Experimental study of shale drillability with different bedding inclinations under varying wellbore pressure conditions

Shuai Chen1 · Xiangchao Shi1 · Heng Bao1,2 · Leiyu Gao1 · Jie Wu1

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Abstract
In the practice of shale gas development engineering, it is important to understand the physical and mechanical properties of shale. The bedding inclinations of shale are known to significantly influence its physical and mechanical properties. This study mainly examined the influence of bedding inclinations on drillability under different wellbore pressures. The bedding inclinations used in this study varied from 0° to 90°, with a gradient of 15°. The wellbore pressure values used varied from 0 to 25 MPa, with a gradient of 5 MPa. The results show that the drillability index of shale increases exponentially with increasing wellbore pressure at different bedding inclinations. The proposed exponential empirical model can describe the relationship between the drillability index and wellbore pressure. When the wellbore pressure is less than 15 MPa, bedding inclinations significantly influence the drillability index, and the drillability index of shale shows a “W”-type variation trend as the bedding inclinations increase in the range of 0° to 90°. The influence of bedding inclinations on drillability decreases gradually with increasing wellbore pressure. When the wellbore pressure increases to 25 MPa, the impact of bedding inclinations on drillability is virtually undetectable. The results of this study can provide reasonably insight into the effect of bedding inclinations on shale deformation under the drill bit, and useful prediction for the drillability index under in situ conditions.

Keywords Drillability · Wellbore Pressure · Bedding Inclinations · Shale

Introduction
Rock drillability was first proposed in 1927 by Tillson, who suggested that drillability reflects the degree of difficulty involved in breaking rock (White 1969). The concept has been used in formation classification, bit type selection, and drilling engineering design (Deng et al. 2007; Kelesisdis 2011; O Yarali and Kahraman 2011). The physical and mechanical parameters and logging information of rock are often used to describe rock drillability (Liu et al. 2005; Morris and I. 1969; S Hoseinie et al. 2012; Spaar 1995; Zou and Chen 1996) but cannot completely reflect the nature of drillability. Microdrilling experiments are generally adopted as an effective method to evaluate rock drillability (HEAD 1951; Rollw 1962; Tarkoy and Hendron 1975). The simulated bottom-hole conditions of a microdrilling experiment can be used to objectively evaluate rock drillability under real drilling conditions. The results of field drilling show that bottom-hole pressure conditions significantly influence rock drillability (Carpenter and Chris 2015; Nas et al. 2010), and laboratory experiments have shown that there are significant differences in the same rock under different bottom-hole pressures (Mao et al. 2018). Strong dipping strata usually result in severe borehole inclination (Da et al. 2015), which is an important technical problem in drilling engineering. Many scholars have conducted a large amount of research on the anisotropy characteristics of shale (Kolawole et al. 2021). However, few studies have examined how bedding inclination causes borehole inclination (Teng et al. 2017), especially in simulated bottom-hole conditions. However, controlling the wellbore along a predetermined trajectory is critical for subsequent oil and gas production.

In this study, a microdrilling experiment was used to study shale drillability. The effect of varying bottom-hole pressure on shale drillability with different bedding inclinations was studied using the action of a polycrystalline
diamond composite (PDC) microdrill bit. This study is the first to consider the influence of bedding inclinations on drillability under different wellbore pressures. Previous scholars studied drillability from the perspective of experimental equipment and the drilling environment. The research in this paper not only includes the above factors but also includes the influence of rock properties on drillability. Finding out the influence of bedding inclinations on rock breaking of the drill bit can provide the scientific basis for the selection of PDC drill bit in different bedding inclinations formation. Studying the impact of shale on drillability can improve the efficiency of bit fracturing in the formation and thus reduce drilling cost.

