Cluster Index Modulation for mmWave Communication Systems

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In this study, a novel cluster index modulation (CIM) scheme, which is based on indexing the available clusters in the environment, is proposed for future mmWave communication systems. Exploiting the fact that the available clusters in the system are well separated in terms of their angular distribution, we selected the best path for each of them and then performed IM in an algorithmic manner to convey information bits. It is shown that by means of large antenna arrays and analog RF beamforming with the indexed clusters, the destructive effect of inter-beam/cluster interference can be remarkably mitigated. Also, we designed a hybrid beamforming architecture at the transmitter to further reduce the effect of residual inter-beam/cluster interference, where the analog RF beamformer is followed by a digital baseband precoder using the zero-forcing technique. Computer simulations reveal that the proposed scheme can provide better error performance than traditional mmWave communication, and the proposed hybrid architecture outperforms beam index modulation (BIM) for a point-to-point scenario. Semi-analytical derivations and closed-form unconditional pairwise error probability (UPEP) expressions are derived for both analog and hybrid architectures, which confirm the validity and superiority of our proposed scheme.

Keywords: mmWave communications, index modulation, hybrid beamforming, bit error rate, zero-forcing

1 INTRODUCTION

With increasing demands for a higher data rate and spectrum usage, new technologies and novel techniques for future wireless systems are needed. One of the most promising technologies with a large available spectrum is millimeter wave (mmWave) communication (Zhou et al. (2018); Sun et al. (2014); Rappaport et al. (2015); Niu et al. (2015)). Nonetheless, mmWave signals suffer significant path loss due to a sparse-scattered environment (Perović et al. (2016); Heath et al. (2016)). To compensate the effect of path loss, mmWave systems should employ large antenna arrays in both the transmitter and receiver to leverage beamforming gain. Deployment of large antenna arrays in a compact size is possible, thanks to short wavelength of mmWave communications (El Ayach et al. (2014); Xiao et al. (2017)). Normally, in sub-6 GHz systems, MIMO arrays are fully digital, where each antenna element connects to a single RF chain. However, for mmWave systems with large antenna arrays, it is costly and power-consuming to have a huge number of RF chains (Raafat et al. (2018)), which necessitates the use of novel techniques to decrease implementation costs. Hybrid beamforming is a key technology to deal with this problem and to reduce the mmWave implementation costs (Li et al. (2020)). It is shown that hybrid beamforming achieves a spectral efficiency close to the fully digital beamforming, and it also greatly enhances energy efficiency for
mmWave communication systems with large antenna arrays by significantly reducing the number of RF chains (Koc et al. (2020)). While hybrid beamforming is known as an energy- and cost-efficient method to decrease the number of RF chains, there is still a need for a tremendous number of high-precision phase shifters. To decrease the number of phase shifters implemented in the analog network (Yu et al., 2018), proposed a novel hardware efficient structure by adopting a network of fixed phase shifters. A network of dynamic switches was implemented in order to adapt the analog network to the channel states.

Index modulation (IM) is another promising technology with high spectral and energy efficiencies, in which the transmitter performs indexing building blocks, for example, antenna arrays, paths, and subcarriers, to convey additional bits (Basar, 2016a; Basar et al., 2017). In Yüzgeçcioğlu and Jorswieck (2017), the authors investigated array IM in a mmWave communication system. In this study, the considered system consists of several arrays, and an index in each array is specified. Therefore, according to the spatial symbols, one array is selected and traditional symbols are transmitted through that array. Here, each receiver has to resolve traditional constellation and an array index. In Ding et al. (2017), the authors proposed a scheme named spatial scattering modulation (SSM) by indexing spatial directions of scattering clusters. It has been shown that the SSM scheme can perform better than maximum beamforming and random beamforming in the ideal condition of orthogonal paths, in terms of the bit error rate (BER). However, this study did not consider realistic conditions such that the paths are randomly distributed in the environment and the orthogonality is not guaranteed. Mokh et al. (2019) proposed a hybrid beam index modulation (BIM) scheme by adopting a layer of digital precoding to solve the problem of inter-beam interference in mmWave communication systems. The authors showed that the proposed scheme can boost the system performance in comparison with pure analog BIM, due to cancellation of inter-beam interference. Fan et al. (2020) proposed an anti-Doppler IM for wideband mmWave systems. They proposed a Doppler pre-compensator to assist IM in order to decrease the complexity of a maximum likelihood (ML) detector. With such a scheme, they indicated that error performance enhances. A spatial modulation scheme for the uplink mmWave system was proposed in Wang and Zhang (2019). In this scheme, the authors considered a power iteration algorithm to obtain spatial symbols. With such a spatial codebook, it is possible to find the optimal transmission mode by obtaining a trade-off between spatial domain and signal domain. On the other hand, at the base station (BS), they adopted a round-robin path selection algorithm to ensure that selected paths are separated enough with respect to angle of arrival (AoA). Generalized beamspace modulation (GBM) is proposed in Gao et al. (2019) to enhance multiplexing gain and spectral efficiency. A theoretical analysis and numerical simulations demonstrated that this scheme can perform better than non-GBM schemes in terms of BER and spectral efficiency. Finally, (Perović et al., 2016) studied receive spatial modulation (RSM) for indoor line-of-sight (LOS) mmWave systems. To minimize symbol error probability (SEP), they derived optimal channel conditions, and based on this optimization, they proposed a simple structure for the transmitter and the receiver.

