Design and implementation of the NaI(Tl)/CsI(Na) detectors output signal generator

ZHOU Xu(周旭)1,2, LIU Cong-Zhan(刘聪展)1,2, ZHANG Jian-Ling(张健领)1,2, ZHANG Fei(张飞)1,2,
ZHANG Yi-Fei(张翼飞)1, LI Zheng-Wei(李正伟)1,2, ZHANG Shuo(张硕)1,2, LI Xu-Fang(李旭芳)1,
LU Xue-Feng(路雪峰)1, XU Zhen-Ling(许振玲)1, LU Fang-Jun(卢方军)1

1 Institute of High Energy Physics, Chinese Academy of Sciences, Beijing 100049, China
2 University of Chinese Academy of Sciences, Beijing 100049, China

Abstract: We designed and implemented a signal generator that can simulate the output of the NaI(Tl)/CsI(Na) detectors’ pre-amplifier onboard the Hard X-ray Modulation Telescope (HXMT). Using the development of the FPGA (Field Programmable Gate Array) with VHDL language and adding a random constituent, we have finally produced the double exponential random pulse signal generator. The statistical distribution of the signal amplitude is programmable. The occurrence time intervals of the adjacent signals contain negative exponential distribution statistically.

Key words: FPGA, M sequence, rejection technique, Gaussian distribution, signal generator

PACS: 95.55.Ka DOI: 10.1088/1674-1137/38/2/026002

1 Introduction

HXMT is the first X-ray astronomy satellite in China. The High Energy X-ray Detector (HED), which consists of 18 collimated units, is the core payload on HXMT. Every unit of HED is made up of a NaI(Tl)/CsI(Na) phoswich, photomultiplier tube (PMT), high-voltage divider and pre-amplifier [1]. This paper introduces a new random pulse generator to simulate the pre-amplifier’s output of an actual scintillator detector, such as the HED. The project of design, electric circuit principle design, software design of random pulse generator and pulse output circuit are introduced. The amplitude and time intervals of the signal are adjustable, and so the generator can be used as a safe and low cost signal source for the High energy Electronics System (HES) of HXMT in testing, such as vacuum, temperature, vibration and EMC (Electromagnetic Compatibility) tests [2]. The experiences we obtained are also useful for the development of other kinds of random pulse generators [3].

There are three kinds of interactions between high energy photons and materials: the photoelectric effect, the Compton scattering effect and pair production. For the HED, whose main purpose is to detect X-rays in the energy band 20–250 keV, the main interaction is a photoelectric effect, as illustrated in Fig. 1. However, at energies higher than 100 keV, the Compton scattering effect cannot be simply neglected. Therefore, our signal generator needs to not only simulate the photoelectric effect but also the Compton scattering effect.

Fig. 1. The mass-absorption coefficient of NaI crystal [4].
2 Design of the signal generator

When an X-ray photon hits on the NaI(Tl) or CsI(Na) crystal of the HED, fluorescence light is produced and then collected by the PMT coupled to the back of the CsI (Na) crystal. The light has a fast exponential rise followed by a slower exponential decay and the amount of light is proportional to the energy of the incident photon. To simulate the features of the actual HED signal, the generator should be able to produce a double exponential shape wave whose expected amplitude is adjustable. Furthermore, the statistical distribution of the occurrence time intervals should follow a negative exponential function.

The function block diagram is shown in Fig. 2. FPGA is the centre part of the wave generation. The design idea of FPGA is shown in Fig. 3.

Fig. 2. Illustration of the function blocks of the signal generator.

Fig. 3. Diagrammatic drawing of FPGA inside.

2.1 Realization of the double exponential wave

The design of the shaping circuit to simulate the signals of NaI(Tl) and CsI(Na) detectors’ pre-amplifier is shown in Fig. 4.

The circuit can produce a positive pulse at the rising edge of the square wave and produce a negative pulse at the falling edge. Useless negative pulse is removed by an analog switch. Positive pulse is used to generate the double exponential signal. The detailed analysis is described as follows.

For the CR loop:

\[ I(t) = \frac{U(t)}{R}; \quad (1) \]

\[ U(t) = U_0 - \frac{Q}{C} = U_0 - \frac{1}{C} \int_0^t I(t')dt'. \quad (2) \]

Therefore:

\[ U(t) = U_0 e^{-t/RC}. \quad (3) \]

For the \( R_0C_0 \) loop:

\[ U'(t) = U(t) = U_0 e^{-t/RC}; \quad (4) \]

\[ V(t) = \frac{Q_0}{C_0} - \frac{1}{C_0} \int_0^t U'(t') - V(t') \frac{R}{R_0} dt'. \quad (5) \]

Therefore:

\[ V(t) = U_0 \frac{RC}{RC - R_0C_0} (e^{-t/RC} - e^{-t/R_0C_0}). \quad (6) \]

