Research Article

State and Parameter Estimation of a Nonlinear Servo System Handling Noises and Varying Payloads

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ARTICLE INFO

Article history:
Received 27 September 2020
Accepted 11 February 2021

Keywords:
Extended-Kalman filter,
Noise,
Sliding mode control,
State and parameter estimation,
Varying payload.

ABSTRACT

Payload estimators have many parameters, which are trained using the recorded position, velocity and known payload information. To use these payload estimators in the real-time applications, accurate position and velocity information of the system are required. In this paper, first recently proposed sliding-mode observers (SMOs) are designed and compared for velocity estimation of a nonlinear servo system. Second, a parameter estimation based on sliding-mode super-twisting approach is designed to estimate unknown and varying parameter for a class of nonlinear systems. The convergence property of observers is considered using Lyapunov stability method. In the applications, the constant and varying payloads of the servo system have been estimated using the designed method and compared with Extended-Kalman Filter (EKF). In the final section, artificial noises with different SNR are applied to the measurement signal. When the less amplitude of noise signal is applied, second order SMO estimated the states and the payload better than EKF. However, EKF provides much better estimation results than second order SMO for large amplitude of noise signals. For the sake of generalization, second order SMO is a fast and robust observer for small noise cases. In addition, the filtering property of EKF has still importance for large noise cases.

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1. Introduction

Robotic manipulators in industry, railway vehicles, medical devices and many other equipment require sensory devices [1]. However, measurement device cannot be available or expensive for an application. Therefore, soft sensors/state observers have been designed to estimate unmeasured states and unknown parameters of the linear and nonlinear systems since 60s [2]. The acquired knowledge from soft sensors is essential for monitoring, feedback control, decision making etc. Nowadays, any observer can easily be embedded into the microcontroller and estimated measurements can be conveniently used for specific applications. Besides, microcontrollers are more flexible than past with respect to speed and memory.

State observers have first been introduced for linear systems in [3], and later developed for nonlinear systems in [4, 5]. The other well-known nonlinear observers are high-gain observer (HGO) [4-6], sliding-mode observer (SMO) [7, 8], Extended-Kalman filter (EKF) [9] and other nonlinear Kalman filters [10], Takagi-Sugeno fuzzy observer [11], adaptive fuzzy/neural observers [12, 13]. Recently, there have been many developments on the sliding-mode theory [14] to improve speed, accuracy and stability conditions. The sliding-mode observers based on the sliding-mode theory are known with robustness to uncertainties and distortions [15, 16]. Due to finite-time convergence, SMOs have been recently applied to many real-time systems and compared mostly with other nonlinear observers [17].

The unknown payload of robot manipulators and other mechatronic systems have been estimated using several methods in the literature [18, 19]. Off-line trained fuzzy/neural systems have been designed in [20, 21]. However, these payload estimators have many parameters, which are trained using the recorded position, velocity and

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DOI: 10.18100/ijamec.800716
known payload information. In order to implement these approaches in a real-time application, the correct position and velocity information are needed, which cannot be available for all systems. A robust high precision controller has been developed against unknown payloads in [22]. In [23], an adaptive system based on the prediction error-minimization is proposed that estimates the correct payload online, likewise the velocity measurement is needed. An adaptive robust control method has been developed in [24] for precise motion control and payload estimation. In [25], a neural-network model is trained offline with a large dataset and a Kalman filter is used to online estimation of the payload. The estimated payload has been used in [20, 21] to improve the control performance of the manipulator.

The rest of the paper is organized as follows. First, sliding mode observers and Extended-Kalman filter are summarized in Section 2 and Section 3, respectively. Section 4 introduces the parameter estimation method. Afterward, Section 5 presents the velocity estimation and parameter estimation results. Finally, Section 6 concludes the paper.

2. Sliding-mode Observers

Sliding mode observers create sliding motion of error between the measured system output and observer output [15]. Because of the finite-time, fast convergence, robustness with respect to uncertainties, stability and the possibility of uncertainty estimation, SMOs are widely used in the literature [16, 17] for state estimation and control of nonlinear systems. In the following subsections, classical SMO (CSMO), second-order SMO (SSMO), integral SMO (ISMO), and terminal-mode SMO (TSMO) approaches are briefly explained.

