Research Article

Analytical Study of QoS-Oriented Multicast in Wireless Networks

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Multicast is a very popular bandwidth-conserving technology exploited in many multimedia applications. However, existing standards of high rate wireless networks provide no error recovery mechanism (ARQ) for multicast traffic. ARQ absence in wireless networks unreliable by their nature leads to frequent packet losses, which is inappropriate for most of multimedia applications. In this paper, we study new reliable multicast mechanism proposed recently to support multimedia QoS (packet loss ratio, latency, and throughput) with various wireless technologies. This mechanism is based on the concept of multiple ACK-leaders, that is, multicast recipients responsible for acknowledging data packets. We develop analytical models of the mechanism with various leader selection schemes and use the models to study the schemes efficiency and to optimize them. Numerical results show that the novel multicast mechanism with multiple ACK-leaders can be easily tuned to meet specific QoS requirements of multimedia or any other multicast applications.

1. Introduction

Wide spreading of wireless networks increases diversity of wireless multimedia services. However, it is very hard to meet strict QoS requirements of multimedia services in wireless networks because of the error-prone nature of wireless media and random access techniques commonly used in wireless protocols. In wireless networks, an access method based on channel reservation is the best way to provide parameterized quality of service (QoS) for multimedia streams. Channel reservation is easily provided with centralized control, when the access point (AP), also called the base station, schedules data transmissions according to specific demands of multimedia services and applications. Almost all existing wireless MAC protocols include centralized control: the IEEE 802.16 MAC [1] for wireless MANs is centralized as a whole; in the IEEE 802.11 [2] and 802.15.3 [3] MACs for wireless LANs and PANs, the AP controls access to the channel and can provide collision-free operation periodically. With distributed control, collision-free periods can be provided too via a negotiation process between neighbor stations: see MCCA in IEEE 802.11s mesh networks [4] and DRP in WiMedia WPANs [5].

In this paper, we assume that multimedia flows are transmitted in specially dedicated collision-free periods. Arranging such intervals, modern MAC protocols of high rate wireless networks support perfectly parameterized QoS for unicast transmission. As to multicast transmissions, parameterized QoS is not supported because conventional automatic repeat request (ARQ) schemes used for unicast are not applicable to multicast connections.

Multicast itself is known to be a bandwidth-conserving technology that reduces traffic by delivering the same data stream to multiple recipients simultaneously. Stations interested in receiving the data stream are included into the related multicast group and are referred to as multicast group members. At MAC layer, a multicast group is identified by a multicast MAC address. The stream originator sends its packets with the destination address field set to the multicast MAC address.

Various applications such as TV and radio broadcasting, gaming, videoconferencing, corporate communications, distance learning, news, and so forth, which use multicast transmission techniques, already crowded the market. In addition, most of these applications impose strict QoS requirements, such as minimal throughput, maximal packet...
loss ratio (PLR), and latency, and so forth, implying a large number of devices in the network.

Almost all multicast applications rely on network layer multicast protocols only. However, these multicast solutions do not take advantages of the broadcast nature of the wireless medium. The efficiency of network layer multicast protocols in terms of QoS can be greatly improved by providing additional local QoS support at the underlying MAC layer. In this paper, we focus on multicast QoS support at the MAC layer, that is, reliable data delivery across single-hop wireless links by facilitating local error recovery.

It is known that reliable traffic delivery is one of the main application requirements. The reliability index is PLR. Unfortunately, multicast QoS in part of requirement on maximal PLR is not supported by modern MAC protocols of high rate wireless networks because of ARQ absence for multicast. However, these protocols have potential tools to implement multicast ARQ schemes. In the next section, we give some background on existing ARQ-based MAC layer approaches, which aim to achieve multicast reliability. Further, in Sections 3–5, we focus on reliable multicast schemes which parameters can be tuned to meet application QoS requirements, develop analytical models of these multicast schemes, and use the models to optimize the schemes. Finally, we present numerical results and summarize the paper.

2. Multicast ARQ Schemes

To our best knowledge, all reliable MAC layer multicast proposals have been developed for 802.11 WLANs (some of them have been presented at IEEE 802.11 Working Group sessions), but ideas of the proposals can be extended and/or adapted to other MAC protocols of high rate wireless networks.

In 2001, Kuri and Kasera [6] described leader-based protocol (LBP). In LBP, the only leader is selected from all the multicast recipients. This leader is responsible for sending Clear-To-Send (CTS) frames in reply to ready-to-send (RTS) frames and acknowledgements (ACKs) in reply to data frames. The leader is also allowed to send negative CTS (NCTS) or negative ACK (NAK) in cases when either it is not ready to receive the data because of some reasons, or the received data frame is corrupted. All other multicast recipients are only allowed to send NCTS and NAK. The problem of leader choice is not solved in [6].

Chao et al. proposed in [7] the random leader technique, according to which the leader is chosen randomly among all recipients with equal probabilities. However, this choice technique does not seem efficient because recipients usually operate in different channel conditions.

In 2007, LG Electronics and INRIA used the idea of LBP in their proposal [8] to IEEE 802.11v task group. However, the proposal did not include all original LBP features due to incompatibility of original LBP with conventional IEEE 802.11. NCTS and NAK mechanisms were removed from original LBP, because of their absence in conventional IEEE 802.11. According to the proposed leader selection scheme [8], the recipient operating in the worst channel conditions is selected as a leader.

Obviously, the only leader may be not enough to provide reliable multicast and thus to meet QoS requirements for all multicast recipients. Batch mode multicast MAC (BMMM) [9], broadcast support multiple access [10] and broadcast medium window (BMW) [11] protocols represent an alternative approach, according to which all recipients are requested to send ACKs. (Further, we refer to this approach as to the BMMM one.)

In BSMA proposed in 2000, the ARQ scheme is based on the NAK frames and thus has the same drawbacks as the original LBP. Furthermore, collisions of CTS frames sent by all recipients are inevitable in BSMA. The idea of the BMW protocol (see Figure 1(a)) is to implement ARQ for every multicast packet as multiple unicast transmissions of CTS, RTS and positive ACK frames, that is, using the conventional IEEE 802.11 DCF MAC with some minor modifications.

