About estimations of an one-photon background in neutrino oscillation experiments at low neutrino energies

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Abstract

The possible sources of one-photon radiation as background for quasi-elastic reaction $\nu_\mu + n \rightarrow \mu^- + p$ are considered. The ones are relevant in experiments on determination of oscillation parameters at low neutrino energies ($E_\nu \sim 1 \text{ GeV}$). The estimation for the cross section of reaction $\nu_\mu + n \rightarrow \mu^- + p + \gamma$ is given at $E^{lab}_\nu = 0.7 \text{ GeV}$ as 0.65% from the corresponding cross section of quasi-elastic reaction. The mechanisms of quasi-elastic reaction are also considered at low neutrino energies on quark level.

The current now accelerator experiments on $\nu_\mu - \nu_e$ neutrino oscillation deal with neutrino beams at low energies ($E_\nu \sim 1 \text{ GeV}$). To shed light on the neutrino oscillation parameters, the rather precise knowledge of the neutrino-nucleon interactions in this energy region is required. Since Cherenkov detectors employed in these experiments poorly distinguish an electron from a photon, it is extremely important to study the possible background from other reactions with one or two photons to the main quasi-elastic reaction a neutrino on a nucleon:

$$\nu_\mu + n \rightarrow \mu^- + p.$$  \hspace{1cm} (1)

In this work we give estimations of the cross-sections of the processes, which are interested for us, at neutrino energy in laboratory system $E^{lab}_\nu = 0.7 \text{ GeV}$.

The processes with neutral currents

$$\nu_\mu + p \rightarrow \nu_\mu + p,$$

$$\nu_\mu + n \rightarrow \nu_\mu + n$$ \hspace{1cm} (2)
are not interested in experimental analysis of neutrino oscillations. However, reaction

$$\nu_\mu + p \rightarrow \nu_\mu + p + \gamma$$

(3)
can contribute to the one-photon background. At the same time, the ratio of the cross sections in the given neutrino energy is known from experiments 1:

$$\frac{(\nu_\mu p \rightarrow \nu_\mu p)}{(\nu_\mu n \rightarrow \mu^- p)} \sim 0.1.$$ (4)

The $Q^2$ interval, over which this ratio was measured, is $(0.3 \div 1.0) \text{ GeV}^2$. The approximately same ratio is valid for the cross sections of the one-photon reactions

$$\frac{(\nu_\mu p \rightarrow \nu_\mu p\gamma)}{(\nu_\mu n \rightarrow \mu^- p\gamma)}.$$ (5)

The following contribution of reaction (3) is essentially less than the contribution of reaction

$$\nu_\mu + n \rightarrow \mu^- + p + \gamma.$$ (5)
The calculation of the cross section of reaction (5) is the first goal of the present study.

The two-photon background in our case is determined by reaction

$$\nu_\mu + n \rightarrow \mu^- + p + \pi^0.$$ (6)
The experimental cross section of reaction (6) at $E_{\text{lab}}^{\nu_\mu} = 0.7 \text{ GeV}$ is $\sigma \simeq 0.07 \times 10^{-38} \text{ cm}^2$ 1. The pair of photons from $\pi^0$ decay is successfully identified by data processing of experiments except of the restricted kinematic configurations.

Reaction (6) together with reaction

$$\nu_\mu + n \rightarrow \mu^- + n + \pi^+$$ (7)
can also contribute to the one-photon background. The experimental cross section of reaction (7) is approximately the same as that of reaction (6) and at $E_{\text{lab}}^{\nu_\mu} = 0.7 \text{ GeV}$ it equals to $\sigma \simeq 0.07 \times 10^{-38} \text{ cm}^2$. If the isobar $\Delta^+$ is produced in the reactions (6) and (7), it can decay via the channel:

$$\Delta^+ \rightarrow p + \gamma.$$ (8)
The branching ratio of the decay (8) is $\sim 0.5\%$ 2. We are suspected that reactions (6) and (7) go through the formation of an isobar $\Delta^+$. The common contribution to the one-photon background from the reactions (6,7) as well as from the neutral current single pion production $\nu_\mu p \rightarrow \nu_\mu p\pi^0$ is

$$\sigma \leq (0.07 + 0.07 + 0.04) \times 0.005 \times 10^{-38} \text{ cm}^2 \simeq 0.0009 \times 10^{-38} \text{ cm}^2.$$ (9)

It constitutes < 0.09% from the cross section of quasi-elastic reaction. The actual magnitude of one-photon cross section (9) will be essentially less that indicated value,
because considerable non-resonant pion-nucleon contribution there is in the final state.

Therefore, further we will consider only of reactions (1) and (5). It should be noted that without comprehension of the mechanism of quasi-elastic reaction, it is not possible to write out the gauge-invariant amplitude of reaction (5), because this reaction (5) is radiative process from the process (1).