Consider an n-dimensional, nonlinear and continuous-time single-input single-output (SISO) nonlinear system in companion form,

\[ x^{(1)} = x_2, \]
\[ x^{(n)} = f(x, p, u), \]
\[ y = x_1 \]

where \( x(t) \in \mathbb{R}^n \) is the state vector, \( u(t) \in \mathbb{R} \) is the control input applied, \( y(t) \in \mathbb{R} \) is the output measurement and \( p \in \mathbb{R} \) is an unknown parameter of the nonlinear system, respectively. It is assumed that the dynamics of \( f(.) \) is known and continuously differentiable with respect to the states and parameters. The aim in the estimation problem is to get an estimate of unmeasurable states \( \hat{x}(t) \) and unknown parameter \( \hat{p}(t) \) of nonlinear system (1) using available measurement.

2.1. Classical Sliding-Mode Observer

For the given nonlinear system (1), it is assumed that \( x_m^m(m = 1, N) \) is the single measurement available. The classical sliding-mode observer (CSMO) [7] is designed as follows

\[
\begin{align*}
\dot{x}_1 &= -h_1 e_m + \hat{x}_2 - k_1 \text{sign}(e_m) \\
\dot{x}_2 &= -h_2 e_m + \hat{x}_3 - k_2 \text{sign}(e_m) \\
&\vdots \\
\dot{x}_n &= -h_N e_m + \hat{f} - k_N \text{sign}(e_m)
\end{align*}
\]

where \( e_m = \hat{x}_m - x_m \) is the measurement error and \( \hat{f}(x, u) \) is an estimation of \( f(x, u) \). The constants \( h_i \) are chosen as for a classical Luenberger observer to ensure asymptotic error decay, and \( k_i \) constants are the design parameters for switching of the sliding surface. The derived \( N \) th error dynamics are given by following equation.

\[
\begin{align*}
\dot{e}_1 &= -h_1 e_m + e_2 - k_1 \text{sign}(e_m) \\
\dot{e}_2 &= -h_2 e_m + e_3 - k_2 \text{sign}(e_m) \\
&\vdots \\
\dot{e}_n &= -h_N e_m + \Delta f - k_N \text{sign}(e_m)
\end{align*}
\]

\[ \Delta f = \hat{f} - f \] is assumed to be bounded as \( k_N \geq \Delta f \). The asymptotic convergence and stability conditions are proven using Lyapunov stability [8].

2.2. Second-Order Sliding-Mode Observer

The second-order sliding-mode observer (SSMO) with super-twisting algorithm [26] has been introduced and applied to many mechanical systems where the error dynamics are different than that of conventional sliding mode observer as

\[
\begin{align*}
\dot{x}_1 &= x_2 + \lambda |x_1 - \hat{x}_1|^{1/2} \text{sign}(x_1 - \hat{x}_1), \\
\dot{x}_2 &= f(x_1, x_2, u) + \alpha \text{sign}(x_1 - \hat{x}_1),
\end{align*}
\]

where the parameters are selected as

\[
\alpha > f^*, \quad \lambda > \sqrt{\frac{2}{f^*} \frac{(\alpha + f^*)(1 + \rho)}{1 - \rho}}, \quad 0 < \rho < 1.
\]

The \( f^* \) parameter is the double maximum possible acceleration of the system, derived as \( f^* > |\hat{f}(x_1, x_2, \hat{x}_2, u)| \) where \( \hat{f}(.) \) is the functional error of the observer dynamics. The bounds of the parameters are found that the second-order SMO satisfies the Lyapunov stability [26]. The sliding-mode super-twisting approach is very efficient for the estimation and control of second order nonlinear systems and applied to real-time systems [27].
2.3. Integral Sliding-Mode Observer

Integral sliding-mode observer (SMO) [28] of the nonlinear systems has been designed as
\[
\dot{x}_1 = \dot{x}_2 + v_1, \\
\dot{x}_2 = f(x_1, x_2, u) + v_2, \\
y = \dot{x}_1,
\]
where
\[
v_1 = \rho_1 e + \gamma_1 \text{sign}(s), \\
v_2 = \rho_2 e + \gamma_2 \text{sign}(s),
\]
with sliding surface \(s(t) = e(t) + \sigma \int_0^t e(\tau)d\tau\). The measurement error in the equation of the sliding surface is defined as \(e = y - \hat{y}\) where \(y\) is the measured output, \(\hat{y}\) is the estimated output. The selected positive constants drive the observer in stable region.

