THE OUTER DISKS OF DWARF IRREGULAR GALAXIES

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Received 2011 March 7; accepted 2011 July 25; published 2011 September 13

ABSTRACT

In order to explore the properties of extreme outer stellar disks, we obtained ultra-deep V and GALEX ultraviolet (UV) images of four dwarf irregular galaxies and one blue compact dwarf galaxy, and ultra-deep B images of three of these. Our V-band surface photometry extends to 29.5 mag arcsec$^{-2}$. We convert the FUV and V-band photometry, along with H$\alpha$ photometry obtained in a larger survey, into radial star formation rate profiles that are sensitive to timescales from 10 Myr to the lifetime of the galaxy. We also obtained H$\alpha$-line emission data and compare the stellar distributions, surface brightness profiles, and star formation rate profiles to H$\alpha$-line emission maps, gas surface density profiles, and gas kinematics. Our data lead us to two general observations. First, the exponential disks in these irregular galaxies are extraordinarily regular. We observe that the stellar disks continue to decline exponentially as far as our measurements extend. In spite of lumpiness in the distribution of young stars and H$\alpha$ distributions and kinematics that have significant unordered motions, sporadic processes that have built the disks—star formation, radial movement of stars, and perhaps even perturbations from the outside—have, nevertheless, conspired to produce standard disk profiles. Second, there is a remarkable continuity of star formation throughout these disks over time. In four out of five of our galaxies the star formation rate in the outer disk measured from the FUV tracks that determined from the V-band, to within factors of five, requiring star formation at a fairly steady rate over the galaxy’s lifetime. Yet, the H$\alpha$ surface density profiles generally decline with radius more shallowly than the stellar light, and the gas is marginally gravitationally stable against collapse into clouds. Outer stellar disks are challenging our concepts of star formation and disk growth and provide a critical environment in which to understand processes that mold galaxy disks.

Key words: galaxies: individual (DDO 53, DDO 86, DDO 133, NGC 4163, IZw 115) – galaxies: irregular – galaxies: star formation – galaxies: structure

Online-only material: color figures

1. INTRODUCTION

Outer parts of galaxy disks present an extreme environment for star formation. Dwarf irregular (dI) galaxies already challenge models of star formation because of their low gas densities even in the central regions (Hunter & Plummer 1996; Meurer et al. 1996; van Zee et al. 1997; Hunter et al. 1998). Outer parts of dI galaxies with their exceptionally low gas densities, therefore, present a particularly difficult test of our understanding of the cloud/star formation process. Furthermore, knowledge of the star formation histories of outer stellar disks provides information on the way in which the disk has grown with time and tests current models for disk growth (see, for example, Azzollini et al. 2008).

Stars have formed even to very low disk surface brightness levels. For example, Saha et al. (2010) have detected an exponential stellar disk in the Large Magellanic Cloud (LMC) that extends to 12 disk scale lengths, the equivalent of an I-band surface brightness of 34 mag arcsec$^{-2}$. Although the number of young stars relative to older stars declines with radius, stars as young as a few Gyr are found to about 8.3 disk scale lengths. In the late-type spiral M33, Barker et al. (2011) have found stars younger than 0.5 Gyr at four and five disk scale lengths, although the bulk of the stars are older. And in M31, Richardson et al. (2008) find evidence for star formation over the past 0.25–2 Gyr as far out as 56 kpc. Furthermore, satellite ultraviolet (UV) imaging has revealed extended UV disks in many spiral galaxies that indicate ongoing star formation in outer disks (Thilker et al. 2007). For example, GALEX images of M83 revealed UV-bright stellar complexes to 7 kpc, about four times the radius at which most of the H$\alpha$ regions were detected (Thilker et al. 2005).

Given the importance of outer stellar disks to our understanding of galaxy formation and evolution, we have conducted a program to detect and measure the extreme outer stellar disks of a sample of dI galaxies through ultra-deep imaging in the optical and UV. In addition, we have mapped the galaxies in H$\alpha$-line emission. We use these data to examine the structure,
stellar populations, and star formation activity in extreme outer dIm disks.

Our program objects were selected from a large survey of dIm, blue compact dwarf (BCD), and Sm galaxies (Hunter & Elmegreen 2006). They were chosen to be representative of the larger dIm sample in terms of absolute magnitude. They were also chosen to be relatively free of nearby bright stars that would compromise photometry at ultra-low light levels. The new deep imaging data will be referred to here as the “deep” data, while the shallower survey data of the larger sample will be referred to as the “survey” data. The galaxies and several important characteristics are listed in Table 1.

2. OBSERVATIONS

2.1. Optical Images

2.1.1. Data Acquisition and Basic Reductions

The deep optical imaging observations are summarized in Table 2 and V-band and Hα images are shown in Figures 1–5. The Hα images are part of the survey data (Hunter & Elmegreen 2004). Reductions were done using the Image Reduction and Analysis Facility (IRAF11).

In 2002 May, we obtained deep B and V images of DDO 133 and V images of IZw 115 with the Mosaic Imager on the Kitt Peak National Observatory (KPNO) 4 m Mayall telescope. The Mosaic Imager consists of eight 2k × 4k SITe CCDs and gives a single final image in each filter. The Mosaic Imager was calibrated using field images and Landolt (1992) standard stars observed with the Lowell Observatory 1.1 m telescope. Because IZw 115 was not observed in B, a (B − V)0 of 0.4 was assumed to calibrate instrumental V magnitudes. Uncertainties in the calibration are given in Table 2.

11 IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under cooperative agreement with the National Science Foundation.

Table 1
Galaxy Sample

| Galaxy  | Other Namesa | Typeb | Dc | E (B − V) f, | log SFRg  |
|---------|--------------|-------|----|-------------|----------|
| DDO 53  | PGC 24050, UGC 4459, A0829+66, VIIZw238 | Im    | 3.6 | 0.03        | −2.50    |
| DDO 86  | PGC 32048, UGC 5846, A1041+60, Mailyan 057 | Im    | 16.9 | 0.00        | −2.74    |
| DDO 133 | PGC 41636, UGC 7698, A1230+31          | Im    | 6.1  | 0.00        | −2.93    |
| NGC 4163| PGC 38881, UGC 7199, KUG 1209+364      | Im    | 2.8  | 0.00        | −2.43    |
| IZw 115 | PGC 55381, UGC 9893, VV 720, A1531+46, KIG 686 | BCD   | 12.3 | 0.01        | −2.87    |

Notes.

a Selected alternate identifications obtained from NED.
b Morphological Hubble types are from de Vaucouleurs et al. (1991). If no type is given there, we have used types given by NED.
c Photometric calibration rms for the filters listed in Column 4.
d FWHM of a stellar profile on the final combined image.

e Integrated star formation rate derived from the Hα luminosity, divided by πR2D, where R_D is the disk scale length determined from the inner V-band surface brightness profile from Hunter & Elmegreen (2004).

Table 2
Optical Observations and Photometry Parameters

| Galaxy  | Date (mmyy) | Tel. | Filters | Exposures | Seeing | Scale Calib | P.A. | b/a | Step | Center (J2000) |
|---------|-------------|------|---------|-----------|--------|-------------|------|-----|------|---------------|
| DDO 53  | 0104        | 2.1m | V       | 34 × 1200 | 1.4    | 0.30        | 81.0 | 0.56| 15.2 | 08 34 08.1   |
| DDO 86  | 0304        | 2.1m | B       | 25 × 1800 | 1.6    | 0.30        | −46.0| 0.86| 10.6 | 10 44 30.2   |
| DDO 133 | 0502        | 4m   | B       | 5 × 1000  | 1.5    | 0.27        | −2.0 | 0.69| 10.0 | 12 32 55.6   |
| NGC 4163| 0207        | 2.1m | V       | 10 × 900  | 1.4    | 0.27        | 15.0 | 0.67| 11.2 | 12 12 09.0   |
| IZw 115 | 0507        | 2.1m | B       | 12 × 1800 | 1.4    | 0.30        | 40.7 | 0.47| 10.0 | 15 32 57.1   |

Notes.

a Kitt Peak National Observatory telescope used for the observations.
b FWHM of a stellar profile on the final combined image.
c Photometric calibration r.m.s for the filters listed in Column 4.
d Position angle P.A., minor-to-major axis ratio b/a, ellipse semi-major axis step size, and position of center used to do photometry in concentric ellipses.
We obtained optical images of DDO 53, DDO 86, and NGC 4163 with the Cassegrain Focus Imager on the KPNO 2.1 m telescope. The T2KA CCD was used for V observations of DDO 53 and DDO 86, and T2KB was used for observations of DDO 53 in B and of NGC 4163 in V and B. The 2048 × 2048 pixel format yields a 10.′4 field of view. Landolt (1992) standard stars were also observed for photometric calibration, and the rms of the calibrations is given in Table 2. We used observations of an illuminated white spot hanging in the dome (dome flats) to remove pixel-to-pixel variations, and dark sky flats to remove large-scale structure across the CCD.

Our experience has been that the best method for flat-fielding varies from telescope to telescope. Discussion of this point can be found in Massey & Jacoby (1992). In some cases, such as at the KPNO 4 m, bright twilight flats can be used to remove both the pixel-to-pixel variations and the large-scale gradients. But in other cases, such as the KPNO 2.1 m, twilight flats do not work well and blank-sky flats work best. Therefore, for the KPNO 2.1 m data, we constructed a dark sky flat for each observing run. We obtained multiple images with the same exposure time and moon conditions as the galaxy observations. “Blank sky” targets were used, but there were still many stars in the images. The telescope was stepped between exposures and the series of images was co-added with an algorithm that removed the stars by comparing the images pixel-by-pixel and rejecting pixels that deviated more than 3σ from the median, where the σ is determined from the noise and gain parameters of the CCD. Because the sky flats showed no structure changes from night to night, a single sky flat was constructed for an entire observing run. The resulting sky flat was smoothed. We normalized the sky flat to a mean value of one near the center, and divided the object images by this sky flat.

In the case of the V-band image of DDO 53, however, we discovered after the observing run that the “blank sky” was contaminated by Milky Way nebular structure (4h29m45s, 54°15′33″[J2000]). The Milky Way emission produced diffuse filamentary structure across the field of view and so could not be used to construct a dark sky flat. On the other hand, the galaxy itself was small and contained in the center of the field of view; even at low light levels the galaxy occupied only 14% of the pixels of the image. Therefore, for this galaxy/filter only, we used the galaxy images themselves to construct a dark-sky flat: we combined the images to produce a single star-free average and fit the non-galaxy portion of the image with an order five Legendre function, interpolating across the area of the image containing galaxy. The galaxy-free region was defined by looking at the extent of the galaxy with the image displayed to see faint noise variations in the background.

We observed the galaxies only at relatively low airmass (⩽1.4), high transparency, and no moonlight. In all cases we took a series of exposures of the galaxy, and the telescope was stepped between exposures in order to move the galaxy around...
the chip and average over flat-fielding imperfections. We only retained images with less than 7% transparency differences and with point-spread function FWHM less than 50% greater than the best in the series. The flat-fielded galaxy images were shifted to align the stars and co-added to build signal to noise. We used an algorithm to remove cosmic rays and adjusted parameters so that the photometric properties, as determined in a simple average of the images, were preserved.

In spite of our great care in determining flat-field data, the night-sky brightness at KPNO (or any dark site) is about 22.5 mag arcsec$^{-2}$ (see, for example, Neugent & Massey 2010), and so achieving 29.5 mag arcsec$^{-2}$ requires going 7 mag below the sky. No flat-field will be good to 1 part in 6000 (10% photometry) at these light levels. Fortunately, it does not have to be. The key to measuring these low light levels is not in the flat-fielding, but rather in the sky subtraction. The flat-fielding helps in getting the sky relatively flat from one side of the frame to the other, but even if there are 1% residual gradients in the flat-fielding, this is dealt with by fitting the sky with a two-dimensional function, as we did.

