Spin and Flavor Strange Quark Content of the Nucleon

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Abstract

Several spin and flavor dependent parameters characterizing the strangeness content of the nucleon have been calculated in the chiral constituent quark model with configuration mixing (\(\chi\text{CQM}_{\text{config}}\)) which is known to provide a satisfactory explanation of the “proton spin crisis” and related issues. In particular, we have calculated the strange spin polarization \(\Delta s\), the strangeness contribution to the weak axial vector couplings \(\Delta_8\) etc., strangeness contribution to the magnetic moments \(\mu(p)^s\) etc., the strange quark flavor fraction \(f_s\), the strangeness dependent quark flavor ratios \(\frac{2s}{u+d}\) and \(\frac{2s}{u+d}\) etc.. Our results are consistent with the recent experimental observations.
The recent measurements by several groups SAMPLE at MIT-Bates, G0 at JLab, A4 at MAMI and by HAPPEX at JLab regarding the contribution of strangeness to the electromagnetic form factors of the nucleon have triggered a great deal of interest in finding the strangeness magnetic moment of the proton (\(\mu(p)^s\)). The SAMPLE experiment has observed \(\mu(p)^s\) to be 0.37 ± 0.26 ± 0.20 whereas G0, A4 and HAPPEX have observed the combination of electric and magnetic form factors. A global fit has also been carried out by including the data from SAMPLE, G0, A4 and HAPPEX and it gives \(\mu(p)^s = 0.12 ± 0.55 ± 0.07\). The first lattice calculations by Dong et al. give \(-0.36 ± 0.20\) whereas a recent phenomenology study with lattice inputs also predicts a very small value for the strange magnetic moment, \(\mu(p)^s = -0.046 ± 0.19\mu_N\). In the naive constituent quark model (CQM), \(\mu(p)^s\) is predicted to be zero. The broader question of contribution of strangeness in the nucleon has also been discussed by several authors recently. It is widely recognized that a knowledge about the strangeness content of the nucleon would undoubtedly provide vital clues to the non-perturbative aspects of QCD.

The existence of strangeness in the nucleon has been indicated in the context of low energy experiments whereas it has been observed in the deep inelastic scattering (DIS) experiments. In the context of DIS, the strange spin polarization of the nucleon looks to be well established through the measurements of polarized structure functions of the nucleon. Apart from the observations of DIS data regarding strangeness dependent spin polarization functions, several interesting facts have also been revealed regarding the quark flavor distribution functions in the DIS experiments. In particular, the NuSea Collaboration have given the results for the integrals of \(\bar{u} - \bar{d}\) and \(\bar{u}/\bar{d}\) asymmetries indicating that the flavor structure of the nucleon is not limited to \(u\) and \(d\) quarks only. Also the CCFR Collaboration and more recently the NuTeV collaboration have given fairly good deal of information regarding the integrals of strangeness dependent quark ratios in the nucleon given as \(\frac{2\bar{s}}{u+d} = 0.099_{-0.006}^{+0.009}\) and \(\frac{2\bar{s}}{u+d} = 0.477_{-0.053}^{+0.063}\). In the context of low energy experiments, the large pion-nucleon sigma term value indicating non-zero strange quark flavor fraction \(f_s\) is also indicative of the presence of strange quarks in the nucleon although there is no consensus regarding the various mechanisms which can contribute to \(f_s\). Therefore, the indications of the strange quark degree of freedom in DIS as well as low energy experiments provide a strong motivation to examine the strangeness.
contribution to the nucleon thereby giving vital clues to the non-perturbative effects of QCD.