As a result, the expression of PMT’s output of the phoswich detector is that:

\[ U_{\text{NaI+CsI}}(t) = U_0^{\text{NaI}} \frac{R_{\text{NaI}}C_{\text{NaI}}}{R_{\text{NaI}}C_{\text{NaI}} - R_0C_0} (e^{-t/R_0C_0} - e^{-t/R_0C_0}) \]

\[ + U_0^{\text{CsI}} \frac{R_{\text{CsI}}C_{\text{CsI}}}{R_{\text{CsI}}C_{\text{CsI}} - R_0C_0} (e^{-t/R_0C_0} - e^{-t/R_0C_0}). \quad (7) \]

The first-part of the expression is the contribution of NaI, and the second-part accounts for the CsI signal. \( U_0 \) is the gain coefficient of each signal; \( R_0C_0 \) is the parameter (300 ns, empirical value) of forming time in the circuit. It depends on the charge-discharge in the \( R_0C_0 \) loop. By assigning \( RC \) (\( RC \) stands for the fluorescence light decay constant of the scintillator) here, NaI is 230 ns and CsI is 630 ns. In addition, rising-time, falling-time and wide are confirmed. We can produce the wave we hoped, which is shown in Fig. 5.

In practice, we use fixed value capacitor \( C \) and adjustable resistor \( R \), so that different decay time can be produced [5, 6].
2.2 The method to make the expected amplitude adjustable

The thought of M sequence is used in the random number module. The widely used M sequence is also called pseudorandom sequence or pseudorandom code, which has extensive applications in communication as an equally distributed random number generator [7]. We construct the M sequence by using the VHDL language, and collect the output of being transformed by the DAC (Digital Analog Converter) in the multichannel analyzer MCA8000A, as shown in Fig. 6.

On the basis of central limit theory: for $N$ equally distributed random variables, if $N$ is large enough, the distribution of the sum is close to a Gaussian distribution. Testing shows that when $N$ is equal to or larger than 12, the result is almost perfect [3]. So in this paper we make $N$ equal to 12. That means the sum of 12 different initial values’ random series contains the Gaussian distribution. We can make it in the FPGA. The output of the signal generator is transformed by the DAC, and we sample the output of the DAC by the multichannel analyzer, as shown in Fig. 7.

Meanwhile, we can simulate the photoelectric effect conditions at different energies. For example, we can simulate the photoelectric effects at 60 keV, 122 keV and 250 keV at the same time. The probability of X-ray photons absorbed by the NaI(Tl) or CsI(Na) crystal at different energies is obtained by GEANT4 simulation. Table 1 listed below is the resulting approximate fraction of X-ray photons having a photoelectric effect in NaI or CsI scintillation crystals.

In order to meet the proportion demands above, for an incident X-ray photon with a specific energy, we set

\[
\chi^2 = \sum_{i=1}^{n} \left( \frac{(y_i - y_{i,\text{pred}})^2}{\sigma_i^2(N-1)} \right) = 6.31, \quad y_{i,\text{pred}} \quad \text{stands for the expected model value}, \quad N-1 \quad \text{stands for the degree of freedom}, \quad \sigma_i^2 = y_{i,\text{pred}}.
\]

It is better near the central value, but error is relatively obvious far away from the central value).

Fig. 5. The oscilloscope screenshot of the NaI wave.

Fig. 6. Equiprobability random statistical distribution generated by the random number module. ($\delta_i = y_i - \bar{y}$, the standard deviation of $\delta_i$ is 89.81, which is about 3% of the mean counting value $\bar{y}$).

Fig. 7. Gaussian statistical distribution obtained by the M sequence method (the fitting function $y = 2394 \exp\left(-\left(\frac{x-87}{41}\right)^2\right)$, $\chi^2/(N-1) = \sum_{i=1}^{n} \left( \frac{(y_i - y_{i,\text{pred}})^2}{\sigma_i^2(N-1)} \right) = 6.31$, $y_{i,\text{pred}}$ stands for the expected model value, $N-1$ stands for the degree of freedom, $\sigma_i^2 = y_{i,\text{pred}}$. It is better near the central value, but error is relatively obvious far away from the central value).

Fig. 8. The energy spectrum of the simulated NaI(Tl)/CsI(Na) detection of the 60 keV, 122 keV and 250 keV X-ray photoelectrons.
Table 1. The probability of photoelectric interaction of X-ray photons with different energies in the NaI(Tl) or the CsI(Na) scintillators.

| scintillator | layer | thickness/mm | 60 keV(%) | 122 keV(%) | 250 keV(%) |
|-------------|-------|--------------|-----------|------------|------------|
| NaI(Tl)     | outer | 3.5          | 100       | 75         | 20         |
| CsI(Na)     | inner | 40           | 0         | 25         | 80         |

a threshold in the code. If the equiprobability random is smaller than the threshold, the signal generator will output a NaI(Tl) signal; otherwise a CsI(Na) signal will be output. Then the energy spectrum is sampled by the multichannel analyzer, as shown in Fig. 8.