Therefore, we edited foreground stars and background galaxies from the images and determined a two-dimensional fit of the sky pixels in the edited image—interpolating across the galaxy. This procedure works because the galaxies are a small portion of the total field of view of the image: approximately 14% for DDO 53, 12% for DDO 86, 10% for DDO 133, 26% for NGC 4163, and 4% for IZw 115 and its detached region. It is necessary because there is structure in the sky. Typical variations of the background across the image were of order 0.2%–0.6%. We used a Legendre function with the minimum order that produced a satisfactory sky. Typical orders were 3–5.

We determined the success of a fit to the sky empirically by examining row and column cuts through the sky-subtracted image. We expected the background to be flat with noise around zero, and we varied the $x$ and $y$ orders until we achieved that. This procedure produced an image of the sky. We then subtracted the sky image from the original co-added image and from the edited image to yield sky-subtracted images with and without the foreground/background object contamination.

A legitimate question is whether or not our fits to the sky structure are affected by the presence of the galaxy and/or contaminating stars in the field. That can be answered best by comparing results obtained on the same galaxy using different telescopes/instruments with differing fields of view. This comparison is made in Section 2.1.2. We further gain confidence in our results in the outer disks of the dwarfs from the fact...
that we see similar profiles from data obtained with different telescopes/instruments and reduced with different types of sky flats (DDO 133 and IZw 115 imaged with the Mosaic Camera on the KPNO 4 m and reduced with twilight flats, and the other galaxies imaged with the Cassegrain Focus Imager on the KPNO 2.1 m telescope and reduced with dark sky flats).

2.1.2. Surface Photometry

Removal of background galaxies and foreground stars is essential for meaningful azimuthally averaged surface photometry. We attacked this problem in two ways for each image. First, we used the edited sky-subtracted images, with some additional masking of small areas close to the galaxy. A problem with this approach is in distinguishing, without radial velocity information, stellar clusters in the galaxy from foreground/background object contamination. We used the various passband images of the galaxy at our disposal to make the best guess as to whether a discrete object in the image was a part of the galaxy or foreground/background contamination. The area surrounding the galaxy is a good clue to the type of contamination we should expect across the galaxy. Nevertheless, subjective judgment was involved in this step.

The second method we used to account for foreground/background contamination was to use the unedited sky-subtracted image and determined an average “sky” value around the galaxy that included the foreground/background component. This statistically corrects for interlopers, and assumes that the fields around the galaxy represent the contamination across the galaxy itself. The problem with this method is that a given annulus in the surface photometry might not contain an exactly representative amount of light from extraneous objects, and a single foreground star or background object in the faint, outer parts of the galaxies can severely affect the surface photometry. For this reason, we prefer the surface photometry obtained with the first method of editing contamination from the images, but we applied both methods. In fact the two methods produced similar results. The comparison is shown in Figures 6 and 7 for the V-band and GALEX NUV photometry, respectively. The surface photometry is cut off where there is a large jump in the uncertainty, usually around 1 mag arcsec$^{-2}$.

Because dIm galaxies are lumpy, we determined the center of the galaxy, position angle (P.A.), and ellipticity from an outer isophote in a contour plot of a smoothed version of the V image. Then we integrated the photometry in fixed ellipses that increase in semi-major axis length. The step size is given in Table 2, and
Figure 4. As in Figure 1, for NGC 4163. The Hα image is not shown as the logarithm. Contours of integrated H\textsc{i} emission are 1.8 and 3.03 to 7.89 in steps of $2.43 \times 10^{19} \text{ cm}^{-2}$ and 1.7 to 8.1 in steps of $0.91 \times 10^{20} \text{ cm}^{-2}$.

was chosen to be $\geq 150$ pc and, as seen by eye, to cover a sufficient area of the galaxy to average over the most severe local fluctuations. We geometrically matched the continuum-subtracted Hα images to the V-band images and applied the same ellipse integrations. The outermost ellipse is shown superposed on the V, NUV, and Hα images in Figures 1–5.

We corrected the photometry for reddening using the foreground reddening, given in Table 1, plus 0.05 mag in $E(B-V)$ for internal reddening in B and V and 0.1 mag in $E(B-V)$ for internal reddening in Hα. This level of internal reddening is consistent with measurements of the Balmer decrement in H\textsc{ii} regions in a sample of 39 dI\text{m} galaxies (Hunter & Hoffman 1999). There, the average reddening in H\textsc{ii} regions is 0.1, and we have taken half this to represent the stars outside of H\textsc{ii} regions. We used the Cardelli et al. (1989) extinction curve.

We used a single extinction correction for all radii within each galaxy. This is justified by the lack of metallicity gradients in dwarfs (see, for example, Croxall et al. 2009) and the correlation between metallicity and attenuation seen in spirals (Boissier et al. 2007). On the other hand, little is known about the outer disks of dwarfs, beyond where Hα emission is no longer detected, although there are some hints of dust emission even there (see, for example, Hinz et al. 2006). Boissier et al., based on IRAS observations, suggest that there is no attenuation in the outer disks of two dwarfs (IC1613, WLM), but uncertainties are large due to low IRAS fluxes.

There is a region of stellar emission near, but detached from, I Zw 115 that we did not include in the galactic photometry. It is located at 15h32m51s, 46°25′51″ (2000), 101′′5 (= 6.0 kpc) from the center of I Zw 115, southwest along the galaxy’s major axis, and is marked in images in Figure 5. In a circular aperture of radius 14′85, the region has a V magnitude of 20.39 ± 0.04 and a surface brightness $\mu_V$ of 26.9 mag of 1 arcsec$^{-2}$. If it is at the distance of I Zw 115, it has an $M_V$ of $-10$ and a diameter of several kpc. Thus, it could be a very small dwarf companion.
DDO 133 is clearly barred, and the outer isophote that was used to determine the galaxy morphology is located beyond the bar. The bar has a P.A. that is $-13^\circ$, an $11^\circ$ twist from the outer isophote. The center of the bar is located at 12h32m54.5, 31°32'27", 18'8 (= 560 pc) from the center of the outer isophote. The minor-to-major axis ratio $b/a$ of the bar is 0.44, compared to 0.69 for the outer isophote, so the outer isophote is rounder. The major axis of the bar is $133^\circ$ (= 3.9 kpc) long. We experimented with changing the centering and P.A. of the photometry ellipses, but found that there was no significant change in the photometry for a reasonable alternate choice of the center (10'' offset to the southwest) and P.A. (5° counterclockwise).

DDO 86 presents a special challenge to determining the position angle of the major axis. At an outer isophote ($\mu_V \sim 27.2$ mag arcsec$^{-2}$), the P.A. of the major axis is $85^\circ$ and the minor-to-major axis ratio $b/a$ is 0.86. This is close to the galaxy morphology determined in the survey data: P.A. $\sim 72^\circ$ and $b/a \sim 0.82$ (Hunter & Elmegreen 2006). However, in the deeper imaging data that we have here, we see that there is a faint extension of starlight to the north. At an isophote level that includes this extension ($\mu_V \sim 28.4$ mag arcsec$^{-2}$), the P.A. of the galaxy rotates clockwise to $32.5^\circ$, although the shape remains the same ($b/a \sim 0.87$). An inner isophote ($\mu_V \sim 25.6$ mag arcsec$^{-2}$) has a major axis that is rotated counterclockwise from both of these (113:5) and the galaxy is more elongated ($b/a \sim 0.65$). Finally, the kinematical major axis determined from the H$\alpha$ velocity field has a P.A. of $-46^\circ$. It is possible that this sequence of optical P.A.'s—rotating clockwise from higher surface brightness to fainter—and change in shape—becoming rounder in the middle and outer parts—represents an offset bar; the center of the inner isophote is located 360 pc to the southwest of the center of the extreme outer isophote. For the surface photometry we have chosen to use the P.A. from our H$\alpha$ kinematic analysis.

Since we have surface photometry from the survey images of each of these galaxies, we compare the deep imaging photometry with that from the survey data in Figure 6. We see that the agreement is quite good in most cases. In addition, the breaks in the surface brightness profiles seen in the survey data of DDO 86 and DDO 133 are there at the same radius and surface brightness level in the deep data. And, the azimuthally averaged $B-V$ colors in DDO 133 match closely the survey data.

Figure 5. As in Figure 1, for IZw 115. The H$\alpha$ image is not shown as the logarithm. Contours of integrated H$\alpha$ emission are 1.3 to 27.2 in steps of $2.59 \times 10^{20}$ cm$^{-2}$. The region of stars that is detached from the main body of IZw 115 is marked in the V and NUV images. The southern H$\alpha$ tail in the color composite image extends over the detached region.
in the region of overlap. The exception to the good agreement is DDO 53. Beginning at a radius of 1.2 (1.25 kpc) and a $\mu_V$ of 25.8 mag arcsec$^{-2}$ the new surface photometry is systematically fainter. The differences are greater than the uncertainties in the photometry. The survey $B - V$ color is also systematically redder than the deep photometry beginning at a radius of 0.77 (0.81 kpc; $\mu_V \sim 24.9$ mag arcsec$^{-2}$). In the survey data, there is a gradient in $B - V$, with the galaxy becoming redder with radius. In the deep data, the color is relatively constant. We note that the integrated $B - V$ of DDO 53 from the deep image (0.30 ± 0.01, not corrected for reddening) is close to that given by de Vaucouleurs et al. (1991; 0.35), while that from the survey data (0.48) is significantly redder. Therefore, we suspect that the deep photometry is better than that measured from the survey data for this galaxy in the region of overlap.

From the ellipse photometry we can derive several quantities. First, the last ellipse yields integrated photometry and that is given in Table 3. Second, fits to the surface brightness profiles yield disk scale lengths $R_D$ and central surface brightnesses $\mu_{V,0}$. These are listed in Table 4. Four of the five galaxies—DDO 53, DDO 86, DDO 133, and NGC 4163—exhibit double exponentials. The profile in the outer disk falls off more steeply than that in the inner disk in DDO 53, DDO 86, and DDO 133. In NGC 4163 the outer profile is shallower than the inner. DDO 86 and DDO 133 were already known to have double exponentials from the survey data, but the survey data of DDO 53 did not go

Figure 6. Deep $V$, and in some cases $B - V$, surface photometry with different methods of determining the background/foreground object contamination: “edit” refers to editing and masking individual unwanted objects, “stat” refers to using the surrounding field to determine a statistical correction, and “stat-2” refers to the statistical method carried out by a different co-author. We also compare the deep surface photometry to the shallower survey surface photometry from Hunter & Elmegreen (2006). Uncertainties are only shown where they are larger than the symbols. $R_{25}$ and $R_H$ mark the radius at the $B$-band 25 mag arcsec$^{-2}$ isophote and the Holmberg radius ($B = 26.66$ mag arcsec$^{-2}$), respectively.

(A color version of this figure is available in the online journal.)
out far enough to give a hint of the break in the profile. The break in NGC 4163 is more subtle than in the other three galaxies. Nevertheless, the scale lengths are different—0.26 ± 0.02 kpc versus 0.31 ± 0.004 kpc, and the central surface brightnesses implied by each differ by 0.54 mag. For those four galaxies with breaks, the $R_B$ and $\mu_{V,0}$ are given for both the inner and outer parts of the profiles, along with the break radius $R_{br}$ at which the slope changes. In addition DDO 53 and IZw 115 show breaks at small radii, a little over one disk-scale length that coincide with concentrations of star formation. These are marked in the surface brightness plots, but not included in Table 4. The surface photometry and color profiles are shown in Figures 8–12.

2.2. Ultraviolet Images

We obtained deep images of our sample galaxies with the Galaxy Evolution Explorer (GALEX; Martin et al. 2005) satellite to trace and characterize star formation into the outer disks of...
Figure 8. Azimuthally averaged surface photometry and colors of DDO 53, corrected for reddening, plotted against radius from the galaxy center normalized to the disk scale-length $R_D$. Top: H\textsc{i} properties, including the gas surface density, rotational velocity, velocity dispersion of the rotational component, and the ratio of gas surface density to critical density. $\Sigma_{\text{crit}}$ is the critical threshold density for large-scale gravitational instabilities in a differentially rotating thin disk (Toomre 1964). $\Sigma_{\text{gas}}$ includes H\textsc{i} and He. Bottom: optical and ultraviolet properties, including $V$, $H\alpha$, NUV, and FUV surface photometry. $R_{25}$ and $R_{B}$ mark the radius at the $B$-band 25 mag arcsec$^{-2}$ isophote and the Holmberg radius (26.66 mag arcsec$^{-2}$), respectively. The dashed vertical black lines mark breaks in the $V$-band profile.

