Superimposed Coding Based CSI Feedback Using 1-Bit Compressed Sensing
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Abstract—In a frequency division duplex (FDD) massive multiple-input multiple-output (MIMO) system, the channel state information (CSI) feedback causes a significant bandwidth resource occupation. In order to save the uplink bandwidth resources, a 1-bit compressed sensing (CS)-based CSI feedback method assisted by superimposed coding (SC) is proposed. Using 1-bit CS and SC techniques, the compressed support-set information and downlink CSI (DL-CSI) are superimposed on the uplink user data sequence (UL-US) and fed back to base station (BS). Compared with the SC-based feedback, the analysis and simulation results show that the UL-US’s bit error ratio (BER) and the DL-CSI’s accuracy can be improved in the proposed method, without using the exclusive uplink bandwidth resources to feed DL-CSI back to BS.

Index Terms—Channel state information (CSI), compressed sensing (CS), feedback, superimposed coding (SC).

I. INTRODUCTION

As one of the key technologies for fifth-generation (5G) wireless networks, frequency division duplex (FDD) massive multiple-input multiple-output (MIMO) has drawn increased attention due to the improvement in spectral and energy efficiencies

With a large number of antennas deployed at base station (BS), the performance improvement of massive MIMO system significantly relies on accurate channel state information (CSI). In time-division duplexing (TDD) system, the downlink CSI (DL-CSI) can be obtained at BS via the channel reciprocity

However, the channel reciprocity is not available in FDD massive MIMO system due to the different uplink and downlink spectral bands. Therefore, the DL-CSI should be fed back to base station (BS) through the uplink channel

The codebook-based approaches are usually adopted to reduce feedback overhead. Nevertheless, due to the exponential measurement complexity caused by large number of antennas at BS, this approach is not practical in FDD massive MIMO system

In practice, 1-bit quantization is particularly attractive because the construction of the quantizer is simple and cost-effective

To the best of our knowledge, the SC-based CSI feedback using 1-bit CS method for FDD massive MIMO systems has not been studied in existing literatures. The main contributions of this paper are summarized as follows:

1) Introducing “1-bit CS” technique into the SC-based CSI feedback scheme improves DL-CSI’s NMSE and UL-US’s BER. In [12], an unquantized and uncoded DL-CSI is estimated, and then the estimated DL-CSI is used to reduce superimposed interference. Unlike the case in [12], 1-bit CS transforms a CSI estimation problem into the problem of bit (or sign) information detection

2) The support-set of CSI is superimposed on UL-US and fed back to BS to further improve the NMSE of DL-CSI. In CS-based CSI feedback schemes, the support-set of CSI is required to be recovered at BS

3) From [13], the accuracy of reconstruction algorithm can be effectively improved with the priori information of support-set. Based on the de-spread support-set and binary iterative hard thresholding (BIHT) algorithm (other similar reconstruction algorithms can be applied as well), a SC-aided BIHT (SCA-BIHT) algorithm is proposed to improve the recovery of the compressed DL-
CSI at BS.

Notation: Boldface letters are used to denote matrices and column vectors; $(\cdot)^T$, $(\cdot)^H$ and $(\cdot)^{-1}$ denote the transpose, conjugate transpose, matrix inversion. $I_p$ is the identity matrix of size $P \times P$. 0 is the matrix or vector with all zero elements, the $l_2$ norm of a vector $x$ is written as $\|x\|_2$. $\odot$ denotes the operation of Hadamard product for two vectors or matrices. $\eta_k(x)$ represents computing the best $k$-term approximation of $x$ by thresholding. $\text{dec}(\cdot)$ is the hard decision operation, in which the current data is determined as the modulated data with the smallest Euclidean distance from current data. $\text{sgn}(\cdot)$ denotes an operator that performs the sign function element-wise on the vector, e.g., the sign function returns +1 for positive numbers and (0) otherwise.

