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Prospects for indirect MeV Dark Matter detection with Gamma Rays in light of Cosmic Microwave Background Constraints

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The self-annihilation of dark matter particles with mass in the MeV range can produce gamma rays via prompt or secondary radiation. The annihilation rate for such light dark matter particles is however tightly constrained by cosmic microwave background (CMB) data. Here we explore the possibility of discovering MeV dark matter annihilation with future MeV gamma-ray telescopes taking into account the latest and future CMB constraints. We study the optimal energy window as a function of the dominant annihilation final state. We consider both the (conservative) case of the dwarf spheroidal galaxy Draco and the (more optimistic) case of the Galactic center. We find that for certain channels, including those with one or two monochromatic photon(s) and one or two neutral pion(s), a detectable gamma-ray signal is possible for both targets under consideration, and compatible with CMB constraints. For other annihilation channels, however, including all leptonic annihilation channels and two charged pions, CMB data rule out any significant signal of dark matter annihilation at future MeV gamma-ray telescopes from dwarf galaxies, but possibly not for the Galactic center.

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I. INTRODUCTION

Dark matter is a key element in the current cosmological paradigm, the so-called ΛCDM concordance model of a cosmological constant plus cold dark matter. Such a picture is highly consistent with all latest cosmological observations, including those of the Cosmic Microwave background (CMB) and of galaxy distributions [1]. Little is known, however, about the dark matter fundamental properties as an elementary particle, and about whether or not the dark matter is coupled to the Standard Model other than via gravity. If dark matter particles annihilate (or decay – we will not consider decay here, however) into Standard Model particles, it is possible to discover a non-gravitational signal through astrophysical observations. One way to search for this kind of signal is by looking for excess photon emission, typically in an energy range close to the dark matter particle mass, from dark-matter-rich targets such as the Galactic Center, local clusters of galaxies, Dwarf Spheroidal or local Milky-Way-like galaxies, where the expected signal-to-noise is often optimal [2]. An especially interesting case is when the dark matter annihilation events produce monochromatic photons in the final state, and the particle mass can be related to the energy of the expected photon lines (in the simplest case of a two-photon annihilation mode, the line approximately corresponds to the dark matter particle mass, for non-relativistic annihilating particles) [3–9].

The search for gamma rays as indirect probes of dark matter annihilation has been extensively pursued both theoretically and observationally; one of the most recent results is from the Fermi-LAT collaboration, and it covers the energy range ~4.8 GeV up to ~ 250 GeV [10–12]. The forthcoming GAMMA-400 space mission [13] is anticipated to launch at the beginning of 2020 and will search for gamma rays in the energy range from ~ 100 MeV up to 3 TeV, thus overlapping Fermi’s energy range. The energy range between ~ 0.2 MeV up to ~ 100 MeV is however still vastly untapped and largely unexplored [1], and potentially critical to search for dark matter with a mass in the few MeV to few hundred MeV range. Several proposed mission concepts have recently been discussed to deploy an MeV detector capable to eliminate this “MeV gap” [10], including for example the e-ASTROGAM gamma-ray space mission [17] and many others such as GRIPS [18], PANGU [19], ACT [20], and AdEPT [21].

The MeV range is a new exciting frontier for future indirect dark matter searches with gamma rays. With this experimental motivation in mind, in the present study we analyze the projected capability of future MeV gamma-ray detectors in exploring MeV dark matter models, as a function of the dominant pair-annihilation finals state and compare with the tightest constraints on the allowed

† With the partial exception of the now defunct COMPTEL [14] and EGRET [15] telescopes, featuring however relatively low effective area and poor energy resolution.
annihilation rate as a function of the particle mass stem from the induced distortions to the spectrum of the CMB [23, 24]. We remain agnostic as to the specific UV realization of the particle models at hand, and assume that one of the kinematically allowed annihilation final states dominates.

In this work we exclusively focus on s-wave annihilating dark matter. In the case of p-wave pair-annihilation the constraints from CMB are largely relaxed, as we discuss in section III but the prospects for gamma-ray detection are also not as promising as in the s-wave case. We compute the parameter space ranges on the $(m_\chi, (\sigma v)_{s\text{-wave}})$ plane allowed by CMB for six different annihilation channels and we then proceed to compare those ranges with the values producing a 5$\sigma$ detection for some hypothetical detector specification, inspired by currently proposed experimental designs for future MeV detectors.

