Optimization of Power Generation Grids: A Case of Study in Eastern Mexico

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Abstract: Optimization of energy resources is a priority issue for our society. An improper imbalance between demand and power generation can lead to inefficient use of installed capacity, waste of fuels, worse effects on the environment, and higher costs. This paper presents the preliminary results of a study of seventeen interconnected power generation plants situated in eastern Mexico. The aim of the research is to apply a linear programming model to find the system-optimal solution by minimizing operating costs for this grid of power plants. The calculations were made taking into account the actual parameters of each plant; the demand and production of energy were analyzed in four time periods of 6 h during a day. The results show the cost-optimal configuration of the current power infrastructure obtained from a simple implementation model in MATLAB® software. The contribution of this paper is to adapt a linear programming model for an electrical distribution network formed with different types of power generation technology. The study shows that fossil fuel plants, besides emitting greenhouse gases that affect human health and the environment, incur maintenance expenses even without operation. The results are a helpful instrument for decision-making regarding the rational use of available installed capacity.

Keywords: optimization; linear programming; energy central

1. Introduction

Due to the increase in energy demand, the requirement to reduce its costs, and the need for a transition from a centralized to a distributed power generation system, global integration of energy supply must be planned and managed. Proper management guarantees a more efficient and sustainable delivery. Thus, within the electricity generation sector, different variables and parameters must be considered to enhance its performance. Some of these considerations are the energy demand, the installed capacity, a plant’s ability to ramp up or shut down quickly, and generation costs, among other things [1,2]. Studies based in stochastic techniques have been implemented to forecast the generation or demand for short, medium, and long term analysis [3]. These techniques consider time interval series that allows historical data to be examined to establish the statistical behavior of these variables and predict the values that may occur in the future. [4–6]. These variables delineate the cost-optimal configuration of the power generation grid.

The optimization technique is a mathematical tool that finds the best solution for a modeled system. The solutions are formulated considering system restrictions [7,8], which permits efficient decision-making conditions. Using these optimization models in the energy industry brings benefits such as minimizing costs, increasing utilities, preventing harmful environmental effects, and defining optimal power flow. Thus, this type of tool allows energy generation processes to be more reliable, productive, and cost effective.
Otherwise, neglecting prediction models could impact energy production costs, profit reduction, electrical power losses, and the overuse of non-renewable resources [9].

By means of a mathematical model considering all the system variables and parameters, it is possible to obtain conditions that have an efficient energy system. Each plant’s conditions and the optimal distribution of its resources allow the reduction of expenses and losses generated in the power generation process [10,11]. Some of these methods and algorithms are linear programming (LP) [12], quadratic programming (QP) [13], multi-criteria optimization [14], genetic algorithms (GA) [15], particle swarm optimization (PSO) [16], simulated annealing (SA) [17], the ant colony (ACO) [18], Taboo search (TS) [19], bee colony (ABC) [20], and optimal control techniques [21]. These mathematical methods apply to any production system, no matter the nature or application.

Recently, genetic algorithms have been proposed to optimize power plants [22], where the objective is to minimize power losses in the transmission process. Additionally, the particle swarm algorithm [23] minimizes generation costs where it converges to a solution; its advantage is the reduced use of computational resources. However, the drawback of these metaheuristic algorithms is that they are optimal approximation algorithms and search for feasible solutions. Such solutions are close to the optimal and are not the most efficient, generating only local and not absolute optimal results [24].

The economic dispatch technique for optimizing electric power plants has been suggested as an attractive method [25,26]. This linear programming model finds the optimal solution for the generation system according to the parameters concerning minimization or maximization: For example, the minimization of operating costs in the generation of electrical energy [27,28]; the minimization of greenhouse gas emissions [29] from the different fossil fuel plants; and the economic dispatch (ED) problem in fossil fuel power systems including discontinuous prohibited zones, ramp rate limits, and cost functions [30]. Some other studies have addressed solving the economic dispatch problem concerning minimization of losses and costs in a microgrid incorporating renewable energy sources, but not on a large scale [30–34].

