Heterogeneous impact of a lockdown on inter-municipality mobility

Hygor P. M. Melo, João Henriques, Raquel Carvalho, Trivik Verma, João P. da Cruz, and N. A. M. Araújo

1Centro de Física Teórica e Computacional, Faculdade de Ciências, Universidade de Lisboa, 1749–016 Lisboa, Portugal
2NOS, SGPS, S.A., 1600–404 Lisboa, Portugal
3Altran Portugal, 1990–096 Lisboa, Portugal
4Faculty of Technology, Policy and Management, Delft University of Technology, 2628BX Delft, the Netherlands
5Closer Consultoria, 1070–101 Lisboa, Portugal
6Departamento de Física, Faculdade de Ciências, Universidade de Lisboa, 1749–016 Lisboa, Portugal

Without a vaccine, the fight against the spreading of the coronavirus has focused on maintaining physical distance. To study the impact of such measures on inter-municipality traffic, we analyze a mobile dataset with the daily flow of people in Portugal in March and April 2020. We find that the reduction in inter-municipality traffic depends strongly on its initial outflow. In municipalities where the mobility is low, the outflow reduced by 10 – 20% and this decrease was independent of the population size. Whereas, for municipalities of high mobility, the reduction was a monotonic increasing function of the population size and it even exceeded 60% for the largest municipalities. As a consequence of such heterogeneities, there were significant structural changes on the most probable paths for the spreading of the virus, which must be considered when modeling the impact of control measures.

I. INTRODUCTION

In response to the coronavirus pandemics, many governments have imposed lockdowns, closing several public places, such as, schools, restaurants, sport centers, and shopping malls [1]. Companies and public services have opted for giving employees the choice to work from home [2]. These non-pharmacological interventions are believed to be responsible for a significant slowdown of the spreading in different countries [3–10]. However, one still lacks an understanding on how the mobility patterns have changed and how such changes affect the most probable pathways for the spread of the virus.

With digitalization and advancements in global data collection, the public expectations for knowledge-based strategies to control the spreading of the coronavirus have been high. Daily, the public is swamped with statistics about new infections, deaths, and recoveries around the world [11][12]. Models and metrics are being proposed and further developed to turn data into actionable insights [13]. But, statistics of demographic variations of the impact of a virus are not enough. An extensive body of research on recent public health threats, such as the 2013 MERS-CoV, 2014 Ebola, and 2016 Zika viruses, has shown that to estimate the spread and implement efficient actions for controlling it, one needs to rigorously investigate the mobility patterns [14][17]. Depending on the level of granularity, mobility data might be obtained from civil aviation statistics [18][19], national censuses [10][20], public transit ridership [21][23], or mobile phone tracking [20][24]. By May 2020, there were more than 60k travel restrictions issued around the world to control inter- and intra-country travelling [24]. The mobility patterns today are very different from the ones in February 2020 and these publicly available data sets are no longer representative.

Epidemic spreading is a network-driven process [24][20][28]. To understand the complex spatiotemporal spreading dynamics, one needs to replace the traditional view based on geographical distance by a probabilistically motivated effective distance computed from the flux of people [29]. With such a change of paradigm, one can identify the set of most probable paths for the spreading of the virus and the relative arrival times of an epidemics, which are both independent of the epidemic parameters. Thus, the role of a municipality on the global dynamics depends on its daily flow and effective distance to other municipalities.

Here, we study this impact by analyzing mobile phone data for the inter-municipality daily flow of people in Portugal in March and April 2020. The first confirmed case of COVID-19 in Portugal was reported on March 2, 2020. Ten days later, the total number of cases added up to 78 and the government announced a first set of control measures, which included school closures from March 14 onward. With a total of 642 identified cases, on March 19, the government decided to declare the state of emergency and social distance. We show that, the impact of the different measures was neither instantaneous nor homogeneous throughout the country. It extended over several days and the relative impact was strongly dependent on the population size of the municipality. We also analyze how the changes in mobility impacted on the distances.
We show that the effective distances changed differently for each municipality. The structure of the set of most probable paths and relative arrival times also changed, with a significant impact on the spreading dynamics.

II. RESULTS

We analyze a national-scale mobile dataset provided by NOS, a Portuguese telecommunication company. This dataset contains the daily number of people that moved within and between municipalities in Portugal in March and April 2020, obtained from the mobile recurrent usage of residents and non-residents (see Materials and Methods for further details). The non-residents are defined as users with a SIM card from a foreign mobile network. A user is registered in the dataset if they stay for, at least, 60 minutes within the boundaries of a municipality (see Materials and Methods for further details).

