Combination of B-mode and color Doppler mode using mutual information including canonical correlation analysis for breast cancer diagnosis

Tongjai Yampaka, Prabhas Chongstitvatana

Department of Computer Engineering, Chulalongkorn University, Bangkok, Thailand

Abstract

Aim: This study proposes the combination of B-mode and color Doppler mode using Mutual Information including Canonical Correlation Analysis (MI-CCA) to improve breast cancer diagnosis. Materials and methods: The dataset consisted of 53 benign lesions and 202 malignant lesions including B-mode, and color Doppler mode. Convolutional Neuron Networks (CNNs) was applied to automatically extract the features from breast ultrasound images. Then, MI-CCA was performed to fuse with maximized correlation. Finally, the classification model was built via the support vector machine technique to distinguish breast tumors. Diagnosis performances of single modes, combination modes, and other fusion strategies were compared. Results: The single B-mode obtained 90.92% accuracy, while the color Doppler mode obtained 97.16% accuracy. The MI-CCA fusion reveals a significant improvement with 98.80% accuracy. The results indicated that the fusion of two modes tended to offer a more accurate diagnosis than the single mode. In addition, the unsupervised-PCA was high (AUC 0.91, 95% CI [0.90, 0.91]) and no significant difference was observed with the unsupervised-CCA (AUC 0.90, 95% CI [0.84, 0.90]). The supervised-PCA was the lowest (AUC 0.93, 95% CI [0.91, 0.93]) and no significant difference was observed with the supervised-CCA (AUC 0.95, 95% CI [0.91, 0.94]). The proposed MI-CCA was the highest performance (AUC 0.99, 95% CI [0.93, 0.99]). These results indicated that the supervised strategies tended to give a more accurate diagnosis than unsupervised strategies. Conclusion: By using the combination of ultrasound modes, this approach achieves high performance compared with the single mode and other fusion strategies. Our methodology may be a beneficial tool for the early detection and diagnosis of breast cancer.

Keywords: breast cancer diagnosis; canonical correlation analysis; mutual information

Introduction

Breast cancer is the leading cause of death for women. Early screening is key to reduce the death rate. However, early screening requires accurate and reliable tools. Computer-Aided Diagnosis (CAD) has been developed to help the radiologists in the detection and diagnosis of breast cancer. In recent years, several previous studies have suggested that CAD systems can increase early cancer detection rates [1]. Ultrasound (US) has been used in screening as a supplementary tool especially in women with dense breast tissue [2]. The most abnormal breast lesions are easy to find by using the conventional US, while some lesions are still hidden. Therefore, multiple US modes have been performed to extract different information from lesions. For example, B-mode (Brightness) displays the acoustic impedance of a two-dimensional cross-section of tissue, while color Doppler mode displays blood flow, the motion of tissue over time, the location of blood, the presence of specific molecules, the stiffness of tissue, or the anatomy of a three-dimensional...
region. In previous studies, a single US mode has been improved. According to Ko et al [3], non-mass lesions were defined in four types. Positive predictive values could have been improved but the differentiation of NMLs by B-mode remained ambiguous and required further exploration. After intensive research, the elastography mode was well-established in cases of breast masses [4-5]. Guo et al [6] used contrast agent CEUS to depict the microcirculation of breast masses and provide qualitative and quantitative analysis for classifying breast lesions. These studies showed that the elastography mode could be helpful, but they note that it remained imprecise in its interpretation. Color Doppler mode, which used to supplement in the conventional US, showed high sensitivity, low angle dependency, and no aliasing [7]. Nevertheless, the compilation with recent clinical research [8] reported that the Doppler image alone was not able to significantly distinguish from a solid mass. Consequently, multiple US modes have been widely considered to combine B-mode and color Doppler mode for improving diagnosis performance. When B-mode was always examined together with color Doppler mode, the fusion of B-mode and color Doppler mode was performed [9,10]. These studies reported that combining the B-mode and color Doppler mode showed high accuracy and specificity to guide the decision for biopsy for non-mass breast lesions. Laurence et al [11] evaluated the performance fusion of B-mode, color Doppler, and SWE measurements. The result could significantly (p <0.001) improve characterization of testicular masses and, therefore, could avoid inappropriate total orchiectomy. Although previous studies demonstrated that the combination of US modes could improve the overall accuracy, these investigations were not performed with the CAD system. In addition, when the US examination is interpreted by an inexperienced radiologist, some pitfalls may appear by the human error. Lee et al [12] investigated the effect of CAD (S-detectTM) on breast US when inexperienced radiologists described and categorized breast lesions, especially in comparison with experienced radiologists. In their conclusion, the CAD system can be more beneficial and educational for less experienced radiologists than for experienced radiologists, not only when describing lesions, but also when determining if the lesion is malignant. Thus, automatic breast lesion detection established with CAD could be beneficial to help radiologists in breast US. To our knowledge, there have been few studies that automatically combined multiple US modes. The CAD using four state-of-the-art methodologies for breast lesion detection were introduced to improve diagnostic performance. For instance, Radial Gradient Index (RGI) Filtering [13] and Multifractal Filtering [14] have been widely cited works in this area, while Rule-based Region Ranking [15] and Deformable Part Models [16] also included two recent approaches. Although the state-of-the-art method took advantage, it was not designed for fusing multiple input images.

