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Precision Measurement of CP Violation in $B_S^0 \rightarrow J/\psi K^+ K^-$ Decays

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The time-dependent CP asymmetry in $B_S^0 \rightarrow J/\psi K^+ K^-$ decays is measured using pp collision data, corresponding to an integrated luminosity of 3.0 fb$^{-1}$, collected with the LHCb detector at center-of-mass energies of 7 and 8 TeV. In a sample of 96 000 $B_S^0 \rightarrow J/\psi K^+ K^-$ decays, the CP-violating phase $\phi_s$ is measured, as well as the decay widths $\Gamma_S$ and $\Gamma_H$ of the light and heavy mass eigenstates of the $B_S^0$--$\bar{B}_S^0$ system. The values obtained are $\phi_s = -0.058 \pm 0.049 \pm 0.006$ rad, $\Gamma_S = (2.660 \pm 0.0027 \pm 0.0015) \text{ps}^{-1}$, and $\Delta \Gamma_S = \Gamma_S - \Gamma_H = 0.0805 \pm 0.0091 \pm 0.0032 \text{ps}^{-1}$, where the first uncertainty is statistical and the second, systematic. These are the most precise single measurements of those quantities to date. A combined analysis with $B_S^0 \rightarrow J/\psi \pi^+ \pi^-$ decays gives $\phi_s = -0.010 \pm 0.039$ rad. All measurements are in agreement with the standard model predictions. For the first time, the phase $\phi_s$ is measured independently for each polarization state of the $K^+ K^-$ system and shows no evidence for polarization dependence.

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The CP-violating phase $\phi_s$ arises in the interference between the amplitudes of $B_S^0$ mesons decaying via $b \rightarrow c \bar{c} s$ transitions to CP eigenstates directly and those decaying after oscillation. In the standard model (SM), ignoring subleading contributions, this phase is predicted to be $-2\beta_s$, where $\beta_s = \arg [-\langle V_{ts} V_{tb}^* \rangle / \langle V_{cs} V_{cb}^* \rangle]$ and $V_{ij}$ are elements of the quark-mixing matrix [1]. Global fits to experimental data give $-2\beta_s = -0.0363 \pm 0.0013$ rad [2]. This phase could be modified if non-SM particles were to contribute to the $B_S^0$--$\bar{B}_S^0$ oscillations [3,4] and a measurement of $\phi_s$ significantly different from the SM prediction would provide unambiguous evidence for processes beyond the SM.

The LHCb Collaboration has previously reported measurements of $\phi_s$ using $B_S^0 \rightarrow J/\psi K^+ K^-$ and $B_S^0 \rightarrow J/\psi \pi^+ \pi^-$ decays [5,6] and determined the sign of $\Delta \Gamma_S$ to be positive [7], which removes the twofold ambiguity in $\phi_s$. These measurements were based upon data, corresponding to an integrated luminosity of up to 1.0 fb$^{-1}$, collected in pp collisions at a center-of-mass energy of 7 TeV in 2011 at the LHC. The D0, CDF, ATLAS and CMS Collaborations have also measured $\phi_s$ in $B_S^0 \rightarrow J/\psi K^+ K^-$ decays [8–11]. This Letter extends the LHCb measurements in the $B_S^0 \rightarrow J/\psi K^+ K^-$ channel by adding data corresponding to 2.0 fb$^{-1}$ of integrated luminosity collected at 8 TeV in 2012 and presents the combined results for $\phi_s$, including the analysis of $B_S^0 \rightarrow J/\psi \pi^+ \pi^-$ decays from Ref. [12]. For the first time, the CP-violating phases are measured separately for each polarization state of the $K^+ K^-$ system. Knowledge of these parameters is an important step towards the control of loop-induced effects to the decay amplitude, which could potentially be confused with non-SM contributions to $B_S^0$--$\bar{B}_S^0$ mixing [13]. The analysis of the $B_S^0 \rightarrow J/\psi K^+ K^-$ channel reported here is as described in Ref. [6], to which the reader is referred for details, except for the changes described below.

The LHCb detector is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing $b$ or $c$ quarks and is described in Ref. [14]. The trigger [15] consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, in which all charged particles with transverse momentum greater than 500 (300) MeV/c are reconstructed for 2011 (2012) data. Further selection requirements are applied off-line, as described in Ref. [6], in order to increase the signal purity.

