First-principles study of cubic perovskites SrMO$_3$ (M = Ti, V, Zr and Nb)

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Using the full-potential linearized-augmented-plane-wave (FLAPW) method, we have analyzed systematically the trends in the structural and electronic properties of the 3d and 4d transition-metal oxides SrMO$_3$ (M = Ti, V, Zr and Nb). The optimized lattice parameters, bulk modules, densities of states, band structures and charge density distributions are obtained and compared with available theoretical and experimental data. The energy gap between 02p - Md bands increases as the covalency of the system decreases going from 3d to 4d based perovskites. The electron configurations of Sr(Ti,Zr)O$_3$ and Sr(V,Nb)O$_3$ usually referred to as d$^0$ and d$^+$ oxides, respectively, differ considerably from these idealized "ionic" configurations, and the deviations increase with increasing of the d-p covalent overlap in the oxides.

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I. INTRODUCTION

Perovskites SrMO$_3$ attract much attention from physicists and material scientists because of the unusual combination of their magnetic, electronic and transport properties. However, the electronic structure features in these complicated systems are not understood comprehensively yet, and attempts to explain their behavior in different conditions are often based on oversimplified models. Through quite a number of publications are known on strontium oxide perovskites with 3d metals on M sites, the research focus has long been on strontium titanate, SrTiO$_3$ - one of the generic representatives of 3d transition-metal oxide perovskites. For instance, the LCAO-based approaches are used in non-self-consistent or self-consistent calculations. Recently more accurate self-consistent full-potential LAPW, LMTO, ab-initio pseudopotential band structure calculations are performed. Some attention is given to the related materials, viz., the 3d metal-like perovskite SrVO$_3$, solid solutions SrTi$_{1-x}$V$_x$O$_3$, SrVO$_3$/SrTiO$_3$ superlattices and heteroepitaxial structures SrVO$_3$/SrTiO$_3$/Sr$_2$O$_2$. Also, the cubic SrVO$_3$ is treated as a model system for discussion of orbital fluctuations and correlation effects. As an example of 4d based perovskites, the cubic SrZrO$_3$ is studied by the discrete variation (DV) molecular orbital method and, recently, the band structure calculations are performed within the local-density approximation (LDA). Finally, the electronic properties of the ideal cubic SrNbO$_3$, which may be considered as an ample family of perovskite-related layered niobates, are investigated in work by means of LMTO-ASA approach. In this Communication, we report results of a systematic study of electronic properties of perovskite-type 3d and 4d transition-metal oxides SrMO$_3$ (M = Ti, V, Zr and Nb) by means of the FLAPW method within the generalized gradient approximation (GGA). We have evaluated a number of physical parameters such as optimized crystal structure, bulk modulus, density of states, band structure and electron density distribution and considered their variations with M-type metal.

II. MODELS AND METHOD

The considered SrMO$_3$ perovskites are assumed to have ideal cubic structure (e.g. Pm3m) where atomic positions in the elementary cell are M: 1a (0,0,0); O: 3d (0,0,1/2); and Sr: 1b (1/2,1/2,1/2). The electronic configurations are taken Ar$^{3d^{2}}$s$^{2}$ for Ti, Ar$^{3d^{2}}$s$^{2}$ for V, Kr$^{4d^{2}}$s$^{2}$ for Zr, Kr$^{4d^{2}}$s$^{2}$ for Nb, Kr$^{5s^{2}}$ for Sr and He$^{2s^{2}}$p$^{4}$ for O. Here, the noble gas cores are distinguished from the sub-shells of valence electrons. The equilibrium structural parameters and bulk modules are calculated using the Vienna package WIEN2k, which is an implementation of the hybrid full potential (linear) augmented plane-wave plus local orbitals (L)APW+lo method within the density-functional theory$^{22}$. The basis set inside each MT sphere is split into core and valence subsets. The core states are treated within the spherical part of the potential only, and are assumed to have a spherically symmetric charge density confined within MT spheres. The valence part is treated with the potential expanded into spherical harmonics up to l = 4. The valence wave functions inside the spheres are expanded up to l = 12. The plane-wave expansion with RMT*KMAX equal to 10 and k sampling with 10$^*$10$^*10$ k-points mesh in the Brillouin zone (BZ) is used. All calculations are carried out with optimized lattice constants. We use the Perdew-Burke-Ernzerhof generalized gradient approximation (GGA)$^{23}$ for the exchange correlation potentials. Relativistic effects are taken into account within the scalar-relativistic approximation.