When the fusion of each dataset is required, different sources of information may be correlated or uncorrelated, so the fusion algorithm should be concerned about the correlation and ensure a compatible model between the two datasets. In recent years, the Principal Component Analysis (PCA) and Canonical Correlation Analysis (CCA), which linearly projects from two sets of random variables to low dimension sub-space and maximizes correlation, have been developed to fuse heterogeneous datasets. However, these methods do not consider the class separation compared to its individual modalities. To address this issue, supervised dimension reduction methods supervised-PCA and supervised-CCA [17,18] have been introduced.

These studies reported that the supervised method is able to fuse data from any number of modalities to a joint subspace that is robust to modality-specific noise. Motivated by recent success in supervised-CCA, this study proposes the Mutual Information Canonical Correlation Analysis (MI-CCA) strategy which is extended from the supervised-CCA for fusing US modes. Thus, this strategy is supposed to achieve a higher predictive performance as compared to single US mode and other fusion strategies such as unsupervised and supervised strategies including unsupervised-PCA, unsupervised-CCA, supervised-PCA, and supervised-CCA.

Material and method

Overview

The contribution of this study aims to fuse B-mode and color Doppler modes for breast cancer diagnosis including (a) feature extraction from two breast US modes (B-mode and color Doppler mode) using CNN, (b) extension of CCA via Mutual Information MI-CCA for data fusion, and (c) building a classifier model to distinguish breast tumor from benign and malignant. Figure 1 shows the overview of method.

Data Acquisition and Data Description

The experiment dataset has been provided by the Department of Radiology of Thammasat University and Queen Sirikit Center of Breast Cancer of Thailand. These lesion images consist of 53 benign lesions and 202 malignant lesions (including 255 B-mode images and 255 color Doppler mode images). Figure 2 shows the STRAD diagram of this approach. The patients’ information has been removed from the images. All lesions were con-
firmed by biopsy, thus it is absolutely clear whether the lesion was malignant or benign. In addition, the lesions were classified by three leading experts as malignant or benign. The consensus decision has been obtained by the majority voting rule (two out of three). The images were obtained by a Philips iU22 US machine in resolution ranges from 200×200 to 300×400 pixels based on the criteria of the provider.

Feature extraction using Deep Convolution Neuron Network: DCNNs

The features were automatically extracted by using computer vision methods. According to modern practice, a set of image features was extracted from the Deep Convolutional Neural Networks (DCNNs) which are powerful models that achieve impressive results for image classification to avoid the cost of hand-crafted feature extraction [19]. The success from many studies [20-23] was applied to large-scale image and video recognition. Inspired by their success, this approach was used to extract the features from US images. The feature extraction was carried out via DCNNs. During the training steps, the image was passed through a stack of convolutional (conv.) layers. These stack layers composed of the 5×5 filter to capture the notion of position followed by a 1×1 convolution filter. Then, spatial pooling layers were carried out by max-pooling layers. Non-linearity rectification (ReLU) activation function, which is a popular choice especially for deep networks, was used to activate the parameter values. Finally, the final layer is the softmax layer to classify the target class. The results of the DCNNs feature extraction is shown in Table I.