The $B_S^0 \rightarrow J/\psi K^+ K^-$ decay proceeds predominantly via $B_S^0 \rightarrow J/\psi \phi$, in which the $K^+ K^-$ pair from the $\phi(1020)$ meson is in a P-wave configuration. The final state is a superposition of CP-even and CP-odd states depending upon the relative orbital angular momentum of the $J/\psi$ and $\phi$ mesons. The $J/\psi K^+ K^-$ final state can also be produced with $K^+ K^-$ pairs in a CP-odd S-wave configuration [16]. The measurement of $\phi_s$ requires the CP-even and CP-odd components to be disentangled by analyzing the distribution of the reconstructed decay angles of the final-state particles. In this analysis, the decay angles are defined in the helicity basis, $\cos \theta_K$, $\cos \theta_\mu$, and $\varphi_\chi$, as described in Ref. [6].

The invariant mass distributions for $K^+ K^-$ and $J/\psi(\rightarrow \mu^+ \mu^-) K^+ K^-$ candidates are shown in Figs. 1(a) and 1(b), respectively. The combinatorial background is modeled with an exponential function and the $B_S^0$ signal shape is parameterized by a double-sided Hypatia function [17].

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FIG. 1 (color online). (a) Background-subtracted invariant mass distributions of the \(K^+K^-\) system in the selected \(B^0\) \(\rightarrow J/\psi K^+K^-\) candidates (black points). The vertical red lines denote the boundaries of the six bins used in the maximum likelihood fit. (b) Distribution of \(m(J/\psi K^+K^-)\) for the data sample (black points) and projection of the maximum likelihood fit (blue line). The \(B^0\) signal component is shown by the red dashed line and the combinatorial background by the green long-dashed line. Background from misidentified \(B^0\) and \(\Lambda^0\) decays is subtracted, as described in the text.

which gives a better description of the tails compared to the sum of two Gaussian distributions used in Ref. [6]. The fitted signal yield is \(95.690 \pm 350\). In addition to the combinatorial background, studies of the data in side-bands of the \(m(J/\psi K^+K^-)\) spectrum show contributions from approximately \(1700\) \(B^0\) \(\rightarrow J/\psi K^+\pi^-\) (\(4800\) \(\Lambda^0_s\) \(\rightarrow J/\psi pK^-\)) decays where the pion (proton) is misidentified as a kaon. These background events have complicated correlations between the angular variables and \(m(J/\psi K^+K^-)\). In order to avoid the need to describe explicitly such correlations in the analysis, the contributions from these backgrounds are statistically subtracted by adding to the data simulated events of these decays with negative weight. Prior to injection, the simulated events are weighted such that the distributions of the relevant variables used in the fit, and their correlations, match those of data.

The principal physics parameters of interest are \(\Gamma_s\), \(\Delta\Gamma_s\), \(\phi_s\), \(|\lambda|\), the \(B^0_s\) mass difference, \(\Delta m_s\), and the polarization amplitudes \(A_k = |A_k|e^{-i\delta_k}\) where the indices \(k \in \{0, \perp, \perp, S\}\) refer to the different polarization states of the \(K^+K^-\) system. The sum \(|A_0|^2 + |A_0|^2 + |A_\perp|^2\) equals unity and by convention \(\delta_0 = 0\). The parameter \(\lambda\) describes CP violation in the interference between mixing and decay and is defined by \(\eta_q(p/q)\langle A_k/A_k\rangle\), where it is assumed to be the same for all polarization states. The complex parameters \(p = \langle B^0_s|B_L^0\rangle\) and \(q = \langle B^0_s|B_{T}\rangle\) describe the relation between mass and flavor eigenstates and \(\eta_q\) is the CP eigenvalue of the polarization state \(k\). The CP-violating phase is defined by \(\phi_s \equiv -\arg \lambda\). In the absence of CP violation in decay, \(|\lambda| = 1\). CP violation in \(B^0_s\)-meson mixing is negligible, following measurements in Ref. [18]. Measurements of the above parameters are obtained from a weighted maximum likelihood fit [19] to the decay-time and angle distributions of the 7 and 8 TeV data, as described in Ref. [6].

The \(B^0_s\) decay-time distribution is distorted by the trigger selection requirements and by the track reconstruction algorithms. Corrections for both 7 and 8 TeV samples are determined from data using the methods described in Ref. [20] and are incorporated in the maximum likelihood fit by a parameterized function, in the case of the trigger, and by per-candidate weights, in the case of the track reconstruction. Both corrections are validated using a sample of \(10^8\) simulated \(B^0_s\) \(\rightarrow J/\psi\phi\) events.

