deep21: a Deep Learning Method for 21cm Foreground Removal

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Abstract. We seek to remove foreground contaminants from 21cm intensity mapping observations. We demonstrate that a deep convolutional neural network (CNN) with a UNet architecture and three-dimensional convolutions, trained on simulated observations, can effectively separate frequency and spatial patterns of the cosmic neutral hydrogen (HI) signal from foregrounds in the presence of noise. Cleaned maps recover cosmological clustering amplitude and phase within 20% at all relevant angular scales and frequencies. This amounts to a reduction in prediction variance of over an order of magnitude across angular scales, and improved accuracy for intermediate radial scales (0.025 < k || < 0.075 h Mpc−1) compared to standard Principal Component Analysis (PCA) methods. We estimate epistemic confidence intervals for the network’s prediction by training an ensemble of UNets. Our approach demonstrates the feasibility of analyzing 21cm intensity maps, as opposed to derived summary statistics, for upcoming radio experiments, as long as the simulated foreground model is sufficiently realistic. We provide the code used for this analysis on GitHub, as well as a browser-based tutorial for the experiment and UNet model via the accompanying Colab notebook.

Keywords: cosmology: radio – reionisation, large-scale structure – foregrounds – deep learning, signal processing

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1 Introduction

Observations of cosmic neutral hydrogen emission hold the promise of making precision measurements of the universe’s evolution at intermediate to late redshifts (0.5 > z > 30) [38, 43, 68, 74], providing an observable to trace both the growth of massive structure from the time of the Cosmic Microwave Background (CMB), as well as constrain the physics of Reionization (10 > z > 6) [23, 53, 58].

Measurement of the 21cm line relies on intensity mapping, in which large fractions of the sky are observed to capture wide-field statistics, instead of resolving individual sources [for an overview see e.g. 38, 53]. This technique has already been used to place constraints on the formation of the first stars and galaxies at z ∼ 9 [50], but the precise nature of the Epoch of
Reionization (EoR) remains unknown [23]. 21cm intensity maps also promise to be a tracer of three-dimensional, large-scale structure growth at later redshifts $z \lesssim 4$, linking late-stage structure to underlying gravitational theory and the primordial density [10, 29]. Upcoming experiments, such as the Square Kilometer Array (SKA) promise to trace EoR physics to large-scale structure formation using this single observable [5].

The greatest challenge for these measurements is mitigating systematics and removing enormous foreground contamination from galactic radio sources such as synchrotron and free-free emission, as well as extragalactic features like point sources [53, 58]. These contaminants tend to be three to four orders of magnitude brighter than the interesting cosmological signal [30, 53]. Furthermore, foregrounds lack detailed analytic descriptions, making 21cm likelihoods hard to specify [3].

The foreground signals have different statistical properties than the cosmological signal, a phenomenon thoroughly covered in the literature [7, 8, 25, 32, 48, 52, 54, 56, 61, 81], with several proposed methods for signal separation [39, 41, 47, 65, 66, 85]. Most foreground contaminants are forecast to be spectrally smooth in frequency, motivating the application of blind signal separation techniques, such as Principal Component Analysis (PCA) [e.g. 2, 19], which require no prior knowledge of the expected signals. However, blind separation techniques are not linked to physical processes and therefore make no use of our physical understanding of these foregrounds. This means that there exists information in the observed signal that is not fully exploited for separation. Blind subtraction for single-dish experiments irretrievably removes the mean of the HI intensity spectrum and can also distort the signal anisotropy [15, 17, 70], placing the focus of analyses on interpreting compressed, sometimes biased [see e.g. 2, 69, 85], summary statistics derived from these maps, such as power spectra. With clean 21cm intensity maps, more fundamental large-scale structure analyses and parameter extraction would be possible using the maps themselves [24, 45, 82, for a review].

We address these problems by constructing a convolutional neural network to recover cosmological 21cm maps from PCA-reduced inputs. Deep learning architectures are ideally suited to similar high-dimensional problems such as image segmentation, classification, and computer vision tasks (see e.g. [27] for a review, and e.g. [31], [33], [79] for applications), in which patterns and higher-order correlations must be captured over a large set of input data. To incorporate an estimate of uncertainties of the separated maps we train an ensemble of networks on a suite of simulated radio skies. We then test these architectures on simulations with altered foreground parameters to assess how well the approach generalizes beyond the fiducial choice of model.

Recent studies have incorporated deep learning techniques to analyze EoR cosmology [12, 24, 34, 37, 44, 46, 78], but have largely focused on retrieving compressed cosmological statistics or higher-order correlations from clean intensity maps. Some novel methods for astrophysical foreground removal include Zhang et al. [88], who present a Bayesian method for power spectrum recovery that effectively limits blind subtraction bias by exploiting the isotropy and homogeneity of the 21cm signal. Deep learning foreground removal techniques have also been investigated, e.g. for CMB maps [87], interferometric 21cm foregrounds [36], and far-field radio astrophysics [78].

However, our study is (to our knowledge) the first to leverage a fully 3D UNet architecture to separate clean 21cm maps from radio foregrounds directly from simulated single-dish observations. These clean maps can then be leveraged in existing 21cm analyses.

The layout of this paper is as follows: in Section 2, we present the physical formalism behind HI intensity mapping and astrophysical foregrounds. In Section 3, we present the fore-
ground subtraction techniques we employ to train our network. We detail the architecture choice and the UNet training procedure in Section 3.3. Results for both blind subtraction and our network are presented in Section 4, followed by tests on foregrounds with altered simulation parameters. We discuss the successes of our network, as well as failure modes in Section 5. The cosmology we assume in our study is the standard flat ΛCDM in agreement with the results from the Planck Collaboration et al. [57], with fiducial parameters \{Ω_m, Ω_b, h, n_s, σ_8\} = \{0.315, 0.049, 0.67, 0.96, 0.83\}.

## 2 Methods and Formalism

In this section we describe the theoretical formalism behind the three main components of the observed HI 21cm sky: the cosmological signal itself, the various galactic and extra-galactic foregrounds, and observational noise. For a deeper discussion of various aspects of these components, we refer the reader to one of the several review papers on the subject such as [23, 53, 58] and [38]. We then describe how these various components are created in the simulated skies that we use to train our machine learning framework.

