Vortex-ring-induced large bubble entrainment during drop impact

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For a limited set of impact conditions, a drop impacting onto a pool can entrap an air bubble as large as its own size. The subsequent rise and rupture of this large bubble plays an important role in aerosol formation and gas transport at the air-sea interface. The large bubble is formed when the impact crater closes up near the pool surface and is known to occur only for drops that are prolate at impact. Herein we use experiments and numerical simulations to show that a concentrated vortex ring, produced in the neck between the drop and the pool, controls the crater deformations and pinchoff. However, it is not the strongest vortex rings that are responsible for the large bubbles, as they interact too strongly with the pool surface and self-destruct. Rather, it is somewhat weaker vortices that can deform the deeper craters, which manage to pinch off the large bubbles. These observations also explain why the strongest and most penetrating vortex rings emerging from drop impacts are not produced by oblate drops but by more prolate drop shapes, as had been observed in previous experiments.

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I. INTRODUCTION

When a liquid drop impacts onto a liquid pool, it can entrap air bubbles of different sizes [1–19]. While the smallest bubbles can dissolve, contributing to the gas transfer into the pool [1], the largest bubbles rise to the surface where they burst. The latter mechanism can produce many smaller bubbles [20] and aerosols in the atmosphere [10,21,22]. Different mechanisms have been identified as being responsible for air entrainment [23]. Recent progress in high-speed video imaging has allowed researchers to explain some aspects of bubble entrainment [12], and even to discover new mechanisms [24–26].

Here we focus on the so-called large bubble entrainment identified by Pumphrey and Elmore [27]. They observed that for a small range of water drop diameters and impact velocities, the cavity produced by the drop expands radially below the pool surface and closes at the top to entrap a large bubble. They already suggested that the drop shape oscillations play an important role in this entrainment. Zou et al. [28] have recently reported a similar large bubble entrainment for horizontally restricted pools. They determined that such bubbles were observed only for prolate drops, i.e., those with a larger vertical extent. Finally, Wang, Kuan, and Tsai [29] have shown that large bubble entrainment on unrestricted pools also occurs only for prolate drops, and over a wider range of conditions than originally observed [27].

However, the underlying mechanism for this large bubble entrainment has remained a mystery until now. We combine herein high-speed imaging and numerical simulations to show the crucial role played by vorticity in deforming the interface and entrapping the large bubble. The role of vorticity in this process has been ignored in the above studies. It is indeed only recently that the effects of vorticity on drop-impact splashing have been demonstrated [24–26,30,31].

II. EXPERIMENTAL SETUP

We use drops pinched off from a nozzle and impacting onto a pool surface. We adjust the impact velocity by varying the impact height $H$. By using slightly different liquids in the drop and the pool, the difference in refractive index reveals the deformation of the interface between the two liquids while keeping the main features of the flow unchanged (see Sec. IV F). Figure 1 shows such a case. The first image shows the presence of a strong vortex ring, made visible by the roll-up of the liquid-liquid interface. The vorticity is produced by the flow around the curved free surface during the early dynamics (see Ref. [32], p. 366) and it has been the subject of many studies [6,33–45], as will be discussed in Sec. V. In the following images, the air-liquid interface is pulled around and toward the core of the vortex, first radially outward in the third frame, then upward in the fourth frame. This creates a tongue of liquid above the cavity, pulled toward the center by surface tension, which finally closes to entrap the large bubble. The pulling on the interface can be explained by the lower pressure at the core of the vortex and the velocity field around it [46,47].

III. NUMERICAL SIMULATIONS

We perform numerical simulations to understand the effect of the different parameters on the vorticity dynamics. We use the GERRIS code [48,49], validated in previous studies on drop impact [24,26]. It solves the Navier-Stokes equations with a volume-of-fluid method for the two-phase flow and a dynamic adaptive grid refinement.
FIG. 1. Side view imaging of a prolate drop impacting into a pool $(D = 5.0 \text{ mm}, V = 0.9 \text{ m/s})$, observed below the pool surface at the following times after the first contact: 7.7, 8.7, 11, 13, 16, 20, 24, and 27 ms. A slightly different liquid is used in the drop (10.5% MgSO$_4$ solution with viscosity 1.96 cP and density $1.105 \text{ g/cm}^3$) and the pool (distilled water) to visualize their interface (hemispherical and curled line in the first frame). The dark region is the air cavity created by the impacting drop. The scale bar is 1 mm long.

