Constraints on the structure and seasonal variations of Triton’s atmosphere from the 5 October 2017 stellar occultation and previous observations*

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ABSTRACT

Context. A stellar occultation by Neptune’s main satellite, Triton, was observed on 5 October 2017 from Europe, North Africa, and the USA. We derived 90 light curves from this event, of which yielded a central flash detection.

Aims. We aimed at constraining Triton’s atmospheric structure and the seasonal variations of its atmospheric pressure since the Voyager 2 epoch (1989). We also derived the shape of the lower atmosphere from central flash analysis.

Methods. We used Abel inversions and direct ray-tracing code to provide the density, pressure, and temperature profiles in the altitude range ~8 km to ~190 km, corresponding to pressure levels from 9 μbar down to a few nanobars.

Results. (i) A pressure of 1.18 ± 0.03 μbar is found at a reference radius of 1400 km (47 km altitude). (ii) A new analysis of the Voyager 2 radio science occultation shows that this is consistent with an extrapolation of pressure down to the surface pressure obtained in 1989. (iii) A survey of occultations obtained between 1989 and 2017 suggests that an enhancement in surface pressure as reported during the 1990s might be real, but debatable, due to very few high S/N light curves and data accessible for reanalysis. The volatile transport model analysed supports a moderate increase in surface pressure, with a maximum value around 2005–2015 no higher than 23 μbar. The pressures observed in 1995–1997 and 2017 appear mutually inconsistent with the volatile transport model presented here. (iv) The central flash structure does not show evidence of an atmospheric distortion. We find an upper limit of 0.0011 for the apparent oblateness of the atmosphere near the 8 km altitude.

Key words. methods: data analysis -- methods: observational -- planets and satellites: atmospheres -- planets and satellites: physical evolution -- techniques: photometric

1. Introduction

The large satellite Triton was discovered in 1846, only 17 days after the discovery of its planet, Neptune. An atmosphere was first speculated by Cruikshank & Silvaggio (1979), with the claimed detection of the gaseous CH₄ spectral signature, although in retrospect the features were due to methane ice on the surface. In any case, the presence of this volatile ice did suggest the existence of an atmosphere. This was to be confirmed ten years later, when the NASA Voyager 2 (V2) spacecraft flew by the Neptunian system in August 1989. During this flyby, Triton's tenuous atmosphere (mainly nitrogen N₂) was detected during the Radio Science Subsystem (RSS) occultation, providing its surface density, pressure, and temperature (Tyler et al. 1989). These results were later improved by Gurrola (1995, G95 hereafter), who derived a surface pressure of \( p_{\text{surf}} = 14 \pm 2 \) μbar. The studies that used RSS data did not, however, provide a thermal profile. Dynamical aspects, such as wind regimes, were studied using V2 images of plumes near Triton’s surface (Yelle et al. 1991), as well as vertical profiles of methane and hazes using V2’s UV images (Strobel et al. 1990; Herbert & Sandel 1991; Krasnopolsky et al. 1993; Krasnopolsky 1993; Krasnopolsky & Cruikshank 1995; Strobel & Summers 1995).

Triton is currently experiencing a rare ‘extreme southern solstice’, a configuration that occurs every ~650 years (Fig. 1). In particular, the sub-solar latitude on the satellite reached about 50° S in 2000. The various measurements of Triton's atmospheric pressure using occultations bracket that epoch, from the RSS results in 1989 to the ground-based stellar occultation of 2017 discussed here. In this context, it is interesting to look for ongoing seasonal effects (if any) occurring in Triton’s atmosphere, especially large pressure variations in the last three decades. Such seasonal variations (or its absence) can then constrain global climate models (GCMs) and volatile transport models (VTMs) that account for volatile transport induced by insolation changes.

Since 1989, only a handful of Earth-based stellar occultations have been observed, and there have been a few spectroscopic studies that detected CO and CH₄ in the near-IR (Lellouch et al. 2010) and CO and HCN with the Atacama Large Millimeter/submillimeter Array (ALMA) in the millimetre (Gurwell et al. 2019). As discussed later, the deepest layers accessible during Triton Earth-based occultations (when a central flash\(^1\) is observed) typically lie at 8 km altitude (~9 μbar pressure level). Conversely, the best light curves can provide information up to an altitude of about 190 km, corresponding to a few nanobars.

Here, we report on results obtained from the 5 October 2017 ground-based stellar occultation. Attempts to view this rare event were made from more than 100 sites in Europe, northern Africa, and the eastern USA. We extracted 90 occultation light curves from this campaign, among which 42 show a central flash. This is by far the most observed stellar occultation by Triton ever monitored (and among the most observed event of its kind, all Solar System objects combined) both in terms of latitudinal coverage of the satellite and central flash sampling.

Our goals are to (1) provide Triton’s atmospheric profiles (density, pressure, temperature) derived from this event, (2) compare the results with those obtained from previous occultations, including the V2 RSS experiment, (3) constrain the seasonal variations of Triton’s atmosphere, (4) compare the results with current GCMs, and (5) and derive the shape of the central flash layer.

The 5 October 2017 event is discussed in Sect. 2. The methods used are given in Sect. 3, and in Sect. 4 we present the results. We reanalyse previous events, including a new approach to retrieve new information from the V2 experiment in Sect. 5. In Sect. 6 we discuss the atmospheric seasonal variations, using pressure values from our work and from other works. Section 7 focuses on the analysis of the central flashes. We mention some issues that are to be addressed at a future date in Sect. 8. Concluding remarks are provided in Sect. 9.

2. The 5 October 2017 stellar occultation

2.1. Prediction

In the past two decades, Neptune has been crossing regions with low surface-density of stars. In the early 2010s, faint star surveys up to \( R = 19 \) were made using the Wide Field Imager attached

\(^1\) A central flash is a sharp increase in the intensity of the stellar light observed during a stellar occultation. It is observed near the central path of the occultation shadow and is produced by the refraction of light in the atmosphere of the occulting object.
to the 2.2 m Max-Planck telescope at the European Southern Observatory (ESO; Assafin et al. 2010, 2012; Camargo et al. 2014). They provided many candidates for occultations by Pluto, large Trans-Neptunian Objects and Centaurs, but no suitable Triton events for 2008–2015.

Predicting occultations by Triton is problematic for two reasons: (1) Neptune’s orbit may have systematic errors, causing a systematic shift of Triton’s position with respect to the stars; (2) Triton’s neptunocentric orbit may have systematic errors due to the large brightness and colour differences between Neptune and Triton, and also from changes in Neptune’s magnitude, making their relative colour variable (Schmude et al. 2016). Both points affect differently the ground-based measurements of Triton and Neptune, resulting in a distorted neptunocentric orbit for the satellite. A way to overcome these problems is to use R or I filters to minimise differential refraction during observations and distribute Triton observations evenly along its orbit around Neptune. Triton’s path is then set by the average ephemeris offsets found for right ascension (α) and declination (δ).

In this context, we gathered more than 4700 charge-coupled-device (CCD) images of Triton in R between 1992 and 2016 with the 0.6-m B&C and 1.6-m P&E telescopes at Pico dos Dias Observatory (OPD) in Brazil (IAU code 874). The observations were reduced with the best available astrometric catalogue at that time, the UCAC4 (Zacharias et al. 2013), following the same procedures described in Gomes-Júnior et al. (2015). From the average ephemeris offsets of many nights, and after sigma-clipping, we found an overall offset (Δα cos δ, Δδ) = (+1 ± 45, −16 ± 45) milliarcsecond (mas), with error bars at 1σ level, with respect to the DE435/NEP081 ephemeris from the Jet Propulsion Laboratory (JPL). Applying this offset and searching for post-2015 events, we uncovered the promising occultation by Triton of a relatively bright star with V = 12.7, G = 12.2 (UCAC4 410-143659; Gaia DR2 2610107911326516992) that was to occur on 5 October 2017, crossing all Europe and northern Africa and reaching the eastern USA.

Closer in time to the event, a dedicated 8-night run on the OPD 1.6 m telescope was conducted between 15 and 23 September 2017 to further improve the accuracy of the prediction, in particular to pin down the path of the central flash. The field of view of the images was 6.1′ × 6.1′ with a pixel scale of 180 mas/pixel. At that point, digital coronagraphy (Assafin et al. 2009; Camargo et al. 2015), which mitigates Neptune’s scattered light, proved to be unnecessary. Chromatic refraction corrections to Triton’s position were carried out, but proved to be negligible too, as the observations were made in the I band. Observations from two nights were discarded due to bad weather, but we were able to cover a complete orbit of Triton around Neptune (about 6 days) with more than 1000 images.

Prior to Gaia Data Release 2 (DR2), published in April 2018 (Gaia Collaboration 2016, 2018), the Gaia team released a preliminary Gaia subset DR2 with 431 stars (R = 12–17) surrounding Triton’s path in the sky plane during the eight nights of our run. The main improvement with respect to DR1 is the inclusion of the stars’ proper motions, leading to mas-level accuracy of stellar positions at epoch. Using these reference stars and the PRAIA package (Assafin et al. 2011), we obtained a mean offset (Δα cos δ, Δδ) = (+7.8 ± 5.4, −17.6 ± 2.6) mas with respect to the JPL DE435/NEP081 ephemeris. The corresponding prediction uncertainty was about 60 km cross-track and 8 s in time. Figure 2 displays the mean offset (Δα cos δ, Δδ) for the eight nights, using the Gaia DR2 catalogue. This is a large improvement from a prediction using only the Gaia DR1 catalogue, shifting the shadow path about 370 km to the south in the sky plane, or some 500–700 km when projected on Earth, depending on the station considered, as well as reducing the offsets uncertainties by factors of about 1.5 and 2.2, respectively. Since the run covers a full synchronous revolution, and rotational, period of Triton, the average offset reflects an error in Neptune’s heliocentric position rather than a neptunocentric error in Triton’s ephemeris.

The ± 60 km cross-track uncertainty on the prediction was essential for better planning observations of the central flash, keeping in mind that the width of the region where that central flash is significant (e.g. more than 20% of the unocculted stellar flux; see Fig. 3) typically spans ±100 km in the sky plane.

Fig. 1. Sub-solar latitude on Triton over time. Upper panel: overview of the sub-solar latitude on Triton versus time over the last millennium. The blue part corresponds to the period from the V2 encounter (August 1989) to the 5 October 2017 stellar occultation. It shows that during this interval, Triton experienced an extreme summer solstice in its southern hemisphere, with a minimum sub-solar latitude of 50° S in 2000. Lower panel: close-up view of the upper panel around the year 2000. The black points correspond to occultations observed, distinguishing from the black triangle (V2 RSS experiment). The larger symbols are from the data that we use in this paper.
Table 1. Occultation prediction using Gaia-DR2 position for the star and JPL DE435/NEP081 for Neptune’s and Triton’s ephemerides and the additional offset deduced from the OPD observations.

| Occultation circumstances (5 October 2017) |       |
|------------------------------------------|-------|
| Predicted time of geocentric closest approach | 23h51m38.0s ± 8 s UTC |
| Predicted geocentric closest approach Triton-star | 196 mas |
| Position angle between Triton and star at closest approach | 347.51 deg |
| Geocentric shadow velocity at closest approach | 16.80 km s⁻¹ |
| Retrieved time of geocentric closest approach | 23h51m28.92s ± 0.02 s UTC |
| Retrieved geocentric Triton-star closest approach | 196.58 ± 0.05 mas |

Occulted star (from Gaia DR2)

| Star source ID (stellar catalogue) | 2610107911326516992 |
| Geocentric star position (ICRF) at epoch | α = 22h54m18.4364s ± 0.2 mas, δ = -08°00’08.318” ± 0.2 mas |
| G-mag / RP mag | 12.5/12.0 |
| Stellar diameter projected at Triton’s distance(1) | 0.65 km |

Notes. (1) Using van Belle (1999)’s formulae and magnitudes B = 13.305, V = 12.655 (AAVSO photometric survey) and K = 11.080 (2mass) for the star; see http://vizier.u-strasbg.fr/viz-bin/VizieR

Fig. 2. Average offsets in (α, δ) mas of the eight nights of OPD observations using the preliminary Gaia DR2 catalogue for the astrometric reduction. Positions in lighter colours were not accounted for to compute the average offset, due to lower quality associated with poor weather conditions. Lower panel: number of images taken for each night.

Combining the pre-event Triton’s ephemeris offset with the geocentric astrometric Gaia DR2 position of the occulted star, we obtained the parameters describing the nominal prediction listed in Table 1. This updated prediction was promptly released to the scientific community before the event⁴ and the corresponding map of the shadow track on Earth is displayed in Fig. 4.

2.2. Observations of the occultation

The event was attempted from over one hundred stations in Europe, northern Africa, and the eastern USA, resulting in a total of 90 occultation light curves. Figure 5 displays the corresponding occultation chords and Table A.1 lists the circumstances of observations for the respective sites.

The first part of this table lists the stations that were eventually used in a simultaneous fit to a Triton’s atmospheric template model. The second part of the table lists other stations that were not used because the light curves had insufficient signal-to-noise ratios (S/N) to provide relevant contribution to that fit. The last part of the table provides information on the sites that were involved in the campaign, but could not gather data due to bad weather or technical problems.

The rule we used for deciding to include or not a light curve in the global fit is as follows. The S/N was first estimated by calculating the standard deviation σ of the flux outside the occultation. The resulting S/N 1/σ per data point was then re-calculated for a fixed time interval of one second. Assuming a gaussian noise, this implies a multiplicative factor of \sqrt{1/exposure time} to be applied to the S/N obtained above. Finally, the noise level must be compared to the ‘useful’ information, that is, the actual drop of signal caused by the occultation, not the total signal. This implies a new multiplicative factor of ΔΦ applied to the S/N per second obtained above, where ΔΦ is the flux drop observed during the occultation. Consequently, some light curves were eliminated due to a low contrast caused by light contamination from Neptune (see for instance the Abington, Caserta, Agorala 50 cm, or Catania 28 cm light curves in Fig. C.2).

The normalisation described above then allows us to compared consistently the various datasets. We used a normalised S/N cut-off of ten prior to the global fit. There are a few exceptions to that rule for light curves containing a strong central flash (see for instance the Le Beausset and Felsina data in Fig. C.1). They have a poor overall S/N, but we have kept them in the global fit (without flash; Sect. 4.2) to test the effect of the central flash inclusion (see Fig. 3 and Sect. 7.2). This approach allowed us to ensure that the central flashes provide a shadow centre which is consistent with, but more accurate than the one given by the global fit (see Sect. 7.2).

This said, the cut-off of ten remains somehow arbitrary. We have tested other cut-off values, and we did not obtain any significant changes in the results of the fits presented in the rest of the paper.

The analysis of the light curves (as described in the next section) allowed us to reconstruct the geometry of the event by
Fig. 3. Simultaneous fits of the data (black dots) by synthetic light curves (blue lines), based on the temperature profile displayed in Fig. 10 (black line) and the pressure boundary condition $p_{1400} = 1.18$ µbar (Table 4). The green curves are the residuals of the fits. The lower and upper horizontal dotted lines mark the zero-flux level and the total star plus Triton unocculted flux, respectively. We also note that the three bottom light curves are plotted at a different vertical scale from the others to accommodate the presence of a strong central flash. The stations are sorted from left to right and top to bottom from the northernmost track (St Caprais) to the southernmost track (Calar Alto; see next figure). Each panel has a duration of five minutes and is centred around the time of closest approach (or mid-occultation time) of the station to Triton’s shadow centre, as indicated under the lower left panel in each block of six light curves. For reference, the vertical red line marks the time 23:48 UTC. The stations with exposure times of less than 1 s have been smoothed to have a sampling time as close as possible to 1 s, for easier S/N comparison of the various datasets. We note that in this approach, the sampling of the Constância, Le Beausset, and Felsina Observatory light curves (0.64 s) is kept at its original value so that full resolution versions of the corresponding strong flashes at those stations are displayed here. The same kinds of plots showing all the stations, but with the flashes excluded from the fits, are displayed in Fig. C.1.
providing Triton’s position with respect to the occulted star (see Table 1). The reconstructed geometry of the occultation implies a shift of $(\Delta \alpha \cos \delta, \Delta \delta) = (-7.2, +0.6)$ mas of Triton’s position with respect to the latest prediction described in the previous section. This means that the occultation occurred about 9 s earlier than expected, and that the shadow centre was 12 km north of the predicted path in the sky plane.