In this study, a mmWave communication scenario in which the paths are uniformly distributed in the environment is studied, and normally, these paths are not orthogonal. In our proposed scheme, named cluster index modulation (CIM), the best path from each cluster is chosen for IM. Due to the well separation of clusters in terms of their angular distribution, the selected paths are also separated. It is worth mentioning that when two paths are physically separated enough, they become near orthogonal. Extensive computer simulations evaluate superiority of the proposed CIM scheme against traditional mmWave communication. Our contributions are summarized as follows:

- A novel IM scheme based on indexing separated clusters in the mmWave communication environment is proposed. Simulation results reveal that our proposed scheme can perform better than traditional mmWave communication in terms of BER in the presence of non-orthogonal paths.
- We proposed hybrid architecture in the transmitter, which benefits from a digital ZF precoder to further mitigate inter-beam interference. Simulation results demonstrated the superiority of our proposed hybrid scheme in comparison with the BIM scheme.
- We studied our scheme in the case of analog and hybrid architectures at the transmitter and derived our semi-analytical derivations and closed-form analytical unconditional pairwise error probability (UPEP) expressions for both architectures, which prove the validity of our proposed scheme. We further noted that our derivations based or semi-analytical models provide useful approximation on the actual BER.

The rest of this article is organized as follows. In Section 2, our channel model has been introduced. The BER performance analysis is given in Section 3. Simulation results are provided in Section 4; and the conclusion of this study can be found in Section 5.

## 2 SYSTEM MODEL

In this section, we presented the proposed system and its generic architecture. Figure 1 illustrates the proposed system model with $C$ clusters in the environment. It is assumed that each cluster consists of several paths with uniformly distributed angle of arrival (AoA) or departure (AoD) within a predefined interval. We considered that the clusters have non-overlapping angular support (i.e., AoA and AoD). Hence, they are well separated from each other. As shown in Figure 1, the number of transmit and receive antennas are assumed as $N_t$ and $N_r$, respectively. At both the transmitter and the receiver, each antenna element is connected to a phase shifter for the purpose of analog beamforming to compensate the effect of path loss. A point-to-point communication scenario is considered; hence, at the transmitter, we have a single RF chain. At the receiver side, $C$ beams should form simultaneously, where $C$ is the number of indexed clusters; hence, $C$ RF chains are needed at the receiver. With taking into consideration $M$ as the constellation order, the
spectral efficiency is given as  
\[ \eta = \log_2 C + \log_2 M \text{ bits per channel use (bpcu)}. \]

We adopted the Saleh–Valenzuela channel model to characterize a mmWave non-line-of-sight (NLOS) channel in an indoor environment (Ying et al. (2020); Akdeniz et al. (2014)). The channel matrix \( H \in \mathbb{C}^{N_t \times N_r} \) is expressed as follows:

\[
H = \sqrt{N_t N_r} \sum_{i=1}^{C} \sum_{l=1}^{L_i} a_r^{l}_i a_t^{l}_i(e^{j \Theta_i^{l}_r} e^{j \Phi_i^{l}_t}), \tag{1}
\]

where \( a_l^i \) shows \( l \)-th path gain in the \( i \)-th cluster that follows \( a_l^i \sim \mathcal{CN}(0,1) \) distribution; \( L_i \) is the number of available paths in the \( i \)-th cluster and \( a_r(.) \in \mathbb{C}^{N_r \times 1} \) and \( a_t(.) \in \mathbb{C}^{N_t \times 1} \) are the receive and transmit antenna array responses, respectively; \( \Theta_i^{l}_r \) and \( \Phi_i^{l}_t \) are the azimuth AoA and AoD corresponding to \( l \)-th path in the \( i \)-th cluster, respectively. Considering both transmitter and receiver equipped with uniform linear arrays, the array responses \( a_r(.) \) and \( a_t(.) \) are respectively defined as follows (Balanis (2015); Koc and Le-Ngoc (2021)):

