Measurement of the polarized structure function $\sigma_{LT'}$ for $p(\vec{e}', e'p)\pi^0$ in the $\Delta(1232)$ resonance region

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Numerical results are presented for the structure function $\sigma_{LT}$ for $p(\bar{e}, e'p)$ in the $\Delta(1232)$ resonance region.
The polarized longitudinal-transverse structure function $\sigma_{LT}$ has been measured in the $\Delta(1232)$ resonance region at $Q^2 = 0.40$ and 0.65 GeV$^2$. Data for the $p(e,e'p)\pi^0$ reaction were taken at Jefferson Lab with the CEBAF large acceptance spectrometer (CLAS) using longitudinally polarized electrons at an energy of 1.515 GeV. For the first time a complete angular distribution was measured, permitting the separation of different nonresonant amplitudes using a partial wave analysis. Comparison with previous beam asymmetry measurements at MAMI indicate a deviation from the predicted $Q^2$ dependence of $\sigma_{LT}$, using recent phenomenological models.

The $\gamma^*p \rightarrow \Delta^+(1232)$ transition has long served as a benchmark for testing nucleon models. In the SU(6) symmetric quark model, this strong magnetic dipole excitation is described as originating from a single quark spin flip. Residual spin-dependent and tensor-type interactions between the quarks are needed to explain the $N-\Delta$ mass difference and the small quadrupole transition strength observed in partial wave analyses of experimental pion electroproduction data [1–3]. Understanding the origin of these residual interactions and their role in resonance formation and decay is a fundamental challenge for modern QCD-inspired hadronic models.

In particular, the dynamical effects of the pion cloud are predicted to strongly modify the electromagnetic couplings at sufficiently low $Q^2$. Chiral-quark and bag models that incorporate pion couplings [4–7] generally describe the $\Delta(1232)$ photocoupling multipoles better than a purely quark/gluon framework [8,9]. Recent dynamical models derived from effective chiral Lagrangians explicitly treat pion multiple scattering [10,11] and predict strong modifications to both resonant and nonresonant amplitudes. The role of the pion cloud in electromagnetic interactions is also being studied using heavy baryon chiral perturbation theory [12] and unquenched lattice QCD [13].

Unfortunately, cross section measurements alone do not provide sufficient information to separate the $\Delta(1232)$ excitation reaction mechanisms from nonresonant backgrounds and the tails of higher-mass resonances. Single spin polarization observables, on the other hand, are directly sensitive to the interference between resonant and nonresonant processes and together with precise cross sections can provide powerful constraints to models.

In this Rapid Communication we report new measurements of the longitudinal-transverse polarized structure function $\sigma_{LT}$ obtained in the $\Delta(1232)$ resonance region using the $p(e,e'p)\pi^0$ reaction. Recent measurements of polarization observables [14–17] and unpolarized cross sections [2,18] for $Q^2 < 0.2$ GeV$^2$ show disagreement with some dynamical models near the $\Delta(1232)$ peak. However, so far only narrow angular and kinematic ranges have been studied, yielding few clues as to the origin of the discrepancy. The present experiment was performed at four-momentum transfers $Q^2 = 0.40$ and 0.65 GeV$^2$ and covers a range of invariant mass $W = 1.1 - 1.3$ GeV with full angular coverage in $\cos \theta^*_\pi$ and $\phi^*_\pi$ in the $p\pi^0$ center of mass (c.m.).

The data were taken at the Thomas Jefferson National Accelerator Facility (Jefferson Lab) using a 1.515 GeV, 100% duty-cycle beam of longitudinally polarized electrons incident on liquid hydrogen target. The electron polarization was determined by frequent Möller polarimeter measurements to be $0.69 \pm 0.009$ (stat) $\pm 0.013$ (syst). Scattered electrons and protons were detected in the CLAS spectrometer [19]. Electron triggers were enabled through a hardware coincidence of the gas Čerenkov counters and the lead-scintillator electromagnetic calorimeters. Protons were identified using momentum reconstruction in the tracking system and time of flight from the target to the scintillators. Software fiducial cuts were used to exclude regions of nonuniform detector response. Kinematic corrections were applied to compensate for drift chamber misalignments. The $p\pi^0$ final state was identified by requiring the missing neutral to have a mass squared between $-0.01$ and 0.05 GeV$^2$. Background from elastic Bethe-Heitler radiation was suppressed to below 1% using a combination of cuts on missing mass and $\phi^*_\pi$ near $\phi^*_\pi = 0^\circ$. Target window backgrounds were suppressed with cuts on the reconstructed $e'p$ target vertex.