**Materials and methods**

**Material characterization**

The shale samples considered in this study originated from Pengshui County, Chongqing, China (E108.51 N29.44). The mineral composition of shale is approximately 30% clay and 37% quartz. The mineral composition of the shale used in this study is shown in Fig. 1. The average porosity of the shale was measured as 3.27%. The shale was too compact to measure the gas permeability. The bedding plane of the shale was well developed. The rock samples were prepared with different bedding inclinations. When the loading direction was parallel with the direction of the bedding plane, the inclination direction was set to 0°. When the loading direction was perpendicular to the bedding plane, the inclination direction was set to 90° (see Fig. 2). The HS-YS2A rock acoustic testing instrument was used to measure the effect of

![Fig. 1 XRD results for the shale used in this study: a total mineral contents; b clay mineral contents](image1)

![Fig. 2 Preparation of rock samples with different bedding inclinations](image2)

![Fig. 3 Shear wave variation with bedding inclinations](image3)
bedding planes on P-waves. The results are shown in Fig. 3. When the rock bedding inclination ranged from 15° to 45°, the shear wave velocity of the rock tended to increase. When the rock bedding inclination ranged from 45° to 75°, the shear wave velocity of the rock tended to decrease. The influence of bedding planes on acoustic waves was in good agreement with research on the anisotropy characteristics of shale (Tutuncu 2010; Tutuncu and AI Mese 2012). Therefore, the samples were well suited for studying the effect of bedding inclination on borehole inclination.

**Experimental method**

**Uniaxial compression test**

Uniaxial compression experiments were performed in a servo-hydraulic apparatus (GCTS RTR-2000, GCTS Company, Phoenix, AZ, USA). The specimens were processed into standard specimens with dimensions 25 mm × 50 mm. To limit the friction effect, the slenderness ratio of a compressive sample should be large enough. This can be manifested from a recommended slenderness ratio of 2 or larger for static compressive tests of rocks by the ISRM (Bieniawski and Bernede 1979). During the tests, the axial loading was carried out under the displacement control mode. The applied force and loading displacement were recorded simultaneously at the same sampling frequency during the entire deformation process. The maximum force applied along the axial direction of the sample was 600 kN. The displacement control at a strain rate of 0.2 mm/min was used to obtain the stress–strain relationship of the rock samples.

**Drillability test**

The tests were carried out on an independently developed rock drillability apparatus (Mao et al. 2018). The detailed experimental apparatus, shown in Fig. 4, could simulate the bottom-hole conditions including confining pressure, wellbore pressure, pore pressure, bit weight, and rotational speed. The maximum value of the confining pressure, wellbore pressure, and pore pressure was 100 MPa. The rotation speed could be set freely between 0 and 200 rpm. The bit weight could be set freely between 0 and 3000 N. The test samples were cylindrical specimens of 50 mm diameter and 80 mm height. Both the cone microdrill bit and PDC microdrill bit were used to test the rock drillability. The cone microdrill bit was assembled with eight blades and nine spacers and had a diameter of 31.75 mm. The diameter of the PDC microdrill bit was 32 mm with two cutters. The two PDC cutters were installed at a back dip angle and roll angle of 20° and 5°, respectively (see Fig. 5). In this study, the PDC rock drillability of shale for the PDC microdrill bit was tested, and the drilling parameters and evaluation methods were mainly based on the petroleum and natural gas industry standards of China (Standards 2016). The weight of the bit (500 N) and rotational speed (55 rpm) for the PDC microdrill bit were set. When the confining pressure, wellbore pressure, and pore pressure reached the set values, the drilling began. The timer started when the drilling depth reached 0.2 mm, the drill penetrated 3 mm, the drilling time was recorded, and the drilling was stopped. The relationship (Standards 2016) between the rock drillability index \( K_d \) and drilling time \( T \) is defined in Eq. (1):

![Fig. 4 Rock drillability test apparatus](image-url)
Results and discussion

Shale mechanical characteristics

The stress–strain curves of shale from the uniaxial compression experiment are shown in Fig. 6a. The peak strength of the tested specimens was evaluated as shown in Fig. 6b. The peak strength displays “U”-type variation trends with respect to the bedding inclination. The minimum value of 66.91 MPa was obtained when the bedding inclinations were 45°. The maximum value was observed at \( \beta = 75° \). The tested rock samples are shown in Fig. 7. Tensile splitting along the bedding plane occurred when the bedding inclination angle was 0° and 15°. The bedding plane was nearly parallel to the loading direction, and tensile fractures were easily caused along the bedding planes. Shear along the bedding plane occurred when the rock bedding inclinations were 30°. However, when the rock bedding inclinations were 45° and 60°, the shear along the bedding plane did not occur, and shear fractures through the bedding plane were extended. Shear through the bedding plane occurred on shale samples with bedding inclinations of 75° and 90°. According to the experimental results, bedding inclinations have a significant impact on the failure behavior of shale. The experimental results of this paper are basically consistent with those of Yang et al.’s study (Yang et al. 2020).