One may think that the strangeness content of the nucleon perhaps can be obtained through the generation of “quark sea” perturbatively from the quark-pair production by gluons. However, this kind of “sea” is symmetric w.r.t. $\bar{u}$ and $\bar{d}$, negated by the observed value of $\bar{u} - \bar{d}$ asymmetry. Therefore, one has to consider the “quark sea” produced by the non-perturbative mechanism. One such model which can yield an adequate description of the “quark sea” generation through the chiral fluctuations is the chiral constituent quark model ($\chi$CQM) which is not only successful in giving a satisfactory explanation of “proton spin crisis” but is also able to account for the violation of Gottfried Sum Rule, baryon magnetic moments and hyperon $\beta$–decay parameters. Recently, it has been shown that configuration mixing generated by spin-spin forces improves the predictions of $\chi$CQM regarding the quark distribution functions and spin polarization functions. Further, the chiral constituent quark model with configuration mixing ($\chi$CQM$_{\text{config}}$) when coupled with the quark sea polarization and orbital angular momentum through the Cheng-Li mechanism is able to give an excellent fit to the octet magnetic moments. It, therefore, becomes desirable to carry out a detailed analysis in the $\chi$CQM$_{\text{config}}$ of the strangeness dependent spin polarization functions as well as the quark distribution functions, particularly in the light of some recent observations.

The purpose of the present communication is to carry out detailed calculations of the parameters characterizing the strangeness of the nucleon within the $\chi$CQM$_{\text{config}}$. In particular, we would like to calculate the strange spin polarization $\Delta_s$, strangeness contribution to the weak axial vector couplings $\Delta_3$, $\Delta_8$ and $\Delta_0$, strangeness contribution to the magnetic moments $\mu(p)^s$ and $\mu(n)^s$, the strange quark flavor fraction $f_s$, the strangeness dependent quark flavor ratios $\frac{2s}{u+d}$ and $\frac{2s}{u+d}$. For the sake of completeness, we would also like to calculate the strangeness contribution to the magnetic moments of decuplet baryons $\mu(\Delta^{++})^s$, $\mu(\Delta^+)^s$, $\mu(\Delta^-)^s$ and $\mu(\Delta^0)^s$ which have not been observed experimentally.

To make the mss. more readable as well as for ready reference, we mention the essentials of $\chi$CQM$_{\text{config}}$, for details we refer the reader to [21, 25, 26]. The basic process in the $\chi$CQM formalism is the emission of a Goldstone boson (GB) by a constituent quark which further splits into a $q\bar{q}$ pair, for example,
where $q\bar{q}$ and $q'$ constitute the “quark sea” [21] and the ± signs refer to the quark helicities. The effective Lagrangian describing interaction between quarks and a nonet of GBs, consisting of octet and a singlet, can be expressed as

$$\mathcal{L} = g_8 \bar{q} \left( \Phi + \zeta \eta \sqrt{\frac{3}{I}} \right) q = g_8 \bar{q} \left( \Phi' \right) q,$$

where $\zeta = g_1/g_8$, $g_1$ and $g_8$ are the coupling constants for the singlet and octet GBs, respectively, $I$ is the $3 \times 3$ identity matrix. The GB field which includes the octet and the singlet GBs is written as

$$\Phi' = \begin{pmatrix}
\frac{\pi^0}{\sqrt{2}} + \beta \frac{\eta}{\sqrt{6}} + \zeta \frac{\eta'}{\sqrt{3}} & \pi^+ & \alpha K^+ \\
\pi^- & -\frac{\pi^0}{\sqrt{2}} + \beta \frac{\eta}{\sqrt{6}} + \zeta \frac{\eta'}{\sqrt{3}} & \alpha K^0 \\
\alpha K^- & \alpha K^0 & -\beta \frac{2\eta}{\sqrt{6}} + \zeta \frac{\eta'}{\sqrt{3}}
\end{pmatrix} \quad \text{and} \quad q = \begin{pmatrix} u \\ d \\ s \end{pmatrix}.$$

SU(3) symmetry breaking is introduced by considering $M_s > M_{u,d}$ as well as by considering the masses of GBs to be nondegenerate ($M_{K,\eta} > M_\pi$ and $M_{\eta'} > M_{K,\eta}$) [21, 25]. The parameter $a = \left| g_8 \right|^2$ denotes the probability of chiral fluctuation $u(d) \rightarrow d(u) + \pi^+(-)$, $\alpha^2 a$, $\beta^2 a$ and $\zeta^2 a$ respectively denote the probabilities of fluctuations $u(d) \rightarrow s + K^-(0)$, $u(d, s) \rightarrow u(d, s) + \eta$ and $u(d, s) \rightarrow u(d, s) + \eta'$. Further, to make the transition from $\chi$CQM to $\chi$CQM$_{\text{config}}$, the nucleon wavefunction gets modified because of the configuration mixing generated by the chromodynamic spin-spin forces [8, 9, 10, 26] as follows,

$$|B\rangle = \cos \phi |56, 0^+\rangle_{N=0} + \sin \phi |70, 0^+\rangle_{N=2},$$

where $\phi$ represents the $|56\rangle - |70\rangle$ mixing. For details of the spin, isospin and spatial parts of the wavefunction, we refer the reader to [29].