### 2.1 Cosmological HI Signal

The component of the 21cm sky that we care about most is the redshifted HI signal itself. This signal is often described in terms of a brightness temperature, \(T_b\), which relates the observed intensity of the signal at a given sky position and frequency to a temperature [20, 21]. In the Rayleigh-Jeans limit \(\hbar \nu_{21} \ll k_B T_b\), this brightness temperature can be related to the underlying cosmology at a given line of sight \(\hat{n}\), and frequency, \(\nu\) as [43]

\[
T_b(\hat{n}, \nu) = \frac{3hc^3A_{21}}{16k_B\nu_{21}^2} H(z) n_{HI}(z, \hat{n}),
\]

where \(n_{HI} \propto (1 + \delta_{HI})\) is the comoving number density of HI, \(H(z)\) is the Hubble parameter as a function of redshift, \(z\), \(k_B\) is Boltzmann’s constant, \(\nu_{21}\) is the frequency associated with the HI fine-structure line, \(h\) is the reduced Planck’s constant, and \(A_{21} = 2.876 \times 10^{-15}\) Hz is the 21cm line Einstein emission coefficient. Using the standard values for the various constants along with a standard flat ΛCDM cosmology for the evolution of \(H(z)\), this expression can be written in terms of the HI overdensity, \(\delta_{HI} = \rho_{HI}/\bar{\rho}_{HI} - 1\), redshift, and cosmological parameters [23, 43] as

\[
T_b(\hat{n}, z) = 0.19055 \times \frac{\Omega_b h(1 + z)^2 x_{HI}(z)}{\sqrt{\Omega_m (1 + z)^3 + \Omega_\Lambda}} (1 + \delta_{HI}(\hat{n}, z)) \text{ mK}
\]

where \(h \equiv H_0/(100 \text{ km/s/Mpc})\) is the dimensionless Hubble constant, \(x_{HI}\) is the fraction of baryonic mass comprised of HI, and \(\Omega_b\) and \(\Omega_m\) are the baryon and total matter fractions, respectively. The observed 21cm signal can thus be related to the underlying cosmological model and relevant parameters for inference studies [1, 9, 63, 76, 77]. The 21cm signal can thus be used as a tracer of the large-scale structure of the Universe.

The CRIME simulation code, described in [3], generates a dark matter field and then utilizes a log-normal model to generate the cosmological HI intensity maps. Concisely, Gaussian density and velocity perturbations are generated on a Cartesian grid with no redshift effects. The “observer” is placed at the center of the grid, and the signal is projected onto
the observer’s light cone. The Gaussian density field then undergoes localized log-normal transformations to generate the non-uniform HI density field. The results are projected onto spherical sky maps at different frequencies corresponding to the redshift of the structure from the observer, using the HEALPix pixelization scheme [28]. The brightness temperature $T_b$ is related to the underlying HI number density $n_{\text{HI}}$, as shown in Equation 2.1. The simulations are generated in a box of size $8850 \, h^{-1} \, \text{Mpc}$ per side with $3072^3$ box cells. The interpolated sky maps were generated using a HEALPix resolution of $N_{\text{side}} = 256$, which corresponds to a per-pixel frequency-independent resolution of $\theta_{\text{pix}} \approx 14\arcmin$.

2.2 Foregrounds

21 cm foregrounds currently lack a detailed analytic description, making them difficult to separate from the cosmological HI signal. However, descriptive numerical simulations exist [e.g., 80], largely extrapolated from observed radio maps, such as the Haslam and Planck maps [30, 57]. The foregrounds that we hope to remove from the observed sky can be separated into galactic and extra-galactic components. Extragalactic foreground sources are expected to be distributed according to a clear power spectrum [16, 48, 61], while galactic foregrounds, such as synchrotron emission, are expected to be localized, particularly in the galactic plane [61, 80].

For galactic sources, the CRIME simulations extrapolate foregrounds from the 408 MHz map of Haslam et al. [30] to the relevant frequencies, as described in Santos et al. [61]. For weaker foregrounds such as point sources and free-free emission, as well as for synchrotron effects on small scales, we adopt Gaussian realizations of the generic power-spectrum based model

$$C_\ell(\nu_1, \nu_2) = A \left( \frac{\ell_{\text{ref}}}{\ell} \right)^\beta \left( \frac{\nu_{\text{ref}}}{\nu_1 \nu_2} \right)^\alpha \exp \left( -\frac{\log^2(\nu_1/\nu_2)}{2\xi^2} \right)$$ (2.3)

with values given in Table 1 (see [61] for details). While we train our network on these fiducial values, we explore model generalization to new foreground parameters in Section 4.6.

2.2.1 Polarized Foregrounds.

Foreground polarization arises when synchrotron emitting electrons traverse the Milky Way’s magnetic fields, changing their polarization angles due to Faraday rotation [see e.g., 60]. Despite some empirical observations [e.g., 18, 62, 84], this effect on radio foregrounds is poorly understood, except perhaps at very low radio frequencies, as purported by the Experiment to Detect the Global Epoch of Reionization Signature (EDGES) [51]. Several models have been

| Foreground Component       | $A$ [mK$^2$] | $\beta$ | $\alpha$ | $\xi$ |
|---------------------------|-------------|--------|---------|-------|
| Galactic Synchrotron      | 1100        | 3.3    | 2.80    | 4.0   |
| Point Sources             | 57          | 1.1    | 2.07    | 1.0   |
| Galactic free-free        | 0.088       | 3.0    | 2.15    | 35    |
| Extragalactic free-free   | 0.014       | 1.0    | 2.10    | 35    |

Table 1: Fiducial foreground $C_\ell(\nu_1, \nu_2)$ model parameters used in this study, adapted from [61] for the pivot values $\ell_{\text{ref}} = 1000$ and reference frequency $\nu_{\text{ref}} = 130$ MHz.
proposed to describe this phenomenon. The CRIME simulation package defines the Faraday depth at a distance $s$ along a line of sight (LOS), $\hat{n}$, as:

$$\psi(s, \hat{n}) = \frac{e^3}{2\pi(m_e c^2)} \int_0^s ds' n_e(s', \hat{n}) B_{\parallel}(s', \hat{n})$$

where $m_e$ is the electron mass, and $n_e(s, \hat{n}) B_{\parallel}$ are the number density of electrons and galactic magnetic field contribution for the given LOS. As shown in [3], the correlation over frequency for the polarization leakage field $\mu$ can then be written as:

$$\langle \mu_{lm}(\psi) \mu_{l'm'}^* \rangle \propto \delta_{ll'} \delta_{mm'} (\ell_{\text{ref}} \ell) e^{-\frac{1}{2} \left[ \psi - \psi' \chi_{\text{polar}} \right]^2}$$

where the correlation length, $\xi_{\text{polar}}$, and amplitude are free parameters. The rest of the numerical values are given in [3]. The polarized emission correlation length is usually phenomenologically chosen. For example, [67] use an equivalent correlation length scale $\xi_{\text{polar}}$ of $0.1 - 0.05$ rad m$^{-2}$ to fit observations, while [3] choose a typical value of $0.5$ rad m$^{-2}$ to match simulations obtained by the Hammurabi code [80]. We vary this parameter to probe failure modes in our foreground subtraction method in Section 4.6.

### 2.3 Observational Noise

The third component of the observed 21cm signal is (largely thermal) observational noise. Radio observational noise can be simply modeled as zero-centered Gaussian noise for single-dish experiments [9, 38].