2.4. Terminal Sliding-Mode Observer

The nonlinear system (1) is assumed in the following form,
\[
\begin{align*}
\dot{x} &= Ax + f(x) + Bu, \\
y &= Cx,
\end{align*}
\]
where \(x(t) \in \mathbb{R}^n\) is the state vector, \(u(t) \in \mathbb{R}^r\) is the vector of applied control input and \(y(t) \in \mathbb{R}\) is the output. The terminal sliding-mode observer (TSMO) [29] has been designed as a second-order nonlinear systems as follows.
\[
\begin{align*}
\dot{x} &= A\hat{x} + f(\hat{x}) + Bu + Le + v, \\
y &= x_1,
\end{align*}
\]
where
\[
v_1 = -a \text{sign}(e_1), \\
v_2 = \beta e_2^{\gamma/p},
\]
and \(1 < \frac{\gamma}{p} < 2\). The feedback gain \(L = [L_1 \ L_2]^T\) is designed as linear observer gain using Lyapunov equation
\[
A_0^2P + PA_0 + \frac{1}{\epsilon}PP + \gamma I_n = Q,
\]
where \(A_0 = \begin{bmatrix} -a & -L_1 \\ -a^2 & -L_2 \end{bmatrix}\) where \(\epsilon > 0\), \(P > 0\), \(Q < 0\) and \(y\) is the Lipschitz constant of the system. Following the requirements of the constants, the solution of the (10) for the observer gain satisfies the stability of the observer.

3. Extended-Kalman Filter

The Kalman filter has been introduced as an optimal filter for linear systems in [30] and used to estimate the unmeasurable states of the linear systems for a half century. For the state estimation of nonlinear systems, the Kalman filter estimate is based on the linearized system, and the filter is called “Extended-Kalman filter” (EKF) [9]. The EKF has been also utilized for the parameter estimation in [31]. The continuous-time EKF dynamics are summarized as follows.

i. The nonlinear system dynamics are
\[
\begin{align*}
\dot{x} &= f(x, u, p, w), \\
y &= h(x, v), \\
w &\sim N(0, Q), \\
v &\sim N(0, R),
\end{align*}
\]
where \(f(.)\) and \(g(.)\) are nonlinear functions, \(x\) is the system state, \(u\) is the input and \(p\) is the unknown parameter of the system. In (12), \(v\) and \(w\) are normally distributed state and measurement noises, respectively. \(Q\) and \(R\) are the corresponding covariance matrices.

ii. The linearized dynamics around the current estimate are
\[
\begin{align*}
F &= \left. \frac{\partial f(x)}{\partial x} \right|_{x = \hat{x}}, \\
N &= \left. \frac{\partial f(x)}{\partial w} \right|_{x = \hat{x}}, \\
H &= \left. \frac{\partial h(x)}{\partial x} \right|_{x = \hat{x}}, \\
M &= \left. \frac{\partial h(x)}{\partial v} \right|_{x = \hat{x}}.
\end{align*}
\]

iii. The following matrices will be used for update:
\[
Q_c = NQN^T, \quad R_c = MRM^T.
\]

iv. The extended-Kalman filter update equations are
\[
\begin{align*}
\dot{x} &= f(\hat{x}, u, w) + K[y - h(\hat{x}, v)], \\
K &= PH^TR_c^{-1}, \\
P &= FP + PF^T + Q_c - PH^TR_c^{-1}HP,
\end{align*}
\]
where \(K\) is the Kalman gain matrix and \(P\) is the error covariance matrix. The initialization of \(P\) is based on the estimated initial states of the system. In (15b) and (15c), the \(K\) and \(P\) matrices are updated using the linearized system dynamics (13) and (14). Afterward, the states and parameters of the Kalman filter (15a) are updated using \(K\) and error \(e = y - h(\hat{x}, v)\). For the parameter estimation of system (1) using EKF, the unknown parameter is added as an additional state to original states and its estimate is updated using the derivative of \(f(.)\) w.r.t unknown parameter inside \(F\) matrix to calculate the error covariance matrix \(P\) and Kalman gain \(K\) [10].
4. Parameter Estimation

In this paper, the parameter adaptation method is designed using the sliding-mode theory. For the system given in (1), the parameter estimate is designed as

$$\dot{\hat{p}} = e \text{sign}(e) \frac{\partial f(\hat{x}, \hat{p}, u)}{\partial \hat{p}}$$

