TOPICAL REVIEW

Revisiting some chalcogenides for thermoelectricity

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Abstract
Thermoelectric materials that are efficient well above ambient temperature are needed to convert waste-heat into electricity. Many thermoelectric oxides were investigated for this purpose, but their power factor (PF) values were too small (∼10^{-4} \, \text{W} \, \text{m}^{-1} \, \text{K}^{-2}) to yield a satisfactory figure of merit \(zT\). Changing the anions from \(\text{O}^{2-}\) to \(\text{S}^{2-}\) and then to \(\text{Se}^{2-}\) is a way to increase the covalency. In this review, some examples of sulfides (binary \(\text{Cr–S}\) or derived from layered \(\text{TiS}_2\)) and an example of selenides, \(\text{AgCrSe}_2\), have been selected to illustrate the characteristic features of their physical properties. The comparison of the only two semiconducting binary chromium sulfides and of a layered \(\text{AgCrSe}_2\) selenide shows that the PF values are also in the same order of magnitude as those of transition metal oxides. In contrast, the PF values of the layered sulfides \(\text{TiS}_2\) and \(\text{Cu}_0\text{TiS}_2\) are higher, reaching ∼10^{-3} \, \text{W} \, \text{m}^{-1} \, \text{K}^{-2}. Apparently the magnetism related to the Cr–S network is detrimental for the PF when compared to the d\(^0\) character of the Ti\(^{4+}\) based sulfides. Finally, the very low PF in \(\text{AgCrSe}_2\) (\(PF = 2.25 \times 10^{-4} \, \text{W} \, \text{m}^{-1} \, \text{K}^{-2}\) at 700 K) is compensated by a very low thermal conductivity (\(\kappa = 0.2 \, \text{W} \, \text{m}^{-1} \, \text{K}^{-1}\) from the measured \(C_p\)) leading to the highest \(zT\) value among the reviewed compounds (\(zT_{700 \, \text{K}} = 0.8\)). The existence of a glassy-like state for the \(\text{Ag}^+\) cations above 475 K is believed to be responsible for this result. This result demonstrates that the phonon engineering in open frameworks is a very interesting way to generate efficient thermoelectric materials.

Keywords: thermoelectricity, chromium sulfide, chromium selenide, titanium sulfide

1. Introduction

Increasing the figure of merit, \(z\), for thermoelectric materials to convert waste-heat into electricity is a fascinating challenge for the solid state chemists and physicists. The product of figure of merit and temperature, \(T\), is a dimensionless parameter defined as \(zT = (S^2/\rho \kappa)T\), where \(S\), \(\rho\) and \(\kappa\) are the Seebeck coefficient, electrical resistivity and thermal conductivity, respectively; \(z\) is also the power factor, \(PF = S^2/\rho\), divided by \(\kappa\). Best \(zT\) values require a combination of semiconducting properties, as the highest PF values are typically found in degenerate semiconductors, together with low thermal conductivities that are dominated by the lattice contribution. This explains why Bi\(_2\)Te\(_3\) is the only commercial thermoelectric (TE) material [1].