Before proceeding further, we briefly discuss the strangeness dependent spin polarization functions, quark distribution functions and the related quantities of the nucleon. To begin with, we consider the spin structure of a nucleon defined as [21]

$$\hat{B} \equiv \langle B \mid N \mid B \rangle,$$

where $|B\rangle$ is the nucleon wavefunction defined in Eq. (4) and $N$ is the number operator given by

$$N = n_{u_+}u_+ + n_{u_-}u_- + n_{d_+}d_+ + n_{d_-}d_- + n_{s_+}s_+ + n_{s_-}s_-,$$
\( n_{q_\pm} \) being the number of \( q_\pm \) quarks. Following Ref. [26], the contribution to the proton spin by different quark flavors in \( \chi \text{CQM}_{\text{config}} \) can be given by the spin polarizations \( \Delta q = q_+ - q_- \) expressed as

\[
\Delta u = \cos^2 \phi \left[ \frac{4}{3} - \frac{a}{3}(7 + 4\alpha^2 + \frac{4}{3}\beta^2 + \frac{8}{3}\zeta^2) \right] + \sin^2 \phi \left[ \frac{2}{3} - \frac{a}{3}(5 + 2\alpha^2 + \frac{2}{3}\beta^2 + \frac{4}{3}\zeta^2) \right],
\]

(7)

\[
\Delta d = \cos^2 \phi \left[ -\frac{1}{3} - \frac{a}{3}(2 - \alpha^2 - \frac{1}{3}\beta^2 - \frac{2}{3}\zeta^2) \right] + \sin^2 \phi \left[ \frac{1}{3} - \frac{a}{3}(4 + \alpha^2 + \frac{1}{3}\beta^2 + \frac{2}{3}\zeta^2) \right],
\]

(8)

\[
\Delta s = \cos^2 \phi \left[-a\alpha^2\right] + \sin^2 \phi \left[-a\alpha^2\right].
\]

(9)

A closer look at the above equations reveals that \( \phi \) represents the configuration mixing angle, the constant factors represent the CQM results and the factors which are multiple of \( a \) represent the contribution from the “quark sea”. It is important to mention here that the presence of \( s\bar{s} \) in the “quark sea” (Eq. (1)) involves the terms \( \alpha^2a, \beta^2a \) and \( \zeta^2a \) respectively denoting the fluctuations \( u(d) \to s + K^{+}(0), u(d,s) \to u(d,s) + \eta \) and \( u(d,s) \to u(d,s) + \eta' \).

It is clear from the above fluctuations that the strange quarks come from the fluctuations of the \( u \) and \( d \) quarks as well and therefore, apart from contributing to the strange spin polarization, the strange quarks also contribute to the spin polarizations of \( u \) and \( d \) quarks. It should also be noted that the \( \bar{d} - \bar{u} \) asymmetry in this case can be easily understood in terms of the above fluctuations where the valence \( u \) quarks are likely to produce more \( \bar{d} \) than the valence \( d \) quarks producing \( \bar{u} \) in the proton. The spin polarization functions are also related to the axial vector couplings measured in the baryon weak decays [18], for example, the non-singlet combinations of the quark spin polarizations (\( \Delta_3 \) and \( \Delta_8 \)) can be expressed as

\[
\Delta_3 = \Delta u - \Delta d = F + D,
\]

(10)

\[
\Delta_8 = \Delta u + \Delta d - 2\Delta s = 3F - D,
\]

(11)

where \( F \) and \( D \) are the usual \( SU(3) \) parameters characterizing the weak matrix elements. The flavor singlet combination on the other hand can be related to the total spin carried by the quarks as

\[
\Delta_0 = \frac{1}{2} \Delta \Sigma = \frac{1}{2} (\Delta u + \Delta d + \Delta s).
\]

