ or 2 for the fitting procedure. The variations in pulsation amplitudes rule out a meaningful application of different weights on the amplitudes (Castanheira & Kepler 2008).

Assuming better visibility of $l = 1$ modes over $l = 2$ modes (see e.g. Castanheira & Kepler 2008 and references therein), we prefer models that gave at least three $l = 1$ solutions with low $\sigma_{\text{rms}}$ values. We summarize the parameters of the best-fitting models in Table 6. It shows the model parameters, calculated pulsation periods with their $l$ and $k$ values and the corresponding $\sigma_{\text{rms}}$ value. We find that the mode identifications of the best-fitting models are typically quite different from model to model. This is due to the fact that over the span of 400 K, the periods of the relatively high overtone modes observed can change by about 40 s. As a result, the cooling of models for a given structure causes different $l = 1$ or 2 modes to fit a given observed period best. Note that since our current models use about 400 zones, the uncertainty of the model periods is $\sim 1$ s (Brassard & Fontaine 2005); therefore, differences in periods below 1 s are within the ‘noise’ of our modelling accuracy. The presence of shorter period modes could give stronger constraints on the stellar structure, resulting in fewer solutions with low $\sigma_{\text{rms}}$. However, within the $\sim 1$ s uncertainty of our modelling we can map the possible groups of models in the parameter space determined by spectroscopy.

5.2.1 Results for the main stellar parameters

Models with stellar masses within the $1\sigma$ log $g$ range are typeset in boldface in Table 6. We found six models out of the 13 that fulfil this criterion. The best fit over all with $\sigma_{\text{rms}} = 0.93$ has $M_*=0.65 M_\odot$ which corresponds with the expected mass from the spectroscopic log $g$ value. Fig. 7 shows the 13 selected models in the $T_{\text{eff}}$–$\log g$ plane. Closed and open circles denote the models within and out of the $1\sigma$ log $g$ range, respectively. The spectroscopic solution with the corresponding uncertainties determined by Fontaine et al. (2001, 2003) is also given in Fig. 7.

Assuming that the largest amplitude modes at 829, 866 and 993 s are $l = 1$, we favour the models which give this solution. Within the $1\sigma$ log $g$ range we find the 0.645, 0.650 and 0.680 $M_\odot$ models in accordance with this criterion. Taking into account that $T_{\text{eff}} = 11\,290 \pm 200$ K is expected also by spectroscopy, the 11 800 K solutions are over the $1\sigma$ limit and seem to be too hot. This means that the 0.645 $M_\odot$ model would be our best choice.

Table 6 shows the hydrogen layer masses of our models are between $10^{-4}$ and $4 \times 10^{-8} M_\odot$. Restricting ourselves to the six models selected by log $g$, we find that five of them have $M_{\text{H}} = 10^{-4}$–$6 \times 10^{-6} M_\odot$. We can give additional constraints on the hydrogen layer mass if we take into account only the three ‘favoured’ models between 0.645 and 0.680 $M_\odot$. In this case $M_{\text{H}} = 2.5 \times 10^{-5}$–$6.3 \times 10^{-6} M_\odot$.

5.2.2 Mode identification

According to our selection criterion, the models have mostly $l = 1$ solutions for the pulsation modes. Models with solely $l = 1$ modes exist only out of the $1\sigma$ log $g$ range ($M_* = 0.725$ and $0.74 M_\odot$).

Considering the full range of best-fitting models, we cannot uniquely assign an $l$ value to any mode. At least one model has an $l = 2$ mode solution for each period. We cannot provide unique assignments for the overtone numbers either; however, the range of stellar and hydrogen layer masses of our models constrains the $k$ values.

