On Possibilities of Studying of Supernova Neutrinos at BAKSAN

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We consider the possibilities of studying a supernova collapse neutrino burst at Baksan Neutrino Observatory (Institute for Nuclear Research, Russian Academy of Sciences) using the proposed 5-kt target-mass liquid scintillation spectrometer. Attention is given to the influence of mixing angle \( \theta_{13} \) on the expected rates and spectra of neutrino events.

Introduction

Neutrino fluxes of natural origin are known to carry information both about their sources inaccessible to direct observation and about the properties of the neutrino themselves.

We consider a program of research on natural low-energy (< 100 MeV) antineutrino fluxes using a large scintillation spectrometer to be installed at Baksan Neutrino Observatory (BNO) of the Institute for Nuclear Research, Russian Academy of Sciences, at a depth of \( \sim 5000 \text{ m.w.e.} \) The planned spectrometer target mass is about 5 kt.

The main research directions and goals are the following:

1. Neutrino geophysics. Determining the radiogenic component of the Earth’s heat flow through the detection of antineutrinos emitted by daughter uranium and thorium decay products; detemining the total abundance of these elements in the Earth.

2. Testing the hypothesis that a chain fission reaction is burning at the Earth’s centre (“georeactor”).

1. Neutrino Astrophysics. Studying the Supernova (SN) explosion dynamics by recording the neutrino burst intensity and energy spectrum. Searching for an isotropic flux of antineutrinos accumulated in the Universe over several billion years during SN explosions and the formation of neutron stars and black holes.

The first section of the research program has been schematically considered in recent publications [1-4]. This paper is devoted to the possibilities of studying the neutrino burst when cores of high-mass stars gravitationally collapse to produce SNe.

The burst of “Thermal” neutrinos begins simultaneously with gravitational collapse of the iron core of a high-mass \( (M \geq 8M_\odot) \) star and lasts for about 20 s. All six types of active neutrinos are produced in a hot core: \( \nu_e, \bar{\nu_e}, \nu_\mu, \bar{\nu_\mu}, \nu_\tau \) and \( \bar{\nu_\tau} \). These neutrinos carry away the vast bulk of the gravitational energy, \( \sim 3 \times 10^{53} \text{ erg} \), released during the collapse. Only several tens of minutes or several hours later does the explosion reach the surface, and a Supernova seen with the naked eye and by the methods of optical, X-ray, radio and gamma-ray astronomy flares up in the sky. On competition of the explosion, the bulk of the stellar matter is dispersed in space and a neutron star (or a black hole) is left at the place of the core.

By neutrino burst onset, the inner part of the core becomes opaque to neutrinos because of its high density. Before their escape, the neutrinos are multiply scattered, absorbed and remitted. The surface from which the neutrinos can leave the core is called a neutrinosphere. Because of the difference in interaction cross sections, the neutrinosphere radii differ for different types neutrinos. The \( \nu_\mu, \bar{\nu_\mu}, \nu_\tau \) and \( \bar{\nu_\tau} \) neutrinospheres (radius \( \sim 30 \text{ km} \)) are deepest, the \( \nu_e \) neutrinosphere (\( \sim 50 \text{ km} \)) follows next, and the latter is followed by the \( \nu_\tau \) neutrinosphere (\( \sim 70 \text{ km} \)). This explains the predicted difference in mean energies of the neutrinos escaping from the core. The larger the radius, the lower the mean energy. However, as calculations show, all types of neutrinos divide the collapse energy carried away by them approximately evenly.

A short pulse (\( \sim 10^{-2} \text{ s} \)) of electron neutrinos, \( \nu_e \), produced via neutronization of the core that reached the stability (Chandrasekhar) limit is emitted immediately before the “thermal” pulse. These \( \nu_e \)’s with energies 15-20 MeV, carry away 5-10% of the energy released during the collapse.

Studying the neutrino bursts in laboratories is a powerful tool for investigating the energetics and dynamics of collapsing stars and the properties of neutrinos themselves.

