Power calculations for detecting differences in efficacy of fecal microbiota donors

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Abstract

Fecal microbiota transplantation (FMT) is a recommended therapy for recurrent Clostridioides difficile infection and is being investigated as a potential therapy for dozens of other indications, notably inflammatory bowel disease. The immense variability in human stool, combined with anecdotal reports from FMT studies, have suggested the existence of “donor effects”, in which stool from some FMT donors is more efficacious than stool from other donors. In this study, simulated clinical trials were used to estimate the number of patients that would be required to detect donor effects under a variety of study designs. In most cases, reliable detection of donor effects required more than 100 patients treated with FMT. These results suggest that previous reports of donor effects need to be verified with results from large clinical trials and that patient biomarkers may be the most promising route to robustly identifying donor effects.

Introduction

Fecal microbiota transplantation (FMT), the transfer of stool from healthy donors into ill patients, is a recommended therapy for multiply recurrent Clostridioides difficile infection, the most common hospital-acquired infection in the United States [1]. FMT is also being investigated as a potential therapy for dozens of other indications, including inflammatory bowel disease, metabolic diseases, cancer, and central nervous disorders [1, 2]. Although FMT’s molecular mechanisms for treating C. difficile infection are not fully understood, FMT’s efficacy for treating C. difficile has motivated its experimental use in these other areas [3].

Stool donors are selected by a process of exclusion designed to maximize patient safety. Candidate donors are excluded based on blood and stool tests for known pathogens, risk factors for pathogen
carriage, and personal and family history of potentially microbiome-mediated diseases [4]. However, given
the enormous complexity of stool—which includes bacteria, viruses, fungi, microbe-derived molecules, and
host-derived molecules—and the variability of stool from person to person [5, 6], it stands to reason that
different stool could have different ability to treat disease. Anecdotes from FMT research, particularly
in ulcerative colitis [7, 8], have created interest in the possibility of “donor effects”, that is, in potential
variability in the efficacy of different donors’ stool [9, 10, 11, 12].

A “donor effect” refers to the possibility that stool from some donors is more efficacious than stool
from other donors for treating some indication. For example, some FMT studies have tested for the
possibility that one donor produced more efficacious stool than the other donors in the study [13, 7, 8].
Others have tested for the possibility that donors with greater microbiota diversity, or a differential
abundance of some microbial taxon, is more efficacious [14, 15, 16, 17, 18]. Finally, at least one study has
tested for the possibility that the composition of a donor’s gut microbiota is associated with outcome of a
patient treated with that donor’s stool [19]. If donor effects do exist—if some donors, or some particular
stool is more efficacious than other stool—they would be crucial to improving FMT as a therapy and
to clarifying FMT’s molecular mechanisms [10].

Although multiple studies have tested for donor effects, these tests were all performed post hoc. In
no case was a search for a donor effect part of the experimental design. It remains unclear if we can
expect today’s FMT studies, mostly 20 to 40 patients in size [2], to reliably determine if donor effects
exist. A key barrier to discovering donor effects, then, is a lack of statistical power methodology. Here
we expand on previous theoretical models of donor effects [9, 20] and use simulations to estimate FMT
studies’ statistical power to detect donor effects.

Methods

Four designs for detecting donor effects were investigated.

Contingency table model

In this model, variations of which were used in two previous theoretical studies of donor effects [9, 20],
donors are assumed to be efficacious (“good”) or inefficacious (“bad”) and the distribution of donor
efficacies is bimodal. Donor effects are tested for using a contingency table of patients outcomes by their
associated donor. This approach was designed to model the statistical tests used to search for donor
effects in previous FMT studies [13, 8, 7].

Specifically, a fraction $\phi$ of donors, the “efficacious” donors, have an efficacy $\varepsilon_+$ (i.e., each patient
treated with stool from an efficacious donor has a probability $\varepsilon_+$ of a positive outcome). The remaining
proportion $1 - \phi$ of donors, the “inefficacious” donors, have efficacy $\varepsilon_- < \varepsilon_+$. To simplify the model, we make the assumptions that $\phi = \frac{1}{2}$ and the mean efficacy $(\varepsilon_- + \varepsilon_+)/2 = \frac{1}{2}$ (i.e., $\varepsilon_- = 1 - \varepsilon_+$), leaving only a single parameter $\Delta \varepsilon = \varepsilon_+ - \varepsilon_-$ (Figure 1).