This paper presents an optimization study of an electric power generation plant network through the economic dispatch model, which is a linear programming scheme. The proposed model applies to one of the most significant energy production regions in Mexico, called the eastern zone. This region has different types of power generation technologies. Within the analysis presented, actual parameters such as the maximum and minimum powers of each plant, the ramp up and down according to the type of technology, variable costs, fixed costs, and shut-down costs are considered. Fluctuations in energy production by renewable energy plants are estimated based on a probability function according to the historical measured data of each renewable resource in the zone. The study allows a reduction of generation costs during four time periods, without risking the secure supply of energy. The applied model shows a day with 100 percent renewable energy output, 94.90% from hydroelectric plants, 4.32% from wind plants, and 0.78% from geothermal. These three renewable resources show to be profitable options due to their low generation costs and big environmental benefit. Furthermore, the study indicates that plants based on fossil fuels do not significantly contribute to satisfying the demand during the monitored period. This behavior is noticed because the variable costs are directly related to the cost of fuels, which means the operating cost of fossil fuels plants increases.

Power Energy Generation in Mexico

The supply of electrical energy in Mexico is provided through various interconnected transmission networks. Public and private electric utilities compose the national electricity system, and the Federal Electricity Commission, a state-owned electric company, is the institution that supplies electricity to consumers [35]. According to the National Ministry of Energy [36], Mexico has an installed capacity of 75,685.00 MW, of which fossil fuels generate 79.88%; the other 17.08% is generated by renewable energy, and 3.04% by other methods such as nuclear energy. In terms of daily peak demand, it is 48,750 Megawatts, which an
increase of around 15% annually due to population growth, economic development, and industrialization.

The energy distribution system in Mexico consists of nine zones, as shown in Figure 1. Each zone has its characteristics of supplying energy according to the requested demand [37].

![Figure 1. Mexican Electric System denoted by zones. The zone of interest is shaded (zone 8). [34].](image)

The eastern part of Mexico has 110 generation plants, of which the primary source is hydroelectric and wind energy, as shown in Figure 2. This feature is due to its geographical location and high wind potential.

![Figure 2. Classification of generation plants in the Eastern Zone of Mexico according to technology used [37].](image)
As shown in Figure 2, the range of generation technologies permits a higher installed capacity in the zone according to the regional demand. This feature allows 22% of energy generation to contribute to the Mexico national requirements [37] and supply other areas such as the Central and Peninsular zones. In the Central Zone, the population density is around 899 inhabitants per km$^2$. Big corporations established in this zone contribute to 27% of the country’s gross domestic product (GDP) [38]. Therefore, the energy demand is much higher compared to the supply capacity in the central zone. On the other hand, there is a high energy demand in the Peninsular Zone because it is a substantial touristic infrastructure [38]. Therefore, it is necessary to promote energy end-use efficiency and optimize energy resources in these zones. The following section describes the implemented model in our case study.

2. Materials and Methods

As we mentioned, economic dispatch is a mathematical model that aims to manage system resources. For our purposes, this model permits efficiently handling all power plant supplies in an interconnected network. The objective is to obtain the optimal combination in each generator’s contribution to satisfy the energy demand and minimize its generation costs. The modeling considerations incorporate real characteristic parameters of each of the plants to obtain useful results for decision-making. In the following, the proposed mathematical model is described.

