Design and simulation of CONWIP in the complex flexible job shop of a Make-To-Order manufacturing firm

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This paper presents a methodology for the design and integration of CONWIP in a make-to-order firm. The approach proposed was applied directly to the flexible job shop of a real manufacturing firm in order to assess the validity of the methodology. After the description of the whole plant layout, attention was focused on a section of the shop floor (21 workstations). The CONWIP system deals with multiple-product families and is characterized by path-type cards and a pull-from-the-bottleneck scheme. The cards release strategy and a customized dispatching rule were created to meet the firm’s specific needs. After the simulation model of the present state was built and validated, the future state to be implemented was created and simulated (i.e. the CONWIP system). The comparison between the two systems achieved excellent results, and showed that CONWIP is a very interesting tool for planning and controlling a complex flexible job shop.

1. Introduction

The market of products having high added value has undergone a profound change in the past decades. Consumers require a variety of products, product quality, quick and reliable delivery times, and short lead times. On the other hand, managers and shareholders ask for minimal work-in-process (WIP) and maximum utilization of resources. For these reasons, modern manufacturing systems are becoming more and more familiar with concepts like flexibility, quality and adaptability to consumers’ demands, particularly when operating in a make-to-order (MTO) environment (Sultana & Ahmed, 2014).

Unfortunately, the above mentioned goals (i.e. variety, quality, short lead times, minimal WIP and maximum utilization of resources) appear to be conflicting: one of the main objectives of modern production planning and control systems is to find a compromise solution amongst them (Lengyel et al., 2003). The first systems that tried to attain such a solution are the well-known master production schedule (MPS), material requirement planning (MRP) and manufacturing resource planning (MRPII) (Gibson et al., 1995). They have been (and they still are) excellent long term planning, scheduling and control tools (Vollman et al., 1997), but they have also revealed a series of problems which are often associated with push systems (Lambrecht & Decaluwe, 1988; Ramsay et al., 1990; Adetunji &
Pull systems, on the other hand, instead of scheduling the start of jobs, authorize them. The best known pull system is kanban (the Japanese word for card), described and analysed in depth by Hall (1981), Ohno (1988) and Monden (1998). MRP is generally considered to be applicable to many more manufacturing firms than kanban is. However, kanban seems to produce superior results when it can be applied (Spearman et al., 1990). Hodgson and Wang (1991) also assert that push and pull control strategies have different advantages and disadvantages, and that combinations of push and pull strategies may be easier to implement and may achieve better results than either pure push or pure pull. After this study, several researchers tried to combine these two types of control systems (Flapper et al., 1991; Larsen & Alting, 1993; Villa & Watanabe, 1993, to name a few). Spearman et al. (1990) proposed a hybrid production planning and control system called CONWIP (CONstant Work In Process or, as some researchers argue, CONtrolled Work In Process), with the objective of sharing the positive aspects of pull systems with the wide applicability of push systems. Although this system is relatively recent, Framinan et al. (2003) report that the acronym CONWIP was firstly coined in 1988 and its basic mechanics dates as back as 1963.

Since 1990, CONWIP has been the object of research from many points of view, especially by comparing it with scheduling and control systems such as MRP, JIT and synchro-MRP (for a literature review and description of synchro-MRP see Bertolini et al., 2013). According to Benton and Shin (1998), the studies in literature that simultaneously address push/pull systems (MRP/JIT) can be classified into comparison studies and integration studies, and their approach may be either conceptual (broader and more general) or analytical (narrower and more specific); in analytical comparison and integration studies, methods like simulation and mathematical analysis are the most frequently used. Amongst these studies, Geraghty and Heavey (2004), Yang et al. (2007), Koulouriotis et al. (2010) and Chong et al. (2013) have focused on advantages (or disadvantages) of a CONWIP system and on his potential improvements. Sharma and Agrawal (2009) used AHP algorithm to compare kanban, CONWIP and a hybrid system proposed by Bonvik et al. (1997). Other studies of CONWIP simulate a whole supply chain, such as the works by Rubiano Ovalle and Crespo Marquez (2003), Özbayrak et al. (2006), Pettersen & Segestedt (2009), or even extend the use of CONWIP to Project Management (Anavi-Isakow & Golany, 2003). Some papers also evaluate performances of CONWIP by studying card setting and control (Framinan et al., 2006; Renna, 2010; Braglia et al., 2011) or simulate a simple production system (Huang et al., 1998; Duri et al., 2000). However, though most of the papers claim that CONWIP is superior to both MRP and JIT (Roderick et al., 1994; Huang et al., 1998; Pettersen & Segerstedt, 2009), all the previously mentioned studies suffer from one specific limitation: they fail to address the integration of CONWIP into the shop floor of a real complex firm. Preliminary work on this matter was undertaken by Li (2010), although his main focus is the coordination of layout change and quality improvement, rather than general guidelines for the integration of CONWIP into MTO systems. In order to attempt to fill this gap, this paper presents a simulative study for the design and integration of CONWIP into the flexible job shop of an MTO firm, operating with a general job shop configuration. The study is developed in cooperation with a well-known firm, world leader in the manufacturing and assembling of oil hydraulic accessories.