We modify the white noise model with a stochastic component in order to train and test cleaning methods on a wide range of possible observational thermal noise, capturing a range of possible current and future intensity mapping configurations. For each full-sky simulation, we adopt a frequency-dependent hierarchical noise model, which has the added advantage of better training our networks (see Section 3.3):

1. $\alpha_{\text{noise}} \sim \log U(0.05, 0.5)$
2. $\sigma_{\text{noise}} = \alpha_{\text{noise}} \langle T_b(\nu) \rangle$
3. $\epsilon_{b,i} \sim N(0, \sigma_{\text{noise}})$
4. $\hat{T}_{b,i} = T_{b,i} + \epsilon_{b,i}$

where we relate the variance of the noise to the average fiducial cosmological temperature at a given frequency, $\langle T_b(\nu) \rangle$. The observed signal at pixel $i$, written as $\hat{T}_{b,i}$ is then given by the true signal, $T_{b,i}$, with the addition of the Gaussian noise $\epsilon_{b,i}$. For comparison, the noise model employed by [2] and [76] correspond to an amplitude of $0.025 < \alpha_{\text{noise}} < 0.12$. By sampling a large and competitive range of amplitudes for realizations of the per-pixel Gaussian noise, we allow the network to learn despite a variable range of noise.

It should be noted that, strictly speaking, our noise model allows for the observed signal $\hat{T}_{b,i}$ to be negative, which is unphysical, but not an uncommon observable in radio astronomy as a result of readout noise [see e.g. 83]. However, given the range of $\alpha_{\text{noise}}$ values taken above, this is a very rare occurrence.
3 Foreground Removal Methods

Since foreground contaminants are several orders of magnitude brighter than cosmological signal, the biggest challenge for upcoming observational data analysis will be to separate the two signals [19, 48]. In this section we review blind data preprocessing for foreground subtraction and introduce our improved method.

3.1 Blind Foreground Subtraction

Fortunately, foregrounds are expected to be spectrally smooth in frequency [40, 57, 72], while the cosmological signal is expected to vary with frequency according to Equation 2.1 [38, 48]. Current separation techniques therefore rely on the statistical distinctions between 21cm spectral components.

As we outlined in the last section, the observed 21cm signal can be modeled as the sum of three components: cosmological, noise, and foreground modes. Formally, we write:

\[ T_{\text{obs}}(\nu, \hat{n}) = T_{\text{fg}}(\nu, \hat{n}) + T_{\text{cosmo}}(\nu, \hat{n}) + T_{\text{noise}}(\nu) \]  

(3.1)

where each component is described with respect to a given frequency, \( \nu \), and line of sight direction, \( \hat{n} \). In a system of discrete frequencies, we can write a linear system for each line of sight over frequency:

\[ x = \hat{A} \cdot s + C_0 \]  

(3.2)

where each \( x_i = T_{\text{obs}}(\nu_i, \hat{n}) \), and \( A_{ik} = f_k(\nu_i) \) and \( s_k = S_k(\hat{n}) \) are linearly separable basis functions and foreground sky components, respectively. The cosmological signal and thermal noise can then be packaged as \( C_0 = T_{\text{cosmo}}(\nu, \hat{n}) + T_{\text{noise}}(\nu) \). We see that in these terms, foreground subtraction becomes a residual learning problem, such that we aim to reconstruct \( C_0 = x - \hat{A} \cdot s \) as accurately as possible.

3.2 PCA Residual Analysis

Principal Component Analysis (PCA) makes use of the statistical properties of foreground signals by simultaneously fitting foreground sky maps, \( s_k \), and foreground functions, \( A_{ik} \) [2, 19]. Intuitively, PCA can be thought of as fitting a multidimensional ellipsoid to a feature space, with orthogonal axes (eigenvectors) pointing in the directions of the largest variance. PCA is an orthogonal transformation which maps the data from a set of basis vectors in which the data is correlated, to a basis in which the data is linearly uncorrelated. Since foregrounds are expected to be smooth and highly correlated in frequency [19, 48, 58], removing the components of largest eigenvalue (see Section 4.6 in this work and Figure 1 in Alonso et al. [2]) is expected to preserve the cosmological signal on large angular scales relevant to cosmology. The method has been employed for foreground cleaning in both simulated and real 21cm data [11, 47, 71].

For our analysis, we repeat Alonso et al. [2]’s PCA removal procedure here. First we bin our observed maps (foreground and cosmological signal) into \( N_{\nu} = 64 \) frequency bands. We define a correlation matrix, \( C \) in frequency for all \( N_{\text{pix}} \) pixels in our simulation:

\[ C_{ij} = \frac{1}{N_{\text{pix}}} \sum_{n=1}^{N_{\text{pix}}} \frac{T(\nu_i, \hat{n}_n) T(\nu_j, \hat{n}_n)}{\sigma_i \sigma_j} \]  

(3.3)
Each full-sky simulation is comprised of 192 HEALPix pixels at 690 different frequencies. We first diagonalize each sky in frequency and remove the first 3 principal components. We then take 64 frequencies from the first bin in Table 2 to generate 3D voxels of dimension $64^3$ for deep21 to process in batches of 16. Each epoch we process $80 \times 192$ training and $10 \times 192$ validation voxels.

where $T(\nu_i, \hat{n}_i)$ is the observed 21cm map signal and $\sigma_i$ are root-mean-square fluctuations of $C_0$ in mK, in the $i$th frequency band. Each $\sigma_i$ is estimated iteratively from the data [2, 73]. The covariance $C$ can then be diagonalized via eigenvalue decomposition:

$$\Lambda = U \Lambda^T = \text{diag}(\lambda_1, \ldots, \lambda_N),$$

where $\Lambda$ is the diagonal eigenvalue matrix for $C$, and $U$ is an orthogonal matrix comprised of the corresponding eigenvectors. $\Lambda$ is ordered by decreasing eigenvalues (principal components). For every pixel $n$ we compute the PCA spectrum in frequency, and then project onto $\Lambda$. We then remove the first $N_{\text{comp}}$ components, and generate a filtered spectrum from the remainder, $C_0$, which is then assigned to the pixel as the output.

For our analyses, we preprocess observed radio sky maps and remove both the first three and first six principal components from our foreground maps. Henceforth, the notation $\text{PCA} - N_{\text{comp}}$ corresponds to signal for which the first $N_{\text{comp}}$ principal components have been removed.

Despite its ability to recover cosmological statistics in some frequency ranges, as demonstrated in [2, 19], it is important to realize that blind subtraction techniques do not guarantee that HI overdensity anisotropy will be preserved at all scales, since they are not based on a signal likelihood. PCA is best suited to removal of bright foregrounds that occupy smoother, low-rank modes compared with the cosmological signal. Unfortunately, the cosmological signal exhibits similar, smoothly varying structure on large scales, meaning PCA will remove cosmological clustering information needed for different studies (e.g. primordial non-Gaussianities [64]). Furthermore, polarization leakage from galactic synchrotron emission can create choppy foreground signal that is difficult for blind methods to distinguish from the cosmological signal (see [75] and Section 4.6). This motivates finding an approach in which a separation scheme is informed of the signal and foreground patterning.
3.3 deep21 Neural Network

In this section we present our novel method for cleaning foregrounds from 21cm maps. We adopt a convolutional neural network (CNN) architecture based on the UNet model of [59], which maps images to images via a symmetric encoder-decoder convolution scheme. This simulation-trained learning approach seeks to make a more informed separation of signals since the network has access to both foreground and cosmological axes in training.

