Phase diagram of a superconductor / ferromagnet bilayer

M. Lange, M. J. Van Bael, and V. V. Moshchalkov

Laboratory for Solid State Physics and Magnetism,
Nanoscale Superconductivity and Magnetism Group,
K.U. Leuven, Celestijnenlaan 200 D, 3001 Leuven, Belgium

(Dated: March 22, 2022)

The magnetic field \( (H) \) - temperature \( (T) \) phase diagram of a superconductor is significantly altered when domains are present in an underlying ferromagnet with perpendicular magnetic anisotropy. When the domains have a band-like shape, the critical temperature \( T_c \) of the superconductor in zero field is strongly reduced, and the slope of the upper critical field as a function of \( T \) is increased by a factor of 2.4 due to the inhomogeneous stray fields of the domains. Field compensation effects can cause an asymmetric phase boundary with respect to \( H \) when the ferromagnet contains bubble domains. For a very inhomogeneous domain structure, \( T_c \propto H^2 \) for low \( H \) and \( T_c \propto H \) for higher fields, indicating a dimensional crossover from a one-dimensional network-like to a two-dimensional behavior in the nucleation of superconductivity.

PACS numbers: 74.25.Dw 74.25.Ha 74.76.Db 75.70.Kw

I. INTRODUCTION

In hybrid superconductor / ferromagnet (SC/FM) bilayers the FM modifies quite substantially the superconducting properties of the SC layer. In particular, strong vortex pinning was reported recently for superconducting films covering arrays of ferromagnetic dots with in-plane and out-of-plane magnetization \(^7,8,9,10\) and for continuous SC/FM bilayers. \(^6,7,8,9,10\) Theoretical investigations showed that supercurrents and vortices can be induced in the SC by the stray field of the FM \(^13,14,15,16\) and that the domain structure of soft FM's can be influenced by the presence of the SC. \(^15\) Furthermore, \(^15\) Radovic et al predicted the appearance of the so-called \( \pi \)-phase state in SC/FM multilayers, where the phase of the superconducting order parameter \( \psi \) shifts by \( \pi \) when crossing a ferromagnetic layer. \(^16\) Recently the existence of the \( \pi \)-phase state was confirmed by observing sharp cusps in the temperature dependence of the critical current in SC/FM/SC junctions. \(^13\) Earlier experiments were performed in order to find the \( \pi \)-phase state by measuring the predicted oscillatory dependence of the critical temperature \( T_c \) of SC/FM multilayers on the FM layer thickness \( d_{fm} \). \(^10,13,14,15,16\) However, the results of these experiments were not conclusive, because the nonmonotonic \( T_c(d_{fm}) \) behavior could also appear due to the presence of magnetically ”dead” layers at the SC/FM interfaces. \(^23\)

The theory of the anomalous \( T_c(d_{fm}) \) dependence is based on the Usadel equations describing the proximity effect of FM and SC layers, but neglecting a possible influence of the domains in the FM. In this manuscript we will show that an inhomogeneous stray field \( B_{stray} \) produced by the domain structure of a FM can actually also lead to a significant change in \( T_c \). To demonstrate this effect, we measure \( T_c \) as a function of the perpendicularly applied magnetic field \( H \) of a Pb film on top of a Co/Pt multilayer with perpendicular magnetic anisotropy. In this sample the proximity effect is suppressed by an amorphous Ge layer between Pb and Co/Pt. The domain structure in the Co/Pt multilayer can consist of stable band or bubble domains. The FM layer can also be in a single domain state, depending on the preceding magnetization procedure, as was shown in a recent study of the vortex pinning in this system. \(^20\) Due to field cancellation effects between \( H \) and \( B_{stray} \), and due to the suppression of \( \psi \) by \( B_{stray} \), \( T_c(H) \) can be controlled by changing the microscopic domain structure.