Simulated clinical trials were run to determine the relationship between the effect size $\Delta \varepsilon$ and the statistical power of the study. In each simulated trial, $N_P$ patients were evenly distributed among $N_D$ donors. Each donor’s underlying efficacy, either $\varepsilon_-$ or $\varepsilon_+$, is randomly set according to $\phi$. Each patient’s dichotomous outcome is randomly determined depending on the efficacy of their donor. Heterogeneity among the donors’ efficacies was tested for using a $\chi^2$ test with Yates’s correction on the $N_D \times 2$ contingency table of patient outcomes by donor.

**Donor biomarker model**

In this model, donor effects are detected by searching for an association between some continuous-valued donor biomarker and the associated patients’ outcomes. This approach was designed to model the statistical tests used to search for donor effects in previous FMT studies, where the biomarker in question is typically the donor’s gut microbiota community diversity or the abundance of particular microbial taxa in the donor [21].

Specifically, each donor has a continuous-valued biomarker $X$, drawn from a normal distribution with standard deviation $\sigma$, which determines that donors’ efficacy according to $\text{logit}^{-1}(\beta X)$. To simplify the model, we assume that donors with the mean biomarker values have efficacy $\frac{1}{2}$. Then the model has one effect size $\beta \sigma$, which is the log odds ratio in donor efficacy per standard deviation increase in biomarker value. In other words, donor efficacies are log-normal distributed with shape parameter $\beta \sigma$. High $\beta$ means that donors with different biomarkers have more distinct efficacies; high $\sigma$ means that a sample of donors will have a wider range of biomarkers and efficacies.

For example, for $\beta \sigma = 0$, all donors have efficacy $\frac{1}{2}$. For $\beta \sigma = 1$, a donor with a biomarker one standard deviation above the mean has an efficacy of $\text{logit}^{-1}(1) \approx 73\%$, while a donor one standard deviation below the mean has efficacy $\text{logit}^{-1}(-1) \approx 27\%$. For $\beta \sigma \gg 1$, half the donors have 0% efficacy and the other half have 100% efficacy (i.e., the same distribution of efficacies as for the contingency table model for $\Delta \varepsilon = 1$). Below the critical value $\beta \sigma = \sqrt{2} \approx 1.4$, the distribution of donor efficacies is unimodal; above that value, it is bimodal.

In each simulated clinical trial, $N_P$ patients receive FMT, each from a different donor, and their outcomes are simulated based on the randomly-sampled donor biomarkers $X$ (Figure 2). A donor effect is detected using a Mann-Whitney test.
Donor microbiota model

In this model, a donor effect is detected by looking for a separation in the donor gut microbiota composition by the donors’ associated patient outcomes. This approach was designed to model the investigation performed in Jacob et al. [19].

In this model, like in the contingency table model, donors have one of 2 efficacies, $\varepsilon_-$ or $\varepsilon_+$, and patients have dichotomous outcomes. Again, we make the simplifying assumptions that $\phi = \frac{1}{2}$ and $(\varepsilon_+ - \varepsilon_-)/2 = \frac{1}{2}$. In this model, donor effects are detected based on separation of the microbiota of donors associated with patients who had positive outcomes, compared to the microbiota of donors associated with negative outcomes. A PERMANOVA test [22] checks for whether donors’ microbiota composition are associated with those donors’ associated patient outcomes.

This model has two relevant effect sizes. The first is the same effect size as in the contingency table model, $\Delta \varepsilon$. The second is more subtle: how distinguishable are efficacious and inefficacious donors, in terms of their microbiota composition? To model “strong” versus “weak” separation in microbiota composition, data from previous case-control studies of diarrhea [23] and obesity [24] were used. The gut microbiota composition of cases with diarrhea are easily distinguishable from controls (in a random forest classifier, AUC $\approx 0.98$), while obesity cases only weakly separate from healthy controls (AUC $\approx 0.69$) [25].