This mismatch between observation and prediction is at a $\sim 1.3\sigma$-level, and is thus insignificant at our accuracy level. It shows in particular that the Gaia DR2 astrometry was crucial in getting an accurate prediction that allowed the detection of the central flash at various stations.

2.3. Occultation light curves
All our occultation light curves are displayed in Figs. C.1–C.2. As was done in Table A.1, the first group of figures corresponds to light curves that had sufficient S/N to be used in Triton’s

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Fig. 3. continued. NB. ‘JAVA.’ is the abbreviation of Javalambre, used so that the name of the station fits into the plot.
We first adopt a bootstrap method to retrieve the molecular density $n(r)$, pressure $p(r)$, and temperature $T(r)$ of Triton’s atmosphere as a function of the distance to Triton’s centre, $r$. To do so, one approach is the Abel inversion of our refractive occultation light curves that have the highest S/N. Its primary result is the density profiles $n(r)$, from which the $p(r)$ and $T(r)$ profiles are derived by using the hydrostatic and ideal gas equations.

The other approach is a direct one. It is used once the inversion procedures have provided the density profiles $n(r)$. These profiles are smoothed and parameterised according to physical arguments (discussed later). Then, a ray-tracing scheme generates synthetic light curves that are fitted to the occultation light curves, thus describing the global structure of Triton’s atmosphere, as illustrated in Fig. 5. One product of this fit is the location of Triton’s centre, which is used iteratively with the Abel inversion, thus improving the accuracy on the altitude scale. The other product of our approach is the value of the pressure at a prescribed radius for comparison with previous results, aimed at detecting possible long-term seasonal effects.

The final approach is to fit the central flashes observed in some light curves and to measure the departure (if any) from the spherical shape of Triton’s deep atmosphere, which is eventually used to constrain its wind regime. The other goal of this fit is to reveal possible absorbing material (by comparing the height of the central flash in stations that provided observations in different wavelengths) along the line of sight, such as hazes just above Triton’s surface.

Technical details on the inversion technique are given in Vapillon et al. (1973), ray-tracing schemes and central flash fitting are described in Sicardy et al. (1999), and applications to Pluto’s atmosphere are presented in Dias-Oliveira et al. (2015, DO15 hereafter), and Meza et al. (2019). Numerical values used in both our inversion and ray-tracing codes are summarised in Table 2.
Fig. 6. Best two light curves obtained during the Triton occultation of 5 October 2017, at La Palma and Helmos stations (see details in Table 1). Both telescopes were equipped with the same E2V CCD 47-20 detector with quantum efficiency peaking at 600 nm and reaching zero near 300 and 1000 nm, respectively. *Left panel:* full resolution light curve (cycle time 0.635 s) for the La Palma station. *Right panel:* same for the Helmos station (cycle time 0.674 s). The spectral ranges used for each instrument are indicated in the figures (I+z at La Palma and V+R at Helmos). The blue lines are the best simultaneous fits obtained with our ray-tracing approach (see Sect. 4).

### Table 2. Adopted physical parameters for Triton and its atmosphere.

| Parameter | Value |
|-----------|-------|
| Triton’s body | |
| Mass$^{(1)}$ | $G M_T = 1.428 \times 10^{12}$ m$^3$ s$^{-2}$ |
| Radius$^{(1)}$ | $R_T = 1353$ km |
| Triton’s geometry on 5 October 2017 | |
| Triton pole position$^{(2)}$ | $\alpha_T = 20h, 09m, 29.40s$ |
| (J2000) | |
| Sub-solar latitude | $40.0^\circ$ S |
| Sub-observer latitude | $40.5^\circ$ S |
| Sub-observer longitude | $169.9^\circ$ E |
| N. pole position angle$^{(3)}$ | $305.7^\circ$ |
| Geocentric distance | $D = 4.3506 \times 10^9$ km |
| Triton’s atmosphere parameters | |
| N$_2$ molecular mass | $\mu = 4.652 \times 10^{-26}$ kg |
| N$_2$ specific heat | $c_p = 1.04 \times 10^3$ J K$^{-1}$ kg$^{-1}$ |
| at constant pressure | |
| N$_2$ refractivity | $K = 1.091 \times 10^{-23}$ |
| (visible bands$^{(4)}$) | $+(6.282 \times 10^{-26}/\lambda_2^{1/2}$) |
| Refractivity at 3.6 cm$^{(5)}$ | $K = 1.0945 \times 10^{-23}$ cm$^3$ molecule$^{-1}$ |
| Boltzmann constant | $k_B = 1.380626 \times 10^{-23}$ J K$^{-1}$ |

Notes.  
$^{(1)}$McKinnon et al. (1995), where $G$ is the constant of gravitation.  
$^{(2)}$On 5 October 2017, using Davies et al. (1996), with corrections available at http://ftp.imcce.fr/pub/iauwg/poles.pdf.  
$^{(3)}$Position angle of Triton’s north pole projected in the sky plane. Counted positively from celestial north to celestial east. (4) Washburn (1930). (5) G95.

### 3.2. Assumptions

Our inversion and ray-tracing schemes assume that:

1. The atmosphere is composed of pure N$_2$. The next most abundant species (CH$_4$) has a volume mixing ratio (hereafter referred to as mixing ratio) of less than $10^{-3}$ (Strobel & Summers 1995; Lellouch et al. 2010). Our ray-tracing code shows that such an abundance causes a fractional change of the synthetic flux of about $10^{-3}$ near the half-light level, these effects are negligible considering the noise level of the data.

2. The atmosphere is transparent. The deepest layers reached during Earth-based occultations are those that cause the central flash, at an altitude of about 8 km (see Appendix B). The validity of this assumption will be discussed in Sect. 8.

3. The upper atmosphere is globally spherical. This hypothesis is supported by the fact that the observed central flashes are consistent with a spherical shape (Sect. 7). Small departures from the spherical model, however, are observed in some central flash shapes, and are discussed in Sect. 7.

The limitations of our approach described above are presented in Appendix B.

### 4. Results

#### 4.1. Inverted profiles

We used the three datasets with highest S/N to perform our inversion method, more precisely the light curves from La Palma (2-m Liverpool telescope, Spain), Helmos (2.28-m Aristarchos telescope, Greece) and Calern (1.04-m C2PU telescope, France) (see Table A.1). At half-light times (where the star flux has been reduced by 50%) and for ingress and egress, each of these stations probe different locations in Triton’s atmosphere. The corresponding latitudes, longitudes, and local solar times of the sub-occultation points are provided in Table 3. The paths of the stellar images over Triton’s surface as seen from these stations are plotted in Fig. 8.

The results of the inversions are displayed in Figs. 9–11. We also plot in these figures the profiles retrieved from our analysis of the RSS occultation (see Sect. 5.1 for more details, as well as a discussion on the connection of these profiles with our results). There are five noteworthy features. First, all six $n(r)$ and $p(r)$ inverted profiles are very similar, showing that the stations at La Palma, Helmos and Calern probed essentially identical atmospheric layers at their ingress and egress points. No significant variations versus local time and latitude are observed.

Second, in their common range of probed altitudes, our density profiles and the RSS profile coincide, to within the noise level of the RSS experiment (the noise level in our retrieved profiles being much smaller). Third, the pressure profiles from RSS and from our inversions are also close to each other. However,
contrary to the density profile, some small differences appear. This is discussed in Sect. 5.

Fourth, the general positive gradient in the upper parts of our retrieved thermal profiles is a mere result of the choice of our initial conditions. This is intended to match the general temperature profiles obtained independently by Strobel & Zhu (2017), which were constrained by the RSS occultation data taken in 1989 (see Appendix B).

Fifth, all of our six retrieved thermal profiles show, however, a marked turning point in their deepest parts, where the temperature gradient becomes negative. This gradient is always well below (in absolute value) the local dry adiabatic gradient, so that the atmosphere is convectively stable in those parts (Fig. 11).

### 4.2. Ray-tracing approach

For all the datasets used here, we employed the same procedure as in DO15, which consists of simultaneously fitting the refractive occultation light curves with synthetic profiles generated by the ray-tracing code. For each station, a least-squares fit is performed to adjust the synthetic light curve to the observation. Due to the uncertainties in the determination of $\phi_0$ (the fraction of the flux attributed to Triton; see Appendix B) for some stations, and the lack of calibration for most of them, we considered $\phi_0$ as a free parameter when performing these fits. We note that this adds one degree of freedom per station to the fit, and thus increases the error bars on the retrieved atmospheric parameters.

Our ray-tracing method is mainly sensitive to the half-light level. It corresponds to a radius of about 1415 km in Triton’s atmosphere (altitude ~60 km) and a pressure level of ~0.55 µbar. For a prescribed temperature profile $T(r)$, this method returns two best fitting parameters. One parameter is the pressure $p_{\text{ref}}$ at a reference radius, here $r_{\text{ref}} = 1400$ km. This particular choice stems from the fact that this reference radius has been used in previous works (e.g. Olkin et al. 1997; Elliot et al. 2000b), thus allowing consistent comparisons.

To proceed forward, we have defined a template $T(r)$ profile that matches the inverted profiles obtained at the station with the best S/N (La Palma). It has the same functional variation with altitude as in Dias-Oliveira et al. (2015), where it was applied to Pluto’s atmosphere, except for the upper branch, which is not isothermal but rather has a constant thermal gradient that connects the lower atmosphere to an upper thermosphere. The adopted parameters for the template profile $T(r)$ are provided in Appendix B.2.

The lower part of the profile has been adjusted so as to fit the central flashes (see Appendix B.2 for details). That adjustment provides constraints on the thermal profile between the lowest inverted point of La Palma (~20 km altitude) down to the central flash level (~8 km altitude). Finally, below 8 km, the profile has been connected to the surface’s temperature at 38 K. This is a ‘blind part’ of the profile, as it does not contribute significantly to the refracted stellar flux received on Earth.

The resulting synthetic temperature profile is shown as a thin black line in Fig. 10. Starting from the surface, the profile first has a strong positive temperature gradient of 5 K km$^{-1}$. This gradient decreases rapidly (Fig. 11) and the temperature reaches a maximum value of about 50 K at $r = 1363$ km (10 km altitude), thus implying an average gradient of 1.2 K km$^{-1}$ in that lower part. Our data show a hint of a mesosphere with a negative gradient (also seen in Elliot et al. 2003) that reaches $-0.2$ K km$^{-1}$ at $r = 1375$ km (23 km altitude), before connecting with the general positive gradient of the upper branch.

The strong surface temperature gradient at the surface derives from the need to connect our inverted profiles to the surface at 38 K. Since we do not have information in this lower portion of the atmosphere, we employed the simple hyperbolic form of DO15 to connect our profile to the surface, so that our surface gradient does not necessarily reflect the real value at that level.

This said, the general positive gradient can be achieved by considering the heating by CH$_4$ stemming from near IR absorbing bands. For instance, we estimate that a CH$_4$ mixing ratio of 0.0004 yields $T = \approx 52$ K at 1363 km, and thus could explain our result. Strobel & Zhu (2017) ran their model for discrete values of the CH$_4$ mixing ratios not included in their paper and found that a CH$_4$ surface mixing ratio $\sim 0.00015$ would suffice to support a temperature rise $\sim 9$ K, and a CH$_4$ surface mixing ratio $\sim 0.0004$ a temperature rise $\sim 12$ K, in the first 10 km. Because CH$_4$ is photochemically destroyed in the lower atmosphere, its scale height is roughly half the N$_2$ scale height and in terms of CH$_4$ column density one needs a higher surface CH$_4$ mixing ratio to compensate for its smaller scale height. For remote sensing observations it is the column density that is important and not just the surface mixing ratio that is relevant. We note that the 0.0004 value is smaller than, but roughly consistent with the range found by Lellouch et al. (2010) for the CH$_4$ mixing ratio, 0.0005–0.0010. Moreover, some complications may arise, like the existence of a troposphere.

The troposphere on Triton has been shown to be controlled by turbulent mixing above the surface, and to be sensitive to surface thermal contrasts between N$_2$ ice and the volatile free bedrock (due to different surface albedo or thermal inertia, Vangvichith 2013). On Pluto, climate models showed that the sublimation of cold N$_2$ ice and subsequent transport of the cold N$_2$ air in the impact basin Sputnik Planitia yield a km-thick cold troposphere as observed by New Horizons Forget et al. (2017); Hinson et al. (2017).

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**Table 3.** Local circumstances at the three stations (ingress and egress) used for the Abel inversion analysis.

| Site          | Time (UT)  | Location on surface | Local solar time  |
|---------------|------------|---------------------|------------------|
| La Palma, ingress | 23:48:27   | 251°E, 10°N         | 06:36 (sunrise)  |
| La Palma, egress  | 23:50:52   | 18°E, 46°S          | 22:08 (sunset)   |
| Helmos, ingress   | 23:45:38   | 254°E, 7°N          | 06:24 (sunrise)  |
| Helmos, egress    | 23:47:58   | 12°E, 47°S          | 22:32 (sunset)   |
| Calern, ingress   | 23:46:28   | 228°E, 32°N         | 08:08 (sunrise)  |
| Calern, egress    | 23:49:15   | 50°E, 30°S          | 19:00 (sunset)   |

**Notes.** (1)UTC time at half-light level, 5 October 2017. (2)One ‘hour’ corresponds to a 15° rotation of Triton. A local time before (resp. after) 12.0 h means morning (resp. evening) limb.
The pressure at any level can then be deduced by using the temperature template described above. In particular, the surface pressure $p_{\text{surf}}$ can be obtained by the relation $p_{\text{surf}} = 12.0 \times p_{1400}$. This ratio will be used to extrapolate $p_{1400}$ from $p_{\text{surf}}$ or vice versa. The other fitted parameter is Triton’s DE435/NEP081 ephemeris offset perpendicular to its apparent motion projected in the sky, $\Delta \phi$. We note that the ephemeris offset along Triton’s motion is decoupled from that fit (see DO15 for details).

Error bars are obtained from the classical function

$$
\chi^2 = \sum_i \left( \frac{f_i^{\text{obs}} - f_i^{\text{syn}}}{\sigma_i} \right)^2,
$$

which reflects the noise level $\sigma_i$ of each of the $N$ data points, where $f_i^{\text{obs}}$ and $f_i^{\text{syn}}$ are the observed and synthetic fluxes at the $i^{\text{th}}$ data point, respectively.

We simultaneously fitted a selected pool of 52 light curves obtained during the 5 October 2017 occultation. Other light curves were not considered at this stage because they are affected by higher or non-normal noise that would degrade the global fit. In a first step, we excluded from the fit the parts of the light curves where a strong central flash is present. This is to avoid giving too much weight to those parts, while they reflect only the properties of the deepest atmospheric layers. So, the goal of this fit is to get the global properties of the atmosphere, and in particular, to constrain $p_{1400}$ and the location of the shadow centre with respect to the occultation chords. In a second step, we included the central flashes in the fit to assess the shape of Triton’s atmosphere and to check if the central flash location coincides with the centre found by the global approach.