© 2009 The Authors. Journal compilation © 2009 RAS, MNRAS 399, 1954–1963

Downloaded from https://academic.oup.com/mnras/article-abstract/399/4/1954/1034273 on 30 July 2018
Table 6. Best-fitting solutions for KUV 02464+3239 in the mass range 0.525–0.74 $M_{\odot}$. We represent the results of former spectroscopic observations ($T_{\text{eff}}, \log g$; Fontaine et al. 2001), the expected seismological mass derived by Bradley (1996) and the observed pulsation periods as reference values. Models that have masses within 1σ in the log $g$ range are typeset in boldface.

| $M_*/M_{\odot}$, (log $g$) | $T_{\text{eff}}$ (K) | $-\log M_H$ | $X_0$ | $X_{\text{eff}}$ | Model periods in seconds ($l$, $k$) | $\sigma_{\text{rms}}$ (s) |
|-----------------------------|------------------|-------------|------|--------------|-----------------|------------------|
| 0.525, (7.85)               | 11400            | 6.9         | 0.7  | 0.5          | 620.4 (1.8), 777.1 (1.1), 830.3 (1.1), 865.4 (2.2), 992.3 (1.1), 1250.7 (1.2) | 0.95 |
| 0.525, (7.85)               | 11600            | 7.2         | 0.5  | 0.4          | 620.3 (2.1), 776.3 (1.1), 830.7 (1.2), 866.0 (2.2), 992.6 (1.1), 1251.0 (1.2) | 1.12 |
| 0.575, (7.97)               | 11000            | 6.2         | 0.7  | 0.5          | 619.8 (2.1), 777.4 (1.2), 831.0 (1.3), 868.7 (2.3), 994.0 (1.6), 1250.5 (1.4) | 1.45 |
| 0.585, (7.99)               | 11000            | 6.4         | 0.5  | 0.4          | 617.9 (2.1), 775.4 (1.2), 827.1 (1.3), 866.9 (2.3), 991.6 (1.6), 1250.5 (1.4) | 1.44 |
| 0.615, (8.03)               | 11800            | 4.0         | 0.7  | 0.3          | 616.4 (1.1), 777.4 (1.2), 828.8 (2.3), 865.6 (1.2), 991.1 (1.2), 1249.7 (2.4) | 1.51 |
| 0.625, (8.04)               | 11000            | 7.4         | 0.5  | 0.2          | 620.6 (1.9), 780.0 (1.2), 827.4 (2.3), 866.8 (1.4), 994.1 (2.2), 1252.1 (2.8) | 1.50 |
| 0.645, (8.07)               | 11400            | 5.2         | 0.9  | 0.2          | 618.1 (2.2), 779.7 (1.5), 828.2 (1.5), 865.7 (1.4), 991.9 (1.2), 1251.8 (2.4) | 1.33 |
| 0.650, (8.08)               | 11800            | 4.6         | 0.6  | 0.1          | 620.3 (1.2), 776.6 (2.3), 827.1 (1.7), 866.2 (1.2), 992.8 (1.1), 1249.6 (2.8) | 0.93 |
| 0.680, (8.13)               | 11800            | 5.0         | 0.5  | 0.1          | 618.8 (1.2), 778.1 (2.2), 826.6 (1.7), 865.2 (1.2), 992.1 (1.1), 1251.9 (2.8) | 1.26 |
| 0.685, (8.14)               | 11400            | 4.8         | 0.6  | 0.4          | 618.7 (1.2), 778.6 (1.6), 826.4 (1.7), 866.4 (2.3), 994.1 (2.3), 1249.9 (2.7) | 1.12 |
| 0.725, (8.2)                | 11800            | 5.8         | 0.7  | 0.4          | 620.4 (1.2), 778.5 (1.6), 828.4 (1.7), 865.6 (1.2), 995.3 (1.2), 1249.5 (1.2) | 1.11 |
| 0.725, (8.2)                | 11200            | 5.4         | 0.8  | 0.4          | 616.9 (1.2), 778.5 (1.6), 828.9 (1.7), 865.2 (1.2), 992.7 (2.3), 1251.6 (2.7) | 1.26 |
| 0.740, (8.23)               | 11800            | 6.0         | 0.6  | 0.4          | 620.0 (1.2), 778.9 (1.6), 828.1 (1.7), 867.0 (1.2), 991.3 (1.2), 1250.7 (1.2) | 1.09 |

Reference values:

| 0.65, (8.08)               | 11290            | 619.3       | 777.6 | 828.7 | 866.2 | 993.2 | 1250.3 |

Figure 7. The 13 models of Table 6 in the $T_{\text{eff}}$–$M_*$ plane. Closed and open circles denote the models within and out of the 1σ log $g$ range determined by spectroscopy. The black square denotes the spectroscopic solution with its uncertainties given by Fontaine et al. (2001, 2003). The grid with dashed lines corresponds to the step sizes of our model grid.