We simulate the axisymmetric impact of a water drop onto a water pool initially at rest, including gravity. A passive tracer is initially placed into the drop (colored in red) to identify the origin of the water, in a similar way as in the experiment in Fig. 1. The main tracer used to follow the air-water interface is not affected by this additional tracer.

The use of numerical simulations allows for a precise control of the drop shape, independently of the impact velocity. We compare here the impact of a spherical drop to ellipsoids of revolution. The equivalent drop diameter is defined as $D = (D_h^2 D_v)^{1/3}$, with horizontal diameter $D_h$ ($a = D_h/D$) and vertical diameter $D_v$ ($b = D_v/D$). The vertical diameter is obtained by volume conservation: $b = 1/a^2$. The simulation starts before the drop touches the pool, with a uniform vertical drop impact velocity $V$.

In the axisymmetric domain of size 1, the drop has a radius of 0.13 and the pool depth is $2.5D$. The mesh is refined near the air/water interface, the passive tracer interface, and in the regions of high vorticity, at a maximum refinement level of 11, corresponding to the smallest cells of size $2^{-11} (D/\delta x = 532)$. Some numerical details are given in Thoraval et al. [24]. Only at the upper boundary of the parameter regime do we see some effect of increasing resolution (see the supplemental material [50]). This would benefit from an even higher level of mesh refinement, but it is prohibitive due to the long duration of the entrapment process, especially compared to the first ejecta studied in [24], were such superresolution simulations are feasible.

All variables marked with an asterisk are nondimensionalized with $D$ and $V$, including $t^* = t/\tau$, with $\tau = D/V$.

IV. RESULTS

Figure 2 shows a typical time evolution leading to the large bubble entrapment, for a prolate drop under conditions similar to Fig. 1. Despite the use of different liquids in the experiments,
FIG. 3. Influence of gravity on large-bubble entrapment. This sequence is for the same conditions as in Fig. 2, which includes gravity, while in this figure gravity has been excluded. $t^* = -0.05, 0.18, 0.41, 0.87, 2.99, 4.80$. $D = 5 \text{ mm}$, $V = 1.0 \text{ m/s}$, and $a = 0.9$.

and the uncertainty on the drop shape, the simulation captures very well the dynamics, including the rectangular shape of the bubble after pinchoff, and the vertical jet in the center. We see clearly the early shedding of vorticity on the side of the drop [inset of Fig. 2(b)], hidden in experiments because of the curved interface above the pool surface, but visible by x rays [30]. The side vortex ring then rolls-up with the trailing vortex sheet into a larger vortex ring, which pulls radially on the interface below the surface of the pool (see videos in the supplemental material [50]).

A. Role of gravity

What is the role of gravity in this entrapment process? This can be directly addressed in the numerical simulations, where we can simply turn gravity off. The typical Froude number $Fr = V/\sqrt{gD}$ is rather low ($Fr = 4.5$ in Fig. 2). Gravity can therefore be neglected during the initial impact of the drop ($t^* \leq 1$), but it may affect the dynamics at later times. This is indeed what is observed. Figure 3 shows that large bubble entrapment still occurs even if gravity is removed. The sequence shows no significant difference up to the time of entrainment of the bubble. Only in the last image, at time $t^* = 4.8$, does gravity influence the bottom shape of the bubble. Gravity is therefore not responsible for large bubble entrapment.

In contrast, gravity plays a key role in regular bubble entrapment, which is produced at the bottom of the collapsing impact crater [2,4,51] and is greatly affected by the hydrostatic pressure. This was also verified with our simulations, as shown in Fig. 4. Regular entrainment, by pinchoff of the bottom of the crater, is no longer observed if gravity is removed.

This difference is consistent with the different time scales of these entrainment mechanisms. The large bubble entrapment occurs at $t^* \sim 3$ [see Figs. 2 and 6(a)], while the regular entrainment is observed at longer times ($t^* \sim 5.6$ in our simulations, or 9.4 in Fig. 4 of Ref. [27]).