Comparing with BSMA which shows little reliability improvement over the legacy IEEE 802.11 multicast, the BMW protocol is more reliable, because the sender retransmits the data frame until it receives an ACK from every recipient. In spite of its high reliability, the BMW protocol is inefficient for delay-sensitive applications due to multiple contention phases between consecutive ACKs following a multicast data packet. For example, given N multicast recipients in the network, the protocol needs to perform N contention phases to receive an ACK from every recipient.

In 2002, the BMMM protocol was proposed [9], which consolidates N contention phases of the BMW protocol into one phase (see Figure 1(b)). The multicast originator sends unicast RTSs to every device in multicast group. If the originator does not receive a CTS frame from any of the recipients in multicast group, it defers the transmission and enters the contention phase. Otherwise, it sends a multicast data frame and then unicast Request for ACK (RAK) frames to each of the multicast recipients successively.

BMMM and BMW are the most reliable protocols among ones described above. But in contrast to BMW, there are no contention phases between consecutive ACKs in BMMM. However, the BMMM overhead increases with the number of devices in the multicast group. Even with a few number of recipients, the overhead consisting in RTSs, CTSs, RAKs and ACKs is bigger than the multicast packet itself.

In [9], the BMMM extension called location aware multicast MAC protocol (LAMM) was proposed. Authors propose to use location information obtained by means of global position system (GPS) to further improve the BMMM. Since a GPS receiver must be implemented together with IEEE 802.11 transmitter, this may result in considerable increasing of power consumption and cost of IEEE 802.11 devices, while industry and market are moving towards low-power portable mobile devices, which must be as cheap as possible.

The same problems are inherent to other reliable multicast protocols [12, 13], which utilize so-called busy tones. By incorporating busy tones into the protocol, authors attempt to reduce the probability of multicast frame corruption due to collisions and hence the number of retransmissions. These
approaches assume that every device has an additional RF circuit to transmit and receive on busy tones. Additional spectrum bands are needed to utilize the busy tones. Moreover, the intruder hazard becomes the central issue. The tones are absolutely unprotected against clogging. An unauthorized signal emitted by any device in the coverage area of the multicast originator even at one of the tones may lead to complete blocking of multicast data flow.

With regard to above discussion, it becomes clear that an ARQ policy with positive ACKs is preferable to one with NAK. Utilizing additional frequency bands as long as additional transceivers is also unacceptable.

So, in 2007 we developed new reliable multicast scheme called the enhanced leader based protocol (ELBP) [14] using the most appropriate LBP and BMMM approaches as base points. LBP assumes the recipient operating in the worst channel conditions is chosen to be the leader responsible for sending ACKs. This method provides very low delays, but at the expense of high PLRs for nonleader recipients. Assuming every recipient to be a leader, BMMM provides the best reliability and thus the lowest PLR at the expense of high delay. The method we proposed and presented to the IEEE 802.11 VTS (video traffic streaming) study group [15, 16] takes into account the trade-off between reliability and delay and can meet specific QoS requirements.

As mentioned above, BMMM overhead that includes a transmission of a lot of ACKs after every packet increases with the number of recipients. To reduce the huge BMMM overhead per packet, ELBP uses the block acknowledgment scheme introduced in IEEE 802.11e [17]: a recipient requested by the Block ACK request (BAR) frame acknowledges a burst of multiple data frames by only one Block-ACK (B-ACK) frame. B-ACK frame includes a bitmap with positive or negative feedback on each packet transmitted in the burst. To protect data frames in the burst, IEEE 802.11e recommends to carry out the RTS-CTS exchange before the data burst transmission. In scenarios without hidden stations, it is enough to send the RTS frame to only one of recipients (as shown in Figure 2), which can be chosen randomly for every multicast data transmission. Obviously, the RTS/CTS exchange is not needed at all if the ELBP burst is transmitted within a collision-free interval. If the multicast originator exchanges BAR and B-ACK frames with all multicast recipients (similarly to the BMMM approach), it may cause long transmission delay which is not appropriate for some applications (real-time multimedia streaming, gaming, etc.) due to their QoS requirements, especially when there are many multicast recipients in the network. To reduce the delay, in the ELBP the multicast originator sends BARs to not all recipients, but only to a subset of them. In the extreme case, the number of stations in this subset can be reduced to one as it is in LBP. But the only leader may be not enough to provide reliable multicast and thus, to meet QoS requirements for all multicast recipients. To not rely on the only leader, ELBP uses several leaders which reply with B-ACK and are referred to as ACK-leaders. Figure 2 shows a typical ELBP burst where all frames are separated by SIFS intervals. After transmission of recurrent data burst, the multicast sender prepares multicast packets for the next burst transmission, including both new packets and packets not acknowledged previously by all ACK-leaders and which life time is not expired.

ELBP was actively discussed in the IEEE 802.11aa task group, which was created from the IEEE 802.11 VTS study group in 2008 to enhance the 802.11 MAC for robust audio video streaming. In particular, original ELBP and its modifications were described in [18]. The common goal of these modifications is to decrease the ELBP overhead by sending the only multicast BAR instead of several unicast BARs. If ACK-leaders receiving the multicast BAR reply immediately, B-ACK collisions are inevitable. The collisions can be avoided in different ways. The first way is to use delayed ACKs instead of immediate ACKs, but it increases the delay because of several contention phases separated B-ACKs. The second way is to transmit the ELBP burst, using some protection mechanism (HCCA, MCCA, or PSMP as in [18]), and to schedule strictly B-ACK transmissions within a contention-free interval dedicated for the ELBP burst.

Specifically, the D0.02 draft of the IEEE 802.11aa amendment [19] introduced more reliable groupcast (MRG) service representing a modified ELBP. According to MRG Block Ack procedure, the AP being a source of multicast traffic asks a subset of recipients for acknowledgments by sending a special multicast BAR frame with immediate ACK-policy: see Figure 3. The frame differs from the legacy BAR in the
Information field indicating an ordered list of ACK-leaders. An ACK-leader indicated the \( n \)th in the list shall transmit B-ACK at a delay of \((n + 1)\text{SIFS} + nT_{B-ACK}\) after the BAR, where \(T_{B-ACK}\) is B-ACK transmission duration.