After exploring a grid of values for $\Delta \phi$ and $p_{1400}$, we obtained the $\chi^2(\Delta \phi, p_{1400})$ map displayed in Fig. 12. A satisfactory fit should provide a minimum value $\chi^2_{\text{min}}$ close to $N - M$, where $M$ is the number of fitted parameters. Besides $p_{1400}$ and $\Delta \phi$, we considered Triton’s contribution to the light curve ($\phi_0$) as a free parameter for all light curves. This is because no satisfactory values of $\phi_0$ have been obtained for any of the light curves (see Appendix B.2). Thus, the fitted parameters are the values of $\Delta \phi$ and $p_{1400}$, plus the 52 values of the $\phi_0$ (i.e. a total of $M = 54$ fitted parameters). On the other hand, we used $N = 68,446$ data points. We then obtain a global value of $\chi^2$ per degree of freedom, $\chi^2_{\text{dof}} = \chi^2_{\text{min}} / (N - M) = 0.85$, indicating a satisfactory global fit to the data. An examination of values of $\chi^2_{\text{dof}}$ for individual light curves also shows values near unity for all of them. Thus, none of our light curves show significant discrepancies when compared to the synthetic light curves derived from the synthetic density model shown in Fig. 9. This confirms the spherical symmetry of Triton’s atmosphere on a global scale.

Without considering $\Delta \phi$, the marginal distribution for $1 \sigma$ and $3 \sigma$ error contours on $p_{1400}$ are estimated by tracing the isolines $\chi^2_{\text{min}} + 1$ and $\chi^2_{\text{min}} + 9$, respectively, as shown in Fig. 12. The best-fitting value of $p_{1400}$, its $1 \sigma$ error bar and the quality of the fit, $\chi^2_{\text{dof}}$, are listed in Table 4. The best-fitting value of $\Delta \phi (\sim -359.3 \pm 1 \text{ km})$, Fig. 12) is used to retrieve the closest geocentric approach distance between Triton and the star (projected in the sky plane) and its corresponding time (see Table 1).

Finally, the best simultaneous fit corresponding to the minimum of $\chi^2$ is displayed in Fig. C.1–C. For the sake of completeness, Figs. C.2–C show the synthetic light curves superimposed on the light curves that have not been included in the fit. Although they have poorer S/N, they all confirm that our global model satisfactorily fits these data.

The negative gradient in the mesosphere, reminiscent of the more extended mesosphere on Pluto (Lellouch et al. 2017; Young et al. 2018), calls for the existence of a coolant. It must cool the atmosphere above its peak temperature of $\sim 50 \text{ K}$, as well as radiate away the downward thermal heat flux from the upper atmosphere where $T \sim 100 \text{ K}$. There are a few candidates for this coolant: haze particles and/or influx of dust particles that may either be pure H$_2$O ice or with silicate cores and coated with H$_2$O ice (see Ohno et al. 2021 for more details).
5. Reanalysis of results from previous events

5.1. The Voyager 2 radio occultation

During its Triton flyby on the 25 August 1989, the V2 spacecraft sent its radio signal (RSS experiment) back to Earth as it passed behind the satellite. Details on the gathering of the V2 RSS data are given in G95.

The main product of this observation was the temperature and pressure at Triton’s surface. However, although it becomes quite noisy above the 20 km altitude level, the RSS phase delay still provides useful constraints on Triton’s lower atmosphere, with some science left to explore. Here, we give a summary of Gurrola’s work, and describe how we use the V2 phase delay to retrieve Triton’s atmospheric structure in the 10–20 km above the surface.

The V2 high gain 3.7-m antenna transmitted to Earth two radio signals at 3.6 and 13 cm (X band and S band, respectively). The phases in these bands are related to one another by

$$\Delta \phi = \frac{121}{112} \left( \phi_x - \frac{3}{11} \phi_s \right)$$

(1)

where $\phi_x$ is the phase in the X band, $\phi_s$ is the phase in the S band, and $\Delta \phi$ is the corrected radio phase corresponding to the neutral atmosphere at the X-band wavelength. This calculation is done to remove plasma effects on the phase. Due to problems in fitting the ingress data, as there seemed to be sudden changes in slope, G95 used only the egress data for his analysis.

Gurrola provided us with the corrected phase delay $\Delta \phi(r)$ versus altitude above Triton’s surface, as well as the results from his models to obtain only the ‘pure atmosphere phase delay’. This corresponds to the phase delay once a general polynomial trend has been subtracted from $\Delta \phi$ to account for thermal noise.

### Table 4. Atmospheric pressure on Triton.

| Date            | Pressure at 1400 km ($p_{1400}$ (µbar)) | Pressure at the surface ($p_{surf}$ (µbar)) | Fit quality (χ^2) | Fit quality (χ^2) | Fit quality (χ^2) |
|-----------------|----------------------------------------|---------------------------------------------|-------------------|-------------------|-------------------|
|                 |                                          |                                              | N/A               | N/A               | N/A               |
| 25 August 1989  | 1.0 ± 0.2                               | 12.5 ± 0.5                                  | N/A               | N/A               | N/A               |
| 18 July 1997    | 1.90 ± 0.45                             | (22.8 ± 1.4)                                | 0.95              | 0.95              | 0.95              |
| 21 May 2008     | 1.15 ± 0.37                             | (13.8 ± 1.4)                                | 0.93              | 0.93              | 0.93              |
| 5 October 2017  | 1.18 ± 0.03                             | (14.1 ± 0.4)                                | 0.85              | 0.85              | 0.85              |
|                 |                                          |                                              | N/A               | N/A               | N/A               |
| 25 August 1989  | N/A                                     | 14 ± 2                                      | N/A               | N/A               | N/A               |
| 14 August 1995  | 1.4 ± 0.1                               | (17 ± 1)                                    | N/A               | N/A               | N/A               |
| 18 July 1997    | 2.23 ± 0.28                             | (26.8 ± 3.4)                                | N/A               | N/A               | N/A               |
| 4 November 1997 | 1.76 ± 0.02                             | (21.1 ± 0.2)                                | N/A               | N/A               | N/A               |

### Notes.

(1) The values in parentheses assume a constant ratio of 12.0 between the pressures at the surface and at 1400 km, as derived from our best model (Fig. 10). (2) See discussion in Sect. 4.2. (3) Using our own inversion of the V2 RSS phase delay profile (text). (4) G95. (5) Olkin et al. (1997). (6) Elliot et al. (2000a, 2003). (7) This value is the average over ingress and egress obtained by Elliot et al. (2003).
and instabilities in the frequency reference on board V2. These polynomials, referred to as baselines in G95, were designated as B₁, B₂, and B₃. B₁ is the linear baseline used by Tyler et al. (1989), determined using 120 km of the data obtained. G95 considered this insufficient to reliably estimate the drift of the instrument over the atmosphere, as it did not extrapolate from high enough altitudes (so that the atmosphere is too thin to affect the signal phase) downwards towards Triton’s surface. On the other hand, baselines B₂ and B₃ used about 700 km of the data, and are, respectively, the second and third-order polynomials of G95’s best fit at egress. The preferred solution of this author is B₂. The resulting Δφ(r) is displayed in green in Fig. 13.

Using the B₂ solution, we derive the profiles displayed as green curves in Fig. 9. In order to compare this result to ours, we generated for comparison the phase delay at 3.6 cm that would be observed with our best profiles n(r) (the black line in Fig. 9) as if it were obtained by V2:

\[ \Delta \phi(r) = \frac{2 \pi}{\lambda} K \sigma_{N_2}(r), \]  

Fig. 9. Density and pressure profiles of the atmosphere of Triton as a function of radius, r (the distance to Triton’s centre). Upper panel: density profiles of Triton’s atmosphere as a function of radius, retrieved by inverting three light curves obtained during the 5 October 2017 occultation and from the V2 radio phase delay at 3.6 cm. The colour codes are indicated in the upper right part of the plot. The same codes are used in Figs. 10–11 and Figs. 14–15. The thin black curve is a smooth synthetic density profile that fits the inverted profiles and is extrapolated down to the surface. It is derived from the smooth temperature profiles shown in Fig. 10. The solid horizontal line marks Triton’s surface (at radius \( R_T = 1353 \) km), the dashed line indicates the central flash layer (near 1360 km), and the dotted horizontal line marks the reference radius, \( r_{ref} = 1400 \) km. Lower panel: corresponding pressure profiles.

Fig. 10. Temperature profiles as a function of radius (upper panel) and pressure (lower panel). The oblique dotted line in the lower panel is the wet adiabat, i.e. the vapour pressure equilibrium line for \( N_2 \), taken from Fray & Schmitt (2009).

Fig. 11. Temperature gradient corresponding to the upper panel of Fig. 10. The dot-dashed line is the dry adiabatic temperature gradient \( \Gamma = -g/c_p \), i.e. the limit of convective instability, where \( c_p \) is the specific heat at constant pressure for \( N_2 \) and \( g = GM_T/r^2 \) is the acceleration due to gravity.

where \( \lambda \) is the wavelength (3.6 cm), \( K \) is the corresponding molecular refractivity of \( N_2 \) (see Table 2), and \( \sigma_{N_2}(r) \) is now the column density stemming from our best model. The resulting Δφ(r) profile is shown in black in Fig. 13, together with the phase delays deduced from the inversions of La Palma and Helmos’ light curves (in colours).
During the occultation of 5 October 2017, using the $\phi_0$ corresponding to the temperature profile in Fig. 10. The inner green line contour is the 1σ limit of the fit, while the outer green line is the 3σ limit.

Conversely, we used the V2 corrected X-band radio phase to retrieve the refractivity profile from the Abel inversion

$$\nu(r) = \frac{\lambda}{2\pi^2} \int_0^{\infty} \frac{d\Delta \phi}{dR} \frac{dR}{\sqrt{R^2 - r^2}} = \frac{\lambda}{2\pi^2} \int_0^{\infty} \frac{d\Delta \phi}{R} \frac{dR}{R},$$

using the auxiliary variable $l = \sqrt{R^2 - r^2}$ to calculate the integral. Finally, the density profile $n(r) = \nu(r)/K$ can be deduced.

With this, we can directly compare our results to those of V2. We note that the RSS profiles probe altitude interval levels that overlap our ground-based occultation levels. This overlapping region extends from the lowest inverted points of the La Palma station, $r = 1373$ km (20 km altitude), up to roughly the reference level, $r = 1400$ km (47 km altitude), at which point the RSS profiles become too noisy to be reliable, reaching a factor of about 2 at that level.

The examination of the upper panel of Fig. 14 shows that no significant difference in density is detected between the 1989 and 2017 profiles, especially at the 'junction level' at $r = 1373$ km. We note that the RSS density profile is rather insensitive to the particular solution B1, B2, or B3 chosen to retrieve $n(r)$.

Integrating the weight of the atmospheric column provides the RSS pressure profile (lower panel of Fig. 9). However, this profile includes a contribution of the weight of the layers above $r = 1400$ km, where the RSS phase delay is very noisy. We note that the B1 pressure profile is quite offset in slope with respect to the B2 and B3 solutions (lower panel of Fig. 14). So, and contrarily to the density profiles, the general slope of $\log_{10}(p)$ versus radius $r$ is quite sensitive to the particular choice of the polynomial baseline. In this context, it is difficult to conclude if the break in slope between the RSS profile and our ground-based results of 2017 is real or not.

Using the preferred B2 model, and using the Abel inversion (Eq. (3)), we obtain $p_{\text{surf,RSS}} = 13.6$ bar and $p_{1373,\text{RSS}} = 3.77$ bar as of 1989. The main result of the inversion is the density profile; to translate this into pressure, we need an estimate of the surface temperature $T_{\text{surf}}$. The error bar on $p_{\text{surf,RSS}}$ caused by the uncertainties on $T_{\text{surf}}$ will be discussed next.

In any instance, our results are consistent with the analysis of G95, $p_{\text{surf,RSS}} = 14 \pm 2$ bar. This is also fully consistent with our estimation of the surface pressure as of 2017, 14.1 $\pm 0.3$ bar (Table 4). Thus, no significant variations of surface pressure is found when comparing the RSS results of 1989 and the results derived from the ground-based occultation of 2017.

The value $p_{1373,\text{RSS}} = 3.77$ bar that we find is 21% smaller than the value we obtained in 2017 at that level, 4.58 bar. Propagating this 21% difference to the 1400 km radius then yields $p_{1400,\text{RSS}} = 0.97$ bar. Estimating the error bar on that value is difficult, because the RSS pressure depends on the (noisy) pressure values obtained above, as mentioned earlier. If we adopt the error bar $p_{\text{surf,RSS}} = 14 \pm 2$ bar of G95 and propagate it upwards, this yields $p_{1400,\text{RSS}} = 0.97 \pm 0.14$ bar.

Another, more robust way to estimate $p_{\text{surf,RSS}}$ is to use the RSS density profile alone. The counterpart is that we need an independent measurement of the surface temperature $T_{\text{surf}}$ in order to derive the pressure from the ideal gas equation $p_{\text{surf,RSS}} = n_{\text{surf,RSS}} k_B T_{\text{surf}}$. These temperature measurements (given below) are more accurate than G95’s estimation ($T_{\text{surf}} = 42 \pm 8$ K) and thus reduce the $\pm 2$ bar uncertainty of G95’s value of $p_{\text{surf,RSS}}$. However, this approach is valid only if these temperature measurements apply to the N2 ice surface that the RSS experiment probed, and if the vapour pressure equilibrium between the N2 ice and the gas is achieved.

Estimations of $T_{\text{surf}}$ are given by various authors (see also Fig. 15): 38.3 K (Conrath et al. 1989), 38.2 K (Tryka et al. 1993), the range 36.5-41 K (Grundy et al. 1993) and 37.5 $\pm$ 1 K (Merlin et al. 2018). Adopting a value of $n_{\text{surf,RSS}} = 2.4 \times 10^{15}$ cm$^{-3}$ derived from our RSS phase delay inversion (Fig. 14), we find surface pressures of 12.3$^{+1.3}_{-0.5}$ bar, 12.3$^{+0.6}_{-0.3}$ bar, a range 11.5–13.3 bar and 12.4 $\pm 0.3$ bar, respectively, for the four choices of surface temperatures. We note that all these values are consistent with the surface being in vapour pressure equilibrium with the atmosphere, as shown in Fig. 15. This supports the hypothesis that the reported temperatures are indeed representative of the N2 ice surface.

In summary, we estimate from the surface temperatures given above, a safe surface pressure range of 12.5 $\pm$ 0.5 bar can be derived at the V2 epoch. In this case, the error bar essentially stems from the uncertainties on the temperatures. Comparing this value with our estimation $p_{\text{surf}} = 14.1 \pm 0.4$ bar in 2017 (Table 4), and assuming a constant factor (12.5/14.1) throughout the profile, we formally obtain $p_{1400} = 1.05 \pm 0.04$ bar in 1989. This is consistent with our estimate made above, $\sigma_{1400,\text{RSS}} = 0.97 \pm 0.14$ bar. We thus estimate a conservative range of $p_{1400,\text{RSS}} = 1.0 \pm 0.2$ bar for the pressure at 1400 km in 1989.

5.2. The 18 July 1997 stellar occultation

This campaign involved one station in the USA and three stations in Australia. It was a joint effort between two groups, and, therefore, both have access to the data. The circumstances of observations are listed in Table A1 and the geometry of the event is displayed in Fig. 16. More details on these observations and their analysis are given in Elliot et al. (2000a).

