DC Current Driven Critical Current Variation in \(\text{Sr}_2\text{RuO}_4\)-Ru Junction Proved by Local Transport Measurements

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To search for new evidence of the chiral \(p\)-wave superconducting domain in \(\text{Sr}_2\text{RuO}_4\), we investigated the unconventional local transport characteristics of a microfabricated \(\text{Sr}_2\text{RuO}_4\)-Ru eutectic junction. We found that the anomalous hysteresis in voltage-current characteristics [as reported in H. Kambara \textit{et al.}: Phys. Rev. Lett. 101 (2008) 267003.] is strongly affected by dc currents, but not by magnetic fields. This suggests that dc current acts as a driving force to move chiral \(p\)-wave domain walls; a domain wall trapped at a pinning potential is forced to shift to the next stable position, thereby forming a larger critical current path and resulting in the anomalous hysteresis.

KEYWORDS: \(\text{Sr}_2\text{RuO}_4\), \(p\)-wave superconducting junction, eutectic, critical current, chiral domain, hysteresis

1. Introduction

Layered perovskite \(\text{Sr}_2\text{RuO}_4\) (SRO)\(^1\) is now widely believed to be one of rare examples of odd-parity spin-triplet pairing superconductors.\(^2,3\) Its superconducting order parameter is represented as the so-called chiral \(p\)-wave state with broken time-reversal symmetry, which is similar to the superfluid \(\Lambda\)-phase of \(^3\)He.\(^4\) The pure SRO phase has a sharp superconducting transition temperature \((T_c)\) of 1.5 K (1.5-K phase), while the SRO-Ru eutectic system shows a remarkable enhancement of \(T_c\) onset up to 3 K with its resistivity gradually decreasing to zero at 1.5 K. The superconductivity observed at 3 K is called the 3-K phase.\(^5-7\) The 3-K phase is regarded as the interface superconductivity in the SRO region between SRO and Ru inclusions because its superconducting volume fraction has been found to be considerably smaller than that of the pure 1.5-K phase from specific heat measurement.\(^7\) Tunnel junction experiments using Ru interfaces\(^8,9\) showed a zero-bias conductance peak due to Andreev resonance,\(^10\) suggesting that the 3-K phase shows non-\(s\)-wave superconductivity. Recently, we have performed local transport measurements on microfabricated samples of the SRO-Ru eutectic system and observed the development of the superconducting linkage channels connecting Ru inclusions with decreasing temperature below 3 K.\(^11\) From the measurement of the critical current \((I_c)\) in the linkage channels, we found that the 3-K phase also has odd-parity pairing symmetry, similar to the 1.5-K phase.\(^11\) This shows that the SRO-Ru eutectic system includes naturally formed \(p\)-wave superconducting junctions in itself depending on temperature; the 3-K phase region—normal-state region—3-K phase region as the superconductor(S)—normal-metal(N)—S junction at 3 K > \(T\) > 1.5 K, while the 3-K phase region—1.5-K phase region—3-K phase region as the S–S′–S junction at \(T < 1.5\) K (Fig. 1).

We observed quite anomalous hysteresis in the voltage–current \((V – I)\) and differential-resistance–current \((dV/dI – I)\) characteristics of these junctions below 2 K.\(^11\) “Anomalous” hysteresis implies that it is different from the usual hysteresis observed in usual Josephson junctions (JJs). That is, (i) voltage discontuously decreases when the \(V – I\) curve switches to the next branch with increasing current, and therefore, (ii) the hysteresis loop shows the opposite direction compared to usual JJs.\(^12\) Thus, these features indicate the emergence of the internal degrees of freedom of the superconducting state. One possible explanation of the anomalous hysteresis is due to the existence of chiral \(p\)-wave domains reflecting the chiral \(p\)-wave pairing of SRO. The existence of chiral domains in SRO has been suggested by several experiments; the domain size has been estimated to be approximately 50–100 \(\mu\)m from Kerr effect measurement\(^13\) and approximately 1 \(\mu\)m from a SRO-Cu-Pb...
junction experiment.\textsuperscript{14)}

To investigate such anomalous transport properties in detail and examine chiral domains, we measured the local transport characteristics of microfabricated SRO-Ru eutectic samples, both in-plane and out-of-plane directions. The advantage of milling a sample down to the micrometer scale by a focused ion beam (FIB) is that one can extract each conducting channel from a complex network\textsuperscript{15)} and detect anomalous features without averaging over the bulk sample. In this paper, we report that the anomalous hysteresis is strongly affected by dc currents, but not affected by magnetic fields. This suggests a dc-current-driven $I_c$ variation, which is explained by the discontinuous motion of the chiral domain wall trapped at a pinning potential, which is discussed below.

