Tunneling conduction in graphene/(poly)vinyl alcohol composites

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Graphene/(Poly)vinyl alcohol (PVA) composite film with thickness $60\mu m$ were synthesized by solidification of a PVA solution comprising of dispersed graphene nanosheets. The close proximity of the graphene sheets enables the fluctuation induced tunneling of electrons to occur from one sheet to another. The dielectric data show that the present system can be simulated to a parallel resistance-capacitor network. The high frequency exponent of the frequency variation of the ac conductivity indicates that the charge carriers move in a two-dimensional space. The sample preparation technique will be helpful for synthesizing flexible conductors.
INTRODUCTION

Recently, graphene and graphene-based materials have attracted considerable attention not only because of deriving rich physics from it, but also to exploit these for fabricating simpler and more efficient devices [1–9]. To design graphene-based nanoscale devices, quantum transport mechanism has to be kept in view. Synthesis of composites with single or few layer graphene sheets has been reported recently. This requires large scale production of graphene, and their homogeneous distribution in various matrices [10]. Several systems have been studied of which transparent and electrically conducting graphene/silica [11] and graphene/polystyrene composites made by complete exfoliation of graphite [10] may be mentioned. Graphene/(poly)aniline composites [12] have been used for hydrogen gas sensing. Theoretically it had been shown that graphene’s volume fraction, or the aspect ratio of the graphene sheet had a profound effect on the resistance of the graphene-based polymer composites [13]. We had previously synthesized graphene/PVA composite, with a particular concentration of graphene sheets in the polymer matrix to study the magnetodielectric effect [14]. From the above, it can be seen that so far electrical conductivity involving graphene has been investigated either in its percolative configuration [15] or in a composite structure [10, 11]. In the present work, our objective is to study the conduction mechanism in a graphene based polymer composite, where the graphenes will be at close proximity to each other but not in percolative configuration. The details of our findings are reported in this letter.

EXPERIMENTAL

A simple chemical method was employed to synthesize the graphene/(poly)-vinyl alcohol(PVA) composite. The synthesis of graphene from the chemical exfoliation of graphite oxide (GO) has been described elsewhere [3, 14]. Firstly, a modified Hummers method was employed to synthesize graphene oxide from high purity graphite flakes (LOBACHEMIE). 0.01 g of GO was dispersed in 10 mL water, and then 6 mL of hydrazine hydrate was mixed with it. Ammonia solution was added to keep the pH of the mixture at 10. After 3h of stirring graphene dispersion was achieved.

(Poly)vinyl alcohol (PVA 0.505 g) powder (as obtained from S-d fine-Chem,India, $M_w \approx 14000$) was dissolved in 20 mL of water and stirred at 333 K for 3 h. to form a homogeneous polymer solution. 6 mL of dispersed graphene was mixed with PVA (12 mL)solution and stirred for 4 h. to form a homogeneous mixture. To obtain the film, the mixture was cast on a teflon coated petri-dish and solidified at room temperature. It is to be noted here that the preparation entailed 1.95% GO and 98.05% of PVA (by weight) as precursors. The graphene was characterized previously by Fourier Transform Infrared Spectroscopy (FTIR) and transmission electron microscopy [14]. Electrical measurements were carried out after applying silver electrodes (silver paint supplied by M/S Acheson Colloiden,The Netherland) on both sides of a piece of graphene-PVA composite film using a Keithley 617 electrometer. The current voltage characteristic was measured using a Kiethley 2400 source meter. For dielectric measurements an Agilent 4980 precision LCR meter was used.

RESULTS AND DISCUSSION

It was observed [14] from the FTIR spectra that, hydroxyl and epoxide functional groups present on the basal plane of GO, and carbonyl and carboxyl groups at the edges of GO were removed (absence of any C=O) due to the chemical reaction of GO with hydrazine hydrate.

A typical voltage current characteristic for the composite, obtained at room temperature is shown in figure 1. The linear behaviour indicates a non-blocking nature of the electrodes used.

The variation of logarithm of dc resistivity as a function of $T^{-1}$ for the composite film of thickness 0.006 cm is shown in figure 2. This semiconductor like behaviour in the temperature dependence of the resistivity can be due to the existence of potential barriers between highly conducting regions. In this kind of situation the conduction arises due to hopping or tunneling of the charge carriers from one conducting island to another. We have fitted the experimental data with the fundamental equation of the activated process,

$$\rho = \rho_0 \exp \left(\frac{\phi}{k_B T}\right)$$

where, $\rho$ is the resistivity, $k_B$ is Boltzmann constant, $\phi$ is the activation energy and $T$ is the absolute temperature.
FIG. 1. Variation of current with voltage measured at room temperature (306 K).

