Measurement of double-polarization asymmetries in the quasi-elastic $^3\text{He}(\vec{e},\vec{e}'d)$ process

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We present a precise measurement of double-polarization asymmetries in the $^3\text{He}(\vec{e},\vec{e}'d)$ reaction. This particular process is a uniquely sensitive probe of hadron dynamics in $^4\text{He}$ and the structure of the underlying electromagnetic currents. The measurements have been performed in and
around quasi-elastic kinematics at $Q^2 = 0.25 \text{ (GeV}/c)^2$ for missing momenta up to 270 MeV/c. The asymmetries are in fair agreement with the state-of-the-art calculations in terms of their functional dependencies on $p_m$ and $\omega$, but are systematically offset. Beyond the region of the quasi-elastic peak, the discrepancies become even more pronounced. Thus, our measurements have been able to reveal deficiencies in the most sophisticated calculations of the three-body nuclear system, and indicate that further refinement in the treatment of their two- and/or three-body dynamics is required.

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The $^3\text{He}$ nucleus lies at the very heart of nuclear physics and, along with the deuteron, represents the perfect playground to test nuclear dynamics (see, for example, [1,3] and references therein). The understanding of its structure has far-reaching implications not only for nuclear physics itself, but also for a variety of $^3\text{He}$-based experiments seeking to extract the neutron information by exploiting $^3\text{He}$ as an effective neutron target. These experiments rely on a virtually perfect theoretical knowledge of the ground-state spin structure of $^3\text{He}$. In particular, the statistical precision of double-polarization experiments on $^3\text{He}$ has become comparable to the systematic uncertainty implied by our imperfect knowledge of the polarization of the protons and the neutron within the polarized $^3\text{He}$ nucleus. This increase in precision needs to be matched by the best theoretical models which, in turn, require increasingly accurate input to adjust their parameters, complete understanding of the spin and isospin dependence of the reaction-mechanism effects such as final-state interactions (FSI) and meson-exchange currents (MEC), as well as an evaluation of the possible role of three-nucleon forces.

The most fruitful approach to studying the $^3\text{He}$ nucleus is by electron-induced knockout of protons, neutrons, and deuterons. In this paper we focus on the deuteron channel. In the $^3\text{He}(e,e'd)\text{p}$ reaction, the virtual photon emitted by the incoming electron transfers the energy $\omega$ and momentum $q$ to the $^3\text{He}$ nucleus. The process is best studied by measuring its response as a function of the magnitude of its missing momentum, which is defined as the difference between the momentum transfer and the detected deuteron momentum, $p_m = |q - p_4|$, hence $p_m$ corresponds to the momentum of the recoiled proton.

The unpolarized $^3\text{He}(e,e'd)$ process has been studied at Bates and NIKHEF facilities [4,7], yielding information on nucleon momentum distributions, isospin structure of the currents, FSI, and MEC. However, these measurements lacked the selective power of those experiments that exploit polarization. Only a handful of such experiments exist. The $^3\text{He}(e,e'p)\text{pn}$ and $^3\text{He}(e,e'p)\text{d}$ channels have been studied at NIKHEF [8] and Mainz [9,10], but no published data on the polarized $^3\text{He}(e,e'd)\text{p}$ exist, chiefly due to the fact that previous experiments, though attempted, lacked present-day highly polarized beams and targets, which resulted in poor experimental figures-of-merit and prohibitive uncertainties.

It has been shown, both in the diagrammatic approach [11,13], as well as in independent full Faddeev calculations of the Hannover/Lisbon (H/L) [14,17] and the Bochum/Krakow (B/K) [18,19] groups, that the $^3\text{He}(e,e'd)\text{p}$ reaction exhibits strong sensitivities to the sub-leading components of the $^3\text{He}$ ground-state wavefunction and, possibly, three-nucleon forces. Due to a particular isoscalar-isovector interference, this channel is also a unique source of information on the isospin structure of the electromagnetic current. It is the sensitivity brought about by the polarization degrees of freedom, augmented by the extended lever arm in $p_m$, that lends the present experiment its benchmark strength. Especially the extended kinematic coverage in $p_m$ up to 270 MeV/c represents a crucial advantage, because the calculations enumerated above indicate that the manifestations of various $^3\text{He}$ wave-function components exhibit very different signatures as functions of $p_m$. Moreover, these $p_m$-dependencies in each $^3\text{He}$ breakup channel appear to be rather distinct.

