Dual D-Brane Actions on $AdS_5 \times S^5$

Jaemo Park$^a$ and Soo-Jong Rey$^b$

School of Natural Sciences, Institute for Advanced Study
Olden Lane, Princeton NJ 08540 USA$^a$

Physics Department & Center for Theoretical Physics
Seoul National University, Seoul 151-742 KOREA$^b$

jaemo@sns.ias.edu, sjrey@gravity.snu.ac.kr

abstract

Utilizing coset superspace approach, dual actions of super D1- and D3-branes on $AdS_5 \times S^5$ are constructed by carrying out duality transformation of world-volume $U(1)$ gauge field. Resulting world-volume actions are shown to possess expected $SL(2, \mathbb{Z})$ properties. Crucial ingredient for deriving $SL(2, \mathbb{Z})$ transformation property of the D-brane actions is covariance of $SU(2, 2|4)$ coset superspace algebra under $SO(2)$ rotation between two ten-dimensional Type IIB Majorana-Weyl spinors.

---

$^1$ Work supported in part by the U.S. Department of Energy under Grant No. DE-FG02-90-ER40542, KOSEF Interdisciplinary Research Grant and SRC-Program, Ministry of Education Grant BSRI 97-2418, SNU Faculty Research Grant, and The Korea Foundation for Advanced Studies Faculty Fellowship.
1 Introduction

Recently, motivated by the Maldacena’s conjecture on AdS/CFT correspondence, closed forms of $\kappa$-symmetric superstring and D3-brane actions have been constructed using the coset superspace approach [1, 2]. The formal superspace expression of the superstring or D-brane actions on Type-IIB supergravity backgrounds have been constructed previously by various authors [3, 4, 5]. However, using the coset superspace approach, it has become possible to obtain an explicit form of the action in terms of the coordinate fields $(x, \theta)$. This development is quite exciting since, for example, it now opens up a possibility for solving large-$N$ limit of $\mathcal{N} = 4$ super-Yang Mills theory exactly.

As is now well-known, Type IIB string theory possesses $SL(2, \mathbb{Z})$-duality symmetry [6], which is believed to hold not only for flat spacetime but also for any classical background. Hence, it would be of some interest to check whether the D-brane actions on $AdS^5 \times S^5$ has indeed the right transformation property under the $SL(2, \mathbb{Z})$-duality. In particular, on the $AdS^5 \times S^5$ background, the D3-brane action should be self-dual under $SL(2, \mathbb{Z})$, and the actions for D1- and D5-branes should form a multiplet of $SL(2, \mathbb{Z})$.

In this paper, we prove explicitly the expected $SL(2, \mathbb{Z})$ transformation properties of the D1- and D3-brane actions on $AdS_5 \times S^5$, at least in the semi-classical limit. The formal expression of $AdS_5 \times S^5$ D3-brane action obtained in [1] is quite similar to the action in flat spacetime [7]. This then suggests that the proof of the $SL(2, \mathbb{Z})$ duality symmetry ought to be similar to that for the flat spacetime case [8]. An important ingredient in the proof of the $SL(2, \mathbb{Z})$ symmetry in the flat spacetime has been that the $S$-generator of the $SL(2, \mathbb{Z})$ corresponding to $\tau \to -\frac{1}{\tau}$ acts as a finite $SO(2)$ rotation in the space of the two fermionic coordinates [8, 9]. We show that the same continues to be true on $AdS_5 \times S^5$ background. In fact, the $\mathcal{N} = 2$ Type IIB supersymmetry algebra from which the Mauer-Cartan equations are derived is covariant under the $SO(2)$ rotation. Stated differently, if a set of the two supercharges, $Q_1$ and $Q_2$, is related to an another set, $Q'_1$ and $Q'_2$, by a $SO(2)$ rotation, then the $\mathcal{N} = 2$ supersymmetry algebra turns out to retain the same form when expressed in either set of the supercharges.