Influence of wellbore pressure on shale drillability with bedding inclinations

Figure 8 depicts the ultimate shale sample after the test. Each sample was drilled into a pit, and no specific difference was observed. However, the time required to drill 3 mm was accurately recorded. According to Eq. (1), the drillability index could be obtained. The experimental results of

\[
K_d = \log_2 T
\]
the drillability index of the shale samples under different bedding inclinations and wellbore pressures are shown in Table 1.

To understand the influence of wellbore pressures on the drillability of each bedding inclination sample, the relationship between wellbore pressure and drillability is plotted in Fig. 9. Figure 9 illustrates the impact of the bedding inclination on the drillability index under various wellbore pressures. It can be seen that the wellbore pressure has a significant effect on the drillability of shale with any bedding inclination and the drillability index increases with increasing wellbore pressure. The effect of wellbore pressure on the rate of penetration (ROP) is very significant in drilling engineering (Eckel 1958). As early as 1965, Maurer (Maurer 1965) experimentally demonstrated the effect of wellbore pressure on ROP. Maurer called this effect the holding down effect. According to his study, there are two reasons for the slow rate of mechanical drilling under wellbore pressure. First, the wellbore pressure significantly influenced the rock mechanics; second, drill cuttings cannot be removed from a borehole and brought to the surface, which can lead to repeated breakage of rock. To ensure the rapid removal of the drill cuttings, we used an inverted drill bit to break the rock in this study. According to Mao et al., the drillability index increases exponentially with increasing wellbore pressure for basalt, clay shale, and sandstone (Mao et al. 2018).

We found that the drillability index increases exponentially with increasing wellbore pressure for shales without different bedding surfaces. When the wellbore pressure is < 15 MPa, the drillability index increases almost linearly with increasing wellbore pressure. When the wellbore pressure is ≥ 15 MPa, the drillability index increases gently. This

Table 1  Drillability index of shale with different bedding inclinations

| Bedding inclinations (°) | Wellbore pressure (MPa) |
|-------------------------|-------------------------|
|                         | 0  | 5  | 10 | 15 | 20 | 25 |
| 0                       | 6.97 | 7.29 | 8.55 | 8.24 | 8.04 | 8.05 |
| 15                      | 6.17 | 6.6 | 6.88 | 8.22 | 8.65 | 8.09 |
| 30                      | 5.81 | 6.68 | 7.33 | 8.5 | 8.55 | 8.19 |
| 45                      | 7.17 | 7.88 | 8.71 | 8.04 | 8.68 | 8.1 |
| 60                      | 5.97 | 6.93 | 7.24 | 7.88 | 8.39 | 8.16 |
| 75                      | 5.87 | 7.05 | 7.97 | 7.68 | 8.04 | 8.11 |
| 90                      | 5.58 | 7.53 | 7.62 | 7.78 | 8.00 | 8.07 |
Fig. 9 Drillability index of shale under varying wellbore pressure.
indicates that the exponential increase in the drillability index with increasing wellbore pressure is consistent with published studies; however, more experimental results are needed to confirm this finding. In this paper, the empirical equation for calculating the drillability index under different wellbore pressures is proposed as follows:

$$K_{cd} = K_d + b \times P_d \times e^{-a\times P_d}$$  \hspace{3cm} (2)

where $K_{cd}$ is drillability index related to wellbore pressure, $K_d$ is drillability index at 0 wellbore pressure, $P_d$ is wellbore pressures, and $a, b$: Fitting coefficient.