3.3.1 Input Preprocessing

Since PCA has been shown to effectively remove the majority of foregrounds [2, 19], we focus our analysis on recovering the physical, cosmological signal from the PCA residuals. We feed in PCA-3 residual maps, processing input maps using scikit-learn [55], which implements [73]’s probabilistic PCA algorithm. Removing the first three components centers input signal on zero and drastically reduces input amplitudes, but does not remove too much small-scale cosmological clustering, as shown in [2]. PCA preprocessing thus has the added benefit of scaling inputs appropriately for neural networks, which perform best for inputs in the range $[-1, 1]$ [27]. Unlike previous analyses (see e.g. [2, 17, 19, 76]), we do not perform instrument-dependent Gaussian beam smoothing as a preprocessing step, since we want to test the ability of our model to recover signal in the limit of pixel-size resolution.

3.3.2 Dataset Assembly

To test our foreground separation methods, we generated a suite of 100 full-sky cosmological and foreground CRIME simulations over 690 frequencies, $350 < \nu < 1044$ MHz, each separated
by $\Delta \nu \sim 1\text{MHz}$. We then add a copy of the foreground and cosmological maps together, and split the dataset into 80 training simulations, 10 validation, and 10 (hidden) test simulations.

The UNet architecture is ideally suited to image-like data. For this reason, we split each simulation into 192 equal-area windows via the HEALPix pixelization scheme [28]. We then stack maps in frequency, drawing 64 frequencies evenly within the designated redshift bin, yielding 192 cubic voxels of dimension $(N_{\theta_x}, N_{\theta_y}, N_{\nu}) = (64, 64, 64)$ pixels, shown schematically in Figure 1. According to the train-validation-test split, the network sees $80 \times 192 = 15,360$ training voxels each epoch, followed by $10 \times 192 = 1,920$ validation voxels. We set aside 10 hidden test simulations with which to assess our cleaning methods.

The UNet architecture maps input voxels to output voxels via a contracting path, in which input dimensionality is halved and feature channels doubled iteratively via stride-2 downsampling convolutional layers, depicted schematically by green prisms in Figure 2. At each depth of the network, we perform $w$ convolutions. Data are then upsampled via transposed convolutions through a symmetric upsampling path. Skip connections concatenate features from one side of the network to the other, allowing each depth of the network to focus on learning a specific scale of correlations at a time. These correlations are then summed as the network upsamples on the output side. We employ batch normalization and ReLU activation between convolutional layers, except for the last convolutional block on the output side. Once voxels have been processed by the network, we reconstruct the full-sky cosmological maps to compute power spectra and clustering statistics.

3.3.3 Loss Function

To train the networks, we would like to minimize a pixel-wise loss function of the form $\mathcal{L}(p, t) = \sum_i L(|p_i - t_i|)$ between prediction, $p$, and simulation target, $t$ of each $i^{th}$ voxel, and $L(x)$ is the pixel-wise loss function. We find empirically that the standard Mean Square Error (MSE) loss proved volatile early in training. For this reason we selected the Log-Cosh loss function

$$\mathcal{L}(p, t) = \sum_i \log \cosh(p_i - t_i). \quad (3.5)$$

This function behaves much like the L1 norm for poor predictions (large values of $|p_i - t_i|$), making it robust to outliers, and approaches $(p_i - t_i)^2/2$ for small residuals. For network performance validation and test statistics we look at the Log-Cosh loss, as well as the standard MSE metric.

3.4 Training Procedure

In training our selected architecture we make use of a combination of the AdamW optimizer [42] and a step-wise learning rate reduction conditioned on validation data. This choice of learning routine provides weight decay regularization, as well as a fine-tuning of network optima.

Every training epoch the network sees 80 simulations of foregrounds added to cosmological signal, subject to a new observational noise realization for a sampled $\alpha_{\text{noise}}$. The observed maps are first preprocessed by the PCA-3 subtraction and then pixelized into HEALPix voxels described above. The PCA-3 residuals are then processed by the UNet network.

We split our frequency range to test our foreground cleaning in the context of analyses such as [76]. Redshift shells and corresponding co-moving distances are shown in Table 2. For our analysis we focus on evaluating network performances in the co-moving shell of lowest frequency, since these high-redshift regions are interesting for both Baryonic Acoustic Oscillation (BAO) measurement, as well as post-EoR structure analysis [58]. Furthermore, these
regions have consistently proven difficult for blind foreground techniques to clean, especially in angular power spectrum recovery [3, 76].

3.5 Hyperparameter Tuning

In choosing our network architecture, we first compared architectures with 2D and 3D convolutional kernels with different network depths. We anticipate that training 3D convolutional kernels perform better than 2D convolutions, since inputs in this scenario are treated as full 3D volumes, capturing frequency patterning in $\nu$, as well as angular patterns in $\theta_x$ and $\theta_y$.

Other important hyperparameters we considered were UNet depth, $h$, or number of down-convolutions (denoted by green prisms in Figure 2), and the number of convolutions at a given dimension, $w$ (convolutional block width). To test hyperparameters, we developed a dynamic UNet model compatible with the HyperOpt Python library [6]. Our architecture draws hyperparameters from proposal distributions and trains the resulting architecture on a smaller set of training data. We selected the hyperparameter combination that yielded the lowest validation loss after testing 550 trial architectures. The priors from which we drew our hyperparameters are listed in Appendix A. The results yielded the interesting result that deeper, wider UNets outperformed shallower networks (see [49] for a theoretical investigation). We found that in particular, architectures with network width $2 < w < 4$ and height satisfying

$$h = \log_{\text{stride}} n_{\text{filters}}; \quad \text{stride} = 2$$

(3.6)

consistently yielded the lowest losses. Too many convolutions per block frequently obscured the sharp $T_b$ distribution (see Figure 6), and Equation 3.6 guarantees an architecture that compresses inputs down to dimension $1^3$ for stride-2 down-convolutions, meaning the network learned correlations on a pixel-sized scales. Our optimized architecture, henceforth deep21, is displayed graphically in Figure 2.

Neural network outputs are generally not probabilistically interpretable [14], and no tractable image-producing Bayesian neural networks currently exist, so quantifying the variability of foreground cleaning on a given dataset is not possible with a single UNet.

Motivated by the methodology of deep ensembles [22, 35] we train an ensemble of $M = 9$ networks with independently Glorot-Uniform-initialized weights [26] for 300 epochs in parallel. The HEALPix data inputs are also subject to the stochastic noise model as before, as well as random sky-sized rotations on the sphere, such that the networks learn to denoise pixels independently of orientation. To gauge the uncertainty of the cleaning method, each ensemble member then performs foreground separation on ten test simulations, subject to competitive observational noise with a fixed $\alpha_{\text{noise}} = 0.25$, falling in the upper range of our amplitude prior and roughly twice the maximum noise amplitude utilized by Alonso et al. [2]. This practice allows us to estimate the epistemic uncertainty on the summary statistics obtained from the predicted full-sky maps.