In summary, we can say that the observed pattern of modes can be described with high accuracy assuming mostly $l = 1$ modes. Considering the three ‘favoured’ models the modes at 619 and 778 s are always different $l$ values. The 1250 s mode is always $l = 2$ for both these models.

5.2.3 Varying the He layer mass

In our second scan, we varied the mass of the He layer in the grid from $10^{-2}$ to $10^{-4} M_*$ in three steps. This way we could check the sensitivity of our solutions to the thickness of the He layer. In this case we ran a more sophisticated version of the WDEC with core composition profiles based on stellar evolution calculations done by Salaris et al. (1997). This grid covers the temperature and hydrogen layer mass range we used previously ($T_{\text{eff}}$ = 10 800–11 800 K and $M_H = 4 \times 10^{-8} M_*$). We varied the stellar mass between 0.60 and 0.69 $M_\odot$. Step sizes were as well 200 K ($T_{\text{eff}}$), 0.005 $M_\odot (M_*)$ and $10^{-0.2} M_{\odot} (M_*)$.

According to our first criterion we searched for models with at least three $l = 1$ solutions and low $\sigma_{\text{rms}}$ values. We found two acceptable models at 0.61 and 0.635 $M_\odot$. Both models have the same helium layer masses ($10^{-3} M_*$). However, none of them has all of the large amplitude modes as $l = 1$. The mode at 993 s is always $l = 2$, which would imply a much larger physical amplitude for this...
mode since it has the largest light amplitude. These two models have hydrogen layers with masses of $2.5 \times 10^{-6}$ and $10^{-6} M_\odot$. These values are at the thin side of the range given by the previously selected models. Although we cannot rule out helium layer masses thinner than $10^{-3} M_\odot$, our favouring the three largest amplitude modes being $l = 1$ implies that $M_{He} = 10^{-2} M_\odot$ is the preferred value.

5.2.4 Seismological parallax

According to the luminosity of a selected model we can give an estimation on the distance and parallax of the star. Unfortunately, there is no trigonometric parallax measurement for KUV 02464+3239. However, we can still predict what the parallax should be.

The first step is to derive the bolometric magnitude ($M_{bol}$) of the star:

$$M_{bol} = M_{bol}^\odot - 2.5 \log \left( \frac{L}{L^\odot} \right),$$

where $M_{bol}^\odot = +4.75$ (Allen 1973) and $L^\odot = 3.854 \times 10^{33}$ erg s$^{-1}$ (Sackmann, Boothroyd & Craemer 1993). $M_{bol}$ can be related to the absolute visual magnitude using the bolometric correction: $M_v = M_{bol} - BC$. Bergeron, Wesemael & Beauchamp (1995a) performed colour-index and magnitude calculations using DA and DB model grids. According to table 1 in Bergeron et al. (1995a) BC = −0.441 and −0.611 at temperatures 11 000 and 12 000 K, respectively. In view of the apparent visual magnitude $m_v = 16.07$ and using the distance modulus formula we can derive the distance and the parallax of KUV 02464+3239.

The six models selected by log $g$ have log $L/L^\odot = -2.56$ to −2.71 where the most and least luminous models are at 0.615 and 0.625 $M_\odot$, respectively. In these cases, the calculated seismological parallax values are between 13.5 and 15.4 mas (milliarcsecond) with a 14.6 mas average. Restricting ourselves to the three ‘favoured’ models with log $L/L^\odot = -2.6$ to −2.66, the parallax angles are 14.8, 14.2 and 14.7 mas for the 0.645, 0.650 and 0.680 $M_\odot$ models, respectively. These results imply a distance of ~70 pc for KUV 02464+3239.

5.3 Mode trapping

KUV 02464+3239 was mentioned by Fontaine et al. (2001) to be a photometric twin of another cool DAV, GD 154. In spite of the similarities between the shape of their light curves we find significant differences if we compare their pulsational properties. The Fourier spectrum of GD 154 is dominated by three normal modes and their harmonics (Pfeiffer et al. 1996). Subharmonics of the 1186 s mode were also detected by Robinson et al. (1978). In the case of KUV 02464+3239 even with single-site observations we could determine six modes and using the whole light curve, only the first harmonic of the dominant mode was found. Clear presence of further harmonics and subharmonics can be seen only by some parts of the light curve (Bognár et al. 2007).

