Multiangle static and dynamic light scattering in the intermediate scattering angle range

Elisa Tamborini, Luca Cipelletti

To cite this version:

Elisa Tamborini, Luca Cipelletti. Multiangle static and dynamic light scattering in the intermediate scattering angle range. Review of Scientific Instruments, American Institute of Physics, 2012, 83 (9), pp.093106. 10.1063/1.4751864. hal-00725045

HAL Id: hal-00725045
https://hal.archives-ouvertes.fr/hal-00725045
Submitted on 23 Aug 2012

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Multiangle static and dynamic light scattering in the intermediate scattering angle range

E. Tamborini\textsuperscript{1,2,}\textsuperscript{a) and L. Cipelletti\textsuperscript{1,2}

\textsuperscript{1) Université Montpellier 2, Laboratoire Charles Coulomb UMR 5221, F-34095, Montpellier, France
\textsuperscript{2) CNRS, Laboratoire Charles Coulomb UMR 5221, F-34095, Montpellier, France

(Dated: 23 August 2012)

We describe a light scattering apparatus based on a novel optical scheme covering the scattering angle range 0.5 deg \(\leq \theta \leq 25\) deg, an intermediate regime at the frontier between wide angle and small angle setups that is difficult to access by existing instruments. Our apparatus uses standard, readily available optomechanical components. Thanks to the use of a charge-coupled device detector, both static and dynamic light scattering can be performed simultaneously at several scattering angles. We demonstrate the capabilities of our apparatus by measuring the scattering profile of a variety of samples and the Brownian dynamics of a dilute colloidal suspension.

PACS numbers: 07.60.-j,42.15.Eq, 42.30.Kq

Keywords: static light scattering, dynamic light scattering, CCD

I. INTRODUCTION

Light scattering methods are a powerful tool for investigating the structure and the dynamics of soft and biological matter. The typical space and time scales that are probed range from tens of nanometers to tens of microns, and from a fraction of a microsecond to several hours, respectively. Typical applications include particle sizing, the characterization of aggregation phenomena, the determination of interparticle interactions, the investigation of the structure and the relaxation dynamics of complex fluids. The diversity of systems that can be studied makes the technique appealing for both academic laboratories and industry: suspensions of colloidal particles or emulsions, solutions of polymers and proteins, foams, and surfactant phases are but a few examples of such systems.

Scattering methods may be divided in two classes: static and dynamic light scattering. In static light scattering (SLS)\textsuperscript{1}, one probes the structure of a sample by measuring the time-averaged scattered intensity as a function of the scattering angle. By contrast, dynamic light scattering (DLS)\textsuperscript{2} focuses on the temporal fluctuations of the scattered intensity in order to extract valuable information on the sample dynamics. In both cases, the sample is typically illuminated by a laser beam, while photodiodes, avalanche photodiodes, photomultiplier tubes or CCD or CMOS cameras are used as a detector.

A wide variety of light scattering apparatuses have been developed, many of which are commercially available. The design of a setup is in general optimized according to the range of scattering angles to be covered and the kind of measurements to be performed (static or dynamic). Wide-angle light scattering (WALS) setups often provide both SLS and DLS measurements, covering approximately the range 10 deg \(\leq \theta \leq 180\) deg, corresponding to length scales of order \(2\pi^{-1}\) ranging from 0.2 \(\mu m\) to 2.3 \(\mu m\). Here \(q = 4\pi n \lambda^{-1} \sin(\theta/2)\) is the scattering vector, with \(n\) the solvent refractive index, \(\lambda\) the in-vacuo laser wavelength and \(\theta\) the scattering angle. However, it should be noted that in practice it is difficult to obtain reliable data below \(\theta = 20\) deg, because the cylindrical sample geometry that it is usually adopted in WALS limits the quality of the optical interfaces. Small-angle and ultra-small-angle light scattering setups (SALS and USALS, respectively) are specialized for measurements close to the forward direction, with scattering angles covering up to two decades, up to approximately 10 deg for SALS and a few degrees for USALS. The corresponding length scales vary between a few microns and tens or even hundreds of microns. While some of these setups use dedicated photodiode detectors optimized for SLS but unfit for DLS\textsuperscript{3–6}, the adoption of a CCD or CMOS detector is increasingly popular, since it allows for both static and dynamic light scattering to be performed\textsuperscript{7,8}, as first shown by the pioneering work of Wong and Wiltzius\textsuperscript{7}.

It should be noted that there is little if any overlap between the range of scattering angles of typical WALS and SALS or USALS setups: this leaves uncovered a crucial angular range corresponding to probed length scales on the order of a micron, the characteristic size of many colloidal objects of industrial and fundamental science interest. Additionally, absolute intensity measurements are notoriously difficult in light scattering, especially for SALS or USALS, thus making it difficult to merge data from different setups on the same scale. To circumvent this problem, a few apparatuses covering the “mid-angle” range (mid-angle light scattering, MALS) have been proposed in the past. The apparatus described in Ref.\textsuperscript{4} covers an impressive angular range (2 deg –60 deg), using

