QSPR analysis of Alkanes with certain degree based topological indices

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Abstract
The topological indices are the important tools in QSPR studies. Recently Hosamani et. al., [11] studied the QSPR analysis of some degree based topological indices by selecting the linear model: \( P = a + (TI)b \), where \( P \) is the physical property and \( TI \) is the topological index. In this paper, we carry forward their work by studying the quadratic and logarithmic models for the set 67 alkanes.

Keywords
Topological indices, QSPR-analysis, octane isomers.

AMS Subject Classification
05C90, 05C35, 05C12.

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1. Introduction

The topological indices are a convenient means of translating chemical constitution into numerical values which can be used for correlation with physical properties in quantitative structure-property/activity relationship (QSPR/QSAR) studies. In this paper, we have considered the following topological indices for the QSPR study.

Randić Index \([13]\)

\[
R(G) = \sum_{u \sim v} \frac{1}{\sqrt{d_G(u)d_G(v)}}
\]  

(1.1)

Reciprocal Randić Index \([13]\)

\[
RR(G) = \sum_{u \sim v} \sqrt{d_G(u)d_G(v)}.
\]  

(1.2)

Second Zagreb Index \([4]\)

\[
M_2(G) = \sum_{uv \in E(G)} d_G(u)d_G(v)
\]  

(1.3)

Atom-Bond Connectivity Index \([1]\)

\[
ABC(G) = \sum_{u \sim v} \sqrt{d_u(G) + d_v(G) - 2} \frac{d_u(G)d_v(G)}{d_u(G)d_v(G)}
\]  

(1.4)
We have used here 08 degree based topological indices, viz., (mr) at 20 taken from \[ \text{n-butanes to nonanes. Values for these property were} \]

\[ \text{sions (st), molar volumes (mv) at 20 points (BP), molar volumes (mv) at 20} \]

\[ \text{for modeling eight representative physical properties [boiling} \]

\[ \text{refer the interested reader to the articles [5–10, 12].} \]

\[ \text{Augmented Zagreb Index [3]} \]

\[ AZI(G) = \sum_{uv \in E(G)} \left( \frac{d_{G}(u)d_{G}(v)}{d_{G}(u) + d_{G}(v) - 2} \right)^{3}. \]  

\[ \text{Geometric-Arhithmetic Index [14]} \]

\[ GA(G) = \sum_{uv \in E(G)} \frac{2\sqrt{d_{u}(G)d_{v}(G)}}{d_{u}(G) + d_{v}(G)} \]  

\[ \text{Harmonic Index [2]} \]

\[ H(G) = \sum_{uv \in E(G)} \frac{2}{d_{u}(G) + d_{v}(G)} \]  

\[ \text{Sum Connectivity Index [15]} \]

\[ SCI(G) = \sum_{uv \in E(G)} \frac{1}{d_{u}(G) + d_{v}(G)} \]  

For recent work on degree-based topological indices, we refer the interested reader to the articles [5–10, 12].

2. The Use of Selected Degree Based Topological Indices in QSPR Studies

We have used here 08 degree based topological indices, viz., \( M_2(G), R(G), ABC(G), AZI(G), GA(G), H(G), SCI(G), RR(G) \) for modeling eight representative physical properties [boiling points(BP), molar volumes (mv) at 20°C, molar refractions (mr) at 20°C, heats of vaporization (hv) at 25°C, surface tensions (st) 20°C and melting points (mp)] of the 67 alkanes from n-butanes to nonanes. Values for these property were taken from [11]. The values are compiled in Table 1 and Table 2 in [11].

3. Regression Models

The following statistical models have been used for the study:

- Linear Model:

\[ P = a(TI) + b \]  

- Quadratic Model :

\[ P = a(TI)^2 + b(TI) + c \]  

- Logarithmic Model:

\[ P = a + b \ln(TI) \]  

where \( P \) is a physical property, \( TI \) is a topological index and \( a, b \) and \( c \) are constants.

Now we have obtained the following different regression models for each degree based topological index, which are listed below.