\[
a_t^{l}_i(e^{j \Theta_i^{l}_t}) = \frac{1}{\sqrt{N_t}} \left[ 1 \ e^{j \Phi_i^{l}_t} \ldots e^{j \Phi_i^{l}_{(N_t-1)}} \right]^T, \tag{2}
\]

\[
a_r^{l}_i(e^{j \Phi_i^{l}_r}) = \frac{1}{\sqrt{N_t}} \left[ 1 \ e^{j \Theta_i^{l}_r} \ldots e^{j \Theta_i^{l}_{(N_r-1)}} \right]^T, \tag{3}
\]

where \( \Theta_i^{l}_t = 2 \pi \frac{d_r}{\lambda} \sin(\Theta_i^{l}_r) \), \( \Phi_i^{l}_t = 2 \pi \frac{d_t}{\lambda} \sin(\Phi_i^{l}_t) \), \( d_r \) and \( d_t \) are the distances between antenna elements at the transmitter and receiver respectively, and \( \lambda \) is the signal wavelength. In this study, half-wavelength separation between antenna elements is assumed (i.e., \( d_r = d_t = \frac{\lambda}{2} \)). In the following, we described the proposed analog and hybrid beamforming architecture.

2.1 Analog Beamforming Architecture

In this setup, completely analog architectures are considered at the transmitter and receiver; hence, there is no digital signal processing in the system. The received signal vector \( y \in \mathbb{C}^{N_t \times 1} \) at the receiver can be expressed as follows:

\[
y = H f_r s + n, \tag{4}
\]

where \( f_r \in \mathbb{C}^{N_t \times 1} \) is the analog beamformer of the best path of the selected cluster, i.e. cluster \( i^* \), at the transmitter, and \( n \in \mathbb{C}^{N_t \times 1} \) is the noise vector which has the circularly symmetric complex Gaussian distribution with variance \( \sigma^2 \), i.e. \( n \sim \mathcal{CN}(0, \sigma^2 I_{N_t}) \). \( s \) is the traditional transmitted data symbol. In this study, the best path in each cluster is considered to be the path with strongest path gain. The transmitter selects one of the indexed clusters according to the spatial symbol and conveys the conventional constellation through the best path of that cluster. For the sake of statement simplicity, when we mentioned indexed cluster, we meant the best path of that cluster. Analog beamformer \( f_r \) at the transmitter can be expressed as follows:

\[
f_r = \frac{1}{\sqrt{N_t}} \left[ 1 \ e^{j \Phi_i^{l}_r} \ldots e^{j \Phi_i^{l}_{(N_t-1)}} \right]^T, \tag{5}
\]

where \( \Phi_i^{l}_t = 2 \pi \frac{d_t}{\lambda} \sin(\Phi_i^{l}_r) \), and \( \Theta_i^{l}_t \) is the angle of transmission (AoT) of the beam corresponding to the selected cluster. The receiver uses analog combiners to resolve the spatial symbol. To do so, the receiver searches among all indexed clusters by multiplying corresponding vectors of analog combiners \( w_i \). Hence, the received signal after analog combiner can be shown as follows:

\[
y_i = w_i^{H} H f_r s + w_i^{H} n. \tag{6}
\]

Analog combiner of \( l \)-th path of the \( i \)-th cluster can be expressed as follows:

\[
w_i = \frac{1}{\sqrt{N_t}} \left[ 1 \ e^{j \Phi_i^{l}_r} \ldots e^{j \Phi_i^{l}_{(N_t-1)}} \right]^T, \tag{7}
\]

where \( \Phi_i^{l}_t = 2 \pi \frac{d_t}{\lambda} \sin(\Phi_i^{l}_r) \), and \( \Theta_i^{l}_r \) is the angle of reception (AoR) of the beam corresponding to the \( i \)-th cluster. In Eq. 6, \( i^* \) shows the correct index that is adopted by the transmitter; however, a receiver should resolve the index used at the transmitter. Therefore, we used the unknown index \( i \) for the combiner to emphasis this fact. In this study, it is assumed that AoT and AoR
are equal to AoD and AoA of the strongest path of the indexed cluster, respectively, unless specified otherwise. As shown in Figure 1, the receiver consists of C RF chains connecting to a network of phase shifters, and each of them forms the received beam toward the strongest path of a specific indexed cluster for the received signal. In this way, all analog combiners work simultaneously to resolve the spatial symbol.