(A color version of this figure is available in the online journal.)

Table 3

| Galaxy   | $M_V$ | $\sigma_{M_V}$ | $B - V$ | $\sigma_{B-V}$ | $M_{\text{NUV}}$ | $\sigma_{M_{\text{NUV}}}$ | $FUV - NUV$ | $\sigma_{FUV-NUV}$ |
|----------|-------|----------------|---------|----------------|-----------------|-------------------|-------------|-------------------|
| DDO 53   | −13.80| 0.01           | 0.23    | 0.01           | −12.89          | 0.01              | 0.05        | 0.01              |
| DDO 86   | −16.46| 0.01           | ···     | ···            | −15.19          | 0.01              | 0.21        | 0.01              |
| DDO 133  | −15.95| 0.01           | 0.37    | 0.01           | −14.71          | 0.01              | 0.20        | 0.01              |
| NGC 4163 | −14.44| 0.01           | 0.56    | 0.01           | −12.51          | 0.01              | 0.39        | 0.01              |
| IZw 115  | −16.01| 0.01           | ···     | ···            | −14.54          | 0.01              | 0.37        | 0.01              |

Note. $^aM_{\text{NUV}}$ is an AB magnitude.

Table 4

| Galaxy   | $R_D$ | $\sigma_{R_D}$ | $\mu_{V,0}$ | $\sigma_{\mu_{V,0}}$ | $R_{Br}$ | $\sigma_{R_{Br}}$ | $\mu_{V,0}$ | $\sigma_{\mu_{V,0}}$ |
|----------|-------|----------------|-------------|----------------------|----------|------------------|-------------|----------------------|
| DDO 53   | 0.60  | 0.03           | 23.74       | 0.13                 | 1.98     | 0.43             | 0.01        | 22.36                | 0.20              |
| DDO 86   | 1.72  | 0.09           | 23.18       | 0.10                 | 4.70     | 1.16             | 0.07        | 21.76                | 0.34              |
| DDO 133  | 2.16  | 0.09           | 23.80       | 0.05                 | 3.80     | 0.69             | 0.01        | 19.70                | 0.14              |
| NGC 4163 | 0.26  | 0.03           | 21.25       | 0.14                 | 0.73     | 0.31             | 0.00        | 21.79                | 0.06              |
| IZw 115  | 0.61  | 0.01           | 21.41       | 0.05                 | ···      | ···              | ···         | ···                  | ···               |

Note. $^aR_{Br}$ is the break radius at which the surface brightness profile changes slope. The profile of IZw 115 does not show this break.
dwarf galaxies where Hα may not be an effective tracer of recent star formation (see, for example, Thilker et al. 2005, 2007; Boissier et al. 2007). The UV—ultraviolet light coming directly from OB stars—can easily trace young stars in the outer galaxy, and the UV has the advantage in a patchy star-forming environment of integrating over a longer timescale than does Hα (10 Myr).

The galaxies are listed in Table 5 along with the exposure times and tile name of the GALEX images. GALEX imaged simultaneously in two channels: FUV with a bandpass of 1350–1750 Å, an effective wavelength of 1516 Å, and a resolution of 4′0 and NUV with a bandpass of 1750–2800 Å, an effective wavelength of 2267 Å, and a resolution of 5′.6. The images were processed through the GALEX GR4/5 pipeline and were retrieved as final intensity maps with a 1′5 pixel scale. The GALEX field of view is a circle with 1′ diameter, and we have extracted a portion around our target galaxies.

We corrected the UV photometry for extinction using the same total reddening $E(B - V)$, as was used for correcting the optical. We combined the $E(B - V)$, with the extinction law of Cardelli et al. (1989) to produce the extinction $A_{\text{FUV}} = 8.24E(B - V)$, and, interpolating over the 2175 Å bump, $A_{\text{NUV}} = 7.39E(B - V)$. However, the FUV extinction law is known to vary from galaxy to galaxy, and the NUV filter straddles the 2175 Å extinction feature, which also varies not only from galaxy to galaxy but from place to place within galaxies (for example, Gordon et al. 2003). Star formation activity appears to play as important a role, perhaps even more important, than metallicity in determining the UV extinction curve and the strength of the 2175 Å bump. In the metal-poor Small Magellanic Cloud (SMC), for example, Gordon & Clayton (1998) have shown that lines of sight through the actively star-forming bar have UV extinction curves that are linear with $1/\lambda$, rising more steeply into the FUV than in the Milky Way, and no 2175 Å bump is present, while a sight line through the quiescent wing has an extinction curve that is similar to that in the Milky Way with a shallower slope into the FUV and a 2175 Å bump. In our dwarf galaxies, the level of star formation activity is highly variable from galaxy to galaxy and from place to place within a galaxy, potentially resulting in a variable FUV extinction law. Wyder et al. (2007) have dealt with this for a large sample of galaxies by adopting the Cardelli et al. extinction law for the Milky Way and determining the best average reddening from convolving theoretical galaxy spectral energy distributions (SEDs) with the GALEX filter transmission curves. In Hunter et al. (2010), we examined the results of convolving different SMC, LMC, and Milky Way extinction curves (Cardelli et al. 1989; Gordon et al. 2003) with constant SFR galaxy SEDs constructed from the Bruzual & Charlot (2003) stellar population library and with

![Figure 9](image_url)
Figure 10. Azimuthally averaged surface photometry and colors of DDO 133, corrected for reddening, plotted against radius from the galaxy center normalized to the disk scale-length \(R_D\). Top: H\(_i\) properties, including the gas surface density, rotational velocity, velocity dispersion of the rotational component, and the ratio of gas surface density to critical density. \(\Sigma_{\text{crit}}\) is the critical threshold density for large-scale gravitational instabilities in a differentially rotating thin disk (Toomre 1964). \(\Sigma_{\text{gas}}\) includes H\(_i\) and He. Bottom: optical and ultraviolet properties, including \(V\), \(H\alpha\), NUV, and FUV surface photometry. \(R_{25}\) and \(R_H\) mark the radius at the \(B\)-band 25 mag arcsec\(^{-2}\) isophote and the Holmberg radius (26.66 mag arcsec\(^{-2}\)), respectively. The dashed vertical black line marks the break in the \(V\)-band profile.

(A color version of this figure is available in the online journal.)

the GALEX filter transmission curves. The \(A_V/E(B-V)\) varies by 1.5 mag depending on the extinction curve. Considering the variety of environments represented by our sample and the fact that extinction is minimal except for a few galaxies with higher than average foreground extinction, we decided to adopt the Wyder et al. extinctions: \(A_{\text{FUV}} = 8.24E(B-V)_1\) and \(A_{\text{NUV}} = 8.2E(B-V)_1\). For most of our galaxies, the variations represented by alternate extinction laws result in differences of order 0.05 mag.

Surface photometry of the NUV and FUV images proceeded in the same manner as for the optical images. We edited foreground/background objects from the images, fit the cleared area around the galaxy, and subtracted this from the edited and from the unedited images. For the unedited sky-subtracted image, we determined the average background light from contaminating objects and subtracted this from the image. We then geometrically transformed the UV images to match the \(V\)-band scale and orientation and measured surface photometry on the edited and unedited images using the same ellipse parameters as for the \(V\)-band images. The two methods of accounting for background/foreground contamination are shown in Figure 7. The results of the two methods agree well. Integrated photometry is given in Table 3. The surface photometry and color profiles are shown in Figures 8–12.

Since we are looking at faint light levels in outer disks, we need to consider whether the UV light we see truly comes from young stars or whether there might be other sources of light that dominate out there. One such potential source is white dwarf stars. DDO 133, as a test case, has an FUV – NUV color of order 0.1 mag in the outer disk, not counting the colors with relatively high uncertainties. A white dwarf of that color has an effective temperature of order 16,000 K. At a distance of 10 pc, a star with \(\log g = 6\) and a radius \(R = R_\odot\) would have an absolute NUV AB magnitude of \(M_{\text{NUV}} = 1.84\) (L. Bianchi 2009, private communication). Assuming a mass for the white dwarf of 0.7 \(M_\odot\), the star should have a radius of 0.1 \(R_\odot\). Thus, the apparent NUV magnitude would be 35.7. To reproduce a \(\mu_{\text{NUV}}\) of 28 mag arcsec\(^{-2}\) at a radius of 2 \(R_D\) in DDO 133, we would need about 1.4 white dwarfs pc\(^{-2}\). That is two times higher than the density of white dwarfs in the solar neighborhood. For white dwarfs with smaller radii or higher \(\log g\), the number of white dwarfs that are needed goes up, so this is probably a lower limit. However, the solar neighborhood should have a much higher stellar density than the outer disk of a dwarf. In the solar neighborhood \(\mu_V = 22.7 \pm 0.2\) (Ishida & Mikami 1982), and that is a factor of 30 higher than the surface brightness in DDO 133 at the radius we are considering \(\mu_V = 26.5\). So, the stellar density of white dwarfs needed to account for the UV light in DDO 133 fails by a factor of about 60. Even 3 mag fainter—at the edge of our detection, the numbers needed are four times too high and so it is unlikely that white dwarfs alone could produce the UV starlight that
Figure 11. Azimuthally averaged surface photometry and colors of NGC 4163, corrected for reddening, plotted against radius from the galaxy center normalized to the disk scale-length \( R_D \). Top: H\textsc{i} properties, including the gas surface density, rotational velocity, velocity dispersion of the rotational component, and the ratio of gas surface density to critical density. \( \Sigma_{\text{crit}} \) is the critical threshold density for large-scale gravitational instabilities in a differentially rotating thin disk (Toomre 1964). \( \Sigma_{\text{gas}} \) includes H\textsc{i} and He. Bottom: optical and ultraviolet properties, including \( V \), H\textsc{a}, NUV and, FUV surface photometry. \( R_{25} \) and \( R_{H} \) mark the radius at the \( B \)-band 25 mag arcsec\(^{-2} \) isophote and the Holmberg radius (26.66 mag arcsec\(^{-2} \)), respectively. The dashed vertical black line marks the break in the \( V \)-band profile.

(A color version of this figure is available in the online journal.)
weighting, which gives the highest signal to noise but at the expense of long wings in the beam, and “uniform” weighting, which gives the best resolution but at the cost of signal to noise and the presence of negative sidelobes. We chose a sample weighting that gives a formal increase of only 5% in noise yet with a significant improvement in beam profile over what would have been achieved with “natural” weighting. The resulting synthesized beam FWHM are given in Table 6. We deconvolved the maps until there were roughly comparable numbers of positive and negative components.

To remove the portions of each channel map without emission that are only contributing noise to the map, we used the maps smoothed to twice the beamsize for a conditional transfer of data in the unsmoothed maps. The channel maps were blanked wherever the flux in the smoothed maps fell below 2.5σ. Flux-weighted moment maps were made from the resulting data cube. Integrated emission—moment zero—maps are shown in Figures 13–17, along with velocity field (moment one) and velocity dispersion (moment two) maps. Integrated H I contours superposed on the V-band images are shown in Figures 1–5.

2.3.2. Velocity Fields

Position–velocity diagrams (panel e), velocity fields (panels b and d), and velocity dispersions (panel c) are shown in Figures 13–17. Panel (b) shows the standard intensity-weighted mean velocity field, and panel (d) shows the velocity field that results from fitting profiles with a Gauss–Hermite h3 polynomial.

