Metallic states appearing at interfaces between dissimilar insulating oxides exhibit intriguing phenomena such as superconductivity and magnetism. Despite tremendous progress in understanding their origins, very little is known about how to control the conduction pathways and the distribution of charge carriers.

Using optical spectroscopic measurements and density-functional theory (DFT) simulations, we examine the effect of SrTiO$_3$ (STO) spacer layer thickness on the optical transparency and carrier distribution in La $\delta$-doped STO superlattices. We experimentally observe that these metallic superlattices remain highly transparent to visible light; a direct consequence of the appropriately large gap between the O 2p and Ti 3d states. In superlattices with relatively thin STO layers, we predict that three-dimensional conduction would occur due to appreciable overlap of quantum mechanical wavefunctions between neighboring $\delta$-doped layers. These results highlight the potential for using oxide heterostructures in optoelectronic devices by providing a unique route for creating novel transparent conducting oxides.

High mobility two-dimensional electron gases (2DEGs) formed at atomically-well defined heterointerfaces provide an ideal platform for exploring novel quantum phenomena and developing advanced high-speed electronic devices. Indeed the layer-by-layer growth of heterostructures with precisely-controlled chemical compositions at the atomic scale have opened the door to the artificial design of interface-engineered heterostructures; an advancement at the core of the semiconductor industry. A prominent discovery, borne out of such an interface-engineered heterostructure, is the presence of a 2DEG. In semiconductors, 2DEGs reveal extremely high mobility, especially, at low temperatures. Furthermore, they reside at quantized energy levels and, therefore, offer many intriguing quantum phenomena, such as the quantum Hall effect and the fractional quantum Hall effect. 2DEGs derived from transition-metal oxide heterostructures would offer another degree of freedom for manipulating the electrical properties through the strong correlations of d-band electrons.

Recently, it has been demonstrated that such a 2DEG could be created in an oxide heterostructure through interfacial electronic reconstruction or the introduction of oxygen vacancies at the STO surface. The former includes a heterostructure composed of the Mott insulator LaTiO$_3$ (LTO) and the band insulator STO, which generates a high-density of carriers, up to 0.5 electrons per unit cell area or $n_{2D} \sim 3 \times 10^{14}$ cm$^{-2}$ (Ref. 13), with transport that occurs along multiple channels resulting in high mobility through alleviated transport bottlenecks in a superlattice structure. These features offer tremendous promise for realizing oxide electronics or photovoltaics with 2DEGs. However, the spatial extent of the conducting carriers away from the interfaces in a short-period superlattice has not been fully explored. Despite an early scanning transmission electron microscopy (STEM)-electron energy loss spectroscopy (EELS) study by Ohtomo et al., which demonstrated that the spatial extent of the electron distribution was ~2 nm or ~5 unit cells (u.c.) away from the interface at room temperature, very little effort has been focused on understanding the consequences of this leakage for electronic transport within a superlattice.

In this regard, $\delta$-doped superlattices present the ideal framework for understanding the electronic reconstruction that can occur at oxide interfaces, both from theory and experiment. For example, we recently demonstrated that by controlling the fraction of “dopant” ions at the interface one can achieve a significant enhancement in the mobility of the carriers at an interface. Moreover, since the effects are purely driven by chemistry, physical mechanisms such as the polar-catastrophe do not apply and thus it is possible to explore the effects of the thickness of the insulating layer (i.e. STO) using standard experimental geometries. From the perspective of
Here, we investigate the effect of the STO insulating layer thickness on the optical properties and electronic structures of La δ-doped STO superlattices. Using atomically controlled superlattices, we experimentally show that these materials remain highly transparent to visible light, irrespective of STO spacer thicknesses. Our DFT calculations indicate that this is a direct consequence of minimal changes in the band gap between O 2p and Ti 3d states. Furthermore, using DFT we examine the effect of STO layer thickness on the amplitude of charge density in the STO spacer region due to the overlap of the wavefunctions permeating from neighboring, conductive δ-doped layers. Our results for thinner STO spacers indicate a clear crossover from 2D carrier density profiles to 3D, with the emergence of a single electronic band with light effective mass. This may be indicative of enhanced conductivity perpendicular to the interface. Together, these results illustrate that it is possible to create a 3D, transparent conducting oxide by engineering the wavefunction of 2D materials. These results have importance for building design concepts for tuning the properties at oxide interfaces; with particular consequences for the field of mesoscale optoelectronics.

