Observability of evaporating lava worlds

M. Zilinskas\textsuperscript{1}, C.P.A. van Buchem\textsuperscript{1}, Y. Miguel\textsuperscript{1,2}, A. Louca\textsuperscript{1}, R. Lupu\textsuperscript{3}, S. Zieba\textsuperscript{4,1}, and W. van Westrenen\textsuperscript{5}.

\textsuperscript{1} Leiden Observatory, Leiden University, Niels Bohrweg 2, 2333CA Leiden, the Netherlands
\textsuperscript{2} SRON Netherlands Institute for Space Research, Niels Bohrweg 4, 2333 CA Leiden, the Netherlands
\textsuperscript{3} Eureka Scientific Inc, Oakland, CA 94602
\textsuperscript{4} Max-Planck-Institut für Astronomie, Königstuhl 17, D-69117 Heidelberg, Germany
\textsuperscript{5} Department of Earth Sciences, Vrije Universiteit Amsterdam, De Boelelaan 1085, 1081 HV Amsterdam, the Netherlands

e-mail: zilinskas@strw.leidenuniv.nl

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ABSTRACT

Lava worlds belong to a class of short orbital period planets reaching dayside temperatures high enough to melt their silicate crust. Theory predicts that the resulting lava oceans outgas their volatile components, attaining equilibrium with the overlying vapour. This creates a tenuous, silicate-rich atmosphere that may be confined to the permanent dayside of the planet. The James Webb Space Telescope (JWST) will provide the much needed sensitivity and spectral coverage to characterise these worlds. In this paper, we assess the observability of characterisable spectral features by self-consistently modelling silicate atmospheres for all the currently confirmed targets having sufficient sub-stellar temperatures (> 1500 K). To achieve this we used outgassed equilibrium chemistry and radiative transfer methods to compute temperature-pressure profiles, atmospheric chemical compositions, and emission spectra. We explore varying melt compositions, free of highly volatile elements, accounting for possible atmospheric evolution. Our models include a large number of neutral and ionic species, as well as all up-to-date opacities. The results indicate that SiO and SiO\textsubscript{2} infrared features are the best unique identifiers of silicate atmospheres, which are detectable using the MIRI instrument of JWST. Detection of these two species in emission would allow for strong constraints on the atmospheric thermal structure and possibly the composition of the melt. We also propose that certain species, for example TiO, may be directly tied to different classes of melts, possibly revealing surface and interior dynamics. Currently, there are nearly a dozen confirmed lava planets ideal for characterisation of silicate atmospheres using JWST, with two of these already accepted for the initial General Observers programme.

Key words. Planets and satellites: atmospheres – Planets and satellites: terrestrial planets – Techniques: spectroscopic

1. Introduction

The James Webb Space Telescope (JWST) Cycle 1 General Observers (GO) programme has approved observations of 17 rocky exoplanets\textsuperscript{1} with eight most irradiated on the list having sub-stellar temperatures large enough to sustain a molten surface crust. Close-in rocky planets, due to their short orbital periods, are readily found by survey missions like the Transiting Exoplanet Survey Satellite (TESS; Ricker et al. 2014). Because of their large day-side temperatures, which allow for formation of silicate atmospheres, lava planets are particularly interesting targets for follow up characterisation with infrared spectroscopy. Figure\textsuperscript{1} showcases all currently confirmed < 2 R\textsubscript{⊕} (along with TESS candidates) transiting exoplanets with equilibrium sub-stellar temperatures above 1000 K (assuming zero albedo).

Extensive research has been conducted on silicate atmosphere formation and the possibility of their characterisation. Models by Schaefer & Fegley\textsuperscript{2} (2009) showed that silicate atmospheres would be composed primarily of Na, O\textsubscript{2}, and SiO. Based on their work, Miguel et al.\textsuperscript{3} (2011) studied the entire population of Kepler super-Earths and found that these atmospheres are likely to be diverse in their composition, which is strongly

Fig. 1: Confirmed transiting short period exoplanets (including current TESS candidates) with radii < 2 R\textsubscript{⊕} and equilibrium sub-stellar temperatures > 1000 K. Planets to the left of the ultrashort period (USP) line have orbital periods < 1 day. Named planets are approved for the JWST Cycle 1 GO programme. The colour indicates the theoretical sub-stellar temperature of the planet. The marker size is proportional to the radius of the planet. Over 800 confirmed planets and more than 150 TESS candidates are displayed. The complete table of all shown planets with their parameters can be downloaded as supplementary material.
The effectiveness of this, however, is strongly dependent on the rapidity of material recycling in the interior (Kite et al. 2016). Following this, Nguyen et al. (2020) and Ito & Ikoma (2021) modelled evaporation-driven hydrodynamics with radiative-transfer and found that atmospheres dominated by SiO are much more likely to be stable against circulation and escape effects compared to ones dominated purely by Na. The current consensus is that silicate atmospheres may lack volatile Na and instead would be largely dominated by SiO or SiO2, both of which could be characterised through emission features.

Following the approach from Miguel et al. (2011) and Ito et al. (2015) and motivated by the possible evaporation evolution (Schaef er & Fegley 2009; Kite et al. 2016; Nguyen et al. 2020), we extensively modelled outgassed equilibrium chemistry and the atmospheric structure in order to investigate JWST observability for the shown short period rocky planets (Fig. 1). We put constraints on the current target list and indicate possible atmospheric features that could help characterise lava planets through low resolution spectroscopy. Our models are self-consistent, accounting for the changes in thermal structure caused by the chemistry, and were done with the inclusion of all up-to-date opacities that could potentially shape silicate atmospheres.

This paper is organised as follows. In Section 2, we describe our approach to modelling silicate atmospheres, including the use of outgassed equilibrium chemistry and radiative transfer methods. We present our findings for non-evolved atmospheres in Section 3.1. For evolved atmospheres, the results are outlined in Section 3.2. Section 3.3 highlights the results of models with different initial melt compositions. Overall implications and observability of silicate atmospheres are discussed in detail in Section 4. Finally, we conclude by summarising our key findings in Section 5.

2. Methods

2.1. Outgassed chemistry

Sustained planetary surface magma will preferentially outgas its most volatile components and eventually equilibrate itself with the overlying vapour, forming a silicate atmosphere. We determine the total atmospheric elemental budget by using the published results of the melt-vapour equilibrium code MAGMA, which has been used to calculate outgassing on solar system bodies and exoplanets (Fegley & Cameron 1987; Schaefer & Fegley 2004; 2009; Miguel et al. 2011; Kite et al. 2016). Its output is determined by the given initial composition of the melt, surface temperature and evaporation percentage. The involved chemistry considers the oxides of: Al, Ca, Fe, K, Mg, Na, Si and Ti. We make the assumption that due intense irradiation from the host star, highly volatile elements (H, C, N, S) are completely void from the atmosphere. In such a case the atmospheric composition is controlled only by the continuous evaporation of the underly ing melt and not by past accretion of volatiles (Schaef er & Fegley 2009; Kite et al. 2016).