The self-consistent calculations were considered to have converged when the difference in the total energy of the crystal did not exceed 0.1 mRy as calculated at consecutive steps. We have adopted the MT radii of 1.7 a.u. for O, 1.8 a.u. for M, and 2.5 a.u. for Sr. The lattice constants and bulk modules are calculated by fitting the total energy versus volume according to the
TABLE I: Calculated and experimental values for the lattice parameters, bulk modules and its pressure derivative of SrMO₃ (M= Ti, V, Zr and Nb).

| Parameters | Lattice constant (Å) | Bulk modulus B₀ (GPa) | B₀' |
|------------|----------------------|-----------------------|-----|
|            | Calcul. | Exper. | Calcul. | Exper. | Calcul. | Exper. | Calcul. | Exper. |
| SrTiO₃     | 3.9456* | 3.905** | 167.9* | 191* | 3.878* | 3.71* | 182.8* | 193.3 |
| SrVO₃      | 3.8662* | 3.841** | 182.8* | - | 4.1794* | 3.8456* | 183.3* | 4.56* |
| SrZrO₃     | 4.1794* | 4.109** | 158.28* | 150* | 4.0730* | 3.9456* | 167.9* | 191* |
| SrNbO₃     | 4.0730* | - | 170.0* | - | 3.71* |

* - our FLAPW-GGA data

Murnaghan’s equation of state. The total density of states (DOS) was obtained using a modified tetrahedron method.

III. RESULTS AND DISCUSSION

The lattice constants of the selected perovskites SrMO₃, where M = Ti, Zr, V and Nb, were calculated under constrain of cubic symmetry. The results and some available experimental and theoretical data are summarized in Table 1. It is seen that for SrTiO₃ and SrZrO₃ the calculated LDA constants are smaller compared to experimental ones. The GGA improves the lattice constants over the LDA. In fact, the obtained GGA lattice constants are very close to experimental data; the deviations for SrTiO₃, SrZrO₃ and SrVO₃ achieve only about 1%. The bulk modules decrease going from SrTiO₃ to SrZrO₃ and from SrVO₃ to SrNbO₃; and B₀ values for metal-like SrVO₃ and SrNbO₃ are higher than for insulating SrTiO₃ and SrZrO₃ perovskites. These trends correlate with changes in the lattice constants.

The dispersion E(k) in the high-symmetry directions in the Brillouin zone are shown in Fig.1 where similarity in the energy bands is evident in the oxide perovskites under study. The general features in the spectra can be specified in more detail with the use of SrTiO₃ as example. The lower bands, which are not shown in Fig.1, contain 12 electrons in Sr4p and O2s semi-core states located about -15.5 eV below the Fermi level.

The upper valence band (VB) with the width of about 4.6 eV is derived mainly from O2p orbitals with some admixture of Ti and Sr states, and it contains 18 electrons. The bottom of the conduction band (CB) is composed mainly of Ti3d t₂g and eₗg states, and at higher energies the Sr4d - like bands are placed. The valence-band top of SrTiO₃ is composed of O2p orbitals, and it is located at the R point, while the VB maximum at the M point is about 0.09 eV lower than the R. The conduction-band bottom is at the G point. The CB minimum at X is by 0.11 eV higher than at the Γ point. Thus the indirect gap between R and Γ points is 1.81 eV, and the direct gap at Γ is 2.16 eV. These features of the band structure agree well with the previous calculations, see Table 2. At the same time the experimentally determined indirect band gap in SrTiO₃ achieves about 3.30 eV, while the direct band gap energy is equal to 3.75 eV.