To harvest waste-heat at temperature beyond 600 K, other TE candidates have been intensively studied such as skutterudites derived from (Co, Fe)Sb\(_3\); thermoelectric materials composed of tellurium, antimony, germanium and silver (TAGS); clathrates; and Zintl phases such as Y\(_{14}\)MnSb\(_{11}\) [2]. Transition metal oxides (TMO) provide another large class of potential TE materials [3]. Depending
on the TM-O bonding, the 3d electrons in TMO can be localized or delocalized with electronic correlations that invalidate the degenerate semiconductor picture. However, the typical PF values for best TE oxides are $\sim 10^{-4} \text{Wm}^{-1} \text{K}^{-2}$, as for Na$_2$CoO$_2$ or ‘Co$_3$Co$_2$O$_6$’ [4]. Increasing the PF requires systems with larger covalency, which can be achieved by changing the anions. Interesting candidates for TE materials can also be found among TM chalcogenides, but contrasting with the oxides, anion–anion bonding in chalcogenides can lead to molecular anion. Besides, the higher covalency in chalcogenides favors the metal–metal interactions [5]. Concerning the thermoelectric selenides, several recent reports illustrate this different chemistry for Bi$_2$Se$_3$ nanostructures [6], doped PbSe [7], quaternary tin selenide K$_{1-x}$Sn$_x$-Bi$_{1+y}$Se$_{2}$ [8], p-type Cu$_{2+y}$Zn$_{1-y}$GeSe$_4$ [9] and Ag$_2$Se [10]. Also $\overline{z}T = 0.6$ at 1150 K for a (Cu/Fe)$_2$Mo$_8$Se$_8$ Chevrel phase was reported [11]. In these molybdenum chalcogenides, the Mo ions are forming [Mo$_6$] octahedra surrounded by a distorted cubic of anions. The Mo$_8$X$_8$ framework creates channels that are partly filled with rattling cations such as Cu/Fe in the aforementioned compound. These cations are believed to be responsible for unexpectedly low $\kappa$ values in metallic compounds ($\rho_300K \sim 1 \text{m}\Omega \text{cm}^{-1}$), as low as $\kappa \approx 1.3 \text{W m}^{-1} \text{K}^{-1}$ at 1000 K in (Cu/Fe)$_2$Mo$_8$Se$_8$. Sulfides have covalency intermediate to those of oxides and selenides. They have been broadly investigated for their thermoelectric properties, as illustrated by the recent reports on BaVS$_3$ [12], TiS$_2$ [13], complex layered TiS$_2$-based compounds [14] and doped PbS [15]. In that respect, the review by Rao and Pishardy [5] is very instructive. All the transition metal sulfides (TMS) and disulfides (TMS$_2$) were described. Among the TM sulfides, the possibility of transition from semiconductors to metals in the range CrS to Cr$_2$S$_3$ attracted our attention to the Cr–S binary system. The investigation of sulfides was also motivated by the report of a high $zt$ value for the ternary compound, CuCr$_2$S$_3$, in the form of crystals flakes, reaching $zt = 2$ at 300 K [16]. As for the TMO, in which the magnetism was shown to play a role with the spin and degeneracy term $\beta$ used in the modified Heikes formula [17], it is also important to report on the physical properties including magnetic and electronic properties as to evaluate these materials for thermoelectricity.

In this review, a limited number of chalcogenides was selected to illustrate some relationships between structure, magnetism and thermoelectric properties. Most of the Cr$_{1-x}$S binary compounds, including Cr$_2$S$_3$, crystallize in structures derived from NiAs type; the Cr analogue to the TiS$_2$ was not reported. Two examples were chosen, Cr$_2$S$_3$ and CrS$_6$, a semiconductor and a metal. Furthermore, in contrast to all Cr/S binary compounds, including Cr$_2$S$_3$, which are antiferromagnetic, the magnetism of CrS$_6$ is unique with a ‘ferromagnetic-like’ transition [18]. Then two layered ternary chalcogenides, Cu$_2$TiS$_2$ [19] and AgCrS$_2$ [20], are reviewed to emphasize the important role of the CdI$_2$-type layers. Intercalation of the countercations between these layers can be used to reach low $\kappa$ values.

### 2. Synthesis

As the measurements of thermoelectric properties require very dense (porosity $\sim 0\%$) materials, all the present chalcogenides have been prepared by a two-step method. In the first step, elements (Cr, Ti, Ag, S and Se) were mixed in stoichiometric amounts to prepare about 10 g of Cr$_2$S$_3$, CrS$_6$, TiS$_2$ and AgCrS$_2$ powders. After pressing, bars of typical dimensions $2 \times 2 \times 10 \text{mm}$ were set in silica tubes and sealed under primary vacuum. The ampoules were heated at temperatures $T_h$ for durations $t$ that are summarized in table 1. After cooling down to room temperature in $\sim 6h$, the reacted bars were crushed to obtain the powders used for the spark plasma sintering (SPS, the second step). The temperature used for the SPS ($T_{SPS}$) and the time at $T_{SPS}$ ($t_{SPS}$) are also indicated in table 1. The typical time for cooling down from $T_{SPS}$ to room temperature was 10 min. The density of all the sintered cylinders was higher than 95% of the theoretical density. In the case of Cu$_2$TiS$_2$, the stoichiometric amount $x$ of metallic copper was added to the TiS$_2$ powder to obtain a homogeneous mixture prior to the SPS treatment.

### 3. Structural characterizations

Structural characterizations were performed by powder x-ray diffraction (XRD) measured at ambient temperature after the first synthesis step and then after the SPS process. For that purpose, we used a PANalytical Xpert Pro diffractometer with CuK$\alpha$ radiation ($5^\circ \leq 2\theta \leq 120^\circ$). In some cases, transmission electron microscopy (TEM) was employed for electron diffraction, energy dispersive x-ray (EDX) analysis and high-resolution imaging.

