WAVELENGTH-RESOLVED NEUTRON TOMOGRAPHY FOR CRYSTALLINE MATERIALS

S. V. Venkatakrishnan*  Luc Dessieux †  Philip Bingham*

* Imaging, Signals and Machine Learning Group, Oak Ridge National Lab, Oak Ridge, TN 37831
† Department of Physics, University of Tennessee, Knoxville, TN 37931

ABSTRACT

Wavelength-resolved (WR) neutron transmission tomography is an emerging technique to characterize engineering materials. While tomographic reconstruction for amorphous samples is straightforward, it is challenging to reconstruct samples with single-crystal domains because the attenuation of the sample varies as a function of its orientation with respect to the incident beam due to Bragg scattering. In this paper, we present an algorithm that can reconstruct samples with single-crystal domains from WR neutron tomographic measurements. In particular, we use a model-based iterative reconstruction (MBIR) technique that reconstructs the volume by identifying and leaving out the regions of the measurement that are affected by Bragg scatter. We combine the output of the MBIR method with an algorithm that matches the reconstruction to the identified Bragg scatter to reconstruct a feature that corresponds to the local crystallography of the sample being measured. Using simulated data, we demonstrate how our algorithm can reconstruct materials with single-crystal domains, thereby adding a powerful new capability for WR neutron imaging instruments.

1. INTRODUCTION

Neutron imaging is a powerful tool for characterizing engineering materials because they can penetrate thick specimens and provide a complimentary contrast to X-rays [1,2]. Driven by the recent advent of spallation (pulsed) neutron sources and the availability of time-of-flight imaging detectors [3], there has been an emergence of wavelength-resolved (WR)/time-of-flight (ToF) neutron imaging instruments [4,7]. While WR imaging instruments have been used for tomographic characterization of amorphous samples (for example [8]), using them to image samples with single-crystal domains is not common because of Bragg-scatter (that manifests as sharp drops in transmitted intensity) which makes it difficult to invert the measurements.

Engineering materials containing single-crystal domains can be characterized using neutron diffraction [9]. However, neutron diffraction involves point-wise raster scanning of a beam across the sample making it extremely time-consuming for large samples. This has led to the development of neutron diffraction contrast tomography [10] using a pair of detectors, one in a transmission geometry and the other in reflection mode, to reconstruct the shape and crystallographic orientation of individual domains (grains) in a sample. Recently, Cereser et al. [11] used a WR neutron imaging detector in transmission geometry to tomographically reconstruct the morphology of large domains (grains) by using an algorithm to detect Bragg scatter events in the measurements and back-projecting them to obtain an approximate shape. From a tomographic reconstruction perspective, the central challenge in WR neutron transmission tomography for samples with single-crystal domains is that the regions diffract the incident beam resulting in measurements that cannot be accurately inverted using analytic algorithms such as the filtered-back projection (FBP).

In this paper, we propose an algorithm for reconstructing samples with single-crystal domains using WR neutron tomography measurements. In particular, we use the robust model-based iterative reconstruction (R-MBIR) of [12] that casts the reconstruction as minimizing a regularized cost function. In addition to the 3D hyper-spectral volume of the attenuation coefficients, this algorithm also generates a map of regions in the original measurements that were identified as anomalous which we refer to as “Bragg-maps”. We then develop an algorithm to segment the reconstructed volume and the Bragg-maps and associate each component of the Bragg-map with a segmented domain in the reconstruction. In summary, our method makes use of all the measurement data and can quantitatively reconstruct the sample including the morphology of the single-crystal domains and a crystallographic signature for each of those domains, thereby adding a vital new capability to WR neutron imaging instruments.
2. OVERALL APPROACH FOR WAVELENGTH-RESOLVED TOMOGRAPHY OF CRYSTALLINE SAMPLES

Fig. 1. Linear attenuation coefficient of a sample of (a) powder and (b) single-crystal as a function of rotation angle and wavelength (displayed in range [5.5, 15] × 10^{-5} \mu m^{-1}). For the powder, the attenuation does not change as a function of rotation angle, while for the crystal it changes significantly.