According to Stevenson et al. (2005), different shop floor configurations are available for MTO industries, namely (i) pure flow shop, (ii) general flow shop, (iii) general job shop and (iv) pure job shop. Key differences among these configurations are the direction of material flow and the degree of customization (for further details on flow routing matrices see Enns, 1995). Besides, Mahdavi et al. (2010) suggest that a flexible job shop is characterized by the presence of a set of workstations in which an operation may be performed by any machine/assembly station of the work centre.

The remainder of the paper is organized as follows: in Section 2 we will present and briefly describe the proposed approach. This approach was directly implemented in an industrial case of relevance which sets a good example and assesses the validity of our approach. The case study is presented in Section 3: after a description of the firm, subsections 3.1 to 3.11 scrupulously follow and apply the
guidelines of the proposed approach. Finally, Section 4 describes and analyses the results of the simulation and Section 5 reports conclusions and possible future developments.

2. The proposed approach

The proposed approach for the design and integration of CONWIP into the flexible job shop of a real manufacturing system is similar to the one proposed in Bertolini and Romagnoli (2013), and structured according to Table 1.

Table 1
Steps of the proposed approach

| Step | Guideline |
|------|------------|
| 1    | Classify workstations and machines |
| 2    | Group jobs in families |
| 3    | Connect every family with an average value of Cycle Time (CT) and Sample Standard Deviation (SSD) |
| 4    | Choose characteristics of the CONWIP system |
| 5    | Define the cards release strategy |
| 6    | Define a dispatching rule |
| 7    | Build the simulation model of the current state |
| 8    | Validate the simulation model |
| 9    | Build the simulation model of the future state |
| 10   | Simulate the future state |
| 11   | Analyze results |
| 12   | Possibly implement the simulated future state |

The first step of the approach consists in the identification and classification of workstations and machines, and in most cases can be directly achieved from the shop floor. Afterwards, the investigation moves from workstations and machines to jobs, and it is often necessary to group jobs into families. This last statement is particularly appropriate for job shops, and one of the instructions on how to group jobs is to attribute a single routing to each family, when possible. Every job family must then be connected with an average value of CT and SSD, prior to the selection of the general characteristics of the CONWIP system to be implemented (steps 3 and 4). Strict attention must be paid to the cards release strategy (step 5), i.e. a general characteristic of the CONWIP system that much too often defines the behaviour of the future state. Together with the cards release strategy, it is also important to define a dispatching rule, so as to sort jobs as they arrive at machines. Afterwards, the simulation model must be built and validated, i.e. the as is state of the system must be reproduced by a simulation model that is an accurate representation of the real system. Once the simulation model of the as is state has been built and validated, the future state model can be built and its critical parameters can be determined. Finally, the future state is simulated (step 11) and, after an analysis of the results it has produced, possibly implemented (step 12).

3. Industry application

The firm we collaborated with is a joint-stock company that designs and produces hydraulic pumps and motors. Attention was focused on the assembly phase of oil hydraulic pumps. Main objectives of this company are the high quality of end products, high flexibility in product design and manufacturing, and a strong commitment to short delivery times. In order to meet these goals, rigorous testing is carried out on every product and several customizations are available to customers. The company produces through a mix of job production and batch production methods, and its manufacturing philosophy follows an assemble-to-order production approach for 1/3 of the products, whilst the remaining 2/3 follow a MTO approach (and, rarely, an engineer-to-order approach). Despite its complexity, as often happens in real enterprises, the main production approach of the firm is MTO.
Given the wide variety of manufacturing methods and philosophies, as well as the need for high production flexibility, the company’s organization follows a flexible general work shop layout, where the following characteristics can be found:

- each job passes through a different number of workstations;
- on some WSs, operations may be performed by any machine/assembly station of the work centre;
- the routing may be different from job to job;
- CTs on each machine are often different from job to job;
- the workflow is not unidirectional, though a dominant flow direction exists.

In the present configuration, production planning and control is completely based on a push system (MRP) with EDD dispatching rule and expediting. With a classic MRP system, the firm exercises direct control on throughput and indirect control on WIP; for this reason, in order to ensure the maximum production rate, every station is provided with a certain load (i.e. a certain amount) of parts to be processed, so as to avoid starvation, even if this condition highly increases the WIP. As a matter of fact, the current situation relies on an operator who daily verifies all the orders that must be dealt with and short lists the priority ones.

An analysis of the flow times of any product code shows how, with an average flow time of 10 working days, effective flow times range from 1 to 100 days. A first attempt at controlling flow times was made in early 2007 by adopting assembly kits (set of all parts needed to assemble a given product). This solution became necessary so as to allow a fixed position assembly line to deal with a wide range of different products.

The plant layout of the company is divided into different areas: (i) machining and quality control area, (ii) acceptance and storage area, (iii) assembling and testing area, (iv) finished product storage area. Our attention focused on the assembling and testing area (iii), core business of the company.

