Short-term VHE variability in blazars: PKS 2155-304

F.M. Rieger¹ 2 and F. Volpe¹

¹ Max-Planck-Institut für Kernphysik, Saupfercheckweg 1, 69117 Heidelberg, Germany; e-mail: frank.rieger@mpi-hd.mpg.de
² European Associated Laboratory for Gamma-Ray Astronomy, jointly supported by CNRS and MPG

Received 02/2010; accepted 07/2010

ABSTRACT

Context. The γ-ray blazar PKS 2155-304 has attracted considerable attention because of its extreme TeV variability characteristics during an exceptional flaring period in 2006. Among the observed key findings are (i) a minimum variability timescale as short as ~ 200 sec and (ii) highly variable TeV emission, which in the frequency interval [10⁻⁴ Hz, 10⁻² Hz] can be described by a log-normal distribution and suggests an underlying multiplicative (and not additive) process.

Aims. Simultaneously accounting for these findings appears difficult within conventional approaches. Following earlier suggestions for the TeV blazar Mkn 501 (Rieger & Mannheim 2003), we explore a possible scenario where PKS 2155-304 is supposed to harbor a supermassive binary black hole system and where the observed TeV variability is dominated by emission from the less massive black hole.

Methods. We analyze the constraints on the very high energy (VHE) source imposed by the observed variability characteristics and the integrated VHE luminosity output, and discuss its implications for a binary black hole system.

Results. We show that for a secondary mass of \( m_{BH} \sim 10^7 M_{\odot} \), fluctuations in the disk accretion rate that feed the jet could account for the observed red-noise type variability process down to frequencies of ~ 10⁻² Hz. Jet curvature induced by orbital motion, on the other hand, could further relax constraints on the intrinsic jet speeds.

Conclusions. Because a binary system can lead to different (yet not independent) periodicities in different energy bands, a longterm (quasi-) periodicity analysis could offer important insights into the real nature of the central engine of PKS 2155-304.

Key words. galaxies: active – galaxies: jets – radiation mechanism: non-thermal – gamma rays: theory – individual: PKS 2155-304

1. Introduction

Active Galactic Nuclei (AGNs) show significant variability over a large range of timescales. Usually, a variety of information can be extracted from the data with statistical methods based on Fourier techniques. In the X-ray domain, for example, variability in accreting compact objects has commonly been described by means of power spectral densities (PSD), characterizing the amount of variability power \( P(\omega) \) as a function of temporal frequencies \( \omega \), or timescales \( 1/\omega \) (e.g., van der Klis 1997). For (Seyfert) AGNs the resultant PSDs quite often appear to follow power laws \( P(\omega) \propto \omega^{-\beta} \), which on long timescales (small frequencies) are approximately described by \( \beta \) close to 1 (flicker noise), but break to a steeper slope (≥ 2) on timescales shorter than a break timescale \( \tau_B \). Active Galactic Nuclei thus vary more strongly towards lower frequencies (longer timescales). Recent studies have shown that the X-ray PSDs of AGNs can be qualitatively similar to the high state of black hole X-ray binary systems (e.g., McHardy et al. 2004, 2006). Based on these and other similarities, AGNs have sometimes been interpreted as scaled-up Galactic black hole systems.

In the very-high-energy (VHE) domain, the experimental situation is usually much less favorable. However, one object where it became recently possible to employ similar analysis techniques is the TeV blazar PKS 2155-304 (\( \gamma = 0.116 \)). Usually detected only with a low VHE flux of ~ 10% of the Crab nebula, PKS 2155-304 underwent a dramatic outburst in July 2006, with VHE flux levels varying between 1 and 15 Crab units, allowing an unprecedented variability analysis (Aharonian et al. 2007; Abramowski et al. 2010; Degrange et al. 2008). The Fourier analysis of its VHE light curve of, e.g., MJD 53944 indicates a red (Brownian) noise-type VHE PSD with an exponent close to 2 within the frequency range [10⁻⁴ Hz, 10⁻² Hz] (Aharonian et al. 2007). Similar results have been obtained in X-rays (1.5-10 keV) with BeppoSAX in 1996 and 1997 (Zhang et al. 1999). Moreover, similar to findings in the X-ray domain (Zhang et al. 1999, 2005), where linear relations between (absolute) rms variability amplitude and (mean) X-ray flux have been previously reported, a significant rms-flux correlation has been observed in the VHE data set (Degrange et al. 2008). This is known to be characteristic of a non-linear, log-normal stochastic process where the relevant, normally distributed variable is the logarithm of the flux log(\( X \)), and not just the flux itself (see Uttley et al. 2005 for a general treatment, and Superina et al. 2008 for application to PKS 2155). A log-normal distribution can be thought of as the result of many multiplicative random effects, whereas additive effects would give rise to a normal (Gaussian) distribution. Indeed, if the variability would be caused merely by an additive stochastic process, the fluxes would be normally distributed and no linear rms-flux relation would be expected, because all Fourier coefficients would be statistically independent. Therefore, the finding that the variations on short timescales (determining the rms) decrease in amplitude when the long timescale variations (determining the mean flux) decrease, indicates that the process driving the variations is a multiplicative process (as in a cascade) and not just an additive one (e.g., shot-noise), nor one resulting from independent variations in many separate regions (Uttley et al. 2005; McHardy 2008).