To account for the experimental decay-time resolution, the signal probability density function (PDF) is defined per candidate and is convolved with the sum of two Gaussian functions with a common mean, \(\mu\), and independent widths. The widths are given by the per candidate decay-time uncertainty, estimated by the kinematic fit used to calculate the decay time, multiplied by separate scale factors. The scale factors are determined from the decay-time distribution of a control sample of prompt \(J/\psi K^+K^-\) candidates that are selected as for signal except for decay-time requirements. The average value of the \(\sigma\) distribution in the sample of prompt candidates is approximately 35 \(\text{fs}\) and the effective average resolution is 46 \(\text{fs}\).

The flavor of the \(B^0_s\) candidate at production is inferred using two independent classes of flavor tagging algorithms, the opposite-side (OS) tagger and the same-side kaon (SSK) tagger, which exploit specific features of the production of \(bb\) quark pairs in \(pp\) collisions. The OS tagger algorithm is described in Ref. [6] but is recalibrated using data sets of flavor-specific decays, yielding a tagging power of \((2.55 \pm 0.14)\%\). The SSK algorithm deduces the signal production flavor by exploiting charge-flavor correlations of the kaons produced during the hadronization process of the \(b\) quark forming the signal \(B^0_s\) meson. The tagging kaon is identified using a selection based on a neural network that gives an effective tagging power of \((1.26 \pm 0.17)\%\), corresponding approximately to a 40\% improvement in tagging power with respect to that in Refs. [6]. The SSK algorithm is calibrated using a sample of \(B^0_s \rightarrow D_s^-\pi^+\) decays [21]. For events that have both OS and SSK tagging decisions, corresponding to 26\% of the tagged sample, the effective tagging power is \((1.70 \pm 0.08)\%\). The combined tagging power of the three overlapping tagging categories defined above is \((3.73 \pm 0.15)\%\).

Due to different \(m(K^+K^-)\) line shapes of the \(S\) and \(P\)-wave contributions, their interferences are suppressed by an effective coupling factor after integrating over a finite \((m(K^+K^-))\) region. The fit is carried out in six bins of \(m(K^+K^-)\), as shown in Fig. 1(a), to allow measurement of the small \(S\)-wave amplitude in each bin and to minimize correction factors in the interference terms of the PDF.

The results of the fit are consistent with the measurements reported in Ref. [6] and are reported in Table I where the first uncertainty is statistical and the second, systematic. The correlation matrix is given in Ref. [22]. In contrast to Ref. [6], the value of \(\Delta m_s\) is unconstrained in this fit.
TABLE I. Values of the principal physics parameters determined from the polarization-independent fit.

| Parameter           | Value                                  |
|---------------------|----------------------------------------|
| $\Gamma_s$ (ps$^{-1}$) | $0.6603 \pm 0.0027 \pm 0.0015$          |
| $\Delta \Gamma_s$ (ps$^{-1}$) | $0.0805 \pm 0.0091 \pm 0.0032$          |
| $|A_{1\perp}|^2$        | $0.2504 \pm 0.0049 \pm 0.0036$          |
| $|A_0|^2$             | $0.5241 \pm 0.0034 \pm 0.0067$          |
| $\delta_\perp$ (rad) | $3.26^{+0.17}_{-0.10} \pm 0.06$         |
| $\delta_\parallel$ (rad) | $3.08^{+0.14}_{-0.15} \pm 0.06$         |
| $\phi_s$ (rad)       | $-0.058 \pm 0.049 \pm 0.006$            |
| $|\lambda|$           | $0.964 \pm 0.019 \pm 0.007$             |
| $\Delta m_s$ (ps$^{-1}$) | $17.711^{+0.055}_{-0.057} \pm 0.011$    |

thereby providing an independent measurement of this quantity, which is consistent with the results of Ref. [23]. The projections of the decay time and angular distributions are shown in Fig. 2.

The results reported in Table I are obtained with the assumption that $\phi_s$ and $|\lambda|$ are independent of the final-state polarization. This condition can be relaxed to allow the measurement of $\phi_s^\perp$ and $|\lambda^\perp|$ separately for each polarization, following the formalism in Ref. [24]. The results of this fit are shown in Table II, and the statistical correlation matrix is given in Ref. [22]. There is no evidence for a polarization-dependent $CP$ violation arising in $B_s^0 \to J/\psi K^+ K^-$ decays.