To quantify the inter-municipality mobility, we measure the daily number of users moving within and between municipalities and define relative mobility as this number rescaled by the average relative mobility from March 2 to 6 (baseline), which is a period before any control measures (March 12), the mobility started to decrease. However, this change in mobility was not instantaneous; it occurred over several days and only reached a steady level after March 21, with a decrease of about 20% for residents and 45% for non-residents. The periodic structure observed in the steady regime corresponds to

the expected weekday (Monday to Friday) and weekend (Saturday to Sunday) differences, with a clear decrease in mobility during the weekends. In the same figure, we show also the spatial distribution of the relative mobility for three specific days (March 9, March 19, and April 23), for residents (R1, R2, and R3) and for non-residents (N1, N2, and N3).

FIG. 1. Effect of the lockdown in the mobility pattern of residents and non-residents in Portugal. The relative mobility is calculated as the total number of people that moved between two different municipalities on that day divided by the average between March 2 and 6 (see Materials and Methods for further details). The first control measures were announced in March 12, and the state of emergency was declared on March 18. We see that after the lockdown the mobility of residents and non-residents decreased to about 20% and 45% of the baseline. The maps show the spatial distribution of the relative mobility for three specific days (March 9, March 19, and April 23), for residents (R1, R2, and R3) and for non-residents (N1, N2, and N3).
FIG. 2. **Shortest–path trees and effective distances before the lockdown.** Shortest–path trees from Lisbon (A), Braga (B), and Campo Maior (C) (central nodes). Each node is a different municipality and the distance to the central node is proportional the effective distance $D_{\text{eff}}$, as defined in the Materials and Methods. The effective distances are calculated from the origin–destination matrix of the average mobility between March 2 and 6. The nodes are colored according to the geographical distance to the central node. In the bottom row are the country maps, where the color of each municipality is given by the effective distance from the corresponding central municipality marked by a black circle.

show three examples of the shortest–path trees, for (A) Lisbon, (B) Braga, and (C) Campo Maior, using an OD matrix obtained from the average mobility from March 2 to 6. All nodes are placed at a distance from the central node proportional to their effective distance to it. For the sake of comparison, the color of a node is given by the geographic distance from the central node. The size of the node is given by the value of the betweenness centrality, which is defined as the number of shortest paths that go from the central node to any other node on the tree through that node. In the figure, below each tree, we also show a color map displaying the spatial distribution of effective distances from each center. It is clear that, some municipalities can be geographically far from the central municipality, but have a small value of effective distance, indicating that the relation between effective distances and geographic distances are non-trivial.

Since the change in mobility was heterogeneous throughout the country, as shown in Fig. [1], it is expected that both the effective distances and structure of the shortest–path trees have changed. To illustrate such changes, we show in Fig. [2] (A) the time evolution of the shortest–path tree for Lisbon. We discover a change from a star-like structure to a more branched structure. Figure [2] (B) shows the time evolution of the average effective distance $\langle D_{\text{eff}} \rangle$ to all other municipalities for Lisbon, Braga, and Campo Maior. With the lockdown, $\langle D_{\text{eff}} \rangle$ increased, consistent with a much slower propagation dynamics. The maximum on the Easter holidays (gray region) is reflective of a set of additional measures imposed by the Portuguese government for those days to avoid the traditional family gatherings, which included severe restrictions to the inter-municipality mobility. For each day $d$, we calculated the Spearman’s correlation between the effective distance $D_{\text{eff}}(d)$ and the initial effective distance $D_{\text{eff}_0}$, obtained from the average mobility network from March 2 to 6 (before the lockdown). The Spearman’s correlation $r$ for the entire set of municipalities is defined as