(12)

After discussing the spin polarization functions, we would like to discuss the formalism for the strangeness contribution to the magnetic moments. It would be important to mention
here that the predictions for all the octet and decuplet baryon magnetic moments including the transition magnetic moments have been discussed in detail in Ref. [27] and have been found to be in good agreement with the recent measurements as well as other theoretical estimates. The magnetic moment of a given baryon in the $\chi$CQM can be expressed as

$$\mu(B)_{\text{total}} = \mu(B)_{\text{val}} + \mu(B)_{\text{sea}},$$

(13)

where $\mu(B)_{\text{val}}$ represents the contribution of the valence quarks and $\mu(B)_{\text{sea}}$ corresponding to the "quark sea" (Eq. (1)). Further, $\mu(B)_{\text{sea}}$ can be written as

$$\mu(B)_{\text{sea}} = \mu(B)_{\text{spin}} + \mu(B)_{\text{orbit}},$$

(14)

where the first term is the magnetic moment contribution of the $q^{'}$ in Eq. (1) coming from the spin polarization and the second term is due to the rotational motion of the two bodies, $q^{'}$ and GB, corresponding to the fluctuation given in Eq. (1) and referred to as the orbital angular momentum by Cheng and Li [21].

To find the strangeness contribution to the magnetic moment of the proton $\mu(p)^s$ we should note that there are no ‘strange’ valence quarks, therefore $\mu(p)^s$ receives contributions only from the “quark sea” and is expressed as

$$\mu(p)^s = \mu(p)^s_{\text{spin}} + \mu(p)^s_{\text{orbit}}.$$

(15)

Following Ref. [27], $\mu(p)^s_{\text{spin}}$ in the chiral constituent quark model with configuration mixing can be expressed as

$$\mu(p)^s_{\text{spin}} = \sum_{q=u,d,s} \Delta q(p)^s_{\text{sea}} \mu_q,$$

(16)

where $\mu_q = \frac{e_q}{2M_q}$ ($q = u, d, s$) is the quark magnetic moment, $e_q$ and $M_q$ are the electric charge and the mass respectively for the quark $q$. The contribution of strangeness to the spin polarization functions is given as

$$\Delta u(p)^s_{\text{sea}} = \cos^2 \phi \left[ -\frac{a}{3} (4\alpha^2 + \frac{4}{3}\beta^2 + \frac{8}{3}\zeta^2) \right] + \sin^2 \phi \left[ -\frac{a}{3} (2\alpha^2 + \frac{2}{3}\beta^2 + \frac{4}{3}\zeta^2) \right],$$

(17)

$$\Delta d(p)^s_{\text{sea}} = \cos^2 \phi \left[ -\frac{a}{3} (-\alpha^2 - \frac{1}{3}\beta^2 - \frac{2}{3}\zeta^2) \right] + \sin^2 \phi \left[ -\frac{a}{3} (\alpha^2 + \frac{1}{3}\beta^2 + \frac{2}{3}\zeta^2) \right],$$

(18)

$$\Delta s(p)^s_{\text{sea}} = \cos^2 \phi \left[ -a\alpha^2 \right] + \sin^2 \phi \left[ -a\alpha^2 \right].$$

(19)
Similarly, the contribution of the orbital angular momentum of the “quark sea” to the magnetic moment of a given quark is expressed as
\[
\mu(p)^{\text{orbit}} = \frac{4}{3} \mu(u_+ \rightarrow s_-) - \frac{1}{3} \mu(d_+ \rightarrow s_-), \tag{20}
\]
where
\[
\mu(q_+ \rightarrow s_-) = \frac{e_s}{2M_q} \langle l_q \rangle + \frac{e_q - e_s}{2M_{GB}} \langle l_{GB} \rangle. \tag{21}
\]
The quantities \(l_q, l_{GB}\) and \((M_q, M_{GB})\) are the orbital angular momenta and masses of quark and GB, respectively. The orbital angular momentum contribution to the magnetic moment due to all the fluctuations is then given as