In section 2, we recapitulate relevant part of the construction [1] of D3-brane action on $AdS_5 \times S^5$. We then prove the self-duality of the action under $SL(2, \mathbb{Z})$ by performing the duality transformation on the world-volume fields as well as the background fields. The proof is in fact almost the same as that for the flat space case [8]. In section 3, we proceed to the D1-brane and construct the action on $AdS_5 \times S^5$. We then show that the action is, as expected,
As our work is being finished, we have received related works [12]. In [12], gauge fixing of the \( \kappa \)-symmetry was indispensible for showing the \( SL(2, \mathbb{Z}) \) symmetry. Our proof is based only on the covariance of the \( SU(2, 2|4) \) superalgebra under the \( SO(2) \)-rotation and hence proves the \( SL(2, \mathbb{Z}) \) duality symmetry without any gauge fixing.

2 \( SL(2, \mathbb{Z}) \) Invariance of The D3-brane on \( AdS_5 \times S^5 \)

The superstring or the D3-brane action can be constructed using the \( SU(2, 2|4) \) superalgebra. If we consider the coset superspace \( \frac{SU(2, 2|4)}{SO(1,4) \times SO(5)} \), the even part is \( \frac{SO(2,4)}{SO(1,4) \otimes SO(5)} \approx AdS^5 \otimes S^5 \). The corresponding algebra is described in \( SO(1,4) \times SO(5) \) basis, as shown in [1]. The even generators are two pairs of translation and rotation, \( (P_a, J_{ab}) \) for \( AdS_5 \) and \( (P'_a, J'_{ab}) \) for \( S^5 \) and the odd generator are the two 10-d Majorana-Weyl spinors \( \bar{Q}_{\alpha \alpha'} \). Let \( \gamma_a \) and \( \gamma'_a \) be the \( 4 \times 4 \) matrices generating the \( SO(1,4) \) and \( SO(5) \) Clifford algebra with the signature \( \gamma^{(a,b)} = (-++++) \) and \( \gamma^{(a',b')} = (+++++) \). The 10-dimensional \( 32 \times 32 \) Dirac matrices \( \bar{\Gamma} \) of \( SO(1,9) \) are represented as

\[
\bar{\Gamma}^a = \gamma^a \otimes I \otimes \tau_1, \quad \bar{\Gamma}^{a'} = I \otimes \gamma^{a'} \otimes \tau_2
\]

where \( I \) is the \( 4 \times 4 \) unit matrix and \( \tau_i \) are the Pauli matrices. In [1], the diagonal Majorana condition is chosen

\[
\bar{Q}_{\alpha \alpha}' \equiv (Q^{\beta \beta'}_{\alpha})^\dagger (\gamma^{\beta \beta'})_{\alpha} \delta^{\beta \beta'}_{\alpha} = -Q^{\beta \beta'}_{\alpha} C_{\beta \alpha} C'_{\beta' \alpha'}
\]

where \( C = (C_{\alpha \beta}) \) and \( C' = (C'_{\alpha' \beta'}) \) are the charge conjugation matrix of the \( SO(4,1) \) and \( SO(5) \) Clifford algebra. The part of the supersymmetry algebra containing the spinors is

\[
\begin{align*}
[Q_I, P_a] &= -\frac{i}{2} \varepsilon_{IJ} Q_J \gamma_a \\
[Q_I, P'_a] &= \frac{1}{2} \varepsilon_{IJ} Q_J \gamma'_a \\
[Q_I, J_{ab}] &= -\frac{1}{2} Q_I \gamma_{ab} \\
[Q_I, J'_{a'b'}] &= -\frac{1}{2} Q_I \gamma'_{a'b'}
\end{align*}
\]

\[
\{Q_{\alpha \alpha'}, Q_{\beta \beta'}\} = \delta_{IJ}(-2i C_{\alpha' \beta'} (C \gamma^a)_{\alpha \beta} P_a + 2C_{\alpha \beta} (C' \gamma^{a'}_{\alpha' \beta'}) P'_{a'}) + \varepsilon_{IJ} (C_{\alpha' \beta'} (C \gamma^{ab})_{\alpha \beta J_{ab}} - C_{\alpha \beta} (C' \gamma^{a'b'})_{\alpha' \beta'} J'_{a'b'}). \tag{3}
\]
Note that the diagonal Majorana condition is preserved under the $SO(2)$ rotation between $Q_1$ and $Q_2$. And one can easily check that the $SU(2,2|4)$ superalgebra is covariant under the $SO(2)$ rotation, as $\delta_{ij}$ and $\varepsilon_{ij}$ are invariant under $SO(2)$.

