Flexible polarimetric probe for $3 \times 3$ Mueller matrix measurements of biological tissue

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Polarimetry is a noninvasive method that uses polarised light to assess biophysical characteristics of tissues. A series of incident polarisation states illuminates a biological sample, and analysis of sample-altered polarisation states enables polarimetric tissue assessment. The resultant information can, for example, help quantitatively differentiate healthy from pathologic tissue. However, most bio-polarimetric assessments are performed using free-space optics with bulky optical components. Extension to flexible fibre-based systems is clinically desirable, but is challenging due to polarisation-altering properties of optical fibres. Here, we propose a flexible fibre-based polarimetric solution, and describe its design, fabrication, calibration, and initial feasibility demonstration in ex vivo tissue. The design is based on a flexible fibre bundle of six multimode optical fibres, each terminated with a distal polariser that ensures pre-determined output polarisation states. The resultant probe enables linear $3 \times 3$ Mueller matrix characterization of distal tissue. Potential in vivo Mueller matrix polarimetric tissue examinations in various directly-inaccessible body cavities are envisioned.

The use of polarised light to assess and quantify tissue biophysical properties noninvasively and without exogenous contrast agents is known as tissue polarimetry. Biological components (e.g., cells and their nuclei, collagen fibres, blood capillaries) alter the polarisation of incident light upon interaction, as specified by the geometry and inherent optical properties of these heterogeneous scattering structures$^1$. The most complete polarimetry description is the sample’s Mueller matrix, a 16-element ($4 \times 4$) polarimetric transfer function of the probed tissue. Useful biophysical quantities derived from this Mueller matrix, such as linear retardance (a measure of tissue anisotropy), can reveal precursors of malignant disease related to connective tissue and fibrillar protein morphology$^2$, while depolarisation contrast (a measure of tissue micro-organization) can help identify tumour margins in pre-clinical breast cancer models$^3$.

Bulky polarisation optics and lenses limit traditional free-space polarimetry to studies of ex vivo tissue, histology slides, or easily and directly accessible sites such as human skin. However, in vivo examination of various mucosal tissue linings where much pathology originates is paramount for early detection and surveillance in oncology and beyond (e.g., colon cancer$^4$, bladder cancer$^5$, and Barrett’s oesophagus$^6$). These important clinical sites are currently inaccessible to Mueller matrix examinations, because the flexible endoscopes necessary to reach and probe these sites contain optical fibres that greatly distort the polarisation information upon bending. Thus, the often small and subtle tissue polarimetric signature would be overwhelmed by system-delivery polarisation artefacts. Polarisation-maintaining fibres offer a possible way to guide polarised light, but these are specific to one polarisation and suffer from low single mode fibre numerical aperture, limiting the light collected back from tissue.

Several research groups are actively pursuing novel solutions to reduce such system artefacts and enable true distal tissue polarimetry. For example, Myakov et al. and Turzhitsky et al. have constructed flexible fibre-based probes, however they are only used for polarised reflectance spectroscopy$^7,8$, and are unable to extract the Mueller matrix of tissue necessary to yield its full polarisation signature. Vizet et al. have reported a flexible fibre-based probe capable of measuring basic polarisation properties$^9$, however the light collection efficiency is low as limited by single mode fibre acceptance angle (numerical aperture NA = 0.12), requiring sensitive detectors; further, the multi-wavelength use introduces the issue of different wavelength photons interacting within different tissue sampling volumes/depths. Their recent advance$^{10}$ uses a dual-wavelength approach where the polarisation effect

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of the fibre must be characterized at one wavelength and decoupled from the sample Mueller matrix measured at the other wavelength. Qi and Elson have made a polarisation-resolved endoscope capable of full wide-field 4 × 4 Mueller imaging\textsuperscript{11}, but their approach is limited to rigid, forward-viewing endoscopy. The rigidity provides certain inherent advantages such as technological simplicity, longer shelf life, low chromatic aberrations, and ease of manoeuvring. However, their utility is limited to relatively accessible clinical sites, so they are often not feasible for investigation of difficult-to-reach inner cavities such as the bladder, colon, airways, and upper gastrointestinal tract.

As flexible endoscopy is the clinical standard for examinations of internal body surface linings and cavities, the inherent and varying birefringence of flexible single- and multimode optical fibres must be overcome. This birefringence causes alterations in the polarisation of transmitted light that are often unpredictable and amplified by fibre bending. Here we propose an alternative, single-wavelength photonic design compatible with flexible probes using high light collection efficiency multimode optical fibres (fibre NA = 0.39) terminated with distal polarising elements. The distal location of the polarisers ensures that the light incident on the tissue has a user-defined, known polarisation state, and the polarisation analyser characteristics that detect tissue-reflected light are similarly known. The inevitable fibre artefact distortions still exist, but they now manifest as variations in incident light intensity instead of variations in polarisation, and can be accounted for with careful calibration, as described in section 2.3.

