Forced electrostriction by constraining polarization switching enhances the electromechanical strain properties of incipient piezoceramics

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Recently developed lead-free incipient piezoceramics are promising candidates for off-resonance actuator applications due to their exceptionally large electromechanical strains. Their commercialization currently faces three critical challenges: the high driving electric field required for delivering the potentially large strains; large strain hysteresis, which is inappropriate for precision devices; and relatively high temperature dependencies. We propose that instead of utilizing incipient piezoelectric strains, harnessing the maximum possible electrostriction would provide a highly effective way to resolve all these challenges. This concept was experimentally demonstrated using textured 0.97Bi$_{1/2}$(Na$_{0.78}$K$_{0.22}$)$_{1/2}$TiO$_3$-0.03BiAlO$_3$ as an exemplary incipient piezoceramic, whereby texturing was achieved using a reactive templated grain-growth technique. The manufactured textured ceramic is characterized by $S_{\text{max}}/E_{\text{max}}$ of 995 pm V$^{-1}$ and an electrostrictive coefficient, $Q_{33}$, of 0.049 m$^4$ C$^{-2}$. Both these parameters are as large as those of single crystals. The current work presents a significant advancement in the field of lead-free ceramics and can guide future efforts in this direction. In addition, the concept presented here can be easily transferred to other disciplines involving the design of functional properties of various materials.

INTRODUCTION

Since the first report on incipient piezoelectric strain (IPS) in a (Bi$_{1/2}$Na$_{1/2}$)TiO$_3$ (BNT)-based lead-free ceramic, there have been numerous attempts to enhance the strain properties of these materials. These studies have concluded that IPS is a common feature of relaxor ferroelectrics as long as their freezing temperature is below room temperature, that is, they are in the ergodic relaxor state, whereas ferroelectric long-range order is only stable under the application of a certain or higher electric field. It should be noted that the electric-field-induced strain in a normal ferroelectric material is approximately half the strain inherently available for the given system. This result is due to the presence of the remanent state, which typically occupies ~0.1% of the entire phase. Piezoelectric strain commonly refers to the difference between the maximum and remanent strain levels, and it may be greatly enhanced by minimizing the remanent strain, as is the case for IPS.

Thus far, most useful IPSs have been found in relaxor ferroelectrics, indicating that the inherently large poling field, $E_{\text{pol}}$, (poling field: an electric field required for inducing ferroelectric state out of the existing relaxor state, determined at the inflection point of the electric-field-dependent strain curve as illustrated in Figure 1a) with a consequently large hysteresis, is unavoidable. This result is due to the considerably large nucleation energy barrier that has to be overcome for a ferroelectric phase to be born in a pure relaxor phase. In addition, the temperature-dependent strain properties are commonly expected to be poor because the electric field for a relaxor-to-ferroelectric transition increases significantly with temperature. This finding means that the driving electric field must be accordingly increased with increasing temperature to preserve the expected strain values. However, such an effect is practically impossible to achieve due to the simultaneous decrease in the breakdown electric field. Therefore, the strain characteristics of samples prepared by conventional solid-state reaction (CSSR) methods have a series of challenges to overcome, including large hystereses, large driving electric fields and relatively large temperature dependence. It follows that for incipient piezoceramics to be of practical importance, the three challenging issues, that is high $E_{\text{pol}}$, large degree of hysteresis and poor temperature stability, must be overcome reliably.

Considering the mechanism for IPS, a potentially simple solution to the aforementioned challenges could be via the control of the nucleation kinetics of the electric-field-induced ferroelectric
phase formation out of the initial relaxor phase. A common strategy used to facilitate the electric-field-induced relaxor-to-ferroelectric transition includes the tailoring of microstructures. A breakthrough in the form of experimental validation of this strategy was made with the design of a heterogeneous microstructure consisting of a ferroelectrically active core and a paraelectric shell. Here the core acted as a ferroelectric nucleus. This core-shell approach seems ideal for resolving the challenges of IPS. However, it suffers from a disadvantage, namely that it is difficult to achieve precise control over the composition of the core and the shell.