The existence of a neutrino burst that accompanies collapse was first pointed out in 1965 [5]. Intensive calculations of the SN explosion dynamics and neutrino emission were performed in succeeding years [6-9]. There are a number of detailed reviews (see [10, 11] and references therein). A neutrino burst detection method was also suggested in 1965 [12]: a statistically significant series of signals must be observed in a massive low-background neutrino detector.
However a SN explosion is a very rare event (one SN explosion in ~30 years is expected in our Galaxy). Therefore, the authors of [12] suggested synchronizing the operation of various detectors to increase reliability and information content. In our days there exists The International SuperNova Early Warning System (SNEWS) that combines all of the detectors capable of detecting SN neutrinos is currently operating.

The neutrinos produced during collapse play an important role in nucleosynthesis [15-17]. The observed abundances of several light elements ($^9$Be, $^{11}$B, $^{19}$F, and others), and the abundances of so-called bypassed elementes heavier than iron, can be explained in terms of neutrino reactions within $\sim$1000 km of the stellar core centre.

The signal from SN 1987A in the Large Magellanic Cloud was recorded on February 23, 1987, with three neutrino detectors - KII in Japan, IMB in the USA and the Baksan detector. This signal was analyzed in details in a number of papers (see, e.g. [18, 19]). A total of 24 neutrinos were recorded in the above detectors (the explosion occurred at a distance of 50 kpc, which a factor 5 larger than the mean distance from the Earth to the stars of our Galaxy). On the whole, the picture obtained is consistent with the outlined neutrino burst scenario, although poor statistics severely limits the information content of the analysis.

Note that SN neutrino burst detection is an oscillation experiment with a baseline of $\sim$30 thousand light years and that the neutrinos produced in the star traverse regions that are a factor of $\sim$ 10$^9$ denser than the matter the solar center. The flavour composition of neutrinos incident on the detector depends on the mixing parameter $\sin^2 \theta_{13}$ and on the type of mass hierarchy (normal or inversed) [20, 21]. The conversions $\nu_\mu, \bar{\nu}_\tau \Rightarrow \bar{\nu}_e$, open the possibility of studying the intensities and energies of $\bar{\nu}_\mu$ and $\nu_\tau$, whose signal is virtually impossible to isolate directly by currently available methods.

Below, we (1) schematically describe the neutrino detector, (2) give the characteristics of a “standard” thermal neutrino burst, (3) calculate the spectra and rates of expected neutrino events in the detector, (4) consider the effects of oscillations on the number and spectrum of neutrino events and, (5), in conclusion, discuss our results.

\section*{I. NEUTRINO DETECTOR}

The planned detector will consist of three concentric zones. The central spherical zone about 23 m in diameter is filled with a liquid organic scintillator and serves as a target for neutrinos. The target is separated from the second zone filled with a nonscintillating oil by a strong transparent film. Photomultiplier tubes (PMTs) are installed on the surface of the second zone and view the target through a 4-meter layer of liquid. The outer zone of the detector is an anticoincidence zone. It is separated from second zone by an opaque metall structure filled with water (or oil) and is viewed by PMTs that record Cerenkov radiation from cosmic muons and showers. The outer size of the detector is $\sim$33 m.

The PMT photocathodes viewing the target cover about 25\% of the surface. The expected signal is 80-100 photoelectrons per 1 MeV.

The main difference between the detector under consideration and the already existing LVD [21] and SNO [22] detectors, which are capable of detecting a neutrino burst, is a larger target mass, a good energy resolution, a low detection threshold, and the ability to detect “terrestrial” antineutrinos. The detector under construction is closest in structure to the KamLAND array [23], differing from it by a larger target mass and a deeper position underground. The recently suggested LENA project [24] has a program similar to ours, but it supposes constructing a detector with much larger target mass.

The main (in time) mode of operation of the spectrometer is a set of statistics of events generated by terrestrial antineutrinos produced via $^{238}$U and $^{232}$Th decays and by the hypothetical georeactor [1-4]. The number of useful events of this type is $\sim$500 per year. In the mode of neutrino burst detection, the expected number of events can reach several thousand over a period of $\sim$20 s.