Here we provide the results of our own approach to constrain $p_{1400}$. In particular, we adopt the same temperature profile $T(r)$ as for 2017 (see Fig. 10), but varying $p_{1400}$ to fit the synthetic light curves to the data. The $\chi^2 / \sigma^2$ map is displayed in Fig. 17 and the best fit is shown in Fig. 18. This yields $p_{1400} = 1.90^{+0.45}_{-0.30}$ bar and $\chi^2_{\text{def}} = 0.95$, indicating a satisfactory fit.
5.3. The 21 May 2008 stellar occultation

This event was observed from Namibia (two stations) and from La Réunion island (two stations; see Table A.1). Given that each pair of stations are close together, only two effective chords have been obtained (see Fig. 19). Moreover, these chords being grazing, there is a strong correlation between the closest approach distances of the chords to Triton’s shadow centre and the retrieved reference pressure $p_{1400}$ (see Fig. 20). The best fit is also shown in Fig. 21. As a consequence, the value of $p_{1400}$ is poorly constrained at the $1\sigma$ level, $p_{1400} = 1.15^{+1.03}_{-0.37}$ mbar. At the $3\sigma$ level, the value is so unconstrained that it does not bring any information on the temporal seasonal variations of the pressure (Fig. 22).

6. Atmospheric seasonal variations

6.1. Occultation results

Table 4 lists our values of $p_{1400}$ at various epochs, as well as values taken from other works. Extrapolations to the surface have also been included, assuming a constant ratio $p_{\text{surf}}/p_{1400} = 12.0$. The corresponding seasonal variations of $p_{1400}$ with time is displayed in Fig. 22.

The value of Olkin et al. (1997) indicates a 40% increase in pressure between 1989 and 1995, but at a low significance level of $1.8\sigma$. From the 18 July 1997 event, Elliot et al. (2000a) obtained $p_{1400} = 2.23 \pm 0.28$ mbar, whereas with the same dataset, we obtain $p_{1400} = 1.90^{+0.45}_{-0.30}$ mbar. The difference between the two results amounts to a factor of 0.85 and stems from the use of a different template model $T(r)$. This said, this difference remains at the $0.6\sigma$ level and is statistically insignificant. Using our value of $p_{1400}$ for 1997 indicates a pressure increase by a factor of 1.9 between 1989 and 1997, but at a marginally significant $2.5\sigma$ level only.

The 4 November 1997 value obtained by Elliot et al. (2000a, 2003), $p_{1400} = 1.76 \pm 0.02$ mbar, has a much lower error bar due to the high S/N of the light curve, obtained with the Hubble Space Telescope. Taken at face value, this implies an increase in pressure by a factor of 1.76 between 1989 and 1997, at a $3.8\sigma$ level. However, this observation was a single-chord event, and a model was used to retrieve the astrometry of this event. Consequently, there is an uncertainty that was not accounted for. Since we do not have access to these data, it is impossible for us to verify their result using our own methods, and therefore, confirm this increase.

Finally, the 21 May 2008 event provided only two grazing chords, bringing no new information. Thus, no firm conclusion can be drawn on any change of pressure between 1989 and 2008.

In summary, we estimate that the surge of pressure reported in the 1990s (compared to the V2 epoch) seems to be confirmed by our own analysis, but it remains debatable considering the paucity of data points available, and the lack of a fully consistent analysis of all the observed events. We note that the 2017 data rules out the concept of a monotonic increase in Triton’s pressure over time, but does not rule out the observed increase in 1995-1997. Regardless, the much more accurate value of $p_{1400}$ that we obtain in 2017 is fully compatible with that derived from the V2 RSS experiment. If we consider the $3\sigma$ level, Fig. 22 shows that no increase can be claimed between the two measurements. So, either no surge occurred between 1989 and 2017 or, if it did, the pressure was back to its V2 value in 2017.

From high-resolution spectroscopy in July 2009, Lellouch et al. (2010) obtained the first detection of methane gas in Triton’s atmosphere since V2, and the first CO gas detection. Their analysis yielded a CH$_4$ gas number density at the surface $4.0^{+7.5}_{-2.5}$
Fig. 14. Close-up view of Fig. 9. Upper panel: close-up view of the density profiles. Various profiles derived from the RSS occultation are shown in green. The dashed line is the profile retrieved by Tyler et al. (1989) using a polynomial extrapolation $B_1$ to correct for the RSS phase instability. The thin solid line is the profile retrieved by G95 using the polynomial extrapolation $B_2$. The dotted line is the same by G95, but using the polynomial extrapolation $B_3$. The thick solid line is the best model of G95, based on the $B_2$ profile. Lower panel: same for the pressure profiles.

Fig. 15. Close-up view of the lower panel of Fig. 10. The width of each coloured box is Triton’s surface temperature ($T_{surf}$), as estimated by the various authors mentioned just above the boxes (see text for details). The heights of the boxes are the range of surface pressures, $p_{surf}$, using the ideal gas law $p_{surf} = n_{surf,RSS}k_BT_{surf}$, where $n_{surf,RSS} = 2.4 \times 10^{15}$ cm$^{-3}$ is the surface molecular nitrogen density derived from our inversion of the RSS data (see text). We note that all the boxes intersect the vapour pressure equilibrium, which is plotted as a dotted line. This shows that the RSS surface density and the estimated surface temperatures are mutually consistent with a pressure being controlled by the $N_2$ ice sublimation.

Fig. 16. Geometry of the 18 July 1997 occultation, with the same conventions as in Fig. 5.

Fig. 17. Same as Fig. 12, but for the 18 July 1997 occultation.

larger than inferred from V2 (Herbert & Sandel 1991; Strobel & Summers 1995). Assuming that the $N_2$ pressure would qualitatively follow a similar seasonal variation, they estimated a 40 µbar pressure in 2009. This value (which did not represent a direct measurement of the $N_2$ pressure) is clearly at odds with the picture shown in Fig. 22, in particular with the 21 May 2008 point.

6.2. Climatic context from numerical volatile transport modelling

The climatic context of Triton is described and analysed in detail in a recent paper by Bertrand et al. (2022). Bertrand et al. (2022) employed the VTM of Triton, developed at the Laboratoire de Météorologie Dynamique (LMD), to investigate the long-term and seasonal volatile cycles of $N_2$ and $CH_4$ on Triton. Their simulations are constrained by the surface pressure derived from the stellar occultations presented in this paper. In this section, we summarise the main results of this paper that are relevant for the interpretation of our observations.
Fig. 18. Simultaneous fits to the 18 July 1997 light curves. The panel covers 300 s in time. All the light curves have been shifted so that the mid-occultation times are aligned. The red vertical tick marks indicate 10:10 UTC at the Brownsville station (USA) and 10:18 UTC for the three Australian stations. The blue lines are simultaneous fits to the data (black dots), using the best value found in Fig. 17, $p_{1400} = 1.9$ µbar, and the temperature profile shown in Fig. 10. The green dots are the fit residuals. For each light curve, the upper dotted line is the normalised value of the star plus Triton flux, and the lower dotted line is the background flux. We note that the data from the Brownsville station were normalised during the event, as shown in Elliot et al. (2000a).

Fig. 19. Geometry of the 21 May 2008 occultation, with the same conventions as in Fig. 5.

Fig. 20. Same as Fig. 12 but for the 21 May 2008 occultation.

Fig. 21. Fit to the 21 May 2008 light curves. The same conventions as for Fig. 18 are used, except that the panel now covers 720 s in time. The synthetic light curve for Piton Lacroix is plotted in grey because it is not used in the fit, due to the high noise level. The red vertical tick marks indicate 01:51 UTC for Piton Lacroix and Mão, and 01:41 UTC for Hakos.

In VTM simulations, the surface pressure peak occurs slightly after the southern summer solstice (2000) between years 2000 and 2010 (see Fig. 23). The surface pressure seasonal variations obtained by Bertrand et al. (2022) is similar to that obtained by Spencer & Moore (1992), when they artificially maintained a permanent large southern cap of bright N$_2$ (see their Fig. 7). The larger the northern cap, the more it can serve as a condensation area and buffer N$_2$ sublimation in the southern hemisphere, which results in a lower and earlier surface pressure peak. The amplitude of the surface pressure peak is strongly attenuated if N$_2$ ice remains between 30° S - 0°, because condensation will dominate over sublimation between the years 1980 and 2020.

According to the model, Triton’s atmospheric surface pressure will remain at 5 µbar during the next solstice season if the north polar cap extends to 60° N and the south polar cap extends to 0°. The amplitude of the pressure peak is attenuated if N$_2$ ice deposits remain between 30° S - 0° because these latitudes are
dominated by condensation rather than sublimation after the year 2000.

These results suggest that a northern cap extending down to at least $45^\circ$ N - $60^\circ$ N is needed in 2017 to restore the surface pressure back to the V2 measured value ~14 µbar. Otherwise, the surface pressure will remain higher than 16 µbar in 2017 with no northern cap. A strong increase in surface pressure cannot occur before 2000 if $N_2$ ice remains between $30^\circ$ S - 0°. To ensure that the surface pressure remains greater than 5 µbar during the opposite season (southern winter) a permanent northern cap extending down to $45^\circ$ N is required.

In their simulations, Bertrand et al. (2022) also investigated the CH$_4$ cycle by taking into account a small amount of pure CH$_4$ ice at the surface in addition to the $N_2$-rich mixture (Merlin et al. 2018). In the case where this pure CH$_4$ ice is placed at the south pole of Triton, covering 2% of the surface of the visible projected disk, they obtain a large increase in the CH$_4$ gas abundance from 1990 to 2005, without any significant change in $N_2$ surface pressure. Since CH$_4$ is not completely mixed with $N_2$ ice, it implies that the large increase in CH$_4$ (with relation to V2) reported by Lellouch et al. (2010) could be decoupled from the $N_2$ seasonal variations and, therefore, does not necessarily represent a measurement of the global pressure of the atmosphere.

For more details on the $N_2$ and CH$_4$ seasonal variations as simulated by the VTM, the reader is referred to Bertrand et al. (2022).

### 7. Triton’s lower atmosphere: central flash

The detection of a central flash during the 5 October 2017 occultation offered a unique opportunity to study Triton’s lower atmosphere. Our ray-tracing code shows that the flash is caused by a layer having a typical thickness 2 km, lying at about 8 km above Triton’s surface (radius of 1361 km). In that altitude range, the Abel inversion method is no longer valid, due to the coexistence of two stellar images along Triton’s limb (see Fig. B.2). This problem arises at altitude levels of about 20 km, corresponding to the deepest layers probed by the light curve obtained at La Palma. Consequently, the central flash allows us to gain about 12 km downwards (about 0.6 scale height) compared to the inversion method. The explanation for this is shown in Fig. B.1 and further detailed in Appendix B.2.

#### 7.1. The central flash: observations

The central flash swept Europe along the lines shown in grey in Fig. 4. Among the 90 light curves shown in Figs. C.1–C.2, 42 show evidence of a stellar flux increase near mid-occultation, and 23 of them have enough S/N to be used in the central flash modelling.

Figure 24 displays the reconstructed intensity map of Triton’s shadow, with in particular the presence of a bright dot (central flash) near the shadow centre.

At Calar Alto, which passed at about 300 km from the shadow centre at closest approach (C/A), the increase in stellar flux is barely noticeable (Fig. 3), while it reaches the full unoccluded stellar flux at Calern, which passed at 29 km from the centrality. At Constância (C/A 8.4 km), the maximum of the flash peaks at three times the unoccluded stellar flux, and about 3.4 times the unoccluded flux at Le Beausset (C/A 6.7 km, the closest of all stations; see Figs. 3 and 7).

The fit of the central flash is described in Sect. 4.2, except that we now allow a departure from sphericity of the layer responsible for the flash (see Sicardy et al. 2006 for details). We note that the ray-tracing code accounts for both the primary and secondary stellar images. Thus, we are not restricted in using this code as would be the case for the Abel inversion scheme (Appendix B.3).

#### 7.2. The central flash: spherical fit

Assuming a spherical flash layer, we obtain the best simultaneous fits (now including the central flashes) displayed in Fig. 3. The quality of the fit ($\chi^2_{\text{red}} = 0.80$) is comparable to the quality.
obtained without the flashes ($\chi^2_{\text{ref}} = 0.85$), showing that no departure from sphericity is detected. A more quantitative assessment for the upper limit for such a departure (some 1.5 km along the limb, as projected in the sky plane) is provided in the next subsection. A closer visual examination of the residuals for the strongest flashes with best S/N reveal, however, some minor and localised features, possibly due to atmospheric waves (Fig. 7), but no global departure from the spherical model.

There is another argument supporting the spherical nature of Triton’s atmosphere. The centre of Triton’s shadow, as determined by the simultaneous fit to all the flashes, including the ingress and egress parts of the light curves, coincides to within 0.1 km with the shadow centre determined by a global fit to all 52 light curves, by excluding the central flashes but including the ingress and egress parts. This 0.1 km offset is not significant, considering that the global fit centre has a typical 1σ error of 1 km cross-track (Fig. 12). In other words, the centre of the central flash layer, which is sensitive to the 8 km altitude level, coincides with the global shadow centre, which is sensitive to the 60 km altitude level. It could be that both atmospheric levels are close to spherical, but displaced in the same way with respect to Triton’s centre, but this configuration seems unlikely.

7.3. The central flash: Limit on atmospheric distortions and winds

We now assess a possible departure of Triton’s lower atmosphere from sphericity, restricting ourselves to the simple model of a globally oblate flash layer. Testing more complex shapes will be performed once Triton’s 3D GCMs are available, something that is beyond the scope of this paper. Once projected in the sky plane, an oblate layer appears as an ellipse with apparent semi-major and semi-minor axes $a’$ and $b’$, respectively. The centres of curvature of that ellipse form a diamond-shaped caustic curve where abrupt flux variations are observed (see examples in Fig. 25). The equation of the caustic is (Elliott et al. 1997):

\[(a’x)^{2/3} + (b’y)^{2/3} = (a^2 - b^2)^{2/3},\]

where $Oxy$ is a Cartesian reference system whose origin $O$ is fixed at the ellipse centre, and where $Ox$ (resp. $Oy$) is aligned with $a’$ (resp. $b’$). Since the flash layer lies at ~8 km altitude, we have $a’ \sim 1360$ km. We note that the orientations of the $a’$ and $b’$ axes are still to be specified.

We define the apparent oblateness of the flash layer as $\epsilon’ = (a’ - b’)/a’$. We have explored values of $\epsilon’$ from zero (i.e. a spherical flash layer) to some maximum value, and tracked the corresponding variations of $\chi^2$ stemming from a simultaneous fit to central flashes. In this study, only the central flashes of the Varages, Calern, Constância, Le Beausset, and Felsina Observatories have been considered. The other stations are too far away from centrality and/or with lower quality to usefully constrain $\epsilon’$. This is because the four cusps of the diamond-shaped caustic curve extend up to $\sim 2\epsilon’a$ from the shadow centre according to Eq. (4). As we obtain upper limits of ~0.002 for $\epsilon’$ (see below), we have $2\epsilon’a \sim 5$ km for $a’ \sim 1360$ km. Thus, only the immediate vicinity of the shadow centre (typically less than 20 km) is sensitive to departures from sphericity. More distant stations essentially probe flashes that are indistinguishable from a spherical solution.