The nine occupied bands at the Γ point consist of three triply degenerate levels (Γ₁₅, Γ₂₅ and Γ₁₅) with energies of -2.82, -1.17 and -0.39 eV below Eₚ, respectively. The splitting of the levels (Γ₁₅ - Γ₂₅) and (Γ₂₅ - Γ₁₅) is due to the crystal field effects and electrostatic interaction between O2p orbitals. The triply degenerate (Γ₂₅, +1.81 eV) and the doubly degenerate levels in the conduction band originate from t₂g (π*) and eₗg (σ*) bands of titanium, and they are separated with the energy gap of 2.31 eV.

The calculated total (TDOS) and partial (PDOS) densities of states are shown in Fig.2 within the energy interval [Eₚ - 6 eV ≤ E ≤ Eₚ + 8 eV]. The TDOS is almost entirely composed from the PDOSs for Ti3d and O2p states. The valence TDOS originates predominantly from O2p states, which is consistent with SrTiO₃ being a formal d⁶ system with titanium in 4+ oxidation state. There is also a small contribution in the valence TDOS from strontium 5s states. However, there is a Ti3d PDOS in the occupied energy range due to the hybridization with the O2p states indicating the presence of a covalent bonding. Note also that within the cubic symmetry of SrTiO₃ the hybridization between t₂g and eₗg states is forbidden, and the orbitals within both bands are degenerate. Nevertheless, because of the Ti-O hybridization the admixture of the both t₂g and eₗg states to the oxygen 2p bands and also their partial overlapping occur. It is seen from Fig. 2 that the eg states (directed towards oxygen atoms so that they form σ bonds with respective O 2p orbitals) have lower energy in comparison with Ti t₂g states forming π-like bonds with O 2p states.

The TDOS profile is formed basically of four peaks.
### Table II: Calculated and experimental values for the bandwidths (in eV) of SrMO$_3$ (M= Ti, V, Zr and Nb).

| Parameters       | SrTiO$_3$ | SrZrO$_3$ | SrVO$_3$ | SrNbO$_3$ |
|------------------|-----------|-----------|----------|-----------|
|                  | 4.59*     | 3.86*     | 7.18*    | 8.12*     |
| Valence band     | 4.95*     | 4.32*     | 7.52*    | 6.12*     |
| Conduction band  | -         | -         | 1.05*    | 1.21*     |
| (occupied part)  | -         | -         | 1.13*    | 1.18*     |
| Band gap:        |           |           |          |           |
| direct(Γ)        | 2.16*     | 3.75*     | 1.40*    | 2.79*     |
| indirect(R-Γ)    | 1.81*     | 3.30*     | 1.02*    | 2.38*     |
|                  | 1.92*     | 3.37*     | 2.35*    |           |
|                  | 3.25*     | 5.63*     |           |           |
|                  | 3.58*     |           |           |           |

* - our FLAPW-GGA data
* - Experimental data

The comparison of the band structures of the isostructural SrTiO$_3$ and SrZrO$_3$ shows that the dispersion of the bands in SrTiO$_3$ is much stronger than in SrZrO$_3$. For example, the VB bandwidth in SrTiO$_3$ is about 0.73 eV larger. This means that Ti-O bonds are more covalent than respective bonds between zirconium and oxygen. Another obvious difference is that the band gap (which remains indirect in SrZrO$_3$; the bottom of the conduction band is located at the Γ point in the cubic BZ while the top of the valence band is at the R point) is about 1.49 eV (45%) larger than that of SrTiO$_3$. In the case of SrZrO$_3$ the splitting of the bands (Γ$_{15}$ - Γ$_{25}$) and (Γ$_{25}$ - Γ$_{15}$) is about 0.75 and 0.62 eV, respectively.

Band structures for SrVO$_3$ and SrNbO$_3$ are presented in Fig.1, and band structure parameters are listed in Table 2. The VBs of SrVO$_3$ and SrNbO$_3$ consist of completely occupied oxygen 2p bands and partially occupied (V,Nb)3d bands. The electronic states near the Fermi level originate mainly from 3d ($t_{2g}$) states.