II. SYSTEM MODEL

We consider a massive MIMO system consists of a BS with $N$ antennas and $K$ single-antenna users. The DL-CSI is superimposed on UL-US and then fed back to BS. In this way, the overhead of uplink bandwidth resources, particularly used to feed back DL-CSI, is avoided. Similar to [8–11], we assume the DL-CSI has been estimated at users and mainly focus on CSI feedback[9]. After the processing of matched-filter (MF) (i.e., the conventional multiuser detector structure consists of a MF bank front [20]), the received signal $\tilde{Y}_k$ sent by the $k$-th user, $k = 1, 2, \ldots, K$ can be given by

$$\tilde{Y}_k = G X + \tilde{n}_k$$

where $G$ is a $N \times 1$ uplink channel matrix, $\rho \in [0, 1]$ stands for the power proportional coefficient of DL-CSI, $E_k$ represents the total transmitting power, $d_k \in C^{1 \times P}$ denotes the UL-US signal; $\tilde{n}_k \in C^{N \times P}$ represents the feedback link noise whose elements are with zero-mean and variance $\sigma_n^2$ [6]; In particular, the $s_k \in C^{1 \times P}$ in (1) is the superposition signal that consists of compressive DL-CSI, sparsity and support-set. III-A would explicate the $s_k$ to this paper.

III. THE PROPOSED FEEDBACK METHOD USING 1-BIT CS

In this section, we first present how to introduce 1-bit CS technique into the SC-based CSI feedback scheme (see III-A). Then, in III-B, the DL-CSI reconstruction and UL-US detection are described, where we especially explain the details of proposed SCA-BIHT. Finally, the analysis of computational complexity for SCA-BIHT is given.

A. SC based DL-CSI Feedback

After exploiting the sparsity structure (by using methods mentioned in [7–11]), the sparse DL-CSI $h_k$ can be compressed according to 1-bit CS technique, i.e.,

$$\begin{cases} y_{\text{real}} = \text{sgn}(\text{Re}(h_k \Phi_k)) \vspace{1mm} \\ y_{\text{imag}} = \text{sgn}(\text{Im}(h_k \Phi_k)) \end{cases}$$

1Note that, due to limited computational power, the users should employ some low-complexity channel estimation methods, which require simplicity but go beyond the scope of this letter. Since we mainly focus on CSI feedback, we assume that the DL-CSI has been estimated perfectly at user.

where $\Phi_k$ is a $N \times M$ measurement matrix and the DL-CSI $h_k$ is a $1 \times N$ vector. In [2], $y_{\text{real}}$ and $y_{\text{imag}}$ are used to represent the DL-CSI compression’s real and imaginary parts, respectively.

We assume the DL-CSI $h_k$ features $\xi_k$-sparsity, i.e., only $\xi_k$ non-zero elements in $h_k$ [7]. For convenience, a set $z_k \in \{0, 1\}^{1 \times N}$ is employed to label the set of indices of DL-CSI’s non-zero elements (i.e., the support-set). That is, the index of DL-CSI’s zero elements is labeled by 0 and the index of DL-CSI’s non-zero elements is labeled by 1. For example, $h_k = (h_1, h_2, \ldots, h_5)$ and $z_k = [1, 1, 0, 0, 1]$ mean the value of $h_1, h_2$ and $h_5$ are non-zero elements, $h_3 = h_4 = 0$.

With the bit-form of $\xi_k$ as $k_{bin} \in \{0, 1\}^2$, the feedback vector $w_k$, which merges $y_{\text{real}}, y_{\text{imag}}, z_k$ and $k_{bin}$, can be expressed as

$$w_k = [y_{\text{real}}, y_{\text{imag}}, z_k, k_{bin}]. \quad (3)$$

It is worth noting that the elements of $w_k$ only contain 0 and 1, which can be viewed as a bit stream. With digital modulation, such as the quadrature phase shift keying (QPSK), $w_k$ is mapped to a $1 \times L$ modulated vector $x_k$. Without loss of generality, the UL-US’s length $P$ is larger than $L$ due to main task of the user services. Thus, a spreading method can be utilized to capture a spread spectrum gain. The superposition signal $s_k$ can be obtained via the using of pseudo-random codes (e.g., the Walsh codes) to spread $x_k$, i.e.,

$$s_k = x_k q^T, \quad (4)$$

where $q \in \mathbb{R}^P \times L$ consists of $L$ codes of length $P$ satisfying $q^T q = P \cdot I_L$. Then the superposition signal $s_k$ and UL-US $d_k$ are weighted and superimposed, i.e., $\sqrt{\rho E_k} s_k + \sqrt{(1-\rho) E_k} d_k$,

and fed back to BS, which is described in (1) as well.