#### 3.1. Cr$_2$S$_3$

The as-prepared powder corresponds to the $\overline{R} \bar{3}$ space group $[a = 5.9339(1) \text{Å} \text{and } c = 16.67724(4) \text{Å} \text{with a Cr/S atomic ratio from EDX in good agreement with the value of 2/3 from the chemical formula [21]. Interestingly, the sample obtained by SPS crystallizes in the crystallographic form reported for trigonal Cr$_2$S$_3$, i.e. in a trigonal structure [SG: P3 1c; a = 5.9441(1) \text{Å} \text{and } c = 11.20339(2) \text{Å}]. Both sets of unit cell parameters are consistent with previous studies [22–24]. The different set found for the SPS-treated sample could be related to two factors. The first one is the deviation from the 2:3 Cr/S atomic ratio in the SPS sample, with a 2:2.8 ratio detected by EDX, and the second one is the rapid cooling used at the end of the SPS process. The second reason is consistent with previous reports in which

| $T_h$ (C) | $t$ (h) | $T_{SPS}$ (C) | $t_{SPS}$ (min) |
|----------|---------|--------------|-----------------|
| Cr$_2$S$_3$ | 900 | 12 | 1100 | 30 |
| CrS$_6$ | 900 | 12 | 900 | 10 |
| Cu$_2$TiS$_2$ | 650 | 12 | 900 | 30 |
| AgCrS$_2$ | 900 | 12 | 700 | 30 |
Figure 1. Structural models for Cr$_2$S$_3$ (left) and Cr$_5$S$_6$ (right). The stacking of S layers creates octahedral voids which are fully occupied to form a dense CrS layer of CrS$_6$ edge-shared octahedra which alternates with a partially filled layer, Cr$_{1/3}$S (left) and Cr$_{2/3}$S (right) for Cr$_2$S$_3$ and Cr$_5$S$_6$, respectively.

Figure 2. Structural models for Cr$_2$S$_3$. Two sequences, 1–2–3 and 1–2–1–2, are obtained along the stacking direction c, corresponding to the rhombohedral and trigonal forms, respectively.

quenching was necessary to stabilize the trigonal form. In the following, the SPS-prepared form is labeled ‘$T$-Cr$_2$S$_{2.8}$’ and the precursor ‘$R$-Cr$_2$S$_3$’.

3.2. Cr$_5$S$_6$

The powders of both as-prepared and SPS Cr$_5$S$_6$ were found to crystallize in the $P\overline{3}1c$ trigonal space-group, with $a = b \approx 5.98$ Å and $c \approx 11.509$ Å. These values are close to those first reported in [24]. They are also close to that of the trigonal form of Cr$_2$S$_3$ showing that these structures all derive from the NiAs type. Small amounts (~1% from x-ray data) of Cr$_3$S$_4$ impurity were found in the $T$-Cr$_2$S$_{2.8}$ sample, which could be related to the S departure. Similarly, a Cr$_7$S$_8$ impurity was detected in the SPS-prepared Cr$_5$S$_6$ phase.

4. Structural relationships

4.1. Cr$_{1-x}$S sulfides

The NiAs-type structure of CrS can be described by starting from the hexagonal packing of the S atoms (figure 1). In that network, octahedral voids are created that can be fully or partially occupied by the Cr cations. In $R$-Cr$_2$S$_3$, $T$-Cr$_2$S$_{2.8}$ and trigonal $T$-Cr$_5$S$_6$, the Cr vacancies are ordered in every alternate layer along the $c$-axis with a 1/3 occupation by Cr in Cr$_2$S$_3$ and 2/3 in the case of Cr$_5$S$_6$ (figure 1). In addition to their different atomic ratio, the difference between $R$-Cr$_2$S$_3$ and $T$-Cr$_2$S$_{2.8}$ originates also from the ordering and disordering, respectively, of the Cr species at the level of the Cr-deficient layer over three different crystallographic positions (figure 2). Thus, going from Cr$_2$S$_3$ to Cr$_5$S$_6$, one expects a more 3D Cr–S magnetic network in the latter, and
for the Cr formal oxidation state (considering $S^{2-}$), a decrease from $\nu_{C2} = 3$ to $\nu_{C1} = 2.4$, i.e. a larger electron concentration in $Cr_3S_6$, with an intermediate value $\nu_{C1} = 2.8$ for $T$-$Cr_2S_3$.