The described six-fibre probe is small enough to fit through and bend with the working channels of commercial flexible cystoscopes and colonoscopes (diameter ~3mm), to offer a potential polarimetric enhancement to such endoscopies. At present the probe implementation is limited to measuring a 9-element (3 × 3) Mueller matrix, as it uses linear polarisers only. It is possible to incorporate quarter wave plates (QWP) for circular polarisation measurements, and hence measure the full 4 × 4 16-element Mueller matrix. Here for proof of concept, linear polarisers were used exclusively.

In this paper we report on our linear Mueller probe design, fabrication, approach for data acquisition and calibration, and performance in probing known optical polarisation samples and ex vivo birefringent biological tissues.

Materials and Methods

Probe Design and Fabrication. The probe uses six multimode, 400-μm-diameter core fibres for light delivery or collection (Thorlabs M28L01, NA = 0.39, refractive index (RI) = 1.457 at 635 nm, cut in half and cleaved straight, leaving an SMA adapter on one end). A ~30 cm fibre length was employed for this particular probe embodiment; different fibre lengths can be used, e.g. several metres long to accommodate gastro-intestinal endoscopy, with similar negligible losses. To determine a 9-element Mueller matrix uniquely, at least 9 different measurements must be performed using all input/output combinations of 3 different linear polarisations\textsuperscript{12}. Since we do not illuminate and collect light through the same fibre simultaneously (for this proof-of-principle prototype only; the use of circulators will enable this in future probe versions\textsuperscript{13,14}) 2 fibres are needed per polarisation, hence 6 fibres were used.

The micron-scale polarisers (‘micro-polarisers’) were manufactured by cutting a linear polariser plate (Thorlabs LPVISB050, 2 mm thickness, RI = 1.52 at 635 nm, 10,000:1 extinction ratio) with an automatic dicing saw (Disco DAD3220, 100-μm thick diamond blade) into 500 μm × 500 μm squares (to adequately cover the whole fibre cross-section). The polariser was cut into squares with edges aligned with its transmission axis for easy orientation; circular cuts would have made it more difficult to keep track of the transmission axes, and more difficult to assemble with the desired orientations. A holder with square channels was 3D-printed (MED610 photopolymer material, Stratasys PolyJet printer) to house and maintain relative alignment of the micro-polarisers, which were placed in the 3D-printed holder, and then the cleaved ends of the optical fibres were attached. The fibres were glued to each micro-polariser using Norland #85 glue (RI = 1.46 in visible range) and cured with a UVB light source (Dymax). This glue had the lowest index of refraction to both the fibre and polariser so as to allow robust determination of the 3 × 3 linear Mueller matrix via 9 intensity-based measurements. These 9 measurements can be modelled by a Stokes vector formalism that describes the light polarisation by

Mathematical Description. The three orientations of the micro-polarisers used in the probe sufficiently span the linear polarisations (this is analogous to spanning the Poincaré sphere\textsuperscript{6,17} in 4 × 4 Mueller polariometry), allowing robust determination of the 3 × 3 linear Mueller matrix via 9 intensity-based measurements. These 9 measurements can be modelled by a Stokes vector formalism that describes the light polarisation by
where \( I \) is the overall intensity of the light (sum of any two orthogonal polarisation states), \( Q \) is the difference between the intensity of horizontally (0°) and vertically (90°) polarised light, \( U \) is the difference between the intensity of +45° and −45° polarised light, and \( V \) is the difference between the intensity of right (R) and left (L) circularly polarised light; note that we don’t pursue the \( V \) parameter in our current experimental demonstration of the linear Mueller matrix probe. Vectors and matrices are represented in bold. The tissue Mueller matrix \( M \) is calculated using

\[
S_{\text{INPUT}} = M \cdot S_{\text{OUTPUT}},
\]

where \( S_{\text{INPUT}} \) and \( S_{\text{OUTPUT}} \) are the input (pre-sample interaction) and output (post sample interaction) Stokes vectors. The Mueller matrix is the transfer function of the sample, representing its complete polarisation fingerprint. Once determined, intrinsic tissue biophysical polarisation properties such as retardance, diattenuation, and depolarisation can be obtained from it via polar decomposition18,19.

Here we use the following 9 probe measurements to determine the Mueller matrix of a sample: H1H2, H1V2, H1B1, V2H1, V2V1, V2B1, B1H1, B1V2, and B1B2, where the first letter and number indicates which channel is used to illuminate, and the second indicates which channel is used to collect. Note we do not perform the measurements in redundancy here to improve SNR (e.g. determine the HV data from H1V2, H1V1, H2V2, and H2V1 measurements) for mathematical simplicity in our proof-of-principle probe.