We first assume that the semi-minor axis $b’$ is aligned with Triton’s pole. This corresponds to an oblate flash layer maintained by an axisymmetric zonal wind regime that has a constant angular velocity around that axis. By using the $\chi^2 < \chi^2_{\text{min}} + 1$ (resp. $\chi^2 < \chi^2_{\text{min}} + 9$) criterion, we find $1\sigma$-level (resp. $3\sigma$-level) upper limits of $\epsilon’ < 0.0011$ (resp. $\epsilon’ < 0.0014$) for the apparent oblateness of the flash layer. The flash intensity map corresponding to this limit is displayed in Fig. 25. This apparent oblateness must be ‘deprojected’ to obtain the actual oblateness, $\epsilon$, through the relation

\[\epsilon = 1 - \frac{\sqrt{(1 - \epsilon’)^2 - \sin^2 B}}{\cos B} \sim \frac{\epsilon’}{\cos^2 B},\]

where $B = 40.5^\circ$ S is the sub-observer latitude (Table 2), and where the approximation holds for $\epsilon’ \ll 1$. Using $\epsilon’ < 0.0011$, this yields a $1\sigma$-level upper limit $\epsilon < 0.0019$ for the deprojected oblateness. This corresponds to a difference between the equatorial and polar radii $r_e$ and $r_p$ of the layer, respectively, of $r_e - r_p \sim 3$ km, using $r_e = a’ = 1360$ km.

We assume that the flash layer shape is entirely supported by zonal winds. In particular, we assume the absence of a horizontal temperature gradient, so that the isobar level also corresponds to the isopycnic (constant density) layer. The radius $r$ of the flash layer is given as a function of the latitude $\varphi$ by the equation (Hubbard et al. 1993; Sicardy et al. 2006)

\[\frac{1}{r} \frac{dr}{d\varphi} = - \frac{f \cos(\varphi) \sin(\varphi)}{1 - f \cos^2(\varphi)},\]

where $f = r(\varphi)/GM\cos^2(\varphi)$. This equation states that the isobar is locally perpendicular to the effective gravity field, where both the gravity field of the (spherical) body and centrifugal forces are accounted for. Introducing in that expression the polar equation of an oblate flash layer,

\[r = \frac{r_e r_p}{[r_e \sin^2(\varphi) + r_p \cos^2(\varphi)]^{1/2}}.\]
we obtain to lowest order in \( \epsilon = (r_e - r_\text{rot})/r_e \) the velocity

\[
v = \sqrt{\epsilon} \sqrt{\frac{2GM_T}{r_e}} \cos \varphi \sim 1450 \sqrt{\epsilon} \cos \varphi \text{ m s}^{-1},
\]

(5)

the value of \( GM_T \) is listed in Table 2. Using \( \epsilon < 0.0019 \), this provides a 1\( \sigma \)-level upper limit for the zonal wind at the equator of \( |v| < 63 \text{ m s}^{-1} \).

We note that this motion can be prograde (positive sign) or retrograde (negative sign), and that it is measured in an inertial frame. Thus, noting \( v_\text{e} \) the zonal wind in a frame rotating with Triton (which thus measures the atmospheric circulation at that level), we have \( v_e = v'_e + v_\text{rot} \), where \( v_\text{rot} = 17 \text{ m s}^{-1} \) is the equatorial velocity stemming from Triton’s rotation (see Fig. 24).

Consequently, a retrograde zonal wind regime \( (v'_e < 0) \) implies a \( 1\sigma \) limit \( |v'_e| < 63 + 17 = 80 \text{ m s}^{-1} \), while a prograde regime \( (v'_e > 0) \) implies \( v'_e < 63 - 17 = 46 \text{ m s}^{-1} \). Those values are respectively 87 m s\(^{-1}\) and 53 m s\(^{-1}\) if the 3\( \sigma \) upper limit is considered.

Information on the atmospheric circulation of Triton was obtained in 1989 by V2: while surface wind streaks suggested eastward surface winds between latitudes of 15\( \degree \) S and 45\( \degree \) S (Hansen et al. 1990), the deflection of plumes showed that in the atmosphere above, at 8 km near 49\( \degree \) S and 57\( \degree \) S, the wind was westward and prograde (Hansen et al. 1990; Yelle et al. 1995). On the basis of theoretical consideration, Ingersoll (1990) proposed that this could result from a temperature contrast between the cold frost-covered pole and the warm un-frosted equator. More realistic GCMs simulations, including the N\(_2\) condensation-sublimation cycle, have been reported in Vangvichith (2013), and additional relevant simulations have been performed to explore the circulation on Pluto, which is similar to Triton in terms of rotation rate and atmospheric composition (see Forget et al. 2021 and reference therein). These models show that if N\(_2\) significantly sublimes in the southern hemisphere and condenses in the northern hemisphere, the circulation should be dominated by a retrograde circulation resulting from the conservation of angular momentum of the flow, with velocities that cannot be higher than the rotation of the planet (17 m s\(^{-1}\)). This is significantly less than the upper limits that we derive from our observations.

In any case, as mentioned above, global retrograde winds were not observed in 1989: to get prograde rotation in the mid southern latitude as suggested by the V2 plume observations, the inter-hemispheric condensation must be weak. In that case a thermal gradient could create a weak prograde wind as suggested by Ingersoll (1990), reaching a few metres per second in GCM simulations. However, modelling Pluto suggests that in some conditions a regime of super-rotation (like on Venus or Titan) could occur (Forget et al. 2017). This could explain the plume direction on Triton. Such a super-rotation is thought to initially result from the formation of a high-mid-latitude jet (due to thermal balance between a warm equator and a colder pole, or condensation flow from low latitudes to the pole). Then barotropic waves can transport angular momentum to and from the equator and seriously accelerate the entire atmosphere. In their Pluto GCM, Forget et al. (2017) found mean equatorial zonal wind up to 15 m s\(^{-1}\). However, this could be model-dependant. It is not easy to set a theoretical limit to such a super-rotation. Our upper limit on prograde wind near 50 m s\(^{-1}\) provides a constraint for such a hypothetical super-rotation in 2017.

We have considered other orientations for the central flash layer, as projected in the sky plane, by relaxing the condition that \( b' \) should be aligned with Triton’s pole. This might be the case if other causes of distortion than zonal winds are at work, for example tidal forces from Neptune or Triton’s potential anomalies. Those orientations provide more stringent upper limits of the apparent oblateness \( \epsilon' \) because the cusps of the caustic can then get closer to the paths of the central-most stations (Fig. 25). For instance, rotating the caustic by 45 degrees imposes the more...
stringent $1 \sigma$ upper limit, $\epsilon < 0.00074$ (instead of 0.0019). This requires an equatorial wind of $\sim 40 \text{ m s}^{-1}$, which is still quite a bit larger than the values $\sim 10 \text{ m s}^{-1}$ expected from GCMs, and thus not a constraining limit as far as GCMs are concerned.

We now compare our upper limit for the deprojected oblateness of the central flash layer ($\epsilon < 0.0024$) with the value obtained by Elliot et al. (1997) from a single cut inside the central flash region during the 14 August 1995 occultation. Two solutions are considered by those authors, an oblate flash layer with $\epsilon = 0.042$ and a prolate one with $\epsilon = -0.032$. Adopting the $\epsilon = 0.042$ value, we obtain the central map displayed in the right panel of Fig. 25. This would imply the crossing of the caustic by the five stations shown in the map, and result in strong flux variations at those crossings that are not observed in the data (see Fig. 7). A similar conclusion would be drawn by adopting the prolate value $\epsilon = -0.032$ of Elliot et al. (1997). We note that the closest approach distance to the shadow centre during the central observation flash of 1995 was about 100 km, which is well outside the diamond-shaped caustic displayed in the right panel of Fig. 25. Thus, caustic crossings could not be tested at that epoch.

The main problem of the large oblateness values obtained by Elliot et al. (1997) is that they imply unrealistically large wind velocities to maintain such distortions. For instance, taken at face value, $\epsilon = 0.042$ results in an equatorial wind velocity of $v_e \sim 300 \text{ m s}^{-1}$, more than twice the sonic velocity near Triton’s surface ($\sim 130 \text{ m s}^{-1}$ at $\sim 40 \text{ K}$) and much larger than predicted by GCMs (see above). A possibility considered by Elliot et al. (1997) was that Triton’s atmospheric distortion was restricted to mid-latitude regions (i.e. it was local rather than global). This permits lower values of wind speeds ($110-170 \text{ m s}^{-1}$) depending on whether prolate or oblate solutions are considered. This is still essentially supersonic and not expected from circulation models. Moreover, this distortion would also be detected in our dataset, which densely sampled the central flash region.

An alternative explanation proposed by Elliot et al. (1997) is the presence of hazes that absorbed part of the stellar flux at some specific locations along Triton’s limb, thus altering the central flash shape. However, according to those authors, neither the optical depth obtained for those hazes at the corresponding altitude levels, nor its dependence with wavelength, were consistent with the V2 results. The haze problem is discussed in more detail in Sect. 8.

Finally, the shape of Triton’s solid body as observed in V2 images indicates an oblateness smaller than 0.0004 (Thomas 2000), which is too small to explain the claimed distortions. Moreover, non-radial components of Triton’s inner gravitational field might also cause atmospheric distortions, but they would then be permanent and thus, should be observed also in 2017. From all this, we conclude that the large oblatenesses reported by Elliot et al. (1997) are both theoretically unexpected and inconsistent with our observations.

At this point, we think that the mismatches between the flash models and its observation in 1995 (as well as small departures from our spherical model in Fig. 7) could be caused by small local corrugations of the flash layer induced by gravity waves. As the caustic is the locus of the limb centre of curvatures, its shape is very sensitive to local (but small) corrugations of that layer. Examples of such effects have been investigated for explaining flash shapes in the cases of stellar occultations by Neptune (Hubbard et al. 1988) and Titan (Sicardy et al. 2006). As mentioned earlier, this approach remains beyond the scope of this paper, as long as zonal wind and gravity wave regimes are not available for Triton’s lower atmosphere.

8. Pending issues

8.1. Hazes

In the present work, we assumed that Triton’s atmosphere is clear (i.e. free of absorbing material). However, V2 observations in 1989 revealed two kind of absorbing features in the lower atmosphere: hazes and clouds. These features were detected in the visible through the imaging system (Rages & Pollack 1992) and during the UV occultation experiment (Krasnopolsky et al. 1992, 1993; Krasnopolsky & Cruikshank 1995).

The general picture that emerges from the V2 observations is reviewed in Yelle et al. (1995) and is described as follows: hazes are detected up to an altitude of about 30 km, they were observed around the entire Triton’s limb, except for a small clear region near east longitude 280° and between latitudes 4 and 18° S. Thus, unless drastic changes in haze formation occurred, they should also be present during our observation of 5 October 2017. Clouds are observed closer to the surface compared to hazes (i.e. below an altitude level of about 8 km). Contrary to hazes, they exhibit a patchier distribution along the limb.

Due to their low altitudes, absorbing materials should be best detected in the central flash structures, caused by a layer at about 8 km altitude. Estimation of the integrated (down to the surface) vertical optical depth of the hazes at 0.47 μm is $\tau_{\text{vis}} = 0.005 \pm 0.001$, with a typical scale height of $H_h \sim 12 \text{ km}$ (Krasnopolsky et al. 1993; Rages & Pollack 1992). Thus, the integrated vertical optical depth down to the 8 km altitude level should be reduced by a factor of $\exp(-8/H_h) \sim 0.5$. Moreover, the slant optical depth (along the line of sight) is amplified by a factor of $\sqrt{\pi R/\tau H} \sim 27$, yielding a slant optical depth of hazes at 8 km of the order of 0.005 $\sqrt{\pi R/\tau H} \exp(-8/H_h) \sim 0.07$, and a reduction in the flash amplitude by 5–10% if no changes have occurred since 1989.

Clouds are much denser than hazes, with vertical optical depth to the surface of 0.1 or higher. Cloud particles have a vertical distribution with a scale height $H_c$ comparable to or larger than the atmospheric scale height (about 20 km). Thus, the slant optical depth of clouds at 8 km should be in the order of 0.1 $\sqrt{\pi R/\tau H} \exp(-8/H_c) \sim 1.4$ or larger, corresponding to a decrease in the flash amplitude by a factor of 4 or more.

To summarise, hazes are expected to have a mild effect on the central flash heights, with an expected reduction of only 5–10%. We do not see any departure from the model at that level on the best flash profiles. Moreover, we do not detect trends on the observed flash amplitudes versus wavelength. For instance, the strong flash at Constância (Fig. 7) observed at an effective wavelength of $\sim 0.6 \mu$m agrees with the model at the same satisfaction level as the Varages flash, observed at $\sim 1.3 \mu$m (Fig. 3). The same is true with the Calar Alto observation, which was made simultaneously in the visible (0.4–1.0 μm) and the near IR (1.0–1.7 μm) (see Fig. 3 and Table A1). A flash is observed at that station, but it is too faint to reveal a difference between the two channels. Finally, the dual observation made at Kryoneri (R and I bands) was too far away from the centre line to show a central flash, but does not show significant differences anyway in the fits by the synthetic light curve (Fig. C.1).

Taken at face value, these results indicate that hazes have no detectable effect on the flash shapes. This result is true a fortiori for the clouds, which would reduce the flash amplitudes by a factor of 4 or greater; this is not observed in the data. In other words, our model consistently explains all the flashes using a clear atmosphere.
However, a difficulty arises at this point since the height of the flash actually depends on the assumed template temperature profile. In order to disentangle the haze versus temperature effects, independent information on the thermal profile of the lower atmosphere is required. This requirement could be met with the ALMA results reported by Gurwell et al. (2019). This issue remains, for the moment, beyond the scope of the present paper.

8.2. Troposphere

Yelle et al. (1991) inferred a troposphere from the V2 observations of geysers and clouds. We do not observe this, as our deepest layer probed, at the central flash level, which coincides with the expected altitude of the tropopause. Therefore, our model is consistent with our central flashes, as discussed in Sect. 7, and there is no need to include a troposphere to accommodate for the data. However, this does not mean that we can exclude a troposphere as we do not have information down to this part of the lower atmosphere.

The absorption, caused by hazes and clouds, impacts our data and the model. For a troposphere to be included, we need independent measurements of the lower atmosphere.

8.3. Gravity waves

In Sect. 7 and Fig. 7 we mention that the residuals in these light curves show minor features that are probably attributed to atmospheric waves. They present themselves as small fluctuations, with little effect on the overall light curve shape, and therefore we did not study them in detail. This topic needs further analysis that is beyond the scope of the present paper.

8.4. $\phi_0$ of inverted profiles

The determinations of the baseline levels $\phi_0$ used for inverting the profiles of La Palma and Helmos remain an open issue, as they provide inconsistent results in the deepest parts of the $T(r)$ profiles (Appendix B.2). This matter must be analysed further and needs independent results, in particular from ALMA, to confirm which $\phi_0$ should be used.

9. Concluding remarks

In this paper we present results obtained from the ground-based stellar occultation by Triton observed on 5 October 2017. The main goals were (i) retrieve the general structure of Triton’s atmosphere between altitude levels of $\sim 8$ km ($\sim 9$ bar) and $\sim 190$ km (few-nanobar level) and (ii) compare these results with other ground-based occultations and the V2 radio occultation to assess the pressure seasonal variation over the last three decades.

The 2017 event yielded 90 positive observations, 42 of which showed a central flash. We used Abel inversions to retrieve density, pressure, and temperature profiles from our three best S/N light curves. We find a hint of a mild negative temperature gradient ($\sim -0.2$ K km$^{-1}$) at the deepest part of our profiles (i.e. below the altitude of $\sim 30$ km). This constitutes a mesosphere just above an expected stratosphere with a positive temperature gradient that connects the atmosphere to the cold surface.

