The Relation between Thermodynamics and the Information Theories: The Introduction of the Term Enmorphy

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Abstract

This study aims to present the relation of thermodynamics to the information theories. Thermodynamically, material systems are considered to be understood in terms of Matter, Energy and Entropy. We discuss the significance of the work and the others who contributed for the development of the thermodynamics. In parallel to this fact, the evolution of information theories begins with the mathematization of information. However, Stonier discussed in terms of Matter and Information, considering order to be the inverse of disorder, Or=1/D. Going ahead with the information theories we introduced the term of Enmorphy. We present the concept of Matter-Information–Enmorphy as a system parallel to Matter- Energy-Entropy. The new concept includes the terms: Matter, Information, related to structure, organization and dynamics and the term Enmorphy related to disorder or to the Entropy.

Keywords: Matter-energy-entropy; Matter-information-enmorphy; Analogical thinking

Introduction

Concerning thermodynamics and information theory

The literature on physics, chemistry, biology, medicine, social sciences, arts and other related aspects demonstrates in the last years a very strong trend in the use of Information Theory. Specially the strong interdisciplinary interest [1-3] the complexity studies [4-6] and some recent publications [7,8] demonstrated that there is no consensus on what information is, no consensus on the necessity of an epistemological conception of information. This goal would require the exploration of a wide variety of disciplines including philosophy and science.

Many of the publications [1-8] mentioned before have used the term “Information” as defined by Shannon in 1948 [9]. The way Shannon introduced the definition of information, is a similar one, parallel to the Boltzmann-Gibbs entropy [10-14].

Following paragraphs resume the evolution of the notions of Boltzmann-Gibbs Entropy and the Shannon’s information. We must have in mind that Clausius gives the statements of the first and second law of thermodynamics in 185010, overcoming the caloric theory, but preserving Carnot’s principle. In 1854, in the Clausius Theorem, he established [11] the importance of dQ/T, but he did not named the respective quantity. Only in 1865 he introduced the modern macroscopic concept of Entropy [12,13]. Inspired in the term Energy, the Greek combination of εν and εργια (energia in Latin languages), being ‘work-content in English, werk-inhalt in German, he devised the term Entropy as a corresponding designation for the transformation-contents (verwandlungsinhalt) of a system and for this reason the terms “Εντροπια, Entropie, Entropia, Entropy”.

In the latter part of the nineteenth century, Ludwig Boltzmann almost single-handedly established the field now known as statistical mechanics. One of his major contributions and undoubtedly the most controversial was his H-theorem. According to Tolman and Boltzmann, he stated the equation for the temporal development of distribution functions in phase space and published his H-theorem [14] in 1872. According to Brush [15], the scientific community was initially skeptical of Boltzmann’s result and a lengthy controversy ensued. The Boltzmann’s H-theorem was incapable to relate directly H to the entropy except for very near the final or equilibrium state and it fails to identify the source of irreversibility [16]. The H theorem was published with the intent of showing that the second law of thermodynamics derives from the laws of mechanics. Now it is agreed that the attempted proof was unsuccessful. Boltzmann began by defining the function H for a dilute gas comprised of spherical particles [15]. In this point we have to remember that the content of the Boltzmann’s functional also appears in Shannon’s theory of Information.

According to Müller [17], Gibbs published in 1876 and 1878 two papers with discussion of phase equilibria, statistical ensembles, the free energy as the driving force behind chemical reactions and chemical thermodynamics in general. In the same time, 1877, Boltzmann stated [17,18] the relationship between entropy and probability. This classical thermodynamics evolution was crowned in 1909 with Carathéodory’s [19] axiomatic description of thermodynamics. In his conception, temperature is mathematically defined as the integrating factor who permits the integration of the non-exact differential of the energy conservation expression (first law), proving this way the classical thermodynamics relationship between Energy, Entropy and Temperature. The quantum physics development received in 1927 a very important contribution by Neumann [20] who introduced the density matrix representation and established quantum statistical mechanics.

Concerning Information, the period before and immediately after the second world war was characterized by a huge necessity of efficient and accurate acquisition of information and fast, efficient and error free communication. Is exactly in 1948 when Claude Elwood Shannon establishes “A mathematical theory of communication” and related Information to Entropy [21]. Similar conceptions to Shannon were originally presented by Nyquist [22] and Hartley [23] however, not...
exactly in the same context. Nyquist presented the paper, certain factors affecting telegraph speed [22] contains a theoretical section quantifying "intelligence" and the "line speed" at which it can be transmitted by a communication system, giving the relation

\[ W = K \log m \quad (1) \]

Where \( W \) is the speed of transmission of intelligence, \( m \) is the number of different voltage levels to choose from at each time step and \( K \) is a constant. Hartley’s paper [23] “Transmission of Information”, uses the word information as a measurable quantity, reflecting the receiver’s ability to distinguish one sequence of symbols from any other, thus quantifying information as

\[ H = \log S = n \log S \quad (2) \]

Where \( S \) was the number of possible symbols and \( n \) the number of symbols in a transmission.