4. Randić index \( RR(G) \)

1. Linear Model

\[ bp = -76.519 + [RR(G)]15.433 \]

\[ mv = 71.458 + [RR(G)]24.968 \]

\[ mr = 11.965 + [RR(G)]7.546 \]

\[ hv = 12.352 + [RR(G)]7.270 \]

\[ ct = 39.946 + [RR(G)]68.560 \]

\[ cp = 42.875 - [RR(G)]4.459 \]

\[ st = 12.463 + [RR(G)]2.337 \]

\[ mp = -160.901 + [RR(G)]15.931 \]

2. Quadratic Model

\[ bp = 199.335[RR(G)]^2 - 22.750[RR(G)] - 304.298 \]

\[ mv = 22.884[RR(G)]^2 + 0.320[RR(G)] + 74.660 \]

\[ mr = 7.546[RR(G)]^2 - 7.526[RR(G)] + 11.964 \]

\[ hv = 5.351[RR(G)]^2 + 0.295[RR(G)] + 15.307 \]

\[ ct = 156.322[RR(G)]^2 - 13.499[RR(G)] - 98.213 \]

\[ cp = -7.446[RR(G)]^2 + 0.459[RR(G)] + 47.975 \]

\[ st = 4.948[RR(G)]^2 - 0.401[RR(G)] + 8.444 \]

\[ mp = -39.589[RR(G)]^2 + 8.559[RR(G)] - 76.219 \]

3. Logarithmic Model

\[ bp = -98.213 + \ln[RR(G)]164.078 \]

\[ mv = 64.861 + \ln[RR(G)]76.576 \]

\[ mr = 9.942 + \ln[RR(G)]23.165 \]

\[ hv = 10.487 + \ln[RR(G)]22.253 \]

\[ ct = 11.673 + \ln[RR(G)]7.305 \]

\[ cp = 44.262 - \ln[RR(G)]13.873 \]

\[ st = 11.673 + \ln[RR(G)]7.305 \]

\[ mp = -161.902 + \ln[RR(G)]46.179 \]

5. Reciprocal Randić Index \( R^R(G) \)

1. Linear Model

\[ bp = -36.550 + [R^R(G)]10.479 \]

\[ mv = 88.599 + [R^R(G)]5.283 \]

\[ mr = 10.916 + [R^R(G)]1.613 \]

\[ hv = 17.878 + [R^R(G)]1.5 \]

\[ ct = 94.651 + [R^R(G)]13.654 \]

\[ cp = 38.098 - [R^R(G)]0.815 \]

\[ st = 13.613 + [R^R(G)]0.529 \]

\[ mp = -154.694 + [R^R(G)]3.816 \]
2. Quadratic Model

\[ b_{p} = 29.569[RR(G)]^2 - 0.777[RR(G)] - 143.624 \]
\[ m_{v} = 8.562[RR(G)]^2 - 0.135[RR(G)] + 70.362 \]
\[ m_{r} = 2.231[RR(G)]^2 - 0.025[RR(G)] + 13.481 \]
\[ h_{v} = 2.884[RR(G)]^2 - 0.057[RR(G)] + 10.179 \]
\[ c_{t} = 26.563[RR(G)]^2 - 0.526[RR(G)] + 22.245 \]
\[ c_{p} = -2.633[RR(G)]^2 + 0.074[RR(G)] + 48.296 \]
\[ s_{t} = 0.769[RR(G)]^2 - 0.010[RR(G)] + 12.284 \]
\[ m_{p} = 2.732[RR(G)]^2 - 0.047[RR(G)] - 149.022 \]

3. Logarithmic Model

\[ b_{p} = -204.147 + \ln[RR(G)]120.671 \]
\[ m_{v} = 10.071 + \ln[RR(G)]58.499 \]
\[ m_{r} = -6.826 + \ln[RR(G)]17.771 \]
\[ h_{v} = -4.673 + \ln[RR(G)]16.701 \]
\[ c_{t} = -115.874 + \ln[RR(G)]154.217 \]
\[ c_{p} = 51.429 - \ln[RR(G)]9.499 \]
\[ s_{t} = 5.777 + \ln[RR(G)]5.844 \]
\[ m_{p} = -206.274 + \ln[RR(G)]40.018 \]

6. Second Zagreb index \( M_{2}(G) \)

1. Linear Model

\[ b_{p} = 3.194 + [M_{2}(G)]3.582 \]
\[ m_{v} = 108.696 + [M_{2}(G)]1.806 \]
\[ m_{r} = 22.911 + [M_{2}(G)]0.556 \]
\[ h_{v} = 23.808 + [M_{2}(G)]0.505 \]
\[ c_{t} = 145.038 + [M_{2}(G)]4.713 \]
\[ c_{p} = 34.082 - [M_{2}(G)]0.248 \]
\[ s_{t} = 15.125 + [M_{2}(G)]0.198 \]
\[ m_{p} = -144.169 + [M_{2}(G)]1.462 \]