Following Eq. (2), for a sample that is interrogated by an arbitrary pair of excitation and collection channels, the resultant detected polarisation vector, \( S_{\text{OUTPUT}} \), is:

\[
S_{\text{OUTPUT}} = M \cdot S_{\text{INPUT}},
\]

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Following Eq. (2), for a sample that is interrogated by an arbitrary pair of excitation and collection channels, the resultant detected polarisation vector, \( S_{\text{OUTPUT}} \), is:

\[
S_{\text{OUTPUT}} = M_{\text{COLLECTION FIBRE}} \cdot M_{\text{MICRO--POLARISER}} \cdot M_{\text{SAMPLE}} \cdot S_{\text{INPUT}},
\]

where \( S_{\text{INPUT}} \) is the Stokes vector incident on the sample, and \( S_{\text{OUTPUT}} \) is the polarisation state exiting the proximal end of the collection fibre (whose intensity will be measured with a photodetector in our data acquisition scheme). As per Eq. (3), \( S_{\text{INPUT}} \) is transformed into \( S_{\text{OUTPUT}} \) by the product of the sample’s Mueller matrix, the Mueller matrix of the collection micro-polariser, and the Mueller matrix of the collection fibre.

The 9 intensity measurements of the sample are equivalent to the \( I_S \) (total intensity) Stokes parameters of each respective \( S_{\text{OUTPUT}} \): that is, we need only know the \( I \) Stokes parameter of the collected light in determining tissue
sample's Mueller matrix. Note that since the current probe's fibres are ~30 cm long, we assume the total intensity of collected light is conserved after traversing the distal micro-polariser, with negligible losses through the collection fibre. Therefore, we neglect the inconsequential effect of \( M_{\text{collection fibre}} \) on the total intensity of \( S_{\text{output}} \). Thus, Eq. (3) reduces to:

\[
I_{\text{output}} = \frac{1}{2} [p_{11} \quad p_{12} \quad p_{13}] \cdot M_{\text{sample}} \cdot S_{\text{input}}.
\]

where \( I_{\text{output}} \) is the total intensity of \( S_{\text{output}} \) at the proximal end of the collection fibre and \( \frac{1}{2}[p_{11} \quad p_{12} \quad p_{13}] \) is the first row of the Mueller matrix of the collection fibre's micro-polariser. The second and third row of \( M_{\text{micro-polariser}} \) do not contribute to the magnitude of \( I_{\text{output}} \).

For an ideal linear polariser, the first row elements of its Mueller matrix, \( [p_{11} \quad p_{12} \quad p_{13}] \) are equivalent to the normalized Stokes parameters, \( [I \quad Q \quad U] \), of light whose polarisation is parallel to the ideal polariser's transmission axis. Since we can't measure \( M_{\text{micro-polariser}} \) directly (i.e., the Stokes vectors of light that pass through the micro-polariser into the collection fibre are not accessible since they are altered by the polarisation properties of the fibre, before reaching a detector), we use the Stokes parameters of light emerging out the micro-polariser into free space and reverse the sign of the \( U \) parameter (the Stokes vector of light emanating out of, vs. after the micro-polariser, differ by \( 180^\circ - \theta \) in the reference frame of travelling light, thus corresponding to a sign change of \( U \)). Therefore we represent the first row of the micro-polariser's Mueller matrix by:

\[
\frac{1}{2} [p_{11} \quad p_{12} \quad p_{13}] = \frac{1}{2} [I \quad Q \quad -U],
\]

where \( U \) is what emerges from the micro-polariser, and \(-U\) is what would be collected.
For example, the $H_1H_2$ intensity measurement can be expressed as:

$$H_1H_2 = \frac{1}{2} \begin{bmatrix} I_{H12} & Q_{H12} & U_{H12} \end{bmatrix} \begin{bmatrix} m_{11} & m_{12} & m_{13} \\ m_{21} & m_{22} & m_{23} \\ m_{31} & m_{32} & m_{33} \end{bmatrix} \begin{bmatrix} I_{H11} \\ Q_{H11} \\ U_{H11} \end{bmatrix}$$

(6)

where $m_{ij}$ are the $i^{th}$-row and $j^{th}$-column elements of $M_{\text{Sample}}$ and the subscripts on $I$, $Q$, and $U$ denote which probe channel they are associated with. Multiplying and rearranging:

$$H_1H_2 = \frac{1}{2} \begin{bmatrix} I_{H12} & Q_{H12} & U_{H12} \end{bmatrix} \begin{bmatrix} I_{H11} \\ Q_{H11} \\ U_{H11} \end{bmatrix} = \begin{bmatrix} I_{H11} & Q_{H11} & U_{H11} \end{bmatrix} \begin{bmatrix} m_{11} \\ m_{12} \\ m_{13} \end{bmatrix}$$

(7)