In this study, we studied both brute-force and two-stage greedy-maximum likelihood (ML) detectors to analyze the performance of the proposed CIM. To use brute-force detector, all switches (i.e. SWc, i = 1, 2, ..., C) should be closed. Afterward, the receiver jointly detects indexed and M-ary bits as follows:

\[ [\hat{i}, \hat{m}] = \arg \min_{i=1,...,C} |y_i - \hat{w}_i^H Hf_i s_m|^2. \]  

(8)

For the case of a greedy-ML detector, amplitude detectors (AD) measure the received power of signals from each cluster to detect the one with the most power; henceforth, the corresponding switch to that path is closed while the other switches remain open. Therefore, we have the first stage detection to resolve indexed bits as follows:

\[ \hat{i} = \arg \max_{i=1,...,C} |y_i|^2. \]  

(9)

At the second stage, we adopt ML detector to detect M-ary symbols as follows:

\[ \hat{m} = \arg \min_{m=1,...,M} |y_i - \hat{w}_j^H Hf_i s_m|^2. \]  

(10)

### 2.2 Hybrid Beamforming Architecture

In the hybrid architecture, a digital precoder is adopted at the transmitter to further suppress inter-beam interference and boost the system performance. By applying the zero-forcing (ZF) criterion to the indexed clusters, the transmitter can null the inter-beam interference. The received signal vector y can be expressed as follows:

\[ y = HFDx + n. \]  

(11)

Notice \( D = [d_1, \ldots, d_c] \in \mathbb{C}^{N_t \times C} \) is the digital ZF precoder, where \( d_i \in \mathbb{C}^{N_t \times 1} \) is a digital precoder vector related to the \( i \)-th indexed cluster. \( F = [f_1, \ldots, f_c] \in \mathbb{C}^{N_r \times C} \) contains analog beamforming vectors of all indexed clusters, and \( x = [0 \ldots 0 \; s \; 0 \ldots 0]^T \in \mathbb{C}^{N_r \times 1} \) whose \( i \)-th element is \( s \), that is, \( M \)-ary constellation symbol. To define ZF precoder, first we defined effective channel \( H_e \in \mathbb{C}^{N_r \times C} \) as follows:

\[ H_e = W^H Hf_i. \]  

(12)

where \( W = [w_1, \ldots, w_c] \in \mathbb{C}^{N_r \times C} \) includes all analog combiner vectors of all indexed clusters. Next, \( D \) is defined as follows:

\[ D = \epsilon H_e^H (H_e H_e^H)^{-1}, \]  

(13)

where \( \epsilon \) is the normalization scalar and can be obtained as follows:

\[ \epsilon = \frac{1}{\sqrt{\text{tr} (F^H H_e^H (H_e H_e^H)^{-1} H_e^H F)}}. \]  

(14)

where \( \text{tr}(.) \) is the trace operation. It is worth mentioning that, channel characteristics at the transmitter can be obtained via both online and offline approaches (Zheng et al., 2018; Wang et al., 2015; Zhu et al., 2021). The received signal vector after analog combiner can be stated as follows:

\[ y^* = W^H HFDx + W^H n, \]  

(15)

where \( y^* = [y_1^* \ldots y_C^*]^T \in \mathbb{C}^{N_r \times 1} \). It is worth mentioning that \( y_i^* \) is the received signal from the \( i \)-th indexed cluster after the analog combiner that can be expressed as follows:

\[ y_i^* = w_i^H HD_i s_m + w_i^H n \]  

(16)

Finally, in order to jointly detect indexed and M-ary bits, the brute-force detector is defined as follows:

\[ [\hat{i}, \hat{m}] = \arg \min_{i=1,...,C, m=1,...,M} |y_i^* - w_i^H HD_i s_m|^2. \]  

(17)

### 3 BER PERFORMANCE ANALYSIS

In this section, the BER performance of the proposed analog and hybrid beamforming schemes are derived. We used \( i^* \) and \( s^* \) to present the true cluster index and symbol, whereas \( \hat{i} \) and \( \hat{s} \) are used to represent detected cluster index and symbol.

#### 3.1 Analog Beamforming Architecture

Using the brute-force detector, conditional pairwise error probability (CPEP) can be stated as follows:

\[ P(|i^*, s^*| \rightarrow [i, s]|a_i^1, \ldots, a_i^C) = P(|y_i - w_i^H HD_i s|^2 > |y_i - w_i^H HD_i s|^2), \]  

(18)

where

\[ |y_i - w_i^H HD_i s|^2 = |w_i^H n|^2. \]  

(19)

To solve CPEP expression, we considered two cases, correct cluster index detection \( \hat{i} = i^* \) and erroneous cluster index detection \( \hat{i} \neq i^* \). In this study, we did not consider the case of erroneously index detection and correct symbol detection because when the detector resolves the cluster erroneously, the error spreads to the symbol.