Send offprint requests to: F.M. Rieger
In accreting galactic black hole (BH) systems these variations have been frequently related to small, independent fluctuations in the accretion rate, occurring on local viscous timescale \( t_{\text{vis}}(r) \) over a range of disk radii \( r \) that are large compared to the inner radius of the disk (Lyubarskii 1997; King et al. 2004; Arevalo & Uttley 2006). If not damped, these fluctuations can propagate inwards and couple together in a way to produce the multiplicative characteristics noted above. Any emission process linked to the tidal inner region (e.g., as X-ray production or jet launching site) may then eventually be modulated over a frequency interval ranging from the inverse accretion time near the outer to the one at the innermost disk radius, respectively. While this scenario sounds very attractive (cf. also Giebels & Degrange 2009 for BL Lac), a generalization to a supermassive source like PKS 2155-304 seems challenging given the detected VHE minimum variability (doubling) timescale of \( t_v \sim 200 \) sec. As we show below, a consistent approach along this line may require the presence of a putative binary BH system in PKS 2155-304 (cf. Rieger & Mannheim 2003). It is this conjecture which we wish to explore here in more detail.

2. The origin of variability in PKS 2155-304

According to the VHE variability analysis for July 2006, there are two major findings which need explanation: (i) First, the extreme short-term variability on a timescale as low as \( t_v \sim 200 \) sec (in the observer’s frame\(^1\)) and (ii) secondly, the log-normal distribution of fluxes, which points to an underlying, multiplicative process. Consider the first finding (i):

If the luminosity of the host galaxy of PKS 2155-304 is indeed as high as reported, i.e., \( M(R) \approx -24.4 \) mag (Kotilainen et al. 1998), its central BH mass is (even if one takes the scatter in the \( M_{\text{BH}} - L_{\text{bulge}} \) relation into account) expected to exceed (McLure & Dunlop 2002)

\[
M_t \geq 2 \times 10^8 M_\odot. \tag{1}
\]

Accounting for the observed rapid variations based on conventional assumptions has thus proved challenging (see, e.g., Levinson 2007 and Begelman et al. 2008 for detailed discussions): In the galaxy’s rest frame, the characteristic scale of any disturbance produced by the central engine cannot be smaller than its minimum size \( r_g \), so that the minimum variability timescale for temporal fluctuations of the ejected fluid is \( r_g t_v / c \), where \( r_g = GM/c^2 \) is the gravitational radius (Levinson 2008). Only if parts of the jet flow would collide with a small external disturbance, e.g. a cloud, may smaller variability times get imprinted. Yet, in this case the bulk power that can be tapped for producing radiation will be correspondingly smaller, and the noted PSD shape and lognormal flux distribution may still be in need of explanation. If the observed minimum variability would indeed reflect the size of the central engine, \( t_v \sim (1 + z) r_g / c \), the allowed maximum BH mass would be almost one order of magnitude smaller than the one inferred from the host galaxy luminosity relation, i.e.,

\[
M_e \lesssim 4 \times 10^7 \left( \frac{t_v}{200 \text{ sec}} \right) M_\odot. \tag{2}
\]