2. Experiment

Eutectic crystals of SRO-Ru were grown in an infrared image furnace by the floating zone method.\textsuperscript{16)} The sample preparation is as follows. First, a thin platelet of a crystal was prepared by cleaving a crystal along the $ab$-plane and mechanically polishing it down to a thickness of a few tens of micrometers along the $c$-axis. Second, the platelet was roughly cut into a small piece of submillimeter width in the $ab$-plane. Third, the small piece was glued on a SrTiO$_3$ substrate using epoxy adhesive. Last, four contacts for transport measurement were formed on the piece using an evaporated gold film. Then, the sample was milled by an FIB to form a “microbridge” between the voltage lead contacts (Fig. 2(a)). Since electric fields concentrate in the microbridge (typical size is shown in Fig. 2(b)), the measured electric resistance is predominated by the electric resistance of the microbridge. Thus, we can study local transport properties by focusing on the microbridge from a complex network of linkage channels spread over the entire sample. To measure transport characteristics along $I//c$, we formed a crank-shaped path by milling two alternate slits along the $c$-axis by an FIB (Figs. 2(c) and 2(e)) in a manner similar to the fabrication of intrinsic JJs of high-$T_c$ cuprates.\textsuperscript{17, 18)} We confirmed the existence of Ru inclusions in the microbridge region by FIB milling after the transport measurements were done (Fig. 2(f)). Figure 2(f) shows that a piece of Ru inclusion was embedded slightly below the top surface at the center of the microbridge. We observed about six pieces of Ru inclusions including small ones between the $c$-axis slits. The transport measurements were performed by dc and ac methods. In the ac method, ac modulation with an amplitude of 30 $\mu$A$_{rms}$ and a frequency of 977 Hz was used. The sample was cooled below 1 K using a He cryostat. External magnetic fields were applied parallel to the $c$-axis for evaluating the magnetic field effects.

3. Results

3.1 $R$ – $T$ curves of FIB-milled samples

Figures 2(b) and 2(c) show schematic sample configurations for $I//ab$ (sample 1) and $I//c$ (sample 2), respectively (note: sample 1 is the same as sample D used in ref. 11). In sample 2, we note that the resistance of the $I//c$-part is high and that of the $I//ab$-part is low ($\sim$18%) at 4.2 K. In this study, we regard the configuration of sample 2 as $I//c$. Figure 2(d) shows the differential resistance at zero-bias current ($R$) versus temperature ($T$) curves of samples 1 and 2. If we assume that the overlap path length (0.7 $\mu$m) along the $c$-axis only contributes to the $c$-axis resistivity, the ratio of out-of-plane resistivity ($\rho_c$) to in-plane resistivity ($\rho_{ab}$) of this material is estimated to be $\rho_c/\rho_{ab} \simeq 40$ at 4.2 K. This is comparable to previously reported data.\textsuperscript{6)}

3.2 Anomalous $V$ – $I$ and $dV/dI$ – $I$ characteristics

Figures 3(a) and 3(b) show typical $V$ – $I$ and $dV/dI$ – $I$ characteristics of samples 1 (Figs. 4(a) and 4(b) in ref. 11) and 2 obtained by the dc and ac methods, respectively. The most peculiar feature of these systems is that the absolute values of voltage abruptly decrease at the thresholds $I_{th1} = \pm 3$ mA and $I_{th2} = \pm 4.3$ mA for sample 1, and at $I_{th1} = \pm 3.1$ mA and $I_{th2} = \pm 4.7$ mA for sample 2 with increasing absolute values of dc currents, which are shown by bold arrows in the $V$ – $I$ characteristics of Figs. 3(a) and 3(b). For the ac method, since the $dV/dI$ – $I$ peaks or steps correspond to the $I_c$s of the superconducting linkage channels,\textsuperscript{11)} we can see that $I_c$ becomes larger with decreasing current rather than increasing current. Furthermore, no negative $dV/dI$ – $I$ value means that the unusual voltage decrease is a switching phenomenon in...
which no intermediate states exist. Thus, we found that the anomalous hysteresis is a common feature observed not only in the in-plane direction but also in the out-of-plane direction. The peaks in $dV/dI - I$ of $I//c$ (sample 2) are considerably sharper than those of $I//ab$ (sample 1) reflecting a quasi-two-dimensional conductor; a junction behaves like a tunnel along the $c$-axis; on the other hand, it behaves as a weak link in the $ab$-plane. We note that the reproducibility of the hysteresis after thermal cycling (warming up to 300 K and cooling again) was amazingly high up to around 10 cycles for both samples 1 and 2. Furthermore, we note that the anomalous hystereses were observed for most of the samples of SRO-Ru. Thus, the anomalous hysteretic feature is not an incidental phenomenon, but an intrinsic property.