\textsuperscript{a)Electronic mail: elisa.tamborini@univ-montp2.fr}
a custom made cell and dedicated photodiode arrays and electronics. Ferri and coworkers report a setup covering scattering angles up to 15 deg\(^{5,6}\), using a commercially available cell but again a custom photodiode array with dedicated electronics. A different approach is used in the commercially available apparatus of Ref.\(^9\), which covers scattering angles from a fraction of degree up to about 40 deg by varying the propagation direction of the incident beam. Accordingly, several distinct measurements are required to sample the full angular range, each measurement covering about 5 deg. Chou and Hong\(^{10}\) report a CCD-based setup in the range 2 deg < \(\theta\) < 25 deg using a scheme originally proposed by Ferri for a CCD-based SALS\(^{3}\). Unfortunately, however, no detailed description and characterization of the apparatus performances are provided. Finally, one may take advantage of the good-quality optics of modern microscopes to build an apparatus that combines imaging with low- or mid-angle scattering. Kaplan et al.\(^{11}\) report a DLS apparatus based on an inverted microscope that covers scattering angles between 20.6 deg and 55.1 deg, while Celli et al.\(^{12}\) demonstrate DLS in a upright microscope for \(\theta\) \(\leq\) 12 deg. In both cases, measurements are performed at one single angle at a time. In Ref.\(^{13}\), a microscope- and CCD-based static light scattering instrument is presented, covering the range 0.9 \(\mu\)m \(\leq\) \(q\) \(\leq\) 18 \(\mu\)m, corresponding approximately to 3.3 deg \(\leq\) \(\theta\) \(\leq\) 70 deg.

With the exception of the setups of Refs.\(^{10,13}\) that could in principle be extended to DLS, these apparatuses are unfit for simultaneous static and dynamic light scattering at multiple angles, either because the angular range is sampled sequentially, as in Refs.\(^{9,11,12}\), or because photodiodes that cover a very large number of speckles are used, as in Refs.\(^4-6\), a design not appropriate for DLS\(^2\). It is worth noting that photodiode arrays are typically larger than CCD or CMOS detectors: this makes it difficult to transpose the optical layout of Refs.\(^4-6\) to a CCD-based apparatus and would impose extra constraints on the cell dimensions, in particular its thickness \(L\), as we shall discuss in the following. Additionally, photodiode arrays can easily accommodate a small hole to let through the transmitted beam, a crucial requirement for small angle measurements, while this is not possible for a CCD or CMOS detector. Thus, existing designs for MALS cannot be easily generalized to an apparatus for both SLS and DLS.

In this paper, we present a CCD-based mid-angle light scattering apparatus that covers the intermediate range 0.5 deg \(\leq\) \(\theta\) \(\leq\) 25 deg thanks to a novel optical layout. Our MALS setup allows for simultaneous measurements at all accessible scattering angles. Both SLS and DLS measurements can be performed and no stringent limitations on the sample thickness are imposed. Finally, the setup uses only standard components that are readily available off the shelf. The rest of the paper is organized as follows. To better understand the difficulties in extending the angular range of SALS or USALS setups to larger angles, we review some of the most popular optical layouts in Sec. II. We then present our new MALS apparatus in Sec. III, before describing its angular calibration in Sec. V. A series of tests of the apparatus’ performances for both SLS and DLS are presented in Sec. VI, before the concluding remarks of Sec. VII.

II. POPULAR OPTICAL LAYOUTS FOR SALS AND USALS

Most MALS setups are based on the same optical layout as that for SALS and USALS, examples of which are shown in Fig. 1. In the top scheme, Fig. 1a, adopted in Refs.\(^4,9,14,15\), the scattered intensity is measured in the focal plane \(\Sigma\) of a so-called Fourier lens of focal length \(f\). Neglecting refractions at the solvent-cell and cell-air interfaces, a point on \(\Sigma\) at a distance \(r\) from the optical axis corresponds to a scattering angle \(\theta = \arctan(r/f^{1-1})\). In order to avoid artifacts due to light leaking from the intense transmitted beam, a hole may be drilled in the detector to let the transmitted beam pass through \(\Sigma^{4,6,14,15}\). Alternatively, a screen may be placed in the plane \(\Sigma\) and a CCD camera may be used to record the intensity distribution on the screen. In both cases, this geometry prevents a CCD camera to be placed directly in the plane \(\Sigma\), making DLS measurements impossible. In addition, detectors and lenses used in this configuration must often be custom-made to efficiently remove the transmitted beam and to limit aberrations associated with large scattering angles. The scheme of Fig. 1b, described in Refs.\(^5,6\), is equivalent to the top one, provided that one replaces \(f\) by the sample-detector distance \(d_s\) in the calculation of \(\theta^{16}\). The advantage is that large scattering angles may be attained simply by reducing \(d_s\), without changing \(f\) and with no stringent requirements on the numerical aperture of the Fourier lens. However, the sample thickness \(L\) must satisfy \(L << d_s\), since the mapping between \(r\) and \(\theta\) depends on the distance of a scatterer from \(\Sigma\). When using a CCD detector, typical values of \(d_s\) are a few cm at most, limiting \(L\) to about 1 mm. Additionally, the remarks on removing the transmitted beam discussed for the top scheme apply also here. Thus, the middle scheme is limited to SLS measurement on thin samples. The scheme of Fig. 1c was proposed by Ferri for a CCD-based SALS apparatus\(^3\) and extended to larger angles by Chou and Hong\(^{10}\) and to DLS by Cipelletti and Weitz\(^2\). It is similar to the top scheme, except that a beam block is placed in \(\Sigma\) and a second lens is used to image the intensity distribution in the Fourier plane onto a CCD. This scheme can not be easily extended to MALS because the numerical aperture of commercially available lenses limits in practice the maximum scattering angle to about 15 deg, beyond which vignetting sets in.
part is formed by the two pairs of lenses