#### 3.1.1 Correct Cluster Index Detection \( \hat{i} = i^* \)

When the cluster index is detected correctly, by using Eq. 6 and right-hand side of Eq. 18, we can derive the following equation:

\[ |y_i - w_i^H HD_i s|^2 = |w_i^H n + w_i^H HD_i (s^* - s)|^2. \]  

(20)

Therefore, by substituting Eq. 19 and Eq. 20 into Eq. 18, CPEP expression can be as follows:

\[ P(|i^*, s^*| \rightarrow [i, s]|a_i^1, \ldots, a_i^C) = P(\zeta < 0), \]  

(21)

where
\[ \zeta = 2 \Re \{ \mathbf{n}^H \mathbf{w}_r \mathbf{H}_f \mathbf{r} (s^* - \delta) \} + | \mathbf{w}_r^H \mathbf{H}_f \mathbf{r} (s^* - \delta) |^2. \]  

Hence, \( \zeta \) follows Gaussian distribution with mean \( \mu_\zeta \) and variance \( \sigma_\zeta^2 \). These mean and variance values can be calculated as follows:

\[
\mu_\zeta = | \mathbf{w}_r^H \mathbf{H}_f \mathbf{r} (s^* - \delta) |^2, 
\]

\[
\sigma_\zeta^2 = 2\sigma^2 | \mathbf{H}_f (s^* - \delta) |^2. 
\]  

Accordingly, substituting Eq. 19 and Eq. 32 into Eq. 18 results into following CPEP expression:

\[
\mathbb{P}(|i^*, s^*| -> |i, \delta| |a_{i,1}^*, \ldots, a_{i,5}^*| = \mathbb{P}( |w_i^H \mathbf{H}(f_r, s^* - f_\delta) + w_i^H \mathbf{n}|^2 < 0).
\]  

Let us define

\[
\xi_1 = |w_i^H \mathbf{H}(f_r, s^* - f_\delta) + w_i^H \mathbf{n}|^2, 
\]

\[
\xi_2 = |w_i^H \mathbf{n}|^2.
\]  

Similarly, \( \chi_2 \) is a central chi-square random variable with two degrees of freedom and non-centrality parameter \( \Lambda_A \):

\[
\Lambda_A = \frac{2|w_i^H \mathbf{H}(f_r, s^* - f_\delta)|^2}{\sigma^2}. 
\]  

To acquire semi-analytical results, we can use the following expression:

\[
\mathbb{P}(|i^*, s^*| -> |i, \delta| |a_{i,1}^*, \ldots, a_{i,5}^*| = \frac{1}{25} \sum_{t=1}^{S} \exp \left( -\frac{\Lambda_A(t)}{4} \right). 
\]  

### 3.1.2 Erroneous Cluster Index Detection \( i \neq i^* \)

Considering erroneous detection of the cluster index, by using Eqs 6, 18, the following expression can be derived:
where \( \Lambda_A(t) \) is the \( t \)-th random sample of \( \Lambda_A \) and \( S \) stands for the number of random realizations.

To obtain UPEP by using the Distribution Fitter tool, the random part of Eq. 38 can be considered as follows:

\[
Y = |w_i^H H(f, s') - f, s')|^2.
\]

(40)

Hence, we can rewrite Eq. 38 as follows:

\[
h(Y) = \frac{1}{2} \exp\left(-\frac{Y}{2\sigma^2}\right).
\]

(41)

By taking expectation over \( h(Y) \), given that \( Y \) has a PDF of \( f_Y(y) \), we can derive UPEP as follows:

\[
\mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\} = E[h(Y)] = \int h(y) f_Y(y) dy.
\]

(42)

In Section 4, we obtain the PDF of \( Y \) for the deployed scenario; subsequently, UPEP can be calculated by using Eqs 41, 42.

### 3.2 Hybrid Beamforming Architecture

By following the same procedure, we can easily calculate CPEP for the hybrid beamforming architecture. Therefore, for the case of \( i = i^* \) and \( \hat{i} \neq i^* \), CPEP can be expressed as follows, respectively:

\[
\mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\}|a_1^*, \ldots, a_C^*\} = Q\left(\frac{\sqrt{Hf_i, \ldots, s^* - \hat{s}}}{2\sigma^2}\right),
\]

(43)

\[
\mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\}|a_1^*, \ldots, a_C^*\} = \frac{1}{2} \exp\left(-\frac{\Lambda_H}{4}\right),
\]

(44)

where

\[
\Lambda_H = \frac{2|w_i^H H(d, s^* - d, \hat{s})|^2}{\sigma^2}.
\]

(45)

Regarding Eq. 43, let us define \( M_H \) as follows:

\[
M_H = \frac{\|Hf_i, \ldots, s^* - \hat{s}\|^2}{2\sigma^2}.
\]

(46)

Semi-analytical results can be obtained by using the following expression:

\[
\mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\} = \frac{1}{S} \sum_{t=1}^{S} \mathbb{Q}\left(\sqrt{M_H(t)}\right),
\]

(47)

where \( M_H(t) \) is the \( t \)-th random sample of \( M_H \). Similarly, we can calculate semi-analytical UPEP for the case of \( \hat{i} \neq i^* \) as follows:

\[
\mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\} = \frac{1}{2S} \sum_{t=1}^{S} \exp\left(-\frac{\Lambda_H(t)}{4}\right),
\]

(48)

where \( \Lambda_H(t) \) is the \( t \)-th random sample of \( \Lambda_H \).