In each simulation, a donor was assigned as efficacious or inefficacious, as in the contingency table model. Then, each efficacious donor was assigned a microbiota composition drawn at random from the controls in one of the two case-control studies. Each inefficacious donor was assigned a case’s microbiota composition (Figure 3). Next, 1 patient was assigned to each donor, and each patient’s outcome was determined at random according to the associated donor’s efficacy. Finally, a donor effect was searched for with a PERMANOVA test, comparing the donors’ microbiota condition on the patients’ outcomes.

Microbiota compositions were drawn from MicrobiomeHD [26], which processed 16S rRNA taxonomic marker gene sequences as described previously [25]. For the diarrhea study, non-\textit{Clostridioides difficile} diarrhea patients were used as cases. For the obesity study, obese subjects were used as cases. The beta diversity matrix input into PERMANOVA was computed using the Bray-Curtis distance metric.

Patient biomarker model

In this model, the donor effect is not restricted to efficacy of dichotomous donor outcomes. Instead, it is assumed that there is some continuous-valued biomarker measured in patients after the FMT, such as fecal calprotectin in the case of ulcerative colitis [27, 28] or a microbiome biomarker such as microbial engraftment. Heterogeneity in donors is detected using a Kruskal-Wallis test.
Specifically, each patient’s biomarker outcome is drawn from a normal distribution with standard deviation $\sigma_P$, which is common to all patients, but centered on a mean value $\mu_d$ that is specific to the donor $d$ used to treat that patient. The donor-associated values $\mu_d$ are themselves drawn from a hyperdistribution with standard deviation $\sigma_D$ (Figure 4). The relevant effect size is the ratio $\sigma_D/\sigma_P$. For $\sigma_D/\sigma_P > 0$, the variance in patients’ outcomes is due mostly to donor effects. For $\sigma_D/\sigma_P = 0$, the variance is due solely to patient factors.

Simulations

For all models, the number of patients was varied over 12, 24, 48, 96, and 196. For the contingency table and patient biomarker models, the number of donors was varied over 2, 4, 6, 8, and 12. For the donor biomarker and donor microbiota models, the number of donors was equal to the number of patients. For the contingency table and donor microbiota models, the effect size $\Delta \epsilon$ was varied over $[0, 1]$. For the donor biomarker model, $\beta \sigma$ was varied over $[0, \log 25]$. For the patient biomarker model, $\sigma_D/(\sigma_P + \sigma_D)$ was varied over $[0, 1]$.

At 11 points along a grid of effect sizes in each model’s range, 1,000 simulations were conducted to compute the statistical power at the 0.05 confidence level. All calculations were performed using R (version 3.6.0) [29]. $\chi^2$ tests were formed using chisq.test, Mann-Whitney tests using wilcox.test, Kruskal-Wallis tests using kruskal.test, and PERMANOVA tests using the function adonis in the vegan package (version 2.5-6) [30]. Code is available at Zenodo (DOI: 10.5281/zenodo.3755048)

Results

In the contingency table model, 80% statistical power was achieved in simulations similar to a typical FMT trial (i.e., with 24 patients), but the minimum effect size to achieve that power was $\Delta \epsilon_+ = 0.76$ (Figure 1). In other words, the difference between efficacious and inefficacious donors had to be so great that on average 88% of patients assigned to efficacious donors had positive outcomes (i.e., $\epsilon_+ = \frac{4}{1} + \Delta \epsilon / 2 = 0.88$), and only 12% of patients assigned to inefficacious donors had positive outcomes. As the number of patients in the simulated trials was increased, the minimum effect size to achieve 80% power decreased: for simulated trials with 192 patients receiving FMT, the minimum effect size was $\Delta \epsilon = 0.3$.

In the donor biomarker model, 80% statistical power was achieved with 24 patients and a minimum effect size of $\beta \sigma = 1.5$ (Figure 2). This effect size means that a donor with a biomarker one standard deviation above the mean has an efficacy of $\logit^{-1}(1.5) \approx 82\%$, and a donor one standard deviation below the mean has an efficacy of 18%. For 192 patients, this minimum effect size declined to 0.5 (i.e.,
donors one standard deviation above the mean have efficacy logit\(^{-1}(0.5) \approx 62\%.