2.1. Modeling for a Certain Time

In an electrical generation system, there are several plants with particular characteristics. These, concerning the central, are denoted by $j$, that is $j = 1, 2, \ldots, J$. Where $J$ is the total number of generation plants in the system and each one $j$ works under certain limits. No plant can operate below the minimum operating power, which is described as:

$$P_{min \cdot v_j} \leq P_j$$

where $P_{min}$ is the minimum power of the central and $v_j$ is a binary operating variable. If $v_j = 1$, it means that the central is working. When $v_j$ is multiplied by the minimum power, it will not be below its nominal value and $P_j$ is the optimal power to be generated by each plant. To exemplify these conditions, suppose we have a system of three plants and plant 1 has a minimum power of 45 MW, plant number two is 35 MW and plant 3 is 40 MW. Implementing these parameters in Equation (1), it remains:

$$45v_1 \leq P_1$$
$$35v_2 \leq P_2$$
$$40v_3 \leq P_3$$

On the other hand, no control unit can operate above the maximum operational power $P_{max}$:

$$P_j \leq P_{max \cdot v_j}$$

Similarly, if the plant $j$ is working, the power to be generated must not be exceeded. The power generated by each plant must satisfy the demand $D$ requested by the electrical distribution grid; therefore:

$$D = \sum_{j=1}^{J} P_j$$

On the other hand, demand fulfillment generates individual costs which determine the total cost of generation, called $R$. For this reason, resources must be correctly assigned to minimize them. Thus, the whole cost function $R$ is given as:
\[ R = \sum_{j=1}^{l} (A_j \cdot v_j + B_j \cdot p_j + M_j \cdot z_j) \quad (4) \]

The first term \( A_j \) indicates the fixed cost of plant \( j \) and \( v_j \) is the binary variable described above (\( v_j = 1 \) is working and \( v_j = 0 \) is off). The term \( B_j \cdot p_j \) corresponds to the contribution of the cost assumed to be proportional to the production of the plant, where \( B_j \) is the variable cost and \( p_j \) the production for the plant \( j \). Besides, a plant also generates costs just for being stopped. This contribution is represented by the third term \( M_j \cdot z_j \), where \( M_j \) is the cost of having each plant stopped and \( z_j \) is also a binary stop variable that takes the value 1 if plant \( j \) stops and 0 indicates the opposite case.

This model describes the conditions to satisfy energy demand in a given time, limiting the power plants’ administration because it does not allow long-term planning. The following section describes the mathematical considerations in the modeling for time intervals to have a more significant representation in the resources assigned.

2.2. Model for Various Periods

The problem of scheduling power plants by periods consists of determining for the planning horizon both the start-up and shut-down of each power plant and the allocation of energy to be generated. These three parameters must satisfy the demand in each cycle of time, reduce costs, and comply with specific technical and operational safety restrictions in each plant \( j \). These planning horizons are divided into a day by time cycles. These time cycles are denoted by \( k \), so the planning horizon consists of the periods: \( k = 1, 2, \ldots, K \), where \( K \) is determined by the number of cycles defined in total for the study. Each of the \( j \) power plants cannot operate below their minimum energy generation, being established for various periods such as:

\[ E_{\text{min}} j \cdot v_{jk} \leq E_{jk} \quad (5) \]

where \( E_{\text{min}} j \) is the minimum energy to generate plant \( j \) in period \( k \); \( E_{jk} \) is the energy that plant \( j \) will generate in period \( k \); and \( v_{jk} \) is the binary variable described above. Suppose, for example, we have a system of three plants and three established periods, if we talk about the minimum energy to be generated in plant 2 in period 3 it is established as:

\[ E_{\text{min}} 2 \cdot v_{2,3} \leq E_{2,3} \]

Similarly, the power plants cannot produce more than the established maximum energy \( E_{\text{max}} j \); then:

\[ E_{jk} \leq E_{\text{max}} j \cdot v_{jk} \quad (6) \]

The energy to be produced in each plant in one period cannot increase abruptly in the immediately following period above a maximum quantity. This energy is known as the maximum load rise ramp \( U_j \), expressed as:

\[ E_{jk} + E_{jk+1} \leq U_j \quad (7) \]