The left invariant Cartan 1-forms $L^A = dX^M L_M^A$, $X^M = (x, \theta)$ are given by

$$G^{-1}dG = L^AT_A = L_a P^a + L_{a'} P^{a'} + \frac{1}{2} L_{ab} J_{ab} + \frac{1}{2} L_{a'b'} J_{a'b'} + L^{\alpha'I} Q_{\alpha'i}$$  \hspace{1cm} (4)$$

where $G = G(x, \theta)$ is a coset representative in $SU(2, 2|4)$, $L^a$, $L^{a'}$ are the 5-beins, $L^{\alpha'I}$ are two spinor 16-beins and $L^{ab}, L^{a'b'}$ are the Cartan connection.

The D3-brane action presented in [1] is

$$S = -\int d^4\sigma \sqrt{-\det (G_{ij} + e^{-\frac{2}{3}F} F_{ij} - b_{ij})} + \int (C_4 + C_2 \wedge (e^{-\frac{2}{3}F} - b_2) + \frac{1}{2} C_0 F \wedge F) . \hspace{1cm} (5)$$

Here we have $G_{ij} = L_i^a L_j^b = \partial_i X^M L^a_M \partial_j X^N L^b_N$, where $\hat{a} = (a, a')$ run through the $SO(1, 4)$ and $SO(5)$ indices and $L^a(X(\sigma)) = d\sigma^i L_i^a$. Also $b_2 \equiv \frac{1}{2} b_{ij} d\sigma^i d\sigma^j$ and $db_2 = i\mathcal{L}_{\tau_3} \mathcal{L} L$ with $\mathcal{L}_i = L_i^a \Gamma^a$. Finally $C_4$ and $C_2$ are determined by the condition

$$H \equiv d(C_4 + C_2 \wedge (e^{-\frac{2}{3}F} - b_2)) = \frac{i}{6} \mathcal{L}_{\tau_3} \tau_1 L + i\mathcal{L}_{\tau_1} (e^{-\frac{2}{3}F} - b_2) \mathcal{L} L + \frac{1}{30} (\varepsilon^{a_1\ldots a_5} L^{a_1} \wedge \ldots \wedge L^{a_5} + \varepsilon^{a_1'\ldots a_5'} L^{a_1'} \wedge \ldots \wedge L^{a_5'}) . \hspace{1cm} (6)$$

From this condition one obtains the following useful identity:

$$dC_4 - C_2 \wedge db_2 = \frac{i}{6} \mathcal{L}_{\tau_3} \tau_1 \mathcal{L}^3 L + \frac{1}{30} (\varepsilon^{a_1\ldots a_5} L^{a_1} \wedge \ldots \wedge L^{a_5} + \varepsilon^{a_1'\ldots a_5'} L^{a_1'} \wedge \ldots \wedge L^{a_5'}) . \hspace{1cm} (7)$$

In Eq. (5), for later convenience, we have written down the dilaton dependence in the Einstein frame of the $AdS_5 \times S^5$ background. In fact, the string and Einstein frames are equivalent for D3-brane, since the dilaton takes a constant value on $AdS_5 \times S^5$. The $C_0$ term in Eq. (5) is absent in [1], but it is a total derivative term (or boundary term) that can be added to the action without changing the classical equations of motion. The inclusion of the constant $C_0$ is consistent since the dilaton remains constant in the $AdS^5 \times S^5$ background. In fact, a constant shift of $C_0$ is a trivial classical symmetry of the action. Inclusion of the $C_0$ term, however, is quite crucial for the proof since the $SO(2)$ duality symmetry is promoted to the full $SL(2, \mathbb{R})$ symmetry in the presence of both dilaton and $C_0$ field background.

Adding a Lagrange multiplier term $\int d^4\sigma \frac{1}{2} \tilde{H}^{ij} [F_{ij} - (\partial_i A_j - \partial_j A_i)]$ to the action Eq. (5), the $A_i$ equation of motion can be solved by $\tilde{H}^{ij} = \varepsilon^{ijkl} \partial_k B_l$. The duality transformation is essentially the same as in the flat case [8] and the resulting action is