FIG. 2. Variation of logarithm of resistivity with $T^{-1}$ for the composite. The solid line represents the least squared fitted curve, with equation 1. The points indicate the experimental data. The slope of the straight line was extracted as $0.0805 \pm 0.001$, from which we have calculated the activation energy $\phi$ as $0.016$ eV. The low value of activation energy suggests that the charges tunnel from one graphene sheet to another through the polymer. Given that each graphene is coated with the polymer, which acts as the potential barrier for the inter graphene hopping, it is likely that electrical conductivity in this system is governed by tunneling between conductive regions. In order to get more insight about the conduction mechanism, we invoked the model of fluctuation induced tunneling of charge carriers between highly conducting regions for inhomogeneous conductors [16]. This model for disordered material is mainly used for the conduction of charge carriers from large sized conductors, separated by small insulating regions. The concentration of the graphene sheets dispersed in PVA matrix, being much higher than that used earlier [14], the separation between graphene sheets is very small, hence this type of transport mechanism is to be expected. The temperature variation of the conductivity in this fluctuation induced tunneling model, is given by, [16],

$$\sigma_{dc} = \sigma_0 \exp \left( -\frac{T_1}{T + T_0} \right)$$
FIG. 3. Variation of logarithm of dc conductivity with temperature for the composite. The solid line represents the least squared fitted curve, with equation (2).

where, $T_1$ is the temperature required for an electron to cross the insulator gap between conductive regions, and $T_0$ is the temperature above which thermal activated conduction over potential barrier begins to occur. The experimental data and the least square fitted curve with equation (2) are shown in fig. 3. $T_1$ and $T_0$ are material constants and related to the energy barrier $U$ by,

$$T_1 = \frac{16AU^2}{8\pi k_Bwe^2} \quad (3)$$

and

$$T_0 = \frac{2hT_1}{\pi w(2mU)^{\frac{1}{2}}} \quad (4)$$

where, $e$ and $m$ are the electronic charge and mass respectively, $w$ the intergraphene gap width, and $A$ the area of capacitance formed at the junction, $k_B$ stands for the Boltzman Constant. Our fitting of the experimental data with eq. (2) yielded the values of $T_1$ and $T_0$, which were used as parameters, as 746.23 K (or 0.06eV) and 244.8 K (or 0.021eV) respectively. Since we do not have the data to observe the distribution of $T_1$ and $T_0$, these observed values, should be interpreted as indicative of the median values of these parameters. However, it is worth noting, that the activation energy is smaller than that obtained previously for granular metal films [17]. Previously, [14] we have reported that for lower concentration of the graphene sheets in the PVA matrix, the activation energy has a value of 0.38 eV. In this particular work we have stuck to fluctuation induced tunneling as the conduction mechanism, and ruled out the possibility of other activated processes, such as, Frenkel-Poole and Fowler-Nordheim tunneling or hopping mechanisms which are responsible for charge conduction in this type of disordered materials. The reasons for this are as follows. The experimental data are significantly different from the

$$\ln\rho \sim \left[\frac{E^\frac{\pm}{2}}{T}\right] \quad (5)$$

of Frenkel-Poole type or

$$\ln\left(\frac{j}{E^2}\right) \sim \left[\frac{1}{E}\right] \quad (6)$$

of Fowler-Nordheim type of tunneling. The hopping mechanism were excluded since the resistivity data doesnot follow the stretched exponential function of the type $\exp[a/T^\alpha]$ for a single value of $\alpha$ [13].

The dielectric permittivity of the composite film was measured and we have delineated the real and imaginary parts of the same. The variation of real ($\epsilon'$) and imaginary ($\epsilon''$) parts of the dielectric permittivity with frequency measured at room temperature (306 K) are shown in figures 4 and 5 respectively. It is seen that, real part of the dielectric permittivity ($\epsilon'$) decreases slowly as a function of frequency in the range studied, whereas the imaginary
FIG. 4. Variation of real part of the dielectric permittivity ($\epsilon'$) of the nanocomposite as a function of the frequency measured at 306 K.

FIG. 5. Variation of imaginary part of the dielectric permittivity ($\epsilon''$) of the composite with the frequency measured at 306 K.

part ($\epsilon''$) decreases drastically from a high value. This type of variation is expected in case of a circuit consisting of a parallel combination of resistance and capacitance. We believe that the graphene films form the resistive network whereas, the PVA film makes up the capacitive element in the network system. The high value of the imaginary part of dielectric permittivity also signifies that there has been a high loss factor associated with the sample for a resistive network. A Cole-Cole diagram of the composite has been shown in figure. A single semi-circle signifies that there is one conduction mechanism operative in the composite. From the Cole-Cole diagram, the dc resistance was extracted from $z_{im} \rightarrow 0$ and found to be around 13 kΩ. The linear fitting of the current voltage data shows the resistance of the composite to be 23.6 kΩ which is of the same order of magnitude as that obtained from the Cole Cole diagram. The frequency dependent dispersion of conductivity is one of the characteristic features of electronic conduction in the disordered material. The frequency independent part at low frequency is observed to show a frequency dependence after a particular characteristic frequency, $\omega_0$. After $\omega_0$ the conductivity increases in a power law manner,

$$\sigma = A\omega^\beta$$ (7)

The variation of logarithm of ac conductivity as a function of logarithm of angular frequency for the graphene/PVA composite measured at 306 K is shown in figure.
FIG. 6. Cole-Cole diagram of the composite measured at 306 K.