Results

Optical properties. Typically, doped conducting transition-metal oxides, for instance La-, Nb-, or oxygen vacancy-doped STO, have high light-absorption due to accompanying defects and/or deep-level impurities\(^1\), resulting in significant opacity (e.g., see the inset of Figure 1a). As such transition-metal oxides with partially filled \(d\)-band electrons are generally considered to be poor candidates for transparent conducting oxides (TCOs). However, LTO/STO superlattices with electronically-constructed interfaces represent completely different band structures as compared to those of chemically-doped STOs, which typically create in-gap states\(^1\). Figure 1a depicts the optical transmittance (\(T\)) for [L1/S2], [L1/S4] and [L1/S6] superlattices grown by pulsed laser deposition (PLD) on TiO\(_2\)-terminated (001) STO single crystal substrates (i.e. STO spacer thicknesses of 2, 4 and 6 layers, respectively). Similar to an undoped STO crystal, all of the La δ-doped STO superlattices are transparent in the visible range, while showing clear evidence of conducting carriers, i.e., the Drude absorption, in the low photon energy region (<1.5 eV). Using a simple Drude model fit, we have calculated the extinction coefficient (\(k\)) of the complex refractive index (\(\hat{n} = n + ik\)) as a function of photon energy. This fit confirms that the δ-doped superlattices remain transparent in the visible range (Figure 1b). Note that the higher interface density in the [L1/S2] superlattices results in lower transmittance as compared to the longer period superlattices (Figure 1). It is worth noting that both the measured transmittance and resistivity of the superlattices are comparable to those of the most widely used TCO, i.e. Sn-doped In\(_2\)O\(_3\) (ITO) (\(T = 80\%, \rho = 200 \mu\Omega\)-cm\(^2\)), and the superlattices’ room-temperature carrier mobility is also comparable to that of ITO as we reported elsewhere\(^13\).

As evident from the density of states (DOS) shown in Figure 2, δ-doped superlattices have their Fermi levels residing within the Ti bands and the gap between the O 2p states and Ti 3d\(-t_2g\) states (the allowed optical transition) remains, relatively, the same as in undoped STO. As such, these materials should be transparent to visible light. (N.B.: Our DFT calculations underestimate the band gap; thus, even though they are smaller than the required 3 eV, the results are consistent with a material that would be optically transparent). This is unlike the O-deficient SrTiO\(_2\)\(_{87.5}\), where dopants result in the narrowing of the band gap through the creation of in-gap states (see Figure 2 and 3b). Additionally, analysis of the band structure (Figure 3c and d) shows that the transitions from the conduction states to higher lying unoccupied 3d-states are ~2 eV or less, consistent with the Drude feature observed experimentally (Figure 1a).

Electronic reconstruction. While these superlattices have very similar optical properties, their electronic properties could be very different. Indeed, we know from experiment that the spatial extent of the electrons is roughly 3–5 unit cell\(^1\)\(^6\)\(^9\) away from the interface which could result in significant overlap in the carrier densities in superlattices with thinner STO spacer regions. In order to fully explore the dimensional behavior, we examine the spatial distribution of the 2DEG carrier densities as a function of STO.