4 Results and Analysis

4.1 Visual Inspection

Most current and upcoming cosmological experiments are aimed at reconstructing relevant clustering statistics from brightness temperature maps. Therefore it is prudent to ensure that our network outputs clean maps that capture temperature distributions at given frequencies. An initial check for deep21’s performance is a qualitative one: Figure 3 shows each
Figure 3: 2D slices at $\nu = 392$ MHz comparing raw foreground signal (top left), PCA-3 UNet inputs (top right), to the UNet ensemble prediction (lower left) and target cosmological signal (lower right). \texttt{deep21} is able to correctly reconstruct the signal from minimal PCA-3 subtracted inputs.

cleaning method’s performance on a HEALPix pixel slice drawn from the test set. The top two panels display observed input signal and the initial PCA-3 preprocessing network inputs. The bottom row compares the network-cleaned panel compared with the target cosmological signal. \texttt{deep21} is able to recover intricate cosmological signal from corrupted inputs almost indistinguishable from the simulated targets.

In Figure 4, we compare the per-pixel scaled cosmological signal (greyscale panel) to the
Figure 4: Temperature map residuals for PCA-6 (middle) and deep21 (right) map residuals compared to scaled intensity of the simulated cosmological signal (left) for the same 2D slices as Figure 3. The UNet ensemble recovers a much more accurate tomography than the PCA method, the latter failing to capture details around high-intensity regions and voids. Removal of the first moment in the PCA method results in a significant deviation (∼200%) from the true signal, while deep21 predictions yield small, positive residuals.

Relative residual error for cosmological brightness temperature $T_b$,

$$\delta_{err,i} = \frac{p_i - t_i}{t_i}$$  \hspace{1cm} (4.1)

where $p_i$ and $t_i$ are the pixel-wise predicted and target signals, respectively. Here we compare the best-case (PCA-6) blind subtraction to deep21. We note that PCA predictions over-subtract the signal, particularly in low-density regions. deep21’s residuals are all well within order unity of the target, with some deviations above zero.

4.2 Clustering Statistics

The most important cosmological parameter constraints from HI intensity mapping will most likely come from power spectra of the 21cm brightness temperature, since two-point correlation functions contain the vast majority of information regarding underlying cosmology on large, linear, scales. For this study, we consider angular and radial power spectra separately, capturing clustering patterning on the sky and along each line of sight, respectively.

For a fixed frequency and assuming a full-sky survey, the angular power spectrum of the brightness fluctuations $\Delta T_b$ is computed first by calculating the spherical harmonic components:

$$a_{\ell m}(\nu) = \int d\hat{n}^2 \Delta T_b(\nu, \hat{n}) Y^*_{\ell m}(\hat{n})$$  \hspace{1cm} (4.2)

where $Y_{\ell m}(\hat{n})$ are the spherical harmonic basis functions. We can then estimate the power spectrum by averaging over the moduli of the harmonics:

$$\tilde{C}_\ell = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |a_{\ell m}|^2$$  \hspace{1cm} (4.3)

where small $\ell$ correspond to the largest scales. We calculated the angular power spectra for our maps using the healpy Python library [89].
Table 2: Comparison of the four redshift co-moving shells used in the UNet assessments. Co-moving shells were chosen by splicing the simulation into bins with equal numbers of frequency. Our analysis focuses on the highest-redshift bin because this is where blind foreground techniques such as PCA reduction have been shown to perform the worst in the literature.

| $\nu$ (MHz) | $z$ | $\langle z \rangle$ | Vol. (h$^{-1}$Gpc)$^3$ | $N_{\text{side}}$ |
|-------------|-----|-------------------|------------------|-----------------|
| [868 – 1044] | [0.36 – 0.60] | 0.47 | 12 | 256 |
| [667 – 886] | [0.60 – 1.12] | 0.87 | 50 | 256 |
| [476 – 667] | [1.12 – 1.88] | 1.50 | 108 | 256 |
| [350 – 491] | [1.88 – 3.05] | 2.47 | 187 | 256 |
| [252 – 347] | [3.05 – 4.12] | 3.47 | 356 | 256 |

To capture radial clustering in an HI survey independent of redshift effects, one must make two assumptions, namely 1) each line-of-sight (HEALPix pixel) window satisfies the flat-sky assumption [3], and 2) that the redshift bin under consideration is narrow enough that no significant cosmological expansion occurs between the edges of the bin. The resulting power spectrum then describes the clustering distribution independently of cosmological expansion effects. Given these two assumptions, we can average over all possible radial lines of sight, $i = 1, \ldots, N_{\theta}$, to obtain the radial power spectrum:

$$P_{\parallel}(k_{\parallel}) = \frac{\Delta \chi}{2\pi N_{\theta}} \sum_{i=1}^{N_{\theta}} |\Delta \hat{T}_{b}(\hat{n}, k_{\parallel})|^2$$

(4.4)

where the Fourier coefficients $\Delta \hat{T}_{b}$ are estimated using the Fast Fourier Transform (FFT) over each line of sight, and $\Delta \chi = \chi(z_{\text{max}}) - \chi(z_{\text{min}})$ is the comoving width of the given redshift bin. Given a constant frequency interval separating the spherical surfaces, $\delta \nu$, the same interval is expressed in the conjugate space as $\delta k_{\nu} = 2\pi/\Delta \nu$. The radial coordinate, $k_{\parallel}$, can then be defined as [3]:

$$k_{\parallel} = \frac{\nu_{21}H(z_{\text{eff}})}{(1 + z_{\text{eff}})^2} k_{\nu},$$

(4.5)

where $z_{\text{eff}}$ is the effective redshift for the comoving volume under consideration.

To capture uncertainty over the space of the deep21 ensemble, we compute a weighted average, $\bar{Z}_{w}$, and standard deviation, $\sigma_{w}(Z)$, of each network’s independent estimate of a given statistic, $Z$. We employ proper scoring weights by computing the inverse globally-averaged MSE for each network’s prediction over test data: $w_{m} = 1/(\left\langle \text{MSE} \right\rangle)$ for $m = 1, \ldots, 9$ independent networks. Here we do not explicitly assume a Gaussian form, so $\sigma$ does not correspond to the 68% inclusion interval. We note that to apply this procedure in a real observational setting, scores for each ensemble member would need to be computed for a set of validation simulations, and then used to compute statistics obtained from the cleaned observed sky.

We consider the power spectra calculated for the residual maps for each cleaning method, defined for $P \in \{C_{\ell}, P_{\parallel}\}$ as:

$$\rho_{\text{res}} = \frac{P_{\text{res}}}{P_{\text{cosmo}}} = \frac{P(p - t)}{P(t)}$$

(4.6)

where $t$ is the target cosmological signal and $p \in \{T_{\text{PCA}}, T_{\text{deep21}}\}$ is the given cleaning method’s predicted map. We additionally consider $\rho_{\text{res}}$ computed for the noise map, $P(T_{\text{noise}})$, generated for the test simulation.
Figure 5: Comparison of angular (left) and radial (right) residual map power spectra as a fraction of the target cosmological signal predicted by the deep21 UNet ensemble (green) blind PCA reduction (purple), and noise realization (black) with $\alpha_{\text{noise}} = 0.25$ over a single full-sky test simulation. Confidence intervals corresponding to $\pm 2\sigma_w$ over the space of ensemble parameters is estimated in shaded green. We display deep21’s angular resolution via the black dashed vertical line. The angular power spectrum shown is computed for a single frequency, $\nu = 357$ MHz, while the radial power spectrum is computed for the lowest frequency bin, with mean redshift $\langle z \rangle = 2.5$. The network successfully learns to marginalize out additive observational noise in the radial direction at smaller scales ($k_\parallel > 0.015$).