Because of the possible presence of multiple velocity components, we have deconvolved ordered from non-ordered motions using the method described by Oh et al. (2008). First, an approximate rotation curve is derived from the major-axis position–velocity diagram and this is used to create an artificial velocity field. Then in an automated method, we fit single Gaussians to the major velocity component in each profile across the galaxy. The velocities of these components are compared to the artificial velocity field. If they deviate more than a prescribed amount, the program examines the possibility that the bulk motion at that point is represented by a secondary velocity component. From this, we extract the bulk velocity field that then becomes the input velocity field for the next iteration, which is now fit using the “tilted ring model” rather than the major-axis position–velocity diagram. This loop continues until the mean difference between successive velocity fields is less than three times the channel width. This gives a final bulk velocity field. Parameters derived from this process (center position, P.A., inclinations) are summarized in Table 7. Following Bureau & Carignan (2002) we corrected the rotation velocities for asymmetric drift, and the final rotation curves are shown in the graphs in Figures 8–12.

The velocity fields of DDO 86 and DDO 133 exhibit well-behaved ordered rotation. In IZw 115 the velocity field is less well-behaved, but still ordered motion is present. The velocity fields in DDO 53 and NC 4163, on the other hand, are quite peculiar. Here we discuss each galaxy individually.

DDO 53. DDO 53 is a part of the THINGS study of H I in nearby galaxies (Walter et al. 2008) and has been analyzed by S.-H. Oh et al. (2011, in preparation). The kinematical axis of DDO 53 is at a position angle of 155°, while the optical major axis is at an angle of 81°, a difference of 74°. Furthermore, the
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Figure 13. Moment maps and a major-axis position–velocity diagram of DDO 53. (a) Integrated H\textsc{i} map (moment 0). Contours run from 0 to 2 Jy beam\(^{-1}\) km s\(^{-1}\) with a spacing of 0.2 Jy beam\(^{-1}\) km s\(^{-1}\). The R.A., decl. axes can be used to match the field of view with that in Figure 1 (middle right panel). (b) Intensity-weighted mean velocity field (moment 1). Contours run from \(-20\) km s\(^{-1}\) to 35 km s\(^{-1}\) with a spacing of 2 km s\(^{-1}\). (c) H\textsc{i} velocity dispersion map (moment 2). Velocity contours run from 1 to 17 km s\(^{-1}\) with a spacing of 2 km s\(^{-1}\). (d) Hermite \(h_3\) velocity field. Contours run from \(-20\) km s\(^{-1}\) to 35 km s\(^{-1}\) with a spacing of 2 km s\(^{-1}\). (e) Position–velocity diagram taken along the average position angle (155\(^\circ\)) of the major axis. Contours start at +3\(\sigma\) in steps of 3\(\sigma\). The dashed lines indicate the systemic velocity and position of the kinematic center derived from the tilted-ring analysis. Overplotted is the Hermite velocity field rotation curve corrected for the average inclination (27\(^\circ\)).

Figure 14. Moment maps and a major-axis position–velocity diagram of DDO 86. (a) Integrated H\textsc{i} map (moment 0). Contours run from 0 to 0.38 Jy beam\(^{-1}\) km s\(^{-1}\) with a spacing of 0.08 Jy beam\(^{-1}\) km s\(^{-1}\). The R.A., decl. axes can be used to match the field of view with that in Figure 2 (middle right panel). (b) Intensity-weighted mean velocity field (moment 1). Contours run from 1000 km s\(^{-1}\) to 1050 km s\(^{-1}\) with a spacing of 5 km s\(^{-1}\). (c) H\textsc{i} velocity dispersion map (moment 2). Velocity contours run from 1 to 20 km s\(^{-1}\) with a spacing of 2 km s\(^{-1}\). (d) Hermite \(h_3\) velocity field. Contours run from 1000 km s\(^{-1}\) to 1050 km s\(^{-1}\) with a spacing of 5 km s\(^{-1}\). (e) Position–velocity diagram taken along the average position angle (317\(^\circ\)) of the major axis. Contours start at +3\(\sigma\) in steps of 3\(\sigma\). The dashed lines indicate the systemic velocity and position of the kinematic center derived from the tilted-ring analysis. Overplotted is the Hermite velocity field rotation curve corrected for the average inclination (32\(^\circ\)).

Fit to the H\textsc{i} velocity field yields a variable inclination angle. The kinematic center and the optical center are 32\(^\prime\) apart, with the kinematic center being northeast of the optical center. The fit to the velocity field is quite poor, and the rotation curve is only meaningful out to a radius of 0.9 kpc.

**DDO 86.** The bulk velocity field of DDO 86 is well determined with clean fits to the position angle of the kinematic axis, the center position, and the inclination of the H\textsc{i} disk. The optical, however, is more problematic, as discussed in Section 2.1.2: the V-band major axis rotates clockwise from higher surface brightness to fainter. This may indicate the presence of an off-center bar. So, for the optical and UV surface photometry we used the P.A. derived from the H\textsc{i} kinematics. The optical center determined from outer isophotes agrees within 14\(^\prime\) with the H\textsc{i} center, with the H\textsc{i} center being northwest of the optical.
**Figure 15.** Moment maps and a major-axis position–velocity diagram of DDO 133. (a) Integrated H\textsc{i} map (moment 0). Contours run from 0 to 3 Jy beam\(^{-1}\) km s\(^{-1}\) with a spacing of 0.5 Jy beam\(^{-1}\) km s\(^{-1}\). The R.A., decl. axes can be used to match the field of view with that in Figure 3 (middle right panel). (b) Intensity-weighted mean velocity field (moment 1). Contours run from 280 km s\(^{-1}\) to 400 km s\(^{-1}\) with a spacing of 5 km s\(^{-1}\). (c) H\textsc{i} velocity dispersion map (moment 2). Velocity contours run from 1 to 20 km s\(^{-1}\) with a spacing of 2 km s\(^{-1}\). (d) Hermite \(h_3\) velocity field. Contours run from 280 km s\(^{-1}\) to 400 km s\(^{-1}\) with a spacing of 5 km s\(^{-1}\). (e) Position–velocity diagram taken along the average position angle (358\(^{\circ}\)) of the major axis. Contours start at \(+1\sigma\) in steps of 3\(\sigma\). The dashed lines indicate the systemic velocity and position of the kinematic center derived from the tilted-ring analysis. Overplotted is the Hermite velocity field rotation curve corrected for the average inclination (46\(^{\circ}\)).

**Figure 16.** Moment maps and a major-axis position–velocity diagram of NGC 4163. (a) Integrated H\textsc{i} map (moment 0). Contours run from 0 to 1.9 Jy beam\(^{-1}\) km s\(^{-1}\) with a spacing of 0.2 Jy beam\(^{-1}\) km s\(^{-1}\). The R.A., decl. axes can be used to match the field of view with that in Figure 4 (middle right panel). (b) Intensity-weighted mean velocity field (moment 1). Contours run from 150 km s\(^{-1}\) to 170 km s\(^{-1}\) with a spacing of 2 km s\(^{-1}\). (c) H\textsc{i} velocity dispersion map (moment 2). Velocity contours run from 1 to 17 km s\(^{-1}\) with a spacing of 2 km s\(^{-1}\). (d) Bulk velocity field. Contours run from 150 km s\(^{-1}\) to 170 km s\(^{-1}\) with a spacing of 2 km s\(^{-1}\). (e) Position–velocity diagram taken along the average position angle (15\(^{\circ}\)) of the major axis. Contours start at \(+1\sigma\) in steps of 3\(\sigma\). The dashed lines indicate the systemic velocity and position of the kinematic center derived from the tilted-ring analysis. Overplotted is the Hermite velocity field rotation curve corrected for the average inclination (48\(^{\circ}\)).

**DDO 133.** The bulk velocity field of DDO 133 is well behaved. The kinematic P.A., inclination, and center agree very well with those determined for the optical.

**NGC 4163.** Although rotation is seen in the gas, the velocity field is so peculiar that parameters for the tilted ring model—center, P.A., and inclination—were taken from the optical.

**IZw 115.** IZw 115 shows rotation, although the velocity field is rather peculiar. The position angle of the kinematic axis was found to vary between 50\(^{\circ}\) and 78\(^{\circ}\), while the optical major axis is at an angle of 41\(^{\circ}\). On the other hand, the inclinations agree within 7\(^{\circ}\), and the centers, within 4\(\arcsec\). The detached region seen in the optical and NUV (Figure 5) shows a hint of rotating independently of the main body of IZw 115. Panel (d) in Figure 17, which shows the velocity field resulting from fitting profiles with a Gauss–Hermite \(h_3\) polynomial, can be interpreted as showing overall rotation with an axis at a position angle of...
Figure 17. Moment maps and a major-axis position–velocity diagram of IZw 115. (a) Integrated H\textsc{i} map (moment 0). Contours run from 0 to 0.2 Jy beam\textsuperscript{−1} km s\textsuperscript{−1} with a spacing of 0.03 Jy beam\textsuperscript{−1} km s\textsuperscript{−1}. The R.A., decl. axes can be used to match the field of view with that in Figure 5 (middle right panel). (b) Intensity-weighted mean velocity field (moment 1). Contours run from 600 km s\textsuperscript{−1} to 700 km s\textsuperscript{−1} with a spacing of 5 km s\textsuperscript{−1}. (c) H\textsc{i} velocity dispersion map (moment 2). Velocity contours run from 1 to 15 km s\textsuperscript{−1} with a spacing of 2 km s\textsuperscript{−1}. (d) Hermite \(h_3\) velocity field. Contours run from 600 km s\textsuperscript{−1} to 700 km s\textsuperscript{−1} with a spacing of 5 km s\textsuperscript{−1}. (e) Position–velocity diagram taken along the average position angle (51°) of the major axis. Contours start at +3\(\sigma\) in steps of 3\(\sigma\). The dashed lines indicate the systemic velocity and position of the kinematic center derived from the tilted-ring analysis. Overplotted is the Hermite velocity field rotation curve corrected for the average inclination (61°).

Table 7

| Galaxy  | \(\log M_{\text{H}\textsc{i}}\) | \(V_{\text{sys}}\) (km s\textsuperscript{−1}) | P.A. (deg) | Incl. (deg) | Max R (arcsec) | Annuli Widths (arcsec) |
|---------|------------------|-----------------|------------|-----------|----------------|----------------------|
| DDO 53\textsuperscript{a} | 7.85 | 08 34 08.9 | 66 11 08 | 17 | 155 | −304 to +79 | 200 | 25 |
| DDO 86  | 9.01 | 10 44 28.8 | 60 22 13 | 1021 | 317 | 32 | 150 | 15 |
| DDO 133 | 8.54 | 12 32 55.6 | 31 32 18 | 331 | 358 | 46 | 262 | 50 |
| NGC 4163\textsuperscript{b} | 7.20 | 12 12 09.0 | 36 10 13 | 162 | 195 | 48 | 150 | 25 |
| IZw115  | 8.09 | 15 32 56.8 | 46 27 12 | 655 | 50–78 | 61 | 90 | 15 |

Notes.

\textsuperscript{a} Ring parameters are taken from THINGS (S.-H. Oh et al. 2011, in preparation).

\textsuperscript{b} Ring parameters are taken from the optical.

roughly 90°, clearly distinct from IZw 115. This could indicate that the detached region is a small companion galaxy that is interacting with IZw 115.

2.3.3. Surface Density Profiles

The azimuthally averaged H\textsc{i} surface densities \(\Sigma_{\text{H}\textsc{i}}\), and velocity dispersions \(\sigma_{\text{vel}}\) of the rotational component were determined using the center, P.A., and inclination angle given in Table 7. The \(\Sigma_{\text{H}\textsc{i}}\) was corrected for He to produce the gas surface density \(\Sigma_{\text{gas}}\). The gas surface density profiles and average velocity dispersions are shown as a function of radius in Figures 8–12.

3. STARS IN THE OUTER DISKS

3.1. Where do dIm Stellar Disks End?

We have traced starlight in the V-band to ultra-low surface brightness levels. Yet, the stellar surface brightnesses in the outer disks of our five galaxies continue to decline exponentially as far as we can measure it. That is, we run out of signal to noise before we convincingly run out of galactic starlight. We have not found the edges of the stellar disks. This is consistent with results from stellar photometry that have traced the stellar disks in the LMC (Saha et al. 2010), M33 (Barker et al. 2011), and M31 (Richardson et al. 2008) to even more extreme radii.