The $H_1H_2$ measurement makes up 1 out of 9 intensity measurements required to determine the linear $3 \times 3$ Mueller matrix of a sample. A similar equation can also be written for each of the 8 remaining intensity measurements ($H_1V_2$, $H_1B_1$, $V_2H_1$, etc.). Together, these 9 equations allow a unique solution for the Mueller matrix. Due to the slow manual switching of fibres with the current probe, these 9 measurements take approximately 5 minutes to perform. Grouping these equations together, the following expression is derived:

$$\begin{bmatrix} H_1H_2 \\ H_1V_2 \\ H_1B_1 \\ V_2H_1 \\ V_2V_2 \\ V_2B_2 \\ B_1H_1 \\ B_1V_2 \\ B_1B_2 \end{bmatrix} = \frac{1}{2} \begin{bmatrix} I_{H12} & I_{H11} & I_{H11} & Q_{H12} & Q_{H11} & Q_{H11} & U_{H12} & U_{H11} & U_{H11} & -U_{H12} & -U_{H11} & -U_{H12} & -U_{H11} \\ I_{V12} & I_{V11} & I_{V11} & Q_{V12} & Q_{V11} & Q_{V11} & U_{V12} & U_{V11} & U_{V11} & -U_{V12} & -U_{V11} & -U_{V12} & -U_{V11} \\ I_{B12} & I_{B11} & I_{B11} & Q_{B12} & Q_{B11} & Q_{B11} & U_{B12} & U_{B11} & U_{B11} & -U_{B12} & -U_{B11} & -U_{B12} & -U_{B11} \\ I_{V12} & I_{V11} & I_{V11} & Q_{V12} & Q_{V11} & Q_{V11} & U_{V12} & U_{V11} & U_{V11} & -U_{V12} & -U_{V11} & -U_{V12} & -U_{V11} \\ I_{B12} & I_{B11} & I_{B11} & Q_{B12} & Q_{B11} & Q_{B11} & U_{B12} & U_{B11} & U_{B11} & -U_{B12} & -U_{B11} & -U_{B12} & -U_{B11} \\ I_{V12} & I_{V11} & I_{V11} & Q_{V12} & Q_{V11} & Q_{V11} & U_{V12} & U_{V11} & U_{V11} & -U_{V12} & -U_{V11} & -U_{V12} & -U_{V11} \\ I_{B12} & I_{B11} & I_{B11} & Q_{B12} & Q_{B11} & Q_{B11} & U_{B12} & U_{B11} & U_{B11} & -U_{B12} & -U_{B11} & -U_{B12} & -U_{B11} \end{bmatrix} \begin{bmatrix} m_{11} \\ m_{12} \\ m_{13} \\ m_{21} \\ m_{22} \\ m_{23} \\ m_{31} \\ m_{32} \\ m_{33} \end{bmatrix}$$

(8)

where the abbreviated matrix above (we refer to this matrix of measured Stokes parameters as the system matrix ‘Z’) in its full form is:

$$Z = \begin{bmatrix} I_{H21} & I_{H12} & I_{H12} & I_{H11} & I_{H11} & I_{H11} & I_{H11} & I_{H11} & I_{H11} & I_{H11} & I_{H11} & I_{H11} \\ I_{V21} & I_{V12} & I_{V12} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} \\ I_{B21} & I_{B12} & I_{B12} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} \\ I_{V21} & I_{V12} & I_{V12} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} \\ I_{B21} & I_{B12} & I_{B12} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} & I_{B11} \\ I_{V21} & I_{V12} & I_{V12} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} & I_{V11} \end{bmatrix}$$

(9)

This system matrix can be determined by measuring the normalized Stokes vectors of light emanating from each channel. This probe characterization step needs only to be done once (after manufacturing of the probe, before the calibration described later); the normalized Stokes vectors of light exiting each channel will not change with fibre bending. For improved accuracy, we do not assume cardinal angle orientations (−45, 0, and 90 degrees) of the micro-polarisers, but rather measure these independently (Thorlabs PAX5710VIS-T free-space polarimeter, ±0.25° orientation accuracy).

Thus, by measuring these Stokes parameters to construct the system matrix, and using the probe to measure the 9 intensities after interaction with an unknown (tissue) sample, all nine elements of the sample’s $3 \times 3$ Mueller matrix can be determined through inversion of Eq. (8):
Eq. (10) is valid if the 6 probe channels all couple light equally (both inter- and intra-channel). Since this is likely not the case in practice, we must calibrate the probe. Our calibration procedure (see below) generates 9 coefficients ($c_1, c_2, \ldots, c_9$) that scale each of the 9 experimental sample intensity measurements to account for coupling differences. This turns Eq. (10) into:

$$
\begin{bmatrix}
  m_{11} \\
  m_{12} \\
  m_{13} \\
  m_{21} \\
  m_{22} \\
  m_{23} \\
  m_{31} \\
  m_{32} \\
  m_{33}
\end{bmatrix}
= 2 \cdot Z^{-1} \cdot
\begin{bmatrix}
  H_{1}H_{2} \\
  H_{1}V_{2} \\
  H_{1}B_{1} \\
  V_{1}H_{1} \\
  V_{1}V_{1} \\
  V_{1}B_{1} \\
  B_{1}H_{1} \\
  B_{1}V_{1} \\
  B_{1}B_{1}
\end{bmatrix}
$$