B. UL-US Detection and DL-CSI Reconstruction

1) UL-US Detection: With the received signal $\tilde{Y}_k$ in equation (1), the de-spreading signal can be obtained by

$$\hat{x} = \frac{1}{P} \tilde{Y}_k q$$

$$= \sqrt{\rho E_k} G x_k + \sqrt{(1-\rho) E_k} G d_k q + \frac{1}{P} \tilde{n}_k q. \quad (5)$$

Subsequently, the estimation that contains DL-CSI and support-set can be acquired via minimum mean square error (MMSE) detection, i.e.,

$$\hat{x}_{\text{MMSE}} = \text{dec} \left( P \sqrt{\rho E_k} \left[ (1 + (P - 1) \rho) E_k G^H G + \sigma_n^2 \right]^{-1} G^H \tilde{x} \right). \quad (6)$$

Then, taking advantage of interference cancellation described in [12], the interference caused by DL-CSI can be eliminated in such a way:

$$\hat{d}_k = \hat{y}_k - \sqrt{\rho E_k} G \hat{x}_{\text{MMSE}} q^T$$

$$= \sqrt{(1-\rho) E_k} G d_k + \sqrt{\rho E_k} G (x_k - \hat{x}_{\text{MMSE}}) q^T + \tilde{n}_k. \quad (7)$$

With the application of MMSE detection in (6), the estimated UL-US $d_k$ is obtained, then $w_k$ can be recovered from
TABLE I
SCA-BIHT ALGORITHM

Input: measurement matrix \(\Phi_k\), real part and imaginary part of 1-bit noise measurement \((\tilde{y}_{\text{real}}\) and \(\tilde{y}_{\text{imag}}\)), sparsity \(\xi_k\), and received support-set \(\tilde{z}_k\).

Initialize: maximum number of iterations \(\text{Iter}_{\text{max}}\), iteration count \(t = 0\), the real part and imaginary part of reconstructed data are set to zero, i.e., \(r_{\text{real}}^0 = 0\) and \(r_{\text{imag}}^0 = 0\).

Begin:
1) Increment: \(t = t + 1\);
2) Gradient update:
   \[
   r_{\text{real}}^t = \eta_k (r_{\text{real}}^{t-1} + (\tilde{y}_{\text{real}} - \text{sgn}(r_{\text{real}}^{t-1} \Phi_k))\Phi_k^T),
   \]
   \[
   r_{\text{imag}}^t = \eta_k (r_{\text{imag}}^{t-1} + (\tilde{y}_{\text{imag}} - \text{sgn}(r_{\text{imag}}^{t-1} \Phi_k))\Phi_k^T),
   \]
   \[
   \text{supp}(r^t) = \text{supp}(r_{\text{real}}^t) \cup \text{supp}(r_{\text{imag}}^t);
   \]
3) Go to step 5) if \(\text{supp}(r^t) \cap \tilde{z}_k = \emptyset\), else go to the next step;
4) Auxiliary correction:
   \[
   r_{\text{real}}^t = r_{\text{real}}^t \odot \tilde{z}_k;
   \]
   \[
   r_{\text{imag}}^t = r_{\text{imag}}^t \odot \tilde{z}_k;
   \]
5) Go to step 1) if \(t < \text{Iter}_{\text{max}}\), else go to next step;
6) Combination:
   \[
   \tilde{h} = r_{\text{real}}^t + i \times r_{\text{imag}}^t;
   \]
7) Normalization:
   \[
   \tilde{h}_k = \tilde{h} / \|\tilde{h}\|_2;
   \]

End

Output: Reconstructed DL-CSI \(\tilde{h}_k\).

TABLE II
COMPUTATIONAL COMPLEXITY

| Algorithm | Complexity |
|-----------|------------|
| BIHT      | \(O((MN) \times \text{Iter}_1)\) |
| SCA-BIHT  | \(O((MN) \times \text{Iter}_2)\) |

\(\tilde{r}_{\text{MMSE}}\): The sign information \(\tilde{y}_{\text{real}}, \tilde{y}_{\text{imag}}, \text{sparsity } \tilde{\xi}_k\), and support-set \(\tilde{z}_k\) can be restored via the position relation in equation [3].