A ray-tracing approach was used for a global fit to the best 52 light curves, providing a pressure $p_{1400} = 1.18 \pm 0.03$ bar at radius $1400$ km. It also provides a synthetic and smoothed model to extrapolate the density, pressure, and temperature down to the surface.

A new analysis of the V2 radio experiment, with useful information extracted from the surface up to around $1400$ km, shows that the pressure retrieved in the 2017 event is consistent with the pressure obtained in 1989. A survey of pressure values obtained between 1989 and 2017 was conducted. The two past occultations (in 1997 and 2008), reanalysed using our methods, indicate that the surface pressure reported in the 1990s is real, but this remains debatable due to the scarcity of high S/N light curves and the lack of a fully consistent analysis of the best datasets used by other teams.

The pressure that we obtain from the 2017 occultation is consistent with that derived from the Voyager radio experiment, meaning that the pressure is back to its 1989 level. Results from a VTM of Triton, described in detail in Bertrand et al. (2022), do not support a strong increase in surface pressure in the last few decades but instead a modest increase, with a surface pressure reaching up to 20 bar in the intervening 28 yr. The VTM simulations also suggest that (1) a strong increase in surface pressure before 2000 cannot be obtained if N2 is present between latitude $30\degree$ S - $0\degree$, and (2) a northern polar cap should have extended down to at least $45\degree$ N - $60\degree$ N in 2017 to have the surface pressure back at the V2 level from 1989.

Finally, the central flash analysis does not reveal any evidence of an atmospheric distortion. The atmosphere appears as globally spherical, with a $1\sigma$ upper limit of $0.0011$ for its apparent oblateness near the $8$ km altitude. This corresponds to a global difference of less than $1.5$ km between the largest and smallest atmospheric radii at that altitude. This is much smaller than values reported in the literature. In particular, this does not support the existence of supersonic winds previously claimed by Elliot et al. (1997).

Open issues, requiring a more specific analysis of our dataset, will be addressed elsewhere. These include the possible presence (or absence) of hazes and of a troposphere just above Triton’s surface, as well as the possible detection of gravity waves.

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Meekrap-oord 3, 3991 VE Houten, The Netherlands
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ADAGIO, Belesta observatory (A05: MPC code), Belesta en Llauragais 31 - France
13200 Arles, France
Observatoire les Pléiades, Latrape, France
Observatoire des Baronnies Provençales, 05150 Meyrargues, France
Association Photographie Astronomie Montredonnaise (APAM), France
75000 Paris, France
Observatoire de la Côte d’Azur (OCA), Boulevard de l’Observatoire, Nice, France
Ciel et Espace, 63-65 boulevard Massena, 75013 Paris, France
78180 Montigny le Bretonneux, France
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Appendix A: Circumstances of observations

See table A.1.

Appendix B: Retrieval of atmospheric structure

Here we discuss some limitations and caveats associated with the approach mentioned in the main text.

Appendix B.1: Upper and lower limits of probed atmosphere

The density \( n(r) \) is reliably retrieved up to the level where the flux standard deviation \( \sigma_\phi \) due to photometric noise is comparable to the drop of stellar flux caused by the occultation (DO15). This corresponds to a density of

\[
\frac{n_{\text{upper}}}{K} \approx \frac{\sigma_\phi}{F} \sqrt{\frac{H^2}{2\pi r D^2}},
\]

where \( K \) is the molecular refractivity of \( N_2 \), \( H = -n/(dn/dr) \) is the scale-height and \( D \) is Triton’s geocentric distance.

Using the values of \( K \) and \( D \) listed in Table 2, considering that \( H \approx 30 \) km around \( r = 1500 \) km, and taking \( \sigma_\phi \approx 0.011 \) for our best dataset (La Palma station), we find that reliable density values cannot be obtained above \( r_{\text{upper}} \approx 1540 \) km, where \( n \approx 4 \times 10^{11} \) cm\(^{-3} \), corresponding to pressures of a few nanobars.

The relative error on \( n(r) \) reduces as \( \exp[-(r - r_{\text{ap}})/H] \) when deeper layers are probed. In practice, only the inversion of the best light curves provide useful retrieved profiles. In our case, this concerns the light curves from La Palma and Helmos stations, providing the profiles displayed in Figs. 9-11.

The deepest layers probed when inverting an occultation light curve are those corresponding to the closest approach of the observing station to Triton’s shadow centre. In our case, La Palma’s light curve provides data down to a radius of about \( r = 1375 \) km (i.e. just above the 20 km altitude level). However, the central flashes provide constraints that go further down, typically just under the 8 km altitude level (see Sect. 7).

Appendix B.2: Constructing the temperature profile template

A difficulty encountered during the inversion of the light curves is the assessment of Triton’s contribution to the total flux. We define \( \phi_0 = F_T/(F_S + F_T) \), where \( F_T \) (resp. \( F_S \)) is the flux coming from Triton (resp. the unocculted star). Thus, \( \phi_0 \) corresponds to the zero stellar flux level in the normalised occultation light curves. Changing its value mainly changes the deepest parts of the retrieved profiles (see Fig. B.1).

Measuring \( \phi_0 \) relies on images where Triton and the star are angularly separated. It is generally a difficult task, since a photometric accuracy of better than 1% is necessary to bring useful constraints. To mitigate differential chromatic effects (as the star and Triton have different colours), images were taken at the same elevation as for the occultation, either during the same nights or during nights before or after the event. As a sanity check, it is also desirable to use another reference star with flux \( F_R \) and see if the sum of the ratios \( F_S/F_R \) and \( F_T/F_R \) outside the event matches the ratio \( (F_S + F_T)/R_S \) during the event. Mismatches may then reveal possible variabilities in any of the objects involved (the target and reference stars, and/or Triton), and serve as an estimator of systematic sources of errors.

Such calibration images were acquired at the La Palma and Helmos sites, which provided the best datasets in terms of S/N. The focal lengths of those two telescopes are large enough to clearly resolve Triton from Neptune and from the occulted star and to avoid, in particular, flux contamination from the planet in the occultation light curve.

The calibration results are self-consistent for both instruments, with small internal error bars on \( \phi_0 \) (i.e. \( \phi_0 = 0.3445 \pm 0.0003 \) for La Palma and \( \phi_0 = 0.360 \pm 0.013 \) for Helmos). We note that there is no reason why the \( \phi_0 \) should be the same for the two stations, as different filters were used: \( I+g \, (720 \text{ nm}) \) at La Palma and \( V+R \) at Helmos. Also, different observation conditions were prevailing at the two stations. In particular, the different airmasses (1.3 and 2.4 at La Palma and Helmos, respectively) may also affect the flux ratios star/Triton. However, the different values of \( \phi_0 \) at La Palma and Helmos are mutually inconsistent (to within error bars) in the sense that they provide significantly different bottom parts for the \( T(r) \) profiles.

This is particularly problematic for La Palma, where we obtain a temperature profile that peaks at \( T \approx 58 \) K just above the flash layer, using the value \( \phi_0 = 0.3445 \) derived from the calibration (Fig. B.1). This imposes a strong inversion layer in order to connect the temperature profile 38 K at the surface (see Fig. 15 and associated discussion). When used in our ray-tracing code, this profile yields inconsistent synthetic central flashes when compared with observations (Fig. 3). In particular, it is not possible to fit simultaneously the flashes lying north and south of the shadow centre.

We have no satisfactory explanations for the inconsistencies induced by the photometric calibration (i.e. by the retrieved values of \( \phi_0 \)). It could stem from unaccounted light contamination from Neptune, although the biggest telescopes should be free of this problem, as mentioned above. We tested the effect of digital coronagraphy to remove any such possible contamination. However, no significant changes of \( \phi_0 \) are obtained with and without the use of coronography. Possible variations of Triton’s flux due to rotational light curves of the satellite have also been considered. However, considering the low amplitude of those rotational curves (Buratti et al. 2011), and the fact that calibrations were made about 90 minutes before the occultation at La Palma, Triton’s flux variation should be well below the 1% level, and thus have a negligible effect on the retrieved value of \( \phi_0 \).

In these conditions, we have opted for another approach. We have varied the value of \( \phi_0 \) for the best dataset (i.e. the La Palma light curve). For each value, we have inverted the light curve to obtain \( T(r) \), and then derived a template temperature profile using the Dias-Oliveira et al. (2015) modelling, except that the upper branch of \( T(r) \) is not isothermal, but has a constant gradient \( dT/dr \sim 0.1 \text{ K km}^{-1} \) to account for the general temperature increase (thermosphere) described in Strobel & Zhu (2017).

Each particular value of \( \phi_0 \) provides a set of prescribed \( T(r) \) boundary conditions (the green dots in Fig. B.1). Then it is possible to interpolate those prescribed values for any \( \phi_0 \) using smooth polynomial functions, and finally get a one-parameter family of \( T(r) \) profiles depending only on \( \phi_0 \).

The main goal here is to find the value of \( \phi_0 \) that best matches all the central flashes, thus constraining the deepest part of the \( T(r) \) profile. The best \( T(r) \) profile (with \( \phi_0 = 0.35885 \)) is shown as a thicker line in the upper panel of Fig. B.1, and is adopted throughout this paper every time we use our ray-tracing code. An example of an output of our tracing code is displayed in the lower panel of Fig. B.1.

Using the notations of Dias-Oliveira et al. (2015), the \( T(r) \) profile is constructed by adopting the parameters of Table B.1. We note that although both the \( T \) and \( dT/dr \) profiles are continuous, the \( d^2T/dr^2 \) profile is not. This is evident in Fig. 11 at
Table B.1. Parameters of the temperature template profile.

| $r_1$, $T_1$, $dT/dr(r_1)$ | 1353 km, 38 K, 5 K km$^{-1}$ (surface) |
| $r_2$, $T_2$ | 1363 km, 49.8 K ('elbow') |
| $r_3$, $T_3$ | 1375 km, 48.2 K (inflection point) |
| $r_4$, $T_4$, $dT/dr(r_4)$ | 1403 km, 49.3 K, 0.105 K km$^{-1}$ (upper branch, thermosphere) |

Admittedly, there is not a unique way to find a template $T(r)$ model that best fits the flashes. However, our solution should capture the main properties of the real profile, with a temperature maximum reached just above the central flash layer, and a mesosphere with a mild negative temperature gradient above that temperature peak. We note that the inversion layer connecting the profile to the surface at 38 K (i.e., below the temperature peak) has a vanishing effect on the synthetic light curve as the surface is approached, thus defining a ‘blind zone’ as far as our data are concerned.

**Appendix B.3: The secondary stellar image issue**

The Abel inversion assumes that only one stellar image (the near-limb, or primary refracted image) contributes to the recorded flux. In reality, Triton’s atmosphere also produces a far-limb (secondary) stellar image whose flux is added to the light curve. This is a source of error, especially in the central flash region, where the primary and secondary images have comparable fluxes (see for instance the lower panel of Fig. B.1).

We have performed tests to assess this effect on La Palma’s light curve. At closest approach, the station was at about 685 km from the shadow centre, providing information down to the ~20 km altitude level (Fig B.2). A smooth $T(r)$ profile is used to generate synthetic light curves at this station, one with the flux of the primary image only, and one with the sum of the fluxes of the primary and secondary images.

As expected, the inversion of the one-image light curve correctly retrieves the temperature at the 0.2 K accuracy level (Fig B.2), and the density and pressure profiles at the 0.1% accuracy level. Conversely, the inversion of the two-image light curve correctly retrieves the upper parts of the profiles, but it fails in reproducing the lower parts. For instance, at the deepest point reached by La Palma’s light curve, the primary flux is 0.061 (normalising the unocculted stellar flux to unity), while the secondary flux is 0.0072, about 8.5 times fainter than the primary flux. At that point, the temperature is retrieved to within 0.9 K and the pressure at the 1% level, a satisfactory result at our accuracy level.

However, this discrepancy rapidly increases as deeper levels are probed. For instance at $r \approx 1362$ km (9 km altitude level, where the temperature locally reaches a maximum; see the upper panel of Fig. B.2), the discrepancy between the original and retrieved temperature is about 3 K. We also note that in this case the retrieved temperature profile has an unrealistic behaviour as it extends below Triton’s surface. Although the pressure profile is satisfactorily retrieved even if the secondary image is present, it suffers nevertheless the same unrealistic behaviour as $T(r)$, as it also extends below Triton’s surface (lower panel of Fig. B.2).

In summary, the inversion procedure cannot provide reliable results below the 20 km altitude level. In particular the central flash region cannot be used in the inversion procedure. We note, more images can be produced in the central flash region for a non-spherical atmosphere.

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The inflection point labelled ‘3’ in Fig. B.1. The discontinuity of $dT/dr$ creates a very small kink at the corresponding point in the synthetic light curve (see the lower panel of Fig. B.1). This kink is well below the noise level of all the observed light curves, and thus, has a negligible effect on the fit to the data.
Fig. B.2. Effect of the secondary stellar image on the inversion results. 
*Upper panel:* Effect on the temperature profiles. The smooth black line connects these profiles to the surface at 38 K, where the pressure is set to 14 \( \mu \)bar. The resulting density profile is used to generate synthetic light curves that feed the Abel inversion procedure. The solid green line is the retrieved \( T(r) \) profile with only the primary image accounted for. The green dotted line is the retrieved profile where the primary and secondary images have been added. The profiles obtained from the inversion of La Palma’s light curve at ingress and egress (in red and blue, respectively) are shown for comparison (see also Figs. 9-11). Black horizontal solid and dotted lines show Triton’s surface and reference radius (1400 km). *Lower panel:* Same, but with the pressure profiles.

However, that the direct (ray-tracing) approach does include the primary and secondary fluxes, and as such, it can be used to constrain the atmospheric profiles in the central flash region.