It is our opinion that Shannon’s information theory formulated the basis for a development similar to that of the industrial revolution induced by the steam machine. The field is at the intersection of mathematics, statistics, computer science, physics, chemistry, biology, materials science, neurobiology, communications and electrical engineering additional to other scientific disciplines.

The Shannon-Boltzmann-Gibbs “Information-Entropy” isomorphism was strongly criticized by different authors, from different scientific and philosophical disciplines. Shannon never claimed to have developed a theory of information; rather he considered his contribution to have been a theory of communication. In order to follow the criticism on the Shannon theory let present the main conception and the respective definitions.

In the Shannon theory the measure of information is known as entropy, which is equivalent to the average number of bits needed for storage or communication. Entropy quantifies the uncertainty involved when encountering a random variable. The inspiration for adopting the word entropy in information theory came from the close resemblance between Shannon’s formula and very similar known formulae from thermodynamics. Exactly when and how Shannon developed his theory is still uncertain. According to Thomsen [24] there are some evidences about the genesis of Shannon’s information theory. John von Neumann encouraged him to use for the measure of information instead of the word of “uncertainty” the word of “entropy”. “You should call it entropy, for two reasons. In first place, there are some evidences about the genesis of Shannon’s information theory. Stonier in his approach “Information and the Internal Structure of the Universe” [27,28] presents an information theory and assumes that information is a basic property of the universe - as fundamental as matter and energy. Specifically, a system may be said to contain information if such a system exhibits organization. Similarly to mass which is a reflection of a system containing matter and Heat which is a reflection of a system containing energy, the Organization is the physical expression of a system containing information. By ‘organization’ is meant the existence of a nonrandom pattern of particles, energy fields, or other sub-units comprising the system. Considering that the Shannon theory handles manly with message, it is of great importance to discuss the quest information versus message. It is necessary to differentiate between the concept ‘information’ and the concept ‘message’. Similarly to thermodynamics, Energy, in pre-relativity physics, was considered as the more abstract quantity which, when added to matter, manifested itself as heat. Information may be considered as the more abstract quantity which, when added to matter, manifests itself as structure, as organization. "This concept of information leads to a different quantitative definition from that of Shannon." The Stonier’s theory assumes that there exists a direct linear relationship between the degree of organization and the quantity of structural information.

On this basis it is not unreasonable to consider that there exists a direct linear relationship between the amount of organization and the quantity of information. Stonier, affirms that it is needless to say, the verification of this assumption must await the confrontation of theory with physical reality. The starting point of the Stonier’s alternative theoretical approach is Boltzmann's equation as proposed by Schrödinger [29] in 1944.

Where \( \rho \) is the density matrix of the quantum mechanical system. In the Shannon’s formalism the entropy, \( H \), of a discrete random variable \( X \) is a measure of the amount of uncertainty associated with the value of \( X \). Information can be quantified as follows. If \( H(X) \) is the set of all messages \( x \) that \( X \) could be and \( p(x) \) is the probability of \( X \) given \( x \) and then the entropy of \( X \) is defined:

\[ H(X) = E[I(x)] = - \sum_{x} p(x) \log p(x) \quad (5) \]

In equation 5, \( I(x) \) is the self-information, which is the entropy contribution of an individual message and \( EX \) is the expected value. In this representation Shannon equals the expected information to total entropy. An important property of entropy is that it is maximized when all the messages in the message space are equiprobable.

\[ p(x)=1/n, \]

—i.e., most unpredictable - in which case \( H(X)=\log n \).

The special case of information entropy for a random variable with two outcomes is the binary entropy function \( H_b(p) \) given by the equation 6.

\[ H_b(p) = -p \log p - (1-p) \log (1-p) \quad (6) \]

The formalism of Shannon, stemming from Hartley’s original ideas, received strong conceptual criticisms from different authors. Cherry [25] in 1978 has commented that: ‘it is a pity that the mathematical concepts stemming from Hartley have been called ‘information’ at all’. Cherry goes on to point out that the formula derived by Shannon for the average information contained in a long series of symbols is really a measure of the statistical rarity or ‘surprise value’ of a course of message signs. “This is hardly a true measure of the information content of a message”.

The other important critic was formulated by Wicken [26] in 1987 how has shown that: "While the Shannon equation is symbolically isomorphic with the Boltzmann equation, the meanings of the respective equations bear little in common".