3.1 Classify workstations and machines

The workstations (WSs) of the assembling and testing area of the plant are reported and classified in Fig. 1. Note that the organization of Fig. 1 is mainly illustrative, because product routings are often not linear (i.e. not from top to bottom) and they seldom call at every zone of the assembling and testing area. For these reasons, as well as for the sake of comprehensibility, materials and information flow are not reported in Fig. 1.

![Fig. 1. Workstations (WSs) of the assembling and testing area and their classification](image-url)
The attention of the study was directed to the assembling and testing area because this is the core business of the firm itself. As Fig. 1 shows, this area can be divided into six zones between raw material inventory and finished goods inventory: (i) pre-assembling, (ii) assembling, (iii) pre-testing, (iv) testing, (v) post-testing, (vi) painting and shipping.

The **pre-assembly zone** (2 WSs) is the junction point between the inbound stock point and the assembly zone: here the list of products to be manufactured is supplied by the MRP, and the workers, i.e. 4 people per shift on two 8-hour shifts a day, fill the assembly kits according to the Bill Of Materials.

The **assembly zone** (5 WSs) of the plant works on a single 8-hour shift and roughly assembles 2,600 products per day. The assembly operations vary according to the product variant; they can be carried out on a fixed-position assembly layout or an unpaced multi-model assembly line (for a classification of assembly lines see Scholl, 1999). This zone is directly fed by the pre-assembly zone and the assembly lines are divided as follows:

- aluminium – 4 mixed-model unpaced assembly lines. Each line counts 3 assembly stations (i.e. 3 workers) that perform all of the assembly operations;
- cast iron – 2 mixed-model unpaced assembly lines. Each line counts 3 assembly stations;
- piston pumps – 3 fixed-position multi-model assembly lines. Each line counts 2 workers that pre-assembles products (if necessary) and carry out the entire assembly process;
- special products – 6 fixed-position multi-model assembly lines. Each line counts 1 worker who pre-assembles products (if necessary) and carries out the entire assembly process;
- other products – 1 fixed-position multi-model assembly line with 1 worker.

The main difference between the aluminium and the cast iron assembly lines is that the latter needs a subassembly operation for the mounting of bushings and bearings on the casing.

Within the **pre-test zone** (1 fixed-position multi-model assembly line with 1 worker), jobs coming from the assembly zone may be modified and adapted to the following test zone. Examples of adjustments may be the assembling of multiple flow pumps, such as the cast iron-aluminium double pump or the piston-gear double pump. In order to assemble multiple pumps (i.e. WIP coming from different assembly lines), the synchronization of jobs is very important at this stage.

The **test zone** (7 WSs) is fed by the assembled products and processes every item; since product and routing variability is very wide, the number of products entering the testing queue experience great variability too. The testing zone includes a total of 12 test benches: 2 benches each for WS10 to WS14, and 1 bench for WS9 and WS15. The entire work cycle of the pump is performed at these benches and burrs are created so as to ensure better operating conditions of the end product. As at the assembly zone, testing WSs and benches are classified according to the jobs they process. In this case, however, distinctions are not so important, since most of the benches may test most of the products (at the price of significantly longer setup times).

The test phase also verifies if the performances of the products comply with standards; if this should not be the case, the products are to undergo repairs and a new test is performed. The average defect rate is 2.5% and is not dependent on product family, batch, shift or raw materials (i.e. random). Since the testing zone processes more items than the assembly zone (because of repairs) and has long CTs (up to 45 minutes), it works on three 6.5-hour shifts per day.

The **post-test zone** operates on a single 8-hour shift per day, and counts 4 WSs with 1 worker each (fixed position). Repairs and other post-testing operations are performed here, so as to identify and solve problems that may arise during the testing phase.
In the **painting and shipping zone** (2 WSs) items are painted and prepared for shipping, when needed. Before shipping, purchase orders must be fulfilled, i.e. all the items must be synchronized. This zone is directly fed by the post-test zone and works on a single 8-hour shift per day.

A close analysis of the firm suggests that the plant bottleneck is located at the test zone: indeed, these WSs appear to be the ones with the highest long term utilization (hence they work on three shifts per day), because of long CTs and the need to test every product at least once (or even twice, if repairs are needed).

### 3.2 Group jobs into families

The description hitherto presented has not mentioned CTs, SSDs and production rates of each workstation of the plant. All of these data, in fact, may be measured for each job at each WS, but there are far too many to manage. The number of different product codes, in fact, is roughly equal to 25,000, with an average process batch of 10 parts, while the workstations identified in this part of the plant amount to 21. For this reason, jobs were grouped into families with the same routing so as to allow the (future) simulation processes. The number of jobs was reduced from 25,000 different jobs to 195 different routings, each one passing in the same sequence through 21 WSs, though not necessarily through the same machine/assembly station at each WS.