The difference between energy produced in the immediately following period and the current period’s energy must be less than or equal to the maximum rising ramp of \( U_j \) of the plant \( j \). Similarly, no power plant can reduce its energy production under a limit called the maximum load descent ramp \( F_j \). So:

\[ E_{jk} - E_{jk+1} \leq F_j \quad (8) \]

Additionally, it is convenient to define two conditions that allow setting the starting and braking for each plant, in order to have greater control of the costs that may be generated. For the first case, let us consider that a plant that is operating in a period \( k \) is
established to be in operation and a previous period $k - 1$ is also in operation. In this case, it cannot start in period $k$ expressed as:

$$v_{jk} - v_{jk-1} \leq y_{jk}$$

(9)

where $y_{jk}$ is also a binary start-up variable, and if $y_{jk} = 1$ indicates the central $j$ is working in a period $k$ and $y_{jk} = 0$ for the opposite case. In the same way, if a plant is in operation, it cannot be stopped and vice versa, therefore:

$$v_{jk} + z_{jk} = 1$$

(10)

where $z_{jk}$ is the stop binary variable that indicates $z_{jk} = 1$ plant $j$ is stopped in period $k$ and $z_{jk} = 0$ when not; thus, it is possible to establish an equation that determines the state and allows these conditions to be fulfilled, given by:

$$v_{jk} - v_{jk-1} + y_{jk} - z_{jk} \leq 0$$

(11)

To verify that the general conditions and any exchange are valid, consider the following particular example. Suppose that control unit 1 is stopped in period 1, but in the following period, it is in operation, which means that in period 2, it is going to start. Therefore it cannot be stopped in the same period 2. The equation for this situation is expressed:

$$v_{1,1} - v_{1,2} + y_{1,2} - z_{1,2} \leq 0$$

(12)

To verify that this last situation is consistent under the proposed model, consider the case that the power plant was off in period 1 and remained off in period 2, which is obtained from Equation (12):

$$0 - 0 + 0 - 1 \leq 0$$

$$-1 \leq 0$$

Thus, employing the example proposed in Equation (12), it is verified that all the variables describe the logic of possible states in the system. On the other hand, the proposed model must supply the demand in each period. In consequence:

$$D_k = \sum_{j=1}^{J} E_{jk}$$

(13)

where $D_k$ is the total demand to cover in period $k$, the proposed Equations (5)–(12) are the restrictions inherent to each power plant in the system, where it is sought to reduce generation scabs by satisfying the demand established in Equation (13).

The cost minimization $R$ now considered in all time intervals must include all the regular electric power production plants’ programming. Therefore, it must be expressed in terms of all possible contributions:

$$R = \sum_{k=1}^{K} \sum_{j=1}^{J} \left( A_j \cdot v_{jk} + B_j \cdot E_{jk} + C_j \cdot y_{jk} + M_j \cdot z_{jk} \right)$$

(14)

where it is the sum of all the costs of the plants in each of the periods. The first term of Equation (14) incorporates the fixed cost $A_j$ of each generation plant. The second term associates the variable cost $B_j$, considering that it is proportional to the plant’s production and directly related to the cost of fossil fuels. The next cost in this model is considered the start-up $C_j$ of a plant, where it is assumed to be constant throughout the periods. Finally, the fourth term of Equation (14) incorporates the cost $M_j$, generated when a plant is off. As can be seen, each of the costs described is established according to the state parameters defined by the activation or shut-down binary $v_{jk}$, $p_{jk}$, $y_{jk}$, and $z_{jk}$, respectively.
The conditions established to satisfy the different energy demands in the time intervals allow long-term planning, maintaining the optimal distribution of resources and minimizing the total cost of generation from the model as shown in Table 1.

