Dynamic Structure to Define a Corporate Channel for Courier Companies

Daniel Alexander Méndez Rey\textsuperscript{1,}*, Jorge Eduardo Ortiz Triviño\textsuperscript{2}

\textsuperscript{1}Faculty of Engineering National University of Colombia Bogotá, Colombia
\textsuperscript{2}Department of Industrial and Systems Engineering, Faculty of Engineering National University of Colombia Bogotá, Colombia

Abstract The document presents a stochastic linear programming model, providing a network structure to meet corporate clients to courier companies as a strategy of upkeep and increment in revenue. By reviewing the state of art about location models in different outlets in retail businesses over time, we take a courier company to define a location model of retail sales points, based on major revenue customer, the result gives optional strategies for network structure, where the model outputs are validated under changes in demand and network capacity in different scenarios, generating strategic options to be implemented in companies with the same characteristics. The project finds a form to eliminate the subjectivity that exists in the decision-making with location sales points problems in retail services companies.

Keywords Retail, Location and Stochastic Linear Programming

1. Introduction

When a company begins a growth process, where its organizational approach is oriented to attend their customers through a sale’s point network, sell their products and/or services, they’ll come to the following question, what would be the ideal structure of the network, about quantity and location of self-sale’s points and franchises to maintain their clients and generate new revenue?

In present times, this case has taken strength by having companies dedicated to perform consults to define ideal channel strategies for every type of business, under the premise: "Customer Satisfaction", this is an approach that strives to move an entire company to find new customer needs and participate actively in their satisfaction\textsuperscript{[1]}.

However, companies have based their strategies in the search of profit without focusing on what really generates it, the client\textsuperscript{[1]}, from the 60s we can find models that begin the search for the best location for retail points, with the goal of eliminating the subjectivity of decisions of this type, oriented at the discretion who takes it, which have evolved until eliminating this subjectivity.

Within the literature review we can find that this type of analysis is always trying to locate potential market access and penetration characteristics, this practice is being developed in courier companies that establish a network to cover their clients in a national basis, in the particular case of the project, working on a strategy of upkeep and diversification of actual customers, with the goal of maintaining of Pareto customers, where we define the strategies for satisfying them regarding their own retail points, franchises and collection circuits.

The project scope is the definition of how many and where by municipalities should there be new owned sale points, franchises and collection circuits, finding strategies to expand the current network. To this purpose, we select a Pareto customer on which the company sees major revenues and analyses their needs for access to the network, thus generating the target location for the company.

After doing the previous selection of the objective client to study, we proceed to identify his characteristics allowing us to find out where should a courier network be implemented, by taking into account all the possible locations the customer has access to, which are more than 300 municipalities and each one having different office locations on them.

Afterwards we establish the municipalities where the study is to take place; we proceed to find out how is the state of the company’s network on these sites, generating arrays as the model’s parameters. This leads us to defined a lineal programming model with stochastic processes which focus on the client’s demand, allowing us to establish an ideal network structure, focused under the strategic options that the company should pursue in order to guarantee customer satisfaction.

From the model result, we establish the need to generate optional scenarios, defining the strategic options given by...
the company, through three different scenarios, in which we monitor an initial profit (Revenues vs. network cost) on each, giving the necessary tools for the decisions to take.

Lastly, we validate the results, establishing the network’s benefits, that the company will have in other to commercialize their products and services.

2. Companies’ Retail Points Locations

As a fundamental principle for the growth of a company oriented to the generation of revenue, involving a set of strategies allowing the upkeep and development of this through time where most of its revenue is perceived from their sales points, by selling their products or providing a service, the company is forced to analyse where to locate these retail points, guaranteeing their participation in the objective market.

Trough studies done by SBA (Small Business Administration)[2], poor location of retail points could generate problems of capital shortage and eventually trigger a company’s down fall. On the other hand, poor location can be compensated with a good marketing strategy and / or promotions (bargains/deals), which would represent higher expenses for the company affecting the amount of profit it makes.

The decision in where these locations should be situated is mainly motivated by:

- **Start of a new business**: This makes reference to the creation of a new company or a new business line which is in need of having retail points in order to participate in the objective market.
- **Business growth**: We define expansion as the need to be participating of the market, trough the network expansion allowing the increment of revenue and aiming to generate more profit, keeping in mind the possible need to relocate as the behaviour dictates.