### 3.3 Connect every family with an average value of CT and SSD

Each family of products was then associated with the total part number, average CT and SSD of all the product codes and part numbers belonging to it. The average CTs ($\bar{t}_{i,n}$) and SSDs ($s_{i,n}$) of every product family at each workstation were calculated as follows.

\[
i = 1 \text{ to } 195 \quad [n] \quad \text{family of products } F_i
\]

\[
j = 1 \text{ to } N_i \quad [n] \quad \text{number of jobs belonging to } F_i
\]

\[
p_{j,i} = 1 \text{ to } N_{j,i} \quad [n] \quad \text{number of parts belonging to } J_i
\]

\[
WS_n \quad n = 1 \text{ to } 21 \quad [n] \quad \text{workstations}
\]

\[
t(P_{j,i} ; n) \quad [\text{min}] \quad \text{cycle time of } P_{j,i} \text{ at } WS_n
\]

\[
\bar{t}_{i,n} \quad [\text{min}] \quad \text{average CT of } F_i \text{ at } WS_n
\]

\[
s_{i,n} \quad [\text{min}] \quad \text{sample standard deviation of } F_i \text{ at } WS_n
\]

and

\[
\bar{t}_{i,n} = \frac{\sum_{j=1}^{N_i} \sum_{p_{j,i}=1}^{N_{j,i}} t(P_{j,i} ; n)}{\sum_{j=1}^{N_i} N_{j,i}} \quad (1)
\]

\[
s_{i,n} = \sqrt{\frac{\sum_{j=1}^{N_i} \sum_{p_{j,i}=1}^{N_{j,i}} [t(P_{j,i} ; n) - \bar{t}_{i,n}]^2}{\sum_{j=1}^{N_i} (N_{j,i}) - 1}} \quad (2)
\]

Table 2 reports the routing, $\bar{t}_{i,n}$ and $s_{i,n}$ for families from 1 to 5 according to Eq. (1) and Eq. (2) (see also Bertolini & Romagnoli, 2013). For example, a part belonging to $F_3$ will visit $WS_3$ with an average CT of 0.73 min and a SSD of 0.094, then $WS_8$ with an average CT of 1.39 min and a SSD of 0.176 etc. Families in Table 2 are arranged in decreasing order of the total number of parts ($\sum_{j=1}^{N_i} N_{j,i}$). In the same way, routings, average CTs and SSDs were calculated for the 195 families. The data reported in Table 2 suggest the following considerations:
- since values of CT and SSD are connected with families of different products (even if sharing the same routing), it may be that several products of a family experience simple operations at some WSs, and this leads to short average CTs;
- it often happens that WS$_1$ and WS$_{21}$ experience simple operations (such as applying stickers or preparing small kits) and this leads to short CTs at these WSs;
- sometimes post testing operations only involve visual inspections on products;
- finally, it may be seen that, though a dominant flow direction exists between WSs (i.e. ascending order), the workflow is not unidirectional (see for example F$_1$).

| Family | Workstation | Average CT [min] | Sample Standard Deviation [min] |
|--------|--------------|------------------|---------------------------------|
| F$_1$  | WS$_{17}$    | 0.31             | 0.101                           |
|        | WS$_1$       | 0.08             | 0.021                           |
|        | WS$_3$       | 5.13             | 1.857                           |
|        | WS$_{11}$    | 1.95             | 0.730                           |
|        | WS$_{18}$    | 0.46             | 0.078                           |
|        | WS$_{21}$    | 0.15             | 0.046                           |
| F$_2$  | WS$_1$       | 0.60             | 0.071                           |
|        | WS$_3$       | 5.13             | 0.920                           |
|        | WS$_{12}$    | 3.61             | 0.943                           |
|        | WS$_{18}$    | 0.55             | 0.067                           |
|        | WS$_{21}$    | 0.14             | 0.058                           |
| F$_3$  | WS$_3$       | 0.73             | 0.094                           |
|        | WS$_8$       | 1.39             | 0.176                           |
|        | WS$_{14}$    | 3.71             | 1.066                           |
|        | WS$_{18}$    | 0.20             | 0.022                           |
| F$_4$  | WS$_3$       | 5.17             | 1.870                           |
|        | WS$_{11}$    | 1.81             | 0.504                           |
|        | WS$_{21}$    | 0.13             | 0.047                           |
| F$_5$  | WS$_8$       | 1.44             | 0.220                           |
|        | WS$_{13}$    | 3.83             | 1.535                           |
|        | WS$_{20}$    | 1.83             | 0.728                           |

### 3.4 Choose characteristics of the CONWIP system

After a close examination of the production system, we chose to simulate the implementation of a CONWIP production plan and control with multiple-product families and the following features (see Hopp & Spearman, 2008):

- **pull-from-the-bottleneck scheme**: cards trigger strategy is based on the bottleneck status, where the bottleneck was identified at the test zone, i.e. at WS$_9$ to WS$_{15}$. This means that cards only flow from the beginning of each routing to the test zone, and the WIP level is held constant in the WSs up to and including the bottleneck;

- **path type cards**: each card defines the WS in which testing will follow (i.e. the 7 testing WSs, from WS$_9$ to WS$_{15}$), and therefore product families will be grouped according to their testing WSs. This choice leads to 7 different types of cards and offers the following advantages: (i) setup times at testing workstations are shorter because test benches are dedicated; (ii) WIP...
traceability is higher, because we already know in which queue (in front of a testing workstation) the product will be waiting for processing; (iii) boxes (or posts) for CONWIP cards are smaller, though increased in number, and this improves internal logistics;

- **common unit to measure WIP**: the sum of the working capacities (in minutes) that all the jobs released will occupy at the 7 testing WSs.