However, it appeared that IEEE 802.11 channel access method (CSMA/CA) should be changed to transmit B-ACKs according to the strict schedule indicated in the BAR. Due to the reason the MRG service was removed from the draft of the IEEE 802.11aa amendment. The current draft of the IEEE 802.11aa amendment [20] introduces groupcast with Retries (GCR) service with block-ACK retransmission policy which is very similar to the original ELBP approach. The IEEE 802.11aa Task Group approved the GCR service as a base approach of reliable multicasting in IEEE 802.11 standard. Since that, the GCR/ELBP is a very promising reliable multicast technique for infrastructure and mesh IEEE 802.11 networks and is a matter of special interest for analysis and optimization. In the paper, we develop analytical models of the GCR/ELBP mechanism with various leader selection schemes and use the models to study leader selection schemes efficiency and to optimize them.

In [21] we have shown that the ELBP approach, when multiple multicast packets related to the same stream are set as a single burst and a subset of recipients are requested for acknowledgments, can be used also in IEEE 802.16 networks. IEEE 802.16 network operation time is divided into fixed size frames by means of time division duplexing operation mode. A frame consists of a downlink subframe for transmission from the base station to subscriber stations and an uplink subframe for transmissions in the reverse direction. IEEE 802.16 frame structure is shown in Figure 4. In the downlink subframe, the downlink MAP (DL-MAP) and Uplink MAP (UL-MAP) messages are transmitted by the base station, which comprise the bandwidth allocations for data transmission in both downlink and uplink directions, respectively. An ARQ is provided by allocating a special ACK-Channel (ACK-CH) in the uplink subframe for subscriber stations. Bandwidth allocated for this channel depends on how many stations replies with ACK and could not be very large because the uplink subframe itself is tightly bounded and there are a lot of other data in it.

Forming the DL- and UL-MAP, the base station allocates the necessary channel to transmit a multicast data burst in the downlink subframe and to receive ACKs from ACK-leaders in the uplink subframe. On receiving the DL- and UL-MAP, recipient(s) become(s) aware when the multicast burst is going to be transmitted and if an ACK arrival is expected from the recipient, that is, if an ACK slot in the ACK-CH part of the uplink subframe is allocated for the recipient. By the ACKs, the base station finds out which of burst packets were corrupted and should be retransmitted. (This new functionality can be easily added to the existing IEEE 802.16 base station software, using the novel modular architecture approach developed in the EU FP7 project FLAVIA [22].)

The main open issue of the ELBP approach is how to select ACK-leaders. In the next section, we show that the answer depends on QoS requirements. In Sections 4 and 5, we propose accurate analytical models helping to select ACK-leaders and to tune other ELBP parameters, assuming that ELBP bursts are transmitted in contention-free intervals provided by some protection mechanism.

### 3. ELBP Parameters and QoS Requirements

In ELBP, there are two interconnected questions to answer. The first question is how many ACK-leaders should be selected. The second question is which recipients are the best candidates to be ACK-leaders or, in other words, how to select the required number \( J \) of ACK-leaders from all \( N \) recipients. We may choose them randomly with equal probabilities for every new burst, as in [7]. However, it seems that equiprobable leader choice is not the best way to support reliability and to meet QoS requirements, because the scheme does not take recipients’ PLR, throughput and latency into account. Generally, ACK-leader selection scheme may be a function of QoS requirements, reliability and
performance indices, as well as some other metrics, for example, packet error rate (PER).

Since the way of ACK-leaders selection depends highly on QoS requirements, a precise QoS definition is necessary. In this paper, we consider three QoS requirements.

The first one is the maximum PLR $\eta_{max}$. The PLR index of any recipient can be defined as the ratio of the number of packets lost by some reason to the total number of packets transmitted by the multicast sender. Obviously, PLRs depend on channel conditions, that is, PER, and thus, may be different for recipients. Multicast transmission is assumed to meet QoS requirement on the maximum PLR if the PLRs $\eta_j$ among all the recipients $j = 1, \ldots, N$ in the coverage area are not greater than $\eta_{max}$, that is,

$$\max_{j=1, \ldots, N} \eta_j \leq \eta_{max}. \tag{1}$$

The second QoS requirement is the maximum latency $T_{max}$. In our case, latency is the time interval spent to transmit a packet, including possible retransmissions, or in other words, the time interval between the ends of transmissions of consecutive packets. This performance index is very important for delay-sensitive applications. If a packet is not transmitted for $T_{max}$, there is no need to transmit it further. Thus, the multicast scheme must meet the QoS requirement on the maximum latency. It may be done by setting the MAC layer maximal lifetime of a packet to $T_{max}$.

The last QoS requirement we consider is the minimum reserved rate or, in other words, minimum throughput $S_{min}$. In general, throughput $S_j$ of recipient $j$ can be defined as the average number of the considered multicast stream payload bits successfully received by the recipient per time unit. Obviously, throughput is the major performance index which depends on PLR and, thus, is different for the recipients in various channel conditions. Multicast transmission is assumed to meet QoS requirement on minimum throughput if the throughputs $S_j$ of all recipients $j = 1, \ldots, N$ in the network are not less than $S_{min}$, that is,

$$\min_{j=1, \ldots, N} S_j \geq S_{min}. \tag{2}$$

From the above definitions, one can see that measures aimed at improving reliability and performance, are opposite. Indeed, if we want to increase the reliability, that is, decrease the PLR, we must retransmit a packet more times, what results in increasing latency and in decreasing the throughput, and vice versa. Thus, some trade-off between PLR, latency and throughput must be found to meet all QoS requirements. To achieve the trade-off, we can tune 3 ELBP parameters:

(i) the burst size $B$, that is, the number of multicast data packets in a burst;

(ii) the periodicity $T$, with which the considered multicast stream is granted with bandwidth, that is, the interval between starts of consecutive bursts;

(iii) the number $J$ of ACK-leaders for every data burst transmission.