(10)

The coefficients $c_i$ take into account the factors of fibre coupling efficiency, inter-channel geometry (see Fig. 2), and possible slight internal reflections at glued interfaces induced by refractive index mismatches. For instance, consider the case of the probe set up directly facing a mirror. For this case $H_1H_2$ and $V_1V_2$ should give identical results. If the intensity of the $H_1H_2$ measurement was measured to be ¾ of that of the $V_1V_2$ measurement, then the calibration coefficient for $H_1H_2$ would be ~ 4/3 that of the coefficient for $V_1V_2$. Further, the intensity of light that emerges from each fibre will vary depending on its micro-polariser orientation and if/how the fibre is bent. For example, despite our efforts to depolarise the laser source before coupling into the probe fibres, the light was still partially polarised (degree of polarisation (DOP) = ~15%); thus the orientation of this small DOP with respect to the micro-polarisers will influence the intensity of light emerging from each channel. The calibration procedure to determine the $c_i$ coefficients is thus necessary, as these various sample-independent experimental factors can affect the detected light intensity and thus distort the determined tissue Mueller matrix results.

**Calibration Procedure.** For probe calibration, the linear Stokes vectors ($[I \ Q \ U]$) exiting out of the distal end of each channel were measured with an external Thorlabs polarimeter, to determine the system matrix $Z$ in Eq. (9). Then a 2-inch-diameter linear polariser oriented horizontally ($\theta = 0^\circ$) followed by a front-surface-coated mirror were placed perpendicularly to the probe end, as depicted in Fig. 3. The 635 nm laser was coupled to the $H_1$ fibre, thus passing through the $H_1$ micro-polariser and the external horizontal polariser, reflecting off the mirror, traversing through the external horizontal polariser again, and entering the $H_2$ channel where its intensity was...
Table 1. Top row: (1) Probe vs. independently measured Mueller matrix of a 45° linear polariser double pass. See Fig. 4 for graphical representation. Bottom row: (2) Probe vs. independently measured Mueller matrix of QWP double pass whose fast axis was oriented at 45°. See Fig. 5 for graphical representation. The errors are the standard deviation from 3 independent measurements. In between each of the 3 measurements, the sample was repositioned and the probe was recalibrated.

|                  | Independent check with free-space polarimetry |
|------------------|-----------------------------------------------|
| (1) M of 45° linear polariser double pass (probe) | (2) M of 45° quarter wave plate double pass (probe) |
|                  | 0.50 ± 0.00 -0.02 ± 0.02 0.49 ± 0.00 | 0.50 ± 0.00 -0.01 ± 0.00 0.49 ± 0.00 |
|                  | -0.02 ± 0.01 0.01 ± 0.01 -0.01 ± 0.01 | -0.01 ± 0.01 0.00 ± 0.00 -0.01 ± 0.01 |
|                  | -0.51 ± 0.02 -0.01 ± 0.04 -0.51 ± 0.02 | -0.50 ± 0.01 0.01 ± 0.00 -0.49 ± 0.00 |

Note that all probe fibres were kept immobile during all measurements, as only the laser input and detector connections were switched at the proximal end of the probe.

For these calibration measurements, the “sample Mueller matrix” \( M_{\text{SAMPLE}} \) was known to be that of polariser double-pass (at its three different examined angles 0°, 30°, 60°), specifically:

\[
M_{\text{SAMPLE}} = M_{\text{POLARISER AT 180° - \theta}} \cdot M_{\text{MIRROR}} \cdot M_{\text{POLARISER AT \theta}}
\]  

(12)

Note that on the second pass through the polariser, its orientation angle becomes 180° − θ. This is due to the change in reference frame that occurs when light switches direction upon reflection at the mirror. \( M_{\text{POLARISER AT \theta}} \) and \( M_{\text{POLARISER AT 180° - \theta}} \) were measured independently with a free-space Thorlabs polarimeter, and the mirror was assumed to be described by:

\[
M_{\text{MIRROR}} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{bmatrix}
\]  

(13)

We then solved for the \( c_1\)–\( c_9 \) coefficients via ‘best fit’ nonlinear regression, by numerically minimizing the mean absolute difference between the elements of the normalized Mueller matrix as measured by the probe (using Eq. (11)), and the ‘true’ \( M \) of the polariser-mirror-polariser system (Eq. (12)). The resultant calibration “\( c \)” coefficients that scale the \( H_1H_1 \), \( H_1V_2 \), \( H_1B_2 \), \( V_2H_1 \), \( V_2V_1 \), \( V_2B_1 \), \( B_1H_1 \), \( B_1V_2 \), and \( B_1B_2 \) measurements are: 1.18, 0.83, 0.74, 0.70, 1.21, 1.51, 1.24, 1.17, and 1.42. The standard deviation of the coefficients about the mean value (1.1 ± 0.3) represents the various probe manufacturing imperfections, as well as the partially polarised nature of the light emanating from the laser that seeds the system. Note that these non-ideal numbers represent the first probe prototype (and are adequately dealt with by the calibration procedure); subsequent probe implementation and the use of an unpolarised light source will likely make these coefficients approach unity. This may even potentially obviate the need for such extensive calibration altogether.