Similar results are obtained if the variability is taken to be produced by the collision of shells moving at different speeds (as in classical internal shock scenarios). In all these cases, the inferred minimum source size (in the rest frame of the galaxy) becomes independent of any Doppler or Lorentz factor\(^2\) Interestingly, similar small BH masses \( M_e \lesssim 3 \times 10^7 M_\odot \) for PKS 2155-304 have been previously inferred based on its X-ray variability properties (Hayashida et al. 1998; Czerny et al. 2001). Moreover, Lachowicz et al. (2009) have recently suggested that the detection of a possible ~ 4.6 h X-ray quasi-periodic oscillation (QPO) with XMM-Newton in 2006 might be related to a hot spot orbiting in the disk close to the innermost stable orbit. If this interpretation is correct, is would imply a firm upper limit on the BH mass of \( 3 \times 10^6 M_\odot \) (Schwarzschild) and \( 2.1 \times 10^7 M_\odot \) (extreme Kerr), respectively.

One obvious possibility to reconcile these apparently divergent central mass estimates is related to the putative presence of a close binary BH system where the jet that dominates the high-energy emission originates from the less massive (secondary) BH. In such a case, host galaxy observations may only be indicative of the total (primary and secondary) BH mass, whereas high-energy observations could actually reveal signatures of the less massive BH. We note that the possible presence of close binary BH systems in blazar-type AGN sources has been repeatedly invoked to account for a variety of observational findings, most notably for the detection of mid-and long-term quasi-periodic variability (e.g., see Rieger 2007 for a review).

If the observed VHE output in PKS 2155-305 were dominated by emission from the secondary BH, however, its mass cannot be supposed to be too small if one also wishes to account for the required jet power. Suppose that the maximum possible jet power is constrained by the Eddington accretion limit \( L_E \sim 10^{46} (M_{\text{BH}}/10^7 M_\odot) \) erg/s. The maximum spin power, for example, which can be extracted from the rotational energy of a BH (via a Blandford-Znajek-type process) is on the order of \( L_s \sim 10^{44} (M_{\text{BH}}/10^7 M_\odot)^2 \left( B_{\text{BH}}/10^8 \right)^2 \) erg/s. With an Eddington equipartition magnetic field strength \( B_{\text{BH}} \sim 1/ \sqrt{M_{\text{BH}}} \), the extractable spin power thus becomes comparable to \( L_E \), i.e., \( L_s \sim L_E / 3 \). The average VHE gamma-ray flux detected by H.E.S.S. implies an isotropic VHE luminosity \( L_{\text{iso}} \sim (5 - 10) \times 10^{46} \) erg/s (Aharonian et al. 2007). If the radiation is produced within two, oppositely directed, conical jets of an opening angle \( \theta \sim 0.1 \) rad, the required (minimum) jet power would be \( L_j \sim (1 - 2) \times 10^{42} (\theta/0.1)^2 \) erg/s. For a BH accreting at close to the Eddington limit (see below) or with maximal spin power, the required minimum mass thus becomes

\[
M_t \sim 10^7 M_\odot \left( \frac{\theta}{0.1} \right)^2, \tag{3}
\]

which would be consistent with the variability constraints (Eq.\(^2\)) and be suggestive of a binary mass ratio \( m_2/m_1 \approx M_{\text{BH}}/M_t > 0.01 \).

In reality, the variability constraint of Eq.\(^2\) is probably too optimistic, in particular if one wishes to account for the second finding (ii) (i.e., the log-normal VHE flux distribution) based on fluctuations in the accretion flow that feeds the jet. Consider again the fluctuating disk model (Lyubarskii 1997), where fluctuations of the disk parameters at some radius, which occur on local viscous timescale, can lead to variations in the accretion rate at smaller radii that are of the flicker- or red-noise type. Then the relevant timescale to be employed is the viscous timescale \( t_{\text{vis}} \) close to the inner radius of the disk, and not the dynamical...
timescale $r_g/c$. In terms of the $\alpha$ parameter and the disk scale height to radius ratio $(h/r)$, this timescale can be expressed as

$$t_{\text{visc}} = \frac{1}{\alpha} \left( \frac{r}{h} \right)^2 \left( \frac{r}{r_g} \right)^{3/2} \frac{r_g}{c},$$