This statistic quantifies each cleaning method’s residuals as a fraction of the true cosmological signal in both the angular and radial directions. The noise residual demonstrates to what degree observational error obscures the structure estimate.

We compare deep21 to the PCA-6 residual noise realization generated with $\alpha_{\text{noise}} = 0.25$ in Figure 5. deep21 (green) outperforms PCA (purple) in both the angular and radial directions, and successfully fits cosmological signal at small scales despite high observational noise contribution (black dashed line). We interpret this result as a successful marginalization of the observational noise. Through training, deep21 has learned to distinguish cosmological clustering from noise fluctuations at small scales. By contrast, the PCA-6 residual asymptotically approaches the noise boundary in both plots, indicating a limit to the blind foreground cleaning at small scales. deep21 also substantially reduces the loss of signal at large radial scales incurred by the PCA method. The larger PCA-6 residual at small $k_\parallel$ indicates large-scale information lost to the foreground subtraction as demonstrated in [2].

4.3 Intensity Distributions

We also compare how well each cleaning method captures the distribution of the cosmological signal at each frequency. Figure 6 compares cosmological temperature distributions at several frequencies throughout a single test simulation. We see that the PCA method reproduces a more symmetric temperature distribution that is zero-centered. This result is anticipated by the definition of the method (which removes the mean of the distribution to diagonalize the signal in frequency). It is clear from comparison to the true signal that deep21 captures the asymmetric distribution much more accurately than the PCA.
Figure 6: Comparison of the distribution of pixel temperatures from the PCA-6 (purple) and deep21 (green) cleaned maps to those of the cosmological simulations (black) at several different frequencies. deep21 captures the target asymmetric temperature PDF much more effectively than the PCA.

4.4 Power Spectrum Recovery

We additionally report clustering statistics based on the analysis by [2]. We introduce the power spectrum correlation statistic

\[ r(k) = \frac{P_p \times t(k)}{\sqrt{P_p(k)P_t(k)}} \]  

(4.7)

where \( P_p \) is the predicted auto-power spectrum from the foreground cleaning method under consideration, \( P_t \) is the auto-power spectrum generated by the target cosmological map, and \( P_p \times t \) is the cross-spectrum between the predicted and target maps. This statistic quantifies discrepancies in phases introduced by each cleaning method. We also define the transfer function for coordinate \( k \in \{ \ell, k_\parallel \} \)

\[ T(k) = \sqrt{\frac{P_p(k)}{P_t(k)}} \]  

(4.8)

which quantifies discrepancies in amplitude as a function of scale \( k \) between cleaned and target maps. For a perfect foreground cleaning, both \( r(k) \) and \( T(k) \) approach 1.

The statistic \( 1 - r^2(k) \) describes the fraction of variance in cleaned maps that isn’t accounted for in the target map. We compare this variance as a function of scale for angular and radial power spectra in Figure 7. deep21 (green) outperforms the PCA-6 consistently at both large and small angular and radial scales, capturing the correct phase within \( \sim 80\% \) accuracy within the comoving bin. This statistic demonstrates the results displayed in Figure 6 as a function of scale: network-based cleaning captures the non-Gaussian cosmological signal with much higher accuracy, particularly in the angular direction. This is because unlike the PCA, deep21’s convolutional filters have access to neighboring pixels in the spatial axes, meaning foreground separation can be learned simultaneously in \{\( \theta_x, \theta_y, \nu \}\}.

The consistency of the deep learning approach should be emphasized here: the deep21 method is largely scale-independent in foreground removal and signal reconstruction. Moreover, these results are not reliant on statistical marginalization over many data realizations.
Figure 7: Residual variance $1 - r^2(k)$ for both angular (left) and radial (right) power spectra. The angular spectrum is computed at $\nu = 357$ MHz, with the angular resolution of a deep21 input voxel shown via the black dashed vertical line. deep21 (green) outperforms the PCA-6 subtraction on all angular scales. In the radial direction, deep21 offers a significant improvement in preserving phase information on intermediate scales.

like the analyses done in [2] and [76], meaning fewer observations need to be made in a realistic setting in order to achieve a consistent, successful foreground removal with estimated uncertainties. Furthermore, with more computational power, larger voxels can be expected to be processed in the future, resulting in an improvement in large-scale network recovery.

4.5 Noise Performance and Instrument Effects

deep21’s training procedure includes variable levels of observational noise to improve test performance and incorporate uncertainty regarding noise levels in upcoming intensity mapping experiments. To test whether or not the ensemble learned to marginalize out this effect, we tasked the trained network with cleaning the same foreground simulation with a variable noise amplitude, $\alpha_{\text{noise}}$. We plot the corresponding MSE metric in Figure 8. The network’s test MSE remains fairly constant until we exceed the noise threshold, $\max\{\alpha_{\text{noise}}\} = 0.5$, encountered in training. This shows that deep21 indeed captures the statistical properties of the observational noise it encountered during training, and subsequently marginalizes over it. In contrast, the blind PCA subtraction, whose MSE is dominated by the removal of the first moment of signal, does not increase in MSE until $\alpha_{\text{noise}} = 1$, or order unity with the mean cosmological signal at a given frequency (see Equation 2.6). This result shows that a network ensemble can be trained to be robust to observational noise and more complicated instrument effects, so long as a statistical model is specified and varied enough during training, a significant advantage over blind approaches with no access to this information.

4.6 Generalization to new foreground parameters

Despite training deep21 on many foreground and cosmological realizations, we assumed the same fiducial model for all training data generation. For a foreground cleaning experiment with real data, one would ideally train deep21 on a range of foreground and cosmological models. As a final test for our trained UNet ensemble, we task the network, trained on fiducial simulation parameters, with cleaning observed signal generated by different input parameters.

To do this, we chose to alter the galactic synchrotron foregrounds via the CRIME simulation package, since these represent the largest of the foreground contaminants. Since the
Figure 8: Noise performance testing for deep21 and PCA-6 cleaning routines. 20 maps were generated with increasing noise amplitude \( \alpha_{\text{noise}} \). As anticipated, deep21 performs consistently for \( \alpha < \alpha_{\text{max}} = 0.5 \), since this represents the level of noise the network encountered during training according to Equation 2.6. The network’s error quickly increases in variance and magnitude beyond this threshold.

PCA processing removes synchrotron amplitude information, we elected to alter its correlation structure according to Equation 2.3, namely 1) angular scale dependence, 2) frequency dependence and 3) switching on polarization effects. We display recovered power spectra for the correlation structure analysis in Figure 9.