2. Quadratic Model

\[ b_{p} = 9.5[M_{2}(G)]^2 - 0.11[M_{2}(G)] - 67.612 \]
\[ m_{v} = 4.654[M_{2}(G)]^2 - 0.042[M_{2}(G)] + 82.216 \]
\[ m_{r} = 1.132[M_{2}(G)]^2 - 0.11[M_{2}(G)] + 16.132 \]
\[ h_{v} = 1.316[M_{2}(G)]^2 - 0.015[M_{2}(G)] + 14.259 \]
\[ c_{t} = 10.197[M_{2}(G)]^2 - 0.0101[M_{2}(G)] + 79.430 \]
\[ c_{p} = -0.990[M_{2}(G)]^2 + 0.014[M_{2}(G)] + 42.965 \]
\[ s_{t} = 0.340[M_{2}(G)]^2 - 0.003[M_{2}(G)] + 13.466 \]
\[ m_{p} = 2.612[M_{2}(G)]^2 - 0.25[M_{2}(G)] - 155.608 \]

3. Logarithmic Model

\[ b_{p} = -157.572 + \ln[M_{2}(G)]80.309 \]
\[ m_{v} = 35.344 + \ln[M_{2}(G)]38.120 \]
\[ m_{r} = 0.678 + \ln[M_{2}(G)]11.632 \]
\[ h_{v} = 23.808 + \ln[M_{2}(G)]0.505 \]
\[ c_{t} = -57.195 + \ln[M_{2}(G)]102.888 \]
\[ c_{p} = 46.458 - \ln[M_{2}(G)]5.931 \]
\[ s_{t} = 7.282 + \ln[M_{2}(G)]4.115 \]
\[ m_{p} = -195.718 + \ln[M_{2}(G)]28.122 \]

7. Atom-Bond Connectivity index \( ABC(G) \)

1. Linear Model

\[ b_{p} = -64.716 + [ABC(G)]33.687 \]
\[ m_{v} = 85.034 + [ABC(G)]14.889 \]
\[ m_{r} = 16.060 + [ABC(G)]4.501 \]
\[ h_{v} = 16.908 + [ABC(G)]4.219 \]
\[ c_{t} = 84.789 + [ABC(G)]38.735 \]
\[ c_{p} = 38.675 - [ABC(G)]2.310 \]
\[ s_{t} = 13.480 + [ABC(G)]1.445 \]
\[ m_{p} = -162.007 + [ABC(G)]11.401 \]

2. Quadratic Model

\[ b_{p} = 82.424ABC(G)^2 - 5.262[ABC(G)] - 170.576 \]
\[ m_{v} = 42.667[ABC(G)]^2 - 3.003[ABC(G)] + 24.767 \]
\[ m_{r} = 12.555[ABC(G)]^2 - 0.871[ABC(G)] - 1.414 \]
\[ h_{v} = 13.605[ABC(G)]^2 - 1.015[ABC(G)] - 3.456 \]
\[ c_{t} = 126.152[ABC(G)]^2 - 9.438[ABC(G)] - 105.087 \]
\[ c_{p} = -11.102[ABC(G)]^2 + 0.949[ABC(G)] + 57.771 \]
\[ s_{t} = 4.686[ABC(G)]^2 - 0.351[ABC(G)] + 6.452 \]
\[ m_{p} = 13.132[ABC(G)]^2 - 0.188[ABC(G)] - 165.747 \]
8. Augmented Zagreb Index $AZI(G)$

1. Linear Model

\[
\begin{align*}
bp &= 12.424 + [AZI(G)]2.153 \\
mv &= 113.239 + [AZI(G)]1.068 \\
mr &= 24.599 + [AZI(G)]0.322 \\
hv &= 24.513 + [AZI(G)]0.311 \\
ct &= 144.923 + [AZI(G)]3.102 \\
cp &= 34.848 - [AZI(G)]0.180 \\
st &= 16.409 + [AZI(G)]0.991 \\
mp &= -134.675 + [AZI(G)]0.672
\end{align*}
\]

2. Quadratic Model

\[
\begin{align*}
bp &= 7.32[AZI(G)]^2 - 0.063[AZI(G)] - 82.098 \\
mv &= 1.644[AZI(G)]^2 - 0.007[AZI(G)] + 102.697 \\
mr &= 0.526[AZI(G)]^2 - 0.002[AZI(G)] + 20.875 \\
hv &= 0.416[AZI(G)]^2 - 0.001[AZI(G)] + 22.595 \\
ct &= 7.423[AZI(G)]^2 - 0.053[AZI(G)] + 65.599 \\
cp &= -0.379[AZI(G)]^2 + 0.002[AZI(G)] + 38.502 \\
st &= 0.216[AZI(G)]^2 - 0.001[AZI(G)] + 14.281 \\
mp &= -2.142[AZI(G)]^2 - 0.035[AZI(G)] - 84.780
\end{align*}
\]