B. Parameter space

We explore the effect of impact velocity $V$, drop diameter $D$, and drop shape on large bubble entrapment. Figure 5(a) shows the $D-V$ parameter space where large bubbles are entrapped ($\blacktriangle$). For all cases in the figure, we have simulated five different drop shapes with horizontal diameter $a = D_h/D$

and values of 0.9, 0.95, 1, 1.05, and 1.1. Large bubble entrapment occurs only for the largest vertical elongation of the drop (the most prolate), i.e., $a = 0.9$, in the parameter range reported

FIG. 4. Role of gravity on regular bubble entrapment, at the bottom of the collapsing crater. Same impact conditions as in Fig. 2, but now for a spherical drop, $a = 1$. With gravity (top) or without (bottom), $t^* = -0.05, 0.18, 0.41, 0.87, 1.80, 2.99, 3.64, 4.80, 5.72, and 7.64$. $D = 5 \text{ mm}$, $V = 1.0 \text{ m/s}$.

FIG. 5. (a) Parameter space where a large bubble is entrapped ($\blacktriangle$) or is not ($\bullet$). All simulations are for a prolate water drop with a horizontal axis $a = D_h/D = 0.9$. No large bubble entrapment was observed for other drop aspect ratios when $a$ is 0.95, 1, 1.05, and 1.1. Large bubble entrapment occurs only for the largest vertical elongation of the drop (the most prolate), i.e., $a = 0.9$, in the parameter range reported
in Fig. 5(a). The goal of this study is to understand the underlying mechanism of the large bubble entrapment, rather than mapping an extensive parameter space. By comparing here drops with the same volume and impact velocity, we are able to confirm the crucial effect of the drop shape, as previously suggested. The parameter space is consistent with the experiments of Wang et al. [29], showing similar lower and upper limits on both axes. The less clear upper limit in impact velocity \((V \approx 1.6 \text{ m/s})\) is probably due to insufficient numerical refinement for such a high Reynolds number \((\text{Re} = \rho DV/\mu = 8000)\), as was demonstrated by the very high refinement needed in the study of Thoraval et al. [24], when capturing the details of the earliest contact. Keep in mind that our regime of \((\triangle)\) is continuous, whereas in experiments, the prolate phase of the pinched-off oscillating drop is restricted to certain discrete release heights and thereby impact velocities [26,29].

The size of the large bubble increases with the impact velocity [Fig. 5(b)], except for the last point, which lies at the limit of the entrapment region. The bubble diameter is 20–75% larger than the drop. For the highest impact velocities, these simulation numbers are still sensitive to refinement level. This trend is consistent with the experiments of Zou et al. [28], although their study was on a horizontally confined pool.

The top enclosure and entrapment occurs in most cases at \(t^* \approx 3.3\) with a couple of the higher-velocity impacts closing in shorter time \(t^* \approx 2.8\) [Fig. 6(a)]. This is consistent with Fig. 1 \((t^* \approx 3.2)\) and previous observations \((t^* \approx 3.5\) in [27] and 2.7 in [28]). The bubble closes below the original pool surface, at about one drop radius in depth [Fig. 6(b)].

**C. Vortex pulling**

To understand the mechanism responsible for large bubble entrapment, from hereon we focus on one typical impact condition \((D = 5 \text{ mm}, V = 1 \text{ m/s}), and we change the drop shape. Figure 7 gives a clear indication of the role of the drop shape in large bubble entrapment. It changes the strength and dynamics of the vortex ring and its interaction with the interface. The relevant time scale for the drop entry time into the pool and the early formation of the cavity is \(\tau_c = D_c/V = \tau/a^2\). By comparing the impact for five different drop shapes at the same nondimensional time \(t/\tau_c\), we observe that the vortex pulls on the interface and self-destructs earlier for the flatter drop (larger \(a\)). Therefore, it cannot pull on the interface to produce the large bubble.

This can be further analyzed by tracking the strongest vortex ring shed into the pool (Fig. 8), as shown in Fig. 2(b) and the second row of Fig. 7. The time when the vortex ring strongly pulls on the interface can be identified in its trajectory when it moves together with the deformed interface. This shows the vortex move rapidly radially outward, and then being deflected upward, forming a characteristic hump in Fig. 8(b). As a consequence of this pulling, a tongue of the interface penetrates into the vortex ring, leading to a sharp decrease in intensity [Fig. 8(a)]. This also helps to promote an inward motion in the case of large bubble entrapment (starting from the \(\downarrow\) on the curve).