Given the diverse population of stars, it is likely that melt compositions are highly varied. Approximations can be made from the particular host star (Brugman et al. 2021), this is however beyond the scope of this study. Bulk Silicate Earth (BSE) has been widely used in research of silicate atmospheres (Schaef er & Fegley 2009; Miguel et al. 2011; Ito et al. 2015; Kite et al. 2016). We adopt BSE as the main composition, but also briefly investigate a selection of other possible, silicate based melts. All used compositions are listed in Table 1.

In our models the surface temperature is solved for the substellar point, which is continuously adjusted using radiative-transfer methods that couple the surface and the overlying atmospheric layer (described in Section 2.2). This is process is done until convergence between the outgassed chemistry and thermal structure is achieved. Kite et al. (2016) has shown that for atmospheres with substellar temperatures > 2400 K, atmospheric evaporation is faster than surface-interior exchange, implying that continuous evaporation would rapidly drive the surface magma composition away from its initial values. While we do not directly simulate loss of material from the atmosphere through condensation or escape, we mimic the process using continuous removal of the most volatile components from the system. As described in Schaef er & Fegley (2004), this is done in a step-wise manner, until a set percentage of total melt mass is lost. We explore continuous removal of up to 60 percent mass of the given melt composition.

With elemental abundances established, atmospheric chemistry is solved using the thermochemical equilibrium code FASTCHEM (Stock et al. 2018) in accordance with the thermal structure of the atmosphere. We consider the following neutral components: Al, AlO, AlO2, Al2O, Al2O2, Ca, CaO, Fe, FeO, FeO2, K, KO, K2, K2O, Mg, MgO, Na, NaO, Na2, Na2O, O, O2, O2+, O3, Si, SiO, SiO2, Si2, Ti, TiO, TiO2; as well as ions: Al++, Ca++, Fe++, K++, Mg++, Na+, O+, O++, O3+, O4+ and ions: Si++, Ti++, TiO++. The thermal data is compiled from Burcat NASA thermodynamics polynomial database. We note that our inclusion of various components is only limited by the availability of thermodynamical data.

2.2. Temperature structure

We solve for the temperature structure using the radiative-transfer code HELIOS (Malik et al. 2017; Malik et al. 2019b). Profiles are converged to radiative-convective equilibrium consistently with the chemistry (convection has negligible effect for silicate atmospheres), assuming no surface albedo. The surface temperature itself is affected by the overlying atmospheric and is thus calculated according to the propagating flux. The exact implementation of the surface layer for rocky planets in HELIOS can be found in Malik et al. (2019a) Appendix A.

We consider 25 different opacity sources that could potentially affect the temperature structure, which the list of can be seen in Fig. 2. Atomic opacities (excluding Na) are calculated with the opacity calculator HELIOS-OP (Grimm & Heng 2015; Grimm et al. 2021), for which we use the Kurucz (Kurucz 2017). Atomic opacities (excluding Na) are calculated with the opacity calculator HELIOS-OP (Grimm & Heng 2015; Grimm et al. 2021), for which we use the Kurucz (Kurucz 2017). Atomic opacities (excluding Na) are calculated with the opacity calculator HELIOS-OP (Grimm & Heng 2015; Grimm et al. 2021), for which we use the Kurucz (Kurucz 2017). Atomic opacities (excluding Na) are calculated with the opacity calculator HELIOS-OP (Grimm & Heng 2015; Grimm et al. 2021), for which we use the Kurucz (Kurucz 2017).
any hotter stars we scale the shortwave VPL solar spectrum, stars, with temperatures covered in the MUSCLES database. For ing PHOENIX models (Husser et al. 2013) with scaled short-struct stellar spectra shaping the thermal structure of an atmosphere. We thus con-

peratures, shortwave absorption becomes an important factor in approximates shortwave energy flux. When dealing with high tem-

Appendix Table A.1. parameters and sources of all the opacities can be found in the of broadening theories for arbitrary atmospheres. The complete the current work, emphasising the need for future development 

broadening may have non-negligible e

There are no currently existing equivalent theories for silicate 

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The last thing to account for is stellar irradiation. For cooler 

for each of the individual stars by combin-

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nospheres. The wavelengths covered by the instrument are 5 - 12 

λ

PANDEXO

encompasses the coverage of all instruments of JWST.

For notable targets we assess JWST noise levels using 
PANDEXO

Batalha et al. (2017), which is built on the Pandex engine. We only simulate MIRI Low Resolution Spectroscopy (MIRI LRS with λ/Δλ = 100) in slitless mode, as it is likely to be the most suitable mode for characterisation of silicate atmospheres. The wavelengths covered by the instrument are 5 - 12 μ.

3. Results

3.1. Bulk silicate earth atmospheres

3.1.1. Opacities & Chemistry

The thermal structure in an atmosphere is shaped by wavelength dependant absorption of the incoming stellar radiation. Silicate atmospheres possess numerous different species that are good absorbers in the UV/Visible (shortwave) and infrared (IR) wave-

lengths. Generally, if the opacity at short wavelengths exceeds that of IR, the temperature of the absorbing region increases, causing an inversion to occur (Gandhi & Madhusudhan 2019; Maluk et al. 2019b). In cases with no shortwave absorbers, efficient cooling through IR will cause the temperature to decrease with increasing altitude.

Figure 2 shows example opacities of the 25 absorbing species investigated in this study. All values are weighted to abundances of a non-evolved stage of an atmosphere, formed from a BSE melt. Values are shown for a pressure of 10^−4 bar, a typical region where the photosphere begins to take shape. For each given temperature and wavelength, the opacity contribu-

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tion is calculated relative to the total added opacity of all present
species. Different species will dominate distinct wavelength regions, allowing us to easily track their effect on the thermal structure and emission spectrum.

Most ions, even though increasingly abundant in hot atmospheres, can be dismissed as potential absorbers. Their opacities are significantly lower in value compared to their neutral counterparts. There are exceptions to this, notably Fe$^+$ and Ti$^+$, that have meaningful inherent opacity; however, their outgassed BSE abundances are relatively small, and thus do not contribute to the models. On the neutral side, some of the strongest absorbers include Na and SiO, both of which have been noted in previous studies as potentially the most important constituents of silicate atmospheres ([Schafer & Fegley 2009] [Miguel et al. 2011] [Ito et al. 2013]).