In the donor microbiota model, 80\% statistical power was achieved with 24 patients when using the diarrhea case-control data as simulated efficacious and inefficacious microbiota, with a minimum effect size of $\Delta \varepsilon = 0.76$ (i.e., efficacious donors have an efficacy $\varepsilon_+ = \frac{1}{2} + \Delta \varepsilon/2 = 88\%$; Figure 3). For 196 patients, the minimum effect size dropped to $\Delta \varepsilon = 0.29$. When using the obesity case-control data, representing a more subtle difference between efficacious and inefficacious donors’ microbiota, 80\% power was achieved only with 192 patients and $\Delta \varepsilon = 0.72$.

In the patient biomarker model, 80\% statistical power was achieved in simulations with 24 patients with a minimum effect size effect size $\sigma_D/\sigma_P = 3.4$ (Figure 4). In other words, the variability in the mean patient biomarkers induced by different donors $\sigma_D$ must be more than three times larger than the variability $\sigma_P$ in patient biomarkers who receive FMT material from the same donor. For 192 patients, the minimum effect size declined to less than 0.8.

**Discussion**

In this study, using 4 different models of donor effects, the minimum effect size required to achieve to achieve reasonable statistical power for a given number of patients were estimated. In the contingency table, donor biomarker, and donor microbiota models, 80\% statistical power was achievable with 24 patients only when the effect sizes were implausibly large. These results suggest that current FMT trials, which typically include 20 to 40 patients treated with FMT, would seem unlikely to discover a true donor effect when using one of these approaches, and large clinical trials will be needed to verify previous reports of donors effects. The patient biomarker model, however, was more powerful than the other approaches.

**Contingency table model**  In the clinical study [7] that motivated two previous modeling studies [20, 9], 38 patients were treated with FMT, the efficacy of the apparently efficacious donor was estimated as $\varepsilon_+ = 7/18 = 39\%$, and the efficacy of the remaining inefficacious donors was estimated as $\varepsilon_- = 2/20 = 10\%$. In our simulations, a 30 percentage point difference in efficacy between the two classes of donors (i.e., $\Delta \varepsilon = 0.3$) required more than 96 FMT-treated patients to be reliably detected.

**Donor biomarker model**  In one clinical study [14], 13 patients were treated with FMT, and a significant difference in donor biomarkers (microbiota community diversity) between donors based on their associated patients’ outcomes was detected (Mann-Whitney test, $p = 0.012$). The results here suggest that, if such an effect were to be robustly detected in 12-patient trials, it would need to be
implausibly large, with donors one standard deviation above the mean (i.e., 16% of donors) having an

efficacy of at least 83%.

**Donor microbiota model** In one clinical study [19], 20 patients were treated with stool from 4
donors, with each patient receiving a mixture of 2 donors’ stool. A statistically significant separation in
the mixtures’ microbiota composition based on the associated patients’ outcomes was detected (PER-
MANOVA, \( p = 0.044 \)). By contrast, the results from this study suggest that reliable detection of such
an effect in 24-patient studies would require both that efficacious and inefficacious donors have markedly
different microbiota compositions (as different as diarrhea patients from healthy controls) and that their
efficacies were implausibly distinct (\( \Delta \varepsilon = 0.76 \), or 88% vs. 12% efficacy). These results broadly accord
with previously work showing that microbiome studies are unlikely to robustly detect individual taxa
mediating FMT patients’ outcomes [31].

**Patient biomarker model** The term “donor effects” has mostly been restricted to referring to
differences in donor efficacy. However, finding any robust difference among donors in the effect that
FMT has on patients would be helpful for understanding the molecular mechanism of FMT [10]. In
the case of fecal calprotectin as a patient biomarker in inflammatory bowel disease, it appears that the
variability in the biomarker among patients with the same disease severity is comparable to the variability
in the mean biomarkers for different severities [28, 27]. In other words, if FMT from some donors could
reliably move patients from severe to mild disease (i.e., \( \sigma_D \approx \sigma_P \)), then the results of these simulations
suggest that a donor effect could feasibly be detected with trials with as few as 48 patients. Furthermore,
donor effects could feasibly be detected in animal studies when there is a relevant biomarker, even if the
animal does not reach a clinical endpoint in the sense of a human clinical trial [32].