where $\alpha$ is the viscosity coefficient. Consequently, the inner disk needs to be sufficiently thick and viscous $(h/r)^2 \alpha \geq 0.1$ in order to minimize the variability timescale without violating the luminosity constraint eq. (3). Similar conditions seem to be required to account for the X-ray spectral-timing properties of both AGNs and BH X-ray binaries (Arevalo & Uttley 2006). Suppose therefore that in its innermost parts the disk is geometrically thick (as, e.g., for an ADAF). Within a more global scenario, one may then naturally expect a transition to a standard cooling-dominated (geometrically-thin) disk to occur at some radius $r_g$. These transition regions are known to be prone to dynamical instabilities (e.g., Gracia et al. 2003). Interestingly, on longer timescales the X-ray (RXTE) PSD of PKS 2155-304 seems to show a characteristic rollover-timescale of $t_r \sim 1$ day (Kataoka et al. 2001). If this is indicative of the location of the transition region, i.e., $t_{\text{visc}}(r_g) \sim t_r$, a reasonable transition radius $r_g \sim 50 r_g$ might be inferred (note that for ADAFs $(h/r) \sim 1$ throughout). In order to account for the observed VHE variability characteristics, suppose therefore that fluctuations in the disk accretion rate on timescales as short as $t_r$ are efficiently transmitted to the jet, leading to red noise-type fluctuations in the injection rate for Fermi-type particle acceleration. Obviously we will only be able to observe emission with red noise-characteristics if these signatures do not get blurred by processes occurring on a longer timescale within the source: For an observer, flux changes will always appear to be convolved and thus dominated by the longest timescales (Salvati et al. 1998), i.e.,

$$\Delta t_{\text{obs}} = \max\{t_r, \Delta t_r, \Delta t_{\text{rad}}\},$$

where $t_r$, $\Delta t_r$, and $\Delta t_{\text{rad}} \geq t_{\text{acc}}$ are the timescales (as seen by an observer) for injection, for photons traveling across the radial width of the source, and for the relevant radiative processes, respectively. For the radial travel time across the source one has

$$\Delta r \approx \frac{r}{\Gamma b c},$$

where $\Gamma b \geq 10$ denotes the characteristic bulk Lorentz factor and $r$ the radial source dimension in the rest frame of the galaxy (note that length contraction only affects the dimension along the direction of motion). Typical bulk Lorentz factors inferred for the VHE emission region(s) in PKS 2155-305 during the 2006 high state are in the range of $\Gamma b \sim (30 - 50)$ and perhaps even higher (e.g., Begelman et al. 2008). For the model to be consistent, one thus requires a radial source dimension that satisfies $r < 2 \times 10^{14} t_r/200 \text{sec}(\Gamma b/30) \text{cm}$. Either the VHE region is thus located very close to the BH, or the jet exhibits an internal velocity stratification of the (fast) spine - (slow) sheartype where the VHE emission is e.g. produced by Compton up-scattering within a fast moving spine, similar to the needle-in-jet model recently proposed (Ghisellini & Tavecchio 2008).

Consider next the radiative timescale and assume synchrotron losses to dominate the high-energy branch of the energetic particle distribution $n_e(\gamma')$ that is responsible for the up-scattering of soft photons to the VHE regime. The radiative timescale thus is

$$\Delta t_{\text{rad}} \approx 40 \left( \frac{5 \times 10^5}{\gamma'} \right) \left( \frac{1 \text{ G}}{B'} \right)^2 \left( \frac{40}{\Gamma b} \right) \text{sec}.$$

Hence, in order to work successfully, the proposed scenario requires co-moving magnetic field strengths that are sufficiently high $(B' \sim 1 \text{ G})$ and electrons responsible for up-scattering that are sufficiently energetic $(\gamma' \geq 10^3)$. These parameters are again consistent with recent model fits to the observed spectral energy distribution of PKS 2155-304 within the needle-in-jet framework (Ghisellini & Tavecchio 2008). Obviously, extreme short-term variability may for these (and other) reasons not necessarily show up at lower energies. As a consequence: If synchrotron radiation from the fast "needle" component would dominate the emission in the optical domain, then the detectable minimum variability timescales are expected to be correspondingly longer, e.g., on the order of a few to several tens of minutes for the above noted parameters. This might be compared with the minimum variability timescale of ~ 15 min during an optical observational campaign on PKS 2155-304 in 1995 (Paltani et al. 1997).