\[
\mu(u_+ \rightarrow s^-) = a \left[ -\frac{M_u^2}{2M_\pi(M_u + M_\pi)} - \frac{\alpha^2(M_K^2 - 3M_\eta^2)}{2M_K(M_u + M_K)} + \frac{(3 + \beta^2 + 2\zeta^2)M_\eta^2}{6M_\eta(M_u + M_\eta)} \right] \mu_N, \tag{22}
\]

\[
\mu(d_+ \rightarrow s_-) = a \frac{M_u}{M_d} \left[ -\frac{\alpha^2M_K^2}{2M_K(M_d + M_K)} - \frac{(\beta^2 + 2\zeta^2)M_\eta^2}{12M_\eta(M_d + M_\eta)} \right] \mu_N, \tag{23}
\]
where \(M_\pi, M_K\) and \(M_\eta\) are the masses of pion, Kaon and \(\eta\) respectively and \(\mu_N\) is the Bohr magneton. The strangeness contribution to the magnetic moments of the neutron \(n(ddu)\) as well as the decuplet baryons \(\Delta^{++}(uuu), \Delta^{+}(uud), \Delta^0(udd)\) and \(\Delta^-(ddd)\) can be calculated similarly.

The integral of the quark distribution functions incorporating the strangeness content in the \(\chi\)CQM are expressed as \cite{21, 26}

\[
\bar{u} = \frac{1}{12} [(2\zeta + \beta + 1)^2 + 20]a, \quad \bar{d} = \frac{1}{12} [(2\zeta + \beta - 1)^2 + 32]a, \quad \bar{s} = \frac{1}{3} [(\zeta - \beta)^2 + 9\alpha^2]a, \tag{24}
\]

\[
u - \bar{u} = 2, \quad d - \bar{d} = 1, \quad s - \bar{s} = 0. \tag{25}
\]
The integral of the quark distribution functions would henceforth be referred to as ‘averaged’ quark distribution functions.

Similarly, the other important quantities having implications for the strangeness contribution to the nucleon are the averaged quark flavor fractions \(f_q = \frac{q^+q}{\sum_q(q^+q)}\) which are expressed in terms of the \(\chi\)CQM parameters as

\[
f_u = \frac{12 + a(21 + \beta^2 + 4\zeta + 4\zeta^2 + \beta(2 + 4\zeta))}{3(6 + a(9 + \beta^2 + 6\alpha^2 + 2\zeta^2))},
\]

\[
f_d = \frac{6 + a(33 + \beta^2 - 4\zeta + 4\zeta^2 + \beta(-2 + 4\zeta))}{3(6 + a(9 + \beta^2 + 6\alpha^2 + 2\zeta^2))},
\]

\[
f_s = \frac{4a(\beta^2 + +9\alpha^2 - 2\beta\zeta + \zeta^2)}{3(6 + a(9 + \beta^2 + 6\alpha^2 + 2\zeta^2))}. \tag{26}
\]
It is clear from the above expressions that the non zero value of the parameters $a$, $\alpha$, $\beta$ and $\zeta$ implies $f_s \neq 0$ as well as modify $f_u$ and $f_d$ due to the strangeness contributions coming from the “quark sea”. Further, the ratio of the functions

$$f_3 = f_u - f_d, \quad f_8 = f_u + f_d - 2f_s,$$  \hspace{1cm} (27)

and the averaged ratios

$$\frac{2s}{(u + d)} = \frac{4a(9\alpha^2 + \beta^2 - 2\beta \zeta + \zeta^2)}{18 + a(27 + \beta^2 + 4\beta \zeta + 4\zeta^2)}, \quad \frac{2\bar{s}}{\bar{u} + \bar{d}} = \frac{4(9\alpha^2 + \beta^2 - 2\beta \zeta + \zeta^2)}{27 + \beta^2 + 4\beta \zeta + 4\zeta^2},$$  \hspace{1cm} (28)

have also been measured, therefore providing an opportunity to check the strange quark content of the nucleon.