### Table 1. Model equations.

| Equation Type                          | Mathematical Expression |
|----------------------------------------|--------------------------|
| **Minimum Energy**                     | \( E_{min_j} \cdot v_{jk} \leq E_{jk} \) |
| **Maximum Energy**                     | \( E_{jk} \leq E_{max_j} \cdot v_{jk} \) |
| **Maximum Load Rise Ramp**             | \( E_{jk+1} - E_{jk} \leq U_j \) |
| **Maximum Load Descent Ramp**          | \( E_{jk} - E_{jk+1} \leq F_j \) |
| **Start**                              | \( v_{jk} - v_{jk-1} \leq y_{jk} \) |
| **On/Stop**                            | \( v_{jk} + z_{jk} = 1 \) |
| **State**                              | \( v_{jk} - v_{jk-1} + y_{jk} - z_{jk} \leq 0 \) |
| **Demand**                             | \( v_{jk} - v_{jk-1} + y_{jk} - z_{jk} \leq 0 \) |

### 3. Implementation and Discussion of Results

The control area selected to carry out the study consists of 110 power plants that provide 16,992 MW of installed capacity with different technologies. The demand \( D \) in the area has a value from 6750 MW to 8500 MW on average per hour, according to the National Center for Energy Control (known by its spanish accronim, CENACE) in Mexico.

From 110 power plants, we select 17 representative power plants which correspond to 57% of the area’s installed capacity. This selection maintains the proportionality of the installed capacity of the area by type of technology. These plants have characteristic parameters such as maximum energy \( (E_{max_j}) \) and minimum energy \( (E_{min_j}) \), variable costs \( (B_j) \), fixed cost \( (A_j) \), start-up costs \( (C_j) \), and shut-down costs \( (M_j) \) as is shown in Table 2.
Table 2. Parameters of the Electric Power Plants [39].

| Central                  | $E_{minj}$ (MWh) | $E_{maxj}$ (MWh) | $B_j$ ($/MWh$) | $A_j$ ($/h$) | $C_j$ ($) | $M_j$ ($/h$) |
|-------------------------|------------------|------------------|----------------|-------------|----------|-------------|
| 1. Bioenergy            | 295.14           | 78.75            | 3.94           | 265.524     | 0        | 330         |
| 2. Combined cycle       | 2883.9           | 742.5            | 2.72           | 92.28       | 0        | 210         |
| 3. Combined cycle       | 5721.06          | 1474.5           | 2.69           | 90.174      | 0        | 216         |
| 4. Efficient Cogeneration | 2138.28         | 551.1            | 2.73           | 93.318      | 108.3    | 210         |
| 5. Internal Combustion  | 86.22            | 23.55            | 3.16           | 168.264     | 108.3    | 258         |
| 6. Wind power           | 294.9048         | 246              | 0              | 149.778     | 0        | 240         |
| 7. Wind power           | 450.4491         | 375.75           | 0              | 149.778     | 0        | 240         |
| 8. Wind power           | 420.7788         | 351              | 0              | 149.778     | 0        | 240         |
| 9. Geothermal           | 301.98           | 80.4             | 0.06           | 522.708     | 0        | 270         |
| 10. Hydroelectric       | 4728.24          | 1350             | 0              | 151.464     | 0        | 246         |
| 11. Hydroelectric       | 3152.16          | 900              | 0              | 151.464     | 0        | 246         |
| 12. Hydroelectric       | 12,608.64        | 3600             | 0              | 151.464     | 0        | 246         |
| 13. Hydroelectric       | 5673.888         | 1620             | 0              | 151.464     | 0        | 246         |
| 14. Nuclear power plant | 8742.9           | 2265             | 2.25           | 588         | 0        | 660         |
| 15. Thermal             | 2001.3           | 525              | 2.2            | 170.862     | 472.86   | 258         |
| 16. Thermal             | 647.64           | 172.8            | 3.94           | 265.524     | 468.6    | 330         |
| 17. Turbogas            | 715.5            | 181.05           | 4.19           | 51.102      | 216.6    | 120         |

For wind power plants, the maximum and minimum energy to be generated are obtained based on the statistics of the historical wind speed data of the place where they are located as reported by the Mexican ministry of energy [36]. The wind statistics are obtained through the Weibull probability density model, and in the same way with respect to hydroelectric plants, but it is a probability function of the flow and level they present.