In Fig. 1 the cross section of quasi-elastic reaction (1) as a function of the neutrino energy in laboratory system is shown. The cross section is calculated in the conventional theory with parameters and form factors taken from Refs. [1, 3]. The strong dependence of the form factors from a transfer momentum squared allows one to describe the behavior of this cross section of reaction (1) in a broad energy range from threshold and up to $E_{\nu}^{\text{lab}} \sim 10 \text{ GeV}$. Nevertheless, two different mechanisms of quasi-elastic reaction are seen from Fig. 1. First is at energies from a threshold of reaction and up to $E_{\nu}^{\text{lab}} \sim 1.3 \text{ GeV}$, and second is at $E_{\nu}^{\text{lab}} > 1.3 \text{ GeV}$, i.e. in the Bjorken scaling region.

To find the gauge-invariant amplitude of radiation process (5) within the standard formalism, it is needed to consider the diagrams of an internal Bremsstrahlung as well as to account for the contributions of the direct vector and axial radiation. In any case there are some free parameters, which have to be determined from the experiment. We are interested in an estimation of the cross section of process (5) at low neutrino energy $E_{\nu}^{\text{lab}} = 0.7 \text{ GeV}$. The cross section of reaction (1) at $E_{\nu}^{\text{lab}} = 0.7 \text{ GeV}$ from our calculation (see, Fig. 1) is:

$$\sigma \simeq 0.95 \times 10^{-38} \text{ cm}^2.$$  (10)

In Ref. [4] for description of a hadron current in $K_{\mu3}$ decay the representation of current of constituent quarks was used.

We use this approach for the description of the amplitude of process (1). We suppose that at the first stage of reaction (1) neutrino interacts with $d$ quark, existing in the neutron, with formation of muon and $u$ quark with a definite momentum (see, Fig. 2). The produced $u$ quark is going some time freely. At the second stage the confinement in a proton demands that all system of three quarks is moving with an produced $u$ quark momentum. The cross section of reaction (1) is determined basically by the first stage of the process.

The diagram of process (1) on quark level

$$\nu_{\mu}(k) + d(p) \rightarrow \mu^{-}(k') + u(p')$$  (11)

is displayed in Fig. 3. Amplitude of process (1) is given by

$$T = \frac{G_F}{\sqrt{2}} |V_{ud}| \bar{u}_u(p') \gamma^\mu (1 - \gamma_5) u_d(p) \bar{u}_d(k') \gamma^\mu (1 - \gamma_5) u_\nu_{\mu}(k).$$  (12)

Here, $\bar{u}_u(p'), u_d(p)$ are 4-spinors of constituent quarks, the masses of constituent quarks as well as paper [4] and also in papers [5, 6], in particular values of masses $m_u = m_d = 0.305 \text{ GeV}$ [4] were used. In Fig. 4 the angular distribution of a muon for reaction $\nu_{\mu} + n \rightarrow \mu^{-} + p$ in a laboratory system at $E_{\nu}^{\text{lab}} = 0.7 \text{ GeV}$ is shown.
The quark amplitude (12) determines an angular distribution of a muon in reaction (1). The cross section of process (11) on one quark is determined also imploing the amplitude (12) and at $E_{\nu}^{lab} = 0.7 \text{ GeV}$ it equals to

$$\sigma \simeq 0.53 \times 10^{-38} \text{ cm}^2. \quad (13)$$

It is known that the point weak interaction is incoherent. For obtaining the cross section of reaction (1) on a neutron, containing two $d$ quarks, it is necessary to double the cross section (14). So, the cross section of quasi-elastic reaction $\nu_\mu + n \rightarrow \mu^- + p$ at $E_{\nu}^{lab} = 0.7 \text{ GeV}$ is equal to

$$\sigma \simeq 1.06 \times 10^{-38} \text{ cm}^2. \quad (14)$$

It corresponds to value (10) by an order of magnitude.

In Fig. 5 the similar angular distribution of muon in reaction (1) in a laboratory system calculated using the conventional model [1, 3] is shown. Let us note that in K2K experiment on muon neutrino oscillation [7] the deficit of one-track events, whose muons are at angles near the direction of the neutrino beam, was observed, when Monte Carlo simulation with the conventional description of quasi-elastic reaction was carried out. In an angular distribution of a muon, shown in Fig. 4, such deficit of one-track events at small angles, contrary to the case of Fig. 5, was not observed.

The conducted analysis allows one to make some qualitative conclusions:

1. The description of an experimental angular distribution of a muon in a laboratory system in quasi-elastic reaction $\nu_\mu + n \rightarrow \mu^- + p$ is reached without use of the phenomenological form factors (see, Fig. 4). The neutrino interacts with a quark via the process (11).