In the paper, we look for an admitted region of these parameters values, in which QoS requirements are met for all recipients, and then optimize the values, remaining in the admitted region, to minimize the bandwidth allocated for
a given multicast stream. In terms of the introduced ELBP parameters, the optimization criterion is

\[
\min \left\{ \beta = \frac{T_{\text{burst}}}{T} \right\} = \min \left\{ \frac{O + BT_P + JT_a}{T} \right\},
\]

where \(T_{\text{burst}}\) is the bandwidth granted with every data burst transmission; \(T_P\) is the bandwidth consumed with one multicast data packet transmission followed (or preceded) possibly by an interframe space; \(T_a\) is the bandwidth consumed with one B-ACK transmission followed possibly by an interframe space; \(O\) is a burst transmission overhead independent from the burst size \(B\) and the number \(J\) of ACK-leaders. Obviously, \(O, T_P\) and \(T_a\) values should be determined, depending on the ELBP approach implementation: for the original ELBP (see Figure 2) working under 802.11 HCCA or 802.11s MCCA protection,

\[
O = \text{DIFS} - \text{SIFS}, \quad T_P = T_{\text{DATA}} + \text{SIFS}, \quad T_a = T_{\text{BAR}} + T_{\text{B-ACK}} + 2 \cdot \text{SIFS},
\]

for the IEEE 802.11 standard; for the IEEE 802.11aa MRG,

\[
O = T_{\text{BAR}} + \text{DIFS}, \quad T_P = T_{\text{DATA}} + \text{SIFS}, \quad T_a = T_{\text{B-ACK}} + \text{SIFS};
\]

and for the IEEE 802.16 ELBP described at the end of the previous section,

\[
T_P = n_{\text{sp}}t_{\text{OFDM}}, \quad T_a = n_{\text{sa}}t_{\text{OFDM}},
\]

where \(n_{\text{sp}}\) and \(n_{\text{sa}}\) are the numbers of OFDM symbols (or OFDMA slots) per packet and per ACK, respectively, and \(t_{\text{OFDM}}\) is OFDM symbol duration. Similarly, periodicity \(T\) also depends on the wireless technology: for 802.11 HCCA and MCCA, \(T\) can be of any value larger than \(T_{\text{burst}}\). For WiMAX networks, \(T\) should be multiple of 802.16 frame duration \(t_{\text{frame}}\), that is, \(T = M_{\text{frame}}t_{\text{frame}}\) and criterion (3) can be rewritten in the following form:

\[
\min \left\{ \beta = \frac{Bn_{\text{sp}} + Jn_{\text{sa}}}{M_{\text{frame}}} \right\},
\]

Anyway, there exists a lower limit \(T_{\min}\) of \(T\): \(T_{\min} = T_{\text{burst}}\) for 802.11 HCCA and MCCA and \(T_{\min} = t_{\text{frame}}\) for 802.16 networks.

Leader selection scheme is another ELBP powerful tool. We have already mentioned that equiprobable leader choice may be not the best way to meet QoS requirements for all recipients. Another possible way of ACK-leaders selection is to fix \(J\) recipients, based on the experienced PER, and consider them as ACK-leaders for every burst transmission. In particular, we propose to select the recipients with higher PER and fix them as ACK-leaders. Further, we refer to this ACK-leader selection scheme as to ELBP with fixed ACK-leaders or just fixed ELBP.

One more scheme is to select recipients as ACK-leaders randomly according to some PER dependent weight function. Every round of multicast transmission, multicast originator selects \(J\) ACK-leaders out of all \(N\) recipients according to weights assigned to every recipient by some weight function \(W(\cdot)\). Further, we refer to this ACK-leader selection scheme as to ELBP with weighted ACK-leaders or weighted ELBP for short.

In the next two sections, we develop analytical models of fixed and weighted ELBP leader selection schemes. In Section 6, we use the models to find the best solution for various multicast usecases.

4. ELBP with Fixed ACK-Leaders

4.1. Analytical Study. To develop an analytical model of this multicast scheme, we need to make some definitions and assumptions, first. Let \(N\) and \(J\) be the numbers of multicast recipients and ACK-leaders respectively, where \(J \in [1, \ldots, N]\). All packets are assumed to be of the same payload size \(L\) in bytes. Multicast originator is assumed to work in saturation. Let \(p_j\) be the PER for the \(j\)th recipient. We enumerate recipients in the order of decreasing PERs, that is, the first recipient has the highest PER \(p_1\) and first \(J\) recipients serve as ACK-leaders. Due to 802.11 control frames (as well as ACK messages, DL- and UL-MAP in 802.16) are relatively short and are usually transmitted with highest coding gain, we neglect their error probabilities.

As mentioned above, it is reasonable to set the MAC layer maximal lifetime of a packet to \(T_{\text{max}}\) to meet the QoS requirement on the maximum latency. Since there may be the only attempt of transmission of a given packet during an interval \(T\), the maximum number \(K\) of transmission attempts of a data packet is

\[
K = \left\lfloor \frac{T_{\text{max}}}{T} \right\rfloor.
\]

where \(\lfloor \cdot \rfloor\) is a flooring function. Further, we use \(k = 1, \ldots, K\) as the transmission attempt number.

Let us find the probability that all ACK-leaders have received a given packet exactly after \(k\) attempts, that is, exactly \(k\) attempts appear to be needed to transmit the packet successfully

\[
\pi_k = \prod_{j=1}^{J} \left(1 - p_j^k\right) - \prod_{j=1}^{J} \left(1 - p_j^{k-1}\right).
\]

Similarly, we find the probability \(\tilde{\pi}_k\) that not all ACK-leaders have received the data packet after \(k\) attempts, that is, \(k\) attempts appear to be not enough to transmit the packet successfully

\[
\tilde{\pi}_k = 1 - \prod_{j=1}^{J} \left(1 - p_j^k\right).
\]
The throughput in question: $\eta_j$ with probability $B$ can receive this packet successfully several times, but the transmission process including possible retries, the recipient's MAC layer to the higher network protocol layer ratio of the average number of payload bits delivered by the higher network protocol layer with probability (1

To calculate the throughput, first, we find the average and recipient $j$ never receives the packet successfully, then for an arbitrary attempt of the packet transmission, the packet payload is delivered to the recipient's MAC layer to the higher network protocol layer with probability $\eta_j$.