The $\chi_{\text{CQM}}^{\text{config}}$ involves five parameters, four of these $a$, $a\alpha^2$, $a\beta^2$, $a\zeta^2$ representing respectively the probabilities of fluctuations to pions, $K$, $\eta$, $\eta'$, following the hierarchy $a > \alpha > \beta > \zeta$, while the fifth representing the mixing angle. The mixing angle $\phi$ is fixed from the consideration of neutron charge radius \cite{10}, whereas for the other parameters we would like to update our analysis using the latest data \cite{31}. In this context, we find it convenient to use $\Delta u$, $\Delta_3$, $\bar{u} - \bar{d}$ and $\bar{u}/\bar{d}$ as inputs with their latest values given in Tables \ref{table1} and \ref{table3}. Before carrying out the fit to the above mentioned parameters, we would like to find their ranges by qualitative arguments. To this end, the range of the symmetry breaking parameter $a$ can be easily found by considering the spin polarization function $\Delta u$, by giving the full variation to the parameters $\alpha$, $\beta$ and $\zeta$, for example, one finds $0.10 \lesssim a \lesssim 0.14$. The range of the parameter $\zeta$ can be found from averaged $\bar{u}/\bar{d}$ using the latest experimental measurement \cite{19}, and it comes out to be $-0.70 \lesssim \zeta \lesssim -0.10$. Using the above found ranges of $a$ and $\zeta$ as well as the latest measurement of $\bar{u} - \bar{d}$ asymmetry \cite{19}, $\beta$ comes out to be in the range $0.2 \lesssim \beta \lesssim 0.7$. Similarly, the range of $\alpha$ can be found by considering the flavor non-singlet component $\Delta_3$ and it comes out to be $0.2 \lesssim \alpha \lesssim 0.5$. After finding the ranges of the symmetry breaking parameters, we have carried out a fine grained analysis using the above ranges as well as considering $\alpha \approx \beta$ by fitting $\Delta u$, $\Delta_3$ \cite{31} as well as $\bar{u} - \bar{d}$, $\bar{u}/\bar{d}$ \cite{19} leading to $a = 0.13$, $\zeta = -0.10$, $\alpha = \beta = 0.45$ as the best fit values. The parameters so obtained have been used to calculate the spin polarization functions and the averaged quark distribution functions. The calculated quantities pertaining to spin polarization functions have been corrected by including the gluon polarization effects...
and symmetry breaking effects \[21, 25\]. Similarly, the averaged quark distribution functions have been corrected by including the symmetry breaking effects. The orbital angular momentum contributions to magnetic moment are characterized by the parameters of \( \chi \text{CQM} \) as well as the masses of the GBs. For the \( u \) and \( d \) quarks, we have used their most widely accepted values in hadron spectroscopy \[21, 29\], for example, \( M_u = M_d = 330 \text{ MeV} \). For evaluating the contribution of GBs, we have used its on mass shell value in accordance with several other similar calculations \[33\].

In Tables I-III we have presented the results of our calculations pertaining to the strangeness dependent parameters in \( \chi \text{CQM}_{\text{config}} \). For comparison sake, we have also given the corresponding quantities in CQM. To begin with, we first discuss the quality of fit pertaining to the spin polarization functions. In Table II we have presented the strangeness incorporating spin polarization functions and the weak axial vector couplings. Using \( \Delta u \), \( \Delta d \) along with \( \bar{u} - \bar{d}, \bar{u}/\bar{d} \) from Table III as inputs, we find that we are able to achieve a fairly good fit in the case of spin polarization functions and the weak axial vector couplings. In particular, the agreement in terms of the magnitude as well as the sign in the case of \( \Delta s \) is in good agreement with the latest data \[15, 16\]. The agreement in the case of \( \Delta g \) and \( \Delta_0 \), which receives contribution from \( \Delta s \) also, not only justify the success of \( \chi \text{CQM}_{\text{config}} \) but also strengthen our conclusion regarding \( \Delta s \). Similarly, the agreement obtained in the case of the ratio \( F/D \) again reinforces our conclusion that \( \chi \text{CQM}_{\text{config}} \) is able to generate qualitatively as well as quantitatively the requisite amount of strangeness in the nucleon.