\section*{II. THE THERMAL NEUTRINO BURST}

We calculate the expected effects in the detector based on the quantitative characteristics of the neutrino burst given below.

(1) Thermal neutrinos carry away an energy of $3 \times 10^{53}$ erg, which is divided evenly between the six flavours: $\nu_e, \bar{\nu}_e, \nu_\mu, \bar{\nu}_\mu, \nu_\tau$ and $\bar{\nu}_\tau$.

(2) The neutrino energy distribution is described by Fermi-Dirac distribution with an additional factor that provides a faster falloff of the spectrum at high neutrino energies:

\[ N(E)dE = \frac{C \cdot E^2 dE}{1 + e^{E/T} e^{-\alpha(E/T)^2}}, \]  

(1)
where $C$ is the normalization constant, $E$ and $T$ — are the energy and temperature (in MeV) and $\alpha \ll 1$ is a dimensionless parameter.

The numerical values of the quantities that characterize spectrum (1) were taken from [7] (see Table I).

The last two lines in Table I give the mean neutrino energies of neutrino calculated from distribution (1) and the burst-time-integrated flux densities of various types of neutrinos on the detector. The distance from the collapsing star to the detector was assumed to be 10 kpc (remind that 1 pc $\approx 3.086 \times 10^{18}$ cm).

The spectra of the neutrinos incident on the detector are shown in figure 1. Note a peculiarity of our model that is important for subsequent analysis: the $\nu_x$ neutrinos = $(\nu_\mu, \bar{\nu}_\mu, \nu_\tau, \bar{\nu}_\tau)$ have an appreciably harder spectrum than $\nu_e$ and $\bar{\nu}_e$.

III. NEUTRINO REACTIONS IN THE DETECTOR

In this section we consider the effects expected in the detector without neutrino oscillations. (see the second line in Table II). We assume that the useful target volume contains $4 \times 10^{32}$ hydrogen atoms, $2 \times 10^{32}$ $^{12}$C atoms, and $16 \times 10^{32}$ electrons.

3.1. The inverse beta-decay reaction in which a free proton converts into a neutron and positron,
TABLE II: Effects of oscillations on the numbers of neutrino events (normal mass hierarchy)

| Reaction                                      | without oscillation | LMA MSW $\sin^2 \theta_{13} > 10^{-3}$ | LMA MSW $\sin^2 \theta_{13} < 10^{-5}$ |
|-----------------------------------------------|---------------------|----------------------------------------|----------------------------------------|
| $\bar{\nu}_e + p \to n + e^+$                | 1157                | 1479                                   | 1479                                   |
| $\bar{\nu}_e + ^{12}\text{C} \to ^{12}\text{B} + e^+$ | 14.4                | 35.5                                   | 35.5                                   |
| $\nu_e + ^{12}\text{C} \to ^{12}\text{N} + e$  | 5.8                 | 132                                    | 93.5                                   |
| $\sum \text{CC on } ^{12}\text{C}$             | 20.2                | 167                                    | 129                                    |
| $\sum (\nu_e, ^{12}\text{C}) \to ^{12}\text{C} + 15.1 \gamma$ | 236                | 236                                    | 236                                    |
| $\sum (\nu_e, e) \to (\nu_e, e)$               | 70.6                | 62.2                                   | 61.4                                   |

\begin{equation}
\nu_e + p \to n + e^+. \tag{2}
\end{equation}

has the largest cross section. The $\bar{\nu}_e$ threshold is 1.806 MeV. Light signals correlated in time and space are recorded in the detector from the positron and from the $\gamma$-ray photons of the capture of the neutron from reaction (2) by scintillator hydrogen. The mean neutron lifetime before the capture is $\sim 200$ $\mu$s. The energy released by the positron in the scintillator $E_{\text{vis}}$ (MeV), is related to the energy of the incoming $\bar{\nu}_e$ by:

\begin{equation}
E_{\text{vis}} = E_{\nu} - R_n - 0.78, \tag{2a}
\end{equation}

where $R_n$ is the neutron recoil energy. The energy averaged over the positron escape angles, $R_n$, increases quadratically with incoming neutrino energy and reaches $\sim 2$ MeV at $E_{\nu} = 50$ MeV. When calculating the cross sections and spectra, we used results from [25]. A total of about 1200 events of the reaction under consideration is expected over the burst.