4.2. TiS$_2$ and AgCrSe$_2$

TiS$_2$ crystallizes in the CdI$_2$ structure within the $P\overline{3}$1$m$ space group. The edge-shared layers of TiS$_6$ octahedra are interconnected through van der Waals forces, creating octahedral sites that can be occupied by intercalated species [25]. The as-prepared TiS$_2$ precursor can be indexed in the $P\overline{3}$1$m$ space group with parameters $a = 3.4062$ Å and $c = 5.707$ Å in good agreement with the values from the literature ($a = 3.4073$ Å and $c = 5.6953$ Å [26]). After SPS, the Cu intercalation with starting composition corresponding to $Cu_xTiS_2$ with $x \leq 0.10$ was confirmed by EDX and powder XRD. In particular, the $c$-axis parameter along the stacking direction of the TiS$_2$ slabs increased from 5.707 Å to 5.760 Å with $x$ increasing from $x = 0$ to $x = 0.10$ [19].

In AgCrSe$_2$ [27], the CrSe$_2$ layers, also of the CdI$_2$ type, are stacked in a way that half tetrahedral sites are occupied by Ag$^{+}$ in the interspace (figure 3). In fact, the network made by the tetrahedra centers forms a honeycomb network with only one type of tetrahedra occupied below 475 K (ordered form). At higher temperatures it evolves toward a disordered state where the two types of tetrahedra are randomly occupied. At 300 K, the unit cell parameters are fitted in the polar space group $R\overline{3}$m with $a = 3.682$ Å and $c = 21.23$ Å [27].

For the Cu$_x$TiS$_2$ and AgCrSe$_2$ layered compounds, as pressure is used during the SPS treatments, it tends to align parallel the largest faces ($ab$-plane) of the platelet-like microcrystals leading to a clear texturation [19]. For these materials, all the $\rho$, $S$ and $\kappa$ measurements have been performed along the directions lying in the conducting planes $ab$.

5. Magnetoresistance: role of the spins on the transport properties in $Cr_2S_3$ and $Cr_3S_6$

The comparison of the temperature-dependent magnetic susceptibilities ($\chi$) of the $Cr_2S_3$ samples [21], measured with a SQUID magnetometer, shows that depending on the crystallographic form, either a ferromagnetic-like component develops for $R$-$Cr_2S_3$ below $T_N = 120$ K, the antiferromagnetic (AF) transition, or for $T$-$Cr_2S_3$ a pure AF transition occurs below 100 K (figure 4). The presence of a ferromagnet-like component in $R$-$Cr_2S_3$, in good consistency with the literature [28], creates some spin scattering above $T_N$, so that a clear decrease of the electrical resistivity ($\rho$) is seen below $T_N$ (figure 5(a)). Accordingly, upon application of an external magnetic field, a negative magnetoresistance effect is observed in $R$-$Cr_2S_3$ but not in $T$-$Cr_2S_3$ (figure 5(a)). These data are supported by the isothermal curve collected at 100 K showing a negative magnetoresistance of $-8\%$ in 9 T for the $R$-$Cr_2S_3$ compound (figure 5(b)).