Functionally, it may be divided into two parts. The first

centers around the transmitted beam position.

light scattered at a given angle

aperture of the various elements, we use pairs of identi-

fication. In order to increase the numerical

components and of their position are provided in the Supple-

tails of the various optical and opto-mechanical compo-

III. THE MALS SETUP

A scheme of our MALS setup is shown in Fig. 2. De-

tails of the various optical and opto-mechanical compo-

ments and of their position are provided in the Supple-

mentary Information. In order to increase the numerical

aperture of the various elements, we use pairs of identi-

cal lenses placed in contact, for which the effective focal

length is half of that of each lens, thereby doubling the

numerical aperture. The apparatus maps the cone of

light scattered at a given angle $\theta$ onto a ring of CCD

pixels centered around the transmitted beam position.

Functionally, it may be divided into two parts. The first

part is formed by the two pairs of lenses $L_{1a}, L_{1b}$ and

$L_{2a}, L_{2b}$, which are confocal and act as an (inverted) tele-

scope. Their purpose is two-fold: on the one hand, they

demagnify the angle of the light scattered by the sam-

ple, thus mapping the MALS range to a more manage-

able, lower-angle range. On the other hand, a beam stop

can be conveniently placed in the focal plane $\Sigma$ common

to both pairs, thereby removing the transmitted beam.

The second part comprises the pair of lenses $L_{3a}, L_{3b}$

that act as a Fourier lens, in whose back focal plane a

CCD detector is placed. The focal length of the various

lenses is $f_{1a} = f_{1b} = 62.9$ mm, $f_{2a} = f_{2b} = 150$ mm

and $f_{3a} = f_{3b} = 75.6$ mm. The resulting demagnifica-

tion ratio of the inverted telescope is $f_{2a}/f_{1a} \approx 2.4:1$.

In order to cover the MALS range, we use plano-convex

lenses and work well beyond paraxial propagation; there-

fore, the thin lens approximation does not apply. We use

a ray-tracing software (Optical Ray Tracer 2.817) to test

the performances of the real lenses and to fine tune the

position of the sample and that of the third pair of lenses.

To avoid vignetting, the sample must be close enough to

$L_{1a}$, while a minimum distance of about 5 mm is im-

posed by the thickness of the cell wall and the sample

and lens holder. Using the ray-tracing software, we de-

termine the optimum sample-$L_{1a}$ and $L_{3b}$-CCD distances

to be 17 mm and 30 mm, respectively. With this layout,

the maximum relative spread of the spot formed on the

CCD plane by light scattered at the same $\theta$ is 1.7%, for

$\theta = 25^\circ$ and a 10 mm thick sample.

The light source is an intensity-stabilized, linearly po-

larized He-Ne laser (117A by Spectra-Physics) that op-

erates at a wavelength $\lambda = 632.8$ nm, and at a power

of 1.0 mW. The laser beam is coupled to a polarization-

maintaining single-mode fiber optics (LPC-04-633-4/125-

P-0.9-4.5AS-60-A3A-3A-2 by OZ Optics), through which

only the TEM$_{00}$ mode can propagate. A set screw is used

to partially block the beam before coupling it to the fiber,

so that the beam power can be attenuated as required. The

beam exiting the fiber is collimated to a diameter of

0.9 mm and it is directed on a beam splitter (BS) that

partially forwards it onto a photodiode (PDM), which

monitors any fluctuations in the incident power for fur-

ther data normalization. The transmitted component im-

pings onto the sample, which is typically contained in a

parallelepiped cell of thickness 2, 5 or 10 mm (Hellma).

A small mirror M is placed in the focal plane $\Sigma$ to intercep-

t the transmitted beam and direct it to a second photo-

diode (PDT), allowing for the measurement of the sam-

ple transmission and preventing unscattered light from

reaching the CCD sensor. Following Ref. 3, the mirror is

obtained by cutting at 45 deg and polishing a drill bit of

thickness 300 $\mu$m. To minimize light reflections, all lenses

are antireflection coated and are tilted by a few degrees

with respect to the optical axis. The same precaution is

taken for the scattering cell. The cell is mounted on a

custom-designed holder that allows one to vary both its

height with respect to the optical axis and its distance

from $L_{1a}$. The cell can be removed from the holder and

replaced exactly at the same position, i.e. for taking an

optical background as described later. The CCD camera

(Pulnix TM-1300) has a pixel matrix of 1285 $\times$ 1029 pix-

els, 6.7 $\mu$m in size. A frame grabber (Meteor II Digital

PCI by Matrox) is used to control the camera and trans-

fer the images to a PC. The whole instrument is placed

under a box made of high density expanded polystyrene

panels, to minimize temperature fluctuations and to pro-

tect the setup from ambient light.

IV. DATA ACQUISITION AND PROCESSING

We use a custom C++ code to process the CCD images

in real time, in order to perform both static and dynamic

light scattering measurements.
FIG. 2. The Mid-Angle Light Scattering apparatus described in this paper. The two pairs of lenses $L_{1a}$, $L_{1b}$ and $L_{2a}$, $L_{2b}$ are confocal and act as an (inverted) telescope. The beam stop $M$ is placed in their common focal plane $\Sigma$ to remove the transmitted beam. The pair of lenses $L_{3a}$, $L_{3b}$ acts as a Fourier lens and the CCD detector is placed in its back focal plane. OF: optical fiber; BS: beam splitter; PDM, PDT: monitor and transmitted photodiode, respectively; PC: personal computer. The optical elements are drawn in scale, the cell-CCD distance is 28.8 cm.