To obtain approximate UPEP, the same approach as the analog architecture can be adopted; hereby, we defined \( \tilde{X} \) and \( \tilde{Y} \) as random variables for Eq. 43 and Eq. 44 as follows, respectively:

\[
\tilde{X} = \|Hf_i, \ldots, s^* - \hat{s}\|^2,
\]

(49)

\[
\tilde{Y} = |w_i^H H(d, s^* - d, \hat{s})|^2.
\]

(50)

Subsequently, we can rewrite CPEP expressions of Eqs 43, 44 as follows, respectively:

\[
\mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\}|a_1^*, \ldots, a_C^*\} = g(\tilde{X}) = Q\left(\frac{\sqrt{\tilde{X}}}{2\sigma^2}\right),
\]

(51)

\[
\mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\}|a_1^*, \ldots, a_C^*\} = h(\tilde{Y}) = \frac{1}{2} \exp\left(-\frac{\tilde{Y}}{2\sigma^2}\right).
\]

(52)

Finally, by taking the expectation over \( g(\tilde{X}) \) and \( h(\tilde{Y}) \), and having the PDF of \( f_{\tilde{X}}(\tilde{x}) \) and \( f_{\tilde{Y}}(\tilde{y}) \), we can calculate analytical UPEP for the cases of \( i^* = \hat{i} \) and \( i^* \neq \hat{i} \) as follows, respectively:

\[
\mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\} = E[g(\tilde{X})] = \int g(\tilde{x}) f_{\tilde{X}}(\tilde{x}) d\tilde{x},
\]

(53)

\[
\mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\} = E[h(\tilde{Y})] = \int h(\tilde{y}) f_{\tilde{Y}}(\tilde{y}) d\tilde{y}.
\]

(54)

It is worth noting that in Section 4, we obtained a PDF for \( \tilde{X} \) and \( \tilde{Y} \) based on implemented system. Therefore, we can acquire UPEP by adopting Eqs 51–54.

### 3.3 BER Derivation

We can derive BER using union bound as follows:

\[
Pr \leq \frac{1}{N_b N(i^*, s^*)} \sum_{r=1}^{S} \sum_{t=1}^{S} E_b\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\} A,
\]

(55)

where \( N_b \) is the total number of transmitted bits, \( N(i^*, s^*) \) is the total number of realizations of \( i^* \) and \( s^* \), and \( E_b\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\} \) is the number of erroneous bits when \( i^* \) and \( s^* \) are transmitted but \( \hat{i} \) and \( \hat{s} \) are detected. As it is mentioned earlier, there are two cases of errors, that is, both index and symbol are erroneous, or just only symbol is erroneously detected. To obtain semi-analytical results, we defined \( A = \mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\} \) which can be obtained by using Eqs 28, 39 for analog beamforming architecture, or by using Eqs 47, 48 for hybrid beamforming architecture. It is worth mentioning that \( S = 10^4 \) has been considered during numerical expectation. On the other hand, to obtain approximate analytical results with the Distribution Fitter tool, we can define \( A = \mathbb{P}\{i^*, s^*\} \rightarrow \{\hat{i}, \hat{s}\} \), which can be acquired by using Eqs 31, 42 for the analog beamforming architecture, and Eq. 53 and Eq. 54 for the hybrid beamforming architecture.

### 4 SIMULATION RESULTS

Two architectures are considered for the proposed scheme, that is, analog and hybrid scheme. First, we provide computer simulation results for the analog scheme. Then the hybrid scheme, which includes a ZF precoder block to suppress interbeam interference, is analyzed.

#### 4.1 Analog Beamforming Architecture

The number of antenna elements at the transmitter and receiver is considered to be 128. The total number of paths in all clusters is considered to be 20, that is, \( \sum_{i=1}^{L} L_i = 20 \). In this study, it is assumed that the number of paths in each cluster is the same.
We study scenarios with one and two extra bits, thanks to IM. It is further assumed that the number of clusters is four (i.e., $C = 4$), and the distance between central angles of two adjacent clusters is $\pi/5$. It is worth mentioning that in each cluster, AoD/AoA is uniformly distributed in an interval with a length of $\pi/12$. Detailed information on AoD/AoA intervals are provided in Table 1, which shows the range of angles in each cluster. In this study, unit transmit power is assumed; hence, the signal to noise ratio is defined as $\text{SNR} = \frac{1}{\sigma^2}$.