This paper is organized as follows: In section II we discuss the particle dark matter models and assumptions, and present the photon spectrum for the different annihilation channels; In section III we briefly discuss the thermal history of the Universe and how extra energy injection can alter the residual free-electron fraction after recombination, leading to distortions in the CMB Power Spectrum. In section IV we discuss how we construct the hypothetical detector and what energy range can enhance the detection for each channel, and, finally, we conclude in section V.

II. GAMMA-RAYS FROM MEV DARK MATTER ANNIHILATION

We consider dark matter masses in the range between the neutral pion mass ($\sim 135$ MeV) and 1 GeV. We remain agnostic about the underlying UV theory and about the spin of the dark matter particle; rather, we describe a given model realization by the triplet given by the dark matter particle mass $m_\chi$, the thermally-averaged zero-temperature pair annihilation cross section times relative velocity $(\sigma v)$, and the dominant annihilation final state. For simplicity, we assume that, whenever kinematically open, the two-pion final state dominates over $n\pi$, $n > 2$, and over final states involving heavier mesons, although this depends on the matching of the UV theory onto the light meson degrees of freedom [24]. This is somewhat justified, however, because of phase-space suppression of the sub-dominant annihilation final states.

With these assumptions, the two-body final states we consider in this work are:

(i) two photons, $\gamma\gamma$; 
(ii) photon and neutral pion, $\gamma\pi^0$, open for $\sqrt{s} > m_{\pi^0}$; 
(iii) two neutral pions, $\pi^0\pi^0$, for $\sqrt{s} > 2m_{\pi^0}$; 
(iv) two charged pions, $\pi^+\pi^-$, for $\sqrt{s} > 2m_{\pi^\pm}$; 
(v) two charged leptons, $\ell\ell$ (l=e, $\mu$) state, accessible for $\sqrt{s} > m_\ell$.

Here $s \approx 2m_\chi$ is the Mandelstam variable, $m_{\pi^0}$, $m_e$ and $m_\mu$ are the pion, electron, and muon mass, respectively. We do not consider channels involving neutrinos since they do not affect the CMB nor do they produce (significant amounts of) photons. The $\gamma$-ray spectrum, $dN/dE_\gamma$, generated by the annihilation channels listed above are quite simple for the first three cases. For the $\gamma\gamma$ final-state the spectrum is a delta function centered at the dark matter particle mass, 

$$dN/dE_\gamma = 2\delta(E_\gamma - m_\chi).$$

The spectrum generated by the $\gamma\pi^0$ final state is a delta function for the prompt photon and a box-shaped spectrum for the subsequent decay of the $\pi^0$ into two photons, 

$$dN/dE_\gamma = \delta(E_\gamma - E_0) + \frac{2}{\Delta E},$$

where, $E_0 = \sqrt{\frac{s}{2}} \left(1 - \frac{m_{\pi^0}^2}{s}\right)$, and a $\Delta E$ given by $\Delta E = \sqrt{\frac{s}{2}} \left(1 - \frac{m_{\pi^0}^2}{s}\right)$ [10]. For the two neutral pions, $\pi^0\pi^0$, we have a box-shaped spectrum

$$dN/dE_\gamma = \frac{4}{\Delta E},$$

where $\Delta E = \sqrt{\frac{s}{4}} - m_{\pi^0}$. For the $\pi^+\pi^-$ channel we used numerical results from Ref. [24], which include radiative photon production from both muons and electrons in the $\pi^\pm$ decay chain.

In the case of dark matter annihilating into leptons, the spectrum is quite different since the photon final state comes from radiative processes, and it is approximately given by [25] [26]

$$\frac{dN}{dy} \simeq \frac{\alpha}{\pi} \left(1 - \frac{1}{y} - \frac{y}{1 - y}\right) \left(\ln \frac{s(1 - y)}{m_\ell^2} - 1\right),$$

where $y \equiv E_\gamma/m_\chi$ and the approximate leading-log formula applies for $m_\chi \gg m_\mu$.

Notice that in this study we neglect secondary photon production [27]. The most relevant process would be inverse Compton, but the typical energies for the up-scattered photons, even in the case of the most energetic and sufficiently dense photon background, typically starlight, for which $E_\gamma \sim 1$ eV, would be [27, 30]

$$E_\gamma \sim \Gamma_\gamma^2 E_\gamma \sim \left(0.1 \times \frac{m_\chi}{m_e}\right)^2 E_\gamma \ll 1 \text{ MeV},$$

where $\Gamma_\gamma$ is the typical Lorentz factor of the $e^\pm$ produced in the dark matter annihilation event. Secondary photons thus largely fall outside the range of interest for future proposed MeV gamma-ray detectors.
III. THERMAL HISTORY AND CMB CONSTRAINTS

The CMB is one of the most important observables on Cosmology. It has been measured with increasingly high precision, and the physics behind it is well understood. As a result, CMB data can be used to constrain dark matter models that inject electromagnetically interacting Standard Model particles, since those would alter the thermal history of the Universe. Specifically, dark matter self-annihilation injects energy in the intergalactic medium (IGM), with possible ionization and heating of the IGM gas, resulting in modifications to the recombination process at redshifts $z \sim 1000$. Free electrons left-over after recombination interact with CMB photons and cause modifications to the CMB power spectrum, which, in turn can be constrained with current CMB data.