Most of Na opacity comes from the strong 0.6 μm doublet (see Fig. 3). For isolated atomic lines, the characteristics of line wings play a significant role in its opacity value. Wings are difficult to model as their exact broadening behaviour is dependant on collisions with the background species. The required theory for arbitrary atmospheres (non-hydrogen) is currently not well understood. In our case, the wings are modelled with an H$_2$ atmosphere in mind, however, as explained in section 2.2 pressure broadening effects are ignored. To avoid opacity overestimation, the wings are also trimmed at an arbitrary length. In terms of chemistry, Na is consistently the leading atmospheric constituent until about 3000 K, at which point it starts to become ionised. Yet, even at lower abundances, its strong opacity keeps it a major shortwave absorber. That said, because Na is the most volatile constituent of silicate atmospheres, its dominance may be short lived, as it is expected to be readily lost through escape and condensation away from the sub-stellar point. Evaporation results are outlined in detail in Section 3.2.

**Silicon** is the second most abundant element outgassed from the melt, mostly residing in the form of SiO. Its abundance is closely followed by SiO$_2$. Contrary to Na, SiO is much less volatile and its abundance increases with increasing temperature. Its opacity is strong in both shortwave and IR regions. SiO shortwave band is strong enough to cause upper atmosphere thermal inversions even if other major shortwave absorbers are excluded. As discussed in Section 3.2 SiO long wavelength bands have distinct features that may prove very useful in characterising silicate atmospheres using low resolution spectroscopy. SiO$_2$ is another major component of silicate atmospheres. It is only recently that the vast SiO$_2$ molecular list, consisting of 33 billion transitions, has been computed ([Owens et al. 2020]). If sustained in gaseous phase, SiO$_2$ abundance is expected to be nearly $10^{-3}$ in volume mixing ratio for atmospheres above 2500 K, about 2 orders of magnitude lower than the abundance of SiO. A significant region of the IR opacity is dominated by SiO$_2$. As its bands do not overlap with SiO, the combination of the two molecules creates a unique spectral pattern. If SiO$_2$ is sustained in the atmosphere as a gaseous species, it should be expected to be a major opacity source for all tenable silicate atmospheres.

Many other species are important contributors. Notably, MgO and TiO are crucial components that further shape the atmospheric structure. MgO is expected to be highly abundant for the entire temperature range with its opacity covering both shortwave and IR wavelength regions, acting as a greenhouse continuum. TiO is present at the higher temperature range and is one of the dominant shortwave absorbers in the upper atmosphere. Inclusion of both molecules strongly affects the temperature structure and the expected emission spectrum. Some other minor opacities that slightly influence the atmosphere include Al, Ca and Mg, but all can be dismissed if necessary.

In Figure 2 the upper panel displays the total, wavelength and temperature dependant opacity. The contribution for the given temperature is represented by the colour intensity. The fitted curve shows which temperatures have dominant opacity values per each defined wavelength. At $10^{-4}$ bar and atmospheric temperatures above 2000 K, shortwave opacity will be greater than its longer wavelength counterpart. This imbalance will shape the temperature-pressure profile, causing an inversion to occur. This is only true for low pressures. When the pressure increases, molecules become more abundant, thus resulting in greater IR opacity. At high surface temperatures, the thermal structure of silicate atmospheres should be expected to have distinct regions with opposing temperature gradients.

### 3.1.2. Temperature-pressure structure

All temperature-pressure (T-P) profiles for lava planets with substellar temperatures $> 1500$ K are shown in Figure 3. At $1500$ K the atmosphere is extremely tenuous, sustaining just above $10^{-7}$ bar surface pressure. At these pressures the chemistry mainly consists of atomic, shortwave absorbers, resulting in large surface temperature jumps, but otherwise a nearly isothermal profile. Low pressure atmospheres are of little use for observations using low resolution techniques. However, because outgassed pressure scales exponentially with the temperature of the melt, at $2000$ K it reaches nearly $10^{-3}$ bar. This pressure is enough to allow for more complex molecular composites, such as SiO, to exist in abundance. The effects of this are twofold. First, the increased total opacity pushes the photosphere away from the surface, eliminating the sharp temperature discontinuities. Second, at high pressures IR opacity becomes larger than the shortwave opacity, causing inversions to become confined only to the upper atmospheric regions.

At $2500$ K the IR opacity of silicate atmospheres increases substantially. The surface pressure now reaches $10^{-2}$ bar. Lower regions follow a dry adiabat, with a clear temperature minimum that is followed further up by an inversion. The temperature minimum, otherwise defined as the tropopause, is a good indication of the average photospheric pressure level. Without modelling emission features, one should expect to see strong contributions from the regions just above and below the tropopause.

Increasing the temperature further will render the atmosphere completely opaque in shortwave and IR wavelengths. Regions below the photosphere are trapped, no longer efficiently radiating. This results in a deep isothermal layer that is inaccessible to observations. While models indicate that at $4000$ K the surface pressure would equate to 10 bar, it is unclear whether such strongly irradiated systems could be sustained. It is very likely that the large deposition of irradiation would result in rapid loss of material caused by erosion ([Owen & Wu 2017] [Owen 2019]).

Observable emission features depend on the probed thermal structure of the atmosphere ([Zilinskas et al. 2021]). The shape of the T-P profile is determined by the shortwave/IR absorption of stellar irradiation. The spectral energy distribution coming from hotter stars is much more weighted towards shorter wavelengths. As opposing to cooler stars that peak in IR wavelengths, emitting only a small fraction of energy in the UV/Visible. Figure 4 demonstrates how the inversion strength scales with temperature of the host star and the sub-stellar surface temperature of planet, which, for BSE, is generally within 50 K of the predicted theoretical value $T_{eq}^{12}$. Inversion strength is defined by the ratio of the atmosphere completely opaque in shortwave and IR wavelengths. Regions below the photosphere are trapped, no longer efficiently radiating. This results in a deep isothermal layer that is inaccessible to observations. While models indicate that at $4000$ K the surface pressure would equate to 10 bar, it is unclear whether such strongly irradiated systems could be sustained. It is very likely that the large deposition of irradiation would result in rapid loss of material caused by erosion ([Owen & Wu 2017] [Owen 2019]).

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Fig. 2: Sampled opacities of a silicate atmosphere. Shown for a typical Bulk Silicate Earth melt composition with a surface temperature of \( \sim 2700 \) K and atmospheric pressure of \( 10^{-4} \) bar. The individual species indicate contributed absorption to the total opacity, with the minimum cutoff threshold of 5\%. The upper panel shows temperature-specific absorption contribution relative to the maximum opacity for all wavelengths, with a minimum threshold of \( 10^{-10} \). The curve is fitted to indicate the maximum, wavelength-specific opacity for all temperatures. Note that the labelled temperatures are atmospheric, which represent the temperature of the melt.