Canonical Correlation Analysis (CCA)

Features extracted from the feature selection were defined as:

\[ f(x_1), f(x_2), \ldots, f(x_i); i \in 1, 2, \ldots, n. \]
Given the first and the second dataset were defined as: 
\[ x_i^1, i \in \{1, 2, ..., n\}, x_i^2, i \in \{1, 2, ..., n\}. \]
Features matrix were defined as: 
\[ X_1 = [x_1^1, x_2^1, ..., x_n^1], X_2 = [x_1^2, x_2^2, ..., x_n^2]. \]

CCA accounts to fusion more than two datasets based on cross correlation. Although the correlation of more than two datasets were not easy to examine, the subspace which maximizes the correlations of each pair in sequential has been approximated instead [24]. Given n data samples comprise of \( n = n_1 + n_2 + ... + n_M \) features \( X_1, X_2, ..., X_M, M \in \{1, 2, ..., n\} \) \( X \) from M dataset, this implementation of pairwise CCA attempts a set of linear transformations: \( w_i \in R^{n \times 1}, w_i^2 \in R^{n \times 1}, w_M \in R^{n \times 1} \) such that the sum of the correlations across all pairs of modalities is maximized, shown as:

\[
\rho = \arg \max_{w_1, w_2, ..., w_M} \frac{\text{trace}(W_i^T C_{mm} W_i)}{\sqrt{\text{trace}(W_i^T C_{mm} W_i) \times \text{trace}(W_i^T C_{mm} W_i)}}
\]

where \( C_{mm} \in R^{n \times M} C_{ii} \in R^{n \times M}, \) and \( C_{mt} \in R^{n \times M} \) are the covariance matrices of the features \( X_1 \) and \( X_2 \), respectively. If \( X_1 \) and \( X_2 \) are independent, then knowing \( X_1 \) does not give any information about \( X_2 \), their mutual information is zero. Followed by this concept the parametric distributions over feature and target class, it is convenient to revise from the equation (2), shown as:

\[
H(f(\cdot); y) = \sum_{f(\cdot) \in X} \sum_{y \in Y} p(f(\cdot); y) \log \left( \frac{p(f(\cdot); y)}{p(f(\cdot)) p(y)} \right) (3)
\]

where the set of \( f(\cdot) \) is final output from DCNNs networks, and \( Y \) is the possible target class. The mutual information scores \( H_1(f(x_1); Y), H_2(f(x_2); Y), ..., H_k(f(x_k); Y) \) were computed from the equation (3). Then, the features \( j(\cdot) \) which correspond over the mean score would be selected to the CCA task, shown as:

\[
j_1(f(x_1); Y) > \text{mean}_{H_1} \quad \text{and} \quad j_2(f(x_2); Y) > \text{mean}_{H_2}
\]

where superscript 1 is the first dataset and superscript 2 is the second dataset, respectively. The objective function can be formulated as the following equation (1) that is modified from standard CCA to MI-CCA, shown as:

\[
\rho = \arg \max_{\omega_1, \omega_2, ..., \omega_M} \frac{\text{trace}(W_i^T C_{mm} W_i)}{\sqrt{\text{trace}(W_i^T C_{mm} W_i) \times \text{trace}(W_i^T C_{mm} W_i)}} (4)
\]

where the covariance matrices \( C_{ii} \) were replaced to \( \hat{C}_{ii}, \hat{C}_{22}, \) and \( \hat{C}_{12} \) that were calculated from \( j_1(x_1) \) and \( j_2(x_2) \).

**Data fusion in the context of MI-CCA**

Two modalities can be used to represent in the fusion space. Given \( n \) embedding components \( u_i^1, i \in \{1, 2, ..., n\}, \) are expressed via \( u_i^1 = W_1^T x_1 \) and \( v_i^1, i \in \{1, 2, ..., n\} \) are expressed via \( v_i^1 = W_2^T x_2 \). The embedding components \( u_i^1 \), \( v_i^1 \) will be included in the fusion space based on the \( k\)-largest \( \lambda \) (which is the variance ratio). The fusion space was written as:

\[
S = \text{concatenate}(u_i^1, v_i^1) (5)
\]

where \( i \) is the number of embedding components that corresponding to the top \( k\)-largest explain variance scores. The coordinate of \( f \) in the fusion space is mostly used for visualizing the prediction model instead of the original variables. After the fusion step, the classification task was performed to classify the breast lesions. Table II shows the proposed algorithm of MI-CCA.