A. Static Light Scattering

Data acquisition and processing for SLS involves four steps: i) acquisition of the electrical background, ii) acquisition of the optical background, iii) acquisition of the scattered intensity pattern, iv) applying to iii) corrections for the contribution of i), ii) and geometrical factors in order to obtain the scattered intensity profile $I(q)$. During step i), the laser beam is blocked so as to measure the contribution of the electrical background to the signal. The signals of the monitor and transmitted photodiodes, $M^{\text{EB}}$ and $T^{\text{EB}}$, are averaged over 100 readings and recorded. Similarly, a series of CCD images taken at various exposure times $t_{\text{exp}}$ are recorded, about 20 images being averaged for each $t_{\text{exp}}$. The images are processed in order to calculate the dark background averaged over annuli of pixels centered around the transmitted beam position: $S^{\text{EB}}(q, t_{\text{exp}}) = \langle S^{\text{EB}}_p(t_{\text{exp}}) \rangle_{p \in A_q}$, where $S^{\text{EB}}_p(t_{\text{exp}})$ is the CCD electrical background signal for the $p$–th pixel at a given exposure time and $\langle \cdots \rangle_{p \in A_q}$ indicates an average over the annulus of pixels associated with a given $q$ vector. Pixels that are covered by the beam block are software-masked and excluded from the analysis. The purpose of step ii) is to measure any contributions to the scattered light due to environmental factors that could be repeated, (e.g. for samples that need to undergo a controlled thermal history, as in Ref. 18), we use a custom-designed holder that allows the cell to be removed and replaced with a positioning tolerance of about 10 $\mu$m. During step iii), the intensity scattered by the sample at time $t$ is recorded, together with the corresponding photodiode signals: $S(q, t_{\text{exp}}, t)$, $M(t)$ and $T(t)$. In order to reduce noise, a few images for each $t_{\text{exp}}$ may be averaged. Depending on the number of averages and that of the exposure times, one full acquisition may require as little as 0.1 sec. Note that the use of different exposure times is often mandatory, given the limited dynamic range of CCD detectors and the steep variation of $I(q)$ typically observed over the MALS range. Data stored in steps i) to iii) are processed in real time in order to calculate the $q$ dependent scattering intensity according to

$$I(q, t) = \frac{1}{LN(q)t_{\text{exp}}(M(t) - M^{\text{EB}})} \left\{ S(q, t_{\text{exp}}^*, t) - S^{\text{EB}}(q, t_{\text{exp}}^*) - \frac{T(t) - T^{\text{EB}}}{T^{\text{OB}} - T^{\text{EB}}} \left[ S^{\text{OB}}(q, t_{\text{exp}}) - S^{\text{EB}}(q, t_{\text{exp}}^*) \right] \right\}. \quad (1)$$

In the above equation, all optical signals are corrected for the corresponding electrical background and normalized with respect to the incident power as measured by the monitor photodiode. Before subtracting the optical background (the term between square brackets in the r.h.s. of Eq. (1)), we correct it for the sample transmission, $(T(t) - T^{\text{EB}})/(T^{\text{OB}} - T^{\text{EB}})$, because the flare contribution is decreased when part of the incident beam is scattered by the sample. In Eq. (1), $t_{\text{exp}}^*$ is the best exposure time for a given $q$, allowing for a good signal to noise ratio while preventing pixel saturation. We find that for a 8-bit CCD $t_{\text{exp}}^*$ should be chosen as the largest...
exposure time such that \( S(q, t_{\text{exp}}^*) \lesssim 40 \) grey levels. For larger values, the number of saturated pixels becomes non-negligible, while for smaller values data are affected by digitalization noise. Note that the intensity is normalized with respect to cell thickness \( L \) and exposure time \( t_{\text{exp}}^* \), and by the term \( N(q) \), which accounts for the average value of the solid angle associated to each pixel of a given annulus, as well as for the dipole term \( \sin^2 \psi_p \) that decreases the scattered intensity out of the scattering plane\(^2\), where \( \psi_p \) is the angle between the polarization of the incident light and the propagation direction of the scattered light that reaches the \( p \)-th pixel. More specifically, \( N(q) = \frac{\Delta \Omega_p \sin^2 \psi_p}{> \sin \theta_p} \Delta \psi_p \), with \( \Delta \Omega_p = \sin \theta_p \Delta \theta_p \Delta \varphi_p \) the solid angle, \( \sin^2 \psi_p = 1 - \sin^2 \varphi_p \sin^2 \theta_p \) the dipole factor, \( \theta_p \) the scattering (polar) angle, and \( \varphi_p \) the azimuthal angle. For a pixel \( p \) with coordinates \((x, y)\) with respect to the transmitted beam position one has

\[
\Delta \theta_p = \frac{1}{r} (x \Delta x + y \Delta y) \frac{d \theta_p}{dr}, \quad (2a)
\]

\[
\Delta \varphi_p = \frac{d \varphi_p}{dx} \Delta x + \frac{d \varphi_p}{dy} \Delta y, \quad (2b)
\]

with \( r = \sqrt{x^2 + y^2} \), \( \varphi_p = \arctan(y/x) \), and \( \Delta x \) and \( \Delta y \) the pixel dimensions. The functional form relating \( \theta_p \) to \( r \) and from which the term \( \frac{d \theta_p}{dr} \) can be calculated will be discussed in Sec. V.