3.2. Breaks in the Surface Brightness Profiles

The surface photometry of DDO 133 shows a change in the slope at 1.8 \(R_D\). Beyond there, \(\mu_V\) drops more steeply. Although less extreme, there are noticeable changes in the slopes in the outer disks of DDO 53, DDO 86, and NGC 4163 as well. And, in DDO 86 and DDO 133 the breaks are also apparent in NUV surface brightness profiles. The break in NGC 4163 is coincident with the outer limit to a central bump in NUV and H\textalpha emission. And in DDO 86 and DDO 133, the outer disk breaks occur where H\textalpha ends or declines sharply. In addition to the breaks at several disk scale lengths, there are breaks or variations in the surface brightness profiles at smaller radii. We see these in DDO 53 and IZw 115. The inner bump in the V-band surface photometry in DDO 53 is mimicked in NUV and H\textalpha and corresponds, more or
less, to a change in FUV – NUV and B – V colors. The flattening out of the V-band surface brightness profile in the central 1.5 R_D in IZw 115 is accompanied by a flattening in the NUV profile, and the location of a single bright H II region. The only break that does not coincide with a change in H is the outer break in DDO 53. Thus, most of these breaks appear to be connected with changes in the star formation activity.

Double-exponential surface brightness profiles are also seen in about 1/4 of our survey of dIIm and Sm galaxies (Hunter & Elmegreen 2006) and in the outer parts of many spirals (van der Kruit & Shostak 1982; Shostak & van der Kruit 1984; de Grijs et al. 2001; Kregel et al. 2002; Pohlen et al. 2002; Kregel & van der Kruit 2004), including one low luminosity spiral (Simon et al. 2003). It is now also seen in disks at high redshifts (0.6 < z < 1.0; Pérez 2004; Trujillo et al. 2009). Traditionally, these surface brightness breaks have been called “truncations,” but this implies that the break signals the edge of the stellar disk. In dwarf galaxies, this does not seem to be the case; the break is a rather abrupt change rather than an end. But what changes at that radius? Elmegreen & Hunter (2006) have suggested that the primary driver of star formation changes at the break, from gravitational instabilities in the interior to turbulence compression and supernovae in the outer disk. The nature of the breaks in dwarfs is explored further with our much larger survey data by K. Herrmann et al. (2011, in preparation).

3.3. What is the Star Formation History in the Outer Disks?

To look at the rates necessary to form the stars we find in the outer disks, we have computed azimuthally averaged profiles of SFRs derived from Hα, FUV, and V-band luminosities: SFR_Hα, SFR_FUV, and SFR_V. We use the formulae outlined in Hunter et al. (2010) with a Salpeter (1955) stellar IMF and assuming a constant SFR over long timescales. For the FUV and Hα formulae, we use the formulae from Kennicutt (1998) modified for the sub-solar (Z = 0.008) metallicities appropriate for dwarf galaxies. To determine the SFR averaged over a longer timescale, we use the V-band luminosity to determine the mass in stars and assume a timescale of 12 Gyr for the formation of that stellar mass. We use a stellar M/L_V ratio from Bell & de Jong (2001) that is a function of the (B – V)_0 color. If there is no (B – V)_0 measurement or the uncertainty in the color is > 0.2 mag, we assumed the last good measurement of B – V. In the case of DDO 86 and IZw 115, for which we do not have deep B-band images, we used the survey data. For DDO 86, B – V = constant with radius in the survey photometry; for IZw 115, the color reddens with radius and we used the survey photometry as far out as it goes. The SFR determined from the V-band is the SFR necessary to produce the original mass in stars. We correct this by a factor of two for the mass recycled back into the interstellar medium from Brinchmann et al. (2004).

Now we consider the effects of metallicity and a further correction to the SFR formulae based on the actual metallicities of our sample. Two of the galaxies in our sample have oxygen abundances 12 + log O/H measured from H II regions; the measured value of the oxygen abundance in DDO 53 is 7.5 ± 0.1 according to Hidalgo-Gámez et al. (2003) and 7.82 ± 0.09 according to Croxall et al. (2009). Given the coarseness of the metallicity grid of the models, both measurements give the same SFRs. In DDO 133 the oxygen abundance is 8.0 ± 0.05 (Hunter & Hoffman 1999). For the other galaxies, there are no measured values, so we have estimated the oxygen abundance from M_B and Richer & McCall’s (1995) correlation between M_B and 12 + log O/H. This yields 12 + log O/H of 8.0 for DDO 86 and IZw 115 and 7.7 for NGC 4163. Metallicities are unknown in the outer disks, but are likely to be lower than these values. To modify our star formation formulae for these metallicities, we use the synthesis models of STARBURST99 (Leitherer et al. 1999), with constant SFRs and Salpeter stellar IMFs. Their Figure 54 gives the luminosity at 1500 Å for Z = 0.008, 0.004, and 0.001, and this allows us to adjust our Z = 0.008 formulae for FUV-based SFRs to lower metallicities. Similarly, their Figure 78, which gives the number of photons below 912 Å, enables us to correct our Hα formula, and finally Figure 58 allows us to correct B – V, which enters into the formula for M/L_V and the V-band SFR.

Table 8 gives the luminosity at 1500 Å for Z = 0.008, 0.004, and 0.001, and this allows us to adjust our Z = 0.008 formulae for FUV-based SFRs to lower metallicities. Similarly, their Figure 78, which gives the number of photons below 912 Å, enables us to correct our Hα formula, and finally Figure 58 allows us to correct B – V, which enters into the formula for M/L_V and the V-band SFR.

For our galaxies, the SFRs at a radius where μ_V = 29.5 mag arcsec^{-2} are given in Table 8. Only SFR_FUV and SFR_V

| Galaxy     | R (kpc) | log SFR_FUV | σ_{FUV} (M⊙ yr^{-1} kpc^{-2}) | log SFR_V | σ_{V} (M⊙ yr^{-1} kpc^{-2}) |
|------------|---------|-------------|--------------------------------|-----------|-----------------------------|
| DDO 53     | 2.8     | -5.5        | 0.8                            | -5.1      | 0.1                         |
| DDO 86     | 7.5     | -4.7        | 0.3                            | -4.8      | 0.2                         |
| DDO 133    | 6.1     | -5.1        | 0.5                            | -4.9      | 0.1                         |
| NGC 4163   | 2.2     | -5.0        | 1.0                            | -4.6      | 0.2                         |
| IZw 115    | 4.6     | -5.0        | 0.6                            | -4.9      | 0.2                         |

Note. SFR_FUV is measured from the FUV luminosity. SFR_V is determined from the mass in stars derived from L_V. See the text for formulae.
are given since Hα is not detected at those radii. In DDO 133, for example, the stars continue for at least another 1.5 kpc beyond where Hα emission is no longer detectable. In DDO 133 at an annulus centered at \( \mu V = 29.5 \) mag arcsec\(^{-2} \), the SFR determined from the stellar mass SFR\( V \) is 0.00001 \( M_\odot \) yr\(^{-1} \) kpc\(^{-2} \). That corresponds to 0.0004 \( M_\odot \) yr\(^{-1} \) in the 1 kpc wide annulus we are using as an example. This corresponds to approximately six Orion Nebulae over an area of 40 kpc\(^{2} \). This is the level of activity that we should expect to find on average at any given moment.

The azimuthally averaged SFR profiles are shown in Figure 18 as ratios of SFR\( H_\alpha \) and SFR\( FUV \) to SFR\( V \). We are able to measure SFRs from FUV and V-band images out to 3–7 disk scale lengths. Again, Hα is not detected as far out as V and FUV emission, and so is not a good indicator of star formation in the outer disk (see Hunter et al. 2010 for a discussion of this issue, as well as Meurer et al. 2009 and Lee et al. 2009). However, in the region where Hα and FUV emission overlap, the two measures of SFRs track each other well except in NGC 4163. This is obvious to the eye as parallel curves in Figure 18. In addition, within the likely systematic uncertainties, the absolute levels of the Hα and FUV SFRs are the same except in the center of DDO 53, within 1.5 \( R_D \) of NGC 4163, and in I Zw 115. In those cases the Hα SFR is significantly lower than the FUV SFR, implying a higher SFR several 100 Myr ago compared to the most recent 10 Myr.

These three measures of the SFR can track star formation over different timescales: 10 Myr, several times 100 Myr, and over 1000 Myr, respectively, for SFR\( H_\alpha \), SFR\( FUV \), and SFR\( V \). What then do these profiles tell us about the radial variations in the star formation histories in our five galaxies?

**DDO 53.** In the central 2 \( R_D \) of DDO 53 the SFR over the recent 10–300 Myr has been higher than the average in the past by factors of 3–4, while in the outer disk the SFR is suppressed by similar factors compared to the past average. Recent star formation in DDO 53 has retreated to the central regions. This is also reflected in the color profiles: FUV–NUV is constant in the inner disk scale length and becomes progressively redder beyond that; \( B – V \) is slightly bluer in the central regions.

**DDO 86.** Star formation in DDO 86 has been approximately constant over the past 1 Gyr at all radii with only a slight depression of the current SFR relative to the average past rate in the center. Similarly, the FUV–NUV color is nearly constant with radius.

**DDO 133.** In the central 0.5 \( R_D \) of DDO 133 the SFR over the recent 10–300 Myr is depressed compared to the average in the past by factors of several, but beyond that the SFR has been roughly constant until it drops a bit beyond 2 \( R_D \). The FUV–NUV color is red in the center and becomes steadily bluer with radius until it turns a bit redder again at 2 \( R_D \). \( B – V \), on the other hand, is nearly constant with radius to 2.5 \( R_D \). This flat color profile implies that the longer timescale star formation history has been the same throughout the entire galaxy, including the outer edges.

**NGC 4163.** In the central 1 \( R_D \) the SFR averaged over the past several 100 Myr is comparable to that measured over the past 1 Gyr, but the SFR measured over the past 10 Myr is down by a factor of about 10. Thus, in the center of NGC 4163 star formation has recently declined significantly. Outside of the central 1 \( R_D \), the recent star formation activity is depressed relative to the past average by a factor of up to 30. It seems that only the center of this galaxy is currently engaged in significant star formation. In terms of the colors, FUV–NUV becomes steadily redder with radius beyond 1 \( R_D \). \( B – V \) becomes redder to 2.5 \( R_D \) and then is constant with radius.

**IZw 115.** I Zw 115 is a BCD, which are often assumed to be starburst or post-starburst systems. In the case of I Zw 115, however, the SFR\( FUV \) is comparable to the average past rate in the central 2 \( R_D \) and is depressed by factors of a few in the outer disk. However, the most recent star formation, as seen in Hα, is down by a factor of order 10 where it is detected in the inner 2.5 \( R_D \). Thus, star formation in the center of I Zw 115 was much higher in the past several 100 Myr than it is now. In that sense, it is post-starburst. The FUV–NUV color reflects this, becoming steadily redder with radius.

4. GAS MORPHOLOGY AND KINEMATICS: NO NORMAL GALAXIES

4.1. DDO 86 and a Hole in the ISM

The H\(_1\) distribution in DDO 86 is dominated by a central hole with a higher density gas ring around it. The hole is not as distinct as a simple circular region of low gas density; there are several minima and some gas “clouds” within the shell. But the general hole/ring morphology is clearly present. The hole, measured from the inner edge of the shell, has a diameter of order 5.2 kpc, the structure, measured from the midpoint of the shell, has a diameter of order 6.9 kpc, and the shell itself is of order 2.0 kpc thick. The mass of H\(_1\) in the shell, about \( 4 \times 10^8 \) \( M_\odot \), is 41% of the total mass of the galaxy. Many other dwarf galaxies exhibit this type of morphology (see, for example, Dopita et al. 1985; Puche et al. 1992; Martin 1998; Walter & Brinks 1999; Parodi & Bingelli 2003; Cannon et al. 2005, 2011; de Blok & Walter 2006). One galaxy with a similar appearance and similar hole/shell dimensions and relative mass is DDO 88 (Simpson et al. 2005).

Although DDO 86 has a beautifully normal bulk rotation velocity field, at almost every point within the shell and hole...
there are weak non-circular motions as well. In particular there appears consistently to be a component that is $\sim 10$–$25$ km s$^{-1}$ off the rotation speed at a given position. This suggests that the shell is young enough to still be expanding at $\sim 10$–$25$ km s$^{-1}$.