**Comparative Data Fusion Strategies**

While dimension reduction methods such as CCA or PCA are able to fusion for 2 views, when used for classification, these representations do not consider class separation compared to its individual modalities. Therefore, supervised dimension reduction methods sPCA and sCCA were introduced. This study presents MI-CCA, which considers the labeled data to improve classification performance compared to supervised dimension reduction methods. The MI between random variables \( X \) and \( Y \) can estimate the underline probability distribution from the posterior knowledge of the pointwise mutual information \( H(X; Y) \). If \( X \) given \( Y \) are the events, then the true frequencies of all combinations of \( (x; y) \) pairs can be estimated by counting the number of times each pair occurs in the data. The mutual information scores were computed using the equation, shown as:

\[
H(X; Y) = \sum_{x \in X} \sum_{y \in Y} p(x, y) \log \left( \frac{p(x, y)}{p(x)p(y)} \right) (2)
\]
sCCA are introduced. This study aims to develop a fused algorithm with a higher predictive performance as compared to other unsupervised strategies and supervised strategies including unsupervised PCA, unsupervised CCA, supervised PCA, and supervised CCA.

**Statistical analysis**

**Experiment 1: Exploration of correlation analysis via Pearson correlation**

Because the objective of the data fusion method is the strongest correlation between two datasets, the Pearson correlation was used to measure the distance of linear relationships between variables to confirm our contribution and compare between other strategies. When the correlation coefficient is close to 1 or −1, their correlation is the strongest. The correlation coefficient is close to 0, their correlation is weak. The calculation formula is as follows:

\[ \rho(X, Y) = \frac{\text{cov}(X, Y)}{\sigma_X \sigma_Y} \]

where \( \text{cov} \) is the covariance, \( \sigma_X \) is the standard deviation of \( X \), and \( \sigma_Y \) is the standard deviation of \( Y \).

**Experiment 2: Comparing the fusion of B-mode and color Doppler modes vs. single US mode**

Confusion matrices were used to evaluate the performance and compared with single B-mode and color Doppler mode. These matrices computed sensitivity (true positive rate), specificity (true negative rate) and accuracy of models. The predictive formulas were defined as:

\[ \text{Sensitivity} = \frac{TP}{TP + FN} \quad (7), \quad \text{Specificity} = \frac{TN}{TN + FP} \quad (8), \]

\[ \text{Accuracy} = \frac{TP + TN}{TP + FP + TN + FN} \quad (9) \]

**Experiment 3: Comparing MI-CCA fusion vs. other fusion methods**

The comparison was the receiver operating characteristic curve (AUC). ROC is a probability curve and AUC represents the degree or measure of separation. It shows the capable of distinguishing between classes. The higher AUC shows a better model for distinguishing between patients with benign and malignant lesions. The ROC curve is plotted with TPR against the FPR where TPR is on y-axis and FPR is on the x-axis.

\[ TPR = \frac{TP}{TP + FN} \quad (10), \quad FPR = 1 - \text{Specificity} \quad (11) \]

where TP is true positive, TN is true negative, FP is false positive and FN is false negative.

**Results**

**Experiment 1: Exploration of correlation analysis via Pearson correlation**

Fig 3a shows the comparisons of Pearson correlation of unsupervised and supervised strategies. First, the unsupervised strategies (fig 3b, 3c) showed that unsupervised PCA had a lower correlation (0.30) than unsupervised CCA (0.90). Second, the supervised strategies (fig 3d) showed that supervised PCA had the lowest correlation (0.08). The supervised CCA (fig 3e) had an inverse correlation (-0.80), while proposed MI-CCA (fig 3f) had a lower correlation than supervised CCA. These results indicate that the unsupervised strategies seem to be the relevant information between the two datasets rather than supervised strategies. The unsupervised strategies are performed to maximize variable correlation, while the supervised strategies not only are performed to maximize variable correlation but also performed to maximize the class label.