The energy per unit volume per unit time injected in the IGM by dark matter particle pair-annihilation is usually cast as:

$$\frac{dE}{dtdV} = \rho_c^2 c^2 \Omega_X^2 (1 + z)^6 P_{\text{ann}}(z),$$

where $\rho_c$ is the critical density of the Universe, $\Omega_X$ is the dark matter density and the annihilation parameter,

$$P_{\text{ann}} \equiv f(z) \langle \sigma v \rangle \frac{m_X}{\chi}$$

is given in terms of the dark matter particle mass, $m_X$, the thermally averaged cross section $\langle \sigma v \rangle$, and a redshift-dependent efficiency function $f(z)$. Equation (5) is coupled to the evolution of the free-electron fraction and medium temperature, so one has to solve both and include the result in the CMB fluctuations analysis. The standard methodology of solving these equations in presence of dark matter annihilations is extensively described in Ref. [31], and is implemented in Boltzmann codes as CLASS [32].

In this work, we use the current constrains to the s-wave dark matter annihilation, given by the latest Planck constraints [1],

$$P_{\text{ann}} < 4.1 \times 10^{-28} \text{cm}^3 \text{s}^{-1} \text{GeV}^{-1},$$

which, by means of equation (5), translates into an excluded region in the mass vs cross-section plane. However, the annihilation probability $P_{\text{ann}}$ is in principle a redshift-dependent quantity through the efficiency function. Fortunately, it has been demonstrated that one can use an effective redshift-independent efficiency function $f_{\text{eff}}$; the authors of Ref. [23] have proved that by making this change, the CMB power spectrum is altered in the same way as if one were including a redshift-dependent efficiency function. Following reference [23], the $f_{\text{eff}}$ is computed as:

$$f_{\text{eff}} = \frac{1}{2m_X} \int_0^{m_X} E dN \left( f_{\text{eff}}^\gamma(E) \frac{dN}{dE} + 2 f_{\text{eff}}^{\pi^0}(E) \frac{dN}{dE} \right),$$

where the functions $f_{\text{eff}}^{(\gamma)(e^+)}$ are provided in Ref. [23].

One therefore exclusively needs to know the injected photon and electron-positron spectrum for a given annihilation final state to compute the effective efficiency function and apply the Planck constraints, Eq. (7), for each annihilation channel. For the cases of dark matter annihilating into $\gamma\gamma$, $\gamma\pi^0$, $\pi^0\pi^0$ and $e^+e^-$ this is straightforward using the spectra presented in Section II, Eq. (1), (2) and (4). For the $e^+e^-$ case we need to add a delta-like function centered at the dark matter mass besides the internal bremsstrahlung photon spectrum, while for the muon pair case, besides the photon spectrum of Eq. (4), we use the electron-positron spectrum fit given in Ref. [33], valid since we are in the range $m_X > m_\mu$. Finally, for the case of charged pions, the electron-positron spectrum was computed following the results of Ref. [34]–[36]. The effective functions $f_{\text{eff}}$ for all these channels as a function of the dark matter particle mass are presented in Fig. 1.

With all these ingredients in hand, one can set constrains on the parameter space ($\langle \sigma v \rangle, m_X$) through:

$$\langle \sigma v \rangle < \frac{m_X}{f_{\text{eff}}} P_{\text{ann}}.$$  (9)

Such constraints correspond to the solid lines in Fig. 3 and in the following figures, which will be discussed in detail below.