3. Sales Points Location Model: State of Art

As we mentioned before, retail companies should focus their efforts to successfully locate their retail points, because it is a vital point as a profitability model for the company. For this propose models have been designed over time trying to ease the decision making on this field, next we’ll present some cases

3.1. Check List Method

This method was first propose be seen Applebaum (1965)[2], who tried to provide a procedure for the information evaluation related with the locations potential. From here, the factor check list is created which is used by the company with the objective to place retail locations according to the strategy option which are a priority in the development or their action plans.

Some categories within in the check lists are: The Company’s strategies, basic economic factors, politics and government, taxes, licenses, environmental laws, commodities, international factors, competences amongst others. However, this type of analysis can become a subjective one as it focuses in the personal preferences of the one making it, slanting the location of the sales points to particular criteria.

3.2. Weighted Location Model

This model consists in the making on the relative evaluation of each factor involved in the decision making of the retail points location, it’s a variation of the check list that gives a mathematical support for the decision making. In general, it evaluates each location for the preselected factor, next we present a brief description of this model[2]:

**Step 1**: Allocation of relative importance to evaluat each factors: (1) Not Important, (2) Important and (3) Very Important. This classification can vary depending on the criteria of the one who applies it.

**Step 2**: Classification of possible places to evaluate, for each of criteria selected in relevance with the numeric qualification, a scale from 1 - n is defined, where 1 is low score until we reach n as highest possible score.

**Step 3**: Score for each analysed location, generated trough the multiplication of step 1 and 2, for each place and criteria establishing a total by location and choosing the site with the highest score.

3.3. LMMD Model

The LMMD model is a weighted location model that was proposed by Richard Davis and Howard Rudd (1983) who used an easy model that can be applied to any retail company through a decision array that involves[2]:

![Figure 1. Decision making process for the location of retail points](image-url)
• Classification of location criteria.
• Weighted criteria with a subjective evaluation by the one making the array.
• Given score under a set scale defined by experts.

The main characteristics of this model are: (1) The use of Delphi appreciation to evaluate the criteria in each location (Experts scoring), (2) The implementation process is short and (3) Advanced mathematics knowledge is not necessary for the execution of the model. This model integrates model A and B which simplify scoring by taking into account Delphi appreciations trying to minimize the subjective level on the decision making.

3.4. Analogic Method

This method was introduced by Cohen (1960) and Applebaum (1960, 1968), it is a subjective approach to evaluate[3]:
• Similar sales points to the one desired to open, with the objective to know how analogous stores attract clients form different areas.
• Form this information we estimate the possible locations for these sales points according to analysis previously made.

This method is frequently use when a company doesn’t have the necessary studies to locate their offices and references the competition establishing as a given that analogous companies make other types of analysis.

3.5. Regression Model

It is a more rigorous model which tries to combined the check list method and the analogous method through a regression model that allows us to determine the factors that affect the profitability of a sales point in a specific location.

There are several investigations about regression for this type of model, however, the profit \( Y = f (L, S, M, P, C) \) is always defined as a lineal function, the \( L \) location, sales points characteristics \( (S) \), market characteristics \( (M) \), prices \( (P) \) and competition \( (C) \)[3].

3.6. Other Locations Models

In general terms, a company that wants to locate sales points needs to answer two main questions: (1) How does the sales points should be located? and (2) How to locate a sales points network from the same company to prevent cannibalization of the market? (Gérard Cliquet 2008)[4].

According to the first question several models have emerged of which we have mentioned some already:
• Check list: Applebaum – 1966, Kane 1966 and Nelson 1958
• The analog method: Applebaum – 1968
• Proximal areal method (Mid-Point): Ghosh and McLafferty 1987
• Polynomials of Thiessen and Dirichlet: Dirichlet 1850 and Thiessen 1911
• Gravity Models: Converse 1949 and Huff 1964
• Interaction Models: Nakanishi and Cooper 1974

As to the second question we can find the next models:
• MULTILOC: Achabal 1982
• P-Media Approach: Weber 1909 and Cooper 1963
• Combination model with MCI (Multiplicative Competitive Interaction): Nakanishi and Cooper 1974
• Qualitative Approach based on administrative criteria: Durvasula 1992
• Multi-objective approach: Pirkil 1987, Current and Storbeck 1963 and Kolly y Evans 1999

4. Present Intake Network

After looking up the different options there are for the attention point’s locations, we can see the structure of the selected company to generate the proposed model, taking as a first step a diagnostic of the present network.