Varying galactic synchrotron angular correlation dependence

Having trained deep21 on foregrounds with fiducial galactic synchrotron \( \beta_o = 3.3 \), we vary the synchrotron \( \ell \) dependence according to Equation 2.3 by \( \pm 30\% \) to \( \beta = 1.3 \beta_o \) and \( \beta = 0.7 \beta_o \), generating a new full-sky simulation of 192 HEALPix voxels for each case. Increasing \( \beta \) yields a smaller foreground correlation in \( \ell \), reflected in deep21’s over-estimate of the power spectrum in Figure 9a. Likewise, the network under-estimates the power spectrum for lower \( \beta = 2.3 \). This indicates that the network has indeed captured the fiducial foreground model in the training data.

Varying galactic synchrotron frequency correlation dependence

We repeated the same analysis for the \( \alpha \) parameter, varying the galactic synchrotron \( C_\ell \) model’s dependence on frequency by \( \pm 35\% \). We recovered a similar trend in deep21 performance in Figure 9b. Here, decreasing \( \alpha \) results in a smaller correlation amplitude as a function of frequency. deep21 produces an over-estimate of the radial power spectrum since it is trained on \( \alpha = 2.8 \). Increasing \( \alpha_v = 1.35 \alpha_o \) produces little difference in the ensemble estimate, indicating that the model might generalize well in this regime.

In contrast, PCA-6 cleaning (dashed orange) yields almost identical results for changes in the correlation parameters, indicating that the blind method is robust to changes in correlation structure. We display foreground cleaning results at different scales for our test and generalization cases in Table 3.

Polarized foregrounds

We also tested simulations contaminated by a galactic synchrotron polarization leakage of 1%. Polarized foregrounds due to the Milky Way’s magnetic effects could wreak a catastrophic
Figure 9: Generalization testing for deep21. We compare two-point statistics on test data by varying foreground parameters, keeping training data and trained network ensembles constant. We vary the galactic synchrotron $\beta$ and $\alpha$ in Figures 9a and 9b, respectively, according to Equation 2.3. We display power spectra (top), transfer function, i.e. the square root of predicted to true spectrum (middle), and residual variance fraction $1 - r^2(k)$ (bottom) for both angular (at $\nu = 357$ MHz) and radial statistics.

effect on signal recovered using blind techniques, since poorly-understood polarization leakage could induce foregrounds to interfere with cosmological signal modes [3, 38]. To motivate a follow-up study, we enabled galactic synchrotron polarization within the CRIME simulation package, varying the polarized correlation length $\xi_{\text{polar}}$, and cleaned the resulting observed maps with our technique. We recovered substantial differences in performance for PCA-6 and deep21, as shown in Figure 10. Reducing the correlation length, $\xi_{\text{polar}}$ makes leaked galactic synchrotron foreground emission behave similarly to the cosmological signal in frequency (see lefthand plot for $\xi_{\text{polar}} = 0.01$, and Figure 8 in [3]). The PCA subtraction fails since synchrotron foregrounds can no longer be smoothly resolved from the choppy cosmological signal. This is shown formally in [2], Figure 1, where decreasing polarization correlation length spreads foreground contamination across diagonalized PCA eigenvalues, making it more difficult to know when foregrounds have been successfully removed. As expected, deep21 does not generalize well to polarized foregrounds, since PCA-3 preprocessing is unable to remove the 1% synchrotron leakage. We do, however, note that deep21 does produce a slight improvement in radial power spectrum recovery (Figure 10, right-hand side).

For a more complete understanding of polarized foregrounds and deep21’s effectiveness
Figure 10: Foreground cleaning errors due to 1% galactic synchrotron polarization leakage. (Left) \texttt{deep21} temperature recovery compared with several PCA subtractions for $\xi_{\text{polar}} = 0.01$. Removing as many as 21 PCA components does not resolve the cosmological signal in the presence of polarization leakage. (Right) Transfer function for \texttt{deep21} recovery of radial power spectrum recovery for various values of $\xi_{\text{polar}}$. Here the PCA-6 subtraction is shown for the given simulation as a dashed line, and shaded contours show $\pm 2\sigma_w$ \texttt{deep21} estimates. Shrinking the polarization correlation length makes leaked galactic synchrotron foregrounds behave similarly to the cosmological signal in frequency, rendering blind methods and \texttt{deep21} ineffective.

in removing them, a follow-up study is warranted. Existing codes such as \texttt{Hammurabi} [80] make use of detailed three-dimensional Milky Way simulations to model the magnetic fields responsible for polarization leakage. Training \texttt{deep21} on these detailed foregrounds is a necessary next step for real data-preparedness.

| test phase | MSE (global) | $T(\ell = 50)$ | $T(k_i = 0.02)$ | $\rho_{\text{res}}(\ell = 50)$ | $\rho_{\text{res}}(k_i = 0.02)$ | $T(\ell = 500)$ | $T(k_i = 0.15)$ | $\rho_{\text{res}}(\ell = 500)$ | $\rho_{\text{res}}(k_i = 0.15)$ | $\alpha_{\text{noise}} = 0.25$ |
|------------|--------------|----------------|-----------------|-------------------------------|-------------------------------|-----------------|-----------------|-------------------------------|-------------------------------|-----------------|
| deep21     | 0.877±0.156  | 0.899±0.186    | 0.728±0.087     | 3.857±1.178                  | 1.099±0.307                  | 0.848±0.085      | 0.868±0.088      | 1.099±0.13        | 0.648±0.115           |                  |
| PCA-6      | 17.15        | 0.611          | 1.095           | 8.2                          | 1.184                        | 0.814            | 1.195            | 2.417             | 1.005               |
| $\beta = 2.3$ |             |                |                |                              |                              |                 |                 |                                |                                |
| deep21     | 0.872±0.152  | 0.895±0.212    | 0.728±0.088     | 4.45±4.414                   | 1.076±0.3                   | 0.839±0.086      | 0.867±0.088      | 1.063±0.135       | 0.649±0.115           |                  |
| PCA-6      | 17.15        | 0.542          | 1.093           | 11.49                        | 1.183                        | 0.773            | 1.194            | 2.397             | 1.005               |
| $\beta = 4.3$ |             |                |                |                              |                              |                 |                 |                                |                                |
| deep21     | 1.04±0.289   | 0.977±0.19     | 0.738±0.081     | 5.83±5.094                   | 1.297±0.46                   | 0.853±0.114      | 0.874±0.103      | 1.344±0.291       | 0.666±0.132           |                  |
| PCA-6      | 17.16        | 0.607          | 1.092           | 9.025                        | 1.21                         | 0.763            | 1.195            | 2.805             | 1.006               |
| $\alpha = 1.3$ |             |                |                |                              |                              |                 |                 |                                |                                |
| deep21     | 1.764±0.056  | 1.57±0.505     | 0.84±0.081      | 23.76±23.8                   | 1.999±0.785                  | 0.867±0.111      | 0.87±0.114       | 1.588±0.321       | 0.691±0.143           |                  |
| PCA-6      | 17.15        | 0.534          | 1.095           | 7.945                        | 1.186                        | 0.755            | 1.194            | 2.536             | 1.005               |
| $\alpha = 3.3$ |             |                |                |                              |                              |                 |                 |                                |                                |
| deep21     | 0.871±0.152  | 0.907±0.229    | 0.727±0.088     | 3.13±3.146                   | 1.07±0.3                    | 0.828±0.083      | 0.867±0.088      | 1.164±0.151       | 0.649±0.114           |                  |
| PCA-6      | 17.15        | 0.534          | 1.095           | 7.945                        | 1.186                        | 0.755            | 1.194            | 2.536             | 1.005               |