Fig. 3: Temperature-pressure profiles of confirmed lava planets with sub-stellar temperatures > 1500 K. Calculated using non-evolved (0\% fractional vaporisation) Bulk Silicate Earth compositions. All profiles are converged to radiative-convective chemical equilibrium using the opacities described in Section 2.2. The colour is indicative of stellar irradiation temperature.

The high sensitivity and large spectral coverage (0.6-28 \( \mu \)m) of the JWST will make characterisation of lava planets achievable. While the tenuous and confined nature of silicate atmospheres render low resolution transmission spectroscopy methods, which rely on atmospheric scale height, unreliable, the scorching day-side temperatures and orbital periods of less than a day make multiple orbit, thermal emission spectroscopy ideal. In addition to outgassed chemical signatures, thermal emission directly probes the temperature structure of the atmosphere, giving us insight into the atmospheric dynamics and occurring radiative processes.

3.1.3. Observability

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How good a planet is for silicate atmosphere characterisation is determined by several important factors. First, the planet itself has to be of large enough surface temperature to outgas and sus-
The standout gets, as well as several TESS candidates that should be considered for the JWST observations, however, there are some excellent targets below 2500 K have pressures lower than 10⁻² bar, which is barely enough to start forming a photosphere. Ideally, a substellar temperature of nearly 3000 K is required to produce an atmosphere that would show large flux deviations from expected blackbody emission. The flux ratio between the planet and the star has to be also large enough to be detectable. This renders a large portion of currently known systems, where the star is too hot or too large in comparison to the planet, unsuitable, even in the IR, where most of the planetary emission comes from. Lastly, the observed system has to be bright enough to have reasonable noise levels, but not so bright that it would saturate the sensors. For MIRI LRS, the saturation limit is expected to be around 5-6 J magnitude (Beichman et al. 2014). The lower observable limit for the instrument is likely to be around 9-10 J magnitude. MIRI LRS mode itself has spectral capabilities between 5 and 12 µm, making it the ideal mode for characterising the presence of the 9 µm SiO feature that has been previously shown to be the best, if not the only characterizable feature of silicate atmospheres (Io et al. 2015).

In Figure 5 we showcase the observability distribution of all modelled lava planets in terms of the above mentioned criteria. Majority of planets are too dim and too cold to be considered for the JWST observations, however, there are some excellent targets, as well as several TESS candidates that should be considered. The standout, TOI-1807 b, is a recently discovered super-Earth orbiting a K dwarf (Hedges et al. 2021). In the provided sample, it is by far the best candidate for atmospheric characterisation. Its stellar host is comparatively cool and small, resulting in expected planetary flux from the dayside relative to the stellar flux (i.e. eclipse depth) at 9 µm of over 400 ppm. The sub-stellar temperature of the planet is expected to be just over 3000 K which would result in an outgassed atmosphere of 10⁻¹ bar (BSE melt with Na). In addition, with a J magnitude of 8.1, the system falls perfectly within the range of sensitivity for MIRI LRS. Simulated noise levels for 20 hours of observations (3 eclipses, binned to R=10) are just 21 ppm. TOI-1807 b is an exceptional target with no current equal alternatives.

In terms of dayside flux, the closest two planets to TOI-1807 b are K2-141 b and TOI-2431 b. As their sub-stellar temperatures are comparable to TOI-1807 b, both of the planets are also expected to possess substantial silicate atmospheres. With both systems being reasonably bright for the JWST and emission flux reaching nearly 300 ppm, these planets are good candidates for follow up characterisation. K2-141 b is a well studied target (Baragán et al. 2018, Malavolta et al. 2018, Nguyen et al. 2020; Zieba et al. in submitted) and is even approved for JWST GO Cycle 1 programme for over 20 hours with MIRI LRS (Dang et al. 2021) and 12 hours with NIRSpec (Espinoza et al. 2021). While TOI-2431 b has not been selected for the JWST observations, it may prove to be just as good of a target as K2-141 b for future proposals.

Other notable targets within the brightness limits of MIRI LRS include: a 3300 K super-Earth orbiting a sun-like star TOI-561 b; a similar but cooler, 2300 K super-Earth HD 3167 b and a very bright, 3000 K super-Earth HD 213885 b. HD 80653 b and Kepler-21 b are strongly irradiated planets that fall into the MIRI range; however, their secondary eclipse flux values are below 100 ppm, making atmospheric characterisation much more difficult. While GJ 367 b is a nearby sub-Earth that is also approved for JWST, its equilibrium temperature is lower than 2000 K, resulting in an outgassed atmospheric pressure of < 10⁻⁷ bar. Such, relatively cool, targets are also unlikely to be good candidates for characterisation of silicate atmospheres.

55 Cnc e currently stands as the brightest known super-Earth. The planet has been under extensive investigation, with the current conclusion that it may harbour a thick, volatile-rich atmosphere, possibly dominated by nitrogen, carbon and/or oxygen bearing species (Demory et al. 2016, Angelo & Hu 2017). TOI-2431 b is at the time of writing still a TESS planet candidate but the target is likely to be confirmed soon due to an accepted HST programme (GO 16660, S. Quinn 2021).
Their 141 b and TOI-1807 b orbit cooler K stars, resulting in weaker fluxes of over 100 ppm and lie perfectly within the sensitivity range of the MIRI LRS mode.

The indicated MIRI coverage region includes both, low resolution and medium resolution modes. Shaded SiO (9 µm) and SiO₂ (7 µm) are likely to be strongest characterizable features of silicate atmospheres. Note that SiO also has an additional band between 4 - 5 µm, however, its magnitude is, in most cases, small. The noise at 4 - 5 µm is an artefact of generated synthetic stellar spectra.

Fig. 6: Synthetic emission spectra of four selected lava planets with outgassed silicate atmospheres: HD 213885 b, 55 Cnc e, K2-141 b and TOI-1807 b. The spectra are computed for the entire JWST wavelength range and convolved to a resolution of R=800. The blue curves denote blackbody emission of numerically converged surface temperature. Corresponding temperature profiles for each planet are shown in the inset. Error bars are simulated only for the MIRI LRS slitless mode assuming 20 hours of observations and binned to a resolution of 3000 K, with 55 Cnc e being slightly on the cooler side, but they vary strongly in brightness and emission flux. K2-141 b and TOI-1807 b orbit cooler K stars, resulting in weaker thermal inversions, but otherwise similar thermal structure. Their respective temperature profiles are given in the top left inset of the figure.