To get rid of $\eta_j$, we rearrange (13) using (11) to the following form:

$$\eta_j^{\text{ACK}} = p_j - \left(1 - p_j\right) \sum_{k=1}^{K-1} \left(\tilde{\eta}_k p_j^k\right).$$

Using (12) and (14), we can rewrite it in the following form:

$$p_1^{\text{ACK}} \leq \eta_{\text{max}}.$$ 

Inequality (20) is the necessary condition for reliable multicast. Indeed, if the right inequality in (20) does not hold, the QoS can not be supported by the ELBP. In this case, we recommend to decrease $p_1$ to the necessary value by decreasing the packet length and/or bit rate.

Using the second inequality in (19), we prove the following theorem.

**Theorem 1.** Recipients which PERs are less than

$$p_{\text{bound}} = \sqrt[2]{\left(1 - p_j\right)^2 + \eta_{\text{max}} p_j - \frac{1 - p_j}{2p_1}}$$

should not be selected as ACK-leaders.

**Proof.** We need to prove that with any $J > 1$

$$\eta_j < \eta_{\text{max}} \quad \text{if} \quad p_j < p_{\text{bound}}, \, j > J.$$ (22)

First consider the ELBP with the only ACK-leader ($J = 1$). We have $\tilde{\eta}_k = p_1^k$. As $\eta_j^{\text{ACK}}$ decreases with $K$, we can obtain the following inequality from (14), setting $K = 2$:

$$\eta_j^{\text{ACK}}(K > 2) < \eta_j^{\text{ACK}}(K = 2) = p_j - \left(1 - p_j\right)p_1 p_j.$$

Solving the quadratic inequality $\eta_j^{\text{ACK}}(K = 2) < \eta_{\text{max}}$, we prove that it holds with $p_j < p_{\text{bound}}$ where $p_{\text{bound}}$ is determined by (21). Thus, (22) holds with $J = 1$.

Now let $J > 1$. As follows from (10), $\tilde{\eta}_k$ increases with $J$ and hence $\eta_j^{\text{ACK}}(J > 1) < \eta_j^{\text{ACK}}(J = 1)$. Since (22) holds with $J = 1$, it also holds with $J > 1$.

Thus, the PLR of recipients, which PER is less than $\eta_{\text{max}}$, should not be selected as ACK-leaders.

Now, we consider throughput QoS requirement $S_{\text{min}}$. Since PLR sequences $\{\eta_{\text{ACK}}\}$ and $\{\eta_j^{\text{ACK}}\}$ are nonincreasing, then using (17), we can derive the following inequality:

$$\frac{8LB}{T_{\text{yk}}} \left(1 - \max(\eta_j^{\text{ACK}}, \eta_j^{\text{ACK}})\right) \geq S_{\text{min}}.$$ (24)
According to (10) and (16), \( \gamma_k \geq \gamma_2 = 1 + \tilde{\alpha}_1 \) and \( \tilde{\alpha}_1 \) increases with \( J \), that is, \( \tilde{\alpha}_1 > \rho_1 \). Hence the inequality \( \gamma_k \geq 1 + \rho_1 \) holds. At the same time, we have \( \max(n_1^{ACK}, n_2^{ACK}) \geq p_1^k \). This allows us to rewrite the previous inequality in the following form:

\[
B \geq B_0(T) = \frac{T(1 + \rho_1)S_{\min}}{8L(1 - p_1^{1/T})},
\]

(25)

Thus, in the optimization we need to consider \( B \geq B_0(T) \) and \( J < J_0 \) only, where \( J_0 \) is the minimal recipient number which PER is less than \( \rho_{\text{bound}} \) defined by (21).

### 5. Analytical Model of ELBP with Weighted ACK-Leaders

For the ELBP with weighted ACK-leaders, \( J \) ACK-leaders are reselected every time before a burst transmission. The selection is performed from the whole set of recipients, according to their weights \( w_i \), \( i = 1, \ldots, N \). Let us partition all recipients into \( M \) sets. In set \( m = 1, \ldots, M \), there are \( N_m \) recipients, which PER is nearly the same and approximately equal to \( p_m \). Obviously, we assign the same weights \( w_m \) to all \( N_m \) recipients of set \( m \) that makes optimization of the weight distribution easier. This partition makes numerical analysis and optimization of the weighted ELBP much easier in the case of a large number of recipients. Of course, the partition is not reasonable with a small number of recipients. In this case, we just set \( M = N \) and \( N_m = 1 \).

As \( J \) ACK-leaders are to be selected, the selection procedure is carried out in \( J \) steps. At step \( j \), an ACK-leader from set \( h \) is selected with probability

\[
\hat{\xi}_{h,j} = \frac{(N_h - u_{h,j-1})w_h}{\sum_{m=1}^{M} (N_m - u_{m,j-1})w_m},
\]

(26)

where \( u_{m,j} = 1, \ldots, N_m \) is the number of recipients selected to be ACK-leaders in set \( m \) after \( j \) selection steps. That is, \( \hat{U}_j = \{ u_{m,j} \} \), \( m = 1, \ldots, M \), is a selection vector indicating which recipients have been selected after \( j \) steps. Obviously, \( \hat{U}_0 = \emptyset \) and vector \( \hat{U} \equiv \hat{U}_j \) indicates all current ACK-leaders responsible for acknowledging the current data burst transmission. The multicast sender stops transmitting a packet when all current ACK-leaders acknowledge the packet and thus, receive the packet successfully.

Taking (26) into account, the probability distribution \( \varphi(\hat{U}) \equiv \varphi(\hat{U}_j) \) of \( \hat{U} \) can be found recursively

\[
\varphi(\hat{U}_j) = \sum_{U_{j-1}=\hat{U}_j}^{M} \left( \sum_{m=1}^{M} (u_{m,j} - u_{m,j-1}) \hat{\xi}_{m,j} \varphi(\hat{U}_{j-1}) \right),
\]

\[
\hat{\xi}_{m,j} = \frac{(N_h - u_{h,j-1})w_h}{\sum_{m=1}^{M} (N_m - u_{m,j-1})w_m},
\]

(27)

where \( U_{j-1} = \{ \hat{A} : \hat{A} \leq \hat{U}_j, |\hat{U}_j - \hat{A}| = 1 \} \). Here and further, for any \( \hat{X} = \|x_i\| \) and \( \hat{Y} = \|y_i\| \), \( \hat{X} \leq \hat{Y} \) if for all \( i \), \( x_i \leq y_i \) and \( |\hat{Y} - \hat{X}| = \sum_i(y_i - x_i) \).