Because the shale was very tight, pore pressure could not be applied, and the influence of pore pressure on shale could not be obtained. The effect of pore pressure on the drillability index was ignored in this study. Table 2 shows the fitting results of the experimental data using Eq. (2). It can be seen that the fitting effect was relatively good. The correlation coefficients were above 0.6, most of which exceeded 0.9. Therefore, the wellbore pressure influenced the drillability indexes with an exponential relation.

To further analyze the influence of wellbore pressure and bedding inclination on the drillability index, the relationship between wellbore pressure and drillability was plotted again, as shown in Fig. 10. Figure 10a shows the relationship between the drillability index and wellbore pressure when the wellbore pressure is $< 15 \text{ MPa}$ and $\geq 15 \text{ MPa}$, respectively. It can be clearly observed in Fig. 10a that when the wellbore pressure is $< 15 \text{ MPa}$, the drillability index shows a “W” shape with a change in bedding inclinations. With increasing wellbore pressure, the influence of wellbore pressure on shale drillability decreases significantly. When the wellbore pressure is 25 MPa, there is a little difference in the drillability index for shales with different bedding inclinations.

The experimental results show that the bedding inclinations significantly influence drillability under low wellbore pressures ($< 15 \text{ MPa}$), and high wellbore pressure reduces variability in drillability. The results of the cutting experiments by Wang et al. indicate that the torques during rock breakage show the same trend without considering the borehole conditions (Teng et al. 2017); however, the reasons for this are well worth investigating. It is well known that fractures tend to expand along weak planes, which may be an important reason for this phenomenon (Jiang et al. 2020; Song et al. 2020). Schormair and Thuro further proved by numerical simulation that this is still the case in the process of tool rock breakage (Schormair and Thuro 2007). The stress generated during the cutting tooth invasion must overcome the tensile or shear strength of the weak planes before the crack can be generated. The effects of the confining pressure and wellbore pressure are mainly reflected in the inhibition of crack propagation along the weak planes. With increasing confining pressure and wellbore pressure, the stress acting on the weak planes was sufficiently high to make the rock stiffer by increasing the difficulty for the induced crack to propagate along the weakest plane of the rock. As the wellbore pressure increases, the difference in the drillability index decreases. When the wellbore pressure is 25 MPa, the drillability of shale with different bedding inclinations is almost the same, as shown in Fig. 10. The

Table 2  Fitting results of experimental data using Eq. (2)

| Bedding inclination (°) | $a$     | $b$     | $R^2$     |
|------------------------|---------|---------|-----------|
| 0                      | 0.04376 | 0.12000 | 0.67409   |
| 15                     | 0.01694 | 0.14108 | 0.84065   |
| 30                     | 0.03527 | 0.25674 | 0.93166   |
| 45                     | 0.04190 | 0.14000 | 0.60363   |
| 60                     | 0.03058 | 0.20044 | 0.96730   |
| 75                     | 0.04100 | 0.25000 | 0.92857   |
| 90                     | 0.04076 | 0.28000 | 0.83922   |

Fig. 10  Relations between drillability indexes and bedding inclinations under different wellbore pressures
mechanism of the influence of bedding inclinations on the invasion of bit teeth requires further research.

**Conclusion**

Drillability experiments were carried out for shale with different bedding inclinations under different wellbore pressures. The effect of borehole pressure and bedding inclinations on drillability was studied. Borehole pressure has a significant impact on the drillability index of shale. The drillability indexes of shale with different bedding inclinations increase exponentially with increasing borehole pressure. An empirical exponential model is proposed to describe the relationship between the borehole pressure and drillability index. This model can describe the effect of wellbore pressure on drillability. The bedding inclinations significantly influence the drillability index of shale, but the effect varies significantly under different borehole pressures. Under the condition of borehole pressure less than 15 MPa, the drillability indexes of shale show a “W” shape with increasing bedding inclinations. With increasing borehole pressure, the influence of bedding inclinations on drillability gradually decreases. When the wellbore pressure reaches 25 MPa, the bedding inclinations have little effect on the drillability indexes. In this study, the influence of temperature on the test results is not considered when the bit is simulated in the real rock-breaking environment of formation. The following research can consider the combined effect of temperature and wellbore pressure on rock drillability.

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**Declarations**

**Conflict of interest** The authors declare no conflict of interest.

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