In the case of polarized beam and polarized target, the cross-section for the $^3\text{He}(e,e'd)\text{p}$ reaction has the form

$$
\frac{d\sigma(h,\vec{S})}{d\Omega} = \frac{d\sigma_0}{d\Omega} \left[ 1 + \vec{S} \cdot \vec{A}^0 + h(A_e + \vec{S} \cdot \vec{A}) \right],$$

where $d\Omega = d\Omega_4 dE_\text{p} d\Omega_4$ is the differential of the phase-space volume, $\sigma_0$ is the unpolarized cross section, $\vec{S}$ is the spin of the target, and $h$ is the helicity of the electrons. The $A^0$ and $A_e$ are the asymmetries induced by the polarization of only the target or only the beam, respectively, while the spin-correlation parameter $\vec{A}$ is the asymmetry when both the beam and the target are polarized. If the target is polarized only in the horizontal

![FIG. 1. Schematic drawing of the experimental setup. The orientations of the in-plane target polarization along the beamline and perpendicular to it correspond to the spherical angles about the $\vec{q}$-vector of $\theta^* = 71^\circ$ and $\theta^* = 160^\circ$, respectively, with $\phi^* = 0^\circ$ in both cases.](image-url)
plane defined by the beam and scattered electron momenta (see Fig. 1), the term $S \cdot A^0$ does not contribute \( \tilde{A} \), while $A_e$ is parity-suppressed and is negligible with respect to $\tilde{A}$.

The orientation of the target polarization is defined by the angles $\theta^*$ and $\phi^*$ in the frame where the $z$-axis is along $\mathbf{q}$ and the $y$-axis is given by $\mathbf{p}_e \times \mathbf{p}'$. Any component of $\tilde{A}$, i.e., the asymmetry at given $\theta^*$ and $\phi^*$ is then

$$A(\theta^*, \phi^*) = \frac{(d\sigma/d\Omega)_+ - (d\sigma/d\Omega)_-}{(d\sigma/d\Omega)_+ + (d\sigma/d\Omega)_-},$$

where the subscript signs represent the beam helicities.

In this paper we report measurements of these asymmetries in the $^3\text{He}(e, e'd)$ process in quasi-elastic kinematics at the average four-momentum transfer of $Q^2 = q^2 - \omega^2 = 0.25 \text{ (GeV/c)}^2$, performed during the E05-102 experiment at the Thomas Jefferson National Accelerator Facility in experimental Hall A [20].

We used an electron beam with an energy of 2.425 GeV and currents in excess of 10 mA. The beam was longitudinally polarized, with an average polarization of $P_e = (84.3 \pm 2.0)\%$ measured by a Møller polarimeter. The beam helicity was flipped at 30 Hz in $++$ or $−−$ structures in pseudorandom sequence.

The beam was incident on a 40 cm-long glass target cell containing the $^3$He gas at approximately 9043 g/cm$^2$, which was polarized by hybrid spin-exchange optical pumping [21,24]. The in-plane orientation of the polarization was maintained by two pairs of Helmholtz coils. To measure the $A(160^\circ, 0^\circ)$ asymmetry, the coils were used to rotate the $^3\text{He}$ spin vector to the left of the beam, at $160^\circ$ with respect to $\mathbf{q}$, while for the $A(71^\circ, 0^\circ)$ asymmetry it was maintained along the beamline, at $71^\circ$ with respect to $\mathbf{q}$ (both values are averages over the whole spread of angles). Electron paramagnetic resonance and nuclear magnetic resonance [25,27] were used to monitor the polarization of the target, $P_\tau$, which was between 50 % and 60 % throughout the experiment and was taken into account on a run-by-run basis.

The scattered electrons were detected by a High-Resolution magnetic Spectrometer (HRS) positioned at $\theta_e = 12.5^\circ$ and equipped with a detector package consisting of a pair of scintillator planes used for triggering and time-of-flight measurements, vertical drift chambers for particle tracking, and a gas Čerenkov counter and lead-glass calorimeters for particle identification.

The ejected deuterons and protons were detected by the large-acceptance spectrometer BigBite equipped with a detector package optimized for hadron detection [28], consisting of a pair of multi-wire drift chambers used for tracking and two scintillator planes used for triggering, time-of-flight determination, and particle identification.