In parallel-beam WR neutron tomography, a sample is typically rotated about a single axis and at each angle a WR/hyper-spectral projection image is measured. The measurements corresponding to each wavelength are then used to reconstruct a 3D volume using a tomographic reconstruction algorithm like FBP [8] and then combined to obtain a spectral tomographic reconstruction. Extending this approach to characterize samples with single-crystal domains has been avoided because these regions diffract the beam when they satisfy the Bragg condition,

$$n\lambda = 2d\sin(\theta)$$

where \(n\) is some integer, \(\lambda\) is the wavelength of incident neutrons, \(d\) is the crystallographic spacing and \(\theta\) is the angle between incident beam and the normal to the crystallographic plane. Specifically, the linear attenuation coefficient of the single-crystal region changes with respect to its orientation to the incident beam for a specific wavelength. Fig. 1 shows the simulated attenuation coefficient of a 1 mm × 1 mm voxel as a function of wavelength and rotation angle about a single axis generated using SinPol [13], a WR neutron transmission simulator. When the sample is amorphous (also called a powder), the linear attenuation coefficient does not vary as a function of rotation angle as is typical in standard tomography problems. However, if the sample is a single-crystal, the attenuation of the voxel can change as a function of the rotation angle because at certain orientations it satisfies the Bragg condition leading to a sharp increase in attenuation (Fig. 1(b)).

Our goal is to design an algorithm to reconstruct samples with single-crystal domains in-order to be able to infer the attenuation coefficient, morphology and some local crystallographic information from WR tomography measurements.

3. ROBUST HYPER-SPECTRAL MODEL-BASED TOMOGRAPHY

In this section, we present a method for wavelength resolved tomography when the measurements include Bragg scatter (observed as sharp drops in the transmitted intensity). Our approach will simultaneously identify the Bragg-scatter measurements and reconstruct the hyper-spectral attenuation coefficients in 3D. We use the robust model-based iterative reconstruction (R-MBIR) method of [12] which has a Huber-like penalty to account for outliers (like Bragg scatter) and extend it to the hyper-spectral case. For each wavelength channel \(k\), the reconstruction is obtained as

$$\left(\hat{f}_{k}, \hat{B}_{k}\right) \leftarrow \text{R-MBIR}(g_{k}; T_{k}, \sigma_{f,k})$$

where \(g_{k}\) is a vector of normalized transmission measurements at wavelength index \(k\), \(f_{k}\) is a vector of linear attenuation coefficients of all the voxels in 3D, \(B_{k}\) is a binary Bragg-map of the same dimensions as \(g_{k}\) that indicates which of the original measurements are anomalous, \(T_{k}\) and \(\sigma_{f,k}\) are parameters of the reconstruction algorithm. This method has the...
Fig. 3. Block diagram of the overall algorithm. The input are the WR/hyper-spectral images taken at different rotation angles. The output is the 3D reconstruction of attenuation coefficients, morphology and a binary signature which indicates the local orientation of the crystals in different domains of the 3D reconstruction.

In particular, the reconstruction for a given wavelength using the R-MBIR approach is obtained as

\[
\hat{f} \leftarrow \arg\min_f c(f)
\]

where

\[
c(f) = \frac{1}{2} \sum_{i=1}^{M} \beta_T \left( (g_i - [Af]_i) \sqrt{W_{ii}} \right) + R(f; \sigma_f)
\]

is a generalization of the Huber function \[15, 16\] and \( T \) is the outlier threshold. Using a majorization-minimization approach with quadratic surrogates along with an optimized gradient method \[17\], we obtain the 3D reconstruction and a map of measurements that have been identified as being anomalous (whose normalized fitting error is greater than \( T \)).

4. RECONSTRUCTION OF CRYSTAL SIGNATURES

Given the wavelength-resolved 3D reconstruction, \( \left( \hat{f}_1, ..., \hat{f}_K \right) \), and the Bragg-maps, \( \left( \hat{B}_1, ..., \hat{B}_K \right) \), we use a correlation based approach to associate each of the connected components in the Bragg-maps to the connected-components in the 3D volume. This approach will output a binary feature map for each domain (connected component) in the tomographic reconstruction that indicates if it met the Bragg condition at a specific view angle and wavelength, thereby providing information about the local crystallography of the sample. In essence, this feature vector is a binary thresholded version of the attenuation profile in Fig. 2(b) for each domain in the 3D volume.