3. Logarithmic Model

\[
\begin{align*}
bp &= -187.696 + \ln[AZI(G)]79.188 \\
mv &= 29.399 + \ln[AZI(G)]35.203 \\
mr &= -0.952 + \ln[AZI(G)]10.693 \\
hv &= 0.279 + \ln[AZI(G)]10.204 \\
ct &= -121.818 + \ln[AZI(G)]108.188 \\
cp &= 49.847 - \ln[AZI(G)]49.847 \\
st &= 8.076 + \ln[AZI(G)]3.142 \\
mp &= -158.803 + \ln[AZI(G)]14.474
\end{align*}
\]

9. Geometric-Arithmetic Index $GA(G)$

1. Linear Model

\[
\begin{align*}
bp &= -53.490 + [GA(G)]25.569 \\
mv &= 82.145 + [GA(G)]12.497 \\
mr &= 15.201 + [GA(G)]3.777 \\
hv &= 15.556 + [GA(G)]3.624 \\
ct &= 69.372 + [GA(G)]33.814 \\
cp &= 40.776 - [GA(G)]2.201 \\
st &= 13.365 + [GA(G)]1.186 \\
mp &= -151.482 + [GA(G)]7.566
\end{align*}
\]

2. Quadratic Model

\[
\begin{align*}
bp &= 197.073[H(G)]^2 - 24.379[H(G)] - 266.711 \\
mv &= 35.395[H(G)]^2 - 1.870[H(G)] + 65.270 \\
mr &= 11.768[H(G)]^2 - 0.074[H(G)] + 8.699 \\
hv &= 8.455[H(G)]^2 - 0.221[H(G)] + 13.124 \\
ct &= 186.977[H(G)]^2 - 19.760[H(G)] - 110.657 \\
cp &= -8.281[H(G)]^2 + 0.631[H(G)] + 47.065 \\
st &= 5.597[H(G)]^2 - 0.555[H(G)] + 8.644 \\
mp &= -54.423[H(G)]^2 + 11.565[H(G)] - 55.220
\end{align*}
\]

10. Harmonic Index $H(G)$

1. Linear Model

\[
\begin{align*}
bp &= -52.343 + [H(G)]48.668 \\
mv &= 81.662 + [H(G)]24.018 \\
mr &= 15.150 + [H(G)]7.228 \\
hv &= 15.059 + [H(G)]7.072 \\
ct &= 63.098 + [H(G)]66.687 \\
cp &= 41.516 - [H(G)]4.439 \\
st &= 13.506 + [H(G)]2.219 \\
mp &= -156.398 + [H(G)]15.763
\end{align*}
\]
3. Logarithmic Model

\[
bp = -62.629 + \ln[H(G)]145.849 \\
mv = 81.125 + \ln[H(G)]68.205 \\
mr = 14.917 + \ln[H(G)]20.586 \\
hv = 15.005 + \ln[H(G)]19.995 \\
ct = 54.741 + \ln[H(G)]195.002 \\
cp = 41.773 - \ln[H(G)]12.730 \\
st = 13.276 + \ln[H(G)]64.57 \\
mp = -150.996 + \ln[H(G)]39.806
\]

11. Sum-Connectivity Index \(SCI(G)\)

1. Linear Model

\[
bp = -67.446 + [SCI(G)]52.484 \\
mv = 75.934 + [SCI(G)]25.463 \\
mr = 13.319 + [SCI(G)]7.695 \\
hv = 13.662 + [SCI(G)]7.412 \\
ct = 50.335 + [SCI(G)]69.578 \\
cp = 42.146 - [SCI(G)]4.567 \\
st = 15.125 + [SCI(G)]0.198 \\
mp = -157.805 + [SCI(G)]16.178
\]

2. Quadratic Model

\[
bp = 185.047[SCI(G)]^2 - 22.097[SCI(G)] - 254.170 \\
mv = 22.264[SCI(G)]^2 + 0.533[SCI(G)] + 80.439 \\
mr = 7.089[SCI(G)]^2 + 0.101[SCI(G)] + 14.172 \\
hv = 4.756[SCI(G)]^2 + 0.442[SCI(G)] + 17.402 \\
ct = 148.589[SCI(G)]^2 - 13.170[SCI(G)] - 60.957 \\
cp = -7.799[SCI(G)]^2 + 0.375[SCI(G)]^2 + 45.291 \\
st = 0.340[SCI(G)]^2 - 0.003[SCI(G)] + 13.466 \\
mp = -31.545[SCI(G)]^2 + 8.001[SCI(G)] - 90.965
\]