(17)

where $$e = y - \hat{y}$$ with $$y = x_1$$. The nonlinear function of the system is differentiable with respect to unknown parameter such that it is assumed in the form of

$$f(\hat{x}, p, u) = \hat{p}\psi(\hat{x}, u) + \delta(\hat{x}, u),$$

(18)

where $$\psi(\hat{x}, u)$$ is a nonzero function. The stability of the state observer is not affected from the parameter estimation due to bounded uncertainties which means that $$f^- < f(\hat{x}, p, u) < f^+$$. Afterward, the convergence of the estimated parameter can be shown using Lyapunov stability as follows. The parameter error is defined as $$\hat{p} = p - \tilde{p}$$ where its derivative is found as $$\dot{\hat{p}} = 0 - \dot{\tilde{p}} = -e \text{sign}(e)\psi(\hat{x}, u)$$. The error dynamics of the super-twisting SSMO is

$$\dot{x}_1 = \dot{x}_2 - \lambda |e|^{1/2}\text{sign}(e),$$

$$\dot{x}_2 = \hat{p}\psi(x, u) - \alpha \text{sign}(e).$$

(19)

The Lyapunov function of the parameter estimation is given as

$$V = \frac{1}{2} \hat{p}^2,$$

(20)

and its time derivative is derived as

$$\dot{V} = \frac{1}{2} \hat{p} \ddot{\hat{p}} + \frac{1}{2} \dot{\hat{p}} \dot{\hat{p}},$$

$$= -\hat{p} \dot{\hat{p}},$$

$$= -\hat{p} e \text{sign}(e)\psi(\hat{x}, u).$$

(21)

The estimation error of the second state goes to zero in time and its time derivative is assumed equal to zero as $$\dot{x}_2 = 0$$. Then the parameter error is found as $$\hat{p}\psi(\hat{x}, u) = \alpha \text{sign}(e)$$. The time change of the Lyapunov function is finally derived as

$$\dot{V} = -\alpha^{-1} |e| (\hat{p}\psi(\hat{x}, u))^2 < 0,$$

(22)

where $$\alpha > f^+$$. The time change of the Lyapunov function implies that the function $$V$$ is monotonically decreasing until

$$|e| (\hat{p}\psi(\hat{x}, u))^2 = 0,$$

(23)

which means that both state estimation error and parameter estimation error goes to zero as $$t \to \infty$$. In other words, the parameter change drives also the convergence of the estimation error. Then, we can write,

$$\lim_{t \to \infty} \dot{\hat{p}} = p. $$

(24)

Further, we have bounded the parameter estimate to get rid of possible damage to state estimation using the priori known bound of the unknown parameter. These bounds are usually known for most of the real-time systems such as here the maximum and minimum payload value of the servo system is known in application part.

The estimated parameter of the nonlinear system is assumed to be bounded as $$|\hat{p}| < M_p$$. Then the parameter adaptation rule is modified as,

$$\dot{\hat{p}} = \begin{cases} \Delta \hat{p} \text{ if } \hat{p} < M_p, \\ T[.] \text{ if } \hat{p} \Delta \hat{p} < 0 \text{ and } |\hat{p}| = M_p, \end{cases}$$

(25)

where $$\Delta \hat{p} = -e \text{sign}(e)\psi(\hat{x}, u)$$. The well-known projection operator [32] is defined as $$T[.] = \Delta \hat{p} - \frac{\Delta \hat{p}}{|\hat{p}|} \hat{p}$$.

5. Numerical Applications

In this section, first recently proposed sliding-mode observers are designed and compared for velocity estimation of a nonlinear servo system. Second, a parameter estimation based on sliding-mode super-twisting approach is designed to estimate unknown and varying parameter for a class of nonlinear systems. The dynamics of the nonlinear servo system are given as

$$\dot{x}_1 = x_2,$$

$$\dot{x}_2 = \frac{-K^2 - BR}{Rf} x_2 - \frac{gL}{f} \sin(x_1) m_L + \frac{K}{Rf} u,$$

(16)

where $$x_1$$ is the position of the payload in radians and $$x_2$$ is the angular velocity of the payload in rad/sec. $$m_L$$ is the payload of the system where the payload is assumed as an unknown parameter and estimated when it takes constant and time-varying values. The servo system is shown in Figure 1 and its parameters are listed in Table 1.