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**Figure 1 |** (a) Optical transmittance (\(T\)) of the [L1/S2], [L1/S4] and [L1/S6] superlattices (60 nm in total thickness) on STO substrates as a function of photon energy (\(\omega\)). Optical spectra for a bare STO substrate and an oxygen-vacancy-doped STO film (100 nm thick) on STO are also shown for comparison. Superlattice samples clearly show the Drude absorption and no noticeable absorption due to in-gap states. Inset: Photographs of bare STO substrate, [L1/S4], and oxygen-vacancy-doped STO film. The oxygen-vacancy-doped STO absorbs a significant portion of visible light with clear evidence of in-gap defect states, as marked with arrows. (b) Extinction coefficient (\(k\)) and refractive index (\(n\)), and (c) optical conductivity (\(\sigma\)) of the [L1/S2], [L1/S4] and [L1/S6] superlattices obtained from a Drude fit to the experimental transmittance data. The net carrier density and mobility for each sample are listed for convenience. For all three samples the carrier density is within experimental error bars of 0.5 e\(^+/\)interface\(^13\).
To compute the number of electrons that contribute to the 2DEG carrier density, we sum up the atomic projected DOS for the partially occupied states just below the Fermi level, $E_F$ (see Figure 3). In agreement with previous studies, for all three superlattices, the total DOS sums up to exactly 1 electron (or rather 0.5 e/2interface$^{24–26}$. (Note: Due to the integration sphere for computing the atom projected DOS, the partial DOS for the [L1/S2], [L1/S6] and [L1/S10] sum up to 0.95 electrons.) As seen in Figure 4c, in the [L1/S10] superlattice, the extra electron due to the electronic reconstruction is adequately screened in the bulk of STO, indicating that the accumulated charge extends to roughly 3 unit cells away from the interface. Similar results are observed for the [L1/S6] superlattice (Figure 4b). However, in this case, while there is a substantial drop in the charge density profile away from the interface, the relatively thinner STO layers in the [L1/S6] system allow for some wavefunction overlap and therefore the charge density does not completely disappear as in the [L1/S10] superlattices. These results are in good agreement with previous theory and experiment$^{9,11,24–29}$.

Moreover, the spatial distribution of the electrons is expected to play an important role in controlling transport away from the oxide interface in superlattices with shorter STO spacer regions. Indeed in the [L1/S2] superlattice, the wavefunction overlap results in very little change in the total number of conduction electrons within the STO layers (Figure 4a). This charge density profile indicates that the conductivity in the direction perpendicular to the oxide interface.

A detailed comparison of the electronic band structure of the [L1/S2] and [L1/S6] heterostructures reveals two important features (as shown in Figure 3). First, we observe a significant difference in the Fermi surfaces (FS) of the two systems. Specifically, we find an increased FS volume in the [L1/S2] superlattice. Four rods extending along the $C_X$-X and the $C_X$-Y directions indicate the large contribution from $d_{xz}$ and $d_{yz}$ states. Second, this increased FS volume is accompanied by the population of a light electron effective mass band in the $C_X$-Z direction again originating from the $d_{xz}$ and $d_{yz}$ states (as determined from a $k$-resolved DOS analysis; see Supplementary Information Figure S1). These two features point to enhanced...
mobility in the out-of-plane direction; signaling a crossover from 2D to 3D conductivity.

Experimentally, angle-dependent Shubnikov de Haas (SdH) oscillations can be used to confirm the dimensional crossover from 2D to 3D conductivity; with the oscillations disappearing in the 2D conducting case as the angle is rotated away from the \( k_x-k_y \) plane.\(^{9,26,27,28} \) However, while resistivity measurements clearly show that the samples are highly conducting, we were unable to observe SdH oscillations in our samples even at temperatures down to 25 mK and magnetic fields up to 35 T. It is important to note the large FS cross-sectional areas computed for the \([L1/S2]\) superlattice (5.43 nm\(^2\) for the smallest FS) and the \([L1/S6]\) superlattice (5.84 and 0.76 nm\(^2\) for the two smallest FS). (FS areas were computed as circles with a radius along the \( \Gamma-M \) direction.) These FS areas are much larger than the previously reported experimental values for Nb \( \delta \)-doped STO (0.36 nm\(^2\)\(^{29} \)) and La-doped STO thin films (0.26 nm\(^2\)\(^{30,31} \)) and are in fact on the order of the FS cross-sectional areas found in \( \text{YBa}_2\text{Cu}_3\text{O}_{6.5} \) (5.1 nm\(^2\)\(^{32,33} \)). Of course, as the \([L1/S6]\) superlattice includes some smaller FS areas that are on the order of those in Nb/La-doped STO, we should expect to observe SdH oscillations in these samples. However, we believe that the contributions from the larger FS may suppress the SdH oscillations. This large FS size suggests that it may be only possible to observe angle-dependent SdH oscillations in our superlattices at much higher magnetic fields.