**Appendix C: Fit to the data**
Fig. C.1. Data (black dots) fitted simultaneously with synthetic light curves (blue lines), based on the temperature profile displayed in Fig. 10 (black line) and the pressure boundary condition $p_{1400} = 1.18 \mu\text{bar}$ (Table 4). The green dots are the residuals of the fits. We note that the central flash regions have been excluded from the fit so that we obtain a global fit that is not influenced by the deepest atmospheric layers. The stations with exposure times smaller than 1 s have been smoothed to have a sampling time close to 1 s, allowing a direct visual comparison of S/N of the various datasets. The lower and upper horizontal dotted lines mark the zero-flux level and the total star plus Triton unocculted flux, respectively. We note that the three central-most stations (Constância, Le Beausset, and Felsina observatories in Fig. C) are plotted at a different vertical scale to accommodate the presence of a strong central flash. Each panel has a duration of five minutes and is centred around the time of closest approach (or mid-occultation time) of the station to Triton’s shadow centre. The stations are sorted from left to right and top to bottom from the northernmost track (Newark) to the southernmost track (Athens; see Fig. C), projected on Triton in the sky plane (Fig. 5). For reference, the vertical red lines mark 23:48 UTC for the European and African stations, and 23:55 UTC for the US stations (Newark, Ithaca, and Dark Sky observatories).
Fig. C.1 Continued.
Fig. C.1 Continued. NB. ‘JAVA,’ is the abbreviation of Javalambre, used so that the name of the station fits into the plot.
Fig. C.1 Continued.
Fig. C.1 Continued.
Fig. C.2. The same as Figs. C.1, but for stations that were not used in the simultaneous fit.
Fig. C.2 Continued.
Fig. C.2 Continued.
Fig. C.2 Continued.
### Table A.1. Circumstances of observations.

| Site          | Coordinates                  | Telescope aperture (m) | Exp. Time/Cycle (s) | Observers                           |
|---------------|------------------------------|------------------------|---------------------|-------------------------------------|
| **Site**      | **Altitude (m)**             | **Instrument/filter**  |                     | **Observers**                       |
| **Observations that provided light curves that are used in Triton’s atmospheric fit** | | | | |
| **Agerola**   | 40 37 26.2 N                 | CCD/clear              | 0.28                | 0.86/0.86                           | L. Morrone                          |
| **Italy**     | 14 33 50.6 E                 |                        |                     |                                     |                                     |
| **Albox**     | 37 24 20.0 N                 | CCD/clear              | 0.41                | 2.00/3.34                           | J. L. Maestre García                |
| **Spain**     | 02 09 07.0 W                 |                        |                     |                                     |                                     |
| **Alcantarilha** | 37 07 58.8 N               | CCD/red                | 0.36                | 0.33/0.64                           | F. Marques Dias                     |
| **Portugal**  | 08 21 54.0 W                 |                        |                     |                                     |                                     |
| **Algiers**   | 36 47 52.1 N                 | video/clear            | 0.81                | 0.04/0.04                           | D. Baba Aissa,                      |
| **Algeria**   | 03 01 56.2 E                 |                        |                     |                                     | Z. Grigahcene                       |
| **Ariana**    | 36 53 03.0 N                 | CCD/clear              | 0.20                | 0.50/0.60                           | S. Kamoun                           |
| **Tunisia**   | 10 11 42.0 E                 |                        |                     |                                     |                                     |
| **Athens**    | 37 58 06.8 N                 | CCD/clear              | 0.40                | 1.00/3.50                           | K. Gazeas,                          |
| **Greece**    | 23 47 00.1 E                 |                        |                     |                                     | E. Karampotsiou,                    |
| **Belgica**   | 43 26 39.4 N                 | video/clear            | 0.30                | 0.64/0.64                           | P. Andre,                           |
| **France**    | 01 48 58.6 E                 |                        |                     |                                     | M. Llibre,                          |
| **Boissettes** | 48 31 41.0 N               | CCD/clear              | 0.30                | 0.50/0.50                           | M. Irzyk                            |
| **France**    | 02 37 28.0 E                 |                        |                     |                                     |                                     |
| **Calar Alto** | 37 13 24.7 N               | VIS: 0.063/0.063       | 1.23                | VIS: 0.063/0.063                     | R. Hueso,                           |
| **(2 channels)** | 02 32 44.9 W               | SCMS/VIS: (0.4-1.0 μm) |                     | SWIR: 0.11/0.11                      | S. Pérez-Hoyos,                     |
| **Spain**     | 2160.0                       |                        |                     |                                     | A. Sánchez-Lavega                   |
| **Calern**    | 43 45 13.2 N                 | 1.04                  | 0.10/0.11           | J. Ferreira, P. Machado              |
| **France**    | 06 55 22.4 E                 | CCD/I'                 |                     | P. Tanga, J.-P. Rivet               |
| **Clanfield** | 1268.0                       |                        |                     |                                     |                                     |
| **England**   | 37 41 35.8 N                 | 0.80                  | 0.80/1.70           | G. Leto,                            |
| **Catania**   | 14 58 29.1 E                 | CCD/clear              |                     | R. Zamar Sanchez,                   |
| **Italy**     | 1725.0                       |                        |                     | P. Bruno, G. Occhipinti             |
| **Clanfield** | 50 56 19.2 N                 | 0.61                  | 0.16/0.16           | D. Briggs,                          |
| **England**   | 01 01 10.6 W                 | video/clear            |                     | S. Broadbent                        |
| **Constância**| 39 29 41.6 N                 | 0.51                  | 0.64/0.64           | R. Gonçalves,                       |
| **Portugal**  | 08 19 25.2 W                 | video/clear            |                     | M. Ferreira                         |
| **Côtes de Meuse** | 49 00 07.2 N               | 0.83                  | 0.06/0.06           | S. Renner,                          |
| **France**    | 05 41 06.6 E                 | EMCCD/clear            |                     | M. Kaschinski                       |
| **Cuq les Vielmur** | 44 29 05.0 N            | 0.20                  | 2.00/4.00           | A. Cailleau,                        |
| **France**    | 01 55 50.0 E                 | CCD/clear              |                     | V. Pic,                             |
| **Dark Sky Obs.** | 36 15 09.6 N          | 0.36                  | 1.50/2.50           | L. Granier                          |
| **United States** | 81 25 01.2 W           | CCD/clear              |                     | J. Pollock,                         |
| **Elvas**     | 38 50 47.6 N                 | 0.27                  | 0.30/0.30           | D. B. Caton                         |
| **Portugal**  | 07 12 27.4 W                 | CCD/clear              |                     | V. Kouprinov                        |
| **Felsina Obs.** | 44 21 22.0 N              | 0.40                  | 0.64/0.64           | W. Beisler                          |
| **Italy**     | 11 09 09.0 E                 | video/clear            |                     |                                     |
| **Forcarei**  | 42 36 38.4 N                 | 0.51                  | 0.64/0.64           | R. Di Luca,                         |
| **Spain**     | 08 22 15.1 W                 | video/clear            |                     | D. Alboreli                         |
| **Hartley Wintney** | 51 18 23.2 N              | 0.36                  | 1.00/3.31           | G. Thurston                         |

*Continued on next page*
Table A.1 – Continued from previous page.

| Site                     | Coordinates     | Telescope aperture (m) | Exp. Time/Cycle (s) | Observers                      |
|--------------------------|-----------------|------------------------|---------------------|--------------------------------|
| England                  | 00 54 44.9 W    | CCD/Johnson V          | 0.60/0.674          | E. M. Xilouris, I. Alikakos,   |
|              | 65.0            |                        |                     | A. Gourzelas, V. Charmandaris  |
| Greece                  | 37 59 08.1 N    | 2.28                   | 0.60/0.64           | F. Denyer                      |
|              | 22 11 54.6 E    | CCD/V+R                |                     |                               |
|              | 2323.0          |                        |                     |                               |
| Hornchurch              | 51 33 06.4 N    | 0.24                   | 0.64/0.64           |                               |
| England                 | 00 11 38.8 E    | video/clear            | 0.20/0.36           | J. Lloyd, M. El Moutamid, C. Lamearche |
|              | 14.0            |                        |                     |                               |
| Ithaca                  | 42 27 29.4 N    | 0.60                   | 0.20/0.36           |                               |
| United States           | 76 23 05.5 W    | CCD/clear              | 0.15/0.15           | S. Alonso, A. Román Reche      |
|              | 530.0           |                        |                     |                               |
| Javalambre Astrophysical Observatory (2 telescopes) | 40 02 30.6 N | 0.40 Rx40 CCD/clear 2.00/2.50 | R. Iglesias-Marzoa,          |
| Spain                   | 01 00 57.6 W    | 0.28 Excalibur CCD/clear 2.00/3.00 | J. Abril Ibáñez,           |
|              | 1955.0          |                        |                     |                               |
| Kryoneri (2 channels)   | 37 58 19.0 N    | 1.20                   | 0.19/0.20           |                               |
| Greece                  | 22 37 07.0 E    | sCMOS/R and I          | 0.6/0.635           |                               |
|              | 930.0           |                        |                     |                               |
| La Palma                | 28 45 43.2 N    | 2.00                   | 0.64/0.64           |                               |
| Spain                   | 17 52 39.3 W    | Liverpool Tel.         |                     | J. Marchant, B. Sicardy       |
|              | 2340.0          | CCD/I+Z                |                     |                               |
| La Carolina             | 38 16 27.0 N    | 0.64                   | 0.15/0.15           |                               |
| Spain                   | 03 36 55.0 W    | CCD/clear              | 0.20/0.20           | J. Desmars, R. Tanguy, J. David |
|              | 595.0           |                        |                     |                               |
| La Roche-Sur-Yon        | 46 32 48.4 N    | 0.40                   | 2.5/5.5             |                               |
| France                  | 01 19 37.8 W    | CMOS/clear             | 0.53/0.53           |                               |
|              | 48.0            |                        |                     | B. Timerson                   |
| Le Beausset             | 43 11 38.1 N    | 0.25                   | 2.00/6.80           |                               |
| France                  | 05 48 05.9 E    | video/clear            | 0.25/0.25           |                               |
|              | 197.0           |                        |                     |                               |
| Marrakech               | 31 35 16.2 N    | 0.60                   | 2.5/5.5             | A. Daassou, K. Barkaoui, Z. Benkhaldoun, M. Guennoun, J. Chouqar |
| Morocco                 | 08 00 46.9 W    | CCD/clear              | 1.50/2.10           | D. Lavandier, D. Walliang     |
|              | 494.0           |                        |                     |                               |
| Nancy                  | 48 39 51.6 N    | 0.25                   | 0.25/0.25           |                               |
| France                  | 06 09 28.7 E    | CCD/luminance          | 0.25/0.25           |                               |
|              | 284.0           |                        |                     |                               |
| Newark                  | 43 00 23.7 N    | 0.25                   | 0.53/0.53           |                               |
| United States           | 77 07 06.5 W    | video/clear            | 0.53/0.53           |                               |
|              | 165.0           |                        |                     |                               |
| Oukaimeden              | 31 12 23.0 N    | 0.50                   | 2.00/6.80           |                               |
| Morocco                 | 07 51 59.0 W    | CCD/clear              | 0.25/0.25           |                               |
|              | 2727.0          |                        |                     |                               |
| Paris                   | 48 52 17.0 N    | 0.15                   | 0.25/0.25           |                               |
| France                  | 02 23 07.0 E    | CCD/clear              | 0.25/0.25           |                               |
|              | 92.0            |                        |                     |                               |
| Pic du Midi Obs.        | 42 56 12.0 N    | 0.60                   | 0.05/0.05           |                               |
| France                  | 00 08 31.9 E    | EMCCD/visible          | 0.10/0.10           |                               |
|              | 2862.0          |                        |                     |                               |
| Puimichel               | 43 58 53.1 N    | 0.60                   | 0.10/0.10           |                               |
| France                  | 06 02 10.0 E    | EMCCD/visible          | 0.10/0.10           |                               |
|              | 714.0           |                        |                     |                               |
| Reading                 | 51 30 23.8 N    | 0.30                   | 0.64/0.64           |                               |
| England                 | 00 48 58.1 W    | video/red              | 0.32/0.32           |                               |
|              | 80.0            |                        |                     |                               |
| Sabadell                | 41 33 00.2 N    | 0.50                   | 0.16/0.16           |                               |
| Spain                   | 02 05 24.8 E    | video/clear            | 0.16/0.16           | A. Selva, C. Perello, V. Cabedo |
|              | 224.0           |                        |                     |                               |
| Saint Caprais (2 telescopes) | 43 52 25.9 N | 0.20 CCD/Johnson V 1.00/1.58 | A. Klotz, Y. Rieugnie, A. N. Klotz |
| France                  | 01 43 05.8 E    | 0.94 SWIR/clear        | 0.10/0.10           |                               |
|              | 285.0           |                        |                     |                               |
| Seysses                 | 43 30 06.3 N    | 0.31                   | 0.32/0.32           |                               |

Continued on next page
Table A.1 – Continued from previous page.

| Site                     | Coordinates Altitude (m) | Telescope aperture (m) Instrument/filter | Exp. Time/Cycle (s) | Observers                         |
|--------------------------|--------------------------|------------------------------------------|---------------------|-----------------------------------|
| France                   | 01 17 20.3 E 183.0       | video/UV-IR block                        |                     | J. L. Ortiz,                      |
| Sierra Nevada Spain      | 37 03 51.0 N 2925.8      | 1.50                                      | 0.04/0.04           | P. Santos-Sanz,                   |
| England                  | 01 22 28.1 W 16.0        | CMOS/clear                                | 0.25/0.25           | N. J. Haigh                       |
| Southampton Germany      | 50 55 18.9 N 346.0       | 0.40                                      | 0.64/0.64           | A. Eberle                         |
| Spain                    | 03 23 05.0 W 82.0        | video/clear                               |                     | K. Rapp                           |
| England                  | 00 19 35.4 E 163.0       | CCD/clear                                 |                     | M. Delcroix                       |
| Spain                    | 39 56 42.0 N 2160.0      | CCD/clear                                 | 0.50                | V. Peris,                         |
| England                  | 00 06 05.4 W 407.0       | CCD/clear                                 | 1.00/2.00           | O. Brevia                         |
| Spain                    | 02 32 44.9 W 407.0       | CCD/clear                                 |                     |                                  |
| England                  | 01 06 05.4 W 300.0       | InGaAs/RG1000 (effective λ=1.3 µm)       |                     |                                  |
| Spain                    | 37 03 24.0 N 59.0        | video/clear                               |                     |                                  |
| Italy                    | 16 55.2 W 660.0          | video/clear                               |                     |                                  |
| Italy                    | 37 33 50.6 E 191.0       | video/clear                               |                     |                                  |
| Spain                    | 37 03 24.0 N 191.0       | video/clear                               |                     |                                  |
| England                  | 37 33 36.4 E 191.0       | video/clear                               |                     |                                  |
| Spain                    | 37 32 44.9 W 191.0       | video/clear                               |                     |                                  |
| England                  | 37 32 44.9 W 595.0       | video/clear                               |                     |                                  |
| Spain                    | 51 19 09.4 N 59.0        | video/clear                               |                     |                                  |
| England                  | 00 04 01.4 W 695.0       | video/clear                               |                     |                                  |
| Spain                    | 52 01 59.3 N 685 nm long pass | video/clear                               |                     |                                  |

Observations that provided light curves that are not used in Triton's atmospheric fit

- Abingdon, England
- Agerola, Italy
- Calar Alto, Spain
- Caserta, Italy
- Catania, Italy
- Charles Fehrenbach Observatory, La Biette, France
- Glyfada-Athens, Greece
- Guirguillano, Spain
- Hamsey Green, England
- Houten, Netherlands
- La Hita Observatory (2 telescopes), Spain

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Table A.1 – Continued from previous page.