Fig. 7: Opacity contribution of an outgassed silicate atmosphere for TOI-1807 b with a non-evolved (0% fractional vaporisation) Bulk Silicate Earth melt composition. Intensity shaded pressures indicates optically thick regions. All marked species are major contributors of the denoted wavelengths. The corresponding temperature profile and the resulting spectrum are shown in [6].

While these atmospheres are filled with many strong absorbers, the only two relevant species that have broad, visible features are SiO and SiO₂. SiO is expected to be the major constituent of all silicate atmospheres. Equilibrium chemistry shows that it is consistently abundant throughout the entire atmosphere, making its opacity relevant even for upper regions, where thermal inversions take place. SiO has a strong 9 µm band that is 3.5 µm wide. Because its opacity comes from higher up in the atmosphere, the feature shows up as increased flux. As inversions become weaker with increasing sub-stellar temperature of the planet (see Fig. 4), the magnitude of SiO features will be diminished for the hottest targets. The bands of SiO₂, however, do not manifest as emission, but rather as absorption. SiO₂ is mostly confined to the lower, cooler layers of the atmosphere. Its 7 µm SiO₂ band does not overlap with SiO, creating a large contrast between the two molecules. The combination could prove to be the best characterisable feature of silicate atmospheres, allowing to probe distinct thermal regions of the atmosphere.

In Figure 7 we show the opacity contribution for the atmosphere of TOI-1807 b. Intensity shaded pressures represent the photosphere being probed by emission spectroscopy. The opacity of the 9 µm SiO feature is not confined to single atmospheric pressure, but rather becomes non-negligible at pressures as low as 10⁻⁵ bar, extending for several orders of magnitude downwards. On the contrary, SiO₂ is confined to a region that is less than order of magnitude wide. At 10⁻² bar, it mostly coincides with the minimum of the temperature profile, which results in an absorption feature. Going further beyond of the 9 µm SiO band, the opacity comes mostly from MgO, which acts more or less as a continuum for silicate atmospheres. As with SiO₂, its presence is also mostly confined to the lower temperature regions. Apart from the small flux change at 13 µm, MgO does not have any distinct features. If MgO was absent from the atmosphere, beyond 9 µm the spectrum would instead show absorption of SiO₂, which has a distinctive band between 11 - 16 µm.

While there are additional strong shortwave absorbers, such as Na and TiO, their spectral features are extremely minor and likely undetectable with low resolution spectroscopy. Even the 0.6 µm Na doublet results in only slightly increased flux. In this study we omit pressure broadening effects, which can result in broader Na features, but even then its characterisation might...
prove difficult. Note that this is only true for this particular case. Other outgassed compositions can have increased abundances of shortwave absorbers, resulting in stronger emission features (see Section 3.3).

3.2. Evolved atmospheres

As shown by circulation models in Kite et al. (2016), planets with sub-stellar temperatures > 2400 K are likely to be ‘atmosphere-dominated’, meaning that the surface melt composition is dragged away from its initial state by atmospheric evolution itself. This is a direct consequence of material being lost from the atmosphere either through escape to space or being carried to the cooler regions and condensing out from the system. For strongly irradiated planets this evolution is rapid and is expected to outpace mass recycling between the interior and the surface melt.

In the outgassing code, MAGMA, atmospheric evolution is simulated with fractional vapourisation. It is essentially sequential removal of the most volatile constituents until a set percentage of the total mass has been removed from the system. Na is the most volatile component and is in all cases rapidly lost. At 3000 K sub-stellar temperature its abundance becomes vanishingly small at less than 10% removed material. Because it is a major vapour, its removal causes a large drop in atmospheric pressure, as well as decrease in shortwave opacity. Continuing the evolution, abundances of K and Fe elements slowly decrease, but neither are completely removed when the melt temperature is 3000 K. Si is also lost from the system, albeit much more slowly. While volatile species are reduced, the dominance of refractory elements grows. Abundances of Mg, Ti, Ca and Al all steadily increase. Appendix B contains figure for the evolution of major atmospheric abundances with fractional vapourisation. Readers looking for a much more detailed analysis of fractional vapourisation and possible removal of volatiles are directed to Schaefer & Fegeley (2004, 2009); Kite et al. (2016).

Figure 8 showcases T-P profiles at 60% fractional vapourisation, for surface temperatures larger than 2000 K. The faint background curves indicate T-P profiles with no vapourisation (from Fig. 3). Depletion of Na has the largest effect on the thermal structure, causing the pressure to drop nearly two orders of magnitude at sub-stellar temperatures near 2000 K. At higher temperatures, Na is less dominant, hence its removal has a lesser effect on the total vapour pressure. However, in all cases, its shortwave opacity is completely removed, causing thermal inversions to weaken. With removal of volatiles, MgO becomes more abundant, causing the photosphere and the temperature minimum to shift upwards to lower pressures. The surface temperature of the planet is also affected by the changes in opacity, resulting in a greenhouse effect of up to 200 K. The severity of this is greater for hotter planets that are subject to stronger shortwave irradiation.

The resulting differences in emission spectra are indicated in Figure 9. The coloured spectra represent the original, non-evolved cases. The black spectra show 60% fractional vapourisation models. While differences seem small, we find that planets around cooler stars will have their spectral features severely diminished. This is the combined result of the temperature profile shifting closer to an isotherm (reduced inversions), as well as decreased abundances of the absorbers, e.g., SiO and SiO2. The spectra now coincide closely with the expected lower blackbody emission limit. The effect is slightly lesser for planets around hotter stars, but generally similar. Needless to say, removal of Na removes any possible emission from 0.6 µm doublet. Different vapourisation percentages show similar results, with the general trend of spectral features disappearing and the spectra moving closer to blackbody emission. If the effects of vapourisation are prominent on lava worlds, it would make characterisation of their atmospheres with low resolution spectroscopy much more demanding.

3.3. Atmospheres of varying melt compositions

The bulk composition of lava planets can be estimated from their measured density (Dorn et al. 2015), the properties of the specific host star (Santos et al. 2017; Putirka & Rarick 2019), or even from polluted white dwarfs (Klein et al. 2011; Putirka & Xu).
However, besides inherent degeneracy of interior models complicating the matter, the formation history of the planet can also strongly affect the composition \cite[Bond et al. 2010; Carter-Bond et al. 2012]{Bond2010}. If the predictive assumption of silicate atmospheres is correct, determining atmospheric abundances from observations could allow for better constraints on melt compositions and possibly interiors. Until then, our best examples come from our own solar system. \cite{Hart1986} introduced the term Bulk Silicate Earth, representing the combined composition of the early Earth’s crust and mantle, which excludes the iron-rich core. While strongly irradiated rocky worlds may resemble early Earth, currently there is no evidence for it. Thus, besides BSE, we consider several other viable melts that vary in their oxide ratios.