\footnote{Our convention is that whenever an integral without $d^n\sigma$, it is an integral of a differential form.}
\[ S_D = -\int d^4\sigma \sqrt{-\text{det} \left( G_{ij} + \frac{1}{\sqrt{1 + e^{2\phi}C_0^2}}(\epsilon^i_\tau \tilde{F}_{ij} + C_{ij} + e^\phi C_0 b_{ij}) \right)} + \int \Omega_D, \quad (8) \]

where

\[
\Omega_D = C_1 - b_2 \wedge C_2 - \frac{1}{2} e^\phi C_0 b_2 \wedge b_2 \wedge \left( e^\phi \tilde{F} + C_2 + e^\phi C_0 b_2 \right)
- \frac{e^\phi C_0}{2(1 + e^{2\phi}C_0^2)} \left( e^\phi \tilde{F} + C_2 + e^\phi C_0 b_2 \right) \wedge \left( e^\phi \tilde{F} + C_2 + e^\phi C_0 b_2 \right) \quad (9)\]

where \( \tilde{F} = dB \). If we define rotated \( SO(2) \) Pauli matrices

\[
\tau'_1 \equiv -\left( \tau_3 + e^\phi C_0 \tau_1 \right) / \sqrt{1 + e^{2\phi}C_0^2} \\
\tau'_3 \equiv +\left( \tau_1 - e^\phi C_0 \tau_3 \right) / \sqrt{1 + e^{2\phi}C_0^2} \quad (10)\]

and using Eq. (7) and the identity \( \tau_3 \tau_1 = \tau'_3 \tau'_1 \), we were able to show that

\[
d\Omega_D = \frac{i}{6} \hat{L} \hat{L}^3 \tau'_3 \tau'_1 L + i \hat{L} \tau'_1 \left( \frac{e^\phi}{\sqrt{1 + e^{2\phi}C_0^2}} \tilde{F} - b'_2 \right) \hat{L} L + \frac{1}{30} (e^{a_1 \cdots a_5} L^{a_1} \wedge \cdots \wedge L^{a_5} + e^{a_1' \cdots a_5'} L^{a_1'} \wedge \cdots \wedge L^{a_5'}). \quad (11)\]

Thus the dual action can be written as

\[
S = -\int d^4\sigma \sqrt{-\text{det} \left( G_{ij} + \frac{e^\phi}{\sqrt{1 + e^{2\phi}C_0^2}} \tilde{F}_{ij} - b'_i \right)} + \int \left\{ C'_4 + C'_2 \wedge \left( \frac{e^\phi}{\sqrt{1 + e^{2\phi}C_0^2}} \tilde{F} - b'_2 \right) - \frac{e^2\phi C_0}{2(1 + e^{2\phi}C_0^2)} \tilde{F} \wedge \tilde{F} \right\}. \quad (12)\]

where the tensor fields \( C'_4, C'_2 \) and \( b'_2 \) are the same as \( C_4, C_2 \) and \( b_2 \) but with \( SO(2) \) rotated Pauli matrices in the corresponding expression. The resulting action still has the \( \kappa \)-symmetry since the Mauer-Cartan equation and Fierz identity used in the derivation of the \( \kappa \)-symmetry are covariant under the \( SO(2) \) rotation.

Also, we can check the transformation of the dilaton and the axion under the duality transformation. From the coefficient of \( \tilde{F} \) in the Born–Infeld part of Eq. (12), we obtain the transformation

\[
e^{-\phi} \quad \rightarrow \quad + \frac{e^\phi}{1 + e^{2\phi}C_0^2} = \frac{1}{e^\phi + e^{-\phi}C_0^2}. \quad (13)\]

From the coefficient of \( \tilde{F} \wedge \tilde{F} \), we also have

\[
C_0 \quad \rightarrow \quad - \frac{e^{2\phi} C_0}{1 + e^{2\phi}C_0^2} = - \frac{e^\phi C_0}{e^{-\phi} + e^\phi C_0^2}. \quad (14)\]
Combining this transformation with the symmetry under a constant shift of $C_0$, at the classical level, one deduces that the D3-brane action has $SL(2, \mathbb{R})$ symmetry. Once semi-classical quantum effects on the D3-brane world-volume are taken into account, one finds that magnetic monopoles should be introduced as ends of the D-strings. In this case, the constant shift of $C_0$ is replaced by a quantized shift, much as in QCD. Thus, the $U(1)$ gauge group is compact, and the surviving symmetry group of quantum Type IIB string theory is $SL(2, \mathbb{Z})$.