In the one-photon-exchange approximation, the electroproduction cross section factorizes as follows:

$$\frac{d^5\sigma}{dE_{e'}d\Omega_{e'}d\Omega_{\pi}} = \Gamma_v \frac{d^2\sigma^h}{d\Omega_{\pi}}$$

(1)
where $\Gamma_{\gamma}$ is the virtual photon flux and $d^{2}\sigma^{h}/d\Omega_{\pi}^{\gamma}$ is the differential cross section for $\gamma^{*}\pi^{0}\rightarrow p\pi^{0}$ with electron beam helicity ($h=\pm 1$). For an unpolarized target, $d^{2}\sigma^{h}$ depends on the transverse ($e$) and longitudinal ($\epsilon_{L}$) polarization of the virtual photon through five structure functions: $\sigma_{T}, \sigma_{L}$, and their interference terms $\sigma_{TT}, \sigma_{LT}$, and $\sigma_{LT'}$:

$$
\frac{d^{2}\sigma^{h}}{d\Omega_{\pi}^{\gamma}} = \frac{p_{\gamma}^{*}}{k_{\gamma}^{*}} \sigma_{0} + h \sqrt{2} \epsilon_{L}(1-e) \sigma_{LT'} \sin \theta_{\pi}^{*} \sin \phi_{\pi}^{*} + \epsilon \sigma_{TT} \sin^{2} \theta_{\pi}^{*} \cos 2 \phi_{\pi}^{*} + \sqrt{2} \epsilon_{L}(1+e) \sigma_{LT} \sin \theta_{\pi}^{*} \cos \phi_{\pi}^{*},
$$

where $(p_{\pi}^{*}, \theta_{\pi}^{*}, \phi_{\pi}^{*})$ are the $\pi^{0}$ c.m. momentum, polar, and azimuthal angles, $e = \sqrt{1 + 2 |q^{*}| \tan^{2}(\theta_{\gamma}/2)} / |Q^{2}|$, $\epsilon_{L} = (Q^{2} / |k^{*}|^{2}) |e|$, and $k_{\pi}^{*}$ and $|k^{*}|$ are the virtual photon c.m. momentum and equivalent energy.

The structure functions $\sigma_{LT}$ and $\sigma_{LT'}$ determine the real and imaginary parts of bilinear products between longitudinal and transverse amplitudes:

$$
\sigma_{LT} : \text{Re}(L^{*} T) = \text{Re}(L) \text{Re}(T) + \text{Im}(L) \text{Im}(T),
$$

$$
\sigma_{LT'} : \text{Im}(L^{*} T) = \text{Re}(L) \text{Im}(T) - \text{Im}(L) \text{Re}(T).
$$

Detection of a weak nonresonant background underlying the peak of the $\Delta(1232)$ can be enhanced through its interference in $\sigma_{LT'}$, with the strong transverse magnetic multipole $\text{Im}(M_{1+})$. Sensitivity to real backgrounds is suppressed in $\sigma_{LT}$ due to the vanishing of $\text{Re}(M_{1+})$ at the resonance pole.

Extraction of $\sigma_{LT'}$ was made through a measurement of the electron beam asymmetry $A_{LT'}$:

$$
A_{LT'} = \frac{d^{2}\sigma^{+} - d^{2}\sigma^{-}}{d^{2}\sigma^{+} + d^{2}\sigma^{-}} = \frac{\sqrt{2} \epsilon_{L}(1-e) \sigma_{LT'} \sin \theta_{\pi}^{*} \sin \phi_{\pi}^{*}}{\sigma_{0}},
$$

Figure 1 shows $\sigma_{LT'}$ extracted at $Q^{2} = 0.40$ GeV$^{2}$ and $Q^{2} = 0.65$ GeV$^{2}$, where the cos $\theta_{\pi}^{*}$ dependence is plotted for $W$ bins of 1.18, 1.22, and 1.26 GeV. The measured angular distributions show a strong backward peaking for $W$ bins around the $\Delta(1232)$ mass. The curves show predictions from recent models [10,22,23] which use different methods to satisfy unitarity in the $\pi^{0}p$ final state. These models, which are fitted to previous photoproduction and unpolarized electroproduction data, include backgrounds arising from Born diagrams and $t$-channel vector meson exchange. The Sato-Lee [10] and Dubna-Mainz-Taipei [22] (DMT) models use an off-shell $\pi N$ reaction theory to calculate unitarity corrections, while the more phenomenological MAID2000 model [23] incorporates $\pi N$ phases directly into the background amplitudes. While the models describe the data qualitatively, none of the calculations is able to describe both the overall magnitude and the slope of the measured c.m. angular distributions consistently.

A more quantitative comparison was made through fitting the extracted $\sigma_{LT'}$ angular distributions using the Legendre expansion:

\[ \text{FIG. 1. CLAS measurement ( ) of } \sigma_{LT'} \text{ vs cos } \theta_{\pi}^{*} \text{ extracted at } Q^{2} = 0.40 \text{ GeV}^{2} \text{ (top) and } Q^{2} = 0.65 \text{ GeV}^{2} \text{ (bottom). Curves show model predictions. Shaded bars show systematic errors.} \]
near the peak of the difference terms involving where $P_l$ is the corresponding Legendre moment. Each moment can be decomposed into interference terms involving the leading-order magnetic ($M_{l_{\pi^p}}$), electric ($E_{l_{\pi^p}}$), and scalar ($S_{l_{\pi^p}}$) multipoles:

$$D'_0 = \text{Re}[(M_{l_{\pi^p}} - M_{l_{\pi^p}} + 3E_{l_{\pi^p}})S_{l_{\pi^p}} + E_{l_{\pi^p}}^* S_{l_{\pi^p}} - 2S_{l_{\pi^p}}]$$

$$D'_1 = -6 \text{Re}[(M_{l_{\pi^p}} - M_{l_{\pi^p}} + E_{l_{\pi^p}})S_{l_{\pi^p}} + E_{l_{\pi^p}}^* S_{l_{\pi^p}} - \cdots]$$

$$D'_2 = -12 \text{Re}[(M_{l_{\pi^p}} - E_{l_{\pi^p}})S_{l_{\pi^p}} + 2E_{l_{\pi^p}}^* S_{l_{\pi^p}} - \cdots],$$

where $l_{\pi}$ is the $\pi^0 p$ angular momentum whose coupling with the nucleon spin is indicated by $\pm$.