Listed in Table [1] are: BSE, Continental, Oceanic, Komatiite, and Mercury. Continental and Oceanic represent parts of the Earth’s upper lithosphere, which formed from the molten silicate mantle. Compared to BSE, both compositions are substantially less dominated by Mg oxides, but much richer in Si, Al, Na, and Ti. Oceanic contains a large amount of Ti and Ca, while Continental is more enriched in K. It has been argued the Komatiite lava, erupted on the early Earth, might be more representative of molten, more massive Earths \cite{Miguel2011}. Komatiite is resembled by BSE, but with slightly higher Si and lower Mg content, while also being much more rich in Fe. Mercury melt is uniquely poor in Fe and due to its close formation proximity to the Sun, it is essentially void of two most volatile components, Na and K. Its composition is otherwise similar to Komatiite.

Resulting atmospheric abundances for each of the compositions are indicated in Figure [10]. The selected cases are for 55 Cnc e, with sub-stellar temperature ranging between 2600 - 2800 K. The showcased species are all major absorbers of silicate atmospheres.

BSE and Komatiite melts result in nearly identical atmospheric abundances and structure. This is not surprising, since the two melts have very similar volatile reservoir. While Komatiite does have lower Mg content, diminishing atmospheric pressure, its higher Fe abundance counteracts this effect. In terms of characterisation, the two compositions are essentially identical.

With Mercury having nearly depleted NaO and K$_2$O in the melt, the results are somewhat similar to the previous compositions. Na is so volatile that even a small fraction of it in the melt results in it being a major outgassed species. Partial pressures are now more evenly divided between all different elements (normally dominated by just Na or SiO). Since this melt is less volatile, it results in slightly lower total pressure.

The two compositions that stand out from the rest are Oceanic and Continental (crustal melts). Differences are caused mostly by their lack of MgO and high abundance of TiO. Even while the crustal melts are much more abundant in Na, diminished MgO leads to a substantial pressure drop and much lower surface temperatures. Oceanic composition pressure is still largely dominated by Na, whereas SiO is leading for Continental. Crustal compositions are uniquely rich in TiO, enhancing shortwave absorption in the upper atmosphere. Both compositions, in general, have much greater shortwave opacity, resulting is stronger inversions. Altogether, we find that the variation in melt composition results in moderate thermal structure and atmospheric abundance changes.

The caused spectral differences are given in Figure [11]. The three displayed planets are TOI-1807 b, 55 Cnc e, and HD 80653 b; picked to cover a range of different stellar and planet surface temperatures. The T-P profiles (shown in the inset) vary only slightly between the bulk compositions (BSE, Komatiite and Mercury), but are differentiated from crustal melts (Continental, Oceanic), which cause a substantial change in the structure of the lower atmosphere. This is reflected in the blackbody emission range, indicated via shaded blue region, which is now much larger than in previous cases (see Fig. [6] and [9]). The differences are smaller than in previous cases (see Fig. [6] and [9]). The differences are smaller than in previous cases (see Fig. [6] and [9]).

From emission, bulk compositions are likely to be indistinguishable with low resolution spectroscopy. However, outgassed crustal atmospheres have large enough differences to be possibly identifiable. Crustal compositions have stronger inversions and larger SiO abundance, which directly results in more contrasting 9 µm SiO$_2$/SiO features. For bulk atmospheres these features are followed by continuous absorption of MgO. But in crust-like atmospheres MgO is expected to be severely depleted. Since SiO$_2$ has a distinct band between 11 - 16 µm, its opacity may replace MgO. Its features would show up as absorption, coming from the lower regions of the atmosphere. Detected SiO$_2$ features over MgO would imply that the planetary atmosphere is being outgassed from an Earth-like crust. Such melts are also very enriched in Ti, which results in a larger atmospheric abundance of TiO. TiO is a strong absorber < 0.9 µm. In our models its presence causes a relatively large, continuous increase in flux, which may indeed be observable for the very best targets with the JWST.

The situation is similar for evolved atmospheres. Figure [12] indicates melts with 60% fractional vapourisation. Removal of volatile inventory causes atmospheric composition to be more dominated by MgO and TiO, resulting in increased temperatures. Vaporisation causes much larger atmospheric structure difference between the two classes of melts, with the total vapour pressure reduced significantly for crustal compositions. As abundances of Si composites drop and inversions become weaker, its features are also diminished. However, unlike for bulk melts, atmospheres produced from crustal melts still have a strong 9 µm SiO feature. While SiO$_2$ is still present in the atmosphere, its detection in evolved atmospheres may be hindered for all plausible compositions. TiO features are never removed with vaporisation, as its abundance always grows.

4. Discussion

4.1. Characterising lava worlds

Current theory predicts that lava planets are either leftover remnant cores of sub-Neptunes, eroded away by intense irradiation, or are simply formed as rocky worlds, without accreting much volatiles \cite{Owen2017, Lopez2017}. Whether these planets form in situ or are scattered inwards through gravitational interactions is unclear \cite{Ogihara2015, Winn2018}. While there are several observed USP planets inconsistent with volatile-free atmospheres \cite{Demory2016, Hammond2017}, most are found to have densities similar to that of Earth \cite{Dai2019}. It is expected that the permanently irradiated dayside will outgas and sustain a silicate-rich atmosphere \cite{Miguel2011}. Characterisation of short period planets is an intriguing next step in the exoplanet field. JWST will provide much needed spectral coverage to make this possible. The outstanding issue is what exactly do we look for.

Previous studies have put forward SiO as the primary detectable species in silicate atmospheres \cite{Schaefer2021}. However, besides inherent degeneracy of interior models complicating the matter, the formation history of the planet can also strongly affect the composition \cite[Bond et al. 2010; Carter-Bond et al. 2012]{Bond2010}. If the predictive assumption of silicate atmospheres is correct, determining atmospheric abundances from observations could allow for better constraints on melt compositions and possibly interiors. Until then, our best examples come from our own solar system.
Fig. 10: Volume mixing ratio of silicate atmospheres outgassed from Komatiite, Continental, Oceanic, Mercury and BSE melts for 55 Cnc e, with a surface temperatures close to 2700 K. Exact melt compositions are given in Table 1. The five listed species have the dominant opacities that shape the thermal structure and emission spectrum of the atmosphere. Depending on the exact surface temperature and volatile content, the total outgassed pressure will vary between different melts.

Fig. 11: Emission spectra for different melt compositions at R=800. The shown planets are: TOI-1807 b; 55 Cnc e; HD806563 b. For each planet different colours indicate varying melt compositions, while the black curves represent Bulk Silicate Earth melts. Corresponding temperature profiles for each of the compositions are show in the inset. The blue shaded region represents variation in surface temperature, which in this case is largest between Bulk Silicate Earth and Oceanic comps.