 McCray & Kafatos’ (1987) model of stellar blown shells give an age of $60$–$150$ Myr for a shell observed with an expansion velocity of $10$–$25$ km s$^{-1}$ and a radius of $2.6$ kpc. If the ambient gas density before the shell formed was of order $0.1$ cm$^{-3}$, then $100$–$1600$ stars with masses greater than $18 M_\odot$ would have been required to produce the shell. That means that a substantive burst of star formation took place in the center of DDO 86 in the past $200$ Myr.

However, neither the FUV–NUV color in Figure 9 nor the SFRs in Figure 18 is consistent with this picture. The H$\alpha$ minima regions in the center yield an FUV–NUV of $0.24 \pm 0.02$, which indicates an age of order $550$ Myr for a Chabrier stellar IMF, a single starburst population, and a metallicity of $0.008$ (Bruzual & Charlot 2003). A single age stellar population at $200$ Myr of age should have an FUV–NUV color of order $-0.4$. Similarly, the SFR profiles shown in Figure 18 are contrary to expectations: the SFR$_{\text{H}\alpha}$/SFR$_{V}$ and SFR$_{V}$/SFR$_{\nu}$ ratios should show a bump up in the center, indicating a higher recent SFR compared to the average over a long timescale. Instead these ratios show a slight dip in the center. These discrepancies could be due to a combination of factors: for example, a more complex star formation history (see, for example, Cannon et al. 2011), contamination of the younger stellar population by an older underlying disk, local extinction, and UV calibration uncertainties (see Zhang et al. 2011).

4.2. Stellar Bars

One of our galaxies clearly has a stellar bar and a second galaxy probably has one: the bar in DDO 133 is obvious from a casual look at the V-band image, while that in DDO 86 is suspected because the deep V-band image shows a different isophote shape compared to shallower images. Both of these galaxies have normal bulk rotation fields. In DDO 133 we see a slight S-shape to the iso-velocity contours (Figure 15) that is characteristic of a barred disk. Such a feature is not obvious for DDO 86 (Figure 14). Interestingly, DDO 133 also has UV-bright clumps all the way out to two disk scale-lengths and large UV-bright regions are found especially at the ends of the bar. H$\alpha$ profiles are double-peak in the H$\alpha$ minimum that corresponds to a concentration of UV clumps on the northeastern edge of the bar. And H$\alpha$ profiles show broad features, probably due to multiple components, in the H$\alpha$ minima to the east of the bar and in the region of bright UV emission to the south of the bar.

4.3. Peculiar Kinematics

Two of our galaxies are particularly kinematically peculiar. Extracting the bulk rotation from DDO 53 and NGC 4163 was difficult and the rotation curve for DDO 53 is not meaningful outside a radius of $0.9$ kpc (but see Oh et al. 2011). Furthermore, the rotation speeds that were measured are small, less than $10$ km s$^{-1}$. In the outer disk, the H$\alpha$ associated with NGC 4163 sports two “spiral arm” like features—one on the southern edge extending to the west and the other on the northern edge pointing to the northeast (Figure 4). In addition, the iso-velocity contours show a strange extension to the southwest (Figure 16). H$\alpha$ profiles show complex, multiple (3–4) components outside of the central H$\alpha$ bright region, especially in the H$\alpha$ extension to the south of center and along the ridge to the west of the central region. In DDO 53, the region of highest velocity dispersion is found along a grand arc on the southeastern edge of the H$\alpha$ distribution, where the iso-velocity contours are most bunched together (Figure 13). Except for the southern of the two H$\alpha$ clumps, the H$\alpha$ profiles are everywhere broad and complex with multiple components. In neither galaxy is it obvious from the optical morphology that anything unusual is going on in these galaxies other than the fact that the current star formation is concentrated to the center in both systems.

IZw 115 potentially has an excuse at disturbed kinematics, and the bulk velocity field, although more obvious than in DDO 53 and NGC 4163, is not clean. The detached region to the southwest (Figure 5) could be a tiny companion interacting with IZw 115. The gas associated with IZw 115 extends to that region, and the region itself seems to be rotating at a different position angle from the main body of IZw 115. The signal to noise is low, but the H$\alpha$ profiles are everywhere complex, indicating multiple (3–4) velocity components. IZw 115 has one central star-forming complex, as is characteristic of BCDs.

5. COMPARISON OF STARS, GAS, AND STAR FORMATION

To compare the stars and gas, in Figures 8–12 we show the azimuthally averaged surface photometry plotted against radius from the galaxy center. The top panel in the graph includes properties of the gas: the gas surface density $\Sigma_{\text{gas}}$ and velocity dispersion of the rotational component $\sigma_{\text{rot}}$. The second panel shows the optical and UV properties: $V$, $H\alpha$, and NUV surface photometry. The third and fourth panels show optical and UV colors: $(B - V)_0$, and $(\text{FUV} - \text{NUV})_0$. From comparison of H$\alpha$ and optical images (Figures 1–5), we see that the H$\alpha$ does not extend much further than the stars in DDO 53 and DDO 133. In DDO 133, there are bright UV regions that extend almost to the edge of the observed H$\alpha$, and the big UV-bright complexes are found roughly near the ends of the stellar bar. In DDO 53, NGC 4163, and IZw 115 the recent star formation is concentrated to the center, and we do not find any UV-bright knots in the outer disk. In DDO 86 there is a central hole in the gas. Many of the UV knots are associated with clouds around this hole.

In Figure 19, we plot the azimuthally averaged log $\Sigma_{\text{gas}}$ against log SFR for the three star formation measures: SFR$_{\text{FUV}}$, SFR$_{H\alpha}$, and SFR$_{V}$. This is similar to plots by Bigiel et al. (2010) for pixel-by-pixel distributions. We see a general trend of higher SFR for higher gas density except for some radii in DDO 53 and NGC 4163. Those two galaxies are also most peculiar kinematically.

The Toomre (1964) model of a differentially rotating thin disk appears to explain star formation in the inner disks of spirals (Kennicutt 1989). In this model, there is a critical gas density $\Sigma_c$ above which the disk is unstable to ring-like perturbations in the radial direction. Gas that is above $\Sigma_c$ will form star-forming clouds; gas below $\Sigma_c$ is stable to cloud formation. The ratio of $\Sigma_c/\Sigma_c$ is shown as a function of radius in the five galaxies in the top panels of the graphs in Figures 8–12. $\Sigma_c/\Sigma_c$ is everywhere less than one. The ratio is extremely low throughout DDO 53 (<0.03), but that may be due to the extremely low rotation speed in that galaxy. The ratio of $\Sigma_c/\Sigma_c$ is low (<0.3), but roughly constant where it was measured over the disk of IZw 115. For the other three galaxies—DDO 86, DDO 133, and NGC 4163—$\Sigma_c/\Sigma_c$ rises to a peak outside the center and then declines to the outer disk. In DDO 133, for example, the NUV surface photometry extends to the regime where $\Sigma_c/\Sigma_c$ is 0.05,
Figure 19. Azimuthally averaged log $\Sigma_{\text{gas}}$ vs. log SFR for three star formation measures: SFR$_{\text{FUV}}$, SFR$_{\text{H}\alpha}$, and SFR$_{\text{H}_\beta}$. The solid, slanted lines are lines of gas depletion times; the lines are labeled with the gas depletion timescale in years. (A color version of this figure is available in the online journal.)

well below the value to permit star formation. So, how is star formation proceeding at very low gas column densities?

One possibility is that clouds of high enough density for star formation form in outer gas disks through turbulence compression (Elmegreen & Hunter 2006). Our H i maps are of low spatial resolution, but along the northern edge of DDO 86, for example, there appear to be two H i clouds that stand out. Both have peaks that are 6σ above the surrounding gas. At $10^6.44''$22.4, 60°23'55'' and at $10^6.44''$26.17, 60°24'01'' (J2000), the eastern cloud has a mass of $(7 \pm 3) \times 10^6 \, M_\odot$, a diameter of order 2 kpc, and a surface density of order $2 \, M_\odot \, \text{pc}^{-2}$. The western cloud has a mass of $(4 \pm 2) \times 10^6 \, M_\odot$, a diameter $\leq 1.4$ kpc, and a surface density of order $1 \, M_\odot \, \text{pc}^{-2}$. These surface densities are right at the limits where star formation is found to occur in other galaxies: $2-5 \, M_\odot \, \text{pc}^{-2}$ (Gallagher & Hunter 1984; Skillman 1987; Taylor et al. 1994; Meurer et al. 1996; Hunter et al. 1998, 2001; van Zee et al. 1998), but much lower than would be expected for significant quantities of star formation (Bigiel et al. 2010). Thus, clouds like these could potentially form stars. Yet these clouds, at a distance of five disk scale lengths (9.2 kpc) from the center of the galaxy, are surrounded by low column density gas ($1 \times 10^{20} \, \text{cm}^{-2}$).

6. DISCUSSION

6.1. Radial Profiles

Deep V-band images of four dwarf irregular galaxies and one BCD galaxy have been used to measure surface photometry down to $\sim 29.5$ mag arcsec$^{-2}$. Deep B-band images were also used for three of these galaxies. The surface brightness distributions in the V-band were found to be exponential in radius out to 5 inner disk scale lengths ($R_D$) in two cases (DDO 53, DDO 86), 8 $R_D$ in two other cases (NGC 4163, I Zw 115), and 3 $R_D$ in one case (DDO 133). A clear break marks the transition from an inner exponential profile to an outer, steeper exponential profile in three cases. In two of these (DDO 53, DDO 86), the break occurs at $\sim 3 \, R_D$, and in the third (DDO 133) it occurs at $\sim 1.8 \, R_D$. In two cases where the $B - V$ color information goes beyond the break, one (DDO 53) has a transition in the color profile from a slight reddening in the inner disk (from $0.12 \pm 0.005$ to $0.36 \pm 0.03$, a difference of 0.24 mag) to an increasing blueness (down to $-0.13 \pm 0.3$ at the last point shown, a difference of 0.49 mag) in the outer disk; the other (DDO 133) has a relatively flat color profile overall (variations up, down, up, and down again with radius covering an extreme of $0.47 \pm 0.005$ to $0.30 \pm 0.01$, a difference of 0.17 mag).

The remarkable regularity of these underlying exponential disks contrasts with the irregularity observed in this Hubble morphology class. Such regularity has been observed in the inner parts of dwarf galaxies for a long time (Patterson & Thuan 1996; Hunter et al. 1998; Bremnes et al. 1998, 1999; Hopp 1999; van Zee 2000; Taylor et al. 2005; Hunter & Elmegreen 2006; Amorín et al. 2007; but for exceptions see, for example, Hunter & Gallagher 1985; Hunter & Plummer 1996; K. Herrmann et al. 2011, in preparation), but now we see that it extends into the extreme outer disk as well. Somehow the accumulated star formation and radial mass migration over a Hubble time converts the irregular activity at any one time into a standardized disk profile. This conversion seems to be done without grand design spiral or bar torques (only one case, DDO 133, is clearly barred and none have obvious spirals, but see below), and without significant shear in H i velocity maps for at least the inner exponential parts. A lack of bars would mean that the Hohl (1971) mechanism for the formation of exponential profiles by bar and spiral torques is not operating. A lack of shear would suggest that the Lin & Pringle (1987) mechanism in which the SFR is proportional to the shear viscosity is also not operating.

GALEX UV observations were also examined for these galaxies. In four cases, the NUV observations go out as far in the disk as the deep V-band images. The NUV profiles are also exponential and have about the same scale lengths as the V-band profiles. In two of the three cases with exponential breaks in V-band, there is also a break in the NUV profile at the same radius. In the one case with a $B - V$ color change at the break radius (DDO 53), there is no evident break in the NUV profile at all, even though it extends for one inner disk scale length beyond the V break. This lack of a NUV break in DDO 53 could be related to the increasing blueness with radius seen in $B - V$: the blueness could compensate for the steeper mass profile seen in the V-band and make the NUV-band appear continuous.