II. MAGNETIC PROPERTIES OF THE Co/Pt MULTILAYER

The properties of the Co/Pt multilayer have been described before. \(^10\) Briefly, the multilayer has a \([\text{Co}(0.4 \text{ nm})/\text{Pt}(1.0 \text{ nm})]_{10}\) structure on a 2.8 nm Pt base layer on a Si/SiO\(_2\) substrate. The magnetic properties were characterized by the magneto-optical Kerr effect (MOKE) and magnetic force microscopy (MFM), revealing that the sample has perpendicular magnetic anisotropy. Fig. \(4\) shows the magnetization \( M_{fm} \) of the Co/Pt multilayer measured by MOKE, normalized to the saturation magnetization \( M_{sat} \), as a function of the magnetic field \( H \) applied perpendicular to the surface. The loop has an almost rectangular shape with \( \mu_0 H_n = 60 \text{ mT} \), \( \mu_0 H_c = 93 \text{ mT} \), and \( \mu_0 H_s = 145 \text{ mT} \), where \( H_n, H_c \) and \( H_s \) are the nucleation, coercive and saturation field, respectively, and \( \mu_0 \) is the permeability of the vacuum.

Using different magnetization procedures, one can produce different stable domain patterns in the sample. For instance, after out-of-plane demagnetization, band domains are observed by MFM, see Fig. \(4b\). Stable bubble domains with local magnetic moments \( m \) either pointing up \( (m_z > 0) \) or down \( (m_z < 0) \) perpendicular to the sample surface can be created by applying a negative field of \(-1 \text{ T}\), sweeping \( H \) to a positive value between \( H_n \) and
In the demagnetized state the lateral size of the domain is larger (because band domains are extended in one direction). Note also that in the demagnetized state, the boundary between domains with magnetization pointing up and down is well defined, but not straight: several sharp corners of different angles can be seen. No MFM images could be obtained for the $s = 0.5$ state, caused by the difficult magnetization procedure due to the steep slope of the $M_{fm}(H)$ curve, see Fig. 1(a). However, from the image of the $s = 0.3$ state, see Fig. 1(c), one can observe that the domain walls are less sharp defined than in the demagnetized state.

### III. Phase Boundary of the Superconducting Film

After characterizing the properties of the FM, a 10 nm Ge film, a 50 nm Pb film and a 30 nm Ge capping layer are subsequently evaporated on the Co/Pt multilayer at a substrate temperature of 77 K. The amorphous Ge film between Pb and Co/Pt is insulating at low temperatures, so that the proximity effects between Pb and Co/Pt are suppressed. The upper critical field $H_{c2}$ of bulk type-II SCs is given by

$$
\mu_0 H_{c2}(T) = \frac{\Phi_0}{2\pi\xi^2(T)},
$$

with $\Phi_0 = 2.068$ mT $\mu m^2$ the superconducting flux quantum, $\xi(T) = \xi(0)/\sqrt{1 - T/T_{c0}}$ the temperature dependent coherence length in the dirty limit, and $T_{c0}$ the critical temperature at zero field. Hence, the linear slope of $H_{c2}$ as a function of temperature is only determined by the coherence length $\xi$.

$H_{c2}(T)$ can behave differently when the geometry of the SC is changed, e.g. for thin films with thickness $w < \xi(T)$. While eq. (1) is still valid for thin type-II superconducting films with $H$ applied perpendicular to the sample surface, $T_c$ for parallel $H$ is given by

$$
T_c(H) = T_{c0}[1 - \frac{\pi^2\xi^2(0)w^2}{3\Phi_0^2}\mu_0^2 H^2],
$$

with $T_{c0}$ the zero-field critical temperature. In fact, this formula also gives the phase boundary of a mesoscopic line in perpendicular field, because the cross section, exposed to the applied field, is the same for a film of thickness $w$ in parallel $H$ and for a mesoscopic line in perpendicular $H$. For multiply connected mesoscopic lines, $T_c(H)$ can show an even more complex behavior due to fluxoid quantization effects.

The phase boundary of the SC/FM bilayer was measured in a Quantum Design superconducting quantum interference device (SQUID) magnetometer with $H$ applied perpendicular to the surface. Fig. 1 shows the data obtained in two field cooled measurements of the total magnetization $M = M_{fm} + M_{sc}$ ($M_{sc}$ is the magnetization of the SC) at the applied field of $\mu_0 H = 0.5$ mT.