This completes the probe calibration. We now proceed with measurements of unknown samples in order of increasing complexity: (1) linear polariser double pass, at a 0°-orientation different from the three calibration angles, (2) QWP double pass, and (3) biological tissue in reflection mode, in its native and stretched (birefringence-modulated) state.

Data Availability Statement. The data generated and analysed during the current study are available from the corresponding author upon reasonable request.

Results and Discussion. The probe was first used to determine the Mueller matrix of a linear polariser double pass, oriented at \( \theta = 45° \) using the same set-up as depicted in Fig. 3. Again, the ‘true’ Mueller matrix was determined with free-space Thorlabs polarimeter measurements and ideal \( M_{\text{MIRROR}} \) (Eq. (13)) using Eq. (12). Three measurements were made using both the fibre probe and the free-space system. The results are summarized numerically in Table 1, and graphically in Fig. 4. Agreement is seen for all nine \( M \) elements with no statistically significant differences between probe and free-space matrix elements (p > 0.05 for all 2 sample, unpaired, 2-sided t-tests performed for each element).

Notably, the average of both free-space and probe Mueller matrix measurements of the 45° polariser double pass agree well with the theoretical matrix elements, with very small deviations. While the probe performance and accuracy are thus very encouraging, this represents the least-complex test case, in that the examined sample
was not very different from those used for calibration: a linear polariser but at a new, unknown angle. We now move on to the slightly more challenging test of measuring $M$ of a new polarising optical element altogether (while still retaining the calibration measurement geometry of Fig. 3).

(2) Next the probe was used to measure the Mueller matrix of a QWP double pass, oriented at ~45°. The results are shown in Table 1 and graphically in Fig. 5.

The theoretical Mueller matrix of a QWP double pass with fast axis at 45° and linear retardance $\delta = 0.27\lambda$ is:

$$M_{QWP \, DOUBLE \, PASS} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & -0.97 & 0 \\ 0 & 0 & -1 \end{bmatrix}. \quad (14)$$

For a QWP, elements $m_{22}, m_{23}, m_{32}$, and $m_{33}$, are all sensitive to fast axis alignment 0 and retardance $\delta$. Thus, these may be affected by the difference in effective retardances, due to the probe’s high NA fibres. Additionally, sensitivity to fast axis orientation angle means any small experimental (~1°) difference in $\theta$ will influence results; both of these dependencies may be responsible for the slight inter-results variation and statistical differences between probe and free-space values of these elements.

Further, elements $m_{12}, m_{13}, m_{21}, m_{31}$ (first row and column) should all theoretically be zero; both sets of measurements are, but with small deviations. These may be due to small diattenuation of the QWP. The fact that slightly non-zero elements are observed in both the probe and free-space measurements supports this hypothesis. Antireflection coating on the QWP may lessen this effect in the future.

The measured $m_{33}$ elements are slightly less than -1 for both systems. The source of this slight discrepancy is currently being investigated, and could be caused by small laser power or polarisation fluctuations during the measurement procedure, coupled with set-up errors inherent in manual fibre switching in this prototype data acquisition procedure. We are currently adapting a $4 \times 4$ Mueller matrix filtering technique to the $3 \times 3$ probe methodology to minimize these small deviations.

Looking at Figs 4 and 5, we see that the accuracy of the 45° QWP (Fig. 5) is very good, but not at the level of the 45° polariser (Fig. 4). As the QWP is more temperature and path length-sensitive than the polariser, the difference in accuracy is somewhat anticipated. Nevertheless, since no wave plates were used in the probe calibration,
As such, we report the physical tissue retardance $\delta$ between necrotic and viable breast cancer, normal bladder outlet and partial bladder outlet obstruction, and properties such as those present between healthy and pathological tissue (e.g., retardance contrasts in vivo). Thus, the probe’s ability to detect and quantify potentially important changes in tissue polarisation properties is promising and further suggests the validity of our methodology.

(3) Finally the probe was used on a more intrinsically complex biological sample of chicken breast tissue, to determine its Mueller matrix before and after it was stretched along the direction of its muscle striations. Mechanical stretching induces increased tissue anisotropy (an increase in optical birefringence), for example as shown by Alali et al. in ex vivo distended rat bladders. The tissue was fixed in 4% paraformaldehyde for 24 hours, changing its polarisation properties slightly, but enabling much easier tissue handling, stretching, and measurement. The ~2 mm thick fixed chicken breast slice was clamped to a home-built stretching device and positioned at the location of the mirror (Fig. 3) to approximate the calibration conditions; in real clinical scenarios, much smaller calibration and measurement working distances are envisioned. Following its Mueller matrix measurements, the tissue was stretched by ~20% along its muscle fibre direction, repositioned in the probe polarimeter setup, and re-measured. This was repeated on three additional chicken breast tissue samples.