3.3 Dc current sweep width dependence of hysteresis

Next, we show that the shape of the hysteresis strongly depends on the dc current sweep width. Figures 4(b) and 4(d) show $dV/dI - I$ characteristics for different sweep widths of samples 1 (A–D) and 2 (E–J), respectively. For sample 1, no hysteresis was observed in (A and B). On the other hand in (C), a narrow hysteresis, compared with that in (D), was observed. For sample 2, no hysteresis was observed in (E) and a negative-current region in (F). On the other hand in (G), a narrow hysteresis, compared with those in (H and J), was observed. Note that a small difference between the hystereses of (G) and (H and J) appears when current is decreased. Also note that the shapes of the hystereses of (H and J) are almost the same except for the $dV/dI - I$ peak heights. The experimental results show that hysteresis width increases in a steplike manner when currents larger than $I_{th}$s (shown by bold arrows in Figs. 4(a) and 4(c)) are applied. We note that the difference in the presence of hysteresis in (F), i.e., hysteresis in the positive-current region, whereas no hysteresis in the negative-current region, is due to a small fluctuation in $I_{th}$. For the same reason, the curve (H) shows a large hysteresis, which is similar to (J) rather than to (G), though the current sweep width of (H) is slightly small compared with $I_{th}$ in the $V - I$ curve.

3.4 Magnetic field effect on hysteresis

Next, we switched off the fields and measured $dV/dI - I$ at zero field. On the other hand, for ZFC, we cooled the samples under a magnetic field larger than the lower critical field $H_{c1} (\approx 70$ G$^{19}$) parallel to the $c$-axis at 4.2 K (130 G for sample 1 and 1000 G for sample 2), and cooled the samples below 1 K under the magnetic fields. Next, we switched off the fields and measured $dV/dI - I$ at zero field. On the other hand, for ZFC, we cooled the samples under zero field and measured $dV/dI - I$ at zero field. Figures 5(a) and 5(b) (5(c) and 5(d)) show the $dV/dI - I$ curves of FC and ZFC for sample 1 (2), respectively. There was no significant difference between the $dV/dI - I$ curves of FC and ZFC, for both the samples. Figure 5(a) also shows the data obtained under magnetic fields applied after FC. In any case, when the applied magnetic fields are higher than $H_{c1}$, magnetic vortices can penetrate the
samples. If trapped vortices make $I_c$ variation, a difference in the shape of the hysteresis between the $dV/dI - I$ curves of FC and ZFC should be expected. However, no difference is observed between the $dV/dI - I$ curves obtained at zero field before and after the application of the magnetic fields. These results imply that the anomalous hysteresis is not caused by the magnetic vortex effect. In contrast to the dc current effect, magnetic field showed no significant effect on the anomalous hysteresis.

4. Discussion

The experimental results are summarized as follows. (i) Anomalous hystereses appear for both current directions ($I//ab$ and $I//c$). (ii) The width of the hysteresis curves changes discontinuously depending on current sweep width. (iii) Magnetic fields do not affect the hysteresis.

Next, we analyze these experimental results by using the chiral domain model proposed in our previous study. Using this model, we assume that the angular momentum transfer from a given chiral state $(p_x - ip_y)$ to the opposite chiral state $(p_x + ip_y)$ by dc current induces domain wall (DW) motion. Thus, dc current causes an unusual $I_c$ variation as a function of position because $I_c$ is expected to be proportional to the cross-sectional area of spatially inhomogeneous linkage channels. If a DW exists, it is preferentially trapped at a defect at the beginning because a small overlapping area is energetically favorable for different order parameters of antiparallel domains. Thus, $I_c$ would increase with increasing dc currents and cause the anomalous hysteresis. We also note that there is no DW between parallel domains. Thus, the anomalous hysteresis would appear only between antiparallel domains.

Regarding feature (ii), if we assume that $I_{th}$ originates from a pinning potential due to, for example, a type of lattice defect, the well-reproducible $I_{th}$ after thermal cycle is explainable. Assuming that applying dc currents reduces effective pinning potential, the trapped DW can escape when sufficiently large dc currents, which can overcome the pinning potential, are applied. This is analogous to the depinning phenomenon of charge density waves with electric fields exceeding a certain threshold value. Using the simplest model in this case, we consider a tilted washboard potential as the pinning potential, although the pinning sites are not aligned periodically in an actual case. Then, the effective potential $U_{eff}$ is given as a function of the position $x$ as $U_{eff} \approx -U \cos kx - \alpha Ix$, where $U$ is the amplitude of the potential corrugation and $k$ and $\alpha$ are numerical constants.