Information related to structure and organization

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\[ S = k \log D \]  
(7)

Where \( S \) is the entropy of the system, \( k \) = Boltzmann’s constant and \( D \) is the state of disorder of the system. Although Schrödinger did not write it as an equation, it is clear from the text that he considered ‘order’ to be the inverse of ‘disorder’, \( O = 1/D \) and implicit in his writing is the equation:

\[ S = k \log O \]  
(8)

Where \( O \) is the state of order of the system. Using the assumption of a direct linear relationship between the amount of organization (\( O \)) and the quantity of information (\( I \)), that is:

\[ I = c(O) \]  
(9)

Where \( c \) represents a constant to be defined. By substituting in equation (9) one may derive the relationship between information and entropy,

\[ I = c e^{-S/k} \]  
(10)

The constant \( c \), upon further examination, has proven to be equal to the information content of a system when its absolute entropy equaled zero. Equation (10) can be modified as:

\[ I = (I_0) e^{-S/k} \]  
(11)

\[ S = -k \ln (I_0 / I) \]  
(12)

Where \( I_0 \) is the information content of the system when \( S = 0 \).

The \((I/I_0)\) may be restated as a probability function, at which point its values correspond to Boltzmann’s original W (Worscheinlichkeit). It is important to realize that Boltzmann’s equations were derived from studies in gases in which \( I \) would never exceed \( I_0 \).

This approach indicates a very different relationship between information and entropy from that understood by the communications engineers (Shannon and others). Instead of there being a direct relationship between information and entropy, as proposed by Shannon and Weaver [21], or a negative one as modified by Brillouin [30], states that information and entropy are inversely related. To be more precise, entropy is the multiplicative inverse of information, not, as is generally viewed today, the additive inverse. Furthermore, entropy must not be viewed as a simple metaphor for describing information.

**The attempt to unify theories of information**

Trying to elucidate and understand the nature of information and the related theories we have to comment the interdisciplinary very broad contribution edited by Hofkirchner [31] in 1999. “The quest of a Unified theory of information” includes a series of works related to the unification of the presented Information Theories.

Between other papers, Flückiger presents a paper [32] with the title “Towards a Unified Concept of Information: Presentation of a New Approach”. In this paper he differentiates between two main streams of Information Theories, namely: a) Functional-cybernetic information theories: In this category information is understood as functionality, functional meaning or as a feature of organized or self-organized systems which explain some dynamical aspects of information. (This includes mainly the conceptions of Shannon and neo-Shannonites) and b) Structural-attributive information theories: In these theories, information is understood as structure, diversity, order, etc. These theories are based in the statement that “Each animate or inanimate individual has an inner structure, the diversity of which constitutes the individual’s information content. In this category, he includes Szilard [33], Wiener [34], Brillouin [32], McKay [35], Delvin [36] and Stonier [28].

It is the reality that the two types of information theories explain different aspects of information and both types have remained useful to this day. However many issues remain objects of strong controversy between the two different information theories. Until today, in so far our knowledge, there was no success in the unification attempt which confirms the actual historical point.

### Toward the introduction of enmorphy

The attempts to unify the Functional-cybernetic information theories with the Structural-attributive information theories were and continue remaining without success: In this point we would try to contribute with a critical analysis aiming to elucidate the origin of the difference between the two main information theories. In order to proceed, let as have in mind some fundamental notions of sciences like: a) the wave function which describes the spatial and temporal periodicity characteristics of a material system, b) the time correlation and autocorrelation function, c) the spatial correlation function, d) the numerical simulation analysis techniques between other similar issues. The mentioned notions are some of the fundamentals for the description of spatial and temporal characteristics of physical systems which constitute the main elements of system morphology [37-40].

Actually, the quantification of morphological analysis is creating the strongly increasing area of “Morphometry” [41-44]. The evolution of informatics becomes a “tsunami” for the scientist. Counting, measuring and analyzing aspects of morphometry becomes increasing in the last decade. Davatzikos [45-47] is one of the innumerous examples in the brain morphology. Alain [48] and Adams [49,50] and their coworkers are some examples of the area of biology and dimensional analysis. Consider that the definition of Entropy was given in relation to heat, in other words related to energy involved in a process. Connections between information-theoretic entropy and thermodynamic entropy, are explored by Jaynes [51] including the important contributions by Landauer [52]. The absolute temperature was inversely related to the differential of entropy, \( dS \), through the equation \( dS = dQ/T \). According to Carathéodory [19] the parameter \( 1/T \) transforms the heat in integrable quantity and the integration result is the Entropy. Resuming, we observe that the entropy (Boltzmann-Gibbs or Neumann) is strictly related to the total probability of the possible distinct energy states of the material system. Similarly the Rényi entropy theory [53] and the q-statistics of Tsallis [54,55] generalize the conception of entropy. Tsallis introduced the entropic index \( q \) which is intimately related to the microscopic dynamics of the observed system and characterizes the degree of non-extensivity. The values \( q<1, q=1 \) and \( q>1 \) correspond respectively to superadditivity (superextensivity), additivity (extensivity) and subadditivity (subextensivity). The introduction of the generalized q-statistics is surely affecting the area of the information theories ones they are intimately related to the entropy [49].