To find \( \hat{n}_h \), we consider a process of a given packet transmission. Let us introduce a success vector \( \tilde{V}_k = |v_{m,k}| \), \( m = 1, \ldots, M \), where \( v_{m,k} = 1, \ldots, N_m \) is the number of recipients in set \( m \), which successfully receive the packet after \( k \) transmission attempts. Obviously, \( \tilde{V}_0 = \emptyset \) and \( \tilde{V}_{k-1} \leq \tilde{V}_k \). The probability of the success vector change from \( \tilde{V}_{k-1} \) to \( \tilde{V}_k \) after the \( k \)th attempt, given that the \( (k-1) \)-th attempt failed for at least one of recipients which were current ACK-leaders, is

\[
R(\tilde{V}_k, \tilde{V}_{k-1}) = \prod_{m=1}^{M} C_{N_m - v_{m,k-1}}^{v_{m,k} - v_{m,k-1}} (1 - p_m)^{v_{m,k} - v_{m,k-1}} p_m^{N_m - v_{m,k}},
\]

(28)

where \( C^x_y = x! / y!(x - y)! \).

Let \( \pi^*_k(\tilde{V}_k) \) be the probability that after \( k \) attempts \( (k < K) \) the packet transmission process does not complete successfully and the success vector is \( \tilde{V}_k \). \( \pi^*_k(\tilde{V}_k) \) is calculated recursively:

\[
\pi^*_k(\tilde{V}_k) = R(\tilde{V}_k, \tilde{V}_{k-1}) \left[ 1 - \sigma(\tilde{V}_k) \right],
\]

(29)

\[
\sigma(\tilde{V}_k) = \sum_{\tilde{V}_{k-1} \leq \tilde{V}_k} \pi^*_{k-1}(\tilde{V}_{k-1}) R(\tilde{V}_{k-1}, \tilde{V}_{k-1}) \left[ 1 - \sigma(\tilde{V}_{k-1}) \right],
\]

where

\[
\delta_{\text{inh}} = \text{Kronecker symbol}
\]

To find \( \hat{n}_h \), we introduce the probability \( \hat{R}_h(\tilde{V}_k, \tilde{V}_{k-1}) \) that the success vector changes from \( \tilde{V}_{k-1} \) to \( \tilde{V}_k \) so that the given recipient does not receive the packet by the end of \( k \)th attempt:

\[
\hat{R}_h(\tilde{V}_k, \tilde{V}_{k-1}) = \prod_{m=1}^{M} C_{N_m - (v_{m,k} - v_{m,k-1}) - \delta_{\text{inh}}}^{v_{m,k} - v_{m,k-1}} (1 - p_m)^{v_{m,k} - v_{m,k-1}} p_m^{N_m - v_{m,k}},
\]

(32)

where \( \delta_{\text{inh}} \) is Kronecker symbol.

Thus, the probability \( \hat{n}_h(\tilde{V}_k) \) that after the \( k \)th attempt, the packet transmission process does not stop, the given recipient from set \( h \) does not receive the packet and the
success vector is \( \hat{V}_k \), is obtained recursively for all \( \hat{V}_k \) such that \( v_{h,k} < N_h \):

\[
\hat{n}_{h,k}(\hat{V}_k) = \sum_{\hat{V}_{k-1} : \hat{V}_{k-1} \in \hat{V}_{h,k-1} \in N_h} \hat{n}_{h,k-1}(\hat{V}_{k-1}) \times \hat{R}_h(\hat{V}_k, \hat{V}_{k-1}) [1 - \sigma(\hat{V}_k)], \tag{33}
\]

\[
\hat{n}_{h,1}(\hat{V}_1) = \hat{R}_h(\hat{V}_1, 0) [1 - \sigma(\hat{V}_1)].
\]

Now, we can find expressions for probabilities \( \rho_{h,k} \) that \( k \) attempts have been carried out to transmit the packet and the given recipient from set \( h \) has not received the packet in any of these attempts. We have:

\[
\rho_{h,1} = \sum_{\hat{V}_{1} : v_{h,1} < N_h} \hat{R}_h(\hat{V}_1, 0) \sigma(\hat{V}_1),
\]

\[
\rho_{h,k} = \sum_{\hat{V}_{1} : v_{h,k} < N_h} \sum_{\hat{V}_{k-1} : v_{h,k-1} < N_h} \hat{n}_{h,k-1}(\hat{V}_{k-1}) \hat{R}_h(\hat{V}_k, \hat{V}_{k-1}) \sigma(\hat{V}_k), \tag{34}
\]

when \( k = 2, \ldots, K - 1 \), and

\[
\rho_{h,K} = \rho_h \sum_{\hat{V}_{K-1} : v_{h,K-1} < N_h} \hat{n}_{h,K-1}(\hat{V}_{K-1}). \tag{35}
\]

Thus, the PLR for a recipient from set \( h \) is:

\[
\eta_h = \sum_{k=1}^{K} \rho_{h,k}. \tag{36}
\]

Throughput for any recipient from set \( h \) is given by (17), where we substitute \( \eta_h \) for \( \eta_j \).

### 6. Numerical Results

In this section, we use our analytical models to investigate and to optimize ELBP multicast schemes with different wireless technologies and in different use cases. As we don’t apply any simplifications and assumptions about original ELBP multicast schemes, our mathematical models are accurate and there is no need to validate them via simulation. Although we use some simulation to obtain the input data (the dependence of recipient’s PER on distance) for our analytical models.

#### 6.1. Fixed ELBP in 802.11 HCCA

As the first use case, let us consider an 802.11 HCCA WLAN, where the AP is the source of saturated multicast traffic. We assume that the AP transmits multimedia data packets with \( L = 1 \) KB payload at 54 Mbps bit rate, using original ELBP scheme shown in Figure 2 (without RTS/CTS exchange since HCCA provides necessary protection). All model parameters correspond to the IEEE 802.11a defaults [23]. Let all recipients be partitioned into sets so that the recipients of the same set have the same PERs; see Table 1 for recipients with PER > 0.01.