### Table III: Occupation indices (in e) of M e$_g$ and t$_{2g}$ bands of SrMO$_3$ (M= Ti, V, Zr and Nb).

| Band/system | SrTiO$_3$ | SrZrO$_3$ | SrVO$_3$ | SrNbO$_3$ |
|-------------|-----------|-----------|----------|-----------|
| M e$_g$     | 0.642*    | 0.742     | 0.307    | 0.533     |
| M t$_{2g}$  | 0.473     | 1.313     | 0.234    | 0.791     |

One can see from Fig.2 that for SrVO$_3$ and SrNbO$_3$ there is some contribution of the t$_{2g}$ and e$_g$ bands in the energy intervals from -7.2 to -2.1 eV and from -8.3 to 3.6 eV, respectively, because of the hybridization with O2p states. In the case of SrVO$_3$ the splitting of the bands (Γ$_{15}$ - Γ$_{25}$) and (Γ$_{25}$ - Γ$_{15}$) are about 1.94 and 0.81 eV; for SrNbO$_3$ these values are about 0.95 and 0.74 eV, i.e. larger than for SrTiO$_3$ and SrZrO$_3$, respectively. For SrVO$_3$ and SrNbO$_3$ the t$_{2g}$ states are dominant in the vicinity of the Fermi level. The e$_g$ and t$_{2g}$ bands are well separated in the CB, and the maximum of the DOS in the eg band is centered above the upper band edge of the t$_{2g}$ band.

The obtained results show that the total density of states at the Fermi level N$_{tot}(E_F)$ in SrVO$_3$ (1.678 states/eV/cell) is about 20% higher than in SrNbO$_3$ (1.256 states/eV/cell). The main contribution to N$_{tot}(E_F)$ in both systems originates from the t$_{2g}$ bands, and the N$_{tot}(E_F)$ changes are also controlled by the contributions from t$_{2g}$ states: going from SrVO$_3$ to SrNbO$_3$, these contributions decrease rapidly from 1.109 to 0.542 states/eV/cell. In order to illustrate the bonding picture in systems under consideration we have plotted the charge density maps for SrTiO$_3$ and SrVO$_3$, Fig. 3. It is seen that the covalent interaction between Ti and O or V and O atoms is very strong.

Finally, the perovskites SrTiO$_3$ and SrVO$_3$ (and their 4d analogues) are usually referred to as d$^0$ and d$^1$ oxides in the literature. It is seen, however, from Table 3 that calculated electron configurations (viz., Ti3d$^{1.115}$, Zr4d$^{0.541}$, V3d$^{2.055}$ and Nb4d$^{1.324}$) differ considerably from the idealized "ionic" configurations, and the respective deviations increase with the d-p covalent overlap in the oxides.

### IV. CONCLUSIONS

In summary, we have performed FLAPW calculations in order to systematically study ground state properties and electronic structure features in 3d and 4d transition-metal oxides SrMO$_3$, where M = Ti, V,
Zr and Nb. The energy gap between 2p oxygen and d metal bands increases with the decrease in the covalent p-d overlap. The optimized lattice parameters, bulk modules, densities of states, band structures and charge density distributions are obtained and compared with the available theoretical and experimental data. The analysis of the d band population reveals that the deviation of the d metal electron configurations from the formal ionic state (d⁰ for SrTiO₃, SrZrO₃ and d¹ for SrVO₃ and SrNbO₃) increases with p-d covalent overlap.

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FIG. 1: Band structures of cubic perovskites: 1- SrTiO$_3$ 2- SrVO$_3$ 3- SrZrO$_3$, 4- SrNbO$_3$. The Fermi level corresponds to 0.0 eV.
FIG. 2: Total and projected DOSs for the cubic perovskites SrBO$_3$ (B = Ti, V, Zr and Nb).
FIG. 3: Charge densities maps for SrTiO$_3$ and SrVO$_3$ in (100) plane.