The surface pulling occurs later for more prolate drops, which confirms the previous observation from Fig. 7. For \(a = 0.9\), it even occurs for \(t/\tau_V > 1\). The location of the pulling is also very different. For the flattest drop (\(a = 1.1\)) it occurs above the pool surface, while for \(a = 0.9\) it is lower than \(-D/3\). This changes the curvature and orientation of the interface where the vortex pulls, leading to different crater structures. For the oblate drop, the vortex starts to pull on the side of the drop before it has fully entered the pool. The resulting liquid protrusion is thinner and more vertical, and therefore is rapidly pulled back by surface tension. In contrast, the prolate drop pulls on the interface below the pool surface, on the side of the cavity created by the impacting drop (fifth panel of Fig. 2). The thicker and more horizontal liquid tongue is thus able to collapse on the central axis to entrap the large bubble.

**D. Vortex dynamics**

To understand how the shape of the drop changes so drastically the time and location of the pulling, we need to analyze the earlier dynamics of the vortex ring. First, we observe that a more oblate drop produces a stronger vortex ring [Fig. 8(a)]. This is due to a geometrical effect: when a flatter drop meets the pool surface, the neck shape forms a sharper cusp than for a circular or prolate drop. A stronger curvature will produce stronger vorticity (see Sec. V). Then, we also observe that the dynamics of the vortex ring changes...
with the drop shape. Although the vortex rings closely follow the neck in the radial direction in all cases up to \( t/\tau_v = 0.5 \) (see Fig. S3 [50]), the dynamics is different in the vertical direction. The vortex ring separates from the interface earlier for more prolate drops [Fig. 8(d)].

These two effects both contribute to the delayed pulling of the vortex ring on the interface for the prolate drop, leading to large bubble entrainment. As the vortex is weaker and further away from the interface in that case, it exerts a smaller force on the interface. It is therefore able to move deeper into the pool before pulling on the interface.

This explains why the pulling of the interface occurs later for prolate drops, only when the opening cavity brings again the interface closer to the vortex. It also explains why the vortex ring is able to generate a stronger vortical flow, as it is further away from the interface. The key role of the vorticity shedding in the dynamics of drop impacts was first observed in Thoraval et al. [24], and further studied in [30,31,45]. However, the complex process of vorticity production and separation from the free surface is still not fully understood. This study brings another contribution to this problem, showing the effect of drop shape on vorticity shedding.

The earlier vorticity shedding for more prolate drops is probably due to the faster vertical motion of the sharp interface point on the side of the drop (wider angle between the drop and the pool). As the liquid from the pool moves faster vertically on the side of the drop (see Fig. 2), the corner where vorticity is generated is pushed against the dominant downward velocity, thus promoting vorticity shedding.

**E. Energy and momentum**

To understand the effect of the vortex on the larger-scale dynamics, we can decompose the kinetic energy and momentum in the radial and vertical directions (Fig. 9). The radial (vertical) kinetic energy \( EK_R \) \( (EK_Z) \) is defined as the volume integral over the whole domain of \( \frac{1}{2} \rho V_R^2 \) \( (\frac{1}{2} \rho V_Z^2) \), where \( V_R \) \( (V_Z) \) is the radial (vertical) component of the velocity. The total kinetic energy is the sum of the two for this axisymmetric simulation: \( EK = EK_R + EK_Z \).

The dominant energy in the impact is the kinetic energy, while the initial surface and potential energy represent only 17% and 10%, respectively, for the typical case studied here. The surface energy of the ellipsoidal shapes is larger than that of the spherical drop, as it is the minimal surface. However, for the shapes studied here, the surface energy changes by less than 1.7%, and therefore less than 0.3% of the initial kinetic energy. This difference can therefore be neglected. The kinetic energy is initially only vertical, and the radial kinetic energy is produced as the drop enters the pool.

We also normalize the time by \( \tau_v \) based on the vertical diameter, as it is the relevant time scale at which the energy is transferred from the impacting drop to the pool. Even in this rescaled time frame, the release of vertical kinetic energy is initially slower for the drops with a larger vertical extension. This can be understood by an added mass effect, as the resistance from the pool will be lower for the drops showing a smaller horizontal extent perpendicular to the impact direction.
FIG. 9. Kinetic energy $E K$ in radial (a) and vertical (b) directions, normalized by the initial kinetic energy of the drop. The total combined kinetic energy is shown in Fig. S4 of the Supplemental Material [50].