3 $SL(2, \mathbb{Z})$ Covariance of The D1-brane on $AdS_5 \times S^5$

We now turn to the D1-brane on $AdS_5 \times S^5$. The action of the D1-brane with $\kappa$-symmetry is given by

$$S = -\int d^2\sigma e^{-\phi}\sqrt{-\det(G_{ij} + F_{ij} - b_{ij})} + \int e^{-\phi}C_2. \quad (15)$$

where $C_2$ is determined by $dC_2 = i\bar{\theta}\tau_1\hat{L}L$. We were able to check explicitly, using Mauer-Cartan equation and Fierz identity, that $dC_2$ is closed. Alternatively, we can make a $SO(2)$ rotation mapping $\tau_1$ to $\tau_3$. The resulting 3-form is the standard closed 3-form appearing in the superstring action [2]. In Eq. (15), we have expressed the dilaton dependence in the string frame. The $\kappa$-symmetry transformation is given by

$$\delta_\kappa x = 0, \quad \delta_\kappa \theta = \kappa, \quad (16)$$

where the $\kappa$-parameter satisfies

$$\Gamma\kappa = \kappa, \quad \Gamma^2 = 1 \quad (17)$$

and the matrix $\Gamma$ is given by

$$\Gamma = \frac{\epsilon^{i_1i_2}}{\sqrt{-\det(G_{ij} + F_{ij} - b_{ij})}} \left(\frac{\tau_1}{2}\hat{L}_{i_1}\hat{L}_{i_2} + \frac{i\tau_2}{2}(F_{i_1i_2} - b_{2i_1i_2})\right). \quad (18)$$

The corresponding variation of $G_{ij}$ and $F_{ij} - b_{ij}$ is given by

$$\delta_\kappa G_{ij} = -2i\delta_\kappa \theta(\hat{L}_iL_j + \hat{L}_jL_i) \quad (19)$$

$$\delta_\kappa (F - b_2) = +2i\delta_\kappa \theta\hat{L}_3L. \quad (20)$$

One can also add a total derivative term

$$e^{-\phi}C_2 \rightarrow e^{-\phi}C_2 - C_0F, \quad (21)$$

where $C_0$ is a constant “axion” background field. Since $C_0F$ is a total derivative, it does not affect the classical equations of motion. As in the previous section, a constant shift of $C_0$ is a
trivial classical symmetry of the action Eq. (13). At quantum level, the symmetry is reduced to a discrete shift symmetry, $T$-symmetry of $SL(2, \mathbb{Z})$.

Now we perform the duality transformation. We first introduce a Lagrange multiplier field $\tilde{H}^{ij} = -\tilde{H}^{ji}$ as follows:

$$S' = \int d^2 \sigma \left( -e^{-\phi} \sqrt{-\det (G_{ij} + F_{ij} - b_{ij})} + \frac{1}{2} \tilde{H}^{ij} (F_{ij} - 2 \partial_i A_j) + \frac{1}{2} e^{-\phi} \tilde{e}^{ij} C_{ij} - \frac{1}{2} C_0 \tilde{e}^{ij} F_{ij} \right)$$

(22)

and regard the field-strength $F_{ij}$ to be an independent field. Varying the action with respect to $A_j$ yields

$$\partial_i \tilde{H}^{ij} = 0,$$

which implies that $\tilde{H}^{ij} = \tilde{\epsilon}^{ij} \Lambda$ with $\Lambda$ constant. If we use the equation of motion for $F$ to rewrite the action in terms of $\Lambda$ instead of $F$, the total action can be written as

$$S_D = \sqrt{e^{-2\phi} + (\Lambda - C_0)^2} \int d^2 \sigma \left( -\sqrt{-\det G_{ij}} - \frac{1}{2} \tilde{\epsilon}^{ij} b_{ij} \right)$$

(23)

where $db = iL \tau_3' \hat{L} L$ and $\tau_3'$ is defined to be

$$e^{-\phi} \tau_1 - (\Lambda - C_0) \tau_3 \equiv \sqrt{(e^{-2\phi} + (\Lambda - C_0)^2)} \tau_3'$$

(24)

The action Eq. (23) is the $\kappa$-symmetric superstring action in the Nambu-Goto form with the modified tension

$$T' = \sqrt{e^{-2\phi} + (\Lambda - C_0)^2}.$$  

(25)