Current characteristics of the shop floor and assumptions made for the simulation of the present and future states of the system are summarized in Table 3.

### Table 3

| Element of comparison | Factory conditions | Simulation (AS IS) | Simulation (TO BE) |
|-----------------------|--------------------|--------------------|--------------------|
| **Scheduling system** | MRP                | MRP                | Pull-from-the-bottleneck CONWIP with path type cards |
| **Dispatching rule**  | EDD                | EDD                | \((\text{Due Date} - \alpha) - \frac{\text{number of jobs in process}}{\text{total number of jobs}}\) |
| Correction on dispatching rule | Expediting | None | Value of \(\alpha\) and percentage of jobs in process belonging to the same purchase order |
| **WIP**               | Not controlled     | Not controlled     | Limit on the total load (i.e. sum of occupied capacities) of all jobs to the testing WSs |
| Part transfer         | Negligible         | Not considered     | Not considered     |
| Number of jobs        | 25,000             | 195 families       | 195 families       |

3.5 Define the cards release strategy

The logic behind the releasing of the cards is illustrated below.

\[
WS_n \ n = 9 \text{ to } 15 \quad [n] \quad \text{WS of the testing zone}
\]

\[
f_n = 1 \text{ to } M_n \quad [n] \quad \text{number of jobs released that will be tested at } WS_n
\]

\[
L_n \quad [\text{min}] \quad \text{maximum product load at } WS_n \text{ (working minutes)}
\]

\[
RC_n \quad [\text{min}] \quad \text{residual capacity at } WS_n
\]

\[
OC_{J,n} \quad [\text{min}] \quad \text{occupied capacity by job } J \text{ at } WS_n
\]

\[
OR_{J,n} \quad [0; 1] \quad \text{releasing of a card for job } J \text{ that will be tested at } WS_n
\]

\[
OF_{J,n} \quad [0; 1] \quad \text{finishing of job } J \text{ at } WS_n
\]

In this context, each one of the 7 testing WSs (let’s say WS\(_{11}\)) will process a maximum number \(M_n\) of jobs. In the same time, WS\(_{11}\) is characterized by a **product load** \((L_{11})\), i.e. the process variable that indicate the maximum total amount of WIP (expressed in testing minutes at station 11) allowed in the system for that specific working station, and by two variables, **residual capacity** \((RC_{11})\) and the **capacity occupied** by a general job \(J\) \((OC_{J,11})\).

Each job \(J_{11}\) released in the system will occupy an average capacity of \(OC_{J,11}\) testing minutes at WS\(_{11}\), and the residual capacity of a general WS\(_n\) is defined in Eq. (3).

\[
RC_n = L_n - \sum_{j=1}^{M_n} OC_{J,n}
\]
As Eq. (3) shows, $RC_n$ is always less than or equal to $L_n$. By means of $RC_n$ the system deals with the possibility of releasing new cards for jobs that will be processed at WS$_n$, as is shown below.

**Initialization of the system**

\[
OR_{J,n} = 0 \\
OF_{J,n} = 0 \\
\text{for } n = 9 \text{ to } 15 \text{ do} \\
RC_n = L_n \\
J_n = 1 \\
\text{if } RC_n > 0 \text{ then } OR_{J,n} = 1 ; J_n = J_n + 1 ; RC_n = RC_n - OC_{J,n} \\
\text{else } OR_{J,n} = 0 \\
\text{end if} \\
\text{next}
\]

**Running phase**

\[
\text{if } OF_{J,n} = 1 \text{ then } RC_n = RC_n + OC_{J,n} \\
\text{if } RC_n > 0 \text{ then } OR_{J,n} = 1 ; J_n = J_n + 1 ; RC_n = RC_n - OC_{J,n} \\
\text{else } OR_{J,n} = 0 \\
\text{end if}
\]

The first loop previously illustrated (initialization of the system) ends when all residual capacities are not positive, so no other card can be released in production. Afterwards, during the running phase, when the capacity of a general $J_n$ is freed (for its test has finished), the $OC_{J,n}$ is released and if $RC_n$ becomes positive, the card for a new job to be tested at WS$_n$ will be released. In this way, we achieve a CONWIP system capable of keeping WIP under control up to the bottleneck through path type cards by measuring WIP in minutes of occupied capacity at the testing workstation (WS$_n$). Once released, jobs follow their routing up to the testing zone: each time a job $J_n$ finishes its test, the value of the occupied capacity of $J_n$ ($OC_{J,n}$) is added to the residual capacity of WS$_n$ ($RC_n$), where $n$ is the WS in which the testing of $J_n$ takes place. Fig. 2 shows a diagram of this process. As can be seen in Fig. 2, another main difference between the current and the future state is the organization of the backlog list. By now, the backlog is a list of jobs to be processed sorted according to the EDD rule. In the future state, backlogs will be created for each testing WS, so as to create 7 different backlog lists associated with WS$_9$ to WS$_{15}$. Section 3.6 explains how jobs will be released into the system from the backlog list, as well as how they will be dispatched when queueing in front of a processing workstation.