The small number of GD 154’s eigenmodes compared to other cool DAVs implies a very efficient mode selection mechanism – possibly trapping of the modes by a very thin ($M_H \sim 10^{-10} M_\odot$) hydrogen layer (Pfeiffer et al. 1996). We can use our models on KUV 02464+3239 to test whether some of the modes are trapped.

One possible way to find trapped modes is to construct period spacing diagrams and search for minima. Mode trapping causes departures from the uniform period spacings of consecutive $k$ modes. Trapped modes have lower kinetic energies and, as Bradley & Winget (1991) showed, minima in period spacing diagrams correspond to minima in kinetic energies. Accordingly, we made a simple statistical fit on the six models selected by log $g$. We collected how often we find a period near or at a minimum of a model’s corresponding period spacing diagram. We found that the largest amplitude modes (at 829, 866 and 993 s) frequently occur near or at period spacing minima and in these cases the $l = 1$ solution is preferred. The 1250 s mode has not been found at a minimum in any of the cases. Fig. 8 shows the period spacing diagrams of the six selected models. Filled and open circles denote the model periods with $l = 1$ or $l = 2$ solutions, respectively. Vertical dashed lines are drawn corresponding to the observed period values. Model periods found to be the closest of the observed ones are denoted with open squares.

6 SUMMARY AND CONCLUSIONS

We have presented the analyses of our observations on the DA variable KUV 02464+3239.

Using the analyses of data subsets we accepted six frequencies as normal modes of pulsation. With the analysis of the whole data set we determined seven additional frequencies as possible modes. Since remarkable amplitude variations (up to 30–60 per cent) occurred on a time-scale of weeks, we performed tests for the possible sources of the amplitude variability. Neither beating of the six modes nor the effect of noise resulted in large enough variations. The test cases of closely spaced modes or rotational triplets revealed large amplitude variability, but only in unrealistic amplitude and phase relations. A real amplitude variation seems to be plausible.
The best asteroseismological models have $M_\ast = 0.645, 0.650 \text{ and } 0.680 \, M_\odot$ and the mass of their hydrogen layer is between $2.5 \times 10^{-5}$ and $6.3 \times 10^{-6} \, M_\ast$. Although we cannot exclude thinner helium layers, $M_{\text{He}} = 10^{-2} \, M_\ast$ models reproduce the observed properties of the star better. Asteroseismological parallax values calculated by the luminosity of the three models are between 14.2 and 14.8 mas. Using period spacing diagrams we conclude that mode trapping can explain the high amplitude modes, but is not required.

The best way to discriminate between models would be to obtain observational constraints on the $\ell$ values of at least the large amplitude modes. It may be possible by time-dependent UV spectra or chromatic amplitudes, but due to the faintness of the star and its complicated pulsation spectra this would be a challenging task. Our results show the effectiveness of long, single-site observations. Multisite campaign(s) on KUV 02464+3239 would enable us to find additional pulsation modes and possibly signs of rotational splittings, and this would give further constraints on the stellar structure.

Resolving the closely spaced modes expected in the case of KUV 02464+3239 we could exclude the beating of modes as a cause of the observed amplitude variability. Our tests on amplitudes indicate this possibility. This would mean that we see real energy content variations of the individual modes. In this case, the observed variability is presumably due to non-linear processes like mode coupling and/or interaction between pulsation and convection. Finding the real physical explanation of amplitude variations is a key issue not only in the case of KUV 02464+3239, but also for other long-period white dwarf pulsators.

ACKNOWLEDGMENTS

The authors would like to thank the referee, S. O. Kepler, for his helpful comments and suggestions. This research was partly supported by HSO project No. 98022.