As Ito et al. (2015) argue, due to strong thermal inversions, the 9 μm SiO band would show up as a significant increase in flux coming from the planet. In our models thermal inversions are not as prevalent and mostly confined to just the upper regions. The discrepancy is mainly due to our inclusion of up-to-date opacities while also using more accurate stellar irradiation and self-consistent radiative-transfer models. However, because SiO opacity is so dominant, it becomes significant even in very low pressures, where inversions do occur. Thus we still see the 9 μm SiO band as emission, though to a much lesser extent.

The additional inclusion of SiO$_2$ in our models indicates that it would manifest as absorption bands, possibly surrounding the 9 μm emission of SiO. SiO$_2$ abundance increases significantly towards the lower parts of the atmosphere, which coincide with decreasing atmospheric temperatures. The combination of the two molecules at different atmospheric regions may prove to be unique, identifying features of silicate atmospheres. Detecting both as absorption and emission would allow us to put strong constraints on the temperature gradient. Presence of SiO$_2$ may also indicate a lack of MgO, which can be tied to the composition of the melt. Lack of SiO$_2$ could also suggest volatile depleted melts and/or possibly strong atmospheric dynamics.

Overall, we find that the variation of melt compositions and the stage of evolution (volatile material removal through escape or condensation) will impact characterisation. Depending on the melt composition, certain emission features may be strongly enhanced or completely removed. Melts that deviate substantially from the expected norm (crustal compositions) will result in large spectral differences. Variation caused by fractional vaporisation is also non-negligible. While with volatile removal the temperatures in the atmosphere are generally increased, the total pressures are lowered. Shortwave opacity reduction also makes inversions weaker. The combination of all these effects can result in the largest emission features, e.g., 9 μm SiO band, being reduced and certain bands entirely removed (SiO$_2$ absorption). As inversion strength decreases with decreasing stellar host temperature, planets orbiting cooler M or K dwarfs may show weaker emission signs, if any at all. Hotter stars will prove to be much better candidates for observing emission features, however, their
larger radii and increased temperatures weaken planetary signal, rendering majority of currently known targets unfavourable.

JWST instruments will allow us to easily distinguish between volatile-rich and silicate atmospheres. However, characterising spectral features in silicate atmospheres may only be possible at longer wavelengths. MIRI LRS instrument covering wavelengths between 5-12 µm is ideal for SiO and SiO₂ bands. Its high sensitivity will allow for detection of absorption and emission features in just a few secondary eclipses. For the best possible outcome we recommend focusing on targets with expected sub-terrestrial temperatures larger than 2500 K, preferably orbiting K stars. Some of the best current targets for secondary eclipse observations with MIRI LRS include: TOI-1807 b, 55 Cnc e, TOI-2431 b, K2-141 b, HD 3167 b, TOI-561 b and HD 213885 b (see Figure 5).

4.2. Melts and interiors

The two melts that may be observationally distinguishable from the rest are Earth’s oceanic and continental crust. The Earth’s oceanic crust is magnesium and iron-rich, dense, and relatively thin (~8 km); efficient recycling through the action of plate tectonics maximises the age of oceanic crust on Earth today to about 200 million years (White & Klein 2014). In contrast, the continental crust is richer in silicon and aluminium, less dense, and thicker (~40 km). Due to its low density, recycling of crust into the interior is far less efficient, which leads to the fact that parts of the continental crust on Earth today exceed 4 billion years in age (Ricker et al. 2014). Although the crust of the Earth (oceanic+continental) constitutes only ~0.6% of the mass of the present-day silicate Earth, it contains between 20% and 70% of the highly incompatible⁴ trace element budget (Rudnick & Fountain 1995). Hence, this explains the elevated Al₂O₃, CaO, Na₂O, TiO₂, and K₂O values when comparing to the crustal to the other melts in Table 1. For such crustal melts to co-exist, plate tectonics is likely required (Rudnick & Gao 2014). The presence of Earth-like plate tectonics in turn necessitate the presence of a weaker interior layer on which the plates can move, and liquid water is a likely prerequisite to form such a weak layer (e.g. Mierdel et al. 2007).

Observed spectral signatures correlating with these compositions could indicate that the planet in question has had a recent history of plate tectonics and hence the presence of liquid water. The fact that lava oceans are most likely well mixed with the mantle (Kite et al. 2016) means that the melting of the crust must have occurred very recently due to, for example, a recent giant impact or the host star entering the red giant phase. Therefore it is unlikely that such signatures will be found on targets that are believed to have a long-lived lava ocean. Alternatively, if such signatures are found then it may be an indication that the upper layers of the melt are chemically evolved in such a way that they resemble crustal composition or that the planet has a mantle with a unique bulk composition.

4.3. Limitations of 1D equilibrium models

There are obvious predictive limitations of 1D equilibrium models. This is especially true for lava planets where the atmosphere is likely to be confined to the permanently irradiated dayside. Away from the sub-stellar point, the sharp drop in temperature will induce an enormous pressure gradient, causing strong horizontal winds towards the nightside (Castan & Menou 2011; Kite et al. 2016; Nguyen et al. 2020). Material removed via winds is bound to condense at cooler regions, settling down onto the surface, where it may or may not be reincorporated into the outgassing cycle via surface and interior transport. In this study we have mimicked this effect to some extent using fractional vaporisation, but this is a very simplistic assumption. For a more accurate assessment of observability, 2D Circulation models combined with simplified outgassed chemistry and radiative transfer may prove to be the reasonable next step.

Use of equilibrium chemistry models also ignores the potential effects of photochemistry and vertical mixing. Photochemical destruction/ionisation of strong absorbers, e.g., SiO or Na, may cause substantial changes in thermal structure and observability of the specific species. Decrease in shortwave absorption will result in weaker thermal inversions. This effect is apparent with evolved cases, where Na is removed from the system while SiO abundance is slightly reduced (Fig. 8). Approximations of SiO photochemistry done by Ito et al. (2015) show that only pressures below 10⁻⁵ bar would be strongly affected, however, the significance is unclear without employing full kinetic photochemistry networks. The possibility of photochemical haze formation is also not considered.

5. Conclusions

Characterisation of lava worlds is exciting new frontier to be explored in the imminent future. Decade old studies have predicted formation of silicate-rich atmospheres, outgassed from the molten surface of irradiated planets (Schafer & Fogley 2009; Miguel et al. 2011). With the launch of JWST, the topic has received more interest than ever, including many predictive and observational studies (Ito et al. 2015; Kite et al. 2016; Dai et al. 2019; Nguyen et al. 2020; Ito & Ikoma 2021; Zieba et al. submitted). Several lava planets have been confirmed for the initial observers programme of JWST, which may lead to first evidence of silicate atmospheres on exoplanets (Hu et al. 2021; Brandeker et al. 2021; Dang et al. 2021; Espinoza et al. 2021).