3. Logarithmic Model

\[
bp = -73.005 + \ln[SCI(G)]153.008 \\
mv = 76.842 + \ln[SCI(G)]71.244 \\
mr = 13.577 + \ln[SCI(G)]21.543 \\
hv = 13.999 + \ln[SCI(G)]20.678 \\
ct = 47.812 + \ln[SCI(G)]198.806 \\
cp = 42.171 - \ln[SCI(G)]12.932 \\
st = 7.282 + \ln[SCI(G)]4.115 \\
mp = -154.564 + \ln[SCI(G)]42.865
\]

12. Discussion and Concluding Remarks

By inspection of the data given in tables 1 and 2, and regression equations it is possible to draw a number of conclusions for the given degree based topological indices.

- The Randic index plays an useful role in QSPR studies. The correlation coefficient value ranges from 0.073 to 0.924 for linear model with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. For quadratic model the correlation coefficient value ranges from 0.086 to 0.943 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. Finally, for logarithmic model the correlation coefficient value ranges from 0.065 to 0.942 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively.

- The reciprocal Randic index shows less predictive power than the Randic index. The correlation coefficient value ranges from 0.082 to 0.925 for linear model with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for molar refractions of alkanes respectively. For quadratic model the correlation coefficient value ranges from 0.082 to 0.928 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for molar refractions of alkanes respectively. Finally, for logarithmic model the correlation coefficient value ranges from 0.081 to 0.917 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively.

- The classical topological index namely the second Zagreb index shows the following applications in QSPR studies of alkanes. The correlation coefficient value ranges from 0.073 to 0.807 for linear model with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for molar refractions of alkanes respectively. For quadratic model the correlation coefficient value ranges from 0.075 to 0.924 for linear model with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. Finally, for logarithmic model the correlation coefficient value ranges from 0.079 to 0.943 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively.

- The atom bond connectivity index found to be useful topological index. The correlation coefficient value
ranges from 0.093 to 0.825 for linear model with minimum correlation coefficient value for melting points of alkanes and maximum correlation coefficient value for boiling point of alkanes respectively. For quadratic model the correlation coefficient value ranges from 0.093 to 0.855 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for boiling point of alkanes respectively. Finally, for logarithmic model the correlation coefficient value ranges from 0.093 to 0.848 with minimum correlation coefficient value for melting points of alkanes and maximum correlation coefficient value for boiling point of alkanes respectively.

- The augmented Zagre index found to be less useful topological index than the ABC-index. The correlation coefficient value ranges from 0.049 to 0.723 for linear model with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. For quadratic model the correlation coefficient value ranges from 0.088 to 0.785 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. Finally, for logarithmic model the correlation coefficient value ranges from 0.021 to 0.761 with minimum correlation coefficient value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively.

- The geometric-arithmetic index has a good predictive power for the set of alkanes. The correlation coefficient value ranges from 0.068 to 0.927 for linear model with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. For quadratic model the correlation coefficient value ranges from 0.080 to 0.944 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. Finally, for logarithmic model the correlation coefficient value ranges from 0.084 to 0.942 with minimum correlation coefficient value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively.

- The harmonic index has the following applications in QSPR study. The correlation coefficient value ranges from 0.070 to 0.819 for linear model with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. For quadratic model the correlation coefficient value ranges from 0.097 to 0.870 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. Finally, for logarithmic model the correlation coefficient value ranges from 0.055 to 0.857 with minimum correlation coefficient value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively.

- The sum connectivity index found to be useful topological index. The correlation coefficient value ranges from 0.074 to 0.926 for linear model with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. For quadratic model the correlation coefficient value ranges from 0.066 to 0.944 with minimum correlation coefficients value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively. Finally, for logarithmic model the correlation coefficient value ranges from 0.084 to 0.942 with minimum correlation coefficient value for melting points of alkanes and maximum correlation coefficient value for critical temperature of alkanes respectively.

13. Correlation of Topological Indices with Physico-Chemical Properties of Alkanes

In the following figures, the correlation of topological indices with above mentioned physical properties of alkanes are shown:
14. Conclusion

The results of QSPR studies reveals that the regression models (3.1)-(3.3) are the most significant models to predict
the physicochemical properties of molecular graphs.

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