The electrons in the HRS were selected by applying cuts on the Čerenkov detector signals. The most reliable selection of deuterons in BigBite was achieved by using graphical cuts in two-dimensional histograms of scintillator ADC (particle energy loss) vs. particle momentum as determined from track reconstruction. Depending on the kinematics, $(1−2)\%$ of protons may become misidentified as deuterons, which has a minute influence on the final results. For the extraction of the asymmetries, only electron-deuteron coincidence events were retained, based on the measurement of coincidence time. Additional cuts on the location of the target vertex (to eliminate the contribution from the cell walls) and on the quality of the reconstructed tracks were used to further purify the event sample.

The experimental asymmetry for each orientation of the target polarization was determined as the relative difference between the number of coincidence events (after all cuts and background subtraction) corresponding to positive and negative beam helicities, $A_{\text{exp}} = (N_+ - N_-)/(N_+ + N_-)$, where $N_+$ and $N_-$ have been corrected for helicity-gated beam charge asymmetry, dead time and radiative effects. The corresponding physics asymmetries were calculated as $A = A_{\text{exp}}/(P_e P_\tau)$.

The resulting asymmetries as functions of $p_m$, shown in Fig. 2. The largest contribution to the systematic error of the measured asymmetries comes from the relative uncertainty in the target polarization, $P_\tau$, which has been estimated at $\pm 5\%$, followed by the uncertainty due to protons being misidentified as deuterons ($\pm 3\%$) and the absolute uncertainty of the beam polarization, $P_e$ ($\pm 2\%$). The uncertainty in the target orientation angle represents a minor contribution ($\pm 0.6\%$) to the total uncertainty, which adds up to $\approx 7\%$ (relative).

Figure 2 also shows the results of the state-of-the-art three-body calculations of the Hannover/Lisbon [14,17], Bochum/Krakow [18,19] and Pisa [29] groups. The B/K calculations are based on the AV18 nucleon-nucleon potential [30,31] and involve a complete treatment of FSI and MEC, but do not include three-nucleon forces; the Coulomb interaction is taken into account in the $^3\text{He}$ bound state. The H/L calculations are based on the coupled-channel extension of the charge-dependent Bonn potential [32] and also include FSI and MEC, while the $\Delta$ isobar is added as an active degree of freedom providing a mechanism for an effective three-nucleon force and for exchange currents. Point Coulomb interaction is added in the partial waves involving two charged baryons.

The Pisa calculations are based on the AV18 interaction model (augmented by the Urbana IX three-nucleon force [33]), in which full inclusion of FSI is taken into account by means of the variational pair-correlated hyperspherical harmonic expansion, as well as MEC. Coulomb interaction is included in full (not only in the $^3\text{He}$ ground state). In contrast to the B/K and H/L approaches, the Pisa calculations are not genuine Faddeev calculations but are of equivalent precision and are expected to account for all relevant reaction mechanisms.
FIG. 2. (Color online.) The asymmetries $A(71^\circ,0^\circ)$ (top) and $A(160^\circ,0^\circ)$ (bottom) in the quasi-elastic $^3$He($e,e'd$) process as functions of missing momentum, compared to the acceptance-averaged calculations of the Hannover/Lisbon, Bochum/Krakow and Pisa groups. The double error bars on the data denote the statistical and total uncertainties (statistical and systematical part added linearly). The shaded (yellow) bands indicate the uncertainties implied by the acceptance-averaging procedure. They have been placed on the H/L curves because that calculation has been averaged over the finest mesh. Empty symbols (shifted for clarity) and thin curves denote the data and the corresponding H/L calculation with a cut on the quasi-elastic peak.


tances of HRS and BigBite, the theoretical asymmetries were averaged over these acceptances. The averaging was performed over the whole accepted region of the $(E_e',\theta_e)$ plane in 63 bins for the H/L calculations and 35 bins for the B/K and Pisa calculations. In each of these bins, the asymmetries were evaluated on a mesh of $p_m$ and deuteron azimuthal angles with respect to $q$, and interpolated. The acceptance-averaged theoretical asymmetries for each $p_m$ bin and their errors originating in this procedure were then obtained by evaluating a weighted average and mapped onto the seven $p_m$-bins used to display the measured asymmetries.