$$r = \frac{\text{cov}(rk_d, \overline{rk})}{\sigma(rk_d)\sigma(rk)},$$

where $rk_d$ is the rank of $D_{\text{eff}}(d)$, $\overline{rk}$ is the rank of $D_{\text{eff}_0}$, $\text{cov}(rk_d, \overline{rk})$ is the covariance of the rank, and $\sigma(rk)$ is the standard deviation. An $r = 1.0$ means that the rank of effective distances has not changed, while $r = 0$ corresponds to a new rank that is uncorrelated from the original one. The daily evolution of $r$ is shown in Fig. [2] (C).
FIG. 3. The effect of the lockdown on the mobility network. (A) Shortest–path tree from Lisbon for three different days. The position of the nodes is given by the Fain Hu layout [30], designed to distribute symmetrically the nodes and minimize edge crossing. The color of each node is given by the effective distance from Lisbon. (B) Time dependence of the average effective distance in the shortest–path trees shown in Fig. 2. Before the lockdown, for these three municipalities, Lisbon had the shortest average distance to the rest of the country, followed by Braga and Campo Maior. With control measurements, the three average effective distances increased, reaching a maximum in the Easter holidays, when the Portuguese government imposed more severe mobility restrictions to inter-municipality travels. (C) Spearman’s correlation coefficient \( r \) between the effective distance from the average origin–destination matrix from March 2 to 6, and all the days of March and April. With the lockdown, the rank of the effective distances have changed as shown. (C) Time evolution of the node degree \( k \) (number of edges) for Lisbon, Braga, and Campo Maior, for the shortest–path trees shown in Fig. 2. Initially, Lisbon was connected directly to more than 90% of the municipalities. With the lockdown, the \( k \) decreases reaching a minimum at the Easter holidays, with only less than 50% of the municipalities connected with Lisbon by only one edge.

For the three municipalities, \( r \) decreased with the lockdown. This result suggests that the hierarchical organization of municipalities in a spreading process was affected significantly by the lockdown.

Figure 3(D) depicts the evolution of the degree \( k \) of the central node (Lisbon, Braga, and Campo Maior), corresponding to the number of municipalities that are directly connected to the central node in the shortest–path tree. Before the lockdown, Lisbon was connected by a single edge to 90% of the municipalities. With the lockdown, Lisbon, in average, became only connected directly to 55% of the municipalities. This is in line with a change from a star-like to a branched structure, as observed in Fig. 3(A). We see a similar behavior for Braga, starting with the fraction of municipalities connected directly, decreasing from 58% to 33%, and for Campo Maior, where the drop is from 23% to 15%.

In Fig. 3 we compare the outflow before and after the lockdown. The outflow is defined as the total number of resident users of a municipality that were also identified in a different municipality during the day (see Materials and Methods). The values before the lockdown are averages from March 2 to 6 and after the lockdown from April 13 to 17. We find that, although the control measures were the same for the entire country, their impact on the outflow strongly depends on the initial value of the outflow. For municipalities with low values of outflow, we observe a linear relation between the outflows before and after, which suggests that the relative impact is the same. However, for the municipalities with higher values of the outflow, we observe a sublinear relation between the two. The larger the initial value of the outflow the stronger is the impact of the control measures. Since the outflow of a municipality correlates strongly with the population size [32], in the inset of Fig. 3 we plot the relative decrease in outflow as a function of the population size.
The impact of the lockdown depends on the mobility pattern of the municipality. Outflow of each municipality before and after the lockdown. To reduce the statistical noise, the outflow corresponds to averages over five days: before any control measurements, we considered March 2 to 6, and for after the lockdown April 13 to 17. Each colored circle is a municipality and the black solid line is a guide for the eyes and corresponds to a linear relation between the two. The color of each data point represents the population size of the municipality, following the log-spaced bins shown in the inset. We can see that the effect of the lockdown is not homogeneous across the country, municipalities with large values of mobility at the beginning of March showed a large reduction in April. In the inset is the relative change on outflow of each municipality (cyan circles) as a function of its population size. The relative change is calculated by the outflow difference between March and April divided by the one in March. The colors are given by the average relative change on outflow in log-spaced bins (based on the population size). The dashed lines are best fits for a logarithmic dependence of the relative mobility (RO) on the population size (P). For smaller municipalities (< 18000 people), we find $RO = 0.034 \log_{10}(P) - 0.25$, while for the larger ones $RO = -0.27 \log_{10}(P) + 1.02$. The population for each municipality was obtained from Ref. [31].

For municipalities with less than 18000 users, the outflow decreased by 10 − 20%, without a clear dependence on the population size. Whereas, for larger municipalities, the relative decrease in the outflow scales logarithmically with the population size (dashed line) and it exceeds 60% for the largest municipality (Lisbon).