---

**FIG. 1:** Magnetic properties of the Co/Pt multilayer: (a) Hysteresis loop measured by magneto-optical Kerr effect with $H$ perpendicular to the sample surface. MFM images ($5 \times 5 \mu m^2$) show that the domain structure of the sample consists of band domains after out-of-plane demagnetization (b), bubble domains in the $s = 0.3$ (c) and $s = 0.93$ (d) states. $H_s$, and then removing $H$. The parameter $s$, which gives the fraction of magnetic moments that are pointing up ($m_z > 0$) to the total amount of magnetic moments, is used to describe the different remanent magnetic states obtained after this magnetization procedure. The value of $s$ can be found from the MFM images by dividing the dark area ($m_z > 0$) by the total area, or from measurements of $M_{fm}$ as will be described later.

The lateral size of the domain structures can be estimated from the MFM images. The typical diameter of the bubble domains is about $\sim 300$ nm. The same value is obtained for the average width of the band domains. Although the magnetic moments of the Co/Pt multilayer are equally distributed between up- and down-directions in both the demagnetized and the $s = 0.5$ state, there are distinct differences between these two domain states:

- For multiply connected mesoscopic lines, $T_c(H)$ can show an even more complex behavior due to fluxoid quantization effects.

- The phase boundary of the SC/FM bilayer was measured in a Quantum Design superconducting quantum interference device (SQUID) magnetometer with $H$ applied perpendicular to the surface. Fig. 1 shows the data obtained in two field cooled measurements of the total magnetization $M = M_{fm} + M_{sc}$ ($M_{sc}$ is the magnetization of the SC) at the applied field of $\mu_0 H = 0.5$ mT.
after the samples were brought in the $s = 0.5$ and $s = 0$ states. Above $T_c$, $M$ has a constant value for both states, given by the contribution of the FM $M_{fm}$, from which $s$ can be derived. When the sample is cooled through $T_c$, a diamagnetic response of the SC appears. These kinds of measurements were used to determine $T_c(H)$ as the temperature where $M$ starts to deviate from $M_{fm}$. Repeating these measurements at several applied fields $|H| < 25$ mT did not change the offset $M_{fm}$ above $T_c$, implying an unchanged domain state.

A. $T_c(H)$ with magnetized FM

The phase boundary for the $s = 0$ state (all $m_z < 0$) obtained by several $M(T)$ measurements in varying fields is shown in Fig. 1(a). A linear behavior of the phase boundary is observed, which can be fitted by eq. (1) with $\xi(0) = (41.2 \pm 0.2)$ nm and $T_{c0} = (7.227 \pm 0.002)$ K. This implies that in this state, the FM no influence on the superconducting film, because both the linear behavior and the values of $T_{c0}$ and $\xi(0)$ are in good agreement with those of pure Pb films. It is important to note that the temperature dependence of $\xi(T) = \xi(0)/\sqrt{T - T_{c0}}$ derived for this domain state is the same for all domain states, since we are always dealing with the same Pb film. Let us consider the magnetic stray field $B_{stray}$ of a homogeneously magnetized film in the $s = 0$ state, schematically drawn in Fig. 1(b). $B_{stray}$ has its largest amplitude at the sample boundary and is negligible above the center of the FM. Intuitively this can be understood by considering the stray field of a single magnetic dipole in the center of the sample: The negative field above the dipole is compensated by the returning positive stray field of the surrounding magnetic dipoles. Therefore, the main central part of the superconductor is only weakly influenced by $B_{stray}$, and the measured $T_c(H)$ curve resembles the one of a single Pb film.