By establishing a contract relationship with corporate clients through a sales force, the client will have to his disposition the needed attention points in order to make their shipments, in this particular case if the client has offices in Bucaramanga, Cúcuta, Barranquilla, Cartagena, Cali, Pasto, Villavicencio, Tunja, Medellín, Manizales, Pereira, Armenia, Ibagué and Bogotá, he will have access to recollection circuits in their work place with a previous set time.

Lastly, if the customer is located in a place without this kind of service, he or she could come to one of the agencies that act as thirds that also cover the functions of intake of packages for corporate clients. The figure 2 clarifies what was mentioned before.

![Figure 2. Present structure of the intake network](image)

In relation to self own points, the company covers 136 municipalities, having 180 attention points for corporate clients. The agents are located in 954 municipalities, for a total of 1,151 agents in the whole country.

5. Inputs Model Information

With the goal to determine the sufficient information for the development of the model, next we will present how the client on which the analysis is done, is selected, in order to determine the usage of the company’s services during the specific year, as well as other information needed for the development of the model.

5.1. Client Selection

For the development of the project is necessary to select a client by whom we would try to improve the access level when it comes to the intake of his shipments on the present
network; for this we took into account the revenue during the
reference year and we selected the client with the major
participation, this client is responsible for 4.53% of the
company’s revenue reflected by 699,441 shipments done.

With the objective to validate the model’s result, we
determined the demand during 3 years, like this: (1) Client’s
growth of 11% - (First year), (2) increment by 30% of the
client’s demand (Second year) and (3) increment by 40% of
the client’s demand (Third year).

5.2. Present Network Cost

The present network cost for the attention of corporate
clients, according to description given before, are established
under the knowledge of the business by the company of the
sector, where it’s defined that from the total network’s cost,
83% corresponds to infrastructure used for corporate clients.

5.3. Creation Cost of New Location or Third Party

The company defines two options for the creation of new
attention points, a self-point or through a third party agent, an
allied network which fulfills with the location of the sales
point and has an administration that assumes the functionalty cost and defines a remuneration system with the
company.

5.4. Client Structure

First we chose a client established since the year 1991,
which has offices, in 377 municipalities throughout the
country and also has 625 different locations in given
municipalities. The models that the courier company applies
must guarantee access to the service offered to the client in
all their locations.

6. Corporative Channel Attention Model

The model is born from the need of expansion of a courier
company that wants to change the strategy of their
corporative channel, based on the increase of revenue, but
focusing on customer satisfaction keeping in mind a Pareto
client, prioritizing present customers making it a growth
strategy on current clients, that would later allow us to obtain
new customers through the structure of the channel.

According to the information gathered for the formulation
of the project, next we will show the lineal programing
model with stochastic processes for the customer demand,
which as a result gives us strategies for the aperture of
locations (own points or third party agents) and
implementation of recollection circuits.

6.1. Model Structure

The objective of this model is to widen the corporative
client’s attention channel through minimizing costs for the
channel, based on strategic options from the company for the
aperture of locations (own points or third party agents) and
implementation of recollection circuits.

Index:

- \( i \): Municipalities where the Pareto client is located
- \( t \): Months of the year when the revision of the stochastic
demand of the Pareto client is done.

Variables:

- \( x_i \): Number of new own attention points in the network
per municipalities \( i \)
- \( w_i \): Number of new third party attention points in the
network per municipalities \( i \)
- \( r_i \): Number of new recollection circuit per municipalities

Parameters:

- \( DM_i \): Demand per municipalities \( i \)
- \( PRM_i \): Attention points of the Pareto client per municipalities
- \( CPP \): Monthly average capacity in present own locations
- \( NMZ \): Number of blocks strategic option of own locations
- \( NMZT \): Number of blocks strategic option of third party
locations
- \( MZ_i \): Number of blocks per municipalities \( i \) where
there are own points
- \( CT \): Opening cost for new own sales point, first month
- \( CA \): Upkeep cost for own sales points, per month
- \( CN \): Opening cost for third party points, first month
- \( CE \): Upkeep cost for third party points, per month
- \( CR \): Average monthly cost for collection circuits
- \( MRM \): Top num ber of collection circuits per municipalities
- \( PP_i \): Number of present own sales points per
municipalities \( i \)
- \( PT_i \): Number of present third party points per
municipalities \( i \)