In this section, we provide BER comparison of the proposed CIM scheme with traditional mmWave communication, while our system uses a two-stage greedy-ML detector. Our motivation for designing this detector is the insufficient performance of the brute-force detector in terms of BER. Figure 2 illustrates the performance of the greedy-ML detector in comparison with the brute-force detector. In a mmWave system, analog combiners at the receiver can result into different effective noises for each indexed cluster. This results into more errors in the brute-force detector in comparison with the greedy-ML detector. Let us assume a system with two indexed clusters, and cluster one is the correct cluster. Under these circumstances, if the effective noise of the first cluster is more powerful, the greedy-ML detector benefits from it, while the brute-force detector may not detect the symbol correctly. Figure 3 depicts the superiority of the proposed scheme in comparison with traditional communication, wherein the system uses a two-stage greedy-ML detector. The corresponding computer simulation configurations are provided in Table 2. It is noticeable that in the traditional mmWave communication, one can transmit through the best path regarding path gain strength, without considering any IM. As shown in Figure 3, computer simulations for 4 bpcu and 6 bpcu spectral efficiency have been provided. In each case, we compare traditional mmWave communication with one extra bit and two extra bits provided by the proposed scheme, that is, CIM. As we can see, when we adopted our scheme to transmit one extra bit, the performance is better in comparison with traditional mmWave communication. We can improve the BER performance further by transmitting two extra bits. However, when we increased the spectral efficiency, BER increases as well. This is because with increasing spectral efficiency, the distance between $M$-ary constellation symbols, and the distance among indexed paths decreases; therefore, the receiver has more difficulty to resolve both conventional and spatial symbols. Figure 4 illustrates BER performance of the proposed scheme and derived a theoretical bound on the BER. As shown in Figure 4, our semi-analytical results behave as an upper bound on the computer simulation results and confirm their validity. Table 2 shows detailed information on the used $M$-ary constellations. In all cases one extra bit is modulated with CIM. As aforementioned earlier, to have analytical results with the Distribution Fitter, we have to obtain the PDF of random components in CPEP. We consider the random variables $X$ and $Y$ in Eqs 29, 40, for two cases of $i = i^*$ and $i \neq i^*$, respectively. The Distribution Fitter tool in MATLAB shows that $X$ and $Y$ can be approximated to have the generalized distribution.

### Table 1 | AoA/AoR interval ranges for cluster index modulation (CIM).

| First cluster | Second cluster | Third cluster | Fourth cluster |
|---------------|----------------|--------------|---------------|
| AoD/AoA intervals | $\left[ -\frac{4\pi}{12}, -\frac{3\pi}{12} \right]$ | $\left[ -\frac{17\pi}{120}, -\frac{7\pi}{120} \right]$ | $\left[ \frac{7\pi}{120}, \frac{17\pi}{120} \right]$ | $\left[ \frac{31\pi}{120}, \frac{41\pi}{120} \right]$ |

![FIGURE 2 | BER performance for greedy-ML detector (1 bit CIM).](image)

![FIGURE 3 | BER performance for analog architecture with greedy-ML detector.](image)
TABLE 2 | Simulation parameters.

|            | Cluster index modulation 1 extra bit | Cluster index modulation 2 extra bit | Traditional communication |
|------------|--------------------------------------|--------------------------------------|--------------------------|
| η = 3 bpcu | 4-QAM                                | QPSK                                 | 16-QAM                   |
| η = 4 bpcu | 8-QAM                                | 8-QAM                                | 64-QAM                   |
| η = 5 bpcu | 16-QAM                               | 16-QAM                               |                          |
| η = 6 bpcu | 32-QAM                               | 32-QAM                               |                          |

![Figure 4](image_url)

**FIGURE 4 |** Theoretical and simulation performance comparison for the analog architecture.

TABLE 3 | PDF approximation parameters.

|            | ξx        | sx        | μx        | ξy        | sy        | μy        |
|------------|-----------|-----------|-----------|-----------|-----------|-----------|
| η = 3 bpcu | 0.22      | 48,776.2  | 107,306   | 0.01      | 15,226.8  | 29,021.8  |
| η = 4 bpcu | 0.73      | 43,470.9  | 55,581.1  | 0.61      | 15,326.2  | 17,274.7  |

extreme value distribution with parameters described in Table 3. If a random variable \( Z \) has a generalized extreme value, the PDF of \( Z \) can be calculated as follows (Muraleedharan et al., 2011):

\[
f_Z(z) = \frac{1}{s_z} \left[ \left( 1 + \xi_z \left( \frac{z - \mu_z}{s_z} \right) \right)^{-\xi_z^{-1}} \right] \exp \left( - \left( 1 + \xi_z \left( \frac{z - \mu_z}{s_z} \right) \right)^{-\xi_z^{-1}} \right).
\]  