As current theory predicts, these atmospheres should be depleted in highly volatile material. Thus characterisation with low resolution spectroscopy is likely to be only feasible via infrared emission coming from the dayside of the planet. In this work we have modelled 1D outgassed equilibrium chemistry consistently with radiative-transfer for all currently confirmed short period rocky exoplanets. We have considered a large number of possible species, including ions, as well as all up to date opacities. Finally, we have assessed observability of the best targets with the MIRI LRS instrument. Our results indicate the following:

1. Thermal inversions may not be as dominant in silicate atmospheres as previously thought. We find that inversions extend all the way to the surface only for planets with substellar temperatures below 2000 K. With larger surface temperature, due to increasing IR dominance over shortwave opacity inversions weaken and become confined to the upper atmospheric regions. Inversion strength also decreases with decreasing stellar temperature, implying that lava planets around M and K dwarfs may show only slightly increased emission flux, if any at all. This severely impacts characterisation of silicate atmospheres.

2. The dominant opacity sources for non-evolved silicate atmospheres with substellar temperatures > 2500 K are SiO, SiO₂, MgO, Na and TiO. Excluding these absorbers from

⁴ (In)compatibility is a geochemical term used to describe how easily a minor or trace element is able to replace major elements in a mineral.
models may result in inaccurate temperature-pressure profiles.
3. The best observable features come from silicon oxides, specifically 7 μm SiO2 and 9 μm SiO bands. SiO2 is confined to the lower, cooler regions, manifesting as absorption features. SiO is highly abundant in the low pressure, inversion dominated regions. While our temperature result in relatively small atmospheric features, we find that for the best targets, observations of only a few eclipses with MIRI LRS are needed for a detection.
4. The composition of the melt and possible volatile removal from the system will impact observability. Fractionally evaporated volatiles will have reduced SiO and SiO2 features and will prove much more difficult to characterise. Large flux from TiO (< 1 μm) could suggest atmospheres outgassed from melts resembling the Earth’s Continental or Oceanic crust. Detection 11-16 μm SiO2 features imply depletion of MgO, which is also characteristic of crust-like compositions. Detection of certain atmospheric abundances may allow us to constrain melt compositions, surface activity and even interior dynamics.
5. The recommended targets for silicate atmosphere characterisation with low resolution infrared spectroscopy are lava planets with sub-sterrestrial temperatures of at least 2500 K that ideally orbit cooler K dwarfs. Some of the currently confirmed planets to keep an eye on include: TOI-1807 b, 55 Cnc e, TOI-2431 b, K2-141 b, HD 3167 b, TOI-561 b, HD 213885 b, 55 Cnc e and K2-141 b are confirmed for the JWST Cycle 1 GO programme.

We stress the fact that 1D equilibrium models are limited in their predictability. The large temperature contrast between the day and the night side, circulation and interior effects, photochemistry and kinetics are all likely to influence the thermal structure and atmospheric abundances. There is also a need for more accurate modelling of opacities, accounting for pressure broadening effects and the high temperatures of silicate atmospheres.

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Supplemental material, including star spectra, temperature-pressure profiles, emission spectra or planetary parameters can be downloaded at https://github.com/zmantas/LavaPlanets.
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Table A.1: Sources and parameters of opacities used in this work

| Source | Line list | Cutting Length (cm$^{-1}$) |
|--------|-----------|---------------------------|
| Al     | This work$^a$ | Kurucz$^1$ | - |
| AlO    | DACE$^b$ & This work | ATP$^2$ | 100 |
| Ca     | This work | Kurucz | - |
| CaO    | DACE & This work | YBATHY$^3$ | 100 |
| Fe     | This Work | Kurucz | - |
| K      | This Work | Kurucz | - |
| Mg     | This Work | Kurucz | - |
| MgO    | DACE & This work | LiTY$^4$ | 100 |
| Na     | This Work$^c$ | VALD3$^5$ | Varied (300 max) |
| O      | This Work | Kurucz | - |
| O$_2$  | This Work | HITRAN$^6$ | 100 |
| Si     | This Work | Kurucz | - |
| SiO    | This Work | Kurucz (shortwave) & EBJT$^7$ | Varied (300 max) |
| SiO$_2$| DACE | OYT3$^8$ | 100 |
| Ti     | This Work | Kurucz | - |
| TiO    | DACE & This Work | Toto$^9$ | 100 |

$^a$ Opacities are computed with HELIOS-K [https://github.com/exoclime/HELIOS-K (Grimm & Heng 2015);
Grimm et al. (2021)]; $^b$ DACE database https://dace.unige.ch/; $^c$ Na doublet wings computed using the
unified line-shape theory of Rossi & Pascale (1985); Allard et al. (2007a,b); $^1$ Kurucz (Kurucz 1992);
$^2$ ATP (Patrascu et al. 2015); $^3$ VBATHY (Yurchenko et al. 2016); $^4$ LiTY (Li et al. 2019); $^5$ VALD3
(Ryabchikova et al. 2015); $^6$ HITRAN (Gordon et al. 2017); Chubb et al. 2021); $^7$ EBJT (Gordon et al.
2017); Chubb et al. 2021); $^8$ OYT3 (Owens et al. 2020); $^9$ Toto (McKemmish et al. 2019). We note that
we only use opacities of main isotopes. In this work we make use of the DACE (Grimm & Heng 2015;
Grimm et al. 2021), ExoMol (Chubb et al. 2021), HITRAN (Gordon et al. 2017), Kurucz (Kurucz 1992)
and VALD3 (Ryabchikova et al. 2015) opacity databases.

Appendix A: Opacity Data
Appendix B: Evolution of Atmospheric Abundances

Figure B.1 displays the changes in key atmospheric abundances caused by fractional vaporisation (Schaefer & Fegley 2004, 2009; Miguel et al. 2011; Kite et al. 2016). The process sequentially removes the most volatile species from the system with Na, in all cases, being removed first. Since the outgassed abundances depend on the surface temperature, the vaporisation percentage to remove a certain species is also temperature dependant. Generally, at higher temperatures it takes a larger percentage to remove certain species. With loss of volatiles, refractories become more dominant. This can have substantial effect on the thermal structure of the atmosphere as well as the observable spectrum.

Fig. B.1: Atmospheric abundance changes with fractional vaporisation (removal of volatile material). Shown for a Bulk Silicate Earth Composition for a range of different surface temperatures. Abundances are taken as averages for all pressures larger than 10^{-5} bar, assuming an isothermal temperature profile. Only the most relevant, typically high in abundance, species are shown.