Mathematical Model:

Objective Function:

Minimize the network cost:

\[
Z = \sum_{i=1}^{n} \left( x_i \cdot CT + y_i \cdot CA + w_i \cdot CN + r_i \cdot CR \right) \quad (1)
\]

Subject to:

Demand: The demand for each point was estimated with
normal stochastic demand processes[6][7] which integrate
the Poisson and Weiner processes, for client office per
municipalities \( i \).

\[
DM_i = \text{Proceso Estocástico} \cdot PRM_i \forall i \quad (2)
\]

Capacity: The network capacity is measured according to
the own sales points, guaranteeing the attention of the Pareto
client on an own network.
\[(PP_t + x_i) + CPP \geq DM_i \quad \forall \ i \quad (3)\]

**Strategic option 1:** Strategic as a priority, the company defined that there must be a minimal of one own sales point by each 64 blocks.

\[(PP_t + x_i) \geq (MZ_i/NMZ) \quad \forall \ i \quad (4)\]

**Strategic option 2:** Additionally, the company sets that there must be a minimal of one new third party sales point every 32 blocks.

\[(w_i + PT_i) \geq (MZ_i/NMZT) \quad \forall \ i \quad (5)\]

**Strategic option 3:** The model must guarantee that in the municipalities where competition attention points exist there must be own sales points and/or third party retail points.

\[(PP_t + x_i + w_i + PT_i) \geq MP_i \quad \forall \ i \quad (6)\]

**Strategic option 4:** Moreover, seeking to satisfy the company customer needs, where office of client exists there must be at least an own sales point and/or third party retail point.

\[r_i \geq MR_i \quad \forall \ i \quad (8)\]

**Strategic option 6:** The company is willing to generate one new collection circuit per select municipalities by the strategic option 5, which limits the municipalities output in the model.

\[r_i \leq MRM_i \quad \forall \ i \quad (9)\]

Characteristics of variables: Not Negativity.

\[x_i \geq 0 \quad \forall \ i \quad (10)\]

\[w_i \geq 0 \quad \forall \ i \quad (11)\]

\[r_i \geq 0 \quad \forall \ i \quad (12)\]

### 6.2. Stochastic Demand Processes

A stochastic process \([5]\) is a family collection of random variables \(\{X_t, \text{con} t \in T\}\), ordered by \(t\) which usually indicates time, where \(X_t\) is a random variable, namely for every moment of \(t\), it has an independent random variable, in other words, we can establish that a stochastic process could be interpreted as a sequence of random variables whose characteristics vary along the index \(t\).

For the project case, the analysis demand for municipalities is an independent random variable, that shall be applied over one year, \(\{t, 1, 2, 3 \ldots 12\}\), which is estimated under a normal stochastic process that integrates Poisson and Weiner processes.

According to research conducted by Girlich (1996) at the University of Leipzig in Germany \([6]\), stochastic demand processes must first establish the domestic demand processes which can be approximated by special Gaussian processes and then review the single product or service model, through a Gaussian process, specifically Wiener processes as a demand process.

First, to explain the particular process applied, we must define the cumulative demand.

**Definition 1:** A stochastic demand process \(D = \{D(t), 0 \leq t \leq a\}\) with \(D(0) = 0\), is a stochastic process with independent and homogeneous increments which has finite variances for each \(t \in (0, a)\). \(D(t)\) denotes the cumulative demand during the time interval \((0, t)\).

From the present definition, we specify two important stochastic demand processes.

**Compound Poisson demand process** \([6]\): In products that have low demand, these demand occurs in \((0, t)\) in sizes \(B_1, \ldots, B_{N(t)}\), where \(N(t)\) denotes the random number of demand cases until \(t\). We say that \(N\) is a Poisson process with the parameter \(\lambda\) if for the increments \(N(s, t) = N(t) - N(s), 0 < s < t\), it holds:

\[(i) \quad N(t_1, t_2), N(t_2, t_3), \ldots, N(t_n, t_{n+1})\]

\[0 \leq t_1 < t_2 < \ldots < t_n + 1 \leq \alpha, \quad \text{are independent random variables.} \]

\[(ii) P(N(s, s + \tau) = k) = \exp(-\lambda \tau) \frac{(\lambda \tau)^k}{k!} \quad (13)\]

The quantity \(D(t) = \sum_{i=1}^{N(t)} B_i\) is equal to the cumulative demand in \((0, t)\). We call \(D\) a compound Poisson demand process with the parameters \(\lambda\) and \(F\) if (i) and (ii) hold, and in addition:

(iii) \(B_1, B_2, \ldots\) are independent and identically \(F\)-distributed integer-valued random variables which are independent from \(N\).