B. $T_c(H)$ with demagnetized FM

The phase boundary for the demagnetized state, corresponding to the MFM image shown in Fig. 1(b), is shown in Fig. 1(a). In this state, $T_{c0}$ is suppressed to $(7.048 \pm 0.002)$ K. Moreover, the phase boundary still shows a linear behavior, but with a slope increased by a factor of 2.4. The difference between the phase boundaries in the demagnetized and the $s = 0$ state can be attributed to the influence of the stray field $B_{stray}$, suppressing the order parameter in the superconductor above $T = 7.048$ K. The coherence length at this temperature is $\xi = 260$ nm. This means that superconductivity nucleates when the value of $\xi$ becomes smaller than approximately the width of the band domains. The nucleation first takes place in regions of the Pb film where the effective field in the $z$-direction $\mu_0 H_{eff,z} = \mu_0 H_z + B_{stray,z}$ is minimum. The confinement of these superconducting nuclei leads to the different $T_c(H)$ dependence compared to the magnetized state. Aladyshkin et al. have very recently calculated the $T_c(H)$.
FIG. 4: (a) Magnetic field - temperature phase diagram of the superconducting Pb film covering the Co/Pt multilayer. The Co/Pt multilayer was demagnetized before measuring $T_c(H)$. As a reference we have added the phase boundary of the $s = 0$ state. The dashed lines are guides to the eye. (b) Schematic drawing of the stray field $B_{\text{stray}}$ when the FM has been demagnetized.

FIG. 5: (a) Magnetic field - temperature phase diagrams of the superconducting Pb film covering the Co/Pt multilayer. Before measuring $T_c(H)$, the Co/Pt multilayer was brought into the $s = 0.1$ and $s = 0.85$ states.

two dimensions.

C. $T_c(H)$ with bubbles in the FM

The phase boundary shown in Fig. 5(a) is obtained when the Co/Pt multilayer contains bubble domains. Fig. 5 and Fig. 4 are symmetric with respect to $H$, i.e., $T_c$ is the same for positive or negative $H$, but the presence of the bubble domains causes an asymmetry of $T_c$ with respect to $H$. For bubbles having positive magnetic moments, i.e., $s < 0$, a higher $T_c$ is observed for positive $H$ than for corresponding negative $H$, whereas for bubbles containing negative magnetic moments ($s > 0.5$), $T_c$ is higher for negative $H$. Moreover, both $T_c(H)$ curves shown in Fig. 5(a) show a non-linear behavior with bumps in the field ranges around $|\mu_0 H| \approx 5 - 10$ mT.

To explain the asymmetric $T_c(H)$ curves, let us assume that the sample contains bubble domains with $m_z > 0$ in a matrix of magnetic moments with $m_z < 0$, as shown in Fig. 5(b): $B_{\text{stray,}z}$ is positive above the bubbles and negative between them. A positive $H$ in the $z$-direction compensates the negative $B_{\text{stray,}z}$ between the bubbles and enhances $B_{\text{stray,}z}$ above them, while a negative $H$ has the opposite effect: it enhances $B_{\text{stray,}z}$ between the bubbles and compensates $B_{\text{stray,}z}$ above them. The important point that causes the asymmetric phase boundary is that the absolute value of $B_{\text{stray,}z}$ is larger above
the $m_z > 0$ regions (bubbles) compared to the $m_z < 0$ regions (between the bubbles). When the sample is cooled in positive $H$, superconductivity can nucleate at higher temperatures in the area between the bubbles (where $B_{\text{stray},z} < 0$), compared to cooling the sample in the corresponding negative $H$, where the nucleation takes place in the areas above the bubbles. Note that qualitatively similar non-linear $T_c(H)$ curves as those presented in Fig. 5(a) have also been predicted by Aladyshkin et al.\textsuperscript{30}

The critical temperature of the superconductor decreases when the bubble domains have larger density. To illustrate this effect, Fig. 6 shows the dependence of $T_c(H=0)$ on the parameter $s$. A clear minimum of $T_c$ is observed around $s = 0.5$, which indicates that this domain state has the largest value of the stray field of all investigated domain structures. Note that $T_c$ of the $s = 0.5$ state is even lower than $T_c$ of the demagnetized state, emphasizing the inhomogeneous character of the $s = 0.5$ state. The phase boundary of this domain state will be discussed in the next section.