Figure 1. Nonlinear servo system
The servo system has basically single-link joint manipulator dynamics with a small payload. The servo system locates its payload to different positions between $[-\pi, \pi]$ according to applied input voltage signal. The importance of this system for the applied observers are as follows. It is a second-order nonlinear system and has a simple nonlinearity such that it is suitable for the comparison of the observers for state and parameter estimation and also control methods.

### Table 1. Parameters of the servo system

| Parameter | Value |
|-----------|-------|
| $K$       | 0.0536 N m/A |
| $b$       | $3 \times 10^{-6}$ kg/s |
| $R$       | 9.5 $\Omega$ |
| $J$       | $1.91 \times 10^{-4}$ kg m$^2$ |
| $g$       | 9.81 m/s$^2$ |
| $L$       | 0.042 m |
| $m_L$     | 0 – 100 gr |

**5.1. State Estimation Results**

Except for the classical sliding-mode observer, summarized sliding-mode observers were basically proposed for a specific type of nonlinear systems. However, the applied nonlinear servo system in (16) is suitable for all introduced sliding-mode observers so that we can compare their estimation performances. The observers are in continuous-time and integrated using 4th-order Runge-Kutta method. The step-size or sampling-period of the system is chosen sufficiently small to satisfy integration stability of the observer. The design parameters of the sliding-mode observers and Extended-Kalman Filter are given in Table 2 which are selected by trial-and-error approach from a reasonable interval.

### Table 2. Parameters of the designed observers

| Observer | $h_1$ | $h_2$ | $k_1$ | $k_2$ |
|----------|-------|-------|-------|-------|
| CSMO     | 100   | 1500  | 1     | 1     |
| SSMO     | $\lambda = 100$, $\alpha = 500$. |
| ISMO     | $p_1 = 100$, $p_2 = 200$, $y_1 = 10$, $y_2 = 10$, $\sigma = 1$. |
| TSMO     | $\alpha = 2$, $\beta = 0.5$, $q = 3$, $p = 2$, $L_1 = 100$, $L_2 = 200$; |
| EKF      | $P_0 = 10^2 \text{eye}(2)$, $Q = 10^{-1}I_{n_{x,u}}$. |

The input-output signals of the system are presented in Figure 2 that have been obtained from the real-time feedback-linearization control of the servo system.

Therefore, it has sharp input changes when the reference signal changes. For the system, the position and velocity states are measured. However, for the estimation purpose, only position state is assumed to be measured.

![Figure 2. Control voltage and position of the servo system](image)

Then, estimated velocities using SMOs and measured velocity are compared to determine RMSE values of estimation process. The velocity estimation RMSE performances are given in Table 3 and SSMO has been provided most accurate velocity estimation with least root-mean squared-error (RMSE) performance.

### Table 3. RMSE values of the state estimation

| Observer | Position Estimation | Velocity Estimation |
|----------|---------------------|---------------------|
| CSMO     | 0.0080              | 0.404               |
| SSMO     | 0.0038              | 0.347               |
| ISMO     | 0.0038              | 0.379               |
| TSMO     | 0.0076              | 0.398               |
| EKF      | 0.0076              | 0.491               |
5.2. Constant and Varying Payload Estimation

In this study, in addition to designed SMOs and Kalman-type observer for velocity estimation of a nonlinear servo system, constant or varying parameter estimation was also performed. A constant payload is mounted to the nonlinear servo system.

In numerical results, SSMO with the least root-mean squared-error performance in the most accurate velocity estimation and EKF performance were compared. Figure 4 (a) and Figure 4 (b) show the resulting constant payload estimation and estimation errors of SSMO and EKF, respectively. According to the results, the EKF estimation is much oscillatory, but SMO estimation is more smooth and more robust to the state change. In addition, designing the EKF parameters is much troublesome than SMO when the initialization of the error covariance matrix and noise covariances are not proper, it causes divergence of estimates.

In the same way, EKF and SMO methods have been used to estimate varying payload of the nonlinear servo system. The comparisons of payload estimates are demonstrated in Figure 5(a) and Figure 5(b), respectively. The same design parameters of SMO are utilized with constant payload case such that the parameter estimate is smooth and has less estimation errors than EKF. Both the constant and varying payload estimation results are listed in Table 4 with RMSE values. However, varying payload case has larger RMSE values than constant payload case which is in fact an expected result.
Table 4. RMSE values of the payload estimation

| Case/RMSE       | SMO | EKF |
|-----------------|-----|-----|
| Constant payload| 5.48| 7.22|
| Varying payload | 6.89| 9.35|

5.3. Noisy Case of Varying Payload Estimation

In this subsection, the designed parameter estimation methods are compared under an external noise. An artificial noise is applied to the measured state, which is the position of the payload in simulations. The added artificial noise is a zero-mean noise with 10 dB, 20 dB and 30 dB signal-to-noise ratios (SNR). Therefore, noise variance $R$ parameter of the EKF is selected according to the SNR and variance of the output. The estimation results with 20 dB noise is given in Figure 6(a) and Figure 6(b), respectively.