We say that \(D\) is a Poisson demand process if:

\[0 = F(1 - \varepsilon) < F(1) = 1 \quad \text{For all } \varepsilon > 0. \quad (14)\]

Relation (14) means that the size of a Poisson demand process is equal to 1. In general, \(F\) is the distribution function of a discrete distribution with \(F(0) = 0\). For the expected cumulative demand in \((0, t)\) the following relations hold:

\[ED(t) = \alpha t, \alpha = EB_1 = \int_0^\infty [1 - F(x)]dx \quad (15)\]

Where the variance:

\[varD(t) = \beta \tau; \beta = varB_1 = \int_0^\infty (x-\alpha)^2 dF(x) \quad (16)\]

The incorporation of Poisson demand processes leads again to a Poisson process with parameter \((\lambda)\) of which is equal to the sum of the addends’ rate. The generalization to compound Poisson processes additionally needs a weighted sum of the distribution function that generates the next lemma.

**Lemma 1:** For a sequence of \(n\) independent compound Poisson demand processes \(D_i\) with parameters \(\lambda_i\) and \(F_i\), the distribution of \(\sum_{i=1}^{n} D_i\) is equal to the distribution of a compound Poisson demand process \(D^*_n\) with parameters \(\lambda^*_n\) and \(F^*_n\) with:

\[\lambda^*_n = \sum_{i=1}^{n} \lambda_i, F^*_n = \sum_{i=1}^{n} F_i \frac{\lambda_i}{\lambda^*_n} \quad (17)\]

**Gaussian demand process** \([6]\): For fixed \(t\) let \(G(t)\)
denote a normally distributed random variable with
\[ \mathbb{E}G(t) = m(t), \text{var} G(t) = \sigma^2(t) \]

In some cases, for example when \( m(t) > 3\sigma(t) \), we may describe the demand in \( (0, t) \) by \( G(t) \). A process \( G = \{G(t), t \geq 0\} \) is a Gaussian process if its finite dimensional distributions are all normal. \( G \) is characterized completely by the main function \( m(t) \) and the covariance matrix with the elements
\[ \text{cov}(t_j, \ t_k) = \left( \mathbb{E}[G(t_j) - m(t_j)]G(t_k) - m(t_k) \right) \]

For each finite set \( t_i, \ldots, t_n \in \mathbb{R}_+^1 \). We define a Gaussian demand process \( D \) as a Gaussian process with:
\[ ED(t) = m \cdot t, \quad \text{var} D(t) = \sigma^2 \cdot t \]
\[ \text{cov}D(s, t) = \sigma^2 \cdot \min{s, t} \]

In the special case \( m = 0, \sigma^2 = 1 \), we speak of a Wiener demand process \( W \). Therefore, it holds
\[ D(t) \equiv m \cdot t + \sigma W(t). \]

The equality \( \equiv \) means “distributed as”. \( \text{(18)} \)

Such a Gaussian demand process is also called a Wiener demand process with drift. The roles of Gaussian demand processes will be clearer if we investigate some demand processes.

**Central limit theorems**[6]: In inventory research (in retailing processes) it is a well-known fact that a suitable normalized sum of independent and identically distributed random variables with finite variances converges to a normal distribution. Therefore, the Normal approximation is applicable to normal demands. Such a so-called central limit theorem for random variables may be generalized to stochastic processes.

**Theorem 1**: \( (D_n)_{n \in \mathbb{N}} \) with \( D_n = \{D_n(t), 0 \leq t \leq a\} \) be a sequence of independent copies of a stochastic demand process with \( \text{var} D_n (t) = \sigma^2 \cdot t \). Then the sequence \( (Z_n)_{n \in \mathbb{N}} \) with:
\[ Z_n(t) = \frac{1}{\sqrt{n}} \sum_{k=1}^{n} [D_k(t) - ED_k(t)] \]

Converges to a Gaussian process \( G \) with \( G(t) \equiv \sigma W(t) \).