We should consider the variation in the superconducting condensation energy due to the variation in the cross-sectional area of the channel at the pinning sites. For antiparallel domains, since a small cross-sectional area is energetically favored, an increase in the cross-sectional area means a loss of the condensation energy. Therefore, the energy increase is proportional to the volume $\pi(r^2 - r_0^2)\xi^2$, assuming a simple “horn”-shaped channel (inset of Fig. 6(b)), where $r_0$ is the radius of the channel at the origin ($x = 0$), which has a minimum cross section, $r$ is the radius of the channel away from the origin, and $\xi$ is the coherence length of SRO. Assuming that $r$ is proportional to $x$ away from $x = 0$ in the simplest case, i.e., $r = \beta x$ ($\beta$ is a numerical constant), $U_{eff}$ is rewritten as a function of $x$ (without a constant term) as $U_{eff} \approx -U \cos kx - \alpha Ix + (\mu_0H_c(0)^2/2)\pi\beta^2x^2\xi$, where $\mu_0H_c(0)^2/2$ is the condensation energy per unit volume. We have roughly estimated the order of magnitude of the 3rd term, i.e., the condensation energy loss, to be $\sim 0.1$–1 eV, where $\mu_0H_c(0) = 0.023$ T; $\xi = 66$ nm (in-plane), 3.3 nm (out-of-plane) at $T = 0$ K for the 1.5-K phase; $x \approx 1$ μm; and $\beta \approx 1/20$ from a rough estimation of the ratio of the cross sections. On the other hand, we estimated $U$ to be $\sim 0.1$ eV for an order of magnitude assuming that $U$ is comparable to the typical pinning potential of a magnetic vortex. Thus, these two terms are comparable.

Figure 6(b) shows examples of $U_{eff}$ variation under dc currents for certain values of parameters. If we assume viscous movement for the DW, it will be trapped at the local potential minima. Therefore, the DW moves to the next local potential minimum at $I_{th1}$ and $I_{th2}$ with increasing dc currents from zero (process: 0→1→2). On the other hand, reducing dc currents from $I_{th2}$ to $I_{th1}$ (process: 2→3) does not change the position of the DW. As a result, a larger $I_c$ is observed during decreasing dc current process. An important feature is that the DW moves back to the origin around $I \approx 0$ due to the quadratic potential. Thus, the hysteresis loop starts again from a lower $I_c$ even in the region of negative currents, which is similar to the case of positive currents, and repeats the...
Generally in a chiral domain, edge currents are expected to flow along DWs. Thus, it is naturally expected that magnetic fields would interact with the magnetic moment of the edge currents. Feature (iii), however, seems to contradict this speculation. One possible reason for this inconsistency is that the actual chiral domain is not a simple model of effective pinning potential of domain wall as a function of position of channel under dc currents flowing conditions. The open and solid (red) circles denote the trapped positions at the local minima with increasing and decreasing currents, respectively. The dashed quadratic curve shows the condensation energy loss. Inset: model of chiral domain trapped in horn-shaped channel. \( I_{\text{tr}} \) increases \( \left( I_{\text{tr}}^+, I_{\text{tr}}^- \right) \) with the cross-sectional area of the channel. The hatched light blue parts of the cross section of the domain wall correspond to the volumes of the condensation energy loss.

From feature (i) it is found that, in the chiral domain scenario, the DW can move not only in the in-plane direction but also in the out-of-plane direction, although the chiral domain is usually discussed only in the context of the in-plane direction theoretically. Further experimental work is necessary to validate the existence of chiral domains or to determine whether other models can be applied to the SRO-Ru system.

5. Conclusion

In summary, we have observed anomalous transport characteristics in microfabricated samples of the Sr$_2$RuO$_4$-Ru eutectic system, both in-plane and out-of-plane directions. The anomalous hysteresis in differential-resistance and voltage–current characteristics are explained by the presence of chiral domains. The domain wall, which is trapped at lattice defects, is driven by large currents beyond the pinning potential. The absence of the magnetic field effect on the hysteresis implies the coexistence of the \( p_x \pm ip_y \) and \( p_x(p_y) \) states in a microbridge sample with a size of the order of a few micrometers. All the observed features suggest the emergence of the internal degrees of freedom of the chiral \( p \)-wave state.

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