The similarity between the NUV and V-band profiles introduces another puzzle about the formation and evolution of these galaxies. The average radial profile of the SFR over the last several tenths of a Gyr, as observed in the NUV, follows the underlying mass distribution established by star formation and radial migration over the last Gyr or more, as observed in V. There was no radial mixing of these disks on timescales longer than $\sim 1$ Gyr because that would significantly affect the color profiles. For example, the outer exponential disk should be redder than the inner disk if it was formed or augmented by spiral arm scattering of inner disk stars $\sim 1$ Gyr old or more (e.g., Roškar et al. 2008). Such a color change has been observed for spiral galaxies (Bakos et al. 2008), but in DDO 133 there is no color change and in DDO 53 the outer disk is bluer. Neither galaxy has spiral arms anyway.

Consider an example using the population synthesis models of Bruzual & Charlot (2003). For a Salpeter IMF (the results
are essentially the same for a Chabrier IMF), a burst of star formation older than \(10^8\) yr has NUV - \(V\) > 2 mag, and one older than 1 Gyr has NUV - \(V\) > 3.5 mag. Young stars have NUV - \(V\) < -1. These values were determined by integrating the model stellar population spectra over the filter functions used in the two passbands. Their plot is shown in Figure 21 of our previous paper (Hunter et al. 2010). If we took a group of stars that formed \(10^9\) years ago and moved it to a different place in the disk, then that group would be 3.5 mag fainter in NUV than in \(V\) because of population fading. This 3.5 mag difference means that the displaced group may still stand out in \(V\) but be nearly invisible in NUV. Then the two passbands will have different intensity distributions. This difference of 3.5 mag is so large that even with more continuous star formation than a burst, and with some mixing of the group into other stars, there should still be a significant difference between the NUV and \(V\) intensities of stars \(>1\) Gyr old. Our observations do not show this difference, however. The similarity between the NUV and \(V\) profiles in our galaxies implies that there has not been much migration of stars from the inner disk to the outer disk on timescales longer than \(\sim 1\) Gyr.

The observation of similar radial profiles in NUV and \(V\) bands (and also in the J band for at least the inner regions—see Hunter & Elmegreen 2006) suggests that star formation occurred at a steady rate. Leroy et al. (2008) also found that the SFR in dwarfs was about constant over a Hubble time. The similarity between the NUV and \(V\) profiles in our previous surveys. The H\(_\alpha\) radial profiles extend out to only 2 \(R_D\) or 3 \(R_D\). In the case with the shortest \(V\)-band break radius (DDO 133), the H\(_\alpha\) extends beyond the breaks in \(V\) and NUV and also has a break at the same radius. In all of the galaxies, the H\(_\alpha\) profile is roughly similar to the NUV profile, including local deviations from the exponential. This can be seen in Figure 20 where we plot the ratio SFR\(_{FUV}\)/SFR\(_{H\alpha}\). The implication is that current SFRs, seen in H\(_\alpha\), are about the same at each radius as the average rate over the last few hundred Myr. The H\(_\alpha\) rates today are also about the same, to within a factor of \(\sim 3\), as the \(V\)-band long-term average rates in three of the galaxies (see Figure 18). The two galaxies where these rates differ the most are NGC 4163, which has highly disturbed kinematics as mentioned above (and a current rate in H\(_\alpha\) and the UV that is much lower than the \(V\)-band average at mid-radius), and the BCD galaxy, IZw 115, which also has a low H\(_\alpha\) compared to \(V\) in the inner parts (although the UV rate is the same as the \(V\) rate there). IZw 115 is evidently post-starburst.

### 6.2. Hydrogen Gas

The final piece of evidence related to star formation and galactic structure is the gas distribution. For this, we examined H\(_I\) observations taken at the VLA for this project. The H\(_I\) radial profiles are smoothly declining but flatter than the stellar light profiles in DDO 86, NGC 4163, and IZw 115, and about the same as the stellar light in DDO 133. In DDO 86, there is an H\(_I\) hole in the center and a ring around it that is not present in the optical. These trends show up in the SFR–\(\Sigma_{gas}\) diagrams of Figure 19 too. DDO 86, DDO 133, and IZw 115 have steep near-power-law relations between the \(V\)-band or FUV SFRs and the H\(_I\) column densities, with slopes of \(3\pm1\) to \(4\pm1\). NGC 4163 and IZw 115 have a scattering of points with a somewhat more organized relation for FUV than \(V\)-band SFRs. The near power laws are consistent with other studies of star formation and
H I column density, which also show steep slopes. Bigiel et al. (2010) got a slope of 1.7 for the relation between SFR per unit area and H I column density in faint outer regions. Their plot of $\Sigma_{H_I}$ versus $\Sigma_{SFR}$ for dwarfs in their Figure 8 is similar in shape to ours for the FUV SFR in Figure 19. Star formation follows unseen CO (Bigiel et al. 2011), which is a small fraction of the H I mass in these faint regions (Schruba et al. 2011). The timescale for conversion of H I into stars is the ratio of the x-axis values to the y-axis values in Figure 19, or approximately $10^{11}$ yr (see also Bigiel et al. 2010).

The H I distributions are clumpy with giant clouds that appear associated with star formation. These clouds are most obvious in the inner regions where the SFRs are highest, although faint H I clouds can also be seen in the outer parts where past-average SFRs are very low. Observable clouds typically have masses of around $10^7 M_\odot$ or larger. A few faint clouds in the outer part of DDO 86 with masses of several $\times 10^6 M_\odot$ were discussed as possible future sites of star formation. In general there are no spiral arms or systematic streaming motions in H I. The velocity fields reflect normal rotation curves except for NGC 4163 and DDO 53.

The most extended H I rotation curves are available for DDO 86, DDO 133, and IZw 115. The first two have two rising inner rotation curves that flatten out at the break radius in the V-band profile. The third has a rising rotation curve in the inner part and a falling rotation curve in the outer part, with no break in the exponential profile for comparison. There could be a small companion galaxy near IZw 115 that affects the rotation curve in the outer part. The coincidence in two cases between the turnover point in the H I rotation curve and the break point in the photometric radial profile is interesting but maybe not significant. In our larger sample (Hunter & Elmegreen 2006), there was no correlation between the photometric break radius and the rotation curve turnover radius: only one case had these features at the same radius, five had the break at a larger radius than the turnover, and four had the break at a smaller radius than the turnover. In larger spiral galaxies, the exponential break radii are typically at $\sim$2−5 $R_D$ (Pohlen & Trujillo 2006) and the turnover radii are at $\sim$1 $R_D$, so there is no coincidence of radii for spirals either.

The H I rotation speeds in these dwarf galaxies are typically low: in the three cases with extended rotation curves, they peak at 40 km s$^{-1}$ for DDO 86 and DDO 133, and at 15 km s$^{-1}$ for IZw 115. The H I velocity dispersions are approximately constant with radius at around 10 km s$^{-1}$. For IZw 115, the average rotation speed is comparable to the velocity dispersion inside 3 $R_D$ and possibly in the outer regions too where the rotation curve drops. At the peak of the rotation curve in IZw 115, the ratio of the rotation speed to dispersion is remarkably low, $\sim$1.4. Such slow rotation gives IZw 115 very little dynamical integrity, yet it has a near-perfect exponential disk for 8 $R_D$.

Slowly rotating galaxies should be easily perturbed by interactions with other galaxies and dark matter concentrations, by clumping instabilities in their disks, and by gas blowout during star bursts. This sensitivity to asymmetric forcing and rapidly changing potentials makes the long-range exponential structure of the disks difficult to understand, unless it results from such forcings. The uniform rotation observed in two out of five cases suggests that their recent lives have been quiescent, at least for the last several rotation periods in their outer regions. The rotation period at the outer radius of detection for the H I rotation curve in DDO 133 is 0.9 Gyr. For DDO 86, it is 1.9 Gyr. The SFR ratios shown in Figure 18 are roughly consistent with this long-term quiescence.

The maps of velocity dispersion, “mom2,” in Figures 13–17 show an inverse correlation with the maps of column density, “mom0,” in the sense that higher column densities correspond to lower velocity dispersions. We found this before for NGC 2366 (Hunter et al. 2001). Figure 21 shows this anticorrelation better. Each panel shows a map of mom0 in red and mom2 in green. Overlapping regions turn out yellow. The maps show mostly red and green regions with only a little yellow. This means that the dispersion is high where the column density is low, and vice versa. An anticorrelation is roughly consistent with pressure uniformity in the sense that low density regions have higher turbulent speeds. Piontek & Ostriker (2005) found this in simulations of the magnetorotational instability.

Trujillo & Bakos (2010) looked for a correlation between possible inflection points in the H I velocity dispersion and exponential break radii in the disks of local spiral galaxies. They were considering that the breaks could result from gas disk flaring, but found nothing. We see nothing like that here either.

6.3. Gravitational Stability

The H I appears to be gravitationally stable by itself. The ratios of the gas surface densities to the Toomre (1964) threshold densities are 0.6 or less in DDO 86 and DDO 133, 0.1 or less in NGC 4163, and 0.3 in IZw 115. There are stars mixed with the gas, however, and the stellar velocity dispersions are probably not much larger than the gaseous dispersions, considering the low rotation speeds. This means that stars contribute to the instability in approximate proportion to their mass (Jog & Solomon 1984). We have estimated the mass surface densities of stars in our galaxies using the V-band radial profiles and the $B − V$ colors, where available. The calibration comes from $M/L$ tables in Bell & de Jong (2000). We find that the stellar mass surface densities in the outer parts of our galaxies are comparable to the gas surface densities, or slightly smaller, to within a factor of a few. This can also be derived from the SFRs given in Table 8, which are $\sim 10^{-4.8} M_\odot$ yr$^{-1}$ kpc$^{-2}$ in the V-band at $\mu_V = 29.5$ mag arcsec$^{-2}$. Multiplying this by $10^{10}$ years and converting to pc$^{-2}$, the result is a total stellar surface density today of $\sim 0.2 M_\odot$ pc$^{-2}$ in the far-out parts. Figures 8–12 give $\Sigma_{gas}$ there, and the average is about $1 M_\odot$. Thus, gravitational forcing from stars may be $\sim 20\%$ of that from gas during the growth of an instability, leading to an upward correction to the surface density ratios by $\sim 20\%$. The correction would be larger in the inner regions, where the stellar contribution is larger. These corrections make DDO 86 and DDO 133 only slightly stable, which is typical for galaxies. For example, Leroy et al. (2008) showed that the gas+star stability parameter equals about 1.5 for a wide range of radii inside dwarfs and spirals. The corresponding ratio of column density to critical column density is the inverse of this, 0.6. This is not much different than it is for DDO 86 and DDO 133.

NGC 4163 is not a good case for this stability analysis because the rotation curve is peculiar (Section 4.3). IZw 115 could also have a peculiar rotation curve because of the companion galaxy, but even in the inner parts where the rotation curve is rising, the H I column density is less than the critical value by a factor of five. These inner parts are probably post-starburst, however, so they could well be very stable.
The situation with instabilities is more complicated than this because all of these galaxies have relatively thick disks, as inferred from the high ratios of H\textsc{I} velocity dispersion to rotation speed. Thickness \( H \) decreases the in-plane accelerations from self-gravity at wavenumber \( k \) by a factor of \( (1 + kH)^{-1} \) (Vandervoort 1970), which should be \( \sim 0.5 - 0.7 \) in our case. This lowers the effective stability ratio \( \Sigma / \Sigma_{\text{crit}} \) by the same factor, since \( \Sigma_{\text{crit}} = k \sigma (1 + kH)/\pi G \) for \( Q' = 1 \) with thickness corrections. Here, \( \sigma \) is the velocity dispersion, \( \Sigma \) is the mass column density, and \( Q' = k \sigma (1 + kH)/\pi G \Sigma \) is the thickness-corrected Toomre \( Q \) parameter for epicyclic frequency \( \kappa \) (Elmegreen 2011). The ratios derived above for gas+stars in DDO 86 and DDO 133 without thickness corrections are comparable to those given by Leroy et al. (2008) for dwarf and spiral galaxies without thickness corrections. Therefore both are likely to have comparable stability ratios when thickness is included, which means both are slightly more stable than without the thickness correction. The ratios for the outer parts of dwarfs would still be smaller than they are for spirals.