However, this tendency is later reversed, so that all cases reach a similar vertical kinetic energy around $t/τ_v ≥ 1.5$.

From $t/τ_v ≥ 0.75$ until the pulling time of the vortex on the interface, the radial kinetic energy is larger for the prolate drop [Fig. 9(a)]. However, the outward radial momentum is still lower [Fig. 10(a)]. The larger kinetic energy therefore reveals a stronger inward velocity toward the axis of symmetry, as the dominant radial flow is away from the center. This shows that although the vortex for the prolate drop is initially weaker, it is able to generate a stronger large-scale rotational motion in the flow, beneficial for the closure of the liquid tongue above the large bubble. In contrast, the stronger vortex for the oblate drop self-destructs earlier by pulling on the interface, stopping the development of the vortical flow.

Finally, Fig. 10(b) shows that the radial momentum starts decreasing strongly after $t^* ≃ 2$, nondimensionalized by $τ = D/V$, based on the equivalent diameter of the drop. This is characteristic of the reversing flow due to gravity toward the axis of symmetry, as confirmed by the comparison with the same cases without gravity. Gravity starts playing a significant role from that time, as shown by the large deviation of the dotted curves.

This reversing flow is probably beneficial for the liquid tongue to close the cavity and entrap the large bubble. As the interface pulling occurs later for the prolate drop (also in the rescaled time with $τ_e = D_e/V$), it is closer to the time when the liquid flows back toward the axis. However, even without the effect of gravity, the radial momentum still shows a sharp decrease just before the large bubble entrapment. It therefore shows that the closure of the liquid tongue above the cavity is mostly driven by surface tension, after the strong decrease of radial expansion by the vortical flow.

**F. Other experimental conditions**

Figure 1 uses 10.5% MgSO$_4$ in the water drop to introduce a strong index-of-refraction difference between the drop and the pool liquids, to allow us to visualize clearly their interface and identify vortex structures. This also introduces a density difference $ρ_d/ρ_p = 1.105$ and a viscosity difference, where the drop liquid is 1.95 times more viscous than the distilled water in the pool. However, in the numerical simulations, both liquids are modeled with water properties. To quantify possible effects of the difference in properties, we performed another set of experiments with about half the salt concentration, i.e., for 6% MgSO$_4$. Figure 11 shows that the overall entrapment of a large bubble is the same as for the higher salt concentration. This suggests that the density difference between the drop and the pool does not significantly change the large-bubble entrapment dynamics. The lower concentration reduces the contrast in the imaging.

Figures 12(a) shows the entrapment dynamics for a prolate drop with the same liquid properties as Fig. 1, but at a larger impact velocity. The numerical simulation for similar conditions again reproduces very well the dynamics, including...
FIG. 11. Large bubble entrapment for a drop of 6% MgSO$_4$ giving $\rho_d/\rho_p = 1.06$ and $\mu_d = 1.3$ cP for $D = 5.0$ mm, $V = 0.94$ m/s, and $H = 5.0$ cm. The sequence shows the following times: −2.3, 7, 11, 17, and 25 ms after the first contact. The scale bar is 1 mm long.

the shape of the large bubble and the liquid column at its center [Fig. 12(b)].

For reference, experiments in Fig. 13 show the dynamics for oblate drops at two intermediate impact velocities, where no large bubble is entrapped. However, the collapse of the crater can produce vortex rings, as visible in the last panels. The small drop visible in the fifth panel of both sequences is the satellite produced when the primary drop pinches off from the nozzle.

V. DISCUSSION

Herein we have argued that the vortex ring produced by the early contact of the drop with the pool can explain when a large bubble is entrapped into the pool. It is therefore crucial to explain how this vortex is formed and how its formation relates to the drop shape. This issue of vorticity production was debated two decades ago in the context of drop impact [36–38,52,53], but it appears not to have been universally accepted within the community. The proposed mechanism was not verified either experimentally or numerically, due to the challenges of capturing the dynamics near the interface. It is therefore worthwhile to review some of the underlying arguments behind the theory, and to support it quantitatively with our numerical results. A general review on vorticity production can be found in Brøns et al. [54], while we will focus here only on the case of drop impact.