The $\kappa$-transformation is given by Eqs. (16), (17), (19), but now $\Gamma$ is given by

$$\Gamma = \frac{\epsilon^{i_1 i_2}}{\sqrt{-\det (G_{ij})}} \left( \frac{1}{2} \tau_3 \hat{L}_{i_1} \hat{L}_{i_2} \right).$$

(26)

This result admits the same interpretation as in the flat space. The expression Eq. (23) can be interpreted as the tension for the $SL(2, \mathbb{Z})$ covarainat spectrum of strings provided that one identifies the integer value $\Lambda = m$ as corresponding to the $SL(2, \mathbb{Z})$ dyonic string of charge $(m, 1)$ in the $AdS_5 \times S^5$ background with constant dilaton $\phi$ and axion $C_0$. An equivalent interpretation is that Eq. (23) describes the fundamental $(1, 0)$ string with an $SL(2, \mathbb{Z})$ transformed metric, dilaton and axion. The relevant $SL(2, \mathbb{Z})$ transformations maps $C_0 + ie^{-\phi}$ to $-(C_0 - \Lambda + ie^{-\phi})^{-1}$. Thus the coupling constant of the fundamental string after the duality transformation is given by $e^{\tilde{\phi}} = e^{-\phi} + e^{\phi} (\Lambda - C_0)^2$.

4 Discussion

In this paper, using coset superspace approach, we have investigated the $SL(2, \mathbb{Z})$ duality property of the D1- and D3-brane actions on $AdS_5 \times S^5$ background. We have proven that the
D1-and D3-branes behave as in the expected way under the $SL(2, \mathbb{Z})$ transformation. Moreover, we have shown that the actual dual transformation is formally the same as in the flat space. In both cases, the $SL(2, \mathbb{Z})$ acts on the fermionic coordinates in the same way, viz, as the $SO(2)$ rotation. In particular, with the dilaton and axion field background turned on, we have shown that the full $SL(2, \mathbb{Z})$ duality symmetry follows from the $SO(2)$ duality rotation. Throughout this paper, our discussion has been mainly semi-classical. It would be interesting to extend our proof to the full-fledged quantum level.

S.J.R. thanks Institute for Advanced Study and Aspen Center for Physics for hospitality, where part of this work was carried out.
References

[1] R.R. Metsaev and A.A. Tseytlin, *Supersymmetric D3 brane action in AdS$^5 \times S^5$*, hep-th/9806095.

[2] R.R. Metsaev and A.A. Tseytlin, *Type IIB superstring action in AdS$^5 \times S^5$ background*, hep-th/9805028.

[3] M. Grisaru, P. Howe, L. Mezincescu, B. Nilsson and P. Townsend, Phys. Lett. B162 (1985) 116.

[4] M. Cederwall, A. von Gussich, B.E.W. Nilsson, and A. Westerberg, Nucl. Phys. B490 (1997) 163 hep-th/9610148; Nucl. Phys. B490 (1997) 179 hep-th/9611159.

[5] E. Bergshoeff and P.K. Townsend, Nucl. Phys. B490 (1997) 145 hep-th/9611173.

[6] J. H. Schwarz, Phys. Lett. B360 (1995) 13 (Erratum) B364 (1995) 252 hep-th/9508143; Phys. Lett. B367 (1996) 97, hep-th/9510086.

[7] M. Aganagic, C. Popescu, and J.H. Schwarz, Phys. Lett. 393B (1997) 311 hep-th/9610249; Nucl. Phys. B495 (1997) 99 hep-th/9612080.

[8] M. Aganagic, J. Park, C. Popescu and J. H. Schwarz, Nucl. Phys. B496 (1997) 215, hep-th/9702133.

[9] Y. Igarashi, K. Itoh and K. Kamimura, *Self-Duality in Super D3-Brane Action*, hep-th9806161.

[10] M. Cederwall and A. Westerberg, J. High Energy Phys. 2 (1998) 4 hep-th/9710007.

[11] M. Cederwall and P. Townsend, J. High Energy Phys. 9 (1997) 3 hep-th/9709002.

[12] I. Oda, *Super D-string Action on AdS$^5 \times S^5$*, hep-th/9809076; *SL(2,Z) Self-duality of Super D3-Brane Action on AdS$^5 \times S^5$*, hep-th/9810024.