For the model’s implementation, it is necessary to indicate the requested demand in each period of the area, establishing 52% of the total demand for representing the study plants as shown in Figure 3a, and we are assuming 5% additional to compensate for generation losses that could be generated at the time of transmission, which means a total of 57% being established. Therefore, four periods were established in which each period consists of 6 h in duration, as reflected in Figure 3b. It is worth mentioning that these data are real and were provided by CENACE based on monitoring carried out every hour over a three-week interval.

The model established by Equations (5)–(14) and applied to the geographical area described above was implemented using the MATLAB® programming tool, by means of the intlinprog function, which allows solving mixed-integer linear programming problems, and which has the structure as shown in Figure 4.
Figure 3. The behavior of demand in the Eastern Zone. (a) The corresponding demand in the Eastern Zone per hour. (b) Consumption across periods of 6 h.

\[
\begin{align*}
\text{min} & \quad f^T x \\
\text{subject to} & \quad A \cdot x \leq b \\
& \quad Aeq \cdot x = beq \\
& \quad lb \leq x \leq ub.
\end{align*}
\]

Figure 4. Intlinpro function syntax from MATLAB® [40].

Where \( f \) is a vector of the objective function, \( x \) is a vector of the binary variables of the problem, \( A \) is a matrix, with the values of the left side of the inequalities, and \( b \) is the vector of the right side of the inequalities. \( Aeq \) is a matrix with the values on the left side of the model equations, \( beq \) is the right side of the equations, \( lb \) and \( ub \) are a vector with the maximum and minimum values of the variables. For the generation of these matrices and vectors, the proper values of each plant established in Table 1 are taken, obtaining the matrices with the following dimensions: \( F_{272 \times 1}, \ X_{Intcon_{240 \times 1}}, \ A_{190 \times 272}, \ b_{190 \times 1}, \ Aeq_{72 \times 272}, \ beq_{72 \times 1}, \ lb_{272 \times 1}, \) and \( ub_{272 \times 1} \).

Once the matrices of the system were defined, the results presented in Tables 3–6 and Figures 5–8 were obtained. In them, the values for each variable defined in each of the defined periods are indicated.

In the first period, identified from 00:00 to 06:00 h, an energy demand of 21,832.52 MWh was managed. This demand is the lowest of the four periods considered because they are the first hours of the day and, consequently, cover less human activity. The power plants contributing to related demand are from technologies such as internal combustion, wind, geothermal, and hydroelectric, the contributions of which make it optimal, as shown in Table 3 and Figure 5a.
Table 3. Results of Period 1.

| Central | Power to Be Generated in 6 h | On $V_j$ | Start $Y_j$ | Stop $Z_j$ |
|---------|-----------------------------|---------|------------|------------|
| 1. Bioenergy | 0 | 0 | 0 | 1 |
| 2. Combined cycle | 0 | 0 | 0 | 1 |
| 3. Combined cycle | 0 | 0 | 0 | 1 |
| 4. Efficient Cogeneration | 0 | 0 | 0 | 1 |
| 5. Internal Combustion | 23.55 | 1 | 0 | 0 |
| 6. Wind power | 294.9048 | 1 | 0 | 0 |
| 7. Wind power | 450.4491 | 1 | 0 | 0 |
| 8. Wind power | 420.7788 | 1 | 0 | 0 |
| 9. Geothermal | 80.4 | 1 | 0 | 0 |
| 10. Hydroelectric | 4728.24 | 1 | 0 | 0 |
| 11. Hydroelectric | 3152.16 | 1 | 0 | 0 |
| 12. Hydroelectric | 11062.0373 | 1 | 0 | 0 |
| 13. Hydroelectric | 1620 | 1 | 0 | 0 |
| 14. Nuclear power plant | 0 | 0 | 0 | 1 |
| 15. Thermal | 0 | 0 | 0 | 1 |
| 16. Thermal | 0 | 0 | 0 | 1 |
| 17. Turbogas | 0 | 0 | 0 | 1 |