3.2. The reactions of electron antineutrino and neutrino interaction with carbon in the channels of charged currents,

\begin{equation}
\nu_e + ^{12}\text{C} \to ^{12}\text{B} + e^+(E_{\text{th}} = 13.9 \text{ MeV}); \tag{3}
\end{equation}

\begin{equation}
^{12}\text{B} \to ^{12}\text{C} + e^- (T_{1/2} = 20.2 \text{ ms}), \tag{3a}
\end{equation}

\begin{equation}
\nu_e + ^{12}\text{C} \to ^{12}\text{N} + e^- (E_{\text{th}} = 17.8 \text{ MeV}); \tag{3a}
\end{equation}

\begin{equation}
^{12}\text{N} \to ^{12}\text{C} + e^+ (T_{1/2} = 11 \text{ ms}), \tag{3b}
\end{equation}

produce $^{12}\text{B}$ and $^{12}\text{N}$, which decay with the emission of an electron and positron, respectively. Spatially correlated delayed coincidences and energies escaping charged leptons are recorded in the detector. Because of high reaction thresholds, the number of events is very small (Table II). Their cross sections for reactions (3 and 3a) were found in [26] and are presented in Figure 2.

Neutrinos also can be scattered inelastically by $^{12}\text{C},$

\begin{equation}
\nu_e + ^{12}\text{C} \to ^{12}\text{C} + \gamma, E_{\gamma} = 15.1 \text{ MeV}, \tag{3b}
\end{equation}

to produce a monochromatic line of isolated photons recorded by the detector. Because of low energies, the total contribution from $\nu_e$ and $\bar{\nu}_e$ to their total number does not exceed 5% and the hard $\nu_x$ neutrinos play a dominant role.

3.3. About 70 isolated recoil electrons are expected from the $(\nu, e)$ scattering reaction. The cross sections for these processes are presented in figure 3.

IV. NEUTRINO AFTER OSCILLATIONS

4.1. The oscillations of the neutrinos produced in a stellar core on their way to the detector were considered in detail in [20].
FIG. 2: Cross sections for interactions of neutrinos with $^{12}\text{C}$ in the channels of neutral and charge currents.

FIG. 3: Cross sections of neutrino interaction on electron.

Because of the $\bar{\nu}_e \Leftrightarrow \bar{\nu}_\mu, \bar{\nu}_\tau$, and $\nu_e \Leftrightarrow \nu_\mu, \nu_\tau$ transitions the intensities and spectra of the neutrinos reaching the detector change noticeably compared to the initial ones given in table I, which were used to obtain the results of the previous section in this paper. The probabilities of these oscillation transitions depend on several factors.

(1) On the amplitudes $U_{e1}, U_{e2}$ and $U_{e3}$, with which mass states $m_1, m_2, m_3$ enter into the superposition of $\bar{\nu}_e$ and $\nu_e$ flavour states. In recent years, it has been established (see e.g. [27, 28]), that large mixing angle (LMA) case occurs in Nature. In the subsequent we assume that

$$\tan^2\theta_{12} = |U_{e2}/U_{e1}|^2 = 0.40,$$

(4)
$|U_{e1}|^2 = 0.7, \quad |U_{e2}|^2 = 0.3$

The small, but important quantity $|U_{e3}|^2 \equiv \sin^2 \theta_{13}$ remains uncertain. The following experimental constraint was obtained for it:

$$|U_{e3}|^2 \equiv \sin^2 \theta_{13} \leq 0.03 \text{ (CHOOZ \ [29])} \quad (4a)$$

2. On the influence of stellar matter influence and on the presence and nature of resonances (adiabatic, non-adiabatic) in the stellar matter with a variable density (the Mikheev-Smirnov-Wolfenstein, (MSW) effect).