D. $T_c(H)$ with the FM in the $s = 0.5$ state

The phase boundary of the SC with the FM in the $s = 0.5$ state is shown in Fig. 7. In this domain state, $B_{\text{stray}}$ has a more inhomogeneous character than in the demagnetized state. For a discussion of the differences between these two domain states we refer to section II. $T_c(H)$ follows a non-linear behavior, in contrast to the demagnetized and the $s = 0$ states. $T_c(H)$ for the $s = 0.5$ state can not be described by eq. 1 but rather by eq. 2 in fields $\mu_0H < 15$ mT, see the fit in Fig. 7(b). This indicates that in the $s = 0.5$ state the regions where superconductivity nucleates can be considered as superconducting strips with a width $w \leq \xi(T)$, forming a sort of a superconducting network. When fitting the $T_c(H)$ curve using eq. 2 and $\xi(0) = 41.2$ nm (from the phase boundary for $s = 0$), we obtain values of $w = (213 \pm 6)$ nm and $T_{c0} = (6.994 \pm 0.003)$ K. The value of $w$ determined from this fit can be compared with the typical bubble domain size of $\sim 300$ nm. For $\mu_0H > 15$ mT and $T < 6.90$ K, $T_c(H)$ shows a crossover from the one-dimensional network like to a two-dimensional linear behavior, because the assumption $w < \xi(T)$ for eq. 2 is no longer fulfilled. This is in agreement with the value of $\xi(6.90$ K $) = 194$ nm.

IV. CONCLUSION

In conclusion, the phase boundary between the normal and the superconducting state of FM/SC bilayers has been found to be strongly dependent on the domain structure in the FM. The stray field $B_{\text{stray}}$ of these domains can lead to a significant decrease of $T_c$ in zero applied field, but, on the other hand, it can also enhance $T_c$ in applied fields. It has been demonstrated that the presence of bubble domains leads to the formation of the field-polarity dependent asymmetric phase boundaries $T_c(H)$ with respect to $H$, due to compensation effects between $H$ and $B_{\text{stray}}$. For a specific inhomogeneous domain structure, the $T_c(H)$ phase boundary shows a crossover from a one-dimensional to a two-dimensional nucleation behavior.
Acknowledgments

The authors thank L. Van Look, K. Temst and G. Güntherodt for help with sample preparation, J. Swerts for MOKE measurements and Y. Bruynseraede for fruitful discussions. This work was supported by the Fund for Scientific Research - Flanders (Belgium) (F.W.O.-Vlaanderen), by the Belgian IUAP and the European ESF "VORTEX" Programs, and by the Research Fund K.U.Leuven GOA. ML and MJVB are Postdoctoral Research Fellows of the F.W.O.-Vlaanderen.