### B. Dynamic Light Scattering

The same four steps discussed in the previous subsection are also required for DLS measurements, although of course the data processing in step iv) is different. We use a software multi-tau correlator\(^8\), whose details are discussed in Ref.\(^8\); together with the algorithm for correcting for the electrical and optical background. Here, we simply recall that the correlator calculates in real time the autocorrelation function of the CCD signal,

\[
\langle S_p(t)S_p(t + \tau) \rangle_{\psi, \psi', \theta, \theta', \varphi, \varphi', \Delta \theta, \Delta \varphi}.
\]

After correction for the electrical and optical backgrounds and proper normalization, using the Siegert relation\(^2\) one obtains the field autocorrelation function

\[
g_1(q, \tau) = \frac{\langle E(q, t)E^*(q, t + \tau) \rangle_{\psi, \psi', \theta, \theta', \varphi, \varphi', \Delta \theta, \Delta \varphi}}{\langle I(q, t) \rangle_{\psi, \psi', \theta, \theta', \varphi, \varphi', \Delta \theta, \Delta \varphi}}, \quad (3)
\]

which is directly related to the sample dynamics\(^2\).

### V. ANGULAR CALIBRATION

With the optical layout of Fig. 2 and in the thin lens and paraxial approximations, the relationship between the scattering angle \( \theta \) and the distance \( r \) from the optical axis of a CCD pixel is

\[
\sin \theta = r (r^2 + f_{\text{eff}}^2)^{-0.5}, \quad (4)
\]

where \( f_{\text{eff}} = f_{3a}/2a / (2f_{1a}) \approx 15.9 \) mm is the effective focal length of the Fourier lens, which accounts for both the use of pairs of lenses and the demagnification of the inverted telescope. Note that for the moment we have neglected refraction, assuming that the scatterers are in air. Since deviations are to be expected with respect to this simple formula, we perform an angular calibration of the setup using a diffraction ruling with \( m = 1000 \) lines cm\(^{-1}\). The diffraction grating is positioned perpendicularly to the incident beam, so that the maxima of the diffracted beam occur at angles such that \( \sin \theta_k = mk/\lambda \), \( k = 0, \pm 1, \pm 2, \ldots \). We vary the distance \( d \) between the diffraction grating and \( L_{1a} \) between 14 and 23 mm in steps of 1 mm and for each \( d \) we measure the position \( r \) of the maxima on the CCD sensor. The results are shown in Fig. 3. The highest order observable is \( k = 7 \), corresponding to \( \theta_k = 26.3 \) deg, which we achieve by offsetting the CCD with respect to the optical axis, such that the transmitted beam impinges near one corner of the detector, rather than in its center. The distance \( d \) for which the maxima appear to be sharper is found to be 18 mm, close to \( d = 17 \) mm as evaluated using the ray-tracing software. Thus, thick samples are always positioned such that the cell center is at 18 mm from the first lens. Figure 3 shows that \( \sin \theta_k \) varies approximately linearly with \( r \), as expected from Eq. (4) given that \( f_{\text{eff}}^2 >> r^2 \). However, deviations are observed at large \( r \); more importantly, these deviations depend on \( d \), implying that lens aberrations limit the angular res-
solution of the setup for samples of finite thickness. To quantify these effects, we fit for each \( d \) the data of Fig. 3 using the empirical relation

\[
sin \theta_k = ar + \frac{1}{b - r} - \frac{1}{b},
\]

with \( a \) and \( b \) \( d \)-dependent fitting parameters and where \( r \) is measured in mm. As seen in Fig. 3, this expression is in excellent agreement with the data. For samples of finite thickness and for a solvent of refractive index \( n \), we define the scattering angle associated to a pixel \( p \) laying at a distance \( r \) from the optical axis as

\[
\theta_p = \arcsin \left( \frac{1}{n} \left( \tilde{a}r + \frac{1}{b - r} - \frac{1}{b} \right) \right),
\]

where the \( n^{-1} \) factor accounts for refraction at the solvent-wall and wall-air interfaces and where \( \tilde{a} \) and \( b \) are the average of the fitting parameters \( a \) and \( b \) over the range of \( d \) corresponding to the sample thickness. For a 10 mm-thick cell, we find \( \tilde{a}^{-1} = 17.27 \) mm, about 8.6% larger than \( f_{aq} \) as calculated neglecting aberrations. The \( q \) vector associated with an annular set of pixels is obtained by averaging the corresponding value for each pixel of the annulus:

\[
q = \frac{4\pi n}{\lambda} \left( \sin \left( \frac{\theta_p}{2} \right) \right)_{p \in A_q}
\]

with \( \theta_p \) as obtained from Eq. (6).

The inset of Fig. 3 quantifies the loss of angular resolution due to sample thickness by showing the relative standard deviation of \( \theta \), \( \sigma_q/\theta \), associated with the standard deviation of the coefficients \( a \) and \( b \) over the range of \( d \) corresponding to representative values of the cell thickness \( L \). For \( L \leq 5 \) mm, the relative angular spread is well below 1% over the full range covered by the setup, while for a 10 mm-thick cell, the loss of angular resolution is about 4% at the largest \( \theta \).