3. On the type of mass hierarchy (normal, $m_3^2 >> m_1^2$, or inverted $m_3^2 << m_1^2$). For normal and inverted mass hierarchies, respectively, $\nu_e$ and $\bar{\nu}_e$ undergo the resonant conversions.

Below, we will consider normal mass hierarchy, making one exclusion that clearly demonstrates the role of type of mass hierarchy. For brevity, we will disregard the influence of the Earth’s matter on the neutrino way to the detector.

4.2. Let us now consider the changes in the observed picture of events to which the oscillations $\bar{\nu}_e \leftrightarrow \nu_\mu, \nu_\tau$ lead. The spectrum of $\nu_e$ neutrinos incident on the detector, $d^{osc}N_{\bar{\nu}_e}/dE_{\bar{\nu}_e}$, is given relation

$$\frac{d^{osc}N_{\bar{\nu}_e}}{dE_{\bar{\nu}_e}} = |U_{e1}|^2 \frac{dN_{\nu_\mu}}{dE_{\nu_\mu}} + |U_{e2}|^2 \frac{dN_{\nu_\tau}}{dE_{\nu_\tau}} + |U_{e3}|^2 \frac{dN_{\nu_e}}{dE_{\nu_e}} \quad (5)$$

i.e.,

$$\frac{d^{osc}N_{\bar{\nu}_e}}{dE_{\bar{\nu}_e}} = |U_{e1}|^2 \frac{dN_{\nu_\mu}}{dE_{\nu_\mu}} + (1 - |U_{e1}|^2) \frac{dN_{\nu_\tau}}{dE_{\nu_\tau}} \approx 0.7 \frac{dN_{\nu_\mu}}{dE_{\nu_\mu}} + 0.3 \frac{dN_{\nu_\tau}}{dE_{\nu_\tau}}$$

Relation (5) implies that 70% of the initial soft $\bar{\nu}_e$’s reach the detector in an unchanged form and 30% of the initial hard $\nu_e$ are added to them in the form of $\bar{\nu}_e$’s. As a result, the number of events of inverse beta-decay reaction (2) increases (see Table II) and a hard component appears in the spectrum of positrons from this reaction (figure 4a). In addition the number of events of the reaction $\nu_e + ^{12}\text{C} \rightarrow ^{12}\text{B} + e^+$ increases by several times. Of course the total number of neutrinos is conserved and 30% of the initial $\nu_e$ turn into $\bar{\nu}_e$.

4.3. In the process $\nu_e \leftrightarrow \nu_\mu, \nu_\tau$, a resonance whose nature depends on the small parameter $|U_{e3}|^2 = \sin^2 \theta_{13}$ is observed in stellar matter.

In $\sin^2 \theta_{13} > 10^{-3}$, then only a negligible fraction of the initial soft $\nu_e$ reaches the detector, in fact, the entire flux of hard $\nu_e$ is determined by the $\nu_e \rightarrow \nu_e$ transition.

$$\frac{d^{osc}N_{\nu_e}}{dE_{\nu_e}} = |U_{e1}|^2 \frac{dN_{\nu_\mu}}{dE_{\nu_\mu}} + (1 - |U_{e1}|^2) \frac{dN_{\nu_\tau}}{dE_{\nu_\tau}} \approx \frac{dN_{\nu_e}}{dE_{\nu_e}} \quad (6)$$

As a result, the number of events of the reaction $\nu_e + ^{12}\text{C} \rightarrow ^{12}\text{N} + e^-$ increases by a factor of $\sim 20$ (Table II). The total number of recoil electrons from neutrino scattering by electrons changes insignificantly.

If, alternatively, $\sin^2 \theta_{13} < 10^{-5}$, then 30% of $\nu_e$ reaches the detector, and 70% of $(1 - |U_{e1}|^2)$ of the initial hard $\nu_e$ turn into $\nu_e$. Thus, for $\sin^2 \theta_{13} > 10^{-3}$, the $\nu_e$ spectrum contains more hard neutrinos than for $\sin^2 \theta_{13} < 10^{-5}$.