2) DL-CSI Reconstruction: BS can recover the DL-CSI via the SCA-BIHT algorithm, with the recovered sign information \(\tilde{y}_{\text{real}}, \tilde{y}_{\text{imag}}, \text{sparsity } \tilde{\xi}_k\), and support-set \(\tilde{z}_k\). The details of SCA-BIHT are shown in TABLE I. Similar to [14] [21], the direction of the reconstructed signal is obtained via the normalization step, i.e., step 7) in SCA-BIHT. Need to mention that, we propose SCA-BIHT to improve BIHT, and other similar reconstruction algorithms can naturally be improved according to the same approach. In SCA-BIHT, the input and auxiliary correction are different from BIHT, which are described as follows:

- **Input and Initialization of SCA-BIHT**: The input includes the received support-set \(\tilde{z}_k\), which is not contained in BIHT [19]. Since BS does not need to reconstruct support-set, the proposed method has fewer iterations and lower computational complexity (see III-C for details).
- **Auxiliary Correction**: As shown in step 4), the reconstructed values are corrected by using the received support-set \(\tilde{z}_k\). That is, according to the position of 0 elements in \(\tilde{z}_k\), the elements at the corresponding position in the reconstructed value are set to 0, and the remaining elements are unchanged. But the BIHT doesn’t contain support-set correction.

Compared with the BIHT, the proposed SCA-BIHT is more concise, due to the auxiliary of support-set.

C. Computational Complexity

The comparison of computational complexity between BIHT and SCA-BIHT is given in TABLE III where Iter1 and Iter2 denote the iteration number of BIHT and SCA-BIHT, respectively. For each iteration, SCA-BIHT and BIHT have the computational complexity \(O(MN)\). Despite all this, SCA-BIHT has fewer iterations than BIHT, i.e., Iter2 < Iter1, due to no requirement of support-set reconstruction. Thus, SCA-BIHT has lower computational complexity than that of BIHT.
IV. EXPERIMENT RESULTS

In this section, we give some numerical results of the SC based CSI feedback with 1-bit CS under different conditions. The basic parameters involved are listed below. $h_k$ features $\xi_k$-sparsity, whose elements obey $\mathcal{CN}(0, 1)$. The $N \times M$ measurement matrix $\mathbf{\Phi}_k$ is set as a Gaussian random matrix, whose elements obey $\mathcal{N}(0, 1)$ \cite{19} \cite{21}. UL-US is a $1 \times P$ complex sequence modulated by quadrature phase shift keying (QPSK). We set $P = 1024$, $N = 64$, $\xi_k = 8$, and $T_{\text{max}} = 100$. The sampling rate $c$, signal-to-noise ratio (SNR) in decibel (dB), and NMSE are defined as $c = M/N$, $\text{SNR} = 10\log_{10}(E_k/\sigma_n^2)$ and $\text{NMSE} = \|\mathbf{h}_k - \hat{\mathbf{h}}_k\|^2_2/\|\mathbf{h}_k\|^2_2$, respectively. Three iterations of interference cancellation are employed for \cite{12}, while only one iteration for the proposed scheme. In \cite{12}, simulations show that with three iterations, the SC-based feedback algorithm nearly converges. According to \cite{5}–\cite{7} and DL-CSI reconstruct algorithm in TABLE I, the interference cancellation in proposed scheme is performed only one time. More iterations could not obtain significant improvement but merely increase the complexity. According to \cite{22}, a feedback method based on 1-bit CS is also employed for time division multiplexing (TDM) mode in our experiments, where $P$ modulated UL-US and $cN$ modulated DL-CSI are up-transmitted with an additional 12.5% of uplinking bandwidth are occupied, i.e., $cN/P = 12.5\%$ with $c = 2$.

For simplicity, “Prop-SCA” is used to denote the proposed SC-based CSI feedback; “Prop-BIHT” represents the SC-based CSI feedback without support-set $z_k$, and BS adopts BIHT for DL-CSI reconstruction; “Ref\cite{12}” denotes the SC method in \cite{12}: “Ref\cite{22}” denotes the feedback method in \cite{22} with TDM mode, i.e., the TMD-based feedback.

To verify the effectiveness of proposed scheme. We first make the performance comparison between Ref\cite{12}, Ref\cite{22}, Prop-BIHT and Prop-SCA in Fig. 1. Where $\rho = 0.2$, the sampling rates of scheme Ref\cite{22}, Prop-BIHT and Prop-SCA are respectively set as $c = 2$, $c = 2$ and $c = 1.5$. It is worth noting that this parameter setting of sampling rate is employed to promote Ref\cite{22}, Prop-BIHT and Prop-SCA have the same bit-overhead to bear CSI feedback. For Prop-BIHT and Ref\cite{22}, the bit-overhead is 256 bits according to $c \times N \times 2 = 2 \times 64 \times 2 = 256$, where we produce 2 is due to the consideration of real and imaginary parts. The same bit-overhead can be obtained in Prop-SCA by computing $c \times N \times 2 + N = 1.5 \times 64 \times 2 + 64 = 256$ bits, where we add $N$ is due to the bit-overhead of support-set feedback.