In Table III we have presented the spin and orbital contributions pertaining to the strangeness magnetic moment of the nucleon and \( \Delta \) baryons. From the Table one finds that the present result for the strangeness contribution to the magnetic moment of proton looks to be in agreement with the most recent results available for \( \mu(p)^s \) \[1, 3, 6, 7\]. On closer examination of the results, several interesting points emerge. The strangeness contribution to the magnetic moment is coming from spin and orbital angular momentum of the “quark sea” with opposite signs. These contributions are fairly significant and they cancel in the right direction to give the right magnitude to \( \mu(p)^s \). For example, the spin contribution in this case is \(-0.09\mu_N\) and the contribution coming from the orbital angular momentum is \(0.05\mu_N\). These contributions cancel to give a small value for \( \mu(p)^s = -0.03\mu_N \) which is consistent with the other observed results. Interestingly, in the case of \( \mu(n)^s \), the magnetic
moment is dominated by the orbital part as was observed in the case of the total magnetic moments \cite{27} however, the total strangeness magnetic moment is same as that of the proton. Therefore, an experimental observation of this would not only justify the Cheng-Li mechanism \cite{21} but would also suggest that the chiral fluctuations is able to generate the appropriate amount of strangeness in the nucleon. For the sake of completeness, we have also presented the results of $\mu(\Delta^{++})^s$, $\mu(\Delta^+)^s$, $\mu(\Delta^o)^s$, $\mu(\Delta^-)^s$ and here also we find that there is a substantial contribution from spin and orbital angular momentum. In general, one can find that whenever there is an excess of $d$ quarks the orbital part dominates, whereas when we have an excess of $u$ quarks, the spin polarization dominates.

After finding that the $\chi$CQM$_{\text{config}}$ is able to give a fairly good account of the spin dependent polarization functions, in Table III we have presented the results of averaged quark distribution functions having implications for strangeness in the nucleon. In line with the success of $\chi$CQM$_{\text{config}}$ in describing the spin dependent polarization functions, in this case also we are able to give a fairly good account of most of the measured values. The agreement in the case of $\frac{2s}{u+d}$ and $\frac{f_s}{f_8}$ indicates that, in the $\chi$CQM, we are able to generate the right amount of strange quarks through chiral fluctuation. A refinement in the case of the strangeness dependent quark ratio $\frac{2s}{u+d}$ would have important implications for the basic tenets of $\chi$CQM. The observed result for the case of $f_s$ in the present case also indicates that the strange sea quarks play a significant role in the nucleon. This is in agreement with the observations of other authors \cite{20, 21}.

To summarize, the $\chi$CQM$_{\text{config}}$ is able to provide a fairly good description of the spin dependent polarization functions as well as the averaged quark distribution functions having implications for strangeness in the nucleon. It is able to give a quantitative description of the important parameters such as $\Delta s$, the weak axial vector couplings $\Delta_8$ and $\Delta_0$, strangeness contribution to the magnetic moment $\mu(p)^s$, the strange quark flavor fraction $f_s$, the strangeness dependent ratios $\frac{2s}{u+d}$ and $\frac{f_s}{f_8}$ etc.. In the case of $\mu(p)^s$, our result is consistent with the latest experimental measurements as well as with the other calculations. In conclusion, we would like to state that at the leading order constituent quarks and the weakly interacting Goldstone bosons constitute the appropriate degrees of freedom in the nonperturbative regime of QCD and the “quark sea” generation in the $\chi$CQM$_{\text{config}}$ through the chiral fluctuation is the key in understanding the strangeness content of the nucleon.
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TABLE I: The calculated values of the strangeness dependent spin polarization functions and weak axial vector couplings in the CQM and $\chi_{\text{CQM}}^{\text{config}}$.

| Parameter | Data          | CQM  | $\chi_{\text{CQM}}^{\text{config}}$ |
|-----------|--------------|------|-------------------------------------|
| $\Delta u^*$ | $0.85 \pm 0.05 \ [15]$ | 1.333 | 0.867                               |
| $\Delta d$   | $-0.41 \pm 0.05 \ [15]$ | $-0.333$ | $-0.392$                           |
| $\Delta s$   | $-0.10 \pm 0.04 \ [15]$ | 0   | $-0.08$                             |
| $\Delta s^*$ | $-0.07 \pm 0.03 \ [16]$ | 1.267 | 1.267                               |
| $\Delta s_3$ | $1.267 \pm 0.0035 \ [31]$ | 1.666 | 1.267                               |
| $\Delta s_8$ | $0.58 \pm 0.025 \ [31]$ | 1   | 0.59                                |
| $\Delta s_0$ | $0.19 \pm 0.025 \ [31]$ | 0.50 | 0.19                                |
| $F/D$        | $0.575 \pm 0.016 \ [31]$ | 0.673 | 0.589                               |