* Electronic address: martin.lange@fys.kuleuven.ac.be

1. Y. Otani, B. Pannetier, J. P. Nozières, and D. Givord, J. Magn. Magn. Mat. 126, 622 (1993).
2. J. I. Martin, M. Vélez, J. Nogués, and I. K. Schuller, Phys. Rev. Lett. 79, 1929 (1997).
3. M. J. Van Bael, K. Temst, V. V. Moshchalkov, and Y. Bruynseraede, Phys. Rev. B 59, 14674 (1999).
4. D. J. Morgan and J. B. Ketterson, Phys. Rev. Lett. 80, 3614 (1998).
5. M. J. Van Bael, L. Van Look, K. Temst, M. Lange, J. Bekaert, U. May, G. Güntherodt, V. Moshchalkov, and Y. Bruynseraede, Physica C 332, 12 (2000).
6. L. N. Bulaevskii, E. M. Chudnovsky, and M. P. Maley, Appl. Phys. Lett. 76, 2594 (2000).
7. A. García-Santiago, F. Sánchez, M. Varela, and J. Tejada, Appl. Phys. Lett. 77, 2900 (2000).
8. X. X. Zhang, G. H. Wen, R. K. Zheng, G. C. Xiong, and G. J. Lian, Europhys. Lett. 56, 119 (2001).
9. Y. I. Bespqtykh, W. Wasilevski, M. Gajdek, I. P. Nikitin, and S. A. Nikitov, Phys. Solid State 43, 1827 (2001).
10. M. Lange, M. J. Van Bael, V. V. Moshchalkov, and Y. Bruynseraede, Appl. Phys. Lett. 81, 322 (2002).
11. I. K. Marmorkos, A. Matulis, and F. M. Peeters, Phys. Rev. B 53, 2677 (1996).
12. M. V. Milosevic, S. V. Yampolskii, and F. M. Peeters, Phys. Rev. B 66, 024515 (2002).
13. I. F. Lyuksyutov and V. L. Pokrovsky, Phys. Rev. Lett. 81, 2344 (1998).
14. S. Erdin, I. F. Lyuksyutov, V. L. Pokrovsky, and V. M. Vinokur, Phys. Rev. Lett. 88, 017001 (2002).
15. Y. I. Bespqtykh and W. Wasilevski, Phys. Solid State 43, 224 (2001).
16. E. B. Sonin, Pis’ma Zh. Tekh. Phys. 14, 1640 (1988) [Sov. Tech. Phys. Lett. 14, 714 (1988)]; R. Laiho, E. Lähteeranta, E. B. Sonin, and K. B. Traito, Phys. Rev. B 67, 144522 (2003).
17. A. I. Buzdin and L. N. Bulaevskii, Sov. Phys. JETP 67, 576 (1988).
18. Ž. Radovic, M. Ledvij, L. Dobrosavljević-Grujić, A. I. Buzdin, and J. R. Clem, Phys. Rev. B 44, 759 (1991).
19. V. V. Ryazanov, V. A. Oboznov, A. Y. Rusanov, A. V. Veretennikov, A. A. Golubov, and J. Aarts, Phys. Rev. Lett. 86, 2427 (2001).
20. J. S. Jiang, D. Davidovic, D. H. Reich, and C. L. Chien, Phys. Rev. Lett. 74, 314 (1995).
21. T. Mühge, N. N. Garif’yanov, Y. V. Goryunov, G. G. Khalilullin, L. R. Tagirov, K. Westerholt, I. A. Garifullin, and H. Zabel, Phys. Rev. Lett. 77, 1857 (1996).
22. J. Aarts, J. M. E. Geers, E. Bruck, A. A. Golubov, and R. Coehoorn, Phys. Rev. B 56, 2779 (1997).
23. L. Lazar, K. Westerholt, H. Zabel, L. R. Tagirov, Y. V. Goryunov, N. N. Garif’yanov, and I. A. Garifullin, Phys. Rev. B 61, 3711 (2000).
24. K. Usadel, Phys. Rev. Lett. 25, 507 (1970).
25. M. Tinkham, Introduction to superconductivity (McGraw-Hill, Inc., New York, ed. 2, 1996).
26. M. Tinkham, Phys. Rev. 129, 2413 (1963).
27. V. V. Moshchalkov, L. Gielen, C. Strunk, R. Jonckheere, X. Qiu, C. Van Haesendonck, and Y. Bruynseraede, Nature 373, 319 (1995).
28. V. Bruyndoncx, C. Strunk, V. V. Moshchalkov, C. Van Haesendonck, and Y. Bruynseraede, Europhys. Lett. 36, 449 (1996).
29. L. Van Look, PhD thesis, K.U.Leuven, Belgium (2002).
30. A. Y. Aladyshkin, A. I. Buzdin, A. A. Fraerman, A. S. Mel’nikov, D. A. Ryzhov, and A. V. Sokolov, Domain wall superconductivity in hybrid superconductor-ferromagnetic structures (2003), (unpublished), cond-mat/0305520.
31. M. V. Fomin, J. T. Devreese, and V. V. Moshchalkov, Europhys. Lett. 42, 553 (1998); 46, 118 (1999).
32. V. A. Schweigert and F. M. Peeters, Phys. Rev. B 60, 3084 (1999).