Neither of the three considered theories exactly reproduces the measured $A(160^\circ,0^\circ)$ asymmetry — which is fairly constant at about $-4\%$ throughout the $p_m$ range — except when the $\omega < 140$ MeV cut is applied. A hint of the zero-crossing of the measured asymmetry at high $p_m$ appears to be mirrored by the theoretical one, but it occurs at much lower $p_m$, and the predicted asymme-
tries, in addition to exhibiting a mismatch in the functional form, are roughly a factor of two too small. On the other hand, the measured $A(71^\circ,0^\circ)$ shows a clear zero-crossing at $p_m \approx 130$ MeV/c seen also in all three calculations, although it again occurs at much lower $p_m$.

One could argue that, at low $p_m$, the asymmetries for the deuteron knock-out process $^3$He($e,e'd$) should be similar to the asymmetries for electron scattering almost elastically off a polarized deuteron within polarized $^3$He. To assess this instructive, if simplistic, view we have equated the measured $A(160^\circ,0^\circ)$ and $A(71^\circ,0^\circ)$ for $^3$He at low $p_m$ ($p_m \leq 40$ MeV/c) with the corresponding $e$-$d$ asymmetries, computed at the same ($\theta^e,\phi^e$) and $Q^2$. By using appropriate deuteron form-factors [34] one can extract the vector and tensor spin orientations of the deuteron, $P_z$ and $P_{zz}$, inside $^3$He. From the data, we obtain $P_z(\exp) = 0.75 \pm 0.12$ and $P_{zz}(\exp) = 0.82 \pm 0.15$, indicating — under the above assumptions — that the deuteron in $^3$He is strongly polarized (spin “up”), the third component of zero being disfavored due to $P_{zz} \approx 1$. By applying the same procedure on the theoretical predictions, we obtain $P_z \approx 0.15$ and $P_{zz} \approx 1.1$ in all three cases (see Fig. 3). In this approximation, the inadequate theoretical description of both $^3$He($e,e'd$) asymmetries at low $p_m$ maps to an inadequacy in just one parameter, $P_z$, which is underestimated by a factor of at least 5, while $P_{zz}$ is only slightly overestimated.

FIG. 3. (Color online.) Effective vector and tensor deuteron polarizations (spin orientations) $P_z$ and $P_{zz}$ in $^3$He extracted from the data and theoretical predictions at $p_m \rightarrow 0$ in the approximation of e-$d$ elastic scattering (with 1σ and 2σ covariance ellipses on the experiment (green) and the numerically most reliable theory interpolation (H/L, yellow)). If the spin part of the $^3$He wave-function were given simply by a Clebsch-Gordan combination of the p and d parts, one would expect $P_z = 2/3$ and $P_{zz} = 0$.

The asymmetries as functions of energy transfer, $\omega$, are shown in Fig. 4. At low $\omega$, both measured asymmetries, $A(160^\circ,0^\circ)$ and $A(71^\circ,0^\circ)$, are fairly well reproduced in all approaches in terms of the functional form, but not
in magnitude: again, there is a systematic offset of the asymmetries of about one or two percent (absolute). At high $\omega$, all calculated asymmetries deviate from the measured ones, even in the H/L prediction that has been evaluated on the finest mesh, indicating that the dynamic input in the theoretical treatment of the process in the dip region is incomplete. Among other things, our data will now allow one to check which leading and sub-leading components make up the employed $^3$He wave-function that are consistent with the assumed dynamics, and thereby significantly advance our knowledge of the three-nucleon system.

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In conclusion, we have provided the world-first, high-precision data on a high-level physics observable at two different spin settings in a broad kinematic range. Three most sophisticated theoretical treatments of the $^3$He system are able to qualitatively account for the bulk of our data set; given the small magnitude of the asymmetries and the subtle interplay of the myriad of their ingredients, the agreement is actually quite good — in spite of the systematic offsets in $p_m$- and $\omega$-dependencies and deviations occurring in the dip region. Up to the level of this agreement, the basic theoretical assumptions on the hadron dynamics and on the structure of the electromagnetic currents have been justified, and it appears that a consistent $^3$He ground-state wave-function has been employed. However, the large precision of our measurements has been able to reveal deficiencies in the calculations, indicating a need for further refinement in the treatment of their two- and/or three-body dynamics. In fact, the detailed anatomy of the $p_m$ dependence of asymmetries is already the subject of a major ongoing theoretical effort.
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