Table 4. Results of Period 2.

| Central | Power to Be Generated in 6 h | On $V_j$ | Start $Y_j$ | Stop $Z_j$ |
|---------|-----------------------------|---------|------------|------------|
| 1. Bioenergy | 0 | 0 | 0 | 1 |
| 2. Combined cycle | 0 | 0 | 0 | 1 |
| 3. Combined cycle | 0 | 0 | 0 | 1 |
| 4. Efficient Cogeneration | 0 | 0 | 0 | 1 |
| 5. Internal Combustion | 23.55 | 1 | 0 | 0 |
| 6. Wind power | 294.91 | 1 | 0 | 0 |
| 7. Wind power | 450.45 | 1 | 0 | 0 |
| 8. Wind power | 420.78 | 1 | 0 | 0 |
| 9. Geothermal | 80.4 | 1 | 0 | 0 |
| 10. Hydroelectric | 4728.24 | 1 | 0 | 0 |
| 11. Hydroelectric | 3152.16 | 1 | 0 | 0 |
| 12. Hydroelectric | 12,608.64 | 1 | 0 | 0 |
| 13. Hydroelectric | 2708.79 | 1 | 0 | 0 |
| 14. Nuclear power plant | 0 | 0 | 0 | 1 |
| 15. Thermal | 0 | 0 | 0 | 1 |
| 16. Thermal | 0 | 0 | 0 | 1 |
| 17. Turbogas | 0 | 0 | 0 | 1 |
Table 5. Results of period 3.

| Central                  | Power to Be Generated in 6 h | On $V_j$ | Start $Y_j$ | Stop $Z_j$ |
|--------------------------|------------------------------|----------|-------------|------------|
| 1. Bioenergy             | 0                            | 0        | 0           | 1          |
| 2. Combined cycle        | 0                            | 0        | 0           | 1          |
| 3. Combined cycle        | 0                            | 0        | 0           | 1          |
| 4. Efficient Cogeneration| 0                            | 0        | 0           | 1          |
| 5. Internal Combustion   | 23.55                        | 1        | 0           | 0          |
| 6. Wind power            | 294.91                       | 1        | 0           | 0          |
| 7. Wind power            | 450.45                       | 1        | 0           | 0          |
| 8. Wind power            | 420.78                       | 1        | 0           | 0          |
| 9. Geothermal            | 80.4                         | 1        | 0           | 0          |
| 10. Hydroelectric        | 4728.24                      | 1        | 0           | 0          |
| 11. Hydroelectric        | 3152.16                      | 1        | 0           | 0          |
| 12. Hydroelectric        | 12,608.64                    | 1        | 0           | 0          |
| 13. Hydroelectric        | 4901.96                      | 1        | 0           | 0          |
| 14. Nuclear power plant  | 0                            | 0        | 0           | 1          |
| 15. Thermal              | 0                            | 0        | 0           | 1          |
| 16. Thermal              | 0                            | 0        | 0           | 1          |
| 17. Turbogas             | 0                            | 0        | 0           | 1          |

Table 6. Results of period 4.