**Strengths and limitations** The key strength of this study was that it used straightforward math-
ematical models to make generous estimates of the statistical power of study designs that could detect
donor effects. The key limitation of this study is that it does not account for the many sources of variance
that arise in a clinical trial, most notably patient diagnoses and comorbidities. Thus, the estimates in
this study should be taken as proof-of-concept only. In fact, additional variance coming from variability
between patients, or from attempting an analysis using data from multiple clinical trials, will only
increase the number of patients required to detect these effects.

**Conclusions** Given the large number of patients that would be required to prospectively detect a
donor effect, post hoc detections of donor effects in small clinical trials should be verified with large
clinical trials. The most promising path toward identifying donor effects, and using those effects to
improve microbial therapeutics, appears to lie in using patient biomarkers, rather than donor biomarkers or in patient outcomes alone.

Clinical trialists should take care, however, that different approaches to testing for donor effects require mutually contradictory designs. For example, if a test will be run on patient biomarkers, then 2 to 6 donors should be used to maximize the study’s power to detect a donor effect. Using a different donor for every patient completely precludes the use of an Kruskal-Wallis or ANOVA test. However, if a donor effect will be detected via an association between donor biomarkers and patient outcomes, then a different donor should be used with each patient to maximize the study’s power. In that case, using the same donor to treat more than one patient will only make the subsequent analysis more complex and less powerful.

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Figure 1: Contingency table model. a) In this model, half of donors have efficacy $\varepsilon_+$ and the other half $\varepsilon_-$, with mean efficacy $(\varepsilon_+ + \varepsilon_-)/2 = \frac{1}{2}$. The effect size is $\Delta \varepsilon = \varepsilon_+ - \varepsilon_-$. b) Donors’ efficacies are drawn from the distribution in a. c) Patient outcomes are drawn based on their associated donors’ efficacies. d) Statistical significance is assessed with a $\chi^2$ test on the contingency table of patient outcomes by donor. e) Minimum effect size required to reach 80% statistical power in simulated clinical trials.
Figure 2: Donor biomarker model. a) Donor biomarkers (ticks) are drawn from a normal distribution (curve) with standard deviation \( \sigma \). b) Donor efficacies (points) are determined based on their biomarkers \( X \) and the log odds parameter \( \beta \) according to \( \varepsilon = \logit^{-1}(\beta X) \). The effect size is \( \beta \sigma \), the log odds ratio in donor efficacy per standard deviation of donor biomarker value. Patient outcomes (colors) are randomly determined based on their corresponding donors’ efficacies. c) A difference in donor biomarker values based on the outcomes of their corresponding patients is tested for with a Mann-Whitney test. d) Minimum effect size required to reach 80% statistical power in simulated clinical trials.
Figure 3: **Donor microbiota model.** Two donor efficacies, dichotomous patient outcomes, donor effect measured by separation of microbiota composition. a) An example ordination plot of the data from a microbiota case-control study. b) A subset of cases and controls, representing the simulated donors’ microbiota, are drawn, depending on the number of individuals in the simulated trial. c) Patient outcomes associated with each donor microbiota composition are drawn according to the efficacies $\varepsilon_+$ and $\varepsilon_-$. The effect size $\Delta \varepsilon$ determines the values $\varepsilon_+$ and $\varepsilon_-$ as in the contingency table model. A PERMANOVA test is run on the corresponding dissimilarity matrix of microbiota compositions to detect a donor effect. d) Minimum effect size required to reach 80% statistical power when using the contrast between cases and controls from microbiome studies as a proxy for the microbiome signature difference between efficacious and inefficacious controls.
Figure 4: **Patient biomarker model.** Patient biomarker outcome. a) Each donor (colored ticks) has a mean patient biomarker value drawn from a hyperdistribution with standard deviation $\sigma_D$ (black curve). b) Patients’ biomarkers (colored ticks) are drawn from distributions (colored curves), all with the same standard deviation $\sigma_P$, centered on the mean of their associated donor. The effect size is $\sigma_D/\sigma_P$. c) Donor effects are detected by a Kruskal-Wallis test on patient biomarker values. d) Minimum effect size required to reach 80% statistical power in simulated clinical trials.