4.4. Let us also consider the case of inverted neutrino mass hierarchy, $m_3^2 << m_1^2$. The MSW resonance now occurs during $\bar{\nu}_e \leftrightarrow \bar{\nu}_\mu, \bar{\nu}_\tau$ transitions and depends on $\sin^2 \theta_{13}$.

If $\sin^2 \theta_{13} > 10^{-3}$, then the incident flux $d^{osc}N_{\bar{\nu}_e}/dE_{\bar{\nu}_e}$ is determined almost entirely by the hard $\bar{\nu}_e$ that turned into $\bar{\nu}_e$:

$$\frac{d^{osc}N_{\bar{\nu}_e}}{dE_{\bar{\nu}_e}} \approx \frac{dN_{\nu_e}}{dE_{\nu_e}} \quad (7)$$

As a result, the total number of events of reaction (2) reaches $\sim 2200$ and an intense peak of hard $e^+$ will be observed in the positron spectrum (see figure 4b).

If, alternatively, $\sin^2 \theta_{13} < 10^{-5}$, then the spectrum of $\bar{\nu}_e$ incident on the detector is identical to spectrum (5) that has already been considered above and the positron spectrum does not differ from the shown at figure 4a.

**V. CONCLUSION**

The parameter $|U_{e3}|^2 = \sin^2 \theta_{13}$ plays an important role in the physics of weak interactions. CP-invariance violations in the neutrino sector are possible only if $|U_{e3}|^2 \neq 0$. Ways of improving the experiment limitations on the parameter
FIG. 4: Spectra of the positrons from the inverse beta-decay reaction (2) with oscillations: (a) Spectrum for normal mass hierarchy, (b) spectrum for inverted mass hierarchy, under the condition $\sin^2 \theta_{13} > 10^{-3}$.

and achieving a better sensitivity were suggested immediately after constraint (4b) was obtained on the CHOOZ reactor [30]. At present, preparations are being made for new experiments in the field of the reactors of many countries (see [31] for a brief review). These experiments should be able improve result (4b) by a factor of 5-7. The dependence of the spectrum and number of neutrino events on $\sin^2 \theta_{13}$ (Table II, figure 4) gives hope that this parameter will be determined with a good sensitivity in future astrophysical observations.

Detection of a neutrino burst can give more information than mentioned above.

The processes that take place in the core of a star within the first seconds after its collapse are very complex. It is not surprising that specialists in this field have failed to reach a consensus of opinion on the spectral composition of the emitted neutrinos even after several decades of intensive calculations. Above we used a model ([7], figure 1), in which $\nu_x = \nu_\mu, \bar{\nu}_\mu, \nu_\tau, \bar{\nu}_\tau$ have appreciably higher mean energies than $\nu_e$ and $\bar{\nu}_e$. At the same time, there are studies
TABLE III: Characteristics of the thermal burst neutrino spectrum from various sources

| $< E_{\nu_e} >$, MeV | $< E_{\bar{\nu}_e} >$, MeV | cite | year  |
|---------------------|------------------|-----|------|
| 12.5                | 25.2             | [7] | 1980 |
| 15.4                | 21.6             | [9] | 1998 |
| 11.4                | 14.1             | [32]| 2003 |
| 15.4                | 15.7             | [33]| 2003 |
| $\approx 10 - 12^*$ | $\approx 25$     | [34]| 2005 |

The mean value for $\bar{\nu}_e$ and $\nu_e$ energies are close [32] or almost equal [33], while [34] give data similar to those in [7] (see table III).

What is the dynamics of the core interior temperature within the first seconds after the core collapse? How does the neutrino burst flare up and fade out? How the neutrino gas cools down in the burst time? And, finally, does a rapidly rotating star actually collapses in two stages separated in time, as explained in detail in [35]? Only analysis of a future neutrino burst can give answers to these questions.

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34 D. Nadyozhin, V. Imshennik, astro-ph/0501002
35 V. Imshennik, O. Ryazhskaya, Astron. Lett., 30, 14 (2004); astro-ph/0401613