Thus far we have only discussed CMB constraints for an s-wave annihilating dark matter cross-section, but if we allow the thermally averaged cross section to be velocity dependent, $\langle \sigma v \rangle \propto v^2$, CMB constraints relax very significantly. Specifically, the injected energy due to p-wave annihilating dark matter is

$$\frac{dE}{dt} = c^2 \Omega_X \rho_c^2 (1 + z)^6 \left( \frac{\langle \sigma v \rangle_p}{m_X} \right),$$

(10)
dark matter pair annihilation is given by:
\[
\phi = J(\Delta \Omega) \cdot \frac{1}{4\pi} \langle \sigma v \rangle \int dE \frac{dN}{dE},
\]
where \(J\) is the astrophysical “J-factor”, the line of sight integral of the dark matter density squared integrated over an angular window subtending a solid angle \(\Delta \Omega\). In this work we focus on the dwarf spheroidal galaxy Draco, with a J-factor of \(\log_{10}(J/\text{GeV}^2\text{cm}^{-5}) = 19.05 \pm 0.22\) [43] and on the Galactic center, for which the corresponding J-factor is in the range \(\log_{10}(J/\text{GeV}^2\text{cm}^{-5}) = 22 - 23\) depending upon the chosen dark matter density profile [44]; here we choose an intermediate value, \(\log_{10}(J/\text{GeV}^2\text{cm}^{-5}) = 22.5\). As for the solid angle, in the case of Draco we take \(\Delta \Omega = 1.6 \times 10^{-3}\) sr, corresponding to the angular area subtended in the sky, while for the Galactic center we use the solid angle corresponding to a half aperture of 0.5° (\(\Delta \Omega = 2.4 \times 10^{-4}\) sr).

The number of photons coming from a given target with a given J-factor is given by:
\[
N_s = A_{\text{eff}} \cdot T_{\text{obs}} \cdot \phi,
\]
where \(A_{\text{eff}}\) is the effective area of the detector, \(T_{\text{obs}}\) is the time of observation. The total number of collected signal photons must be large enough so that the corresponding signal-to-noise ratio yields a statistically significant detection. We here assume that a number of signal photon \(N_s \sim N_\sigma \sqrt{N_0}\), where \(N_0\) is the number of background photons that corresponds to a detection of statistical significance \(N_\sigma\). As mentioned in the introduction, our main goal is to explore the plausibility of a dark matter signal using future MeV gamma-ray telescopes. To perform this analysis we considered a hypothetical detector with specifications similar to the proposed ASTROGAM detector [17]; specifically, we assume an effective area of \(A_{\text{eff}} = 500\) cm² and an observation time \(T_{\text{obs}} = 1\) year. Using these numbers and requiring a 5σ detection, \(N_\sigma = 5\), we can derive an expression for \(\langle \sigma v \rangle\) in terms of the mass that would guarantee this detection.

\[
\langle \sigma v \rangle > 10 \sqrt{N_0} \frac{1}{J_{\text{Emin}}} \frac{dE}{dE} \frac{dN}{dE} A_{\text{eff}} T_{\text{obs}} \frac{4\pi}{m^2}.
\]

To fully compute the values for \(\langle \sigma v \rangle\) that can satisfy this, we must know the number of background photons \(N_0\) and the integrated gamma-ray spectrum coming from dark matter annihilations. On one hand, we have that the number of background photons \(N_0\) is proportional to the integrated background diffuse gamma-ray spectrum, which we assume, following Ref. [44], to be given by:

\[
\frac{d\phi}{d\Omega dE} = (2.74) \times 10^{-3} \left( \frac{\text{MeV}}{E} \right)^{-2.0} \text{cm}^{-2}\text{s}^{-1}\text{sr}^{-1}\text{MeV}^{-1},
\]

as obtained from a fit to data from COMPTEL [45] and EGRET [46]. For the case of the Galactic center, we...
The goal of this analysis is: given a certain mass in the case of neutral pions, despite that means our ∆E does not always maximizes the detection we picked the maximum possible ∆E for each mass. The results of this analysis for the annihilation into neutral pions is presented in Fig. 2 where we present the number of event photons (left axis) in the energy range ∆E/m_{\chi}. The right axis, corresponding to the dashed lines, shows the corresponding signal to noise ratio N_e/\sqrt{N_b} (N_{\sigma}), a proxy of the statistical significance. The vertical dashed lines represent the maximum energy-range possible for a certain mass in the case of neutral pions. Despite that for all these cases the maximum of the ratio occurs at ∆E/m_{\chi} \sim 5, we chose a ∆E/E \sim 0.9, which is the value that maximizes the signal to noise.