3. Possible implications of a binary BH model

Following the above analysis, let us suppose that PKS 2155-304 harbors a close binary system consisting of a primary BH with mass $m_1 \sim 5 \times 10^8 M_\odot$ and a secondary one with mass $m_2 \sim 10^7 M_\odot$ (mass ratio $q \sim 0.02$). Evidence for a possible long-term period of $(4 - 7) \text{ yr}$ in the optical V band (Fan & Lin 2000; cf. also Brinkmann et al. 2000 for soft-X-ray hints) might possibly fit well into such a framework: If one requires the secondary to be on an orbit that could intercept the accretion disk around the primary with a typical (maximum) disk size of $10^5 x r_g$, with $x \sim 1$ and $r_g = 2 Gm_1/c^2$ (Goodman 2003), possible Keplerian periods $P_k = 2\pi/\Omega k$ are constrained to be smaller than $P_k \approx 45 (1 + q)^{-1/2} x^{3/2} (m_1/5 \times 10^8 M_\odot) \text{yr}$, a condition that seems well satisfied for PKS 2155-304. This suggests that binary disk interactions could indeed result in optical QPOs on the timescale of several years (see Rieger 2007 for more details). Accordingly, we may derive an upper limit on the intrinsic Keplerian orbital period of the binary

$$P_k \leq \frac{2}{(1 + q)} \frac{P_{\text{obs}}^{\text{opt}}}{7 \text{ yr}} \approx 13 \frac{P_{\text{obs}}^{\text{opt}}}{7 \text{ yr}} \text{ yr},$$

by assuming that the observed optical longterm periodicity is caused by the secondary crossing the disk around the primary twice per orbital period, a situation expected to occur during the initial stage of interaction. In reality, however, this may not be fully appropriate because an alignment of the binary’s orbital and primary’s disk plane typically occurs on comparatively short timescales (e.g., Ivanov et al. 1999). One may thus expect quasi-coplanar orbits, with the binary possibly surrounded by a circumbinary disk, to be much more common. Yet, granted that to be the case, periodically modulated mass transfer across the gap (see below) could still lead to QPOs in the standard disk-dominated infrared-optical regime. Most circumbinary disk simulations suggest that the accretion rate is pulsed over one orbital period, although occasionally two peaks per period are found (e.g., Artyomowicz & Lubow 1996; Bate & Bonnell 1997; Kley 1999; Hayasaki et al. 2007). This indicates that Eq. (8) still provides us with a reasonable constraint on the maximum intrinsic orbital period. If so, then the residual lifetime $t_r$ of the system due to emission of gravitational waves (assuming a quasi-circular orbit) would be in the range $t_r \propto P_k^{2/3} \sim (3 \times 10^{10} - 8 \times 10^{10}) \text{ yr}$. The current separation of the putative binary, on the other hand, would be on the order of

$$d \approx 6 \times 10^{16} \left( \frac{P_k}{13 \text{ yr}} \right)^{2/3} \left( \frac{m_1}{5 \times 10^8 M_\odot} \right)^{1/3} \text{cm} \sim (200 - 400) r_g.$$
Once the secondary becomes embedded in the outer disk around the primary, it starts clearing up an annular gap of a radial size \( \Delta r \sim (h/d) d a^{-0.4} \) in the disk as soon as the timescale for gap-opening via tidal torques becomes smaller than the timescale on which diffusion can refill it (Papaloizou & Lin 1984). It was initially thought that this would cut off the binary BHs from any mass supply (accretion) of the circumbinary disk. However, numerical simulations show that even with significant mass, gap can be supplied to the central binary through tidal, time-dependent gas streams that penetrate the disk gap, periodically approaching and preferentially feeding the secondary (see references above). Accordingly, for non-vanishing binary eccentricity, QPOs with period equal to the orbital one may arise due to a time-modulated accretion rate. The simulations indicate in particular that a reversal of mass accretion rates can occur (i.e., \( m_2 > m_1 \)) despite \( m_2 < m_1 \), acting towards equal-mass binaries and suggesting that the secondary may become more luminous than the primary. If that is the case, then applying variability constraints based on observed emission properties can lead to a spurious identification of the secondary mass with the (total) central BH mass. As suggested above, this may help to explain some of the discrepancies in black mass estimates based on high-energy emission models and host-galaxy observations.