III. CONCLUSIONS

Human mobility sets the stage for global spreading phenomena [19, 27, 29, 33, 34]. Across the world, the most relevant non-pharmacological interventions to contain the spreading of the coronavirus have been related to closing borders and restricting the intra- and inter-country mobility, which has affected the mobility patterns [9]. Here, we studied the impact of such mobility restrictions in the inter-municipality flow of people in Portugal, in March and April of 2020. From a large dataset of mobile phone users, we obtained the origin-destination matrix and the shortest-path trees from all municipalities. These trees represent the most probable paths for the spreading of the virus, when starting from a given municipality [24, 29, 35]. We find that the relative decrease in mobility correlates with the population size of a municipality. For small municipalities, with less than 18000 mobile users, the outflow is decreased by about 10 − 20%, regardless the size of the municipality. However, for larger municipalities, the relative decrease in the outflow depend strongly on the population size and it even exceeds 60% for the largest municipalities. Such a heterogeneous change in mobility affects deeply the structure of the shortest-path trees and, therefore, the relative effective distance between municipalities.

To circumvent the absence of accurate data for mobility, models have been developed to artificially generate them, as for example the gravity and radiation models [32–36], or to account for mobility restrictions in the models [28, 37, 38]. From our findings, it is now possible to extend these models to account for the dependence on the size and mobility of a municipality. This heterogeneous response is an important ingredient to consider in epidemic models, such as the ones developed in Refs. [28, 37, 43], so that governments can respond to the spread more accurately.

IV. MATERIALS AND METHODS

A. Mobility matrix from mobile phones records

The mobile data was obtained from NOS cellular network and its volume goes up to about 8 Terabytes of events, collected from the network interfaces in March and April 2020. Each record in the dataset refers to a unique subscriber id, General Data Protection Regulation (GDPR) compliant regarding Personal Identifiable Information (PII) [46], and it includes the date/timestamp of each respective event and the geographic coordinates of the respective network cell coverage centroid where each event occurred. Such dataset can thus provide an abstraction of subscriber physical displacements over time.

The process to compute the mobility matrices is composed of several steps: from data event aggregation and location estimation to trip count aggregation. Within the data event aggregation part, the events are aggregated in a 10 minutes sliding window with detection counts for each subscriber id performed by cell. The location for each subscriber id is estimated based on the most frequent cell algorithm. Once the location trips are extracted, the process to derive origin-destination flows between geographic areas is the following: i. The geographic area under analysis is divided into municipalities; ii. Origin and destination municipalities, together with starting time are extracted for each subscriber id. iii.
Trips with the same origin, destination, and time frame are grouped together. The result is a matrix whose element represents the number of trips from origin \(i\) to destination \(j\), starting within the time frame. Here, we used the municipal areas in Portugal for the regions and the time frame of 6 am and 8 pm.

From the mobility matrix, the extrapolation process is carried out to represent the whole universe of the population in study. The extrapolation algorithm takes into consideration local as well as international market shares, besides wholesale agreements between parties. After extrapolation, the transformation process takes place to extract features from residents and non-residents, segmenting the data between flows from region \(i\) to \(j\), and the ones that do not move within that time window, which is the same as saying that \(i\) is equal to \(j\). At the end, compliance with the data privacy rules (GDPR) are applied and trips with counts under 6 are omitted.

### B. Shortest–path trees

For the network analysis, we only considered the movement of residents, i.e., in the mobility matrix \(F(d)\), \(F_{ij}(d)\) is the number of resident users who were identified at both municipality \(i\) and \(j\) within the day \(d\). In order to measure the combined number of individuals from \(i\) to \(j\), we considered the undirected mobility network using the standard symmetrization operation \(F = F + F^T\), where \(F^T\) is the transposed matrix of \(F\).

Each element of the origin–destination matrix \(P\) is calculated as \(P_{ij} = F_{ij}/\sum F_{in}\), where the sum is over all municipalities, and quantifies the mobility network, where the nodes are the municipalities and the edges between \(i\) and \(j\) have a weight \(P_{ij}\). If we define the distance \(\ell_{ij} = 1 - \log(P_{ij})\) for each edge, the most probable paths are the ones that minimize the total sum of \(\ell\) [29]. For each node, one can define a shortest–path tree (see Fig. 2) and the effective distance \(D_{\text{eff}}\) from a node \(i\) to \(j\) as the length of the shortest path between these two nodes.

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