Having performed the optimization analysis described above, we proceeded to compare the values of \langle \sigma v \rangle we need for a 5\sigma detection with the current s-wave Planck constraints for the different final state channels. In Fig. 3 we present the case of dark matter annihilating into \gamma\gamma, \gamma\pi^0 and \pi^0\pi^0, for the Draco dSph. For all three cases, we find that there is a mass range allowed by Planck.
constraints where a signal can be detected, although for the case of neutral pions that is limited to masses very close to the pion threshold. In Fig. 4 we present the cases of dark matter annihilating into $e^+e^-$, $\mu^+\mu^-$ and $\pi^+\pi^-$. The figure illustrates how for charged particles no MeV gamma-ray signal is possible from the dSph Draco due to Planck constraints. In addition, future CMB limits are shown, gray lines, indicating the projected constraints from COrE+ (TEP specification), at the level of $P_{\text{ann}} < 3 \times 10^{-28} \text{cm}^3\text{s}^{-1}\text{GeV}^{-1}$.

Fig. 5 and 6 show the same analysis using the Galactic Center (GC) as the target, and using a diffuse background ten times greater and an angular region of $2.4 \times 10^{-4}\text{sr}^{-1}$. The figures illustrate that CMB constraints are up to four orders of magnitude weaker than the minimal annihilation rates needed for detection of an MeV gamma-ray signal for certain channels; all pair-annihilation final state channels can possibly give a detectable gamma-ray signal from the Galactic center compatible with CMB constraints over the entire mass range under consideration here.

V. DISCUSSION

In this work we have considered the indirect detection of s-wave pair annihilation of dark matter with masses in the MeV range (specifically, $m_{\pi^0} < E < 1 \text{ GeV}$) with future MeV gamma-ray telescopes. We investigated six different annihilation channels ($\gamma\gamma, \gamma\pi^0, \pi^0\pi^0, e^+e^-$ and $\mu^+\mu^-$ and $\pi^+\pi^-$), and we assumed a hypothetical detector with specifications similar to the proposed ASTROGAM telescope [17]. We then determined the optimal integration energy range for every given channel, and calculated the values of $\langle\sigma v\rangle$ for a given mass and annihilation final state giving a 5$\sigma$ detection for the conservative case of a virtually background free target such as the Draco dSph and for the Galactic center. We then compared the required annihilation rate with the current s-wave annihilating dark matter CMB constraints, $f_{\text{eff}}(\sigma v)m_{\chi} < 4.1 \times 10^{-28} \text{cm}^3\text{GeV}^{-1}\text{s}^{-1}$, and with future CMB constraints from COrE+, TEP, at the level of $P_{\text{ann}} < 1.38 \times 10^{-28} \text{cm}^3\text{s}^{-1}\text{GeV}^{-1}$.

Our main results are presented in Figs. 3, 4, 5 and 6. For the cases of dark matter annihilating into leptons and charged pions, Fig. 4 illustrates that constraints exclude the possibility of a detection from a dSph such as Draco, but Fig. 6 shows that a detection is possible from the Galactic center. For the case of monochromatic photons and neutral pions, Figs. 3 and 5 show that a detection is generically possible and compatible with CMB constraints. Our results are overall similar to those presented in Ref. [48], with the exception that our CMB limits were calculated with information on $f_{\text{eff}}$ from each individual channel, and that we use different assumptions for the dark matter density profile, the energy integration range, and the detector specifications. Our conclusions are, as a result of all these different choices, somewhat more optimistic than those reported in [48].

One source of uncertainty in our analysis, as in any similar analysis, is the value of the $J$-factors, i.e. the assumed dark matter density profile. Most of the analysis for dwarf spheroidal galaxies report $\log_{10} J \text{ GeV}^{-2}\text{cm}^{-5} \approx 18.8$ [44, 49] instead of the $\log_{10} J \text{ GeV}^{-2}\text{cm}^{-5} \approx 19.05$ we are using. The difference is due to the maximum angle of integration used to compute $J$. Our analysis is sensitive to this choice, a lower value of $J$ implies stronger constraints on the $\langle\sigma v\rangle$ vs $m_{\chi}$ plane. If the lower $J$-factor is used together with CORE+ constraints, this would preclude detectability for most channels.

On the other side, we also analyzed the case for the Galactic Center, Figs. 5 and 6. Given the much larger possible values for the $J$-factor in this case, the detec-
FIG. 5: Same as in Fig. 3 but for the Galactic center specifications

FIG. 6: Same as in Fig. 4 but for the Galactic center specifications

tion line in the $\langle \sigma v \rangle$ vs $m_\chi$ plane improves considerably, making all previously excluded channels promising for detection, even if we consider CORE+ projection constraints. The key uncertainty here is, however, the level of the background MeV emission in the Galactic center, which is largely unknown.

Finally, the detection limits and constraints were computed assuming s-wave annihilating dark matter, and the p-wave annihilation case was not included since the CMB constraints relaxes considerably, and the prospects for gamma-ray detectability depend largely on the velocity distribution of the target dark matter distribution.

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