Let fixed ELBP be used. Since the way of ACK-leaders selection depends highly on QoS requirements, we need to specify them. Let \( \eta_{\text{max}} = 0.08 \), \( S_{\text{min}} = 4 \) Mbps and \( T_{\text{max}} = 6.667 \) ms (this \( T_{\text{max}} \) value corresponds to the usual latency bound for video applications). Based on Theorem 1, we conclude that recipients from sets 1–4 only can be selected as ACK-leaders, that is, \( J_0 = 12 \).

Further, for any tuple \( (T < T_{\text{max}}, B > B_0(T), J \leq J_0) \) we estimate PLR and throughput for every recipient by (12), (14) and (17) and check if QoS requirements (1) and (2) are met. In this way we form an admitted region of \( T, B \) and \( J \). In Figure 5, we show values of consumed bandwidth fraction \( \beta \) defined by (3) with

\[
O = \text{DIFS} - \text{SIFS} = 18 \mu s,
\]

\[
T_p = T_{\text{DATA}} + \text{SIFS} = 196 \mu s,
\]

\[
T_a = T_{\text{BAR}} + T_{\text{B-ACK}} + 2 \cdot \text{SIFS} = 100 \mu s,
\]

\[
(37)
\]

in the found admitted region. We see that the following 2 tuples are close to optimum: \( (T = 1800 \mu s, B = 2, J = 4) \) and \( (T = 2200 \mu s, B = 3, J = 4) \). With \( T > 2200 \mu s \) or \( J < 4 \), QoS requirement on the maximum PLR is not met.

#### 6.2. ELBP with Fixed ACK-Leaders in 802.16 Network

An IEEE 802.16 base station (BS) usually covers a large area with huge number of Subscriber Stations (SSs). To increase the network capacity and QoS provisioning, a BS is equipped with sector antenna. Each sector of this antenna covers a separate area with a part of all SSs in it, achieving spatial diversity. In fact, we can consider each sector as an individual IEEE 802.16 wireless network with its own BS, coverage area.

| Set number | Number of recipients | PER  |
|------------|----------------------|------|
| 1          | 2                    | 0.3  |
| 2          | 2                    | 0.25 |
| 3          | 3                    | 0.2  |
| 4          | 4                    | 0.15 |
| 5          | 10                   | 0.055|

**Figure 5:** Consumed bandwidth fraction versus periodicity.
and set of SSs. So, further results will concern one of such sectors.

Let us assume that the BS is a multicast sender and the only multicast data burst is transmitted in every frame, that is, \( M_{\text{frame}} = 1 \). We also assume that the BS transmits a data burst consisted of multicast multimedia data packets with \( L = 512 \) bytes payload at a maximal PHY data rate \( R = 3/4 \), 64-QAM) using ELBP mechanism with fixed ACK-leaders. With this PHY, one 512 bytes packet takes \( n_{\text{sp}} = 16 \) OFDM symbols, while an acknowledgment takes \( n_{\text{sa}} = 2 \) OFDM symbols. The 802.16 frame duration is \( t_{\text{frame}} = 5 \) ms and the maximum latency is \( T_{\text{max}} = 20 \) ms. So, the maximal number of retransmissions is \( K = 4 \), according to (8).

First, we consider more general case shown in Figure 6. In this usecase, the coverage area of the BS is a sector of circle with radius \( R = 1 \) km and total number \( N \) of SSs uniformly distributed across the sector.

To start numerical analysis we need to derive the dependence of recipient’s PER on distance for the investigated network. We divide the process in two steps. First, we obtain the dependence of signal-to-noise ratio (SNR) on distance according to the path loss model in [24] with a critical parameter \( \gamma = 3.3 \). After that we find PER(SNR) by MATLAB simulation of IEEE 802.16 PHY for the highest PHY data rate \( R = 3/4 \), 64-QAM), using AWGN channel as a noise source.

In Figure 7, we show the simulation data for various packet lengths. We also include the analytical approximation of the dependencies obtained by simulation. We approximate the simulation data using the formula

\[
\text{PER} (\text{SNR}, L) = 1 - \left( 1 - \frac{1}{2} \exp\left( - \exp \left( \frac{\text{SNR} - \zeta}{\alpha} \right) \right) \right)^{8L}, \tag{38}
\]

where \( \alpha = 4.8355 \) and \( \zeta = 10.479 \). As it is shown in Figure 7, the proposed analytical approximation fits perfectly the simulation data. Using (38) with \( L = 512 \), we find PER for every recipient. The PER of the most distant SS is 0.1, that is, 10%. The closest SS has the PER equal to 0.

As follows from (10), (12) and (14), PLR depends on station's PER and the number \( J \) of ACK-leaders only. Thus, for a given number \( N \) of stations and PER distribution, we can find the optimal number \( J_{\text{opt}} \) of ACK-leaders minimizing the bandwidth allocated for a given multicast connection per frame (see (7)), while meeting a certain QoS requirement on PLR for all recipients.

In Figure 8, we show the relationship between \( J_{\text{opt}} \) and the maximal PLR over the network which contains \( N = 25 \), 50 and 100 SSs. The figure shows two of ELBP main advantages.

The first advantage is the scalability. Indeed, even if the number of recipients is quite high \( (N = 100) \), the optimal number of ACK-leaders is still less than 10 for a wide range of \( \eta_{\text{max}} \) values: 2–10%. We can see also that the optimal number \( J_{\text{opt}} \) of ACK-leaders is nearly proportional to the number \( N \) of recipients. So, we can conclude the optimal number of ACK-leaders in fixed ELBP scheme is less than 10% over all multicast recipients in wide range of QoS requirements on maximal PLR.