The results are displayed in Table 2. The Mueller matrices were decomposed to determine the chicken breast’s linear retardance magnitude before and after the axial stretch (20% strain). Since reflected light undergoes a helicity flip, the measured Mueller matrix will contain effects of both the true physical retardance, as well as a geometrical retardance arising from the directional change in light propagation. This effect has been studied in non-depolarising media. In the case of a wave plate of arbitrary retardance with its fast or slow axis oriented vertically (similar to this stretched tissue scenario), the physical retardance, $\delta_{\text{phys}}$, is equal to $180^\circ - \delta_{\text{meas}}$ where $\delta_{\text{meas}}$ is the measured retardance. (For example, the physical retardance of an ideal 30° retarder double pass should be $\delta_{\text{phys}} = 2 \times 30^\circ = 60^\circ$. However, $\delta_{\text{meas}} = 120^\circ$. Thus $\delta_{\text{phys}}$ is found by $180^\circ - \delta_{\text{meas}} = 60^\circ$. The same trend occurs for all retarders with fast or slow axis oriented vertically.) As such, we report the physical tissue retardance as $180^\circ - \delta_{\text{meas}}$.

As seen below, the resultant mean linear retardance due to strain increases by ~15% (from 103° to 120°) for the four chicken breast tissue samples. At a given wavelength, retardance is proportional to the product of sample thickness and its birefringence; the samples naturally become slightly thinner with stretching, and their birefringence increases as well. These two mechanisms can have opposite effects on retardance when measured in transmission geometry, and can in fact be decoupled (for example by an independent thickness measurement). For in vivo applications, likely in retro-reflection geometry, sampled tissue thickness cannot be directly measured. In this case, we can either utilize polarisation-sensitive Monte Carlo simulations to estimate the polarisation sampling volumes (which yields the mean pathlength and thickness estimate) or compare relative values of different linear retardance measurements (without decoupling the separate birefringence or thickness contributions). Other groups have reported birefringence increases between normal and stretched chicken breast tissue, but the quantification of the specific dependence of birefringence on strain (~20% in this case) is unknown, likely varies for different tissue types, and makes quantitative comparisons difficult. But certainly the probe-measured trend of increasing tissue asymmetry upon stretching (as reported by birefringence and/or retardance) makes sense. Thus, the probe’s ability to detect and quantify potentially important changes in tissue polarisation properties such as those present between healthy and pathological/pathological tissue (e.g., retardance contrasts between necrotic and viable breast cancer, normal bladder outlet and partial bladder outlet obstruction, and cervical cancer) is encouraging.

Another interesting metric that naturally emerges from the Mueller matrix decomposition is tissue depolarisation (last row of Table 2). This is also seen to increase upon stretching, although more measurements are needed to properly test statistical significance. Similar findings of higher depolarisation in more birefringent tissue have been observed by Alali et al. where despite having the same transport albedo as porcine kidney cortex, the depolarisation of porcine myocardium muscle was ~25% higher when measured in a free-space backscattering geometry. As in the retardance/birefringence discussion above, the slight tissue thickness decrease upon stretching is again a confounder that would likely contribute to decreased depolarisation; it appears that for these samples, the increased birefringence may have played a larger role in the resultant depolarisation trend.

To further explore these results graphically, we display one tissue sample’s representative Mueller matrices (as in Table 2) via colour maps, and show their difference. Figure 6 shows that upon stretching, most elements slightly decrease in value except a slight increase in $m_{12}$ ($m_{11}$ naturally stays fixed because of normalization). The four lower left elements decrease more than the three upper righthand elements, but the $m_{13}$ element decreases in magnitude the most (~60%). Such large relative decrease in $m_{13}$ magnitude has also been observed in controlled birefringent polyacrylamide phantoms upon stretching.
As evidenced by the presented results, the flexible probe design enables accurate Mueller matrix measurements of an ideal linear polariser and of an ideal retarder (quarter-wave plate). In Mueller matrix polarimetry of birefringent chicken breast, the probe detects an expected increase in strain-induced optical anisotropy between the normal and stretched tissue states. Encouraged by our demonstrated ability to detect and quantify changes in ex vivo tissue, we are currently progressing to in vivo studies to distinguish between healthy and pathologic (or pre-pathologic) tissue regions that likely exhibit birefringence and depolarisation contrasts.