**3.6 Define a dispatching rule**

According to the specific needs of the firm, the following goals were identified as guidelines for the scheduling problem:

- punctuality on delivery of customer orders;
- synchronization of customer orders (when belonging to the same purchase order);
- priority to hot jobs.

Jobs are defined as being *hot* when belonging to an important purchase order and coming from priority customers, i.e. when the delay will cause serious damage to a *hot* customer. Purchase orders are independent, and an analysis of the firm’s database showed that jobs were equally parted in hot (50%) and normal (50%).
We referred to the Pinedo approach (Pinedo, 2002) $a \mid b \mid c$, which indicates:
- $a =$ machine environment, *Flexible Job-shop* with 21 stages of parallel machines (*FJ$_{21}$*);
- $b =$ processing characteristics and constraints, *Release Time* ($r_j$);
- $c =$ objectives, which are (i) average job *Tardiness*, (ii) average *Staging Time* and (iii) average *Weighted Lateness* of purchase orders. The weight criterion, $w$, is set equal to 10 for *hot* jobs and 1 for *normal* jobs, and the Staging Time is equal to the wait-to-match time (i.e. the time some parts ‘wait’ because of lack of synchronization of purchase orders).

According to Thiagarajan and Rajendran (2005), the dispatching rule for product families shall be a mix of:
- *EDD* in order to apply a control on items punctuality;
- *NUJOB*, modified so as to manage the synchronization of different jobs belonging to the same purchase order;
- application of factor $\alpha$, which indicates the advance we plan to have (measured in number of days ahead of schedule, when $\alpha > 0$) so as to consider the importance of a *hot* order.
This leads to the following dispatching rule, where the fraction considers the ratio between the number of jobs already in process and the total number of jobs belonging to the same purchase order (see also Table 3):

\[
\text{Dispatching rule: } (\text{Due Date} - \alpha) - \frac{\text{number of jobs in process}}{\text{total number of jobs}}
\]  

(4)

3.7 Build the simulation model of the current state

The simulation model that has been used is a discrete, dynamic and stochastic discrete-event simulation model, implemented in an object-oriented software, Simul8 (release 12). The model of the assembling and testing area has been organized in 21 workstations, with a variable number of parallel machines, and the simulation of each workstation was made with the utilization of \( \bar{\tau}_{i,n} \) and \( s_{i,n} \), according to the product family (see Section 3.3). CTs and SSDs used in this model refer to year 2008. They are represented as normal distributions with \( \mathcal{N}(\bar{\tau}_{i,n} ; s^2_{i,n}) \).

Replicating the conditions of the actual shop floor attentively, we created all the connections between job-shops and stock points, in order to simulate the routings of 195 product families \( F_i \). For the purposes of the simulation, Simul8 software was linked to several MS Excel worksheets, so as to allow the processing of a greater number of data (to the detriment of simulation times).

3.8 Validate the simulation model

Particular attention was paid to the validation of the current state model. The steady state was graphically identified after a start-up period of 20 working days by monitoring the reciprocal of the standard deviation of daily production rate (see Fig. 3).

![Fig. 3. start-up period definition](image)

We then carried out 10 consecutive simulation runs of the current state, each lasting one year, and analysed their output, i.e. the average values of response variables.

Model validation was implemented by controlling the results we obtained for the following variables: (i) average daily production, (ii) average weekly WIP, (iii) average flow time and (iv) average job tardiness. Table 4 reports the comparison between data retrieved from the firm’s database and the ones obtained with the simulation. Since every response variable, obtained through the simulation model, is close to the reference data from the database, the model is consistent.
Table 4
Comparison between data from the firm’s database and the simulation (AS IS) for the validation of the model

| Validation parameters | Industry database | Current state simulation | Comparison |
|-----------------------|-------------------|--------------------------|------------|
| Average daily production (parts) | 2,600 | 2,615 | + 0.6% |
| Average weekly WIP (parts) | 18,000 | 17,630 | - 2.1% |
| Average flow time (days) | 9.2 | 8.7 | - 5.8% |
| Average job tardiness (days) | 7.2 | 7.8 | + 8.3% |

3.9 Build the simulation model of the future state

Once the validation of the current state was implemented, the future state model was built, in order to simulate a system with the characteristics described in Sections 3.4 to 3.6. Only two important process factors still need to be determined for the optimization of the future state, i.e. the maximum value of WIP allowed in the system and the value of $\alpha$, the planned advance in due date for hot jobs (see Sections 3.4 and 3.5). Factors and levels at this step were chosen by mutual consent with the firm’s management, and they are reported in Table 5. We have proceeded with a quick Design Of Experiment (DOE) applied to the simulation process, according to Montgomery (2001).