A summary of systematic uncertainties is reported in Tables III and IV in the Appendix. The tagging parameters are constrained in the fit and therefore their associated systematic uncertainties contribute to the statistical uncertainty of each parameter in Table I. This contribution is 0.004 rad to the statistical uncertainty on $\phi_s$, 0.004 ps$^{-1}$ to that of $\Delta m_s$, 0.01 rad to that of $\delta_\perp$, and is negligible for all other parameters.

The assumption that the $m(J/\psi K^+ K^-)$ distribution is independent from the decay time and angles is tested by reevaluating the signal weights in bins of the decay time and angles and repeating the fit. The difference in fit results is assigned as a systematic uncertainty. The systematic effect from the statistical uncertainty on the signal weights is determined by recomputing them after varying the parameters of the $m(J/\psi K^+ K^-)$ fit model within their statistical uncertainties and assigning the difference in fit results as a systematic uncertainty.

The effect due to the $b$-hadron background contributions is evaluated by varying the proportion of simulated background events included in the fit by one standard deviation of their measured fractions. In addition, a further systematic uncertainty is assigned as the difference between the results of the fit to weighted or nonweighted data.

A small fraction of $B_s^0 \to J/\psi K^+ K^-$ decays come from the decays of $B_s^\pm$ mesons [25]. The effect of ignoring this component in the fit is evaluated using simulated pseudoexperiments where a 0.8% contribution [25,26] of $B_s^0$-from-$B_s^\pm$ decays is added from a simulated sample of $B_s^\pm \to B_s^0 (\to J/\psi \phi) \pi^\mp$ decays. Neglecting the $B_s^\pm$ component leads to a bias on $\Gamma_s$ of 0.0005 ps$^{-1}$, which is added as a systematic uncertainty. Other parameters are unaffected.

The decay angle resolution is found to be of the order of 20 mrad in simulated events. The result of pseudoexperiments shows that ignoring this effect in the fit only leads to small biases in the polarization amplitudes, which are assigned as systematic uncertainties.

The angular efficiency correction is determined from simulated signal events weighted as in Ref. [6] such that the kinematic distributions of the final state particles match those in the data. A systematic uncertainty is assigned as the difference between the fit results using angular corrections from weighted or nonweighted simulated events. The limited size of the simulated sample leads to an additional systematic uncertainty.

The systematic uncertainty from the decay time resolution parameters is not included in the statistical

FIG. 2 (color online). Background subtracted decay-time and angle distributions for $B_s^0 \to J/\psi K^+ K^-$ decays (data points) with the one-dimensional fit projections overlaid. The solid blue line shows the total signal contribution, which is composed of $CP$-even (long-dashed red), $CP$-odd (short-dashed green), and $S$-wave (dotted-dashed purple) contributions.

TABLE II. Values of the polarization-dependent parameters $\phi_s^\perp$ and $|\lambda^\perp|$ determined from the polarization-dependent fit.

| Parameter           | Value                                  |
|---------------------|----------------------------------------|
| $|\lambda^0|$        | $1.012 \pm 0.058 \pm 0.013$            |
| $|\lambda^1/\lambda^0|$ | $1.02 \pm 0.12 \pm 0.05$             |
| $|\lambda^2/\lambda^0|$ | $0.97 \pm 0.16 \pm 0.01$             |
| $|\lambda^3/\lambda^0|$ | $0.86 \pm 0.12 \pm 0.04$             |
| $\phi_s^0$ (rad)     | $-0.045 \pm 0.053 \pm 0.007$          |
| $\phi_s^1 - \phi_s^0$ (rad) | $-0.018 \pm 0.043 \pm 0.009$          |
| $\phi_s^2 - \phi_s^0$ (rad) | $-0.014 \pm 0.035 \pm 0.006$          |
| $\phi_s^3 - \phi_s^0$ (rad) | $0.015 \pm 0.061 \pm 0.021$          |
uncertainty of each parameter and is now quoted explicitly. It is assigned as the difference of fit parameters obtained from the nominal fit and a fit where the resolution model parameters are calibrated using a sample of simulated prompt-\(J/\psi\) events.