Recently, a 0–3 type ceramic–ceramic composite approach has been proposed as an alternative technique to the core-shell structure. The expected outcome of this approach is the same as that of the core-shell approach. One of the most important advantages of this technique is its practical simplicity. However, a problem arises because 0–3 type composites consist of ceramics with similar compositions consolidated at relatively high temperatures. Because of the high degree of chemical intermixing, this high-temperature processing often leads to chemically inhomogeneous microstructures, which are not amenable to reliable reproduction.

Meanwhile, considerable efforts have been made to induce a crystallographic texture using the so-called templated grain-growth (TGG) technique, inspired by the work of Saito et al. Indeed, TGG allows the incorporation of well-aligned template crystals, the composition of which is different from that of matrix crystals. This technique provides an effective way to reduce $E_{\text{pol}}$ because the energy barrier for heterogeneous nucleation is generally smaller than that for homogeneous nucleation. However, it is difficult to achieve a high degree of texturing with typical TGG processes due to the relatively small aspect ratio of template crystals. It must be noted that the aspect ratio of typical layer-structured template crystals usually decreases significantly during topochemical reactions. In addition, the degree of texturing is critically dependent on the sintering time, which commonly exceeds tens of hours. The long sintering time hinders the use of volatile elements.

Given that the hysteresis in IPS originates from ferroelastic domain reorientation during an electric-field-induced relaxor-to-ferroelectric transition, one possible solution is the optimal utilization of electrostriction while suppressing the relaxor-to-ferroelectric transition. It is known that (Bi$_{1/2}$Na$_{1/2}$)TiO$_3$-based incipient piezoceramics exhibit a comparatively high electrostrictive coefficient. To observe
this effect as clearly as possible, we chose the ceramic 0.97Bi_{1/2} (Na_{0.78}K_{0.22})_{1/2}TiO_3-0.03BiAlO_3 (BNKT-BA). This ceramic has moderate IPS, which therefore has room for further enhancement by the application of the currently proposed methodology. To ensure that the strain mechanism of the electrostrictive effect dominates over domain nucleation and reorientations, the polarization direction of the BNKT-BA was strongly constrained along the direction perpendicular to the electrodes by using highly anisotropic templates with a large aspect ratio (>20, see Supplementary Figure S1). Note that the electrostrictive effect becomes more pronounced when the contribution from domain reorientations vanishes. To provide the largest possible aspect ratio, a reactive templated grain-growth (RTGG) technique was implemented by omitting the topochemical reaction step. The results showed that suppressing the domain reorientation in the presence of electric fields markedly enhances the IPS by reinforcing the electrostrictive contribution to electromechanical strains.

**EXPERIMENTAL PROCEDURES**

**Preparation of Na_{0.5}Bi_{4.5}Ti_4O_{15} (NBiT) templates**

To synthesize plate-shaped NBiT particles, Na_2CO_3, Bi_2O_3 and TiO_2 (99.9% High Purity Chemicals, Tokyo, Japan) were mixed with NaCl (99%, Sigma-Aldrich, St Louis, MO, USA), which was used as a flux to keep the oxide-to-salt ratio at a value of 1:1 by weight. This mixture was reacted at 1100 °C for 4 h. The product was washed more than 20 times with boiled deionized water to isolate the NBiT templates. The average diameter and thickness of the NBiT templates were ~10 μm and 0.5 μm, respectively, and the crystallographic c-axis was in the out-of-plane direction of NBiT templates, as shown in Supplementary Figure S1.

**Preparation of BNKT-BA raw material**

The BNKT-BA matrix powders were synthesized using a conventional solid-state reaction method. Well-dried Bi_2O_3, Na_2CO_3, K_2CO_3, TiO_2 and Al_2O_3 (99.9% High Purity Chemicals) were weighed to conform to the stoichiometry and then ball-milled for 24 h in ethanol using zirconia balls. The milled powder was calcined at 850 °C for 2 h in a covered alumina crucible. The calcined and pulverized powder were mixed with an excess amount of Na_2CO_3, K_2CO_3, TiO_2 and Al_2O_3. The excess amounts were added to compensate the discrepancy between the composition of NBiT templates and the target composition. The resultant mixture was ball-milled again for 24 h and then calcined again at 700 °C for 1 h.