The application results are obtained when same noise is applied to the estimation processes. Table 5 presents the performance results with different SNRs. The remarkable result is that when the amplitude of the noise decreases, SSMO provides the better RMSE result of estimation. In contrast, when the amplitude of the noise increases, EKF provides better performance of estimation. The noise filtering property of the EKF actually surpasses the effect of the noise on the estimation.

Table 5. Noise case of payload estimation

| SNR/RMSE | SSMO | EKF |
|----------|------|-----|
| 10 dB    | 25.62| 8.55|
| 20 dB    | 9.24 | 9.08|
| 30 dB    | 7.46 | 9.37|

6. Conclusions

In this paper, different types of SMOs and EKF were designed for state and parameter estimation of a nonlinear servo system. In the first part, without measurement noise, the observers are compared for velocity estimation and SSMO provided most accurate estimation results. In the second part, without measurement noise, SSMO and EKF are compared for the constant and varying payload estimation. As before, SSMO provided better estimation results. In the final section, artificial noises with different SNR are applied to the measurement signal. When the less amplitude of noise signal is applied, SSMO estimates the states and payload better than EKF. However, EKF provides much better estimation results than SSMO for large amplitude of noise signals. For the sake of generalization, SSMO is a fast and robust observer for small noise cases. However, the filtering property of EKF has still importance for large noise cases.

Acknowledgment

The authors would like to thank Delft Center for Systems and Control for the collection of experimental data from nonlinear servo system.
Author's Note
Abstract version of this paper was presented at 9th International Conference on Advanced Technologies (ICAT'20), 10-12 August 2020, Istanbul, Turkey with the title of “State and Parameter Estimation of A Nonlinear Servo System Handling Noises and Varying Payloads”.