Figure 2 shows typical fits to $\sigma_{LT'}$ angular distributions near the peak of the $\Delta(1232)$ resonance (left), while the $Q^2$ dependence of the extracted Legendre moments is compared to model predictions (right). The largest disagreement with models clearly occurs for $D'_0$, which is dominated by interference terms involving s-wave $\pi N$ multipoles. The CLAS data also require $D'_2 \neq 0$. The fitted $D'_2$ strength has the same sign and overall magnitude as the model predictions, although we cannot differentiate between the models due to large statistical uncertainties. No evidence for $d$ waves was observed in our measurement of $\sigma_{LT'}$.

We also compare our fit results with a recent MAMI measurement [16] of the beam asymmetry $A_{LT'}$ at $Q^2 = 0.2 \text{ GeV}^2$. The published MAMI angular distribution was converted to $\sigma_{LT'}$ using Eq. (6) and MAID2000 for the unpolarized cross section $\sigma_0$. Since the MAMI data do not have sufficient angular coverage to determine $D'_0$, the fit was performed by constraining $D'_2$ relative to $D'_1$ using MAID2000. With $D'_2$ fixed, the remaining Legendre moments estimated from the MAMI data can be compared to the $Q^2$ trend of the CLAS data (Fig. 2, right). Both datasets suggest an anomalous behavior for $D'_0$ with respect to the models. However, a recent Bates measurement [17] of $\sigma_{LT'}$ at $Q^2 = 0.127 \text{ GeV}^2$ and $\theta^p_{LT} = 129^\circ$ found good agreement with MAID2000 and DMT, although no angular distributions were reported.

Figures 3 and 4 show the $W$ dependence of the fitted Legendre moments, $D'_0$ and $D'_1$, respectively. Both moments show strong resonant behavior, suggesting dominance of interference terms involving the multipoles of the $\Delta(1232)$. Our measurement of $D'_0$ is substantially below the predictions of MAID2000, and in closer agreement with the DMT dynamical model at $W = 1.18 \text{ GeV}$, while the Sato-Lee prediction is smaller still. For increasing $W$, our data fall below the DMT curve, while none of the models describes the $W$ dependence well. Note that contributions of higher resonances to $D'_0$ are negligible except near $W = 1.30 \text{ GeV}$. Figure 4 shows the fit results for $D'_1$. Here our comparison with models shows some $Q^2$ dependence. Better agreement with the dynamical models occurs below the $\Delta(1232)$ at $Q^2 = 0.4 \text{ GeV}^2$, while at $Q^2 = 0.65 \text{ GeV}^2$ all of the $W$ points are systematically larger than the predictions.

The large differences between the model predictions for
$D'_0$ arise from the term $\text{Im}(M^{+\dagger}_{I\dagger},S_{0+})$, which produces 70%–75% of the total strength in MAID2000. In contrast, $D'_1$ is more sensitive to higher resonances, which contribute 15%–20% in MAID2000 [coming mainly from $\text{Im}(M^{+\dagger}_{I\dagger},S_{1+})$], while $\text{Im}(M^{+\dagger}_{I\dagger},S_{1+})$ accounts for ∼40% of the total strength. The $S_{0+}$ multipole is an important background affecting the extraction of the $\gamma^*p\rightarrow\Delta(1232)$ $C2$ Coulomb quadrupole transition, and is sensitive to choices of $\pi NN$ coupling and contributions from final state $\pi NN$ rescattering [23]. Unfortunately, a simple rescaling of the $S_{0+}$ strength, as suggested in Ref. [16], is not sufficient to account for the inferred $Q^2$ dependence of $D'_0$.

In summary, complete angular distributions for the polarized structure function $\sigma_{LT}$ were measured for the first time, using the $p(e,e'p)\pi^0$ reaction. In accordance with measurements at lower $Q^2$ [14–17], evidence for significant nonresonant background in the $\Delta(1232)$ region is seen. A departure from the predicted $Q^2$ dependence of various effective Lagrangian based models is seen at the $\Delta(1232)$ peak when the CLAS data are compared to the MAMI data at $Q^2 = 0.2$ GeV². Examination of the Legendre moments $D'_0$ and $D'_1$ shows the discrepancies are largest for $D'_0$. CLAS measurements in the $Q^2$ range of 0.1–0.4 GeV² and also for $W > 1.3$ GeV are currently being analyzed to provide more information on the form factors of the underlying multipoles.

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