Naturally, localization effects are crucial to defining the mobility of electrons at oxide heterointerfaces. Tight-binding simulations show that at disymmetric interfaces there is a strong reduction of the in-plane hopping amplitude of the \( d_{xz} \) and \( d_{yz} \) orbitals\(^{24,25} \), driving the \( d_{xy} \) orbital ordering. Thus, the \( d_{xy} \) orbitals become extremely localized; severely limiting electron mobility in these orbitals. In the two carrier model, the latter states have a high density, but low mobility (HDLM; \( n_s = 0.4 \times 1 \times 10^{16} \) cm\(^{-2}\) and \( \mu = 10 \times 50 \) cm\(^2\)V\(^{-1}\)s\(^{-1}\) at 2 K) while carriers in the \( d_{xz} \) and \( d_{yz} \) orbitals have low densities but high carrier mobilities (LDHM; \( n_s = 0.2 \times 1 \times 10^{16} \) cm\(^{-2}\) and \( \mu = 1 \times 5000 \) cm\(^2\)V\(^{-1}\)s\(^{-1}\) at 2 K).\(^{24} \)

To better understand the effects of delocalization due to enhanced wavefunction overlap, we compute the fractional occupation, \( f \), of the \( d_{xz/yz} \) vs. \( d_{xy} \) orbitals:

\[
f = \frac{n_{xz} + n_{yz}}{n_{xz} + n_{yz} + n_{xy}}
\]

where \( n_i \) (\( i = \text{xx}, \text{yy}, \text{or xy} \)) is the number of electrons in the \( d_{xz}, d_{yz} \) or \( d_{xy} \) orbital, respectively. As depicted in Figure 5, it is clear that the reduction in STO thickness results in a substantial increase in the relative fraction of \( d_{xz/yz} \) orbitals at the heterostructure interface. Assuming that these states remain mostly delocalized, this would suggest higher mobility at these interfaces. Similar effects are likely the cause of the anomalous enhancement in mobilities in the previously studied \( \delta \)-doped oxide superlattices.\(^{24} \) Interestingly, we find that the number of \( d_{xy} \) electrons, \( n_{xy} \), at the interface remains constant in the \([L1/S2]\) and \([L1/S6]\) superlattices (See Supplementary Information Figure S2), and the large change in fractional occupation at the interface is a consequence of an increase in \( d_{xz} \) and \( d_{yz} \) populations.\(^{24} \)

Commensurate with these changes in the relative populations of the \( d_{xz/yz} \) orbitals, we observe significant differences in the off-center displacements relative to their nearest neighbor oxygen octahedral cage, \( \Delta z \), of Ti cations; with the \([L1/S6]\) superlattices exhibiting larger off-centering than the \([L1/S2]\) superlattices. Off-centering is known to be coupled to a larger distribution in electron densities away from the interface. We find that if the off-center displacements in the \([L1/S6]\) superlattice are manually reduced to that of the \([L1/S2]\) superlattice (Figure 5b; reduced \( \Delta z \)) there is a \( \sim 50\% \) increase in the relative populations of the \( d_{xz/yz} \) orbitals. This increase in relative populations is even more dramatic when the off-center displacements are completely eliminated (Figure 5b; \( \Delta z = 0 \)). Again,

we find that the number of \( d_{xy} \) carriers remains relatively constant, while the excess electrons at the interface now occupy the previously low-density \( d_{xz/yz} \) orbitals.

These results emphasize the role of the confinement of electrons near the interface, which results in the population of the high-mobility carriers, \( d_{xz/yz} \) carrier. Furthermore, the fact that the \([L1/S2]\) superlattice has a smaller displacement and a larger carrier density suggests that electronic screening may play a substantial role in the \([L1/S2]\) superlattice; with the superlattice having a smaller effective dielectric constant than that of the \([L1/S6]\) superlattice. Similar results were obtained using model Hamiltonian studies\(^{33,34} \) and hypothesized as the origin of the predicted difference in the distribution of electrons in the \( \delta \)-doped \( \text{KTaO}_3 \) and \( \text{KNbO}_3 \) systems.\(^{25} \) It should be noted that the overall mobility at the interface may be affected by other factors such as carrier interactions at the interface and interface scattering. Nevertheless, the interconnection of the high mobility 2DEGs generated by the interfacial electronic reconstruction and changes in the effective dielectric constant at these interfaces may provide an unprecedented pathway for designing a new class of highly metallic, transparent conducting oxides.