In order to find the connected components in the reconstructed volume, we first apply the K-means segmentation algorithm to the hyper-spectral reconstructed volume. A standard connected components analysis is then applied to the segmented volume to obtain a collection of \( P \) domains. Next, we apply a connected components analysis to the binary Bragg-map images. The result of this processing is a set of \( Q \) connected components each associated with a specific view angle \( \phi \) and a wavelength \( \lambda \). Finally, for each of the \( P \) domains, we forward project it at the different view angles, binarize the projection and compute a correlation score \[12\] with each of the relevant connected components \( Q \). If \( p \) is a binarized version of the projection image of a given particle and \( q \) is the binary anomaly classifier image with the relevant connected component, we define the correlation score as

\[
S = 1 - \frac{\|p^T \bar{q} \|_1 + \|p^T q \|_1}{\|p\|_1 + \|q\|_1}
\]

where \( \bar{q} \) and \( \bar{p} \) refers to the binary complement operator and \( \| \cdot \|_1 \) is the \( l_1 \) norm. If the correlation score crosses a threshold, we declare a Bragg event. Thus upon completion of this process for each of the \( Q \) anomalies, we have identified which one of the \( P \) domains best matched it. In conclusion, for each of the \( P \) domains we have a view-angle and wavelength at which it was potentially in the Bragg-condition.

5. RESULTS

We generate a cylindrical phantom made of a powder (attenuation of Fig. 1(a)) with embedded single-crystal grains of copper (attenuation coefficient in Fig. 1(b)) using the DREAM.3D \[18\] software. All the grains have the same crystallographic orientation with respect to the incident beam. We simulate hyper-spectral images of size \( 128 \times 128 \) at 140 wavelengths between \( 2.25 \) A° and \( 4 \) A° for 180 views between \( 0° \) to \( 180° \) using a Beer’s law model applied to the phantom
with an incident flux of $I_0 = 500$. Fig. 4 shows the simulated data at two views for a fixed wavelength. Notice that some of the regions in Fig. 4(a) are not distinguishable from the background powder in Fig. 4(b) because the grains in the sample met the Bragg condition causing a sharp drop in the transmitted intensity. We reconstruct the sample using cubic voxels with a size of $50\mu$ using the filtered back-projection (FBP) algorithm and the proposed R-MBIR method. For R-MBIR, the value of $T$ is adjusted for each wavelength, while $\sigma_f$ is set to 1 for the q-GGMRF regularizer of \cite{17} resulting in a high quality reconstruction with minimal artifacts. The threshold for the correlation score is set to 0.5. Fig. 5 shows the output of the tomographic reconstruction. Notice that we get a high fidelity reconstruction from R-MBIR in-spite of the grains strongly diffracting the beam away from the transmission path at certain orientations, compared to FBP which has strong streaking artifacts. Furthermore the R-MBIR method reconstructs a Bragg-map (for example - Fig. 5(c) corresponding to the data in Fig. 4(b)) identifying all the anomalous measurements due to Bragg-scatter, which conventional methods like FBP do not produce. Finally, Fig. 6 shows a 3D rendering of the segmented R-MBIR reconstruction along with the reconstructed crystallographic signature of the four largest grains. While this matches the ground truth (Fig. 1(b)) for the large grains (true-positive rates for the 4 grains in anti-clockwise direction $0.94, 0.70, 0.63, 0.14$), there are missed detections especially for the smaller grains due to the chosen threshold value for the correlation score and challenges in segmenting the Bragg-maps in the case of occlusions. However, we note that a fitting routine is used to determine the crystallographic orientation from such signatures \cite{11}, hence a few missed detections will typically not affect the final solution as long as we can determine the parameters from the reconstructed patterns.

6. CONCLUSION

We presented an algorithm that can quantitatively reconstruct samples with single-crystal domains along with some local crystallographic orientation information only using WR neutron transmission tomography measurements, thereby enabling a new measurement capability. In the future, we plan to extend our algorithm to cover a broader range of samples such as those that are purely crystalline, and those with the presence of texture where the Bragg scatter is not as strong.
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