VI. TESTS OF THE APPARATUS PERFORMANCES

We perform a series of experiments to validate the angular calibration determined in Sec. V, determine the angular response of the apparatus and to test its performances for DLS.

A. Static light scattering

Static light scattering tests were performed on representative 2-dimensional and 3-dimensional samples. For all samples, \( I(q) \) was measured for pixel annuli whose average radius ranged from 29 pixels to 1279 pixels, for a total of 126 values equally spaced in a linear scale. The thickness of the annuli is 1 pixel. To cope with the large variation of the scattered intensity over the range covered by the instrument, eighteen exposure times have been used, from 0.08 ms to 80 ms, with a scaling factor of 1.5 between one exposure time and the next one.

To verify the \( q \) calibration and to check for the angular response of the apparatus, we measure the diffraction pattern of a pinhole with a nominal diameter of 10 \( \mu m \) measured for ten values of the sample-\( L_{1a} \) distance \( d \). In the inset, the discrepancy in the \( q \)-calibration and the intensity level for the ten distances at high \( q \) vectors are visible. An image of the pinhole taken with an optical microscope is also shown.

![Diffraction pattern of a pinhole with a nominal diameter of 10 \( \mu m \).](Image)
FIG. 5. Scattering from a ground glass positioned at distances $d$ varying between 14 mm and 23 mm. The inset shows the ratio of the measured intensity with respect to that recorded for $d = 18$ mm, corresponding to the optimum sample-$L_{\text{in}}$ distance.

to the other curves, while it is systematically higher for $d \geq 21$ mm, confirming the trend observed for the pinhole. For $d = 23$ mm an anomalous increment in the intensity profile is visible at $q = 4.6$ µm$^{-1}$ and the same happens at higher $q$ vector for smaller distances. This extra-signal is due to aberrations affecting rays scattered at high $q$ vectors and impinging close to the lens edge. The ray-tracing software shows that these rays are systematically bent towards the optical axis, resulting in a spurious increase of the measured $I(q)$. At even larger $q$, the intensity decreases steeply because of vignetting. To quantify the discrepancy between the ten intensity distributions, the ratio between each curve and the intensity profile measured for $d = 18$ mm is shown in the inset of Fig. 5. If we consider the five distances between 16 mm and 20 mm, the ratio varies between 0.87 and 1.07 (horizontal black lines in the inset), and the maximum accessible scattering vector is 5 µm$^{-1}$. Thus, the response of the instrument for a 5 mm thick sample centred in $d = 18$ mm is flat to within $\pm 10\%$. If we consider the two distances 18 mm and 19 mm (corresponding to a 2 mm-thick sample) the ratio deviates from 1 by less than 5% and the maximum accessible $q$ vector is 5.2 µm$^{-1}$.

We test the setup performances on a typical 3-dimensional sample by measuring the scattering from a suspension of poly(methyl methacrylate)(PMMA) spheres with an average diameter of 2.09 µm and relative polydispersity of 2.5%, as obtained from transmission electron microscopy (TEM). The particles are sterically stabilized by a thin layer of chemically grafted poly-12-hydroxystearic acid (PHSA), and are suspended in a mixture of decalin and tetralin (0.676/0.324 v/v at 20°C). The measurements have been performed at 26.5°C; at this temperature the solvent refractive index is 1.492 and the PMMA refractive index is $n_{\text{PMMA}} \approx 1.501$, as estimated by preparing samples in slightly different decalin/tetralin mixtures and by taking $n_{\text{PMMA}}$ as the refractive index of the solvent for which the scattered intensity is minimal. The suspension was filtered through a 5 µm PTFE membrane and then placed in two cells of thickness 5 mm and 2 mm, respectively. In the first case, the sample volume fraction was $\varphi = 0.2\%$ while for the thinner cell it was $\varphi = 0.4\%$. Fig. 6 shows the intensity distributions measured for the two samples. Data have been rescaled so that $I(q \to 0) = 1$. The line is the form factor from the Mie theory$^4$ applied to polydisperse spheres, calculated using the MiePlot software$^{20}$, for the size distribution obtained by TEM. The agreement between the data and the theory is very good up to 4 µm$^{-1}$. At higher $q$, the intensity distribution is systematically larger than the theoretical curve. This discrepancy is unlikely to stem mainly from a non-uniform angular response of the setup, since the tests with the pinhole and the ground glass suggest that deviations should compensate once integrated over the thickness of the sample. Other possible explanations include deviations from a perfectly spherical particle shape (as observed in the TEM images), scattering from the PHHS corona that may become non-negligible when matching closely the PMMA refractive index, and multiple scattering. Concerning the latter point, we note that although the suspension transmission was very high (90%), even modest amounts of multiple scattering would tend to increase $I(q)$ in those angular ranges where the signal is markedly lower than for nearby $q$ vectors, as observed here.