* Input parameters

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| Parameter                                                                 | Data            | CQM  | $\chi$CQM$_{\text{config}}$ |
|--------------------------------------------------------------------------|-----------------|------|-----------------------------|
| $\mu(p)^s_{\text{spin}}, \mu(p)^s_{\text{orbit}}$                      | $-\mu(p)^s$     | $0, 0$ | $-0.09, 0.05$              |
| $\mu(p)^s$                                                               | $0.37 \pm 0.26 \pm 0.20$ [1] | $0$  | $-0.03$                     |
| $\mu(n)^s_{\text{spin}}, \mu(n)^s_{\text{orbit}}$                      | $-\mu(n)^s$     | $0, 0$ | $0.06, -0.09$              |
| $\mu(n)^s$                                                               | $0.12 \pm 0.55 \pm 0.07$ [5] | $0$  | $-0.03$                     |
| $\mu(\Delta^{++})^s_{\text{spin}}, \mu(\Delta^{++})^s_{\text{orbit}}$ | $-\mu(\Delta^{++})^s$ | $0, 0$ | $-0.29, 0.18$              |
| $\mu(\Delta^{++})^s$                                                    | $-\mu(\Delta^{++})^s$ | $0$  | $-0.11$                     |
| $\mu(\Delta^+)^s_{\text{spin}}, \mu(\Delta^+)^s_{\text{orbit}}$       | $-\mu(\Delta^+)^s$ | $0, 0$ | $-0.14, 0.11$              |
| $\mu(\Delta^+)^s$                                                       | $-\mu(\Delta^+)^s$ | $0$  | $-0.03$                     |
| $\mu(\Delta^o)^s_{\text{spin}}, \mu(\Delta^o)^s_{\text{orbit}}$       | $-\mu(\Delta^o)^s$ | $0, 0$ | $-0.04, -0.03$             |
| $\mu(\Delta^o)^s$                                                       | $-\mu(\Delta^o)^s$ | $0$  | $-0.07$                     |
| $\mu(\Delta^-)^s_{\text{spin}}, \mu(\Delta^-)^s_{\text{orbit}}$       | $-\mu(\Delta^-)^s$ | $0, 0$ | $-0.09, 0.15$              |
| $\mu(\Delta^-)^s$                                                       | $-\mu(\Delta^-)^s$ | $0$  | $0.06$                      |

**TABLE II**: The calculated values of the strangeness contribution to the magnetic moment of nucleon and $\Delta$ decuplet baryons in the CQM and $\chi$CQM$_{\text{config}}$. 
TABLE III: The calculated values of the strangeness dependent averaged quark flavor distribution functions and related parameters in the CQM and $\chi_{CQM_{\text{config}}}$.

| Parameter | Data       | CQM | $\chi_{CQM_{\text{config}}}$ |
|-----------|------------|-----|-----------------------------|
| $\bar{s}$ | $-         | 0   | 0.10                        |
| $\bar{u} - d^s$ | $-0.118 \pm 0.015$ [19] | 0   | $-0.118$                    |
| $\bar{u}/d^s$ | $0.67 \pm 0.06$ [19] | 0   | 0.66                        |
| $\frac{2\bar{s}}{u+d}$ | $0.099^{+0.009}_{-0.006}$ [12] | 0   | 0.09                        |
| $\frac{2\bar{s}}{u+d}$ | $0.477^{+0.063}_{-0.053}$ [12] | 0   | 0.44                        |
| $f_s$     | $0.10 \pm 0.06$ [12] | $-$ | 0.08                        |
| $f_3$     | $-$        | $-$ | 0.21                        |
| $f_8$     | $-$        | $-$ | 1.03                        |
| $f_3/f_8$ | $0.21 \pm 0.05$ [12] | 0.33 | 0.20                        |

* Input parameters