The second advantage is the supremacy over the pure LBP in reliability. Indeed, even if the number of multicast recipients is small \( (N = 25) \), LBP using only one ACK-leader cannot achieve PLR less than 4%. In contrast, ELBP can meet any preassigned QoS requirement \( \eta_{\text{max}} \) on PLR (of course,
Let us consider the case, when there are multiple sets of recipients and recipients of the same set have the same PERs. For certainty, let us assume 3 sets in this usecase, which correspond to 3 small settlements covered by a single sector of an IEEE 802.16 BS as it is shown in Figure 9. The total number of recipients is $N = 25$. The first set consists of $N_1 = 5$ recipients with PER $= 0.1$; the second set has $N_2 = 5$ too and PER $= 0.075$, and the last set has $N_3 = 15$ recipients with PER $= 0.01$.

Let us define QoS requirements. Let the maximum latency $T_{max}$ be 15 ms and thus $K = 3$, maximal PLR $\eta_{max}$ be equal to 0.04, and minimum reserved rate $S_{min}$ be 4 Mbps.

We compare three selection schemes: fixed ELBP, weighted ELBP and full random ELBP. For fixed ELBP scheme, we limit the range of $J$ and $B$ by $B_0 = 6$ and $J_0 = 11$, which are obtained by (16) and (17). For weighted ELBP, weights are assigned according to the principle of minimizing PLR over all stations in the network. Full random ELBP is the special case of weighted ELBP ACK-leader selection scheme with equiprobable weights $w_i = 1/N$.

The PLR characteristics of these multicast schemes are shown in Figure 10. We can see that for weighted ELBP 4 ACK-leaders is enough to meet QoS requirement on maximal PLR, while minimizing $\beta$ in (7). In contrast, the other schemes need much more ACK-leaders. Fixed ELBP requires 8 ACK-leaders, and full random scheme needs to select 11 ACK-leaders.

The next step of our investigation is to find the optimal burst size $B_{opt}$. For that, we find how throughput depends on $B$ with optimal numbers $J_{opt}$ of ACK-leaders found at the previous step. The throughput characteristics are given in Figure 11. This figure shows that the optimal burst size which minimizes $\beta$ in (7) is equal to 7 in case of weighted ELBP, while it is equal to 8 for full random selection scheme and 9 for fixed ELBP.

At last, let us show the allocated bandwidth with these selection schemes. In Figure 12, we can see that the optimal weighted ELBP scheme requires 120 allocated OFDM symbols per frame to meet all QoS requirements of the transmitted multicast stream, while full random selection

6.3. ELBP with Weighted ACK-Leaders. Let us consider the case, when there are multiple sets of recipients and recipients of the same set have the same PERs. For certainty, let us assume 3 sets in this usecase, which correspond to 3 small settlements covered by a single sector of an IEEE 802.16 BS as it is shown in Figure 9. The total number of recipients is $N = 25$. The first set consists of $N_1 = 5$ recipients with PER $= 0.1$; the second set has $N_2 = 5$ too and PER $= 0.075$, and the last set has $N_3 = 15$ recipients with PER $= 0.01$.

Let us define QoS requirements. Let the maximum latency $T_{max}$ be 15 ms and thus $K = 3$, maximal PLR $\eta_{max}$ be equal to 0.04, and minimum reserved rate $S_{min}$ be 4 Mbps.

We compare three selection schemes: fixed ELBP, weighted ELBP and full random ELBP. For fixed ELBP scheme, we limit the range of $J$ and $B$ by $B_0 = 6$ and $J_0 = 11$, which are obtained by (16) and (17). For weighted ELBP, weights are assigned according to the principle of minimizing PLR over all stations in the network. Full random ELBP is the special case of weighted ELBP ACK-leader selection scheme with equiprobable weights $w_i = 1/N$.

The PLR characteristics of these multicast schemes are shown in Figure 10. We can see that for weighted ELBP 4 ACK-leaders is enough to meet QoS requirement on maximal PLR, while minimizing $\beta$ in (7). In contrast, the other schemes need much more ACK-leaders. Fixed ELBP requires 8 ACK-leaders, and full random scheme needs to select 11 ACK-leaders.

The next step of our investigation is to find the optimal burst size $B_{opt}$. For that, we find how throughput depends on $B$ with optimal numbers $J_{opt}$ of ACK-leaders found at the previous step. The throughput characteristics are given in Figure 11. This figure shows that the optimal burst size which minimizes $\beta$ in (7) is equal to 7 in case of weighted ELBP, while it is equal to 8 for full random selection scheme and 9 for fixed ELBP.

At last, let us show the allocated bandwidth with these selection schemes. In Figure 12, we can see that the optimal weighted ELBP scheme requires 120 allocated OFDM symbols per frame to meet all QoS requirements of the transmitted multicast stream, while full random selection
needs 150 symbols and fixed ELBP require 160 OFDM symbols.

Here, we can conclude that weighted ELBP is the optimal approach of QoS support for multicast streaming, although its implementation may be more complicated, comparing with fixed ELBP and full random ELBP.

7. Conclusion

Existing standards of high rate wireless networks consider multicast as unreliable service, which is inappropriate for many multimedia applications making strict QoS demands. In this paper, we study a promising enhanced leader based protocol (ELBP) for reliable multicasting in wireless networks. In ELBP, multicast packets are transmitted in bursts and several multicast recipients called the ACK-leaders are appointed to be responsible for multicast data packets acknowledging.

Specific QoS requirements (maximal packets loss ratio, maximal latency, minimal reserved rate) can be met by varying such ELBP parameters as the number of ACK-leaders as well as the data burst size and periodicity. We consider two types of leader selection schemes: (i) ELBP with fixed ACK-leaders which experience higher PERs than other recipients, and (ii) ELBP with weighted ACK-leaders, where ACK-leaders are reselected according to recipients’ weights before every data burst transmission. We develop accurate analytical models to estimate reliability and performance indices with these schemes and to find their optimal parameters. Numerical results obtained by the models show that ELBP can be used efficiently to meet specific multimedia application QoS demands, in contrast with well-known LBP and BMMM approaches when either only one recipient or all recipients acknowledge multicast packets. Both fixed and weighted ELBP are scalable multicast solutions: according to our model experiments, even with a large number of recipients it is enough to request a few recipients for acknowledgements to provide reliable multicast for all recipients. Comparing fixed and weighted ELBP, we show that weighted ELBP is more efficient in terms of consumed bandwidth.

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