A. Vorticity production in drop impact

The basic concept of the persistence of irrotationality, i.e., fluid originally in irrotational motion will continue to move irrotationally, is one of the foundations of classical hydrodynamics. This theorem is discussed by Batchelor (Ref. [32], pp. 276 and 277), and he attributes it to Lagrange, with the first demonstration by Cauchy in 1815. The theorem applies for homogeneous flows with constant density that are originally irrotational or start from rest. This applies at all times for inviscid fluids, but also for regular viscous fluids away from the boundaries, from where the vorticity must emerge. Batchelor further states the following: “Vortex strength or circulation cannot be created in the interior of the fluid, but once there it is spread by the action of viscosity,” and he continues for motions of a viscous fluid from rest (p. 277 in [32]), “Initially the vorticity is everywhere zero and the motion must remain wholly irrotational unless vorticity diffuses across the surface bounding the fluid.”

This is clearly the basic condition when a drop impacts on a pool. The pool is at rest and the motions within the falling drop are slow and likely well described by basic irrotational shape.
oscillations, which are promoted during the pinchoff from the nozzle. In numerical simulations these initial motions within the drop can be set to zero, and our initial conditions are simply a drop with a uniform vertical velocity. With this initial condition, on the drop flow-field, our numerical simulations reproduce the experimental results. We therefore conclude that the oscillatory motions within the falling drop are not a significant factor during the very rapid impact motions, and they can be ignored. The oscillations only served to change the drop shapes present at initial contact.

The vorticity in the observed vortex ring must therefore arise from the free surface and cannot be produced spontaneously within the pool by the pressure-driven initial flow due to the impact. Those motions must be irrotational as postulated above. This can also be inferred from the absence of the pressure in the vorticity equation.

Next we must ask, what is the nature of the vorticity production?

Cresswell and Morton [37] propose what we believe is the correct origin of the vorticity. Their explanation is based on the vorticity produced by the flow $q$ along a curved free surface, which has a local radius of curvature $R$. The strength of this vorticity generation for a stationary two-dimensional free surface has the form (see p. 366 of Ref. [32] as well as Ref. [55])

$$\Delta \omega = \frac{2q}{R}. \quad (1)$$

This equation essentially arises from the fact that we cannot satisfy simultaneously the stress-free boundary condition and irrotationality and must relax the latter to avoid infinite tangential accelerations of the fluid element at the free surface.

The free surface can be considered circular locally by expansion of the Navier-Stokes equations [56]. In the corresponding local polar coordinates, the two conditions are expressed by the sum and difference of identical terms,

$$\sigma_{r\theta} = \frac{\partial u_{\theta}}{\partial r} - \left( \frac{u_{\theta}}{r} - \frac{1}{r} \frac{\partial u_{r}}{\partial \theta} \right) = 0,$$

which cannot both be satisfied at the same time. Substituting into the $\omega$ equation for $\partial u_{\theta}/\partial r$ from the first equation and realizing that $\partial u_{r}/\partial \theta = 0$ along the circular free surface, we get $\omega = 2u_{r}/r$, thereby recovering Eq. (1). For strong vorticity production, either $q$ must be large or the radius of curvature $R$ must be very small. For the drop-impact case, the sharp corner is formed in the neck connecting the drop to the pool once they have formed a bridge.

Equation (1) is also valid for an interface with a fixed shape moving at a constant velocity (Ref. [32], p. 365). Ohring and Lugt [57,58] have shown that it also gives a correct estimate of the vorticity produced for slowly deforming interfaces. Equation (1) has been generalized to flows along three-dimensional free surfaces by Peck and Sigurdson [39], but this is not needed here.

Although Eq. (1) explains the origin of the vorticity, it only appears as a boundary condition to satisfy on the interface. Once this vorticity is produced, it will diffuse into a thin boundary layer, which can separate to enter the pool. These mechanisms have been studied in [38,59]. However, it still remains a challenge to understand the separation of vorticity in drop impacts and its effects on the interface [30,45].

B. Validation

Our numerical simulations have been able to correctly reproduce the large bubble entrapment that was previously observed experimentally, and to explain it by the pulling of a vortex ring. They can therefore be used to pinpoint the origin of the vorticity in this vortex ring.