Suppose that the size \( r_g \) of the disk around the secondary is comparable to the Roche lobe radius (Eggleton 1983) or the Toomre stability radius (whichever is smaller). For \( m_2 \sim 10^2 M_\odot \) and \( r_g \sim 10^2 r_g \), the viscous timescale at the outer radius \( t_{\text{visc}}(r_g) \sim 50 (0.1/\alpha)(r/r_g)^{1/2} / \nu \) yr (standard disk) then most likely exceeds the orbital period \( P_1 \sim 10 \) yr. Any modulation of the mass supply to the outer disk at the orbital period may thus be damped by the viscosity of the disk, i.e., as the next pulse comes before the former was able to propagate in, the amplitude of variability becomes small as a result of summation of the pulses (Zdziarski et al. 2009). A significant modulation of the jet power (emerging from the innermost part of the disk) solely owing to a periodically changing mass supply (at the outer disk radius) may therefore not become apparent. On the other hand, if variability in the disk occurs on thermal timescale for \( t \sim (r/r_g)^{1/2} r_g / c \), optical (V band) disk variability on orbital timescale might be possible. While a periodically changing mass supply may thus not necessarily lead to significant periodicities in the jet emission, geometrical effects due to the orbital motion could introduce them: if the jet launched is wrapped by a sufficiently strong magnetic field, for example, its overall path can become curved due to the orbital motion of the jet-emitting BH (leading to non-ballistic-type helical motion). Then the constraints on the required minimum bulk Lorentz factors of the outflow (\( \Gamma_{\text{obs}} \), perpendicular to the disk plane) might be somewhat relaxed because the effective Doppler factor will be time-dependent, \( \Gamma(t) \), with the strongest boosting effects occurring whenever the (changing) angle to the line of sight becomes smallest (cf. Rieger 2004). This is illustrated in Fig. 1 for a bulk Lorentz factor \( \Gamma \) in the rest frame of the secondary) of 20 and an inclination \( \theta \) (defined as the angle between the line of sight and the z-axis, in a frame where the orbital plane is in the x-y plane) between \( 2^\circ \) and \( 4^\circ \). Obviously, considerable changes in the effective Doppler factor could occur, which would further influence the detectability of high- and low-level (intrinsically) active source stages, i.e., even if the intrinsic flux would change only moderately, an order of magnitude difference in measured VHE fluxes may become possible. Moreover, the motion of components along curved trajectories could possibly also account for the observed super-quadratic correlation between the X-ray and VHE flux (Costamante 2008; Katarzynski & Walczewska 2010). Of course, this might only be expected as long as the lateral width of the jet remains smaller than the separation distance of the binary, so that the effects caused by orbital motion will not be smeared out. For an expanding jet, this obviously limits the distance up to which extreme Doppler effects may occur. This might partly explain why on larger (radio VLBA) scales, only modest Doppler boosting seems to be present (e.g., Piner & Edwards 2004). Clearly, an accurate identification of active VHE source stages in PKS 2155-304 could help to further assess the influence of differential (geometrical) Doppler effects.

4. Conclusions

The observed, extreme VHE variability characteristics of PKS 2155-304 provide strong constraints on the physical parameters of its engine. We have suggested that similar to Mkn 501 (Rieger & Mannheim 2003), the putative presence of a close supermassive binary BH system could allow (i) to reconcile central mass estimates based on host galaxy observations (indicative of the total primary and secondary mass) with those based on VHE y-ray variability (possibly only indicative of the jet-emitting secondary), (ii) to account for the observed log-normal variability characteristics via accretion disk fluctuations, and (iii) to relax constraints on the jet flow velocity. Obviously, an increased instrumental sensitivity in the TeV domain (by, e.g., a CTA-type instrument) that may allow us to search for even faster variability and, complementary, an advanced QPO analysis in the optical (e.g., Hudec & Basta 2008) could thus be particularly useful to further assess the possibility of a binary scenario for PKS 2155-304. If corroborated by further observations, the analogy to X-ray binary systems might be closer than initially anticipated.

Acknowledgements. Discussions with Felix Aharonian, Amir Levinson and Berrie Giebels are gratefully acknowledged.