References
[1] Y. Jiang, S. Yin, J. Dong and O. Kaynak, "A Review on Soft Sensors for Monitoring, Control and Optimization of Industrial Processors", IEEE Sensors Journal, doi: 10.1109/JSEN.2020.3033153, 2020.
[2] C. Santina, R. L. Truby and D. Rus, “Data-driven disturbance observers for estimating external forces on soft robots”, IEEE Robotics and Automation Letters, 5(4), 5717-5724, 2020.
[3] D. Luenberger, “Observers for multivariable systems”, IEEE Transactions on Automatic Control, 11(2):190–197, 1966.
[4] E. E. Thau, "Observing the state of nonlinear dynamic systems", International Journal of Control, 17:471–479, 1973.
[5] M. Zeitz, “The extended luenberger observer for nonlinear systems”, Syst. Control Lett., 9(2):149–156, 1987.
[6] J.P. Gauthier, H. Hammouri, and S. Othman, “A simple observer for nonlinear systems applications to bioreactors”, IEEE Transactions on Automatic Control, 37(6):875 – 880, 1992.
[7] S. V. Drakunov, “An adaptive quasiostimal filter with discontinuous parameters”, Automatic Remote Control, 44(9):1167–1175, 1983.
[8] J.J.E. Slotine, J.K. Hedrick, and E.A. Misawa, “On sliding observers for nonlinear systems”, ASME Journal of Dynamic Systems and Control, 109:245–252, 1987.
[9] H. Cox, “On the estimation of state variables and parameters for noisy dynamic systems”, IEEE Transactions on Automatic Control, 9(1):5–12, 1964.
[10] D. Simon, “Optimal State Estimation: Kalman, H Infinity, and Nonlinear Approaches” Wiley-Interscience, 2006.
[11] K. Tanaka and H.O. Wang, “Fuzzy regulators and fuzzy observers: a linear matrix inequality approach”, In Proceedings of the 36th IEEE Conference on Decision and Control, volume 2, pages 1315 –1320, San Diego, California USA, 1997.
[12] J.H. Park, P.S. Yoon, and G.T. Park, “Robust adaptive observer using fuzzy systems for uncertain nonlinear systems”, In The 10th IEEE International Conference on Fuzzy Systems, volume 3, pages 749–752, The University of Melbourne, Australia, 2001.
[13] S. Beyhan, “Adaptive dynamic neural-network observer design of velocity feedbacks”, In International Symposium on Innovations in Intelligent Systems and Applications, pages 1 – 5, Trabzon, Turkey, July 2012.
[14] V. I. Utkin, “Variable structure systems with sliding modes”, IEEE Transactions on Automatic Control, 22(2):212–222, 1977.
[15] F. Chen and M.W. Dunnigan, “Comparative study of a sliding-mode observer and Kalman filters for full state estimation in an induction machine”, IEEE Proceedings Electric Power Applications, 149(1):53–64, 2002.
[16] S. K. Spurgeon, “Sliding-mode observers: a survey”, International Journal of Systems Science, 39(8):751–764, 2008.
[17] Y. Zhang, Z. Zhao, T. Lu, L. Yuan, W. Xu, and J. Zhu, “A comparative study of luenberger observer, sliding mode observer and extended Kalman filter for sensorless vector control of induction motor drives”, In Energy Conversion Congress and Exposition, pages 2466 – 2473, 2009.
[18] G. Li, S. Wang, Z. Yu, “Adaptive nonlinear observer-based sliding mode control of robotic manipulator for handling an unknown payload”, Proceedings of the Institution of Mechanical Engineers, Part I: Journal of Systems and Control Engineering, doi:10.1177/0959651820969461, 2020.
[19] Yu, X., & Chen, L., “Observer-based two-time scale robust control of free-flying flexible-joint space manipulators with external disturbances”, Robotica, 35(11), 2201–2217, 2017.
[20] M. Leahy, M. Johnson, and S. Rogers, “Neural network payload estimation for adaptive robot control”, IEEE Transactions on Neural Networks, 2(1):93–100, 1991.
[21] H. C. Ngo and P. Meckl, “Intelligent feedforward control and payload estimation for a two-link robotic manipulator”, IEEE/ASME Transactions on Mechatronics, 8(2):277–283, 2003.
[22] B. Rouzebeh, G. Bone, G. Ashby, and E. Li, “Design, Implementation and Control of an Improved Hybrid Pneumatic-Electric Actuator for Robot Arms”, IEEE Access, 7, 14699–14713, 2019.
[23] S. Abiko and K. Yoshida, “On-line parameter identification of a payload handled by flexible based manipulator”, In Proceedings of the International Conference on Intelligent Robots and Systems, volume 3, pages 2930–2935, Sendai, Japan, 2004.
[24] J. Hu, C. Li, Z. Chen and B. Yao, “Precision Motion Control of a 6-DoF Industrial Robot With Accurate Payload Estimation”, in IEEE/ASME Transactions on Mechatronics, 25(4), 1821–1829, 2020.
[25] M. Savia and H. N. Koivo, “Neural-network-based payload determination of a moving loader”, Control Engineering Practice, 12(5):555–561, 2004.
[26] J. Davila, L. Fridman, and A. Levant, “Second-order sliding-mode observer for mechanical systems”, IEEE Transactions on Automatic Control, 50(11):1785 – 1789, nov. 2005.
[27] N. K. M. Sirdi, A. Rabbi, I. Fridman, J. Davila, and Y. Delanne, “Second order sliding-mode observer for estimation of vehicle dynamic parameters”, International Journal of Vehicle Design, 48(3):190–207, 2008.
[28] R. Sharma and M. Aldeen, “Design of integral sliding mode observers with application to fault and unknown input reconstruction”, In Proceedings of the 48th IEEE Conference on Decision and Control, pages 6958 –6963, December 2009.
[29] C. P. Tan, X. Yu, and Z. Man, “Terminal sliding mode observers for a class of nonlinear systems”, Automatica, 46(8):1401 – 1404, 2010.
[30] R. E. Kalman, “A new approach to linear filtering and prediction problems”, Transactions of the ASME–Journal of Basic Engineering, 82(Series D):35–45, 1960.
[31] V. Aidala, “Parameter estimation via the Kalman filter”, IEEE Transactions on Automatic Control, 22(3):471 – 472, 1977.
[32] Li Xin Wang. “A course in fuzzy systems and control”, Prentice-Hall Inc., London, 1997.