The magnetism of $Cr_3S_6$ is more complex as can be seen on the corresponding $\chi(T)$ curve (figure 6). A crenel
shape curve is observed between two magnetic transitions at 160 and 300 K. The existence of ferrimagnetic (FI) state between these temperatures, followed by an AF one below 160 K, is well documented in the literature [29–31]. However, as mentioned in the first papers by Yuzuri and Nakamura [31], the FI component was found to be dependent on the quality of the vacancy ordering at the level of the Cr$_{2/3}$S layers of the structure. Increasing this disorder was supposed to create some breaking along the magnetic exchange directions. This is supported by the comparison between the curves of the Cr$_{3}$S$_{6}$ precursor prepared in a closed vessel (cooling in 6 h from 900 °C) with that of the final product sintered by SPS with a 10 min cooling. The $\chi'$ values between $T_{C}$ and $T_{N}$ are decreased by at least one order of magnitude after SPS (figure 6). Thus, there is a parallel to be made with Cr$_{2}$S$_{3}$ which ferromagnetic-like component is suppressed after SPS, i.e. in the more disordered trigonal crystallographic form T-Cr$_{2}$S$_{3}$, Cr$_{3}$S$_{6}$ exhibits a more metallic behavior (figure 7) as compared to the Cr$_{2}$S$_{3}$ samples (figure 5(a)), which both show larger $\rho$ values at 5 K than at 300 K. In Cr$_{3}$S$_{6}$, the $d\rho/dT$ coefficient is always positive (figure 7), with a slight change of slope at $T_{N}$ as in Cr$_{2}$S$_{3}$. Despite that an FI-like component is observed on the $\chi(T)$ curves, the absolute values of magnetoresistance are limited, reaching a maximum at 150 K (near $T_{N}$) of only 2% in 7 T (figure 8). Interestingly, these magnetoresistance curves measured with current perpendicular to the magnetic field direction reveal the existence of a transition induced by the external magnetic field, hysteretic and with characteristic magnetic field that decreases as temperature increases from 140 K (below $T_{N}$) to $T_{N}$. This field-induced transition reflects the hysteretic-field-driven transition from AF to FI phase in both the precursor and SPS-prepared sample (figure 8). In 9 T, the maximum magnetization value corresponds to $\sim 0.08 \mu_{B}/\text{Cr}$ in the sample against 0.13 $\mu_{B}/\text{Cr}$ in the precursor. They are similar to the value of 0.07 $\mu_{B}/\text{Cr}$ reached at 100 K (below $T_{N}$) in the R-Cr$_{2}$S$_{3}$ sample (inset of figure 5(a)). The specific heat measurements performed without magnetic field on the Cr$_{3}$S$_{6}$ sample (figure 9) confirm the existence of two magnetic transitions at 160 and 300 K.

![Figure 4](image1.png)

Figure 4. Temperature-dependent magnetic susceptibility ($\chi = M/H$) for Cr$_{3}$S$_{6}$ before (rhombohedral R-Cr$_{3}$S$_{6}$, left $y$-axis) and after SPS (trigonal T-Cr$_{3}$S$_{3}$, right $y$-axis). The measurements were carried out in the zero-field cooling mode.

![Figure 5](image2.png)

Figure 5. (a) Normalized electrical resistivity ($\rho$) as a function of temperature for both Cr$_{3}$S$_{6}$ samples, rhombohedral R-Cr$_{3}$S$_{6}$ and trigonal T-Cr$_{3}$S$_{3}$. The data collected upon cooling in $H = 0$ and 7 T reveal the existence of a negative magnetoresistance in the $T_{N}$ region for the rhombohedral precursor R-Cr$_{3}$S$_{6}$. Inset: magnetic field driven magnetization ($M$) for both Cr$_{3}$S$_{6}$ samples ($T = 100$ K). (b) Magnetic field ($H$) driven normalized resistivity collected at 100 K for both Cr$_{3}$S$_{6}$ samples.

![Figure 6](image3.png)

Figure 6. Temperature dependence of the ac magnetic susceptibility ($\chi'$, real part) for Cr$_{3}$S$_{6}$, before and after SPS ($\mu_{b}H_{ac} = 10$ Oe, $f = 100$ Hz).
Figure 7. Normalized electrical resistivity for Cr$_5$S$_6$ (left y-axis). The corresponding $d\rho/dT = f(T)$ curve is also given for the SPS sample (right y-axis).

![Graph showing normalized electrical resistivity](image1)

Figure 8. Top panel: magnetic field ($H$) driven resistance ratio for Cr$_5$S$_6$. The temperatures are indicated in the bottom panel where the corresponding $M(H)$ curves are given. The measurements were performed with current perpendicular to $H$.

![Graph showing magnetic field driven resistance ratio](image2)

Finally, these measurements demonstrate that not only magnetic properties are sensitive to the preparation technique (i.e. to the structural disorder or/and S stoichiometry) but also the $\rho$ values. This is illustrated for Cr$_2$S$_{3-x}$: densification by SPS allows to reduce its $\rho$ by more than one order of magnitude, down to $\rho_{300K} = 2.65 \text{ m}\Omega \text{ cm}$ for $T$-Cr$_2$S$_{2.8}$ (table 2). This value is even slightly lower than that reported for a trigonal ($P\bar{3}1c$) Cr$_2$S$_{2.84}$ crystal ($\rho_{300K} = 5.0 \text{ m}\Omega \text{ cm}$ [23]).