The trigger decay-time efficiency model, described in Ref. [6], introduces a systematic uncertainty that is determined by fixing the value of each model parameter in the fit and subsequently repeating the fit with the parameter values constrained within their statistical uncertainty. The quadratic differences of the uncertainties returned and those that are significantly different from zero are assigned as systematic uncertainties. The momentum scale uncertainty reported here, was reported in Ref.[12]. The results of the six \(\Lambda\Lambda\rightarrow J/\psi\phi\) decays of \(89\), consistent with the measurements obtained from the nominal and a modified fit. Other sources of systematic uncertainty are assumed to have negligible parameter correlations. The combined statistical and systematic correlation matrix is given in Ref. [22]. A measurement of \(\phi_{s}\) and \(|\lambda|\) by LHCb using \(B_{s}^{0} \rightarrow J/\psi\pi^{+}\pi^{-}\) decays of \(\phi_{s}^{\pi^{+}\pi^{-}} = 0.070 \pm 0.068 \pm 0.008\) rad and \(|\lambda^{\pi^{+}\pi^{-}}| = 0.89 \pm 0.05 \pm 0.01\), consistent with the measurement reported here, was reported in Ref. [12]. The results

TABLE III. Statistical and systematic uncertainties for the polarization-independent result.

| Source                              | \(\Gamma_{s}\) (ps\(^{-1}\)) | \(\Delta\Gamma_{s}\) (ps\(^{-1}\)) | \(|A_{s}|\) | \(|A_{s}|\) | \(\delta_{s}\) (rad) | \(\delta_{s}\) (rad) | \(\phi_{s}\) (rad) | \(|\lambda|\) | \(\Delta m_{s}\) (ps\(^{-1}\)) |
|-------------------------------------|-------------------------------|-------------------------------|-------------|-------------|------------------|------------------|------------------|-------------|------------------|
| Total statistical uncertainty       | 0.0027                        | 0.0009                        | 0.0049      | 0.0034      | +0.10            | +0.14            | 0.049            | 0.019       | +0.055          |
| Mass factorization                  | \ldots                        | 0.0007                        | 0.0031      | 0.0064      | -0.12            | -0.13            | 0.002            | 0.001       | -0.002          |
| Signal weights (statistical)        | 0.0001                        | 0.0001                        | \ldots      | \ldots      | \ldots            | \ldots            | \ldots            | \ldots       | \ldots          |
| \(b\)-hadron background             | 0.0001                        | 0.0004                        | 0.0004      | 0.0002      | 0.02             | 0.02             | 0.002            | 0.003       | 0.001           |
| \(B_{s}^{+}\) feed down             | 0.0005                        | \ldots                        | \ldots      | \ldots      | \ldots            | \ldots            | \ldots            | \ldots       | \ldots          |
| Angular resolution bias             | \ldots                        | \ldots                        | \ldots      | \ldots      | \ldots            | \ldots            | \ldots            | \ldots       | \ldots          |
| Angular efficiency (reweighting)    | 0.0001                        | \ldots                        | 0.0011      | 0.0020      | -0.01            | 0.01             | 0.001            | 0.005       | 0.002           |
| Angular efficiency (statistical)    | 0.0001                        | 0.0002                        | 0.0011      | 0.0004      | 0.02             | 0.01             | 0.004            | 0.002       | 0.001           |
| Decay-time resolution               | \ldots                        | \ldots                        | \ldots      | \ldots      | \ldots            | \ldots            | \ldots            | \ldots       | \ldots          |
| Trigger efficiency (statistical)    | 0.0011                        | 0.0009                        | \ldots      | \ldots      | \ldots            | \ldots            | \ldots            | \ldots       | \ldots          |
| Track reconstruction (simulation)   | 0.0007                        | 0.0029                        | 0.0005      | 0.0006      | +0.01            | -0.02            | 0.002            | 0.001       | 0.001           |
| Track reconstruction (statistical)  | 0.0005                        | 0.0002                        | \ldots      | \ldots      | \ldots            | \ldots            | \ldots            | \ldots       | \ldots          |
| Length and momentum scales          | 0.0002                        | \ldots                        | \ldots      | \ldots      | \ldots            | \ldots            | \ldots            | \ldots       | \ldots          |
| S-P coupling factors               | \ldots                        | \ldots                        | \ldots      | \ldots      | \ldots            | \ldots            | \ldots            | \ldots       | \ldots          |
| Fit bias                            | \ldots                        | \ldots                        | 0.0005      | \ldots      | 0.01             | 0.01             | \ldots            | \ldots       | \ldots          |
| Quadratic sum of systematics        | 0.0015                        | 0.0032                        | 0.0036      | 0.0067      | +0.06            | 0.07             | 0.06             | 0.007       | 0.011           |