**Slurry preparation and sintering of textured BNKT-BA ceramic**

First, the solvent was prepared by mixing 60 vol% methyl ethyl ketone (99.5%, MEK, Daejung Chemical & Metals Co., Ltd, Siheung-Si, Korea) with 40 vol% ethyl alcohol (94%, SK Chemical, Seongnam-Si, Korea). Then, polyvinyl butyral (BM-5Z, Sekisui Chemical Co., Ltd, Osaka, Japan), dibutyl phthalate (94%, Daejung Chemical & Metals Co., Ltd), and BYK-112 (BYK Chemical, Geretsried, Germany) were added in the slurry as a binder, a plasticizer and a dispersant, respectively. The slurry was mixed continuously for 24 h. Then, 10 wt% NBiT templates were added and the slurry was mixed again for 12 h. The prepared slurry was tape-casted using a doctor blade to a uniform thickness of 80 μm and then dried at room temperature. The green sheets were stacked and then pressed at 50 °C under a uniaxial pressure of 50 MPa for 5 s to ensure firm adhesion between layers. Each sheet was laminated and cut to form a green compact. The green compacts were heated in air at 400 °C for 160 h to remove organic ingredients and then sintered in air at 1150 °C for 10 h. The choice of sintering time was based on our preliminary experiments on a ceramic of composition 0.985Bi_{1/2}(Na_{0.78}K_{0.22})_{1/2}TiO_3-0.015BiAlO_3, which is similar to the composition of the current material. As shown in Supplementary Figures 2(a) - 2(c), the RTGG specimen sintered at 1150 °C for 10 h showed clearly defined texture in the X-ray diffraction profiles and a homogeneous distribution of Na, Bi and Ti ions throughout the specimen.
Figure S2, the maximum texture is achieved at 10 h of heat treatment. Randomly oriented BNKT-BA specimens were also prepared by the conventional method for comparison.22

Sample characterization
The phase identity, degree of texture and in situ electric-field-dependent structural transition were characterized by powder X-ray diffraction (X'Pert-PRO, PANalytical, the Netherlands). Diffraction was performed on major surfaces, the normal vector of which was perpendicular to the casting direction. The microstructure of specimens was observed using field-emission scanning electron microscopy (FE-SEM, S-4200, Hitachi, Tokyo, Japan) on the fractured surfaces, which were perpendicular to the major surfaces after mirror-polishing and chemical etching. The compositional homogeneity was analyzed using a secondary ion mass spectrometer (Nano-SIMS 50 L, CAMECA, Gennevilliers, France) with a Cs⁺ Gun at 16 keV of impact energy and 0.4 pA.

RESULTS AND DISCUSSION
Figure 1a presents the state of the art in IPS in comparison to the results of the current study. The results demonstrate that harnessing electrostriction while the direction of polarization is kept perpendicular to the electric field is a highly effective way of tuning the electromechanical strain to the desired level. In addition to \( E_{\text{pol}} \), the degree of hysteresis, defined as \( \eta_{\text{hyst}} = \frac{A_{S_{\text{max}}}}{S_{\text{max}} \cdot E_{\text{pol}}} \times 100 \), is also significantly reduced. It is noted that the strain achieved at a field as low as 4.5 kV mm\(^{-1}\) is ~ 0.45%, which is even larger than that of (001)-oriented Pb(Zn\(_{1/3}\)Nb\(_{2/3}\))O\(_3\) (PZN) and Pb(Mg\(_{1/3}\)Nb\(_{2/3}\))O\(_3\)-0.24PbTiO\(_3\) (PMN-0.24PT) single crystals.23

Figure 1b depicts the bipolar strain hysteresis loop with respect to the square of polarization. Evidently, there is a quadratic dependence of strain on polarization, implying that the strain originates from electrostriction. This result is further supported by the constricted polarization hysteresis loops (Supplementary Figure S3).2 Consistent with the common knowledge that the electrostrictive coefficient is temperature insensitive,24 it is seen that the temperature dependence of the electromechanical strain is far more stable in RTGG than in CSSR (Figure 1c and Supplementary Figure S4).