To further test the angular response of the instrument for $q \geq 4$ µm$^{-1}$, we measure $I(q)$ for fractal aggregates...
made of colloidal particles. Fractal aggregates provide a convenient means to test the apparatus, since the scattering profile has a simple power-law dependence on scattering vector \( q \): \( I(q) \sim q^{-d_f} \), with \( d_f \) the fractal dimension of the aggregate. While the fractal regime only extends beyond the particle size and below the aggregate dimension, it is easy to have the \( I \sim q^{-d} \) regime covering the whole MALS range, by choosing appropriately the particle size and the aggregation time. To form the aggregates, we start by preparing a particle suspension of latex spheres with a diameter of 19 nm in a baseline mixture of Milli-Q water and \( \text{D}_2\text{O} \) (0.5/0.5 v/v), at \( \varphi = 6 \times 10^{-4} \). Separately, a 30 mM solution of MgCl\(_2\) is prepared, using the same solvent. Equal amounts of the particle suspension and the salt solution are mixed directly in the scattering cell (cells with \( L = 5 \text{ mm} \) and \( L = 2 \text{ mm} \) were used), just before starting measurements that are run for about 17 hours. Initially, \( I(q) \) exhibits a power law tail at large \( q \) and a rolloff at lower \( q \) (data not shown), corresponding to the size of the aggregates. As clusters keep growing, the rolloff moves to smaller \( q \), eventually exiting from the MALS window. Figure 7 shows the intensity distribution measured in the two scattering cells at later stages, focussing on the range 1 \( \mu \text{m}^{-1} \leq q \leq 6 \mu \text{m}^{-1} \). The black curve is a power law with exponent \(-d_f\), obtained by fitting the two experimental curves in the range 1.5 \( \mu \text{m} \leq q \leq 3.5 \mu \text{m}^{-1} \), where the previous tests indicate that the instrument response is flat. We find \( d_f = 2.3 \), consistent with typical values for colloidal aggregates\(^{14}\). The fit is in excellent agreement with the data below \( q \leq 3.5 \mu \text{m}^{-1} \). The agreement remains quite good up to \( q \approx 5 \mu \text{m}^{-1} \), where a higher than expected intensity is measured, due to aberrations. At \( q = 5 \mu \text{m}^{-1} \) deviations are 15\% and 24\% for the \( L = 2 \text{ mm} \) and \( L = 5 \text{ mm} \) cells, respectively.

![Figure 7](image7.png)

**FIG. 7.** Intensity distributions measured for fractal aggregates of latex spheres placed in cells of thickness 5 mm and 2 mm. The plot zooms into the high \( q \) range 1 \( \mu \text{m}^{-1} = q = 6 \mu \text{m}^{-1} \). The black curve is a power law with exponent \(-d_f = -2.3\), obtained by fitting the two experimental curves in the range 1.5 \( \mu \text{m}^{-1} \leq q \leq 3.5 \mu \text{m}^{-1} \).

To summarize, the SLS tests indicate that the angular response of the setup is flat for thin samples (\( L \leq 2 \text{ mm} \)) placed at \( d = 18 \text{ mm} \), while for thicker samples \( I(q) \) tends to be overestimated beyond \( q \approx 4 \mu \text{m}^{-1} \). Even in the worst case that we have tested (a 5-mm thick cells), deviations do not exceed 24\% for \( q \) vectors as large as 5 \( \mu \text{m}^{-1} \).

B. Dynamic Light Scattering

To test the DLS capabilities of our apparatus, we measure the field time autocorrelation function of submicron Brownian particles, for which one expects \( g_1(\tau) = \exp(-Dq^2\tau^2) \), where \( D \) is the particle diffusion coefficient. Twelve annuli of pixels were processed simultane-
ously in real time, at a rate of $4$ images per second and using a single exposure time $t_{\text{exp}} = 5$ msec. The annulus average radius ranged from 70 pixels to 1253 pixels, logarithmically spaced with a scaling factor of 1.3 between one annulus and the next one. The width of the innermost annulus was 1 pixel, corresponding to a relative spread in scattering vector $\delta q/q = 1.4\%$. The same ratio was kept for all other annuli. With this annuli selection, the time correlation function is measured in the range $0.29 \mu m^{-1} < q < 5.71 \mu m^{-1}$, corresponding to a variation of three orders of magnitude in the characteristic decay time of $g_1$. The sample is a dilute suspension of polystyrene spheres with diameter $530$ nm and polydispersity $5\%$ (nominal values), suspended in a mixture of Milli-Q water/glycerol (approximately $0.3/0.7$ w/w, $n = 1.421$), at $\varphi = 6.4 \times 10^{-3}$ and loaded in a cell with $L = 5$ mm. The particle size and the solvent viscosity were chosen so that the decay time of $g_1$ be large enough to allow for real time measurements. Data were collected over 30 minutes, 9 hours after loading the cell.