| Site                          | Coordinates | Telescope aperture (m) | Exp. Time/Cycle (s) | Observers          |
|------------------------------|-------------|------------------------|---------------------|--------------------|
|                              | Altitude    | Instrument/filter      |                     |                    |
| Lamandine                    | 44 12 35.0 N | 0.30                   | 0.06/0.06           | M. Miniou          |
| France                       | 01 42 01.7 E | CCD/clear              |                     |                    |
| La Sagra Observatory         | 37 58 58.1 N | 0.36 each              | 1.00/3.79 (tetra1)  | N. Morales,        |
| (4 telescopes)               | 02 34 05.1 W | tetra1, tetra2: CCD/clear | 1.00/3.56 (tetra2)  | J. L. Ortiz,       |
| Spain                        | 15 30.0     | tetra3, tetra4: video/clear | 0.20/0.20          | P. Santos-Sanz     |
| Leeds                        | 53 50 15.6 N | 0.20                   | 1.28/1.28           | A. Pratt           |
| England                      | 01 36 27.8 W | video/IR-UV block      |                     |                    |
|                              | 113.0       |                        |                     |                    |
| Liás                         | 43 33 33.3 N | 0.40                   | 0.13/0.13           | F. Metz,           |
| France                       | 01 06 34.4 E | CCD/clear              |                     | D. Erpelding,      |
|                              | 300.0       |                        |                     | J.-P. Nougayrède   |
| Louargat                     | 48 32 16.7 N | 0.30                   | 0.20/0.20           | B. Reginato,       |
| France                       | 03 21 30.5 W | CMOS/L                 |                     | E. Reginato        |
|                              | 196.0       |                        |                     |                    |
| Massa                        | 44 01 17.2 N | 0.20                   | 5.12/5.12 (1st half)| P. Baruffetti      |
| Italy                        | 10 07 56.7 E | video/clear            | 2.56/2.56 (2nd half)|                    |
| Montigny le Bretonneux       | 48 45 54.0 N | 0.28                   | 0.50/0.51           | O. Dechambre       |
| France                       | 02 00 52.0 E | CCD/clear              |                     |                    |
|                              | 168.0       |                        |                     |                    |
| Mount Agliale Observatory    | 43 59 43.1 N | 0.50                   | 1.50/3.23           | F. Ciabattari      |
| Italy                        | 10 30 53.8 E | CCD/clear              |                     |                    |
|                              | 750.0       |                        |                     |                    |
| Nerpio                       | 38 09 56.0 N | 0.32                   | 1.00/16.11          | E. Briggs          |
| Spain                        | 02 19 35.0 W | CCD/clear              |                     |                    |
|                              | 1650.0      |                        |                     |                    |
| Neutraubling                 | 48 59 23.1 N | 0.28                   | 0.16/0.16           | B. Kattentidt      |
| Germany                      | 12 12 57.3 E | video/clear            |                     |                    |
|                              | 333.0       |                        |                     |                    |
| Nice                         | 43 43 32.9 N | 0.13                   | 2.00/2.00           | M. Conjat          |
| France                       | 07 17 59.4 E | video/clear            |                     |                    |
|                              | 350.0       |                        |                     |                    |
| Observatoire de Biscarmiau   | 43 08 40.4 N | 0.31                   | 0.64/0.64           | G. Vaudescal       |
| France                       | 00 03 31.8 E | video/clear            |                     |                    |
|                              | 488.0       |                        |                     |                    |
| Observatoire des Baronnies Provençales | 44 24 29.7 N | 0.80                 | 2.00/2.00           | M. Bretton         |
| France                       | 05 30 54.4 E | CCD/clear              |                     |                    |
|                              | 820.0       |                        |                     |                    |
| Observatoire Monplaisir      | 43 40 58.3 N | 0.28                   | 1.03/1.49           | J. Ardissone       |
| France                       | 04 38 32.6 E | CCD/clear              |                     |                    |
|                              | 5.0         |                        |                     |                    |
| Ocremont                     | 48 35 28.0 N | 0.10                   | 10.00/10.15         | P. Delay           |
| France                       | 01 48 45.0 E | CCD/IR cut             |                     |                    |
|                              | 165.0       |                        |                     |                    |
| Overath                      | 50 57 11.4 N | 0.20                   | 0.32/0.32           | B. Klemt           |
| Germany                      | 07 14 53.1 E | video/clear            |                     |                    |
|                              | 200.0       |                        |                     |                    |
| Pfünz                        | 48 53 26.0 N | 0.28                   | 1.00/1.20           | B. Gährenk         |
| Germany                      | 11 16 23.0 E | CCD/clear              |                     |                    |
|                              | 488.0       |                        |                     |                    |
| Pic du Midi Obs.             | 42 56 12.0 N | 1.05                   | 0.10/0.10           | F. Colas           |
| France                       | 00 08 31.9 E | sCMOS/clear            |                     |                    |
|                              | 2862.0      |                        |                     |                    |
| Rosenfeld-Britzheim          | 48 17 17.8 N | 0.80                   | 0.40/0.40           | S. Kowollik,       |
| Germany                      | 08 40 38.9 E | CMOS/UV-IR block       |                     | R. Bitzer          |
|                              | 700.0       |                        |                     |                    |
| Saint Chéron                 | 48 32 16.6 N | 0.18                   | 0.08/0.08           | J. Berthier        |
| France                       | 02 07 51.7 E | video/clear            |                     |                    |
|                              | 160.0       |                        |                     |                    |

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Table A.1 – Continued from previous page.

| Site                      | Latitude (°) | Altitude (m) | Telescope aperture (m) | Exp. Time/Cycle (s) | Observers               |
|---------------------------|--------------|--------------|------------------------|---------------------|-------------------------|
| Saint-Maurice-Navacelles  | 43 50 39.3 N | 583.0        | 0.21 CCD/clear          | 0.64/0.64           | J. Lecacheux            |
| France                    | 03 33 47.3 E | 33           |                        |                     |                         |
| Saint Michel              | 43 54 23.3 N | 564.0        | 0.60 EMCCD/clear        | 0.05/0.05           | E. Meza, O. Labrevoir   |
| France                    | 05 43 34.7 E | 33           |                        |                     |                         |
| Selzthal Obs. Friesenheim | 49 50 00.0 N | 0.51         | CMOS/clear              | 0.8/0.8             | G. M. Pielker           |
| Germany                   | 110.0        | 33           |                        |                     |                         |
| Seysses                   | 43 30 06.3 N | 183.0        | 0.23 video/UV-IR block  | 0.32/0.32           | J. Sanchez              |
| France                    | 01 17 20.3 E | 33           |                        |                     |                         |
| Sierra Nevada             | 37 03 51.0 N | 2925.8       | 0.90 CCD/clear          | 1.00/3.33           | J. L. Ortiz, P. Santos-Sanz, V. Casanova |
| Spain                     | 03 23 05.0 W | 33           |                        |                     |                         |
| Valle d’Aosta             | 45 47 23.1 N | 445.0        | 0.81 EMCCD/clear        | 0.2/0.2             | D. Cenadelli, J.-M. Christille, B. Sicardy |
| Italy                     | 07 28 42.3 E | 1675.0       |                        |                     |                         |
| Stations with technical or weather problems that provided no light curves |               |              |                        |                     |                         |
| Bilbao                    | 43 15 43.6 N | 47.0         | 0.5 CCD/clear           |                     | S. Pérez-Hoyos, A. Sánchez-Lavega |
| Spain                     | 02 56 54.6 W | 33           |                        |                     |                         |
| Buthiers                  | 48 17 30.0 N | 87.0         | 0.59 CMOS/L             | 0.10/0.10           | J. L. Dauvergne         |
| France                    | 02 26 18.0 E | 33           |                        |                     |                         |
| Cavarc Observatory        | 44 40 35.2 N | 100.0        | 0.50 CMOS/clear         |                     | J. Rudelle, B. Tregon   |
| France                    | 00 37 43.1 E | 33           |                        |                     |                         |
| Comthurey                 | 53 15 57.8 N | 74.0         | 0.18 CMOS/clear         |                     | K. Guhl                 |
| Germany                   | 13 11 24.6 E | 33           |                        |                     |                         |
| Emmendingen               | 48 06 14.2 N | 210.0        | 0.18 CMOS/clear         | 3.00/3.33           | K.-L. Bath              |
| Germany                   | 07 51 28.6 E | 33           |                        |                     |                         |
| Eppstein-Bremthal         | 50 08 17.4 N | 256.0        | 0.25 video/clear        |                     | O. Klös                 |
| Germany                   | 08 21 50.4 E | 33           |                        |                     |                         |
| Gnosca                    | 46 13 53.2 N | 260.0        | 0.40 CMOS/clear         |                     | S. Sposetti             |
| Switzerland               | 09 01 26.5 E | 33           |                        |                     |                         |
| Grapfontaine              | 49 48 54.2 N | 445.0        | 0.28 video/clear        |                     | F. Van Den Abbeel       |
| Belgium                   | 05 23 57.5 E | 33           |                        |                     |                         |
| Hamburg-Bergedorf         | 53 28 50.0 N | 25.0         | 0.60 CMOS/clear         |                     | V. Perdelwitz           |
| Germany                   | 10 14 29.0 E | 33           |                        |                     |                         |
| Handeloh                  | 53 14 06.4 N | 60.0         | 0.35 CMOS/clear         |                     | K. von Poschinger       |
| Germany                   | 09 49 46.7 E | 33           |                        |                     |                         |
| Observatory Hoher List    | 50 09 42.0 N | 60.0         | 1.00 CMOS/clear         |                     | M. Miller, G. Herbogenrath, D. Frangenber, L. Brandis, I. Pütz |
| Eifel                     | 06 50 55.0 E | 33           |                        |                     |                         |
| Germany                   | 549.0        | 33           |                        |                     |                         |
| Labastide-Murat           | 44 38 43.2 N | 445.0        | 0.20 video/clear        | 0.32/0.32           | E. Frappa               |
| France                    | 01 34 13.9 E | 33           |                        |                     |                         |
| Lauenbrück                | 53 12 26.6 N | 31.0         | 0.50 CMOS/clear         |                     | M. Kretlow              |
| Germany                   | 09 34 36.1 E | 33           |                        |                     |                         |
| Malvilliers               | 47 01 38.5 N | 33           | 0.30 CMOS/clear         |                     | L. Falco                |
| Switzerland               | 06 52 03.0 E | 33           |                        |                     | R. Leiva                |

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Table A.1 – Continued from previous page.

| Site                     | Coordinates | Telescope aperture (m) | Exp. Time/Cycle (s) | Observers              |
|--------------------------|-------------|------------------------|---------------------|------------------------|
| EXPO Observatory         | 52 15 45.0 N | 1.12                   | 0.04/0.04           | P. Riepe, E. Bredner   |
| Melle                    | 08 20 12.0 E | video/clear            |                     |                        |
| Germany                  | 185.0       |                        |                     |                        |
| Meudon                   | 48 48 18.3 N | 1.00                   |                     | T. Widemann, W. Thuillot, |
| France                   | 02 13 51.6 E | CMOS/clear             |                     | D. Hestroffer, E. Lellouch |
| Ondřejov                 | 49 54 33.8 N | 0.50                   | 0.04/0.04           | M. Jelínek, J. Strobl  |
| Czech Republic           | 14 46 52.9 E | EMCCD/R                |                     |                        |
| Saint-Luc Obs. F.-X. Bagnoud | 46 13 41.8 N | 0.30                   |                     | E. Bouchet, M. Cottier |
| Switzerland              | 2200.0      |                        |                     |                        |
| Saulges                  | 47 59 02.0 N | 0.25                   | 0.20/0.20           | T. Midavaine           |
| France                   | 00 24 30.0 W | video/clear            |                     |                        |
| TRAPPIST-North           | 31 12 22.0 N | 0.60                   |                     | E. Jehin               |
| Oukaimeden Morocco        | 07 51 59.0 W | CCD/clear              |                     |                        |
| Uranoscope (2 telescopes) | 48 44 32.0 N | 0.28 video/clear       | 0.25/0.25           | A. Leroy, S. Bouley    |
| France                   | 02 44 32.0 E | 0.36 CMOS/clear        | 0.25/0.25           |                        |
| Valé de Joux             | 46 37 06.0 N | 0.61                   | 1.00/1.15           | R. Barbosa, R. Behrend |
| Switzerland              | 06 13 10.0 E | CMOS/clear             |                     | M. Spano               |
| Vierzon                  | 47 13 23.7 N | 0.25                   |                     | L. Rousselot           |
| France                   | 02 03 09.8 E | CMOS/clear             |                     |                        |
| Zurich                   | 47 24 27.8 N | 0.50                   | 2.00/4.00           | S. Gallego, L. Tortorelli |
| Switzerland              | 08 30 39.5 E | CCD/Johnson R          |                     |                        |
|                         | 553.0       |                        |                     |                        |

Previous occultations

**18 July 1997**

| Brownsville | 25 58 40.9 N | 0.35 | 0.5/0.5 | W. B. Hubbard, H. J. Reitsema, R. Hill |
| United States | 97 32 11.3 W | CCD/clear |                     |                        |
| Bundaberg | 24 56 37.5 S | 0.48 | 0.33/0.33 | E. Hummel, M. Moy, I. Pink, R. Walters |
| Australia | 152 22 35.4 E | 0.35 | 0.66/0.66 | L. Ball, G. Nielsen |
| Ducabrook | 23 53 55.0 S | 0.35 | 0.66/0.66 | W. Beisker, S. Hutcheon |
| Australia | 147 26 40.0 E | 0.35 | 0.66/0.66 |                        |
| Lochington | 23 56 42.5 S | 0.35 | 0.66/0.66 |                        |
| Australia | 147 31 24.8 E | 0.35 | 0.66/0.66 |                        |
| Ballandean Australia | 28 49 05.0 S | 0.48 | 0.48 | K. Lay |
| Australia | 151 48 36.0 E | Visual |                     |                        |
| Ipswich Australia | ~27 38 S | 0.30 | 10 | B. Downs |
| Australia | ~152 45 E | CCD/clear | grazing |                        |
| The Gap Australia | 27 27 42.3 S | 0.40 | 0.40 | P. Anderson |
| 21 May 2008

| Hako | 23 14 11.0 S | 0.5 | 0.67/1.49 | K.-L. Bath |
| Namibia | 16 21 41.5 E | CCD/clear |                     |                        |

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### Table A.1 – Continued from previous page.

| Site          | Coordinates (Altitude (m)) | Telescope aperture (m) | Exp. Time/Cycle (s) | Observers  |
|---------------|----------------------------|------------------------|---------------------|------------|
| Hakos Namibia | 23 14 11.0 S, 16 21 41.5 E | 0.45, 0.23             | 0.84/1.0, 2.56/2.56 | B. Sicardy, J. Lecacheux |
| Maïdo Frane   | 21 04 15.5 S, 55 23 14.2 E | 0.35, 0.23             | 1.48/1.48, 1.48/1.48| H.-J. Bode, T. Payet |
| Tivoli Namibia| 23 27 40.2 S, 18 01 01.2 E | 0.35, 0.28             | 1.48/1.48, 1.48/1.48| H.-J. Bode, T. Payet |
| Hakos Namibia | 23 14 11.0 S, 16 21 41.5 E | 0.45, 0.23             | 0.84/1.0, 2.56/2.56 | B. Sicardy, J. Lecacheux |
| Maïdo Frane   | 21 04 15.5 S, 55 23 14.2 E | 0.35, 0.23             | 1.48/1.48, 1.48/1.48| H.-J. Bode, T. Payet |
| Tivoli Namibia| 23 27 40.2 S, 18 01 01.2 E | 0.35, 0.28             | 1.48/1.48, 1.48/1.48| H.-J. Bode, T. Payet |

**Observations that provided light curves that are not used in Triton’s atmospheric fit**

| Site            | Coordinates (Altitude (m)) | Telescope aperture (m) | Exp. Time/Cycle (s) | Observers   |
|-----------------|----------------------------|------------------------|---------------------|-------------|
| Hakos Namibia   | 23 14 11.0 S, 16 21 41.5 E | 0.45, 0.23             | 0.84/1.0, 2.56/2.56 | B. Sicardy, J. Lecacheux |
| Maïdo Frane     | 21 04 15.5 S, 55 23 14.2 E | 0.35, 0.23             | 1.48/1.48, 1.48/1.48| H.-J. Bode, T. Payet |
| Tivoli Namibia  | 23 27 40.2 S, 18 01 01.2 E | 0.35, 0.28             | 1.48/1.48, 1.48/1.48| H.-J. Bode, T. Payet |

**Stations with technical or weather problems that provided no light curves**

| Site            | Coordinates (Altitude (m)) | Telescope aperture (m) | Exp. Time/Cycle (s) | Observers   |
|-----------------|----------------------------|------------------------|---------------------|-------------|
| Hakos Namibia   | 23 14 11.0 S, 16 21 41.5 E | 0.45, 0.23             | 0.84/1.0, 2.56/2.56 | B. Sicardy, J. Lecacheux |
| Maïdo Frane     | 21 04 15.5 S, 55 23 14.2 E | 0.35, 0.23             | 1.48/1.48, 1.48/1.48| H.-J. Bode, T. Payet |
| Tivoli Namibia  | 23 27 40.2 S, 18 01 01.2 E | 0.35, 0.28             | 1.48/1.48, 1.48/1.48| H.-J. Bode, T. Payet |

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