The room-temperature electrostrictive coefficient was determined to be 0.043 m\(^4\) C\(^{-2}\), which is approximately two times greater than that of the CSSR specimen of the same composition \( Q_{33} = 0.026 \text{ m}^4 \text{ C}^{-2} \). It is believed that this significant increase in the electrostrictive...
coefficient of the sample obtained by the RTGG process can be attributed to the suppression of domain reorientation; otherwise, the externally applied electric field would be dedicated exclusively to domain reorientation. With increasing temperature, the electrostrictive coefficient is observed to increase and is then saturated (Supplementary Figure S5), peaking at 0.049 m² C⁻² at 140 °C. This value is more than two times as large as that of the best-known BNT-based piezoceramics. Furthermore, it is highly comparable to that of lead-based single crystals (Figures 1d and e).6,31,32

Figure 2a presents a representative microstructure of an as-sintered RTGG specimen demonstrating a high degree of texture. It is interesting to see that every grain, without exception, shows clear ferroelectric domain contrast. This result implies that the origin of the currently observed IPS is not due to a relaxor-to-ferroelectric transition, although the same composition in CSSR specimens is an ergodic relaxor.3 The presence of domain contrast, that is, ferroelectric order, even in the absence of an external electric field, indicates that the grain size is sufficiently large for the polarization vector to be crystallographically bound to the templates, thus establishing a long-range order.6,31,32

A quantitative X-ray diffraction analysis of the degree of texture (Figure 2b) is characterized by the Lotgering factor of 95%.3 This value corresponds to one of the best textures induced in BNT-based piezoceramics thus far. It is important to note that the crystallographic orientation of the direction perpendicular to the casting direction is <200> instead of [002], which is commonly targeted for tetragonal systems during the TGG process. Hence, the polarization vector of the final product is strongly excluded from the electric field direction during operation. Possible chemical inhomogeneity, caused by the use of templates of a chemically different composition, was checked by in situ X-ray diffraction, where the size effect on phase transitions in ferroelectric particles. Phys. Rev. B 50, 698–703 (1994).

To clarify the underlying strain mechanism, in situ electric-field-dependent X-ray diffraction studies were performed (Figure 3a). It is interesting to see that when the electric field is applied, the (200) peak shifts significantly to lower angles, whereas the (002) peak remains practically unchanged. Profile fitting after stripping Kα₂ radiation (exemplarily shown in Supplementary Figure S6) revealed that other than the electrostrictive contribution, domain reorientation also contributes to the strain mechanism at fields above 3 kV mm⁻¹. Domain reorientation contributes up to ~20% of the strain value at the maximum electric field of 4.5 kV mm⁻¹, as presented in Figure 3b. The unchanged magnitude of the unit cell vector c in the electric-field-driven reoriented domains may explain why the electrostrictive effect is significantly enhanced in the RTGG specimen. Here the polarization vector was designed not to be influenced by an external electric field. In this case, the existing local field due to the polarization vector may prevent the lattice from shrinking along the c direction during electrostriction, forcing the field direction to expand further due to Poisson’s ratio.

A comparison of the experimentally measured and calculated strain values reveals that the discrepancy between them is only significant for a decreasing electric field. Given that the peak position for (200) and (002) remains practically unchanged, regardless of the X-ray diffraction scan speed, the discrepancy in the hysteresis of the measured and the calculated profiles in Figure 3c may be attributed to domain reorientation kinetics.

In summary, we have demonstrated that maximizing the potentially available electrostriction in relaxor-based materials is a highly effective way of overcoming three critical challenges in IPS, namely, large operation field, large hysteresis and large temperature dependence. To this end, we intentionally aligned the direction of polarization of the given material perpendicular to the direction of the electric field to minimize domain reorientations during operation. The current work opens up the possibility of applying incipient piezoceramics to real-world device applications by exploiting the merits of their exceptionally large displacements.

CONFLICT OF INTEREST
The authors declare no conflict of interest.

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