6. Comparison of the power factors

6.1. Cr$_{1-x}$S sulfides

As mentioned in the introduction, the charge carriers in $R$-Cr$_2$S$_3$ and $T$-Cr$_2$S$_{2.8}$ samples can be anticipated from the chemical formula to be electrons created by the Cr$^{2+}$ species, with carrier concentration increasing from $R$-Cr$_2$S$_3$ to $T$-Cr$_2$S$_{2.8}$ and being even larger in Cr$_5$S$_6$. The comparison of the $S(T)$ curves (figures 10(a) and (b)) confirms that order, with $S_{300K}$ values of $-290$, $-70$, $-15$ and $-22 \mu$V K$^{-1}$ for the samples R-Cr$_2$S$_3$, T-Cr$_2$S$_{2.8}$, Cr$_5$S$_6$ precursor and SPS-Cr$_5$S$_6$, respectively. For both Cr$_2$S$_{3-x}$ samples, a slight change of slope is detected at $T_N$ in good agreement with the change detected on the $\rho(T)$ curves.

Although the $\rho(T)$ dependence differs for these Cr–S samples, all the $S(T)$ curves show a metal-like behavior above the magnetic transition temperatures with an increase of $|S|/T$ up to the highest temperature used for these measurements ($\sim 700$ K). This is illustrated in figure 11 for

| Sample         | $\rho_{300K}$ ($\Omega \text{ cm}$) | $\rho_{700K}$ ($\Omega \text{ cm}$) | $S_{300K}$ ($\mu$V K$^{-1}$) | $PF_{700K}$ ($\text{W m}^{-3} \text{ K}^{-2}$) | $\kappa_{700K}$ ($\text{W m}^{-1} \text{ K}^{-1}$) | $zT_{700K}$ |
|----------------|-------------------------------|-------------------------------|-------------------------------|--------------------------------|-----------------|-----------------|
| $R$-Cr$_2$S$_3$| 0.045                         | --                           | 100                           | $3.4 \times 10^{-4}$         | 2.0              | 0.12            |
| $T$-Cr$_2$S$_{2.8}$ | 0.00265                      | 0.0030                        | $-100$                        | $2.0 \times 10^{-4}$         | 2.8              | 0.05            |
| Cr$_5$S$_6$    | 0.00062                       | 0.00080                       | $-40$                         | 1.1 $\times 10^{-3}$         | 2.2              | 0.34            |
| Cu$_6$TIS$_2$  | 0.0015                        | 0.0070                        | $-270$                        | $1.0 \times 10^{-3}$         | 2.0              | 0.39            |
| $x=0.10$      | 0.0002                        | 0.0015                        | $-130$                        | $2.25 \times 10^{-4}$        | 0.2              | 0.8             |
| AgCrSe$_2$    | 0.12                          | 0.04                          | 300                           | --                            | --              | --              |

Table 2. Physical parameters.
6.2. Layered Cu$_x$TiS$_2$ and AgCrSe$_2$

The PF values of Cr$_5$S$_3$ and Cr$_5$S$_6$ are relatively small and similar to those reported in TE oxides. The values measured in the layered sulfides Cu$_x$TiS$_2$ for $x \leq 0.1$ are all around 1 mW m$^{-1}$ K$^{-2}$ at 700 K (figure 14 and table 2); $\rho$ and Seebeck coefficient depend on the Cu content $x$ which controls the amount of Ti$^{3+}$ electrons in the Ti$^{3+}$ matrix, with both $\rho$ and $|S|$ decreasing with increasing $x$. The AgCrSe$_2$ compound exhibits a lower PF value of $2.25 \times 10^{-3}$ W m$^{-1}$ K$^{-2}$ at 700 K (table 2, from the data of figure 15).

To summarize that part, chromium sulfides and selenide, with either more 3D or 2D structure, all exhibit lower PF values than usually expected for efficient TE materials. Low thermal conductivity values are thus required to increase $zT$ in these materials. The magnetism of Cr$_3^+$ (3d$^3$) is absent as shown for Cu$_x$TiS$_2$, with no magnetic ordering at low temperature, and the PF values are the highest reaching $\sim 10^{-3}$ W m$^{-1}$ K$^{-2}$ at 700 K. It must be also pointed out that the TiS$_2$ compound exhibits a high power factor of $1.7 \times 10^{-3}$ W m$^{-1}$ K$^{-2}$ at room temperature.

