Estimating the effect of healthcare-associated infections on excess length of hospital stay using inverse-probability weighted survival curves.

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Summary

This study illustrates how to estimate the excess length-of-stay due to nosocomial infections in the presence of time-varying confounding. The number of excess days was substantially overestimated when ignoring time-varying confounding, suggesting that future studies should adopt similar methodology.
Abstract

Background: Studies estimating excess length of stay (LoS) attributable to nosocomial infections have failed to address time-varying confounding, likely leading to overestimation of their impact. We present a methodology based on inverse probability-weighted (IPW) survival curves to address this limitation.

Methods: A case-study focusing on intensive care unit-acquired bacteraemia using data from two general ICUs from two London teaching hospitals were used to illustrate the methodology. The area under the curve (AUC) of a conventional Kaplan Meier curve applied to the observed data was compared with that of an IPW Kaplan Meier curve applied after treating bacteraemia as censoring events. Weights were based on the daily probability of acquiring bacteraemia. The difference between the observed average LoS and the average LoS that would be observed if all bacteraemia cases could be prevented was multiplied by the number of admitted patients to obtain the total excess LoS.

Result: The estimated total number of extra ICU days caused by 666 bacteraemia cases were estimated at 2453 (95% CI 1803 – 3103) days. The excess number of days were overestimated when ignoring time-varying confounding (2845, 95% CI 2276 – 3415) or when completely ignoring confounding (2838, 95% CI 2101 – 3575).

Conclusion

ICU-acquired bacteraemia was associated with a substantial excess LoS. Wider adoption of IPW survival curves or alternative techniques that address time-varying confounding could lead to better informed decision making around nosocomial infections and other time-dependent exposures.

Keywords: bacteraemia; infection; excess length of stay; causal inference; confounding
Introduction

Healthcare-associated infections (HCAIs) represent a public health problem and are associated with substantial morbidity, mortality, and costs.[1-5] A substantial proportion of HCAIs can be prevented by implementing infection prevention and control measures.[4,6-9]

While interventions may be effective, it is important to assess whether they are also cost-effective in the context of limited funds for healthcare. A key driver of the costs of HCAIs and – depending on the economic perspective, reimbursement system and intervention – the cost-effectiveness of interventions targeting HCAI incidence is the excess length of stay (LoS) caused by these infections.[6,10] To obtain useful estimates for policy making, studies need to take into account the timing of infection and the fact that patients that acquire an infection may not only differ at the day of admission, but also may deteriorate more before acquiring infection than patients who remain infection-free.[11]

Common methodologies to account for the timing of infection are multi-state models and Cox regression with infection implemented as a time-varying variable.[12-14] Applications of multi-state models often do not adjust for baseline confounding and never correctly adjust for time-varying confounding (e.g. severity of illness),[12,15] which can limit their use. Furthermore, hazard ratios obtained from Cox regression models are often misinterpreted and do not readily translate into excess LoS in days.[16,17]

To address limitations of commonly applied methods, time-varying confounding can be adjusted for using marginal structural models fitted via inverse probability weighting (IPW).[11,18] In the presence of measured time-varying confounding which is affected by past exposure, these and other g-methods have been shown to provide valid results where more conventional methodologies produce biased estimates.[19-22]

When a time-varying confounder is also an intermediate variable on the causal pathway (e.g. severity of illness is affected by the history of infection), adjusting for it would partly remove the
effect of the exposure when using conventional regression techniques; it would moreover introduce
collider-stratification bias, a form of selection bias that occurs when one controls for a common
effect of exposure and outcome. [11,15,23] This has been empirically confirmed in simulation
studies, which showed that a marginal structural model with IPW resulted in unbiased estimates of
the effect of time-dependent harmful exposures on the hazard of hospital discharge. [20] In contrast,
adjusting for time-varying confounding using a conventional Cox regression model with time-varying
covariates, or freezing the time-varying confounder at their level before occurrence of the exposure
resulted in substantial bias. [20]

Previous studies have not applied methods that correctly account for potential time-varying
confounding when estimating excess LoS measured in days. [15] We recently used Cox proportional
hazards regression to estimate what the observed risk of death in and discharge from the ICU would
be if all patients in an ICU would remain bacteraemia free compared to the actual situation where
some patient do acquire bacteraemia. [11] The corresponding survival curves could theoretically be
combined to estimate the excess LoS. However, when the proportional hazards assumption holds
conditional on a set of covariates, then it is almost guaranteed not to hold when one covariate is
added or dropped. It is unlikely that one would have selected the precise set of covariates for which
the proportional hazards assumption holds.