**Summary**

We have investigated the dimensional nature of carrier distribution and optical transport in electronically-reconstructed interfaces via DFT calculations. It has been found that there is a dimensional crossover of carrier conduction from 2D to 3D with a critical STO thickness of \( \sim 2–3 \) nm in thickness. This dimensional crossover is attributed to a significant overlap of quantum mechanical wavefunctions inside the STO matrix when the distance between neighboring conducting layers is thin enough, implying that the wavefunction of oxide superlattices might be engineered by means of structural modifications, dielectric property, and electric field. Even more striking, the electronically reconstructed metallic interfaces uniquely transmit visible light offering a new mechanism for developing transparent conducting films. In essence, by decoupling the dopants from the optically transparent layers it is possible to retain the favorable band gap of STO without introducing in gap states. Considering these unique properties such as tunable electronic wavefunctions and optical transparency, the oxide superlattice is promising for the development of novel optoelectronic devices where the interactions between photons and electrons are critical to the functional behavior of these materials.
Methods
All DFT calculations were performed using ultrasoft pseudopotentials with the local density approximation (LDA) for exchange and correlation as implemented in the QUANTUM ESPRESSO\textsuperscript{a} simulation code. LTO/STO [Li/Sr] superlattices (where \( n = 2, 6 \) and 10) were studied employing a 500 eV cutoff and a \( 16 \times 16 \times 1 \) Monkhorst-Pack \( k \)-point mesh with 1 \( \times \) 1 unit cell in-plane periodicity. In all calculations, the in-plane lattice constants were constrained to the theoretical value of STO (3.863 Å) and the out-of-plane, \( c \), lattice vector was optimized within the \( \text{Pmnnm} \) space group.

Simultaneously, all ionic coordinates were relaxed until all Hellman-Feynman forces were less than 5 meV/Å. Note that the cubic STO lattice constant was obtained using standard LDA, i.e. without the inclusion of a Hubbard \( U \) (Ref. 36) and is in typical LDA agreement with the experimental value of 3.901 Å. For all heterostructure calculations, a Hubbard \( U = 5 \) eV for Ti 3d-states was found to be appropriate. Similar \( U \) values have been used in previous studies of LTO/STO\textsuperscript{36,37} and have been shown to give a reasonable description of the electronic and structural rearrangements that occur in these materials.

La \( \delta \)-doped STO superlattices were grown on TiO\textsubscript{2}-terminated \( (001) \) STO single crystal substrates by PLD (KrF, \( \lambda = 248 \) nm) using polycrystalline \( La_xTi_1-xO_2 \) and single crystalline STO targets. The thickness of each layer was monitored \( \text{in-situ} \) by reflection high-energy electron diffraction (RHEED). During the growth of STO, we inserted one u.c. LTO with various thicknesses of STO spacers ranging from 2 to 10 u.c., resulting in La \( \delta \)-doped STO superlattices. The total thickness of superlattices ranged from 30–60 nm. Detailed growth conditions and structural properties can be found elsewhere\textsuperscript{38}. Quantum transport properties of the superlattices were investigated at temperatures down to 25 mK and magnetic fields up to 35 T. Under these conditions no noticeable quantum oscillations were observed.

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Author contributions
V.R.C. performed the DFT calculations. V.R.C. and S.O. analyzed the theoretical results. S.L. performed the quantum transport measurements and data analysis at ORNL S.S.A.S. carried out optical characterization and analysis. J.S.K. and W.S.C. assisted with measurements and analysis of the dc transport and optical properties. H.N.L. designed the project, coordinated the work, and assisted with sample synthesis and analysis. All authors participated in discussions and manuscript writing.

Additional information
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