Table 5
Factors and levels for the future state

| Factors | Lower Level (-) | Higher Level (+) |
|---------|------------------|------------------|
| A $\alpha$ - days ahead of schedule for important orders (days) | 5 | 10 |
| B WIP - sum of working minutes at testing WSs (minutes) | 28,500 | 34,200 |

Table 6
Design matrix and results of the $2^2$ factorial analysis

| A | B | R_1 Average job Tardiness | R_2 Average Staging time | R_3 Average Weighted Lateness of purchase orders |
|---|---|---------------------------|--------------------------|-----------------------------------------------|
| (1) | 5 | 28,500 | 9.45 | 4.06 | 30.85 |
| a | 10 | 28,500 | 10.32 | 4.00 | 14.16 |
| b | 5 | 34,200 | 9.06 | 4.00 | 19.20 |
| ab | 10 | 34,200 | 8.36 | 4.25 | 24.63 |
| $A_1 = 0.09$ | $A_2 = 0.10$ | $A_3 = -5.63$ |
| $B_1 = -1.18$ | $B_2 = 0.10$ | $B_3 = -0.59$ |
| $AB_1 = -0.79$ | $AB_2 = 0.15$ | $AB_3 = 11.06$ |

Response variables are reported in Section 3.6 (i.e. objectives of the $a \mid b \mid c$ Pinedo approach). We applied a full factorial design and made a $2^2$ sampling campaign with 10 replications. Replications were made by conducting “Trials” in the simulation software (i.e. a series of runs performed with all the same parameters in the simulation except for the random numbers). Results are displayed in Table 6, where each design point is characterized by a factor-level combination and an average outcome of the three response variables ($R_1; R_2$ and $R_3$); at the same time, each response variable is related to the main effect of factor A and B and to the interaction effect (AB). Table 7 reports the ANOVA of the factors related to the three response variables.
Table 7
ANOVA of the three response variables

R1 - Average tardiness

| Source of variation | Sum of squares | DoF | Mean square | F0   | P-value |
|---------------------|---------------|-----|------------|------|---------|
| A                   | 0.08          | 1   | 0.076      | 0.129| 0.721   |
| B                   | 13.80         | 1   | 13.800     | 23.415| 0.000   |
| AB                  | 6.16          | 1   | 6.159      | 10.449| 0.003   |
| Error               | 21.22         | 36  | 0.589      |      |         |
| Total               | 41.25         | 39  |            |      |         |

R2 - Average staging time

| Source of variation | Sum of squares | DoF | Mean square | F0   | P-value |
|---------------------|---------------|-----|------------|------|---------|
| A                   | 0.09          | 1   | 0.091      | 0.491| 0.488   |
| B                   | 0.09          | 1   | 0.088      | 0.477| 0.494   |
| AB                  | 0.25          | 1   | 0.251      | 1.357| 0.252   |
| Error               | 6.67          | 36  | 0.185      |      |         |
| Total               | 7.10          | 39  |            |      |         |

R3 - Average weighted lateness

| Source of variation | Sum of squares | DoF | Mean square | F0   | P-value |
|---------------------|---------------|-----|------------|------|---------|
| A                   | 316.85        | 1   | 316.848    | 64.513| 0.000   |
| B                   | 3.50          | 1   | 3.498      | 0.712| 0.404   |
| AB                  | 1,223.12      | 1   | 1,223.125  | 249.039| 0.000   |
| Error               | 176.81        | 36  | 4.911      |      |         |
| Total               | 1,720.28      | 39  |            |      |         |

As it can be seen from Table 7, response variable number 2 (average staging time) is not influenced by any of the factors (minimum p-value is 0.252). However, factor B (WIP) significantly influences average job tardiness (R1), and factor A (alpha) influences average weighted lateness of purchase orders (R3); furthermore, both R1 and R3 are influenced by the interaction between the factors (AB). If we go back to Table 6, we can deduce that B1 (i.e. the main effect of B measured on R1) is negative but small; that is an increase of B slightly diminishes average job lateness (which is good). On the other hand, A3 is negative but relatively big; and this means that an increase of A significantly diminishes average weighted lateness of purchase orders. Furthermore, the interaction AB3 is positive and big, and this means that, in order to limit R3, the factors must not be both at the high (or low) level (i.e. no ab and no (1) combinations are recommended).

For these reasons, the best configuration was found to be design point a:

- WIP = 28,500 minutes
- α = 10 days

3.10 Simulate the future state

The results of the simulation and the comparison between the current and the future state of the system are reported in Fig. 4 and Table 8. Fig. 4 graphically shows the comparison in average WIP (parts/week), while Table 8 reports average values and standard deviations in production, WIP, flow times, job tardiness, staging times and weighted lateness.
Fig. 4. Comparison between WIP average levels (thousands of parts per week)