Again, trying to elucidate the “Functional-cybernetic and the Structural-attributive Information theories” we observe that: The first one is strongly related to “message” and consequently to communication (storage, emission, reception), consequently related to dynamical aspects of the message structure. The second one is related to static organization, the static order and generally the static structure aspects of the information. As we observed, both theories include information structural aspects, however the first one is mainly dominated by the dynamic (emission, reception) aspects, while the second appears to be time invariant. Let us rationalize in a similar way to classical thermodynamics. Clausius [11-13] added to the terms
Matter and Energy the term Entropy independently of the dynamical aspect. In the same way, it seems obvious, a generalized information theory must include additionally to the Matter, the terms information (related to Structure and organizations) and a new term is introduced for the first time in this paper, namely the term Enmorphy. The choice of the term information (parallel to the energy) seems to be generally plausible and acceptable. By information is meant the existence of a structure or organization of nonrandom pattern of particles, energy fields, or other sub-units comprising a system. It is the term parallel and "analogon to energy. Energy is the entity which produces the energetic states of the material system. Similarly a system can include different and various forms of information expressed as organization, as structure. In this case the term Enmorphy is proposed which is composed by the terms en (Greek εν) and morphe (Greek µορφη) and means "turn the appearance (the morphe) in to inside" similarly to Entropy meaning "turn the energy in to inside". Both terms include the meaning of "loss, hide, occult a property". In the case of entropy a loss of energy inside the system is happened, while in the case of Enmorphy a loss of information in terms of structure or organization is happened inside the system. The term Enmorphy, must be understood similarly to Entropy as the physical entity which in the case of spontaneous processes tends to increase. The above analysis and the respective definitions, primarily eliminates the isomorphism question of the Shannon’s theory. The centrality of the energy is substituted by information and finally the notion of the Boltzmann- Gibbs or von Neumann Entropy is substituted by the notion Enmorphy. The proposed concept creates a new conceptual basis, namely, that of matter, information, enmorphy parallel to the thermo dynamical conception of matter, energy and entropy. Including into concept of matter- information-enmorphy the notion of time we integrate automatically the dynamical aspects, the processing and transmission of information.

Of course, there are many similarities between the Material-Information-Enmorphy and the Material-Energy-Entropy conceptions; however, this would be a challenge to look after the mathematical relations which govern these two conceptions. The construction of a generalized Information Theory based on the proposed concept would needs elevated attention exactly because of the similarity with thermodynamics. The tendency of the "analogical thinking" was and continues constituting an important "instrument" of the human way to think.

Some additional remarks

The proposed concept of Matter-Information-Enmorphy is not philosophically equivalent to the concept of Matter-Energy-Entropy. Sure, there are very important relations between the entities included in the concepts, however it would be not correct to equalize energy to information without definition of process, it would be precipitated to define lows of "information conservation" as a parallel to the "energy conservation" or rules of "Enmorphy additivity" as a parallel to Entropy additivity, as proposed by Boltzman-Gibbs for Entropy. Equally the validity of the Q-statistics has to be discussed in the Matter-Information-Enmorphy concept. Dynamical aspects (time dependence) related to the proposed concept would need elucidation, notions as periodicity (wave functions), time and space correlations, may be discussed adequately in relation to Enmorphy. Finally the notion of Enmorphy and its relation to temperature has to be evaluated and elucidated. Intuitively, it would be necessary to introduce a new relation evolving Information, Enmorphy and Temperature. These remarks aimed to indicate the possibility of opening the new scientific field of Enmorphy.

Conclusion

An analysis of the fundamental ideas of Clausius, Boltzmann, Gibbs and Neumann, then the introduction of the early information theory with the ideas of Shannon, Nyquist and Hartley and later by Stonier, permitted to formulate the new concept of Matter-Information-Enmorphy as a construction parallel to Matter-Energy-Entropy. The concept introducing the notion of Enmorphy overcomes the isomorphism between Shannon-Stoner Information Theories and Boltzmann-Gibbs-Neumann entropy theory. In other words, the Thermodynamics and the Information Theories are described by the same mathematical formalism. What they have in common is the Matter. Matter is what we feel with our senses. Energy is used as the parallel to Information and Entropy as the parallel to Enmorphy. They are four totally different properties, including different content. This is the reason why we have introduced the Enmorphy. The proposed concept of Matter--Information--Enmorphy would probably initiate a new field in sciences.

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