Gravitational instabilities in dwarf irregular galaxies should look different than they do in large spiral galaxies. The characteristic length for spirals or clumps that form in a gravitational instability lies in the range \( \sigma^2 / (\pi G \Sigma)(1 \pm (1 - Q^2))^{-1} \). This is centered at \( \sigma^2 / (\pi G \Sigma) \), which should be compared with the disk scale length. In dwarfs with comparable velocity dispersions for the gas and stars, we can use the total mass column density for \( \Sigma \) and include both components this way. In the outer parts of dwarf galaxies, \( \Sigma \sim 10 M_\odot \text{pc}^{-2}, \Sigma \sim 0.5 \Sigma_c \), and \( \sigma \sim 10 \text{ km s}^{-1} \), so \( \sigma^2 / (\pi G \Sigma) \sim 1.4 \text{ kpc} \). For spiral galaxies, the length scale is about the same because the velocity dispersion for the dominant stars is higher by a factor of \( \sim 3 \), and the mass column density is higher by a factor of \( \sim 10 \). Dwarf galaxies have smaller exponential scale lengths than spirals, however. Three of the dwarfs studied here have \( R_D < 0.7 \text{ kpc} \) and two others have \( R_D \sim 2 \text{ kpc} \) (Table 4). In spiral galaxies, \( R_D \) ranges between \( \sim 1 \) and 5 kpc (van der Kruit 1987), which is larger than in dwarfs by a factor of two or more. This difference means that the characteristic length of a significantly gravitating structure in a large spiral galaxy readily fits into the disk, allowing coherent structures like spiral waves to form. Most dwarfs are too small for this. In addition, the bright parts of dwarf galaxy disks occur in the rising parts of their rotation curves, but the main parts of spiral galaxy disks are in the flat parts of their rotation curves. Gravitational perturbations therefore tend to grow as unsheared clumps in the dwarfs, but they produce spiral wakes and long sheared arms in spirals.

Some dwarf galaxies have spirals, but this situation is rare (Schombert et al. 1995). A dwarf elliptical in the Virgo cluster, IC 3328, has a weak spiral, but it may be confined to a thin sub-component of the main stellar disk where the gravitational length is short (Jerjen et al. 2000; De Rijcke et al. 2003; Lisker & Fuchs 2009). Other dwarf spirals in Virgo were observed by Barazza et al. (2002).

The same considerations apply to the far-out parts of spiral galaxies, where \( \Sigma \) is comparable to that in dwarfs. Then the characteristic length for instabilities may be 10 times higher than it is in the inner spiral disk, and locally much larger than the scale length. Thus the outer parts of spiral disks should have difficulty generating self-gravitating waves on their own, like dwarf galaxies. However, the outer disks of spiral galaxies can have spiral waves that propagate there from the inner disk (Bertin & Amarisco 2010) or were resonantly excited by perturbations from the inner disk (Debattista et al. 2006). Dwarf galaxies have neither source of waves and should produce only clumps of self-gravitating gas.

Disk stability is also relevant to the origin of double exponential profiles, according to the model by Debattista et al. (2006). This model involves angular momentum transfer around bars and spirals. Debattista et al. (2006) showed that the inner parts of barred galaxies with single exponential profiles get flatter with time, out to the outer Lindblad resonance of the spiral that is driven by the bar. The original exponential disk then shows up as the outer steep part of the double exponential, and the bar-modified part is the inner flat region. The degree of flattening depended on \( Q \) in these models. Disks that were more gravitationally stable, with higher \( Q \), did not evolve as much as less stable disks. This result suggests that dwarf galaxies that are weakly self-gravitating may not be responsive to bar torques that modify a single exponential into a double exponential.

Our galaxies with the highest ratios of \( \Sigma_{\text{gas}} / \Sigma_{\text{crit}} \), namely DDO 86 and DDO 133, also have the most obvious breaks in their exponential profiles. DDO 133 is a barred galaxy too. However, the break radius in DDO 133 is at the end of the bar and not the end of a spiral as in the Debattista et al. model. Also in DDO 86, the star formation region and inner bright core in Figure 2 is elongated in the east–west direction, reminiscent of a bar. The end of this elongation corresponds to the break radius. Similarly in DDO 53, there is an elongation of the main disk star-forming region along a position angle of \( \sim 150^\circ \), which is transverse to the major axis. The deprojected length of this elongation is comparable to the break radius. There is not enough H\textsc{I} data to determine \( \Sigma_{\text{gas}} / \Sigma_{\text{crit}} \) for this galaxy. These observations suggest that the inner exponentials of our galaxies were made flatter than the outer exponentials by mass transfer connected with a bar. There are no spirals here, so the bar may be doing here what the spirals did in Debattista et al. (2006).

We looked for a correlation between photometric breaks and the presence of bars in our larger sample (Hunter & Elmegreen 2006). Out of 22 dwarf galaxies with double exponentials of the type discussed here, 8 have some evidence for a bar (even if they are not classified as Hubble bar types), and the rest do not. DDO 133, studied here, was one of the barred cases with a double exponential recognized in that previous study. Among the barred dwarfs, the ratio of the break radius to the end of bar radius is \( 1.8 \pm 0.6 \) on average. Since there are breaks without bars and bars without breaks, we do not see a clear correlation between the two at this time.

### 6.4. Two Peculiarities

We summarize this discussion by highlighting two peculiar things about the present observations: the extraordinarily regular exponential disks in dwarf irregular galaxies, and the continuity of star formation throughout these disks and over time. Exponential disks are made in part by cosmological infall (Freeman 1970; Fall & Efstathiou 1980; van der Kruit 1987) and subsequent dynamical torques from self-gravitating disk structures. There is no regularity to these structures in dwarfs and no systematic presence of bars or spirals. There are only clumps of star formation and maybe some old disk stars mixed in with those clumps. It is conceivable that the clumps of star formation make or maintain the exponential disk, as in numerical simulations of equally clumpy galaxies in the early universe (Bournaud et al. 2007). Or, there could be bar-like dark matter halos (Bekki & Freeman 2002; Tutukov & Fedorova 2006) that redistribute
angular momentum, while also driving in gas to fuel occasional low-level bursts (Hunter & Elmegreen 2004). As for star formation itself, this complex process involving mostly gas seems to follow the underlying exponential disk of old stars better than one would expect from such a stochastic process. Leroy et al. (2008) found the same thing for dwarfs and the outer parts of spiral galaxies. Molecular cloud distributions follow the stellar exponential even when the molecules are an extremely low fraction of the gas mass (Schruba et al. 2011). How do the molecules know to do this? In the current paradigm, star formation follows only the molecules, and molecular abundances depend mostly on the pressure (e.g., Bigiel et al. 2008), but why does this end up reinforcing the underlying exponential disk? There is a purely radial dependence to the cloud and SFRs, in addition to a gas dependence, as in the exponential disk? There is a purely radial dependence to the cloud and SFRs, in addition to a gas dependence, as in the dynamical law of star formation, where the rate is determined by the orbit time (Kennicutt 1998). Bigiel et al. (2010, Figure 7) also found that for a given H I column density, the SFR decreases with increasing radius in spiral and dwarf galaxies. The problem with this is that orbital timescales usually vary with radius as a power law, not an exponential.

Ostriker et al. (2010) proposed that the SFR scales with the total gas surface density multiplied by the square root of the midplane density from stars and dark matter. They get good agreement between this prediction and the radial profiles of star formation in several spiral galaxies. The present results suggest that if this quantity applies to dwarf irregulars, then it should also be proportional to the column density of existing stars so that the color profile does not change much over at least a Gyr. In fact, they find the SFR per unit gas mass proportional to the surface density of existing stars and dark matter in the case where the vertical velocity dispersion is constant (because then the midplane density scales with the square of the stellar and dark matter column density). This matches our result fairly well because the gas column density varies weakly with radius.

Another model is that in highly stable regions, molecular cloud formation and star formation is somehow triggered by field stars. Perhaps Type Ia supernovae are important, or the turbulence that is driven by these supernovae and other fieldstar pressures. Star formation would then follow the underlying stellar density as long as there is enough gas to compress. Since the rate is approximately constant over time, sequential triggering by young star pressures could also be important. Then star formation would move around as illustrated by Gerola et al. (1980). A way to check these models would be to find triggering sources near young stars. Also, the SFR should be more tightly correlated with the stellar column density than with the gas column density, as long as there is enough gas to be triggered.

The break radii in exponential disks could be a clue to these processes if the properties of the gas and cosmic rays near regions of star formation were found to differ inside and outside of this radius. In the present sample of galaxies, we found no clear correlation between the existence of a break and other properties, such as bars, spirals, color jumps, or the turnover in the rotation curve. We found no such correlations in our bigger sample either (Hunter & Elmegreen 2006).

7. SUMMARY

We present ultra-deep V, B, and GALEX UV images obtained in order to detect and measure the extreme outer stellar disks of a sample of four dIm galaxies and one BCD galaxy. Our V-band surface photometry extends to 29.5 mag arcsec\(^{-2}\). We convert our new FUV and V-band photometry, along with Hz photometry obtained in a larger survey, into radial SFR profiles that are sensitive to different timescales—from 10 Myr to the lifetime of the galaxy. We also present H\(\alpha\) emission data and compare the stellar distributions, surface brightness profiles, and SFR profiles to H\(\alpha\) emission maps, gas surface density profiles, and gas kinematics. Our data lead us to two remarkable general observations.

First, the exponential disk in these dwarf irregular galaxies is extraordinarily regular. We observe that the stellar disks continue to decline exponentially as far as our measurements extend. In addition, as is common in outer spiral and dwarf disks, the slope of the V-band surface brightness profiles changes abruptly in the outer disks in most of our systems. In three of our galaxies the outer profile becomes steeper, but the break in the V-band surface brightness profile is mimicked in the NUV profile for two of these systems. The galaxies are lumpy with star formation and the H\(\alpha\) distributions and kinematics have significant non-ordered motions. Yet, the regularity of the exponential profiles in spite of these peculiarities indicates that the sporadic processes that have built the disks—star formation, radial movement of stars, and perhaps even perturbations from the outside—have, nevertheless, conspired to produce standard disk profiles.

Second, there is a remarkable continuity of star formation throughout these disks over time. In four out of five of our galaxies the SFR in the outer disk measured from the FUV tracks that determined from the V-band, to within factors of a few (<5), although the FUV-derived rate reflects a shorter timescale than the V-band derived rate. This requires star formation at a fairly steady rate over the galaxy’s lifetime. But how the galaxy achieves this is not clear. The H\(\alpha\) surface density profiles generally decline with radius more shallowly than the stellar light and, hence, SFR profiles. The star formation instead appears to follow the older stars. There is a general correlation between azimuthally averaged log \(\Sigma\) and log SFR, similar to what is seen by others, except for some radii in the two galaxies with the disturbed kinematics. The gas is marginally gravitationally stable against collapse into clouds in these galaxies.

Outer stellar disks are being traced to ever fainter levels in dwarf galaxies, and these observations are challenging our concepts of star formation and disk growth over cosmic times. Clearly, understanding the processes that mold outer disks, as well as understanding how stars form in the extreme environment of outer disks, are important to our understanding of galaxy formation and evolution.

Support for this work was provided to D.A.H. by the Lowell Observatory Research Fund, by grant AST-0204922 from the National Science Foundation, and by grant NNX08AL66G from NASA/GALEX. Funding to B.G.E. was provided by NSF grant AST-0707426. S.-H.O. acknowledges financial support from the South African Square Kilometre Array Project. M.R. and N.W. are grateful for participation in the Northern Arizona University Research Experiences for Undergraduates program in the summers of 2008 and 2009, respectively. This program is run by Kathy Eastwood and funded by the National Science Foundation through grant AST-0453611. We are also grateful to the VLA, KPNO, and GALEX personnel for access to the superb instrumentation that made this project possible and all of the effort that goes into making such facilities work.

Facilities: VLA, KPNO:2.1m, Mayall, GALEX