References

Abramowski, A. et al. (H.E.S.S. Collaboration) 2010, A&A in press, arXiv:1005.3702
Aharonian, F.A., Khangulyan, D., & Costamante, L. 2008, MNRAS 387, 1206
Aharonian, F. et al. (H.E.S.S. Collaboration) 2007, ApJ 664, L71
Arevalo, P., & Utrile, P. 2006, MNRAS 367, 801

Fig. 1. Time-dependence of the Doppler factor for motion along an idealized orbital-driven helical jet path. Chosen parameters are: \( \Gamma_{\text{obs}} = 20, i = 2^\circ \), \( P_1 \sim 13 \) yr (thick solid line), and \( \Gamma_{\text{obs}} = 20, i = 4^\circ \), \( P_1 \sim 4 \) yr (thick dashed line). Also shown is the time-dependence of the angle \( \theta(t) \), the actual angle of the emission region to the line of sight (in degree, multiplied by a factor 10) for \( \Gamma_{\text{obs}} = 20, i = 2^\circ \) and \( P_1 \sim 13 \) yr.
Artyomowicz, P. & Lubow, S.H. 1996, ApJ, 467, L77
Bate, M.R., & Bonnell, I.A. 1997, MNRAS 285, 33
Begelman, M.C., Fabian, A.C., & Rees, M.J. 2008, MNRAS 384, L19
Brinkmann, W. et al. 2000, A&A 362, 105
Costamante, L. 2008, JMPD 17, 1449
Czerny, B. et al. 2001, MNRAS 325, 865
Degrange, B. et al. 2008, PoS(BLAZARS2008), 16
Eggleton, P.P. 1983, ApJ 268, 368
Fan, J.H., & Lin, R.G. 2000, A&A 355, 880
Ghisellini, G., & Tavecchio, F. 2008, MNARS 386, L28
Giebels, B. & Degrange, B. 2009, A&A 503, 797
Goodman, J. 2003, MNRAS 339, 937
Gracia, J. et al. 2003, MNRAS 344, 468
Hayasaki, K., Mineshige, S., & Sudou, H. 2007, PASJ 59, 427
Hayashida, K. et al. 1998, ApJ 500, 642
Hudec, R. & Basta, M. 2008, PoS (Blazars2008), 76
Ivanov, P.B., Papaloizou, J.C.B., & Polnarev, A.G. 1999, MNRAS 307, 79
Kataoka, J. et al. 2001, ApJ 560, 659
Katarzynski, K., & Walczewska, K. 2010, A&A 510, 63
King, A.R. et al. 2004, MNRAS 348, 111
Kley, W. 1999 MNRAS, 303, 696
Khis, M. van der 1997, in: Statistical Challenges in Modern Astronomy II, eds. G.J. Babu and E.D. Feigelson (Berlin: Springer), p.321
Kotilainen, J.K. et al. 1998, A&A 336, 479
Lachowicz P. et al. 2009, A&A 506, L17
Lyubarski, Y.E. 1997, MNRAS 292, 679
Levinson, A. 2007, ApJ 671, 129
Levinson, A. 2008, PoS(BLAZARS2008), 02
McHardy, I.M. et al. 2004, MNRAS 348, 783
McHardy, I. 2008 PoS(BLAZARS2008), 14
McHardy, I.M. et al. 2006, Nature 444, 730
McLure, R.J., & J.S. Dunlop, J.S. 2002, MNRAS 331, 795
Pallini, S. et al. 1997, A&A 327, 539
Papaloizou, J., & Lin, D.N.C. 1984, ApJ, 285, 818
Piner, B.G., & Edwards, P.G., 2004, ApJ 600, 115
Rieger, F.M., & Mannheim, K. 2003, A&A 397, 121
Rieger, F.M. 2004, ApJ 615, L5
Rieger, F.M. 2007, Ap&SS 309, 271
Salvati, M. et al. 1998, ApJ 495, L19
Superina, G., & Degrange, B. 2008, AIPC 1085 (eds. Aharonian, Hofmann, Rieger), 494
Tagliaferri, G. et al. 1991, ApJ 380, 78
Uttley, P. et al. 2005, MNRAS 359, 345
Zdziarski, A.A., Kawabata, R., & Mineshige, S. 2009, MNRAS 399, 1633
Zhang, Y.H. et al. 1999, ApJ 527, 719
Zhang, Y.H. et al. 2005, ApJ 629, 686