| Central                  | Power to Be Generated in 6 h | On $V_j$ | Start $Y_j$ | Stop $Z_j$ |
|--------------------------|------------------------------|----------|-------------|------------|
| 1. Bioenergy             | 0                            | 0        | 0           | 1          |
| 2. Combined cycle        | 0                            | 0        | 0           | 1          |
| 3. Combined cycle        | 0                            | 0        | 0           | 1          |
| 4. Efficient Cogeneration| 0                            | 0        | 0           | 1          |
| 5. Internal Combustion   | 23.55                        | 1        | 0           | 0          |
| 6. Wind power            | 294.91                       | 1        | 0           | 0          |
| 7. Wind power            | 450.45                       | 1        | 0           | 0          |
| 8. Wind power            | 420.78                       | 1        | 0           | 0          |
| 9. Geothermal            | 80.4                         | 1        | 0           | 0          |
| 10. Hydroelectric        | 4728.24                      | 1        | 0           | 0          |
| 11. Hydroelectric        | 3152.16                      | 1        | 0           | 0          |
| 12. Hydroelectric        | 12,608.64                    | 1        | 0           | 0          |
| 13. Hydroelectric        | 3675.32                      | 1        | 0           | 0          |
| 14. Nuclear power plant  | 0                            | 0        | 0           | 1          |
| 15. Thermal              | 0                            | 0        | 0           | 1          |
| 16. Thermal              | 0                            | 0        | 0           | 1          |
| 17. Turbogas             | 0                            | 0        | 0           | 1          |
Figure 5. Generation and Energy in periods 1 and 2. (a) Period 1. (b) Period 2.

Figure 6. Generation and Energy in periods 3 and 4. (a) Period 3. (b) Period 4.
Table 4 shows the model variables’ results in period 2, where the demand to be satisfied is 24,467.92 MWh, as shown in Figure 5b.

Additionally, in Period 3 (see Table 5 and Figure 6a), the demand to be satisfied is the highest of the four periods, corresponding to 26,661.1 MWh. Here, the power plants that contribute to cover most of the demand are wind and hydroelectric. This aspect can be an
opportunity to incorporate clean technologies for the generation of energy that satisfies the requested demand.

Finally, in period 4, the demand to satisfy is 25,434.44 MWh; the results of which are produced by the model and are described in Table 6 and Figure 6b. It is in this period where the most significant contribution is observed from renewable energies. In this way, we can observe that the model complies with what is proposed because it satisfies the demand for the established periods.

Figure 7 shows the different plants that comprise the study carried out and the contributions of each one of them in the different periods established to satisfy the demand in each one.

The costs obtained in period 1 are illustrated in Figure 8, which shows the behavior, and this trend continues in the following periods. The highest costs come from fossil fuel technology plants. This is mainly due to the various fossil fuels’ high variable costs and the various costs attributed to these technologies. The lowest costs are from clean generation sources because maintenance costs are lower and provide benefits for the ecosystem.

4. Conclusions

In this work, the optimization of an Economic Dispatch model for a power supply network located in Mexico’s eastern zone is presented. The established model incorporates real parameters and intrinsic restriction to each plant. The energy production of the renewable energy plants was estimated by means of probability functions according to the historical data of the location. The considerations incorporate the various types of generation costs and seek their minimization. This allows the state logic to be fulfilled at all times, as can be seen in Tables 3–6; this is due to Equations (10)–(12), which do not allow a power plant to be off and on at the same time, as well as also that a plant does not start in a period when it was on in the previous period. In addition, all costs can be better accounted for by relating them to binary variables, such as the shutdown, operation, and start-up of a plant.

The results show a majority participation of clean energy plants during the study time period. The model shows the costs that each of the power plants has in period 1, and it reflects the lower costs of the power generation mix that contribute to satisfying the demand, being in this case a combination of clean energy plants. In contrast, the study shows that some non-operating fossil fuel plants generate even higher costs than renewable plants in operation.

The mathematical model could be an important tool in decision-making in plant planning and a diagnostic mode that allows visualizing those plants with very high costs when incorporating new electricity generation sources. In future works, longer periods of time should be addressed (one year) to obtain more significant results from the most suitable energy generation mix for the zone. Energy distribution will be incorporated due to the importance of power plants, location, and the loads due to the loss of lines at transmission and their capacities. In this way, there is a broader panorama to analyze the system as a decision-making tool.

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