7. Thermal conductivities

The measurements were carried out above 300 K by combining the thermal diffusivity from the laser flash technique (Netzsch457), with heat capacity (DCS404).

The $\kappa(T)$ values for the dense Cr/S phase prepared by SPS are close to 2–3 W K$^{-1}$ m$^{-1}$ at 700 K (figures 12 and 13). Combining them with the PF$_{700k}$ values yields $zT$ of $0.05–0.1$ (table 2).

In Cu$_x$TiS$_2$, the $\kappa(T)$ curves of the SPS-prepared phases are evolving in the opposite direction with temperature, $\kappa$ decreasing as $T$ increases (figure 14). Although $\rho$ decreases by a factor of 4 as $x$ increases from 0 to 0.10, the values of $\kappa$ are almost independent of $x$. This indicates that the phonon part of $\kappa$, $\kappa_{ph}$, is reduced as $x$ increases (figure 14), i.e. as to compensate the electronic part of $\kappa$ that increases. Such a behavior can be explained by considering the structural disorder generated by the local Cu intercalation between the TiS$_2$ layers. Best $zT$ values are observed for Cu$_{0.10}$TiS$_2$ with $zT = 0.39$ at 700 K (figure 16). At high temperatures, the
The κ values are similar for Cu$_{0.10}$TiS$_2$, Cr$_3$S$_3$ and Cr$_2$S$_2$. The higher zT of Cu$_{0.10}$TiS$_2$ comes from its higher PF values.

In contrast, the measured κ values in AgCrSe$_2$ are much smaller at high temperatures, as low as κ = 0.2 W m$^{-1}$ K$^{-1}$ at 700 K (figure 15). This low κ could be related to the order–disorder transition in the Ag$^+$ separating layers occurring at 475 K. Above this temperature, the Ag$^+$ ions are randomly distributed over the two different crystallographic positions in AgCrSe$_2$, which is known to be a fast ionic conductor [32], and thus the disordered character of that layer is believed to be responsible for the glass-like values for κ. This could explain why κ is so low in that material, even lower than the κ = 0.5 W m$^{-1}$ K$^{-1}$ at 700 K value calculated by using the Dulong–Petit value for the specific heat (figure 17), which leads to \( zT = 0.32 \) instead of \( zT = 0.8 \). A similar behavior was recently reported in Cu$_3$Se [33], another superionic conductor with a liquid-like thermal conductivity, for which the specific heat at high temperatures decreases significantly below the 3Nk$_B$ value of the Dulong–Petit model, where N is the Avogadro constant and k$_B$ is the Boltzmann constant.
8. Conclusions

The reported comparison of several chalcogenides demonstrates that these materials could provide good candidates for thermoelectric devices. In the case of the chromium chalcogenides with structures deriving from either NiAs or CdI₂ types, magnetically ordered states set in at low temperatures. They are related to the magnetism of Cr³⁺, a high-spin d³ cation. In contrast to oxides, for which the Seebeck coefficient of La₁₋ₓSrₓCrO₃ orthochromites is explained at high temperature by considering the Heikes formula with an additional term of spin and orbital degeneracy [34], in the reviewed chromium chalcogenides, no S saturation is observed at high temperatures, the S(T) curves showing |S| α T metallic dependence. Although the physics differs from that of oxides, the power factor values are rather similar. The role of the spins can be evaluated by considering the higher PF value of the layered sulfide Cu₄TiS₂ containing a majority of the d⁰Ti³⁺ cations: at 300 K, the ρ value of Cu₄6₃TiS₂ is lower by one order of magnitude than that of Cr₃S₆ despite |S| of the former is higher. Thus, the spin scattering in the paramagnetic state could be detrimental to the PF. However, low PF values are not redhibitory as the thermal conductivity can be significantly reduced by cation disorder as in AgCrSe₂. In that respect, the compounds crystallizing in 2D structures, where disorder can be created between the conducting planes, are very promising. Finally, the SPS process enables the densification of chromium sulfides. Furthermore, this treatment favors a sulfur nonstoichiometry which is clearly evidenced in the case of ‘Cr₂S₃’ by SPS, the R-Cr₂S₃ precursor leads to a T-Cr₂S₃₋₀.₈ dense ceramic. For this type of binary sulfides such as Cr₂S₃ and Cr₃S₆, SPS densification allows to achieve better thermoelectric properties as compared to the precursors.

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