Furthermore, based on the rejection technique, the Compton scattering effect is added. The thought of the rejection technique is that we can reject the random numbers that we do not want to use and the rest of the random numbers are accepted.

The actual energy spectrum has two dimensions of information: the channel and the count number. We load the actual energy spectrum (detected X-ray in energy band 20–250 keV) into the RAM of the FPGA.

Then we generate two uncorrelated, equal-length random series, A (that stands for channel, value-range equals to maximum channel: 512) and B (which stands for counts, value-range equals to maximum counts), in the FPGA. To a given number $i$, we can get $A[i]$ and $B[i]$ from series A and B respectively. From the pre-loaded spectrum, we get the corresponding counts value $C$ at $A[i]$. If $B[i]$ is less than $C$, then $A[i]$ is sent to the DAC as the amplitude of the next pulse. In this way, the output has the same probability density distribution with the pre-loaded energy spectrum. As an example, Fig. 9 is an actual energy spectrum of $^{241}$Am radioactive source measured in NaI and CsI scintillation crystals and the spectrum in Fig. 10 is generated using our pulse generator and collected by the multichannel analyzer.

By Gaussian fitting for the total energy peak, the location of the total energy peak at 59.5 keV in Fig. 9 and Fig. 10 is 49.61, 49.61 and the $\sigma$ is $3.39\pm0.50$, $3.33\pm0.50$, respectively.

2.3 The negative exponential distribution of the intervals between two neighboring events

We compare the 16 bits equiprobability binary random number with the specific threshold $Y$ (we set up $Y=2000$) in FPGA. If the random number is smaller than $Y$, the result $z$ is assigned to ‘1’; otherwise, $z$ is ‘0’. Obviously, the probability of ‘1’ is $p=Y/2^{16}$ in one test. If the result of the $x$th test is ‘1’ and the results of the previous $(x-1)$ test are all ‘0’, then the probability is that:

$$f(x)=(1-p)^{(x-1)}p=\frac{p}{1-p}e^{\ln(1-p)}.$$  \hspace{0.5cm} (8)

Assigned a discrete stochastic variable $X$ with probability mass function, because $\ln(1-p)<0$, then $X$ contains a negative exponential distribution [2]. We output the signal if $z$ is ‘1’. Obviously, the time-interval of adjacent signals is a stochastic variable with a negative exponential distribution. We sample the output of the signal generator and finally get the fitting chart as shown in Fig. 11.
3 Discussion and conclusions

We developed a new type of signal generator to simulate the output of scintillator detectors' pre-amplifier. The shaping features (amplitude, rising-time, falling-time, etc.) of the signal from this generator can be adjusted easily to simulate detectors with different configurations.

By testing, the max counting rate of the signal generator is about 10000/s and the signal generator's output amplitude is from 0.05 V to 3.2 V. Its output impedance is 14 Ω and its quality is 60 g. Meanwhile, it has the low power about 0.35 W. Generating a simple cyclical signal, our signal generator (instead of the Agilent’s signal generator) is collected by the multichannel analyzer. We find that the most counting is in the same channel, the proportion of the neighboring channel's counting is less than 1%, so the generator’s stability is perfect.

To imitate the output of an actual scintillator detector’s pre-amplifier, it is usual to make the simulation signal take on a statistical distribution on time and amplitude synchronously [3]. However, it is hard to make the expected amplitude adjustable. In this paper, the rejection technique is discussed to add the Compton scattering effect. After the statistical test and performance parameter testing the output pulse, this generator truly imitates the output of an actual scintillator detector’s pre-amplifier. The amplitude and occurrence time are random, the amplitude spectrum is programmable and the occurrence time interval of adjacent signals contains a negative exponential distribution. In brief, the signal from this generator has almost the same behavior as a real detector’s pre-amplifier.

References

1. ZHANG Y F. Performance Study of the Hard X-ray Detector on HXMT (PhD thesis). Institute of High Energy Physics, 2011 (in Chinese)
2. YU Q L. Development of the TestSystem for HES of HXMT (Master thesis). Tsinghua University, 2010 (in Chinese)
3. WANG L J. Technical Development of Random Pulse Generator Simulated Nuclear Signal (Master thesis). University of South China, 2007 (in Chinese)
4. WANG SH G, ZHOU Z Y. X-ray Astronomy Physics. Beijing: Science Press, 1999 (in Chinese)
5. CHEN B X, ZHANG Z H. Nuclear Radiation Physics & Detection. Harbin: Harbin Institute of Technology Press, 2011 (in Chinese)
6. Bloser P F et al. arXiv: astro-ph/9910244
7. LIN ZH H. Modern Electronics Technique, 2009, 32(9): 49 (in Chinese)