2. In reaction $\nu_\mu + n \rightarrow \mu^- + p + \gamma$ the first stage of process proceeds through the interaction a neutrino with a simple system, a quark. Therefore, the direct production of a photon does not take place. So, in general, the contributions of direct radiation in the given reaction will be reduced.

Finally, we estimate the cross section of reaction $\nu_\mu + n \rightarrow \mu^- + p + \gamma$. We can find the ratio of the cross section of reaction (Fig. 6)

$$\nu_\mu(k) + n(p) \rightarrow \mu^-(k') + \gamma(r) \quad (15)$$

and the cross section of reaction (11).

Using the Low theorem [8, 9, 10, 11, 12], the gauge-invariant amplitude of reaction (15) can be written as (within $r^1$):

$$M = e \frac{G_F}{\sqrt{2}} |V_{ud}| \left[ \frac{(k'\epsilon^*)^*}{(k^*)} - \frac{(p'\epsilon^*)^*}{(p^*)} \right]$$

$$\times \bar{u}(\bar{p'}) \left[ F_V^1 \gamma^\mu + F_V^2 i \sigma^{\mu\nu} q_\nu + F_A \gamma^\mu \gamma_5 + F_p q^\mu \gamma_5 \right] u(p)$$

$$\times \bar{u}(\bar{k'}) \gamma^\mu (1 - \gamma_5)u(k) + O(r). \quad (16)$$

Here, $\epsilon_5^*$ is photon polarization, $\bar{k'}$ and $\bar{p'}$ denote the four-momenta of muon and proton in quasi-elastic reaction (11); $q = k - \bar{k'}$; $F_V^1, F_V^2, F_A$ are form factors of the
conventional theory taken from Refs. [1, 3]. We are suspected that the contributions of direct radiation are insignificant at low neutrino energy. As a result of calculation, the value of the cross section of reaction (15) $\sigma_\gamma$ is

$$\sigma_\gamma = 0.61 \times 10^{-40} \text{ cm}^2,$$  

(17)

at $E_\gamma \geq 0.01 \text{ GeV}, E_{\mu}^{\text{max}} - E_\mu \geq 0.01 \text{ GeV}$ in center mass system. It constitutes 0.65\% from the value of the cross section $\sigma$ (10). The cross section for reaction (15) as a function of laboratory neutrino energy is shown in Fig. 7. In Fig. 8 and Fig. 9 the energy distributions of scattered muon and photon for this reaction at laboratory neutrino energy $E_{\nu}^{\text{lab}} = 0.7 \text{ GeV}$ are shown. Dalitz plot density for reaction (15) at this energy $E_{\nu}^{\text{lab}} = 0.7 \text{ GeV}$ is shown in Fig. 10. In the adopted approximation the angular distribution of a muon in reaction (15) will be like on an angular distribution of a muon in quasi-elastic reaction (11). In this case angular distribution of a photon in a center-of-mass system relatively to a direction of neutrino beam will be flat.

The current experiments with high statistics on measurement of neutrino oscillations will essentially influence on refinement of measurements of cross sections of quasi-elastic reaction and attendant reactions. They will help to better understand mechanism of interactions a neutrino of low energies with nucleons.
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Figure 1:
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Fig. 1. Cross sections for the quasi-elastic process $\nu_\mu + n \rightarrow \mu^- + p$ as a function of neutrino energy in conventional theory with parameters taken from [1, 3].

Fig. 2. The neutrino interaction with $d$-quark in a laboratory system.

Fig. 3. Diagram of process $\nu_\mu + n \rightarrow \mu^- + p$ on quark level at low neutrino energies.

Fig. 4. Angular distribution of a muon for reaction $\nu_\mu + n \rightarrow \mu^- + p$ in laboratory system at $E_{\nu}^{lab} = 0.7 \text{ GeV}$ from quark model.

Fig. 5. Angular distribution of a muon for reaction $\nu_\mu + n \rightarrow \mu^- + p$ in laboratory system at $E_{\nu}^{lab} = 0.7 \text{ GeV}$ from conventional theory.

Fig. 6. Diagrams of process $\nu_\mu + n \rightarrow \mu^- + p + \gamma$ on quark level at low neutrino energies.

Fig. 7. Cross section for reaction $\nu_\mu + n \rightarrow \mu^- + p + \gamma$ as a function of laboratory neutrino energy.

Fig. 8. Energy distribution of scattered muons for reaction $\nu_\mu + n \rightarrow \mu^- + p + \gamma$ at $E_{\nu}^{lab} = 0.7 \text{ GeV}$.

Fig. 9. Energy distribution of photon for reaction $\nu_\mu + n \rightarrow \mu^- + p + \gamma$ at $E_{\nu}^{lab} = 0.7 \text{ GeV}$.

Fig. 10. Dalitz plot density for reaction $\nu_\mu + n \rightarrow \mu^- + p + \gamma$ at $E_{\nu}^{lab} = 0.7 \text{ GeV}$.