REFERENCES

Allen C. W., 1973, Astrophysical Quantities. University of London, Athlone Press, London
Bergeron P., Wesemael F., Beauchamp A., 1995a, PASP, 107, 1047
Bergeron P., Wesemael F., Lamontagne R., Fontaine G., Saffer R. A., Allard N. F., 1995b, ApJ, 449, 258
Bischoff-Kim A., Montgomery M. H., Winget D. E., 2008a, ApJ, 675, 1512
Bischoff-Kim A., Montgomery M. H., Winget D. E., 2008b, ApJ, 675, 1505
Bognár Zs. et al., 2007, AN, 328, 845
Böhm K. H., Cassinelli J., 1971, A&A, 12, 21
Bradley P. A., 1993, PhD thesis, University of Texas at Austin
Bradley P. A., 1996, ApJ, 468, 350
Bradley P. A., Winget D. E., 1991, ApJS, 75, 463
Brassard P., Fontaine G., 2005, ApJ, 622, 572
Breger M. et al., 1993, A&A, 271, 482
Castanheira B. G., Kepler S. O., 2008, MNRAS, 385, 430
Csúry Z., Kolláth Z., 2004, in Danesy D., ed., Proc. SOHO 14/GONG 2004 Workshop, Helio- and Asteroseismology: Towards a Golden Future, ESA SP-559. ESA, Noordwijk, p. 396
Fontaine G., Bergeron P., Brassard P., Billères M., Charpinet S., 2001, ApJ, 557, 792
Fontaine G., Bergeron P., Billères M., Charpinet S., 2003, ApJ, 591, 1184
Handler G., 2003a, in Sterken C., ed., ASP Conf. Ser. Vol. 292, Interplay of Periodic, Cyclic and Stochastic Variability in Selected Areas of the HR Diagram. Astron. Soc. Pac., San Francisco, p. 247
Handler G., 2003b, Baltic Astron., 12, 11
Iglesias C. A., Rogers F. J., 1996, ApJ, 464, 943
Kawaler S. D., 1986, PhD thesis, University of Texas at Austin
Kepler S. O. et al., 2003, A&A, 401, 639
Kim A., 2007, PhD thesis, University of Texas at Austin
Kleinnan S. J. et al., 1998, ApJ, 495, 424
Kolláth Z., 1990, Occasional Technical Notes of Konkoly Observatory, No. 1, http://www.konkoly.hu/Mitteilungen/Mitteilungen.html#TechNotes
Kutter G. S., Savedoff M. P., 1969, ApJ, 156, 1021
Landolt A., 1968, ApJ, 153, 151
Lamb D. Q., 1974, PhD thesis, University of Rochester
Lamb D. Q., van Horn H. M., 1975, ApJ, 200, 306
Lenz P., Breger M., 2005, Communications in Asteroseismology, 146, 53
Metcalfe T. S., 2001, PhD thesis, University of Texas at Austin
Montgomery M. H., 1998, PhD thesis, University of Texas at Austin
Mukadam A., Kepler S. O., Winget D. E., 2001, in von Hippel T., Simpson C., Manset N., eds, ASP Conf. Ser. Vol. 245, Astrophysical Ages and Times Scales. Astron. Soc. Pac., San Francisco, p. 65
Nather R. E., Winget D. E., Clemens J. C., Hansen C. J., Hine B. P., 1990, ApJ, 361, 309
Pfeiffer B. et al., 1996, A&A, 314, 182
Provençal J. L. et al., 2009, ApJ, 693, 564
Robinson E. L., Stover R. J., Nather R. E., McGraw J. T., 1978, ApJ, 220, 614
Sackmann I.-J., Boothroyd A. I., Kraemer K. E., 1993, ApJ, 418, 457
Salaris M., Domínguez I., García-Berro E., Hernanz M., Isern J., Mochnovitch R., 1997, ApJ, 486, 413
Saumon D., Chabrier G., von Horn H. M., 1995, ApJS, 99, 713
Unno W., Osaki Y., Ando H., Shibahashi H., 1989, Nonradial Oscillations of Stars, 2nd edn. University of Tokyo Press, Tokyo
Winget D. E., 1981, PhD thesis, University of Rochester
Winget D. E., Kepler S. O., 2008, ARA&A, 46, 157
Wood M. A., 1990, PhD thesis, University of Texas at Austin

This paper has been typeset from a TeX file prepared by the author.