Table 3: Summary of foreground cleaning results. All residuals and MSE metrics are normalized to the corresponding statistic computed for observational noise generated with $\alpha_{\text{noise}} = 0.25$. Angular power spectra are computed for a slice at $\nu = 357\text{MHz}$. Uncertainty intervals for \texttt{deep21} were computed for $\pm 2\sigma_w$ for each statistic.
Figure 11: Mean (left) and variance (right) of angular power spectrum correlation, $r(\ell)$ computed over frequencies in the first comoving shell for PCA (purple) and deep21 methods (green, shaded $\pm 2\sigma_w$). The deep21 ensemble’s correlation with target signal is consistent with one at all but the smallest scales, showing a distinct improvement at large scales. The variance plot shows that the network method is over an order of magnitude more consistent in capturing map phase information than the more variable PCA as a function of scale.

5 Conclusions

In this study we developed a deep learning-based method to improve foreground cleaning techniques for single-dish 21cm cosmology. Our method outputs clean intensity maps instead of derived summary statistics. Training an ensemble of independent U-Net architectures on simulated foregrounds and cosmological signal resulted in the improved recovery of intensity maps and angular and radial power spectra. Figure 11 summarises the network’s performance in the radial direction. The lefthand panel shows that on average over frequency, deep21’s $r(\ell)$ is of order 1, offering a distinct improvement on the largest scales. The righthand plot demonstrates that deep21 is over an order of magnitude more consistent in capturing phase information over frequency than PCA-6. In addition, the ensemble method provides an estimate of uncertainty for the summary statistics of resulting maps. We show that deep21 effectively marginalizes out observational noise at small angular and radial scales, demonstrating a marked improvement in the sensitivity limit of foreground subtraction over PCA. This suggests that a learning separation approach could be hardened against instrument effects, presenting a significant advantage over blind methods. We show that deep21 is sensitive to foreground physics by changing test data simulation parameters, meaning deep networks trained on more detailed (and varied) simulations will likely be able to effectively remove foregrounds in absence of a formal foreground likelihood. We also investigated deep21’s failure modes, namely in the presence of galactic synchrotron polarization leakage. Improved networks trained on polarized foregrounds (including those which require no PCA preprocessing) will be the subject of a future work to mitigate these effects on radio map retrieval. Our method demonstrates that cosmological analyses on previously irretrievable 21cm intensity maps may be possible in an observational setting.

5.1 Future Work

The methods outlined here utilize a simulation-based deep learning method to retrieve intensity maps for radio cosmology. These techniques pave the way for more fundamental studies of the 21cm signal captured by upcoming SKA experiments, as well as future studies with
even higher resolution. The ability to retrieve intensity maps will allow future studies to probe structure formation and EoR physics beyond the power spectrum statistic.

However, before deep21 can be applied to real 21cm data, several key aspects should be addressed in follow-up studies:

- Rigorous quantification of network errors: although deep21 achieves a more consistent foreground cleaning than blind methods, the error in the network method is still not fully understood. A way to quantify this effect is to incorporate a deep21-like cleaning method in a simulation-based inference pipeline for compressed cosmological parameters [see e.g. 4, 13]. If foreground cleaning is performed as a step in a simulation pipeline, cleaning method errors can be propagated to parameter measurement using Approximate Bayesian Computational methods.

- BAO application: a future study might train deep21 on cosmological data without BAO oscillations, and then ask the network to clean data with BAO signal. Training a network with a fiducial BAO radius would introduce a bias, but cleaning a map with a BAO-free network might be trained to leave an unbiased BAO residual signal in the predicted map, since BAO signal is expected to be statistically distinct from foreground and cosmological signal [76, 86].

- A more realistic noise model: the white noise model considered here, while frequency-dependent, will not extend to more complicated intensity map datasets, such as those obtained via interferometry [65]. Thus the impact of nontrivial noise correlations on network performance must be considered before real signals can be reliably separated. A deep21-like study on systematics would additionally benefit from varying observed sky fraction, as is done in Villaescusa-Navarro et al. [76] for 21cm BAO recovery.

- Varying astrophysical parameters: here we trained deep21 on thousands of input voxels derived from the same fiducial cosmological and foreground parameters. While the network performed relatively well in some generalization cases, deep21 would ideally be trained on a range of simulation parameters, like is done by Villanueva-Domingo and Villaescusa-Navarro [78], before asked to clean real data.

- Training on polarized foregrounds: We additionally probed a failure mode of the network in the presence of 1% galactic synchrotron radiation polarization leakage. Here the PCA preprocessing fails to separate the leaked and cosmological signals, making it harder for deep21 to pick out the cosmological signal. A follow-up study might additionally train on more realistic polarized simulations, such as those produced by Hammurabi, as well as bypass the need for a blind preprocessing step.

- Increasing input sizes: deep21’s input voxel sizes were limited by available GPU memory. With improved deep learning computational resources (or a detailed tiling strategy such as the one employed by He et al. [31] for N-Body analyses), Increasing input size will likely improve foreground removal on large scales, since the network will have access to a larger context of information. Ideally, entire maps would only be split into a handful of UNet input units. An increase in input volume might also allow for a larger frequency range to be assessed, which would aid the network in distinguishing cosmological and polarized signals, as well as improve radial power spectrum recovery.
Code Availability

The code used for training and generation of results is publicly available at https://github.com/tlmakin/en/deep21. A browser-based tutorial for the experiment and UNet module is available via the accompanying Colab notebook.

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A Hyperparameter choices

| Symbol    | Prior Distribution | Optimum | Description                                      |
|-----------|--------------------|---------|--------------------------------------------------|
| conv ND   | [2,3]              | 3       | convolution filter dimensions                    |
| h         | disc $\mathcal{U}(2, 6)$ | 6       | no. of down-convolutions                         |
| w         | disc $\mathcal{U}(1, 6)$ | 3       | no. of convolutions for each conv. block         |
| batchnorm | [0,1]              | True*   | batch normalization for given layer              |
| batch size| log$\mathcal{U}(4, 24)$ | 48      | no. of samples per gradient descent step         |
| n\_filters | [8,16,32]        | 32      | initial number of conv. filters                  |
| $\beta_{\text{mom}}$ | log$\mathcal{U}(0.001, 0.75)$ | 0.05    | batch normalization momentum                     |
| $\lambda$ | log$\mathcal{N}(-8.5, 2.5)$ | 0.0002  | learning rate for Adam optimizer                 |

Table 4: Table of UNet parameters varied in architecture design, with optimal values (per GPU processor) shown. The algorithm HyperOpt was used in conjunction with the Adam optimizer tuning according to [6]. The discrete uniform distribution is denoted by disc $\mathcal{U}(\cdot)$. *Batch normalization adopted for encoder layers.