(56)

Therefore, UPEP can be calculated as in Eqs 31, 42, for the case of \( i = i^* \) and \( i \neq i^* \), respectively. As the shape parameter is positive for all cases, that is, \( \xi_z > 0 \), we have to satisfy \( z \geq \mu_z - \frac{s_z}{\xi_z} \). On the hand, from Eqs 29, 40, we have to have \( z \geq 0 \). These two constraints determine the lower bound of integrals given in Eqs 31, 42. We calculate integral numerically with the upper bound of infinity using MATLAB. The results are shown in Figure 4. As we can see, the results approximately match with simulation and semi-analytical results which confirms validity of our simulations. As an example, the outputs of the Distribution Fitter tool for η = 3 bpcu are illustrated in Figure 5.

4.2 Hybrid Beamforming Architecture

For this architecture, we assumed the same parameters with the analog architecture. Figure 6 shows the accuracy of our semi-analytical derivations. We considered scenarios with 3 and 4 bpcu spectral efficiency with 1 extra bit modulated by CIM. Table 2 shows detailed information at the selected M-ary constellation used for each case. As we can see, the derived semi-analytical expressions provide an upper bound for the BER. To achieve analytical results, we need to obtain the PDF of random variables \( X \) and \( Y \) in Eqs 51, 52, respectively. The Distribution Fitter tool in MATLAB reveals that \( X \) and \( Y \) have generalized extreme value distribution with the PDF given in Eqs 56 and parameters described in Table 4. As depicted in Figure 6, analytical results based on PDF derivation can provide an approximation on computer simulation results. It is noticeable that when the shape factor is negative (i.e., \( \xi_z < 0 \)), we have to satisfy \( z \in (-\infty, \mu_z - \frac{s_z}{\xi_z}) \). On the other hand, Eq. 49 and Eq. 50 necessitate us to have \( z \geq 0 \). These two constraints determine the lower and upper bounds of the integrals given in Eqs 53, 54.

In Figure 7, we show the superiority of the proposed scheme in hybrid architecture in comparison with the BIM structure proposed in (Mokh et al. (2019)). In the BIM structure, the dominant paths have been selected for indexing purposes. However, correlation among indexed paths can increase the BER. Hence, in the proposed CIM structure, dominant paths have been selected from the well separated clusters to decrease correlation among them. Simulation results illustrate BER for the spectral efficiency of 4 bpcu with 2 bits IM. We provide computer simulations for both BIM and CIM with different number of paths distributed uniformly in four clusters. As illustrated in Figure 7, when there are 4 paths in the environment, the performance of two schemes are identical because there is only one path in each cluster. However, with increasing the number of paths, the performance of CIM increases significantly, while BIM performs worse. This is because in BIM, indexed paths can be selected from the same clusters which leverage the huge correlation on the selected paths, while CIM guarantees that selected paths are far enough to decrease the effect of inter-beam interference. However, the improvement in the performance of CIM is not permanent with increasing the number of paths, and after a specific number of paths, it
decreases. This is because with increasing number of paths, the transmitted signal experiences leakage on the neighboring paths, which decreases the effective transmitted power in the selected path.

5 CONCLUSION

In this study, we have proposed a novel IM scheme for future mmWave communication systems, which takes into consideration well-separated clusters for indexing purpose. With adopting these separated clusters, the indexed paths become near orthogonal; hence, the inter-beam interference, which is one of the biggest problems in the mmWave communication, decreases significantly. Furthermore, we have studied the architecture of hybrid precoder and considered a ZF precoder at the transmitter to further suppress the inter-beam interference. With such an architecture, we have assumed and studied the system in more realistic conditions. Computer simulation results reveal that CIM can perform...
better than traditional mmWave communication, and hybrid CIM performs better than BIM in terms of BER. We derived semi-analytical and analytical error probability expression for the proposed scheme, which have proven the superiority of our scheme. Our future study might focus on multiuser systems with randomly distributed clusters in the mmWave communication environments to study scenarios under more realistic circumstances.

**DATA AVAILABILITY STATEMENT**

The original contributions presented in the study are included in the article/Supplementary Materials; further inquiries can be directed to the corresponding author.

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**AUTHOR CONTRIBUTIONS**

MR performed computer simulations and analyses. MR and AK organized the manuscript. EB and TL-N supervised the study, proposed the initial concept, and reviewed the manuscript at certain stages.

**FUNDING**

The work of MR and EB was supported by the Scientific and Technological Research Council of Turkey (TUBITAK) under grant 218E035. The work of AK and TLN was supported in part by the Natural Sciences and Engineering Research Council of Canada (NSERC).
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