The inset of Fig. 8a) shows the twelve correlation functions on a semilogarithmic plot. An offset has been subtracted from the raw data, since the baseline is typically somehow larger than zero, due to contributions from stray light that are not fully correct for by the background subtraction described in Ref.8. This offset is at most 0.15 for the smallest and largest $q$ and $\lesssim 0.05$ for most $q$ vectors. In the main figure, the same data are plotted as a function of time rescaled by $q^2$. All data collapse onto a single master curve that is well fitted by an exponential decay (line in Fig. 8a). Both the data collapse and the exponential shape are in agreement with what expected for particles undergoing Brownian diffusion. Note that due to the $q^2$ scaling, the quality of the collapse is quite sensitive to any error in the determination of the scattering vector. Thus, the data of Fig. 8a) confirm the validity of the $q$ calibration. Figure 8b) shows the decay time obtained by fitting separately each correlation function to an exponential decay, as a function of $q$, in a double logarithmic scale (stars). The circles are the decay time measured for the same sample but at larger scattering angles, $20 \deg \leq \theta \leq 120 \deg$ ($6 \mu m^{-1} < q < 30 \mu m^{-1}$), using a conventional DLS apparatus (Amtec goniometer equipped with a Brookhaven BT9000 correlator and an Argon ion laser operating at $\lambda = 514$ nm). The DLS and MALS data follow the same trend, showing that not only does the CCD-based apparatus capture well the shape and $q$ dependence of the correlation functions, but it also measures correctly their decay time on an absolute scale. The line is a power law fit to the data, with a fixed exponent $-2$ as inferred from diffusive motion, showing overall a very good agreement with both data sets. The first four points measured by the MALS apparatus were not included in the fit, because they slightly deviate from the $q^{-2}$ trend. This slight discrepancy is most likely due to additional ballistic dynamics that superimpose to the Brownian motion and originate from convective motion. Indeed, we find this effect to be even more relevant right after filling the cell, when temperature fluctuations and gradients are not stabilized yet. Such ballistic motion, while negligible with respect to diffusion on the small length scales probed by traditional DLS, become increasingly important as $q$ is decreased, since for ballistic motion the relaxation time of $g_1$ scales as $q^{-1}$, as opposed to $q^{-2}$ for Brownian diffusion. Therefore, their impact becomes eventually visible, as observed here in the low $q$ spectrum of the MALS apparatus.

VII. CONCLUSIONS

We have presented a static and dynamic light scattering apparatus that covers the angular range intermediate between those typically covered by small-angle and wide angle setups. Thanks to a novel optical layout, our apparatus does not require custom-made optical or optomechanical components, which should make it relatively easy to duplicate it even by groups with little experience in optics.

As a final remark, we note that we have also tested an alternative choice of lenses, while keeping the same overall layout. In this alternative scheme, the first two pairs of lenses are replaced by single aspherical lenses with a large numerical aperture, while the third pair of lenses is replaced by a single biconvex spherical lens. Details of the alternative lenses are provided in the Supplementary Information. We find that the performances at the largest angles are comparable, while the flare at small angles is slightly larger when using the aspherical lenses, presumably because the optical quality of their surfaces is not as good as for the spherical lenses.

ACKNOWLEDGMENTS

We thank J. Barbat for designing and machining the sample holder and A. Schofield for providing us with the PMMA particles. We gratefully acknowledge discussions with J. Oberdisse and L. Ramos and funding from the CNRS and the ANR (Contract No. ANR-09-BLAN-0198, COMET).

1M. Kerker, The scattering of light, and other electromagnetic radiation (Academic Press, New York, 1969).
2B. J. Berne and R. Pecora, Dynamic Light Scattering (Wiley, New York, 1976).
3F. Ferri, Review of Scientific Instruments 68, 2265 (1997).
4D. Lehner, G. Kellner, H. Schnablager, and O. Glatter, Journal of Colloid and Interface Science 201, 34 (1998).
5F. Ferri, M. Greco, G. Arcovito, F. Baasi, M. De Spirito, E. Pagamini, and M. Rocco, Physical Review E 63, 031401 (2001)
6F. Ferri, M. Greco, G. Arcovito, M. De Spirito, and M. Rocco, Physical Review E 66, 011913 (2002)
7A. P. Y. Wong and P. Wiltzius, Review of Scientific Instruments 64, 2547 (1993).
8L. Cipelletti and D. A. Weitz, Review of Scientific Instruments 70, 3214 (1999)
9 P. A. Webb, *A primer on particle sizing by static laser light scattering*, Micromeritics Instrument Corp. Workshop Series: Introduction to the Latest ANIS/ISO Standard for Laser Particle Size Analysis.

10 C.-M. Chou and P.-D. Hong, Macromolecules 36, 7331 (2003)

11 P. D. Kaplan, V. Trappe, and D. A. Weitz, Appl. Opt. 38, 4151 (1999).

12 J. Celli, B. Gregor, B. Turner, N. H. Afdhal, R. Bansil, and S. Erramilli, Biomacromolecules 6, 1329 (2005).

13 M. T. Valentine, A. K. Popp, D. A. Weitz, and P. D. Kaplan, Optics Letters 26, 890 (2001).

14 M. Carpineti, F. Ferri, M. Giglio, E. Paganini, and U. Perini, Physical Review A 42, 7347 (1990).

15 A. Bassini, S. Musazzi, E. Paganini, U. Perini, and F. Ferri, Review of Scientific Instruments 69, 220 (1998).

16 J. W. Goodman, *Introduction To Fourier Optics* (Roberts and Co., Greenwood Village, 2005), 3rd ed.

17 P. Lutus, *OpticalRayTracer*, see http://www.arachnoid.com/OpticalRayTracer/index.html

18 E. Tamborini, N. Ghofraniha, J. Oberdisse, L. Cipelletti, and L. Ramos, Langmuir 28, 8562 (2012).

19 K. Schätzel, in *Dynamic Light Scattering: The Method and Some Applications*, edited by W. Brown (Clarendon, Oxford, 1993).

20 P. Laven, *Mieplot*, see http://www.philiplaven.com/mieplot.htm.

21 D. Broglioli, A. Vailati, and M. Giglio, Europhysics Letters 63, 220 (2003).

22 D. Roessner and W. Kulicke, Journal of Chromatography A 687, 249 (1994).

23 S. Bernocco, F. Ferri, A. Profumo, C. Cuniberti, and M. Rocco, Biophysical journal 79, 561 (2000).