In view of this, we will instead make use of Kaplan-Meier (KM) curves along with inverse probability
weighting to predict what the LoS distribution would be if nosocomial infections could be prevented
[24,25] Provided all confounders are measured and included in the model to create the inverse
probability weights one can assess excess LoS by comparing the observed LoS with that in the
counterfactual situation, where all patients would remain infection-free. A major advantage of this
method compared to several other approaches currently applied to estimate the excess LoS is that it
simultaneously: i) does not suffer from bias due to ignoring the timing of infection; ii) can address
(measured, time-varying) confounding; iii) does not require a proportional hazards assumption; iv)
has no built-in selection bias; and iv) produces excess LoS measured in days. We show using a case study how excess length of stay due to time-dependent exposures such as ICU-acquired bacteraemia can be estimated using KM estimators with IPW.

Methods

Data

For our case study, we used data from all patients admitted to two 15-bed general ICUs at St Thomas’ Hospitals (London, UK) between January 2002 and March 2006.[11,18] Besides daily measurements on various invasive procedures and markers of severity of illness, these data contain information on admission, discharge, mortality, and administration of antimicrobial therapy.[11] Patients with an ICU LoS of less than three days were excluded because patients could, by definition, only acquire bacteraemia after being two days in the ICU. From the remaining cohort, we excluded patients with a blood culture positive for bacteria during the first two days in the ICU, to exclude community-acquired cases. After applying these exclusion criteria, a first blood culture positive for any bacteria obtained from the patient more than two days after ICU admission was considered an ICU-acquired bacteraemia. In line with other studies,[1-3,11-14,18] only first infections were considered. Onset of infection was defined utilising the time of the specimen taken as a proxy for time of infection.

The final model (see Supplementary Material 1 for more details on all considered confounders and model selection) included age (restricted cubic spline with 2 degrees of freedom) and gender as baseline covariates and the Acute Physiology and Chronic Health Evaluation (APACHE) II score, receipt of any systemic antibiotic (yes/no), mechanical ventilation and central lines as time-varying confounders.[18] For the APACHE score and antibiotic use we used lagged values 2 days before to recognize that these variables measured within 24 hours before the onset of bacteraemia are
possible surrogate markers for an infection that was incubating and may therefore be affected by bacteraemia [11,18,26]. Besides using these lagged values we also adjusted for the cumulative previous time on mechanical ventilation and having received antibiotics (days on treatment, DOT). Furthermore, an interaction between the cumulative previous time on antibiotics and the cumulative previous time having received mechanical ventilation and an interaction between the presence of central lines on the first day of admission and the time-varying 1-day lagged presence of central lines. Interactions were also included in the final model (see Supplementary Material 1, including sensitivity analyses using different lags).

**Analyses**

We estimated the effect of bacteraemia on LoS using several steps. We estimated the survival probabilities up to day 45 in the ICU for the observed data using conventional KM methodology. Subsequently we summed the survival probabilities for each day up to day $t=45$ to obtain the average LoS up to day 45. This is the restricted mean survival time (RMST), which is equivalent to the area under the KM curve up to day 45.[27] It can be interpreted as the average survival time within the interval of interest.[27] In line with others,[2,28] we used a cut-off of 45 days because the effect of bacteraemia acquired later during the ICU stay may have a more limited impact and adjusting for potential time-varying confounding is more challenging for late infections, because there are simply insufficient patients who acquire infection at the same time. Furthermore, only a very small proportion of patients stayed longer than 45 days in the ICU (3%), and the predicted probability of staying for at least 45 days in the ICU if bacteraemia would be prevented was even lower (1.9%).

Subsequently, we treated bacteraemia as a ‘censoring’ event. Because patients who acquire an infection likely differ from patients who remain infection-free, a conventional KM curve based on these censored event times would be biased. We adjusted for this bias using IPW.[29] The weights were constructed using pooled logistic regression models for the probability of censoring on each
day, in this case acquiring bacteraemia.\cite{11} Confounding was removed by reweighting patients in the risk set (those who were still present in the hospital and not artificially censored because of bacteraemia) on each day.\cite{11,19}

KM methodology with IPW was subsequently applied to the data. Subsequently, the survival probabilities for each day up to day $t=45$ were summed to obtain the average LoS in the absence of bacteraemia.

The difference between the average observed LoS and the average LoS that would be observed if all bacteraemias could be prevented was multiplied by the number of admitted patients, to obtain the total excess LoS attributable to ICU-acquired bacteraemias. We estimated 95\% confidence intervals as described in the Supplementary Material 2.