**Engineering Design Considerations and Biological Context.** Having successfully demonstrated proof-of-concept of the flexible polarimetric methodology, there are several areas of performance improvements to consider for its next prototype. Further, a practical and robust calibration procedure suitable for in situ implementation must be developed. The improvements include (1) using an opaque component holder material: in the presented probe, MED610 was used which is a readily available, translucent, and biocompatible 3D printing material. However, its translucency may have permitted some cross talk between the probe channels, so an optically opaque material will be used in the next prototype. (2) Improving resolution via tip sculpting optics: the distal tip of the probe could be enhanced using fibre bevelling or attaching ball lenses that can steer the illumination and collection apertures toward each other, as such, optimizing the interplay between resolution, working distance, overlap sampling volume, and light collection efficiency. Making use of the central channel will also be helpful in this regard. (3) Incorporating optical circulators: these will enable illumination and collection of light through the same channel, which increases overlapping sampling volumes while also reducing the needed number of fibre channels, total probe diameter, variance in illumination intensity, and acquisition time. (4) The next probe prototype will have QWPs, enabling full 4 × 4 Mueller matrix determination. Obtaining such a complete polarisation signature of the sample is important since the additional elliptical/circular polarisation information can reveal even more significant biophysics, for example as related to the detection of chiral glucose molecules. Glucose monitoring is impossible with a 3 × 3 approach but may be possible via 4 × 4 Mueller polarimetry. Further, the complete Mueller matrix determination will also improve the accuracy of the linear polarisation metrics over the partial 3 × 3 formalism, as well as furnish an unambiguous birefringence orientation value (e.g., a 0° QWP and a 90° QWP have the same 3 × 3 Mueller matrix). The probe would require 2 additional fibres (if no optical circulators were used) to illuminate and collect circularly polarised light, each equipped with distal polariser and QWP; with circulators, the minimum number of fibres required would be reduced to 4. Finally, (5) a depolarised light source will be used in place of the current partially polarised diode laser, to minimize the resultant inter-channel intensity modulation effects. In practice for in situ calibration, partial reflectors or a small, switchable mirror (liquid crystal or mechanical) will be mounted at the distal end of the probe. First the probe will be guided to the region of interest via conventional white-light endoscopy. Then for the active opto-electronic control embodiment, the crystal will switch electronically to reflective mode (or mechanically move into the beam path), intensity measurements will be made to generate calibration coefficients, then the crystal will revert to transparency mode (or mechanically move out of the beam path), and the 9 (or 16 for the full 4 × 4 prototype) tissue intensity measurements will be made. In situ calibration must be performed rapidly prior to tissue measurements, to avoid probe and tissue motion artefacts. Programmable optoelectronics and the proposed use of circulators will reduce the requisite acquisition time to milliseconds-seconds range. The engineering details and measurement protocols of this implementation are currently being investigated. High-heat autoclaves will be avoided in favour of chemical disinfection between uses, to preserve the integrity of the distal optics, and possibly opto-electronics.

We envision the probe to be used as a flexible, polarisation-resolved add-on to human endoscopes, with access through the latter’s working/biopsy channels. For example, one application we are currently pursuing is polarisation cystoscopy in urology, with the intent to aid in the treatment guidance of partial bladder outlet obstruction (pBOO). Upon obstruction in rats, Alali et al. found that there were significant regional changes in optical...
anisotropy (birefringence) of the bladder wall, particularly the ventral region close to the urethra. The probe could be used to pinpoint such local regions of high linear retardance changes and optimize surgical procedures (bladder augmentation) in pBOO on an individual patient basis, a vast improvement when compared to the current practice that treats the upper (dome) region of the bladder exclusively.

Another unmet urological need calls for improved detection of early stage bladder cancer, as the current standards of white light cystoscopy, narrow-band imaging, and photodynamic diagnosis ("blue light" cystoscopy) have a high false positive rate. Changes in the bladder extracellular matrix have been successfully detected with polarised light in ex vivo rat studies of pBOO; it is thus likely that in vivo flexible cystoscopic probe polarimetry may help detect pre-cancerous remodelling of the extracellular matrix in humans. Other applications for flexible polarisation endoscopy include probing the uterine cervix and colon for detection of precancerous sites, and liver for improved liver fibrosis diagnosis.

Conclusion

We have demonstrated a flexible, 6-fibre probe with distal micro-polarisers capable of accurate 3 × 3 linear Mueller matrix measurement of polarisation components (polarisers, wave plates) and of birefringent biological tissues. We described the probe manufacturing, its calibration and sample data acquisition procedures, and initial performance characterization in controlled polarisation-optics samples and in ex vivo biological tissues. Several areas of improving the proposed flexible polarimetric methodology have been outlined. Overall, the demonstrated ability to accurately determine the 3 × 3 Mueller matrix of biological tissues via a flexible fibre optic probe bodes well for eventual full polarimetric examinations of difficult-to-reach clinical body sites and tissues.

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Author Contributions
S.A., A.A.L., and A.V. formulated the initial concept of the polarimetric probe. S.F. and A.G. updated the design and constructed the probe prototype. S.F., A.G., and A.V. contributed to the experimental design and interpretation of the data. S.F. performed the experiments, generated the figures, and wrote the manuscript. A.G. and A.V. edited the manuscript. All authors reviewed and commented on the manuscript prior to submission.

Additional Information
Competing Interests: The authors declare that they have no competing interests.

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