Table 8

|                        | as is | to be | Comparison |
|------------------------|-------|-------|------------|
| **Production [parts/day]** |       |       |            |
| Average                | 2,615 | 2,561 | -2.1%      |
| Std Dev                | 12.7  | 18.7  | +47.6%     |
| **WIP [parts/week]**   |       |       |            |
| Average                | 17,630| 10,238| -41.9%     |
| Std Dev                | 749   | 325   | -56.6%     |
| **Flow time [days]**   |       |       |            |
| Average                | 8.67  | 5.28  | -39.1%     |
| Std Dev                | 0.65  | 0.31  | -52.3%     |
| **Job Tardiness [days]** |       |       |            |
| Average                | 7.80  | 10.32 | +32.3%     |
| Std Dev                | 0.66  | 0.63  | -4.5%      |
| **Staging Times [days]** |       |       |            |
| Average                | 7.24  | 4.00  | -44.8%     |
| Std Dev                | 0.43  | 0.62  | +44.2%     |
| **Weighted Lateness [days]** |       |       |            |
| Average                | 22.00 | 14.16 | -35.6%     |
| Std Dev                | 4.69  | 5.26  | +12.2%     |

3.11 Analyse results

Let us consider the outcome of Fig. 4 and Table 8: the average level of WIP (parts/week) is greatly reduced in both its average value (-41.9%) and its standard deviation (-56.6%); the same results could be achieved by measuring WIP in total working minutes at the testing zone, but this is quite obvious, since this parameter is directly controlled by the CONWIP system. Average flow times are also almost 40% shorter than before, and their standard deviation has decreased by more than 50%.

As a control of the dispatching rule adopted, Table 8 also reports the comparison of job Tardiness, Staging Times and Weighted Lateness. It emerges that the future state will increase average job
Tardiness (by more than 30%) without significantly modifying its standard deviation. This result is due to the importance given to hot jobs and to the synchronization of purchase orders. In fact, the application of the dispatching rule (Section 3.6) leads to significant reductions in average Staging Times and Weighted Lateness. In both cases, the increase in their standard deviations can be ascribed to the importance given to hot jobs.

Finally, the average daily production in the future state will be 2% smaller and its standard deviation will be increased, but these are relative losses. In fact, the current system is meeting demand, as often happens in MTO/ETO systems, and the demand profile is highly variable. At present, the plant experiences short order backlogs and high levels of WIP. However, as previously stated, the implementation of the simulated system will lead to lower weighted lateness and a considerable reduction of WIP (to the detriment of order backlogs). Potential consequences of these differences should be gain in market shares, economic savings and, finally, the possibility to invest in new test benches, thus increase bottleneck capacity and productivity.

A visual comparison of results is reported in Fig. 5. We can therefore conclude that the system we have simulated (future state) has fulfilled 2 objectives (out of the three defined) with a significant reduction in flow times and WIP and without significantly affecting the production rate.

Unfortunately, the firm has so far not proceeded with the implementation of the future state, so Section 3.12 is not reported.

4. Conclusions

Modern manufacturing firms need to be planned and controlled by advanced systems. Weak points of push systems were discovered from both the theoretical and practical point of view. Pull systems, on the other hand, usually achieve better results when they can be applied, though their implementation is not so immediate. The paper has presented the simulative implementation of CONWIP in an industrial case (a complex manufacturing firm). The proposed solution consists of a pull-from-the-bottleneck CONWIP with path type cards and a common unit to measure WIP (sum of working capacities occupied at the testing WSs). The approach we followed is first presented in section 2, and then applied to the industrial case (section 3).
The results we have achieved confirm the validity of CONWIP. Average WIP, measured in parts per week, decreased by over 40% and its standard deviation by over 50% without significantly affecting production rate; flow times were also reduced in both their average values and their standard deviation. The reduction in WIP and flow time standard deviations is extremely important, because it can ensure more precise and robust values to rely on when planning production. The dispatching rule we have chosen was evaluated using three indicators that express the system’s capacity to meet management requirements. These indicators are (i) average tardiness, measuring order punctuality, (ii) average staging time, indicating the synchronization of parts belonging to the same purchase order, and (iii) average weighted lateness, reporting the ability to ensure punctuality of hot jobs. All of these indicators were measured in 10 simulation runs and reported in their average values and standard deviations. The synchronization of purchase orders was considerably increased, by reducing average staging time to 4 days (- 44%), and average weighted lateness was decreased by 36%, that is greater attention was paid to hot jobs. Nevertheless, these achievements led to the growth (+ 32%) of average job tardiness, though this result was partially expected: one of the goals of the dispatching rule we adopted is to increase the priority of hot jobs, to the detriment of normal ones and with the increase in average (non-weighted) tardiness. For all of these reasons, we can state that the proposed solution could be an excellent scheduling and control system for the shop floor of a complex manufacturing firm, being integrated in a planning system such as (classic) MRP.

Possible future developments of this study may be the optimization of model factors in a systematic way (i.e. not only relying on practical experience of the firm’s management and common sense). On the other hand, especially when dealing with everyday scheduling problems of the SF, an on-line simulation may be the only way to achieve optimum results in a reasonable amount of time.

Finally, it is important to remark that the main drawback in this approach, even though it is applied to a real manufacturing environment, lies in the impossibility of providing optimum results without the comparison and evaluation of a certain number of different planning and control systems (such as synchro-MRP, workload control and drum-buffer-rope) and/or dispatching rules.

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