TABLE IV. Statistical and systematic uncertainties for the polarization-dependent result.

| Source                              | \(|\lambda^{0}\)| | \(|\lambda^{0}\)| | \(|\lambda^{0}\)| | \(|\lambda^{0}\)| | \(\phi_{s}^{0}\) (rad) | \(\phi_{s}^{0}\) (rad) | \(\phi_{s}^{+} - \phi_{s}^{0}\) (rad) | \(\phi_{s}^{0} - \phi_{s}^{0}\) (rad) | \(\phi_{s}^{0} - \phi_{s}^{0}\) (rad) |
|-------------------------------------|-----------------|-----------------|-----------------|-----------------|------------------|------------------|------------------|------------------|------------------|
| Total statistical uncertainty       | 0.058           | 0.12            | 0.16            | 0.12            | 0.053            | 0.043            | 0.035            | 0.061            |
| Mass factorization                  | 0.010           | 0.04            | 0.01            | 0.03            | 0.003            | 0.005            | 0.003            | 0.016            |
| \(b\)-hadron background             | 0.002           | 0.01            | \ldots          | 0.01            | 0.003            | 0.001            | 0.001            | 0.009            |
| Angular efficiency (reweighting)    | \ldots          | \ldots          | \ldots          | 0.02            | 0.001            | 0.002            | 0.001            | 0.007            |
| Angular efficiency (statistical)    | 0.004           | 0.02            | 0.01            | 0.01            | 0.004            | 0.007            | 0.005            | 0.004            |
| Decay-time resolution               | 0.006           | 0.01            | \ldots          | 0.01            | 0.003            | 0.002            | 0.001            | 0.002            |
| S-P coupling factors               | \ldots          | \ldots          | \ldots          | \ldots          | \ldots            | \ldots            | \ldots            | \ldots          |
| Quadratic sum of systematics        | 0.013           | 0.05            | 0.01            | 0.04            | 0.007            | 0.009            | 0.006            | 0.021            |
from the two analyses are combined by incorporating the $B^0_s \to J/\psi K^+ K^-$ result as a correlated Gaussian constraint in the $B^0_s \to J/\psi \pi^+ \pi^-$ fit, under the assumption that $B^0_s \to J/\psi \pi^+ \pi^-$ and $B^0_s \to J/\psi K^+ K^-$ decays both proceed dominantly via $b \to c \bar{c} s$ transitions and the ratio between loop-induced processes and tree diagrams are the same in each mode. The fit accounts for correlations between common parameters and correlations between systematic uncertainties. The combined result is $\phi_s = -0.010 \pm 0.039$ rad and $|\lambda| = 0.957 \pm 0.017$. The correlation between the parameters is about $-0.02$.

In conclusion, the $CP$-violating phase $\phi_s$, and the $B^0_s$ decay width parameters $\Gamma_s$ and $\Delta \Gamma_s$, are measured using $B^0_s \to J/\psi K^+ K^-$ decays selected from the full LHCb data set from the first LHC operation period. The results are $\phi_s = -0.058 \pm 0.049 \pm 0.006$ rad, $|\lambda| = 0.964 \pm 0.019 \pm 0.007$, $\Gamma_s = 0.6603 \pm 0.0027 \pm 0.0015$ ps$^{-1}$, and $\Delta \Gamma_s = 0.0805 \pm 0.0091 \pm 0.0032$ ps$^{-1}$. The parameter $|\lambda|$ is consistent with unity, implying no evidence for $CP$ violation in $B^0_s \to J/\psi K^+ K^-$ decays. For the first time, the polarization-dependent $CP$-violating parameters are measured and show no significant difference between the four polarization states. The measurements of $\phi_s$ and $|\lambda|$ in $B^0_s \to J/\psi K^+ K^-$ decays are consistent with those measured in $B^0_s \to J/\psi \pi^+ \pi^-$ decays, and the combined results are $\phi_s = -0.010 \pm 0.039$ rad and $|\lambda| = 0.957 \pm 0.017$. The measurement of the $CP$ violating phase $\phi_s$ and $\Delta \Gamma_s$ are the most precise to date and are in agreement with the SM predictions [27–29], in which it is assumed that subleading contributions to the decay amplitude are negligible. Figure 3 compares this measured value of $\phi_s$ with other independent measurements [8–11,30].

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APPENDIX: SUMMARY OF SYSTEMATIC UNCERTAINTIES

See Tables III and IV.

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