The effect per infection can be obtained by dividing the difference between the average observed LoS and the counterfactual average LoS in the absence of infection by the probability of acquiring an infection during the ICU stay. All analyses were performed in R version 3.5.1 (R code in Supplementary Material 3).
Results

In total 2,914 patients were admitted to the ICU and stayed more than 2 days in the ICU, contributing to 3,157 ICU admissions. Table 1 shows the characteristics of included admissions. Most patients had a relatively short total LoS (median 7 days, 25\textsuperscript{th} - 75\textsuperscript{th} percentile: 4 - 15), resulting in a highly skewed distribution (Figure 1, left panel). As mentioned earlier, patients were only included if they stayed more than 2 days in the ICU, however the first 2 days were added to the average LoS. The observed average LoS in the ICU was 11.44 (95\% CI 11.07 – 11.81) days when restricting the follow-up to the first 45 days after admission. There were 666 blood cultures positive for bacteria, with coagulase-negative staphylococci (44\%), mixed bacteria (17\%), \textit{Staphylococcus aureus} (8\%), \textit{Pseudomonas aeruginosa} (6\%) and \textit{Escherichia coli} (4\%) being the most commonly isolated bacteria. The majority (82\%) of the 666 ICU-acquired bacteraemias occurred within the first two weeks after admission (Figure 1, middle panel). However, among those still at risk of acquiring a bacteraemia, the daily probability of acquiring it initially increased over time (Figure 1, right panel). The width of the confidence intervals around these probabilities increased over time due to the decreasing number of patients still at risk, precluding conclusions about the risk of bacteraemia for long-stay patients.

\textit{Inverse-probability weighted survival curves}

Details of the pooled logistic models used to create the inverse-probability weights are provided in the Supplementary Material. The weights had a median and mean of 1.00 and 1.01, respectively, and an interquartile range and standard deviation of 0.06 and 0.13 (range 0.44 – 2.09), respectively. The values raise no concern that our results may be affected by extreme weights.[29] If all 666 ICU-acquired bacteraemias would be prevented, the IPW KM curve predicted that patients would stay on average 10.66 (95\% CI 10.27 – 11.06) days when restricting the follow-up to the first 45 days after admission. The estimated total number of extra days in the ICU due to bacteraemia
were estimated at 2453 (95% CI 1803–3103) days. The estimated number of excess days per infection were 3.7 days \((11.439 - 10.662) \times \left(\frac{666}{3157}\right)^{-1}\).

**Influence of confounding**

When ignoring confounding, using a weight of 1 for each observation, the number of excess days was estimated to be higher during the study period at 2838 (95% CI 2101–3575) days. Similarly, the number of excess days was substantially overestimated when taking only confounders measured at admission into account, with an estimated number of 2845 (95% CI 2276–3415) days attributable to infection.

**Discussion**

In this article, we illustrated how to estimate the excess length-of-stay associated with time-dependent exposures, such as ICU-acquired bacteraemia, in the presence of time-varying confounding. The number of excess days due to ICU-acquired bacteraemia was substantially overestimated when ignoring time-varying confounding, suggesting that future studies should adopt the methodology presented here or alternative techniques [22,23] that correctly address time-varying confounding without inducing collider-stratification bias or removing the indirect effects of early infection on the length-of-stay that are mediated through the considered confounders.

Inverse-probability-weighted KM methodology has appealing features compared to other techniques used in the literature. This includes the ability to simultaneously address the time-dependent nature of health-care acquired infections, time-invariant and time-varying confounding, as well as producing excess LoS estimates measured in days. Moreover, in contrast to many other approaches no (semi-)parametric assumptions are needed on the distribution of LoS. The time-dependent nature of ICU-acquired bacteraemia was taken into account using IPW based on the daily probability of acquiring bacteraemia among those still at risk. Other studies have addressed the
time-dependent nature of nosocomial infections using multi-state models, without accounting for
time-varying confounding.[1-3] Given that one would expect that patients who acquire a
bacteraemia may be more severely ill and have deteriorated more than patients who remain
infection-free, these previous studies have likely resulted in confounded estimates, thereby
potentially overestimating the effect on excess LoS. While there are some recent studies that used g-
methods such as inverse probability weighting to address time-varying confounding to assess the
effect of infections on ICU-mortality and ICU-discharge,[11,18,26,30,31] to our knowledge this is the
first study that uses similar methodology to estimate the effect of time-varying exposures on excess
LoS.
While we focused on ICU-acquired bacteraemia, the methodology proposed here can be applied to
address any research question on the attributable effect of a (dichotomous) time-varying exposure
on an uncensored event time. Whenever disease severity influences the decision to initiate drug
therapy, time-varying confounding is likely.[20] If such confounding is influenced by prior exposure,
thus also being an intermediate on the causal pathway, conventional regression approaches will
provide biased estimates by removing part of the effect of the exposure and introducing selection
bias. If there are competing events or other forms of censoring, our methodology can still be used if
censoring is more broadly defined by treating both the exposure of interest and competing risks as
censoring events, provided that there is no unmeasured confounding.
Our results add to the growing literature showing that ignoring confounding or only adjusting for
confounders measured at baseline could result in substantial bias.[11,19,20,26,30,31] In any case,
evaluating whether (time-varying) confounding might play a role is preferable over directly applying
multi-state or other models without such adjustment, as such approaches implicitly assume that
time-varying confounding can be ignored.
Limitations

There are several limitations to our study.