**Proof**: A stochastic demand process has independent increments which are homogeneous. For that reason the conditions of a proposition given by M. Fisz[7] are fulfilled and thus easily verifies our assertion. The assumption of a sequence of independent copies may be weak.

**Theorem 2**: \( (D_n)_{n \in \mathbb{N}} \) with \( D_n = \{D_n(t), 0 \leq t \leq a\} \) be a sequence of stochastic demand processes with the properties:
(i) \[ ED_n(t) \to 0, \quad \mathbb{E}[D_n(t)]^2 \to t \quad \text{for} \ n \to \infty \]
(ii) For arbitrary \( \varepsilon > 0, \eta > 0 \) there exists a \( \delta > 0 \) with
\[ P \left( \sup_{|s-t| < \delta} \left| D_n(s) - D_n(t) \right| \geq \varepsilon \right) \leq \eta. \]

Then \( (D_n)_{n \in \mathbb{N}} \) converges to the Wiener process \( D_n \to W \).

**Normal approximation**[6]: Now we apply the two limit theorems to compound Poisson demand processes.

**Corollary 1**: \( (D_n)_{n \in \mathbb{N}} \) be a sequence of independent copies of a compound Poisson demand process with parameters \( \lambda_i \) and \( F \). Then, for sufficiently large \( n \) the following approximation holds.
\[ \sum_{i=1}^{n} D_i(t) \approx W(t) \int_{0}^{\infty} x^2 dF(x) + t n \lambda \int_{0}^{\infty} x^2 dF(x) \]

The superposition of identical compound Poisson demand processes may, therefore, be approximated by a Wiener process with drift.

**Corollary 2**: Let \( D_1, D_2, \ldots, D_i, \ldots \) be a sequence of independent compound Poisson demand processes with parameters \( \lambda_i \) and \( F_i \), respectively. Then, for sufficiently large \( n \) the following approximation holds.
\[ \sum_{i=1}^{n} D_i(t) \approx W(t) \int_{0}^{\infty} x^2 dF_i(x) + t n \lambda_i \int_{0}^{\infty} x dF_i(x) \]

Where \( \lambda_i \) and \( F_i \) are given by (17).

**Model Applying**: In this particular case of the model, the demand per municipality is established under the following assumptions for (23):
- \( \lambda \) is taken as a constant value, this estimated with the sample mean of the year available, this parameter is set to distribution population mean and the best estimation for this one is sample mean.
- \( W(t) \sim N(0,1) \), Weiner distribution by definition as a standard normal distribution[7].
- In order to check if in fact the variable \( X \) follows a normal distribution, we proceed to perform a goodness of fit test[8], according to available year information analysed, which shows the fit to this distribution, then comes the test.
- \( F \) follows a Poisson distribution given in (17), with the parameter \( \lambda \), which is estimated under the same presented assumptions.
- \( t \) for the model will be applied to cycles, performed on the index of the same name, which analysed a specific year.

**Stochastic Processes adjusted**: Below we present the stochastic demand processes adjusted that applied to the model, with the goal to generate random numbers in the process to be applied to each municipality.
\[ D_i(t) \approx W(t) \sqrt{\frac{x^2 F_i}{n} + \frac{\lambda x F_i}{n}} \]

Where \( i \) refers to each municipality \( \text{(24)} \)

**Goodness of fit test**[8]: We used this hypothesis test in order to verify the assumption of normal distribution of the \( X \) variable, below we present the application of the test:
- \( H_0 \): Demand per municipality, follows a normal probability distribution
- \( H_1 \): Demand per municipality, doesn’t follow a normal probability distribution
The test statistic is given by: \( \chi^2 = \sum_{i}^{k} \frac{(f_o_i - f_e_i)^2}{f_e_i} \)

Where \( f_o_i \) is observed frequency (sample), \( f_e_i \) as expected frequency (Normal distribution), \( k \) as classes number, \( v = k - p - 1 \) as freedom degrees of \( \chi^2 \), where \( p \) is the number of function parameters expected.

According to the statistics results and the accumulative probabilities set to right of the same (Table 1), and keeping in mind that the refusal region is also set to the right, we can accept a void hypothesis, by saying that there is enough statistic evidence in order to use a normal distribution to supply demand in the municipalities.