**Experiment 2: Comparing the fusion of B-mode and color Doppler modes vs. single US mode**

Table III shows the model performance in sensitivity, specificity, and accuracy. The results indicated that the fusion of two modes tended to achieve a high diagnostic accuracy.

| Mode                  | Sen% | Sp%  | Ac%  |
|-----------------------|------|------|------|
| B-mode                | 92.11| 86.92| 90.92|
| color Doppler mode    | 98.12| 94.23| 97.61|
| MI-CCA Fusion         | 98.66| 96.15| 98.80|

Se, sensitivity; Sp, specificity; Ac, accuracy
Experiment 3: Comparing MI-CCA fusion vs. other fusion methods

Fig 4 shows the comparisons of breast tumor classification accuracy of unsupervised strategies and supervised strategies. First, (fig 4a) unsupervised PCA was high (AUC 0.91, 95% CI [0.90, 0.91]) and no significant difference was observed with the unsupervised CCA (AUC 0.90, 95% CI [0.84, 0.90]). Second, (fig 4b) the supervised PCA was the lowest (AUC 0.93, 95% CI [0.91, 0.93]) and no significant difference was observed with the supervised CCA (AUC 0.95, 95% CI [0.91, 0.94]). The mutual information scores that were over mean would be selected (fig 5) for MI-CCA. The proposed MI-CCA was the highest performance (AUC 0.99, 95% CI [0.93,
MI-CCA is performed using high mutual information between variables and class labels. Therefore, the variables tend to be more compatible with the class labels than other supervised strategies. These results indicated that the supervised strategies tended to a more accurate diagnosis than unsupervised strategies. Figure 2 shows the final diagnosis in STARD diagram of this approach.

Discussion

The popular tool and effective technique for breast cancer screening is digital mammography. However, there are some limitations. For instance, the lesions in the dense breast are hidden by the surrounding tissue. Therefore, breast US has been used in alternative tools to complement breast cancer detection due to its ability, non-radiation, and high sensitivity [25]. The general abnormal breast lesions are easy to find by using the conventional US, while some cases are still hidden. Therefore, multiple US modes have been performed to extract different information from the lesions.

The recent additional US techniques have been suggested and applied in practice to improve diagnostic accuracy. Therefore, CAD has been developed to provide efficient interpretation or second opinion for a lesion detected on breast US [12]. For example, the US CAD system developed by Samsung Medison, Co, Ltd, Seoul, Korea provides additional morphologic analysis of breast masses to detect breast US according to the BI-RADS lexicon and assist in the final assessment for the detected breast masses [26]. According to previous studies using the CAD system, specificity can be improved for the diagnosis of malignant breast mass and assisted the radiologists [27-29]. However, previous studies consider only a single mode. To extend the previous studies, the multiple US modes were fused and applied to the computerized algorithm to improve diagnosis performance as a feature extraction, data fusion, and classification. The result showed an increase in sensitivity, specificity, and accuracy.

Regarding the classification performance, single color Doppler mode was more accurate than the single B-mode because color Doppler mode can display blood flow, motion of tissue over time, the location of blood, the presence of specific molecules, the stiffness of tissue, or the anatomy of a three-dimensional region. This information can be beneficial to improve diagnosis performance, whereas the fusion of B-mode and color Doppler mode achieve the highest performance by complementing the information with each other. In addition, our approach confirmed the previous study, who suggested that other methods may be reduced missing such as the explored correlation of image or integrated of double reading. Therefore, not only high accuracy but also the maximal correlation between fusion dataset has been important. Data fusion as described in Foster et al [30] noted that dataset X and Y will have similar information when there is a maximal correlation. CCA aim to explore the relationship between different views or a variety of datasets the many learning problems applied this technique with a great performance.

In practice the advantage of data fusion should meet two requirements [31]. First, the final layer should be accurate. Second, the fusion layers should be a high relationship among views. Our results differ from Andrew et al [32] that reported maximized the correlation of dataset. Although the proposed MI-CCA had a lower correlation, the mutual information was helpful to maximize the accuracy performance. In addition, early detection and diagnosis of breast cancer is critical for survival [33-35]. Early diagnosis requires an accurate and reliable tool to distinguish benign and malignant tumors. The major cancer screening problems are false negative to take effect with patients who lose the chance of early treatment. The false positive developed unnecessary surgery such as biopsy. Our experiments reduce the false positive and false negative; furthermore, overall accuracy is better than the previous works.

Some limitations of our study should be considered. First, the other information such as patient demographics and health history were not included. Second, other significant tumor characteristics such as dense breast or fat breast were considered. Finally, more sample datasets were included in the future work. In addition, like the clinicians’ decision, other medical evidence should be combined for diagnosis.

Conclusion

This study presents the combination of B-mode and color Doppler modes for improving the diagnosis performance using MI-CCA. Our methodology achieves high performance compared with single mode and other fusion strategies when applied in breast US to classify breast tumors.

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Conflict of interest: none
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