The insets in Fig. 2 show that the vortex ring emerges from the sharp upper corner in the rapidly growing neck. This is consistent with the explanation of Cresswell and Morton [37], suggesting that the largest vorticity should be created in the regions of highest curvature. This is shown in more detail in FIG. 14. Emergence of the vorticity from the growing neck connecting the drop and the pool. The last row is zoomed on the point of highest curvature of the interface, where the vorticity is produced.
We can make another important clarification with this figure: no vorticity is produced at the interface between the liquid originally in the drop or the pool. In the bottom left panel, we observe that two vortices of opposite signs are produced in the upper and lower corner of the neck. This is consistent with the previous results of Josserand and Zaleski [40]. In the last bottom panel, the top corner of the neck has moved further away from the line, together with the point of highest vorticity, demonstrating this even more clearly. For much higher impact velocities than studied here, the two opposite sign vortices can shed, alternatively forming a vortex street [24].

However, no significant vorticity is observed near the line separating the drop and the pool liquids. This is simply because this interface, between the red and blue regions in the top of Fig. 14, is not a material interface. It is only a visualization artifact to identify the origin of the liquid, from the drop or the pool. In reality, it is only a homogeneous liquid. The physical reason for this is that we are solving the Navier-Stokes equations, which do not allow for discontinuity. The contact between the drop and the pool occurs smoothly, due to the air cushioning. The velocity field is continuous even across this line between drop and the pool liquids, without any vortex sheet produced there.

We can also verify the proposed vorticity production mechanism quantitatively with our numerical simulations. Relation (1) is derived for a two-dimensional stationary mechanism with the previous results of Josserand and Zaleski [40]. In the bottom left panel, the top corner of the neck has moved further away from the line, together with the point of highest vorticity, demonstrating this even more clearly. For much higher impact velocities than studied here, the two opposite sign vortices can shed, alternatively forming a vortex street [24].

For a rough estimate, we take the typical example of a water drop of diameter $D = 5$ mm impacting at a velocity $V = 1$ m/s. The vorticity maximum near the interface is $1.4 \times 10^5 \, \text{s}^{-1}$ at $t = 0.52$ ms. The minimum radius of curvature of the interface is observed at the same point, with $R = 10 \, \mu\text{m}$, and the tangential velocity relative to the interface is $q = 1.27 \, \text{m/s}$. The right-hand side of Eq. (1), $2q/R = 2.5 \times 10^5 \, \text{s}^{-1}$, is of the same order of magnitude as the observed vorticity at the interface.

Another simple verification of Eq. (1) can be done by looking at the effect of the geometry. Rescaling the strength of the vortex ring, from Fig. 8(a), by the vertical diameter of the drop $b$ collapses the curves, as can be seen in Fig. 15, where the curves are identical up to the point where the vortex interacts strongly with the free surface. This is consistent with Eq. (1), where the vorticity is proportional to the curvature of the interface, $\propto 1/b$. The early decay of the vorticity follows a $t^{-1/2}$ power law, characteristic of viscous spreading.

VI. CONCLUSIONS

Combining experimental and numerical approaches, we have explained the mechanism underlying large-bubble entrapment during drop impact by a vortex ring that pulls the interface below the pool surface. This pulling occurs earlier for oblate drops, leading to the self-destruction of the vortex. In contrast, prolate drops produce a weaker vortex that can separate from the interface during the early dynamics and develop a vortical flow below the pool surface. As the drop enters the pool and produces a cavity, the interface is pulled by the vortex, leading to the entrainment of the large bubble.

By turning off gravity in the numerical simulations, we also show that hydrostatic pressure plays no role in large-bubble entrapment. Such bubble entrapment is observed for large drops impacting at low velocities, relevant for the impact of secondary drops breaking from Worthington jets [6,60,61], and wave breaking phenomena [20,21,62–67]. It has, therefore, important environmental implications [22,68], but it is also relevant in industry, where it can be beneficial for liquid aeration and gas-liquid chemical reactors [69], and to enhance nucleate boiling [70].

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[1] L. Esmailizadeh and R. Mesler, J. Colloid Interface Sci. 110, 561 (1986).
[2] A. Prosperetti, L. A. Crum, and H. C. Pumphrey, J. Geophys. Res. 94, 3255 (1989).
[3] H. N. Oguz and A. Prosperetti, J. Fluid Mech. 203, 149 (1989).
[4] H. N. Oguz and A. Prosperetti, J. Fluid Mech. 219, 143 (1990).
[5] A. Prosperetti and H. N. Oguz, Annu. Rev. Fluid Mech. 25, 577 (1993).
[6] M. Rein, Fluid Dyn. Res. 12, 61 (1993).