From Fig. 1(a) and Fig. 1(b), introducing 1-bit CS technology into SC-based CSI feedback can improve the DL-CSI’s NMSE and UL-US’s BER. Furthermore, due to the increase of spread spectrum gain, the support-set feedback promotes the proposed Prop-SCA further improve the NMSE of Prop-BIHT. Compared to Ref\cite{22} (i.e., TMD-based feedback), although
the BERs are sacrificed due to the superimposed interference, the 12.5% uplink bandwidth savings and much lower NMSE are captured by of Prop-BIHT and Prop-SCA.

To demonstrate the impacts of different \( \rho \) and \( c \) on Prop-SCA, the BER and NMSE performances are respectively given in Fig. 2(a) and Fig. 2(b) where different \( \rho \) (i.e., \( \rho = 0.1 \) and \( \rho = 0.2 \)) and different \( c \) (i.e., \( c = 2.0 \), \( c = 2.5 \), and \( c = 3.0 \)) are considered.

Fig. 2(c) illustrates the BER performance of Prop-SCA with SNR varying from 0dB to 10dB. It is obvious that the Prop-SCA evidently improves the BER when compared to Ref [12] with the equal \( \rho \), especially for a relatively high SNR, e.g., SNR > 2dB. For each \( \rho \), the impact of \( c \) on BERs of Prop-SCA and Ref [12] is not clear, that is because the identical reconstruction differences of DL-CSI with the various \( \rho \) are considered. A small reconstruction differences of DL-CSI with the various \( \rho \) are considered.

The reason is that the Prop-SCA transforms a CSI estimation problem into the sign detection problem. With the using of SCA-BIHT in TABLE I, the detected noise measurements (i.e., \( \tilde{y}_{\text{real}} \) and \( \tilde{y}_{\text{imag}} \)) leads to less obvious reconstruction differences of DL-CSI with the various \( \rho \).

To validate the robustness of NMSE against the impact of \( \rho \) and \( c \) on Prop-SCA, the NMSE performance is given in Fig. 2(b). This figure reflects that, compared with Ref [12] and Ref [22], Prop-SCA obtains smaller NMSEs. As \( c \) increases, the NMSE of Prop-SCA can be improved due to the increase of measurements, and not significantly affected by the change of \( \rho \). The reason is that the Prop-SCA transforms a CSI estimation problem into the sign detection problem. With the using of SCA-BIHT in TABLE I, the detected noise measurements (i.e., \( \tilde{y}_{\text{real}} \) and \( \tilde{y}_{\text{imag}} \)) leads to less obvious reconstruction differences of DL-CSI with the various \( \rho \).

To sum up, compared to SC-based feedback, the proposed Prop-BIHT and Prop-SCA can improve the UL-US’s BER and the DL-CSI’s NMSE. Compared to Prop-BIHT, the Prop-SCA can further improve the DL-CSI’s NMSE performance. Without using the exclusive uplink bandwidth resources, the Prop-SCA can improve the DL-CSI’s NMSE performance of TMD-based feedback (i.e., Ref [22]). A small \( \rho \) (e.g., \( \rho = 0.1 \)) guarantees the UL-US’s BER of Prop-SCA is only slightly degraded relative to Ref [22], while saving 12.5% uplink bandwidth resources and keeping improvement of DL-CSI’s NMSE. In addition, the Prop-SCA possesses a good robustness against the impact of \( \rho \) and \( c \). Thus, introducing “1-bit CS” technique into SC-based CSI feedback brings us great benefits, and the support-set feedback is attractive.

V. CONCLUSION

In the proposed method, SC technique avoids the occupation of uplink bandwidth resources, 1-bit CS method transforms the DL-CSI estimation problem into a bit (or sign) information detection problem, feeding support-set back to BS significantly reduces the superimposed data, and then the interference cancellation and spread spectrum gain can be effectively improved. Meanwhile, proposed method also adopts SCA-BIHT algorithm to reconstruct DL-CSI at BS as well. The analysis and simulation results show that the proposed method can improve the UL-US’s BER and the DL-CSI’s NMSE, compared with traditional SC-based DL-CSI feedback method. Although the UL-US’s BER is affected by the application of SC, a relatively small power proportional coefficient can still guarantee the BER performance of the proposed method is only slightly degraded relative to TMD-based feedback, while significantly saving uplink bandwidth resources and improving DL-CSI’s NMSE.

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