Regarding our case study, the estimates of the total excess number of ICU days due to ICU-acquired bacteraemia rely on accurate measurements of all relevant confounders. We did not have information on some potential time-varying confounders such as surgeries or abdominal perforation and baseline confounders such as main reason for admission, which may both increase the risk of infection as well as the risk of death independent of infection. Therefore, we may have overestimated the effect of ICU-acquired bacteraemia and underestimated the impact of not accounting for all time-varying confounders, thereby further strengthening the case for collection and correct adjustment for time-varying confounders in future studies. When creating the pooled logistic regression models that are used for estimation of the weights it is important to consider potential relevant interactions and cumulative measures of daily measurements as these typically capture the evolution of severity of illness better than simple daily measurements alone.

The causal inference literature highlights exchangeability (implying no unmeasured confounding, discussed above), positivity (the probability of acquiring bacteraemia or remaining bacteraemia-free being positive for every individual), and consistency (informally the need for a well-defined (hypothetical) intervention) are necessary conditions for causal inference.[30] The mean of our estimated weights was 1.00 and there were no extreme values, thereby raising no concern about violation of the positivity assumption [29]. The need for a well-defined intervention (consistency assumption) has been highly debated in the literature,[32-34] with common misconceptions being that the hypothetical intervention needs to be currently feasible, or that the net effect of the exposure of interest cannot be estimated if there is not a single well-defined (hypothetical) intervention that could be used to alter the exposure.[33,34] Specifically for our study, the results can be viewed as providing an estimate of the harmful net effect of ICU-acquired bacteraemia. This effect likely differs from the effect of an intervention to prevent ICU-acquired bacteraemia because
it is unlikely that such intervention would just prevent the development of bacteraemia without having any other effects.[33]

Onset of infection was defined using the time the first positive specimen was taken, however it is uncertain whether onset may have occurred earlier. We used lagged values measured from the previous day to predict infection (and 2 days for the APACHE score and antibiotic treatment) to prevent adjustment for post-infection measurements.

Some positive blood cultures may have actually been contaminated blood samples (e.g. some of those positive for coagulase-negative staphylococci), thereby potentially leading to an underestimation of the effect of true bacteraemia. Of note, this dataset was from before widespread implementation of infection control bundles for vascular catheter care, when coagulase-negative staphylococci infections were more frequent and significant than now. The proportion of bacterial infections that are resistant to commonly used antibiotics has increased since the end of the study period and antibiotic resistance has been associated with increases in LoS.[2,3] While these studies estimating the effect of resistance on LoS did not adjust for (time-varying) confounding, the current effect of ICU-acquired bacteraemia may be larger than the estimate from this study.

We focused on bacteraemias in general, which is a combination of all different types of bacteria with different antibiotic resistance profiles causing bacteraemia. The effect of specific bacteria and associated resistances could be estimated in larger multi-centre studies using similar methodology.

Finally, we could obtain the average effect per infection using the IPW KM methodology. However, this approach does not provide the excess LoS due to acquisition of an infection on a given day after admission, which is potentially easier to interpret given the likely varying effects of acquisition of infections early after admission or much later during the ICU stay.
Conclusion

ICU-acquired bacteraemia is associated with a substantial number of excess days in the ICU, even after adjusting for time-varying confounding. Inverse probability weighted Kaplan Meier curves form a relatively simple method to estimate the causal effect of time-varying exposures on excess length of hospital stay. Wider adoption of this, or other techniques that correctly address time-varying confounding, could lead to better informed decision making.
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Table 1. Characteristics of patients for ICU admissions of more than 2 days during the first 3-45 days after admission.

| Characteristics                                      | Admissions (N=3,157)$^a$ |
|------------------------------------------------------|--------------------------|
| Male sex (%)                                         | 1915 (61)                |
| Age (years), median (25$^{th}$-75$^{th}$ percentile)  | 64 (50 – 74)             |
| APACHE score at admission, median (25$^{th}$-75$^{th}$ percentile) | 18 (14 – 22)             |
| Central lines at admission (%)                       | 2182 (69)                |
| Number of antibiotics at admission, median (25$^{th}$-75$^{th}$ percentile) | 0 (0 – 2)                |
| Mechanical ventilation at admission (%)              | 2376 (75)                |
| Died in ICU (%)                                      | 626 (20)                 |

$^a$ Given that patients with an ICU-stay less than three days were excluded, the percentage of patients receiving invasive procedures is likely larger than for the average of all patients admitted to the ICU.
Figure 1. Distributions of total length of ICU stay (left), day of bacteraemia onset (middle) and the probability of acquiring bacteraemia on each day (right). The error bars in the right panel represent 95% confidence intervals based on Wilson score intervals.