### 6.3. Model’s Solution tool Selection Process

After we present the model to use and estimate the Pareto’s client demand through a stochastic process, we then begging to go through the tools we have available in order to give solution to the exposed model, we select GAMS (General Algebraic Modelling System) according with the revision made by the University of Waterloo on the scientific software comparison table, GAMS is a proper tool that allows us to give solution to the given model[8]. In this table as we get away from the middle of the diagram, the software becomes more advance but at the same time less friendly, making GAMS a mid-level program comparing it to a basic program like Excel or an advance one like NAG and MINOS.

### 6.4. Solution and Verification of the Model’s Results

As an initial result we find the following table, where we can find the total number of own locations, to be created \( (x) \), third party locations \( (w) \) and recollection circuits \( (r) \); based on these values we then proceed to do a scenario analysis where we modify some restrictions (strategic options) and we run the model to give the company three different strategies to take.

**Scenarios:**

- As a first scenario we find the information given by the company as a strategic option and then we rise of the blocks from own locations and third party locations until we are able to double them on the third scenario (Table 2).
- We take the demand given as a result by the stochastic process applied to the model, we then establish an average price of set pieces the client sends of $4.194 (Col pesos) defining the estimated revenue produced by said customer.
- Taking by reference the information of client selection where we came to know that he or she represents the 4.53% of the company’s revenue, we use this information to polarize the determined revenue and the total of these.

We then calculate the network maintenance cost with the information gathered from the parameters for the remaining eleven (11) months.

### Table 1. Evidence of Adjustment Graciousness Result

| Parameter          | Squared Chi | Freedom Degrees | Probability |
|--------------------|-------------|-----------------|-------------|
| Squared Chi        | 0.218756166 | 6               | 0.9998      |

According to the strategic option given by the company on the case scenario 1, we can see that the margin obtained is of 1.95% the total revenue, keeping in mind that with this option we don’t take into account administrative expenses, and other costs that the company shoulders, it is not recommended to implement this scenario therefore the company should be able to consider either scenario 2 or 3 as better alternatives, on the other hand the company is free to set their own commercial strategies, allowing them to implement the proposed network, which should be able to increase the estimated revenue for the upkeep of the scenario 1 structure.

Additionally, we validated the network’s capacity under each scenario, where by accordance of the revision made we can show that according to the analysis of the company’s capacity, that we used to estimate the admission or intake capabilities on the proposal network under each of the three different scenarios, the usage of this one won’t be higher than 0.5%, showing that without minding which scenario is set, the Pareto client analysed should be able to be taken care of.

Lastly, we proportionate the networks structure for the attention of the corporative clients, which is distributed within own locations, third party (franchise) locations and recollection circuits, where the description given is the result per municipalities that the model outputs in relation with these three variables and additionally we get results by scenario.

### 7. Conclusions and Recommendations

#### 7.1. Conclusions

This project tried to eliminate the subjectivity that exists when it comes to the decision making of where to locate attention points, process which is structured through the lineal programming model, with a stochastic process of demand, giving tools for the decision making of a courier company that wants to define the channel strategy focused on the client.

In the process of generating the network’s structure in order to tend to corporative channel, we used the client’s knowledge to determine it, which implies a detailed analysis of the needs of the client, which then gives us the need of an
organizational change that focuses their efforts not only on delivering the offered service but also offering better and new access tools to their products or services, through a continuous analysis of the networks structure and its portfolio.

According to the model’s results, we established different scenarios allowing us to validate these results, generating three different strategic options that gives us different alternatives to set initial margins (revenue vs. network’s costs) of 1.98% to 52.18% base information in order to define commercial strategies set to increase revenue to over pass these margins.

Continuing with the validation process for the model’s results we made a company’s capacity analysis under the proposed network structure on the three scenarios in own locations: where we can find that the usage proportion of this one does not passes or overlaps 0,4% with Pareto clients. This allows us initially to be certain that the company has a potential growth which must be strengthened through a series of commercial and marketing strategies, trying to accomplish a higher use of the network.

7.2. Recommendations

Within the validation of the model we made an analysis of the network’s capacity in own points (locations) based on the set Pareto client in order to define the model, it is proposed to study the whole capacity of the network’s structure selected under the given scenarios with the total of clients, in order to really know the true capacity available for the company’s growth within the network, allowing us to land a clear view of strategic growth within the available network.