FIG. 7. Variation of logarithm of ac conductivity with logarithm of frequency measured at 306 K. The solid line represents the least squared fitted curve.

We have fitted the conductivity data in the high frequency range, with the above mentioned equation, where $\sigma$ is the ac conductivity 'A' is a constant, $\omega$ is the frequency of the applied electric field and $\beta$ is the exponent. From the fitting the value of the exponent ($\beta$) is determined. The value of $\beta$ determines the dimension in which the conduction is taking place [21–24]. For one dimensional conduction the value of $\beta$ lies around 0.3, whereas, for two and three dimensions its value is around 0.5 and 0.66 respectively [21–24]. The value of $\beta$ in this case is extracted as $0.51 \pm 0.01$, which confirms the electronic motion to be operative in two-dimensions. This is due to the fact that the conduction is governed by the charge carriers of a two dimensional path formed by graphene sheets in close proximity to each other.

Figure 8(a) shows the variation of the imaginary part of dielectric modulus with angular frequency at different temperatures.

Dielectric modulus ($M^*$) is defined as [25]

$$M^* = \frac{1}{\epsilon^*}$$  \hspace{1cm} (8)

where, $\epsilon^*$ is the dielectric permittivity. The curves show prominent peaks, whose position is seen to shift towards the higher frequency side, when the temperature is increased. From the peak positions we have delineated the values of
FIG. 8. (a) Variation of dielectric modulus with logarithm of frequency measured at different temperatures. (b) The variation of logarithm of relaxation time with inverse of temperature. The straight line fitting gives the value of the activation energy for the relaxation process.

the relaxation time ($\tau$) for the composite using the relation:

$$\omega \tau = 1$$  \hspace{1cm} (9)

In figure 8(b), the variation of $ln\tau$ with $T^{-1}$ has been shown. From the slope of this Arrhenius plot the value of the activation energy for the relaxation process was calculated by employing,

$$\tau = \tau_0 \exp\left(\frac{E_a}{k_B T}\right)$$  \hspace{1cm} (10)

where $E_a$ is the activation energy for the relaxation mechanism. The slope of the straight line comes out to be 0.471 ± 0.013 and the corresponding $E_a$ as 0.04 eV. This is of the same order of magnitude as the activation energy estimated from the dc resistivity data. This can be explained as follows. The imaginary part of dielectric permittivity ($\epsilon''$) can be written as

$$\epsilon'' = \epsilon' \tan \delta$$  \hspace{1cm} (11)

where $\epsilon'$ is the real part of the dielectric permittivity and $\tan \delta$ is the dissipation factor. The present sample system has been described earlier as a parallel combination of resistance and capacitance, the former contributed by the two-dimensional conductivity of graphene/PVA composite and the latter arising out of the PVA phase. From eq.(6) therefore, we get,

$$\epsilon'' = \frac{\epsilon'}{\omega \rho \epsilon'} = \frac{1}{\omega \rho}$$  \hspace{1cm} (12)

where, $\omega$ is the angular frequency and $\rho$ is the resistivity of the graphene/PVA composite. Hence, $\epsilon''$ should have a temperature variation identical to that of $\rho$.

**CONCLUSION**

In summary, Graphene/PVA composite has been synthesized such that graphene sheets in two dimensions form a network with the sheets in close proximity to each other. The electrical resistivity variation with temperature shows a low activation energy $\sim 0.02 eV$ indicating an electron tunneling process to be operative. We observed that the fluctuation induced tunneling between graphene sheets was the mode of electronic conduction in the composite. The dc IV characteristic was ohmic, while in general the ac conductivities displayed two regions: a low frequency region of constant conductivity and a high frequency region with conductivity increases as a power law. High frequency
exponent extracted from the ac conductivity data confirms the charge carrier movement to be taking place in a two-dimensional space. Dielectric modulus data at different temperatures were analyzed in terms of a relaxation mechanism, which gave an activation energy similar to that found from dc resistivity data. This is shown to be consistent with the structural aspects of the composite studied here. Using the present fabrication technique, it should be possible to prepare flexible conductors with different conductivities.

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