The project’s result lets us know the amount of attention points and the municipalities where they should be located, parting from this we can define a model of location per municipalities, establishing which are the potential zones for the locations of given attention points, this kind of analysis can be developed with intelligent geographical information system tools as – GIS[9], which groups interest variables together for a company, allowing them to segment the municipalities.

ACKNOWLEDGEMENTS

This project would not have been possible without the support of several people who participated in it in different ways, as well as the support and confidence of the company that gave me the information necessary for the construction of this model, thanks.

REFERENCES

[1] Y. &. R. B. BrandsAsset® Valuator, Empresa Consultora – Estrategia de Canales, Colombia, 2008.

[2] H. F. Rudd, J. W. Vigen y R. N. Davis, «The LMMD model: choosing the optimal location for a small retail business,» Journal of Small Business Management, vol. Vol. 21, pp. p45-52, 1983.

[3] C. S. Craig, A. Ghosh y S. McLaﬀerty, «Models of the retail location process,» Journal of Retailing, vol. 60, n° 32p., pp. p5-36, 1984.

[4] G. Cliquet, «New Challenges for Store Location in a Plural Form Network: An Exploratory Study. Strategy And Governance Of Networks,» Contributions to Management Science, Vols. %1 de %2II, Part 1, pp. 127-145, 2008.

[5] S. M. Ross, Stochastic Processes - Second Edition, United States Of America, 1996.

[6] H.-J. Girlich, «Some comments on normal approximation for stochastic demand processes,» International Journal of Production Economics, vol. 45, n 1–3, pp. 389-395, 1996.

[7] R. E. Walpole, R. H. Myers y S. L. Myers, Probabilidad y Estadística para Ingenieros, Pearson Educación, 1998.

[8] University of Waterloo, «Scientific Software Comparison Chart,» University of Waterloo, Ontario, Canada,[En línea], Available: http://www.dcs.uwaterloo.ca/ec/scientific/scicom.html#top.

[9] S. Lombardo, M. Petri y D. Zotta, «Intelligent Gis and Retail Location Dynamics: A Multi Agent System Integrated with ArcGis,» COMPUTATIONAL SCIENCE AND ITS APPLICATIONS – ICCSA 2004, Lecture Notes in Computer Science , vol. Volume 3044/2004, pp. 1046-1056, 2004.

[10] L. Vanhaverbeke y C. Macharis, «An agent-based model of consumer mobility in a retail environment,» Procedia - Social and Behavioral Sciences, vol. 20, pp. 186-196, 2011.

[11] T. Arentze, A. Borgers y H. Timmermans, «A knowledge-based system for developing retail location strategies,» Computers, Environment and Urban Systems, vol. 24, n 6, pp. 489-508, 2000.

[12] Publicación BIT, La estrategia del Canal, hoy. Colegio Oficial, Asociación Española de Ingenieros de Telecomunicaciones, España, 2005.

[13] B. H. Oszuduru y C. Varol, «Spatial Statistics Methods in Retail Location Research: A Case Study of Ankara, Turkey,» Procedia Environmental Sciences, vol. 7, pp. 287-292, 2011.

[14] T. Nakaya, A. S. Fotheringham, K. Hanaoka, G. Clarke, D. Ballas y K. Yano, «Combining microsimulation and spatial interaction models for retail location analysis,» Journal of Geographical Systems, vol. 9, n° 25p, pp. p345-369, 2007.

[15] V. Labajo González, Trade marketing: La gestión eficiente de las relaciones entre fabricante y distribuidor, España, 2006.

[16] M. F. Goodchild, «ILACS: a location-allocation model for retail site selection,» Journal of Retailing, Vols. 1 de 2 p84-100, n 17p, p. 60, 1984.

[17] A. Díaz Morales, Gestión por categorías y Trade Marketing, España, 2002.

[18] G. Clarke, «Changing methods of location planning for retail
[19] M. V. Bordonaba Juste, «Marketing de relaciones en los canales de distribución: un análisis empírico,» Cuadernos de economía y dirección de la empresa, nº 29, pp. Págs. 5-30, 2006.

[20] Weintraub, Andrés, Handbook of Operations Research in Natural Resources, Springer, 2007.